

QCD

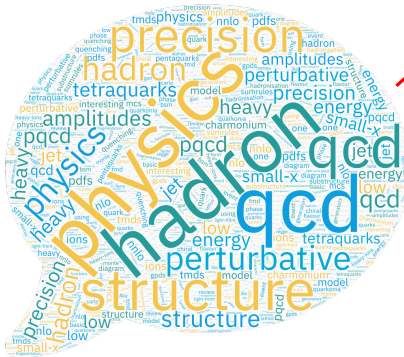
Gregory Soyez

IPhT, CNRS, CEA Saclay

EPS-HEP 2025 — Marseille, France — July 7-11 2025



QCD in the particle-physics ecosystem



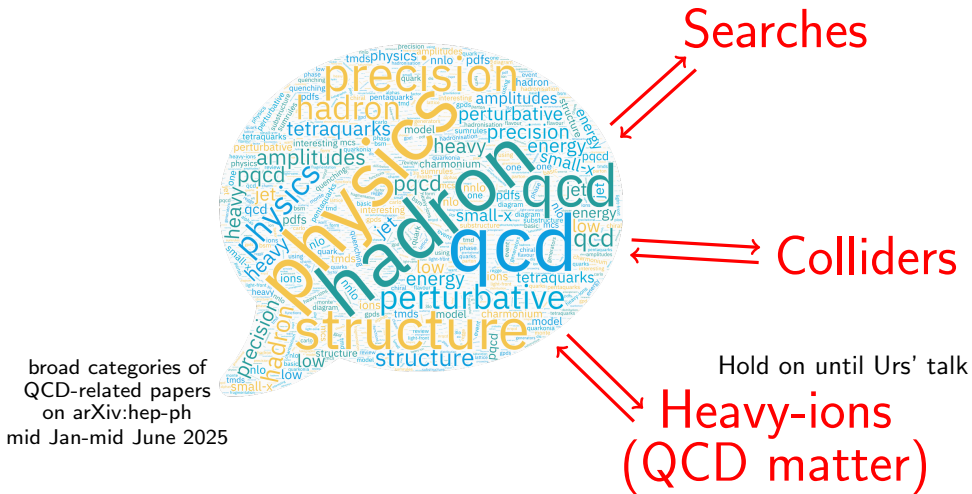
broad categories of
QCD-related papers
on arXiv:hep-ph
mid Jan-mid June 2025

Searches

No BSM without understanding SM
Much of the “precision” era comes from here

Colliders

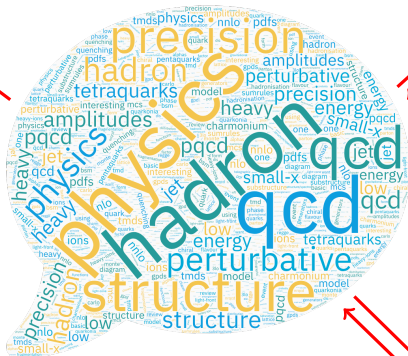
QCD in the particle-physics ecosystem



QCD itself!

- hadron spectra
- hadron structure
- amplitudes
- confinement
- precision physics
- α_s determination
- ...

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Searches

Colliders

⇒ Heavy-ions
(QCD matter)

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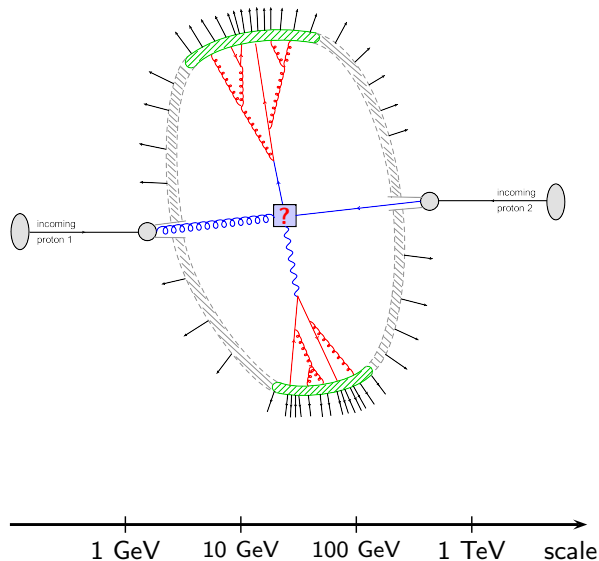
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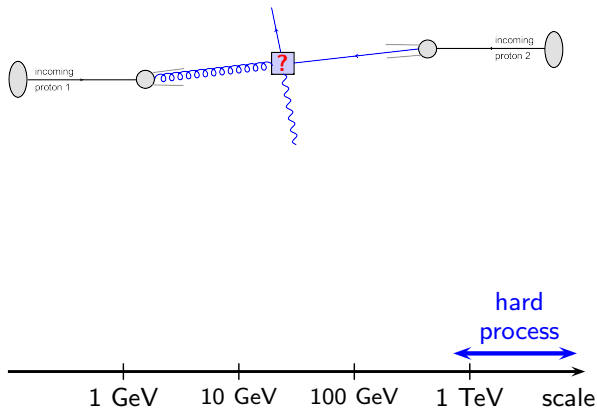
Main focus of this talk

