

**Expected precisions on the Higgs boson mass and ZH production
cross section at $\sqrt{s}=240$ & 365 GeV
at the Future e+e- Circular Collider (FCC-ee)**

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for the

FCC collaboration

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The FCC integrated program (ee + hh) at CERN goes beyond the successful LEP + LHC (1976-2041) program

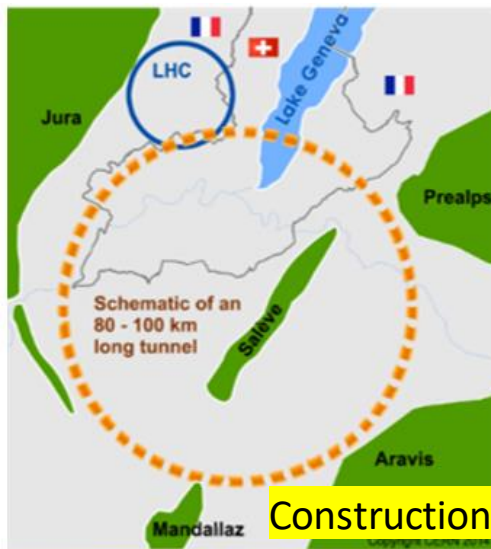
Comprehensive cost-effective program maximizing physics opportunities

- **Construction:** during HL-LHC data-taking
- **Stage 1:** FCC-ee (Z, W, ZH, tt) as first generation Higgs, EW and top e^+e^- factory at highest luminosities.
- **Stage 2:** FCC-hh (~ 100 TeV) as natural continuation at energy frontier

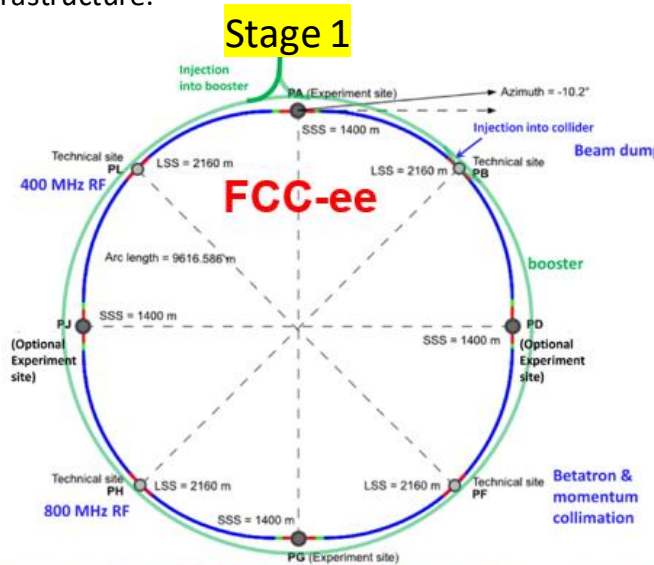
Complementary physics

- Integrating an ambitious high-field magnet R&D program
- Common civil engineering and technical infrastructures
- Building on and reusing CERN's existing infrastructure.

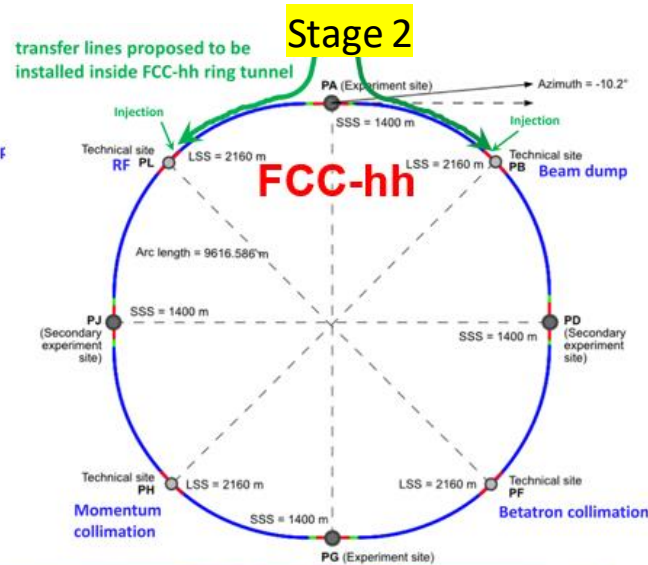
The FCC project is fully integrated with HL-LHC exploitation and provides a natural transition for higher precision and energy



