



# *A causal perspective on reliable and interpretable representation learning*

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#### Artificial Intelligence (AI) has challenges ahead High hopes for AI to transform all economic sectors.

But many technical, strategic and societal issues ahead:

- reliability and ethical issues;
- data and compute requirements;
- pressure on resources and sustainability.

The ugly truth behind ChatGPT: AI is guzzling resources at planet-eating rates Mariana Mazzucato *[The Guardian, May 30th 2024]*

We need general frameworks to address these issues. *Causality* allows to:

- phrase rigorously meaningful requirements for AI,
- derive theoretical guaranties for them,
- formulate problems and explanations in a language understandable by humans.

### What is causality about?

• Representing knowledge about the world *and how it can be changed*.





- Specificity : **Modularity** of the system
- Modules are called "mechanisms"



### What is causality about?

• Representing knowledge about the world *and how it can be changed*.



- Specificity : **Modularity** of the system
- Modules are called "mechanisms"
- $\triangleright$  Make plausible changes to a mechanism to: ➢Explain "why things happen",
	- ➢Make predictions.



**Causal graph** 

*Show the influence of variables on each other*

**Mechanisms = "Structural assignments"**  *Computes child node value as a function of parents*

$$
X_1 := f_{1,\theta_1}(\epsilon_1) \qquad \text{Independent} \\ X_2 := f_{2,\theta_2}(X_1, \epsilon_2) \qquad \text{variables} \\ X_3 := f_{3,\theta_3}(X_1, X_2, \epsilon_3)
$$

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$$

animal **given background**



Probability of



Samples of object-background combination images.

#### Interventions and counterfactuals **Unintervened model**

$$
X_2 \leftarrow X_1
$$
\n
$$
\begin{cases}\nX_1 := f_{1,\theta_1}(\epsilon_1) \\
X_2 := f_{2,\theta_2}(X_1, \epsilon_2) \\
X_3 := f_{3,\theta_3}(X_1, X_2, \epsilon_3)\n\end{cases}
$$

# Interventions and counterfactuals

**Unintervened model Soft intervention: «** *only sharks when in the sea* **»**

$$
X_2 \leftarrow X_1
$$
\n
$$
X_2 :=
$$
\n
$$
X_3
$$
\n
$$
X_2 :=
$$
\n
$$
X_3 :=
$$

 $= f_{1,\boldsymbol{\theta_1}}(\epsilon_1)$ =  $f_{2,\boldsymbol{\theta_2}}(X_1,\epsilon_2)$  $= f_{3,\boldsymbol{\theta_3}}(X_1,X_2,\epsilon_3)$ 



$$
X_1 := f_{1,\theta_1}(\epsilon_1)
$$
  
\n
$$
X_2 := h_{2,\theta_2}(\mathcal{X}_1, \epsilon_2)
$$
  
\n
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# Interventions and counterfactuals

 $\epsilon_3$ )

**Unintervened model Soft intervention: «** *only sharks when in the sea* **»**

 $\bigcap X_1 := f_{1,\boldsymbol{\theta_1}}(\epsilon_1)$ 

 $X_2 := h_{2,\theta_2}(\mathbf{Y}_1,\epsilon_2)$ <br>  $X_3 := f_{3,\theta_3}(\mathbf{X}_1,X_2,\epsilon_3)$ 

$$
X_1
$$
\n
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**Hard intervention: «** *only Sharks, everywhere* **»** $X_1 := f_{1,\theta_1}(\epsilon_1)$ <br>  $X_2 := g_{2,\theta_2}(\epsilon_2)$ <br>  $X_3 := f_{3,\theta_3}(X_1, X_2, \epsilon_3)$  $\leftarrow \hspace{-.15cm}\leftarrow$ 



# Interventions and counterfactuals

**Unintervened model Soft intervention: «** *only sharks when in the sea* **»**

 $\bigcap X_1 \coloneqq f_{1,\boldsymbol{\theta}_1}(\epsilon_1)$ 

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$$
X_1
$$
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### Causal inference

**Causal graph** 

*Show the influence of variables on each other*



*Three types of inference tasks based on data:*  Causal discovery: "finding the arrows" Causal effect estimation: "how strong is causation?" Causal representation learning: "finding the variables" [= building a **mapping** from the observations to causal variables]

*Three types of dataset:*  Observational, interventional, counterfactual.

