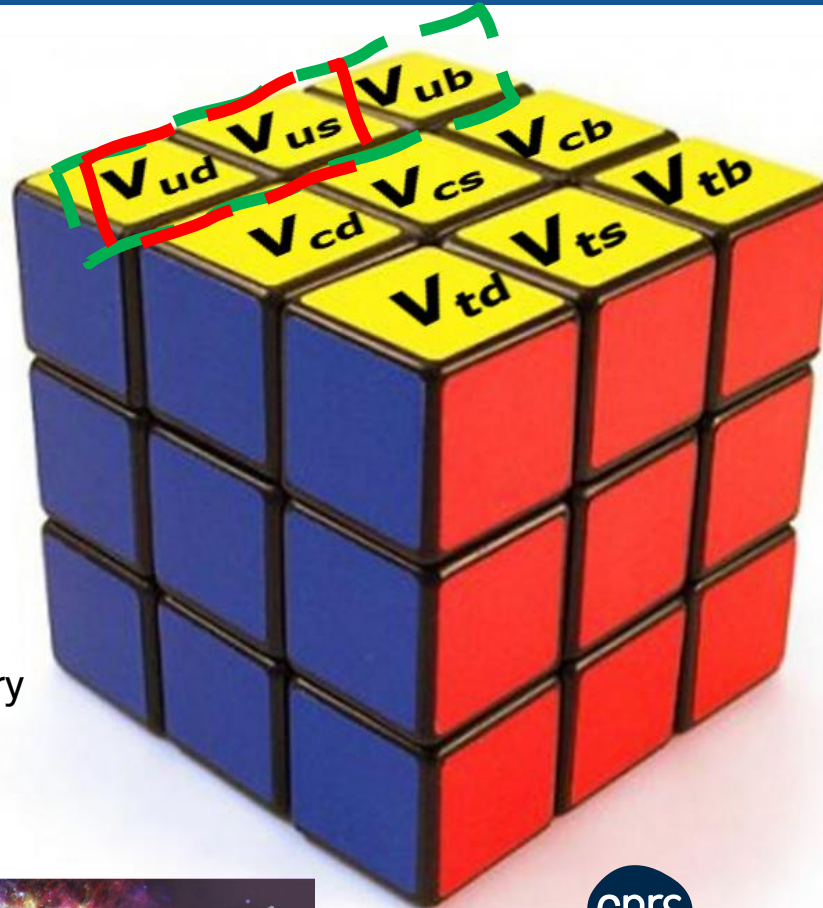


V_{ud} in the CKM matrix: unitary test*

V. Tisserand, LPCA - Clermont Ferrand, France

GANIL Caen, Nov. 5th 2024

Workshop on V_{ud} from pion, neutron and nuclear beta decay



*Is there a problem with V_{us}
→ The Cabibbo anomaly?

🙏 Credits to
E. Passemar

(IFIC Valencia/Indiana Univ)
+ A. Teixeira @ CS IN2P3 24
(LPCA)

+ CKM WS 2023 WG1 summary
+ PDG 2024

INTENSITY

frontier

GDR-Inf

RESANET

Réactions, structure et Astrophysique
Nucléaires: Expériences et Théories



NUCLÉAIRE
& PARTICULES

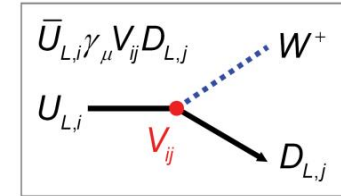


The Standard Model (SM) & the Unitary CKM Matrix

→ mixing of the 3 quarks families & CP violation

- the Higgs boson gives mass to elementary bosons & fermions (quarks, leptons) through Yukawa couplings, but there is not only that ! :

$$\mathcal{L}_{cc}^{\text{quarks}} = \frac{g}{2\sqrt{2}} W_{\mu}^{\dagger} \left[\sum_{ij} \bar{u}_i(q_2) \gamma^{\mu} (1 - \gamma^5) V_{ij} d_j \right] + \text{h.c}$$



charged currents (EW) imply transitions between quark families : quarks decays [there are no neutral current changing flavour (FCNC) at tree level (i.e., GIM mechanism)].

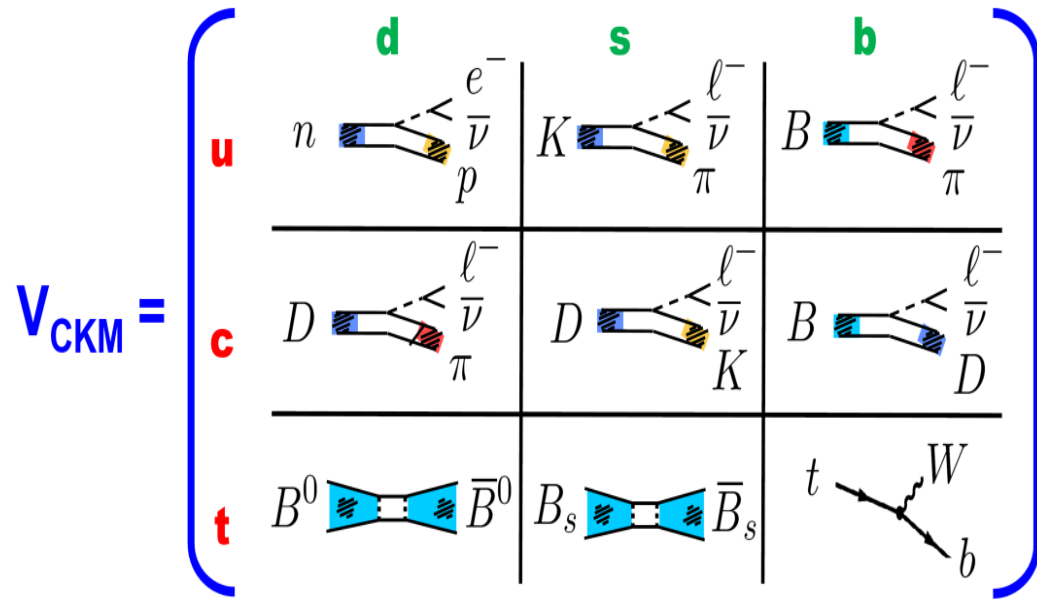
$$V_{\text{CKM}} = \begin{pmatrix} & \mathbf{d} & \mathbf{s} & \mathbf{b} \\ \mathbf{u} & 1-\lambda^2/2 & \lambda & A\lambda^3(\rho-i\eta) \\ \mathbf{c} & -\lambda & 1-\lambda^2/2 & A\lambda^2 \\ \mathbf{t} & A\lambda^3(1-\rho-i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4) \quad (\mathbf{V}\mathbf{V}^{\dagger} = \mathbf{1})$$

- strong hierarchy** in EW V_{ij} couplings for the 3 families (wrt diagonal couplings $\propto \lambda^N \approx (0.225)^N$:

→ Cabibbo angle = V_{us}).

- KM** (Kobayashi-Maskawa) mechanism : **3 generations** → **4 params**: A , λ , ρ & **1 complex part** η which phase is the unique source of CPV in SM.

The CKM Matrix, the unitary triangle & the very rich phenomenology of quark flavours



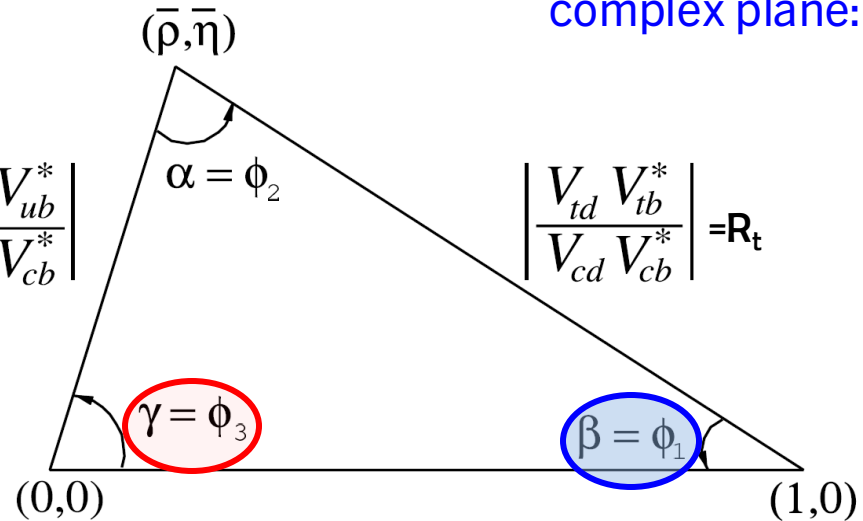
→ 4 parameters (A, λ, ρ & η) to be obtained/tested wrt. data: nucleons, K, D, $B_{(s)}$ & top quark physics.

→ unitarity relation in B_d system (1st line/3rd column):

$$\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} + 1 + \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} = 0$$

$$O(1) + O(1) + O(1)$$

Unitarity triangle in the $(\bar{\rho}, \bar{\eta})$ complex plane:



Parametrisation « à la Wolfenstein » phase invariant & valid at any orders in λ @ CKMfitter (EPJ C41, 1-131, 2005):

$$\bar{\rho} + i\bar{\eta} = -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2}$$

$$A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2}$$

$$R_u = \left| \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right| \quad R_t = \left| \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} \right|$$

The CKM Matrix, testing the unitarity paradigm in the first line/row

Les deux infinis

CKM paradigm of flavour mixing: **FV** encoded in *strongly hierarchical unitary* matrix
 Mostly **successful** description of hadron flavour dynamics!

EW fit and V_{CKM} fit appear to be in good agreement with SM hypotheses!

But recent **tensions** in the determination of the "Cabibbo angle" (and of V_{ud} and V_{us})

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1 \Rightarrow \sin \theta_C = V_{ud}, \cos \theta_C = V_{us}$$

$$\Rightarrow \Delta_{CKM} = |\bar{V}_{ud}|^2 + |\bar{V}_{us}|^2 - 1 = 0$$

Negligible

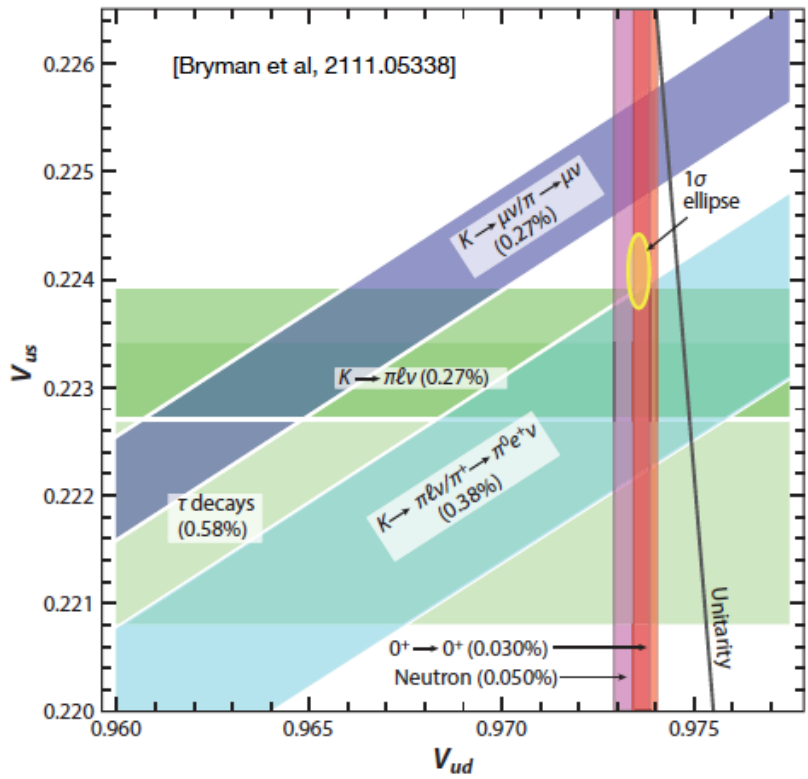
Phenomenological determination of \bar{V}_{ud} and \bar{V}_{us} (recall that $|\bar{V}_{ub}| \approx \mathcal{O}(10^{-3})$)
 \Rightarrow test unitarity of 1st row of CKM

Overview of \bar{V}_{ud} and \bar{V}_{us} constraints:
 nuclear, nucleon, meson & τ decays (1σ bands for V_{ij})

Global fit: $V_{ud} = 0.97379 \pm 0.00025$
 $V_{us} = 0.22405 \pm 0.00035$
 $\Rightarrow \Delta_{CKM} = (-19.5 \pm 5.3) \times 10^{-4}$

[Crivellin et al, 2212.06862]

