

# Signatures of Astrophobic QCD axion

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based on:

*JHEP* 06 (2023) 014 [arXiv:2301.09647], MB, K. Harigaya  
arXiv:2403.05621, MB, K. Harigaya, M. Łukawski, R. Ziegler

see also:

*JHEP* 10 (2021) 181 [arXiv:2107.09708], MB, G. Grilli di Cortona, M. Tabet, R. Ziegler

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# Outline

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- QCD axion
- Why astrophobic axion?
- DFSZ-like models with generation-dependent PQ charges
- Naturally astrophobic QCD axion
- Thermal production of astrophobic axions and the impact on CMB

# QCD axion

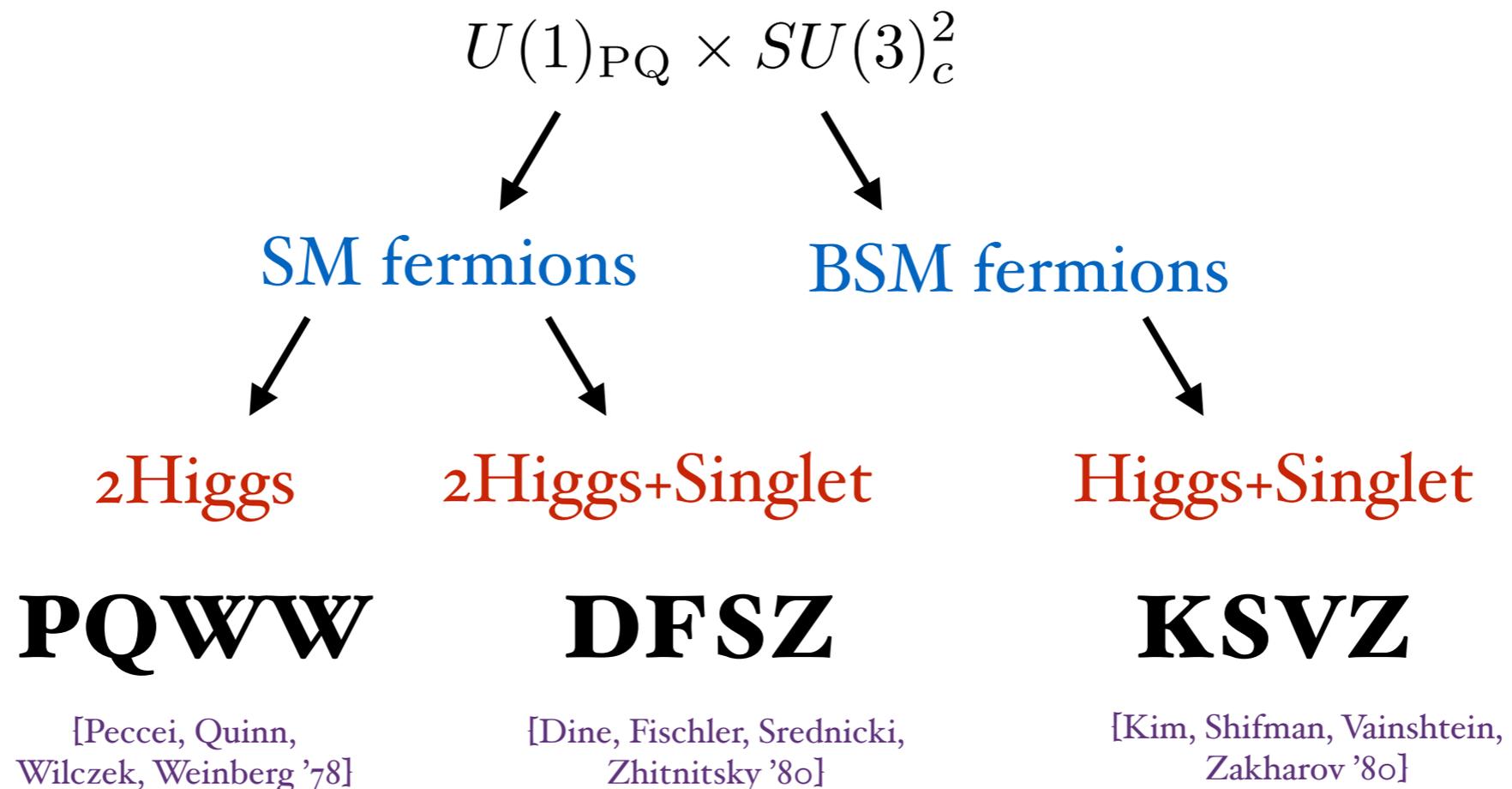
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QCD axion - one of the best candidates for New Physics

- predicted by Peccei-Quinn (PQ) mechanism solving the **strong CP problem**
- constitutes a good **dark matter** candidate
- axion is PNGB of  $U(1)$  PQ symmetry broken by non-perturbative QCD effects

# Axion Models

Need **anomalous** breaking of PQ (**fermion sector**)  
and **spontaneous** PQ breaking (**scalar sector**)



**excluded**

$$J/\psi \rightarrow \gamma a$$

$\langle \text{Singlet} \rangle \gg v$ : “Invisible” axion models

# DFSZ Models

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$$\text{SM fermions} + 2\text{Higgs} + \text{Singlet} \begin{cases} \langle H_1 \rangle = c_\beta v & \langle H_2 \rangle = s_\beta v \\ \langle \Phi \rangle = v_{\text{PQ}} \gg v \end{cases}$$

Construct 2HDM Lagrangian invariant under single U(1)

$$\mathcal{L}_{\text{yuk}} = y_{ij}^u \bar{Q}_i U_j \begin{cases} H_1 \\ H_2 \end{cases} \xrightarrow[\text{U(1) charges}]{\text{flavor-universal}} \begin{matrix} \bar{Q}_i U_j H_1 \\ \bar{Q}_i D_j \tilde{H}_2 \\ \bar{L}_i E_j \tilde{H}_{1 \text{ or } 2} \end{matrix}$$

Break residual U(1) by H-Singlet couplings  $\mathcal{L} \sim H_1^\dagger H_2 \Phi$

