

CP Violation and the Neutron Electric Dipole Moment from Lattice QCD

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DFG Deutsche
Forschungsgemeinschaft

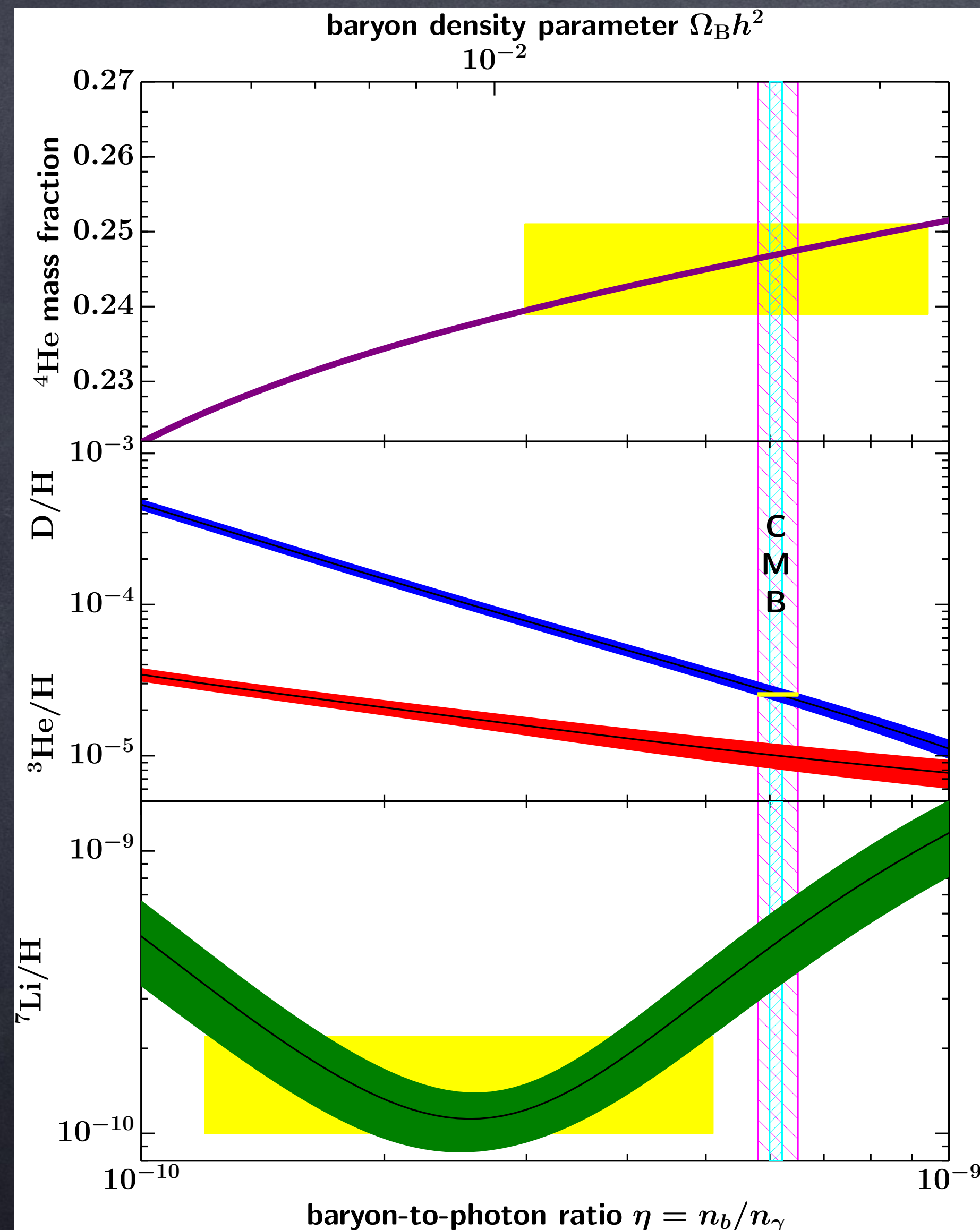


Berkeley



EPS - HEP July, 7 2025

Matter antimatter asymmetry



PDG 2021

$$\eta = \frac{n_B}{n_\gamma} \quad n_B = n_b - n_{\bar{b}} \quad \eta = \frac{(\text{matter}) - (\text{antimatter})}{\text{relic photons}}$$

$$\eta = (6.143 \pm 0.190) \times 10^{-10} \quad \text{Concordance range}$$

$$\Omega_b = \frac{\rho_b}{\rho_{\text{crit}}} \simeq \eta h^{-2} / 274 \times 10^{10} = 0.02244 \pm 0.00069 h^{-2}$$

$$\Omega_b h^2 = 0.02230 \pm 0.00021 \Rightarrow \eta = (6.104 \pm 0.058) \times 10^{-10} \quad \text{PLANCK}$$

Fields, Olive, Yeh, Young: 2020

$$\eta_{\text{SM}} \sim 10^{-26}$$

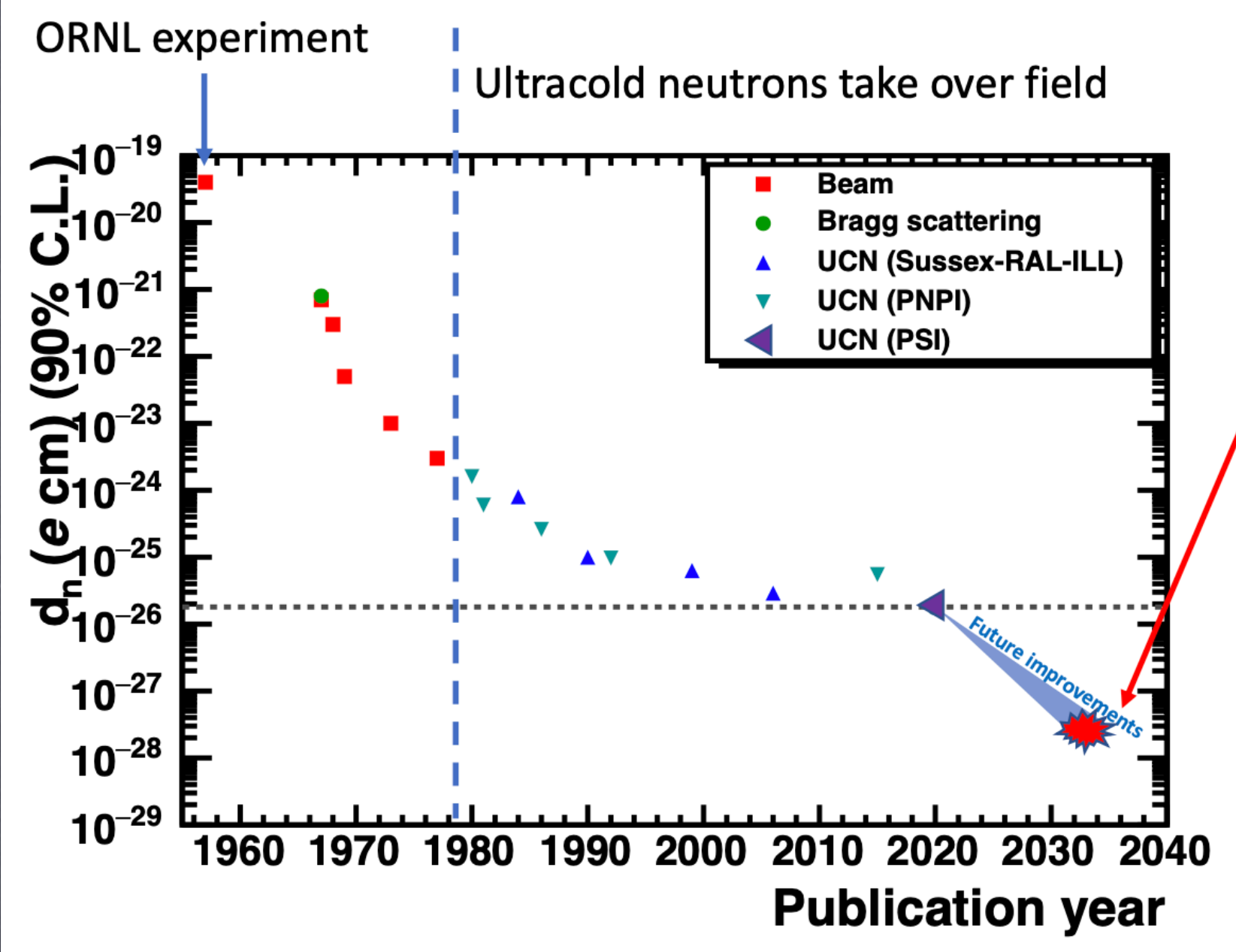
Gavela, Hernandez, Orloff, Pene: 1994

Huet, Sather: 1995

Rules out any mechanism of electroweak baryogenesis that does not make use of a new source of CP violation.

New source of CP violation

Neutron EDM



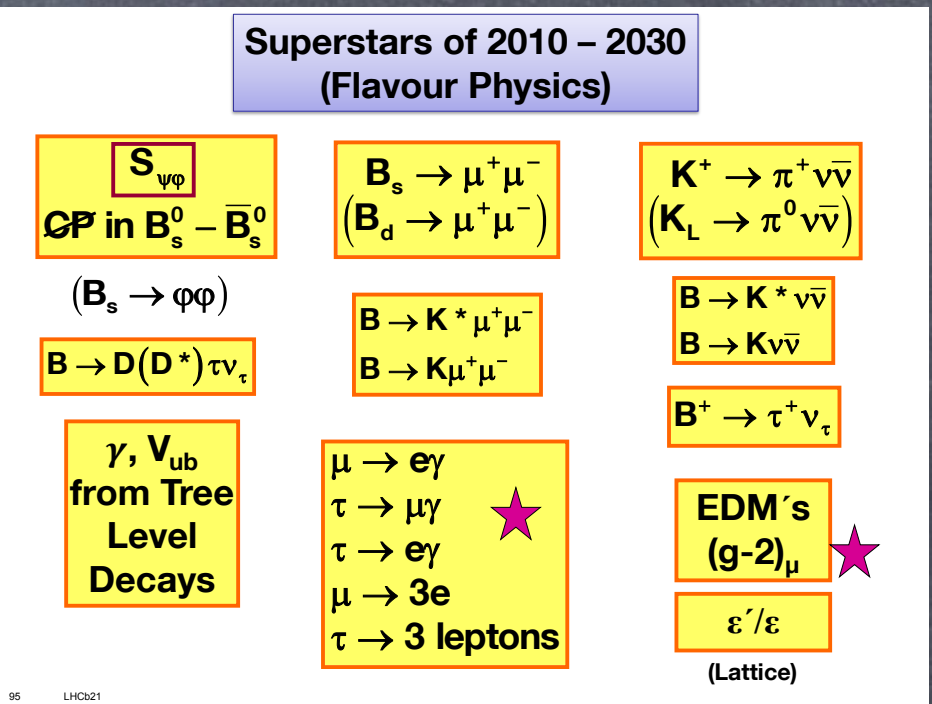
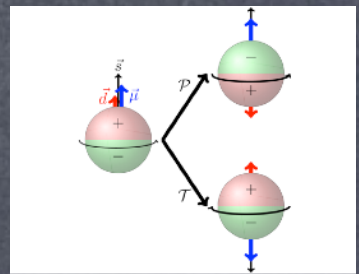
$$|d_n| < 1.8 \times 10^{-26} e \text{ cm (90\% C.L.)}$$

Abel et al.: 2020 (PSI)

Alarcon et al.: 2022

Snowmass Summer Study Report

$$H = -\mu \underline{B} \cdot \frac{\underline{S}}{|\underline{S}|} - d \underline{E} \cdot \frac{\underline{S}}{|\underline{S}|}$$

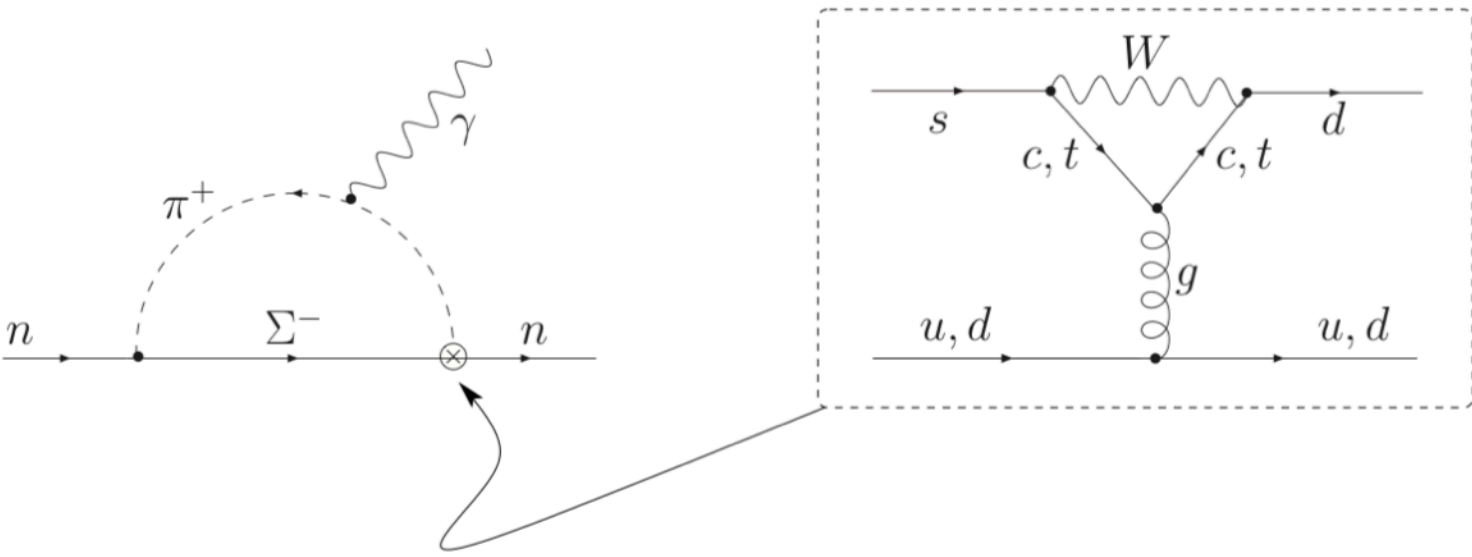


Buras: LHCb21

$$(d_n)_{\text{SM}} = (1-6) \times 10^{-32} e \text{ cm}$$

Shabalin: 1978-1980 Khriplovich, Zhitnitsky: 1982
Gavela et al. : 1982 Seng: 2015

Experiment: Facility	Neutron Source	Measurement Cell	Measurement Techniques	90% C.L. ($10^{-28} e\text{-cm}$) With 300 Live Days	Year 90% C.L. Data Acquired
Crystal: JPARC	Cold Neutron Beam	Solid	Crystal Diffraction (High Internal $\vec{E}$)	< 100	Development
Beam: ESS	Cold Neutron Beam	Vacuum	Pulsed Beam	< 50	~ 2030
PNPI: ILL	ILL Turbine (UCN) PNPI/LHe (UCN)	Vacuum	Ramsey Technique, $\vec{E} = 0$ Cell for Magnetometry	Phase 1 < 100 < 10	Development Development
n2EDM: PSI	Solid D ₂ (UCN)	Vacuum	Ramsey Technique, External Cs Magnetometers, Hg Co-Magnetometer	< 15	~ 2026
PanEDM ILL/Munich	Superfluid ⁴ He (UCN), Solid D ₂ (UCN)	Vacuum	Ramsey Technique, Hg Co- External ³ He and Cs Magnetometers	< 30	~ 2026
TUCAN: TRIUMF	Superfluid ⁴ He (UCN)	Vacuum	Ramsey Technique, Hg Co- Magnetometer, External Cs Magnetometers	< 20	~ 2027
nEDM: LANL	Solid D ₂ (UCN)	Vacuum	Ramsey Technique, Hg Co- Magnetometer, Hg External Magnetometer, OPM	< 30	~ 2026
nEDM@SNS:	Superfluid ⁴ He (UCN)	⁴ He	Cryogenic High Voltage ³ He Magnetometer, External Cs Magnetometer, with SQUIDs, Dressed Spins, Superconducting Magnetic Shield	< 20	~ 2029



CP-violating sources

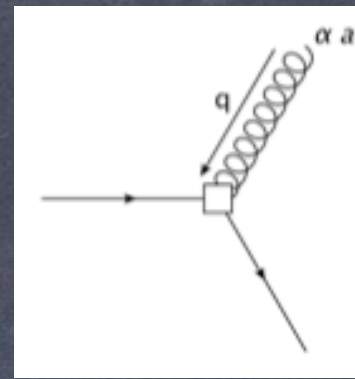
- Full list of dimension 5 and 6 operators is known

Buchmuller, Wyler: 1986
de Rujula et al.: 1991
Grzadkowski et al: 2010

$$O_q^f(x) = \bar{\psi}_f(x) \gamma_5 \sigma_{\mu\nu} \psi_f(x) F_{\mu\nu}$$

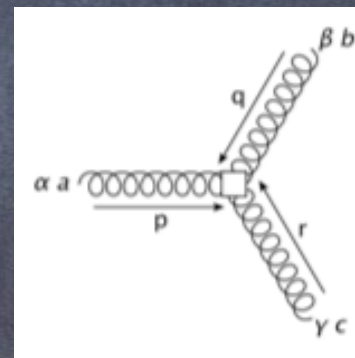
Quark EDM

$$O_{\text{CE}}^f(x) = \bar{\psi}_f(x) \gamma_5 \sigma_{\mu\nu} G_{\mu\nu}^a T^a \psi_f(x)$$



Quark-chromo EDM

$$O_{3g}(x) = \frac{1}{6} i f^{abc} G_{\mu\rho}^a(x) G_{\nu\rho}^b(x) G_{\lambda\sigma}^c(x) \epsilon_{\mu\nu\lambda\sigma}$$



3-gluon CP-odd

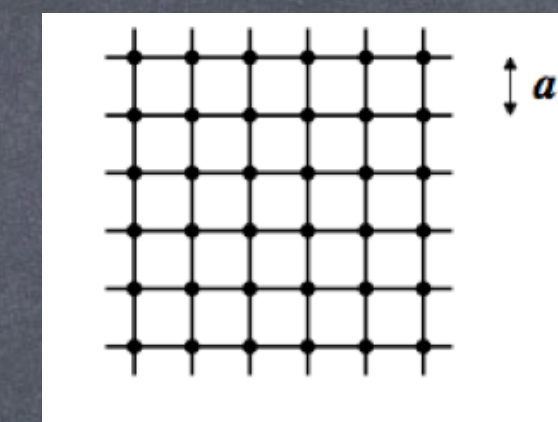
Weinberg: 1989

$$q(x) = \frac{1}{32\pi^2} \epsilon_{\mu\nu\rho\sigma} \text{tr} \{ G_{\mu\nu}(x) G_{\rho\sigma}(x) \}$$

Topological charge density

$$\mathcal{L}_{\text{QCD}+\theta} = \frac{1}{4} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_{f=u,d,s,\dots} \bar{\psi}_f(x) \{ \gamma_\mu [\partial_\mu + g A_\mu^a T^a] + m_f \} \psi_f(x) - i\bar{\theta} q(x)$$

The role of lattice QCD



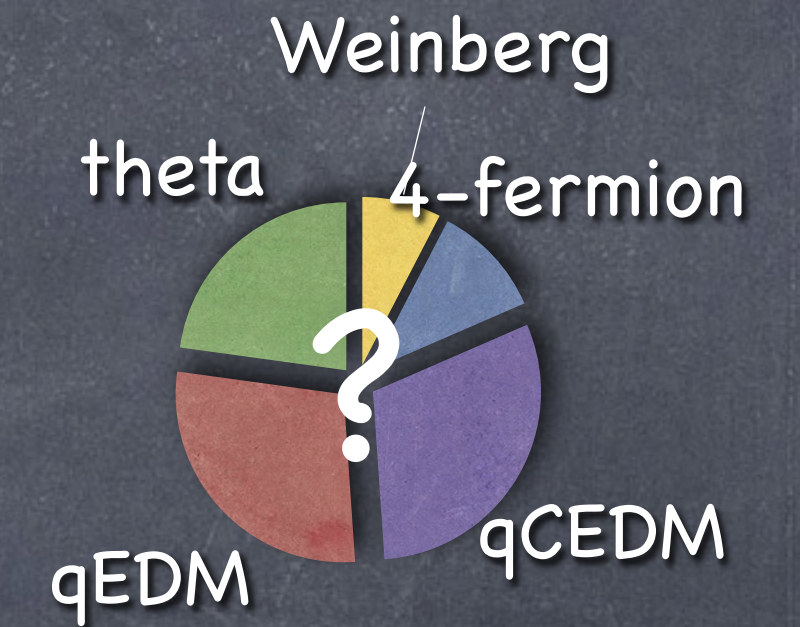
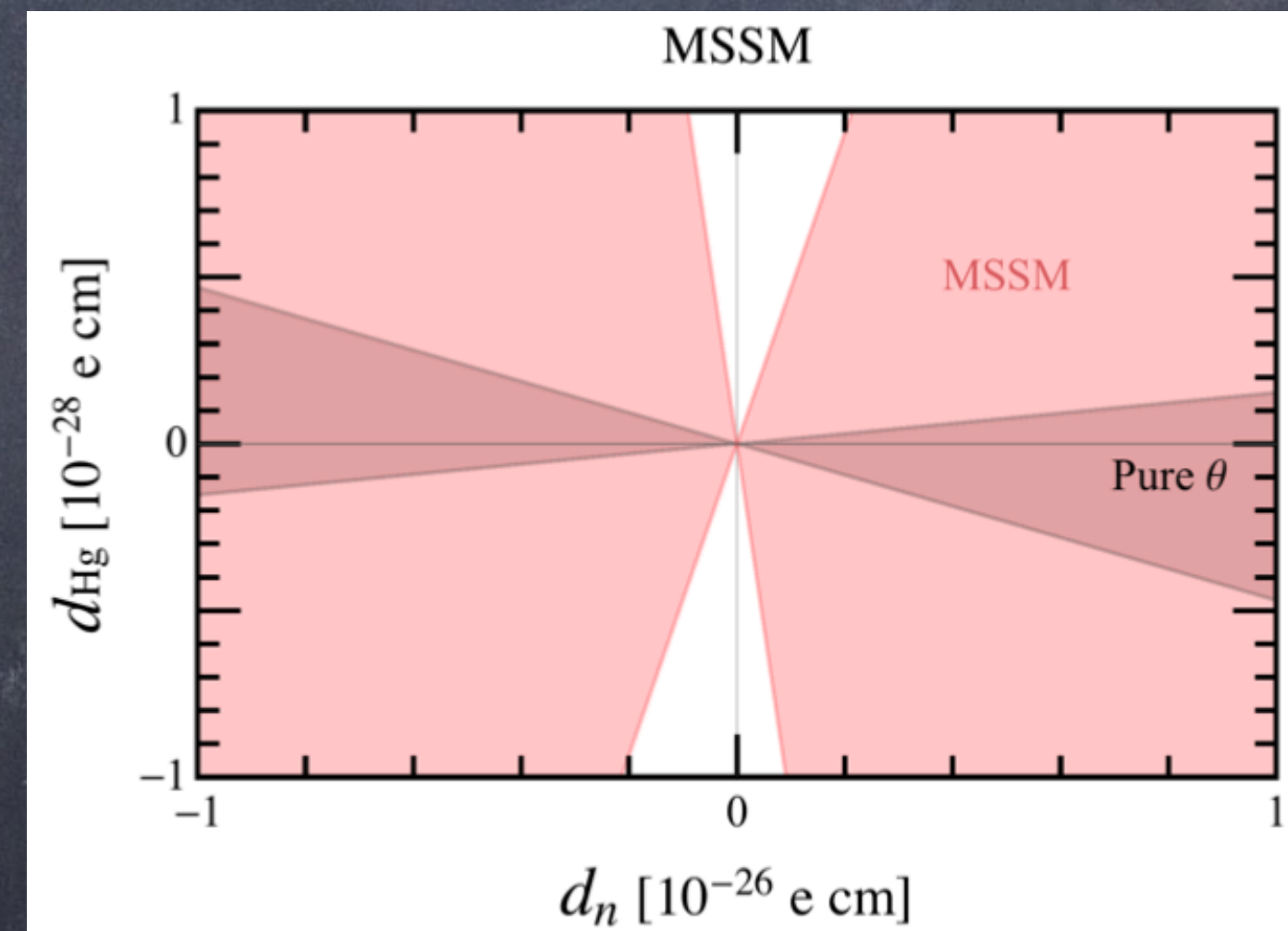
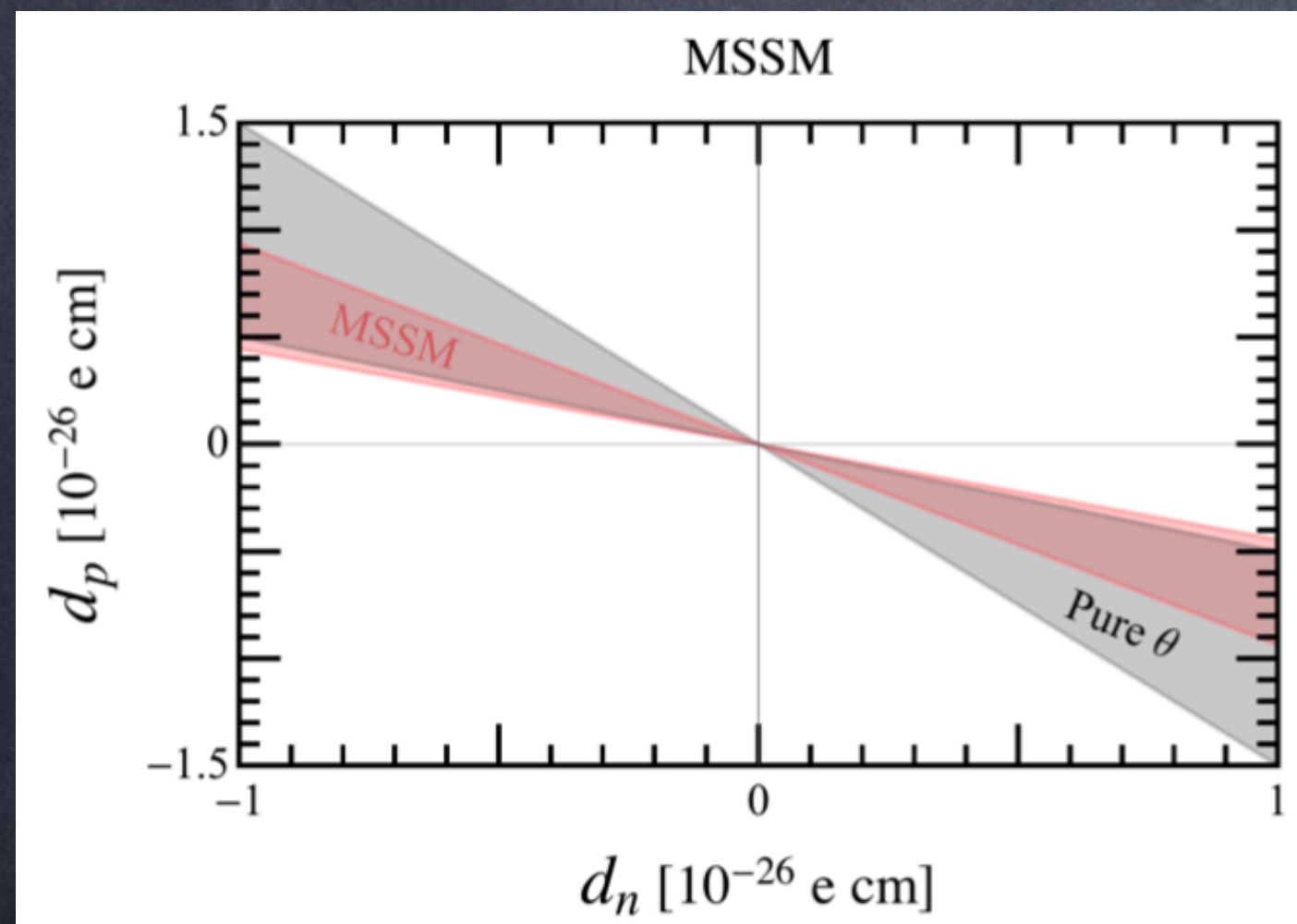
$$d_N = M_N^\theta \bar{\theta} + \left(\frac{v}{\Lambda}\right)^2 \sum_i M_N^{(i)} \tilde{d}_i \quad \langle N | J_\mu \mathcal{O}_{CP} | N \rangle \rightarrow d \underline{E} \cdot \underline{S}$$