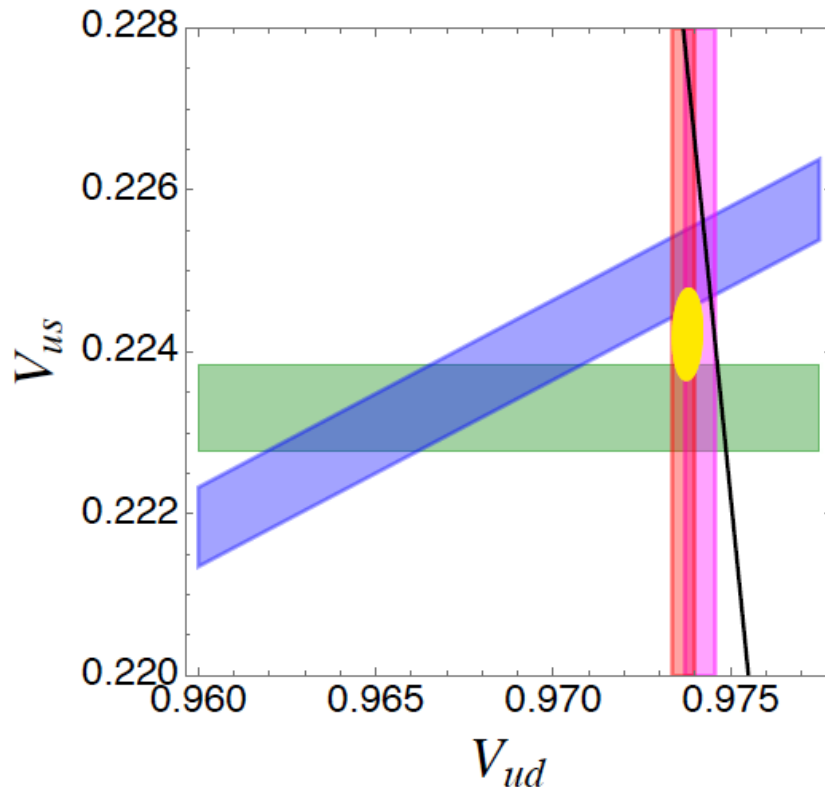
\Rightarrow Deviation from SM unitarity @ 2.8σ



The CKM Matrix, testing the unitarity paradigm in the first line/row

One year back at CKM23 WS @ Santiago de Compostela

Tension in first-row unitarity



Cirigliano, Crivellin, Hoferichter, Moulson 2023

- ▶ Three bands from
 - ▶ $K_{\ell 3} = K \rightarrow \pi \ell \nu_\ell$
 - ▶ $\pi_{\ell 2}/K_{\ell 2}$
 - ▶ β decays (superallowed, neutron)

▶ Tensions

$$\Delta_{\text{CKM}} = |V_{ud}|^2 + |V_{us}|^2 - 1$$
$$\Delta_{\text{CKM}}^{K_{\ell 2}-K_{\ell 3}} = -0.016(6) [2.6\sigma]$$
$$\Delta_{\text{CKM}}^{K_{\ell 2}-\beta} = -0.0010(6) [1.7\sigma]$$
$$\Delta_{\text{CKM}}^{K_{\ell 3}-\beta} = -0.0018(6) [3.1\sigma]$$
$$\Delta_{\text{CKM}}^{\text{global}} = -0.0018(6) [2.8\sigma]$$

- ▶ Need to improve V_{ud} , V_{us} !

In the TODAY/GANIL workshop we review the V_{ud} determination and prospects
I will talk a bit more on V_{us} in this talk

The CKM Matrix, testing the unitarity paradigm in the first line/row

Standard-model coupling of quarks and leptons to W :

$$\frac{g}{\sqrt{2}} W_\alpha^+ (\bar{\mathbf{U}}_L \mathbf{V}_{\text{CKM}} \gamma^\alpha \mathbf{D}_L + \bar{e}_L \gamma^\alpha \nu_{eL} + \bar{\mu}_L \gamma^\alpha \nu_{\mu L} + \bar{\tau}_L \gamma^\alpha \nu_{\tau L}) + \text{h.c.}$$

↑
Single gauge coupling

↑
Unitary matrix

$$\Delta_{\text{CKM}} \equiv |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1$$

$\approx 2 \times 10^{-5}$

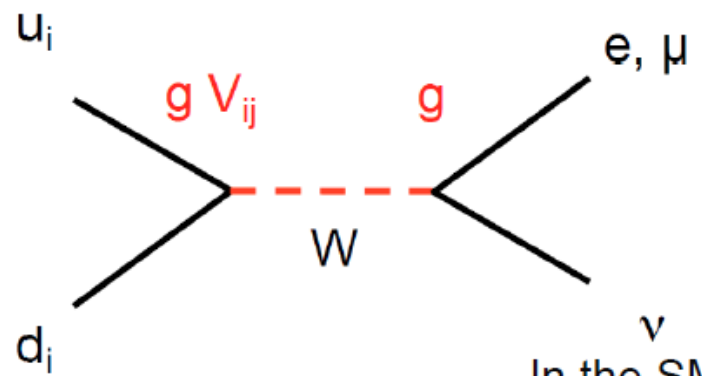
Most precise test of CKM unitarity!

$$\left. \begin{aligned} G_{\text{CKM},ij} &\sim G_\mu V_{ij} \sim (g^2/M_W^2) V_{ij} \\ \delta G_{\text{CKM}} &\sim 1/\Lambda^2 \quad \leftarrow \text{energy scale for NP} \end{aligned} \right\} \text{BSM effects scale as } (M_W^2/g^2)/\Lambda^2$$



For measurement of Δ_{CKM} with total uncertainty σ :

- Scale probed is $\Lambda \sim (M_W/g)/\sqrt{\sigma}$
- For $\sigma \sim 10^{-4} \rightarrow$ probe $\Lambda \sim 20 \text{ TeV}$



This is the so called Cabibbo Anomaly

$$|V_{ud}| = \cos \theta_c \quad \text{and} \quad |V_{us}| = \sin \theta_c$$

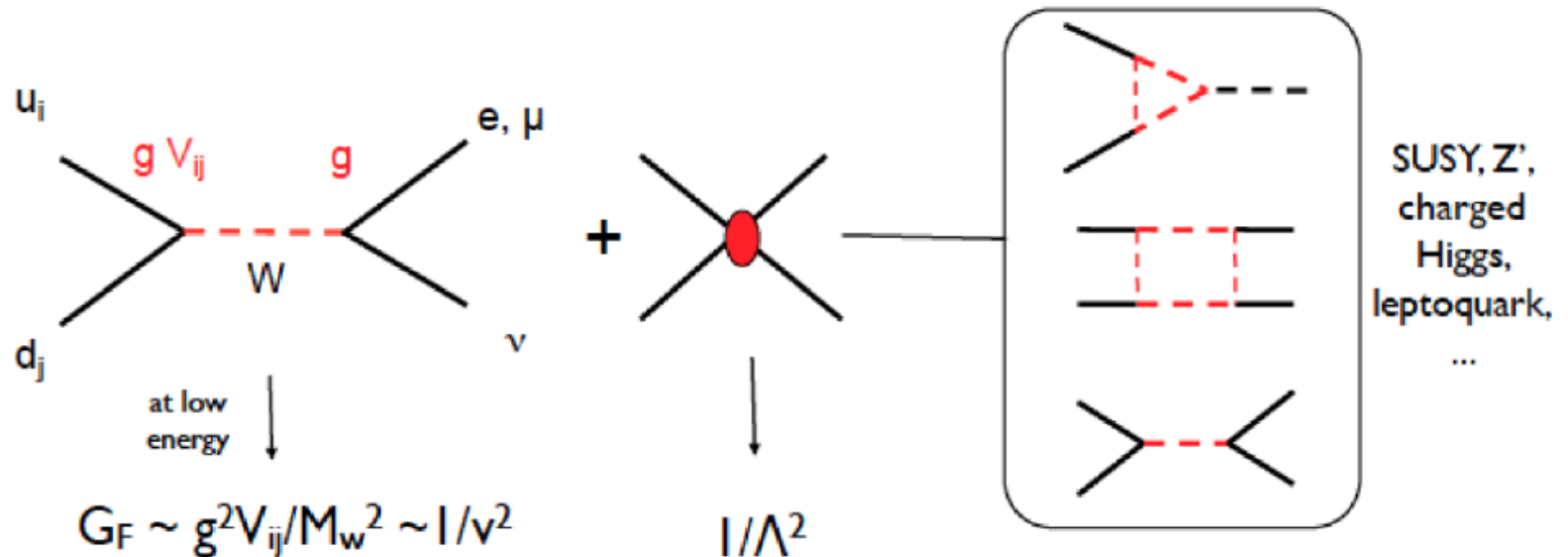
In the SM: W exchange \rightarrow V - A structure only

The CKM Matrix, testing the unitarity paradigm in the first line/row

Constraining BSM/New Physics ?

- BSM: sensitive to tree-level and loop effects of a large class of models

➔
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 + \Delta_{CKM}$$



➔ BSM effects :
$$\Delta \sim \frac{c_n M_W^2}{g^2 \Lambda^2} \leq 10^{-2} - 10^{-3} \leftrightarrow \Lambda \sim 1-10 \text{ TeV}$$

Paths to V_{ud} and V_{us}

- From kaon, pion, baryon and nuclear decays

V_{ud}	$0^+ \rightarrow 0^+$ $\pi^\pm \rightarrow \pi^0 e \nu_e$	$n \rightarrow p e \nu_e$	$\pi \rightarrow l \nu_l$
V_{us}	$K \rightarrow \pi l \nu_l$ KI3	$\Lambda \rightarrow p e \nu_e$	$K \rightarrow l \nu_l$ KI2

$$\Gamma_k = (G_F^{(\mu)})^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \delta_{RC}) \times F_{\text{kin}}$$

Channel-dependent
effective CKM element

Hadronic matrix
element

Radiative corrections

- Recent progress on
- 1) Hadronic matrix elements from lattice QCD
 - 2) Radiative corrections from dispersive methods + Lattice QCD

Determination of V_{ud}

One year back at CKM23 WS @ Santiago de Compostela
WG1 summary

1. **Superaligned β decays** ($0^+ \rightarrow 0^+$ nuclear transitions) Talk by M. Gorchtein
 - ▶ +: many isotopes to average
 - ▶ -: nuclear uncertainties
2. **Neutron decay** ($n \rightarrow pe^+\bar{\nu}_e$) Talks by W. Dekens, B. Märkisch, U. Schmidt
 - ▶ +: no nuclear uncertainties
 - ▶ -: need neutron lifetime τ_n and decay asymmetry $\lambda = g_A/g_V$
3. **Pion β decay** ($\pi^+ \rightarrow \pi^0 e^+ \bar{\nu}_e$) Talk by M. Hoferichter
 - ▶ +: theoretically pristine
 - ▶ -: experimentally challenging

MUCH MORE in the TODAY/GANIL workshop we review the V_{ud} determination and prospects

Determination of V_{us} from kaon decays

One year back at CKM23 WS @ Santiago de Compostela
WG1 summary

Talk by M. Moulson:

$$\Gamma(K_{\ell 3}(\gamma)) = \frac{C_K^2 G_F^2 m_K^5}{192\pi^3} S_{EW} |V_{us}|^2 |f_+^{K^0\pi^-}(0)|^2 \times I_{K\ell}(\lambda_{K\ell}) \left(1 + 2\Delta_K^{SU(2)} + 2\Delta_{K\ell}^{EM}\right)$$

with $K \in \{K^+, K^0\}$; $\ell \in \{e, \mu\}$, and:

C_K^2 1/2 for K^+ , 1 for K^0

S_{EW} Universal SD EW correction (1.0232)

Inputs from experiment:

$\Gamma(K_{\ell 3}(\gamma))$ Rates with well-determined treatment of radiative decays:

- Branching ratios: K_S, K_L, K^\pm
- Kaon lifetimes

$I_{K\ell}(\{\lambda\}_{K\ell})$ Integral of form factor over phase space: λ s parameterize evolution in t

- K_{e3} : Only λ_+ (or λ_+', λ_+'')
- $K_{\mu 3}$: Need λ_+ and λ_0

Inputs from theory:

$f_+^{K^0\pi^-}(0)$ Hadronic matrix element (form factor) at zero momentum transfer ($t=0$)

$\Delta_K^{SU(2)}$ Form-factor correction for $SU(2)$ breaking

$\Delta_{K\ell}^{EM}$ Form-factor correction for long-distance EM effects

Determination of V_{us} from kaon decays

One year back at CKM23 WS @ Santiago de Compostela
WG1 summary

New KLOE measurement of $K_S \rightarrow \pi \ell \nu$

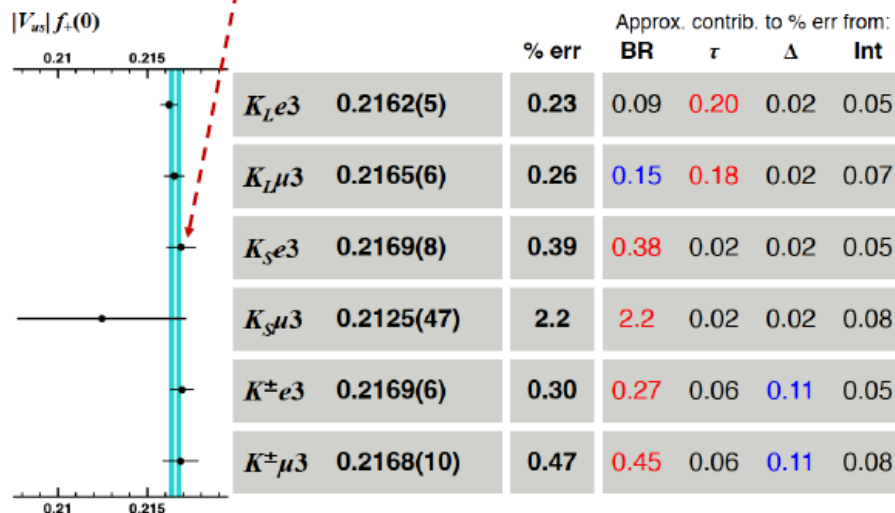
Talk by A. Passeri:

JHEP 02 (2023) 098

KLOE: analysis of the data sample (1.63 fb^{-1}) collected in 2004-05, measured ratio:

$$\mathcal{R} = \frac{\Gamma(K_S \rightarrow \pi e \nu)}{\Gamma(K_S \rightarrow \pi^+ \pi^-)} = \frac{N_{\pi e \nu}}{\epsilon_{\pi e \nu}} \times \frac{\epsilon_{\pi \pi}}{N_{\pi \pi}} \times R_\epsilon = (1.0338 \pm 0.0054_{\text{stat}} \pm 0.0064_{\text{syst}}) \times 10^{-3}$$

$$\mathcal{B}(K_S \rightarrow \pi e \nu) = (7.153 \pm 0.037_{\text{stat}} \pm 0.044_{\text{syst}}) \times 10^{-4} = (7.153 \pm 0.058) \times 10^{-4}$$



Average (M. Moulson):

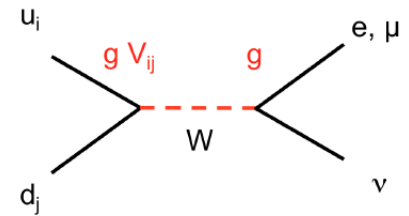
$$|V_{us}|f_+(0) = 0.21656(35)$$

Determination of V_{us} / V_{ud} and K_{l2} decays

One year back at CKM23 WS
@ Santiago de Compostela
WG1 summary

From kaon, pion, baryon and nuclear decays

V_{ud}	$0^+ \rightarrow 0^+$ $\pi^\pm \rightarrow \pi^0 e \nu_e$	$n \rightarrow p e \nu_e$	$\pi \rightarrow l \nu_l$
V_{us}	$K \rightarrow \pi l \nu_l$ Kl3	$\Lambda \rightarrow p e \nu_e$	$K \rightarrow l \nu_l$ Kl2



Talk by M. Moulson:

$$\frac{|V_{us}|}{|V_{ud}|} \frac{f_K}{f_\pi} = \left(\frac{\Gamma_{K\mu 2(\gamma)} m_{\pi^\pm}}{\Gamma_{\pi\mu 2(\gamma)} m_{K^\pm}} \right)^{1/2} \frac{1 - m_\mu^2/m_{\pi^\pm}^2}{1 - m_\mu^2/m_{K^\pm}^2} \left(1 - \frac{1}{2} \delta_{EM} - \frac{1}{2} \delta_{SU(2)} \right)$$

Inputs from experiment:

From K^\pm BR fit:

$$\text{BR}(K^\pm_{\mu 2(\gamma)}) = 0.6358(11)$$

$$\tau_{K^\pm} = 12.384(15) \text{ ns}$$

From PDG:

$$\text{BR}(\pi^\pm_{\mu 2(\gamma)}) = 0.9999$$

$$\tau_{\pi^\pm} = 26.033(5) \text{ ns}$$

Inputs from theory:

δ_{EM} Long-distance EM corrections

$\delta_{SU(2)}$ Strong isospin breaking
 $f_K/f_\pi \rightarrow f_{K^\pm}/f_{\pi^\pm}$

f_K/f_π Ratio of decay constants

Cancellation of lattice-scale uncertainties from ratio

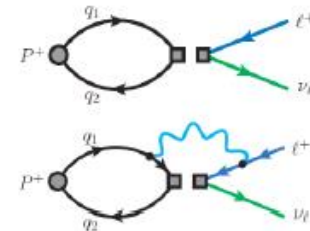
NB: Most lattice results already corrected for $SU(2)$ -breaking: f_{K^\pm}/f_{π^\pm}

Determination of V_{us} / V_{ud} from Lattice

One year back at CKM23 WS @ Santiago de Compostela
WG1 summary

Talk by F. Erben:

- Experiment very accurately determines $|V_{us}/V_{ud}|f_{K^+}/f_{\pi^+}$ [PDG, Prog. Theor. Exp. Phys. 2022, 083C01]
- Ratio of decay constants f_{K^+}/f_{π^+} can also be accurately determined from lattice QCD
- sub-percent precision: **isospin-breaking** and **QED effects** need to be controlled!



Final result:

$$\frac{|V_{us}|}{|V_{ud}|} = \left[\frac{\Gamma(K \rightarrow \mu\nu) m_K (m_\pi^2 - m_\mu^2)}{\Gamma(\pi \rightarrow \mu\nu) m_\pi (m_K^2 - m_\mu^2)} \right]^{1/2} \frac{f_\pi}{f_K} \left(1 - \frac{1}{2} \delta R_{K\pi} \right)$$

with values from experiment, FLAG lattice average, and this calculation:

$$\delta R_{K\pi} = -0.0086(3)_{\text{stat.}} \left(\begin{smallmatrix} +11 \\ -4 \end{smallmatrix} \right)_{\text{fit}} (5)_{\text{disc.}} (5)_{\text{quench.}} (39)_{\text{vol.}}$$

leading to

$$\frac{|V_{us}|}{|V_{ud}|} = 0.23154(28)_{\text{exp.}} (15)_{\delta R_{K\pi}} (45)_{\delta R_{K\pi, \text{vol.}}} (65)_{f_\pi/f_K}$$

- our uncertainty is dominated by finite-volume error due to single lattice spacing - this will improve drastically in the near future! [Matteo Di Carlo, plenary at Lattice23]
- result in agreement with only other lattice calculation [Di Carlo et al., Phys.Rev.D 100 (2019) 3, 034514]
- $|V_{us}|/|V_{ud}|$ uncertainty dominated by f_π/f_K lattice average

New work:

Prospects for a lattice calculation of the rare decay $\Sigma^+ \rightarrow p \ell^+ \ell^-$, [F. Erben et al., JHEP 04 (2023) 108]

V_{us} and V_{us}/V_{ud} from kaons, first-row fit

One year back at CKM23 WS @ Santiago de Compostela
WG1 summary

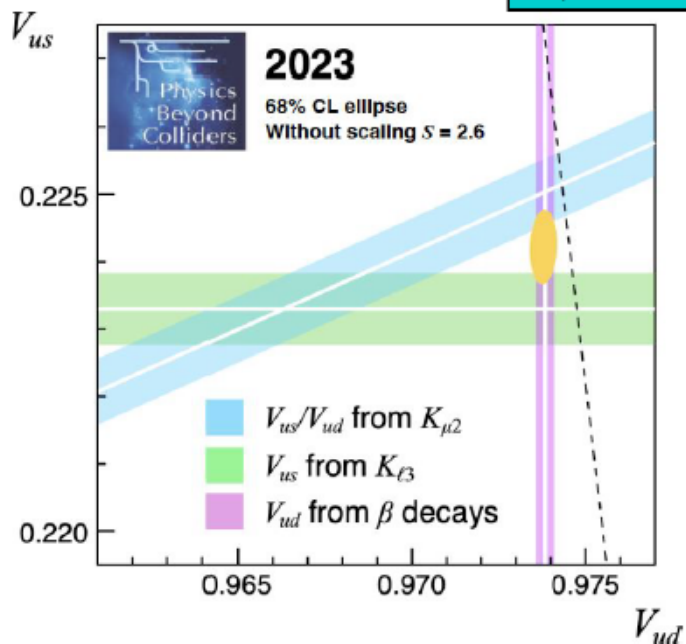
Summary for V_{us}
from kaon decays
and first-row global fit
(M. Moulson)

$K_{\ell 3}$ $V_{us} = 0.22330(35)_{\text{exp}}(39)_{\text{lat}}(8)_{\text{IB}}$
 $f_+(0) = 0.9698(17)$ $(53)_{\text{tot}} = 0.24\%$
 $N_f = 2+1+1$

$K_{\mu 2}$ $V_{us}/V_{ud} = 0.23108(23)_{\text{exp}}(42)_{\text{lat}}(16)_{\text{IB}}$
 $f_K/f_\pi = 1.1978(22)$ $(51)_{\text{tot}} = 0.22\%$
 $N_f = 2+1+1$

Fit results:

$V_{ud} = 0.97378(26)$
 $V_{us} = 0.22422(36)$
 $\chi^2/\text{ndf} = 6.4/2$ (4.1%)
 $\Delta_{\text{CKM}} = -0.0018(6)$
 -2.8σ



Prospects for V_{us} from kaon decays :

- New measurement of $K_{\mu 3}/K_{\mu 2}$ at NA62
- Precision measurements at proposed HIKE High Intensity Kaon Experiments:
 - Phase I, K^+ beam
 - Phase II, K_L beam

See e.g. [HIKE by A. Romano](#)

But HIKE has been cancelled last winter

Paths to V_{ud} and V_{us}

- From kaon, pion, baryon and nuclear decays

V_{ud}	$0^+ \rightarrow 0^+$ $\pi^\pm \rightarrow \pi^0 e \nu_e$	$n \rightarrow p e \nu_e$	$\pi \rightarrow l \nu_l$
V_{us}	$K \rightarrow \pi l \nu_l$ KI3	$\Lambda \rightarrow p e \nu_e$	$K \rightarrow l \nu_l$ KI2

$$\Gamma_k = (G_F^{(\mu)})^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \delta_{RC}) \times F_{\text{kin}}$$

Channel-dependent
effective CKM element

Hadronic matrix
element

Radiative corrections

- Recent progress on
- 1) Hadronic matrix elements from lattice QCD
 - 2) Radiative corrections from dispersive methods + Lattice QCD

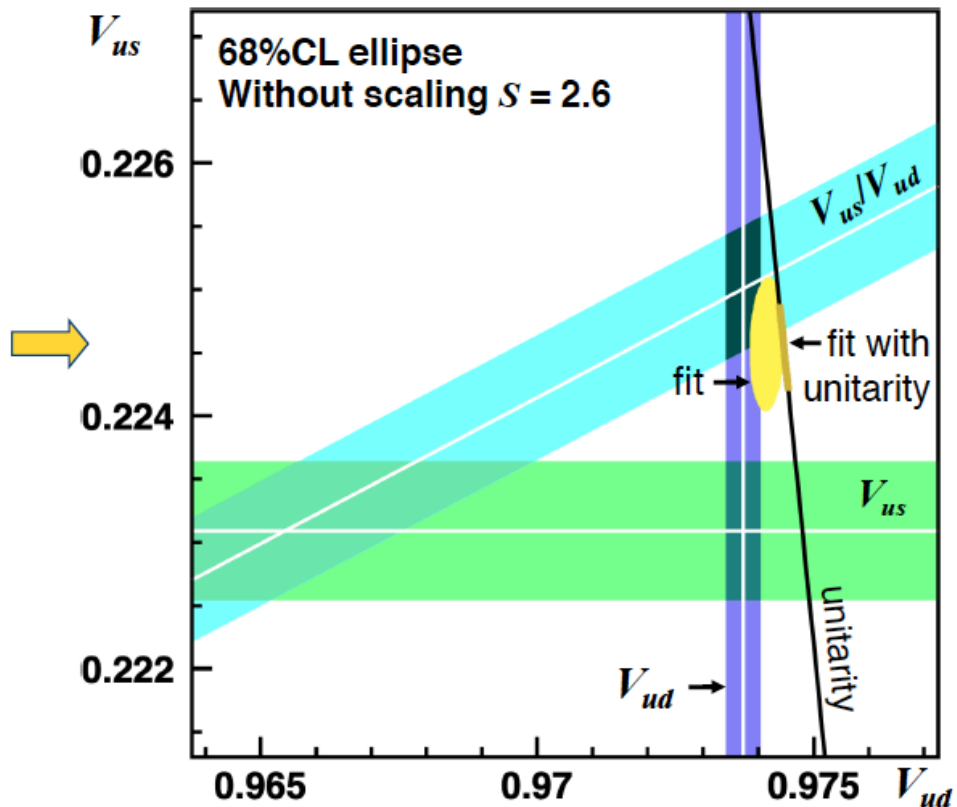
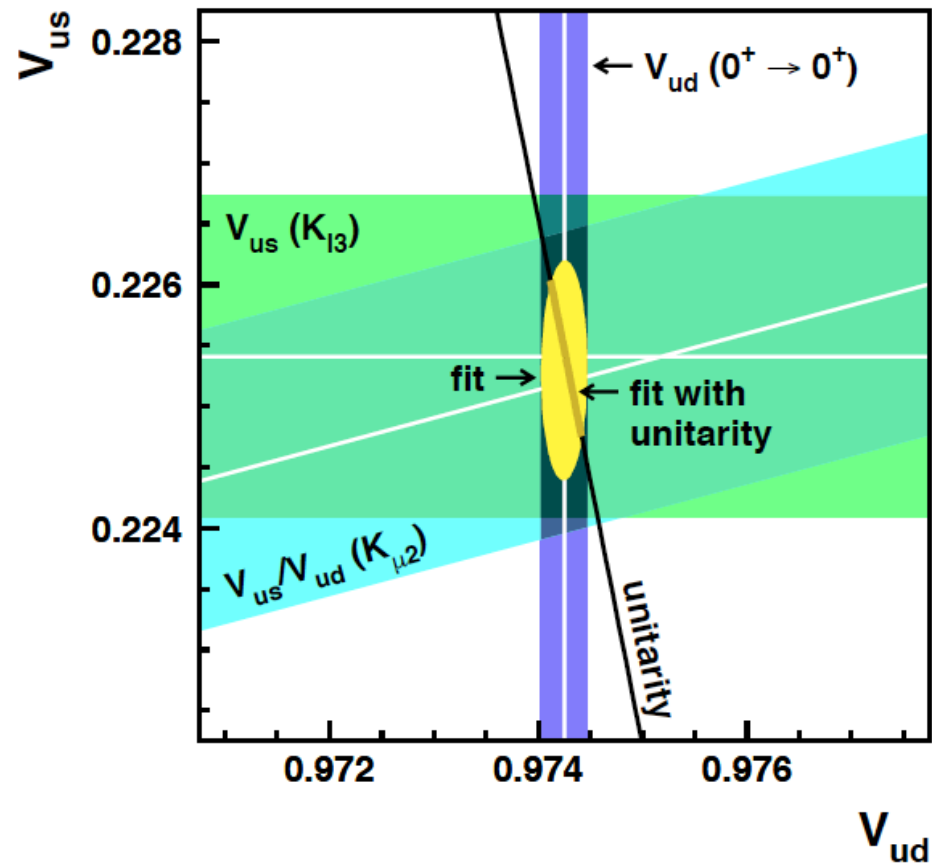
Why this anomaly ?