Theorist view of a collision



**High-energy collision
have several
steps/ingredients**

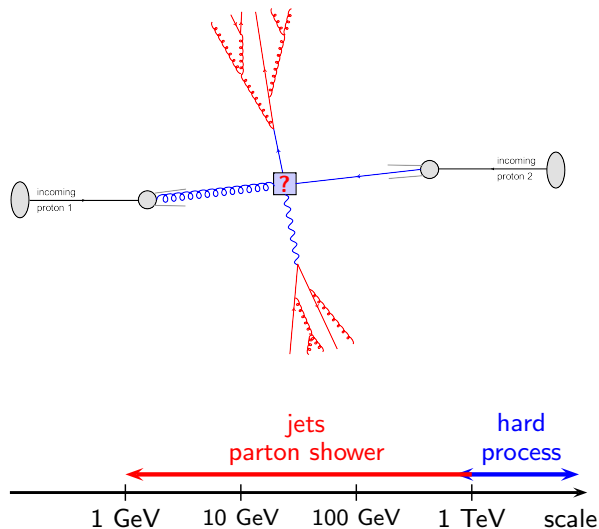
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**High-energy collision
have several
steps/ingredients**

- A hard process

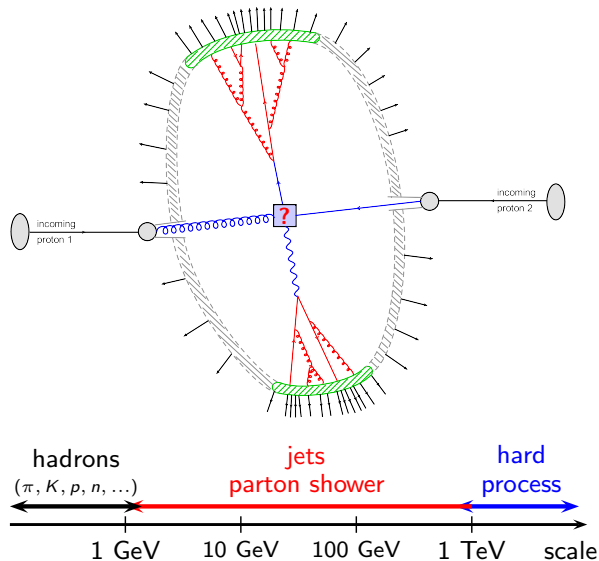
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**High-energy collision
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- A hard process
- Parton shower (initial and final-state)

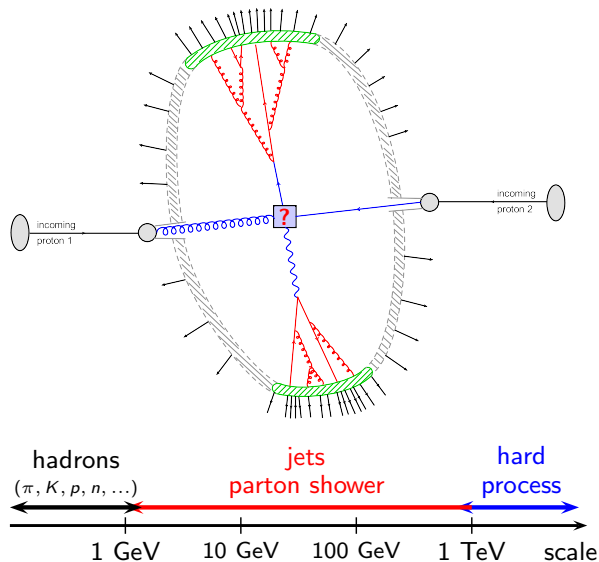
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**High-energy collision
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- A hard process
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- Hadronisation
- Multi-parton interactions
- Hadron decays

