

# QCD & Lund Jet Plane studies at FCC-ee



L. Panwar (Postdoc), L. Delagrang (PhD),  
R.C. Camacho Toro, B. Malaescu, L. Poggioli

ECFA Workshop 2024, Paris, France

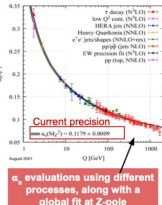
contact email: [lata.panwar@cern.ch](mailto:lata.panwar@cern.ch)

**QCD & Lund Jet Plane studies@FCC-ee**

FUTURE CIRCULAR COLLIDER Innovation Study  
LPNHE PARIS  
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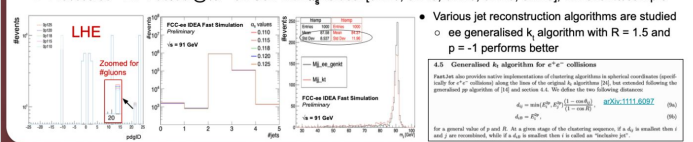
R.C. Camacho Toro, L. Delagrang, B. Malaescu, L. Panwar, L. Poggioli, ECFA, Paris 2024

- Analyse prospects of QCD study@FCC-ee using 3/2 Jet cross-section ( $R_{3/2}$ ) study and Lund Jet Plane (LJP) representation
- Aim to study the sensitivity to  $\alpha_s$  at FCC-ee, to probe  $\alpha_s$  for different energies and test the Renormalization Group Equation (RGE) in QCD
- Also look for the potential use of LJP for improving jet tagging and for the optimization of detector parameters @FCC-ee
- Why FCC-ee?**
  - Provides a clean collision environment with high statistics ( $10^6$  X LEP Data)
  - Expect factor of 10 improvement with respect to the current  $\alpha_s$  precision



### MC Simulation

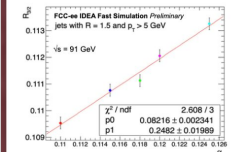
- LHE events from Madgraph (MG5\_aMC@NLO); processed with Pythia8 and Delphes with default IDEA detector card
- Process  $ee \rightarrow Z \rightarrow u\bar{u}d\bar{d} @ \sqrt{s} = 91$  GeV with  $\alpha_s$  values: [0.110, 0.115, 0.118, 0.120, 0.125]; 1M events/sample



### $R_{3/2}$ Study

$$R_{3/2} = \frac{\text{The number of events with at least 3 jets}}{\text{The number of events with at least 2 jets}}$$

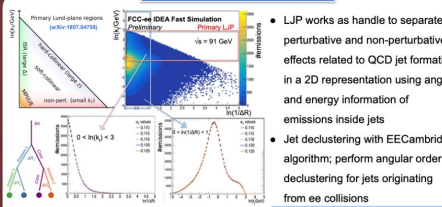
- Select jets with  $p_T > 5$  GeV in an event
- Perform study for  $R=0.5$  and  $R=1.5$  jets
- Observe dependency of  $R_{3/2}$  on  $\alpha_s$



Jets	Variation in $R_{3/2}$
$R=0.5$	$0.38 \pm 0.02 \Delta\alpha_s$
$R=1.5$	$0.25 \pm 0.02 \Delta\alpha_s$

Study ongoing with jets at hadron level

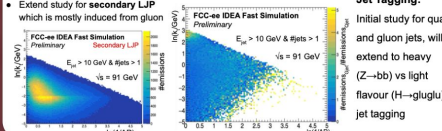
### Lund Jet Plane Study



LJP works as handle to separate perturbative and non-perturbative effects related to QCD jet formation in a 2D representation using angle and energy information of emissions inside jets

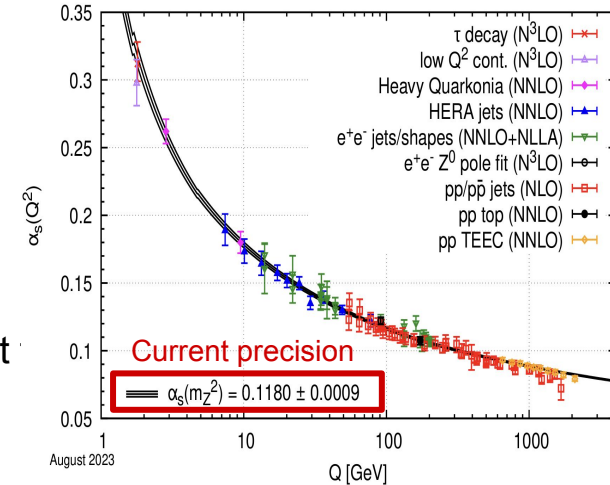
Jet clustering with EECambridge algorithm; perform angular order declustering for jets originating from ee collisions

$\Delta R / k_T =$  angle / transverse momentum of emission with respect to core



# Introduction and motivation

- Analyse prospects of **QCD study@FCC-ee** using **3/2 Jet cross-section ( $R_{3/2}$ )** study and **Lund Jet Plane (LJP) representation**
- Aim to study the **sensitivity to  $\alpha_s$  at FCC-ee**, to probe  $\alpha_s$  for different energies and test the Renormalization Group Equation (RGE) in QCD
  - $\alpha_s$  impacts both jet multiplicity and jet shape (emissions inside jet)
- Also look for the potential use of LJP for improving jet tagging and impact the optimization of detector parameters @FCC-ee
- **Why FCC-ee?**
  - Provides a clean collision environment with high statistics (10<sup>6</sup> X LEP Data)
- Both analyses use FCCAnalysis framework along with centrally produced Delphes samples



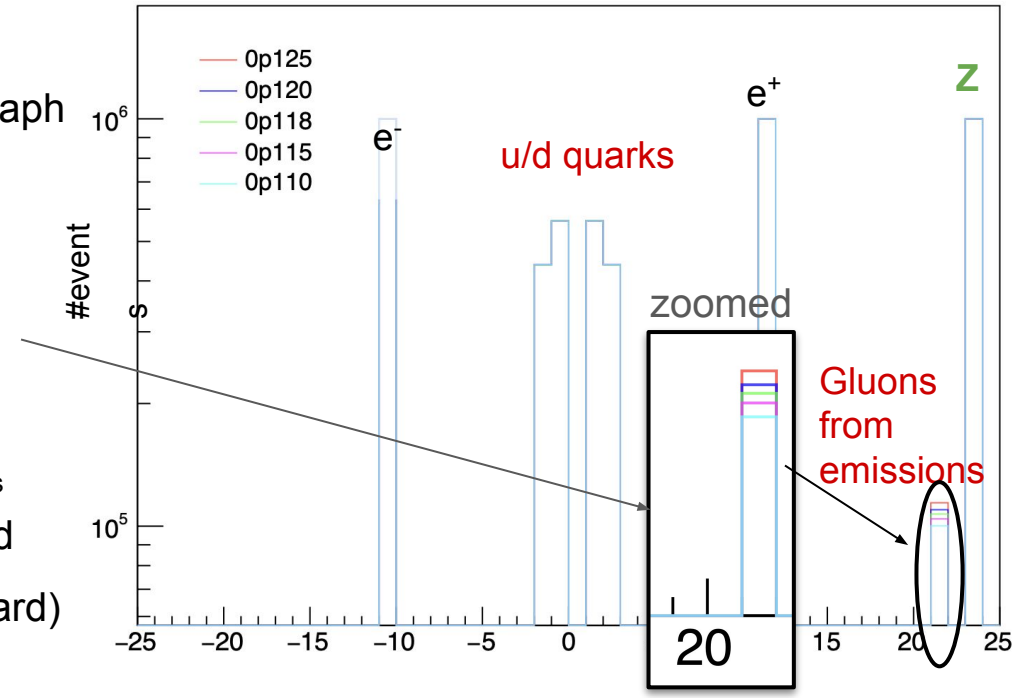
# Samples

Use centrally produced Winter2023 Delphes

samples for IDEA for both the analyses

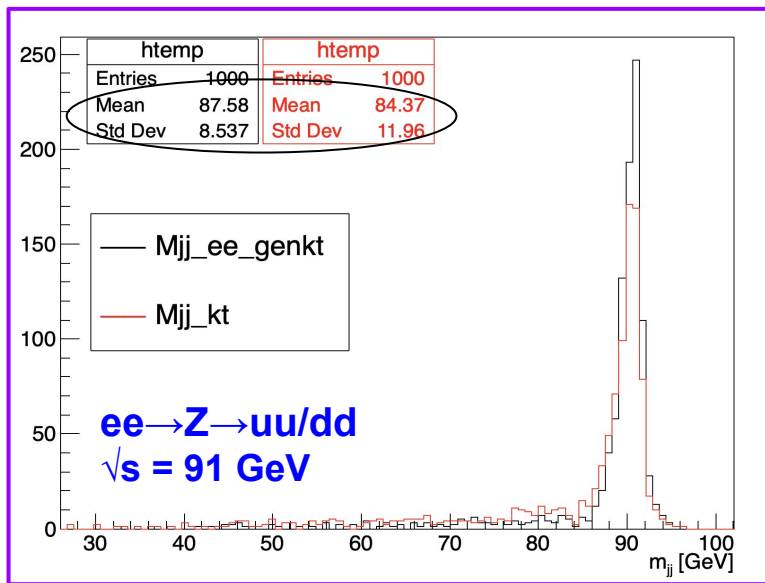
- LHE level events are generated with Madgraph (MG5\_aMC@NLO) for  $ee \rightarrow Z \rightarrow uu/dd$  at  $\sqrt{s} = 91 \text{ GeV}$
- Samples are generated with 5 different  $\alpha_s$  values: [0.110, 0.115, **0.118**, 0.120, 0.125]
- Emitted gluons multiplicity increases with  $\alpha_s$
- Events are further simulated with Pythia and Delphes generators (using IDEA detector card)
- #events = 1 M/sample

