

# QCD & Lund Jet Plane studies at FCC-ee



FUTURE  
CIRCULAR  
COLLIDER



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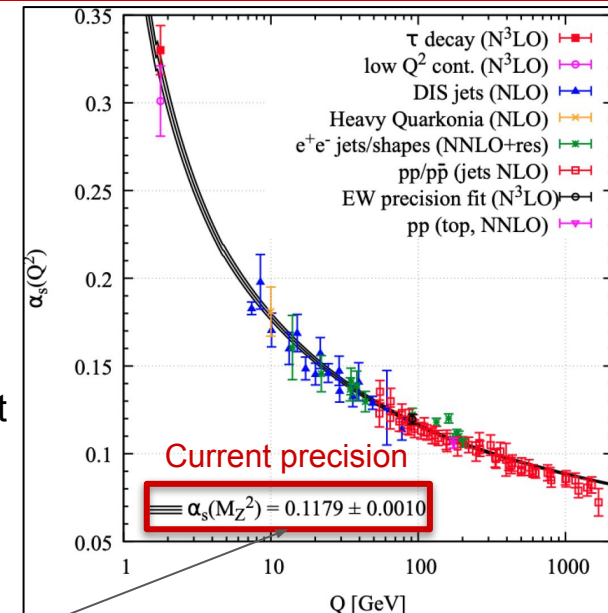
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ECFA Early Career Researchers' Workshop

# Introduction and motivation

- Analyse prospects of **QCD study@FCC-ee** using **3/2 Jet cross-section ( $R_{3/2}$ )** study and **Lund Jet Plane (LJP)** representation
- Aim to study the **sensitivity to  $\alpha_s$  at FCC-ee**, to probe  $\alpha_s$  for different energies and test the Renormalization Group Equation (RGE) in QCD
  - $\alpha_s$  impacts both jet multiplicity and jet shape (emissions inside jet)
- Also look for the potential use of LJP for improving jet tagging and impact for the optimization of detector parameters @FCC-ee
- **Why FCC-ee?**
  - Provides a clean collision environment with high statistics (10<sup>6</sup> X LEP Data)
  - Expect factor of 10 improvement with respect to the current  $\alpha_s$  precision
- Both analyses use FCCAnalysis framework along with centrally produced Delphes samples

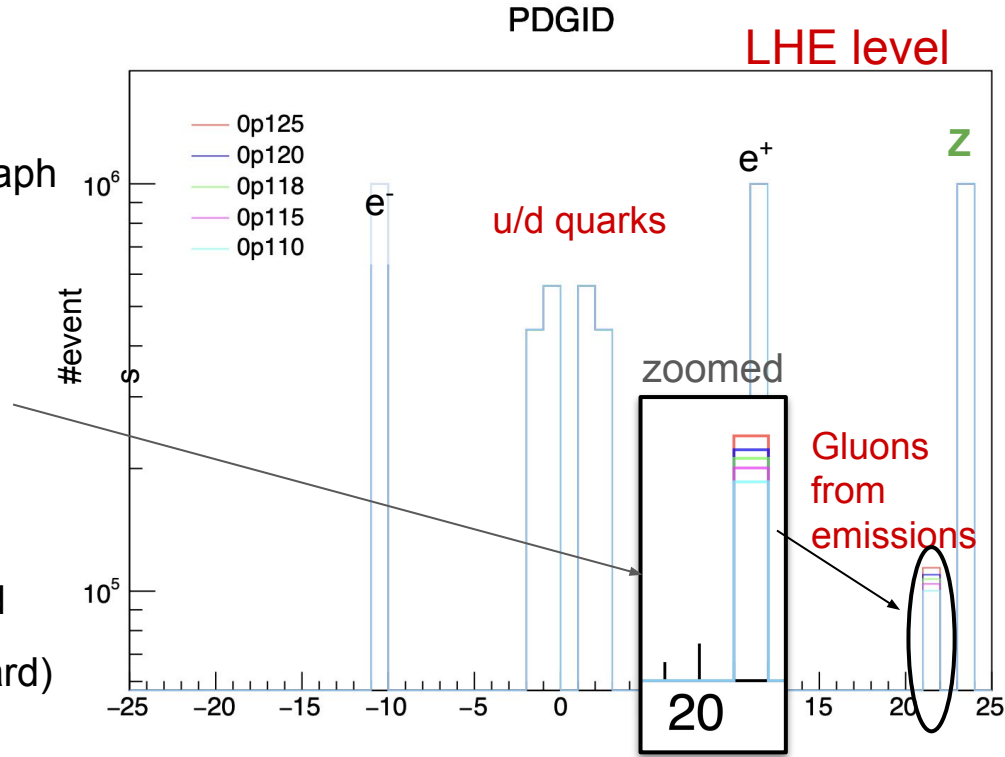


# Samples

Use centrally produced Winter2023 Delphes

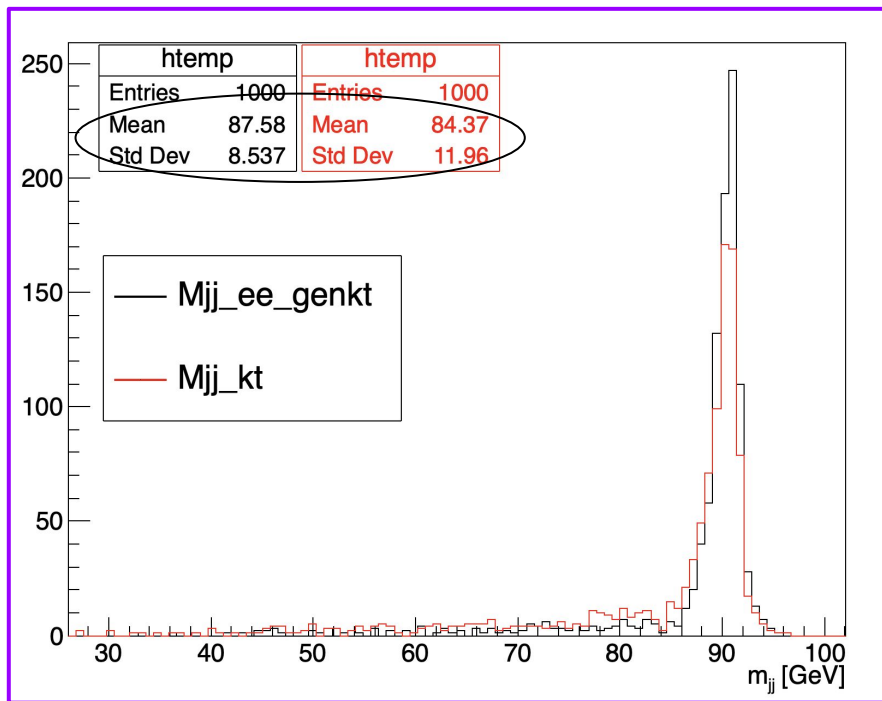
samples for IDEA

- LHE level events are generated with Madgraph (MG5\_aMC@NLO) for  $ee \rightarrow Z \rightarrow uu/dd$  at  $\sqrt{s} = 91 \text{ GeV}$
- Samples are generated with 5 different  $\alpha_s$  values: [0.110, 0.115, **0.118**, 0.120, 0.125]
- Emitted gluons multiplicity increases with  $\alpha_s$
- Events are further simulated with Pythia and Delphes generators (using IDEA detector card)
- #events = 1 M/sample



Other LHE validation plots are in backup

# Jet reconstruction with Delphes samples



- Jet reconstruction with ee generalised  $k_t$  algorithm with  $R = 1.5$  and  $p = -1$
- Better  $m_{jj}$  resolution with  $\theta$ -based  $k_t$  algorithms wrt  $\Delta R(y, \phi)$ -based  $k_t$  algorithms

## 4.5 Generalised $k_t$ algorithm for $e^+e^-$ collisions [arXiv:1111.6097](https://arxiv.org/abs/1111.6097)

FastJet also provides native implementations of clustering algorithms in spherical coordinates (specifically for  $e^+e^-$  collisions) along the lines of the original  $k_t$  algorithms [24], but extended following the generalised  $pp$  algorithm of [14] and section 4.4. We define the two following distances:

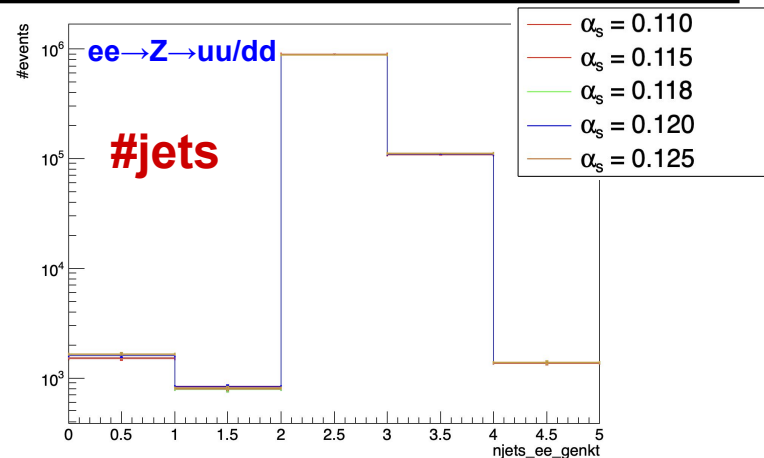
$$d_{ij} = \min(E_i^{2p}, E_j^{2p}) \frac{(1 - \cos \theta_{ij})}{(1 - \cos R)}, \quad (9a)$$

$$d_{iB} = E_i^{2p}, \quad (9b)$$

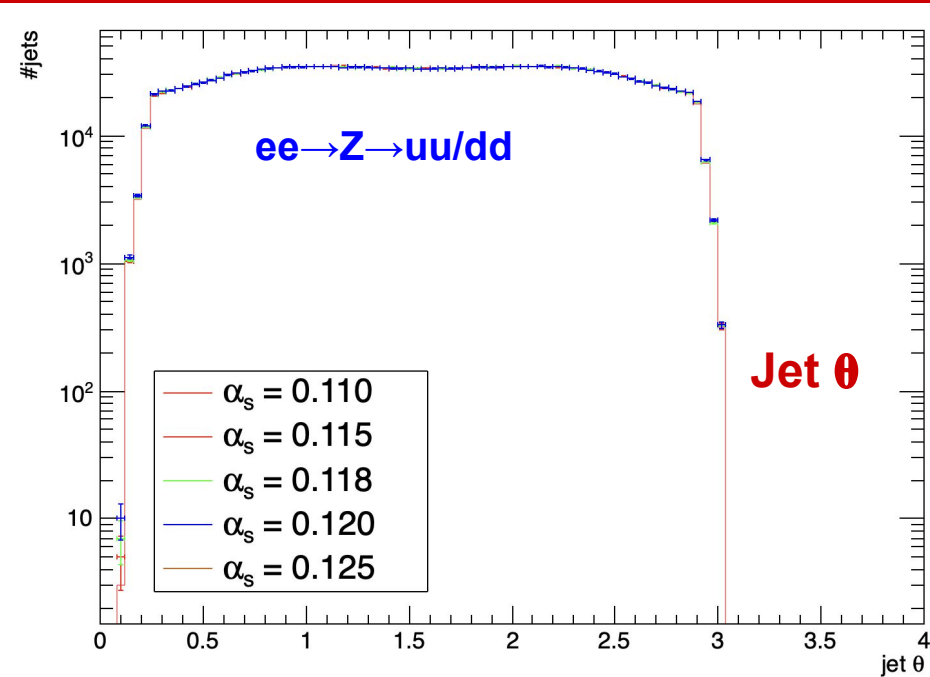
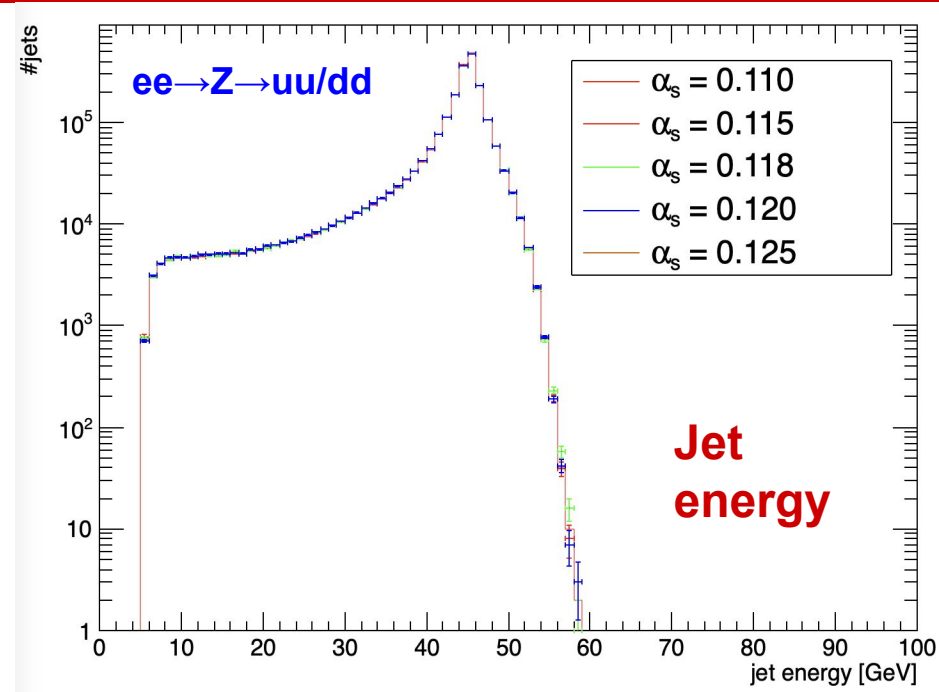
for a general value of  $p$  and  $R$ . At a given stage of the clustering sequence, if a  $d_{ij}$  is smallest then  $i$  and  $j$  are recombined, while if a  $d_{iB}$  is smallest then  $i$  is called an “inclusive jet”.

For values of  $R \leq \pi$  in eq. (9), the generalised  $e^+e^-$   $k_t$  algorithm behaves in analogy with the  $pp$  algorithms: when an object is at an angle  $\theta_{iX} > R$  from all other objects  $X$  then it forms an inclusive jet. With the choice  $p = -1$  this provides a simple, infrared and collinear safe way of obtaining a cone-like algorithm for  $e^+e^-$  collisions, since hard well-separated jets have a circular profile on the 3D sphere, with opening half-angle  $R$ . To use this form of the algorithm, define

```
JetDefinition jet_def(ee_genkt_algorithm, R, p);
```



# Jet Kinematics



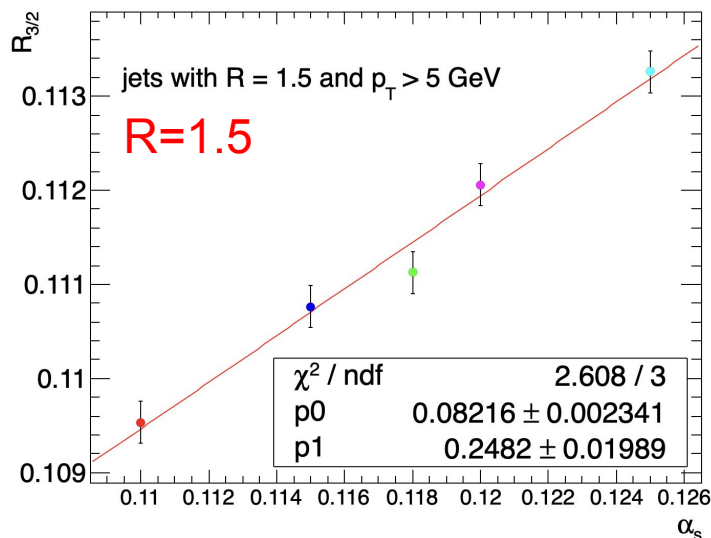
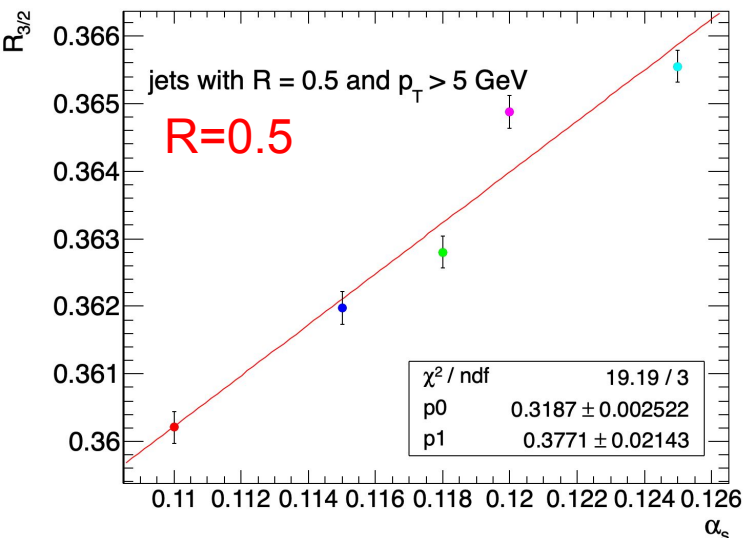
- Jet kinematics look as expected for Z  $\rightarrow$  uu/dd process