**Mechanisms = "Structural equations"**  *Compute child node value as a function of parents*

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*Three types of dataset:*  Observational, interventional, counterfactual.  $\leftarrow$ This presentation



Shark No shark



Shark No shark

**reliable** and **interpretable** technologies and decisions.

### Illustration: shortcut features

Features we are not « interested in » might be used to improve classification...





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Features we are not « interested in » might be used to improve classification...





- Shortcut features are found because they are highly predictive on the training data.
- They are **not an issue** if the deployment data has the same distribution as the training data
	- **-> "same environment"**
- Actually, dropping all such features would typically **decrease the performance**!
- But this makes the AI system not robust to changes of the environment…

## Illustration: shortcut features

We can model the changes of environment with interventions.



- ->"driving in Asia" The intervention affects the shortcut pathway by changing the learnt statistical dependency between object class and some backround features.
	- Avoiding such settings requires scrutinizing the data generating process, in particular dataset collection! -> Hard for most complex real-world data.
	- Typical dangerous cases: data collected with different measurement systems…

…e.g.: replacing a particle detector.

• Automatically learning a good approximation of the causal data generating process could help.

# Intervening in Deep generative models

[Besserve et al., ICLR 2020]









• Many approaches:



[Brock,et al. ICLR 2019]





• Many approaches:

VAE, GAN, Stable Diffusion, ….



[Brock,et al. ICLR 2019]



• Many approaches:

**Dataset** 

 ${\cal D}$ 

VAE, GAN, Stable Diffusion, ….

• Can generate highly realistic samples



[Brock,et al. ICLR 2019]

## ICM for generating counterfactuals

- Generative models have independent latents but dependent properties
- Look for internal variables with proper causal interpretation!





### An approximate causal abstraction

We build a form of causal abstraction [Rubenstein et al, 2017, Beckers et al., 2020], where we group hidden layer neurons into macro-variables on which we want to intervene at once. Groups are meant to encode high level properties of the images.

*Microscopic level*



Idea: group neurons that have similar effect on the generated images.

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#### Counterfactual generation

#### Examples for BigGAN (Brock et al., 2018) on ImageNet

Original 1





Counterfactual



"Counterfactual" object

"Factual" image

- Several early layers allow objectbackground separation,
- Other separate shape-texture

#### We use counterfactuals to probe state of the art classifiers.



[Besserve et al., ICLR 2020]

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[Besserve et al., ICLR 2020]

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# Identifiability of causal representations

[Gresele\*, von Kügelgen\* et al, NeurIPS 2021]

[Buchholz et al., NeurIPS 2022]

[Reizinger\*, Gresele\*, Brady\* et al. NeurIPS2022]

Assumption: Observed data is parameterized by hidden causal variables

$$
X \coloneqq f(Z_1, Z_2, \dots, Z_K) \blacktriangleright (Z_1, Z_2, \dots, Z_K) = f^{-1}(X)
$$





Assumption: Observed data is parameterized by hidden causal variables

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X := f(Z_1, Z_2, \dots, Z_K) \longrightarrow (Z_1, Z_2, \dots, Z_K) = f^{-1}(X)
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*Ground truth Causal representation*



*"Twin" learned Causal representation*





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#### **Identifiability:**

*If the generative model fits the data perfectly, it corresponds to the ground-truth model (up to trivial transformations).* 

#### **Implications:**

*We can do "data augmentation" by fitting the model and performing interventions and counterfactuals.* 

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[Hyvärinen & Pajunen, Neur. Netw. 1999, Locatello et al, ICML 2019]



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*Architecture*



[Hyvärinen & Pajunen, Neur. Netw. 1999, Locatello et al, ICML 2019]



