

Neutron-star crust modelling and unified equations of state *(ongoing projects)*

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in collaboration with LPC Caen, LUTH-Meudon, IAA-ULB, Univ. Montreal, CAMK Warsaw, ...

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IJCLab, Orsay, France



Outline

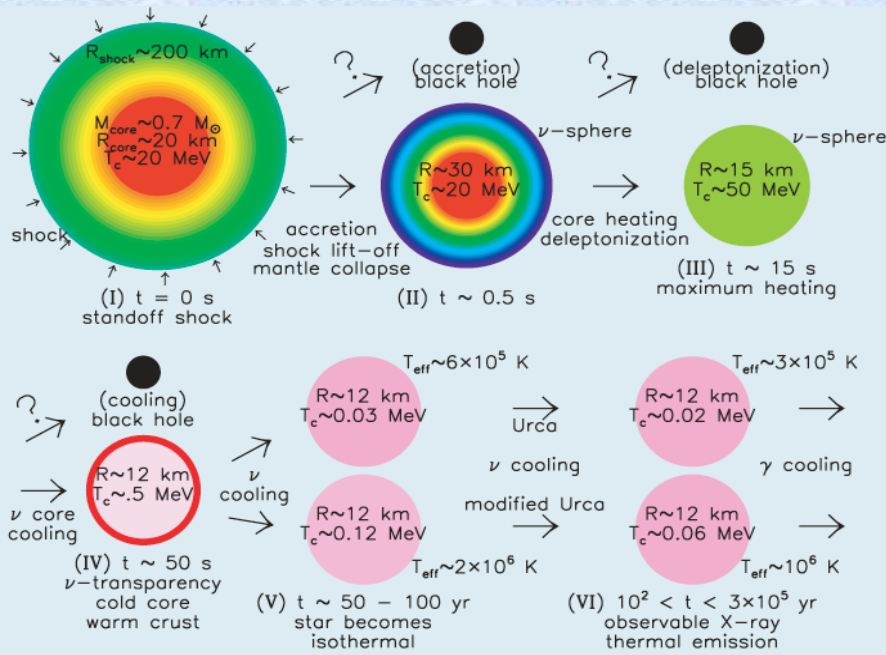
❖ Selected (ongoing) projects + outlooks

- *Catalysed NSs* ($T = 0$, full equilibrium) → see P.J. Davis' talk
- *Accreting NSs* ($T = 0$, crust out of equilibrium)
- *Proto-neutron-star (PNS) crust* ($T \neq 0$, beta equilibrium)
- *Supernova electron-capture rates*



NS (isolated): formation

after shock formation



Lattimer & Prakash, Science 304, 536 (2004)

- NS born hot, $T \sim 10^{10}$ - 10^{11} K
- after few tens of sec – mins
 - beta equilibrium (e.g. [Camelio et al. 2017](#))
 - formation of crust (e.g. [Pons&Viganò 2019](#))
(T below $\sim 10^9 - 10^{10}$ K, $\Delta t \sim$ hr - months)
- cooling → T below $\sim 10^8$ K
 - “cold catalysed” (→ $T = 0$)
 - full thermodynamic equilibrium, $P(n_B)$

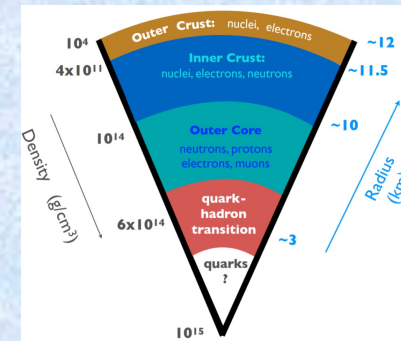


Image Credit: 3G Science White Paper

but: real picture can differ from cold catalysed one

- * Accretion of matter from companion (→ $P(n_B, Y_q)$, not full equilibrium)
- * PNS (→ $T > 0$, $P(n_B, T)$ if beta equilibrium)

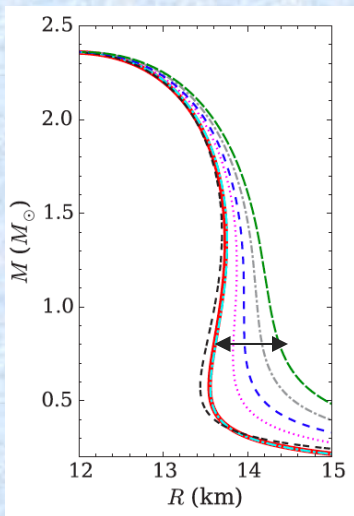
N.B.: “General purpose” EoSs $P(n_B, T, Y_q)$ & B effects not addressed here



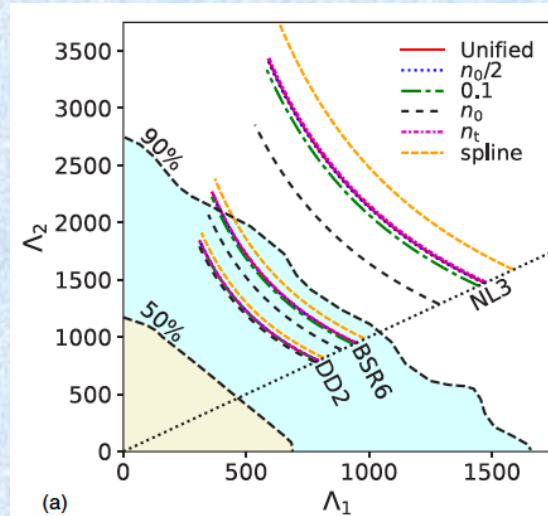
Why a unified treatment ?

Unified treatment of inhomogeneous & homogeneous matter
 → same nuclear model employed in different regions of star

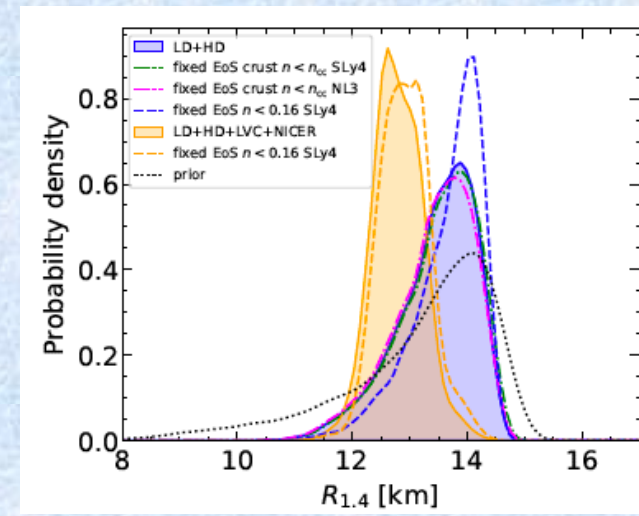
- Challenging because of wide range of thermodynamic conditions
- Challenging because different states of matter
- But: essential to avoid spurious non-physical effects in numerical modelling



Fortin et al., PRC 94, 035804 (2016)



Suleiman et al., PRC 104, 015801 (2021)



Davis et al, A&A in press → P. Davis' talk



Aim: provide thermodynamically consistent and unified EoSs for astro modelling & inference analyses



EoS models used in our works

BSk + ETFSI

- HFB mass model for outer crust
- ETFSI for inner crust
- Brussels-Montreal (BSk) EDFs

MM + CLDM

- CLDM for outer+inner crust
- meta-model (MM) for core
+ also for bulk energy of ion

Unified EoSs

- ✓ Accurately calibrated Skyrme EDFs
 - study specific model dependence
 - benchmark calculations
- ✓ More microscopic
- ✗ No parameter-space exploration

- Ensemble of consistent nuclear inputs for astro models (e.g. EoS , $M(R)$, $\Lambda(M)$, but also nucl. masses, microscopic quantities like pairing gaps, m^* , etc.)