# Study I: $R_{3/2}$ studies

- Study jet cross section ratio between events with at least 3 jets vs 2 jets ( $\alpha_s$  impacts jet multiplicity)
- Observe  $R_{3/2}$  dependency on  $\alpha_s$

$$R_{3/2} = \frac{\text{The number of events with at least 3 jets}}{\text{The number of events with at least 2 jets}}$$

Jets	Variation in $R_{3/2}$
R=0.5	$0.38 \pm 0.02 \Delta\alpha_s$
R=1.5	$0.25 \pm 0.02 \Delta\alpha_s$

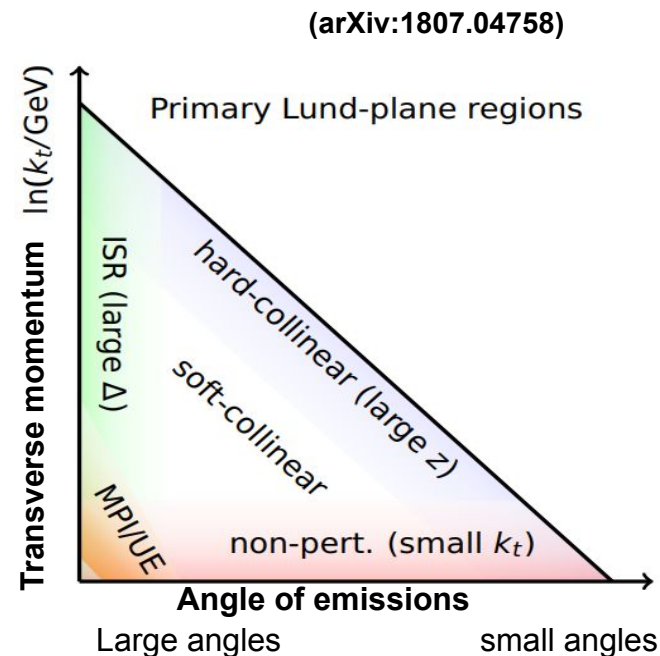


**Next:** Study ongoing with jets at hadron level

# Study II : Lund Jet Plane studies

## Benefits of Lund Jet Plane method (LJP):

- QCD jet formation involves perturbative and non-perturbative effects; presence of these effects impacts the precision of any measurement based on jets
- LJP works as a handle to separate these effects in a 2D representation using angle ( $\Delta R$ ) and transverse momentum ( $k_t$ ) of emissions within the jets and further opens a possibility to understand QCD behaviour separately for these perturbative and non-perturbative effects



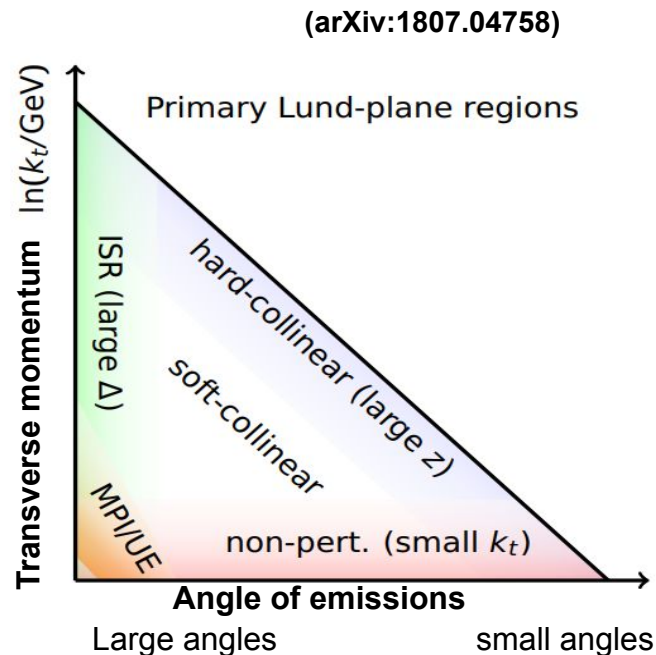
# How to extract $\alpha_s$ ?

- QCD process behind jet formation is related to strong coupling constant  $\alpha_s$ 
  - Running constant which varies with different energies
  - Impacts jet shape (emissions within jets)

Average density of emissions in LJP can be given as:

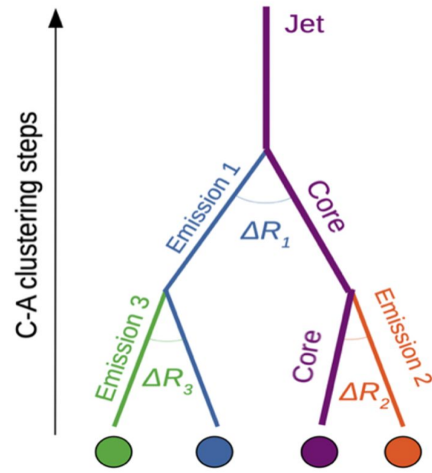
$$\rho(k_T, \Delta R) \equiv \frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T / \text{GeV}) d \ln(R / \Delta R)} \approx \frac{2}{\pi} C_R \alpha_s(k_T)$$

Where  $C_R$  = color factor





# How to build Lund Jet Plane?



- Start with a jet and cluster it again to have angular order information of emissions ([JHEP 12 \(2018\) 064](#))
- Decluster them in reverse (start with wide angle emission first)
- Within the iterative declustering, harder branch is always taken as core branch
- Fill a triangle plane of two Lund variables ( $k_t$  and  $\Delta R$ ) from core and emission

## NOTE:

- Angular ordered Cambridge/Aachen (C/A) declustering (following the theoretical proposal) depends on  $\Delta R$  in  $(\mathbf{y}, \phi)$  plane used for LHC studies (given in [backup](#))
- It is more accurate to perform  $\Delta R$ -based declustering in the  $(\theta, \phi)$  plane for FCC-ee. Therefore, we use EECambridgePlugin algorithm

For “a” core and “b” emission branch

$$k_t \equiv p_{tb} \Delta R_{ab}$$

$$z \equiv p_{tb} / (p_{ta} + p_{tb})$$

$\Delta R_{ab}$  = angle of emission **b** wrt to core **a**

$k_t$  = transverse momentum of **b** wrt **a**

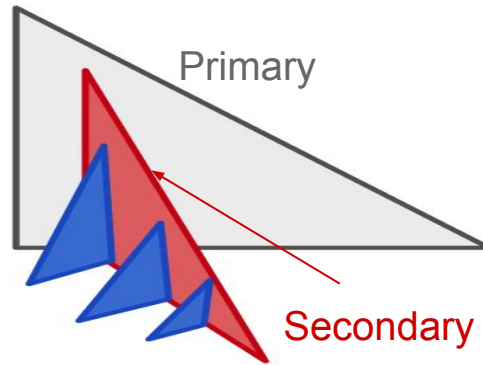
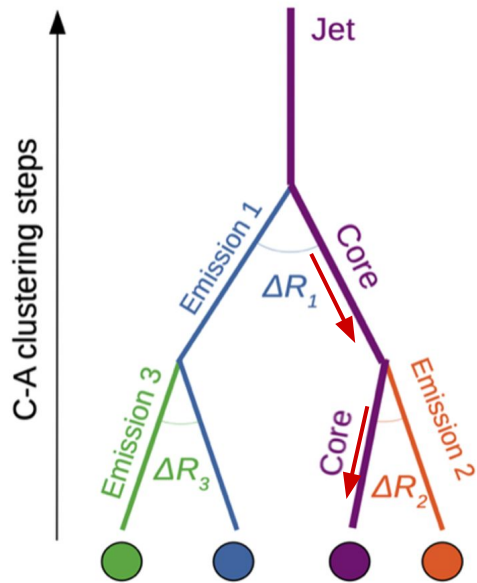
$z$  = momentum fraction taken by **b**