Axion fermion couplings fixed by  $\tan \beta$

# Axion effective Lagrangian

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- UV models can be described by effective Lagrangian well below the PQ scale

$$\mathcal{L} = \frac{a}{f_a} \frac{\alpha_s}{8\pi} G\tilde{G} + \frac{E}{N} \frac{a}{f_a} \frac{\alpha_{\text{em}}}{8\pi} F\tilde{F} + \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (C_{ij}^V + C_{ij}^A \gamma_5) f_j$$

solves strong CP problem  
and generates axion mass:

$$m_a \approx 6 \text{ meV} \left( \frac{10^9 \text{ GeV}}{f_a} \right)$$

axion photon couplings  
allowing to search for  
axions in helioscopes  
e.g. IAXO

axion fermion couplings  
(in general flavor-violating)

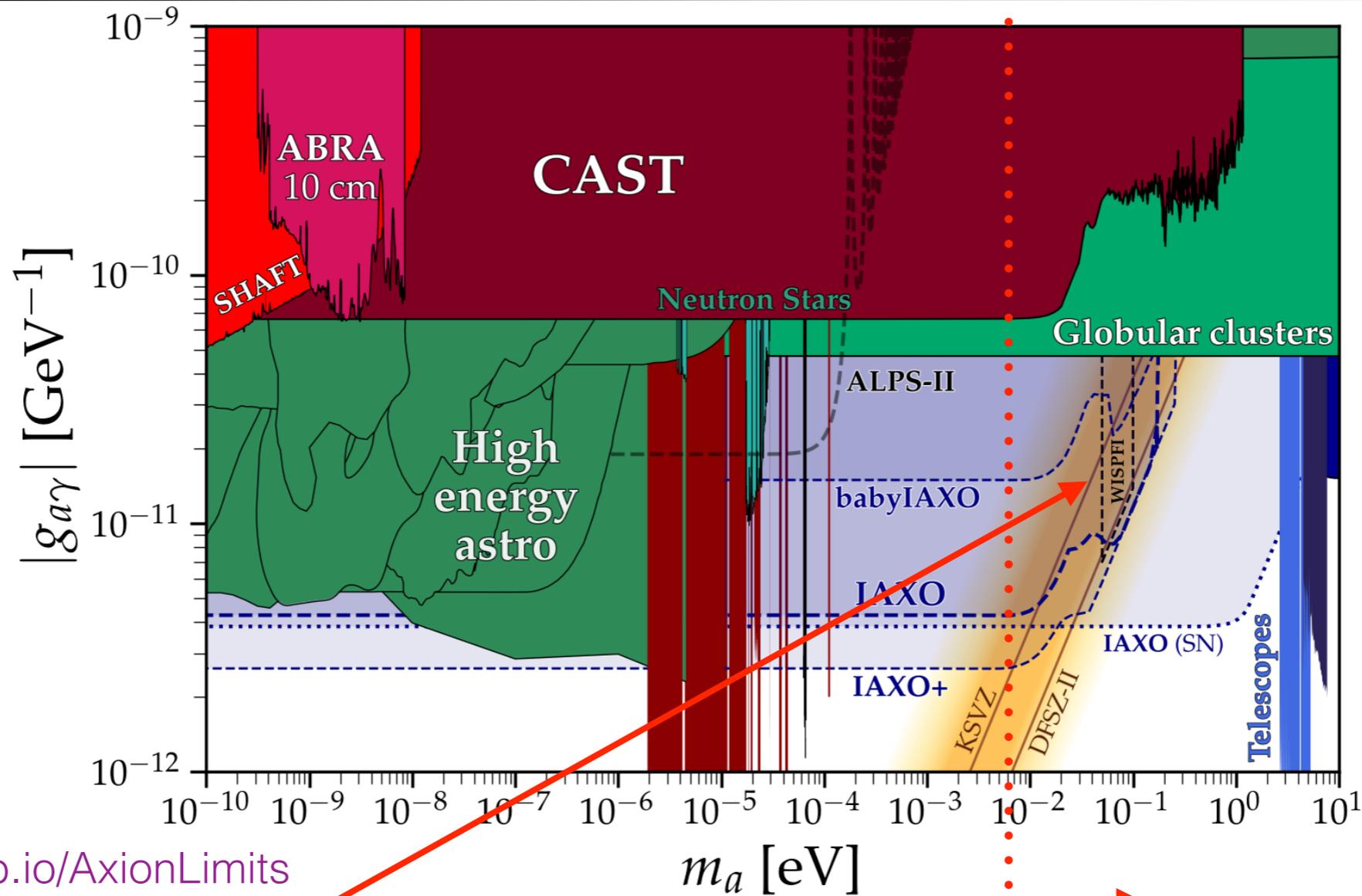
Axion decay constant controls the size  
of axion couplings to SM particles

# Astrophysical constraints on axions

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- Astrophysics provides the strongest lower bounds on the axion decay constant
- Light axions efficiently cool neutron stars via axion bremsstrahlung off nucleons  $N + N \rightarrow N + N + a$
- Neutron star cooling and constraints from SN1987A set lower bound on  $f_a \gtrsim \mathcal{O}(10^9)$  GeV in minimal axion models
- Cooling rate of White Dwarfs constrains axion-electron coupling  $f_a/C_e \gtrsim 3 \times 10^9$  GeV

# Detecting axions in helioscopes



[cajohare.github.io/AxionLimits](https://cajohare.github.io/AxionLimits)

Large axion-photon couplings excluded  $\therefore f_a < 10^9$  GeV  
by astrophysics in minimal models

No signal expected at IAXO unless axion is astrophobic

# Other motivations for astrophobic axions

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- **Stellar cooling hints**

Excessive energy losses have been observed in several stellar environments e.g. anomalous cooling of White

Dwarfs -> axion explanation typically prefers  $f_a \lesssim 10^9$  GeV

[Giannotti, Irastorza, Redondo, Ringwald '16]  
[MB, Grilli di Cortona, Tabet, Ziegler '21]

- **Axiogenesis**

[Co, Harigaya '19]

Baryon asymmetry and dark matter abundance can be explained by axion rotation. Minimal models predict

$$f_a \in (10^6, 10^7) \text{ GeV}$$

# Nucleophobic axion models

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[Di Luzio, Mescia, Nardi, Panci, Ziegler '17]