Theorist view of a collision



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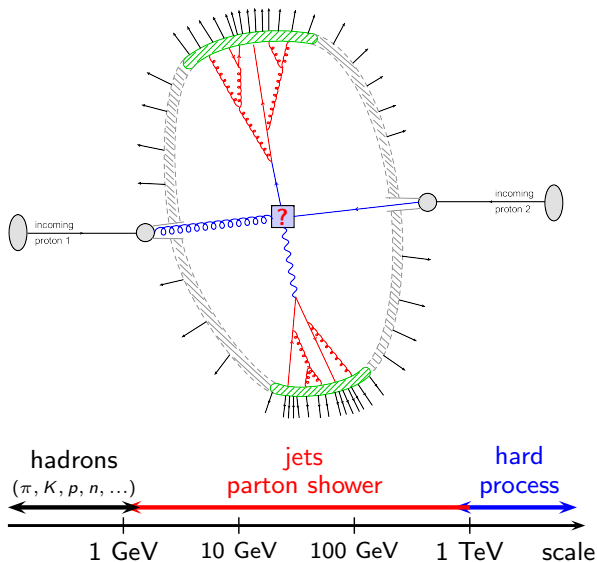
perturbative
“calculable”

non-pert.
“modelled”

various
approaches

- A hard process
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Theorist view of a collision



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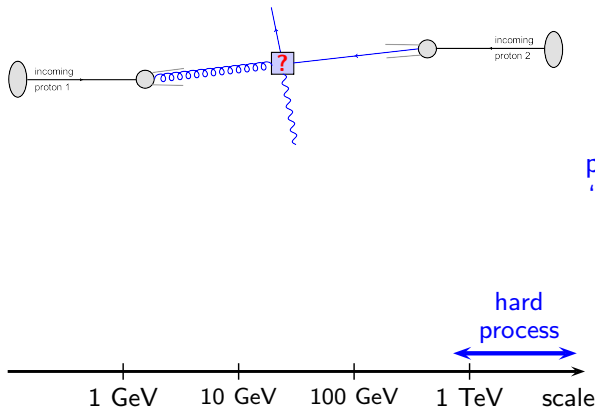
progress at each step

For each step of this collision “steps”:

- 1 Describe the underlying physics/interest
- 2 Highlight recent/ongoing progress
 - analytic viewpoint (most precise for a given observable)
 - Monte Carlo generator viewpoint (4-vectors give flexibility + usage in exp software)
- 3 Give a (tentative) view into the future

Usual caveat: incomplete and biased... but hopefully enough to give you the gist

Theorist view of a collision: focus on the hard process



**High-energy collision
have several
steps/ingredients**

perturbative
“calculable” | ● A hard process

Write hard processes as “ $\text{PDF}_a \otimes \text{PDF}_b \otimes \text{ME}_{\text{partonic}}$ ”:

$$\frac{d\sigma(Q)}{dv} = \int dx_a dx_b f_a(x_a, Q) f_b(x_b, Q) |\mathcal{M}(Q, x_a, x_b)|^2 \delta_{\text{observable}}(v)$$

$$|\mathcal{M}(Q, x_a, x_b)|^2 = |\mathcal{M}(Q, x_a, x_b)|_{\text{LO}}^2 + \alpha_s |\mathcal{M}(Q, x_a, x_b)|_{\text{NLO}}^2 + \alpha_s^2 |\mathcal{M}(Q, x_a, x_b)|_{\text{NNLO}}^2 + \dots$$

- This is the **core of the “precision-era” effort**
- **Crucial for LHC today and forthcoming high-lumi LHC**
Mandatory for future colliders
- Note: **known cases where the above factorisation is violated** (super leading logs)

