

# SDHCAL evolution : Recent developments and algorithmic improvements for the APRIL Particle Flow

Tanguy Pasquier (speaker), Gérald Grenier, Imad Laktineh, Bo Li, Rémi Été

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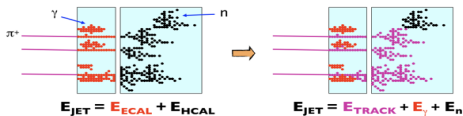
# Contents

- 1 Introduction : Particle flow algorithms, the APRIL Particle Flow and the SDHCAL
- 2 Recent developments : algorithmic improvements, timing inclusion...
- 3 Summary

# Particle flow calorimetry

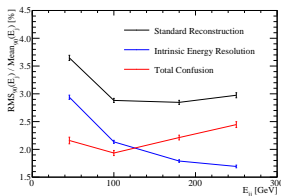
## Particle Flow Algorithm (PFA)

- PFA is the approach chosen for future colliders
- Use optimal sub-detector for jet energy estimation :  
tracker ( $\sim 60\%$ ), ECAL ( $\sim 30\%$ ), HCAL ( $\sim 10\%$ ).
- Separate energy depositions from close-by particles : **high granularity is key point**



Extensive studies have been done with ILD detector option 1 (AHCAL, ILD baseline) and PandoraPFA algorithm. At higher jet energy ( $E \gtrsim 100$  GeV), dominant contribution to resolution is confusion.

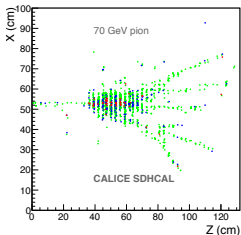
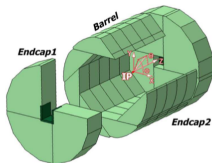
See [Steven Green, Cambridge University Thesis 2017](#)



# Semi-Digital HCAL

## SDHCAL energy reconstruction

$$E_{reco} = \alpha_1 N_1 + \alpha_2 N_2 + \alpha_3 N_3$$



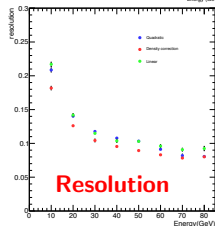
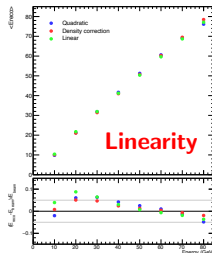
### Options for $E_{reco}$

Thresholds(pC): 0.11, 5, 15

**Quadratic**  $\alpha_i = a_i N_{hit}^2 + b_i N_{hit} + c_i$   
(TB default)

**Linear**  $\alpha_i$  constant (Pandora default).

**Density**  $\alpha_i = \text{above} \times f(N_{neighbour hits})$

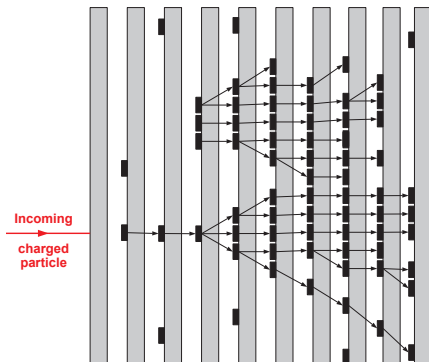


# The APRIL algorithm

- Based on the Arbor concept and implemented in PandoraSDK

APRIL : Algorithm for Particle Reconstruction at ILC from Lyon.

