

Spectrophotometric standardisation of type Ia Supernovae

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JRJC - nov. 2024 - at St-Jacut-de-la-mer

Summary

- Introduction about cosmology with SNe Ia
- Spectro-photometric standardisation methods
- ZTF spectra sample
- Testing standardisation on ZTF
- Conclusion

Type Ia supernovae



SN 1994D in galaxy NGC 4526
Hubble Space Telescope

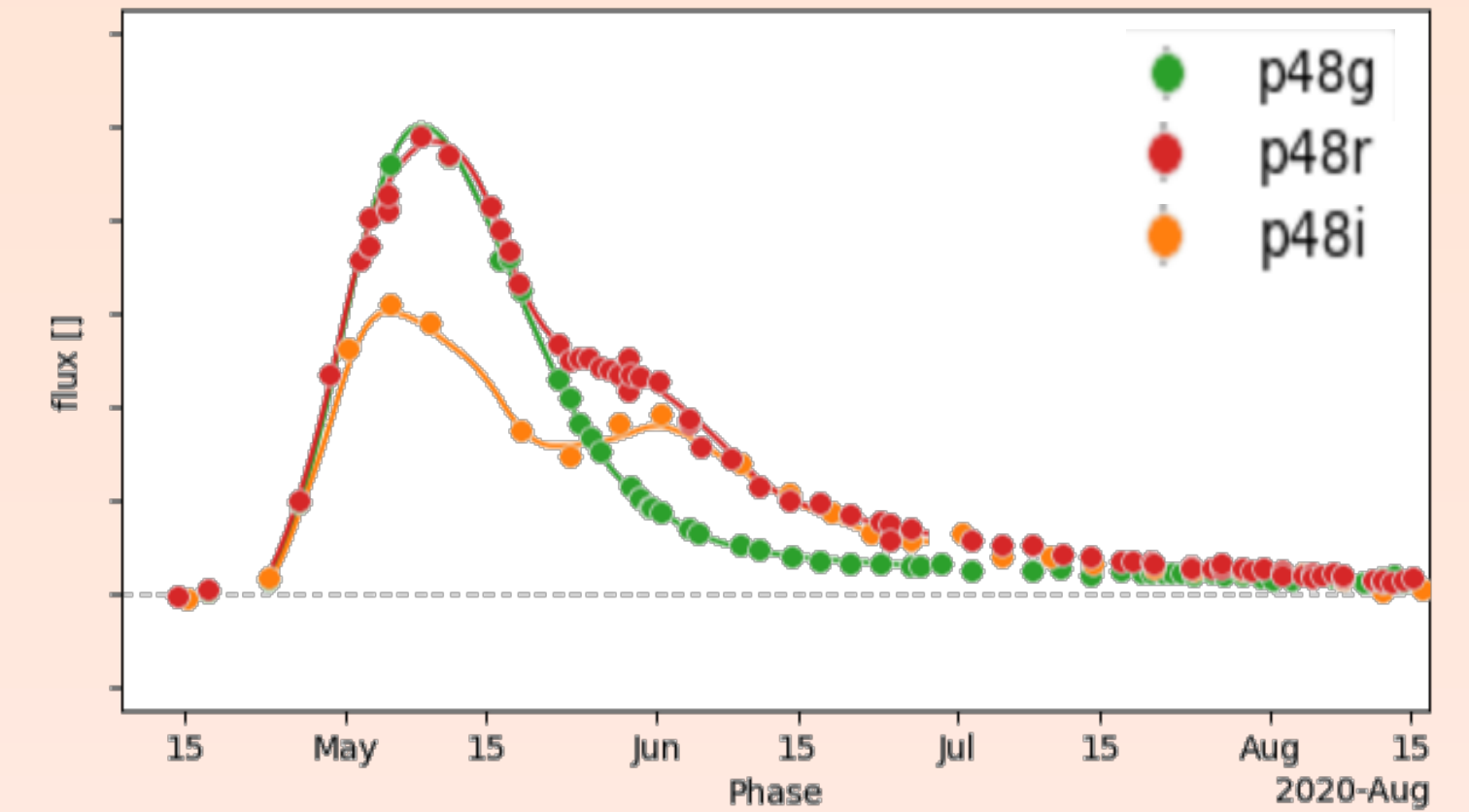
Luminosity \sim constant

Standard candles : $f = \frac{L}{4\pi d_L^2}$

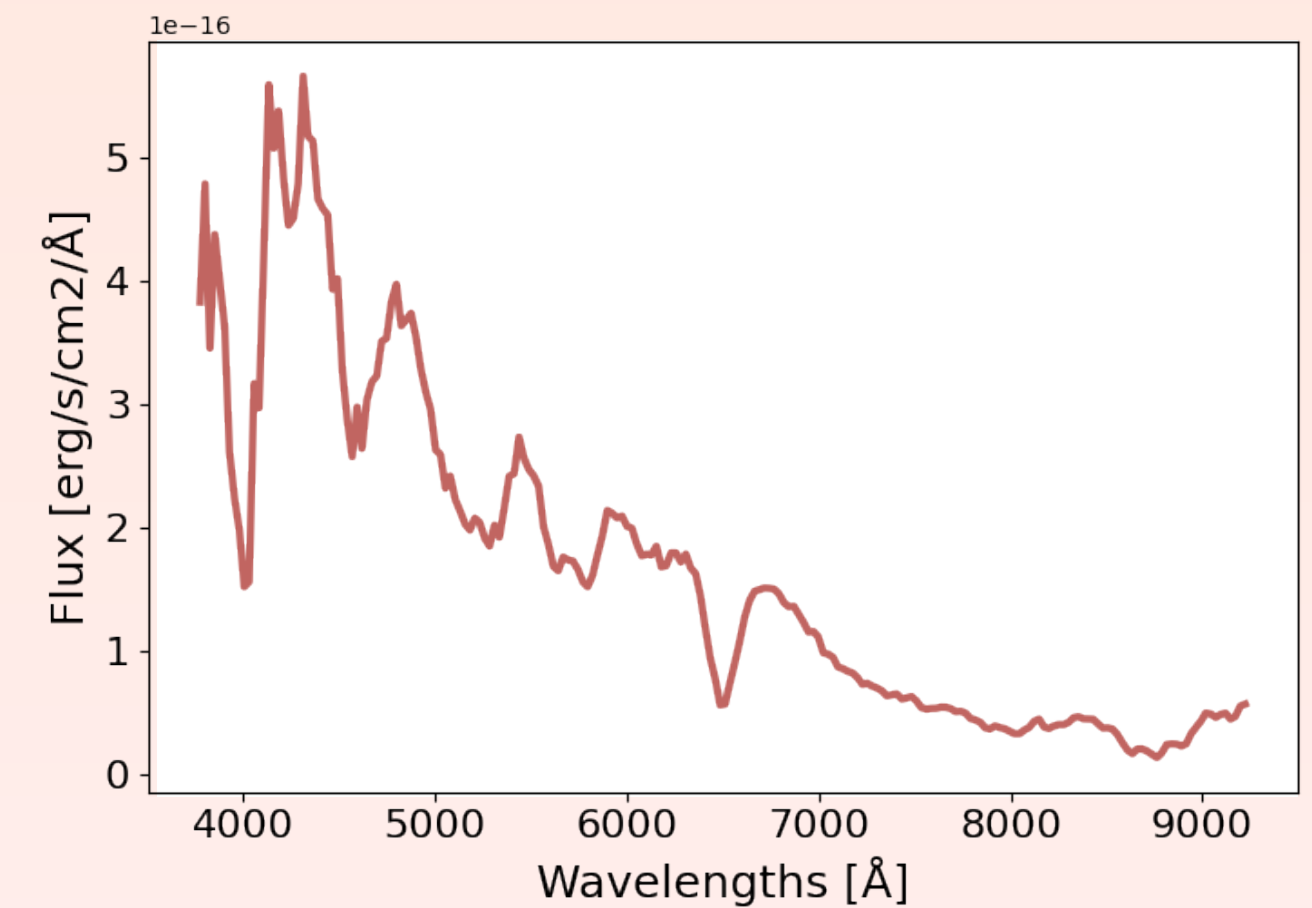
Distance modulus

$$\mu = m_B^{max} - M_B^{max}$$

$$\mu = 5 \log \left(\frac{d_L}{10pc} \right)$$



Lighcurves of ZTF20abxzrqw



Spectra of ZTF20abeqsrn
at phase -5.73

Type Ia supernovae



SN 1994D in galaxy NGC 4526
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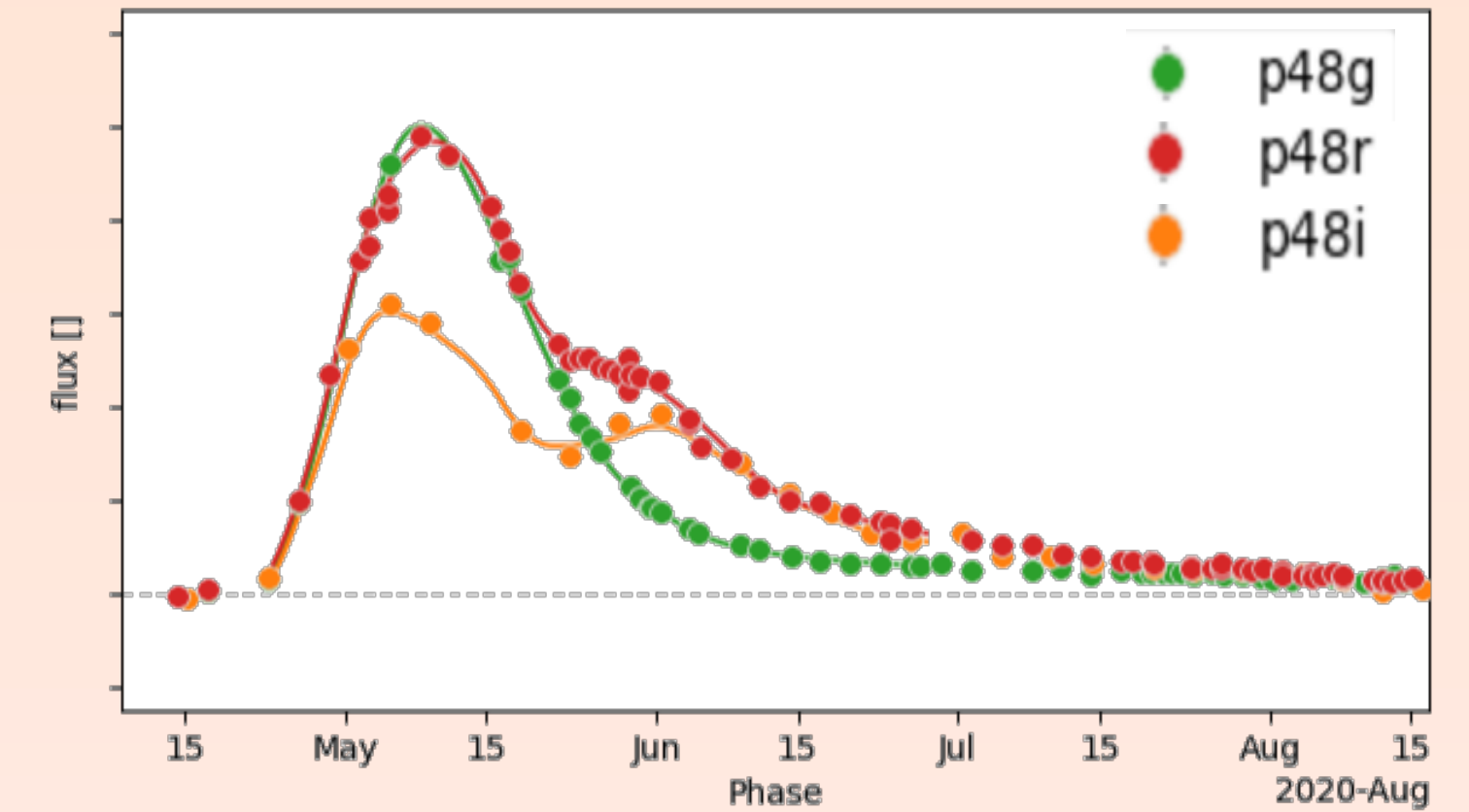
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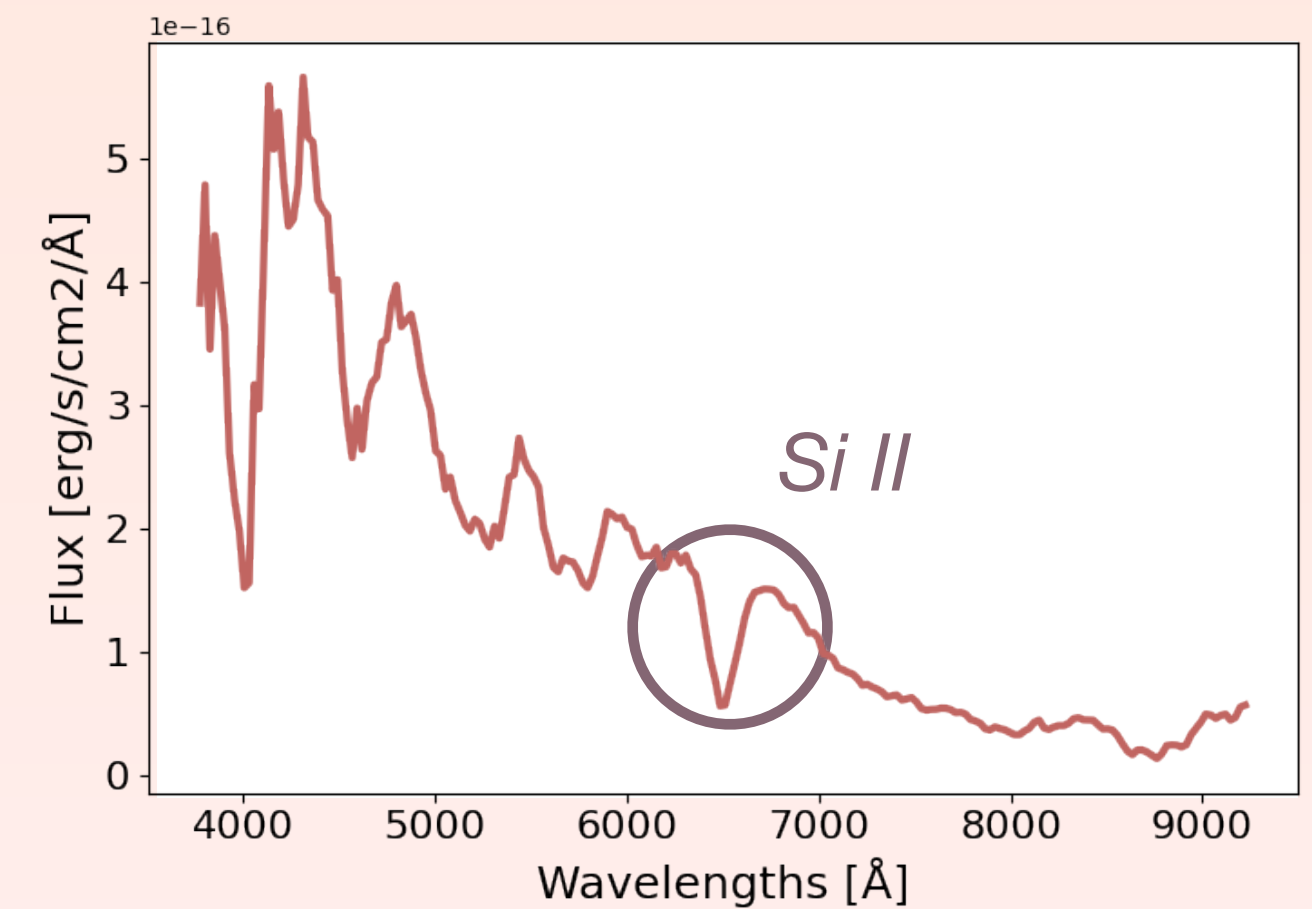
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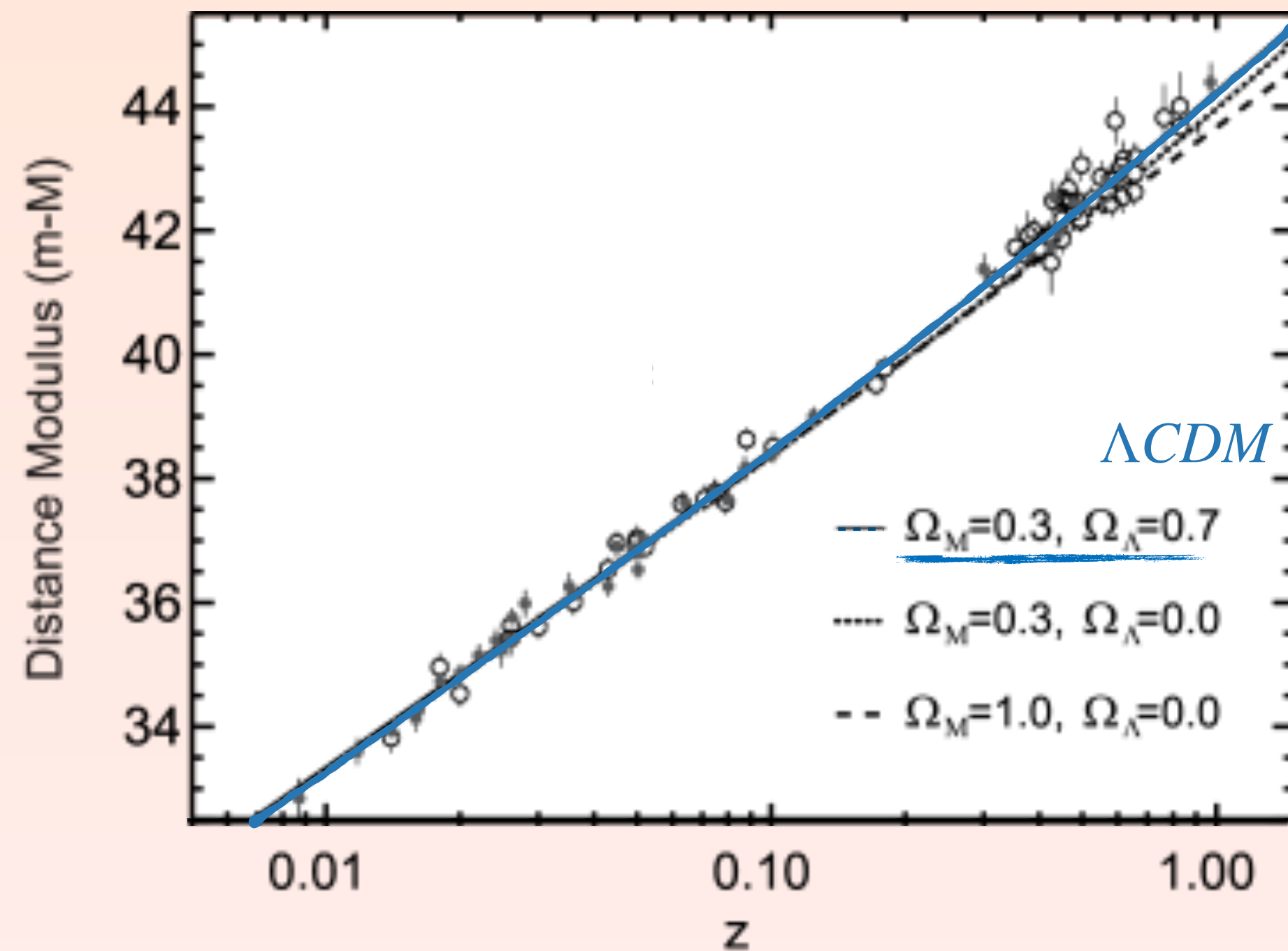


Spectra of ZTF20abeqsrn
at phase -5.73

Goals | *Cosmology*

Distance modulus can be measured on lightcurves

Redshift can be measured on spectrum

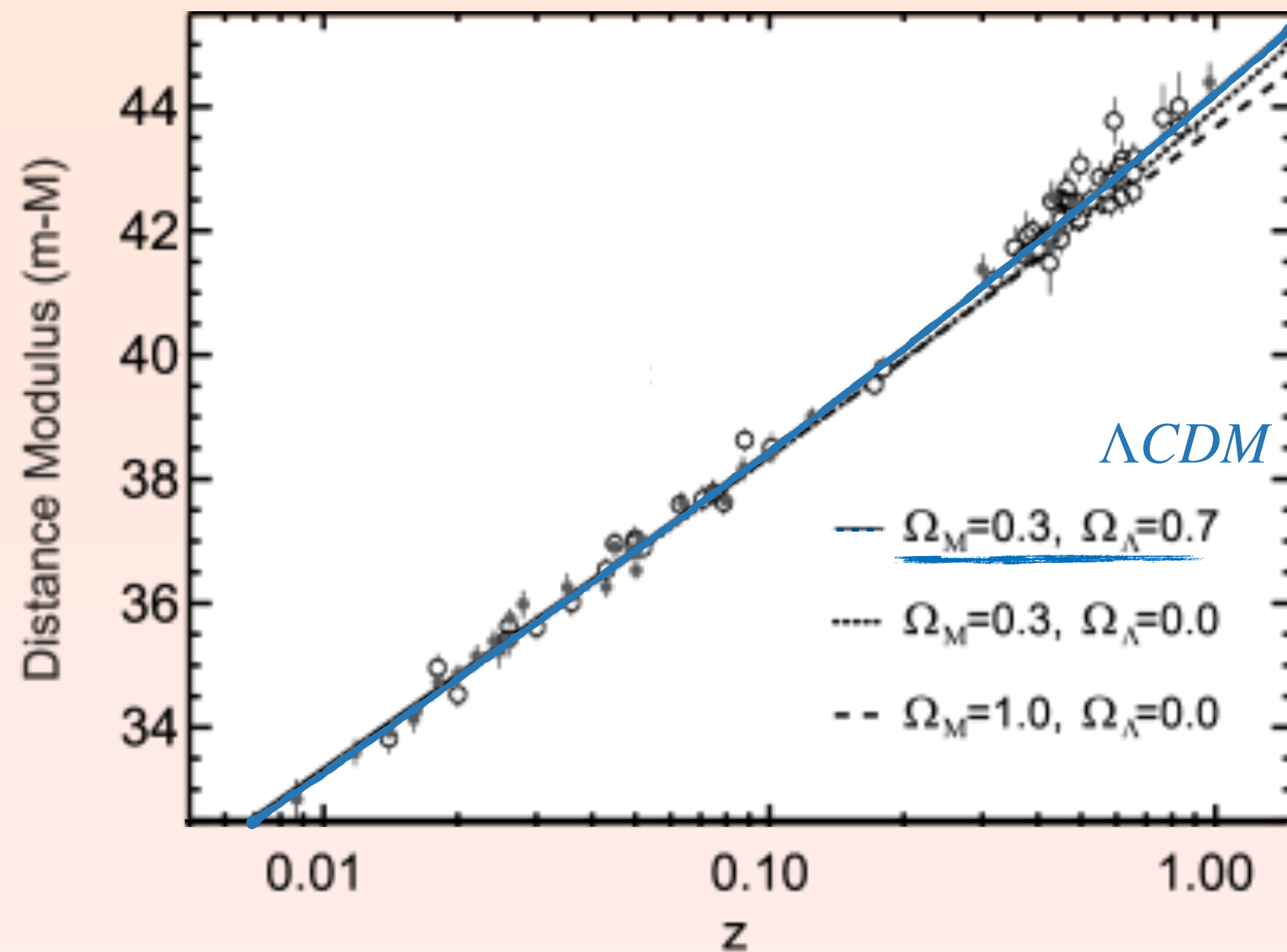


Hubble Diagram - Frieman 2008

Goals | Cosmology

Distance modulus can be measured on lightcurves

Redshift can be measured on spectrum



Hubble Diagram - Frieman 2008

Matter density

Dark Energy density

parameter of the dark energy equation of state

$$H(z) = H_0 \times \sqrt{\Omega_M(1+z)^3 + \Omega_\Lambda(1+z)^{3(1+w)}}$$

Equation of w CDM model

- Flat Universe
- $\Omega_M + \Omega_\Lambda = 1$

Latest Combined result

DESI+CMB+Panth.

