
Nuclear deformation in excited states - Superdeformation at low spins

task coordinators: E. Clément, K. Hadyńska-Klęk (P. Napiorkowski*)

GANIL

Kasia Hadyńska-Klęk

Heavy Ion Laboratory
University of Warsaw



HIL
Heavy Ion Laboratory



COPIGAL mini-WORKSHOP

28-29 November 2024

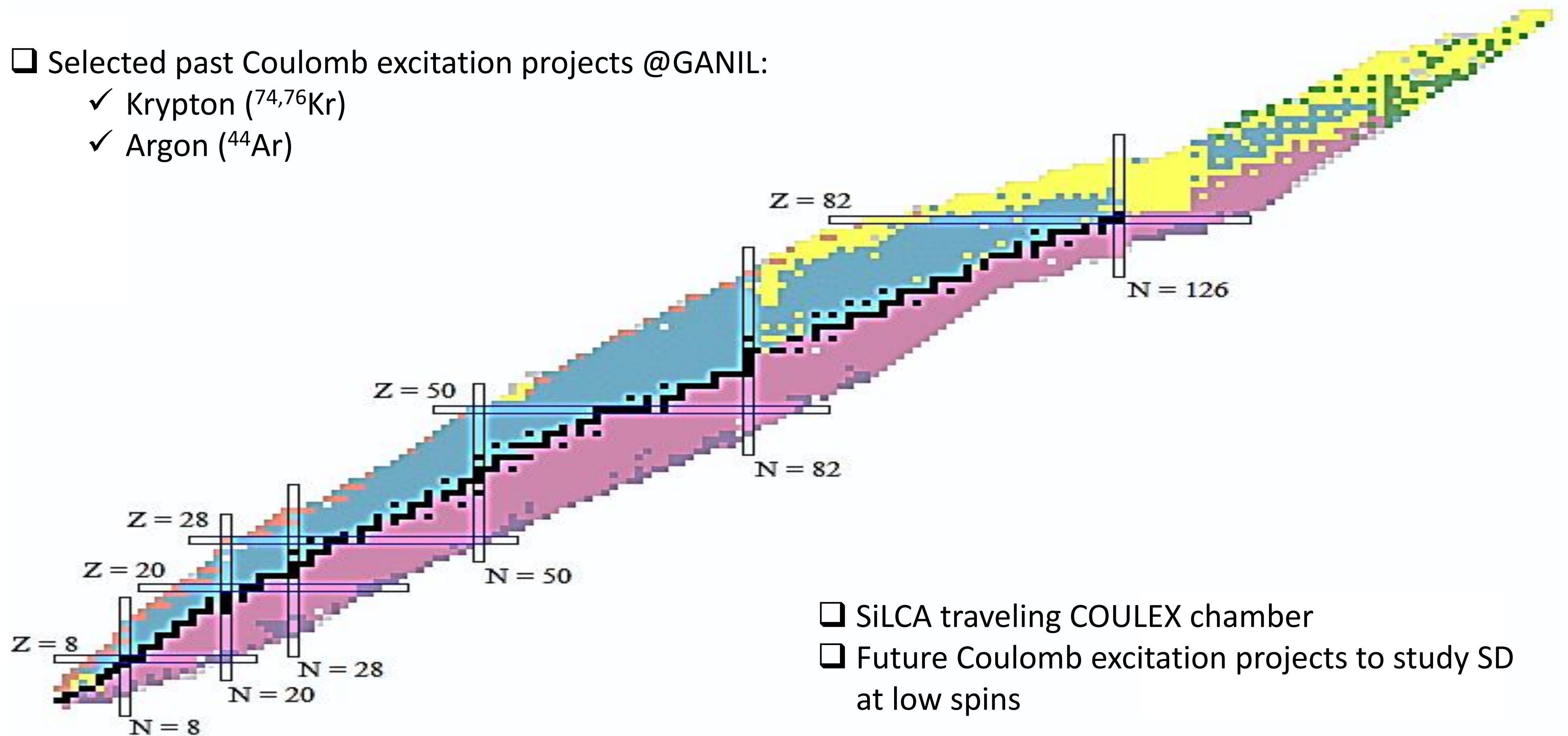
Paris, France

Outline

□ Selected past Coulomb excitation projects @GANIL:

✓ Krypton ($^{74,76}\text{Kr}$)

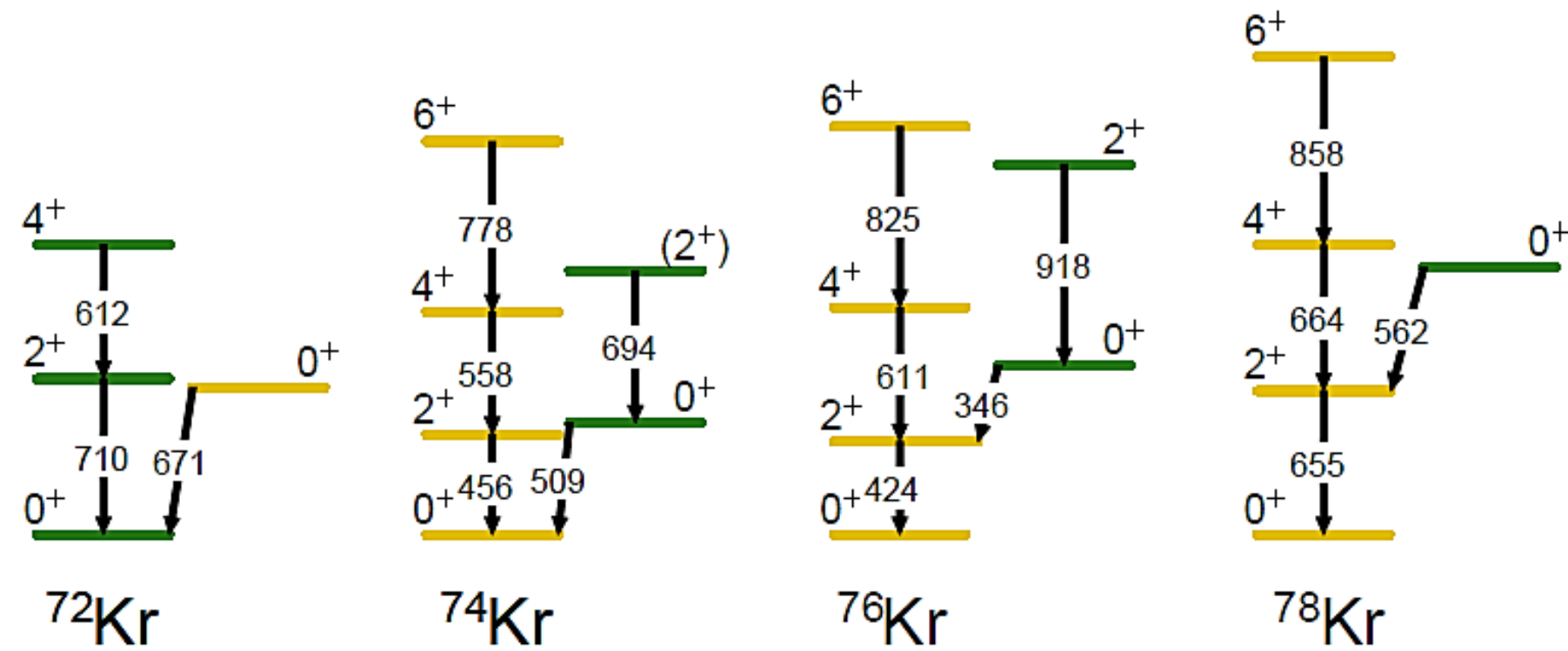
✓ Argon (^{44}Ar)



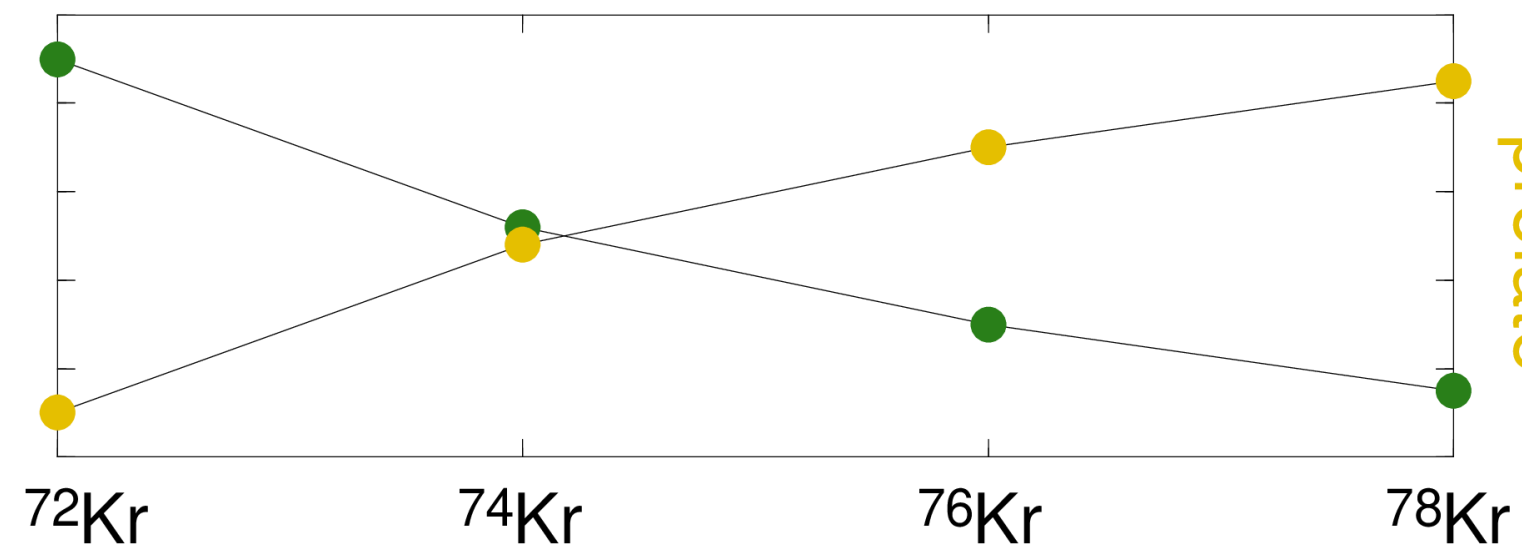
□ SiLCA traveling COULEX chamber

□ Future Coulomb excitation projects to study SD at low spins

Shape coexistence in $^{74,76}\text{Kr}$ @ GANIL [E344S, June 2002+April 2003]



oblate

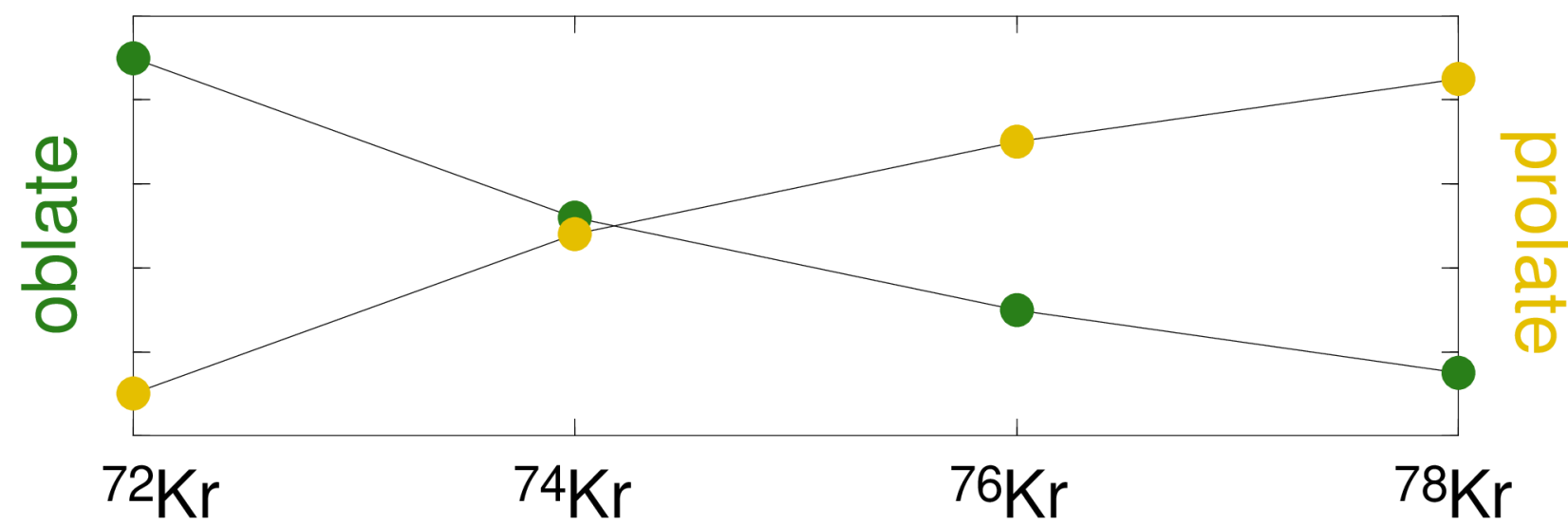
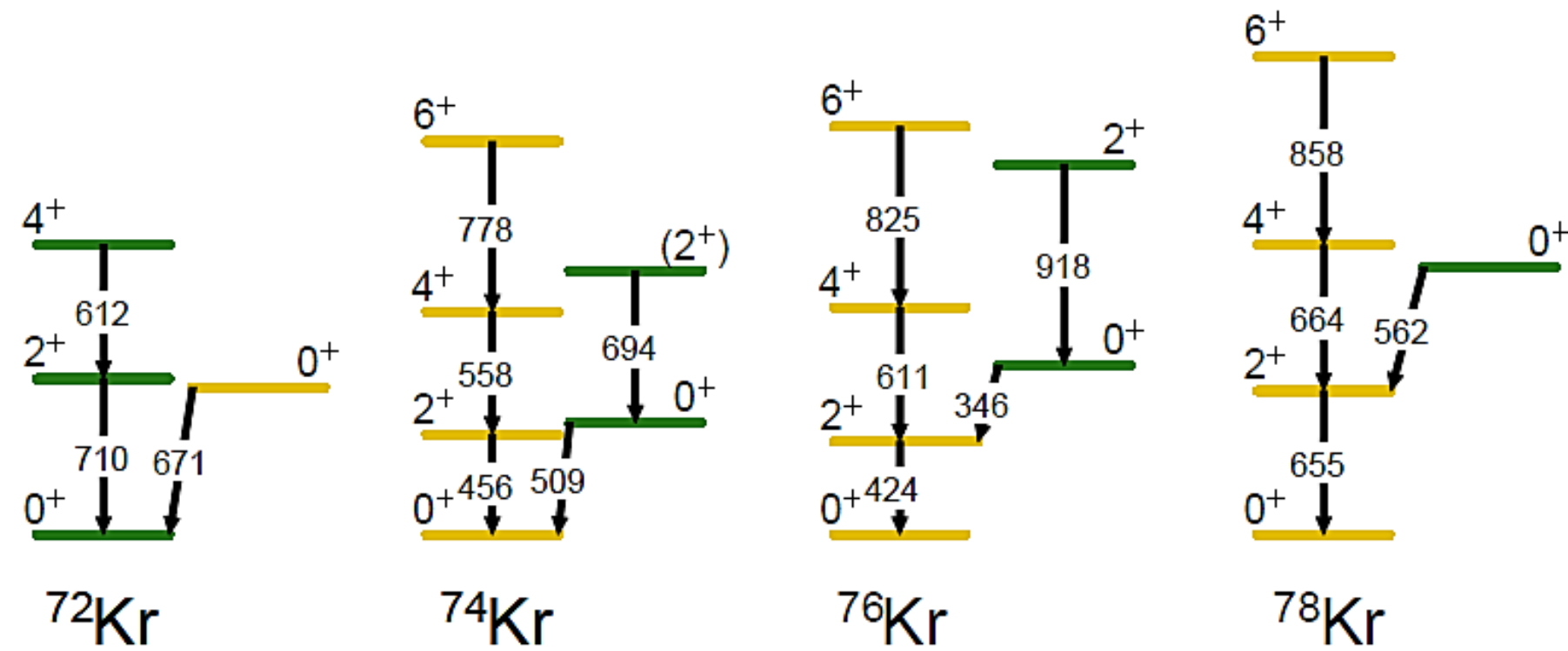


prolate

mixing of 0^+ states deduced from distortion of rotational bands
(E. Bouchez et al. Phys. Rev. Lett. 90, 082502 (2003))

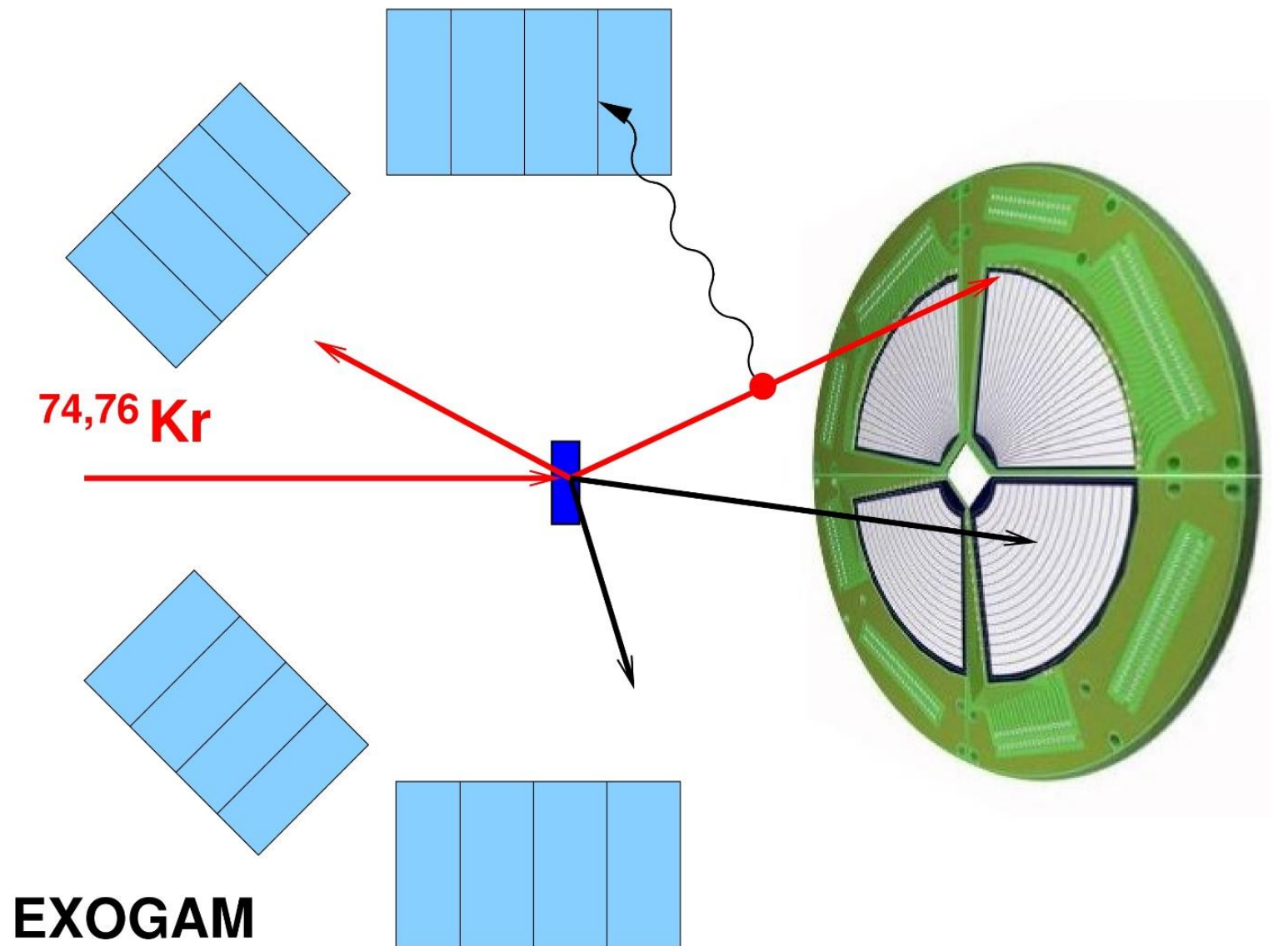
inversion of the ground state and excited 0^+ states

Shape coexistence in $^{74,76}\text{Kr}$ @ GANIL [E344S, June 2002+April 2003]



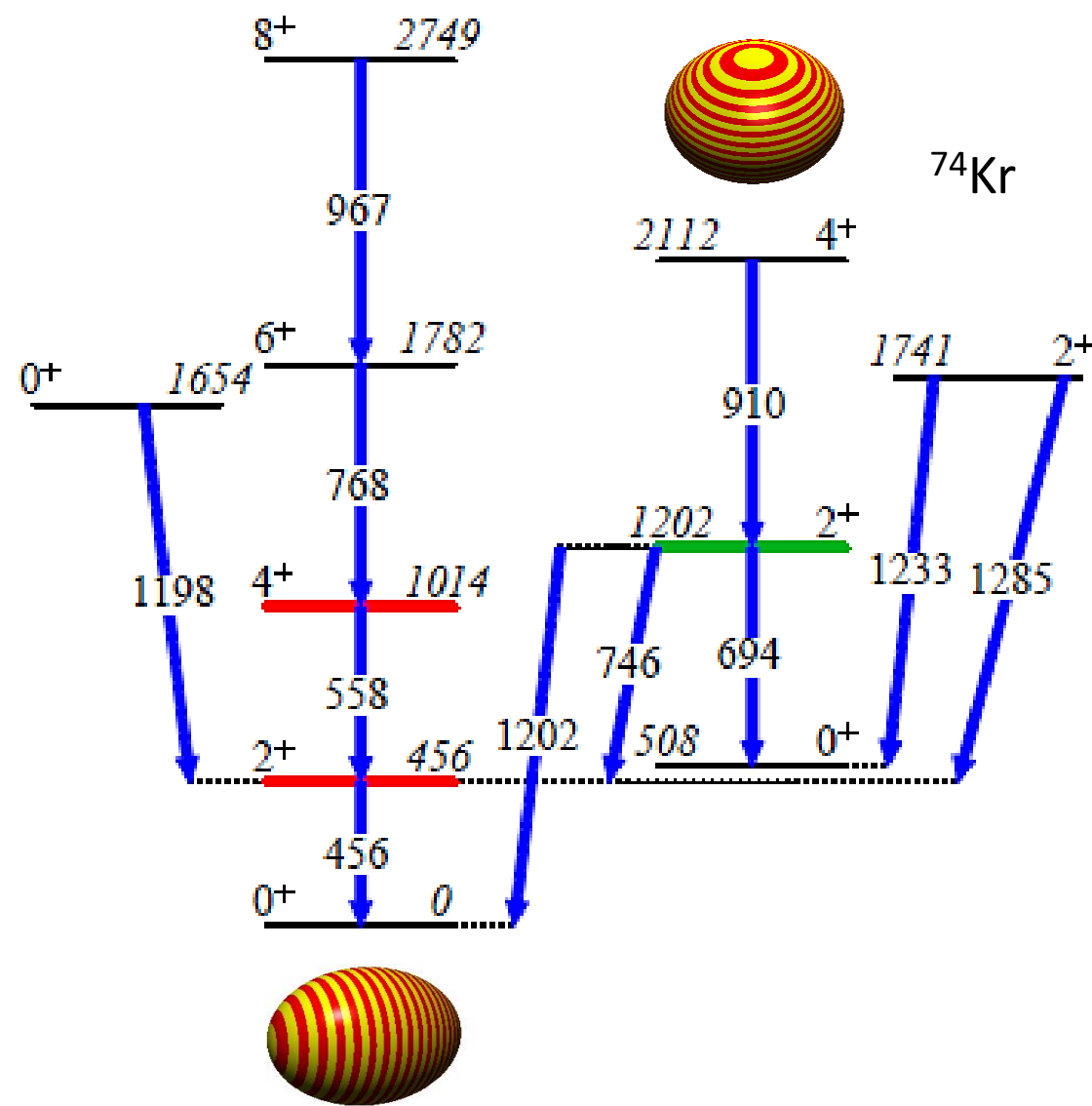
mixing of 0^+ states deduced from distortion of rotational bands
(E. Bouchez et al. Phys. Rev. Lett. 90, 082502 (2003))

inversion of the ground state and excited 0^+ states



Coulomb excitation to directly determine nuclear shapes in $^{74,76}\text{Kr}$ using SPIRAL beams

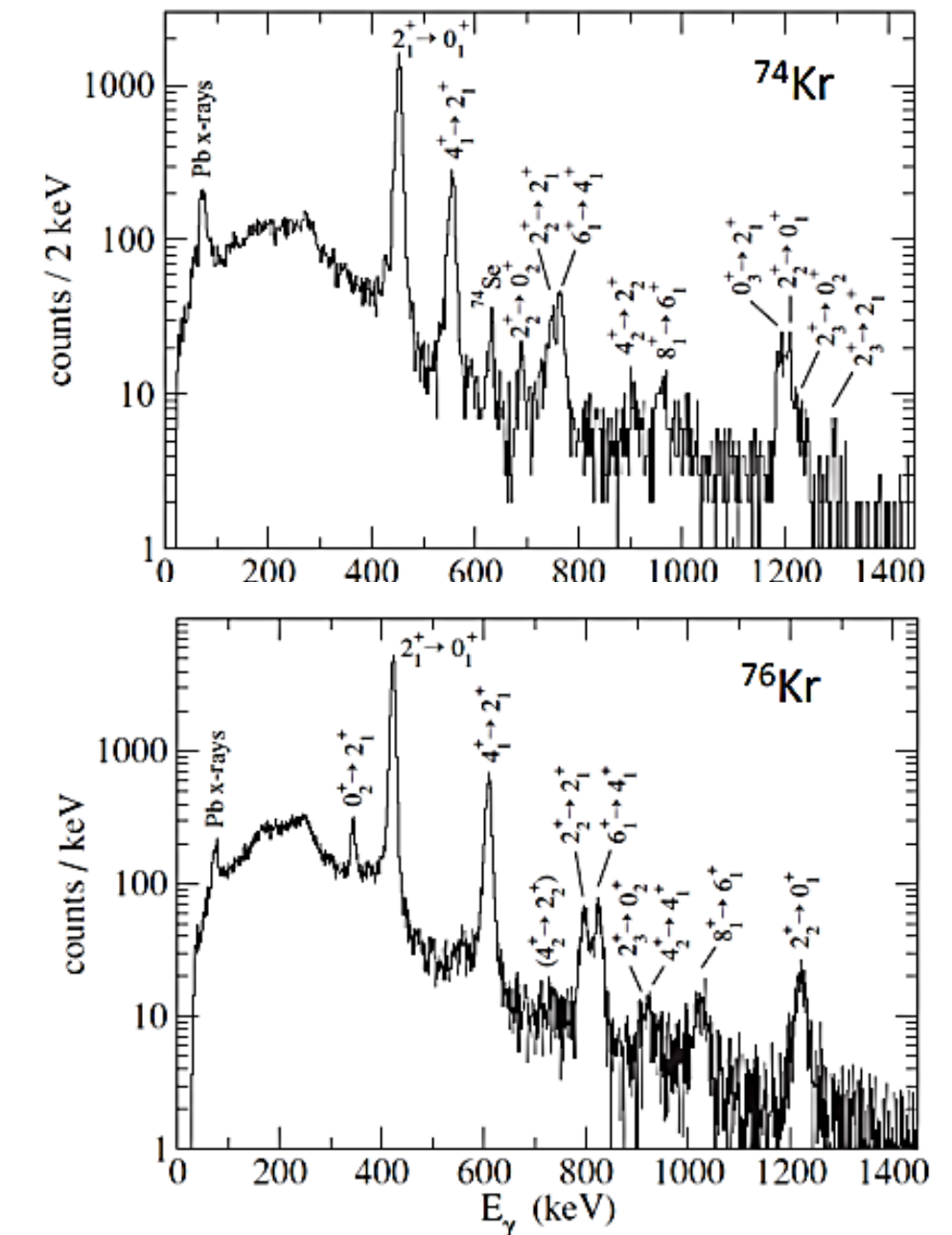
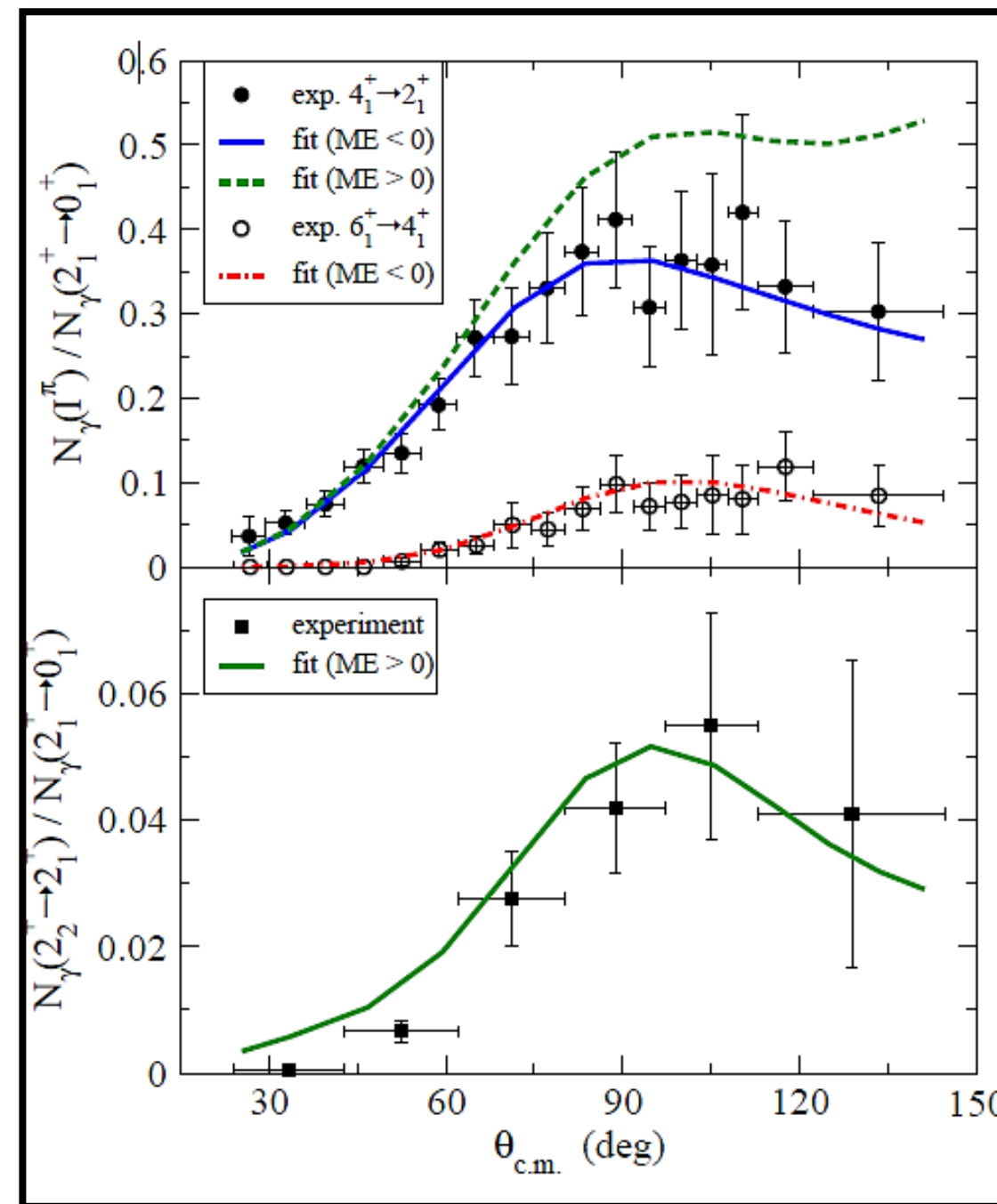
Shape coexistence in $^{74,76}\text{Kr}$ @ GANIL - quadrupole moments



