

## Introduction

Two ways to search for New Physics.


VBF

- More sensitive to specific models
- BUMP! $\Rightarrow$ easier to interpret as NP
- Less prone to systematic effects
- Limited by LHC collision energy

- Sensitive to anything that is not SM.
- Rare decays $\Rightarrow$ more sensitive to NP.
- Use of ratios $\Rightarrow$ can cancel systematics.
- Less limited by LHC collision energy.


## Outline

- Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$.
[LHCb-PAPER-2023-038]
- Search of $B_{c} \rightarrow \pi^{+} \mu^{+} \mu^{-}$and measurement of $\mathcal{B}\left(B_{c} \rightarrow \psi(2 S) \pi^{+}\right) / \mathcal{B}\left(B_{c} \rightarrow J / \psi \pi^{+}\right)$.
[LHCb-PAPER-2023-037]
- Search for $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$. [LHCb-PAPER-2023-045] in preparation
- Amplitude analysis $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$. [LHCb-PAPER-2023-036] in preparation


## Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$

Decay allows us to understand efficiencies at low $q^{2} \equiv m^{2}(\ell, \ell)$.
Data: $5.4 \mathrm{fb}^{-1}$ from 2016, 2017 and 2018.

$$
R_{\phi \pi}^{(s)}=\beta_{\mu / e} \frac{\mathcal{B}\left(D_{(s)}^{+} \rightarrow \pi^{+} \phi\left(\mu^{+} \mu^{-}\right)\right)}{\mathcal{B}\left(D_{(s)}^{+} \rightarrow \pi^{+} \phi\left(e^{+} e^{-}\right)\right)} / \frac{\mathcal{B}\left(B^{+} \rightarrow K^{+} J / \psi\left(\mu^{+} \mu^{-}\right)\right)}{\mathcal{B}\left(B^{+} \rightarrow K^{+} J / \psi\left(e^{+} e^{-}\right)\right)}
$$

Where $\beta_{\mu / e}$ is a phase space factor.

- Low $q^{2}$ : Tracks with $p_{T}>300 \mathrm{MeV} / \mathrm{c}$ and $p>2000 \mathrm{MeV} / \mathrm{c}$.
- Triggered by: Signal e, $\mu, \pi$ or object not associated to candidate.
- Electron bremsstrahlung recovery: Find photons by extrapolating electron track.

- Kinematical constraints: Unlike $R_{K}$ or $R_{K}^{*}, m(\ell, \ell)$ is constrained also in signal channel $\Rightarrow$ better resolution.


## Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$

$D_{s}^{+} \rightarrow \pi^{+} \phi\left(\rightarrow e^{+} e^{-}\right)$backgrounds:
Misidentified:

- $D^{+} \rightarrow K_{\rightarrow e^{+}}^{+} \pi_{\rightarrow e^{-}}^{-} \pi^{+}$: Removed by vetoing mass around $D^{+}$.
- $D^{+} \rightarrow \pi_{\rightarrow e^{+}}^{+} \pi_{\rightarrow e^{-}}^{-} \pi^{+}$: Reduced with PID requirements, dominant

Combinatorial: Warped by constraint on $m\left(e^{+}, e^{-}\right)$to be around $m(\phi)$



Validation of combinatorial and mis-ID backgrounds.
$B^{+} \rightarrow K^{+} J / \psi(\rightarrow \ell \ell)$ backgrounds:

- Partially reconstructed: $B^{0,+} \rightarrow K^{+} \pi^{-, 0} J / \psi\left(\rightarrow e^{+} e^{-}\right)$
- Misidentified: $B^{+} \rightarrow \pi^{+} J / \psi(\rightarrow \ell \ell)$, small
- Combinatorial: Modelled with exponential.


## Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$

Muon

Signal





## Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$

Main systematics:

- $q^{2}$ resolution: Normalization mode corrections do not port well to low $q^{2}$.
- Event multiplicity: Only partial cancellation with normalization mode.


Consistent between channels


Driven by systematics
$\begin{aligned} & R_{\phi \pi}^{d}=1.026 \pm 0.020 \text { (stat) } \pm 0.056 \text { (syst), } \\ & R_{\phi \pi}^{s}=1.017 \pm 0.013 \text { (stat) } \pm 0.051 \text { (syst). }\end{aligned} \quad R_{\phi \pi}=1.022 \pm 0.012$ (stat) $\pm 0.048$ (syst).

$$
6 \% \Rightarrow<2 \%
$$

$$
\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right)=(3.045 \pm 0.049 \text { (stat) } \pm 0.148 \text { (syst) }) \times 10^{-4},
$$

$$
7 \text { / } 18
$$

## $R_{\pi^{+} \mu^{+} \mu^{-} / J / \psi}$ and $R_{\psi(2 S) / J / \psi}$

First search of non-resonant $B_{c}^{+} \rightarrow \pi^{+} \mu^{+} \mu^{-}$, can be used to search for $B_{c}^{+} \rightarrow B_{(s)}^{* 0} \pi^{+}$.