$ee \rightarrow Z \rightarrow uu/dd$   $\sqrt{s} = 91 \text{ GeV}$  LHE level



Other validation plots are in backup

# Jet reconstruction with Delphes samples



- Explored various jet reconstruction algorithms
- Better  $m_{jj}$  resolution with  $\theta$ -based ee generalised  $k_t$  algorithms with  $R = 1.5$  and  $p = -1$  wrt  $\Delta R(y, \phi)$ -based  $k_t$  algorithms
- Jet kinematics distributions are in backup

## 4.5 Generalised $k_t$ algorithm for $e^+e^-$ collisions [arXiv:1111.6097](https://arxiv.org/abs/1111.6097)

FastJet also provides native implementations of clustering algorithms in spherical coordinates (specifically for  $e^+e^-$  collisions) along the lines of the original  $k_t$  algorithms [24], but extended following the generalised  $pp$  algorithm of [14] and section 4.4. We define the two following distances:

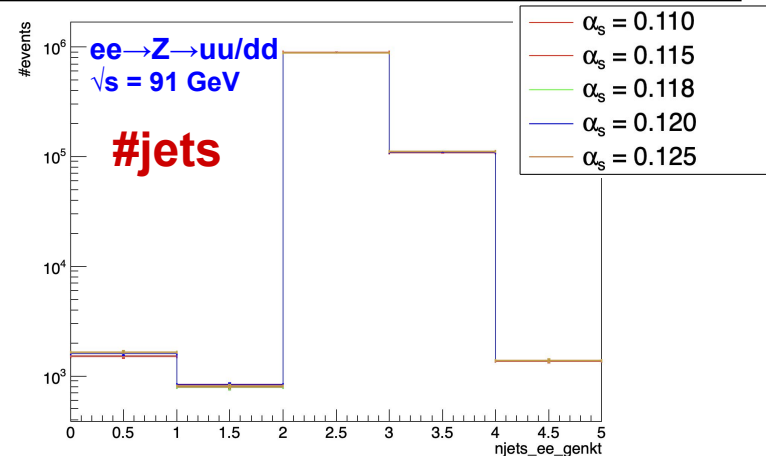
$$d_{ij} = \min(E_i^{2p}, E_j^{2p}) \frac{(1 - \cos \theta_{ij})}{(1 - \cos R)}, \quad (9a)$$

$$d_{iB} = E_i^{2p}, \quad (9b)$$

for a general value of  $p$  and  $R$ . At a given stage of the clustering sequence, if a  $d_{ij}$  is smallest then  $i$  and  $j$  are recombined, while if a  $d_{iB}$  is smallest then  $i$  is called an “inclusive jet”.

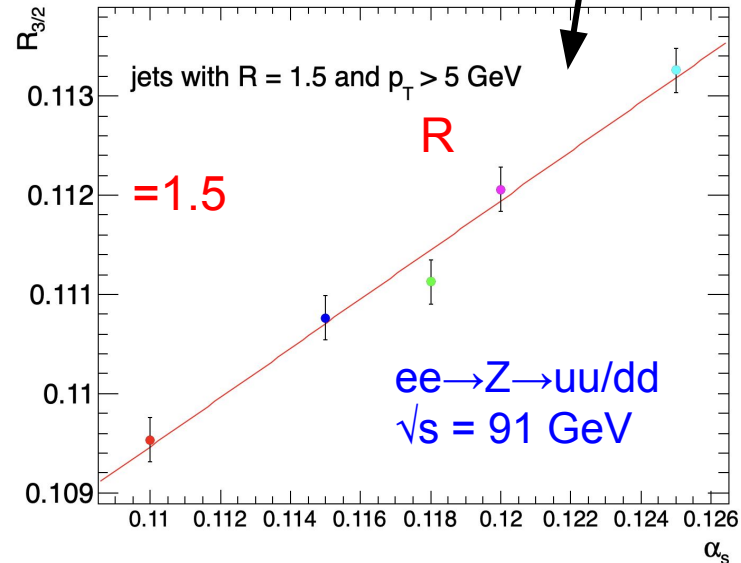
For values of  $R \leq \pi$  in eq. (9), the generalised  $e^+e^-$   $k_t$  algorithm behaves in analogy with the  $pp$  algorithms: when an object is at an angle  $\theta_{iX} > R$  from all other objects  $X$  then it forms an inclusive jet. With the choice  $p = -1$  this provides a simple, infrared and collinear safe way of obtaining a cone-like algorithm for  $e^+e^-$  collisions, since hard well-separated jets have a circular profile on the 3D sphere, with opening half-angle  $R$ . To use this form of the algorithm, define

```
JetDefinition jet_def(ee_genkt_algorithm, R, p);
```



# Study I: $R_{3/2}$ studies

- Study jet cross section ratio between events with at least 3 jets vs 2 jets ( $\alpha_s$  impacts jet multiplicity)
- Observe  $R_{3/2}$  dependency on  $\alpha_s$



$$R_{3/2} = \frac{\text{The number of events with at least 3 jets}}{\text{The number of events with at least 2 jets}}$$

Jets	Variation in $R_{3/2}$
$R=0.5$	$(0.38 \pm 0.02) \Delta\alpha_s$
$R=1.5$	$(0.25 \pm 0.02) \Delta\alpha_s$

## Note:

- Choice of  $p_T$  cut is from default setting in FCCAnalyses framework; plan to switch to E cut
- Error bars represent stat. unc. only

## Next:

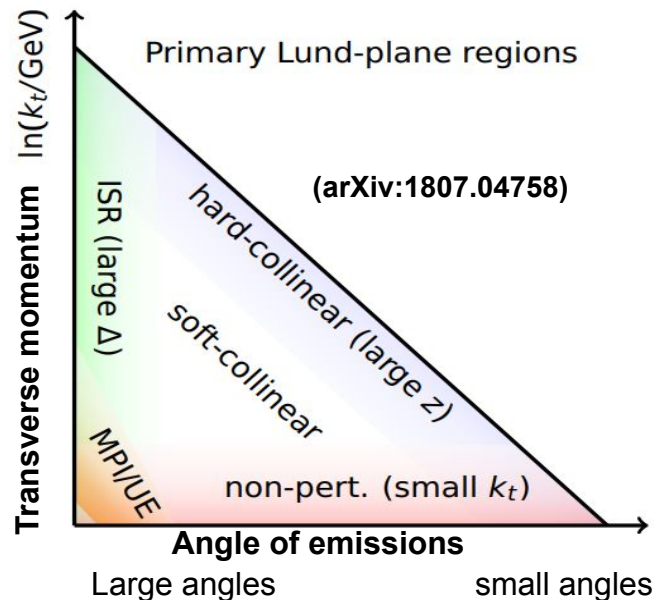
- Study ongoing with jets at hadron level (truth jets)

# Study II : Lund Jet Plane studies

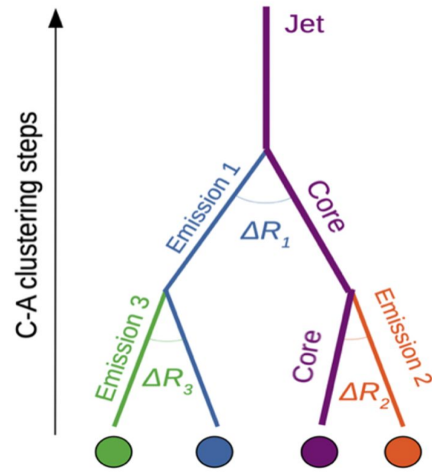
- QCD jet formation involves perturbative and non-perturbative effects; presence of these effects impacts the precision of any measurement based on jets
- LJP works as a handle to separate these effects in a 2D representation using angle ( $\Delta R$ ) and transverse momentum ( $k_t$ ) of emissions within the jets and further opens a possibility to understand QCD behaviour separately for these perturbative and non-perturbative effects
- $\alpha_s$  impacts jet shape (emissions within jets); Average density of emissions in LJP can be given as

$$\rho(k_T, \Delta R) \equiv \frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(k_T / \text{GeV}) d \ln(R / \Delta R)} \approx \frac{2}{\pi} C_R \alpha_s(k_T)$$

