Alexandre Toubiana

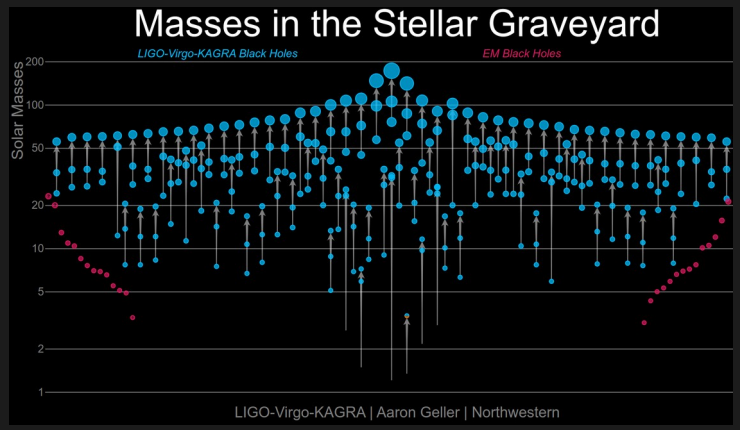
Assemblée générale du GdR OG, 14/10/2024

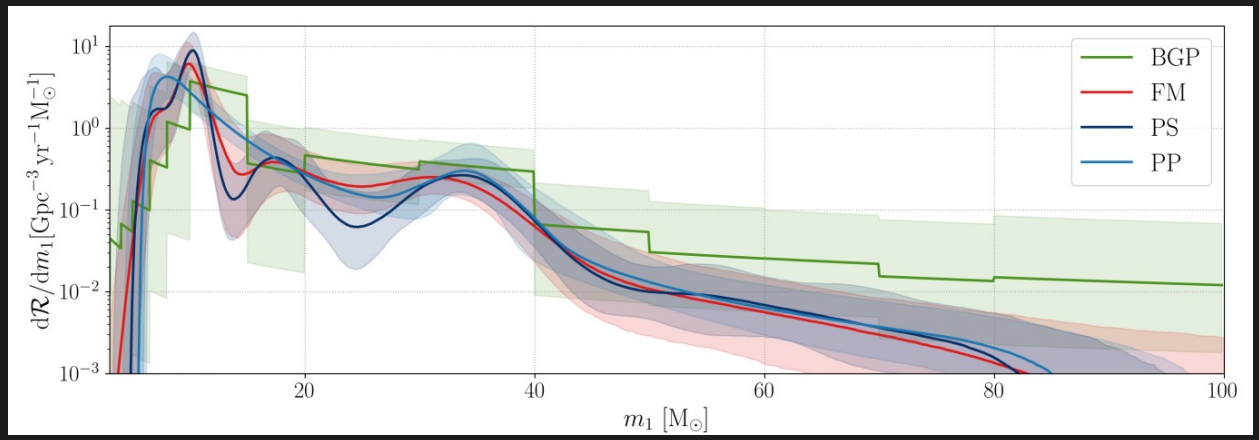
Towards LISA population study

Based on

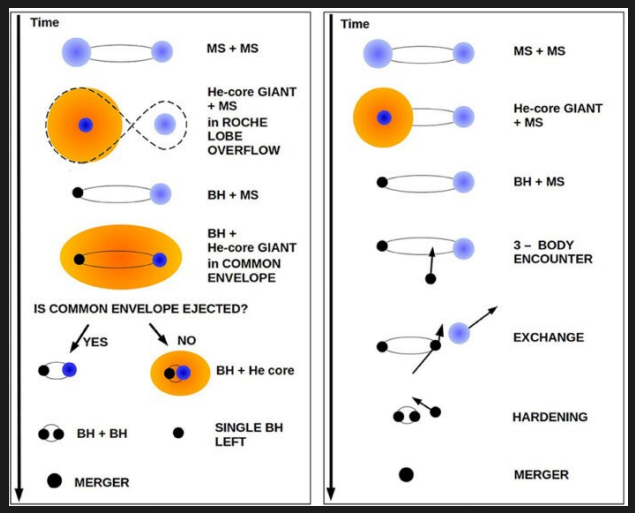
Toubiana, Karnesis, Lamberts, Miller A&A 2024
Toubiana, Sberna, Volonteri, Barausse +, in prep
Toubiana, Gair, ongoing
Santini, Karnesis, Toubiana, on going

Population studies





LVK, PRX 2023

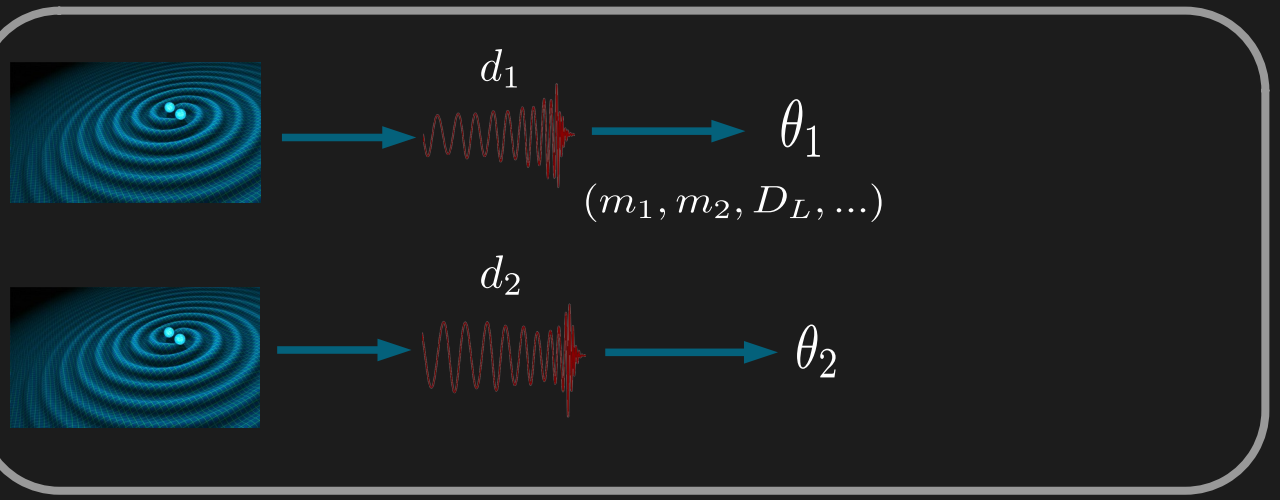


Mapelli, Front. Astron. Space Sci. 2020

Extract global properties of observations to allow the astrophysical interpretation

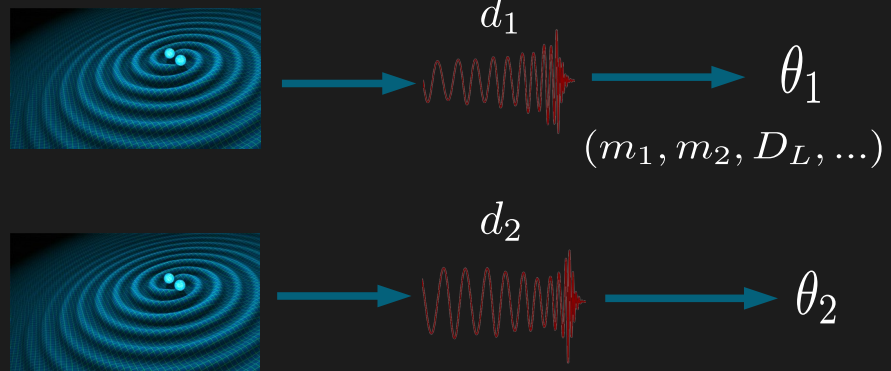
Steps for population studies

Parameter estimation

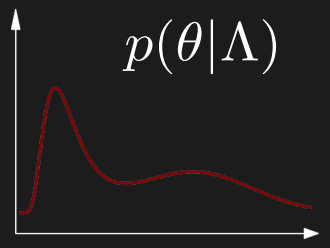


Steps for population studies

Parameter estimation



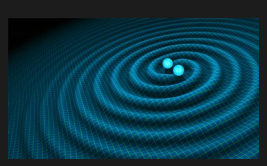
Population model



- astrophysical
- agnostic (parametric/non-parametric)