- Data: $9 \mathrm{fb}^{-1}$, full LHCb dataset.
- Strategy:
- Use $B_{c}^{+} \rightarrow \pi^{+} J / \psi\left(\rightarrow \mu^{+} \mu^{-}\right)$as normalization and control channel to measure:

$$
R_{\psi(2 S) / J / \psi} \equiv \frac{\mathcal{B}\left(B_{c}^{+} \rightarrow \psi(2 S) \pi^{+}\right)}{\mathcal{B}\left(B_{c}^{+} \rightarrow J \psi \pi^{+}\right)} \quad R_{\pi^{+} \mu^{+} \mu^{-} / J / \psi} \equiv \frac{\mathcal{B}\left(B_{c}^{+} \rightarrow \mu^{+} \mu^{-} \pi^{+}\right)}{\mathcal{B}\left(B_{c}^{+} \rightarrow J \psi \pi^{+}\right)}
$$

- Analysis done in bins of $q^{2}$ and constraining $m\left(\mu^{+}, \mu^{-}\right)$to charmonium mass for measurement of $R_{\psi(2 S) / \mathrm{J} / \psi}$.

$$
\begin{aligned}
& B_{c}^{+} \rightarrow J / \psi \pi^{+} \\
& \left|m\left(\mu^{+}, \mu^{-}\right)-m_{J / \psi}\right|<50 \mathrm{MeV} \\
& \\
& B_{c}^{+} \rightarrow \psi(2 S) \pi^{+} \\
& \left|m\left(\mu^{+}, \mu^{-}\right)-m_{\psi(2 S)}\right|<50 \mathrm{MeV}
\end{aligned}
$$

- Trigger on muons.



## $R_{\pi^{+} \mu^{+} \mu^{-} / J / \psi}$ and $R_{\psi(2 S) / J / \psi}$

Unconstrained



## Non-resonant

Fits for $R_{\pi^{+} \mu^{+} \mu^{-} / J / \psi}$
Different MVA cuts


Constrained


Fits for $R_{\psi(2 S) / J / \psi}$
Mass scales and resolutions:

- Rare mode: Constrained to value from $B_{c}^{+} \rightarrow J / \psi \pi^{+}$fits.
- Resonant modes: Floating but shared among components.


## $R_{\pi^{+} \mu^{+} \mu^{-} / J / \psi}$ and $R_{\psi(2 S) / J / \psi}$

No signal observed in non-resonant mode $\Rightarrow$ Set upper limits.



First upper limit

$$
\frac{\mathcal{B}\left(B_{c}^{+} \rightarrow \pi^{+} \mu^{+} \mu^{-}\right)}{\mathcal{B}\left(B_{c}^{+} \rightarrow J / \psi \pi^{+}\right)}<2.1 \times 10^{-4} .
$$

$$
\frac{\mathcal{B}\left(B_{c}^{+} \rightarrow \psi(2 S) \pi^{+}\right)}{\mathcal{B}\left(B_{c}^{+} \rightarrow J / \psi \pi^{+}\right)}=0.254 \pm 0.018(\text { stat }) \pm 0.003(\text { syst }) \pm 0.005(\mathrm{BF}) .
$$

Most precise to date

## Search for the $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$ decay

- Presence of photon lifts chiral suppression and sets its BR at the same order of magnitude as $B_{s}^{0} \rightarrow \mu^{+} \mu^{-}$.
- Upper limit of $\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma\right)<2 \cdot 10^{-9}$ set @ $95 \% \mathrm{CL}$ by PhysRevD.105.012010
$\mathcal{O}_{7}^{\left({ }^{\prime}\right)}{ }^{(a)}$

$\mathcal{O}_{9,10}^{\left({ }^{\prime}\right)}{ }^{(\mathrm{c})}$

$\mathcal{O}_{1,2}$

$\mathcal{O}_{9,10}^{(')}$
(d)


Sensitive to more operators than $B_{s}^{0} \rightarrow \mu^{+} \mu^{-}$

## Search for the $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$ decay

Measurement carried out in 4 bins in $q^{2}$ and studying low- $q^{2}$ bin with $\phi$ veto.

Control channel
$B_{s} \rightarrow \phi\left(\rightarrow K^{+} K^{-}\right) \gamma$ Large statistics

Normalization channel
$B_{s} \rightarrow J / \psi(\rightarrow \mu \mu) \eta$ $\eta \rightarrow \gamma \gamma$
Well known $\mathcal{B R}$

Trigger on:
Muons and photon


## Search for the $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$ decay



Normalization


Control

Normalization: Used to extract $\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma\right)$

$$
\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma\right)=\frac{\mathcal{B}_{\text {norm }}}{N_{\text {norm }}} \times f_{\text {norm }} \times N_{\text {sig }}
$$

Control: Used to calibrate efficiencies.

$$
f_{\mathrm{norm}}=\frac{\epsilon_{\mathrm{norm}}^{\text {Acceptance }}}{\epsilon_{\mathrm{sig}}^{\mathrm{Acceptance}}} \times \frac{\epsilon_{\mathrm{norm}}^{\text {Preselection }}}{\epsilon_{\mathrm{sig}}^{\mathrm{Preselection}}} \times \frac{\epsilon_{\mathrm{norm}}^{\mathrm{PID}}}{\epsilon_{\mathrm{sig}}^{\mathrm{PID}}} \times \frac{\epsilon_{\mathrm{norm}}^{\text {Trigger }}}{\epsilon_{\mathrm{sig}}^{\text {Trigger }}} \times \frac{\epsilon_{\mathrm{norm}}^{\mathrm{MLP}}}{\epsilon_{\mathrm{sig}}^{\mathrm{MLP}}}
$$

$$
\begin{aligned}
f_{\text {norm }}^{\text {bin }} & =0.85 \pm 0.07 \\
f_{\text {norm }}^{\text {bin }} & =0.95 \pm 0.08 \\
f_{\text {norm }}^{\text {bin III }} & =2.20 \pm 0.07
\end{aligned}
$$

## Search for the $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$ decay

No excess $\Rightarrow$ set upper limits


## [LHCb-PAPER-2023-045] in preparation

## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

- Data: $9 \mathrm{fb}^{-1}$, entire LHCb dataset.
- Theory predictions only available for decays through $\Lambda(1520)$
- Complementary analysis to $\Lambda_{b}^{0} \rightarrow p K^{-} J / \psi$ that can access $p K^{-}$masses up to 2.5 GeV .



