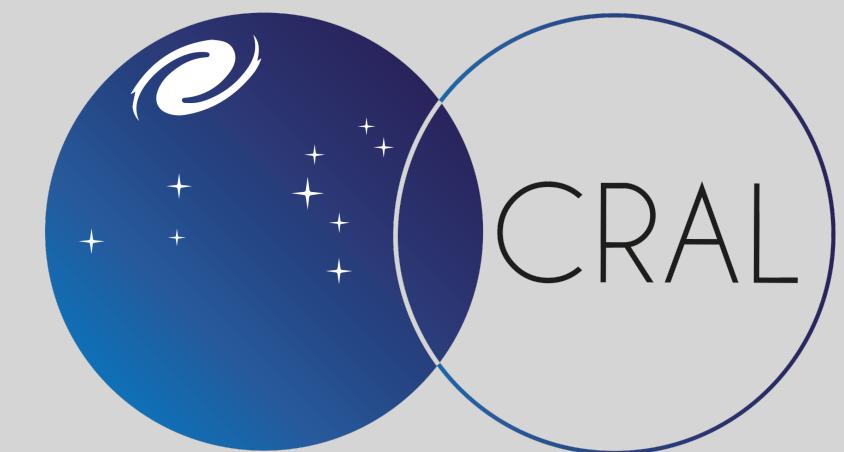
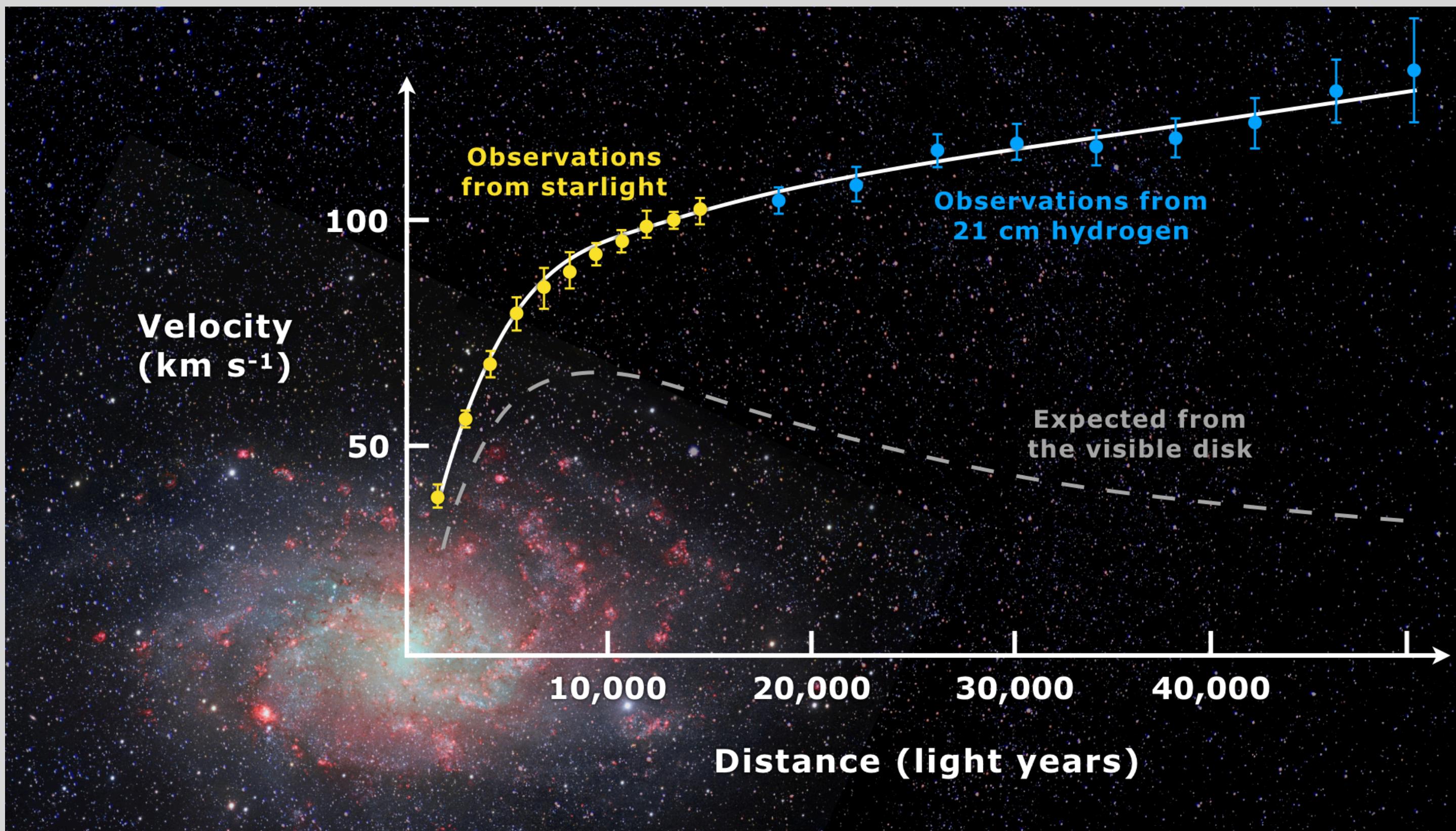


Constraints on Dark Matter from Galaxy Rotation Curves



CENTRE DE RECHERCHE ASTROPHYSIQUE DE LYON

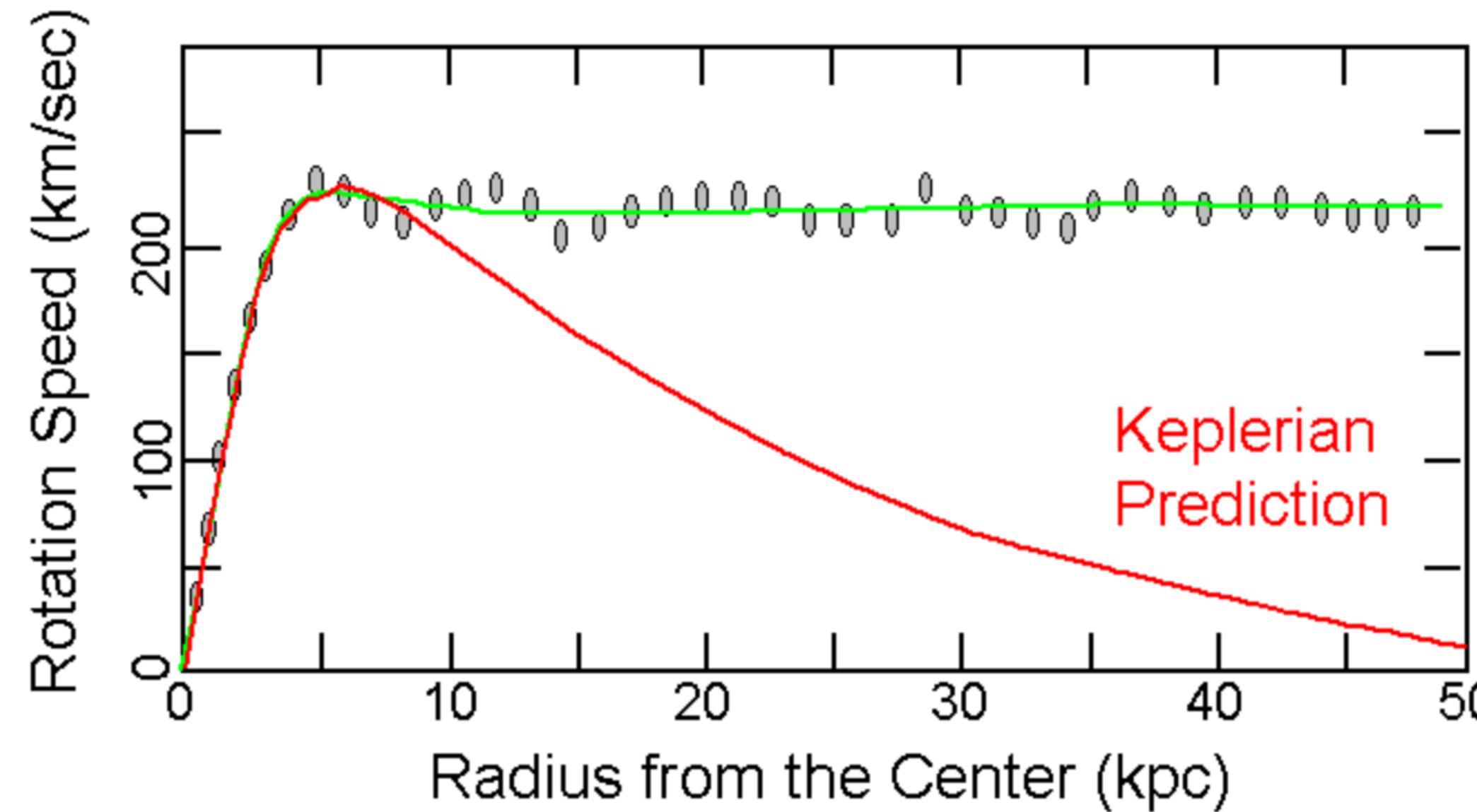
Outline

- 1. Early work**
- 2. Λ CDM**
- 3. Small scale problems of Λ CDM: core cusp problem & diversity of rotation curves**
- 4. Solutions in Λ CDM**
- 5. How to test this observationally?**
- 6. Results from observational studies**
- 7. Solutions beyond Λ CDM**
- 8. Results from observational studies using alternative Dark Matter models**
- 9. Outlook**

Early Work

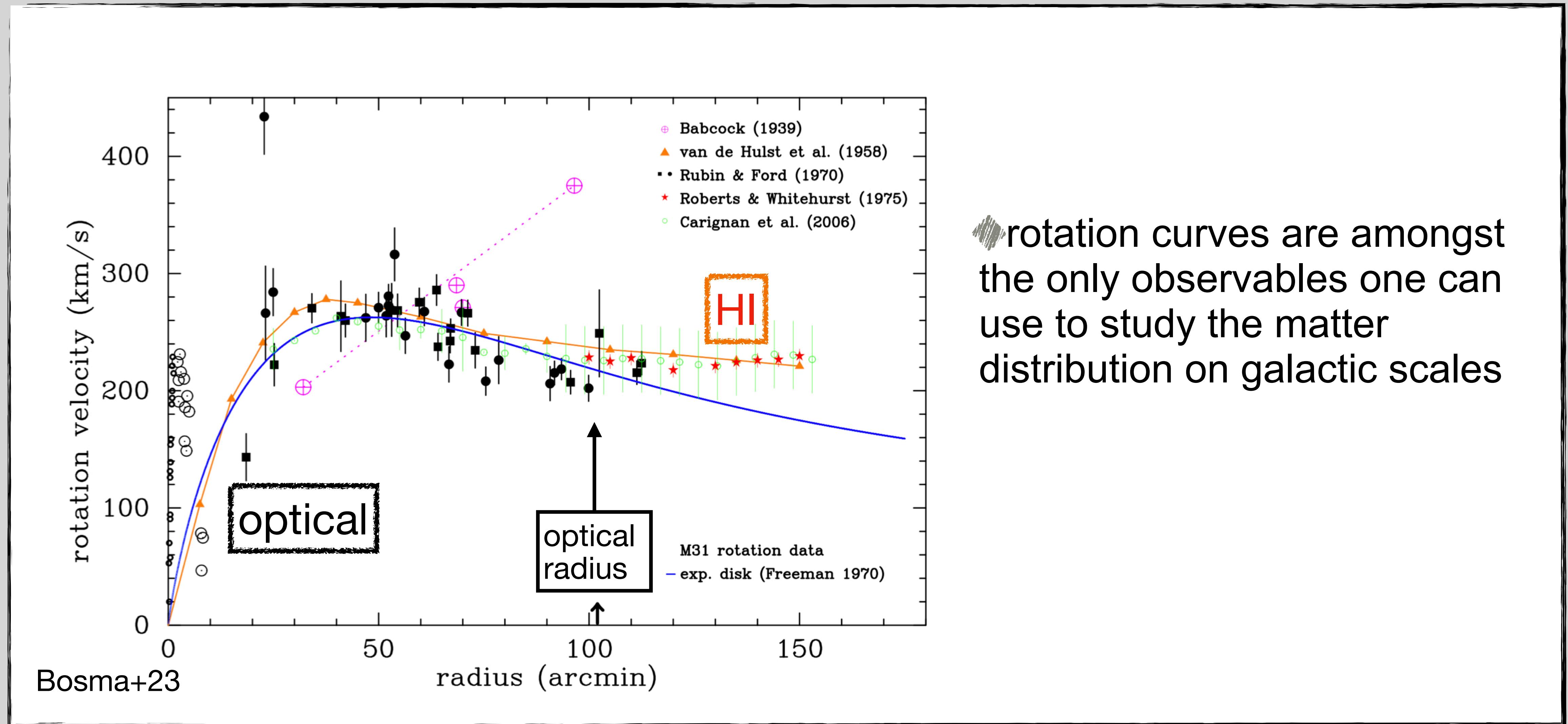
“mass discrepancy problem” in galaxies and cosmology has been around since ~1930 (Oort 1932 and Zwicky 1933).

Observed vs. Predicted Keplerian



► ‘dark matter’ entered mainstream research in ~1970 when observations revealed that galaxy rotation curves remain flat at large galactocentric distances (van de Hulst +1957, Freeman 1970, Rubin & Ford 1970)

Early Work



Dark Matter Candidates

Early work

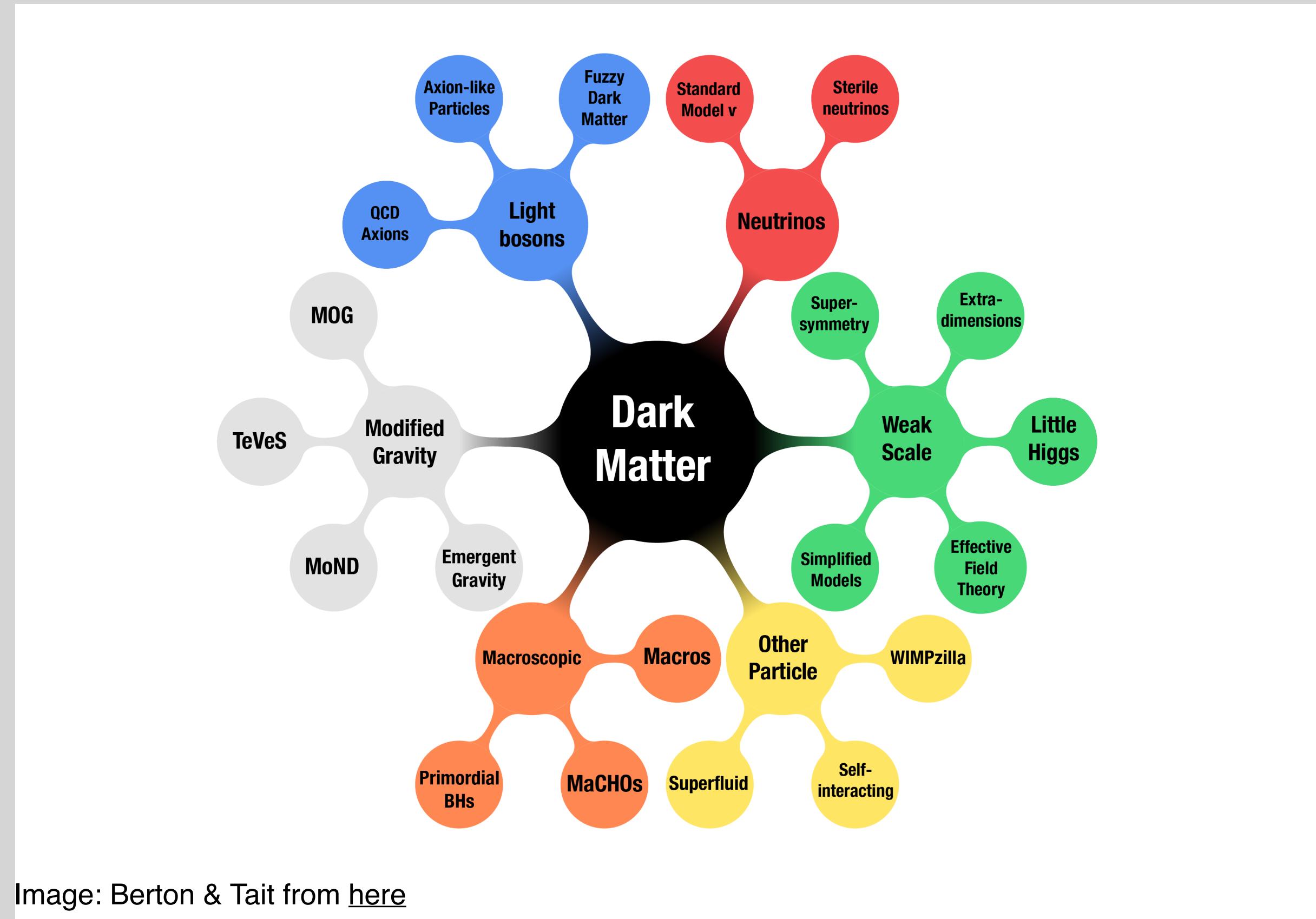
- suggestions as to the identity of the unseen matter include **massive neutrinos** (Cowsik & McClelland 1972), **faint stars** (Ostriker, Peebles & Yahil 1974), **black holes** (Truran & Cameron 1971), and **comets** (Tinsley & Cameron 1974).

Dark Matter Candidates

Early work

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Nowadays



Dark Matter Candidates

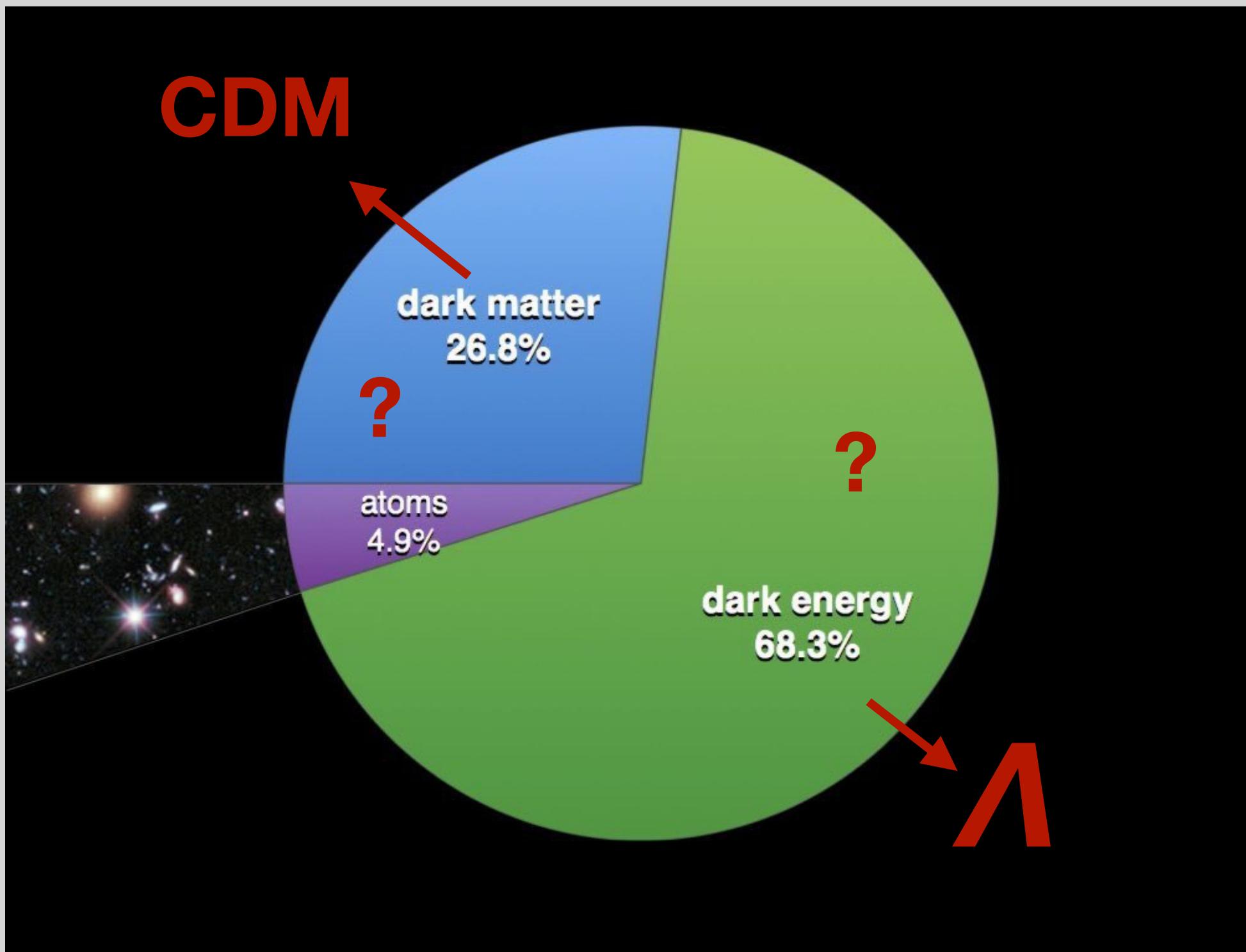
Early work

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Nowadays



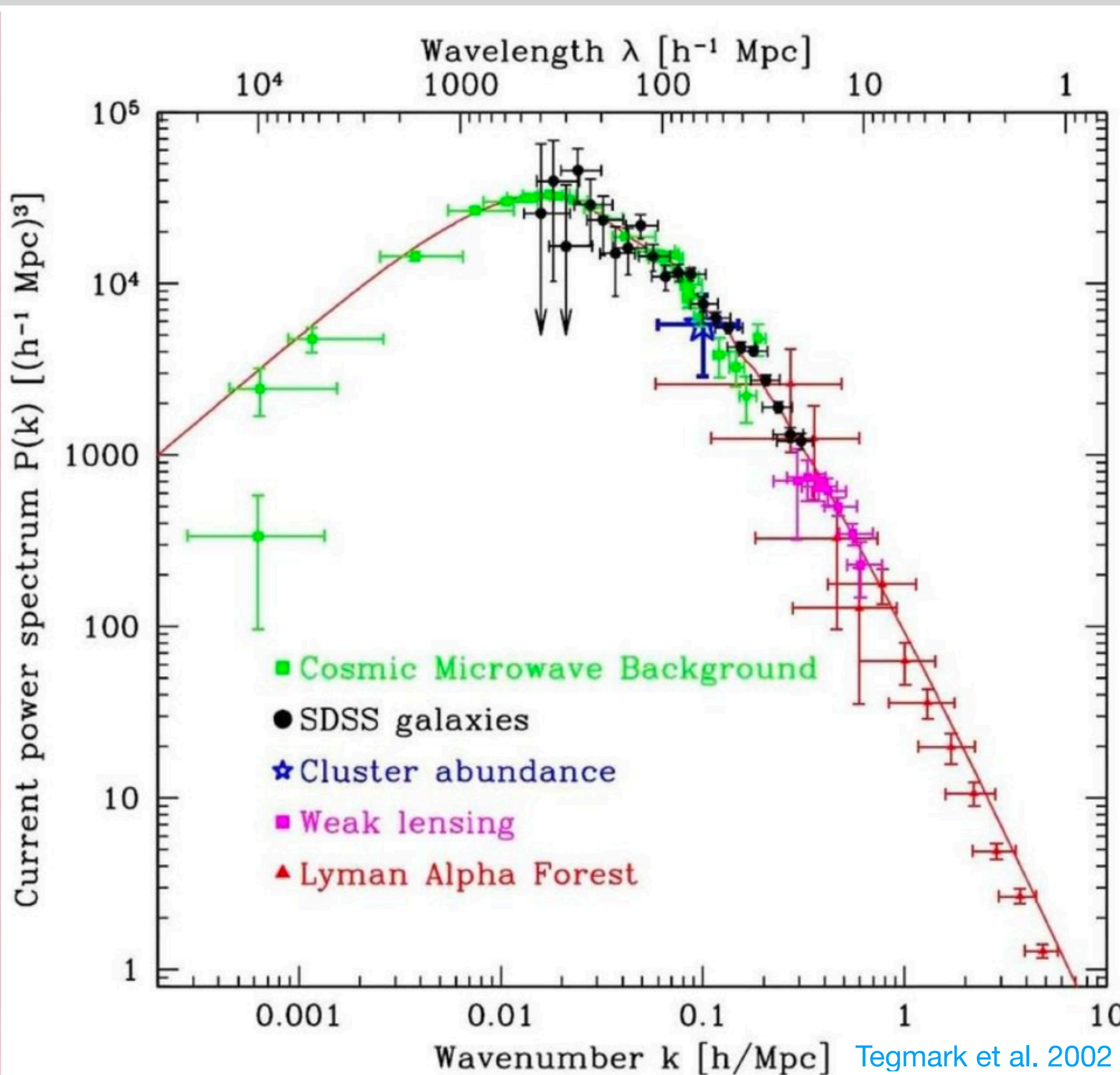
- 3 main components:



- provides a good fit to cosmological observations:

- expansion history of the Universe as inferred from Supernovae type Ia (Riess +1998)
- the matter power spectrum (Gil-Marin+2015)
- the Cosmic Microwave Background data (Planck collaboration, 2020)
- Baryon Acoustic Oscillation (Ross+2015)

Λ CDM

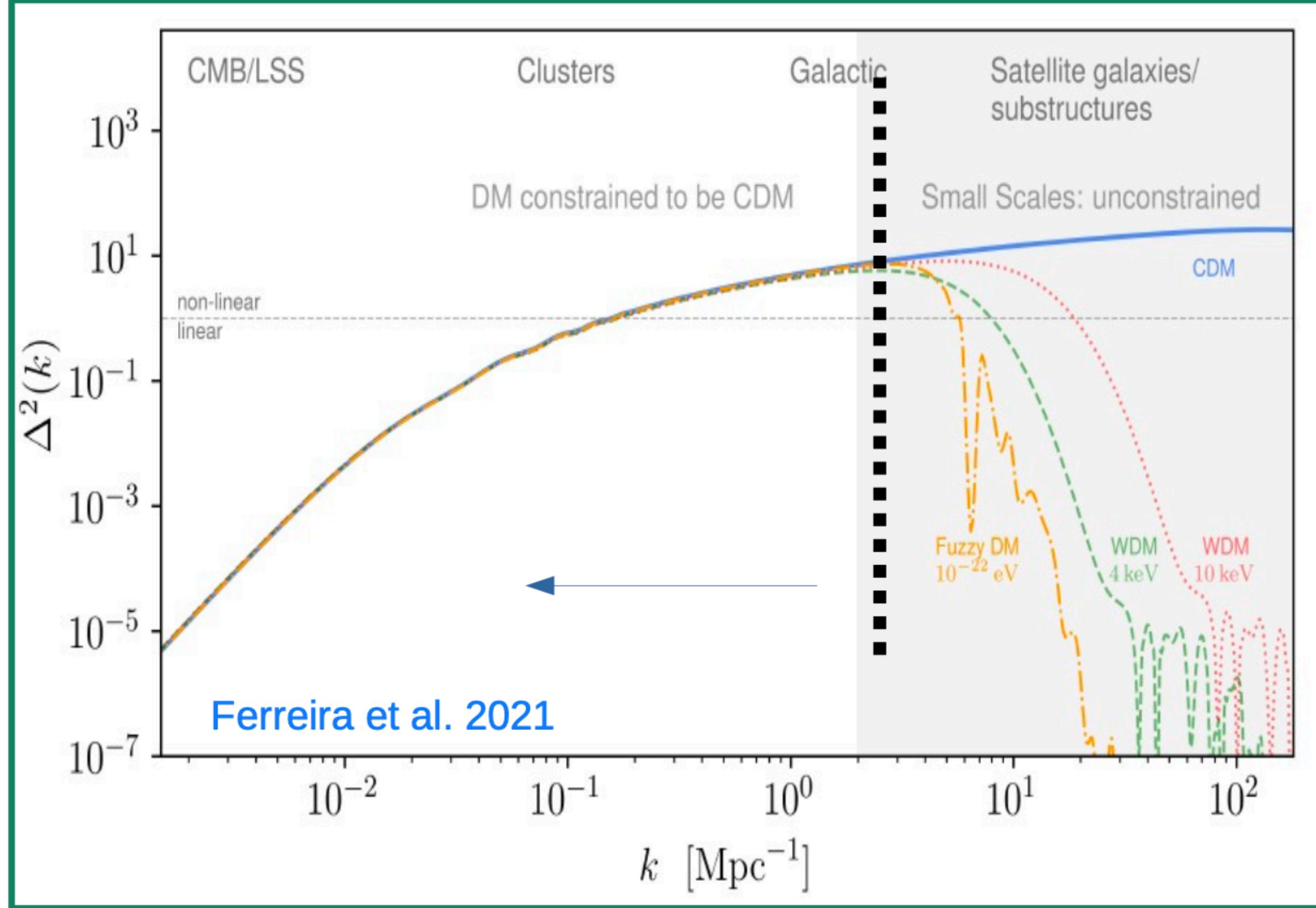


Large scales: Λ CDM is a big success

Large scale ($>>1$ Mpc):

Small scale (<1 Mpc):

A big success



But baryons
Can have an
impact

Small scales: retain information about possible deviations from CDM

On small scales: small scale problems of Λ CDM
(Bullock+2017, Sales+2022)

Λ CDM Tensions with Dwarf Galaxies

No tension

Uncertain

Weak tension

Strong tension

Missing satellites

M_\star - M_{halo} relation

Too big to fail

Diversity of rotation curves

Core-cusp

Diversity of dwarf sizes

Satellite planes

Quiescent fractions

Sales+2022

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(Bullock+2017, Sales+2022)

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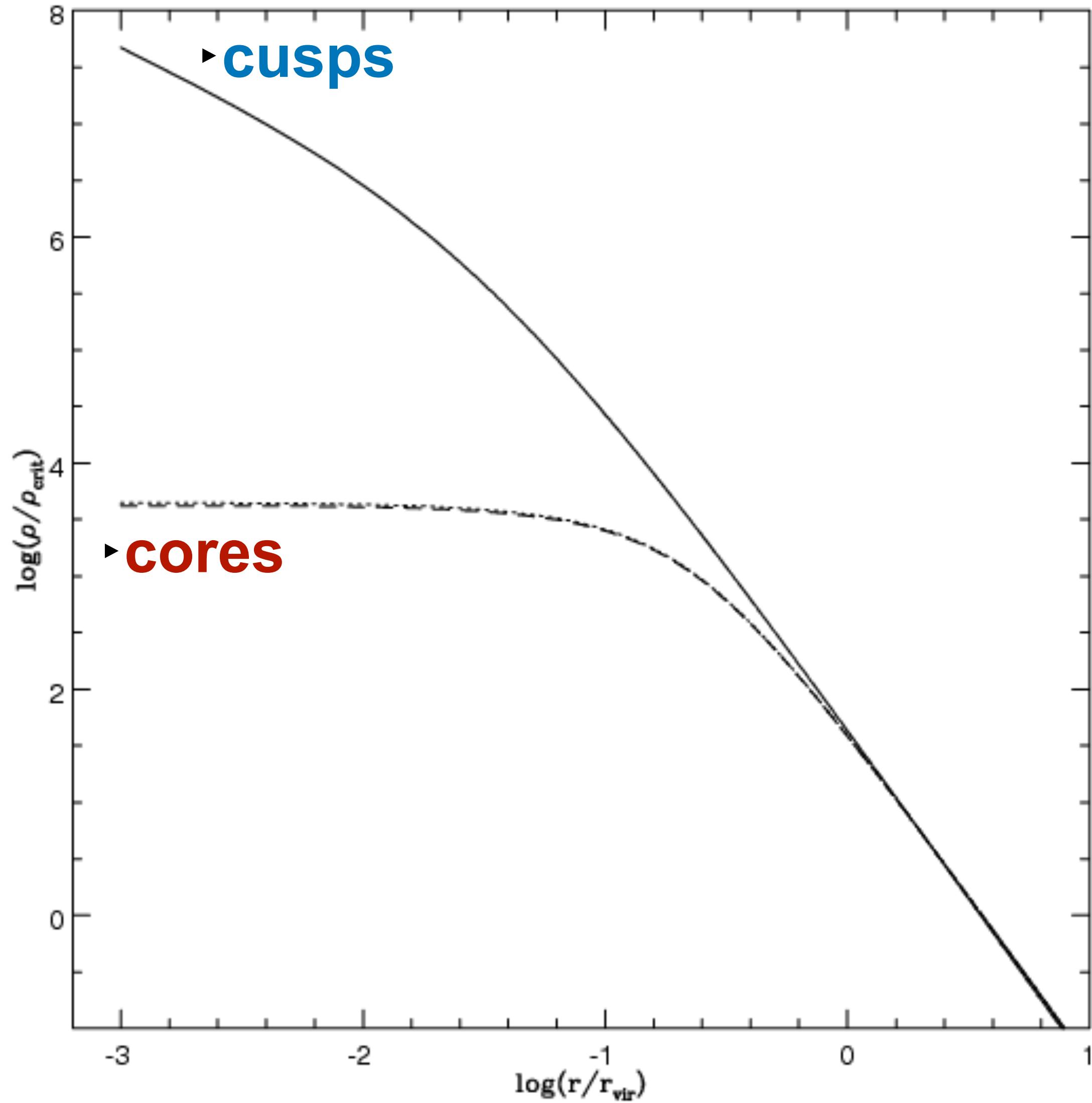
Diversity of dwarf sizes

Satellite planes

Quiescent fractions

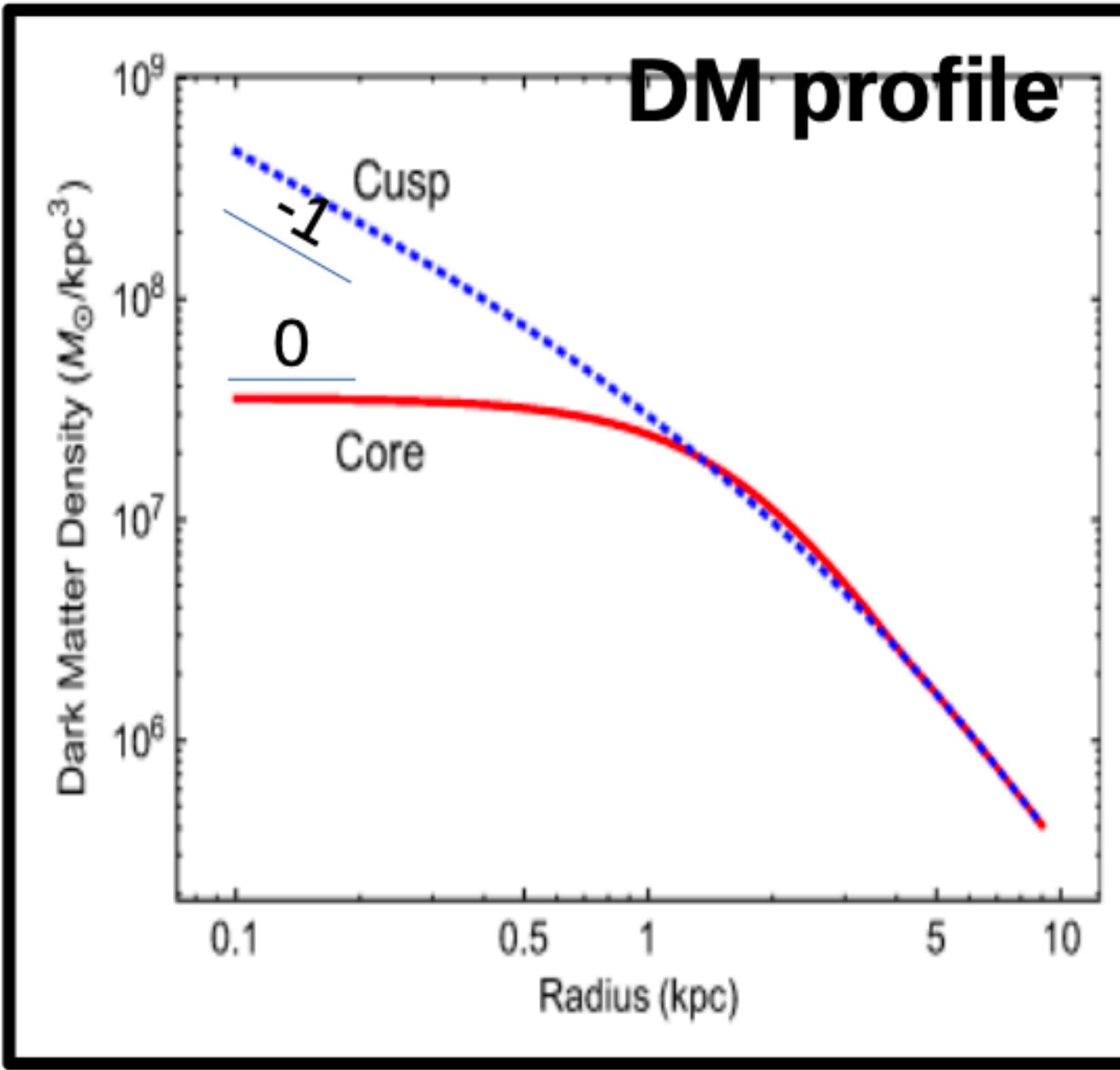
Sales+2022

Core - cusp problem

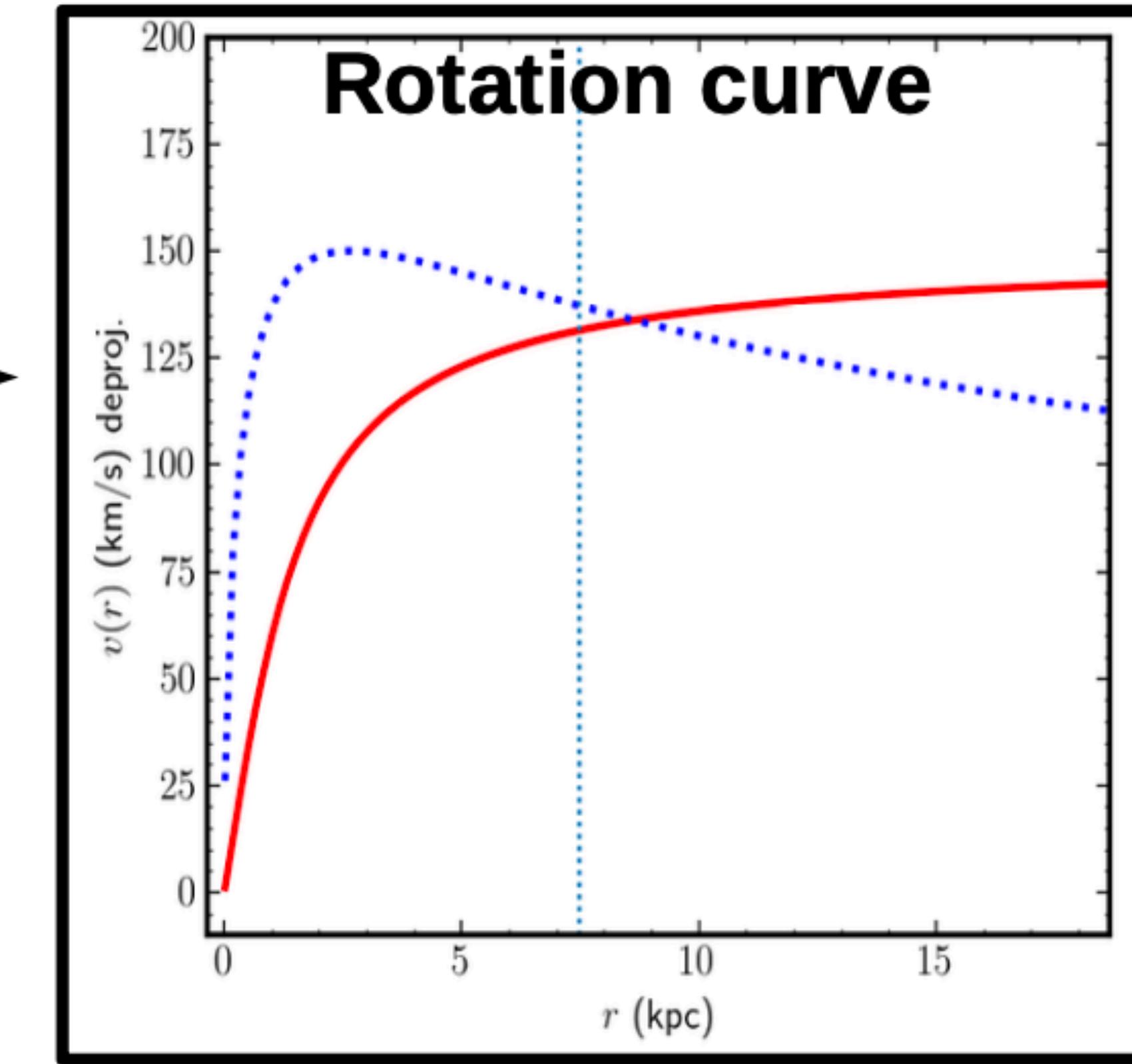


- N-body simulation predicts **cuspy** DM profiles (NFW, [Navarro+1997](#))
- Rotation curves of low-surface brightness galaxies (e.g. [de Blok et al. 2001](#)) indicate constant-density **cores**

