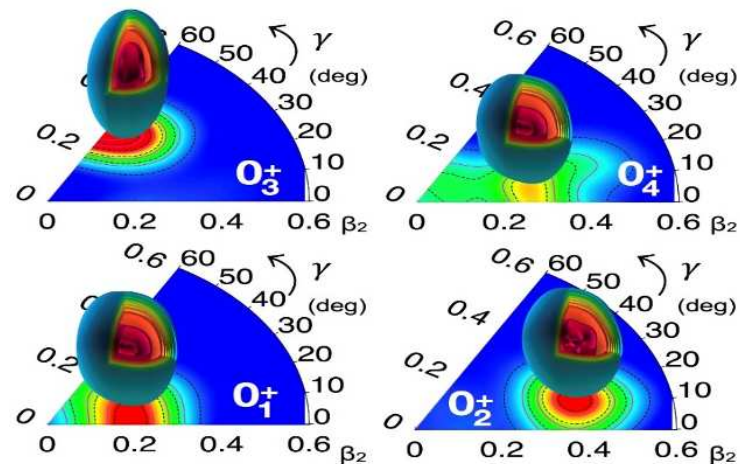


# Nuclear deformation in excited states: Shape coexistence in $A \sim 100$ nuclei

project coordinators: K. Wrzosek-Lipska, M. Zielińska



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## Physics cases studied within the project

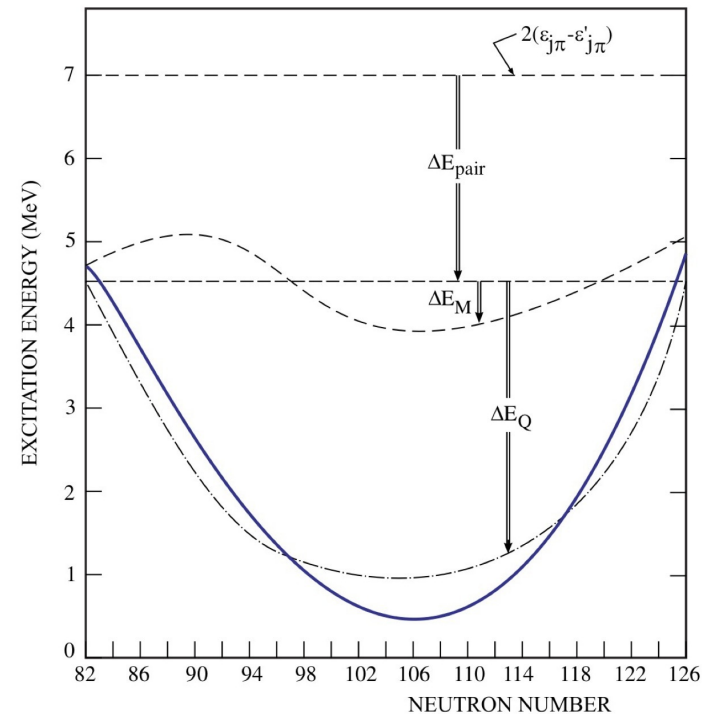
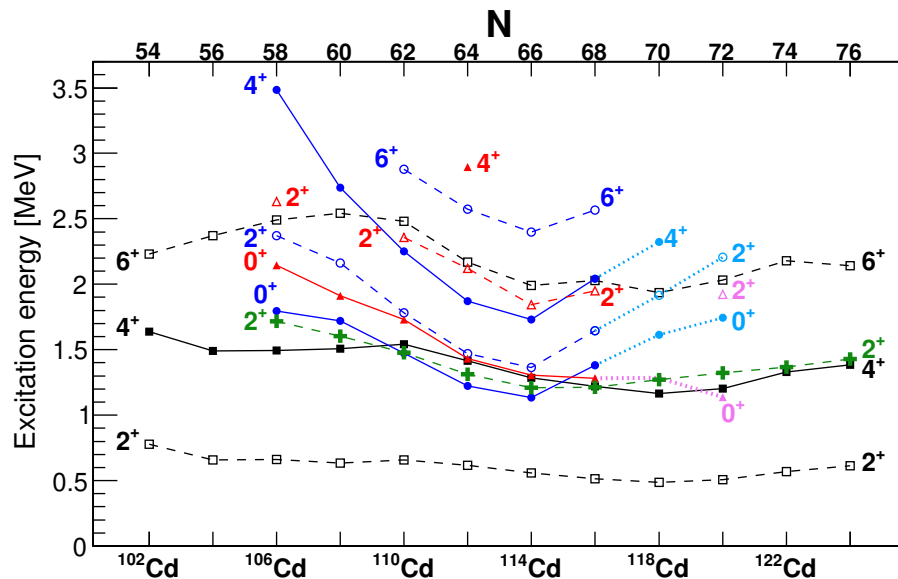
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- **Unsafe Coulomb excitation of  $^{106}\text{Cd}$**  with AGATA at GANIL
  - PhD thesis of D. Kalaydjieva under supervision of M. Zielińska and W. Korten (Université Paris-Saclay, October 2023)
  - Final publication to be submitted to *Eur. Phys. J. A* in the coming weeks
- “Standard” **Coulomb excitation of  $^{110}\text{Cd}$**  at:
  - HIL (EAGLE,  $^{32}\text{S}$  and  $^{14}\text{N}$  beams)
    - MSc project of I. Piętka under supervision of K. Wrzosek-Lipska (University of Warsaw, September 2023)
    - Final publication to be submitted to *Phys. Lett. B* in the coming weeks
  - LNL (AGATA,  $^{60}\text{Ni}$  beam)
    - PhD thesis of I. Piętka under supervision of K. Wrzosek-Lipska and L. Próchniak (University of Warsaw, ongoing)
- “Standard” **Coulomb excitation of  $^{100}\text{Ru}$**  at HIL (EAGLE,  $^{32}\text{S}$  beam)
  - Internship of F.-e. Demyani (PHELMA Grenoble) under supervision of M. Zielińska (Université Paris-Saclay, summer 2024)

# Shapes of Cd nuclei – context

- mid-neutron-shell Cd isotopes used to be considered textbook candidates for spherical vibrational motion based on their energy level schemes that can be arranged into multi-phonon multiplets
- when put into a context of broader systematics, parabolic pattern of level energies is revealed, characteristic for multiparticle-multiphole excitations through a shell gap

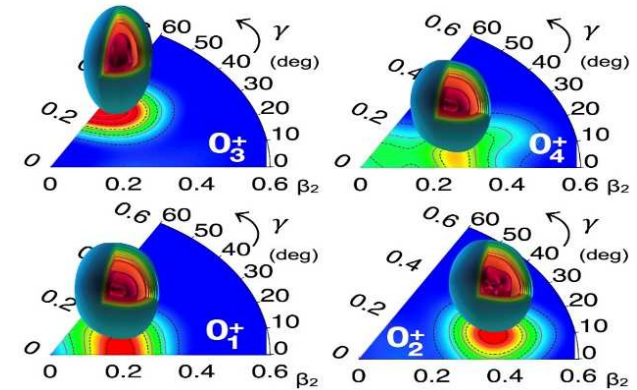
data compilation: P. Garrett, MZ, E. Clément,  
Prog. Part. Nucl. Phys. 124, 103931 (2022)