- Based on graph theory : Reconstruct the showers as spatial trees
- ⇒ APRIL usable as long as you have the positions of the hits



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# Angular corrections

- Recent work on ILD Option 2 (SDHCAL and Videau Geometry) to improve performances
- Linear reconstruction of single KLong samples  $\rightarrow$  HCAL calibration procedure
- $E_{reco}$  too low  $\rightarrow$  Angular corrections needed ( $\varphi, \theta$ )
- Low energy range still needed improvements after correction

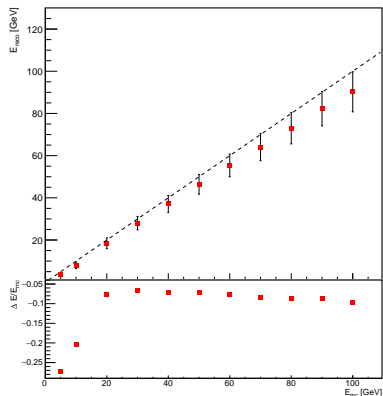


Figure: Before correction

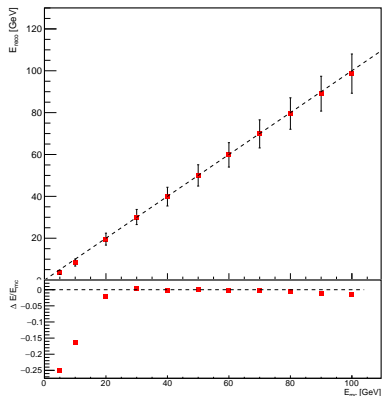
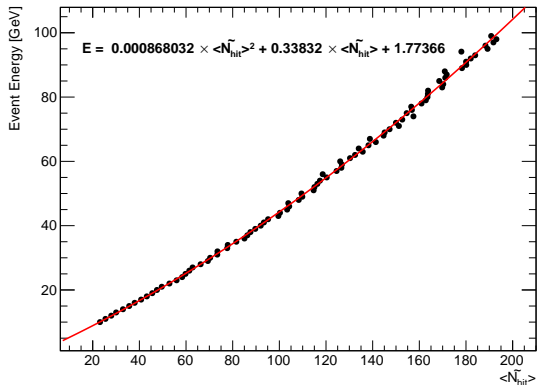


Figure: After correction

# New reconstruction method

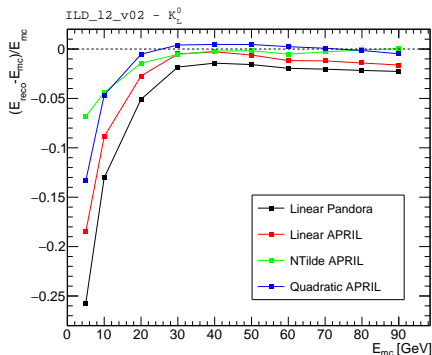
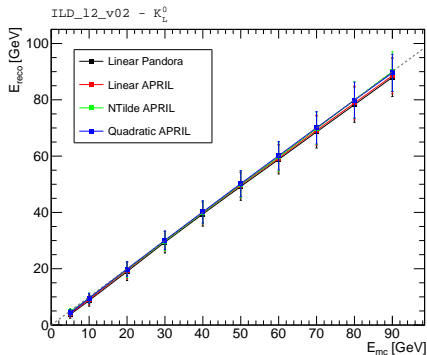
- Quadratic method : works well but implies a lot of parameters + difficult to constrain them
- We define :  $\tilde{N}_{hit} = N_3 + \beta \times (\alpha \times N_1 + N_2)$
- Look at correlations between  $N_1, N_2, N_3$  to extract parameters
- $E$  = quadratic function of  $\tilde{N}_{hit}$
- 5 parameters in total





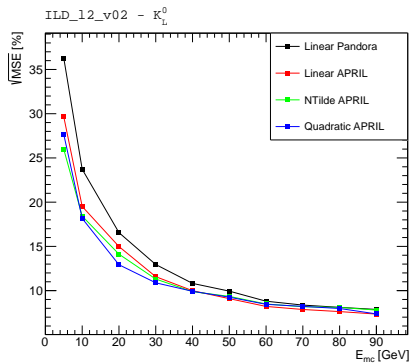
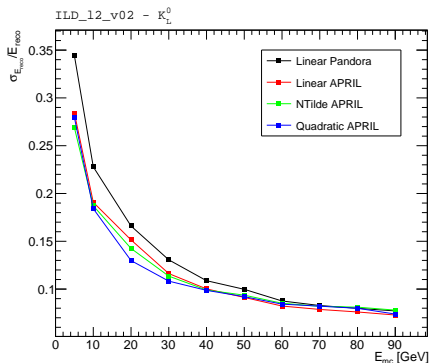
# Results