Core - cusp problem



$$v_c = \sqrt{\frac{GM}{r}}$$

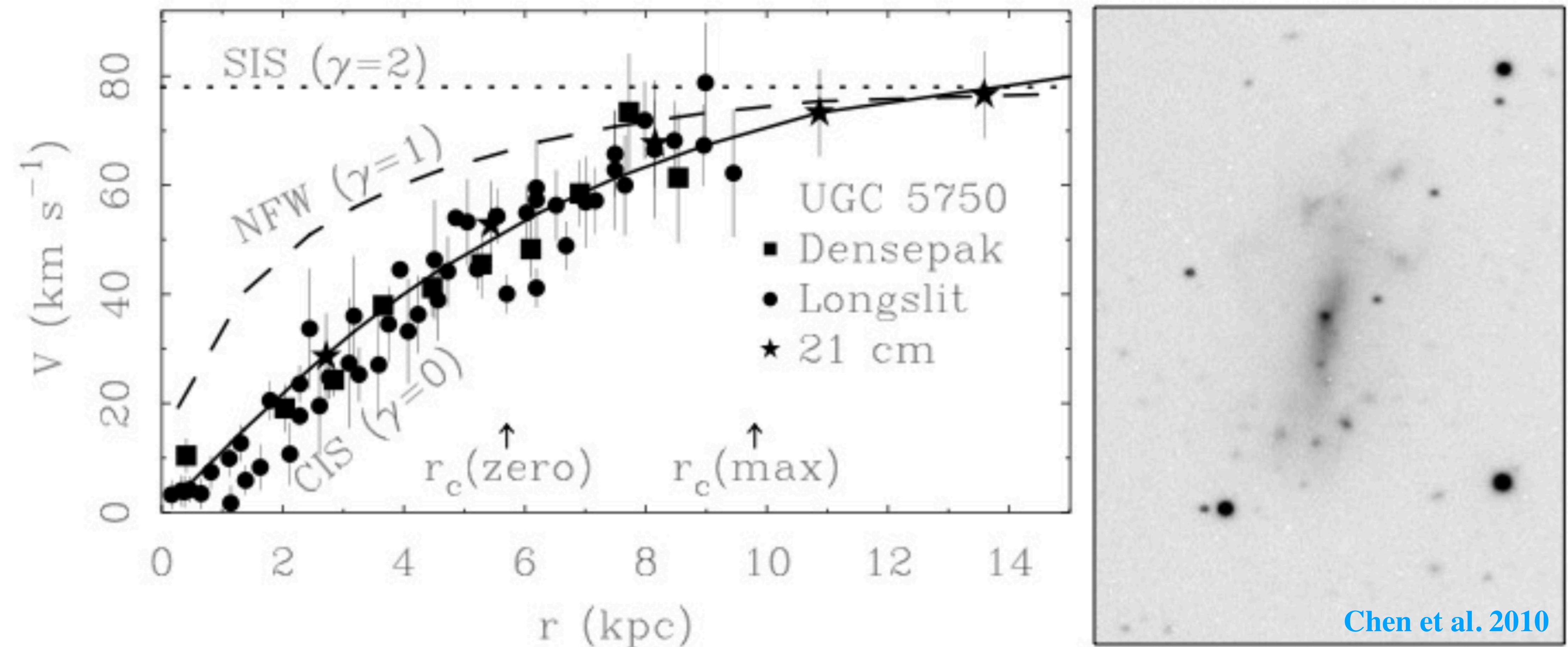


• A core on <1kpc → impact on several kpc

→ the curvature of $v(r)$ relates to inner DM density profiles (CDM, SIDM, FDM, WDM, etc)

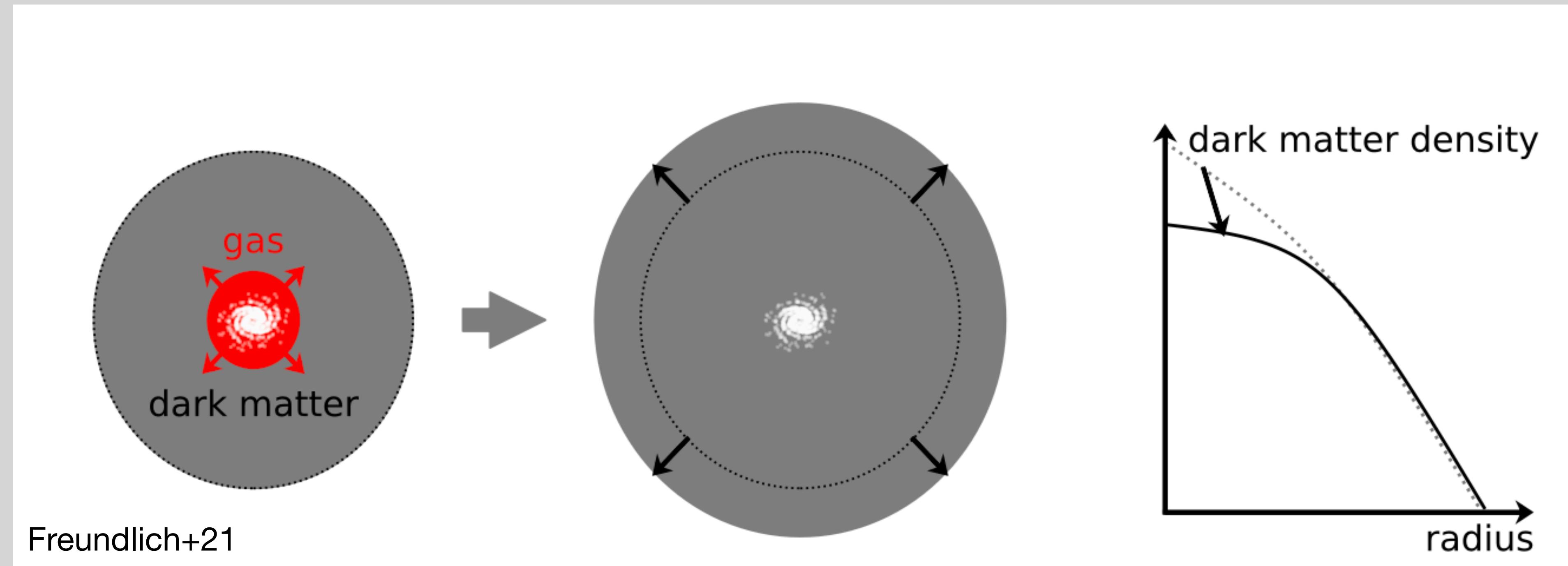
Examples:

Cored galaxy UGC5750; z~0.013



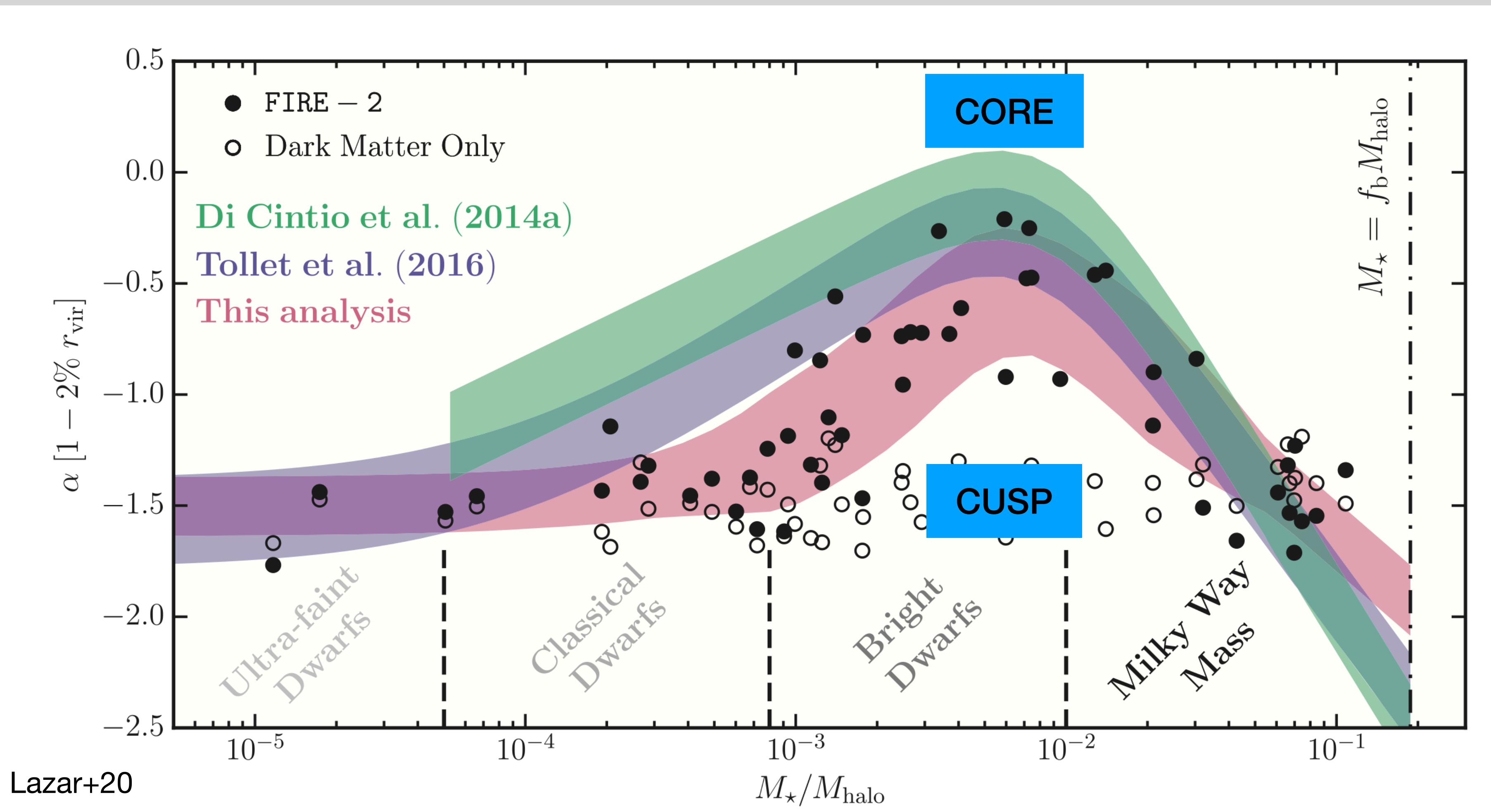
Core-cusp problem: solutions in Λ CDM

- **baryonic processes to the rescue:** stellar feedback, AGN feedback, central stellar bar, infalling clumps
- rapid potential fluctuations



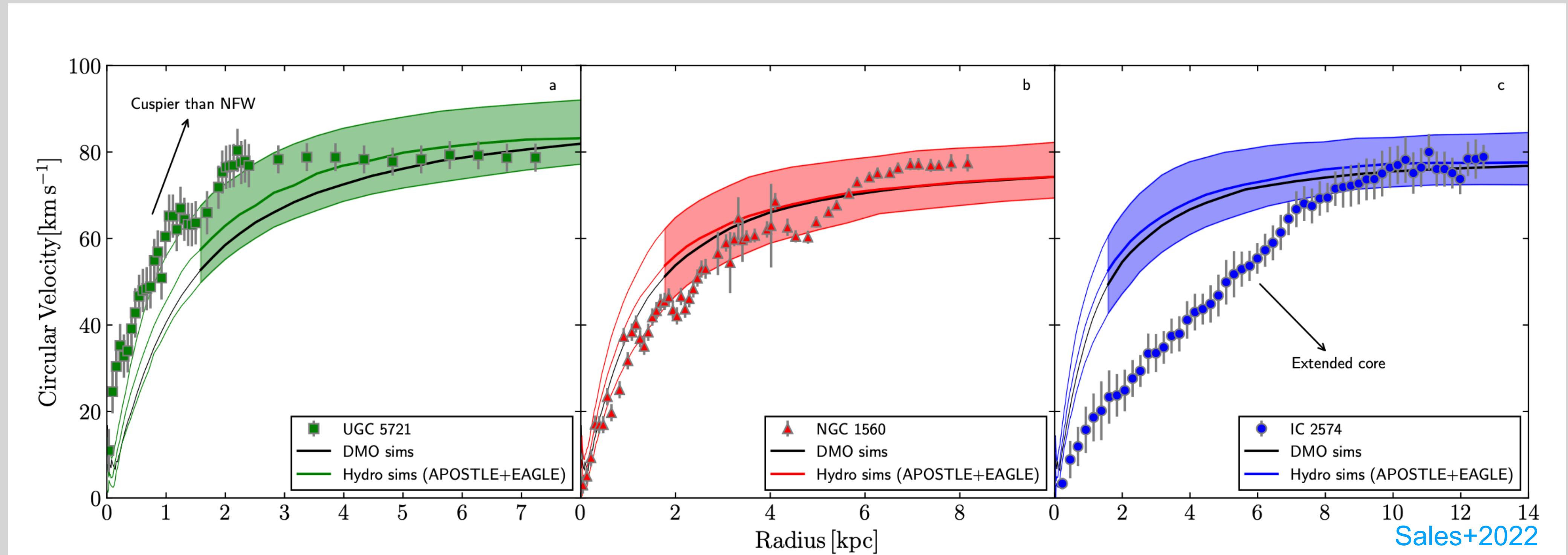
Core-cusp problem: solutions in Λ CDM

Hydrodynamical simulations with stellar feedback



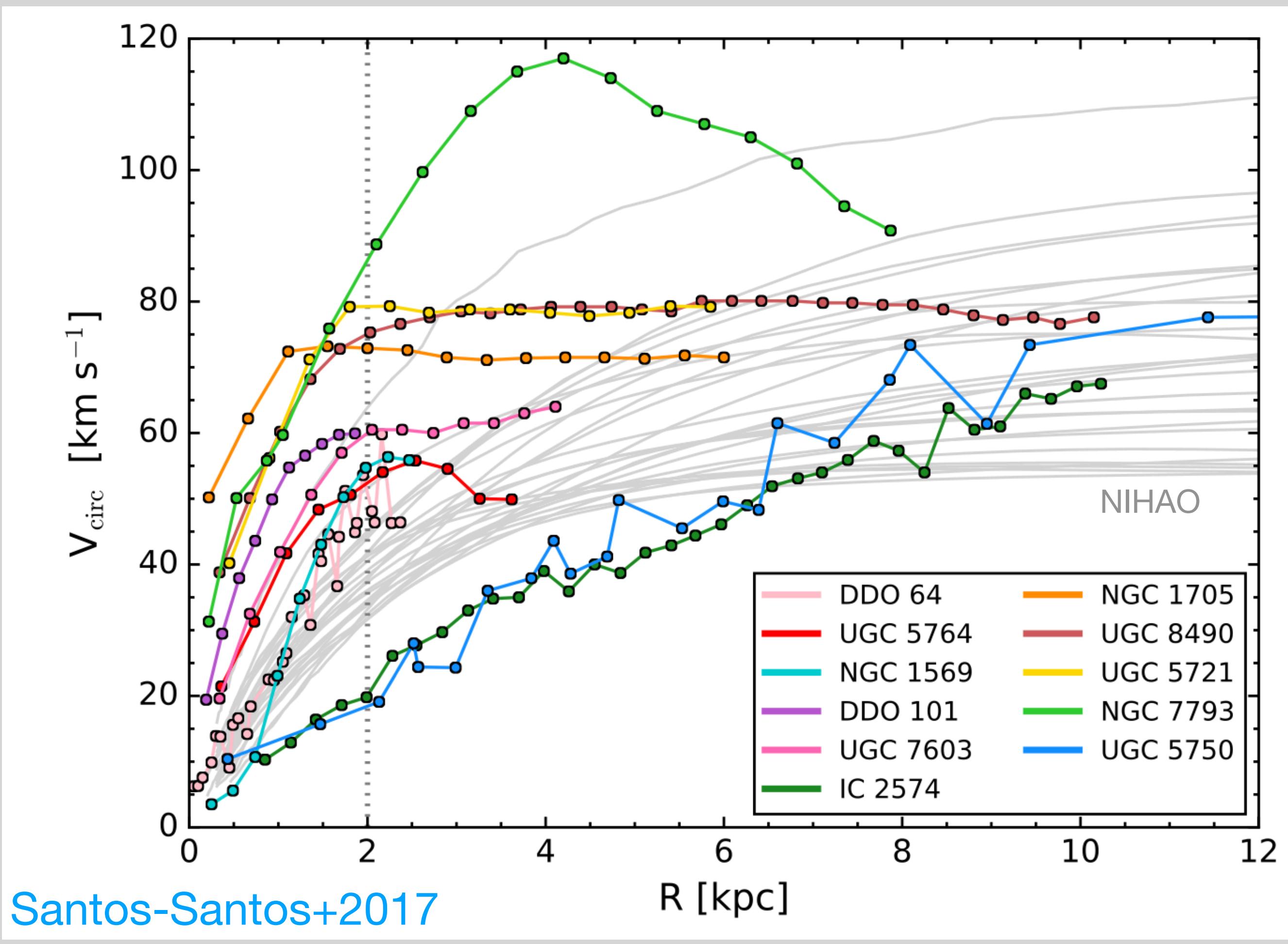
► core formation most efficient for galaxies with $9 < \log(M^*/M_{\odot}) < 10$

Diversity of Rotation Curves problem:



- ▶ in dark matter only simulations, haloes have a universal **cuspy** density profile that results in self-similar rotation curve shapes
- ▶ observed dwarfs of similar masses show a large diversity in the rotation curve shapes

Diversity of Rotation Curves: solutions in Λ CDM



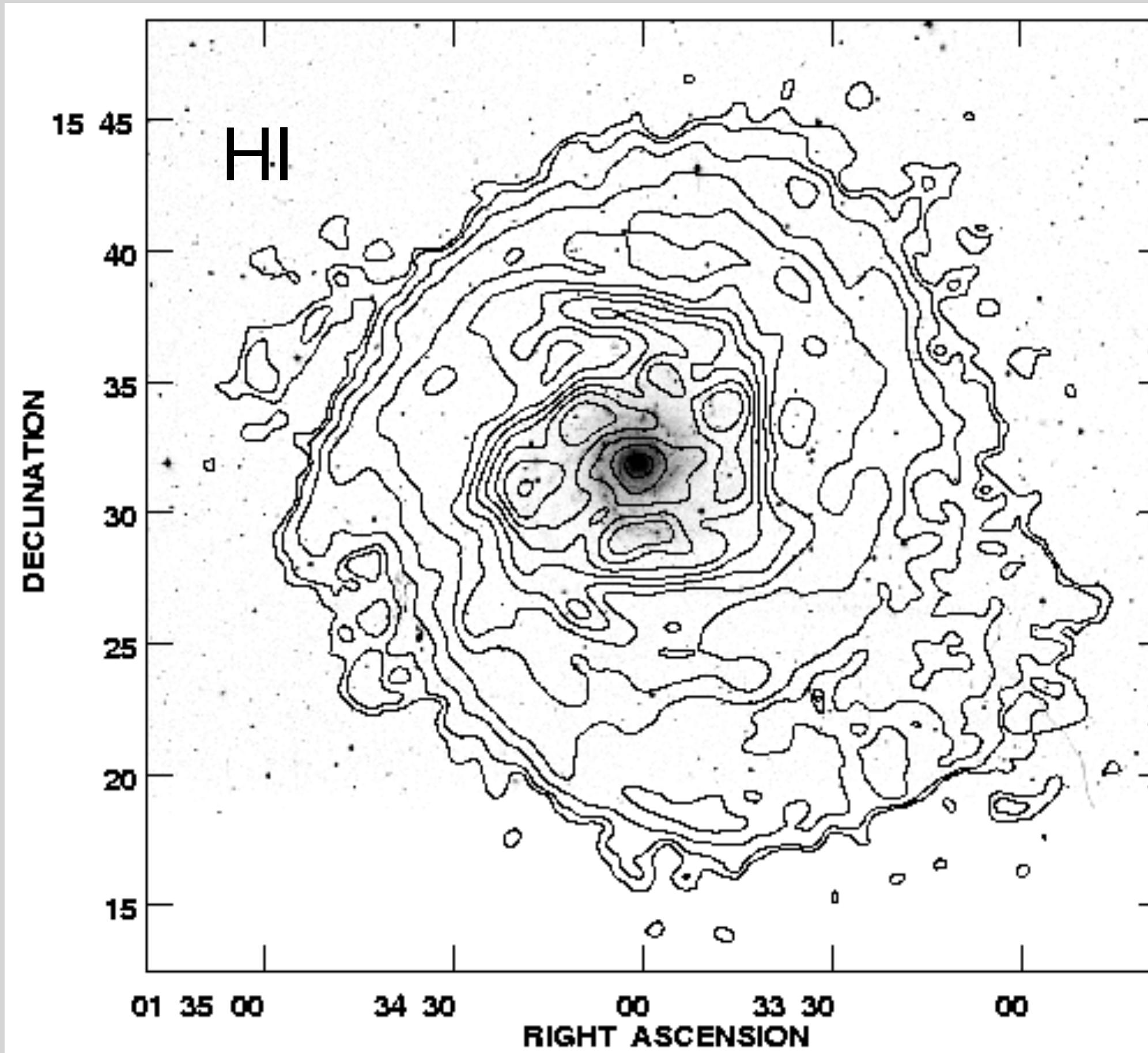
► baryonic processes to the rescue

► Some hydrodynamical Λ CDM simulations ~reproduce the observed diversity

How to test this observationally?

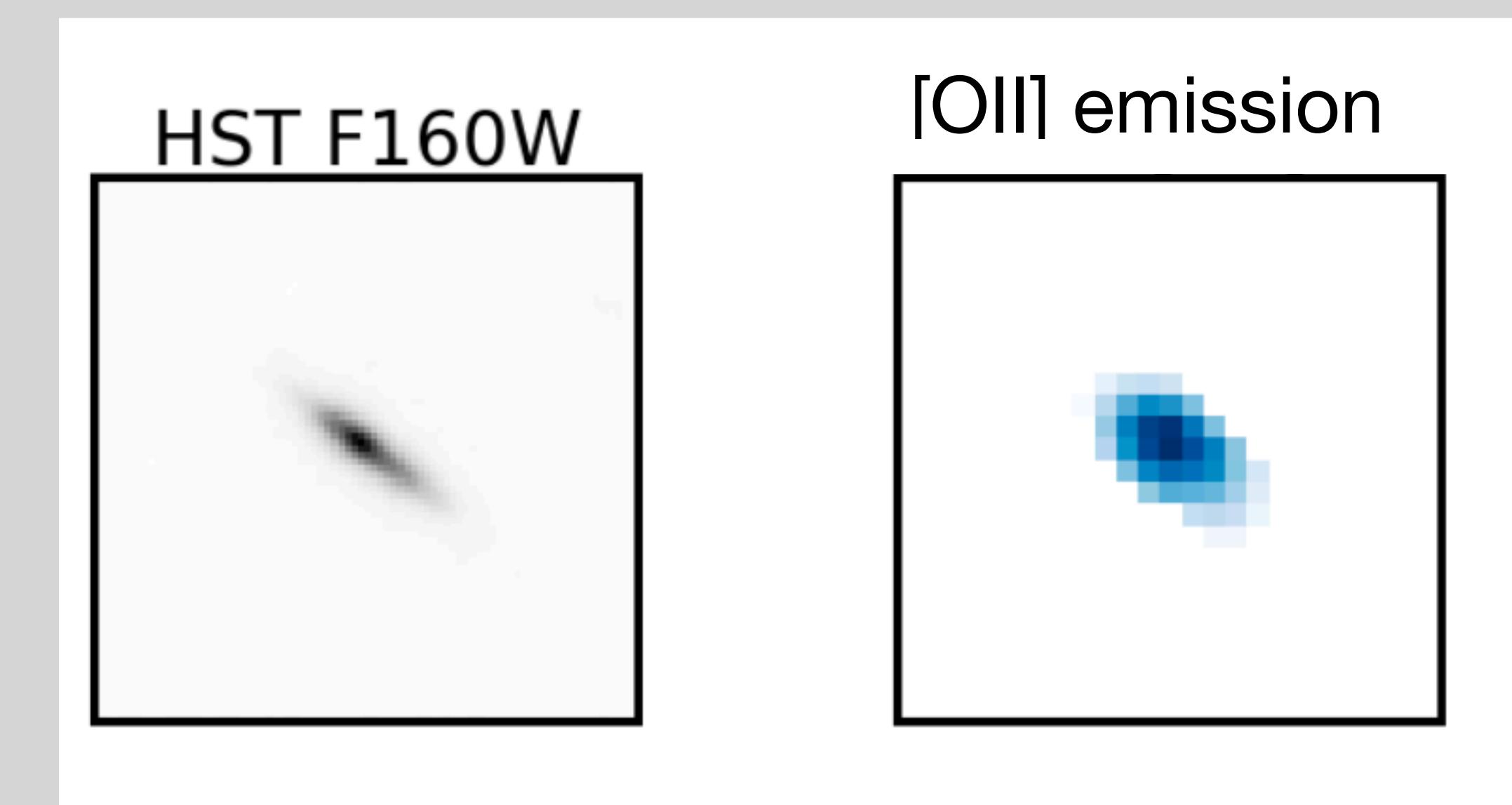
- ▶ Need a kinematic tracer at large galactocentric radii, beyond $2 \times R_e$

$z=0$



Kamphuis and Briggs 1992

$z \sim 1$



optical

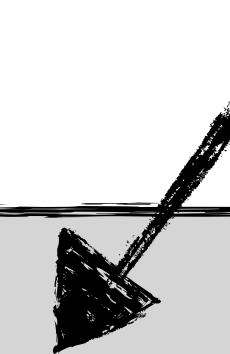
How to test this observationally?

- ▶ Need a kinematic tracer at large galactocentric radii, beyond $2 \times R_e$
- ▶ Precise determination of the rotation curves, from the innermost to the outermost parts of galaxy discs

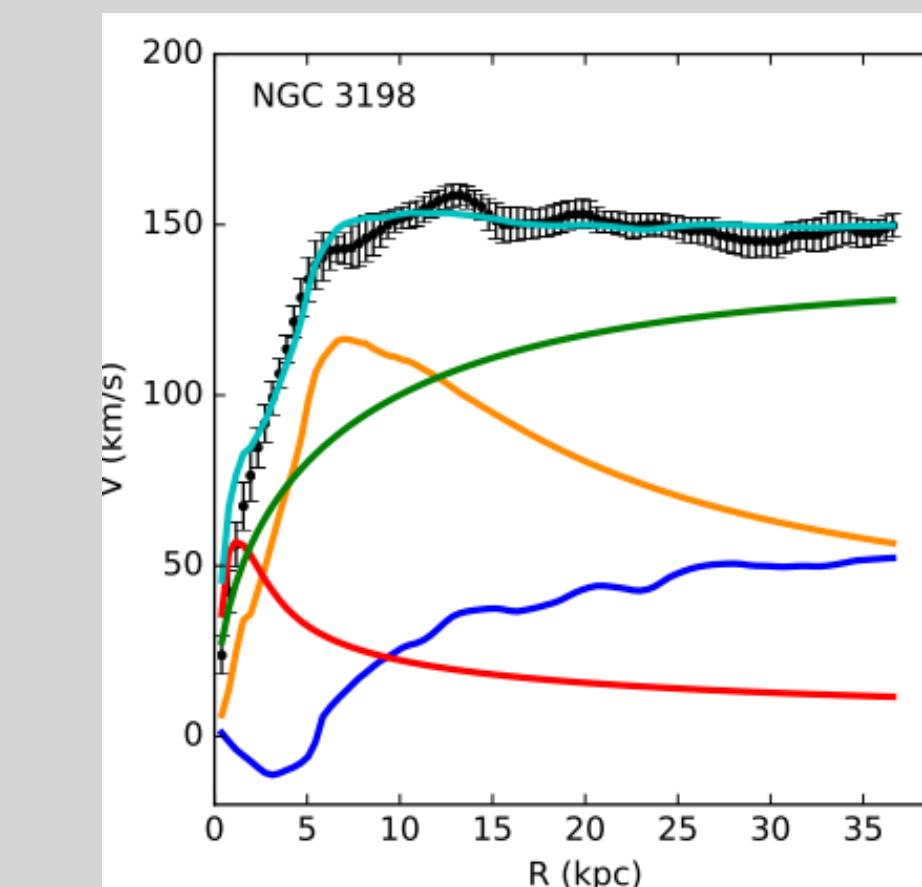
Using 1D methods for disk-halo decomposition:

Tilted ring method (e.g. Rogstad, Lockhart & Wright 1974, Schoenmakers 1999, Simon et al. 2003, Krajnović et al. 2006, Spekkens & Sellwood 2007; Sellwood & Sánchez 2010, Di Teodoro et al. 2015):

- ▶ **Assumptions:** the galaxy's gas is confined to a series of concentric rings, each with its own orientation and rotational velocity
- ▶ **Fitting the Velocity Field:** for each ring at radius r , fit for rotational velocity, inclination, position angle
- ▶ **Reconstructing the Rotation Curve:** the rotation curve is extracted from the fitted rotational velocities $V(r)$ for each ring

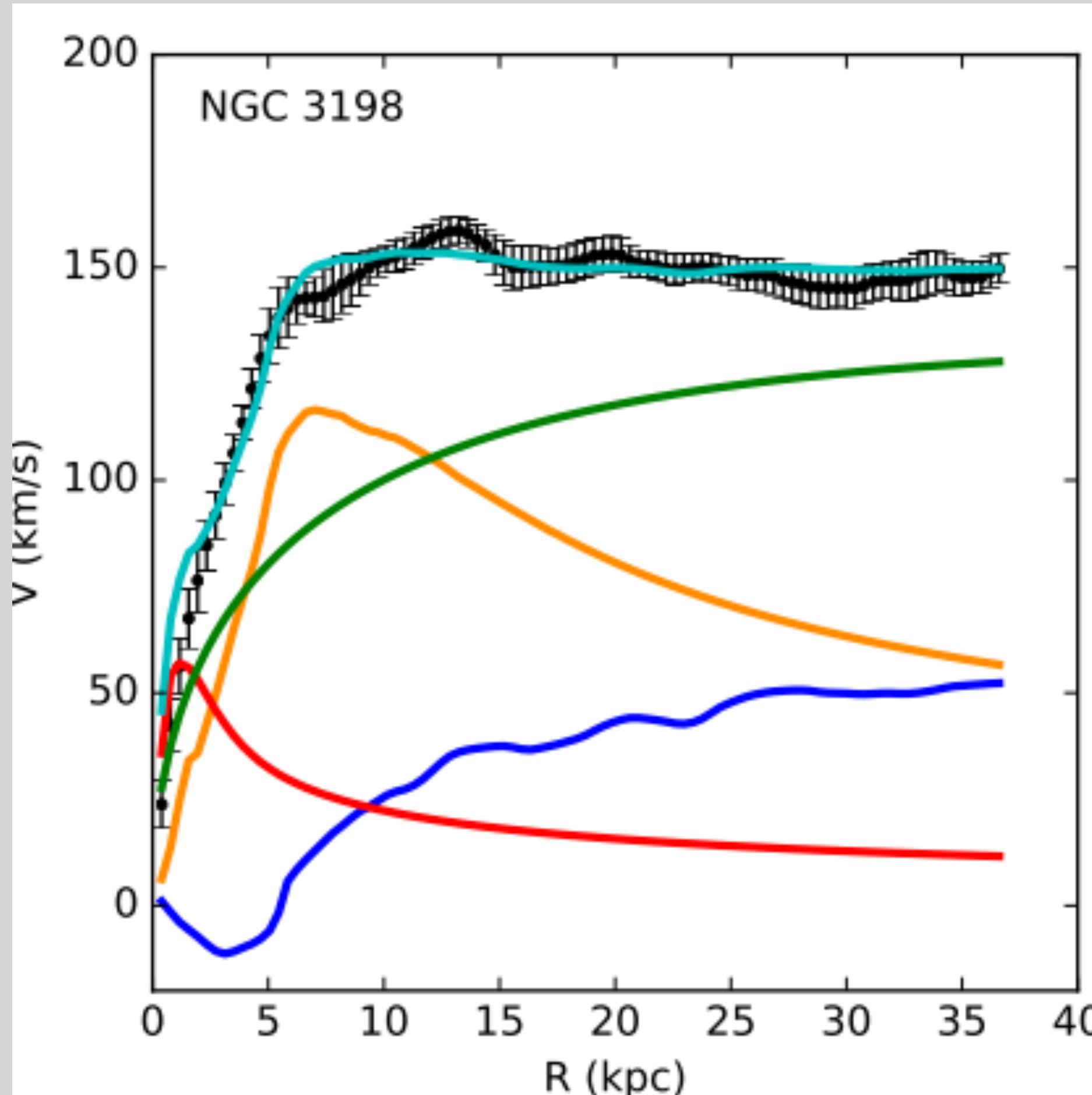


The resulting 1D rotation curve is used for the decomposition



How to test this observationally at $z>0$?

► At $z=0$: « easy » ?



► At $z=1$: « hard » ?

- Galaxies have small angular sizes
- Outer disks are too faint

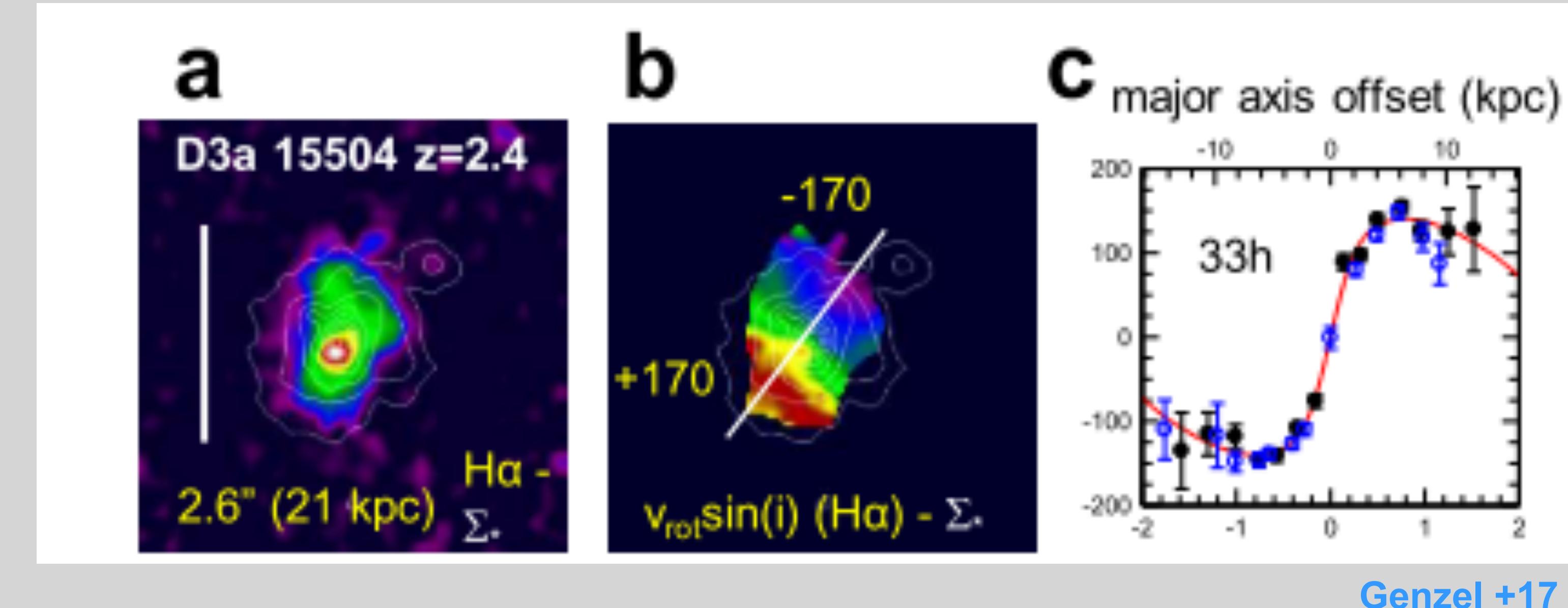
How to test this observationally at z>0?