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Unified EoSs

MM + CLDM

- CLDM for outer+inner crust
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 - + also for bulk energy of ion



- ✓ Flexible, faster computation
 - Parameter-space exploration
 - Bayes analysis
- ✓ Multi-component plasma (MCP)
- ✗ Less microscopic

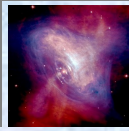


$$P(\mathbf{X}|\mathbf{c}) = \mathcal{N}P_{\text{prior}}(\mathbf{X}) \prod_k P(c_k|\mathbf{X})$$

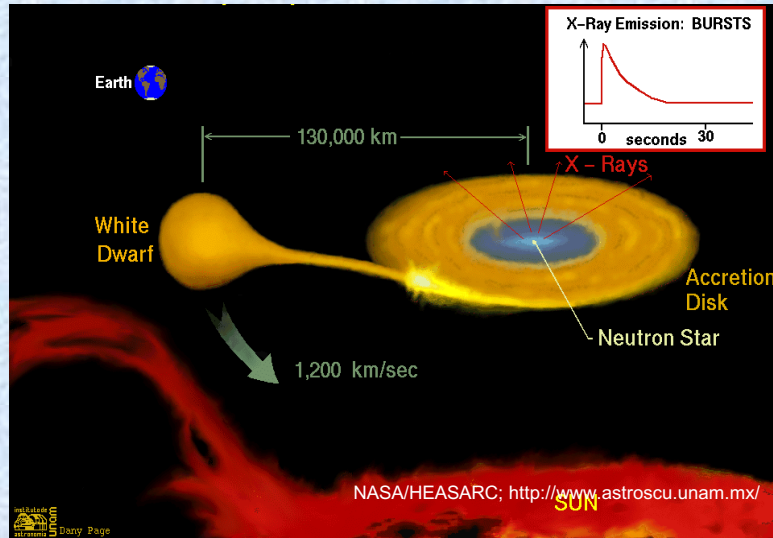
$\mathbf{X}$ = nucl. param.

k
nuclear+astro
constraints

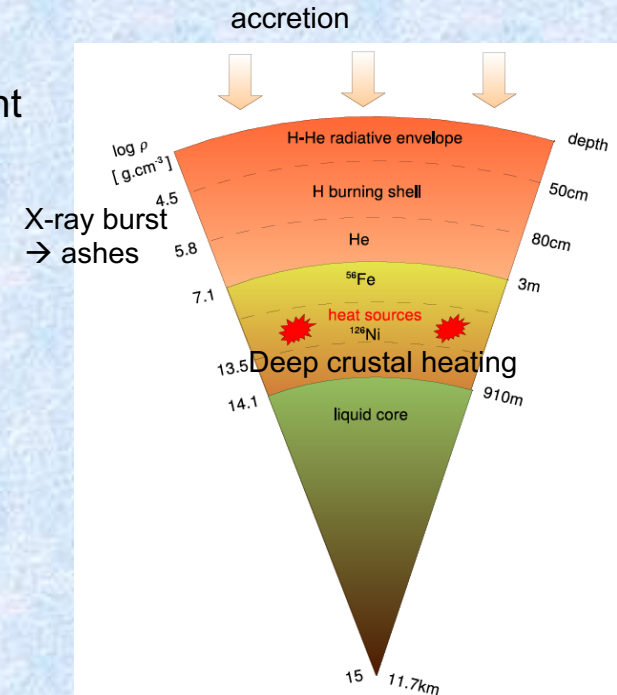
- MCP distributions (e.g. PNS crusts)
- Estimation of uncertainties in astro predictions/inference (e.g. Bayesian)



Accreting NS (Low-mass X-ray binary)

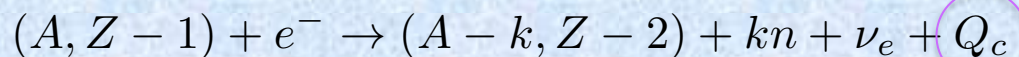
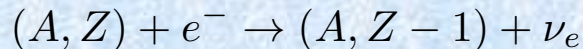


e.g. Soft X-ray transient (SXT)

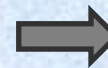
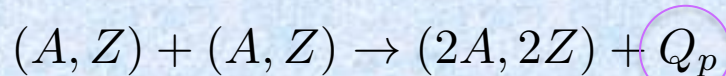


Chamel & Haensel 2008

✧ **Electron captures + neutron emission (inner crust):**



✧ **Pycnonuclear reactions:**



- ✓ **matter off-equilibrium**
- ✓ **reactions possible**
- **energy reservoir**
- **deep crustal heating**

N.B.: uncertainties in pycno reactions → we assume it occurs when $Z = Z_{min} = 8$

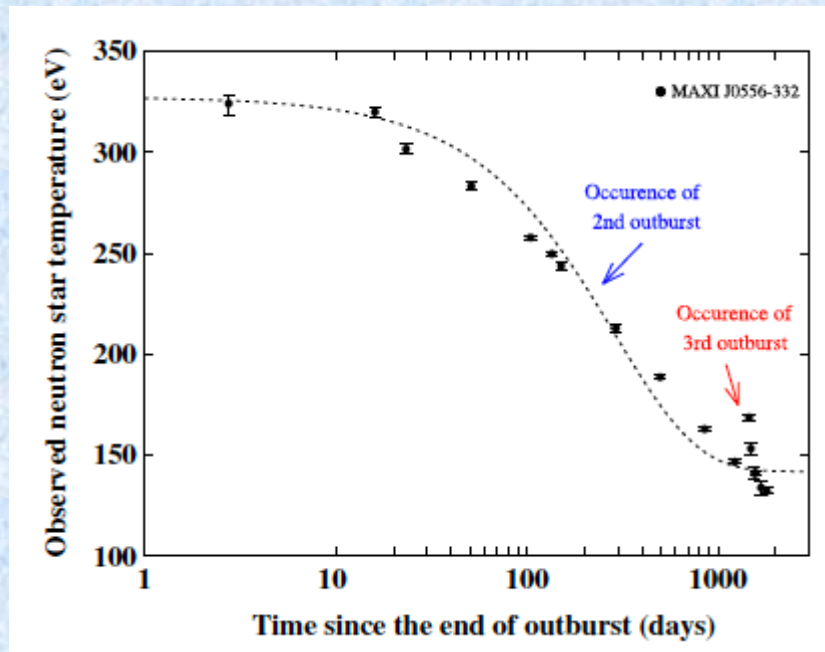
see e.g. Chamel & Haensel, Living Rev. Relativ. 11, 10 (2008); Meisel et al., J. Phys. G, 45, 093001 (2018); Blaschke & Chamel, ASSL 457, 337 (2018); Haensel & Zdunik, A&A 1990, 2003, 2008