- SN1987A and NS bounds can be relaxed if axion nucleon coupling is suppressed which happens for

$$C_u + C_d = 1$$

$$C_u \approx 2/3$$

$$C_i \equiv C_{ii}^A$$

- Nucleophobia realised in **DFSZ**-like models with **non-universal** PQ charges

**Nucleophobia  $\Rightarrow$  flavor-violating axion couplings!**

# Nucleophobic Non-universal DFSZ models

Generalized DFSZ-type models:  
**PQ charges universal only for two generations**

Have non-trivial transition to mass basis

$$X_f = \text{diag}(X_1, X_1, X_3) \rightarrow V_f^\dagger X_f V_f = X_1 \delta_{ij} + (X_3 - X_1) \xi_{ij}^f$$

$$\xi_{ij}^f \equiv (V_f)_{i3}^* (V_f)_{j3} \quad f = u_L, u_R, d_L, d_R, e_L, e_R$$

Generically flavor-violating axion couplings  
depend on 2 misalignment parameters in each sector

$$0 \leq \xi_{ii}^f \leq 1 \quad \sum_i \xi_{ii}^f = 1 \quad |\xi_{ij}^f| = \sqrt{\xi_{ii}^f \xi_{jj}^f}$$

$$C_{ii}^f = X_1 + (X_3 - X_1) \xi_{ii}^f \quad |C_{i \neq j}^f| = |X_3 - X_1| |\xi_{ij}^f|$$

# Non-universal DFSZ 2HDM models

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There are 4 nucleophobic charge assignments in the quark sector: non-universal in q **or** u/d sector

e.g.  $\mathcal{L} \sim \frac{\bar{f}_{L3} f_{R3}}{\bar{f}_{L3} f_{Ra}} \begin{cases} h_1 & u \\ \tilde{h}_2 & d \end{cases} + \frac{\bar{f}_{La} f_{Rb}}{\bar{f}_{La} f_{R3}} \begin{cases} h_2 & u \\ \tilde{h}_1 & d \end{cases}$

Each model in the quark sector can be combined with 4 models in the charged lepton sector

16 nucleophobic models in total

Model	$E_Q/N$	$C_{u_i u_i}^A$	$C_{d_i d_i}^A$	$C_{u_i \neq u_j}^{V,A}$	$C_{d_i \neq d_j}^{V,A}$
Q1	$2/3 + 6c_\beta^2$	$c_\beta^2$	$\xi_{ii}^{dR} - c_\beta^2$	0	$\xi_{ij}^{dR}$
Q2	$-4/3 + 6c_\beta^2$	$c_\beta^2 - \xi_{ii}^{uL}$	$-\xi_{ii}^{dL} + s_\beta^2$	$\pm \xi_{ij}^{uL}$	$\pm \xi_{ij}^{dL}$
Q3	$-4/3 + 6c_\beta^2$	$c_\beta^2 - \xi_{ii}^{uR}$	$-\xi_{ii}^{dR} + s_\beta^2$	$-\xi_{ij}^{uR}$	$-\xi_{ij}^{dR}$
Q4	$-10/3 + 6c_\beta^2$	$-s_\beta^2 + \xi_{ii}^{uR}$	$s_\beta^2$	$\xi_{ij}^{uR}$	0

Model	$E_L/N$	$C_{e_i e_i}^A$	$C_{e_i \neq e_j}^{V,A}$
E1L	$2 - 6c_\beta^2$	$-c_\beta^2 + \xi_{ii}^{eL}$	$\mp \xi_{ij}^{eL}$
E1R	$2 - 6c_\beta^2$	$-c_\beta^2 + \xi_{ii}^{eR}$	$\xi_{ij}^{eR}$
E2L	$4 - 6c_\beta^2$	$s_\beta^2 - \xi_{ii}^{eL}$	$\pm \xi_{ij}^{eL}$
E2R	$4 - 6c_\beta^2$	$s_\beta^2 - \xi_{ii}^{eR}$	$-\xi_{ij}^{eR}$

# Naturally Astrophobic Axion

[MB, Harigaya '23]

- Non-universal DFSZ-like models with 2 Higgs doublets (2HDM) require tuning of parameters to suppress axion couplings to nucleons and electrons
- Astrophobia can be realised without tuning for a specific PQ charge assignment for the SM fermions:

	$\bar{u}$	$\bar{d}$
$Q_f$	2	1

→  $C_u = 2/3 \quad C_d = 1/3$

axion couplings to nucleons and photons naturally suppressed!

↓  
 $\frac{E}{N} = 2$

$$C_\gamma = E/N - 2.07(4)$$

$$f_a \gtrsim 2 \times 10^7 |C_\gamma| \quad (\text{from horizontal branch stars})$$

# Thermal production of axions

# Thermal axion production

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- Axions have also cosmological signatures
- For small enough  $f_a$  axions can be in thermal equilibrium with the SM plasma
- Thermally produced axions contribute to

$$\Delta N_{\text{eff}} = \frac{8}{7} \left( \frac{11}{4} \right)^{\frac{4}{3}} \frac{\rho_a}{\rho_\gamma} \Big|_{T_{\text{CMB}}}$$

leading to lower bounds on  $f_a$  from the CMB data

# Thermal axion production

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- For instantaneous axion decoupling at  $T_{\text{dec}}$  :

$$\Delta N_{\text{eff}} \approx 0.03 \left( \frac{100}{g_{*s}(T_{\text{dec}})} \right)^{4/3}$$

- Current bound from Planck:  $\Delta N_{\text{eff}} \lesssim 0.3$
- Expected CMB-S4 sensitivity:  $\Delta N_{\text{eff}} \lesssim 0.05$
- $\Delta N_{\text{eff}}$  sizeable if axion decouples during or after QCD phase transition