$$\langle 2_1^+ || E2 || 2_1^+ \rangle = -0.70_{-0.30}^{-0.33}$$

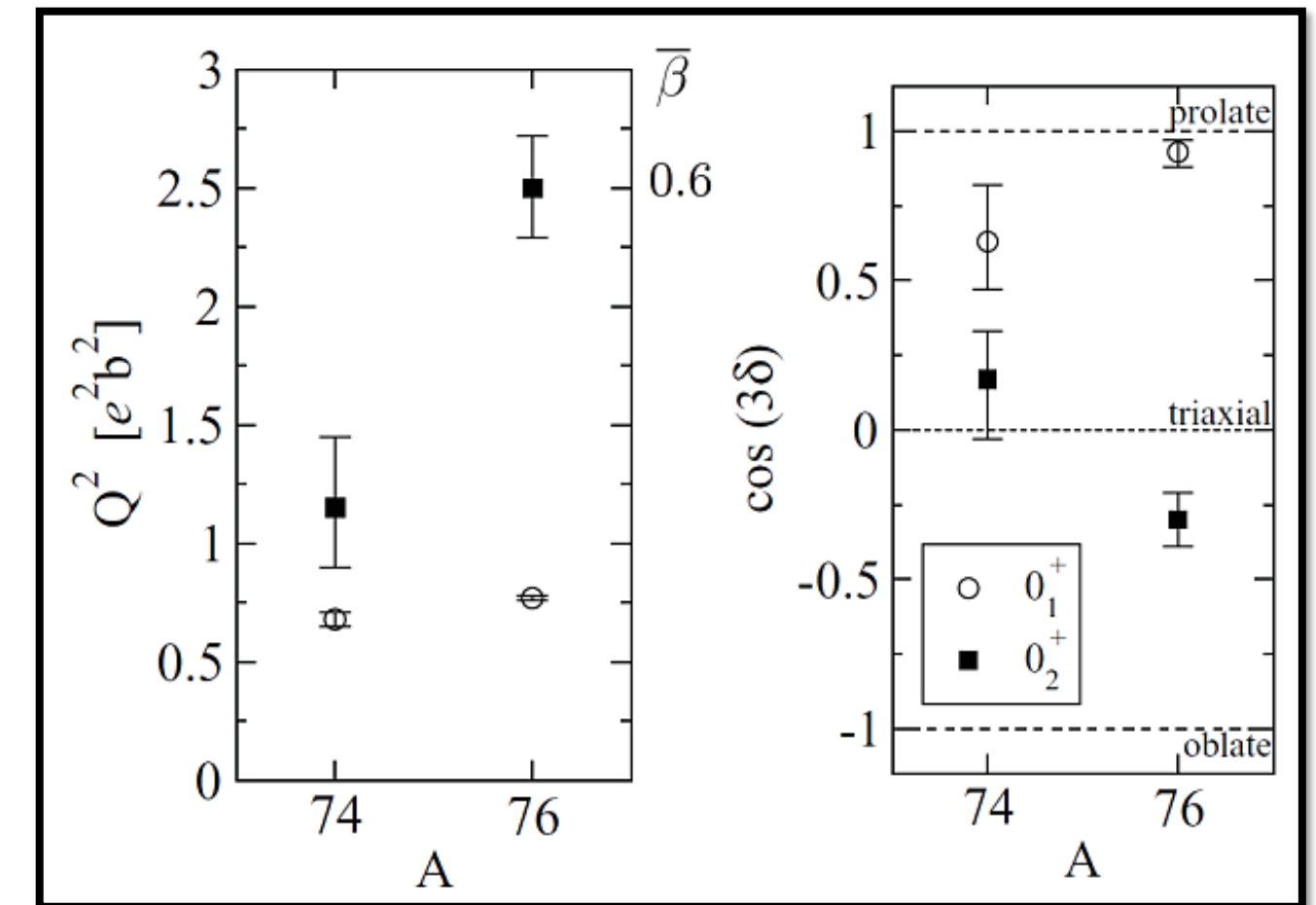
$$\langle 4_1^+ || E2 || 4_1^+ \rangle = -1.02_{-0.21}^{+0.59}$$

$$\langle 2_2^+ || E2 || 2_2^+ \rangle = +0.33_{-0.23}^{+0.28}$$



- first determination of quadrupole moments of excited nuclear states using Coulomb excitation of a radioactive beam
- confirmation of the shape-coexistence scenario
- mixing coefficients obtained from measured transition probabilities consistent with those from level energies

Shape coexistence in $^{74,76}\text{Kr}$ @ GANIL - sum rules and BMF



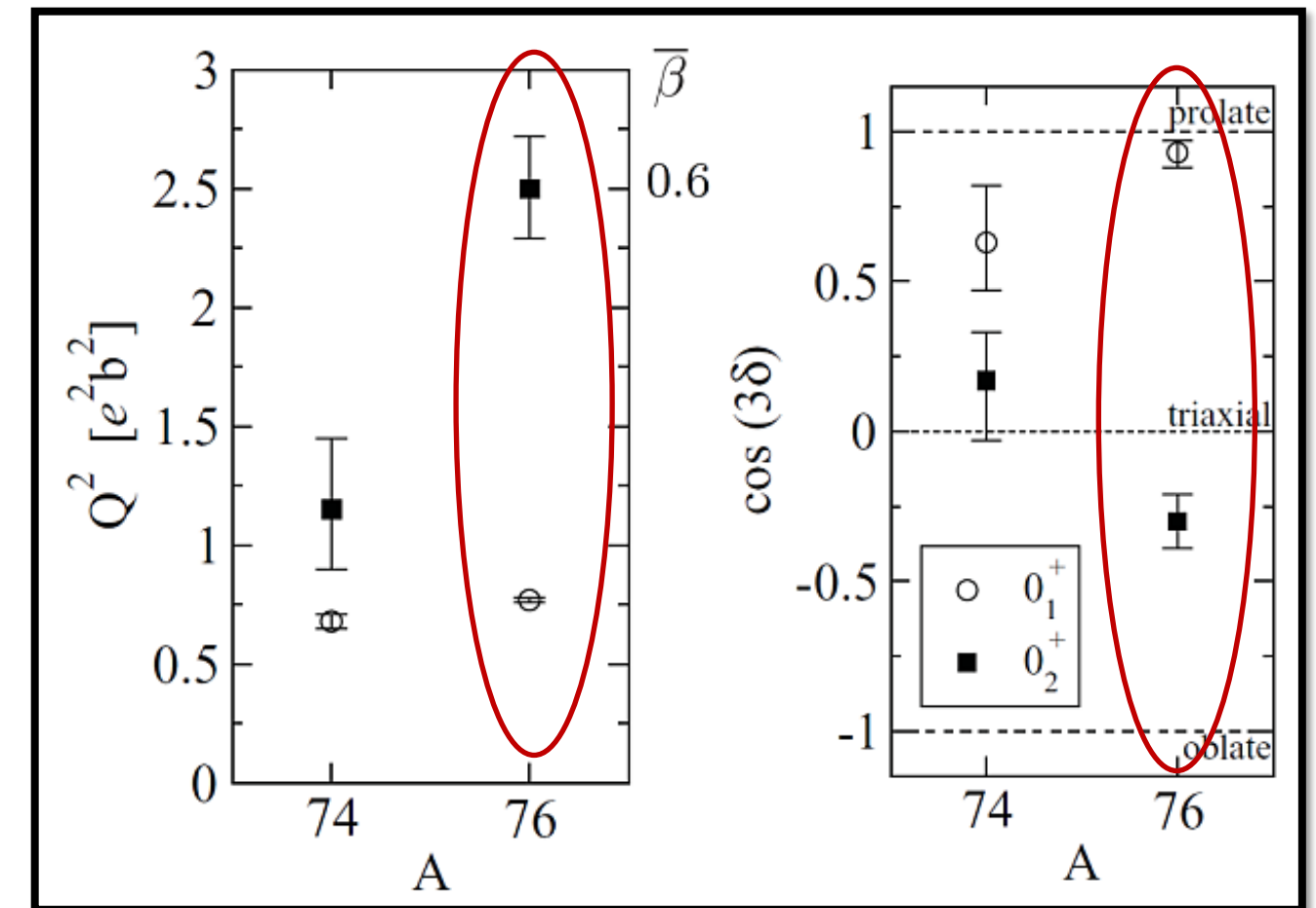
❖ ^{76}Kr :

prolate ground state coexists with a less deformed, oblate/triaxial 0_2^+ state

❖ ^{74}Kr :

Strong mixing of 0_1^+ , 0_2^+ states leading to more similar, triaxial shapes

Shape coexistence in $^{74,76}\text{Kr}$ @ GANIL - sum rules and BMF



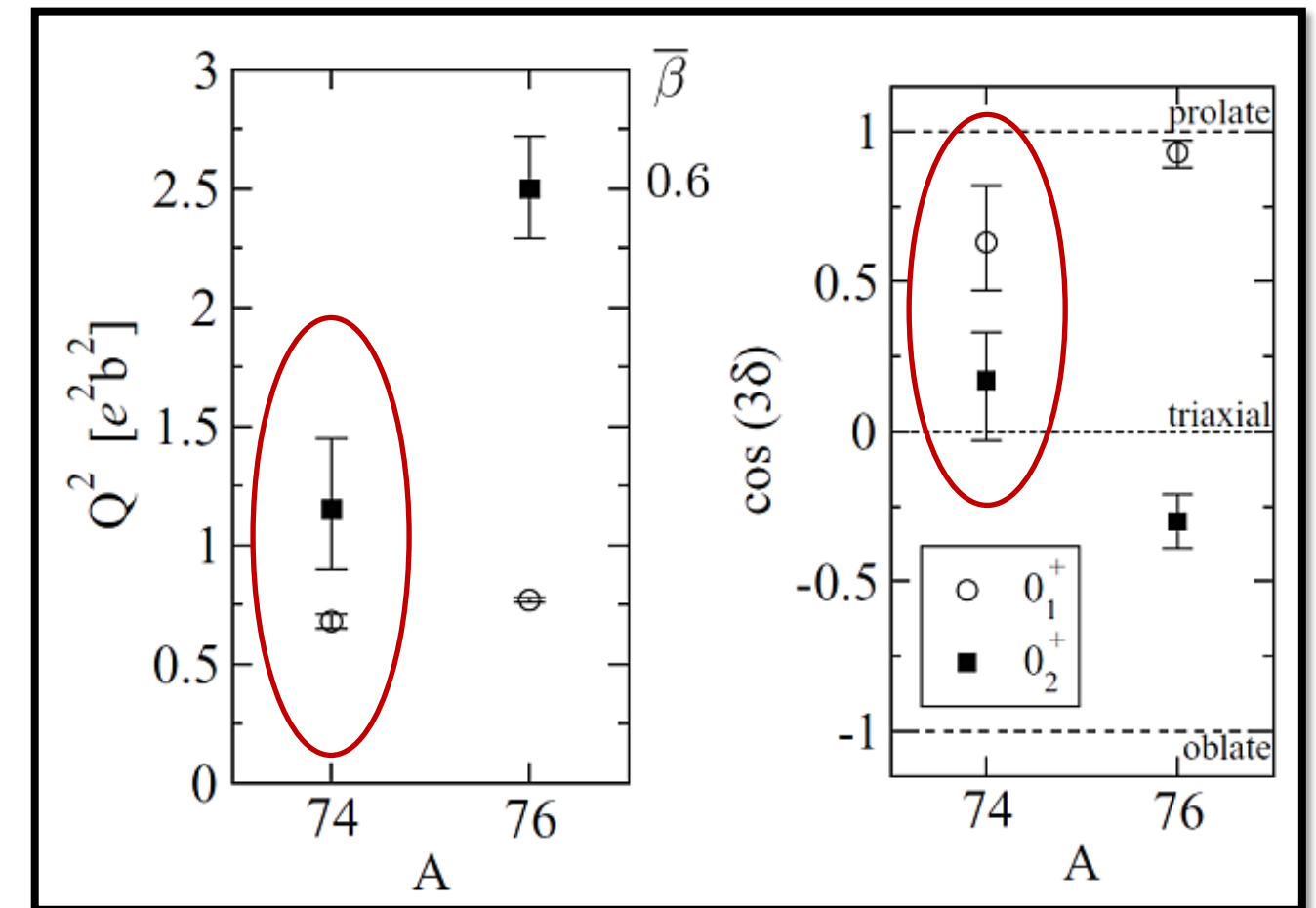
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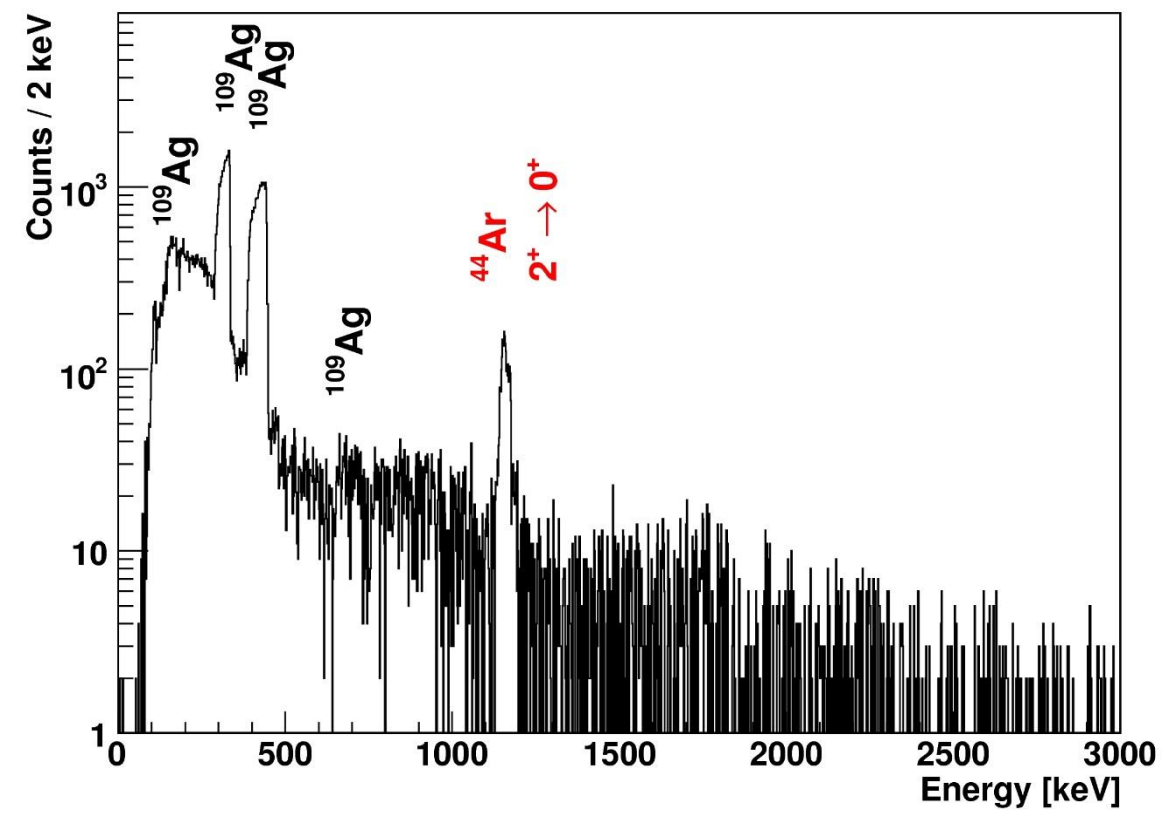
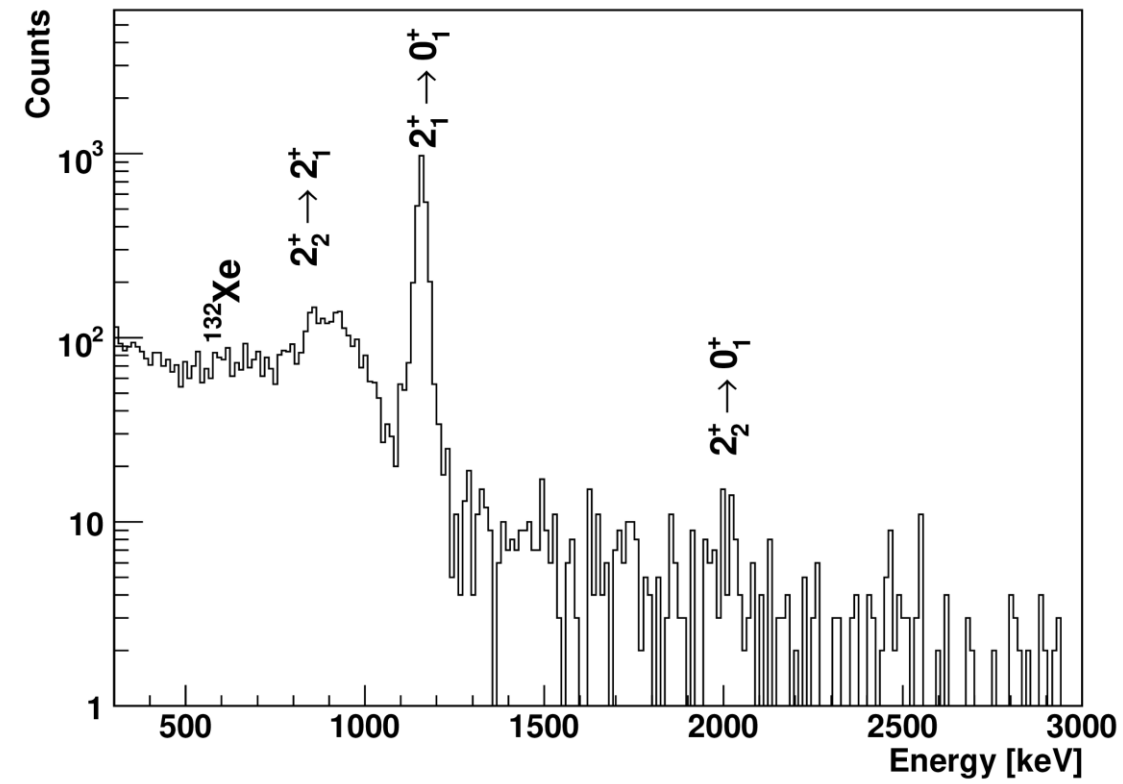
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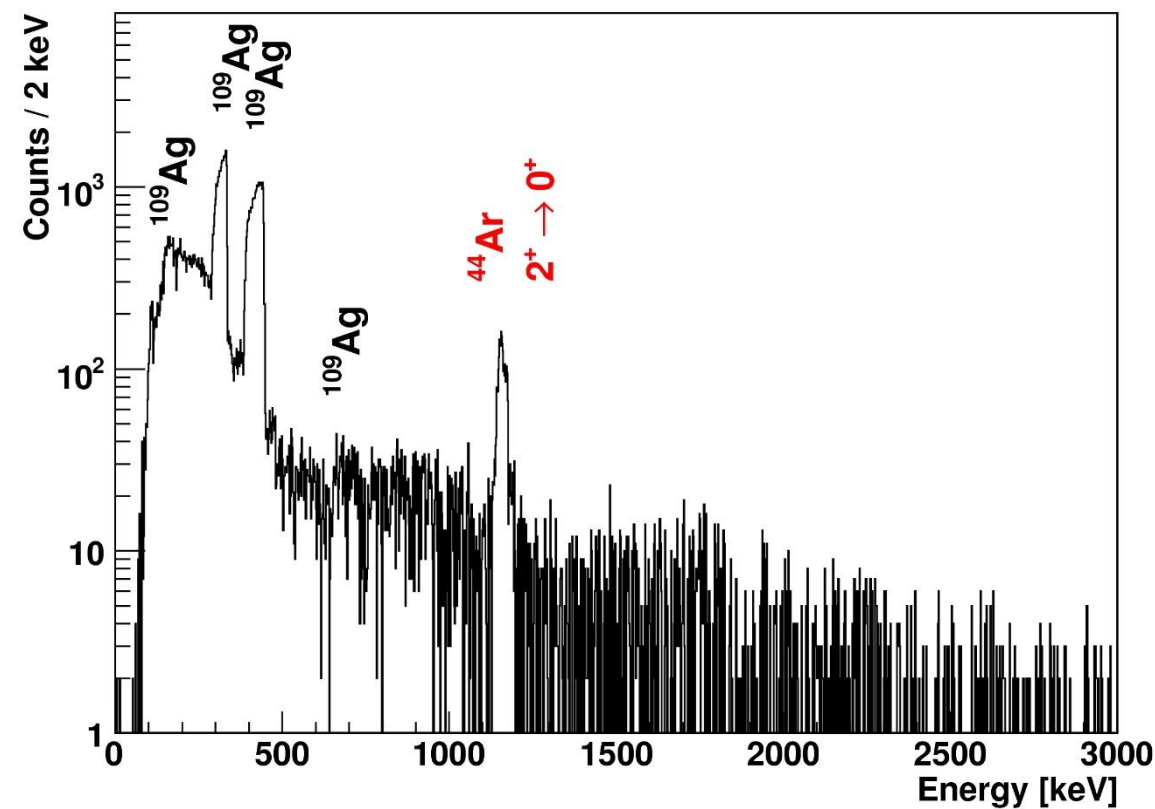
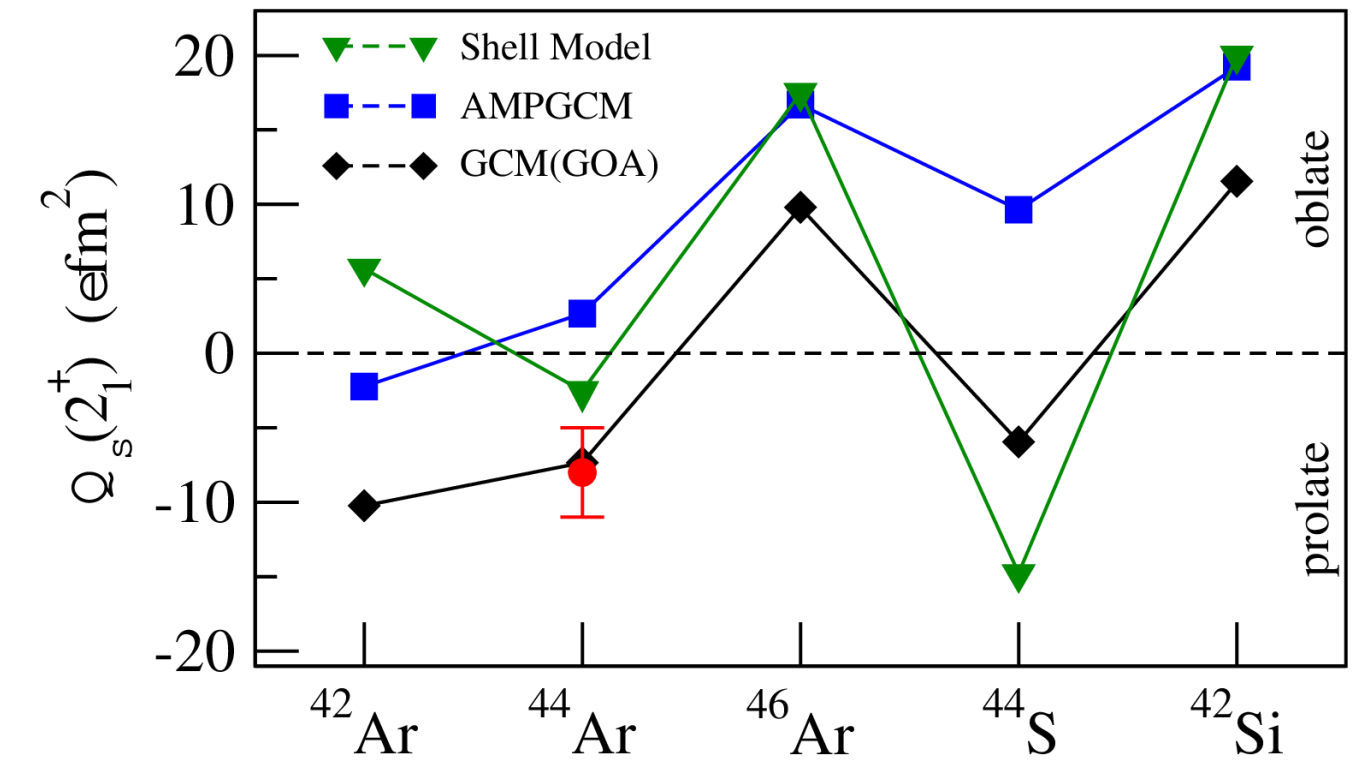
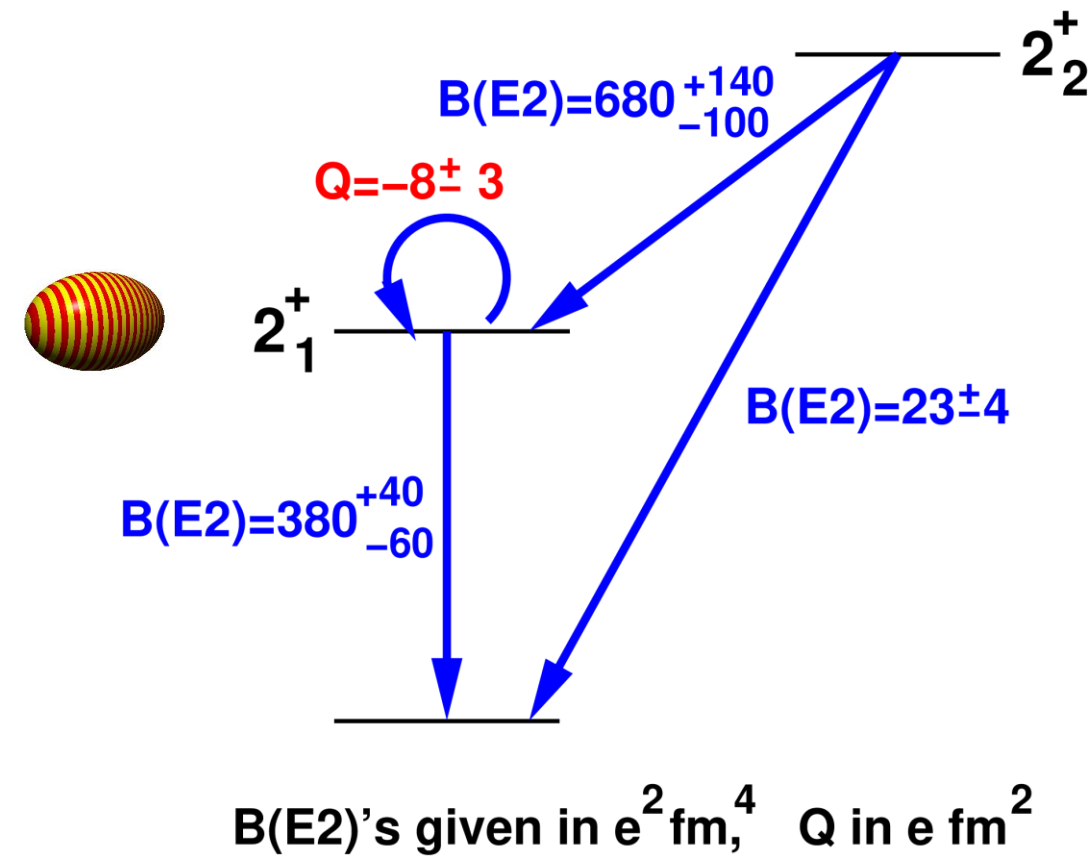
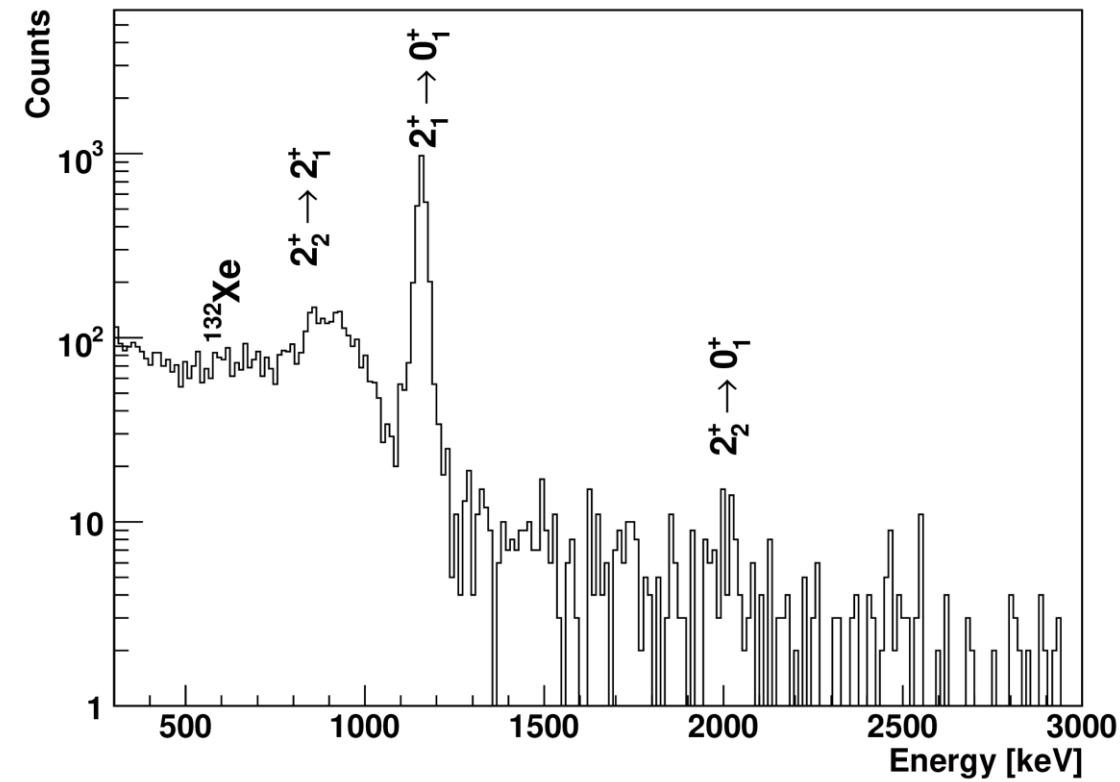
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Strong mixing of 0_1^+ , 0_2^+ states leading to more similar, triaxial shapes