2020 - 2040

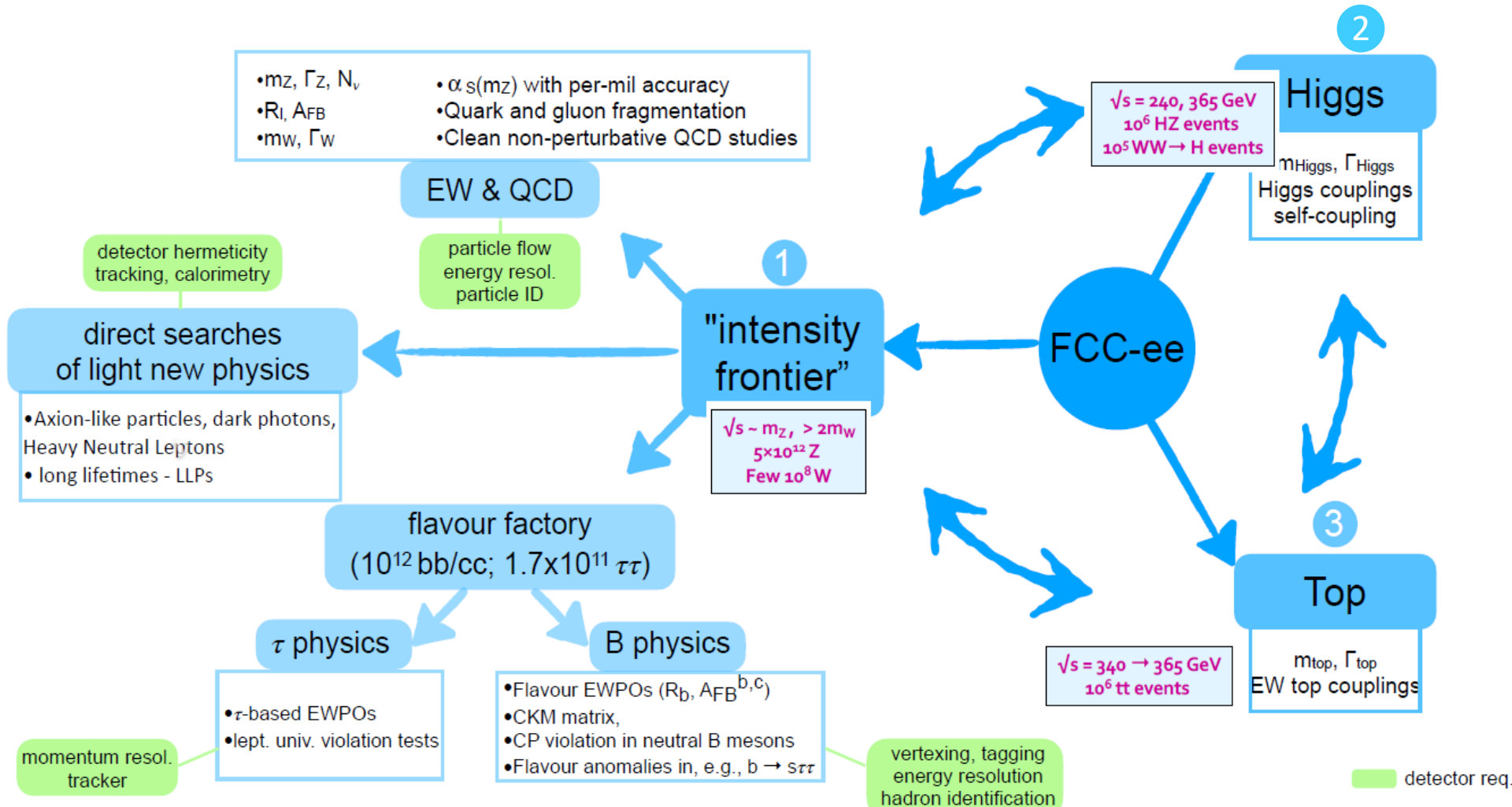


2045 - 2060



2065 - 2090

at Circular Colliders → Rich e^+e^- Physics Program ...



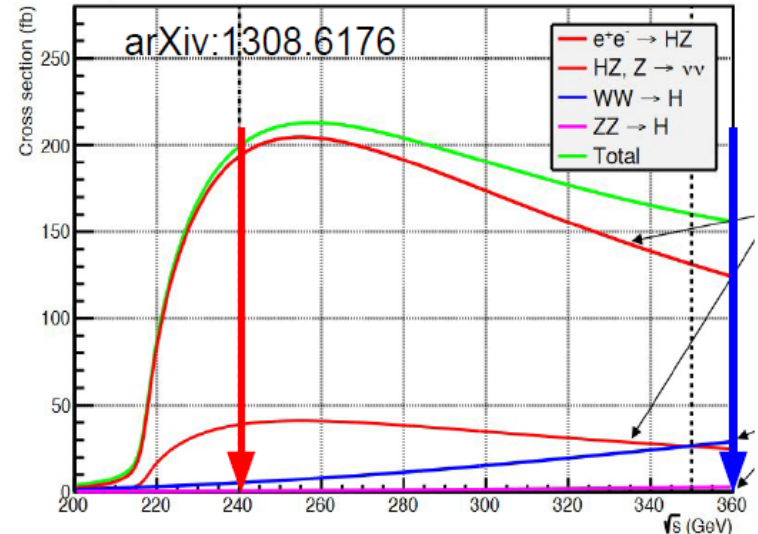
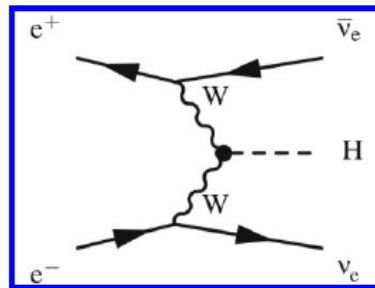
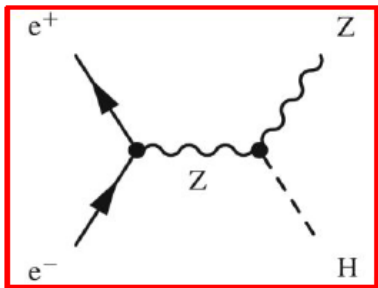
FCC-ee offers broad potential for precision Higgs measurements

- Higgs factory: production of **2M Higgs** bosons
- Clean environment
- Relative small backgrounds, **large S/B**

Total Higgs production @ FCC-ee (baseline – 4 IP)		
Threshold	ZH production	VBF production
240 GeV / 10.8 ab⁻¹	2.2 M	67 k
365 GeV / 3 ab⁻¹	330 k	80 k

Main production mechanisms

- **ZH production** “Higgs–strahlung”
- **Vector boson fusion** (VBF), WW dominant



Higgs Physics at the ZH threshold

Highest precision obtained from ZH analyses @ 240 GeV

Main strategy of such analyses based on recoil method

- Tag the Z boson (tight invariant mass constraints) using leptons or jets
- Compute **recoil**, distribution sharp peaked at Higgs mass, **width**

dominated by detector resolution

$$m_{recoil}^2 = (\sqrt{s} - E_{ff})^2 - p_{ff}^2$$

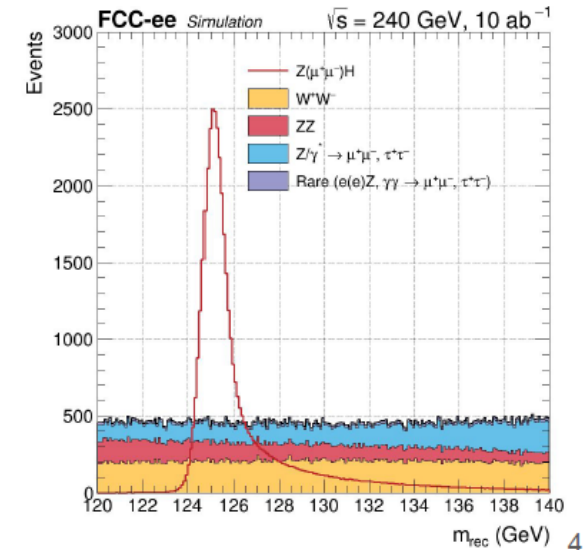
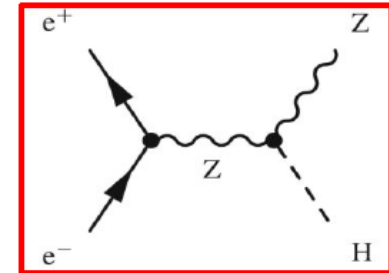
$$= s + m_Z^2 - 2E_{ff}\sqrt{s} \approx m_H^2$$

- tag additional decays of the Higgs – challenging in multijet environment

Backgrounds: dominated by vector boson (pair) production (WW, ZZ) and Z/ γ^*

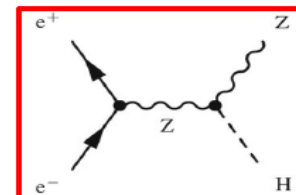
Challenges for the Higgs programme

- Detector performance: tracking, vertexing, timing, angular
- Flavour tagging for Higgs couplings
- Jet clustering algorithms (in particular in fully hadronic final states)



$$m_{recoil} \in [120, 140] \text{ GeV}$$

The total ZH cross section measurement



$$\sigma(e^+e^- \rightarrow ZH) \propto g_{HZZ}^2$$

absolute HZZ coupling meas.