Analysis studies for primary and secondary LJP

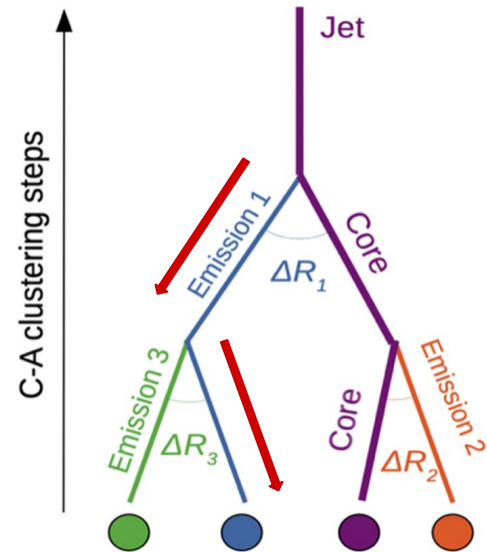
- Motivated from following the theoretical proposal [\[link\]](#) which show secondary LJP is mostly gluon induced

# How to build Primary and Secondary Lund Jet Plane?

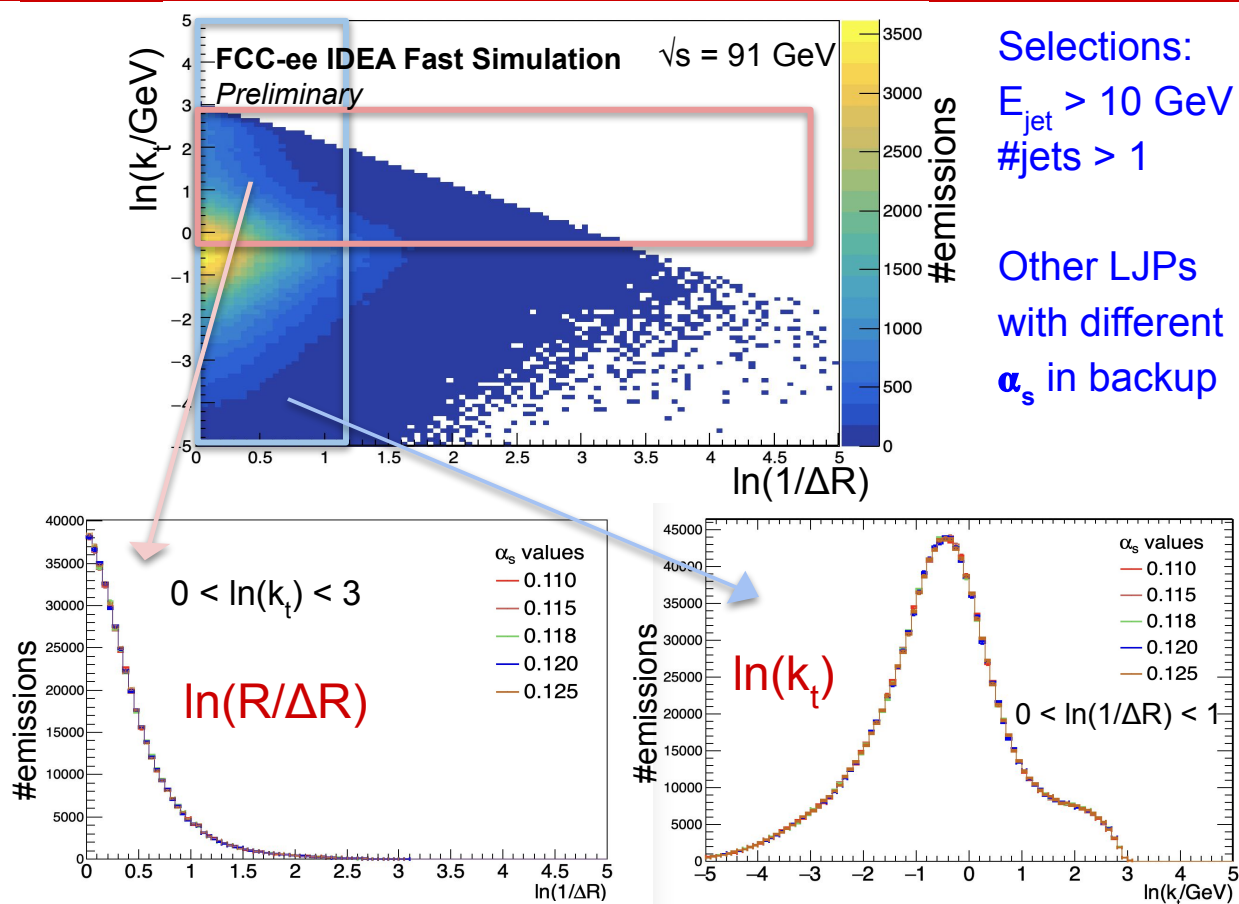
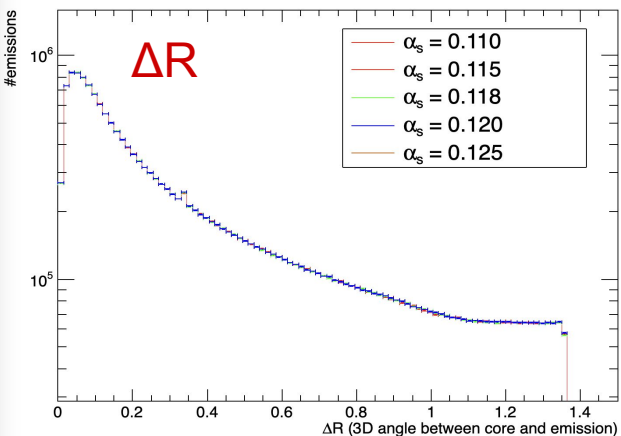
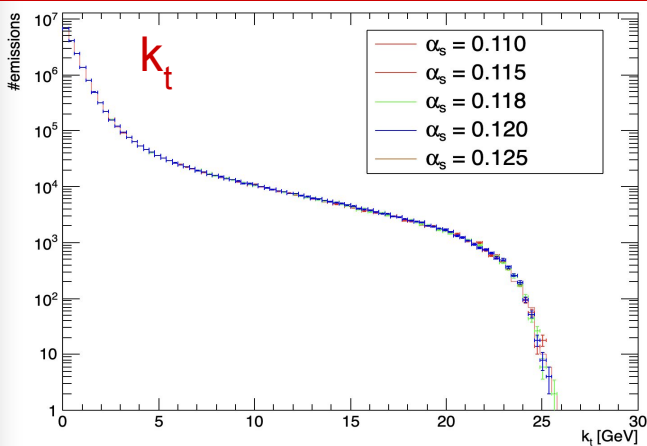
## Primary LJP



