

V_{ud} : Recent theoretical progress and experimental opportunities

Leendert Hayen

V_{ud} workshop GANIL

5 November 2024



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Introduction

Theory progress in the last 5 years

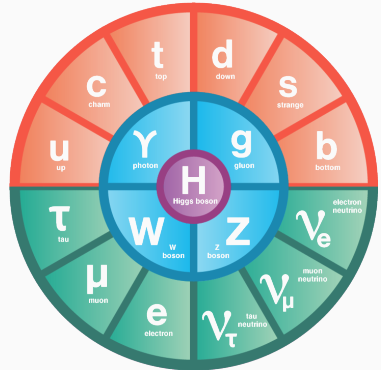
Experimental opportunities

Summary & Outlook

Meet the Standard Model

Three out of four
fundamental forces (no gravity):

Standard Model

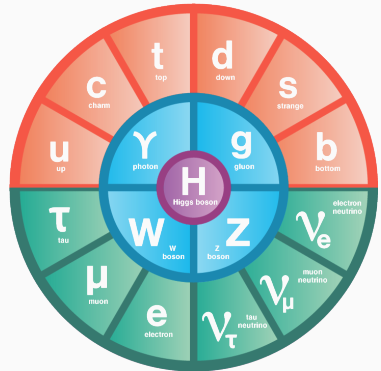


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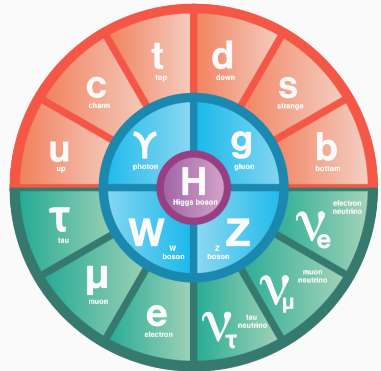
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Great (annoyingly so), consistent
with constraints at $\sim 10^{0-2}$ TeV



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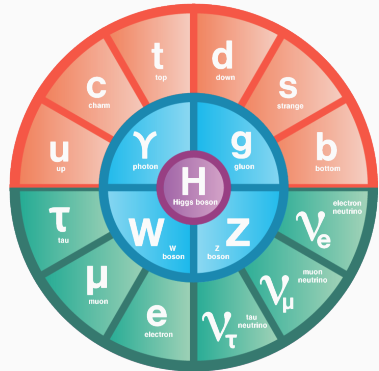
Three out of four
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Open questions: dark matter,
gravity, neutrino masses, ...



Introduction: Standard Model

What to do?

SM tests @ low energy: sensitive to **off-shell** exotic physics
(footprints rather than actual beast)

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Besides precision QED ($a_{e,\mu}, r_p, \dots$), weak interactions probe

- (C)P violation
- CKM unitarity
- Lorentz structure

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SM tests @ low energy: sensitive to **off-shell** exotic physics
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Besides precision QED ($a_{e,\mu}, r_p, \dots$), weak interactions probe

- (C)P violation
- CKM unitarity
- Lorentz structure

Today: **CKM unitarity**

Introduction: Weak interaction & CKM matrix

Cabibbo-Kobayashi-Maskawa matrix relates weak and mass eigenstates

$$\begin{pmatrix} d \\ s \\ b \end{pmatrix}_w = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_m$$

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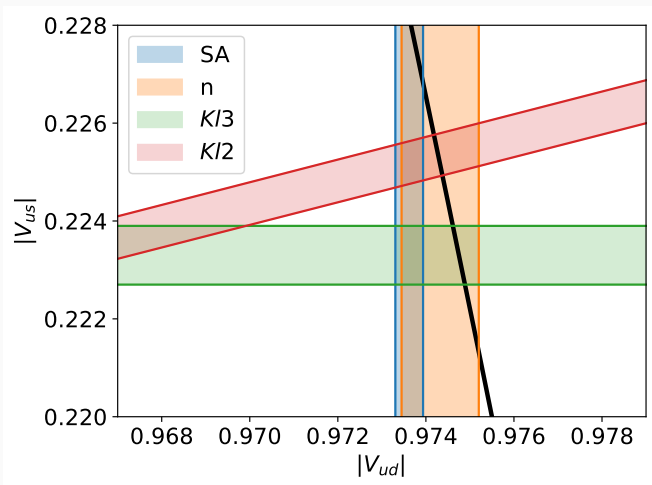
(nuclear) β decay, meson decay (π , K), $|V_{ub}|^2 \sim 10^{-5}$

Violations are sensitive to **TeV scale** new physics!

CKM unitarity: Current status

Signs of non-unitarity at few σ level...

Disagreement between $K/2$ and $K/3$ $|V_{us}|$ 'Cabibbo angle anomaly'



What would new physics look like?

SM has V - A structure, but more generally

$$\mathcal{L}_{\text{eff}} = -\frac{G_F \tilde{V}_{ud}}{\sqrt{2}} \left\{ \bar{e} \gamma_\mu \nu_L \cdot \bar{u} \gamma^\mu [c_V - (c_A - 2\epsilon_R) \gamma^5] d + \epsilon_S \bar{e} \nu_L \cdot \bar{u} d \right. \\ \left. - \epsilon_P \bar{e} \nu_L \cdot \bar{u} \gamma^5 d + \epsilon_T \bar{e} \sigma_{\mu\nu} \nu_L \cdot \bar{u} \sigma^{\mu\nu} (1 - \gamma^5) d \right\} + \text{h.c.},$$

at the quark level

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at the quark level

All ϵ_i are proportional to $(M_W/\Lambda_{BSM})^2$, change kinematics

$\epsilon_i \lesssim 10^{-4} \rightarrow \Lambda_{BSM} \gtrsim 15 \text{ TeV}$ assuming natural couplings

CKM unitarity: V_{ud}

Let's break it down: How to obtain V_{ud} ?

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Semi-leptonic up-down decay rate

$$\Gamma \propto G_F^2 |V_{ud}|^2 (1 + RC) |\langle O_{\text{hadr}} \rangle|^2 \times \text{phase space}$$

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Things you need to know

- G_F (μ lifetime)
- Radiative corrections
- Hadronic theory
- For each β transition: $t_{1/2}$, Q_β , BR , (GT/F mixing)

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Things you need to know

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Master formula

$$ft(1 + \delta'_R)(1 + \Delta_R^V)(1 + \delta_{NS} - \delta_C) = \frac{K}{G_F^2 V_{ud}^2 M_{\text{tree}}^2}$$

CKM unitarity: V_{ud} precision

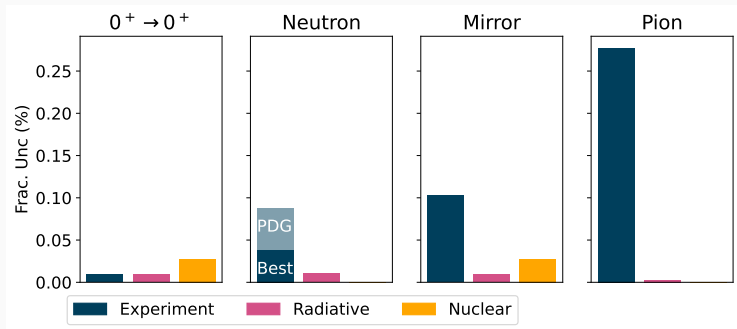
Nuclear sandbox \rightarrow make **hadronic theory** easy

- Pion
- Neutron
- Superallowed $0^+ \rightarrow 0^+$
- $T = 1/2$ mirrors

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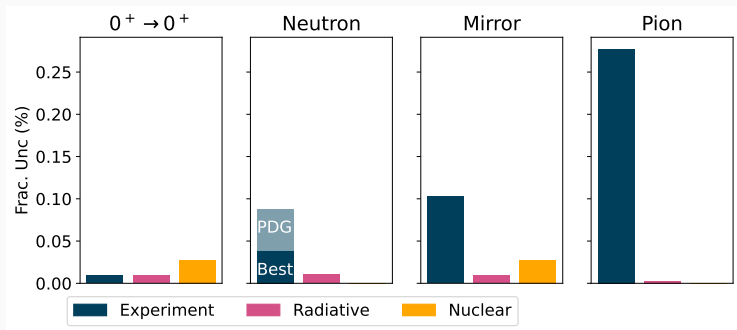


$\pi^+ \rightarrow \pi^0 e^+ \nu_e$ very hard (BR $\sim 10^{-8}$), SA new nuclear corrections!