Where  $C_R$  = color factor



# How to build Lund Jet Plane?



- Start with a jet and cluster it again to have angular order information of emissions ([JHEP 12 \(2018\) 064](#))
- Decluster them in reverse (start with wide angle emission first)
- Within the iterative declustering, harder branch is always taken as core branch
- Fill a triangle plane of two Lund variables ( $k_t$  and  $\Delta R$ ) from core and emission

## NOTE:

- Angular ordered Cambridge/Aachen (C/A) declustering (following the theoretical proposal) depends on  $\Delta R$  in  $(\mathbf{y}, \phi)$  plane used for LHC studies (given in [backup](#))
- It is more accurate to perform  $\Delta R$ -based declustering in the  $(\theta, \phi)$  plane for FCC-ee. Therefore, we use EECambridgePlugin algorithm

For “a” core and “b” emission branch

$$k_t \equiv p_{tb} \Delta R_{ab}$$

$$z \equiv p_{tb} / (p_{ta} + p_{tb})$$

$\Delta R_{ab}$  = angle of emission **b** wrt to core **a**

$k_t$  = transverse momentum of **b** wrt **a**

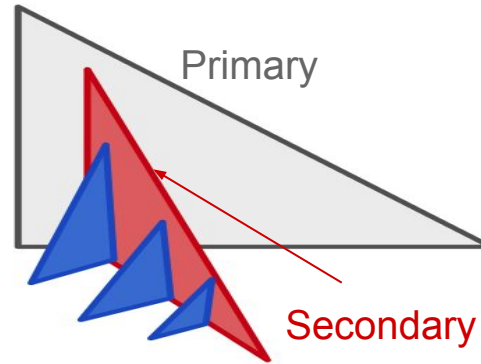
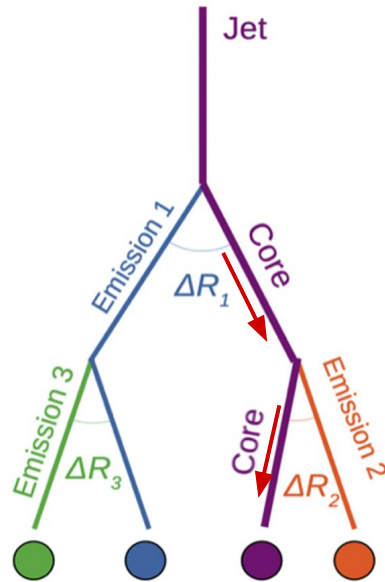
$z$  = momentum fraction taken by **b**

Analysis studies for primary and secondary LJP

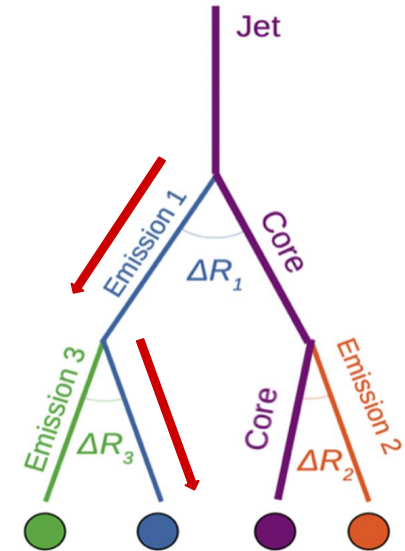
- Motivated from following the theoretical proposal [\[link\]](#) which show secondary LJP is mostly gluon induced

# How to build Primary and Secondary Lund Jet Plane?

## Primary LJP

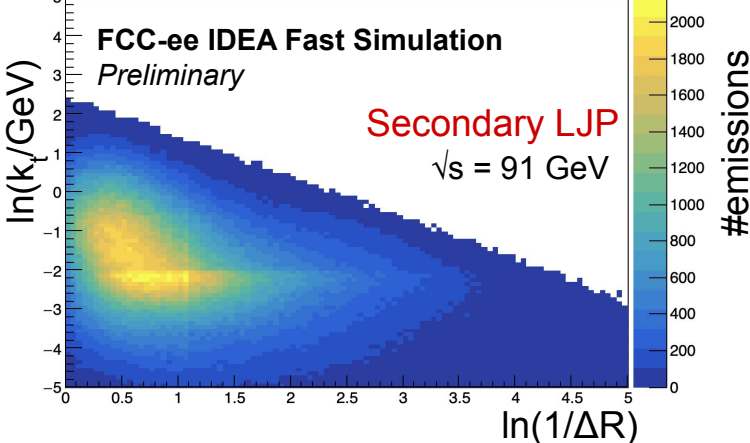
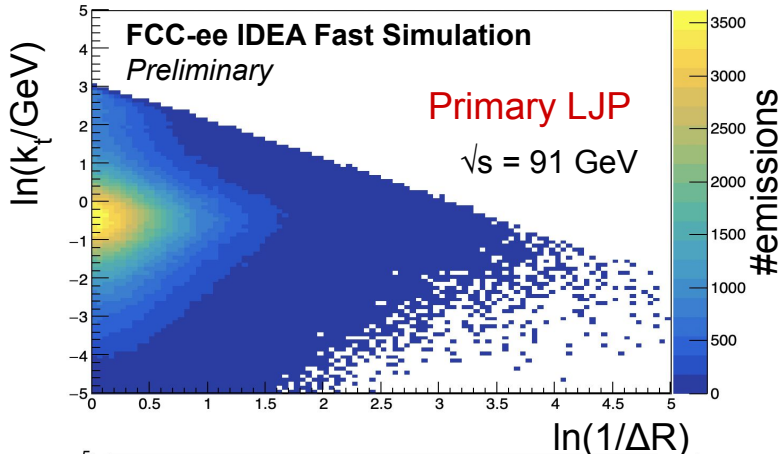
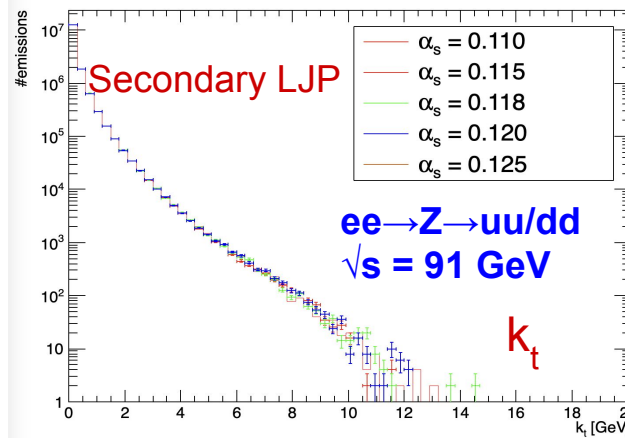
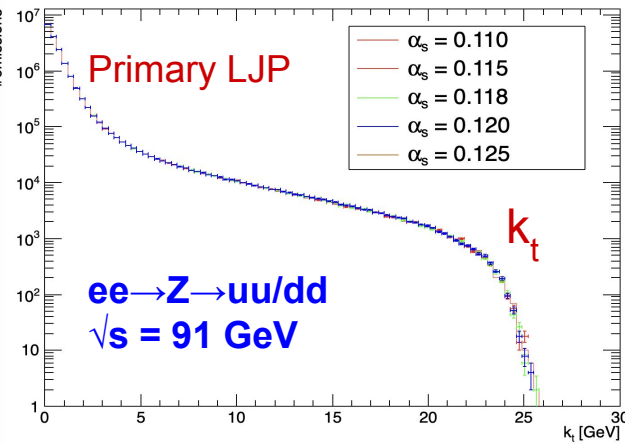


