

# High-K ground states and isomers in superheavy nuclei

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- A. Motivation – how long-lived could be high-K (near) ground states and isomers in SHN?
- B. Method
- C. Candidates for high-K g.s. in (mostly) odd-odd nuclei
- D. Candidates for 3qp K-isomers in odd-even  $Z=101-111$ ,  $N=142-166$
- E. Candidates for 3qp K-isomers in even-odd  $Z=100-112$ ,  $N=141-167$

- K-isomers provide some information on the level scheme /deformation of nuclei.
- There is a hope that **some SH K-isomers could be more stable than the g.s.**, especially if their structure, shape etc. would make fission and alpha decay less probable, e.g. F.R.Xu at al. Phys. Rev. Lett. 92 (2004) 252501, and others.

Heavy isomers living longer than the g.s. :

	g.s.			is.		
$^{256}\text{Es}$	$(1^+, 0^-)$	25.4 m	$\beta^-$	$(8^+)$	7.6 h	$\beta^-$
$^{250}\text{No}$	$0^+$	3.8 $\mu\text{s}$	sf	$(6^+)$	35 $\mu\text{s}$	IT
$^{254}\text{Rf}$	$0^+$	23.2 $\mu\text{s}$	sf	$(16^+)$	247 $\mu\text{s}$	IT
$^{270}\text{Ds}$	$0^+$	100 $\mu\text{s}$	$\alpha$	$(10^-)$	6 ms	$\alpha/\text{IT}$

Microscopic-macroscopic method with a possibility of many various deformations

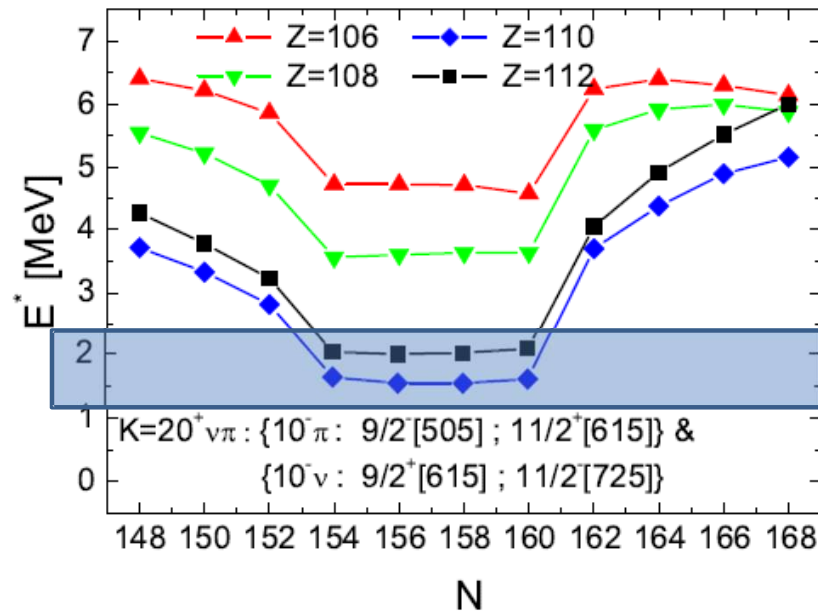
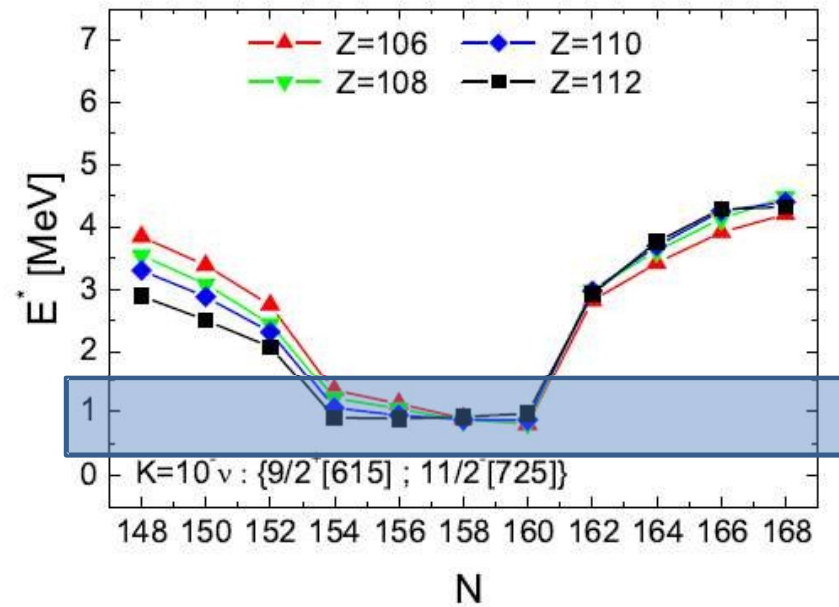
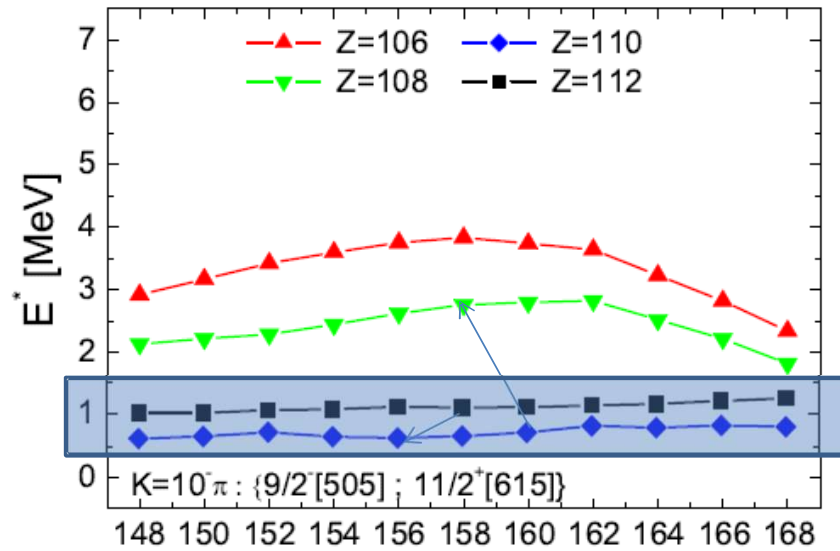
252)

## 2qp & 4qp high-K isomers in even-even SHN

Stability of high-spin isomers against alpha decay is determined mainly by three factors:

- the overlap between final and initial states wherein a similar structure of states favors the transition between them;
- change in angular momentum - a significant change is associated with a large centrifugal barrier which blocks a decay;
- transition energy, which we shall also call  $Q$  for a given decay, that follows from the  $Q$  value for the g.s.->g.s. transition and the difference in the excitation energies of the initial and final state in, respectively, mother and daughter nucleus.





S. Hofmann et al., "The new isotope  $^{270}_{110}$   
 and its decay products  $^{266}_{110}\text{Hs}$  and  $^{262}_{110}\text{Sg}$ ". *Eur.*  
*Phys. J. A.* **10** (1): 5–10, 2001

$^{207}\text{Pb}(^{64}\text{Ni},n)^{270}\text{Ds}$   
 $\sigma = (13 \pm 5) \text{ pb}$

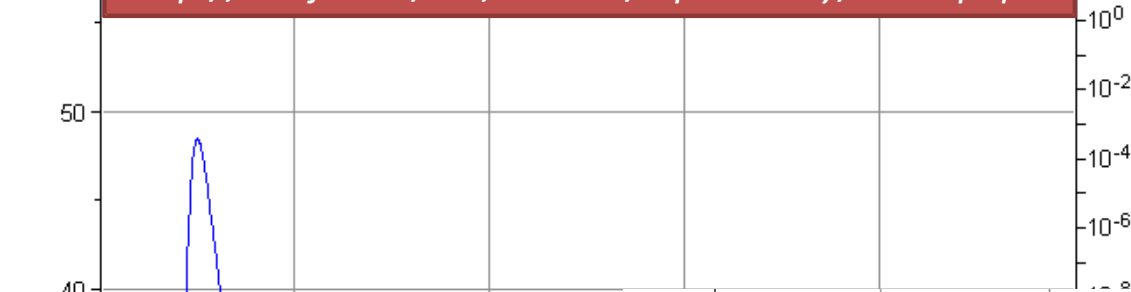
$$HF = \left[ T_{1/2}^{a \rightarrow b} / T_{1/2}^{gs \rightarrow gs} \right]$$

a – initial state; b - final state

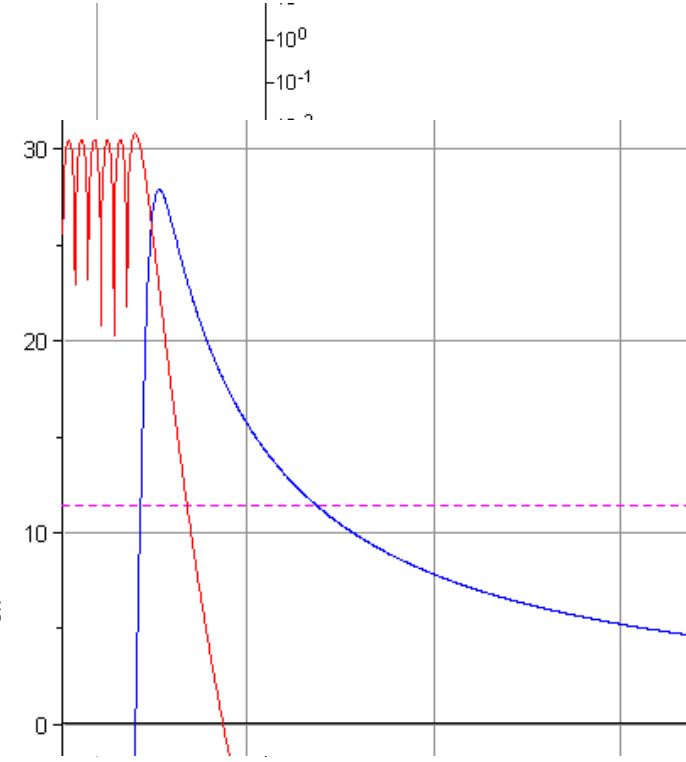
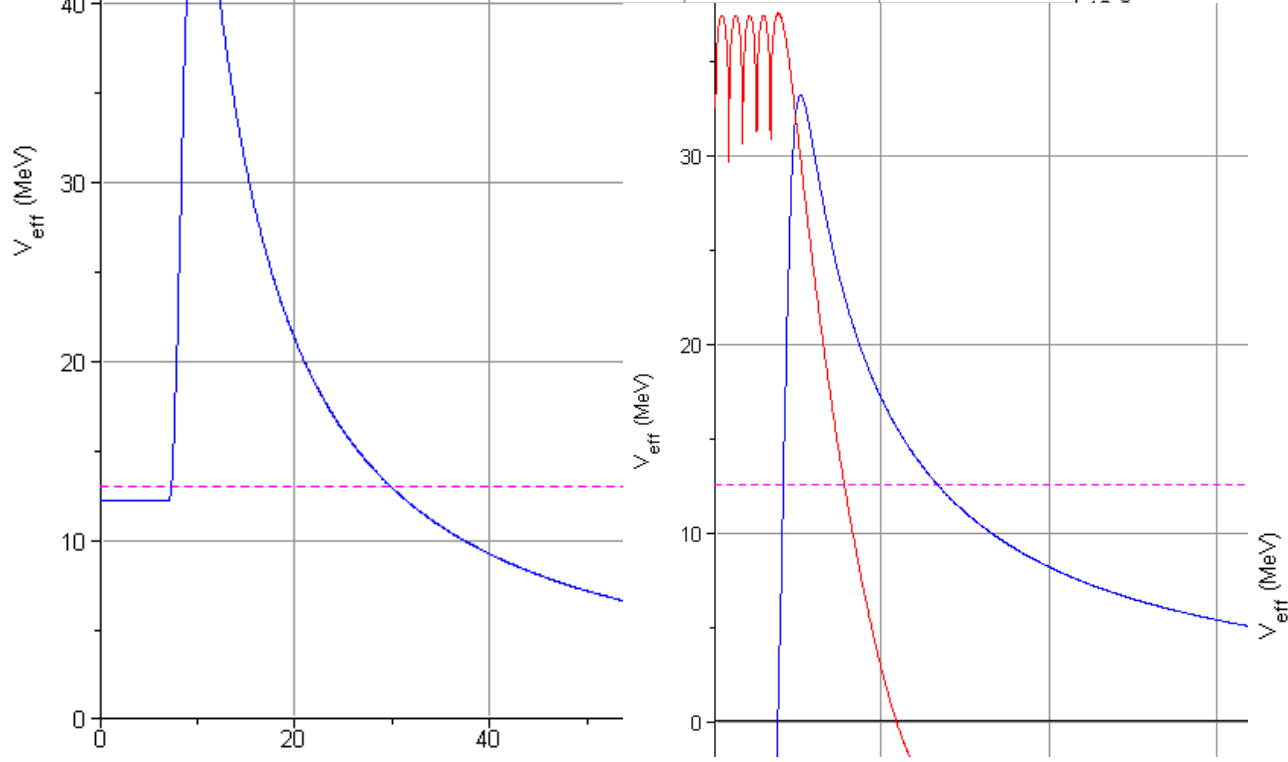
$$HF = \overset{\text{(structural)}}{HF_S} * \overset{\text{(tunneling)}}{HF_\Gamma}$$

$$HF_\Gamma \simeq \overset{\text{(difference in Q)}}{HF_Q} * \overset{\text{(centrifugal)}}{HF_L}$$

<http://nrv.jinr.ru/nrv/webnrv/alphadecay/index.php>



$$E_L = \frac{L(L + 1)}{2mr^2}$$



$\Delta L[\hbar]$   $20\hbar$   
Turning Points [fm]: 7.27; 29.70

$10\hbar$   
8.21; 27.15

$0\hbar$   
8.45; 27.33

$$K=20+ \{KN=10- : 9/2+[615] \& 11/2-[725]\}$$

$$\& \quad \{KP=10- : 9/2-[505] \& 11/2+[615]\}$$

Crucial is the hindrance in the fastest channel, between two identical configurations. This is especially true for four quasi-particle states!

significant increase in the centrifugal barrier.  
With  $L = \Delta K = 20h$

A structural hindrance for 4 q.p. isomers must be also substantial. If one assumes that it is a product of the hindrance factors for protons and neutrons

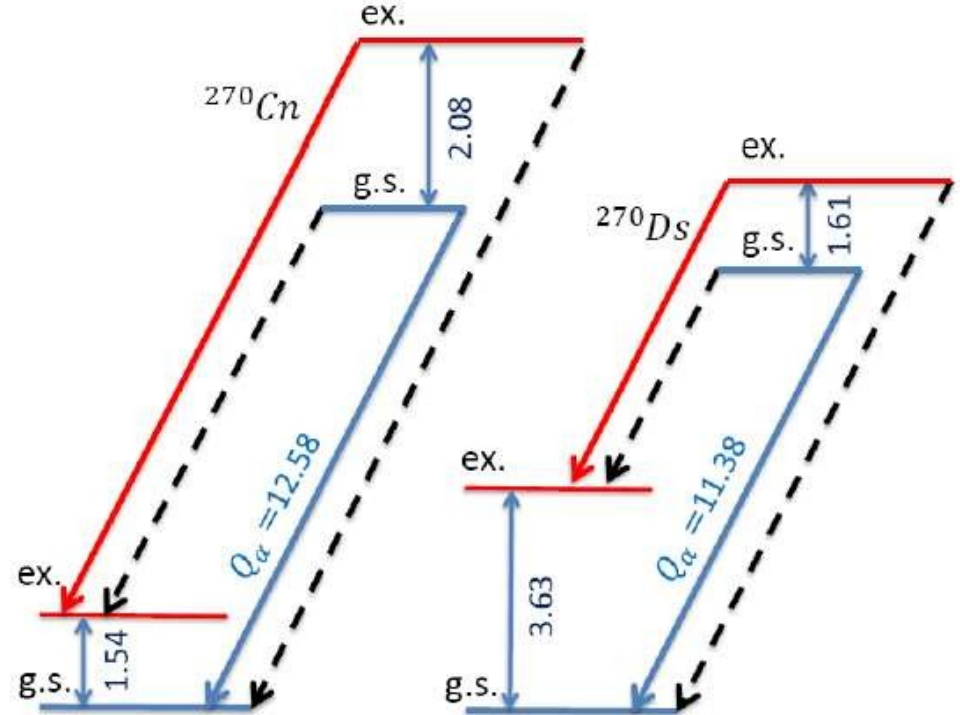
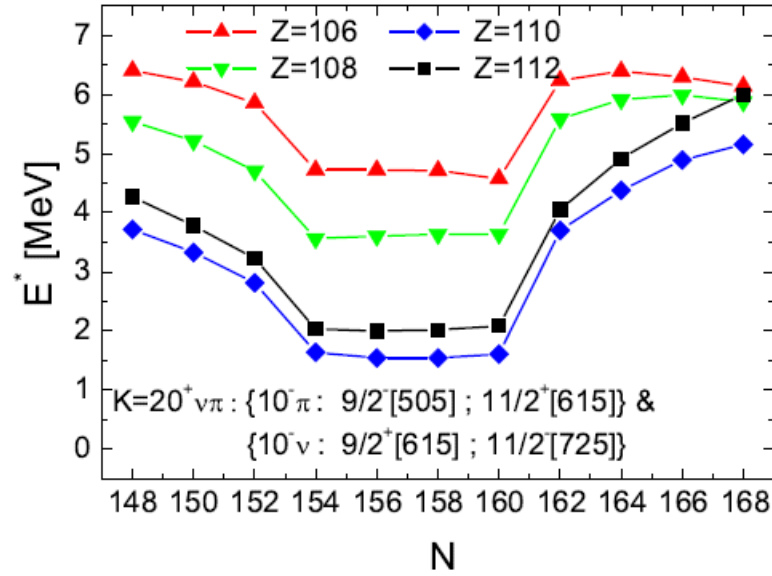
$$HF_L \simeq 10^{12}$$

$$HF_S = 10^9$$

Taken together, this leads to the conclusion that transitions  $ex \rightarrow gs$  or  $gs \rightarrow ex$  are excluded.

TABLE II:  $Q_\alpha$ -values (in MeV) and hindrance factors corresponding to the change  $\Delta Q_\alpha = Q_\alpha^{ex \rightarrow ex} - Q_\alpha^{gs \rightarrow gs}$  for the  $K^\pi = 20^+ \nu\pi : (10^- \nu : \{(9/2^+ [615], 11/2^- [725]\} \otimes 10^- \pi : \{(9/2^- [505], 11/2^+ [615]\})$  configuration in  $^{270}\text{Cn}$  and  $^{270}\text{Ds}$ , calculated using: WKB method (WKB) [34], the formula of Royer [36] (ROY), and the Viola-Seaborg-type formula by Parkhomenko and Sobiczewski (PS) [39].

	$Q_\alpha$	$\Delta Q_\alpha$	$\text{Log}^{WKB} [HF]$	$\text{Log}^{ROY} [HF]$	$\text{Log}^{PS} [HF]$
$^{270}\text{Cn}$	13.06	0.48	-0.87	-0.92	-0.88
$^{270}\text{Ds}$	9.36	-2.02	6.75	5.42	5.13



3qp K - isomers in odd-even Md – Rg nuclei:

(P. Jachimowicz, M. Kowal, J. Skalski, [arXiv:2308.02893](https://arxiv.org/abs/2308.02893))

They are either 1p2n (>2500 conf.) or 3p (>500 conf.).

energy minimization

$$R(\vartheta, \varphi) = R_0 \{1 + \beta_{20} Y_{20} + \cancel{\beta_{30}} Y_{30} + \beta_{40} Y_{40} + \\ + \cancel{\beta_{50}} Y_{50} + \beta_{60} Y_{60} + \cancel{\beta_{70}} Y_{70} + \beta_{80} Y_{80}\}.$$

Four-dimensional minimization

Pairing was treated by three methods: BCS with blocking, in the quasiparticle scheme (sum of BCS qp energies added to the energy of the core) and with the particle number projection (PNP) for the lowest configurations.