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 $\boldsymbol{f}_{\boldsymbol{\theta}}[p_0] = \tilde{\boldsymbol{f}}[p_0], \forall \tilde{\boldsymbol{f}} \in \mathcal{S}_{\boldsymbol{f}}$ 

![](_page_43_Figure_0.jpeg)

![](_page_44_Figure_0.jpeg)

➢*Constraining* **f** to a smaller (large!) model class, via regularized maximum likelihood, with Normalizing flows, favors identifiability [Gresele\*, von Kügelgen\* et al, NeurIPS 2021; Buchholz et al., NeurIPS 2022]

$$
\mathrm{maximize} / \boldsymbol{\theta} \ \ \, \mathcal{L}_{IMA}(\boldsymbol{x}; \boldsymbol{f}_{\boldsymbol{\theta}}, \lambda) = \log p_{\boldsymbol{\theta}}(\boldsymbol{x}) - \lambda . c_{IMA}(\boldsymbol{f}_{\boldsymbol{\theta}}, \boldsymbol{f}_{\boldsymbol{\theta}}^{-1}(\boldsymbol{x}))
$$

![](_page_45_Figure_0.jpeg)

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$$

➢*Variational Auto-Encoders (VAE) implicitly constrain f in the above model class and inherit identifiability benefits.* [Reizinger\*, Gresele\*, Brady\*, et al. NeurIPS2022] *Evidence Lower BOund* :  $\text{ELBO}(x;\theta,\phi) = \log p_{\bm{\theta}}(\bm{x}) - \text{KL}(q_{\bm{\phi}}(\bm{z}|\bm{x}) \| p_{\bm{\theta}}(\bm{z}|\bm{x}))$ *ELBO gap ≥0* minimize/ $\phi$ 

 $maximize / \theta$ 

#### Assumptions for *learning* causal generative AIs

Δ

To identify causal representations, we need either:

(1) **inductive biases** (assumptions on the ground truth model)

[Gresele\*, von Kügelgen\* et al, *NeurIPS* 2021; Buchholz et al., *NeurIPS* 2022;

Reizinger\*, Gresele\*, Brady\* et al. *NeurIPS* 2022; Leeb et al., *ICLR* 2023]

(2**) multi-environment data =** interventions. [Keurti et al., *ICML* 2023; von Kügelgen et al., *NeurIPS*, 2023; Liang et al., *NeurIPS*, 2023]

(3**) multi-view data** = counterfactuals.

[Besserve et al. *AAAI* 2021; von Kügelgen et al., *NeurIPS*, 2021]

![](_page_46_Figure_8.jpeg)

![](_page_46_Figure_9.jpeg)

#### Assumptions for *learning* of causal generative AI

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![](_page_47_Figure_9.jpeg)

#### **[Von Kügelgen et al., NeurIPS, 2023]**

### Assumptions for *learning* of causal generative AI

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(2**) multi-environment data =** interventions.

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(3**) multi-view data** = counterfactuals, and structured sample-dependency

[Besserve et al. *AAAI* 2021: von Kügelgen et al., *NeurIPS*, 2021, Keurti et al., *ICML* 2023]

![](_page_48_Picture_9.jpeg)

![](_page_48_Picture_10.jpeg)

![](_page_48_Picture_88.jpeg)

**[Von Kügelgen et al., NeurIPS, 2021]**

### Sample dependency-based identification: Case 1

- **Data augmentation** is a particular case of **self-supervised learning**:
	- Augmentations change "style" of the image but not "content",
	- Data-set contains *(original, augmented)* pairs of samples
	- Result: augmentation-invariant representations identify content.

![](_page_49_Figure_5.jpeg)

![](_page_49_Picture_6.jpeg)

DA: data augmentation LT: latent transformation

![](_page_49_Picture_60.jpeg)

**[Von Kügelgen et al., NeurIPS, 2021]**

• Challenges: augmentation need to have enough variability, and respect the latent causal structure.