Accreting NS (SXT)

“**Deep crustal heating**” can explain thermal radiation in SXTs in quiescence

but : exceptions ! → *shallow heating* (additional sources in shallow layers)



Wijnands et al., J. Astroph. Astr. 38, 49 (2017)

Inputs to model relaxation / cooling :

➤ **Composition**

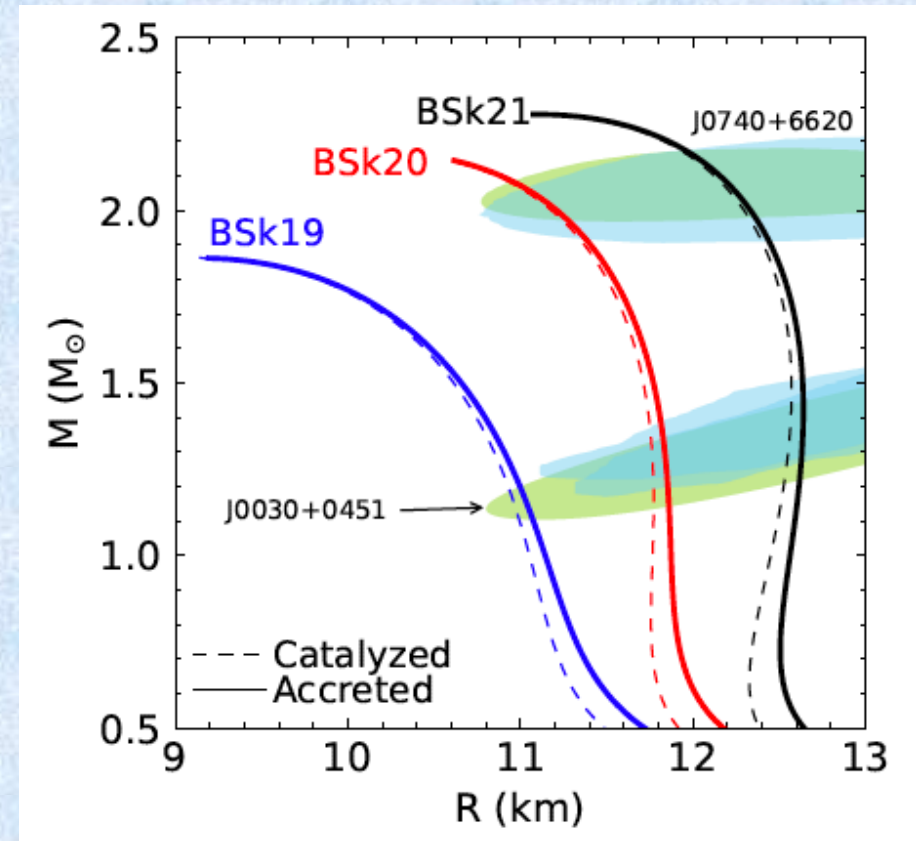
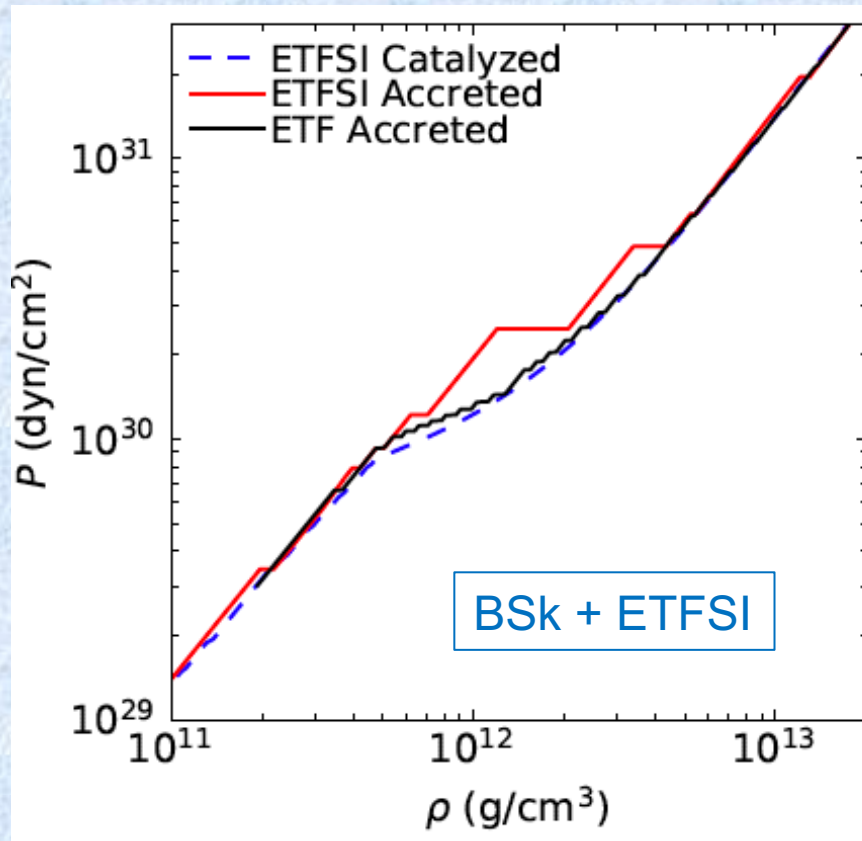
➤ **EoS**

