



tau polarisation in  $e^+ e^- \rightarrow \tau^+ \tau^-$

work in progress

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ECFA meeting, October 2024



why study this process ?

high statistics, simple process

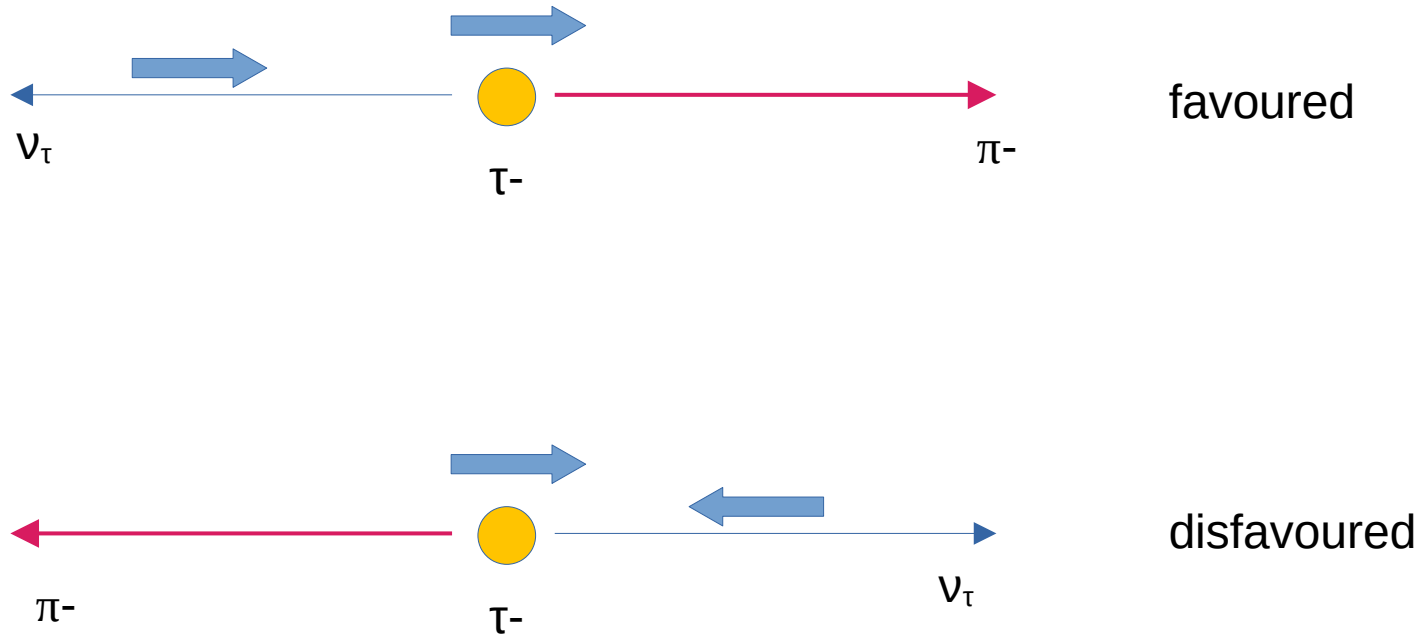
→ precise test of SM

access to tau spin

→ unique handle [together with  $e^+ e^- \rightarrow t \bar{t}$ ]

what are the detector requirements ?

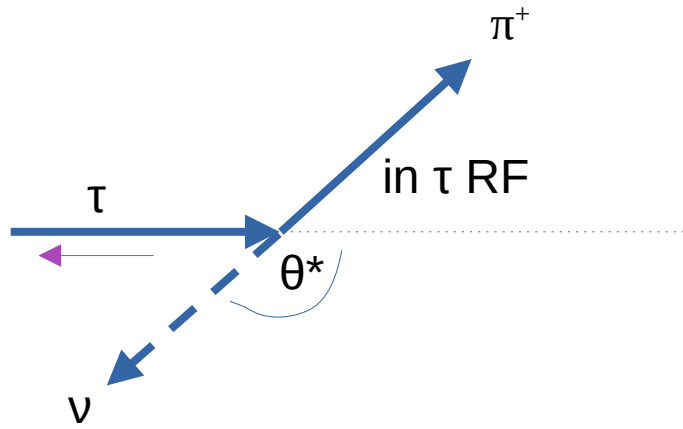
distribution of tau decay products reflect tau's spin orientation



in this simplest tau decay, optimal spin direction estimator “**polarimeter**”