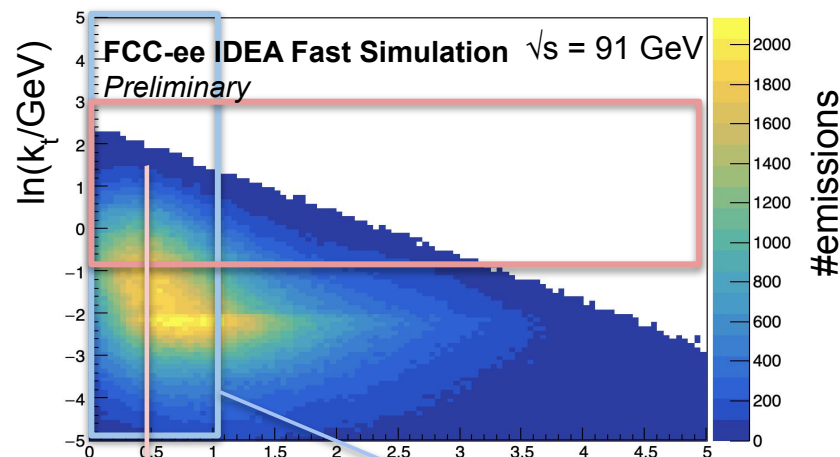
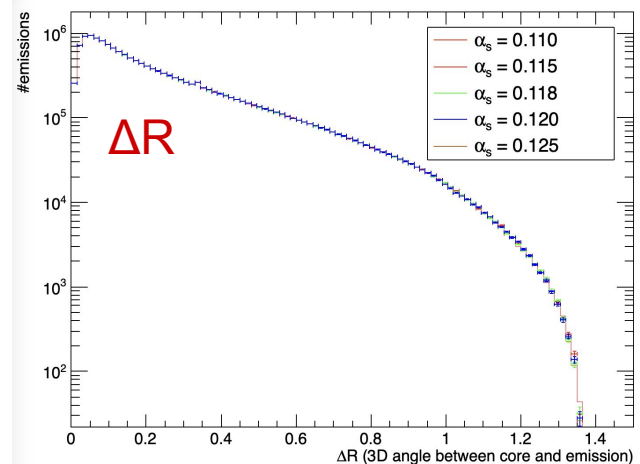
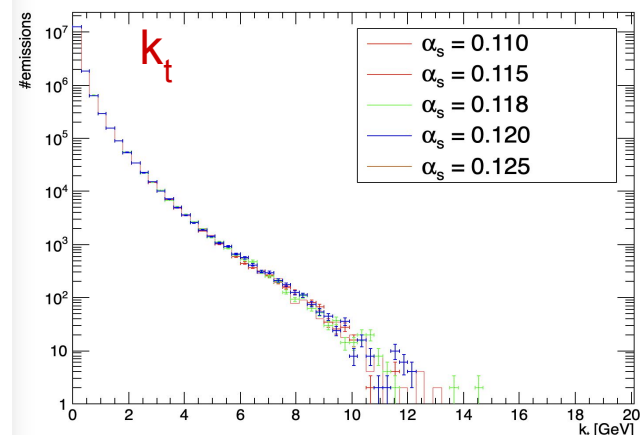
## Secondary LJP



# Preliminary look at LJPs: Primary LJP

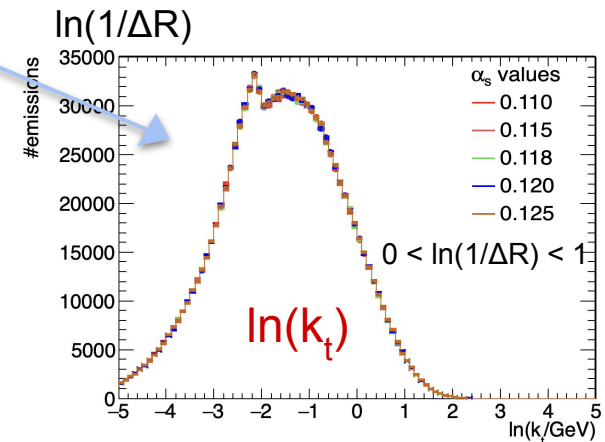
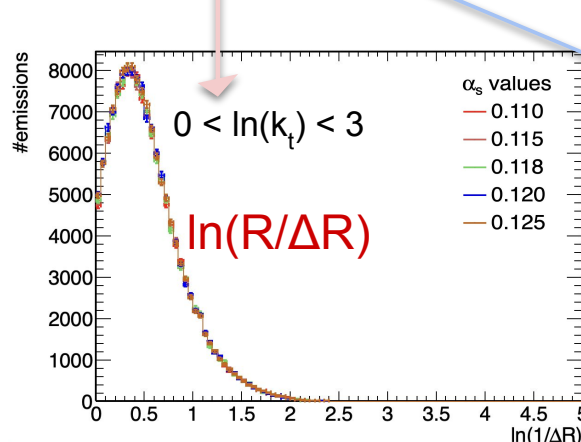


# Preliminary look at LJPs: Secondary LJP



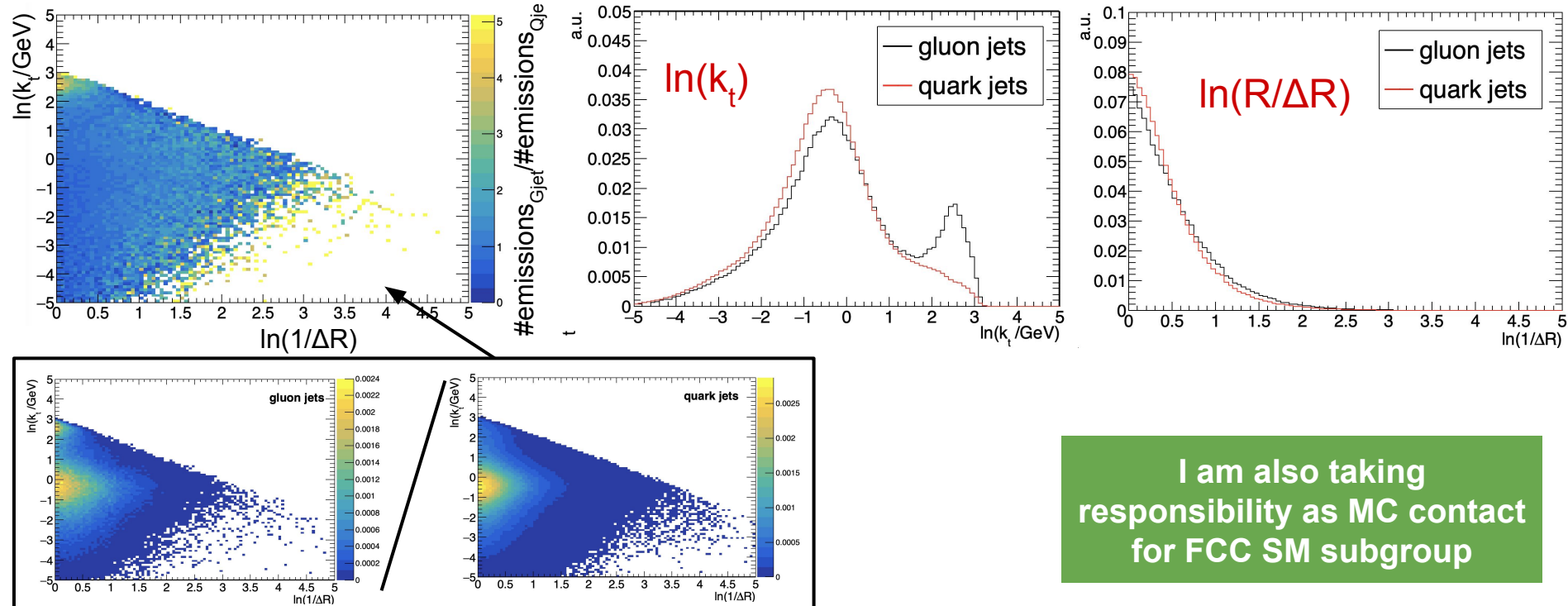
Selections:  
 $E_{jet} > 10$  GeV  
 $\#jets > 1$

Other LJPs  
 with different  
 $\alpha_s$  in backup



# Other efforts and interests

- Our team is also working to study the potential of LJP for jet tagging methods
  - For now study is ongoing for quark and gluon jets; will be extended to heavy ( $Z \rightarrow b\bar{b}$ ) vs light flavor ( $H \rightarrow g\bar{g}l\bar{l}$ ) jets



