



# Workshop Hydrodynamics and related observables in heavy-ion collisions

## Study of collective phenomena via the production of heavy quarks and quarkonia in hadronic collisions with ALICE

Victor Valencia Torres<sup>1</sup>

On behalf of ALICE Collaboration

1. SUBATECH (IMT Atlantique, Nantes Université, CNRS/IN2P3), Nantes, France



# Plan of this talk

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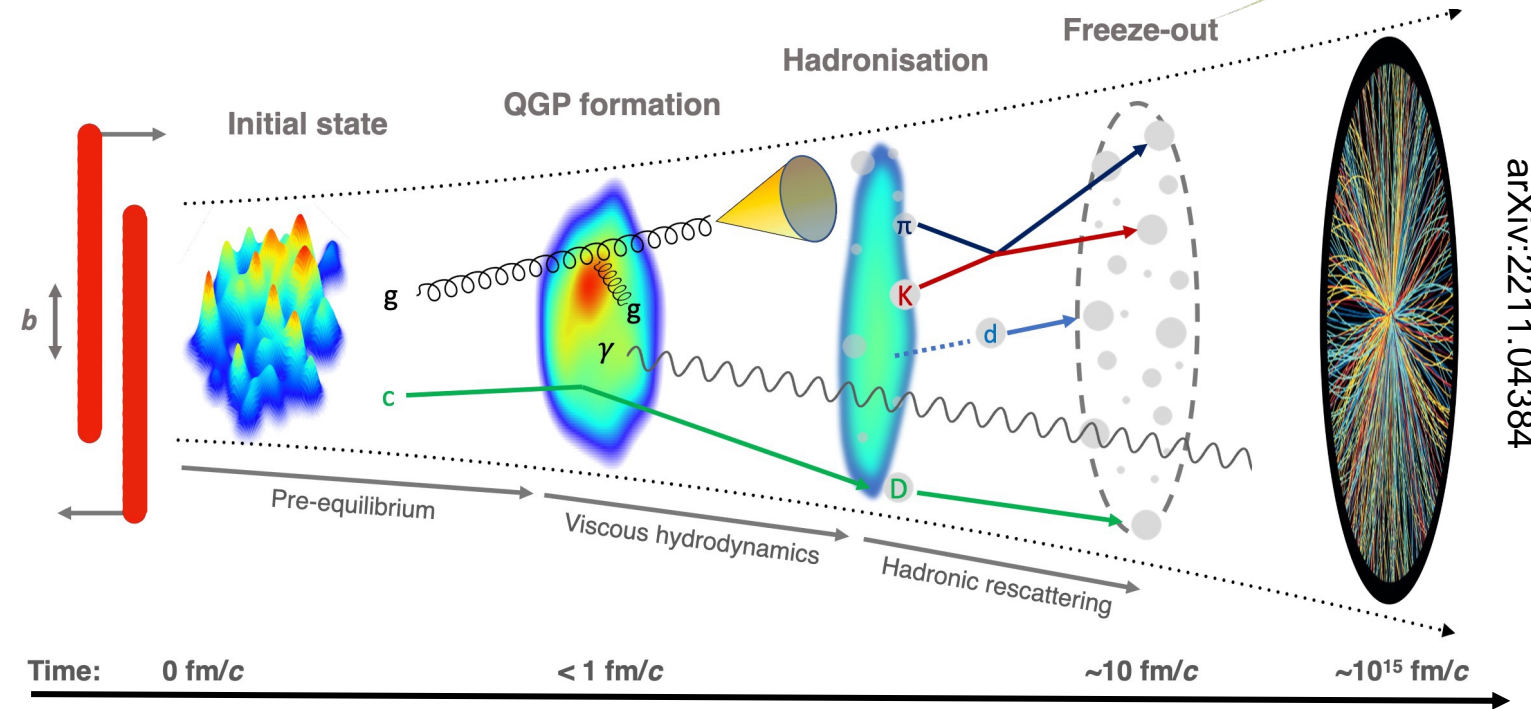
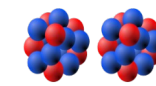


## 1) Introduction

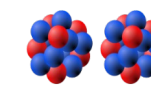
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- 2) Flow measurements in the **heavy-sector** with **Run 2 data**
  - $v_2$  from large to small systems

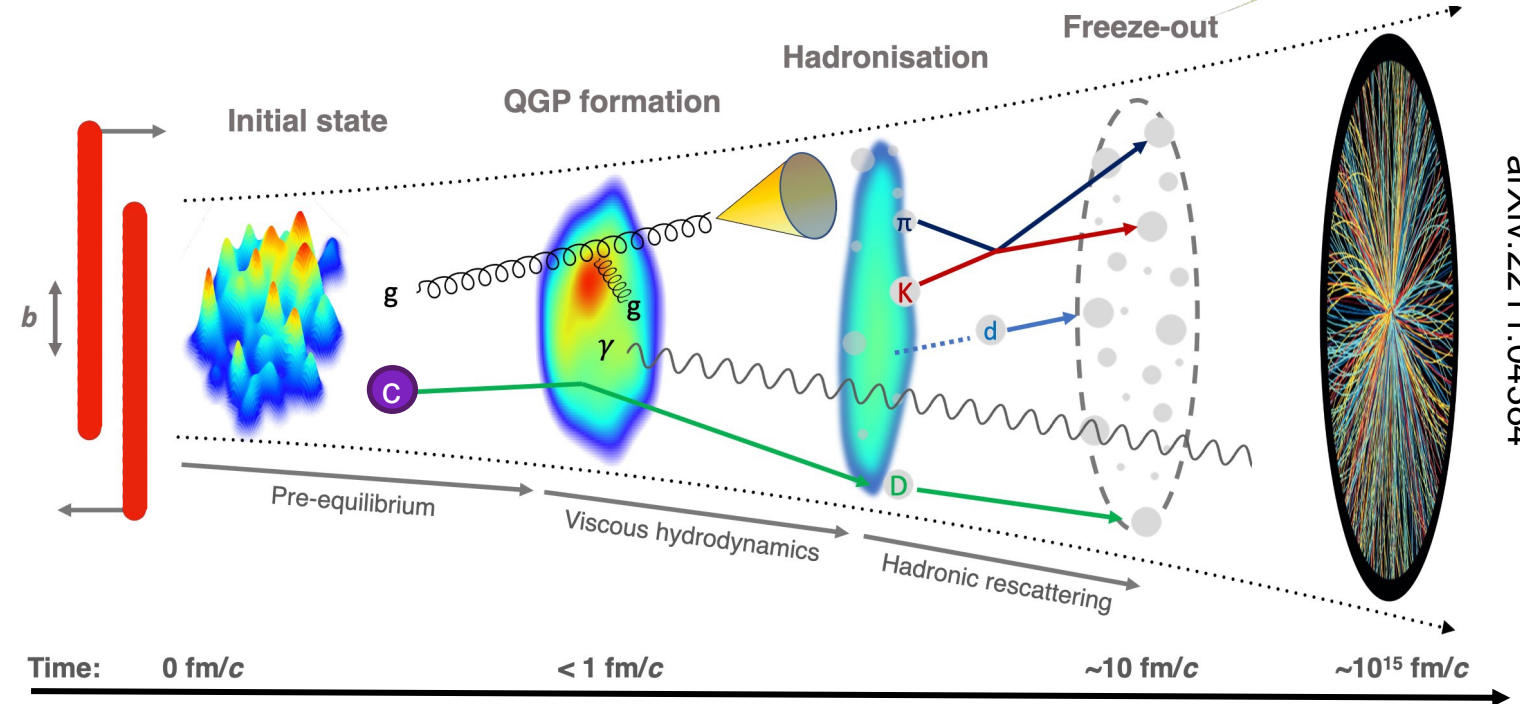
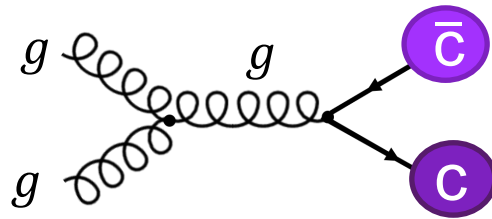
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- 3) New **flow** measurements of **J/ψ** using **Run 3 data**
  - $v_2^{J/\psi}$  using event plane and multi-particle cumulants methods
  - Perspective in Run 3



arXiv:2211.04384



- **Heavy-quark production** occurs at **early times** of the collision
  - $M_{c,b} > \Lambda_{\text{QCD}}$  (pQCD applicable)
  - **Sensitive** to the medium evolution

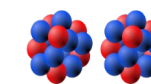


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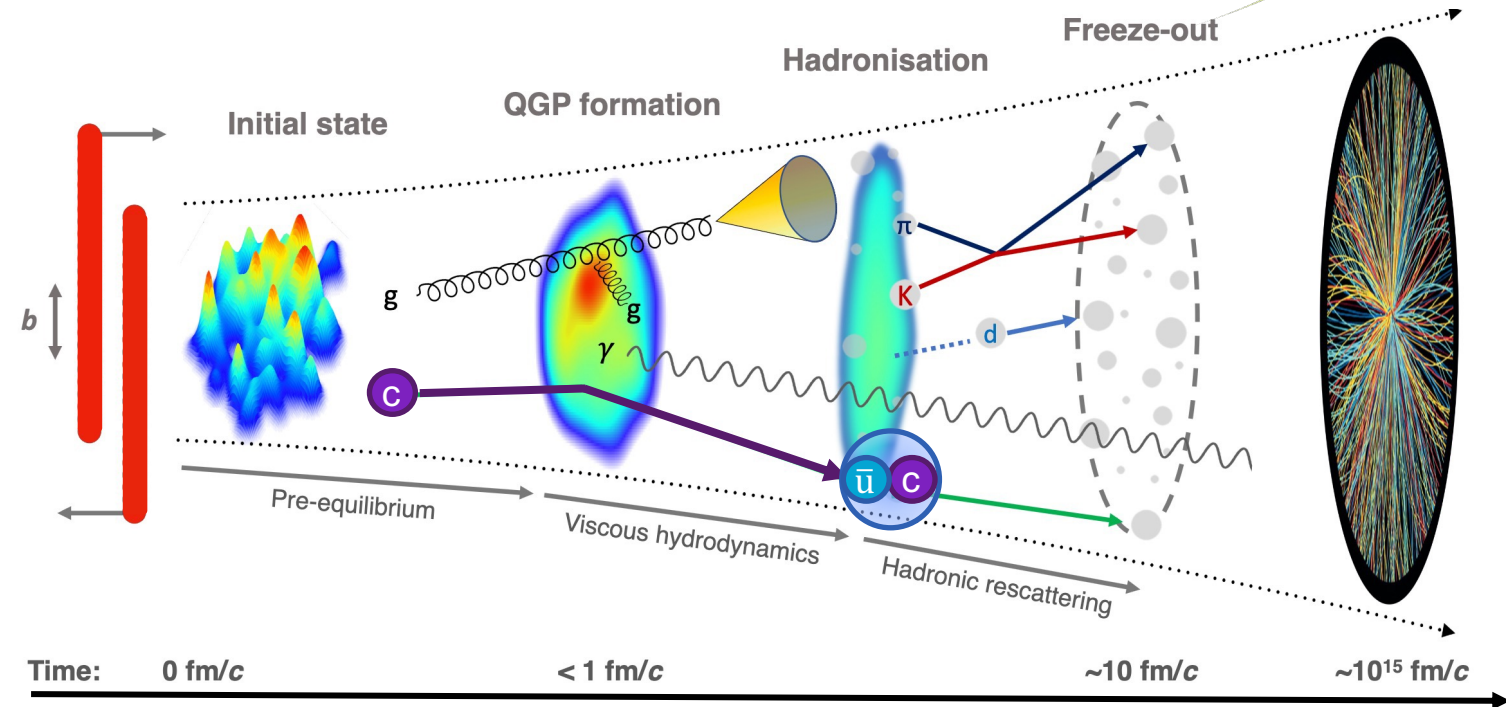
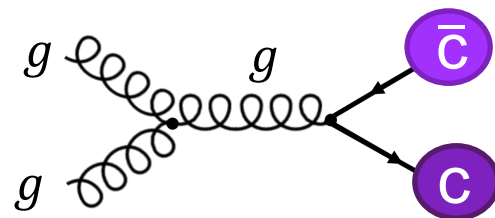


ALICE

# Heavy-flavor and Quarkonia in Pb–Pb collisions

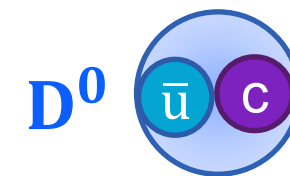


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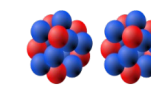


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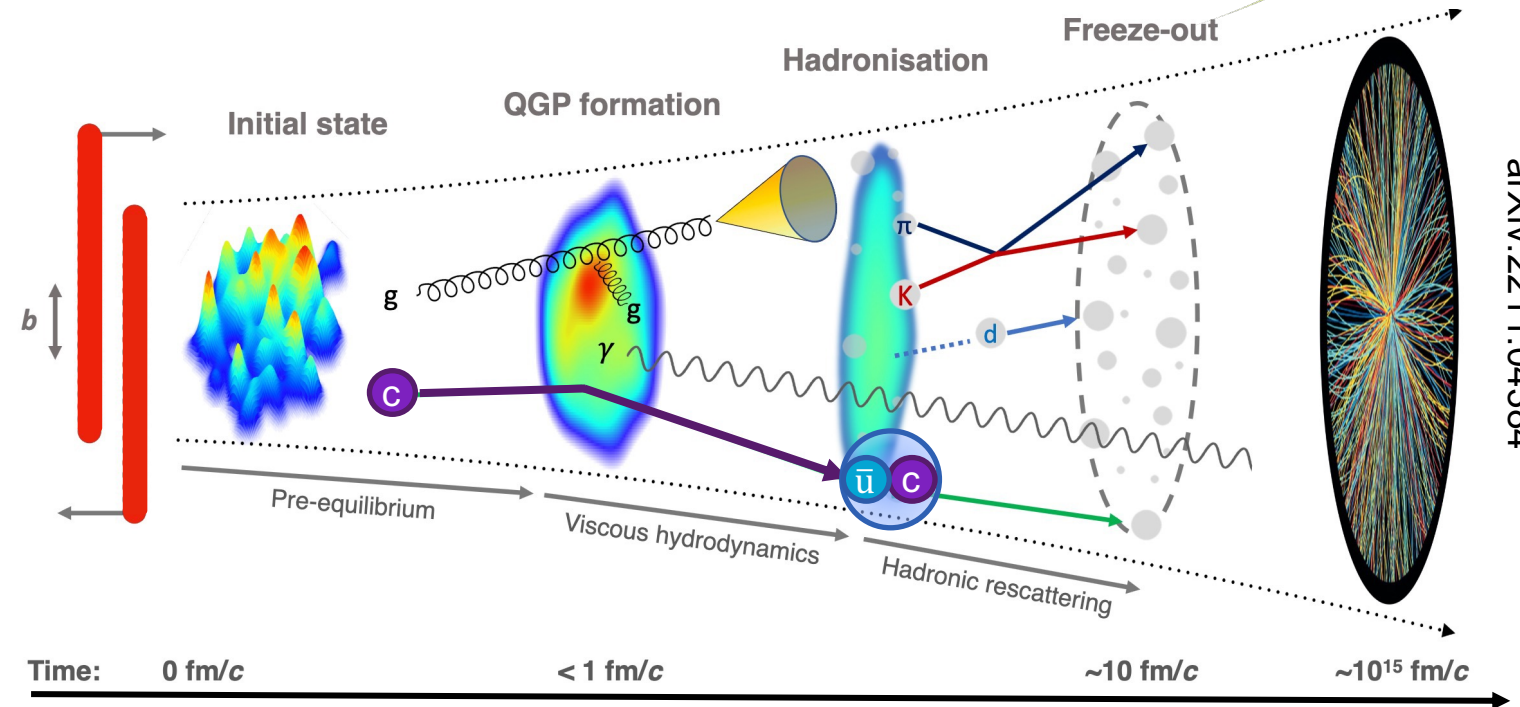
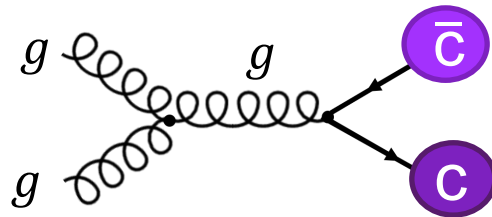
- **Open heavy-flavor hadrons** (made up of **light** and **heavy** quarks) allow to study the transport coefficient of **QGP**, investigating **charm thermalization**





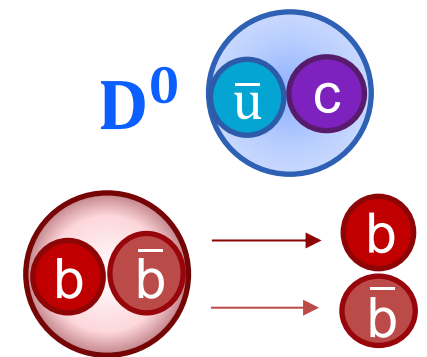


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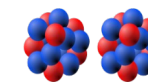
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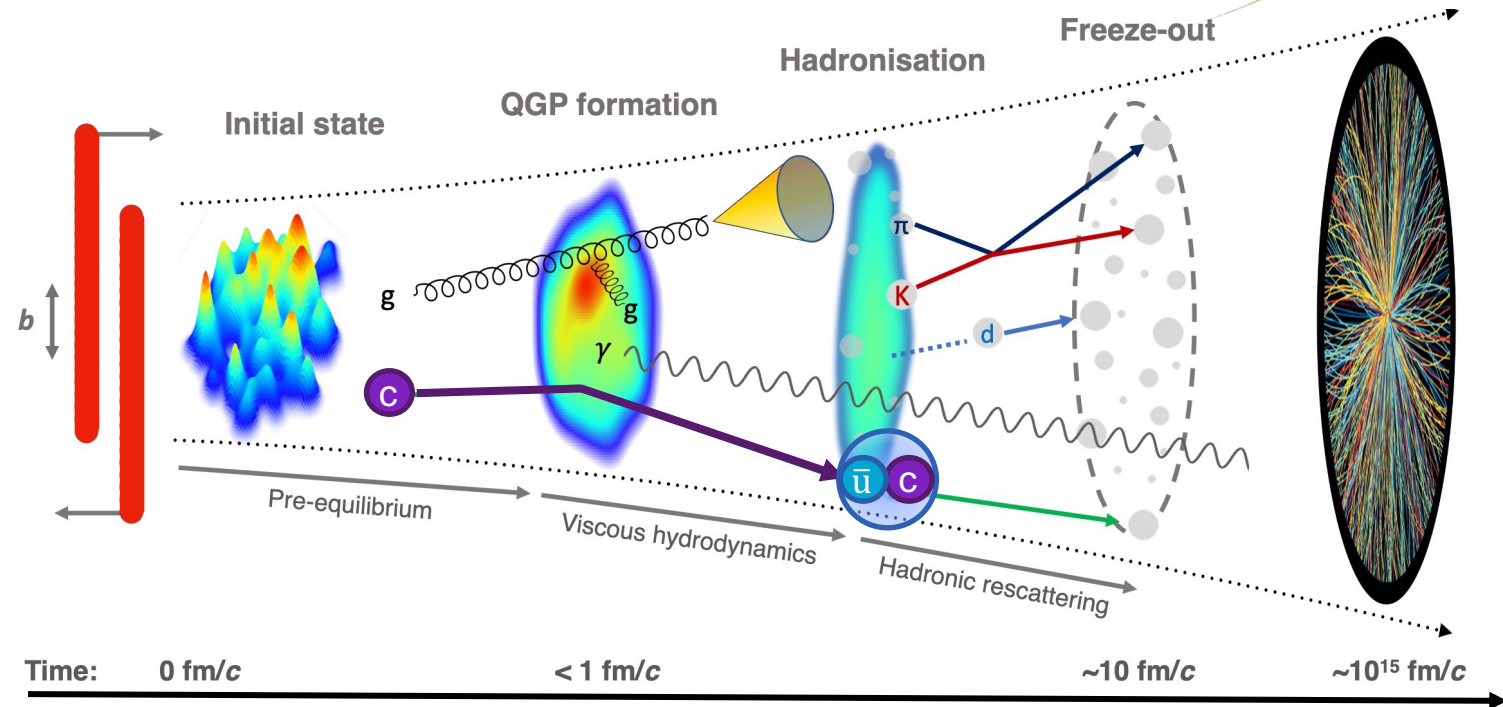
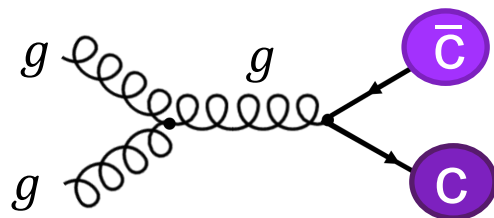


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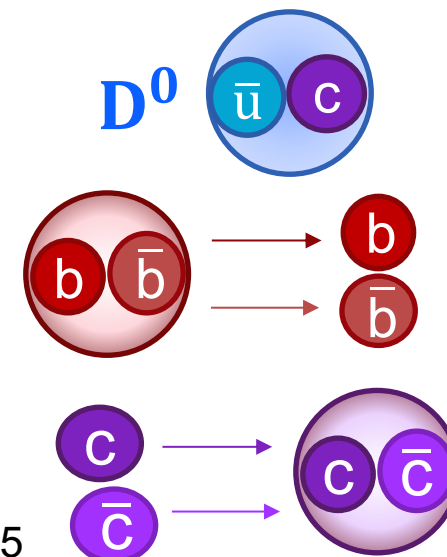


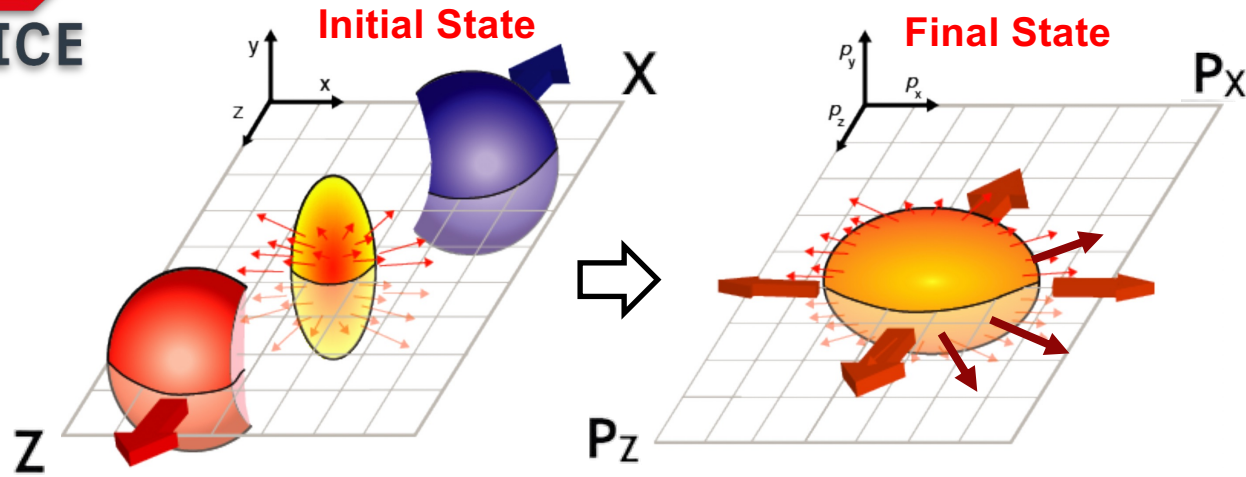
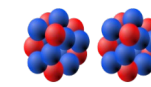
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- **Charmonium** state ( $c\bar{c}$  quark pairs) at **LHC** can be **produced through recombination** of uncorrelated  $c\bar{c}$  pairs (regeneration)
  - P.Braun-Munzinger and J.Stachel, PLB 490 (2000) 196
  - Robert L. Thews et al, PRC 63 (2001) 054905



