Rare beauty and charm decays

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Introduction

Two ways to search for New Physics.



- More sensitive to specific models
- **BUMP!** \Rightarrow easier to interpret as NP
- Less prone to systematic effects
- Limited by LHC collision energy

- Sensitive to anything that is not SM.
- Rare decays ⇒ more sensitive to NP.
- Use of ratios ⇒ can cancel systematics.
- Less limited by LHC collision energy.

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Outline

- Measurement of $\mathcal{B}(\phi o \mu^+ \mu^-)/\mathcal{B}(\phi o e^+ e^-).$ [LHCb-PAPER-2023-038]
- Search of $B_c \to \pi^+ \mu^+ \mu^-$ and measurement of $\mathcal{B}(B_c \to \psi(2S)\pi^+)/\mathcal{B}(B_c \to J/\psi\pi^+)$. [LHCb-PAPER-2023-037]
- Search for $B^0_{
 m s} o \mu^+ \mu^- \gamma$. [LHCb-PAPER-2023-045] in preparation
 - Amplitude analysis $\Lambda^0_b o p \mathcal{K}^- \gamma$. [LHCb-PAPER-2023-036] in preparation

Measurement of ${\cal B}(\phi o \mu^+ \mu^-)/{\cal B}(\phi o e^+ e^-)$

Decay allows us to understand efficiencies at low $q^2 \equiv m^2(\ell, \ell)$. Data: 5.4fb⁻¹from 2016, 2017 and 2018.

$$R_{\phi\pi}^{(s)} = \beta_{\mu/e} \frac{\mathcal{B}(D_{(s)}^+ \to \pi^+ \phi(\mu^+ \mu^-))}{\mathcal{B}(D_{(s)}^+ \to \pi^+ \phi(e^+ e^-))} \left/ \frac{\mathcal{B}(B^+ \to K^+ J/\psi(\mu^+ \mu^-))}{\mathcal{B}(B^+ \to K^+ J/\psi(e^+ e^-))} \right|_{\theta=0}$$

Where $\beta_{\mu/e}$ is a phase space factor.

- Low q^2 : Tracks with $p_T > 300 \text{MeV/c}$ and p > 2000 MeV/c.
- Triggered by: Signal e, μ , π or object not associated to candidate.
- Electron bremsstrahlung recovery: Find photons by extrapolating electron track.



• **Kinematical constraints:** Unlike R_K or R_K^* , $m(\ell, \ell)$ is constrained also in signal channel \Rightarrow better resolution.

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Measurement of ${\cal B}(\phi o \mu^+ \mu^-)/{\cal B}(\phi o e^+ e^-)$

 $D_s^+
ightarrow \pi^+ \phi (
ightarrow e^+ e^-)$ backgrounds: Misidentified:

- $D^+ \to K^+_{\to e^+} \pi^-_{\to e^-} \pi^+$: Removed by vetoing mass around D^+ .
- $D^+ \rightarrow \pi^+_{\rightarrow e^+} \pi^-_{\rightarrow e^-} \pi^+$: Reduced with PID requirements, dominant

Combinatorial: Warped by constraint on $m(e^+, e^-)$ to be around $m(\phi)$



Validation of combinatorial and mis-ID backgrounds.

 $B^+ \to K^+ J/\psi (\to \ell \ell)$ backgrounds:

- Partially reconstructed: $B^{0,+} \rightarrow K^+ \pi^{-,0} J/\psi (\rightarrow e^+ e^-)$
- Misidentified: $B^+ \to \pi^+ J/\psi (\to \ell \ell)$, small
- Combinatorial: Modelled with exponential.

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Measurement of
$${\cal B}(\phi o \mu^+ \mu^-)/{\cal B}(\phi o e^+ e^-)$$



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Measurement of ${\cal B}(\phi o \mu^+ \mu^-)/{\cal B}(\phi o e^+ e^-)$

Main systematics:

- q^2 resolution: Normalization mode corrections do not port well to low q^2 .
- Event multiplicity: Only partial cancellation with normalization mode.



