Holographic approach to QCD and neutron stars





Holography and dense matter workshop APC, Paris June 11, 2024

- Motivation
- Features from holographic approach
- Results for transport
- Summing up

• Matter at extremes is interesting

- quark-gluon plasma
- neutron stars
- Low-energy physical QCD is complicated
 - perturbation theory has limited applicability
 - lattice approach is either too expensive or not trustworthy
 - all-encompassing effective models do not exist
- Alternative approach is to use holography
 - Nomenclature: AdS/CFT, string or gauge/gravity duality, top-down, bottom-up
 - get somewhat close but not QCD (eg. $\textit{N}_{c}=\infty\approx3)$
 - can give an all-encompassing effective model, but uncontrolled approximation
 - gain insights

Holography stems from string theory



• Theoretical green house, where new ideas grow to be transplanted elsewhere



Isotropy and perfect fluid model

$$\begin{aligned} R_{\mu\nu} &- \frac{1}{2} g_{\mu\nu} R = 8\pi G_N T_{\mu\nu}(\epsilon, P(\epsilon)) \quad , \quad \nabla_\mu T^\mu{}_\nu = 0 \\ T_{\mu\nu} &= u_\mu u_\nu(\epsilon + P(\epsilon)) + g_{\mu\nu} P(\epsilon) + (interesting)^{*} later \end{aligned}$$



- Laboratory experiments challenging, especially at high density
- Recent and future progress (LHC, RHIC, FAIR, NICA, ...)
- Incoming experimental data from neutron star measurements! (LIGO/Virgo/Kagra, NICER, ...)



Theoretical results for the phase diagram

- Lattice data only available at zero/small chemical potentials
- Effective field theory works at small densities
- Perturbative QCD: only at high densities and temperatures
- Open questions at intermediate densities



Theoretical results for the phase diagram

- Lattice data only available at zero/small chemical potentials
- Effective field theory works at small densities
- Perturbative QCD: only at high densities and temperatures
- Open questions at intermediate densities
- Approach from strong coupling: AdS/CFT [reviews: Järvinen 2110.08281, Hoyos–NJ–Vuorinen 2112.08422]

Basic idea: extrapolate lattice data to higher density using holography

Two main strategies:

Strategy I: Include confined phase, with $S_{\text{on-shell}} = \mathcal{O}(N_c^0)$, and the transition to a deconfined phase, with $S_{\text{on-shell}} = \mathcal{O}(N_c^2)$

- Used in Improved Holographic QCD and V-QCD models [Gürsoy–Kiritsis 0707.1324; Gürsoy–Kiritsis–Nitti 0707.1349;
 - Järvinen–Kiritsis 1112.1261]
- Fit lattice data above $T = T_c$ Subtract (Missis Filtered) [Gürsoy-Kiritsis-Mazzanti-Nitti 0903.2859]
 - NJ-Järvinen-Remes 1809.07770]

• Faithful to the behavior in the limit of large N_c

Basic idea: extrapolate lattice data to higher density using holography

Two main strategies:

Strategy I: Include confined phase, with $S_{\text{on-shell}} = \mathcal{O}(N_c^0)$, and the transition to a deconfined phase, with $S_{\text{on-shell}} = \mathcal{O}(N_c^2)$

• Used in Improved Holographic QCD and V-QCD models [Gürsoy–Kiritsis 0707.1324; Gürsoy–Kiritsis–Nitti 0707.1349;

Järvinen-Kiritsis 1112.1261]

- Fit lattice data above $T = T_c$ [Gürsoy-Kiritsis-Mazzanti-Nitti 0903.2859; NJ-Järvinen-Remes 1809.07770]
- Faithful to the behavior in the limit of large N_c

Strategy II: Only deconfined black holes: no phase transition at low density

• Fit lattice data at all temperatures

[Gubser-Nellore-Pufu-Rocha 0804.1950; Gubser-Nellore 0804.0434; DeWolfe-Gubser-Rosen 1012.1864; ...; NJ-Järvinen-Piispa 2405.02394]

• Follows the behavior in the phase diagram of QCD (crossover at low density)

Basic idea: extrapolate lattice data to higher density using holography

Two main strategies:

Strategy I: Include confined phase, with $S_{on-shell} = \mathcal{O}(N_c^0)$, and the transition to a deconfined phase, with $S_{\text{on-shell}} = \mathcal{O}(N_c^2)$

• Used in Improved Holographic QCD and V-QCD models [Gürsoy-Kiritsis 0707.1324; Gürsoy-Kiritsis-Nitti 0707.1349;