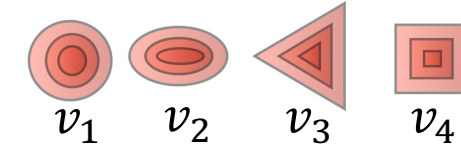


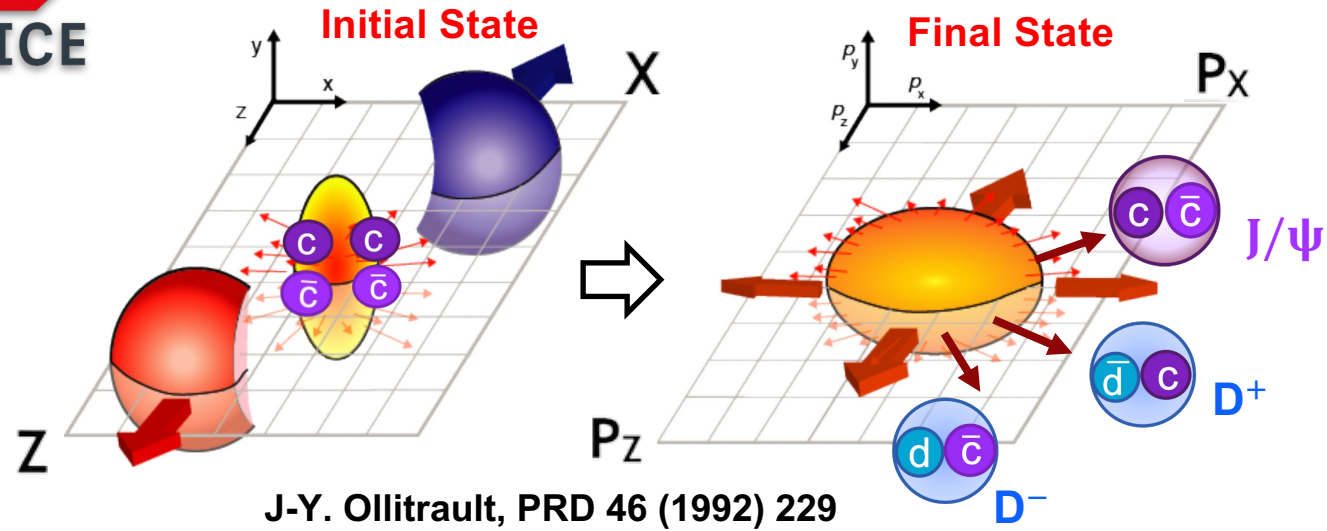
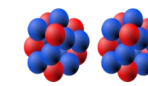
J-Y. Ollitrault, PRD 46 (1992) 229

Anisotropy of particle momentum distribution

$$\frac{dN}{d\varphi} = \frac{1}{2\pi} \left( 1 + \sum_{n=1}^{\infty} 2v_n \cos[n(\varphi - \psi_n)] \right)$$

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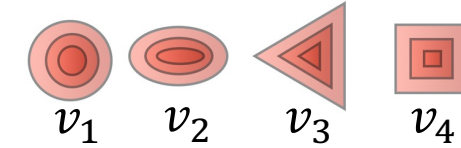


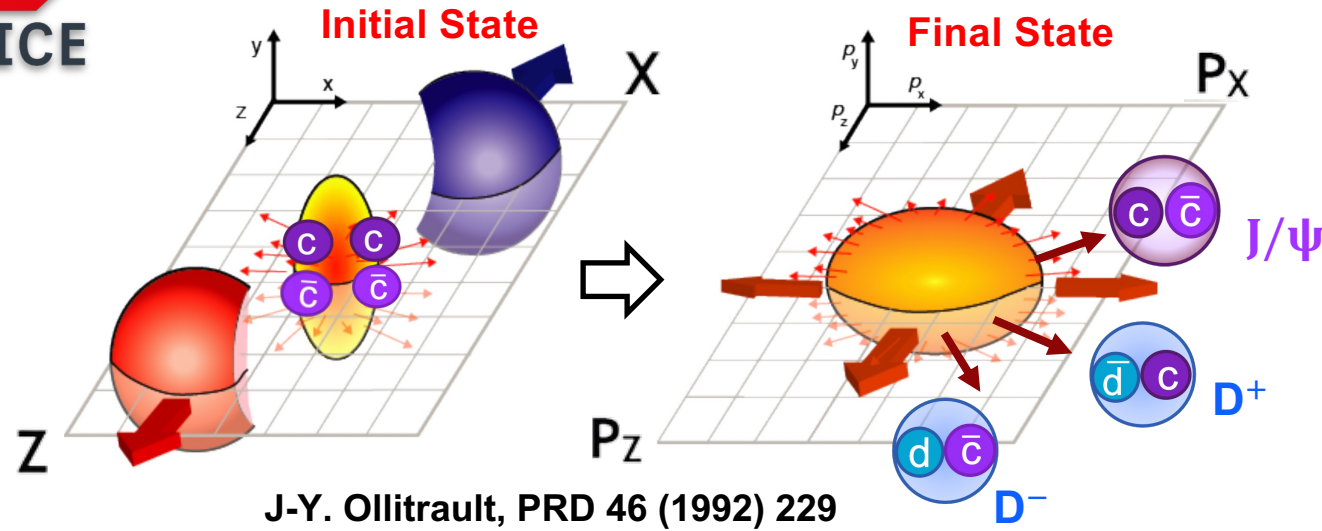
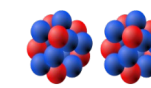


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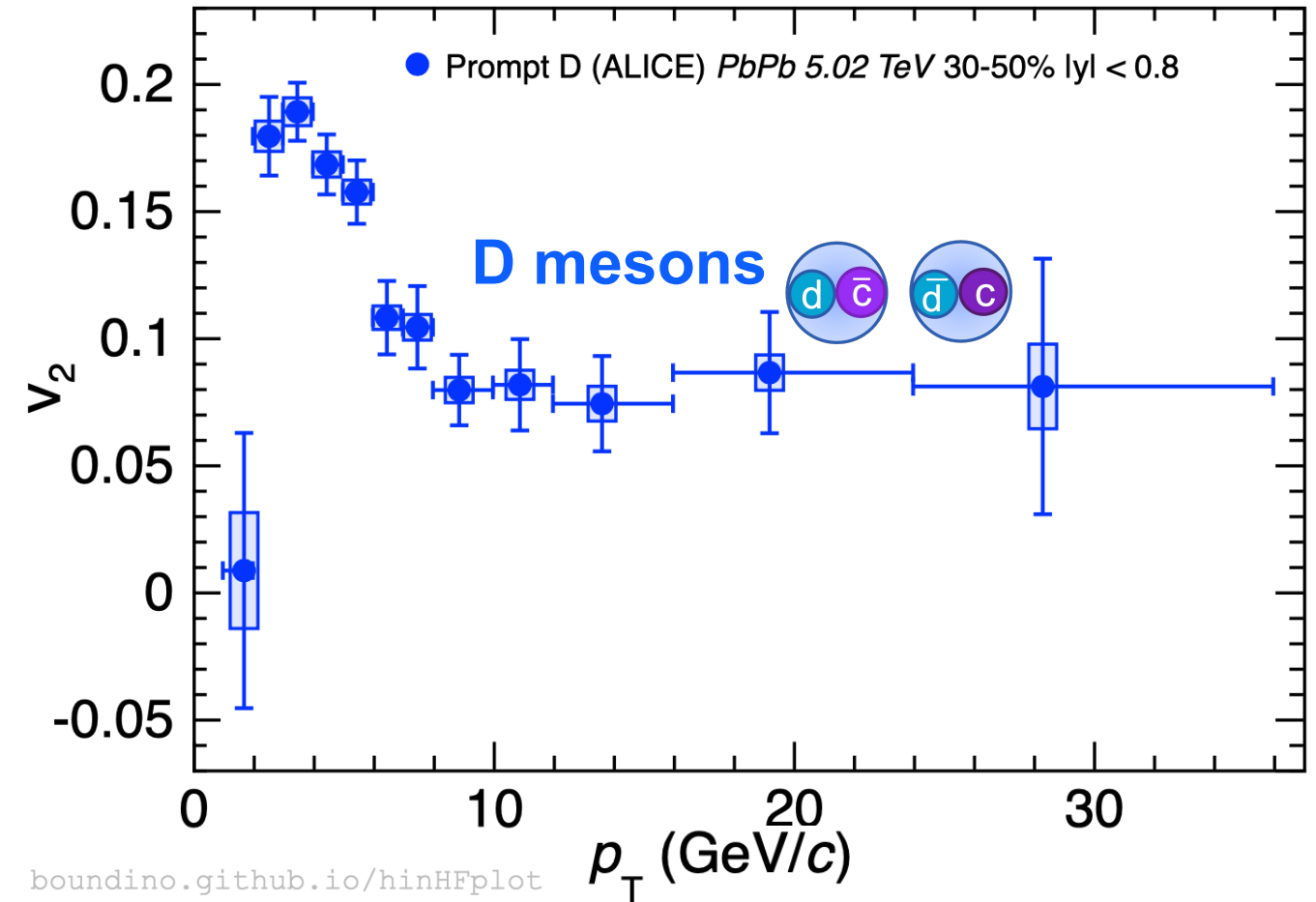


- **D mesons**: lightest hadrons with a **charm quark**
- **Pronounced flow** attributed to the **thermalization** of **light quarks (u, d, s)** and **charm quark** in the **QGP**

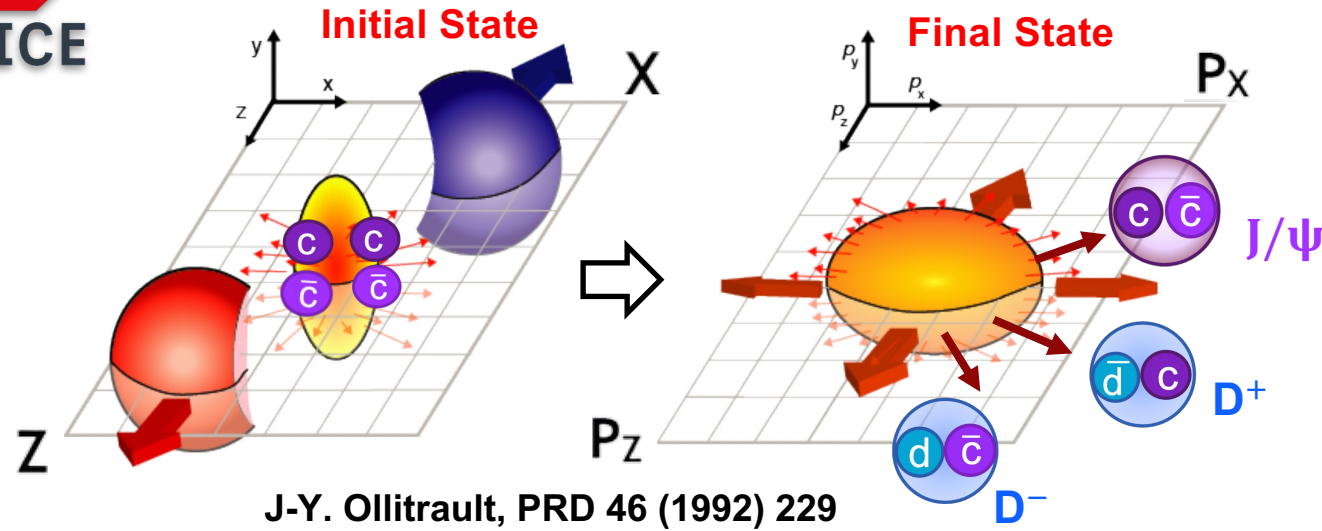
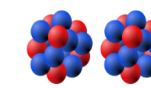
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ALICE, PLB 813 (2021) 136054

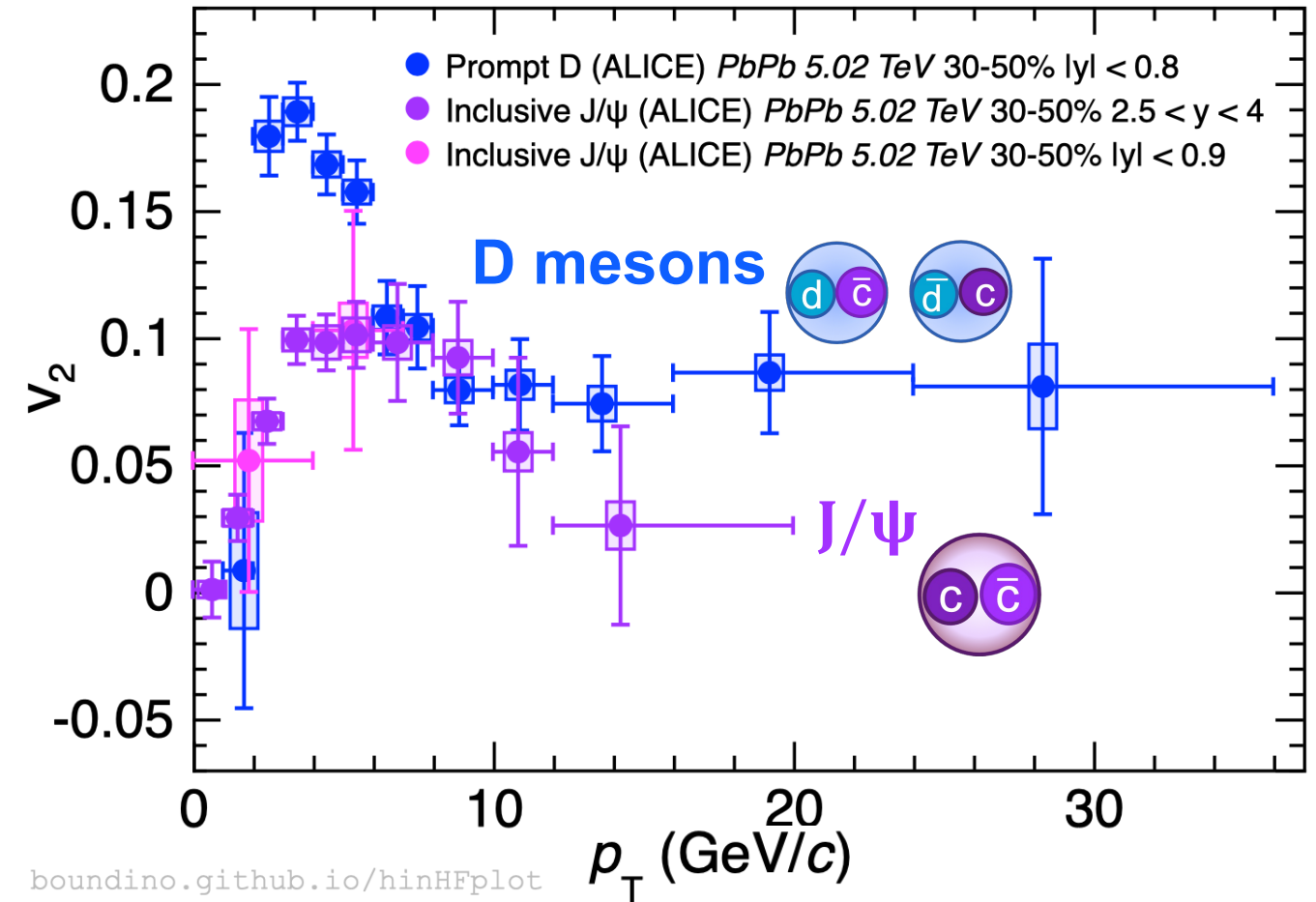


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 → **Flow** at **low  $p_T$**  explained by **regenerated J/ψ**

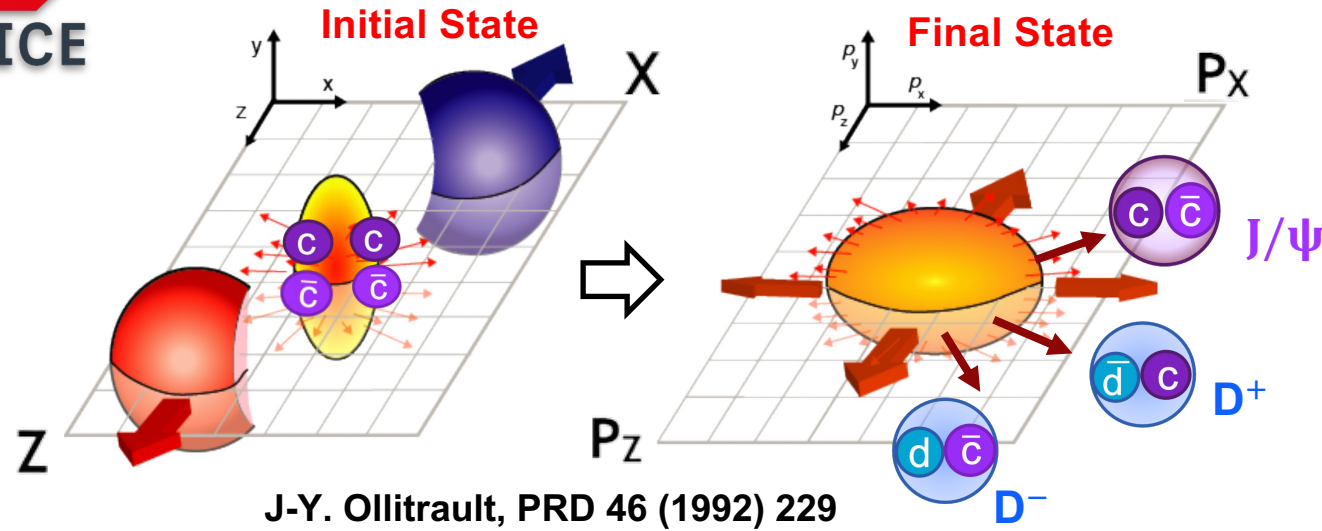
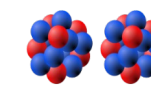
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 ALICE, JHEP 10 (2020) 141

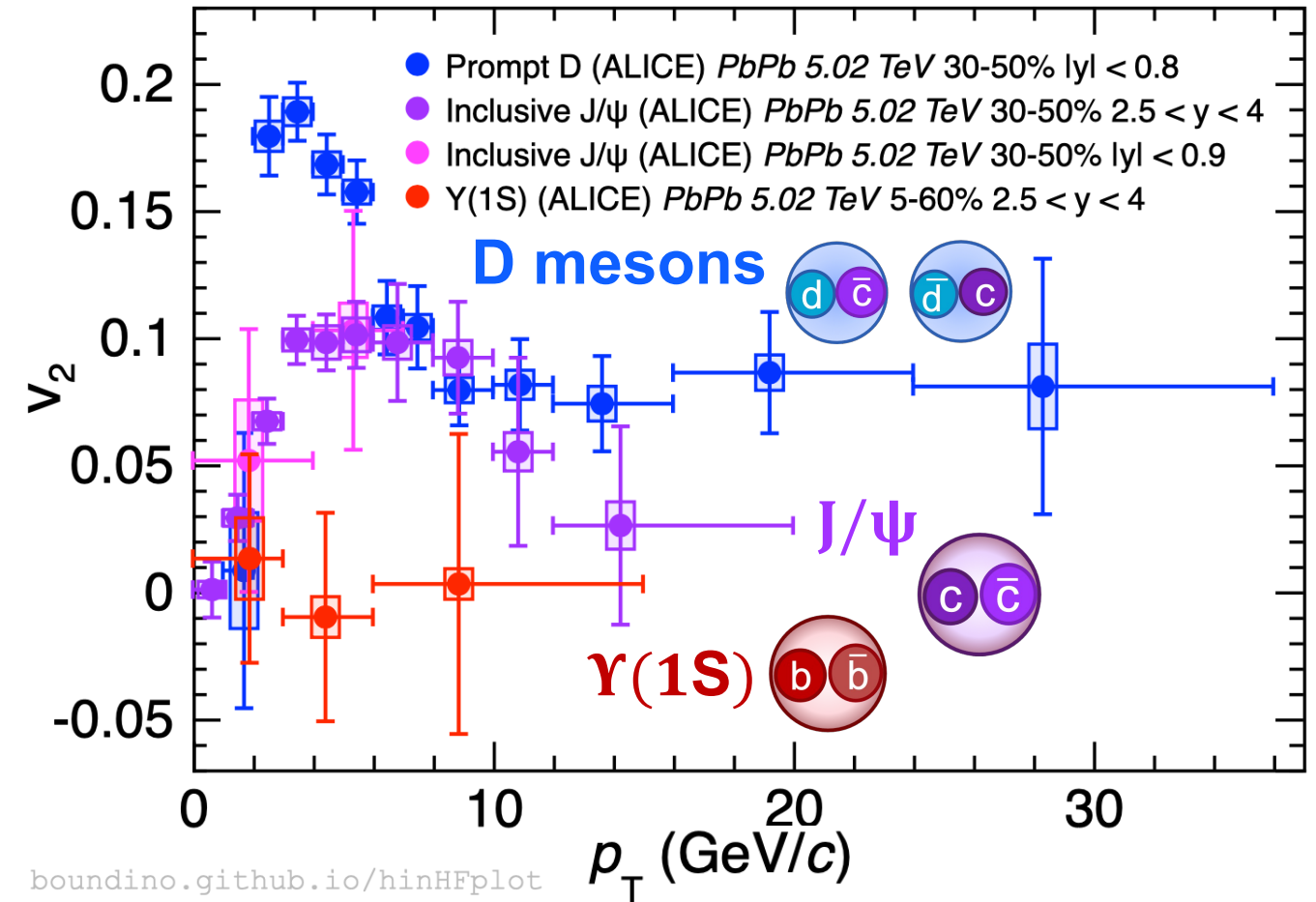


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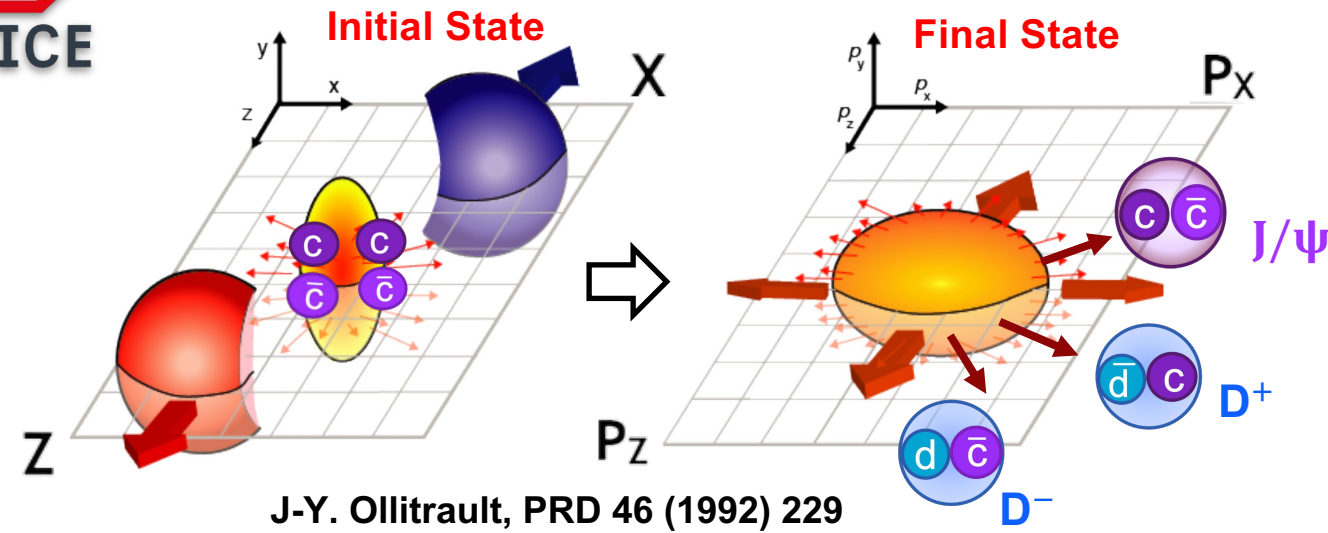
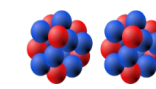
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 →  $v_2^{\Upsilon(1S)} \ll v_2^{J/\psi} < v_2^{D \text{ mesons}}$

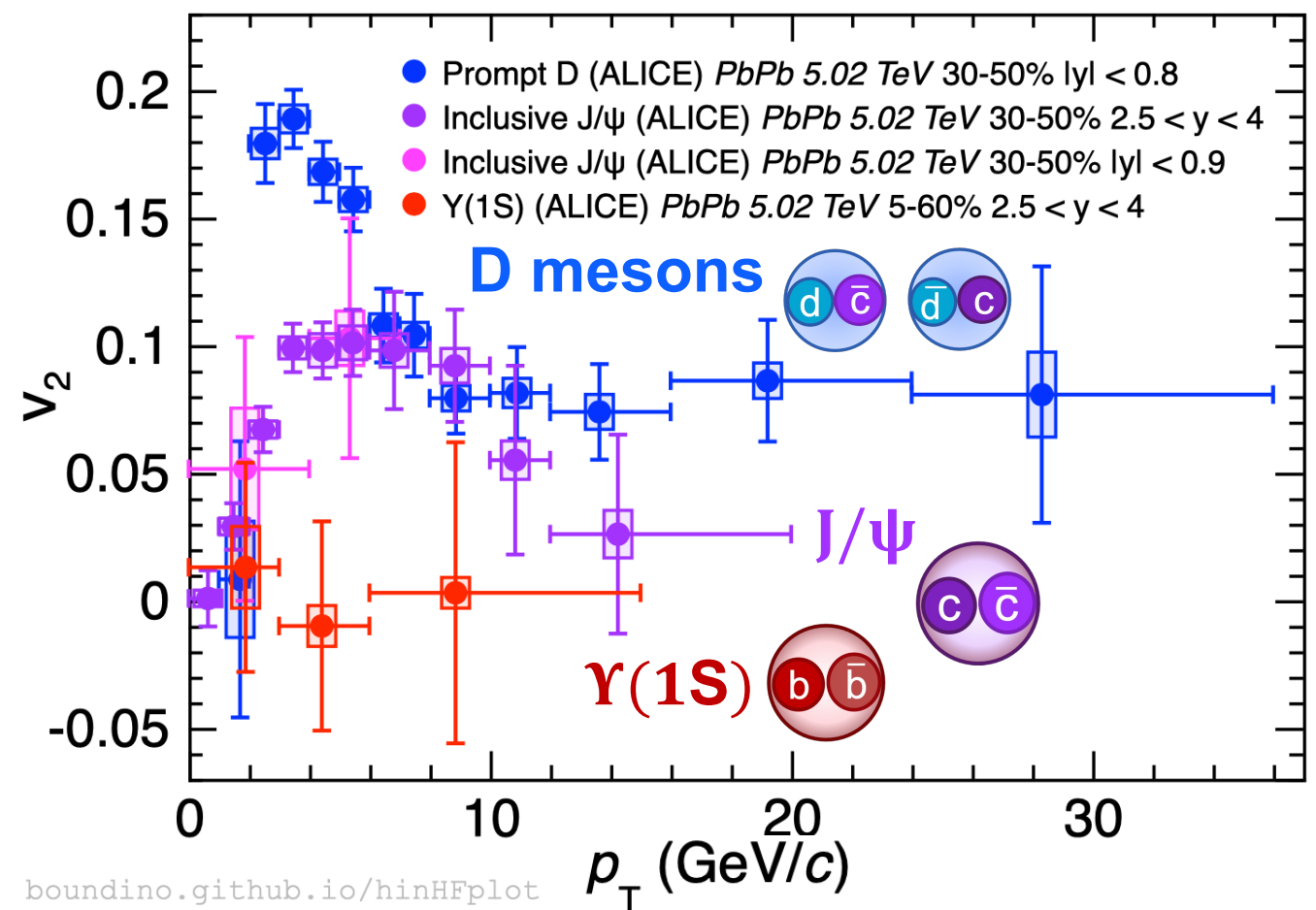
→ Charm quarks exhibit a collective behaviour!