 $R_{\phi\pi}^{d} = 1.026 \pm 0.020 \text{ (stat)} \pm 0.056 \text{ (syst)},$ $R_{\phi\pi}^{s} = 1.017 \pm 0.013 \text{ (stat)} \pm 0.051 \text{ (syst)}.$

 $6\% \Rightarrow <2\%$

$$\begin{split} \mathcal{B}(\phi \to \mu^+ \mu^-) &= (3.045 \pm 0.049 \, (\text{stat}) \pm 0.148 \, (\text{syst})) \times 10^{-4}, \\ & 7 \, / \, 18 \\ \end{split}$$

$R_{\pi^+\mu^+\mu^-/J/\psi}$ and $R_{\psi(2S)/J/\psi}$

First search of non-resonant $B_c^+ \to \pi^+ \mu^+ \mu^-$, can be used to search for $B_c^+ \to B_{(s)}^{*0} \pi^+$.

- Data: 9fb⁻¹, full LHCb dataset.
- Strategy:
 - Use $B_c^+ \to \pi^+ J/\psi(\to \mu^+ \mu^-)$ as normalization and control channel to measure:

$$R_{\psi(2S)/J/\psi} \equiv \frac{\mathcal{B}(B_c^+ \to \psi(2S)\pi^+)}{\mathcal{B}(B_c^+ \to J\psi\pi^+)} \qquad R_{\pi^+\mu^+\mu^-/J/\psi} \equiv \frac{\mathcal{B}(B_c^+ \to \mu^+\mu^-\pi^+)}{\mathcal{B}(B_c^+ \to J\psi\pi^+)}$$

 Analysis done in bins of q² and constraining m(μ⁺, μ⁻) to charmonium mass for measurement of R_{ψ(2S)/J/ψ}.



 $R_{\pi^+\mu^+\mu^-/J/\psi}$ and $R_{\psi(2S)/J/\psi}$



Fits for $R_{\psi(2S)/J/\psi}$

Mass scales and resolutions:

- Rare mode: Constrained to value from $B_c^+ \rightarrow J/\psi \pi^+$ fits.
- Resonant modes: Floating but shared among components.

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[[]LHCb-PAPER-2023-037]

$R_{\pi^+\mu^+\mu^-/J/\psi}$ and $R_{\psi(2S)/J/\psi}$

No signal observed in non-resonant mode \Rightarrow Set upper limits.



 $\frac{\mathcal{B}(B_c^+ \to \psi(2S)\pi^+)}{\mathcal{B}(B_c^+ \to J/\psi\pi^+)} = 0.254 \pm 0.018 \,(\text{stat}) \pm 0.003 \,(\text{syst}) \pm 0.005 \,(\text{BF})$

Most precise to date

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LHCb-PAPER-2023-037

- Presence of photon lifts chiral suppression and sets its BR at the same order of magnitude as $B_s^0 \rightarrow \mu^+ \mu^-$.
- Upper limit of $\mathcal{B}(B_s^0 \to \mu^+ \mu^- \gamma) < 2 \cdot 10^{-9}$ set @ 95% CL by PhysRevD.105.012010



Sensitive to more operators than $B^0_{
m s}
ightarrow \mu^+ \mu^-$

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LHCb-PAPER-2023-045] in preparatior

Search for the $B_s^0 \rightarrow \mu^+ \mu^- \gamma$ decay

Measurement carried out in 4 bins in q^2 and studying low- q^2 bin with ϕ veto.



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Search for the $B^0_{\rm s} \to \mu^+ \mu^- \gamma$ decay



Normalization: Used to extract $\mathcal{B}(B^0_s \to \mu^+ \mu^- \gamma)$

$$\mathcal{B}(B_s^0 \to \mu^+ \mu^- \gamma) = rac{\mathcal{B}_{
m norm}}{N_{
m norm}} imes f_{
m norm} imes N_{
m sig}$$

Control: Used to calibrate efficiencies.

$$f_{\text{norm}} = \frac{\epsilon_{\text{Acceptance}}^{\text{Acceptance}}}{\epsilon_{\text{sig}}^{\text{Acceptance}}} \times \frac{\epsilon_{\text{norm}}^{\text{Preselection}}}{\epsilon_{\text{sig}}^{\text{PID}}} \times \frac{\epsilon_{\text{norm}}^{\text{PTigger}}}{\epsilon_{\text{sig}}^{\text{PID}}} \times \frac{\epsilon_{\text{norm}}^{\text{Trigger}}}{\epsilon_{\text{sig}}^{\text{Trigger}}} \times \frac{\epsilon_{\text{norm}}^{\text{MLP}}}{\epsilon_{\text{sig}}^{\text{MLP}}} \qquad \qquad f_{\text{norm}}^{\text{norm}} = 0.85 \pm 0.07,$$