CKM unitarity: V_{ud} precision

Nuclear sandbox \rightarrow make **hadronic theory** easy

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Status of $0^+ \rightarrow 0^+$ **great nuclear structure triumph**

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Theory changes overview

Recall master equation:

$$ft(1 + \delta'_R)(1 + \Delta_R^V)(1 + \delta_{NS} - \delta_C) = \frac{K}{G_F^2 V_{ud}^2 M_{tree}^2}$$

Every element has received updates/overhauls.

Theory changes overview

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Separate into **tree level** & **loop level**

Summary:

- δ_C : Isospin symmetry breaking of M_F
- f : phase space factor
- δ'_R : 'outer' radiative corrections
- Δ_R^V : single-nucleon 'inner' radiative corrections
- δ_{NS} : Changes in Δ_R^V due to nuclear structure

All except for Δ_R^V are **open questions** to this day!

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Summary of changes:

- δ_C : Ab initio & data-driven methods
- f : weak radii & Fermi function
- δ'_R : RGE methods find differences in $\mathcal{O}(\alpha^2 Z^3)$ and beyond
- Δ_R^V : Dispersion and lattice QCD confirm 'inner' RC change
- δ_{NS} : Focus on coherent quasielastic nuclear response

All except for Δ_R^V are **open questions** to this day!

Isospin breaking updates

Isospin breaking (\sim Coulomb interaction) means

$$M_F^2 = (M_F^0)^2(1 - \delta_C)$$

with $\delta_C \sim 0.1 - 1\%$ for **nuclei**.

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Isospin breaking (\sim Coulomb interaction) means

$$M_F^2 = (M_F^0)^2(1 - \delta_C)$$

with $\delta_C \sim 0.1 - 1\%$ for **nuclei**. Traditional approaches separate into

- δ_{C1} : isospin-mixing meaning $\langle \pi | a_{p,\alpha} | \phi_i \rangle^* \neq \langle \phi_f | a_{n,\alpha}^\dagger | \pi \rangle$
- δ_{C2} : radial mismatch, i.e. proton and neutron orbits are not the same

but conceptual issues already noted 15 years ago (Miller & Schwenk)

See talk by N. Smirnova

Isospin breaking updates

New proposal to use charge radii & ab initio theory. May write

$$\delta_C \simeq \sum_{T=0,1,2} \frac{\langle a; T || V_{\text{ISB}} || g; 1 \rangle^2}{(E_{a,T} - E_{g,1})^2}$$

over all states a and ground state g , **assuming** V_{ISB} is isovector.

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See talk by Michael Heines

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Interesting development: In *single nucleon*, ISB was assumed negligible ($\delta_C \sim (m_u - m_d)^2 / \Lambda_{\text{QCD}}^2$), but recently challenged and can be $\mathcal{O}(10^{-4})!$

PLB 838 (2023) 137654; PLB 846 (2023) 138259

Phase space updates

Integrating over β spectrum in usual expression

$$f = m_e^{-5} \int_{m_e}^{E_0} dE \rho E (E_0 - E)^2 F(Z, E) C(Z, E) K(Z, E)$$

Phase space updates

Integrating over β spectrum in usual expression

$$f = m_e^{-5} \int_{m_e}^{E_0} dE \rho E (E_0 - E)^2 F(Z, E) C(Z, E) K(Z, E)$$

but contains subtleties

- Depends on nuclear wave functions in $C(Z, E) \rightarrow$ weak charge density ρ_{cw}
- Special place for Fermi function $F(Z, E) \rightarrow$ is this a nice QFT object?

First point was long known (C_I in Wilkinson, shell model in H&T), but model-dependent. Data-driven treatment using charge radii

$$\rho_{cw} = \rho_{ch,0} + \frac{Z-1}{2} (\rho_{ch,-1} - \rho_{ch,1})$$

uncertainties $\mathcal{O}(10^{-3-4})$

Phase space and δ'_R updates

Special place of Fermi function is artefact of traditional segmented calculations (actually long-wavelength photon exchange)

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$F(Z, E)$ probes e^\pm density at $r = 0$, but since solution $\rightarrow \infty$, introduce UV cutoff *avant la lettre*: R , the nuclear radius.

Phase space and δ'_R updates

Special place of Fermi function is artefact of traditional segmented calculations (actually long-wavelength photon exchange)

$F(Z, E)$ probes e^\pm density at $r = 0$, but since solution $\rightarrow \infty$, introduce UV cutoff *avant la lettre*: R , the nuclear radius.

Currently called into question: is $F(Z, E)$ a good QFT object? When including higher-order corrections ($F \rightarrow F(1 + \delta_R)$), things become more complicated.

Still an **open question**, confusion due to disagreements with older calculations (1980's Jaus & Rasche)

PRL 133, 021803 (2024), PRD 109, 056006 (2024), PRD 108 (2023) 053003

Δ_R updates

Loop contribution that is (\sim)solved: Δ_R^V

Single-nucleon RC in β -decay can (\sim) be separated into

1. Energy-dependent, QCD-independent part: δ_R
2. Energy-independent, QCD-dependent part: Δ_R

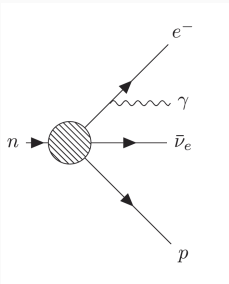
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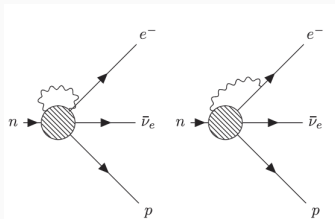
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2. Energy-independent, QCD-dependent part: Δ_R

δ_R mainly originates from
real photon emission



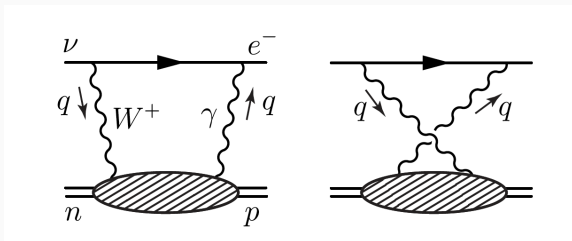
$\Delta_R^{V,A}$ renormalizes $g_{V,A}$

$$g_i^2 \rightarrow g_i^2(1 + \Delta_R^i)$$



Recent changes: Δ_R^V

The culprit for Δ_R^V : famous γW box



Specifically, **axial-vector** contribution \rightarrow symmetries don't save you
& QCD at intermediate effects

Recent changes: Δ_R^V

Recent breakthrough using dispersion relations

2006: Marciano

& Sirlin $\Delta_R^V = 0.02361(38)$,

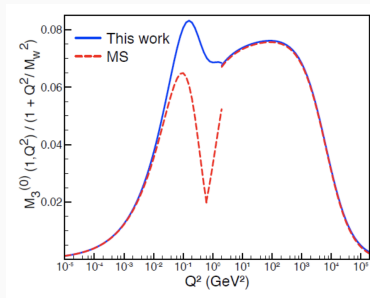
but heuristic uncertainty
from 'intermediate' energy scale

2018: Seng,

Gorchtein, Patel, Ramsey-Musolf

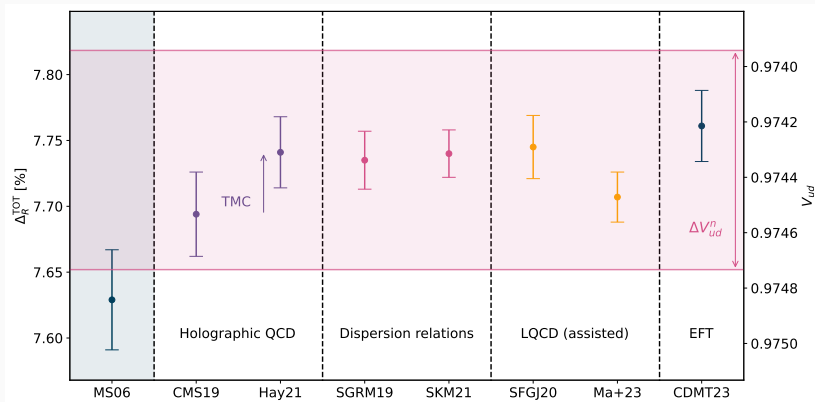
$\Delta_R^V = 0.02467(22)$ **4 σ shift**

Beginning of our CKM debacle!



