

Observing GW from space : The LISA mission

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- Introduction
- LISA Science Objectives
- From LISA Pathfinder to LISA
- Mission description
- Conclusion


Introduction





 LISA Science Objectives

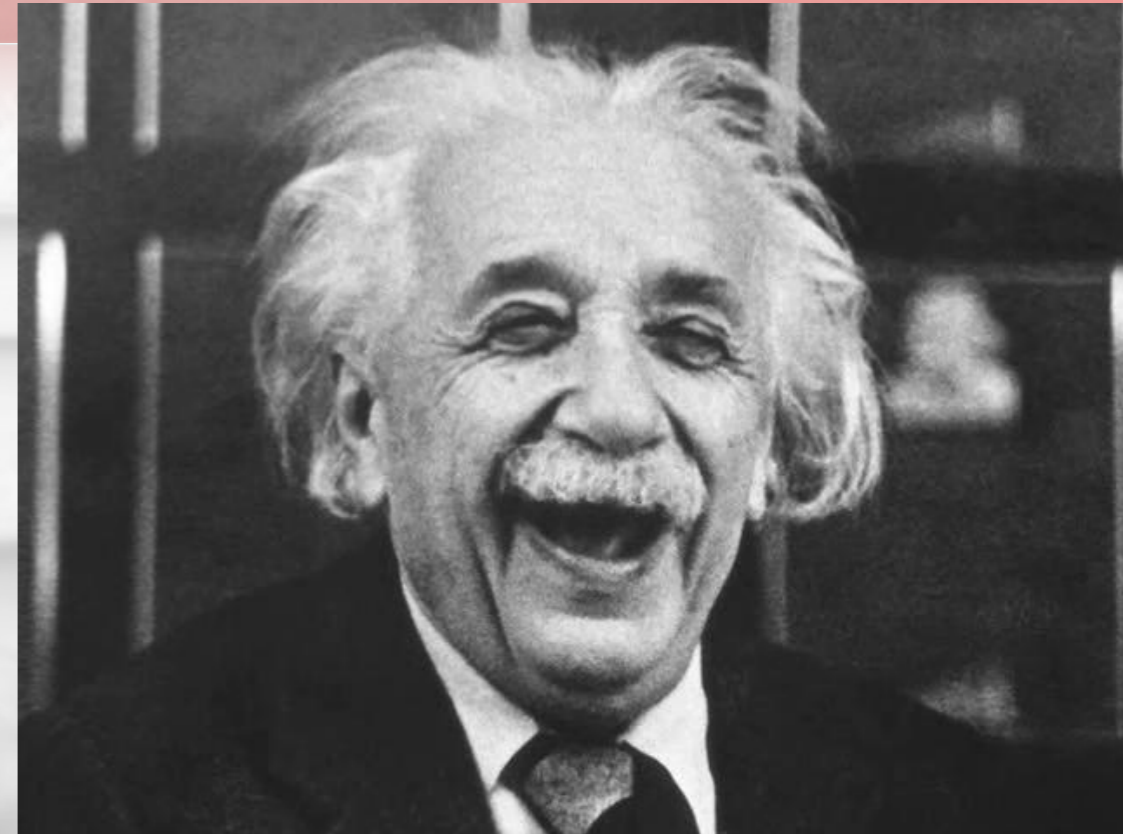
 From LISA Pathfinder to LISA

 Mission description

 Conclusion

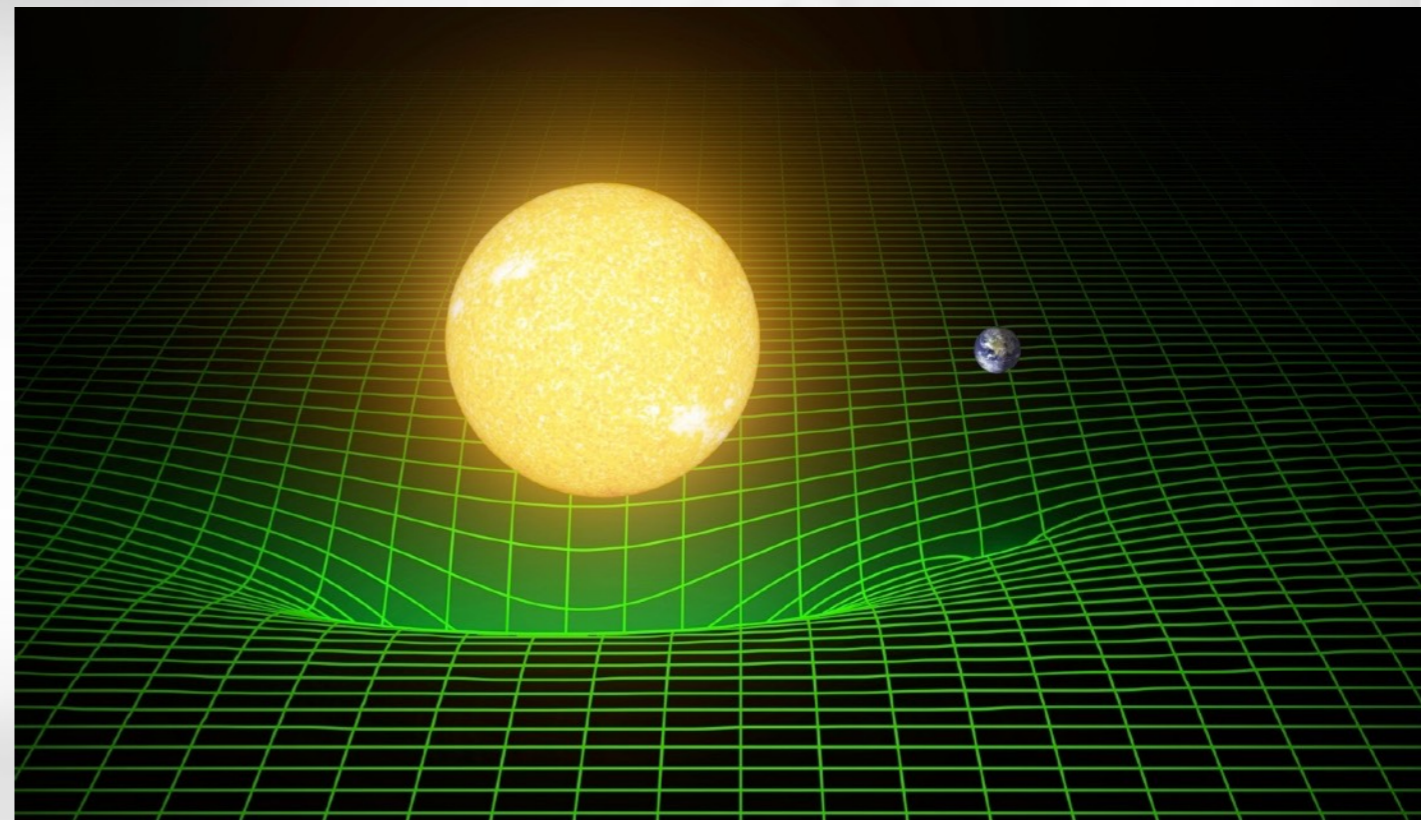
 Albert Einstein (1915) : Gravity is not a force ...

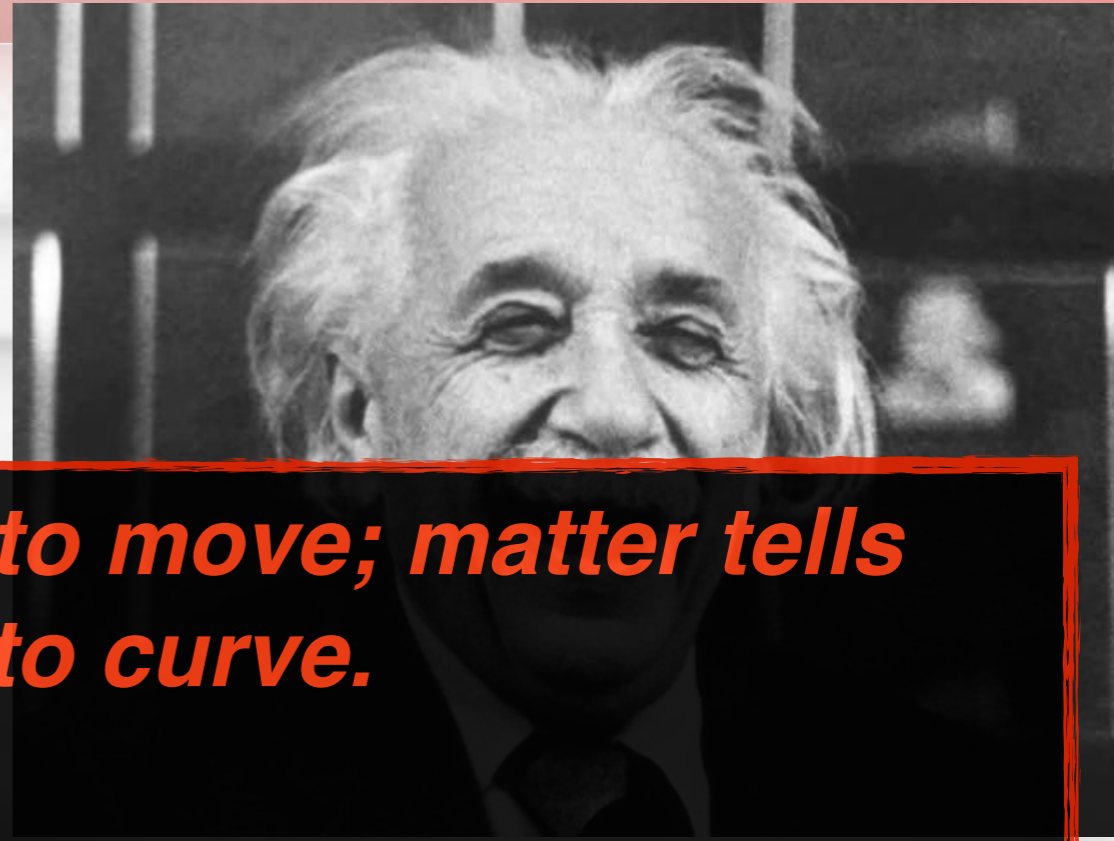
-  Mass deforms geometry of space-time.
-  Bodies are moving in a curved space.
-  Gravitational information propagates at the speed of light.
-  Dissipation of energy through deformation of space-time ==> gravitational waves



$$\boxed{G_{\mu\nu}} = \frac{8\pi G}{c^4} \boxed{T_{\mu\nu}}$$

Geometry of space-time
Energy distribution





• Albert Einstein (1915) : Gravity is not a force ...

• Mass deforms geometry of space-time.

• Bodies are moving in a curved space.

Spacetime tells matter how to move; matter tells spacetime how to curve.

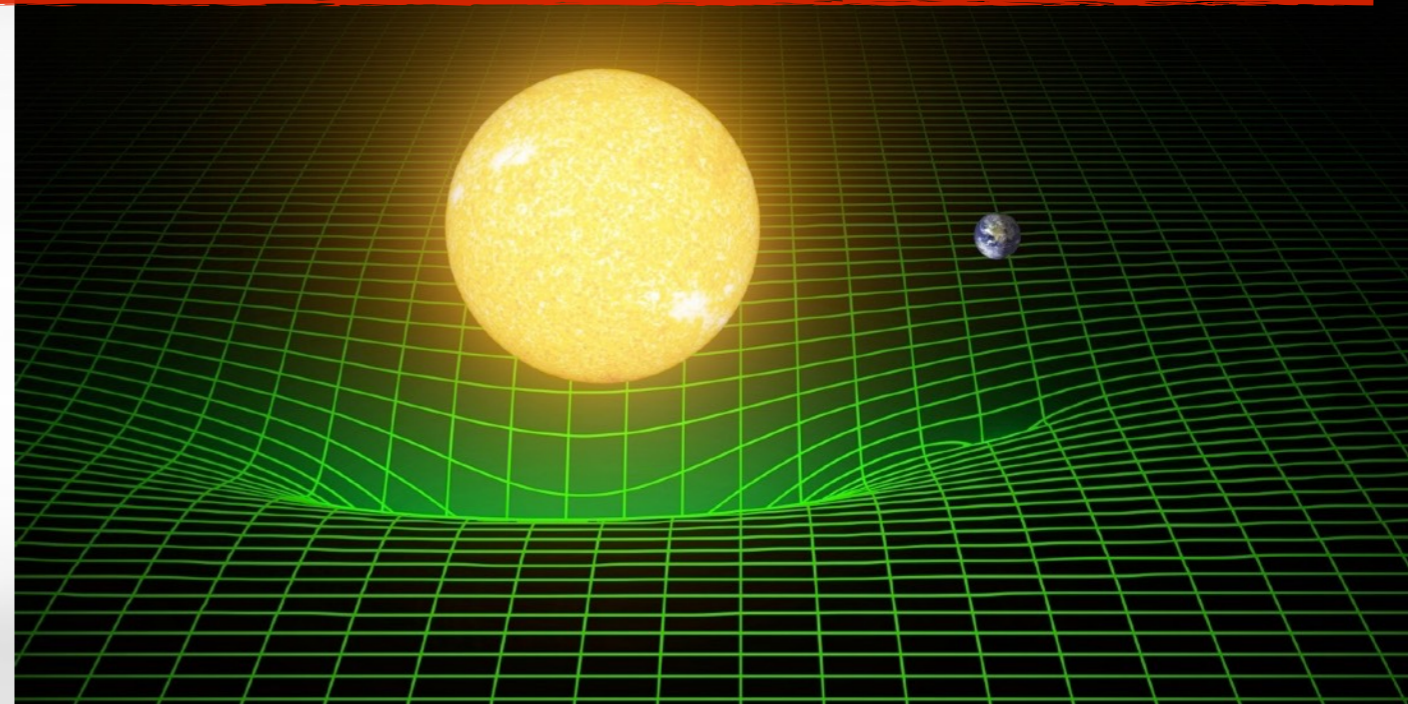
• Dissipation of energy through deformation of space-time => gravitational waves

John Archibald Wheeler, "Geons, Black Holes, and Quantum Foam: A Life in Physics", 1990

$$G_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

Geometry of space-time

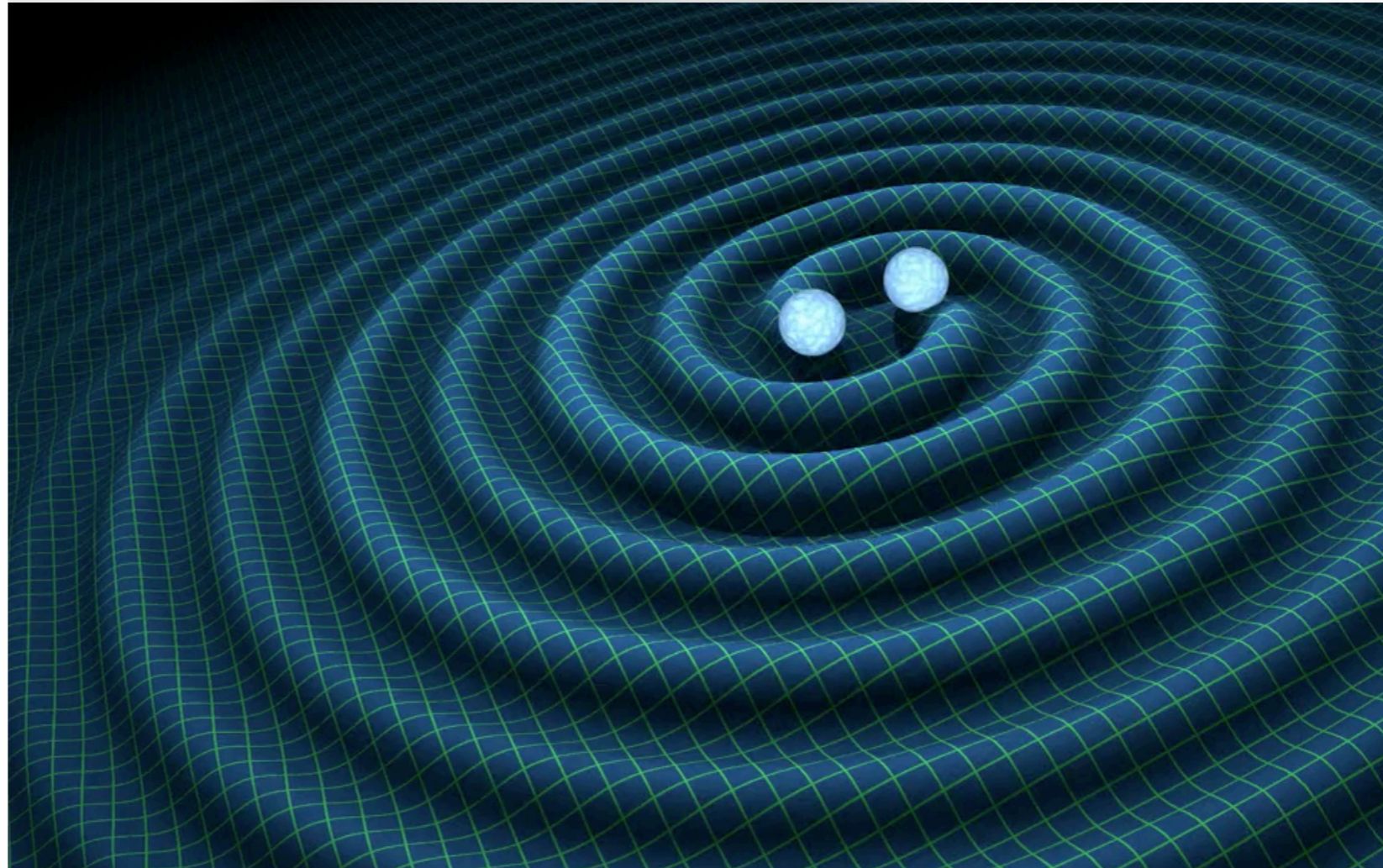
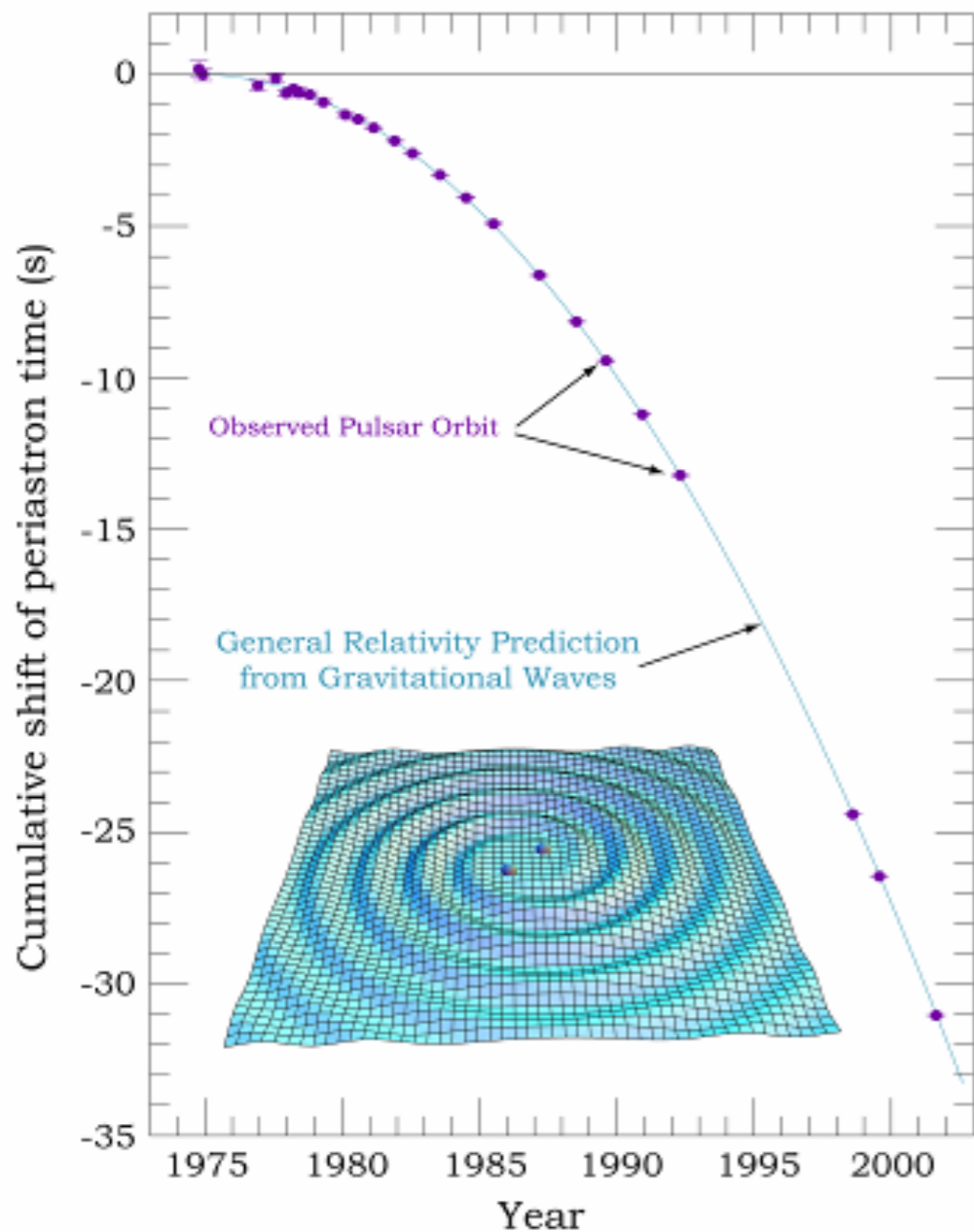
Energy distribution



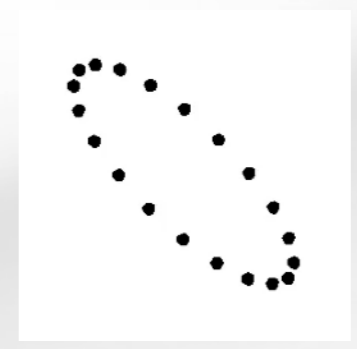
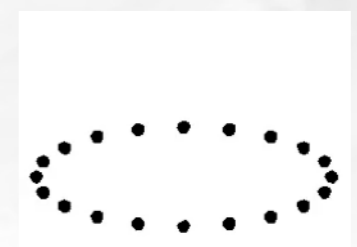
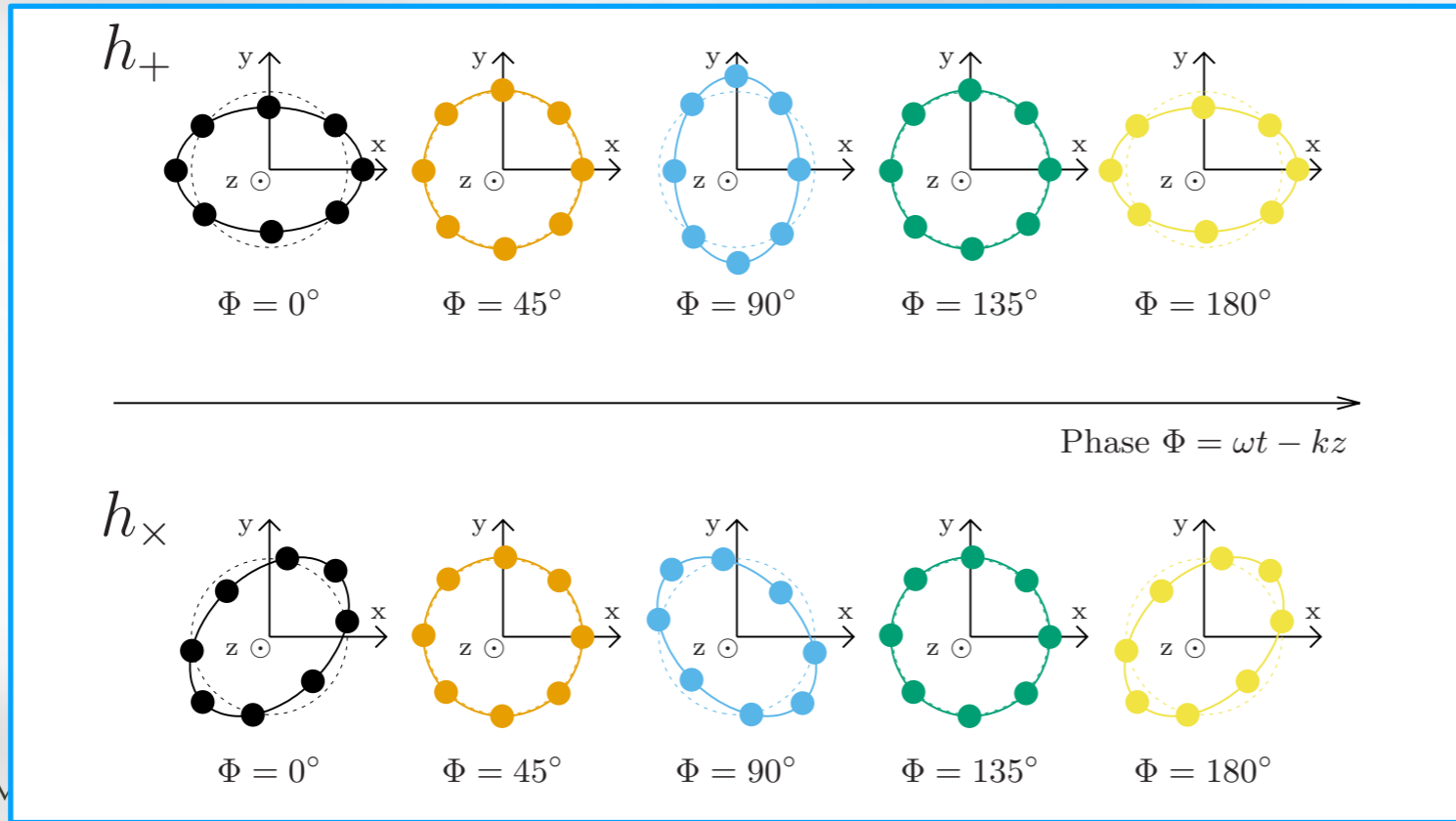
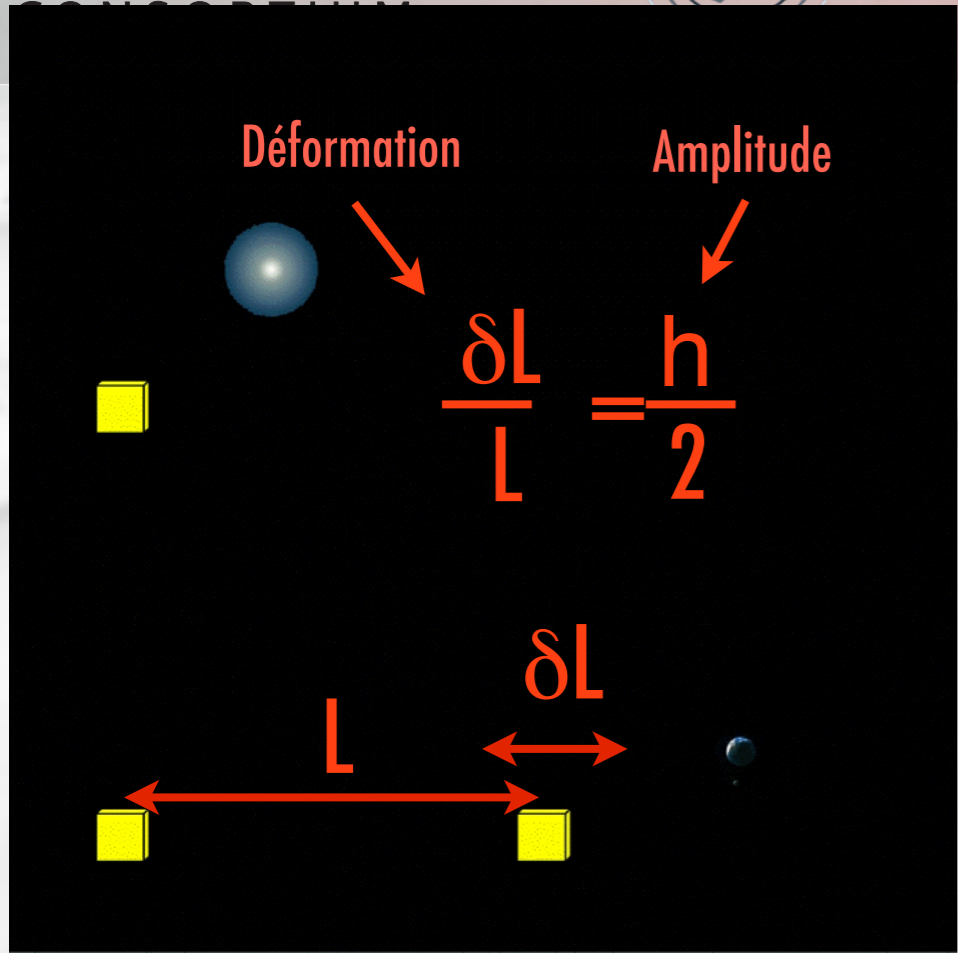
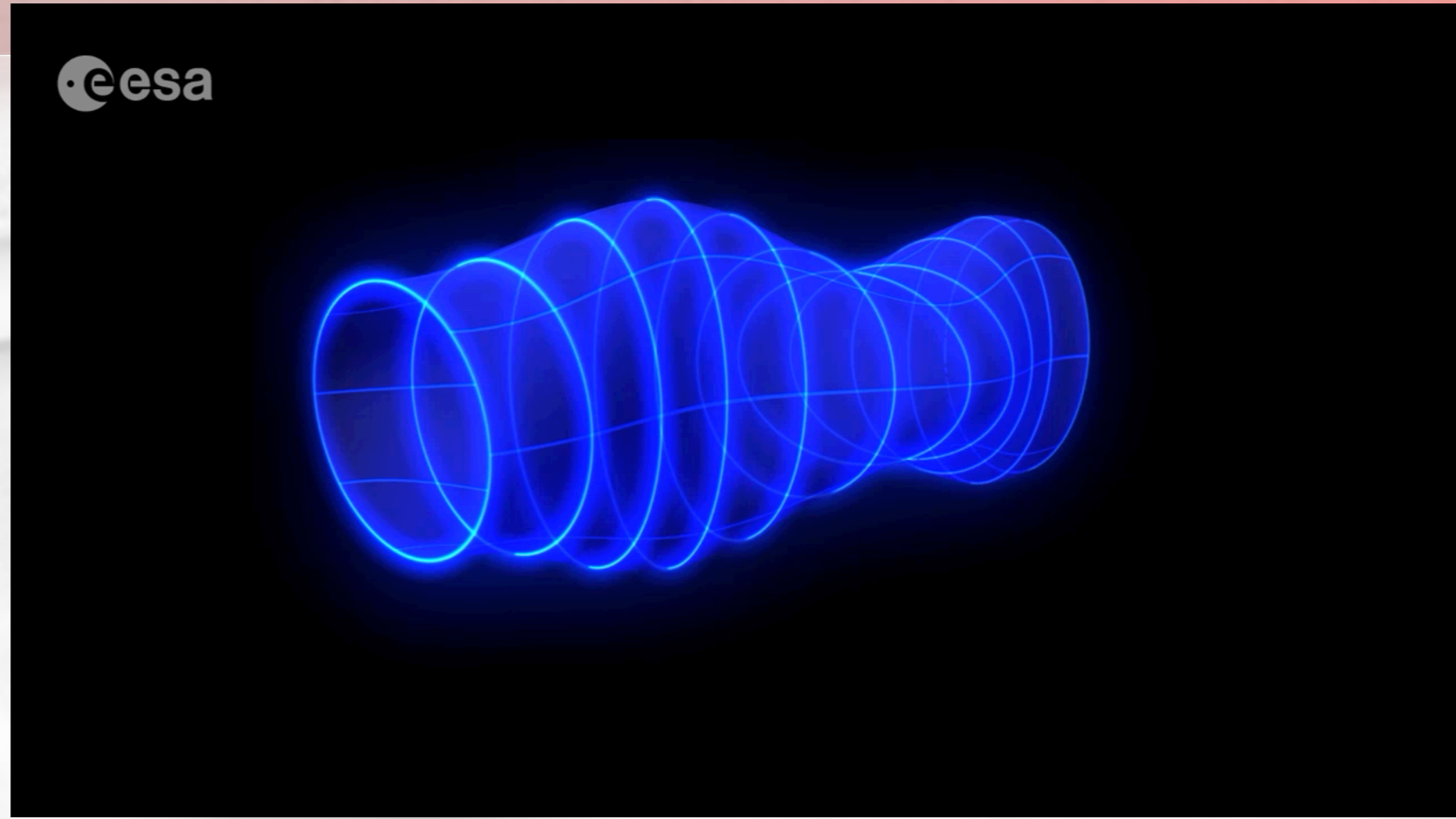
Gravitational waves ?

What are GW ?

- The GW are elastic deformations of the space-time metric
- Transverse, quadrupole waves, 2 polarisations



GW = space-time deformation



Are they detectable ?

- Until 1950's the approximations used to compute the GW induced doubts in their 'real' physical effects.

- Linear perturbations of a flat space-time

- What is the influence of the strong curvature zone close to the source ?

- Traceless, transverse gauge

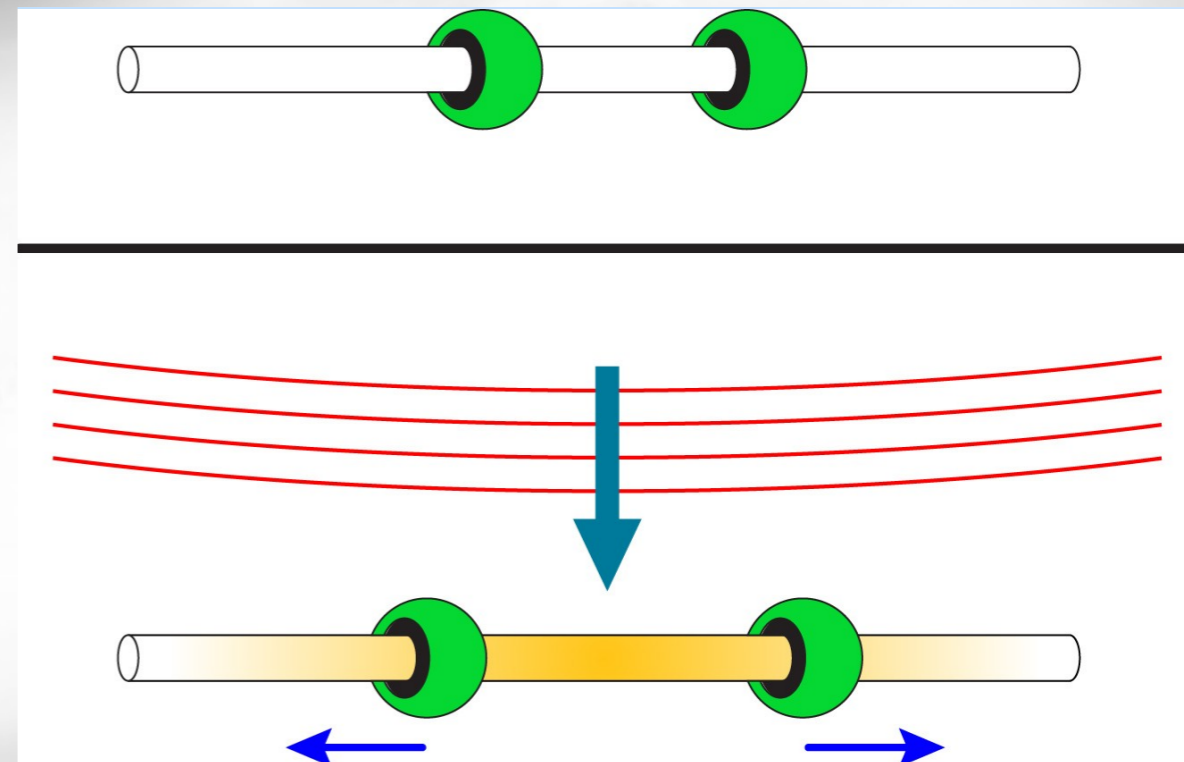
- Could GW be an artefact of this particular choice of coordinate system ?

- Do GWs have an actual physical effect ?

- Pirani [1956] : Yes, space-time curvature changes induce fluctuations in the proper distance between inertial objects

- Do GWs carry energy ?

- Yes : the 'Sticky bead' argument [Feynman & Bondi, Chapel Hill Conference, 1957]



Orders of magnitude

Compacité of a gravitational system

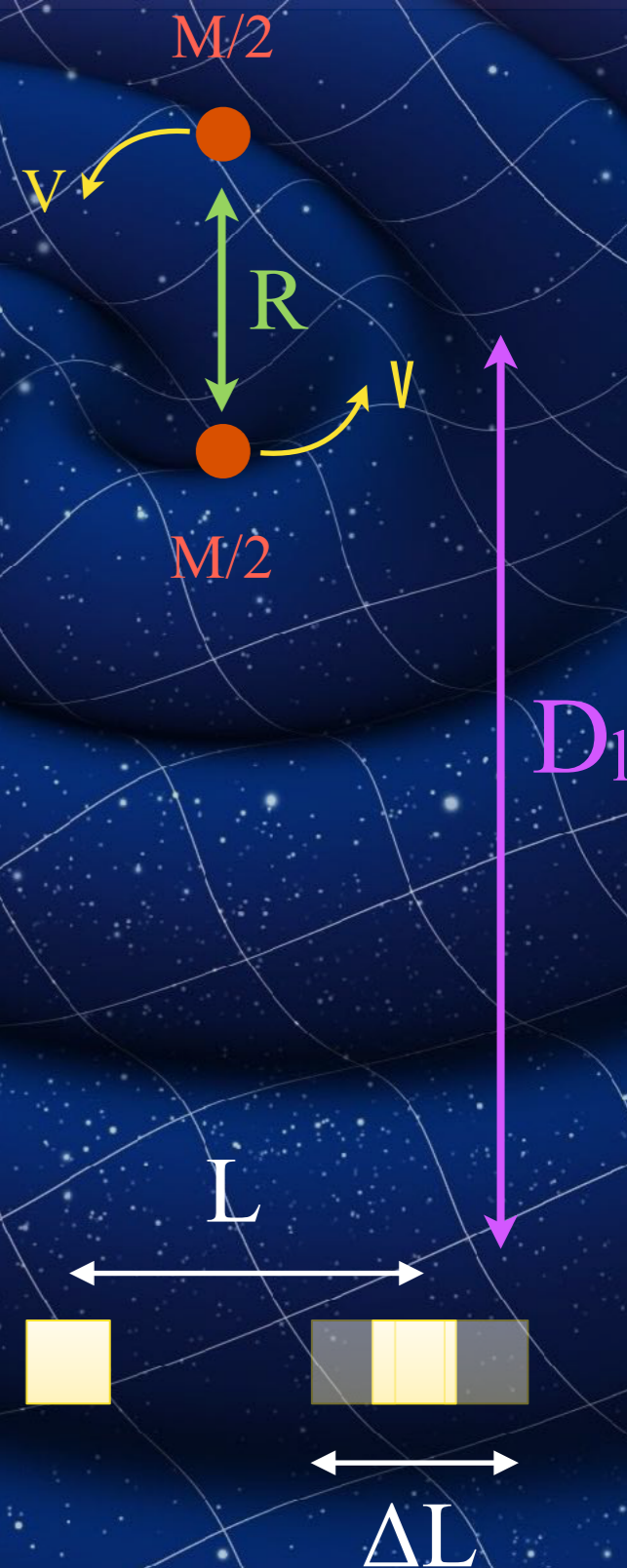
$$\frac{v^2}{c^2} \approx \frac{GM}{Rc^2} = \Xi < 1$$

Wave amplitude

$$h = 2 \frac{\Delta L}{L} \lesssim \frac{\Xi}{10^{-1}} \cdot \frac{M}{10^6 M_\odot} \cdot \frac{10 \text{ Gpc}}{D_1} \text{ nm/Mkm}$$