→ What about smaller systems?

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ALICE

# ALICE detector in Run 2



→ Central barrel

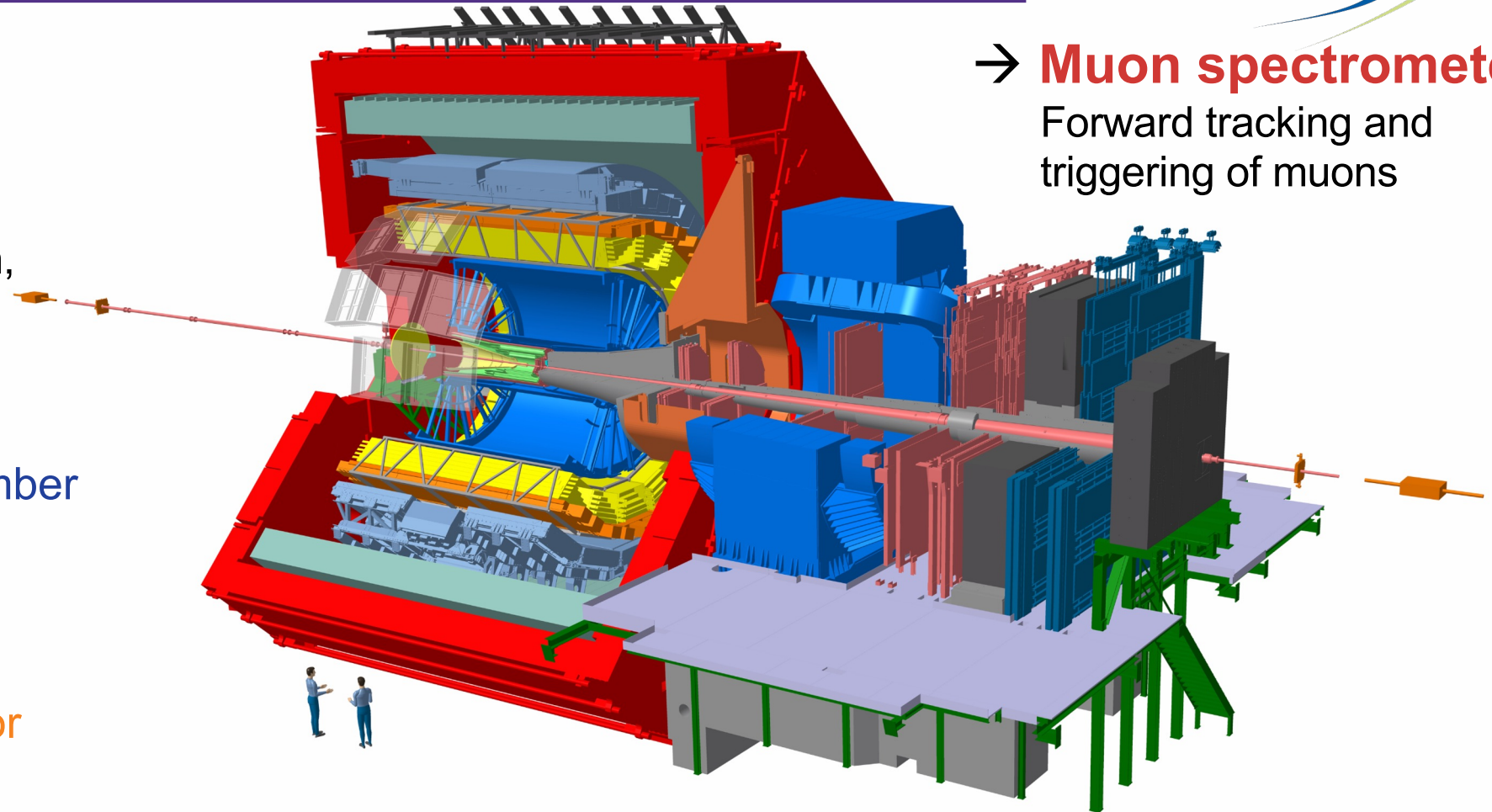
→ Muon spectrometer

Forward tracking and triggering of muons

- **ITS – Inner Tracking System**  
Tracking, vertex reconstruction, multiplicity estimation

- **TPC – Time Projection Chamber**  
PID, tracking

- **TOF – Time Of Flight detector**  
PID





ALICE

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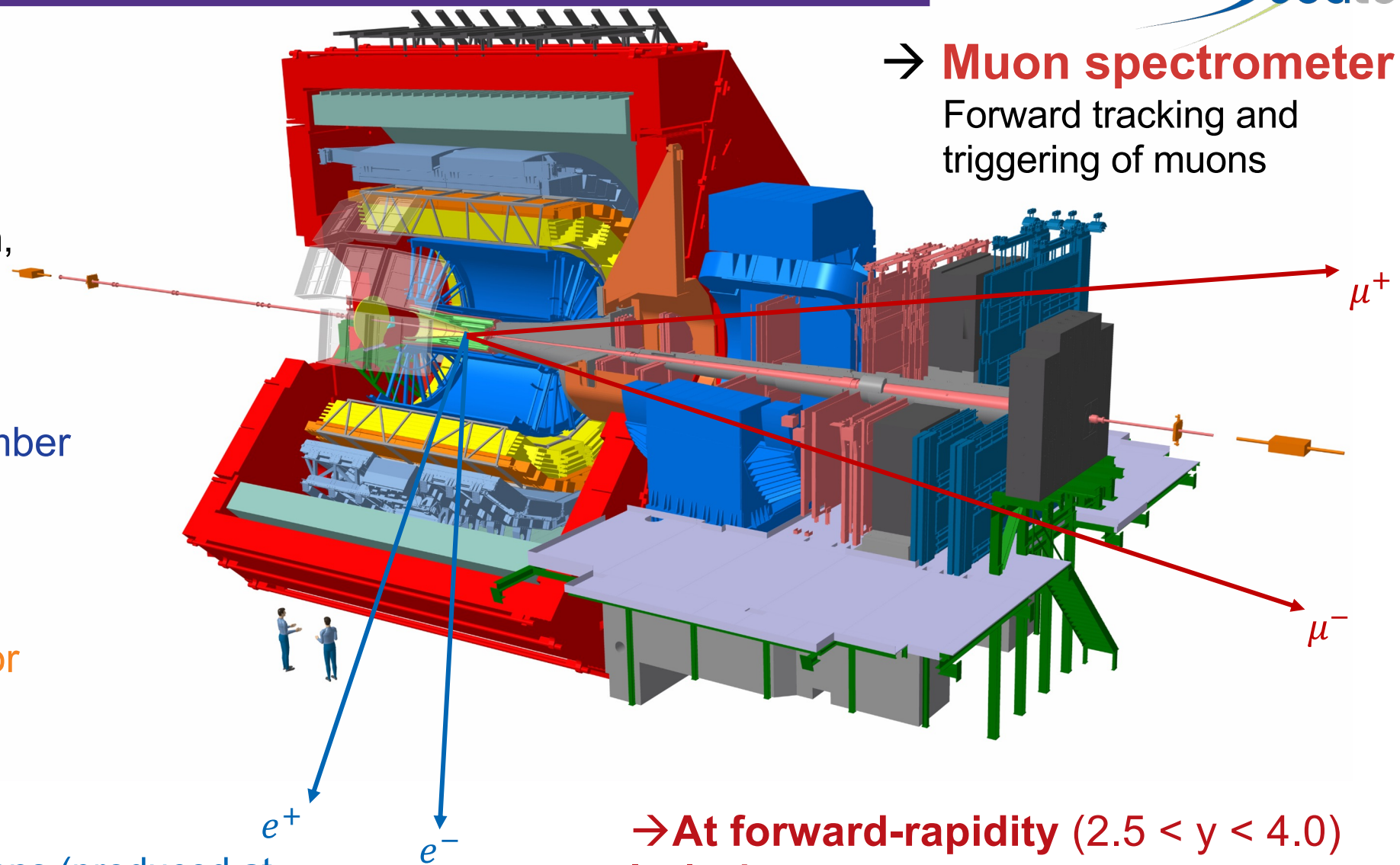


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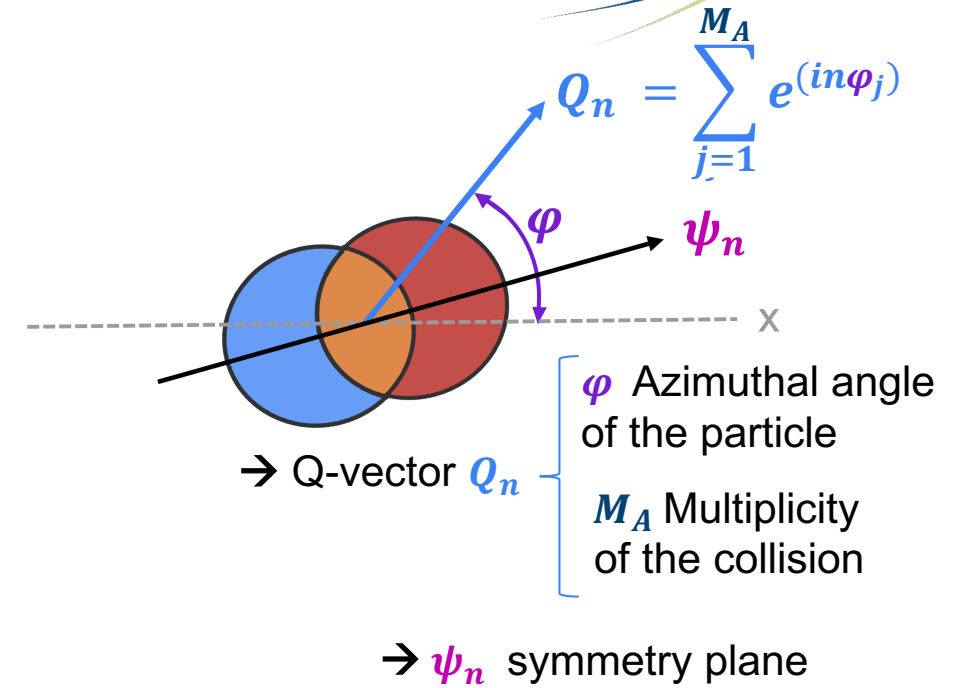
Forward tracking and triggering of muons

→ **At mid-rapidity** ( $|y| < 0.9$ )  
Distinction between **prompt** hadrons (produced at primary vertex) and **non-prompt** (b-hadron decays)

→ **At forward-rapidity** ( $2.5 < y < 4.0$ )  
**Inclusive** measurements

→ Inclusive hadrons can be **measured down to  $p_T = 0$**  (at **midrapidity** and **forward rapidity**)

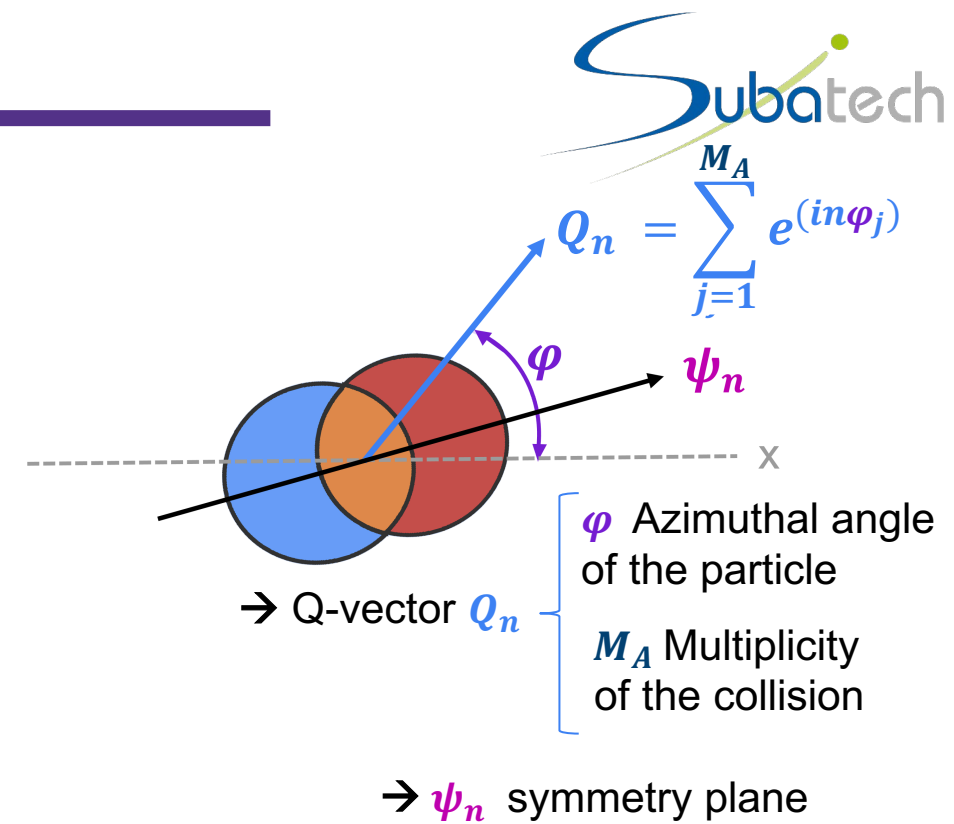
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$$v_n \{EP\} = \langle \langle \cos n(\varphi - \psi_n) \rangle \rangle / R_n^{EP}$$



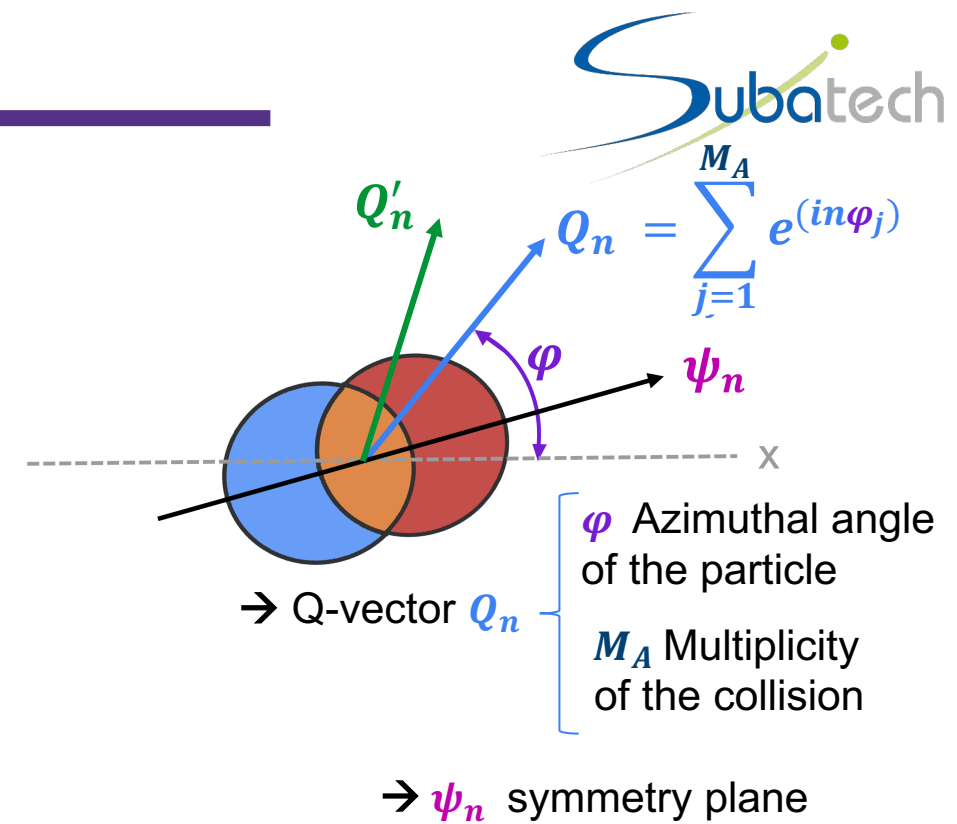
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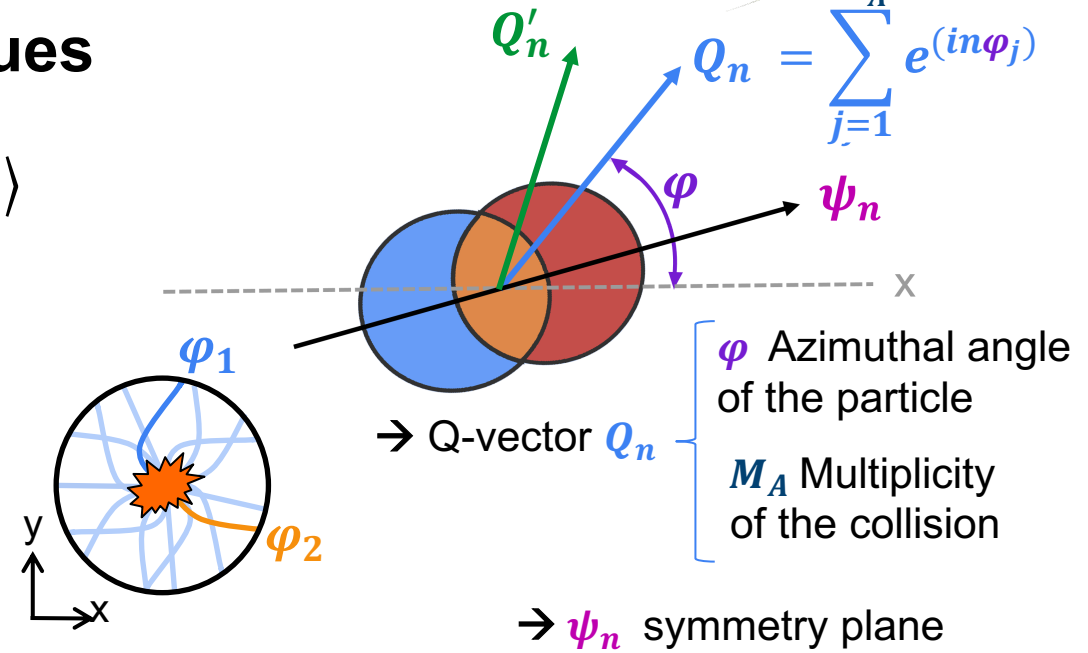
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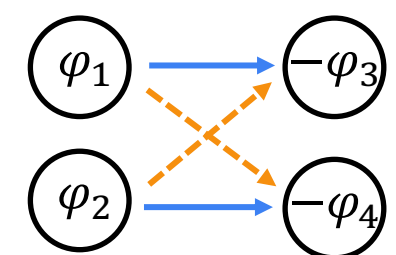
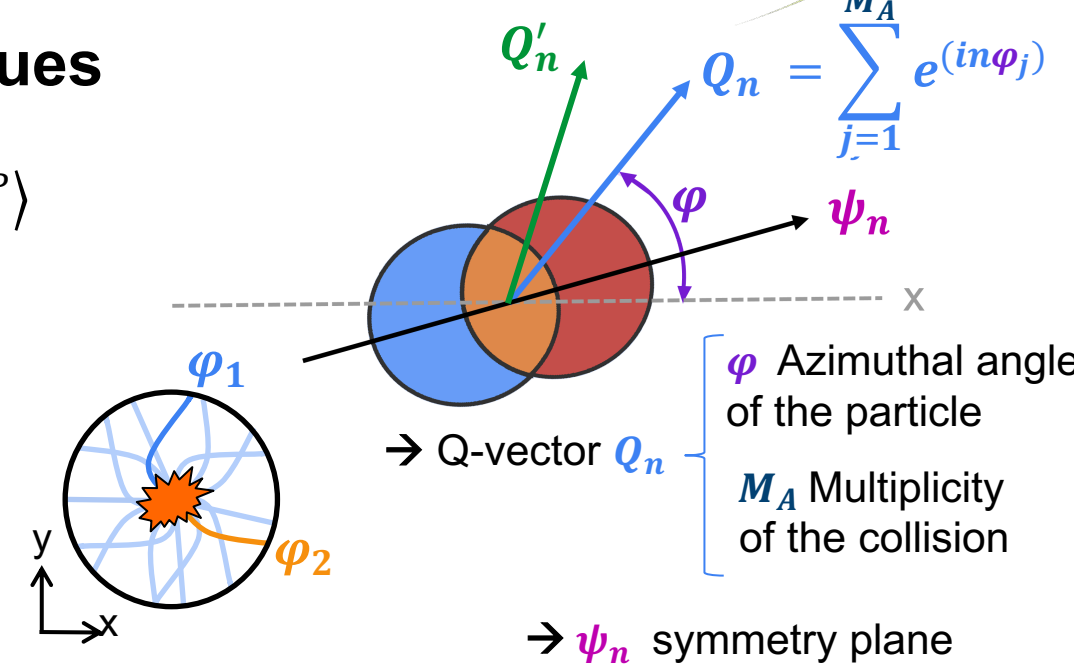
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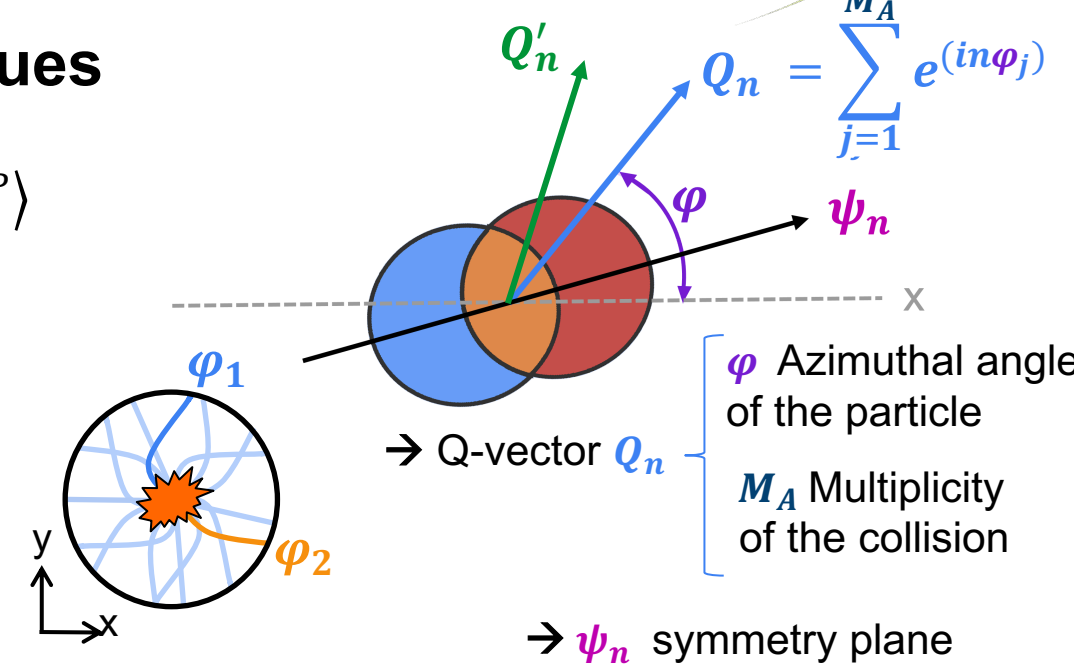
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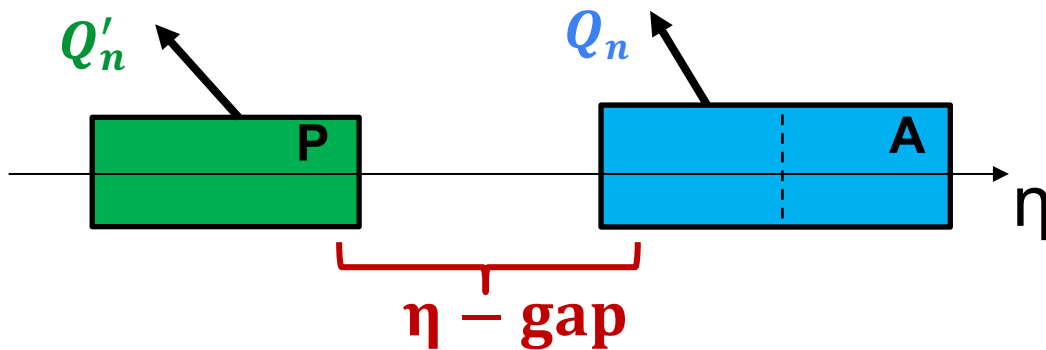
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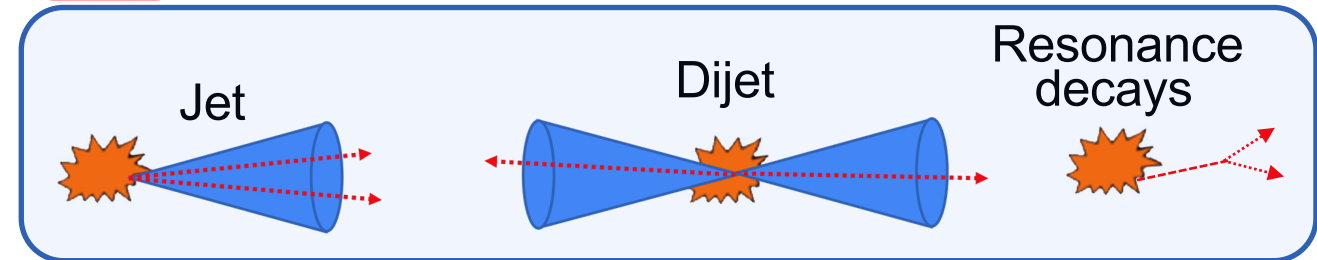
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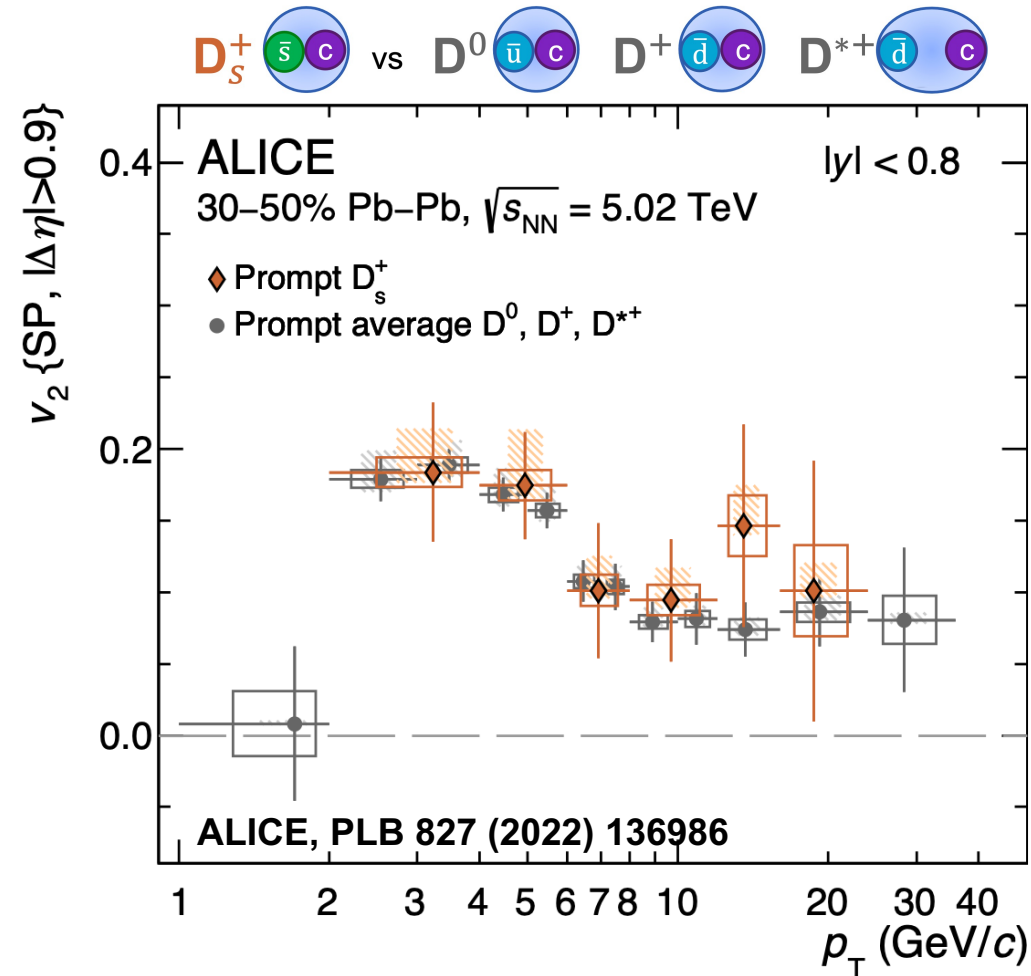
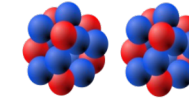
→  **$\eta$  - gap** between measured particles suppresses **non-flow effects**