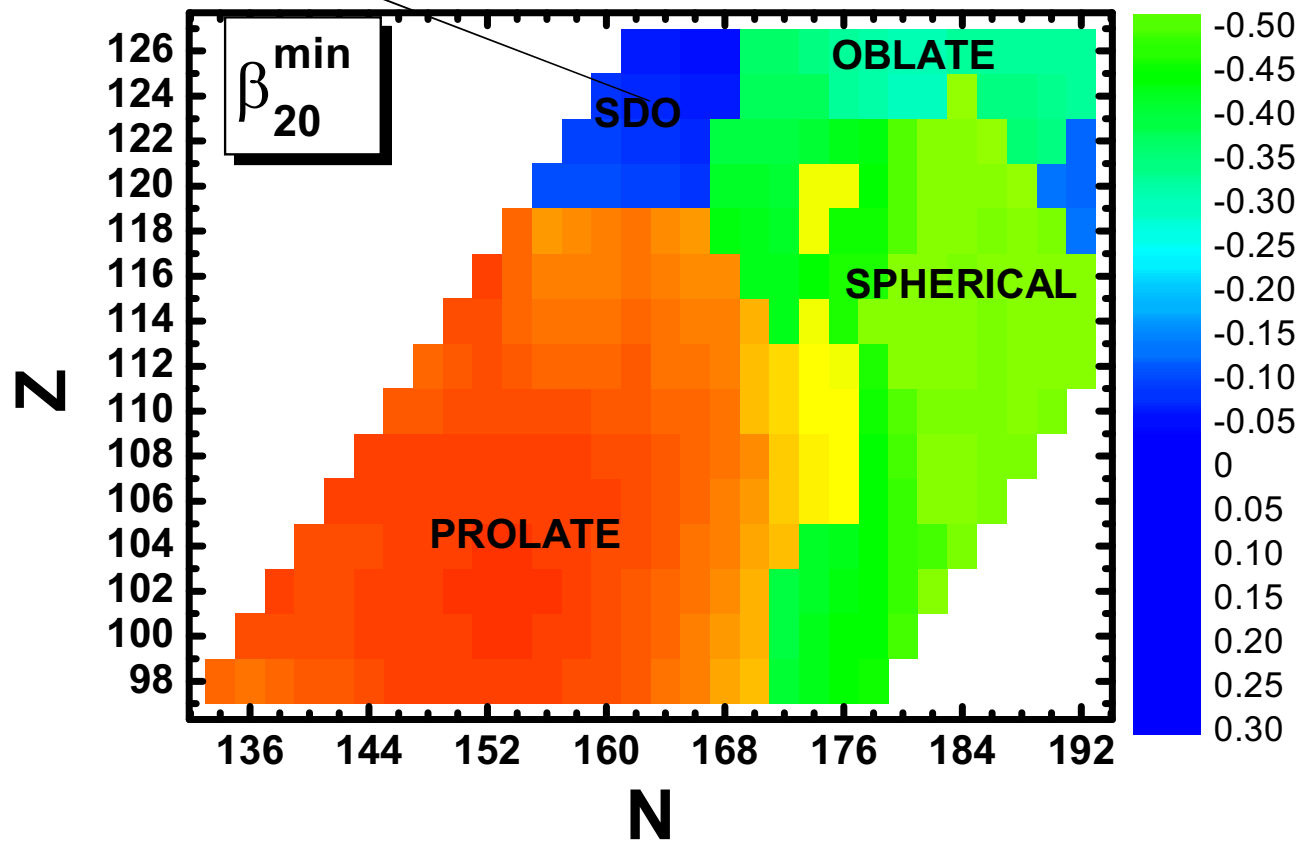
# Ground state shapes

*SDO* :

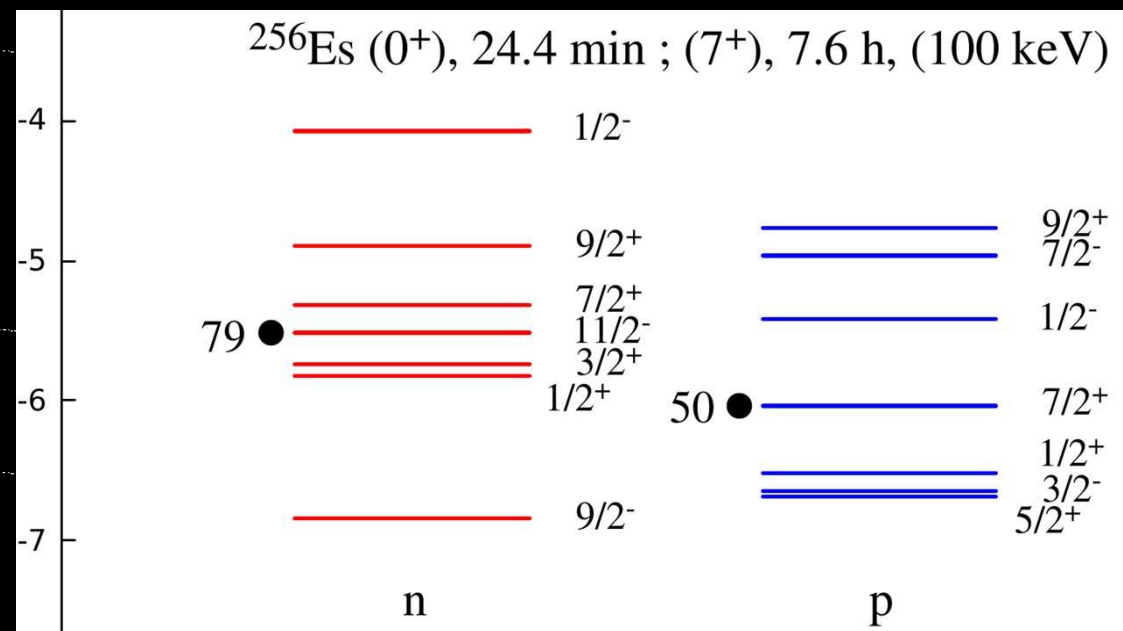
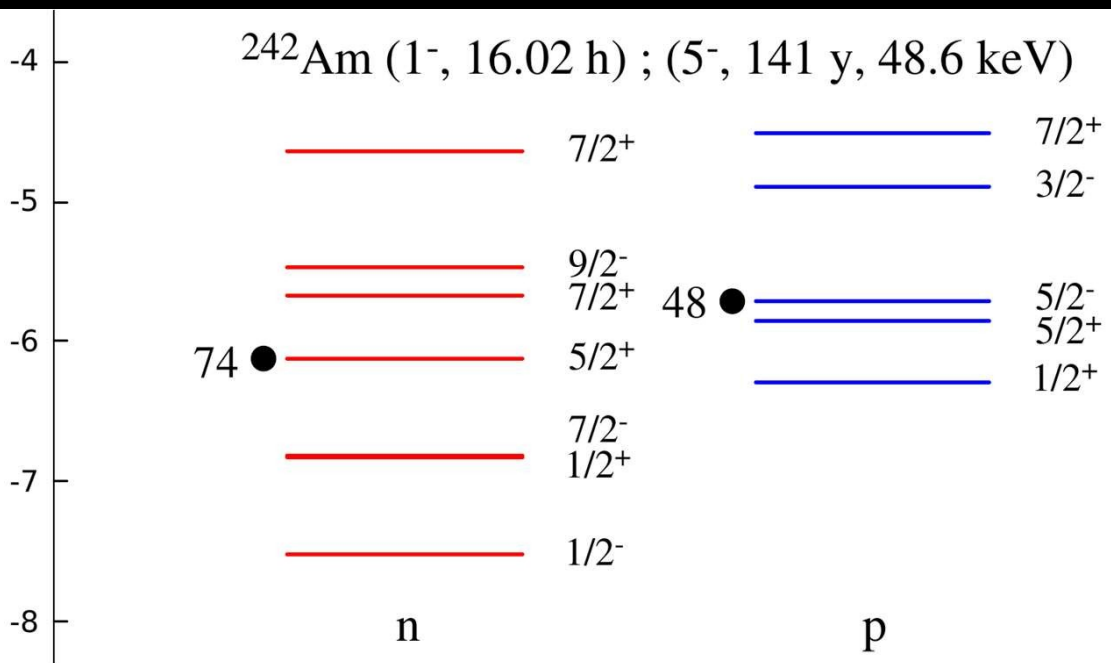
$$\beta_{20} \approx -0.5$$

$$\text{Axis.ratio} \approx \frac{3}{2}$$

Micro-macro results; mostly four - dimensional minimization

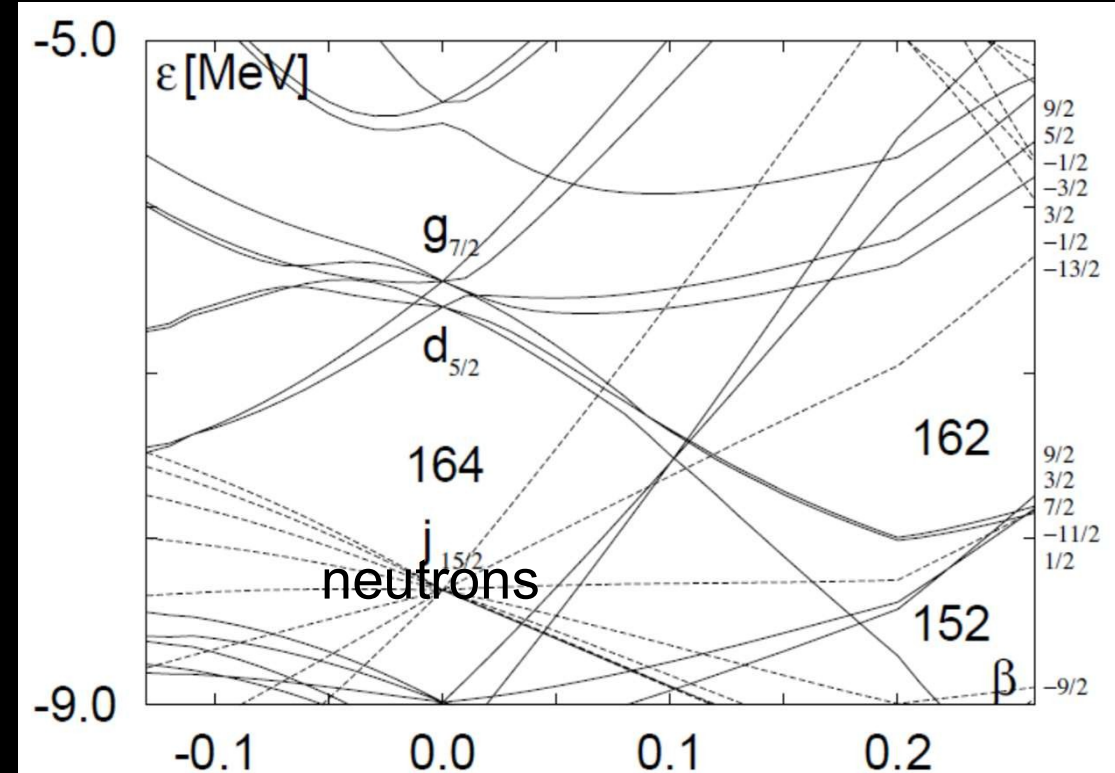
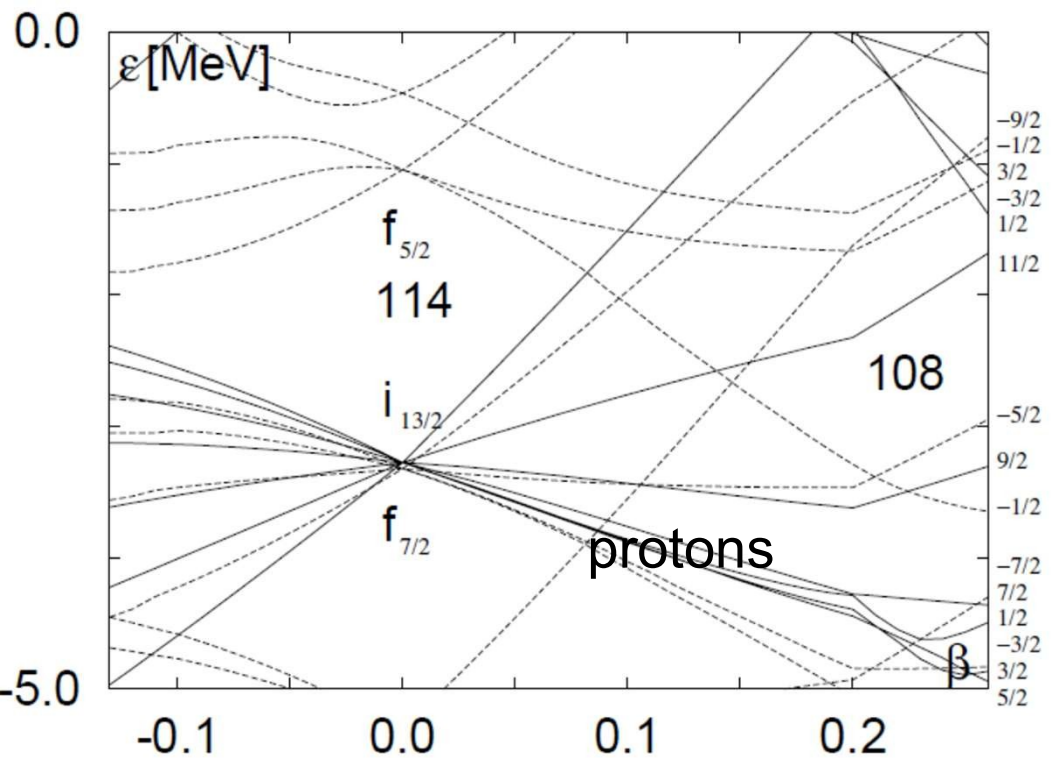


In contrast to many Skyrme forces, Woods-Saxon micro-macro model gives lower barriers and mostly oblate ground states for  $Z \geq 124, 126$  (no magic gap for 126 protons).





## High-K g. s. in odd and odd-odd SHN



The effect of intruder states lying close to the Fermi level is most apparent in heavier nuclei

101 151 1/2- 9/2- 5+  
157 " 11/2- 6+

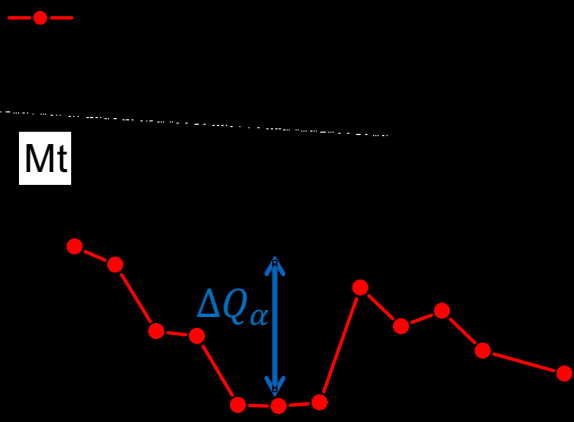
103 149 7/2- 7/2+ 7-  
151 " 9/2- 8+  
157 " 11/2- 9+

105 151 9/2+ 9/2- 9-  
155 " 3/2+ 6+  
157 " 11/2- 10-

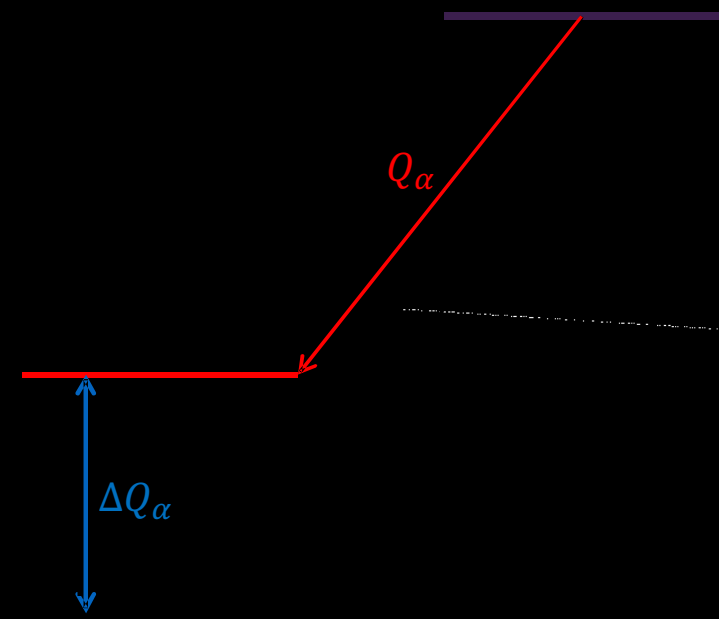
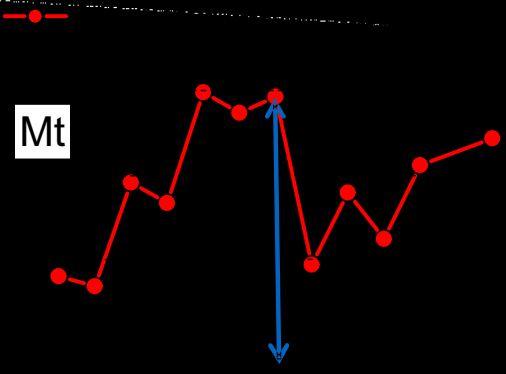
107 157 5/2- 11/2- 8+  
159 " 7/2+ 6-  
161 " 9/2+ 7-  
163 " 13/2- 9+

109 157 11/2+ 3/2+ 7+  
159 " 9/2+ 10+  
161 " 9/2+ 10+  
163 " 13/2- 12-  
165 " 3/2+ 7+  
167 " 5/2+ 8+  
169 " 9/2+ 10+

111 163 3/2- 13/2- 8+  
169 9/2- 5/2+ 8+  
157 " 11/2- 7+



A particular situation occurs above double closed subshells  $N = 162$  and  $Z = 108$  where two intruder orbitals, neutron  $13/2^-$  from  $j_{15/2}$  and proton  $11/2^+$  from  $i_{13/2}$  spherical subshells, are predicted. These orbitals combine to the  $12^-$  g.s. in  $Z = 109, N = 163$ ,