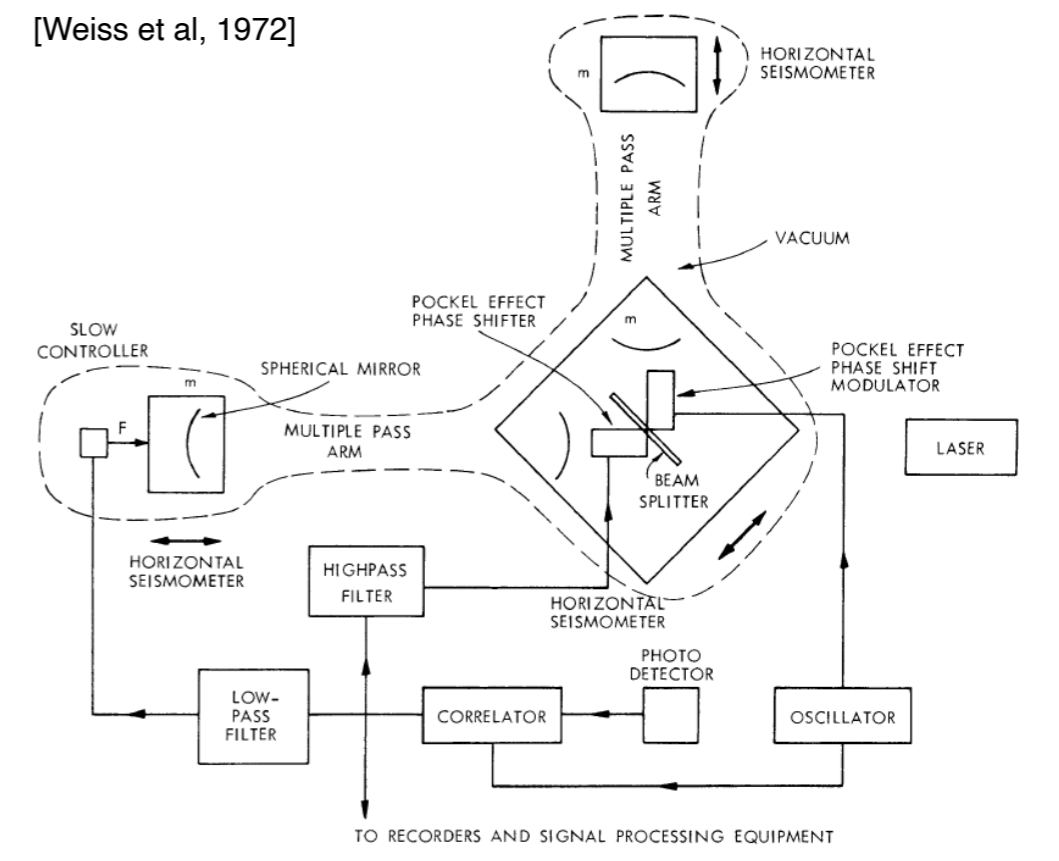
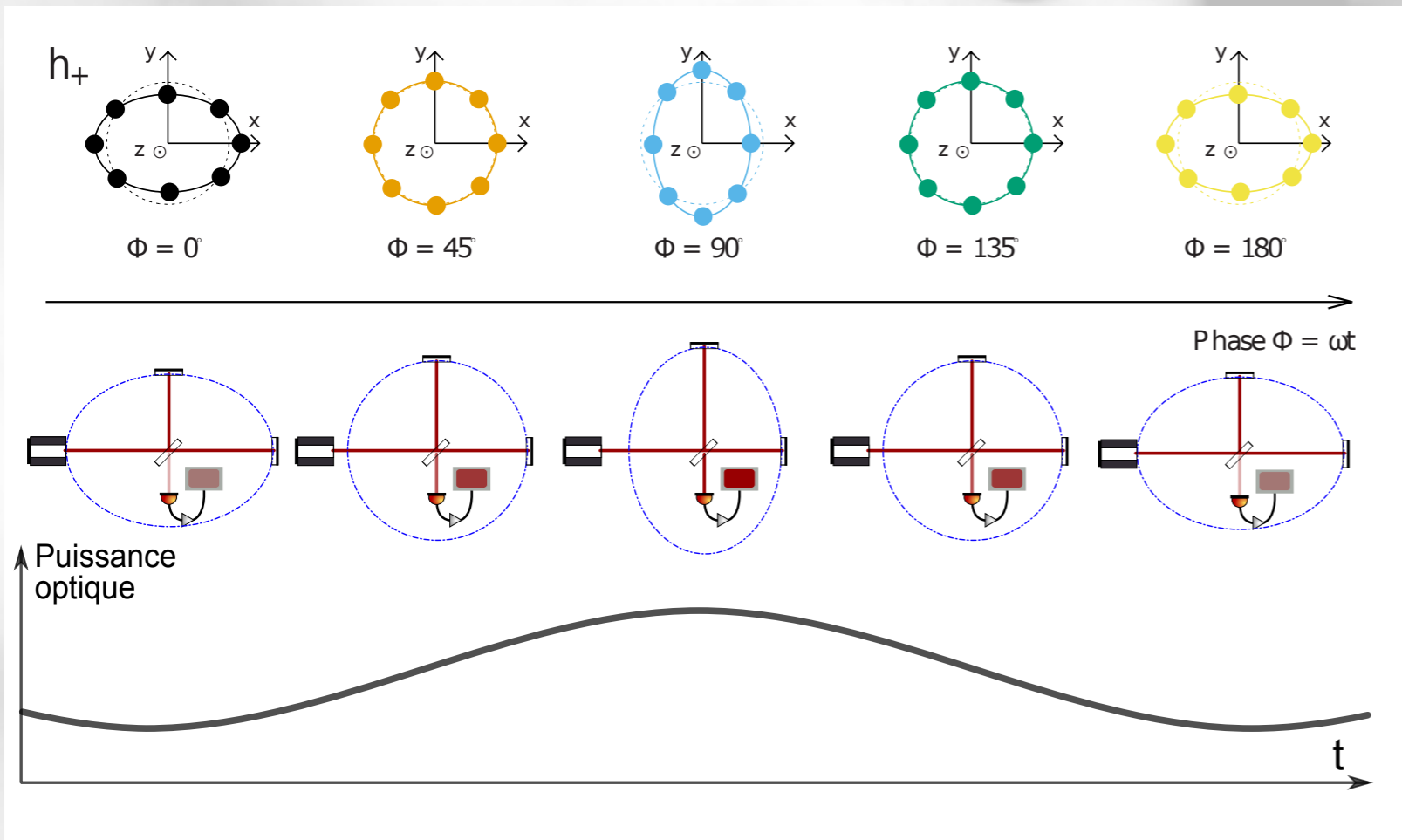
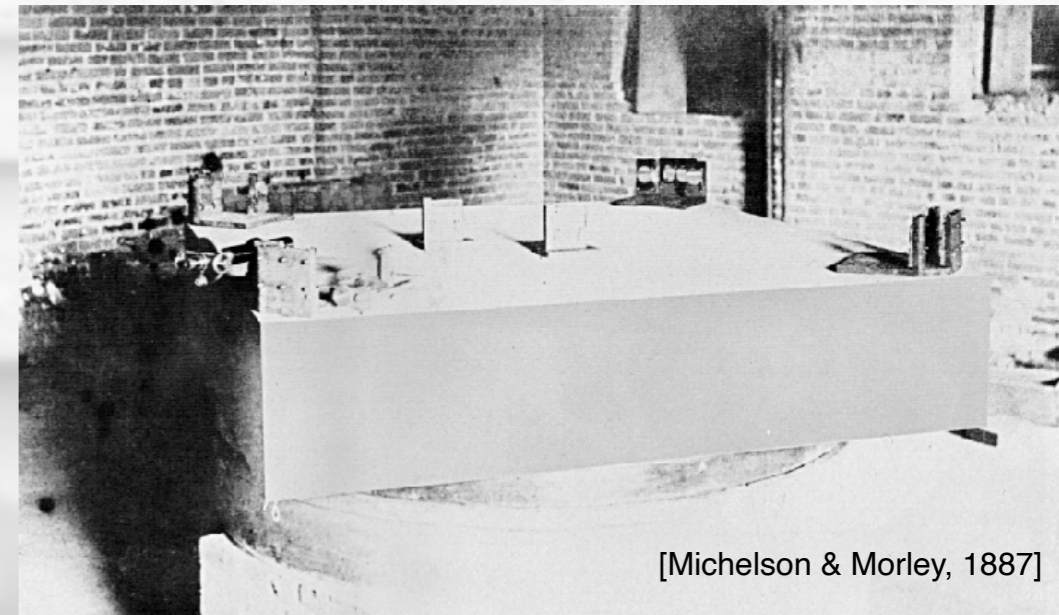
Wave frequency

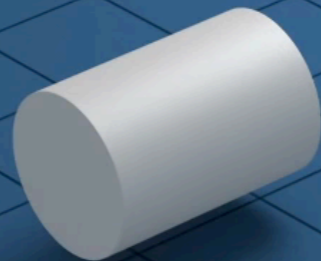
$$f \approx 14 \times \left(\frac{\Xi}{10^{-1}} \right)^{3/2} \cdot \frac{10^6 M_\odot}{M} \text{ mHz}$$



Interferometric detectors

- The geometry and sensitivity of the Michelson interferometer particularly well suited for detecting Gas
 - Require mirrors 'free falling' along the line of sight
- First concepts in the 60's in USSR [Gertsenshtein et Pustovoit, 1963] an in the USA [Moss et al, 1971]
 - R. Weiss, 1972 : identification and computation of the most important sources of noise





Hanford, Washington



LIGO
4 km
armlength

Livingston, Louisiane



VIRGO
3 km
armlength



• *Introduction*

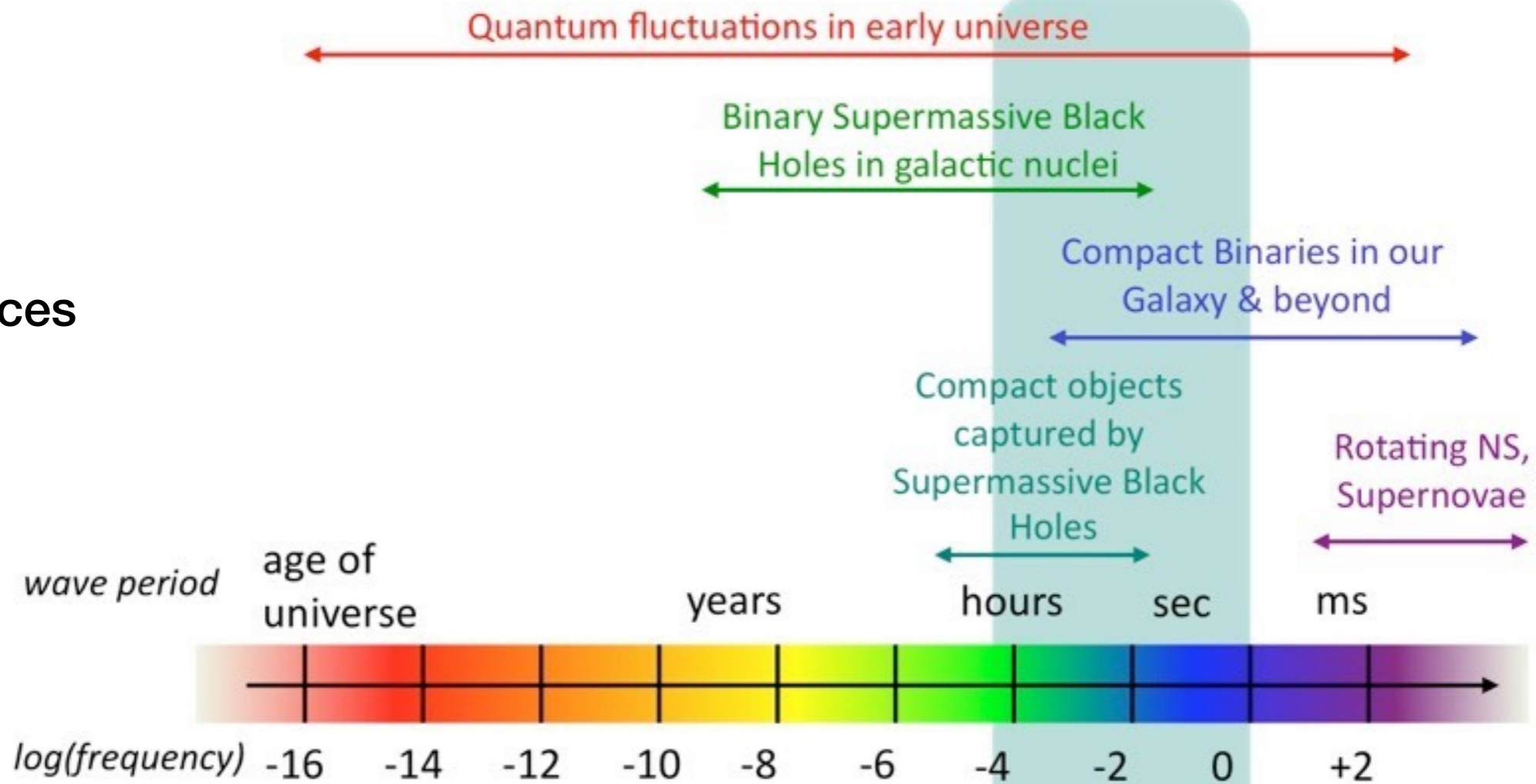
• **LISA Science Objectives**

• From LISA Pathfinder to LISA

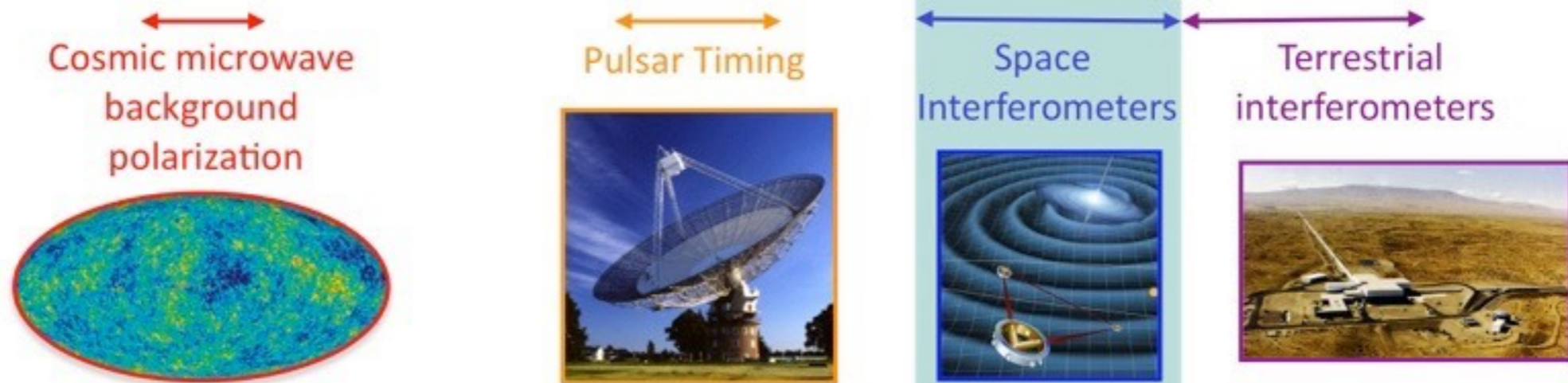
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Sources



Detectors



Study the formation and evolution of compact binary stars in the Milky Way Galaxy.

- Large number of stars are in binary systems

- Evolution in white dwarf (WD) and neutron stars (NS).

- Existence of WD-WD NS-WD and NS-NS binaries

- Estimated population for the Galaxy : $\sim 10^7$.

- Monochromatic sources for LISA (far from coalescence)

- Three categories

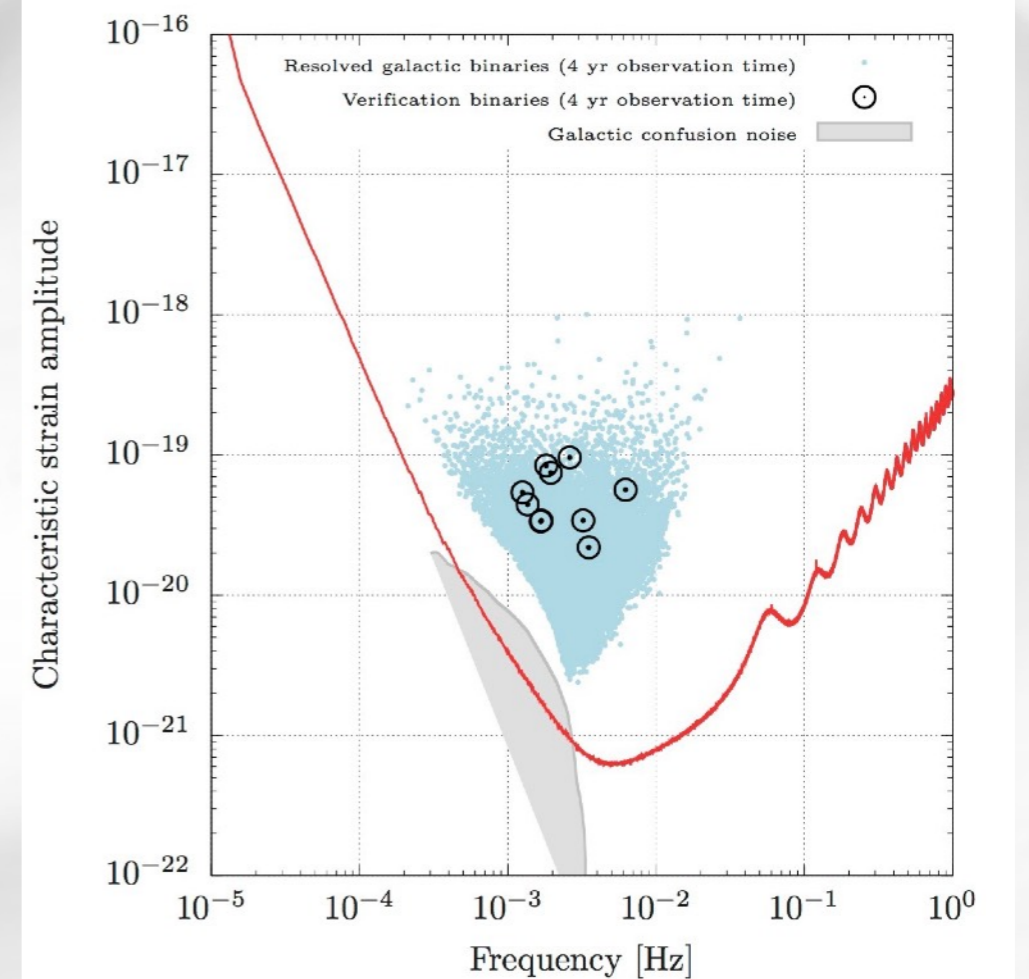
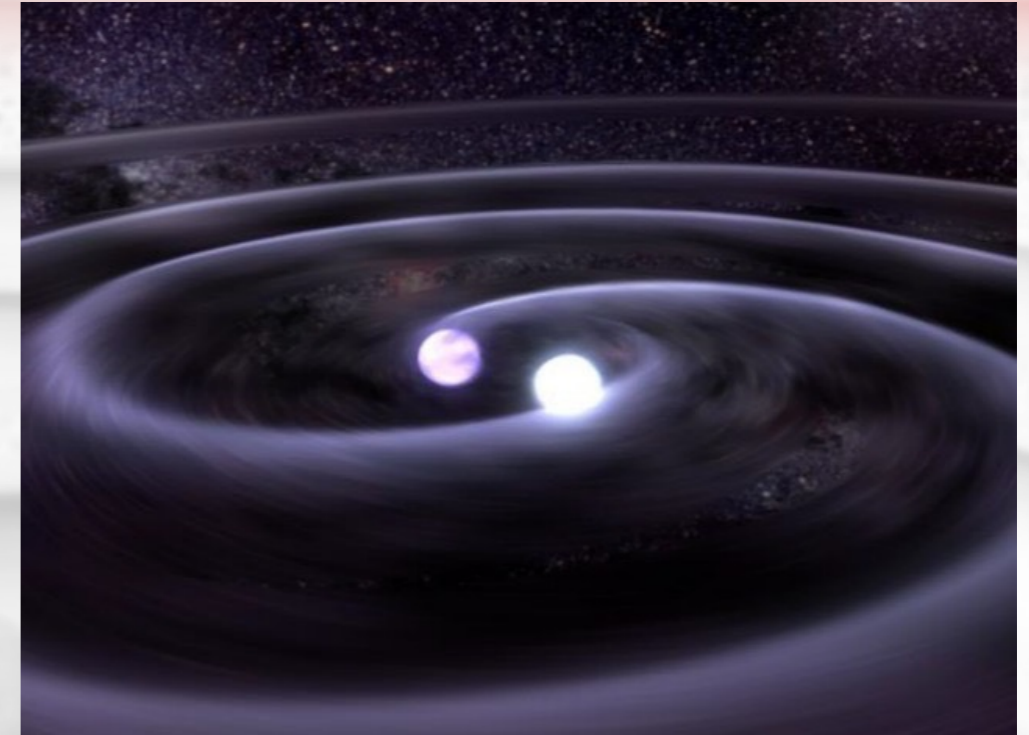
- Joint EM - GW sources (Gaia, LSST)

- Already ~ 10 known verification binaries in the LISA band

- Individually detected : $\sim 10^4$

- Stochastic GW signal

- foreground 'noise'



- Massive BHs in the nucleus of every Galaxy

- $4 \times 10^6 M_{\text{sun}}$ at the center of the Milky Way

- MBHs accumulate mass

- gas accretion

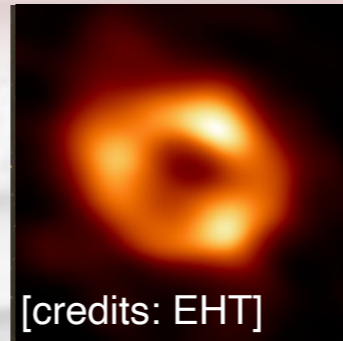
- merging with other BHs

- Galaxies merge

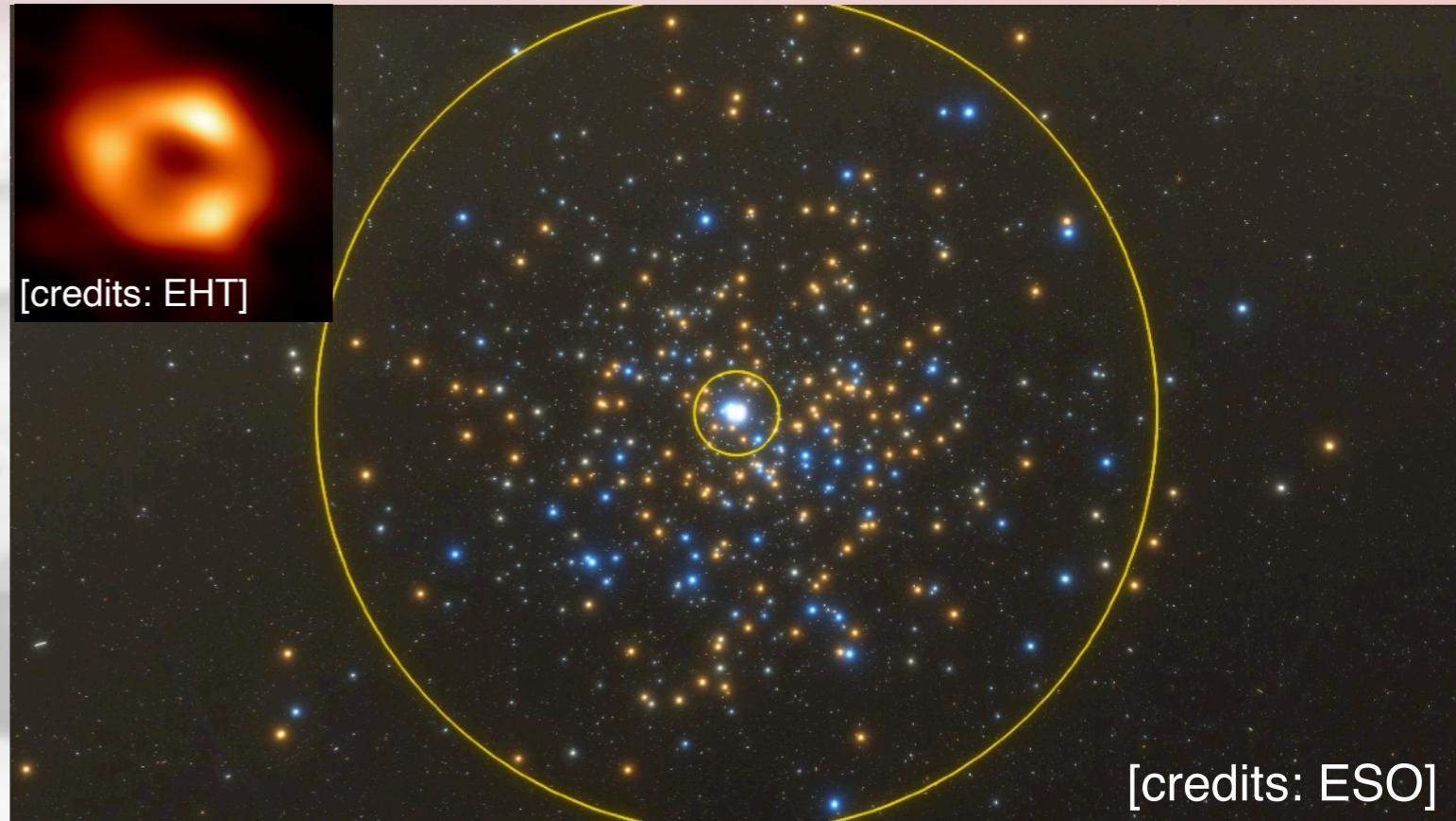
- observed...

- may result in a MBH binary which could merge in a reasonable time

- Stars and/or gas required to dissipate orbital momentum and bring it in GW driven regime



[credits: EHT]

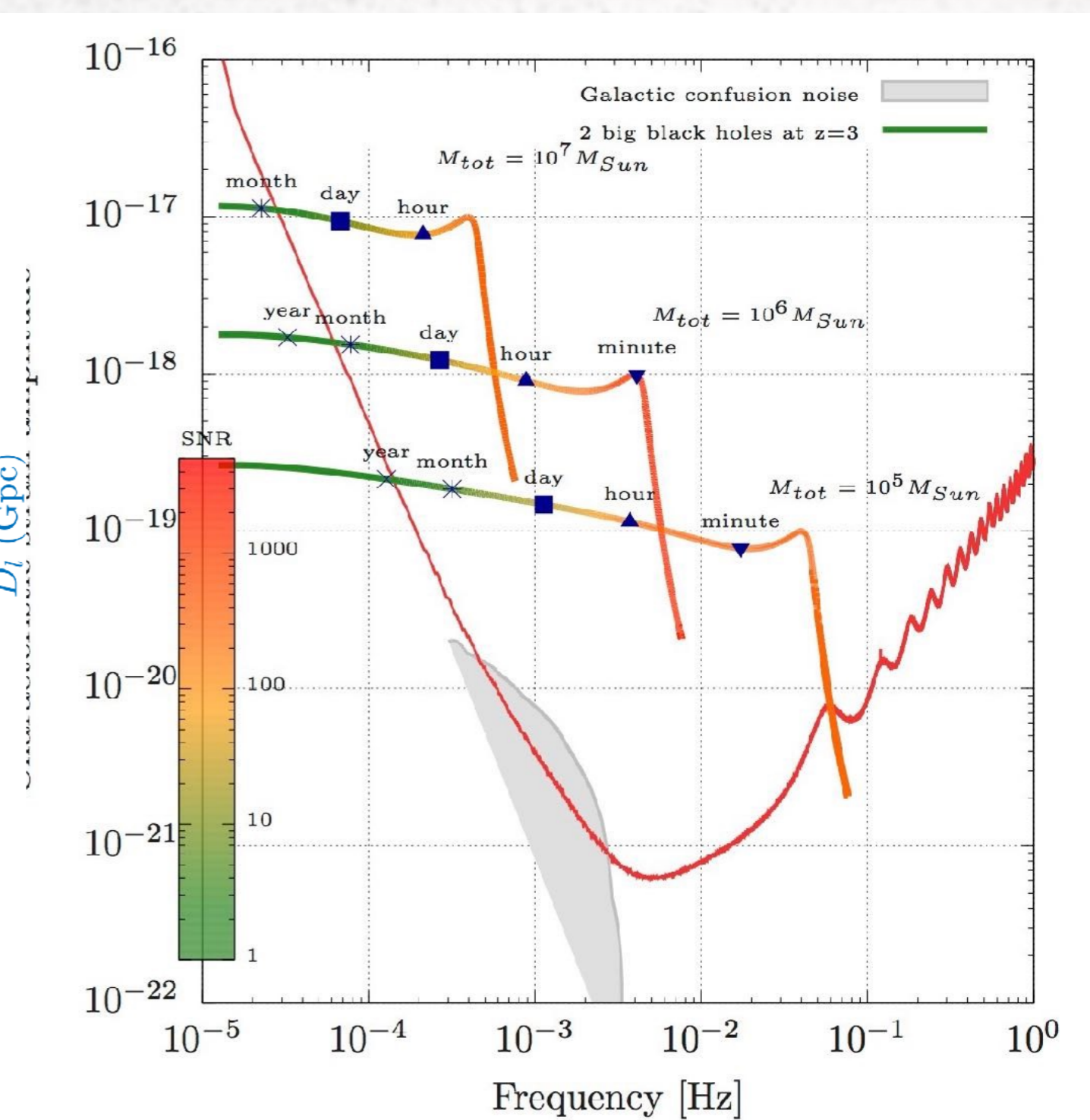
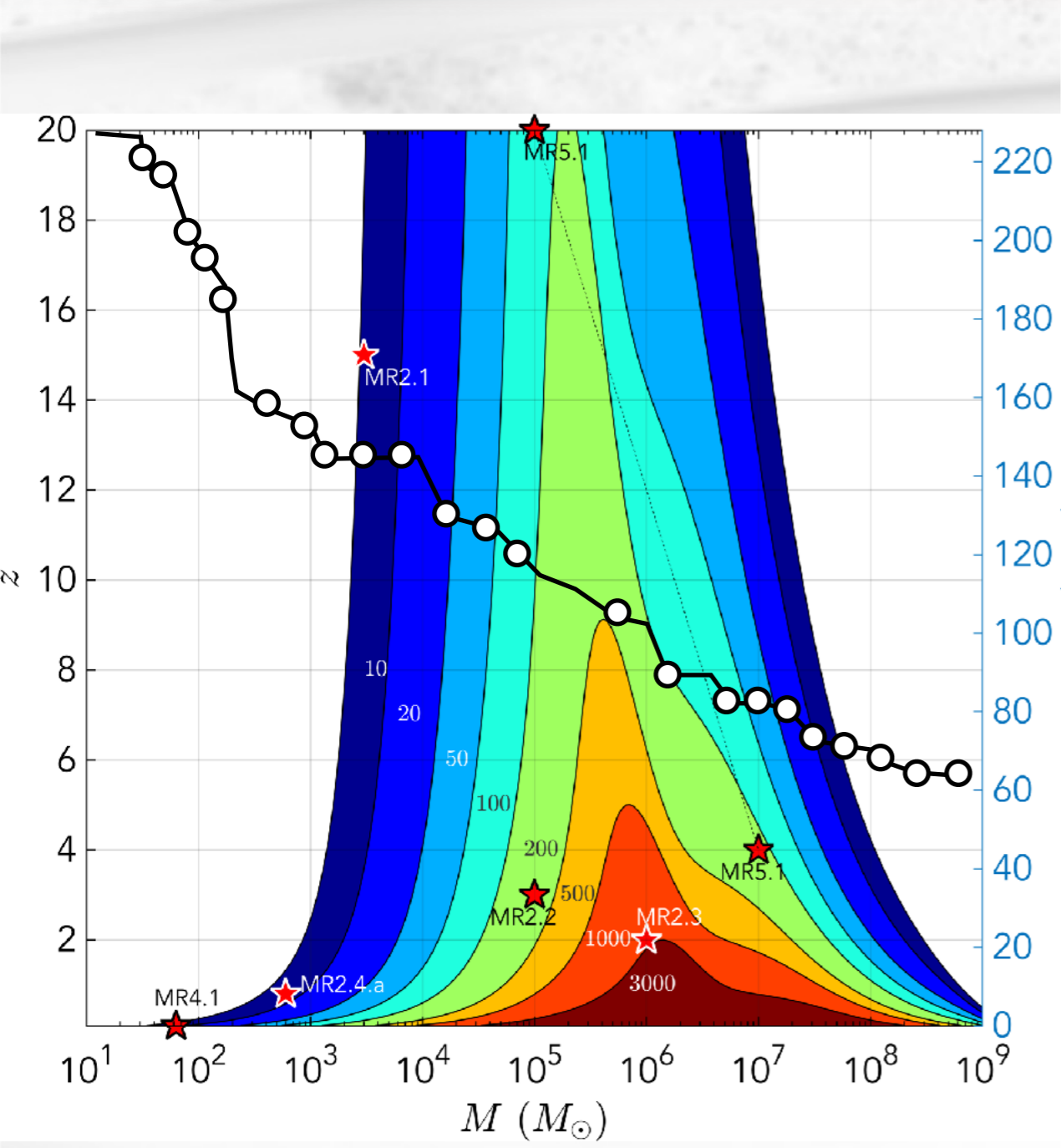


[credits: ESO]



[credits: HST]

Origin, growth and merger history of massive black holes across cosmic ages



- Massive BHs could be embedded in stellar cusps

- high density stellar environment

- Massive BH could capture a compact object

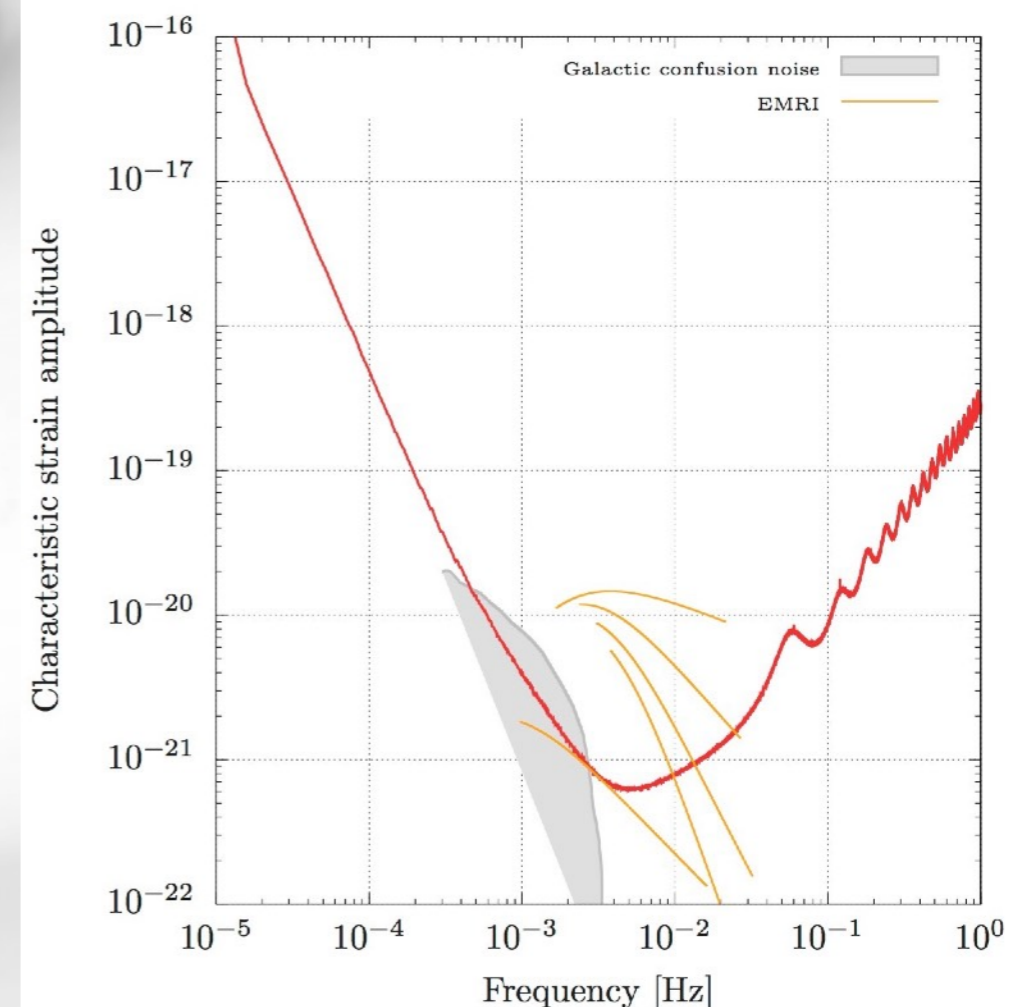
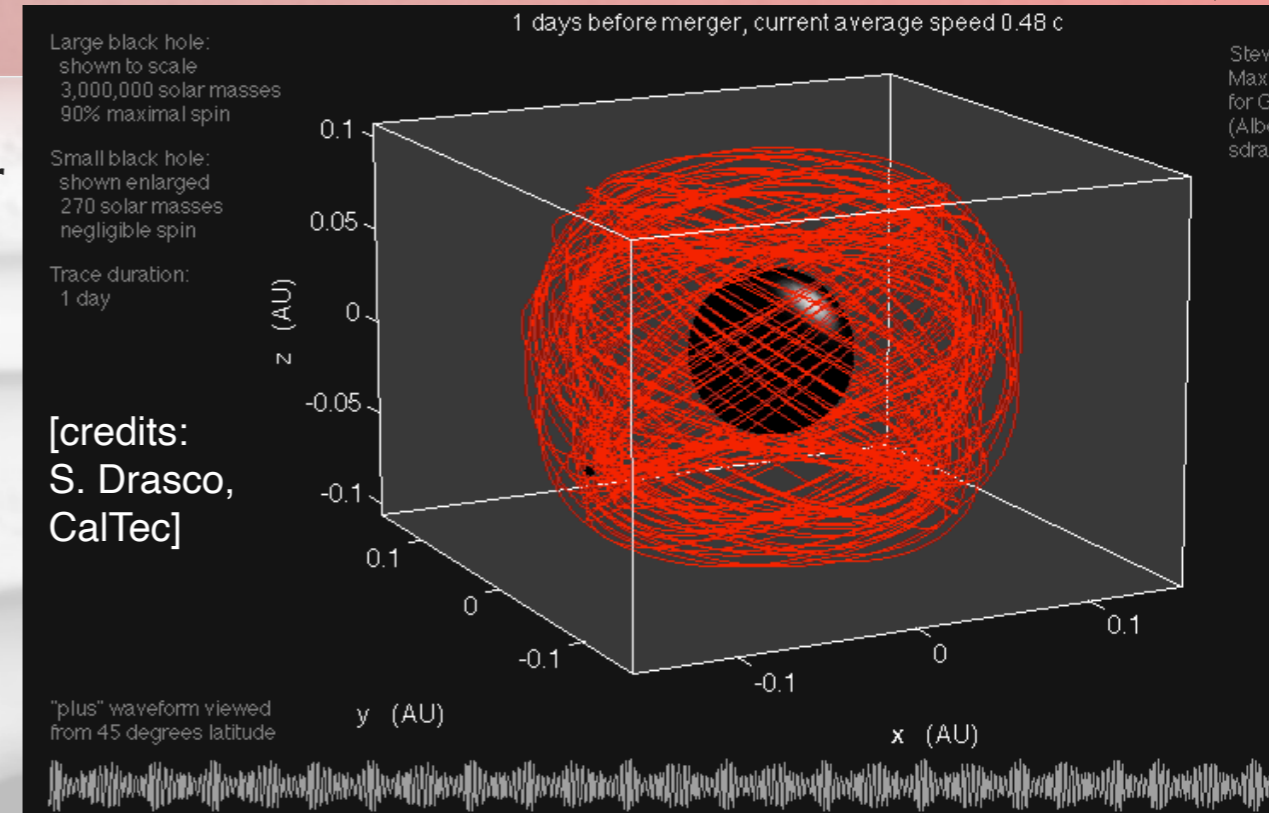
- companion : NS, stellar mass BH
 - very eccentric orbit shrinking under GW radiation

- EMRI: Binary system with an extreme mass ratio: $10^{-7} - 10^{-5}$

- $\sim 10^6$ orbits of the compact object close to the MBH before the plunge

- Companion as 'test particle'

- Strong relativistic effects
 - Complex (and very informative...) waveforms



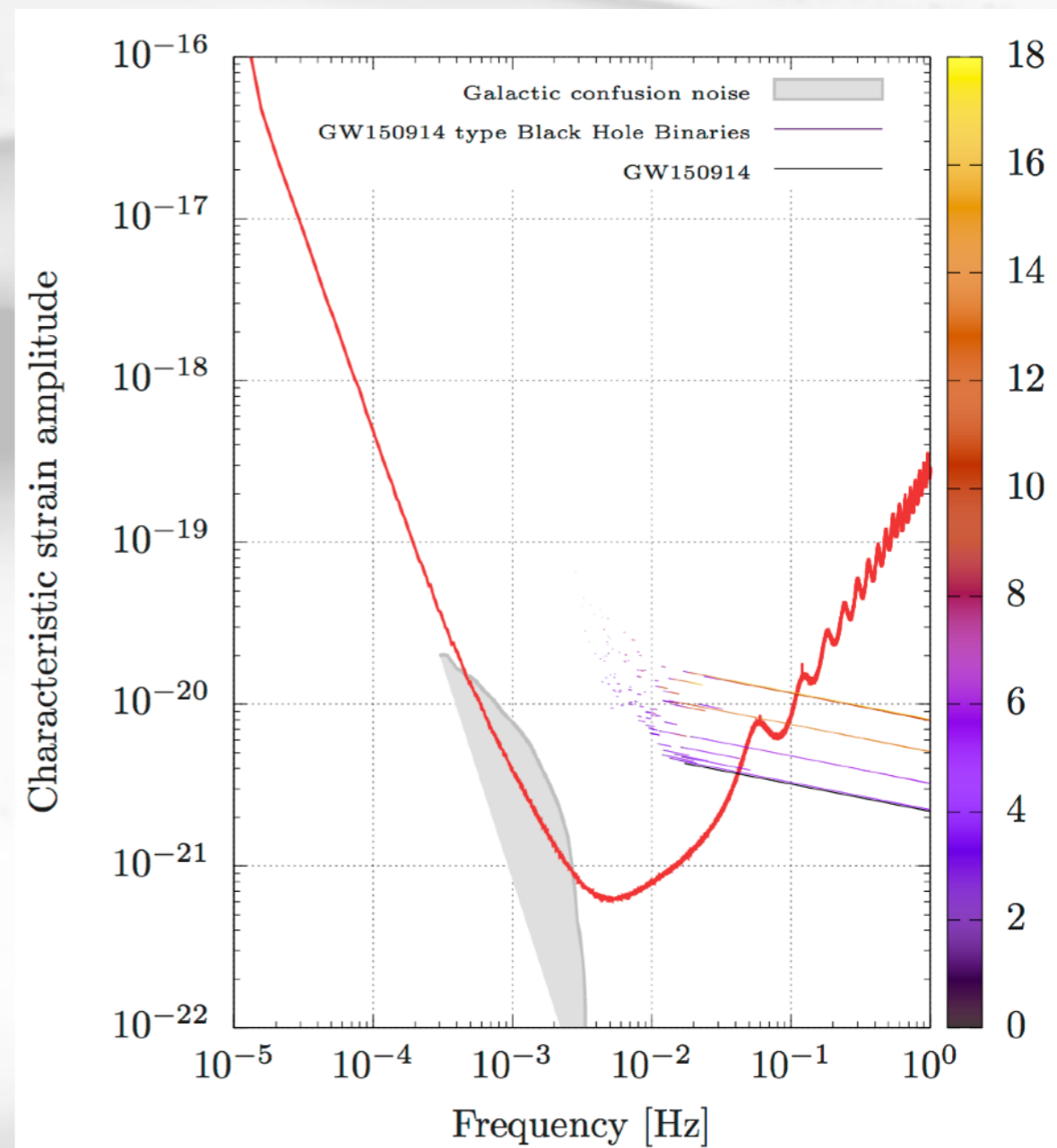
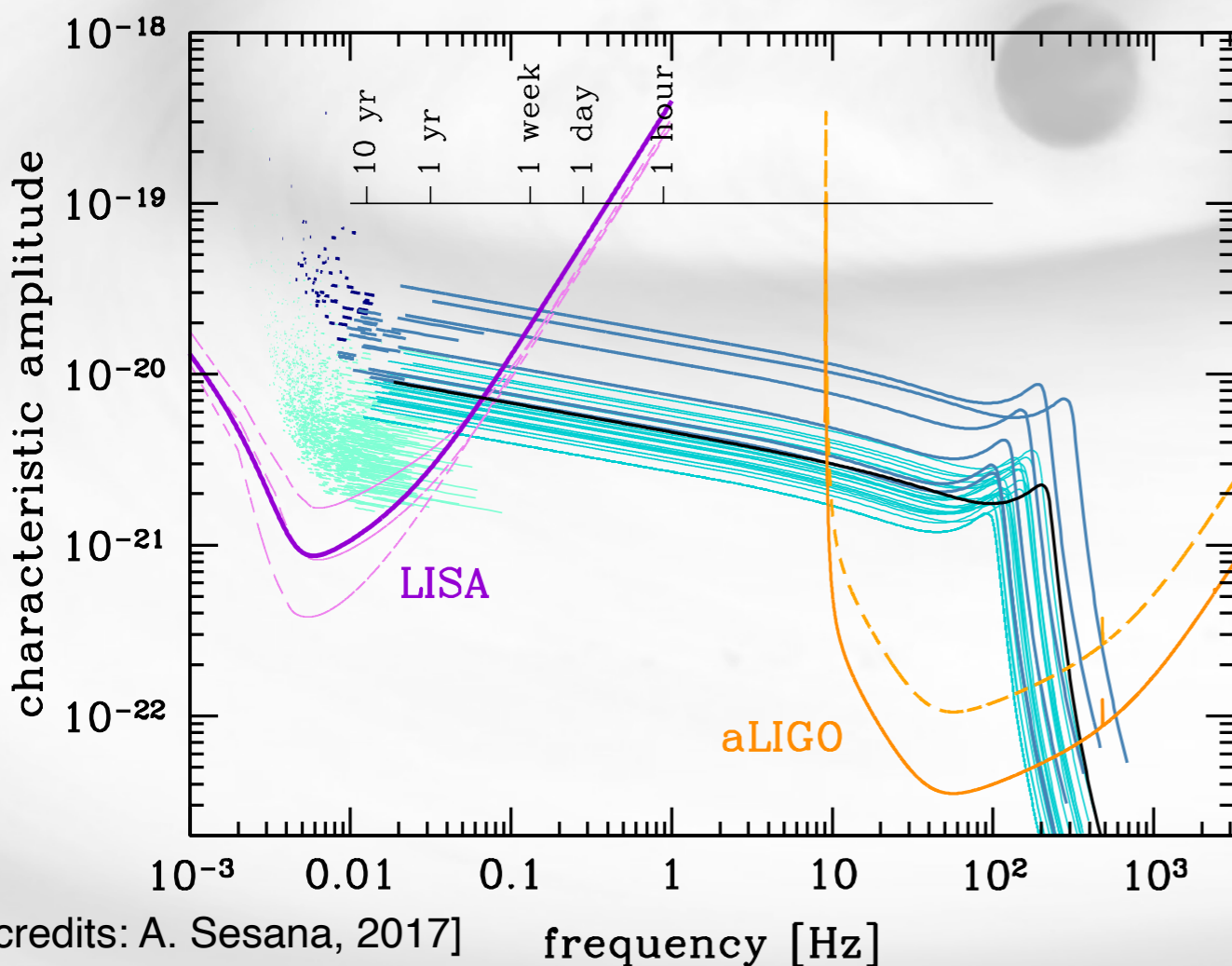
Stellar BH may be detectable by LISA prior coalescing in the ground based detectors band