Selection $\Rightarrow$ mass fit $\Rightarrow$ background subtraction $\Rightarrow$ Amplitude analysis

## Backgrounds:

- Combinatorial: Reduced with MVA using kinematic quantities and isolation
- Mis-ID: Found to be negligible.
- Partially reconstructed: Modelled.


## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

Photon resolution worsens Dalitz plane resolution $\Rightarrow$ Apply mass constraint on $\Lambda_{b}^{0}$ fit to get $m_{\Lambda_{b}^{0}}(p \gamma)$ and $m_{\Lambda_{b}^{0}}(p K)$


Model of amplitude taken from JHEP06(2020)116

$$
\mathrm{NLL} \equiv-\log (\mathcal{L})=-\sum_{\text {Run } 1} \log \left(f_{1}(\mathcal{D})\right) w_{s}-\sum_{\text {Run } 2} \log \left(f_{2}(\mathcal{D})\right) w_{s}
$$

Parameter of Interest: Couplings between $\Lambda_{b}^{0}$ and daughter $\Lambda$ resonances.

- $w_{s}$ : sPlot weights used to background subtract.
- D: 2 coordinates in Dalitz plane.


## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay



Systematics:

- Leading: Lineshapes of $\Lambda$ resonances (external)


## [LHCb-PAPER-2023-036] in preparation

- Subleading: Amplitude model, acceptance, sample size, mass fits, etc (internal)


## Summary

- Rare $B$ meson decays offer an alternative way to search for new physics.
- The first two analyses shown have provided:
- A measurement of $R_{\phi \pi}^{(d, s)}$ and the most precise measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right)$.
- The most precise measurement of $R_{\psi(2 S) / J / \psi}$ and the first upper limit for the non-resonant mode $B_{c}^{+} \rightarrow \pi^{+} \mu^{+} \mu^{-}$.
- The other two have confirmed and strengthened upper bounds on $\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma\right)$ and explored decays of $\Lambda_{b}$ not well known.
- LHCb will start collecting data again this year with its software only trigger.
- Many results will be updated and we expect tighter constrains, specially for the statistically limited measurements.


## Backup

## Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$

Both signal and normalization mode use maximum likelihood fits with constraints on the dilepton mass

| Channel | $\phi(1020)\left[\mathrm{MeV} / \mathrm{c}^{2}\right]$ | $J / \psi\left[\mathrm{MeV} / \mathrm{c}^{2}\right]$ |
| :--- | :---: | :---: |
| Electrons | $870-1110$ | $2450-3600$ |
| Muons | $990-1050$ | $2946-3176$ |

Table: Mass cuts for $\phi$ and $J / \psi$.

| Decay mode | $m_{\phi}\left(\pi^{+} \ell^{+} \ell^{-}\right)$ <br> $\left[\mathrm{MeV} / c^{2}\right]$ | $m_{J / \psi}\left(K^{+} \ell^{+} \ell^{-}\right)$ <br> $\left[\mathrm{MeV} / c^{2}\right]$ |
| :---: | :---: | :---: |
| $e^{+} e^{-}$ | $\notin[1810,2040]$ | $>5580$ |
| $\mu^{+} \mu^{-}$ | $\notin[1840,2000]$ | $>5480$ |


| Decay mode | Yield |  |
| :--- | ---: | ---: |
| $D^{+} \rightarrow \pi^{+} \phi\left(\rightarrow e^{+} e^{-}\right)$ | $7460 \pm$ | 140 |
| $D^{+} \rightarrow \pi^{+} \phi\left(\rightarrow \mu^{+} \mu^{-}\right)$ | $43512 \pm$ | 220 |
| $D_{s}^{+} \rightarrow \pi^{+} \phi\left(\rightarrow e^{+} e^{-}\right)$ | $16740 \pm$ | 210 |
| $D_{s}^{+} \rightarrow \pi^{+} \phi\left(\rightarrow \mu^{+} \mu^{-}\right)$ | $87022 \pm$ | 300 |
| $B^{+} \rightarrow K^{+} J / \psi\left(\rightarrow e^{+} e^{-}\right)$ | $638600 \pm 900$ |  |
| $B^{+} \rightarrow K^{+} J / \psi\left(\rightarrow \mu^{+} \mu^{-}\right)$ | $2187000 \pm$ | 1500 |

Figure: Mass ranges for mass sidebands and fit yields

## Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$

Data driven corrections are applied to simulation before extracting efficiencies.

- Quark kinematics
- Particle identification
- Trigger efficiencies
- Tracking efficiency
- $q^{2}$ resolution.

Total efficiency is obtained by:

- Adding between trigger categories.
- Performing luminosity weighted average between run periods.

Total yield is sum of yields from each run period fit. They are then put together in:

$$
R_{\phi \pi}^{(d, s)}=\frac{N^{(d, s)}\left(\pi^{+} \phi\left(\rightarrow \mu^{+} \mu^{-}\right)\right)}{N^{(d, s)}\left(\pi^{+} \phi\left(\rightarrow e^{+} e^{-}\right)\right)} \frac{\varepsilon^{(d, s)}\left(\pi^{+} \phi\left(\rightarrow e^{+} e^{-}\right)\right)}{\varepsilon^{(d, s)}\left(\pi^{+} \phi\left(\rightarrow \mu^{+} \mu^{-}\right)\right)} / r_{J / \psi}
$$

Can also be written as:

$$
R_{\phi \pi}^{(s)}=\beta_{\mu / e} \frac{\mathcal{B}\left(D_{(s)}^{+} \rightarrow \pi^{+} \phi\left(\mu^{+} \mu^{-}\right)\right)}{\mathcal{B}\left(D_{(s)}^{+} \rightarrow \pi^{+} \phi\left(e^{+} e^{-}\right)\right)} / \frac{\mathcal{B}\left(B^{+} \rightarrow K^{+} J / \psi\left(\mu^{+} \mu^{-}\right)\right)}{\mathcal{B}\left(B^{+} \rightarrow K^{+} J / \psi\left(e^{+} e^{-}\right)\right)}
$$

## Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$

To correct mismodelling due to $q^{2}$ differences, smearing factors are measured in $B^{+} \rightarrow K^{+} J / \psi\left(\rightarrow e^{+} e^{-}\right)$in data.