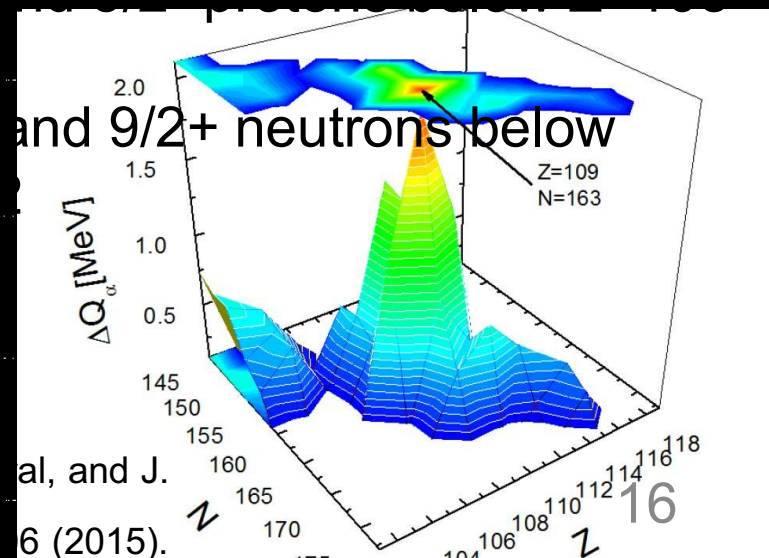


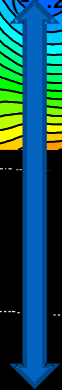
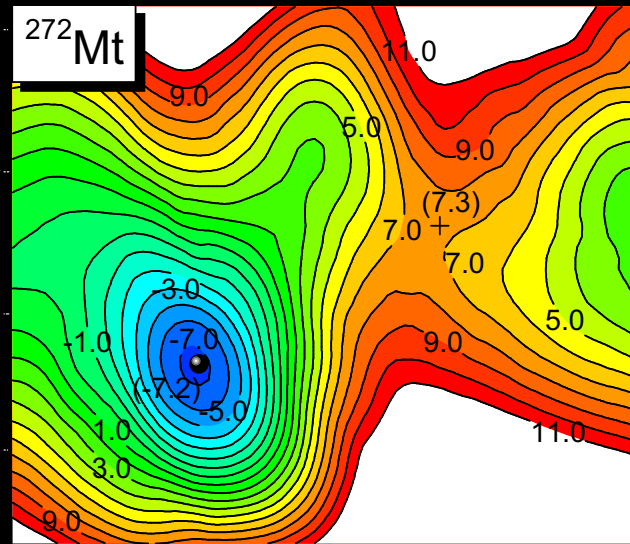
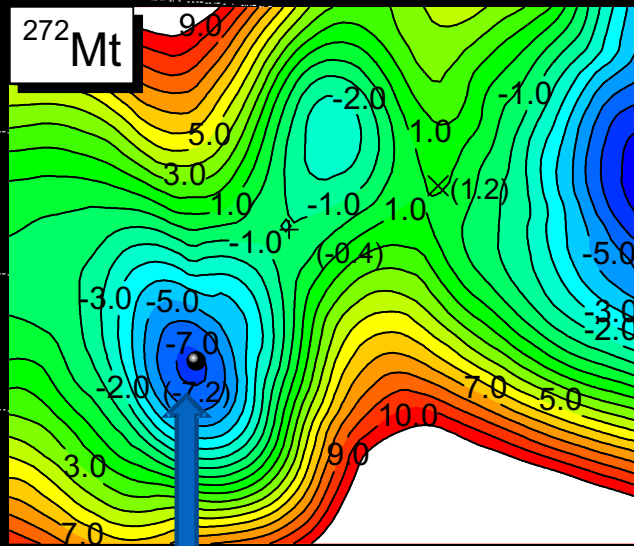
Z	N	$\Omega^p$	$\Omega^n$	$K^\pi$	$\Delta Q_\alpha$
111	169	9/2 <sup>-</sup>	5/2 <sup>+</sup>	7 <sup>-</sup>	0.74
111	163	3/2 <sup>-</sup>	13/2 <sup>-</sup>	8 <sup>+</sup>	1.31
111	161	3/2 <sup>-</sup>	7/2 <sup>+</sup>	7/2 <sup>-</sup>	0.52
110	163		13/2 <sup>-</sup>	13/2 <sup>-</sup>	0.97
109	169	11/2 <sup>+</sup>	9/2 <sup>+</sup>	10 <sup>+</sup>	0.51
109	167	11/2 <sup>+</sup>	5/2 <sup>+</sup>	8 <sup>+</sup>	0.71
109	166	11/2 <sup>+</sup>		11/2 <sup>+</sup>	0.88
109	165	11/2 <sup>+</sup>	3/2 <sup>+</sup>	7 <sup>+</sup>	1.38
109	164	11/2 <sup>+</sup>		11/2 <sup>+</sup>	1.13
<u>109</u>	<u>163</u>	<u>11/2<sup>+</sup></u>	<u>13/2<sup>-</sup></u>	<u>12<sup>-</sup></u>	<u>1.99</u>
109	162	11/2 <sup>+</sup>		11/2 <sup>+</sup>	1.27
109	161	11/2 <sup>+</sup>	9/2 <sup>+</sup>	10 <sup>+</sup>	1.32
109	160	11/2 <sup>+</sup>		11/2 <sup>+</sup>	1.37
109	159	11/2 <sup>+</sup>	9/2 <sup>+</sup>	10 <sup>+</sup>	1.56
109	158	11/2 <sup>+</sup>		11/2 <sup>+</sup>	1.39
109	157	11/2 <sup>+</sup>	3/2 <sup>+</sup>	7 <sup>+</sup>	1.41
108	163		13/2 <sup>-</sup>	13/2 <sup>-</sup>	1.00
107	163	5/2 <sup>-</sup>	13/2 <sup>-</sup>	9 <sup>+</sup>	1.17
107	157	5/2 <sup>-</sup>	11/2 <sup>-</sup>	8 <sup>+</sup>	0.57
106	163		13/2 <sup>-</sup>	13/2 <sup>-</sup>	0.96
105	153	9/2 <sup>+</sup>	1/2 <sup>+</sup>	5 <sup>+</sup>	0.97
103	157	7/2 <sup>-</sup>	11/2 <sup>-</sup>	9 <sup>+</sup>	0.52
103	154	7/2 <sup>-</sup>		7/2 <sup>-</sup>	0.54
103	153	7/2 <sup>-</sup>	1/2 <sup>+</sup>	4 <sup>-</sup>	1.45
103	151	7/2 <sup>-</sup>	9/2 <sup>-</sup>	8 <sup>+</sup>	0.58
103	149	7/2 <sup>-</sup>	7/2 <sup>+</sup>	7 <sup>-</sup>	0.63
101	151	1/2 <sup>-</sup>	9/2 <sup>-</sup>	5 <sup>+</sup>	0.68
101	149	1/2 <sup>-</sup>	7/2 <sup>+</sup>	4 <sup>-</sup>	0.92

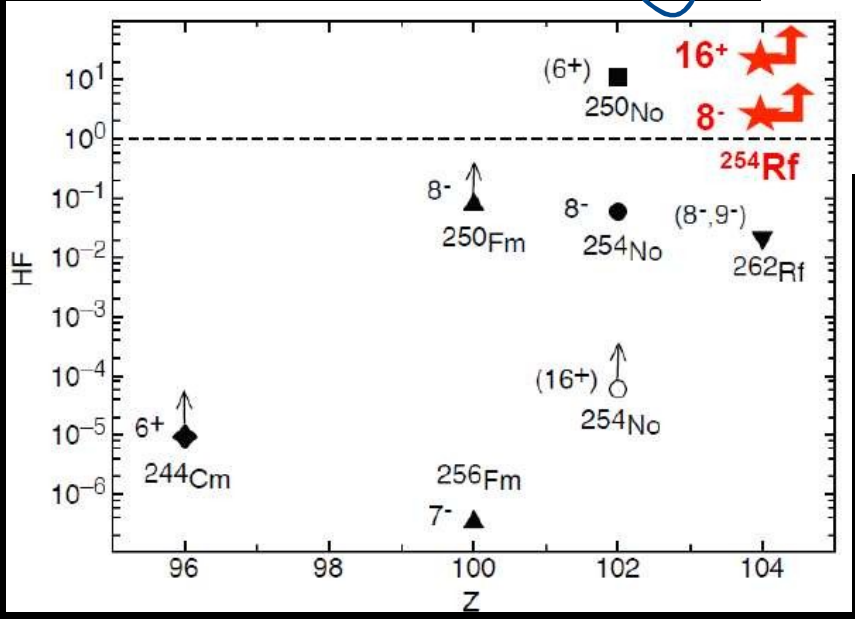
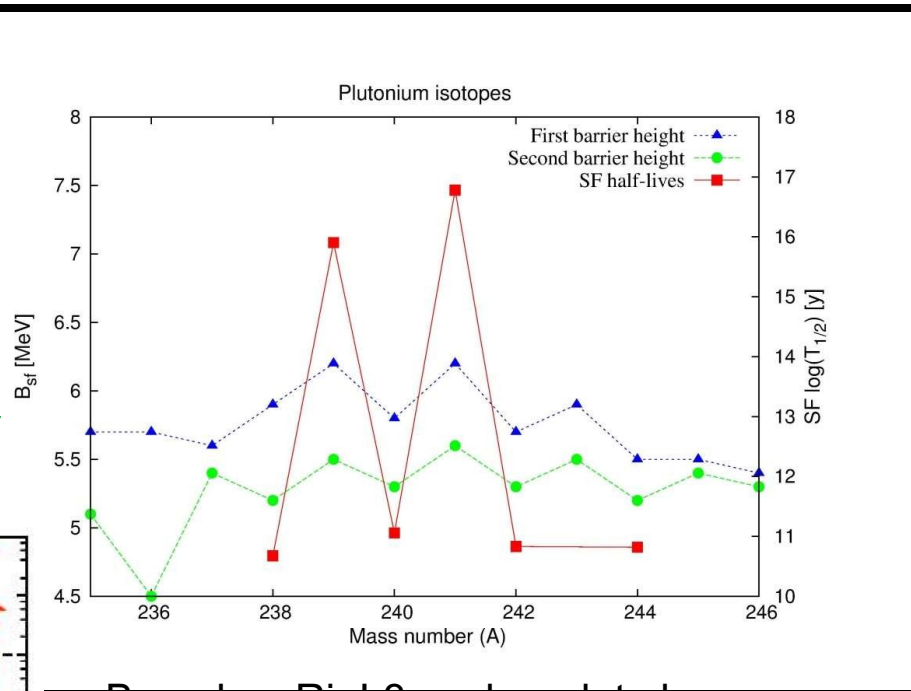
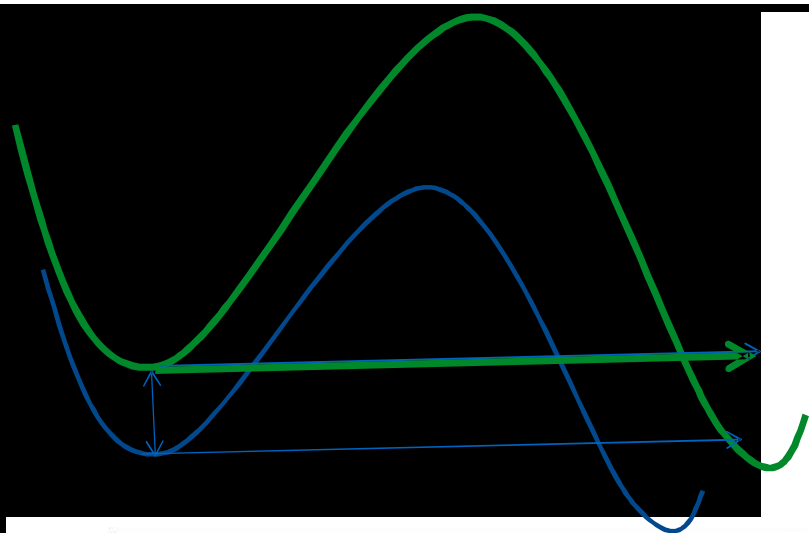
High-K states: a chance for longer half-lives.

Candidates for high-K Ground states.

in odd or odd-odd SHN in the W-S model



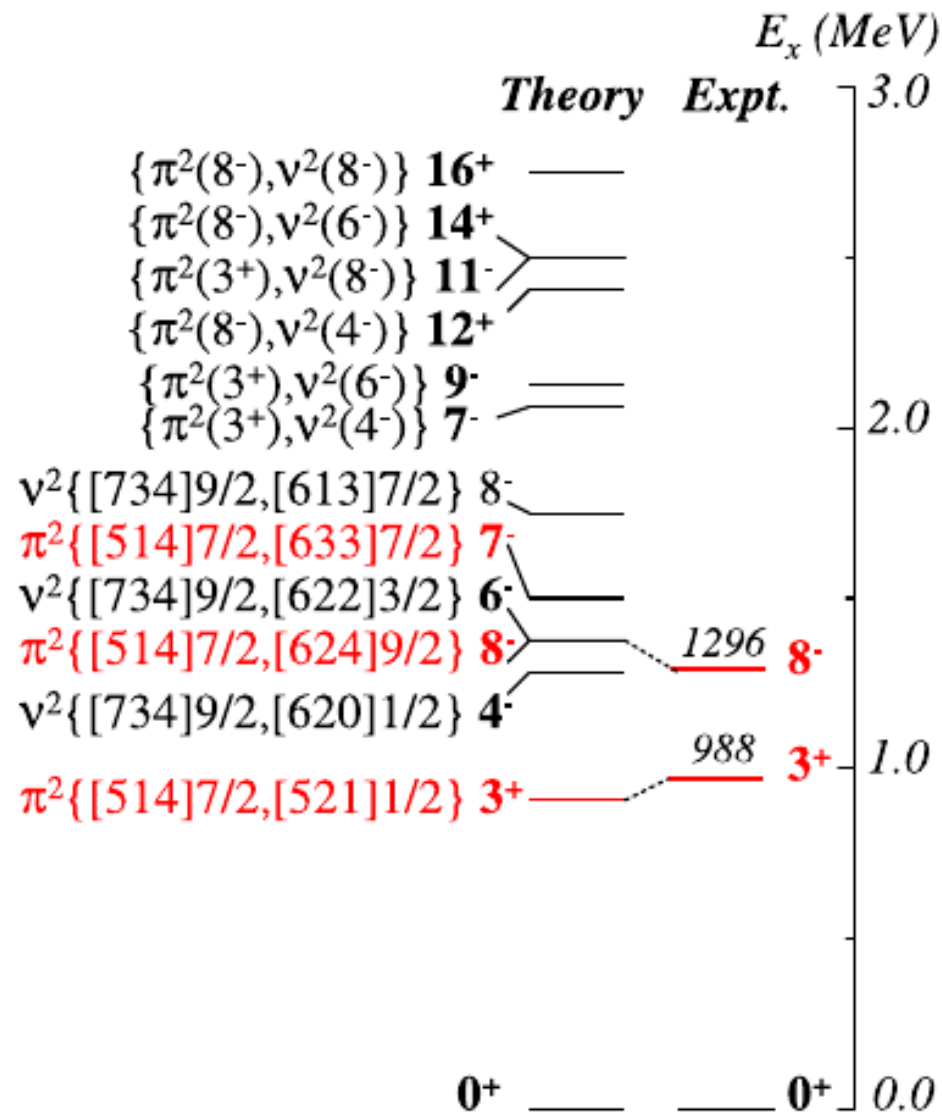




<https://www-nds.iaea.org/RIPL-3/>



F. G. Kondev, G. D. Dracoulis, T. Kibedi, *Atomic Data and Nuclear Data Tables*, 103-104, (2015).

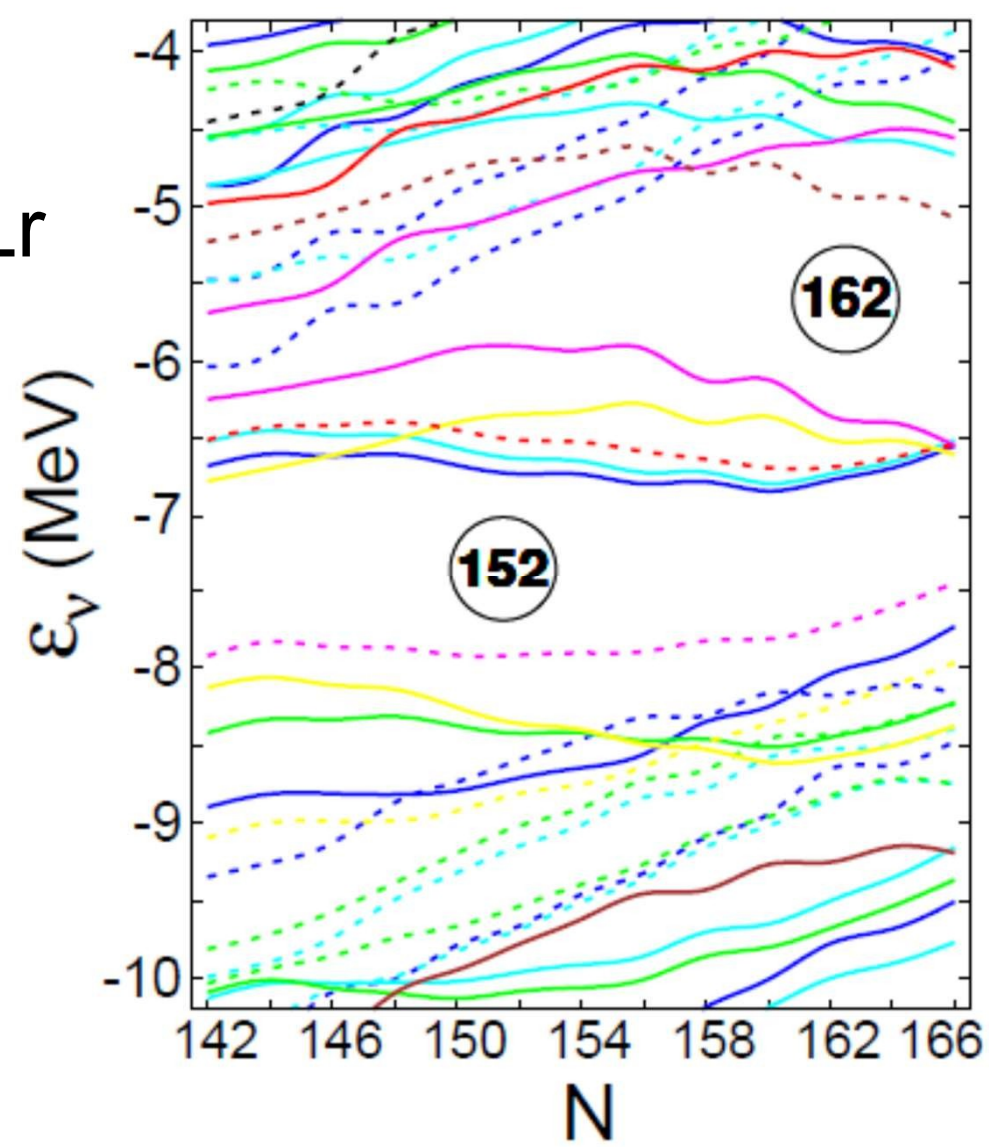
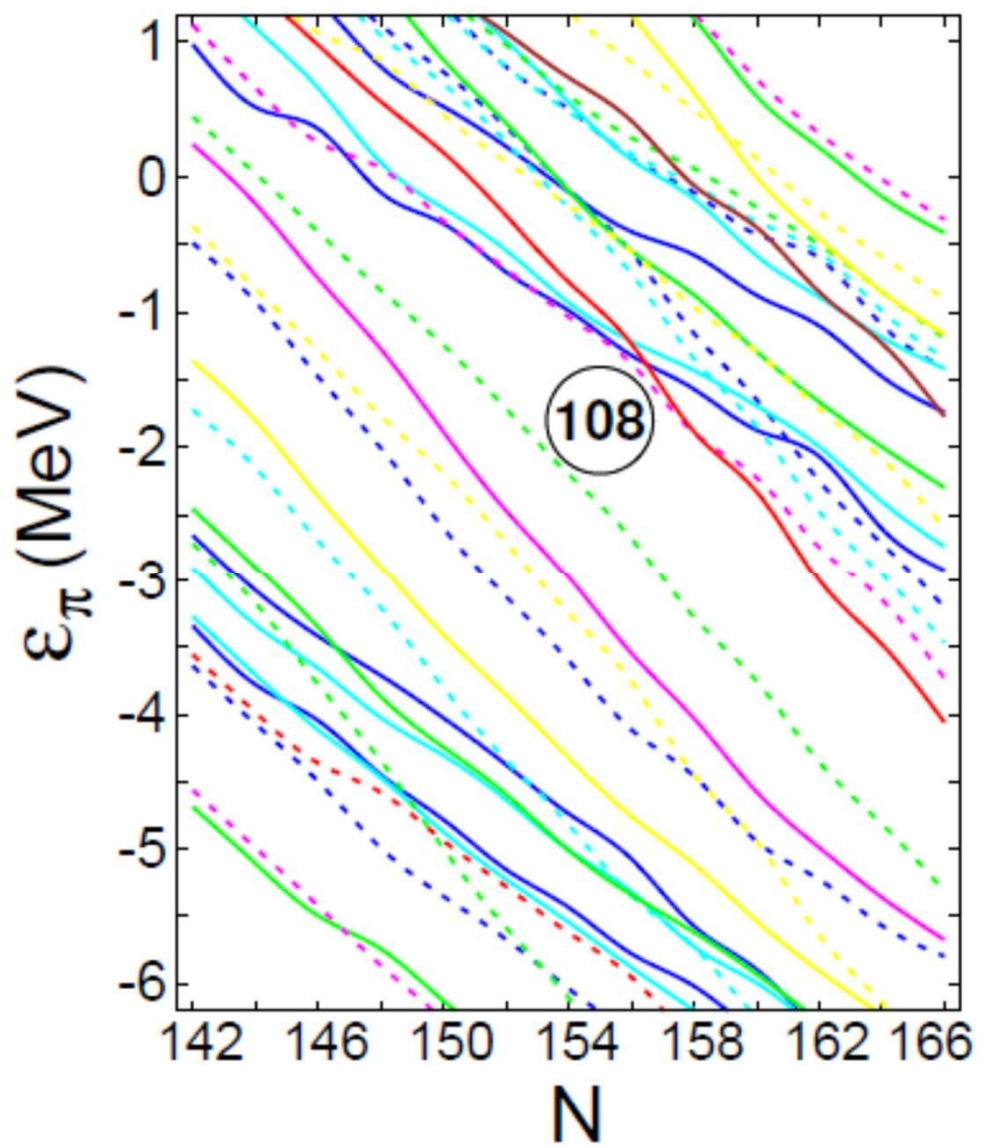


Interpretation of experimental results is often induced by models. Two candidates for the  $8^-$  isomer in  $^{254}\text{No}$ , either a proton or a neutron 2qp configuration, are predicted by the Woods-Saxon model.

Although  $g_K$  factors for two configurations are very different,  $|g_K - g_R|$  controlling intraband transitions are probably similar. (hyperfine structure splitting measurement will decide?)