## Secondary LJP





# Preliminary look at LJPs: Primary and Secondary LJP



**Selections:**

$E_{\text{jet}} > 10 \text{ GeV}$   
 $\#\text{jets} > 1$

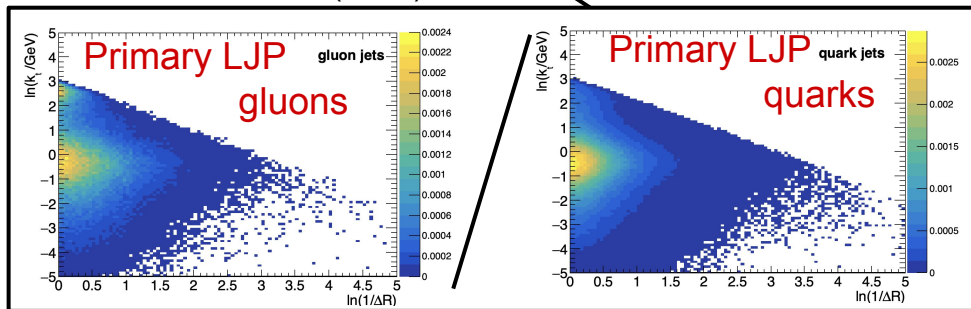
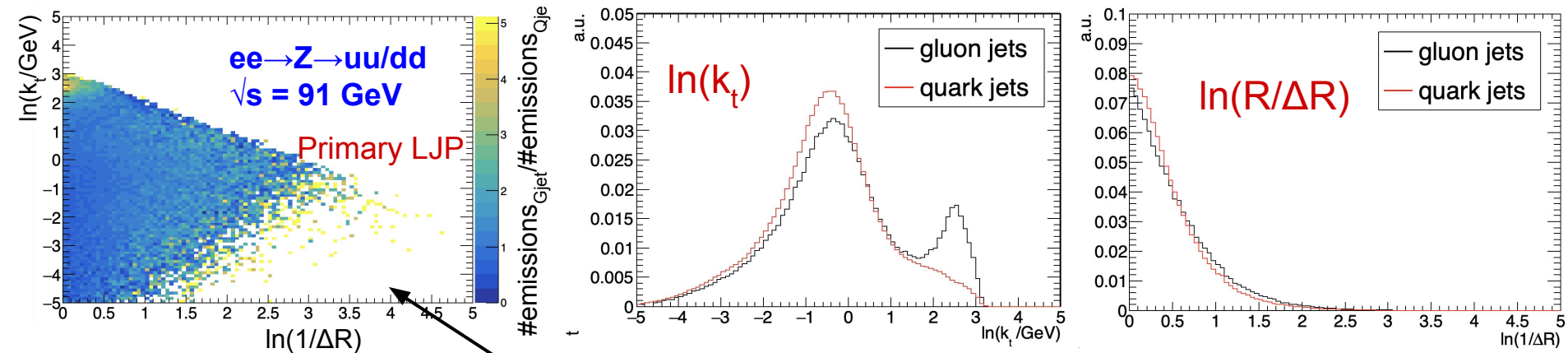
Observe difference for primary and secondary LJPs

Secondary LJP corresponds mostly to gluon emission

- leads towards developing jet tagging methods using LJP

# Potential of jet tagging using LJPs

- For now study is ongoing for quark and gluon jets; will be extended to heavy ( $Z \rightarrow b\bar{b}$ ) vs light flavor ( $H \rightarrow \text{gluon jets}$ ) jets



- Gluons are emitted from quarks in  $ee \rightarrow Z \rightarrow uu/dd$  process

# Summary and next steps

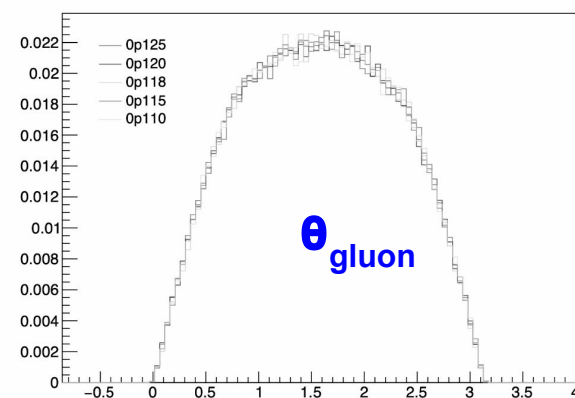
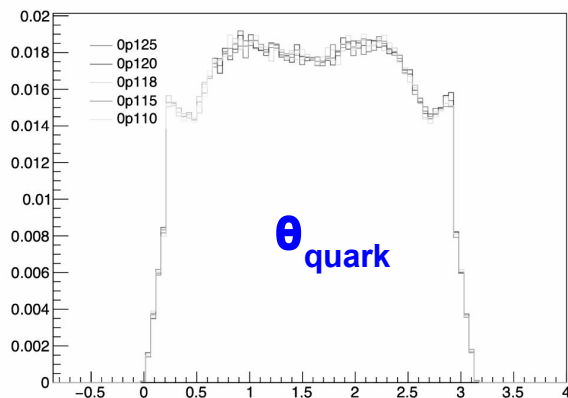
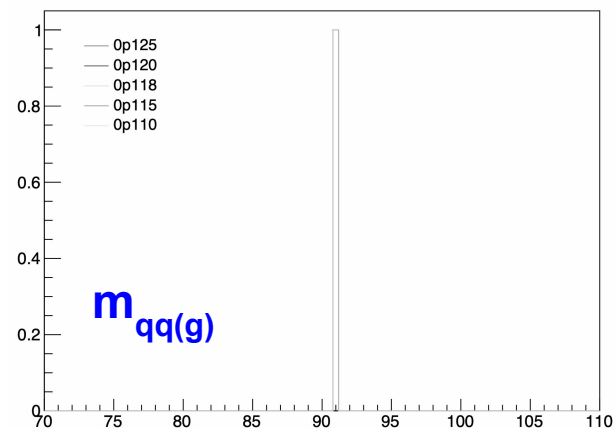
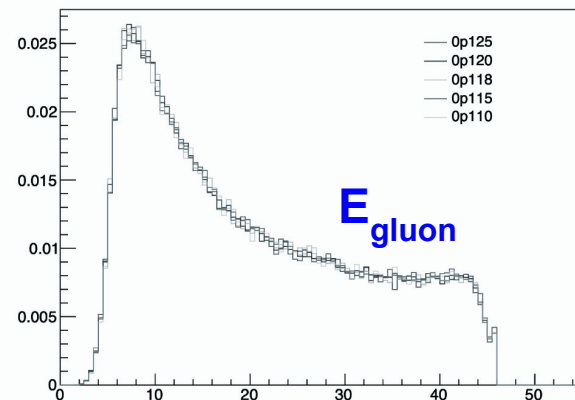
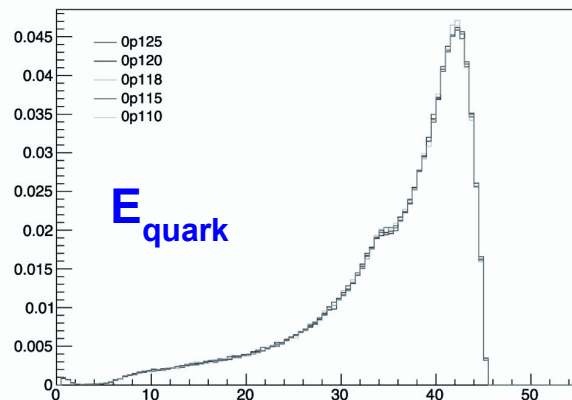
- Present updates of  $R_{3/2}$  jet cross section study and Lund Jet Plane studies at FCC-ee
  - Motivated by the study of the sensitivity to  $\alpha_s$  and test of RGE
- **$R_{3/2}$  study:**
  - Observe dependency of  $R_{3/2}$  on variation of  $\alpha_s$
  - Study ongoing with jets at hadron level
- **LJP Study:**
  - To our knowledge it is the first study that looks at jet substructure at FCC-ee
  - Switch to ee-dedicated algorithm for jet clustering/declustering
  - Plan to explore the sensitivity of the reconstructed LJP to:
    - $\alpha_s$  by doing  $\alpha_s$ -scan
    - Optimization of the detector parameters
    - Also potential use for jet tagging methods at FCC-ee