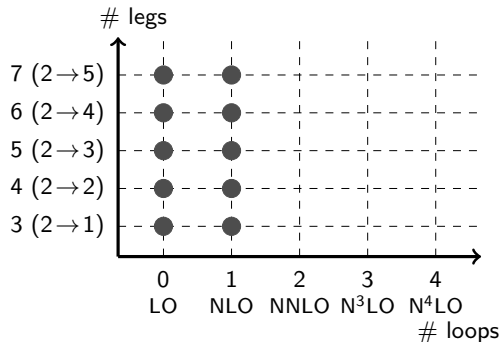
Fixed-order expansion

Two core components:

- **amplitudes calculation**: heavily connected with fundamental properties of gauge theories
- **from amplitudes to (differential) cross-sections** (“subtraction”, connected to Monte Carlo)

Status and recent progress:

- LO, NLO mostly “solved”



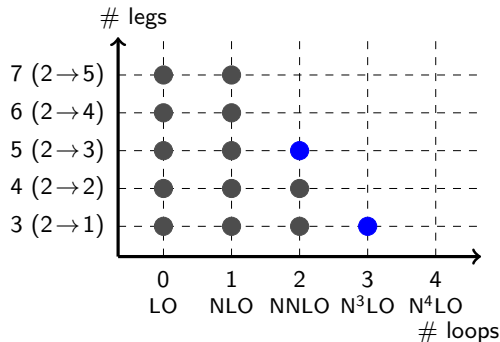
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- NNLO: $2 \rightarrow 3$ massless with full colour [2311.09870]
NNLO becomes the standard
- $N^3\text{LO}$: $2 \rightarrow 1$ known
- + mixed QCD/EW + applications to gravity [1811.10950]



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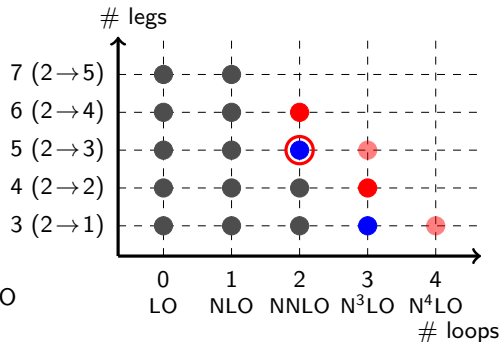
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many ongoing efforts:

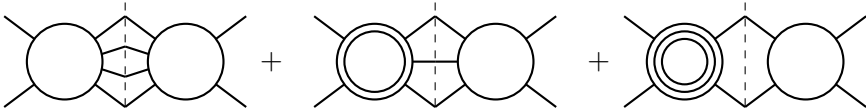
$2 \rightarrow 4$ NNLO (+ massive $2 \rightarrow 3$), $2 \rightarrow 2$ $N^3\text{LO}$, $2 \rightarrow 3$ $N^3\text{LO}$

see e.g. [2504.13011] [2412.19884] [2307.15405] [2504.06490] [2411.18697]

Timescales for extra leg/loop $\mathcal{O}(5 - 10)$ year $\Rightarrow$ future OK



Subtraction

$$\sigma_{\text{NNLO}} =$$


The equation shows three Feynman diagrams representing different orders of perturbation theory. Each diagram consists of two circular vertices connected by a central dashed line. The leftmost diagram has two real emissions (external lines) from each vertex. The middle diagram has one real emission from the left vertex and one virtual loop (represented by a double circle) on the left vertex. The rightmost diagram has two virtual loops (represented by concentric circles) on the left vertex. Plus signs are placed between the diagrams.

2 real emissions 1 real + 1 (virt) loop 2 loops (virt)

Fine cancellations between terms $\longrightarrow$ insert counterterms so that each term is now finite

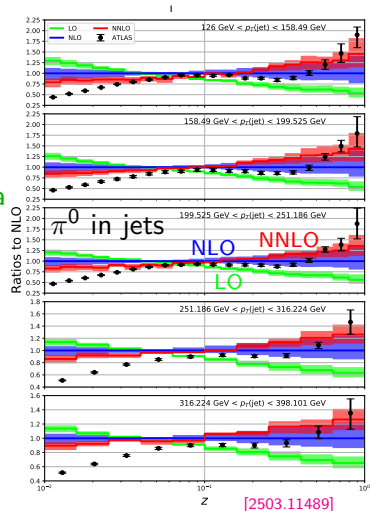
Subtraction

$$\sigma_{\text{NNLO}} = \text{2 real emissions} + \text{1 real + 1 (virt) loop}$$