M_N^θ $\longrightarrow$ Hadronic matrix element topological charge

$M_N^{(i)}$ $\longrightarrow$ Hadronic matrix element CP odd operators

$$d_n = \begin{aligned} & - (1.5 \pm 0.7) \cdot 10^{-3} \bar{\theta} e \text{ fm} \\ & - (0.2 \pm 0.01) d_u + (0.78 \pm 0.03) d_d + (0.0027 \pm 0.016) d_s \\ & - (0.55 \pm 0.28) e \tilde{d}_u - (1.1 \pm 0.55) e \tilde{d}_d + (50 \pm 40) \text{ MeV} e \tilde{d}_G \end{aligned}$$

Dragos, Luu, A.S.,
de Vries, Yousif: 2019



Shintani et al.: 2005
Berruto, Blum, Orginos, Soni 2006
A.S., Luu, de Vries: 2014-2015
Guo, Meißner, et al. : 2010-
Liang, Draper, Liu, Yang
Alexandrou et al. (ETMC): 2015-2020
Abramczyk et al. : 2017-
Dragos, Kim, Luu, Monahan, Rizik,
A.S., de Vries, Yousif: 2015-2021
Yoon, Bhattacharya, Cirigliano,
Gupta, Mereghetti: 2015-2021

de Vries et al.: 2021

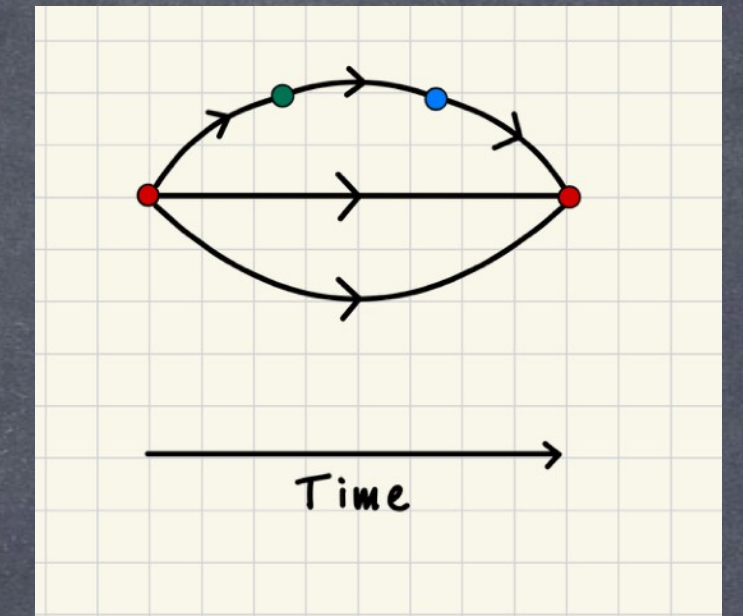
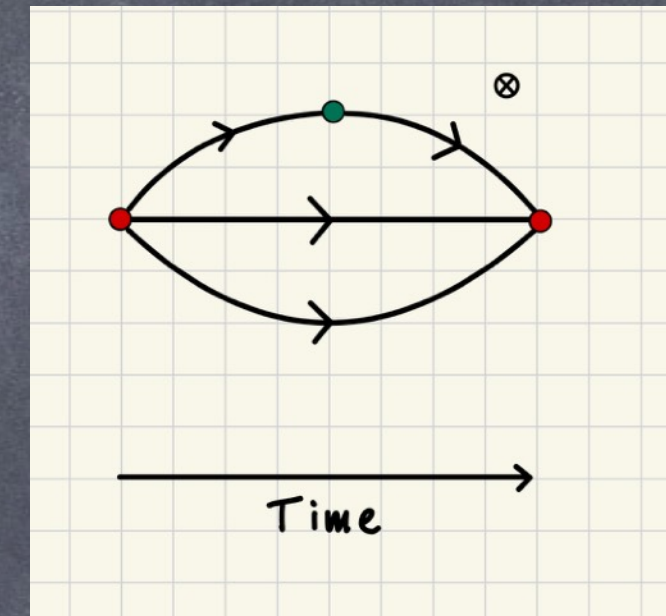
Alarcon et al.: 2022
Snowmass Summer Study Report

How to calculate nEDM

$$\langle N J_\mu^{\text{em}} \bar{N} \rangle_{C/P} \simeq \langle N J_\mu^{\text{em}} O_{C/P} \bar{N} \rangle_{\text{QCD}} \quad \rightarrow \quad \langle N(p_1) | J_\mu^{\text{em}} | N(p_2) \rangle_{C/P}$$

$$\langle N(p_1) | J_\mu^{\text{em}} | N(p_2) \rangle_{C/P} = \bar{u}_N(p_1) \Gamma_\mu^{C/P}(Q^2) u_N(p_2)$$

$$\Gamma_\mu^{C/P}(Q^2) \simeq F_1(q^2) \gamma_\mu + \frac{i}{2M_N} F_2(q^2) \sigma_{\mu\nu} q_\nu + i \bar{d}_{C/P} \frac{1}{2M_N} F_3(q^2) \sigma_{\mu\nu} \gamma_5 q_\nu$$



$$|d_N| = F_3(0)/2M_N \quad q = p_1 - p_2$$

Challenges on the lattice

- Renormalization of $O_{C/P}$ and continuum limit $a \rightarrow 0$

- Excited states contaminations $\sum_i a_i e^{-m_i x_4} \quad E_0 < E_1 < \dots$

- Signal-to-noise ratio

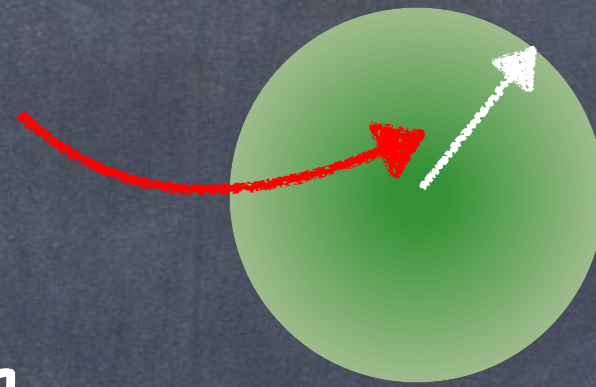
$$x_\mu = (\mathbf{x}, x_4) \quad t \rightarrow \text{flow-time} \quad [t] = -2$$

$$A_\mu(x) \rightarrow B_\mu(t, x)$$

$$\psi(x) \rightarrow \chi(t, x)$$

- Renormalizable smoothing for local fields

- Smoothing at short distance $\sqrt{8t}$



- Gaussian damping at large momenta

- Flowed gauge fields are finite

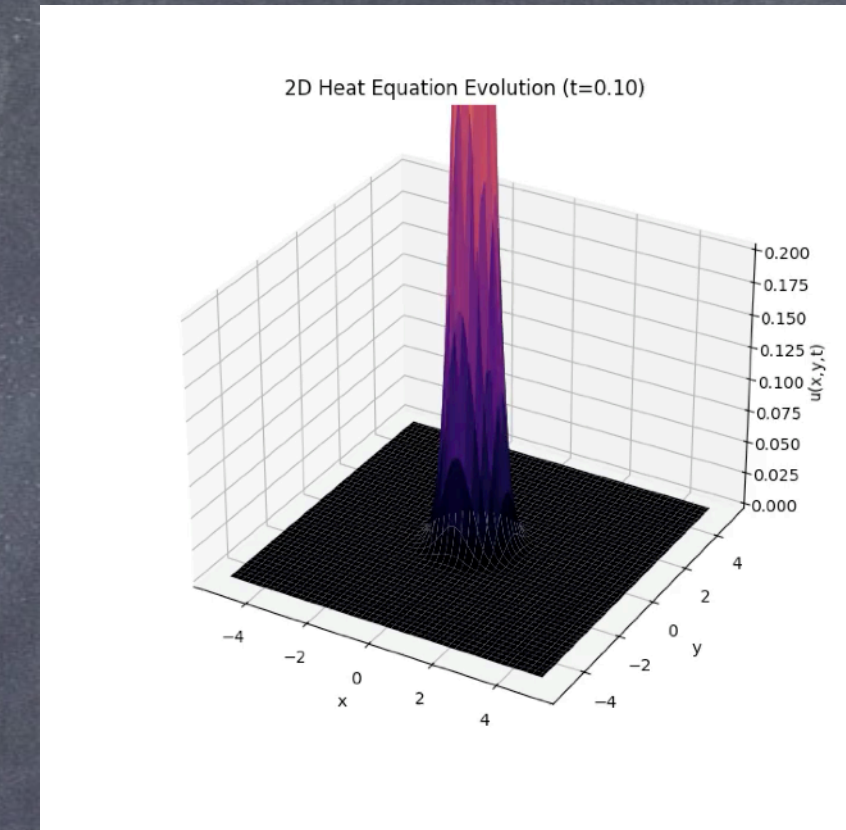
Lüscher: 2010
Lüscher, Weisz: 2011

- Renormalization of fermion operator multiplicative and "universal"

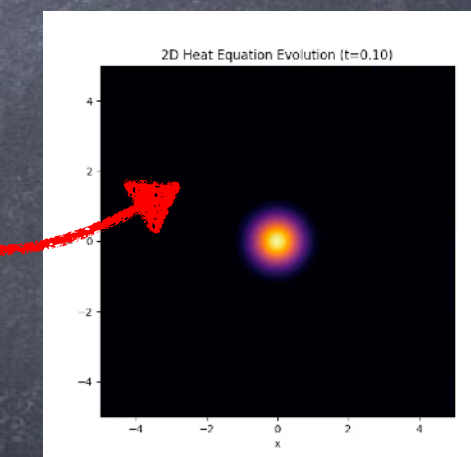
Lüscher: 2013

$$\dot{\chi}(t, x) \propto \frac{\chi(t, x)}{\sqrt{t^2 \langle \bar{\chi}(t, x) \not{D} \chi(t, x) \rangle}}$$

Makino, Suzuki: 2014



$\sqrt{8t}$



What is OpenLat



<https://openlat1.gitlab.io>

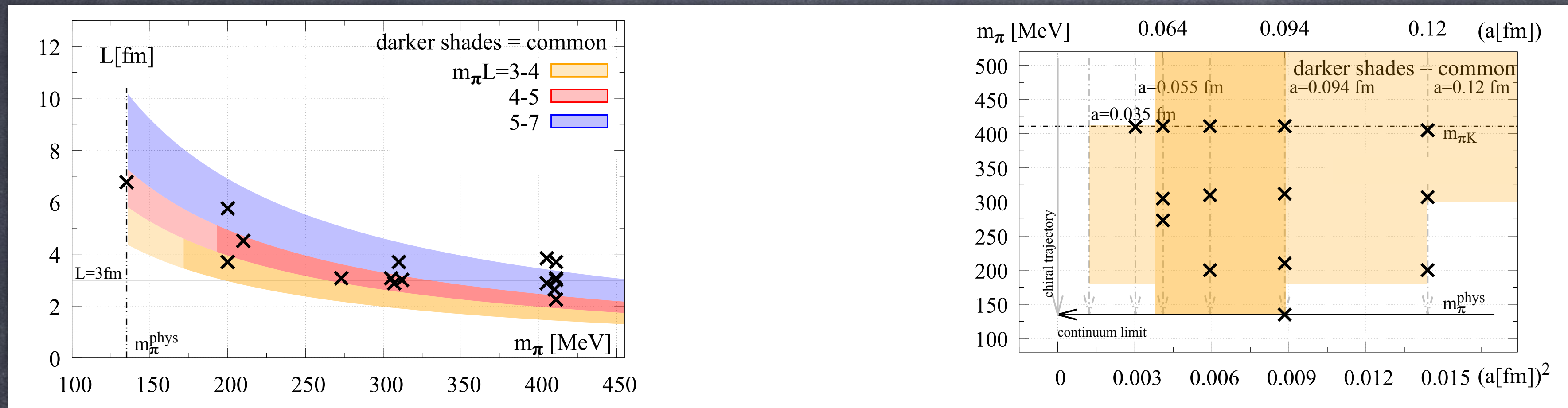
- OpenLat provides open access to cutting-edge (2+1)-flavor QCD gauge field ensembles, enabling the study of strong interaction phenomena with state-of-the-art simulations.
- The initiative bridges the gap for researchers without access to large-scale collaborations, fostering innovation and inclusivity in lattice QCD.
- Strategic choice of stabilized Wilson fermion framework for precision and stability in QCD simulations.



OpenLat: Current Status & Key Research Projects

OpenLat has made significant progress in producing and sharing high-quality lattice QCD ensembles.

Our two main research projects focus on precision studies of the thetaEDM parameter and advancements in lattice PDF calculations.

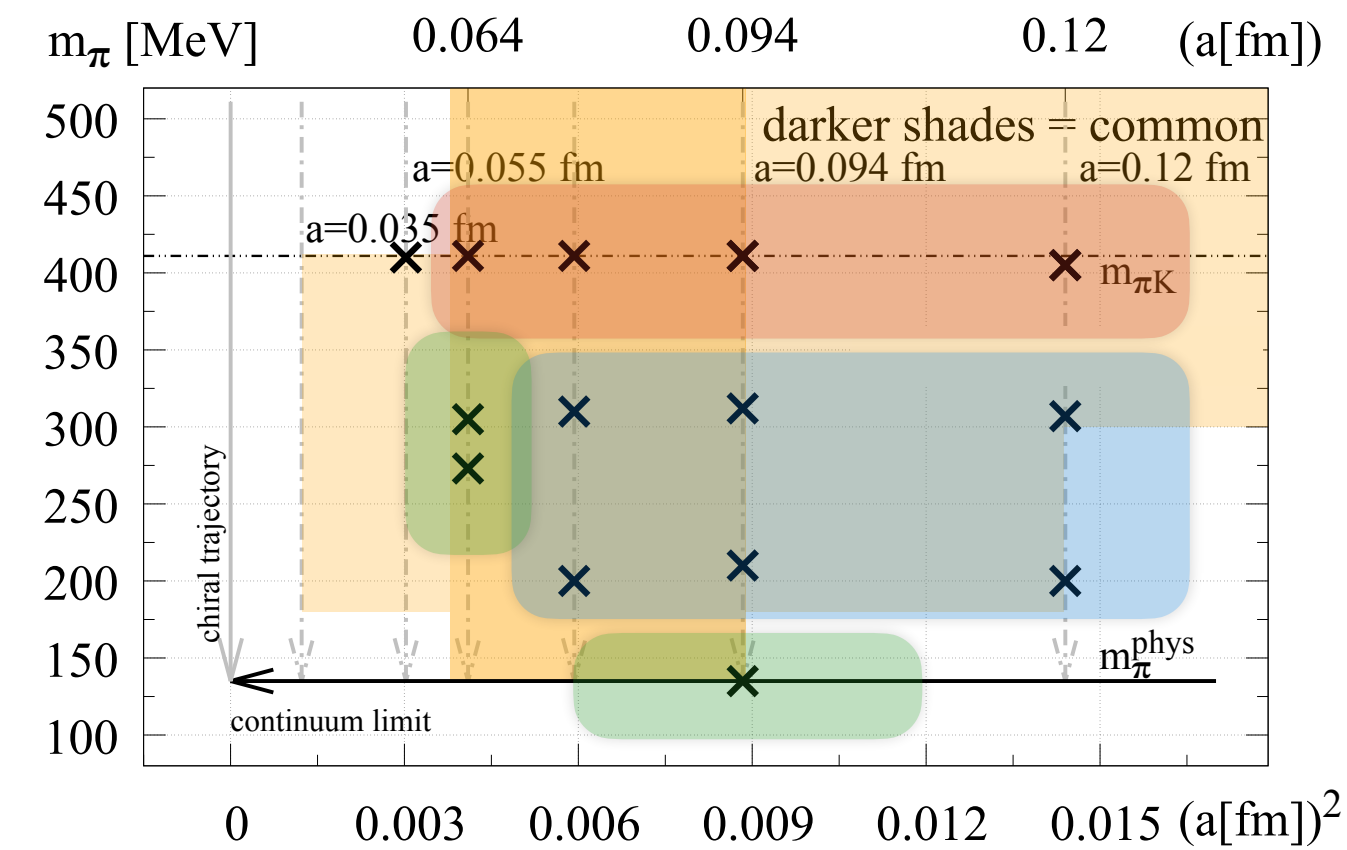
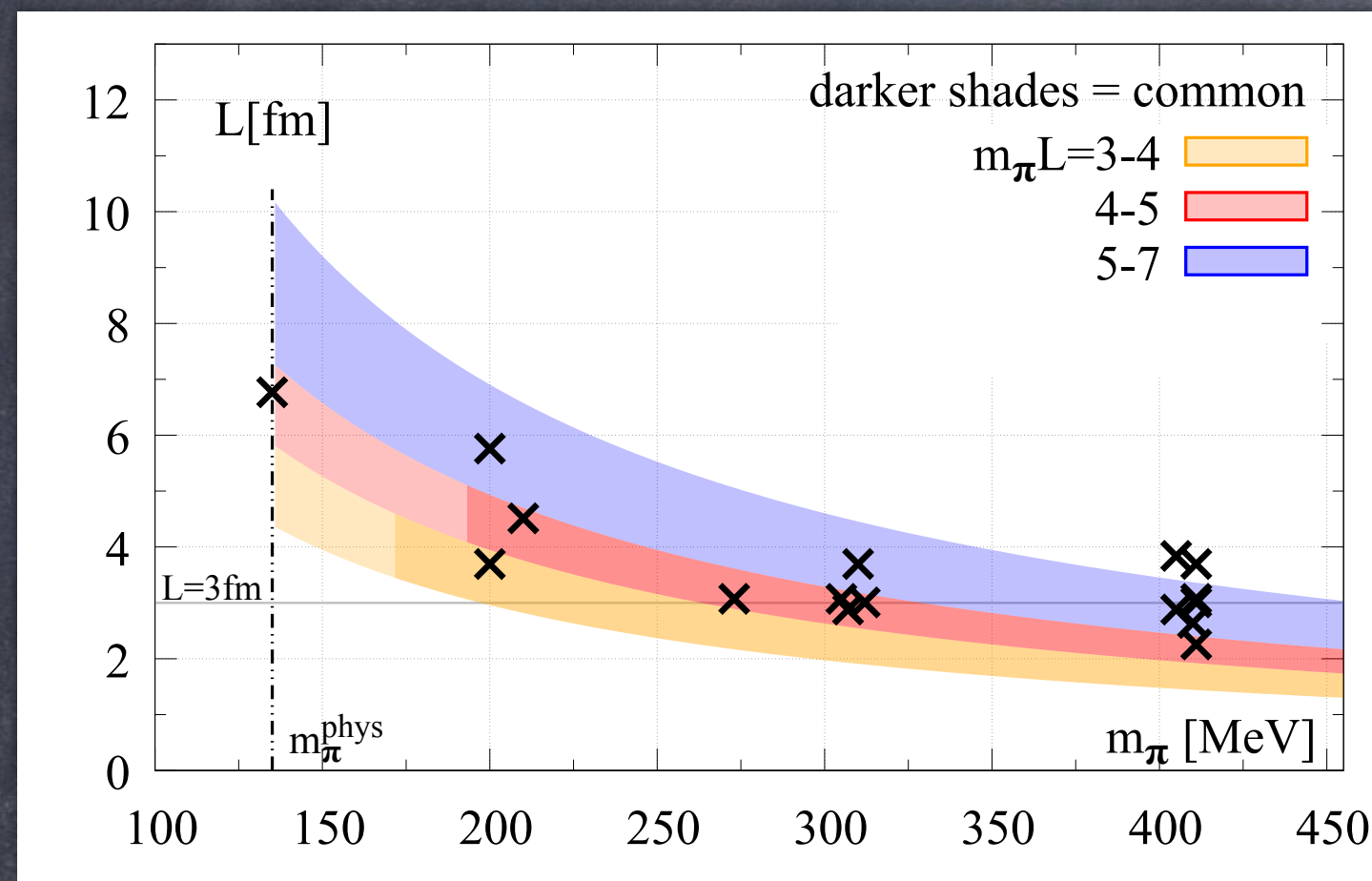


Project	Main Goal	Progress
EDM	Improve constraints on CP-violating effects in strong interactions (SM & BSM)	New lattice ensembles generated; analysis ongoing.
PDF	Develop new lattice techniques for parton distribution function (PDF) determination	Implementation of flowmom method; preliminary results obtained
Multi-hadron interactions		
Flavor physics		

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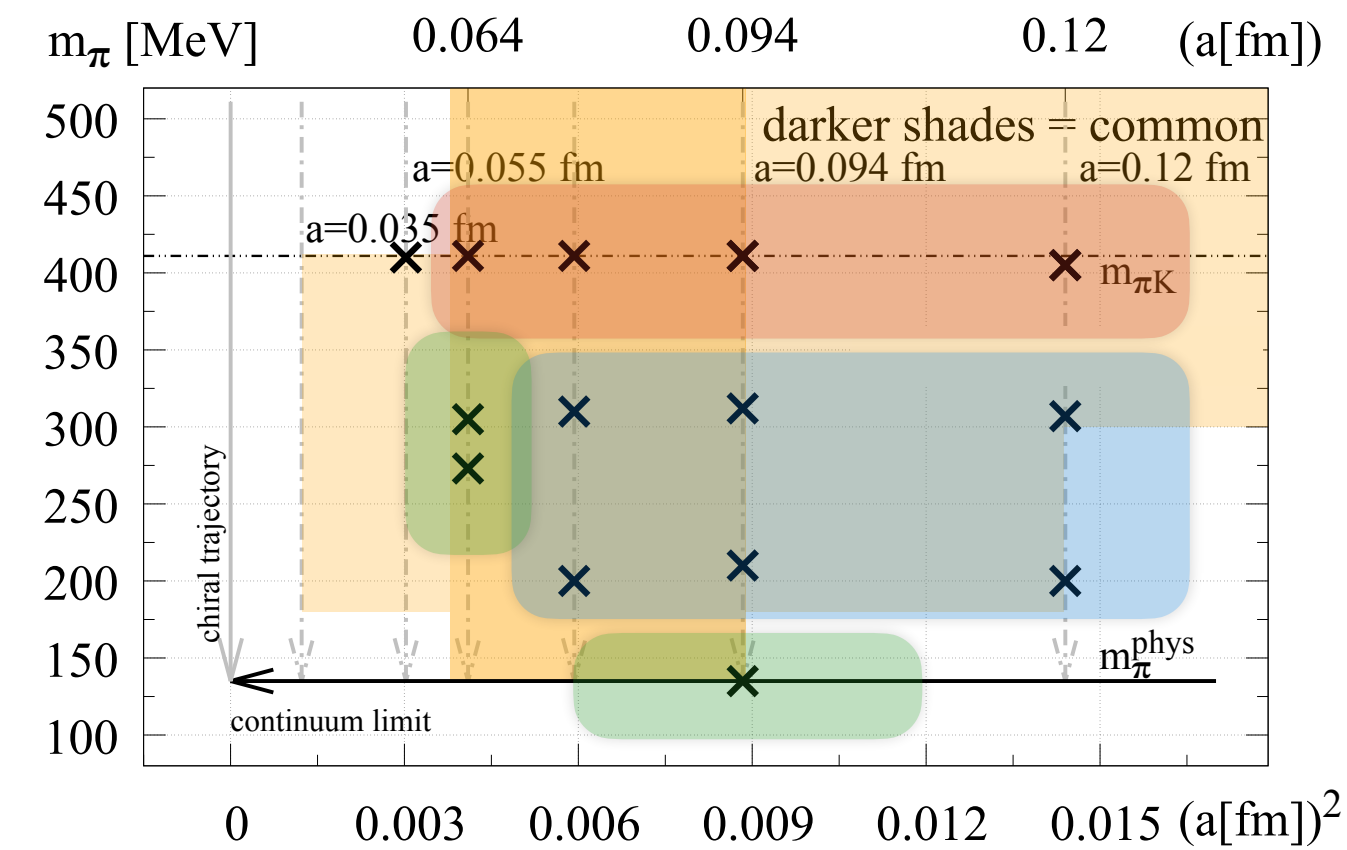
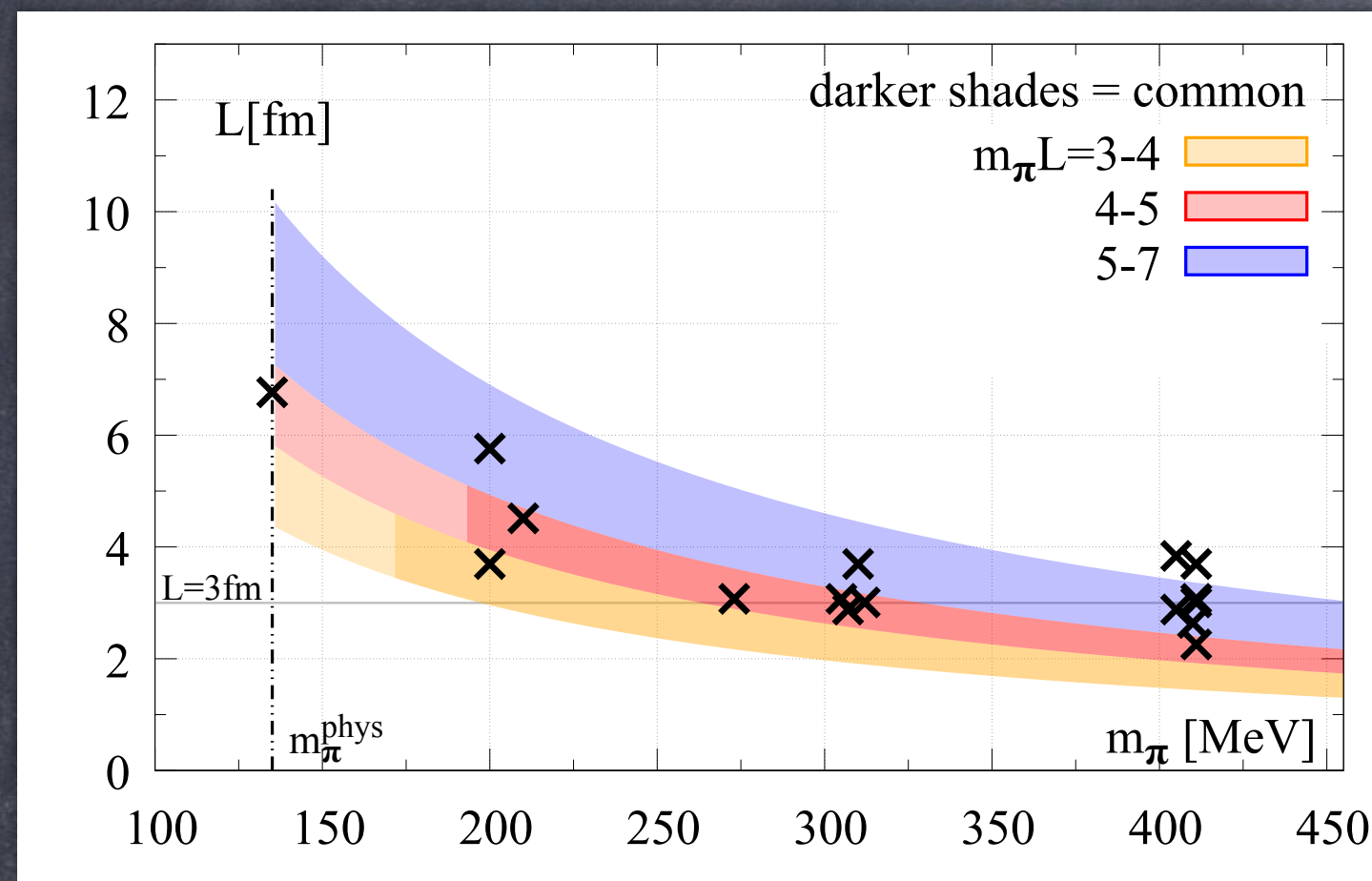


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Perlmutter (NERSC)



JUWELS (FZJ)