Crucial is to measure HZZ coupling strength in a model-independent way

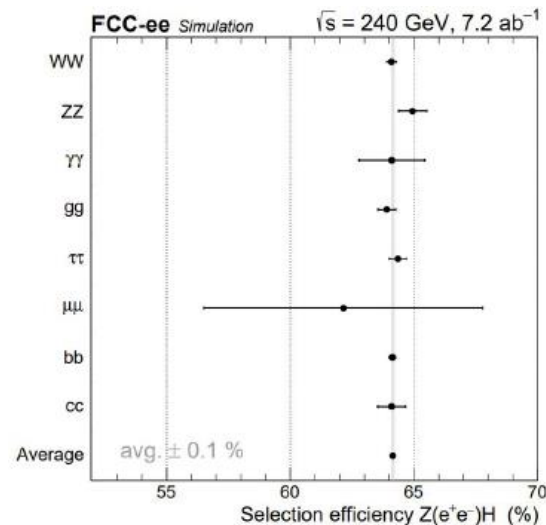
- unique to e^+e^- colliders because of known initial state, not possible at hadron colliders
- challenge to ensure **model-independence**
- once known, **determines couplings to $H \rightarrow XX$** in a model independent way

Example analysis in Z(ll)H(XX) final state

Probe electron and muon final states

- Clean and sharp recoil distribution
- Cutflow + MVA to reduce backgrounds
- Can minimize the model-dependency

Z(qq)H(XX) to be explored to bring uncertainty down, but challenging to retain model-independence



Using Fast simulation **DELPHES**:

➤ **Signal:**

- $Z(\mu^+\mu^-)H$ (Whizard/Pythia)

➤ **Backgrounds:**

- W^+W^- (Pythia)

- e^+e^-Z (Whizard/Pythia)

- ZZ (Pythia)

- $Z/\gamma \rightarrow \mu^+\mu^-$ (Whizard/Pythia)

➤ **Rare backgrounds:**

- $Z(qq)$ (Pythia)

- $Z(\tau^+\tau^-)H$ (Whizard/Pythia)

- $Z(\nu\nu)H$ (Whizard/Pythia)

- $\gamma\gamma \rightarrow \mu^+\mu^-$ (Whizard/Pythia)

- $\gamma\gamma \rightarrow \tau^+\tau^-$ (Whizard/Pythia)

➤ **Events basic selection:**

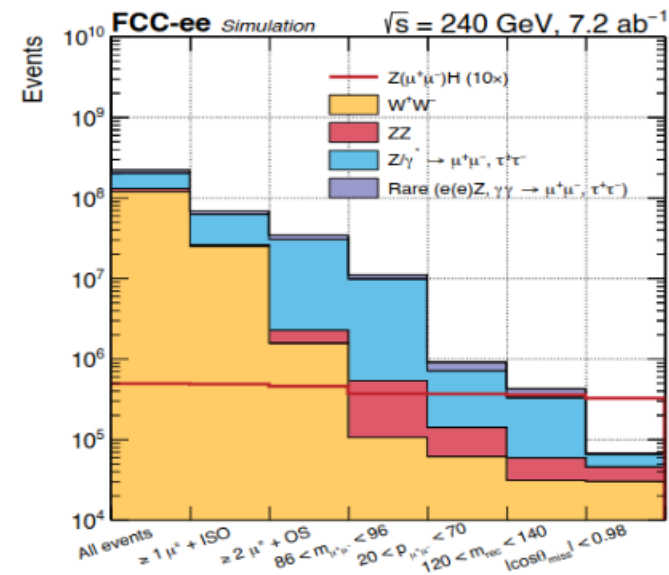
Preselection: Select at least 2 leptons:

- Opposite sign
- One lepton required to be isolated

$m_{l^+l^-} \in [86, 96]$ GeV

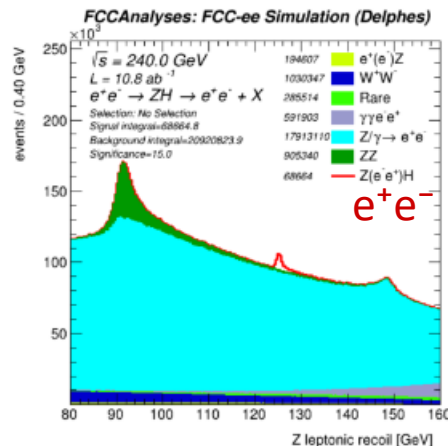
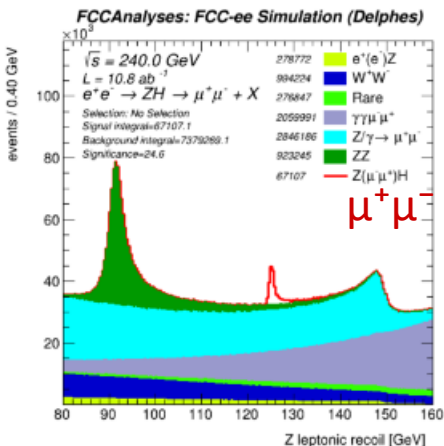
$p_{l^+l^-} \in [20, 70]$ GeV (> 20 GeV at 365 GeV)

$m_{recoil} \in [120, 140]$ GeV

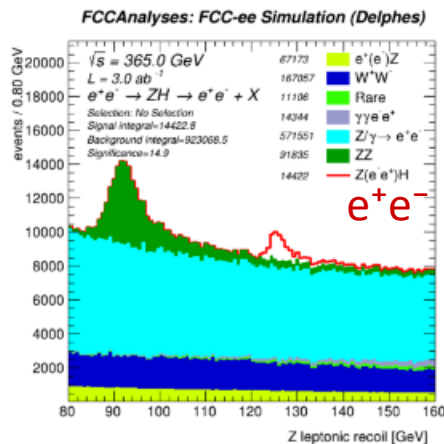
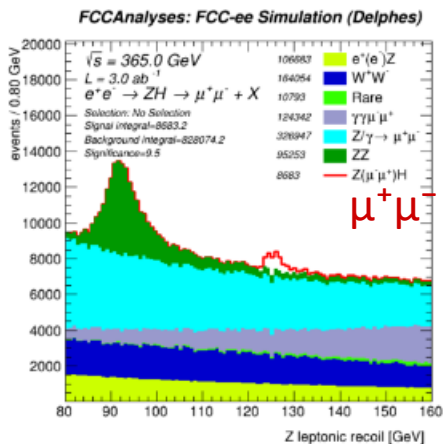


Comparison 240/365 GeV with Preselection Cuts (zoom)