K. Heyde and J. Wood,  
Rev. Mod. Phys. 83, 1467 (2011)

## Shapes of Cd nuclei – context

- departure from the surface-vibration paradigm towards a multiple shape-coexistence scenario:
  - $\beta$  decay ([TRIUMF](#)) + DSAM lifetime measurements ([Kentucky](#)) in  $^{110,112}\text{Cd}$  with guidance from BMF calculations (P.E. Garrett et al, Phys. Rev. Lett. 123, 142502 (2019))
- data can be reconciled with the vibrational picture using partial dynamical symmetry in the IBM (N. Gavrielov et al, Phys. Rev. C 108, L031305 (2023))
- triggered a multitude of new measurements:
  - high-precision beta decay into  $^{110}\text{Cd}$  ([GRIFFIN, TRIUMF – 2022](#))
  - Coulomb excitation of  $^{110}\text{Cd}$  ([AGATA, LNL](#); [GRETINA, ANL – 2022](#))
- also for neighbouring nuclei, in particular  $^{106}\text{Cd}$ :
  - Coulomb excitation of  $^{106}\text{Cd}$ : ([ReA3, MSU – D. Rhodes et al, Phys. Rev. C 103, L051301 \(2021\)](#)); [GRETINA, ANL – T. Gray et al, Phys. Lett. B 834, 137446 \(2022\)](#))
  - RDDS lifetime measurement in  $^{102-108}\text{Cd}$ : ([AGATA, GANIL – M. Siciliano et al, Phys. Rev. C 104, 034320 \(2021\)](#))

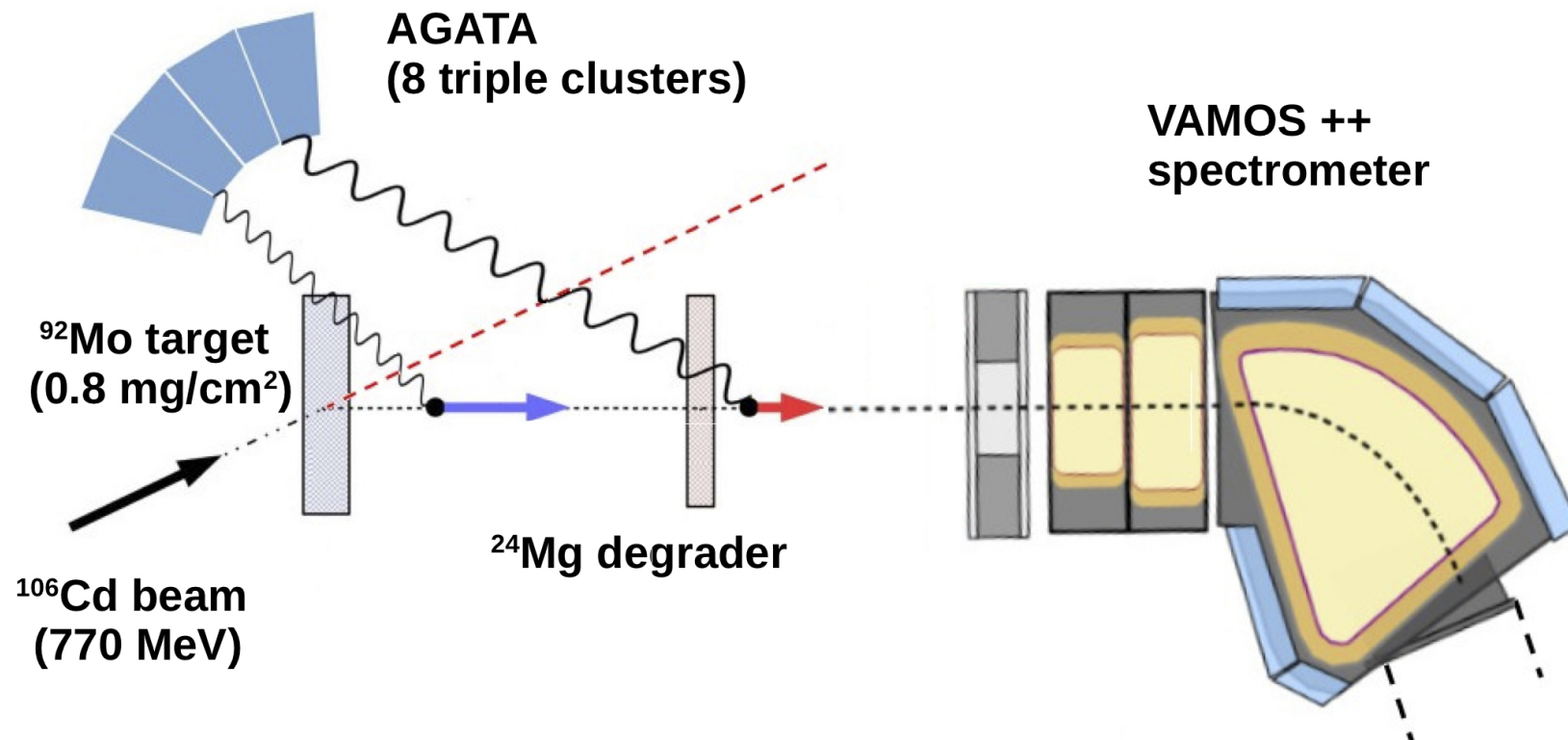


## Unsafe Coulomb excitation of $^{106}\text{Cd}$ at GANIL

- inelastic scattering data on  $^{106}\text{Cd}$ : byproduct of a RDDS lifetime measurement following multinucleon transfer in the  $^{106}\text{Cd} + ^{92}\text{Mo}$  reaction at 7 MeV/A

M. Siciliano et al., Phys. Lett. B 806, 135474 (2020)

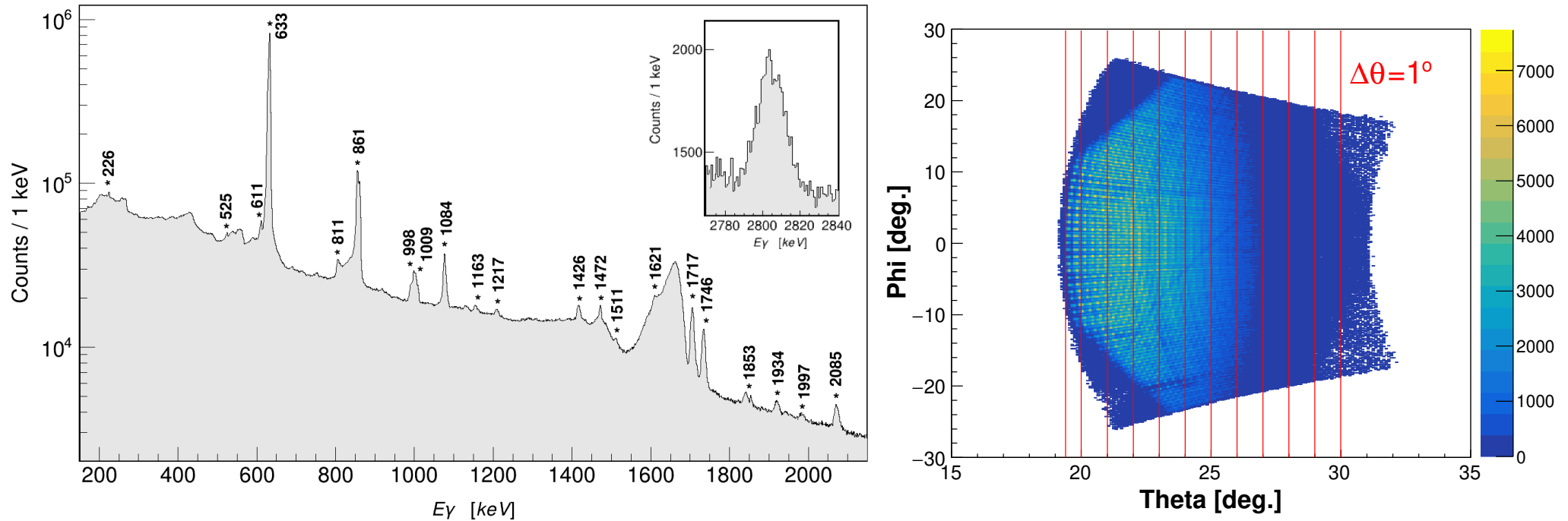
M. Siciliano et al., Phys. Rev. C 104, 034320 (2021)



- VAMOS at grazing angle ( $25^\circ$ ); lowest observed scattering angle ( $19.4^\circ$ ) corresponding to 107% of Cline's safe energy