Steps for population studies

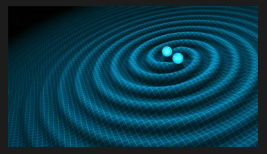
Parameter estimation



d_1

θ_1

$(m_1, m_2, D_L, ...)$



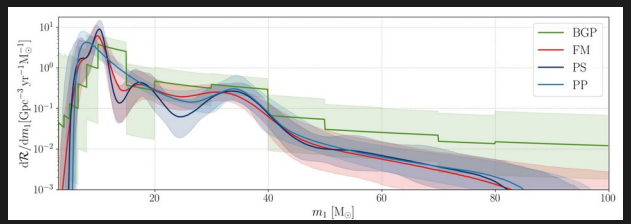
d_2

θ_2

$\{d_1, d_2, ...\}$

Hierachical Bayesian analysis

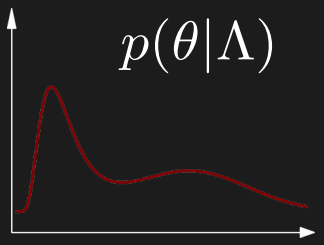
$p(\Lambda|\{d_1, d_2, ...\})$



LVK, PRX 2023

Population model

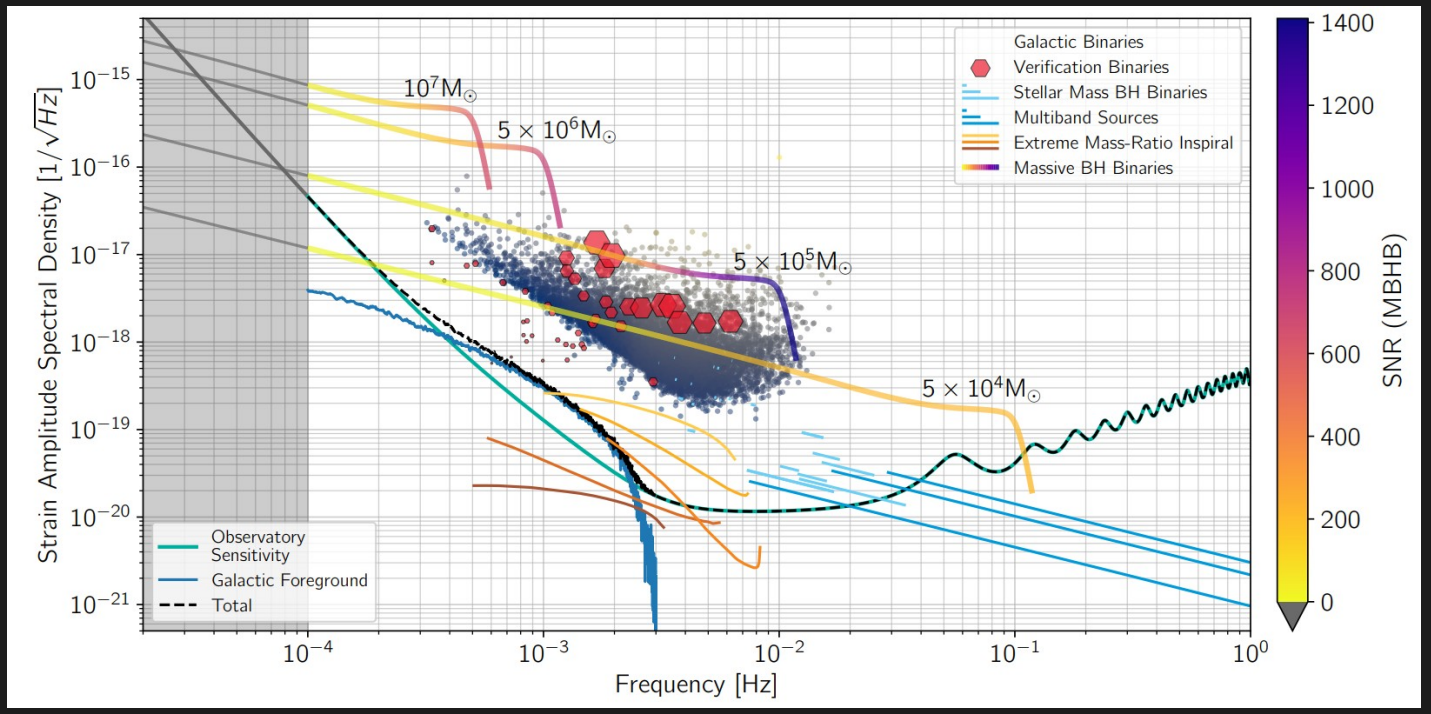
$p(\theta|\Lambda)$



- astrophysical
- agnostic (parametric/non-parametric)

+ selection effects

Challenges for LISA



LISA Redbook, 2024

- Lack of parametrised description of population of sources $p(\theta|\Lambda)$
- Need to fit data all together (Global Fit), problem for hierarchical analysis:
  - signals are not independent
  - variable number of sources
  - selection function?

Massive black hole binaries

- Cosmological and semi-analytic models: explore impact of physical assumptions but high computational cost

- Toubiana+ PRD 2021: using a finite discrete set of model to describe the population can lead to biases

- Goal: develop a framework to describe the formation and evolution of massive black holes suited for analysing data (see also Langen, Tamanini, Marsat, Bortolas 2024)

Parametric model for massive black holes

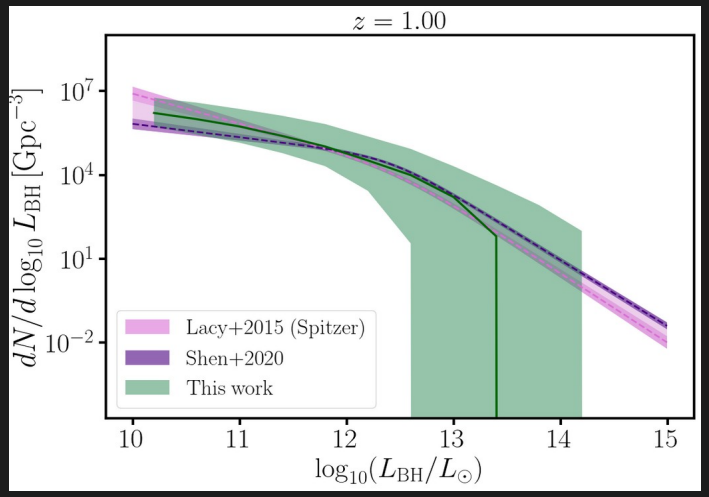
- POMPOCO: Parametrisation Of the Massive black hole POpulation for Comparison to Observations

  (Toubiana, Sberna, Volonteri, Barausse +, in prep)

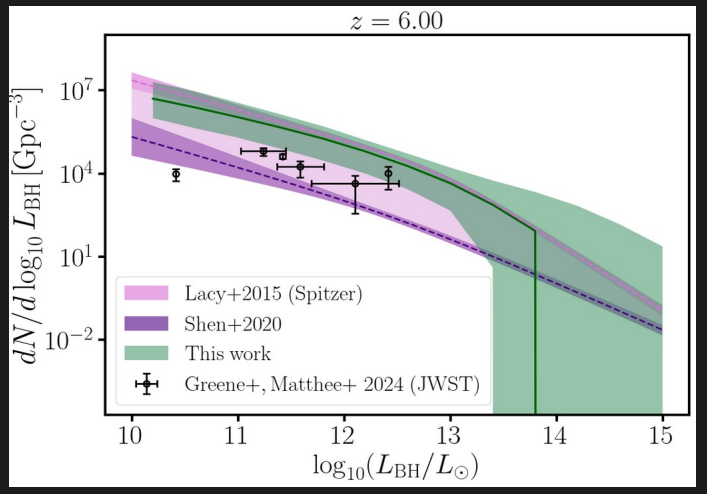
- Describe evolution of massive black holes inside host halos using parametric prescriptions for seeding, accretion and mergers

- Assess compatibility between electromagnetic observations of massive black holes and PTA GW spectrum running full Bayesian analysis, and obtain posterior on the 12 parameters of POMPOCO

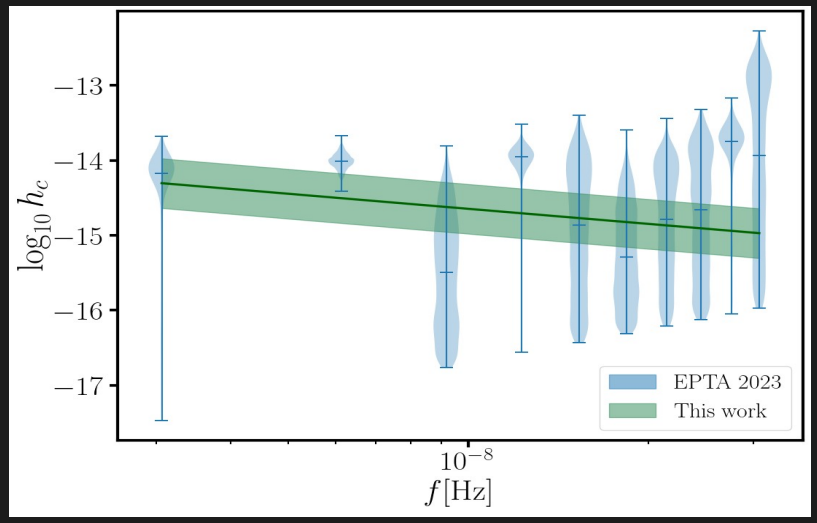
Results of POMPOCO



MBH luminosity distribution in the nearby Universe



MBH luminosity distribution in the distant Universe (JWST)