Observed for ~years in LISA until ~days before merger

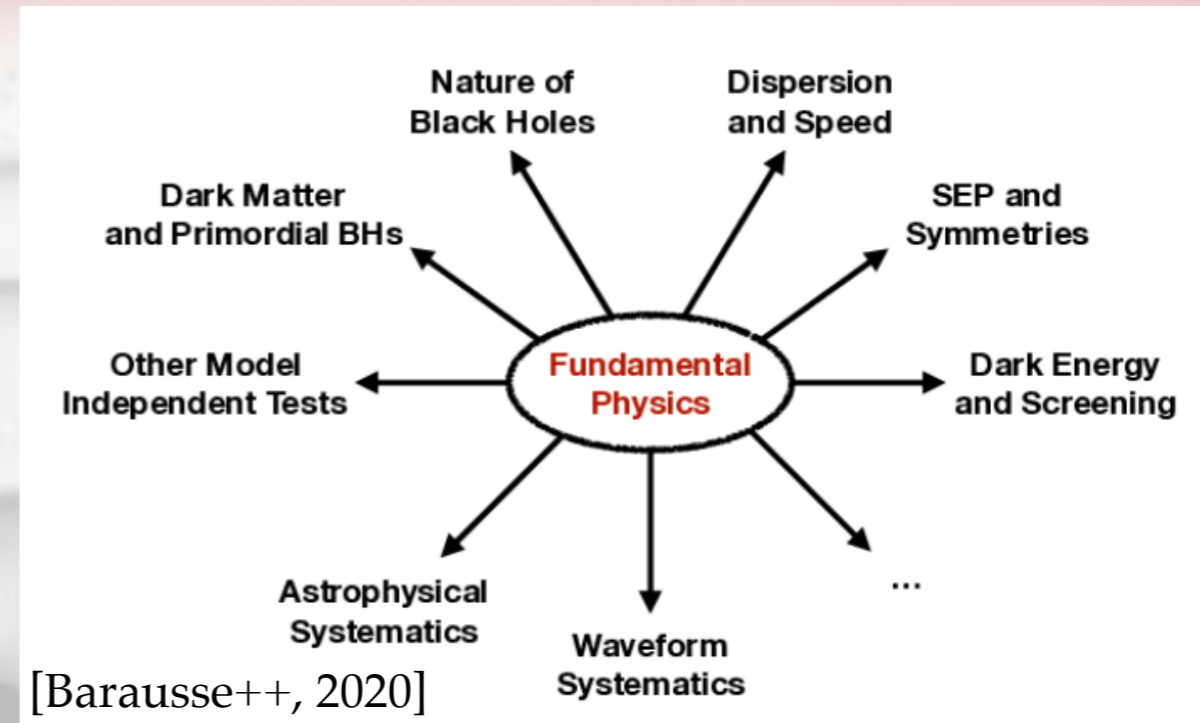
Possible pre-warning

Time of coalescence at ~10s accuracy

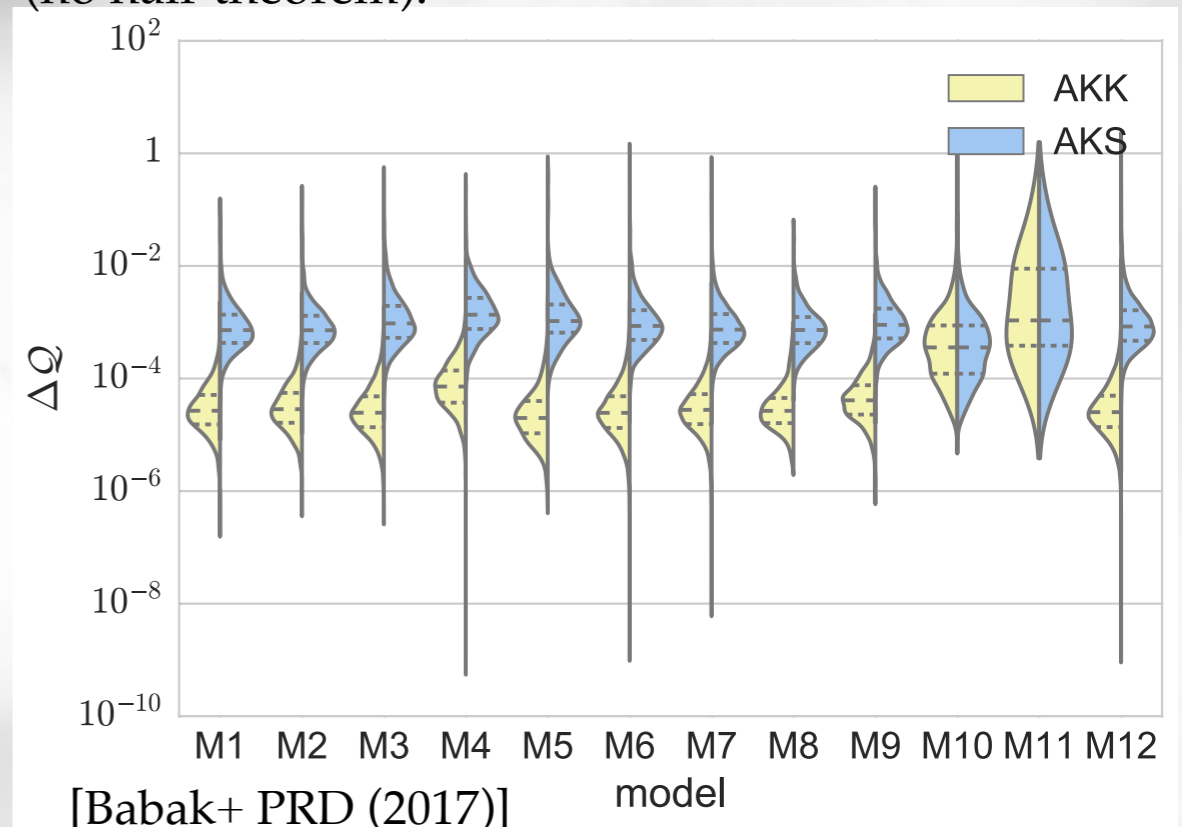
Sky localisation : 0.1 - 1 deg²




- 🚀 Using emitted GW to map the spacetime structure
- 🚀 Tests of GR
 - 🚀 Fundamental principles and symmetries of GR
 - 🚀 Testing GR with compact objects
- 🚀 Tests of the Nature of Black Holes
- 🚀 Dark matter and Primordial Black Holes
- 🚀 Model-independent tests
 - 🚀 Consistency of GR vs constraining Modified Gravity
 - 🚀 Parametrized tests
 - 🚀 Other tests including: Polarisation, GW propagation, Stochastic GW Background
- 🚀 Astrophysical and Waveform systematics



Deviation in quadrupole moment from Kerr value (no hair theorem):



 Possible X-ray emission during the late stages of the SMBH inspiral (days to hours before final merger) comes from:

 **Circumbinary disc:**

 X-ray emission in soft x-rays ($\leq 1\text{keV}$)

 **Mini-discs around black holes**

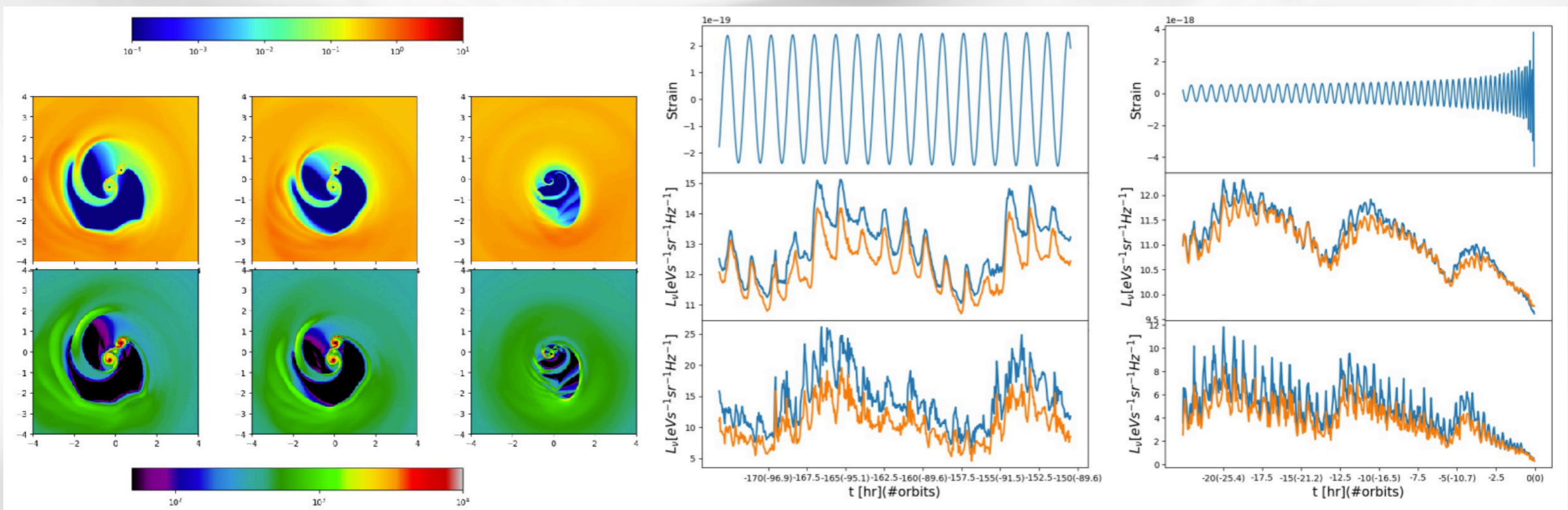
 Hard x-ray emission ($\geq 10\text{keV}$) from accretion of minidisks individually onto each black hole

 **Interaction of circumbinary and mini discs:**

 Accretion of circumbinary disc onto mini-discs via optically thick streams

 Thermal radiation dominated by the inner edge of the circumbinary disc, producing soft x-rays ($\sim 2\text{keV}$)

 X-ray emission shows clear modulation on timescales as short as a few hours



LISA may help on many cosmological problems

Expansion rate of the Universe : late acceleration ?

CMB : $H_0 = 66.93 \pm 0.62 \text{ km.s}^{-1}.\text{Mpc}^{-1}$

SN Ia : $H_0 = 73.5 \pm 1.4 \text{ km.s}^{-1}.\text{Mpc}^{-1}$

Dark energy

Cosmological constant ?

Early dark energy: DE evolves with redshift and contributes to rate of expansion at $z > 1$

Modification of GR on large scale

LISA can probe the Universe at different scales

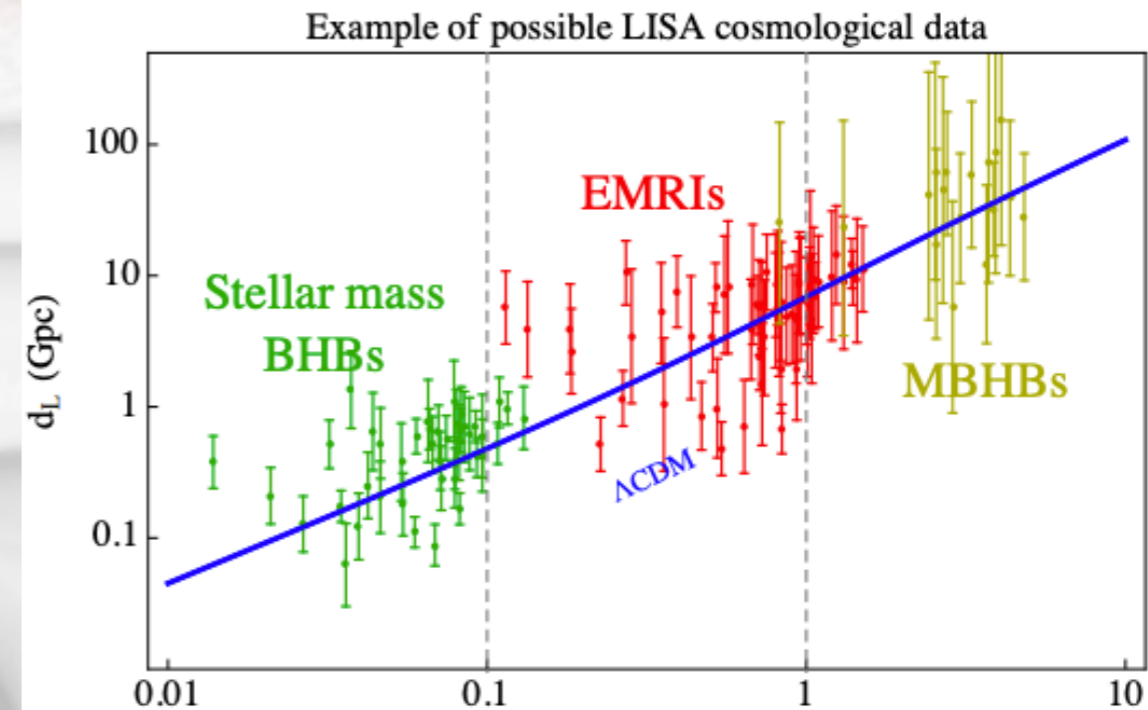
Use BHBs merger events as standard sirens

Requires the knowledge of the redshift

from e/m counterpart of the host galaxy

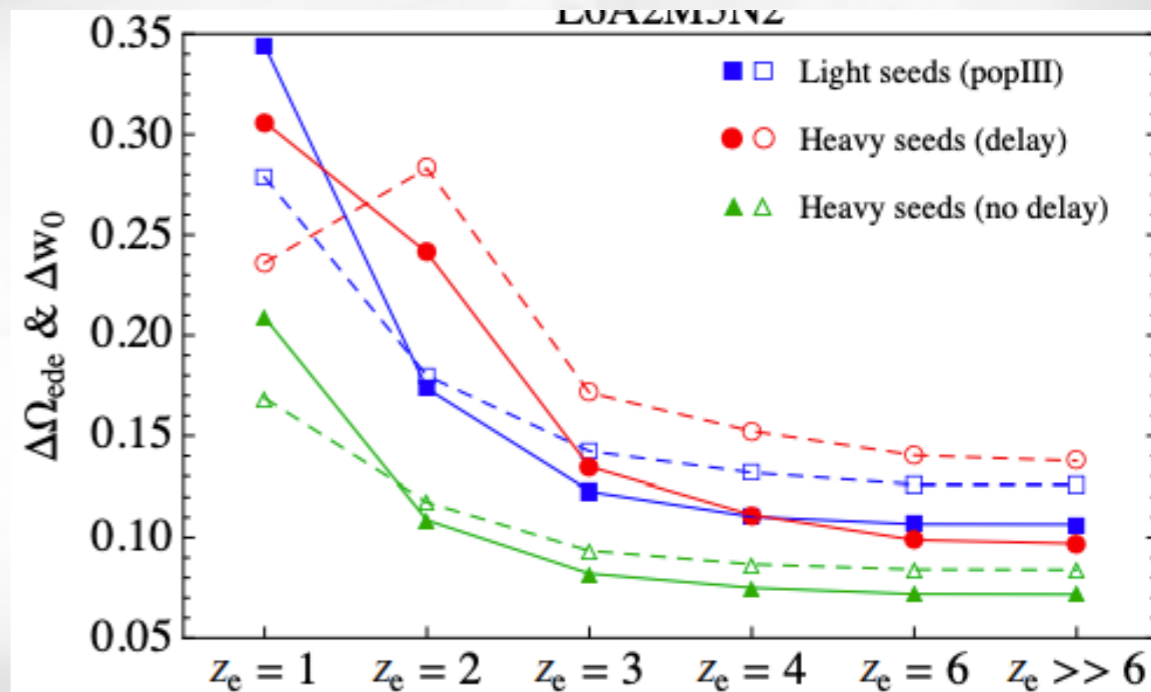
or from statistical inference

Universe expansion rate from GW events :



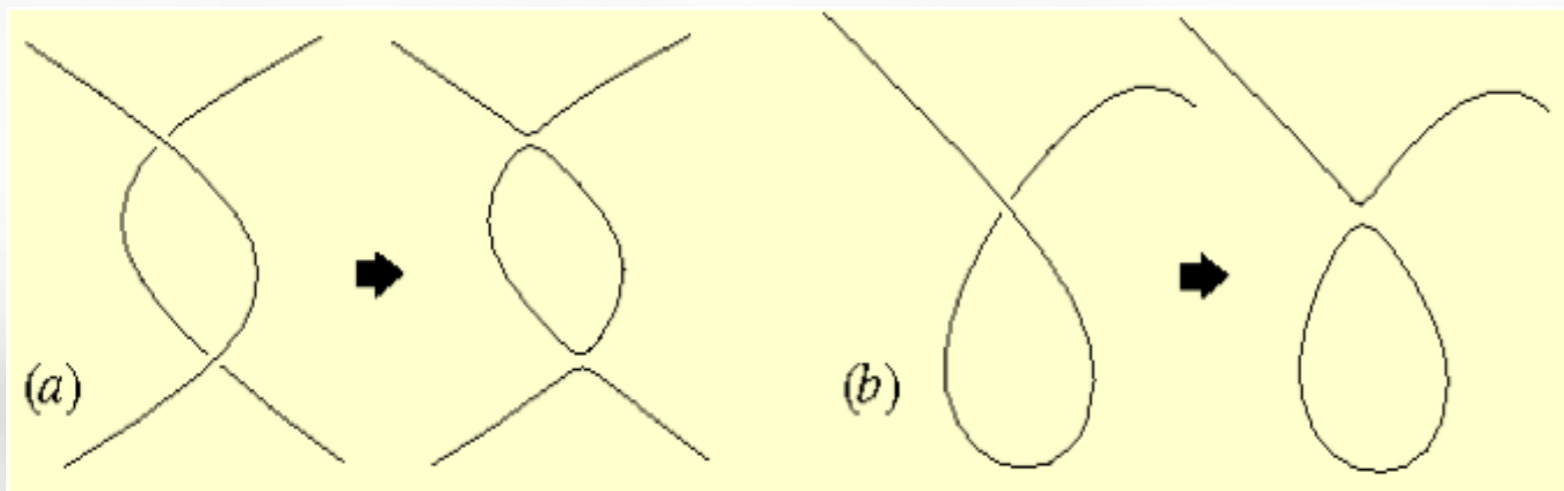
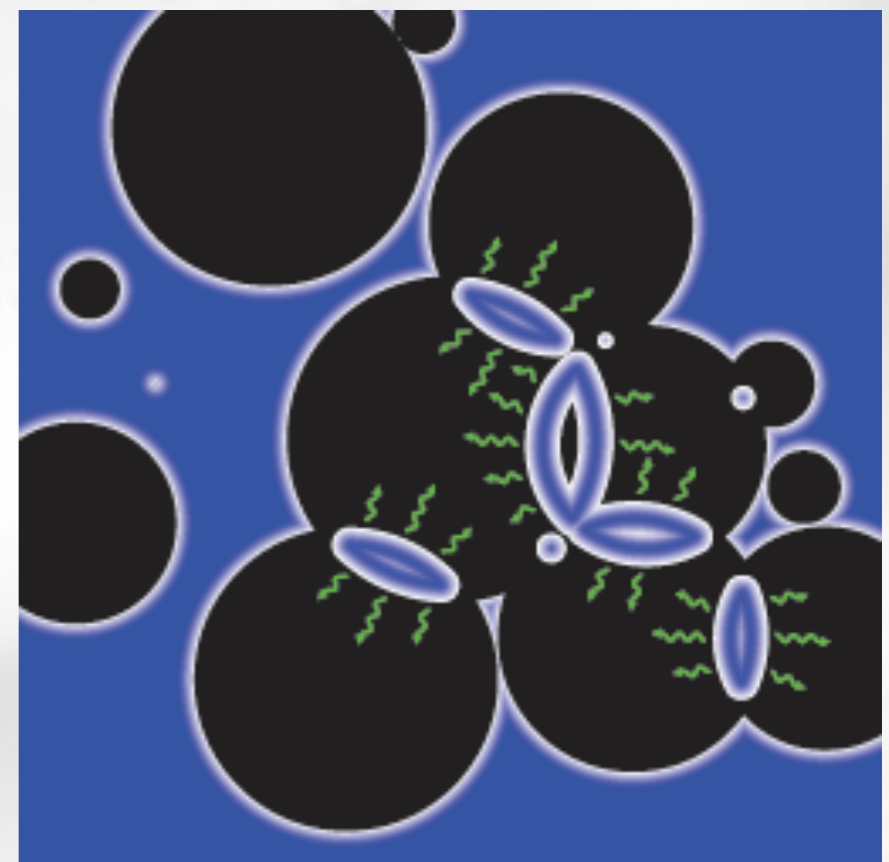
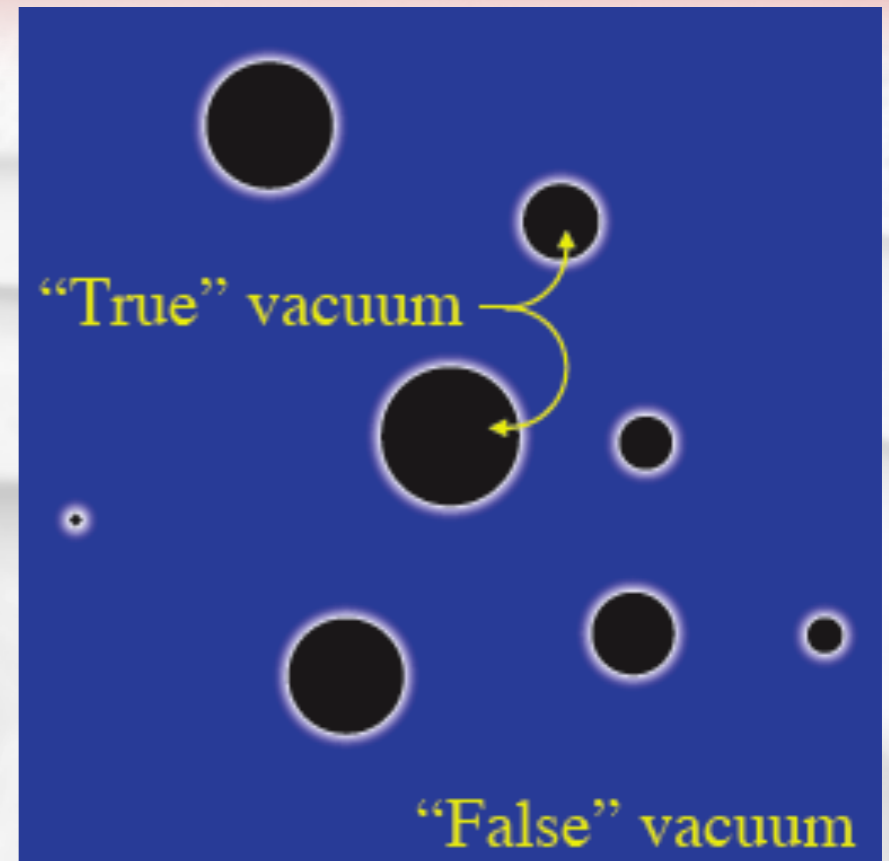
N. Tamanini J. Phys. CF 2016

Universe DE content:



Ch. Caprini, N. Tamanini JCAP 2016

- Violent processes in the early Universe may produce stochastic GW background (SGWB)
- First order phase transition
 - Collision of true vacuum bubbles and conversion to the symmetry-broken phase accompanied with anisotropic stresses.
 - The LISA band (10^{-4} - 0.1 Hz) corresponds to the energy scale of the EW (electroweak) phase transition (up to 10^4 TeV).
 - Formation of sound wave, shocks and turbulence in the plasma
- Cosmic strings:
 - A network of strings formed in the early Universe generates SGWB (as superposition of many uncorrelated sources) and (possibly) individual bursts



Many sources ...

- Compact galactic binaries
- Coalescence of SMBH
- Extrem mass inspirals
- Stochastic background from the early Universe
-

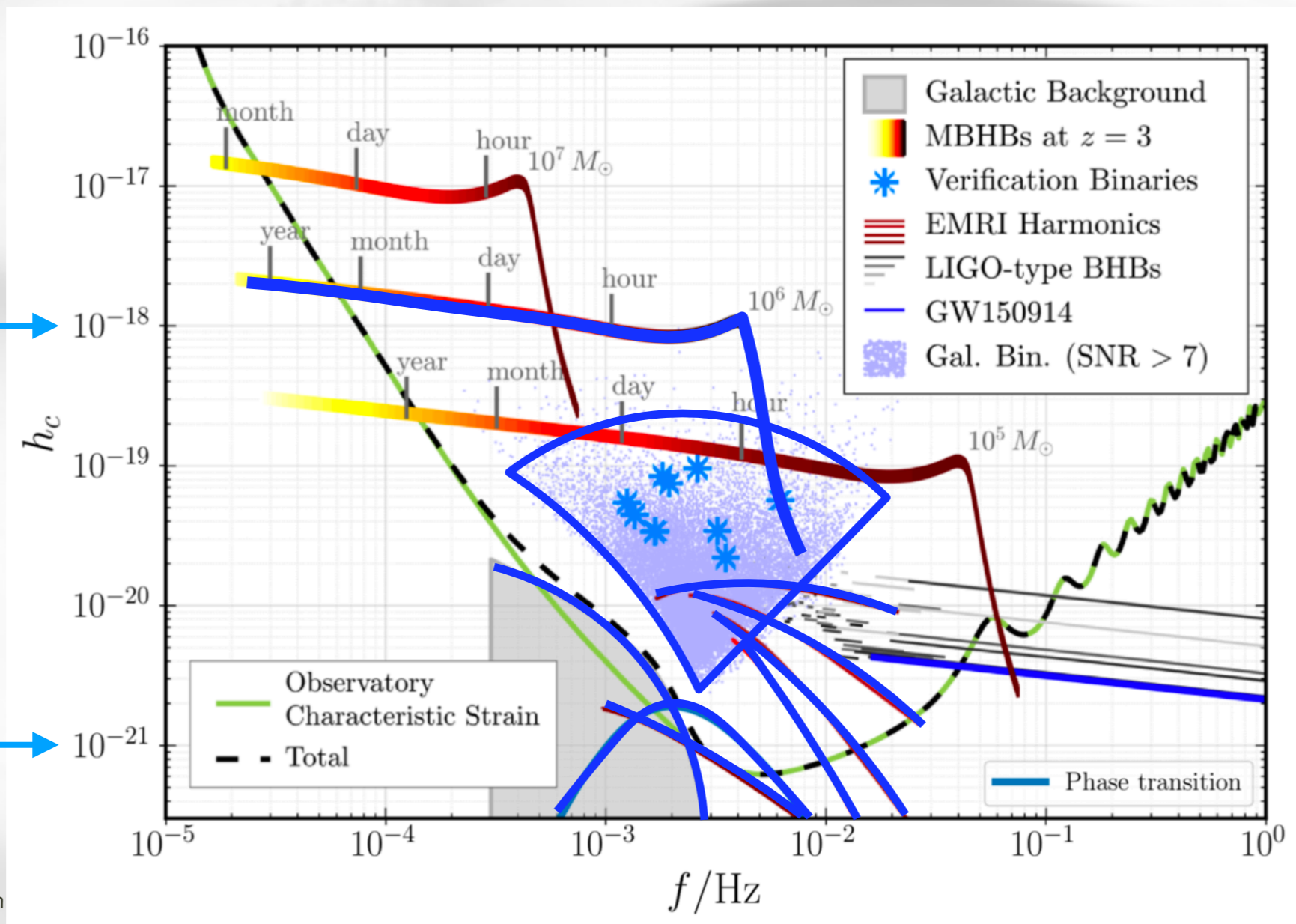
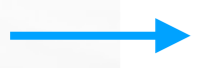
... to answer important scientific questions

- Formation and evolution of compact binaries
- Origin and evolution of BH since the early ages
- Strong field tests of GR
- Estimation of cosmological parameters
- ...

1 nm/Mkm



1 pm/Mkm



- *Introduction*
- *LISA Science Objectives*
- **From LISA Pathfinder to LISA**
- *Mission description*
- *Conclusion*

Why going to space ?

Ground-based interferometers are limited by seismic and Newtonian noises

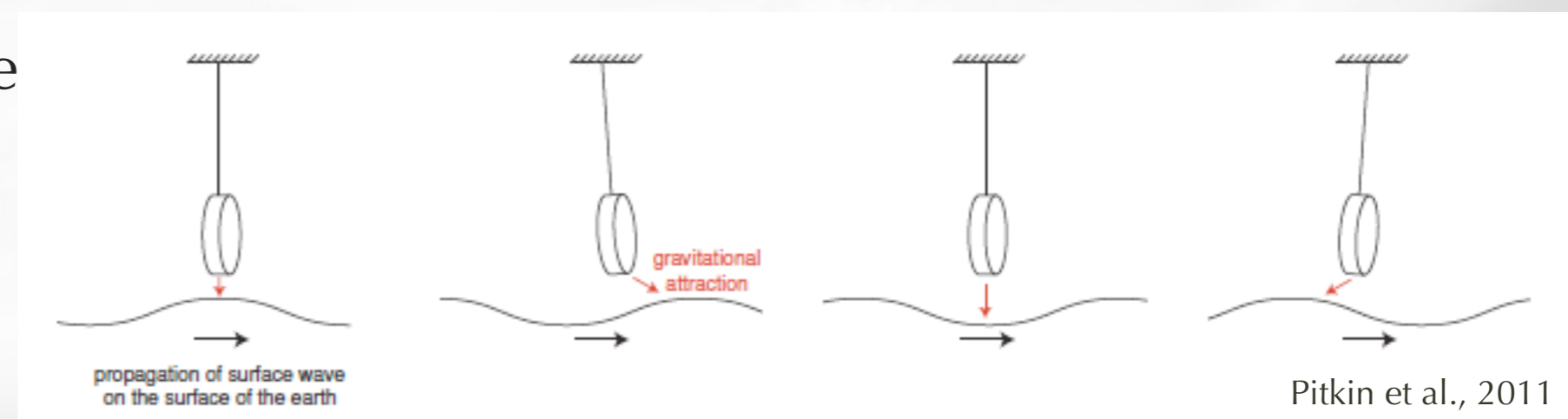
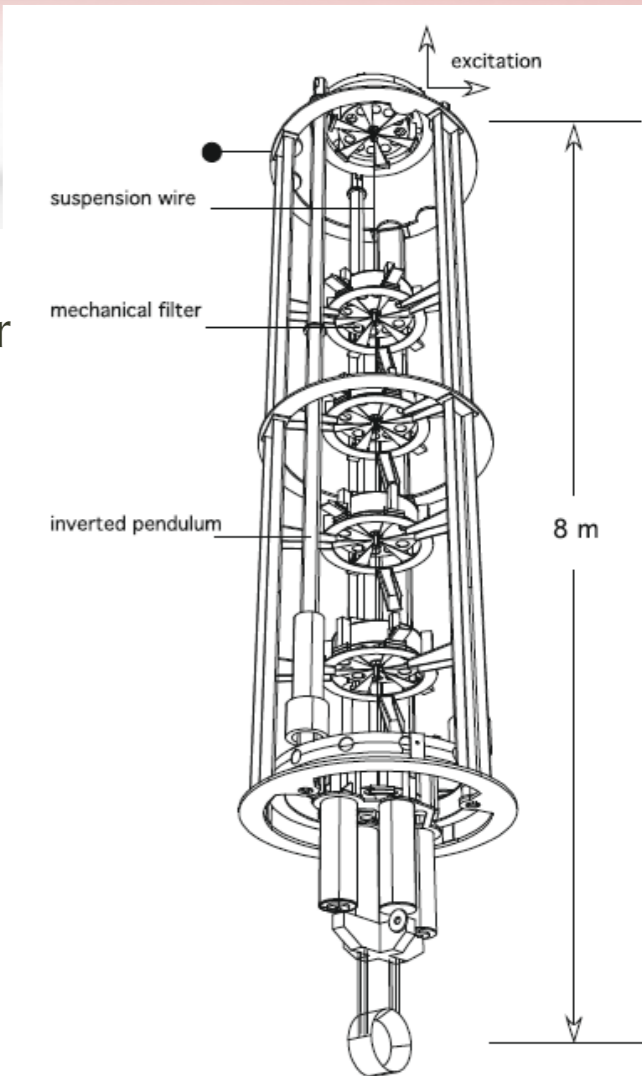
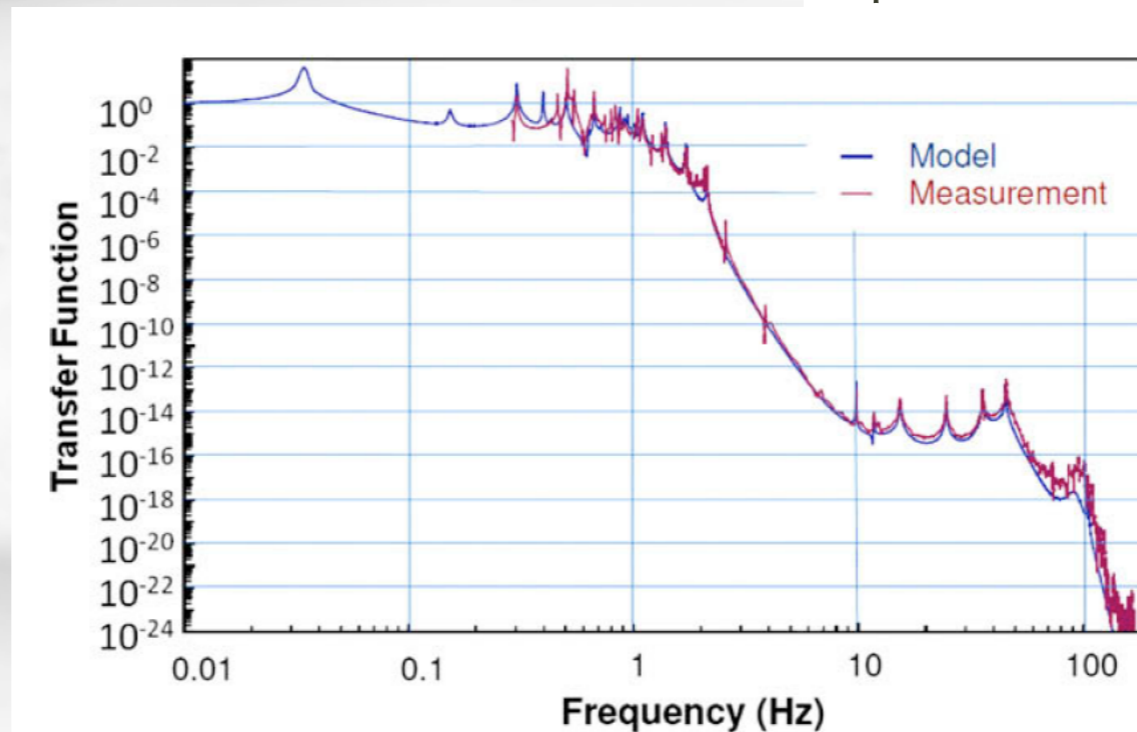
Detection bandwidth ≈ 10 's Hz

(very) long armlength are possible

On ground :
a few km max (eq. to
100's km using cavities
and folding mirrors)

\rightarrow mHz GW observations only possible from space

VIRGO superattenuator





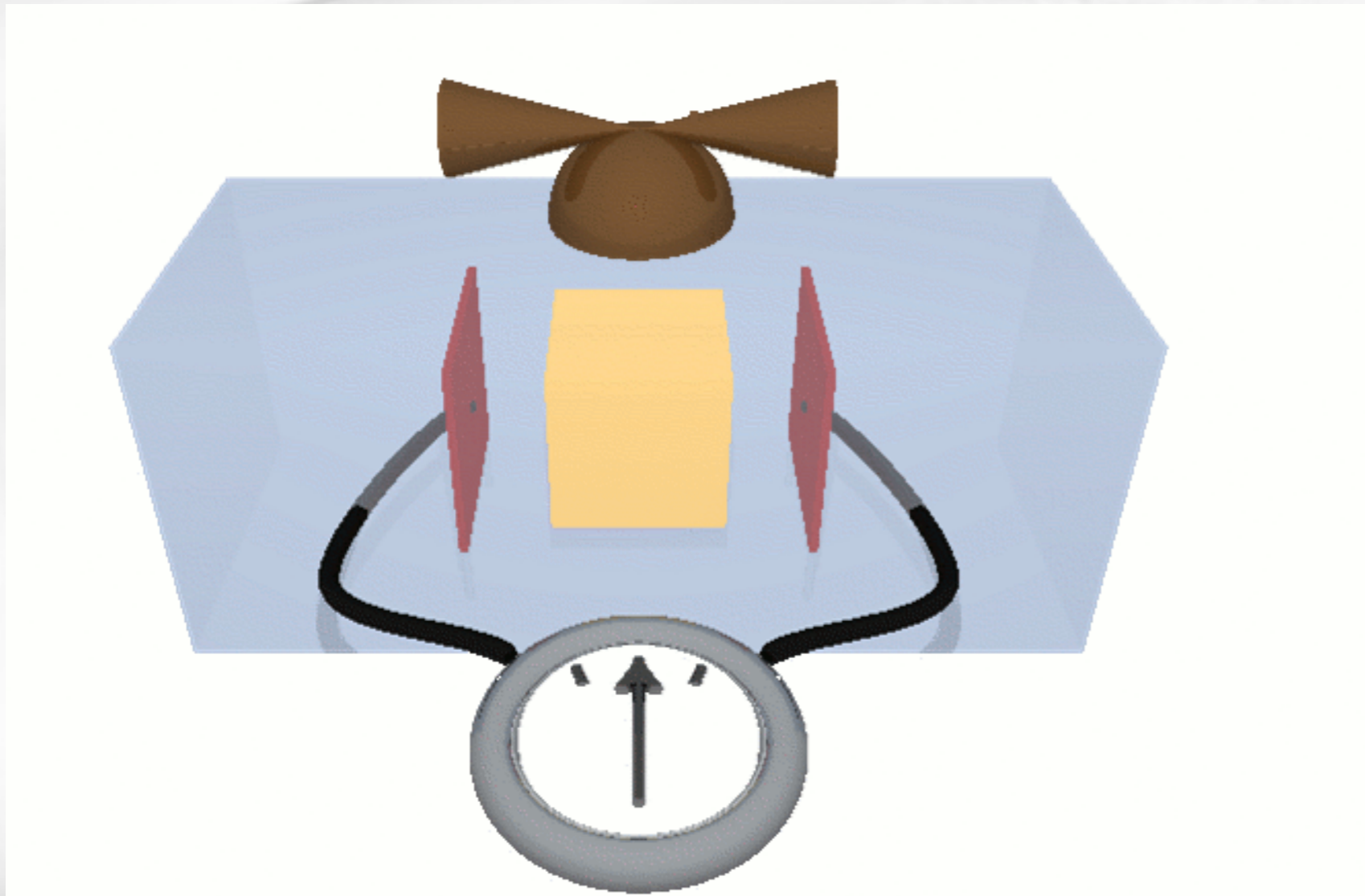
🚀 LISA = Laser Interferometer
Space Antenna

- 🚀 Space-borne, million-km arms, interferometer between free-floating test masses
- 🚀 Response bandwidth : ~ 0.1 mHz - 1 Hz
- 🚀 'Large' ESA mission (Phase B), launch expected in ~ 2035

🚀 LISA Pathfinder = technology demonstrator for LISA

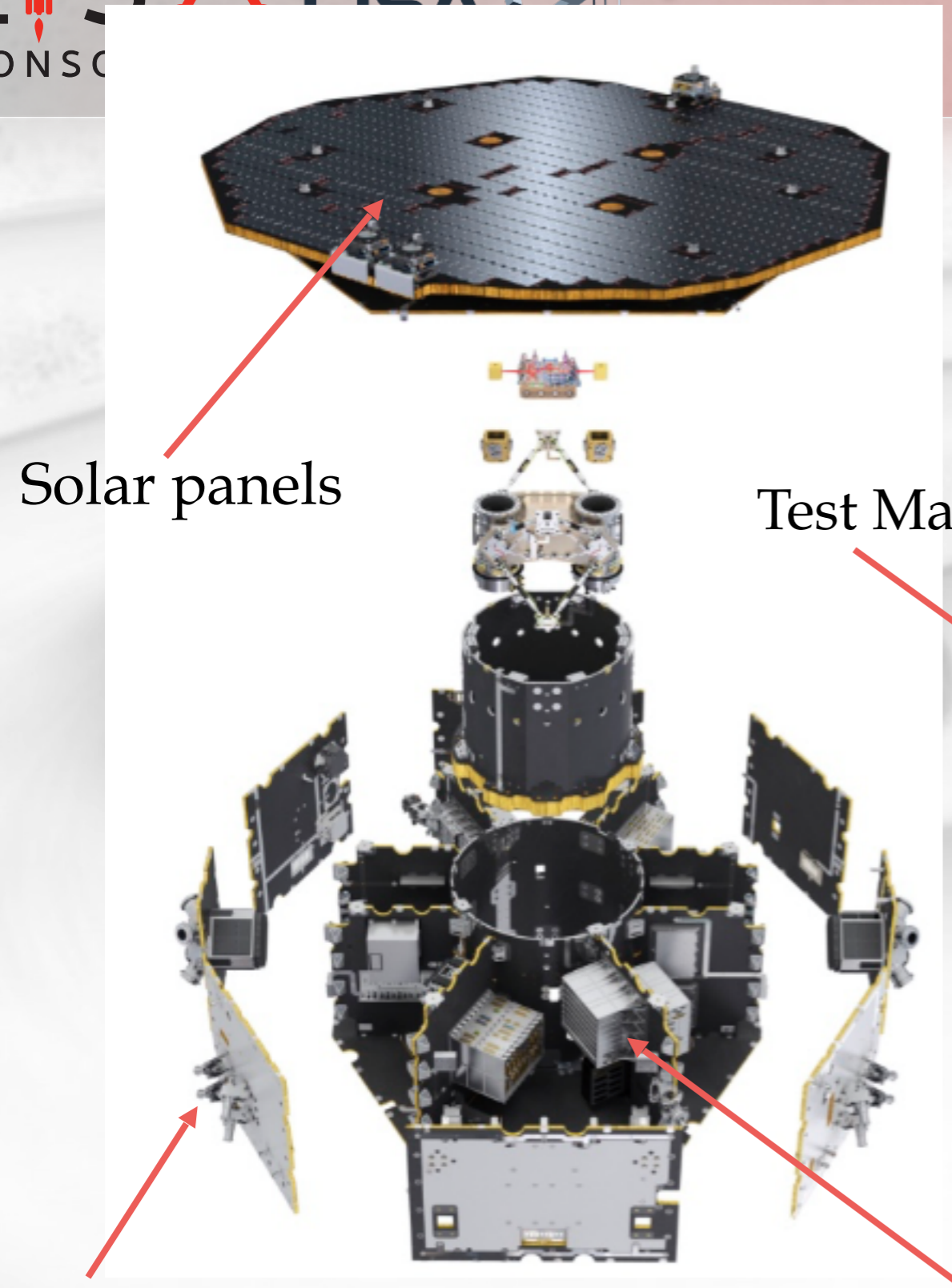
- 🚀 Launched in December 2015
- 🚀 End of mission in July 2017

- Test masses must be protected from external perturbations (mainly solar wind)
- Technology demonstrator : LISA Pathfinder



- Main goal: demonstrate the possibility of "Free Fall" in space at the level of $\approx 10^{-14} \text{ m.s}^{-2}/\sqrt{\text{Hz}}$, around 1 mHz
- A number of effects had to be minimized:
 - The static gravitational potential between the TMs and the SC,
 - Residual links of the TMs w.r.t the SC via the residual vacuum,
 - Cross talk between various electrostatic actuators,
 - TM charging by cosmic rays that is eliminated by UV illumination,
 - Temperature fluctuations,
 - Magnetic field fluctuations,
 - ...