➤ **Heat sources**

→ amount of heat and location



Accreting NS crusts: EoS

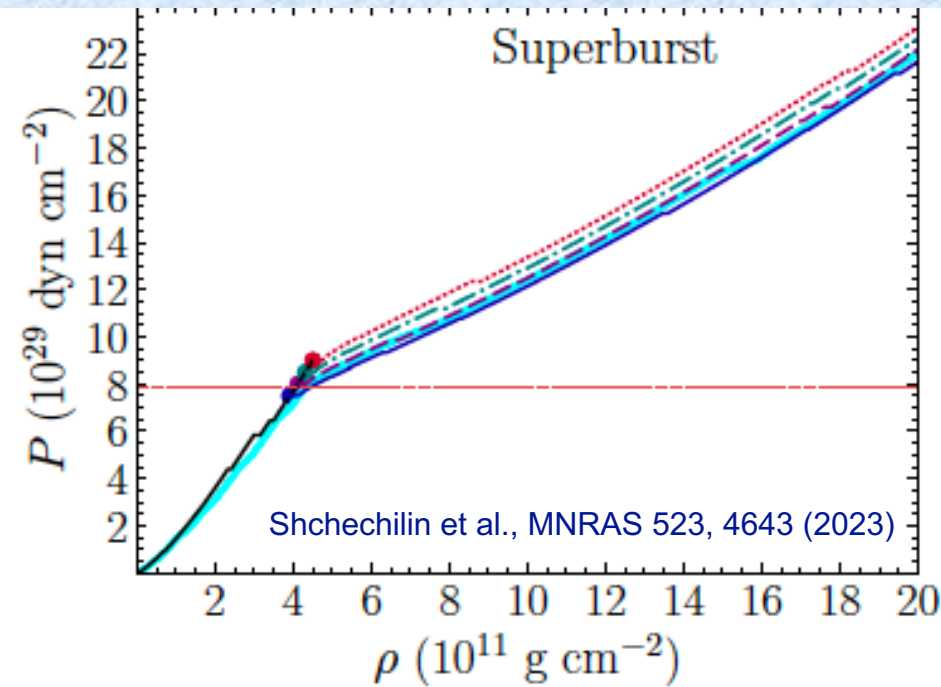
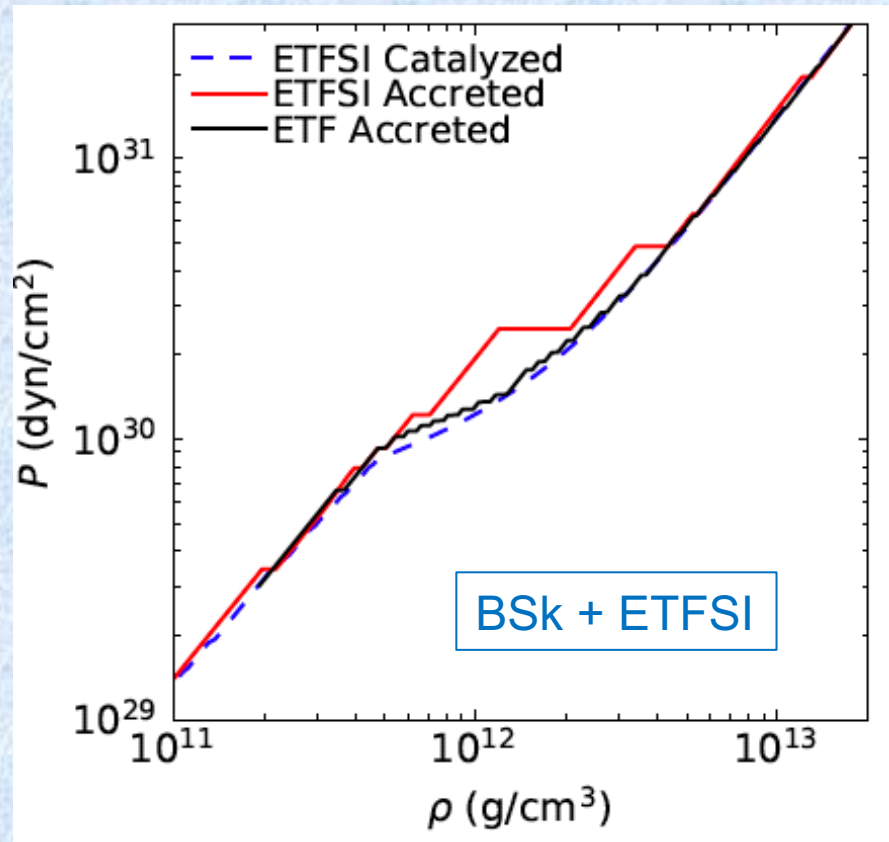


Fantina et al., A&A 665, A74 (2022)

- **Accreting crust EoS stiffer** than catalysed one → larger radii
- ✗ but: difference still smaller than observation uncertainties



Accreting NS crusts: EoS



- **Accreting crust EoS stiffer** than catalysed one → larger radii
- ✗ but: difference still smaller than observation uncertainties
- ✗ EoS closer to catalysed EoS if *n* diffusion (Gusakov & Chugunov 2020; Shchechilin et al. 2023)
- to be investigated (e.g. Allard&Chamel, PRL 2024)



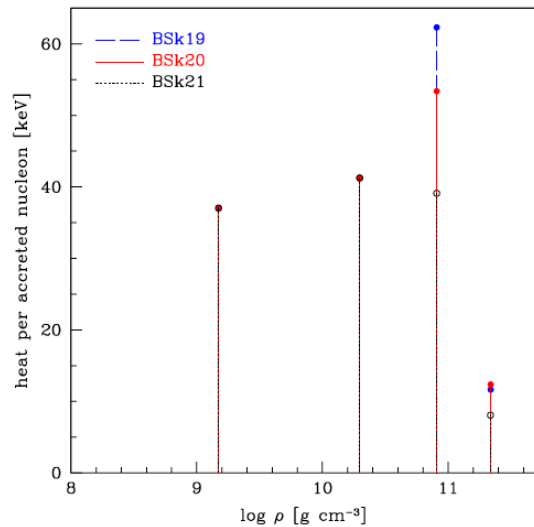
Accreting NS crusts: heat sources

heat sources

BSk + ETFSI

total heat

Outer crust (starting from ^{56}Fe)



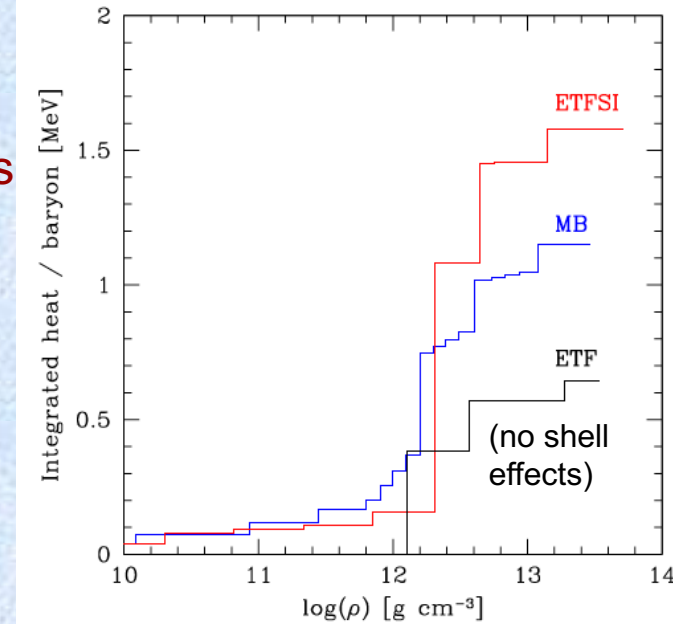
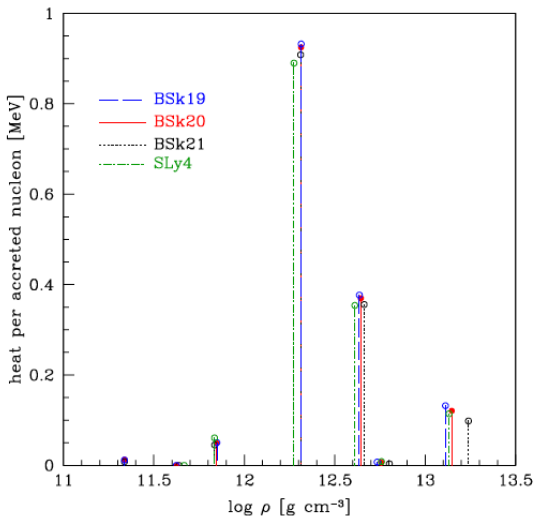
- Importance of shell effects
- $Q_{\text{tot}} = \sim 1.5\text{--}1.6 \text{ MeV/nuc.}$
- Pycnonuclear main sources in inner crust

X but: OCP (^{56}Fe)

- * Q_{tot} comparable with reaction networks
- * Heat for different ashes higher (Chamel, Fantina, et al. 2020)

N.B.: heat sources also in magnetar's crusts
(Chamel, Fantina, et al. 2021;
Chamel & Fantina 2022)

Inner crust



➔ MCP ?