Signal MC is smeared and shape is used to fit $m(e, e)$ in signal events:



Fit quality validates smearing

Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$
No significant trend is seen when $R_{\phi \pi}^{(0, s)}$ is measured in function of different variables.


## Measurement of $\mathcal{B}\left(\phi \rightarrow \mu^{+} \mu^{-}\right) / \mathcal{B}\left(\phi \rightarrow e^{+} e^{-}\right)$

| Source | $R_{\phi \pi}^{d}[\%]$ | $R_{\phi \pi}^{s} \quad[\%]$ |
| :--- | :---: | :---: |
| Resolution on $q^{2}$ | 4.0 | 3.9 |
| Event multiplicity | 2.7 | 2.7 |
| Simulation reweighting | 1.5 | 1.2 |
| Combinatorial background shape parametrisation | 1.5 | 1.0 |
| PID | 0.8 | 0.8 |
| Finite size of control samples | 0.8 | 0.6 |
| Trigger | 0.3 | 0.3 |
| Tracking | 0.1 | 0.1 |
| Background from doubly misidentified electrons | 1.1 | 0.1 |
| Total | 5.5 | 5.1 |

## $R_{\pi^{+} \mu^{+} \mu^{-} / J / \psi}$ and $R_{\psi(2 S) / J / \psi}$

| Component | $\pi^{+} \mu^{+} \mu^{-}$WP | $\psi(2 S) \pi^{+}$WP |
| :--- | :---: | :---: |
| $B_{c}^{+} \rightarrow J / \psi \pi^{+}$ | $3508 \pm 82$ | $6887 \pm 93$ |
| $B_{c}^{+} \rightarrow J / \psi K^{+}$ | $-81 \pm 58$ | $90 \pm 43$ |
| $B_{c}^{+} \rightarrow J / \psi \rho^{+}$ | $41 \pm 11$ | $56 \pm 22$ |
| Comb. bkg. | $101 \pm 25$ | $1254 \pm 60$ |

(a) $\mathrm{J} / \psi$ yields

| Component | Yield |
| :--- | :---: |
| $B_{c}^{+} \rightarrow \psi(2 S) \pi^{+}$ | $256 \pm 18$ |
| $B_{c}^{+} \rightarrow \psi(2 S) K^{+}$ | $13 \pm 10$ |
| $B_{c}^{+} \rightarrow \psi(2 S) \rho^{+}$ | $-4 \pm 5$ |
| Comb. bkg. | $197 \pm 19$ |

(b) $\psi(2 S)$ yields

Simulation corrected for:

- Particle identification
- Track reconstruction efficiency.
- Trigger efficiency.
- $B_{c}^{+}$lifetime, kinematics.
- Track multiplicity.

| $q^{2}$ interval | $N_{\pi^{+} \mu^{+} \mu^{-}}$ | $N_{\text {comb }}$ |
| :---: | ---: | :---: |
| $0.1<q^{2}<1.1 \mathrm{GeV}^{2}$ | $0 \pm 2$ | $25_{-5}^{+6}$ |
| $1.1<q^{2}<8.0 \mathrm{GeV}^{2}$ | $1_{-3}^{+4}$ | $39 \pm 7$ |
| $11.0<q^{2}<12.5 \mathrm{GeV}^{2}$ | $-18_{-10}^{+7}$ | $30_{-9}^{+13}$ |
| $15.0<q^{2}<35.0 \mathrm{GeV}^{2}$ | $0_{-7}^{+8}$ | $232 \pm 17$ |
| All | $-2_{-8}^{+9}$ | $311_{-19}^{+20}$ |

(a) Rare mode yields

## $R_{\pi^{+} \mu^{+} \mu^{-} / J / \psi}$ and $R_{\psi(2 S) / J / \psi}$

## Mass scales are shared between



## $R_{\pi^{+} \mu^{+} \mu^{-} / J / \psi}$ and $R_{\psi(2 S) / J / \psi}$

## Backgrounds:

- Partially reco: $B_{c}^{+} \rightarrow \rho \mu^{+} \mu^{-}, B_{c}^{+} \rightarrow J / \psi \rho^{+}$and $B_{c}^{+} \rightarrow \psi(2 S) \rho^{+}$with $\rho \rightarrow \pi^{+} \pi^{0}$. Included only for resonant fits .
- Single Mis-ID: Decays with Kaons reconstructed as pions in final state are Cabibbo suppresed and further suppressed by particle ID requirements .
- Double Mis-ID: E.g. $B_{c}^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+}$or $B_{c}^{+} \rightarrow c \bar{c}\left(\rightarrow \mu_{\rightarrow \pi^{+}}^{+}, \mu^{-}\right) \pi_{\rightarrow \mu^{+}}^{+}$are suppressed by particle ID .