240 GeV
⇒

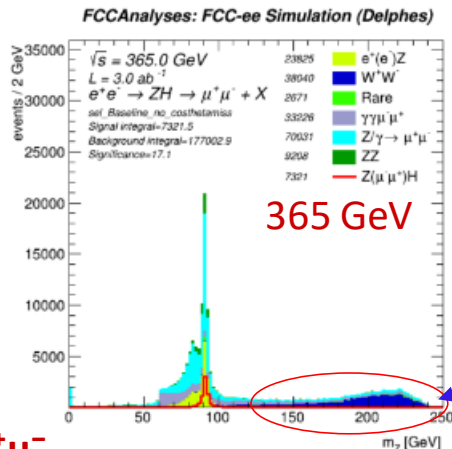
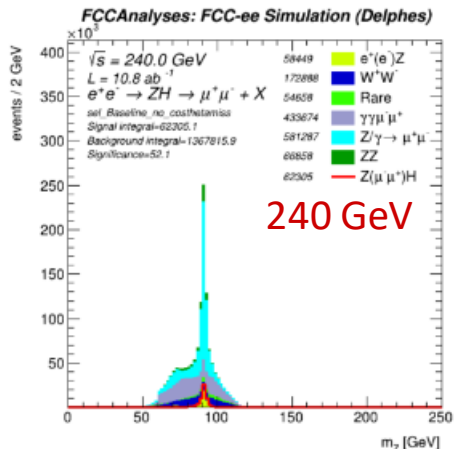


365 GeV
⇒



- Zoom between 80 and 160 GeV
- Luminosity is **10.8** ab^{-1} at $\sqrt{s}=240$ GeV
3.0 ab^{-1} at $\sqrt{s}=365$ GeV
- Different shapes of the background before selection cuts
- Signal peak has **lower resolution** but also less background at 365 GeV

Invariant Mass and Recoil Mass distributions



$\mu^+\mu^-$

➤ Basic event selection:

Pre-selection (2 leptons opposite sign)

+

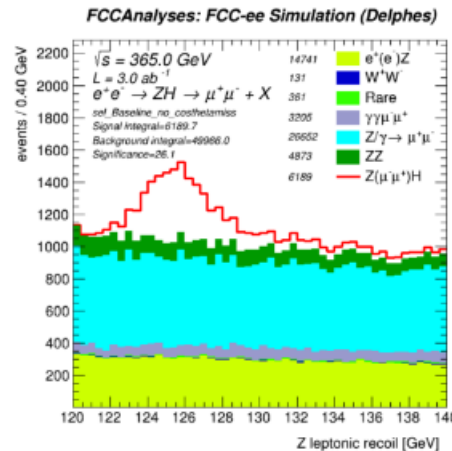
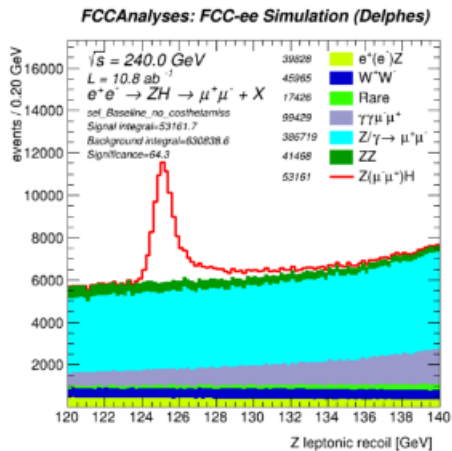
$$m_{l^+l^-} \in [86, 96] \text{ GeV}$$

$$p_{l^+l^-} \in [20, 70] \text{ GeV} \quad (>20 \text{ for } \sqrt{s}=365 \text{ GeV})$$

$$m_{recoil} \in [120, 140] \text{ GeV}$$

➤ **WW becomes negligible** at $\sqrt{s}=365 \text{ GeV}$

Since it « moves » to higher invariant masses and the cut on the Z-mass removes it



➤ Resolution ~ 2.3 times wider at $\sqrt{s}=365 \text{ GeV}$

S/B still needs to be improved to gain precision

- BDT for model independent analysis, ZH cross section
- Cos θ_{miss} cut for Higgs mass analysis

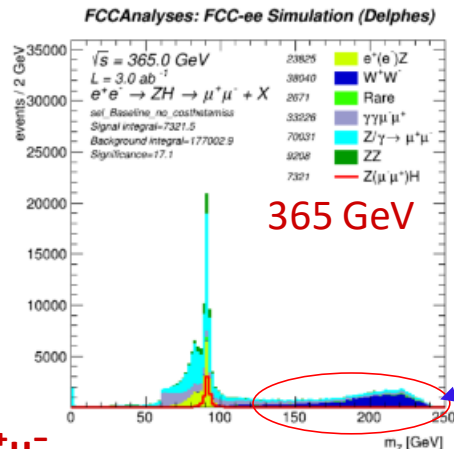
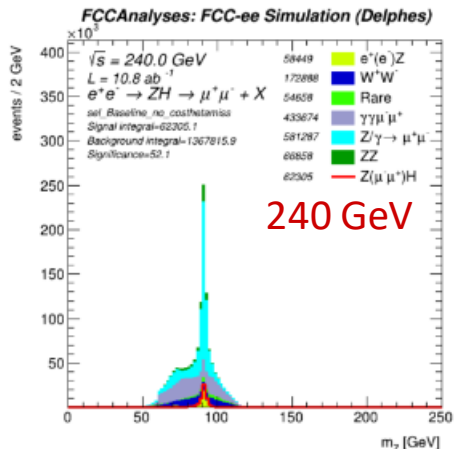
Invariant Mass Distribution

⇒

Recoil Mass Distribution

⇒

Invariant Mass and Recoil Mass distributions



➤ Basic event selection:

Pre-selection (2 leptons opposite sign)

+

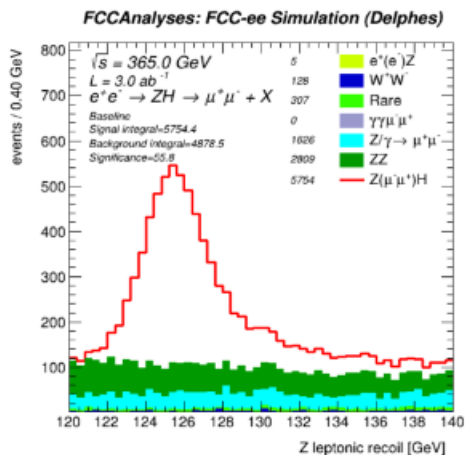
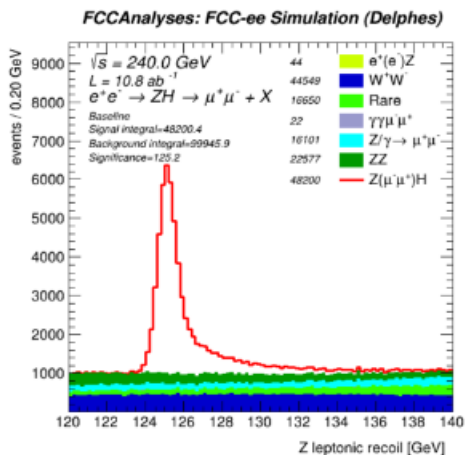
$m_{l^+l^-} \in [86, 96] \text{ GeV}$