Fine cancellations between terms $\longrightarrow$ insert counterterms so that

Status and recent progress:

- many methods: antenna sub [0505111], q_t subt [0703012], sector decomp [0305234], N -jettiness [1505.04794], proj2Born [1506.02660], ...
- recent progress examples: NNLOJet code public [2503.22804], $ee \rightarrow \text{jets}$ N³LO [2505.10618], Geneva V&V + j NNLO [2504.11357]



$$\sigma_{\text{NNLO}} = \text{[diagram: 2 real emissions]} + \text{[diagram: 1 real + 1 (virt) loop]} + \text{[diagram: 2 loops (virt)]}$$

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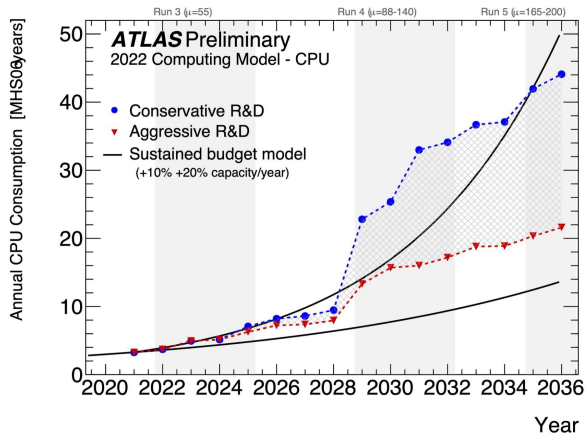
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Future challenges:

- **improvements needed as NNLO becomes standard**
- e.g. computing resources
- **theory uncertainties?**

Example: projected ATLAS CPU usage



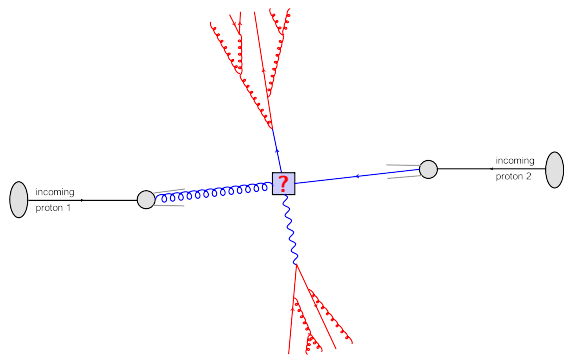
Improved simulations would
be very much appreciated

This covers many aspects on top of
HPC/GPU/...:

- amplitudes/integrals evaluation
- subtraction schemes
- matching (see later)
- ...

[ATLAS Software and Computing HL-LHC Roadmap, 2022]

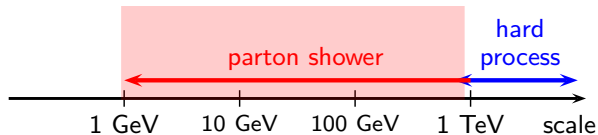
Theorist view of a collision: focus on filling the scale gap



**High-energy collision
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perturbative
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Approaches to connect widely disparate scales

All-order resummations: $N^k\text{LL}$ resums $(\alpha_s L)^n \alpha_s^{k-1}$ for all n (limit $\alpha_s L \sim 1$, $\alpha_s \ll 1$)

Option 1: analytic

High-accuracy but usually done **observable per observable**. Two main approaches:

- 1 **SCET** (effective theory): routinely NNLL; some observables (almost) up to $N^4\text{LL}$
Recent progress: super-leading logs [2107.01212], heavy quarks [2412.06881], energy correlators [2506.09119], links with TMDs and NRQCD, ...
Looking forwards: core (QFT-based) analytic approach to resummation with many applications and clear path towards precision
- 2 **“direct QCD”**: NNLL frequent as well (automatised for simple processes), $N^3\text{LL}$ sometimes

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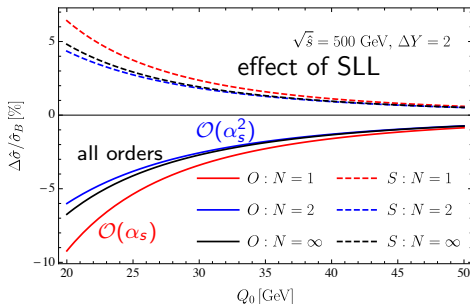
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Option 2: parton shower (core of general-purpose Monte Carlo generators)