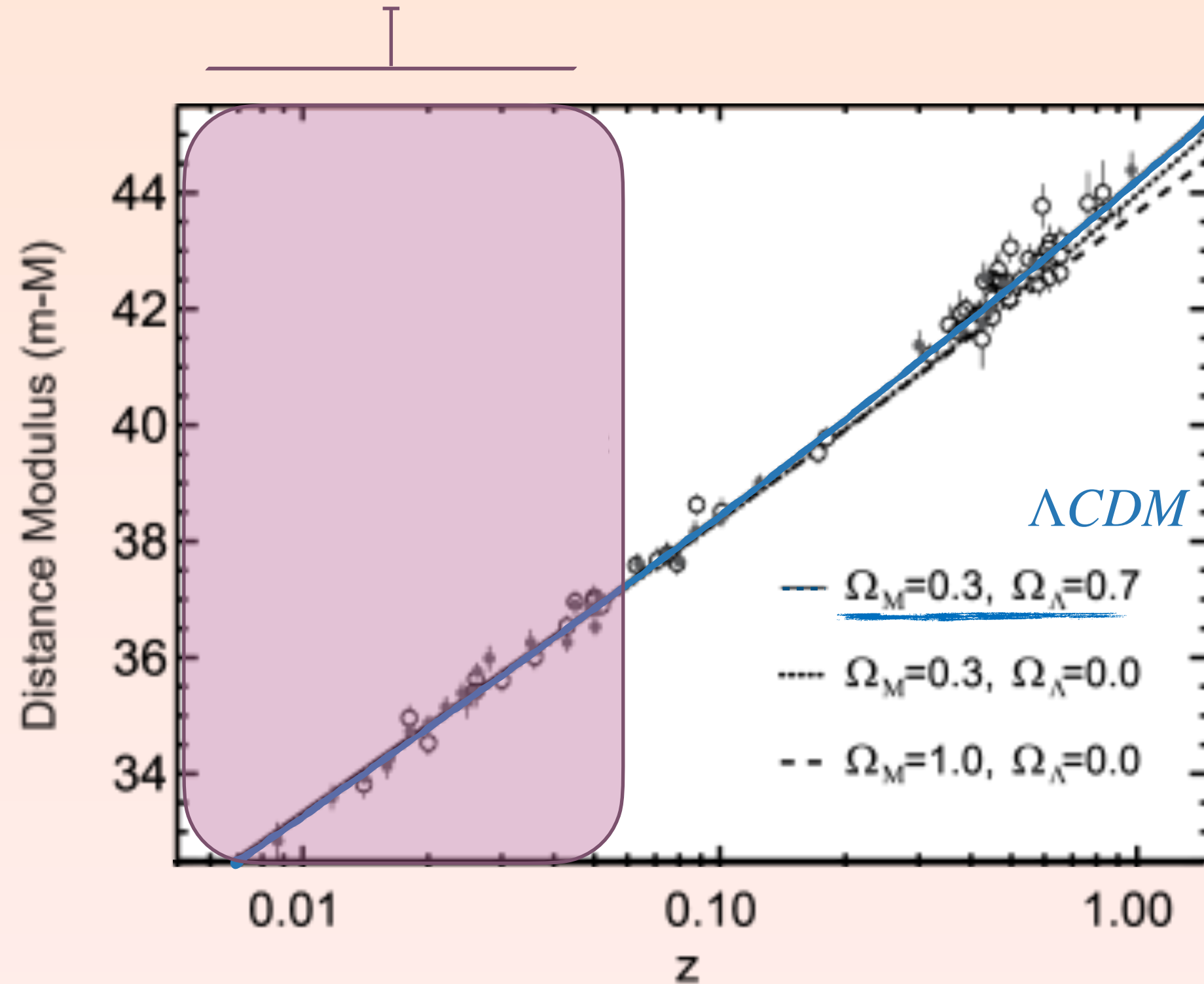
$$H_0 \quad 67.74 \pm 0.71 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

$$\Omega_M \quad 0.3095 \pm 0.0069$$

$$w \quad -0.997 \pm 0.025$$

Goals | Cosmology

Low-redshift ($z < 0.15$)
Constrains H_0



Hubble Diagram - Frieman 2008

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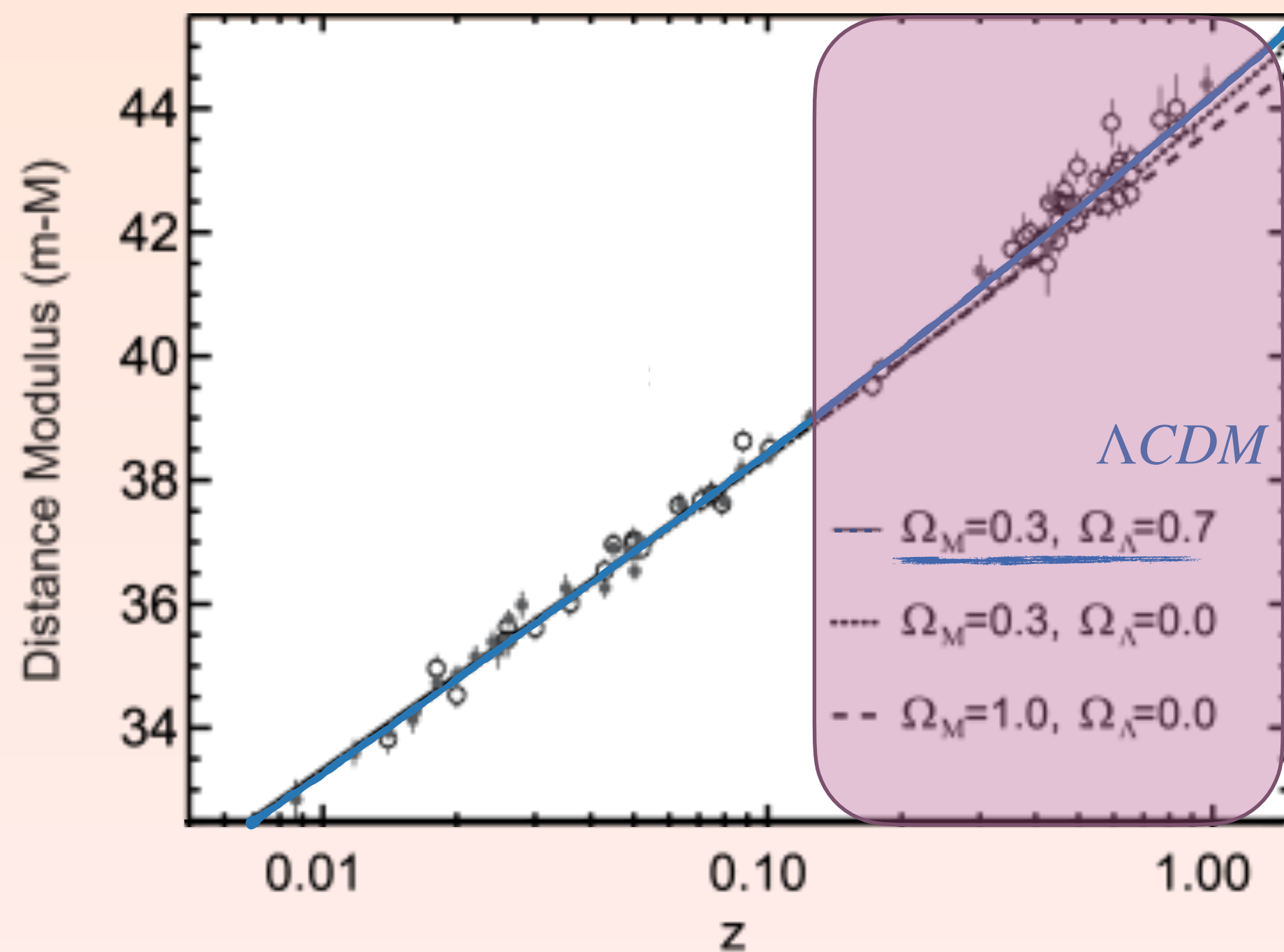
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Goals | Cosmology

High-redshift ($z > 0.15$)
Constrains (Ω_M, Ω_Λ)



Hubble Diagram - Frieman 2008

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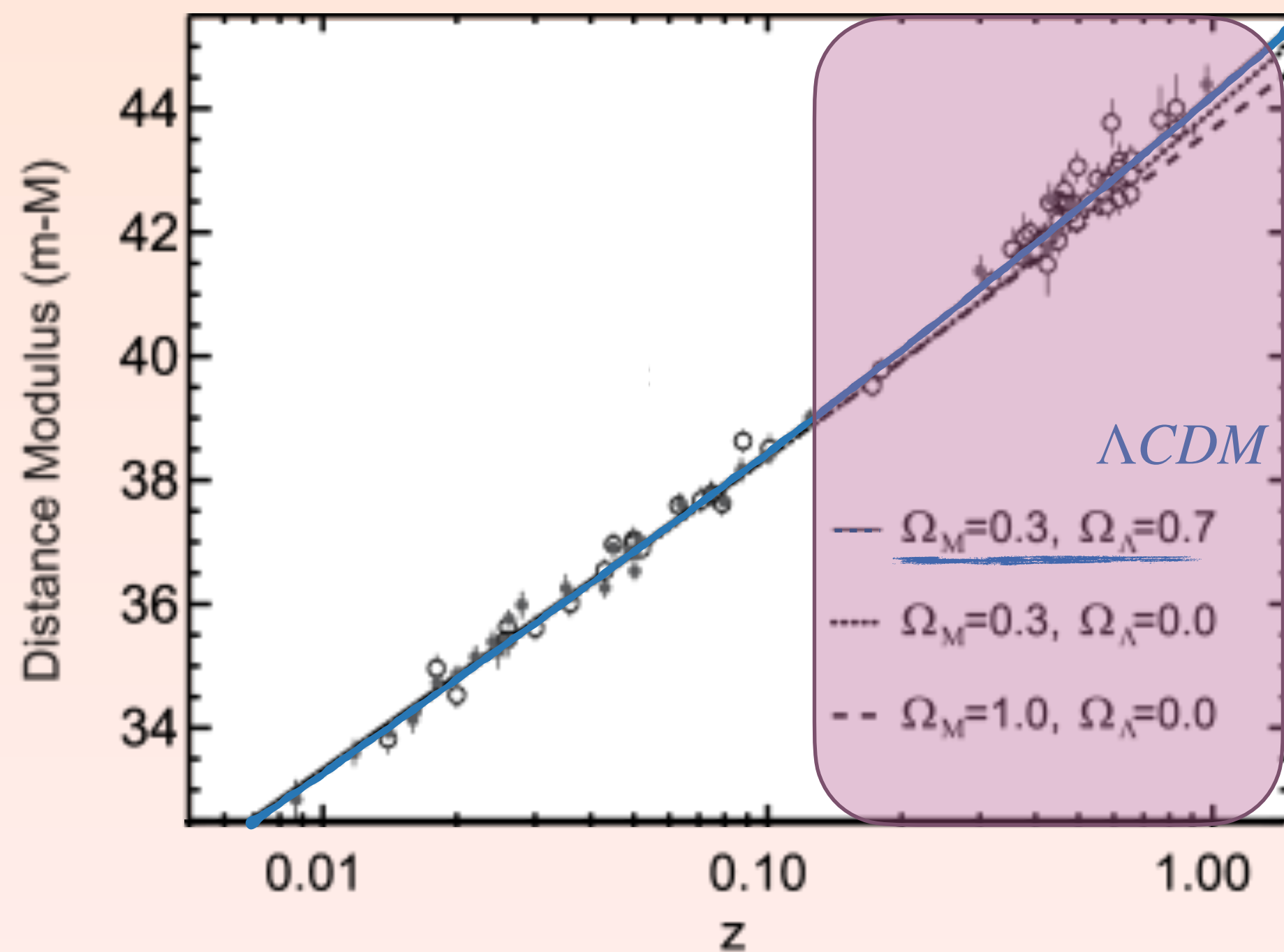
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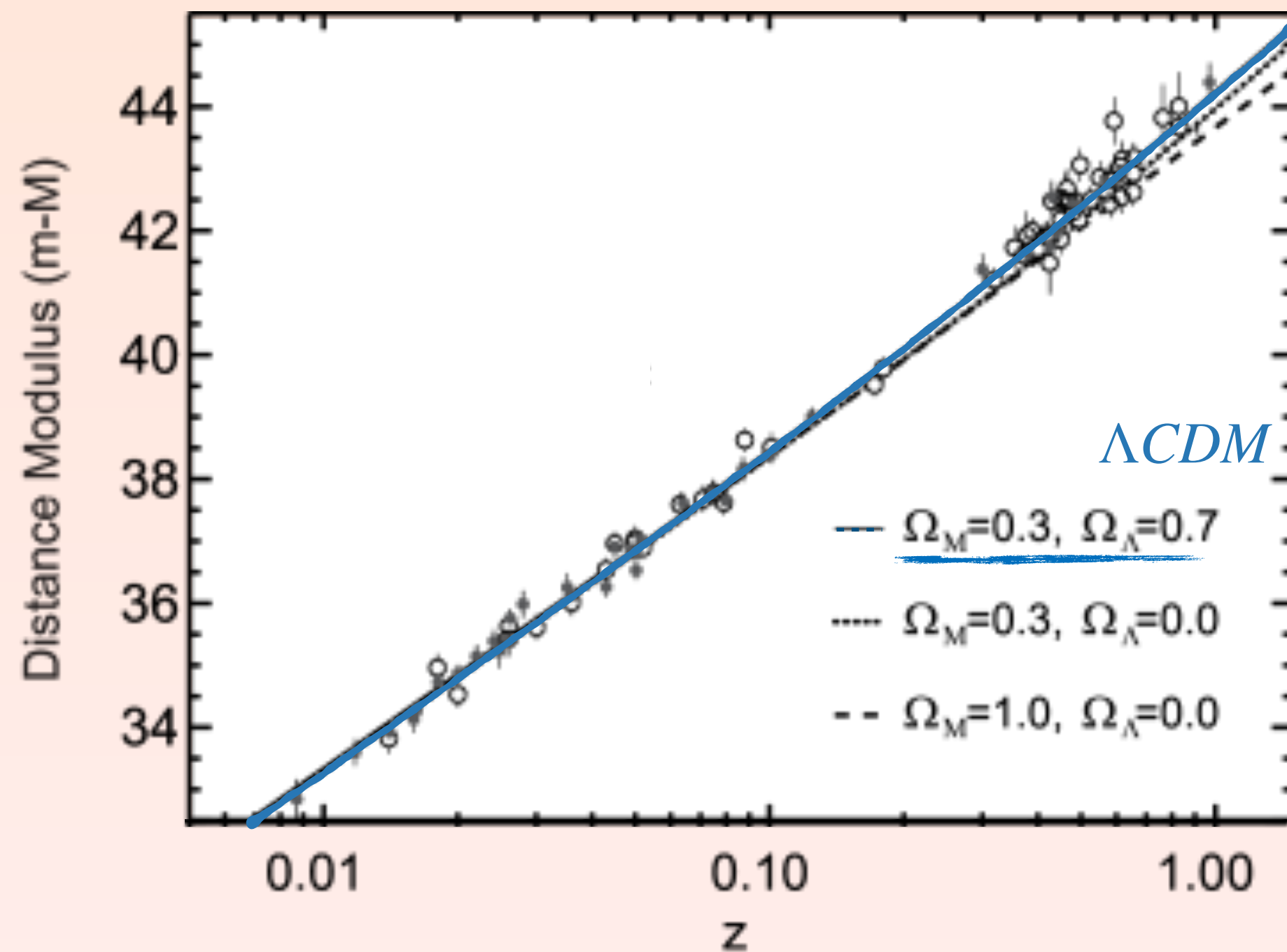
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Goals | Cosmology

w variations are in the thickness of the line :
we compute $\mu - \mu_{\Lambda\text{CDM}}$ to see it



Hubble Diagram - Frieman 2008

Matter density

Dark Energy density

parameter of the dark energy equation of state

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Equation of $w\text{CDM}$ model

- Flat Universe
- $\Omega_M + \Omega_\Lambda = 1$

Latest Combined result

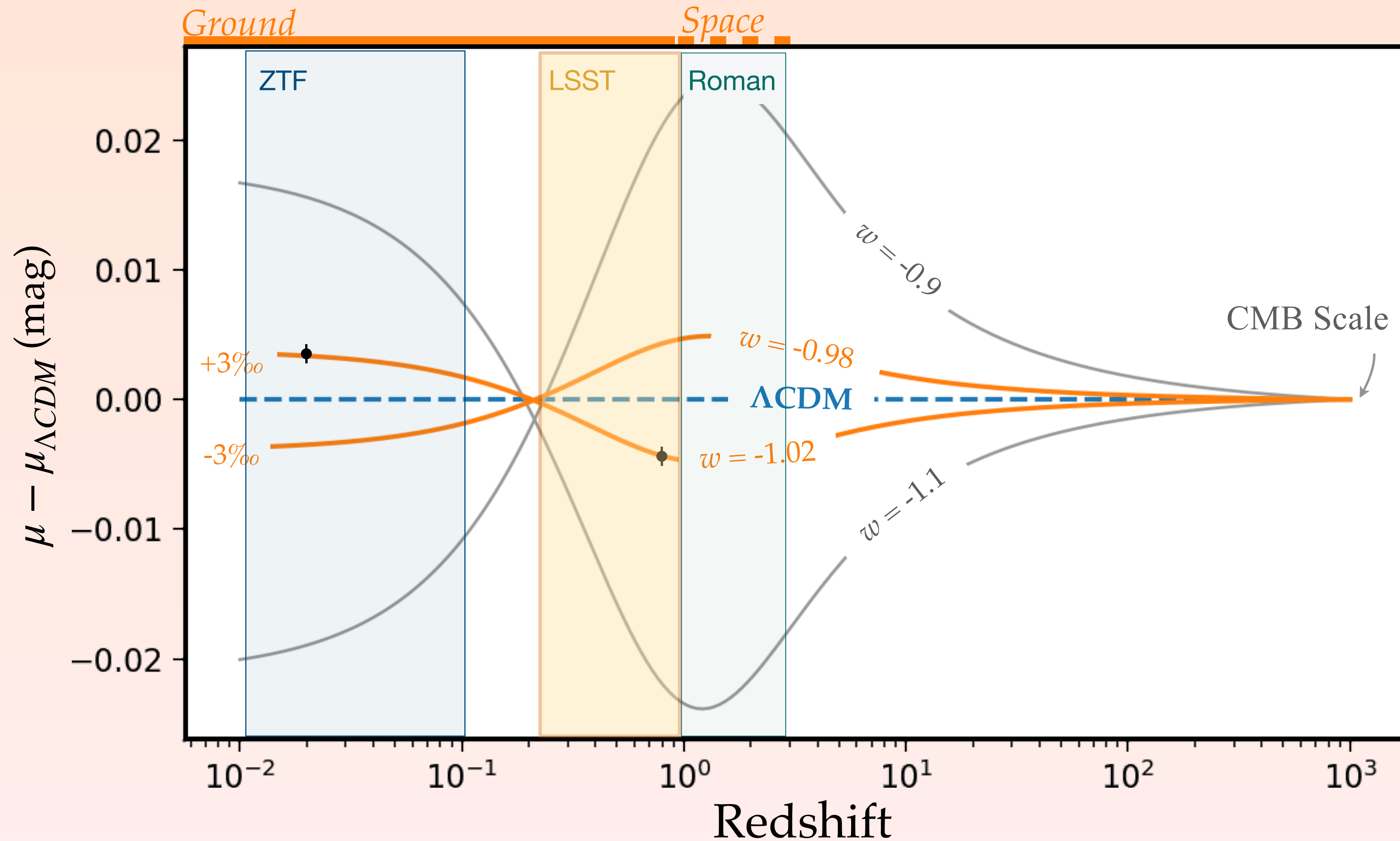
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Goals | *Dark Energy*



Precision required (Systematics)

Calibration :

$$\delta\text{mag} = 0.001$$

Astrophysical bias:

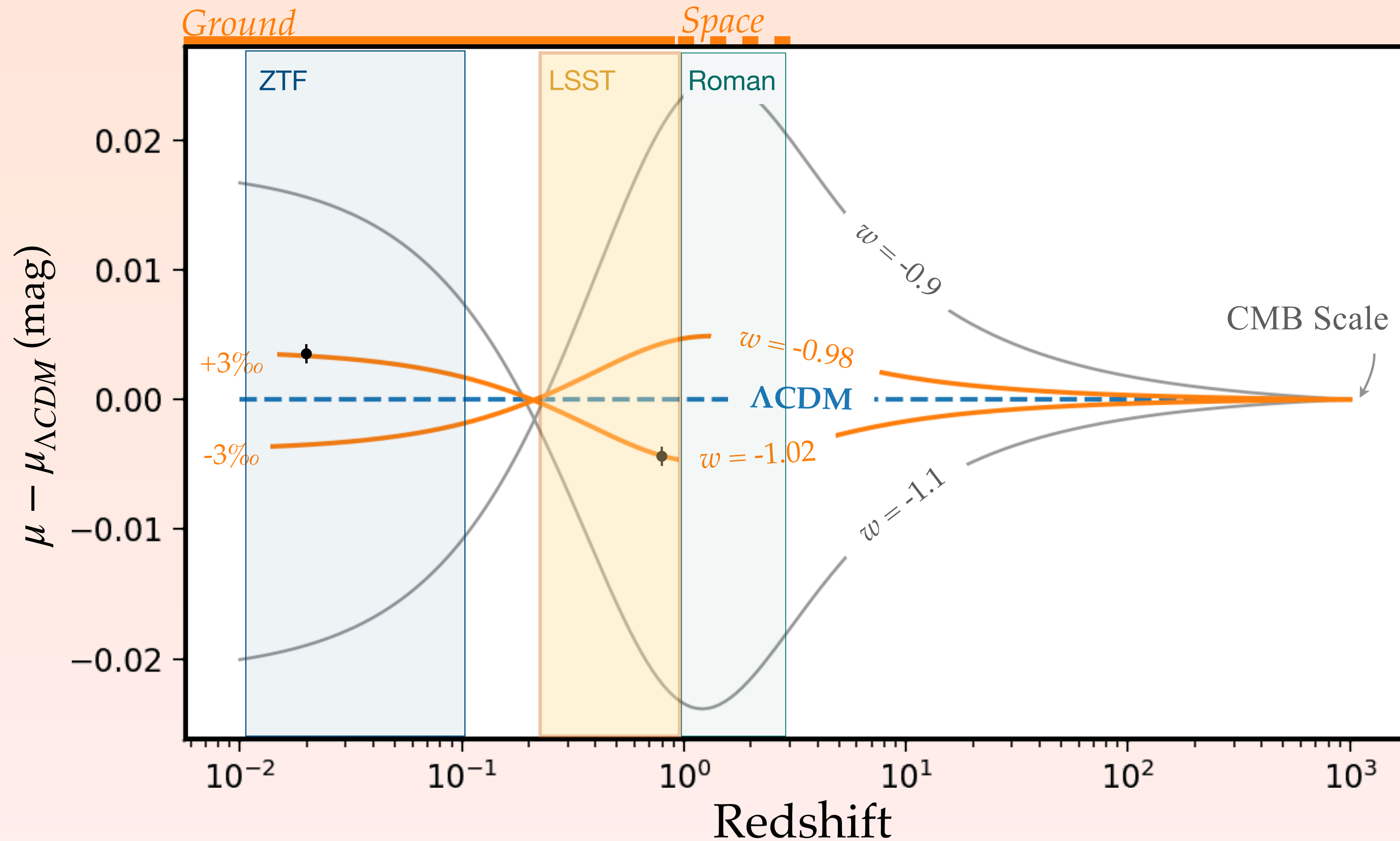
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Dispersion (Statistics)

SNe Ia dispersion :

$$\sigma_{\text{mag}} = 0.40$$

Goals | *Dark Energy*



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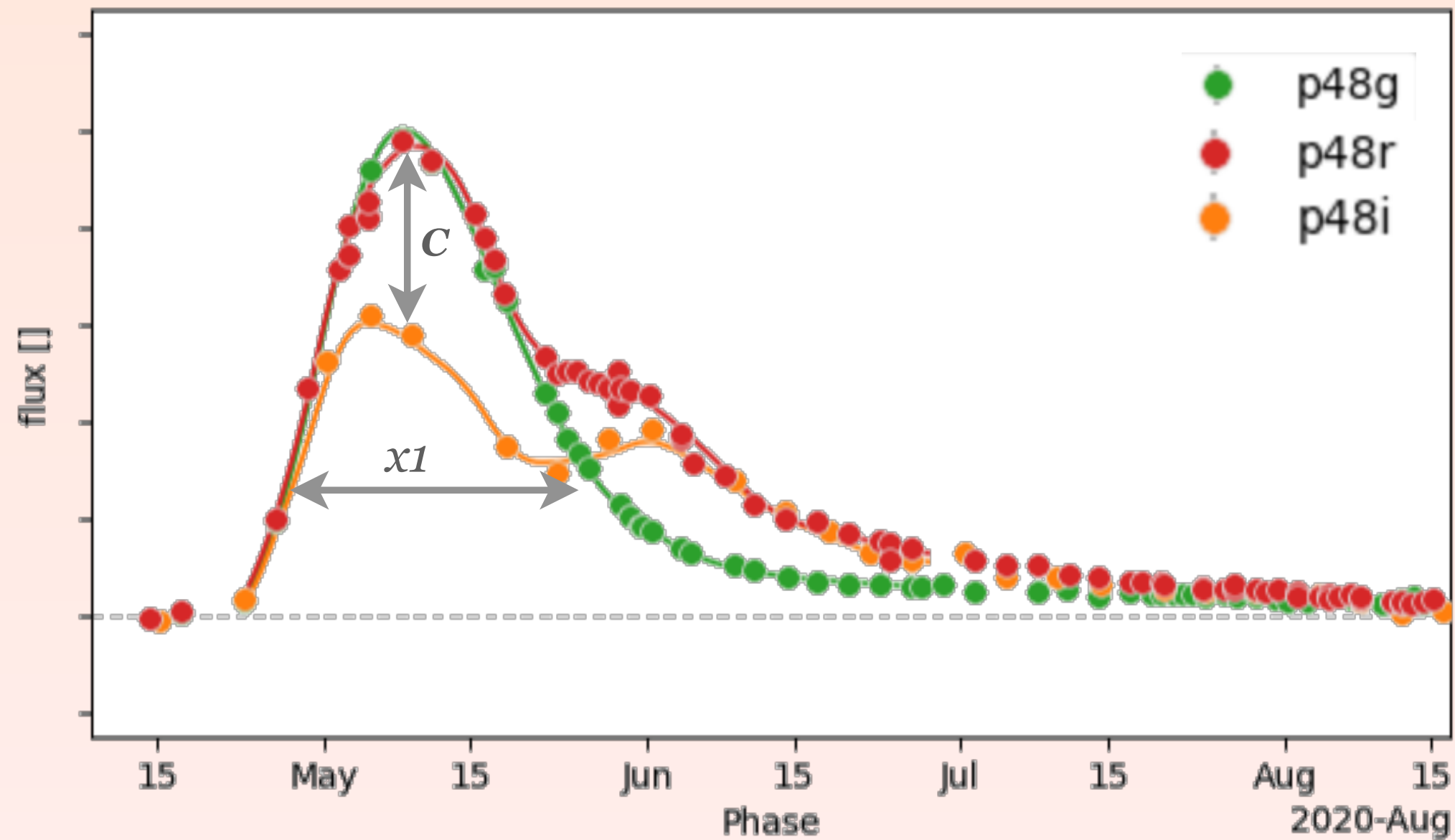
*SNe Ia are not
standard candles !*

Photometric standardisation

Tripp relation (1998):

Corrections
'Slower-brighter' : x_1
'Brighter-bluer' : c

$$\mu_{corr} = m_B^{max} - M_B^{max} + \alpha x_1 - \beta c$$



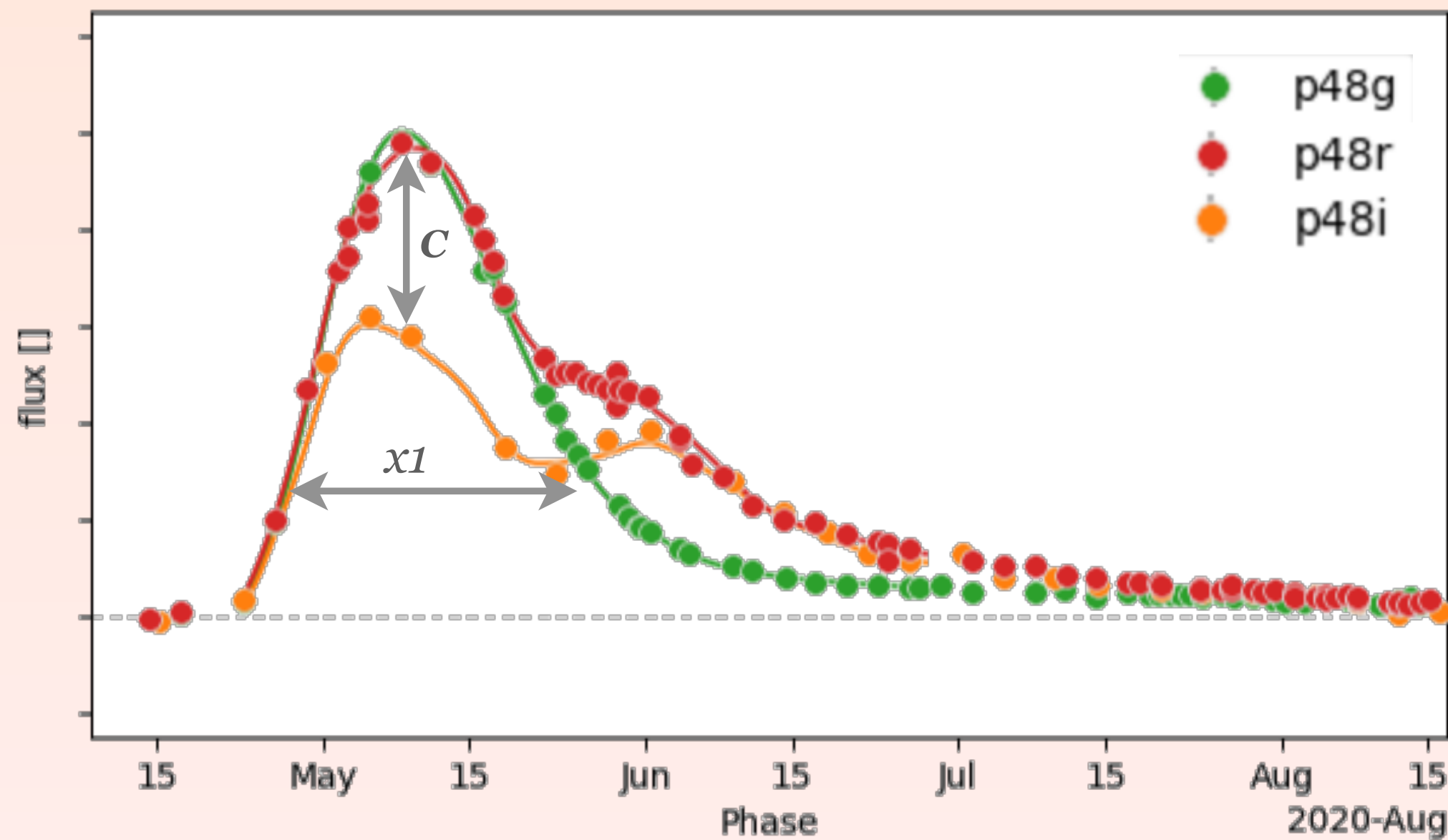
Lightcurves of ZTF20abxzrqw

Photometric standardisation

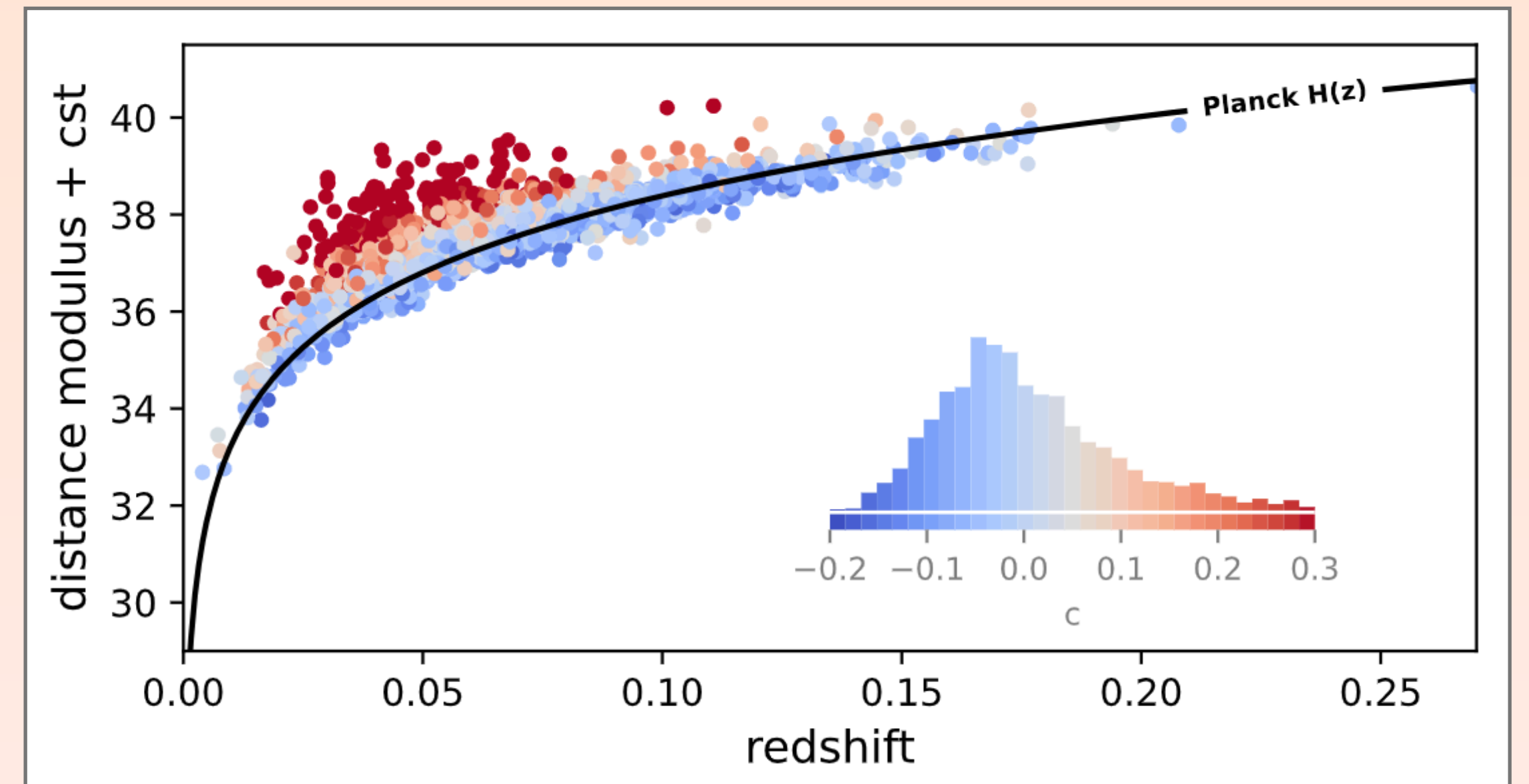
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Lightcurves of ZTF20abxzrqw