$p_{l^+l^-} \in [20, 70] \text{ GeV}$ (>20 for $\sqrt{s}=365 \text{ GeV}$)

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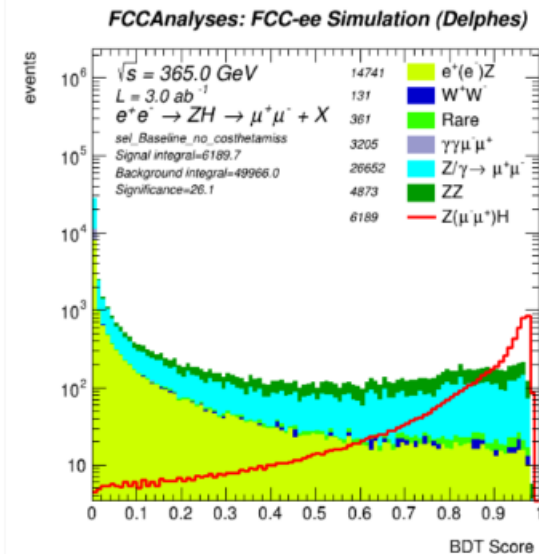
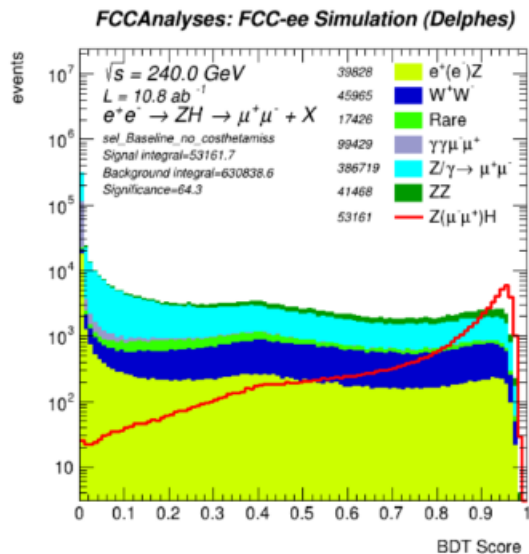
➤ Resolution ~ 2.3 times wider at $\sqrt{s}=365 \text{ GeV}$

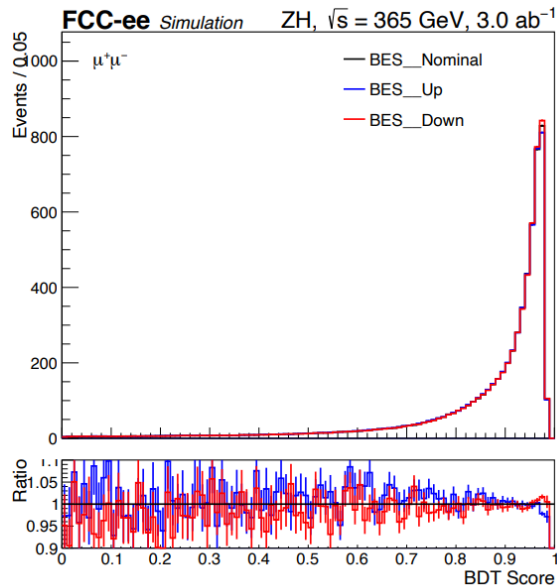
With Cos theta_{miss} cut for Higgs mass analysis, Background strongly reduced

Boosted Decision Tree used for σ_{ZH} analysis

- Use of a Machine learning algorithm to **separate signal** from **background**, a Boosted Decision Tree (BDT)
- The BDT, using only variables from the leptons of the Z, allows for a **model independent** analysis
- Training_variables for BDT:
- **BDT Score comparison** between 365 and 240 GeV
- This **BDT score** is **fitted** to measure the **ZH cross-section value**

Variable	Description
$p_{\ell^+\ell^-}$	Lepton pair momentum
$\theta_{\ell^+\ell^-}$	Lepton pair polar angle
$m_{\ell^+\ell^-}$	Lepton pair invariant mass
$p_{l_{\text{leading}}}$	Momentum of the leading lepton
$\theta_{l_{\text{leading}}}$	Polar angle of the leading lepton
$p_{l_{\text{subleading}}}$	Momentum of the subleading lepton
$\theta_{l_{\text{subleading}}}$	Polar angle of the subleading lepton
$\pi - \Delta\phi_{\ell^+\ell^-}$	Acoplanarity of the lepton pair
$\Delta\theta_{\ell^+\ell^-}$	Acolinearity of the lepton pair





➤ **Beam energy spread, depends on the beam energy.**

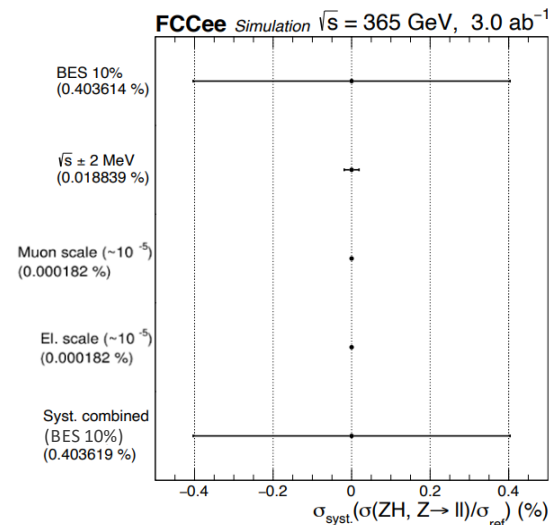
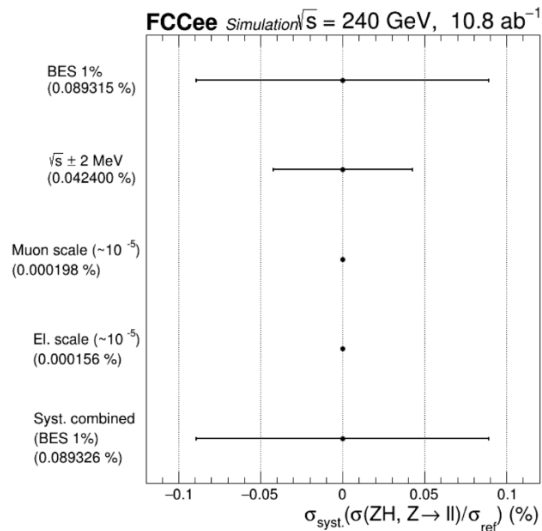
At a center-of-mass energy of 240 (365) GeV, the beam energy spread (BES) is $\pm 0.185\%$ ($\pm 0.221\%$) per beam, i.e. ± 222 (± 403) MeV.