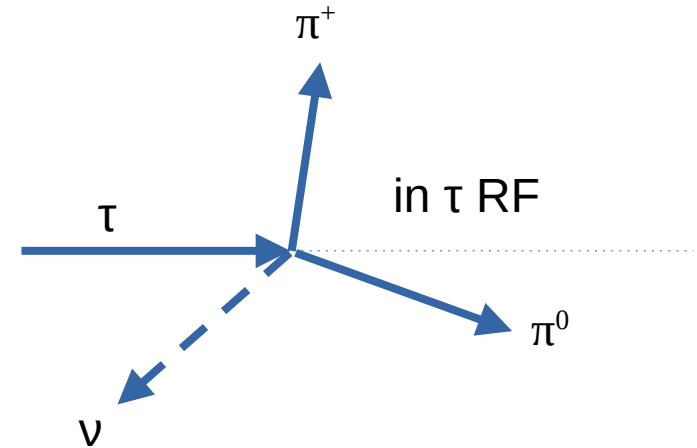
is the pion (or neutrino) momentum direction in the tau rest frame

# tau polarimeter : estimator of spin orientation



neutrino carries tau's angular momentum  
**neutrino direction** is optimal polarimeter

**helicity**  $\sim$  longitudinal polarisation  $\sim \cos(\theta^*)$

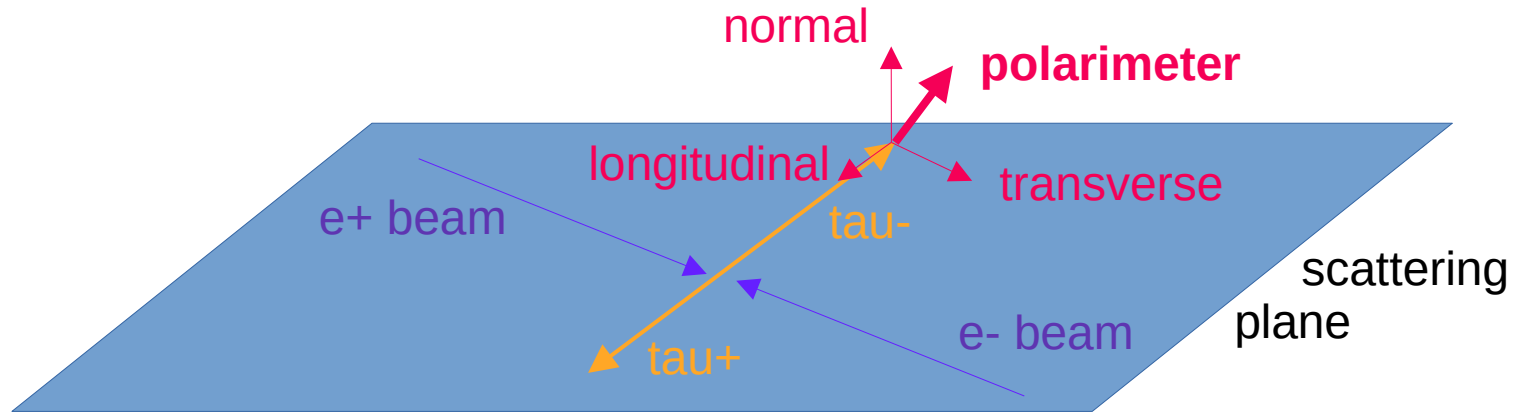


more complicated optimal polarimeter

$$\mathbf{h}(\tau^\pm \rightarrow \pi^\pm \pi^0 \nu) \propto m_\tau (E_{\pi^\pm} - E_{\pi^0}) (\mathbf{p}_{\pi^\pm} - \mathbf{p}_{\pi^0}) + \frac{1}{2} (p_{\pi^\pm} + p_{\pi^0})^2 \mathbf{p}_\nu,$$

to extract optimal polarimeters, need full decay kinematics, including  $\pi^0$ , neutrino  
 in principle polarimeters for all hadronic modes have same sensitivity,  
 extraction simplest for single- and double-pion decays  
 leptonic modes have reduced sensitivity [because of 2 neutrinos/decay]