# Thermal axion production

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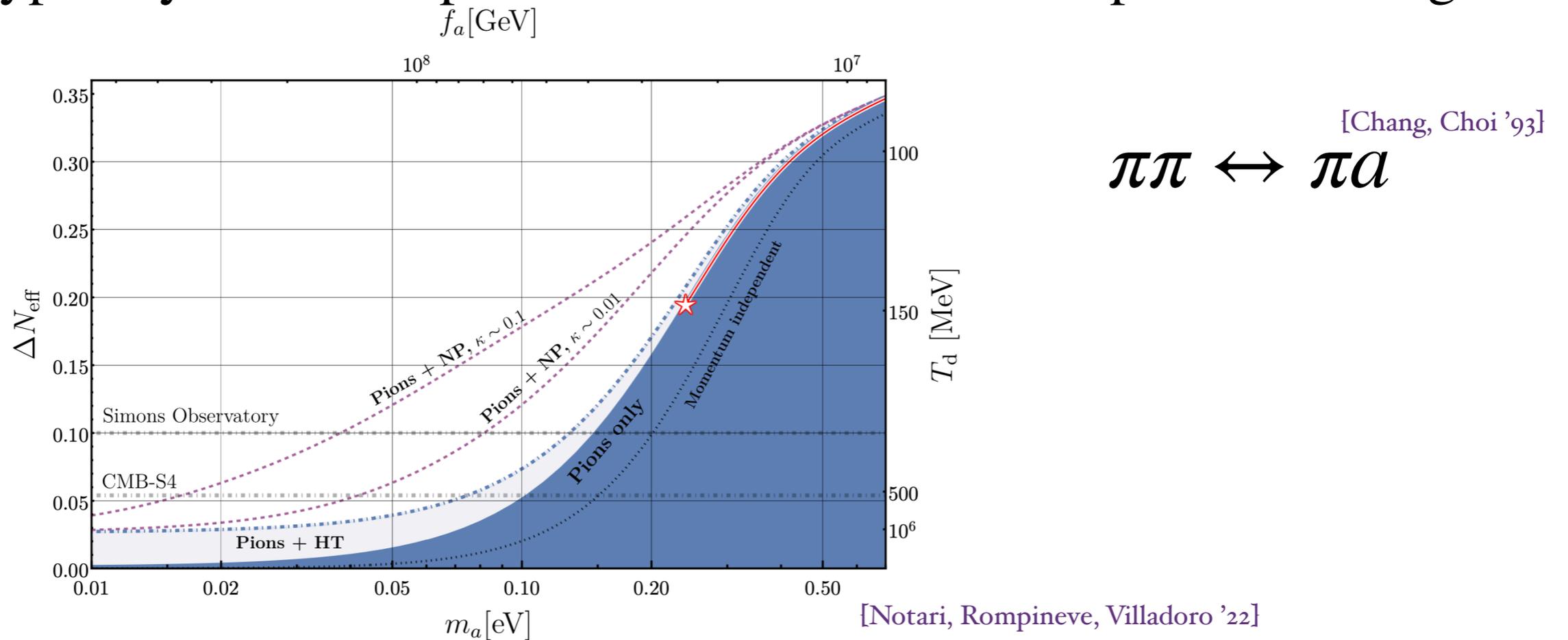
- Around the QCD phase transition  $g_{*s}$  changes rapidly
- Precise determination of  $\Delta N_{\text{eff}}$  requires solving Boltzmann equations (freeze-in also taken into account)

$$\frac{dn_a}{dt} + 3Hn_a = \left( \sum_i \Gamma_i \right) \left( n_a^{\text{eq}} - n_a \right)$$

Thermally averaged axion production rates

# Axion-pion scattering

Typically dominant production channel is axion-pion scattering

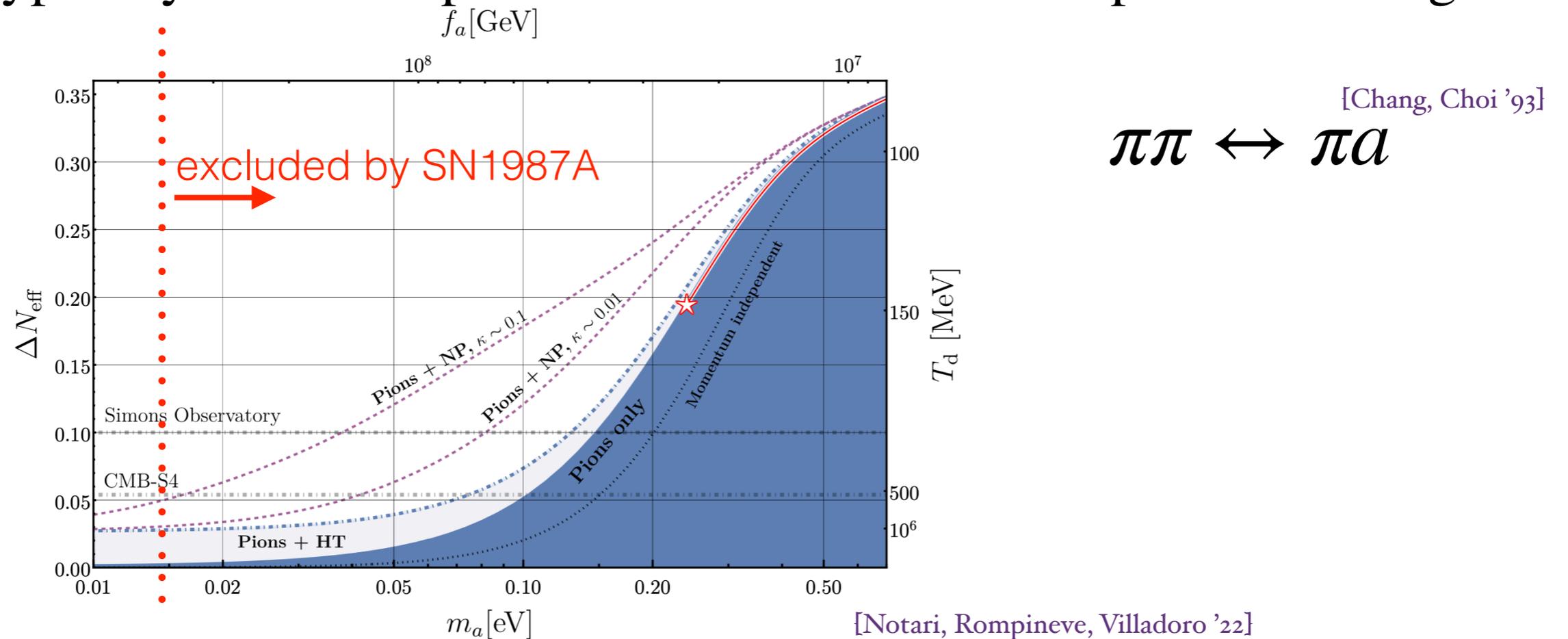


Hot dark matter bound for the KSVZ (hadronic) axion:  
 $m_a \lesssim 0.24 \text{ eV}$  (or  $f_a \gtrsim 2 \times 10^7 \text{ GeV}$ )