$$f_{\text{norm}}^{\text{norm}} = 0.95 \pm 0.08,$$

$$f_{\text{norm}}^{\text{in III}} = 0.95 \pm 0.08,$$

$$f_{\text{norm}}^{\text{in III}} = 2.20 \pm 0.07,$$

$$13 / 18 \qquad \qquad \Delta \text{norm} \in \mathbb{E}$$

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No excess \Rightarrow set upper limits

$$\begin{split} & \mathcal{B}(B^0_s \to \mu^+ \mu^- \gamma)_{\rm I} < 3.6~(4.2) \times 10^{-8}, \\ & \mathcal{B}(B^0_s \to \mu^+ \mu^- \gamma)_{\rm II} < 6.5~(7.7) \times 10^{-8}, \\ & \mathcal{B}(B^0_s \to \mu^+ \mu^- \gamma)_{\rm III} < 3.4~(4.2) \times 10^{-8}, \end{split}$$

Dominated by statistical uncertainty

$$\begin{split} \mathcal{B}(B^0_s &\rightarrow \mu^+ \mu^- \gamma)_{\mathrm{I, \ with \ } \phi \ \mathrm{veto}} < 2.9 \, (3.4) \times 10^{-8}, \\ \mathcal{B}(B^0_s &\rightarrow \mu^+ \mu^- \gamma)_{\mathrm{comb.}} < 2.5 \, (2.8) \times 10^{-8}, \end{split}$$

- **Data:** 9fb⁻¹, entire LHCb dataset.
- Theory predictions only available for decays through $\Lambda(1520)$
- Complementary analysis to $\Lambda^0_b \to p K^- J/\psi$ that can access $p K^-$ masses up to 2.5GeV.



Selection \Rightarrow mass fit \Rightarrow background subtraction \Rightarrow Amplitude analysis

Backgrounds:

- Combinatorial: Reduced with MVA using kinematic quantities and isolation
- Mis-ID: Found to be negligible.
- Partially reconstructed: Modelled.



Model of amplitude taken from JHEP06(2020)116

$$\mathrm{NLL} \equiv -\log(\mathcal{L}) = -\sum_{\mathrm{Run } 1} \log\left(f_1\left(\mathcal{D}\right)\right) w_s - \sum_{\mathrm{Run } 2} \log\left(f_2\left(\mathcal{D}\right)\right) w_s$$

Parameter of Interest: Couplings between Λ_b^0 and daughter Λ resonances.

- *w_s*: sPlot weights used to background subtract.
- \mathcal{D} : 2 coordinates in Dalitz plane.

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Systematics:

- Leading: Lineshapes of Λ resonances (external)
- **Subleading:** Amplitude model, acceptance, sample size, mass fits, etc (internal)

Summary

- Rare *B* meson decays offer an alternative way to search for new physics.
- The first two analyses shown have provided:
 - A measurement of $R_{\phi\pi}^{(d,s)}$ and the most precise measurement of $\mathcal{B}(\phi \to \mu^+ \mu^-)$.
 - The most precise measurement of $R_{\psi(2S)/J/\psi}$ and the first upper limit for the non-resonant mode $B_c^+ \to \pi^+ \mu^+ \mu^-$.
- The other two have confirmed and strengthened upper bounds on B(B⁰_s → μ⁺μ⁻γ) and explored decays of Λ_b not well known.
- LHCb will start collecting data again this year with its software only trigger.
- Many results will be updated and we expect tighter constrains, specially for the statistically limited measurements.

Backup

Measurement of ${\cal B}(\phi o \mu^+ \mu^-)/{\cal B}(\phi o e^+ e^-)$

Both signal and normalization mode use maximum likelihood fits with constraints on the dilepton mass

Channel $ \phi(1020) [\text{MeV}/c^2] J/\psi [\text{MeV}/c^2]$								
Electrons	870-1110	2450-3600						
Muons	990-1050	2946-3176						

Table: Mass cuts for ϕ and J/ψ .