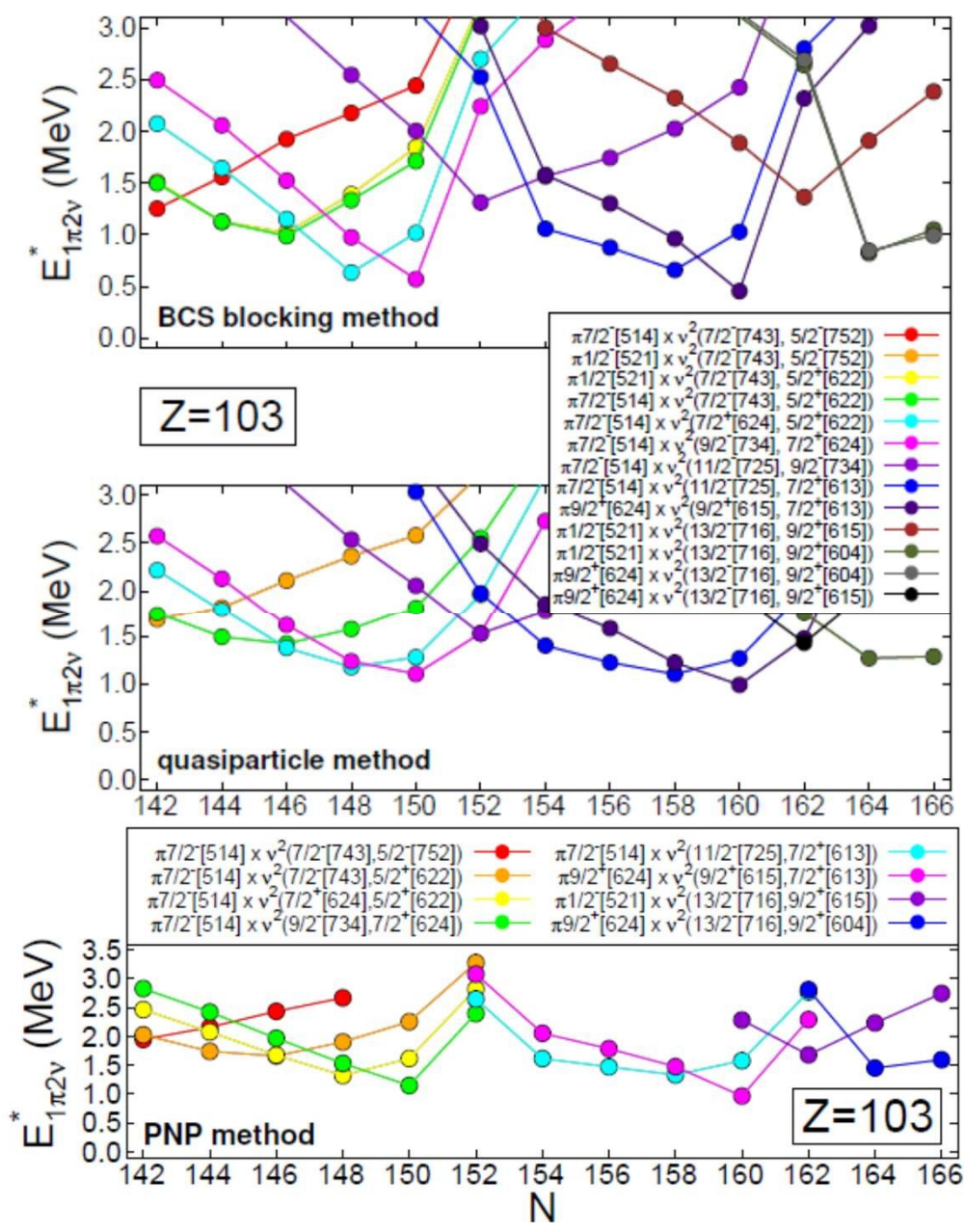
This assignment is related to isomer assignments in Md, Lr and Db nuclei.

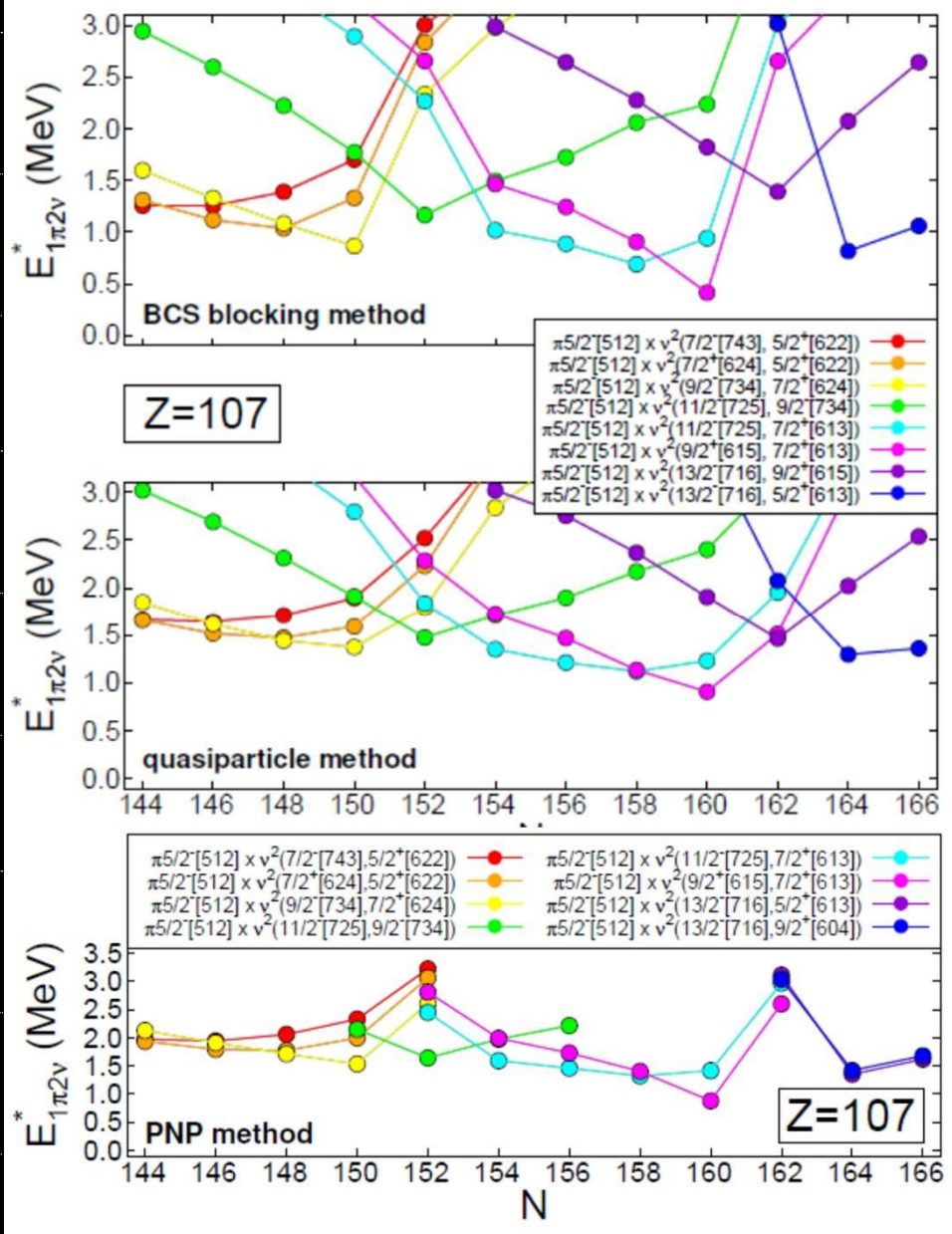


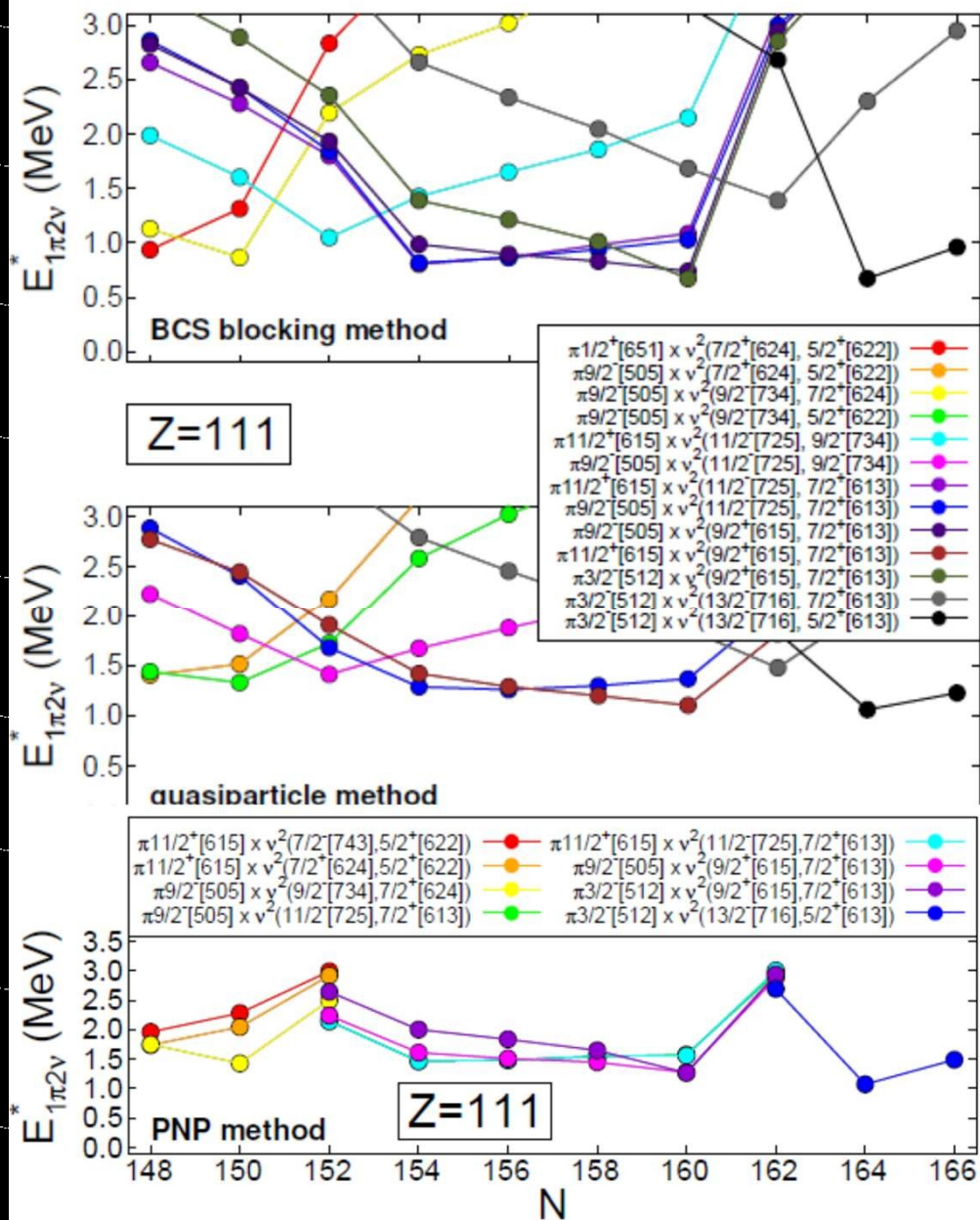


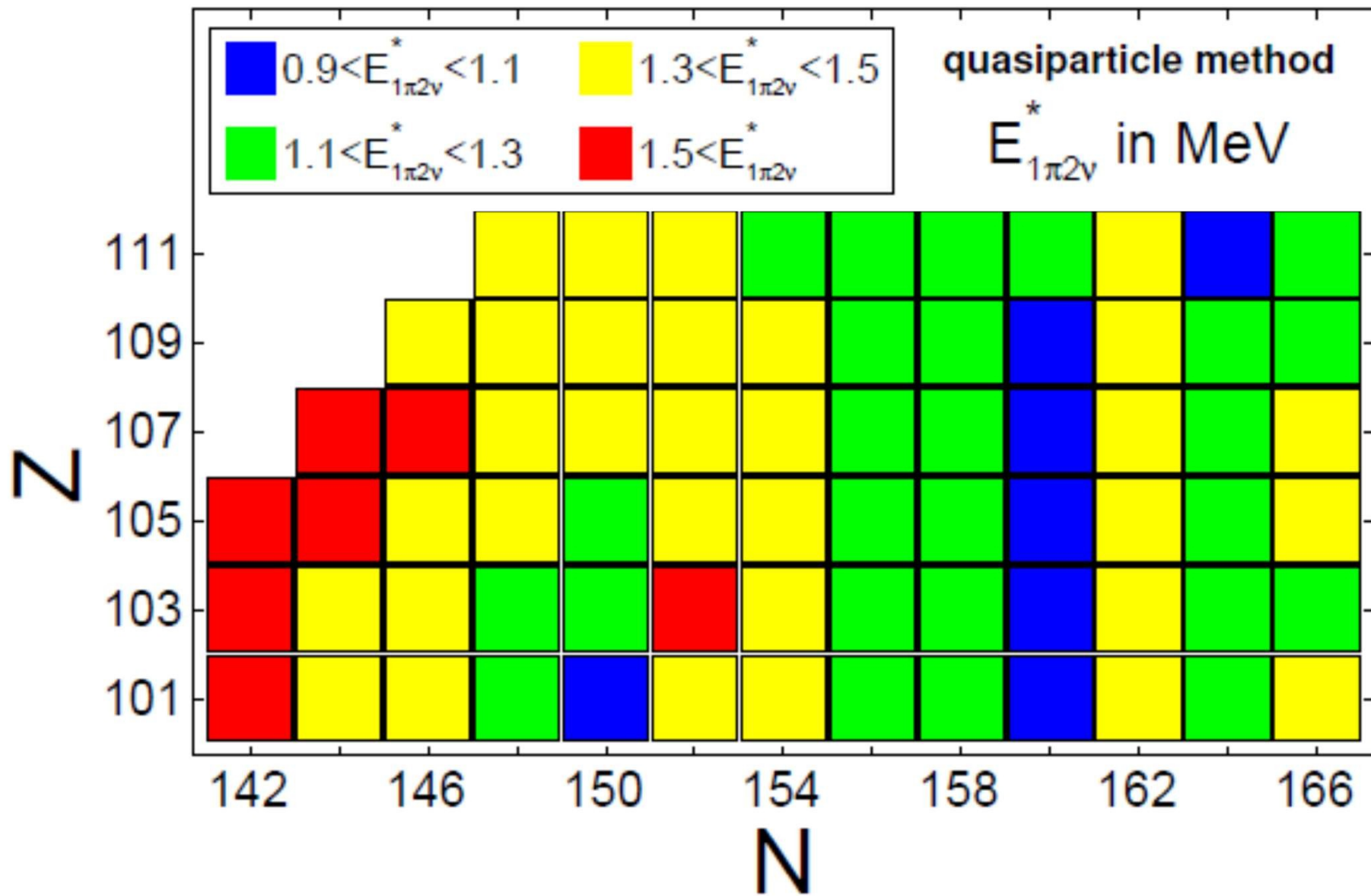
0/0, 1/0, 11/0, red, 12/0, brown, 15/0, black



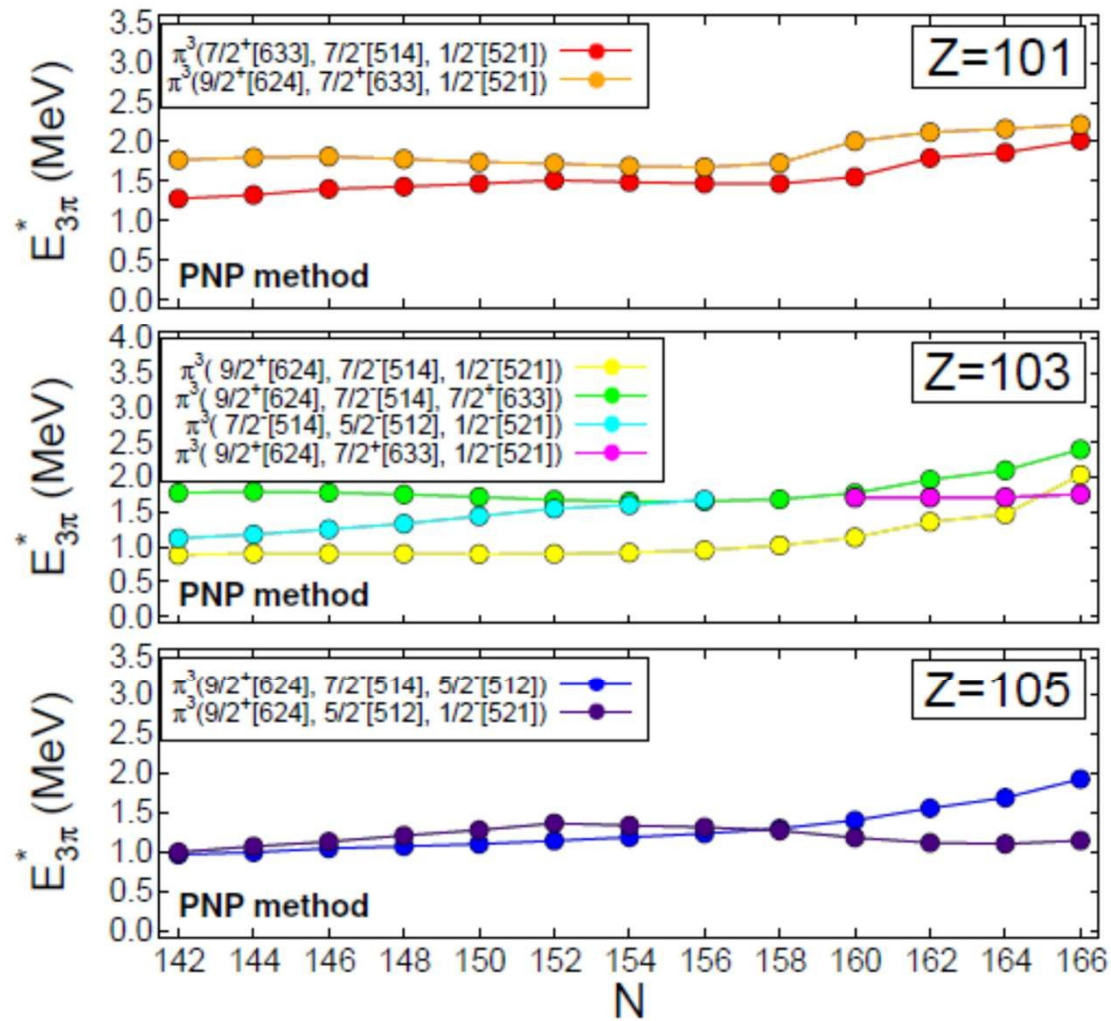
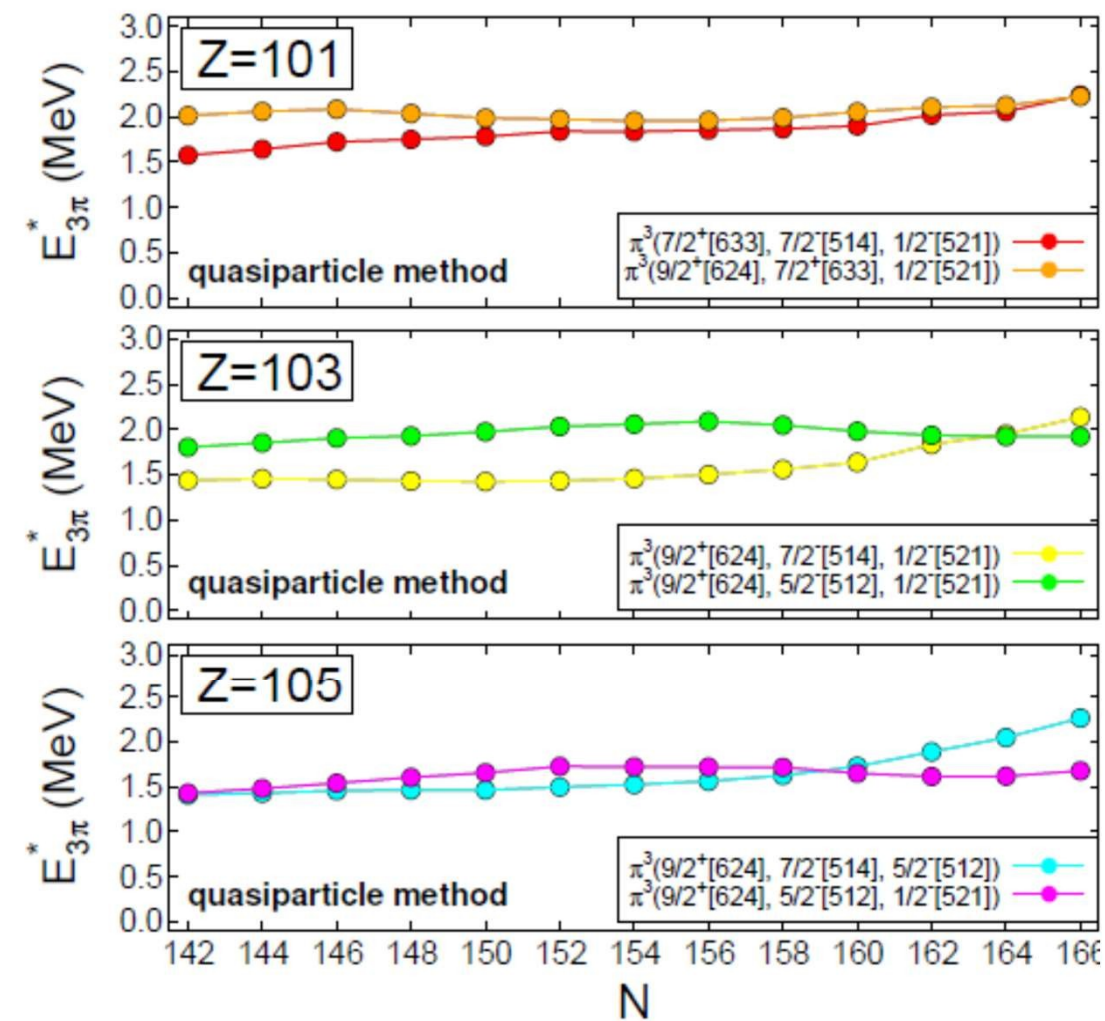