Järvinen-Kiritsis 1112.1261]

- Fit lattice data above $T = T_c$ [Gürsoy-Kiritsis-Mazzanti-Nitti 0903.2859; NJ-Järvinen-Remes 1809.07770]
- Faithful to the behavior in the limit of large N_c

Strategy II: Only deconfined black holes: no phase transition at low density

• Fit lattice data at all temperatures [Gubser-Nellore-Pufu-Rocha 0804.1950; Gubser-Nellore 0804.0434; DeWolfe-Gubser-Rosen 1012.1864; ...; NJ-Järvinen-Piispa 2405.02394]

• Follows the behavior in the phase diagram of QCD (crossover at low density)

(Strategy 0: D3-D7 QFT soluble using string/gravity.)

Basic idea: extrapolate lattice data to higher density using holography

Two main strategies:

Strategy I: Include confined phase, with $S_{\text{on-shell}} = \mathcal{O}(N_c^0)$, and the transition to a deconfined phase, with $S_{\text{on-shell}} = \mathcal{O}(N_c^2)$

• Used in Improved Holographic QCD and V-QCD models [Gürsoy-Kiritsis 0707.1324; Gürsoy-Kiritsis-Nitti 0707.1349;

Järvinen-Kiritsis 1112.1261]

- Fit lattice data above $T = T_c$ [Gürsoy-Kiritsis-Mazzanti-Nitti 0903.2859; NJ-Järvinen-Remes 1809.07770]
- Faithful to the behavior in the limit of large N_c

Strategy II: Only deconfined black holes: no phase transition at low density

• Fit lattice data at all temperatures [Gubser-Nellore-Pufu-Rocha 0804.1950; Gubser-Nellore 0804.0434;

[Gubser–Nellore–Putu–Rocha 0804.1950; Gubser–Nellore 0804.0434; DeWolfe–Gubser–Rosen 1012.1864; ...; NJ–Järvinen–Piispa 2405.02394]

 Follows the behavior in the phase diagram of QCD (crossover at low density)

(Strategy 0: D3-D7 QFT soluble using string/gravity.)

Strategies 0&I have been extended in NS context.

Fitting example: Strategy II

• No phase transition, predict a critical point at nonzero μ



Predictions consistent with heavy-ion collision data at RHIC

Follow Strategy I

- Phase transition at zero μ , extrapolate to NS matter regime
- Intermediate- μ : low-T instanton solution appears: baryons



Hybrid Equations of State

Holo-NM description not reliable at low densities:

- Match nuclear models (low densities) with holography (high densities)
- Variations in model parameters give rise to the band
- Same (holographic) model for NM and QM phases [Ecker–Järvinen–Nijs–van der Schee 1908.03213; NJ–Järvinen–Nijs–Remes



[NJ-Järvinen-Remes 2111.12101]

• CompOSE: 3× 1d JJ(VQCD) follows APR up to 1.6ns

2006.01141]

Holographically aided QCD phase diagram

- Given EoS can be extended to finite-T



- EoS has been used in NS merger simulations
 [see Christian Ecker's talk]
- Systematic extension to finite- T: posterior distributions [work in progress w/ Ecker&Järvinen]

Does deconfined QM exist in nature?

Equation of state determines most important properties of stars,



but is insufficient (masquerading) to address if \exists quark matter.

- No symmetry arguments: quark-hadron continuity
- Sharp deconfinement (Occam's razor) phase transition <u>may</u> lead to distinct signals
- Caveats: surface tension \neq 0, ∞ really, inhomogeneity, anisotropy
- Need to go beyond EoS: root for transport
 - quarks are relativistic unlike hadrons

r-mode instability window

- Non-radial modes are driven unstable if the star rotates fast enough.
- These modes are strongly sheared and damped.

$$\frac{dE}{dt} = -2\frac{E}{\tau}$$

$$\propto \exp\left(i\omega_m(\Omega)t + im\phi - t/\tau_m(\Omega)\right)$$

• Maximum stable frequency for the star:

$$0=1/ au_m(\Omega)=-1/ au_{\mathsf{GW}}+1/ au_\eta+1/ au_\zeta$$



[Figure:Bratton et al.'22]



[Figure: Lindblom'98] 13/22

r-mode instability window

Indirect evidence for quark matter? [Figures: Andersson–Kokkotas gr-qc/0010102,Alford–Schwenzer 1310.3524]



• Bulk viscocity ζ seems interesting

Relevance of transport in stars



[Schmitt-Shternin 1711.06520]

- Damping of oscillations: shear η and bulk ζ viscosities
- Cooling: thermal conductivity κ, neutrino emissivities
- \bullet Magnetic fields: electric σ and thermal conductivities
- Mergers: viscosities, conductivities, evolution far from equilibrium

Caution...