- Achieve good linearity with the different methods for  $E \geq 20$  GeV
- New method gives the best linearity on average



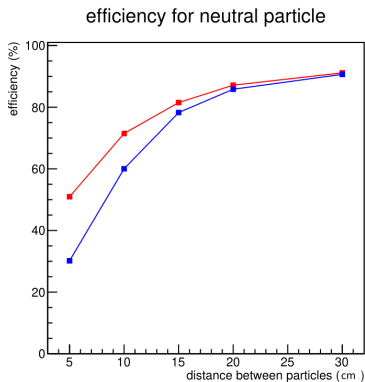
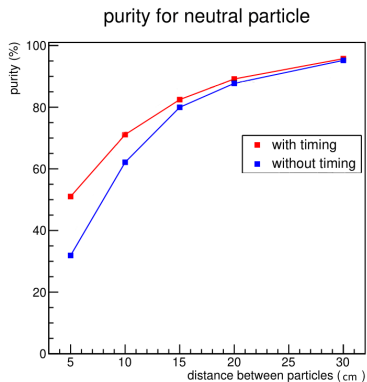
# Results

- $MSE = \left(\frac{\sigma_{E_{reco}}}{E_{reco}}\right)^2 + \left(\frac{E_{reco} - E_{mc}}{E_{mc}}\right)^2$
- Best resolution and MSE with NTilde method for  $E \leq 10$  GeV
- Quadratic still better from 10 GeV to 40 GeV
- All methods tend to converge for higher energies



# PFA with timing

- SDHCAL should allow timing segmentation  $< 100$  ps thanks to MRPC
- Possibility to follow the particles in "real time"
- Previous studies : timing improves separation
- **Goal** : Add timing to APRIL



# Different applications

- Delete non-causal connectors between hits ( $\beta > 1$ )
- Late neutrons tagging to treat them separately
- Identify the seeds of the showers and count them
- Hit ordering by time instead of radius
- Each of the above can be added with a PandoraSDK algorithm

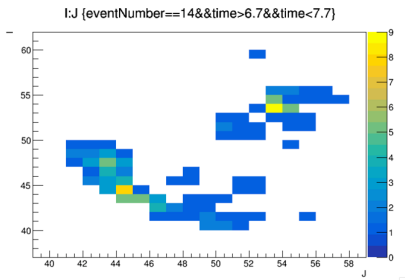


Figure: 1 ns interval

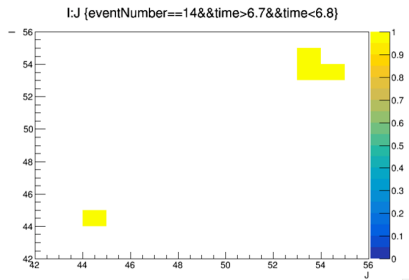


Figure: 100 ps interval

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# Summary and outlook

## Summary

- Angular corrections of the SDHCAL have been added
- A new way of computing the SDHCAL energy has been found and gives encouraging results on samples of single KLong
- Timing inclusion in APRIL has started

## Other activities

- Official inclusion of a "Marlin" processor able to run APRIL PFA and the SDHCAL plugins is underway
- Implementation of split cluster procedure (AMSTER) has started

## Outlook

- Reconstruct jet events to compare the different methods
- Fully include timing in APRIL

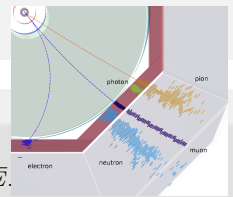
Thank you for your attention !