Lisa Pathfinder : A technology demonstrator

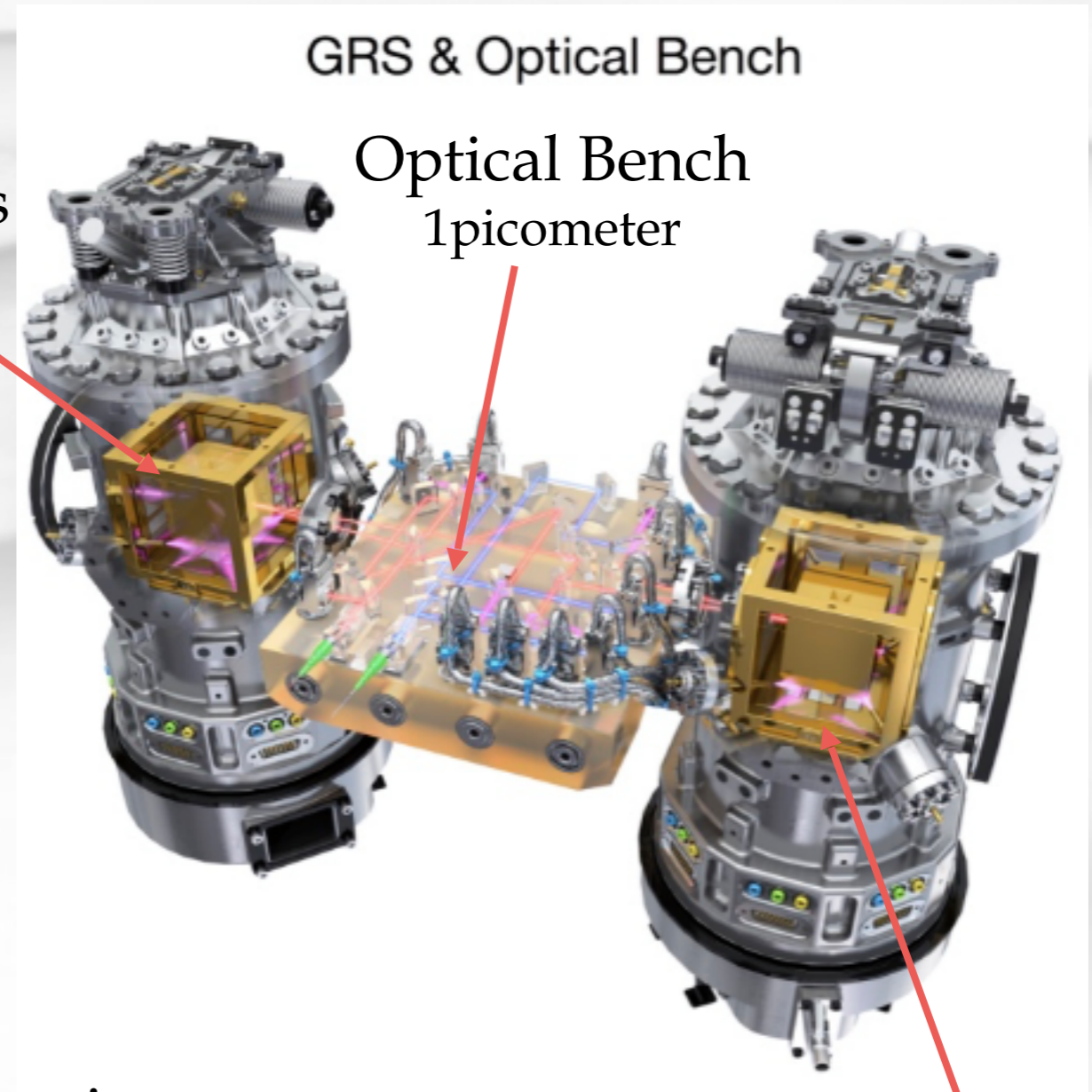


Solar panels

Test Mass

The micro-thrusters
 Cold Gas (μ -Newton)

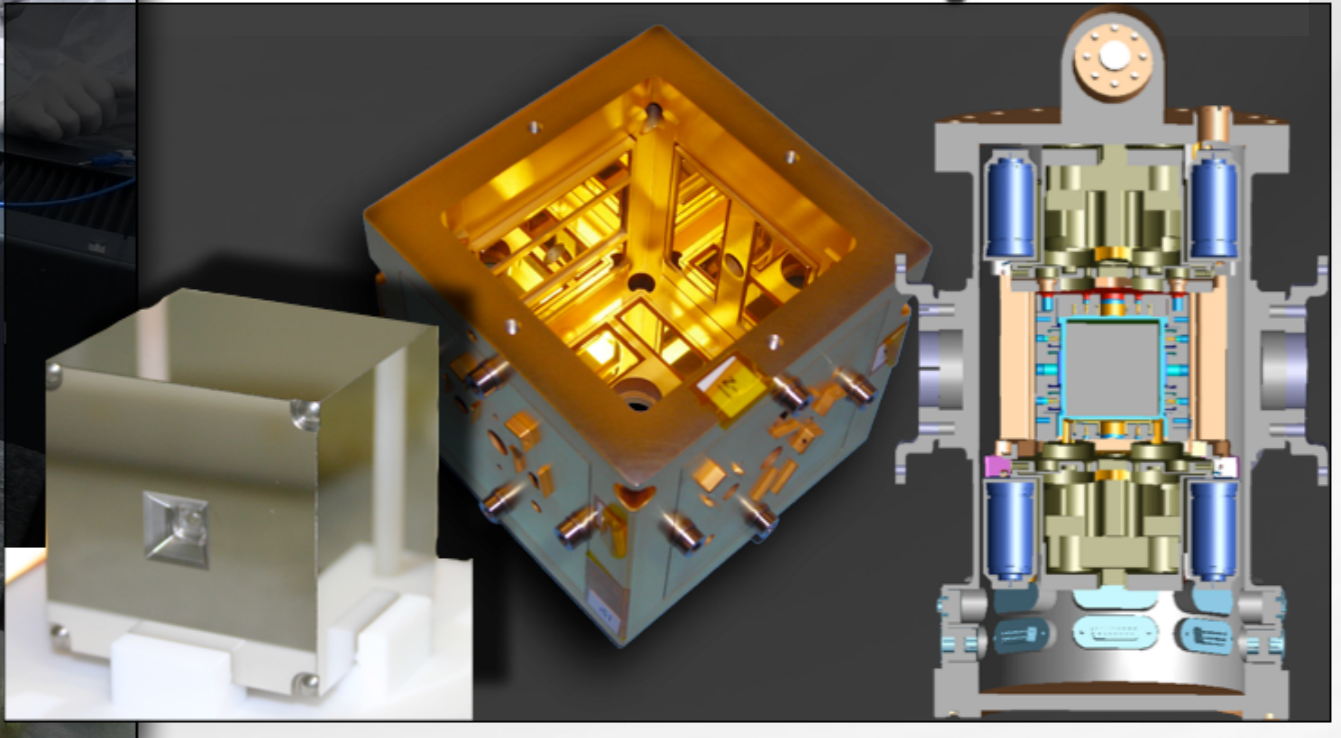
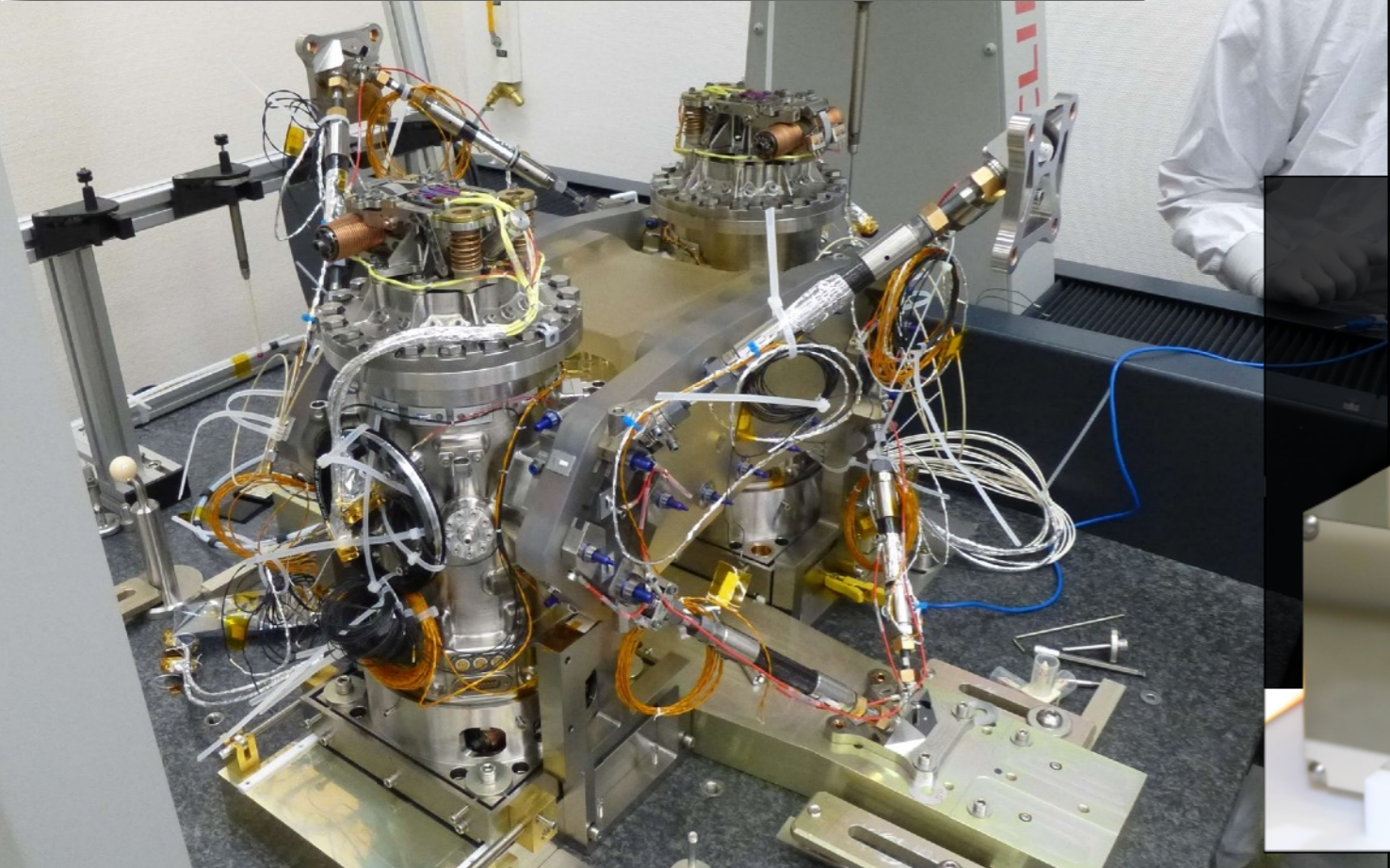
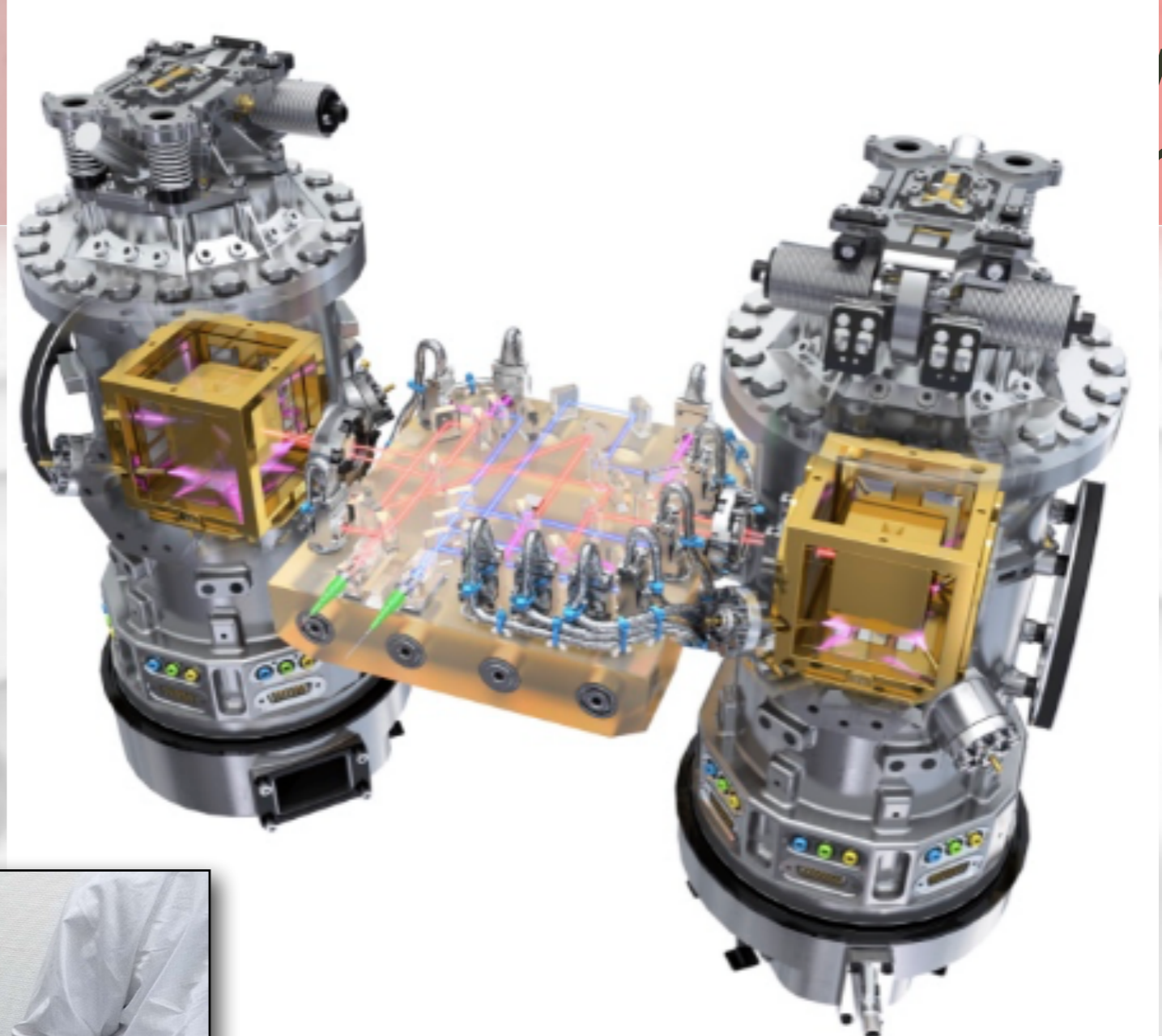
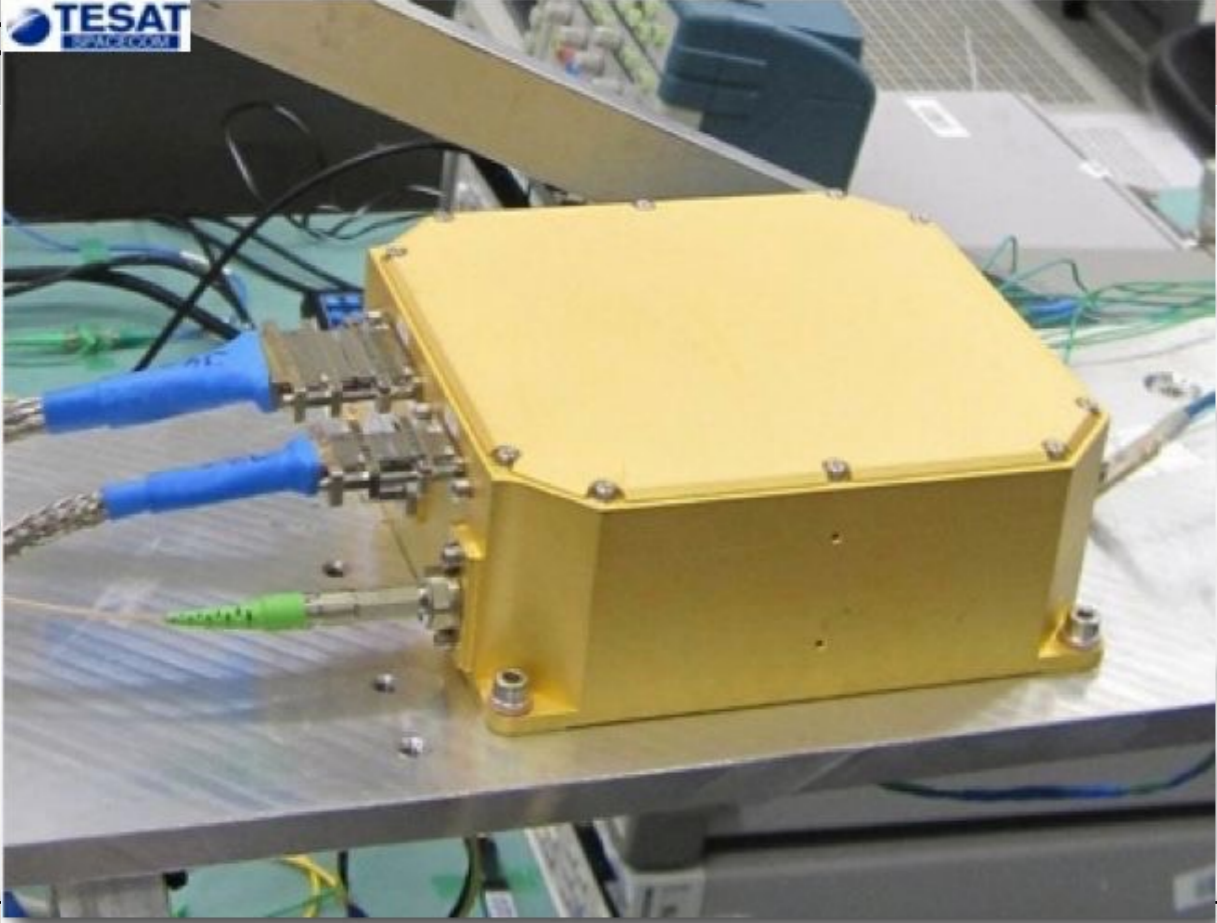
Electronics + computers



GRS & Optical Bench

Optical Bench
 1picometer

UV illumination





Testing inertial flight with LISA Pathfinder

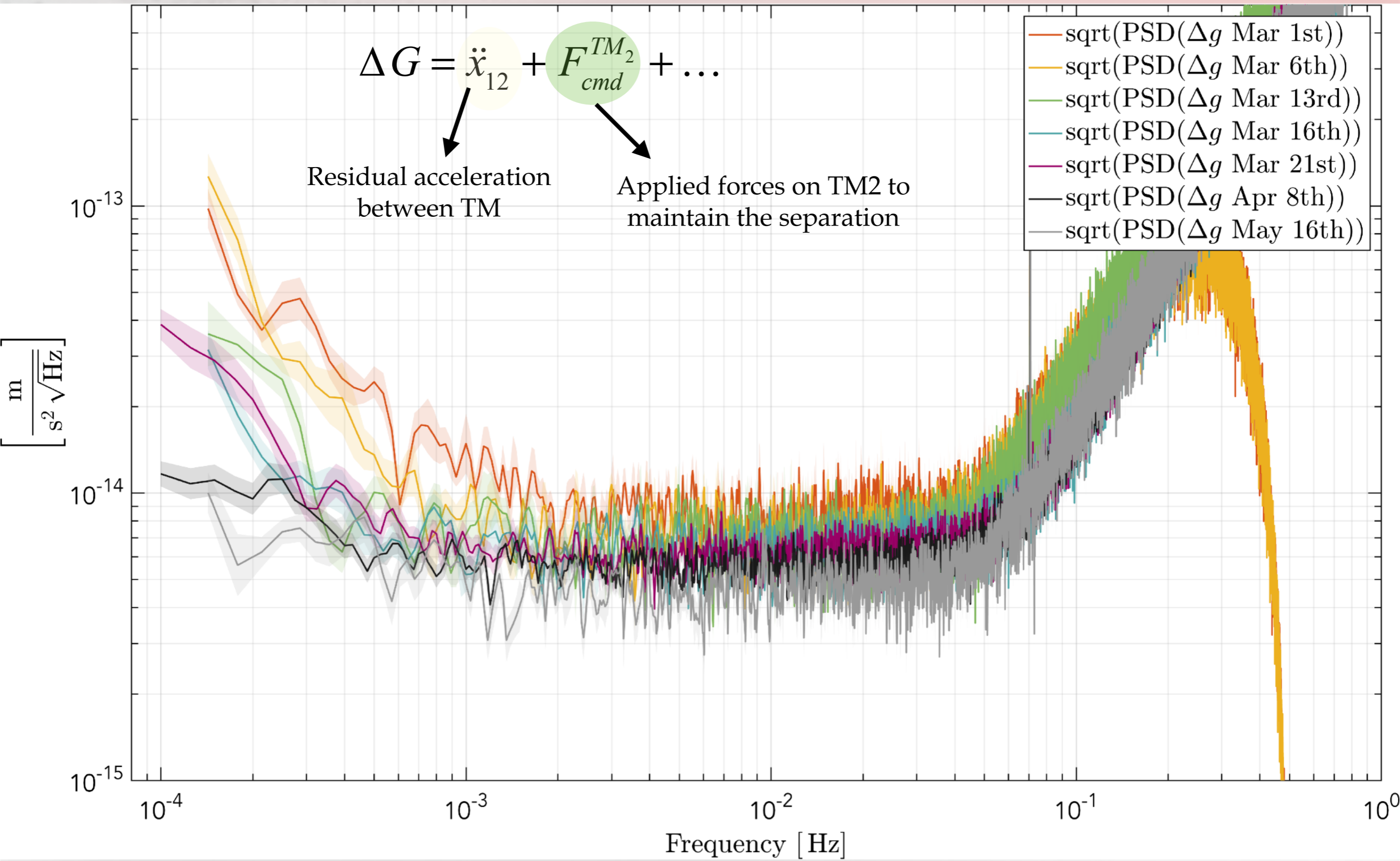




00:28



In-flight performance evolution



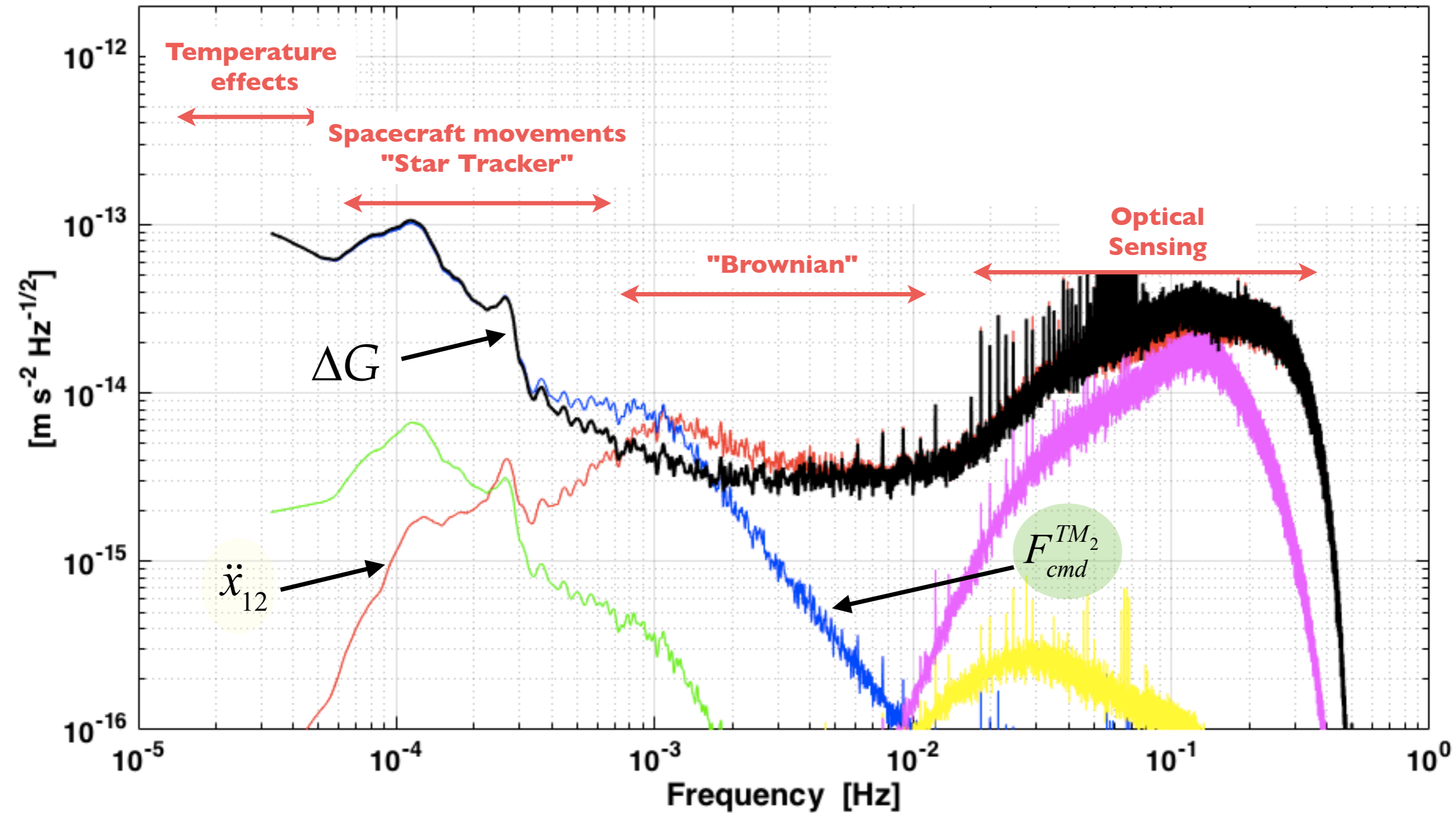
The Different Frequency Ranges

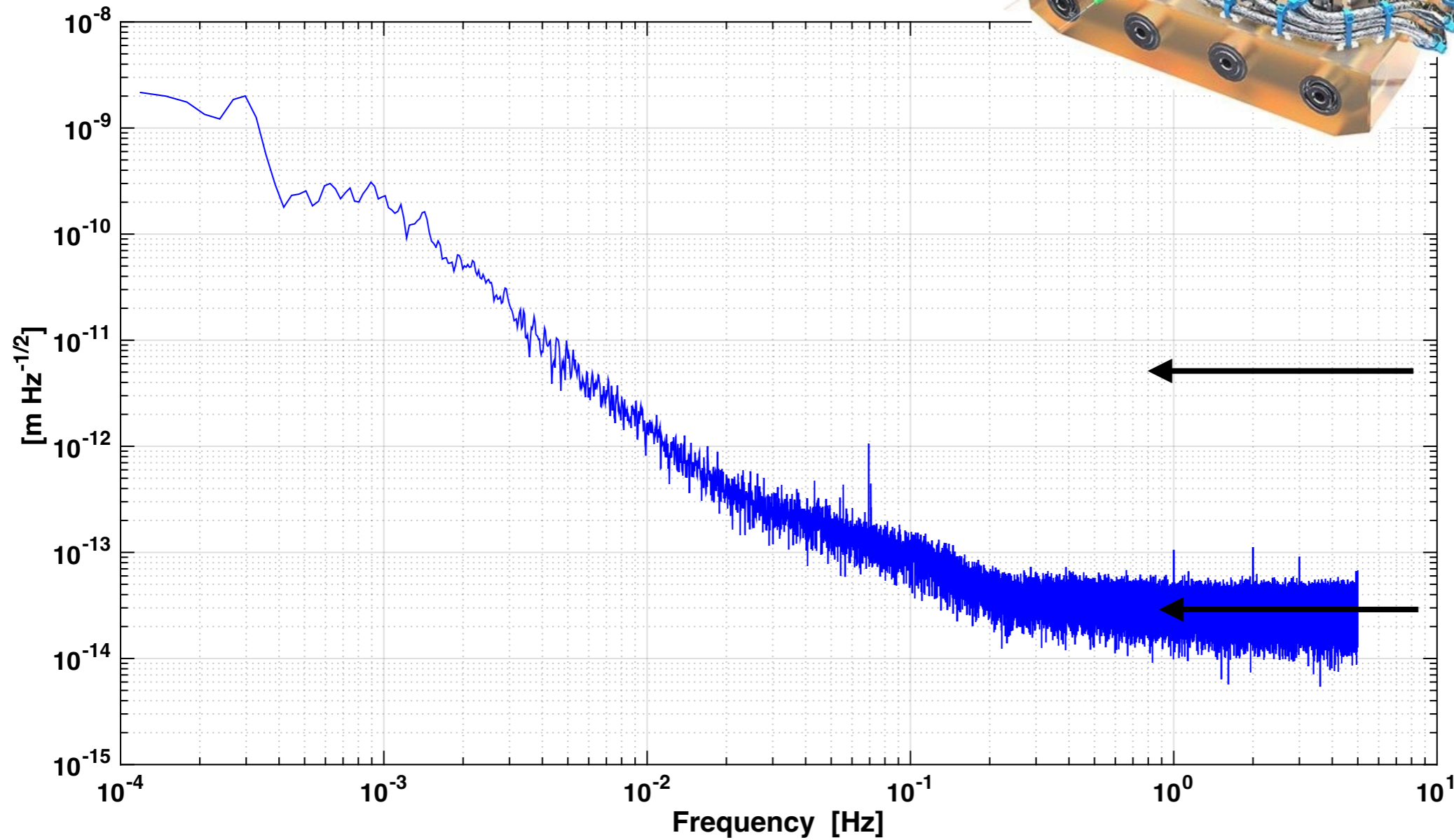
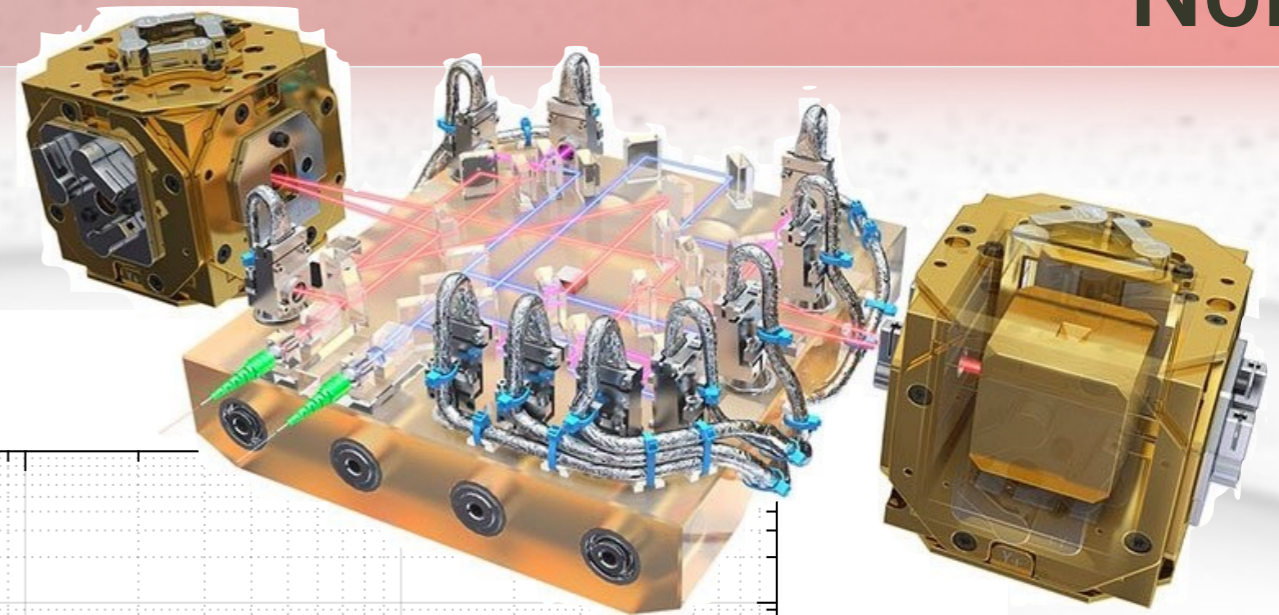
$$\Delta G = \ddot{x}_{12} + F_{cmd}^{TM_2} + \dots$$

x_{12} is measured by the optical bench

Obtained by "on board" telemetry and precisely calibrated.

Decomposition of LPF Residual ΔG

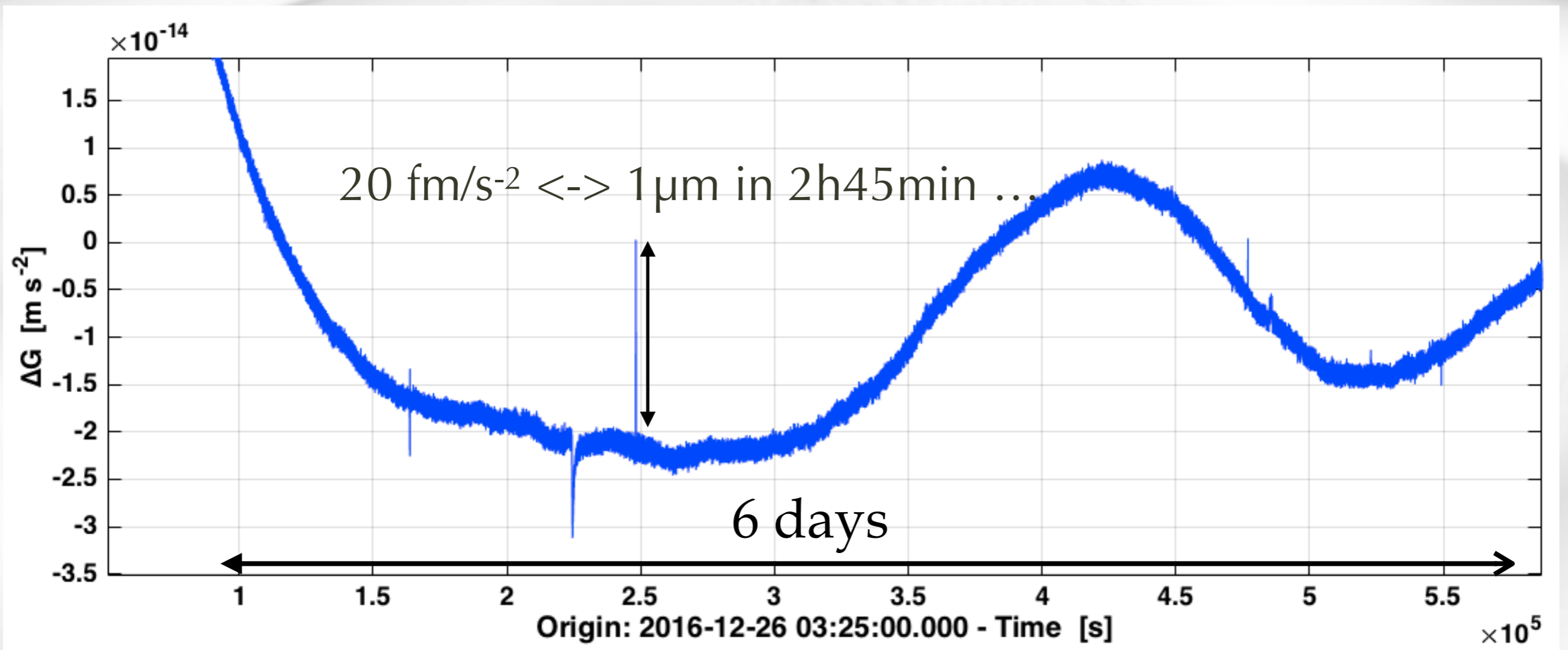




in the lab
6 pm/√Hz

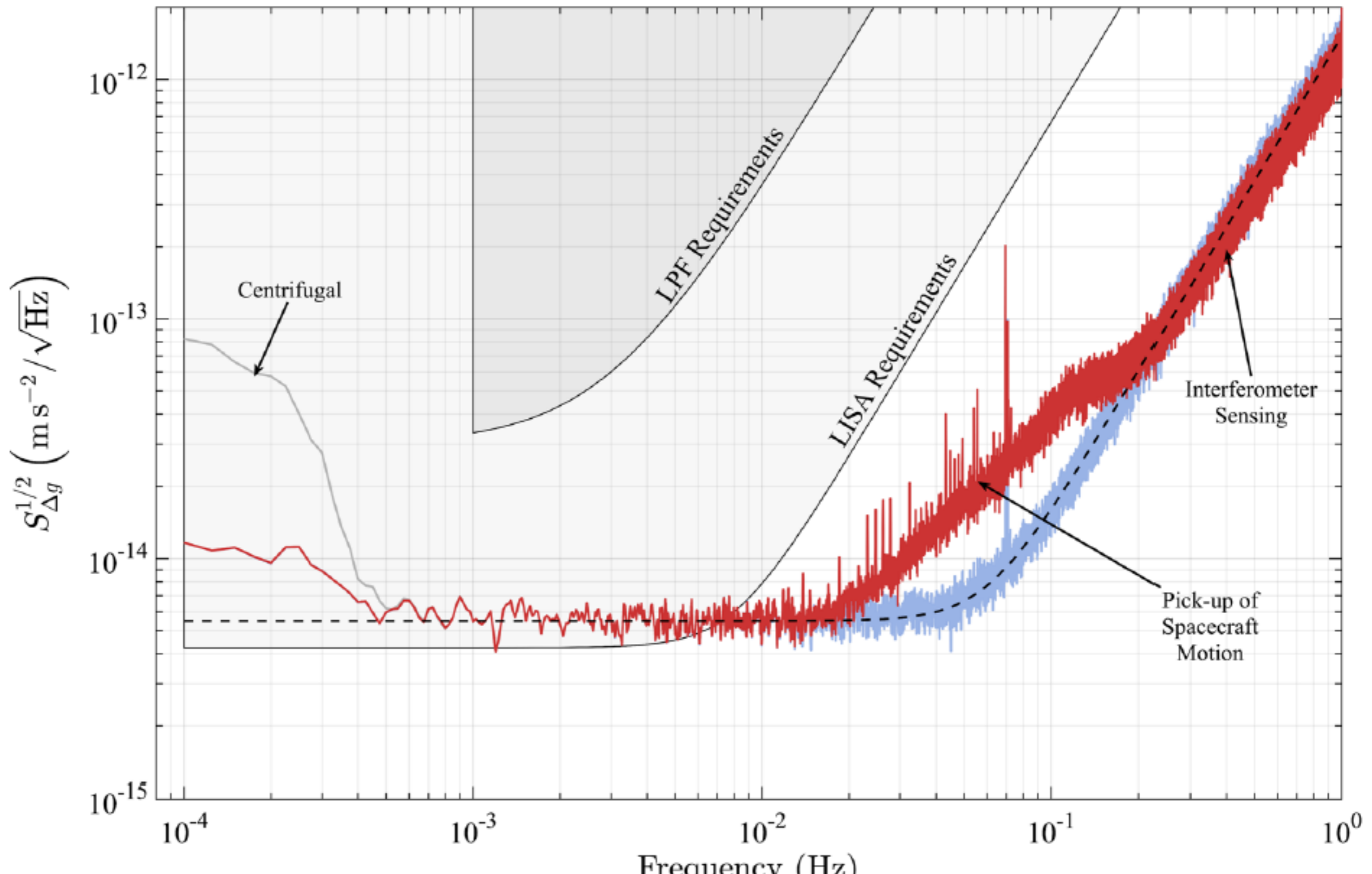
in space
30 fm/√Hz

- Occurred every ~ 1.5 days
- Caused by micro-meteorites and other unknown causes
- Modeled and subtracted from the data

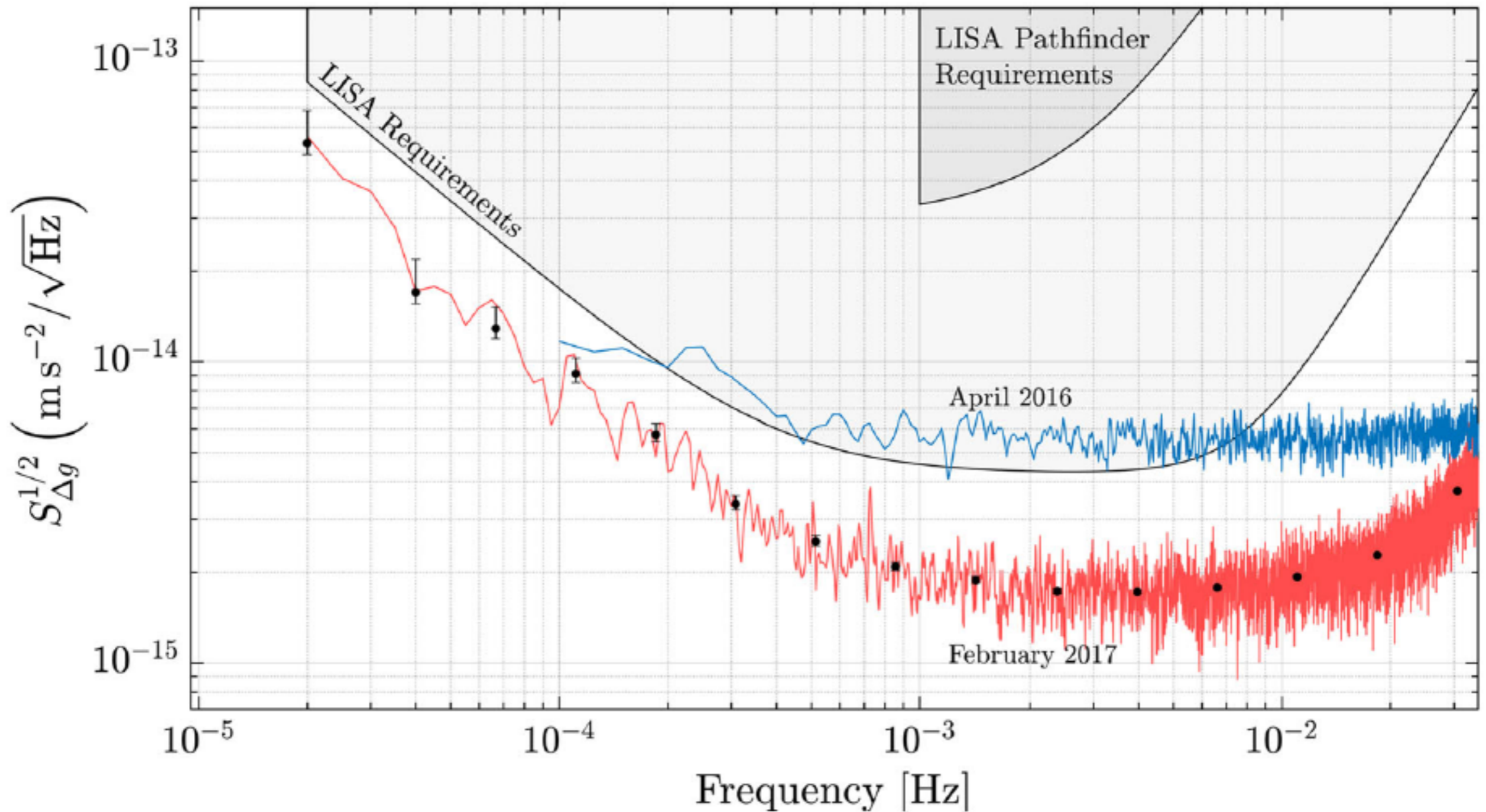




Sub-Femto-g Free Fall for Space-Based Gravitational Wave Observatories: LISA Pathfinder Results



Beyond the Required LISA Free-Fall Performance: New LISA Pathfinder Results down to $20 \mu\text{Hz}$