Uncertainty assumed on the BES value is **~1%** at 240 GeV and **~10%** at 365 GeV → Dominant systematic for ZH cross section measurement

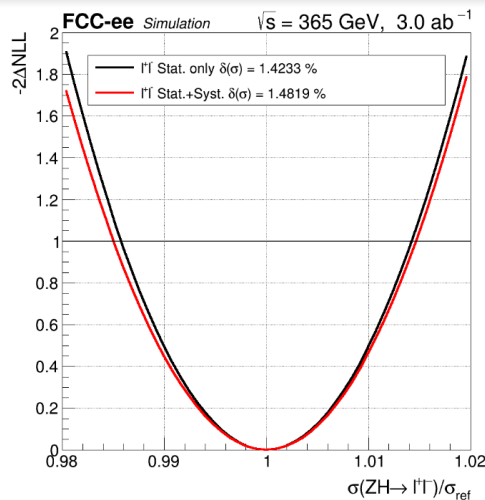
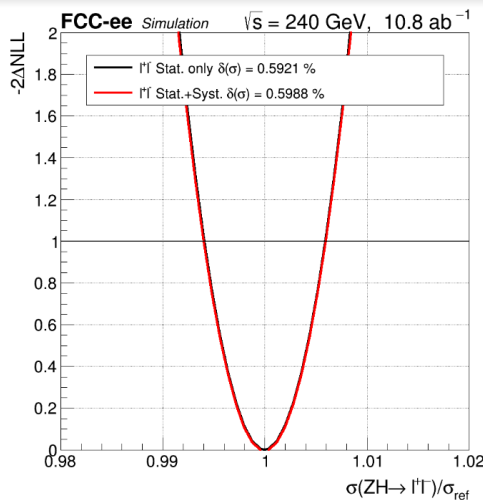
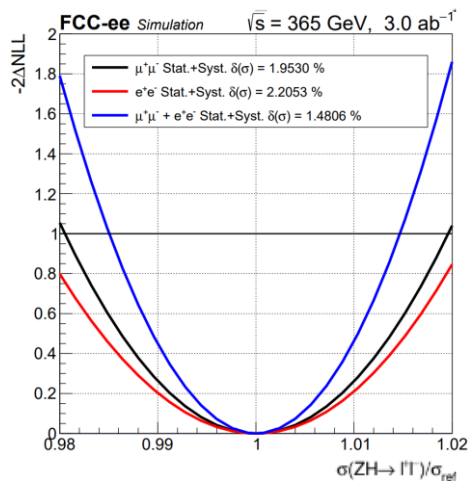
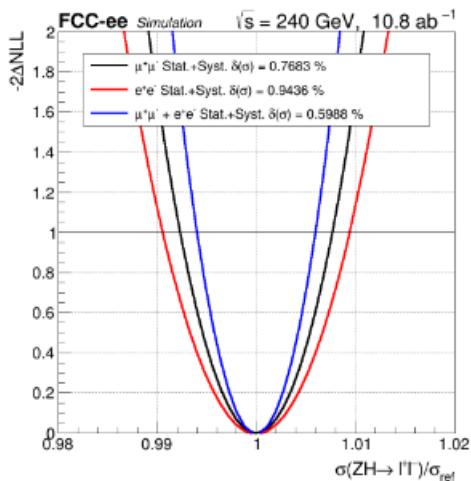
➤ **ISR uncertainty** is not estimated precisely yet, but expected to be smaller

➤ **Centre-of-mass (\sqrt{s}):** Uncertainty on the centre-of-mass energy which is expected to be known at the **~2 MeV** level for 240 and 365 GeV

➤ **Lepton momentum scale:** Uncertainty from the momentum of leptons assumed to be known at **10^{-5}** precision level both for 240 and 365 GeV



ZH cross-section measurements ($\mu^+\mu^-$, e^+e^- and combined) at $\sqrt{s}=240$ & 365 GeV



- By fitting the BDT output we obtain the cross-section, with its **statistical** and **stat+systematics** uncertainties.
- **1.42%** Statistical uncertainty at $\sqrt{s}=365$ GeV compared to **0.59%** at $\sqrt{s}=240$ GeV
- **1.48%** Stat+Syst uncertainties at $\sqrt{s}=365$ GeV compared to **0.60%** at $\sqrt{s}=240$ GeV
- **Systematics are larger at 365 GeV, but ZH cross section precision still dominated by statistics**
- **Intrinsic sensitivity is similar (~25% larger) at 365 GeV vs. 240 GeV for ZH cross section, contrarily to the mass measurement where the difference is much larger (see below)**

Higgs Mass Measurements

Higgs mass enters SM EWK parameters via radiative corrections, depending logarithmically on m_H , e.g.

$$\sin^2 \theta_W = \left(1 - \frac{M_W^2}{M_Z^2}\right) = \frac{A^2}{1 - \Delta r}$$

$$\begin{aligned} \Delta r &\sim \ln(m_H) \\ \Delta r &\sim m_t^2 \\ \Delta r &\sim \text{new physics?} \end{aligned}$$

Needs for FCC-ee

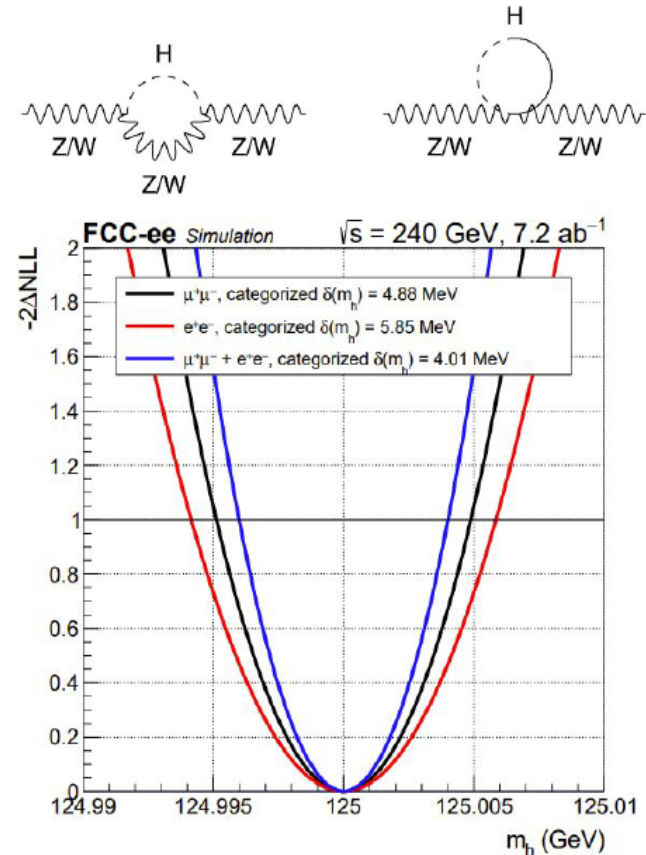
- Very high precision on cross-sections, sub-percent level
- This translates to a Higgs mass requirement $< O(10)$ MeV to control the radiative corrections for the cross-sections and branching fractions

Roadmap for ultimate precision on Higgs mass

TODAY
~ 150 MeV

HL-LHC
~ 20 MeV

FCC-ee
~ 4 MeV



Together with precise Top and W/Z masses, Higgs mass will provide stringent test of the Standard Model