(MCP models exist, e.g. Lau et al. 2018 but only for outer / low-density inner crust)

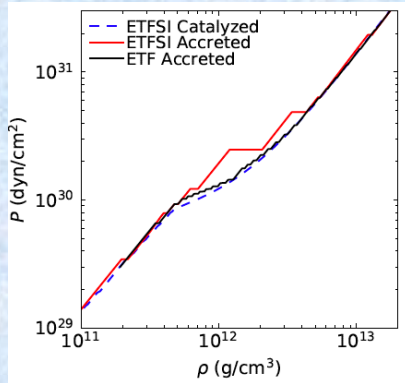
Fantina et al., A&A 620, A105 (2018)



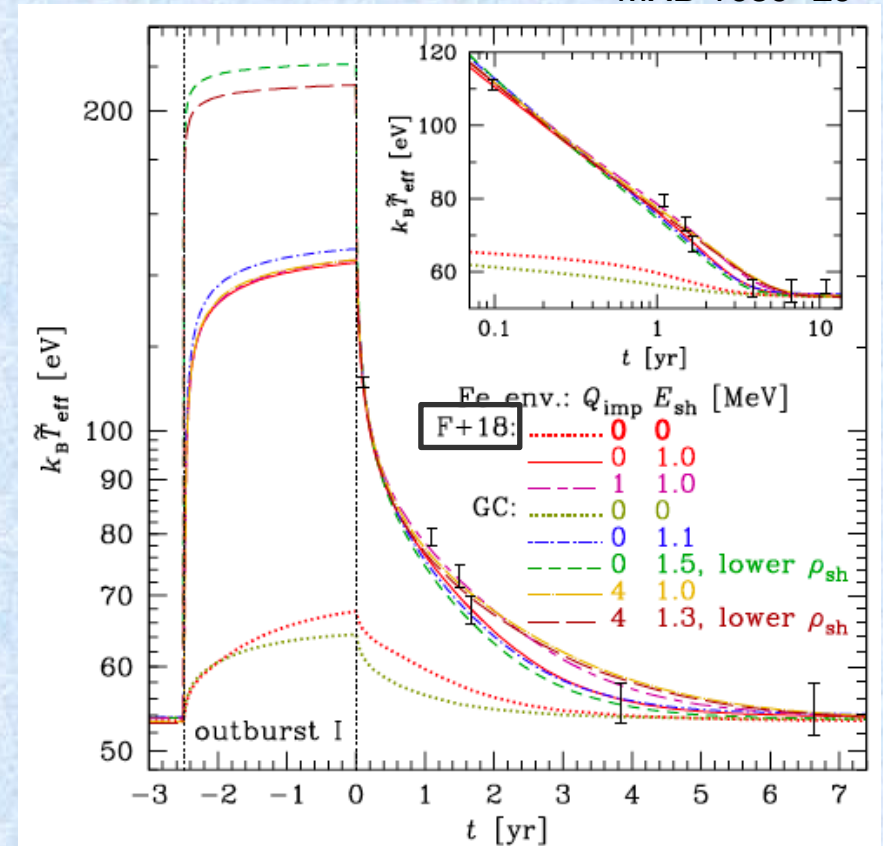
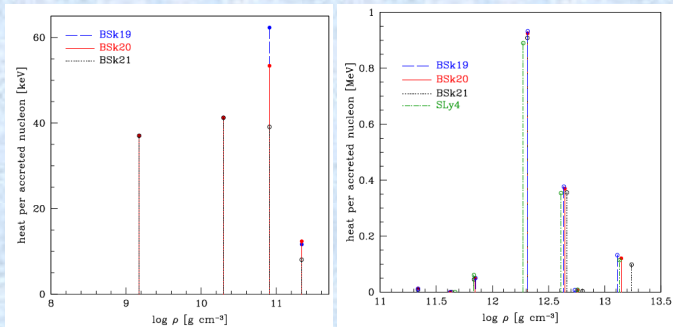
Accreting NSs: thermal evolution

MXB 1659–29

BSk + ETFSI



EoS + heat sources



Potekhin et al., MNRAS 522, 4830 (2023)

- Observations can be reproduced by models (with tuning)
- ✗ but: difficult to discriminate models
- other parameters (Q_{imp} , shallow heating, ...) play a role



Accreting NSs: outlooks

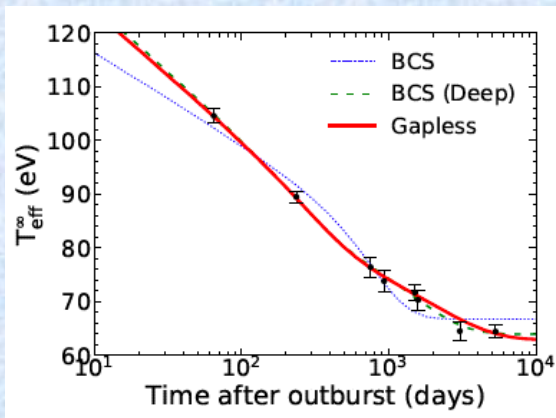
Unified EoS + heat released

data publicly available (tables on CDS, Zenodo* for magnetar's crusts)

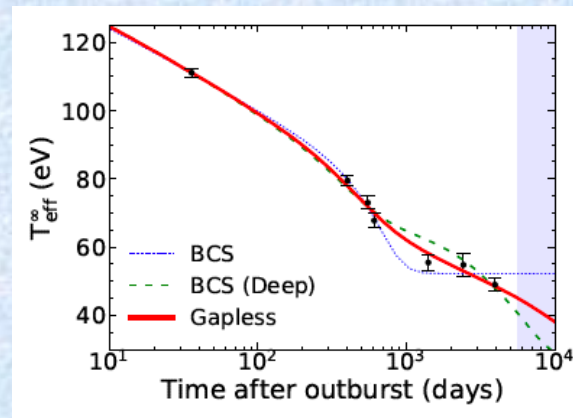
❖ Accreted crust $\neq$ catalysed crust $\rightarrow$ importance of nuclear shell effect

- Inclusion of neutron diffusion ? (Gusakov & Chugunov 2020, 2021, Shchechilin et al. 2022, 2023)
- OCP vs MCP to be explored $\rightarrow Q_{\text{imp}}$, transport coeff. $\rightarrow$ *impact on light curves / cooling*
- Partially accreted crust (e.g. Suleiman et al. 2022)

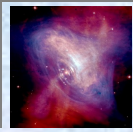
N.B. very recent results on cooling of SXTs with “gapless” superfluidity



Allard & Chamel, PRL 132, 181001 (2024)

