

# Rare and baryonic decays of charmed hadrons at Belle and Belle II

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Belle II collaboration



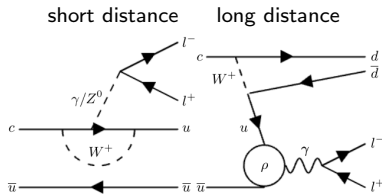
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EPS-HEP 2025

- Rare decays
  - $D^0 \rightarrow K^- \pi^+ e^+ e^-$ ,  $\pi^+ \pi^- e^+ e^-$ ,  $K^+ K^- e^+ e^-$
  - $\Xi_c^0 \rightarrow \Xi^0 \ell^+ \ell^-$
- Branching fractions
  - $\Xi_c^0 \rightarrow \Xi^0 \pi^0$ ,  $\Xi^0 \eta$ ,  $\Xi^0 \eta'$
  - $\Xi_c^+ \rightarrow p K_S^0$ ,  $\Lambda \pi^+$ ,  $\Sigma^0 \pi^+$
  - $\Xi_c^+ \rightarrow \Sigma^+ K_S^0$ ,  $\Xi^0 \pi^+$ ,  $\Xi^0 K^+$
  - $\Lambda_c^+ \rightarrow p K_S^0 \pi^0$
- Excited charm baryons
  - search in  $\Lambda_c^+ \eta$  final state
  - Br's of  $\Lambda_c(2880)^+$ ,  $\Lambda_c(2940)^+ \rightarrow \Lambda_c^+ \eta$ ,  $p D^0$

Data sets: Belle 980  $\text{fb}^{-1}$ , Belle II 428  $\text{fb}^{-1}$

- $c \rightarrow u \ell^+ \ell^-$  are FCNC transitions
  - forbidden in SM at tree level
  - proceed through electroweak box or loop diagrams
  - further suppressed by GIM mechanism
- $D^0 \rightarrow hh' \ell^+ \ell^-$ : short and long distance contributions
  - short distance:  $\mathcal{B} \sim 2 \times 10^{-9}$
  - long distance:  $\mathcal{B}$  up to  $2 \times 10^{-6}$
- NP can enhance decay rates



## Data analysis

- Reconstructed in  $D^{*+} \rightarrow D^0 \pi^+$ 
  - $p^*(D^{*+}) > 2.5 \text{ GeV}/c$  to suppress background
  - particle identification of K,  $\pi$  and e
  - electron bremsstrahlung recovery,  $m_{ee} > 200 \text{ MeV}/c^2$  to suppress BG from  $\pi^0/\eta$
  - vertex fits

$$D^0 \rightarrow K^- \pi^+ e^+ e^-, \pi^+ \pi^- e^+ e^-, K^+ K^- e^+ e^-$$

Belle 942 fb<sup>-1</sup>

## Results (preliminary)

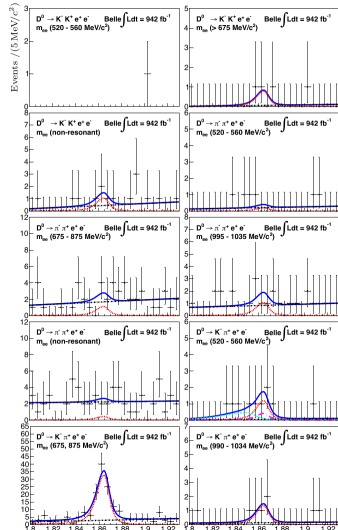
to be submitted to PRDL

- Branching fractions measured relative to  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$ 
  - in  $m_{ee}$  regions of  $\eta$ ,  $\rho/\omega$ ,  $\phi$  and non-resonant
- Significant signal in  $\rho/\omega$  region of  $D^0 \rightarrow K^- \pi^+ e^+ e^-$   
 $\mathcal{B} = (39.6 \pm 4.5 \pm 2.9) \times 10^{-7}$

→ most precise to date

- Others not seen → 90% CL UL's

|                 | $K^+ K^- e^+ e^-$    | $\pi^+ \pi^- e^+ e^-$ | $K^- \pi^+ e^+ e^-$  |
|-----------------|----------------------|-----------------------|----------------------|
| $\eta$          | $2.3 \times 10^{-7}$ | $3.2 \times 10^{-7}$  | $5.6 \times 10^{-7}$ |
| $\rho^0/\omega$ | $3.0 \times 10^{-7}$ | $6.1 \times 10^{-7}$  | -                    |
| $\phi$          |                      | $3.1 \times 10^{-7}$  | $2.9 \times 10^{-7}$ |
| non-res.        | $7.7 \times 10^{-7}$ | $8.1 \times 10^{-7}$  |                      |