- Computing conductivities need care since spatial homogeneity
 - Lorentz invariance: only one hydro transport coeff σ
 - No force condition: [Davison-Goutéraux 1505.05092; Davison-Goutéraux-Hartnoll

1507.07137]



Conductivities

$$J^{i} = \sigma^{ij} E_{j} , \quad \sigma^{ij} = \sigma \frac{\epsilon + p}{Ts} \delta^{ij}$$
$$Q^{i} = -\kappa^{ij} \nabla_{j} T , \quad \kappa^{ij} = \frac{\mu}{T} \sigma \frac{\epsilon + p}{\rho} \delta^{ij}$$

Quiescent stars

- Local charge neutrality: $\frac{2}{3}n_u \frac{1}{3}n_d \frac{1}{3}n_s n_e = 0$
- Beta equilibrium: $\mu_s = \mu_d$, $\mu_u = \mu_d \mu_e$

Holographic models encompassed

Action
$$S = S_{glue} + S_{flavor} w / \kappa_5^2 \sim 1/N_c^2$$
, $\mathcal{T}_b \sim N_f / N_c$:
 $S_{glue} = \frac{1}{2\kappa_5^2} \int d^5 x \sqrt{-g} \left(R - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi, \chi) \right)$
 $S_{flavor} = -\frac{\mathcal{T}_b}{2\kappa_5^2} \int d^5 x Z(\phi, \chi) \sqrt{-\det(g_{\mu\nu} + \kappa(\phi, \chi)\partial_\mu \chi \partial_\nu \chi + w(\phi, \chi)F_{\mu\nu})}$

- metric $g_{\mu
 u} \leftrightarrow$ energy-momentum tensor
- flavor gauge field $A_{\mu} \leftrightarrow$ baryon charge
- "dilaton" $\phi \leftrightarrow$ gauge coupling
- "tachyon" $\chi \leftrightarrow$ quark masses

Our examples include:

- bottom-up V-QCD model (Strategy I)
- top-down D3-D7 model in the quenched approximation (Strategy 0)
- can be applied to Strategy II: predictions in Beam Energy Scan regime @RHIC

[see eg. Grefa et al. 2312.11449]

Transport for flavor independent masses

• DC transport determined at the black hole horizon [Hoyos-NJ-Järvinen-Subils-Tarrio-Vuorinen 2005.14205,2109.12122]

$$T(\text{surface gravity}) , \ s(\text{area}) , \ \rho(\text{electric flux})$$

$$\phi_H = \phi(r_H) , \ \chi_H = \chi(r_H)$$

- Boundary values determine thermo: ϵ, p, μ
- Thermal and electric conductivities

$$\sigma = \frac{w_H}{2\kappa_5^2 g_{xx}^H} \sqrt{(2\kappa_5^2 \rho)^2 + (g_{xx}^H)^3 \mathcal{T}_b^2 w_H^2 Z_H^2}$$

Shear viscosity

$$\eta = \frac{s}{4\pi} = \frac{(g_{xx}^H)^{3/2}}{2\kappa_5^2} + \frac{s_{\text{flavor}}}{4\pi}$$

• Bulk viscosity (QCD part)

$$\frac{\zeta}{\eta} = (s\partial_s\phi_H + \rho\partial_\rho\phi_H)^2 + \frac{2\kappa_5^2}{(g_{xx}^H)^{1/2}}\frac{\kappa_H}{w_H^2}(s\partial_s\chi_H + \rho\partial_\rho\chi_H)^2$$

Transport of cool quark matter



- Predictions for viscosities for unpaired quark matter (dashed $\mu = 450$ MeV, solid $\mu = 600$ MeV)
- Large deviation from pQCD LO results

[Heiselberg–Pethick 1993]

- Tiny results due "idealized" case. Flavor-independent masses so get only QCD contributions, no weak interactions or electrons
- CompOSE: $3 \times 3d$ HJJSTV(VQCD) includes transport for QM

Flavor dependence

• Bulk viscosity can be enhanced by resonant EW processes [Alford–Mahmoodifar–Schwenzer '12]

$$u + d \leftrightarrow u + s$$
 , $\frac{dn_d}{dt} = -\frac{dn_s}{dt} \approx \lambda_1(\mu_s - \mu_d)$