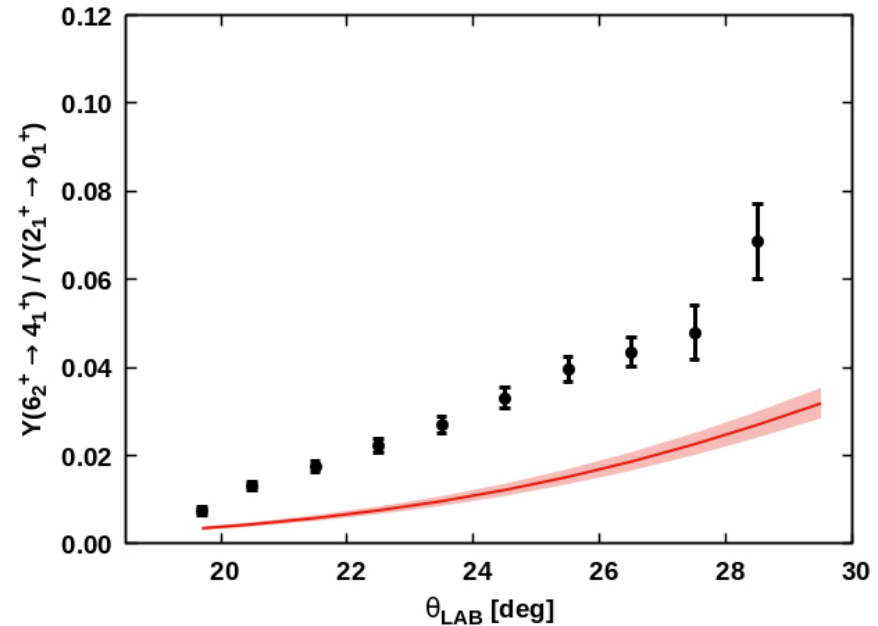
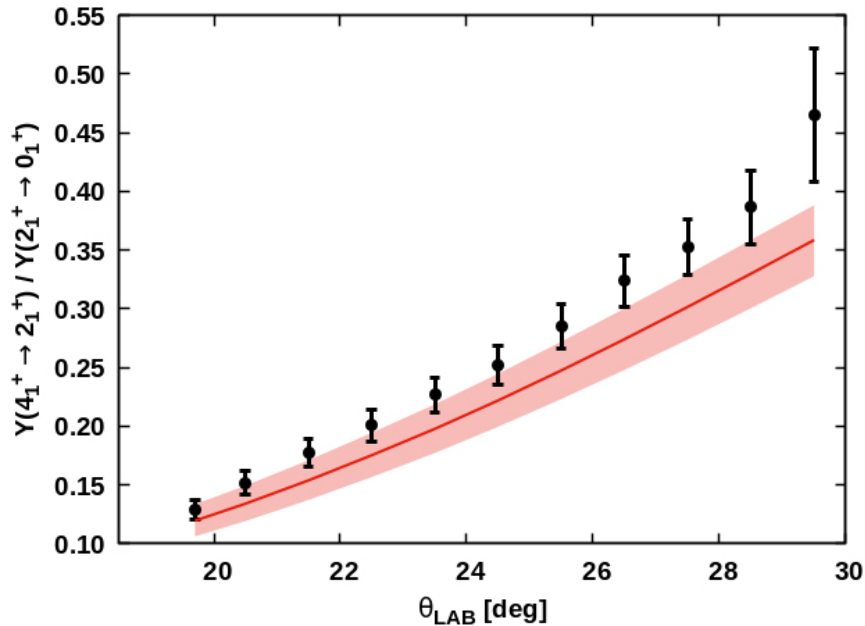
# Unsafe Coulomb excitation of $^{106}\text{Cd}$ at GANIL

- population of 21 excited states observed (up to spin  $6^+$ )



- $^{106}\text{Cd}$  ions identified in VAMOS with  $19.4^\circ \leq \theta_{\text{LAB}} \leq 30^\circ$  (Cline's criterion fulfilled for  $\theta_{\text{LAB}} \leq 18^\circ$ )
- we apply gates on  $\theta_{\text{LAB}}$  with  $1^\circ$  width to study the dependence of the excitation cross sections on scattering angle
- due to complicated acceptance of the spectrometer as a function of  $\theta$ , we normalise the measured  $\gamma$ -ray intensities to that of the  $2_1^+ \rightarrow 0_1^+$  transition

## Sample results (strongly populated states)

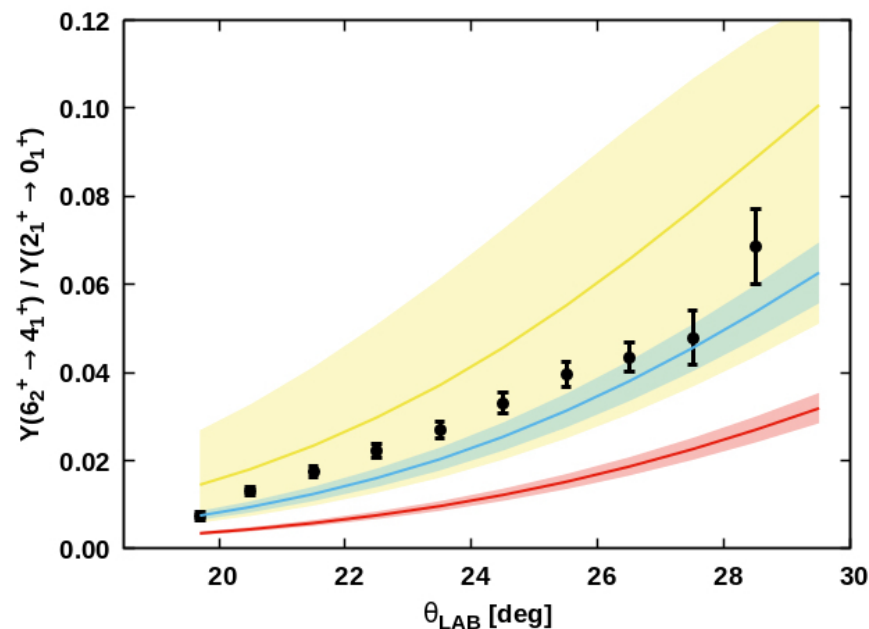
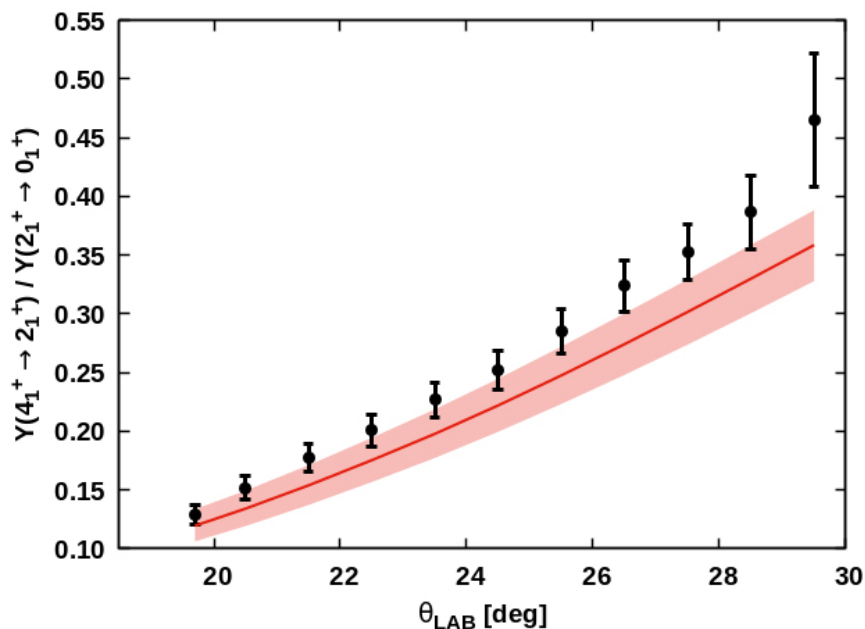