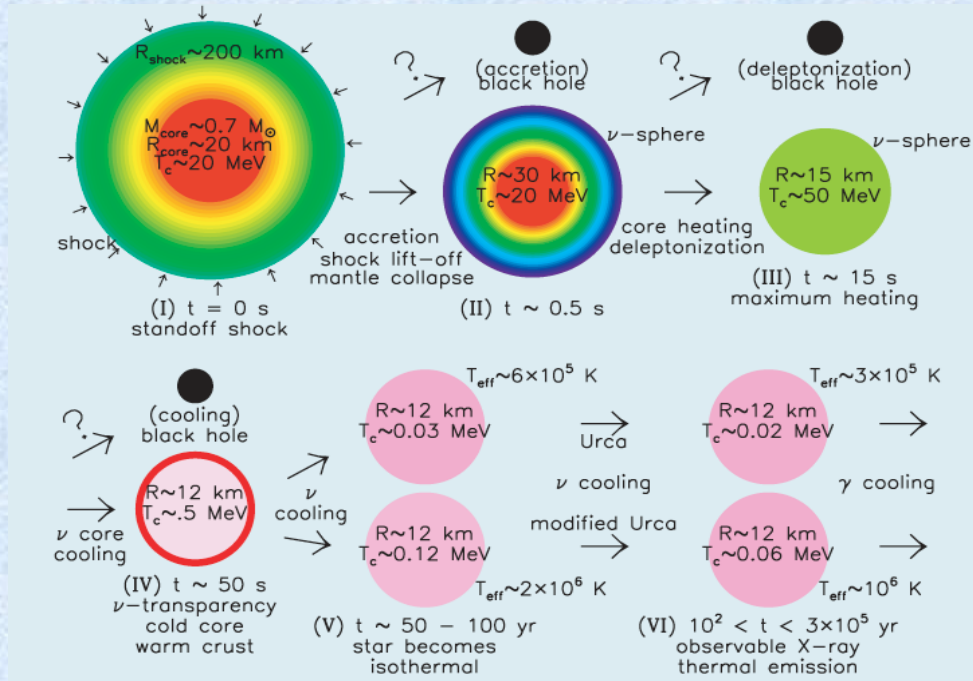


(*) <http://cdsarc.u-strasbg.fr/viz-bin/cat/J/A+A/>, <https://zenodo.org/>

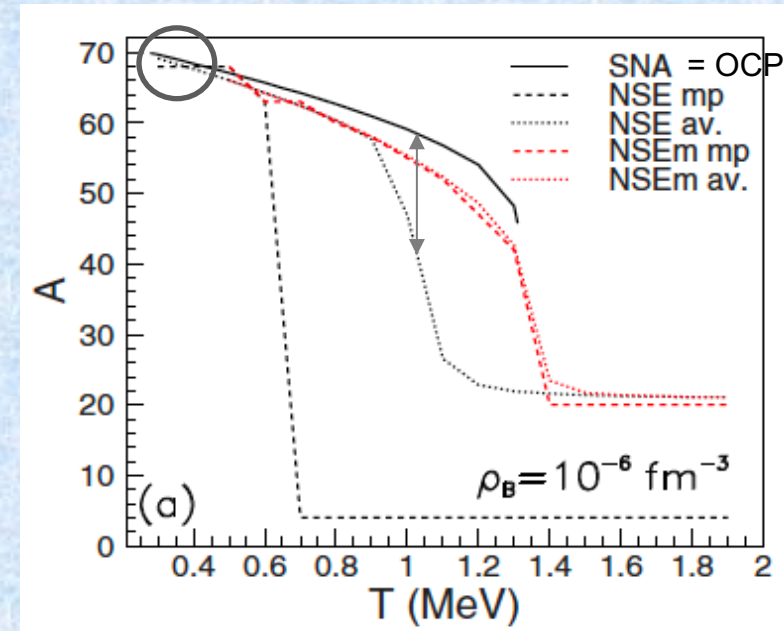


Proto-NS (finite temperature)

NS formation from CCSN



At finite $T \rightarrow$ need to go beyond OCP



Gulminelli & Raduta, PRC 92, 055803 (2015)

Lattimer & Prakash, Science 304, 536 (2004)

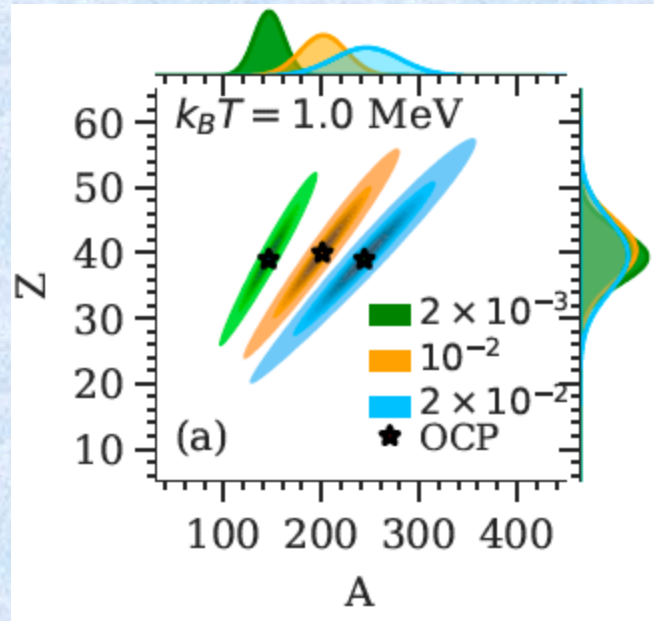
- $\rightarrow$ NS are born hot ($T > 10^{10}$ K $\sim$ 1 MeV) $\rightarrow$ ensemble of nuclei (MCP) expected
- $\rightarrow$ NS crust **crystallises (liquid $\rightarrow$ solid)** at $T_m \sim 0.1\text{--}1$ MeV $\rightarrow$ crust composition “frozen” but:
 - depending on cooling timescales, composition can be frozen at $T > T_m$ (e.g. Goriely et al., A&A 531, A78 (2011))
 - other reactions possible below T_m ? (e.g. Potekhin & Chabrier, A&A 645, A102 (2021))



PNS: composition & impurities



1. Composition can be different from $T = 0$ & OCP one !

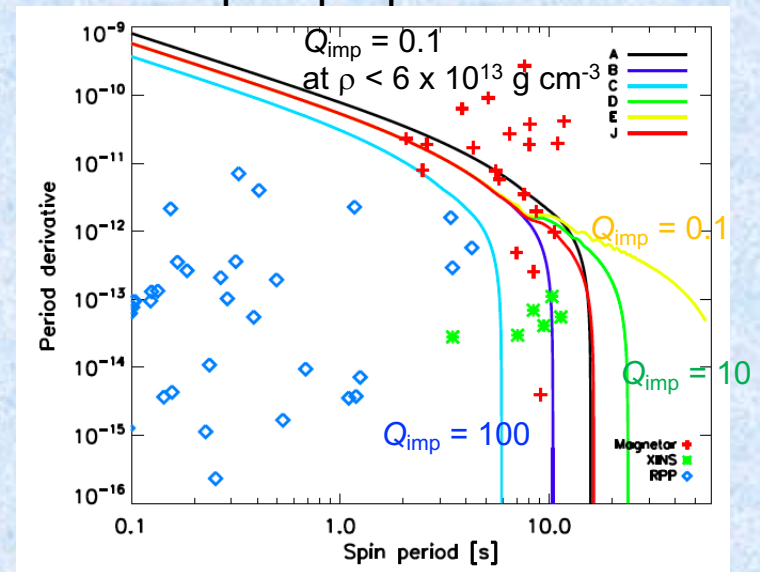


Dinh Thi et al., A&A 677, A174 (2023)
see also Fantina et al., A&A 633, A149 (2020);
Carreau et al., A&A 640, A77 (2021)