 *Introduction*

 *LISA Science Objectives*

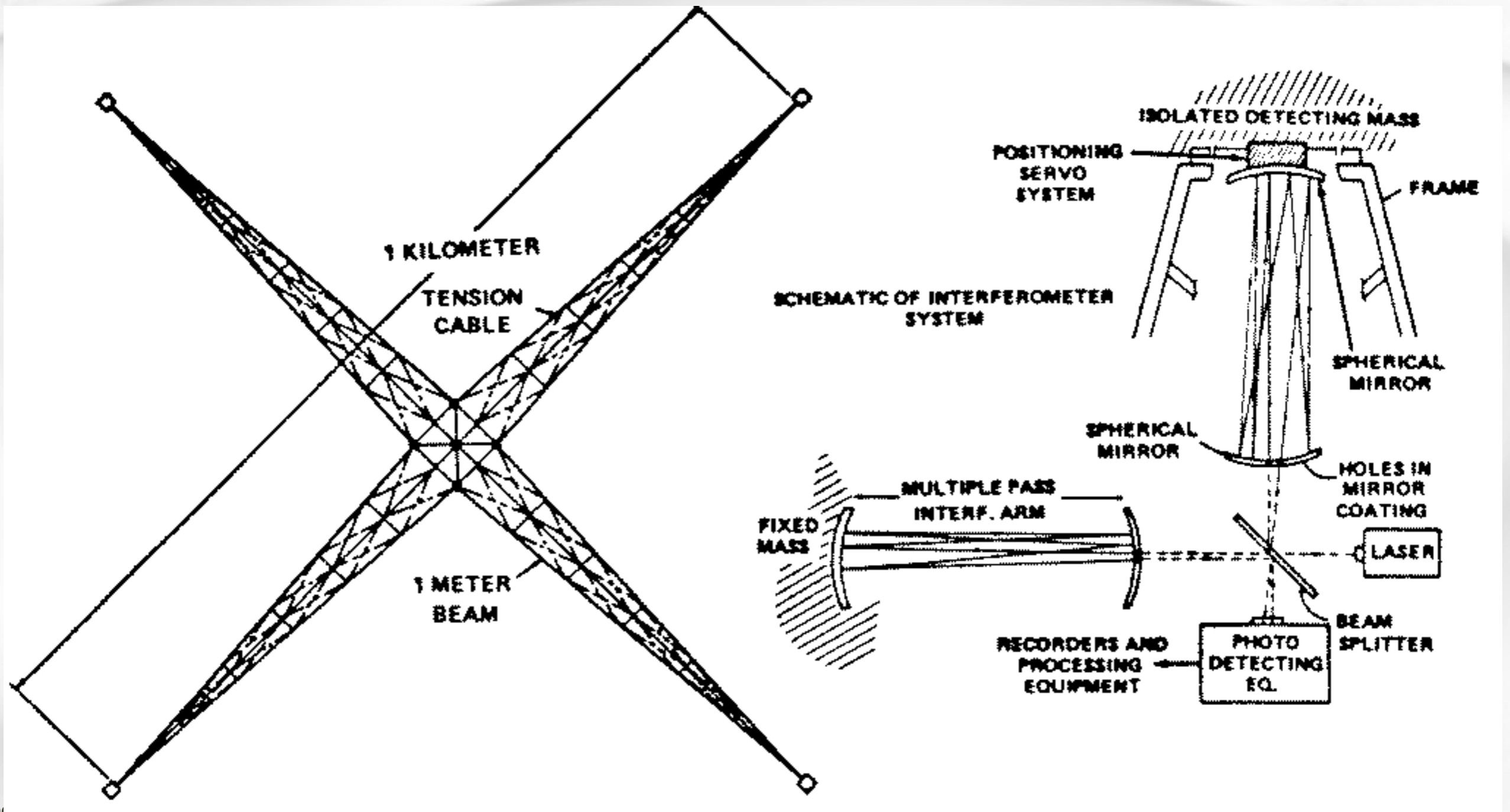
 *From LISA Pathfinder to LISA*

 **Mission description**

 *Conclusion*

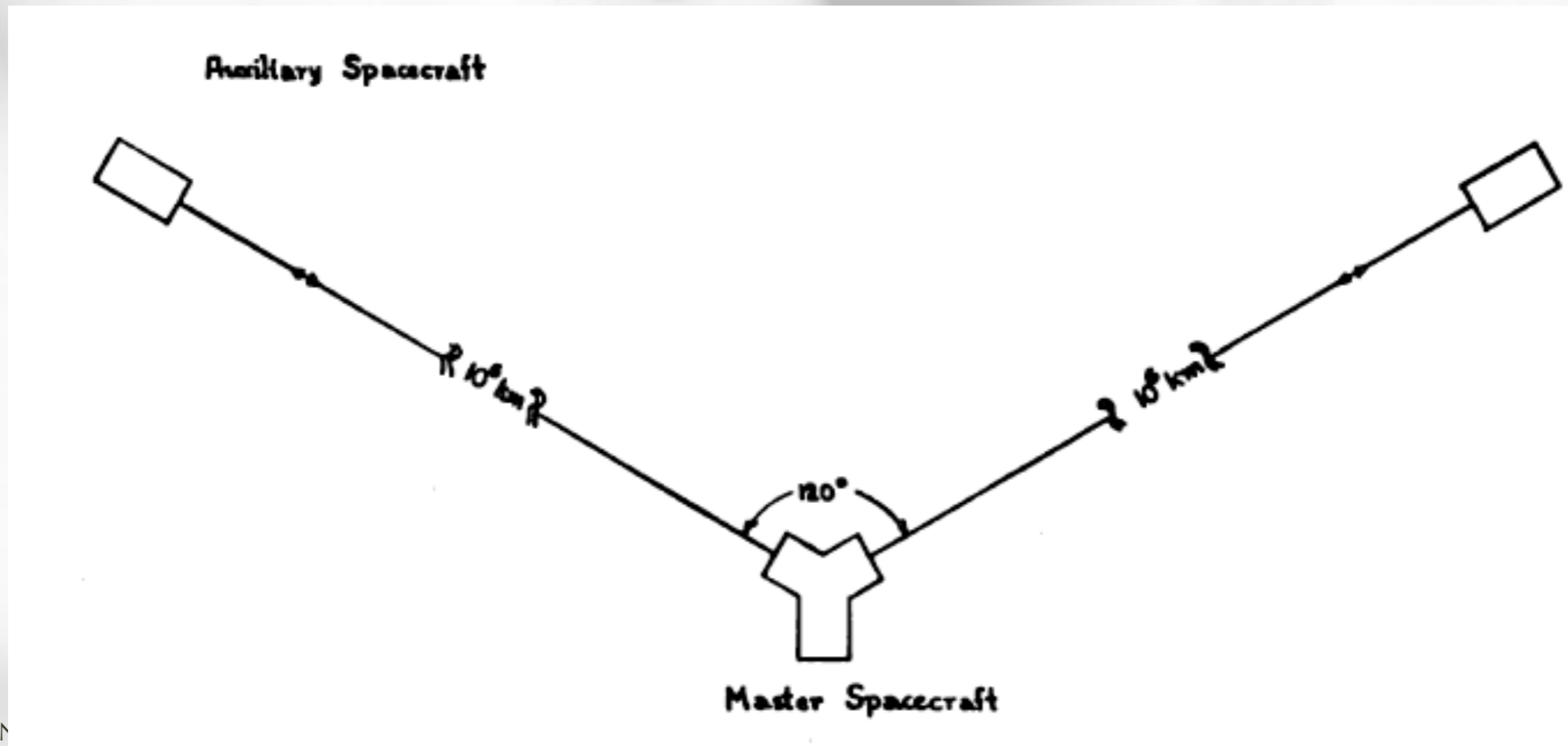
A long awaited mission

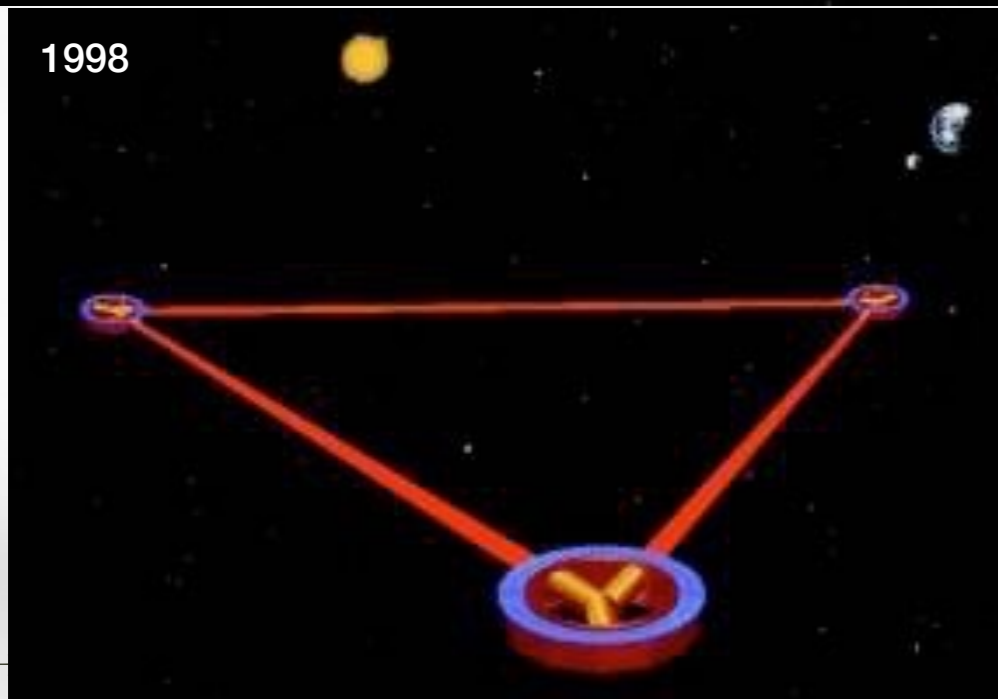
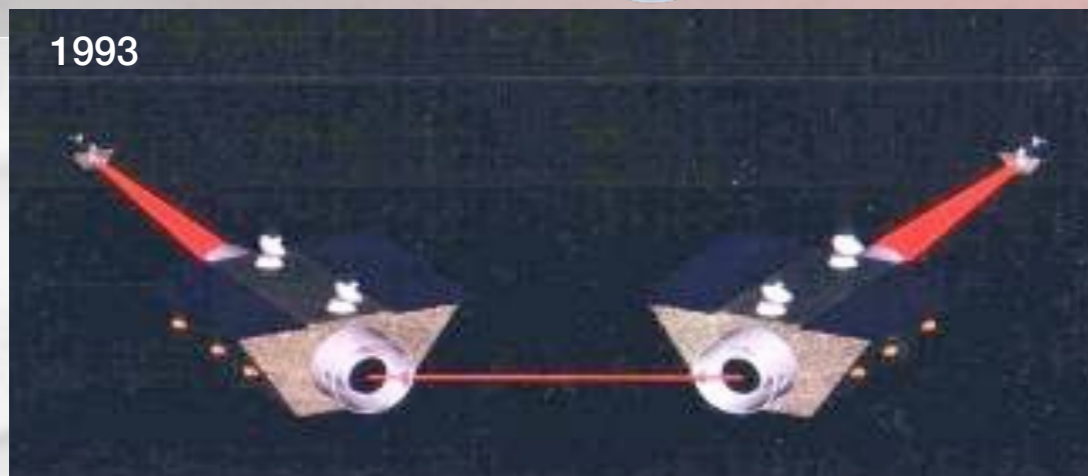
- First NASA studies in 1978
- Deployable rigid structure 1x1 km



-  J.E. Faller, P.L. Bender, J.L. Hall, D. Hills and M.A. Vincent, *Proc. Colloquium «Kilometric Optical Arrays in Space»*, Cargèse (Corsica), **23-25 October 1984**

We are investigating possible designs for a laser gravitational wave antenna in space using free test masses and heterodyne (interferometric) detection. One possibility is to use baselines about 10^6 km long between three spacecraft in nearly circular one-year orbits about the sun. If the orbit elements are chosen properly, the distances between the spacecraft can be kept constant to roughly 1 part in 10^3 without orbit corrections. With milliwatt-transmitted laser power levels and 50 cm diameter optics, a strain sensitivity of $10^{-19}/\sqrt{\text{Hz}}$ over at least the period range from 10 to 10^4 seconds appears feasible. The primary goal of the measurements is to observe gravitational radiation associated with present or past interactions of super-massive objects. A number of binary sources can, however, also be studied. For periods shorter than 10 seconds, the sensitivity for a baseline length of 10^6 km would degrade as a result of multiple gravitational wavelengths being contained in the arm lengths. For longer periods, the main limitation is likely to come from spurious accelerations due to forces other than the gravitational attraction of the sun and planetary bodies.



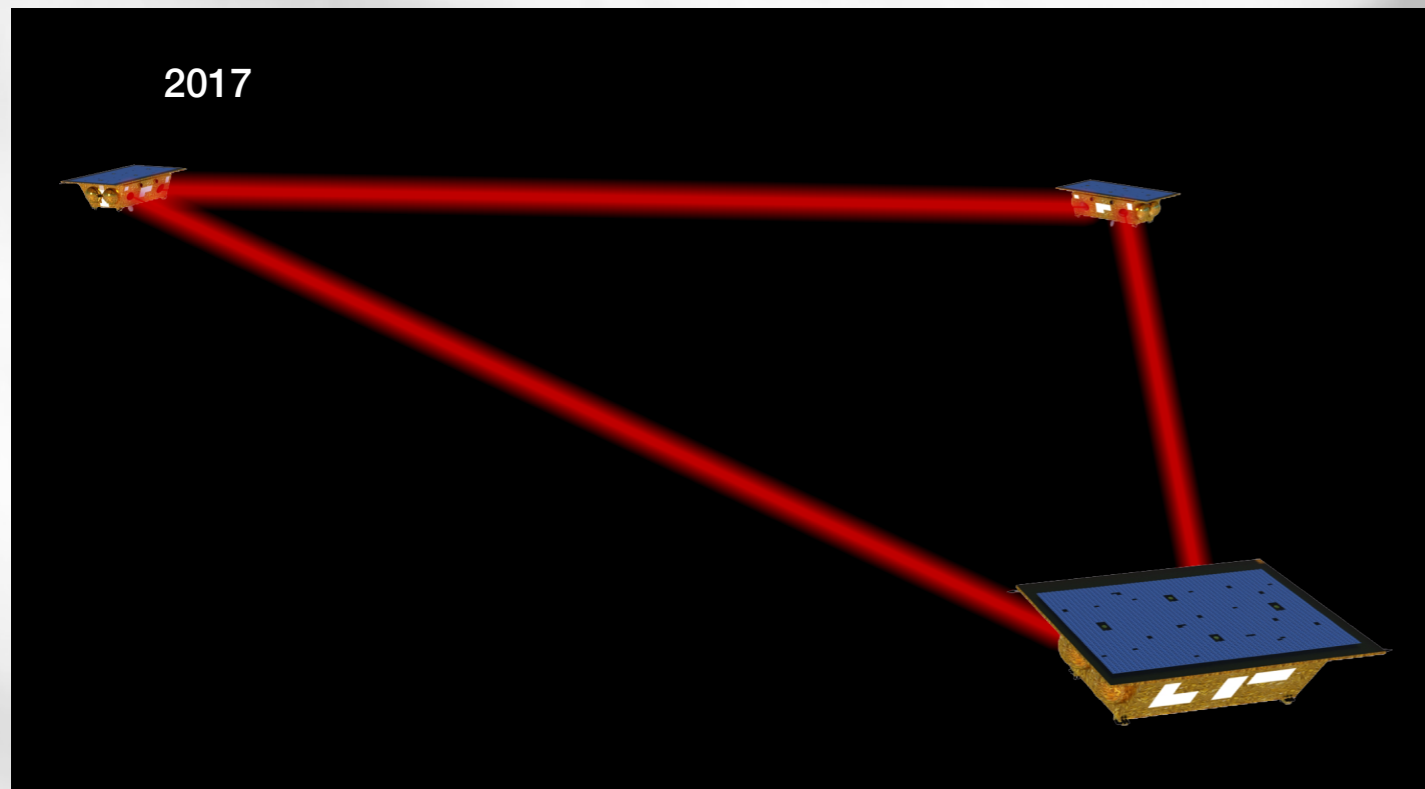


- ✈️ Joint ESA-NASA mission in 1993
 - ✈️ 4 (1993) → 6 (1994) → 3 (1997) satellites
 - ✈️ LISA name appeared (Laser Interferometer Space Antenna) in 1993
 - ✈️ ESA 'Cornerstone' mission, launch before 2010

- ✈️ 2011: NASA out of the project
 - ✈️ Recommendation : « NASA cannot participate to any large mission for the next decade because of the JWST cost »
 - ✈️ ESA decide to go alone, on a 'optimized' (cheaper) design : the eLISA mission concept (only 2, shorter, arms)

THE GRAVITATIONAL UNIVERSE

A science theme addressed by the *eLISA* mission observing the entire Universe



- ✈ 2013 : selection of the 'Gravitational Universe' as the science theme of the 'L3' mission
 - ✈ eLISA as strawman mission concept
 - ✈ Launch in 2034
- ✈ Déc. 2015 - July 2017 : LISA Pathfinder flight
 - ✈ Achieved performance far beyond expectations...
- ✈ 2017 : selection of LISA as the 'L3' mission candidate
 - ✈ NASA back into LISA as 'Junior' partner
 - ✈ 3 interferometric arms, 2.5 Mkm long
- ✈ Since then LISA follows mission development phases
 - ✈ Phase A (feasibility studies) : 2017 - 2021
 - ✈ Phase B (preliminary design) : 2022 - ...
 - ✈ Adoption : expected end 2023
 - ✈ Launch : ~2035

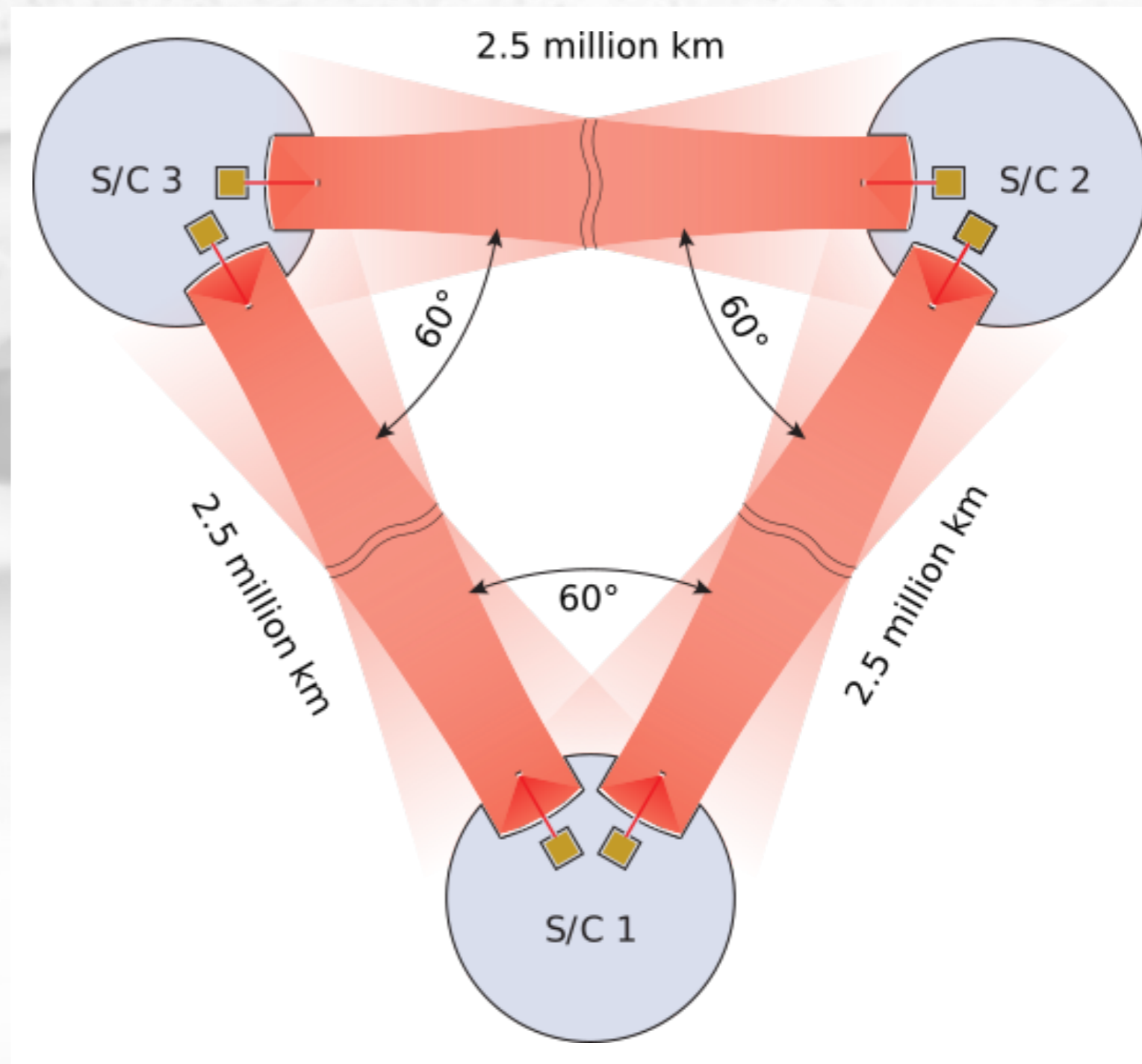
- Equilateral configuration
 - 3 arms / 6 links ; 2.5 Mkm

- Test masses

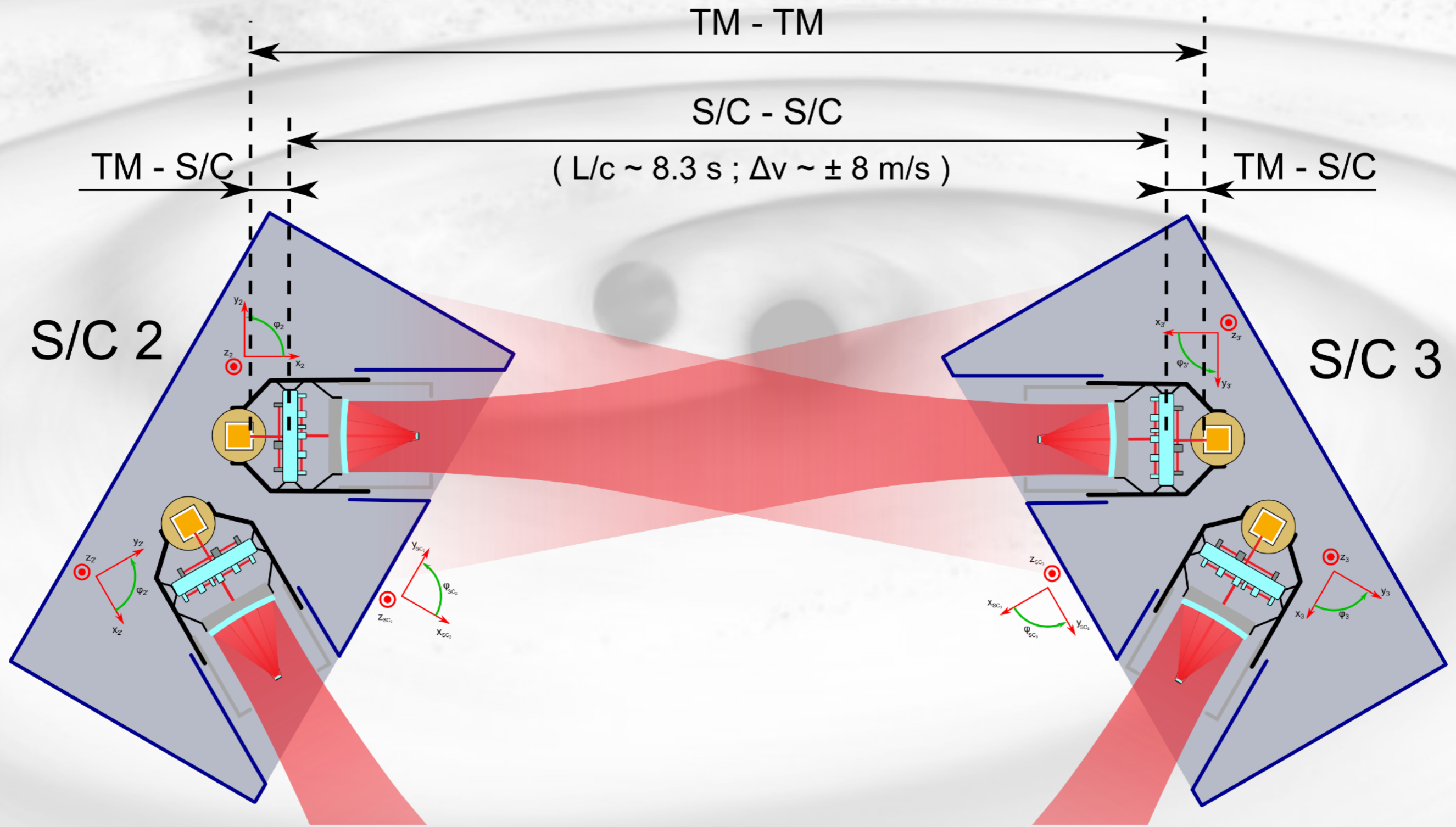
- Direct heritage from LPF
- 2 TM / satellite
- 2 steerable optical benches / satellite

- Typical metrology requirement :

$\sim 10 \text{ pm}/\sqrt{\text{Hz}} @ 1 \text{ mHz}$

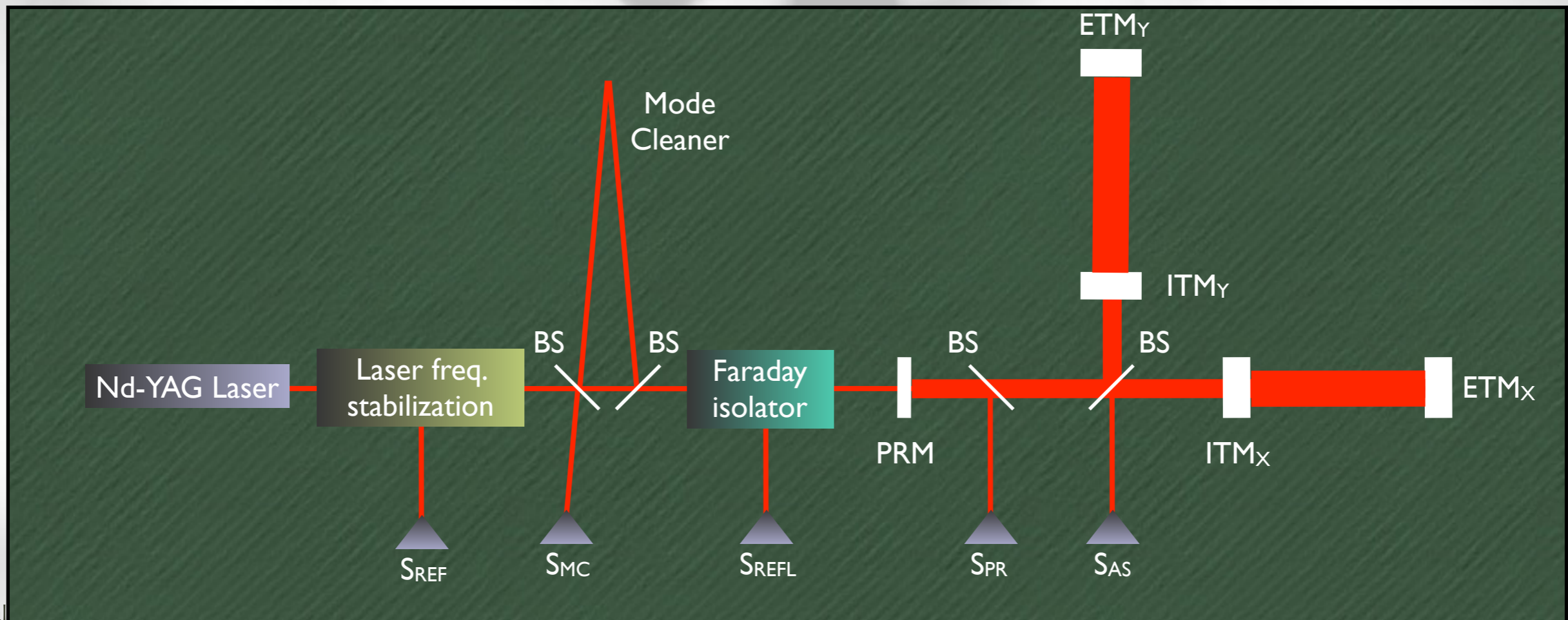


Measurement principle



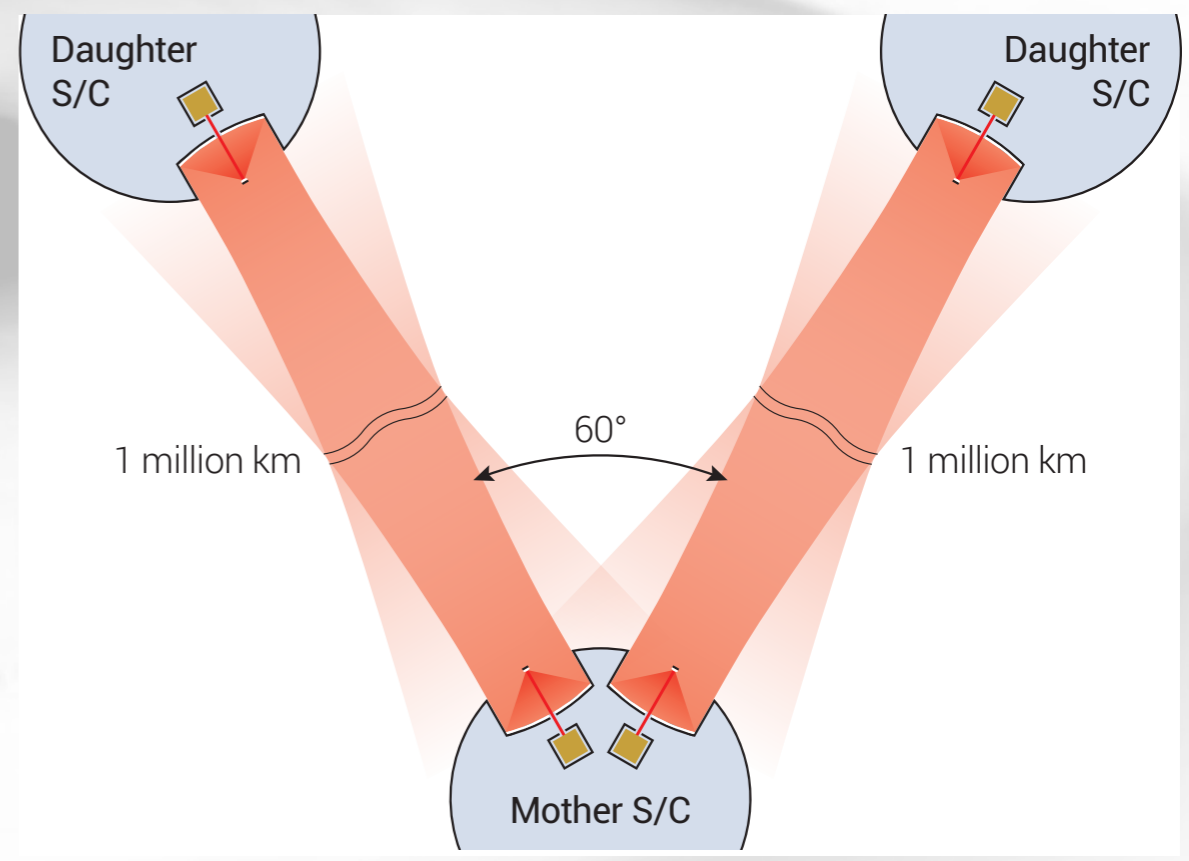
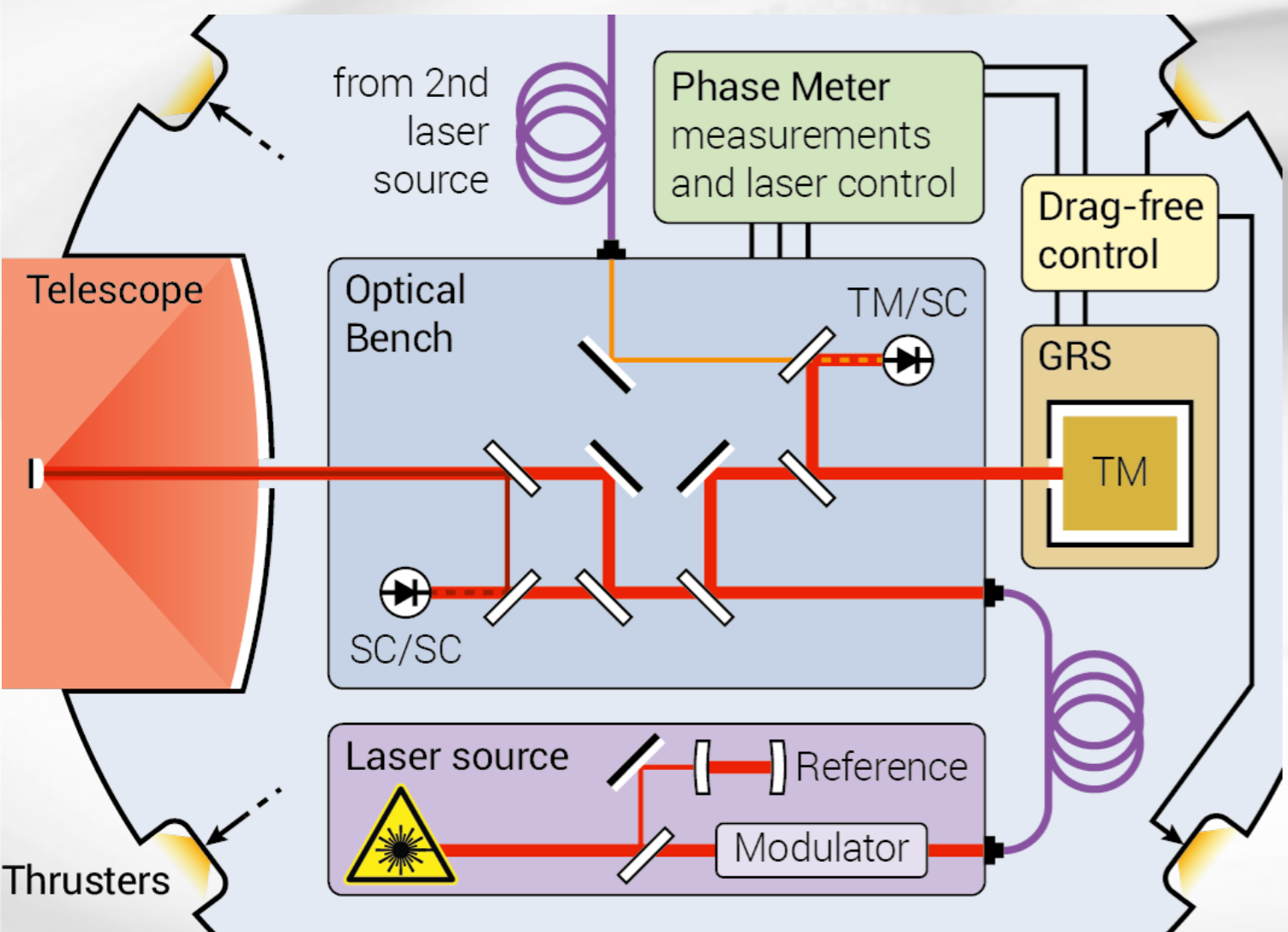
Ground based interferometers

- Test masses = suspended mirrors
- Increase of arm-length using Fabry Perot cavities
- Power recycling mirror
- —> High optical power in the arms !
- —> Linear response only close to resonance: electronic feedback loops to lock the cavities

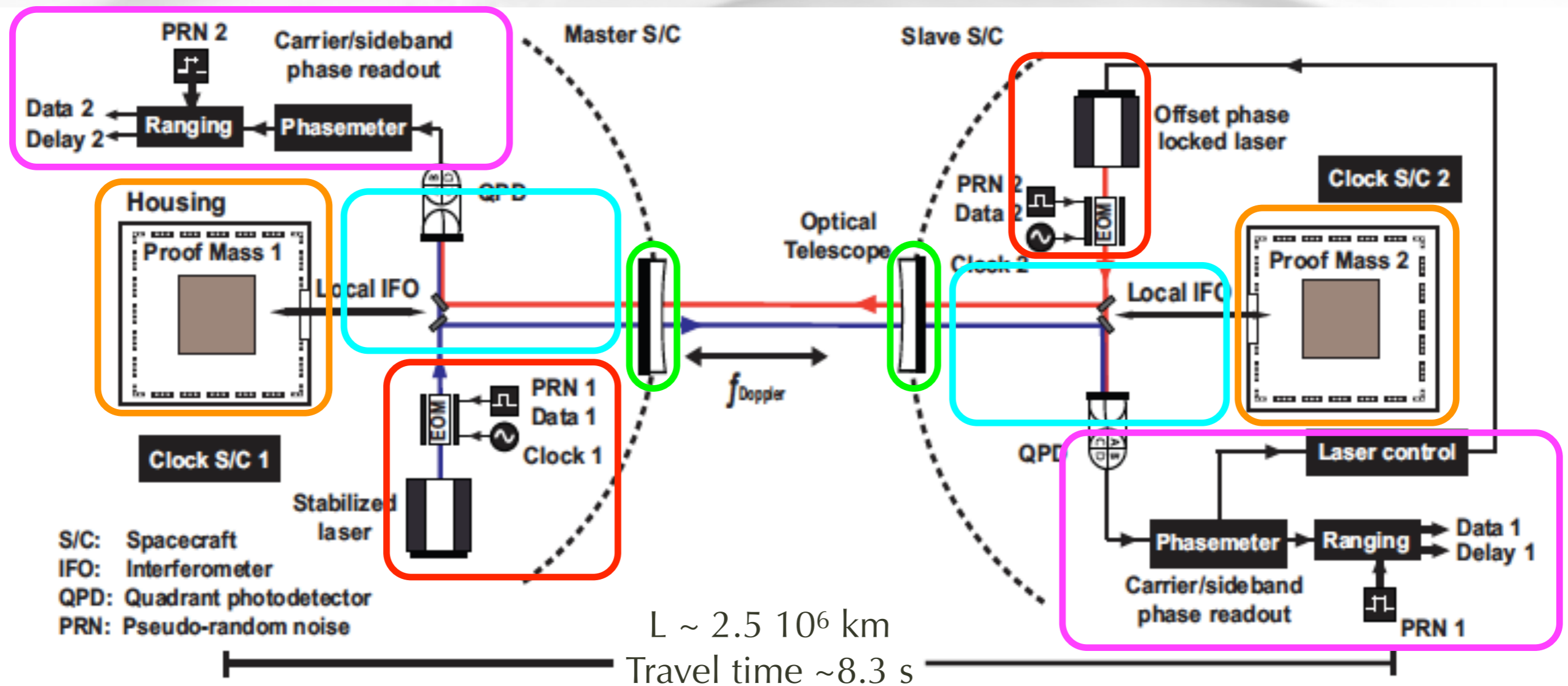


Space-based interferometers

- Test masses : free floating mirrors, long arms
- → in LISA : 1.1 W emitted, 650 pW received
- Keplerian orbits : variable armlength. and Doppler shifts
- → requires heterodyne interferometry : distance measured as phase stability of a RF signal
- Independent S/C
- → phase-locked lasers (transponder mode) + clocks synchronisation signals

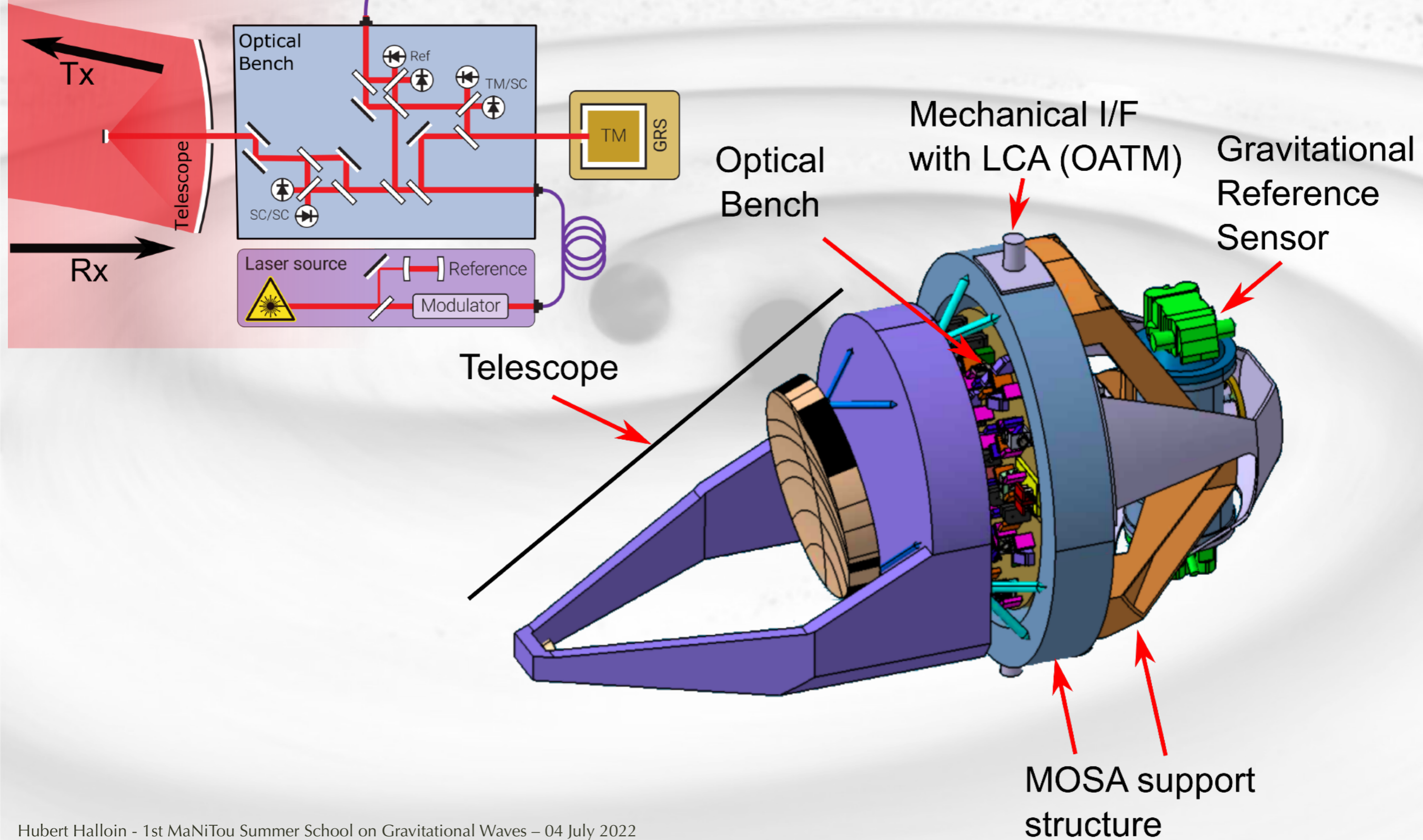


- Main payload elements
 - Gravitational Reference System (GRS)**
 - Zerodur Optical Bench**
 - Phase & frequency extraction (Phasemeter)**
 - Telescope**