- reasonable agreement with literature data for  $4_1^+$  (weighted average of measured lifetimes)
- lifetime of the  $6_2^+$  state deduced from the same data as our transition intensities (M. Siciliano et al., Phys. Rev. C 104, 034320 (2021)) is not consistent with the measured intensity ratios

D. Kalaydjieva, PhD thesis, 2023



## Sample results (strongly populated states)

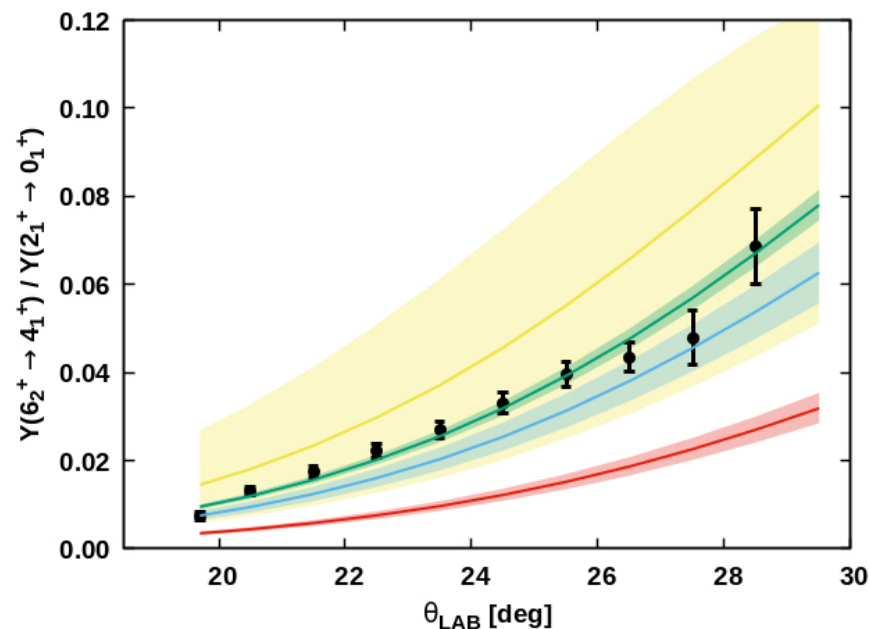
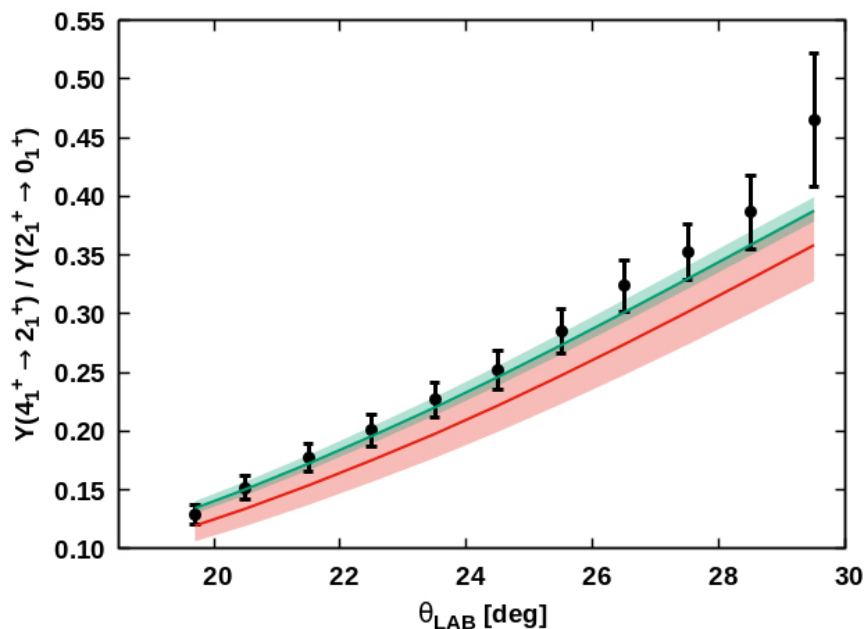


- much better agreement for the  $6_2^+$  state if we assume:
  - $\langle 6_2^+ || E2 || 4_1^+ \rangle$  matrix element from Coulomb excitation ( D. Rhodes et al., Phys. Rev. C 103, L051301 (2021))
  - or  $6_2^+$  lifetime from  $(n, n'\gamma)$  (A. Linnemann, PhD thesis, University of Cologne, 2005 — but here the uncertainty is very large ( $\tau = 0.26^{+0.44}_{-0.14}$  ps))

D. Kalaydjieva, PhD thesis, 2023



## Sample results (strongly populated states)



- finally, we can try to fit a set of matrix elements to the first few points of the cross-section distribution, and compare the resulting lifetimes:

$4_1^+$  – GOSIA fit: **1.23(7) ps**

weighted average of lifetimes:

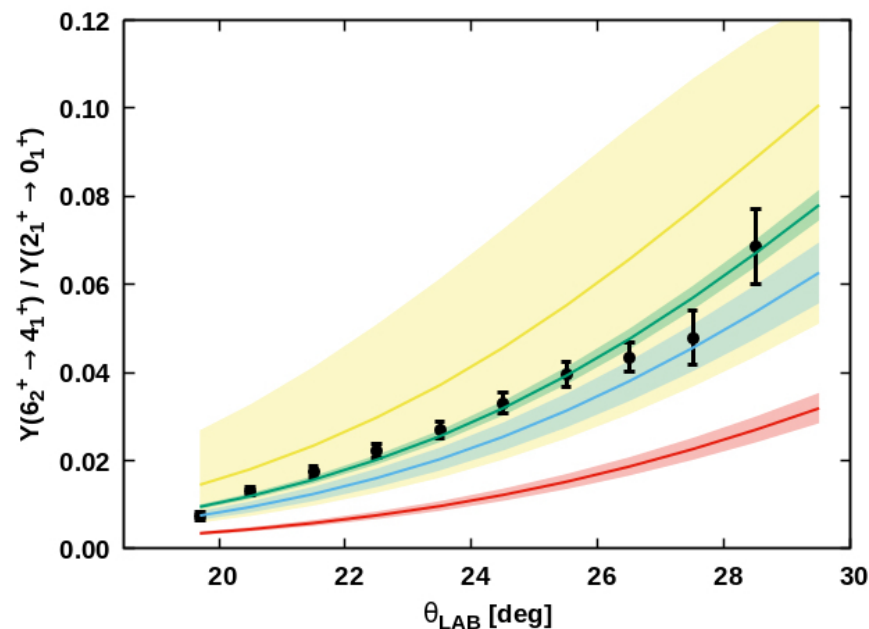
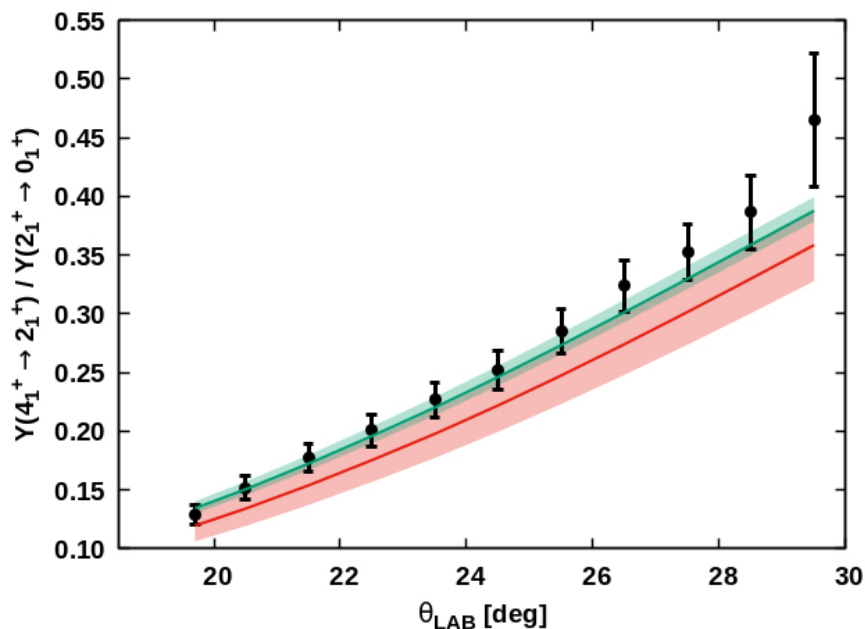
**1.32(12) ps**