*Thank you*

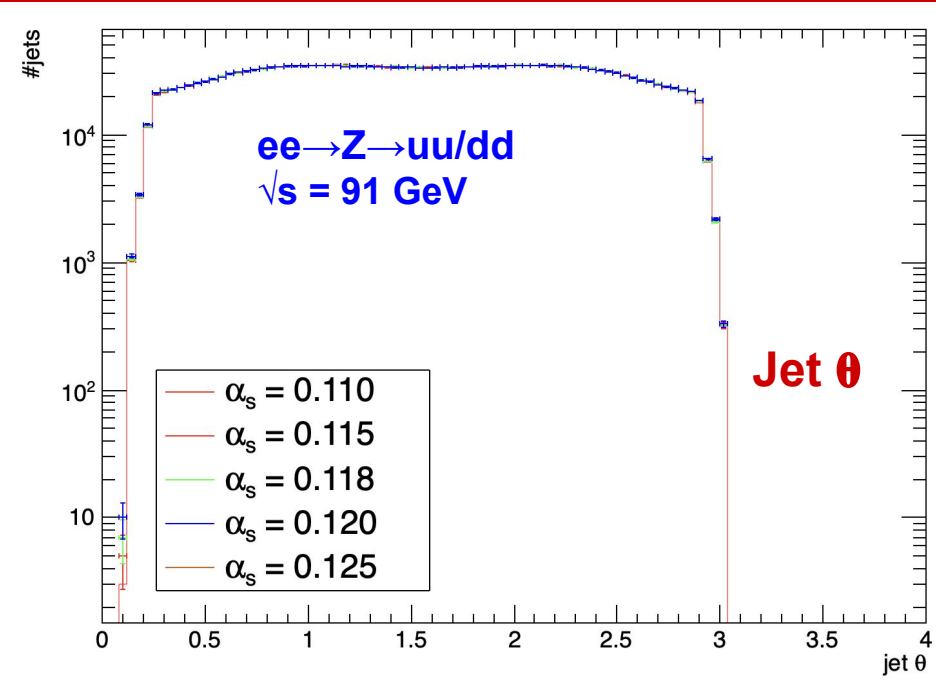
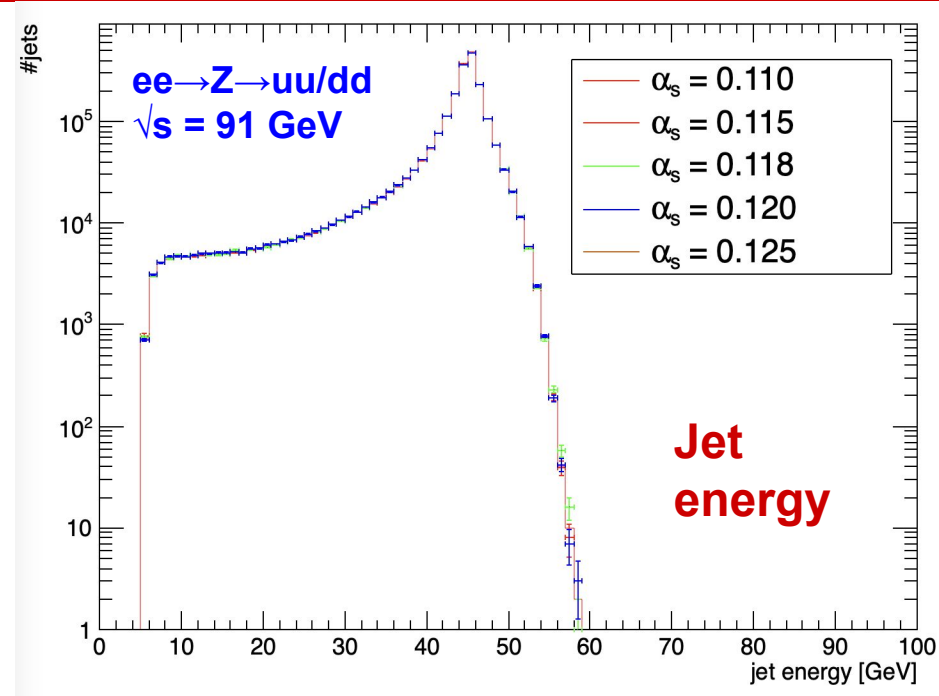
**BACKUP**

# Validation studies:LHE level

- Distributions are shown for different  $\alpha_s$  values and are shape normalized
- No selection at generator level

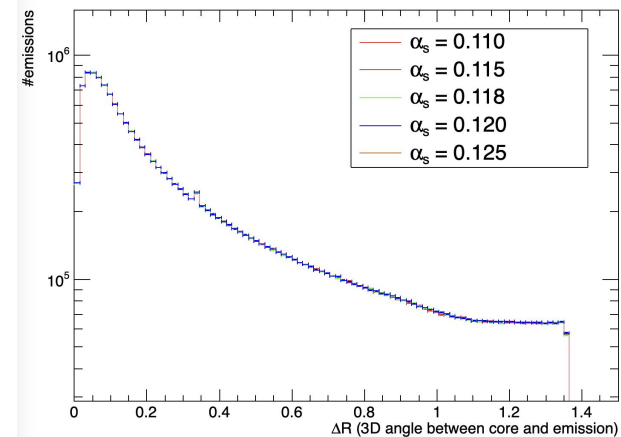
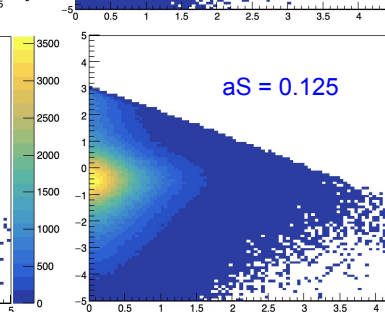
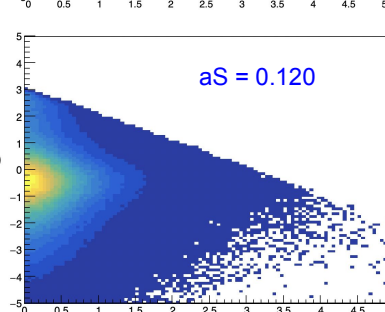
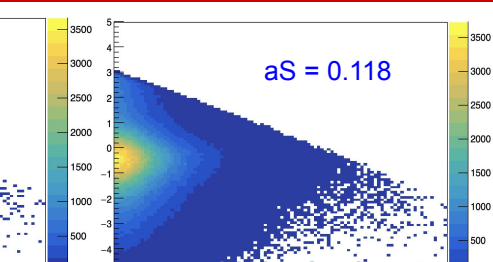
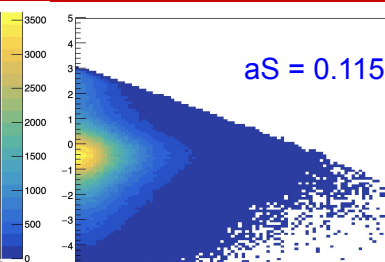
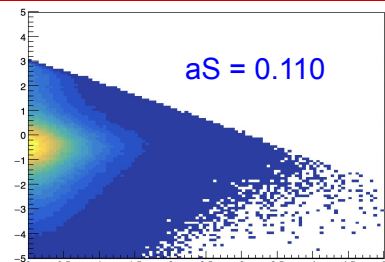
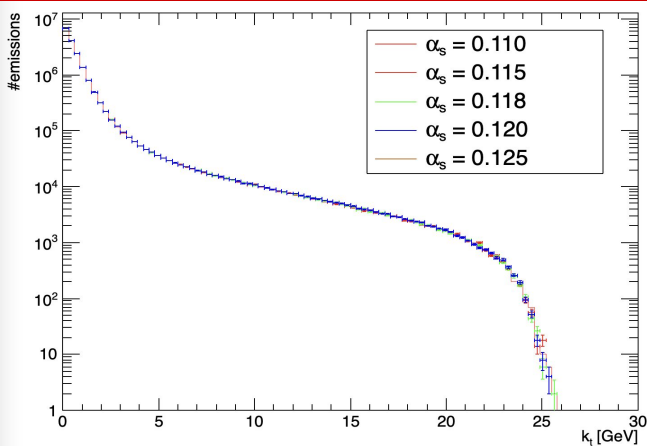