Coulomb excitation of ^{44}Ar @ GANIL [E493S, April 2008]



Coulomb excitation of ^{44}Ar @ GANIL [E493S, April 2008]



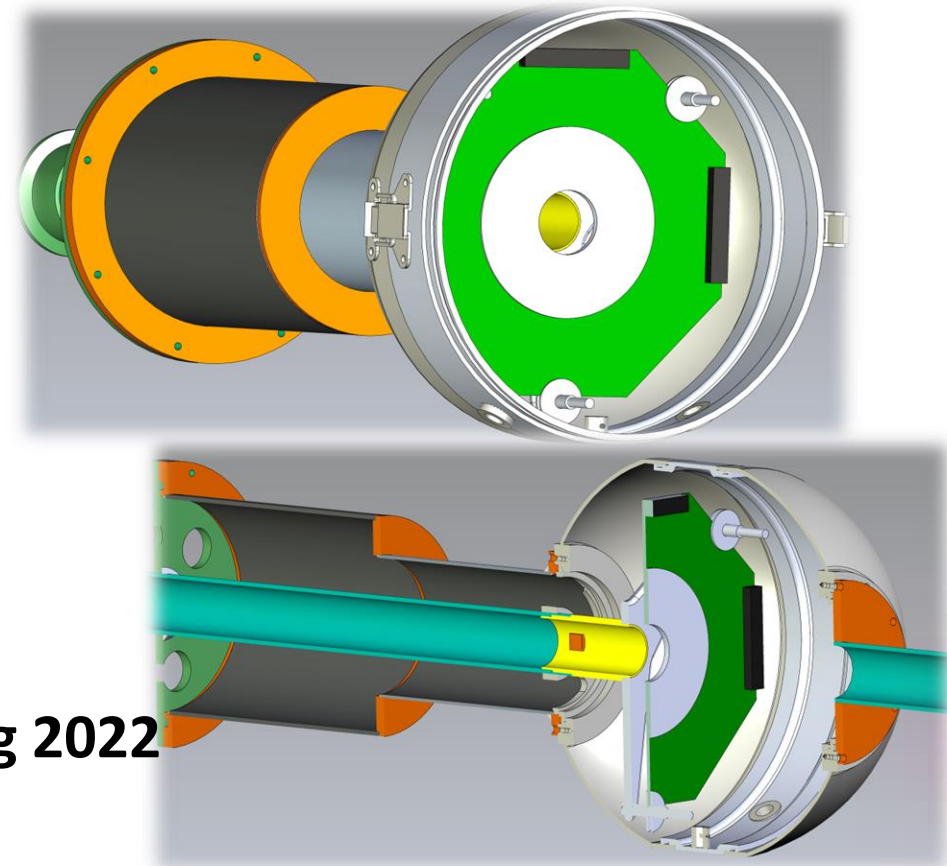
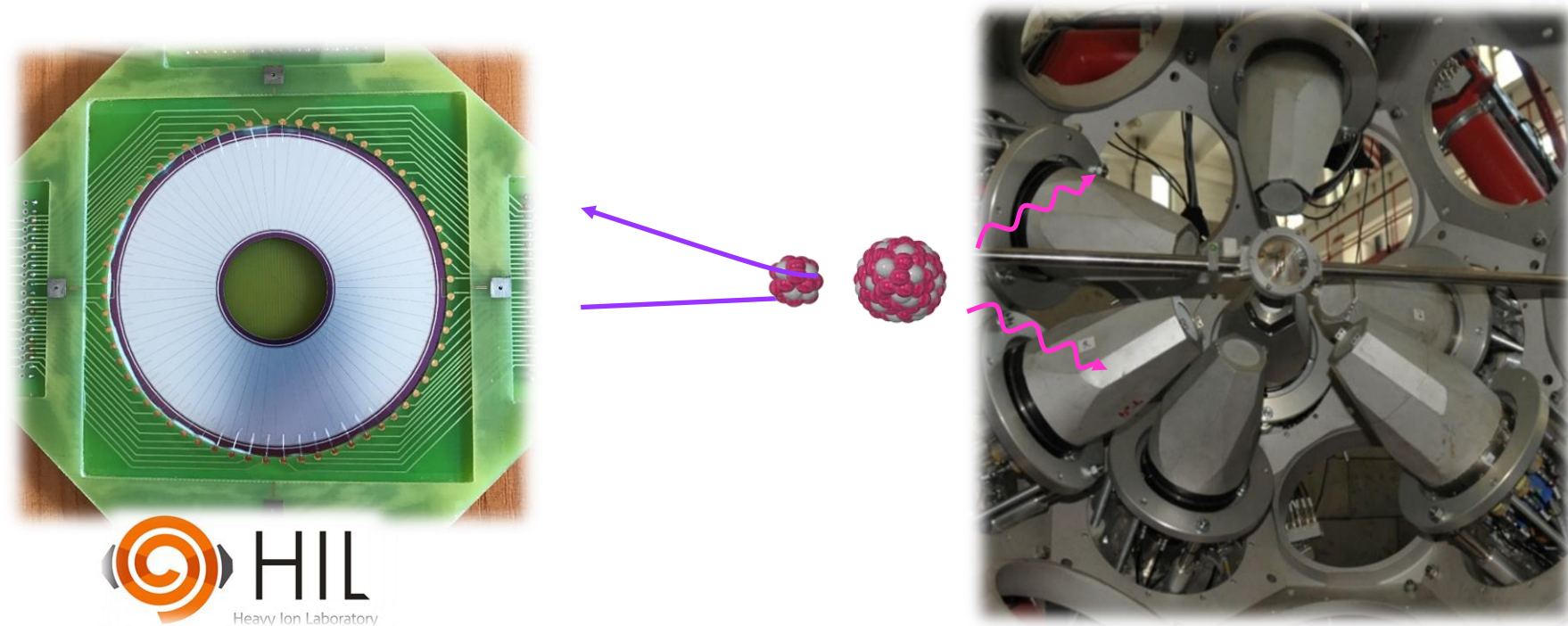
- $B(E2; 2_1^+ \rightarrow 0_1^+)$ in agreement with the result from intermediate-energy Coulex ($345(41)$ e² fm⁴)
- quadrupole moment of the 2_1^+ state measured with precision of 35%
- $B(E2)$ values for transitions deexciting the 2_2^+ state measured for the first time
- ground-state β deformation of nearly 0.3 already already two protons and two neutrons away from doubly magic ^{48}Ca
- diagonal matrix element – 50% of the rotational value \rightarrow triaxiality ?

PHYSICAL REVIEW C 80, 014317 (2009)

Shape of ^{44}Ar : Onset of deformation in neutron-rich nuclei near ^{48}Ca

M. Zielińska,^{1,2} A. Görge, ¹ E. Clément,^{1,*} J.-P. Delaroche,³ M. Girod,³ W. Korten,¹ A. Bürger,^{1,4,†} W. Catford,⁵ C. Dossat,¹ J. Iwanicki,² J. Libert,⁶ J. Ljungvall,^{1,*} P. J. Napiorkowski,² A. Obertelli,¹ D. Piętak,⁷ R. Rodríguez-Guzmán,⁸ G. Sletten,⁹ J. Srebrny,² Ch. Theisen,¹ and K. Wrzosek²

SilCA - Silicon Coulex Array



- $r_{in} = 1.6 \text{ cm}$
- $r_{out} = 4.2 \text{ cm}$
- 64 sectors
(32 readout)
- 32 rings
(16 readout)

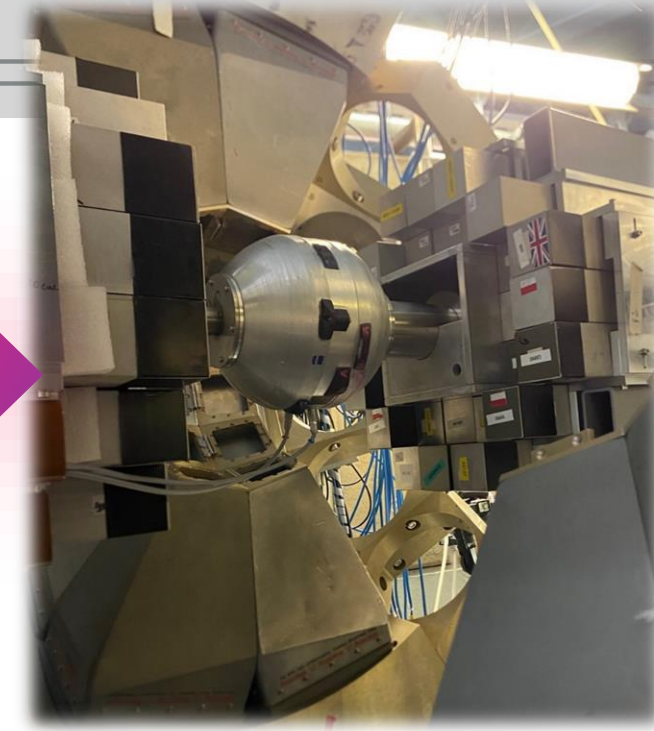
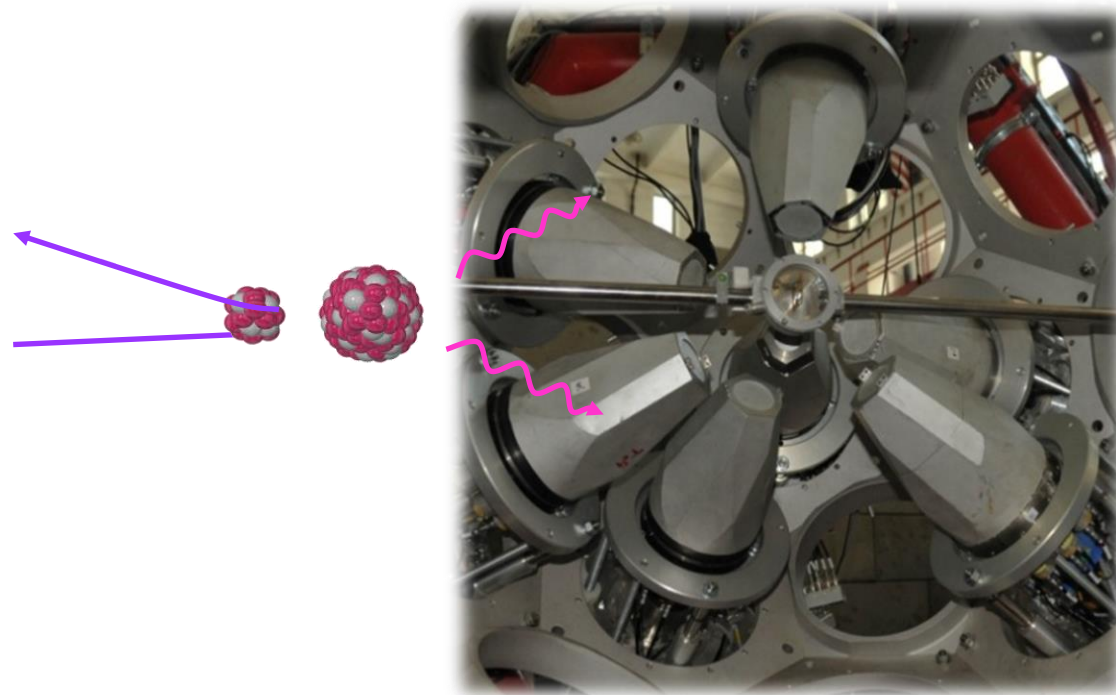
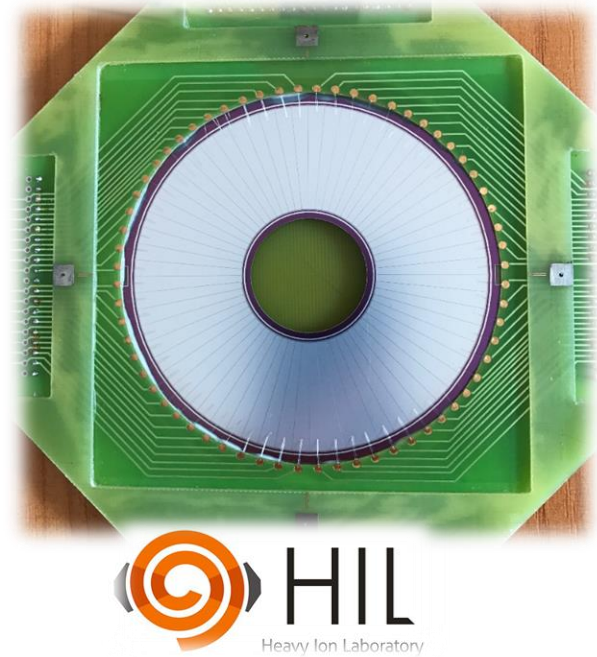
Spring 2022

October 2022

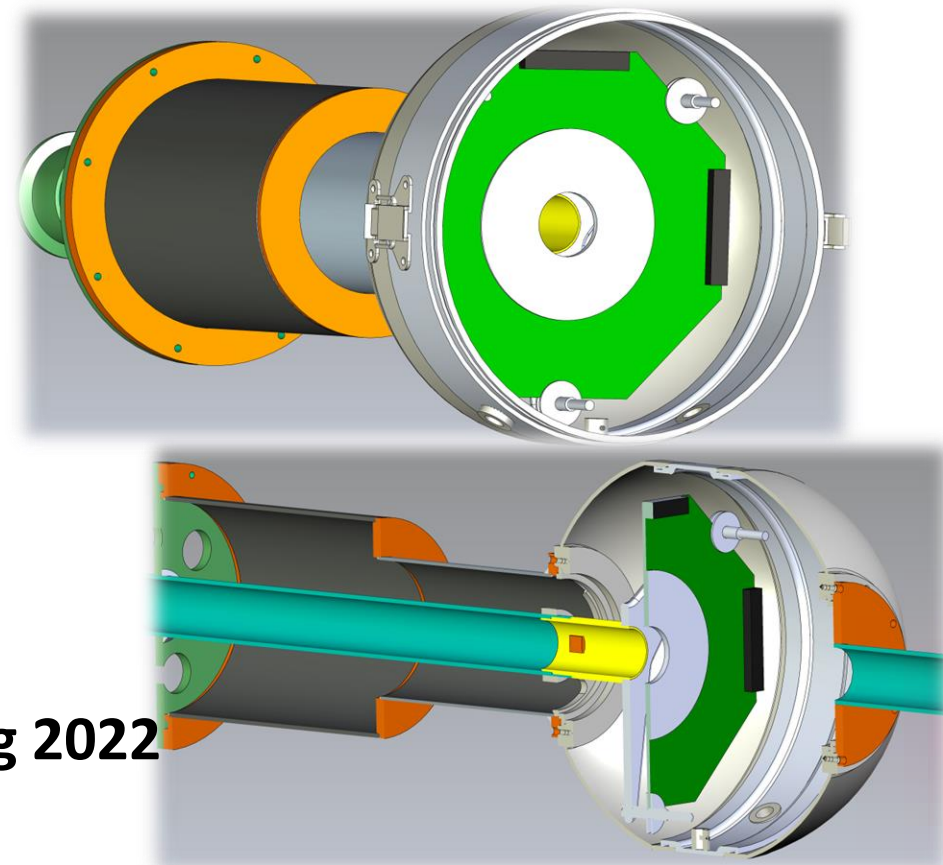


SilCA - Silicon Coulex Array

December 2022



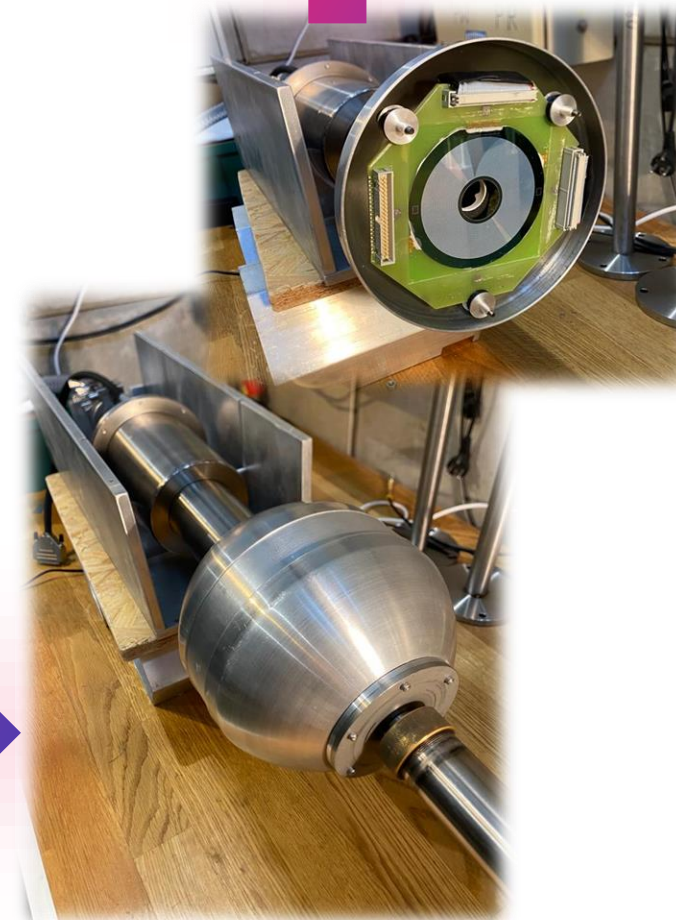
Campaign
DSSD+NuBALL2
(+PARIS)
I-VI 2023
7 experiments
Fully digital, FASTER



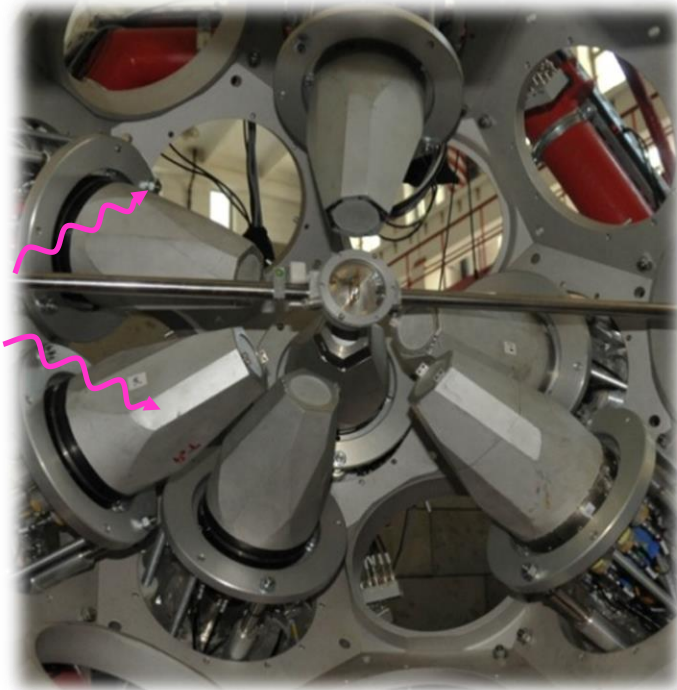
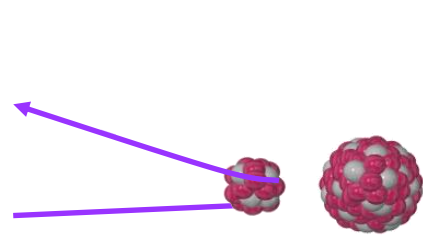
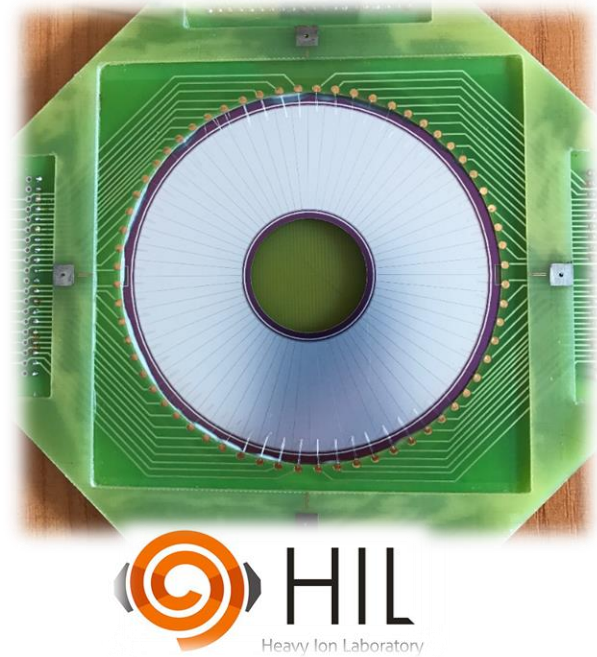
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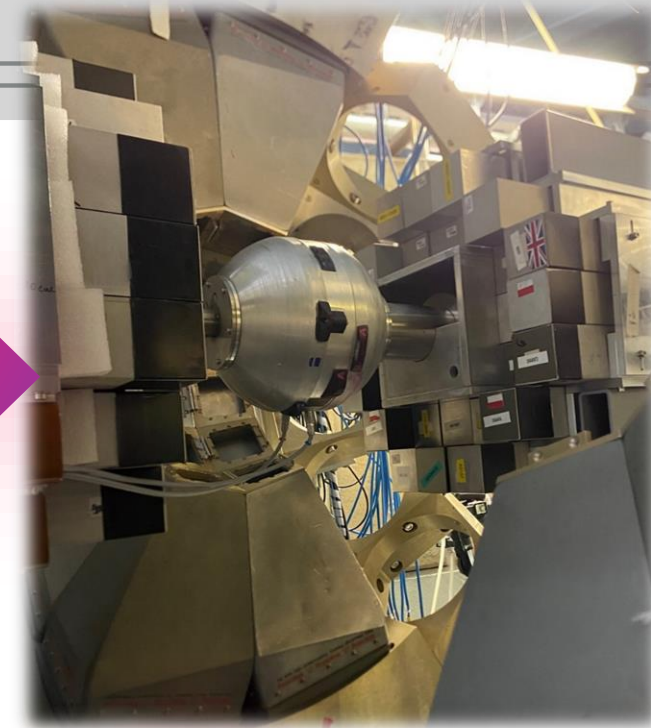
October 2022



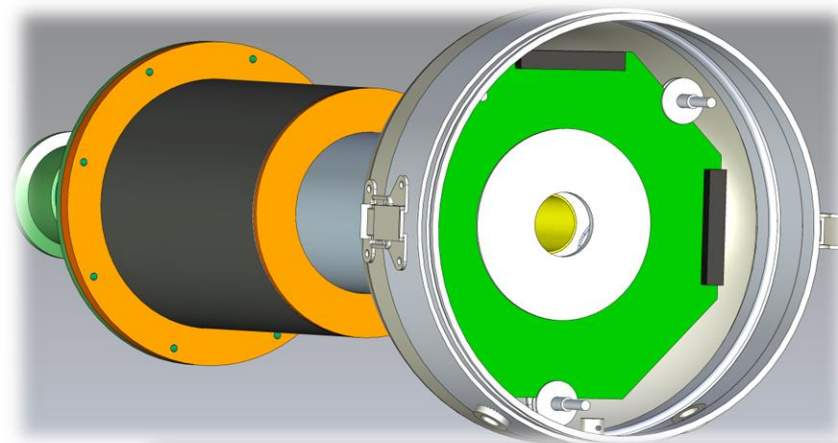
SilCA - Silicon Coulex Array



December 2022

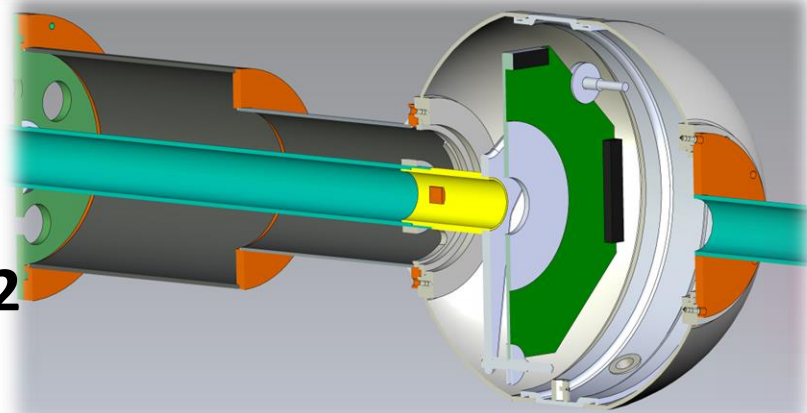


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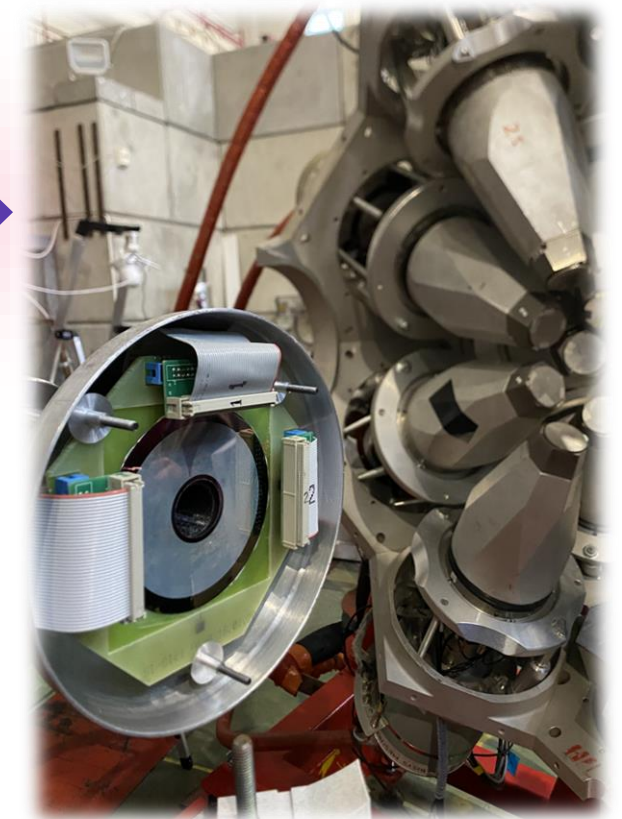
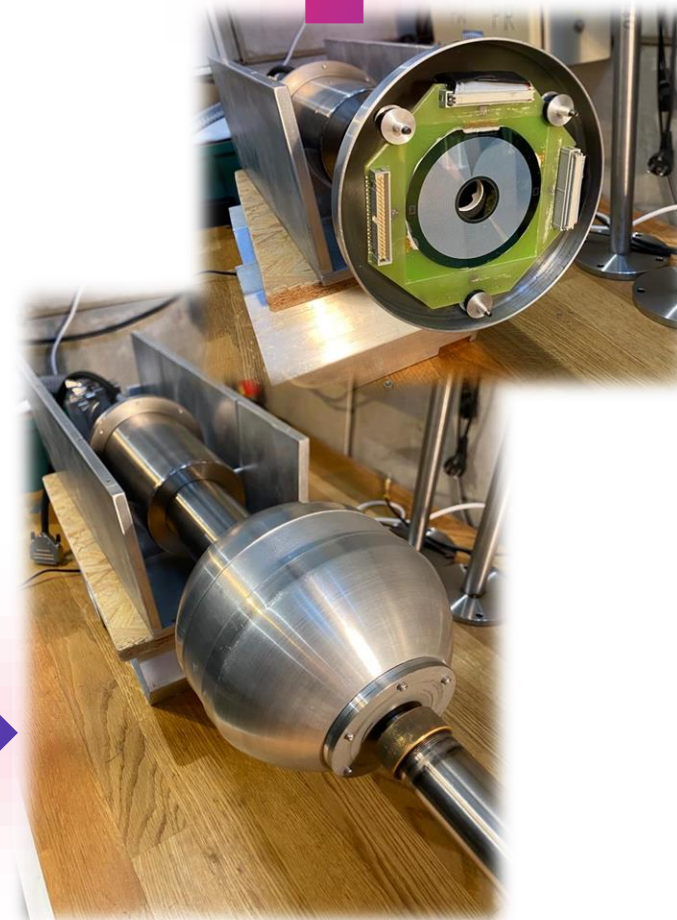