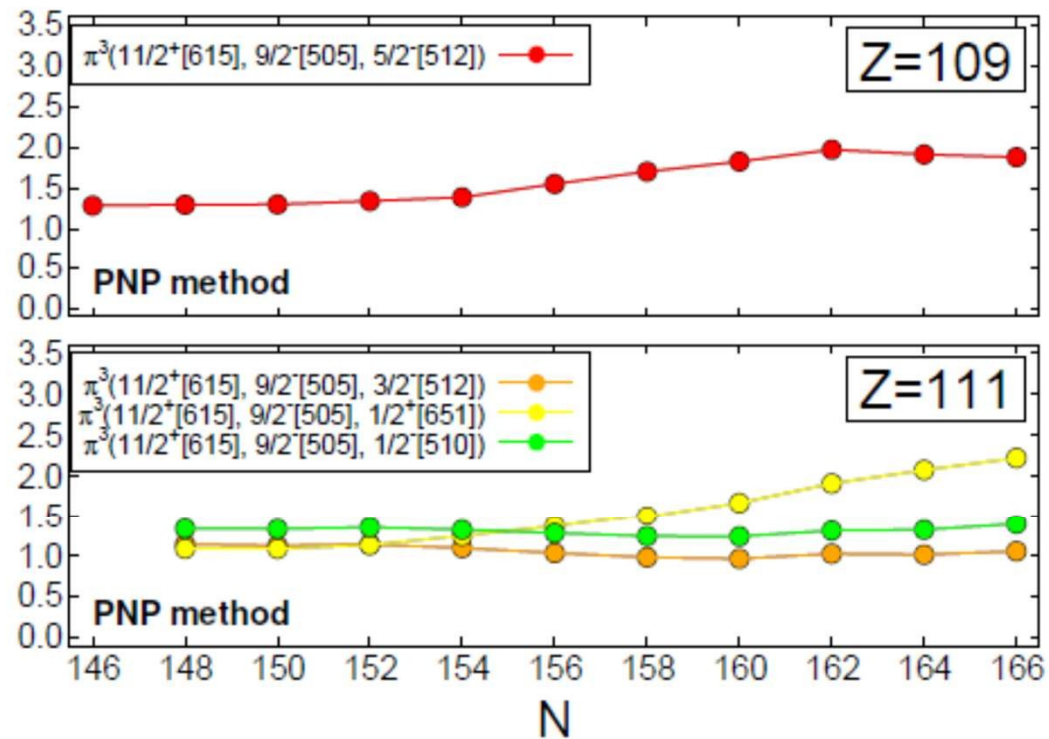
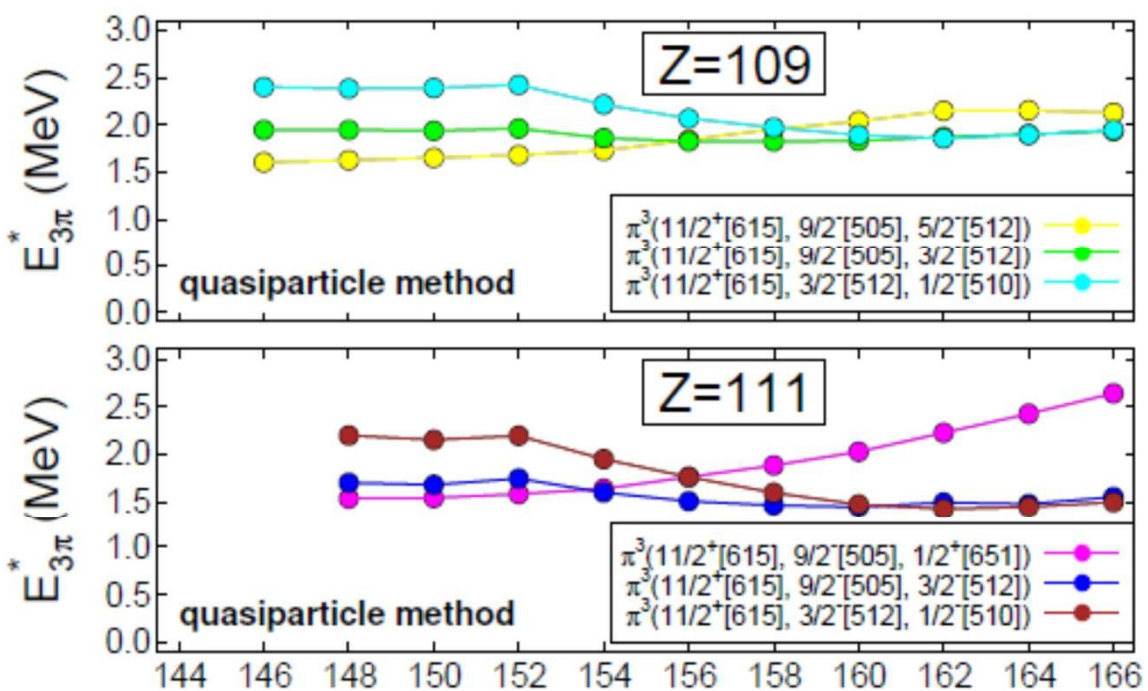




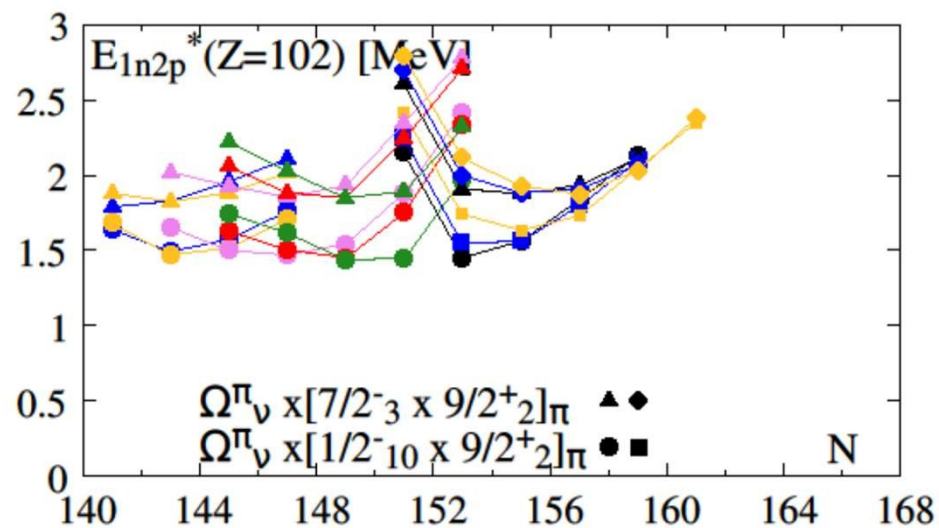
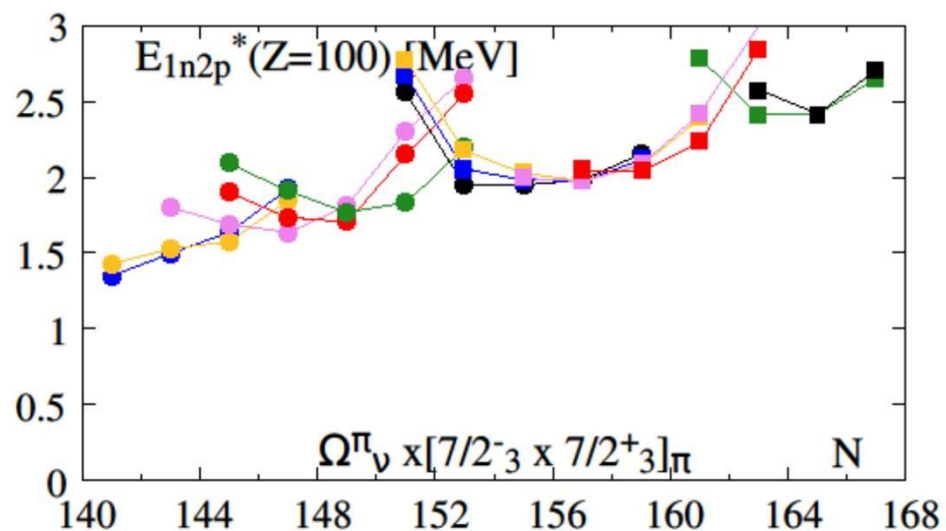




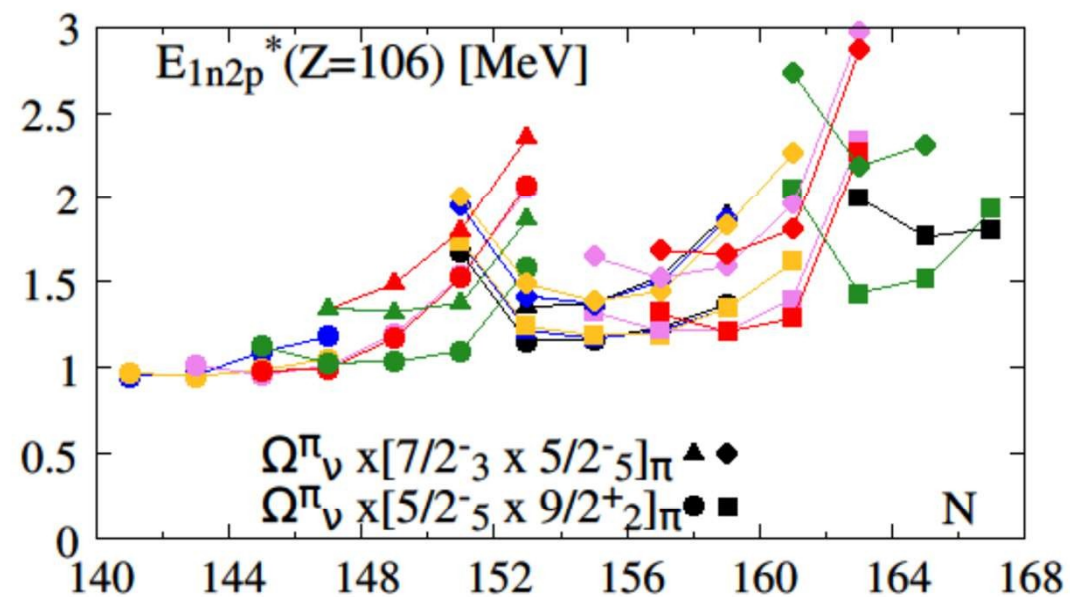
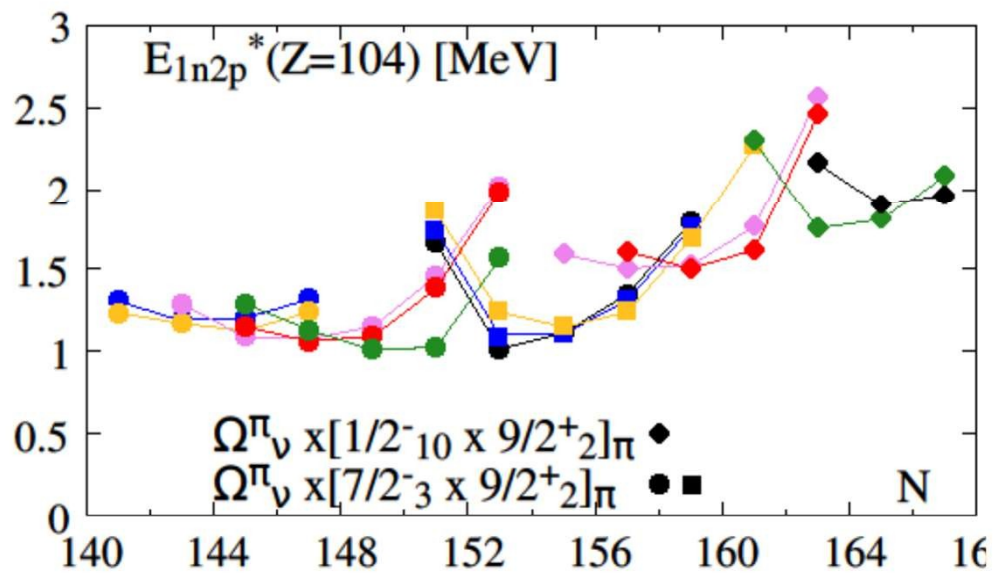




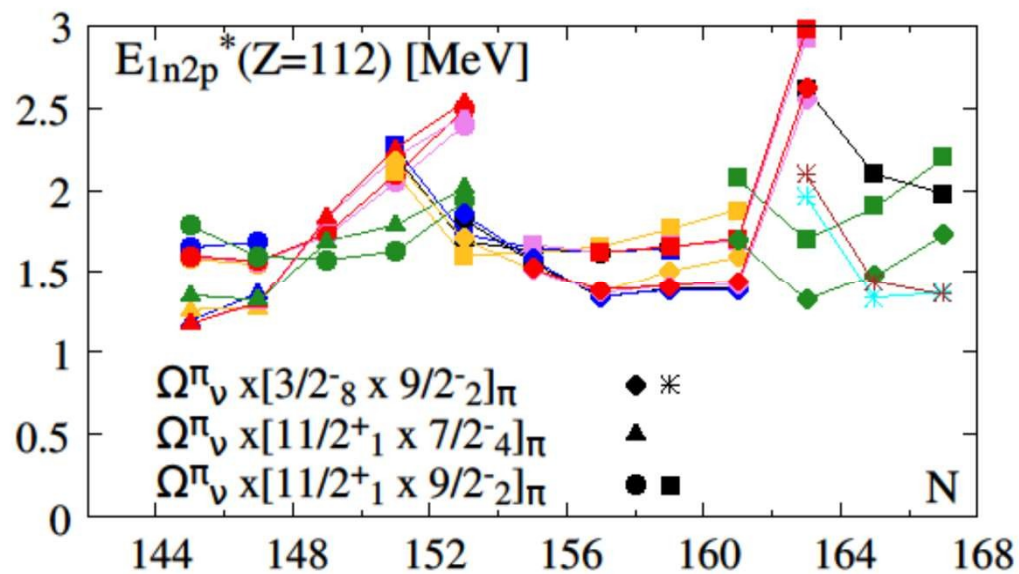
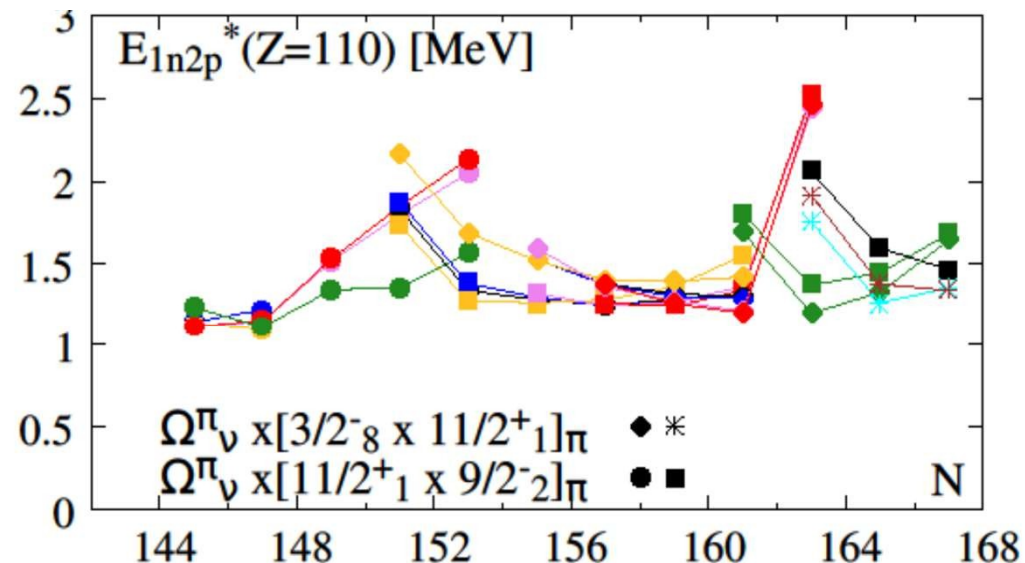
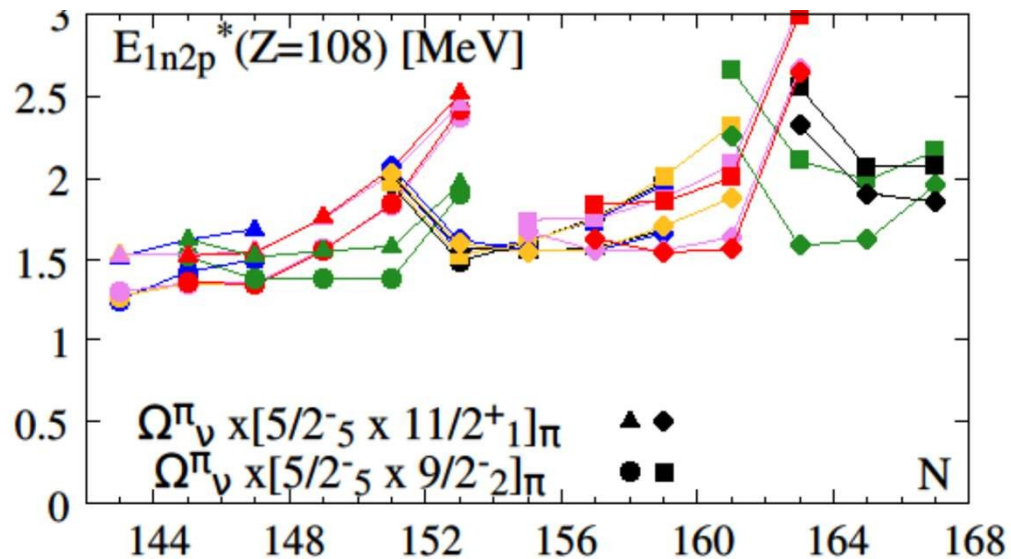
# Even-odd systems $Z=100-112$ , $N=141-167$ ; PNP results, $1n2p$

