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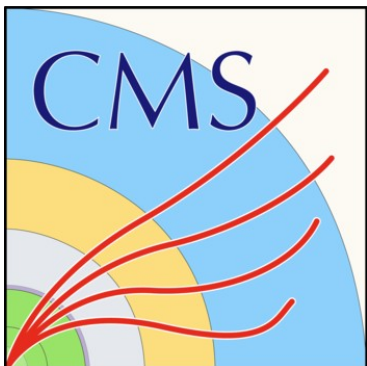


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# Recent Heavy Flavour Physics results by the CMS experiment



Alessio Boletti (LIP, Lisbon)  
on behalf of the CMS Collaboration  
EPS-HEP – 7<sup>th</sup> July 2025 – Marseille

- Search for rare  $D^0 \rightarrow \mu\mu$  decay

[arXiv:2506.06152]  
submitted to PRL

- First full reconstruction of  $B^*$  mesons

- Follow other CMS results:

[CMS-BPH-24-011]

- Lepton flavor (universality) violation studies with heavy flavor at CMS
- Observation of a family of all-charm tetraquarks with spin-2 and positive parity at CMS
- Production of Heavy Flavours at CMS

by Chiara Basile,  
today 3 PM

by Xining Wang,  
tomorrow 4:30 PM  
QCD & hadron physics track

by Marco Buonsante,  
Wed 5 PM

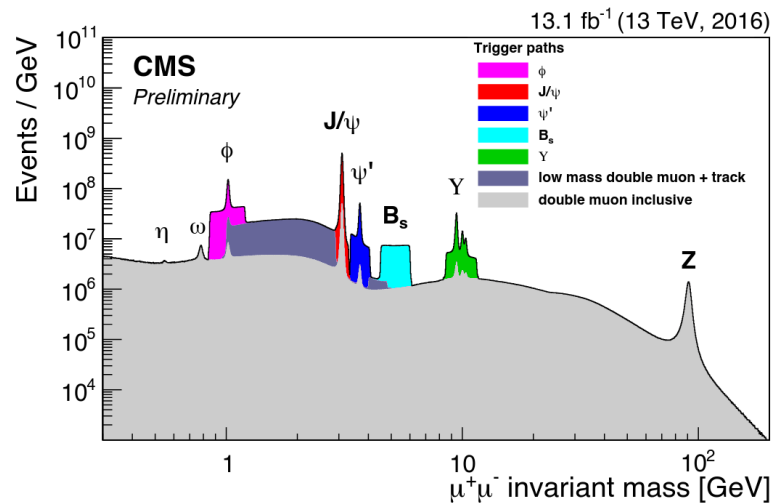
# CMS triggers for heavy-flavor physics

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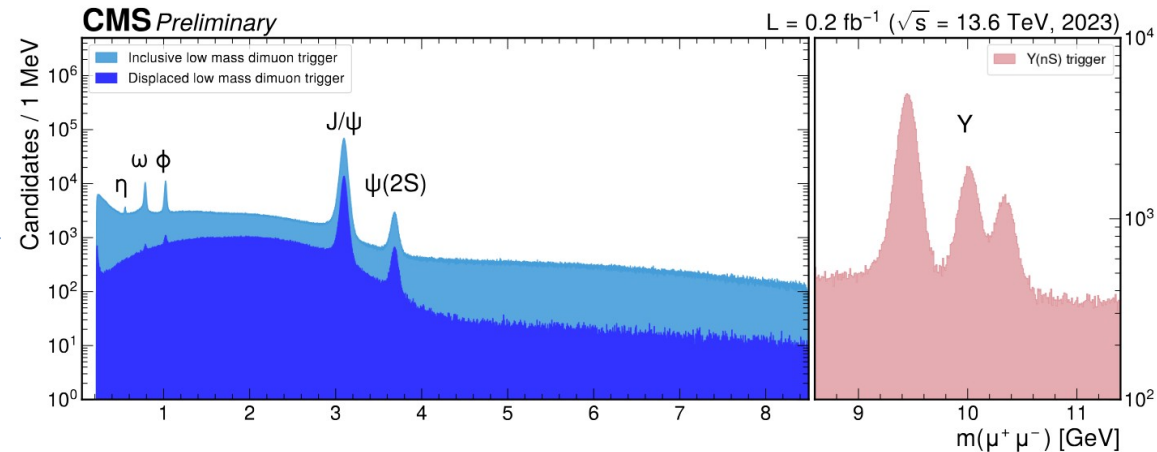
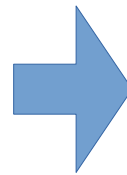
Many heavy-flavor analyses in CMS rely on dimuon triggers

Run2: set of triggers dedicated to specific dimuon mass regions or topologies

Run3: inclusive dimuon trigger with loose requirements on the momenta



[CMS-DP-2016-059]



[CMS-NOTE-2023-007]

# Search for rare $D^0 \rightarrow \mu\mu$ decay

[\[arXiv:2506.06152\]](#)