► At z=1: « hard » ?

- Galaxies have small angular sizes
- Outer disks are too faint

There are only 3 options:

1. Using deep observations (10h-40h exposure times)



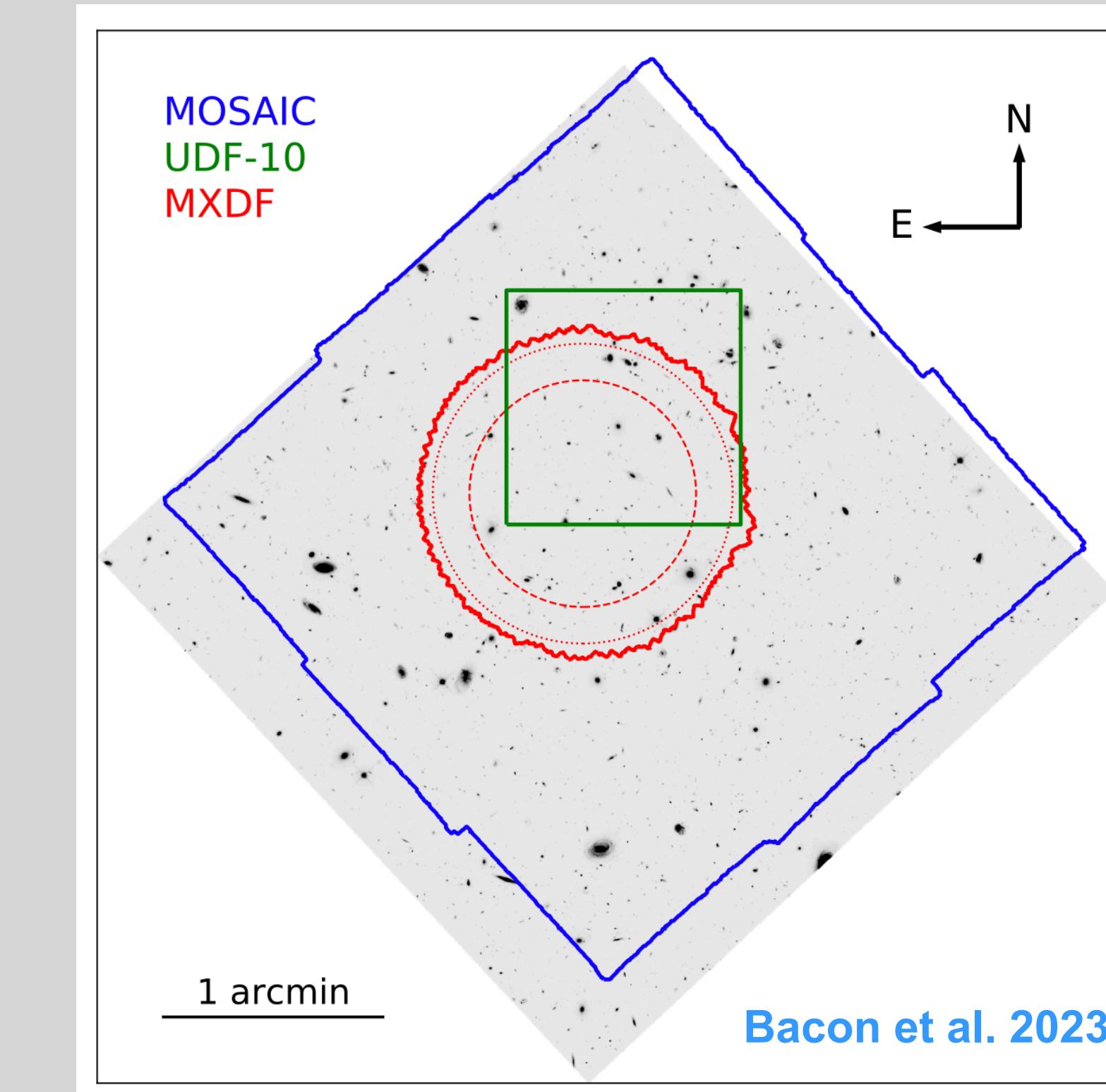
How to test this observationally at $z>0$?

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- Galaxies have small angular sizes
- Outer disks are too faint

There are only 3 options:

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2. Using very deep observations (140h exposure times)



How to test this observationally at $z>0$?

► At $z=1$: « hard » ?

- Galaxies have small angular sizes
- Outer disks are too faint

There are only 3 options:

1. Using deep observations (10h-40h exposure times)
2. Using very deep observations (140h exposure times)
3. Use all information available (3D forward modelling)

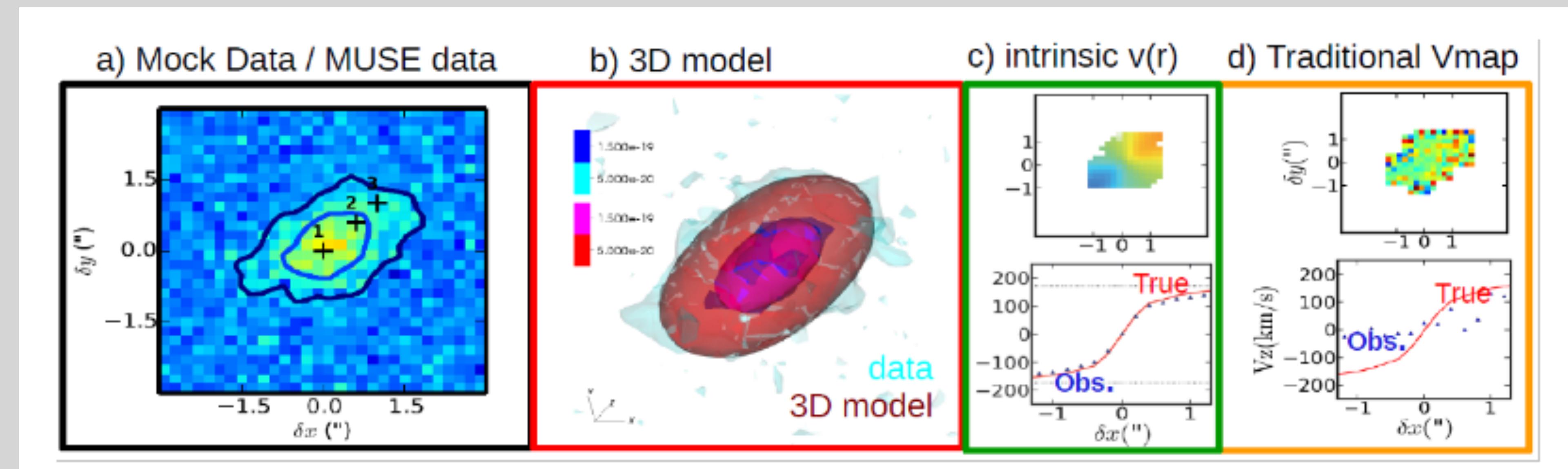


Bouché et al. 2015

Using 3D forward modelling for disk-halo decomposition



Bouché et al. 2015



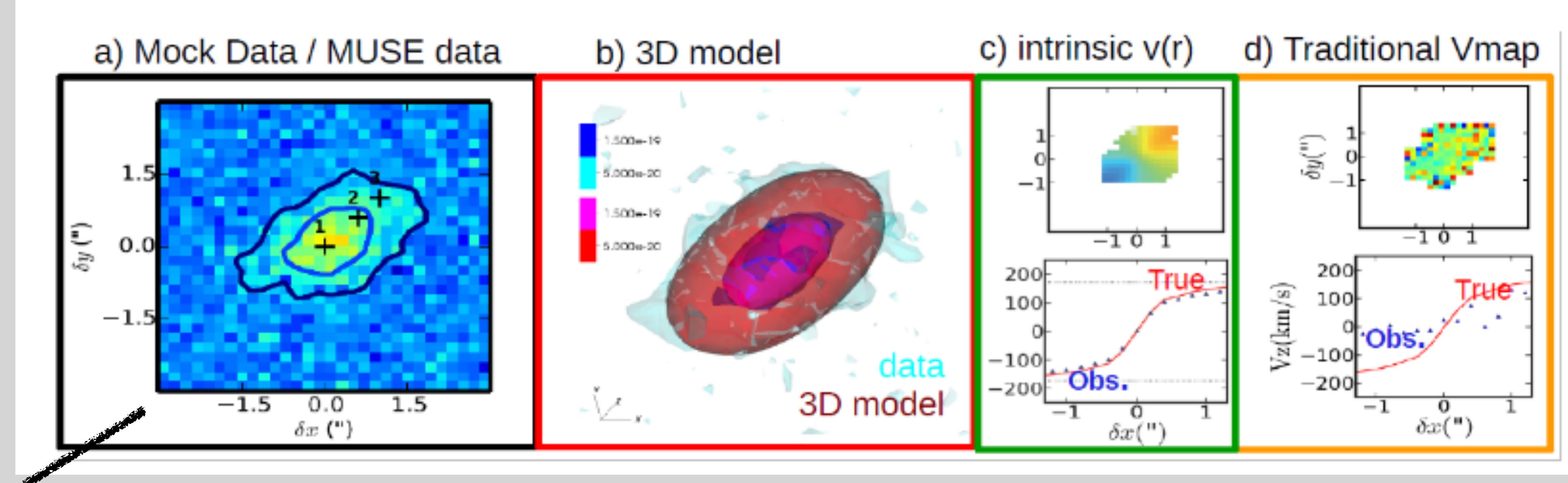
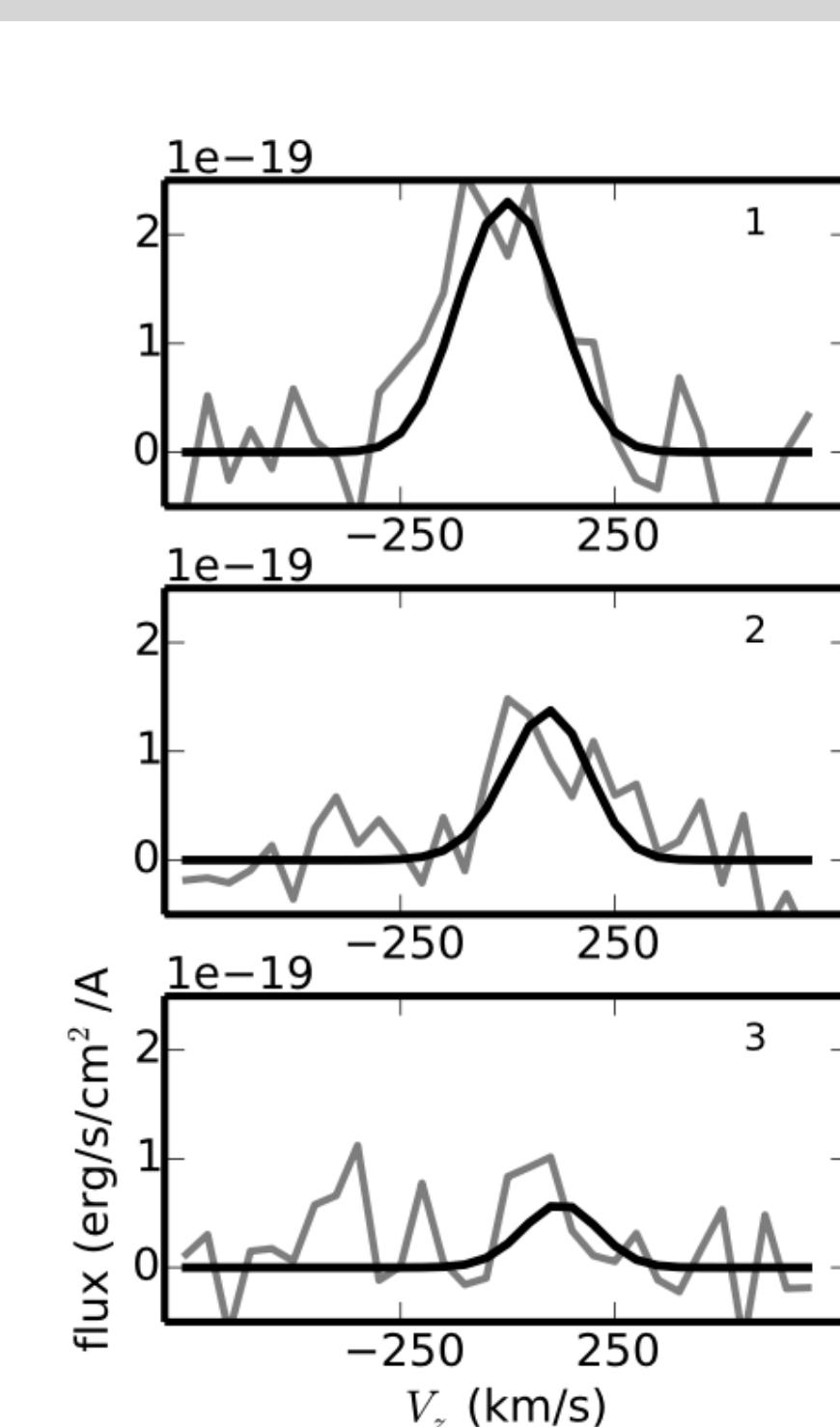
◆ Compares 3D parametric models directly to the IFU data-cube, taking into account the LSF and PSF

◆ Primary assumption: axisymmetric disk

Using 3D forward modelling for disk-halo decomposition



Bouché et al. 2015



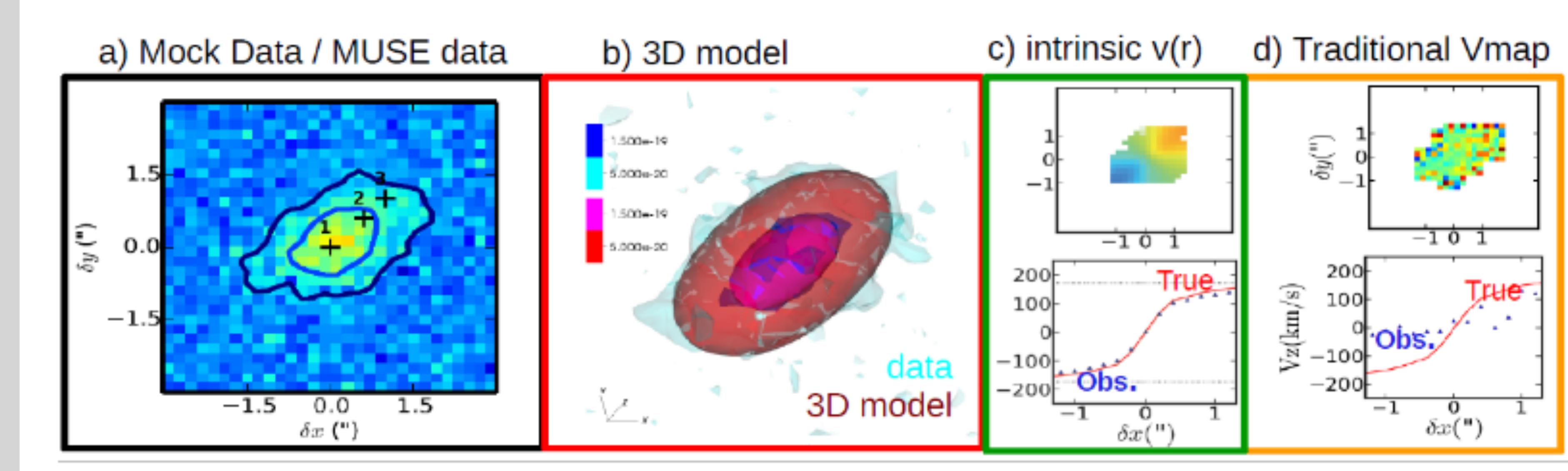
Advantages :

- ◆ Morpho-kinematics yielded simultaneously
- ◆ yields intrinsic parameters (by taking into account LSF & PSF)
- ◆ Works on all spaxels
- ◆ Well suited for low S/N regime [good for $R > Re$]
- ◆ Breaks inclination-Vmax degeneracy
- ◆ Flexible parametric models & MCMC

Using 3D forward modelling for disk-halo decomposition



Bouché et al. 2015



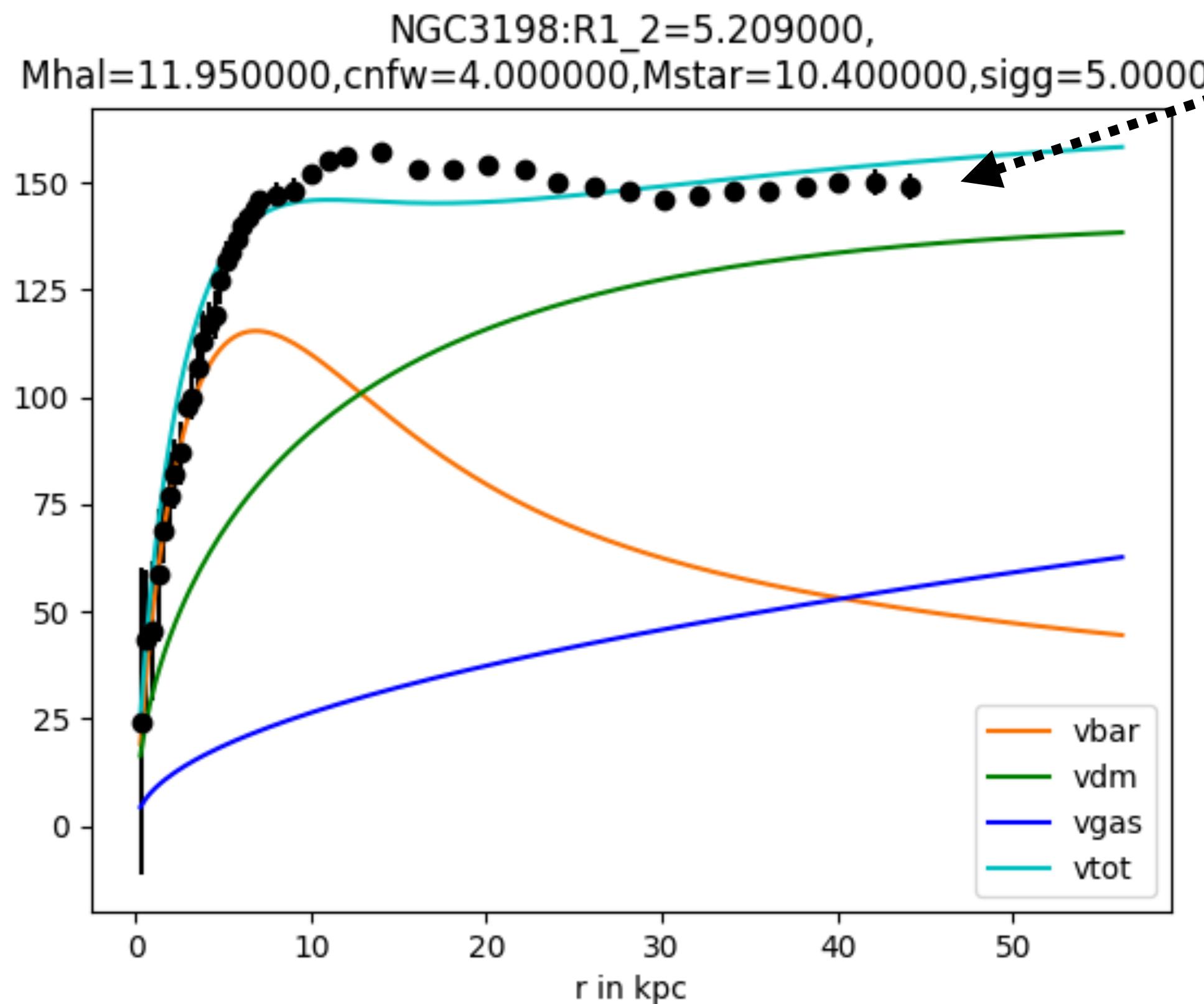
Compare to state-of-the-art :

- ◆ 3D method (vs. 1D)
- ◆ No priors (M^* , inclination)
- ◆ computes the likelihood directly on the 3D data giving us thousands of degrees of freedom

Using 3D forward modelling: Under the hood



Bouché et al. 2015

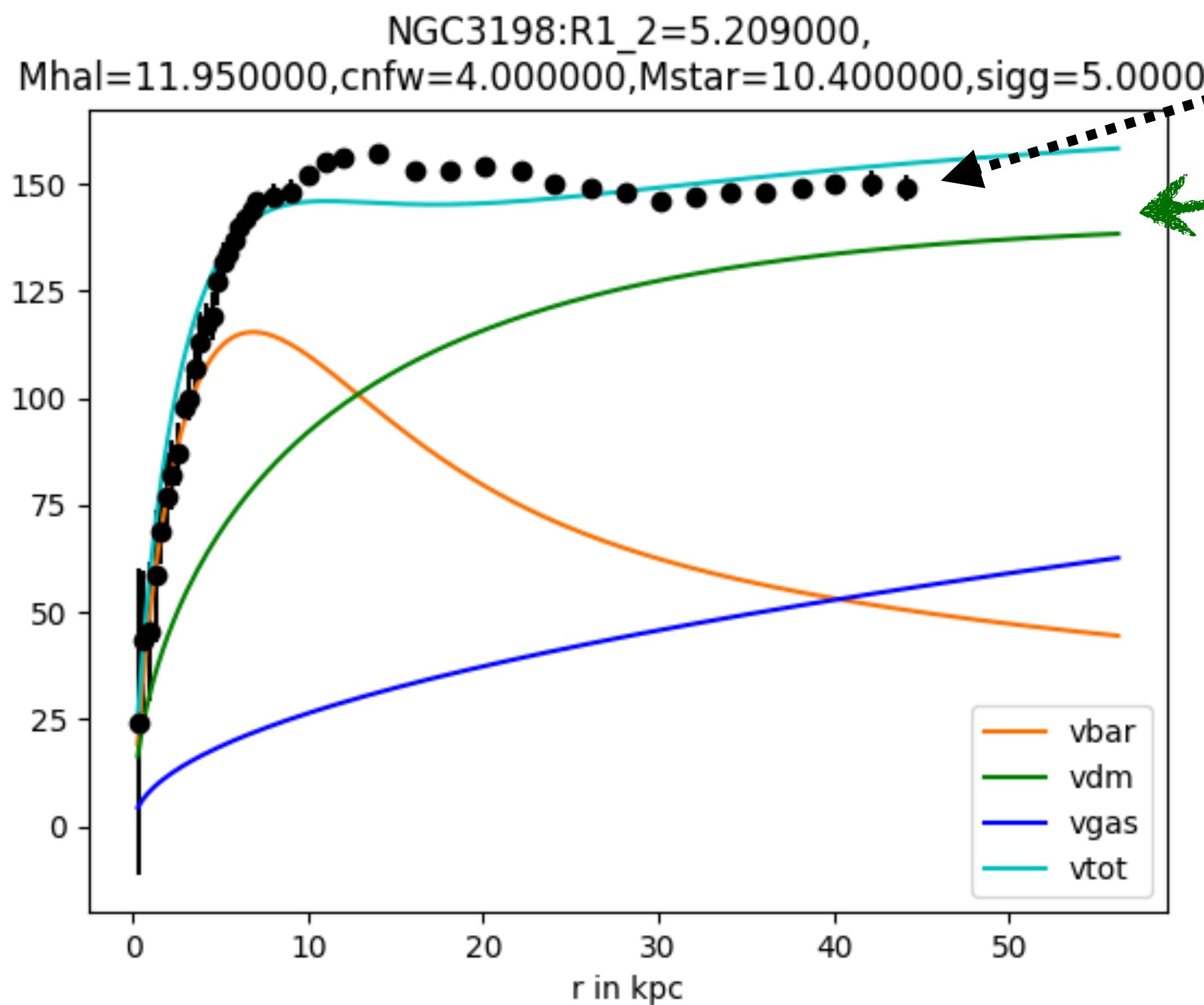


$$v_c(r)^2 = v_{\text{DM}}(r)^2 + v_{\text{disk}}(r)^2 + v_{\text{HI}}(r)^2$$

Using 3D forward modelling: Under the hood



Bouché et al. 2015

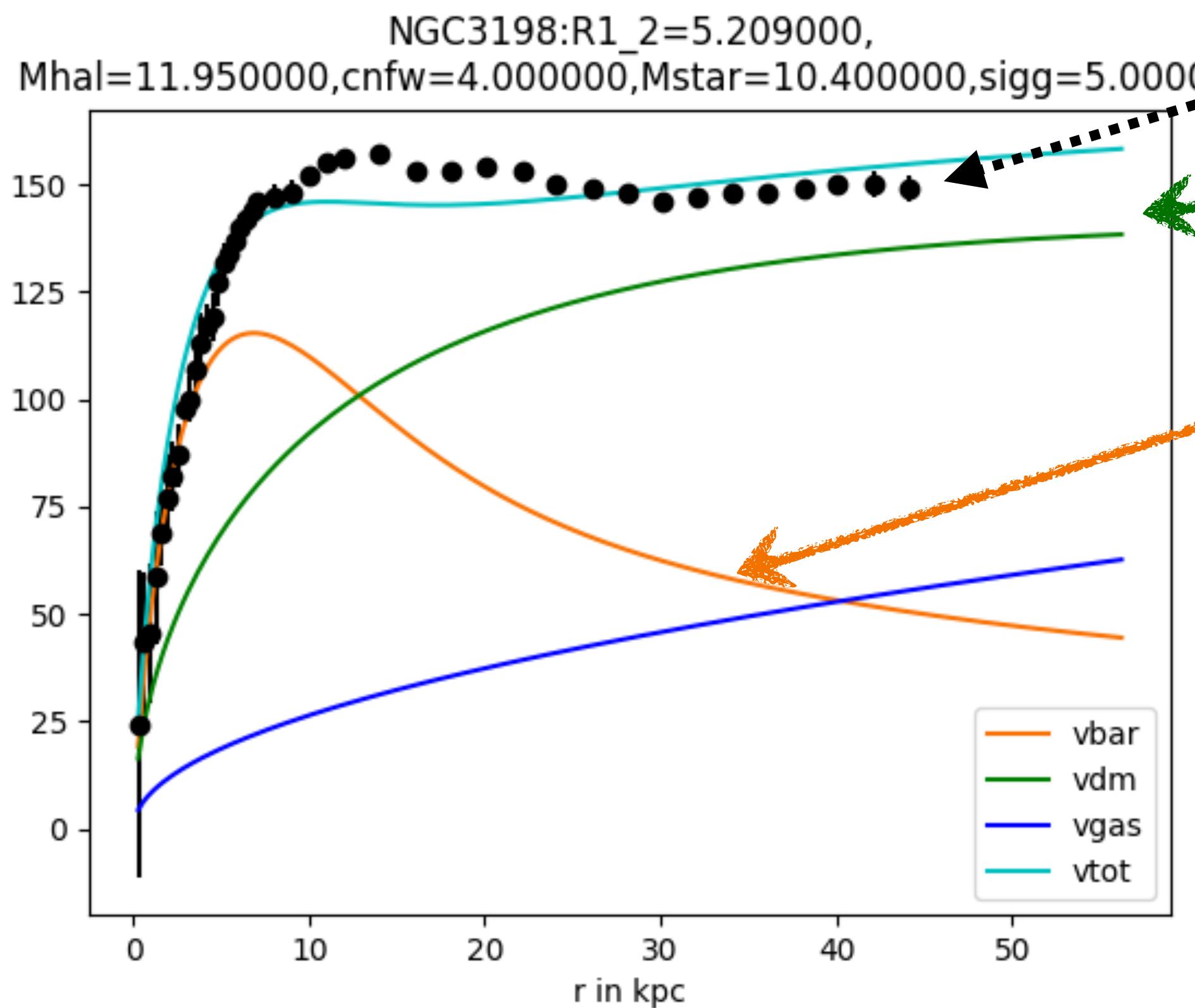


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Using 3D forward modelling: Under the hood



Bouché et al. 2015

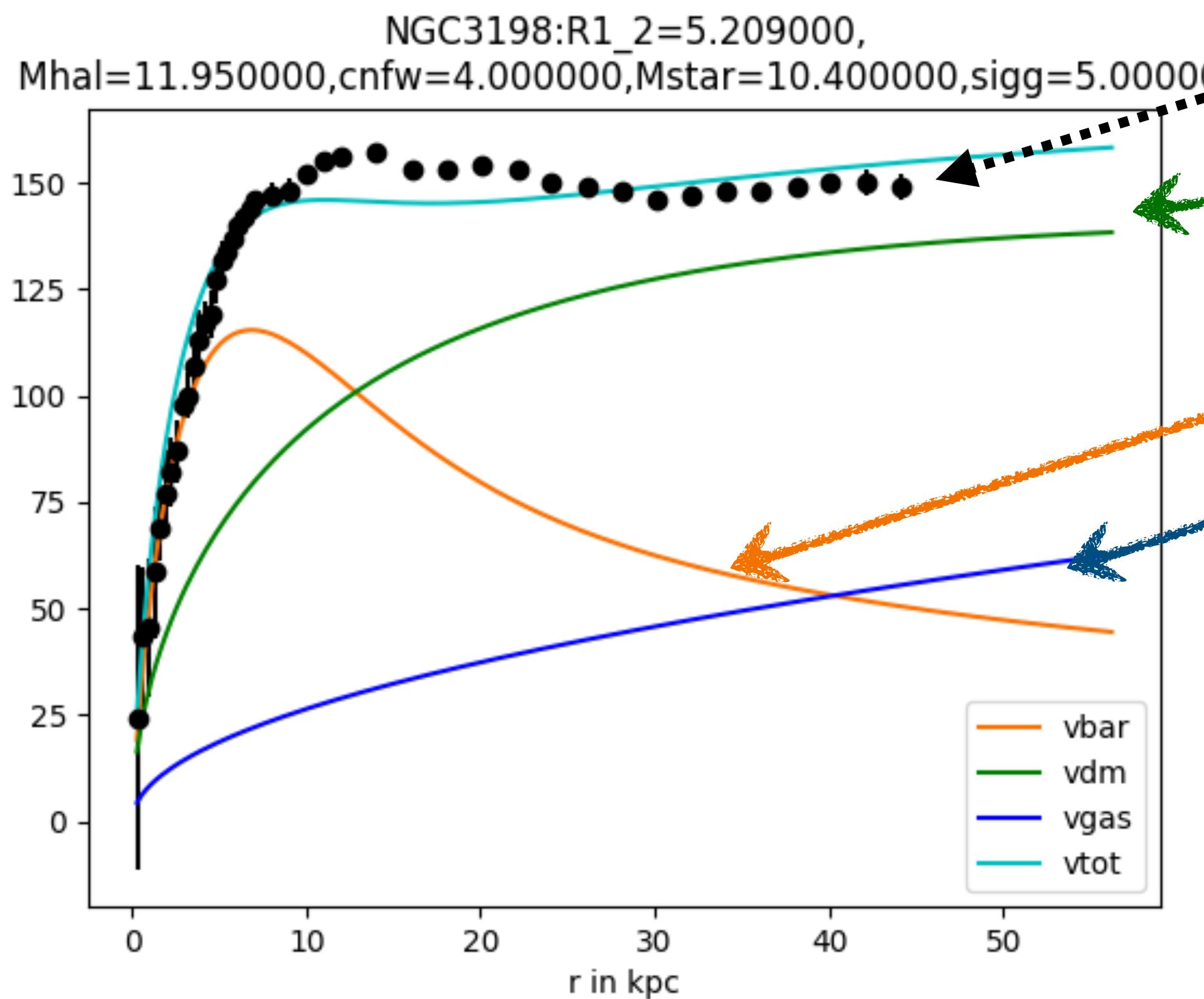


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Bouché et al. 2015

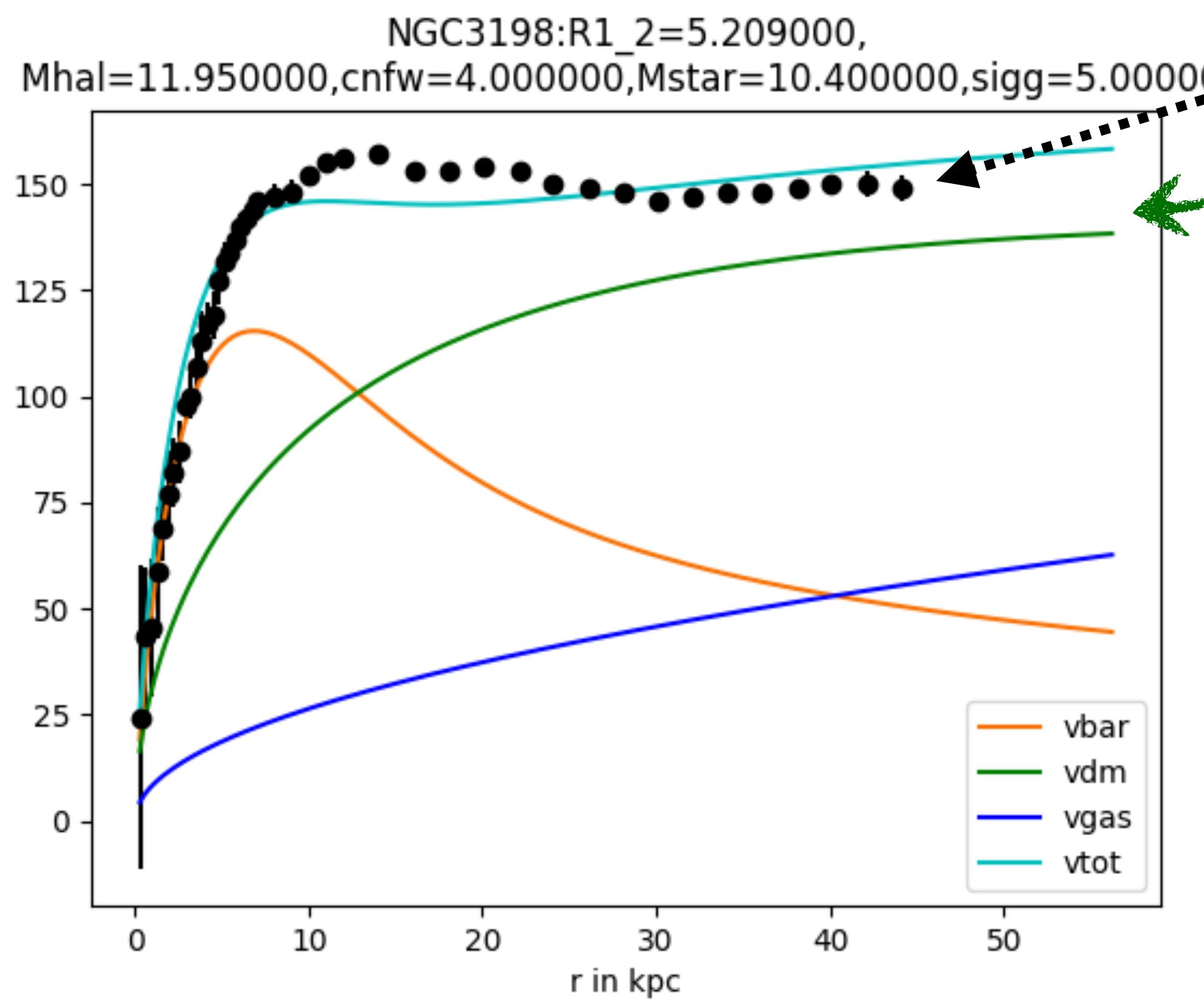


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Using 3D forward modelling: Under the hood