# polarimeter components



for “usual” tau polarisation measurement (LH or RH tau) → longitudinal component

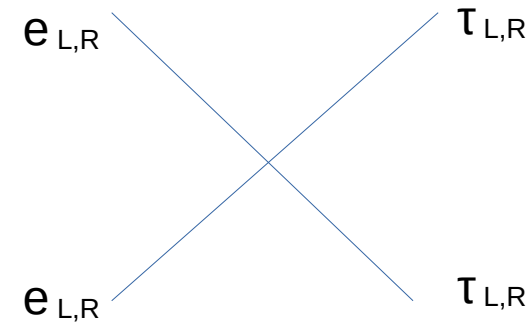
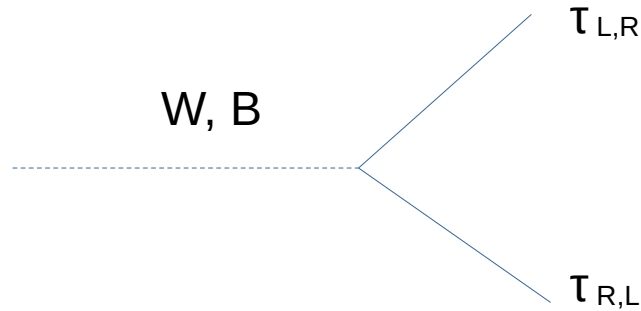
# BSM effects on the $e^+e^- \rightarrow \tau^+\tau^-$ process : EFT approach

## Dimension-Six Terms in the Standard Model Lagrangian\*

B. Grzadkowski<sup>1</sup>, M. Iskrzyński<sup>1</sup>, M. Misiak<sup>1,2</sup> and J. Rosiek<sup>1</sup>

$\psi^2 X \varphi$	
$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W'_{\mu\nu}$
$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$



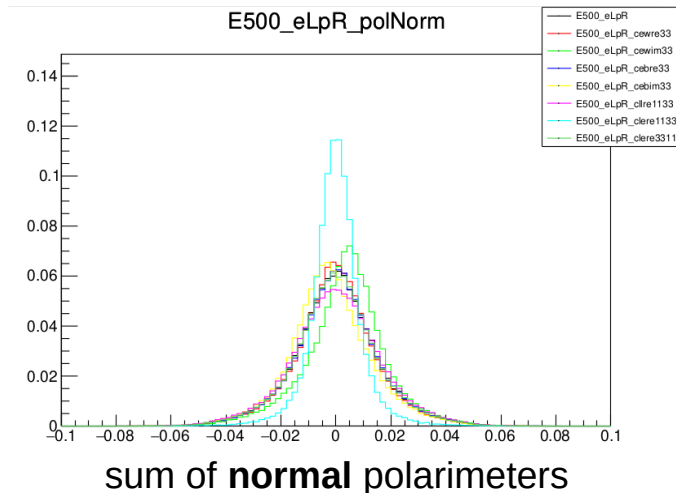
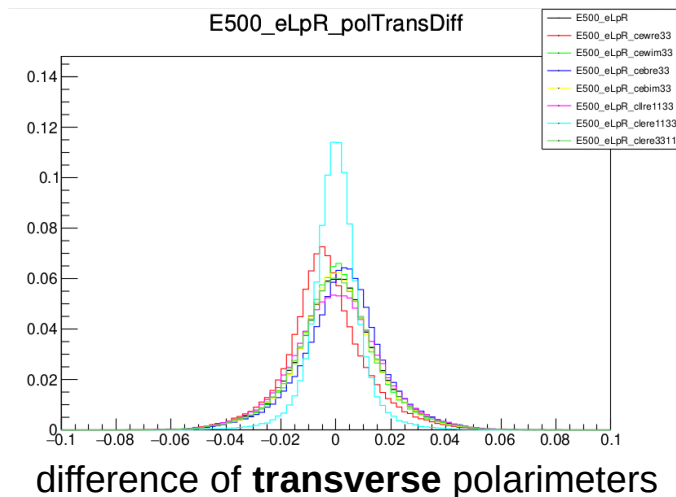
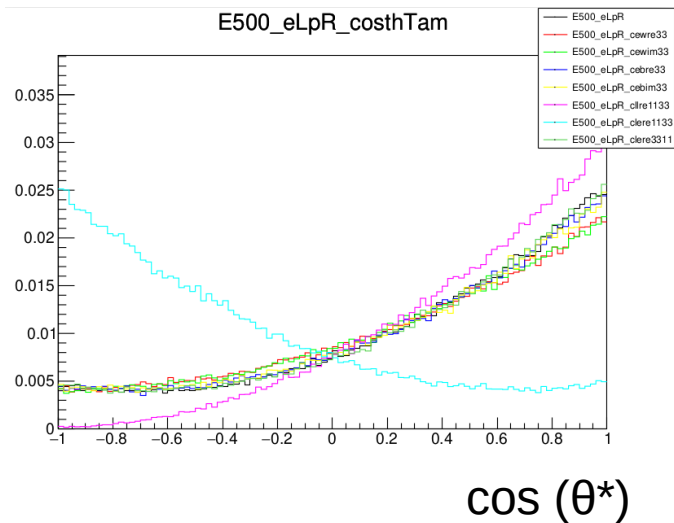
coupling of taus to W, B: mix L, R