Changes on V_{us} and V_{ud} over 10 years since 2011

Flavianet Kaon WG: Antonelli et al'11

Moulson & E.P.@CKM2021



Changes on V_{us} and V_{ud} over 10 years since 2011

- Almost no change on the experimental side since 2011

Flavianet Kaon WG: Antonelli et al'11

$$\Gamma_k = (G_F^{(\mu)})^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \delta_{RC}) \times F_{\text{kin}}$$

Channel-dependent
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Hadronic matrix
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Radiative corrections

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Channel-dependent
effective CKM element

Hadronic matrix
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Radiative corrections

- Changes in *theoretical* inputs:
 - Impressive progress on hadronic matrix element computations from *lattice QCD* for V_{us} and V_{us}/V_{ud} extraction from Kaon decays

FLAG'21

Changes on V_{us} and V_{ud} over 10 years since 2011

- Almost no change on the experimental side since 2011

Flavianet Kaon WG: Antonelli et al'11

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Channel-dependent
effective CKM element

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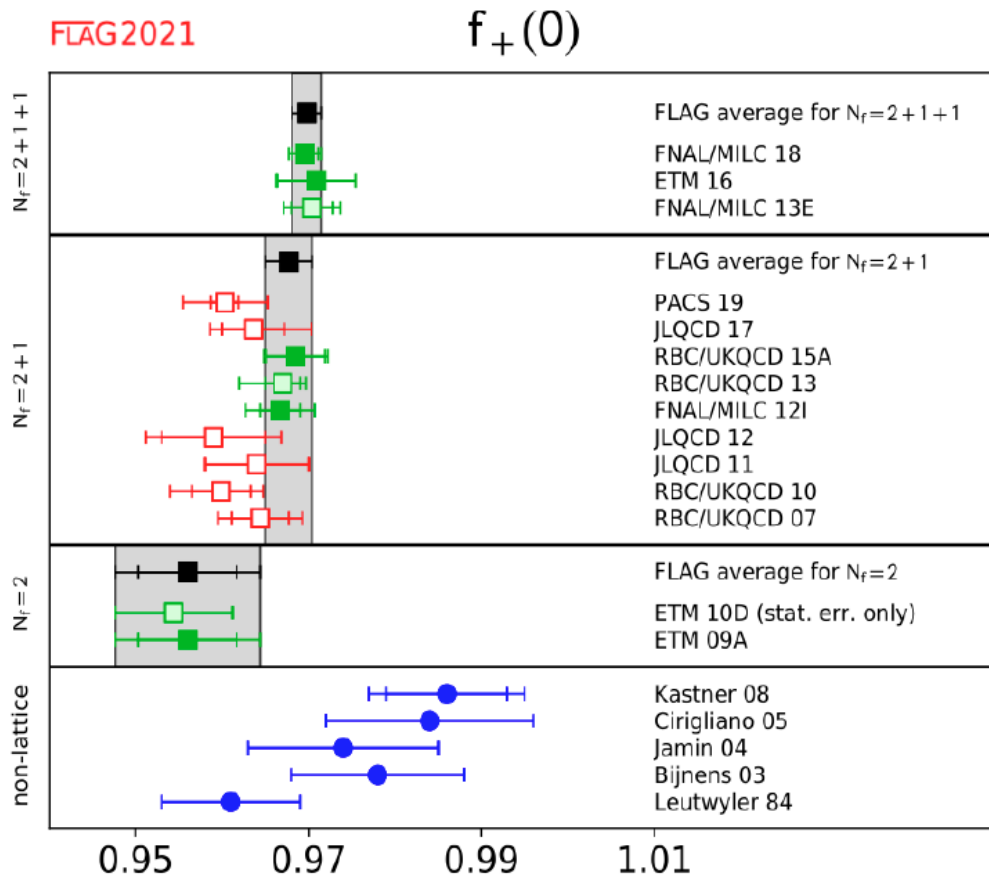
Radiative corrections

- Changes in *theoretical* inputs:
 - Impressive progress on hadronic matrix element computations from lattice QCD for V_{us} and V_{us}/V_{ud} extraction from Kaon decays
 - Radiative corrections from *dispersive methods* for V_{ud} extraction

Seng et al.'18'19, Gorshteyn'18, Cirigliano et al.'22,'24

$f_+(0)$ from Lattice QCD

- Recent progress on Lattice QCD for determining $f_+(0)$



$$f_+(0)_{N_f=2+1+1}^{FLAG21} = 0.9698(17)$$

0.18% uncertainty

to be compared to

$$f_+(0)_{N_f=2+1+1}^{FLAG16} = 0.9704(32)$$

$$f_+(0)_{N_f=2+1}^{2010} = 0.959(50)$$

Uncertainty divided by ~ 2 w/ 2016 and by 25 w/ 2011!

→ Lattice uncertainties at the **same level** as exp.

-3.2 σ away from unitarity!

$$2011: V_{us} = 0.2254(5)_{\text{exp}}(11)_{\text{lat}} \rightarrow V_{us} = 0.2231(4)_{\text{exp}}(4)_{\text{lat}}$$

V_{us} / V_{ud} from K_{l2} / π_{l2}

$$\frac{|V_{us}|}{|V_{ud}|} \frac{f_K}{f_\pi} = \left(\frac{\Gamma_{K_{\mu 2}(\gamma)} m_{\pi^\pm}}{\Gamma_{\pi_{\mu 2}(\gamma)} m_{K^\pm}} \right)^{1/2} \frac{1 - m_\mu^2 / m_{\pi^\pm}^2}{1 - m_\mu^2 / m_{K^\pm}^2} \left(1 - \frac{1}{2} \delta_{EM} - \frac{1}{2} \delta_{SU(2)} \right)$$

- Recent progress on radiative corrections computed on lattice:

Di Carlo et al.'19

- Main input hadronic input: f_K/f_π
- In 2011: $V_{us}/V_{ud} = 0.2312(4)_{\text{exp}}(12)_{\text{lat}}$
- In 2021: $V_{us}/V_{ud} = 0.2311(3)_{\text{exp}}(4)_{\text{lat}}$ the lattice error is reducing by a factor of 3 compared to 2011! It is now of the same order as the experimental uncertainty.

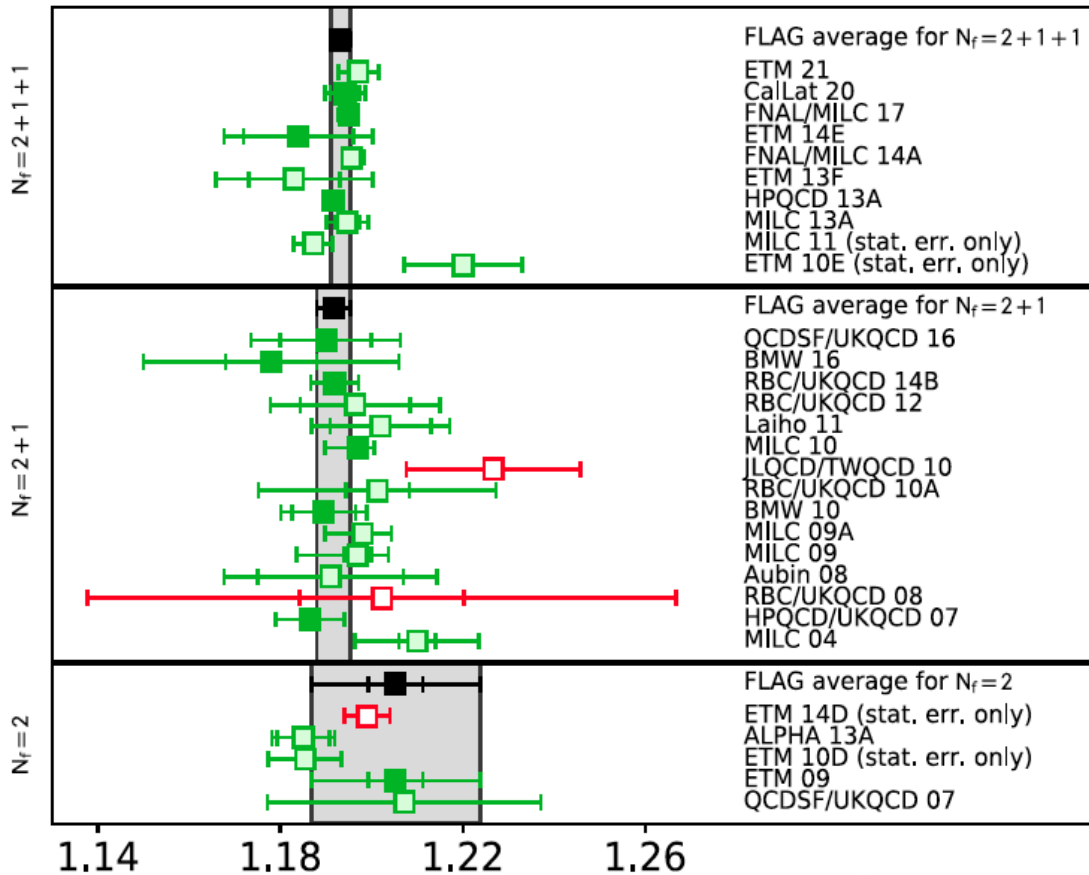
-1.8 σ away from unitarity

f_K/f_π from LQCD

Progress since 2018: \rightarrow new results from *ETM'21* and *CalLat'20*

FLAG2021

f_{K^\pm}/f_{π^\pm}



Now Lattice collaborations include SU(2) IB corr.
For $N_f=2+1+1$, FLAG2021

$$f_{K^+}/f_{\pi^+} = 1.1932(21)$$

0.18% uncertainty

Results have been stable over the years

For average subtract IB corr.