$6_2^+$  – GOSIA fit: **0.48(3) ps**

M. Siciliano et al., Phys. Rev. C 104,  
034320 (2021): **1.22(15) ps**

D. Rhodes et al., Phys. Rev. C 103,  
L051301 (2021): **0.54(8) ps**

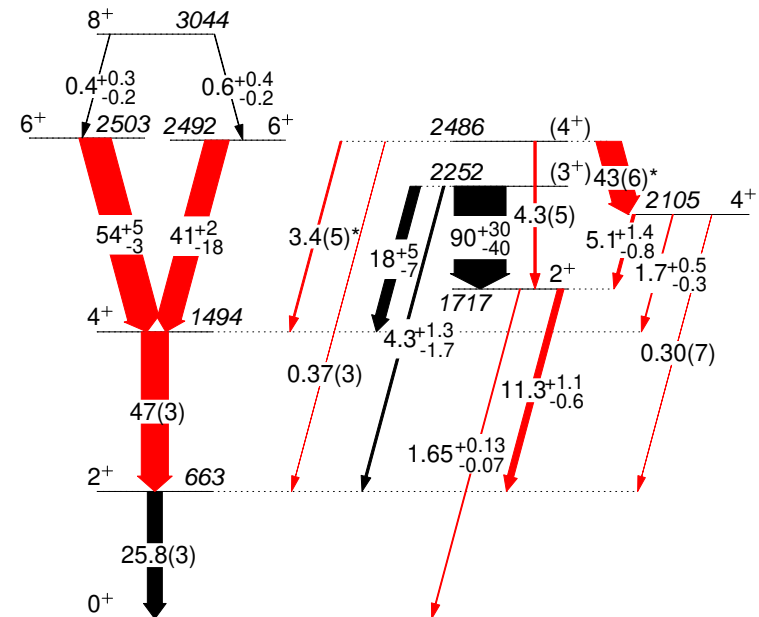
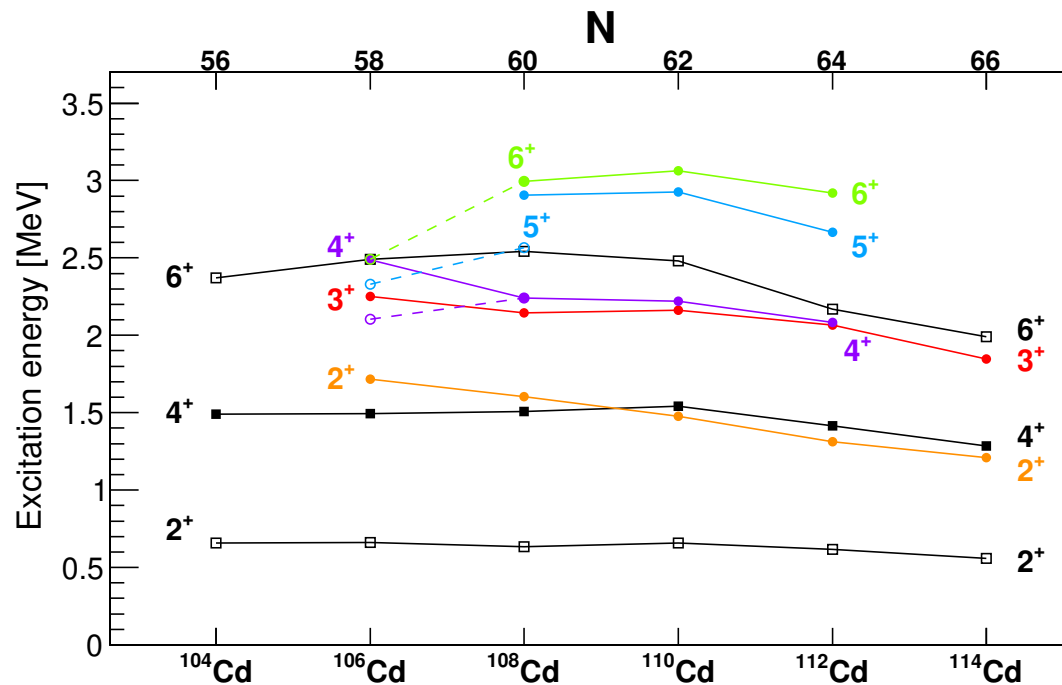
## Sample results (strongly populated states)



- similar analysis has been applied to all observed states, yielding B(E2) values complementary to those obtained from the RDDS analysis of the same date
- contrary to RDDS, it was possible to obtain B(E2) values for the decay of states that have lifetimes shorter than 1 ps