# Backup

- Areas of interest for future colliders:
  - Monolithic CMOS sensors (Tracking system)
  - Full simulation software development (Geometry, reconstruction)
  - Crystal ECAL detector

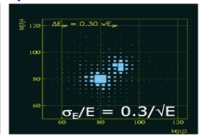
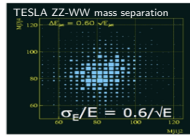
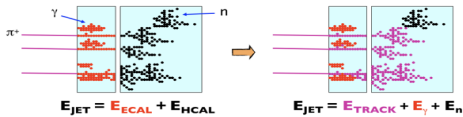


# Particle flow calorimetry

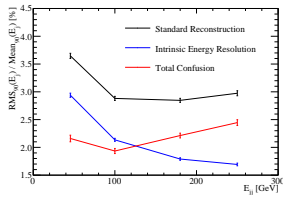


## Particle Flow Algorithm (PFA)

- ILC/CEPC physics program requires  $W/Z \rightarrow q\bar{q}$  mass separation.
- $\Rightarrow$  jets resolution [50, 500] GeV better than  $\sim 3 - 4\% \sim 30\%/\sqrt{E}$ .
- Use optimal sub-detector for jet energy estimation :  
 tracker ( $\sim 60\%$ ), ECAL ( $\sim 30\%$ ), HCAL ( $\sim 10\%$ ).
- Separate energy depositions from close-by particles : **high granularity is key point**



Extensive studies have been done with ILD detector option 1 and PandoraPFA algorithm.  
 At higher jet energy ( $E_{jet} \gtrsim 100$  GeV), dominant contribution to resolution is confusion.  
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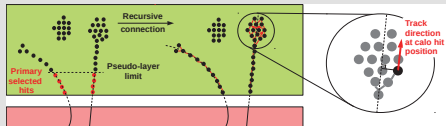


# The APRIL algorithm

APRIL : Algorithm for Particle Reconstruction at ILC from Lyon.

## The clustering strategy

- start from tracks (track driven clustering) extrapolate tracks in calorimeters  $\rightarrow$  cluster hits close to the tracks.



- Perform Arbor Clustering with all hits.
- $\rightarrow$  Clusters containing track cluster define charged clusters.
- Arbor parameters set to avoid making big clusters.
- $\rightarrow$  Some hits remain unclustered.
- Nearby hits merging : remaining unclustered hits are clustered with mlpack DBSCAN (efficient Nearest Neighbour clustering)
- If  $E_{track} > E_{cluster}$ , merge nearby cluster.

# Arbor clustering

Graph theory : a shower is an oriented tree.

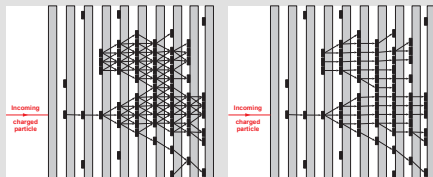
## Orientation

- Rearrange hits in virtual nested cylinders (= pseudo layers)
- Count them from the inside.
- Forward direction = increase pseudo layer number.

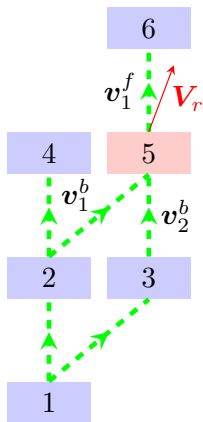


## Arbor

- 1 Connect all neighbouring hits (use mlpack NeighborSearch).
- 2 Clean connectors = keep max one backward connection per hit.