$$f_K/f_\pi = 1.1967(18)$$

In 2011: $f_K/f_\pi = 1.193(6)$

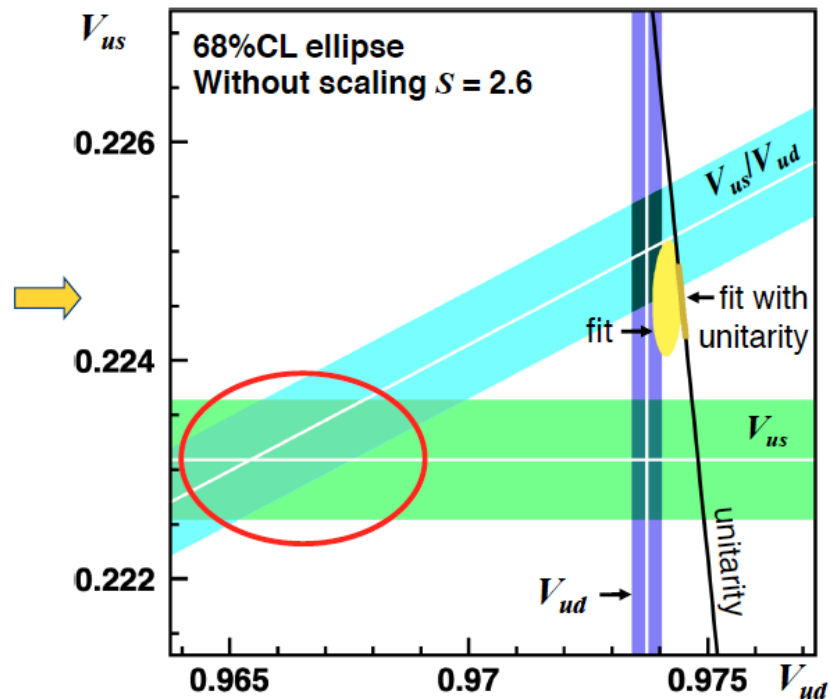
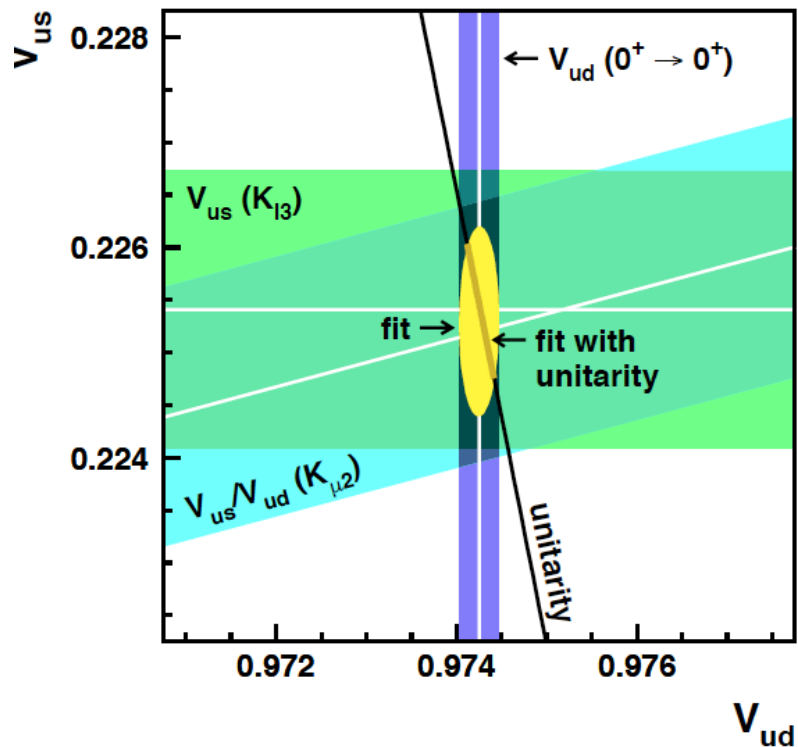
$\rightarrow V_{us}/V_{ud} = 0.23108(29)_{\text{exp}}(42)_{\text{lat}}$

Emilie Passemar

Changes on V_{us} and V_{ud} over 10 years since 2011

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Moulson & E.P.@CKM2021

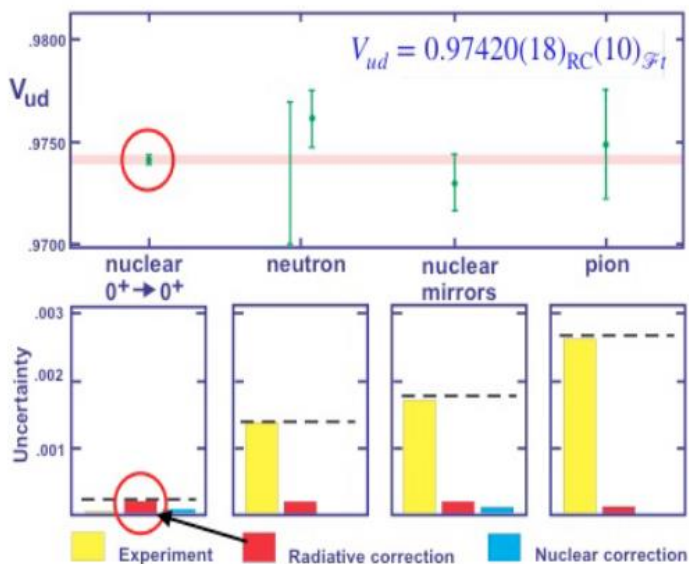


V_{ud} from $0^+ \rightarrow 0^+$ super-allowed β decays

See Talk by Misha Gorshteyn @CKM2021

PDG 2018:

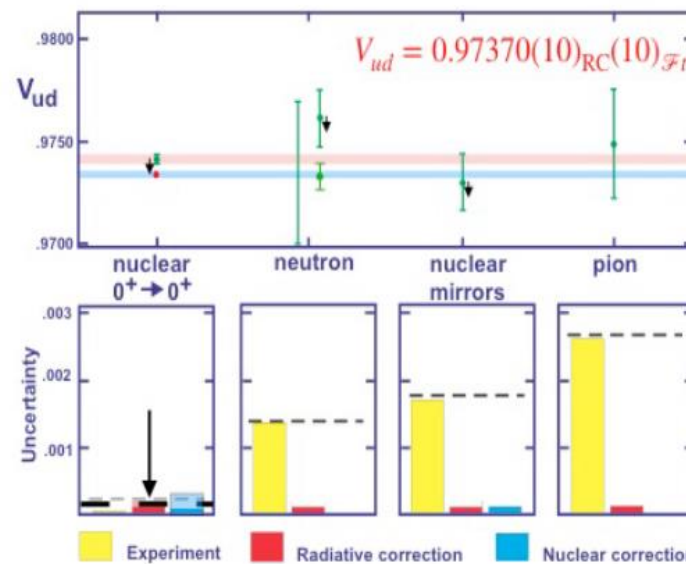
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9994(4)_{V_{ud}}(2)_{V_{us}}$$



PDG 2020:

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9985(3)_{V_{ud}}(4)_{V_{us}}$$

Figure adapted from J. Hardy



Recent improvement on the theoretical RCs + Nuclear Structure Corrections

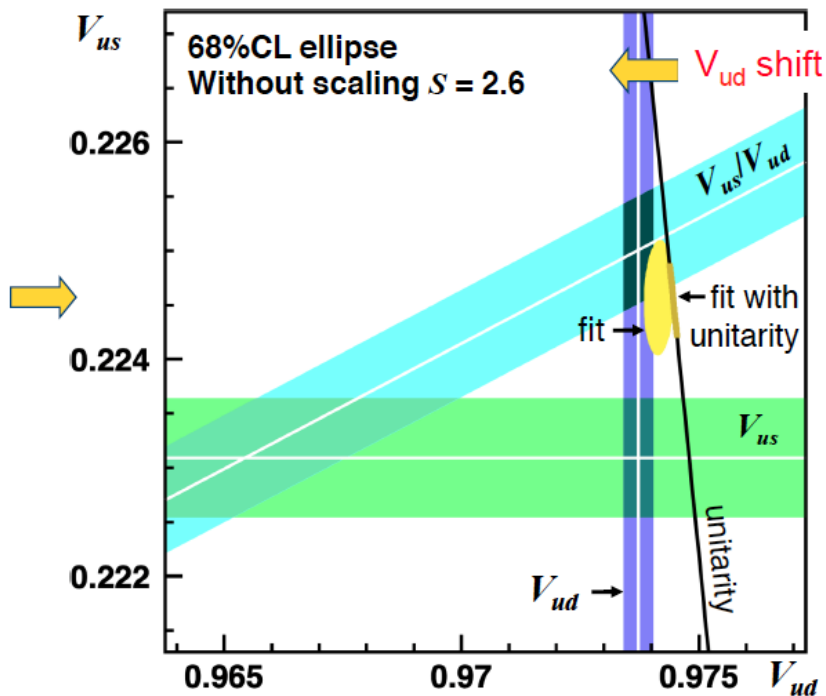
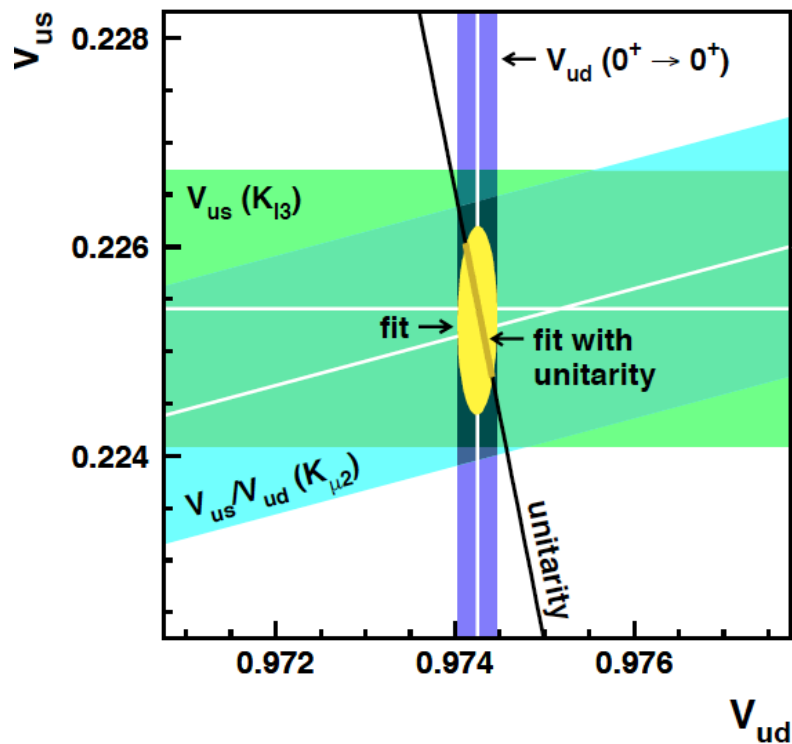
→ Use of a data driven dispersive approach

Seng et al.'18'19, Gorshteyn'18

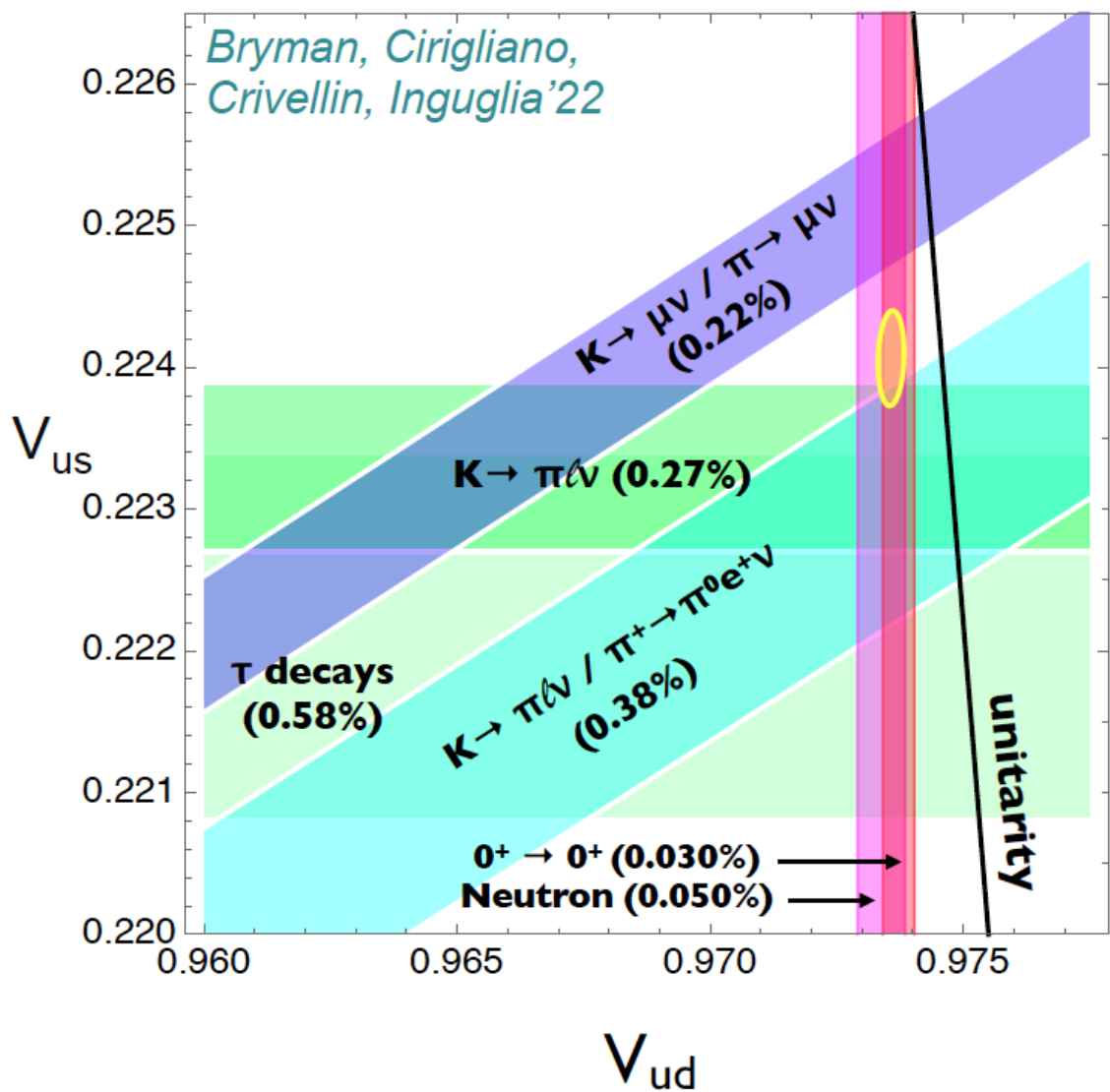
Changes on V_{us} and V_{ud} over 10 years since 2011