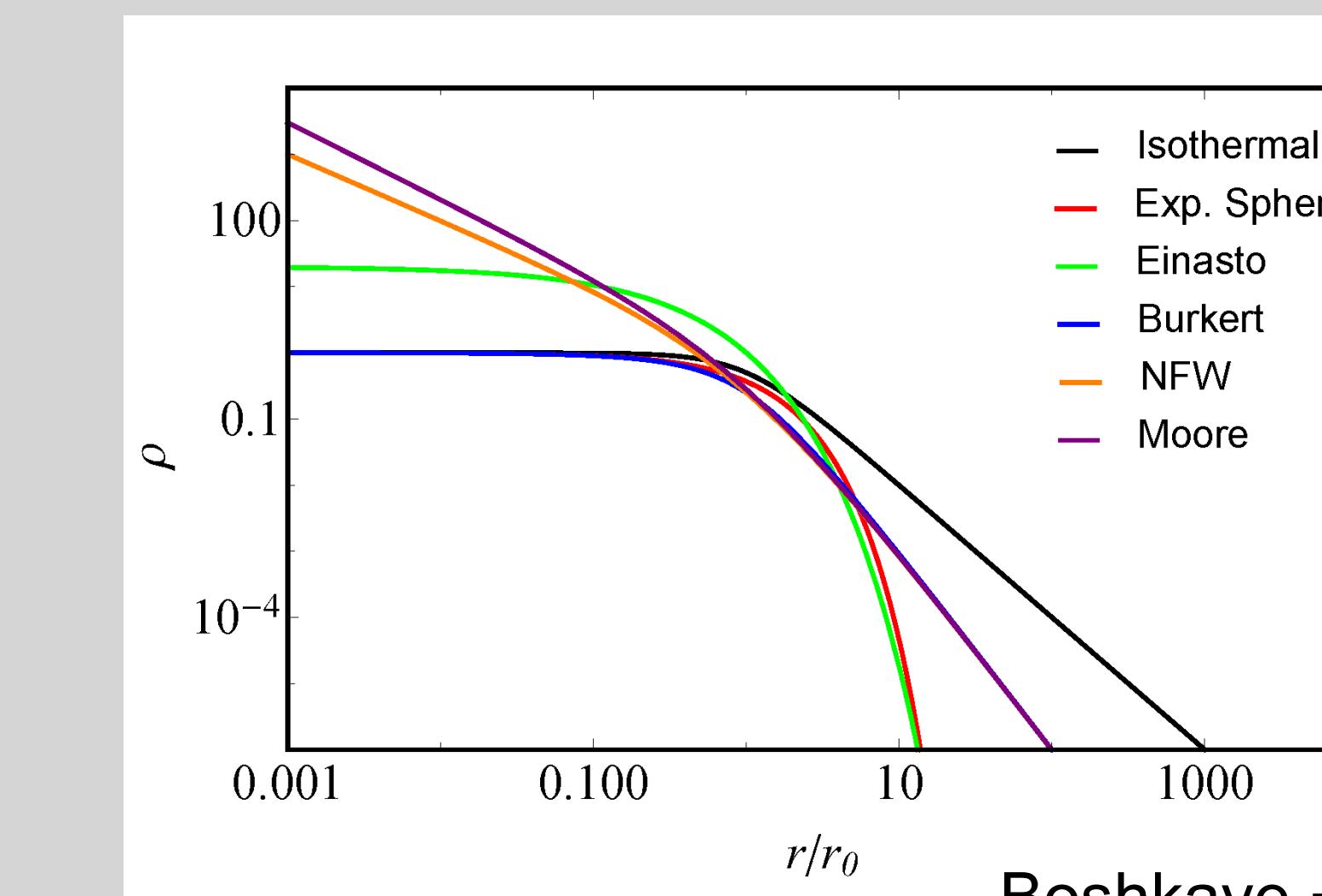


Bouché et al. 2015



$$v_c(r)^2 = v_{\text{DM}}(r)^2 + v_{\text{disk}}(r)^2 + v_{\text{HI}}(r)^2$$

1) DM: different Dark Matter density profiles



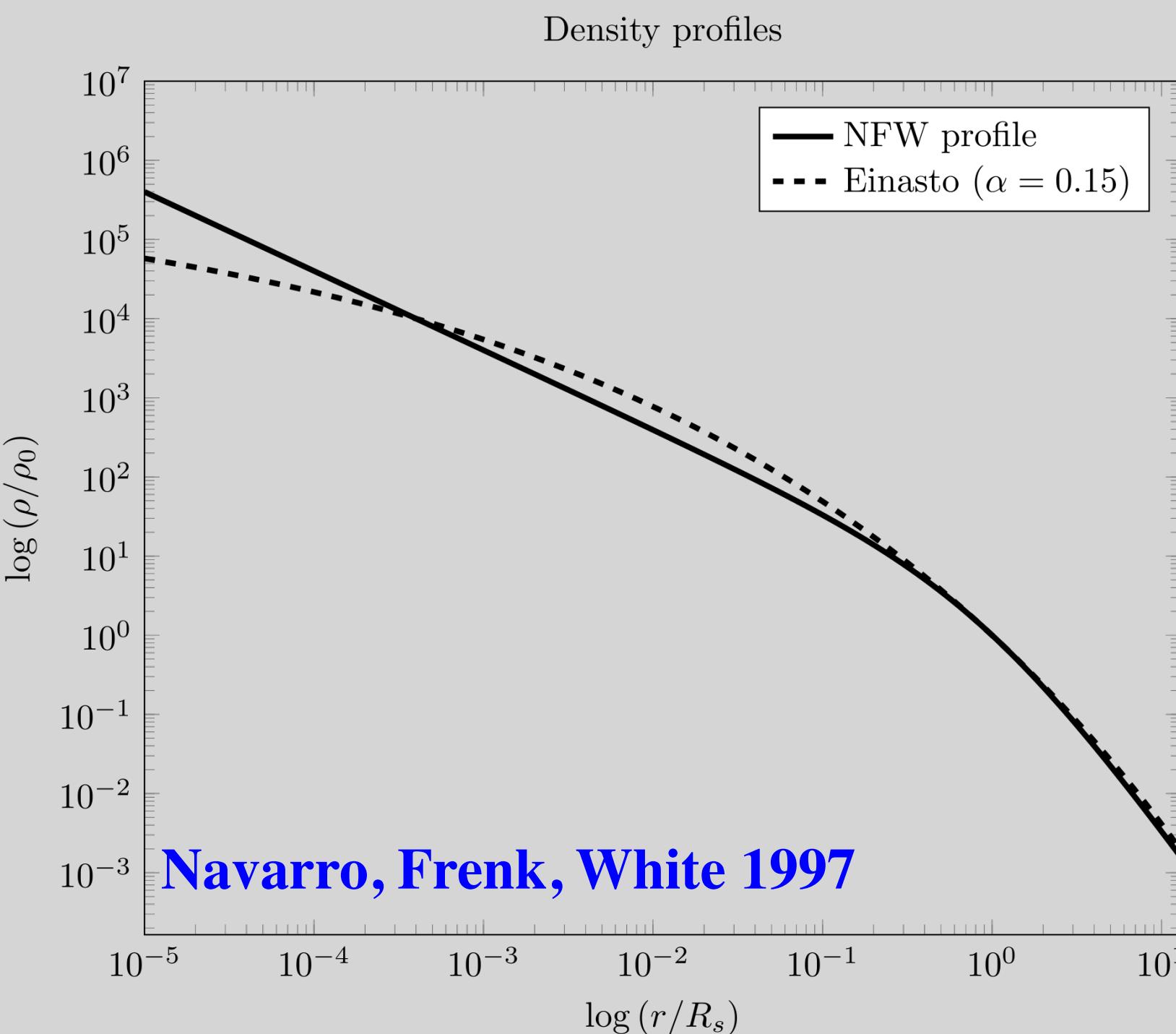
Boshkaye +2020

Examples of Halo profiles - from N-body simulations

CUSP

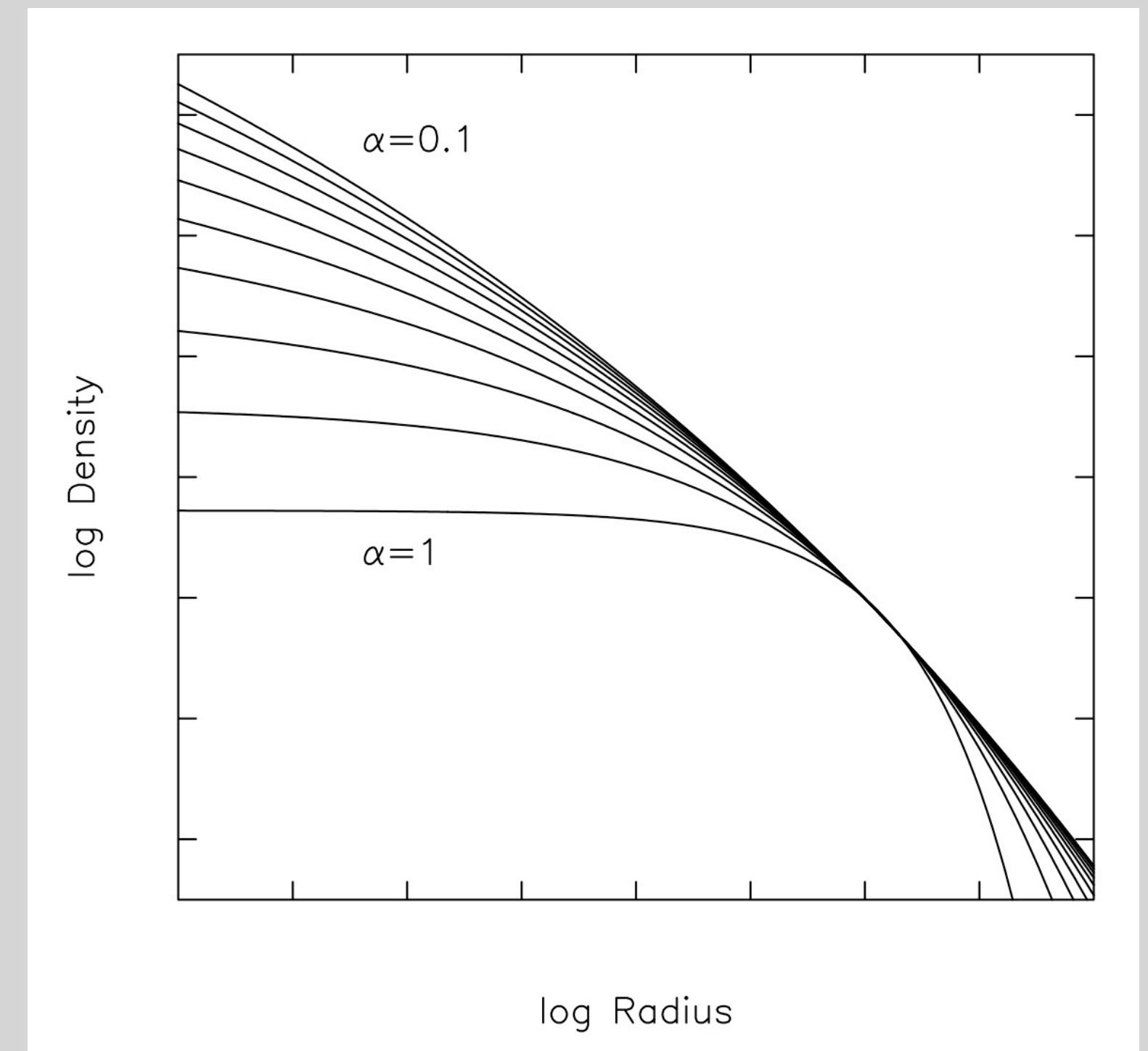
$$\rho_{\text{NFW}}(r) = \frac{\rho_s}{\left(\frac{r}{r_s}\right)\left(1 + \left(\frac{r}{r_s}\right)\right)^2}$$

$$C_{200} = r_{200}/r_s$$



CORE-CUSP

$$\rho_{\text{Einasto}}(r) = \rho_s e^{-\frac{2}{\alpha\epsilon}\left(\left(\frac{r}{r_s}\right)^{\alpha\epsilon} - 1\right)}$$



Navarro et al. (2004)

Examples of Halo profiles - from hydrodynamical simulations

CORE-CUSP

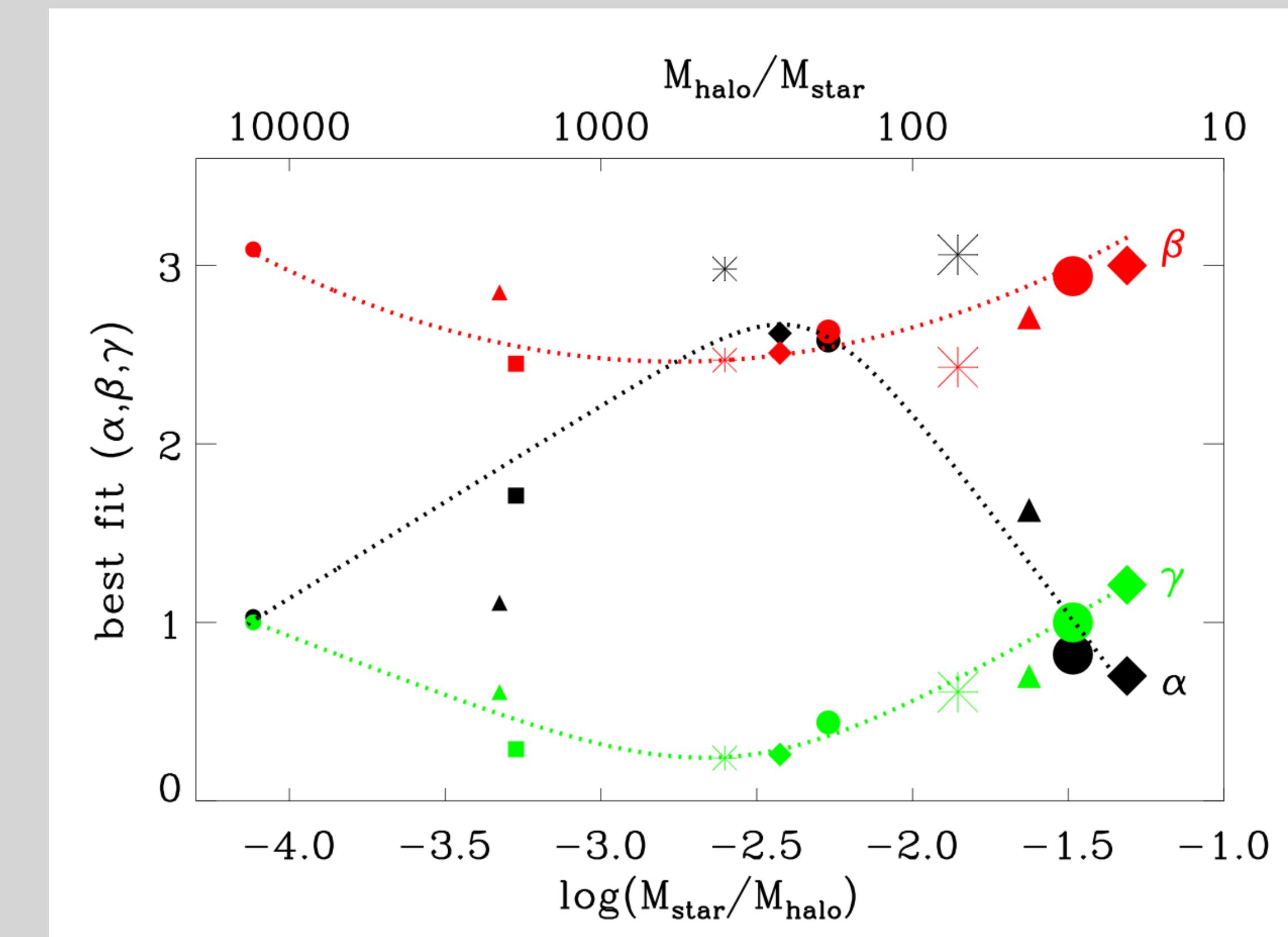
$$\rho_{DC14}(r) = \frac{\rho_s}{\left(\frac{r}{r_s}\right)^\gamma \left(1 + \left(\frac{r}{r_s}\right)^\alpha\right)^{(\beta-\gamma)/\alpha}}$$

$$\alpha = 2.94 - \log[(10^{X+2.33})^{-1.08} + (10^{X+2.33})^{2.29}],$$

$$\beta = 4.23 + 1.34X + 0.26X^2,$$

$$\gamma = -0.06 + \log[(10^{X+2.56})^{-0.68} + 10^{X+2.56}].$$

$$X = \log(M_\star/M_{\text{halo}})$$



Di Cintio et al. 2014

→ takes into account the stellar-to-halo mass dependence
of the response of dark matter to baryonic processes

Examples of Halo profiles - from hydrodynamical simulations

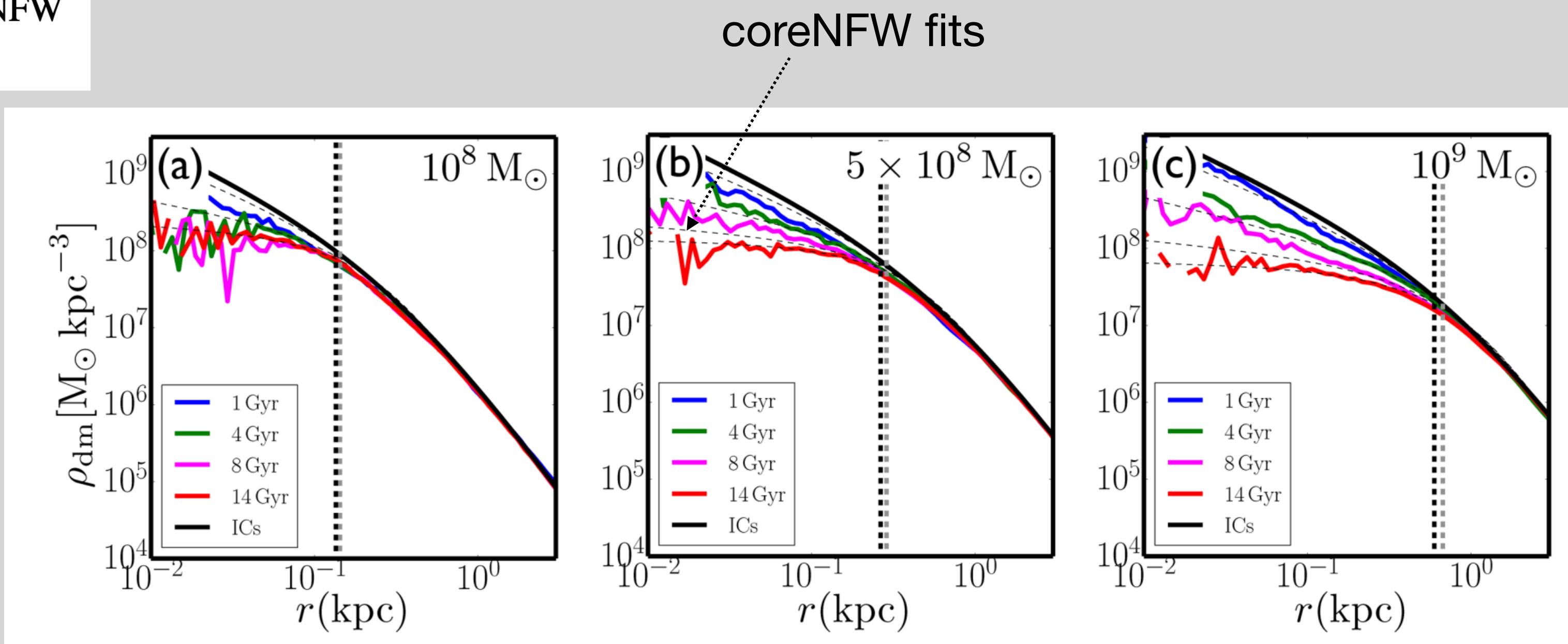
CORE-CUSP

$$\rho_{\text{cNFW}} = f^n(r)\rho_{\text{NFW}} + \frac{n f^{n-1}(r)(1 - f^2(r))}{4\pi r_c^2} M_{\text{NFW}}$$

where

$$f^n(r) = \tanh(r/r_c)^n$$

Read et al. 2016



→ captures the dark matter core growth as a function of star formation time and the projected stellar half-mass radius

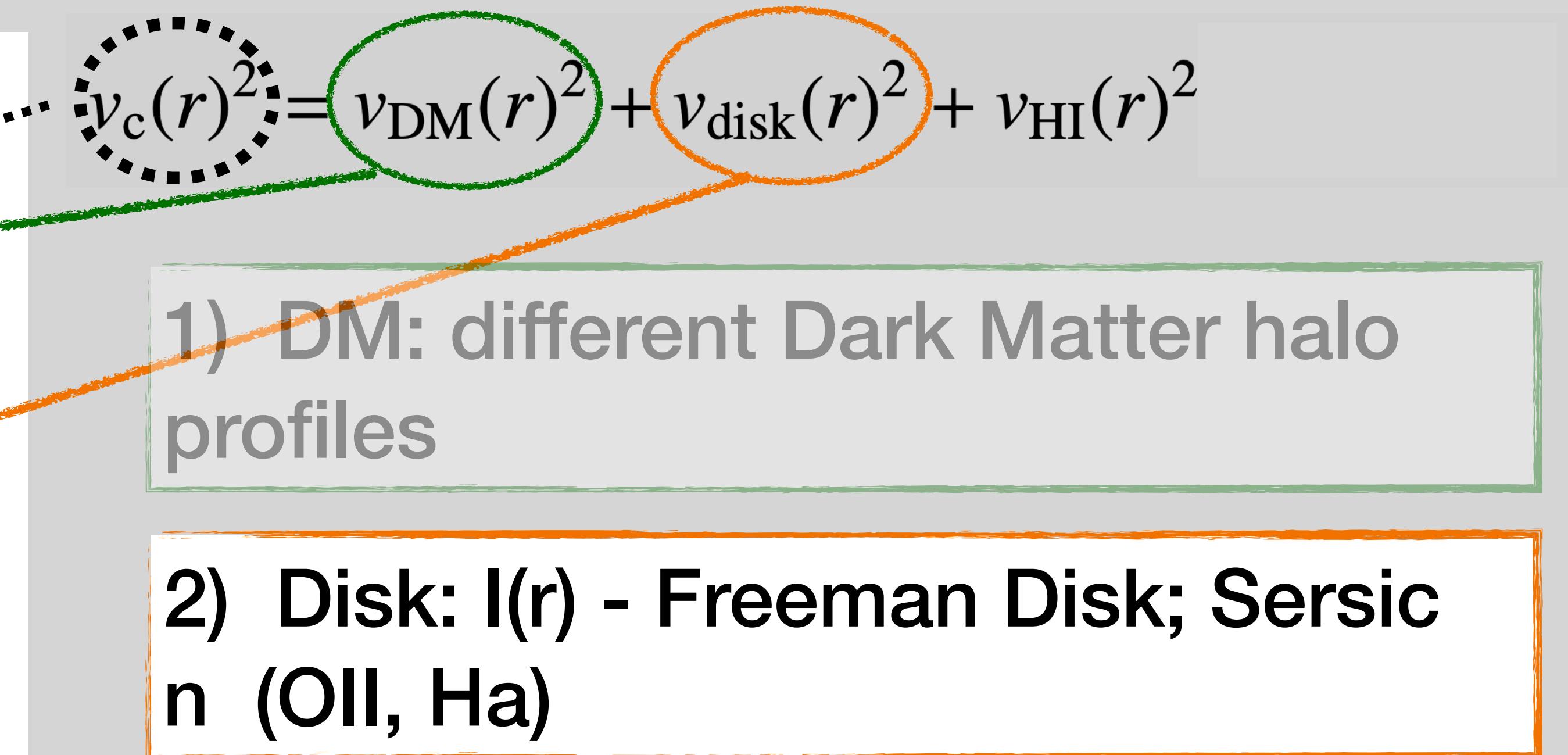
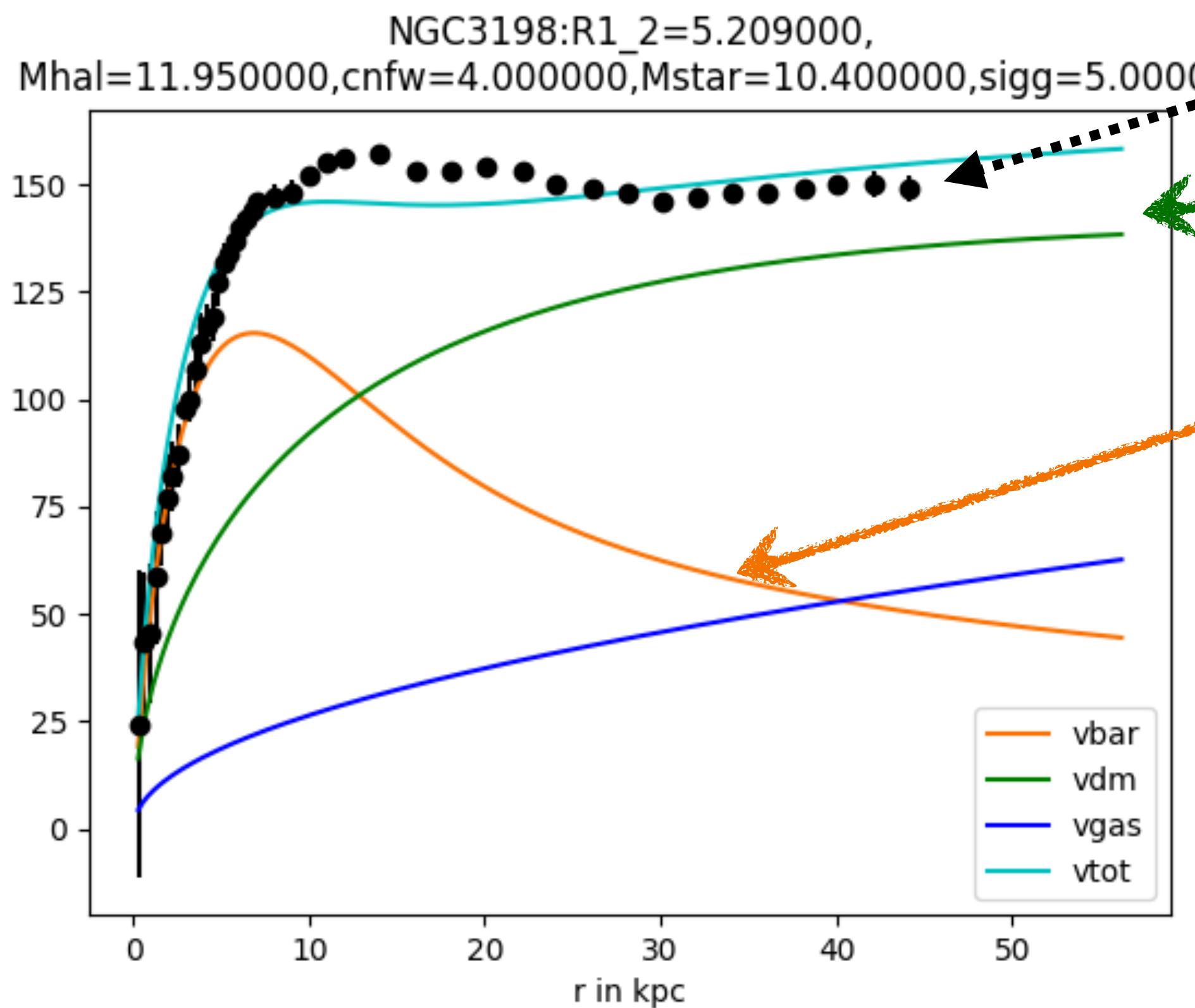
Examples of Halo profiles - many more

- Burkert Profile (Burkert 1995)
- Moore Profile (Moore et al. 1999)
- Isothermal Profile (Binney & Tremaine 1987)
- Hernquist Profile (Hernquist 1990)
- Zhao Profile (Zhao 1996)
- Dekel-Zhao (Freundlich et al. 2020)
- cNFW (Peñarrubia et al. 2012)
- coreEinasto (Lazar et al. 2020)
- Etc

Using 3D forward modelling: Under the hood



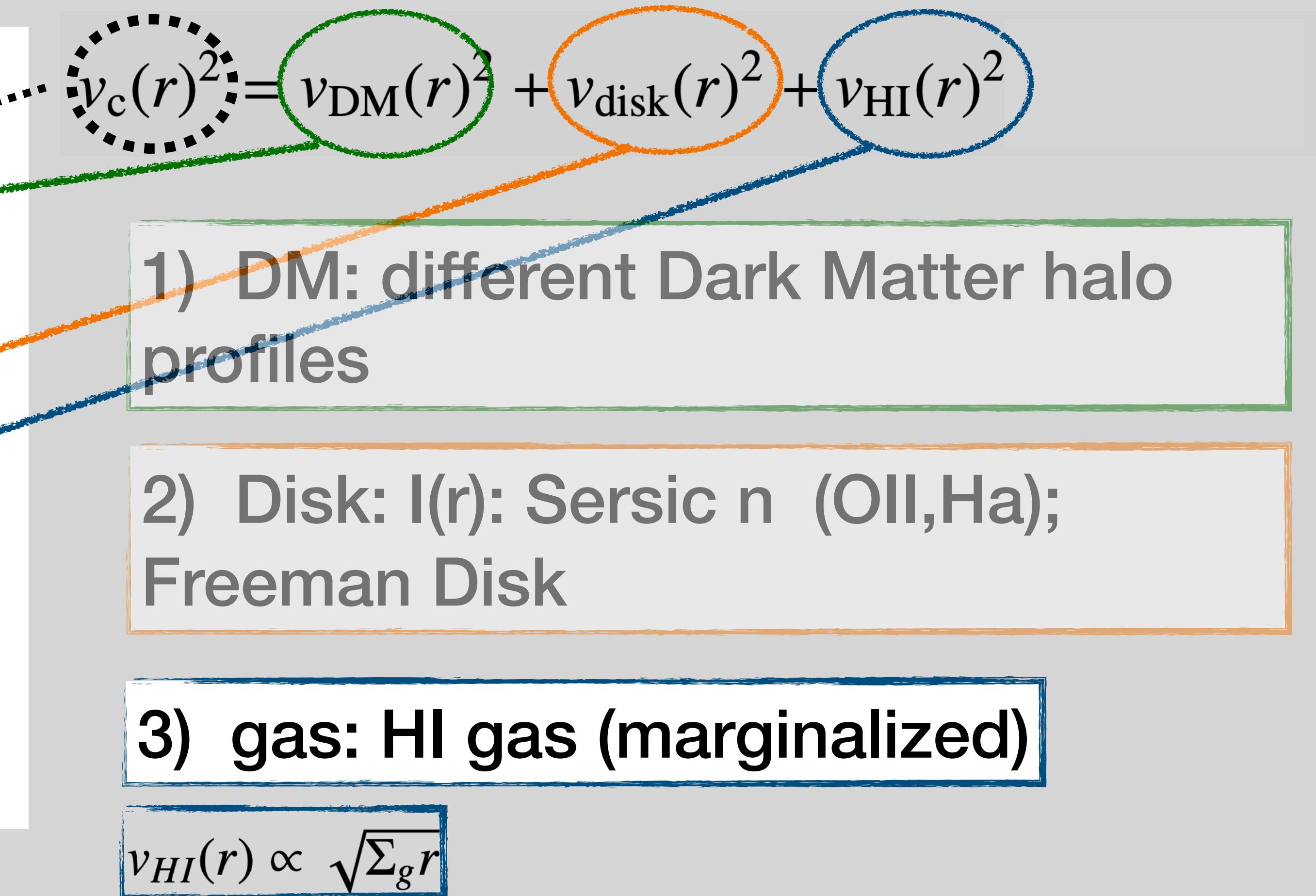
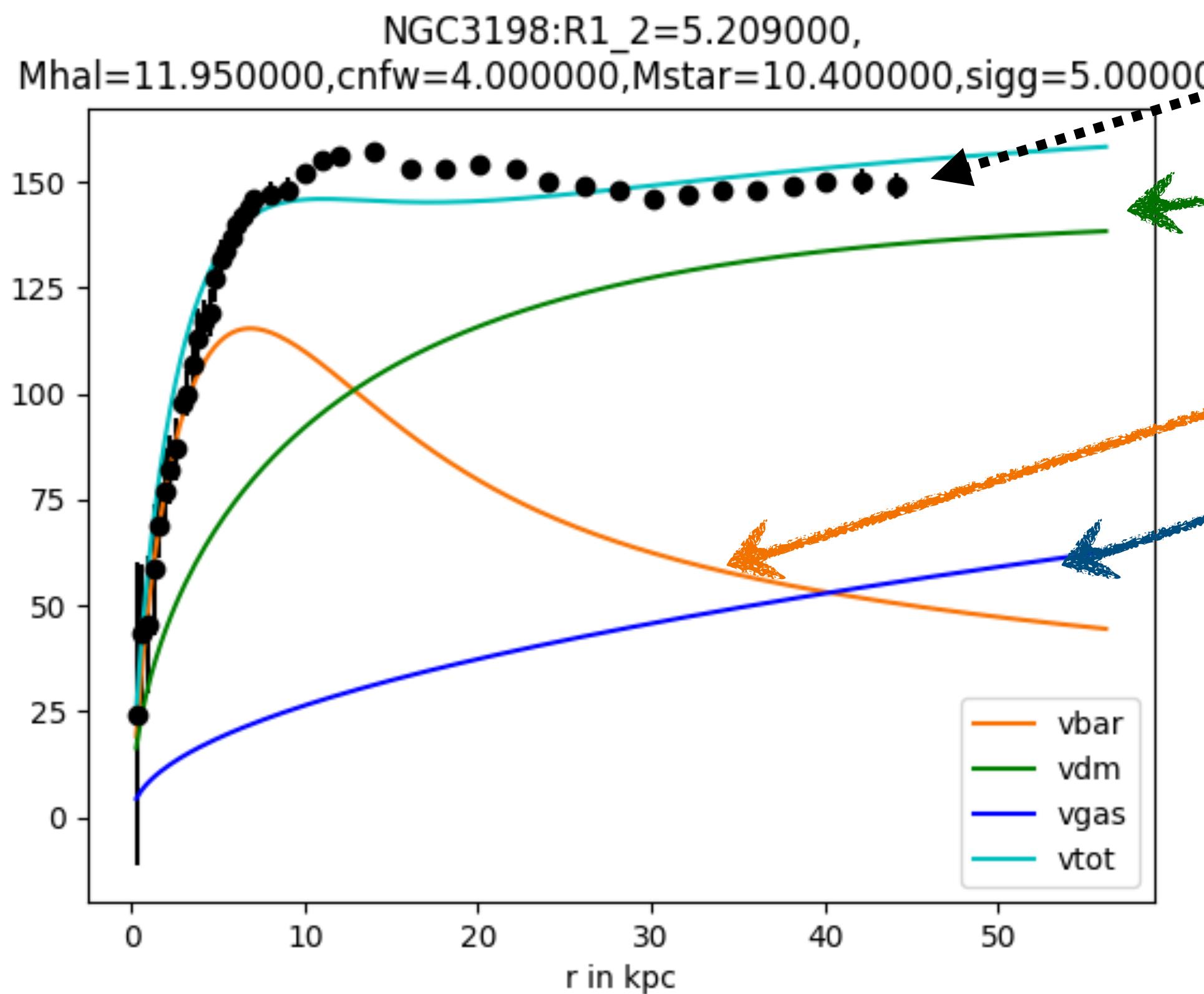
Bouché et al. 2015



Using 3D forward modelling: Under the hood



Bouché et al. 2015

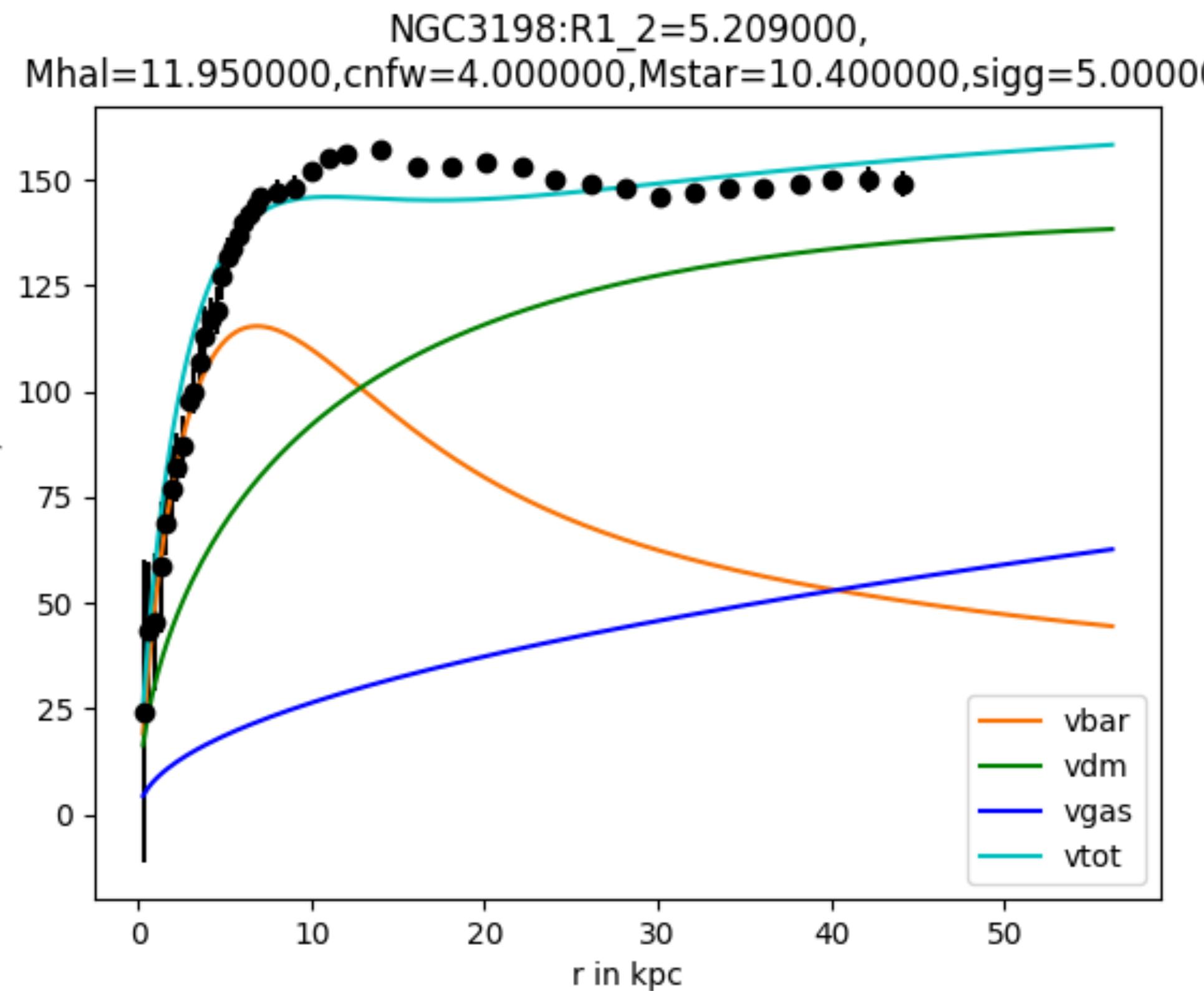


Using 3D forward modelling: Under the hood



Bouché et al. 2015

$$v_c(r)^2 = v_{\text{DM}}(r)^2 + v_{\text{disk}}(r)^2 + v_{\text{HI}}(r)^2$$



1) DM: different Dark Matter halo profiles

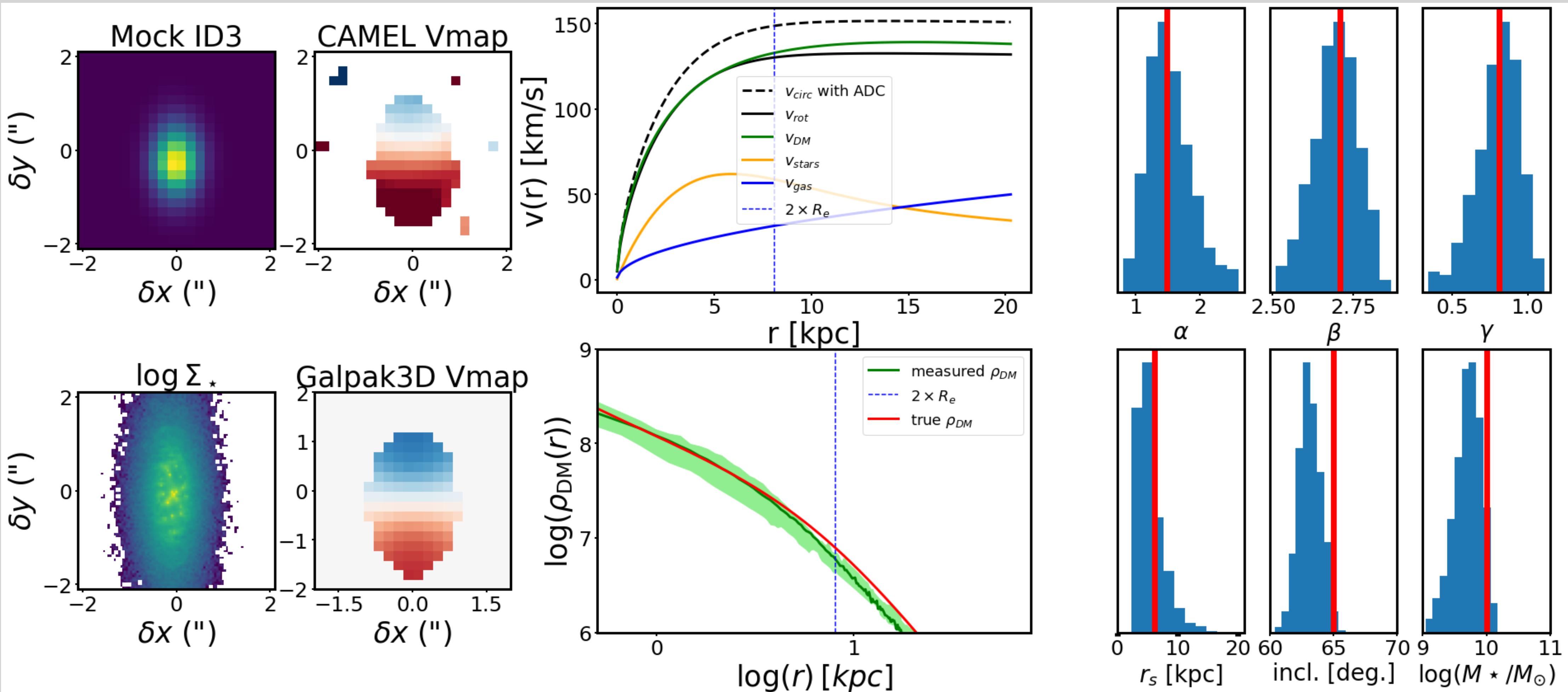
2) Disk: $I(r)$: Sersic n (OII,Ha); Freeman Disk