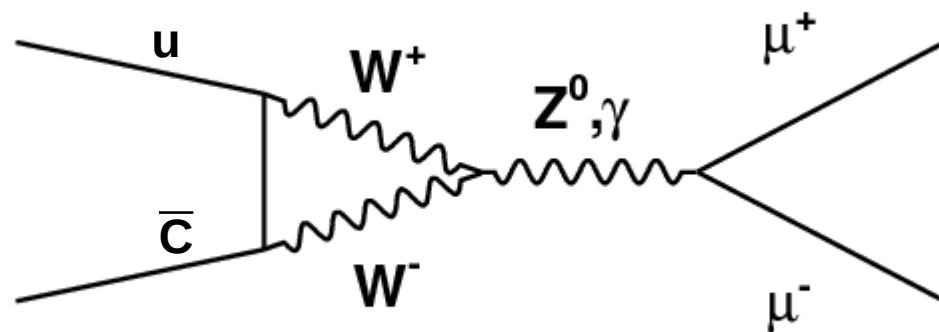
submitted to PRL

# Search for $D^0 \rightarrow \mu\mu$ decay

[arXiv:2506.06152]

Flavour changing neutral currents gained a lot of attention in the last decades

- $bs\ell\ell$  transitions under heavy scrutiny  
ex.  $B_s \rightarrow \mu\mu$  and  $b \rightarrow s\mu\mu$  analyses
- $c\ell\ell$  transitions less studied



$D^0 \rightarrow \mu\mu$  decay heavily suppressed in the SM (loop diagram + helicity):

- BR prediction  $\sim 10^{-13}$
- High sensitivity to new-physics phenomena

Former most sensitive [analysis by LHCb](#) posed a limit at:  $\text{BR}(D^0 \rightarrow \mu\mu) < 3.5 \cdot 10^{-9}$  (95% CL)

This analysis uses 2022+2023 CMS data, and first one using new low- $p_T$  dimuon trigger

# Search for $D^0 \rightarrow \mu\mu$ decay

[arXiv:2506.06152]

Analysis uses  $D^0$  from cascade decays:  $D^{*+} \rightarrow D^0 \pi^+$

- Exploits mass difference  $\Delta m = m(D^{*+}) - m(D^0)$  to strongly suppress combinatorial
- $D^{*+}$  produced promptly or from B-hadron decays
- Final state: two opposite charged muons + track

$D^0 \rightarrow \pi^+ \pi^-$  used as normalization channel:

$$\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) = \mathcal{B}(D^0 \rightarrow \pi^+ \pi^-) \frac{N_{D^0 \rightarrow \mu\mu}}{N_{D^0 \rightarrow \pi\pi}} \frac{\epsilon_{D^0 \rightarrow \pi\pi}}{\epsilon_{D^0 \rightarrow \mu\mu}}$$

Sources of background:

- Combinatorial: suppressed via BDT, exploiting topological and kinematic features
- Peaking backgrounds for signal (w/ misID pions):
  - $D^{*+} \rightarrow D^0(\pi\pi)\pi$
  - $D^{*+} \rightarrow D^0(\pi\mu\nu)\pi$
- Peaking background for normalization channel:
  - $D^{*+} \rightarrow D^0(K\pi)\pi$

# Search for $D^0 \rightarrow \mu\mu$ decay - results

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[arXiv:2506.06152]

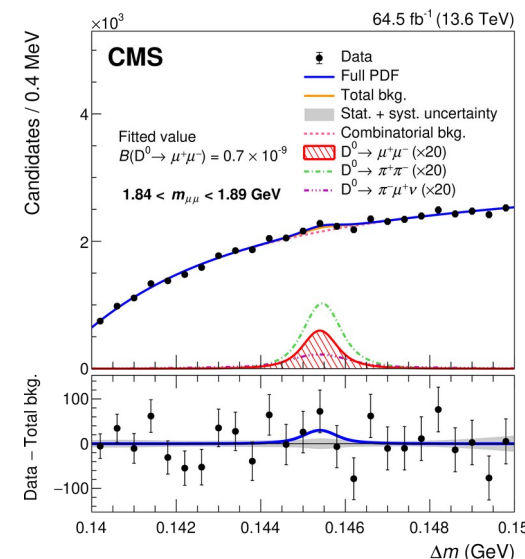
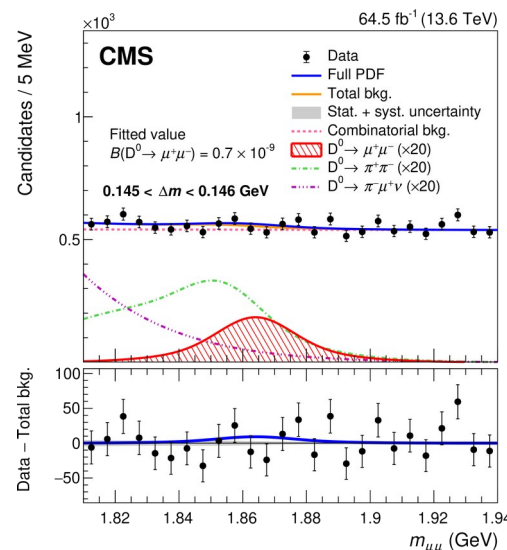
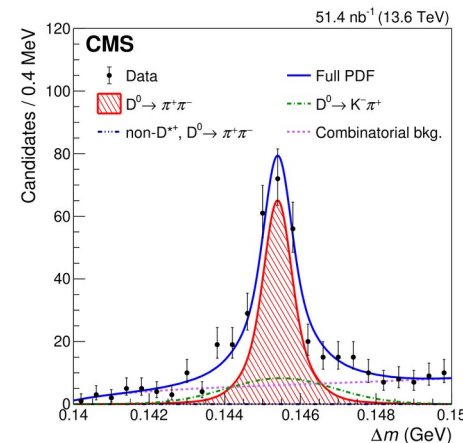
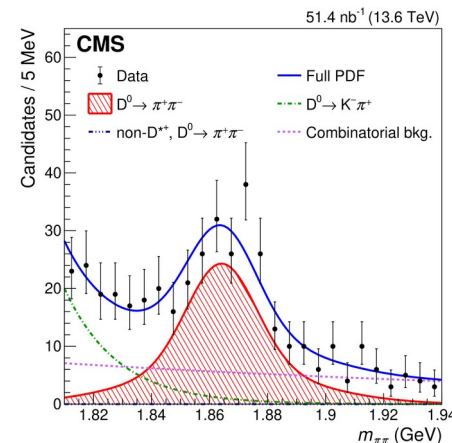
2D UML fits:

- to  $[m(\pi\pi), \Delta m]$  in normalization sample
- to  $[m(\mu\mu), \Delta m]$  in signal sample

No significant signal excess

Resulting limit:

$$\text{BR}(D^0 \rightarrow \mu\mu) < 2.4 \cdot 10^{-9} \text{ at 95\% CL}$$



# Fully exclusive reconstruction of $B^{*+}$ , $B^{*0}$ , $B_s^{*0}$ radiative decays

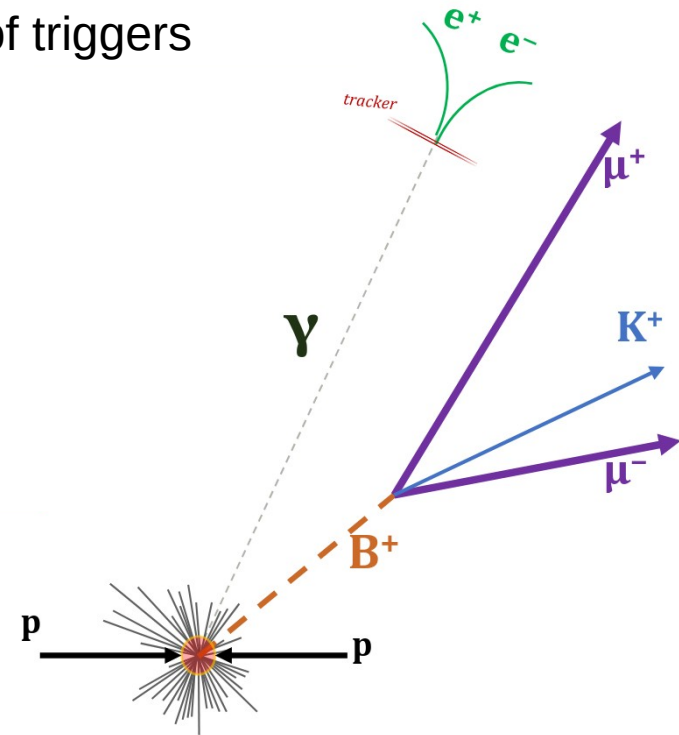
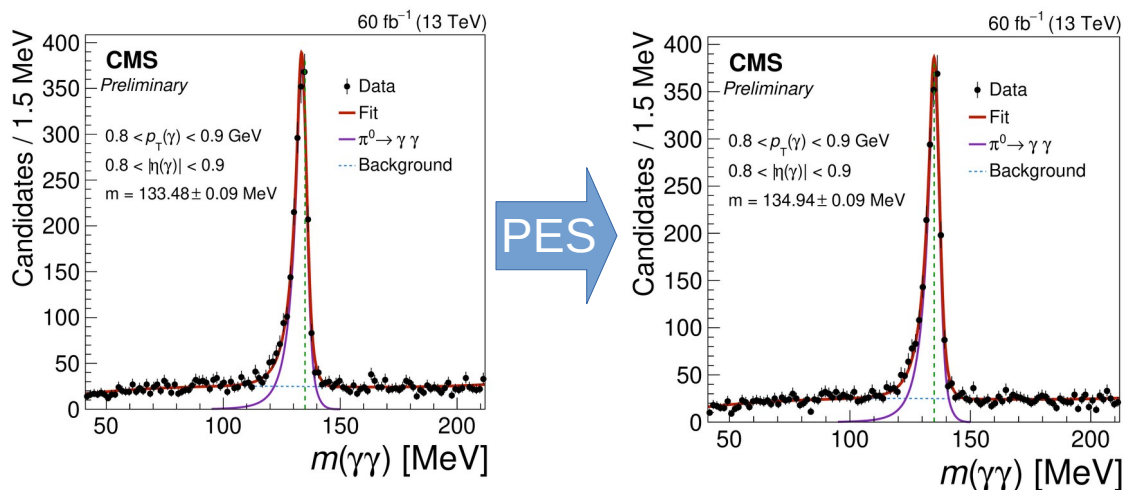
[CMS-BPH-24-011]



# $B^* \rightarrow B\gamma$ full reconstruction

[CMS-BPH-24-011]