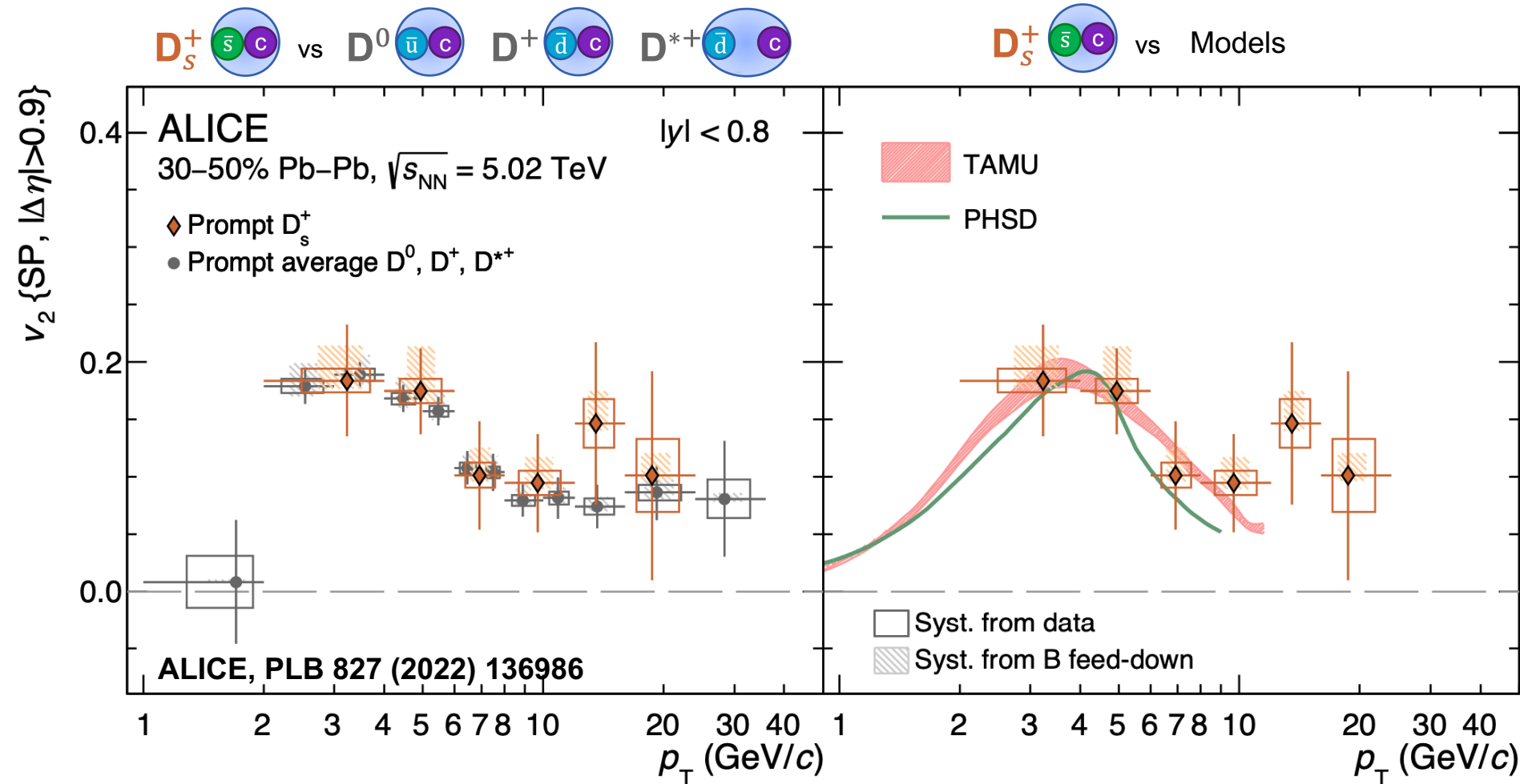
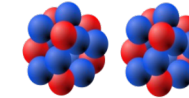
### ! Non-flow effects







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→ Theoretical **calculations** are based on the **charm–quark transport** in a **hydrodynamically expanding QGP**

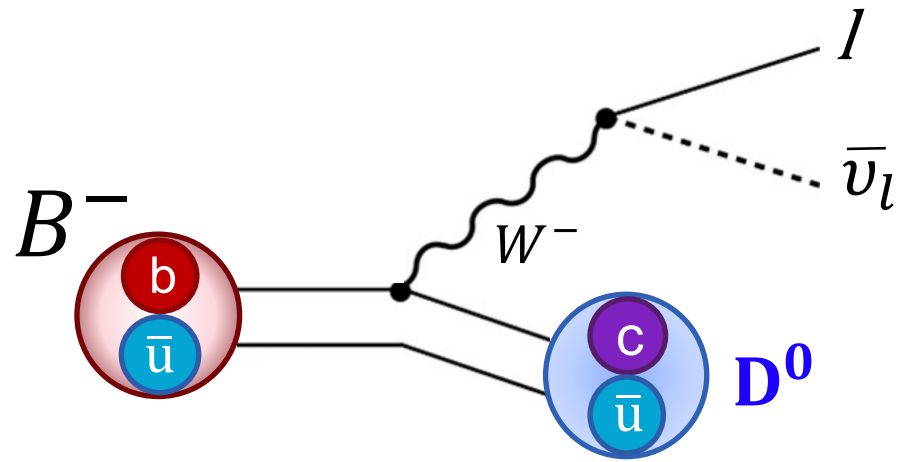
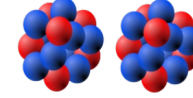
**Transport model TAMU**

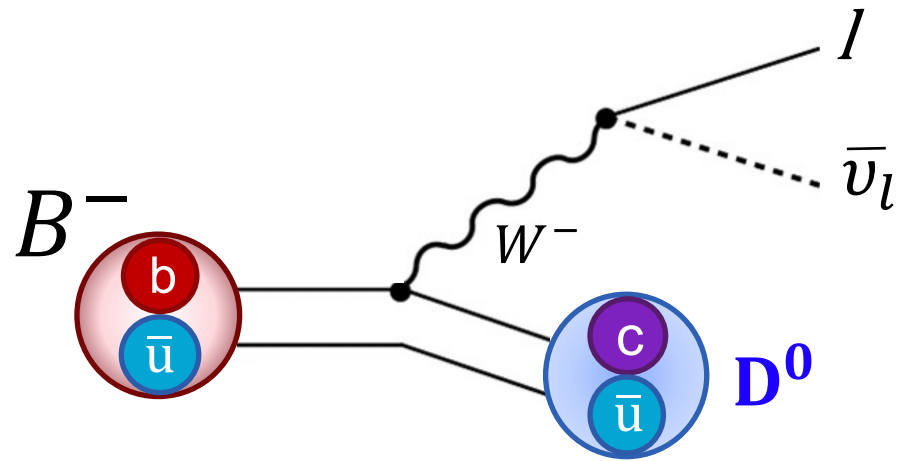
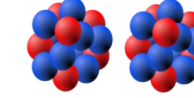
Min He and Ralf Rapp, **PRL 124 (2020) 042301**

**Parton-hadron-string dynamics (PHSD)**

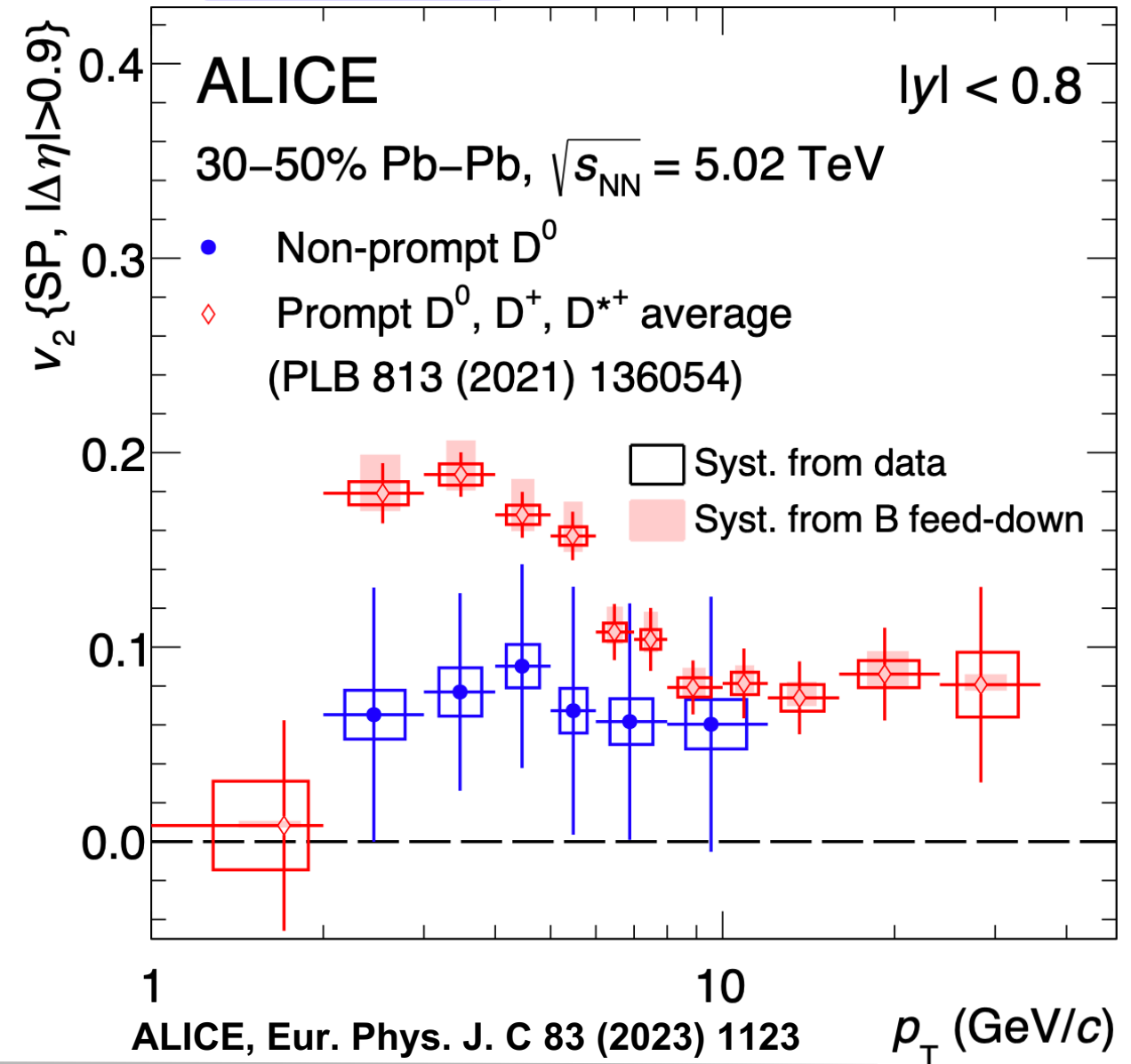
Taesoo Song et al, **PRC 92 (2015) 014910**

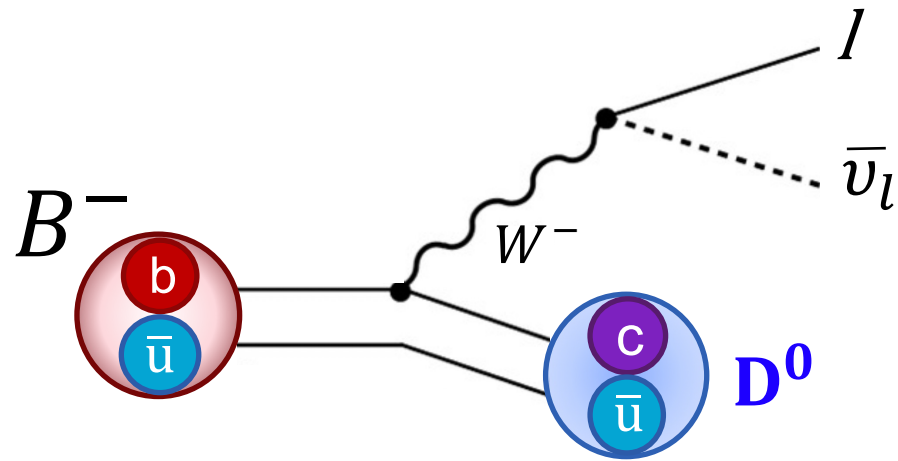
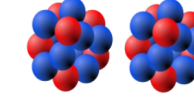
→ Possibility to **probe hadronization via coalescence**



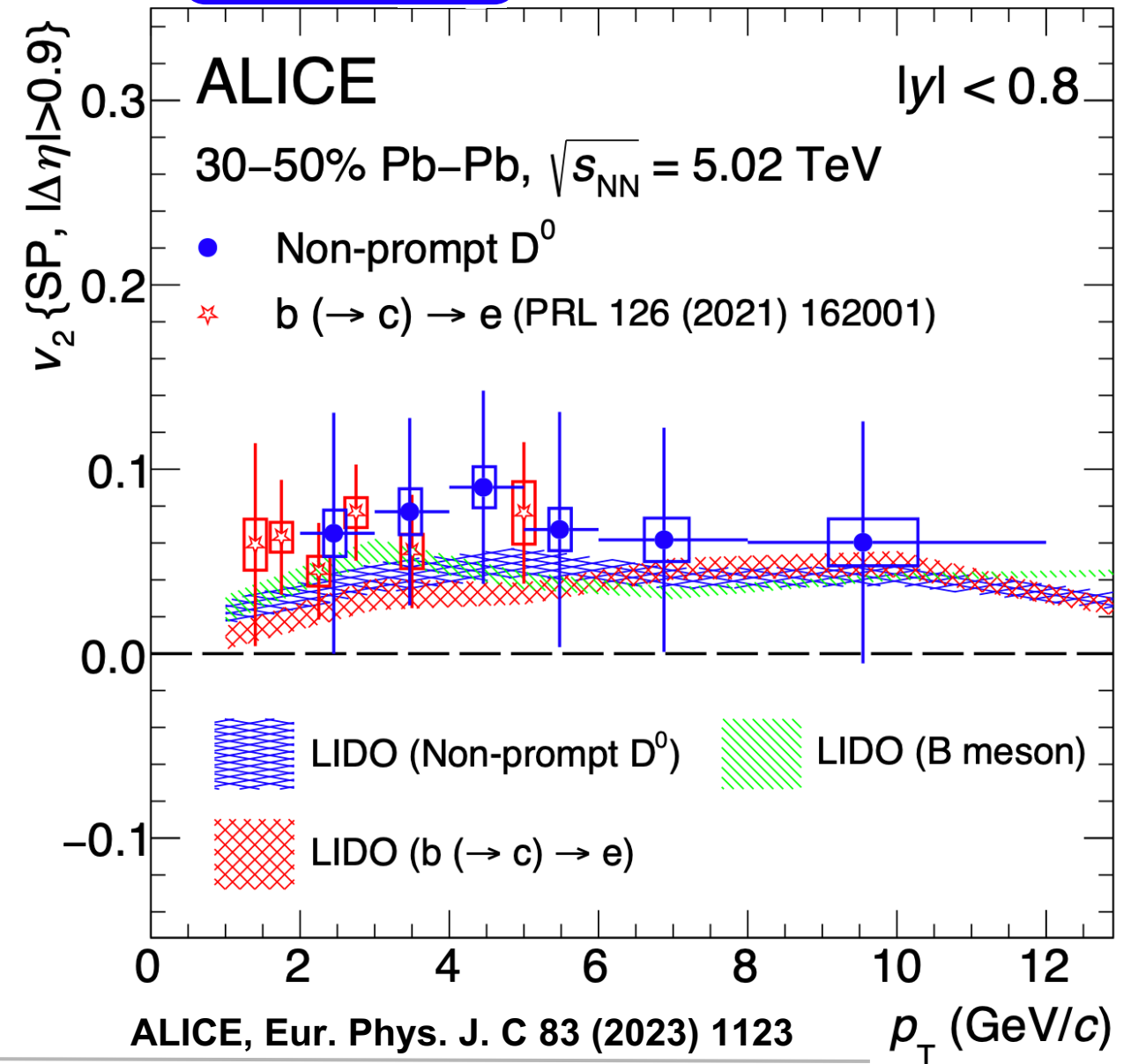


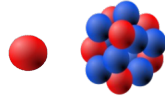
- The **non-prompt  $D^0$ -meson**  $v_2$  is found to be **positive** with a significance of  $2.7\sigma$
- **Non-prompt  $D^0$**  is **lower** by  $3.2\sigma$  than **prompt  $D$ -meson**  $v_2$  in the range  $2 < p_T < 8 \text{ GeV}/c$



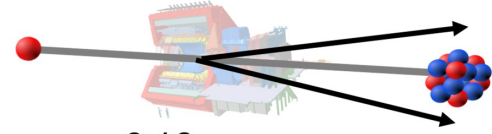


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- **Hybrid transport model LIDO** reproduces the data (Linearized Boltzmann with diffusion)  
 Weiyao Ke et al, *PRC* 98 (2018) 064901  
 Weiyao Ke et al, *PRC* 100 (2019) 064911
- **Decay kinematics doesn't seem to play** a significant role in the **beauty-hadron**  $v_2$  measurements.