			Decay mode	Yield
Decay mode	$m_{\phi}(\pi^+\ell^+\ell^-)$	$m_{J/\psi}(K^+\ell^+\ell^-)$	$D^+ \to \pi^+ \phi (\to e^+ e^-)$	7460 ± 140
	[MeV/c ²]	[MeV/c ²]	$D^+ \to \pi^+ \phi(\to \mu^+ \mu^-)$ $D^+_s \to \pi^+ \phi(\to e^+ e^-)$	43512 ± 220 16740 ± 210
$\mu^+\mu^-$	$\notin [1810, 2040]$ $\notin [1840, 2000]$	> 5480	$D_s^+ \to \pi^+ \phi(\to \mu^+ \mu^-)$ $B^+ \to K^+ U/(\to a^+ a^-)$	87022 ± 300 638600 ± 900
			$B^+ \to K^+ J/\psi (\to e^+ e^-)$ $B^+ \to K^+ J/\psi (\to \mu^+ \mu^-)$	2187000 ± 1500

Figure: Mass ranges for mass sidebands and fit yields

Measurement of $\mathcal{B}(\phi ightarrow \mu^+ \mu^-)/\mathcal{B}(\phi ightarrow e^+ e^-)$

Data driven corrections are applied to simulation before extracting efficiencies.

- Quark kinematics
- Particle identification
- Trigger efficiencies
- Tracking efficiency
- q² resolution.

Total efficiency is obtained by:

- Adding between trigger categories.
- Performing luminosity weighted average between run periods.

Total yield is sum of yields from each run period fit. They are then put together in:

$$R_{\phi\pi}^{(d,s)} = \frac{N^{(d,s)}(\pi^+\phi(\to\mu^+\mu^-))}{N^{(d,s)}(\pi^+\phi(\to e^+e^-))} \frac{\varepsilon^{(d,s)}(\pi^+\phi(\to e^+e^-))}{\varepsilon^{(d,s)}(\pi^+\phi(\to\mu^+\mu^-))} \Big/ r_{J/\psi}$$

Can also be written as:

$$R_{\phi\pi}^{(s)} = \beta_{\mu/e} \frac{\mathcal{B}(D_{(s)}^+ \to \pi^+ \phi(\mu^+ \mu^-))}{\mathcal{B}(D_{(s)}^+ \to \pi^+ \phi(e^+ e^-))} \bigg/ \frac{\mathcal{B}(B^+ \to K^+ J/\psi(\mu^+ \mu^-))}{\mathcal{B}(B^+ \to K^+ J/\psi(e^+ e^-))}$$

Measurement of $\mathcal{B}(\phi
ightarrow \mu^+ \mu^-)/\mathcal{B}(\phi
ightarrow e^+ e^-)$

To correct mismodelling due to q^2 differences, smearing factors are measured in $B^+ \to K^+ J/\psi(\to e^+ e^-)$ in data.

Signal MC is smeared and shape is used to fit m(e, e) in signal events:



Fit quality validates smearing

Measurement of $\mathcal{B}(\phi \to \mu^+ \mu^-) / \mathcal{B}(\phi \to e^+ e^-)$ No significant trend is seen when $\mathcal{R}^{(0,s)}_{\phi\pi}$ is measured in function of

No significant trend is seen when $R_{\phi\pi}^{(0,s)}$ is measured in function of different variables.



Measurement of
$${\cal B}(\phi o \mu^+ \mu^-)/{\cal B}(\phi o e^+ e^-)$$

Source	$R^d_{\phi\pi}$ [%]	$R^s_{\phi\pi}$ [%]
Resolution on q^2	4.0	3.9
Event multiplicity	2.7	2.7
Simulation reweighting	1.5	1.2
Combinatorial background shape parametrisation	1.5	1.0
PID	0.8	0.8
Finite size of control samples	0.8	0.6
Trigger	0.3	0.3
Tracking	0.1	0.1
Background from doubly misidentified electrons	1.1	0.1
Total	5.5	5.1

 $R_{\pi^+\mu^+\mu^-/J/\psi}$ and $R_{\psi(2S)/J/\psi}$

Track multiplicity.

Component	$\pi^+\mu^+\mu^-$ WP	$\psi(2S)\pi^+$ WP	Component	Yield
$B_c^+ \rightarrow J/\psi \pi^+$	3508 ± 82	6887 ± 93	$B_c^+ \rightarrow \psi(2S)\pi^+$	256 ± 18
$B_c^+ \rightarrow J/\psi K^+$	-81 ± 58	90 ± 43	$B_c^+ \to \psi(2S)K$	$^{+}$ 13 ± 10
$B_c^+ \rightarrow J/\psi \rho^+$	41 ± 11	56 ± 22	$B_c^+ \to \psi(2S)\rho^+$	-4 ± 5
Comb. bkg.	101 ± 25	1254 ± 60	Comb. bkg.	197 ± 19