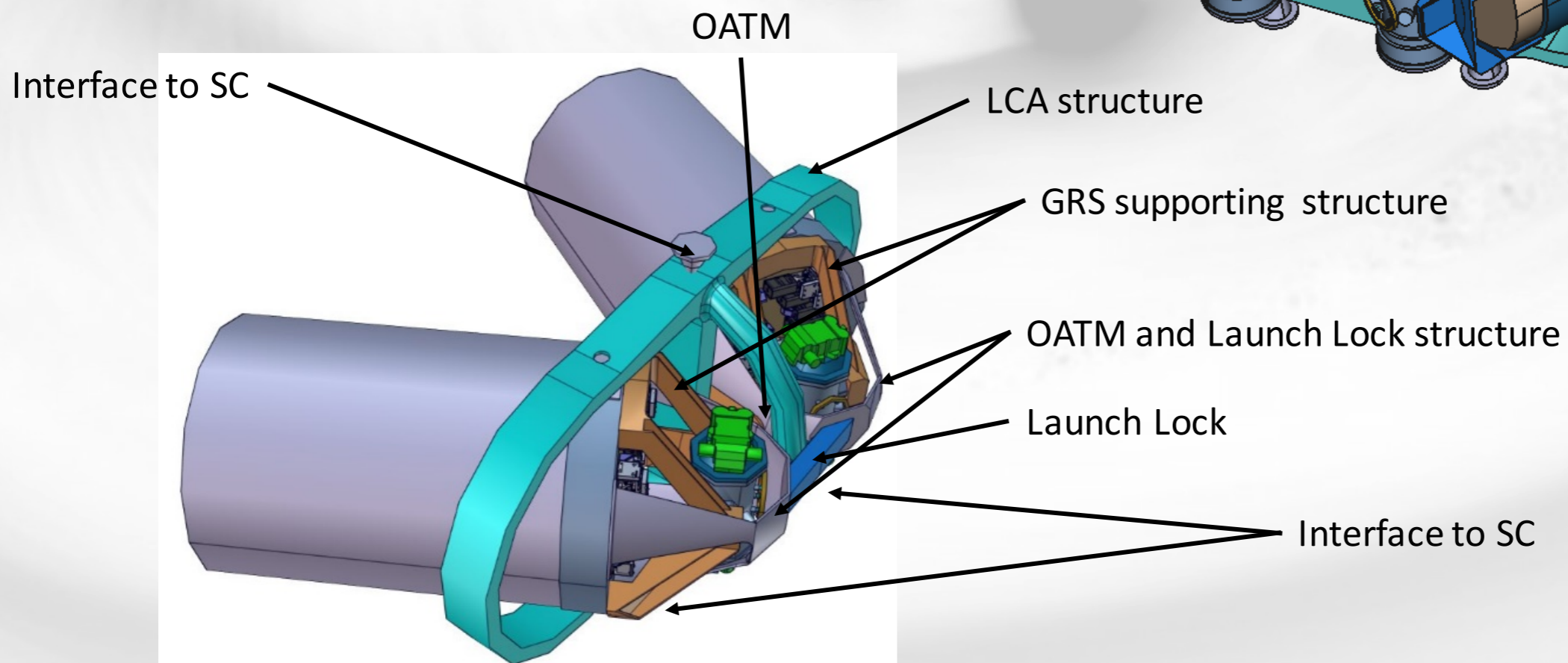
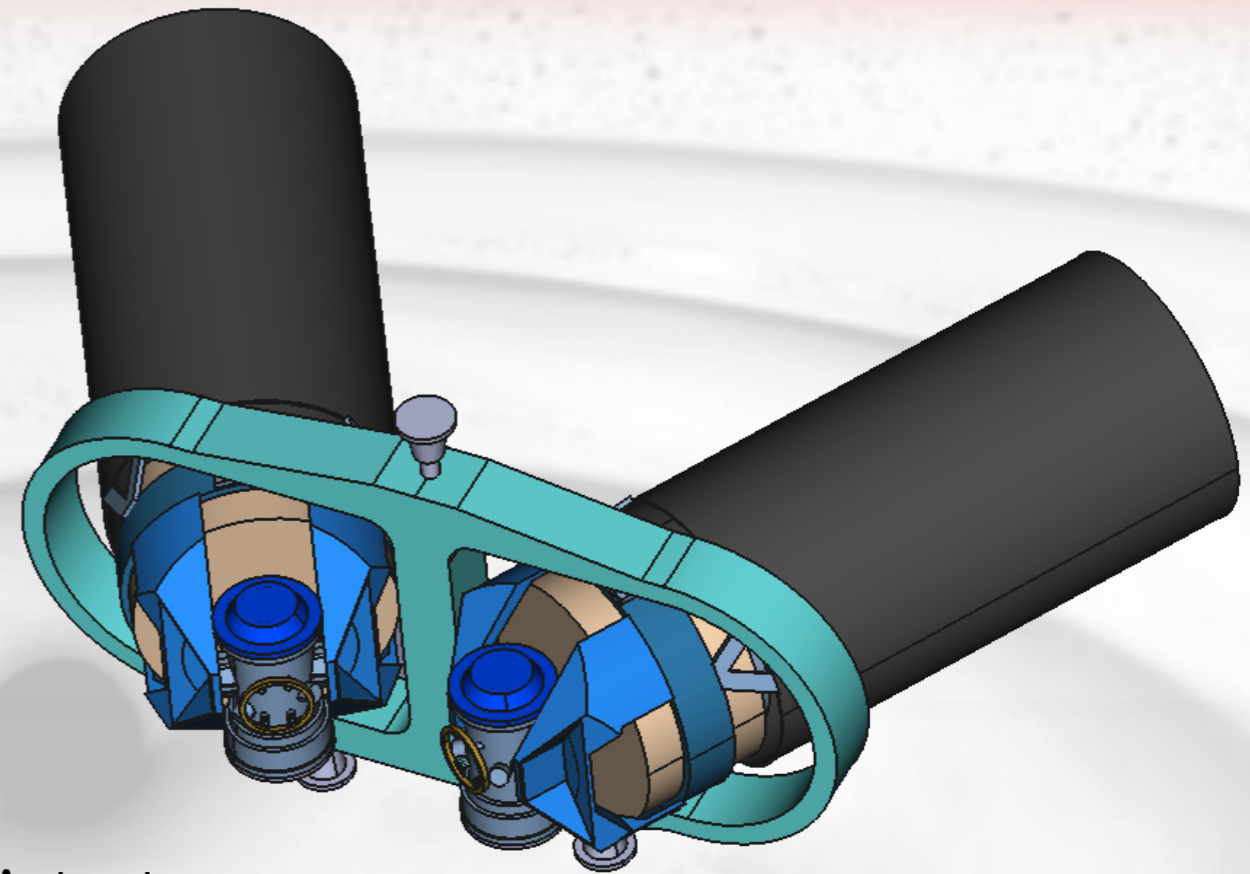
Scheme of a instrument

MOSA = Movable Sub-assembly

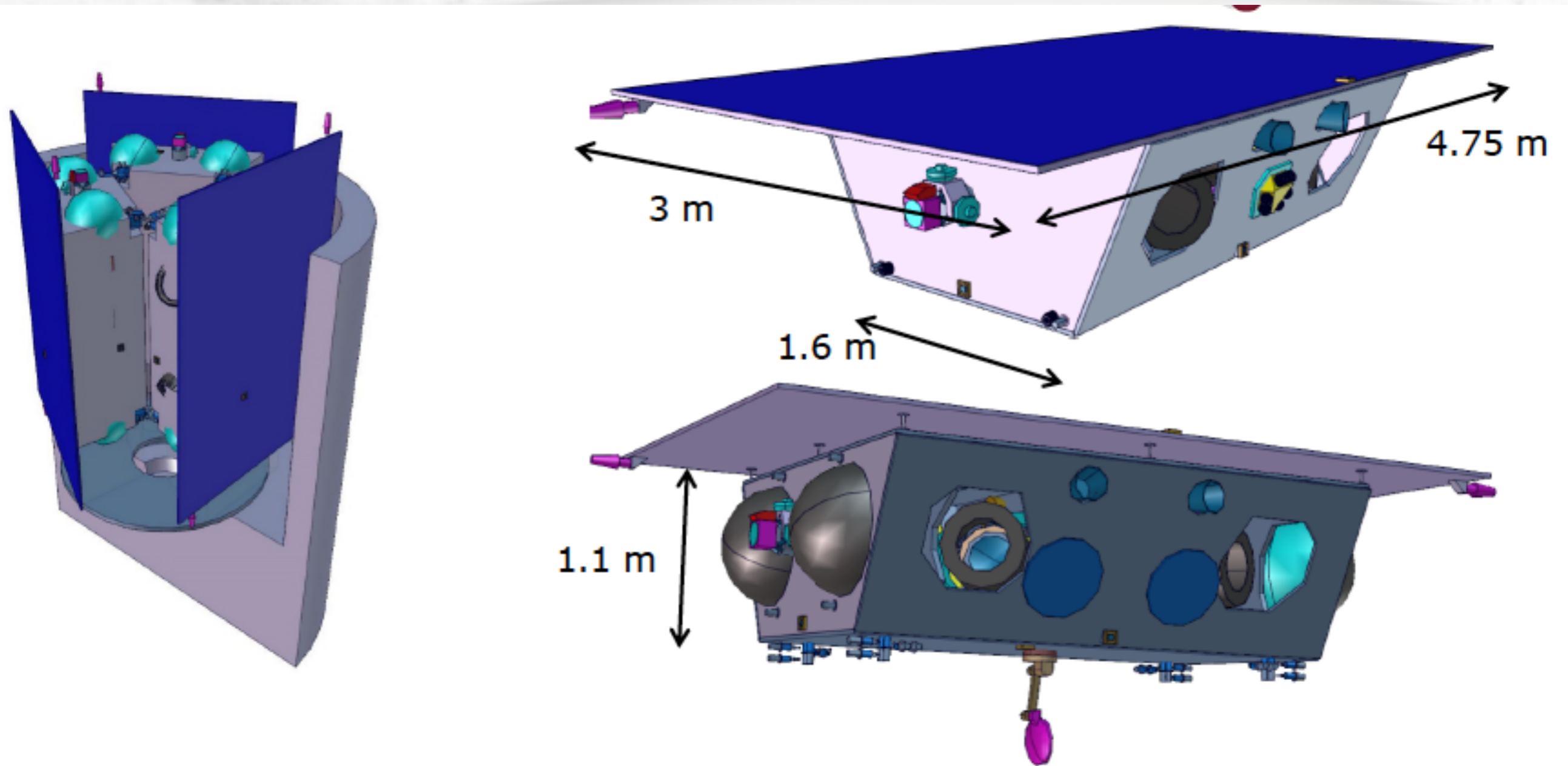




Two MOSAs form an LCA ...

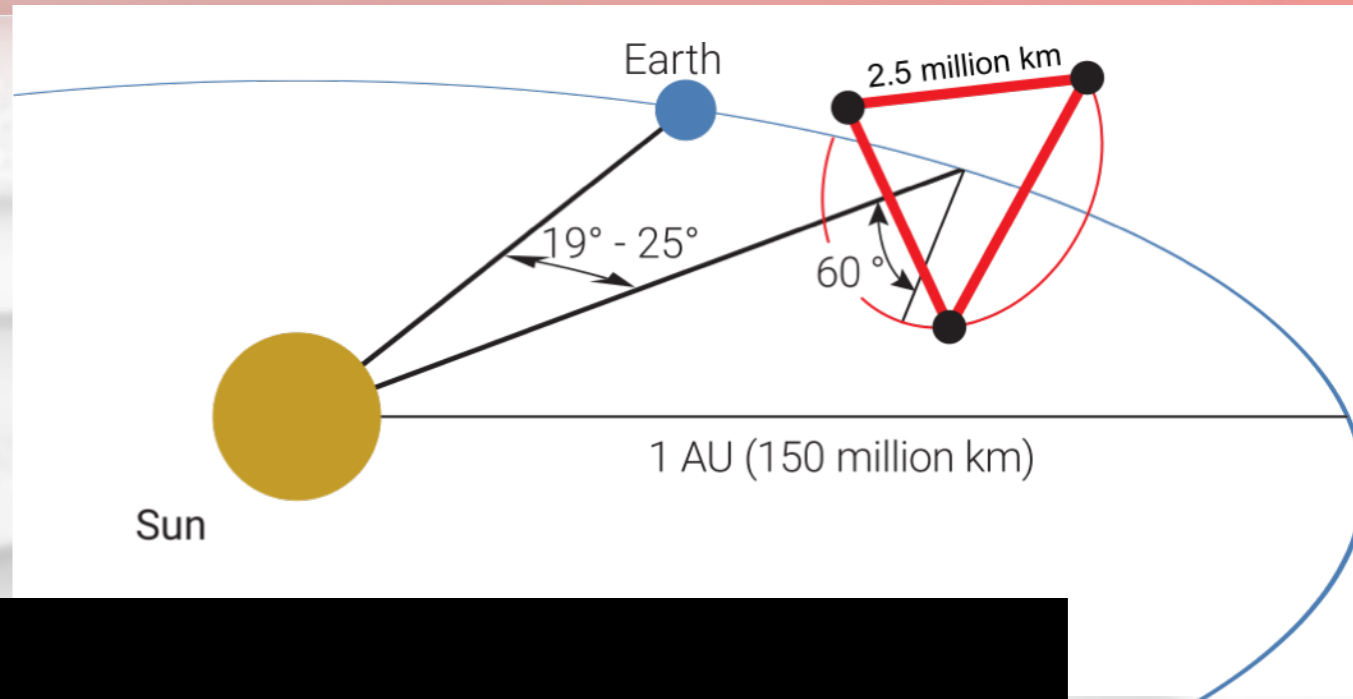
 LCA = LISA Core Assembly



Three S/C fit into an Ariane 6.4



-  Heliocentric orbits
-  19° to 25° trailing the Earth



- The effect of a GW on a laser link is a Doppler shift of the laser frequency

$$\vec{k} = \begin{pmatrix} \sin \theta \cos \phi \\ \sin \theta \sin \phi \\ \cos \theta \end{pmatrix}; \vec{\theta} = \frac{\partial \vec{k}}{\partial \theta} = \begin{pmatrix} \cos \theta \cos \phi \\ \cos \theta \sin \phi \\ -\sin \theta \end{pmatrix}; \vec{\phi} = \frac{1}{\sin \theta} \frac{\partial \vec{k}}{\partial \phi} = \begin{pmatrix} -\sin \phi \\ \cos \phi \\ 0 \end{pmatrix}$$

$$\vec{n} = \vec{r}_B - \vec{r}_A$$

$$\xi_+ = (\vec{\theta} \cdot \vec{n})^2 - (\vec{\phi} \cdot \vec{n})^2; \xi_{\times} = 2(\vec{\theta} \cdot \vec{n})(\vec{\phi} \cdot \vec{n})$$

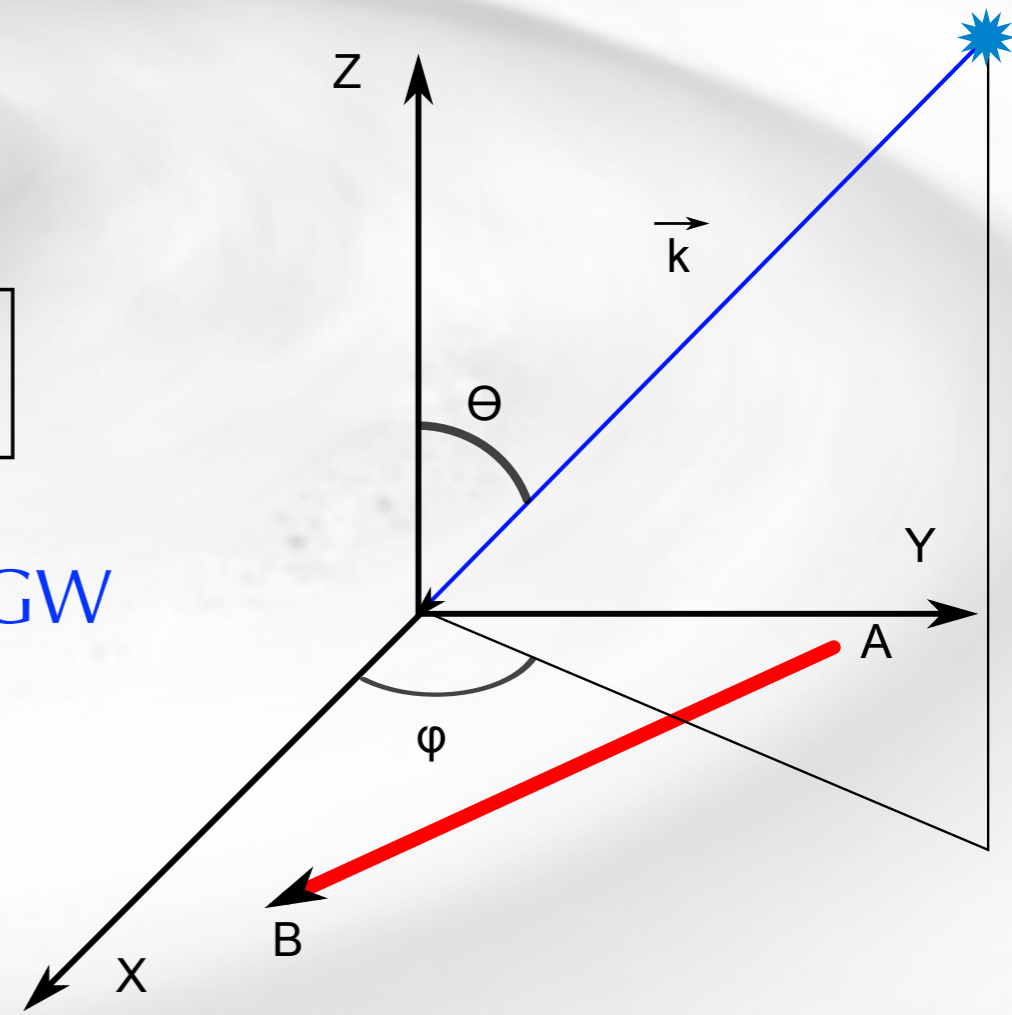
$$H(t) = \xi_+ \cdot h_+(t) + \xi_{\times} \cdot h_{\times}(t)$$

$$\frac{\delta \nu}{\nu_0}(t) = \frac{1}{2(1 - \vec{k} \cdot \vec{n})} \left[H \left(t - \frac{\vec{k} \cdot \vec{r}_B}{c} \right) - H \left(t - \frac{L}{c} - \frac{\vec{k} \cdot \vec{r}_A}{c} \right) \right]$$

- ξ_+ and ξ_{\times} define the angular response to GW

- For a bouncing laser link :

$$\left. \frac{\delta \nu}{\nu_0} \right|_{2ways}(t) = \frac{1}{2(1 - \vec{k} \cdot \vec{n})} \left[H \left(t - \frac{\vec{k} \cdot \vec{r}_B}{c} \right) - H \left(t - \frac{L}{c} - \frac{\vec{k} \cdot \vec{r}_A}{c} \right) \right] + \frac{1}{2(1 + \vec{k} \cdot \vec{n})} \left[H \left(t - \frac{L}{c} - \frac{\vec{k} \cdot \vec{r}_A}{c} \right) - H \left(t - \frac{2L}{c} - \frac{\vec{k} \cdot \vec{r}_B}{c} \right) \right]$$

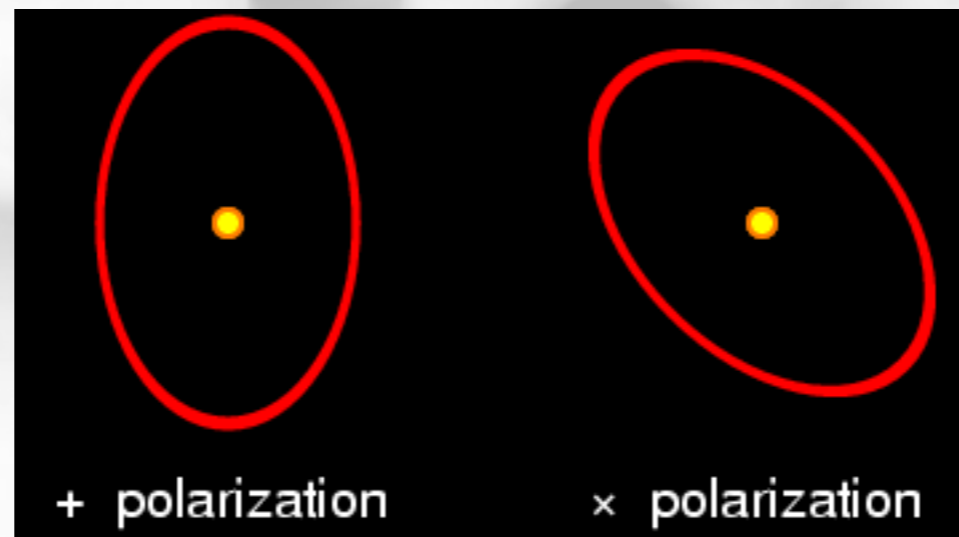


• For $n_1=x, n_2=y, k=-z, \phi=0$

• i.e. Michelson interferometer with the source direction perp. to arms plane.

$$\xi_{+,1} = +1; \xi_{\times,1} = 0; \left. \frac{\delta\nu}{\nu_0} \right|_{2ways,1}(t) = \frac{1}{2} \left[h_+(t) - h_+\left(t - \frac{2L}{c}\right) \right]$$

$$\xi_{+,2} = -1; \xi_{\times,1} = 0; \left. \frac{\delta\nu}{\nu_0} \right|_{2ways,2}(t) = -\frac{1}{2} \left[h_+(t) - h_+\left(t - \frac{2L}{c}\right) \right]$$



$$\left. \frac{\delta\nu}{\nu_0} \right|_{interf}(t) = \left. \frac{\delta\nu}{\nu_0} \right|_{2ways,1}(t) - \left. \frac{\delta\nu}{\nu_0} \right|_{2ways,2}(t) = h_+(t) - h_+\left(t - \frac{2L}{c}\right)$$

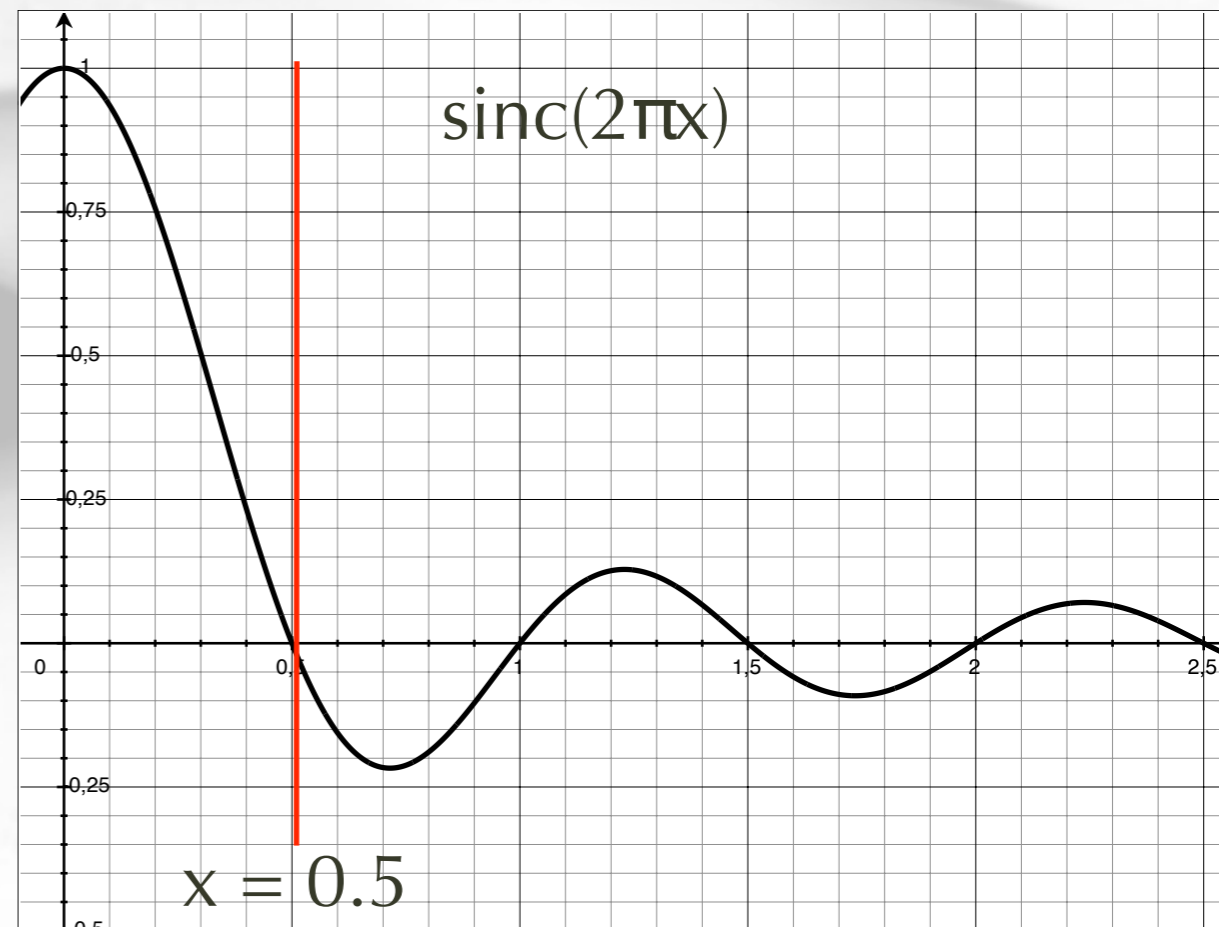
$$\Rightarrow \left. \frac{\delta\tilde{\nu}}{\nu_0} \right|_{interf}(f) = \tilde{h}_+(f) \left(1 - e^{-2i\pi f \frac{2L}{c}} \right) = \tilde{h}_+(f) 2i \sin \frac{2\pi f L}{c} e^{-2i\pi f \frac{L}{c}}$$

$$\Phi(t) = 2\pi \int \nu(t) dt \Rightarrow \delta\tilde{\Phi}\Big|_{interf}(f) = \nu_0 \frac{\delta\tilde{\nu}(f)}{i \cdot f} = 2\pi \times \tilde{h}_+(f) \frac{2L}{\lambda} \text{sinc}\left(\frac{2\pi f L}{c}\right) e^{-2i\pi f \frac{L}{c}}$$





- 🚀 Cut-off frequency at $f_c = c/2L$
 - 🚀 Correspond to more than 1 oscillation in L
 - 🚀 Space based ($L=2.5$ Mkm) $\Rightarrow f_c \sim 60$ mHz
- 🚀 At low frequencies ($f \ll f_c$):

$$\delta\tilde{\Phi}\Big|_{interf}(f) \approx 2\pi \times \tilde{h}_+(f) \frac{2L}{\lambda} e^{-2i\pi f \frac{L}{c}}$$

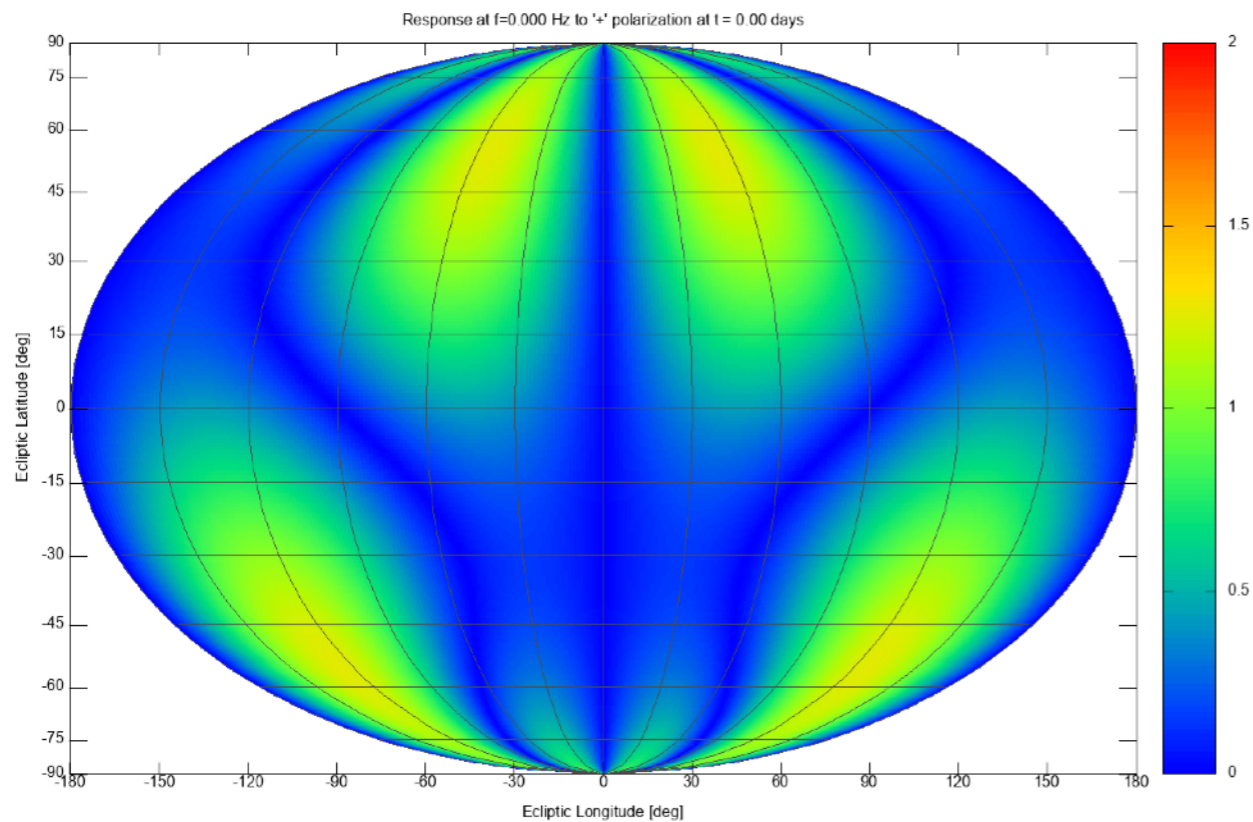
$$\delta\Phi\Big|_{interf}(t) \approx 2\pi \times h_+\left(t - \frac{L}{c}\right) \frac{2L}{\lambda}$$



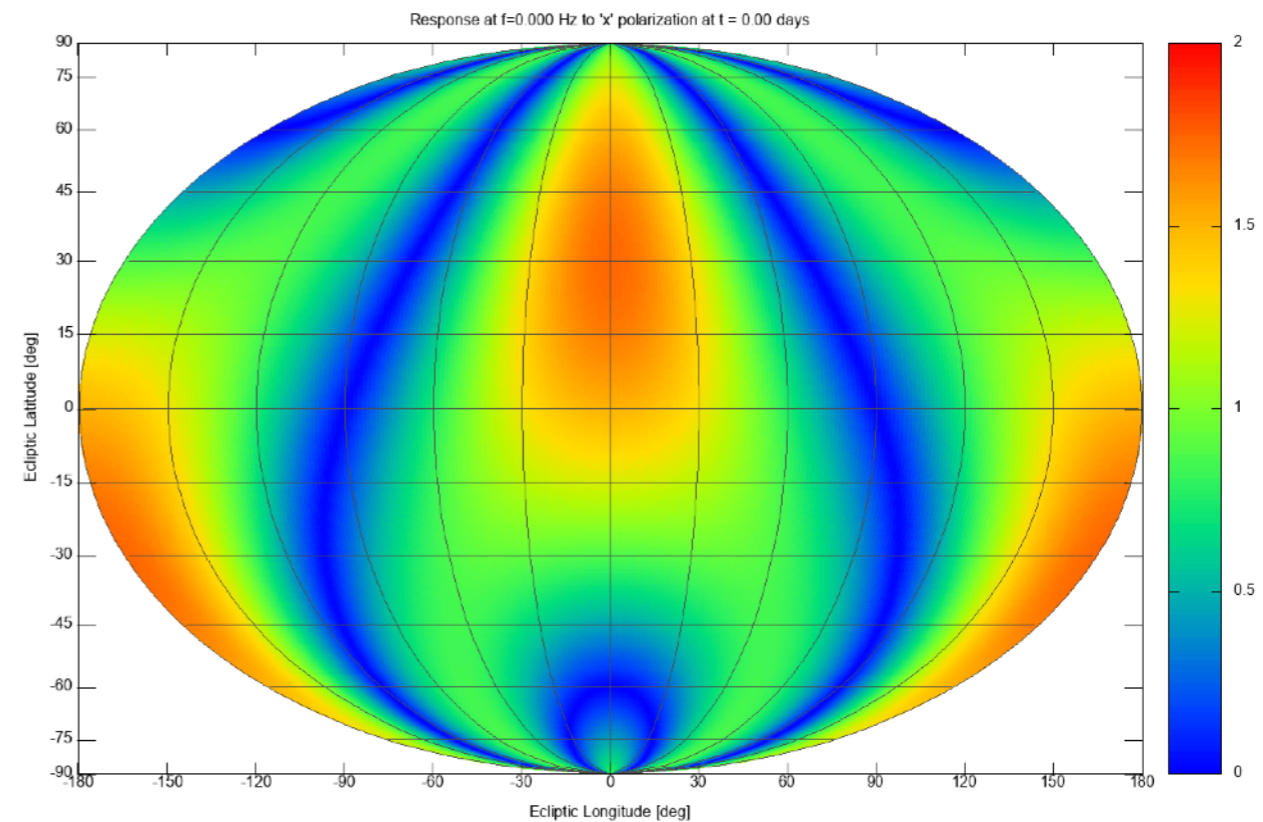
LISA-type response in ecliptic coordinates

-  Neglecting Doppler effects (relative velocity w.r.t the source) and constellation deformations
-  Time modulation of the antenna pattern \rightarrow localization of the source
 -  Also possible at a given time from Doppler shifts
-  The 3 links allow to disentangle polarizations

h_+



h_x

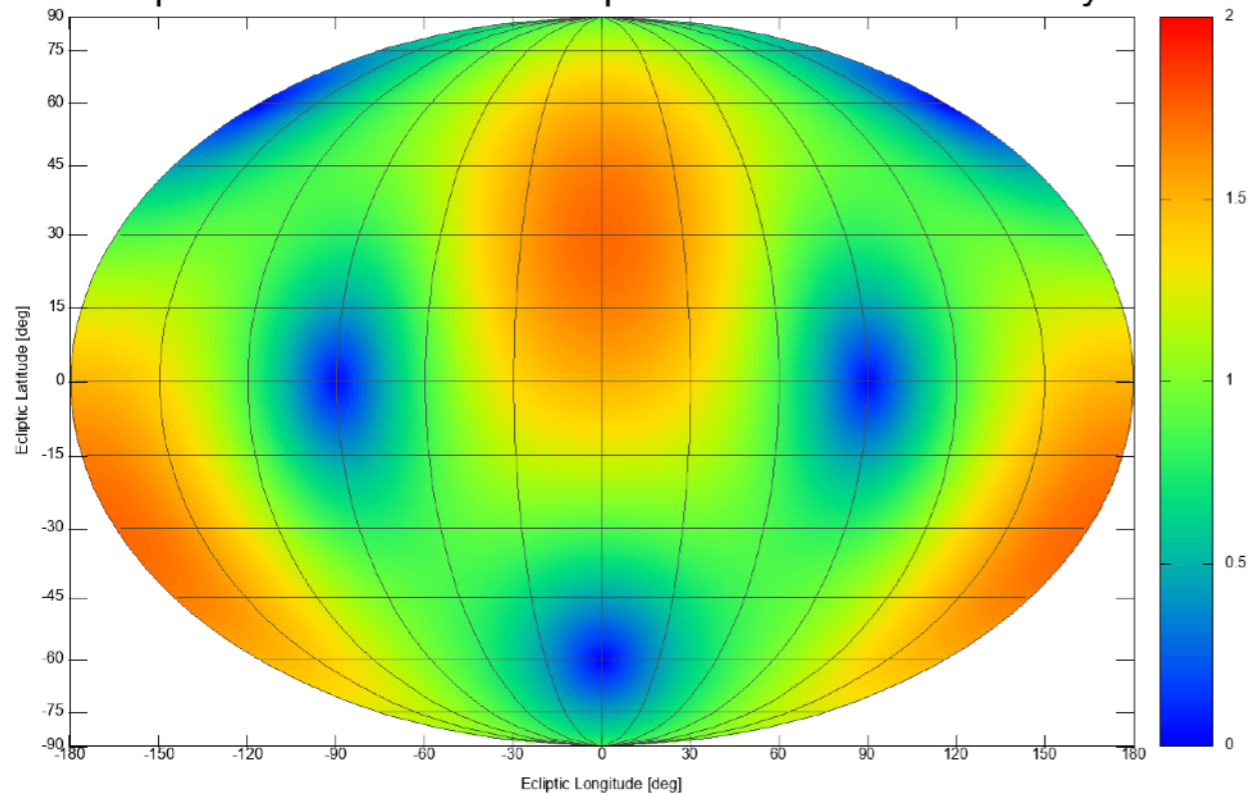


LISA response in ecliptic coordinates

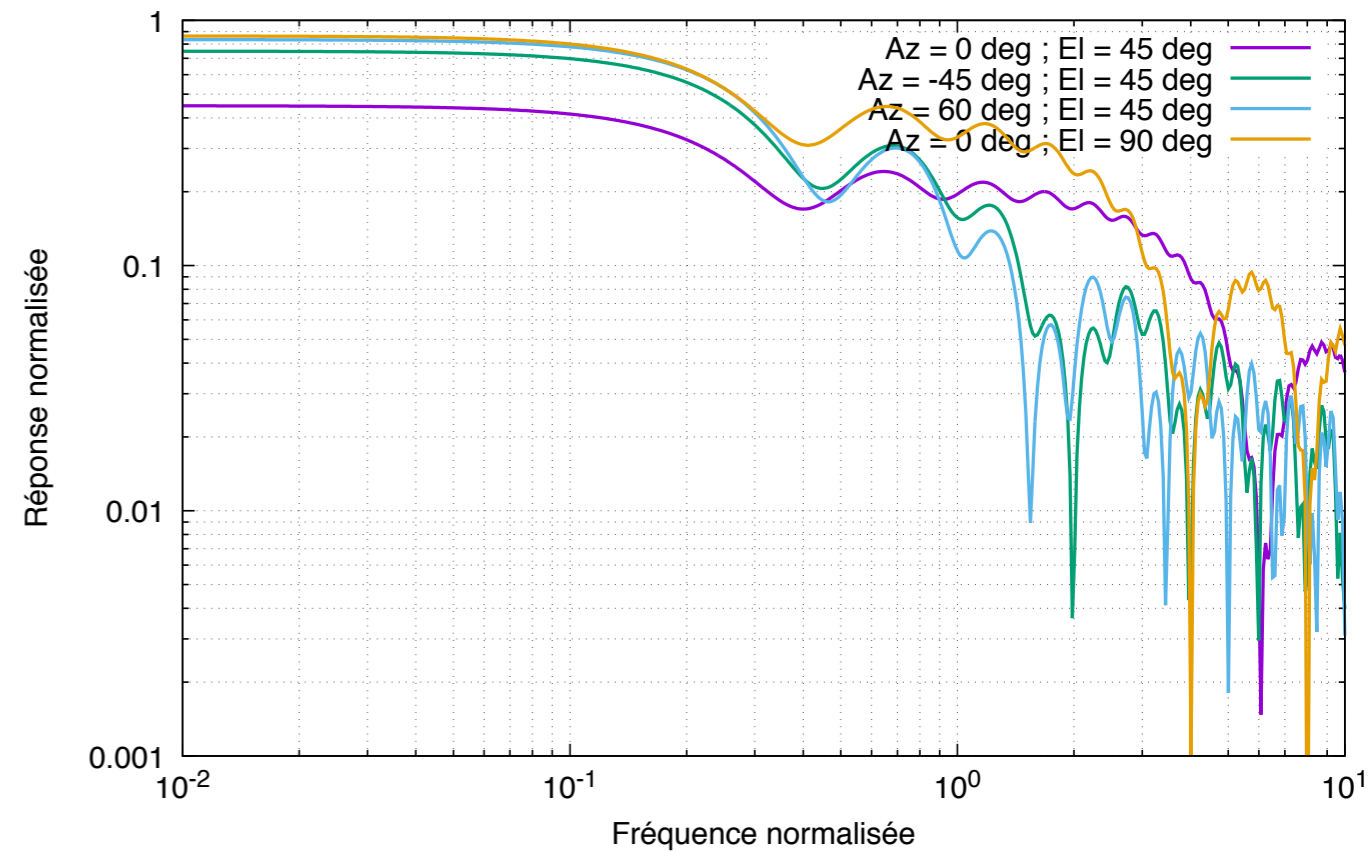
- Neglecting Doppler effects (relative velocity w.r.t the source) and constellation deformations
- Attenuation of the response with wave frequency

Unpolarized

Response at $f=0.001$ Hz to unpolarized GW at $t = 0.00$ days



Réponses moyennes LISALog



🚀 Mission constraints

- 🚀 Stable constellation over 12+ years
- 🚀 Constant inter-S/C distance : ~ 2.5 Mkm
- 🚀 Relative velocity between S/C : $< \sim 20$ m/s (20 MHz)
 - 🚀 Set by the photoreceiver bandwidth
- 🚀 Distance to Earth < 65 Mkm
 - 🚀 Set by the required data rate with Earth
- 🚀 Pure inertial orbits
 - 🚀 Solar pressure compensation, no orbit correction

🚀 —> Do such orbits exists ?

🚀 Yes for a purely central force (i.e only Sun attraction)

- 🚀 Inclination of the constellation on the ecliptic : $\sim 60.3^\circ$
- 🚀 Relative velocities : < 2 m/s (2 MHz)
- 🚀 Armlength : $2.5\text{Mkm} \pm 12\,000$ km

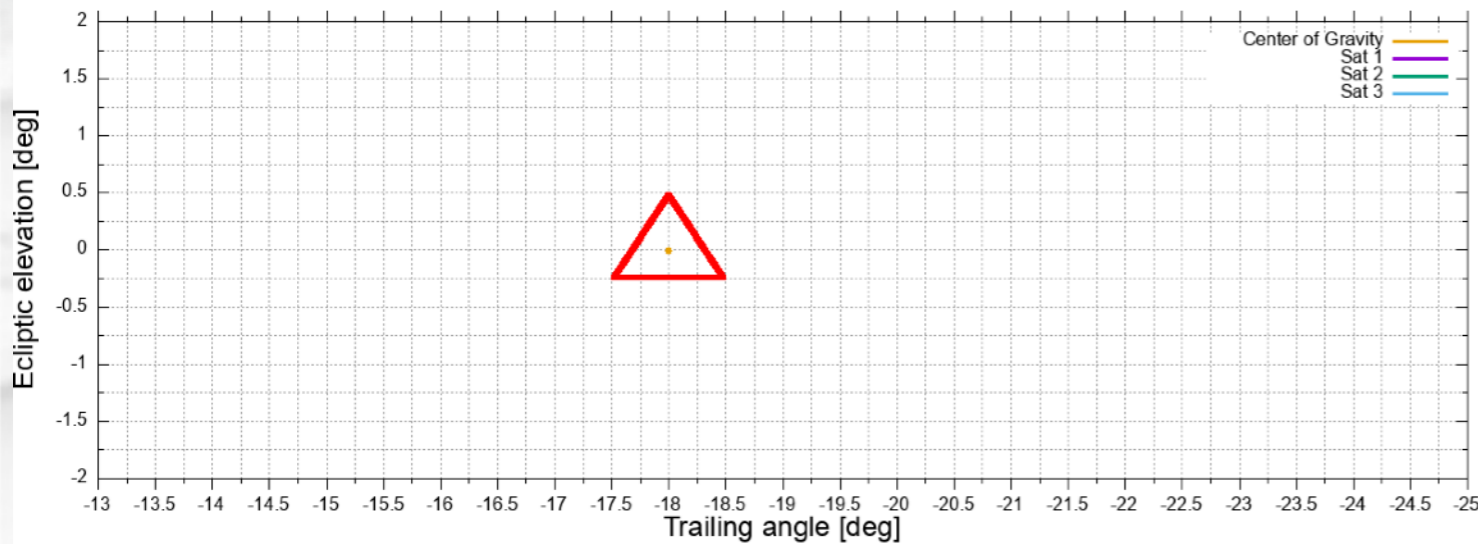
🚀 However ...

- 🚀 Gravitational perturbations from other celestial objects (mostly Earth+Moon)
- 🚀 —> Keplerian solution not suitable
- 🚀 —> Requires numerical optimisation

Orbital stability ?