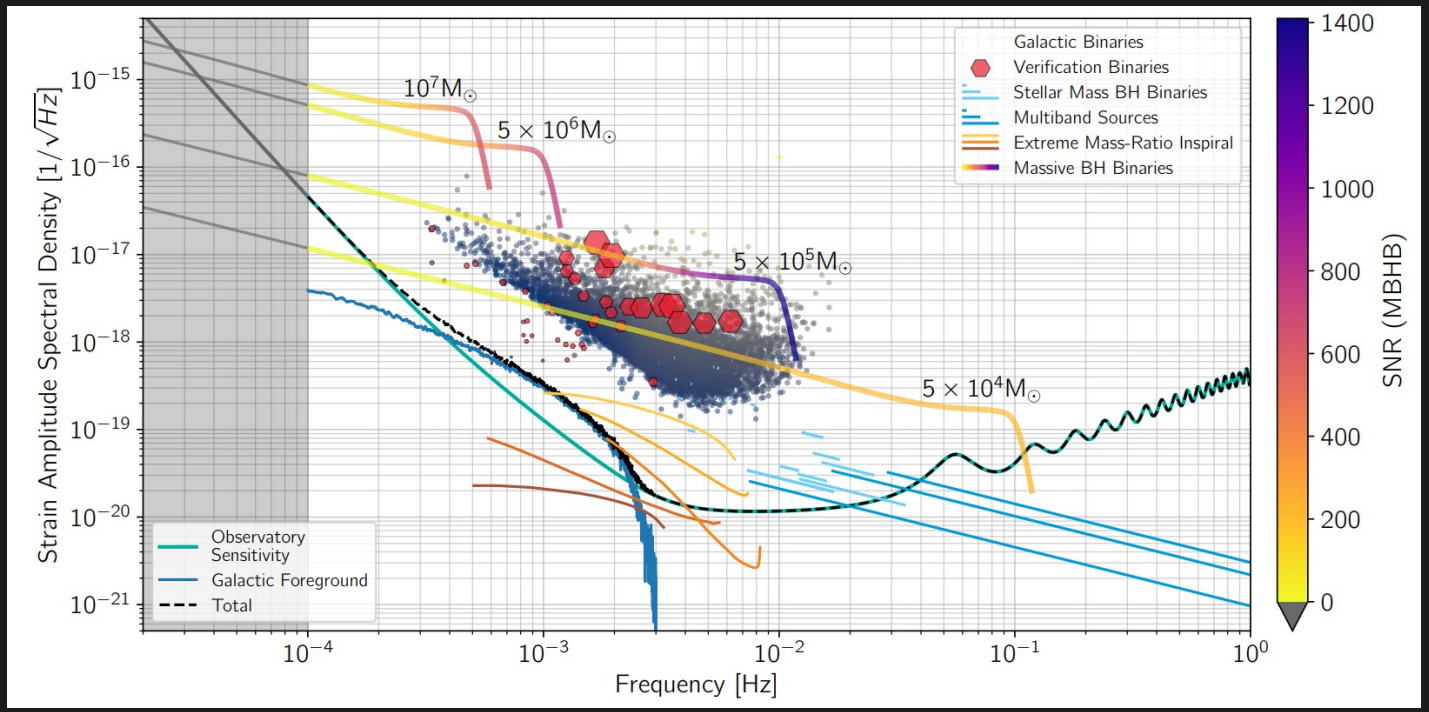


Pulsar Timing Array spectrum

Next:

- Include spins/eccentricity
- Mock LISA analysis

Double white dwarfs



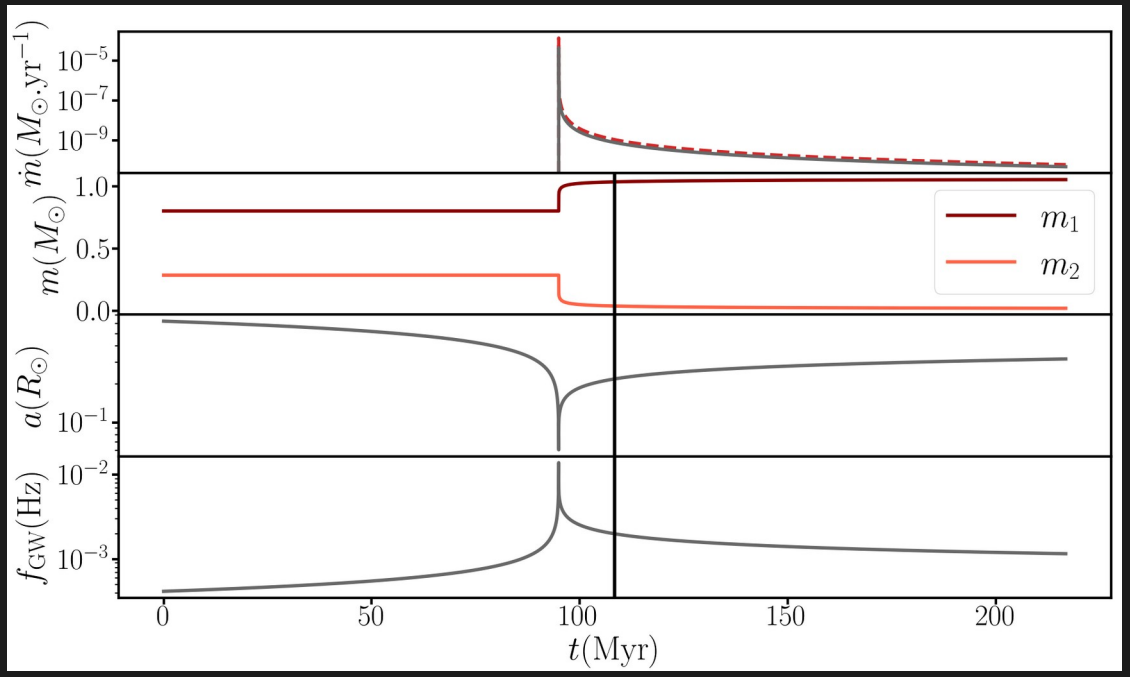
LISA Redbook, 2024

- Stochastic foreground + resolvable population
- Impact of tidal effects and mass transfer?

  Toubiana, Karnesis, Lamberts, Miller A&A 2024

Evolution of double white dwarfs

- Semi-analytic model for the evolution of DWDs after formation (provided by Astrid's simulation)
- Includes the effect of GWs, tides, mass-transfer