(a) J/ψ yields

(b) $\psi(2S)$ yields

Simulation corrected for:	q^2 interval	$N_{\pi^+\mu^+\mu^-}$	$N_{\rm comb}$
 Particle identification 	$0.1 < q^2 < 1.1 \text{GeV}^2$	0 ± 2	25^{+6}_{-5}
 Track reconstruction efficiency. 	$1.1 < q^2 < 8.0 { m GeV}^2$ $11.0 < q^2 < 12.5 { m GeV}^2$	1^{+4}_{-3} -18^{+7}_{-10}	$39 \pm 7 \\ 30 {}^{+13}_{-9}$
 Trigger efficiency. B⁺ lifetime kinematics 	$15.0 < q^2 < 35.0 \mathrm{GeV}^2$ All	$0^{+80}_{-77} \\ -2^{+90}_{-8}$	232 ± 17 311^{+20}_{-19}
\bullet D_c method, kinematics.			

(a) Rare mode yields

 $R_{\pi^+\mu^+\mu^-/J/\psi}$ and $R_{\psi(2S)/J/\psi}$

Mass scales are shared between



$R_{\pi^+\mu^+\mu^-/J/\psi}$ and $R_{\psi(2S)/J/\psi}$

Backgrounds:

- Partially reco: $B_c^+ \to \rho \mu^+ \mu^-$, $B_c^+ \to J/\psi \rho^+$ and $B_c^+ \to \psi(2S)\rho^+$ with $\rho \to \pi^+ \pi^0$. Included only for resonant fits .
- Single Mis-ID: Decays with Kaons reconstructed as pions in final state are Cabibbo suppresed and further suppressed by particle ID requirements .
- Double Mis-ID: E.g. $B_c^+ \to \pi^+\pi^-\pi^+$ or $B_c^+ \to c\bar{c}(\to \mu_{\to\pi^+}^+, \mu^-)\pi_{\to\mu^+}^+$ are suppressed by particle ID .

Selection uses BDT

- Signal: Simulated $B_c^+ \to \pi^+ \mu^+ \mu^-$, $B_c^+ \to \pi^+ J/\psi(\to \mu^+ \mu^-)$, $B_c^+ \to \pi^+ B^{*0}(\to \mu^+ \mu^-)$ and $B_c^+ \to \pi^+ B_s^{*0}(\to \mu^+ \mu^-)$
- Background: Data sidebands in $m(\pi^+\mu^+\mu^-)$, excluding charmonium from $m(\mu^+\mu^-)$ distribution.

MVA optimization FOM is different for each measurement

- $R_{\pi^+\mu^+\mu^-/J/\psi} \Rightarrow \varepsilon/(5/2 + \sqrt{N_B})$
- $R_{\psi(2S)/J/\psi} \Rightarrow N_S/\sqrt{N_S + N_B}$

Photons:

- *p*_T > 1000 MeV
- MVA based photon identification.
- For $p_T>2000$ MeV MVA to separate them from merged photons in $\pi^0\to\gamma\gamma$

Muons:

- *p*_T > 250 MeV
- Good quality and particle identification requirements

Bs

- *p*_T > 500 MeV
- Good vertex quality

Differences with respect to $B_s^0
ightarrow \mu^+ \mu^-
ightarrow$ PhysRevD.105.012010

 $B^0_s \to \mu^+ \mu^- \gamma$

- This reconstructs the photon.
- Mesures $B_s^0 \rightarrow \mu^+ \mu^- \gamma$ as signal
- Thanks to the photon can explore also lower regions in q²

Both have set upper limits.

 $B_s^0 \to \mu^+ \mu^-$

- Reconstructs only the muons
- Measures $B_s^0 \to \mu^+ \mu^- \gamma$ as part of the partially reconstructed background
- Can only have access to high q² regions > 4.9GeV²



Preselection:

- Λ_b^0 : Good vertex quality, momentum pointing to PV
- p, K^- : $IP > 0.1 mm, p_T > 1 \text{GeV}, p > 5 \text{GeV}.$
- γ : $E_T > 3 \text{GeV}$

MVA:

- Uses kinematic variables and isolation
- Background: Upper sideband in data $m(pK\gamma) > m(\Lambda_b^0) + 300$ MeV
- FOM: $S/\sqrt{S+B}$

$$I_{p_{\mathrm{T}}} = \frac{p_{\mathrm{T}}(\Lambda_b^0) - \sum p_{\mathrm{T}}}{p_{\mathrm{T}}(\Lambda_b^0) + \sum p_{\mathrm{T}}}$$

Mis-ID backgrounds:

• $B_s^0 \to \phi(\to KK)\gamma$: Veto $m(p_{\to K}, K)$ mass around m_{ϕ} .