related to tau dipole moments

4-f coupling of  
electron and tau currents

imaginary coefficients ~ CP violation

these SMEFT coefficients influence different distributions in different ways,  
for example:



SM

$$Q_{eW} \quad \left( \bar{l}_p \sigma^{\mu\nu} e_r \right) \tau^I \varphi W_{\mu\nu}^I$$

$$Q_{eB} \quad \left( \bar{l}_p \sigma^{\mu\nu} e_r \right) \varphi B_{\mu\nu}$$

Re  
Im  
Re  
Im

$$Q_{ll} \quad \frac{(\bar{L}L)(\bar{L}L)}{(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)}$$

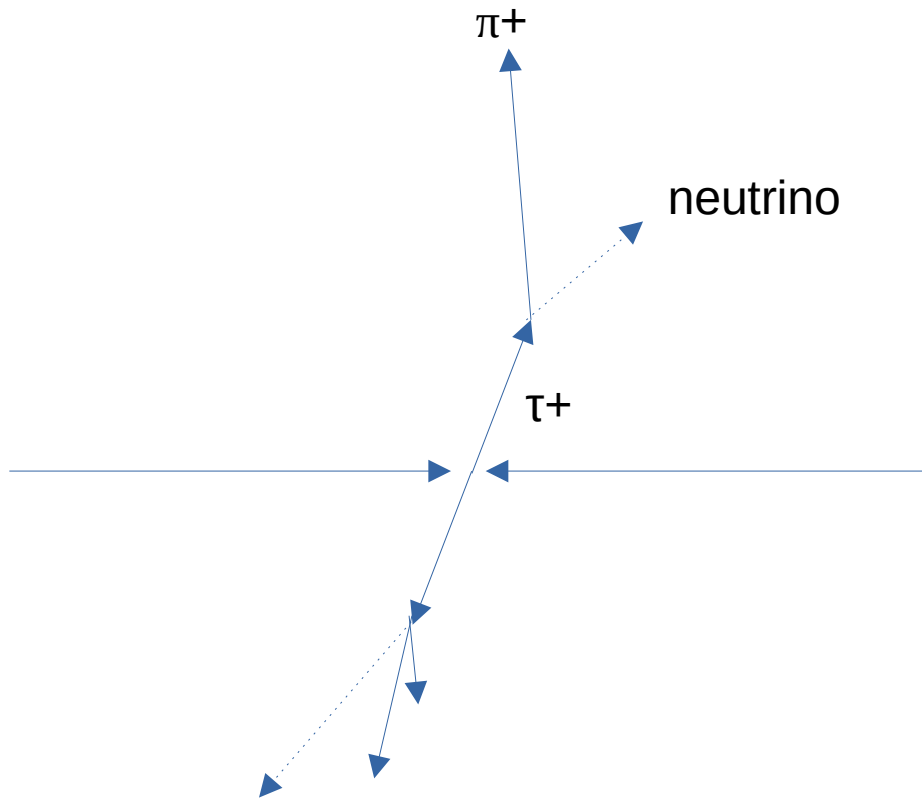
$$Q_{le} \quad \frac{(\bar{L}L)(\bar{R}R)}{(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)}$$