- CMS analysis on Run-2 heavy-flavor datasets, with mixture of triggers
- Exploits charmonium decays of B mesons
  - $B^+ \rightarrow \psi K^+$
  - $B^0 \rightarrow \psi K^*(892)^0 (\rightarrow K^+\pi^-)$
  - $B_s \rightarrow \psi \phi (\rightarrow K^+K^-)$
  - $J/\psi$  or  $\psi(2S) \rightarrow \mu\mu$
- Photon conversion reconstruction in  $e^+e^-$
- Refit of electron tracks and  $B\gamma$  vertex (including other tracks from PV activity) to improve mass resolution

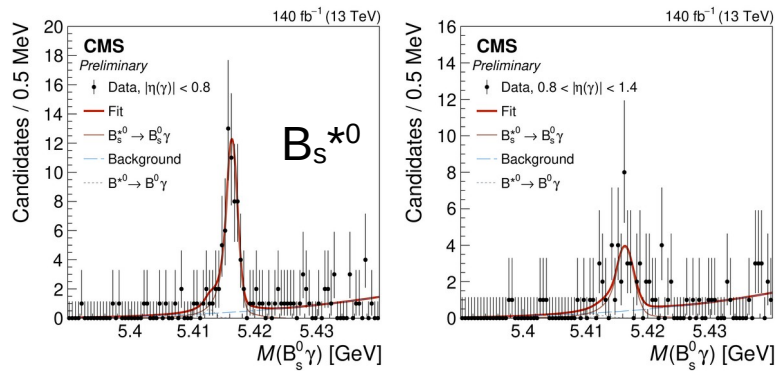
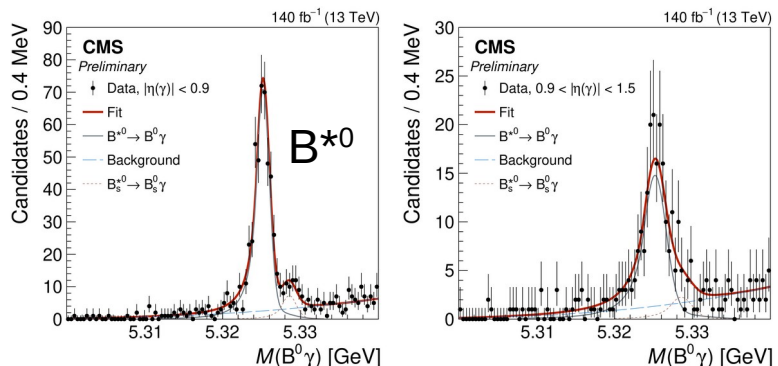
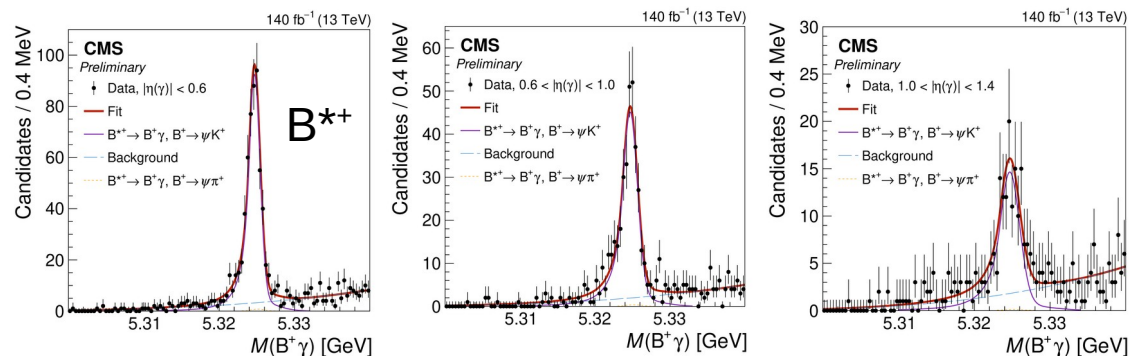


Dedicated photon energy correction:

- $\pi^0 \rightarrow \gamma\gamma$  with double conversion used in bins of p<sub>T</sub> and η
- Successful in correcting energy underestimation

# B\* full reconstruction

[CMS-BPH-24-011]



Simultaneous fit in 7 categories of  $M(X\gamma) = m(X\gamma) - m(X) + M_{\text{PDG}}(X)$


Categories defined by flavor and  $\eta$  ranges with common mass parameters within each flavor

Models include: Signal,  
Combinatorial bkg,  
Peaking bkg:  $B^+ \rightarrow \psi\pi^+$  and  
 $B^{*0} \leftrightarrow B_s^{*0}$  cross-feed

Three states reconstructed fully  
exclusively for the first time!!