Full kinematics, and (roughly) any observable but **limited in accuracy (LL until ~ 2019)**
Recent progress: **NLL revolution** in the past ~ 5 years, starting to get **NNLL** (+ heavy progress on colour)
Looking forwards: will hopefully become competitive in the precision business

example: super-leading logs

- Nasty logs discovered in 2006 [0604094]
non-global, subleading- N_c , pp only, start at $\alpha_s^4 L^5$
- First (SCET) resum in 2021 [2107.01212]



Showers 2019-2024: many now achieve NLL

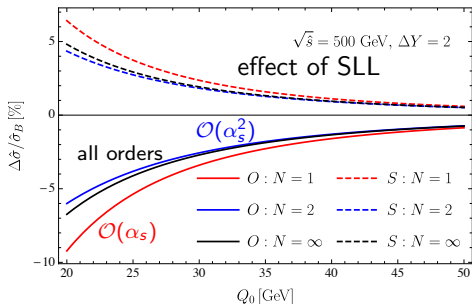
- PanScales [2002.11114] [2011.10054] [2103.16526]
[2111.01161] [2205.02237] [2207.09467] [2305.08645] [2312.13275]
- Deductor [2011.04773] [2011.04777]
- CVolver [1905.08686] [2003.06400] [2011.15087]
- Alaric [2208.06057] [2307.00728] [2404.14360]
- Apollo [2403.19452]

NLL is becoming the new standard

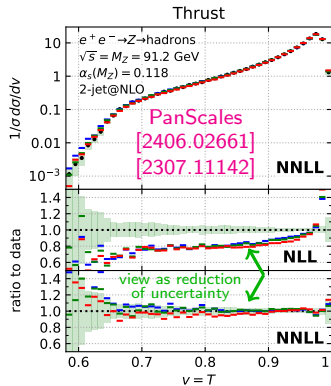
Examples of recent progress

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Showers 2024-now: progress towards NNLL



so far only ee,
large- N_c and
not all obs

but promising
for precise
all-purpose
MC generators
in coming years

Basic concepts:

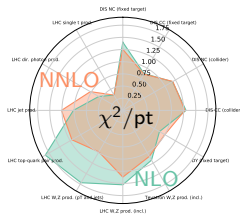
- PDFs appear “core factorisation formula”
- Technically, resum collinear $\log(Q/m_p)$
- Fundamental QCD factorisation theorem:
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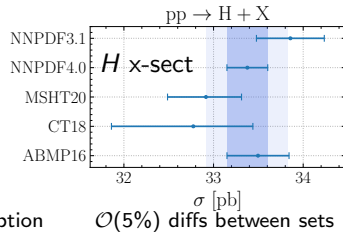
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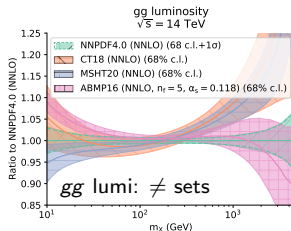
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 $([CTEQ], [MSHT], [NNPDF], \dots)$
- approximate N^3LO start to appear
 Needed for 1%-level (still differences between sets)



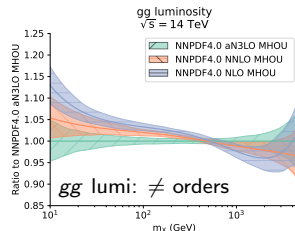
NNLO improves data description



$\mathcal{O}(5\%)$ diffs between sets



$\mathcal{O}(5 - 10\%)$ uncert



sizeable aN^3LO effects

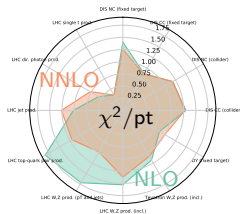
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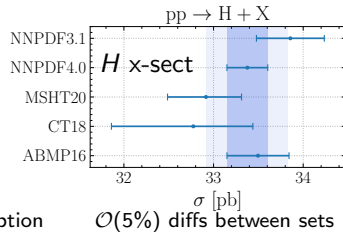
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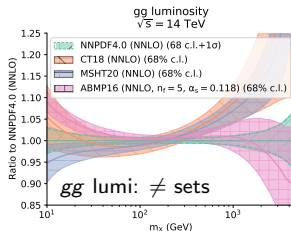
Looking forwards: PDFs will improve!
 e.g. need more N^3LO x-sections (only DIS now)
 Recall: interplay w data through fit!