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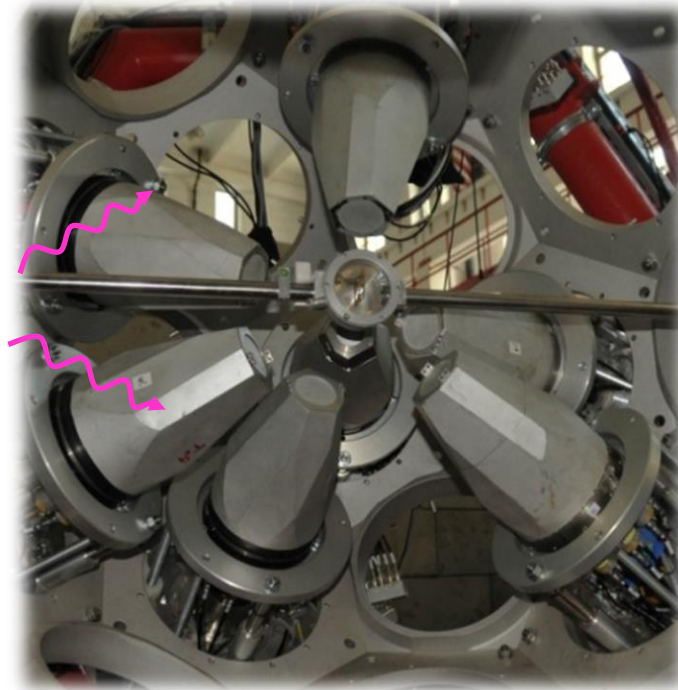
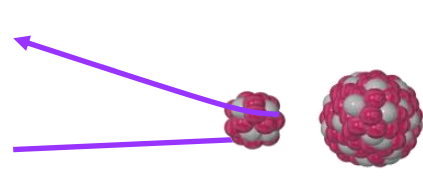


October 2022



First tests (^{241}Am): **February 2024**
DSSD+EAGLE (fully digital, CAEN 1725)

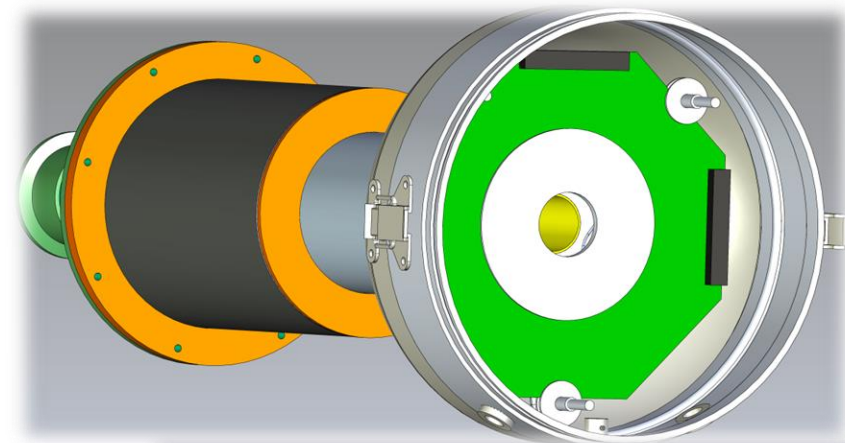
SilCA - Silicon Coulex Array



December 2022

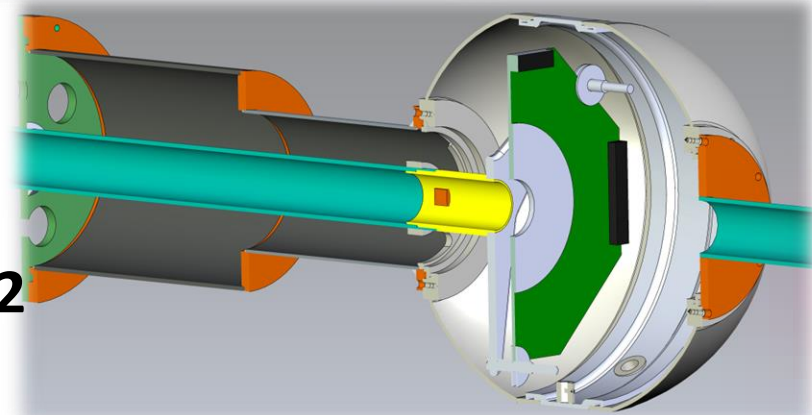


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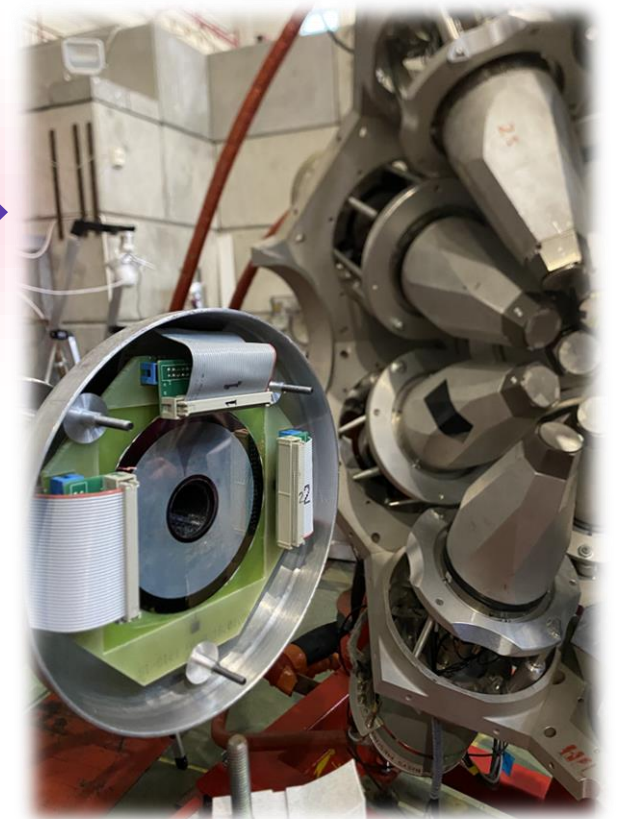
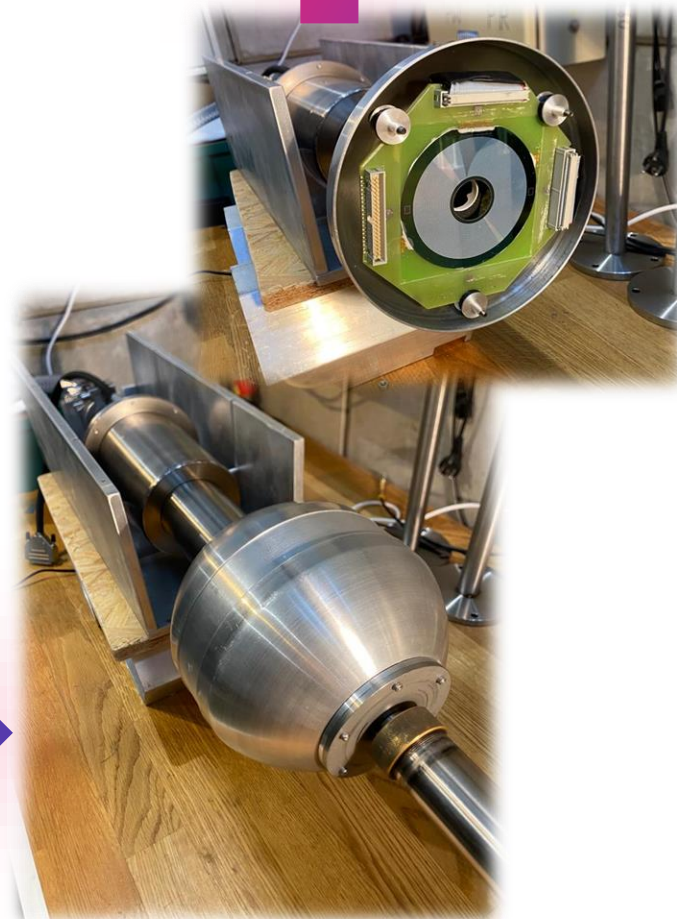


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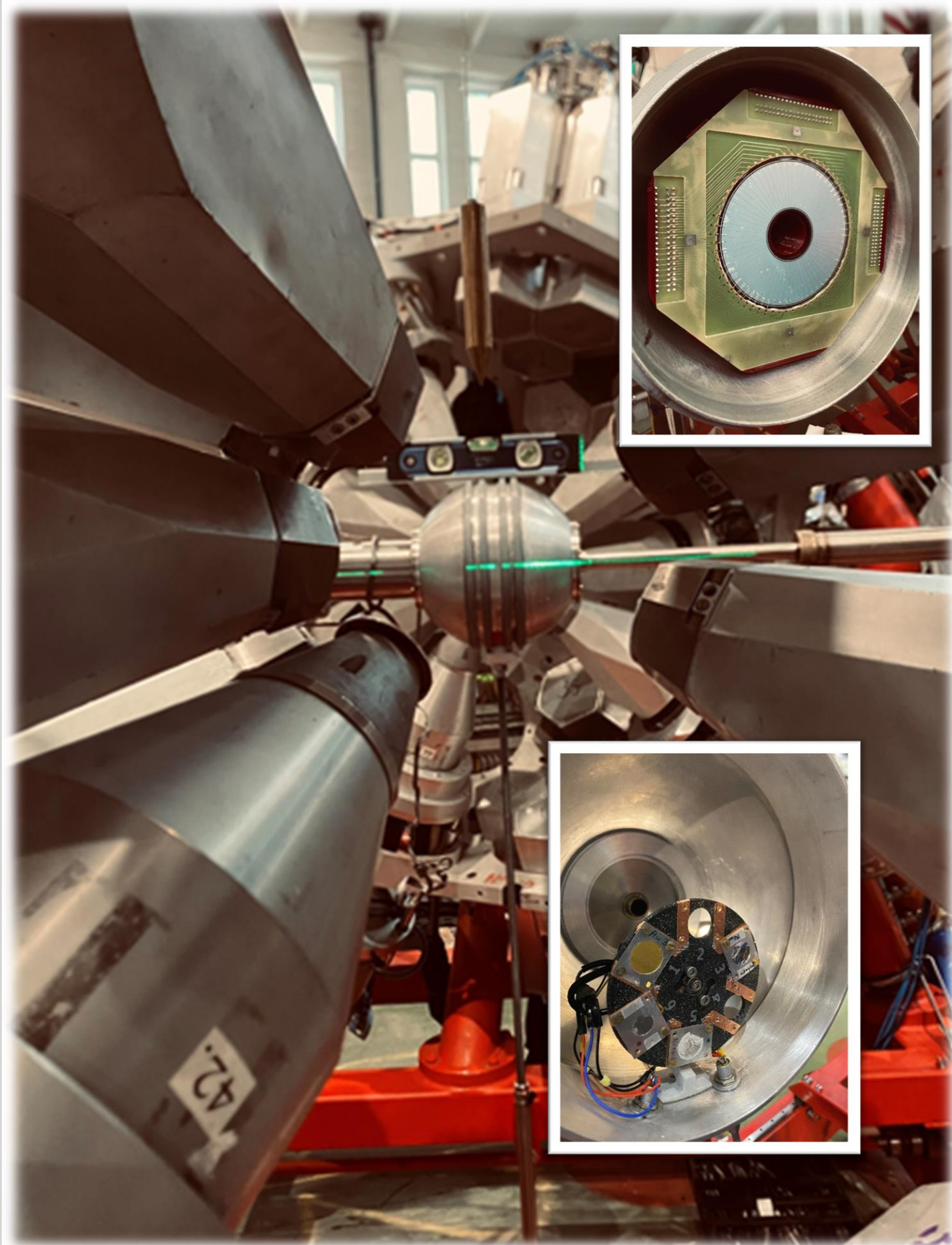


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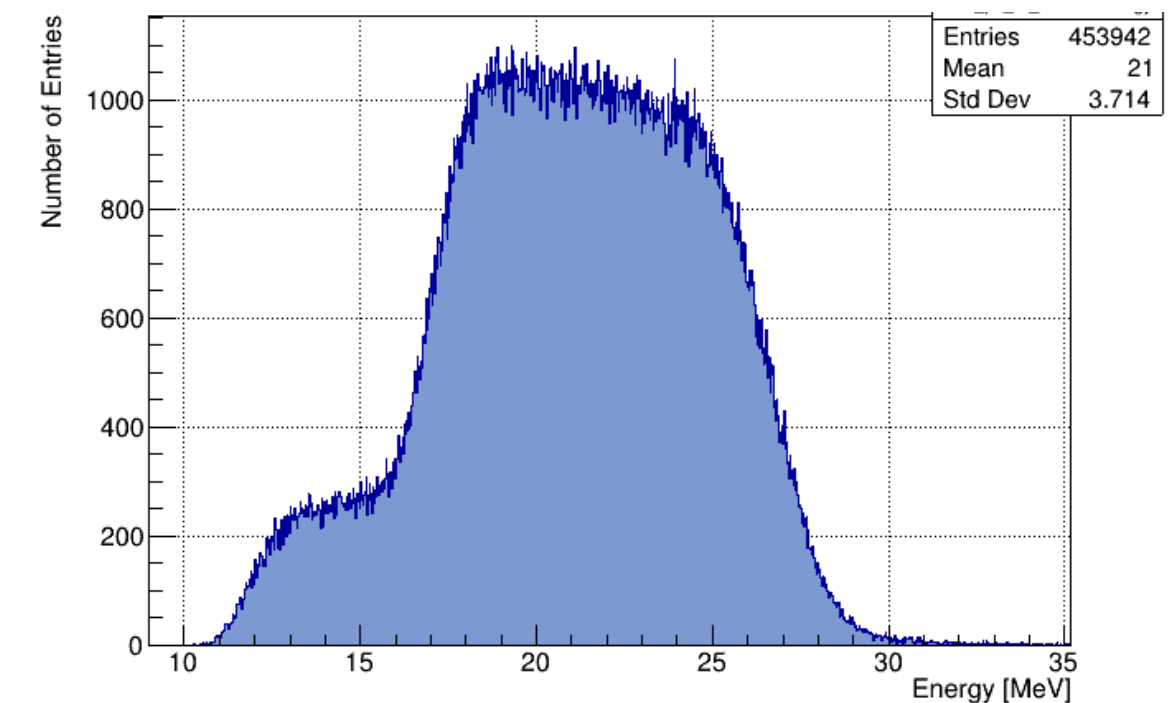
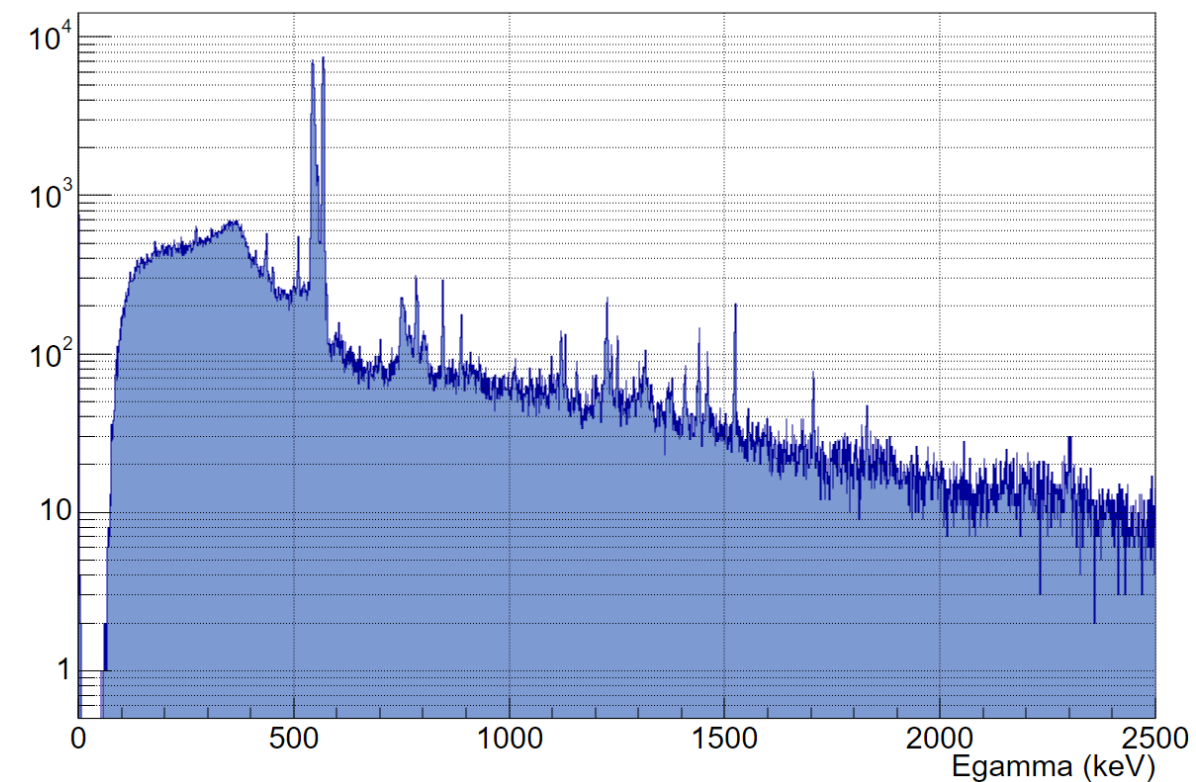
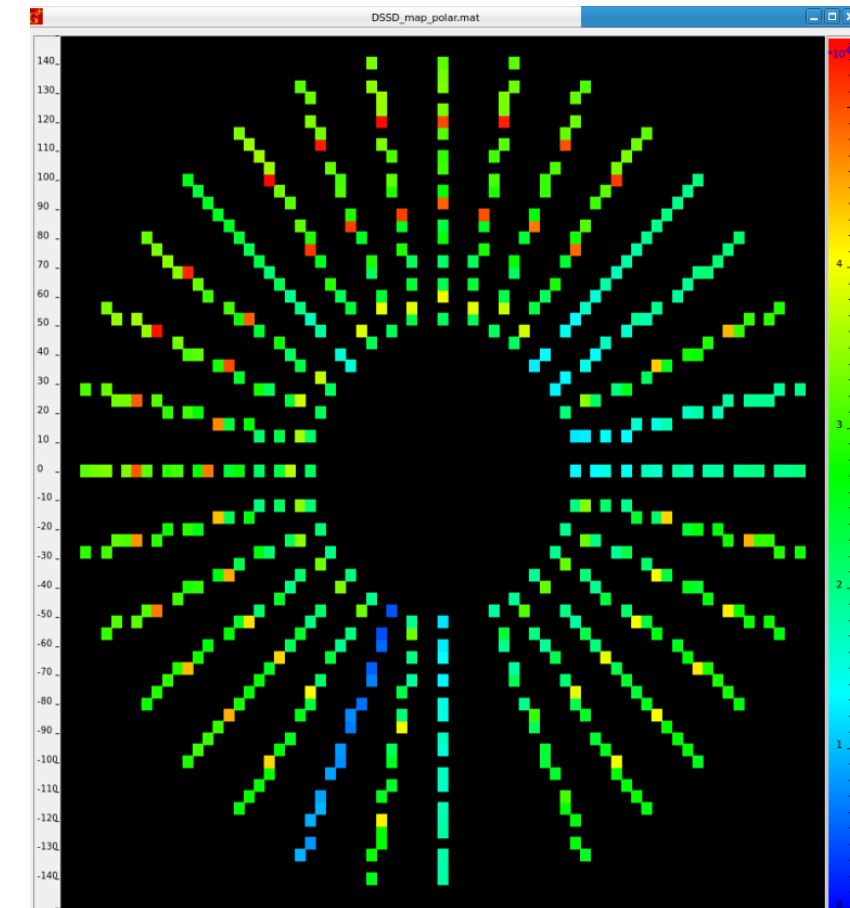
Project: P. Napiorkowski, J. Iwanicki, A. Iwanicki, J. Mierzejewski, KHK

In-beam commissioning of SilCA+EAGLE performed in November 2024
 $^{104}\text{Pd} + ^{32}\text{S}$, Coulomb excitation reaction

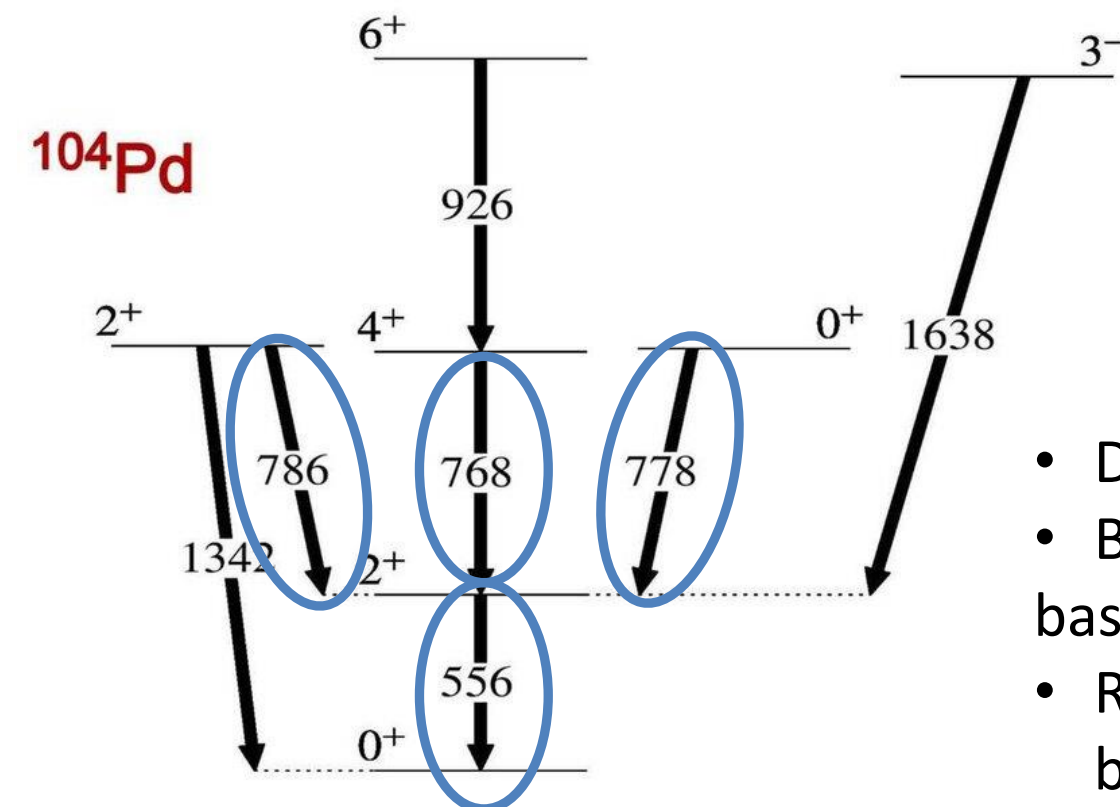
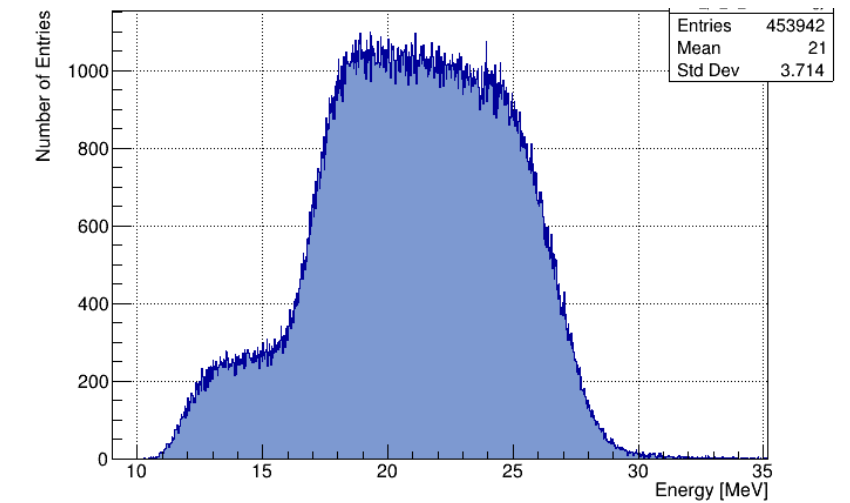
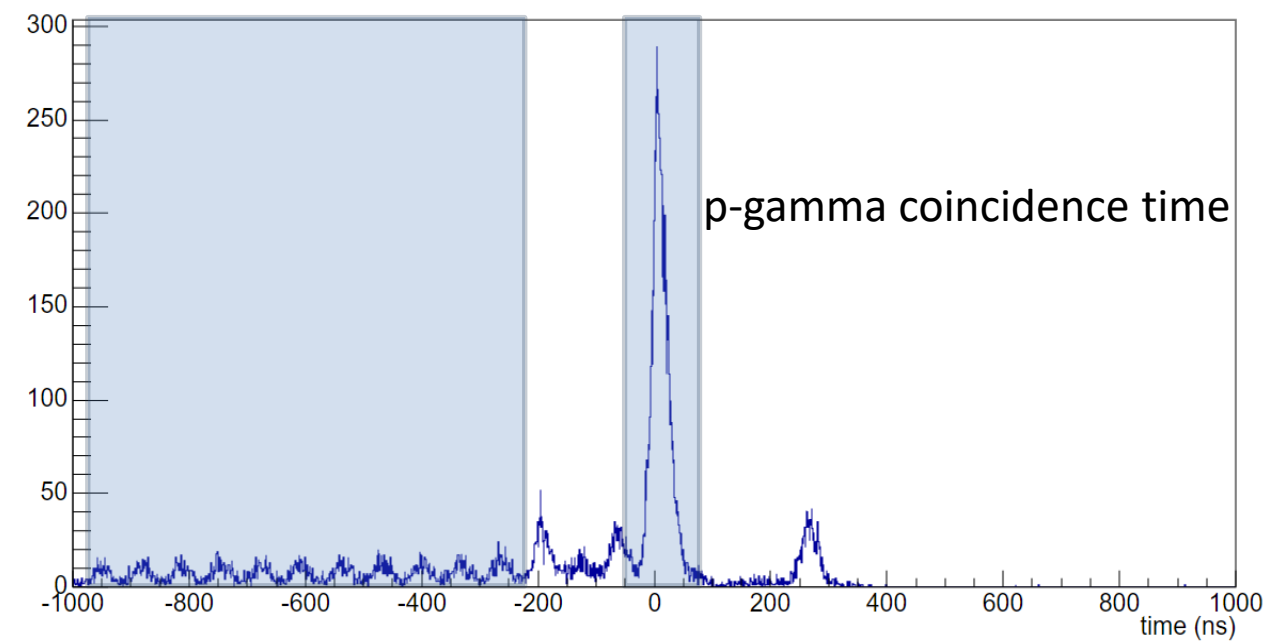
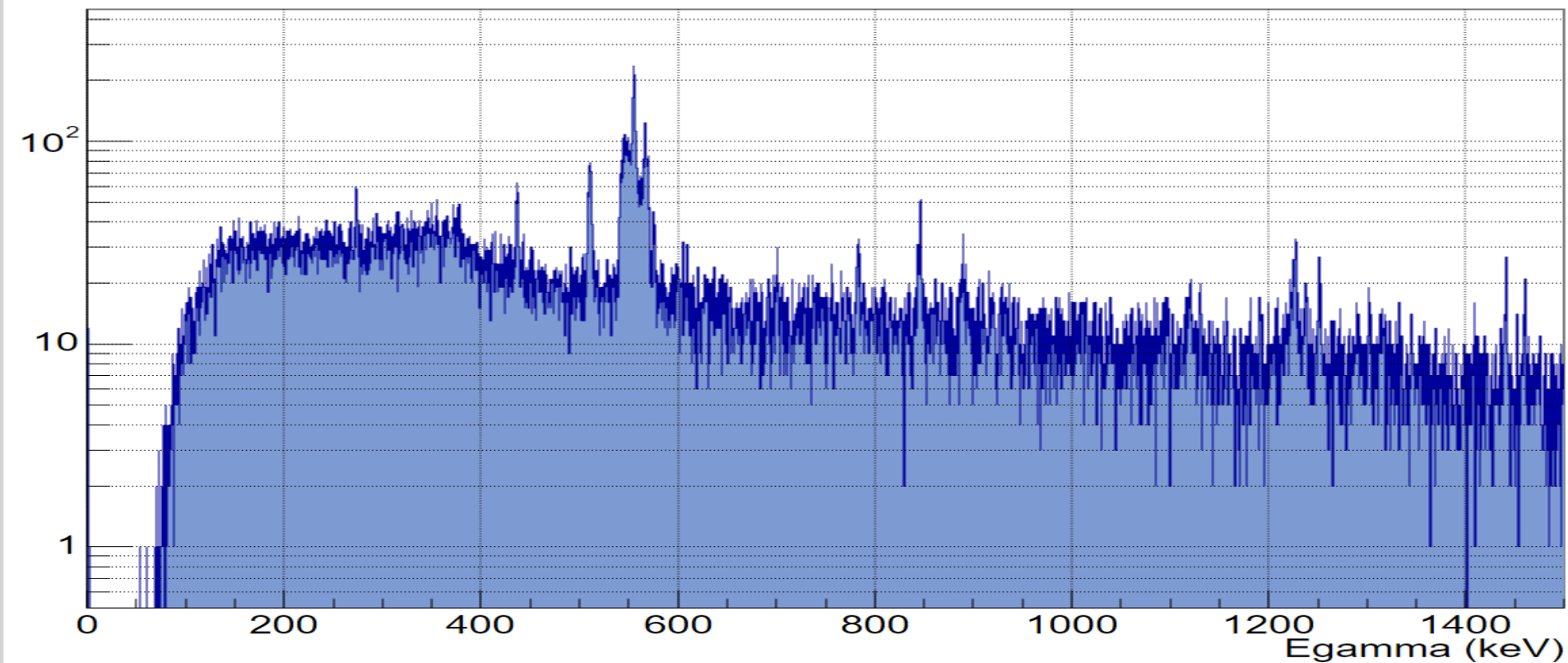
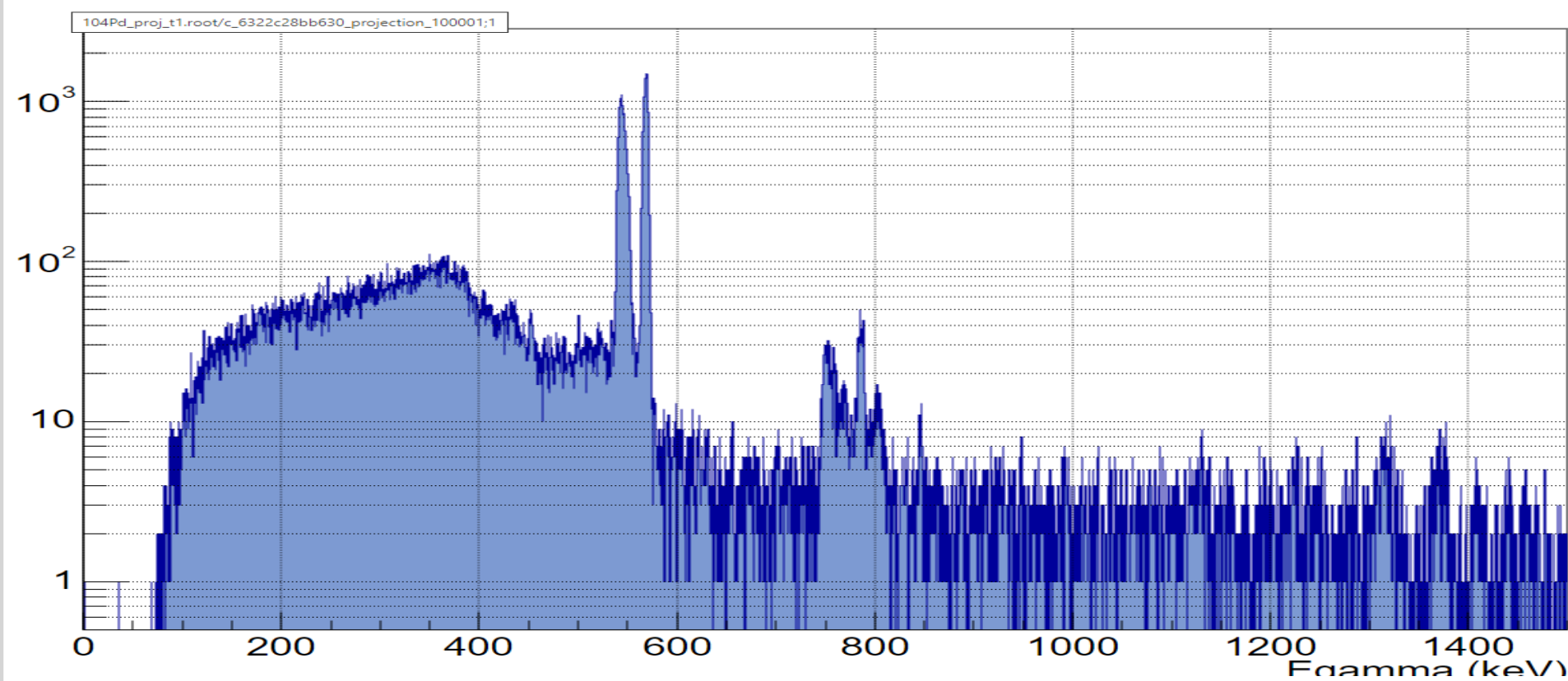
SilCA @ HIL (November 2024) - Coulomb excitation of ^{104}Pd