3) gas: HI gas (marginalized)

→ 13 - 15 free parameters
($x, y, z, \text{incl}, \text{PA}, M^*, M_{\text{vir}}, C_{\text{vir}}, \text{sig0}, R_e, n, \dots$)
→ all optimised simultaneously directly on the 3D IFU cube

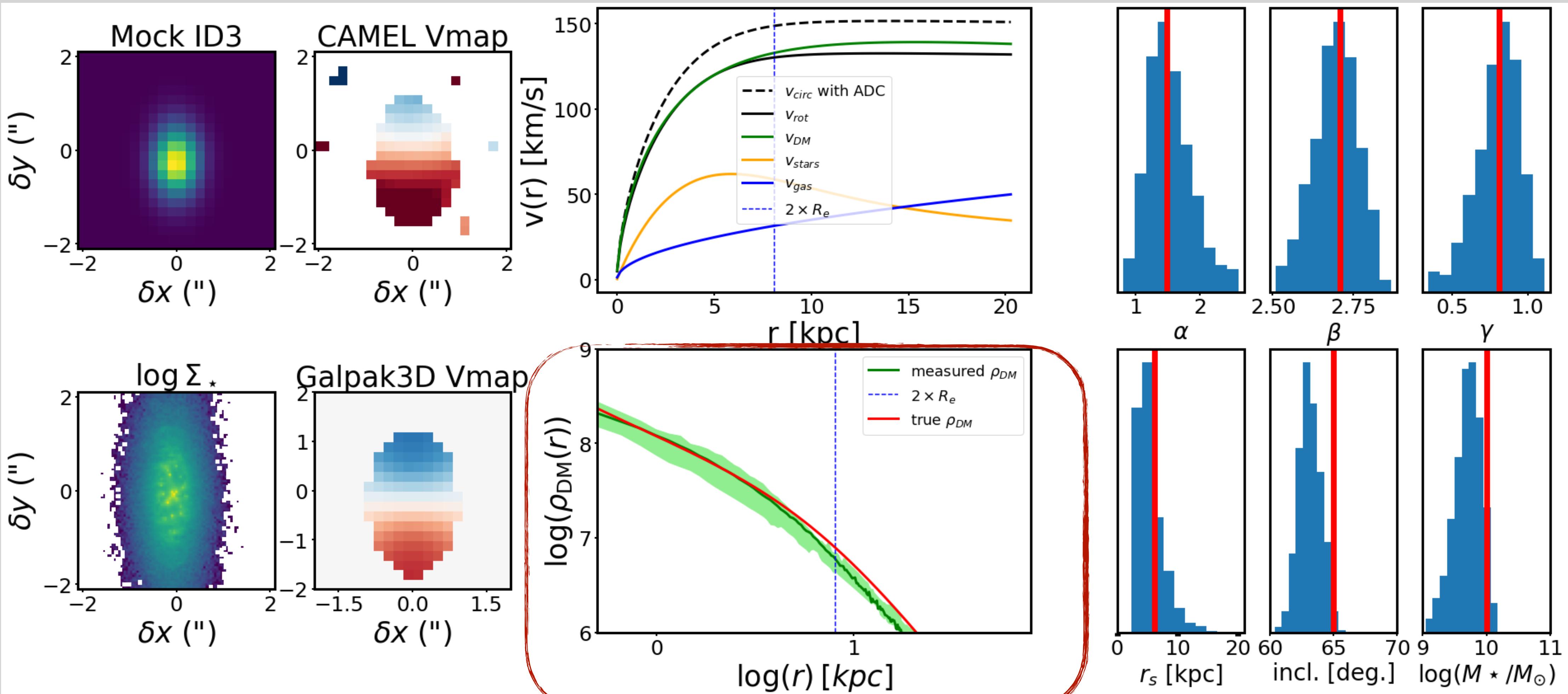
Validation of the methodology:

Apply 3D disk-halo decomposition on mock observations



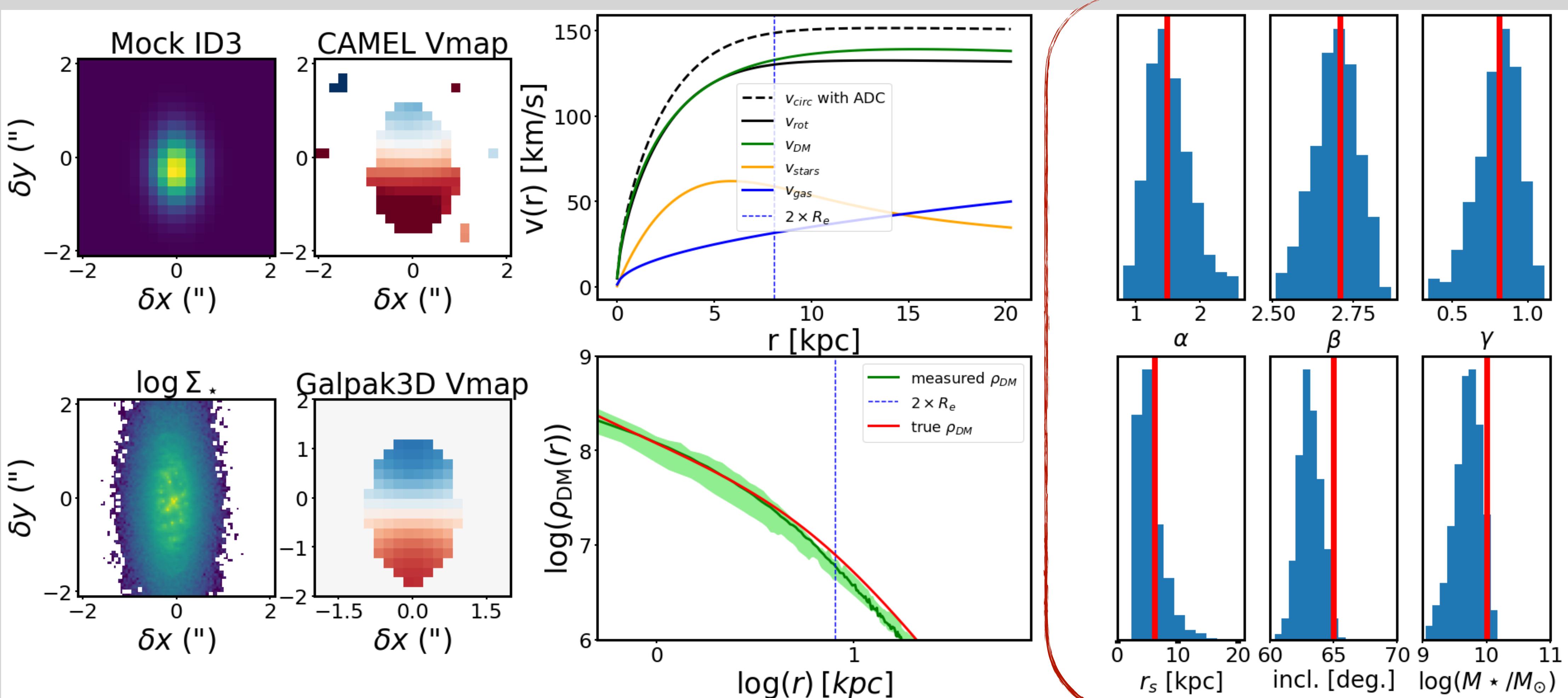
Validation of the methodology:

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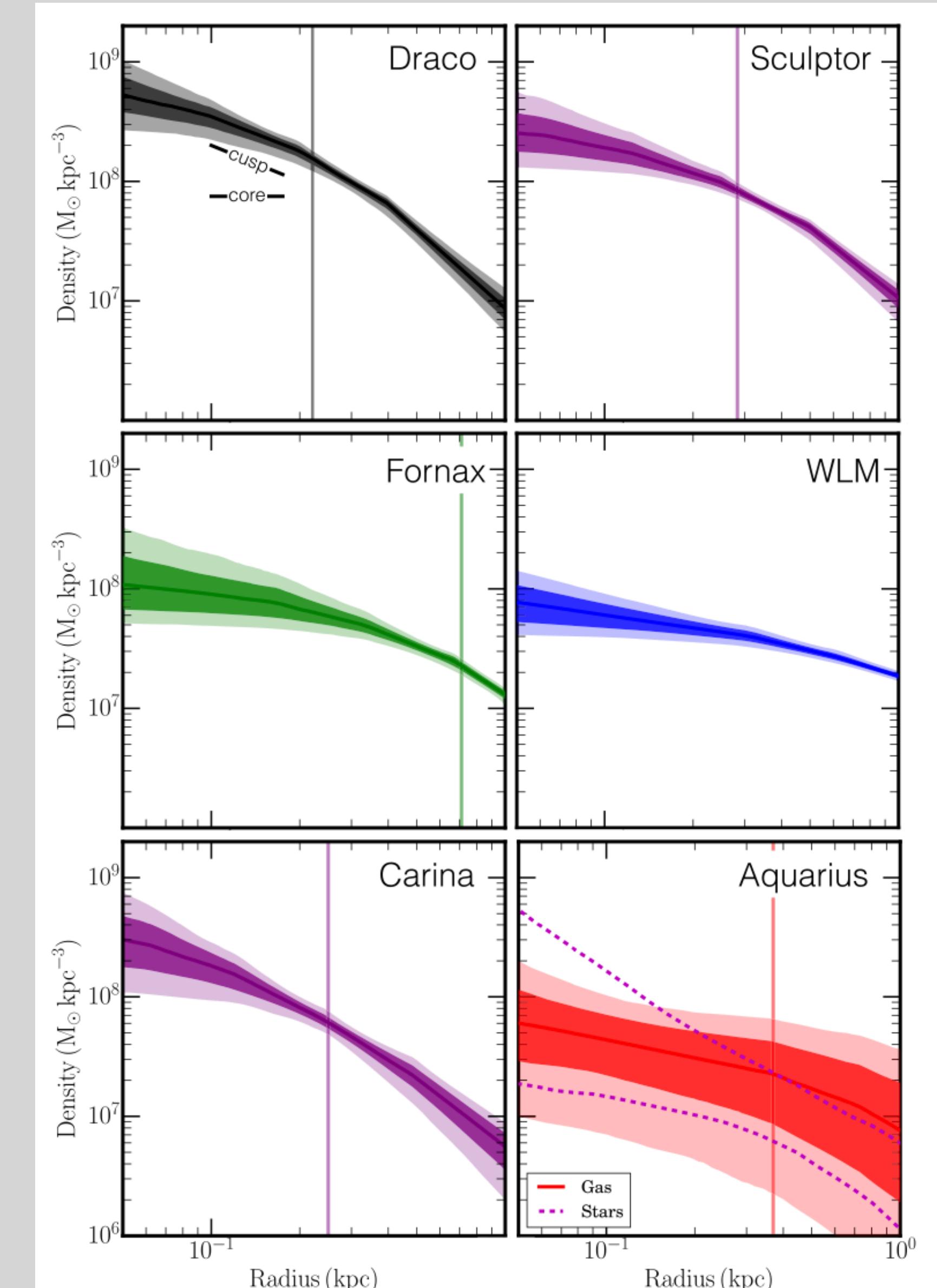
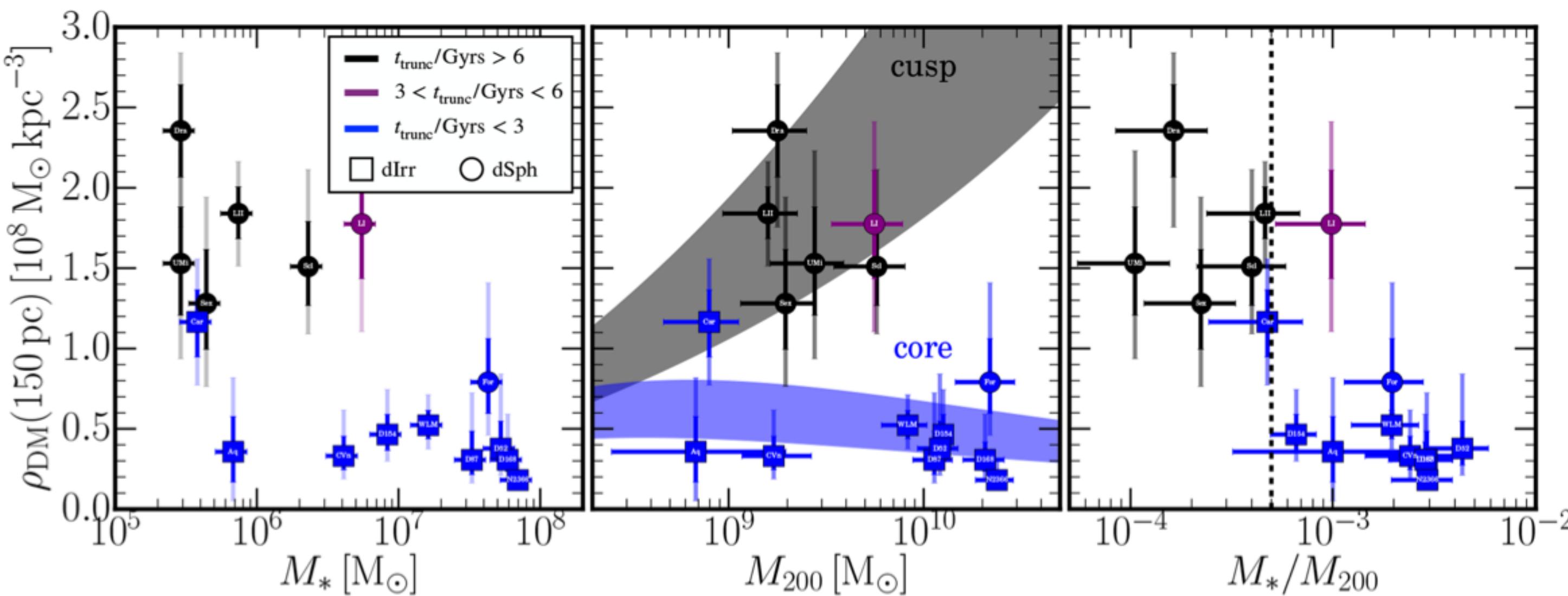
Validation of the methodology:

Apply 3D disk-halo decomposition on mock observations (using DC14 halo profile)



State-of-the-art (z=0): Read et al. 2019

- Dynamical modelling of 8 dwarf spheroidal and 8 dwarf irregular galaxies
 - Use NFW & coreNFW
 - Investigate SFHs
- Find evidence that galaxies which stopped forming stars over 6 Gyr ago show cusps, while those with more extended star formation cores

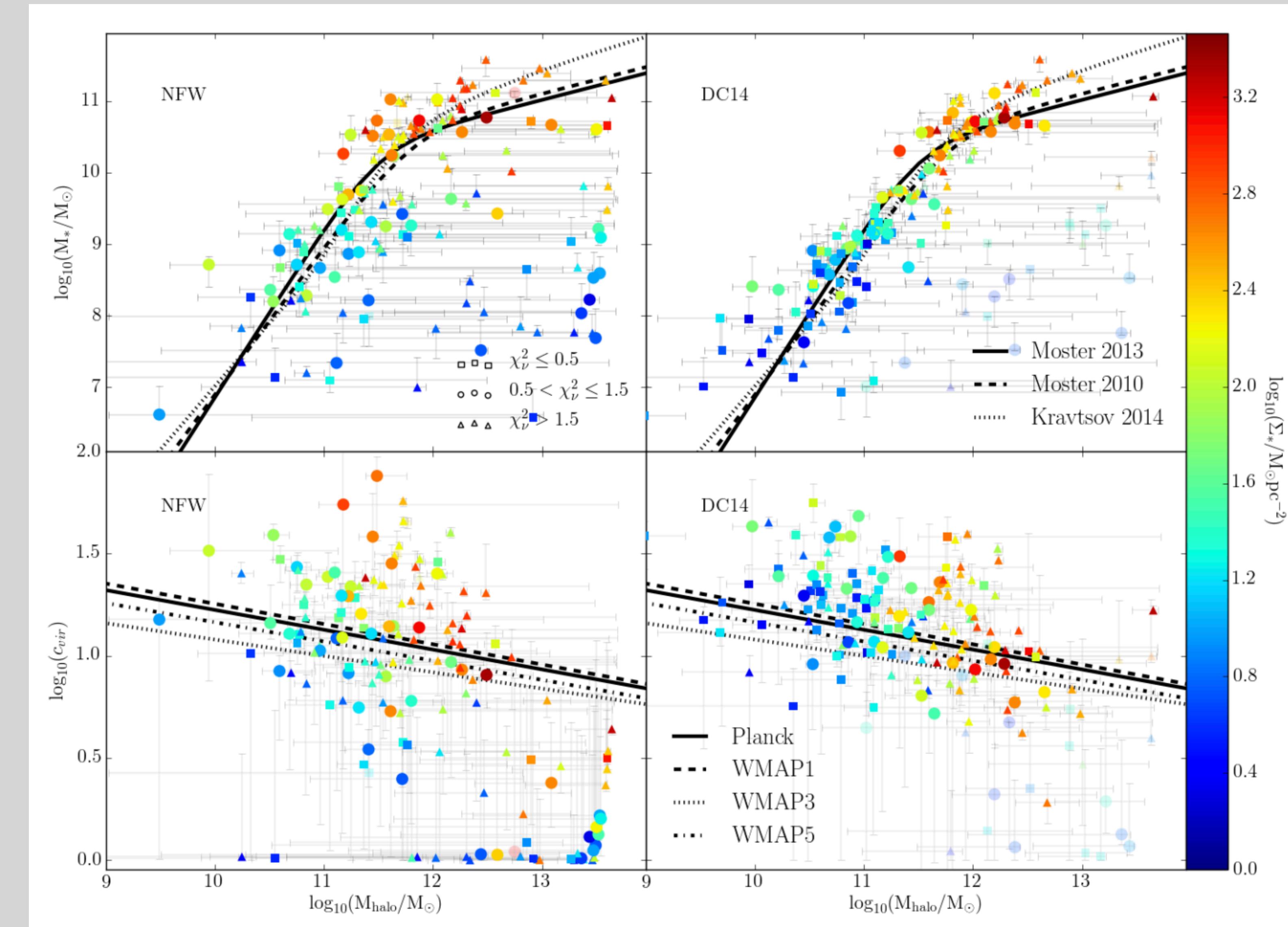


State-of-the-art ($z=0$): SPARC sample - Katz+2017

1D

- Rotation curve decomposition for 147 local galaxies (SPARC sample - Ha+HI)
- Model DM halo with (1) Navaro, Frenk, White +1997 profile; and (2) Di Cintio +2014 profile

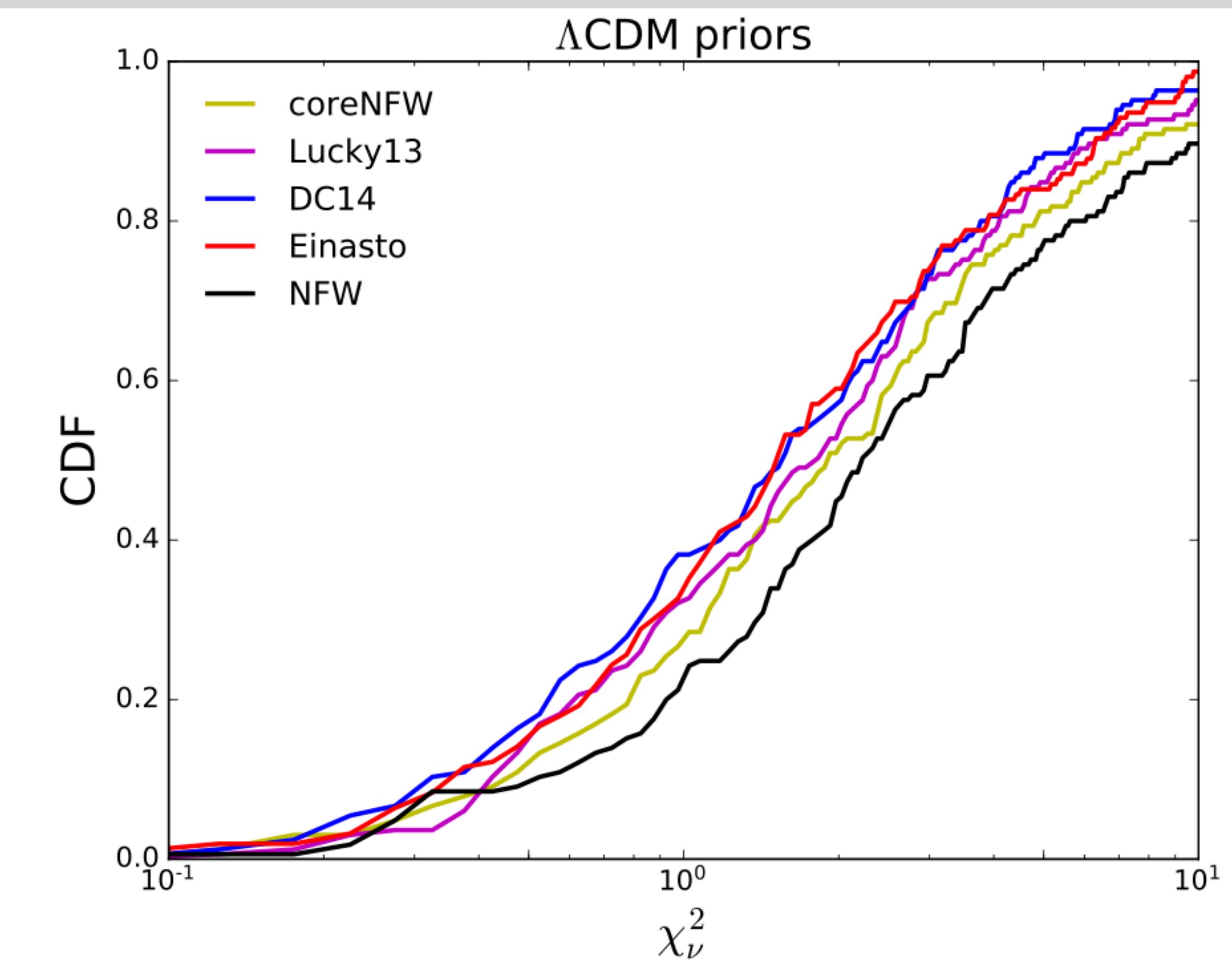
- Di Cintio halo profile provides better fits to the data
- Recover halo mass-concentration & stellar mass-halo mass relations



State-of-the-art ($z=0$): SPARC sample - Li+2020

1D

- Rotation curve decomposition for 175 local galaxies (SPARC sample - Ha+HI)
- Model DM halo with: (1) NFW; (2) Di Cintio +2014 profile; (3) pseudo-isothermal; (4) Burkert; (5) Einasto; (6)cored-NFW; and (7) Lucky13

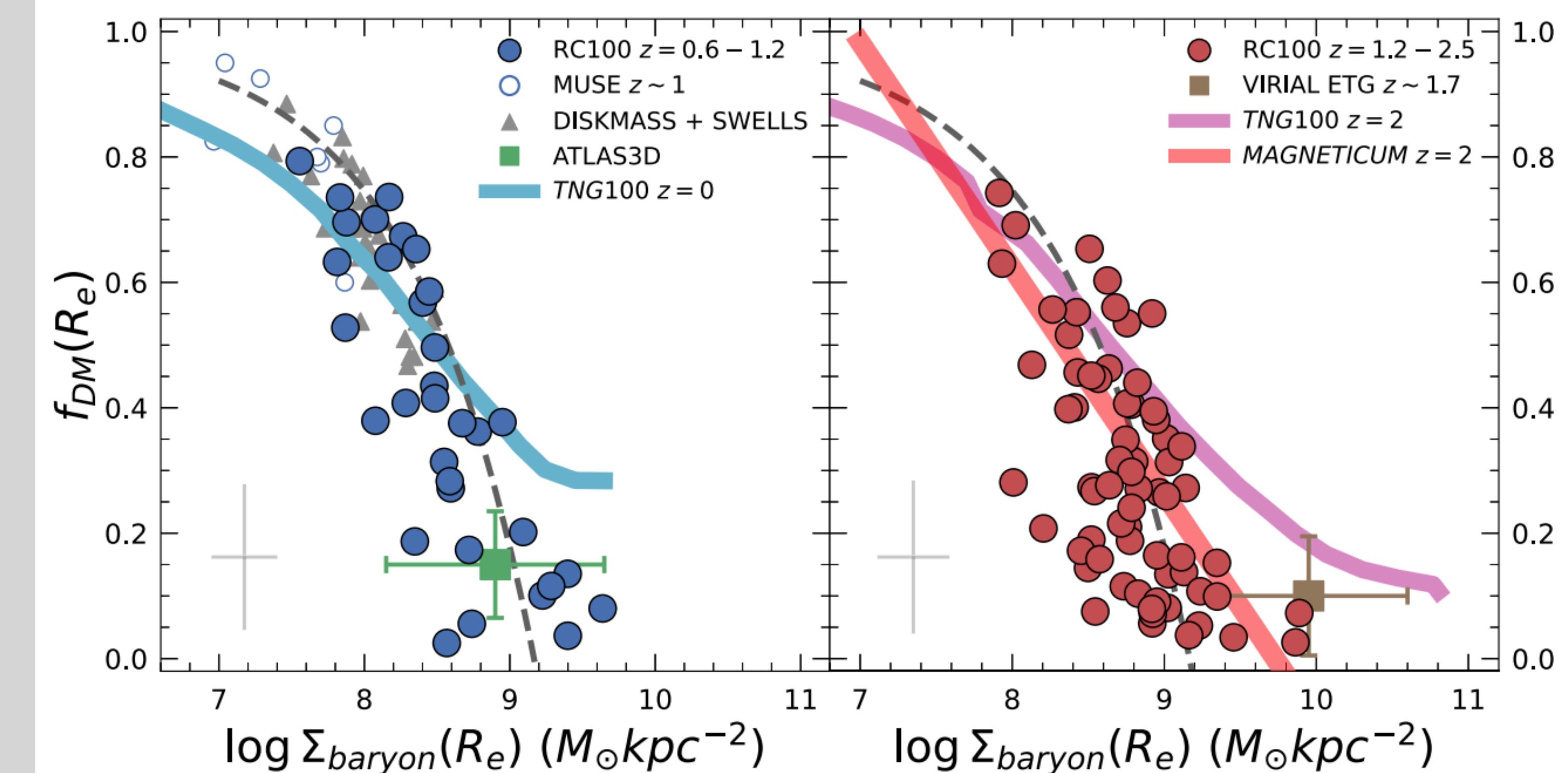


- Find evidence that cored profiles, such as Burkert, coreNFW, DC14, Einasto, and pISO, provide better rotation curve fits than the cuspy NFW profile
- Recover halo mass-concentration & stellar mass-halo mass relations

- Rotation curve decomposition for 100 $z=0.6-2.5$ massive galaxies (CO, Ha)

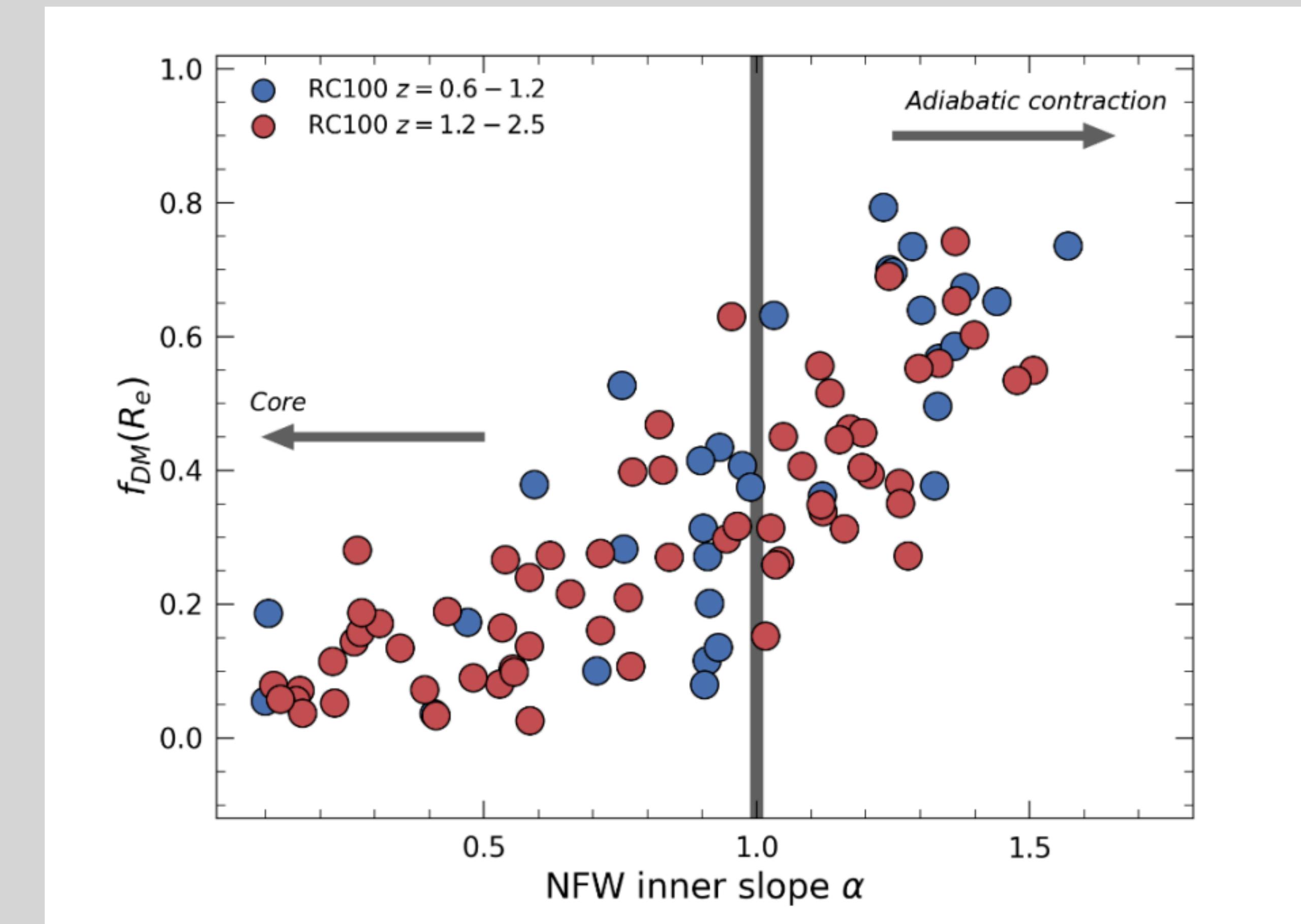
→ fraction of dark to total matter decreases with z

→ DM deficit is more evident at high star formation rate surface densities and galaxies with massive bulges



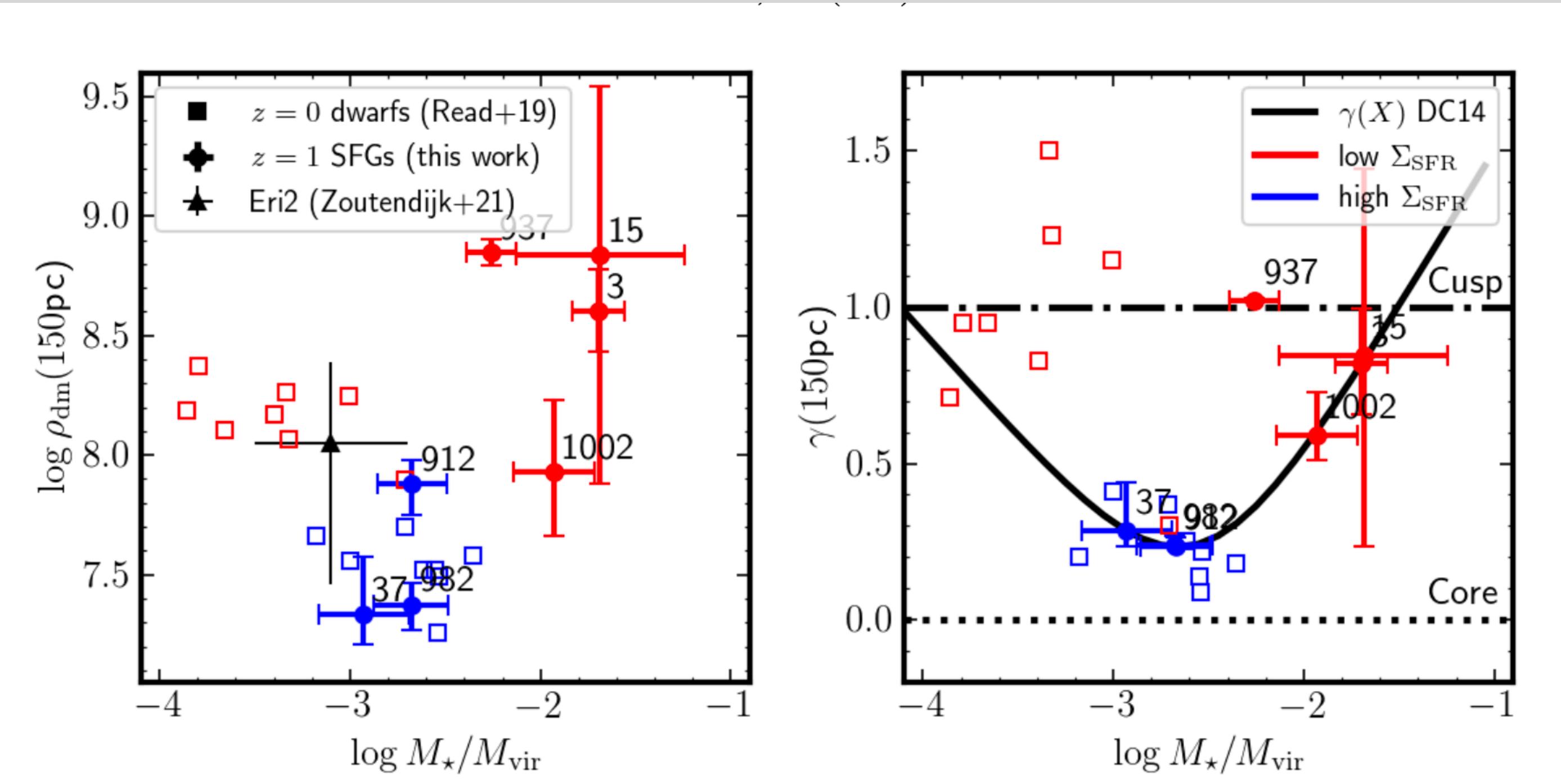
- Rotation curve decomposition for 100 $z=0.6-2.5$ massive galaxies (CO, H α)

- fraction of dark to total matter decreases with z
- DM deficit is more evident at high star formation rate surface densities and galaxies with massive bulges
- low DM fractions can be explained with cored inner DM density