Relevant for flavor-dependent quark masses
 [CruzRojas-Gorda-Hoyos-NJ-Järvinen-Kurkela-Paatelainen-Säppi-Vuorinen 2402.00621]



$$\begin{split} \zeta &= \frac{\lambda_1 A_1(\chi_{ij})^2}{\omega^2 + (\lambda_1 C_1(\chi_{ij}))^2} \Big|_{T=0}^{D3-D7} = \frac{4\lambda_1 \mu_d^6 \left(M_s^2 - M_d^2\right)^2}{\omega^2 \left(M_d^2 - 3\mu_d^2\right)^2 \left(M_s^2 - 3\mu_d^2\right)^2 + \pi^4 \lambda_1^2 \left(-6\mu_d^2 + M_d^2 + M_s^2\right)^2} \\ \lambda_1 &= \frac{64G_F^2 \sin^2 \theta_c \cos^2 \theta_c}{5\pi^3} \mu_d^5 T^2 + \dots \ , \ \forall \ A_1(T) \approx A_1 \ , \ C_1(T) \approx C_1 \end{split}$$

Summary

- Gauge/gravity duality (combined with other approaches) is useful to study dense QCD
- Many details work really well:
 - \checkmark Precise fit of lattice thermodynamics at $\mu\approx 0$
 - ✓ Extrapolated EoS for cold quark matter reasonable
 - \checkmark Simultaneous model for nuclear and quark matter
 - ✓ Stiff EoS for nuclear matter
- Predictions for
 - equation of state of cold and finite-T matter
 - transport in quark matter phase
 - (properties of neutron stars)
 - (gravitational wave spectrum in neutron star mergers)
 - • •

Outlook

- Observable effects in neutron star physics?
- Possible extensions:
 - flavor dependent masses
 - isospin/other chemical potentials
 - neutrino emissivity in NS regime [build on Sarvinen–Kiritsis–Nitti–Préau 2306.00192]
 - magnetic field
 - anisotropic equation of state
 - quark pairing (color "superconductivity")
 - inhomogeneous phases
- Recall caveats:
 - homogeneity seems lost [CruzRojas-Demircik-Järvinen 2405.02399; Demircik-NJ-Järvinen-Piispa

2405.02392]

• surface tension between deconfined and confined phases: accurate lattice results coming up

Thank you!

Inhomogeneity in holographic plasma?



[Nakamura, Ooguri, Park 0911.0679; Ooguri, Park 1011.4144]

- Exponentially growing perturbation at q ≠ 0: a quasi-normal mode with lm ω > 0
- Chern-Simons term can drive a modulated instability at finite density
- Such CS terms automatically included in the holographic model ↔ QCD chiral anomaly
- Modulated 5D gauge fields dual to modulated persistent chiral currents in field theory

Schematic fluctuation equation

$$\psi''(r) + \left(A' + \frac{f'}{f}\right)\psi'(r) + \underbrace{\frac{qn}{\mathcal{M}_{p}^{3}fe^{2A}w(\phi)^{2}}\psi(r)}_{\text{From CS term}} + \left(\frac{\omega^{2}}{f^{2}} - \frac{q^{2}}{f}\right)\psi(r) = 0$$
$$\psi = \delta A_{L/R}^{x} \pm i\delta A_{L/R}^{y}$$





Modulated instability in holo-QM

The region where instability exists [CruzRojas–Demircik–Järvinen 2405.02399; Demircik–NJ–Järvinen–Piispa 2405.02392]



- Instability is found at low T and large density region relevant for neutron stars (expected)
- Instability is also found at higher *T*, near the regime with critical point?! (a big surprise)

Model dependence: strange quark mass

- Model dependence is really mild: [Demircik-NJ-Järvinen-Piispa 2405.02392]
 - varied model parameters \leftrightarrow freedom in fitting to lattice data
 - varied fitting using Strategy I \leftrightarrow Strategy II
 - $\bullet\,$ varied the flavor action DBI \leftrightarrow Yang–Mills truncation
- All holographic massless QM models fitted to lattice data has instability at high- ${\cal T}$
- Flavor dependence in susceptibilities, visible in lattice data? [Borsanyi et al. 1112.4416]
- Naive test: fit instead of the full χ_2 the light quark χ_2 (dashed curves) of the $N_f = 2 + 1$ lattice result



Strong suppression of the instability!