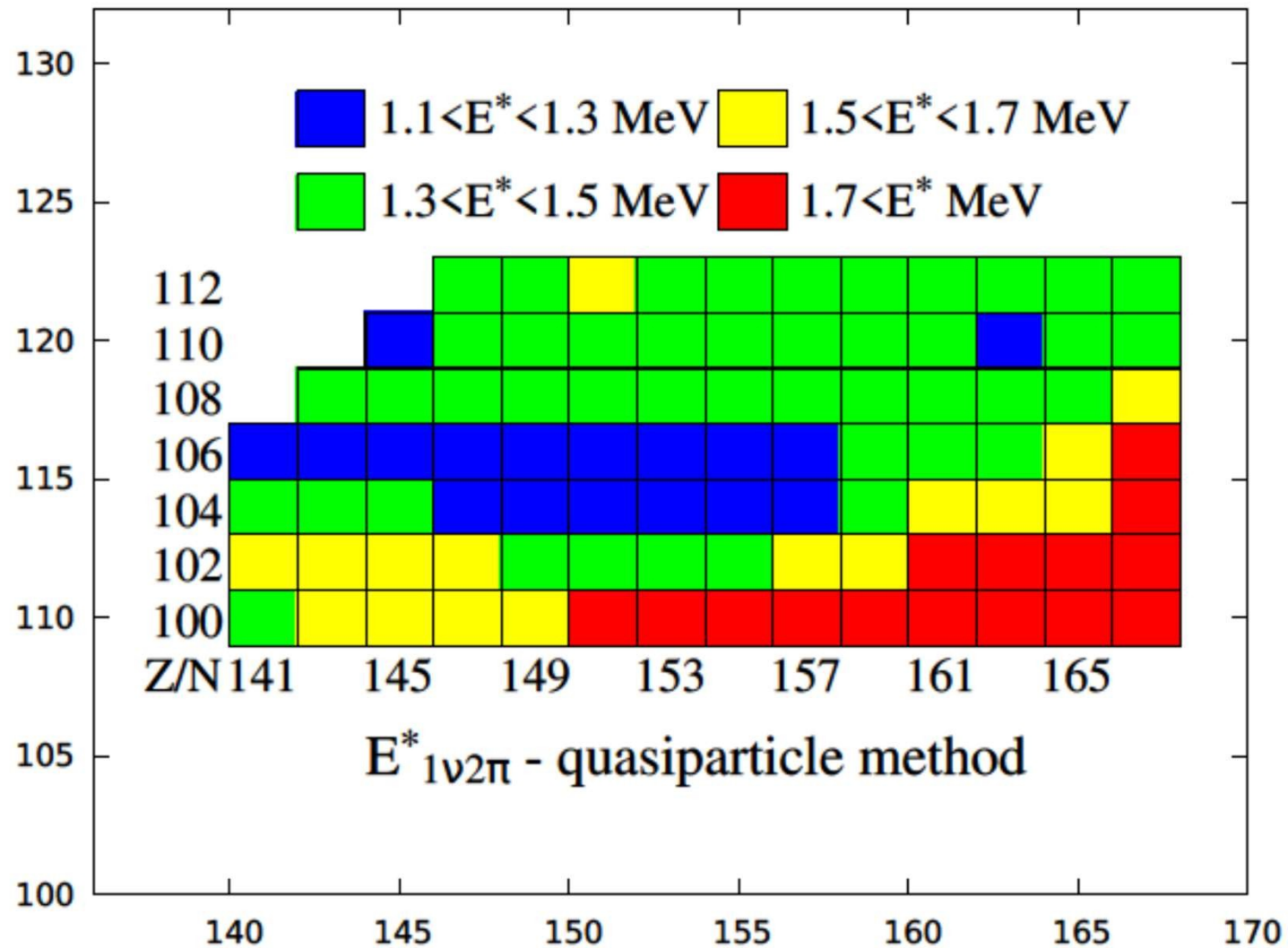


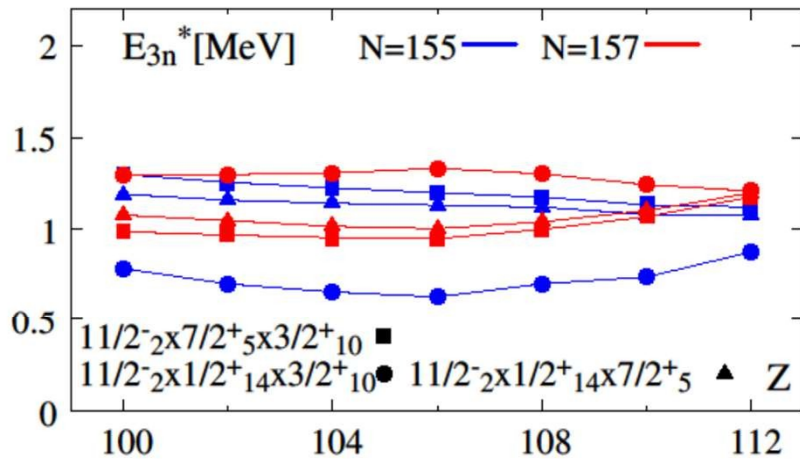
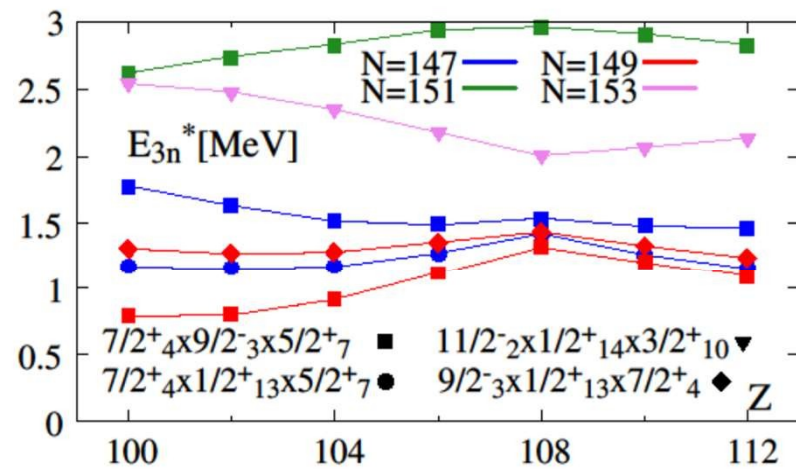
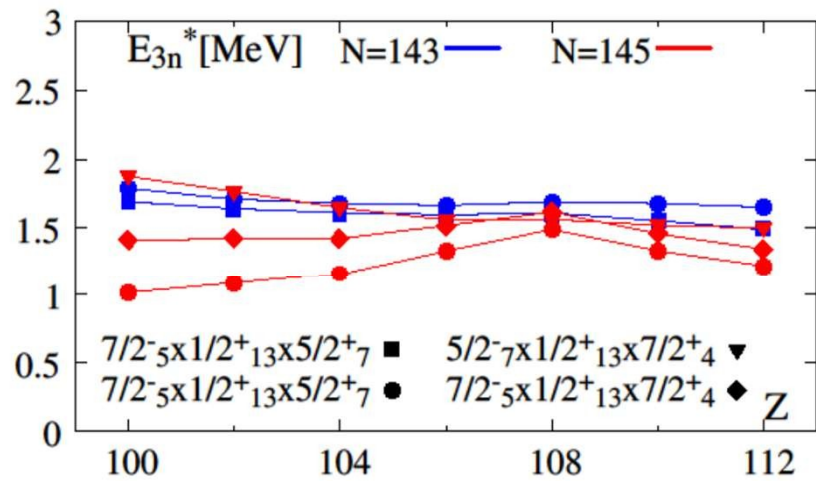




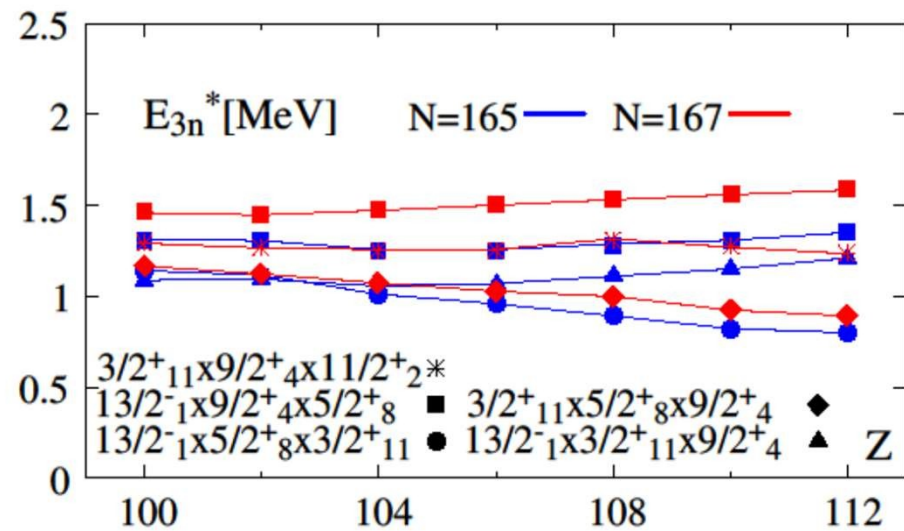
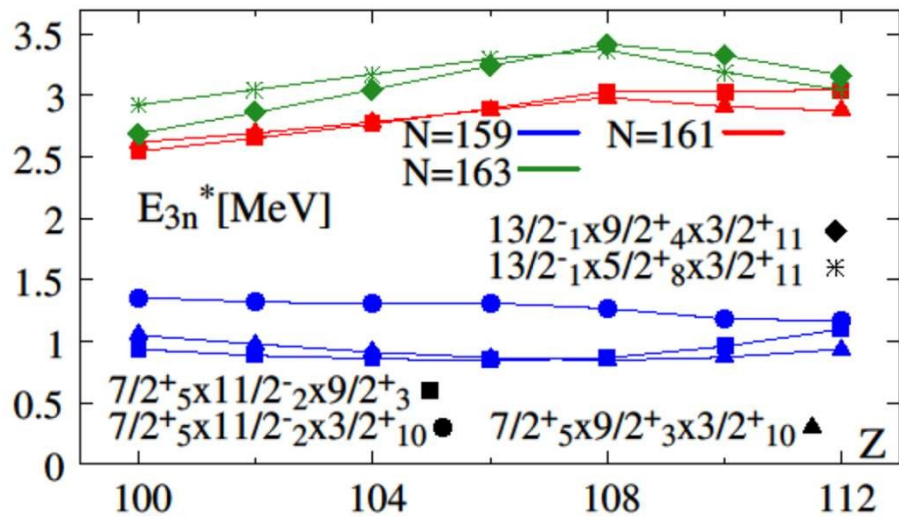




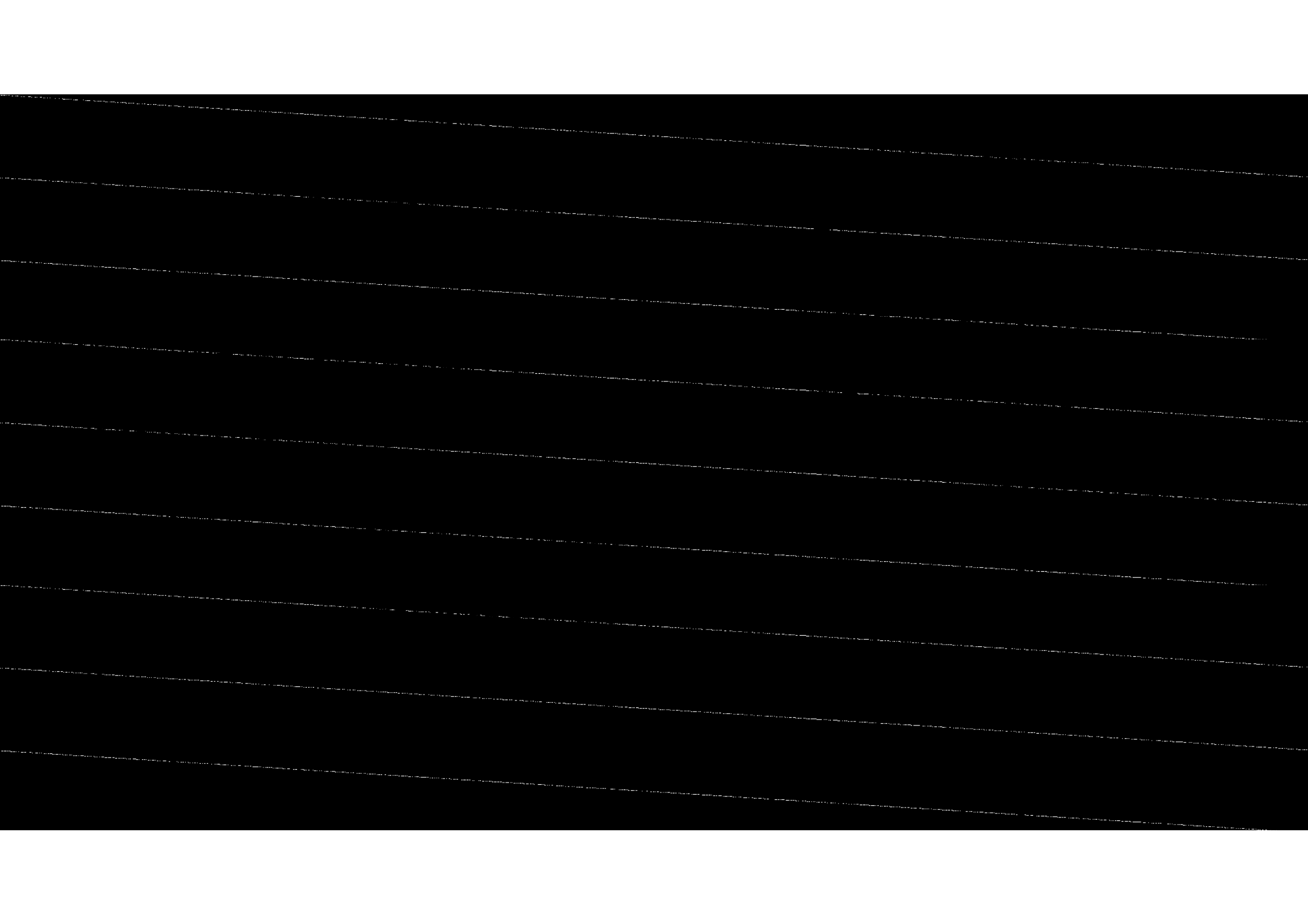




3n – PNP results



# Conclusions





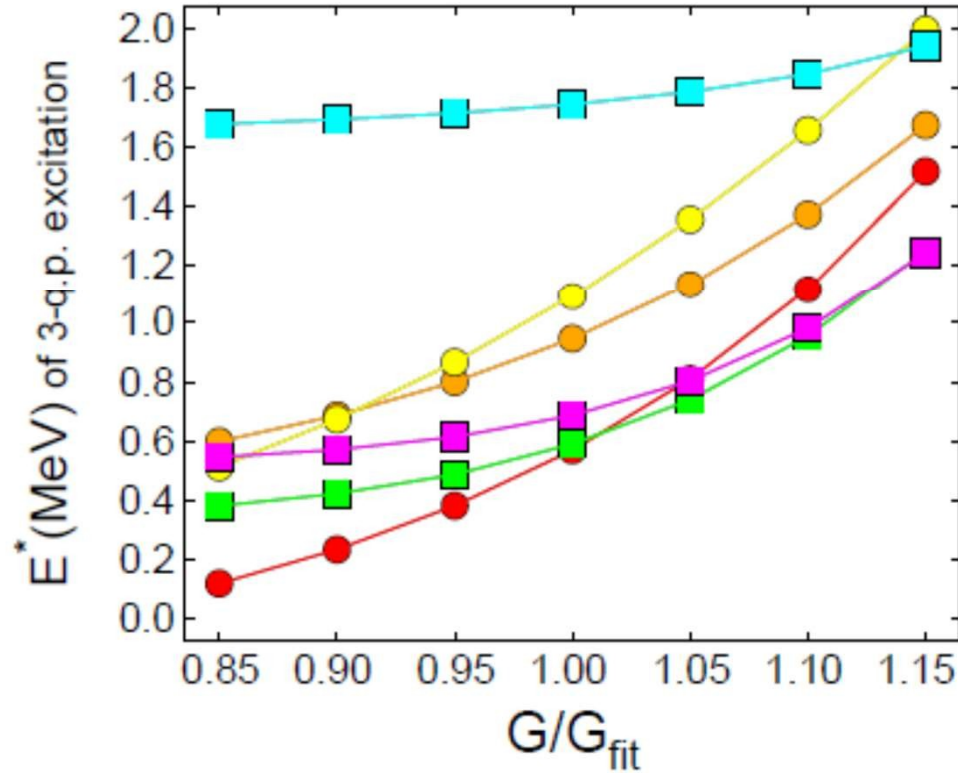
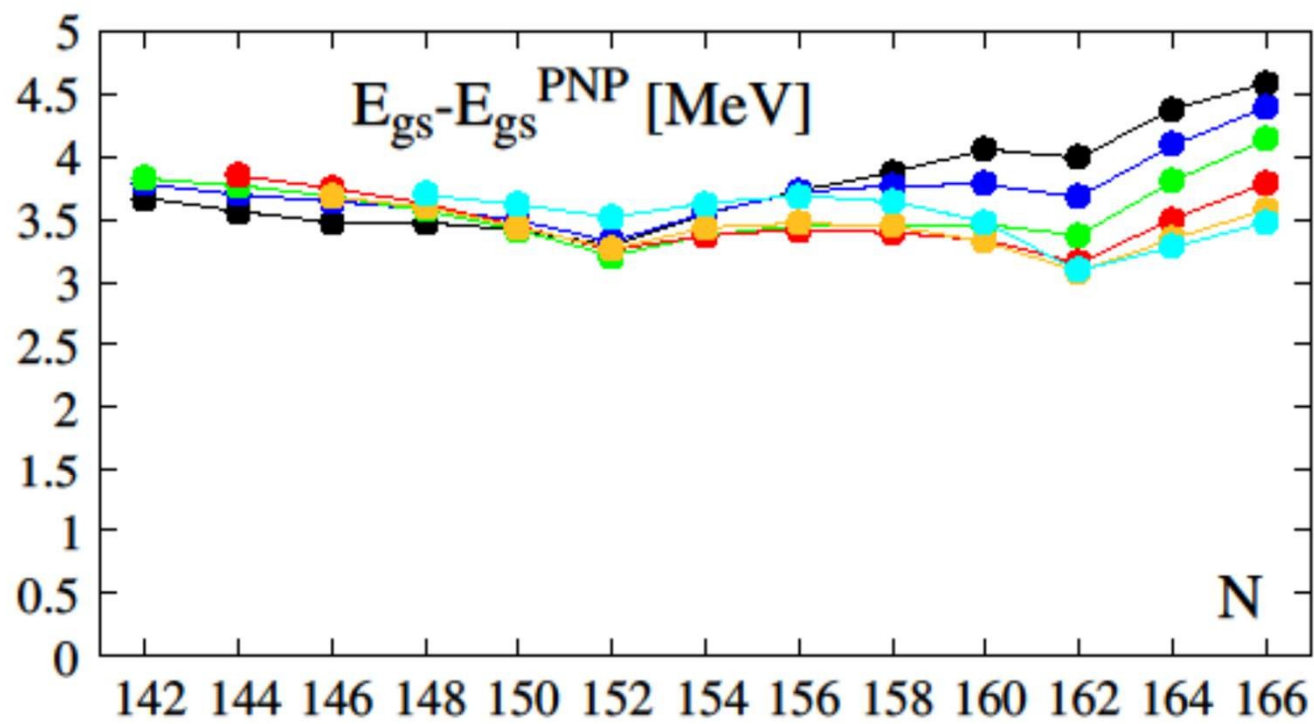
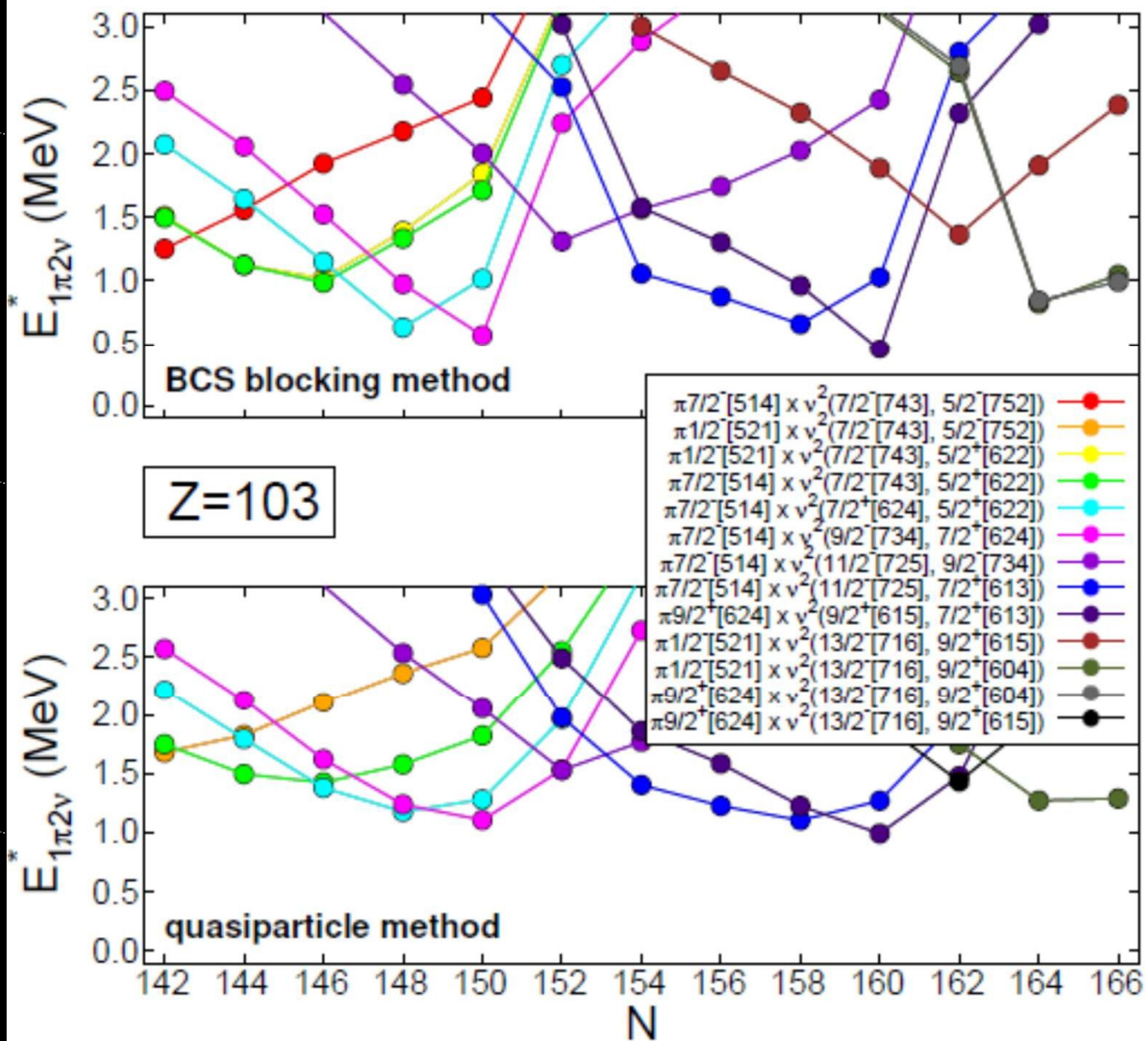
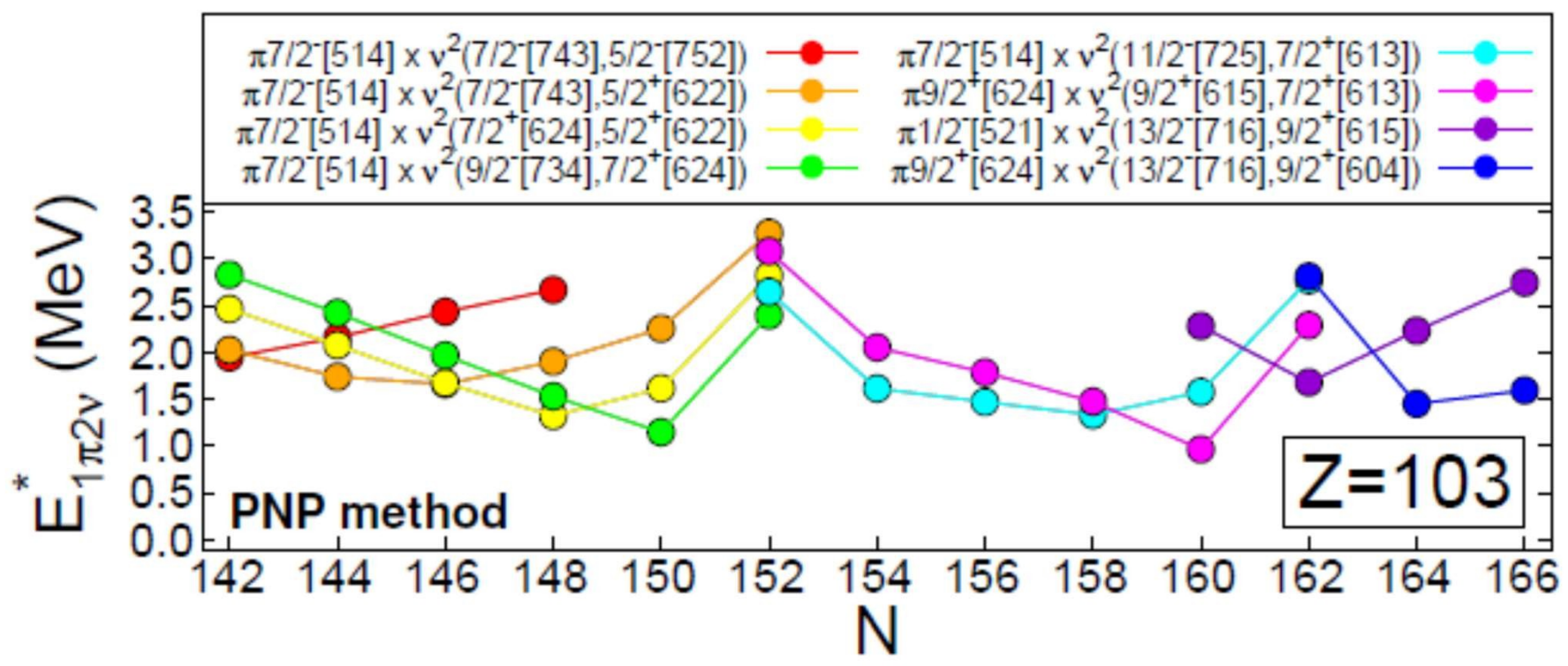