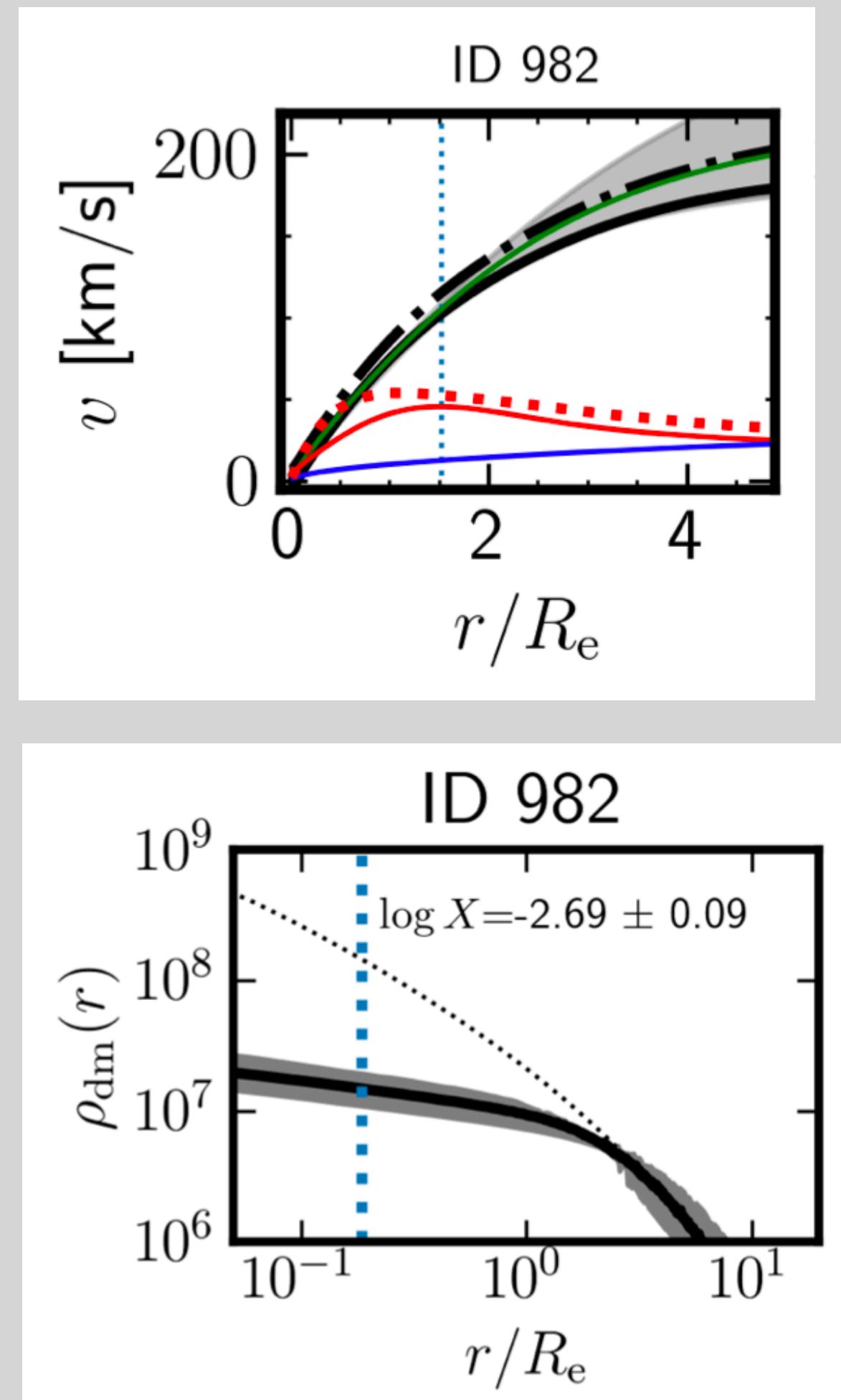


At z~1 - MUSE Hubble Ultra Deep Field: Bouché +2022

- Rotation curve decomposition for 10 z~1 lower mass galaxies
- Model DM halo with: (1) NFW; (2) Di Cintio +2014 profile



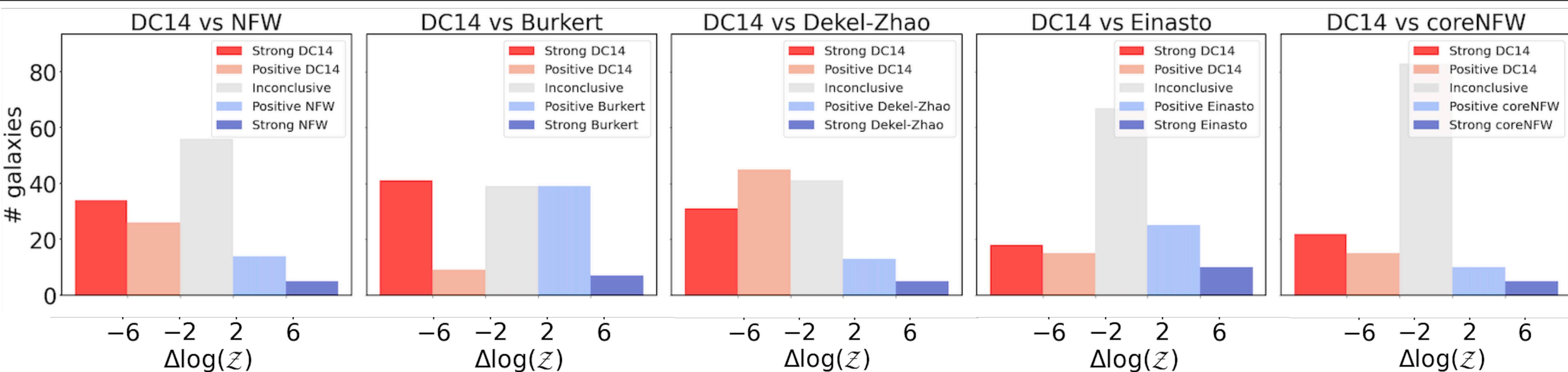
- Di Cintio +2014 profile represents the data better
- Halo parameters agree with expectations
- Evidence for stellar feedback induced cores



At z~1 - MUSE Hubble Ultra Deep Field Survey: Ciocan, Bouché +2024

submitted

- Rotation curve decomposition for 136 galaxies with $0.3 < z < 1.5$ and $7 < \log(M^*/M_\odot) < 11$
- Model DM halos with: (1) NFW; (2) Di Cintio +2014 profile; (3) Burkert (Burkert 1995); (4) Dekel-Zhao (Freundlich et al. 2020b); (5) Einasto (Navarro et al. 2004); and (6) coreNFW

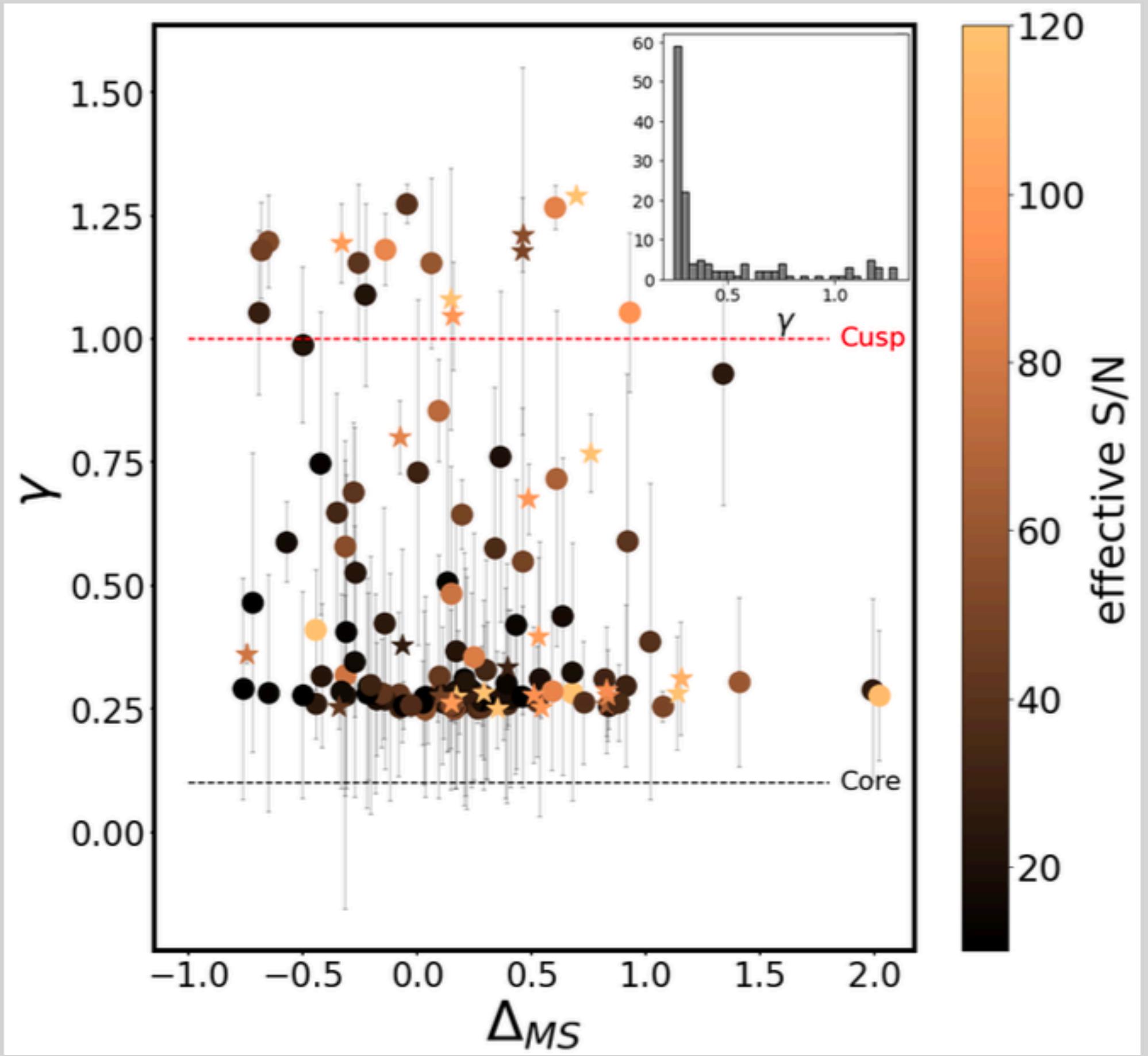


→ Bayesian model comparison: Di Cintio +2014 profile represents the data better



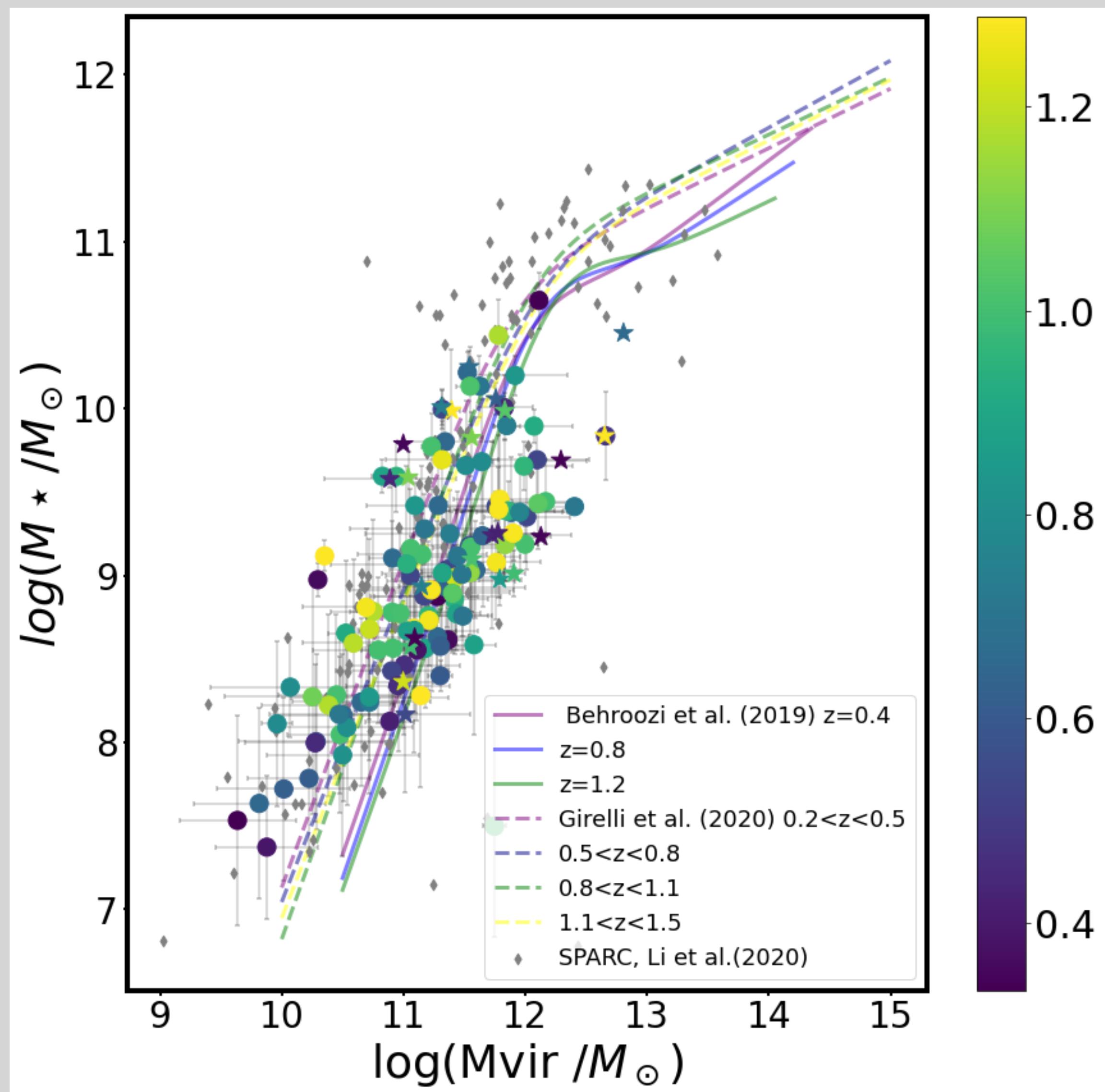
At z~1 - MUSE Hubble Ultra Deep Field Survey: Ciocan, Bouché +2024

- Dark matter inner slope vs offset from star forming main sequence



→ 66% shows cored dark matter density profiles
→ No correlation between the dark matter inner slope and the star formation activity of the sample

► Stellar mass - halo mass relation

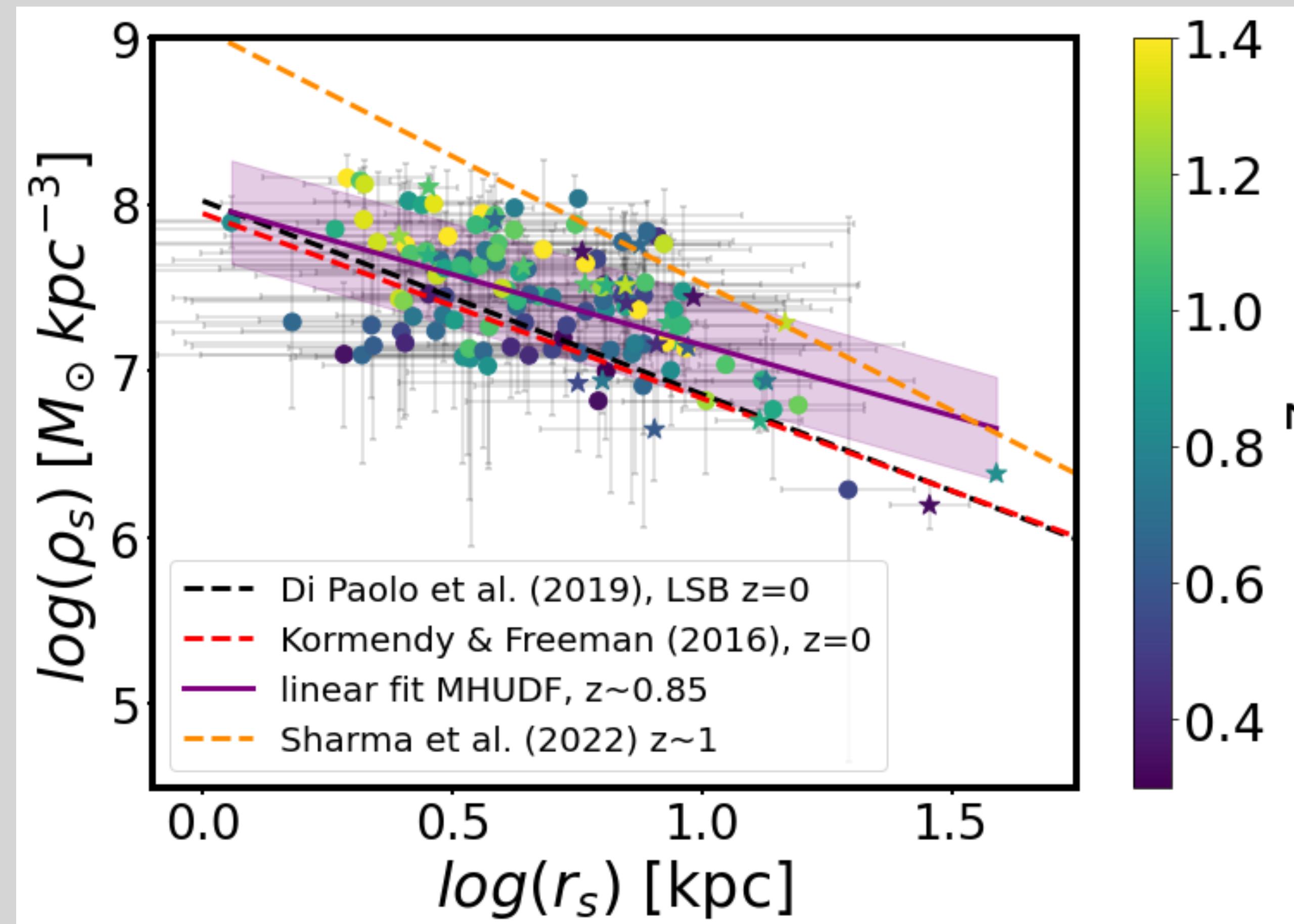


→ in agreement with the predictions
from Behroozi+2019 and Girelli+2020

► Halo scale radius - density relation

3D

GalPaK
galaxy parameters and kinematics



$$\rho \propto R^{-3(3+n)/(5+n)}$$

(Djorgovski 1992)

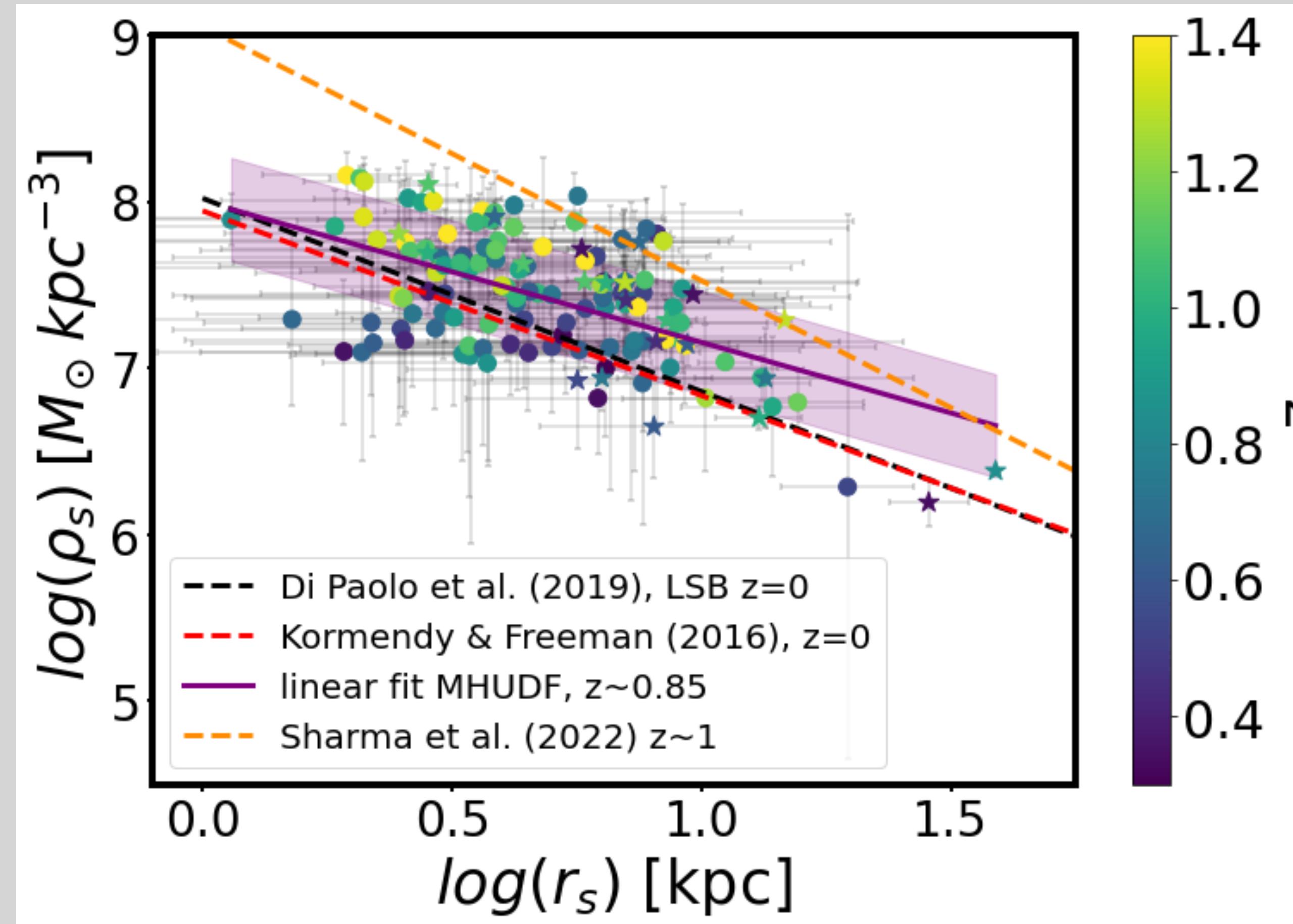
$$n \sim -2$$

→ anticorrelation results from the expected scaling
relation of DM predicted by hierarchical clustering

► Halo scale radius - density relation

3D

GalPaK
galaxy parameters and kinematics



→ evolution of halo characteristic density with z

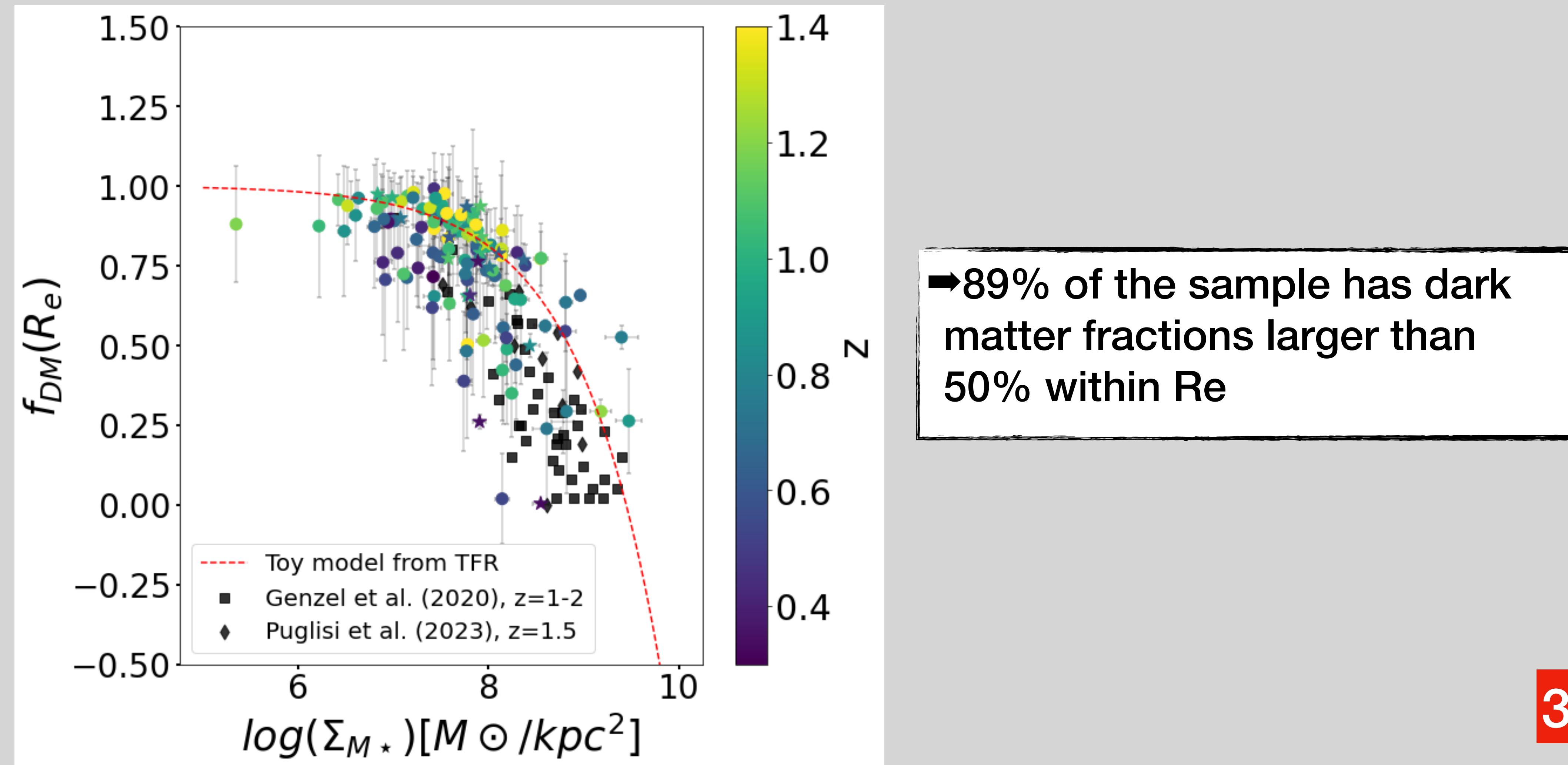
$$\rho \propto R^{-3(3+n)/(5+n)}$$

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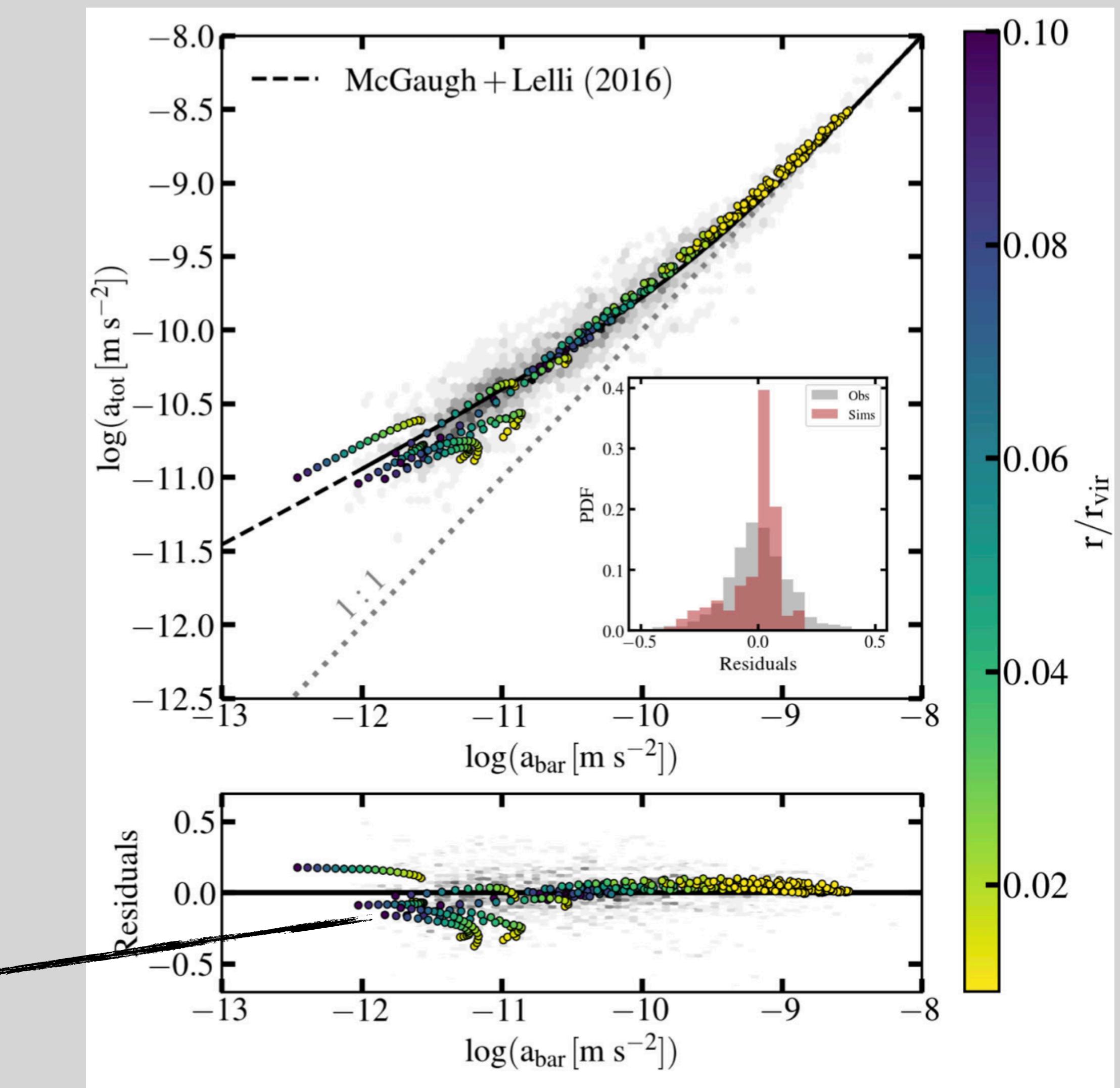
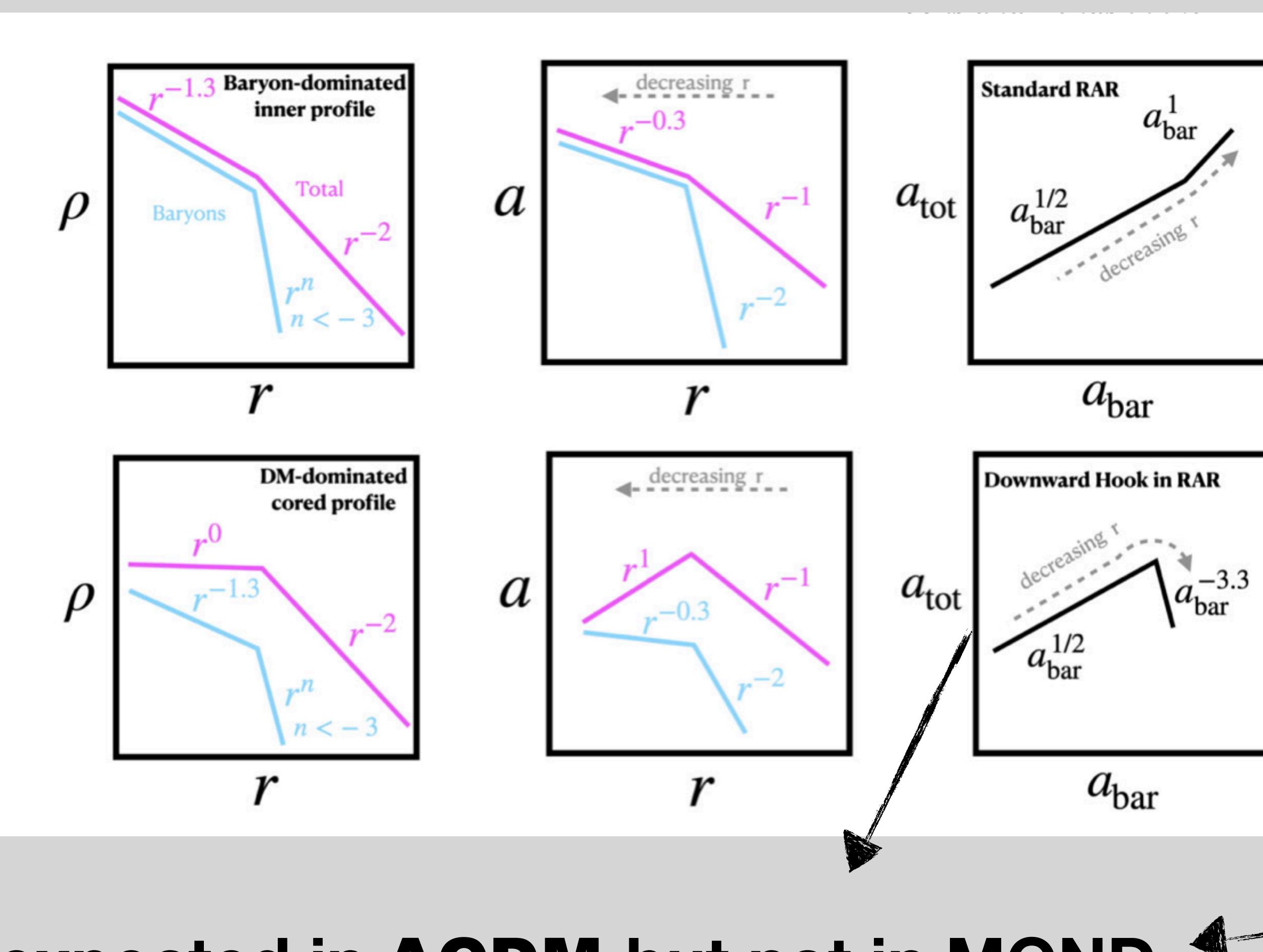
$$n \sim -2$$

→ anticorrelation results from the expected scaling relation of DM predicted by hierarchical clustering

- Dark matter fraction - stellar mass surface density relation

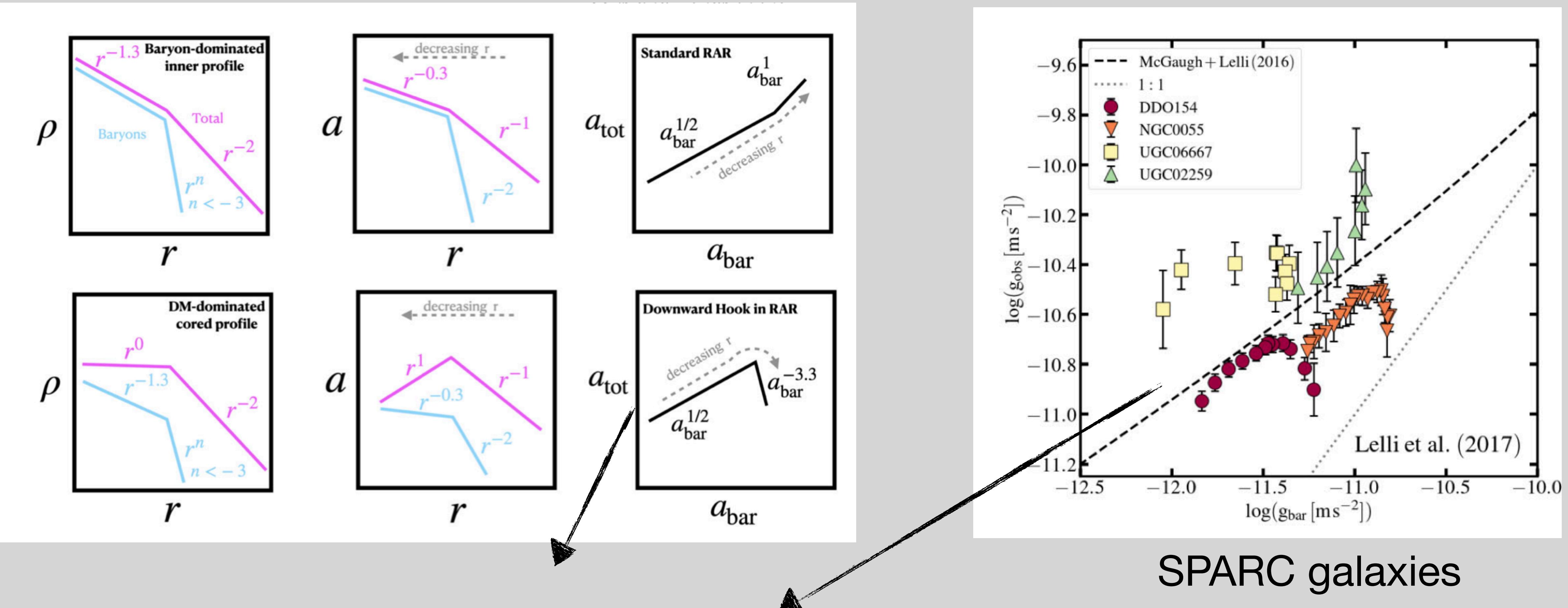


► RAR relation -predictions from FIRE-2 simulations (Mercado+24)

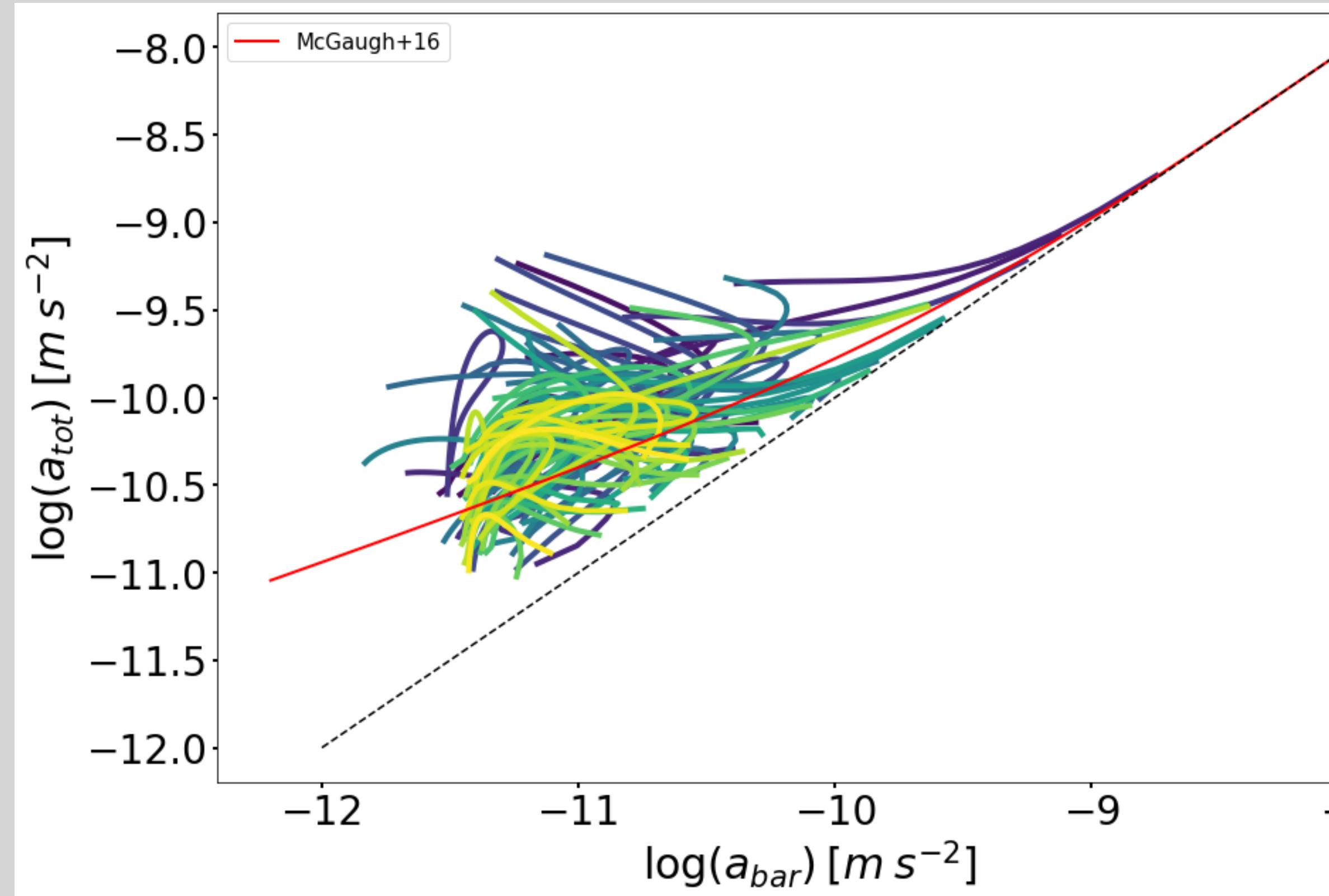


expected in Λ CDM but not in MOND

► RAR relation -predictions from FIRE-2 simulations (Mercado+24)