# B\* mass results

[CMS-BPH-24-011]

|    | Parameter   | Value  |   |   |  |  |
|----|---|--|---|---|--|--|
| 1  | $\Delta m(\text{B}^{*+}) \equiv m(\text{B}^{*+}) - m(\text{B}^+)$                             | $45.277 \pm 0.039 \pm 0.021 \text{ MeV}$         |  | <b>Hyperfine splitting in B system!</b> | One order of magnitude precision improvement wrt PDG 2024:   |  |
| 2  | $\Delta m(\text{B}^{*0}) \equiv m(\text{B}^{*0}) - m(\text{B}^0)$                             | $45.471 \pm 0.056 \pm 0.024 \text{ MeV}$         |   |   |  | $45.34 \pm 0.20$<br>$45.34 \pm 0.20$<br>$48.5 \pm 1.4$   |
| 3  | $\Delta m(\text{B}_s^{*0}) \equiv m(\text{B}_s^{*0}) - m(\text{B}_s^0)$                       | $49.407 \pm 0.132 \pm 0.034 \text{ MeV}$         |   |   |  |  |
| 4  | $m(\text{B}^{*+})$  | $5324.69 \pm 0.04 \pm 0.02 \pm 0.07 \text{ MeV}$ | New masses to add to PDG  |   |  |  |
| 5  | $m(\text{B}^{*0})$  | $5325.19 \pm 0.06 \pm 0.02 \pm 0.08 \text{ MeV}$ |   |   | “B* mass” $5324.75 \pm 0.20 \text{ MeV}$<br>B <sub>s</sub> <sup>*0</sup> mass $5415.4 \pm 1.4 \text{ MeV}$ |  |
| 6  | $m(\text{B}_s^{*0})$  | $5416.34 \pm 0.13 \pm 0.03 \pm 0.10 \text{ MeV}$ |   |   |  |  |
| 7  | $m(\text{B}^{*0}) - m(\text{B}^{*+})$   | $0.50 \pm 0.07 \pm 0.01 \pm 0.05 \text{ MeV}$    | In agreement with CMS-BPH-16-003  |   |  |  |
| 8  | $m(\text{B}_s^{*0}) - m(\text{B}^{*+})$   | $91.66 \pm 0.14 \pm 0.03 \pm 0.12 \text{ MeV}$   |   |   |  |  |
| 9  | $m(\text{B}_s^{*0}) - m(\text{B}^{*0})$   | $91.15 \pm 0.14 \pm 0.03 \pm 0.12 \text{ MeV}$   |   |   |  |  |
| 10 | $m(\text{B}_s^{*0}) - \frac{m(\text{B}^{*0}) + m(\text{B}^{*+})}{2}$                          | $91.40 \pm 0.13 \pm 0.03 \pm 0.12 \text{ MeV}$   |   |   |  |  |
| 11 | $\Delta m(\text{B}^{*0}) - \Delta m(\text{B}^{*+})$   | $0.19 \pm 0.07 \pm 0.01 \text{ MeV}$             |   |   | First measurements   |  |
| 12 | $\Delta m(\text{B}_s^{*0}) - \Delta m(\text{B}^{*+})$   | $4.13 \pm 0.14 \pm 0.03 \text{ MeV}$             |   |   |  |  |
| 13 | $\Delta m(\text{B}_s^{*0}) - \Delta m(\text{B}^{*0})$   | $3.94 \pm 0.14 \pm 0.03 \text{ MeV}$             |   |   |  |  |
| 14 | $\Delta m(\text{B}_s^{*0}) - \frac{\Delta m(\text{B}^{*0}) + \Delta m(\text{B}^{*+})}{2}$     | $4.03 \pm 0.13 \pm 0.03 \text{ MeV}$             |   |   |  |  |
| 15 | $\Delta m(\text{B}^{*0}) / \Delta m(\text{B}^{*+})$   | $1.0043 \pm 0.0015 \pm 0.0002$                   |   |   |  | Some systematics cancel in differences and ratios and theory uncertainty also expected to be reduced |
| 16 | $\Delta m(\text{B}_s^{*0}) / \Delta m(\text{B}^{*+})$   | $1.0912 \pm 0.0031 \pm 0.0007$                   |   |   |  |  |
| 17 | $\Delta m(\text{B}_s^{*0}) / \Delta m(\text{B}^{*0})$   | $1.0866 \pm 0.0031 \pm 0.0007$                   |   |   |  |  |
| 18 | $\frac{2 \cdot \Delta m(\text{B}_s^{*0})}{\Delta m(\text{B}^{*+}) + \Delta m(\text{B}^{*0})}$ | $1.0889 \pm 0.0030 \pm 0.0007$                   |   |   |  |  |

Some systematics cancel in differences and ratios and theory uncertainty also expected to be reduced

# B\* mass – comparison with theory

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[CMS-BPH-24-011]

A few lattice theory papers provide predictions with uncertainties

One paper comments on the ratio of hyperfine splitting

| Parameter  | Measurement, MeV             | Theory, MeV   |
|--|------------------------------|---|
| $\Delta m(B^{*+})$<br>$m(B^{*+}) - m(B^+)$       | $45.277 \pm 0.039 \pm 0.021$ | $50 \pm 3$ [10]<br>$39 \pm 2$ [24]                            |
| $\Delta m(B^{*0})$<br>$m(B^{*0}) - m(B^0)$       | $45.471 \pm 0.056 \pm 0.024$ | $41.7 \pm 5.3$ [25]   |
| $\Delta m(B_s^{*0})$<br>$m(B_s^{*0}) - m(B_s^0)$ | $49.407 \pm 0.132 \pm 0.034$ | $52 \pm 3$ [10]<br>$38 \pm 1$ [24]<br>$37.8 \pm 6.7$ MeV [25] |