# Jet Kinematics

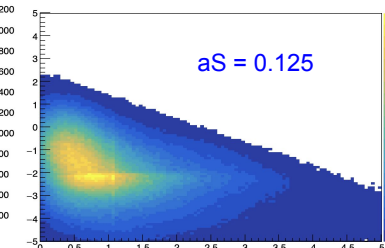
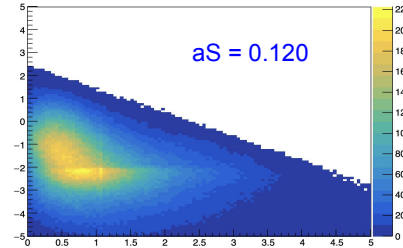
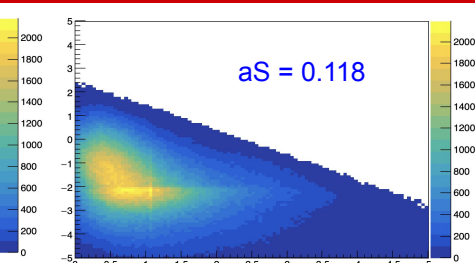
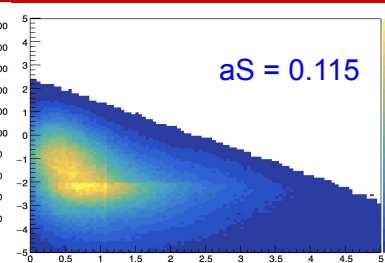
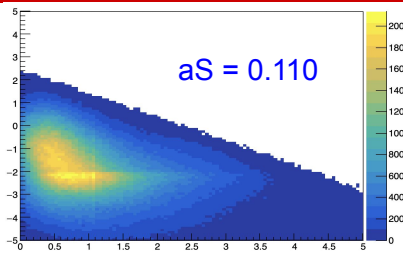
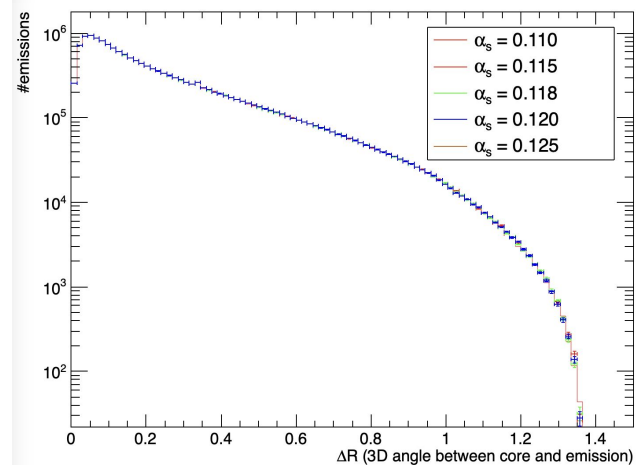
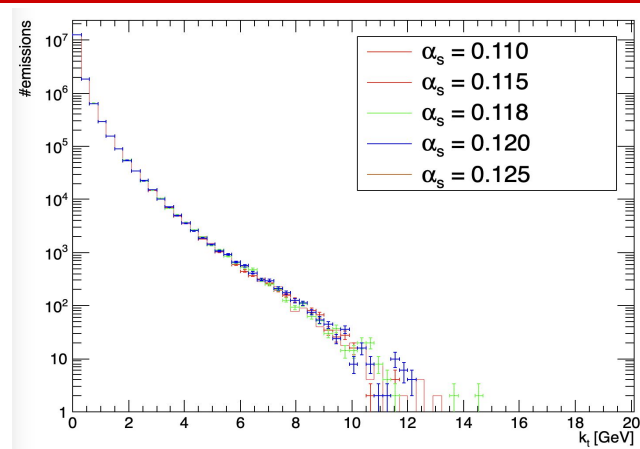


- Jet kinematics look as expected for  $Z \rightarrow uu/dd$  process at  $\sqrt{s} = 91 \text{ GeV}$

# Preliminary look at LJPs: Primary LJP



# Preliminary look at LJPs: Secondary LJP





# Angular order-based jet declustering in $(\theta, \phi)$ plane

- Use ee-dedicated Cambridge algorithm (**EECambridgePlugin**); Implemented in code with help from fastjet experts ([link](#))
- Setup is in place

## 5.4 Plugins for $e^+e^-$ collisions

[arXiv:1111.6097](#)

### 5.4.1 Cambridge algorithm

The original  $e^+e^-$  Cambridge [22] algorithm is provided as a plugin:

```
#include "fastjet/EECambridgePlugin.hh"  
// ...  
EECambridgePlugin (double ycut);
```

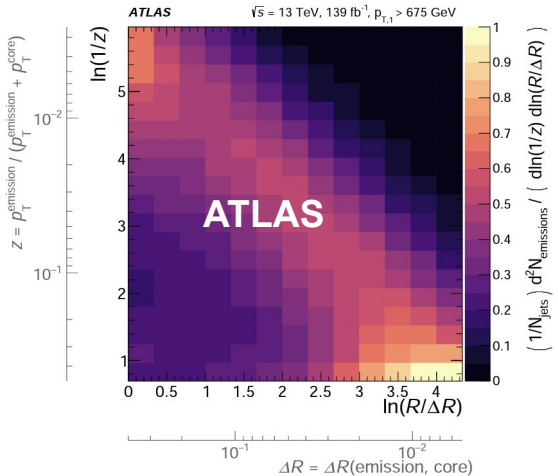
This algorithm performs sequential recombination of the pair of particles that is closest in angle, except when  $y_{ij} = \frac{2\min(E_i^2, E_j^2)}{Q^2}(1 - \cos\theta) > y_{cut}$ , in which case the less energetic of  $i$  and  $j$  is labelled a jet, and the other member of the pair remains free to cluster.

To access the jets, the user should use the `inclusive_jets()`, *i.e.* as they would for the majority of the  $pp$  algorithms.

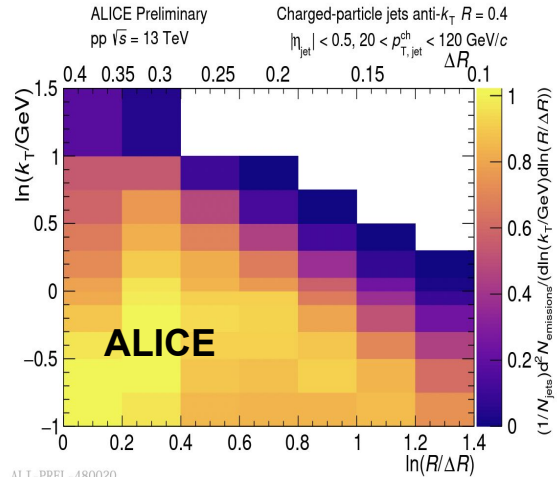
# Recent Lund Jet Plane based measurements

- LJP studies at LHC  $\sqrt{s} = 13$  TeV, following recent theoretical proposal ([JHEP 12 \(2018\) 064](#))
- These studies measure the lund plane density for charged particles jets
- We are interested in following the same for FCC-ee environment

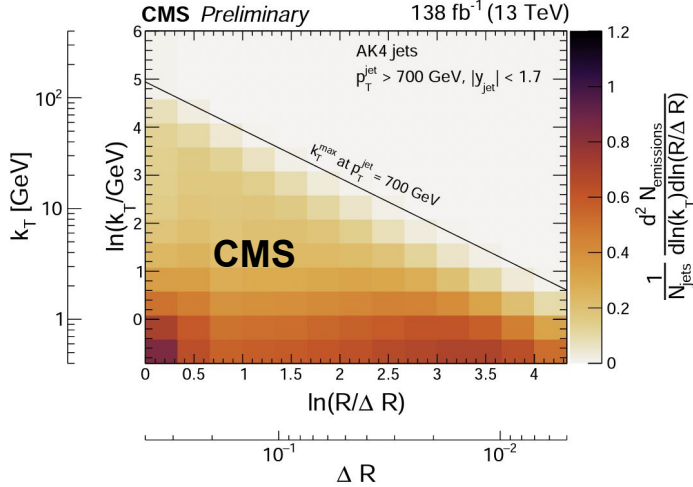
[arXiv 2004.03540](#)



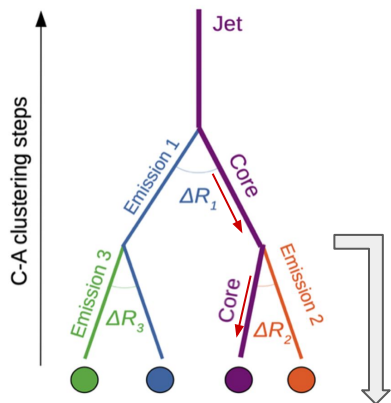
[arXiv 2111.00020](#)



[CMS-PAS-SMP-22-007](#)



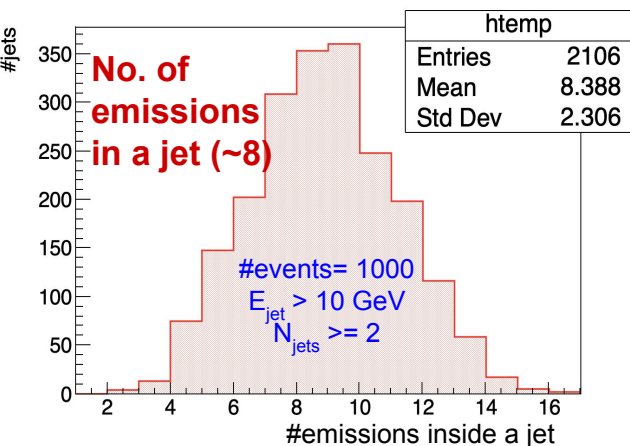
# How to build Primary Lund Jet Plane?