I am also taking responsibility as MC contact for FCC SM subgroup

# Summary and next steps

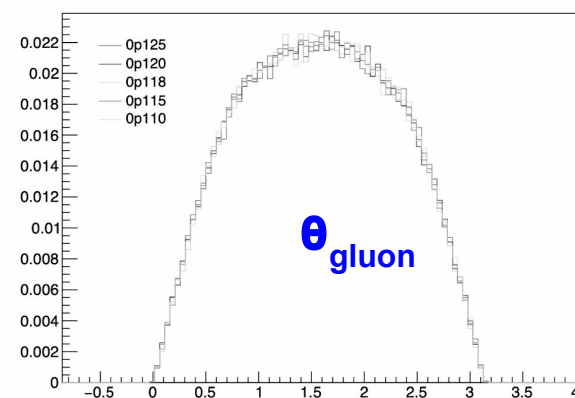
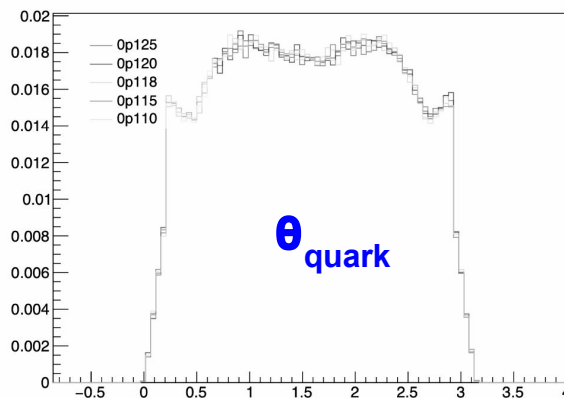
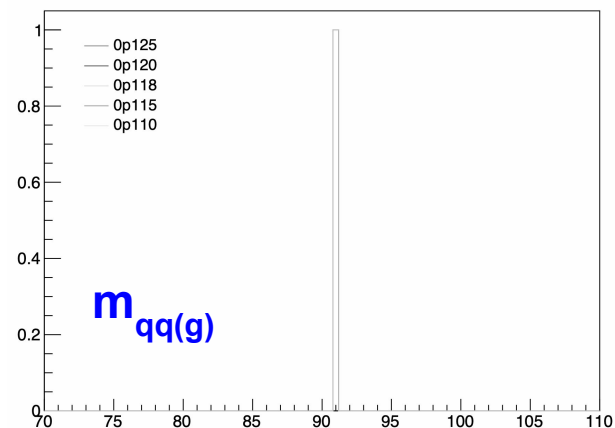
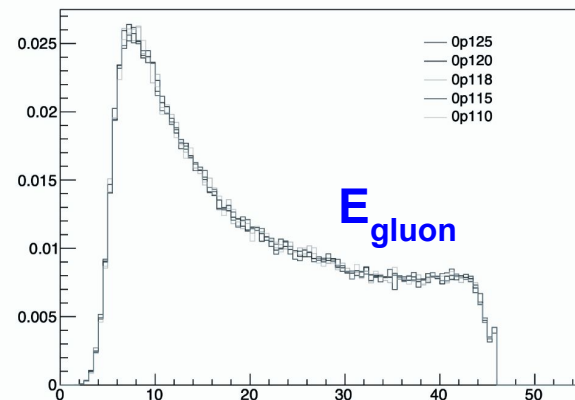
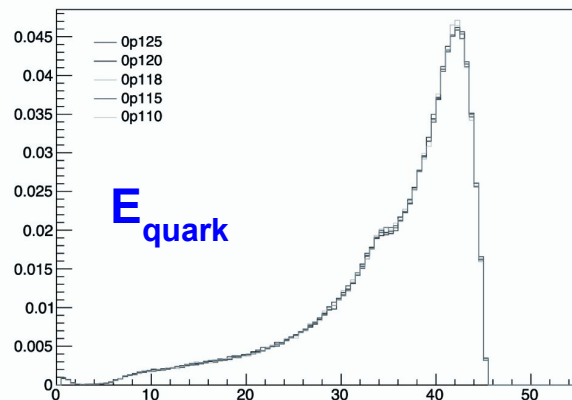
- Present updates of  $R_{3/2}$  jet cross section study and Lund Jet Plane studies at FCC-ee
  - Motivated by the study of the sensitivity to  $\alpha_s$  and test of RGE
- **$R_{3/2}$  study:**
  - Observe dependency of  $R_{3/2}$  on variation of  $\alpha_s$
  - Study ongoing with jets at hadron level
- **LJP Study:**
  - To our knowledge it is first study which looks at jet substructure at FCC-ee
  - Switch to ee-dedicated algorithm for jet clustering/declustering
  - Plan to explore the sensitivity of the reconstructed LJP to:
    - $\alpha_s$  by doing  $\alpha_s$ -scan; (explore both Primary and Secondary LJP)
    - Optimization of the detector parameters
    - Also potential use for jet tagging methods at FCC-ee

*Thank you*

**BACKUP**

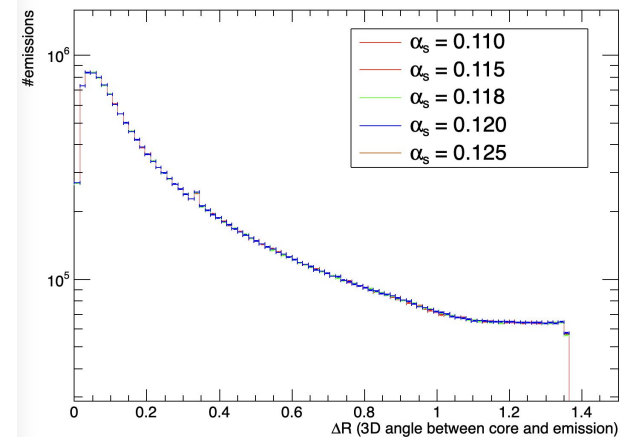
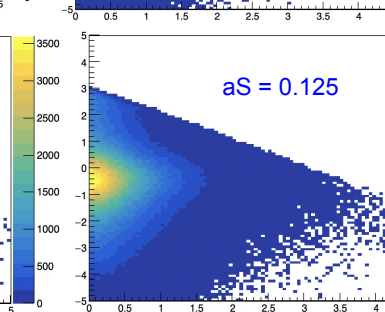
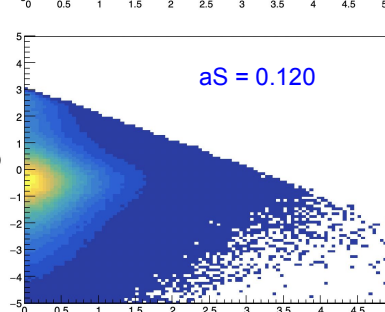
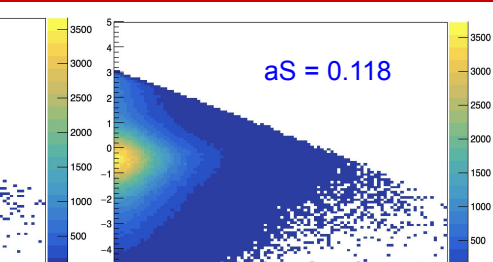
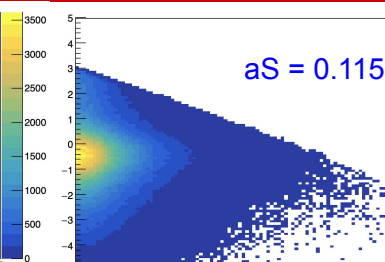
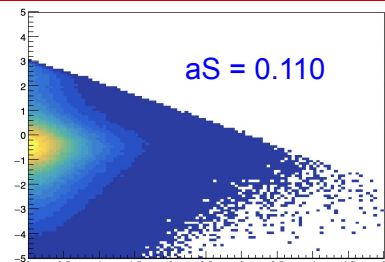
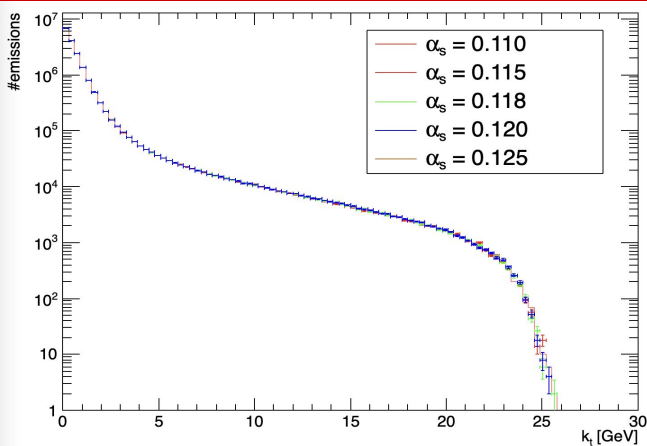
# Validation studies:LHE level

- Distributions are shown for different  $\alpha_s$  values and are shape normalized
- No selection at generator level