## Selection uses BDT

- Signal: Simulated $B_{c}^{+} \rightarrow \pi^{+} \mu^{+} \mu^{-}, B_{c}^{+} \rightarrow \pi^{+} J / \psi\left(\rightarrow \mu^{+} \mu^{-}\right)$, $B_{c}^{+} \rightarrow \pi^{+} B^{* 0}\left(\rightarrow \mu^{+} \mu^{-}\right)$and $B_{c}^{+} \rightarrow \pi^{+} B_{s}^{* 0}\left(\rightarrow \mu^{+} \mu^{-}\right)$
- Background: Data sidebands in $m\left(\pi^{+} \mu^{+} \mu^{-}\right)$, excluding charmonium from $m\left(\mu^{+} \mu^{-}\right)$distribution.

MVA optimization FOM is different for each measurement

- $R_{\pi^{+} \mu^{+} \mu^{-} / J / \psi} \Rightarrow \varepsilon /\left(5 / 2+\sqrt{N_{B}}\right)$
- $R_{\psi(2 S) / J / \psi} \Rightarrow N_{S} / \sqrt{N_{S}+N_{B}}$


## Search for the $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$ decay

## Photons:

- $p_{T}>1000 \mathrm{MeV}$
- MVA based photon identification.
- For $p_{T}>2000 \mathrm{MeV}$ MVA to separate them from merged photons in $\pi^{0} \rightarrow \gamma \gamma$
Muons:
- $p_{T}>250 \mathrm{MeV}$
- Good quality and particle identification requirements
$B_{s}$
- $p_{T}>500 \mathrm{MeV}$
- Good vertex quality


## Search for the $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$ decay

Differences with respect to $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \rightarrow$ PhysRevD.105.012010

$$
B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma
$$

- This reconstructs the photon.
- Mesures $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$ as signal
- Thanks to the photon can explore also lower regions in $q^{2}$

$$
B_{s}^{0} \rightarrow \mu^{+} \mu^{-}
$$

- Reconstructs only the muons
- Measures $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$ as part of the partially reconstructed background
- Can only have access to high $q^{2}$ regions $>4.9 \mathrm{GeV}^{2}$

Both have set upper limits.

## Search for the $B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma$ decay



$$
\begin{aligned}
\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma\right)_{\text {bin I }} & =(1.34 \pm 1.60 \pm 0.28) \times 10^{-8} \\
\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma\right)_{\text {bin II }} & =(0.76 \pm 3.55 \pm 0.30) \times 10^{-8} \\
\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma\right)_{\text {bin III }} & =(-2.55 \pm 2.25 \pm 0.41) \times 10^{-8} \\
\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-} \gamma\right)_{\text {bin I } \phi \text { veto }} & =(0.72 \pm 1.56 \pm 0.29) \times 10^{-8}
\end{aligned}
$$

## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

## Preselection:

- $\Lambda_{b}^{0}$ : Good vertex quality, momentum pointing to PV
- $p, K^{-}: I P>0.1 m m, p_{T}>1 \mathrm{GeV}, p>5 \mathrm{GeV}$.
- $\gamma: E_{T}>3 \mathrm{GeV}$


## MVA:

- Uses kinematic variables and isolation
- Background: Upper sideband in data $m(p K \gamma)>m\left(\Lambda_{b}^{0}\right)+300 \mathrm{MeV}$
- FOM: $S / \sqrt{S+B}$

$$
I_{p_{\mathrm{T}}}=\frac{p_{\mathrm{T}}\left(\Lambda_{b}^{0}\right)-\sum p_{\mathrm{T}}}{p_{\mathrm{T}}\left(\Lambda_{b}^{0}\right)+\sum p_{\mathrm{T}}}
$$

## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

Mis-ID backgrounds:

- $B_{s}^{0} \rightarrow \phi(\rightarrow K K) \gamma$ : Veto $m\left(p_{\rightarrow K}, K\right)$ mass around $m_{\phi}$.
- $B_{s}^{0} \rightarrow K K \gamma, B_{d} \rightarrow K \pi \gamma$ : Less than $0.5 \%$.
- $\Lambda_{b}^{0} \rightarrow p K \eta, \Lambda_{b}^{0} \rightarrow p K \pi^{0}$ : Less than 1-2\%, limited by staying below $2.5 \mathrm{GeVin} m(p, K)$.
- $\Xi_{b}^{0} \rightarrow p K \gamma$ : Negligible

Mis-ID and Combinatorial:

- $D^{0} \rightarrow K K$ and $D^{0} \rightarrow K \pi$ combined with random $\gamma$ : Veto distorts signal acceptance $\Rightarrow$ included in fit.


## Partially reconstructed:

- $\Lambda_{b}^{0} \rightarrow p K^{*-}\left(\rightarrow K^{-} \pi 0\right) \gamma$ Included in fit.


## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

Maximum likelihood fit uses:

- Reduced model: Well-established resonances and interferences.
- Non resonant: Seen to improve fit quality

Projections of 2D fit on $m_{\Lambda_{b}}\left(p K^{-}\right)$


$\begin{array}{ll}\square & \text { interf. }(1 / 2)^{+} \\ \square & -\Lambda(1520) \\ \text { interf. }(1 / 2)^{-} & -\Lambda(1600) \\ \square \text { interf. }(3 / 2)^{-} & -\Lambda(1670) \\ - & \text { interf. }(5 / 2)^{+} \\ -\Lambda(1405) & -\Lambda(1690) \\ & -\Lambda(1800)\end{array}$

- $\Lambda(1810)$
- $\Lambda(2110)$
- $\Lambda(1820)-\Lambda(2350)$
- $\Lambda(1830) \quad$ - $\mathrm{NR}\left((3 / 2)^{-}\right)$
- $\Lambda(1890) \quad+$ Model
$-\Lambda(2100)+$ Data


## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

## Mass fits:

- Combinatorial: Exponential
- Signal: Double sided Crystall Ball, tails from simulation
- Partially reconstructed: From Kernel density estimation on simulated $\Lambda_{b}^{0} \rightarrow p K^{*-}\left(\rightarrow K^{-} \pi 0\right) \gamma$.


## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

| Resonance | $J^{P}$ | $m_{0}$ | $\Gamma_{0}$ | $\Delta m_{0}$ | $\Delta \Gamma_{0}$ | $\sigma_{m_{0}}$ | $\sigma_{\Gamma_{0}}$ | $l$ | $L$ |
| :---: | :---: | :---: | ---: | :---: | ---: | ---: | ---: | :---: | :---: |
| $\Lambda(1405)$ | $1 / 2^{-}$ | 1405 | 50.5 | $\pm 1.3$ | $\pm 2$ | 1.3 | 2 | 0 | 0,1 |
| $\Lambda(1520)$ | $3 / 2^{-}$ | 1519 | 16 | $1518-1520$ | $15-17$ | 1 | 1 | 2 | $0,1,2$ |
| $\Lambda(1600)$ | $1 / 2^{+}$ | 1600 | 200 | $1570-1630$ | $150-250$ | 30 | 50 | 1 | 0,1 |
| $\Lambda(1670)$ | $1 / 2^{-}$ | 1674 | 30 | $1670-1678$ | $25-35$ | 4 | 5 | 0 | 0,1 |
| $\Lambda(1690)$ | $3 / 2^{-}$ | 1690 | 70 | $1685-1695$ | $50-70$ | 5 | 10 | 2 | $0,1,2$ |
| $\Lambda(1800)$ | $1 / 2^{-}$ | 1800 | 200 | $1750-1850$ | $150-250$ | 50 | 50 | 0 | 0,1 |
| $\Lambda(1810)$ | $1 / 2^{+}$ | 1790 | 110 | $1740-1840$ | $50-170$ | 50 | 60 | 1 | 0,1 |
| $\Lambda(1820)$ | $5 / 2^{+}$ | 1820 | 80 | $1815-1825$ | $70-90$ | 5 | 10 | 3 | $1,2,3$ |
| $\Lambda(1830)$ | $5 / 2^{-}$ | 1825 | 90 | $1820-1830$ | $60-120$ | 5 | 30 | 2 | $1,2,3$ |
| $\Lambda(1890)$ | $3 / 2^{+}$ | 1890 | 120 | $1870-1910$ | $80-160$ | 20 | 40 | 1 | $0,1,2$ |
| $\Lambda(2100)$ | $7 / 2^{-}$ | 2100 | 200 | $2090-2110$ | $100-250$ | 10 | 100 | 4 | $2,3,4$ |
| $\Lambda(2110)$ | $5 / 2^{+}$ | 2090 | 250 | $2050-2130$ | $200-300$ | 40 | 50 | 3 | $1,2,3$ |
| $\Lambda(2350)$ | $9 / 2^{+}$ | 2350 | 150 | $2340-2370$ | $100-250$ | 20 | 100 | 5 | $3,4,5$ |

## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

Amplitude fit contains many parameters $\Rightarrow$ unstable.

- Local minima:
- Fit ten times with different starting points.
- Pick fit with lowest NLL.
- Parameter variations: Couplings vary between minima, but same values for
- Fit fractions
- Interference amplitudes
$\Rightarrow$ treat couplings as nuisance parameters and fit fractions and interference amplitudes as parameters of interest.


## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

Resonances used in reduced model

| Resonance | $J^{P}$ | $m_{0}$ | $\Gamma_{0}$ | $\Delta m_{0}$ | $\Delta \Gamma_{0}$ | $\sigma_{m_{0}}$ | $\sigma_{\Gamma_{0}}$ | $l$ | $L$ |
| :---: | :---: | :---: | :---: | :---: | ---: | ---: | ---: | :---: | :---: |
| $\Lambda(1405)$ | $1 / 2^{-}$ | 1405 | 50.5 | $\pm 1.3$ | $\pm 2$ | 1.3 | 2 | 0 | 0,1 |
| $\Lambda(1520)$ | $3 / 2^{-}$ | 1519 | 16 | $1518-1520$ | $15-17$ | 1 | 1 | 2 | $0,1,2$ |
| $\Lambda(1600)$ | $1 / 2^{+}$ | 1600 | 200 | $1570-1630$ | $150-250$ | 30 | 50 | 1 | 0,1 |
| $\Lambda(1670)$ | $1 / 2^{-}$ | 1674 | 30 | $1670-1678$ | $25-35$ | 4 | 5 | 0 | 0,1 |
| $\Lambda(1690)$ | $3 / 2^{-}$ | 1690 | 70 | $1685-1695$ | $50-70$ | 5 | 10 | 2 | $0,1,2$ |
| $\Lambda(1800)$ | $1 / 2^{-}$ | 1800 | 200 | $1750-1850$ | $150-250$ | 50 | 50 | 0 | 0,1 |
| $\Lambda(1810)$ | $1 / 2^{+}$ | 1790 | 110 | $1740-1840$ | $50-170$ | 50 | 60 | 1 | 0,1 |
| $\Lambda(1820)$ | $5 / 2^{+}$ | 1820 | 80 | $1815-1825$ | $70-90$ | 5 | 10 | 3 | $1,2,3$ |
| $\Lambda(1830)$ | $52^{-}$ | 1825 | 90 | $1820-1830$ | $60-120$ | 5 | 30 | 2 | $1,2,3$ |
| $\Lambda(1890)$ | $3 / 2^{+}$ | 1890 | 120 | $1870-1910$ | $80-160$ | 20 | 40 | 1 | $0,1,2$ |
| $\Lambda(2100)$ | $7 / 2^{-}$ | 2100 | 200 | $2090-2110$ | $100-250$ | 10 | 100 | 4 | $2,3,4$ |
| $\Lambda(2110)$ | $5 / 2^{+}$ | 2090 | 250 | $2050-2130$ | $200-300$ | 40 | 50 | 3 | $1,2,3$ |
| $\Lambda(2350)$ | $9 / 2^{+}$ | 2350 | 150 | $2340-2370$ | $100-250$ | 20 | 100 | 5 | $3,4,5$ |

## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

## Reduced model (only resonances)



$\begin{array}{llll}\text { interf. }(1 / 2)^{+} & -\Lambda(1520) & -\Lambda(1810) & -\Lambda(2110) \\ \text { interf. }(1 / 2)^{-} & -\Lambda(1600) & -\Lambda(1820) & -\Lambda(2350) \\ \text { interf. }(3 / 2)^{-} & -\Lambda(1670) & -\Lambda(1830) & \text { \& Model } \\ - \\ \text { interf. }(5 / 2)^{+} & -\Lambda(1690) & -\Lambda(1890) & \text { + Data } \\ -\Lambda(1405) & -\Lambda(1800) & -\Lambda(2100) & \end{array}$

## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

Reduced model plus non-resonant components


## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

Reduced model (resonances and interferences) fit plus non-resonant (constant) components


## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

Reduced model (resonances and interferences) fit plus non-resonant (constant) components


## Amplitude analysis of the $\Lambda_{b}^{0} \rightarrow p K^{-} \gamma$ decay

## Systematics on fit fractions.

| Observable | Amplitude model |  |  |  | Acceptance model |  |  | Mass fit model |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\sigma_{\text {BW }}^{A}$ | $\sigma_{\text {radius }}^{\Lambda}$ | $\sigma_{\text {amp }}$ | $\sigma_{\text {res. }}$ | $\sigma_{\text {finite }}$ | $\sigma_{\text {acc. }}$ | $\sigma_{\text {kin. }}$ | $\sigma_{p K}$ | $\sigma_{p \gamma}$ | $\sigma_{\text {comb }}$. |
| $\Lambda(1405)$ | +1.2 -0.7 | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.9 \\ & +0.2 \end{aligned}$ | ${ }_{-0.4}^{+0.0}$ | ${ }_{-0.2}^{+0.2}$ | $\begin{array}{r} +0.2 \\ { }_{-0.2} \end{array}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0}^{+} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ |
| A(1520) | $\begin{array}{r} +1.0 \\ -1.3 \end{array}$ | $\begin{aligned} & +1.1 \\ & { }_{-1.1} \end{aligned}$ | $\begin{aligned} & +0.3 \\ & +0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & -0.2 \end{aligned}$ | $\begin{array}{r} +0.2 \\ -0.2 \end{array}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.3 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.1} \end{aligned}$ |
| $\Lambda(1600)$ | +3.6 -4.5 | $\begin{aligned} & +1.8 \\ & -1.8 \end{aligned}$ | $\begin{aligned} & +0.5 \\ & +0.0 \end{aligned}$ | $\begin{aligned} & +0.3 \\ & -0.2 \end{aligned}$ | $\begin{aligned} & +0.3 \\ & -0.3 \end{aligned}$ | $\begin{aligned} & +0.2 \\ & -0.2 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ |
| A(1670) | $\begin{aligned} & +1.1 \\ & -0.3 \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.2} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.2} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & -0.2 \end{aligned}$ | ${ }_{-0.1}^{+0.1}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ |
| A(1690) | $\begin{array}{r} +4.1 \\ -0.3 \end{array}$ | $\begin{aligned} & +2.0 \\ & -2.0 \end{aligned}$ | $\begin{aligned} & +1.5 \\ & +0.2 \end{aligned}$ | $\begin{aligned} & +0.6 \\ & -0.5 \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.2} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ |
| $\Lambda(1800)$ | $\begin{array}{r} +3.0 \\ { }_{-5.9} \end{array}$ | $\begin{aligned} & +1.1 \\ & { }_{-1.1} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.8 \end{aligned}$ | $\begin{aligned} & +0.8 \\ & -1.5 \end{aligned}$ | $\begin{array}{r} +0.3 \\ -0.3 \end{array}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.1 \end{aligned}$ | $\begin{array}{r} +0.0 \\ { }_{-0.0} \end{array}$ | $\begin{aligned} & +0.6 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.4 \\ & { }_{-0.0} \end{aligned}$ |
| A(1810) | $\begin{aligned} & +3.7 \\ & -0.7 \end{aligned}$ | $\begin{aligned} & +1.1 \\ & { }_{-1.1} \end{aligned}$ | $\begin{aligned} & +1.5 \\ & +0.1 \end{aligned}$ | $\begin{aligned} & +0.5 \\ & { }_{-1.4} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & -0.2 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ |
| $\Lambda(1820)$ | $\begin{array}{r} +1.8 \\ -4.9 \end{array}$ | $\begin{aligned} & +0.2 \\ & -0.2 \end{aligned}$ | $\begin{aligned} & -0.0 \\ & -0.9 \end{aligned}$ | $\begin{array}{r} +0.3 \\ -0.4 \end{array}$ | $\begin{aligned} & +0.3 \\ & -0.3 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.3 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0}^{+} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.1}^{+} \end{aligned}$ |
| $\Lambda(1830)$ | $\begin{aligned} & +1.3 \\ & { }_{-0.9} \end{aligned}$ | $\begin{aligned} & +0.6 \\ & { }_{-0.6} \end{aligned}$ | $\begin{aligned} & +0.3 \\ & { }_{-0.4} \end{aligned}$ | $\begin{aligned} & +0.3 \\ & -0.5 \end{aligned}$ | ${ }_{-0.1}^{+0.1}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0}^{+} \end{aligned}$ |