Mass-transfer rate

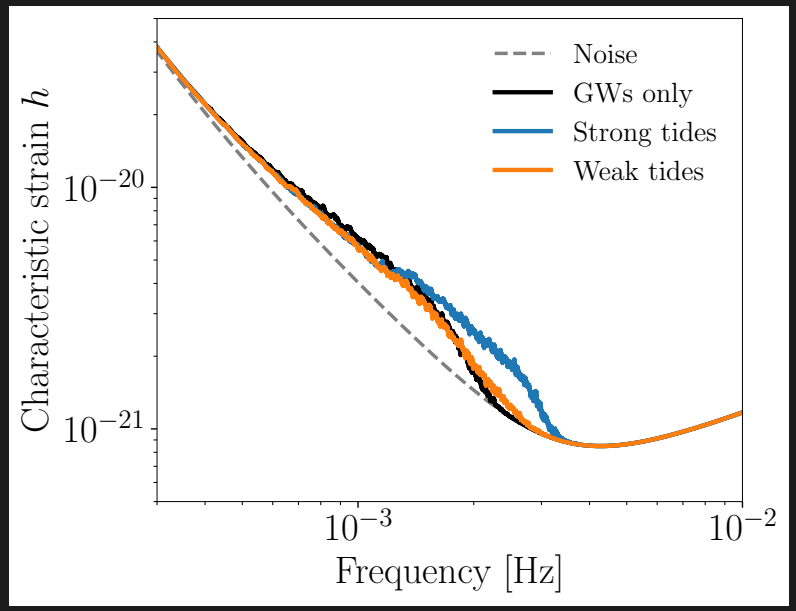
Masses evolution

Separation evolution

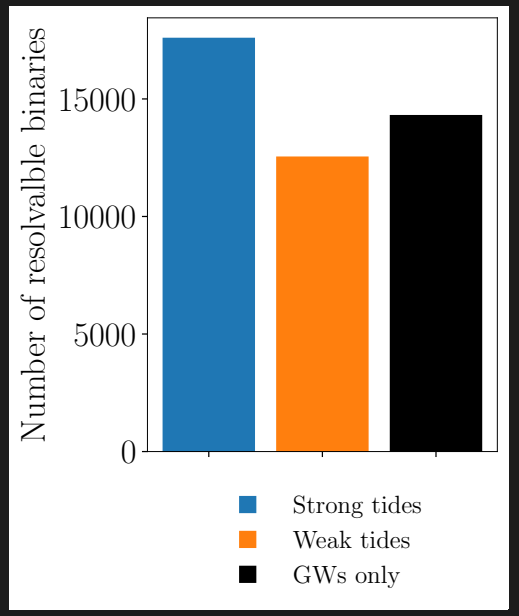
GW frequency evolution

- Tides help the binaries "survive" mass transfer

Impact on LISA observations



Total noise

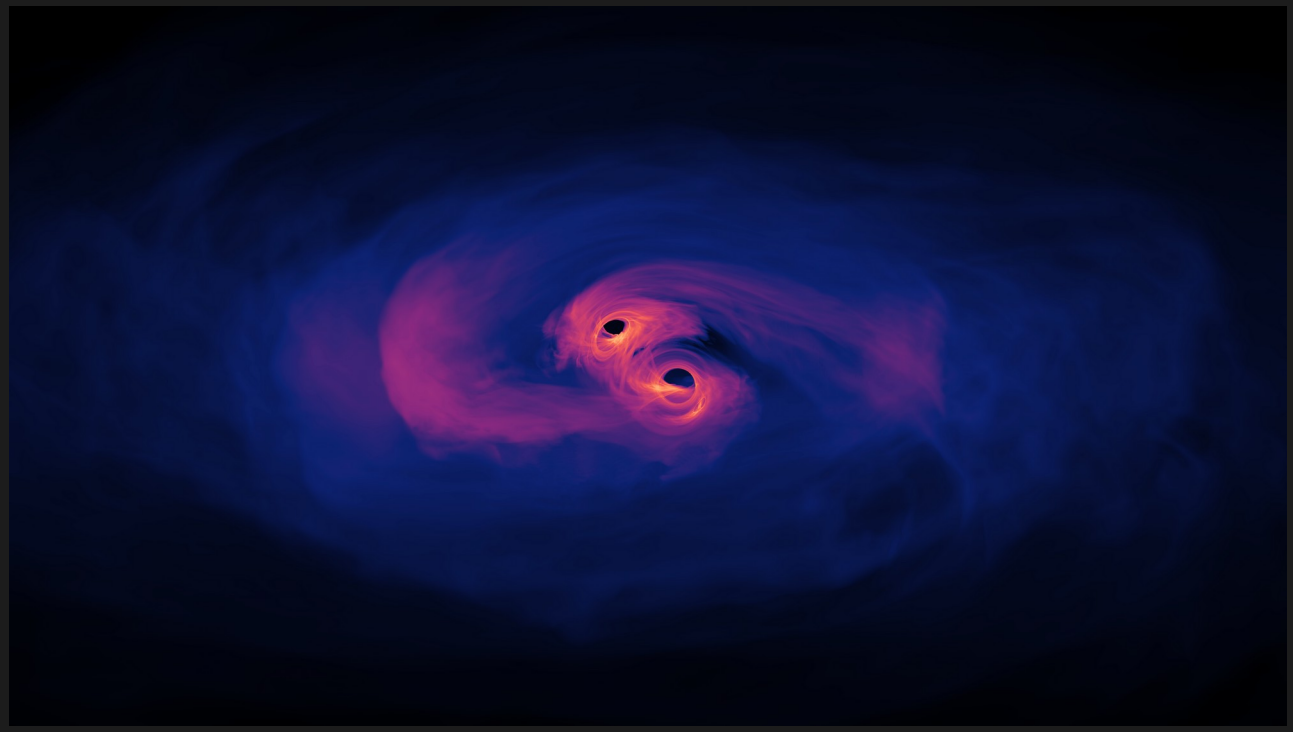


Number of resolvable sources

- Foreground can be used to measure intensity of tidal effects (Santini, Toubiana, Karnesis, on going)
- Combine foreground and resolvable sources for population study (Toubiana, Gair, on going):
  - inverse-mapping from foreground to underlying population?
  - “Selection function”?
  - confusion between populations?

Conclusions

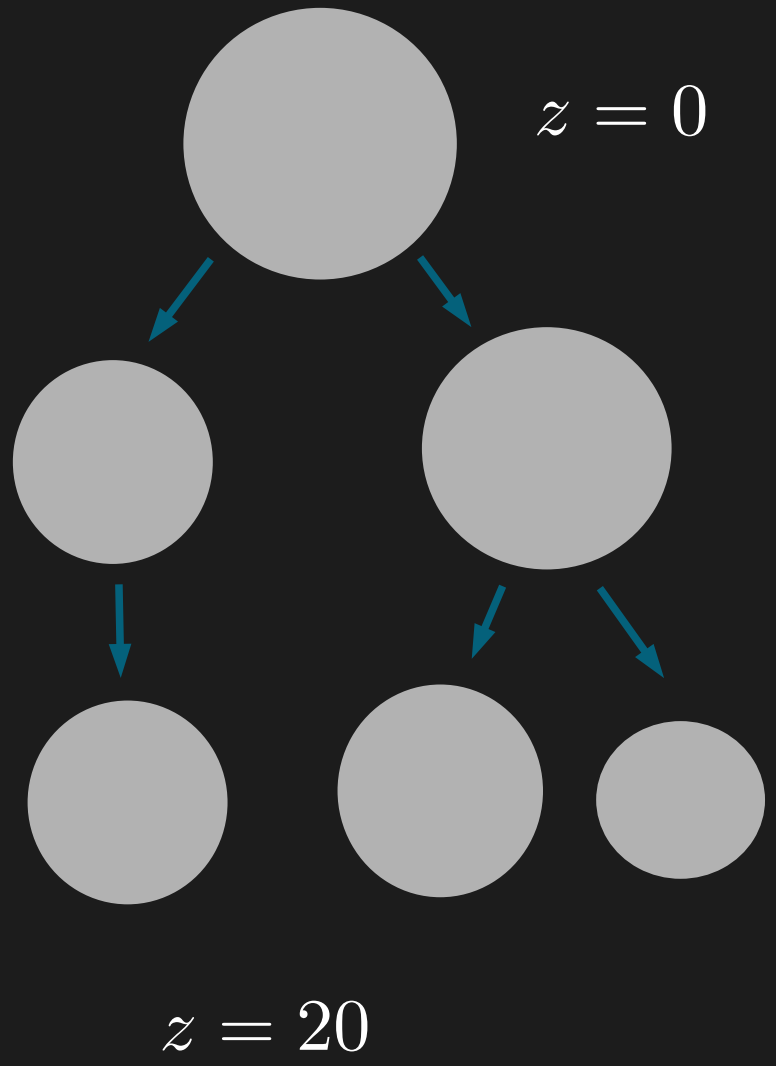
- “New” and numerous sources in LISA require new modelling and analysis techniques. Many challenges to be tackled!



Thank you for your attention!

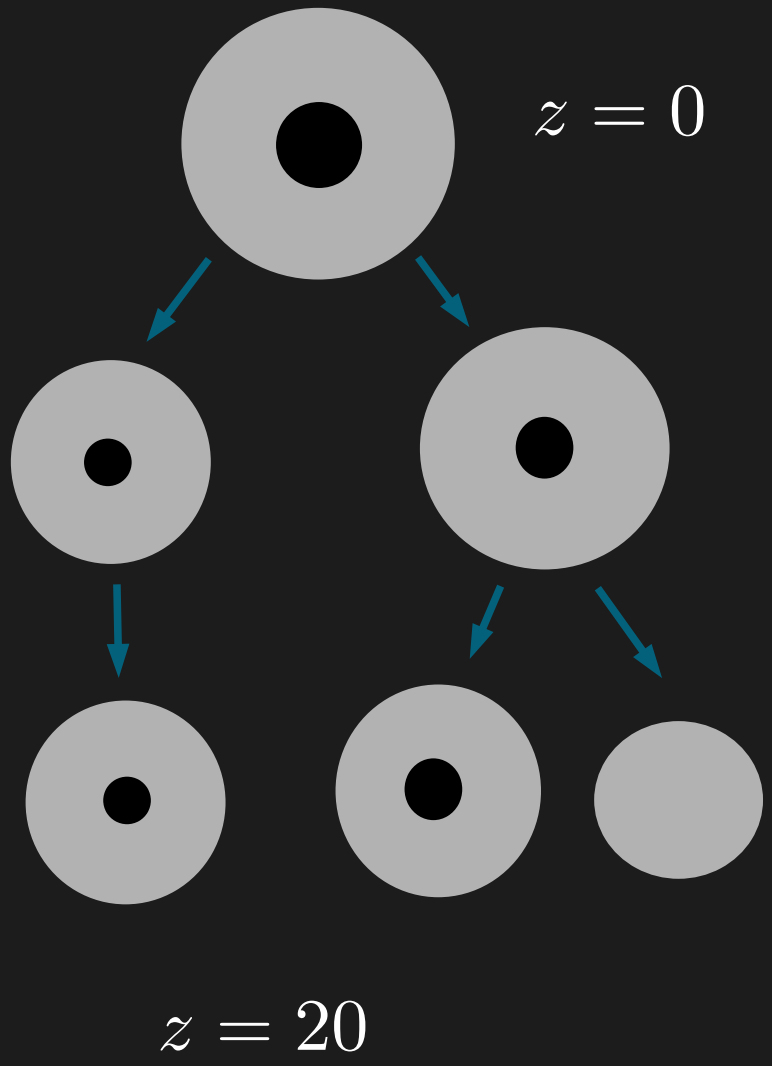
Merger tree

- Extended Press-Schechter (Parkison+2007)