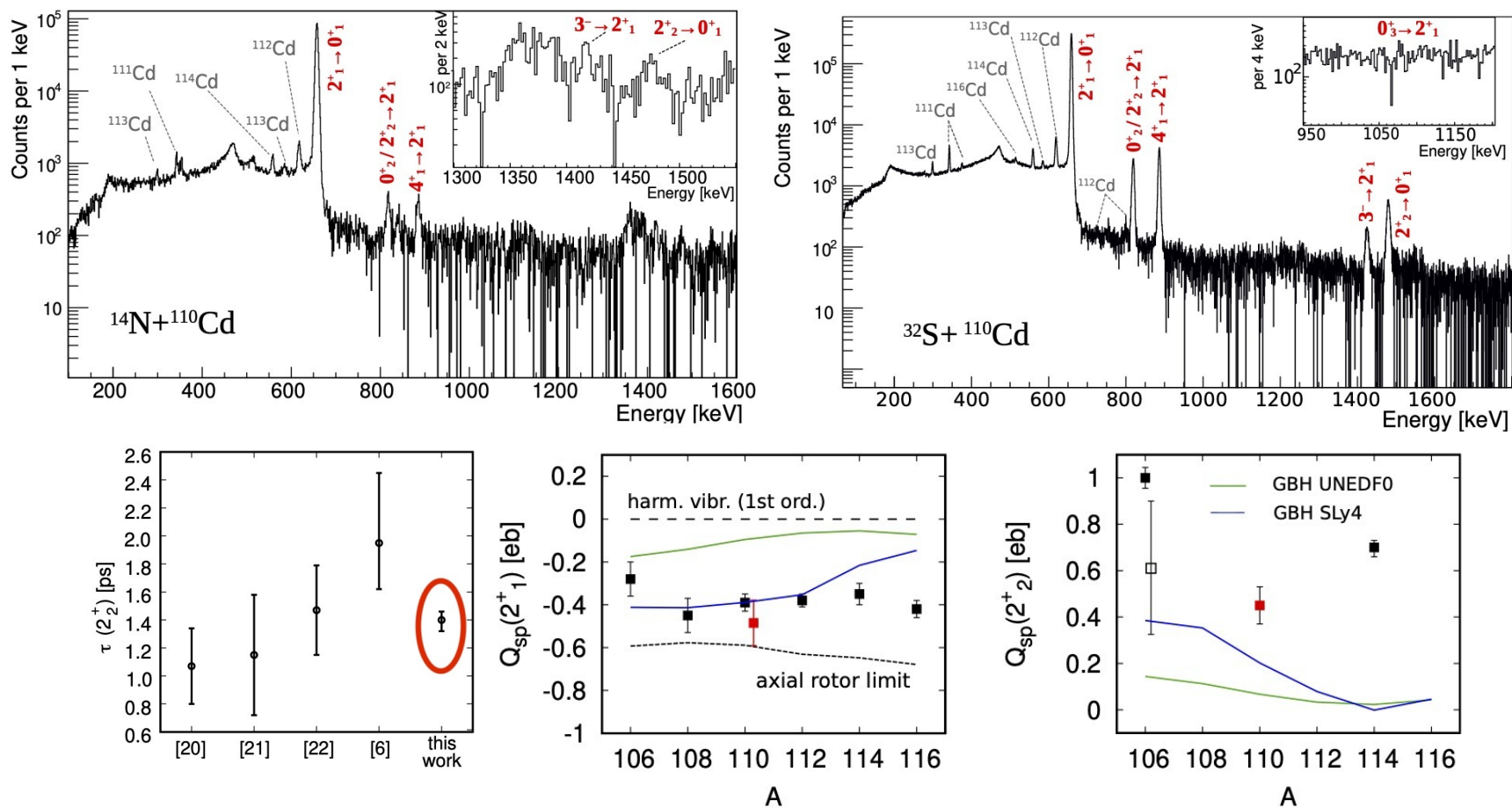
D. Kalaydjieva, PhD thesis, 2023

# Proposed reorganisation of the $^{106}\text{Cd}$ level scheme



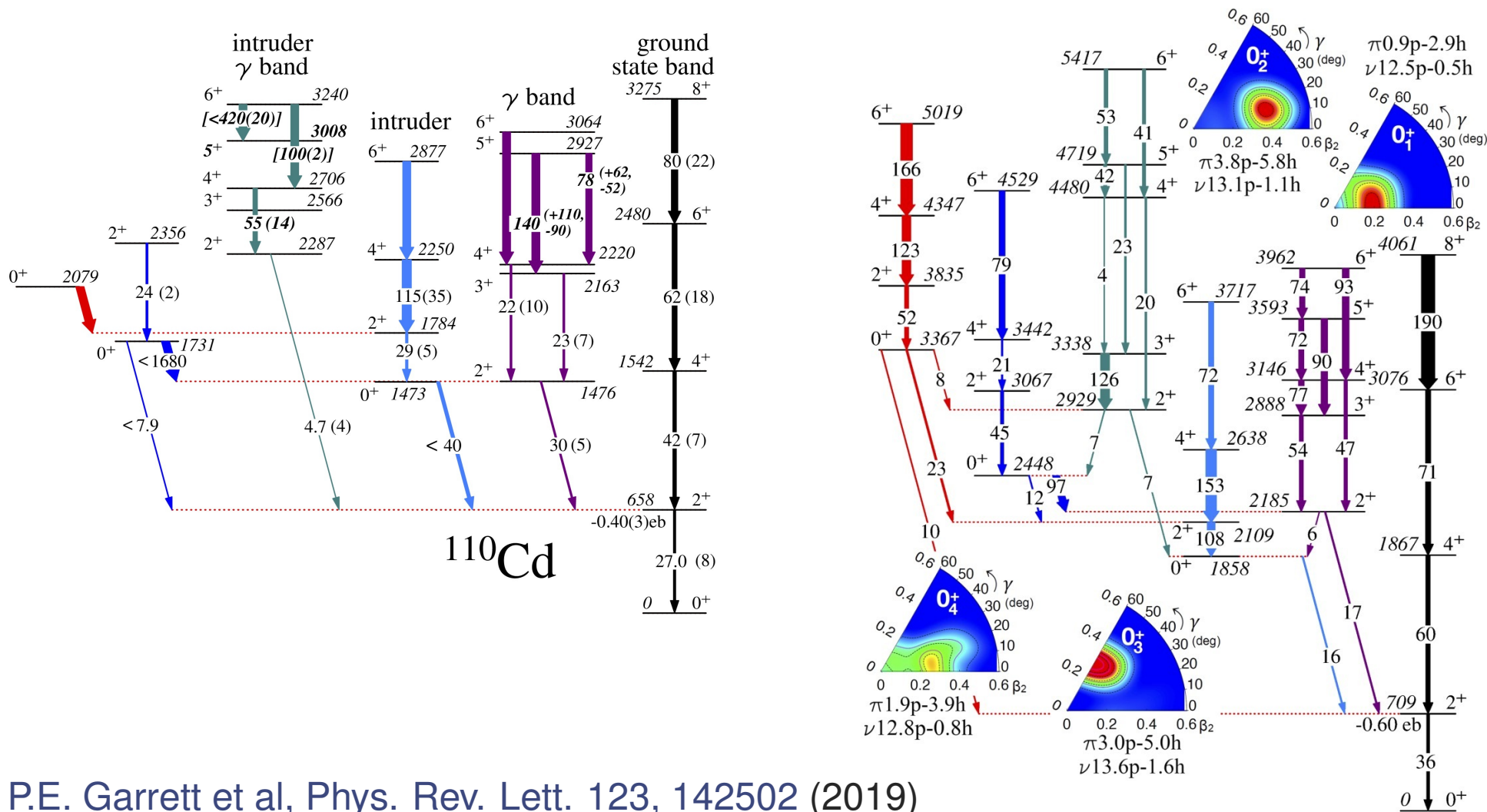
- new  $K=2$   $3^+$  and  $4^+$  and  $K=4$   $4^+$  band members proposed that have expected decay patterns and excitation energies consistent with the systematics
- closely spaced  $6^+$  states suggested to result from a strong mixing of the rotational band member with a seniority state
- non-observation of the 2252-keV state in the present data supports its  $3^+$  spin-parity (Coulomb excitation of odd-spin positive parity states is strongly hindered)
- firm spin assignments will be obtained from a high-statistics  $\beta$  decay study into  $^{106}\text{Cd}$  recently approved at TRIUMF

# Coulomb excitation of $^{110}\text{Cd}$ at HIL Warsaw: EAGLE + 48 PIN diodes



- precise  $2_2^+$  lifetime (I. Piętka et al, to be submitted to Acta Phys. Pol. B)
- first determination of the  $2_2^+$  quadrupole moment – value inconsistent with a two-phonon structure (K. Wrzosek-Lipska et al, to be submitted to Phys. Lett. B)