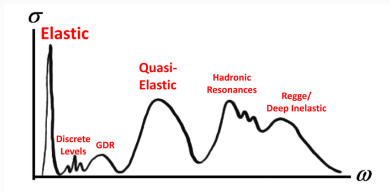
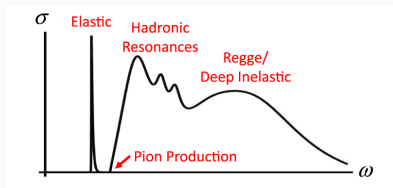
Seng, Gorchtein, Ramsey-Musolf
PRD 100 (2019) 013001

Number of different calculations performed, convergence

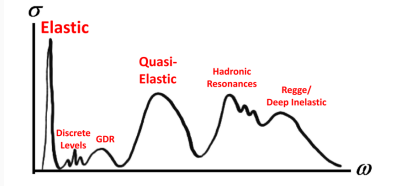
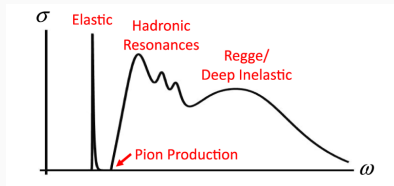


Small differences remain, neutron experimental uncertainty too large to distinguish

Nuclear medium changes nuclear response, but also spectrum



Nuclear medium changes nuclear response, but also spectrum



Paradigm shift in analysis, two major effects

Quasi-elastic contributions

$$\delta_{NS}^A = \frac{\alpha}{\pi} [-0.47 \pm 0.14]^{\text{QE}}$$

Nuclear polarization

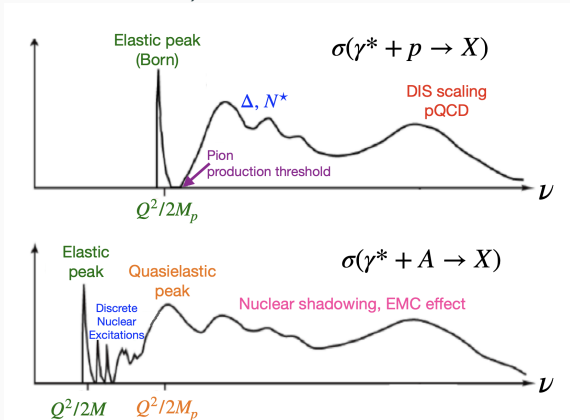
$$\delta_{NS}^A(E) \sim (1.6 \pm 1.6) \times 10^{-4} \left(\frac{E}{\text{MeV}} \right)$$

Estimated using free Fermi gas **Current** $0^+ \rightarrow 0^+$ **bottleneck**

Seng et al., PRD 100 013001

Current status on δ_{NS}

More sophisticated picture, first ab initio calculations emerging
(See talk by Mehdi Drissi)



Energy-dependent effects might be detectable, **nuclear shadowing** effects largely unknown Seng, Gorchtein ARNPS 74 (2024) 1

Open questions for mirror δ_{NS}

Situation is analogous but **more complicated** than $0^+ \rightarrow 0^+$.

Significant questions on:

- How do energy-dependent terms enter for axial transitions?
- What about nuclear shadowing for spin-dependent transitions?

Mirror decays extract $\rho = g_A M_{GT} / g_V M_F$ from angular correlations $(a_{\beta\nu}, A_\beta)$, but **both effects may mean $\rho^{\text{corr}} \neq \rho^{\text{Ft}}$** .

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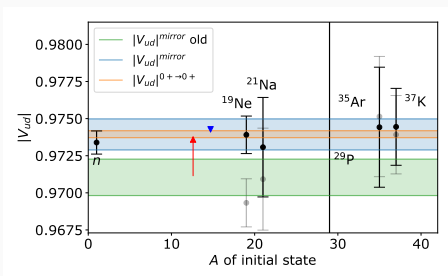
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Happened before:

double counting was resolved and V_{ud}^{mirror} now agrees with $V_{ud}^{0^+ \rightarrow 0^+}$

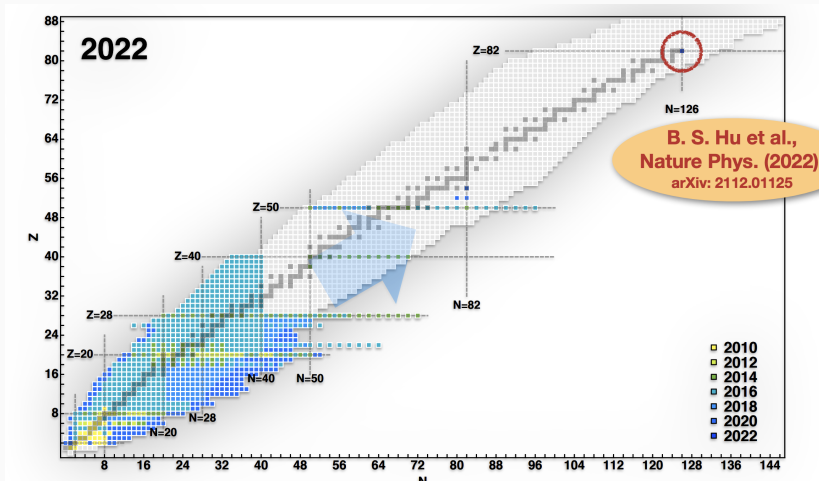
LH, PRD 103, 113001;

LH, ARNPS 74 (2024) 497



Progress in nuclear ab initio theory

Field is charging full steam ahead on nuclear ab initio



Theory summary

Takeaways

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Now, let's talk **experiment**

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Overview experimental opportunities

Several science drivers in parallel

- New experimental techniques to sidestep common systematics
- Spectrum shape measurements for δ_{NS} validation
- Precision measurements on low-mass isotopes for nuclear ab initio ladder benchmark

Overview experimental opportunities

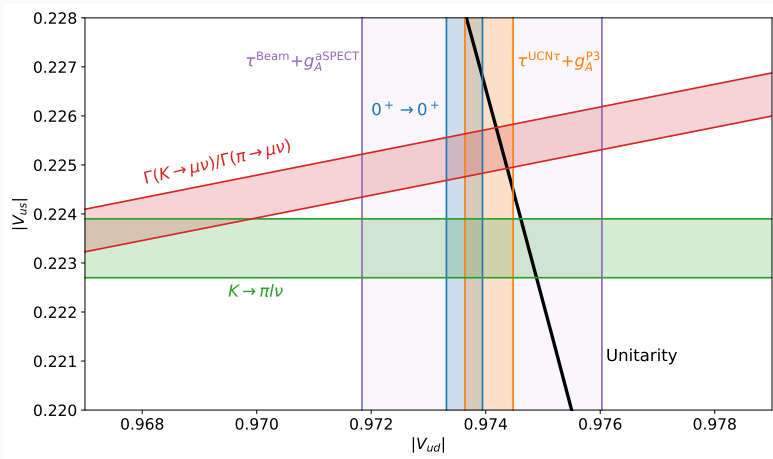
Several science drivers in parallel

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Necessary push in neutrons, opportunities in mirrors, validation in superalloweds

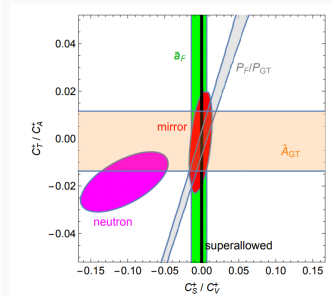
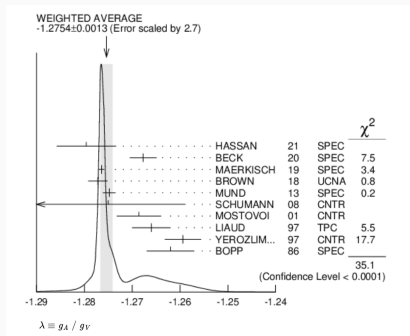
Progress in neutron experiments