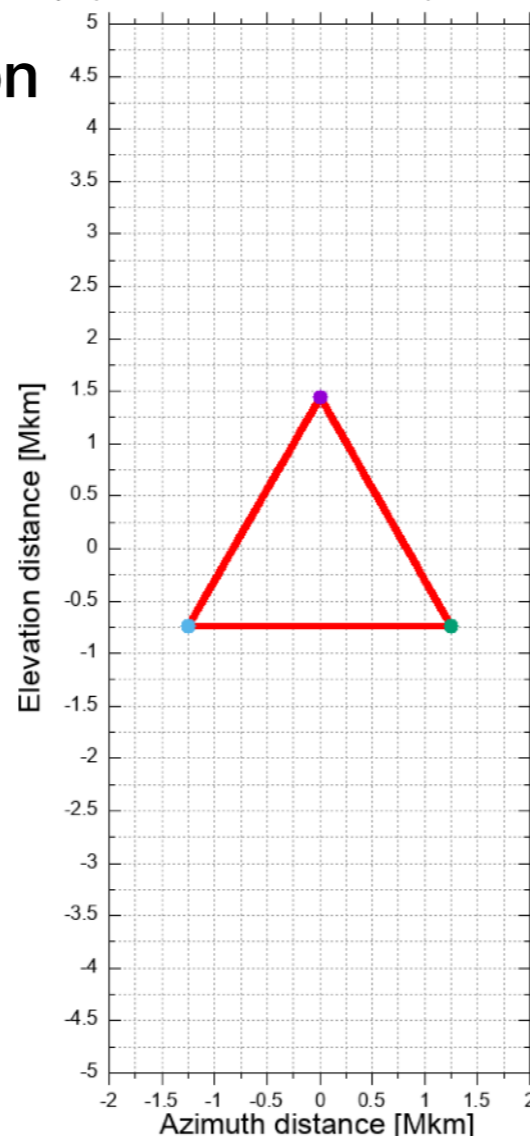
Trailing angle of LISA

Trailing angle - $t = 0$ days / trace = 365 days



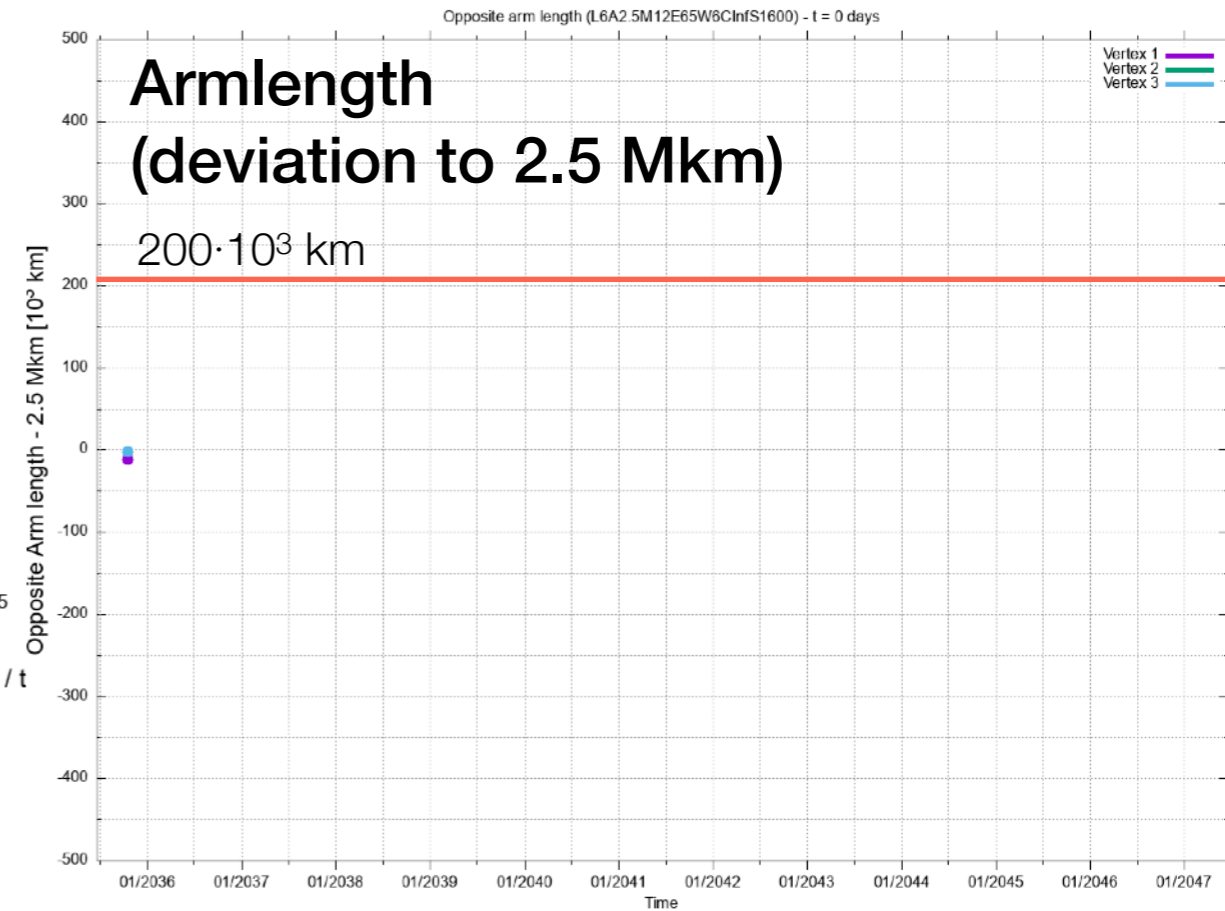
Constellation shape (L6A2.5M12E65W6CInfS1600) - $t = 0$ days / t

Constellation shape

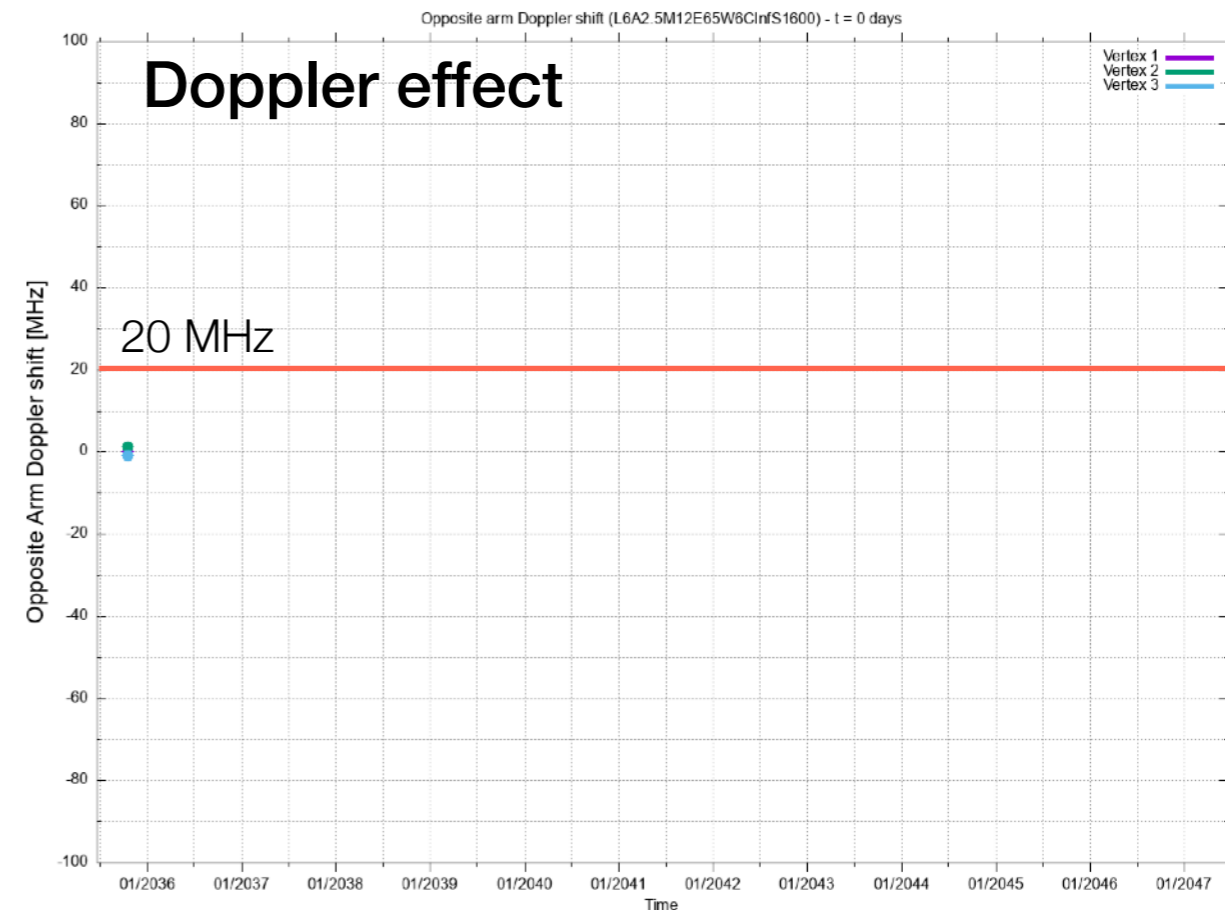


🚀 Using 'optimal' keplerian parameters in presence of Earth gravitational perturbations

Armlength (deviation to 2.5 Mkm)

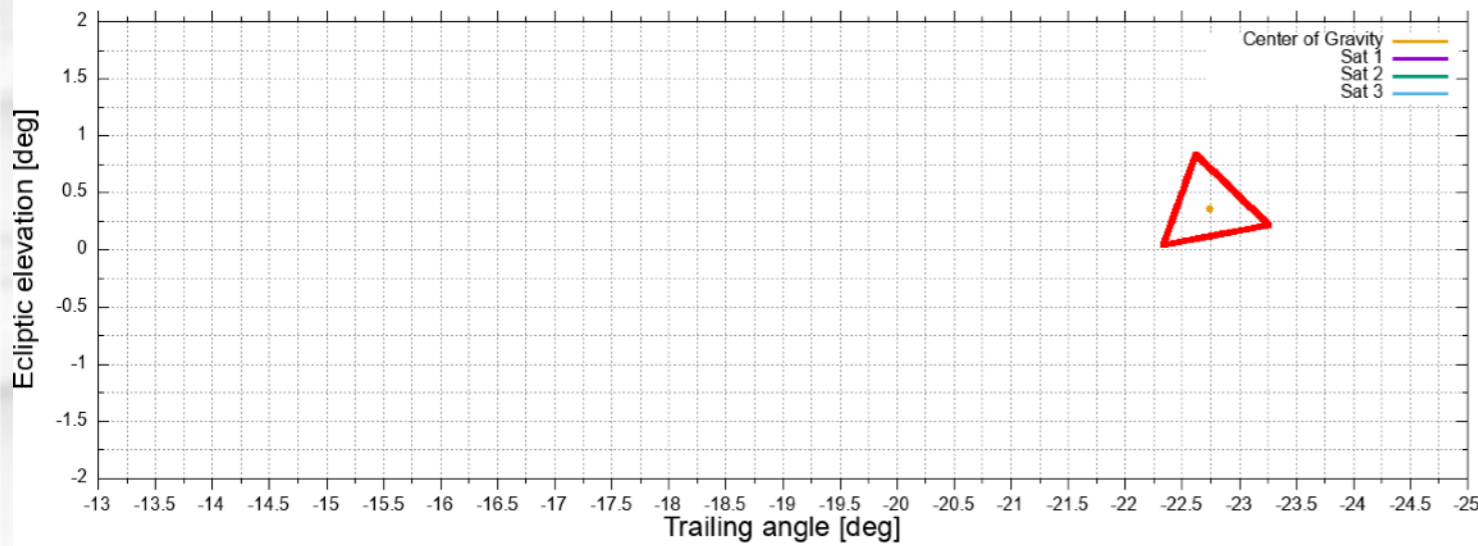


Doppler effect



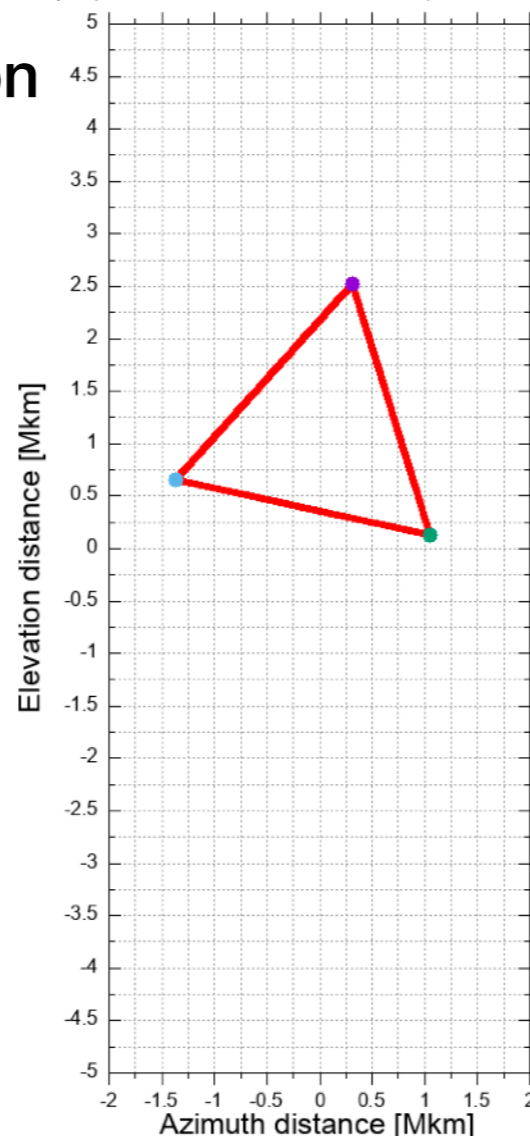
Trailing angle of LISA

Trailing angle - $t = 0$ days / trace = 365 days



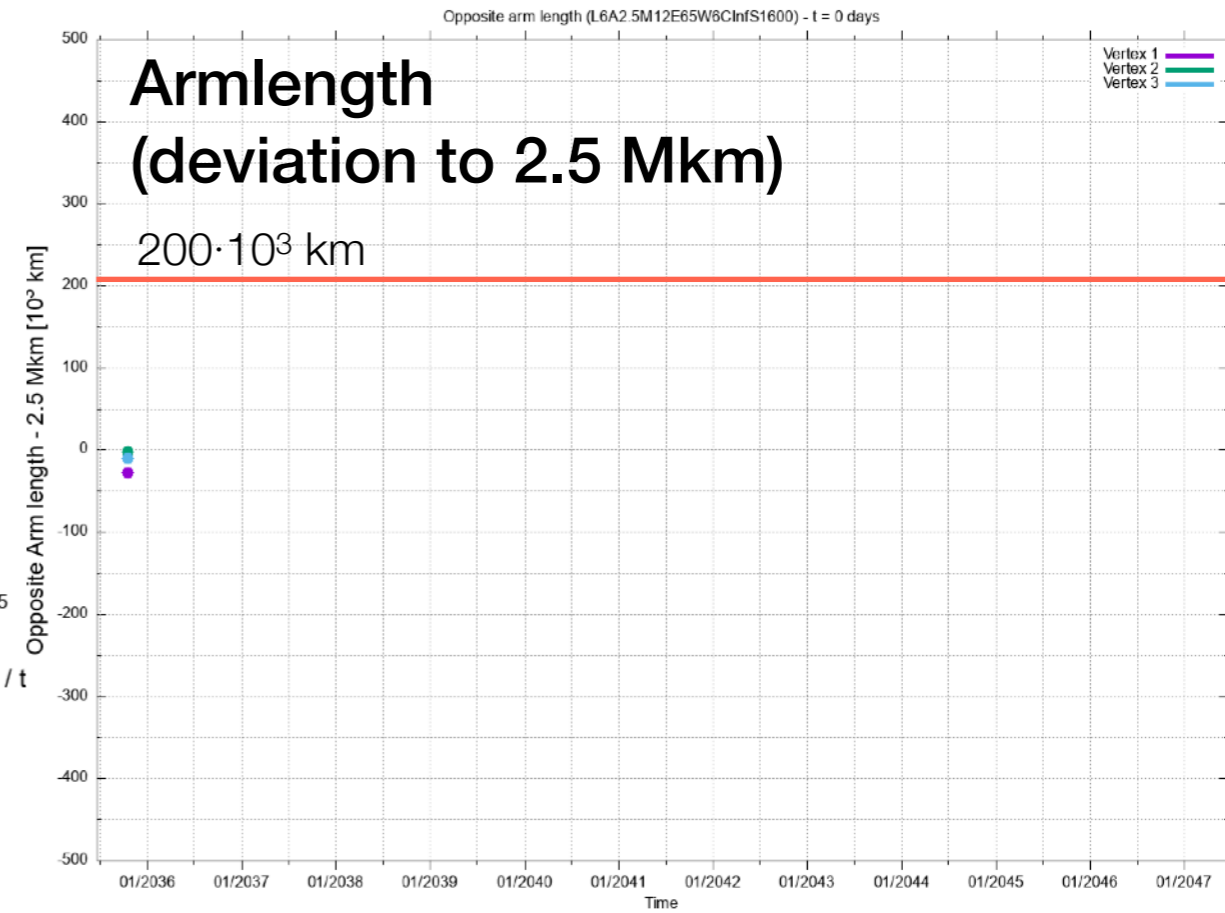
Constellation shape (L6A2.5M12E65W6CInfS1600) - $t = 0$ days / t

Constellation shape

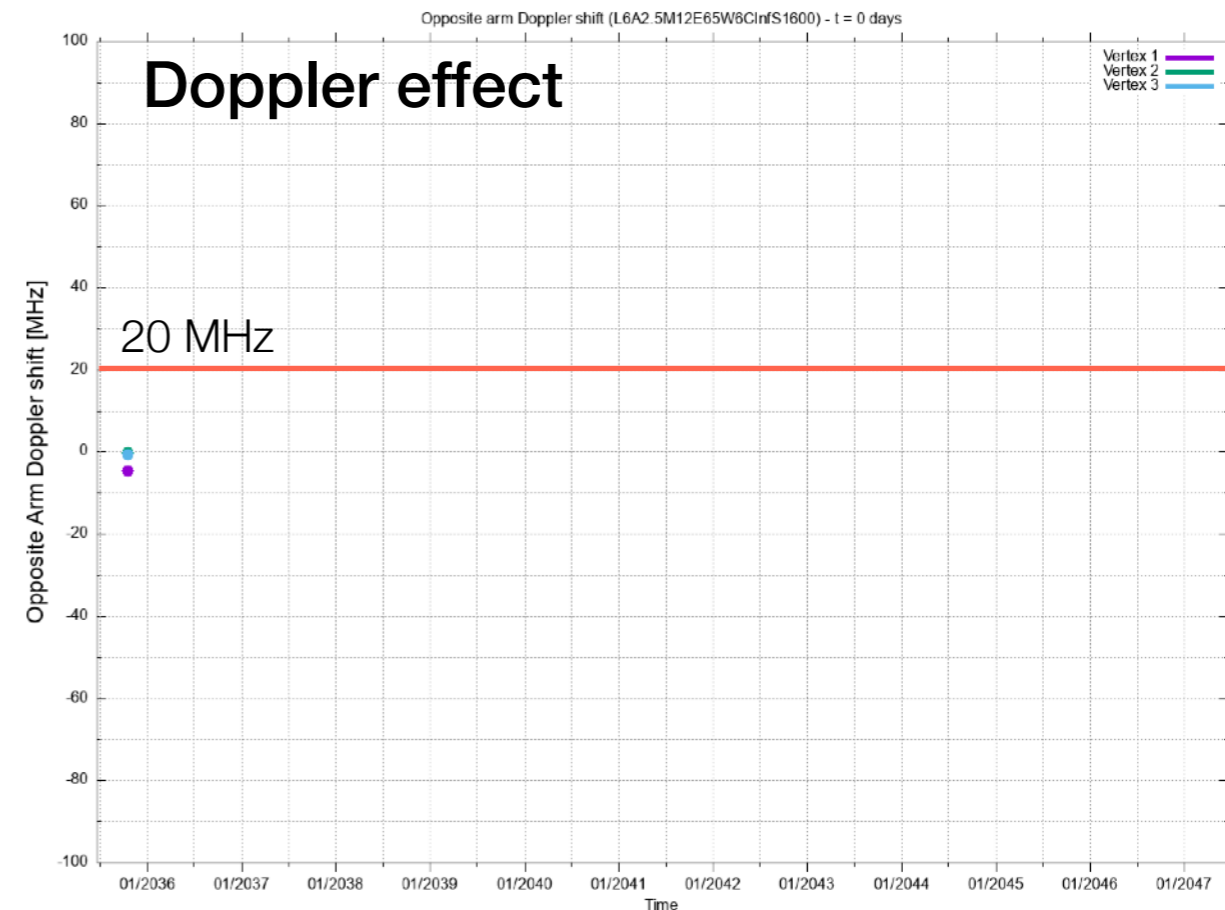


Orbital stability ?

Armlength (deviation to 2.5 Mkm)



Doppler effect








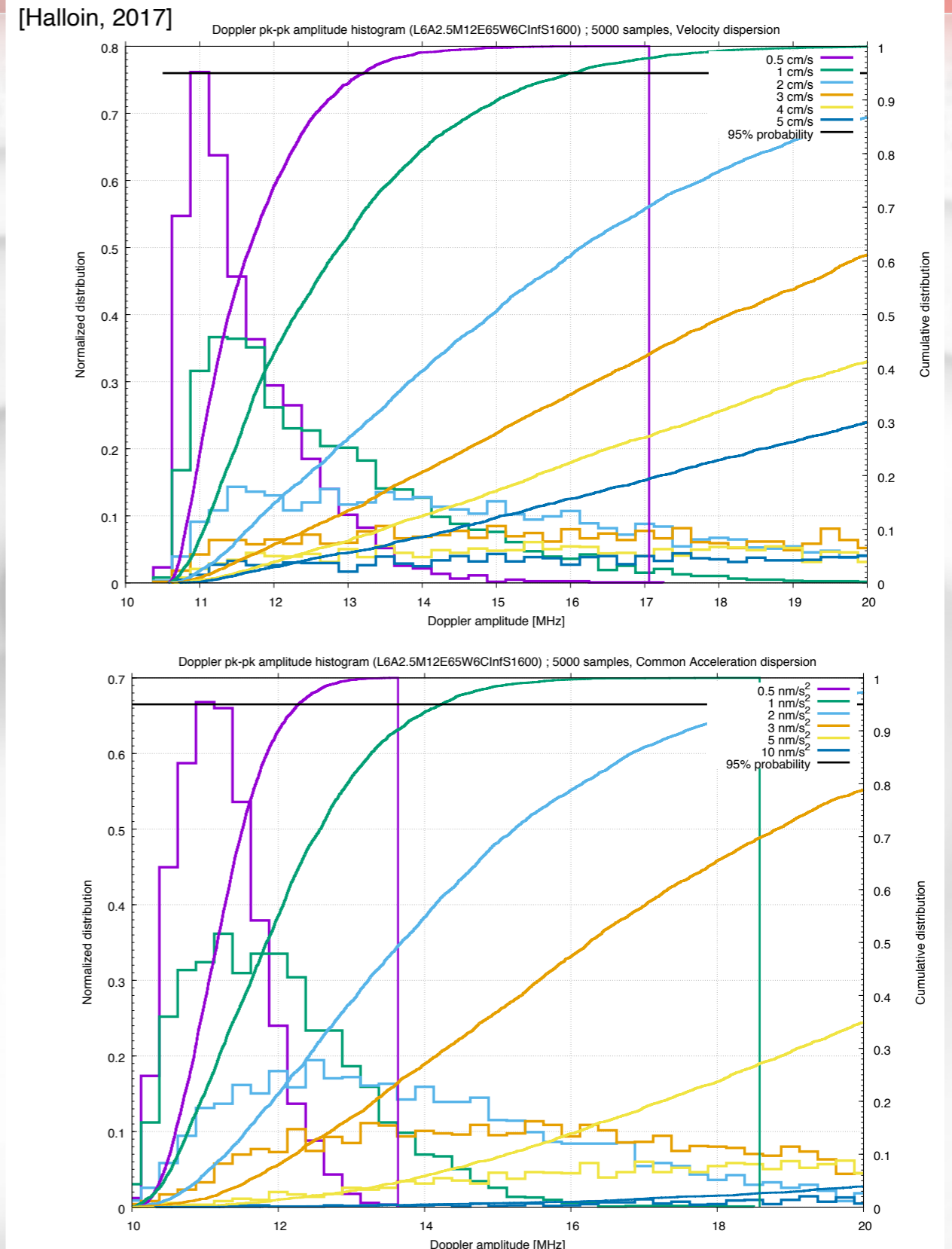
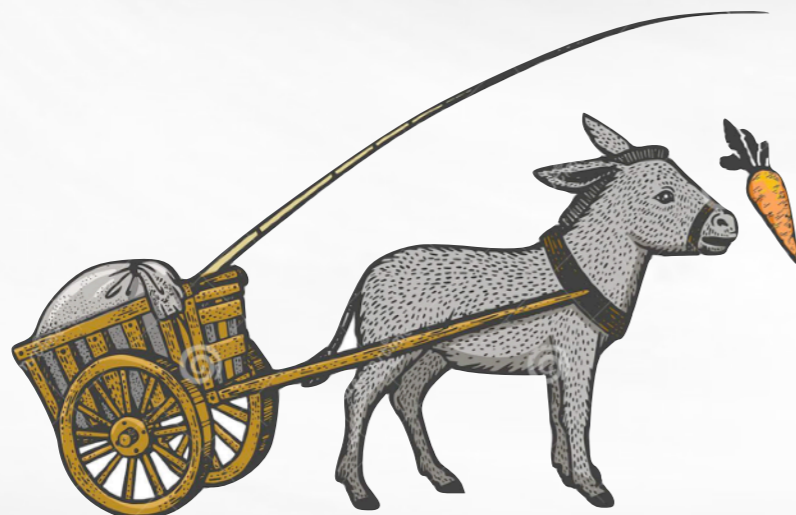
After numerical optimization of the orbital parameters

Yes, it works ;-)

Orbital stability ?

Sensitivity to local disturbances

- 
Constraints on initial S/C positioning and velocity
 - 
 ~50 km and 1 cm / s max
- 
Constraint on residual gravitational field at test mass location
 - 
 ~1,5 nm/s² max
 - 
 Equivalent to 10 kg at 60 cm



- Frequency instability of a laser beam couples to phase noise for unequal armlength

$$\begin{aligned}\delta\Phi &= \Phi(t - 2L/c) - \Phi(t - 2(L - \Delta L)/c) \\ &\approx \frac{2\Delta L}{c} \frac{\partial\Phi}{\partial t}(t - 2L/c) = \frac{2\Delta L}{c} 2\pi\delta\nu \\ \Rightarrow \delta x &= \lambda \frac{\delta\Phi}{2\pi} = 2\Delta L \frac{\delta\nu}{\nu}\end{aligned}$$

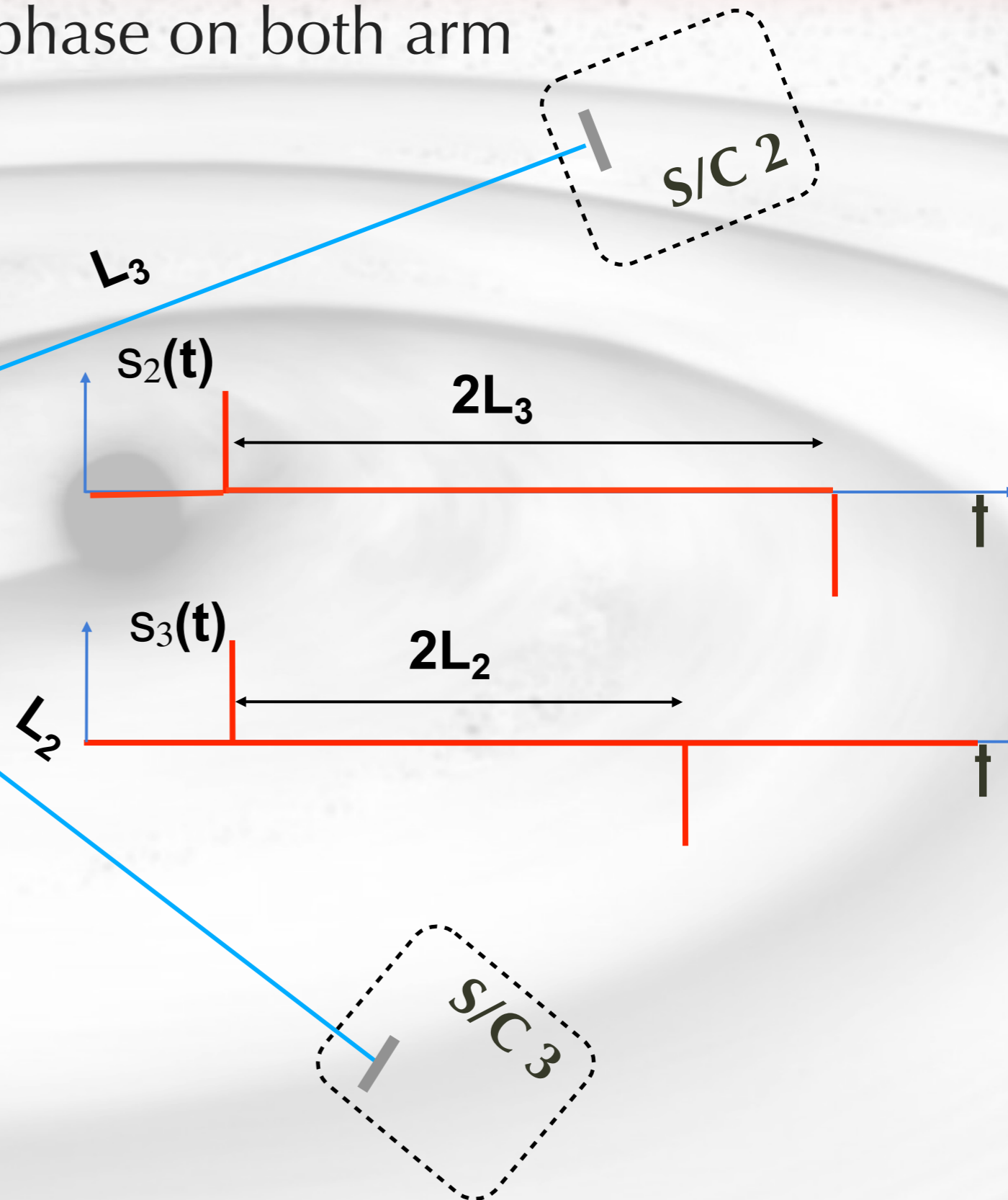
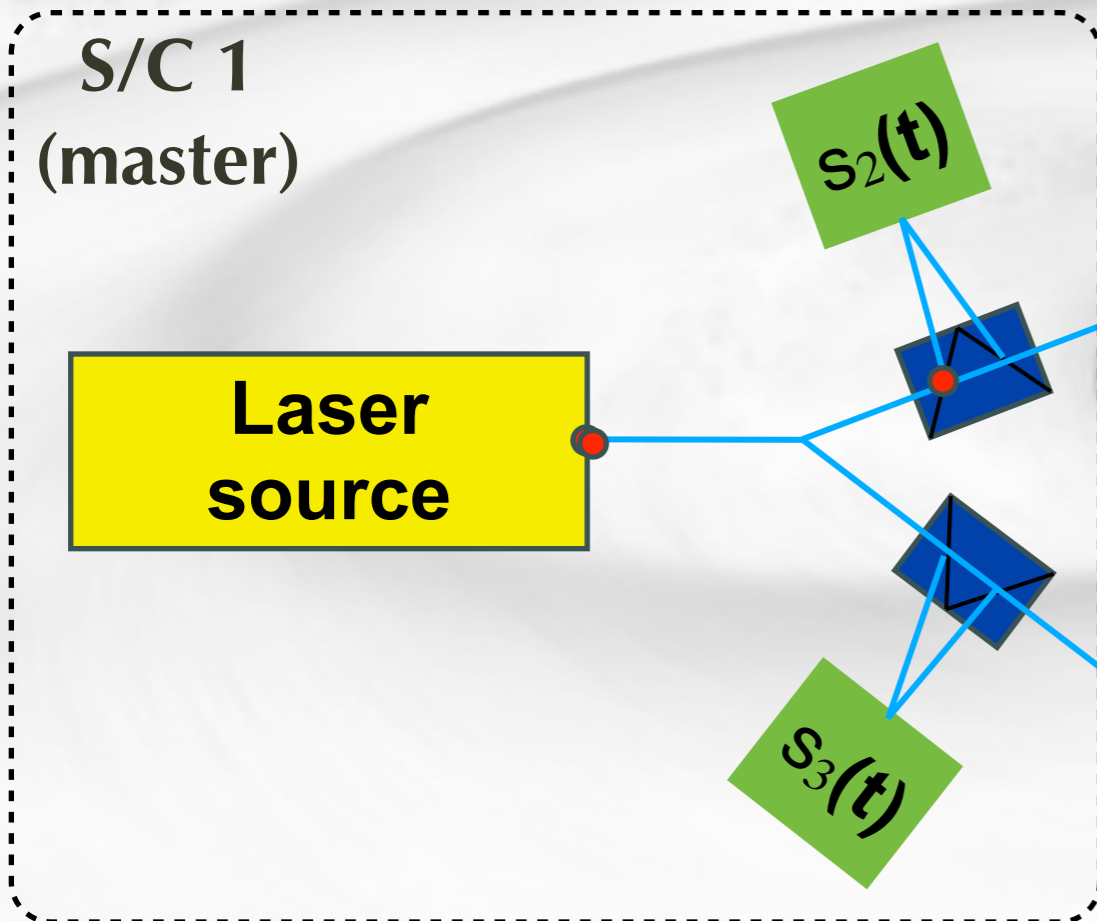
- For space-based detectors :
 - $\Delta L \sim 10\,000$ km (inertial orbits)
 - $\Rightarrow \delta\nu \sim 10^{-6}$ Hz/ $\sqrt{\text{Hz}}$ in the range [0.1 mHz : 10 Hz]

- Best 'transportable' stable laser at ~ 10 Hz/ $\sqrt{\text{Hz}}$...
 - In LISA : ultra-stable Fabry-Perot cavity

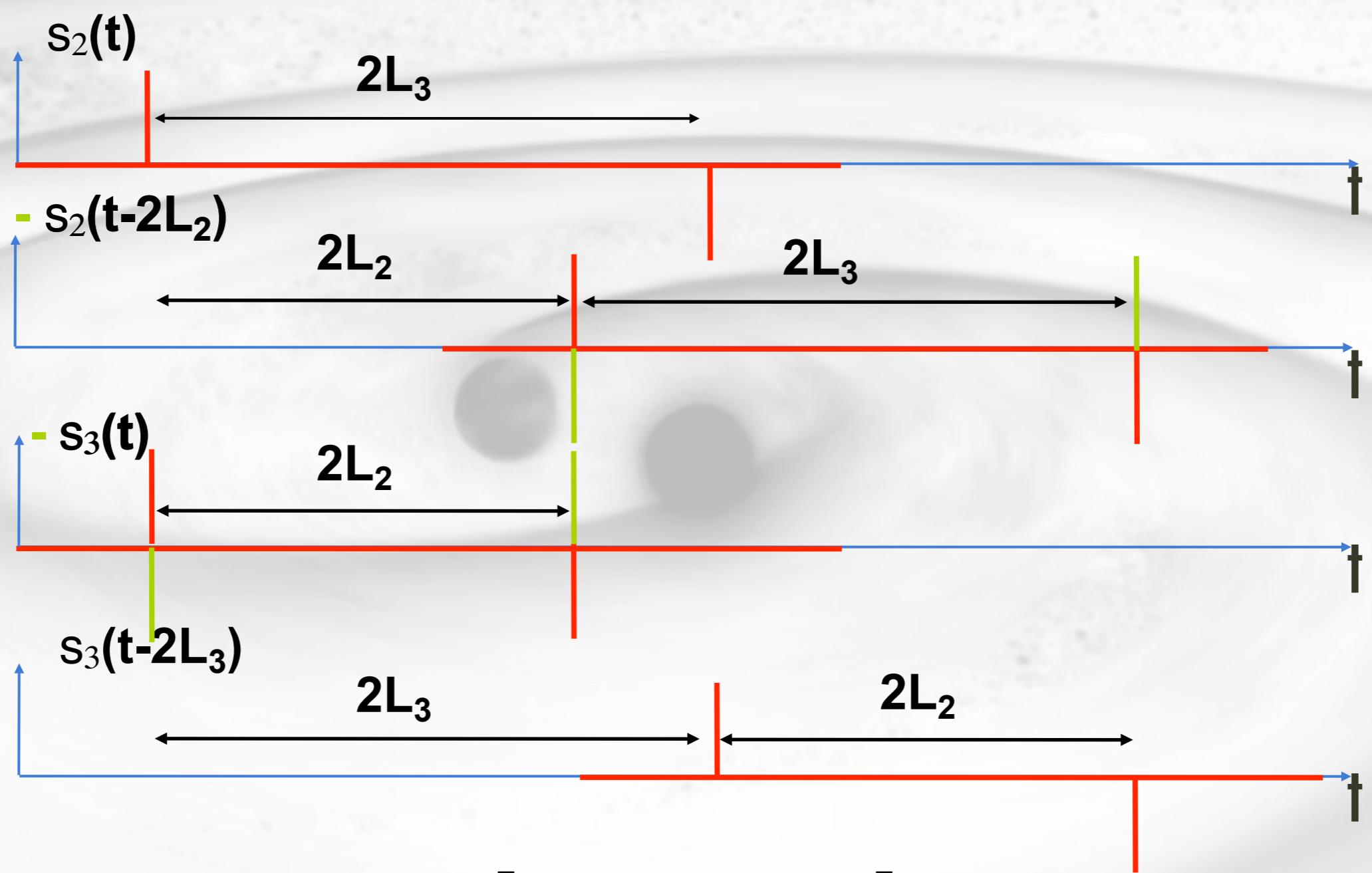
- > How to reduce the frequency noise by 7 orders of magnitude ?
 - Time Delay Interferometry

Time Delay Interferometry

- Separate measurement of the phase on both arm



Time Delay Interferometry




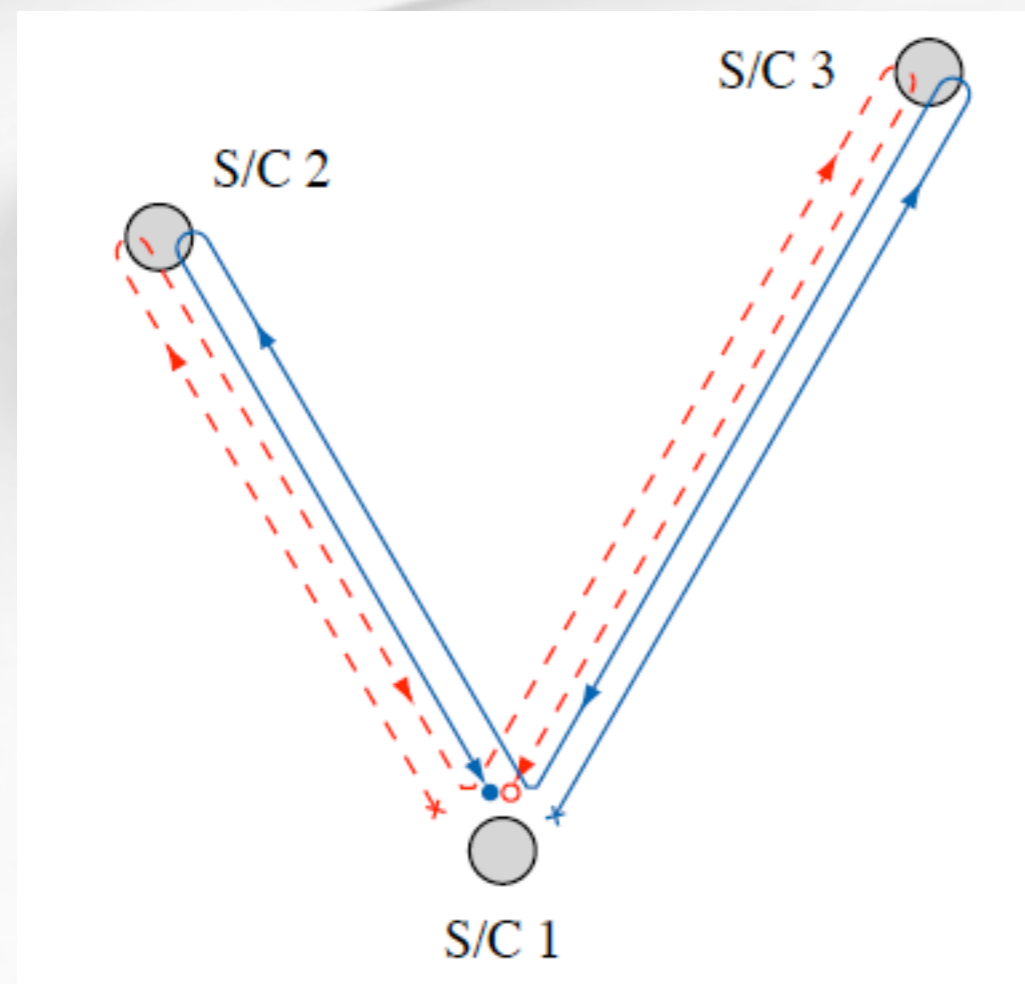
$$s_2(t) + s_3(t-2L_3) - [s_3(t) + s_2(t-2L_2)] = 0 \dots$$

$$s_2(t) + s_3(t-2L_3) - [s_3(t) + s_2(t-2L_2)] = 0 \dots$$

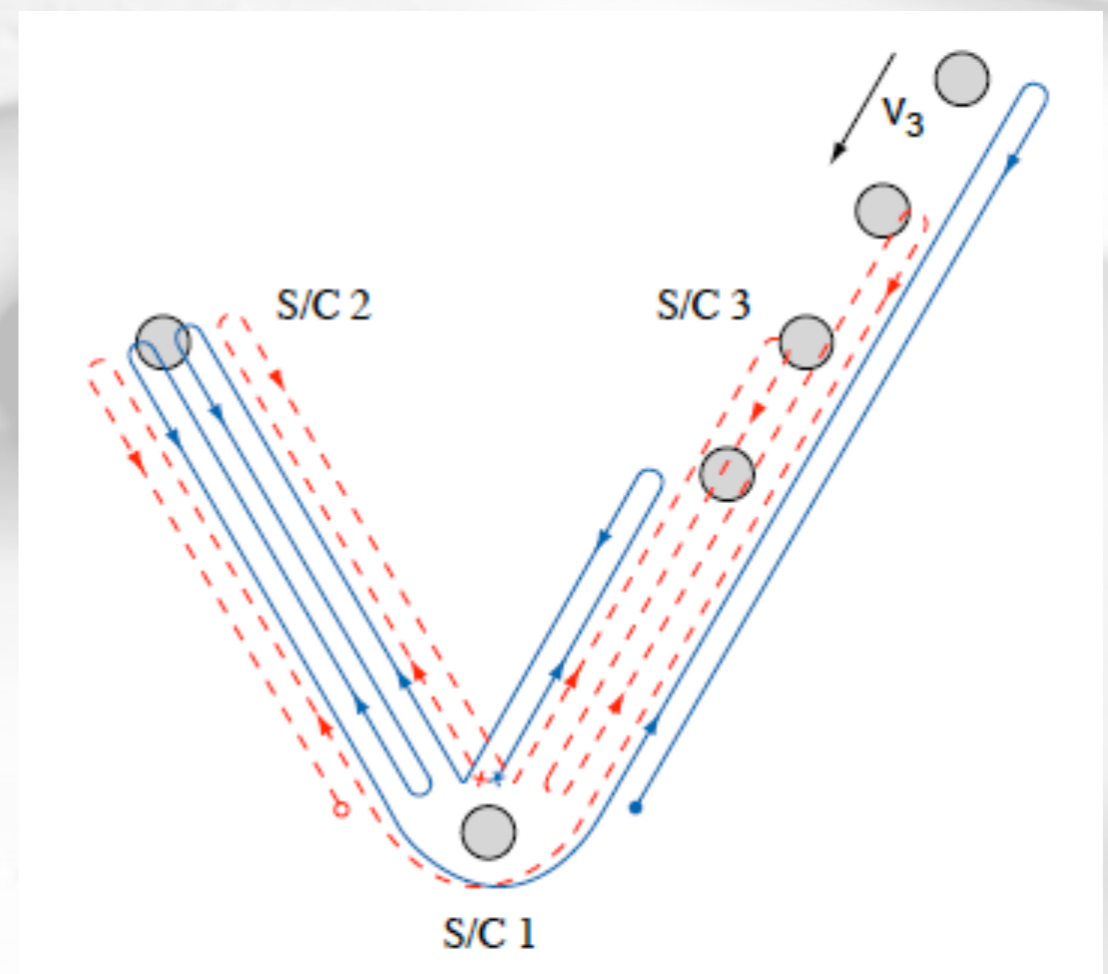
- ❁ The arm length difference is replaced by the uncertainty on the *knowledge* of the armlength
- ❁ Cancellation of propagated noises (mostly laser phase noise)
- ❁ Transfer function shaping (no signal at f multiple of $1/(2L) \sim 60$ MHz)
- ❁ \Rightarrow Requires the knowledge of :
 - ❁ S/C distances with a few meters accuracy
 - ❁ Relative clock drifts at a few ns