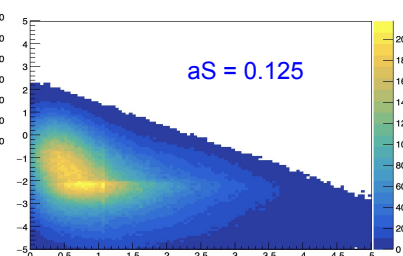
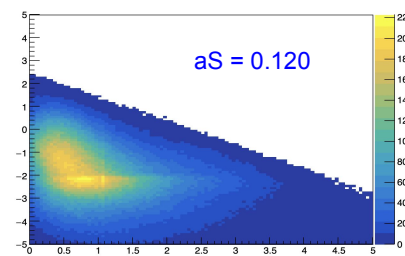
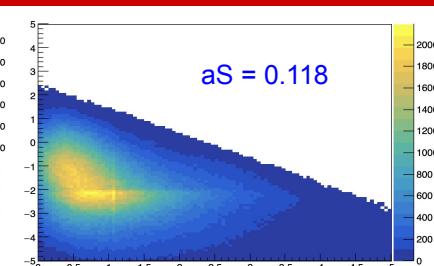
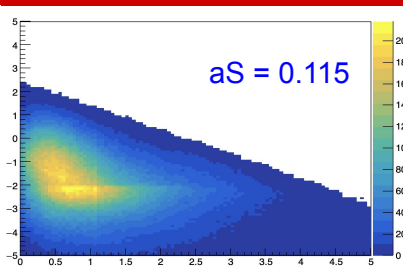
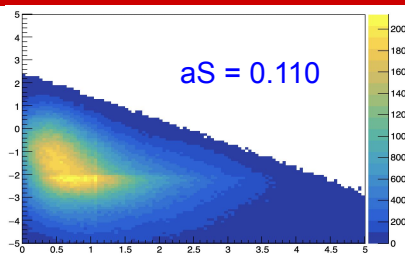
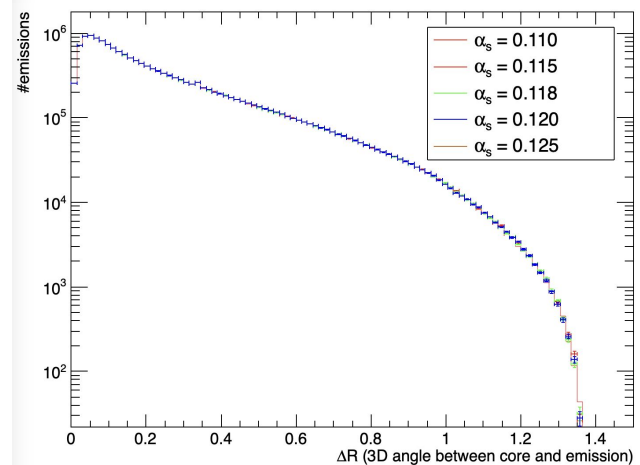
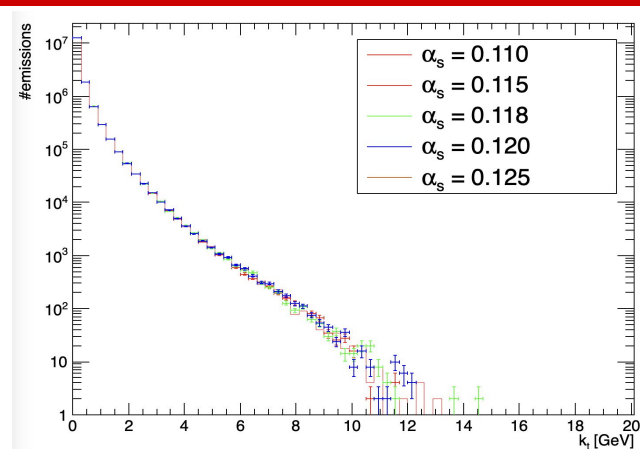




# Preliminary look at LJPs: Primary LJP



# Preliminary look at LJPs: Secondary LJP



# Angular order-based jet declustering in $(\theta, \phi)$ plane

- Use ee-dedicated Cambridge algorithm (**EECambridgePlugin**); Implemented in code with help from fastjet experts ([link](#))
- Setup is in place

## 5.4 Plugins for $e^+e^-$ collisions

[arXiv:1111.6097](#)

### 5.4.1 Cambridge algorithm

The original  $e^+e^-$  Cambridge [22] algorithm is provided as a plugin:

```
#include "fastjet/EECambridgePlugin.hh"  
// ...  
EECambridgePlugin (double ycut);
```

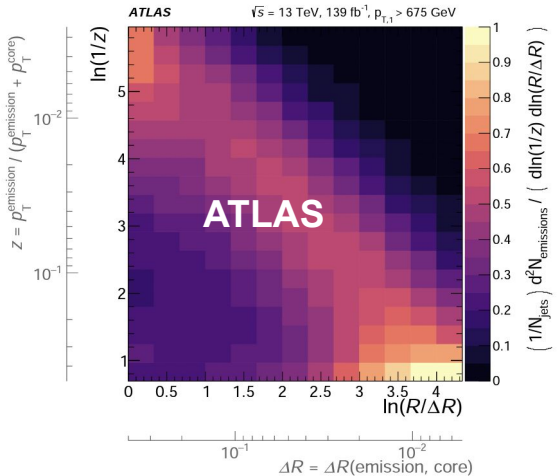
This algorithm performs sequential recombination of the pair of particles that is closest in angle, except when  $y_{ij} = \frac{2 \min(E_i^2, E_j^2)}{Q^2} (1 - \cos \theta) > y_{cut}$ , in which case the less energetic of  $i$  and  $j$  is labelled a jet, and the other member of the pair remains free to cluster.

To access the jets, the user should use the `inclusive_jets()`, *i.e.* as they would for the majority of the  $pp$  algorithms.

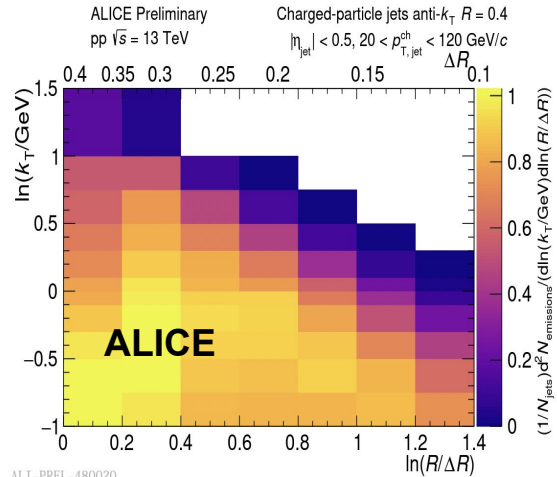
# Recent Lund Jet Plane based measurements

- LJP studies at LHC  $\sqrt{s} = 13$  TeV, following recent theoretical proposal ([JHEP 12 \(2018\) 064](#))
- These studies measure the lund plane density for charged particles jets
- We are interested in following the same for FCC-ee environment

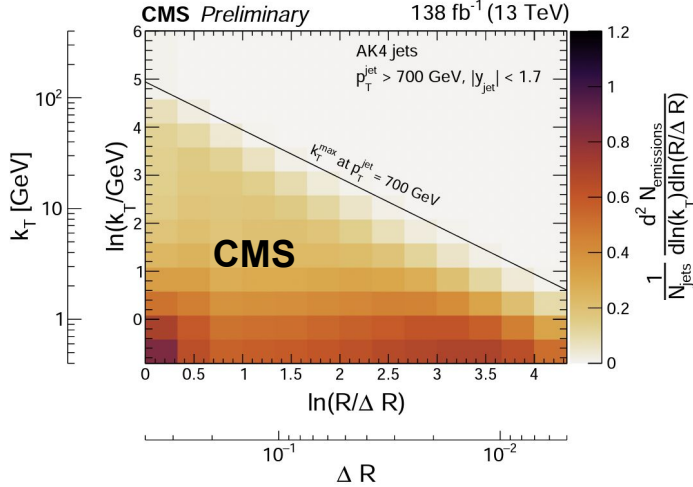
[arXiv 2004.03540](#)



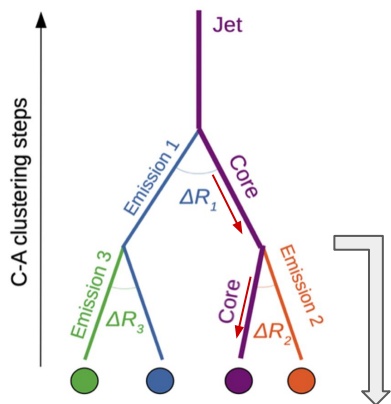
[arXiv 2111.00020](#)



[CMS-PAS-SMP-22-007](#)



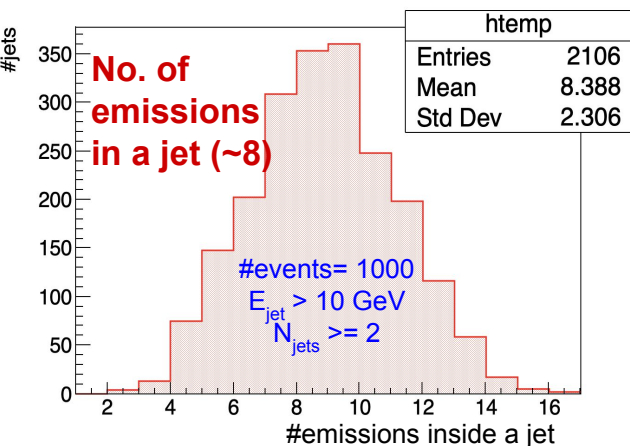
# How to build Primary Lund Jet Plane?