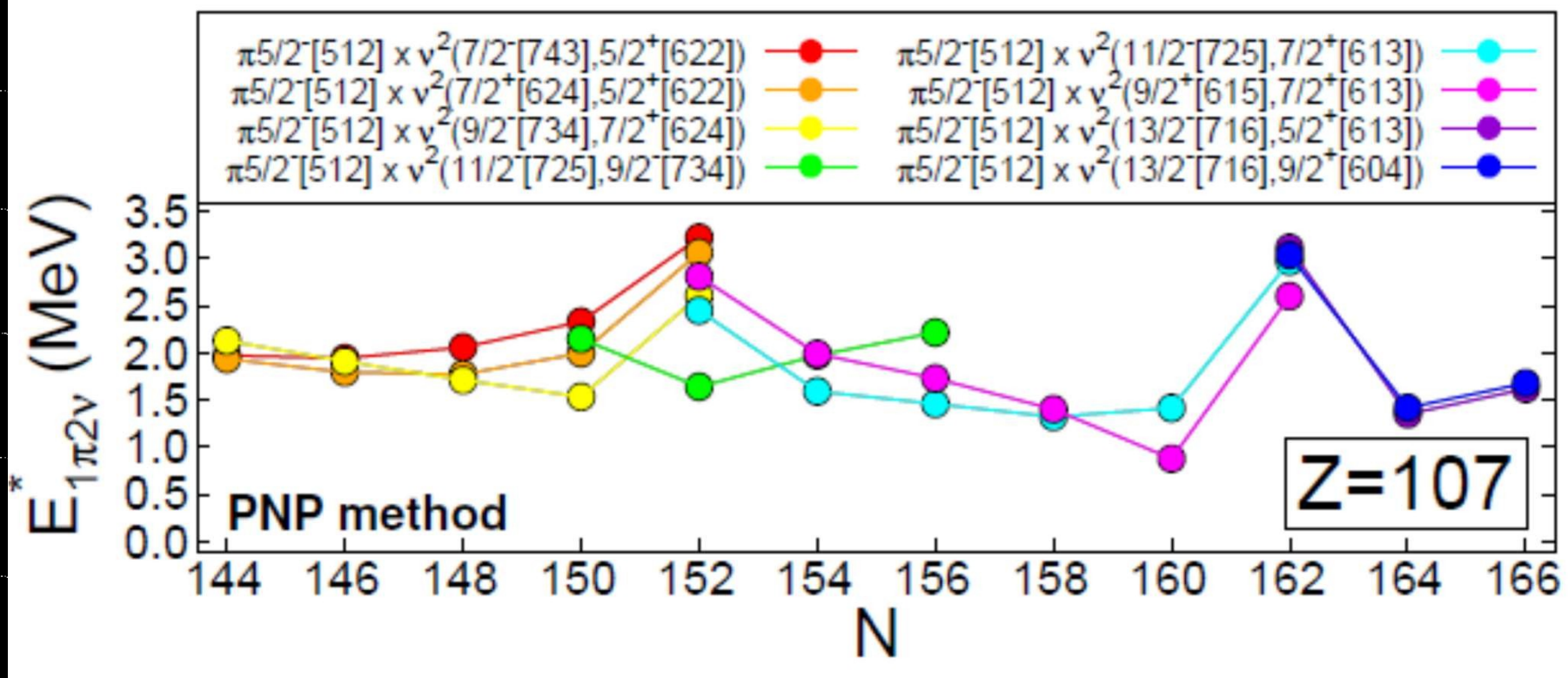
FIG. 17: Energy of the 3-q.p. excitation ( $E_{1\pi 2\nu}^*$  or  $E_{3\pi}^*$  in MeV) from the PNP method vs pairing strength (in units of the value of the fit  $G/G_{fit}$ ) at the fixed, near g.s. shape, for  $1\pi 2\nu$  states in Mt isotopes (dots):  $\pi 9/2_2^- \otimes \nu 7/2_4^+ \otimes \nu 5/2_7^+$  in  $^{255}\text{Mt}$  (yellow),  $\pi 11/2_1^+ \otimes \nu 9/2_3^+ \otimes \nu 7/2_5^+$  in  $^{267}\text{Mt}$  (orange) and  $^{269}\text{Mt}$  (red), and for  $3\pi$  states (squares):  $\pi 7/2_3^- \otimes \pi 9/2_2^+ \otimes \pi 1/2_{10}^-$  in  $^{259}\text{Lr}$  (green),  $\pi 11/2_1^+ \otimes \pi 9/2_2^- \otimes \pi 5/2_5^-$  in  $^{265}\text{Mt}$  (cyan), and  $\pi 9/2_2^+ \otimes \pi 11/2_1^+ \otimes \pi 3/2_8^-$  in  $^{271}\text{Rg}$  (magenta).





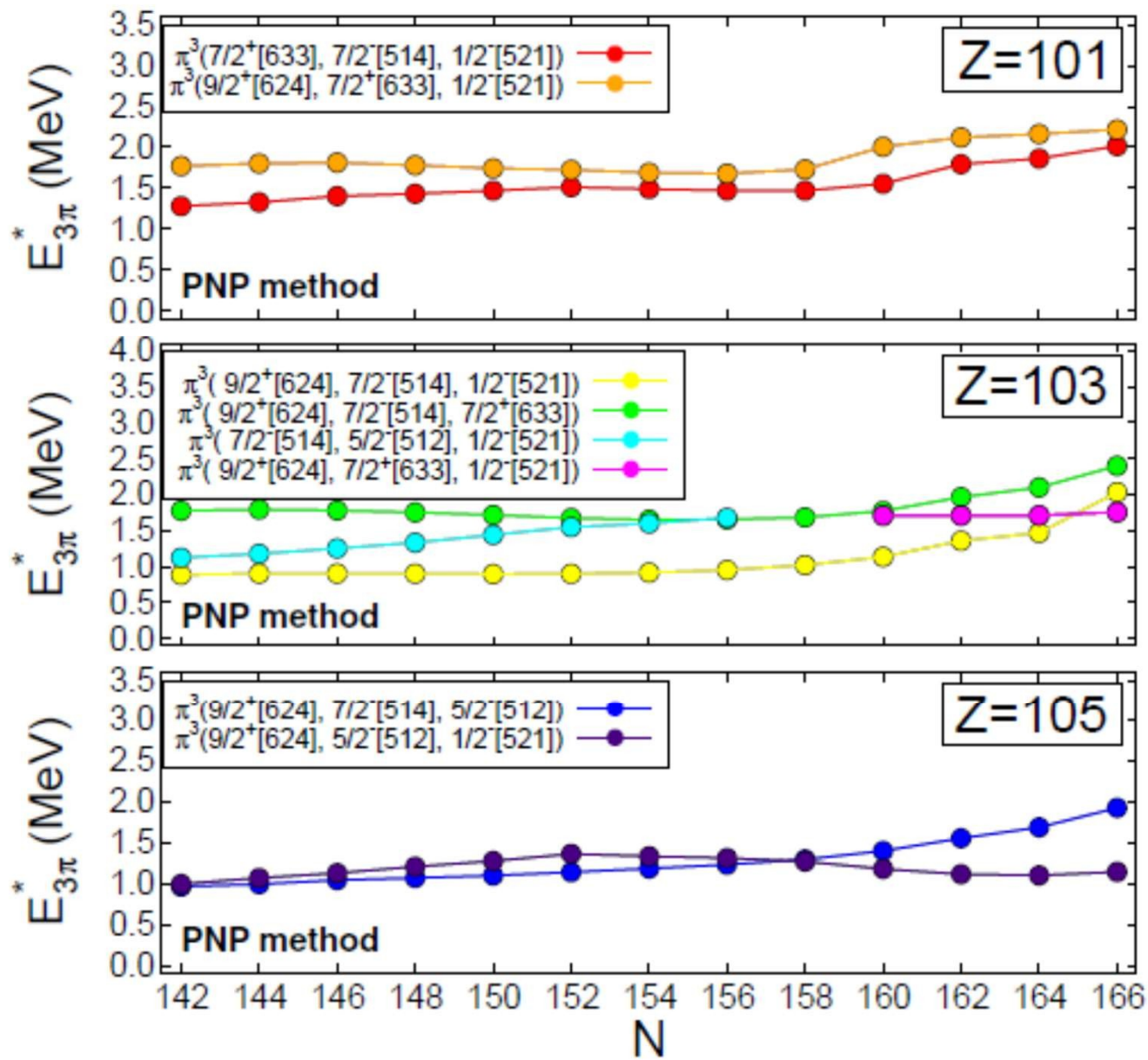


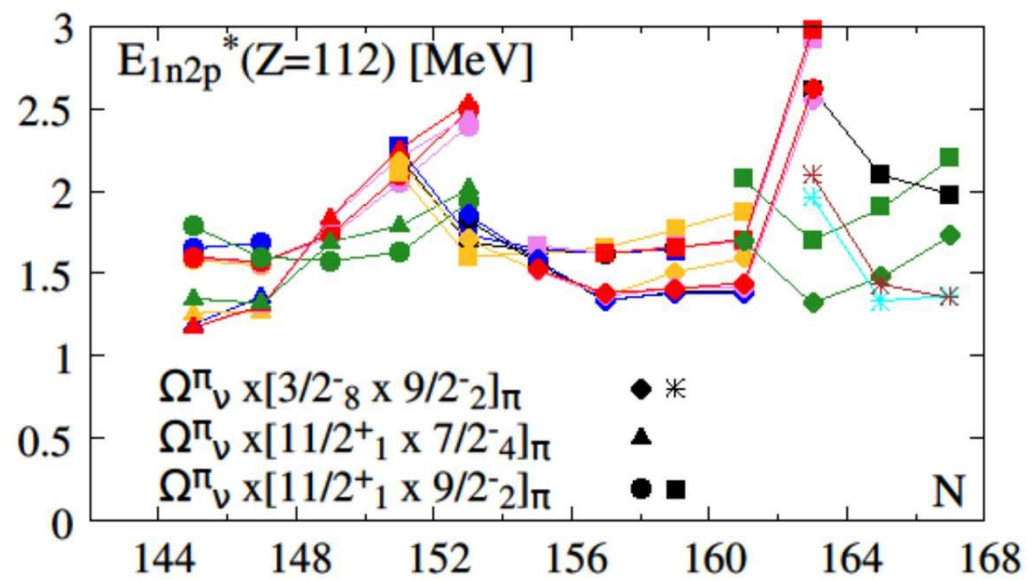










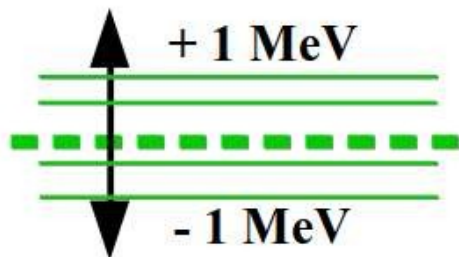




## ODD-A NUCLEI

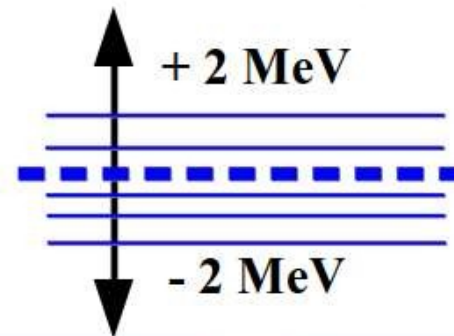
Search for candidates for long-lived **3-qp** isomers in **odd-A** nuclei:  $Z=105-111$ ,  $N=148-166$

**PROTONS:**



Fermi level

**NEUTRONS:**



11 single-quasiproton states

$\times$

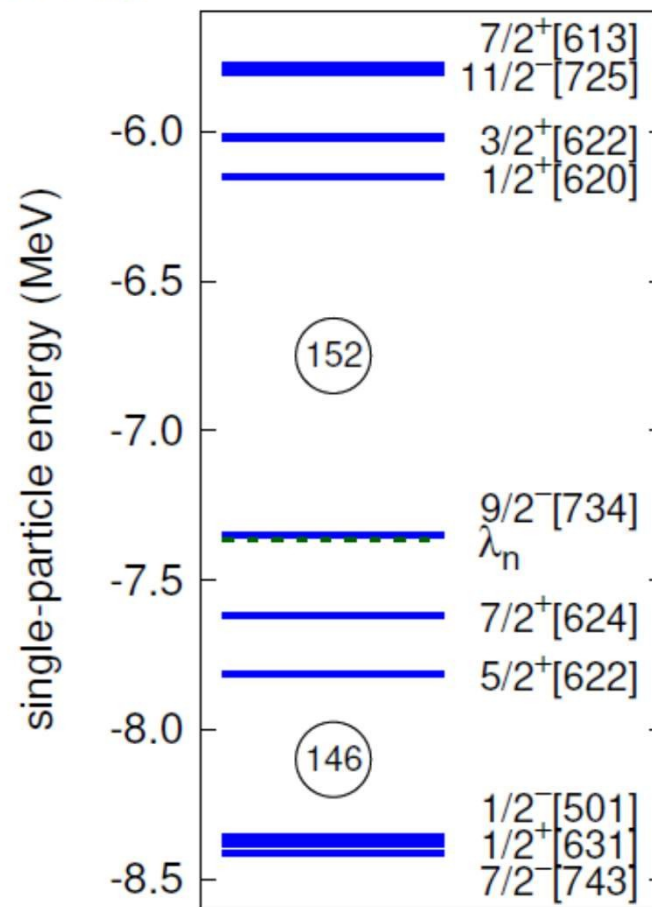
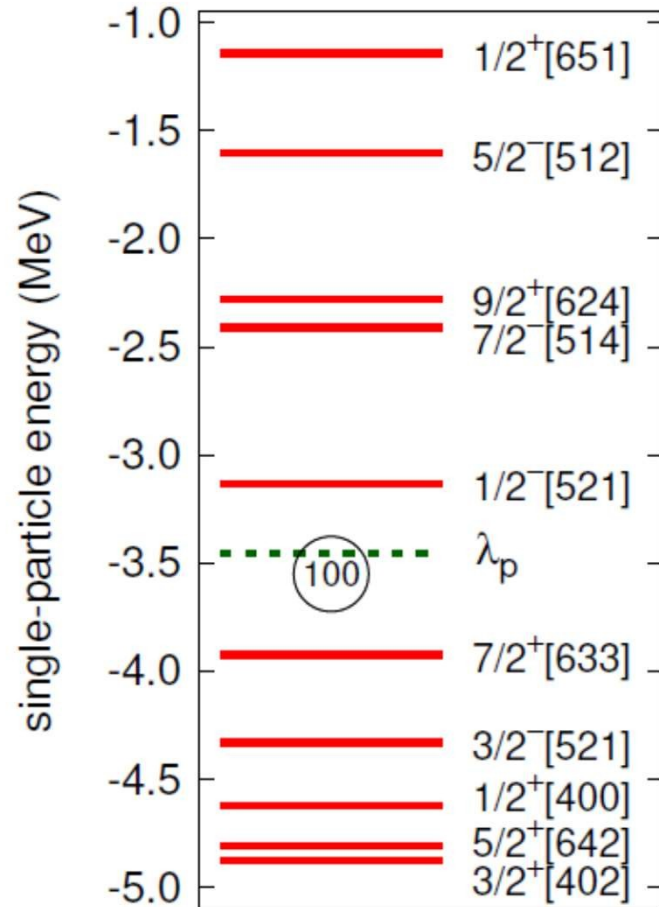
156 two-quasineutron configurations combined to  $K \geq 6$