Situation is complicated in both τ_n and $\lambda = g_A/g_V$ determinations



'Outlier' measurements agree with most precise for CKM unitarity

Current PDG average



aSPECT ($a_{\beta\nu}$) is in tension with other recent measurements (A_β)

Falkowski et al., JHEP04(2021)126

Progress in neutron experiments

Several campaigns worldwide (see talk by Bastian Märkisch)



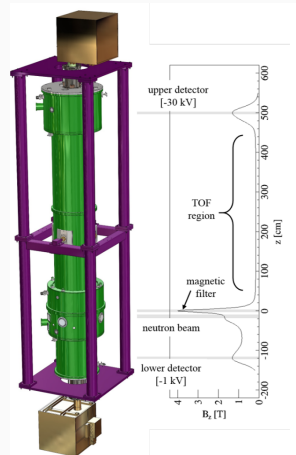
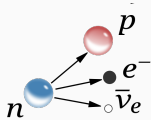
Nab is only $a_{\beta\nu}$ experiment aiming at 0.1%, **crucial input**

Nab - overview

Measurement of β - ν angular correlation

$$d\Gamma \propto d\Gamma_0 [1 + a_{\beta\nu} \beta \hat{p}_e \cdot \hat{p}_\nu]$$

in **neutron β decay** @ SNS (ORNL)

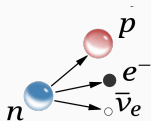


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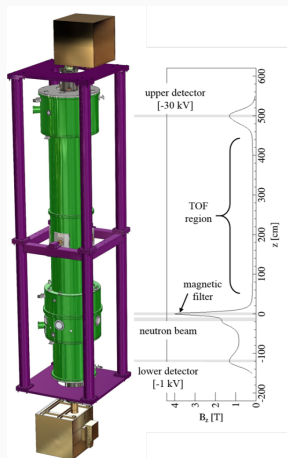
To leading order in SM

$$a_{\beta\nu} = \frac{1 - g_A^2}{1 + 3g_A^2}$$

and

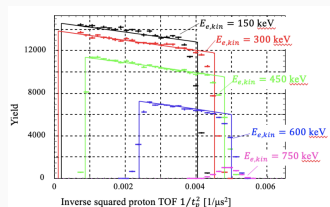
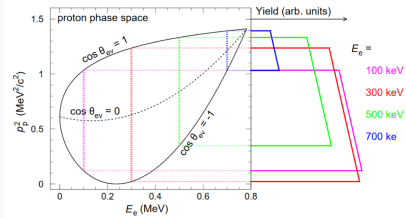
$$\frac{\delta a}{a} \approx 5 \frac{\delta g_A}{g_A}$$

meaning factor 5 sensitivity enhancement!



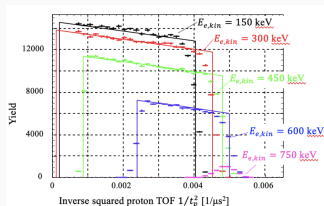
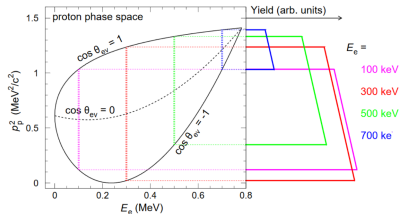
Nab progress

Measure p^+ instead of ν , $\vec{p}_p = -(\vec{p}_e + \vec{p}_\nu)$

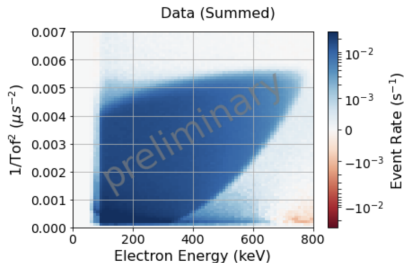
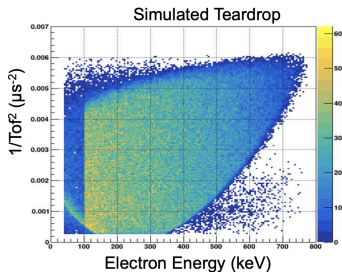


Nab progress

Measure p^+ instead of ν , $\vec{p}_p = -(\vec{p}_e + \vec{p}_\nu)$



First physics runs at ORNL are promising!



Experimental innovation

Community is investi(gati)ng in different ideas

${}^6\text{He}$ -CRES



with **new spectroscopy techniques** & traps

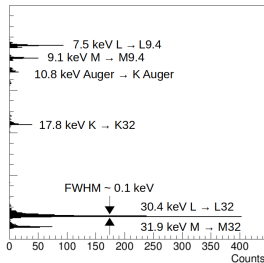
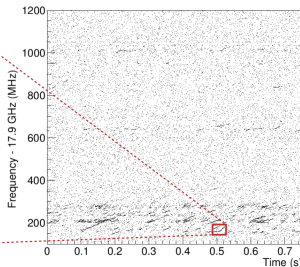
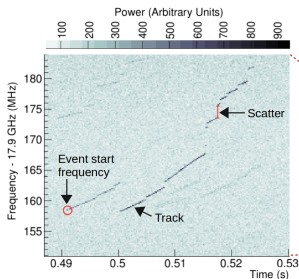
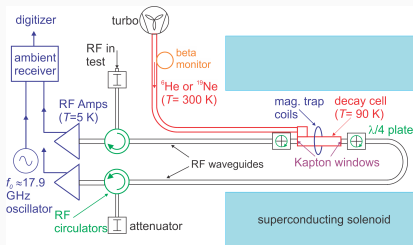
with additional great progress in the $A = 8$ system

New technology: CRES

Cyclotron Radiation Emission Spectroscopy

$$f = \frac{|q|}{2\pi} \frac{B}{m_e + E_{kin}}$$

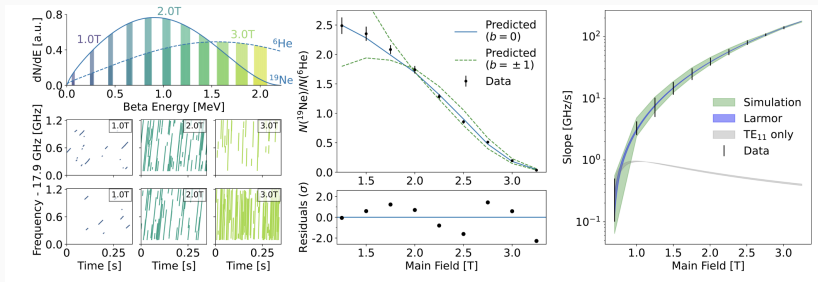
${}^6\text{He}$ and ${}^{19}\text{Ne}$



Physical Review Letters 131 (2023), 082502

New technology: CRES

Use ratio method: ${}^6\text{He}$ and ${}^{19}\text{Ne}$ have opposite b_F sign

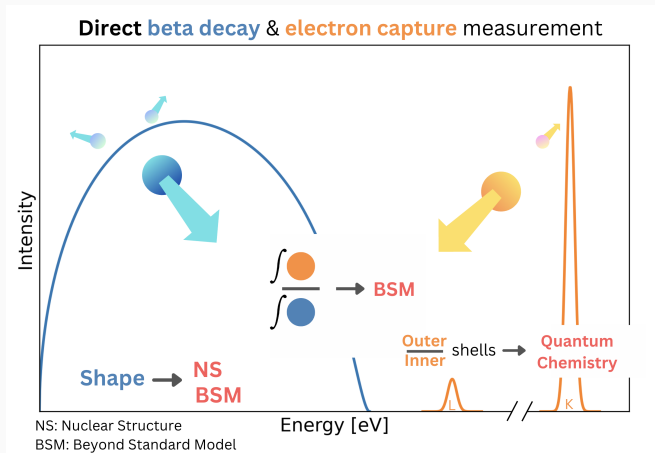


Ratio means many systematic effects cancel to first order

Physical Review Letters 131 (2023), 082502

Direct recoil spectroscopy

Richness in pure recoil spectra, but experimentally very difficult!