- ^{32}S beam, 90 MeV, 1-2 pA
- ^{104}Pd (+ natBa and ^{197}Au targets), 1 mg/cm² each - on the automatic target wheel, 6 spots, camera inside
- 4 days (12-15 Nov 2024)
- 13 HPGe (11 GAMMAPOOL + 2 Phase One)
- SiLCA DSSD – 134-156°, 4cm from the target
- 31/32 sectors and 16/16 rings were working
- Total dark current increased in-beam from 16 to 22 uA
- CAEN 1725 digitizers – 2 for HPGe + ACS, 3 for DSSD, 1 for NEDA + trigger
- AGAVA for the GTS
- XDAQ (LNL upgrade CERN-based DAQ), particle hardware trigger
- GREWARE + SPY – online visualisation (J. Grębosz, IFJ PAN Krakow)



SilCA @ HIL (November 2024) - Coulomb excitation of ^{104}Pd

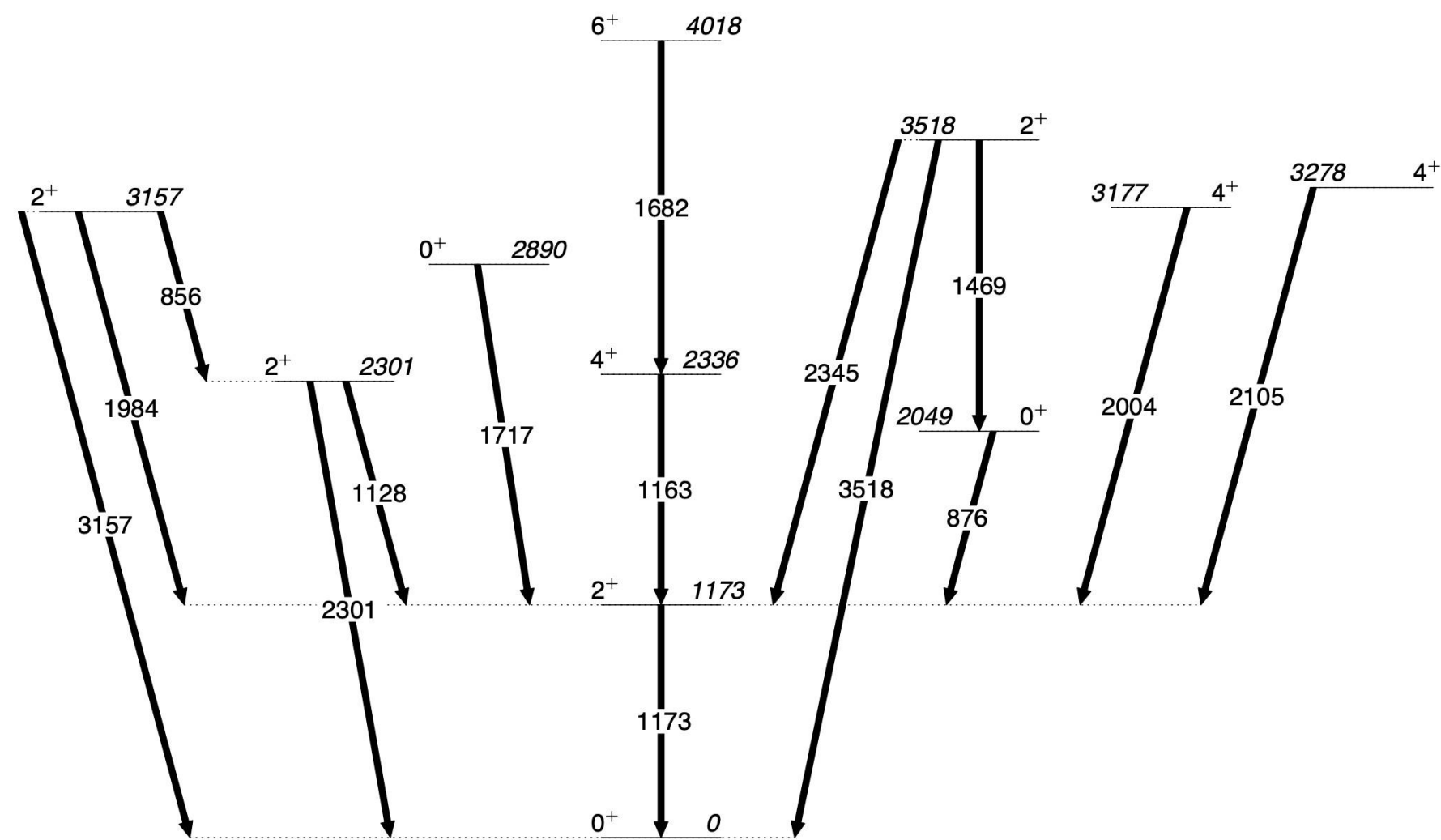


- Doppler Correction – to be done
- BGR subtraction – to be improved: based on the particle spectra + time
- Run-by-run calibration – need to be checked

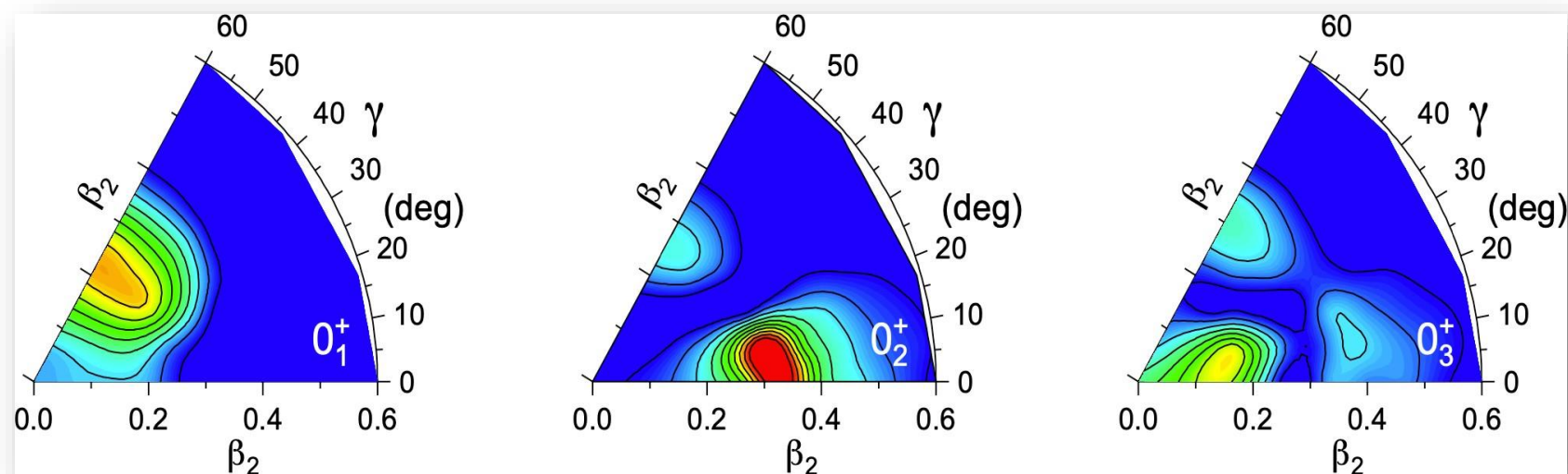
Thanks to (in alphabetical order):

P. Dei, J. Grębosz, C. Hiver, G. Jaworski, M. Komarowska, M. Kowalczyk, A. Krzysiek, A. Malinowski, M. Matuszewski, J. Mierzejewski, P. Napiorkowski, M. Palacz, S. Panasenko, I. Piętka, J. Samorajczyk-Pyśk, P. Sekrecka, K. Solak, A. Spacek, G. Szymanek, K. Wrzosek-Lipska + the target lab (A. Stolarz, J. Kowalska)

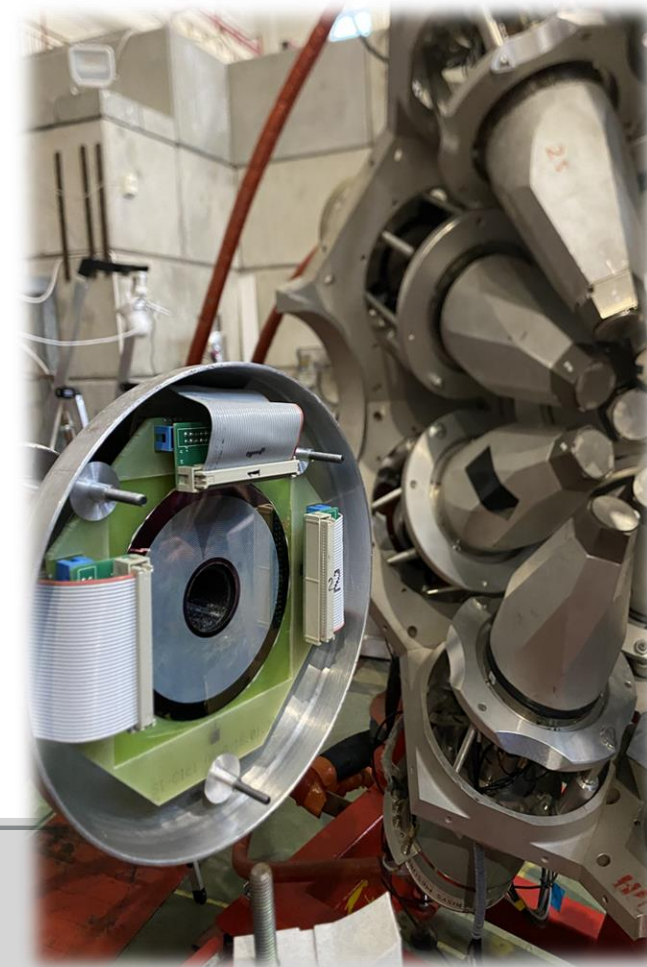
SilCA @ HIL (2025) - Coulomb excitation of ^{62}Ni [HIL 113, accepted]



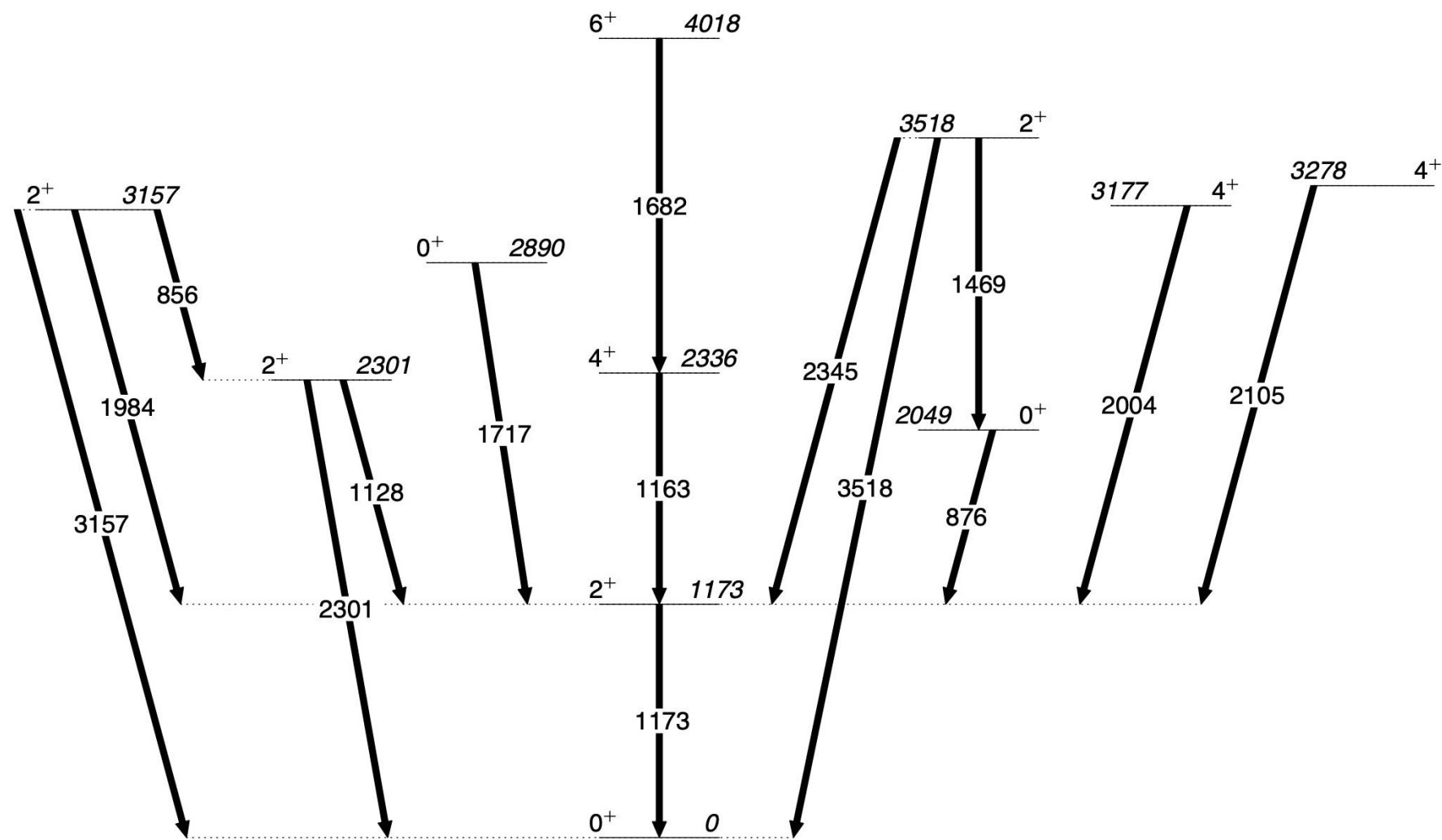
- Safe Coulomb excitation of ^{62}Ni
- Population of 0^+ and 2^+ states needed to understand the low-lying structure of ^{62}Ni
- $Q(2_1^+)$ - weakly known (measured in the reorientation experiment, indicating spherical/slightly oblate GS, but electron scattering is giving completely different value)
- 0_2^+ (2049 keV) - BE2($0_2^+ \rightarrow 2_1^+$) known with 55% uncertainty
- 0_2^+ - a 4p-4h excitation of ^{56}Ni core? A band-head of the superdeformed band?
- Triaxiality of 0^+ states - quadrupole moments of the 2^+ states needed
- Continuation of the project with IJC Lab (Orsay)



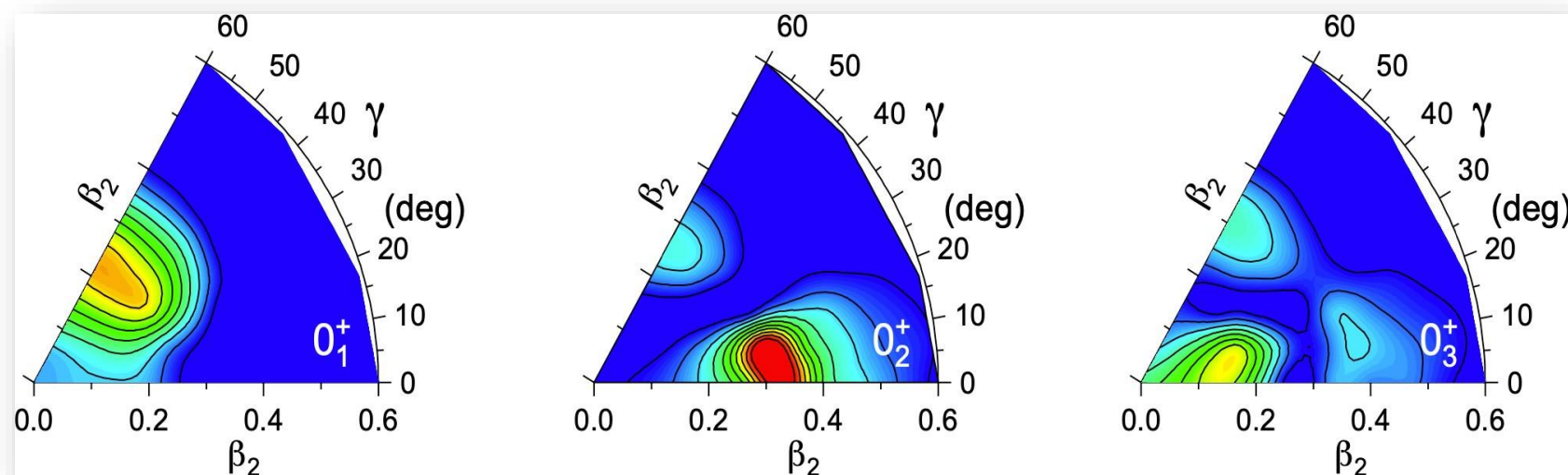
- ▶ ^{62}Ni target, 1 mg/cm²
- ▶ ^{20}Ne beam, 35 MeV, 1 pA
- ▶ 5 days of data taking assumed
- ▶ DSSD (127-154°) + EAGLE (1.4% at 1.3 MeV)



SilCA @ HIL (2025) - Coulomb excitation of ^{62}Ni [HIL 113, accepted]

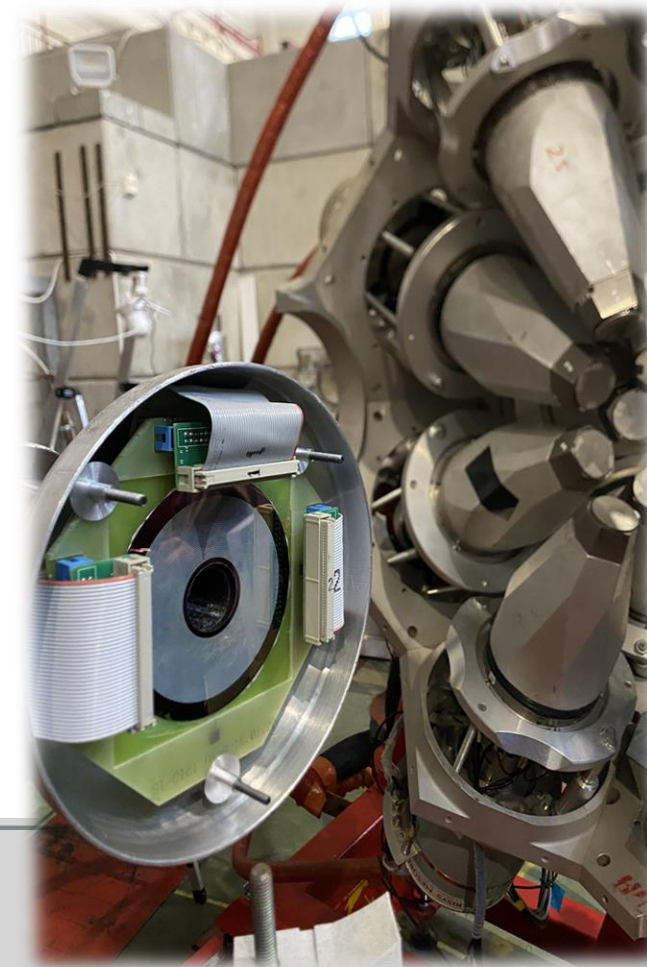


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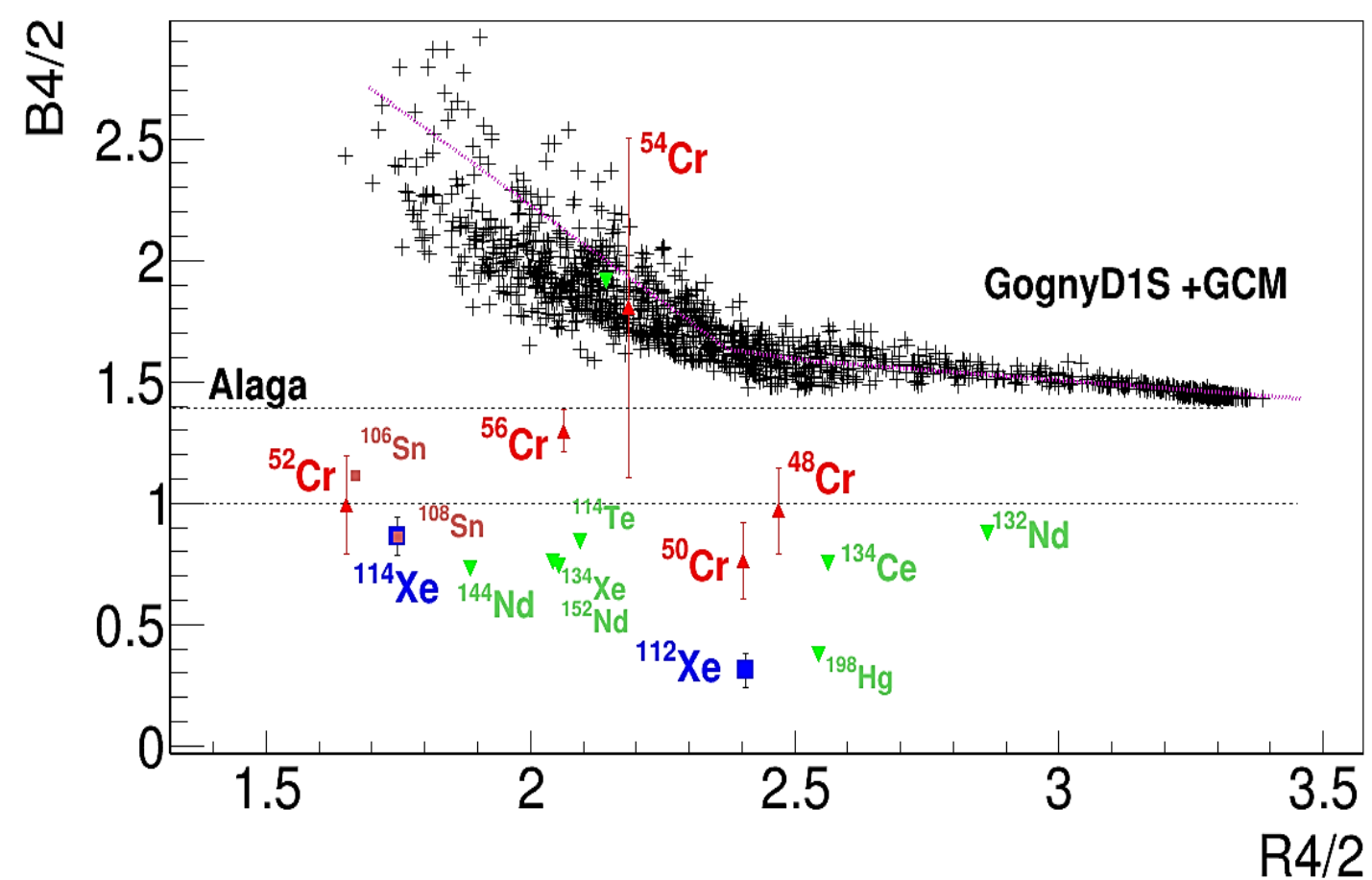
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- ▶ 5 days of data taking assumed
- ▶ DSSD (127-154⁰) + EAGLE (1.4% at 1.3 MeV)

+ 1 accepted: COULEX of ^{34}S
 + 3 new projects submitted to the next HIL PAC

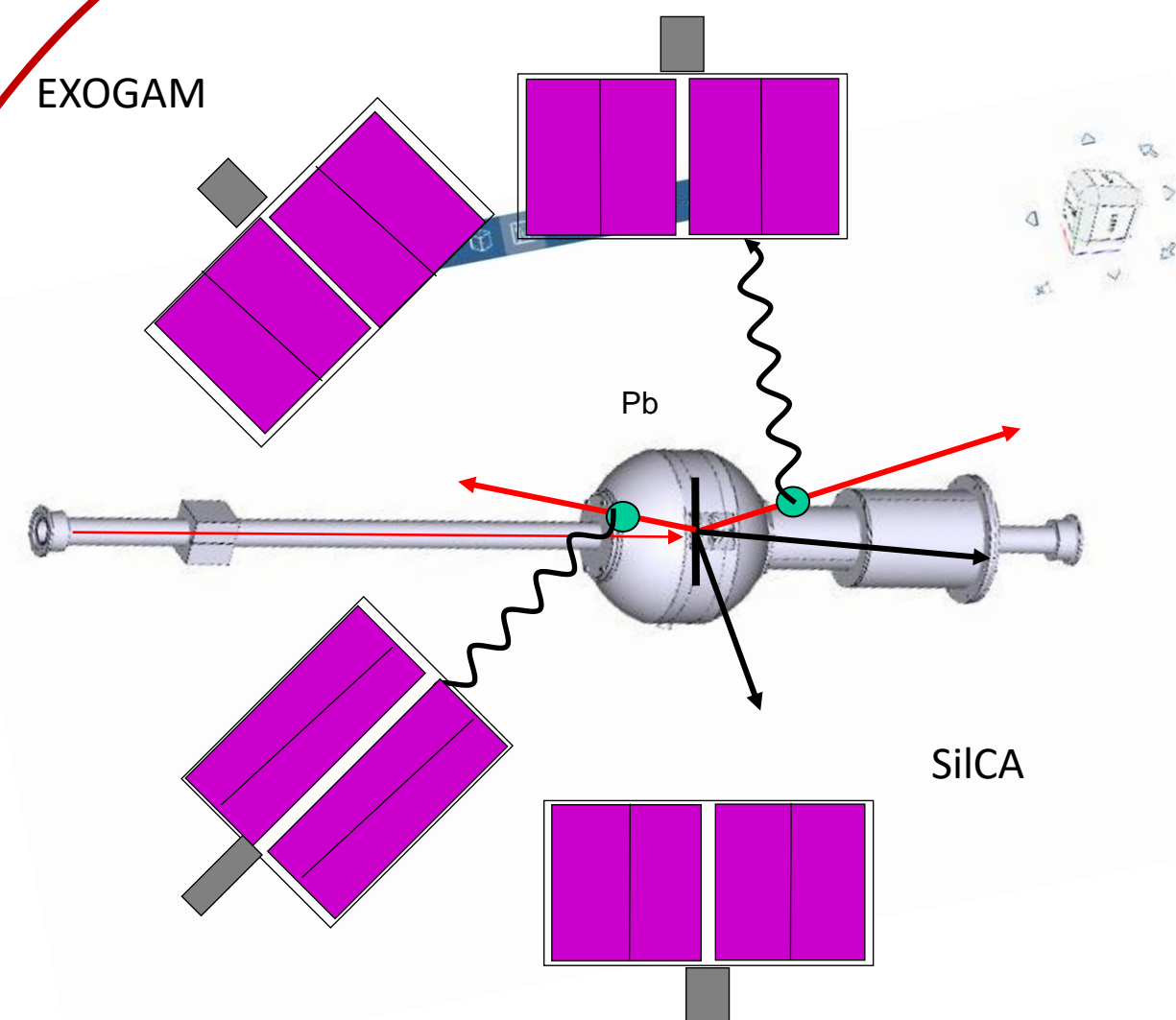


SilCA @ GANIL (2026) - Coulomb excitation of ^{48}Cr [E890_23 accepted]

- Self-conjugate - proton-neutron pairing plays an important role in its structure and collectivity;
- Ideal nucleus to study the alpha-cluster / condensate contribution.
- Milestone in the search for the double neutrino-less beta decay in the $A=48$ chain.
- The large observed deformation, in a relatively small valence space - comparison between mean-field and shell model approaches