| Parameter  | Measurement                         | theory                 |
|--|-------------------------------------|------------------------|
| $\Delta m(B^{*0}) / \Delta m(B^{*+})$<br>$\frac{m(B^{*0}) - m(B^0)}{m(B^{*+}) - m(B^+)}$       | $1.0043 \pm 0.0015 \pm 0.0002$<br>— | —                      |
| $\Delta m(B_s^{*0}) / \Delta m(B^{*+})$<br>$\frac{m(B_s^{*0}) - m(B_s^0)}{m(B^{*+}) - m(B^+)}$ | $1.0912 \pm 0.0031 \pm 0.0007$      | $1.007 \pm 0.034$ [10] |
| $\Delta m(B_s^{*0}) / \Delta m(B^{*0})$<br>$\frac{m(B_s^{*0}) - m(B_s^0)}{m(B^{*0}) - m(B^0)}$ | $1.0866 \pm 0.0031 \pm 0.0007$      |                        |
| $\frac{2 \cdot \Delta m(B_s^{*0})}{\Delta m(B^{*+}) + \Delta m(B^{*0})}$                       | $1.0889 \pm 0.0030 \pm 0.0007$      |                        |

[10] [Phys.Rev.D 86 \(2012\) 094510](#)

[24] [JHEP 01 \(2025\) 123](#)

[25] [Phys.Rev.D 92 \(2015\) 5, 054509](#)

# Summary and conclusions

- Search for rare  $D^0 \rightarrow \mu\mu$  decay
  - Excellent example of application for new CMS soft dimuon triggers
  - New best limit on the branching ratio
  - Still 4 order of magnitude above SM prediction
- First full reconstruction of  $B^*$  mesons
  - Uses converted photons to exclusively reconstruct the  $B^{*+}$ ,  $B^{*0}$ ,  $B_s^{*0}$  states
  - Most precise measurement of hyperfine splitting in B system
  - Theory predictions need to be improved!
- As inclusive dimuon and single-muon triggers keep collecting data, stay tuned for new exiting results to come!

Backup slides

# $D^0 \rightarrow \mu\mu$ systematic uncertainties

| Source                                       | $D^0 \rightarrow \mu\mu$ | $D^0 \rightarrow \pi\pi$ | $D^0 \rightarrow \pi\mu\nu$ |
|--|--------------------------|--------------------------|-----------------------------|
| Trigger efficiency                           | 0.7%                     | 0.7%                     | 0.7%                        |
| Muon efficiency                              | 2%                       | —                        | 1%                          |
| Tracking efficiency                          | 4.6%                     | 4.6%                     | 4.6%                        |
| Pileup                                       | 1%                       | 1%                       | 1%                          |
| $D^0 \rightarrow \pi^+\pi^-$ yield           | 8.7%                     | 8.7%                     | 8.7%                        |
| Efficiency                                   | 0.2%                     | 0.6%                     | 12%                         |
| $d_{\text{MVA}}$ correction                  | 1.2%                     | 2.0%                     | —                           |
| $\mathcal{B}(D^0 \rightarrow \pi^+\pi^-)$    | 1.7%                     | —                        | 1.7%                        |
| $\mathcal{B}(D^0 \rightarrow \pi^-\mu^+\nu)$ | —                        | —                        | 4.5%                        |
| Fit bias                                     | 1%                       | —                        | —                           |
| Misidentification rate                       | —                        | 28%                      | 14%                         |

# $D^0 \rightarrow \mu\mu$ resulting yields

| Range                                  | Signal        | Comb. bkg.         | $D^0 \rightarrow \pi^+\pi^-$ | $D^0 \rightarrow \pi^-\mu^+\nu$ | Data    |
|--|---------------|--------------------|------------------------------|---------------------------------|---------|
| Full range                             | $100 \pm 120$ | $126\,140 \pm 380$ | $278 \pm 51$                 | $231 \pm 40$                    | 126 752 |
| $0.145 < \Delta m < 0.146 \text{ GeV}$ | $67 \pm 81$   | $14\,037 \pm 42$   | $179 \pm 33$                 | $94 \pm 16$                     | 14 412  |
| $1.84 < m_{\mu\mu} < 1.89 \text{ GeV}$ | $90 \pm 110$  | $48\,530 \pm 150$  | $162 \pm 30$                 | $62 \pm 11$                     | 48 798  |



# B\* history (from Sergey's talk @LHCP)

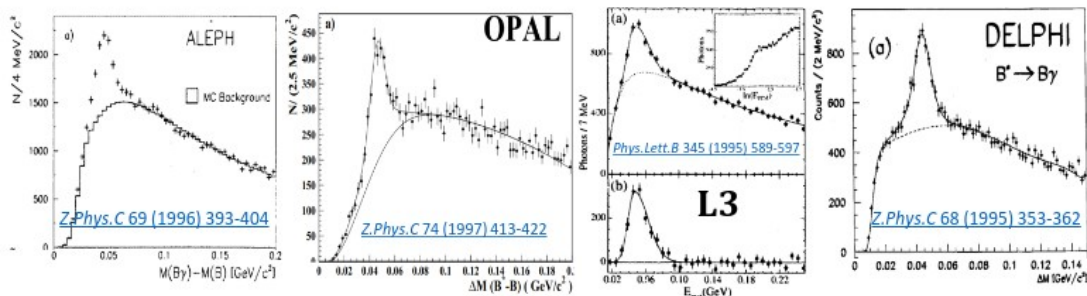
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## HISTORY OF B\* meson studies