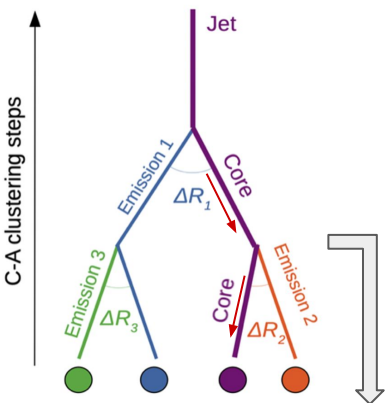
For  $R=1.5$  jets  
clustered with  $k_t$   
algorithm (Kt15)

$ee \rightarrow Z \rightarrow uu/dd @91 \text{ GeV}$

## Emissions from the core branches



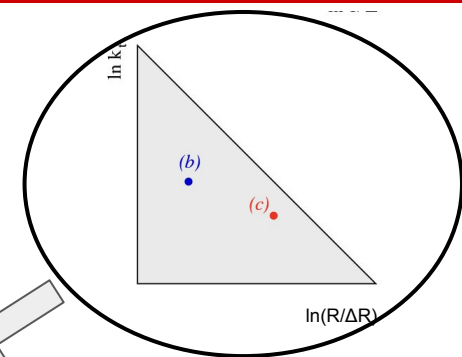
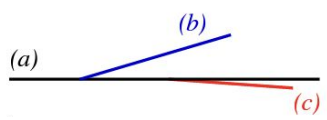
# How to build Primary Lund Jet Plane?



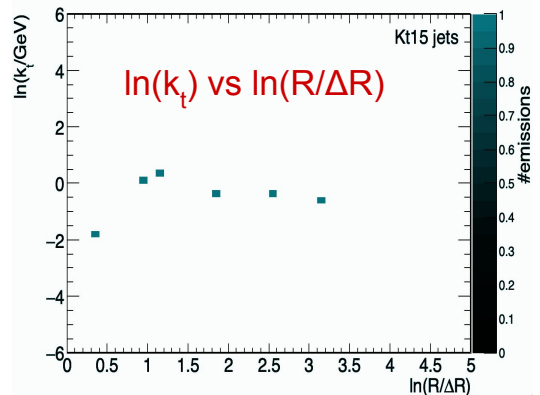
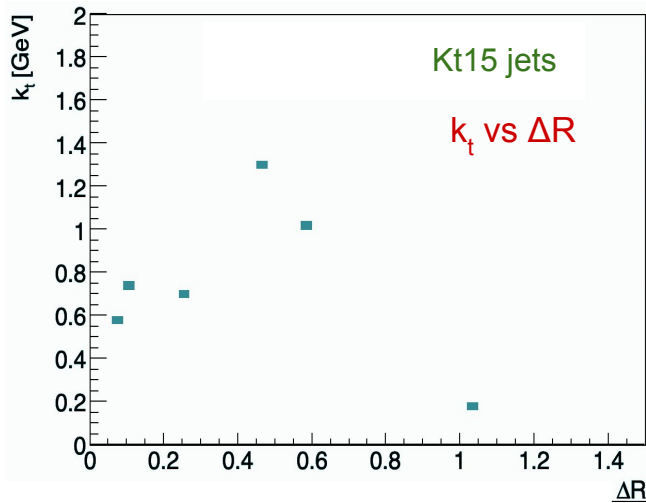
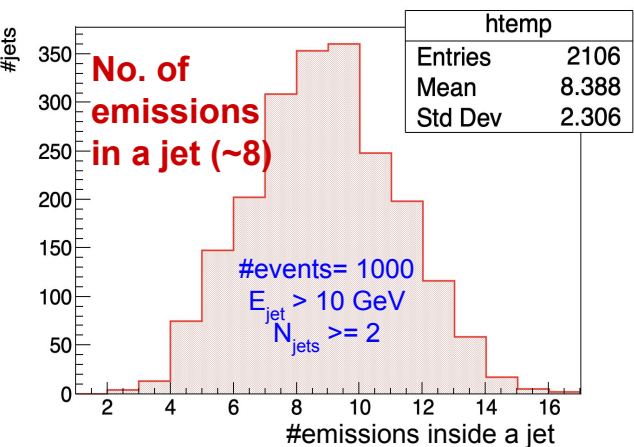
For  $R=1.5$  jets clustered with  $k_t$  algorithm (Kt15)

$ee \rightarrow Z \rightarrow uu/dd$  @91 GeV

JET



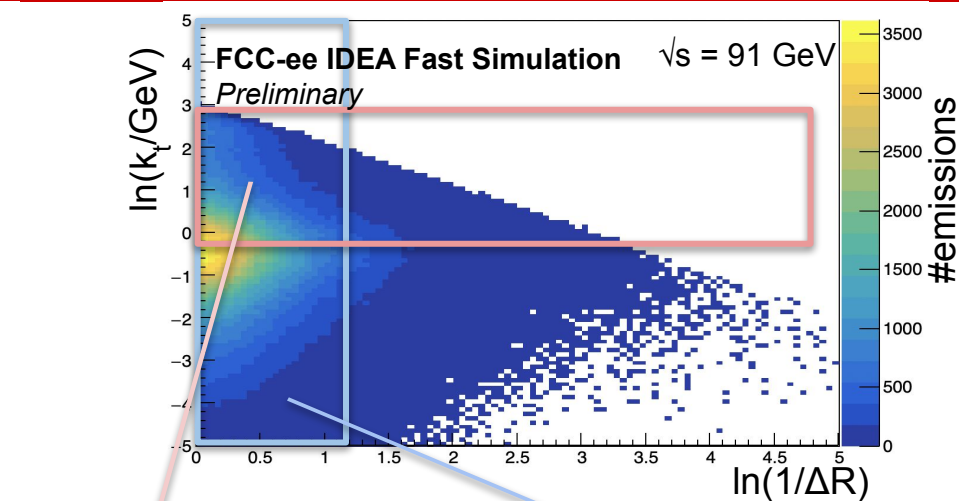
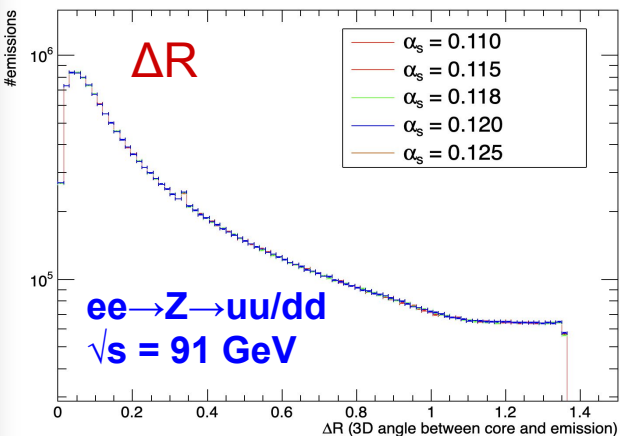
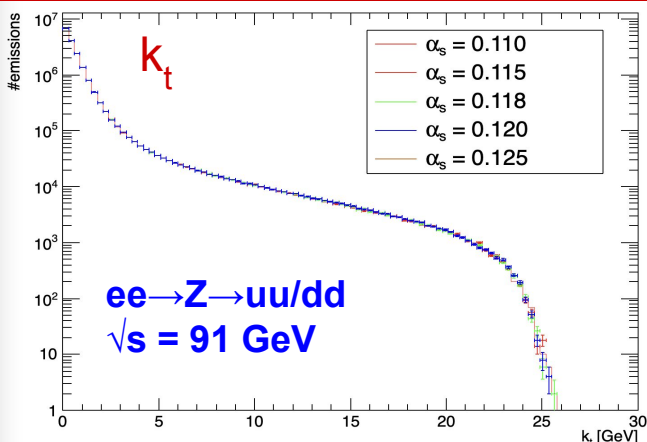
Emissions from the core branches



LJP representation for 1 jet of  $E_{jet} \sim 40$  GeV

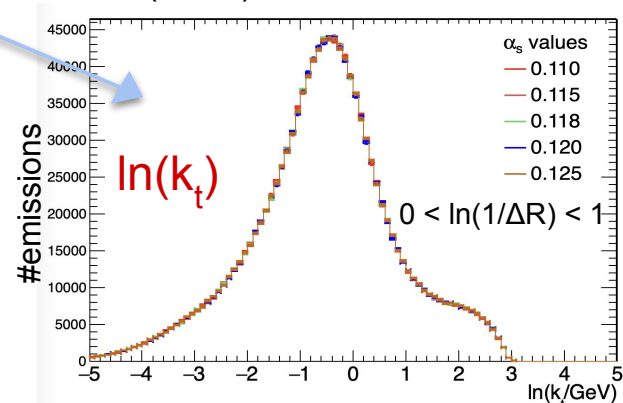
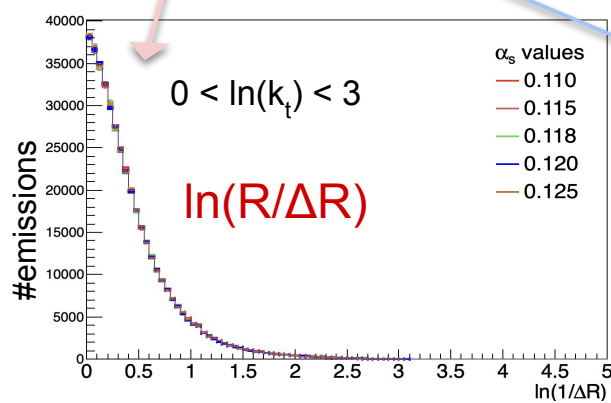
(both plots represent the same jet w/ and w/o log scale)