2. Co-existence of nuclear species
→ “**impurity factor**” (usually free parameter adjusted on cooling data)

$$Q_{\text{imp}} = \langle Z^2 \rangle - \langle Z \rangle^2$$

→ impact dynamic, magneto-rotational and transport properties

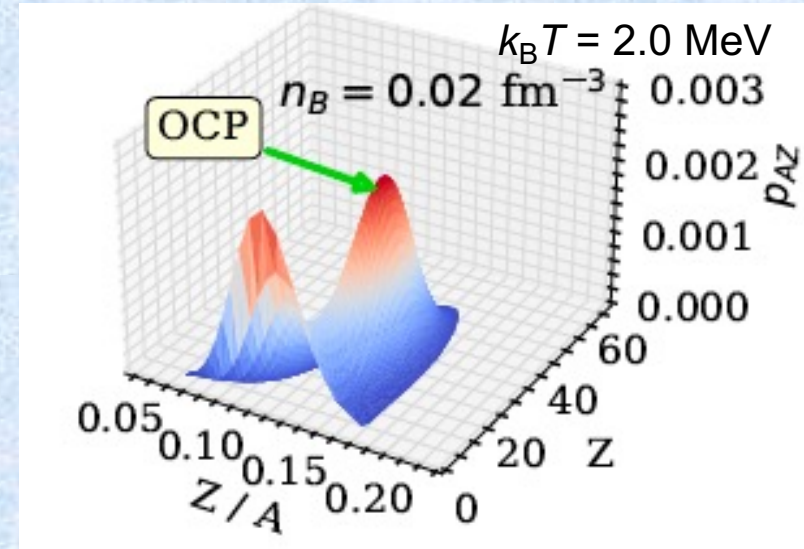
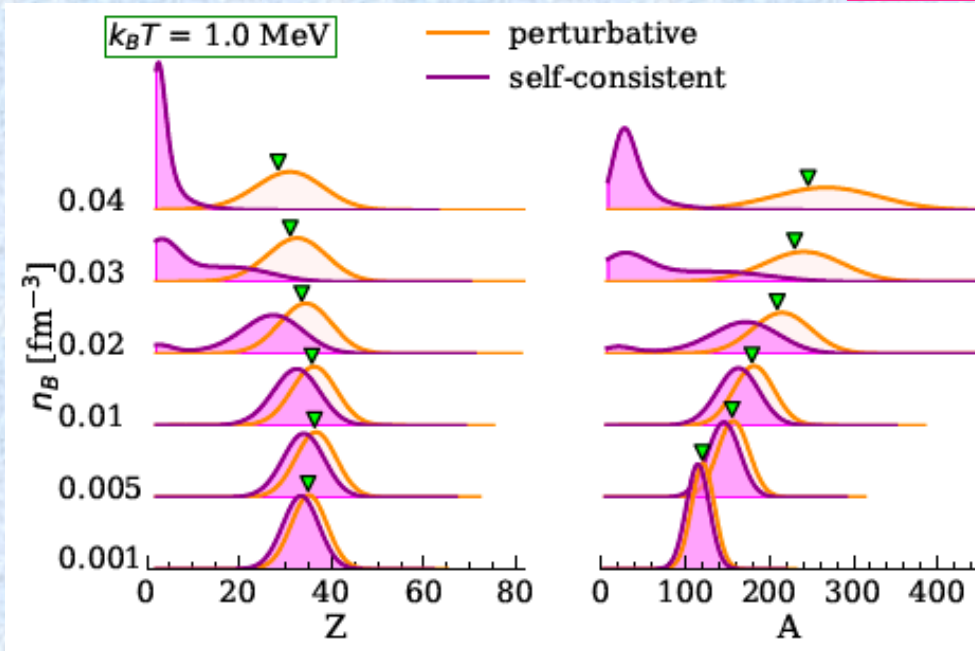


Pons et al., Nature Phys., 9, 431 (2013)
(see also Viganò et al., MNRAS 2013)



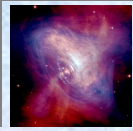
PNS crust (MCP): perturb. vs consistent

MM + CLDM



Dinh Thi et al., A&A 677, A174 (2023) – CLDM with BSk24

- OCP less reliable at higher density and temperature
→ (self-consistent) MCP
- appearance of bi-modal distribution → light clusters !
→ importance of light cluster already highlighted, e.g. Typel et al., PRC 2010; Hempel et al., PRC 2011

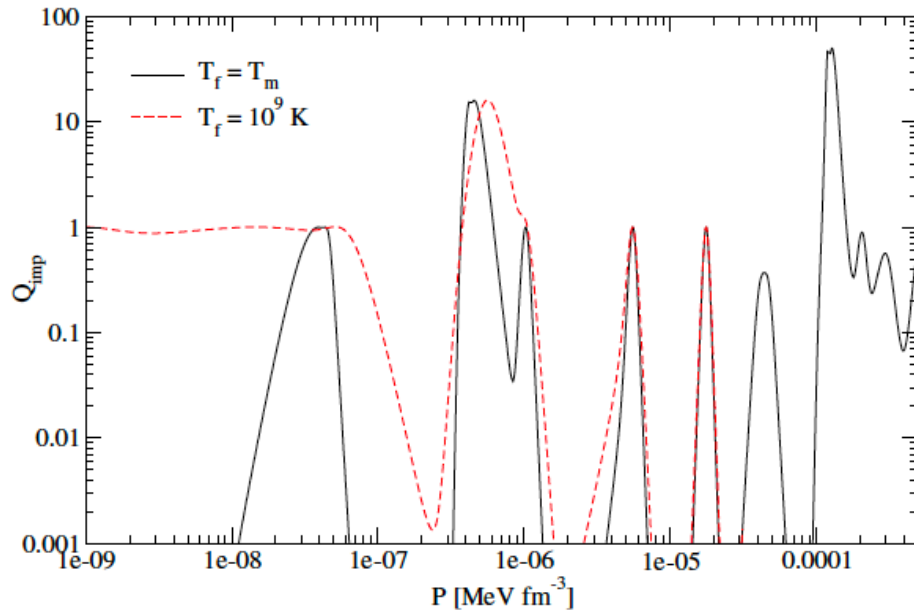


PNS crust (MCP): impurities

- ✓ Self-consistent calculations of $Q_{\text{imp}} = \langle Z^2 \rangle - \langle Z \rangle^2$