Note: **the above bound is highly model dependent!**

# Axion-pion scattering

Typically dominant production channel is axion-pion scattering



The astrophysical bound on  $f_a$  is much stronger than CMB one

Astro bounds on  $f_a$  in the KSVZ model imply negligible  $\Delta N_{\text{eff}}$  beyond the reach of future CMB experiments

# Thermal production of astrophobic axions

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[MB, Harigaya, Łukowski, Ziegler '24]

For astrophobic axions axion-pion scattering is suppressed

$$C_\pi \sim (C_n - C_p) \quad \text{Nucleophobia} \Rightarrow \text{Pionphobia}$$

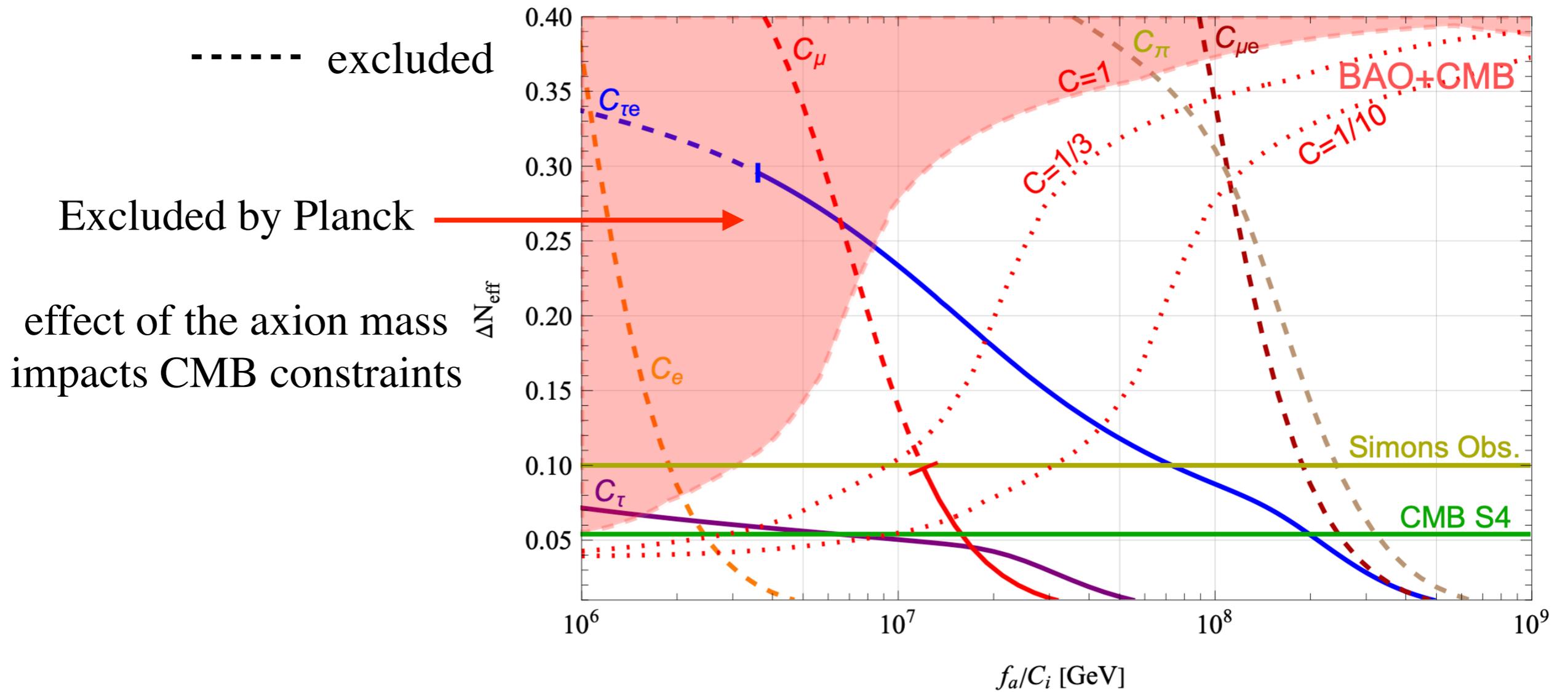
Astrophobic axions thermally produced via:

- flavor-conserving axion-lepton scattering

$$l^\pm \gamma \leftrightarrow l^\pm a \quad l^+ l^- \leftrightarrow \gamma a \quad (l = \mu, \tau)$$

- flavor-violating  $\tau \rightarrow la$  decays ( $l = e, \mu$ )

# $\Delta N_{\text{eff}}$ from dominant channels



For O(1) axion couplings FV  $\tau \rightarrow la$  decays dominate

(bound from Planck is stronger than that from Belle II)

# $\Delta N_{\text{eff}}$ in astrophobic 2HDM models

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DFSZ-like 2HDM models with 2+1 flavor structure of PQ charges:

Nucleophobia+Electrophobia  $\Rightarrow$  LFV axion couplings

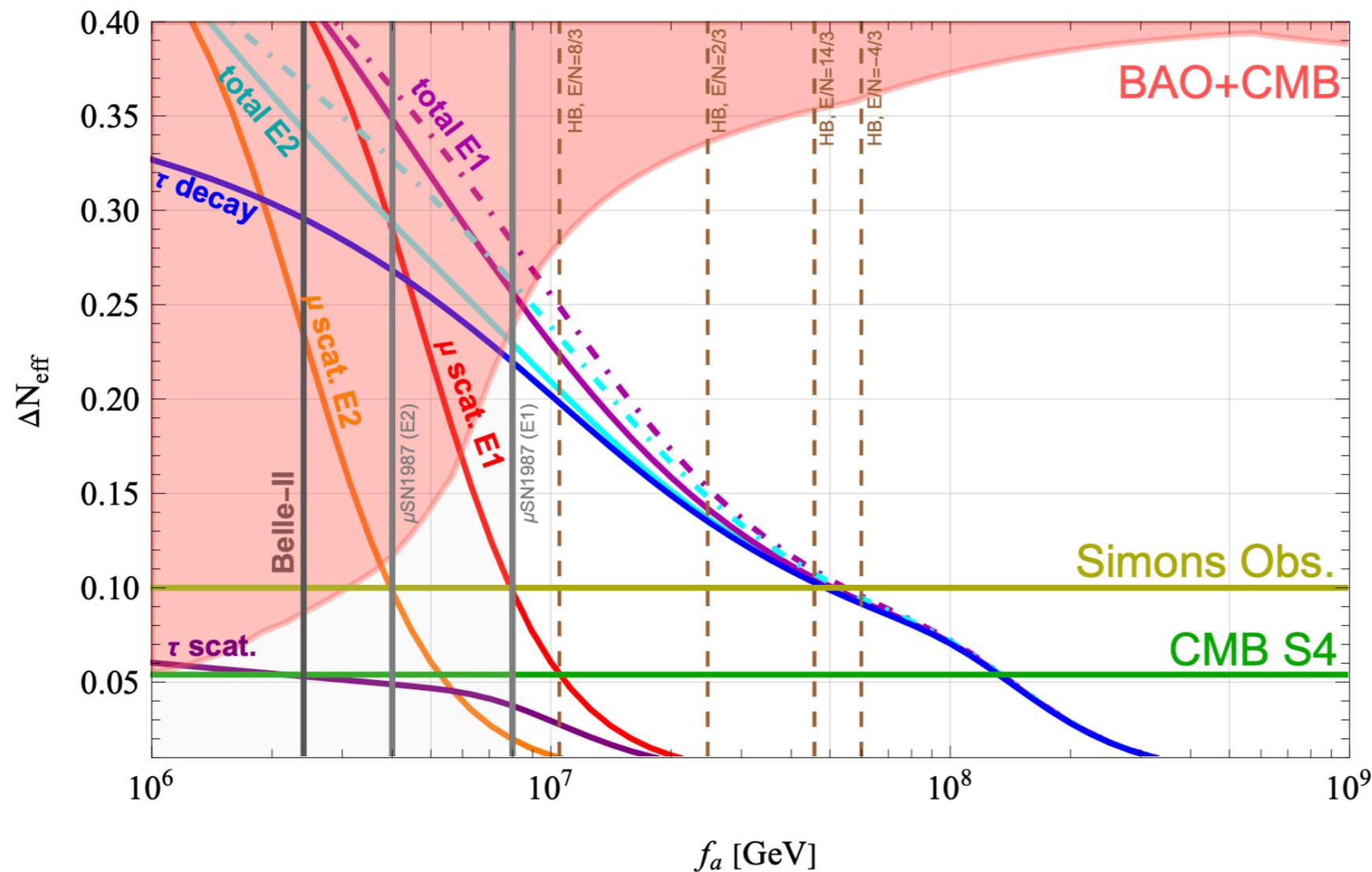
For  $f_a \lesssim 10^8$  GeV all axion couplings in the lepton sector fixed once astro and exp. ( $\mu \rightarrow ea$ ) constraints are imposed:

$$C_{\tau e} \approx \frac{2}{3} \quad C_{\tau} \approx -\frac{1}{3} \quad C_{\mu} \approx -\frac{2}{3} \text{ (or } \frac{1}{3}\text{)}$$

$\Delta N_{\text{eff}}$  predicted as a function of  $f_a$

Astrophobic 2HDM (with different PQ charge assignments for SM fermions) with different predictions for E/N determining the axion-photon coupling

# $\Delta N_{\text{eff}}$ in astrophobic 2HDM models



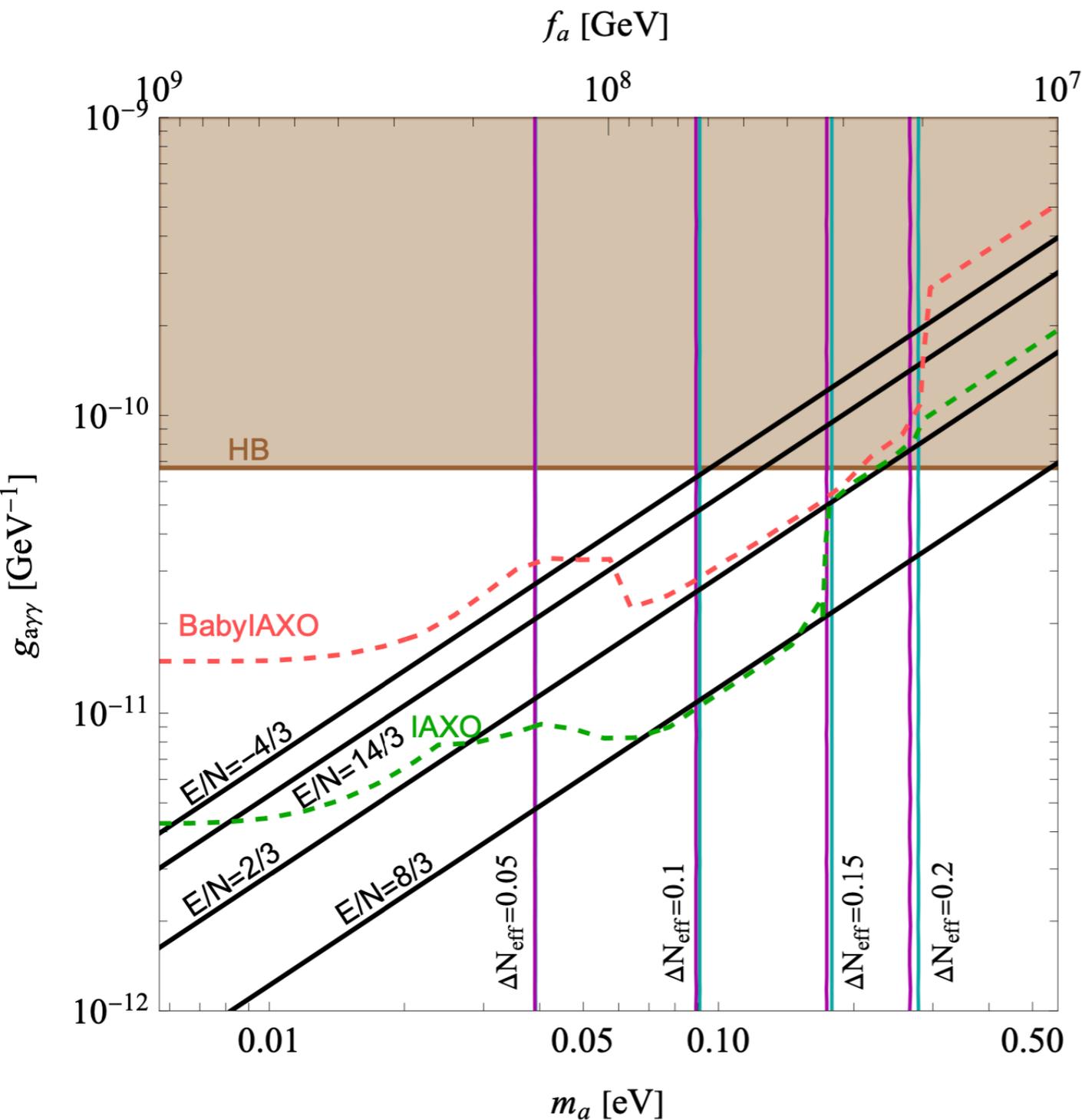
$$C_\mu \approx -\frac{2}{3} \quad (\text{E1})$$