• $B^0_s o KK\gamma$, $B_d o K\pi\gamma$: Less than 0.5%.

- $\Lambda_b^0 \to p K \eta$, $\Lambda_b^0 \to p K \pi^0$: Less than 1-2%, limited by staying below 2.5GeVin m(p, K).
- $\Xi_b^0 \rightarrow p K \gamma$: Negligible

Mis-ID and Combinatorial:

D⁰ → KK and D⁰ → Kπ combined with random γ: Veto distorts signal acceptance ⇒ included in fit.

Partially reconstructed:

•
$$\Lambda_b^0 \to \rho K^{*-} (\to K^- \pi 0) \gamma$$
 Included in fit.

Maximum likelihood fit uses:

- Reduced model: Well-established resonances and interferences.
- Non resonant: Seen to improve fit quality



Projections of 2D fit on $m_{\Lambda_b}(pK^-)$

Mass fits:

- Combinatorial: Exponential
- Signal: Double sided Crystall Ball, tails from simulation
- Partially reconstructed: From Kernel density estimation on simulated Λ⁰_b → pK^{*−}(→ K[−]π0)γ.

Resonance	J^P	m_0	Γ_0	Δm_0	$\Delta\Gamma_0$	σ_{m_0}	σ_{Γ_0}	l	L
$\Lambda(1405)$	$1/2^{-}$	1405	50.5	±1.3	± 2	1.3	2	0	0, 1
$\Lambda(1520)$	$3/2^{-}$	1519	16	1518 - 1520	15 - 17	1	1	2	0, 1, 2
$\Lambda(1600)$	$1/2^{+}$	1600	200	1570 - 1630	150 - 250	30	50	1	0, 1
A(1670)	$1/2^{-}$	1674	30	1670 - 1678	25 - 35	4	5	0	0, 1
$\Lambda(1690)$	$3/2^{-}$	1690	70	1685 - 1695	50 - 70	5	10	2	0, 1, 2
$\Lambda(1800)$	$1/2^{-}$	1800	200	1750 - 1850	150 - 250	50	50	0	0, 1
$\Lambda(1810)$	$1/2^{+}$	1790	110	1740 - 1840	50 - 170	50	60	1	0, 1
$\Lambda(1820)$	$5/2^{+}$	1820	80	1815 - 1825	70 - 90	5	10	3	1, 2, 3
A(1830)	$5/2^{-}$	1825	90	1820 - 1830	60 - 120	5	- 30	2	1, 2, 3
$\Lambda(1890)$	$3/2^{+}$	1890	120	1870 - 1910	80 - 160	20	40	1	0, 1, 2
$\Lambda(2100)$	7/2-	2100	200	2090 - 2110	100 - 250	10	100	4	2, 3, 4
$\Lambda(2110)$	$5/2^{+}$	2090	250	2050 - 2130	200 - 300	40	50	3	1, 2, 3
A(2350)	$^{9/2^{+}}$	2350	150	2340 - 2370	100 - 250	20	100	5	3, 4, 5

Amplitude fit contains many parameters \Rightarrow unstable.

• Local minima:

- Fit ten times with different starting points.
- Pick fit with lowest NLL.
- **Parameter variations:** Couplings vary between minima, but same values for
 - Fit fractions
 - Interference amplitudes

 \Rightarrow treat couplings as nuisance parameters and fit fractions and interference amplitudes as parameters of interest.