Outer crust

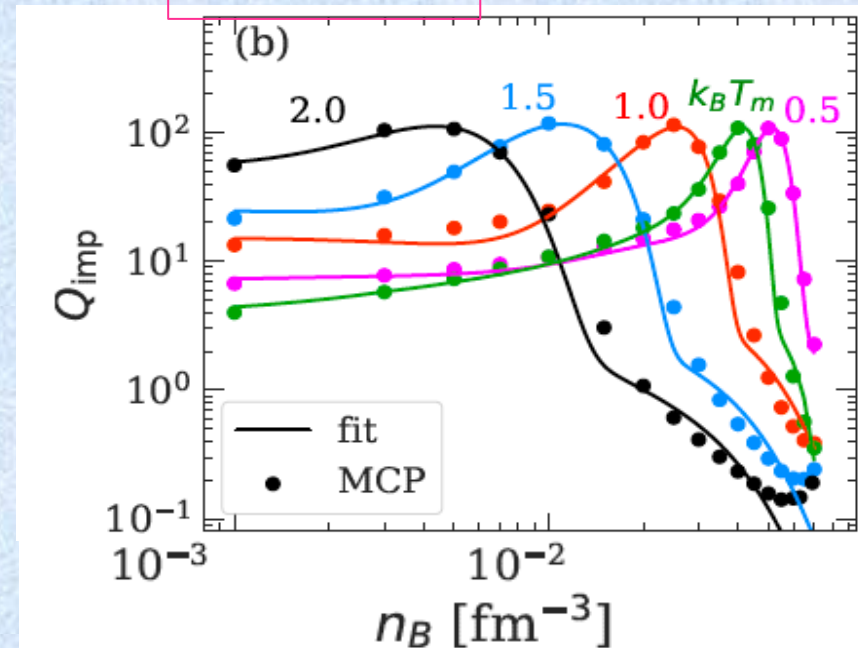
HFB-24 masses



Fantina et al., A&A 633, A149 (2020) – HFB-24
+ data on CDS

MM + CLDM

Inner crust



Dinh Thi et al., A&A 677, A174 (2023); see also Carreau et al., A&A 640, A77 (2020) – CLDM with BSk24
+ data on CDS

- consistent calculations of Q_{imp} throughout the crust
→ impact on transport coefficients / properties

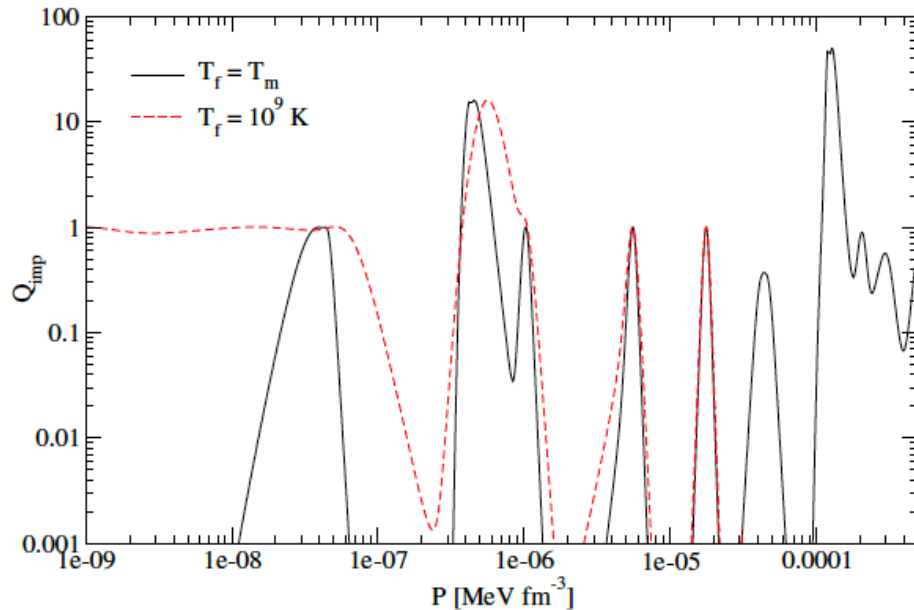


PNS crust (MCP): impurities

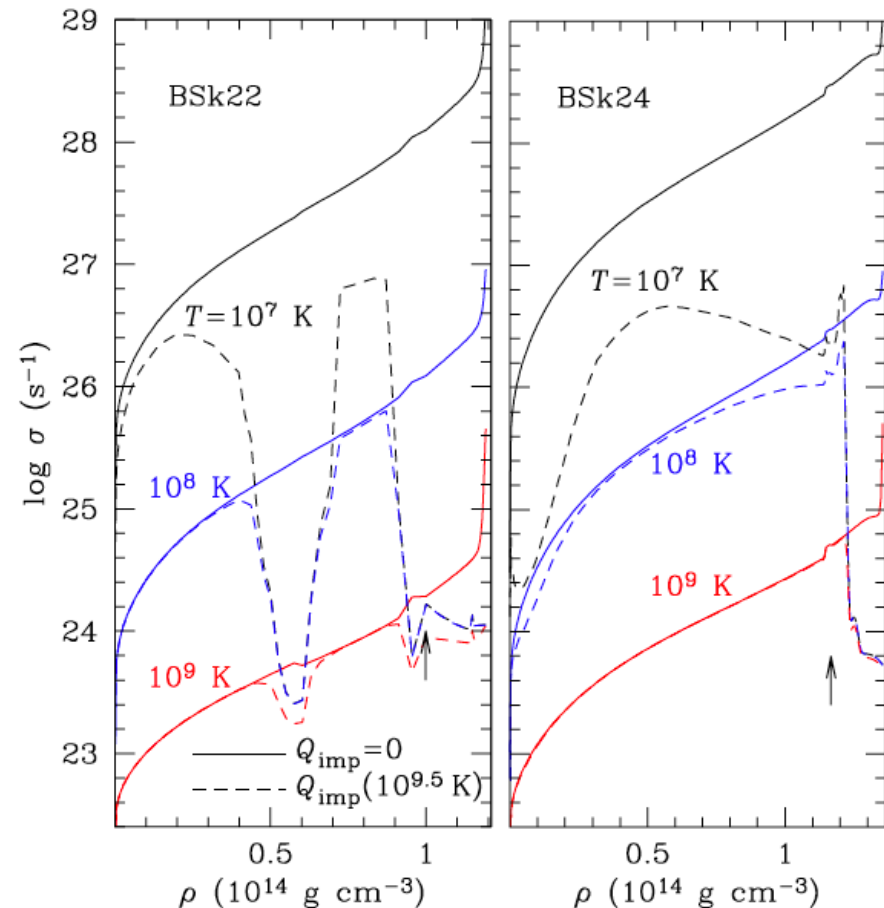
✓ Self-consistent calculations of Q_{imp}

Outer crust

HFB-24 masses



Fantina et al., A&A 633, A149 (2020) – HFB-24
+ data on CDS



Potekhin & Chabrier, A&A 645, A102 (2021)

- consistent calculations of Q_{imp} throughout the crust
- impact on transport coefficients / properties



PNS crust: outlooks

- * Crystallisation of (P)NS crust + (perturbative) MCP
- * Liquid (P)NS crust in self-consistent MCP $\rightarrow Q_{\text{imp}}$ (publicly available)

- ❖ Self-consistent MCP needed at higher ρ, T
 - Inclusion of pasta phase to be done (e.g. Pelicer et al. 2021)
 - $Q_{\text{imp}} \rightarrow$ transport coeff. $\rightarrow$ impact on cooling (e.g. Pelicer et al. 2023)
- ❖ T -dependent parametrisation of surface energy
 - Neutron “skin”, finite $T \rightarrow$ benchmark / fit with more microscopic calculations (collab. ETFSI IAA-ULB)