Irene Joliot-Curie



Gradient flow and topological charge

Lüscher: 2010

$$Q(t) = \int d^4x \, q(x, t) \quad q(x, t) = \frac{1}{32\pi^2} \epsilon_{\mu\nu\rho\sigma} \text{Tr} \{ G_{\mu\nu}(x, t) G_{\rho\sigma}(x, t) \}$$

$$\delta B_\mu(x, t) = \partial_t B_\mu \delta t$$

+

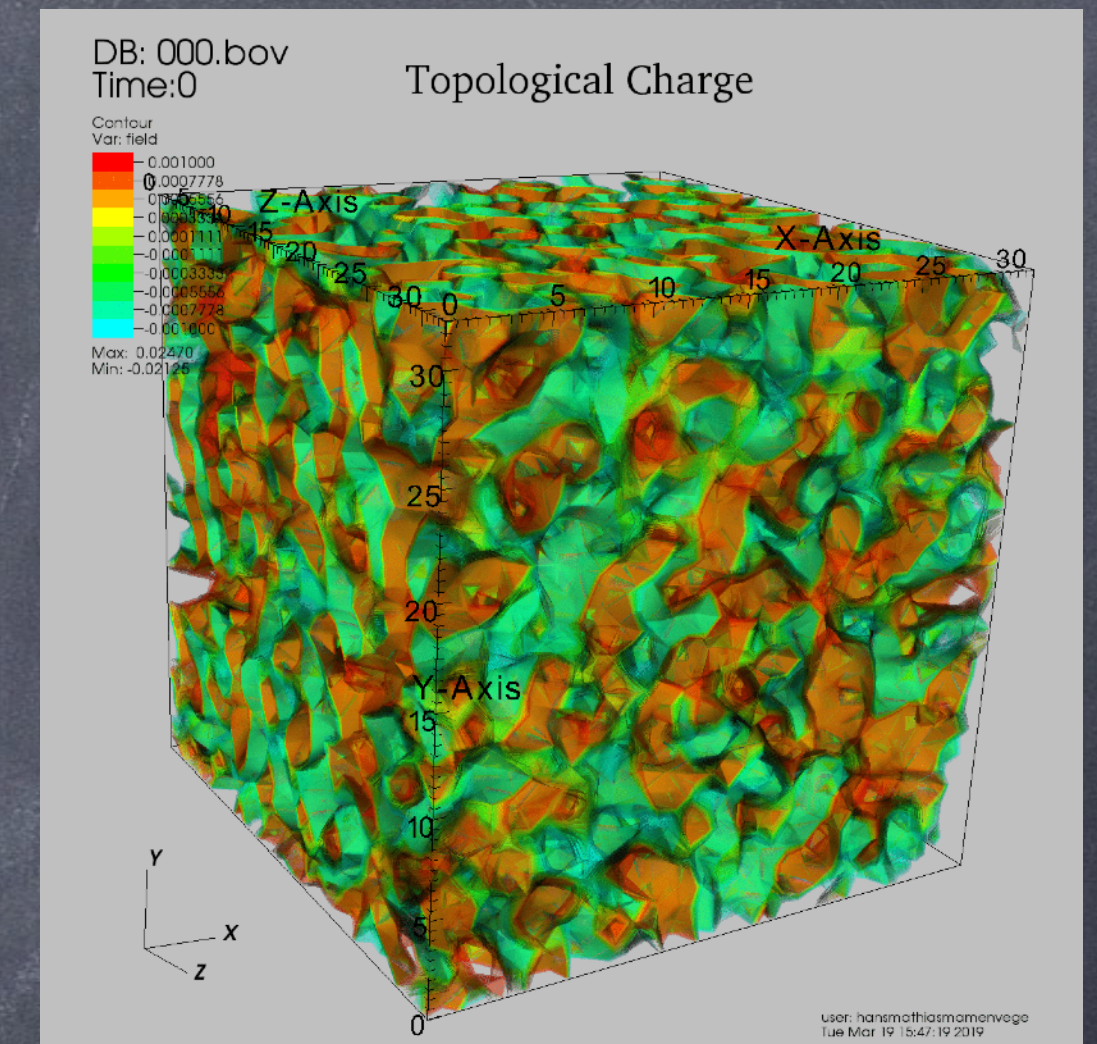
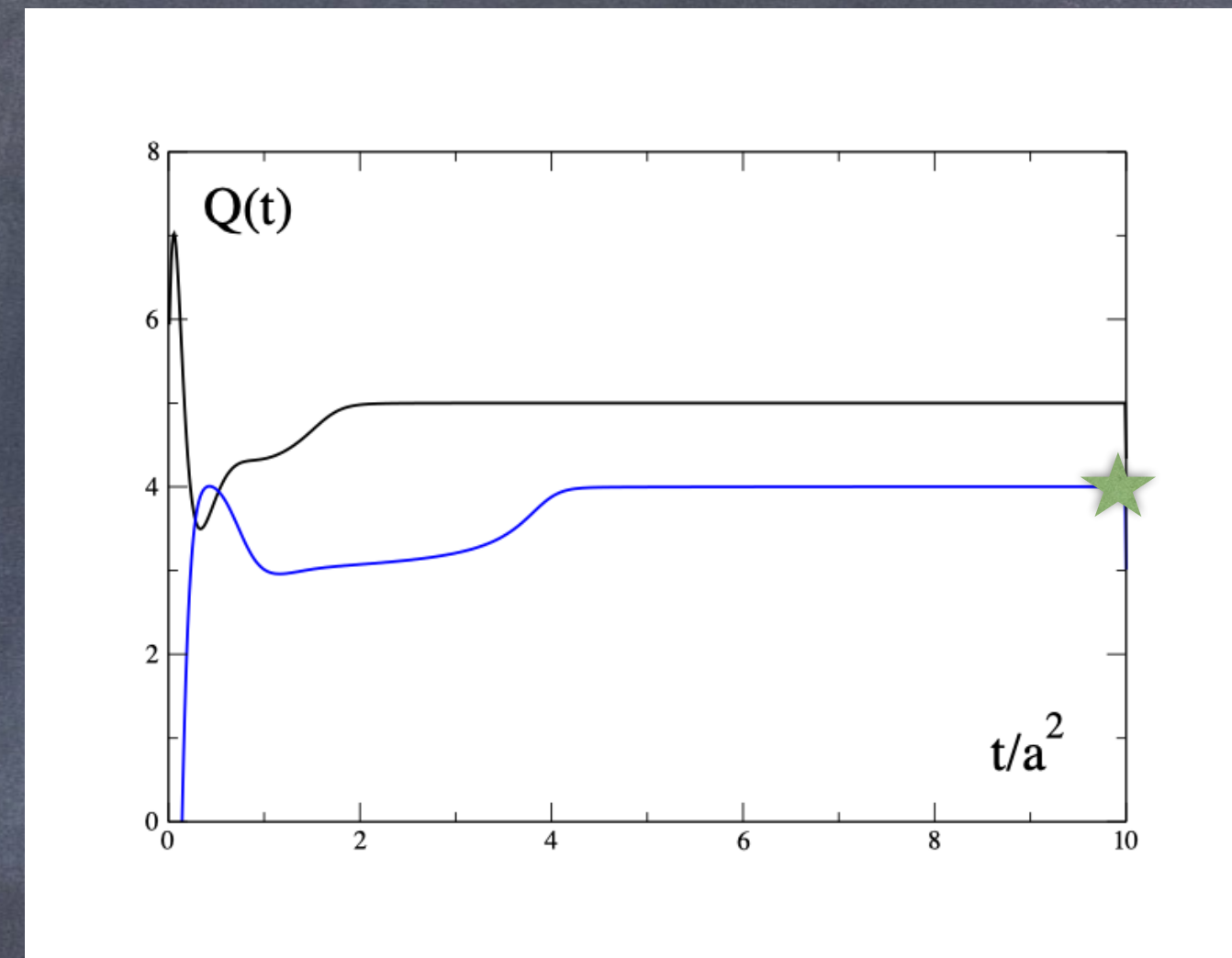
Bianchi identities

$$\partial_t q(x, t) = \partial_\mu \mathcal{K}_\mu(x, t)$$

$$\mathcal{K}_\mu(x, t) = \frac{1}{8\pi^2} \epsilon_{\mu\nu\rho\sigma} \text{Tr} [G_{\nu\rho}(x, t) D_\alpha G_{\alpha\sigma}(x, t)]$$

$$\langle \cdots [Q(t)]_R \cdots \rangle = \langle \cdots Q(t) \cdots \rangle$$

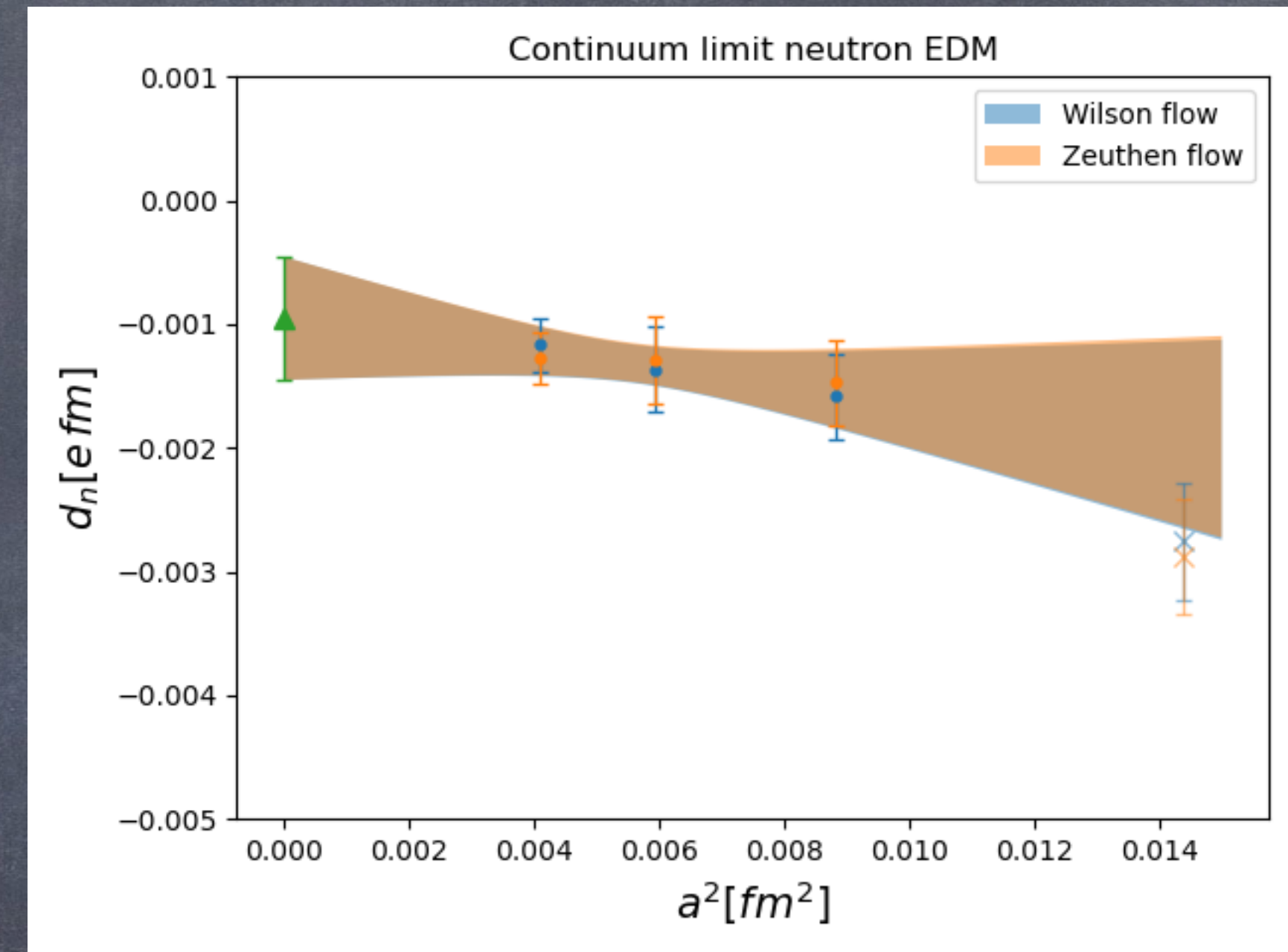
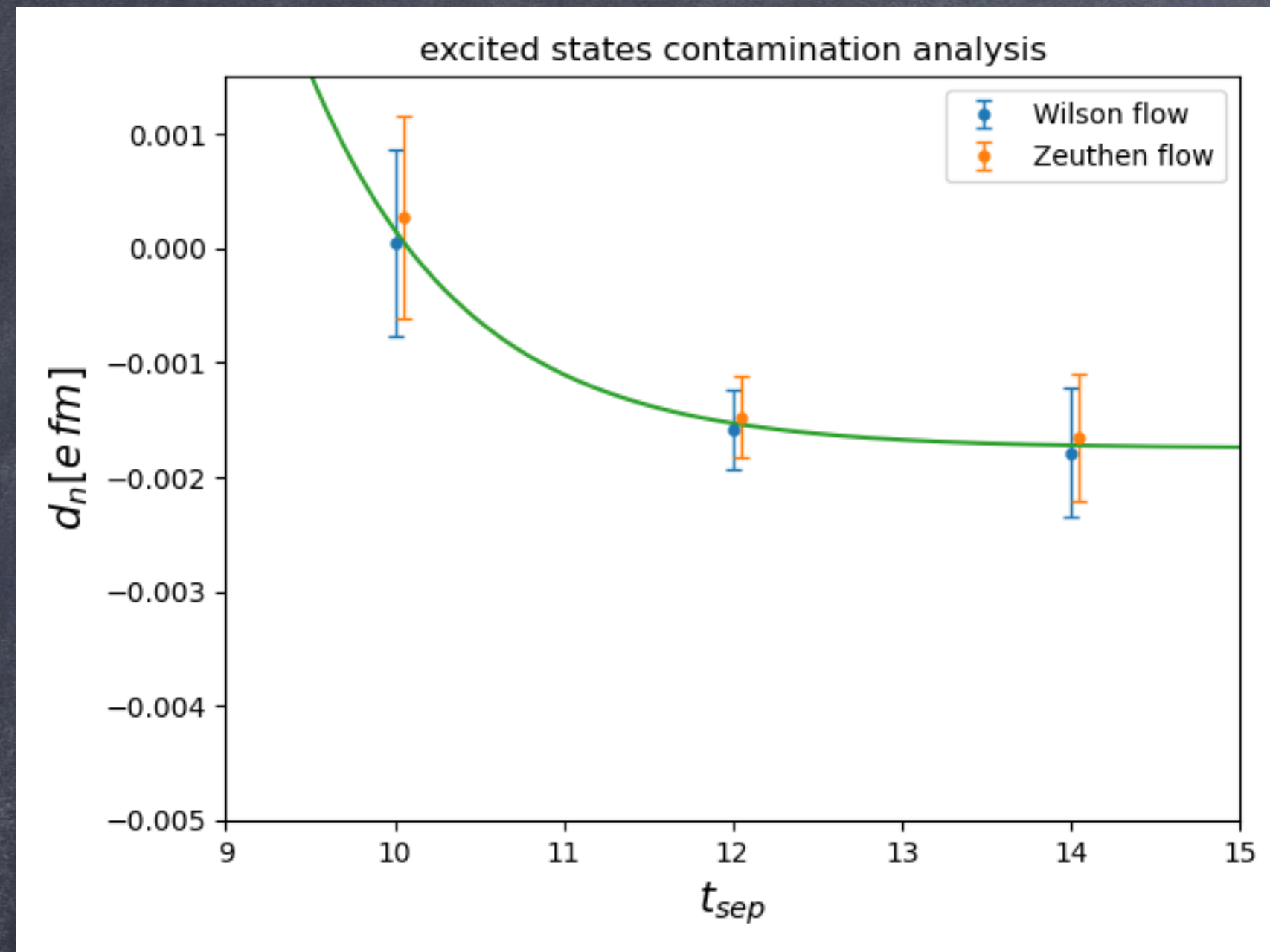
$$\partial_t Q(t) = 0 \quad Q = \int d^4x \, q(x, t) \quad \text{Equivalent to fermionic definition}$$



Pederiva, Vege: 2018
LatViz

Polyakov: 1987, Lüscher: 2010 Ce', Consonni, Engel, Giusti: 2015 Lüscher: 2021 Lüscher, Weisz: 2021

Systematics



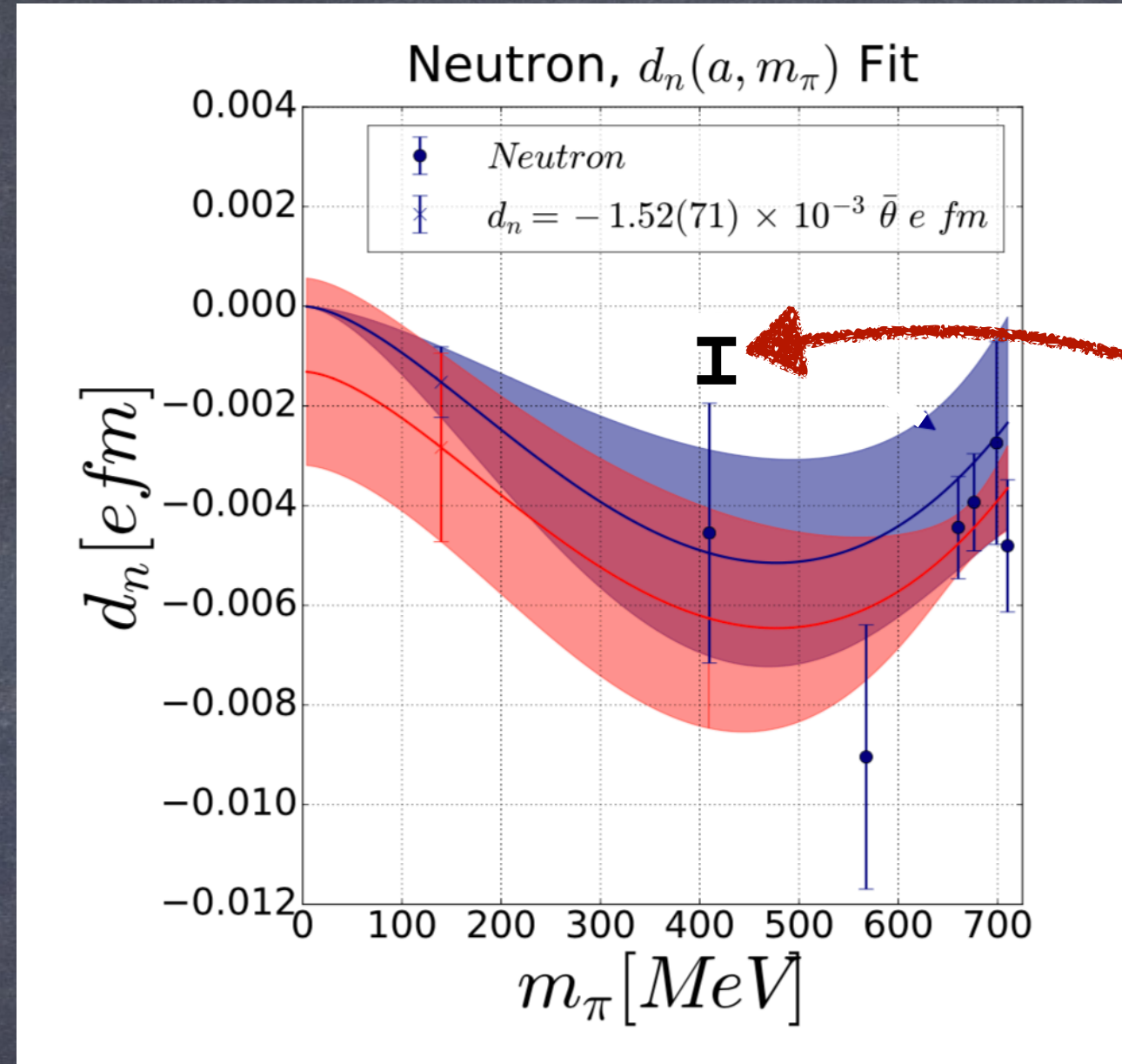
$$d_n(t_{sep}) = d_n + A \cdot e^{-\delta t_{sep}}$$

- ESC under control for $t_{sep} \gtrsim 1.1$ fm for $m_\pi \simeq 410$ MeV
- Compare with χ PT predictions

- Topological charge computed $\sqrt{8t} \simeq 0.56$ fm
- Results consistent with expected $O(a)$ improvement
- Zeuthen flow Sint, Ramos: 2015

Neutron EDM from theta term

Dragos, Luu, A.S.,
de Vries, Yousif: 2019



$$d_n(\bar{\theta}) = \bar{d}_n - \frac{eg_A \bar{g}_0^{\bar{\theta}}}{8\pi^2 F_\pi} \ln \frac{m_\pi^2}{M_N^2}$$

Ottad et al.: 2010
Mereghetti et al.: 2011

$$d_{n/p}(a, m_\pi) = C_1^{n/p} m_\pi^2 + C_2^{n/p} m_\pi^2 \ln \frac{m_\pi^2}{M_N^2} + C_3^{n/p} a^2$$

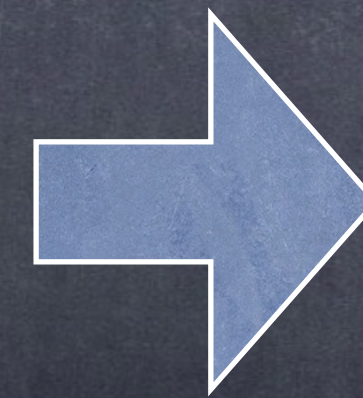
$$d_n(m_\pi = 412 \text{ MeV}) = -0.00095(50) \bar{\theta} e \text{ fm}$$

Kim, A.S. (OpenLat): 2025

$$d_n^{\text{phys}} = -0.00152(71) \bar{\theta} e \text{ fm}$$

$$\bar{g}_0^{\bar{\theta}} = -1.28(64) \cdot 10^{-2} \bar{\theta}$$

Ab-initio determination of $\bar{g}_0^{\bar{\theta}}$



$$|\bar{\theta}| < 1.98 \times 10^{-10} (90\% \text{CL})$$

$$\bar{g}_0^{\bar{\theta}} = -1.47(23) \cdot 10^{-2} \bar{\theta}$$

Crewther et al.: 1980
de Vries et al.: 2015

Quark-Chromo EDM

&

3-gluon CP-odd

Challenges with BSM operators

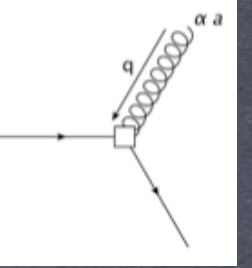
- Operators mix with lower dimensional operators
- Power divergences need to be subtracted non-pertubatively
- Additional complicated mixing pattern

Maiani, Martinelli, Sachrajda: 1992

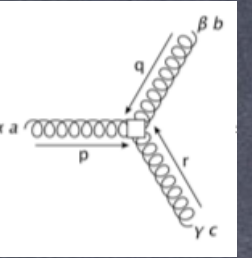
Bhattacharya, Cirigliano,
Gupta, Mereghetti, Yoon: 2015

Cirigliano, Mereghetti, Stoffer: 2020

$$O_{\text{CE}}^f(x) = \bar{\psi}_f(x) \gamma_5 \sigma_{\mu\nu} G_{\mu\nu}^a T^a \psi_f(x)$$



$$O_{3g}(x) = \frac{1}{6} i f^{abc} G_{\mu\rho}^a(x) G_{\nu\rho}^b(x) G_{\lambda\sigma}^c(x) \epsilon_{\mu\nu\lambda\sigma}$$



$$[O_{\text{CE}}]_R = Z_{\text{CE}} \left[O_{\text{CE}} - \frac{C}{a^2} P \right] + \dots$$

$$P^f(x) = \bar{\psi}_f(x) \gamma_5 \psi_f(x)$$

$$[O_{3g}]_R = Z_{3g} \left[O_{3g} - \frac{C'}{a^2} q \right] + \dots$$

$$q(x) = \frac{1}{32\pi^2} \epsilon_{\mu\nu\rho\sigma} \text{tr} \{ G_{\mu\nu}(x) G_{\rho\sigma}(x) \}$$

qCEDM with RI-MOM Off-shell

$$\frac{1}{a} \quad d=4 \rightarrow 2 \text{ operators} + 3 \text{ O(m)}$$

$$\log a \quad d=5 \rightarrow 3 \text{ operators} + (7 + 5) \text{ O(m, m}^2\text{)} + 4 \text{ "nuisance"}$$

Strategy – Short flow-time expansion

$$\dot{O}_i(t) = \sum_j \zeta_{ij}(t, \mu) [O_j(t=0, \mu)]_{\text{R}} + O(t)$$

Lüscher: 2013

A.S., Luu, de Vries: 2014–2015

Dragos, Luu, A.S. de Vries: 2018–2019

Rizik, Monahan, A.S.: 2018–2020

A.S.: 2020

Kim, Luu, Rizik, A.S.: 2020

Mereghetti, Monahan, Rizik, A.S.,

Stoffer: 2021

Crosas, Monahan, Rizik, A.S.,

Stoffer: 2023

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↑
LQCD

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- Calculation of matrix elements with flowed fields
 - Multiplicative renormalization (no power divergences and no mixing)

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- Calculation of Wilson coefficients

- Insert OPE in off-shell amputated 1PI Green's functions

$$\zeta_{ij}(t, \mu) = \delta_{ij} + \frac{\alpha_s(\mu)}{4\pi} \zeta_{ij}^{(1)}(t, \mu) + O(\alpha_s^2)$$

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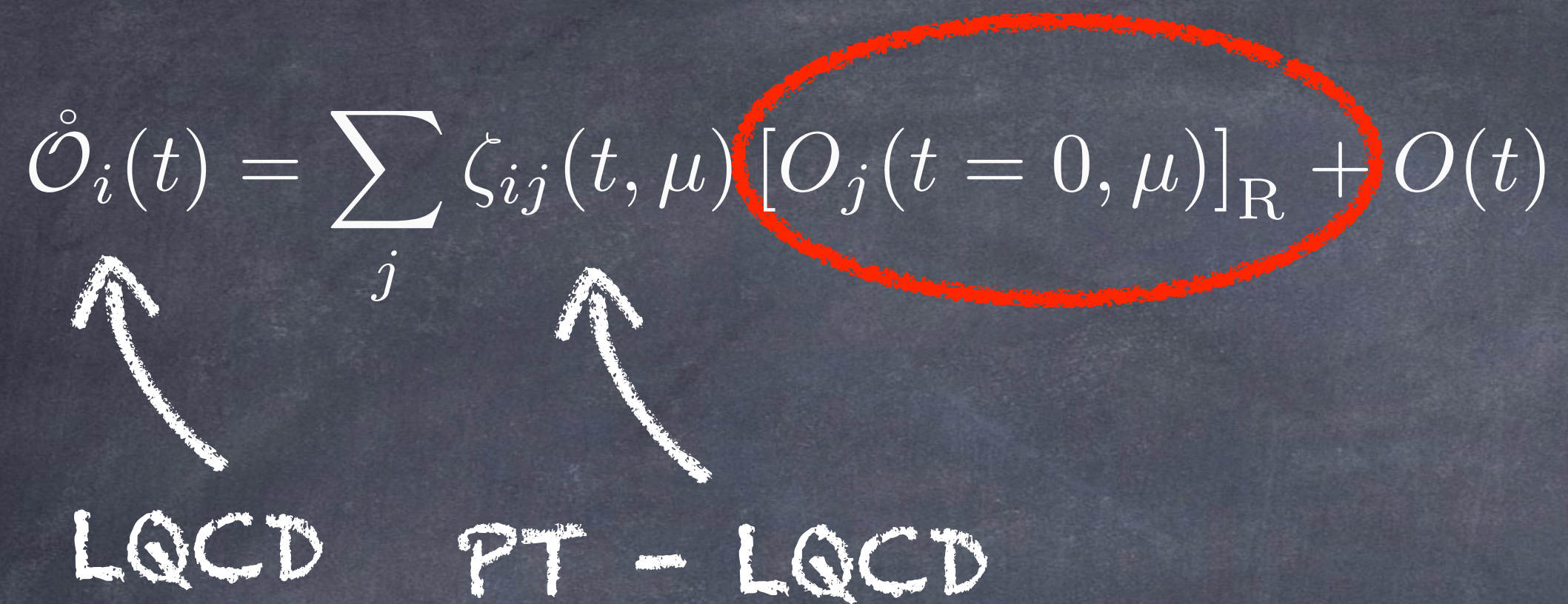
- Insert OPE in off-shell amputated 1PI Green's functions

- Power divergences subtracted non-perturbatively (LQCD)