Merger tree

- Extended Press-Schechter (Parkison+2007)
- Evolve MBHs using parametric prescriptions instead of semi-analytic ones
- Gain in computational power



Seeding

- Seed leaf halos at $z \geq 10$ with $M_{\mathrm{halo}} > M_{\mathrm{cut}}$ with probability f_{BH}

- Draw mass from log-normal distribution

$$\mathcal{N}(\log(\mu_0), \sigma_m)$$

- Limit to 10% of baryonic mass of halo

Accretion

$$\dot{m} = f_{\rm Edd}(1-\epsilon)\dot{m}_{\rm Edd},\ \epsilon = 0.1$$

- Two accretion modes:
  - steady mode: draw $f_{\rm Edd}$ every $T_{\rm steady}$

$$p(\log_{10} T_{\rm steady}) = \mathcal{U}[10^{-3}, 0.5]{\rm Gyr}$$

$$p(f_{\rm Edd}) \propto f_{\rm Edd}^{\gamma_{\rm steady}-1}, f_{\rm Edd} \in [10^{-4}, 1]$$

  - burst mode: draw $f_{\rm Edd}$ after major halo merger ($q_h > 0.13$), valid for time $t_{\rm burst}$

$$p(f_{\rm Edd}) \propto f_{\rm Edd}^{\gamma_{\rm burst}-1}, f_{\rm Edd} \in [10^{-2}, 10]$$

- Stop accretion for $z < z_{\rm cut}$, and

$$\log_{10} m_{\rm MBH} > \log_{10} m_{\rm MBH,0}(1+z)^{\alpha}$$

BH mergers

Following halo mergers:

- If major halo merger, ($q_h > 0.13$) black holes form a binary that merges after $t_{\mathrm{dyn.\ fric.}} + t_{\mathrm{delay}}$
- If minor halo merger, BHs in secondary halo sink for $t_{\mathrm{dyn.\ fric.}}$ before forming a binary that merges within t_{delay}

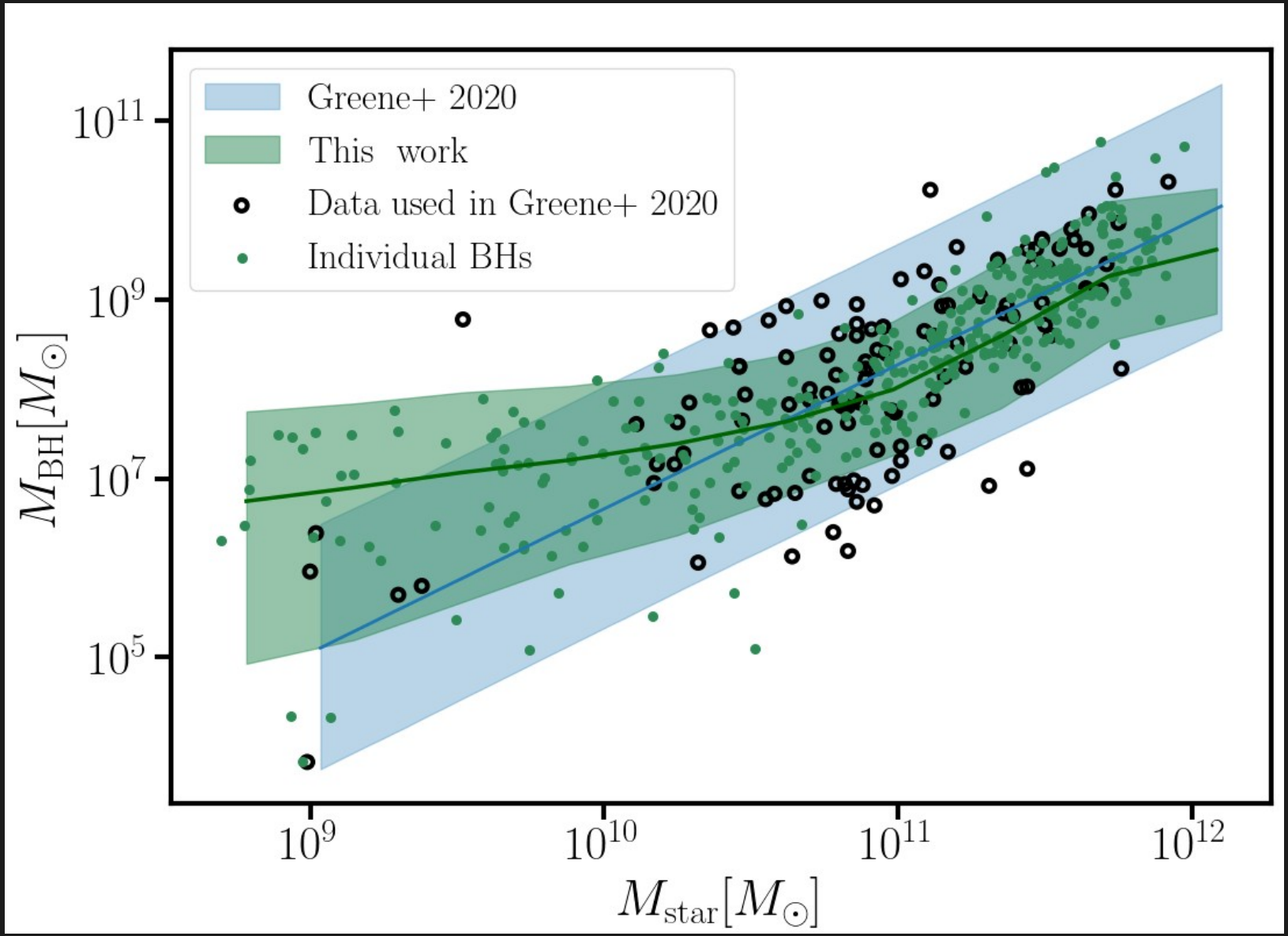
- $t_{\mathrm{dyn.\ fric.}}$ computed from Volonteri et al. 2003
- For triple/quadruple systems use results of Bonetti et al. 2018

Summary of the model

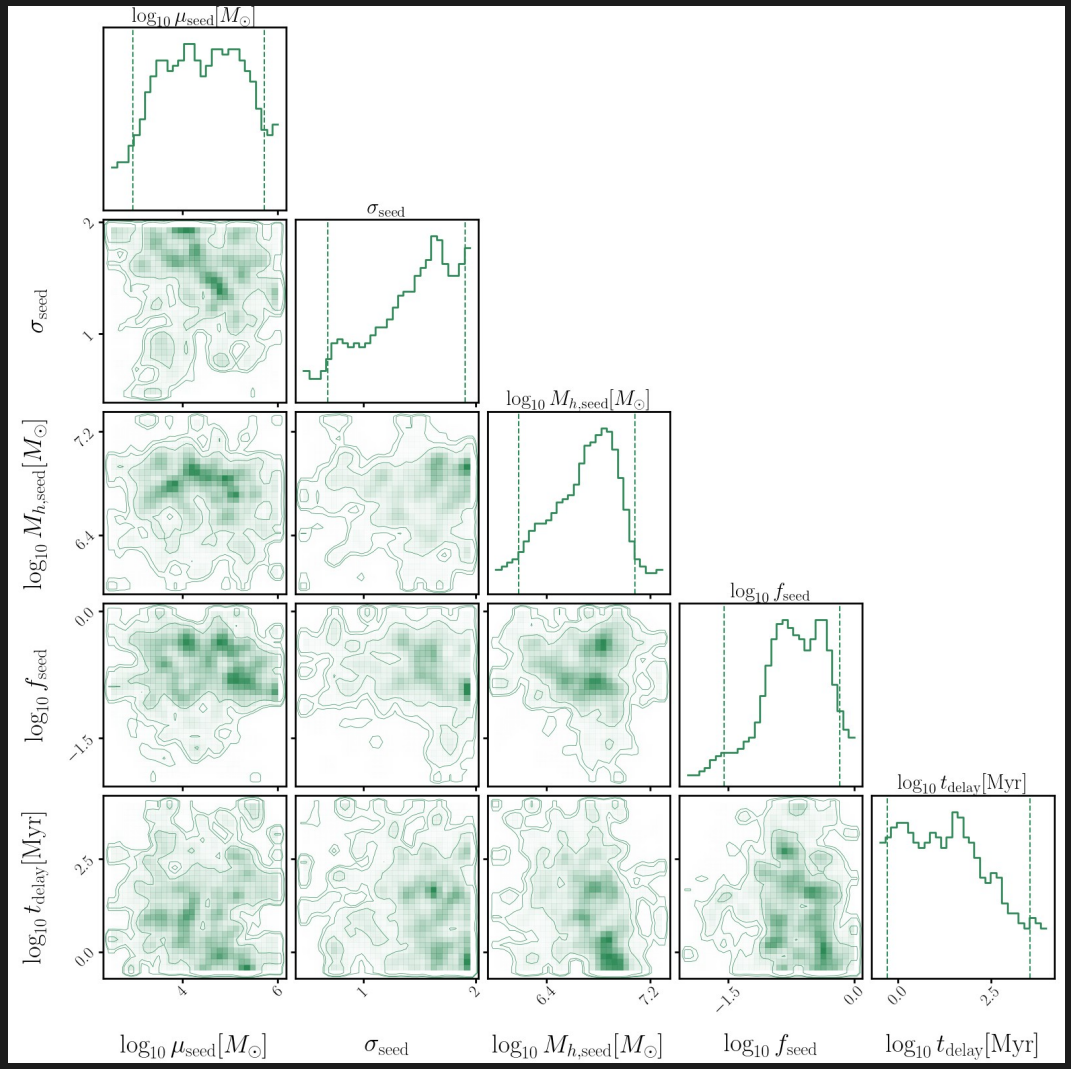
- 12 free parameters:
  - seeding:
    $$\mu_{\rm seed},\ \sigma_{\rm seed},\ M_{h,{\rm seed}},\ f_{\rm seed}$$
  - accretion:
    $$\gamma_{\rm burst},\ t_{\rm burst},\ \mu_{\rm steady},\ \sigma_{\rm steady},\ z_{\rm cut}, m_{\rm cut,0},\ \alpha_{\rm cut}$$
  - Merger: $t_{\rm delay}$