Flavianet Kaon WG: Antonelli et al'11

Moulson & E.P.@CKM2021



The Cabibbo anomaly as of about TODAY



$$|V_{ud}| = 0.97373(31)$$

$$|V_{us}| = 0.2231(6)$$

$$|V_{us}|/|V_{ud}| = 0.2311(5)$$

Fit results, no constraint

$$V_{ud} = 0.97365(30)$$

$$V_{us} = 0.22414(37)$$

$$\chi^2/\text{ndf} = 6.6/1 \text{ (1.0\%)}$$

$$\Delta_{\text{CKM}} = -0.0018(6)$$

-2.7 σ

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 + \Delta_{\text{CKM}}$$

Negligible $\sim 2 \times 10^{-5}$
(B decays)

Prospects



Experimental prospects on V_{us}

On Kaon side

Cirigliano et al'22

- *NA62* could measure **several BRs**: $K_{\mu 3}/K_{\mu 2}$, $K \rightarrow 3\pi$, $K_{\mu 2}/K \rightarrow \pi\pi$
- Note that the high precision measurement of $\text{BR}(K_{\mu 2})$ (0.3%) comes only from a single experiment: KLOE. It would be good to have another measurement at the same level of accuracy
- *LHCb* : could measure $\text{BR}(K_S \rightarrow \pi\mu\nu)$ at the $< 1\%$ level?
 $K_S \rightarrow \pi\mu\nu$ measured by KLOE-II but not competitive
 τ_S known to 0.04% (vs 0.41% for τ_L , 0.12% for τ_{\pm})
- V_{us} from Tau decays at *Belle II*:

Belle II with 50 ab^{-1} and $\sim 4.6 \times 10^{10}$ τ pairs will improve V_{us} extraction from τ decays

Inclusive measurement is an opportunity to have a complete independent extraction of V_{us} \Rightarrow not easy as you have to measure many channels



$$|V_{us}| = 0.2184 \pm 0.0018_{\text{exp}} \pm 0.0011_{\text{th}}$$

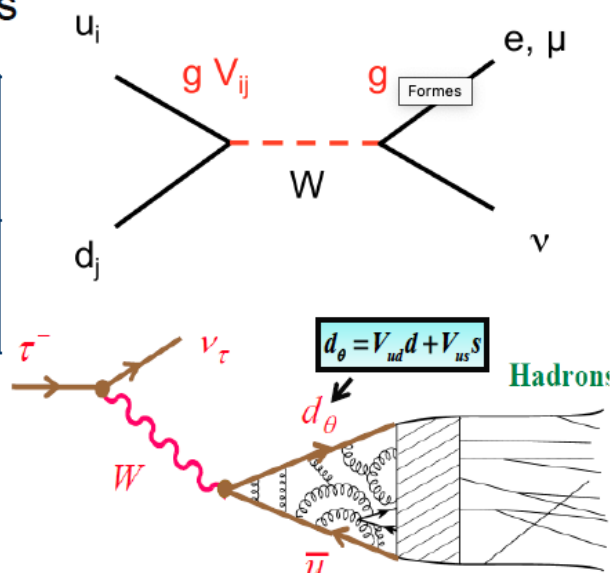
To be competitive theory error will have to be improved as well

HFLAV'21

Can the **TAU** physics help us for **V_{us}** ?

- From kaon, pion, baryon and nuclear decays

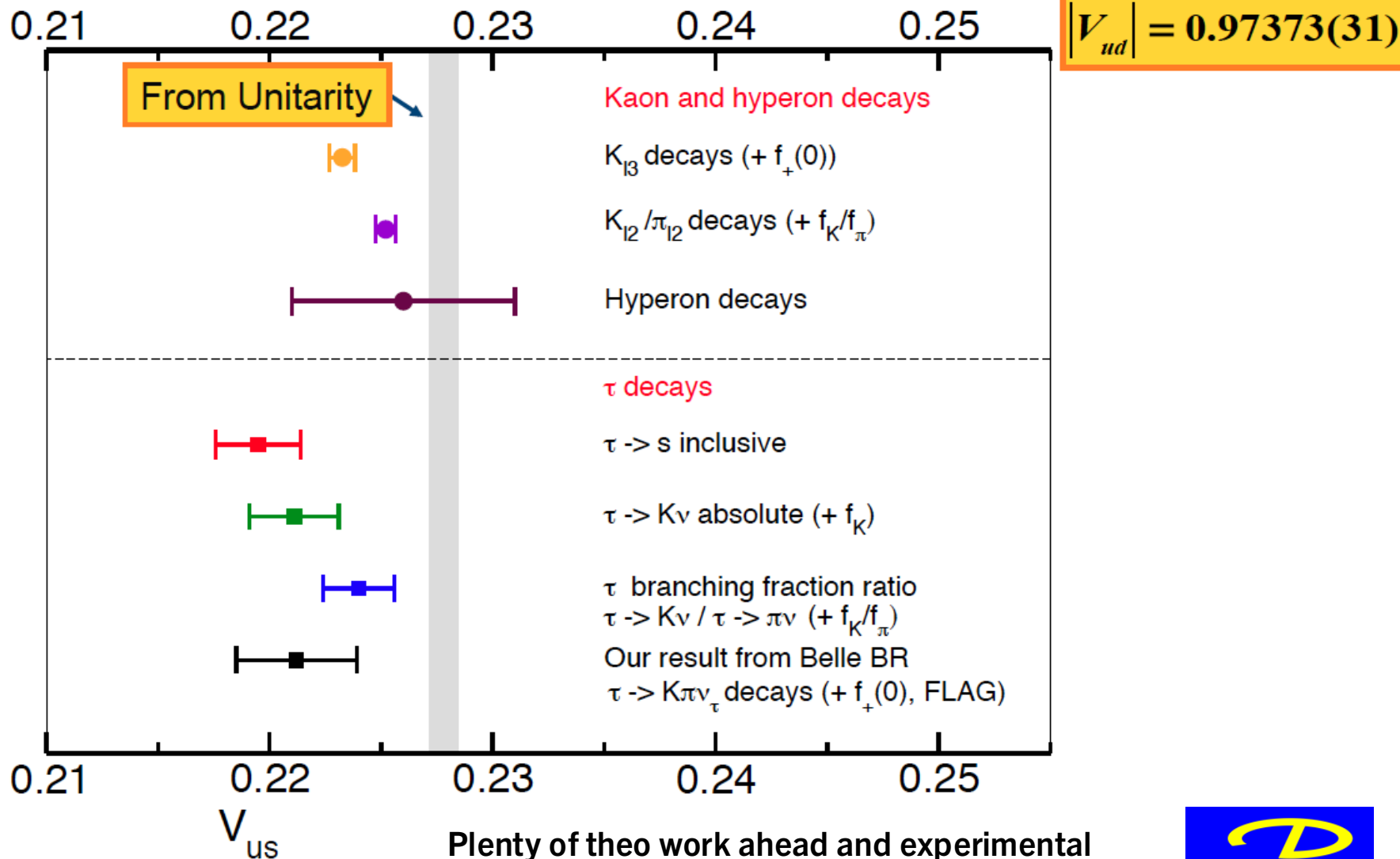
V_{ud}	$0^+ \rightarrow 0^+$ $\pi^\pm \rightarrow \pi^0 e \nu_e$	$n \rightarrow p e \nu_e$	$\pi \rightarrow l \nu_l$
V_{us}	$K \rightarrow \pi l \nu_l$	$\Lambda \rightarrow p e \nu_e$	$K \rightarrow l \nu_l$



- From τ decays (crossed channel)

V_{ud}	$\tau \rightarrow \pi \pi \nu_\tau$	$\tau \rightarrow \pi \nu_\tau$	$\tau \rightarrow h_{NS} \nu_\tau$
V_{us}	$\tau \rightarrow K \pi \nu_\tau$	$\tau \rightarrow K \nu_\tau$	$\tau \rightarrow h_S \nu_\tau$ (inclusive)

Can the **TAU** physics help us for V_{us} ?



Plenty of the work ahead and experimental field is a time for Belle II in Japan (a super tau charm factory in Beijing ?) More at

[E. Passemar Belle II 2024 Oct. Physics Week](#)



V_{us} from hyperon decays

V_{us} can be measured from Hyperon decays:

- $\Lambda \rightarrow p e \nu_e$ Possible measurement at *BESIII, Super τ -Charm factory?*

- Possibilities at *LHCb?*

Talk by Dettori@FPCP20

Channel	\mathcal{R}	ϵ_L	ϵ_D	$\sigma_L(\text{MeV}/c^2)$	$\sigma_D(\text{MeV}/c^2)$	\mathcal{R} = ratio of production ϵ = ratio of efficiencies
$K_S^0 \rightarrow \mu^+ \mu^-$	1	1.0 (1.0)	1.8 (1.8)	~ 3.0	~ 8.0	
$K_S^0 \rightarrow \pi^+ \pi^-$	1	1.1 (0.30)	1.9 (0.91)	~ 2.5	~ 7.0	
$K_S^0 \rightarrow \pi^0 \mu^+ \mu^-$	1	0.93 (0.93)	1.5 (1.5)	~ 35	~ 45	
$K_S^0 \rightarrow \gamma \mu^+ \mu^-$	1	0.85 (0.85)	1.4 (1.4)	~ 60	~ 60	
$K_S^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-$	1	0.37 (0.37)	1.1 (1.1)	~ 1.0	~ 6.0	
$K_L^0 \rightarrow \mu^+ \mu^-$	~ 1	$2.7 (2.7) \times 10^{-3}$	0.014 (0.014)	~ 3.0	~ 7.0	
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	~ 2	$9.0 (0.75) \times 10^{-3}$	$41 (8.6) \times 10^{-3}$	~ 1.0	~ 4.0	
$K^+ \rightarrow \pi^+ \mu^+ \mu^-$	~ 2	$6.3 (2.3) \times 10^{-3}$	0.030 (0.014)	~ 1.5	~ 4.5	
$\Sigma^+ \rightarrow p \mu^+ \mu^-$	~ 0.13	0.28 (0.28)	0.64 (0.64)	~ 1.0	~ 3.0	
$\Lambda \rightarrow p \pi^-$	~ 0.45	0.41 (0.075)	1.3 (0.39)	~ 1.5	~ 5.0	
$\Lambda \rightarrow p \mu^- \bar{\nu}_\mu$	~ 0.45	0.32 (0.31)	0.88 (0.86)	—	—	
$\Xi^- \rightarrow \Lambda \mu^- \bar{\nu}_\mu$	~ 0.04	$39 (5.7) \times 10^{-3}$	0.27 (0.09)	—	—	
$\Xi^- \rightarrow \Sigma^0 \mu^- \bar{\nu}_\mu$	~ 0.03	$24 (4.9) \times 10^{-3}$	0.21 (0.068)	—	—	
$\Xi^- \rightarrow p \pi^- \pi^-$	~ 0.03	0.41(0.05)	0.94 (0.20)	~ 3.0	~ 9.0	
$\Xi^0 \rightarrow p \pi^-$	~ 0.03	1.0 (0.48)	2.0 (1.3)	~ 5.0	~ 10	
$\Omega^- \rightarrow \Lambda \pi^-$	~ 0.001	$95 (6.7) \times 10^{-3}$	0.32 (0.10)	~ 7.0	~ 20	

- To be able to extract V_{us} one needs to compute form factors precisely

➡ Lattice effort from *RBC/UKQCD*

V_{us} from hyperon decay at LHCb ?