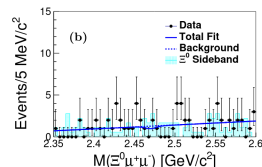
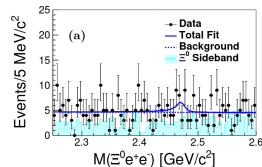
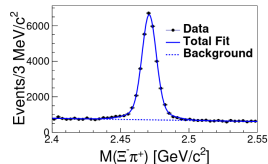
$$\Xi_c^0 \rightarrow \Xi^0 \ell^+ \ell^-$$

Belle 980 fb<sup>-1</sup>

- First search for these decays ( $\ell = e, \mu$ ) PRD 109, 052003 (2024)
  - UL predictions based on  $\Lambda_c^+ \rightarrow p \mu^+ \mu^-$  (LHCb):  $< 2.3 \times 10^{-6}$
- Normalization mode:  $\Xi_c^0 \rightarrow \Xi^- \pi^+$ ,  $\mathcal{B} = (1.43 \pm 0.32)\%$  [PDG2022]
- Data analysis
  - intermediate states reconstructed in  $\Xi^{0/-} \rightarrow \Lambda \pi^{0/-}$ ,  $\Lambda \rightarrow p \pi^-$
  - momentum cut to suppress background
  - particle identification
  - vertex fits (mass constrained for intermediate states)
- Results
  - no signals observed  $\rightarrow$  90% credible upper limits determined

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 e^+ e^-) < 9.9 \times 10^{-5}$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \mu^+ \mu^-) < 6.5 \times 10^{-5}$$



# Branching fractions of charmed baryons

- Nonfactorizable amplitudes arising from internal  $W$ -emission and  $W$ -exchange lead to difficulties for theoretical predictions
  - various approaches have been developed
- Measurements of branching fractions will help to clarify the theoretical picture

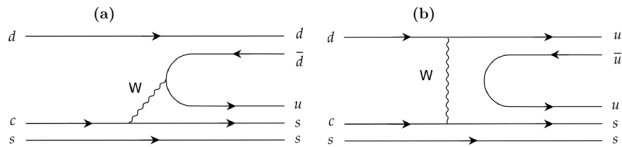


Figure 1. Feynman diagrams for (a) internal  $W$ -emission and (b)  $W$ -exchange in  $\Xi_c^0 \rightarrow \Xi^0 h^0$

- Data analysis is pretty much similar among different decay modes
  - momentum cut to suppress background (mostly from B decays)
  - particle identification
  - vertex fits (mass constrained for intermediate states, IP constrained for final state)
  - best candidate selection (usually based on vertex fit quality)

$$\Xi_c^0 \rightarrow \Xi^0 \pi^0, \Xi^0 \eta, \Xi^0 \eta'$$

Belle + Belle II, 980 + 426 fb<sup>-1</sup>

JHEP10 (2024) 045

- Intermediate states reconstructed in  $\Xi^{0/-} \rightarrow \Lambda \pi^{0/-}, \Lambda \rightarrow p \pi^-, \eta' \rightarrow \pi^+ \pi^- \eta, \eta/\pi^0 \rightarrow \gamma \gamma$
- Normalization mode:  $\Xi_c^0 \rightarrow \Xi^- \pi^+$ ,  $\mathcal{B} = (1.43 \pm 0.27)\%$  [PDG2024]
- Significant signals observed
- Branching fractions

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \pi^0) = (6.9 \pm 0.3_{\text{stat}} \pm 0.5_{\text{syst}} \pm 1.3_{\text{norm}}) \times 10^{-3}$$

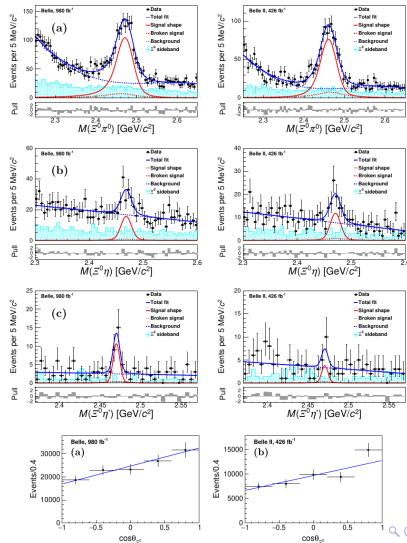
$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta) = (1.6 \pm 0.2_{\text{stat}} \pm 0.2_{\text{syst}} \pm 0.3_{\text{norm}}) \times 10^{-3}$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta') = (1.2 \pm 0.3_{\text{stat}} \pm 0.1_{\text{syst}} \pm 0.2_{\text{norm}}) \times 10^{-3}$$