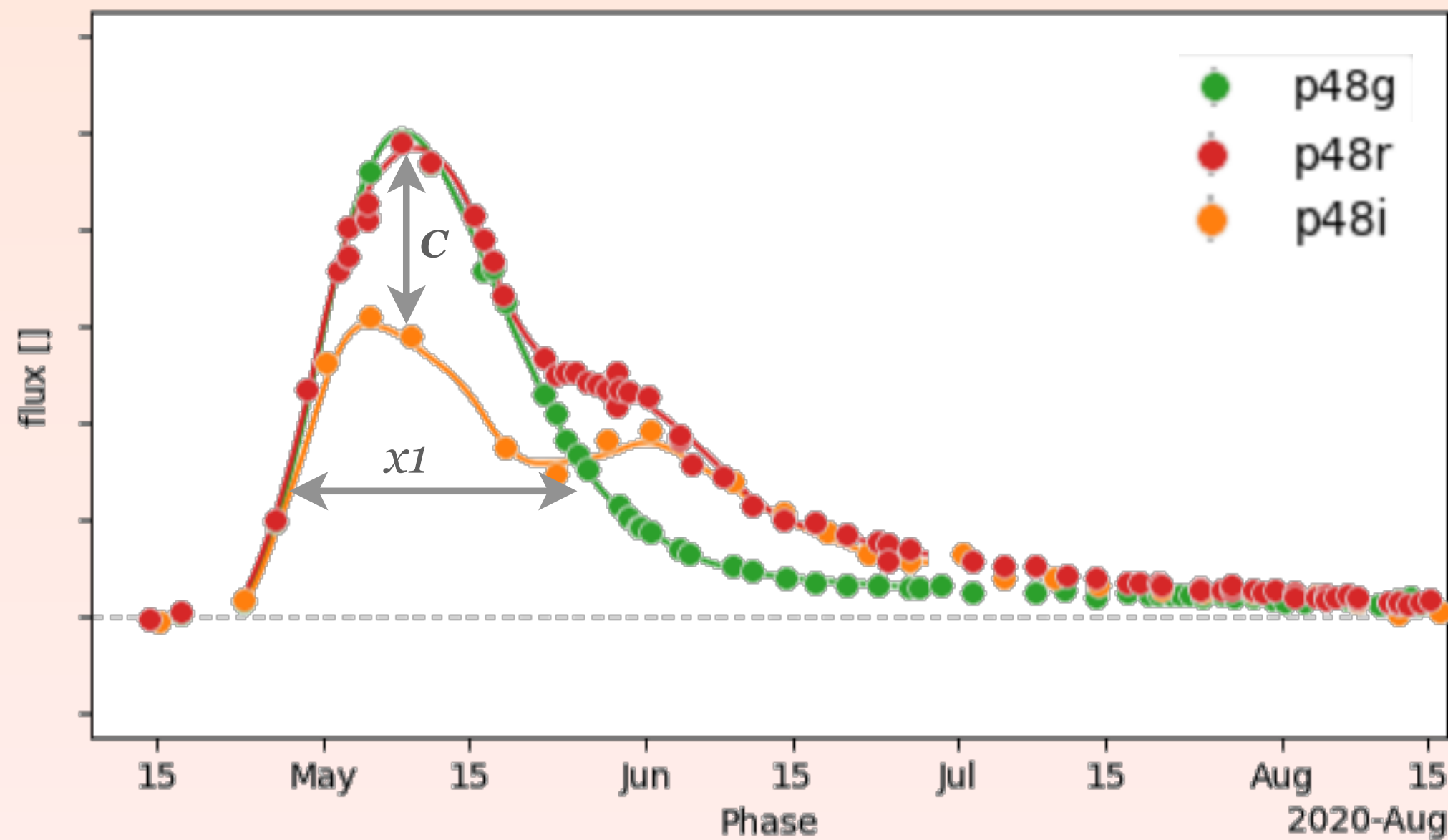
Hubble Diagram photometric standardisation
 Credit : in prep. ZTF "DR2" Data paper, Smith et al.

Photometric standardisation

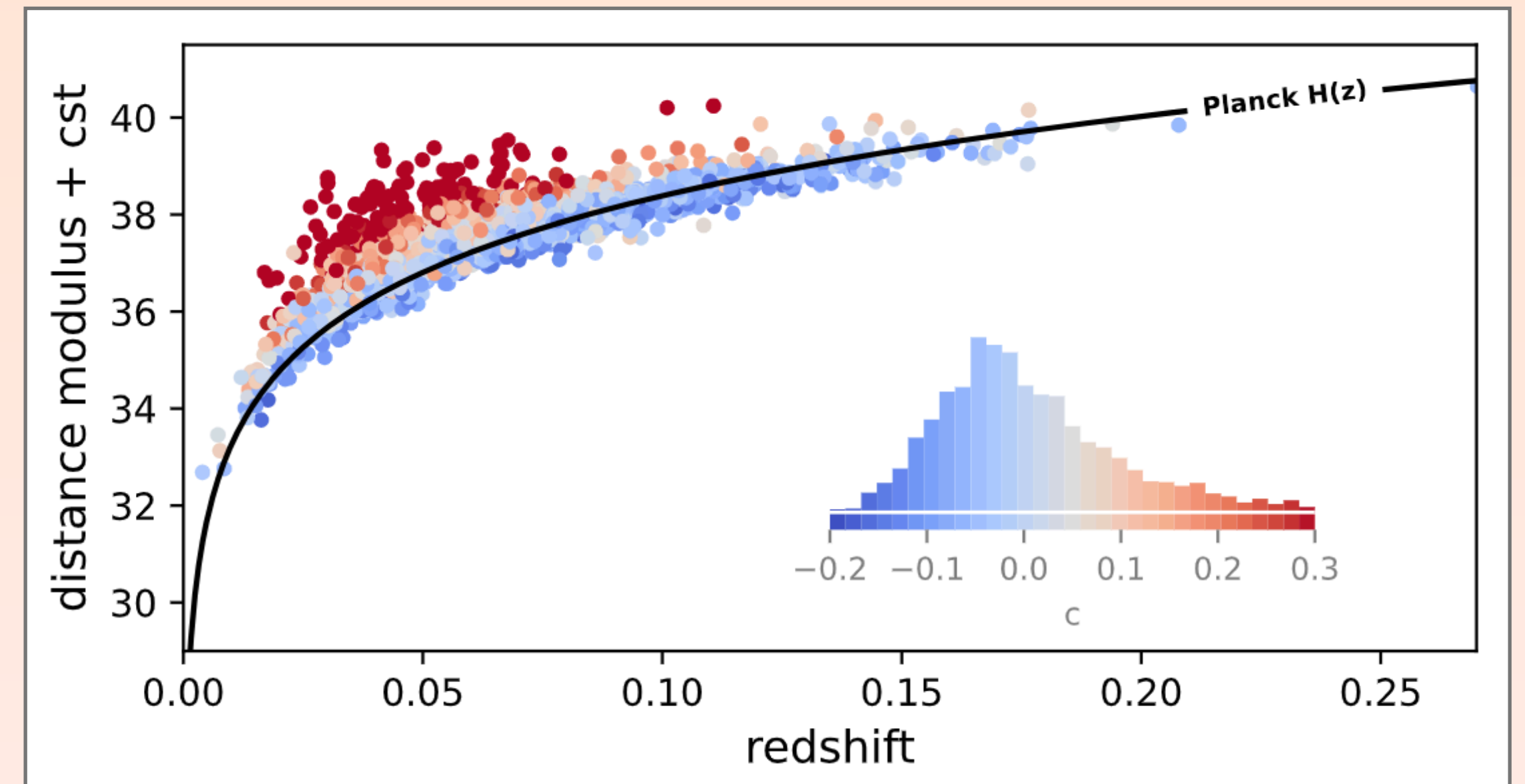
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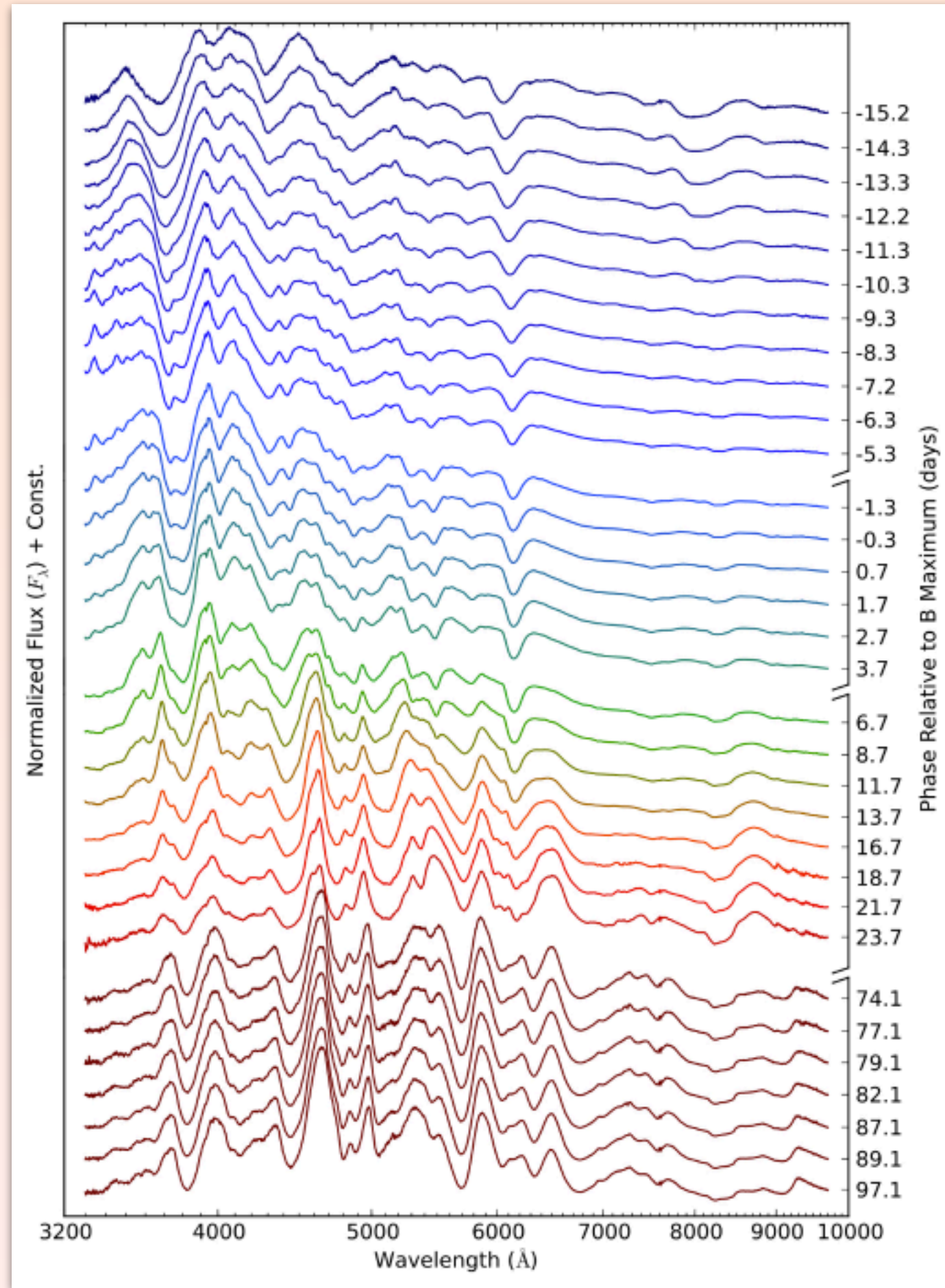
SNe Ia dispersion :

$$\sigma_{mag} = \cancel{0.40} = 0.15$$

with Photometric standardisation

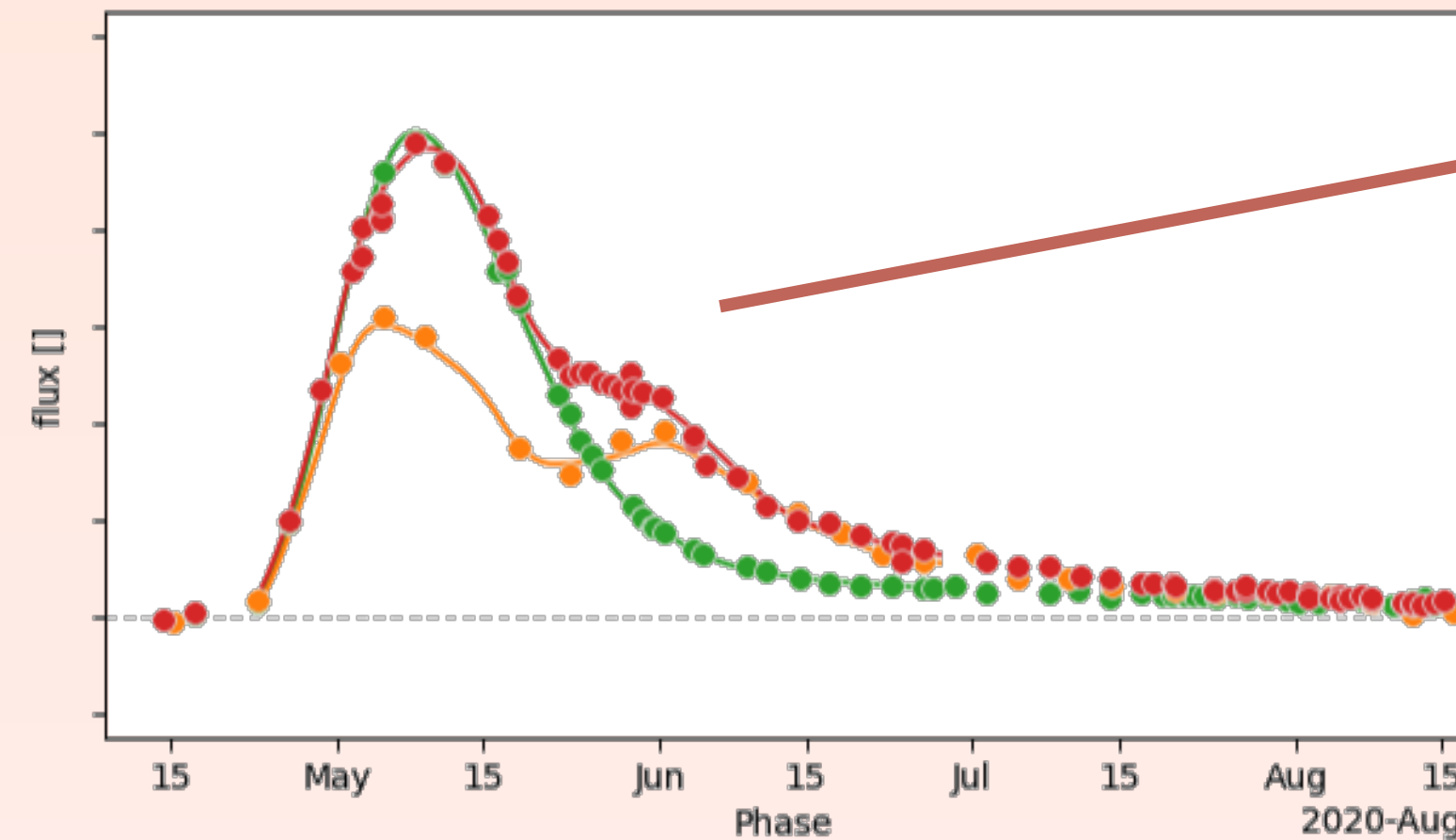
Problem : The origin of the dispersion of 0.15 mag is unknown

Spectro-photometry

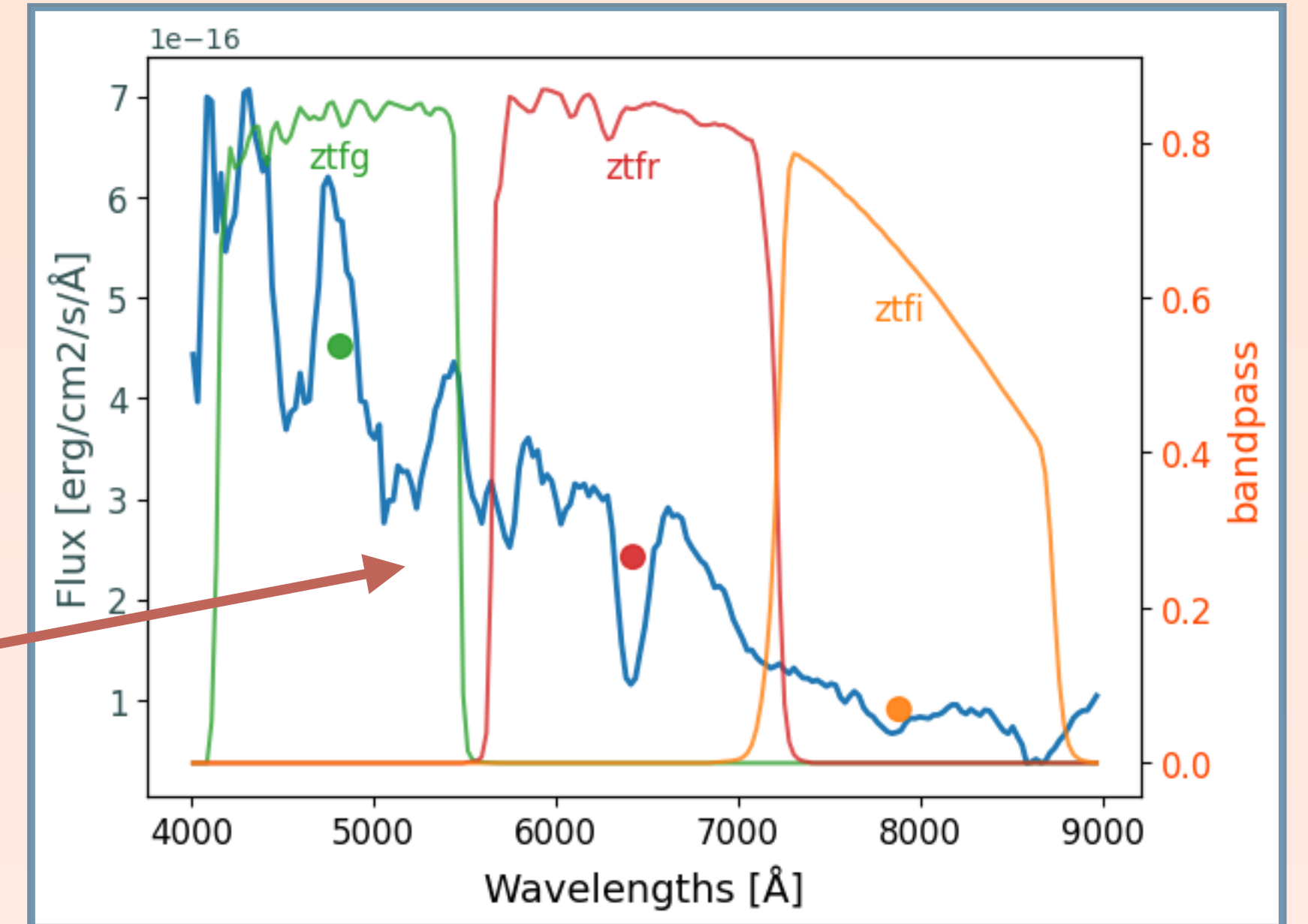


Time series of SN2011fe
between **-15** to **+100** days
Credit: Pereira et al. 2013

A lightcurve datapoint corresponds to the spectrum integrated in the bandpass



Lightcurves of ZTF20abxqrw
In ztf-g, ztf-r, ztf-i filters

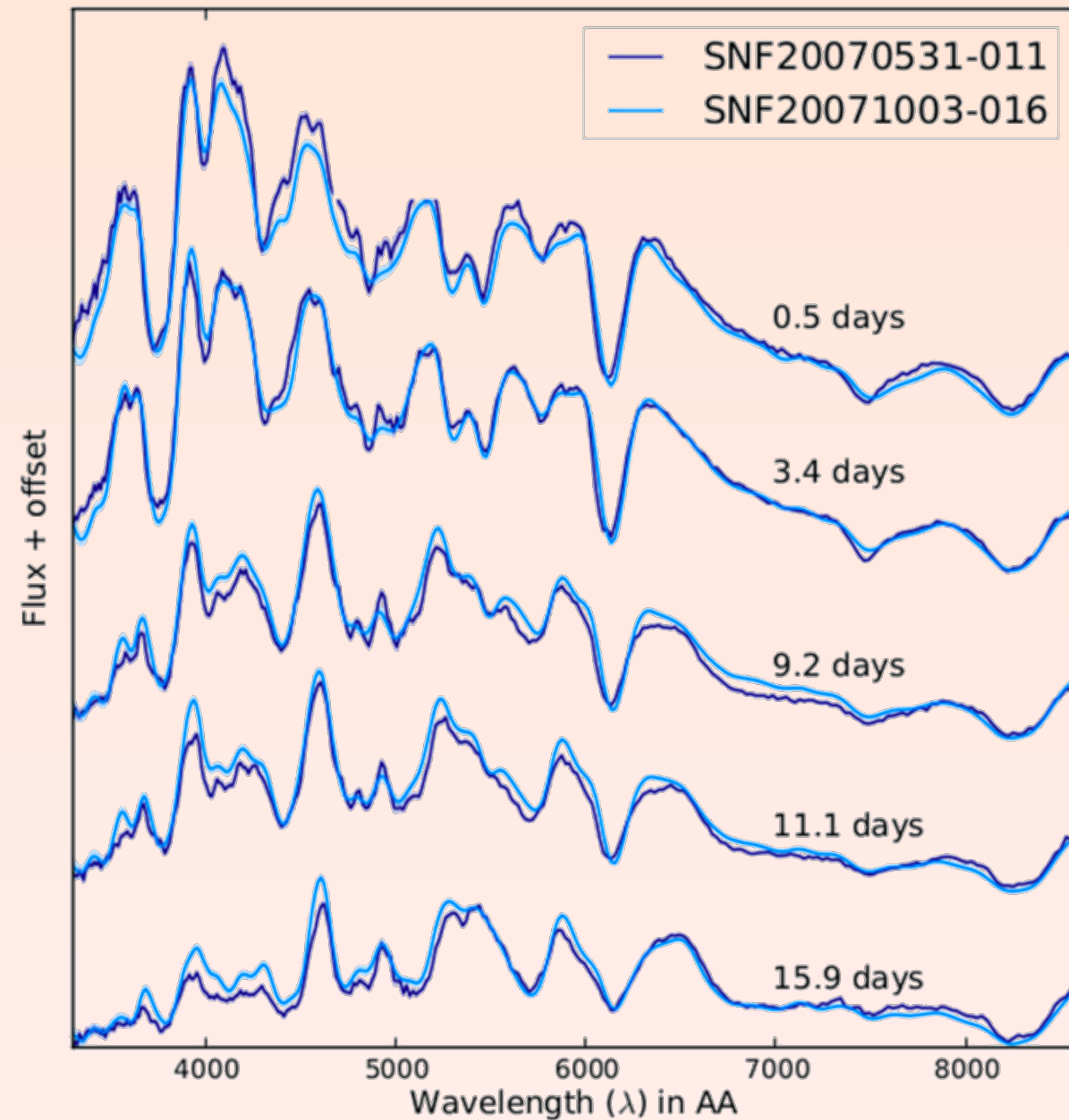


Synthetic photometry in ZTF filters
ZTF20abxqrw at phase +1.29

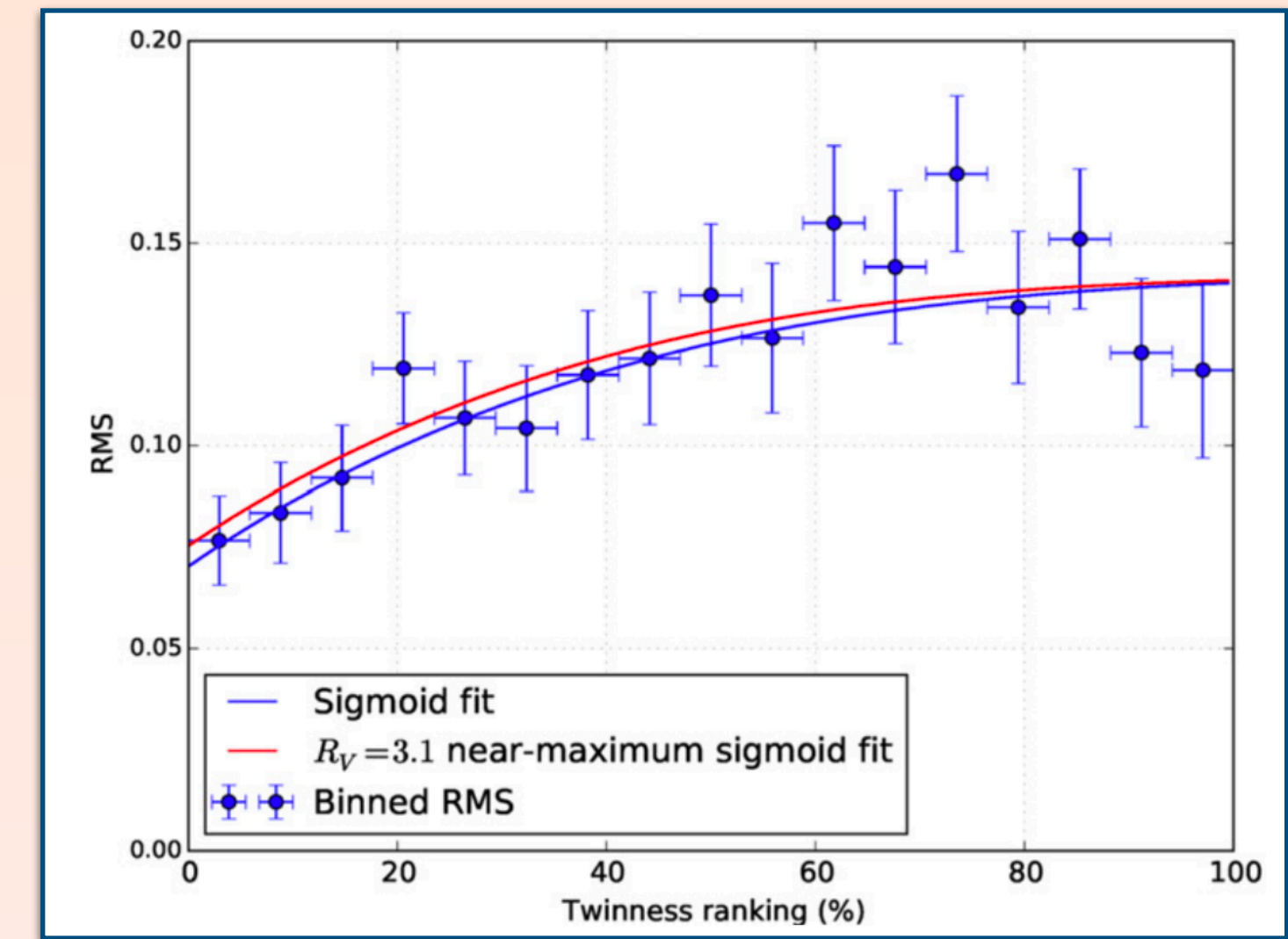
—> *New standardisation of distance modulus, using spectral information?*