Higgs Mass Analysis and Studies

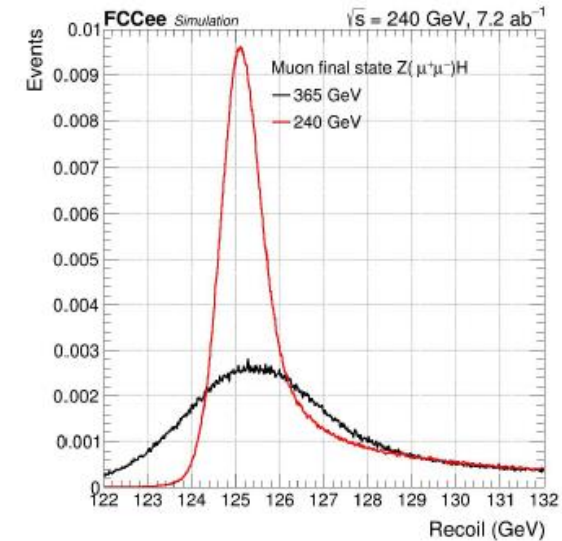
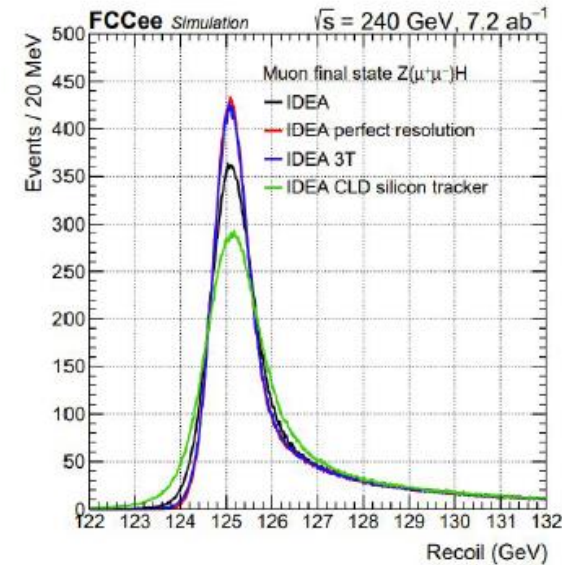
Higgs mass extracted from fitting recoil distribution

$$M_{recoil}^2 = (\sqrt{s} - E_{\bar{l}l})^2 - p_{\bar{l}l}^2 = s - 2E_{\bar{l}l}\sqrt{s} + m_{\bar{l}l}^2$$

- Muon and electron final states
- Tight event selection (follow closely the ZH cross-section selection)
- Categorize in central and forward regions to probe different material budget
 - In total 3 categories: central, forward, central+forward
- Done at center-of-mass 240 and 365 GeV
 - Limited sensitivity at 365 due to small statistics, higher BES and ISR

Simultaneous fit over all the 12 categories (2 flavor, 3 angular categories, 2 ECM)

Final state		Muon	Electron	Combination
Categorized	(7.2 ab ⁻¹ + 3.0 ab ⁻¹)	4.79(5.50)	6.06(6.68)	3.76(4.53)
Inclusive	(7.2 ab ⁻¹ + 3.0 ab ⁻¹)	4.83(5.51)	6.15(6.70)	3.80(4.54)

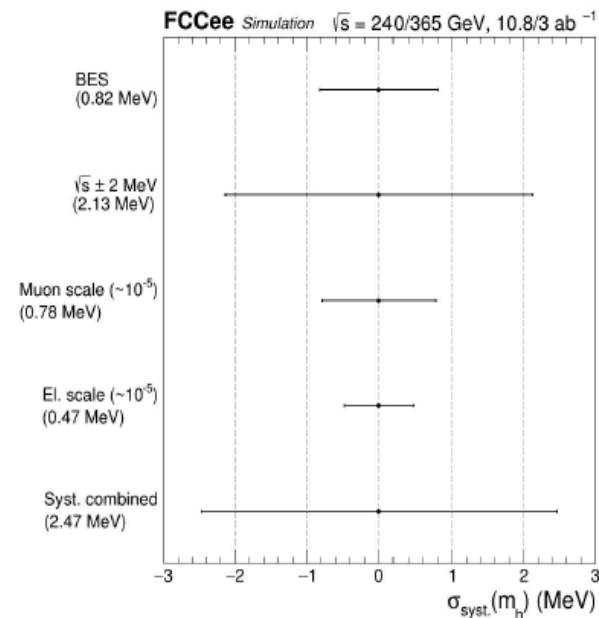
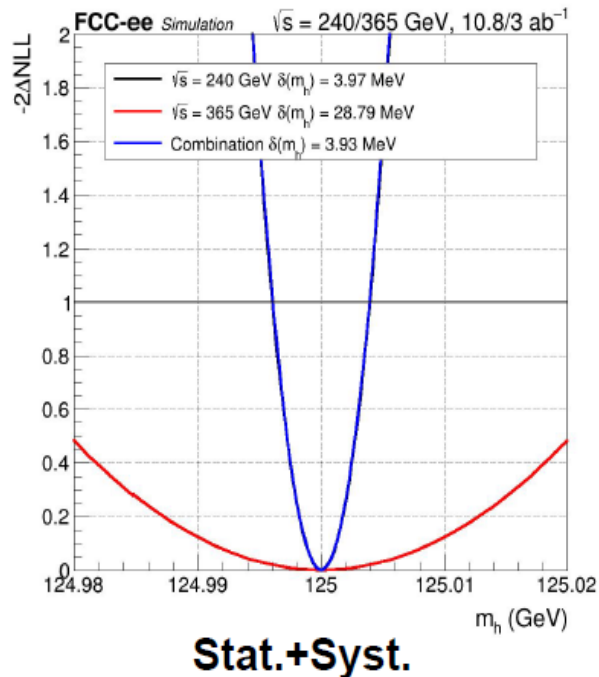
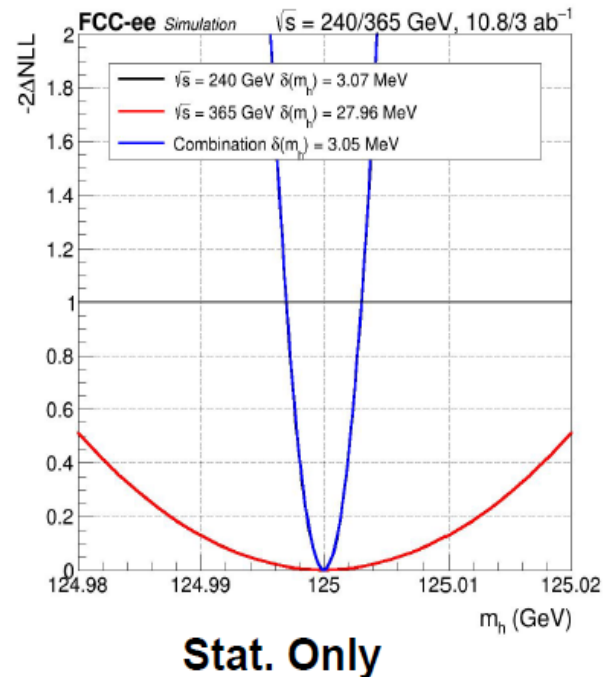