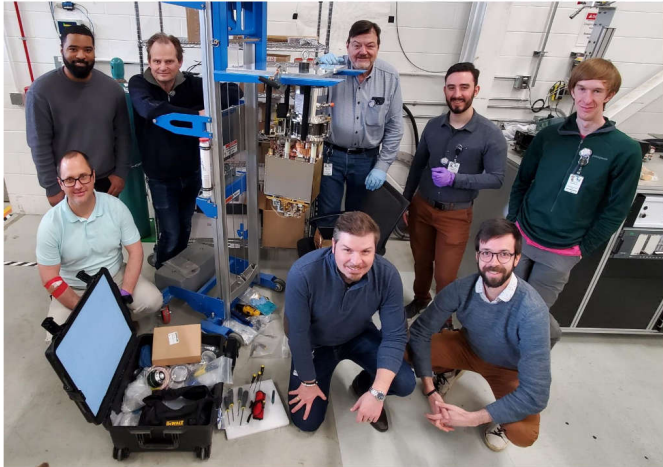


Enabled by novel **superconducting tunnel junctions**

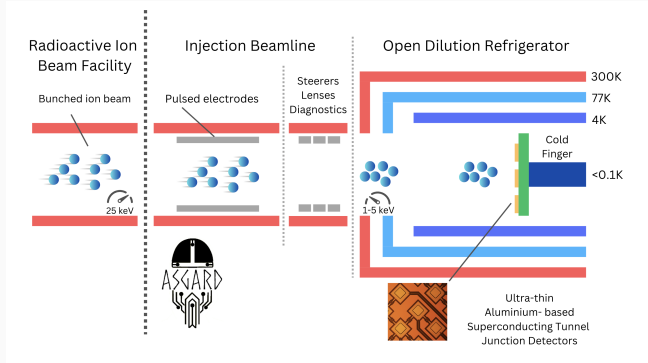
SALER@FRIB: First STJ online measurements



- Acceptance testing complete
- Commissioning started
- Will continue through 2024



Open STJs up to all ISOL beams, precision spectroscopy



Reduce systematic effects by 2-3 orders of magnitude!

(See talk by Mohamad Kanafani)

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Introduction

Theory progress in the last 5 years

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Theory very active, all inputs are being reevaluated. Significant opportunities/challenges for nuclear ab initio

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Better nuclear structure control is in progress, but 5+ years to bring down uncertainty significantly

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Experimentally, neutron has made great progress but more input is crucial. Mirror isotopes continue to be promising due to large enhancements

Summary & Outlook

Theory very active, all inputs are being reevaluated. Significant opportunities/challenges for nuclear ab initio

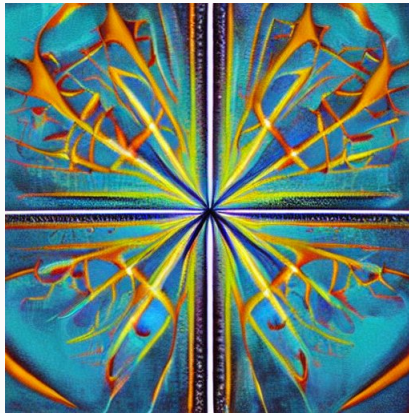
Better nuclear structure control is in progress, but 5+ years to bring down uncertainty significantly

Experimentally, neutron has made great progress but more input is crucial. Mirror isotopes continue to be promising due to large enhancements

New spectroscopy techniques incoming, recoil spectroscopy with quantum sensors is highly promising!

Thank you

Thank you!



β decay symmetries according to Stable Diffusion

Aside: recent progress on Δ_R^A

First $\mathcal{O}(\alpha)$ calculation of Δ_R^A , follow-up with dispersion relations and lattice QCD

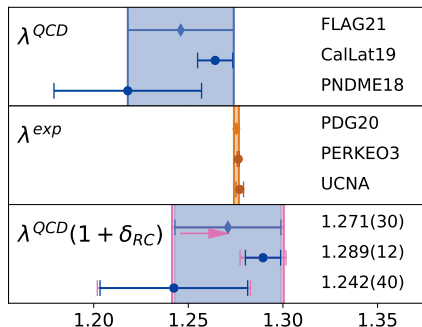
$$\Delta_R^A - \Delta_R^V = 0.13(13) \times 10^{-3}$$

Aside: recent progress on Δ_R^A

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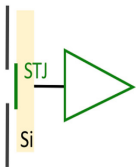
$$\Delta_R^A - \Delta_R^V = 0.13(13) \times 10^{-3}$$

but only first half of the story... also here large ISB effects

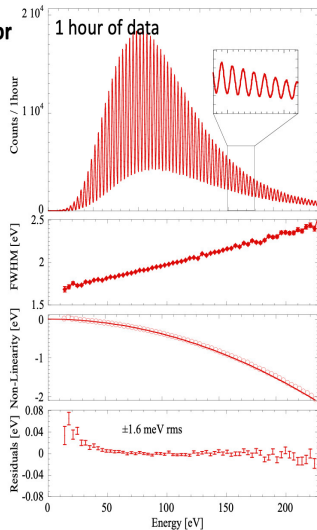


First time: $\delta_{RC}^{(\lambda)} \in \{1.4, 2.6\} \cdot 10^{-2}$ LH, PRD 103 113001; Seng, Particles 2021, 397; Gorchtein & Seng, JHEP 10 53; PRL 129 121801

Superconducting tunnel junctions (Slide by Kyle Leach)



Adiabatic Demagnetization Refrigerator (ADR) – Base Temp ~ 70 mK



S. Friedrich et al., J. Low Temp. Phys. **200**, 200 (2020)

- Pulsed 355 nm (3.49965(15) eV) laser at 5 kHz fed through optical fiber to 0.1 K stage
- Illumination of STJ provides a comb of peaks at integer multiples of 3.5 eV
- Intrinsic resolution of our Ta-based devices is between ~ 1.5 and ~ 2.5 eV FWHM at $\sim 10 - 200$ eV
- Stable response and small quadratic non-linearity (10^{-4} per eV)

The BeEST experiment (Slide by Kyle Leach)

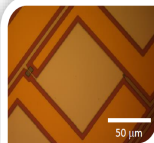


Rare-isotope implantation at TRIUMF-ISAC

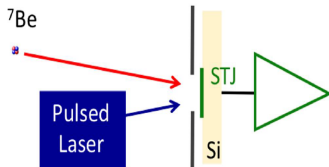


- A. Samanta *et al.*, Phys. Rev. Mat. (in press) (2022)
- S. Friedrich *et al.*, J. Low Temp. Phys. (in press) (2022)
- C. Bray *et al.*, J. Low Temp. Phys. (in press) (2022)
- K.G. Leach and S. Friedrich, J. Low Temp. Phys. (in press) (2022)
- S. Friedrich *et al.*, Phys. Rev. Lett. **126**, 021803 (2021)
- S. Fretwell *et al.*, Phys. Rev. Lett. **125**, 032701 (2020)
- S. Friedrich *et al.*, J. Low Temp. Phys. **200**, 200 (2020)

Ta, Al, and Nb-based STJ Sensors



STAR
CRYOELECTRONICS



GORDON AND BETTY
MOORE
FOUNDATION

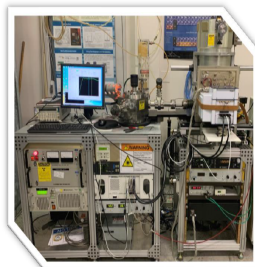


U.S. DEPARTMENT OF
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Office of
Science

EMPIR EURAMET

The EMPIR initiative is co-funded by the European Union's Horizon 2020 research and innovation programme and the EMPIR Participating States



Lawrence Livermore
National Laboratory

Introduction: Weak interaction & CKM matrix

Cabibbo-Kobayashi-Maskawa matrix relates weak and mass eigenstates

$$\begin{pmatrix} d \\ s \\ b \end{pmatrix}_w = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_m$$

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Unitarity requires

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Unitarity requires

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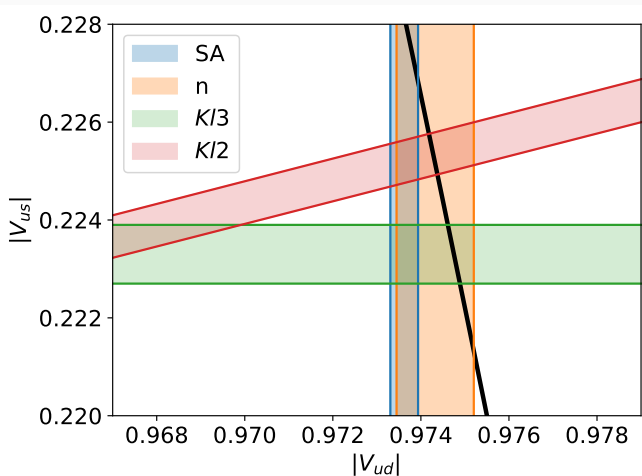
(nuclear) β decay, meson decay (π , K), $|V_{ub}|^2 \sim 10^{-5}$

Violations are sensitive to **TeV scale** new physics!