Spectro-photometric standardisation

Initial discovery :
Twins - Fakhouri 2015



Spectral time-series of two 'Twins' SNe
Credit : Fakhouri et al. 2015



Luminosity RMS for different 'twinness' bins
Credit : Fakhouri et al. 2015

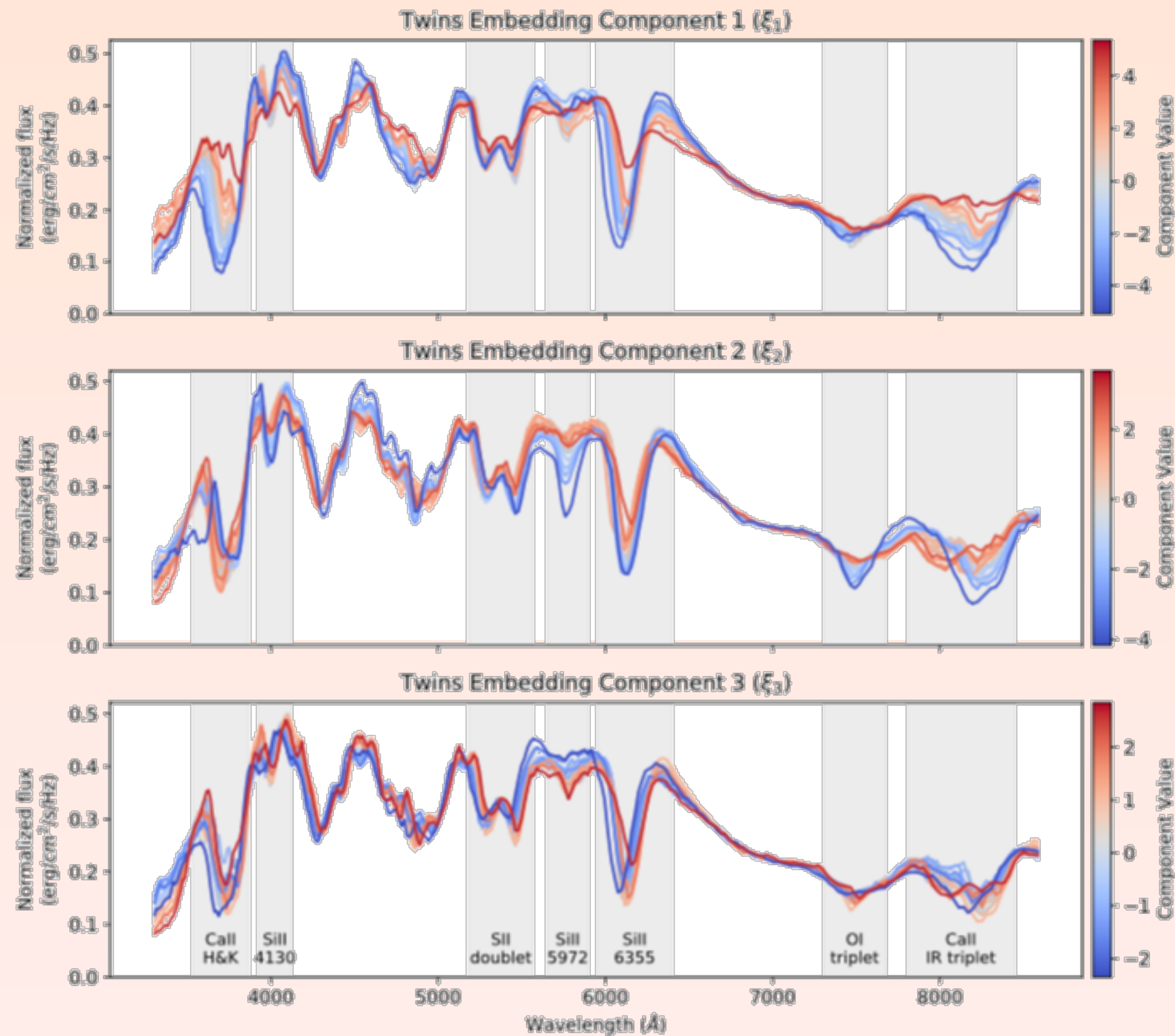
—> magnitude dispersion is smaller for the lowest 'twinness' parameters

—> Only one spectrum at maximum per SN Ia is sufficient to have the variation information

Spectro-photometric standardisation

Full method :

Twins Embedding - Boone 2021



→ New standardisation of distance modulus, using spectral information

→ Describe the spectral variation at phase=0

Twins Embedding components variation effects on spectra. Credit : Boone et al. 2021

Before standardisation :

$$\sigma_{mag} = 0.40\text{mag}$$

Photometry :

$$\sigma_{mag} = 0.15\text{mag}$$

With SNFactory

Twins Embedding :

$$\sigma_{mag} = 0.07\text{mag}$$

SNFactory : ~250 SNe

↓
ZTF : ~700 SNe
(for now)



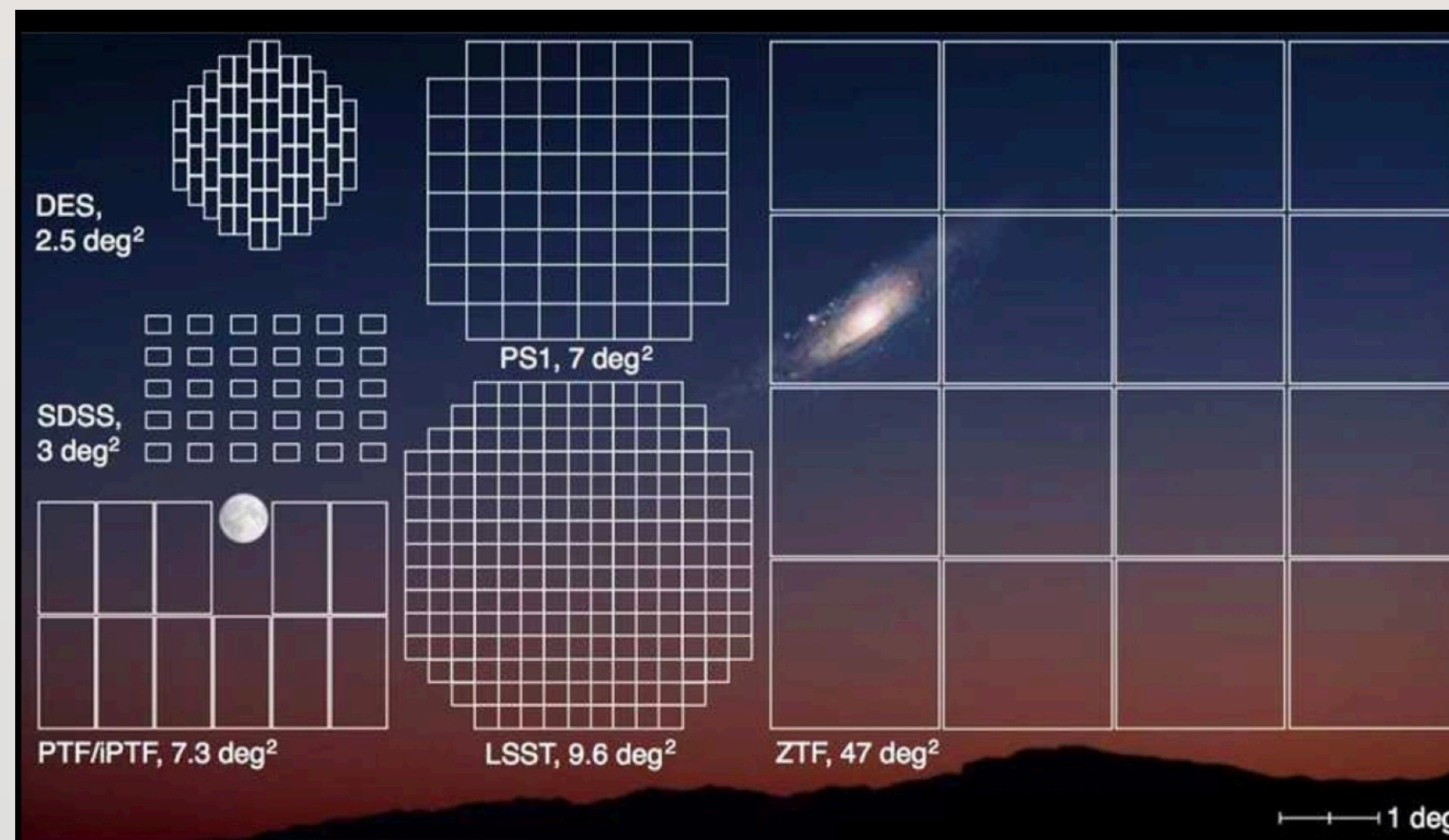
Zwicky Transient Facility

March 2018 to 2027

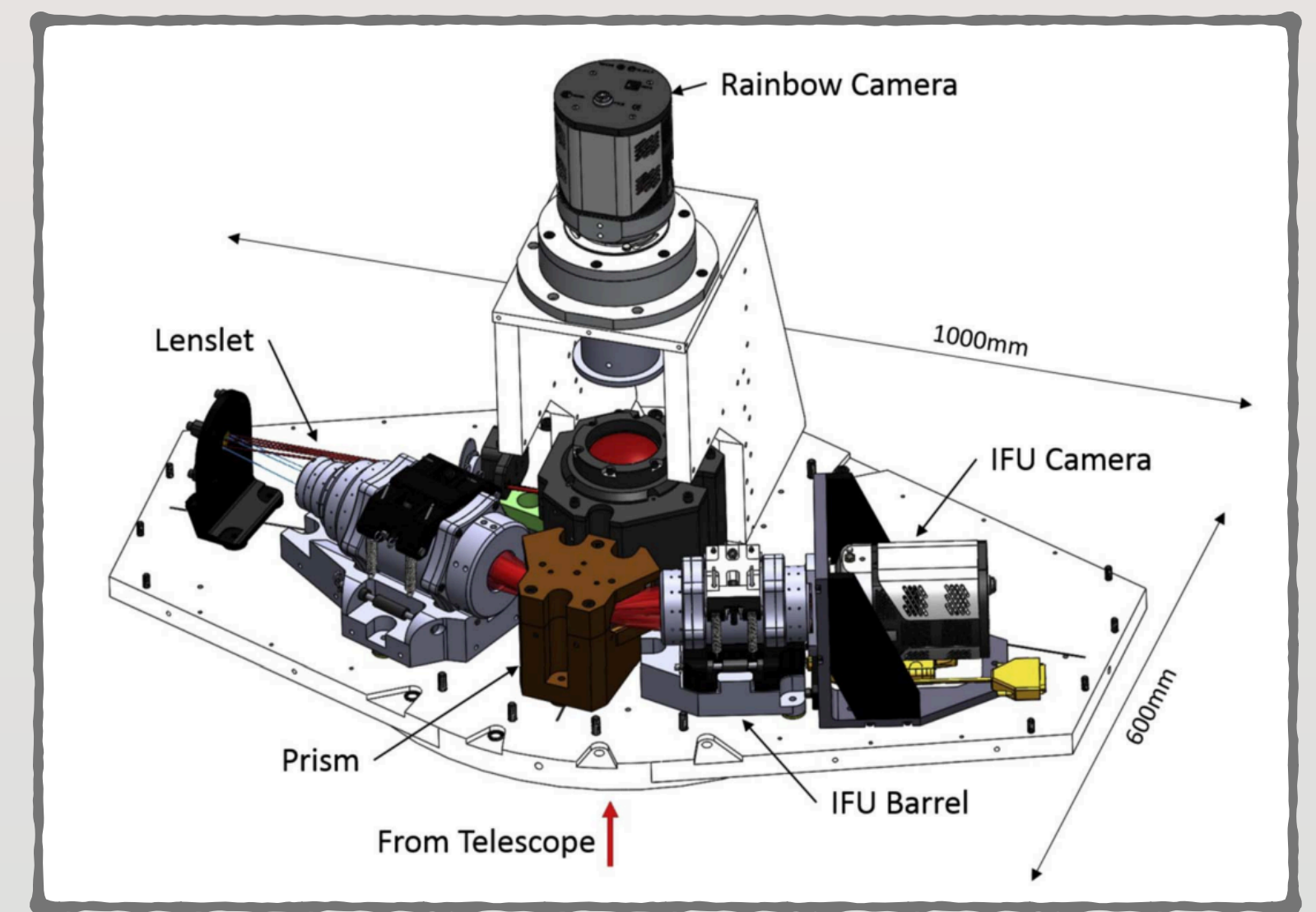
Low-redshift $z < 0.15$
Northern sky
3 filters : g, r, i
Limits in magnitude of $\sim 20\text{mag}$

Two instruments :

- ✱ P48 camera
- ✱ P60 spectrograph



ZTF Camera P48 FoV
Source : Joel Johansson



SEDm (P60)- Integral field Spectrograph
Source : N. Blagorodnova et al. 2018

Located in Mount Palomar in California



SEDmachine

March 2018 to December 2020

$\mathcal{O}(3600)$ Supernovae Ia
 $\mathcal{O}(4000)$ spectra

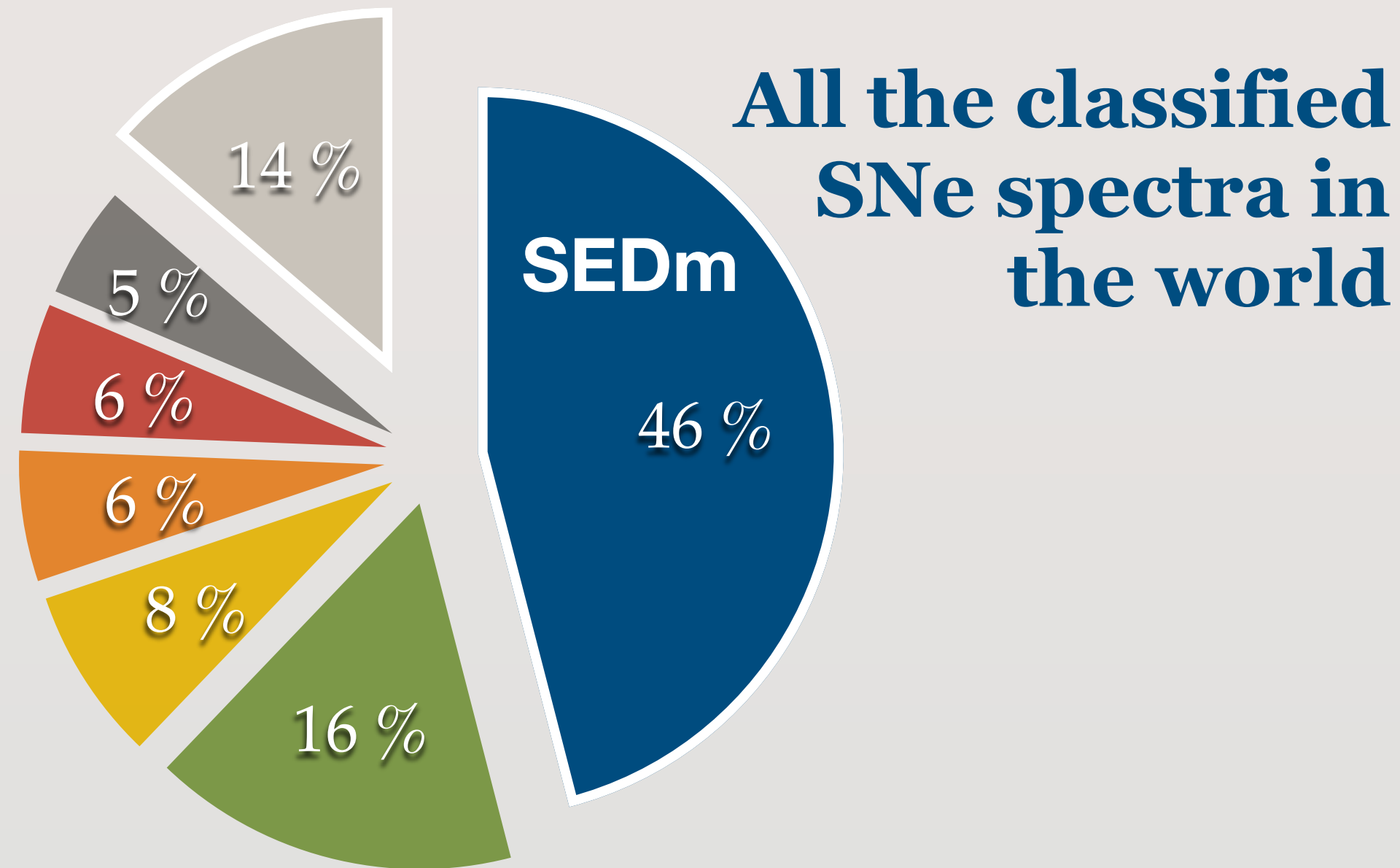
60% SNe Ia
spectra from the
SEDm

Purpose : typing and redshift

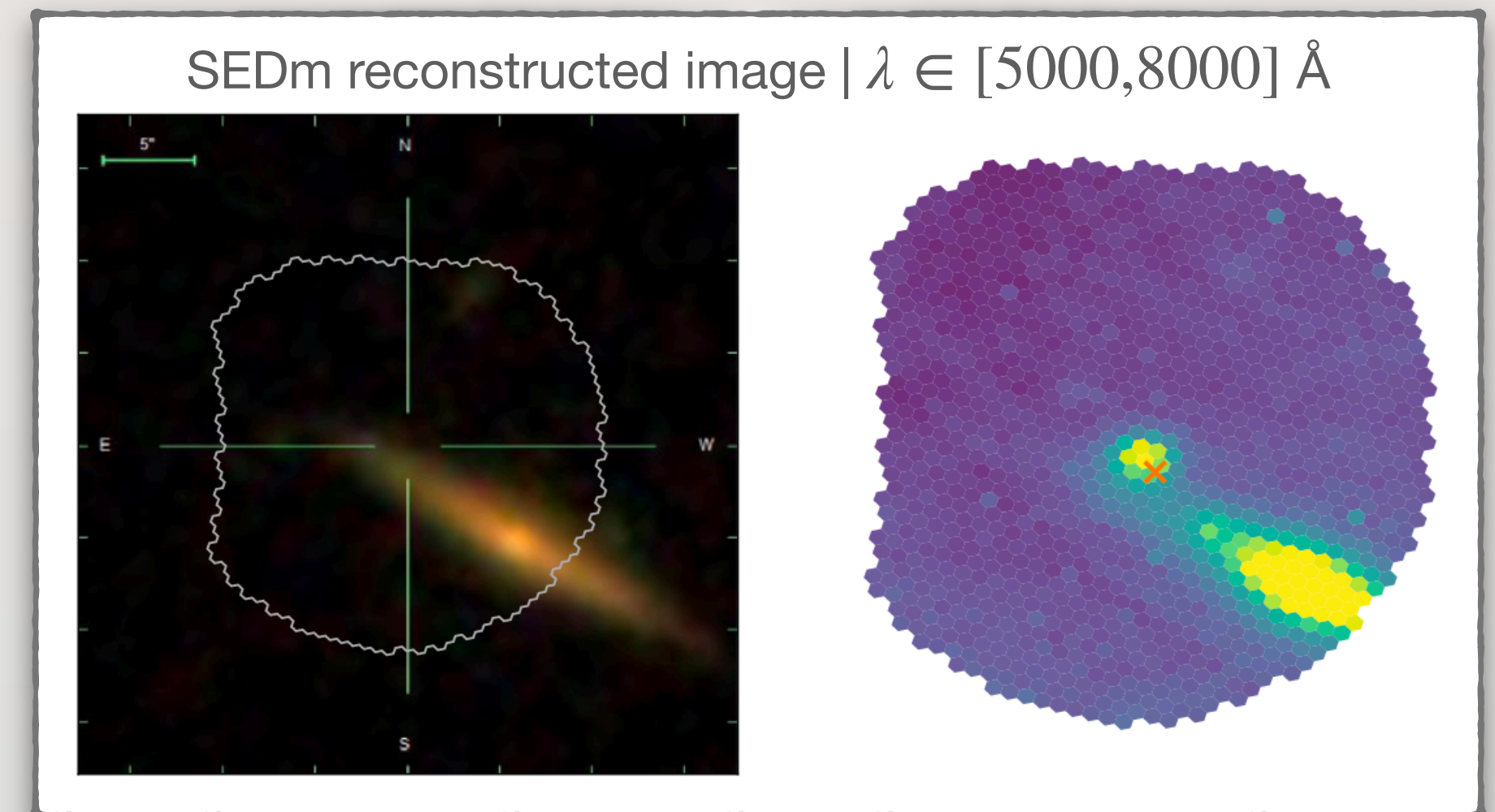
Low resolution : $R = \frac{\lambda}{\Delta\lambda} \sim 100$

Optical window: 3,650 - 10,000 Å

Acquisition of ~1 hour



Source: Transient Name Server
wis-tns.org/stats-maps



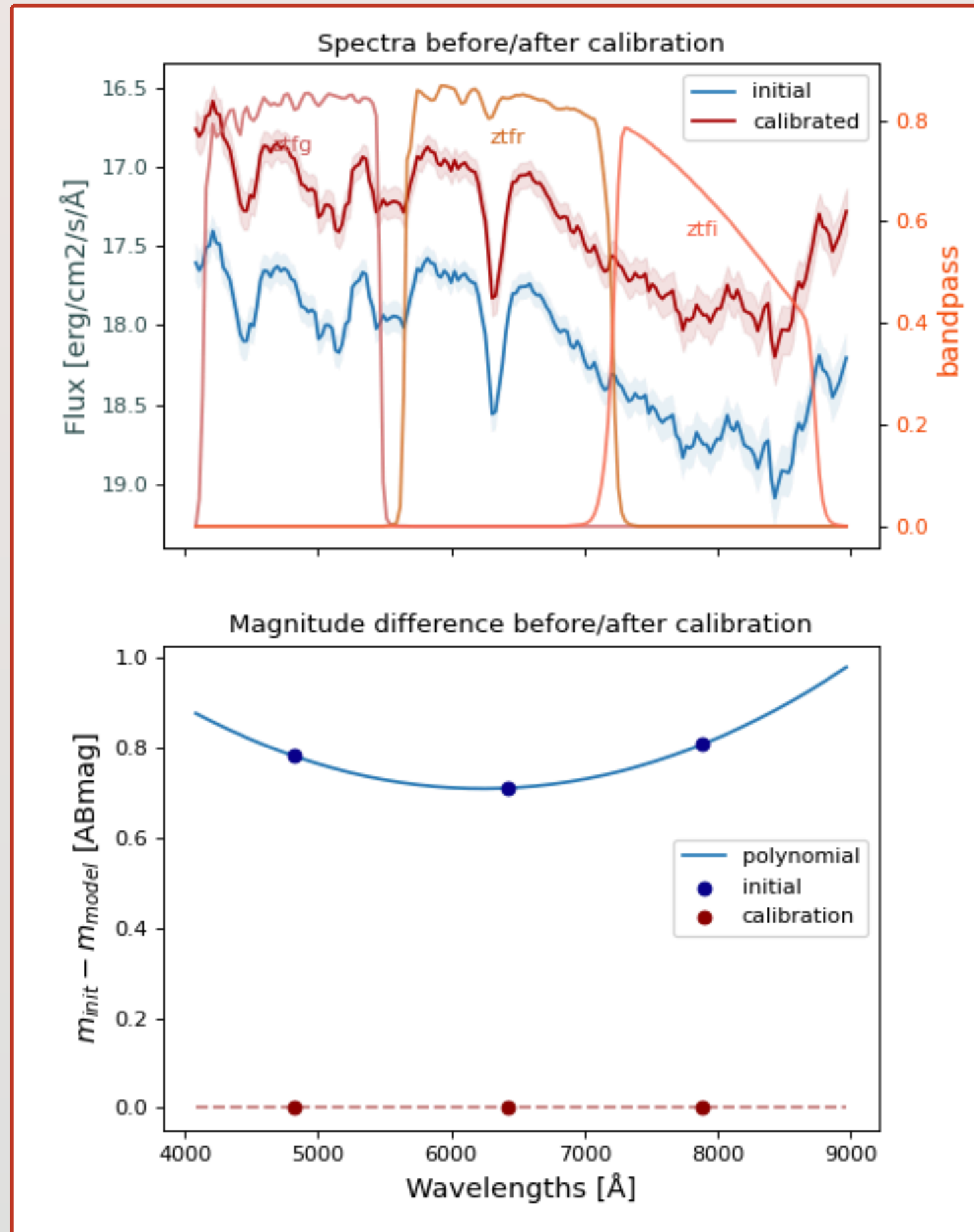
SEDm (P60)- Integral field Spectrograph
field of view of ZTF18abqlpgq