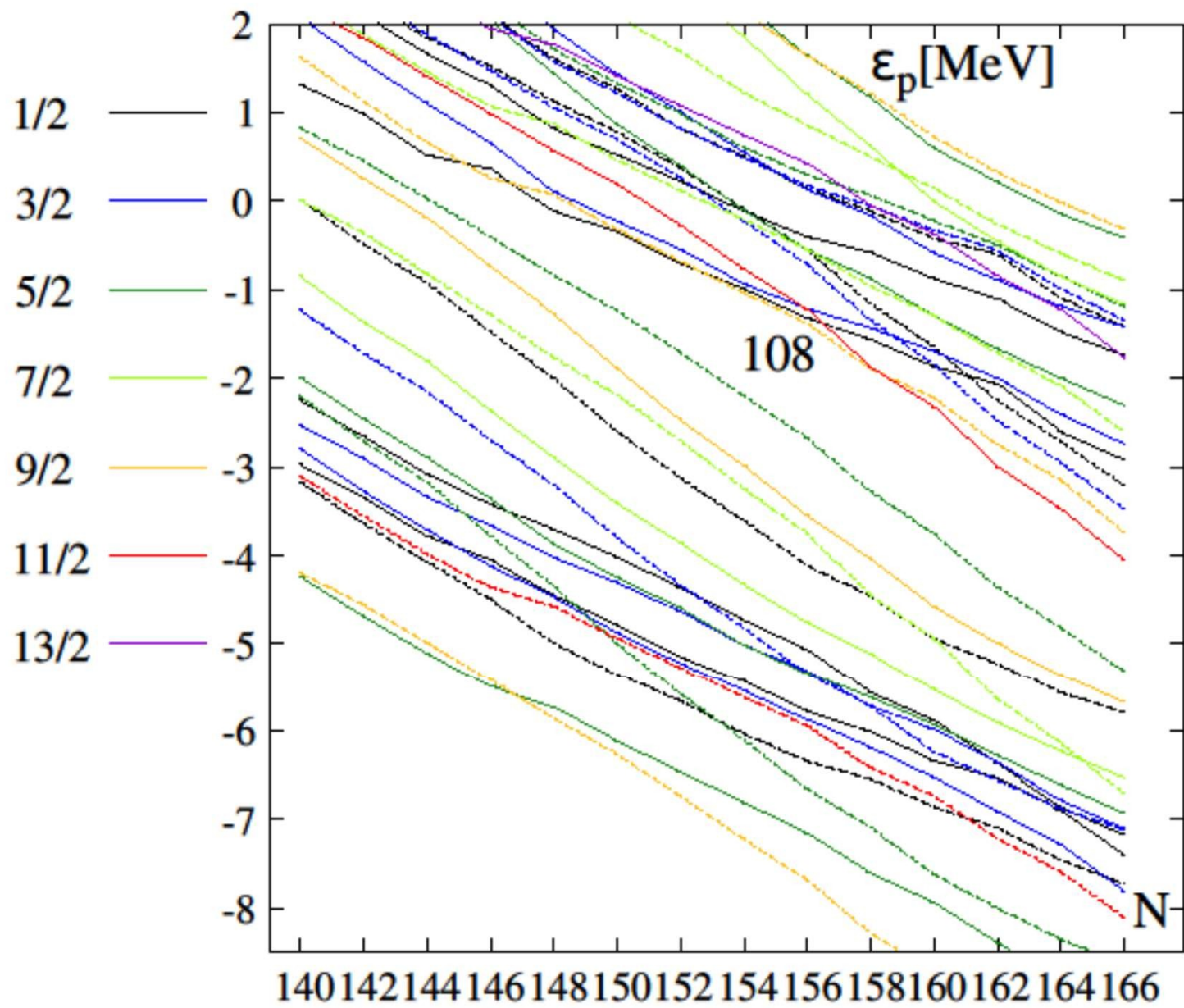
Considered 1716 configurations (3-qp) for each nucleus

# <sup>251</sup>Md

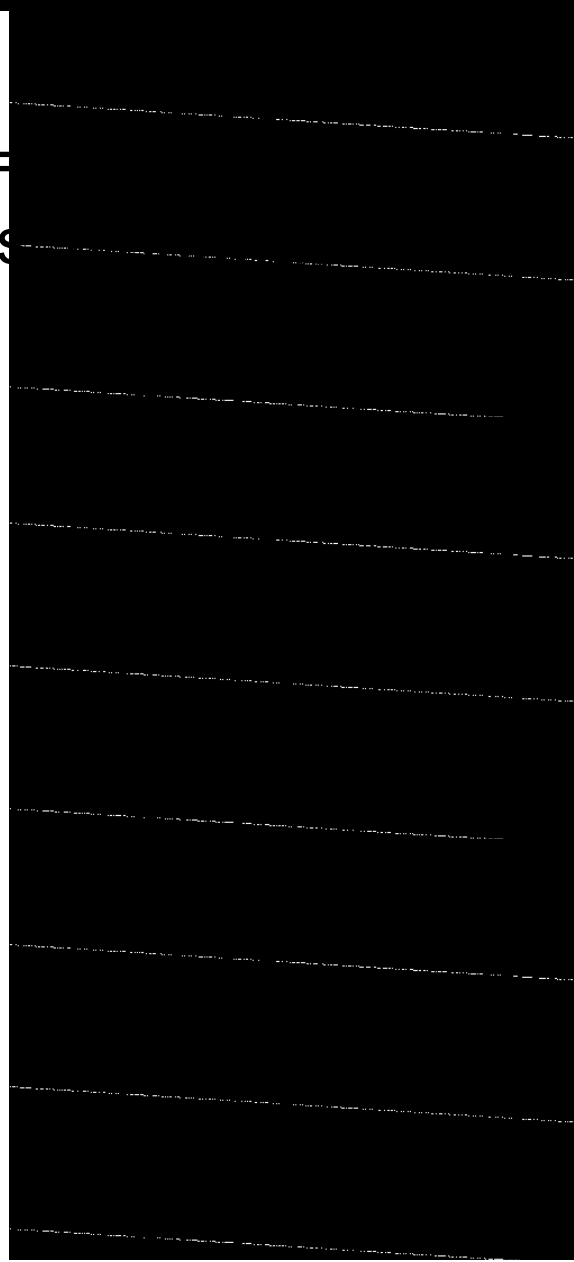
protons

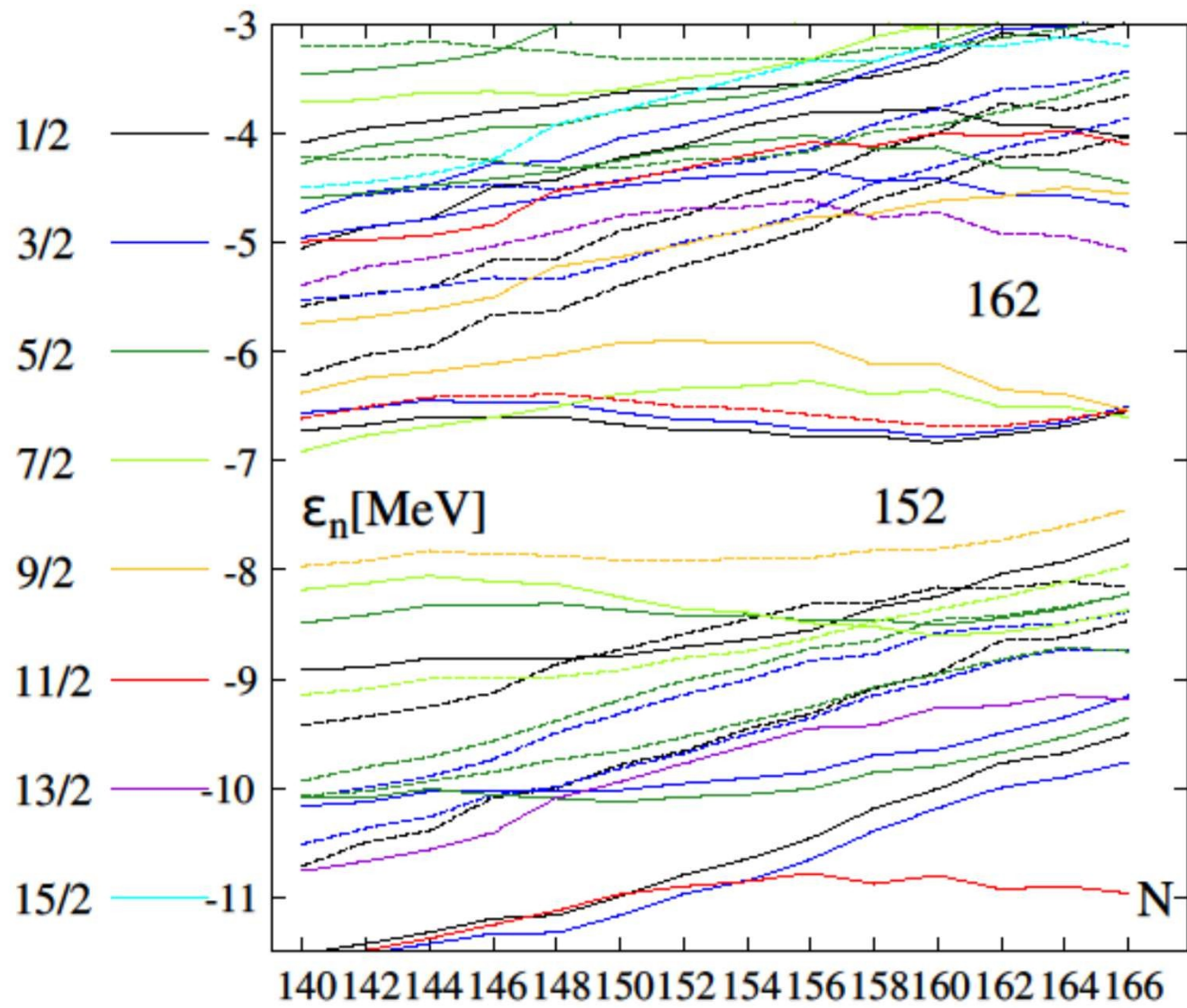
neutrons





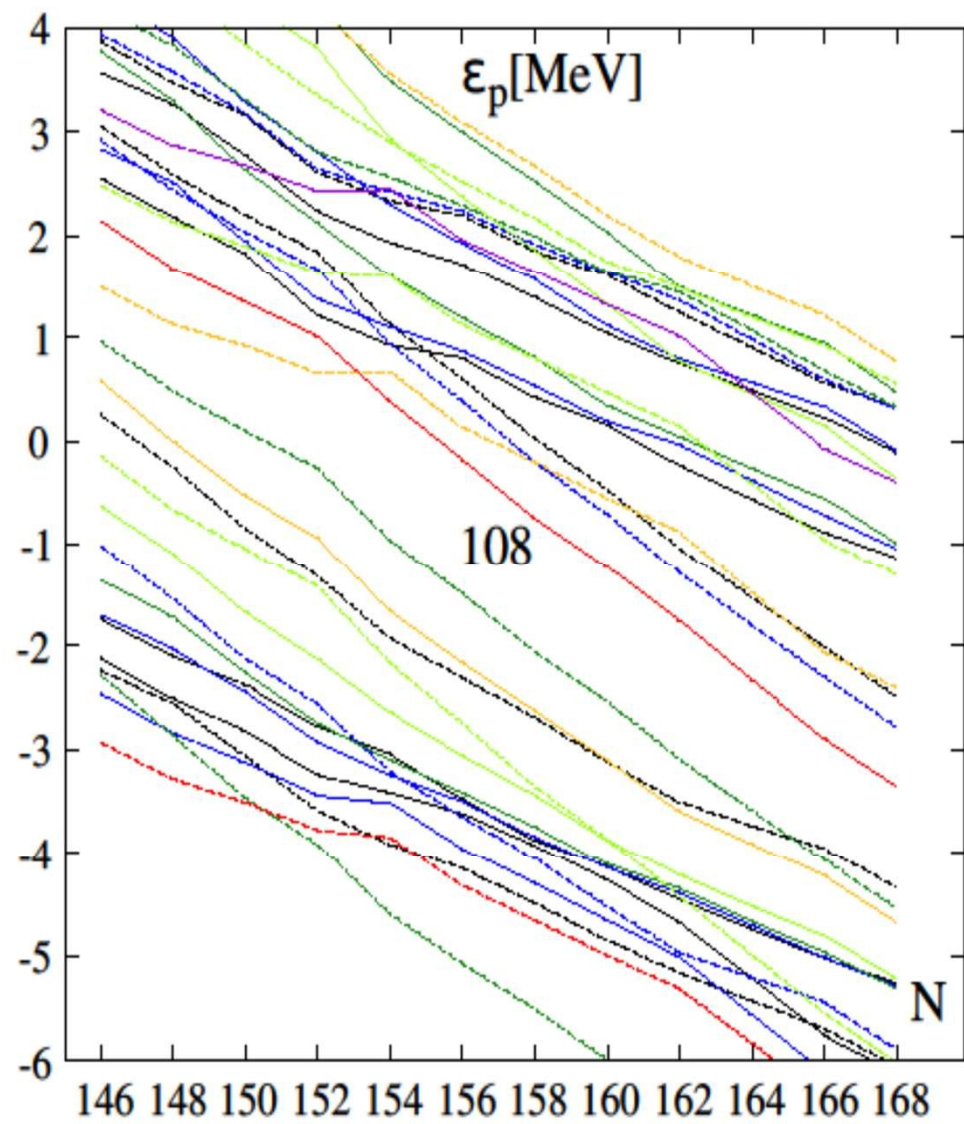
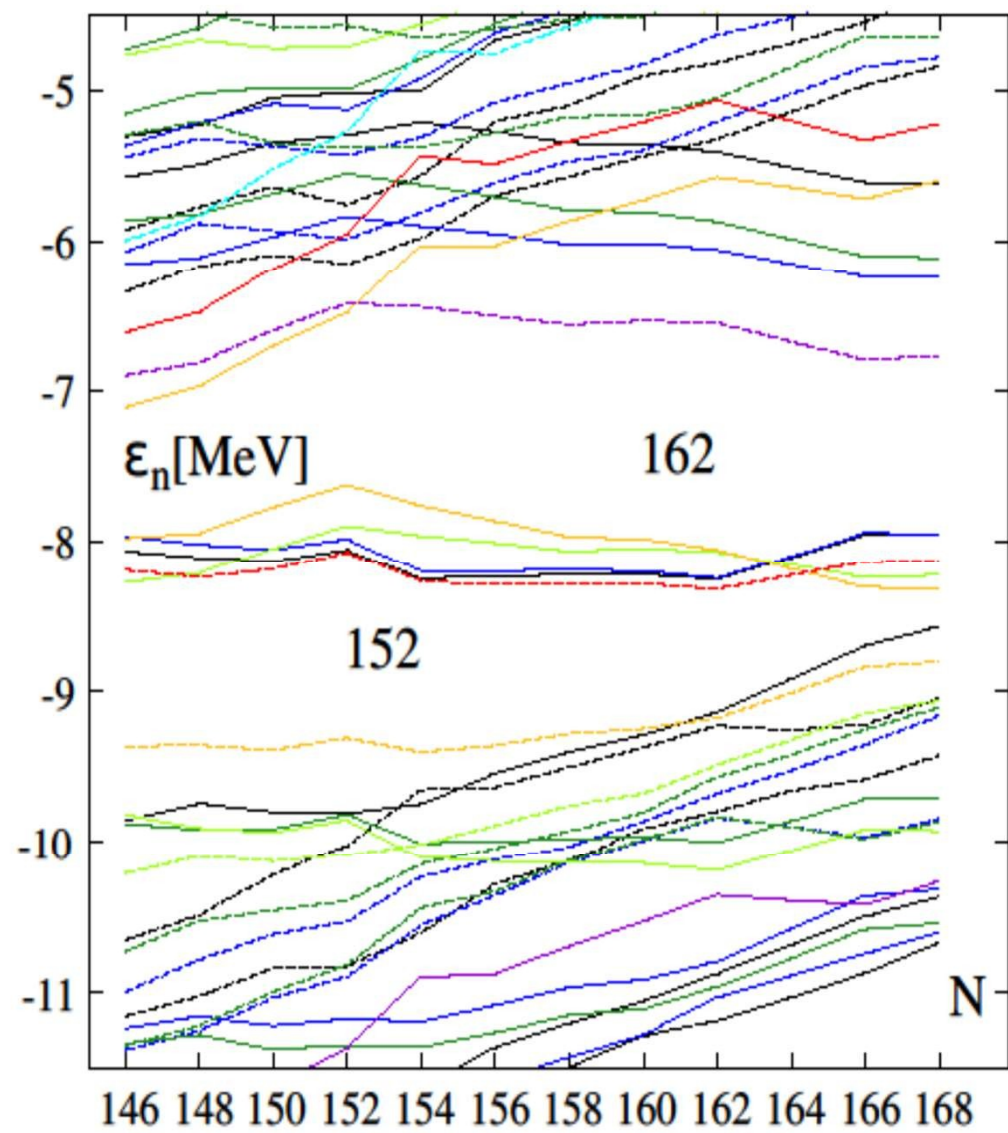
$Z=$   
 $g.s.$





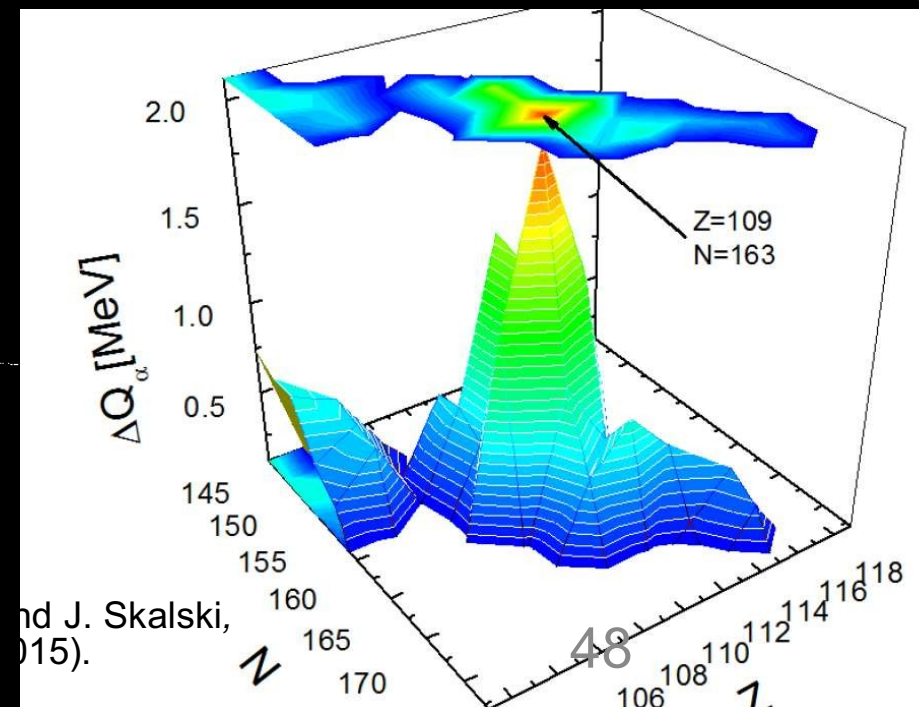
$Z$   
 $g$





Z	N	$\Omega^p$	$\Omega^n$	$K^\pi$	$\Delta Q_\alpha$
111	169	9/2 <sup>-</sup>	5/2 <sup>+</sup>	7 <sup>-</sup>	0.74
111	163	3/2 <sup>-</sup>	13/2 <sup>-</sup>	8 <sup>+</sup>	1.31
111	161	3/2 <sup>-</sup>	7/2 <sup>+</sup>	7/2 <sup>-</sup>	0.52
110	163		13/2 <sup>-</sup>	13/2 <sup>-</sup>	0.97
109	169	11/2 <sup>+</sup>	9/2 <sup>+</sup>	10 <sup>+</sup>	0.51
109	167	11/2 <sup>+</sup>	5/2 <sup>+</sup>	8 <sup>+</sup>	0.71
109	166	11/2 <sup>+</sup>		11/2 <sup>+</sup>	0.88
109	165	11/2 <sup>+</sup>	3/2 <sup>+</sup>	7 <sup>+</sup>	1.38
109	164	11/2 <sup>+</sup>		11/2 <sup>+</sup>	1.13
109	163	11/2 <sup>+</sup>	13/2 <sup>-</sup>	12 <sup>-</sup>	1.99
109	162	11/2 <sup>+</sup>		11/2 <sup>+</sup>	1.27
109	161	11/2 <sup>+</sup>	9/2 <sup>+</sup>	10 <sup>+</sup>	1.32
109	160	11/2 <sup>+</sup>		11/2 <sup>+</sup>	1.37
109	159	11/2 <sup>+</sup>	9/2 <sup>+</sup>	10 <sup>+</sup>	1.56
109	158	11/2 <sup>+</sup>		11/2 <sup>+</sup>	1.39
109	157	11/2 <sup>+</sup>	3/2 <sup>+</sup>	7 <sup>+</sup>	1.41
108	163		13/2 <sup>-</sup>	13/2 <sup>-</sup>	1.00
107	163	5/2 <sup>-</sup>	13/2 <sup>-</sup>	9 <sup>+</sup>	1.17
107	157	5/2 <sup>-</sup>	11/2 <sup>-</sup>	8 <sup>+</sup>	0.57
106	163		13/2 <sup>-</sup>	13/2 <sup>-</sup>	0.96
105	153	9/2 <sup>+</sup>	1/2 <sup>+</sup>	5 <sup>+</sup>	0.97
103	157	7/2 <sup>-</sup>	11/2 <sup>-</sup>	9 <sup>+</sup>	0.52
103	154	7/2 <sup>-</sup>		7/2 <sup>-</sup>	0.54
103	153	7/2 <sup>-</sup>	1/2 <sup>+</sup>	4 <sup>-</sup>	1.45
103	151	7/2 <sup>-</sup>	9/2 <sup>-</sup>	8 <sup>+</sup>	0.58

High-K states: a chance for longer half-lives.  
 Candidates for high-K ground states.  
 in odd or odd-odd SHN in the W-S model.



and J. Skalski,  
 (2015).