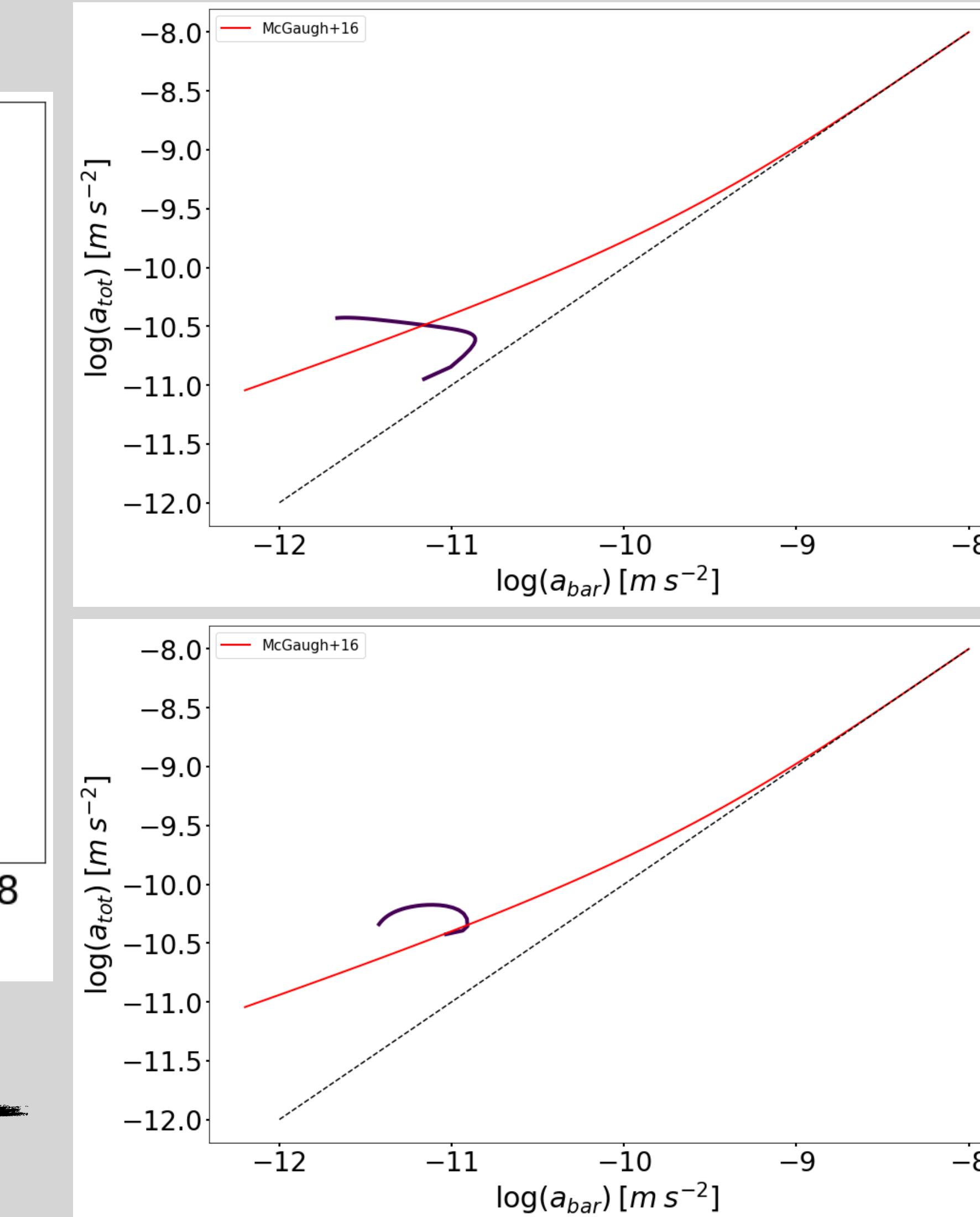


RAR relation



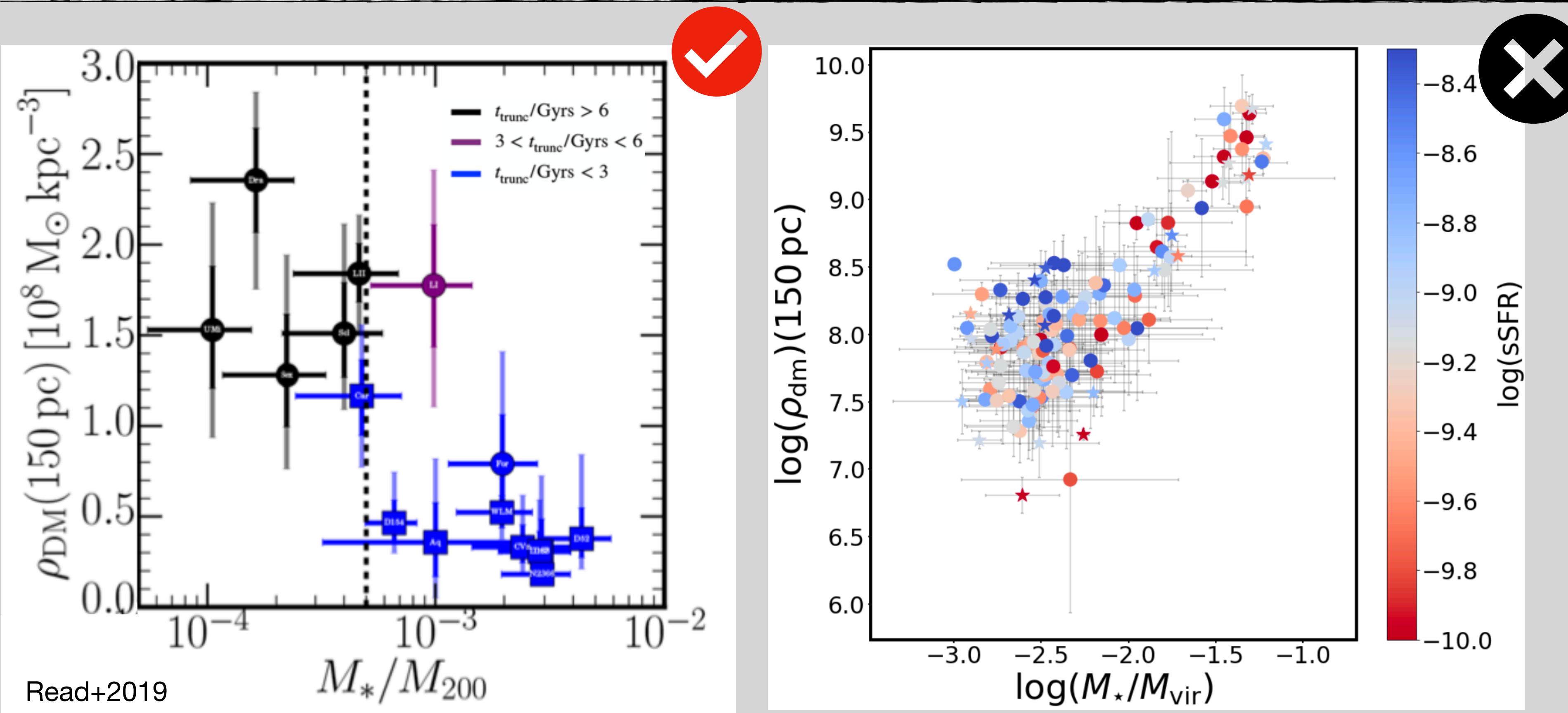
Rules out MOND ???

For cored galaxies



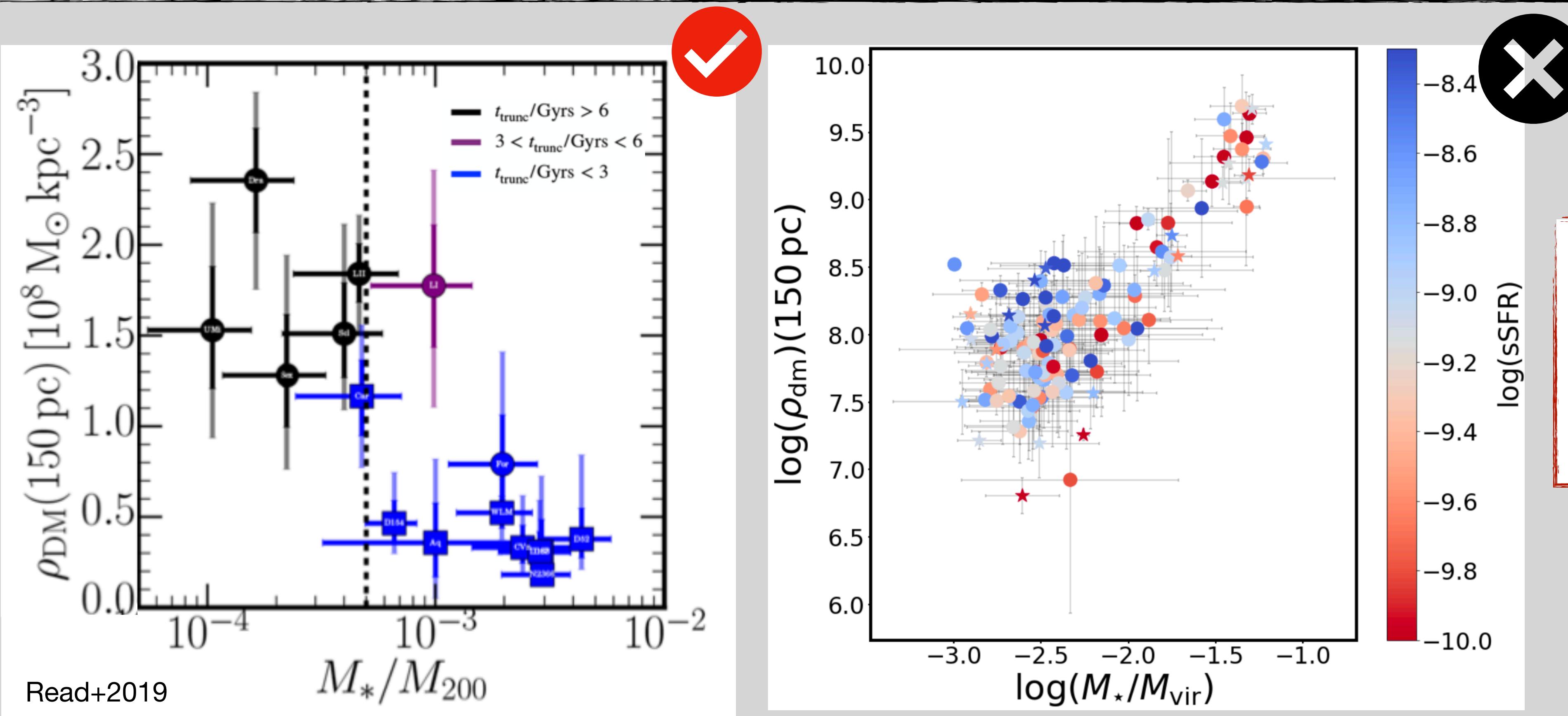
Is baryonic feedback the answer?

- Observationally, cores have been detected up to $z \sim 2$
- No clear correlation between core formation and stellar feedback yet



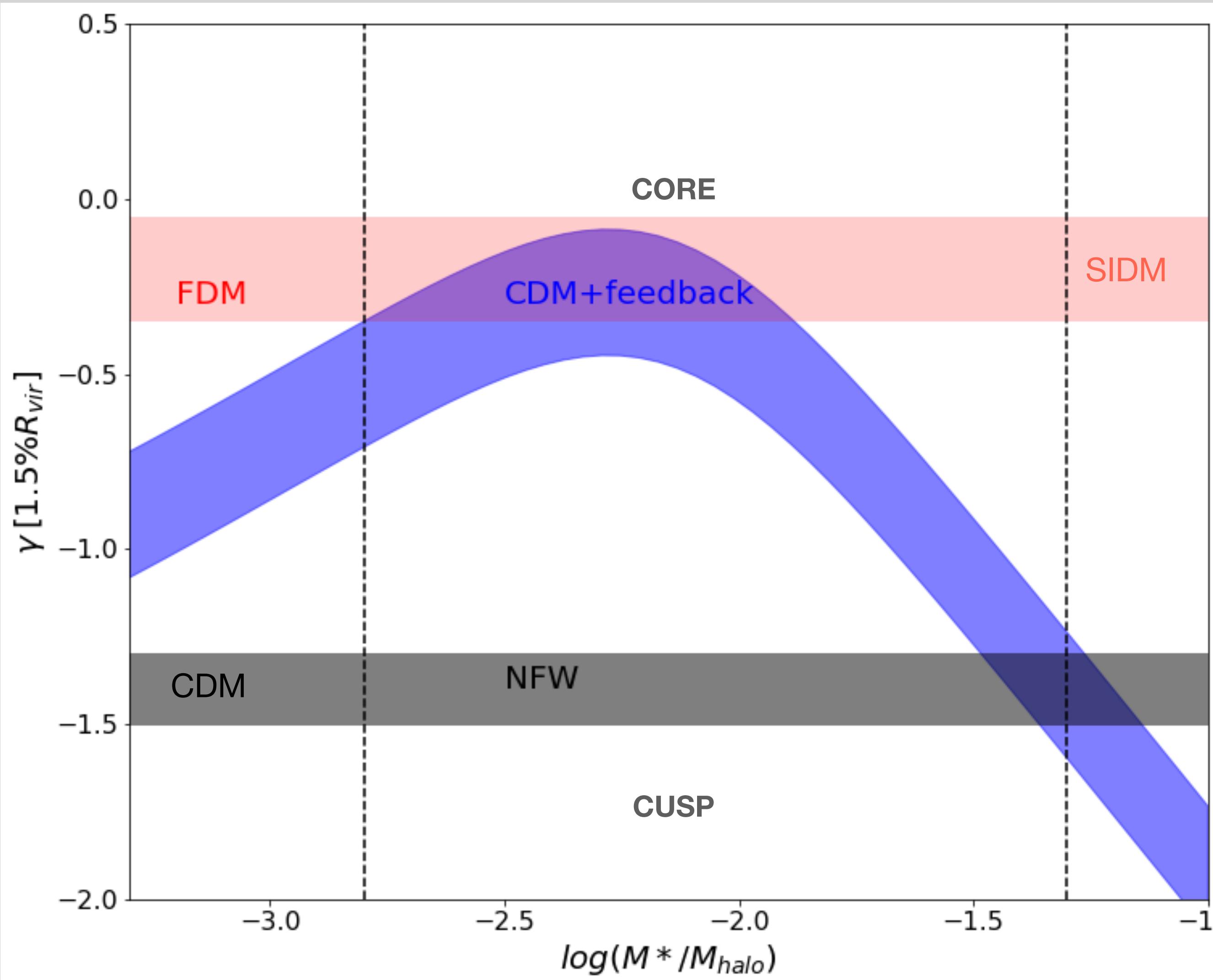
Is baryonic feedback the answer?

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► Need to link dark matter densities / inner slopes to the star formation histories

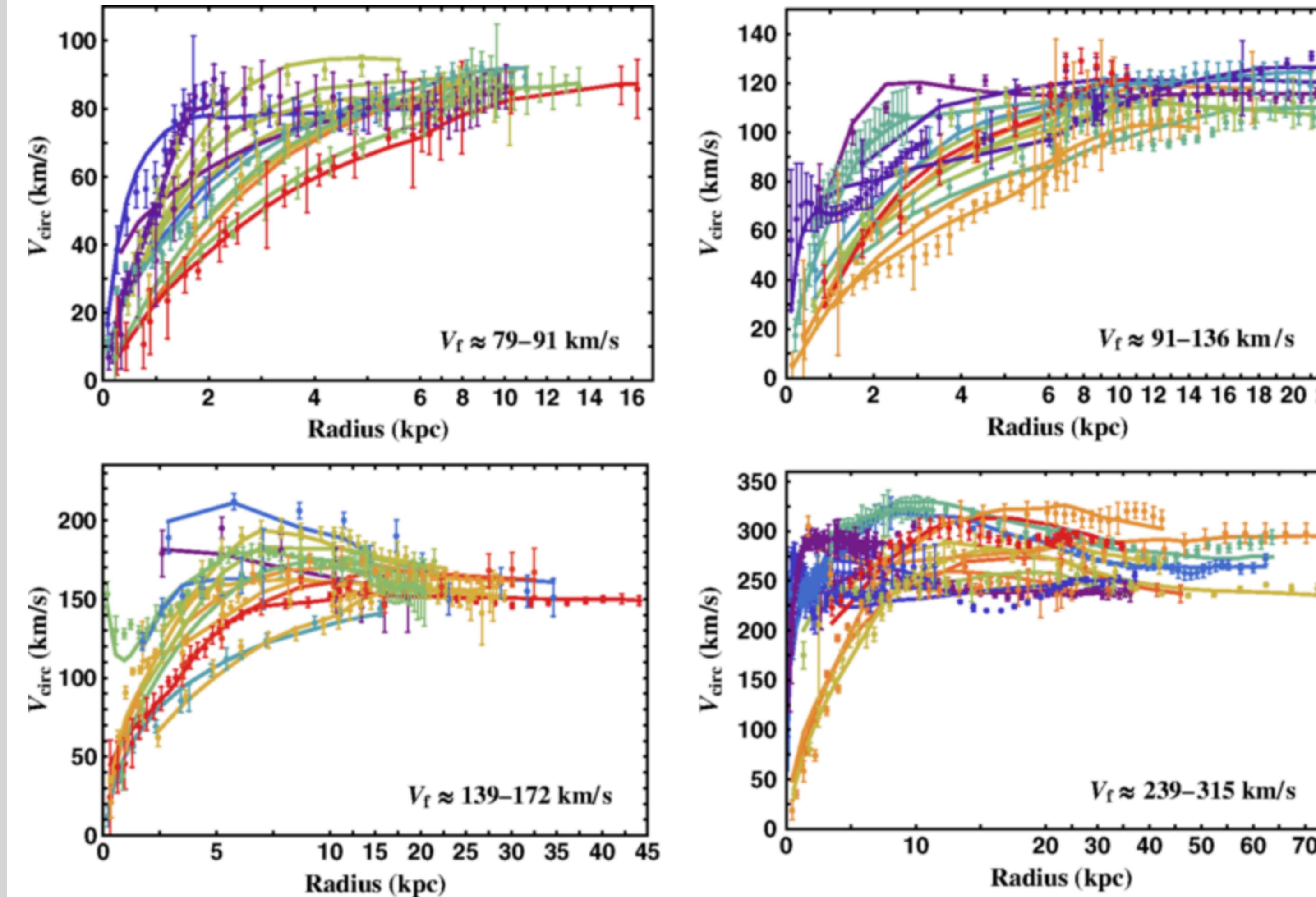
Core-cusp problem: alternative solutions



- alternative models of dark matter:
 - ▶ **self-interacting dark matter** ([Spergel +2000](#))
 - ▶ **axion-like fuzzy dark matter** ([Hu+2000](#))
 - ▶ **warm dark matter** ([Bode+2001](#))

Diversity of Rotation Curves: alternative solutions

FIG. 1.

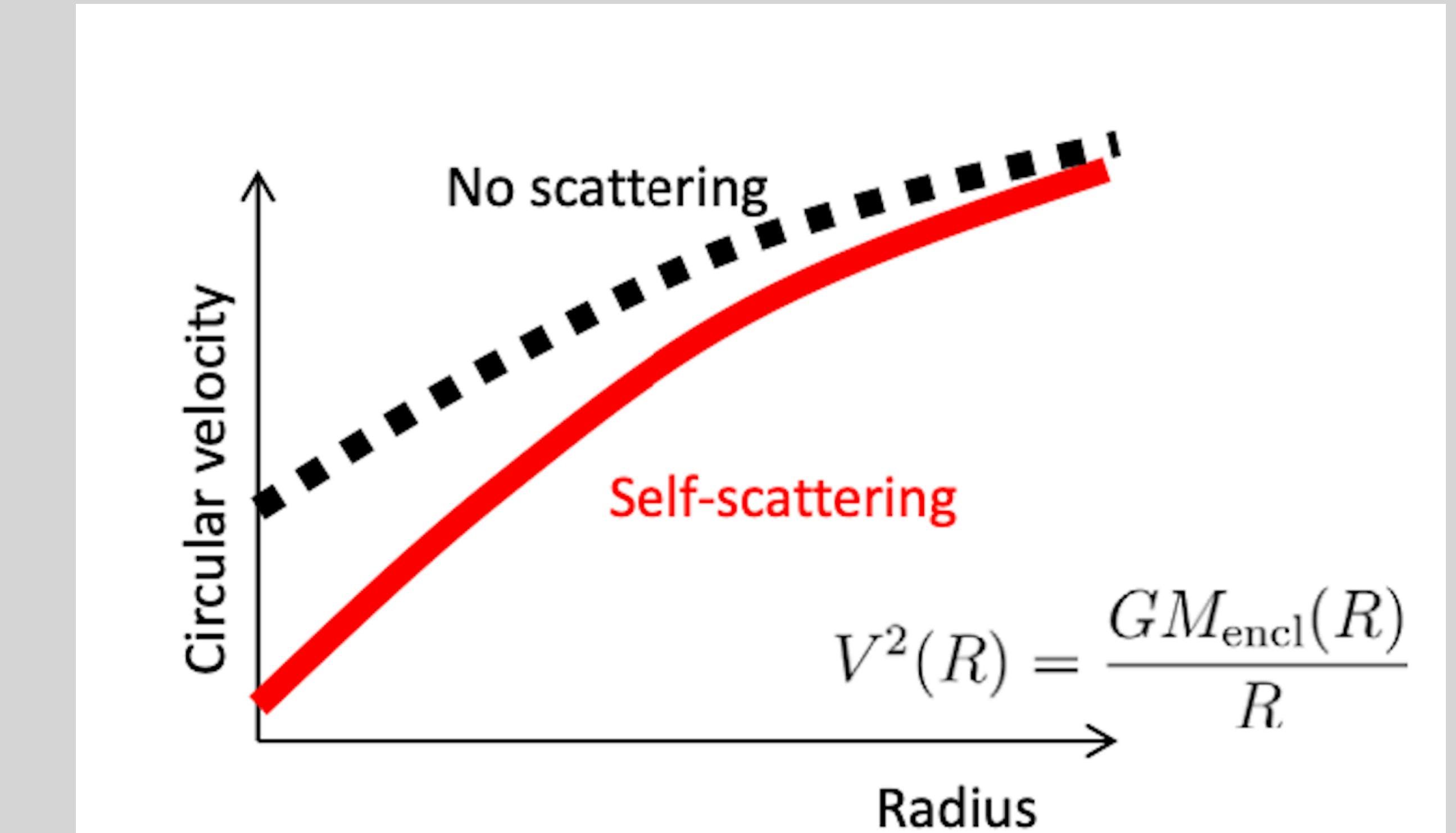
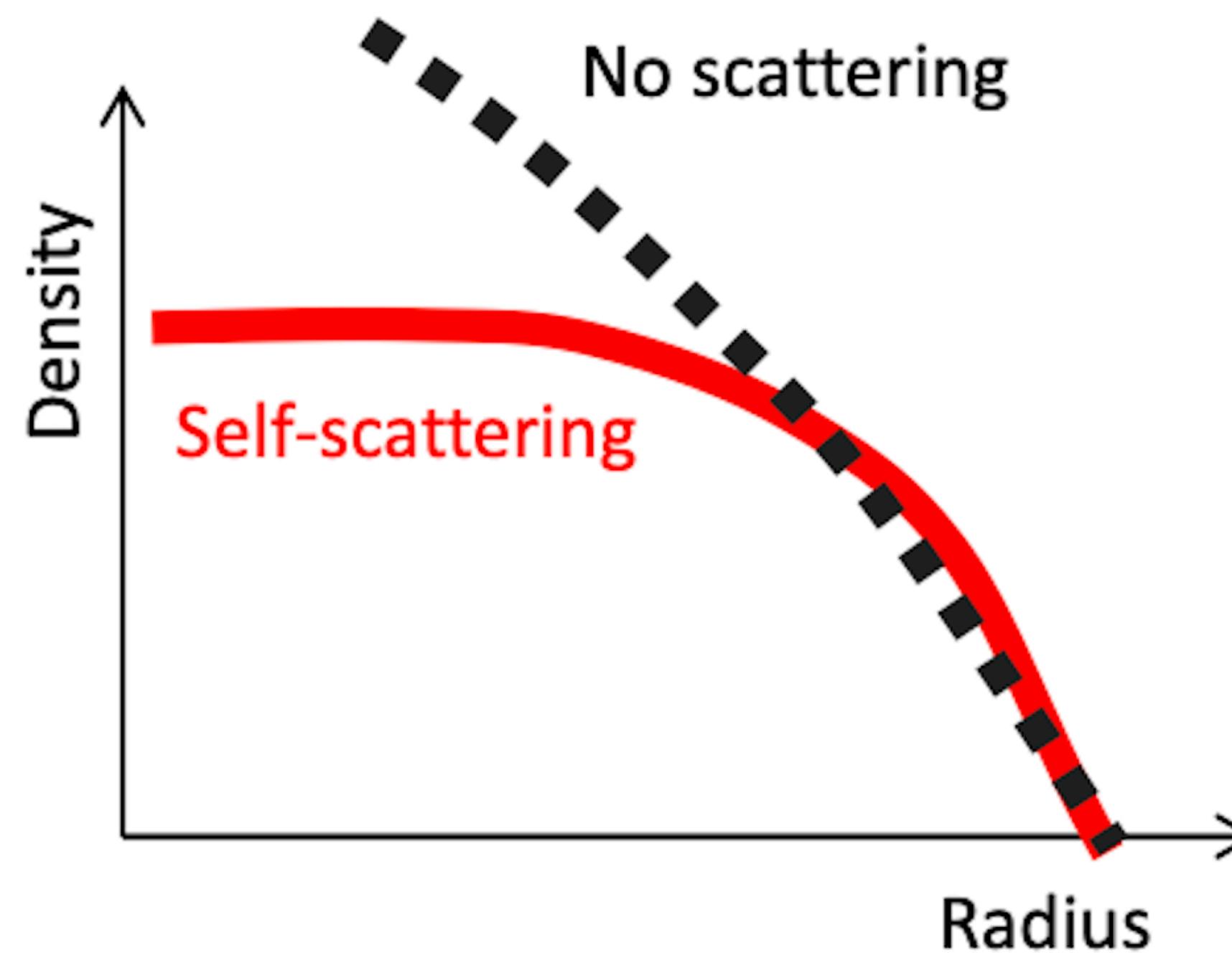


→ alternative models of DM:
► self-interacting dark matter

Ren +2019, Kamada+2017

Self Interacting Dark Matter

→ the particles have a significant self-interaction cross section



Self-interactions solve core-vs-cusp
Particles get scattered out of dense halo centers

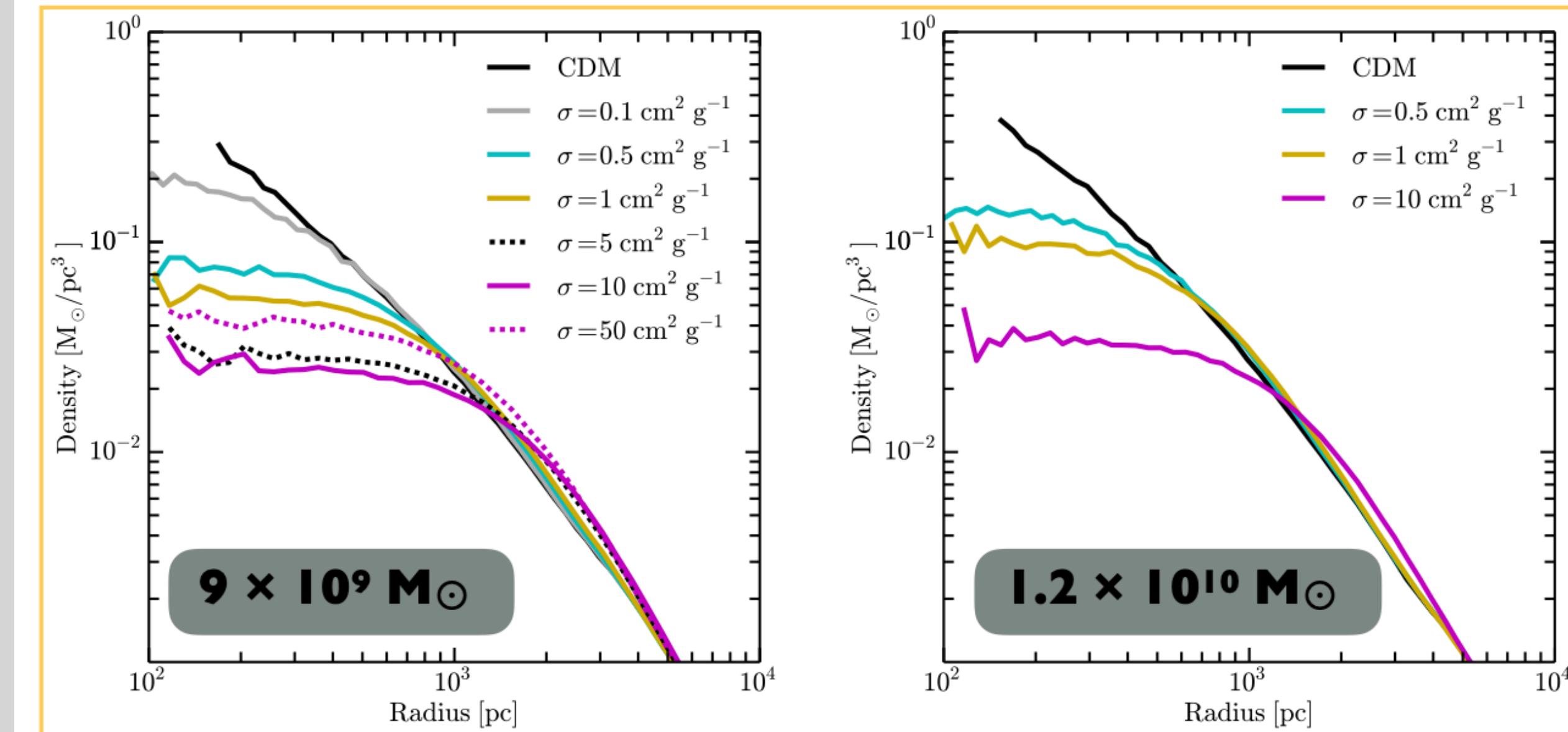
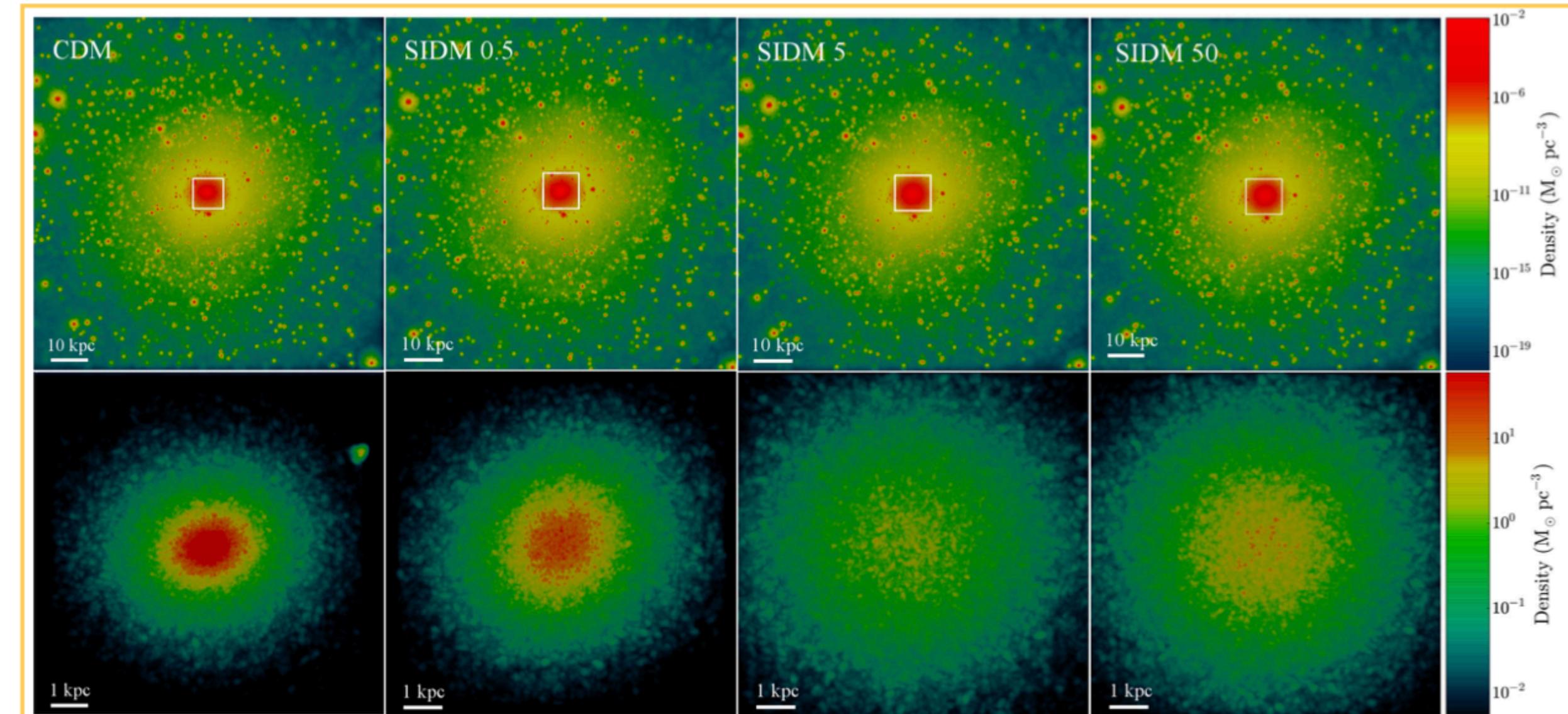
Self Interacting Dark Matter

→ parameter governing the rate of DM particle interactions is the cross section per unit mass: $\sigma/m\chi$

→ $\sigma/m\chi$: velocity dependent

$\sigma/m \sim 0.5 - 50 \text{ cm}^2/\text{g}$ to form kpc core in dwarf galaxy

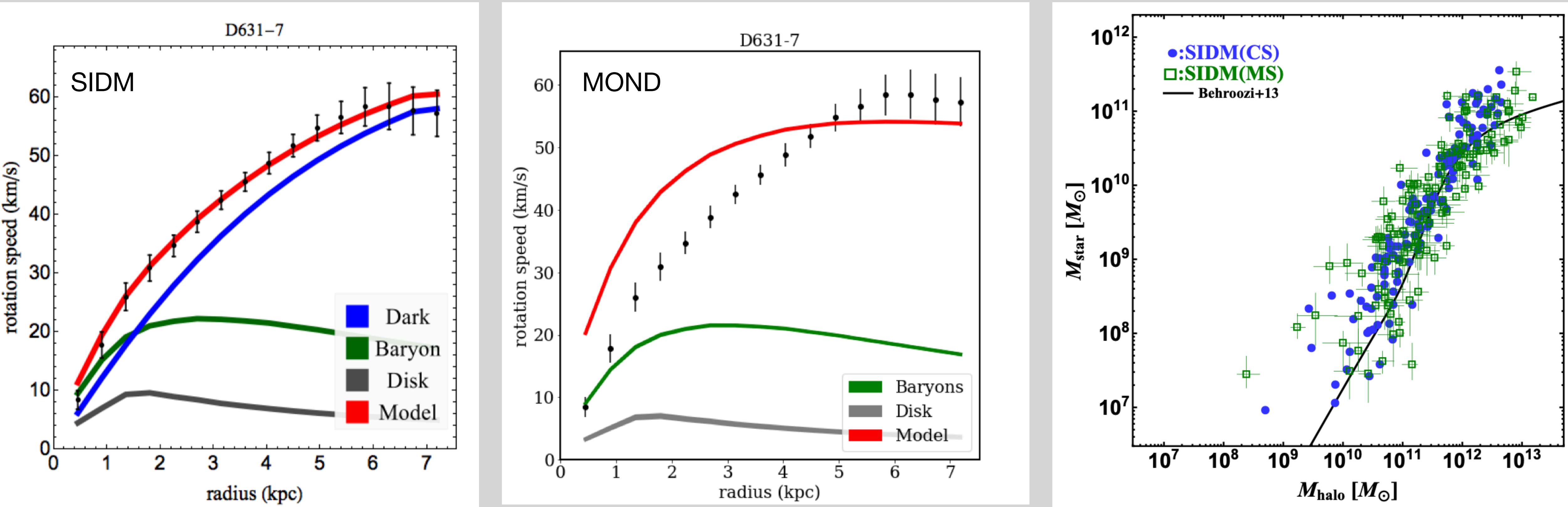
→ shares the success of Λ CDM on large scales