Resonance	J^P	m_0	Γ_0	Δm_0	$\Delta\Gamma_0$	σ_{m_0}	σ_{Γ_0}	l	L
$\Lambda(1405)$	$1/2^{-}$	1405	50.5	±1.3	± 2	1.3	2	0	0, 1
A(1520)	$3/2^{-}$	1519	16	1518 - 1520	15 - 17	1	1	2	0, 1, 2
$\Lambda(1600)$	$1/2^{+}$	1600	200	1570 - 1630	150 - 250	30	50	1	0, 1
$\Lambda(1670)$	$1/2^{-}$	1674	30	1670 - 1678	25 - 35	4	5	0	0, 1
$\Lambda(1690)$	$3/2^{-}$	1690	70	1685 - 1695	50 - 70	5	10	2	0, 1, 2
$\Lambda(1800)$	$1/2^{-}$	1800	200	1750 - 1850	150 - 250	50	50	0	0, 1
$\Lambda(1810)$	$1/2^{+}$	1790	110	1740 - 1840	50 - 170	50	60	1	0, 1
$\Lambda(1820)$	$5/2^{+}$	1820	80	1815 - 1825	70 - 90	5	10	3	1, 2, 3
$\Lambda(1830)$	$5/2^{-}$	1825	90	1820 - 1830	60 - 120	5	30	2	1, 2, 3
$\Lambda(1890)$	$3/2^+$	1890	120	1870 - 1910	80 - 160	20	40	1	0, 1, 2
$\Lambda(2100)$	7/2-	2100	200	2090 - 2110	100 - 250	10	100	4	2, 3, 4
$\Lambda(2110)$	$5/2^{+}$	2090	250	2050 - 2130	200 - 300	40	50	3	1, 2, 3
$\Lambda(2350)$	$^{9/2^{+}}$	2350	150	2340 - 2370	100 - 250	20	100	5	3, 4, 5

Resonances used in reduced model

Reduced model (only resonances)



Reduced model plus non-resonant components



Reduced model (resonances and interferences) fit plus non-resonant (constant) components



Reduced model (resonances and interferences) fit plus non-resonant (constant) components



Amplitude analysis of the $\Lambda_b^0 \rightarrow p K^- \gamma$ decay Systematics on fit fractions.