# Shape coexistence in Cd isotopes: BMF predictions

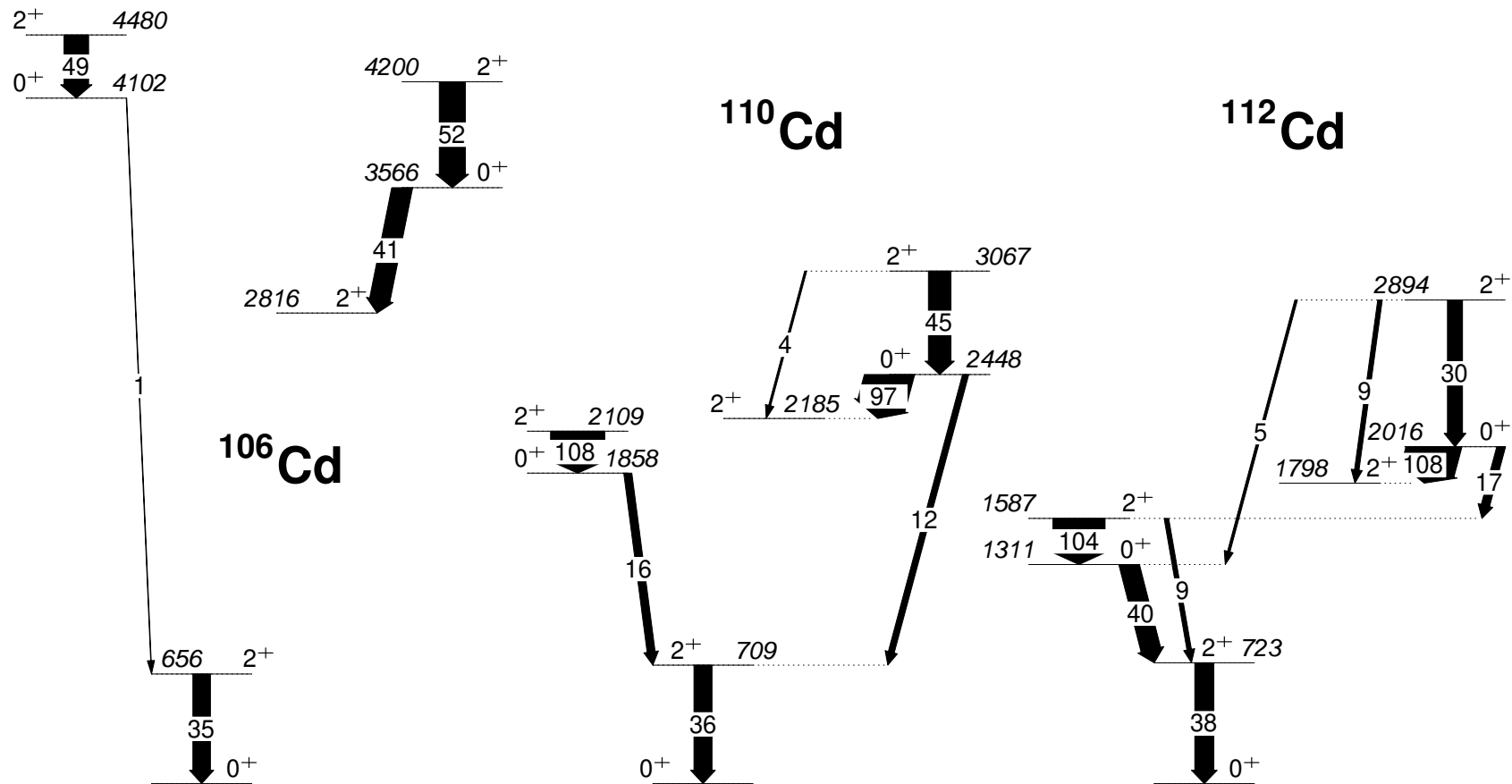


P.E. Garrett et al, Phys. Rev. Lett. 123, 142502 (2019)

calculations: T.R. Rodriguez, symmetry-conserving configuration-mixing method (SCCM) with Gogny D1S

# Shape coexistence in Cd isotopes: BMF predictions

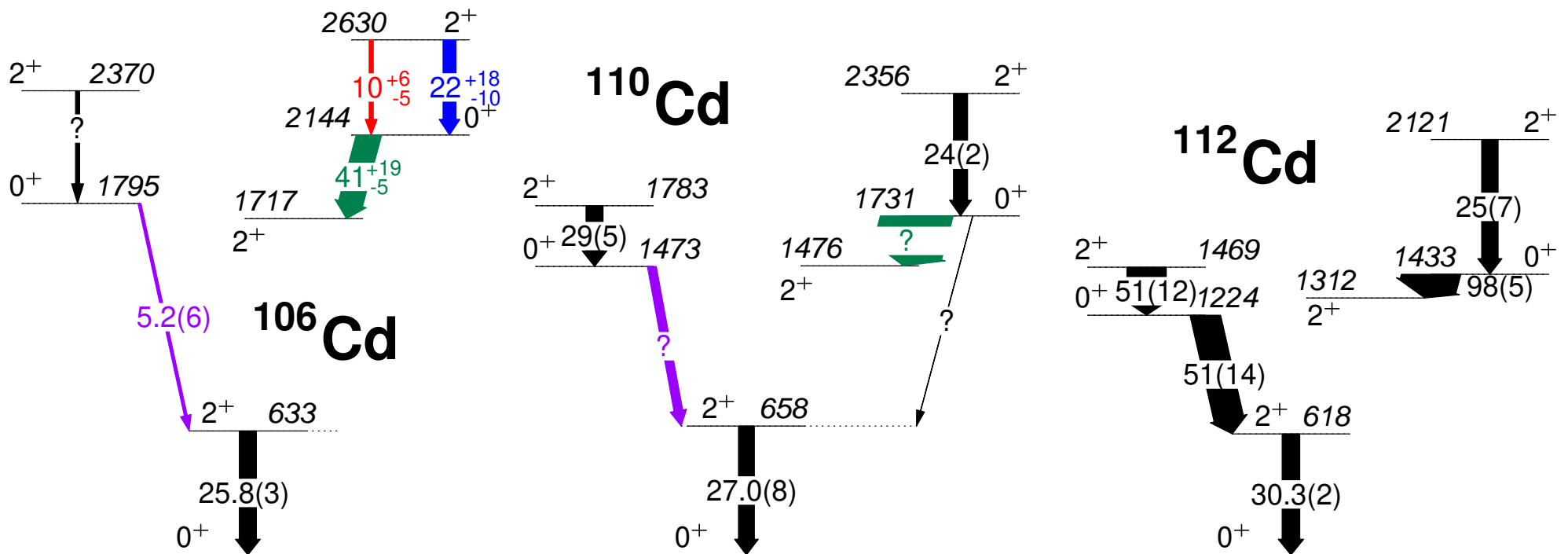
- similar shape-coexisting structures as in  $^{110,112}\text{Cd}$  are predicted in  $^{106}\text{Cd}$
- in-band transition strength in the oblate structure predicted to increase with decreasing  $N$ , while the  $B(E2; 0_3^+ \rightarrow 2_2^+)$  value decreases



SCCM calculations: T.R. Rodriguez

# Coulomb-excitation results

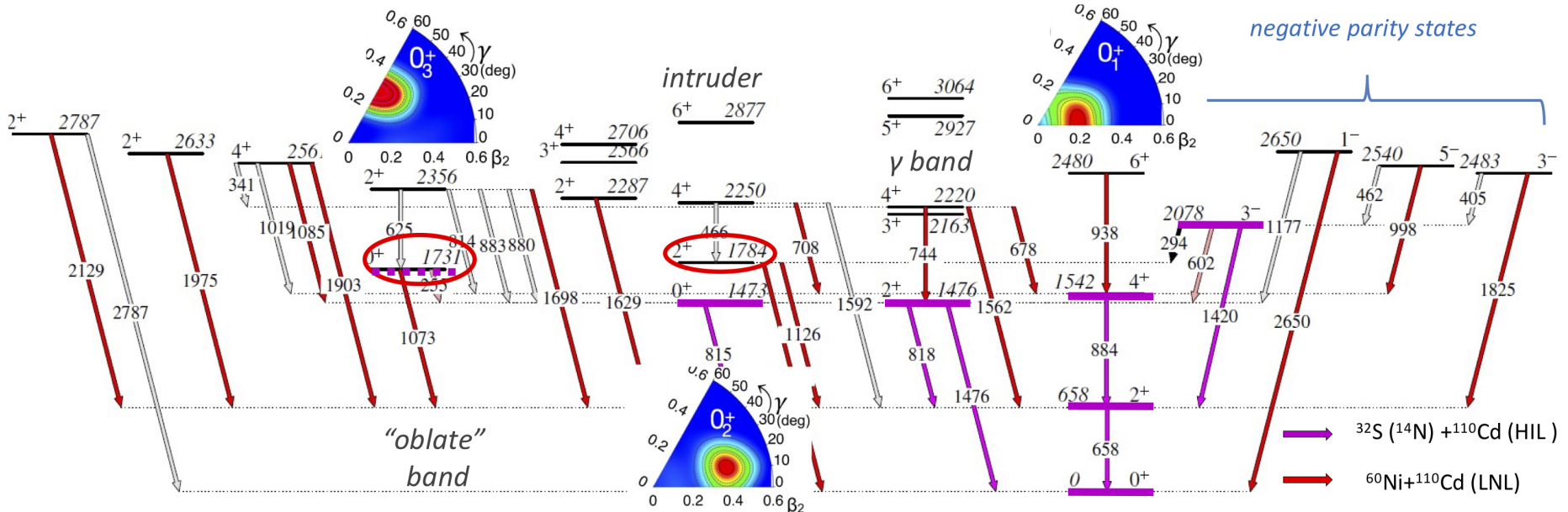
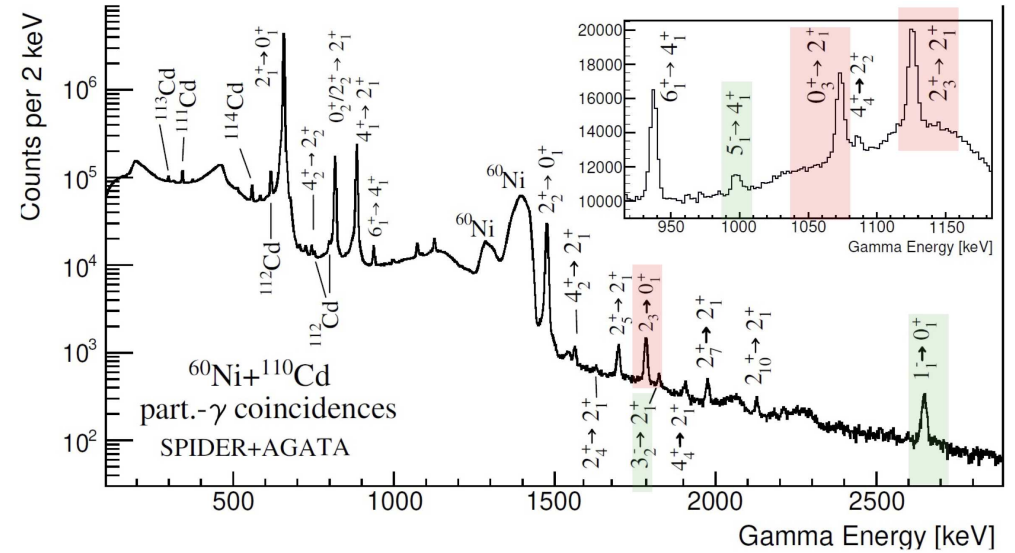
- decay of the **presumably prolate  $0_2^+$  state** in  $^{106,110}\text{Cd}$  agrees well with the SCCM prediction
- similar for the decay of the **presumably oblate  $0_3^+$  state** in  $^{106,110}\text{Cd}$ , but the in-band transition strength has a different trend
  - larger  $B(E2; 2_5^+ \rightarrow 0_3^+)$  (similar to that in the ground-state band) if the branching ratio from [A. Linnemann PhD \(Cologne, 2005\)](#) is assumed instead of the more precise value from [T. Schmidt PhD \(Cologne, 2019\)](#)