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Lüscher: 2013

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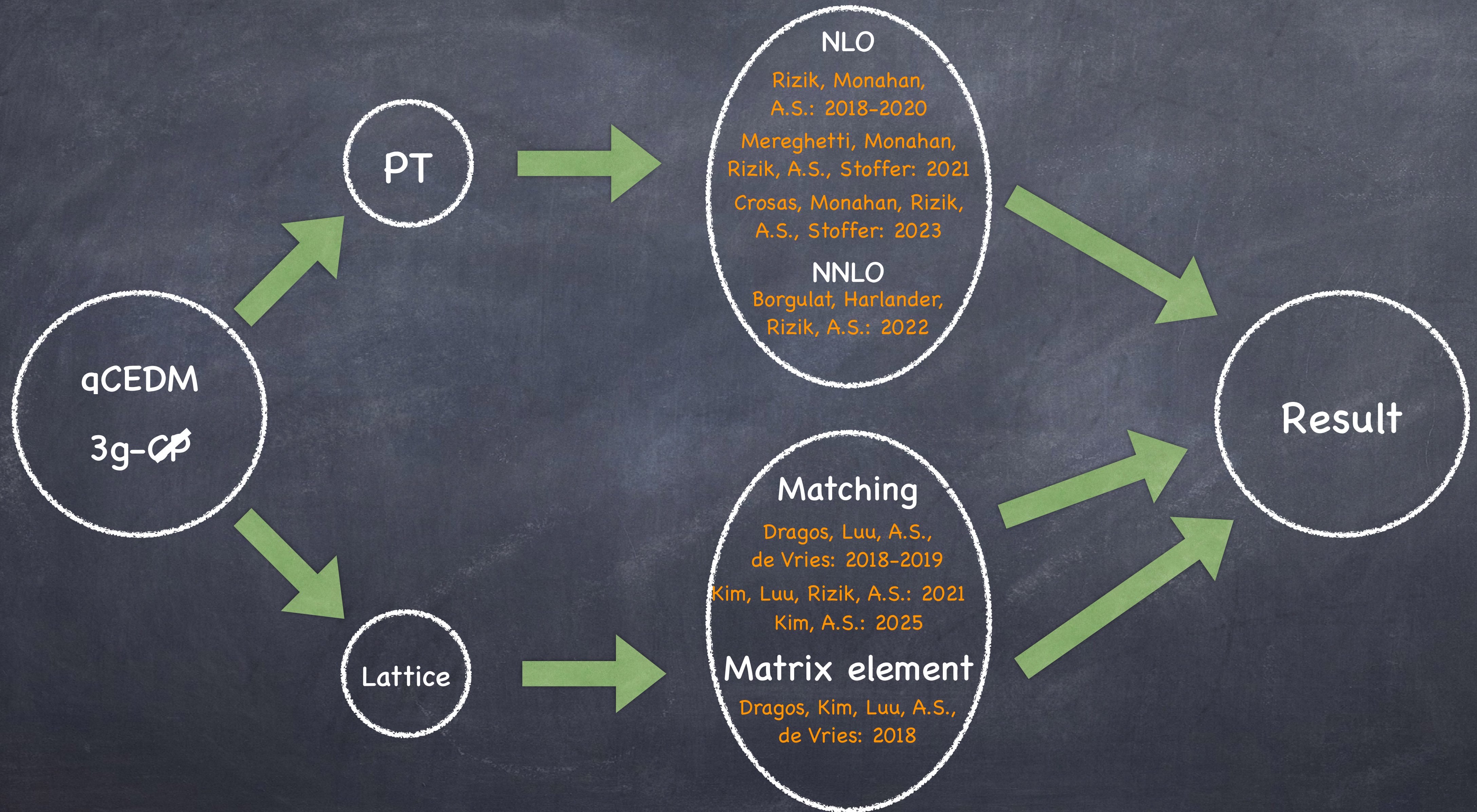
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- Power divergences subtracted non-perturbatively (LQCD)

- Determination of the physical renormalized matrix element at zero flow-time

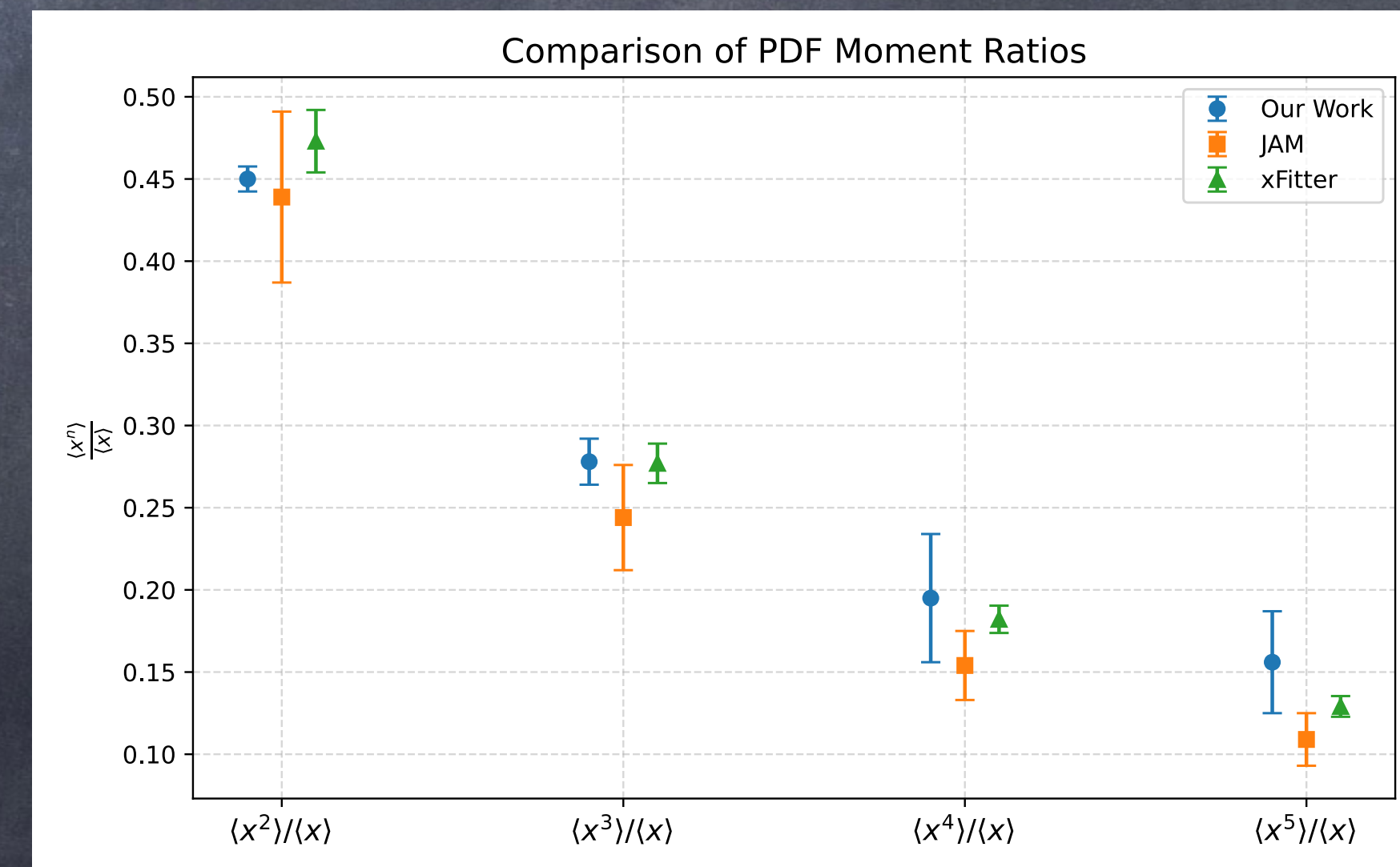
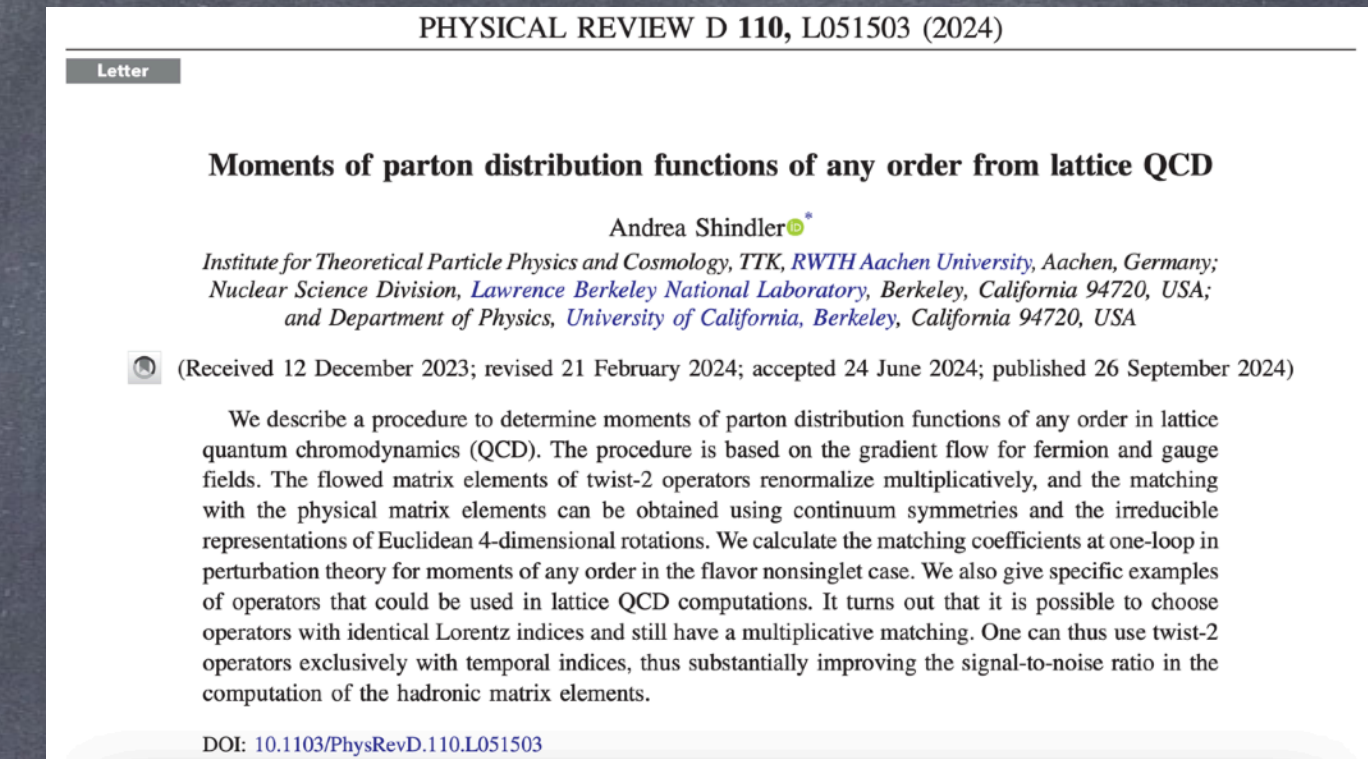
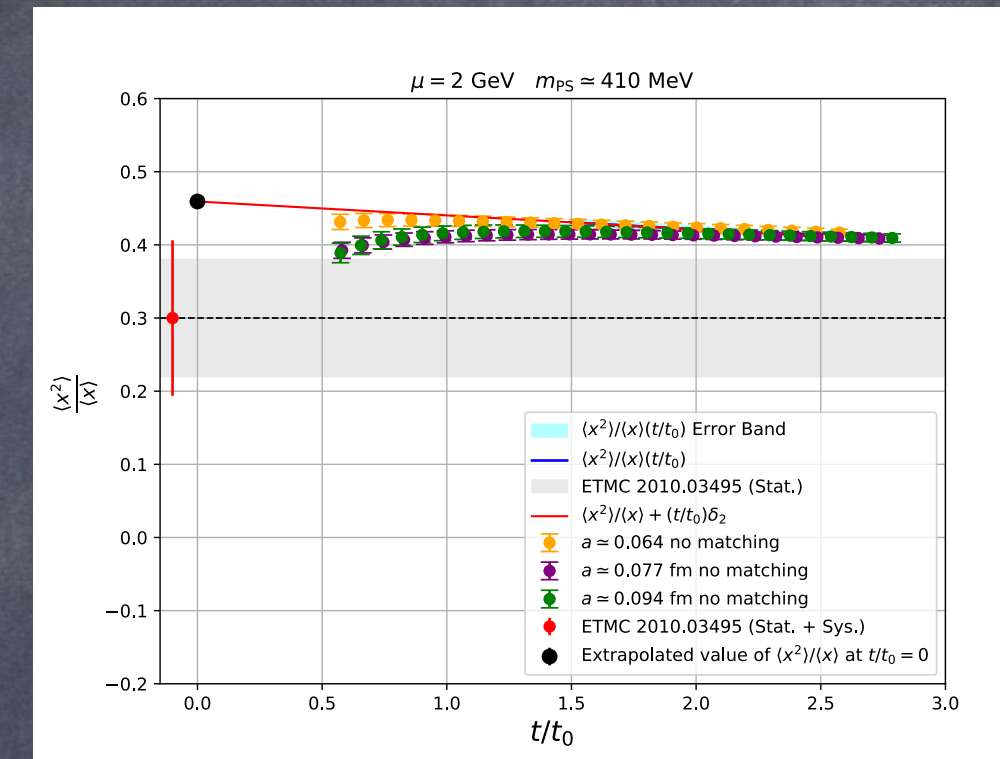
$$\zeta_{ij}(t, \mu) = \delta_{ij} + \frac{\alpha_s(\mu)}{4\pi} \zeta_{ij}^{(1)}(t, \mu) + O(\alpha_s^2)$$

BSM contributions



Flowed moments – success

- PDFs describe quark and gluon structure of hadrons — essential for LHC predictions
- Large Bjorken- x remains poorly constrained due to limited experimental input
- New method to compute arbitrary PDF moments using gradient flow **A.S.: 2023**
- Enables reconstruction of PDFs from **first principles** with controlled uncertainties
- First lattice result for the pion valence PDF **competitive with global fits.**

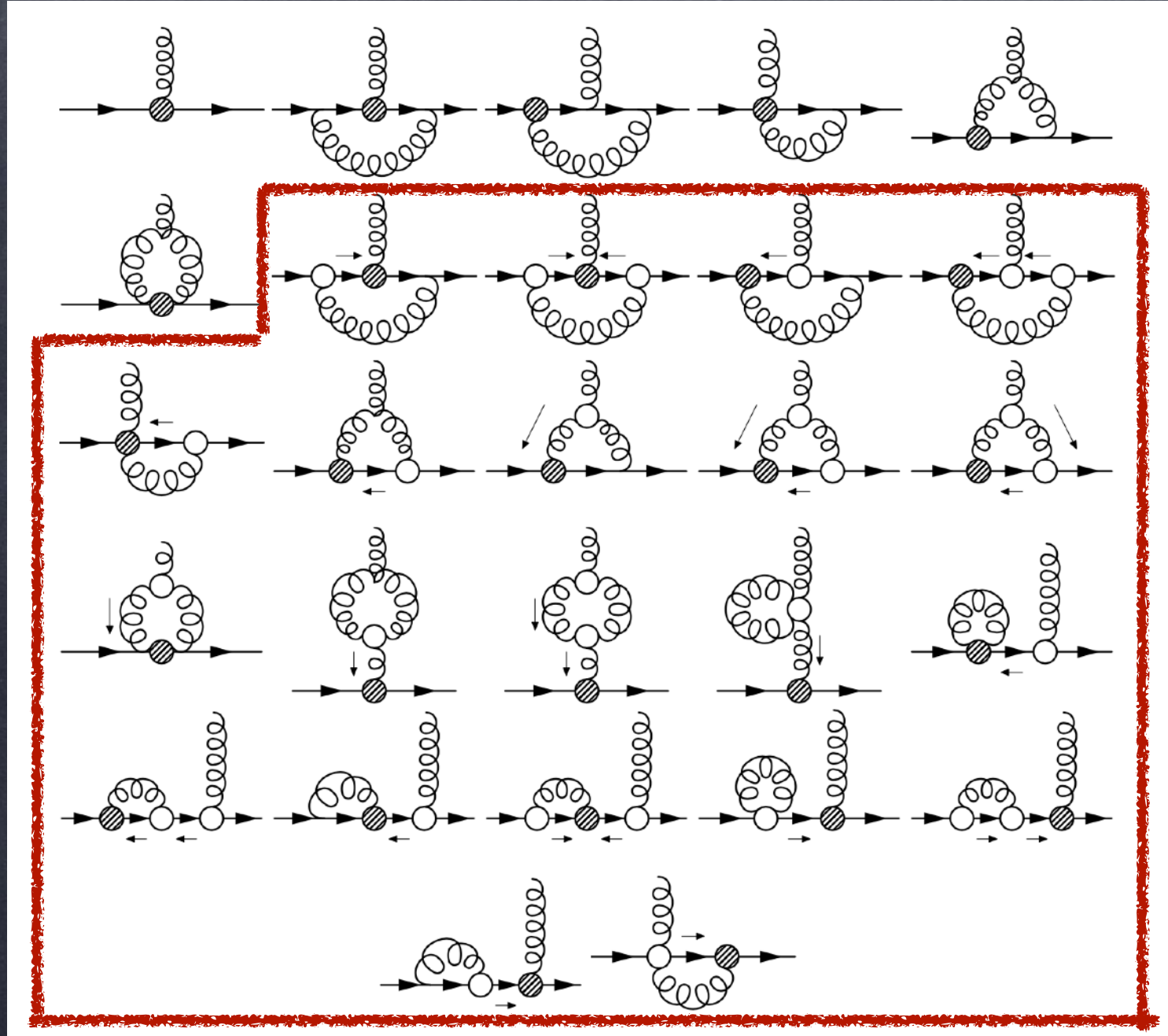


Karur, Kim, Pefkou,
A.S., Walker-Loud (OpenLat): 2025

Quark-Chromo EDM

Rizik, Monahan, A.S.: 2020
Mereghetti, Monahan, Rizik, A.S.,
Stoffer : 2021

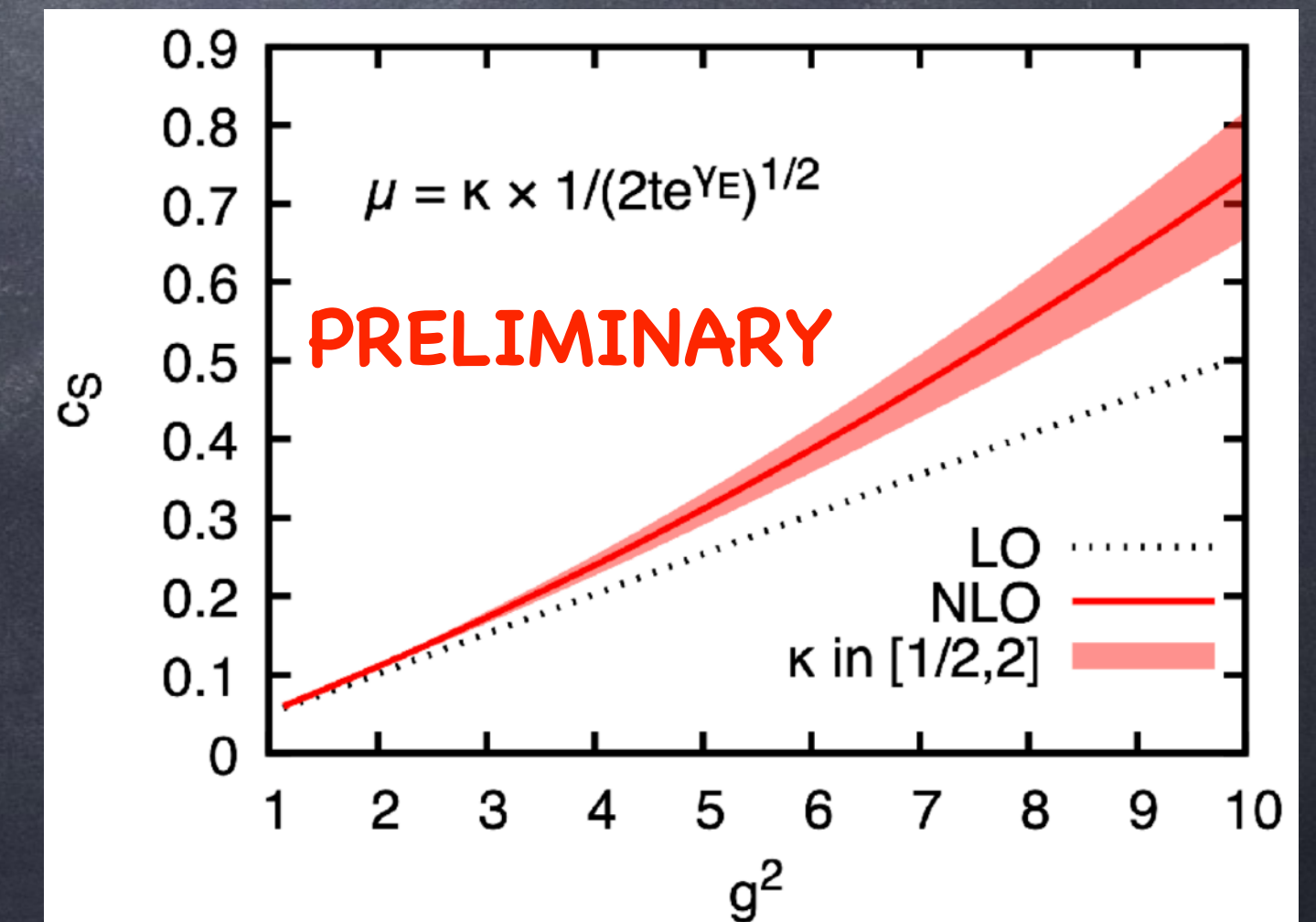
$$\zeta_{\text{CE,CE}}(t, \mu)$$



- Expand integrands of loop integrals in all scales excluding t
 - Analytic structure altered $\rightarrow$ distortion of IR structure
 - in matching equation the IR modification drops out in the difference
 - Expanding loop integrals in the RHS vanish in DR $\rightarrow$ UV and IR are identical
 - The LHS is UV-finite, beside the renormalization of the bare parameters and flowed fermion fields
 - The IR singularities on the LHS exactly match the UV MS counterterms

$$\begin{aligned} \zeta_{\text{CE,CE}}(t, \mu) &= \zeta_{\chi}^{-1} + \frac{\alpha_s}{4\pi} \left[2(C_F - C_A) \log(8\pi\mu^2 t) - \frac{1}{2} \left((4 + 5\delta_{\text{HV}})C_A + (3 - 4\delta_{\text{HV}})C_F \right) \right] \\ &= 1 + \frac{\alpha_s}{4\pi} \left[(5C_F - 2C_A) \log(8\pi\mu^2 t) \right. \\ &\quad \left. - \frac{1}{2} \left((4 + 5\delta_{\text{HV}})C_A + (3 - 4\delta_{\text{HV}})C_F \right) - \log(432)C_F \right] \end{aligned}$$

Borgulat, Harlander, Rizik, A.S.: in progress



Quark-Chromo EDM: power divergences

Kim, Luu, Rizik, A.S.:2020

$$\dot{\mathcal{O}}_{\text{CE}}(t) = \frac{\zeta_{\text{OP}}(t, \mu)}{t} P_{\text{R}}(0, \mu) + \sum_i \zeta_{\text{CE},i}(t, \mu) \mathcal{O}_{i,\text{R}}(0, \mu)$$

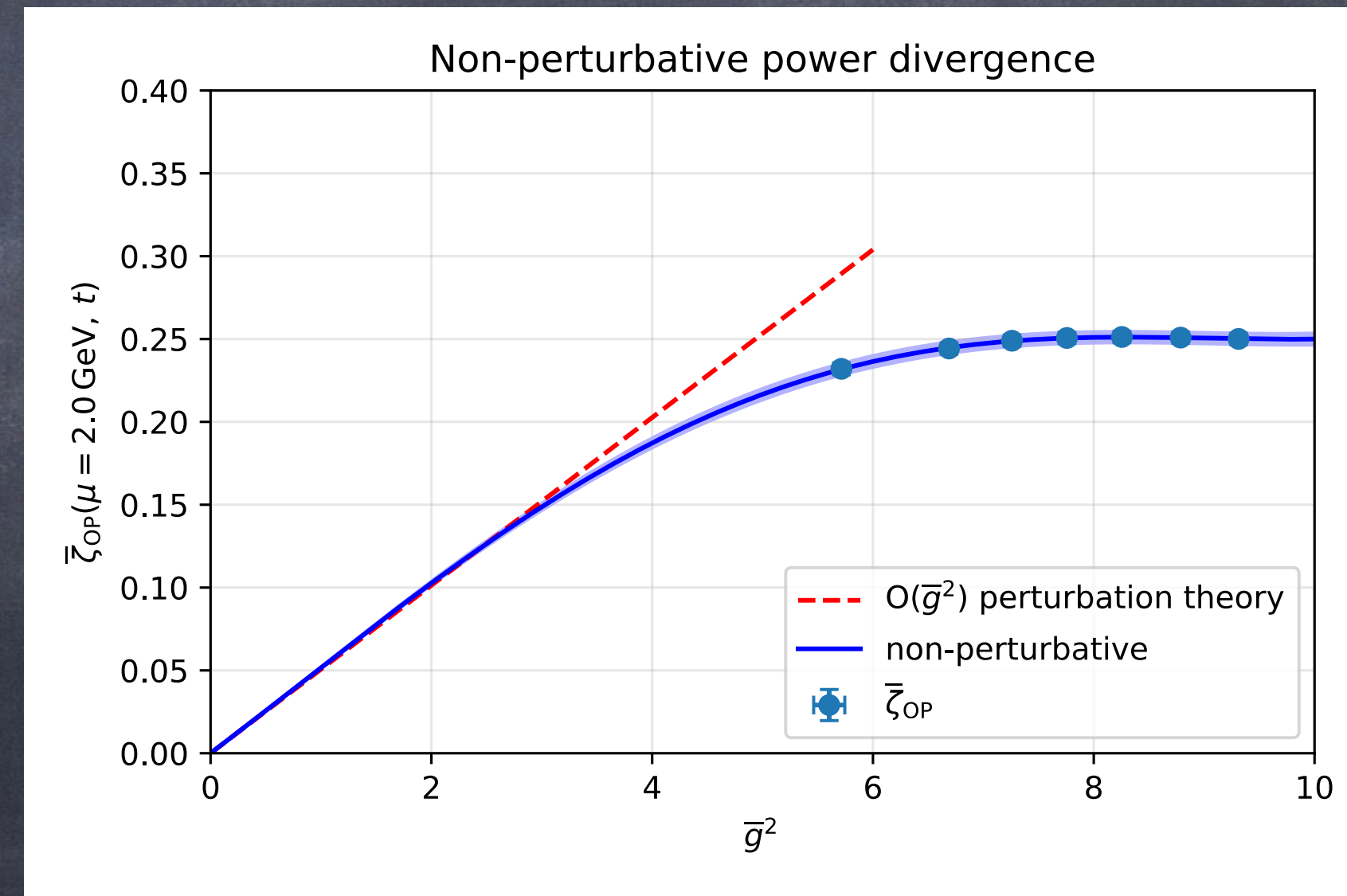
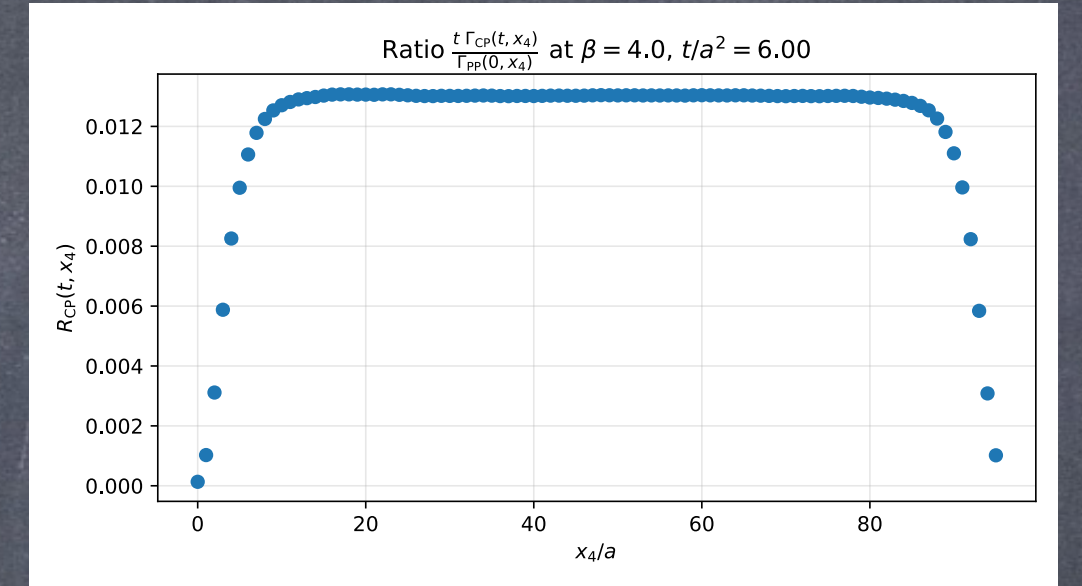
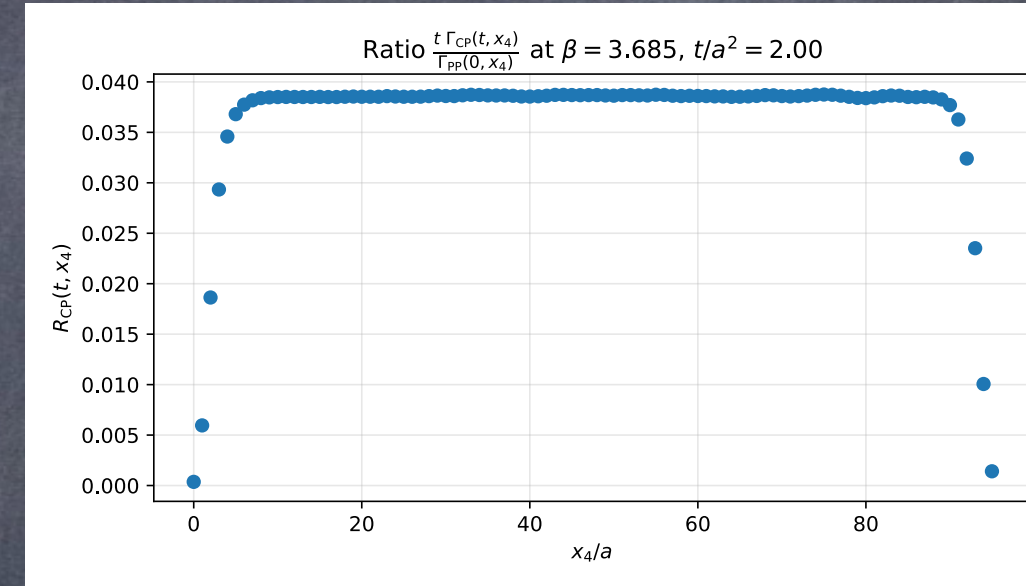
$$\Gamma_{CP}(t, x_4) = a^3 \sum_{\mathbf{x}} \left\langle \mathcal{O}_{CE}^{ij}(t, \mathbf{x}, x_4) P^{ji}(0, \mathbf{0}, 0) \right\rangle$$

$$\Gamma_{PP}(x_4) = a^3 \sum_{\mathbf{x}} \left\langle P^{ij}(x_4, \mathbf{x}) P^{ji}(0, \mathbf{0}) \right\rangle$$

$$R_{\text{CP}}(t, x_4) = t \frac{\langle 0 | \mathcal{O}_{\text{CE}}(t) | \pi \rangle}{\langle 0 | P | \pi \rangle}$$

$$\bar{\zeta}_{\text{OP}}(t, \mu) = t \frac{\langle 0 | \dot{\mathcal{O}}_{\text{CE}}(t) | \pi \rangle}{\langle 0 | P_{\text{R}}(0, \mu) | \pi \rangle}$$

$$\bar{\zeta}_{\text{OP}}(t, \mu) = \frac{1}{2\pi^2} \bar{g}^2 + \Delta^{(2)} \bar{g}^4 + \Delta^{(3)} \bar{g}^4 + \Delta^{(4)} \bar{g}^8$$