#### Sample dependency-based identification: Case 2

• Latent time/space structure

Learning latent Lie group structure by manipulation

![](_page_50_Figure_3.jpeg)

![](_page_50_Figure_4.jpeg)

Keurti et al., *ICML* 2023

Several other results on sequential/spatial models: Hälvä & Hyvärinen, 2020, and many others…

Relevance for spatio-temporal emulators and data assimilation (Jordi and Andrew's talks)

# Learning high-level causal explanations

**[Kekić et al. and MB, UAI 2024]**

### Causal explanations in complex systems

- Experts and decision makers need to get a high-level, simplified representation of complex systems to take decisions.
- This relies on finding "aggregated" indicators to describe the system.
- Those are used to make explicit or implicit causal claims.
- Not obvious these claims are correct!

**Low-level representation**

![](_page_52_Figure_5.jpeg)

**High-level, reduced representation**

![](_page_52_Figure_7.jpeg)

## Analogy to mechanics

![](_page_53_Figure_1.jpeg)

#### Targeted causal model reduction algorithm [Kekić et al., UAI 2024]

#### • Causal consistency principle

![](_page_54_Figure_2.jpeg)

• An ML algorithm to learn high-level causes from simulations.

![](_page_54_Figure_4.jpeg)

#### Targeted causal model reduction algorithm [Kekić et al., UAI 2024]

#### • Causal consistency principle

![](_page_55_Figure_2.jpeg)

• An ML algorithm to learn high-level causes from simulations.

-> A simplified description of a complex system We can interact with through interventions. **The interventions** of the struck of the Target phenomenon

![](_page_55_Figure_5.jpeg)

## Example: double well simulator (Euler method)

- Interventions via random forces applied along the trajectory.
- Target phenomenon: Final position of the ball

![](_page_56_Figure_3.jpeg)

- The algorithm locates the time range where changes are critical for the outcome to happen.
- Ongoing work: enhance interpretability and scalability.

## Example: double well simulator (Euler method)

- Interventions via random forces applied along the trajectory.
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![](_page_57_Figure_3.jpeg)

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## Example: double well simulator (Euler method)

- Interventions via random forces applied along the trajectory.
- Target phenomenon: Final position of the ball

![](_page_58_Figure_3.jpeg)

- The algorithm locates the time range where changes are critical for the outcome to happen.
- Ongoing work: enhance interpretability and scalability.

### Take-home

- Causality is a promising framework to design interpretable AI robust to changes, but also *a philosophy for scientific practice: pay attention to data generating mechanisms.*
- There are **guaranties for causal generative AI**, using diverse inductive biases on function spaces, structure, invariances, multiple environments: can guide the choice of AI model and dataset collection.
- Causal reduction/abstraction of complex models into simpler ones allows human-interpretable explanations and control…

… *and a way for scientists to prioritize the aim of understanding reality despite the growing complexity of models and data-science pipelines.*

### Towards Computational Causal Models (CCM)

![](_page_60_Picture_1.jpeg)

**Real-world measurements Observations/experiments**

addition.

بباشران وأستالمتهم والملمس

![](_page_60_Picture_3.jpeg)

**Computational representation**

![](_page_60_Figure_5.jpeg)

**ML coordination**

## Open questions

![](_page_61_Figure_1.jpeg)

- How to optimally merge scientific knowledge (e.g. physics equations and principles) with flexible machine learning:
	- ML tools improve predictive power, but may lose physical consistency (Laure's talk) -> need an identifiability theory for hybrid/"grey box" models (Takeishi et al., 2021)
	- How learning high-level causal models, can help generalize better from models to the real world? (Sim2real gap),
- Training of smaller and modular AI systems whose parts can be reused for other tasks.

## *Thank you!*

**Bernhard Schölkopf,** 

**Remy Sun, Arash Mehrjou, Luigi Gresele, Julius von Kügelgen, Patrik Reizinger, Jack Brady, Felix Leeb, Hsiao-Ru Pan, Hamza Keurti, Armin Kekić.** 

*References* **Starting a new lab (TU Braunschweig): open positions, collaborations, contact me!**  $\odot$ 

**TÜBINGEN AI CENTER** 

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