| $\Lambda(1890)$ | $\begin{array}{r} +4.2 \\ -5.1 \end{array}$ | $\begin{aligned} & +0.8 \\ & -0.8 \end{aligned}$ | $\begin{array}{r} +0.4 \\ -0.4 \end{array}$ | $\begin{aligned} & +0.1 \\ & +0.4 \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.2} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1}^{+} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0}^{+} \end{aligned}$ |
| A(2100) | $\begin{aligned} & +1.0 \\ & -2.6 \end{aligned}$ | $\begin{aligned} & +0.8 \\ & -0.8 \end{aligned}$ | $\begin{aligned} & +0.9 \\ & -0.7 \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.2} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0} \end{aligned}$ |
| A(2110) | $\begin{aligned} & +5.0 \\ & { }_{-0.6} \end{aligned}$ | $\begin{aligned} & +1.5 \\ & -1.5 \end{aligned}$ | $\begin{aligned} & +1.5 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.3 \\ & { }_{-0.2} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.2} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.0} \end{aligned}$ |
| $\Lambda(2350)$ | ${ }_{-0.1}^{+0.0}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.6 \\ & -0.7 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.0 \end{aligned}$ |
| $\mathrm{NR}\left(\frac{3}{2}^{-}\right)$ | $\begin{aligned} & +2.9 \\ & +0.3 \end{aligned}$ | $\begin{aligned} & +0.4 \\ & -0.4 \end{aligned}$ | $\begin{aligned} & +1.0 \\ & -2.4 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.6} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1}^{+0.1} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1}^{+0.1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.3} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ |
| $\Lambda(1405), A(1670)$ | ${ }_{-0.7}^{+0.7}$ | $\begin{aligned} & +0.3 \\ & -0.3 \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.1 \end{aligned}$ |
| $\Lambda(1405), \Lambda(1800)$ | $\begin{aligned} & +0.5 \\ & { }_{-3.6} \end{aligned}$ | $\begin{aligned} & +0.3 \\ & { }_{-0.3} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-1.9} \end{aligned}$ | $\begin{array}{r} +1.7 \\ -0.4 \end{array}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.2} \end{aligned}$ | $\begin{array}{r} +0.2 \\ -0.2 \end{array}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.3 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.0} \end{aligned}$ |
| $\Lambda(1520), \Lambda(1690)$ | $\begin{aligned} & +0.3 \\ & -2.3 \end{aligned}$ | $\begin{aligned} & +0.9 \\ & -0.9 \end{aligned}$ | $\begin{aligned} & -0.1 \\ & -0.7 \end{aligned}$ | $\begin{aligned} & +0.5 \\ & -0.4 \end{aligned}$ | $\begin{array}{r} +0.1 \\ -0.1 \end{array}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ |
| $\Lambda(1520), \mathrm{NR}\left(\frac{3}{2}^{-}\right)$ | $\begin{array}{r} +1.2 \\ -2.4 \end{array}$ | $\begin{aligned} & +1.5 \\ & -1.5 \end{aligned}$ | $\begin{aligned} & +0.5 \\ & -0.5 \end{aligned}$ | $\begin{aligned} & +0.8 \\ & -0.4 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ |
| $\Lambda(1600), A(1810)$ | $\begin{aligned} & +4.1 \\ & -2.8 \end{aligned}$ | $\begin{aligned} & +0.6 \\ & -0.6 \end{aligned}$ | $\begin{array}{r} +1.5 \\ -0.7 \end{array}$ | $\begin{array}{r} +0.9 \\ -0.4 \end{array}$ | $\begin{aligned} & +0.3 \\ & { }_{-0.3} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.2}^{+} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.4} \end{aligned}$ | $\begin{array}{r} +0.0 \\ -0.4 \end{array}$ |
| $\Lambda(1670), \Lambda(1800)$ | $\begin{array}{r} +1.5 \\ -1.9 \end{array}$ | $\begin{aligned} & +0.4 \\ & -0.4 \end{aligned}$ | $\begin{aligned} & +0.3 \\ & -0.2 \end{aligned}$ | $\begin{aligned} & +0.4 \\ & -0.4 \end{aligned}$ | ${ }_{-0.1}^{+0.1}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1}^{+0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.1 \end{aligned}$ |
| $\Lambda(1690), \mathrm{NR}\left(\frac{3}{2}^{-}\right)$ | $\begin{array}{r} +0.9 \\ -2.2 \end{array}$ | $\begin{aligned} & +1.1 \\ & { }_{-1.1} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & -2.7 \end{aligned}$ | $\begin{aligned} & +0.2 \\ & -0.5 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.1 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0} \end{aligned}$ |
| $\Lambda(1820), \Lambda(2110)$ | $\begin{array}{r} +2.4 \\ -3.1 \end{array}$ | $\begin{aligned} & +1.6 \\ & { }_{-1.6} \end{aligned}$ | $\begin{aligned} & +0.5 \\ & { }_{-1.6} \end{aligned}$ | $\begin{aligned} & +0.3 \\ & { }_{-0.5} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & -0.2 \end{aligned}$ | $\begin{aligned} & +0.1 \\ & { }_{-0.1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.2 \\ & { }_{-0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.3 \end{aligned}$ | $\begin{aligned} & +0.0 \\ & -0.2 \end{aligned}$ |