- ~1h to run 500 parameters
- Run MCMC to fit observations

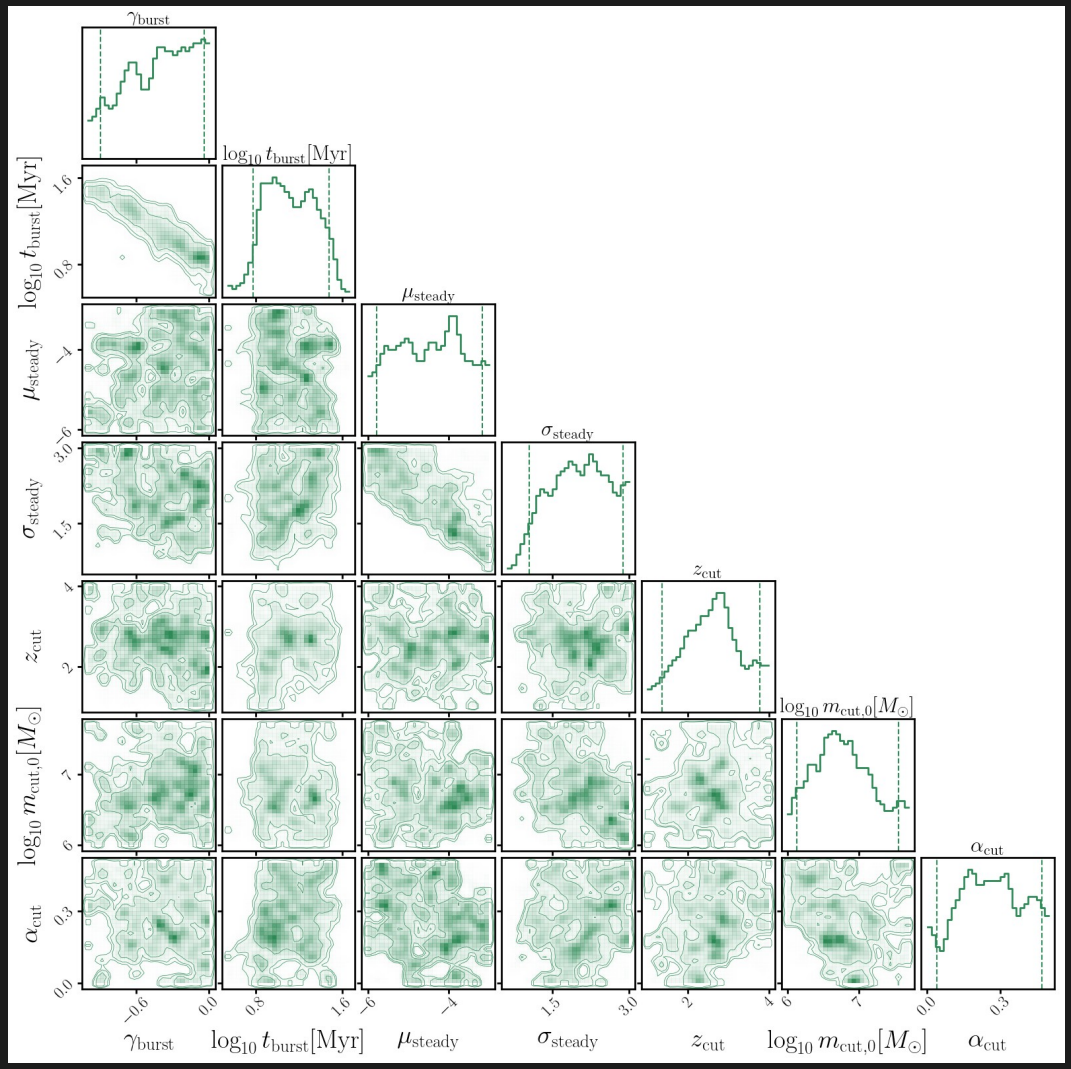
Mstar-Mbh


Greene+ 2020
This work
Data used in Greene+ 2020
Individual BHs
10^{11}
10^{9}
10^{7}
10^{5}
$M_{\rm BH}[M_\odot]$
10^{9}
10^{10}
10^{11}
10^{12}
$M_{\rm star}[M_\odot]$