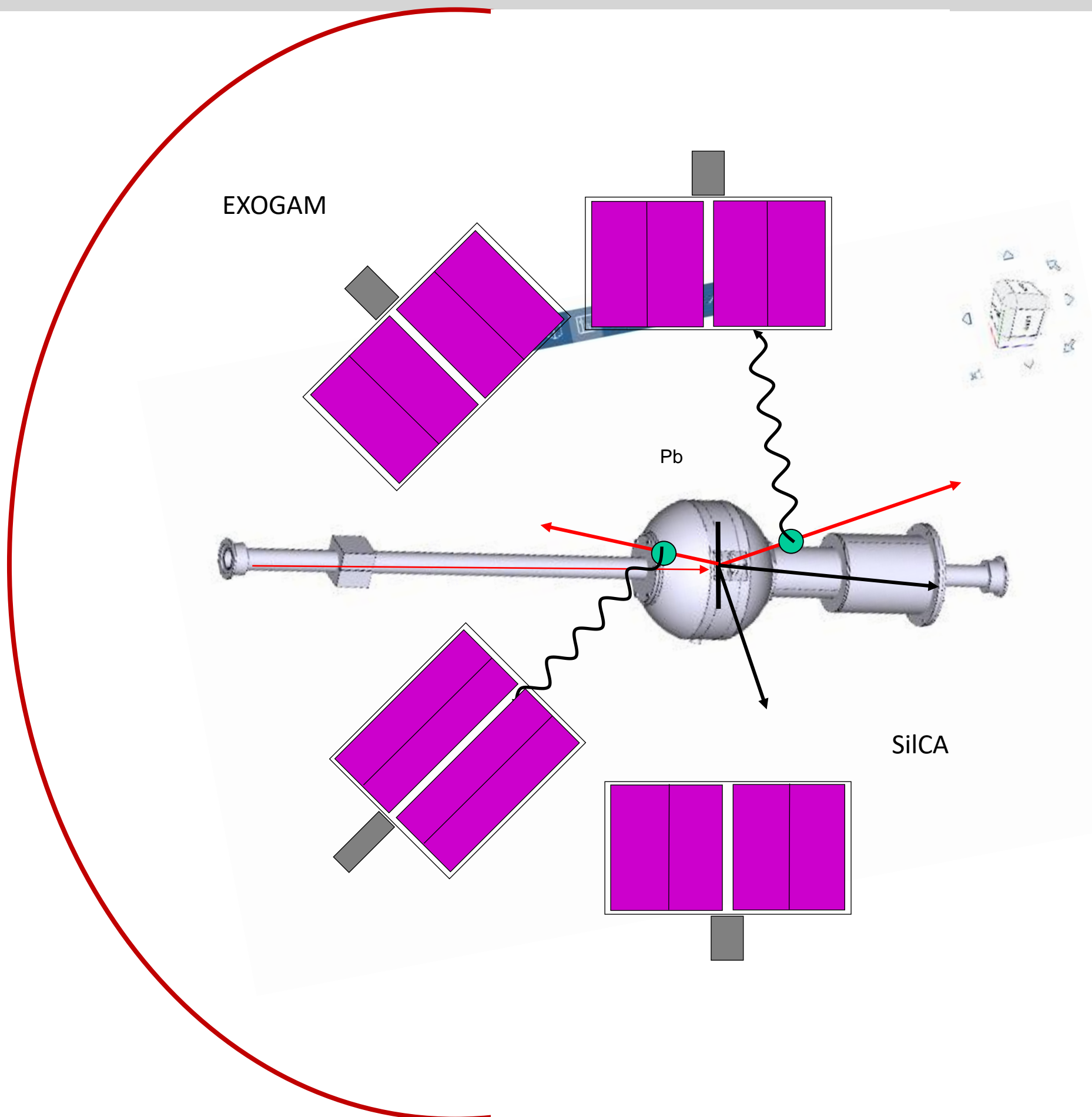
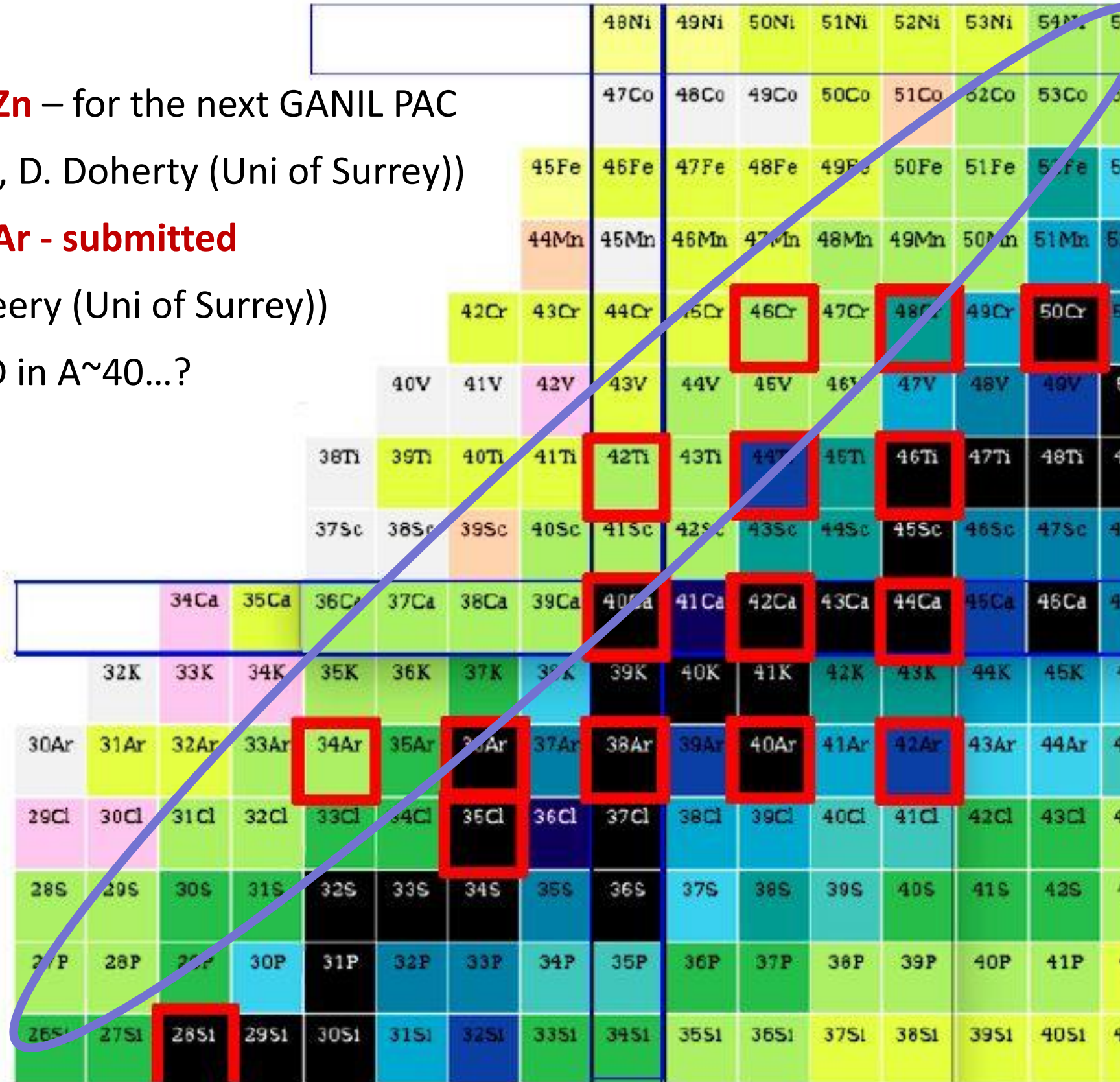
1. An independent measurement of the $B(E2, 4^+ \rightarrow 2^+)$ to study the $B_{4/2}$ anomaly
2. The study of the non-yrast states collectivity
3. A first measurement of $Q_s(2^+, 4^+)$
4. Shape parameters for the 0^+_1



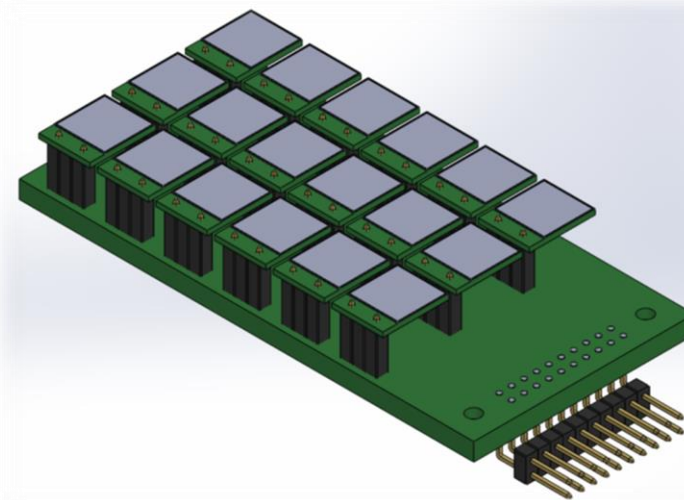
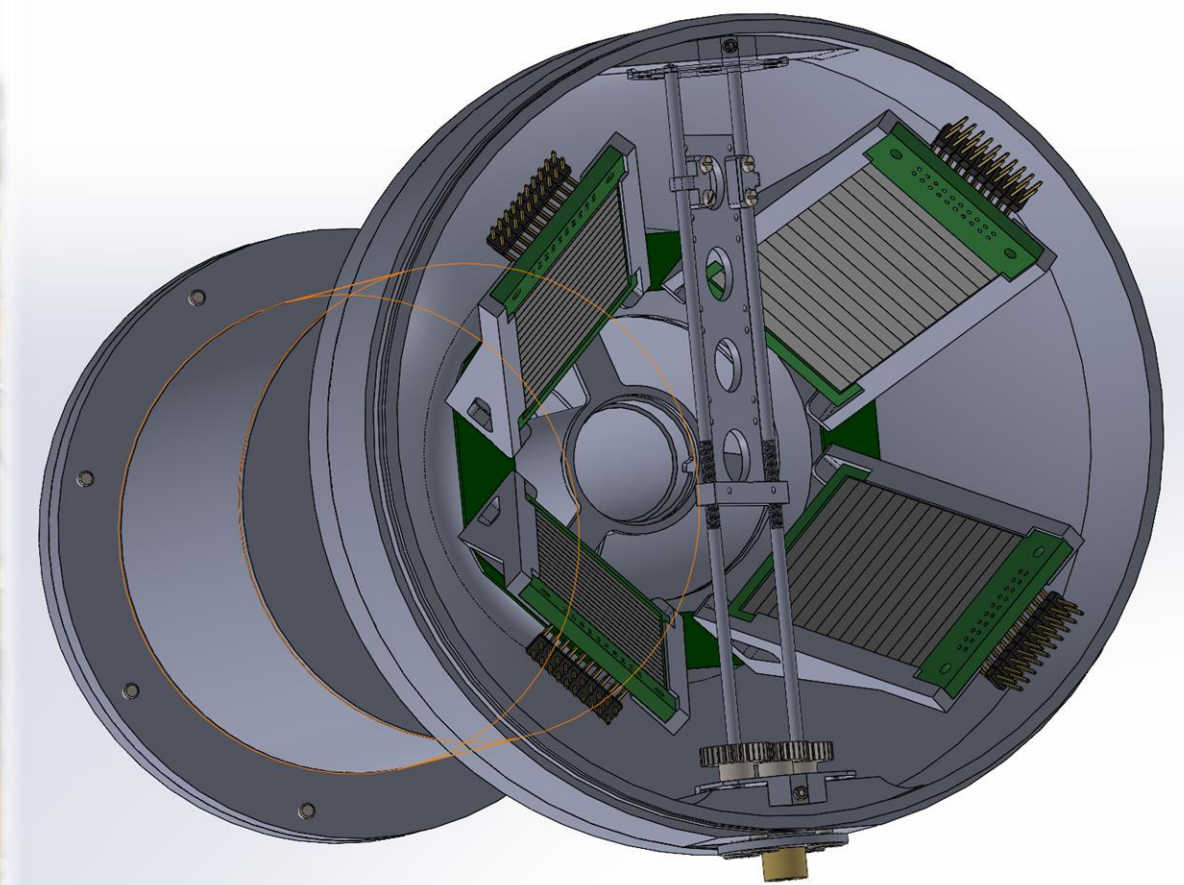
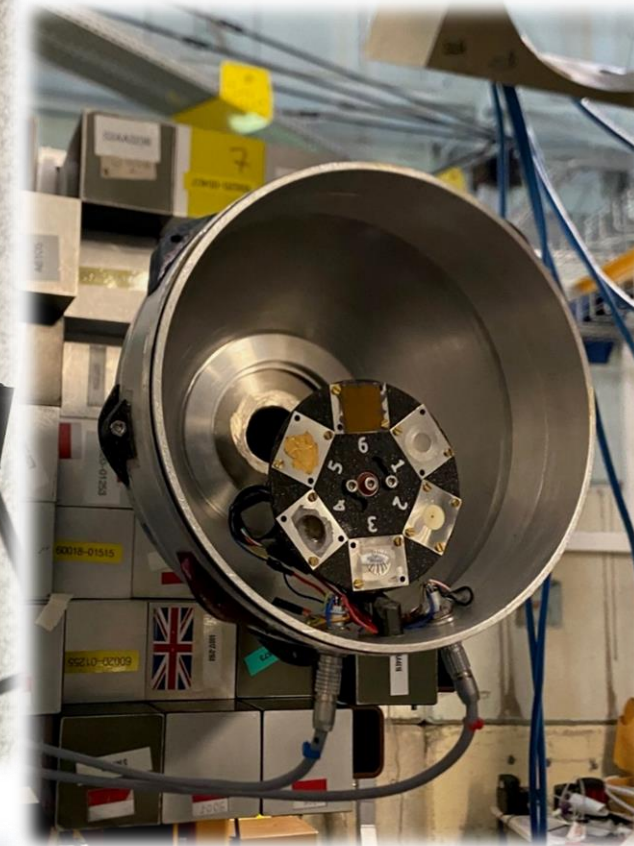
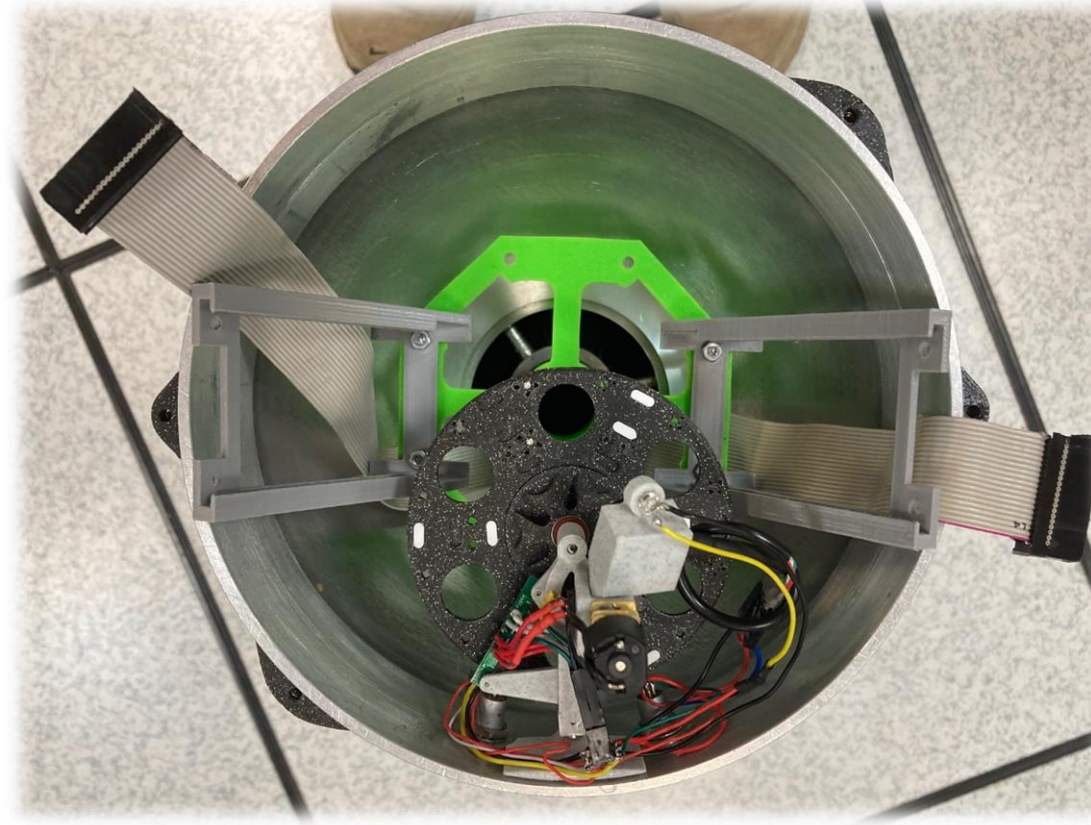
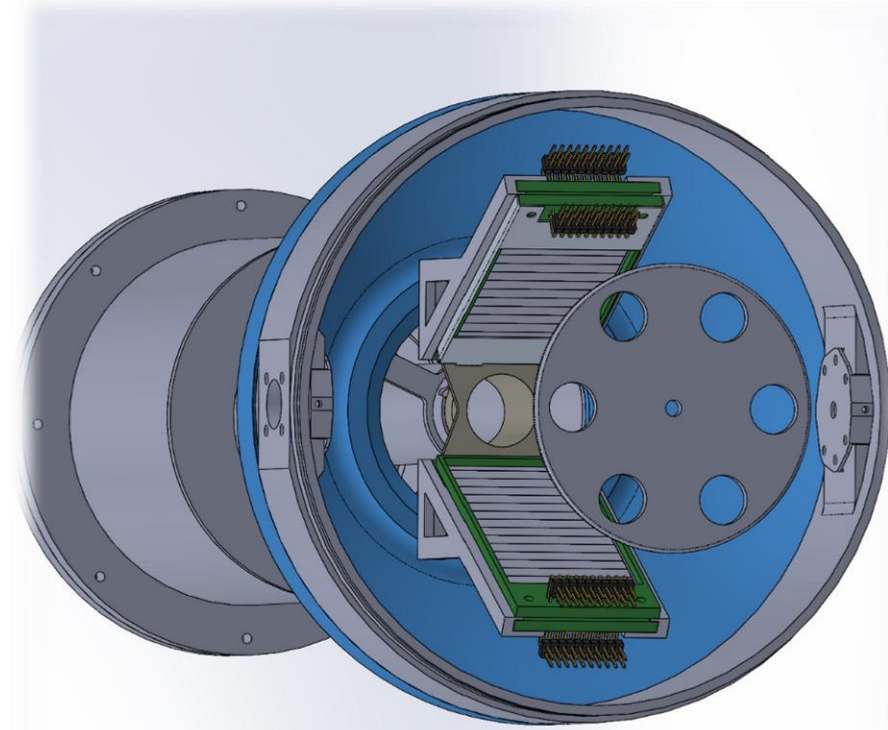
- 1 mg/cm^2 ^{208}Pb target
- 21 UT
- $6 \cdot 10^4$ pps SPIRAL1 beam at the target position
- GOSIA Analysis – PL-FR-Agreement

SilCA @ GANIL (new projects)

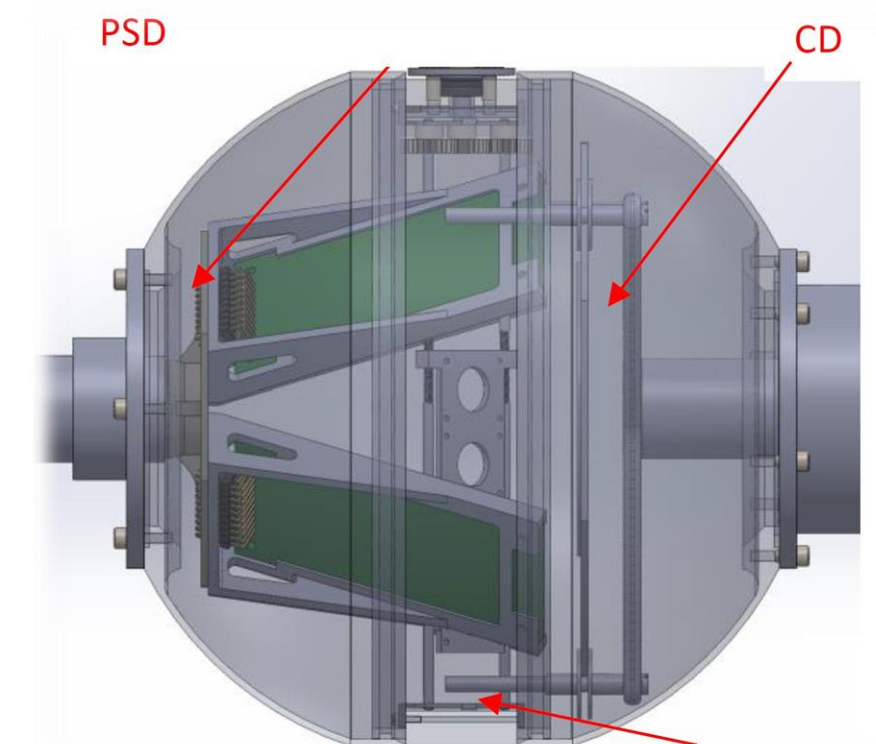
- ^{62}Zn – for the next GANIL PAC
(KHK, D. Doherty (Uni of Surrey))
- ^{34}Ar - submitted
(J. Heery (Uni of Surrey))
- SD in $A \sim 40 \dots ?$



SilCA - DSSD and beyond!



- Position-sensitive DSSD detectors (Micron X3, 43.3 × 78 mm) E or E-dE
- A set of pin-diodes
- Scintillators



Summary

- PAST – exciting
- PRESENT – steady but busy
- FUTURE – bright

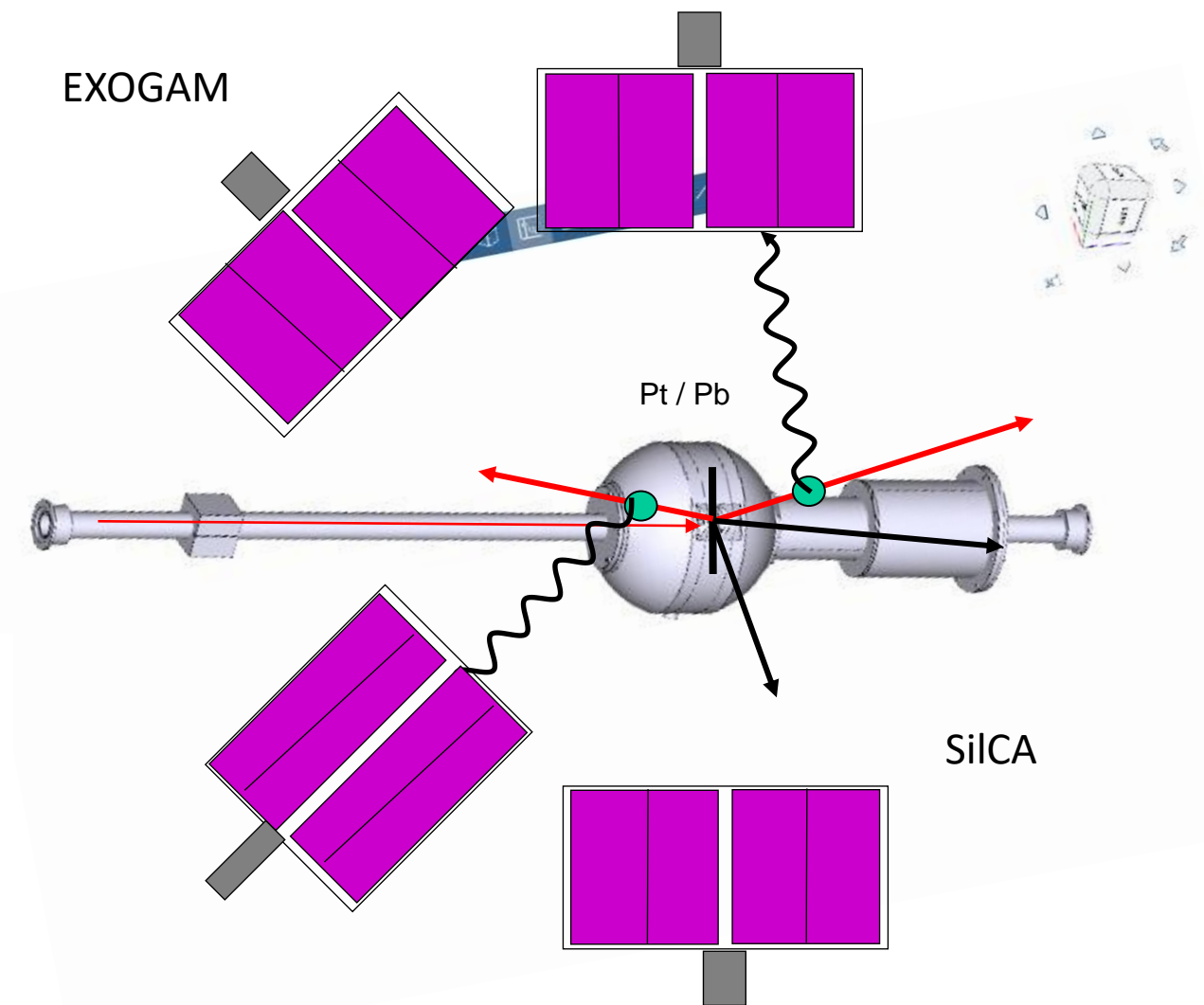
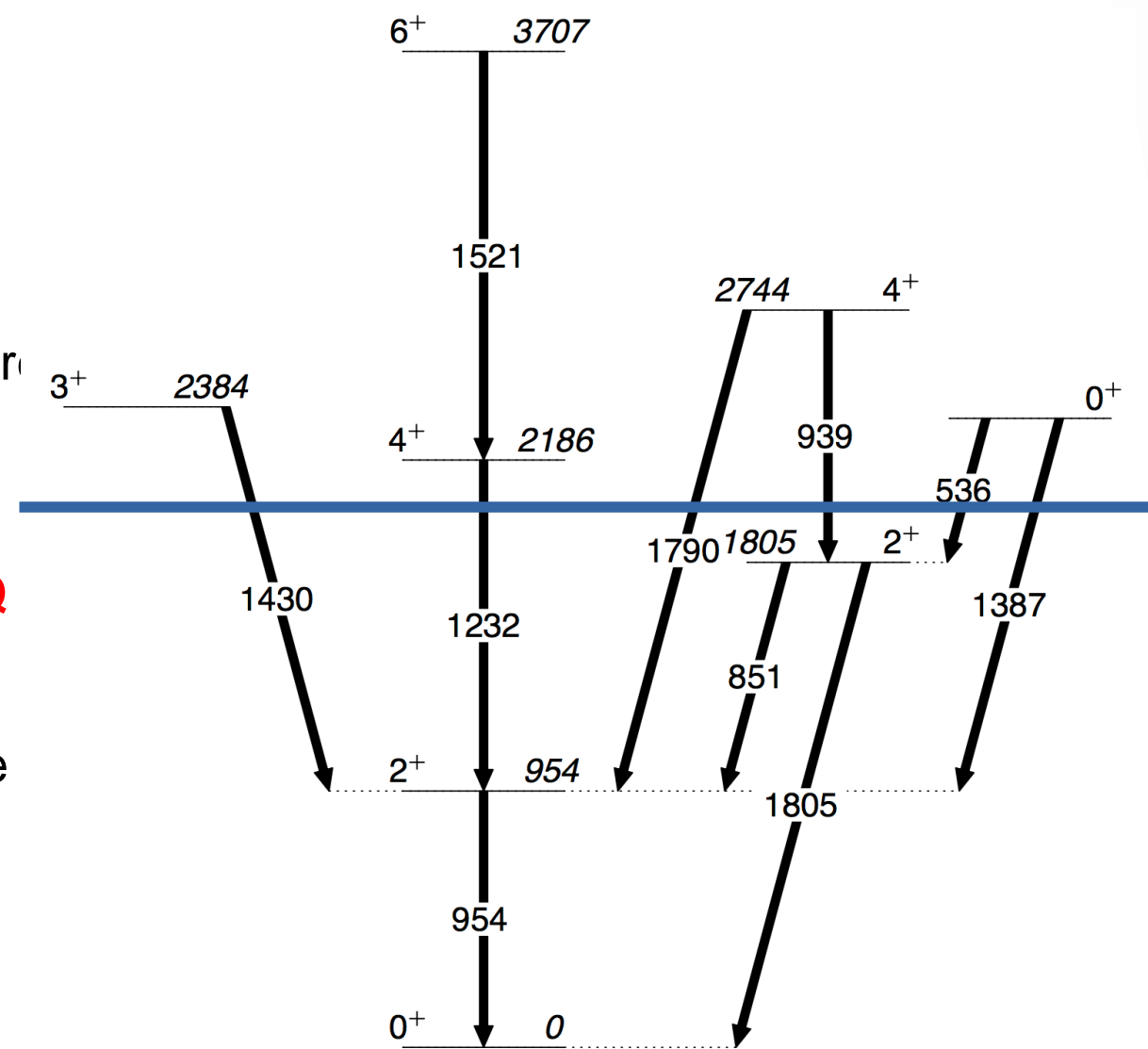