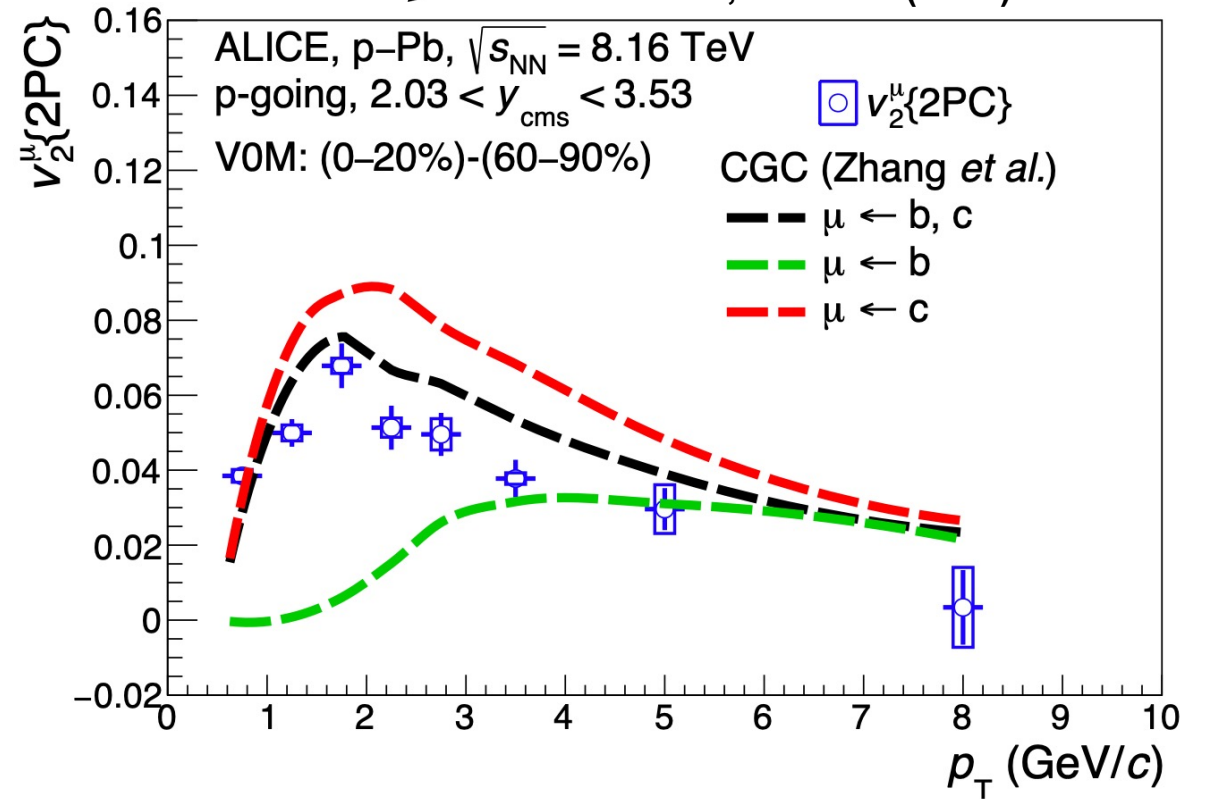
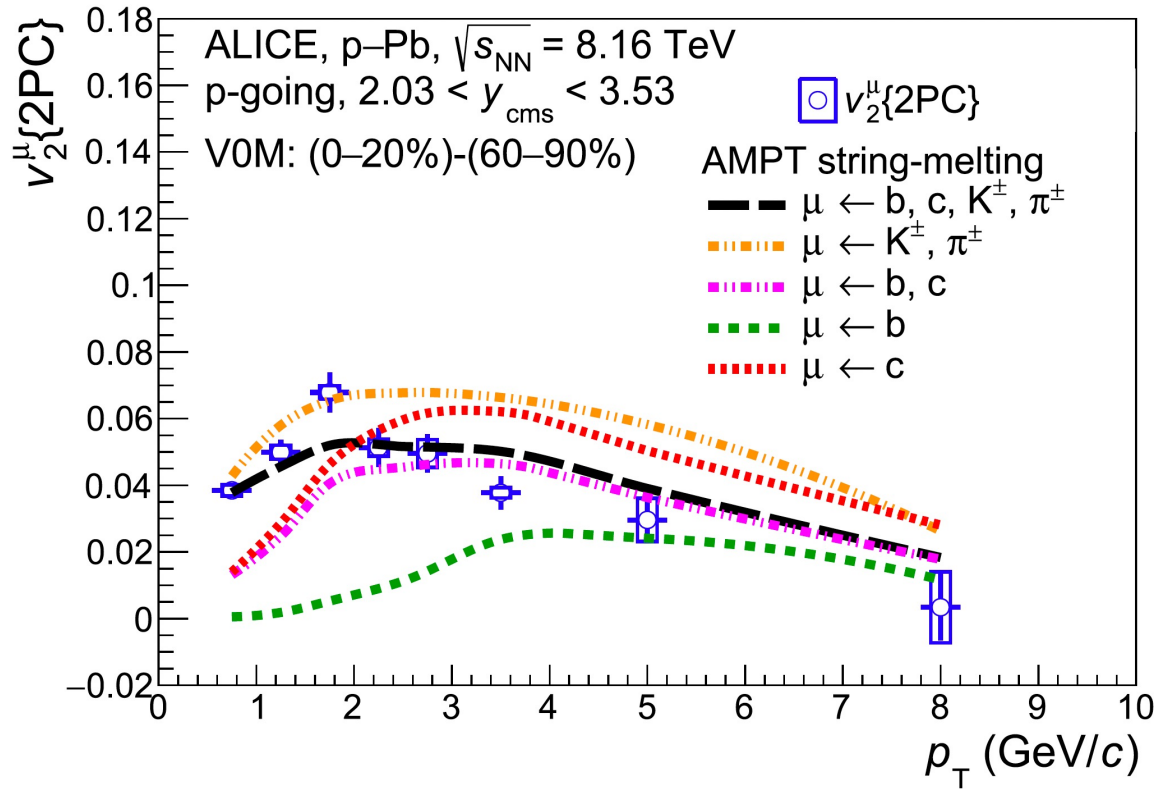




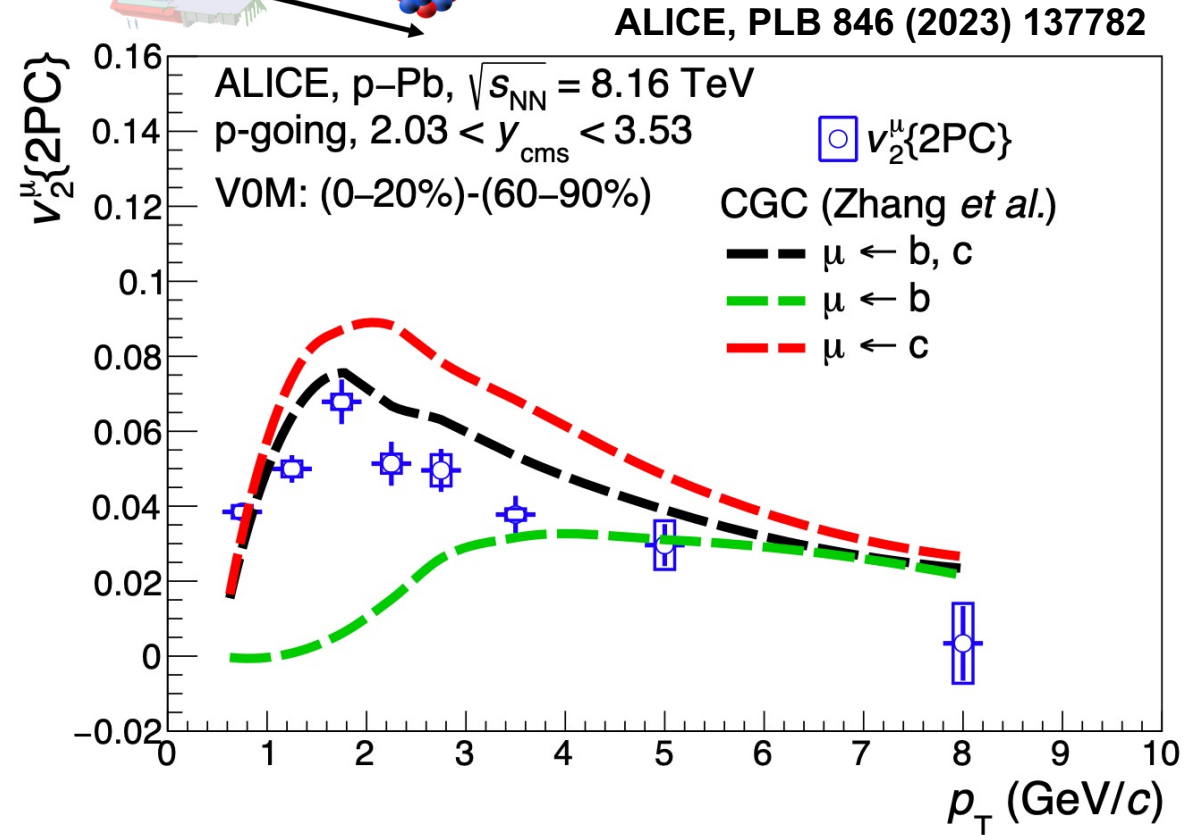
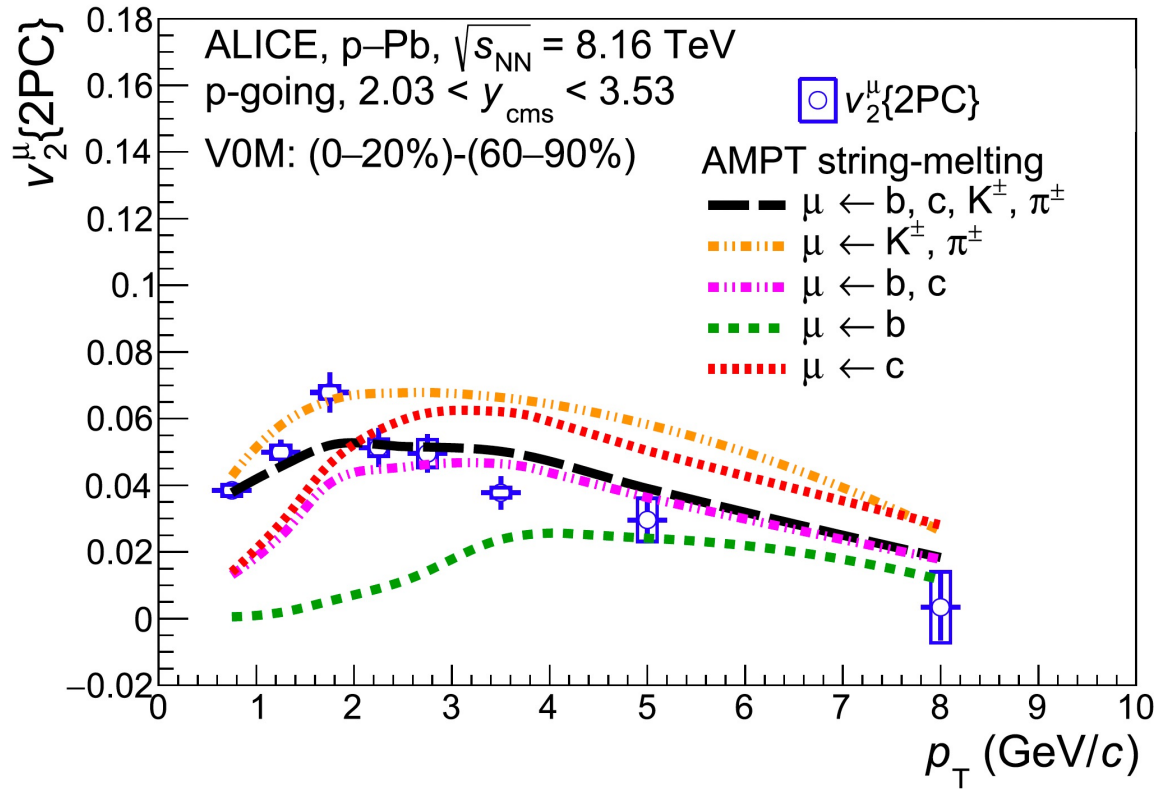
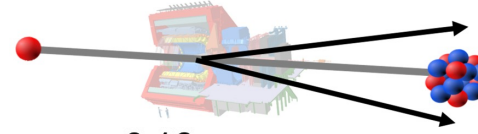
## Forward-rapidity (p-going)



ALICE, PLB 846 (2023) 137782

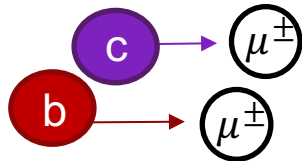


## Forward-rapidity (p-going)



• **Positive muon  $v_2$  measured for the first time over a wide  $p_T$  interval with a significance of  $4.7\sigma$  for  $2 < p_T < 6$  GeV/c**

• **HF- $\mu$  dominate for  $p_T > 2$  GeV/c**



→ **Heavy quarks flow (at mid and high  $p_T$ ) in p-Pb collisions!**

→ **AMPT (A Multi-Phase Transport model)**

Z. W. Lin, PRC 72 (2005) 064901

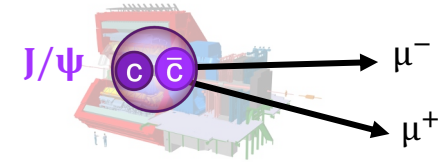
→ **CGC (Color Glass Condensate model)**

Cheng Zhang et al, PRC 122 (2019) 172302

**Models**  
reproduce the  
**data** qualitatively

- ❖ Collective behavior in **Pb–Pb collisions** 



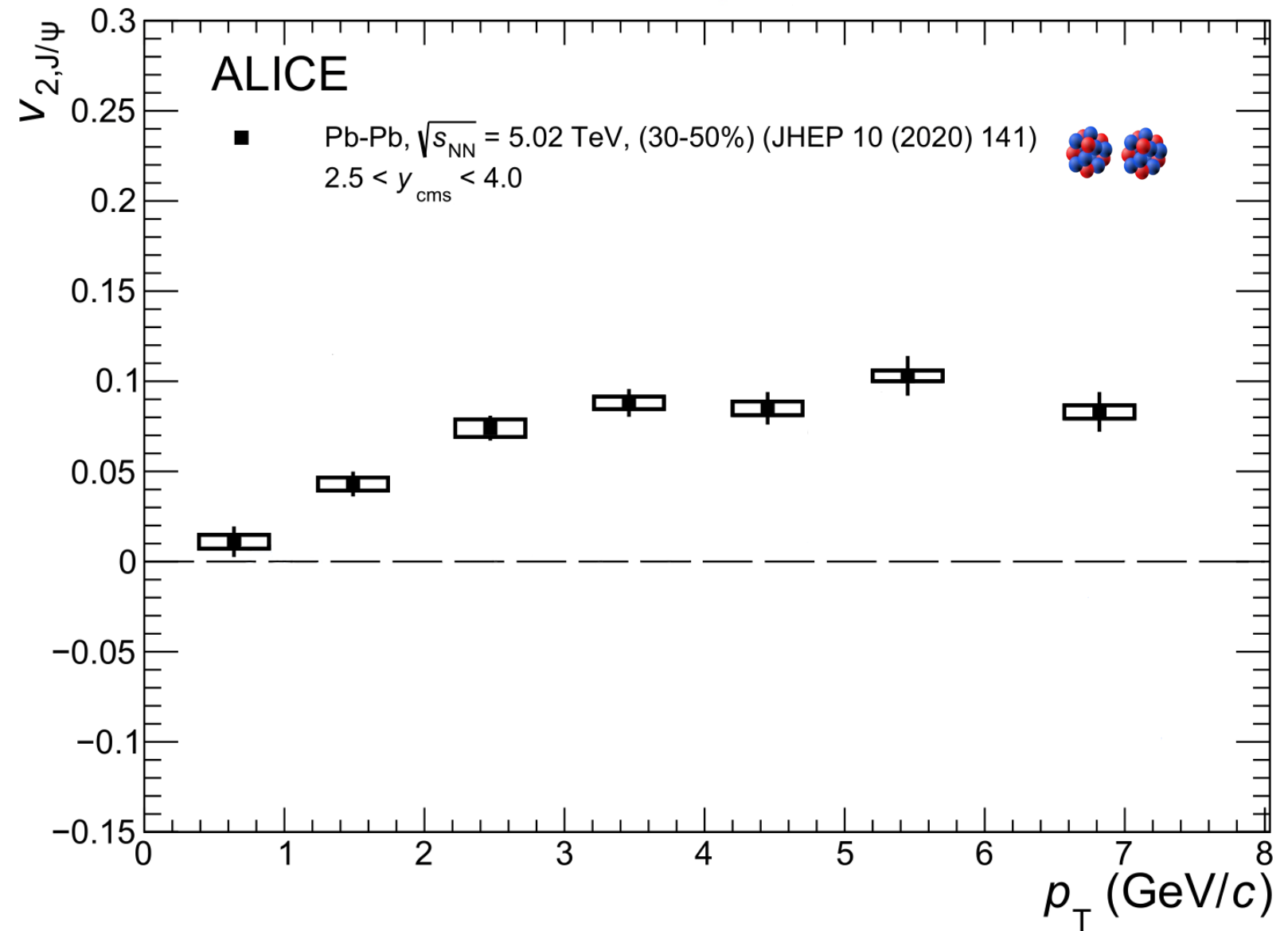


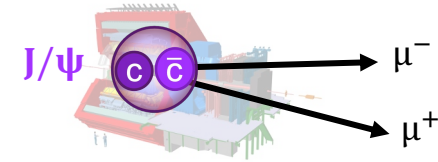
## ❖ Collective behavior in Pb–Pb collisions

### ■ Significant $J/\psi$ $v_2$ over a wide $p_T$ range

→  $J/\psi$  flow at low  $p_T$  interpreted as a consequence of regeneration

→ Result support thermalization of charm quarks in the QGP





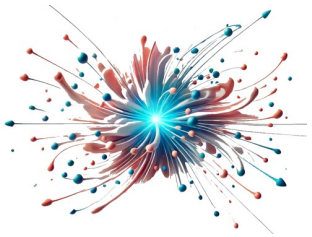
## ❖ Collective behavior in **Pb–Pb collisions**

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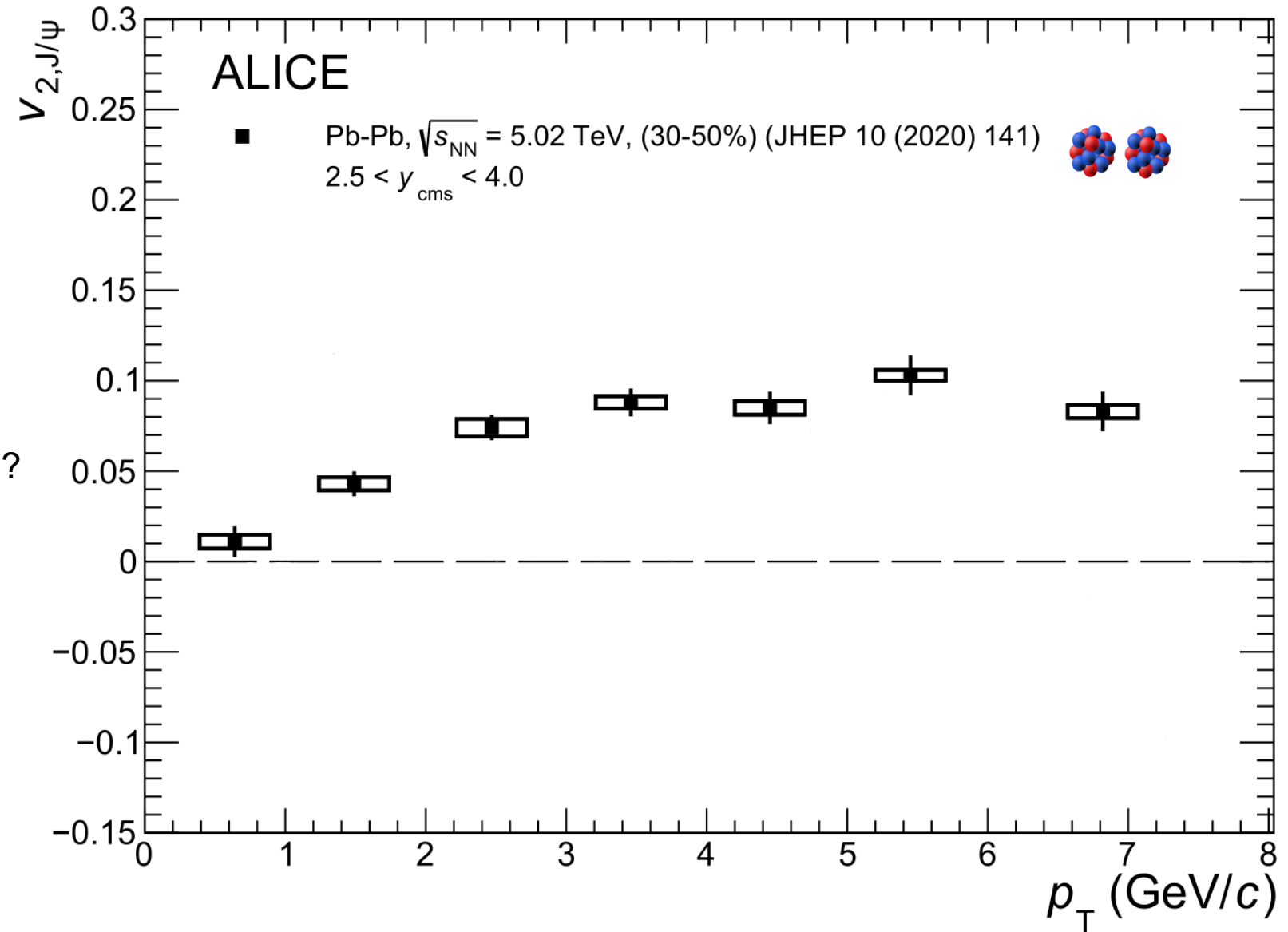
→ Result support **thermalization of charm quarks** in the **QGP**

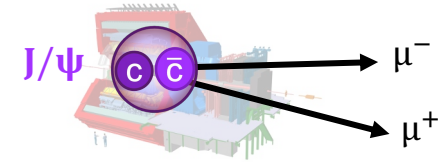
## ❖ Collective behavior in **small systems**?



→ **Initial state dynamics effects?**

→ **QGP in small systems?**





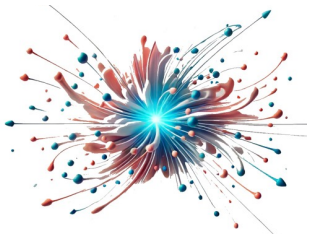
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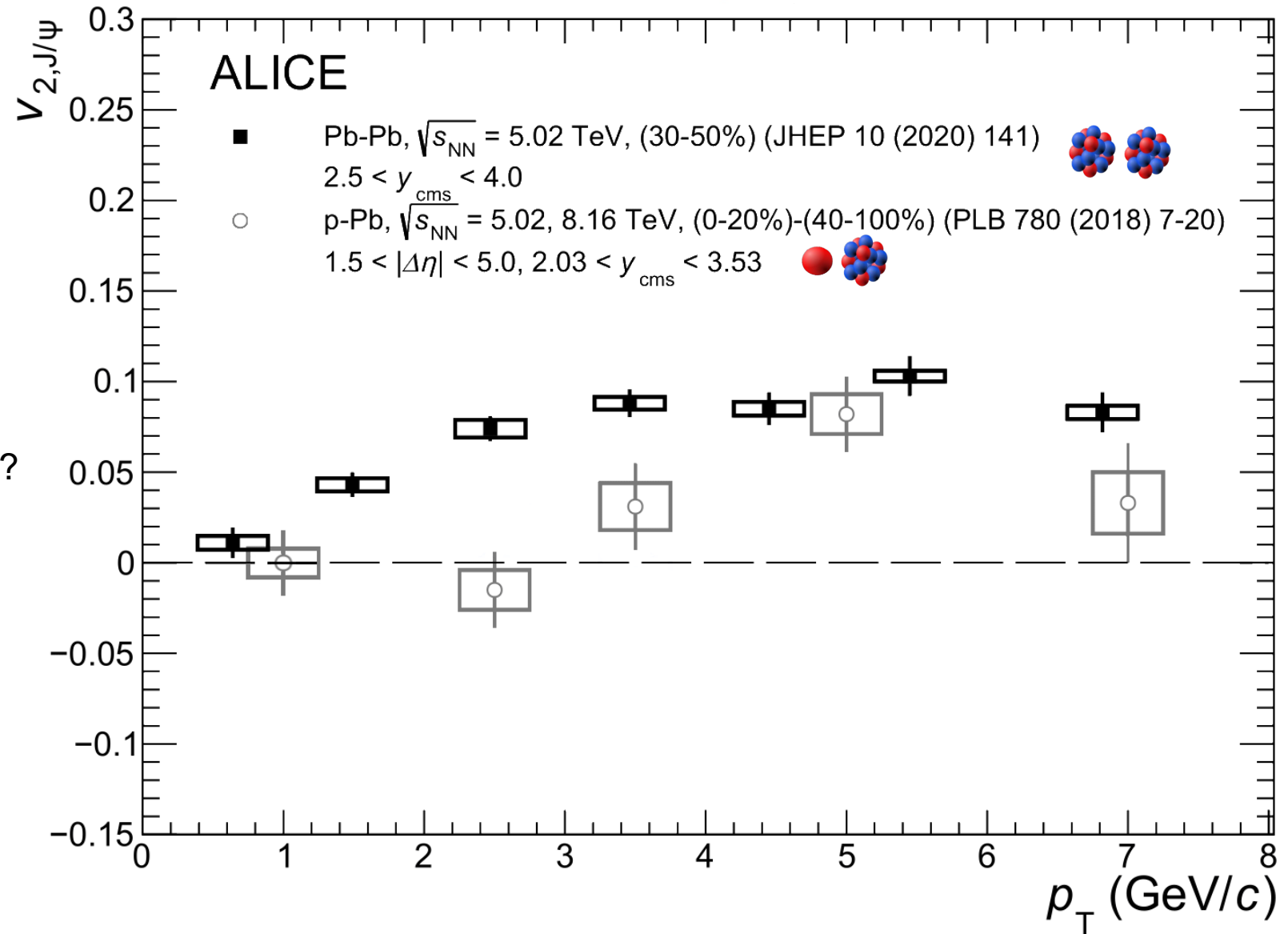
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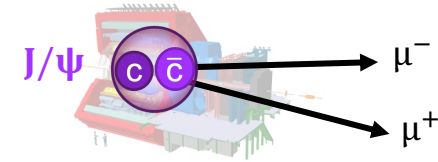


→ Initial state dynamics effects?

→ QGP in small systems?