Rizik, Monahan,
A.S.: 2018-2020

Kim, A.S. (OpenLat): 2025

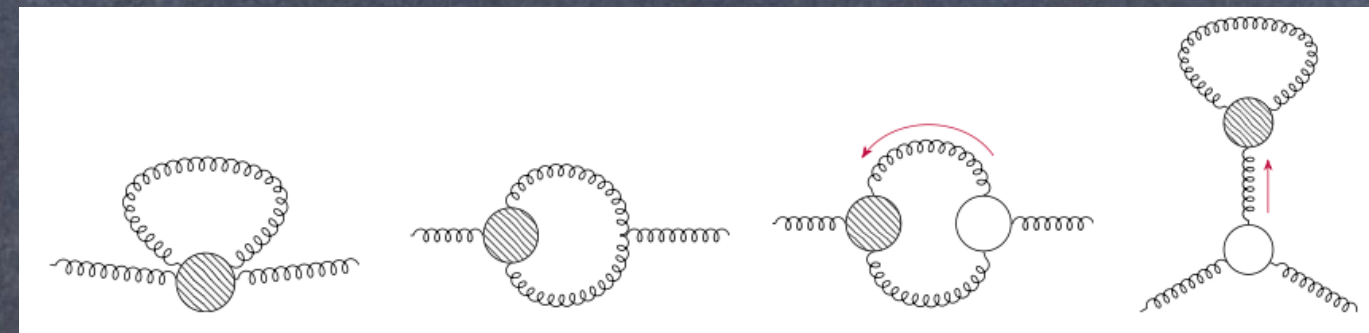
3-gluon CP-odd

Crosas, Monahan, Rizik,
A.S., Stoffer : 2023

$$\mathcal{O}_{\tilde{G}}^R(x, t) = \frac{1}{g^2} \text{tr}[G_{\mu\nu} G_{\nu\lambda} \tilde{G}_{\lambda\mu}] \quad \zeta_{ij}(t, \mu) = \delta_{ij} + \frac{\alpha_s(\mu)}{4\pi} \zeta_{ij}^{(1)}(t, \mu) + O(\alpha_s^2)$$

$$\mathcal{O}_{\tilde{G}}^R(x, t) = \sum_i \zeta_i(t, \mu) \mathcal{O}_i^{\text{MS}}(x, \mu) + \sum_i \zeta_{\mathcal{N}_i}(t, \mu) \mathcal{N}_i^{\text{MS}}(x, \mu) + \sum_i \zeta_{\mathcal{E}_i}(t, \mu) \mathcal{E}_i^{\text{MS}}(x, \mu)$$

$$\zeta_{\theta}^{(1)} = -\frac{9C_A}{4} \frac{1}{t}$$



$$\zeta_{\tilde{G}}^{(1)} = C_A \left[\frac{1}{3} + 6 \log(8\pi\mu^2 t) \right]$$

$$\zeta_{CE}^{(1)} = \frac{iC_A}{8} \left[\frac{31}{6} + 3 \log(8\pi\mu^2 t) \right]$$

$$\zeta_{\partial G}^{(1)} = -\frac{179C_A}{24} \quad \zeta_{\square\theta}^{(1)} = 0$$

$$\mathcal{O}_{\theta} = \frac{1}{g_0^2} \text{tr}[G_{\mu\nu} \tilde{G}_{\mu\nu}]$$

$$\mathcal{O}_{CE} = (\bar{q} \tilde{\sigma}_{\mu\nu} \mathcal{M} t^a q) G_{\mu\nu}^a$$

$$\mathcal{O}_{\tilde{G}} = \frac{1}{g_0^2} \text{tr}[G_{\mu\nu} G_{\nu\lambda} \tilde{G}_{\lambda\mu}]$$

$$\mathcal{O}_{\partial G} = \frac{1}{g_0^2} \partial_\nu \text{tr}[(D_\mu G_{\mu\lambda}) \tilde{G}_{\nu\lambda}]$$

$$\mathcal{O}_{\square\theta} = \frac{1}{g_0^2} \square \text{tr}[G_{\mu\nu} \tilde{G}_{\mu\nu}]$$

Neutron EDM from Lattice QCD

Quark EDM →
simplest calculation with Lattice QCD. Precision
3%–5%. No Disc.

Theta-term nucleon EDM → few calculations: 2σ
effect

→ new result have stronger signal

3 gluon operator → Preliminary lattice QCD
calculation on power divergence, 1-loop matching

4-fermion operators → No Lattice QCD
calculation, 1-loop matching

Quark-chromo EDM →

First result with LO renormalization

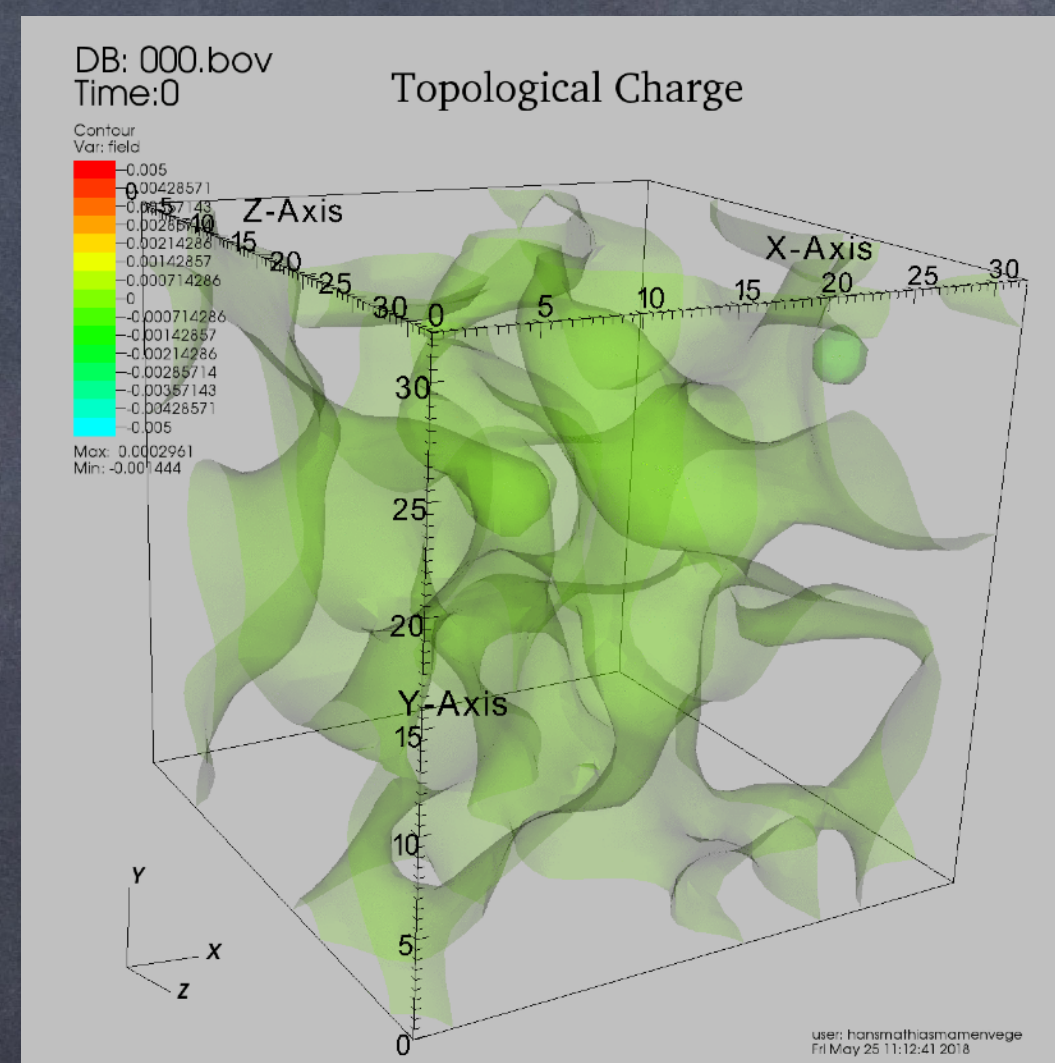
New promising approach based on gradient flow →
1-loop matching, NP power divergence,
2-loop in progress

	Renormalizati on	Continuum limit	Chiral extrapolation	Finite Volume	Excited States
θ - term	●	●	●	●	●
quark EDM	●	●	●	●	●
quark- chromo	●	●	●		
3-gluon	●				
4- fermion	●				

Summary

- Towards a new determination of nEDM from theta-term
 - Moving towards the physical point challenging (interpolation with χ PT)
- Non-perturbative renormalization qCEDM matrix elements
 - Use of gradient flow is critical $\rightarrow$ power divergences
- Perturbative matching of 3g-CP odd at NLO
 - Non-perturbative power divergence determination is in progress
- OpenLat: open science initiative. Gauges with SWF open to the whole community
- Results for parton distribution functions are very encouraging

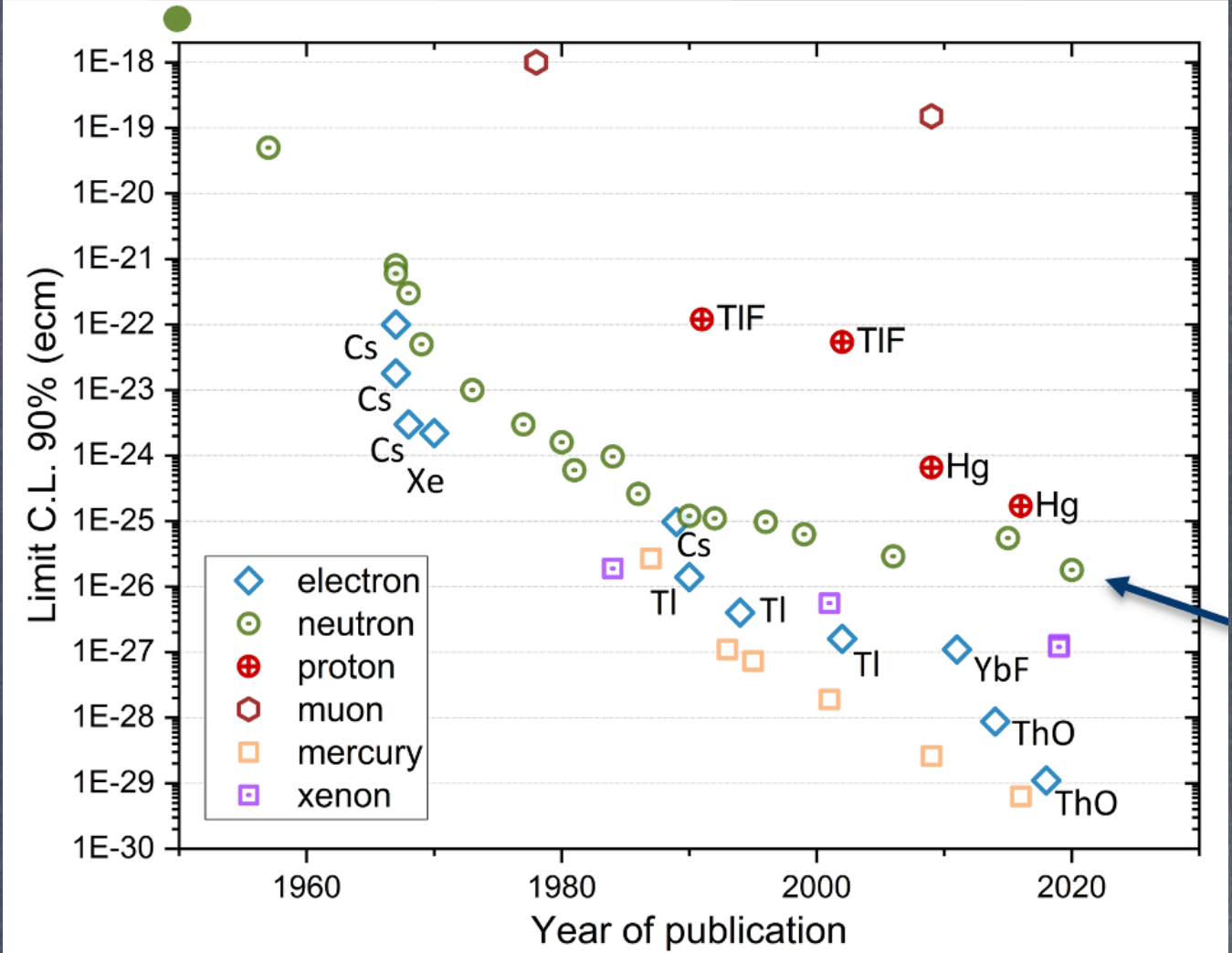
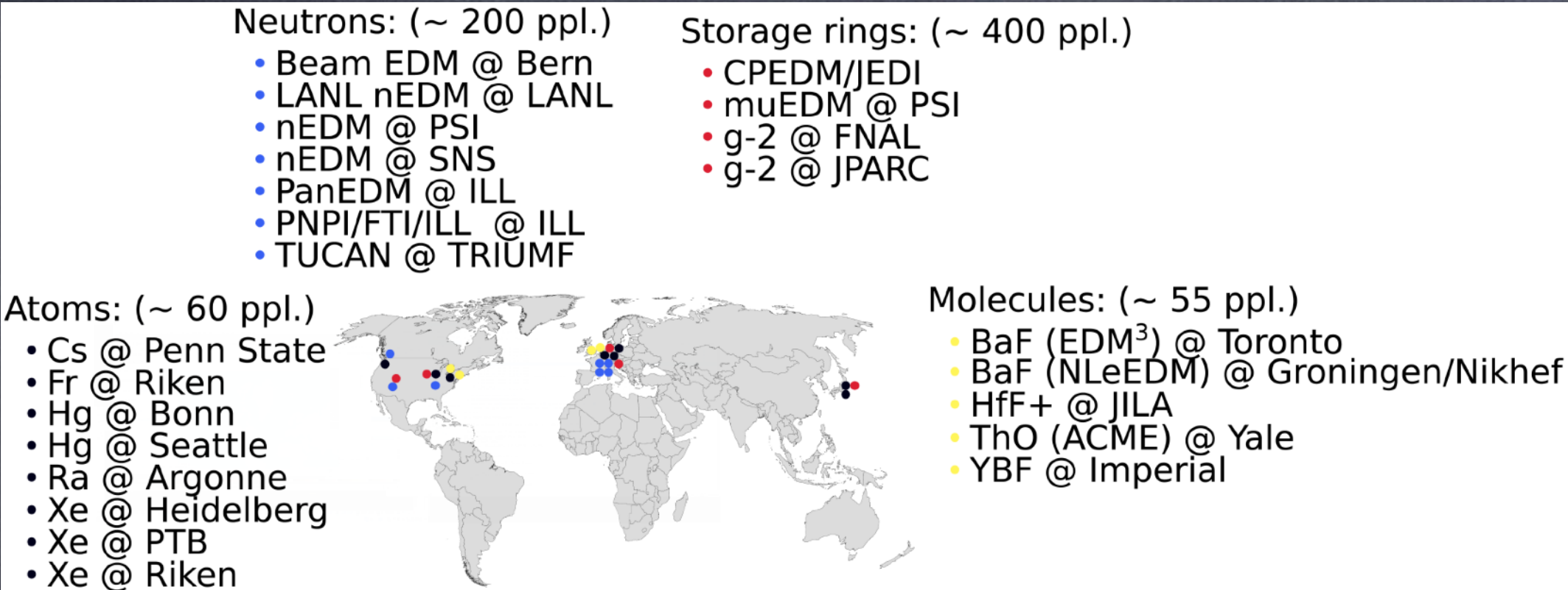
Thank you!



Backup Slides

EDM experiments in the world

Chupp, Fierlinger,
Ramsey-Musolf, Singh: 2019



	Result	95% u.l.
Paramagnetic systems		
Xe ^m	$d_A = (0.7 \pm 1.4) \times 10^{-22}$	$3.1 \times 10^{-22} \text{ e cm}$
Cs	$d_A = (-1.8 \pm 6.9) \times 10^{-24}$	$1.4 \times 10^{-23} \text{ e cm}$
	$d_e = (-1.5 \pm 5.7) \times 10^{-26}$	$1.2 \times 10^{-25} \text{ e cm}$
	$C_S = (2.5 \pm 9.8) \times 10^{-6}$	2×10^{-5}
	$Q_m = (3 \pm 13) \times 10^{-8}$	$2.6 \times 10^{-7} \mu_N R_{Cs}$
Tl	$d_A = (-4.0 \pm 4.3) \times 10^{-25}$	$1.1 \times 10^{-24} \text{ e cm}$
	$d_e = (-6.9 \pm 7.4) \times 10^{-28}$	$1.9 \times 10^{-27} \text{ e cm}$
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ThO	$d_e = (-2.1 \pm 4.5) \times 10^{-29}$	$9.7 \times 10^{-29} \text{ e cm}$
	$C_S = (-1.3 \pm 3.0) \times 10^{-9}$	6.4×10^{-9}
HfF ⁺	$d_e = (0.9 \pm 7.9) \times 10^{-29}$	$1.6 \times 10^{-28} \text{ e cm}$
Diamagnetic systems		
¹⁹⁹ Hg	$d_A = (2.2 \pm 3.1) \times 10^{-30}$	$7.4 \times 10^{-30} \text{ e cm}$
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TlF	$d = (-1.7 \pm 2.9) \times 10^{-23}$	$6.5 \times 10^{-23} \text{ e cm}$
n	$d_n = (-0.21 \pm 1.82) \times 10^{-26}$	$3.6 \times 10^{-26} \text{ e cm}$
Particle systems		
μ	$d_\mu = (0.0 \pm 0.9) \times 10^{-19}$	$1.8 \times 10^{-19} \text{ e cm}$
τ	$Re(d_\tau) = (1.15 \pm 1.70) \times 10^{-17}$	$3.9 \times 10^{-17} \text{ e cm}$
Λ	$d_\Lambda = (-3.0 \pm 7.4) \times 10^{-17}$	$1.6 \times 10^{-16} \text{ e cm}$

$|d_n| < 1.8 \times 10^{-26} \text{ e cm (90% C.L.)}$

Abel et al.: 2020
PSI

$|d_{^{199}\text{Hg}}| < 7.4 \times 10^{-30} \text{ e cm (95% C.L.)}$

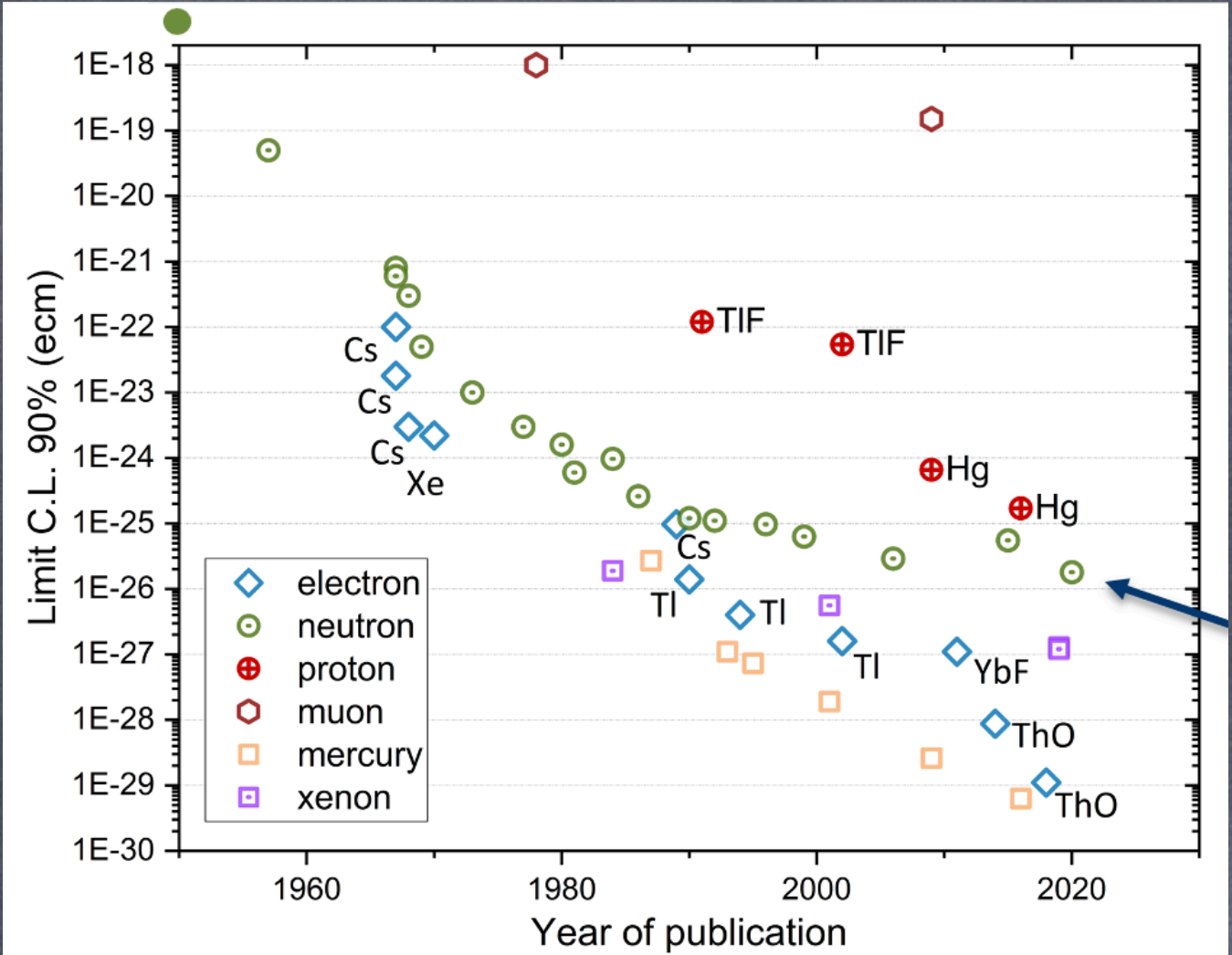
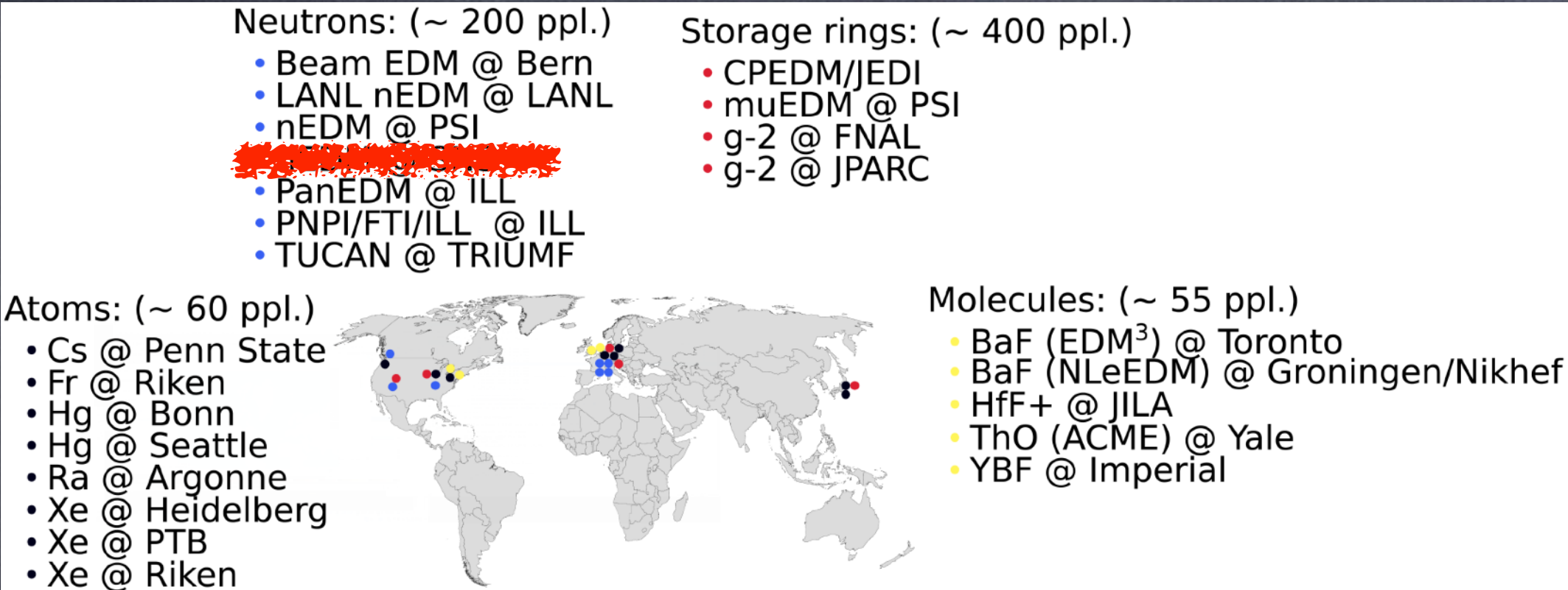
Griffith et al.: 2009
Graner et al.: 2017