# Preliminary look at LJPs: Primary LJP

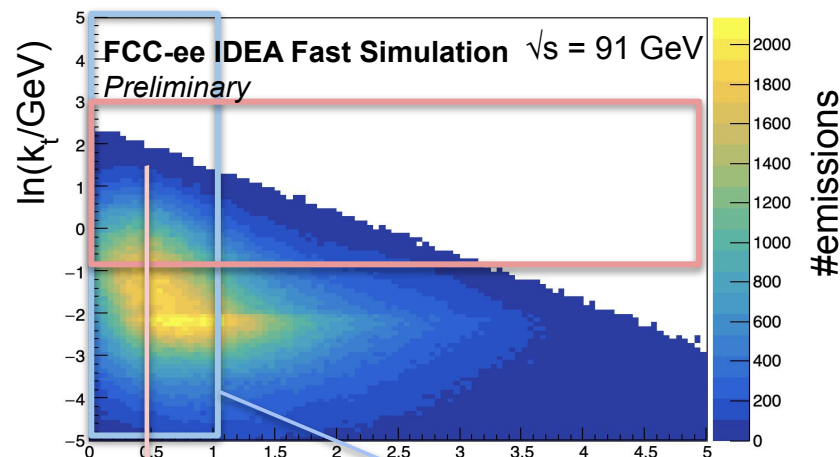
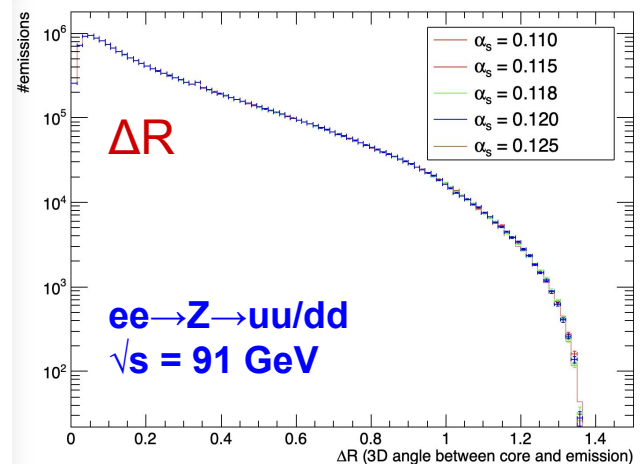
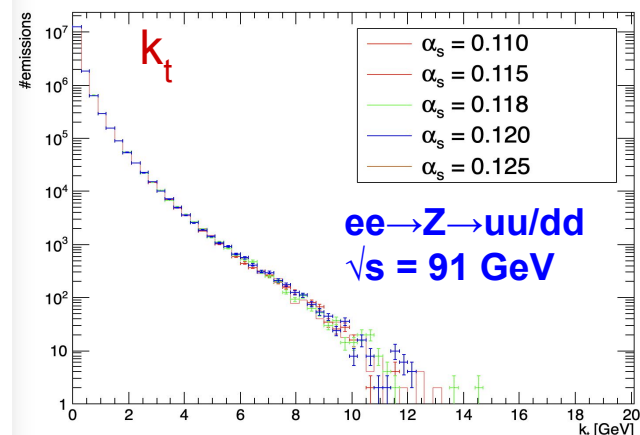


Selections:  
 $E_{\text{jet}} > 10 \text{ GeV}$   
 $\#\text{jets} > 1$

Other LJPs  
with different  
 $\alpha_s$  in backup

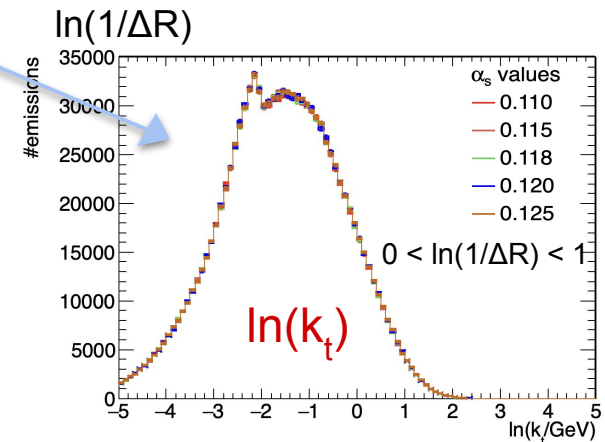
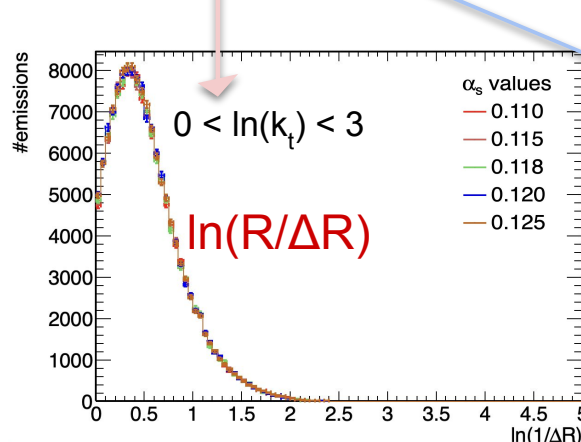


# Preliminary look at LJPs: Secondary LJP

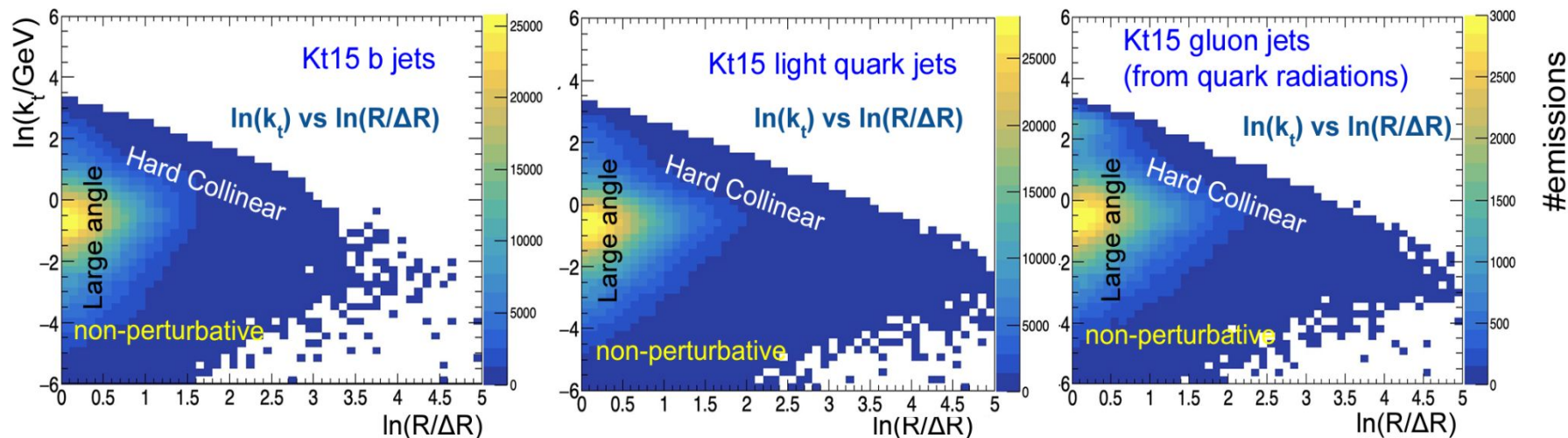


**Selections:**  
 $E_{\text{jet}} > 10 \text{ GeV}$   
 $\#\text{jets} > 1$

Other LJPs  
 with different  
 $\alpha_s$  in backup



# LJP representation for light and heavy flavor jets at higher energy



- For process  $ee \rightarrow Z \rightarrow bb$  and  $ee \rightarrow Z \rightarrow uu/dd$  (+ gluons from quark radiation) @91 GeV ;  
#events = 1 M
- Selection:  $E_{\text{jet}} > 10$  GeV,  $N_{\text{jets}} \geq 2$ ; selection efficiency > 99%; use two leading  $p_T$  jets
- Difference in the large  $\ln(R/\Delta R)$  region shows that light jets are more collimated than heavy flavour jets; working on further understanding in more detail