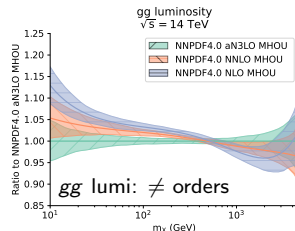
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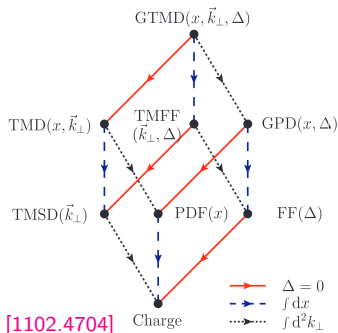


$\mathcal{O}(5 - 10\%)$ uncert



sizeable aN^3LO effects

**Fundamental question:
what is the partonic
contents of a proton?**



- Additional degrees of freedom
 - transverse momentum, $\vec{k}_t$
 - momentum transfer Δ
 - + potential polarisation info
- Gaining in precision: e.g. TMDs at N⁴LL [2305.07473]
- Not only for the proton:
 - nuclear PDFs relevant for heavy-ion collisions
 - other hadrons (like pions)
- Links to lattice determinations: e.g. [2412.01750]
- Links to small-x/saturation physics: e.g. [2503.16162]
- Relevance for pheno: DY, SIDIS, Diffractive DIS
Looking forwards to the EIC!

interesting at many levels

Pheno interlude: matching fixed-order and parton shower

Idea:

Build a prediction that works both in the fixed-order and resummation regimes

e.g. NNLO+NNLL p_{tZ} spectrum would have NNLO for $p_{tZ} \gtrsim M_Z$ and NNLL for $p_{tZ} \ll M_Z$

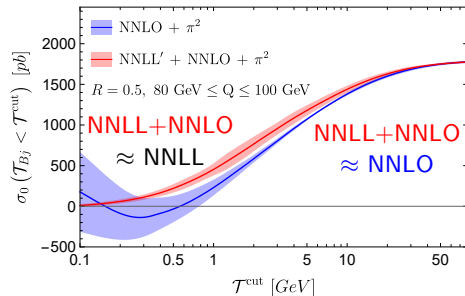
Analytic viewpoint

almost systematic for pheno predictions

Right: Drell-Yan with veto on additional jets [2504.06353]

Several other (recent) examples:

- Soft log resummations in VH , $t\bar{t}$, $t\bar{t}H$ or $t\bar{t}t\bar{t}$
[2502.20331] [2503.18713] [2503.15043] [2505.10381]
- DIS Thrust [2504.05234]
- Small- R jet resummations [2503.21866] [2402.05170]
- TMDs for J/ψ [2504.19617]



Future: multi-scale processes?

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In Monte Carlo generators

NLO+PS matching is standard

[POWHEG] [aMCNLO] [MePsNLO]

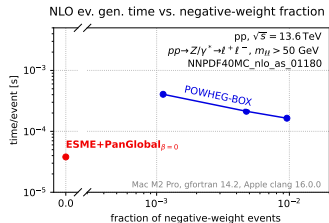
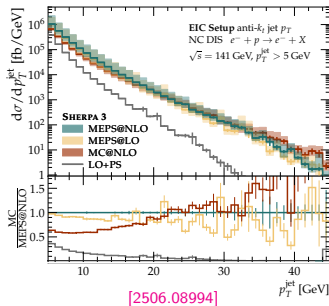
Progressively getting NNLO+PS

e.g. MiNNLO [1908.06987] [2108.05337] [2112.12135]

Looking forwards:

- interplay with shower accuracy
- avoiding negative weights
- CPU budget

NLO+PS matching in DIS



NLO+NLL with positive weights

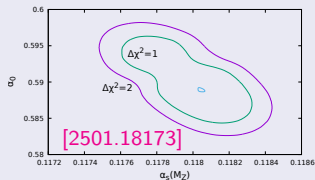
[2504.05377]