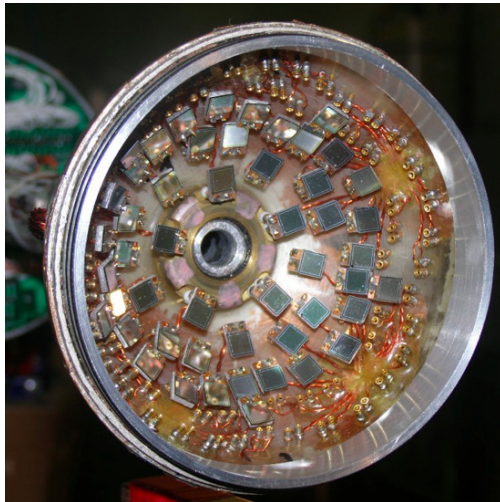
# AGATA experiment on $^{110}\text{Cd}$ (LNL)

- 5 days of  $^{60}\text{Ni}$  beam with AGATA + SPIDER (May + October 2022)
- aim: determination of  $\beta$  and  $\gamma$  parameters of  $0_1^+$ ,  $0_2^+$  and  $0_3^+$  states in  $^{110}\text{Cd}$  using quadrupole sum rules



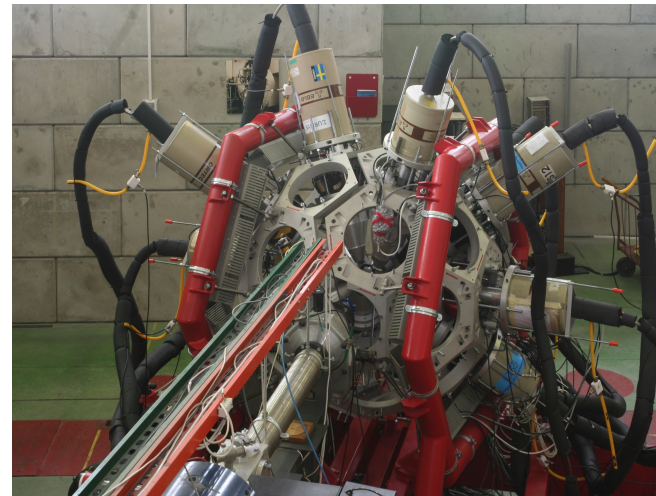
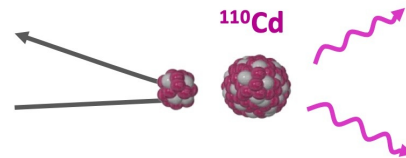
data analysis: PhD thesis of I. Piętka, University of Warsaw, ongoing

# Coulomb excitation of $^{100}\text{Ru}$ at HIL Warsaw

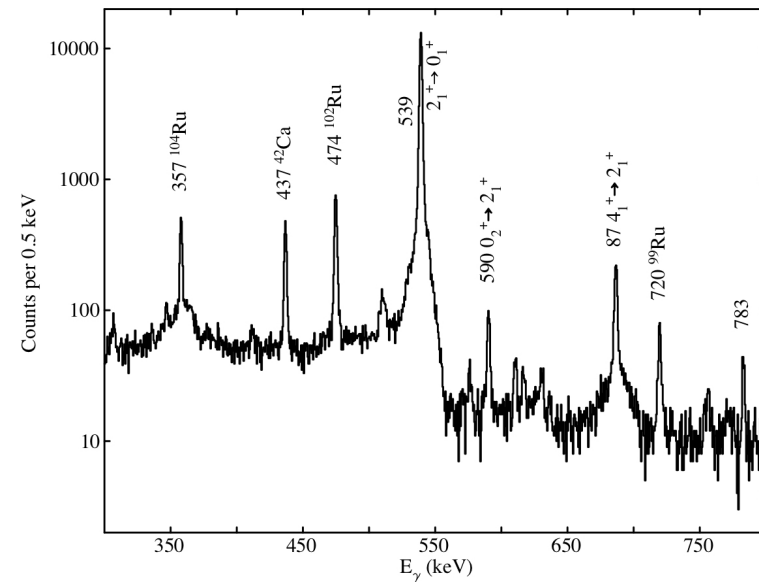


EAGLE + 48 PIN diodes

$^{32}\text{S}$  beam at 83 MeV



- analysis: internship of F.-e. Demyani at CEA
- preliminary results:
  - $Q_s(2_1^+)$  compatible with one of conflicting literature values
  - first determination of  $B(E2; 0_2^+ \rightarrow 2_1^+)$



## Outlook: studies of $^{112}\text{Cd}$

- Coulomb-excitation study of  $^{112}\text{Cd}$  at the Maier-Leibnitz Laboratory (Munich, Germany) using a  $^{12}\text{C}$  beam and a Q3D magnetic spectrograph (analysis completed): verification of lifetimes of  $2^+$  states and  $B(E3; 3_1^- \rightarrow 0_1^+)$  strength
- $\beta$  decay of  $^{112}\text{Ag}$  and  $^{112}\text{In}$  into  $^{112}\text{Cd}$  (TRIUMF, approved;  $^{112}\text{Ag}$  decay scheduled next week): precision branching ratios and E2/M1 transition mixing ratios
- Coulomb-excitation study of  $^{112}\text{Cd}$  with a  $^{60}\text{Ni}$  beam (AGATA at LNL – presented at the recent pre-PAC workshop, will be submitted to the PAC in the coming weeks)
- complementary measurement at HIL with a  $^{32}\text{S}$  beam under consideration