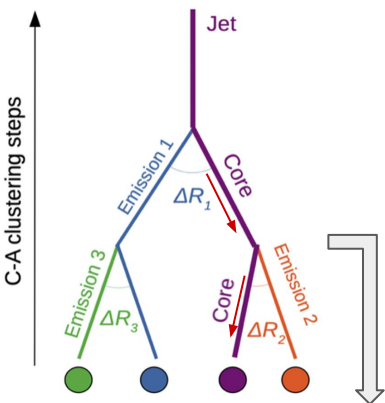
For  $R=1.5$  jets  
clustered with  $k_t$   
algorithm (Kt15)

$ee \rightarrow Z \rightarrow uu/dd$  @91 GeV

## Emissions from the core branches



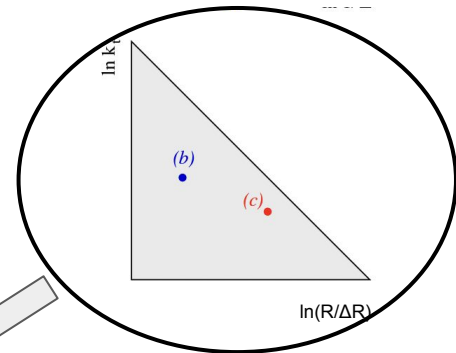
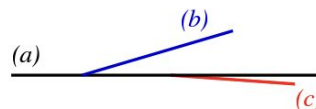
# How to build Primary Lund Jet Plane?



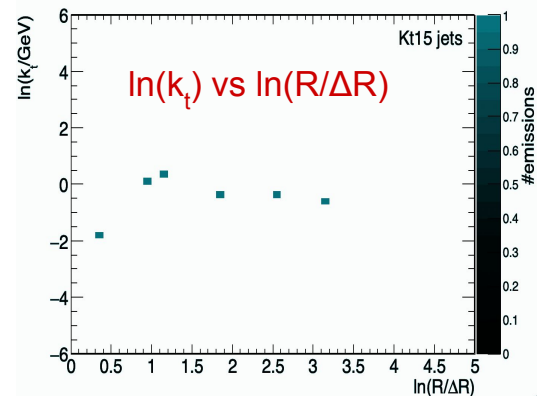
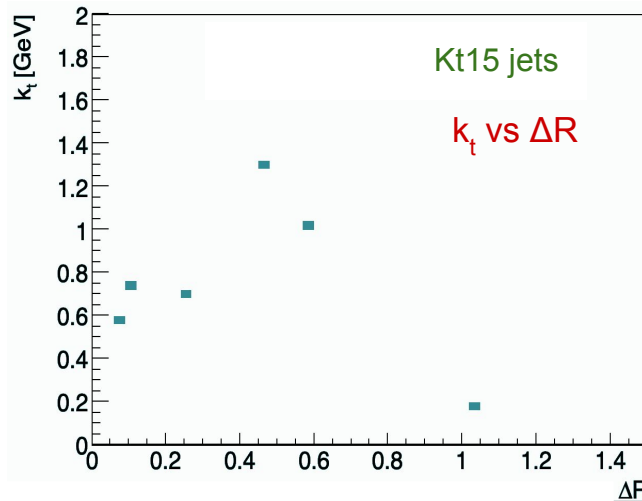
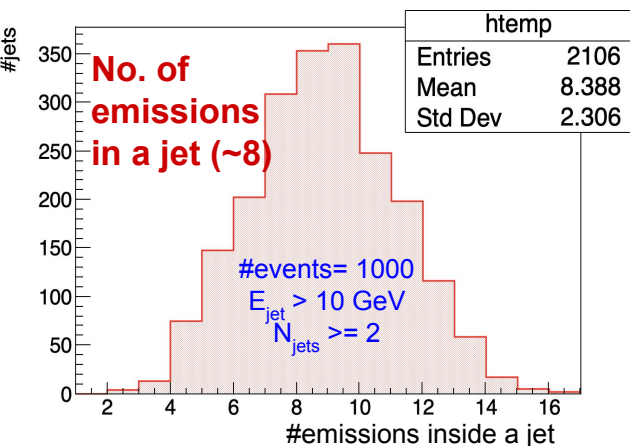
For  $R=1.5$  jets clustered with  $k_t$  algorithm (Kt15)

$ee \rightarrow Z \rightarrow uu/dd$  @91 GeV

JET



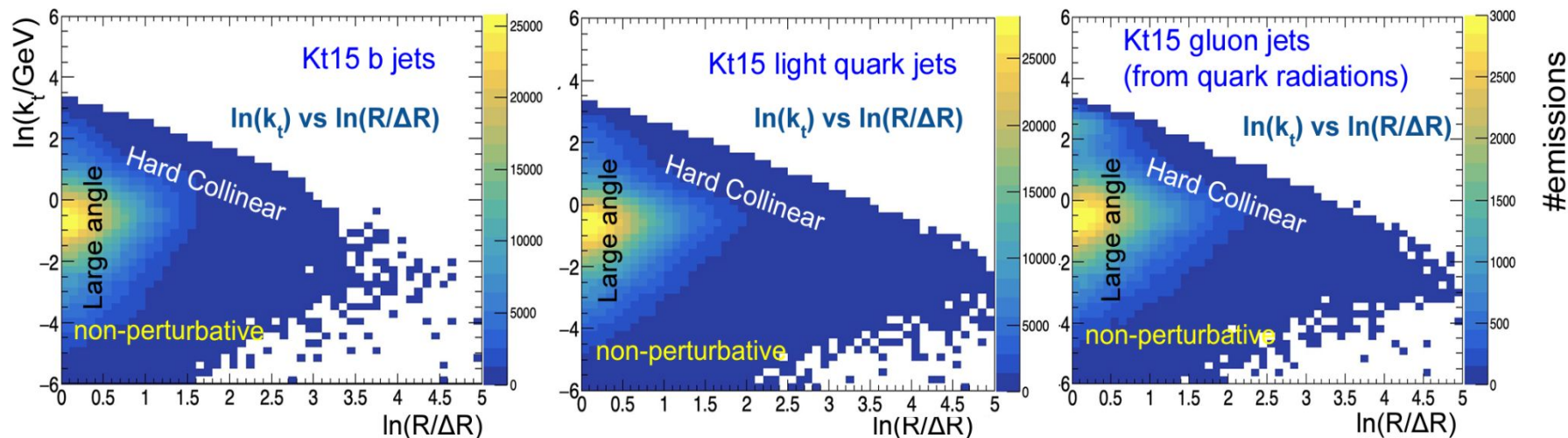
Emissions from the core branches



LJP representation for 1 jet of  $E_{jet} \sim 40$  GeV

(both plots represent the same jet w/ and w/o log scale)

# LJP representation for light and heavy flavor jets at higher energy



- For process  $ee \rightarrow Z \rightarrow bb$  and  $ee \rightarrow Z \rightarrow uu/dd$  (+ gluons from quark radiation) @91 GeV ;  
#events = 1 M
- Selection:  $E_{\text{jet}} > 10$  GeV,  $N_{\text{jets}} \geq 2$ ; selection efficiency > 99%; use two leading  $p_T$  jets
- Difference in the large  $\ln(R/\Delta R)$  region shows that light jets are more collimated than heavy flavour jets; working on further understanding in more detail