CMS-PAS-BPH-24-011

LEP experiments [L3](#), [DELPHI](#), [OPAL](#), [ALEPH](#)  
using  $Z \rightarrow b\bar{b}$  process, **inclusively** reconstruct B meson as **b-jet**  
combine **b-jet** with a **converted photon** (calibrated via  $\pi^0$ )

Measure **averaged between  $B^{*+}$ ,  $B^{*0}$ , and  $B_s^{*0}$**  mass difference  
 $m(B^{*}) - m(B)$



Mass differences also measured via P-wave  $B_s^0$  states

$m(B^{*+}) - m(B^+)$  measured by LHCb using the difference between  $B_{s2}^*(5840)^0 \rightarrow B^{*+} K^-$  and  $B_{s2}^*(5840)^0 \rightarrow B^+ K^-$  peak positions

$m(B^{*+}) - m(B^{*0})$  was measured by [CMS \(BPH-16-003\)](#) via the difference between  $B_{s1}(5830)^0 \rightarrow B^{*0} K_S^0$  and  $B_{s1}(5830)^0 \rightarrow B^{*+} K^-$  peak positions

Assumes  $\Delta m = m(B^{*0}) - m(B^0) = m(B^{*+}) - m(B^+)$   
for D mesons such  $\Delta m$  are different by 1.5 MeV!

| VALUE (MeV)              | EVTS | DOCUMENT ID                                       | TECN |
|--------------------------|------|---|------|
| $m_{B^{*+}} - m_B$       |      |   |      |
| $45.21 \pm 0.21$         |      | OUR FIT   |      |
| $45.42 \pm 0.26$         |      | OUR AVERAGE includes data from $m_{B^{*+}} - m_B$ |      |
| $46.2 \pm 0.3 \pm 0.8$   |      | <sup>1</sup> ACKERSTAFF 1997M                     | OPAL |
| $45.3 \pm 0.35 \pm 0.87$ | 4227 | <sup>1</sup> BUSKULIC 1996D                       | ALEP |
| $45.5 \pm 0.3 \pm 0.8$   |      | <sup>1</sup> ABREU 1995R                          | DLPH |
| $46.3 \pm 1.9$           | 1378 | <sup>1</sup> ACCIARRI 1995B                       | L3   |

28+ year-old measurements!

PDG still has a single "entry" for  $B^{*+}$  and  $B^{*0}$ !

|            |            |  |                                |
|------------|------------|--|--------------------------------|
| $B^+$      | $1/2(1^-)$ | $B^+$ MASS   | $5324.71 \pm 0.21 \text{ MeV}$ |
| $B^0$      | $1/2(0^-)$ | $m_{B^{*+}} - m_B$                                     | $45.21 \pm 0.21 \text{ MeV}$   |
| $B^{*+}$   | $1/2(1^-)$ | $m_{B^{*+}} - m_{B^{*0}}$                              | $45.37 \pm 0.21 \text{ MeV}$   |
| $B^{*0}$   | $1/2(1^-)$ | $ (m_{B^{*+}} - m_{B^{*0}}) - (m_{B^{*0}} - m_{B^0}) $ | $< 6 \text{ MeV CL}=95.0\%$    |
| $B_s^{*0}$ | $1/2(1^-)$ | $m_{B^{*0}} - m_{B^0}$                                 | $0.91 \pm 0.26 \text{ MeV}$    |

Main challenge: very low-energy photons emitted in  $B^{*} \rightarrow B\gamma$

# B\* history (from Sergey's talk @LHCP)

## $B_s^{*0}$ measurements at B-Factories

CMS-PAS-BPH-24-011

$B_s^{*0}$  mass difference w.r.t.  $B_s^0$  was previously measured at B-factories via the energy spectrum of reconstructed  $B_s^0$  mesons assumed to be produced in  $Y(5S)$  decays:

- $Y(5S) \rightarrow B_s^0 \bar{B}_s^0$
- $Y(5S) \rightarrow B_s^{*0} \bar{B}_s^0$
- $Y(5S) \rightarrow B_s^0 \bar{B}_s^{*0}$
- $Y(5S) \rightarrow B_s^{*0} \bar{B}_s^{*0}$

However, the results were not in a good agreement with each other (PDG scale factor 2.9)