- Asymmetry parameter

$$\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0) = -0.90 \pm 0.15_{\text{stat}} \pm 0.23_{\text{syst}}$$

→ first measurements of these decays



JHEP03 (2025) 061

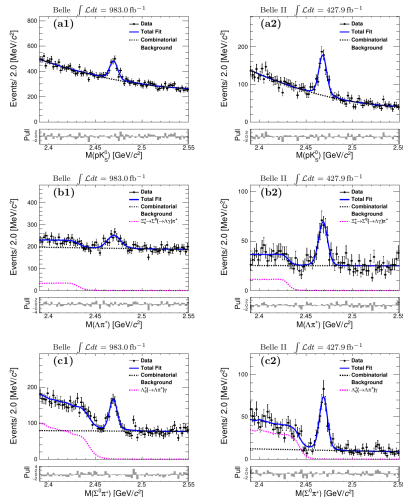
- Singly Cabibbo-suppressed decays
- Intermediate states reconstructed in  
 $K_S^0 \rightarrow \pi^+\pi^-, \Sigma^0 \rightarrow \Lambda\gamma, \Xi^- \rightarrow \Lambda\pi^-, \Lambda \rightarrow p\pi^-$
- Normalization mode:  $\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+$ ,  
 $\mathcal{B} = (2.9 \pm 1.3)\%$  [Belle, PRD 100 (2019) 031101]
- Significant signals observed
- Branching fractions

$$\mathcal{B}(\Xi_c^+ \rightarrow pK_S^0) = (7.16 \pm 0.46_{\text{stat}} \pm 0.20_{\text{syst}} \pm 3.21_{\text{norm}}) \times 10^{-4}$$

$$\mathcal{B}(\Xi_c^+ \rightarrow \Lambda\pi^+) = (4.52 \pm 0.41_{\text{stat}} \pm 0.26_{\text{syst}} \pm 2.03_{\text{norm}}) \times 10^{-4}$$

$$\mathcal{B}(\Xi_c^+ \rightarrow \Sigma^0\pi^+) = (12.0 \pm 0.8_{\text{stat}} \pm 0.7_{\text{syst}} \pm 5.4_{\text{norm}}) \times 10^{-4}$$

→ first observations of these decays (each one > 10σ)





$$\Xi_c^+ \rightarrow \Sigma^+ K_S^0, \Xi_c^0 \pi^+, \Xi_c^0 K^+$$

Belle + Belle II, 983 + 428 fb<sup>-1</sup>

Submitted to JHEP (arXiv:2503.17643)

- Cabibbo-favored and singly Cabibbo-suppressed decays
- Intermediate states reconstructed in  
 $\Xi^{0/-} \rightarrow \Lambda \pi^{0/-}, \Lambda \rightarrow p \pi^-, \Sigma^+ \rightarrow p \pi^0, K_S^0 \rightarrow \pi^+ \pi^-$
- Normalization mode:  $\Xi_c^+ \rightarrow \Xi^- \pi^+ \pi^+$ ,  
 $\mathcal{B} = (2.9 \pm 1.3)\%$  [PDG 2024]
- Significant signals observed
- Branching fractions (preliminary)

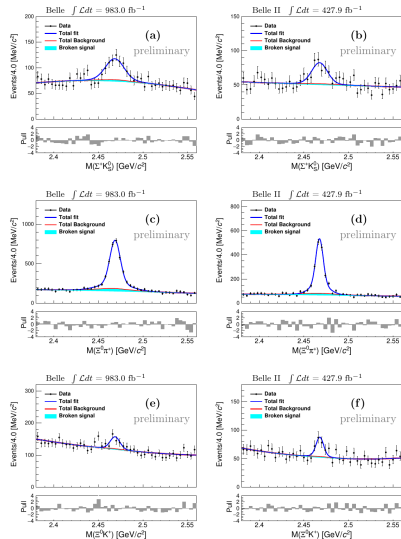
$$\mathcal{B}(\Xi_c^+ \rightarrow \Sigma^+ K_S^0) = (1.94 \pm 0.21_{\text{stat}} \pm 0.09_{\text{syst}} \pm 0.87_{\text{norm}}) \times 10^{-3}$$

$$\mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+) = (7.19 \pm 0.14_{\text{stat}} \pm 0.24_{\text{syst}} \pm 3.22_{\text{norm}}) \times 10^{-3}$$

$$\mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 K^+) = (4.9 \pm 0.7_{\text{stat}} \pm 0.2_{\text{syst}} \pm 2.2_{\text{norm}}) \times 10^{-4}$$