$$C_\mu \approx \frac{1}{3} \quad (\text{E2})$$

$\Delta N_{\text{eff}}$  as large as 0.25 consistent with astro constraints

Good prospects for discovery at future CMB exp. for  $f_a$  up to  $10^8$  GeV

# Complementarity of IAXO and CMB

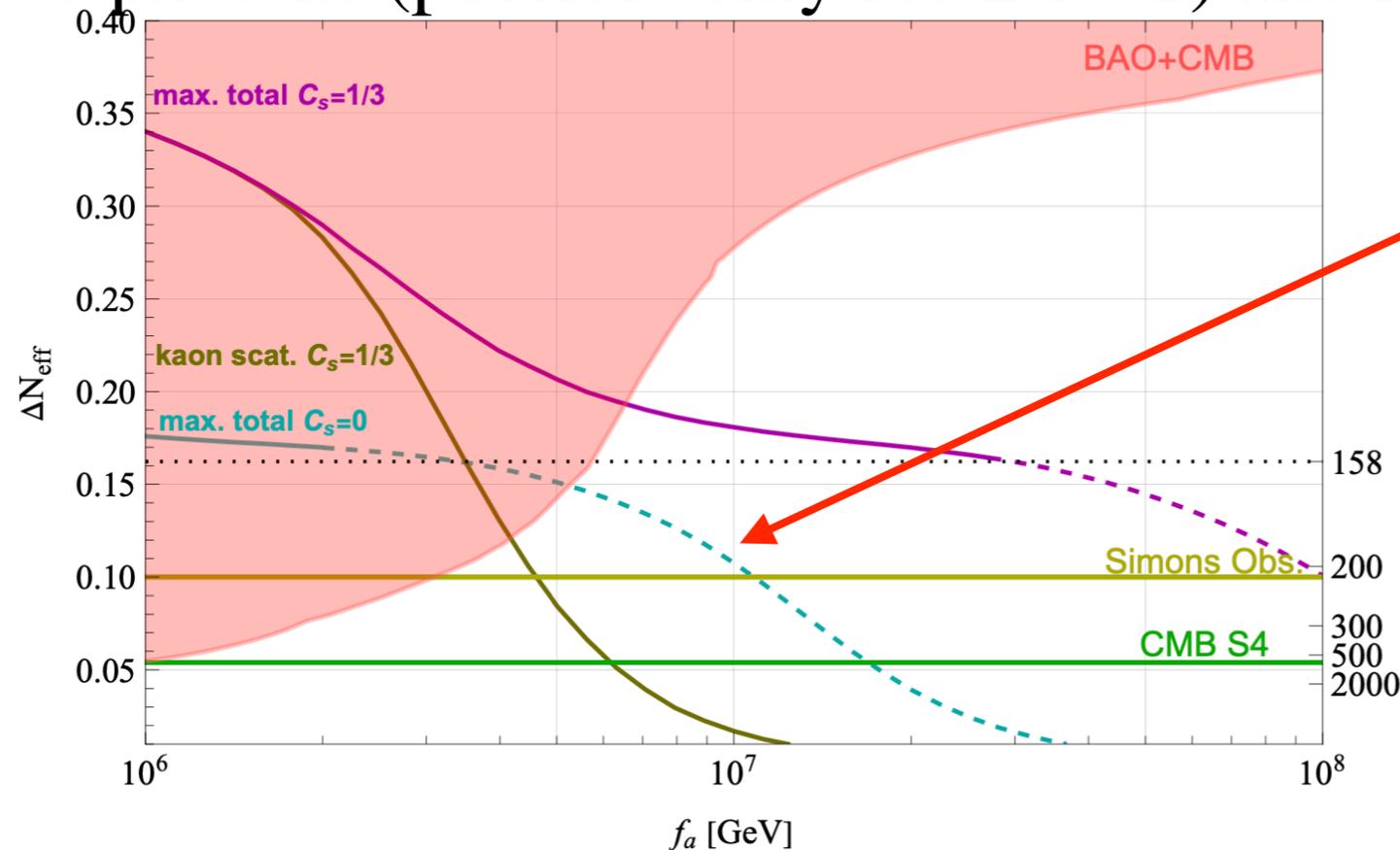


Strong correlations between  $\Delta N_{\text{eff}}$  and axion-photon coupling

If CMB-S4 measures non-zero  $\Delta N_{\text{eff}}$ , (Baby)IAXO will confirm or rule out 2HDM astrophobic models

# $\Delta N_{\text{eff}}$ from Naturally Astrophobic Axion

$f_a < 10^7$  GeV possible due to suppressed axion couplings also to photons (possible only for  $E/N=2$ ) and muons.