○ Non-negligible  $J/\psi$   $v_2$  at high  $p_T$  in p–Pb collisions





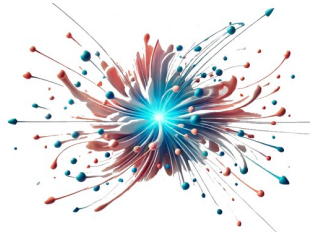
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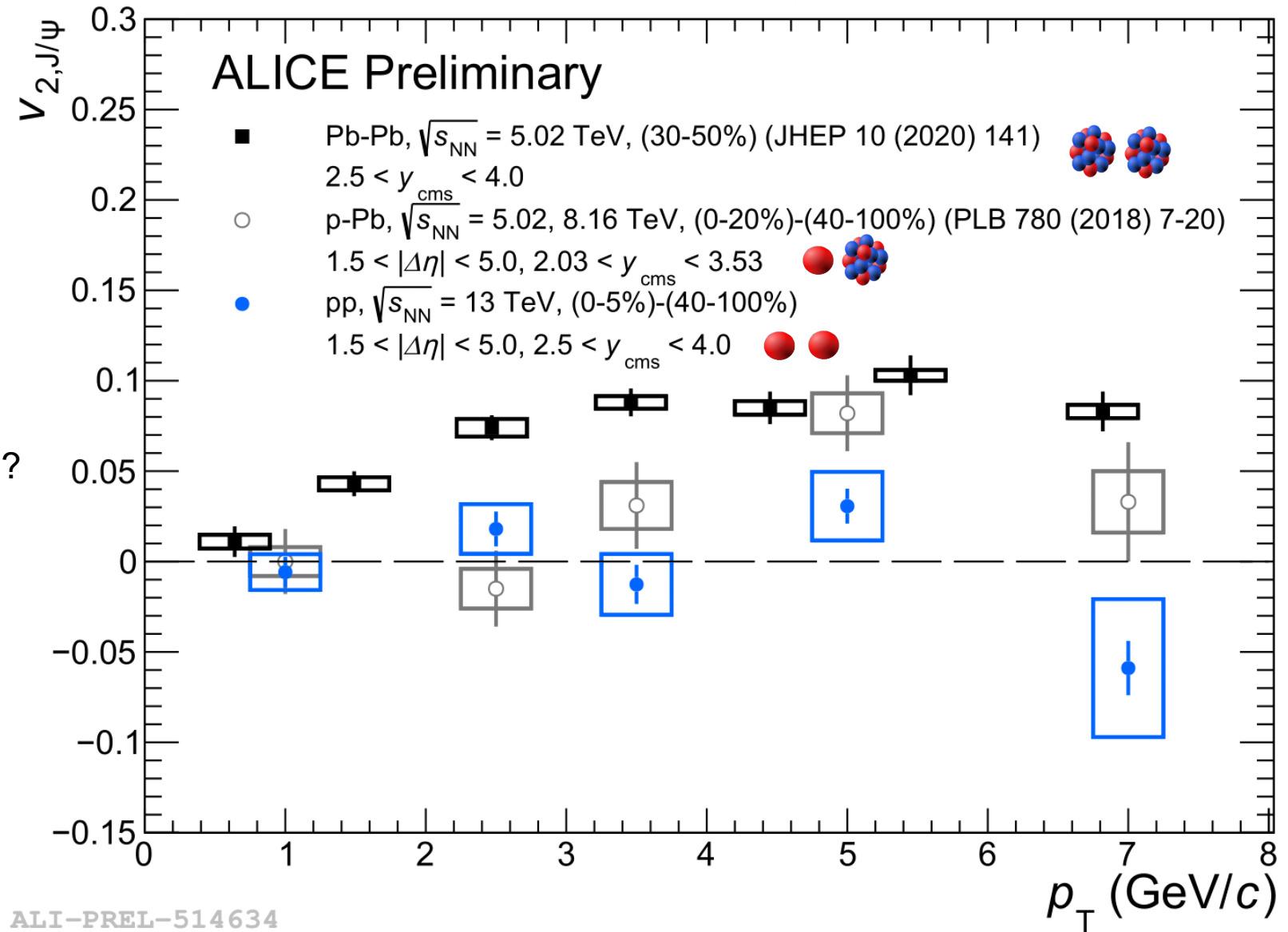
→ Initial state dynamics effects?

→ QGP in small systems?

○ Non-negligible  $J/\psi$   $v_2$  at high  $p_T$  in p–Pb collisions

●  $J/\psi$   $v_2$  compatible with 0 (within uncertainties) in pp collisions

$$v_2^{pp} \ll v_2^{p-Pb} \leq v_2^{Pb-Pb}$$



ALI-PREL-514634

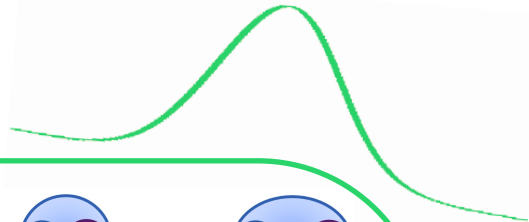
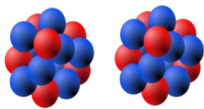


ALICE

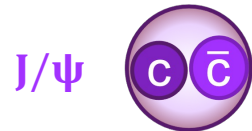
# $v_2$ from large to small systems in Run 2



Pb–Pb



- All prompt D meson flow similarly!

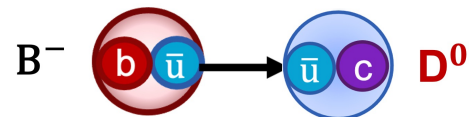


- Significant  $J/\psi$   $v_2$  is observed (Regeneration at low  $p_T$ )

→ Results support the charm quark thermalization scenario in QGP.



- Elliptic flow of  $\Upsilon(1S)$  compatible with zero.



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→ Transport models describe the measurement within uncertainties.

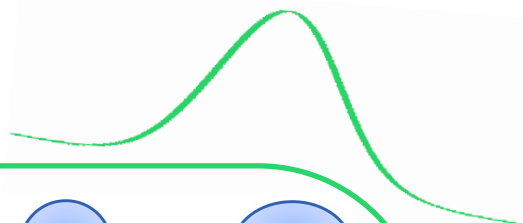
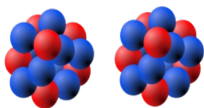


ALICE

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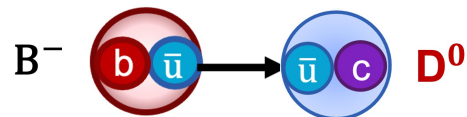


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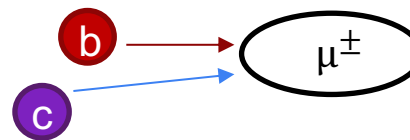
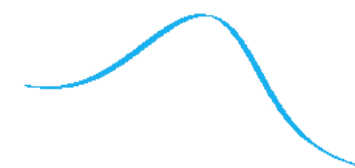
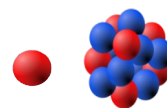
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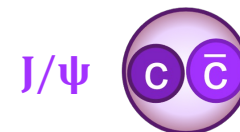
- Non-prompt  $D_0$  –meson  $v_2$  is positive.

→ Transport models describe the measurement within uncertainties.

p–Pb



- Heavy quarks flow significantly across a wide  $p_T$  range.



- $J/\psi$   $v_2$  is consistent with zero at low  $p_T$ .

- Similar magnitude as Pb–Pb at high  $p_T$ .

→ Imply charm quark flows at high  $p_T$ .

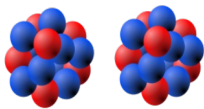


ALICE

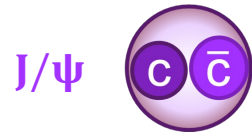
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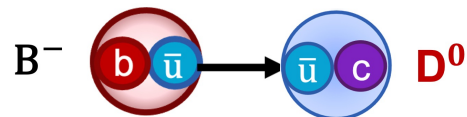


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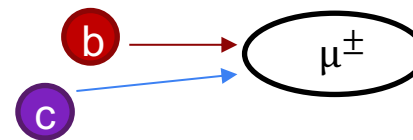
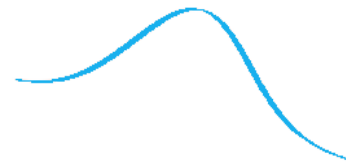
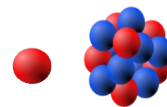
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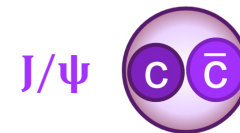
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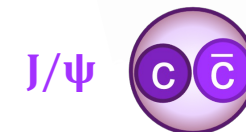
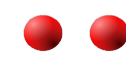


- $J/\psi$   $v_2$  is consistent with zero at low  $p_T$ .

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pp



- $J/\psi$   $v_2$  in pp collisions compatible with 0 within uncertainties.

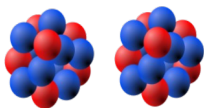


ALICE

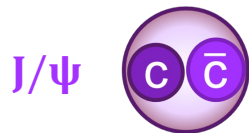
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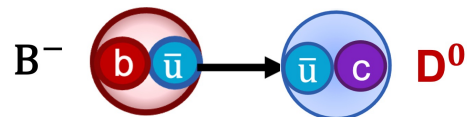


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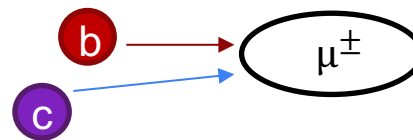
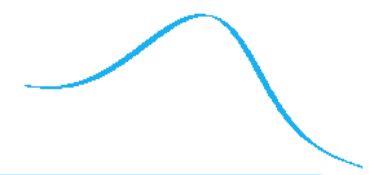
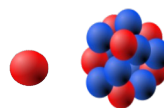
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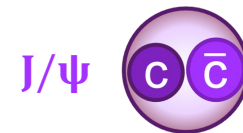
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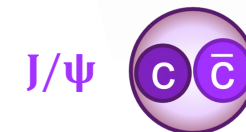
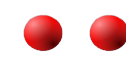


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pp



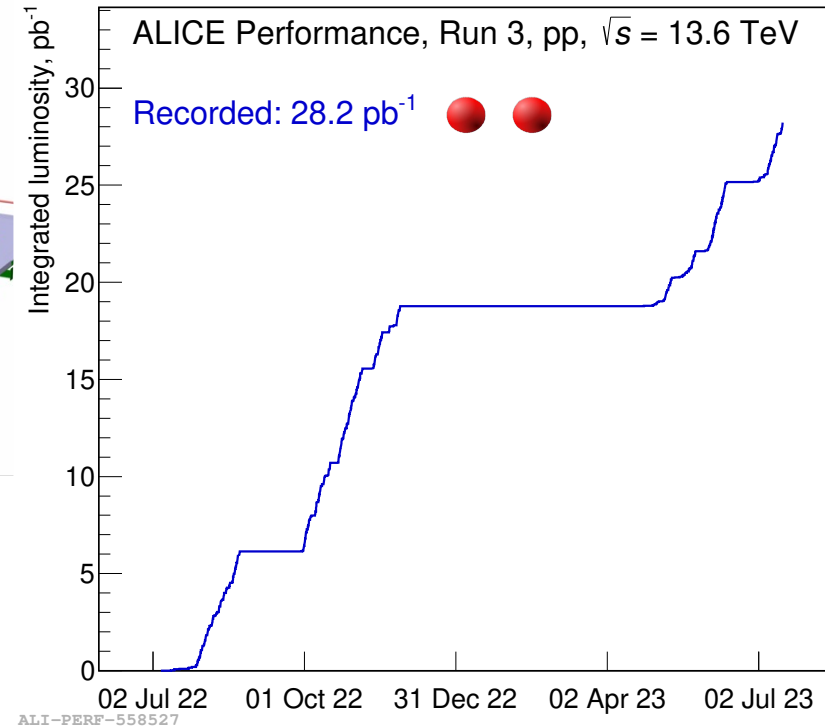
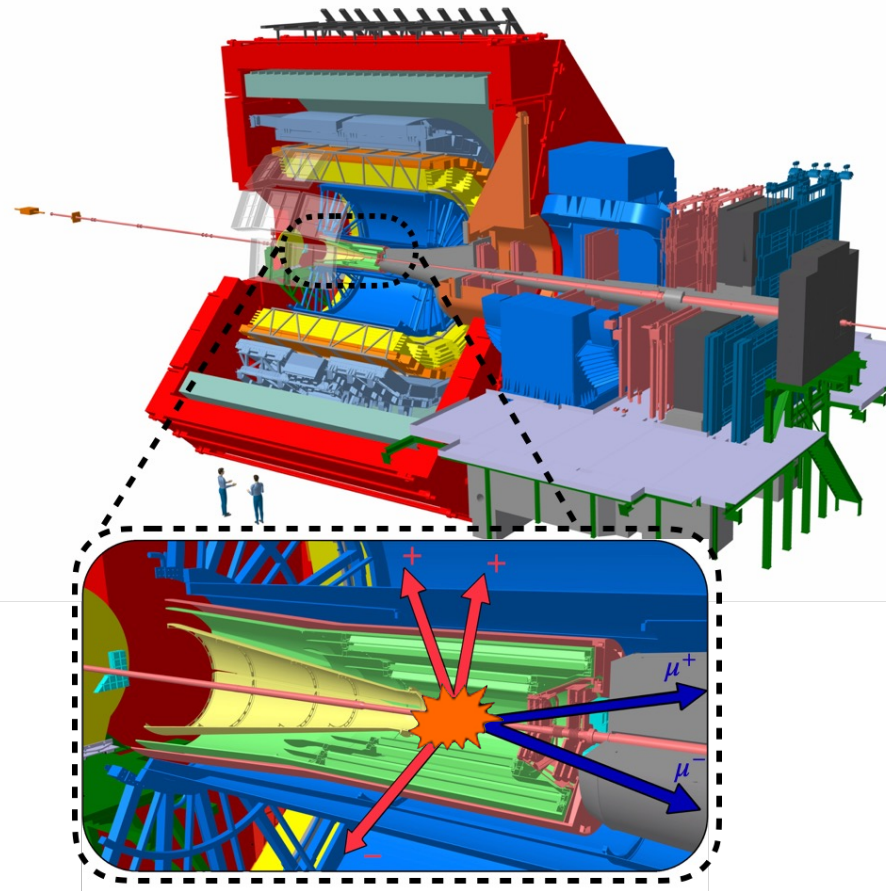
- $J/\psi$   $v_2$  in pp collisions compatible with 0 within uncertainties.

$$v_2^{\text{Pb–Pb}} \geq v_2^{\text{p–Pb}} \gg v_2^{\text{pp}}$$

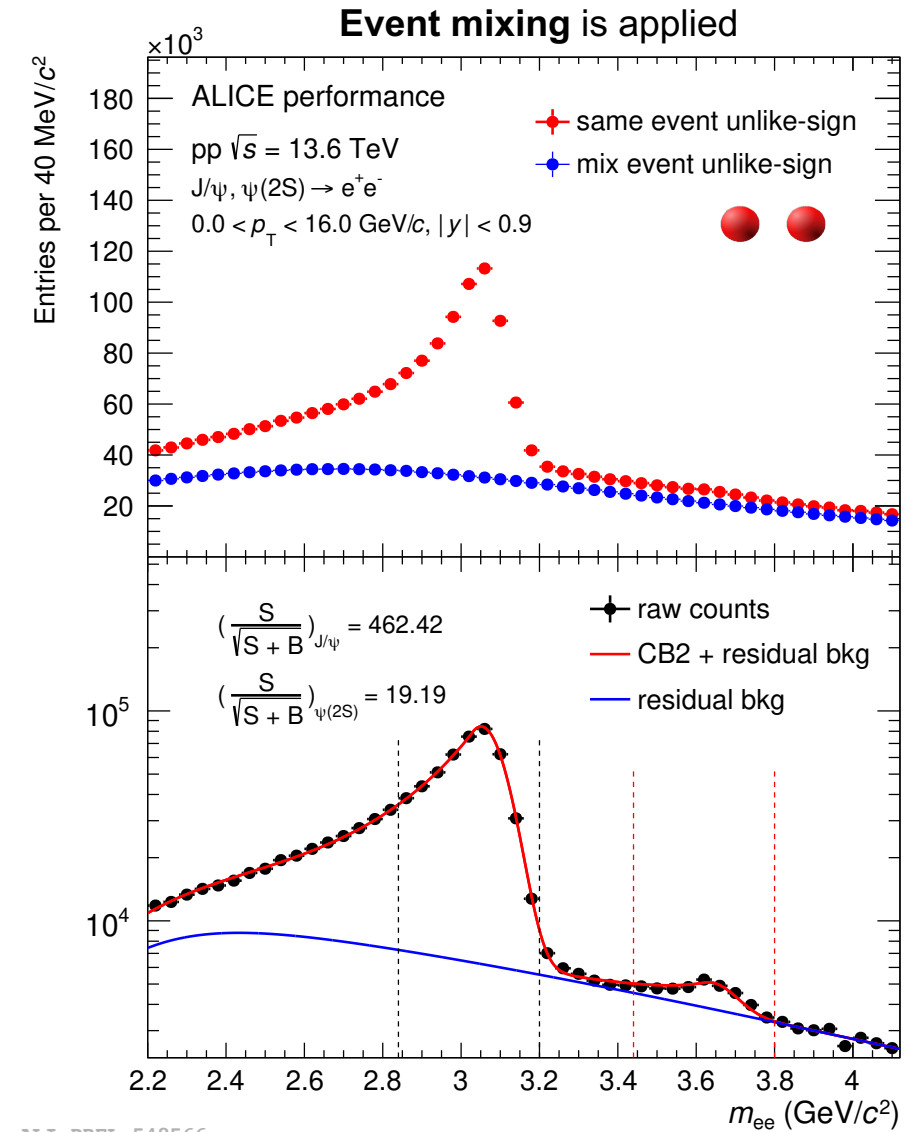
Elliptic flow hierarchy across collision systems!



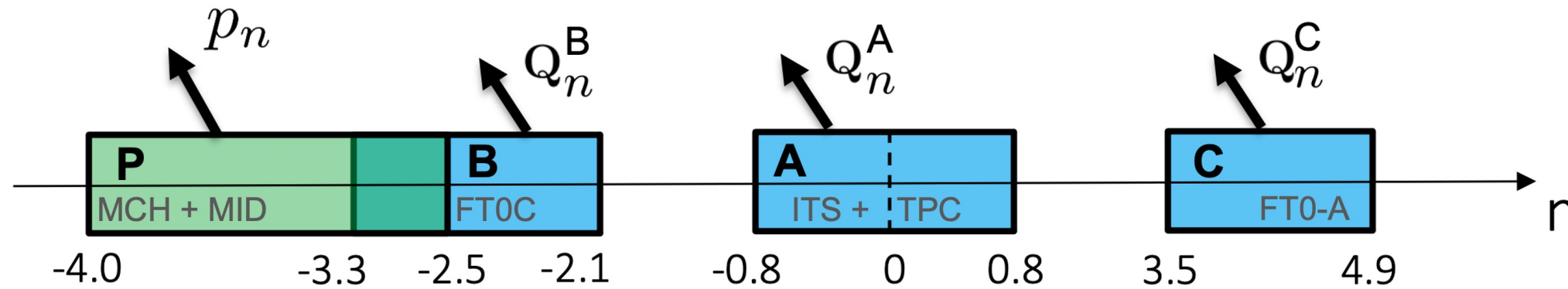
→ Run 3 statistics significantly larger than in Run 1–2 allowing more precise measurements!



→ Fit of  $m_{ee}$  distribution at mid-rapidity!



First  $J/\psi$  signal extraction in pp



Barrel Q-vector  $\rightarrow Q_n = \sum_{i=1}^M e^{(in\phi_i)} = Q_n^X + iQ_n^Y$

Symmetry plane  $\rightarrow \Psi_n = \frac{1}{n} \arctan\left(-\frac{Q_n^Y}{Q_n^X}\right)$

**Scalar product**

$$v_n^{\mu\mu} = \left\langle \frac{\langle p_n Q_n^{*A} \rangle}{R_n} \right\rangle = \sqrt{\langle v_n^2 \rangle}$$

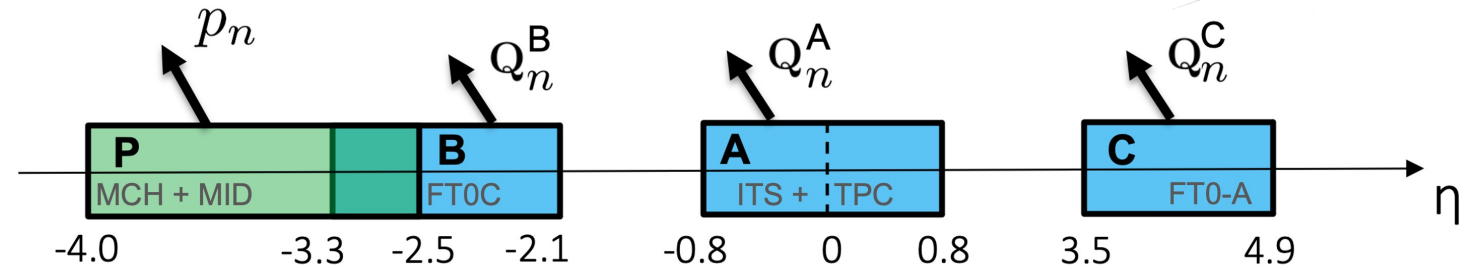
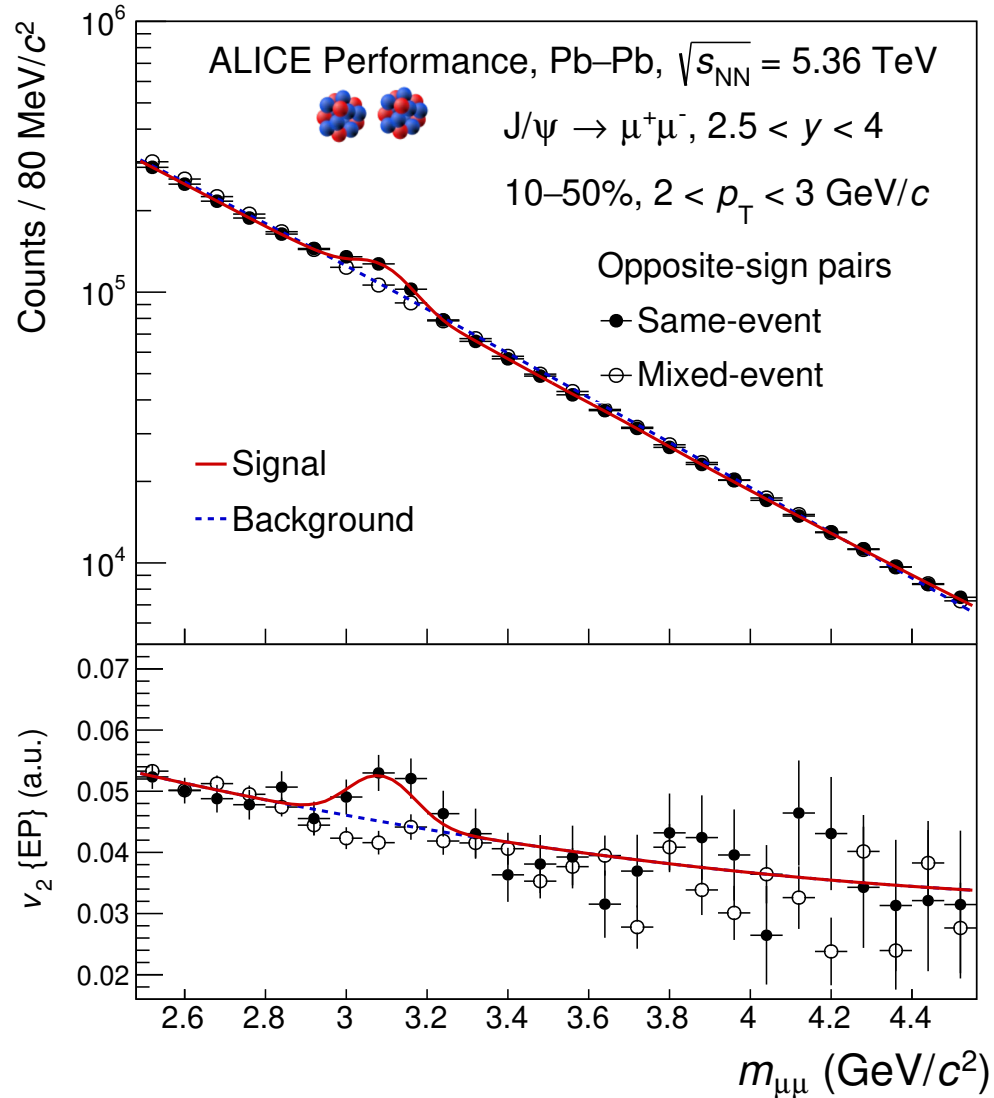
$$R_n = \sqrt{\frac{\langle Q_n^A Q_n^{*B} \rangle \langle Q_n^A Q_n^{*C} \rangle}{\langle Q_n^B Q_n^{*C} \rangle}}$$

**Event plane**

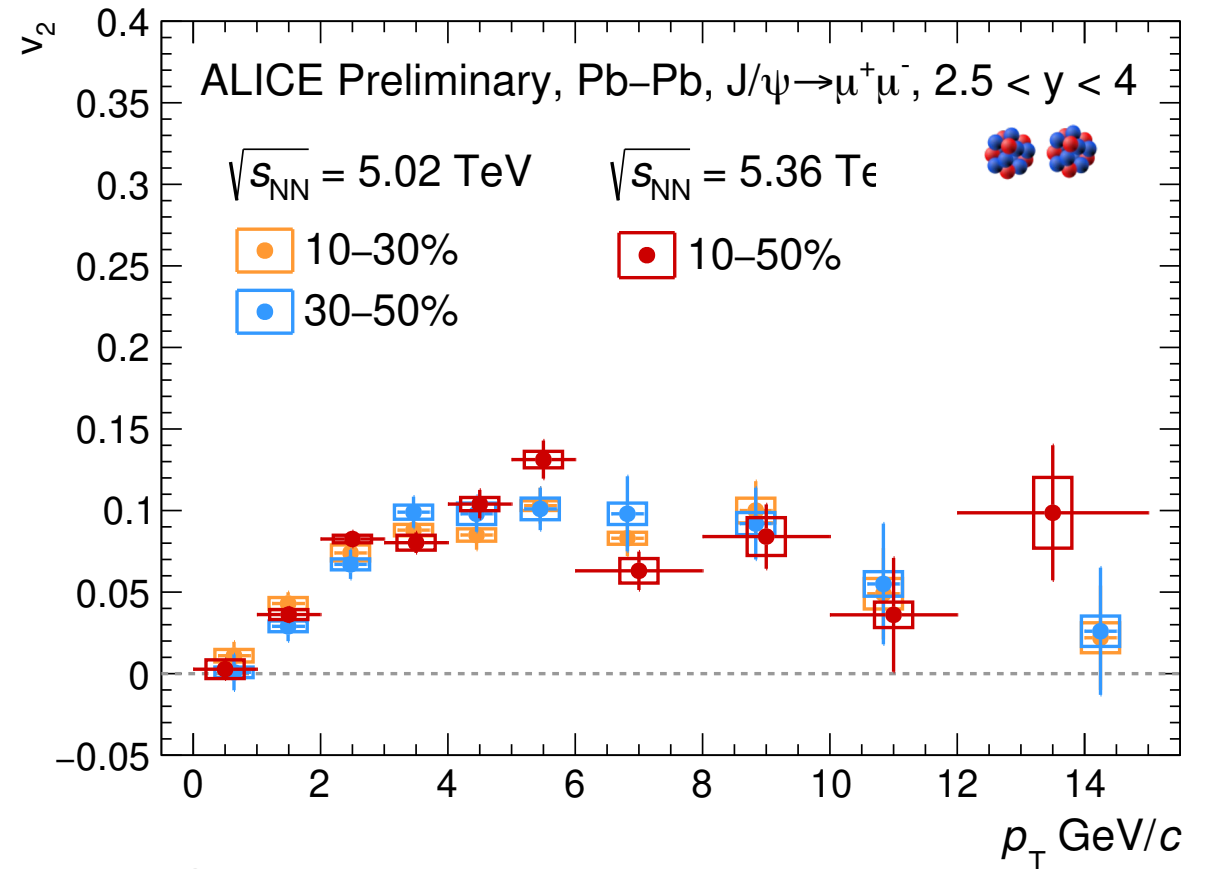
$$v_n^{\mu\mu} = \left\langle \frac{\langle \cos n(\varphi - \Psi_n^A) \rangle}{R_n} \right\rangle = \sqrt{\langle v_n^2 \rangle}$$

$$R_n = \sqrt{\langle \cos n(\Psi_n^B - \Psi_n^C) \rangle}$$

→  $v_2^{J/\psi}$  {EP} extraction at forward-rapidity!