CKM unitarity: Current status

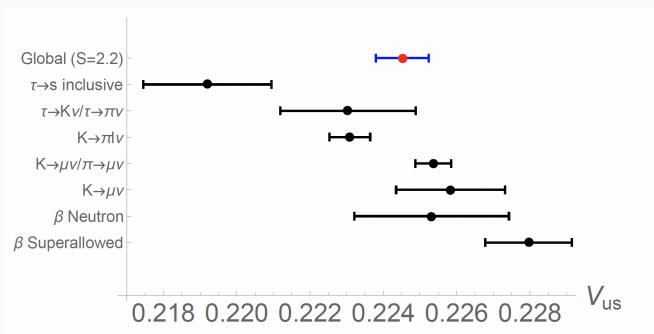
Signs of non-unitarity at few σ level...

Disagreement between $K/2$ and $K/3$ $|V_{us}|$ 'Cabibbo angle anomaly'



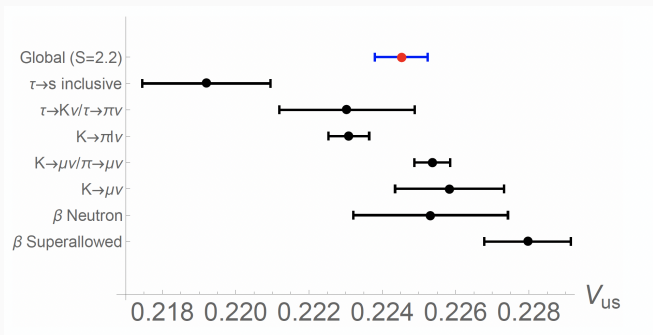
CKM unitarity: Cabibbo Angle Anomaly

Signs of non-unitarity at several σ (Falkowski CKM2021)



CKM unitarity: Cabibbo Angle Anomaly

Signs of non-unitarity at several σ (Falkowski CKM2021)



Takeaways assuming Standard Model physics:

- Most precise V_{ud} & V_{us} not consistent with unitarity
- Significant internal inconsistencies within V_{us}
- Taken at face value $\sim 3\sigma$ for new physics

A more modern way of interpreting BSM physics

Exotic contributions

A more modern way of interpreting BSM physics

Effective field theory: new physics at scale $\Lambda_{BSM} \gg \text{LHC}$

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \sum_{i=1} c_i \frac{\mathcal{O}_{4+i}}{\Lambda_{BSM}^i}$$

effective operators $\mathcal{O}(i)$. Expansion in parameter $c_i/\Lambda_{BSM}^i \ll 1$

Exotic contributions

A more modern way of interpreting BSM physics

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effective operators $\mathcal{O}(i)$. Expansion in parameter $c_i/\Lambda_{BSM}^i \ll 1$

Phenomenological theories will give different $\{c_i\}$,

but **agnostic experimental analysis**

Effective β decay

SM has V - A structure, but more generally

$$\mathcal{L}_{\text{eff}} = -\frac{G_F \tilde{V}_{ud}}{\sqrt{2}} \left\{ \bar{e} \gamma_\mu \nu_L \cdot \bar{u} \gamma^\mu [c_V - (c_A - 2c_R) \gamma^5] d + \epsilon_S \bar{e} \nu_L \cdot \bar{u} d \right. \\ \left. - \epsilon_P \bar{e} \nu_L \cdot \bar{u} \gamma^5 d + \epsilon_T \bar{e} \sigma_{\mu\nu} \nu_L \cdot \bar{u} \sigma^{\mu\nu} (1 - \gamma^5) d \right\} + \text{h.c.},$$

at the quark level

Effective β decay

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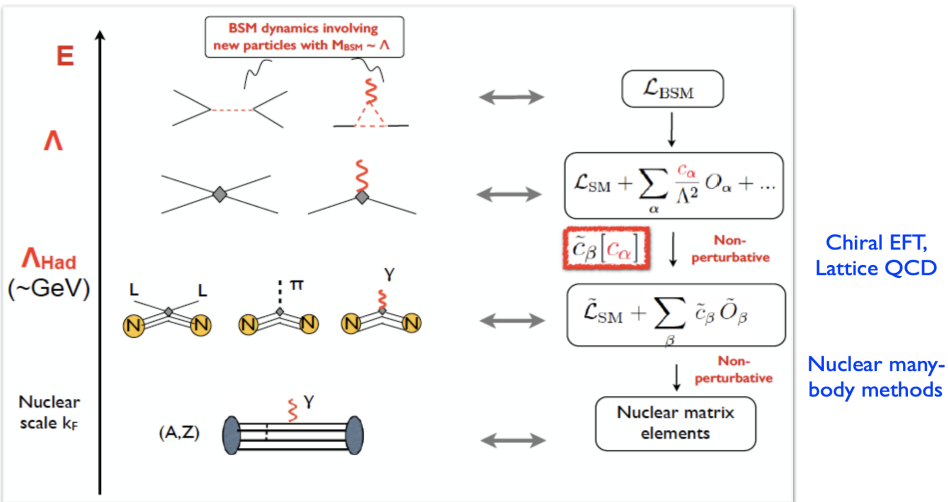
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at the quark level

All ϵ_i are proportional to $(M_W/\Lambda_{BSM})^2$, change kinematics

$\epsilon_i \lesssim 10^{-4} \rightarrow \Lambda_{BSM} \gtrsim 15 \text{ TeV}$ assuming natural couplings

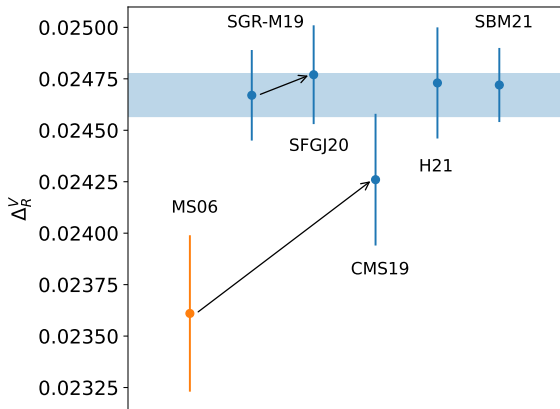
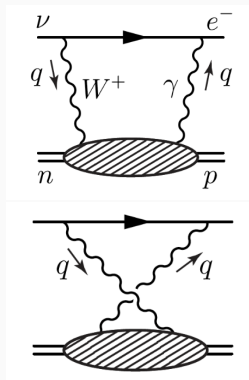
Effective field theory tower Slide by V. Cirigliano



- In order to build L_{eff} , one needs to specify:
 - ★ Relevant low-E **degrees of freedom**: *assume* SM field content
 - ★ One Higgs doublet, no light ν_R and no other light fields
 - ★ **Symmetries**: L_{eff} must reflect symmetries of underlying theory
 - ★ Assume underlying theory respects SM gauge group $SU(3)_c \times SU(2)_W \times U(1)_Y$
 - ★ But not necessarily SM symmetries that result from keeping only terms of dimension ≤ 4
 - ★ **Power counting** in $E/\Lambda, v_{EW}/\Lambda \ll 1$ (recall $v_{EW} = G_F^{-1/2}$): organize analysis in terms of operators of increasing dimension (5,6,...)