Time Delay Interferometry

- 
 More sophisticated combinations exist to account for the non-reciprocity of the delays (Sagnac effect) and the time-varying arm-length (S/C relative velocities)



Fixed, unequal, non-reciprocal propagation delays



Time-varying, unequal, non-reciprocal propagation delays

Key performance values

- 6 laser links, 2.5 Mkm
 - Measurement bandpass : [0.1 mHz : 1 Hz]
- Drag free performance : $3 \text{ fm}\cdot\text{s}^{-2}/\sqrt{\text{Hz}}$
- Telescopes:
 - ~300 mm diameter,
 - Internal pathlength stability: ~ a few pms/ $\sqrt{\text{Hz}}$
- Laser
 - Nd:YAG (1064 nm), 2 W emitted (received ~400 pW)
 - RIN : $<10^{-8} /\sqrt{\text{Hz}}$ above 5 MHz
 - ~30 Hz/ $\sqrt{\text{Hz}}$
- Timing jitter in clock distribution: ~40 fs/ $\sqrt{\text{Hz}}$
- Absolute ranging accuracy: ~1 m
- Thermal stability (optical bench): $< 10 \mu\text{K}/\sqrt{\text{Hz}}$ at 1 mHz
- Laser beam pointing jitter: ~5 nrad/ $\sqrt{\text{Hz}}$

- ❖ Free flying test mass subject to very low parasitic forces:
 - ❖ Drag free control of spacecraft (non-contacting spacecraft)
 - ❖ Low noise microthruster to implement drag-free
 - ❖ Large gaps, heavy masses with caging mechanism
 - ❖ High stability electrical actuation on cross degrees of freedom
 - ❖ Non contacting discharging of test-masses
 - ❖ High thermo-mechanical stability of S/C
 - ❖ Gravitational field cancellation
- ❖ Precision interferometric, local ranging of test-mass and spacecraft:
 - ❖ pm resolution ranging, sub-mrad alignments
 - ❖ High stability monolithic optical assemblies
- ❖ Precision million km spacecraft to spacecraft precision ranging:
 - ❖ High stability telescopes
 - ❖ High accuracy phase-meter
 - ❖ High accuracy frequency stabilization
 - ❖ Constellation acquisition
 - ❖ Precision attitude control of S/C

Free flying test mass subject to very low parasitic forces:

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**Validated with
LISA Pathfinder**

Precision interferometric, local ranging of test-mass and spacecraft:

- pm resolution ranging, sub-mrad alignments
- High stability monolithic optical assemblies

Precision million km spacecraft to spacecraft precision ranging:

- High stability telescopes
- High accuracy phase-meter
- High accuracy frequency stabilization
- Constellation acquisition
- Precision attitude control of S/C**

Free flying test mass subject to very low parasitic forces:

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**Validated with
LISA Pathfinder**

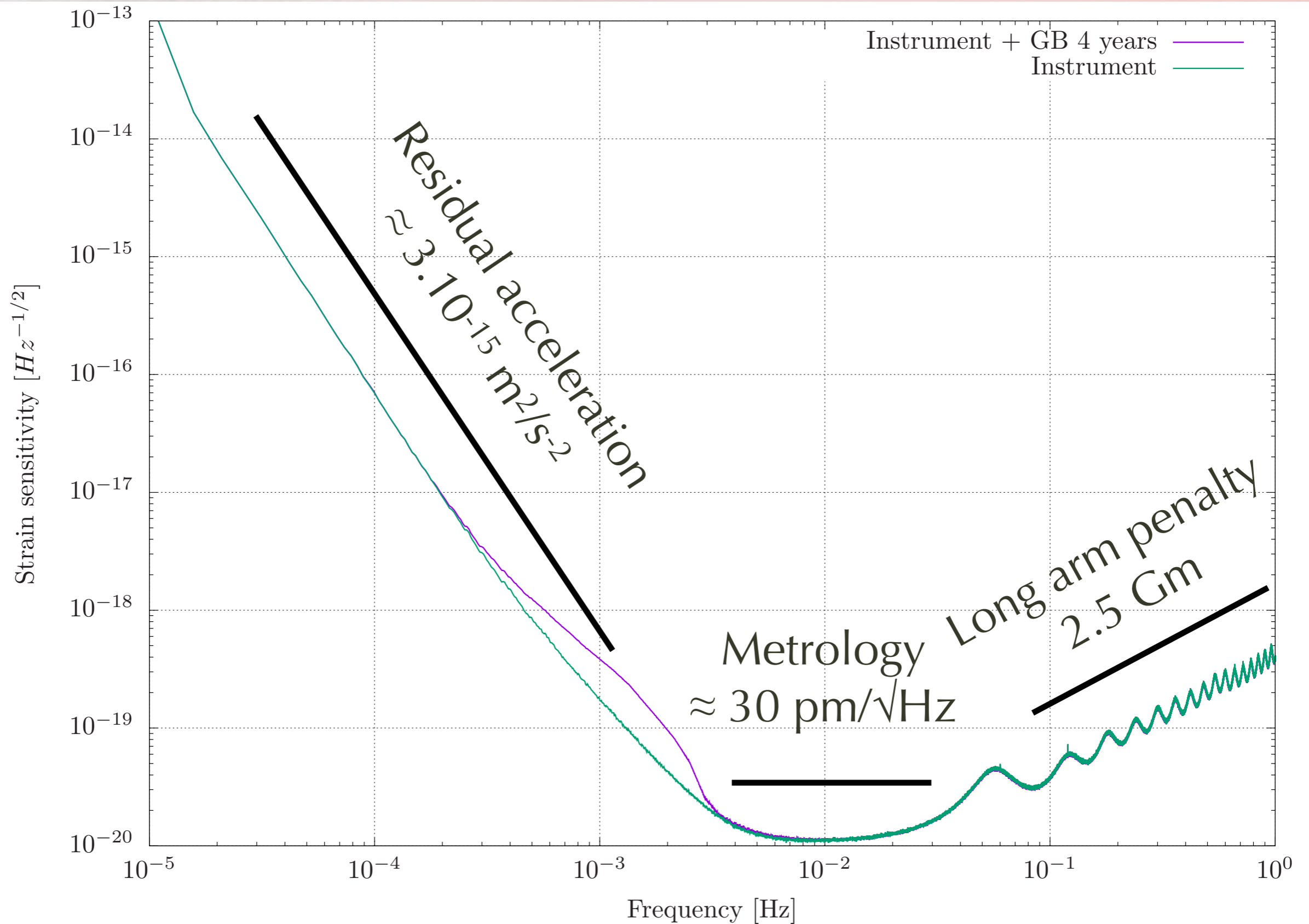
Precision interferometric, local ranging of test-mass and spacecraft:

- pm resolution ranging, sub-mrad alignments
- High stability monolithic optical assemblies

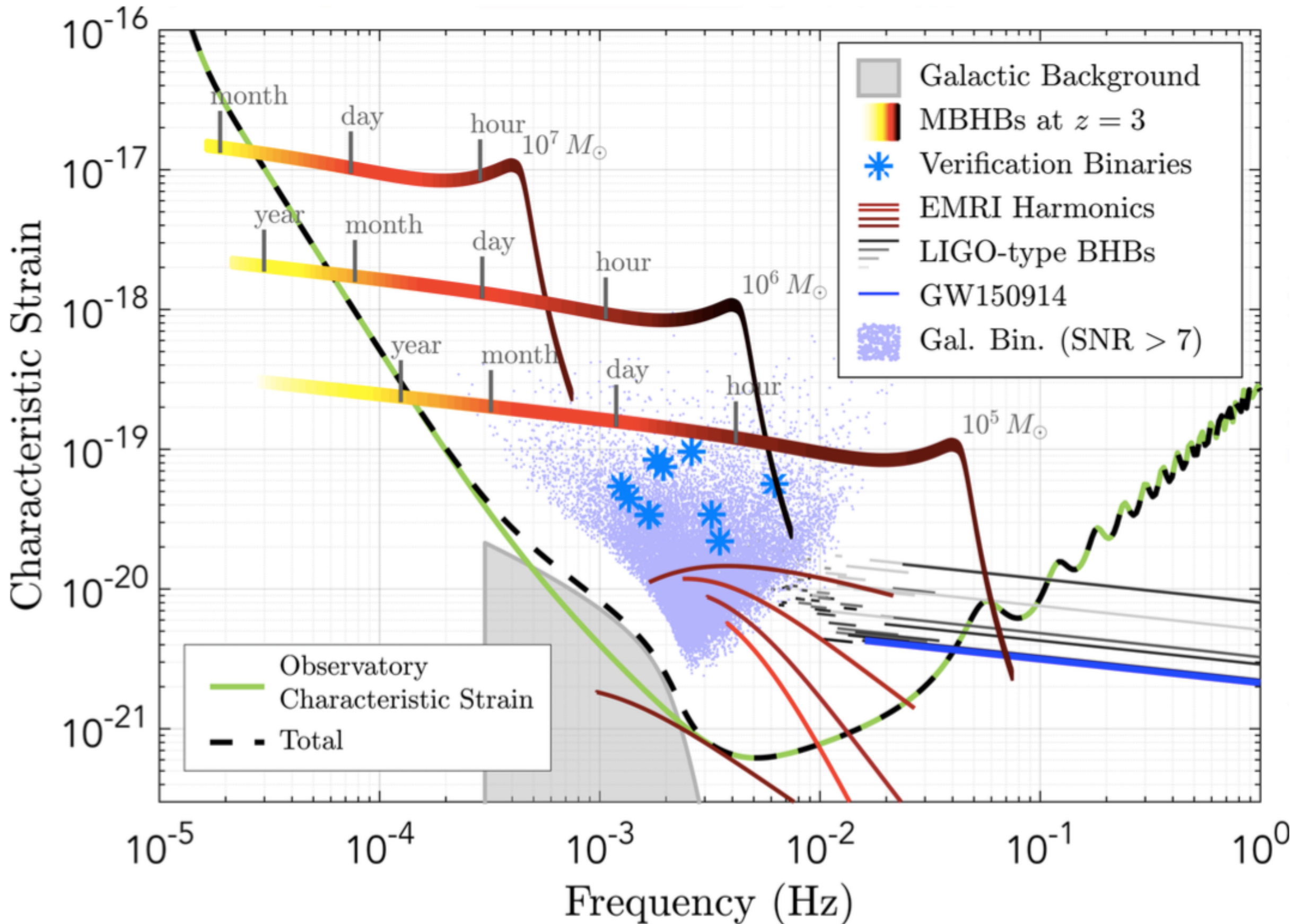
Precision million km spacecraft to spacecraft precision ranging:

- High stability telescopes
- High accuracy phase-meter and frequency distribution
- High accuracy frequency stabilization (incl. TDI)
- Constellation acquisition and low jitter laser pointing
- Precision attitude control of S/C

**Ground-based
demonstrators**

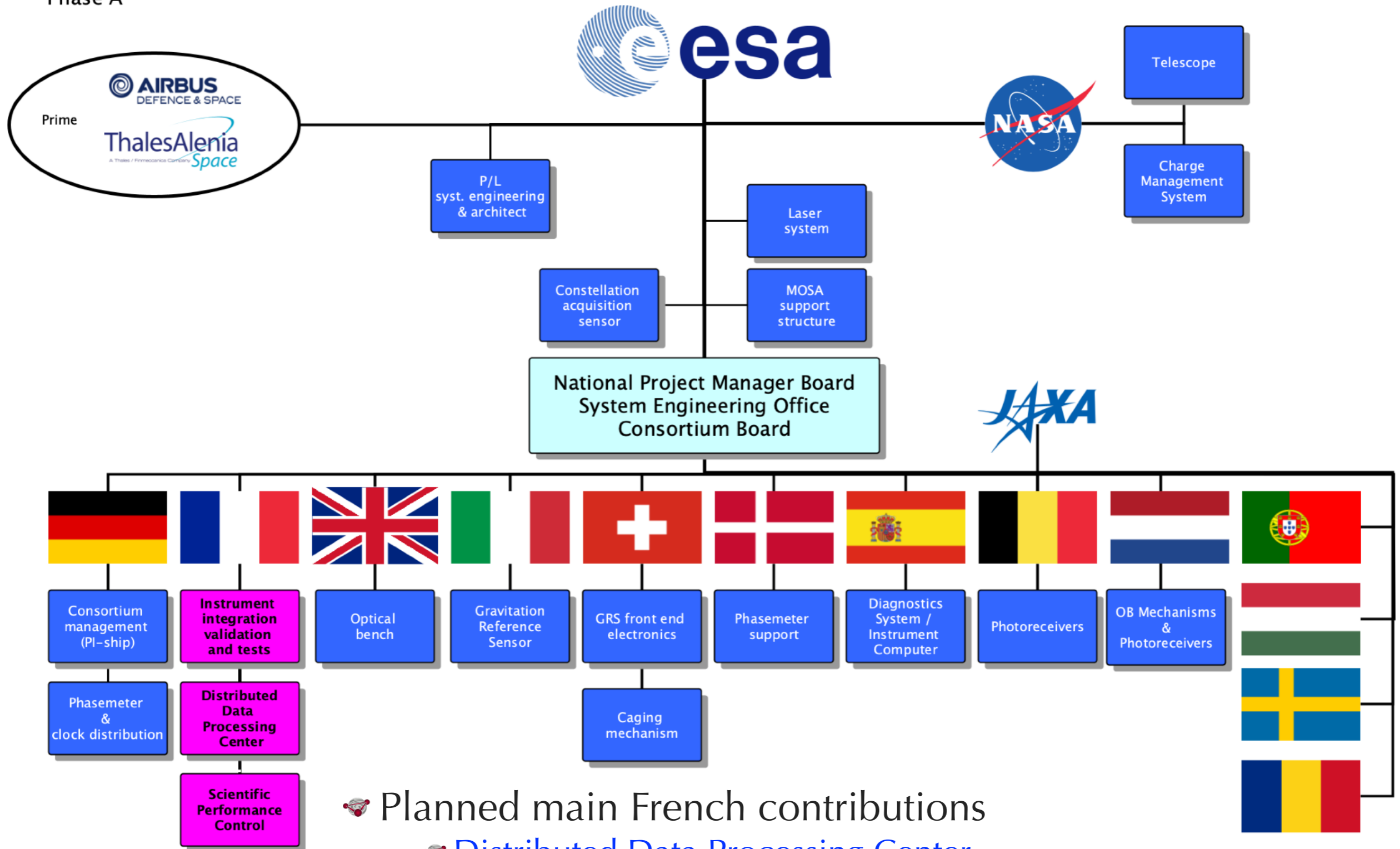


LISA Strain Sensitivity



French contribution to LISA ?

Phase A

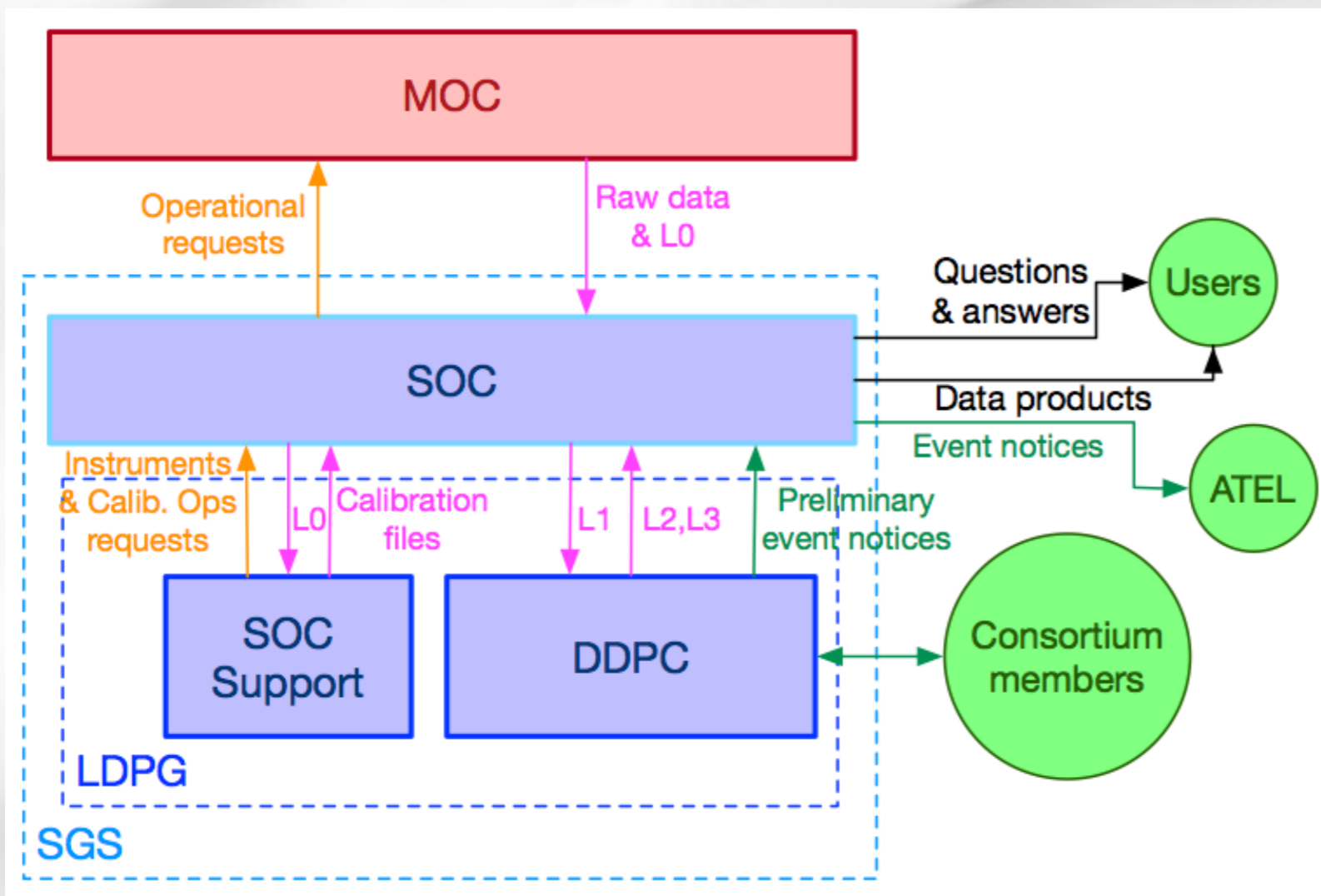


🚀 Planned main French contributions

- 🚀 Distributed Data Processing Center
- 🚀 MOSA AIVT & Perf. Control

- Presently 19 laboratories / research institutes participate to the LISA France collaboration
 - @IN2P3 : APC, CPPM, L2IT, LPCC, LMA/IP2I, CC-IN2P3
 - @INSU : LAM, IAP, LPC2E
 - @INSIS : Institut Fresnel
 - @Obs de Paris / INSU : SYRTE, LUTh
 - @Obs. de la Côte d'Azur / INSIS : ARTEMIS
 - @CEA : IRFU (DEDIP, DIS, DPhN, DPhP, DAP), IPhT
- CNES is managing and supporting the project activities with engineers and financial resources (incl. short-term contracts).

- Development of a Distributed Data Processing Center for LISA
 - Produces scientific L2&L3 data and supports ESA on L0 to L1 software
 - Will implement, maintain and operate simulations and data analysis
 - Supports the LISA community for SW and collaborative tools
 - Prototype architecture based on virtualisation and continuous integration



docker



GitLab



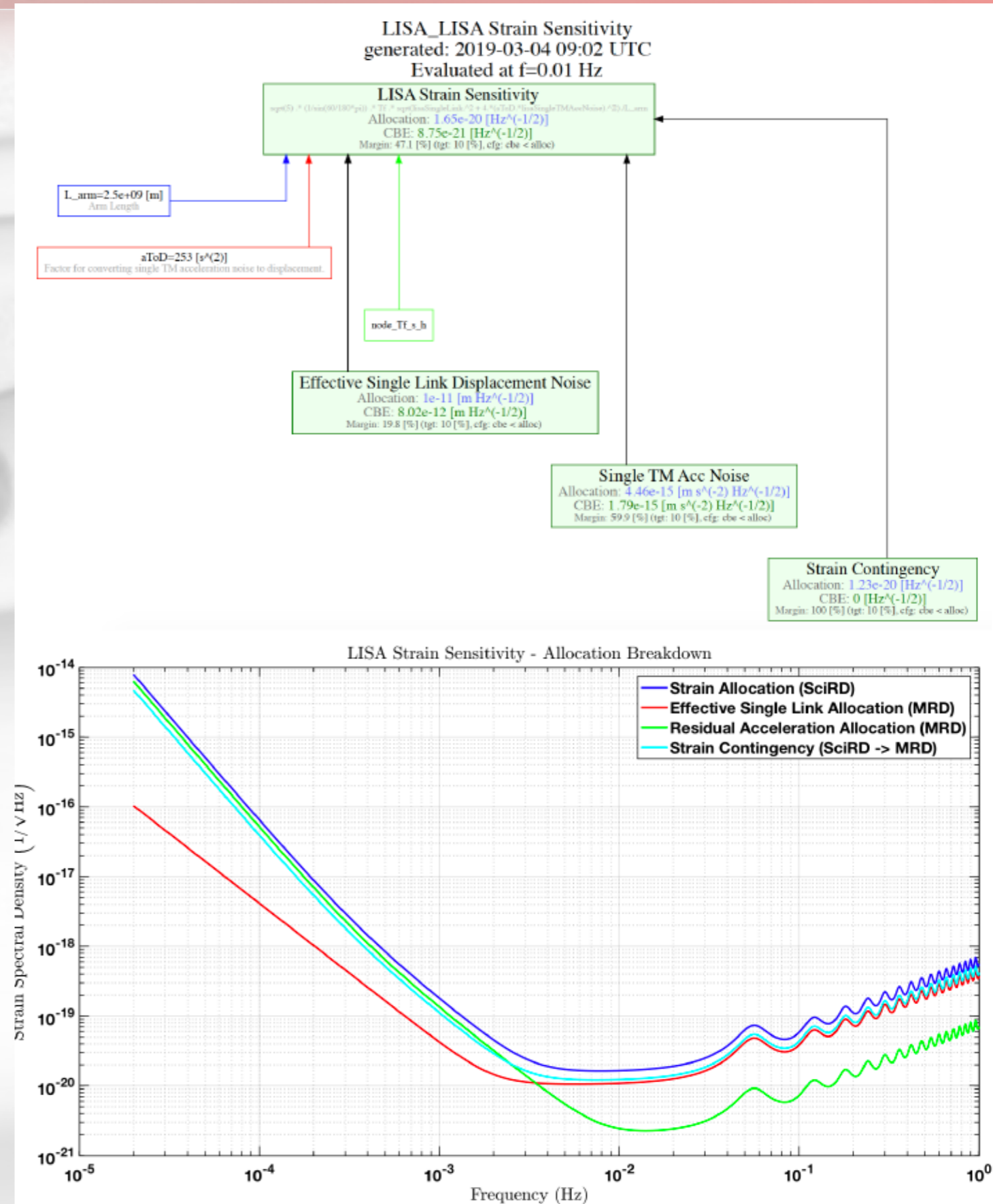
Objective : build a 'simplified', system-level, performance model

- Identify critical items
- Unified view of the system performance from science requirement to sub-systems level.
- Support the allocation breakdown for each sub-system
- Sensitivity analysis to support design trade-off

Different sources of information

- Specific or 'end-to-end' simulations
- Mathematical & physical models
- Lab experiments

Interface with all stakeholders – Consortium, Agencies, Industry.

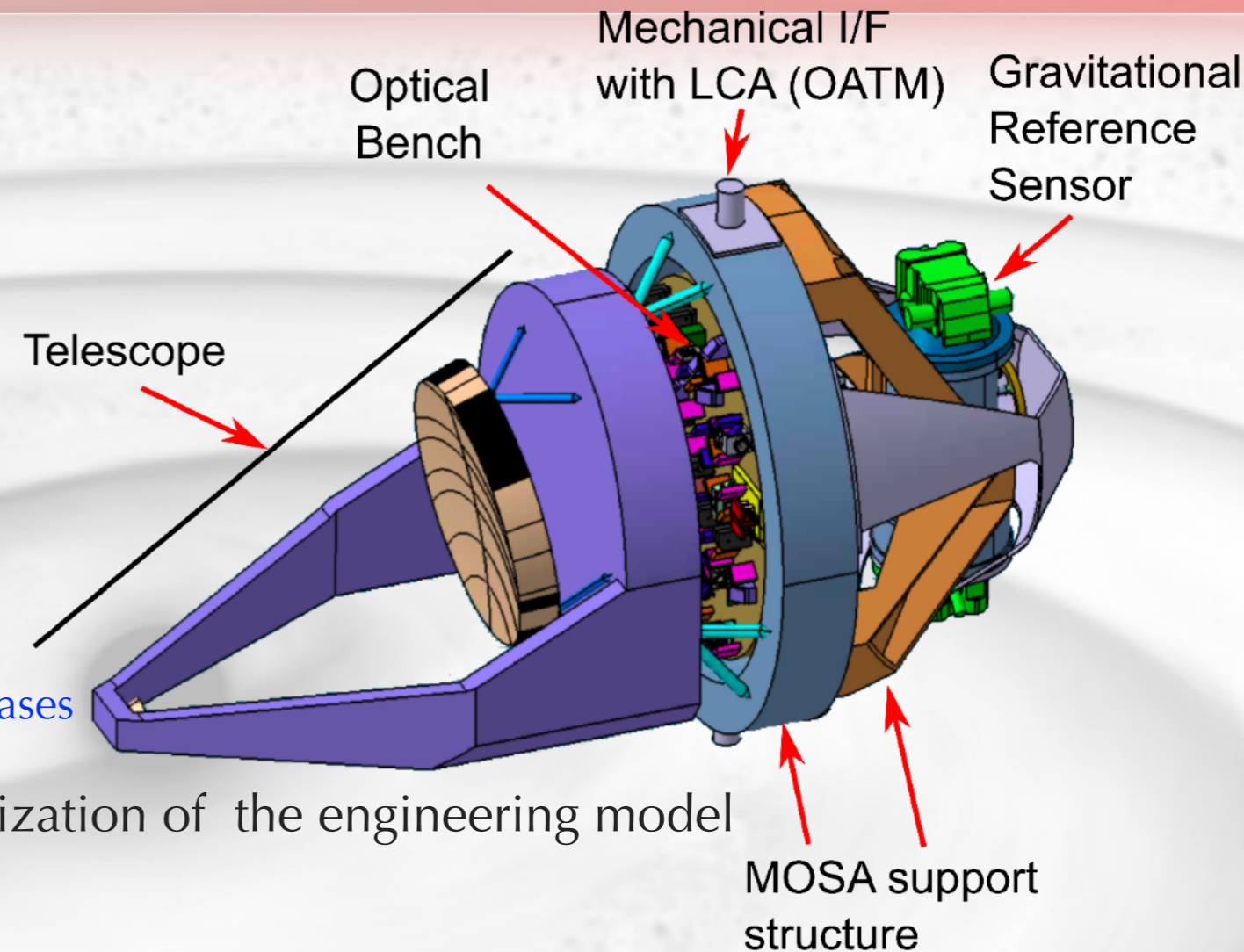


- LISA will be the first instrument of its kind
 - Not a collection of separate instruments
 - Combination of finely designed equipments, forming a Mkm-scale instrument

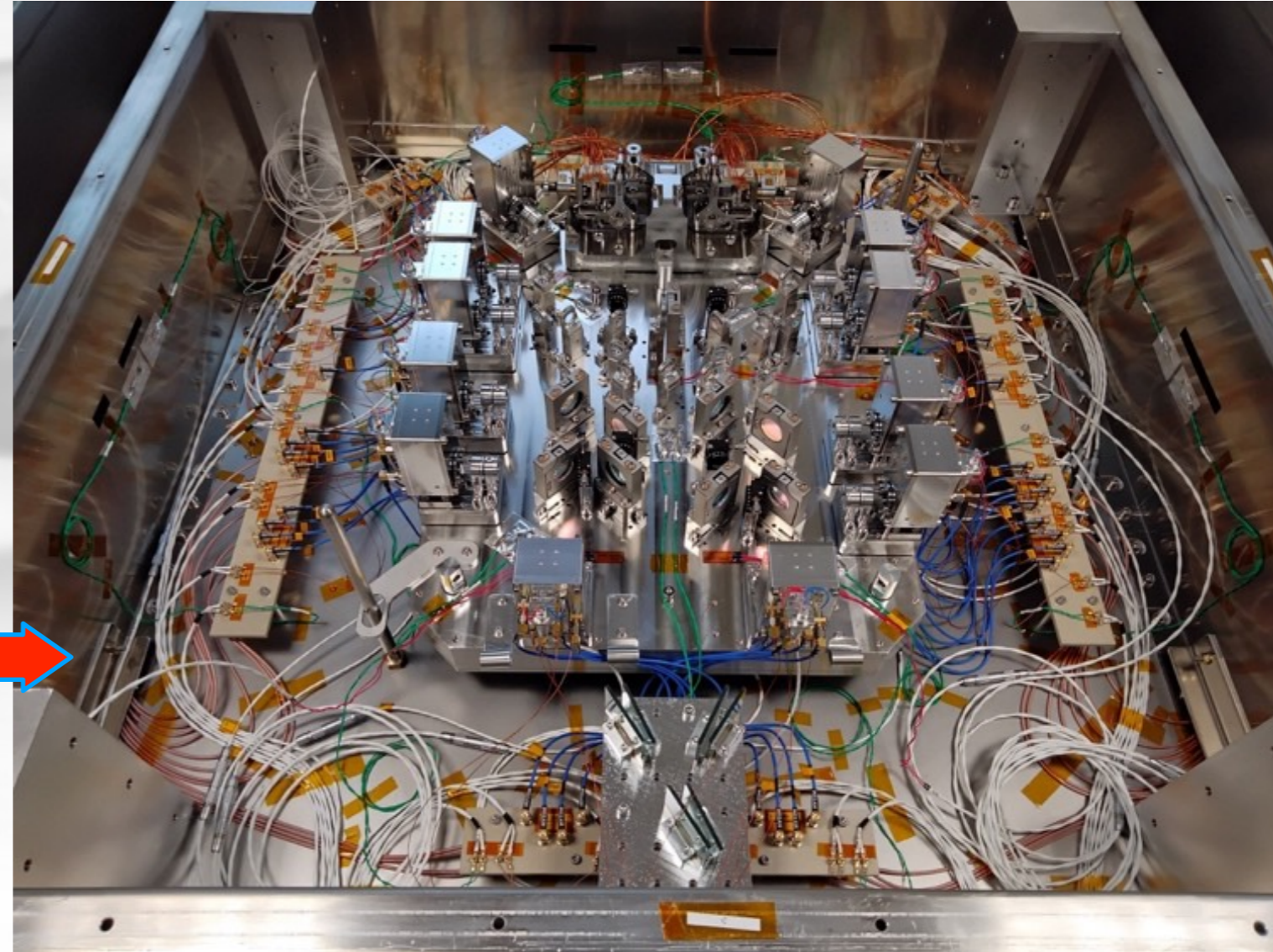
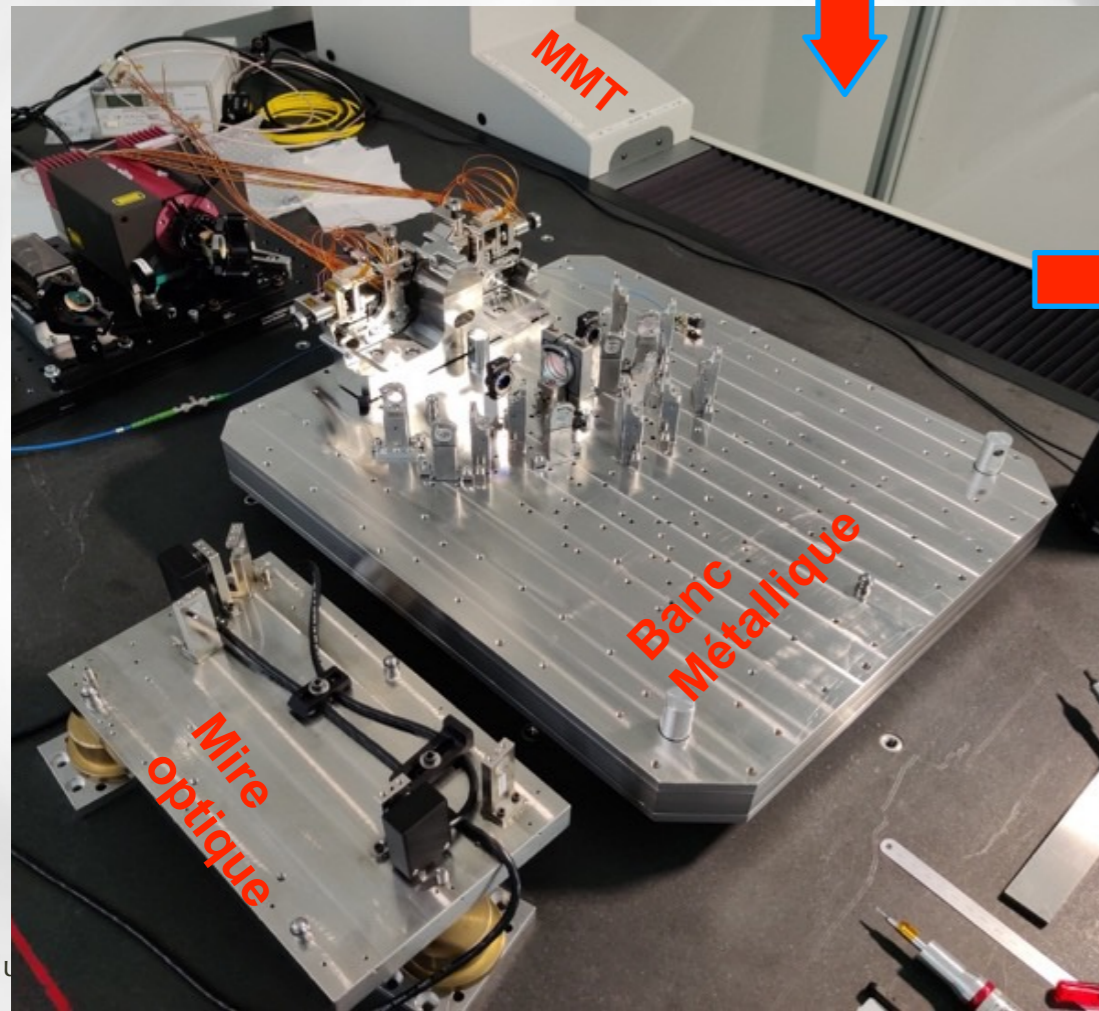
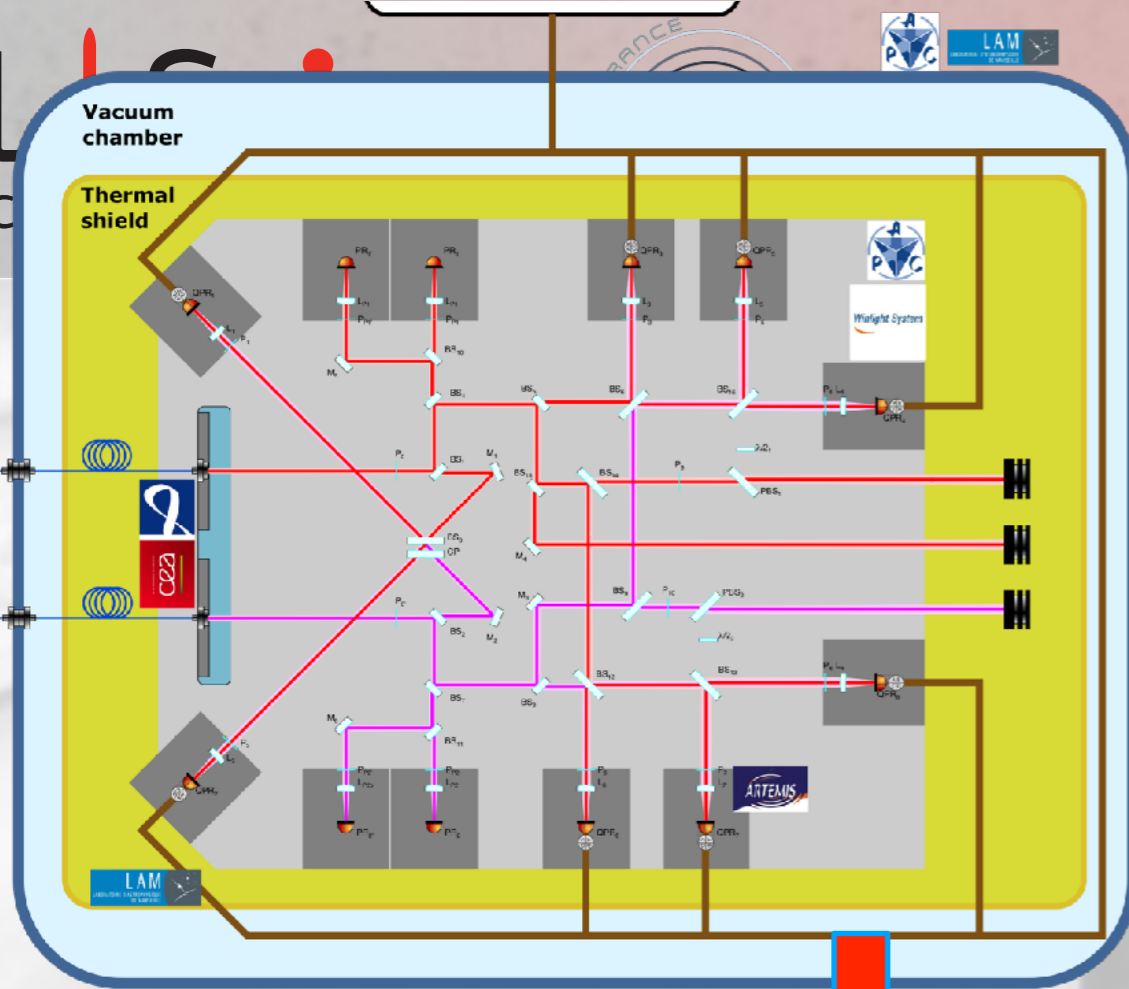
- LISA science return depends on the in-depth performance characterisation of the metrology core
 - Importance of the AIVT and scientific performance modelling
 - Crucial activity giving high visibility and involvement in early instrument development phases

- Development of optical benches and characterization of the engineering model of the instrument 'core'
 - Optical bench + phasemeter + laser

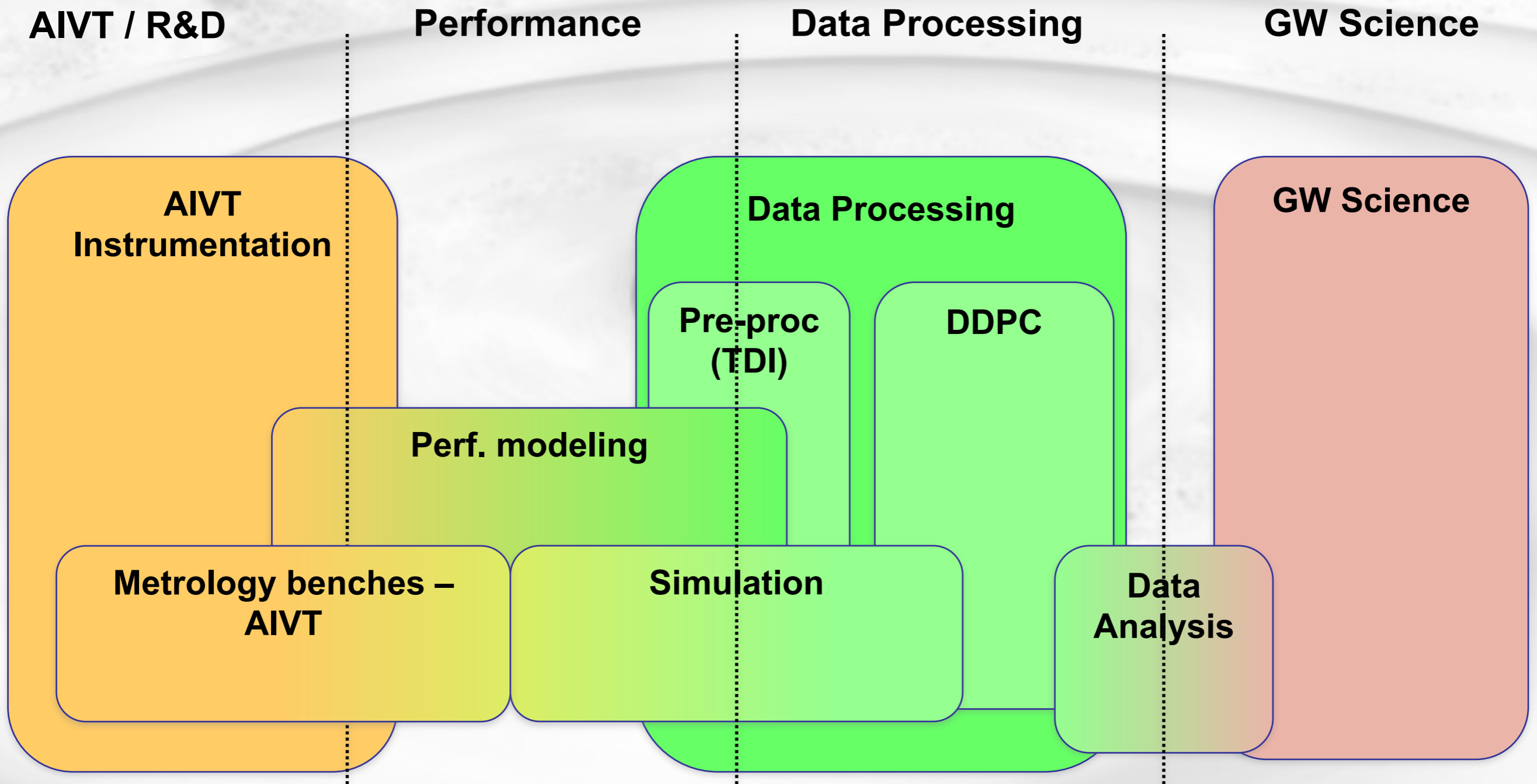
- Integration and tests in close collaboration with industries
 - 10 MOSAs to integrate and validate (1 STM, 1 EQM, 1 PFM, 5 FMs, 2 spares)
 - Research institutes : development of optical metrology test benches and strong involvement in the QM characterisation
 - Experience on MOSA testing transferred to industry for the FMs
 - Industries : integration procedures and semi-serialisation of FMs & spares AIVT
 - The research institutes still follow the process and interpret the measurements



Optical bench prototype



🚀 Broad and continuous coverage, from instrument to GW science



 *Introduction*

 *LISA Science Objectives*

 *From LISA Pathfinder to LISA*

 *Mission description*

 **Conclusion**

- Laser interferometry is currently the most sensitive technique for detecting GWs
- LISA will observe mHz GWs around from space
 - Complementary to ground-based detectors
- Many technological challenges ahead been demonstrated with LISA Pathfinder
- The Preliminary Design Phase of LISA has started
 - Expected mission adoption end 2023
- Crucial contributions from French institutes
 - The hard work has now started ...



Coming soon...