Thank you
Merci
Dziękuję



SilCA @ GANIL (PAC 2026) - ^{62}Zn

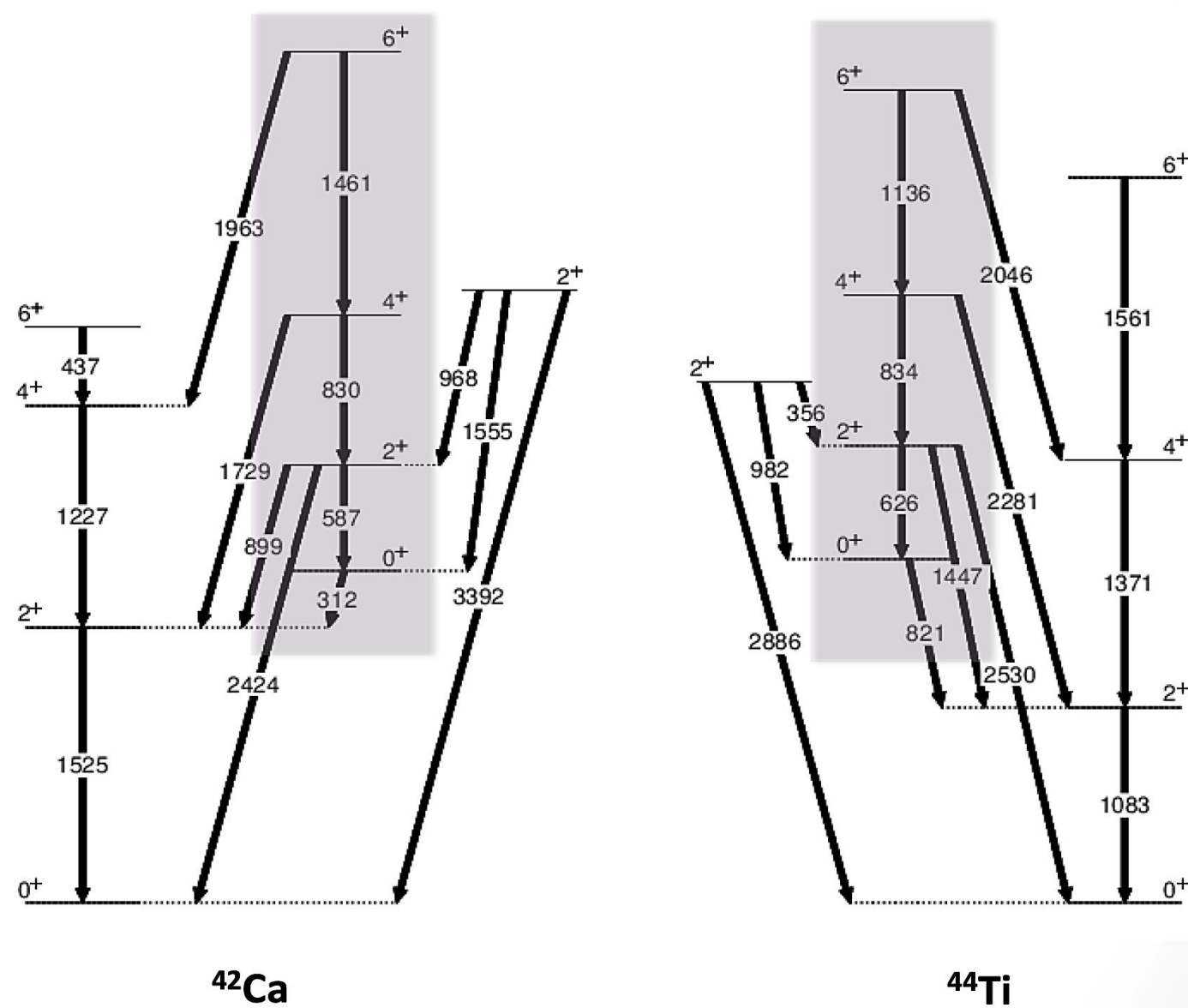
- To populate states in the yrast and non-yrast low-spin states in ^{62}Zn with the safe Coulomb excitation
- To extract a complete set of matrix elements (including $Q(2_1^+)$ and $Q(2_2^+)$) in order to describe the low-lying structure of ^{62}Zn
- To determine quadrupole deformation of the 0_1^+ and 0_2^+ states by applying the Quadrupole Sum Rules method – direct measurement of the deformation
- To provide the experimental input in the discussion of the role of nuclear shapes in the astrophysical *rp*-process
- Excitation of states in ^{62}Zn **above 2 MeV** will help to extract the structure of ^{62}Ge
- States of interest in ^{62}Ge – above proton separation energy: **2053(145) keV** – very low - “exotic” case
- The **quadrupole deformation in ^{62}Zn** is expected to strongly influence **the mirror energy difference** – to be used to predict when these states are placed in ^{62}Ge
- The triaxial degree of freedom has a strong influence on the binding energies, hence the nuclear masses and the reaction Q values**
- If triaxial deformation is established in *p*-rich nuclei taking part of the *rp* process, this would change dramatically **the recent mass systematics** – masses are unmeasured
- Shapes in ^{62}Ge** – unknown – so measurement of shapes in ^{62}Zn – the only way to study states in inaccessible ^{62}Ge



**Safe Coulomb excitation of ^{62}Zn
to be re-proposed at GANIL
KHK, D. Doherty**

- EXOGAM2 + SiLCA
- $\sim 10^5$ pps SPIRAL1 beam at the target position

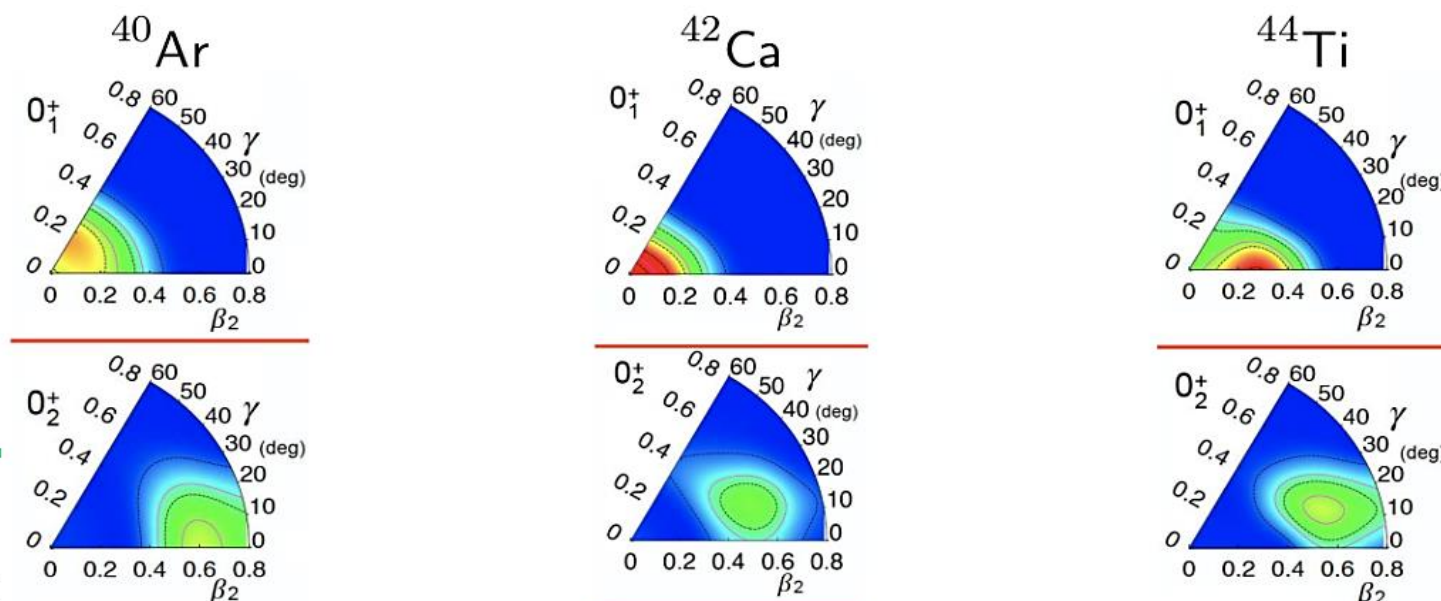
Coulomb excitation of ^{44}Ti @ GANIL or @ IJC Lab



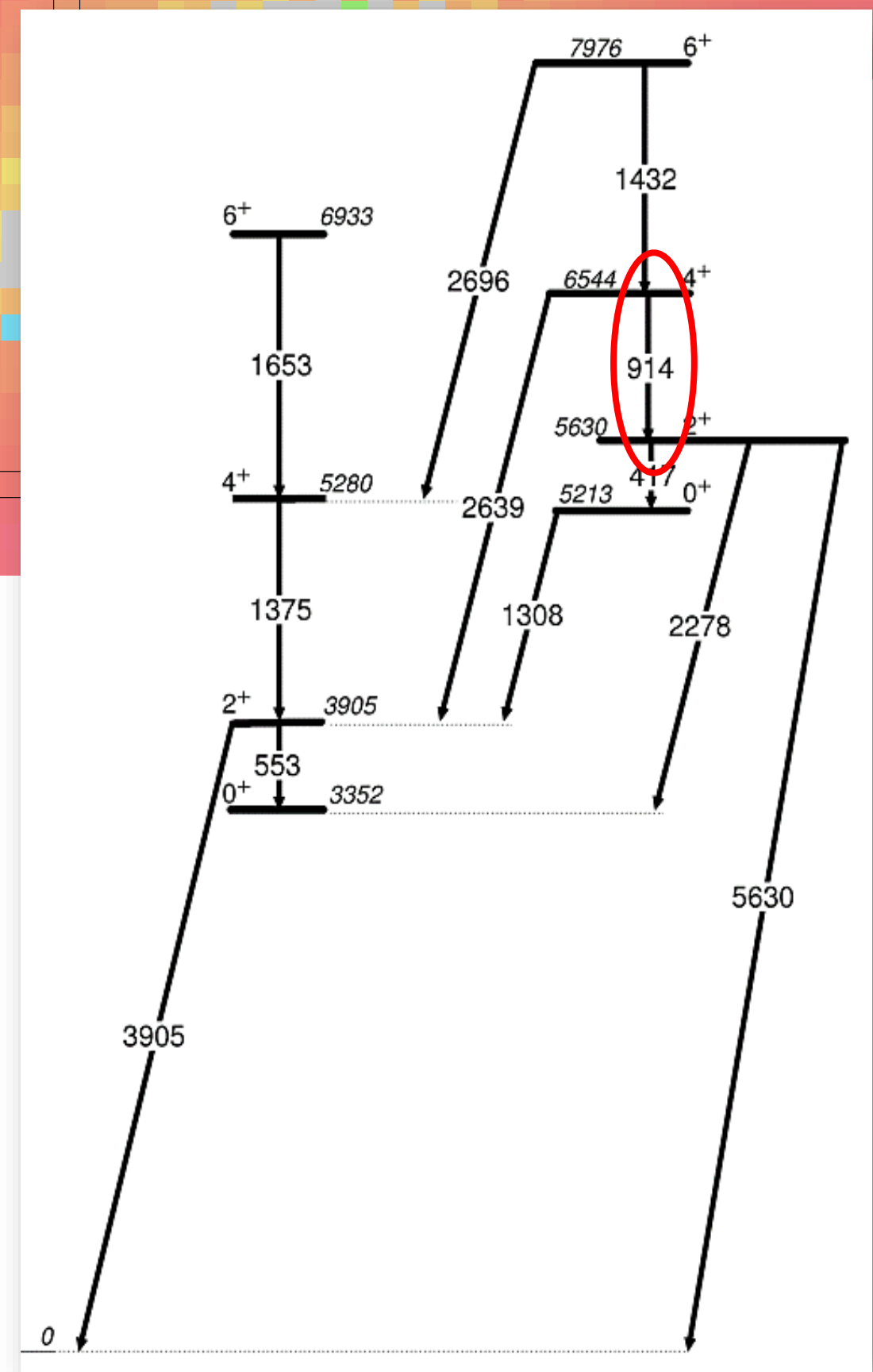
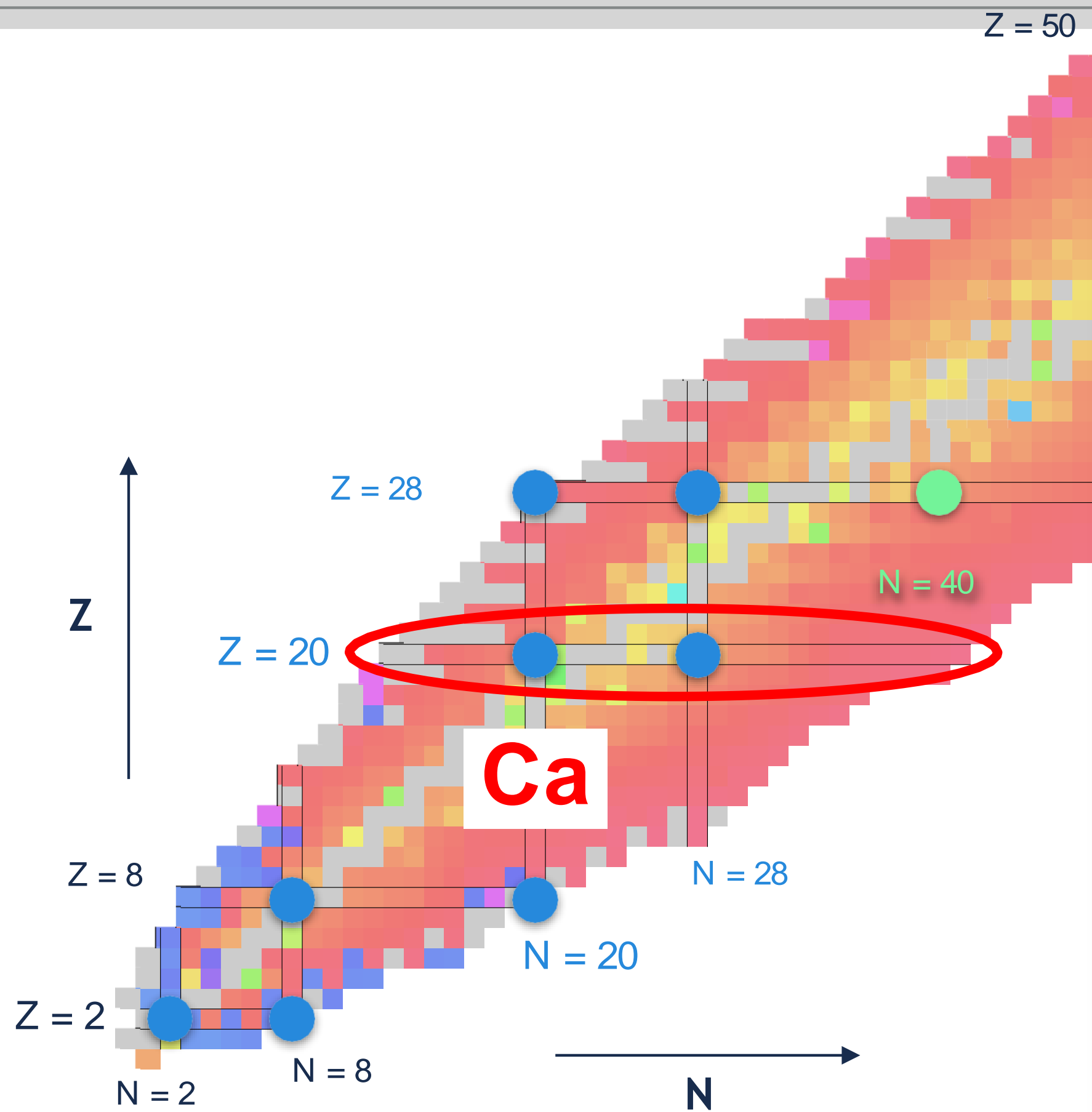
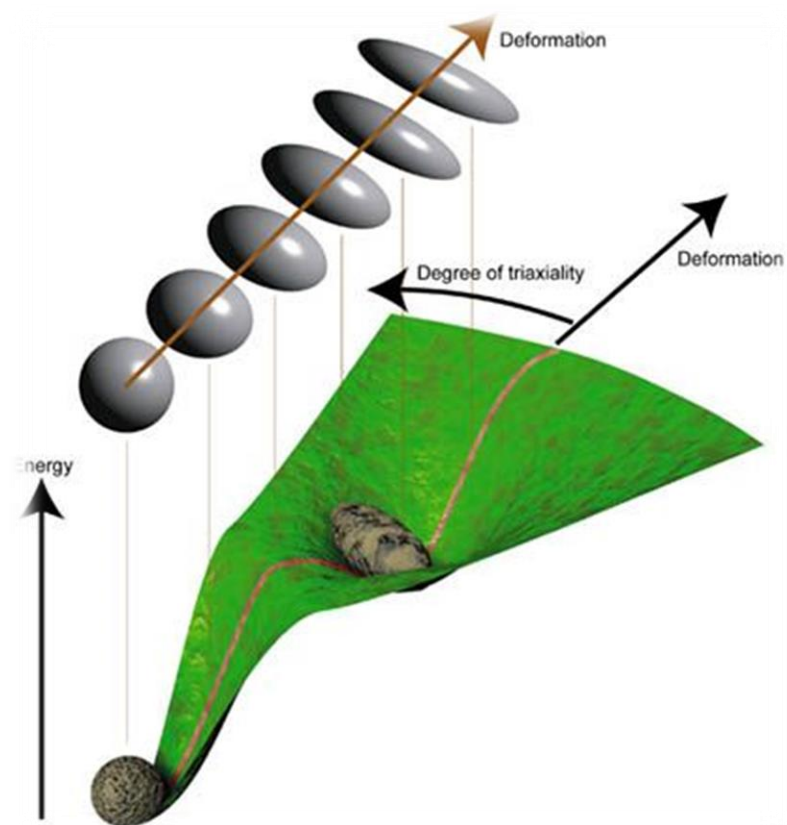
- ✓ A long-lived radioactive nucleus
- ✓ $Q_s(2^+_1)$ and $Q_s(2^+_2)$ unknown
- ✓ 0^+_2 is localized but the lifetime is unknown
- ✓ The decay of the 0^+_2 is unknown
- ✓ The best option would be to populate side band from GS

Additional motivation: **one of a few cosmic γ -ray emitters** to be observed in our Galaxy - may provide the means to unravel the underlying **explosion mechanism of Type-II Supernovae**

- ✓ expected to be synthesized in the **α -rich freeze out process**, via the $^{40}\text{Ca}(\alpha, \gamma)$ reaction
- ✓ how much of the newly produced ^{44}Ti that is caught in the matter of neutron star of a black hole is linked to the hydrodynamics of the star
- ✓ **gamma rays from ^{44}Ti material that falls back will be unable to escape the dense environment and cannot be observed**
- ✓ **the observed ^{44}Ti abundances by modern-day space-based telescopes vs predicted production values will provide a measure of the location of the mass cut.**
- ✓ large uncertainties in the nuclear reactions responsible for the production and destruction of ^{44}Ti in core-collapse SN make these comparisons extremely difficult
- ✓ a key unknown may relate to the **ground state shape of ^{44}Ti .**



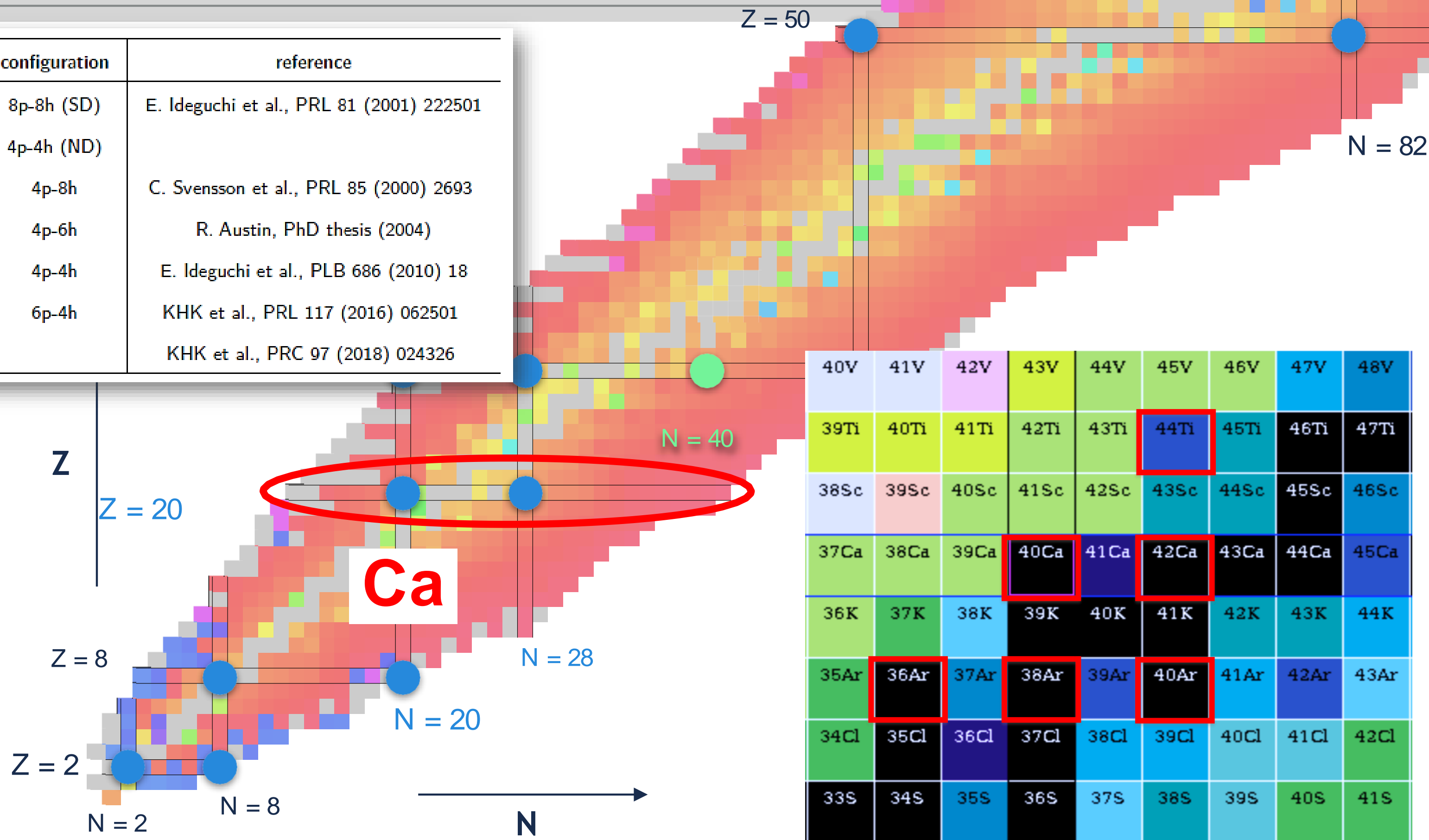
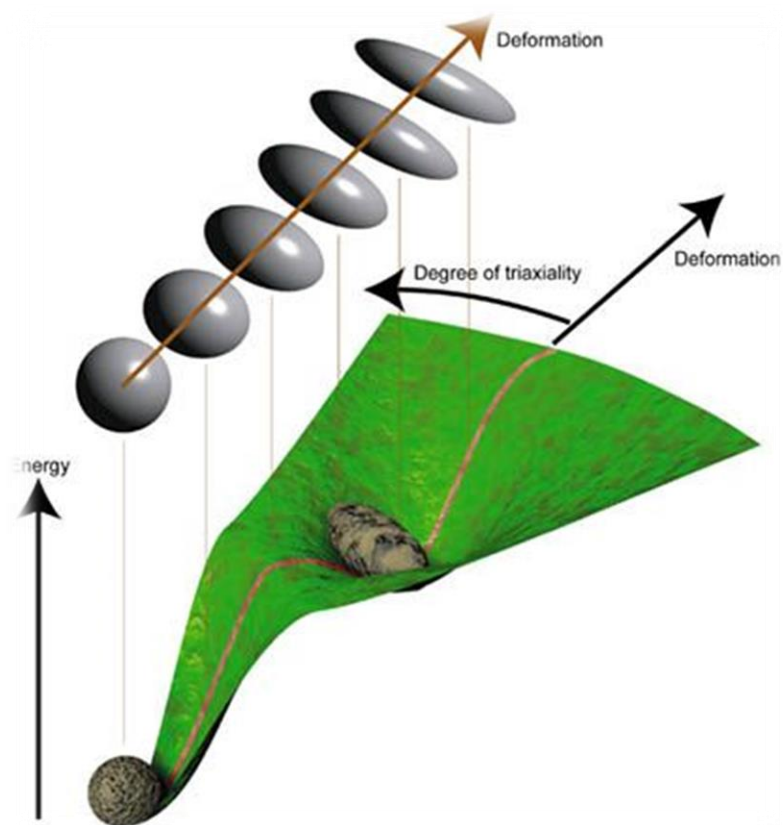
(Super)-Deformation about ^{40}Ca ($Z=N=20$)



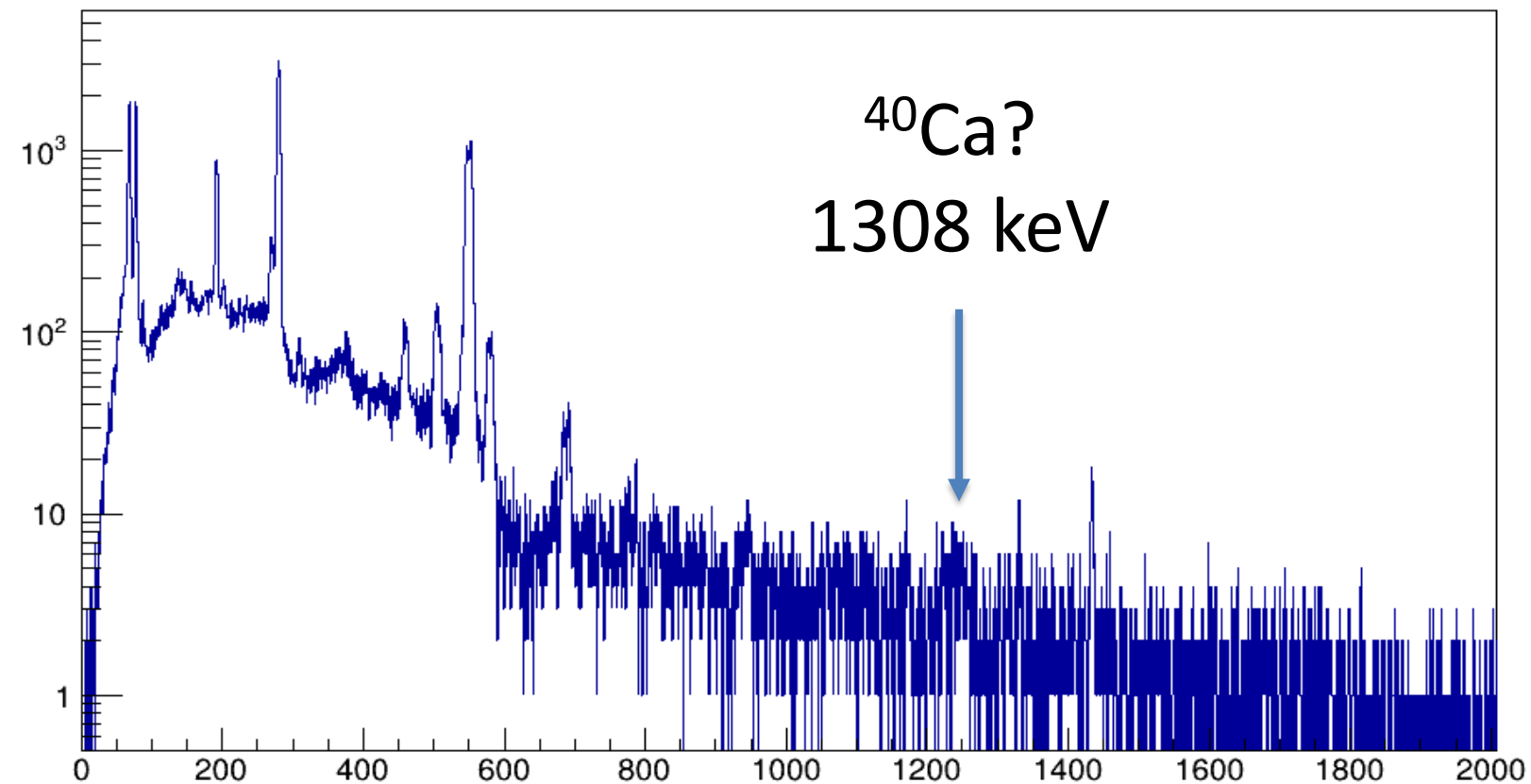
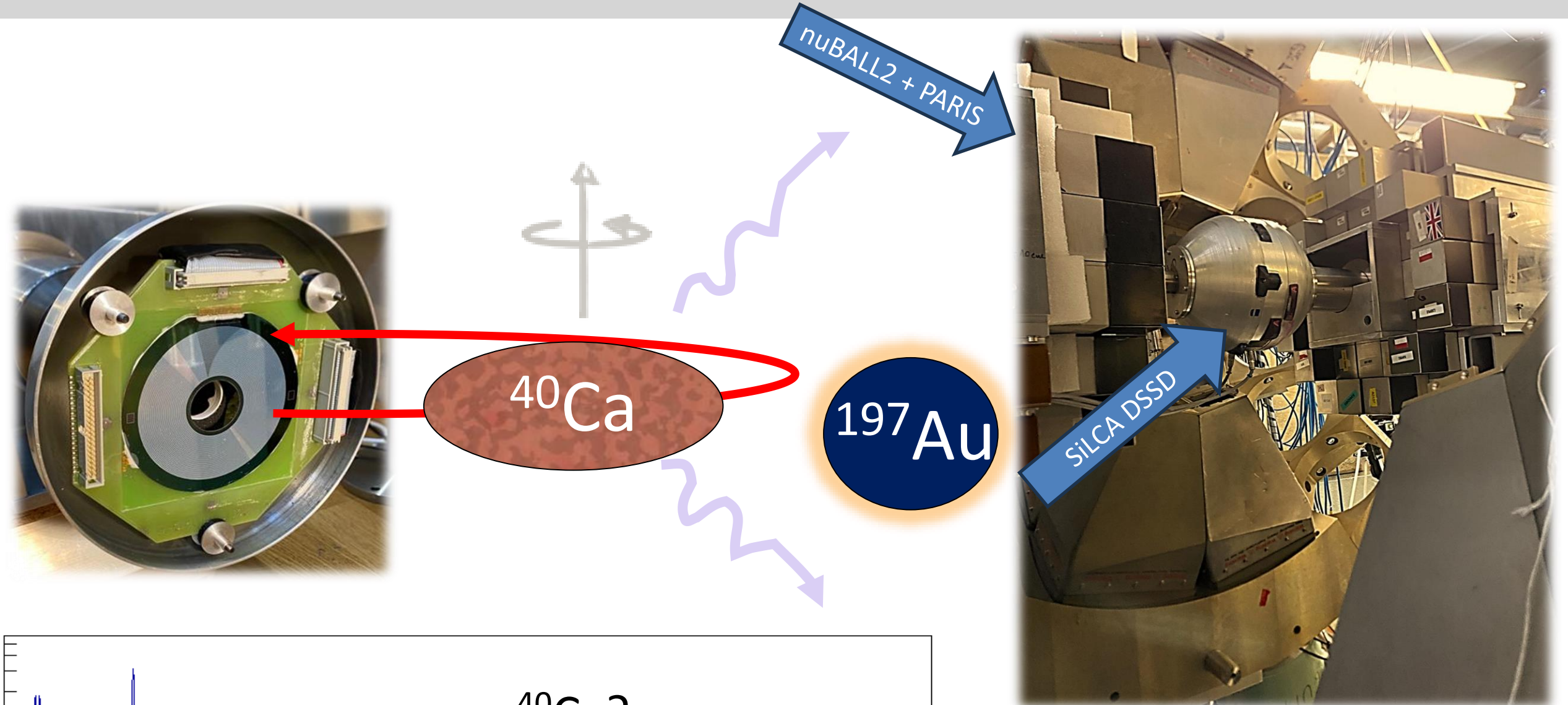
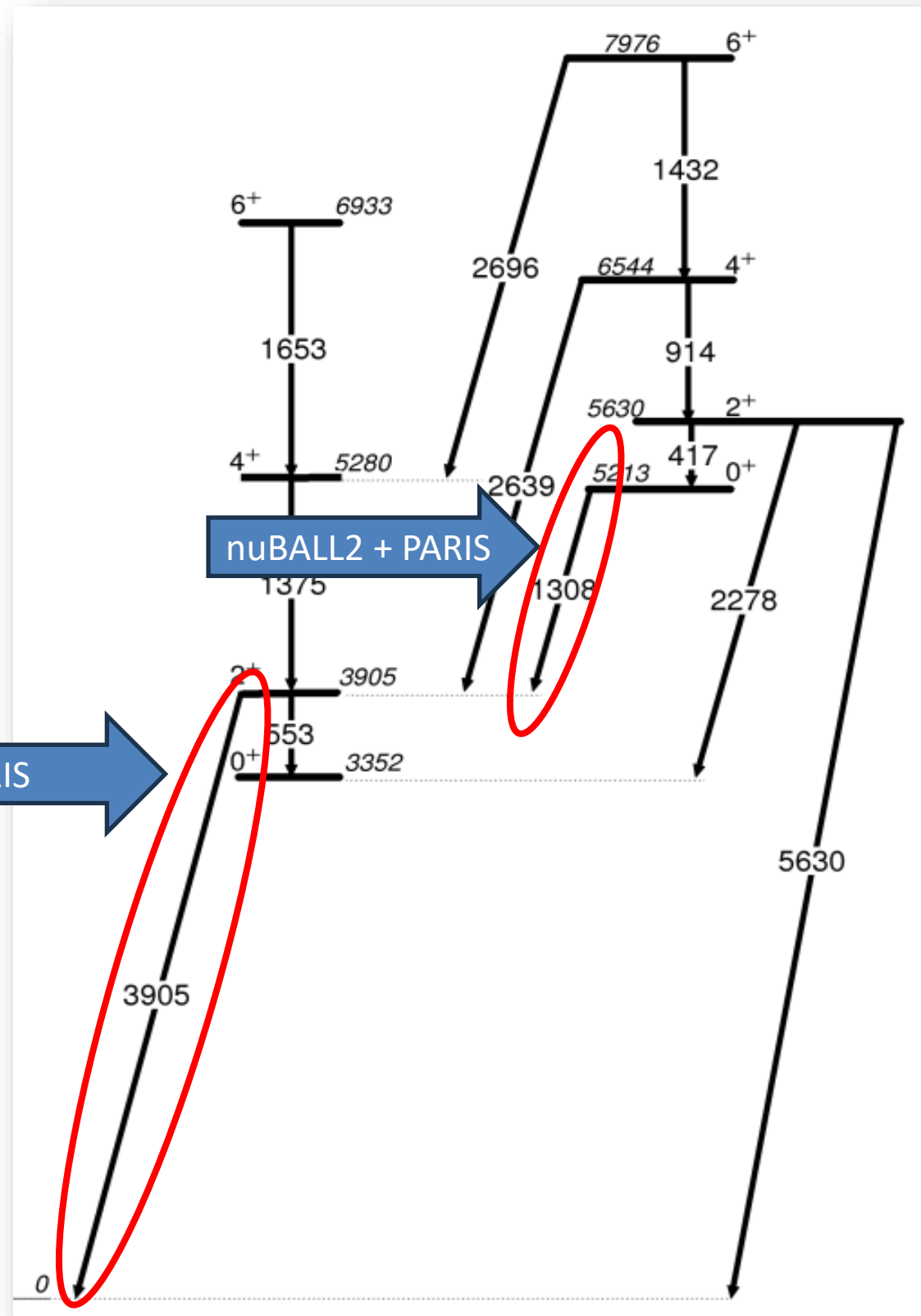
N = 82