Recent changes: Δ_R^V

Number of new calculations performed



Now good convergence: uncertainty halved but about 3σ shift

CKM unitarity: V_{ud} precision

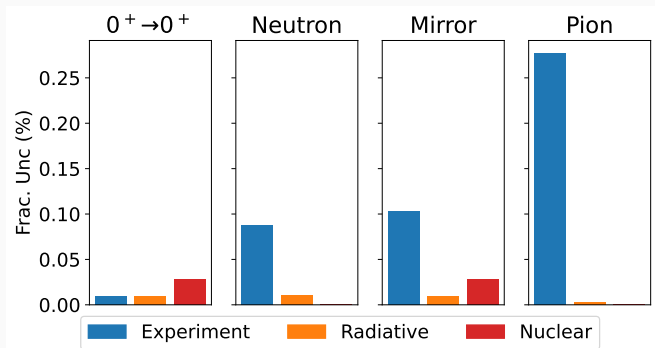
Nuclear sandbox \rightarrow make **hadronic theory** easy

- Pion
- Neutron
- Superaligned $0^+ \rightarrow 0^+$
- $T = 1/2$ mirrors

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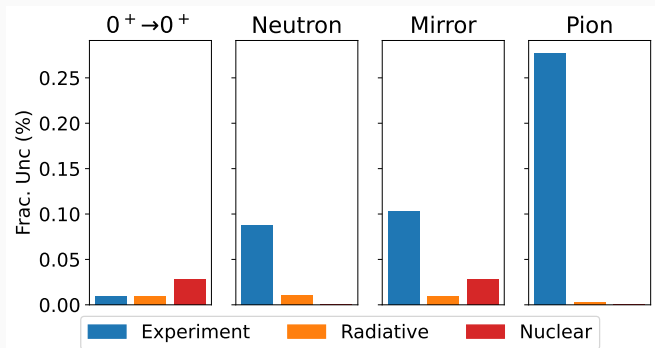


$\pi^+ \rightarrow \pi^0 e^+ \nu_e$ very hard (BR $\sim 10^{-8}$), SA new nuclear corrections!

CKM unitarity: V_{ud} precision

Nuclear sandbox → make **hadronic theory** easy

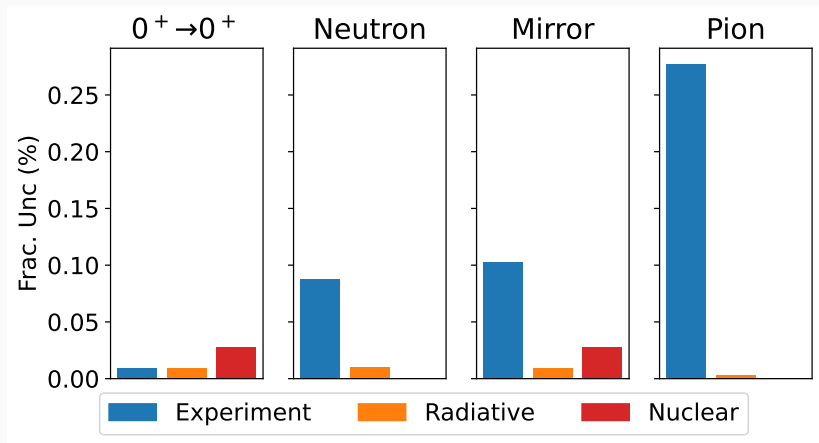
- Pion
- Neutron
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- $T = 1/2$ mirrors



Status of $0^+ \rightarrow 0^+$ **great nuclear structure triumph**

CKM unitarity: V_{ud} precision

Four (\sim)competitive channels of extracting V_{ud}

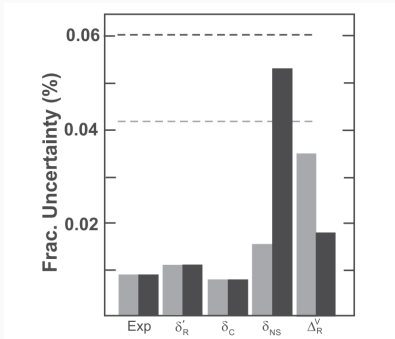
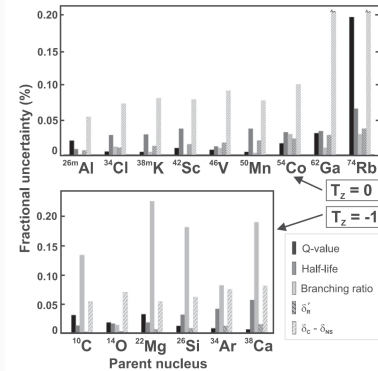


Status of $0^+ \rightarrow 0^+$ **great nuclear structure triumph**

2018-2020 reanalysis nuclear structure current bottleneck

Superaligned uncertainties

Experimentally, $T_z = -1$ limited by BR (new ^{10}C welcome)

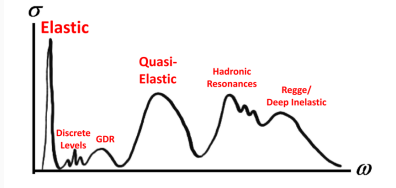
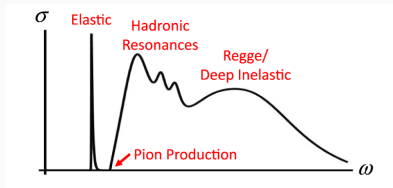


Moving towards mature *ab initio* theory evaluation

Talk by Bertram Blank

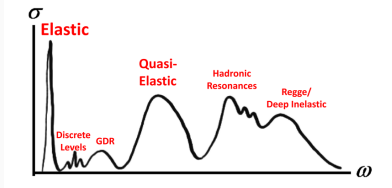
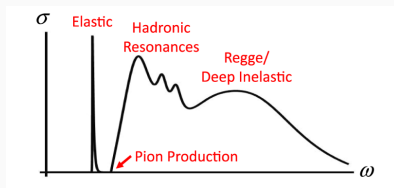
Recent changes: δ_{NS}

Nuclear medium changes nuclear response, but also spectrum



Recent changes: δ_{NS}

Nuclear medium changes nuclear response, but also spectrum



Paradigm shift in analysis, two major effects

Quasi-elastic contributions

$$\delta_{NS}^A = \frac{\alpha}{\pi} [-0.47 \pm 0.14]^{\text{QE}}$$

Nuclear polarization

$$\delta_{NS}^A(E) \sim (1.6 \pm 1.6) \times 10^{-4} \left(\frac{E}{\text{MeV}} \right)$$

Estimated using free Fermi gas **Current $0^+ \rightarrow 0^+$ bottleneck**

Seng et al., PRD 100 013001

On the radar: δ_C

Proton \neq neutron inside nucleus $\rightarrow M_F^2 = 2(1 - \delta_C)$

1. Configuration interaction difference initial \leftrightarrow final
2. Different radial wave function (Coulomb)

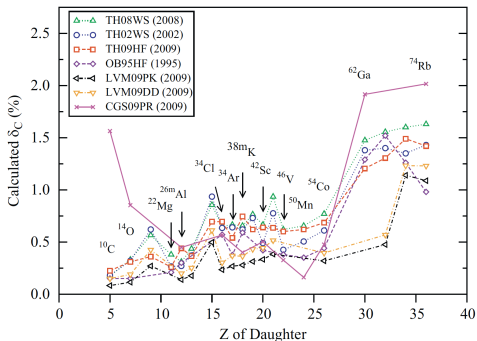
$$\delta_C = \delta_{C1} + \delta_{C2}$$