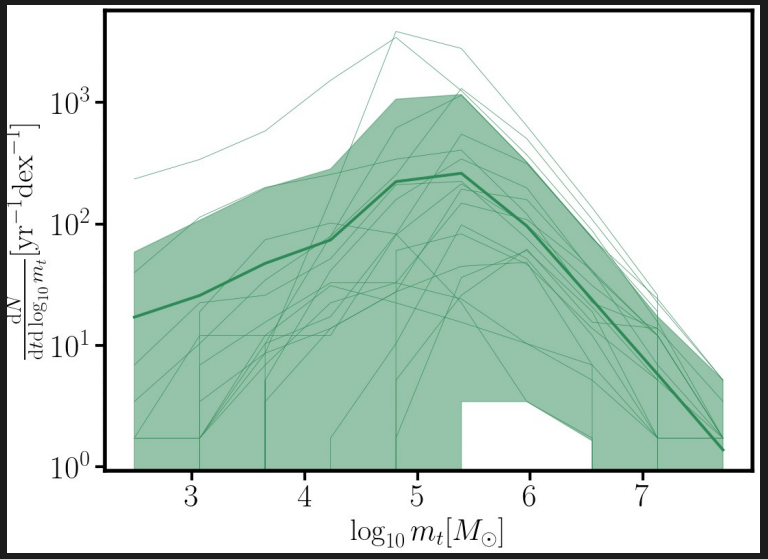
Posterior on hyperparameters

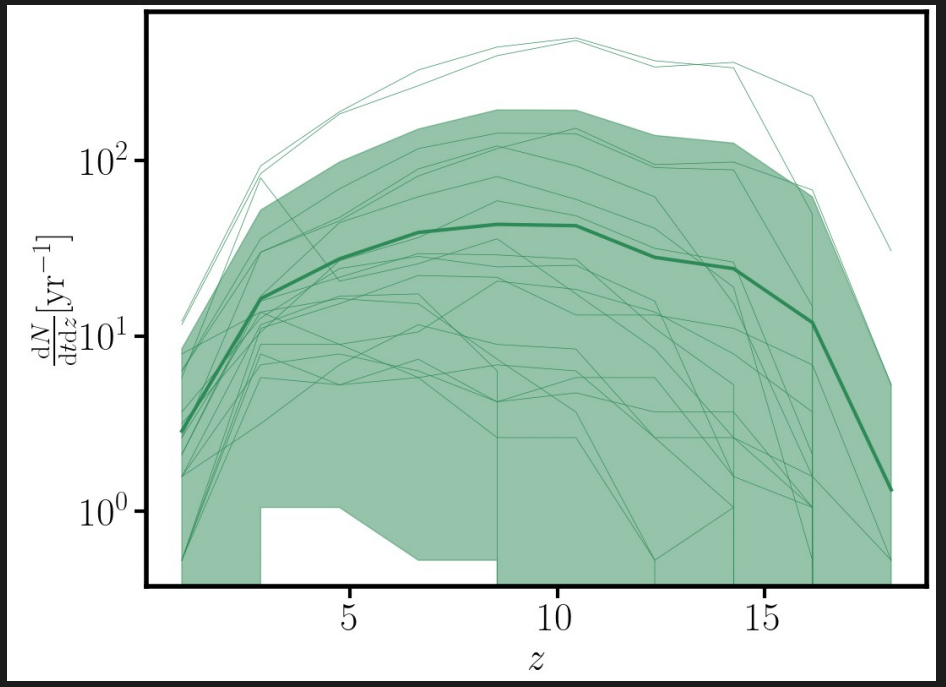


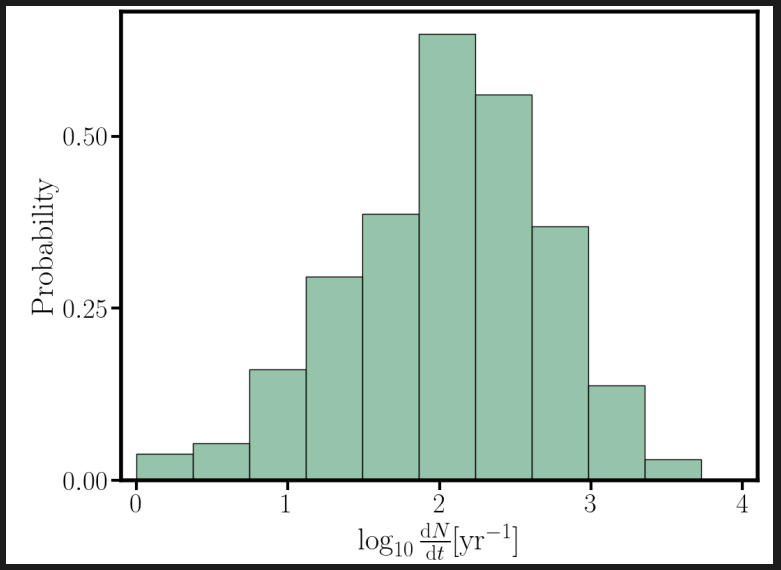
Posterior on hyperparameters



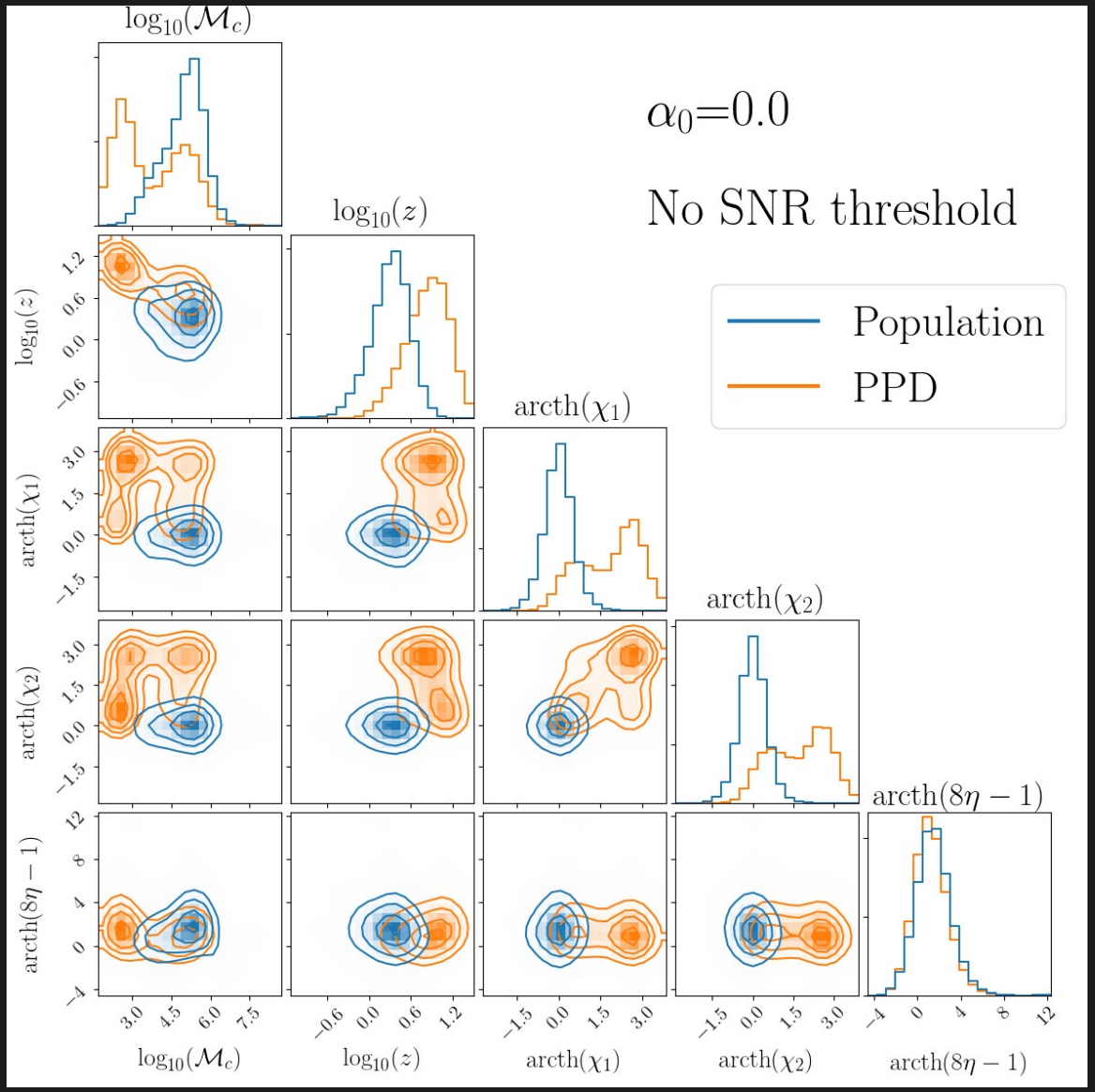
LISA prediction





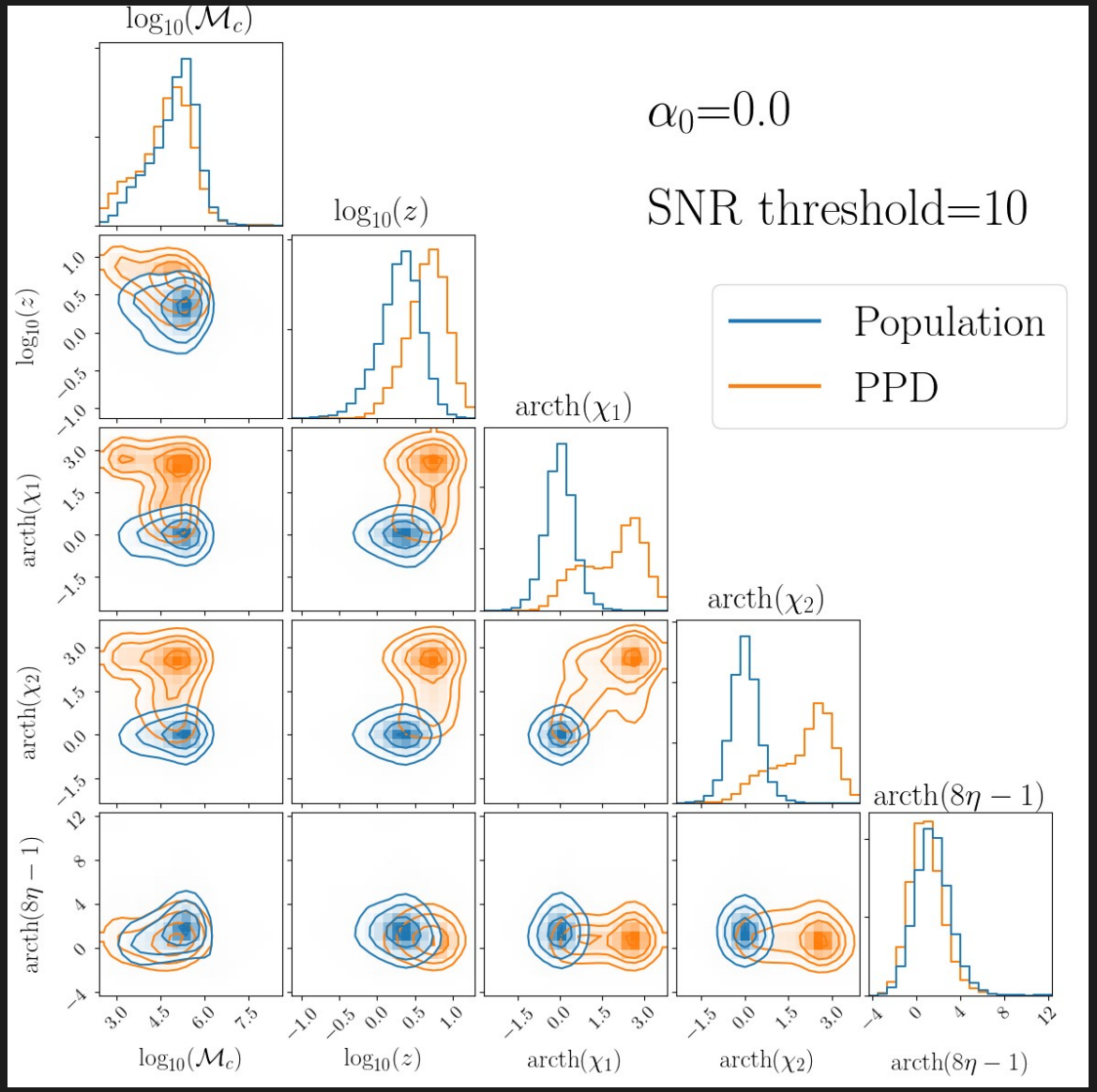


“Systemtatics” in population



Toubiana +, PRD 2021

“Systemtatics” in population



Toubiana +, PRD 2021

POMPOKO

- Pompoco: Parametrisation Of the Massive black hole POpulation for Comparison to Observations ?