[[Phys. Rev. Lett. 114 no. 16, \(2015\)](#)]



[[J. High Energ. Phys. 2019, 48 \(2019\)](#)]

[[J. Phys. Conf. Ser. 1526 012022 \(2020\)](#)]

$$R^{\mu e} = \frac{\Gamma(B_1 \rightarrow B_2 \mu^- \bar{\nu}_\mu)}{\Gamma(B_1 \rightarrow B_2 e^- \bar{\nu}_e)} \quad R_{SM}^{\mu e} = \sqrt{1 - \frac{m_\mu^2}{\Delta^2}} \left(1 - \frac{9 m_\mu^2}{2 \Delta^2} - 4 \frac{m_\mu^4}{\Delta^4} \right) + \frac{15 m_\mu^4}{2 \Delta^4} \operatorname{arctanh} \left(\sqrt{1 - \frac{m_\mu^2}{\Delta^2}} \right) = 0.153 \pm 0.008$$

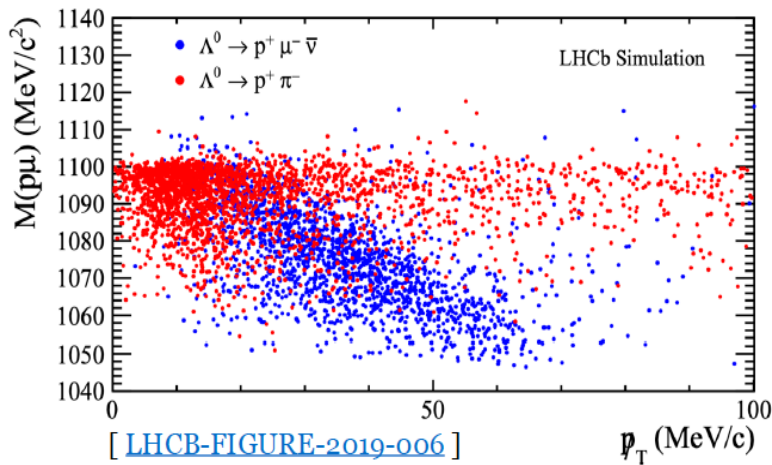
- **Clean theoretical prediction** for the decay rate (going to order δ^2)

$$\Delta = M_1 - M_2 \quad f_1(0) = \text{hyperon vector charge}$$

$$\delta = \frac{M_1 - M_2}{M_1} \quad g_1(0) = \text{hyperon axial charge}$$

- $|V_{us}|$ can be extracted from the BF
- Adding **hyperons** results to the puzzle

$$|V_{us}|^2 \simeq \frac{\Gamma^{SM}(B_1 \rightarrow B_2 \mu^- \bar{\nu}_\mu) 60\pi^3}{R^{\mu e} G_F^2 f_1(0)^2 \Delta^5 \left[\left(1 - \frac{3}{2}\delta\right) + 3 \left(1 - \frac{3}{2}\delta\right) \frac{g_1(0)^2}{f_1(0)^2} \right]}$$



- Best branching ratio measurement from BESIII (2021):
 $\mathcal{B}(\Lambda \rightarrow p \mu^- \bar{\nu}_\mu) = (1.48 \pm 0.21) \times 10^{-4}$ (**14.19 % Uncertainty**)

Dataset: 5.4 fb^{-1} @ $\sqrt{s} = 13 \text{ TeV}$ (Run2), Norm. : $\Lambda \rightarrow p \pi^-$
 44K pre-selected signal events \rightarrow **~1.5 % stat. unc.**
Dominated by systematic uncertainties
 Publication expected **early next year**

$\bar{E}^- \rightarrow \Lambda \mu^- \bar{\nu}_\mu$ proposed as the next natural step

See [A. Brea](#) at the implications of LHCb measurements and future prospects
 CERN, 23–25 October 2024

V_{us} from hyperon decay at LHCb ?

$$\Lambda \rightarrow p \mu^- \bar{\nu}_\mu$$

The main observable for this analysis is the LFU observable $R_{\mu,e}$. V_{us} can also be derived, but we can't compete with the kaon measurements. As it is explained in the slide, we expect a statistical uncertainty around $\sim 1.5\%$ but we also expect to be dominated by systematic uncertainties. I can not provide the final uncertainty of our measurement, but I would say that you can use $\sim 7\%$ (half of the BESIII measurement uncertainty, as an estimate).

I have attached how we are deriving the V_{us} value. The uncertainty from the theoretical part in V_{us}^2 is $26/437$ (see equation 25), so $\sim 6\%$. So, in our final V_{us} result, we may be dominated by theoretical uncertainties. That's why we decided to present this at the implications, because it would be great to see an effort from the theoretical side to try to improve the predictions.

Anyway, If I am not wrong, with the numbers that I provide I think that the final V_{us} extraction from this decay will have $\sim 5\%$ of uncertainty.

See [A. Brea](#) at the implications of LHCb measurements and future prospects
CERN, 23–25 October 2024

Theoretical prospects for V_{us}

- Lattice Progress on hadronic matrix elements: decay constants, FFs
- Full QCD+QED decay rate on the lattice, for **Leptonic decays of kaons and pions** \Rightarrow Inclusion of EM and IB corrections :
 - Perturbative treatment of QED on lattice established
 - Formalism for K_{l2} worked out
- Application of the method for **semileptonic Kaon (K_{l3}) and Baryon decays**
 - \Rightarrow **Aim: Per mille level within 10 years**

Workshop on V_{ud} from pion, neutron and nuclear beta decay

5 nov. 2024, 14:00 → 6 nov. 2024, 13:00 Europe/Paris

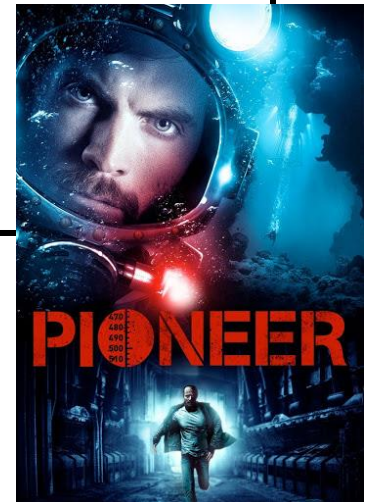
GANIL

Description The workshop will be hosted at the Maison d'Hôtes of [GANIL](#).

The topics to be discussed are:

- Impact of V_{ud} on the search for new physics, CKM fitters viewpoint
- Status and prospects on experimental measurements
 - V_{ud} from pion decay - the PIONEER experiment
 - V_{ud} from neutron decay, half-life and $A\beta$ measurements
 - V_{ud} from nuclear superallowed decays - half life and BR measurements
 - V_{ud} from nuclear mirror decays – half-life, BR & correlation measurements
- V_{ud} theoretical corrections – status and prospects

The workshop is a joint event of the GDR Intensity Frontier and of the GDR RESANET



Some New Physics interpretations



adding **Right-handed** currents to the SM*

Bernard, Oertel, E.P., Stern'08

$$\mathcal{L}_W = \frac{e(1 - \xi^2 \rho_L)}{\sqrt{2}s} \left\{ \bar{N}_L V_{MNS} \gamma^\mu L_L + (1 + \delta) \bar{U}_L V_L \gamma^\mu D_L + \epsilon \bar{U}_R V_R \gamma^\mu D_R \right\} W_\mu^+ + \text{h.c.}$$

- See also *Antonelli et al.'09*
Alioli, Cirigliano, Dekens, de Vries, Mereghetti'17
T. Kitahara@HC2NP 2019

*already advocated a few years ago by [A.Buras, KGemmler & G.Isidori](#) to interpret V_{ub} inclusive vs exclusive discrepancies

adding Right-handed currents to the SM

$$V_{us}^{K_{l3}} = |\sin \theta_C + \epsilon_s| , \quad \leftarrow \text{Vector s quark}$$

$$\left(\frac{V_{us}}{V_{ud}} \right)^{K_{l2}} = \left| \frac{\sin \theta_C - \epsilon_s}{\cos \theta_C - \epsilon_{ns}} \right| \quad \leftarrow \text{Axial}$$

$$V_{ud}^\beta = |\cos \theta_C + \epsilon_{ns}| \quad \leftarrow \text{Vector no s quark}$$

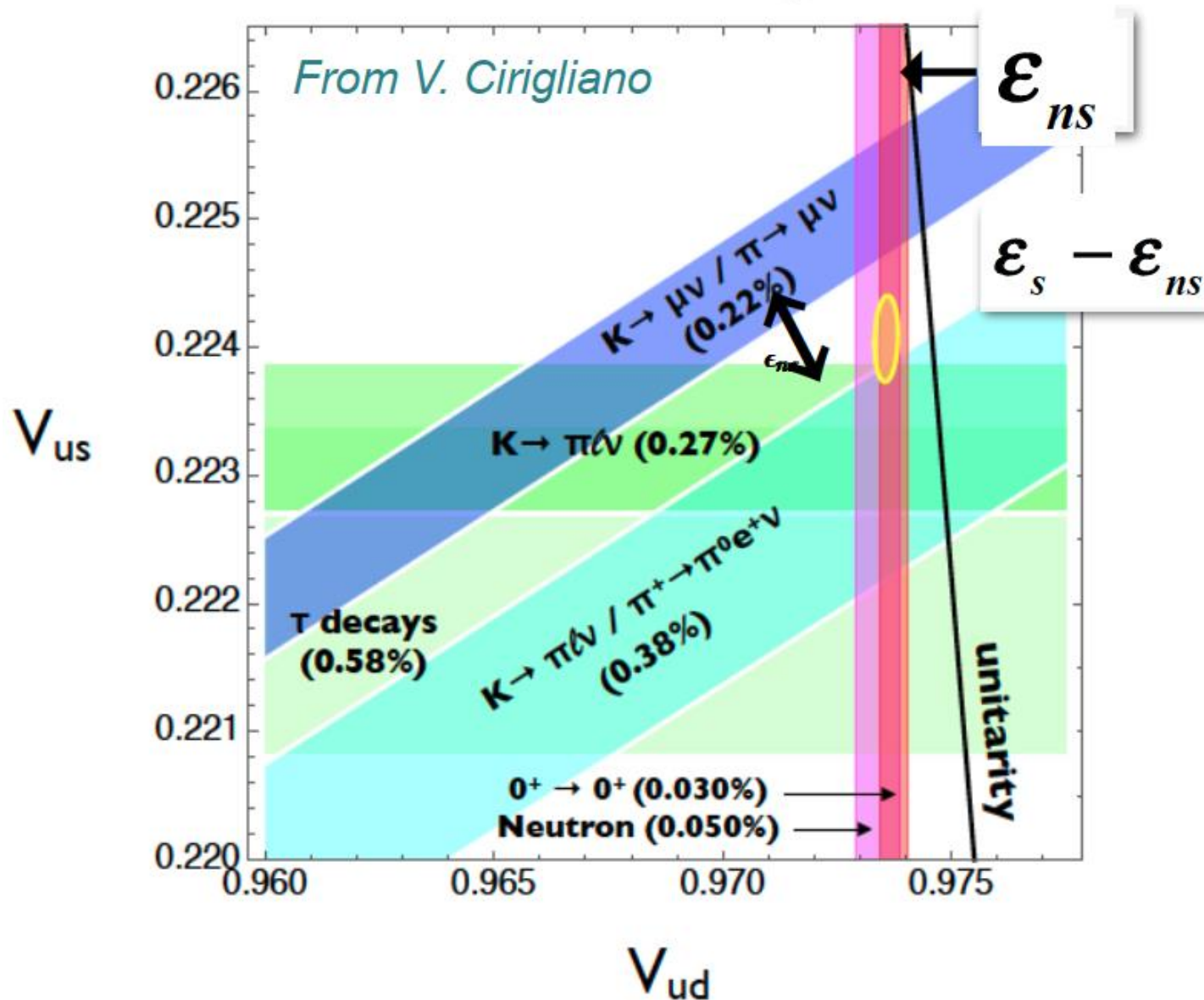
$$\left(\frac{V_{us}}{V_{ud}} \right)^{K_{l3}} = \left| \frac{\sin \theta_C + \epsilon_s}{\cos \theta_C + \epsilon_{ns}} \right| \quad \leftarrow \text{Vector}$$

- The SM is obtained in the limit $\epsilon_s = \epsilon_{ns} = 0$.