Back to basics: how strong is the strong interaction?

fundamental param & impacts many things (e.g. if we are stable)

ee event shapes

3-jet non-pert corrections



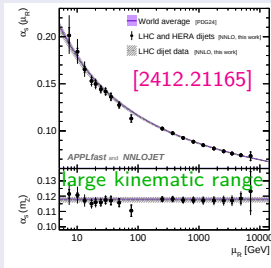
$$\alpha_s(M_Z) = 0.1181^{+0.0018}_{-0.0022}$$

NNLO+N³LL thrust: 0.1181 ± 0.0018

[2502.01570]

Heavy jet mass: $0.1145^{+0.0021}_{-0.0019}$ [2502.12253]

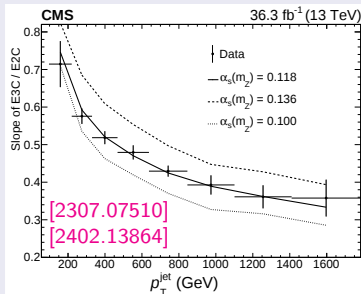
LHC dijets & PDFs



$$\alpha_s(M_Z) = 0.1178 \pm 0.0022$$

aN³LO PDFs: $0.1194^{+0.0007}_{-0.0014}$ [2506.13871]

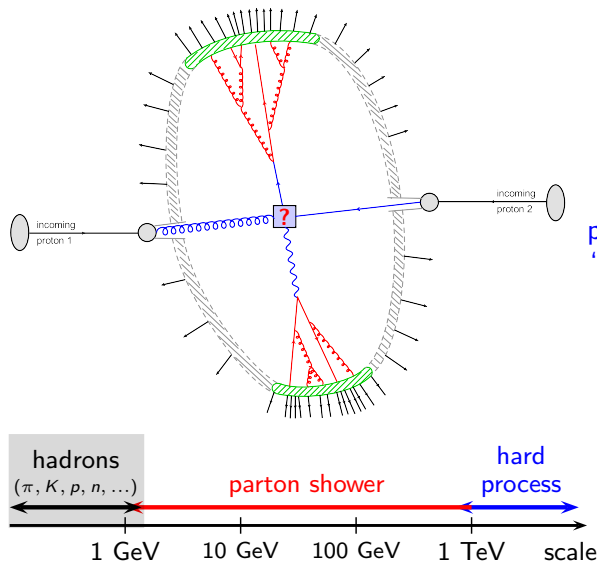
EEC (jet substructure)



$$\alpha_s(M_Z) = 0.1229^{+0.0040}_{-0.0050}$$

Latest lattice result: $\alpha_s(M_Z) = 0.11873 \pm 0.00056$ [2501.06633]

Theorist view of a collision: focus on hadronic physics



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non-pert.
“modelled”

various
approaches

- A hard process
- Parton shower (initial and final-state)
- Hadronisation
- Multi-parton interactions
- Hadron decays

This is where QCD is getting the most complicated! So I will only give a few pointers...

Many systems

- Hadrons/mesons with heavy quarks
- Tetraquarks
- Pentaquarks
- Even hexa/octaquarks

Many questions

- spectrum
- nature
- (rare) decays
- structure/fragmentation

Many approaches

- B physics tentatively perturbative
- light-cone wave-functions
- NRQCD
- EFTs (chiral PT, HQET, SCET, ...)
- sumrules
- potential models
- lattice QCD

Experimental relevance

LHC, Belle, BESIII, ...

Modelling in MC

Trying to better understand/constraint the Lund string and cluster hadronisation models

Large activity
(~300 papers from mid-Jan to mid-June)

data and lots of unknown
⇒ **work for the future**

**QCD is a fundamental component of the standard model
at the core of the (past,) current (and future) particle-physics program**

Tremendous progress

After 50 years: we have reached a phenomenal degree of understanding of the theory:

- structure and properties of hadrons
- control over the perturbative properties (fixed and all-order)
- development of tools (Monte-Carlo generators, jets, AI, ...)

Exciting challenges ahead

Challenges & bright future await:

- more fundamental aspects to be learned
- connection with rich pheno/exp program

Thank you!

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