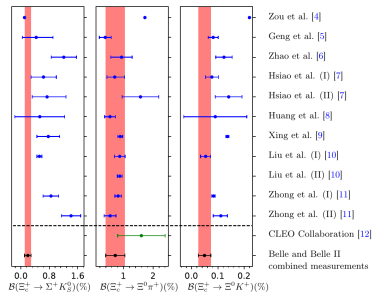
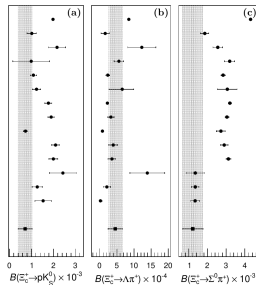
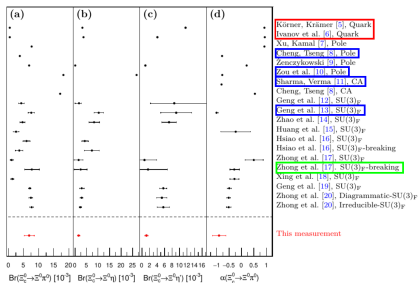
$$R(\Xi^0 K^+ / \Xi^0 \pi^+) = (0.068 \pm 0.010_{\text{stat}} \pm 0.004_{\text{syst}})$$

→ first measurements ( $\Sigma^+ K_S^0, \Xi^0 K^+$ ), most precise ( $\Xi^0 \pi^+$ )



# Comparison with theory predictions

- Theory predictions mostly not far from measurements
- We cannot rule-out any predictions



→ see backup slides

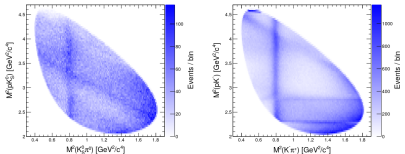
Accepted in PRD (arXiv:2503.04371)

- Improved Br measurement
- Normalization mode:  $\Lambda_c^+ \rightarrow p K^- \pi^+$ ,  
 $\mathcal{B} = (6.24 \pm 0.28)\%$  [PDG 2024]
- Signal yields: 128k ( $p K_S^0 \pi^0$ ) and 1.4M ( $p K^- \pi^+$ )
- Results (preliminary)

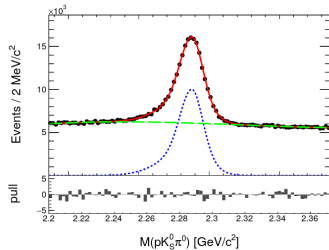
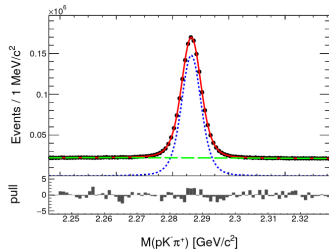
$$\mathcal{B}(\Lambda_c^+ \rightarrow p K_S^0 \pi^0) = (2.12 \pm 0.01_{\text{stat}} \pm 0.05_{\text{syst}} \pm 0.10_{\text{norm}})\%$$

→ consistent w/ BESIII, more precise

→ systematics dominated by  $K_S^0/\pi^0$  reconstruction



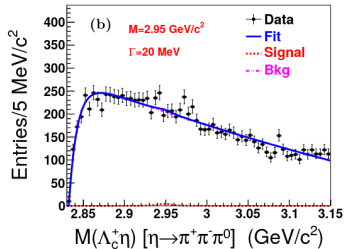
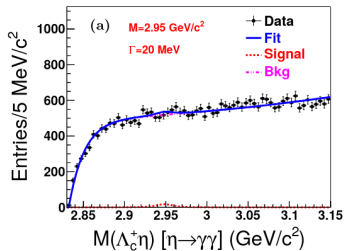
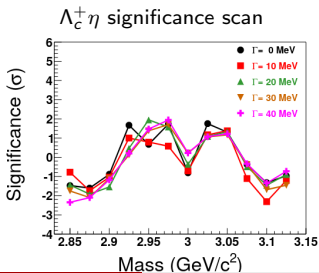
amplitude analysis  
planned in near future