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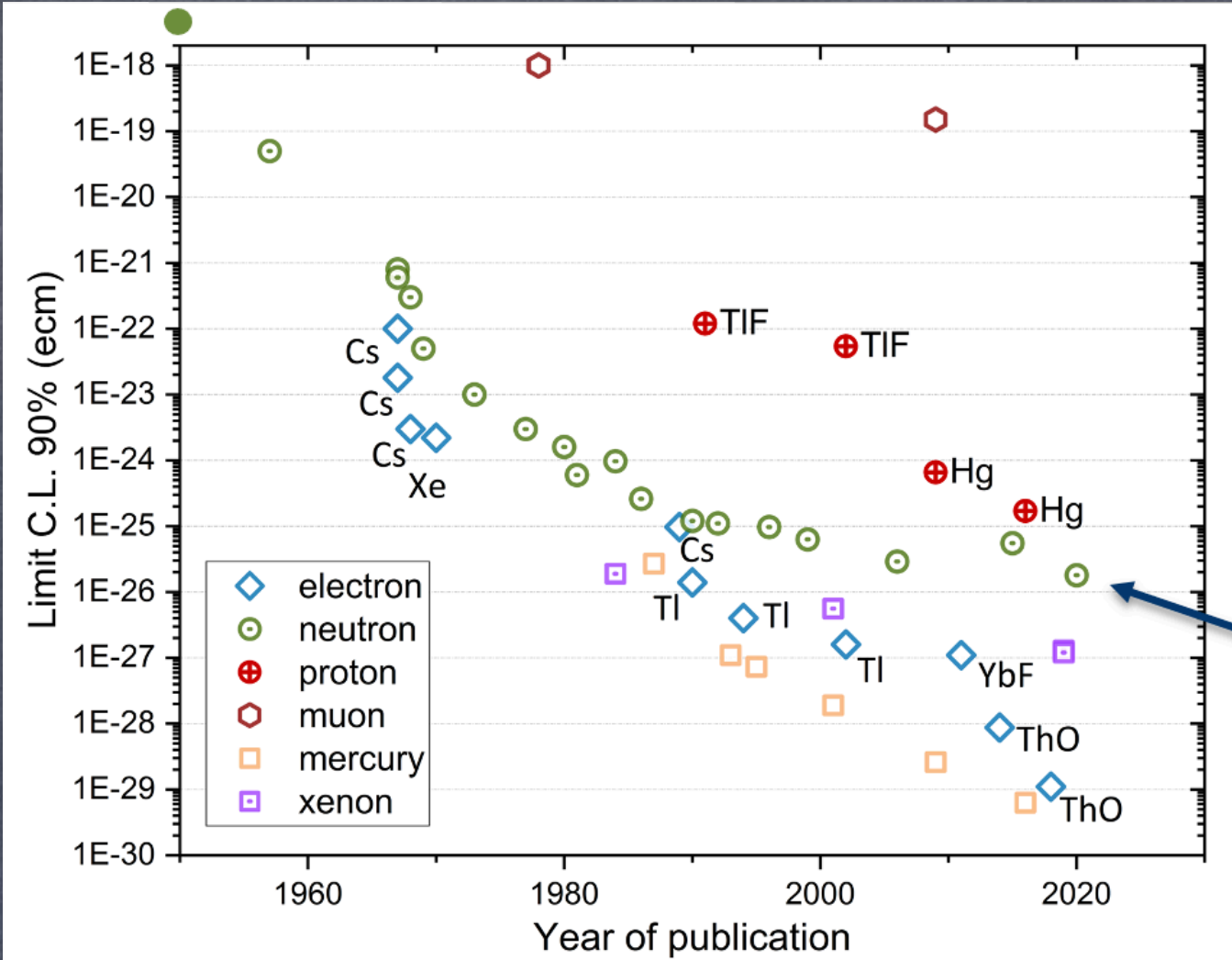
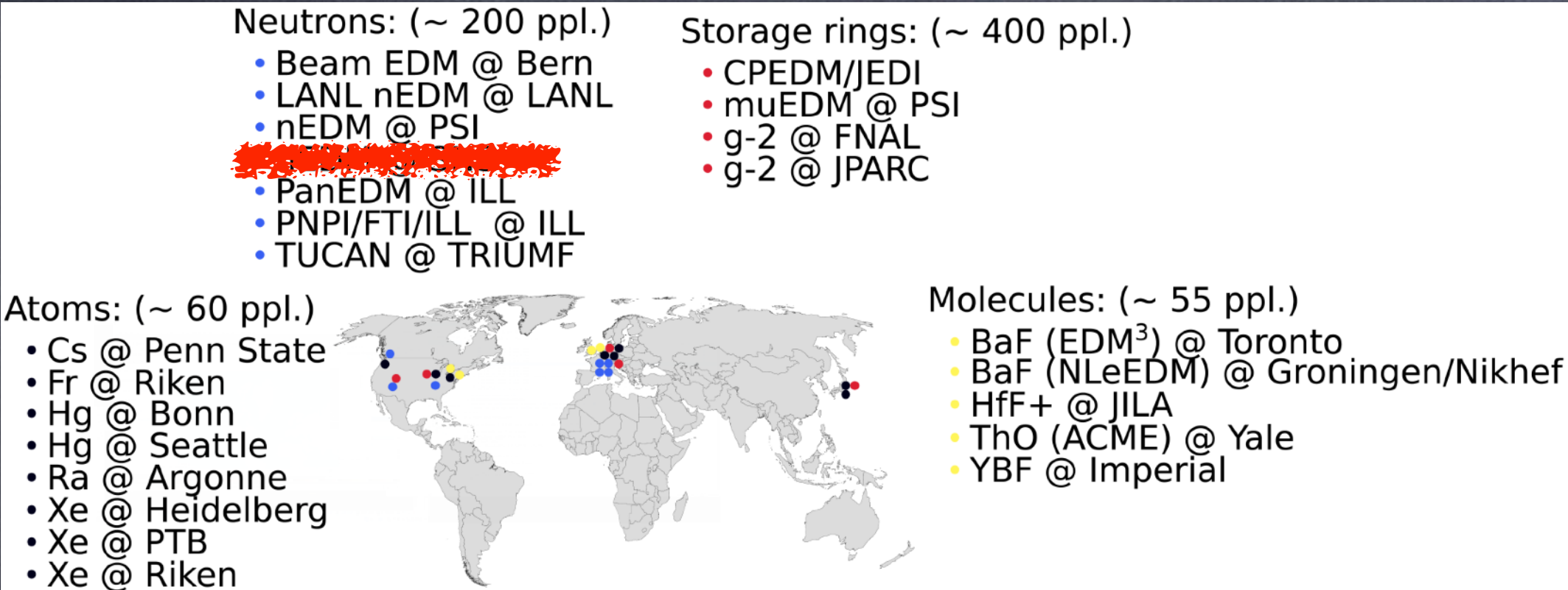
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Abel et al.: 2020
PSI

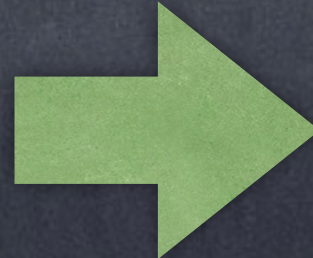
5 (10) yrs

$|d_n| \lesssim 3 \times 10^{-27} \text{ e cm}$

PSI, LANL,...

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Griffith et al.: 2009
Graner et al.: 2017



$|d_{199Hg}| \lesssim 5 \times 10^{-31} \text{ e cm (} 5 \times 10^{-32} \text{ e cm)}$ Bonn

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Bishof et al: 2016

$|d_{225Ra}| \lesssim 3 \times 10^{-27} \text{ e cm}$ ANL

New physics scale

$$d_f \sim eq_f \sin(\delta_{\text{CPV}}) \left(\frac{g^2}{16\pi^2} \right)^l \xi_{\text{FV}} \frac{m_f}{M_{\text{NP}}^2} \quad d_e \leq d_e^{\text{max}}$$

$$M_{\text{NP}} \gtrsim \sqrt{\frac{10^{29} e \text{ cm}}{d_e^{\text{max}}}} \times \begin{cases} 50 \text{ TeV}, & \text{if } l = 1 \\ 2 \text{ TeV}, & \text{if } l = 2 \end{cases}$$

- The discovery potential in EDM searches can be roughly quantified by the reach in mass scale, assuming maximal CP violation.
- In all cases we see that the mass reach is very high – EDMs are exploring uncharted territory.
- if we insist that the scale of new physics is close to the electroweak scale, EDMs probe very small CP-violating couplings, still providing invaluable information for model building and understanding the nature of CP symmetry and its breaking.

Operator	Loop order	Mass reach
Electron EDM	1	$48 \text{ TeV} \sqrt{10^{-29} e \text{ cm} / d_e^{\text{max}}}$
	2	$2 \text{ TeV} \sqrt{10^{-29} e \text{ cm} / d_e^{\text{max}}}$
Up/down quark EDM	1	$130 \text{ TeV} \sqrt{10^{-29} e \text{ cm} / d_q^{\text{max}}}$
	2	$13 \text{ TeV} \sqrt{10^{-29} e \text{ cm} / d_q^{\text{max}}}$
Up-quark CEDM	1	$210 \text{ TeV} \sqrt{10^{-29} \text{ cm} / \tilde{d}_u^{\text{max}}}$
	2	$20 \text{ TeV} \sqrt{10^{-29} \text{ cm} / \tilde{d}_u^{\text{max}}}$
Down-quark CEDM	1	$290 \text{ TeV} \sqrt{10^{-29} \text{ cm} / \tilde{d}_d^{\text{max}}}$
	2	$28 \text{ TeV} \sqrt{10^{-29} \text{ cm} / \tilde{d}_d^{\text{max}}}$
Gluon CEDM	2 ($\propto m_t$)	$22 \text{ TeV} \sqrt[3]{10^{-29} \text{ cm} / (100 \text{ MeV}) / \tilde{d}_G^{\text{max}}}$
	2	$260 \text{ TeV} \sqrt{10^{-29} \text{ cm} / (100 \text{ MeV}) / \tilde{d}_G^{\text{max}}}$

Alarcon et al.: 2022
Snowmass Summer Study Report

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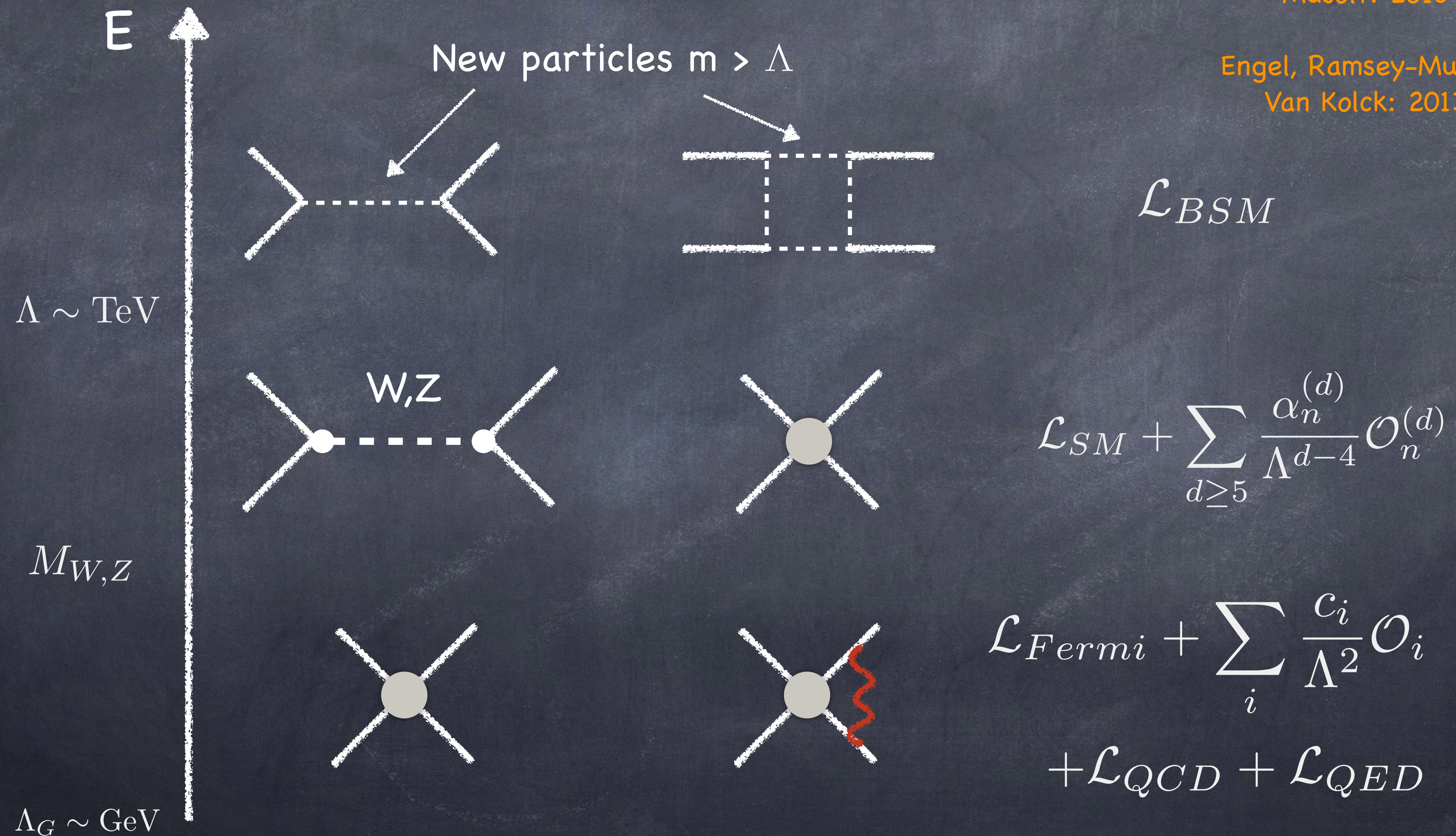
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Alarcon et al.: 2022
Snowmass Summer Study Report

CP-violating effective operators

Cirigliano, Ramsey-Musolf: 2013

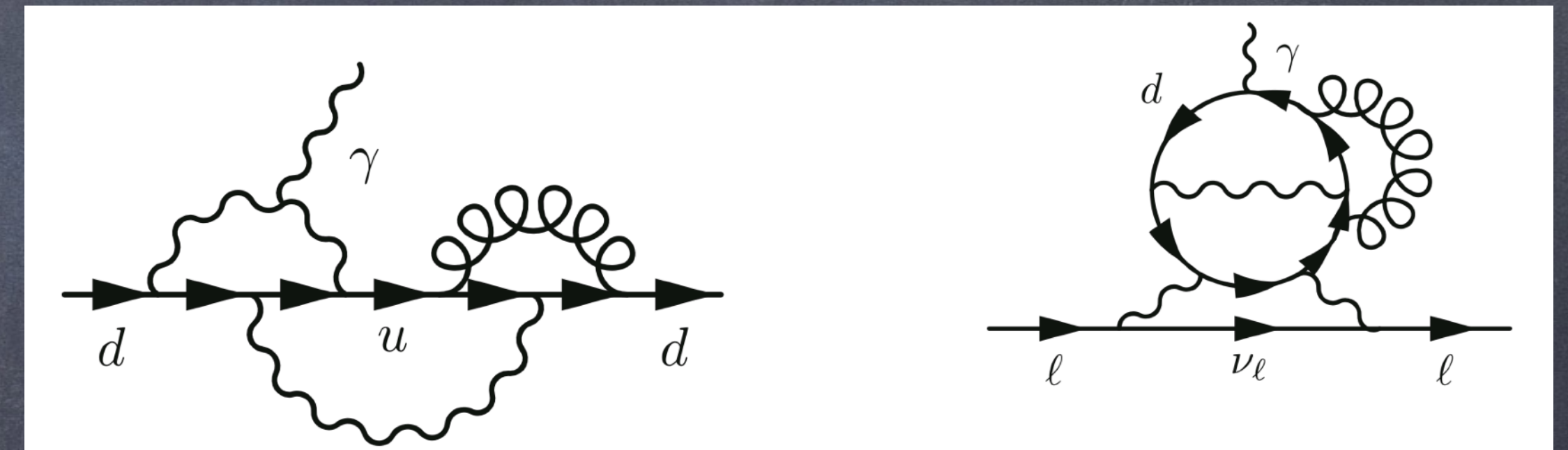
Engel, Ramsey-Musolf, Van Kolck: 2013



EDM from the Standard Model

- No EDMs at 1-loop
- At 2-loops individual diagrams are non-zero, but the sum vanishes
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Electron EDM can be larger due to hadronic loops
EDM of not elementary particles can be larger

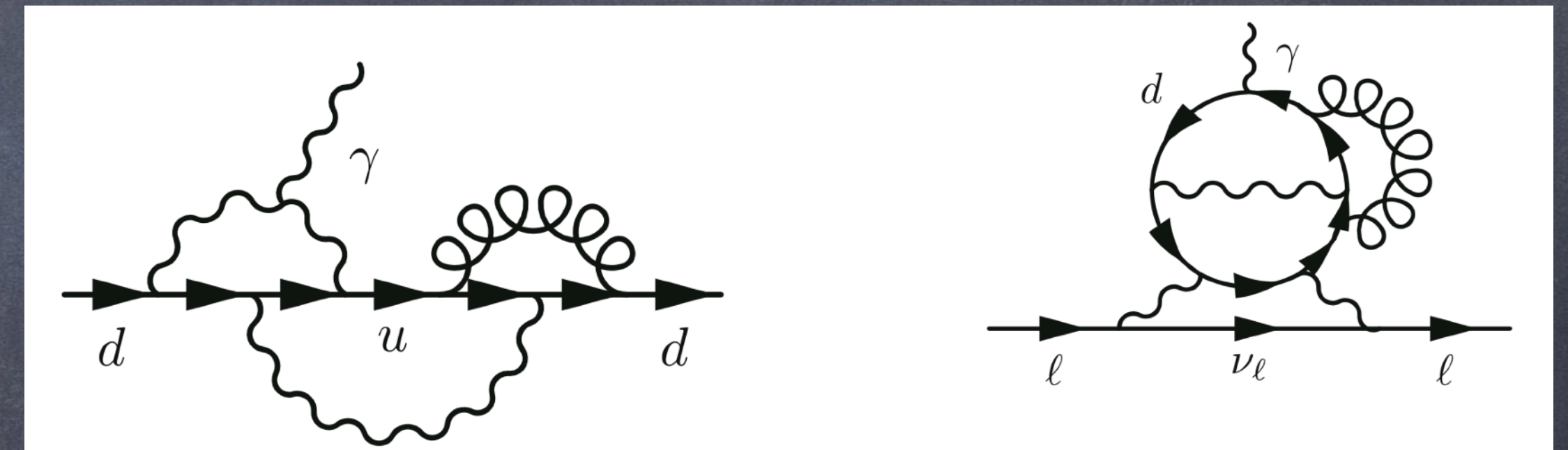


EDM from the Standard Model

Shabalin: 1978–1980 Khriplovich, Zhitnitsky: 1982
Gavela et al. : 1982

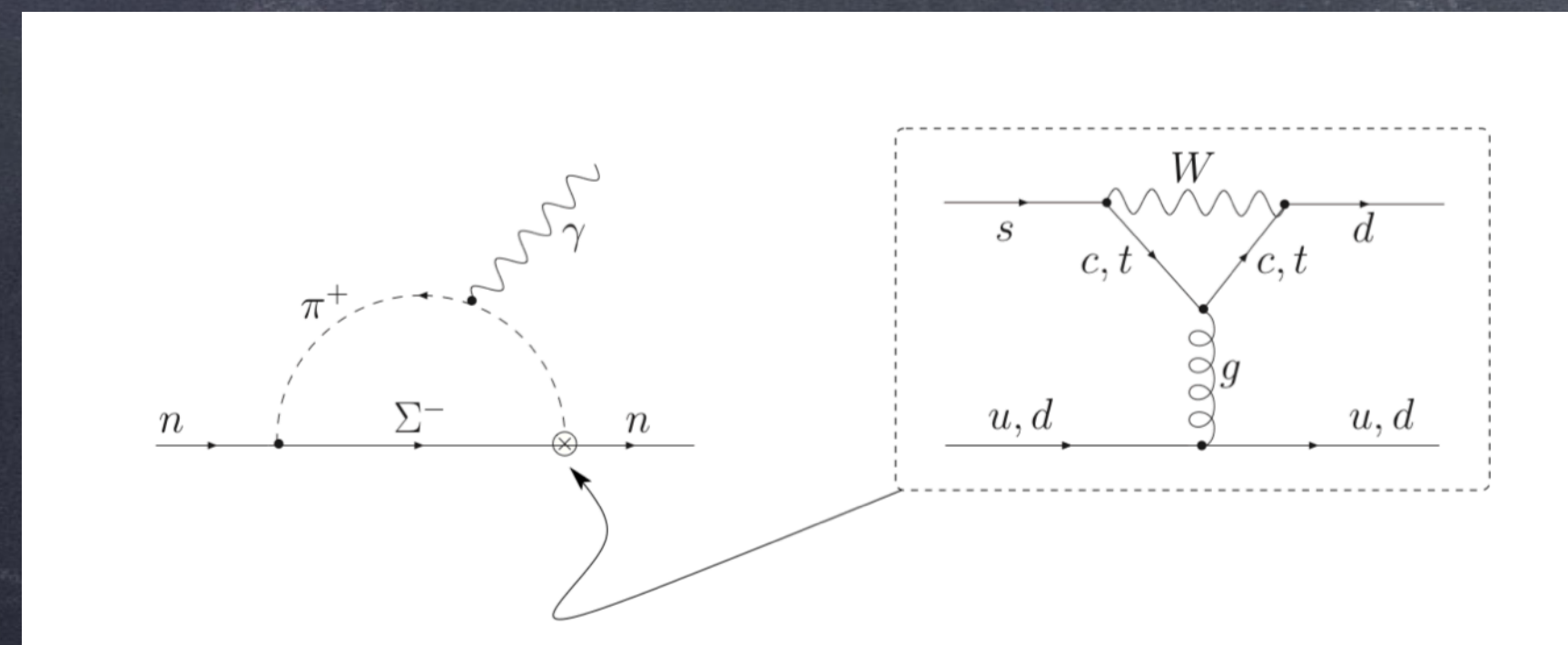
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$$(d_n)_{\text{SM}} = (1-6) \times 10^{-32} e \text{ cm}$$

Seng: 2015

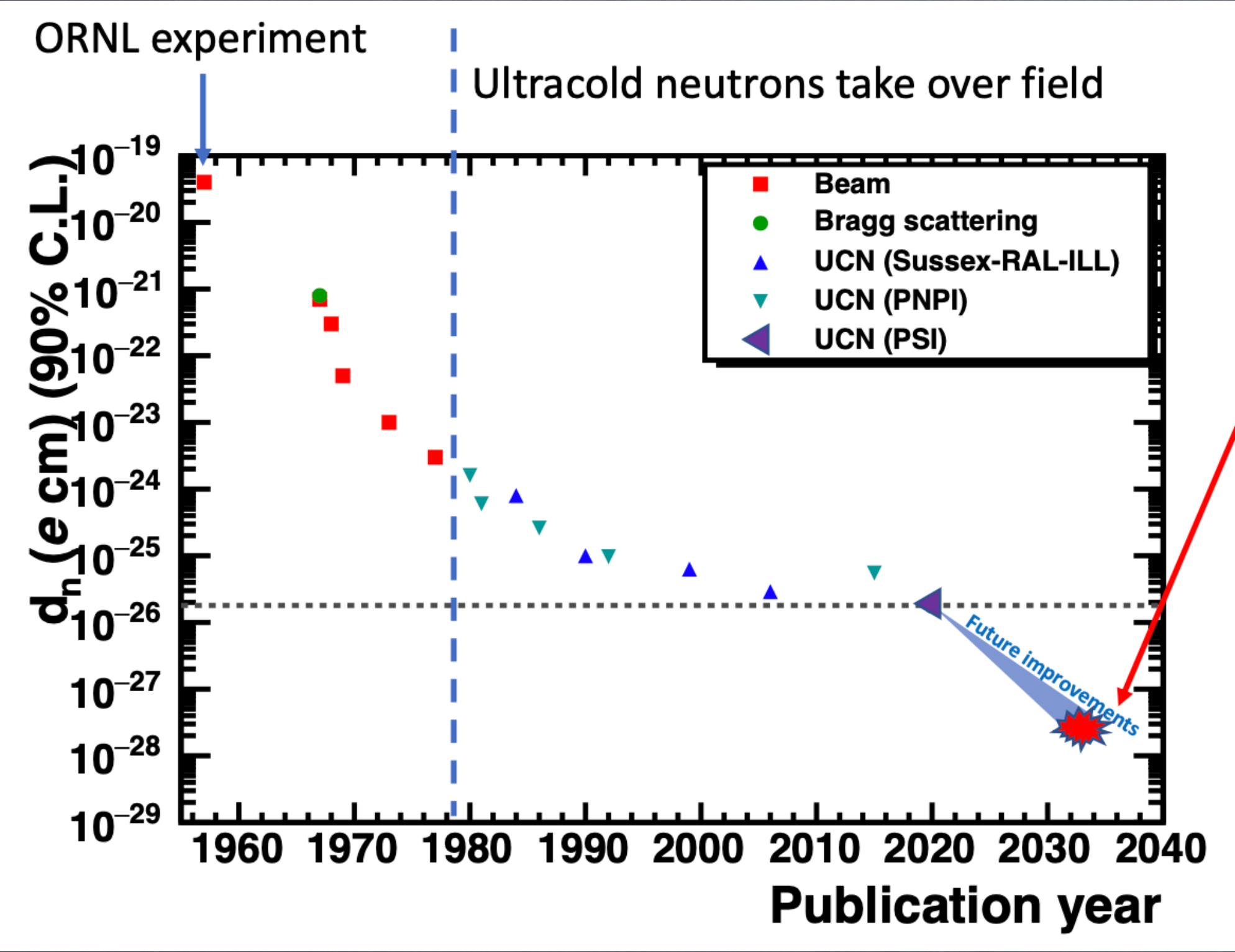


Neutron EDM

$|d_n| < 1.8 \times 10^{-26} \text{ e cm (90\% C.L.)}$

Abel et al.: 2020 (PSI)

Alarcon et al.: 2022
Snowmass Summer Study Report



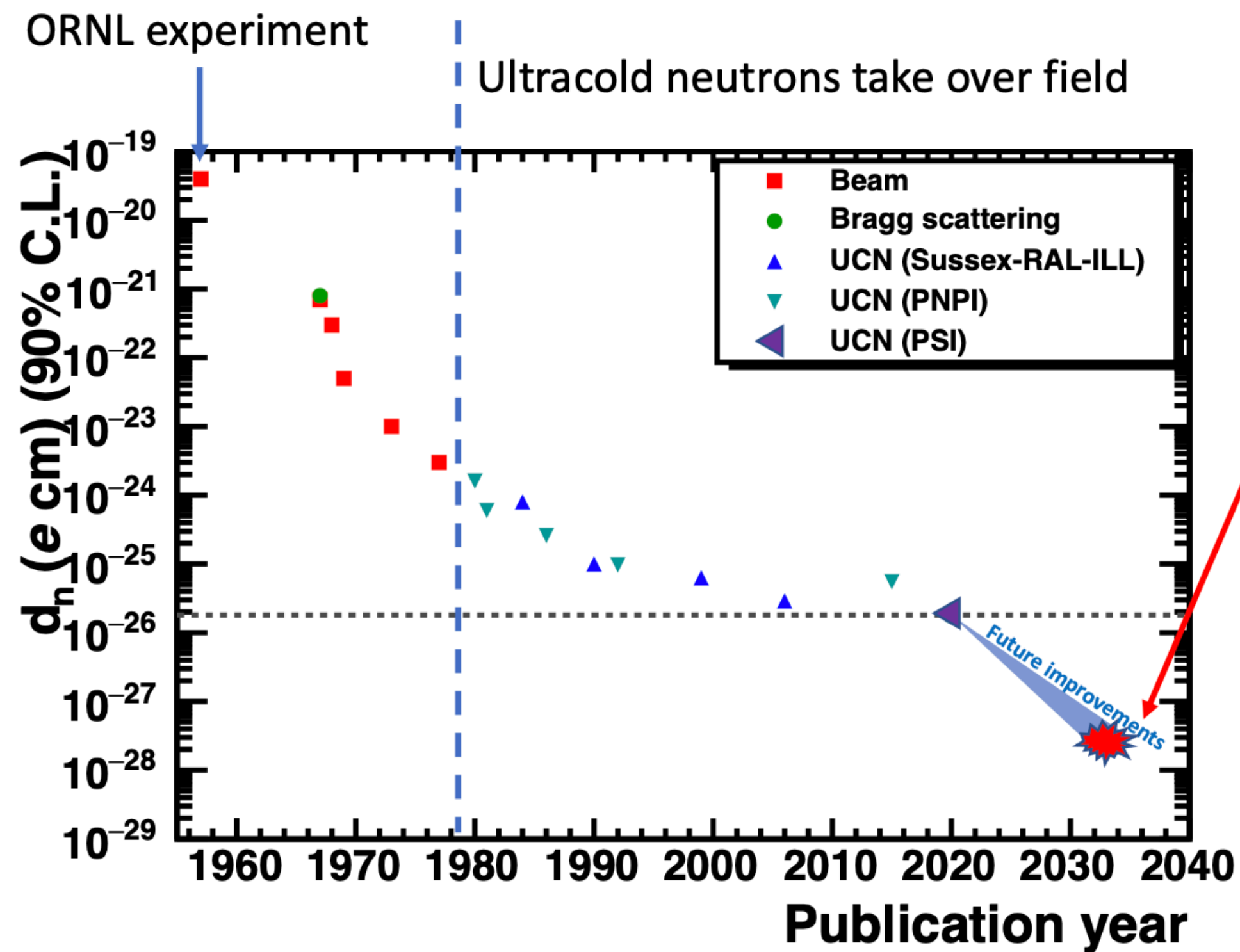
Experiment: Facility	Neutron Source	Measurement Cell	Measurement Techniques	90% C.L. (10^{-28} e-cm) With 300 Live Days	Year 90% C.L. Data Acquired
Crystal: JPARC	Cold Neutron Beam	Solid	Crystal Diffraction (High Internal $\vec{E}$)	< 100	Development
Beam: ESS	Cold Neutron Beam	Vacuum	Pulsed Beam	< 50	~ 2030
PNPI: ILL	ILL Turbine (UCN) PNPI/LHe (UCN)	Vacuum	Ramsey Technique, $\vec{E} = 0$ Cell for Magnetometry	Phase 1 < 100 < 10	Development Development
n2EDM: PSI	Solid D ₂ (UCN)	Vacuum	Ramsey Technique, External Cs Magnetometers, Hg Co-Magnetometer	< 15	~ 2026
PanEDM ILL/Munich	Superfluid ⁴ He (UCN), Solid D ₂ (UCN)	Vacuum	Ramsey Technique, Hg Co- External ³ He and Cs Magnetometers	< 30	~ 2026
TUCAN: TRIUMF	Superfluid ⁴ He (UCN)	Vacuum	Ramsey Technique, Hg Co- Magnetometer, External Cs Magnetometers	< 20	~ 2027
nEDM: LANL	Solid D ₂ (UCN)	Vacuum	Ramsey Technique, Hg Co- Magnetometer, Hg External Magnetometer, OPM	< 30	~ 2026
nEDM@SNS: ORNL	Superfluid ⁴ He (UCN)	⁴ He	Cryogenic High Voltage, ³ He Capture for ω , ³ He Co-Magnetometer with SQUIDs, Dressed Spins, Superconducting Magnetic Shield	< 20 < 3	~ 2029 ~ 2031