	A	Amplitud	le mode	d	Acceptance model		Mass fit model			
Observable	$\sigma^A_{\rm BW}$	$\sigma^A_{\rm radius}$	$\sigma_{\rm amp.}$	$\sigma_{\rm res.}$	$\sigma_{\rm finite}$	$\sigma_{\rm acc.}$	$\sigma_{\rm kin.}$	σ_{pK}	$\sigma_{p\gamma}$	$\sigma_{\rm comb.}$
A(1405)	$^{+1.2}_{-0.7}$	$^{+0.0}_{-0.0}$	$^{+0.9}_{+0.2}$	$^{+0.0}_{-0.4}$	$^{+0.2}_{-0.2}$	$^{+0.2}_{-0.2}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.1}$	$^{+0.1}_{-0.0}$	$^{+0.0}_{-0.0}$
A(1520)	$^{+1.0}_{-1.3}$	$^{+1.1}_{-1.1}$	$^{+0.3}_{+0.0}$	$^{+0.0}_{-0.1}$	$^{+0.2}_{-0.2}$	$^{+0.2}_{-0.2}$	$^{+0.1}_{-0.1}$	$^{+0.3}_{-0.0}$	$^{+0.1}_{-0.0}$	$^{+0.0}_{-0.1}$
A(1600)	$^{+3.6}_{-4.5}$	$^{+1.8}_{-1.8}$	$^{+0.5}_{+0.0}$	$^{+0.3}_{-0.2}$	$^{+0.3}_{-0.3}$	$^{+0.2}_{-0.2}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.1}$	$^{+0.1}_{-0.0}$	$^{+0.0}_{-0.0}$
A(1670)	$^{+1.1}_{-0.3}$	$^{+0.2}_{-0.2}$	$^{+0.2}_{-0.2}$	$^{+0.2}_{-0.2}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$
A(1690)	$^{+4.1}_{-0.3}$	$^{+2.0}_{-2.0}$	$^{+1.5}_{+0.2}$	$^{+0.6}_{-0.5}$	$^{+0.2}_{-0.2}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.1}_{-0.0}$	$^{+0.0}_{-0.1}$	$^{+0.0}_{-0.0}$
A(1800)	$^{+3.0}_{-5.9}$	$^{+1.1}_{-1.1}$	$^{+0.1}_{-0.8}$	$^{+0.8}_{-1.5}$	$^{+0.3}_{-0.3}$	+0.1 -0.1	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.6}_{-0.0}$	$^{+0.4}_{-0.0}$
A(1810)	$^{+3.7}_{-0.7}$	$^{+1.1}_{-1.1}$	$^{+1.5}_{+0.1}$	$^{+0.5}_{-1.4}$	$^{+0.2}_{-0.2}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.1}_{-0.0}$	$^{+0.2}_{-0.0}$	$^{+0.0}_{-0.0}$
A(1820)	$^{+1.8}_{-4.9}$	$^{+0.2}_{-0.2}$	-0.0 -0.9	$^{+0.3}_{-0.4}$	$^{+0.3}_{-0.3}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.3}$	$^{+0.1}_{-0.0}$	$^{+0.0}_{-0.1}$
A(1830)	$^{+1.3}_{-0.9}$	$^{+0.6}_{-0.6}$	$^{+0.3}_{-0.4}$	$^{+0.3}_{-0.5}$	$^{+0.1}_{-0.1}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.2}_{-0.0}$	$^{+0.1}_{-0.0}$	$^{+0.0}_{-0.0}$
A(1890)	$^{+4.2}_{-5.1}$	$^{+0.8}_{-0.8}$	$^{+0.4}_{-0.4}$	$^{+0.1}_{-0.4}$	$^{+0.2}_{-0.2}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.1}_{-0.0}$	$^{+0.1}_{-0.0}$	$^{+0.0}_{-0.0}$
A(2100)	$^{+1.0}_{-2.6}$	$^{+0.8}_{-0.8}$	$^{+0.9}_{-0.7}$	$^{+0.2}_{-0.2}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.1}_{-0.0}$	$^{+0.1}_{-0.0}$
A(2110)	$^{+5.0}_{-0.6}$	$^{+1.5}_{-1.5}$	$^{+1.5}_{-0.1}$	$^{+0.3}_{-0.2}$	$^{+0.1}_{-0.1}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.2}$	$^{+0.0}_{-0.0}$	$^{+0.2}_{-0.0}$
A(2350)	$^{+0.0}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.6}_{-0.2}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.1}_{-0.0}$	$^{+0.1}_{-0.0}$	$^{+0.1}_{-0.0}$
$NR(\frac{3}{2})$	$^{+2.9}_{+0.3}$	$^{+0.4}_{-0.4}$	$^{+1.0}_{-2.4}$	$^{+0.0}_{-0.6}$	$^{+0.1}_{-0.1}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.1}$	$^{+0.0}_{-0.3}$	$^{+0.0}_{-0.0}$
A(1405), A(1670)	$^{+0.4}_{-0.7}$	$^{+0.3}_{-0.3}$	$^{+0.2}_{-0.0}$	$^{+0.1}_{-0.1}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.1}$
A(1405), A(1800)	$^{+0.5}_{-3.6}$	$^{+0.3}_{-0.3}$	$^{+0.1}_{-1.9}$	$^{+1.7}_{-0.4}$	$^{+0.2}_{-0.2}$	$^{+0.2}_{-0.2}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.3}$	$^{+0.1}_{-0.0}$
A(1520), A(1690)	$^{+0.3}_{-2.3}$	$^{+0.9}_{-0.9}$	-0.1 -0.7	$^{+0.5}_{-0.4}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$
$A(1520), NR(\frac{3}{2})$	$^{+1.2}_{-2.4}$	$^{+1.5}_{-1.5}$	$^{+0.5}_{-0.5}$	$^{+0.8}_{-0.4}$	$^{+0.1}_{-0.1}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.1}$	$^{+0.0}_{-0.0}$
A(1600), A(1810)	$^{+4.1}_{-2.8}$	$^{+0.6}_{-0.6}$	$^{+1.5}_{-0.7}$	$^{+0.9}_{-0.4}$	$^{+0.3}_{-0.3}$	$^{+0.2}_{-0.2}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.4}$	$^{+0.0}_{-0.4}$
A(1670), A(1800)	$^{+1.5}_{-1.9}$	$^{+0.4}_{-0.4}$	$^{+0.3}_{-0.2}$	$^{+0.4}_{-0.4}$	$^{+0.1}_{-0.1}$	+0.1 -0.1	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.1}$
$\Lambda(1690), NR(\frac{3}{2}^{-})$	$^{+0.9}_{-2.2}$	$^{+1.1}_{-1.1}$	$^{+0.2}_{-2.7}$	$^{+0.2}_{-0.5}$	$^{+0.1}_{-0.1}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.0}$	$^{+0.0}_{-0.1}$	$^{+0.0}_{-0.0}$
A(1820), A(2110)	$^{+2.4}_{-3.1}$	$^{+1.6}_{-1.6}$	$^{+0.5}_{-1.6}$	$^{+0.3}_{-0.5}$	$^{+0.2}_{-0.2}$	$^{+0.1}_{-0.1}$	$^{+0.0}_{-0.0}$	$^{+0.2}_{-0.0}$	$^{+0.0}_{-0.3}$	$^{+0.0}_{-0.2}$