PRD 110, 032021 (2024)

Search in  $\Lambda_c^+ \eta$  final state

- Motivation: excited hyperons seen in  $\Lambda \eta$  final state
- Intermediate states reconstructed in  $\Lambda_c^+ \rightarrow p K^- \pi^+ / p K_S^0$ ,  $\eta \rightarrow \gamma \gamma / \pi^0 \pi^+ \pi^-$
- No excited states seen in mass range 2.85 - 3.125 GeV/c



Branching-fraction ratios of  $\Lambda_c(2880)^+$  and  $\Lambda_c(2940)^+$

- decaying to  $\Lambda_c^+\eta$  and  $pD^0$
- relative to  $\Sigma_c(2455)\pi$
- Intermediate states reconstructed in  
 $D^0 \rightarrow K^-\pi^+/K^-\pi^+\pi^0/K^-\pi^+\pi^-\pi^+$ ,  $\Sigma_c(2455) \rightarrow \Lambda_c^+\pi$

### Results

$$R_{pD^0}(2880) = 0.75 \pm 0.03 \pm 0.07$$

$$R_{pD^0}(2940) = 3.59 \pm 0.21 \pm 0.56$$

$$R_{\Lambda_c^+\eta}(2880) < 0.13 \text{ (90\% CL)}$$

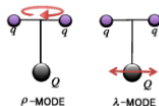
$$R_{\Lambda_c^+\eta}(2940) < 1.11 \text{ (90\% CL)}$$

→ first measurements

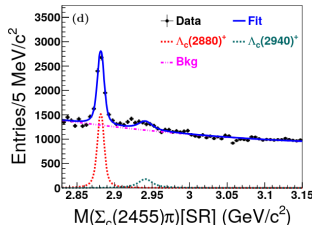
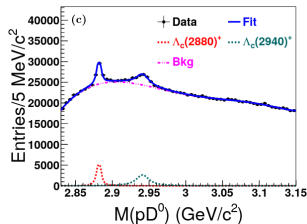
→ results suggest [T. Yoshida et. al., PRD 92, 114029 (2015)]

$\Lambda_c(2880)^+$  is  $\rho$ -mode excited state (predom. to heavy baryon light meson)

$\Lambda_c(2940)^+$  is  $\lambda$ -mode excited state (predom. to light baryon heavy meson)



PRD 110, 032021 (2024)

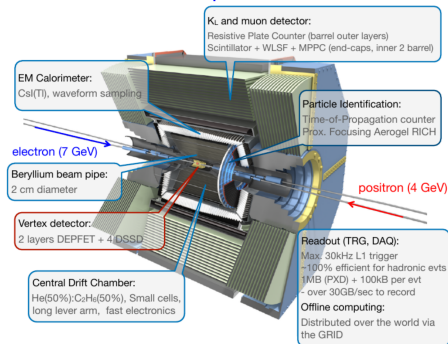


- Recent measurements of rare and baryonic decays of charmed hadrons at Belle and Belle II have been presented.
- Many of these decays have been measured or observed for the first time.
- Work on this topics continues.
- New results can be expected soon.