# Connector cleaning



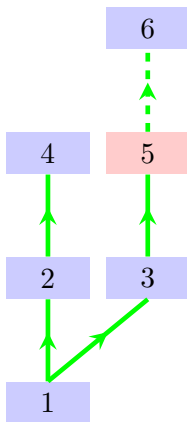
## Reference direction

$$\mathbf{V}_r = w_b \times \sum_i \mathbf{v}_i^b + w_f \times \sum_j \mathbf{v}_j^f$$

- Can use different depth (max distance in pseudolayer) and weight in forward-backward direction.
- Define angle  $\theta$  with respect to  $\mathbf{V}_r$  and distance  $d$  between hits (in  $\lambda_I$  or  $X_0$  unit).
- Keep connector with smallest

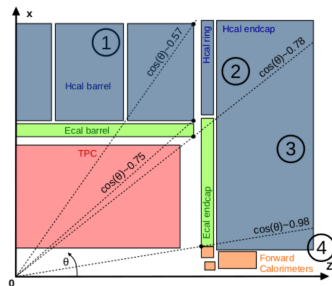
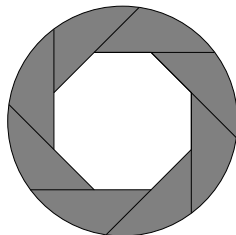
$$\kappa = \theta^{p\theta} \times d^{pd}$$

(if  $\theta = 0$ , smallest  $d$ )



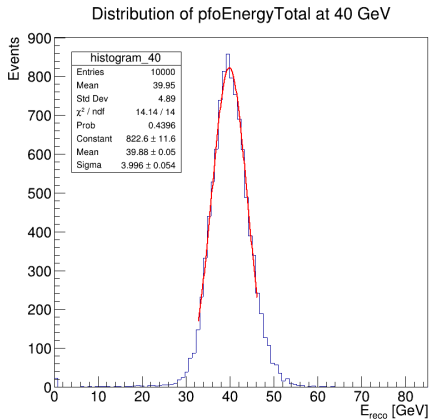
# Angle corrections

- **Goal** : implement angle corrections
- Purely geometric corrections
  - $N_{\text{hit}}^{\text{new}} = N_{\text{hit}} \times \text{Effect}$
  - Effect  $\frac{1}{\cos \theta}$  for endcap
  - Effect  $\frac{1}{\sin \theta}$  for barrel
  - Effect  $\frac{1}{\cos \varphi}$  for barrel only
  - Videau geometry taken in consideration
- Created SDHCALContent for all SDHCAL related plugins [▶ Git repo](#)
- Separating detector (SDHCAL, ILD option 2) from PFA (APRIL).



# Procedure

- Simulate and reconstruct samples of KLong going straight into the barrel ( $\theta = \varphi = \frac{\pi}{2}$ )
- For each energy, we look at the pfoEnergyTotal distribution
- Distributions fitted with Gaussian function in a RMS90 range (smallest interval with  $\geq 90\%$  of the events)
- Mean value and standard deviation of the Gaussian function treated as the reconstructed energy and its resolution



## $\alpha_i$ parameters computation

- Different methods tried
  - Classical method :  $\chi^2$  minimization
  - Solving system of equations with GSL
  - New reconstruction method
- For quadratic :  $\alpha_i = a_i N_{hit}^2 + b_i N_{hit} + c_i$  with  $N_{hit} = N_1 + N_2 + N_3$

### Classical method : $\chi^2$ minimization

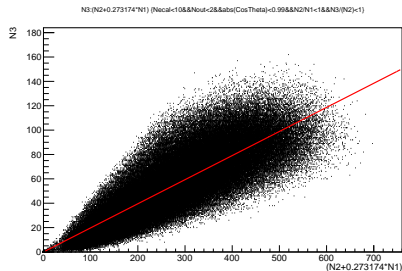
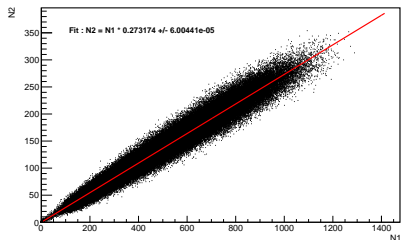
- $\chi^2 = \sum_{i=1}^N \frac{(E_{mc,i} - E_{reco,i})^2}{E_{mc,i}}$ ,  $N$  : Number of events used
- Minimization with TMinuit and MIGRAD (ROOT)