Source : *pysedm* - Rigault, Neill

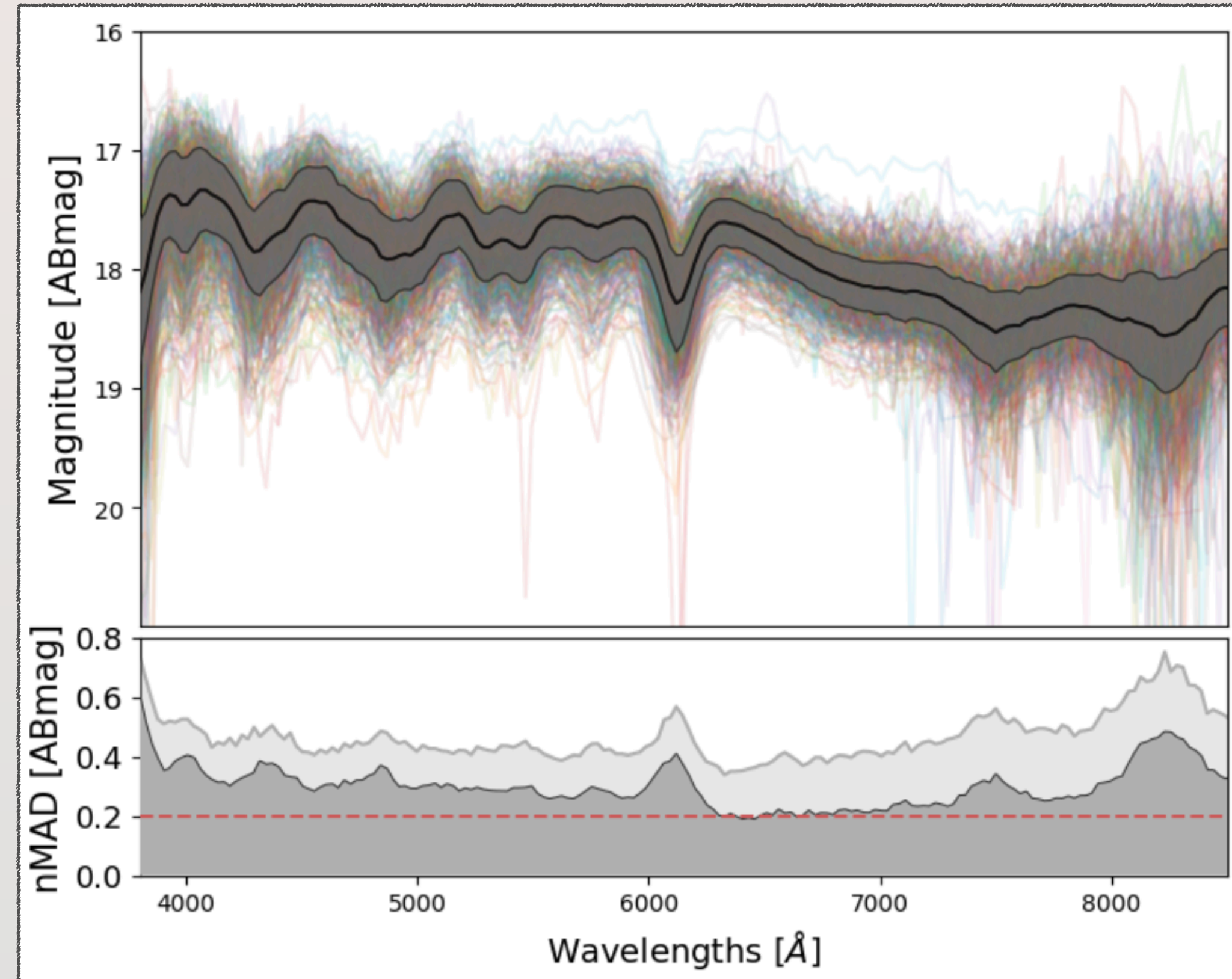
- ♦ spectral extraction by *pysedm*. (Rigault 2019)
- ♦ Correction of host galaxy by *Hypergal* (Lezmy 2022)



ZTF spectra flux-calibration



Exemple of flux calibration
with *ZTF20aayvubx_20200524_SEDm_0*

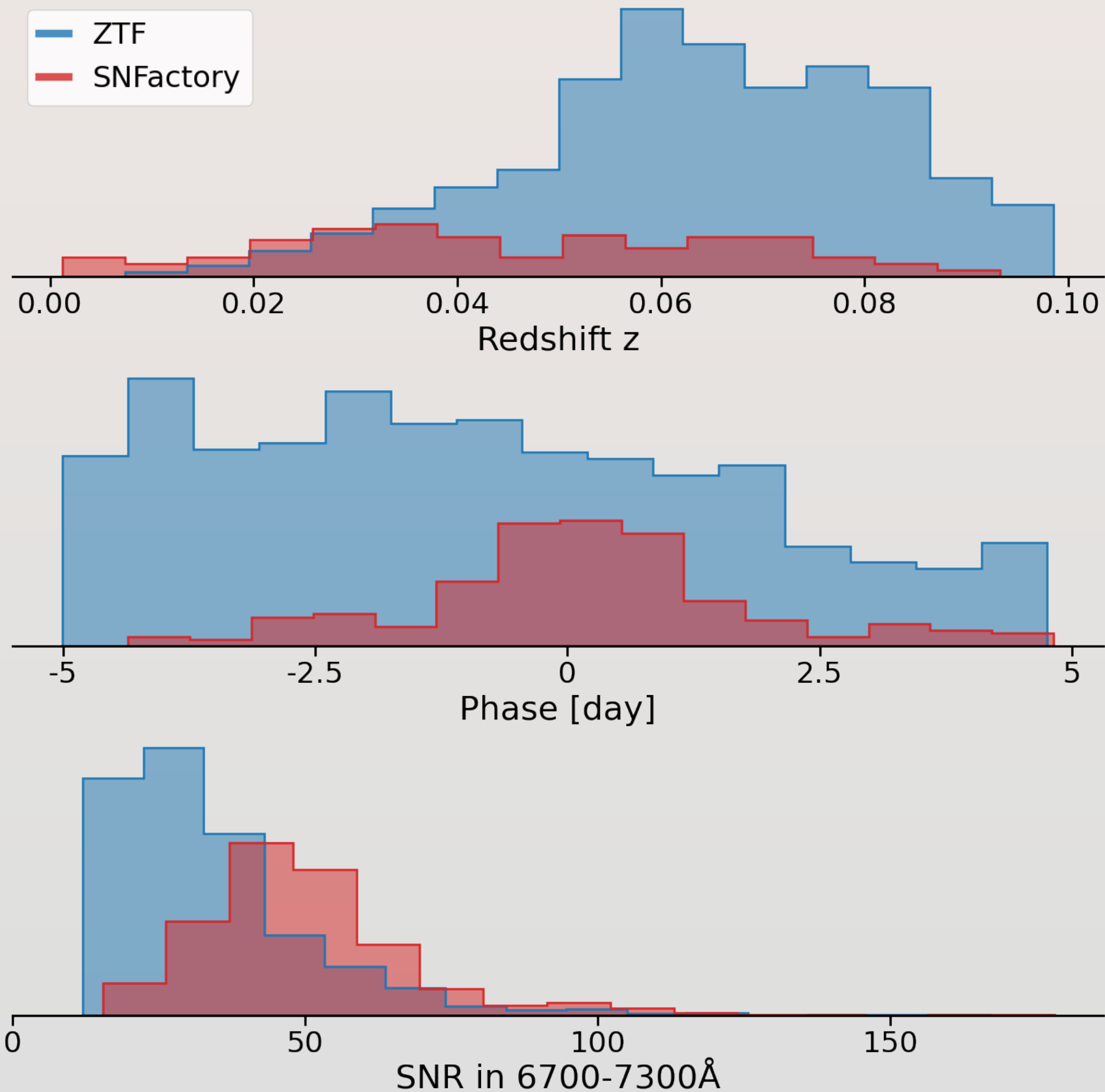


Median+nMAD of **752** ZTF flux-calibrated spectra
at **z=0.05**

For phases in [-5,5], and cosmo cuts

- Flux calibration
- Milky Way correction
- Shift spectra to $z=0.05$

ZTF spectra sample



Cut	Interval	Quantity removed
from SEDm		40 %
Quality		20 %
z	<0.1	around 7/8%
phase	[-5,+5] days	around 50%
cosmo		around 15%

—> **752 spectra from 695 SNe Ia**

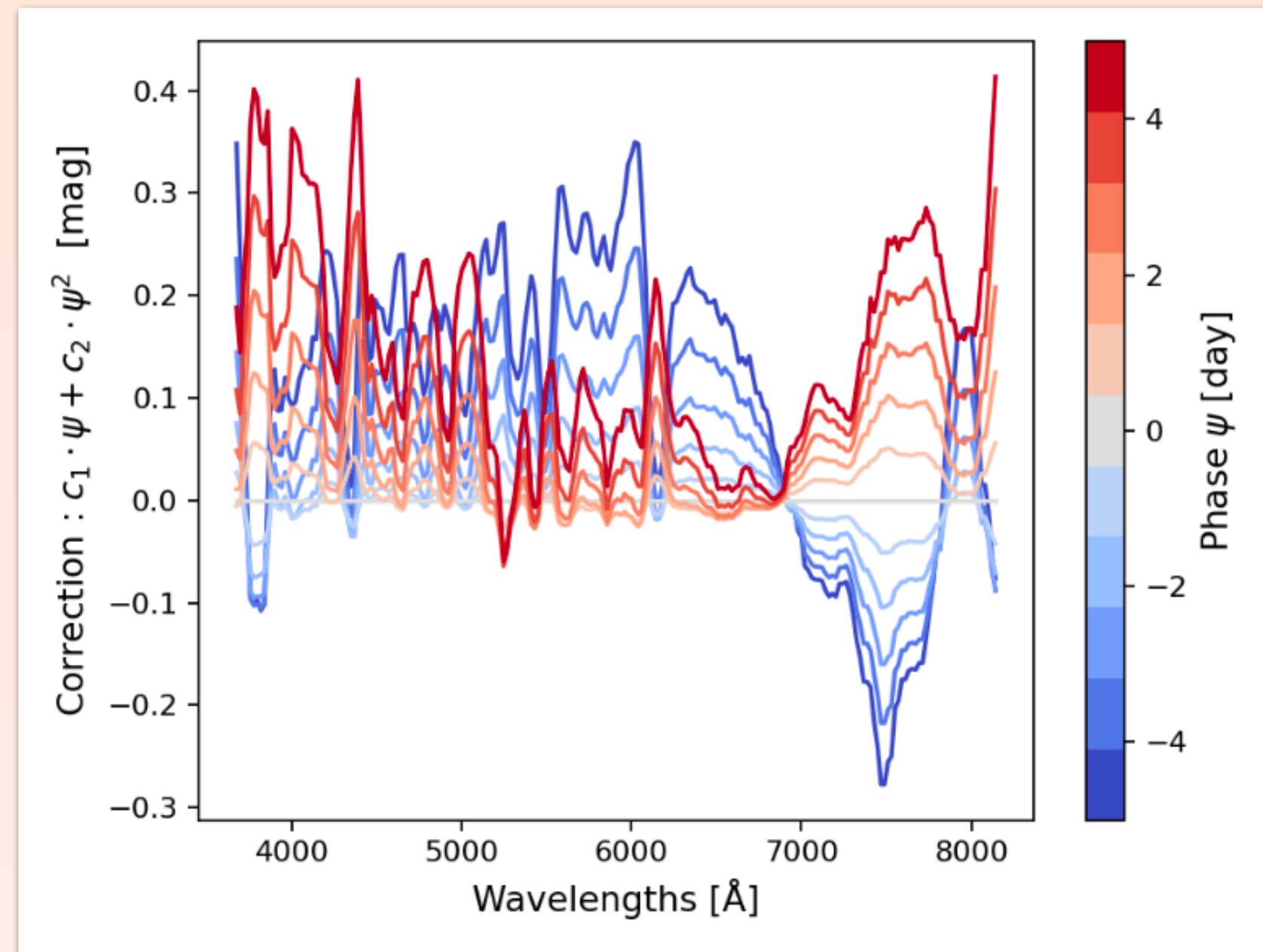
—> *The spectra sample is ready to test the standardisation*

Twins Embedding - Boone et al. 2021

3 steps

1. Generate at maximum luminosity

$$m_i(p; \lambda_k) - m_i(0; \lambda_k) = p \cdot c_1(\lambda_k) + p^2 \cdot c_2(\lambda_k)$$

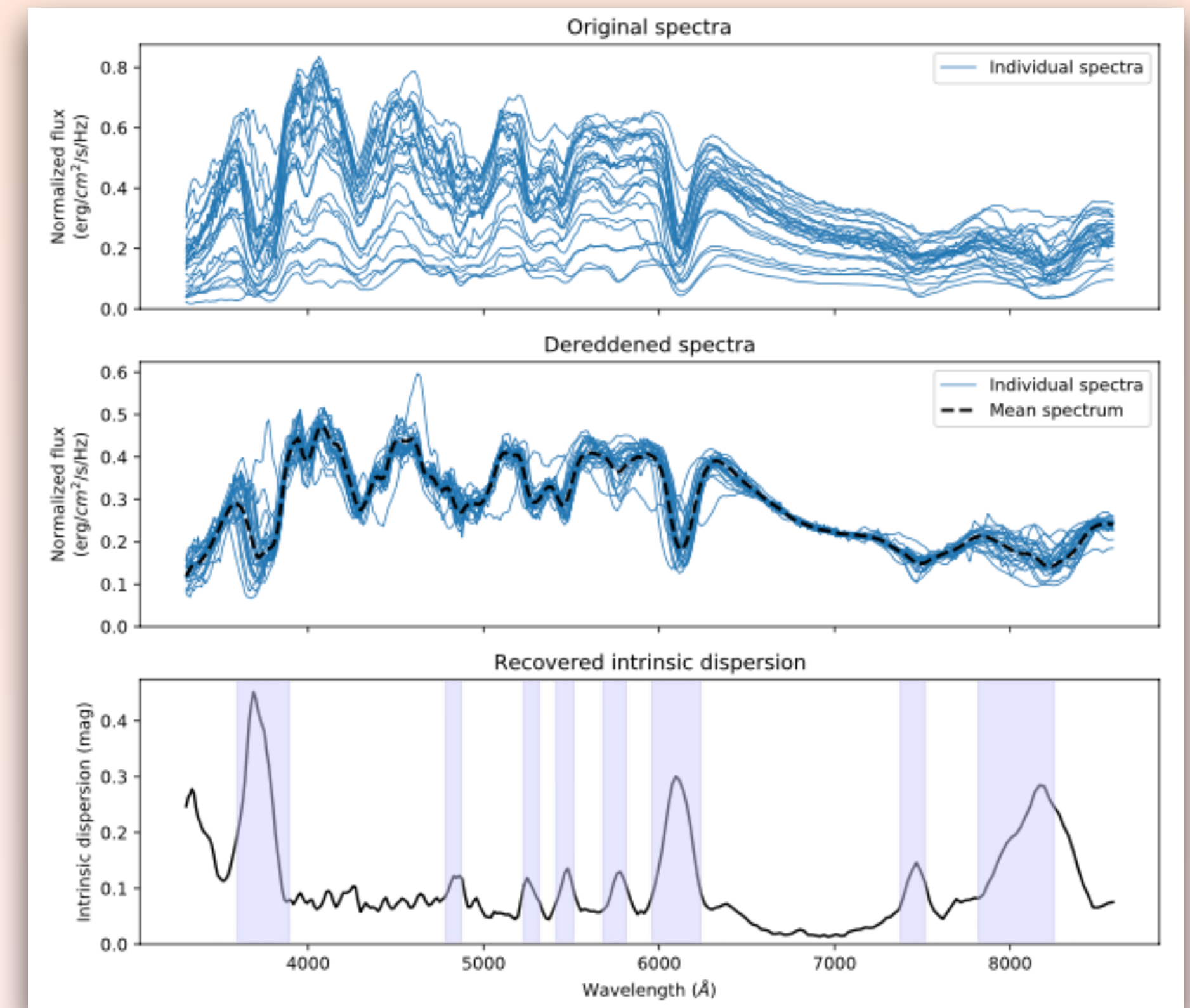


Quadratic evolution in phase of SN Ia spectra

Capture 85% of the spectral **time evolution** variance common to every *Sne* between -5 and 5 days

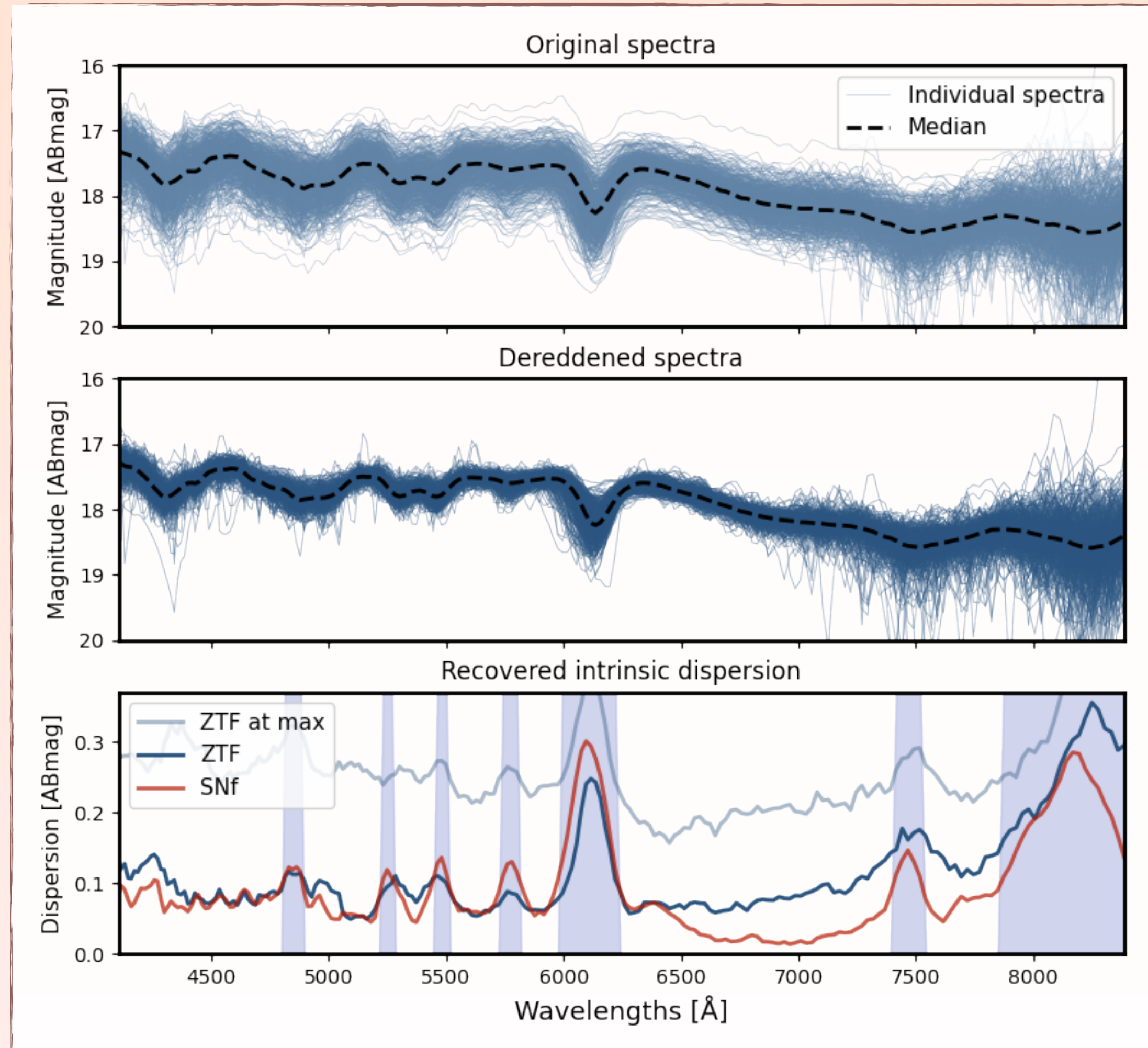
2. RBTL - fit one offset and a color outside the lines

- Δm_i a magnitude offset compared to reference spectrum
- $\Delta \tilde{A}_{V,i}$ a color coefficient compared to reference spectrum

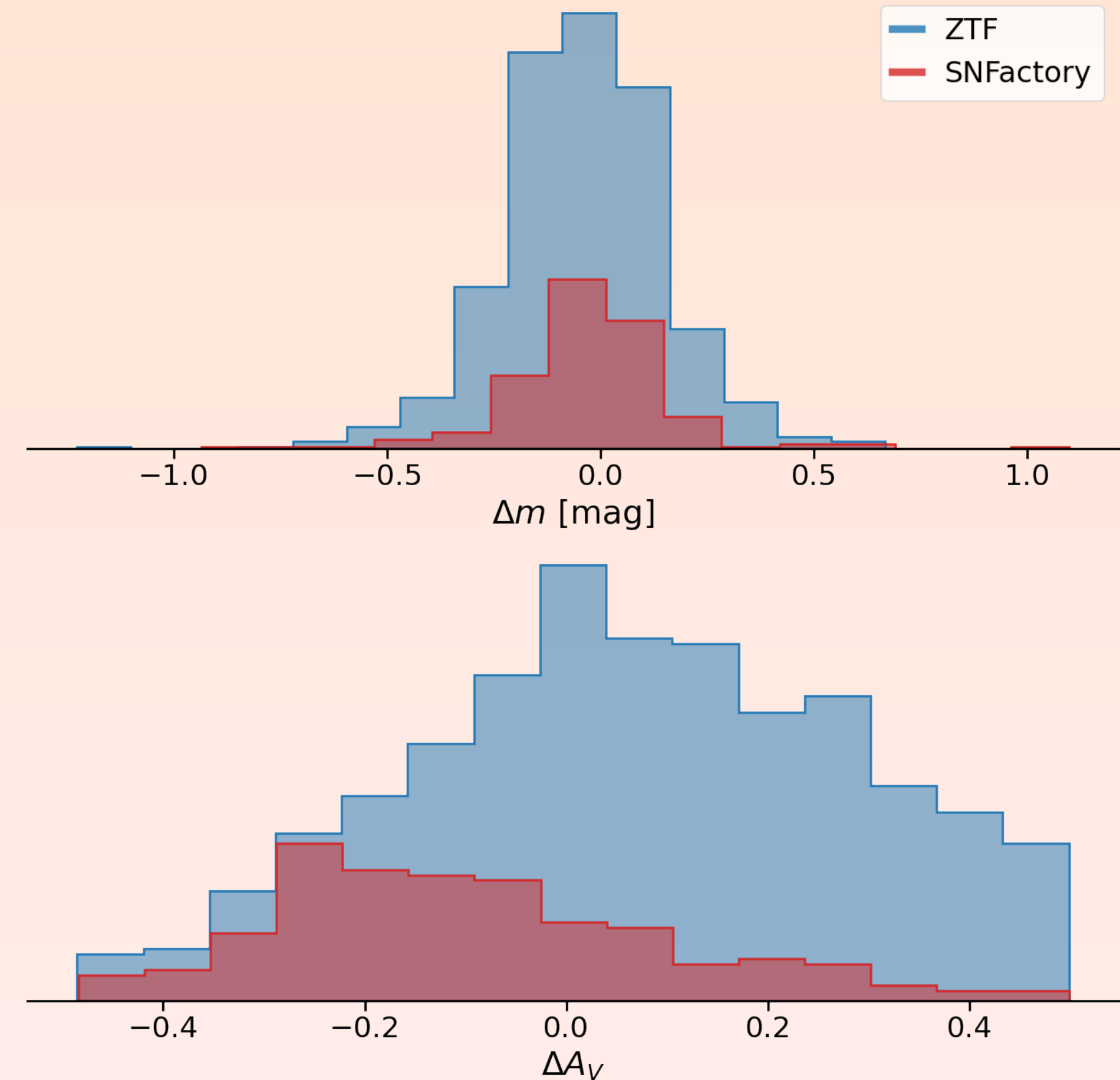


SNFactory spectra before/after dereddening, and residuals intrinsic dispersion (std) Credit : Boone et al. 2021

Twins Embedding on ZTF



ZTF spectra before/after dereddening,
and Spectral dispersion (nMAD)
after RBTL correction for **SNf** and **ZTF**



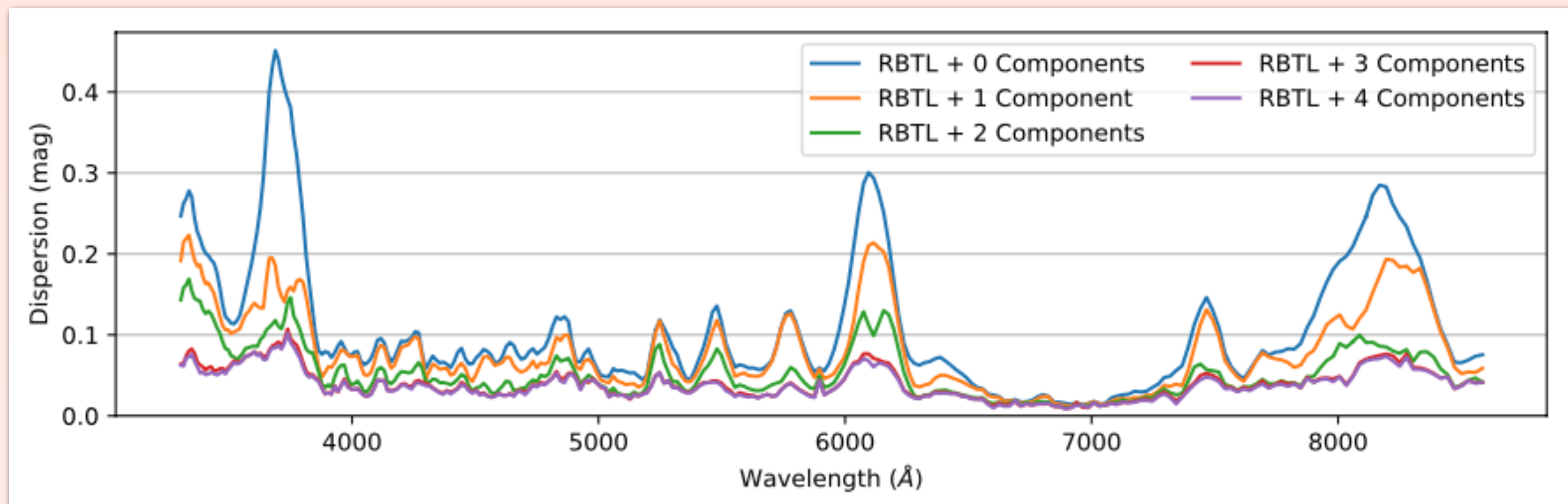
More red SNe in **ZTF** sample,
same distribution shape in magnitude