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nEDM@SNS: ORNL	Superfluid ⁴ He (UCN)	⁴ He	Cryogenic High Voltage, ³ He Capture for ω , ³ He Co-Magnetometer	< 20 < 3	~ 2029 ~ 2031
			With 100 Ls, D ₂ Gas, Spins, $\vec{E}$ Superconducting Magnetic Shield		

Quark–Chromo EDM: power divergences

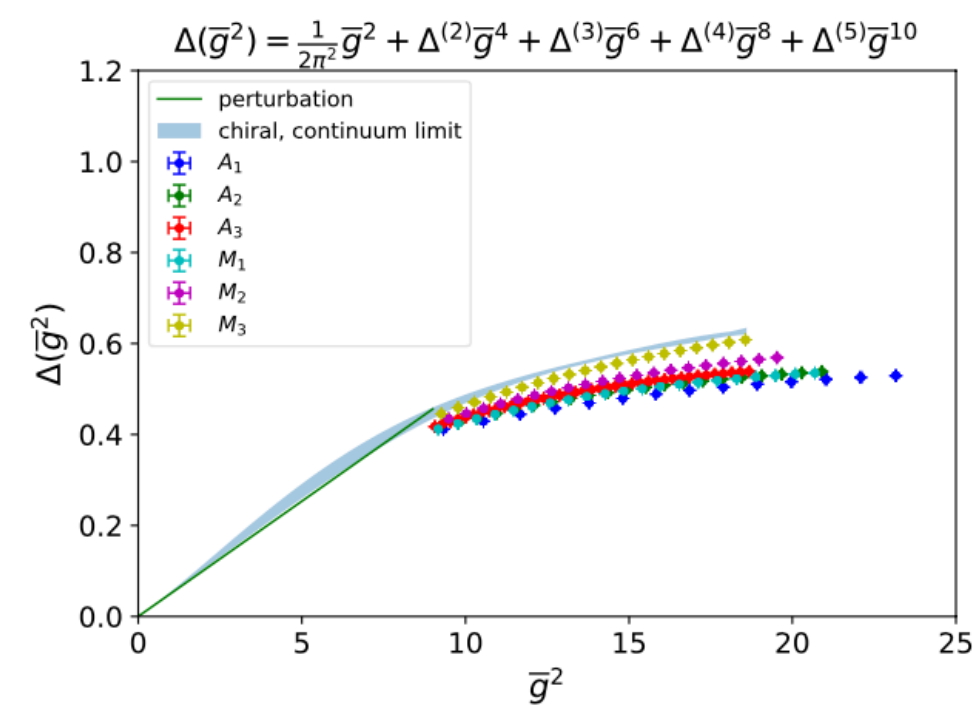
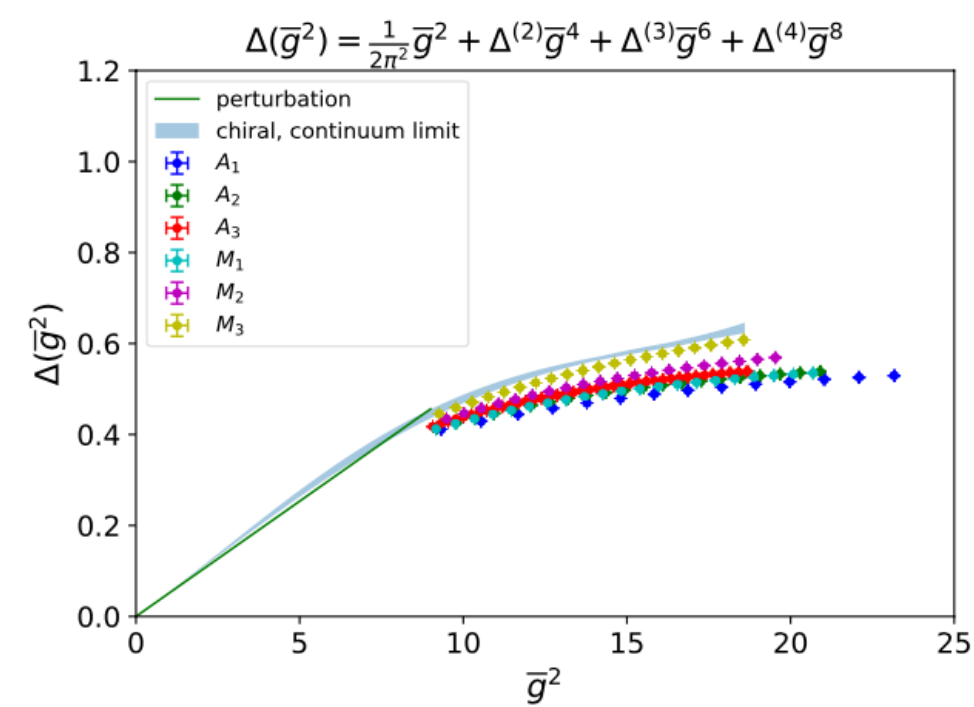
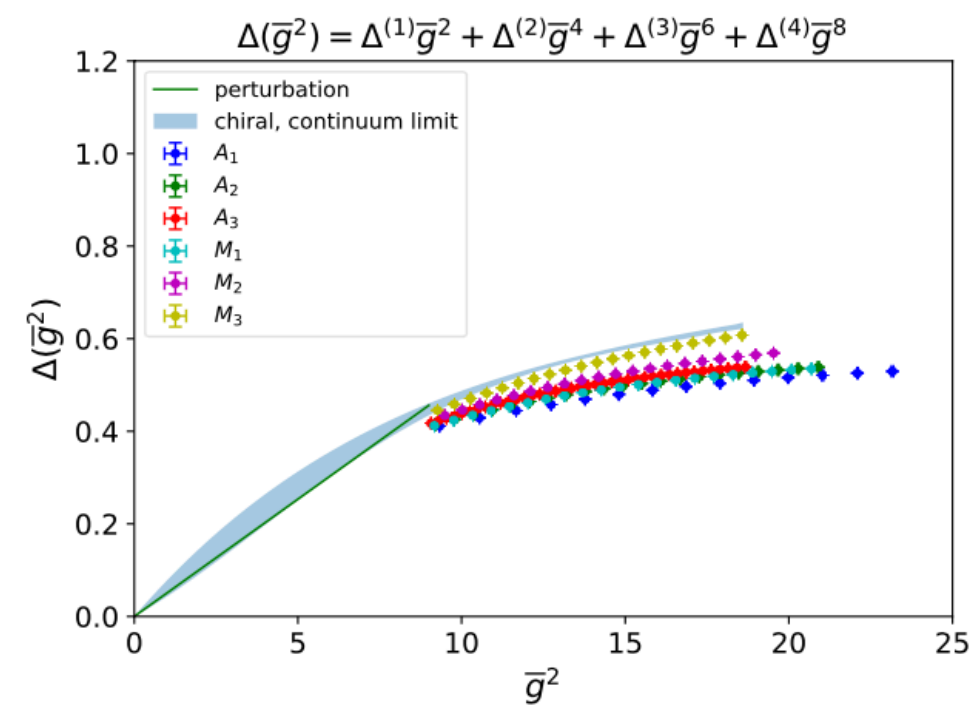
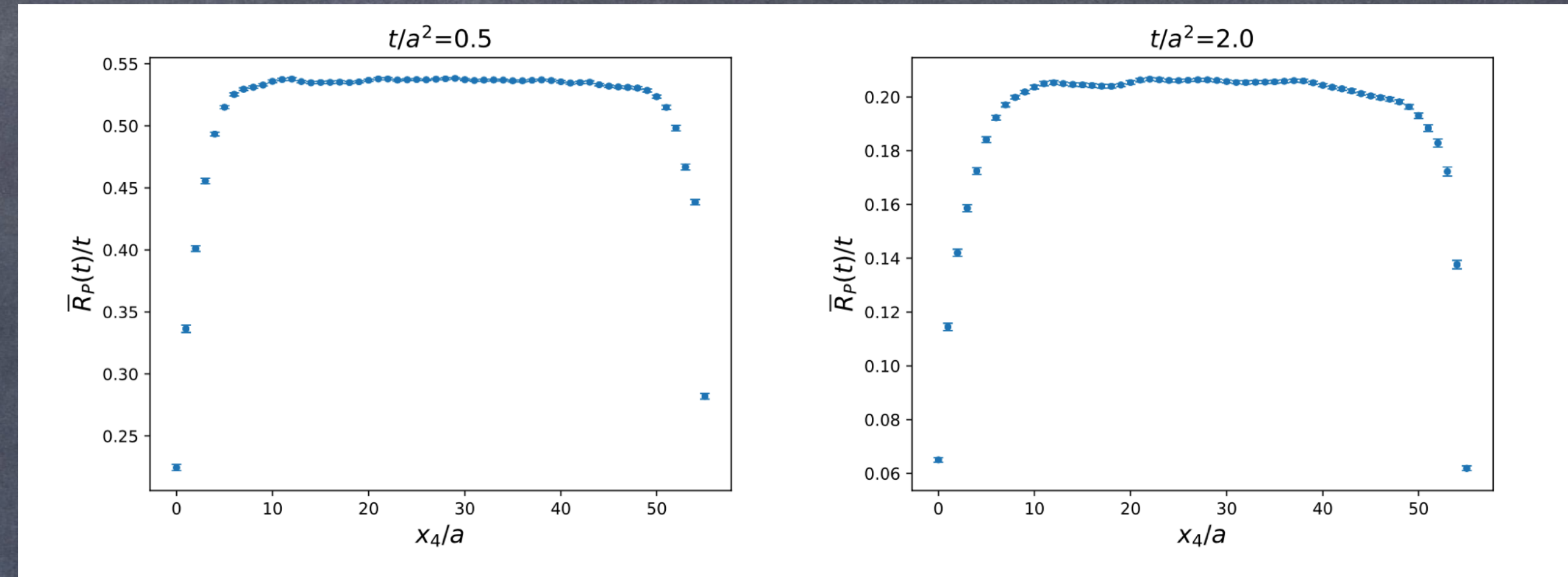
Kim, Luu, Rizik, A.S.:2020

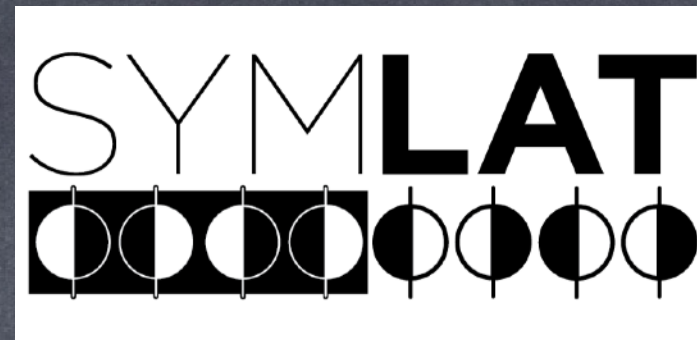
$$\mathcal{O}_{\text{CE,R}}(t) = \frac{c_{\text{OP}}(t, \mu)}{t} P_{\text{R}}(0, \mu) + \sum_i c_{\text{CE},i}(t, \mu) \mathcal{O}_{i,\text{R}}(0, \mu)$$

$$\Gamma_{CP}(x_4; t) = a^3 \sum_{\mathbf{x}} \langle \mathcal{O}_{CE}^{ij}(x_4, \mathbf{x}; t) P^{ji}(0, \mathbf{0}; 0) \rangle$$

$$\Gamma_{PP}(x_4; t) = a^3 \sum_{\mathbf{x}} \langle P^{ij}(x_4, \mathbf{x}; t) P^{ji}(0, \mathbf{0}) \rangle$$

$$\bar{R}_P(x_4; t) = t \frac{\Gamma_{CP}(x_4; t)}{\Gamma_{PP}(x_4, t)}$$





Status

- Theta-term nucleon EDM → first results

1409.2735

1507.02343

- Renormalization, S/N

1809.03487

1902.03254

- Quark-chromo EDM → renormalization

- Power divergences → PT

1810.05637

2005.04199

2111.1149

Non-perturbative

1810.10301

2106.07633

- Logs/mixing →

2111.1149

2212.09824

- 3 gluon operator → PT power divergences

2005.04199

Preliminary studies for renormalization (power divergences)

1711.04730

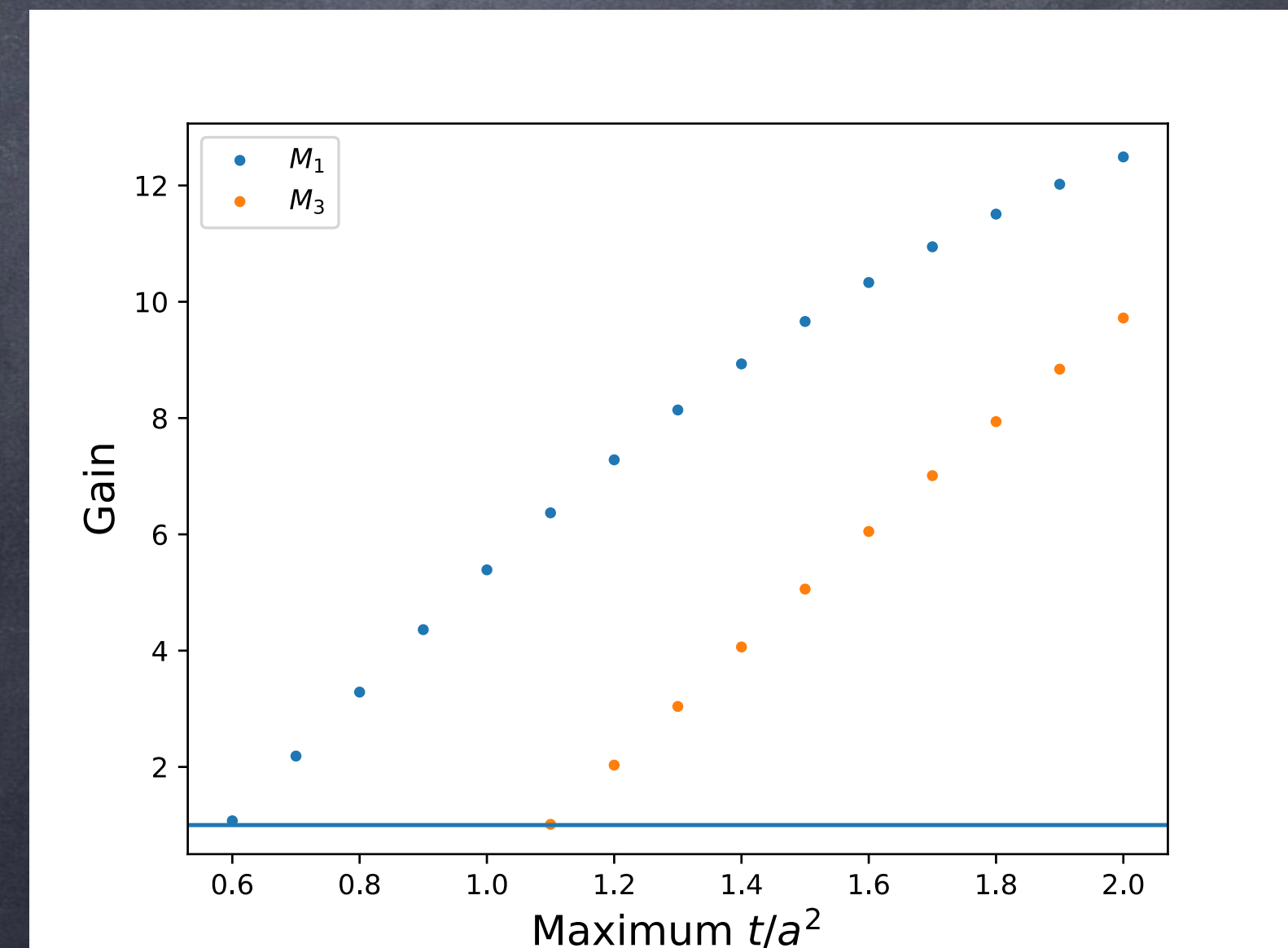
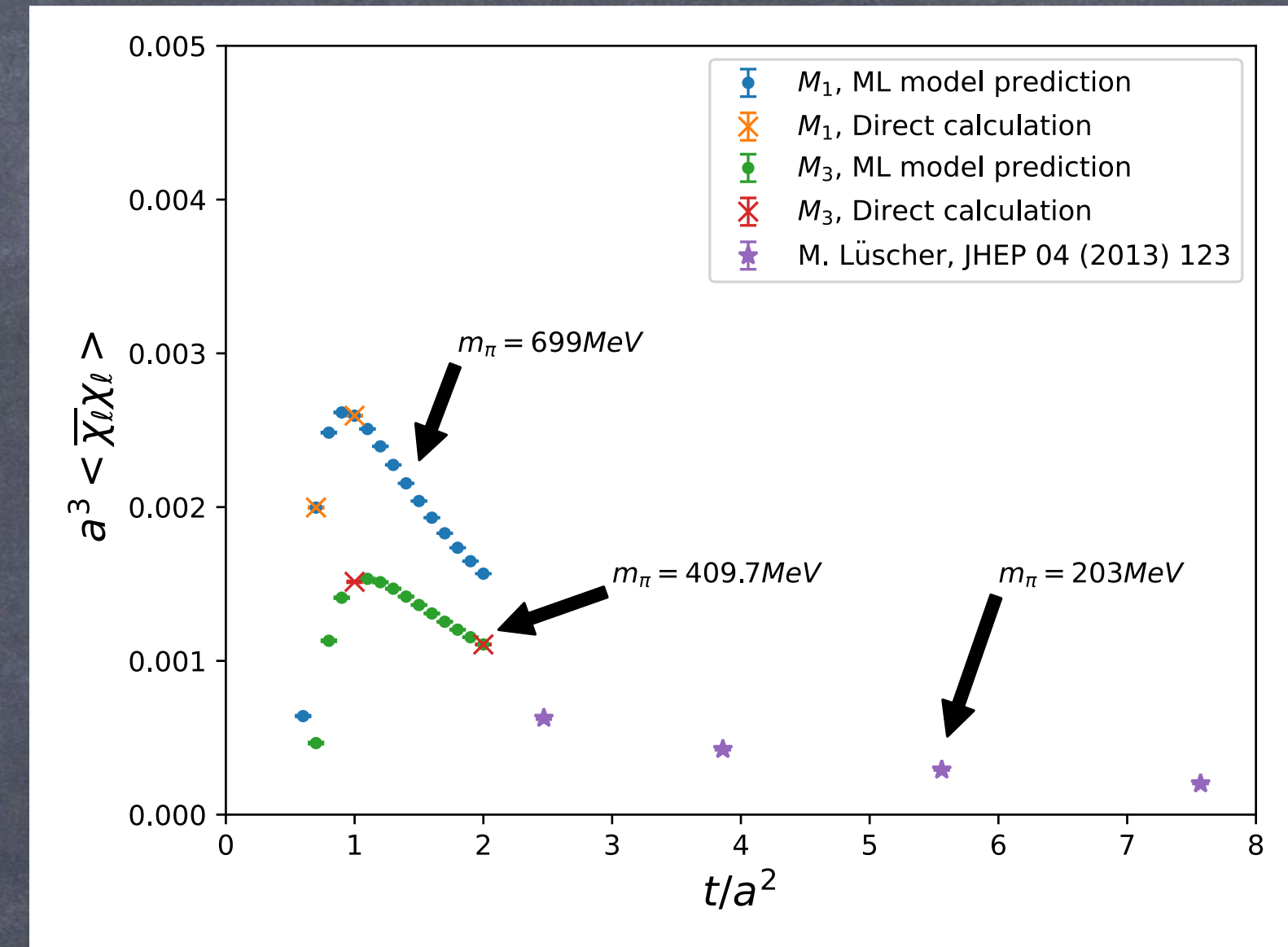
1810.05637

→ Logs/mixing 2308.16221

Scalar condensate

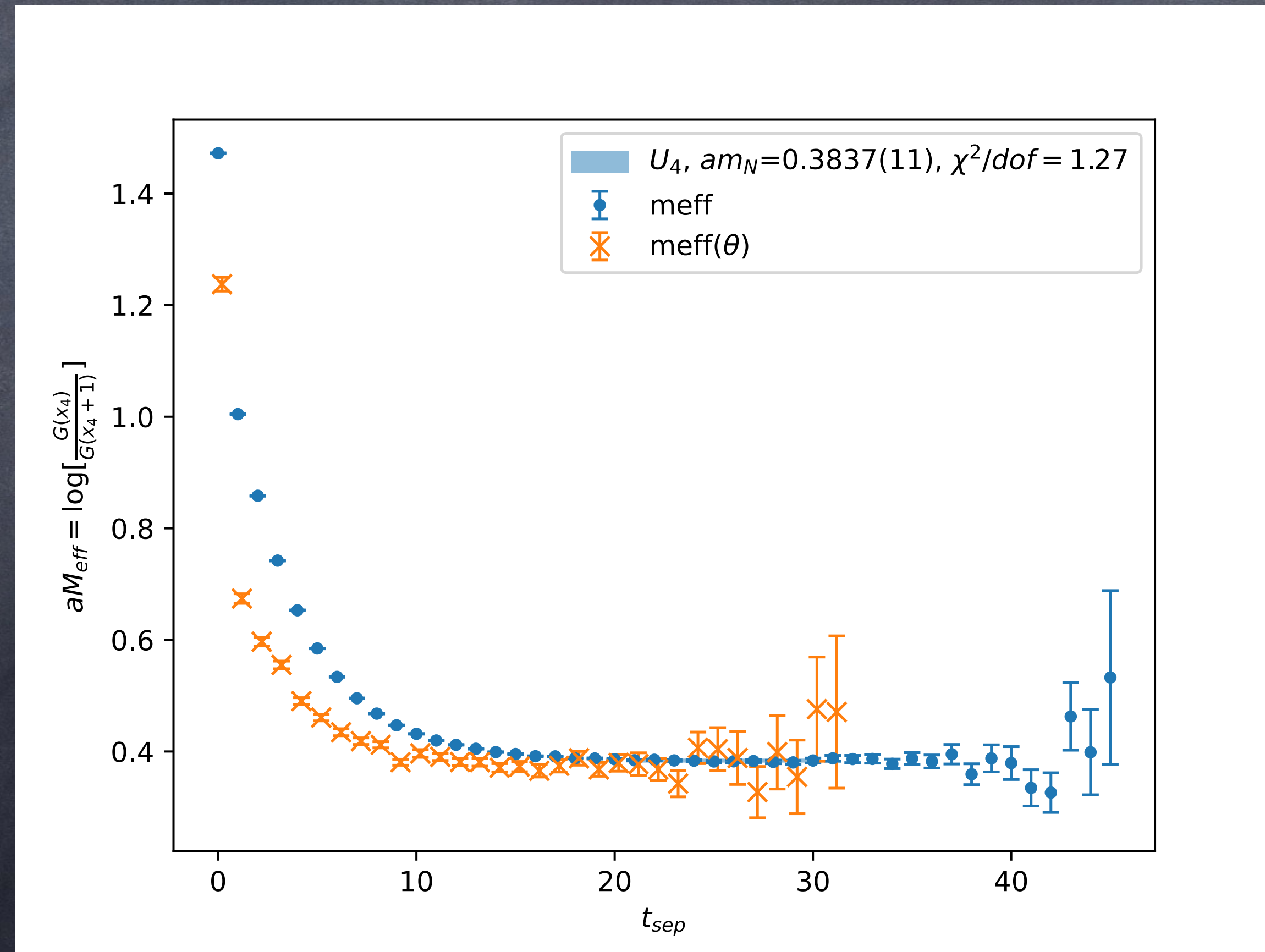
Kim, Pederiva, A.S.: 2024

- Strong correlation between quark disconnected diagrams at different flow times
- Use of translation invariance beneficial
- Decision Tree algorithms reproduces correct distribution
- Results are compatible well below the statistical fluctuations of the lattice QCD direct calculation
- No need to large ensemble for training making use of time translation invariance



Theta-term dependence

$$\mathrm{tr} [P_+ G_{NN}] = 2|Z_N|^2 e^{-M_N x_0} + \dots \qquad \mathrm{tr} [P_+ \gamma_5 G_{NN}^Q] = 2|Z_N|^2 \alpha_N e^{-M_N x_0} + \dots$$



Scale dependence matching coefficients

$$\bar{\mu}_0 = 3 \text{ GeV} \rightarrow \mu_0 = 1.13 \text{ GeV}$$

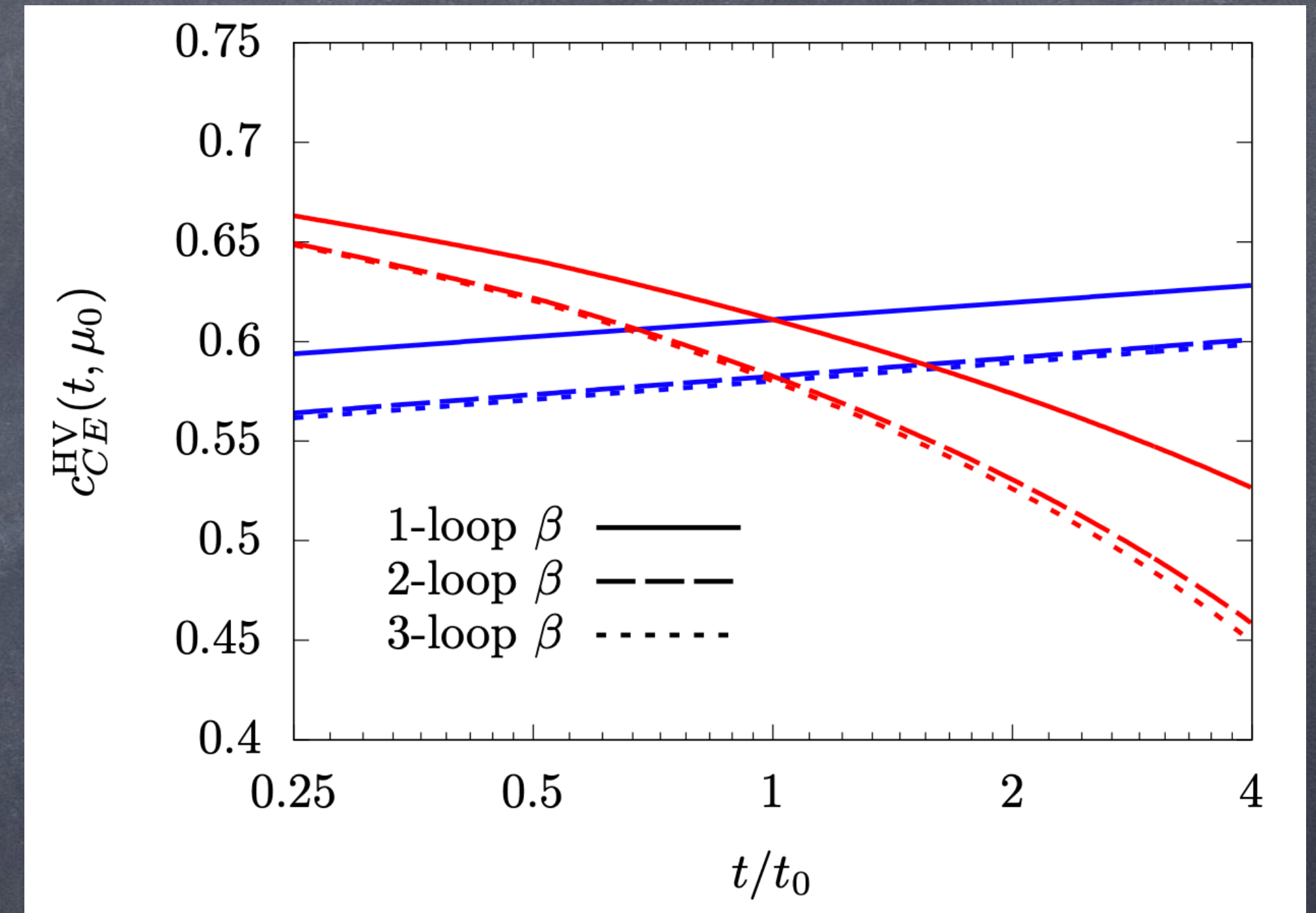
$$t_0 = \frac{1}{8\pi\mu_0^2}$$

Red - Blue =

$$A_1\alpha_s^2(\mu_0^2)\log^2(8\pi t\mu_0^2) + A_2\alpha_s^2(\mu_0^2)\log(8\pi t\mu_0^2) + O(\alpha_s^3)$$