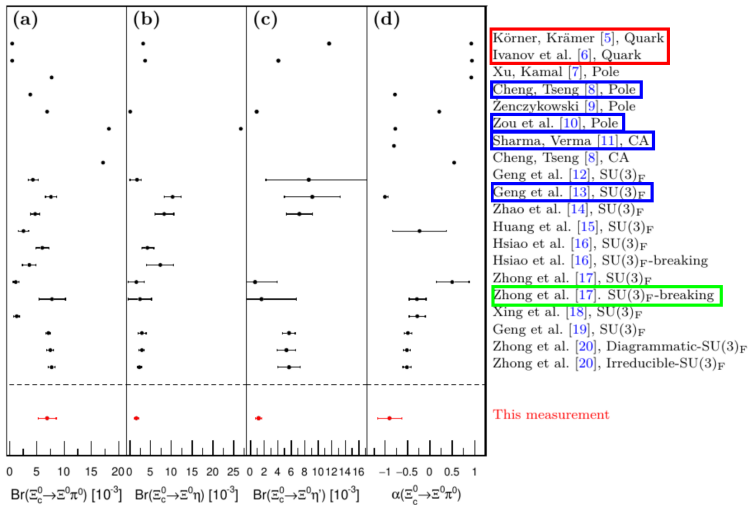
# Backup: Belle and Belle II

- B-factory experiments at KEK, Tsukuba, Japan
  - asymmetric  $e^+e^-$  colliders (KEKB, SuperKEKB) running at or near  $\Upsilon(4S)$
  - $c\bar{c}$  production cross-section similar to  $B\bar{B}$
- Belle (1999 - 2010)
  - general purpose spectrometer
    - vertexing, tracking, neutrals detection, PID
  - KEBK:  $\mathcal{L} = 2 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$
  - collected  $1 \text{ ab}^{-1}$
- Belle II (2019 - )
  - upgraded Belle spectrometer
    - most components replaced  $\rightarrow$  better performance
  - SuperKEKB: nano-beam optics
    - $20\times$  smaller beam spot
  - target luminosity:  $30 \times \text{KEKB}$
  - goal to collect  $50 \text{ ab}^{-1}$

Belle II spectrometer



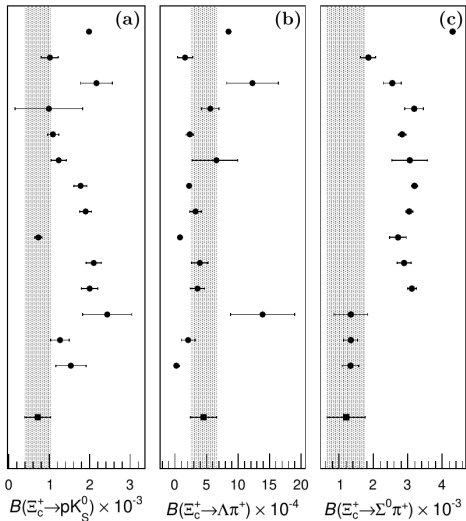
# Backup: $\Xi_c^0 \rightarrow \Xi^0 \pi^0, \Xi^0 \eta, \Xi^0 \eta'$



- SU(3)<sub>F</sub>-breaking model predictions [17] consistent with our Br. measurements but not with  $\alpha$
- predictions for  $\alpha$  are consistent with our measurement for the pole model [8, 10], CA model [11] and SU(3)<sub>F</sub> model [13]
- covariant confined quark model [5, 6] is mildly disfavored



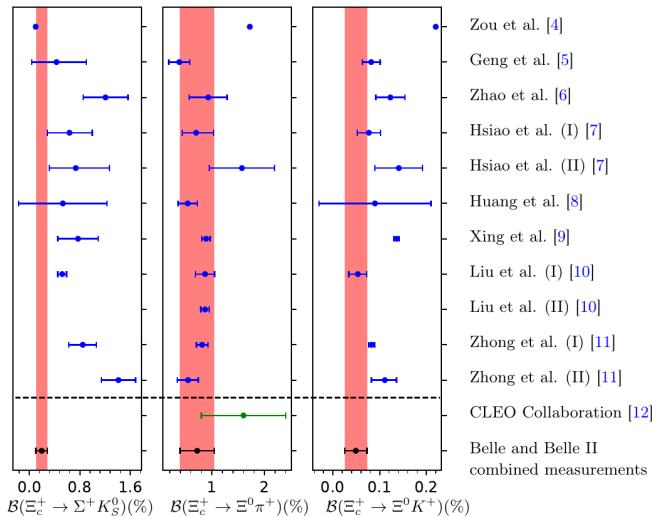
# Backup: $\Xi_c^+ \rightarrow pK_S^0, \Lambda\pi^+, \Sigma^0\pi^+$



Zou et al. [12]  
 Geng et al. [13]  
 Geng et al. [14]  
 Huang et al. [15]  
 Zhong et al. (I) [16]  
 Zhong et al. (II) [16]  
 Xing et al. [17]  
 Geng et al. [18]  
 Liu [19]  
 Zhong et al. (I) [20]  
 Zhong et al. (II) [20]  
 Zhao et al. [21]  
 Hsiao et al. (I) [22]  
 Hsiao et al. (II) [22]  
 Belle and Belle II  
 combined measurement

- predictions (except first one) are within  $4\sigma$  of our measurements
- predictions for  $\Lambda\pi^+$  mode are all within  $2\sigma$  of our measurement
- most predictions for  $pK_S^0$  and  $\Sigma^0\pi^+$  modes are somewhat higher than our measurements

# Backup: $\Xi_c^+ \rightarrow \Sigma^+ K_S^0$ , $\Xi_c^0 \pi^+$ , $\Xi_c^0 K^+$



- good agreement for  $\Xi_c^0 \pi^+$  decay except [4]
- somewhat higher predictions for the other two decay modes