On the radar: δ_C

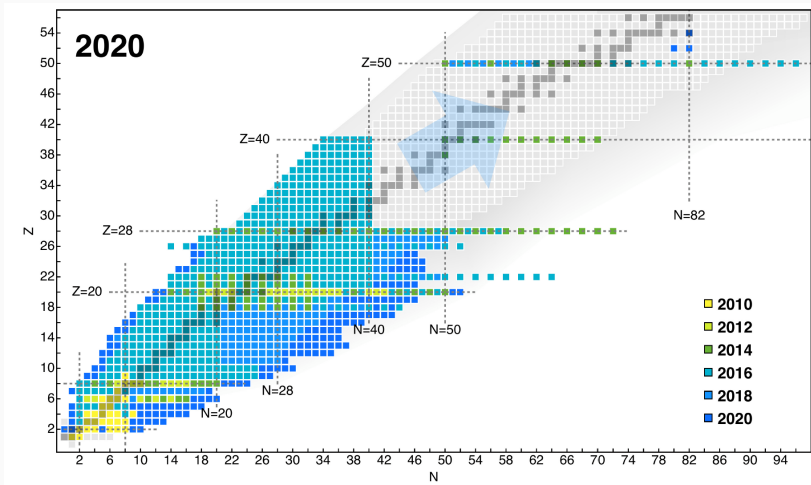
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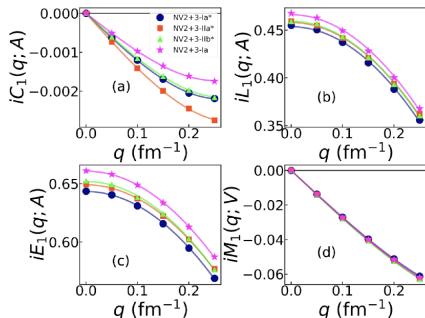
Progress in nuclear ab initio theory



H. Hergert, *Frontiers in Physics* (2020)

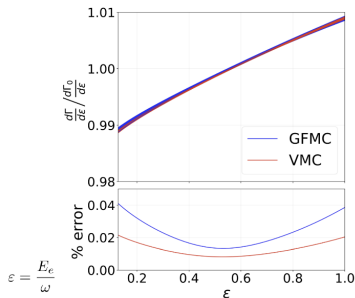
Ab initio is providing **bottleneck input** for spectral measurements

Beta Decay Spectrum



Dominant terms $L_1^{(0)}$ and $E_1^{(0)}$ have model dependence of $\sim 1\%$ to $\sim 2\%$

Standard Model spectrum for ${}^6\text{He}$



$$\tau_{\text{GFMC}} = 808 \pm 24 \text{ ms}$$

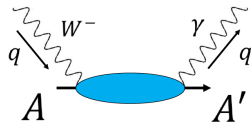
$$\tau_{\text{Expt.}} = 807.25 \pm 0.16 \pm 0.11 \text{ ms}$$

Garrett King et al. [arXiv:2207.11179](https://arxiv.org/abs/2207.11179)

Looking at implementing δ_{NS} for ${}^{10}\text{C}$

Compton amplitude in the NCSM

- Nuclear matrix elements for γW -box
 - 1) Express currents in momentum space
 - 2) Multipole expansion of current operators
 - 3) Connect currents to effective one-body operators



24

Lanczos continued fractions
method to compute Green's
functions!

$$\begin{aligned}
 T_3(q_0, Q^2) = & -4\pi i \frac{q_0}{q} \sqrt{M_i M_f} \sum_{J=1}^{\infty} (2J+1) \\
 & \times \langle A \lambda_f J_f M_f | \left[T_{J_0}^{mag}(q) G(M_f + q_0 + i\epsilon) T_{J_0}^{5,el}(q) + T_{J_0}^{el}(q) G(M_f + q_0 + i\epsilon) T_{J_0}^{5,mag}(q) \right. \\
 & \left. + T_{J_0}^{5,mag}(q) G(M_i - q_0 + i\epsilon) T_{J_0}^{el}(q) + T_{J_0}^{5,el}(q) G(M_i - q_0 + i\epsilon) T_{J_0}^{mag}(q) \right] | A \lambda_i J_i M_i \rangle
 \end{aligned}$$

Going heavier: IM-SRG type methods (Slide by Heiko Hergert)

- IMSRG for closed and open-shell nuclei: IM-HF and IM-PHFB

- HH, Phys. Scripta, Phys. Scripta 92, 023002 (2017)
- HH, S. K. Bogner, T. D. Morris, A. Schwenk, and K. Tuskijama, Phys. Rept. 621, 165 (2016)

- **Valence-Space IMSRG (VS-IMSRG)**

- S. R. Stroberg, HH, S. K. Bogner, J. D. Holt, Ann. Rev. Nucl. Part. Sci. 69, 165

- **In-Medium No Core Shell Model (IM-NCSM)**

- E. Gebrerufael, K. Vobig, HH, R. Roth, PRL 118, 152503

- **In-Medium Generator Coordinate Method (IM-GCM)**

- J. M. Yao, J. Engel, L. J. Wang, C. F. Jiao, HH PRC 98, 054311 (2018)
- J. M. Yao et al., PRL 124, 232501 (2020)

XYZ
define
reference



IMSRG
evolve
operators



XYZ
extract
observables

+ Coupled Cluster, ...

Nuclear theory impact

Major advances in last decade, EFT come into its own

Quantifiable theory uncertainties are **game-changer** for precision FS: paradigm shifts are strong driver of progress in the field

Benefit from 'rigorous' theory overlap at low masses (NCSM, GFMC, QMC)

- $0^+ \rightarrow 0^+$: ^{10}C & ^{14}O
- Promising isotopes: ^6He , ^{11}C , ...

to confidently go higher (CC, IM-SRG, IM-GCM, ...)

Path forward for $0^+ \rightarrow 0^+$ V_{ud}

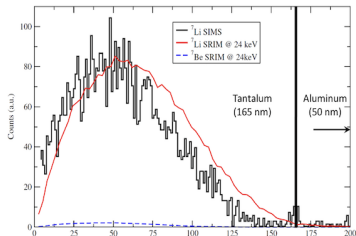
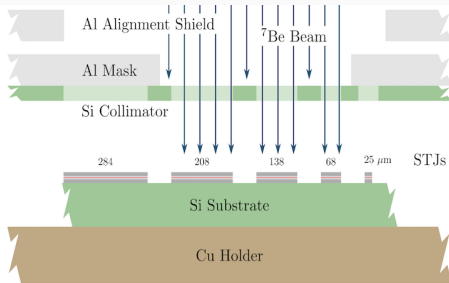
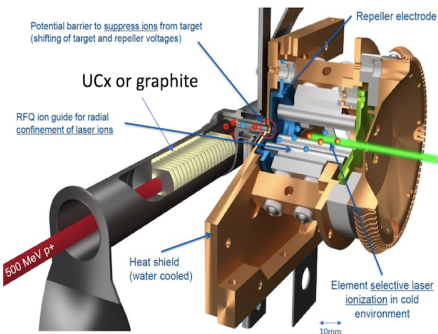
BeEST implantation



Isotope Separation On-Line
(ISOL) Method

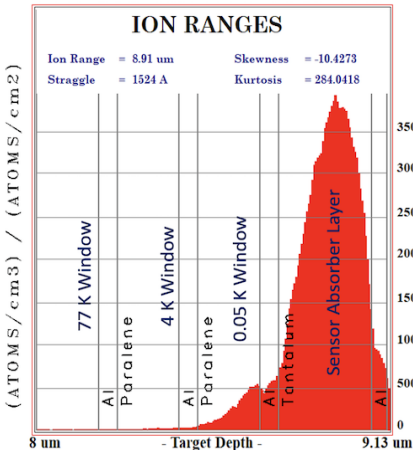
Element- and mass-
selective delivery of ${}^7\text{Be}$:

- Purity > 80%
- Rate > $1\text{e}8$ pps



SALER implantation

11 MeV ^{11}C Beam w/ 8 μm Al foil



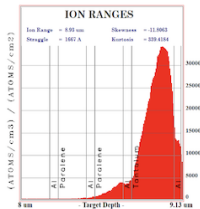
For a given energy, initial beam from ReA can be +/- a few % in spread

1% spread gives ~50 nm width in the depth profile

Total $^{11}\text{C}^+$ to achieve goal: $\sim 10^7$ (< 2 days of beam @ 100 pps)

Purity: 1 part in 10^6

11.1 MeV ^{11}C Beam



10.9 MeV ^{11}C Beam