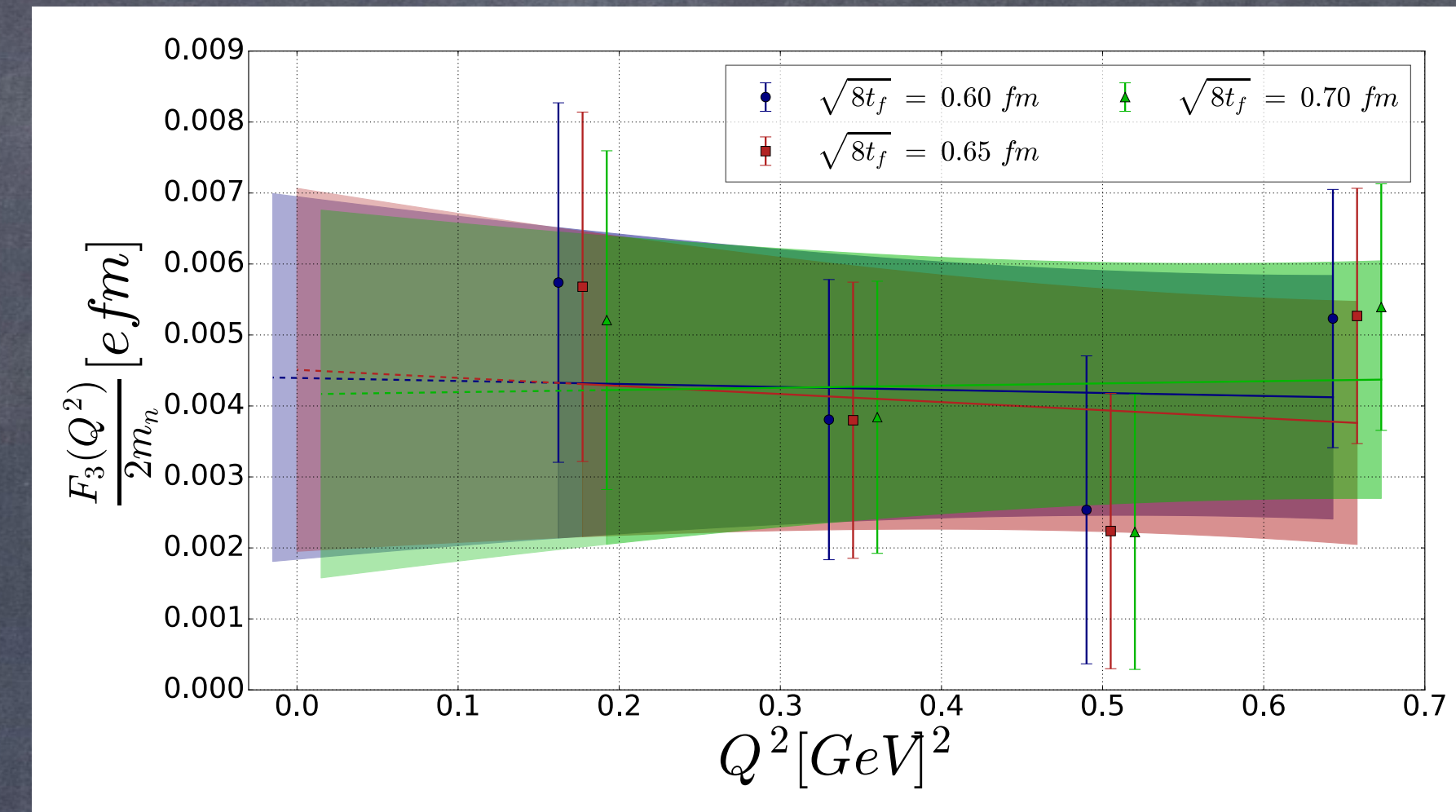
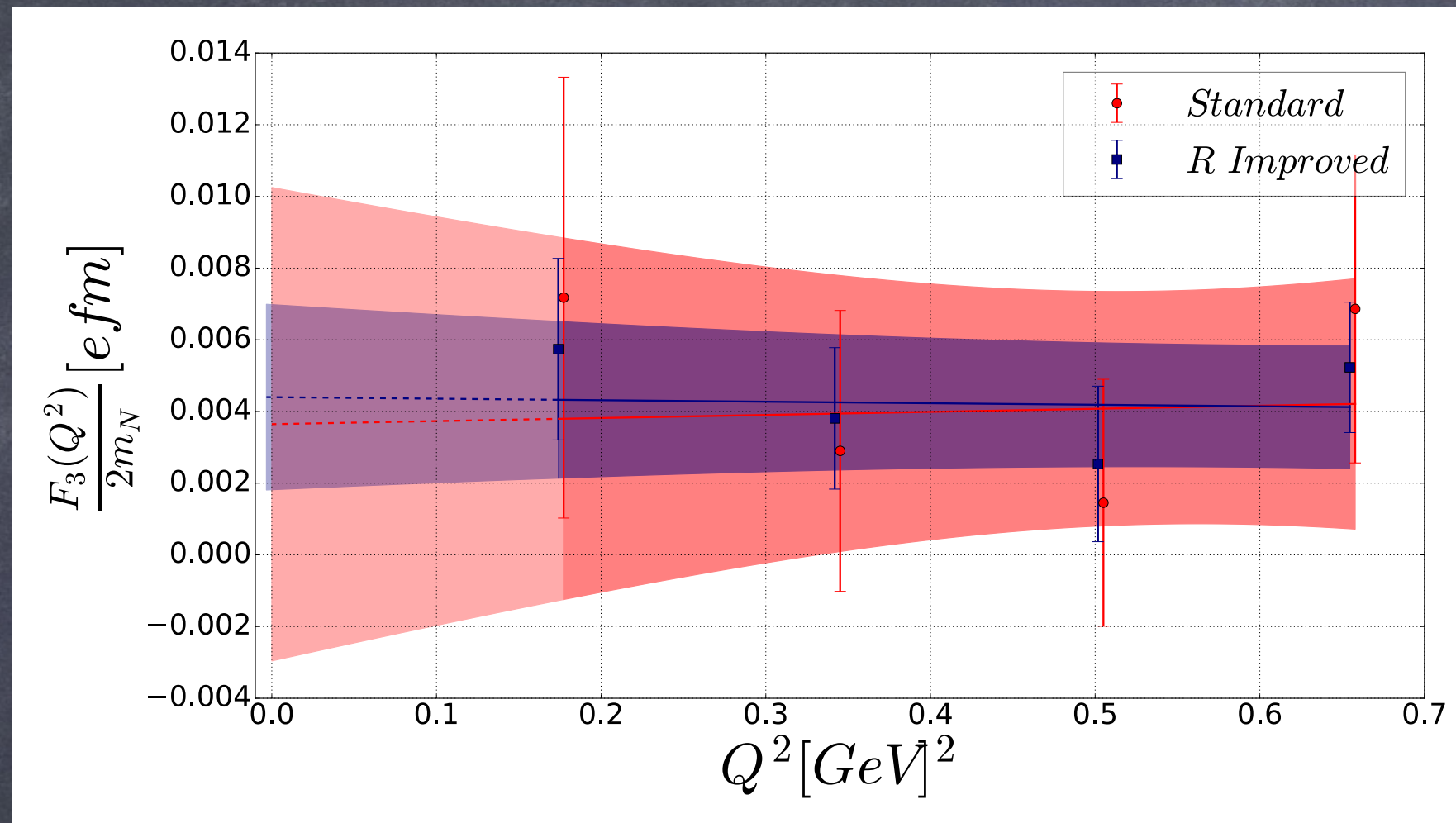
$$t \in [t_0/4, 4t_0]$$

10%-20% uncertainties from PT at 1-loop



CP-odd form factor

Dragos, Luu, A.S.,
de Vries, Yousif:
2019



$$\frac{F_3^{P/N}(Q^2)}{2M_N} = d_{P/N} + S_{P/N}Q^2 + H_{P/N}(Q^2)$$

$$\frac{d_P}{d_N} < 0 \quad \frac{S_P}{S_N} < 0$$

Mereghetti et al.: 2011

Topological charge on the lattice

Discretize $\longrightarrow$ $q(x) = \frac{1}{32\pi^2} \epsilon_{\mu\nu\rho\sigma} \text{tr} \{ G_{\mu\nu}(x) G_{\rho\sigma}(x) \}$

Continuity in space is lost

On the lattice it has no topological significance

Geometrical definition:

extend the lattice gauge field to a continuous one
Field between lattice points $\rightarrow$ judicious interpolation
Smooth gauge fields (bound on field tensor)

Lüscher: 1982

Phillips, Stones: 1986

Fermionic definition:

Anomalous Ward Identity

Smit: 1980

$$\partial_\mu A_\mu = 2mP + \text{extra terms}$$

$$\partial_\mu A_\mu = 2mP + 2iN_f q_L$$

$$Q_L \propto m \sum_x \text{Tr} (\gamma_5 S)$$

$$Q = n_+ - n_-$$

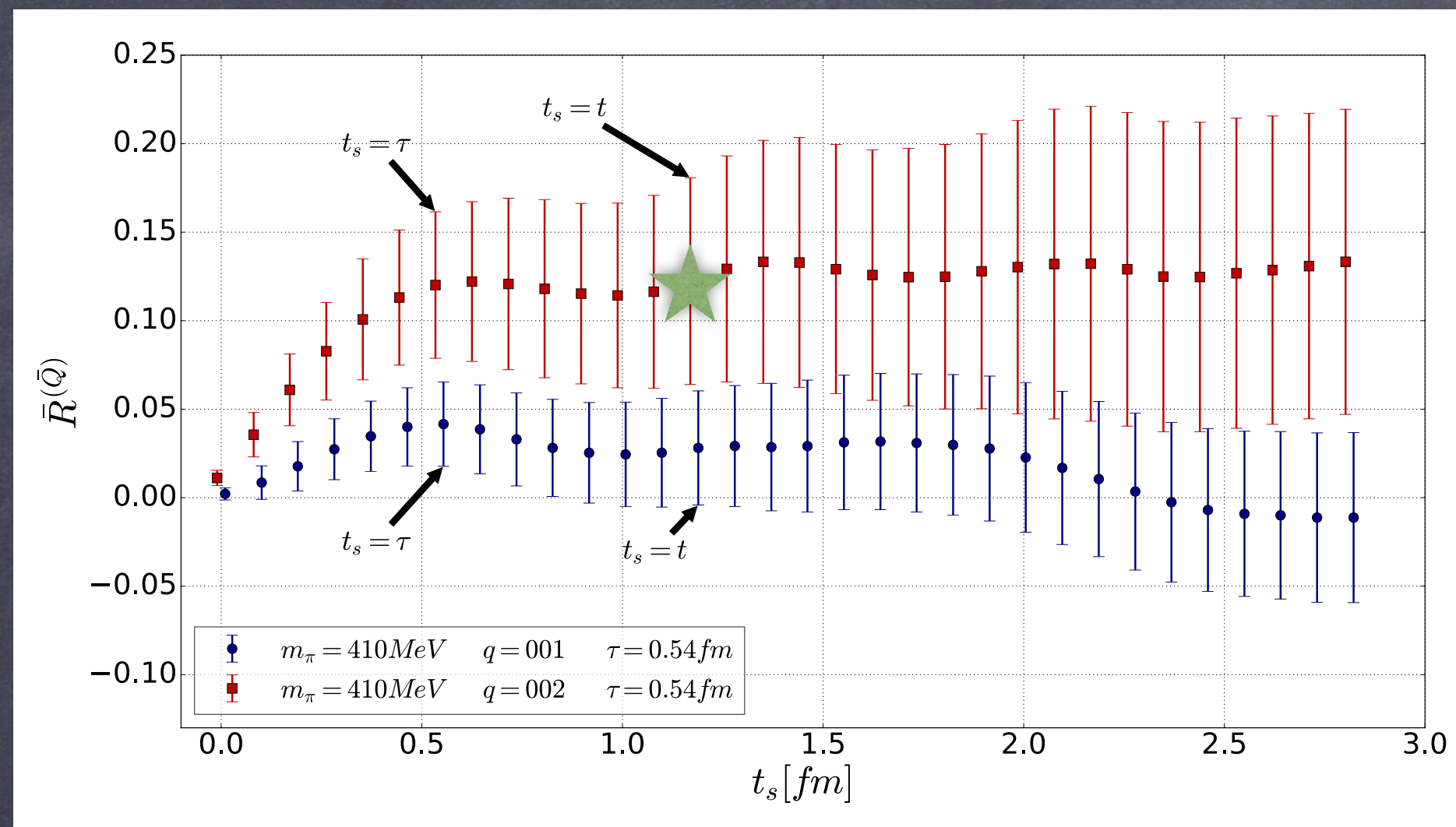
Atiyah, Singer: 1971

P. Hasenfratz: 1998

P. Hasenfratz, Laliena, Niedermeyer: 1998

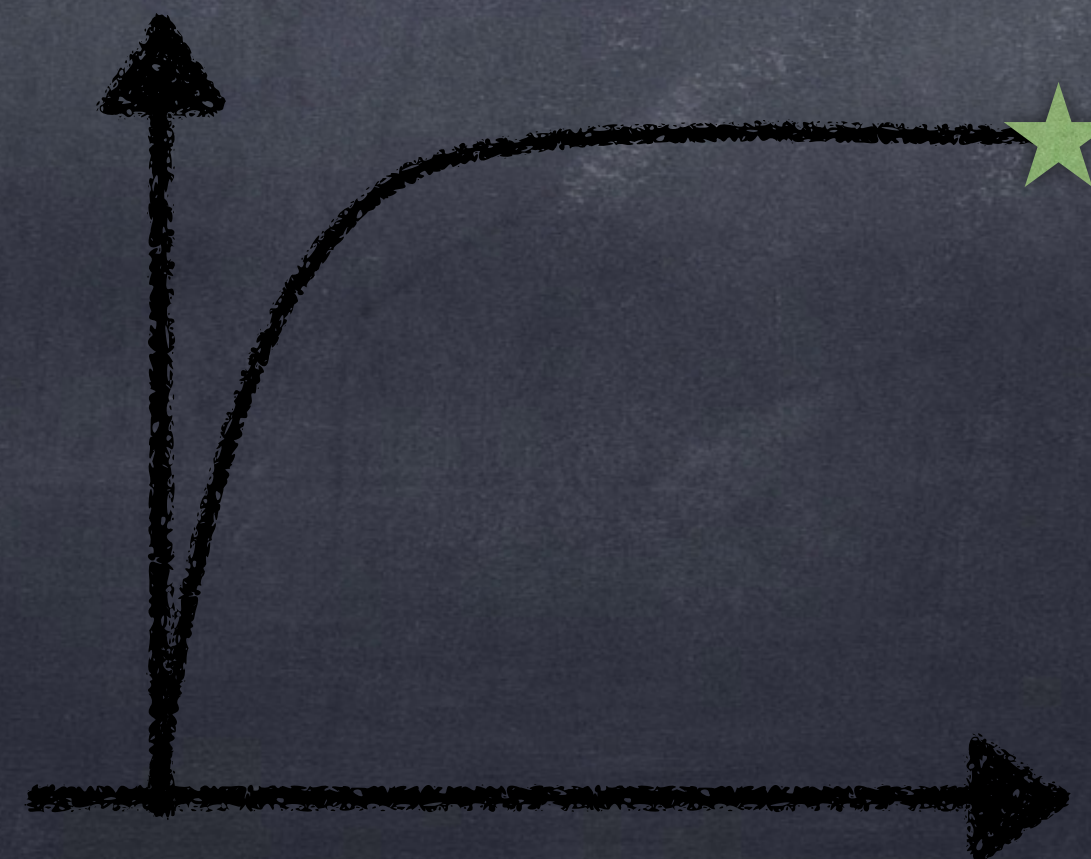
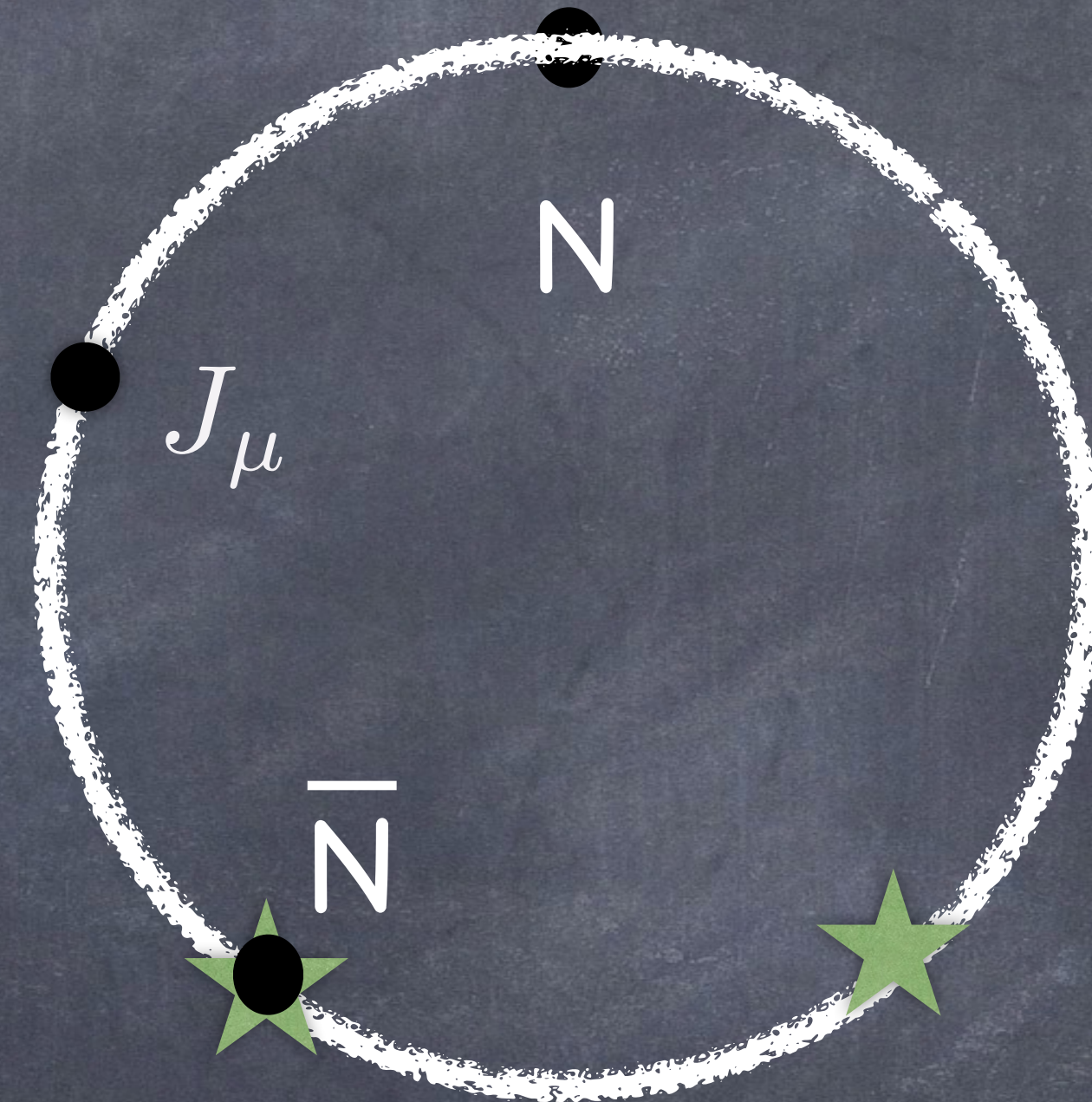
Signal-to-noise improvement

★ = $q(t)$

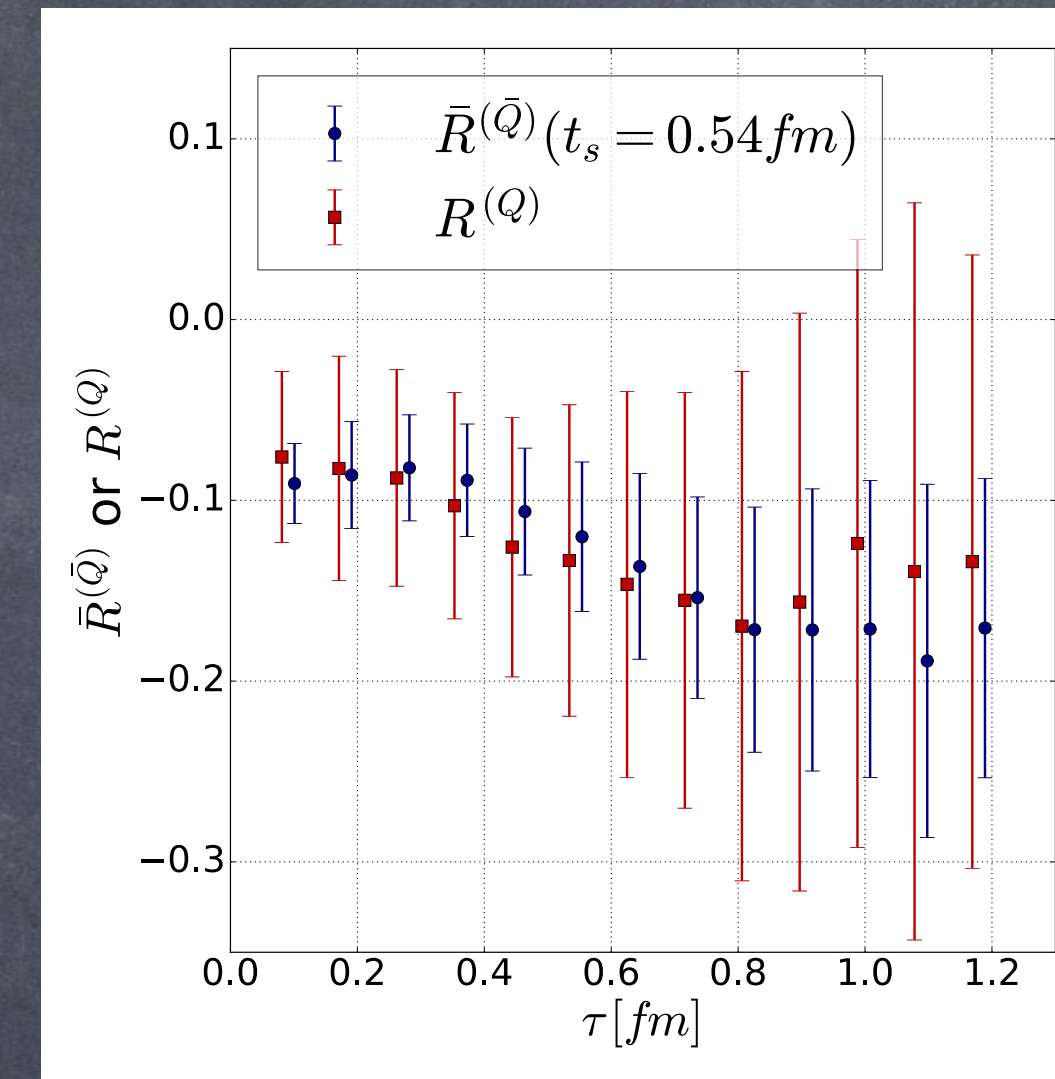
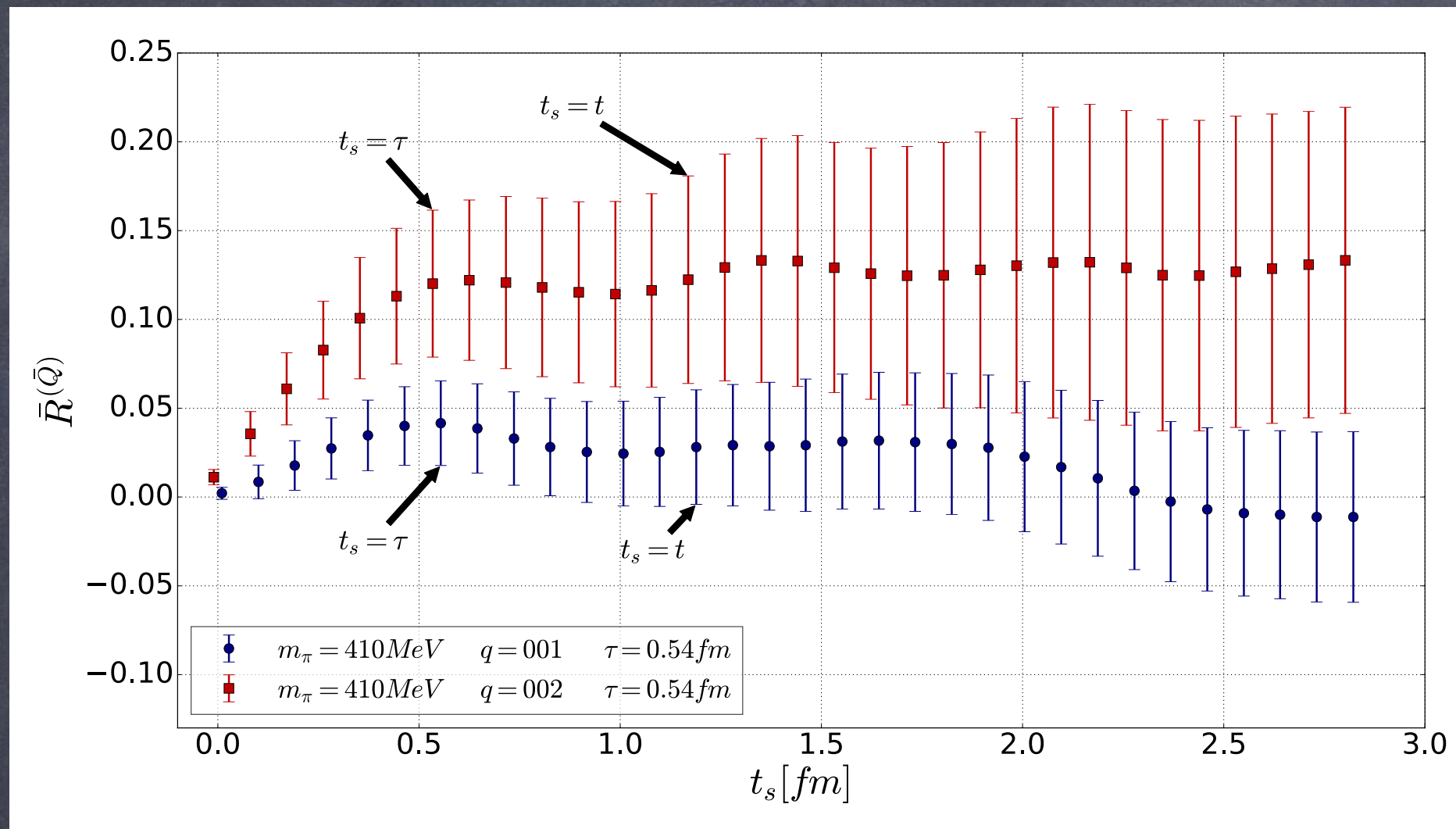


$$R^Q = \frac{G_3^Q(t, \tau, t_f; \underline{p}', \underline{q})}{G_2(\underline{p}', t)} \cdot K(t, \tau; \underline{p}', \underline{q})$$

Dragos, Luu, A.S.,
de Vries, Yousif: 2019



Signal-to-noise improvement



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Dragos, Luu, A.S.,
de Vries, Yousif: 2019