- Perfect fit to data $\chi_{\min, \text{RH}}^2 = 0$

- Not obvious how to define CKM unitarity test in this case

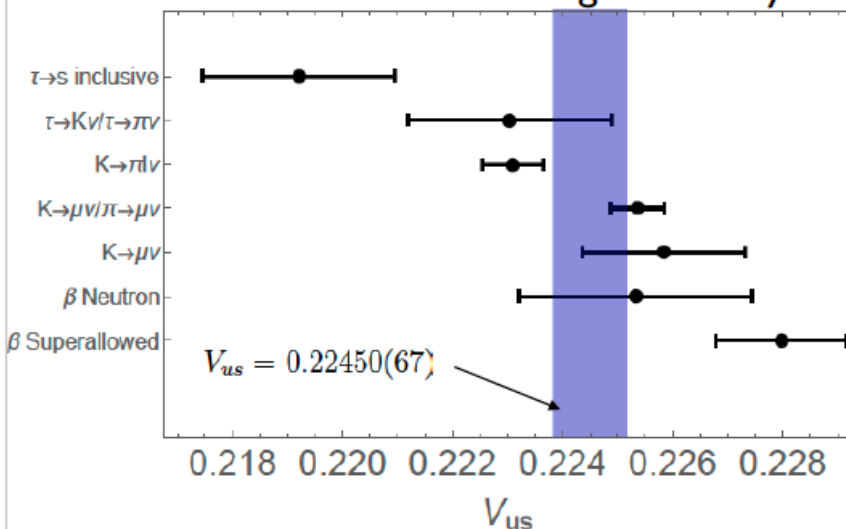
adding Right-handed currents to the SM



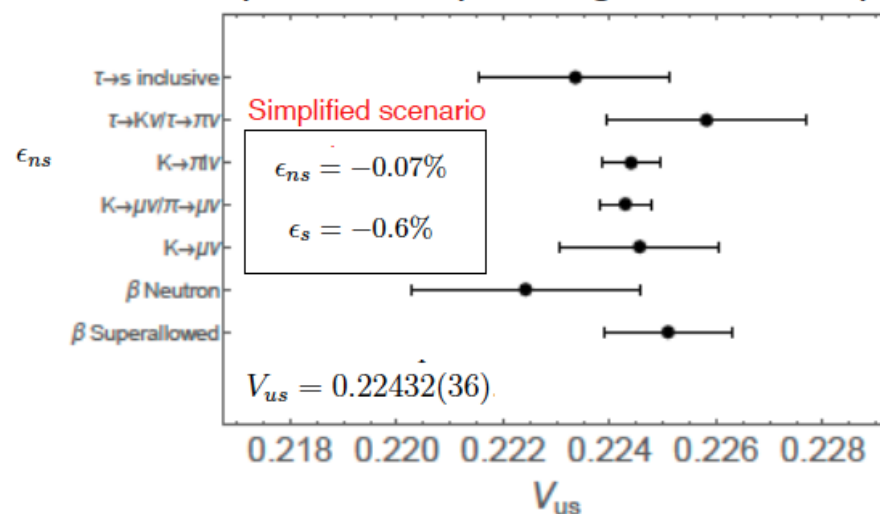
adding Right-handed currents to the SM

- Global fit to CC processes involving light quarks and all lepton families
- SM hypothesis ($\epsilon_s = \epsilon_{ns} = 0$) disfavored (p-value 0.3%)

SM limit: Cabibbo angle anomaly




Anomaly removed by turning on the ϵ_R couplings



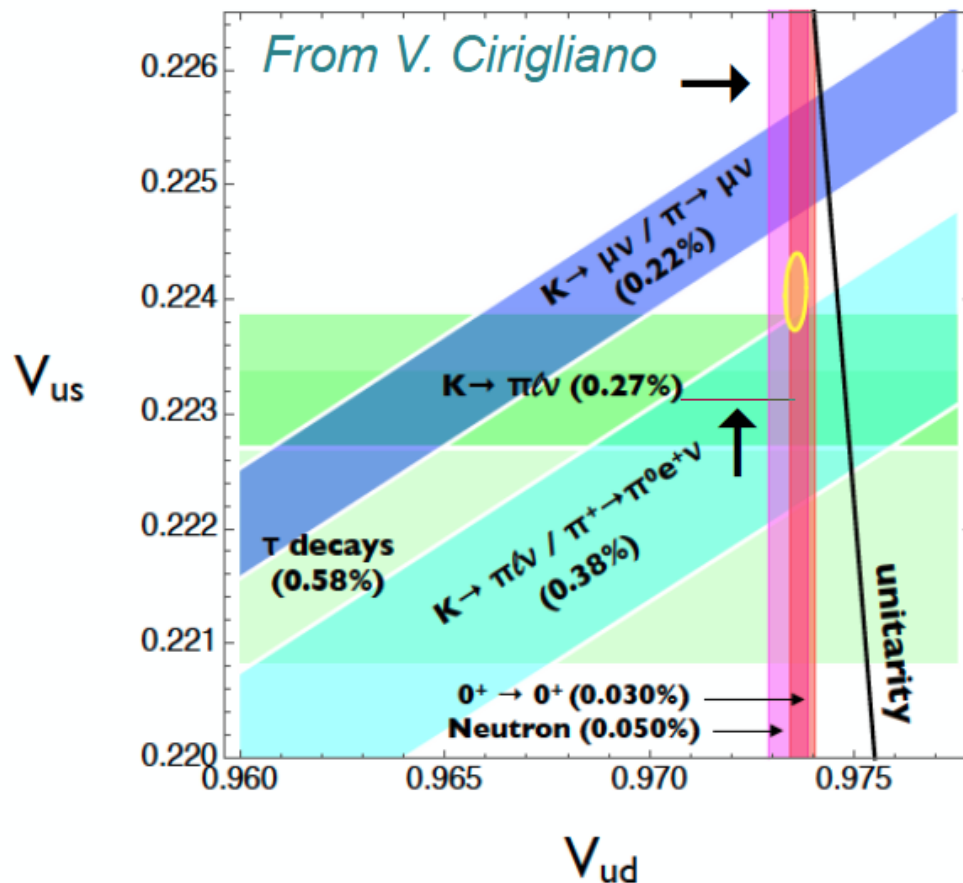
Cirigliano, Diaz-Calderon, Falkowski, Gonzalez-Alonso, Rodriguez-Sanchez'21

Other NP Models on the market

- 4th quark b' *Belfatto, Beradze, Berezhiani'19*
- Gauge horizontal family symmetry
- Turn on only vertex corrections to leptons *Crivellin & Hoferichter'21*


 Shift the location of the V_{ud}, V_{us} bands but do not solve the tension between ratios

And many more....



Other NP Models on the market

- 4th quark b'
- Gauge horizontal family symmetry
- Turn on only vertex corrections to leptons

Belfatto, Beradze, Berezhiani'19

Crivellin & Hoferichter'21

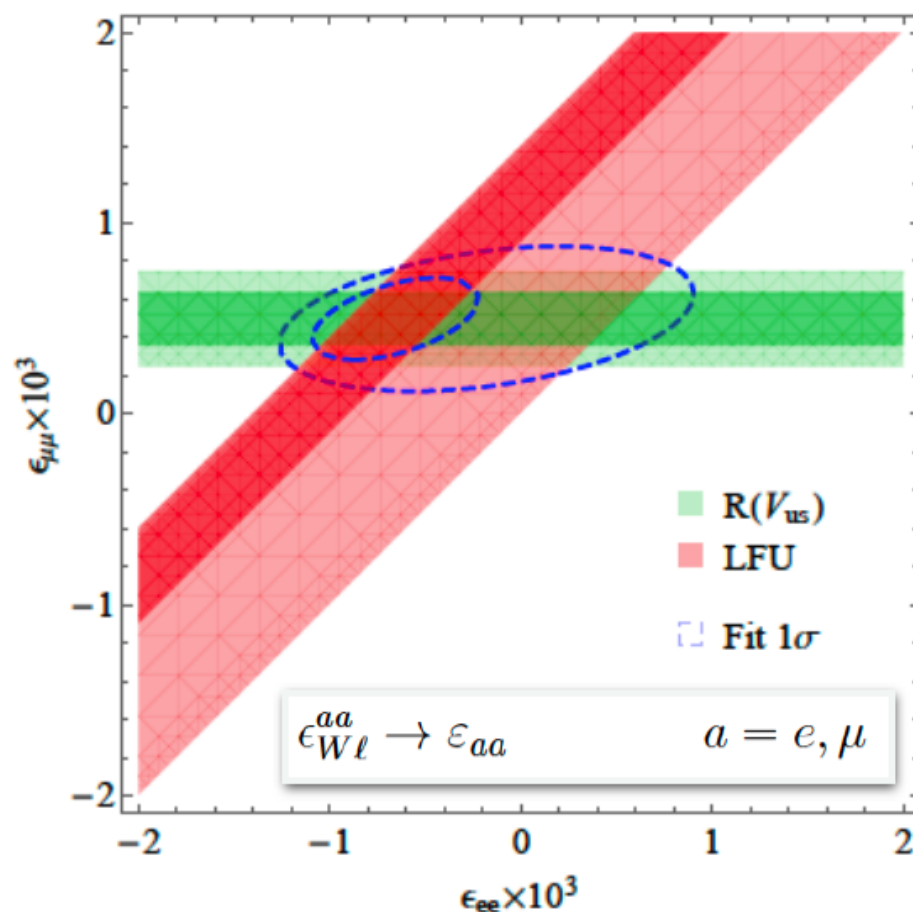
➔ Shift the location of the V_{ud}, V_{us} bands but do not solve the tension between ratios

Connection with $\pi \rightarrow e\nu / \pi \rightarrow \mu\nu$

$$r_\pi = 1 + 2(\epsilon_{Wl}^{ee} - \epsilon_{Wl}^{\mu\mu})$$

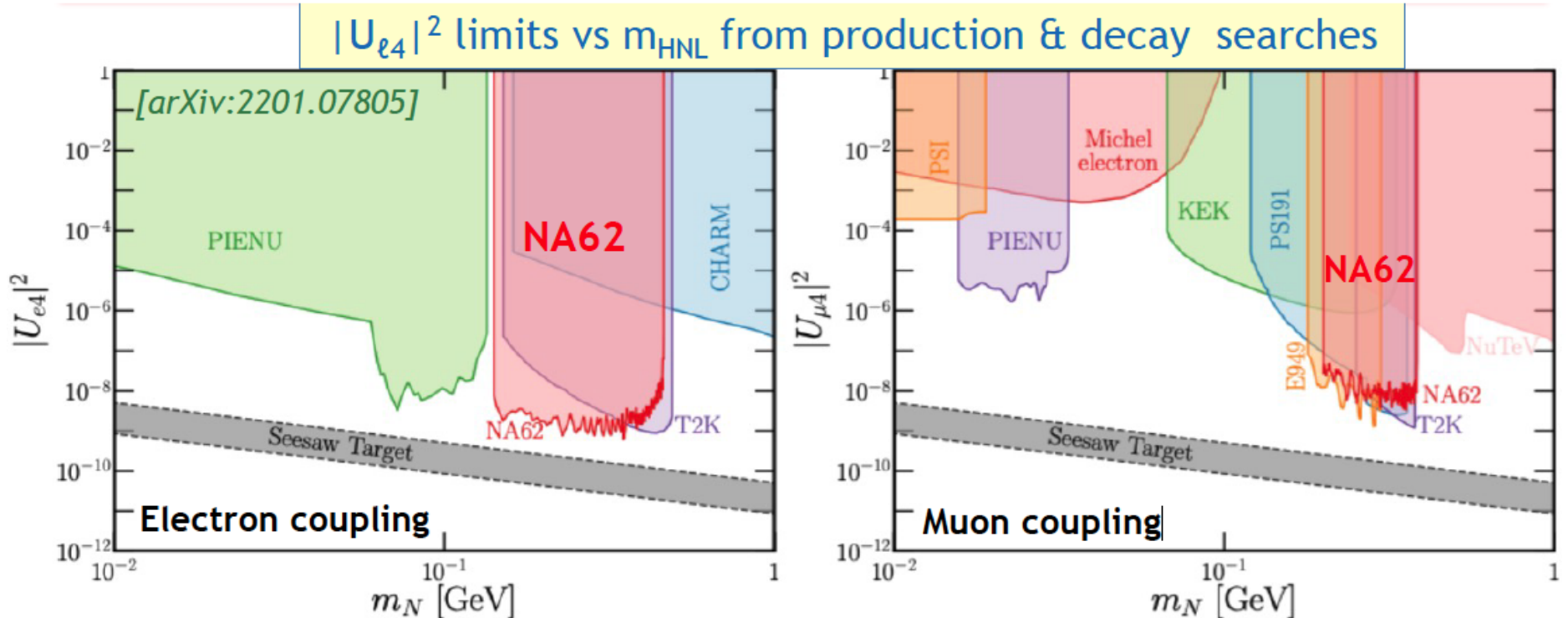
(and other LFU probes)

And many more....



Example: constraints on Heavy Neutral Leptons

Synergy Kaon/pion experiments



- Strongest $|U_{e4}|^2$ limits below **400 MeV**: $K^+, \pi^+ \rightarrow e^+ N$ from *NA62* & *PIENU*.
- Also important limits on $|U_{\mu 4}|^2$ from *E949*, *NA62* and *PIENU*.
- *NA62/E949* limits are complementary to HNL decay searches at T2K.
- Next-generation K^+ and p^+ experiments (*NA62^{++}*, *PIONEER*) to improve by up to factor **10**, reaching the seesaw bound.

For a review see: <https://arxiv.org/pdf/2203.08039>

Conclusion and Outlook

- Recent precision determinations of V_{us} and V_{ud} enable unprecedented tests of the SM and constraints on possible NP models
- Tensions in unitarity of 1st row of CKM matrix have reappeared!
- We need to work hard to understand where they come from:
 - On experimental side:
 - For V_{us} , new measurements in kaons (*NA62: $K_{\mu 3}/K_{\mu 2}$, LHCb?*) but mainly in tau decays from *Belle II*
 - V_{us} from hyperon decays? \Rightarrow *BESSIII, LHCb?*
 - For V_{ud} , understand the situation of the neutron lifetime, beta decay of pion? \Rightarrow *PIONEER* Consider $R_V = \Gamma(K \rightarrow \pi l \nu(\gamma)) / \Gamma(\pi^+ \rightarrow \pi^0 e^+ \nu(\gamma))$
Czarnecki, Marciano, Sirlin'20
 - On theory side:
 - Calculate very precisely radiative corrections, isospin breaking effects and matrix elements
 - Be sure the uncertainties are under control
 - If these tensions are confirmed \Rightarrow what do they tell us?

The first row of the CKM matrix (i.e.: Cabibbo angle even w.o. V_{ub}) contains mysteries motivating measurements/theory work at Intensity Frontier