Evolution of double white dwarfs

- Angular momentum balance equation:

$$\dot{J_{\rm orb}} + \dot{J}_1 + \dot{J}_2 = \dot{J_{\rm GW}} + \dot{J_{\rm loss}}$$

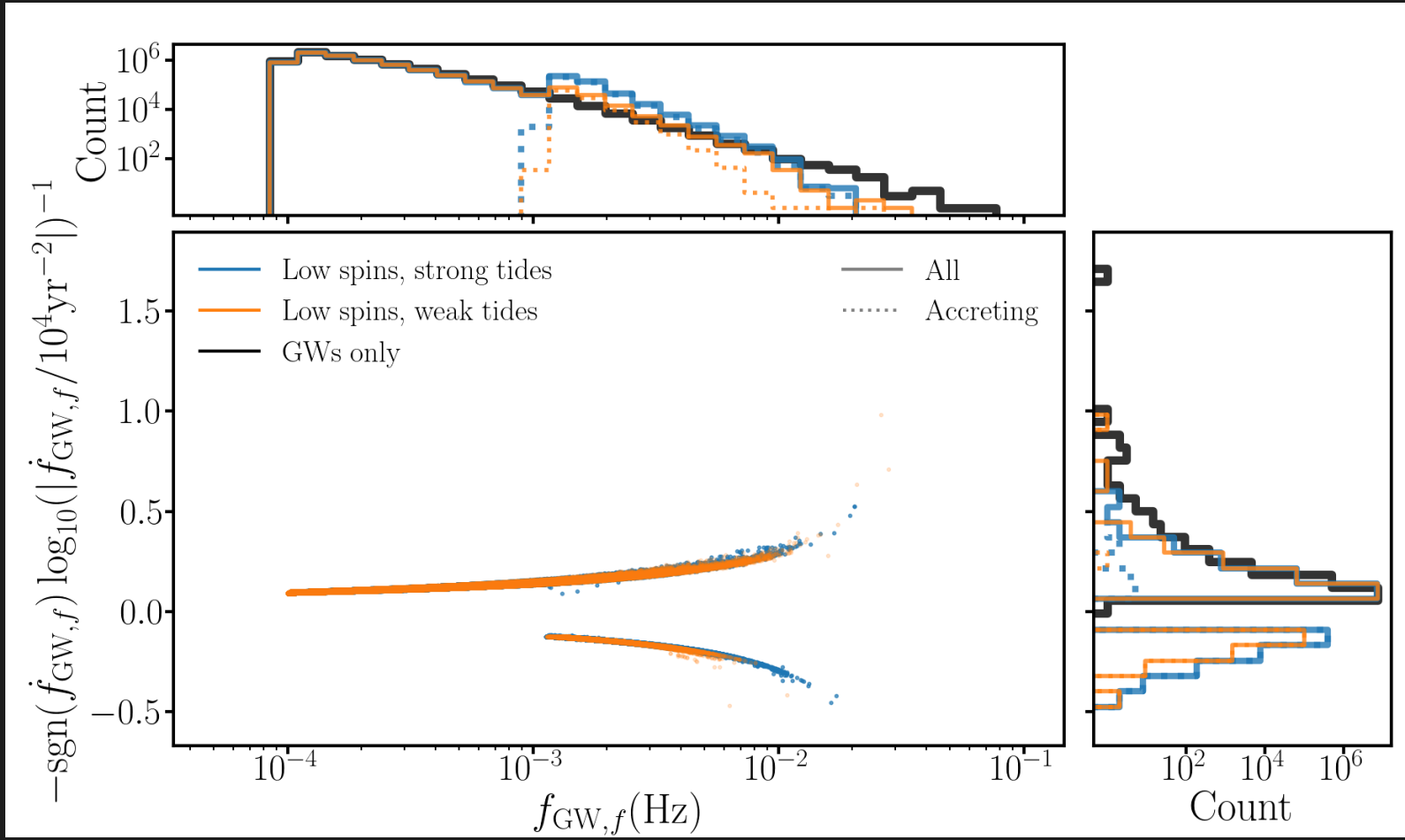
- Evolution of WD's angular momentum:

$$\dot{J}_i = j_i \dot{m}_i - \frac{I_i}{\tau_{s,i}} (\omega_i - \omega_{\rm orb})$$

- Scaling of synchronisation timescale:

$$\tau_{s,i} \propto \left(\frac{m_i}{m_{-i}} \right)^2 \left(\frac{a}{R_i} \right)^6$$

Double white dwarf population



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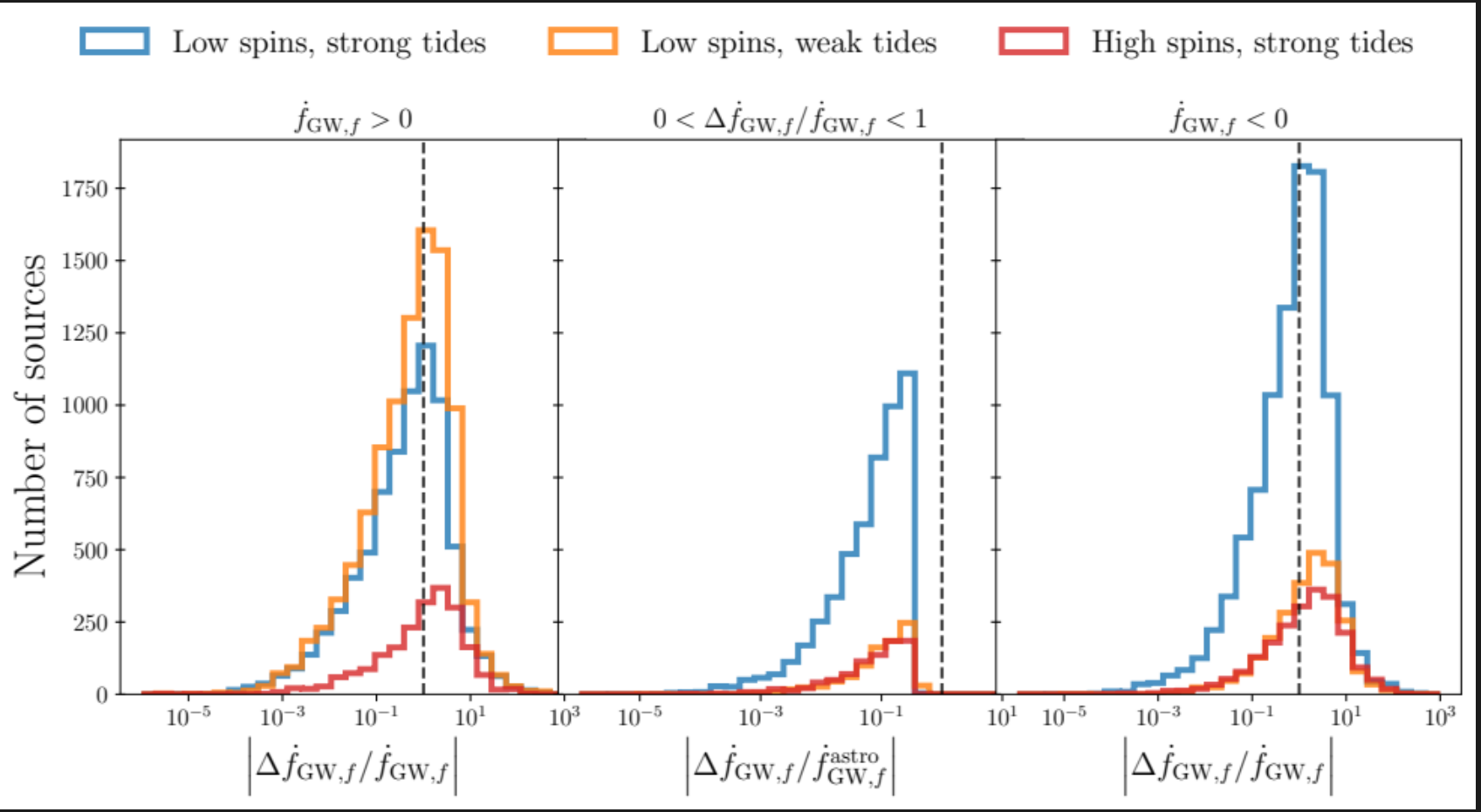

$$\dot{f}^{\mathrm{astro}}_{\mathrm{GW}} = \dot{f}_{\mathrm{GW}} - \dot{f}^{\mathrm{GR}}_{\mathrm{GW}}$$