Central value of the mass difference is larger in comparison to  $B^+$  &  $B^0$

| $m_{B_s^*} - m_{B_s}$  |                                |      |   |  |
|------------------------|--------------------------------|------|---|--|
| VALUE (MeV)            | DOCUMENT ID                    | TECN | COMMENT                                     |  |
| $48.5^{+1.8}_{-1.5}$   | OUR FIT                        |      | Error includes scale factor of <u>2.9</u> . |  |
| $46.1 \pm 1.5$         | OUR AVERAGE                    |      |   |  |
| $45.7 \pm 1.7 \pm 0.7$ | <sup>1</sup> AQUINES 2006      | CLEO | $e^+ e^- \rightarrow Y(5S)$                 |  |
| $47.0 \pm 2.6$         | <sup>2</sup> LEE-FRANZINI 1990 | CSB2 | $e^+ e^- \rightarrow Y(5S)$                 |  |

| $B_s^*$ MASS                                     |                           |      |   |  |
|--|---------------------------|------|---|--|
| From mass difference below and the $B_s^0$ mass. |                           |      |   |  |
| VALUE (MeV)                                      | DOCUMENT ID               | TECN |   |  |
| $5415.4^{+1.8}_{-1.5}$                           | OUR FIT                   |      | Error includes scale factor of <u>2.9</u> . |  |
| $5415.8 \pm 1.5$                                 | OUR AVERAGE               |      | Error includes scale factor of 2.6.         |  |
| $5416.4 \pm 0.4 \pm 0.5$                         | LOUVOT 2009               | BELL |   |  |
| $5411.7 \pm 1.6 \pm 0.6$                         | <sup>1</sup> AQUINES 2006 | CLEO |   |  |

*Do we have enough data in CMS to exclusively reconstruct  $B^{*+}$ ,  $B^{*0}$ , and  $B_s^{*0}$  mesons via  $J/\psi$  modes and provide separate measurements of the respective  $\Delta m$ ?*

# B\* systematics

| Source  | $m(B^{*+}) - m(B^+)$ | $m(B^{*0}) - m(B^0)$ | $m(B_s^{*0}) - m(B_s^0)$ |
|---|----------------------|----------------------|--------------------------|
| Signal model                                  | 4                    | 8                    | 21                       |
| Signal shape parameters                       | 17                   | 18                   | 15                       |
| Yield ratios between $ \eta(\gamma) $ regions | 1                    | 2                    | 10                       |
| Background shape                              | 2                    | < 1                  | 7                        |
| Cross-feed $B_s^{*0} \leftrightarrow B^{*0}$  | < 1                  | 1                    | 10                       |
| PES   | 12                   | 14                   | 16                       |
| Total   | 22                   | 24                   | 34                       |

$\Delta m$  uncertainties  
[keV]

$\Delta m$  differences  
uncertainties [keV]

| Source  | $\Delta m(B^{*0}) - \Delta m(B^{*+})$ | $\Delta m(B_s^{*0}) - \Delta m(B^{*+})$ | $\Delta m(B_s^{*0}) - \Delta m(B^{*0})$ | $\Delta m(B_s^{*0}) - \frac{\Delta m(B^{*0}) + \Delta m(B^{*+})}{2}$ |
|---|---------------------------------------|---|---|--|
| Baseline value                                | 194                                   | 4130                                    | 3936                                    | 4033   |
| Statistical uncertainty                       | 68                                    | 138                                     | 139                                     | 134  |
| Signal model                                  | 4                                     | 23                                      | 23                                      | 23   |
| Signal shape parameters                       | 2                                     | 7                                       | 7                                       | 7  |
| Yield ratios between $ \eta(\gamma) $ regions | 3                                     | 11                                      | 7                                       | 9  |
| Background shape                              | 3                                     | 9                                       | 6                                       | 8  |
| $B^+ \rightarrow J/\psi \pi^+$ yield          | 1                                     | 1                                       | < 1                                     | < 1  |
| Cross-feed $B_s^{*0} \leftrightarrow B^{*0}$  | 1                                     | 10                                      | 12                                      | 11   |
| Photon energy scale                           | 4                                     | 11                                      | 11                                      | 11   |
| Total systematic                              | 8                                     | 31                                      | 31                                      | 31   |

| Source  | $\Delta m(B^{*0}) / \Delta m(B^{*+})$ | $\Delta m(B_s^{*0}) / \Delta m(B^{*+})$ | $\Delta m(B_s^{*0}) / \Delta m(B^{*0})$ | $\frac{2 \cdot \Delta m(B_s^{*0})}{\Delta m(B^{*+}) + \Delta m(B^{*0})}$ |
|---|---------------------------------------|---|---|--|
| Baseline value                                | 1.00428                               | 1.09122                                 | 1.08656                                 | 1.08888  |
| Statistical uncertainty                       | 0.00151                               | 0.00306                                 | 0.00309                                 | 0.00297  |
| Signal model                                  | 0.00009                               | 0.00050                                 | 0.00052                                 | 0.00052  |
| Signal shape parameters                       | 0.00005                               | 0.00014                                 | 0.00016                                 | 0.00016  |
| Yield ratios between $ \eta(\gamma) $ regions | 0.00008                               | 0.00023                                 | 0.00016                                 | 0.00020  |
| Background shape                              | 0.00005                               | 0.00020                                 | 0.00014                                 | 0.00017  |
| $B^+ \rightarrow J/\psi \pi^+$ yield          | 0.00002                               | 0.00002                                 | 0                                       | 0.00001  |
| Cross-feed $B_s^{*0} \leftrightarrow B^{*0}$  | 0.00003                               | 0.00023                                 | 0.00025                                 | 0.00015  |
| Photon energy scale                           | 0.00009                               | 0.00025                                 | 0.00024                                 | 0.00024  |
| Total systematic                              | 0.00017                               | 0.00069                                 | 0.00068                                 | 0.00067  |

$\Delta m$  ratio  
uncertainties