Twins Embedding - *Boone et al. 2021*

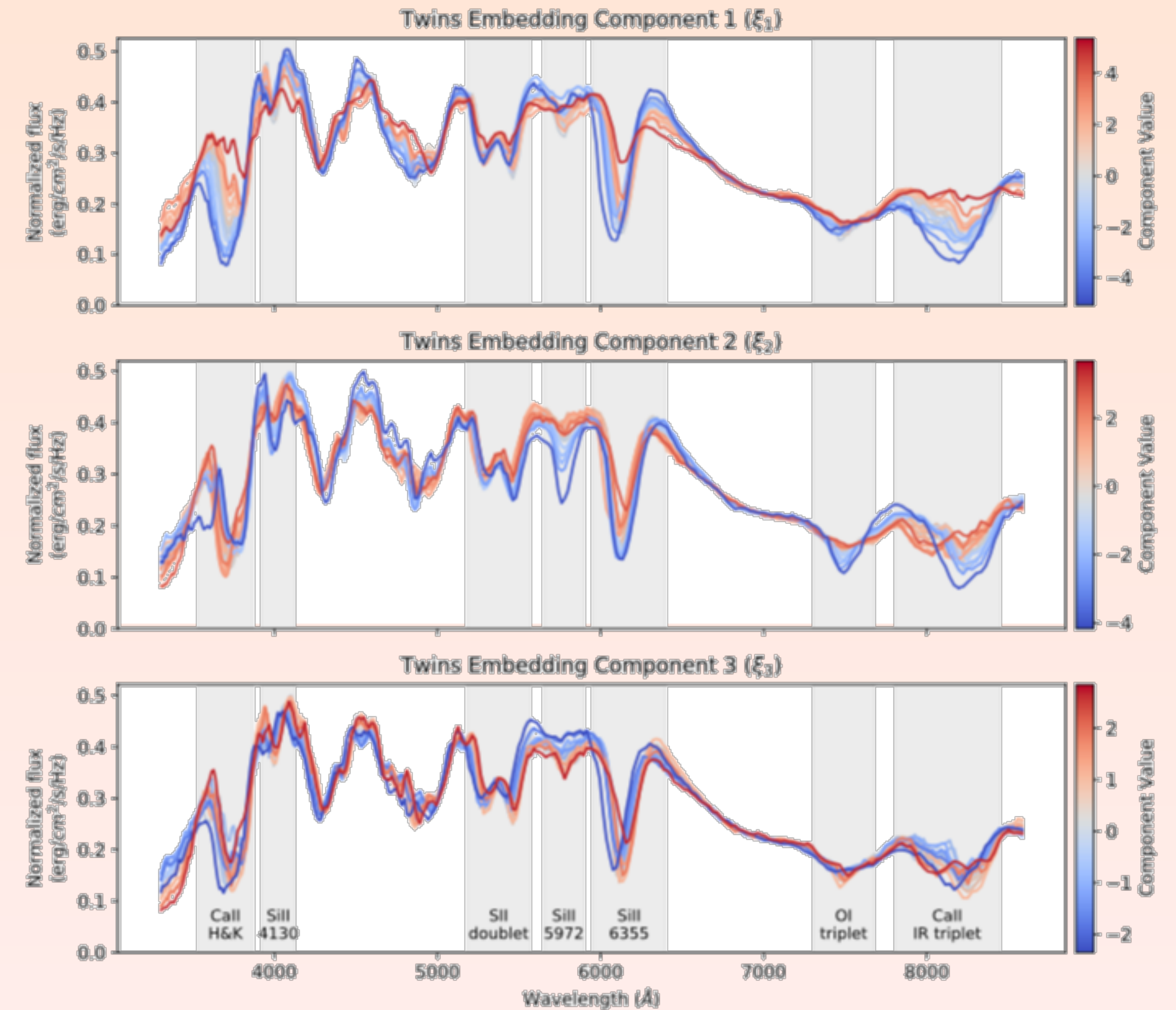
1. Generate at maximum luminosity
2. RBTL - *fit one offset and a color outside the lines*
3. Manifold Learning - *parameters reduction*

3 steps

87% of remaining variance explained with 3 components



SNFactory spectra fluxes STD, in function of wavelengths, for different numbers of Manifold Learning components : **parameter reduction.** *Credit : Boone et al. 2021*



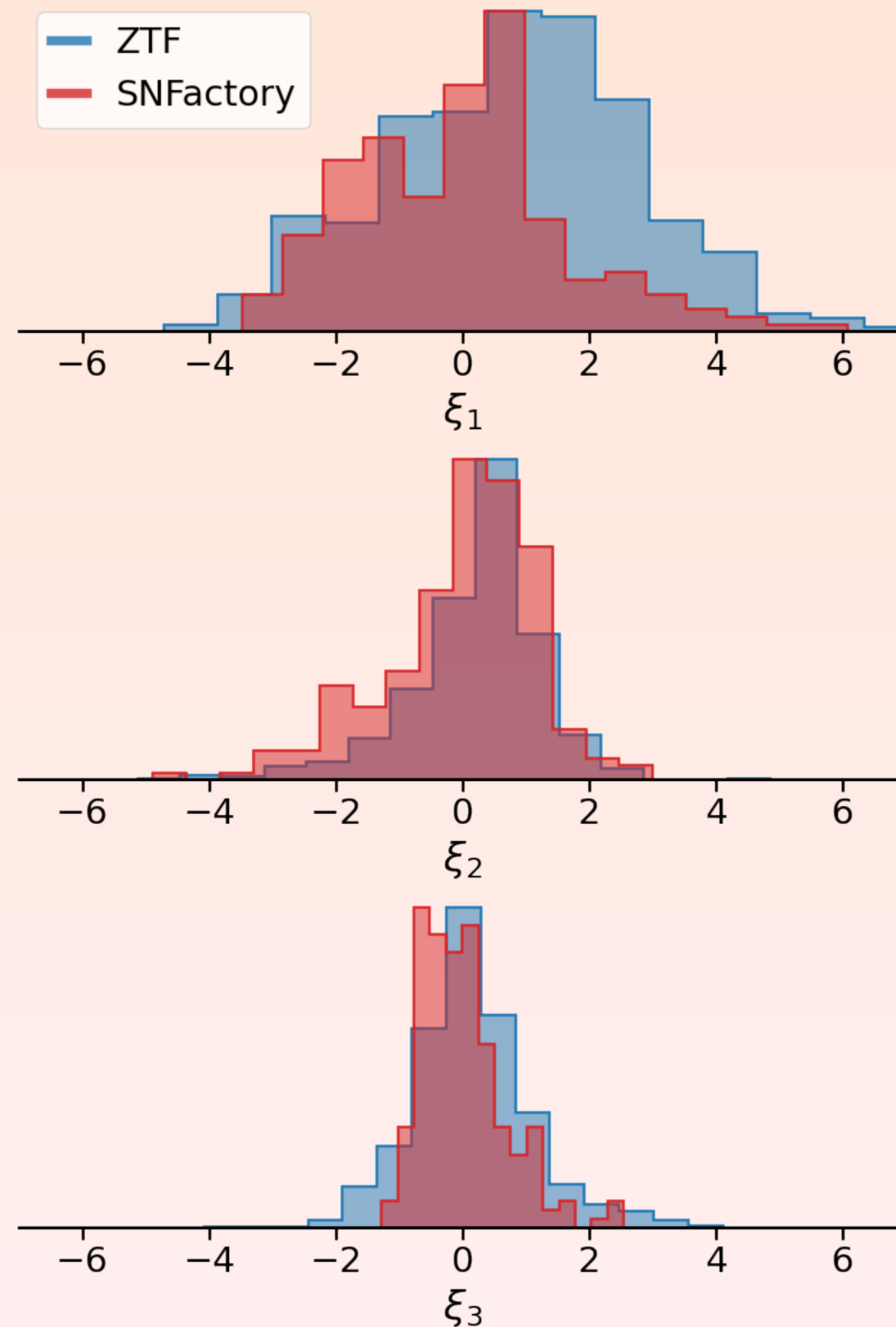
Twins Embedding components variation effects on spectra. *Credit : Boone et al. 2021*

Twins Embedding - Boone et al. 2021

3 steps

1. Generate at maximum luminosity
2. RBTL - fit one offset and a color outside the lines
3. Manifold Learning - parameters reduction

Normalised distributions
of Manifold components
for both ZTF and SNf



- ξ_2 matching
- Differences for ξ_1 and ξ_3 , and outliers have been removed

RBTL standardisation
linear correction

$$\mu = m^{max} - M^{max} - \alpha \cdot \Delta A_V$$

Manifold standardisation
(work in progress)

$$\mu = m^{max} - M^{max} - GP(\vec{\xi})$$

With SNFactory

Twins Embedding:
 $\sigma_{mag} = 0.07\text{mag}$

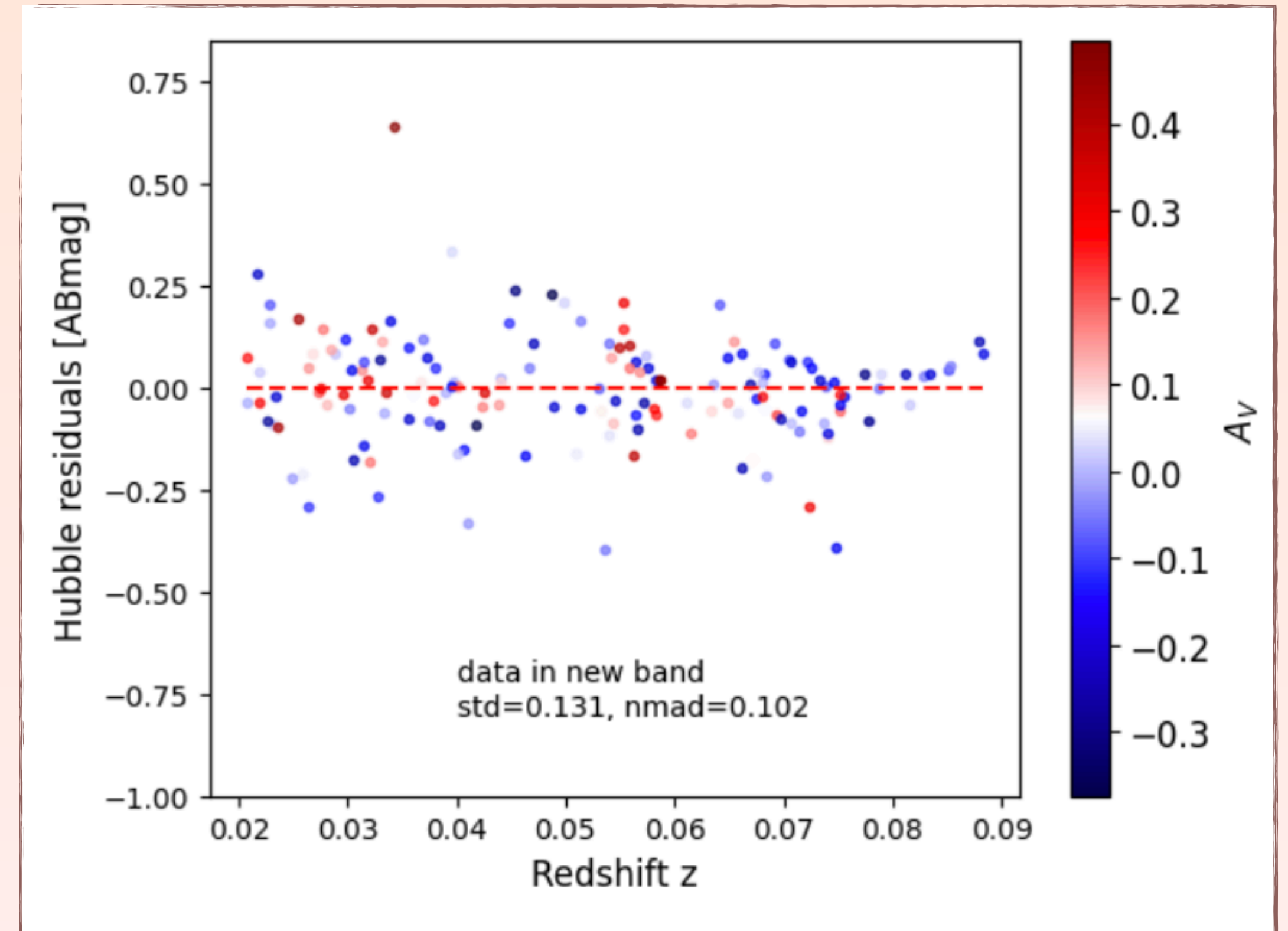
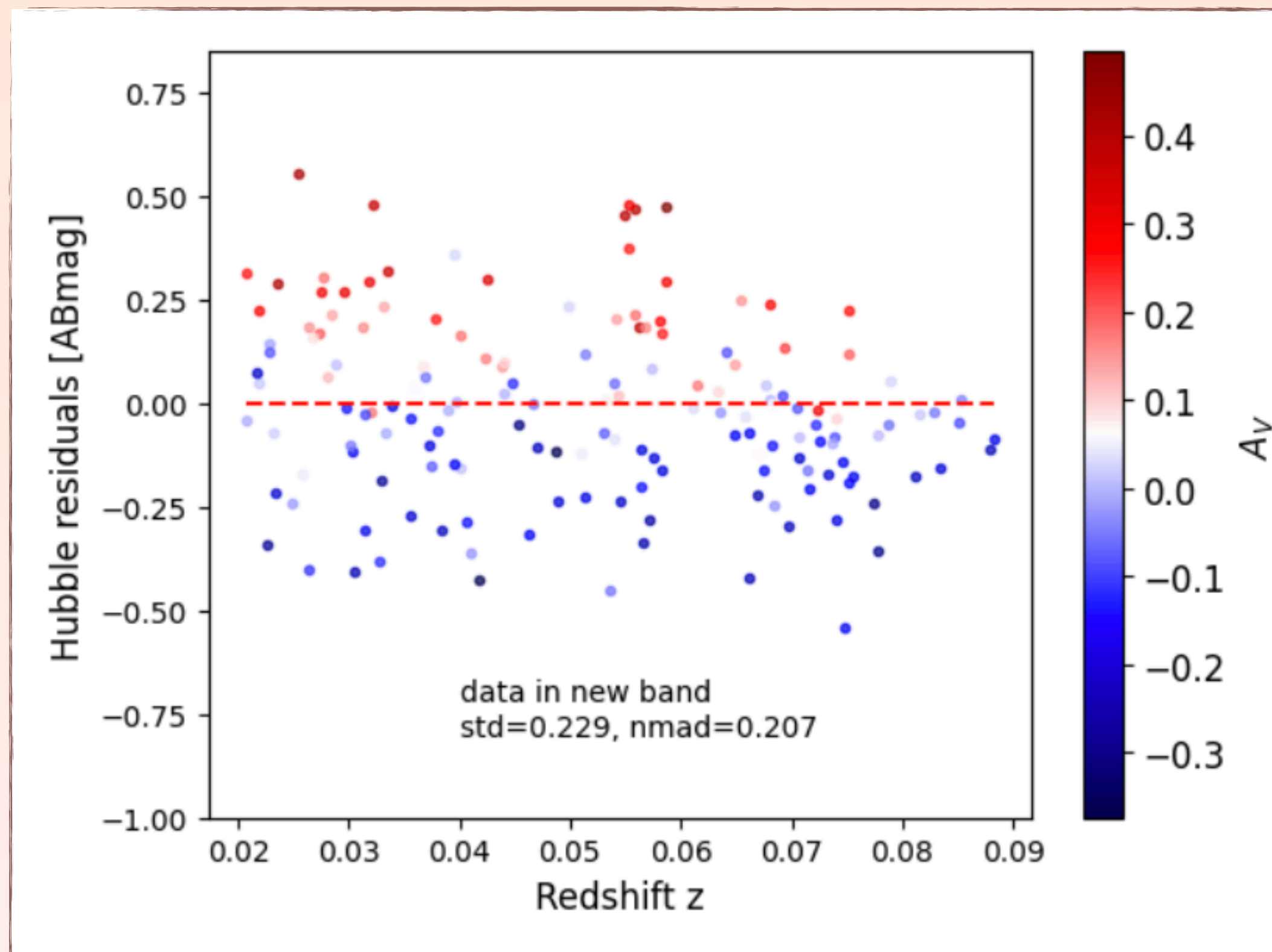
→ what with ZTF ?

RBTL linear standardisation

For SNFactory sample

$$\Delta\mu = \mu_{z=0.05} - (m_{band} - M_{offset})$$

$$-\alpha \cdot \Delta A_V$$



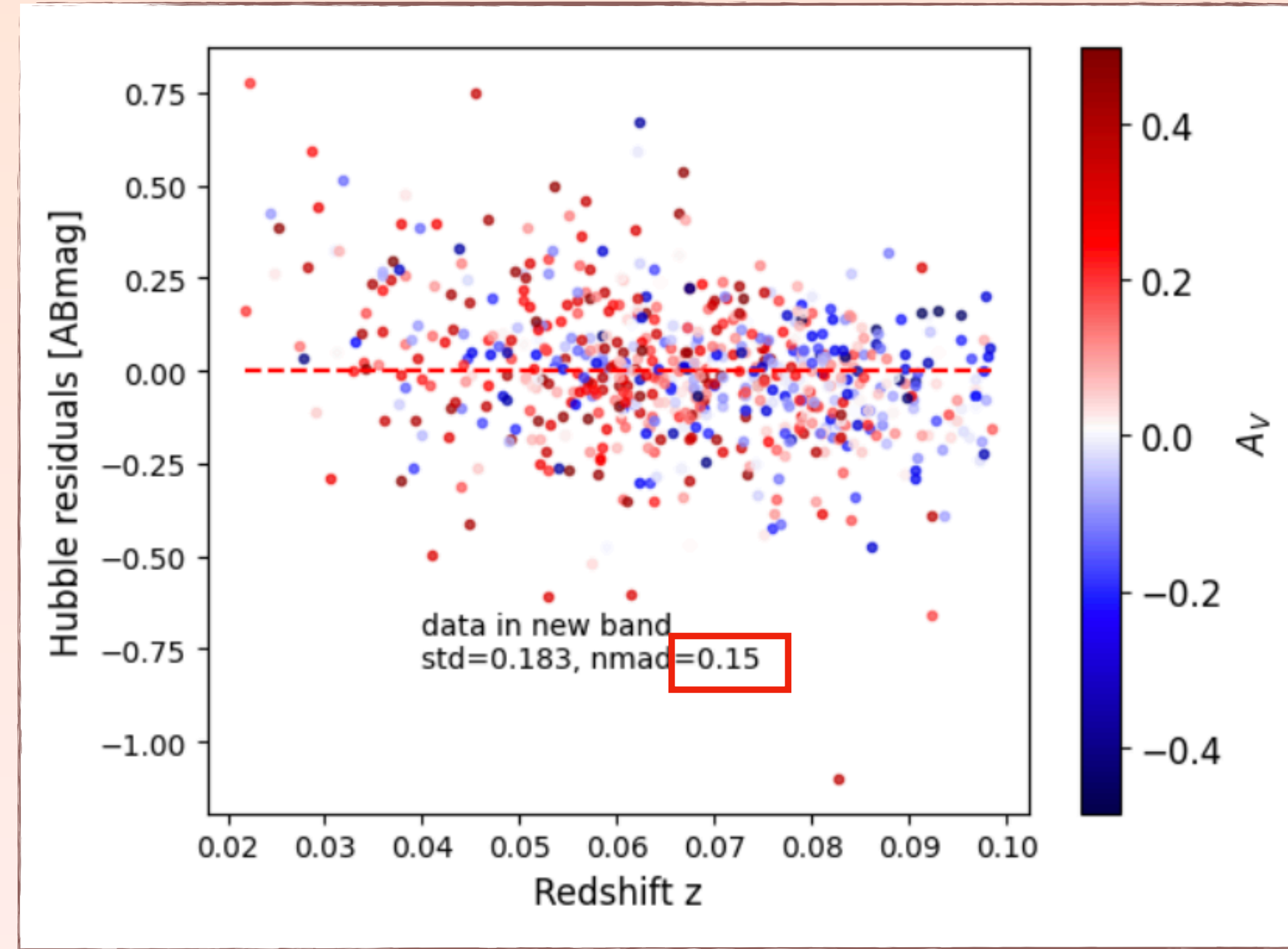
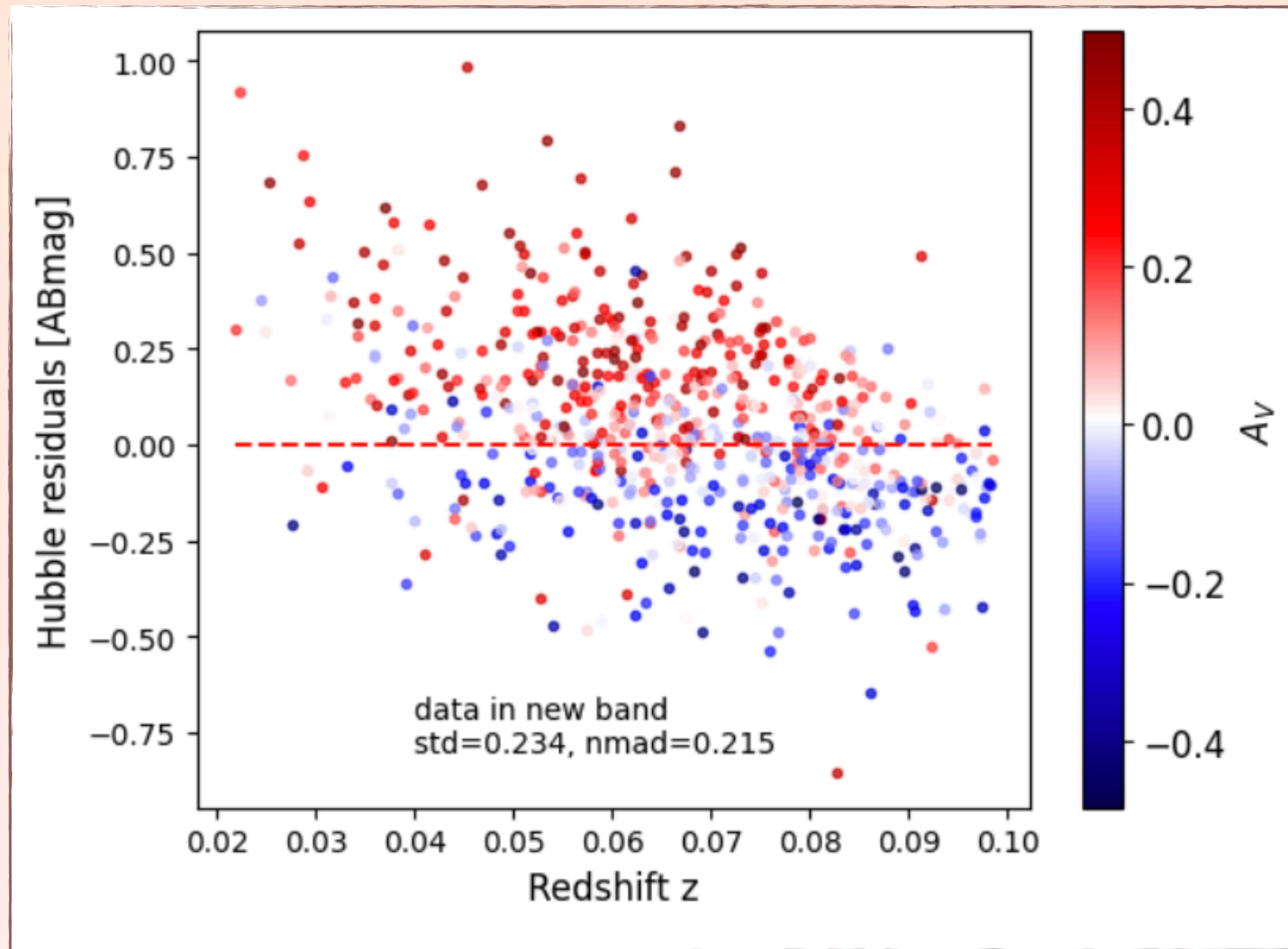
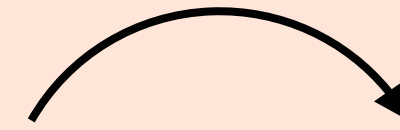
168 SNe Ia before/after standardisation
after a cut on $DA_V < 0.5$

RBTL linear standardisation

For ZTF sample

$$\Delta\mu = \mu_{z=0.05} - (m_{band} - M_{offset})$$

$$-\alpha \cdot \Delta A_V$$



647 SNe Ia before/after standardisation
after a cut on $DA_V < 0.5$ (remove around 7% SNe)

*Comparable dispersion that
photometric standardisation
with only 1 parameter*

Conclusion

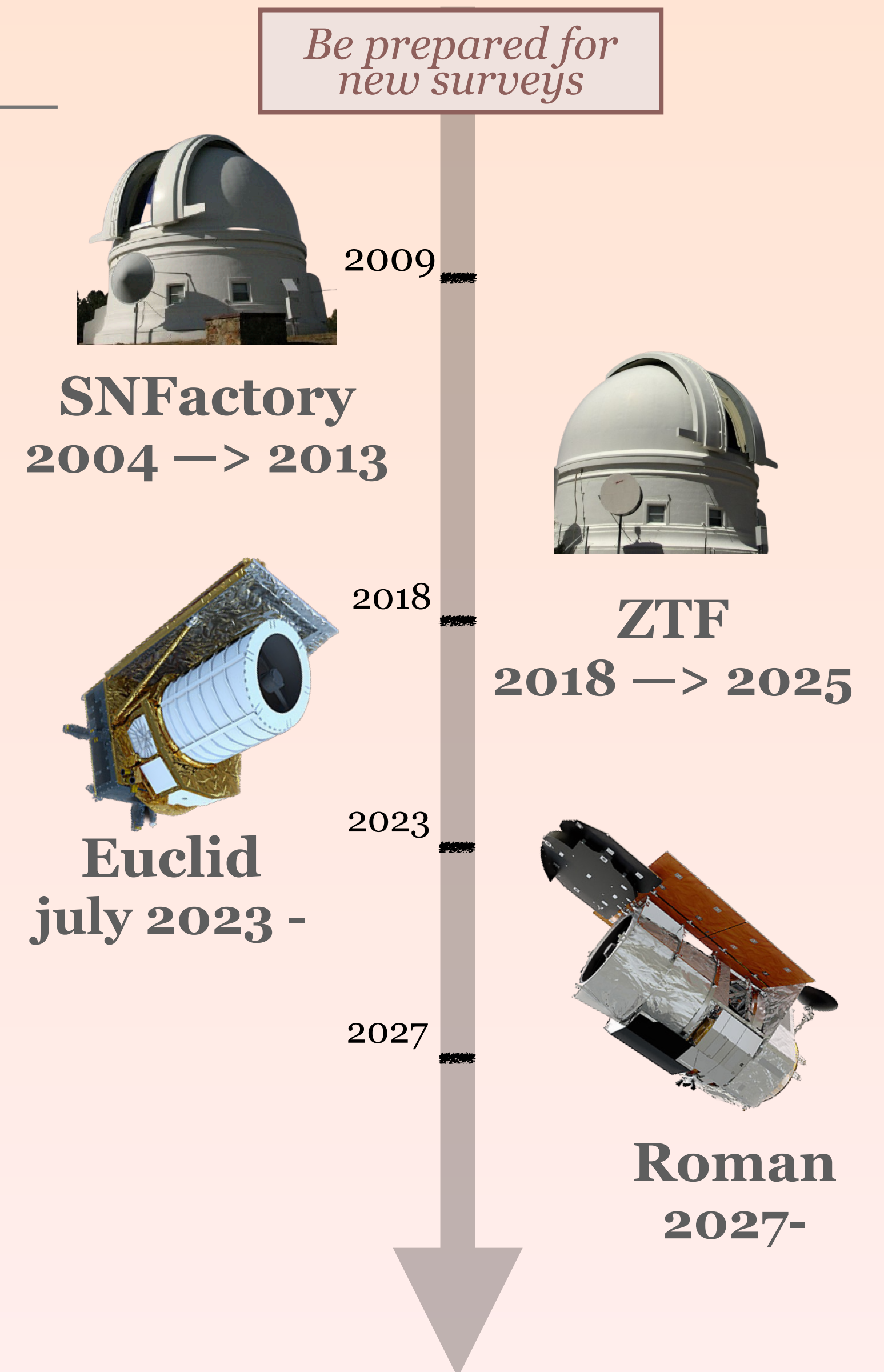
First application results

- RBTL standardisation is working well
- Manifold standardisation still in progress

PhD Calendar

- | | |
|-----------------|--|
| 1st year | Evaluation of Twins Embedding method on ZTF spectra |
| 2nd year | 1st paper on the results

2nd paper on a Hubble Diagram using ZTF and SNLS spectra and Twins Embedding |
| 3rd year | Cosmology with spectro-photometric standardisation |