→  $v_2^{J/\psi}$  {EP} as function of  $p_T$

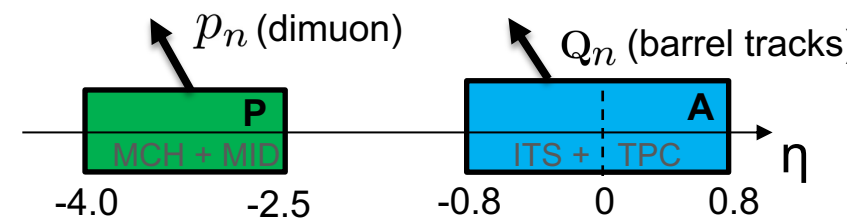


$$Q_{n,k} \equiv \sum_{i=1}^M w_i^k e^{in\phi_i},$$

$$S_{p,k} \equiv \left[ \sum_{i=1}^M w_i^k \right]^p,$$

$$\mathcal{M}_{abcd\dots} \equiv \sum_{i,j,k,l,\dots=1}^M w_i^a w_j^b w_k^c w_l^d \dots$$

$w_i^k$  → Non-uniform acceptance weights



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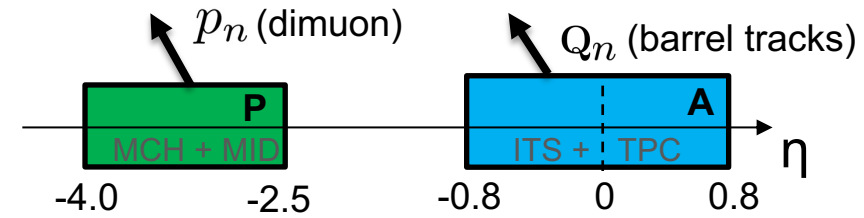
$w_i^k$  → Non-uniform acceptance weights

## POI correlators

→ Average over tracks

$$\langle 2' \rangle = \frac{p_{n,0} Q_{n,1}^* - s_{1,1}}{m_p S_{1,1} - s_{1,1}},$$

$$\langle 4' \rangle = \left[ \begin{aligned} & p_{n,0} Q_{n,1} Q_{n,1}^* Q_{n,1}^* \\ & - q_{2n,1} Q_{n,1}^* Q_{n,1}^* - p_{n,0} Q_{n,1} Q_{2n,2}^* \\ & - 2 \cdot S_{1,2} p_{n,0} Q_{n,1}^* - 2 \cdot s_{1,1} |Q_{n,1}|^2 \\ & + 7 \cdot q_{n,2} Q_{n,1}^* - Q_{n,1} q_{n,2}^* \\ & + q_{2n,1} Q_{2n,2}^* + 2 \cdot p_{n,0} Q_{n,3}^* \\ & + 2 \cdot s_{1,1} S_{1,2} - 6 \cdot s_{1,3} \end{aligned} \right] / \mathcal{M}'_{0111},$$



## REF correlators

→ Average over tracks

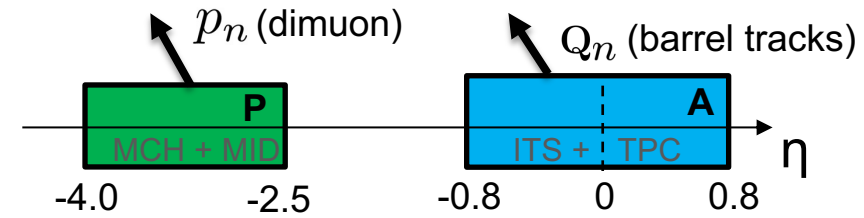
$$\langle 4 \rangle = \left[ |Q_{n,1}|^4 + |Q_{2n,2}|^2 - 2 \cdot \Re [Q_{2n,2} Q_{n,1}^* Q_{n,1}^*] \right. \\ \left. + 8 \cdot \Re [Q_{n,3} Q_{n,1}^*] - 4 \cdot S_{1,2} |Q_{n,1}|^2 \right. \\ \left. - 6 \cdot S_{1,4} - 2 \cdot S_{2,2} \right] / \mathcal{M}_{1111},$$

$$\langle 2 \rangle = \frac{|Q_{n,1}|^2 - S_{1,2}}{S_{2,1} - S_{1,2}},$$

$$Q_{n,k} \equiv \sum_{i=1}^M w_i^k e^{in\phi_i}, \quad S_{p,k} \equiv \left[ \sum_{i=1}^M w_i^k \right]^p,$$

$$\mathcal{M}_{abcd\dots} \equiv \sum_{i,j,k,l,\dots=1}^M w_i^a w_j^b w_k^c w_l^d \dots$$

$w_i^k$  → Non-uniform acceptance weights



## POI correlators

→ Average over tracks

$$\langle 2' \rangle = \frac{p_{n,0} Q_{n,1}^* - s_{1,1}}{m_p S_{1,1} - s_{1,1}},$$

→ Average over all events

$$\langle\langle 2' \rangle\rangle = \frac{\sum_{i=1}^N (\mathcal{M}'_{01})_i \langle 2' \rangle_i}{\sum_{i=1}^N (\mathcal{M}'_{01})_i},$$

$$\mathcal{M}'_{01} \equiv \sum_{i=1}^{m_p} \sum_{j=1}^M w_j$$

$$\langle 4' \rangle = \left[ \begin{aligned} & p_{n,0} Q_{n,1} Q_{n,1}^* Q_{n,1}^* \\ & - q_{2n,1} Q_{n,1}^* Q_{n,1}^* - p_{n,0} Q_{n,1} Q_{2n,2}^* \\ & - 2 \cdot S_{1,2} p_{n,0} Q_{n,1}^* - 2 \cdot s_{1,1} |Q_{n,1}|^2 \\ & + 7 \cdot q_{n,2} Q_{n,1}^* - Q_{n,1} q_{n,2}^* \\ & + q_{2n,1} Q_{2n,2}^* + 2 \cdot p_{n,0} Q_{n,3}^* \\ & + 2 \cdot s_{1,1} S_{1,2} - 6 \cdot s_{1,3} \end{aligned} \right] / \mathcal{M}'_{0111},$$

$$\langle\langle 4' \rangle\rangle = \frac{\sum_{i=1}^N (\mathcal{M}'_{0111})_i \langle 4' \rangle_i}{\sum_{i=1}^N (\mathcal{M}'_{0111})_i},$$

$$\mathcal{M}'_{0111} \equiv \sum_{i=1}^{m_p} \sum_{j,k,l=1}^M w_j w_k w_l$$

## REF correlators

→ Average over tracks

$$\langle 2 \rangle = \frac{|Q_{n,1}|^2 - S_{1,2}}{S_{2,1} - S_{1,2}}, \quad \langle 4 \rangle = \left[ \begin{aligned} & |Q_{n,1}|^4 + |Q_{2n,2}|^2 - 2 \cdot \Re [Q_{2n,2} Q_{n,1}^* Q_{n,1}^*] \\ & + 8 \cdot \Re [Q_{n,3} Q_{n,1}^*] - 4 \cdot S_{1,2} |Q_{n,1}|^2 \\ & - 6 \cdot S_{1,4} - 2 \cdot S_{2,2} \end{aligned} \right] / \mathcal{M}_{1111},$$

→ Average over all events

$$\langle\langle 2 \rangle\rangle = \frac{\sum_{i=1}^N (\mathcal{M}_{11})_i \langle 2 \rangle_i}{\sum_{i=1}^N (\mathcal{M}_{11})_i},$$

$$\mathcal{M}_{11} \equiv \sum_{i,j=1}^M w_i w_j$$

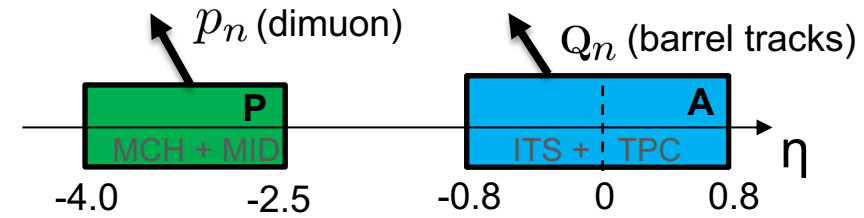
$$\langle\langle 4 \rangle\rangle = \frac{\sum_{i=1}^N (\mathcal{M}_{1111})_i \langle 4 \rangle_i}{\sum_{i=1}^N (\mathcal{M}_{1111})_i},$$

$$\mathcal{M}_{1111} \equiv \sum_{i,j,k,l=1}^M w_i w_j w_k w_l$$

$$Q_{n,k} \equiv \sum_{i=1}^M w_i^k e^{in\phi_i}, \quad S_{p,k} \equiv \left[ \sum_{i=1}^M w_i^k \right]^p,$$

$$\mathcal{M}_{abcd\dots} \equiv \sum_{i,j,k,l,\dots=1}^M w_i^a w_j^b w_k^c w_l^d \dots$$

$w_i^k$  → Non-uniform acceptance weights



## POI correlators

→ Average over tracks

$$\langle 2' \rangle = \frac{p_{n,0} Q_{n,1}^* - s_{1,1}}{m_p S_{1,1} - s_{1,1}},$$

→ Average over all events

$$\langle\langle 2' \rangle\rangle = \frac{\sum_{i=1}^N (\mathcal{M}'_{01})_i \langle 2' \rangle_i}{\sum_{i=1}^N (\mathcal{M}'_{01})_i},$$

$$\mathcal{M}'_{01} \equiv \sum_{i=1}^{m_p} \sum_{j=1}^M w_j$$

$$\langle 4' \rangle = \left[ \begin{aligned} & p_{n,0} Q_{n,1} Q_{n,1}^* Q_{n,1}^* \\ & - q_{2n,1} Q_{n,1}^* Q_{n,1}^* - p_{n,0} Q_{n,1} Q_{2n,2}^* \\ & - 2 \cdot S_{1,2} p_{n,0} Q_{n,1}^* - 2 \cdot s_{1,1} |Q_{n,1}|^2 \\ & + 7 \cdot q_{n,2} Q_{n,1}^* - Q_{n,1} q_{n,2}^* \\ & + q_{2n,1} Q_{2n,2}^* + 2 \cdot p_{n,0} Q_{n,3}^* \\ & + 2 \cdot s_{1,1} S_{1,2} - 6 \cdot s_{1,3} \end{aligned} \right] / \mathcal{M}'_{0111},$$

$$\langle\langle 4' \rangle\rangle = \frac{\sum_{i=1}^N (\mathcal{M}'_{0111})_i \langle 4' \rangle_i}{\sum_{i=1}^N (\mathcal{M}'_{0111})_i},$$

$$\mathcal{M}'_{0111} \equiv \sum_{i=1}^{m_p} \sum_{j,k,l=1}^M w_j w_k w_l$$

## REF correlators

→ Average over tracks

$$\langle 2 \rangle = \frac{|Q_{n,1}|^2 - S_{1,2}}{S_{2,1} - S_{1,2}}, \quad \langle 4 \rangle = \left[ |Q_{n,1}|^4 + |Q_{2n,2}|^2 - 2 \cdot \Re [Q_{2n,2} Q_{n,1}^* Q_{n,1}^*] \right. \\ \left. + 8 \cdot \Re [Q_{n,3} Q_{n,1}^*] - 4 \cdot S_{1,2} |Q_{n,1}|^2 - 6 \cdot S_{1,4} - 2 \cdot S_{2,2} \right] / \mathcal{M}_{1111},$$

→ Average over all events

$$\langle\langle 2 \rangle\rangle = \frac{\sum_{i=1}^N (\mathcal{M}_{11})_i \langle 2 \rangle_i}{\sum_{i=1}^N (\mathcal{M}_{11})_i},$$

$$\mathcal{M}_{11} \equiv \sum_{i,j=1}^M w_i w_j$$

$$\langle\langle 4 \rangle\rangle = \frac{\sum_{i=1}^N (\mathcal{M}_{1111})_i \langle 4 \rangle_i}{\sum_{i=1}^N (\mathcal{M}_{1111})_i},$$

$$\mathcal{M}_{1111} \equiv \sum_{i,j,k,l=1}^M w_i w_j w_k w_l$$

**POI cumulants**

$$\left\{ \begin{aligned} d_n^{\mu\mu}\{2\} &= \langle\langle 2' \rangle\rangle \\ d_n^{\mu\mu}\{4\} &= \langle\langle 4' \rangle\rangle - 2 \cdot \langle\langle 2' \rangle\rangle \langle\langle 2 \rangle\rangle \end{aligned} \right.$$

**POI flow**

$$\left\{ \begin{aligned} v_n^{\mu\mu}\{2\} &= \frac{d_n^{\mu\mu}\{2\}}{\sqrt{c_n\{2\}}} \\ v_n^{\mu\mu}\{4\} &= -\frac{d_n^{\mu\mu}\{4\}}{(-c_n\{4\})^{3/4}} \end{aligned} \right.$$

**REF cumulants**

$$\left\{ \begin{aligned} c_n\{2\} &= \langle\langle 2 \rangle\rangle \\ c_n\{4\} &= \langle\langle 4 \rangle\rangle - 2 \cdot \langle\langle 2 \rangle\rangle^2 \end{aligned} \right.$$

**REF flow**

$$\left\{ \begin{aligned} v_n^{\text{REF}}\{2\} &= \sqrt{c_n\{2\}} \\ v_2^{\text{REF}}\{4\} &= \sqrt[4]{-c_2\{4\}} \end{aligned} \right.$$

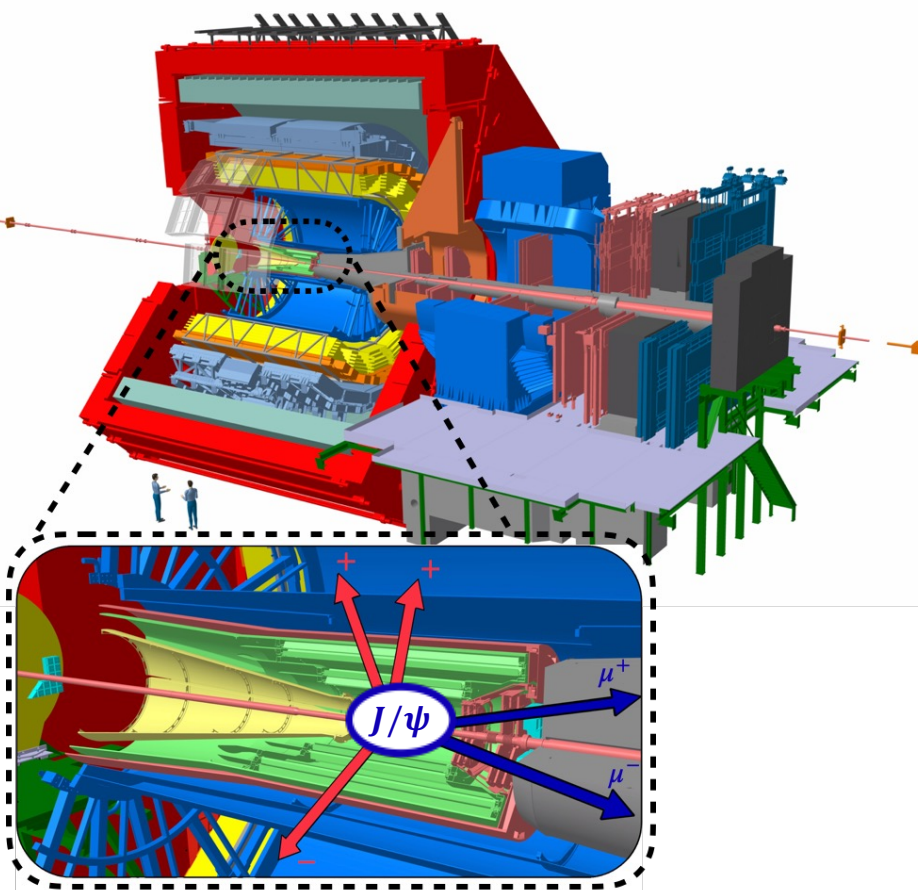
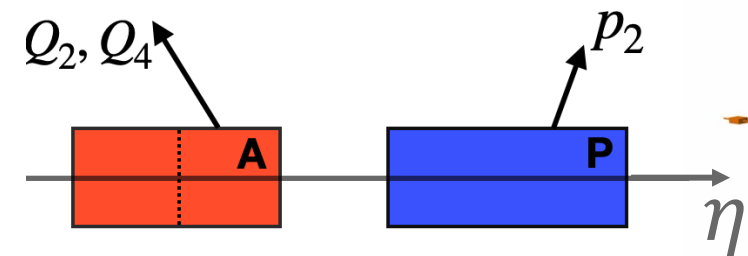


ALICE

# Flow of $J/\psi$ in Run 3 - Multi-particle cumulants

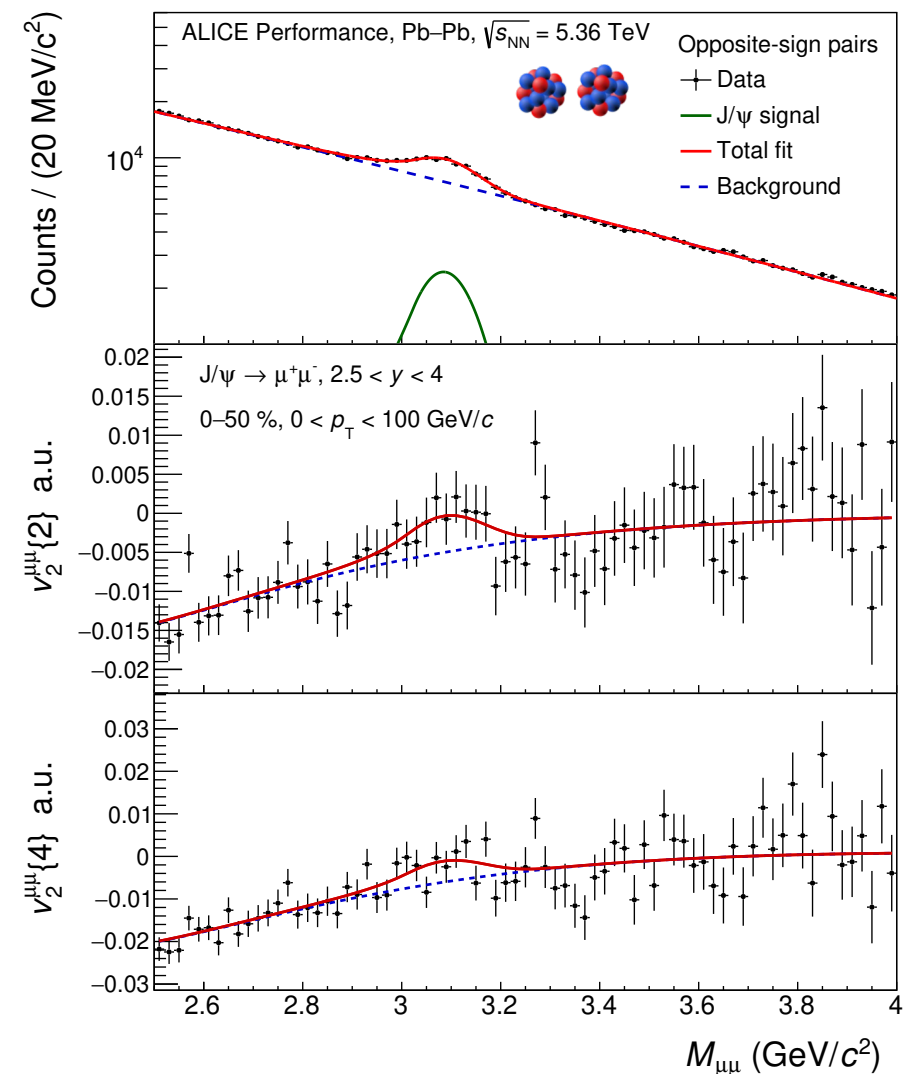


→ Partial statistics of the total 2023 Pb–Pb data



→ Run 3 data will enable more precise measurements for  $v_2^{J/\psi}$  up to higher  $p_T$

→ High order cumulants suppress **non-flow!**



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$$v_2\{2\}^2 = \langle v_2^2 + \delta_2 \rangle \rightarrow \delta_2 \sim 1/M$$

$$v_2\{4\}^4 = -\langle v_2^4 + \delta_4 \rangle \rightarrow \delta_4 \sim 1/M^3$$

Scaling with multiplicity!

→ First  $v_2^{J/\psi}\{2, 4\}$  signal extraction at forward-rapidity!



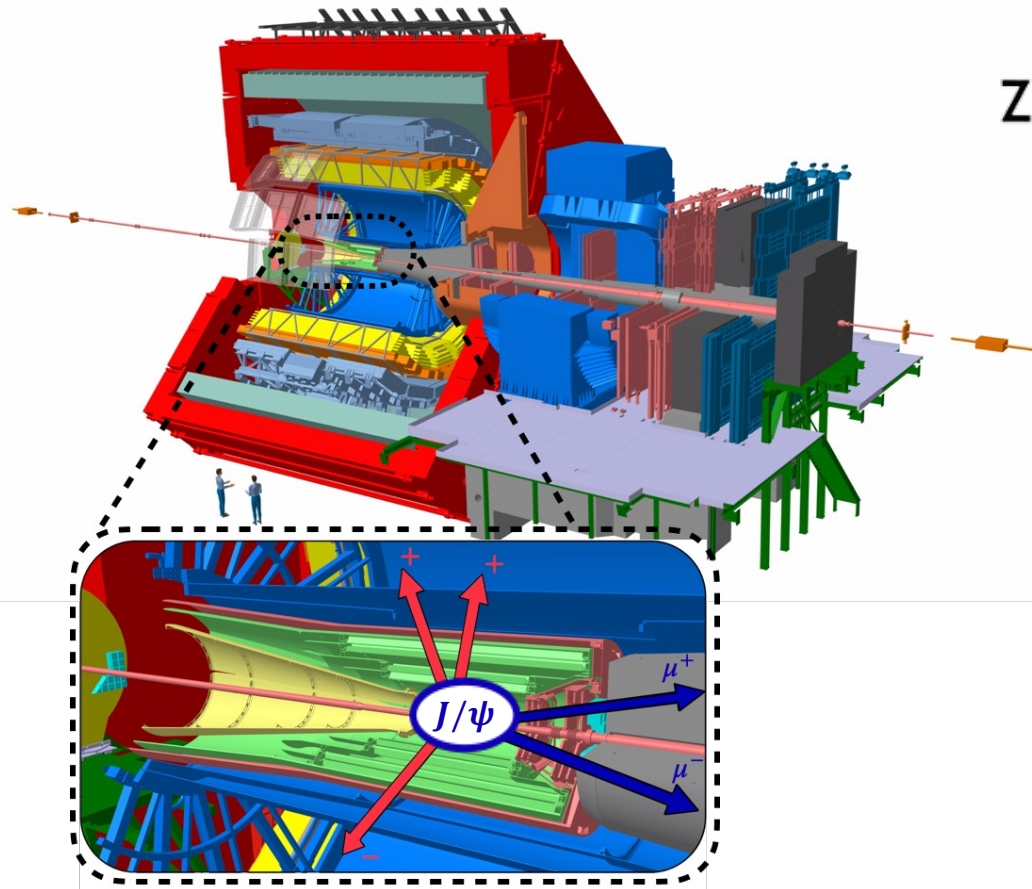


ALICE

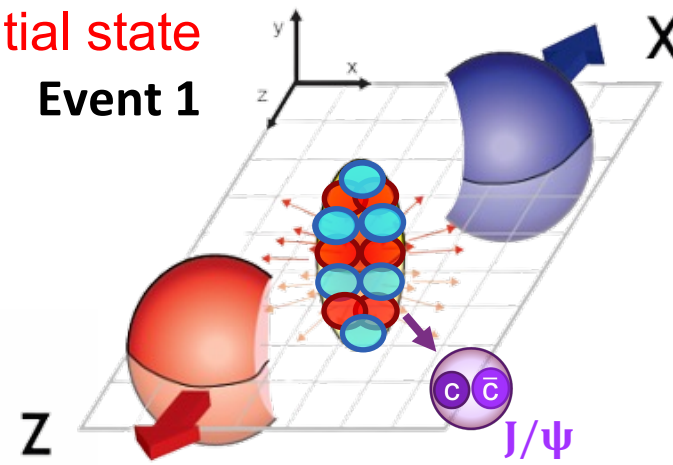
# Flow of $J/\psi$ in Run 3 - Multi-particle cumulants



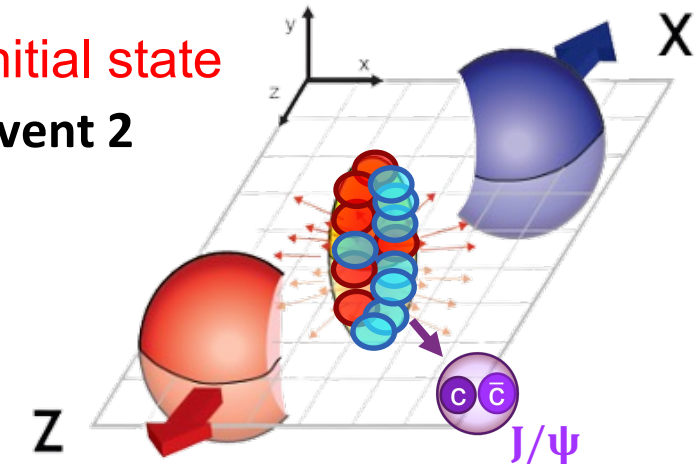
- **Fluctuations** in the positions of nucleons in the overlap region.