Estimate of maximal  $\Delta N_{\text{eff}}$  from axion-quark scattering above QCD PT by taking  $g_s = 4\pi$  (perturbative calc. not reliable for relevant temperatures)

Minimal model predicts negligible  $\Delta N_{\text{eff}}$  from processes below QCD phase transition

Even aggressive estimate of  $\Delta N_{\text{eff}}$  above QCD PT allows for  $f_a \approx 5 \times 10^6$  GeV ( $m_a \approx 1$  eV)

# Summary

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- Astrophobic QCD axions allow for much smaller  $f_a$  giving good prospects for axion discovery at IAXO, future CMB experiments and opening window for minimal axiogenesis
- The simplest models are DFSZ-like models with non-universal PQ charges featuring FV axion-fermion couplings which lead to large contributions to  $\Delta N_{\text{eff}}$
- For appropriate choice of the SM fermion PQ charges the axion is naturally astrophobic and allows for  $f_a$  as small as few  $10^6$  GeV

**Backup**

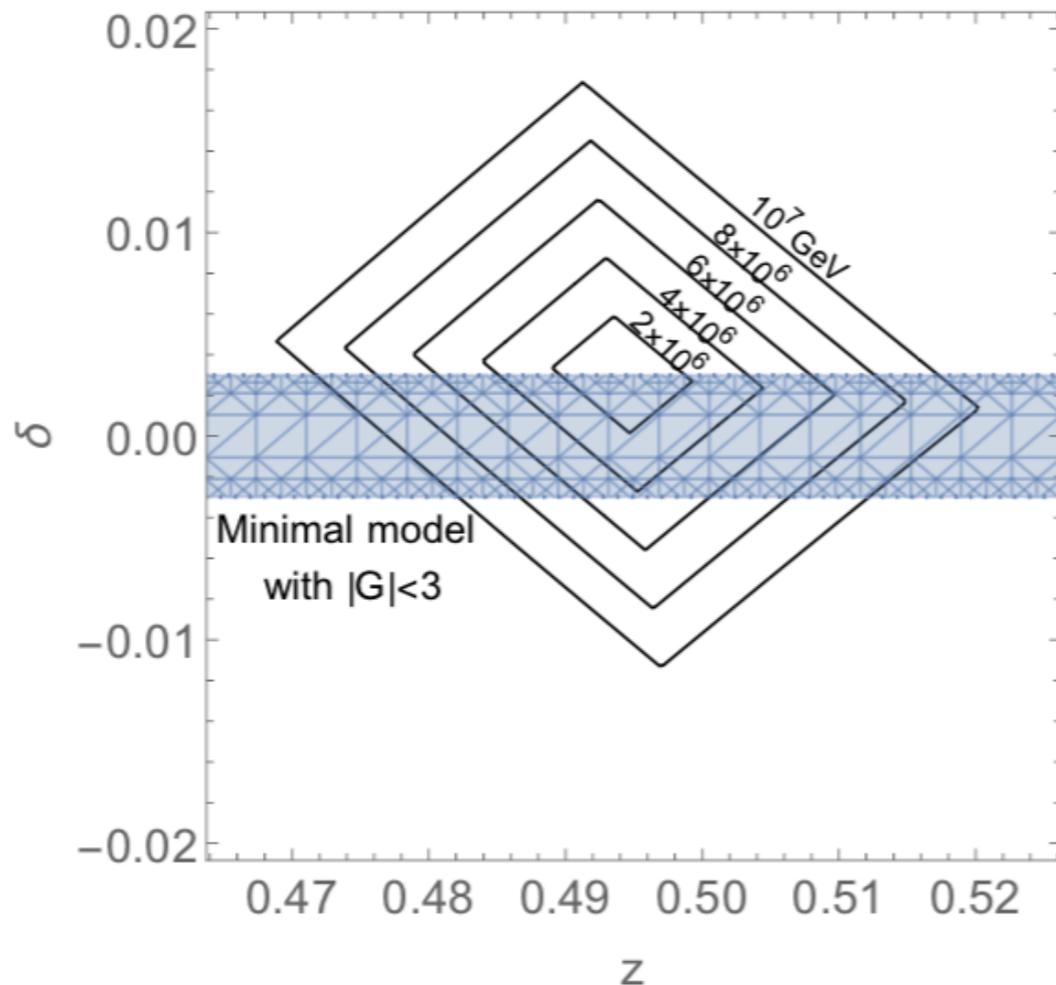
# Naturally Astrophobic Axion, precisely

$$C_p - C_n = (g_A^u - g_A^d) \left( C_u - C_d - \frac{1-z}{1+z+w} \right),$$

$$C_p + C_n = (g_A^u + g_A^d) \left( 0.95(C_u + C_d) + 0.05 - \frac{1+z}{1+z+w} \right) - 2\delta,$$

$$\delta = \sum_{i=s,c,b} \delta_i C_i + \frac{m_\pi^2}{m_{\eta'}^2} \frac{f_\pi}{m_N} \frac{\sqrt{6}z}{(1+z)^2} \times G.$$

$g_A^u - g_A^d$	1.2723(23)	
	$N_f = 2 + 1 + 1$	$N_f = 2 + 1$
$g_A^u + g_A^d$	0.34(5)	0.44(4)
$\delta_s$	0.059(8)	0.044(9)
$\delta_c$	0.0065(39)	0.0092(39)
$\delta_b$	0.0045(12)	0.0063(15)
$z = m_u/m_d$	0.465(24)	0.485(19)
$w = m_u/m_s$	0.023(1)	0.024(1)



$f_a \sim \mathcal{O}(10^7)$  GeV is consistent with the NS cooling bound

( $f_a \sim \mathcal{O}(10^6)$  GeV if  $m_u/m_d \approx 0.49$ )

# UV complete Naturally Astrophobic Axion

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Natural astrophobic axion is obtained e.g. in DFSZ-like models with 3 Higgs doublets:

$$\mathcal{L}_{\text{yuk}} \sim y_d \bar{Q} d H_1 + y_u \bar{Q} u H_2 + y_{f_i} \bar{f}_L f_R H_{SM}$$

$$\langle H_1 \rangle, \langle H_2 \rangle \ll \langle H_{SM} \rangle$$

All SM fermions except up and down