Conclusion

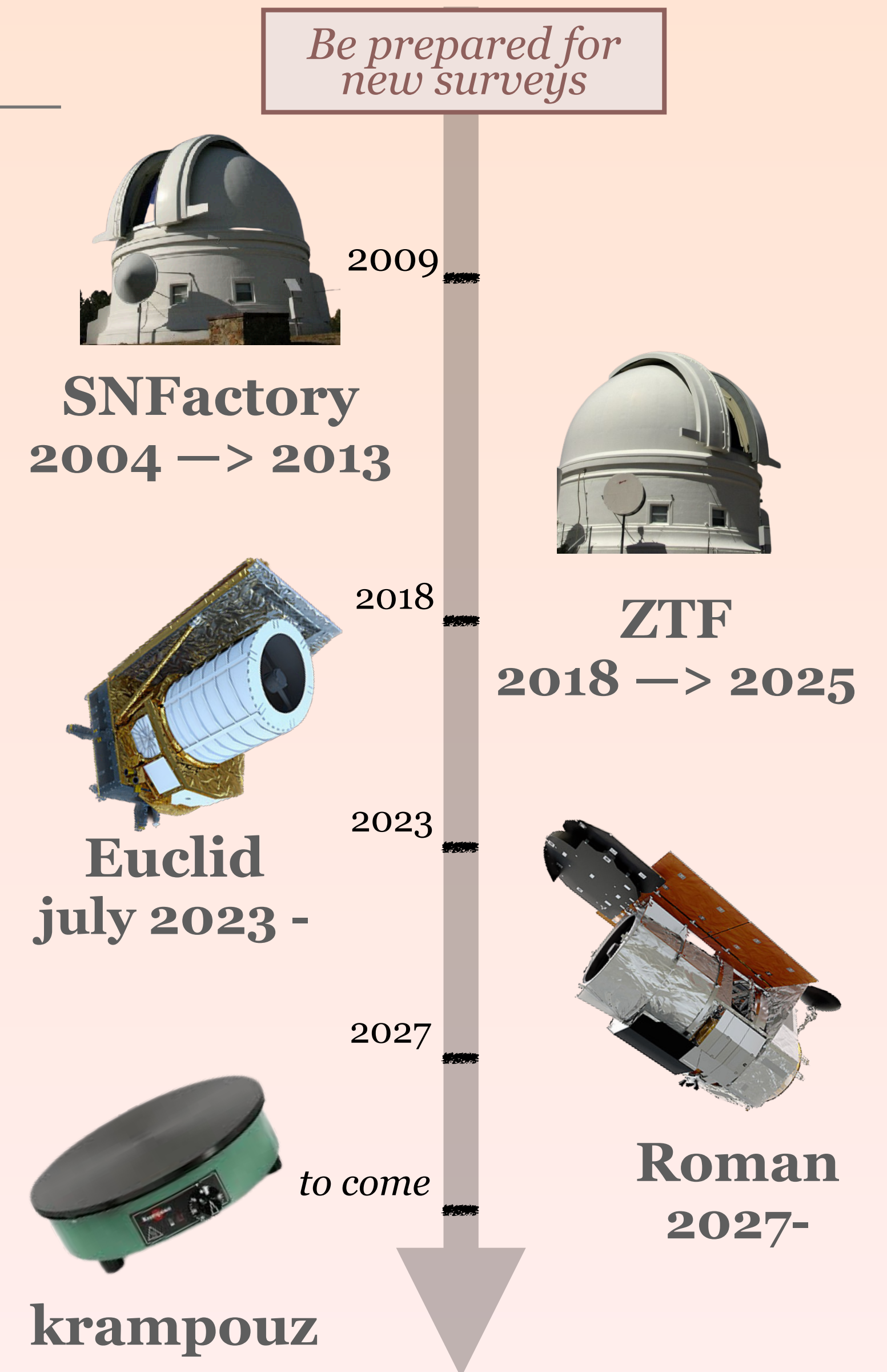
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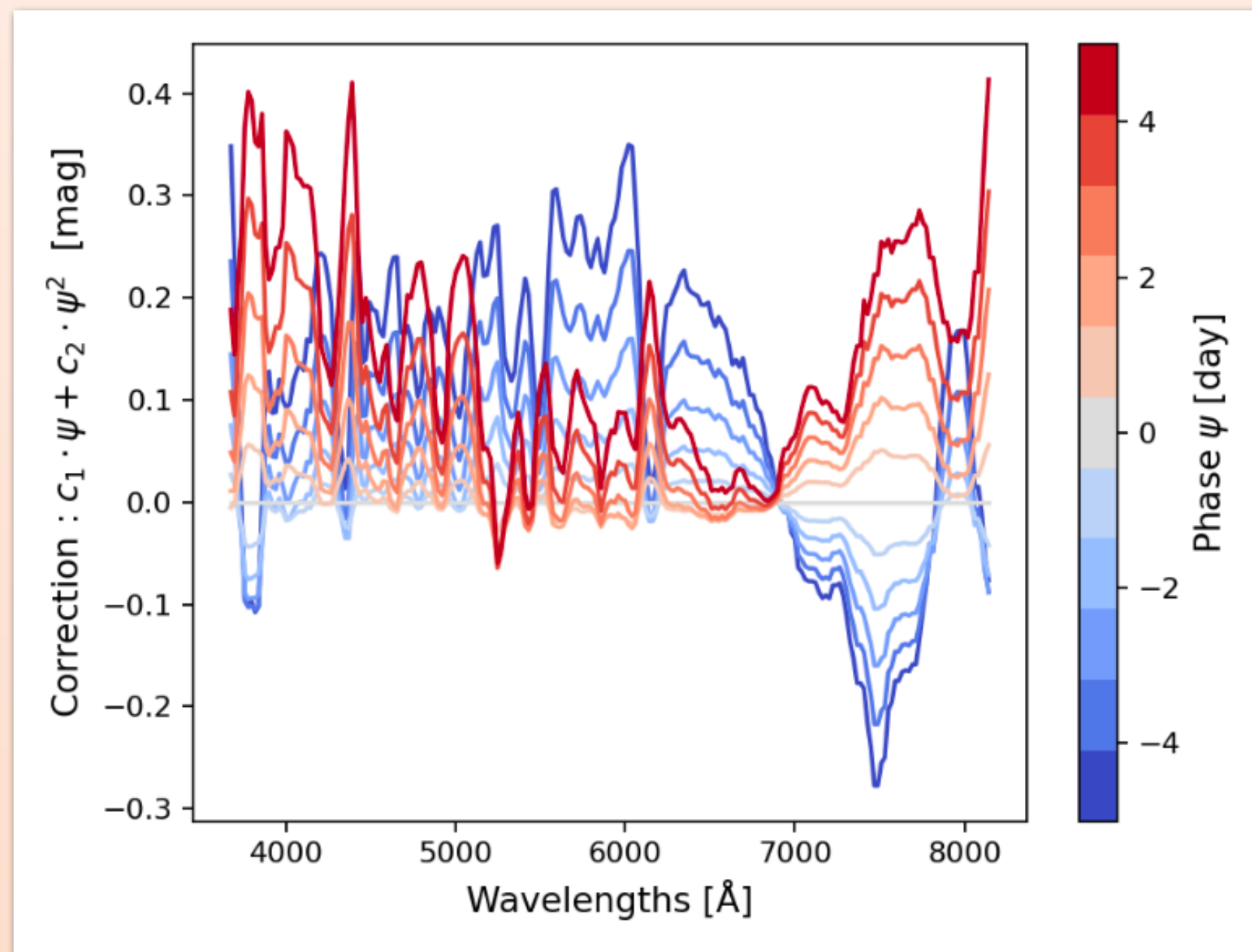
Formula of quadratic evolution in phase :

$$m_i(p; \lambda_k) - m_i(0; \lambda_k) = p \cdot c_1(\lambda_k) + p^2 \cdot c_2(\lambda_k)$$

with p the phase,

$c_{1,2}(\lambda_k)$ the coefficients common to all SNe

$m_i(p, \lambda_k)$ the magnitude of the SN i



Quadratic evolution in phase of SN Ia spectra

$$f_{\text{meas., } s}(p; \lambda_k) \sim N(f_s(p; \lambda_k); \sigma_{\text{tot., } s}^2(p; \lambda_k))$$

$$f_s(p; \lambda_k) = 10^{-0.4(m_i(p; \lambda_k) + m_{\text{gray}, s})}$$

$$\sigma_{\text{tot., } s}^2(p; \lambda_k) = \sigma_{\text{meas., } s}^2(\lambda_k) + (\epsilon(p; \lambda_k) \cdot f_s(p; \lambda_k))^2$$

Fitted parameters :

$f_s(p, \lambda_k)$ the model flux of spectrum s

$\epsilon(p, \lambda_k)$ the model uncertainties common to all SNe,

$m_{\text{gray}, s}$ the gray offset of the spectrum s

$c_{1,2}(\lambda_k)$ the coefficients common to all SNe

Known:

$f_{\text{obs}}(p, \lambda_k)$ the observed flux of spectrum s

Capture 84.6% of the spectral evolution variance common to every SNe between -5 and 5 days

Differential time evolution model

=> Spectra @ max

STEP 1

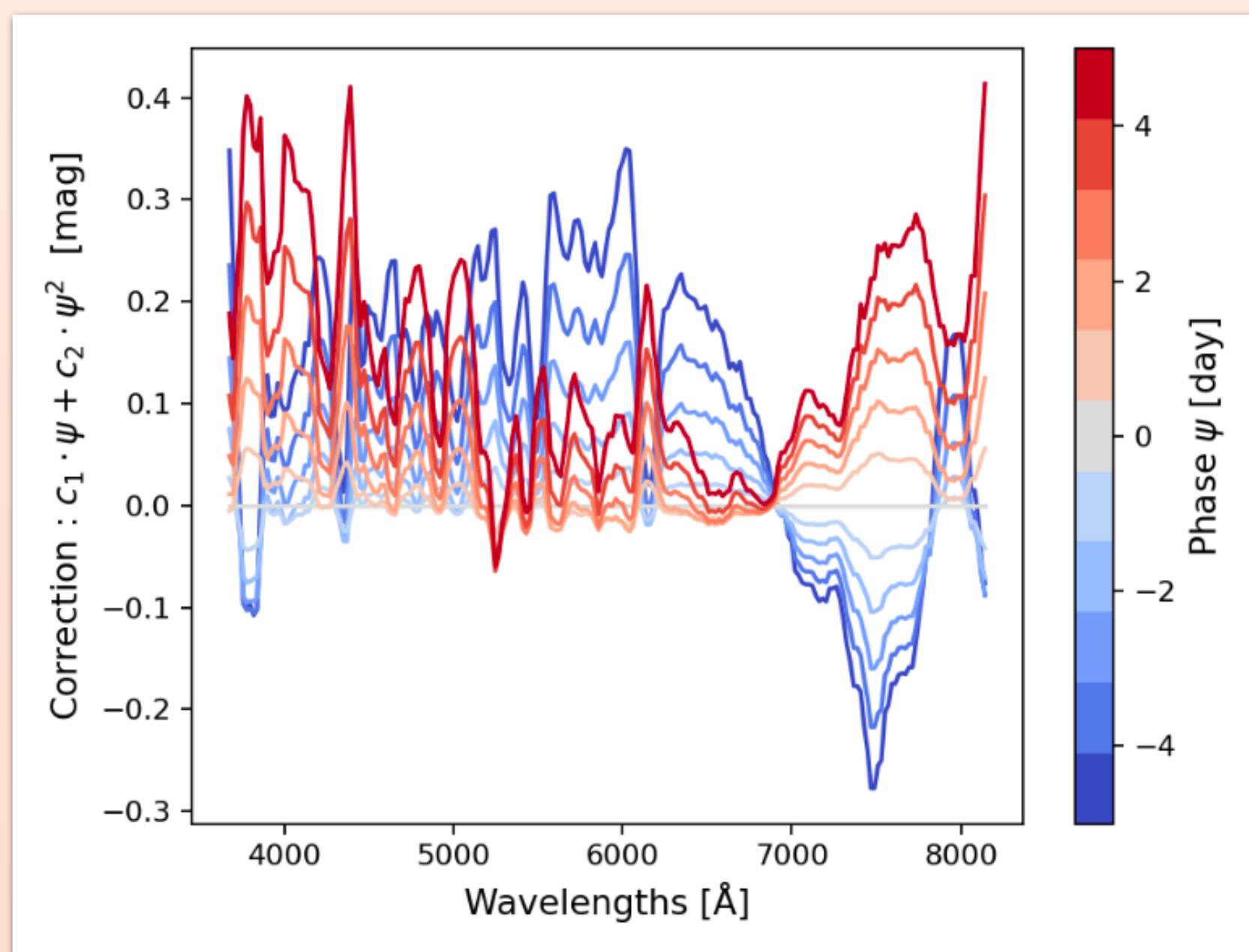
Formula of quadratic evolution in phase :

$$m_i(p; \lambda_k) - m_i(0; \lambda_k) = p \cdot c_1(\lambda_k) + p^2 \cdot c_2(\lambda_k)$$

with p the phase,

$c_{1,2}(\lambda_k)$ the coefficients common to all Sne

$m_i(p, \lambda_k)$ the magnitude of the SN i



Quadratic evolution in phase of SN Ia spectra

$$f_{meas.,s}(p; \lambda_k) \sim N(f_s(p; \lambda_k); \sigma_{obs.,s}^2(p; \lambda_k))$$

$$f_s(p; \lambda_k) = 10^{-0.4(m_i(p; \lambda_k) + m_{gray,s}^{tot.,s})}$$

$$\sigma_{tot.,s}^2(p; \lambda_k) = \sigma_{meas.,s}^2(\lambda_k) + (\epsilon(p; \lambda_k) \cdot f_s(p; \lambda_k))^2$$

Fitted parameters :

$\epsilon(p, \lambda_k)$ the model uncertainties common to all Sne,

$m_{gray,s}$ the gray offset of the spectrum s

$c_{1,2}(\lambda_k)$ the coefficients common to all Sne

Known:

$f_{meas.,s}(p, \lambda_k)$ the observed flux of spectrum s

$\sigma_{meas.,s}(\lambda_k)$ the measured uncertainty of sp. s

Capture 84.6% of the spectral evolution variance common to every Sne between -5 and 5 days

Differential time evolution model

=> Spectra @ max

STEP 1

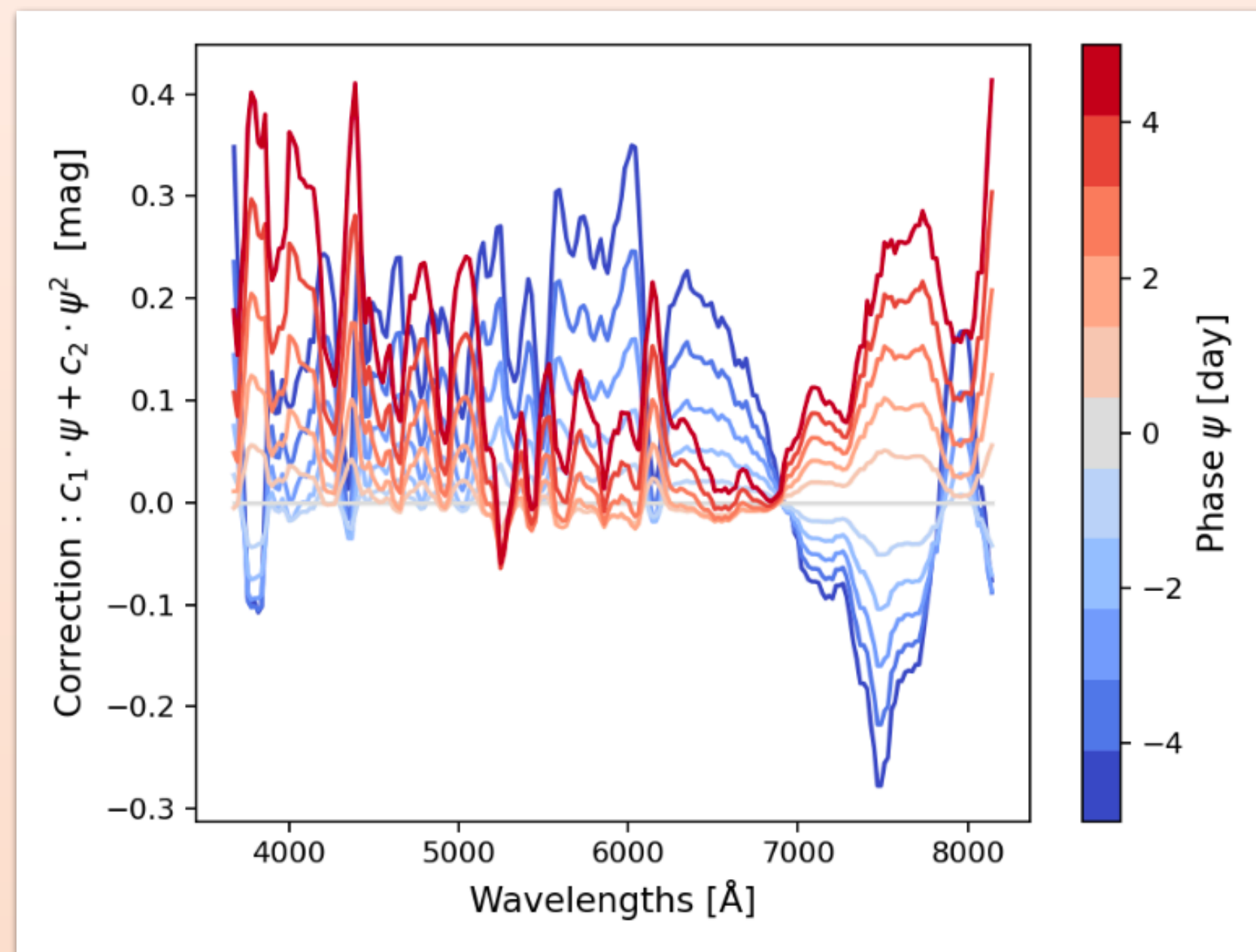
Formula of quadratic evolution in phase :

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with p the phase,

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Quadratic evolution in phase of SN Ia spectra

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$m_{gray,s}$ the gray offset of the spectrum s

$c_{1,2}(\lambda_k)$ the coefficients common to all Sne

Known:

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$\sigma_{meas.,s}(\lambda_k)$ the measured uncertainty of sp. s

Capture 84.6% of the spectral evolution variance common to every Sne between -5 and 5 days

Capture Grey scatter + Extinction

Remove variability:

- Magnitude offset (e.g peculiar velocity of host)
- Extinction (e.g Dust in the host)

Fitted parameters :

Δm_i the offset with mean for SN i

$\Delta \tilde{A}_{V,i}$ the extinction coefficient for SN i

$\eta(\lambda_k)$ the intrinsic dispersion (common to all)

Known:

$f_{max,i}(\lambda_k)/\sigma_{f_{max,i}}^2(\lambda_k)$ the spectrum flux/uncertainty at max for SN i

$f_{mean}(\lambda_k)$ the mean spectrum at max

$C(\lambda_k)$ the extinction law (Fitzpatrick 99)

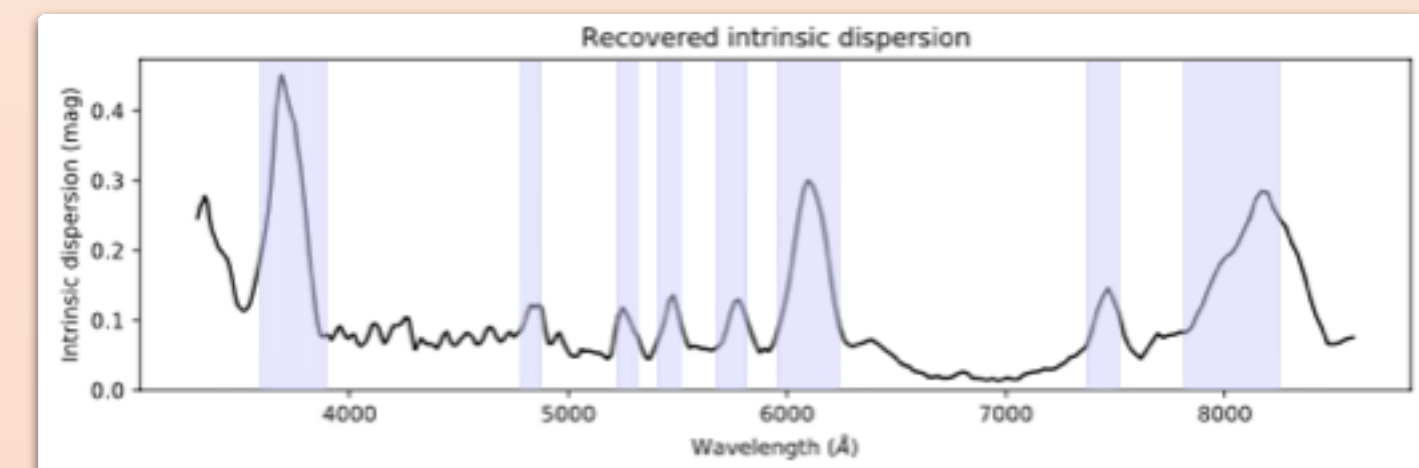
Fit all together with bayesian inference :

$$f_{\text{model},i}(\lambda_k) = f_{\text{mean}}(\lambda_k) \times 10^{-0.4(\Delta m_i + \Delta \tilde{A}_{V,i} C(\lambda_k))}$$

$$\sigma_{\text{total},i}^2(\lambda_k) = \sigma_{f_{\text{max},i}}^2(\lambda_k) + (\eta(\lambda_k) f_{\text{model},i}(\lambda_k))^2$$

$$f_{\text{max},i}(\lambda_k) \sim N(f_{\text{model},i}(\lambda_k); \sigma_{\text{total},i}^2(\lambda_k))$$

Areas with large intrinsic dispersion ($\eta(\lambda_k)$) are
deweight during the fit :



STEP 2

Read between the lines (RBTL)

=> *Explain Scatter
Between the lines*

Capture Grey scatter + Extinction

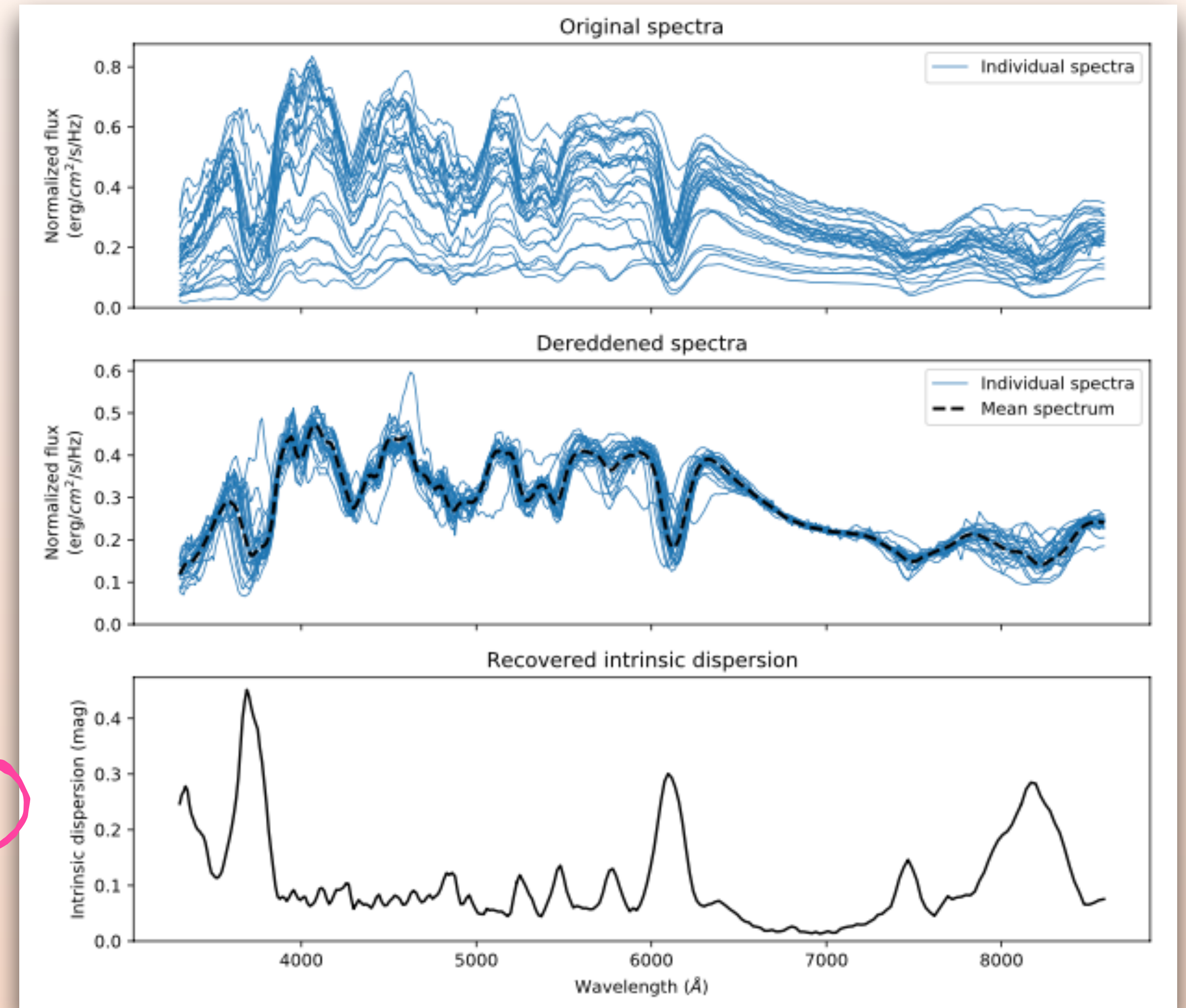
Remove variability:

- Magnitude offset (e.g peculiar velocity of host)
- Extinction (e.g Dust in the host)

$$f_{\text{dered.,}i}(\lambda_k) = f_{\text{max.,}i}(\lambda_k) \times 10^{+0.4(\Delta m_i + \Delta \tilde{A}_{V,i} C(\lambda_k))}$$

$\eta(\lambda_k)$

Areas with large intrinsic dispersion ($\eta(\lambda_k)$) are
deweight during the fit



*SNFactory spectra before/after dereddening, and
residual intrinsic dispersion (std) - from Boone 2021*

STEP 2

Read between the lines (RBTL)

=> *Explain Scatter
Between the lines*

Capture Grey scatter + Extinction

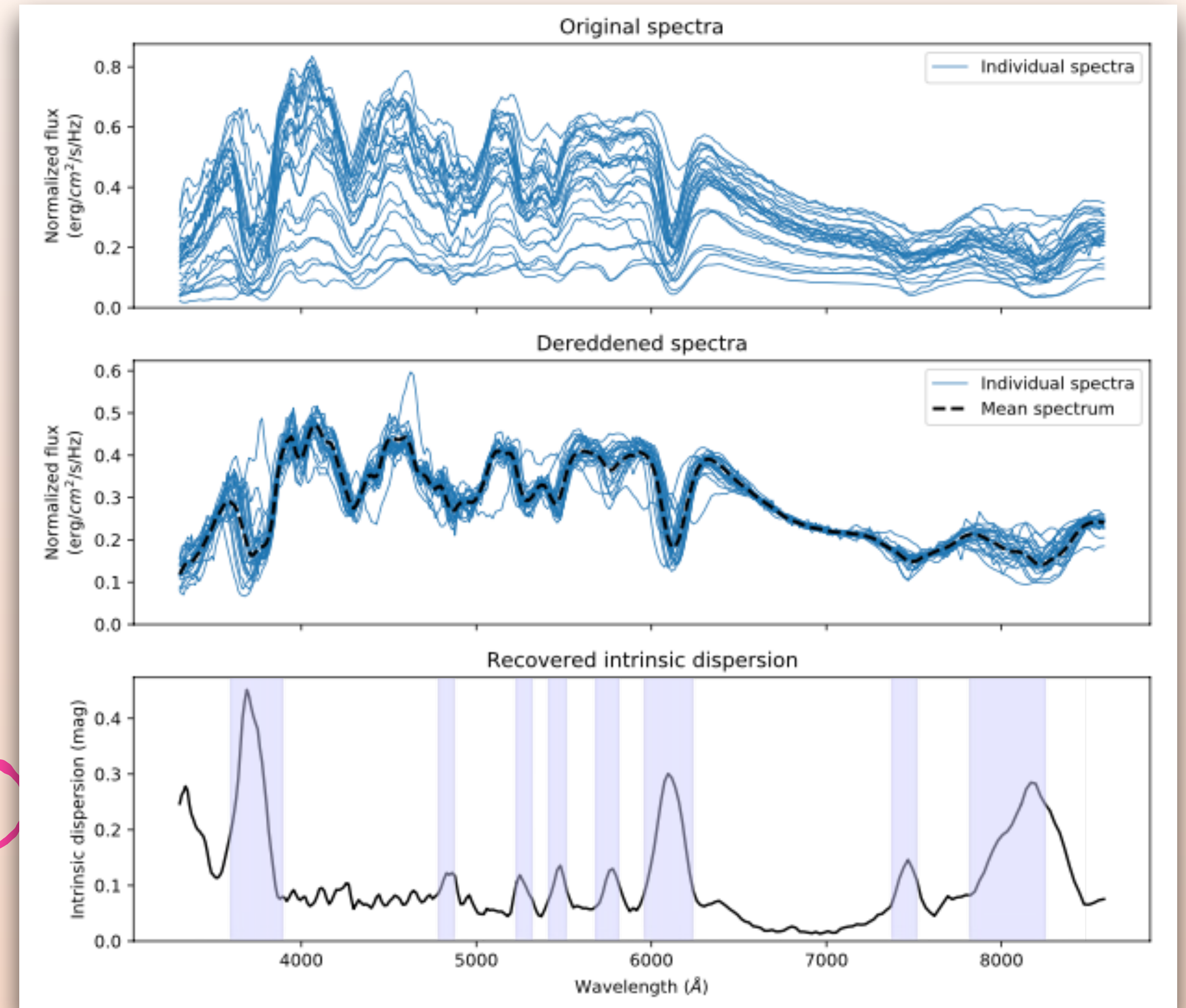
Remove variability:

- Magnitude offset (e.g peculiar velocity of host)
- Extinction (e.g Dust in the host)

$$f_{\text{dered.,}i}(\lambda_k) = f_{\text{max.,}i}(\lambda_k) \times 10^{+0.4(\Delta m_i + \Delta \tilde{A}_{V,i} C(\lambda_k))}$$

$\eta(\lambda_k)$

Areas with large intrinsic dispersion ($\eta(\lambda_k)$) are
deweight during the fit



*SNFactory spectra before/after dereddening, and
residual intrinsic dispersion (std) - from Boone 2021*

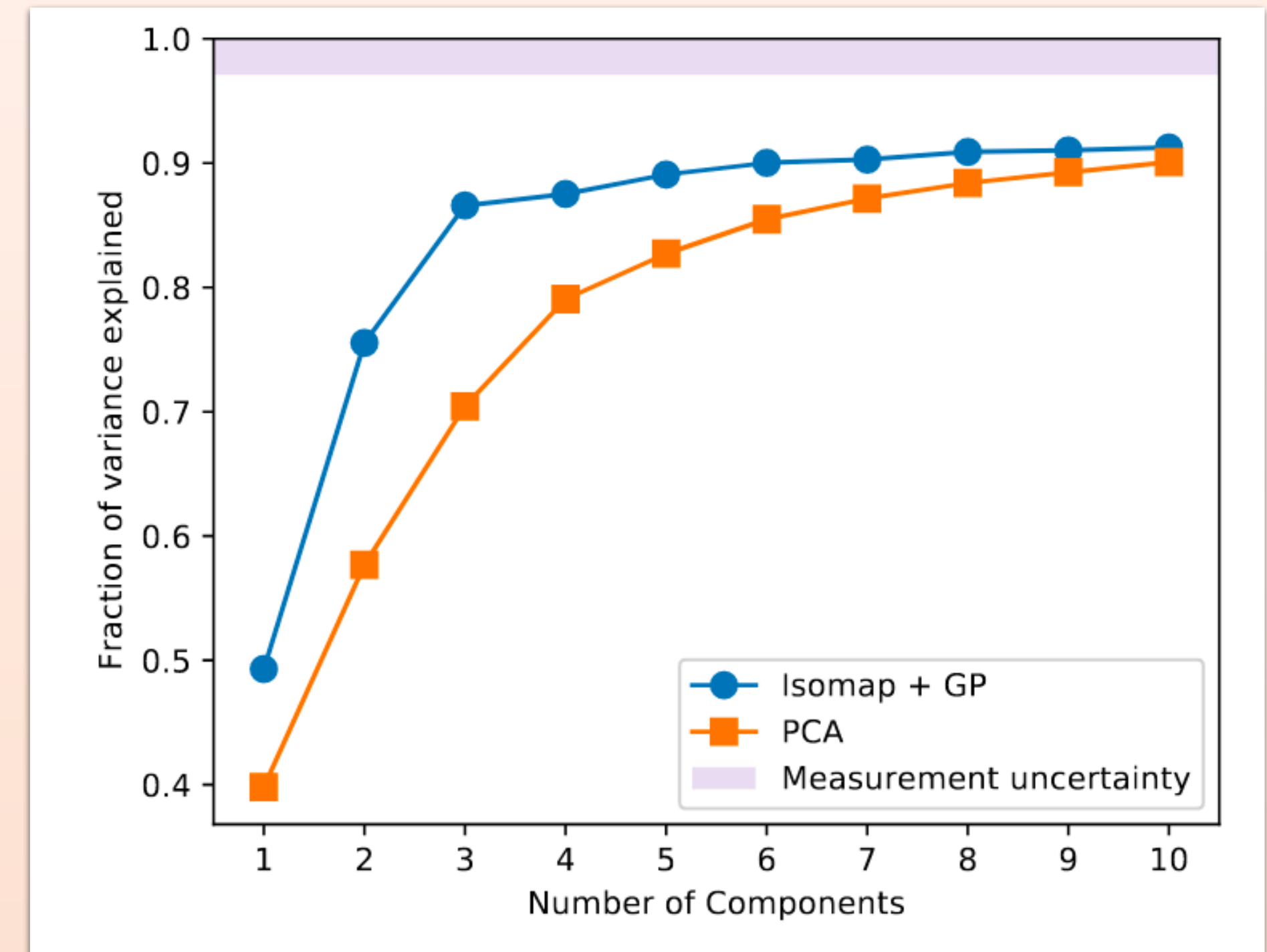
Spectral distance between two SNE i and j :

$$\gamma_{ij} = \sqrt{\sum_k \left(\frac{f_{\text{dered.},i}(\lambda_k) - f_{\text{dered.},j}(\lambda_k)}{f_{\text{mean}}(\lambda_k)} \right)^2}$$

Isomap algorithm embed high-dimensional space to low-dimensional while preserving distances

But it does not provide a model of a spectrum given its coordinates in the embedding : for that they use Gaussian Process

86.6% of variance explained with 3 components



Fraction of the variance explained for different models - from Boone 2021

STEP 3

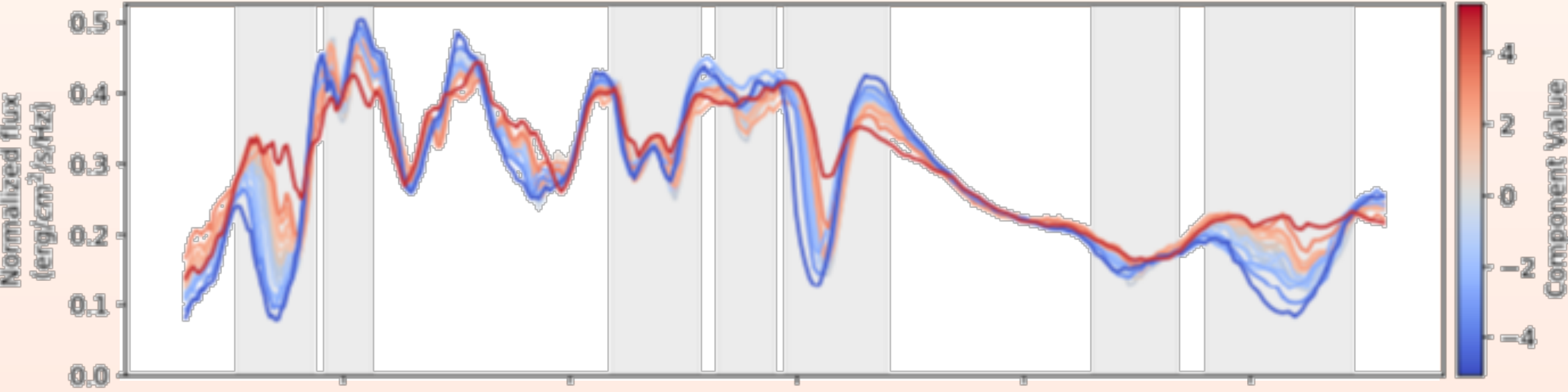
The Twins Embedding parameters space

=> Explain

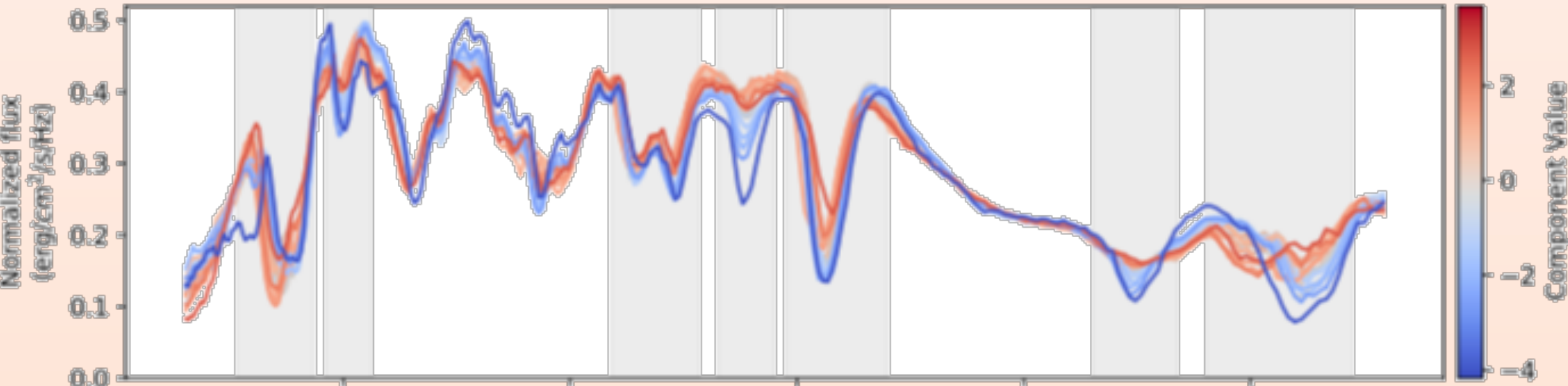
$$\eta(\lambda_k)$$

TWINS EMBEDDING I

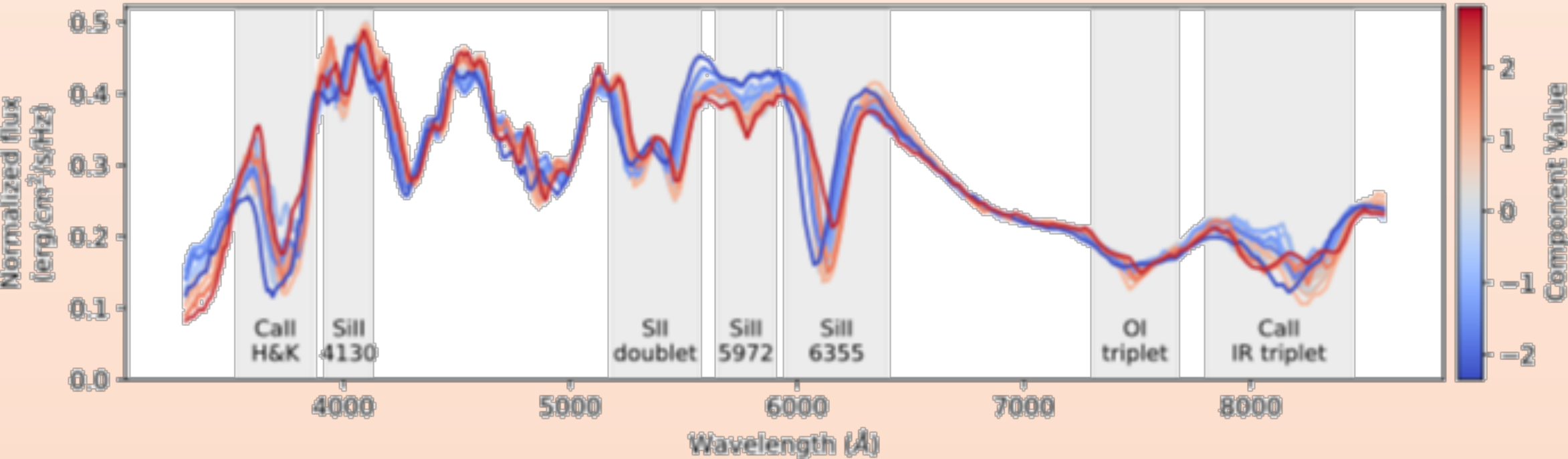
Twins Embedding Component 1 (ξ_1)



Twins Embedding Component 2 (ξ_2)

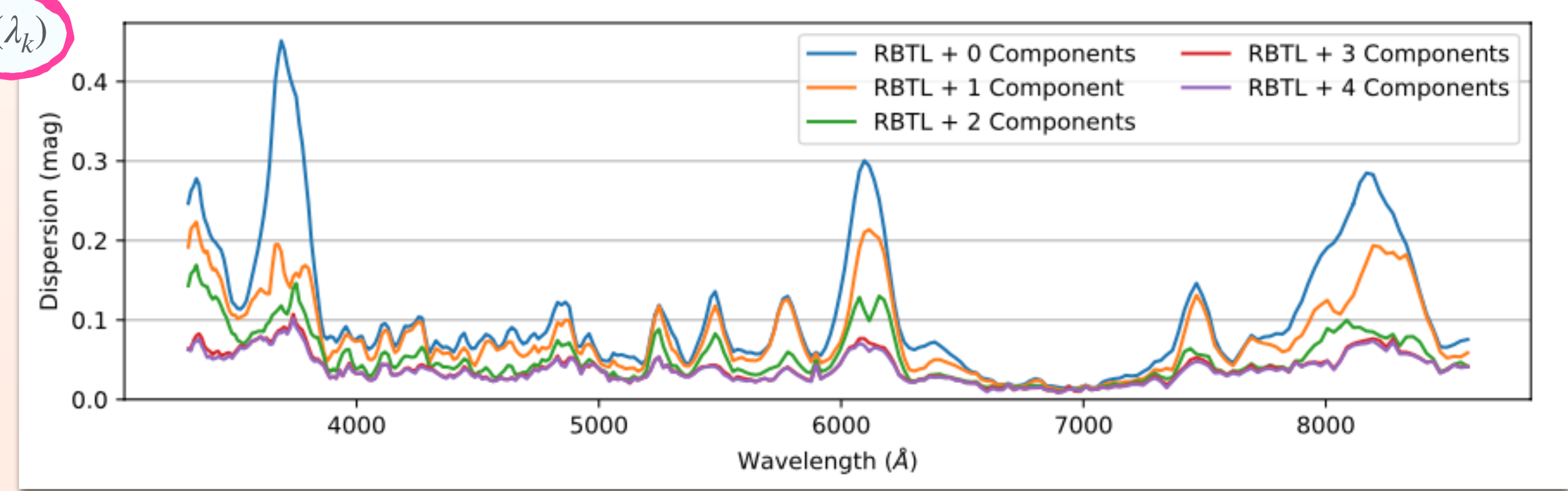


Twins Embedding Component 3 (ξ_3)



Twins Embedding three components variation effects
Figure from Boone 2021

$$\eta(\lambda_k)$$



From **K.Boone et al. 2021**. SN Factory spectra fluxes STD, in function of wavelengths, for different numbers of Manifold Learning components (parameters reduction)

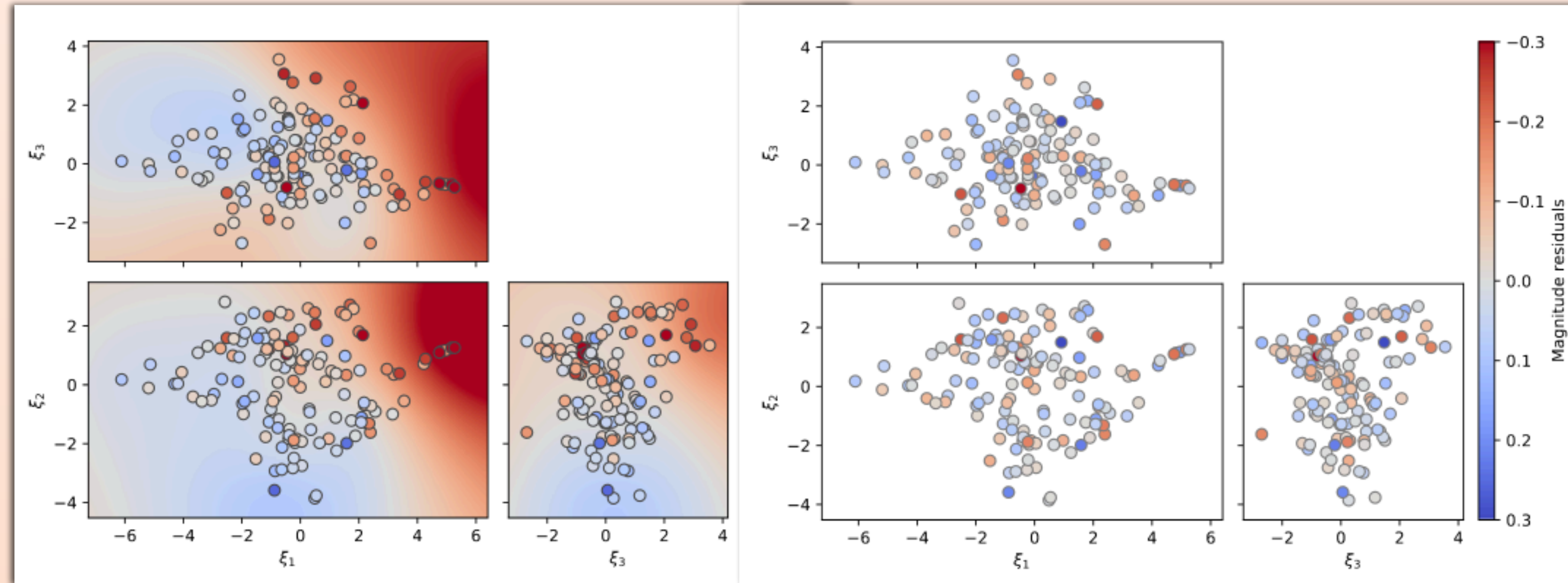
	ξ_1	ξ_2	ξ_3
Added noise, S/N = 20	0.99	0.98	0.96
Added noise, S/N = 10	0.97	0.96	0.89
Added noise, S/N = 5	0.94	0.88	0.79
Added noise, S/N = 2	0.68	0.12	0.22
Binning 2000 km/s	1.00	1.00	1.00
Binning 5000 km/s	1.00	0.99	0.97
Binning 10000 km/s	0.99	0.98	0.90

Dependancy of the variance explained with S/N and binning

The standardisation using Twins Embedding

To map the magnitude residuals through the TE space : linear standardisation not sufficient, instead Gaussian Process regression :

$$\vec{m}_{\text{RBTL}} \sim \mathcal{GP} \left(m_{\text{ref}} + \omega \Delta \vec{A}_V, \mathbf{I} \cdot (\vec{\sigma}_{\text{p.v.}}^2 + \sigma_u^2) + K_{3/2}(\vec{\xi}, \vec{\xi}; A, l) \right)$$



**Before/after correction of magnitude residuals with GP
from Boone 2021b**

Fitted parameters :

m_{ref} a common reference magnitude

ω a linear correction term

σ_u the unexplained residual dispersion

A, l the GP kernel parameters

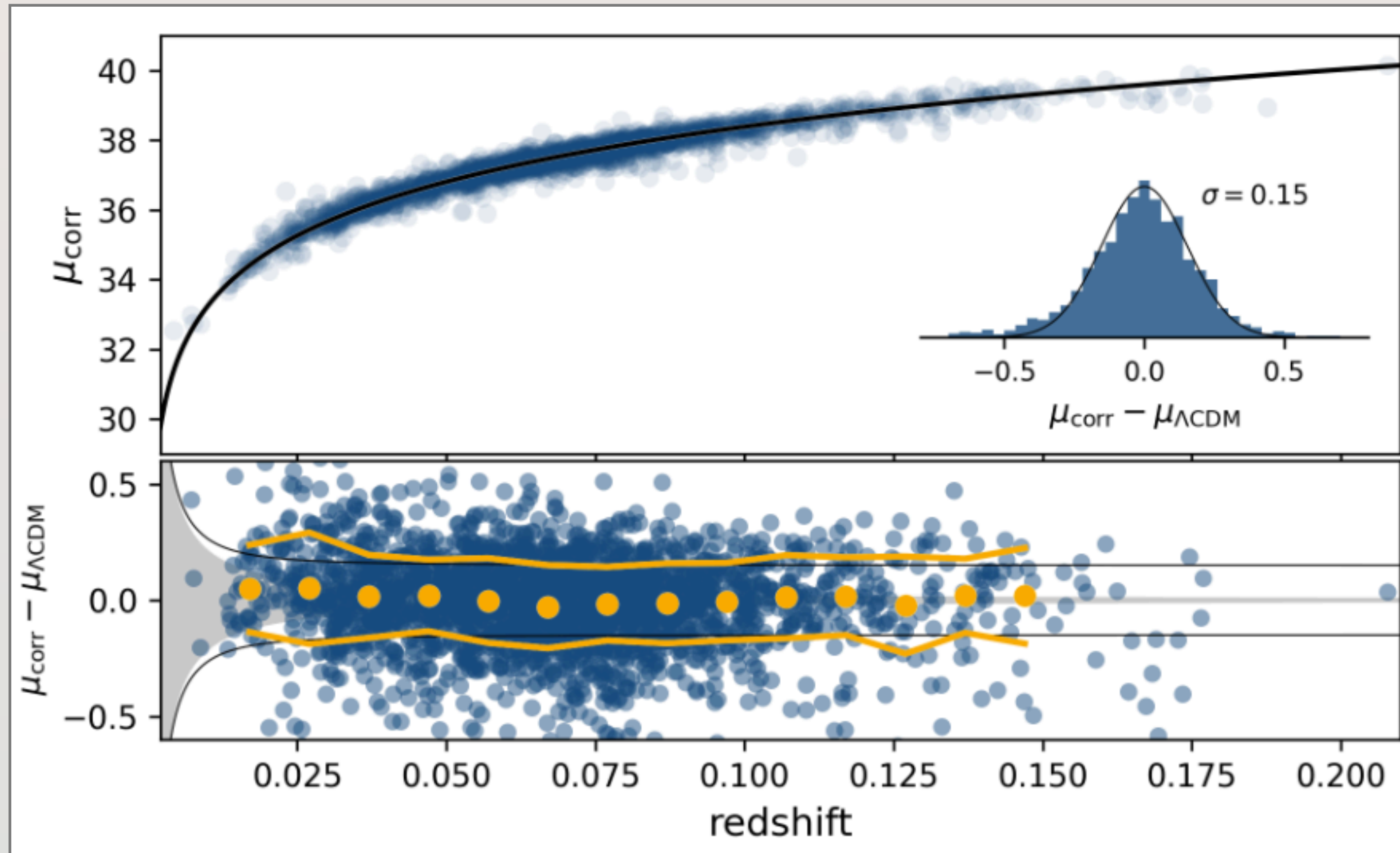
Known :

\vec{m}_{RBTL} the magnitudes residuals of the RBTL ,

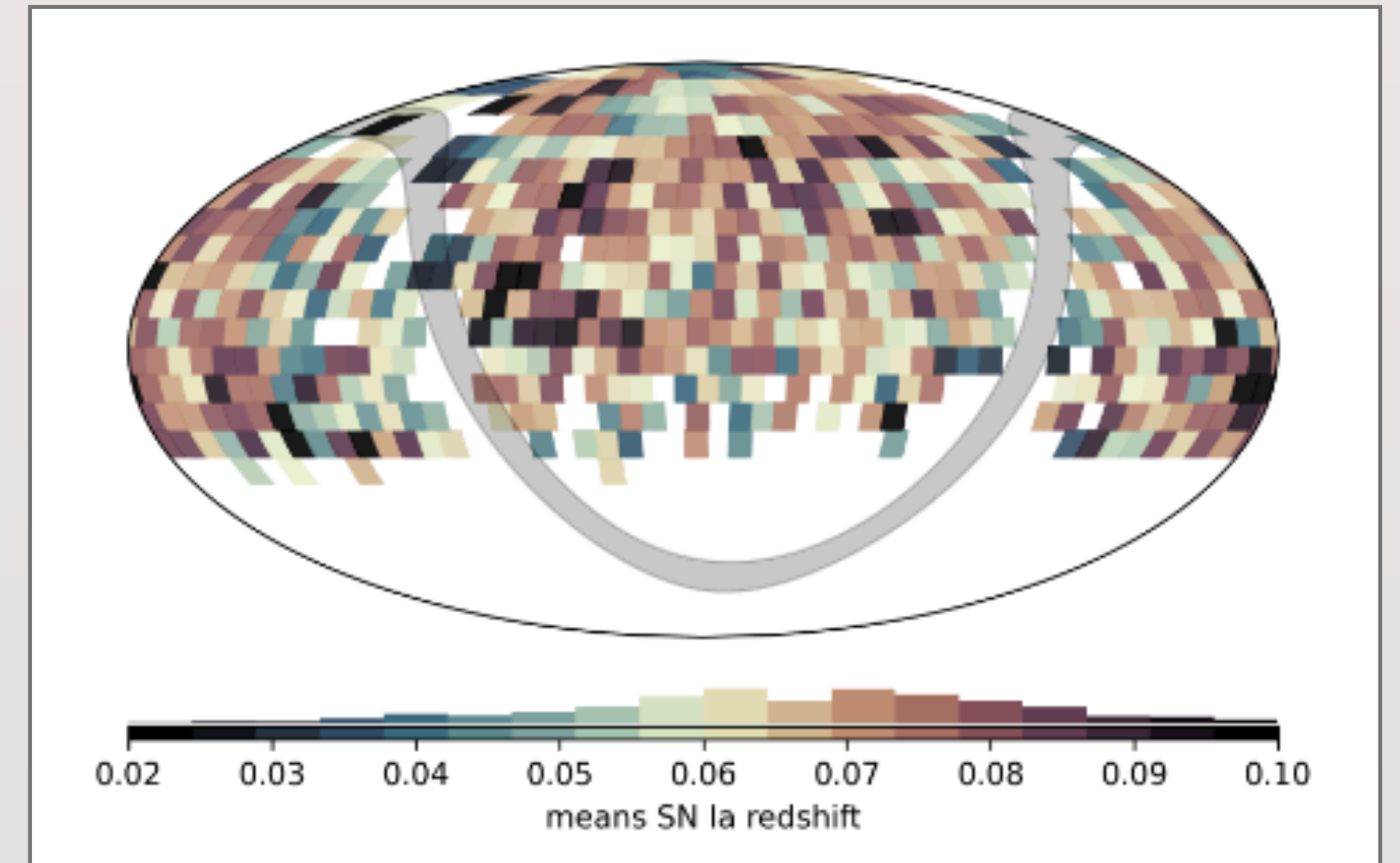
$\vec{\Delta A}_V$ the reddening coefficients ,

$\vec{\xi}$ the coordinates in the TE space,

$\vec{\sigma}_{\text{p.v.}}^2$ the host galaxy peculiar velocity variance



2622 standardized SNe Ia, after minimal cuts
 Credit : ZTF “DR2” Overview paper, Rigault et al.



Sky Map of the **2663** SNe Ia redshifts
 Credit : in prep. ZTF “DR2” Data paper, Smith et al.