Elbert et al. 2015

Self interacting Dark Matter and rotation curves: Ren +2018

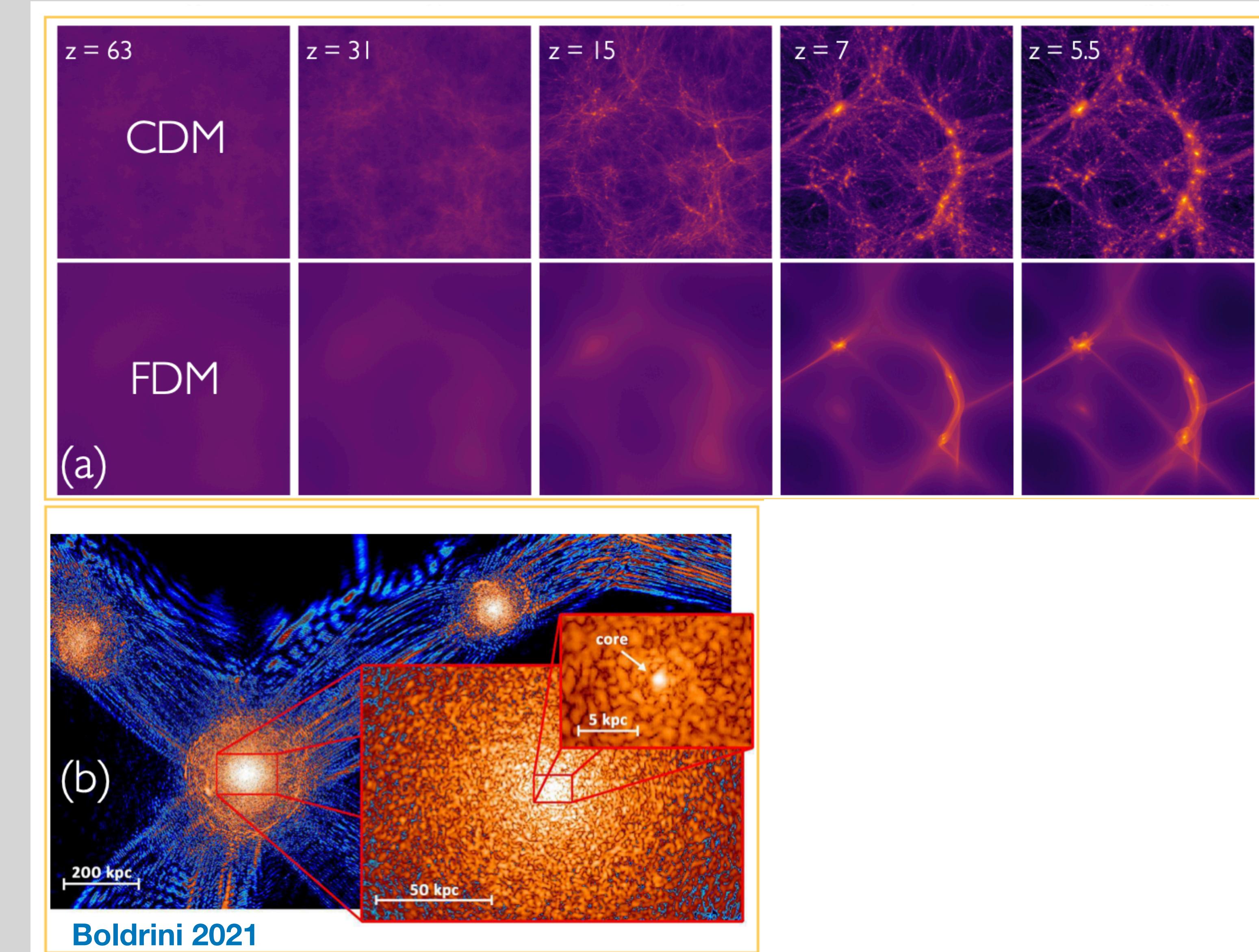
- Rotation curve decomposition for 135 local galaxies (SPARC sample - Ha+HI)
- Constant $\sigma/m = 3 \text{ cm}^2/\text{g}$



- SIDM preferred over MOND
- recover stellar mass-halo mass relation, i.e. host halos are fully consistent with the Planck cosmology

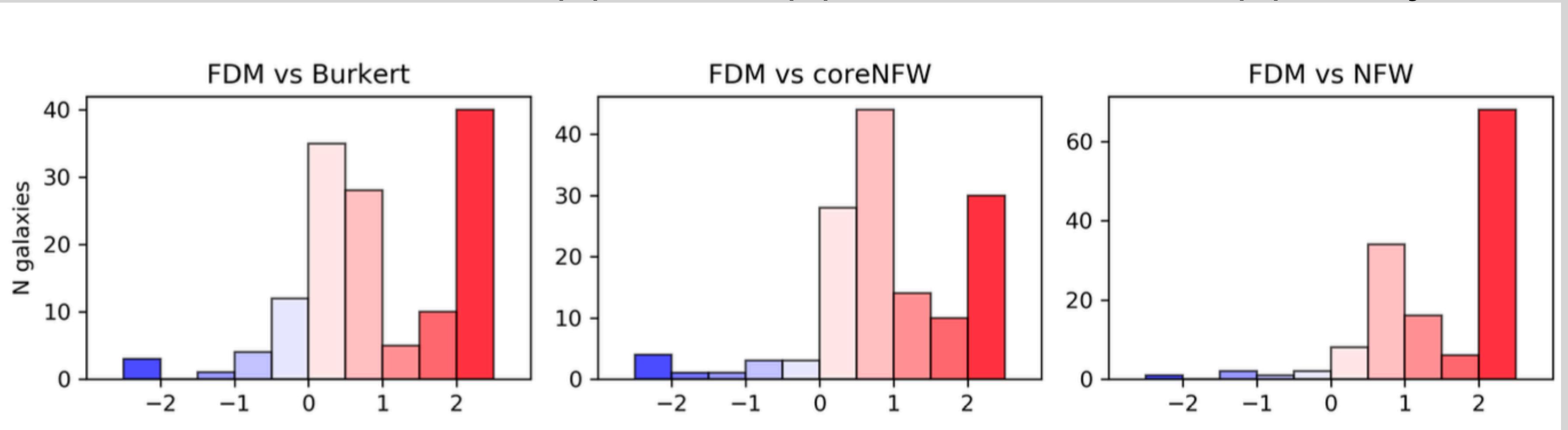
Fuzzy dark matter

- Ultralight scalar field with no self-interactions in the non-relativistic limit
- low masses: $\sim 10^{-24}$ to 10^{-19} eV
- suppresses structure formation on small scales
- wave nature of FDM leads to quantum pressure, preventing cusps
- form a Bose-Einstein condensate soliton

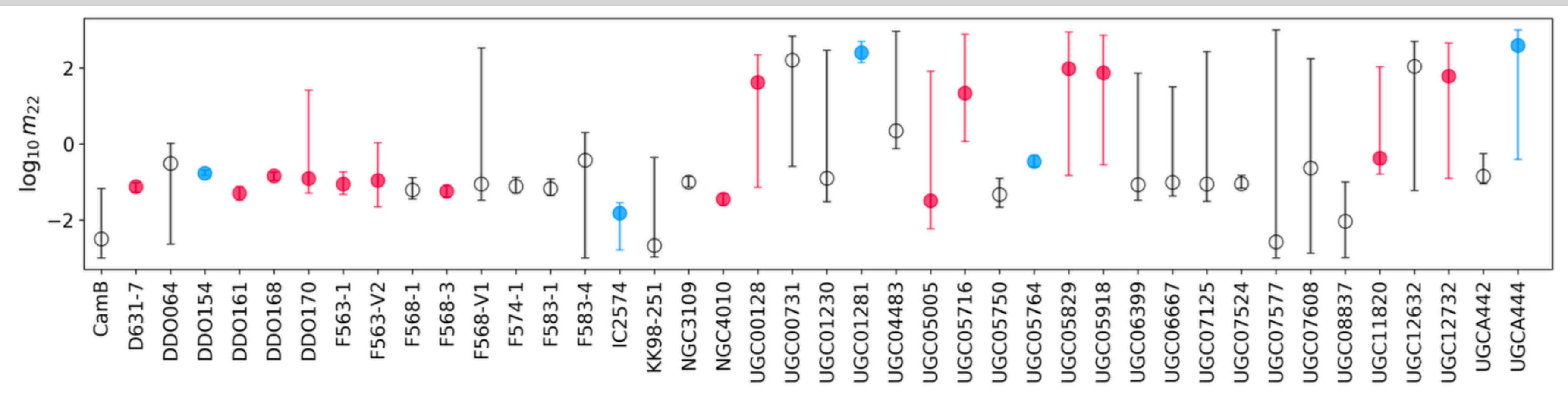


Fuzzy dark matter and Rotation Curves: Khelashvili+23

- Rotation curve decomposition for 175 local galaxies (SPARC sample - Ha+HI)
- Model DM halo with (1) NFW; (2) coreNFW; and (3) fuzzy DM



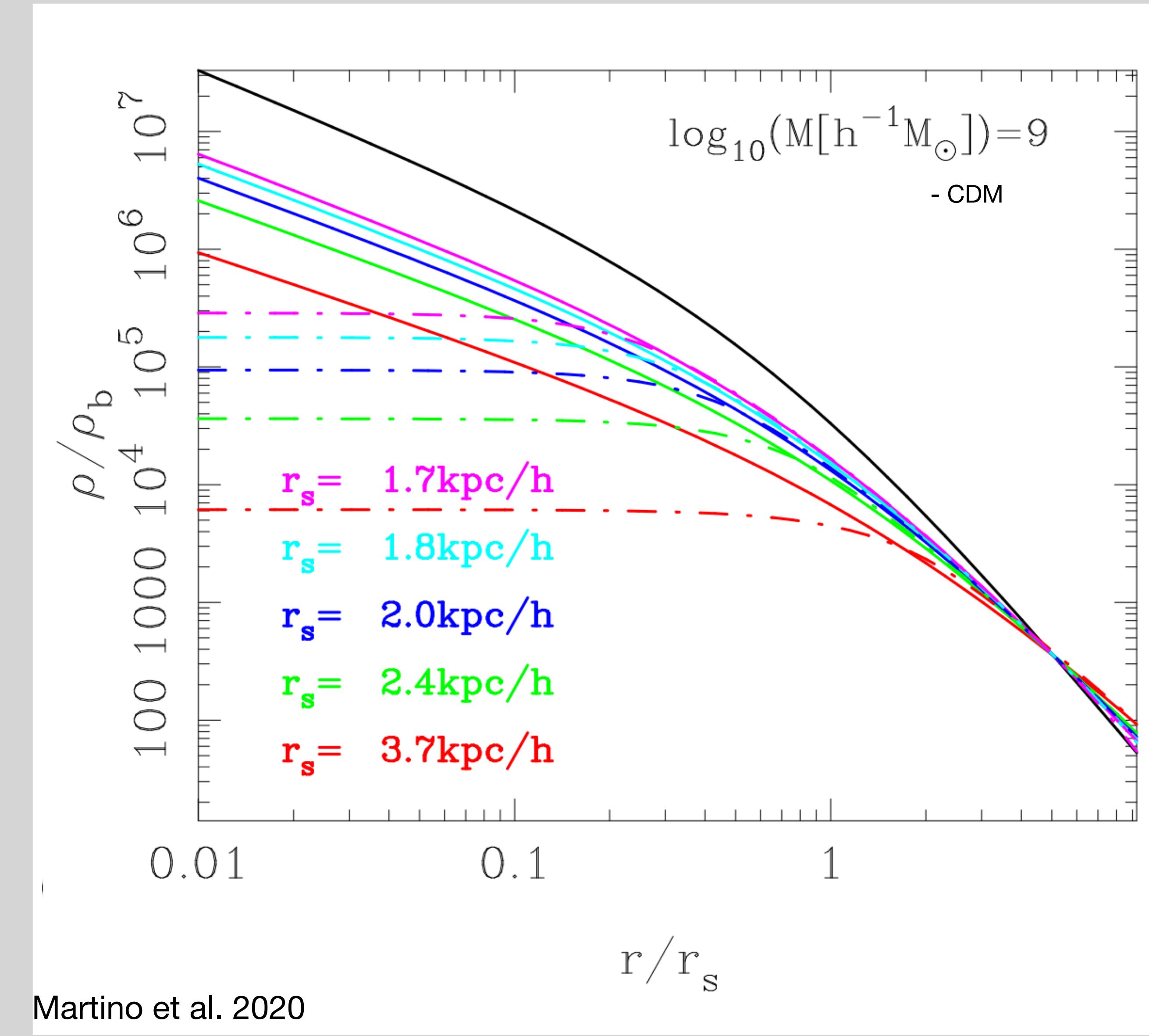
→ Fuzzy DM preferred by >50% of the sample



→ No single value for the particle mass that provides a good fit for all galaxies

Warm Dark Matter

- WDM particles decouple when they are still relativistic
- erase primordial fluctuations on subgalactic scales
- produce a cut-off in the primordial power spectrum
- reduce phase-space density resulting in the formation of cores
- observations of strong gravitational lensing / Lyman-a forest: particle mass of $> 5.58 \text{ keV} / > 3.5 \text{ keV}$

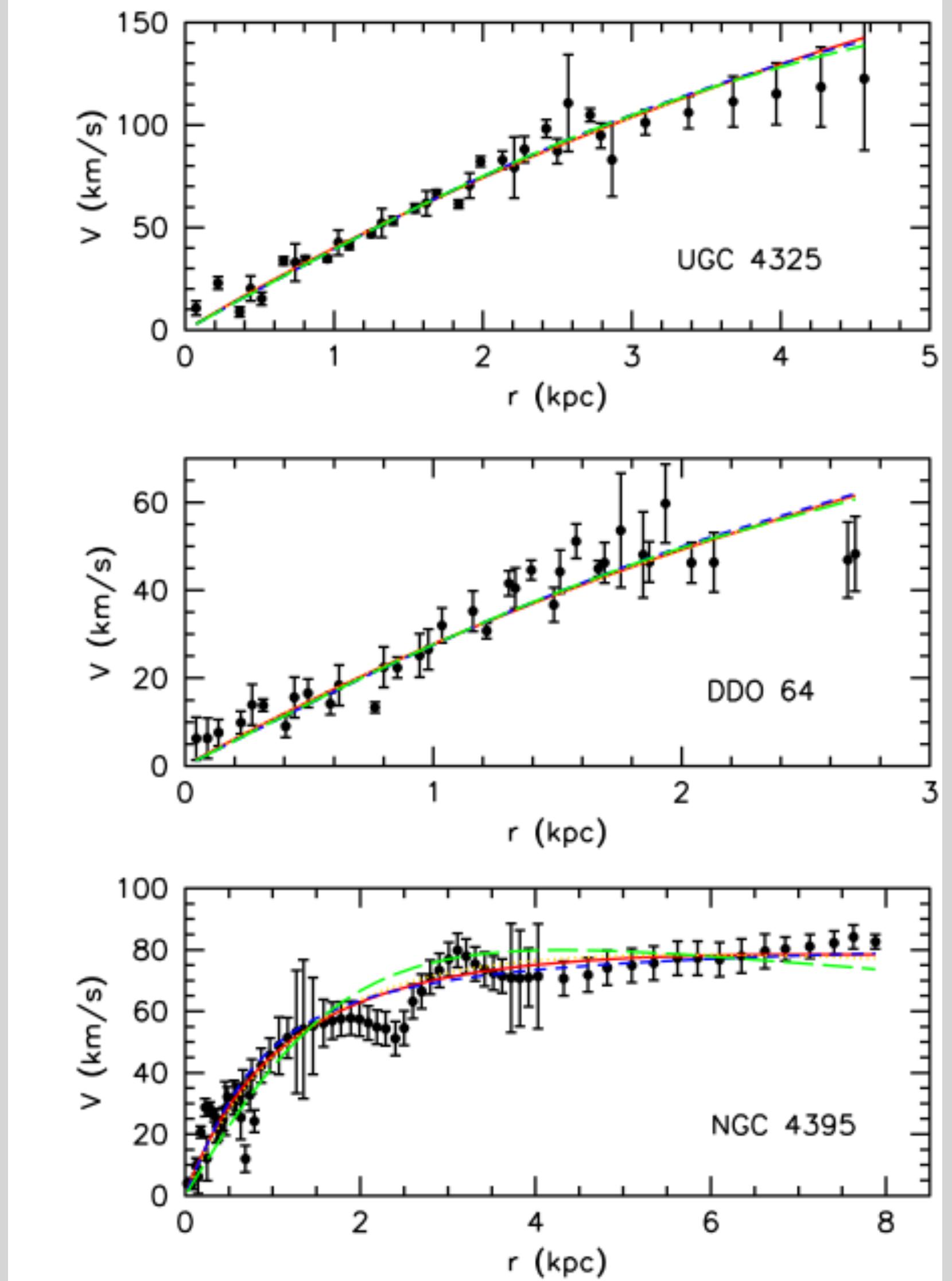
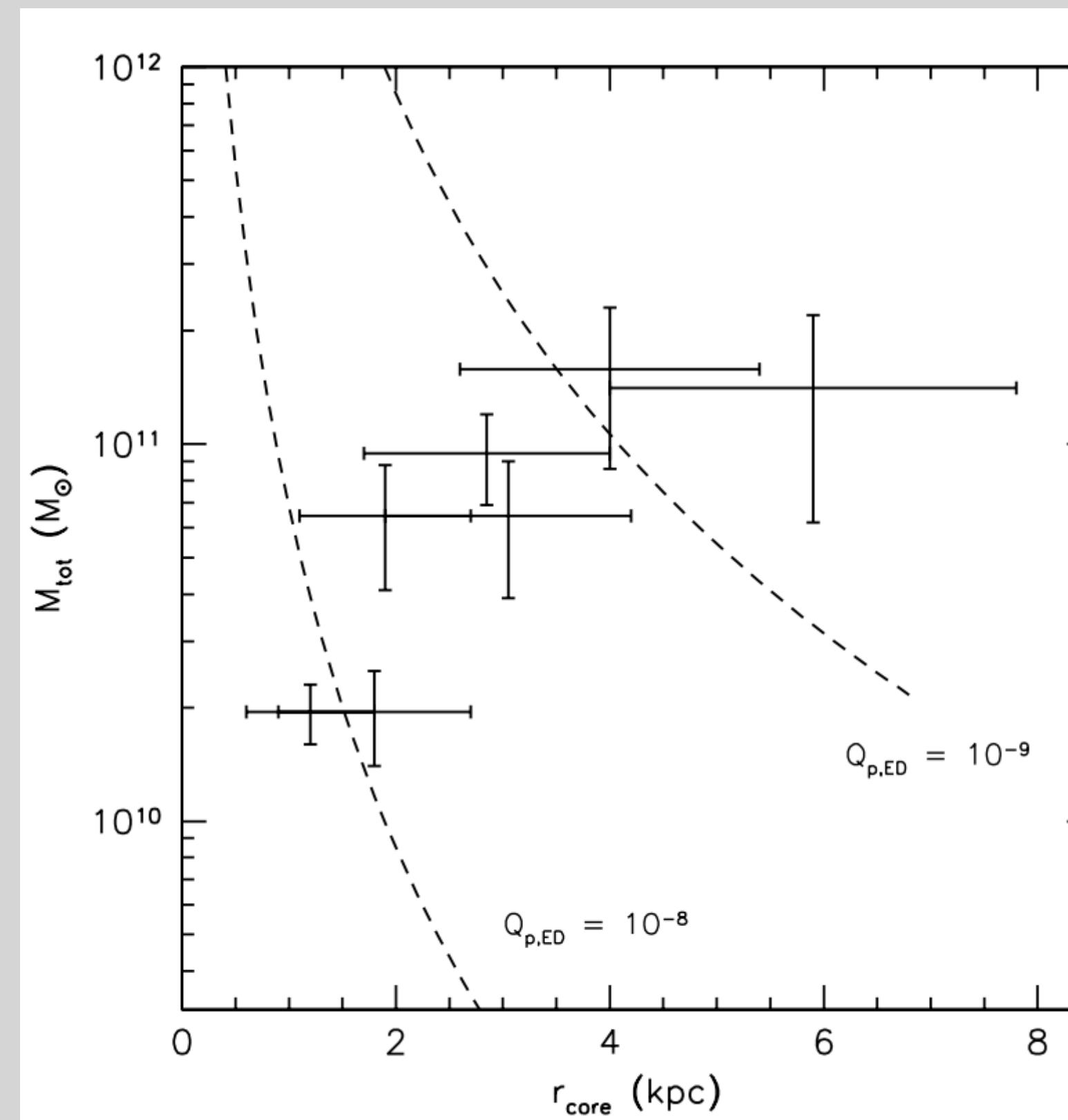


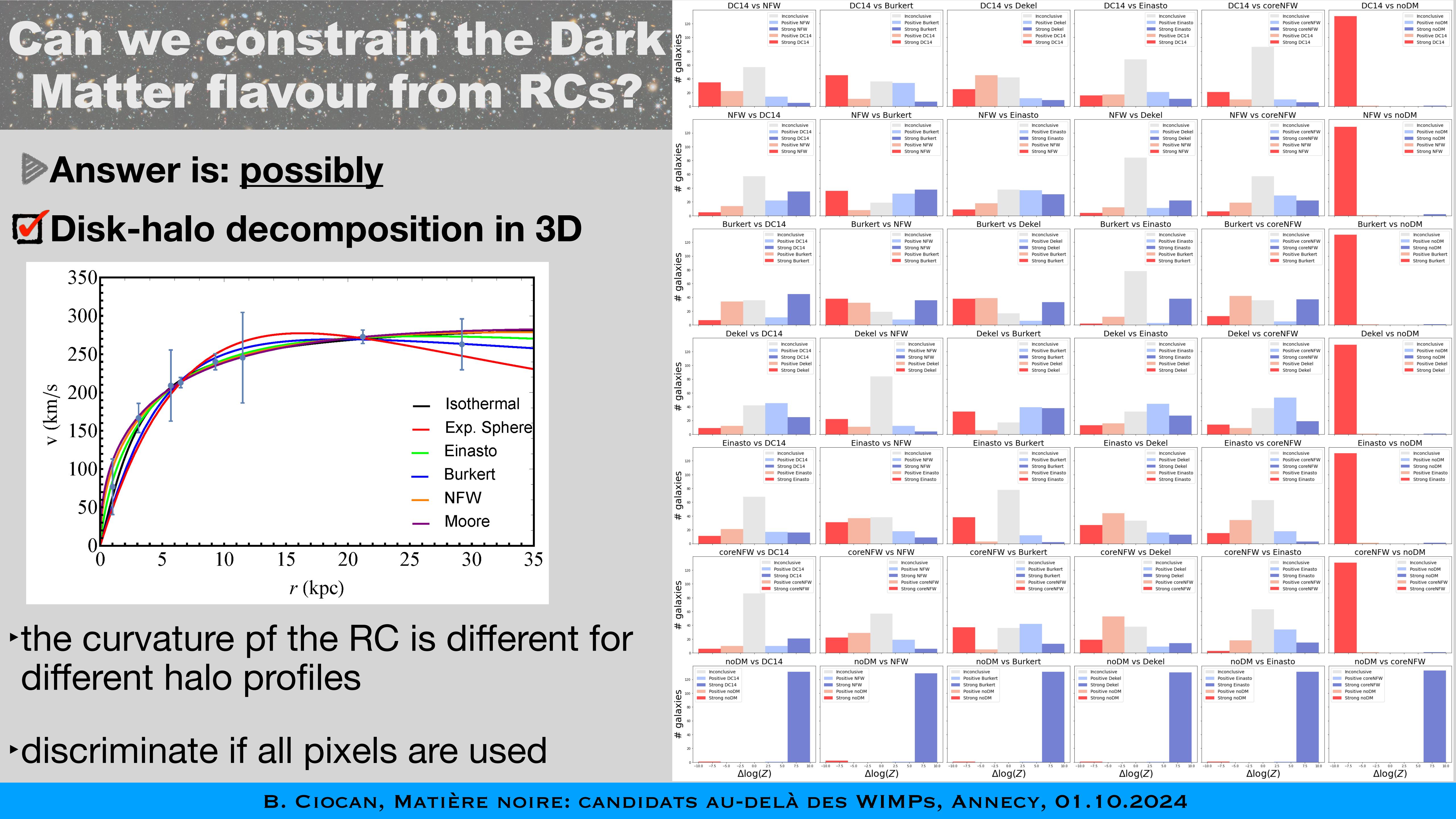
Warm Dark Matter and Rotation Curves: Kuzio de Naray+2010

- use rotation curves of 9 local low surface brightness galaxies
- test WDM, non-thermal WDM, and SIDM

Problems for WDM:

- does not manage to solve core-cusp problem with one particle mass for all galaxies
- inferred r_{core} increase with halo mass while predictions state the opposite

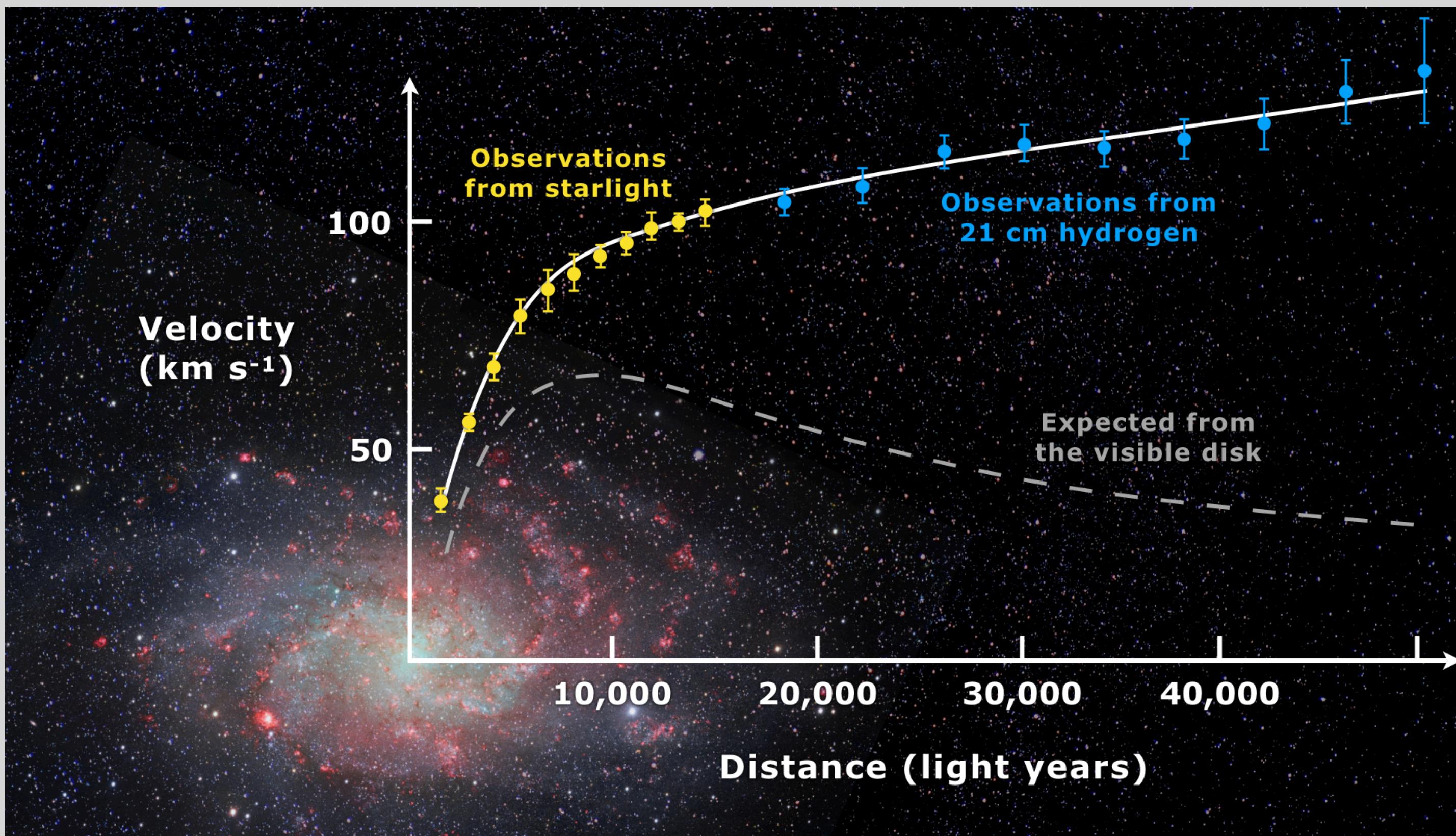




Outlook

- **Improving precision of rotation curve measurements:** Higher resolution, deep IFU data and advancements in 3D modelling techniques can help improving dark matter profile constraints.
- **Probing larger samples (at high redshift $z > 1$):** With more observational data from next generation instruments, we can extend rotation curve studies beyond the local Universe to explore the evolution of dark matter properties over cosmic time.
- **Linking DM profiles to galaxy star formation histories:** Combining star formation histories and DM profiles will offer further insights into the connection between baryonic feedback and DM distribution.
- **Testing alternative DM models:** SIDM, FDM, WDM models need to be tested against larger datasets and a wider variety of galaxy types to refine their viability in addressing small-scale structure problems.
- **Need for simulations:** High-resolution cosmological simulations that incorporate baryonic physics will be crucial to further testing predictions of the alternative DM models.

Thank you for your attention!



Extra

Using 3D forward modelling: Under the hood



Bouché et al. 2015

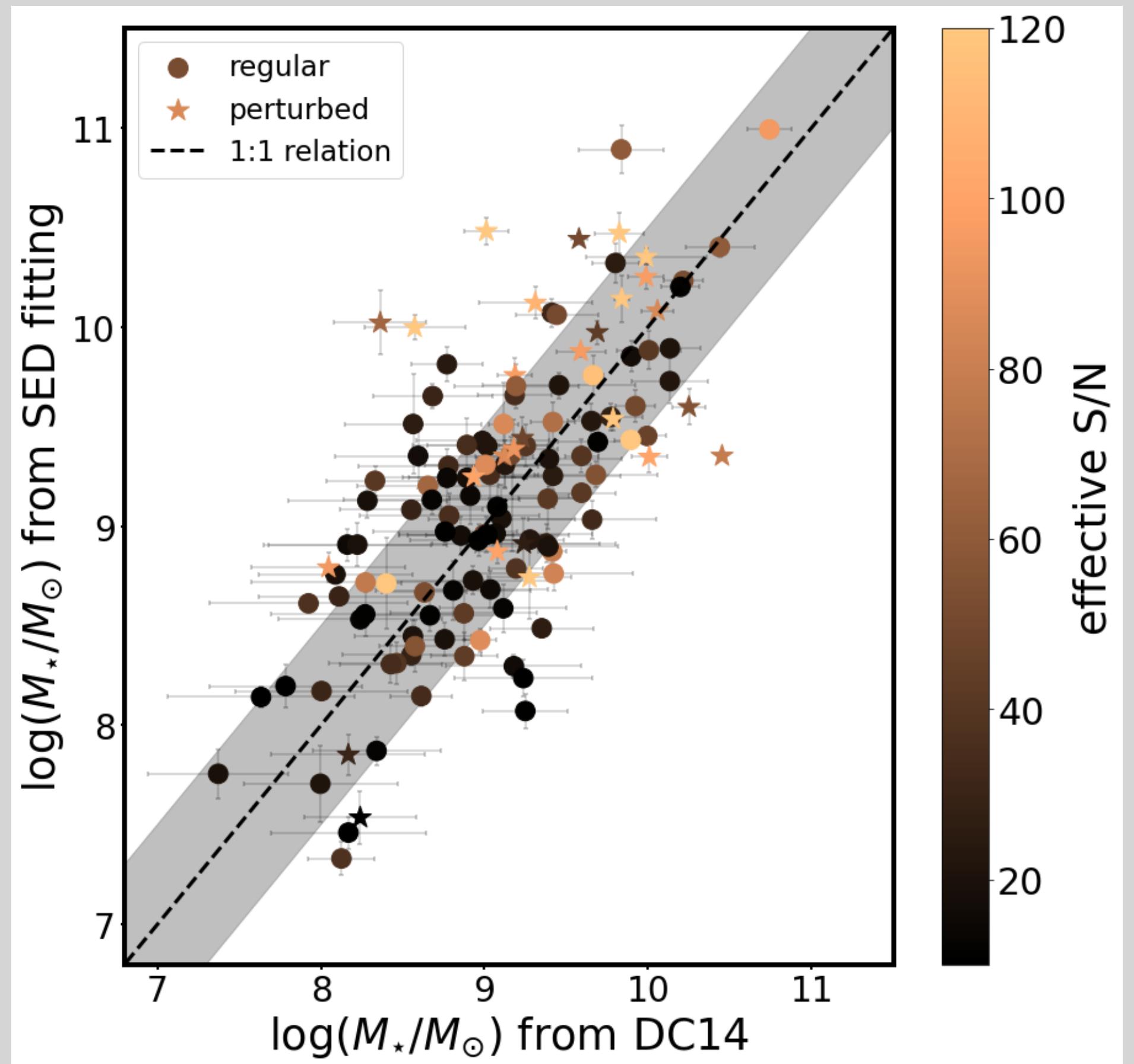
$$v_c(r)^2 = v_{\text{DM}}(r)^2 + v_{\text{disk}}(r)^2 + v_{\text{HI}}(r)^2$$

- 1) DM: different Dark Matter halo profiles
- 2) Disk: $I(r)$: Sersic n (OII,Ha); Freeman Disk
- 3) gas: HI gas (marginalized)
- 4) **pressure support correction (asymmetric drift correction)**

$$v_c(r)^2 = v_{\perp}(r)^2 + v_{\text{AD}}(r)^2$$

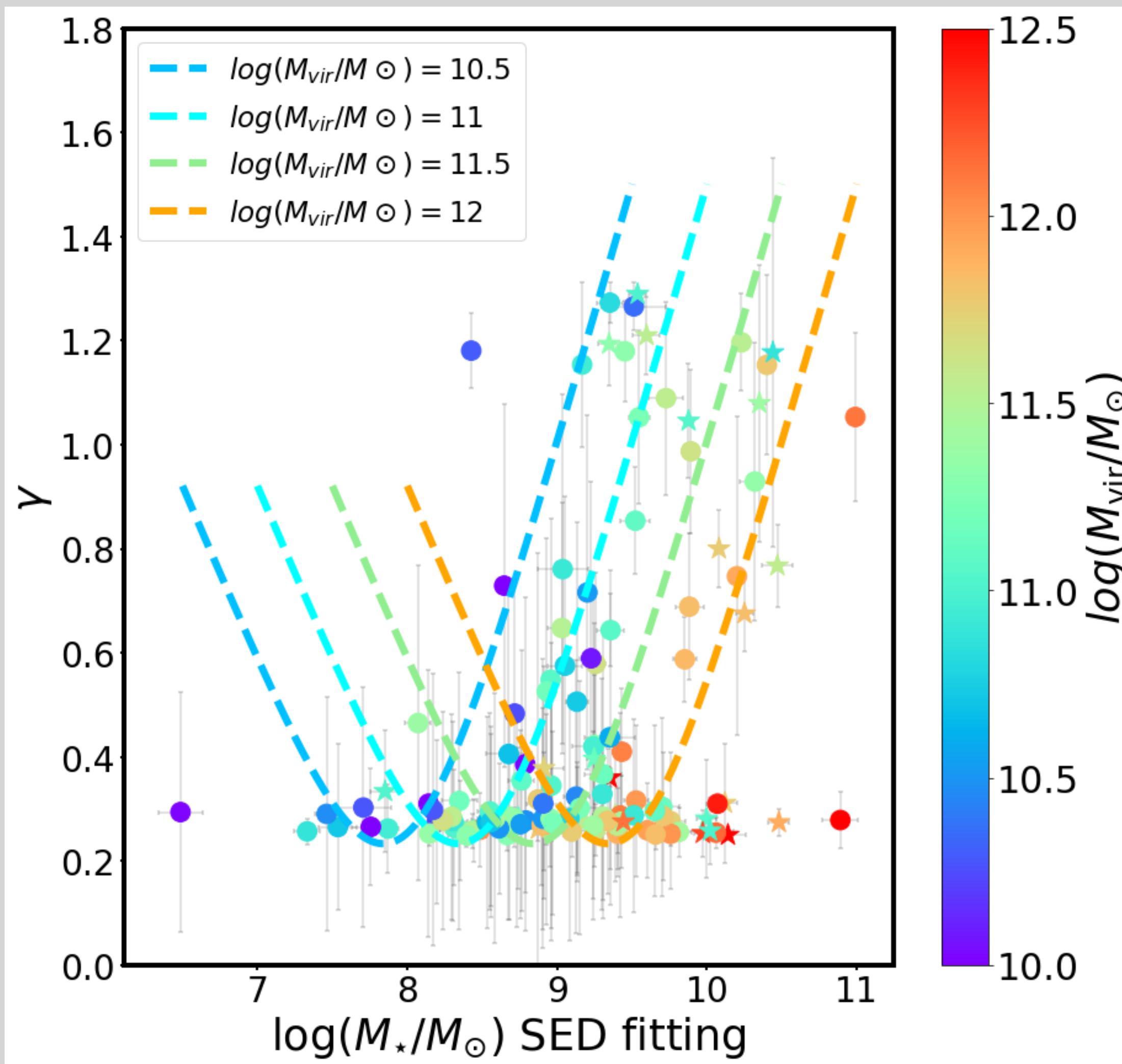
- 13 - 15 free parameters ($x, y, z, \text{incl}, \text{PA}, M^*, M_{\text{vir}}, C_{\text{vir}}, \text{sig0}, \text{Re}, n, \dots$)
- all optimised simultaneously directly on the 3D IFU cube

- **Consistency checks for DC14**



→ The kinematically inferred M^* agree with the ones derived from photometry

► Consistency checks for DC14



→ Inferred DM inner slopes in accordance with the expectations