Using 10.8 ab⁻¹ (240 GeV) and 3 ab⁻¹ (365 GeV)

- Current combined uncertainty: 3.05(3.93) MeV
- Systematics contribute ~2.5 MeV, ecm uncertainty dominant
- Improvement by adding 365 GeV ~ 1%

Systematics:

For the Higgs mass, the systematic uncertainty is dominated by the uncertainty on the c.o.m energy



at 240 GeV, 10.8 ab⁻¹

Nominal configuration

Crystal ECAL to Dual Readout

Nominal 2 T → field 3 T

IDEA drift chamber → CLD Si tracker

Impact of Beam Energy Spread

Perfect (=gen-level) momentum resolution

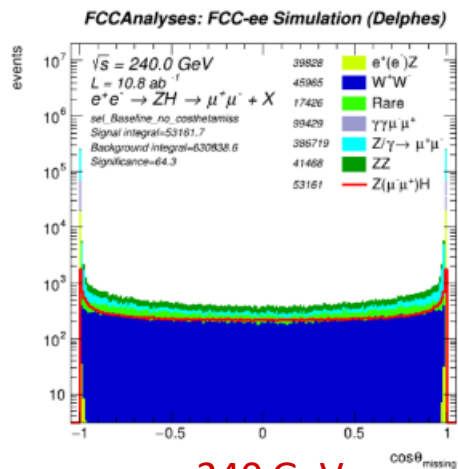
Final state	Muon	Electron	Combination
Nominal	3.92(4.74)	4.95(5.68)	3.07(3.97)
Categorized	3.92(4.74)	4.95(5.68)	3.10(3.97)
Degradation electron resolution			3.24(4.12)
Magnetic field 3T	3.22(4.14)	4.11(4.83)	2.54(3.52)
Silicon tracker	5.11(5.73)	5.89(6.42)	3.86(4.55)
BES 6% uncertainty	3.92(4.79)	4.95(5.92)	3.07(3.98)
Disable BES	2.11(3.31)	2.93(3.88)	1.71(2.92)
Ideal resolution	3.12(3.95)	3.58(4.52)	2.42(3.40)
Freeze backgrounds	3.91(4.74)	4.95(5.67)	3.07(3.96)
Remove backgrounds	3.08(4.13)	3.51(4.58)	2.31(3.45)

- we want to get down to $\Delta m_H \sim \Gamma_H \sim 4 \text{ MeV}$ to allow for electron Yukawa at $\sqrt{s} = 125 \text{ GeV}$
- as expected, tracking resolution highly impacts m_H precision
- light tracker/ **high B field** highly preferable

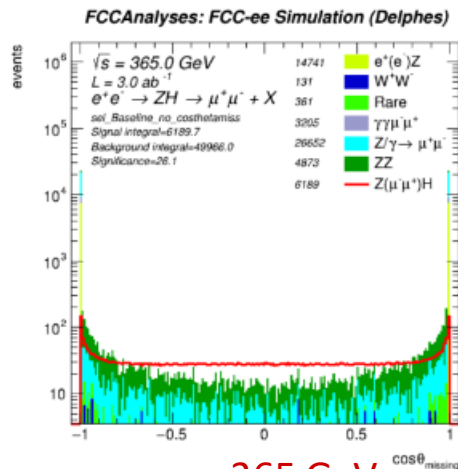
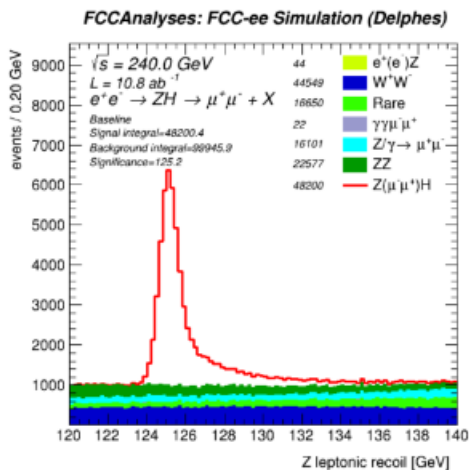
Summary

- The ZH cross section and the Higgs boson masses expected measurements have been presented at 240 GeV and at 365 GeV c.o.m.
- σ_{ZH} is measured in a model independent way with 0.6% accuracy at 240 GeV,
1.5% at 365 GeV
opening the way to precise Higgs couplings measurements
- The Higgs boson mass is measured with 4.0 MeV accuracy at 240 GeV,
3.9 MeV when adding 365 GeV
allowing for precise tests of the SM
- Systematics and detector constraints have been studied and presented, and will help to determine the best detector configurations for FCC-ee in the FCC feasibility study

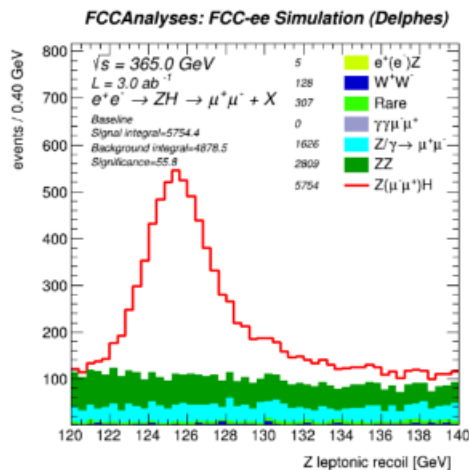
Comparison 240/365 GeV after Selection Cuts



240 GeV



365 GeV



- The requirement $|\cos \theta_{\text{missing}}| < 0.98$ is used for the **mass analysis only**
- θ_{missing} is the **polar angle of the missing momentum vector** with respect to the beam axis
- This requirement is removing the large background concentrated in the **last bins**. The remaining background becomes small
- This Introduces **biases** on the Higgs decay modes that break the **model independence**, which is not crucial for the mass analysis
- Width of the recoil mass becomes more than 2 times larger at 365 GeV (due to BES and lepton momentum resolution)
 - ➔ Significant loss in mass precision

Cos θ_{missing} Distribution



Recoil Mass Distribution



Missing momentum polar angle

- The **missing momentum** is defined by the **negative vectorial sum** of the momenta of all reconstructed particles:

$$\vec{p}_{miss} = - \sum_{n_{part}} \vec{p}_{rec}$$

- $\Theta_{missing}$ is the **polar angle** of the **missing momentum vector** with respect to the **beam axis**
- The requirement $|\cos \Theta_{missing}| < \mathbf{0.98}$ is used for the **mass analysis only**, which means that we are removing events mostly collinear to the beam axis