### Solving system of equations with GSL

- 9 equations with 9 unknowns and  $E_{reco}$  known
- Compute the  $N$  means for each of the 9 energies :  $\langle N_1 \rangle, \langle N_{hit} N_1 \rangle, \dots$
- Solving with GSL (GNU Scientific Library)
  
- Cons :
  - A lot of parameters to adjust (9 for the quadratic formula)
  - Difficult to constrain the parameters

# New reconstruction method

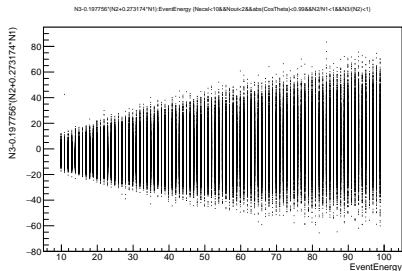
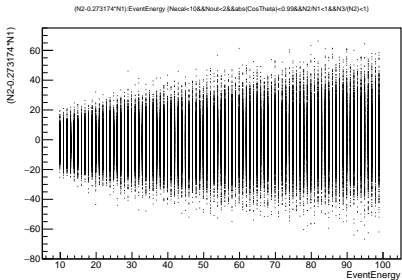
- Initial observation :  $N_2$  behaves approximately as a fraction of  $N_1$ , and  $N_3$  behaves approximately as a fraction of the combination of  $N_1$  and  $N_2$
- $N_2 = 0.273174 \times N_1$
- $N_3 = 0.197756 \times (0.273174 \times N_1 + N_2)$





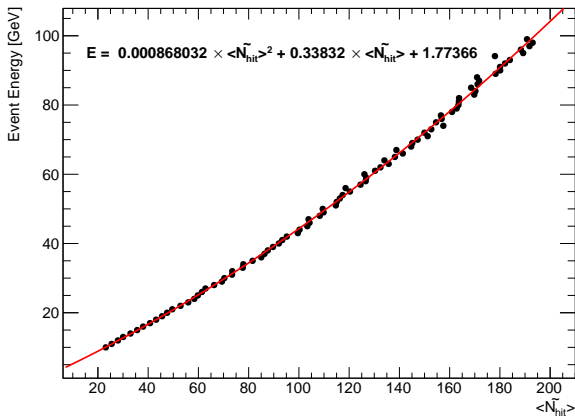
# Checking the coefficients

- Averages around zero when we look at the difference between the different terms as a function of energy
- Relations remain correct no matter what the energy is



# New formula

- We define :  $N_{hit}^{\sim} = N_3 + 0.197756 \times (0.273174 \times N_1 + N_2)$
- We plot  $E = f(\langle N_{hit}^{\sim} \rangle)$
- Best results for  $f(\langle N_{hit}^{\sim} \rangle)$  as quadratic



# Reclustering / Cluster cutting

- Reclustering : Break the cluster and restart clustering with different parameters (Pandora strategy)
- Cluster cutting : cut the cluster and remove some parts

## AMSTER algorithm

- Based on graph theory with Minimum Spanning Tree (MST)
- Cut the connections with bigger weights
- Implementation started and tested on simple cases

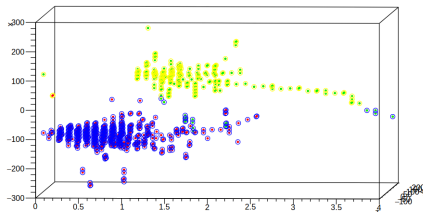


Figure: Event of a  $\pi^-$  (red) and a  $K^0$  (green) in two clusters (blue and yellow)