Initial state  
Event 1



Initial state  
Event 2



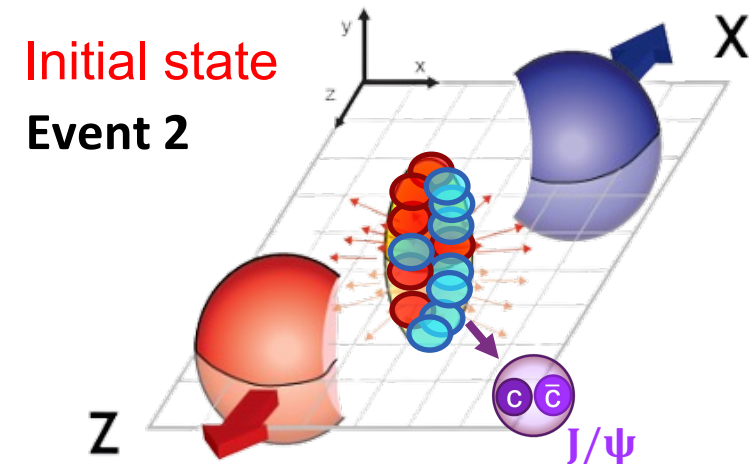
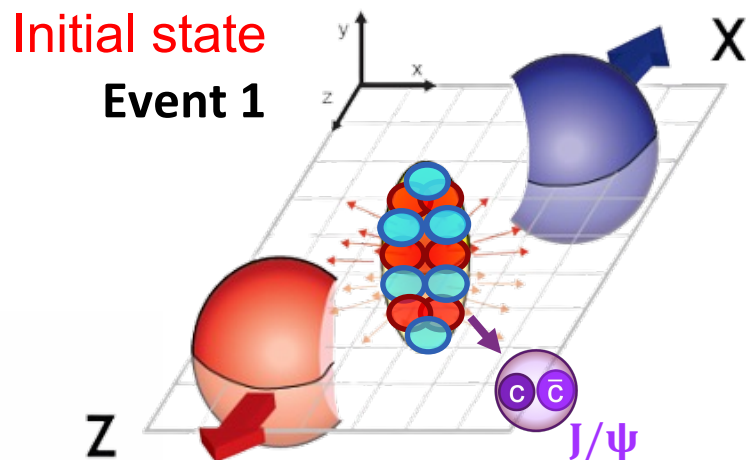
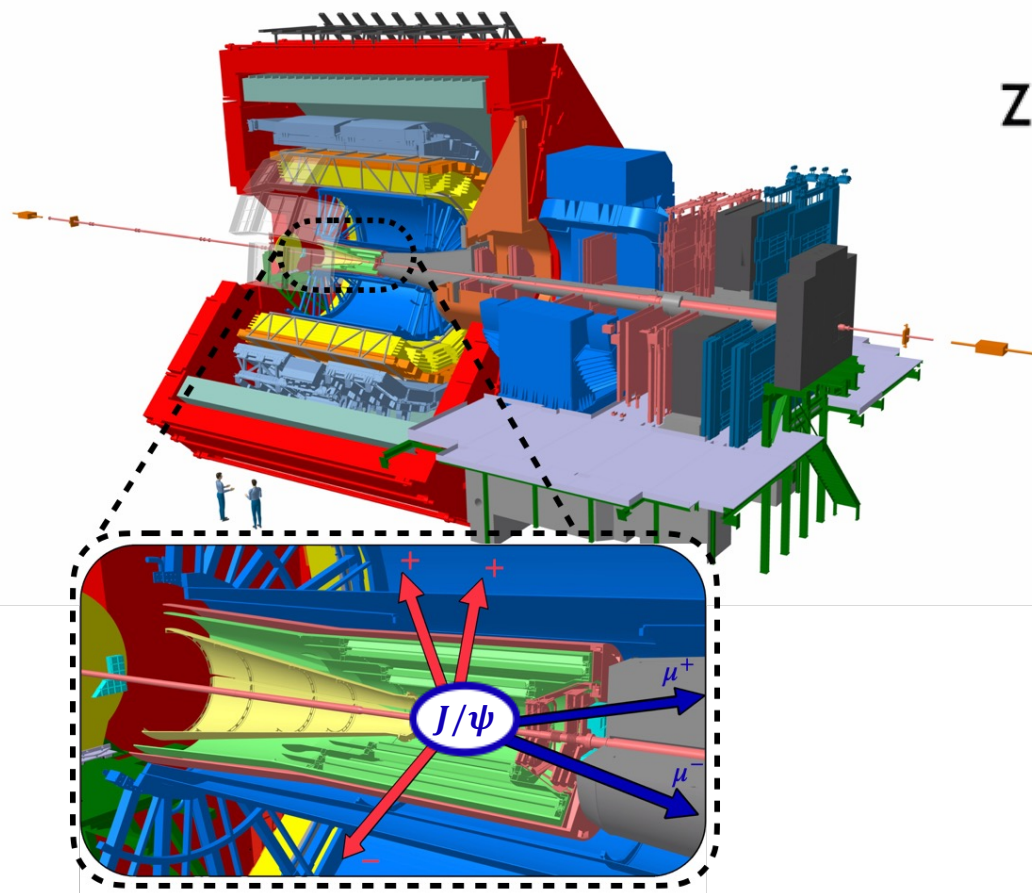


ALICE

# Flow of $J/\psi$ in Run 3 - Multi-particle cumulants



- **Fluctuations** in the positions of nucleons in the overlap region.



**Fluctuation ratio  $\sigma/\langle v_2 \rangle$**

$$v_2\{2\}^2 \approx \langle v_2 \rangle^2 + \sigma^2$$

$$v_2\{4\}^2 \approx \langle v_2 \rangle^2 - \sigma^2$$

$$\left[ \frac{\sigma}{\langle v_2 \rangle} = \sqrt{\frac{v_2\{2\}^2 - v_2\{4\}^2}{v_2\{2\}^2 + v_2\{4\}^2}} \right]$$

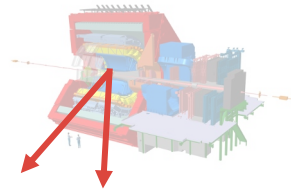
If  $\sigma/\langle v_2^{J/\psi} \rangle$  does not show a  $p_T$  dependence, the observed fluctuations are likely due to variations in the initial-state geometry!

- Larger Run 3 sample will provide **better precision flow measurements**
- **New flow methods** will be used thanks to the **Run 3 continuous readout!**

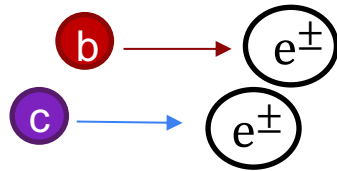
→ Run 3 flow measurements using **different methods**

- **Scalar product**
- **Event plane**
- **Multi-particle cumulant → Fluctuation Ratio!**

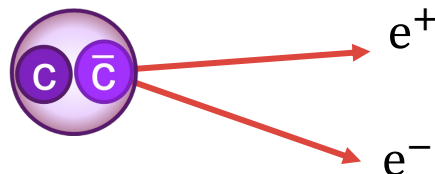
**At mid-rapidity:**



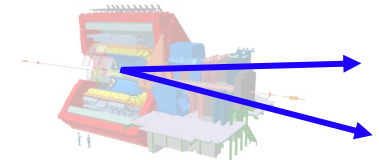
→ Flow of  $e^\pm$  from **charm** and **beauty** decays in Pb-Pb



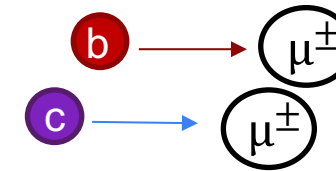
→ Flow of **J/ψ** in pp



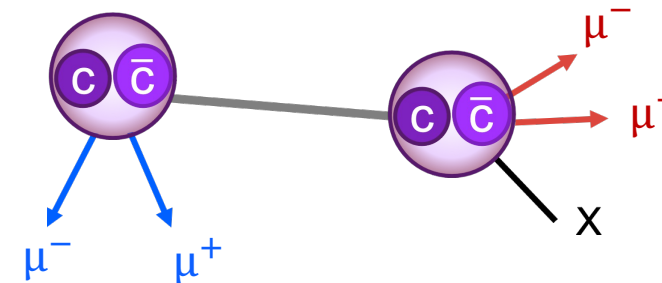
**At forward-rapidity:**



→ Flow of  $\mu^\pm$  from **charm** and **beauty** decays

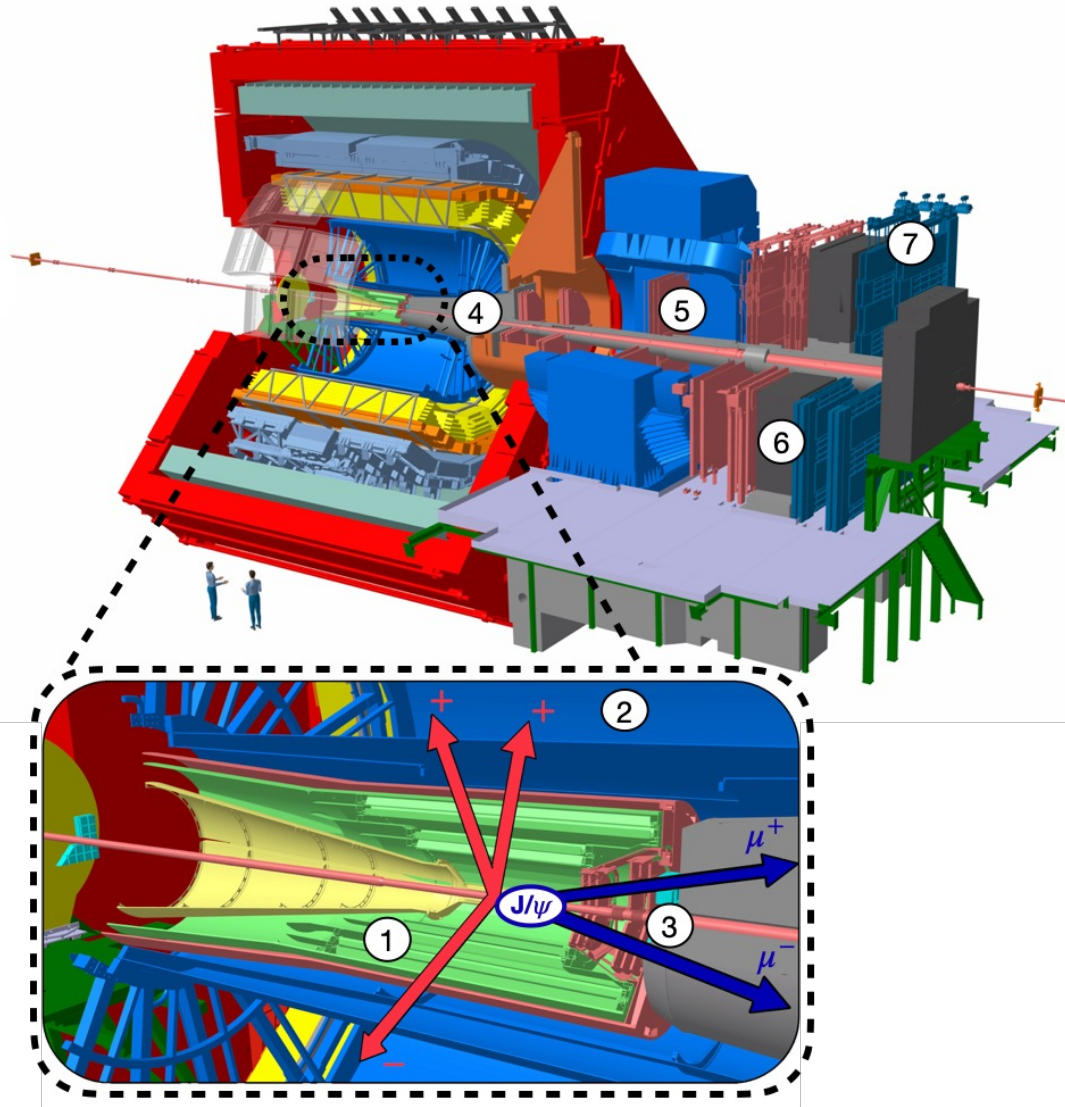


→ Flow of **J/ψ** **prompt** and **non-prompt** in Pb-Pb



→ Thanks to the new Muon Forward Tracker (MFT) detector

# BACK UP



**ITS ①**

→ Vertex identification

**TPC ②**

→ Charged particles tracking

**FT0C ③**

→ Centrality estimation of collisions

**Front Absorber ④**

→ Reduce flux of hadrons by a factor of 100

**MCH ⑤**

→ Muon tracking system

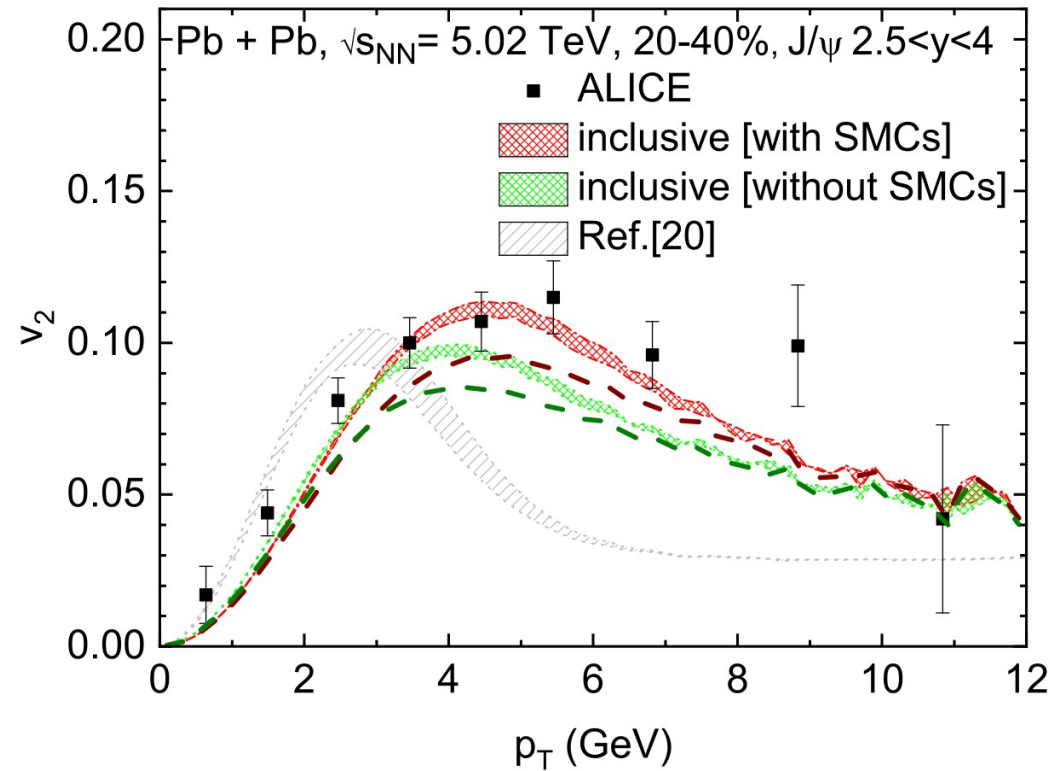
**Muon Filter ⑥**

→ Punch through hadrons

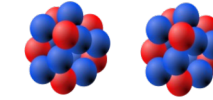
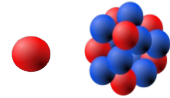
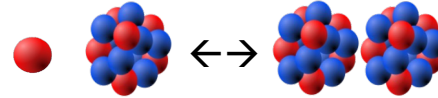
**MID ⑦**

→ Particle identification of muons

HE-WU-RAPP

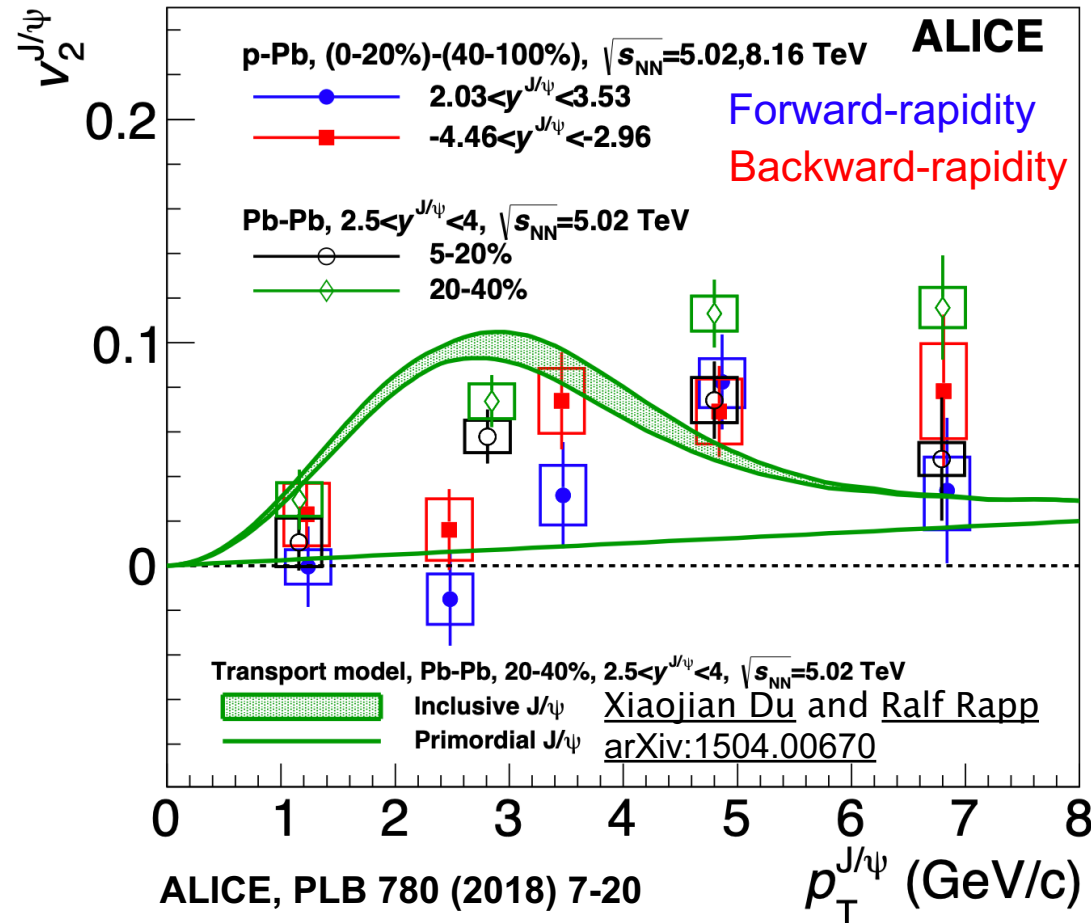


- **Run 2** values were obtained with **Scalar product method**.
- **Data** could be **contaminated by non-flow** (especially at high- $p_T$ )
- **Larger Run 3** sample would provide **better precision measurement for  $v_2$**  up to higher  $p_T$  and for higher harmonic orders.

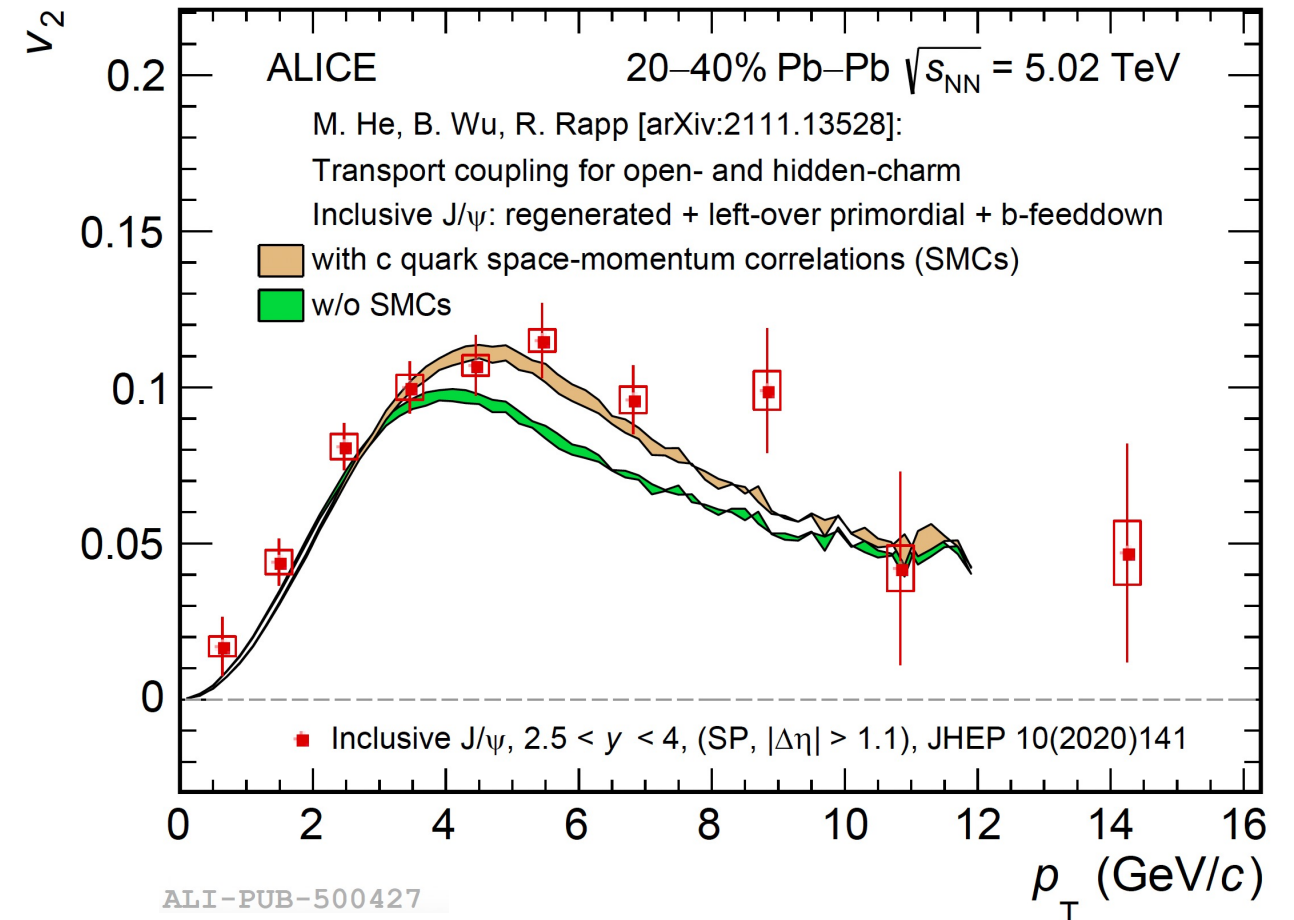


In p-Pb  $\rightarrow$  no expected  $J/\psi$  regeneration  
(no expected QGP formation)

In Pb-Pb  $\rightarrow$  Flow of  $J/\psi$  at low  $p_T$  is  
interpreted as a consequence of regeneration



$\rightarrow$  Comparable magnitude of  $v_2$   $J/\psi$  at high  $p_T$  in p-Pb and Pb-Pb collisions!



$v_2$   $J/\psi$  described well by a transport model where charm quark thermalized in QGP!