(Super)-Deformation about ^{40}Ca ($Z=N=20$)

isotope	0^+ energy	experimental β_2	configuration	reference
^{40}Ca	5.2 MeV	$0.59^{+0.11}_{-0.07}$	8p-8h (SD)	E. Ideguchi et al., PRL 81 (2001) 222501
	3.4 MeV	0.27 ± 0.05	4p-4h (ND)	
^{36}Ar	(4.3 MeV)	0.46 ± 0.03	4p-8h	C. Svensson et al., PRL 85 (2000) 2693
^{38}Ar	3.4 MeV	$0.42^{+0.11}_{-0.08}$	4p-6h	R. Austin, PhD thesis (2004)
^{40}Ar	2.1 MeV	$0.48^{+0.16}_{-0.10} \pm 0.05$	4p-4h	E. Ideguchi et al., PLB 686 (2010) 18
^{42}Ca	1.8 MeV	$0.43(4) (0_2^+)$	6p-4h	KHK et al., PRL 117 (2016) 062501
		$0.45(4) (2_2^+)$		KHK et al., PRC 97 (2018) 024326

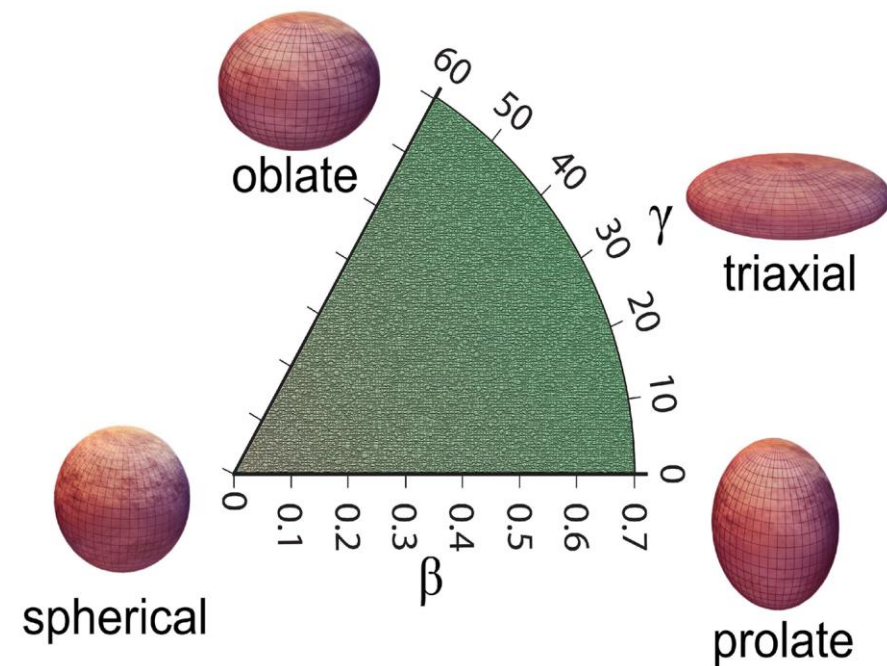


Coulomb excitation of ^{40}Ca @ IJC Lab [N-SI-85]



- nuBALL2:**
2 rings of 12+12 HPGe CLOVERS + ACS
- PARIS:**
LaBr3 / CeBr3 + NaI array
15 cm from the target
- SiLCA DSSD:**
32 sectors + 16 rings
125-152°

Quadrupole shape invariants

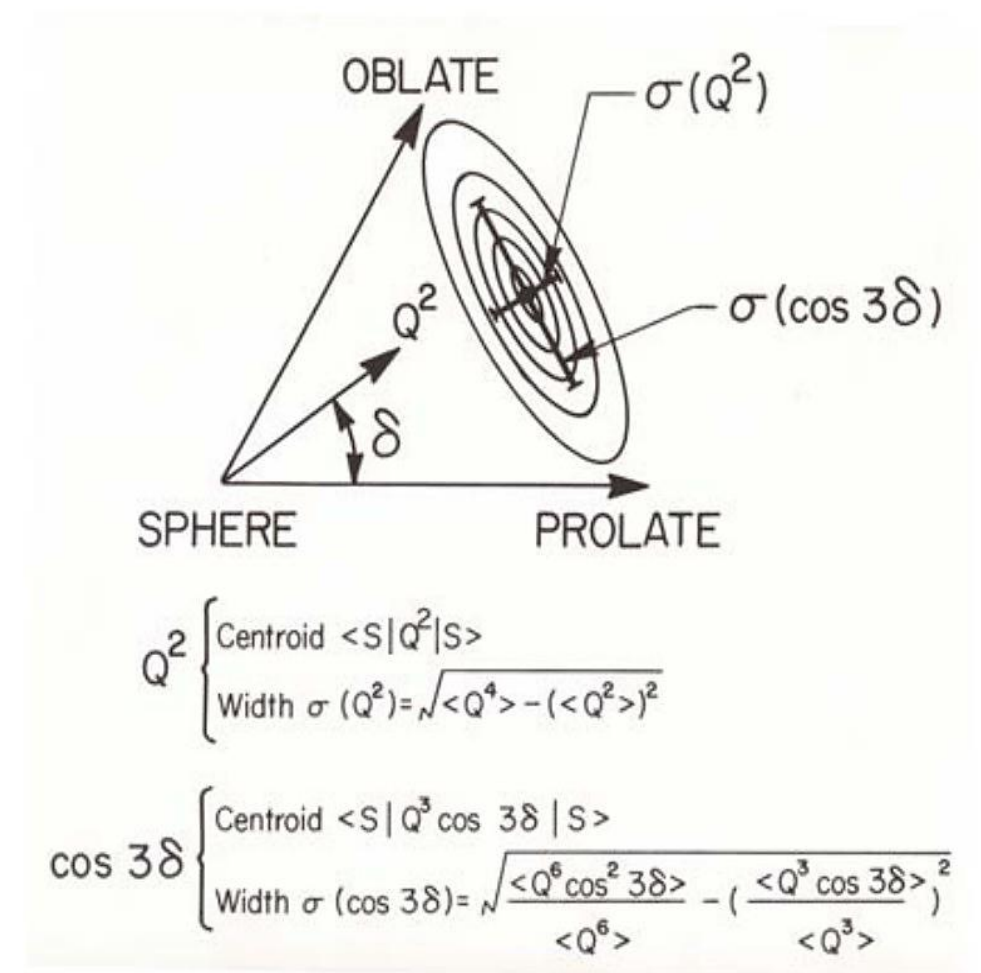
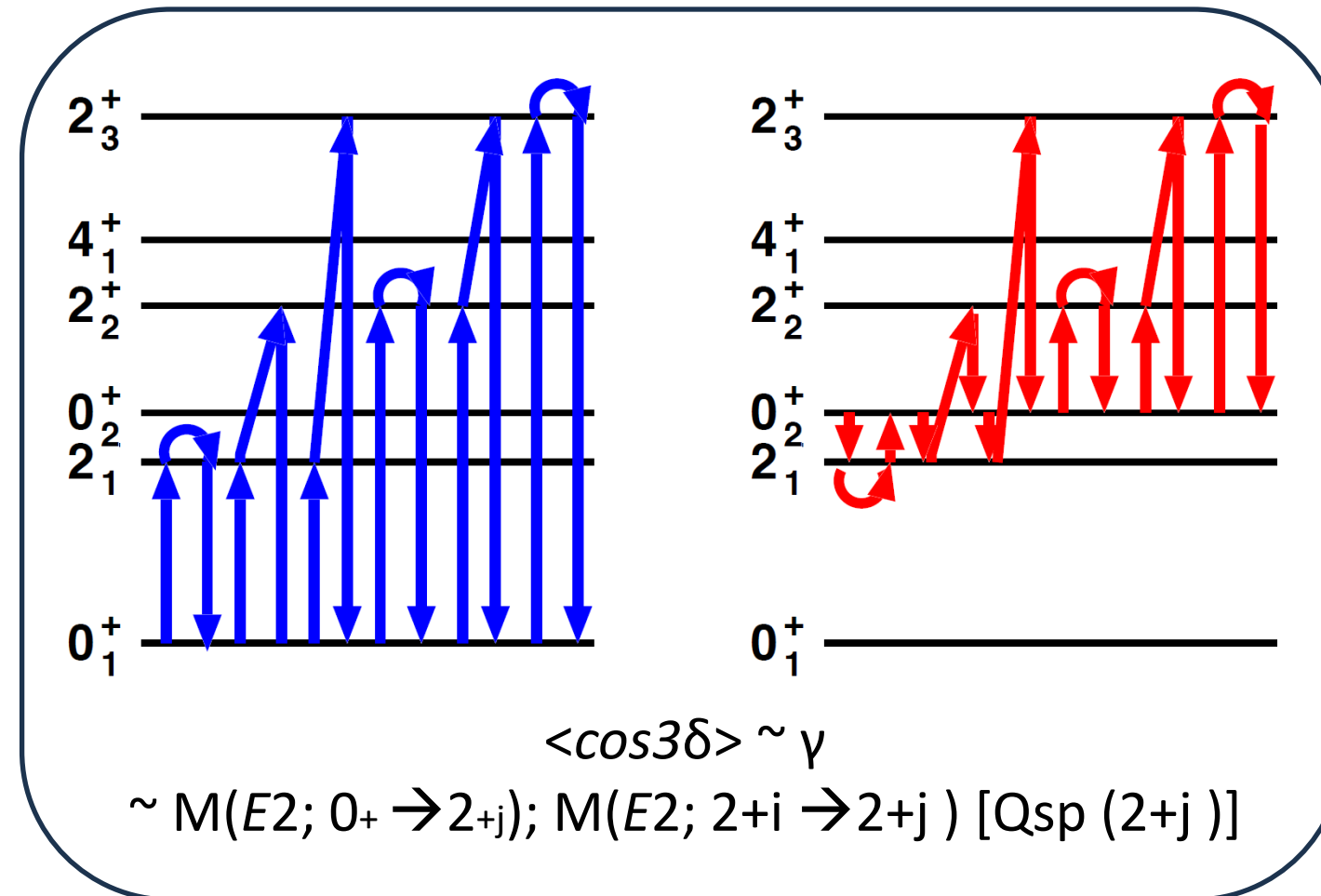
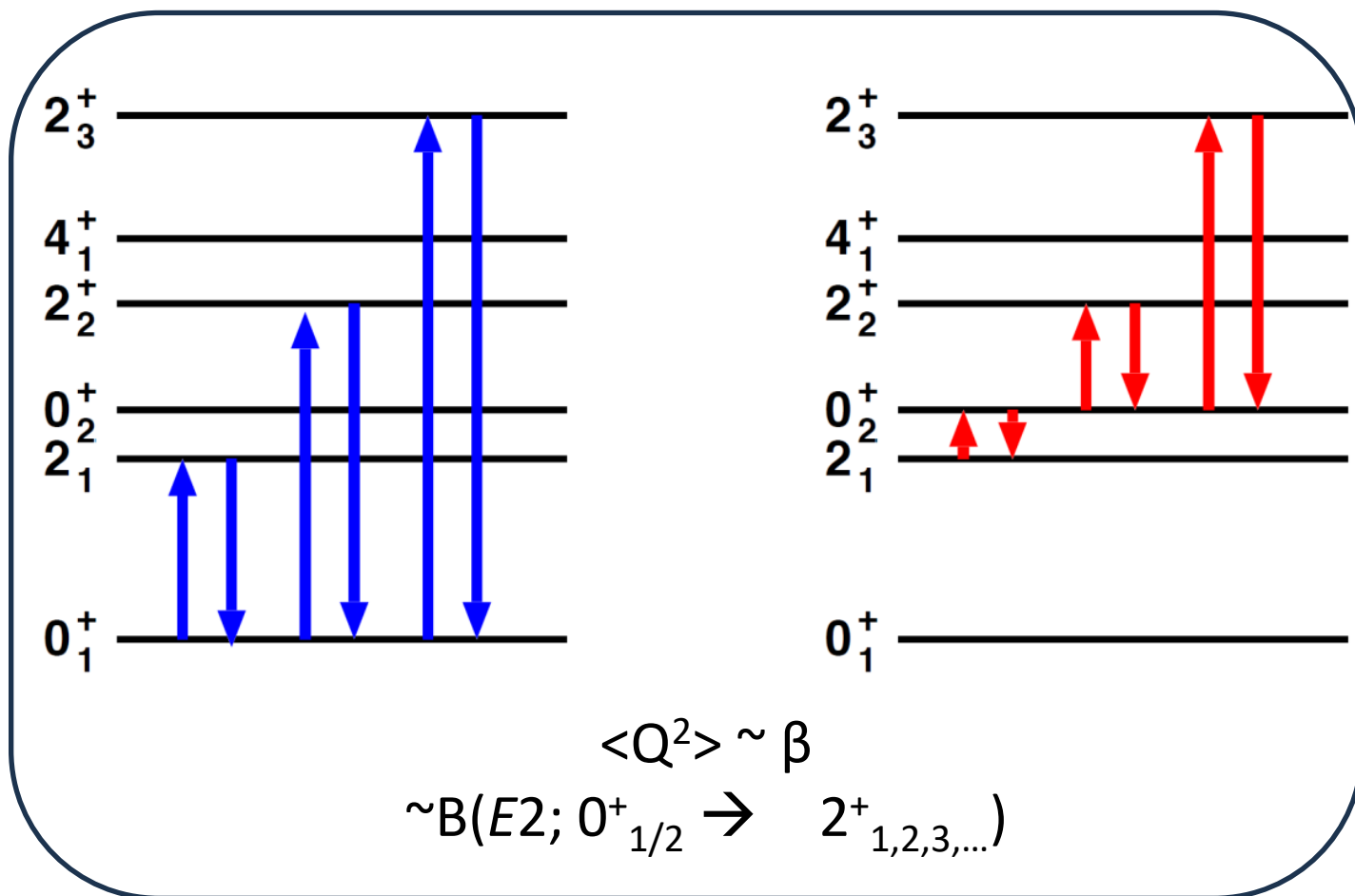


Overall deformation – elongation

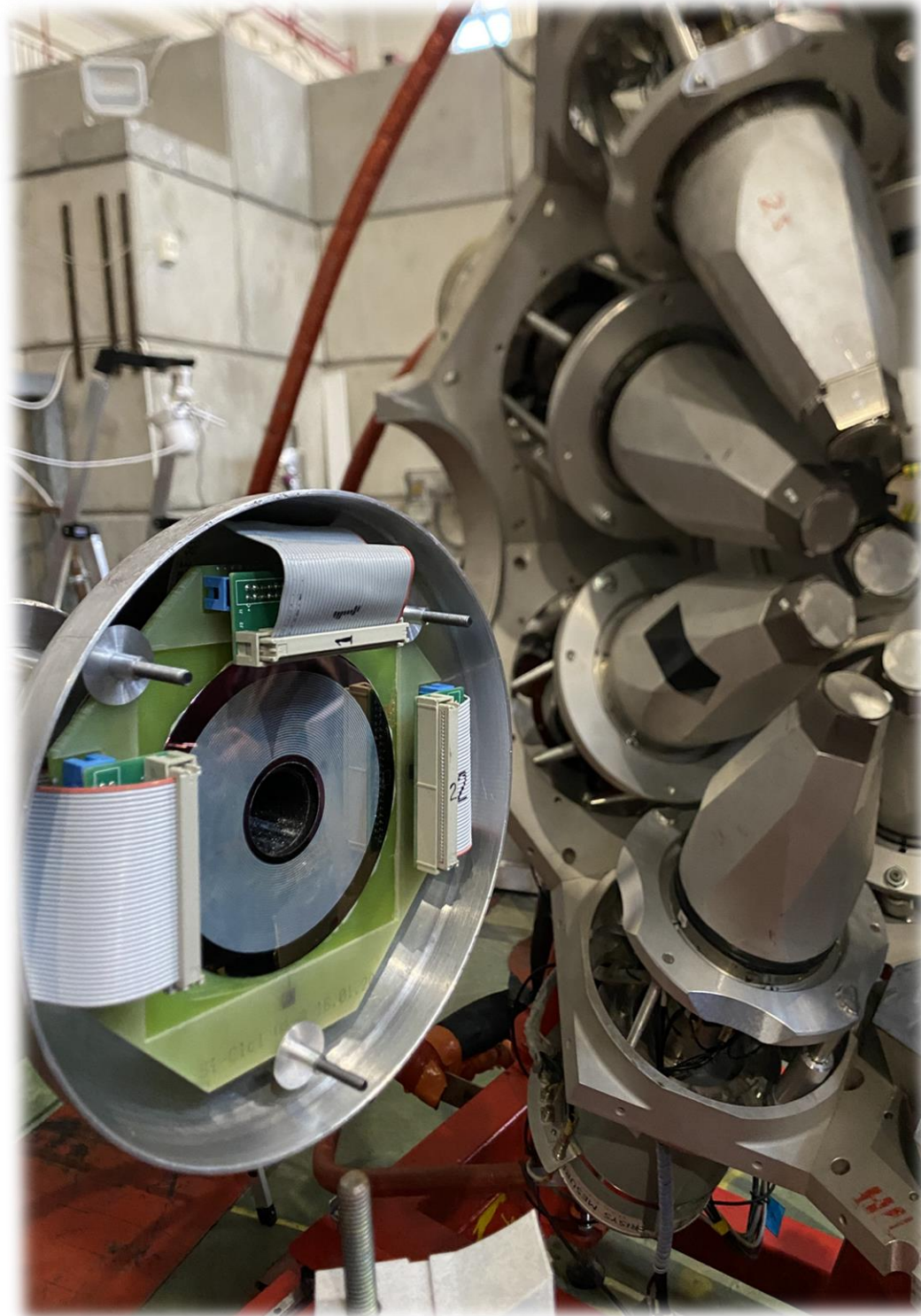
$$\frac{\langle Q^2 \rangle}{\sqrt{5}} = \langle i || [E2 \times E2]^0 || i \rangle = \frac{(-1)^{(2I_i)}}{\sqrt{2I_i + 1}} \sum_t \langle i || E2 || t \rangle \langle t || E2 || i \rangle \begin{Bmatrix} 2 & 2 & J \\ I_i & I_i & I_t \end{Bmatrix}$$

Axial symmetry parameter

$$\sqrt{\frac{2}{35}} \langle Q^3 \cos(3\delta) \rangle = \langle i || \{ [E2 \times E2]^2 \times E2 \}^0 || i \rangle = \frac{(\pm 1)}{\sqrt{2I_i + 1}} \sum_{t,\mu} \langle i || E2 || u \rangle \langle u || E2 || t \rangle \langle t || E2 || i \rangle \begin{Bmatrix} 2 & 2 & 2 \\ I_i & I_t & I_u \end{Bmatrix}$$



DSSD tests with ^{241}Am



Setup:

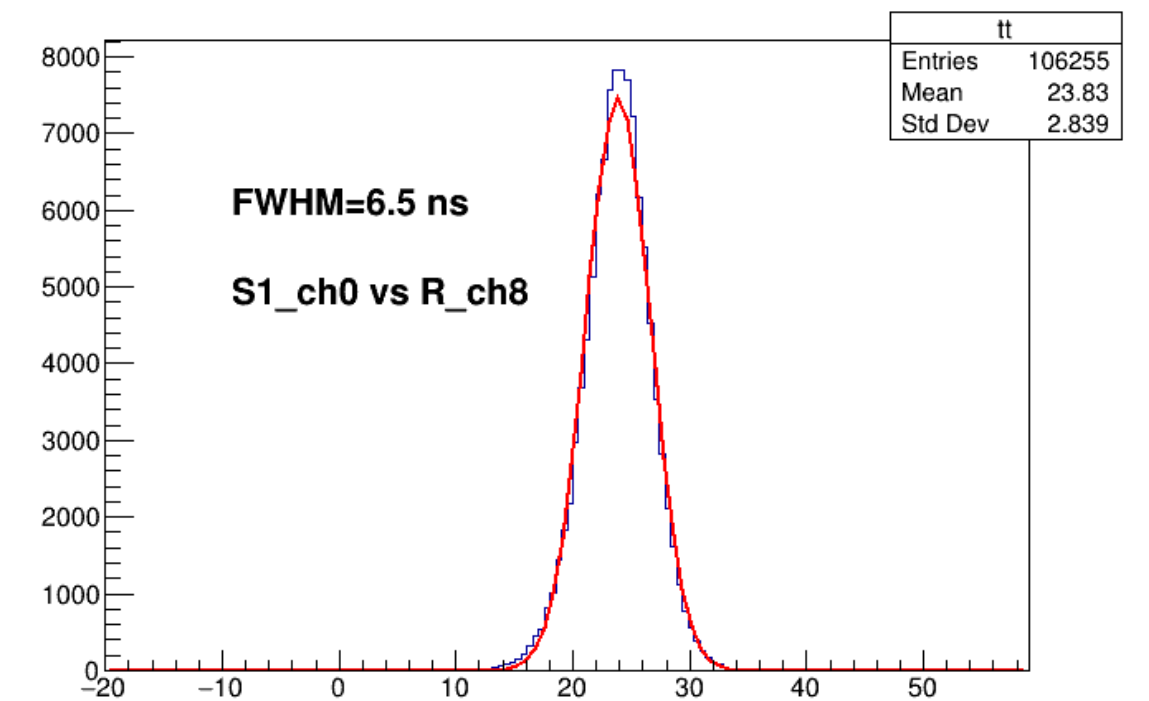
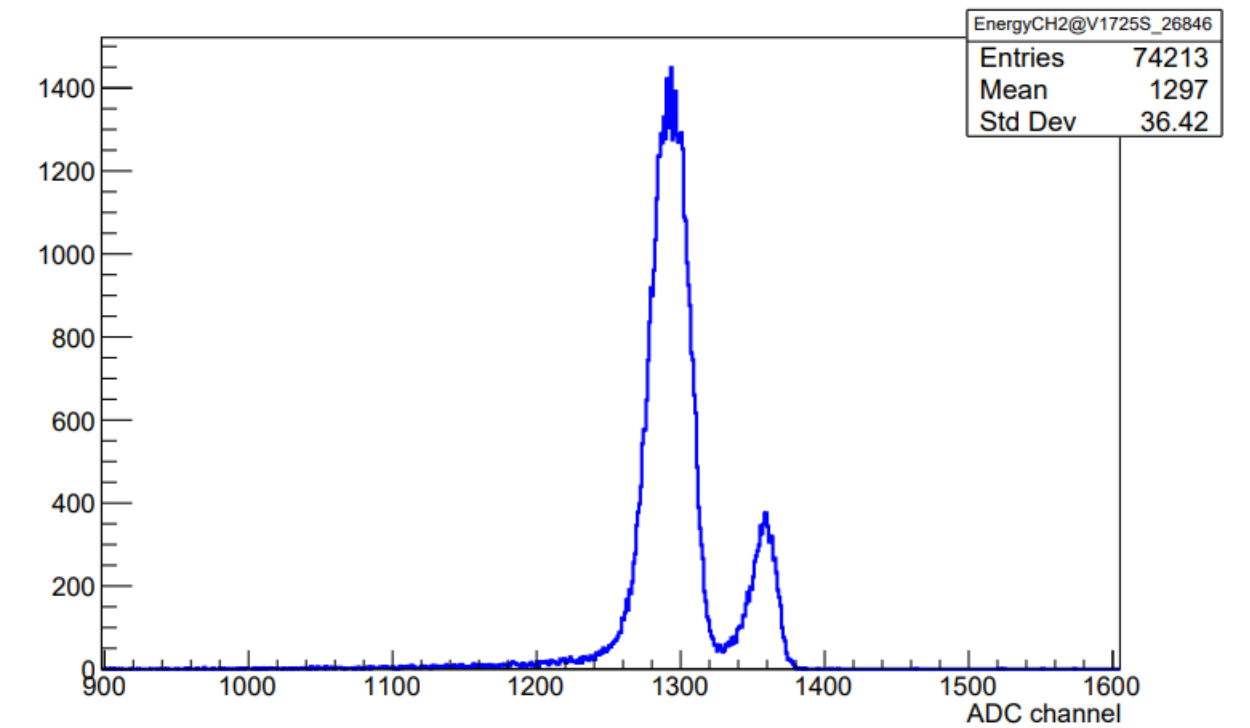
- DSSD detector
- 64 sectors (32 readout)
- 32 rings (16 readout)
- 3 differential-to-single-ended converters (made at HIL & FUW)
- 3 CAEN 1725 digitizers 16-channel, 14 bit, 250 MS/s
- ^{241}Am source
- 5.1 MeV Energy

Data taken with:

- COMPASS (CAEN software)
- xdaq

Results:

- Obtained energy resolution: ~ 50 keV
- Obtained sector-ring timing resolution: 6.5-8.5 (1) ns



In-beam commissioning of SiLCA+EAGLE
scheduled: November 2024
 $^{104}\text{Pd} + ^{32}\text{S}$, Coulomb excitation



Experimental nuclear deformation

- **Nuclear deformation** is one of a central topic in the **COPIN and COPIGAL** collaborations
- Experiments such as **Coulomb excitation** or **gamma-ray spectroscopy** are used to investigate nuclear shapes, including highly deformed or transitional states, to advance the understanding of how atomic nuclei deform and the consequences of these deformations for nuclear structure.

French Institutes:

- **GANIL** (Grand Accélérateur National d'Ions Lourds) in Caen 
- **CNRS/IN2P3** (L'Institut national de physique nucléaire et de physique des particules) facilities, including **IJC Lab** (Laboratoire de Physique des 2 Infinis Irène Joliot-Curie) in Orsay 
- **CEA Saclay** (Commissariat à l'Énergie Atomique et aux Énergies Alternatives) 

Polish Institutes:

- Heavy Ion Laboratory and Faculty of Physics, University of Warsaw 
- Institute of Nuclear Physics (IFJ PAN), Kraków 



Coulomb excitation studies within COPIGAL

Task: Nuclear deformation in excited states

- Superdeformation at low spins (E. Clement, K. Hadyńska-Klęk, P. Napiorkowski*)*
- Shape coexistence in $A \sim 100$ nuclei (M. Zielińska, K. Wrzosek-Lipska)*

Coulomb excitation studies within COPIN tasks:

Task: Exotic nuclear deformations studied at HIL and ALTO (J. Wilson, K. Hadyńska-Klęk)