(ee)<sub>L</sub>( $\tau\tau$ )<sub>R</sub>  
(ee)<sub>R</sub>( $\tau\tau$ )<sub>L</sub>

variations depend on Wilson coefficients, energy, beam polarisation, ...

can we access these polarimetric quantities?





if we know the  
 CM frame of  $\tau^+ \tau^-$  and  
 CM energy,  
 it's a well constrained system

→ can extract tau direction,  
 decay kinematics,  
 "polarimeter"  
 [to within 2-fold ambiguity]

this applies when ISR is negligible:  
 at the Z-pole

→ 4-momentum conservation  
 → tau candidates' invariant mass

"cone method"

neutrino lies on cone around *visible* momentum  
 cone angle depends on  $p_{\text{VIS}}$ ,  $m_{\tau}$ ,  $E_{\tau}$

# kinematic unknowns and constraints in $e e \rightarrow \tau \tau$ , away from the Z pole

at Z-pole: can assume known tau energy,  
back-to-back topology

at higher energies need to take account of  
(usually unseen) ISR

momentum/energy conservation (including ISR)

tau masses

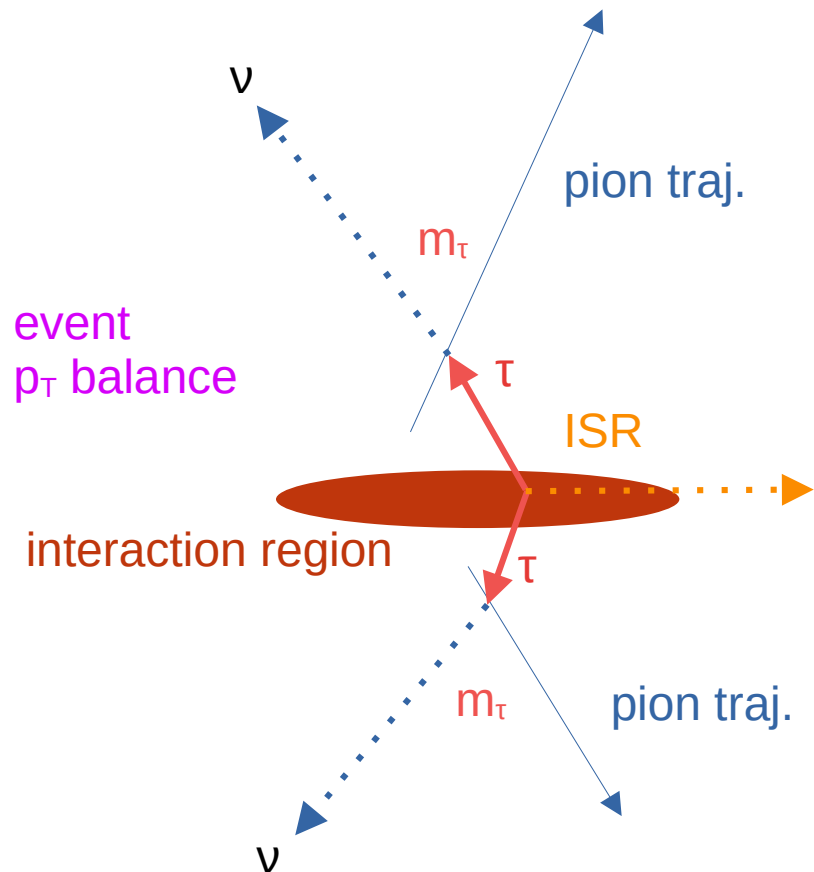
impact parameters w.r.t. beam spot

interaction region

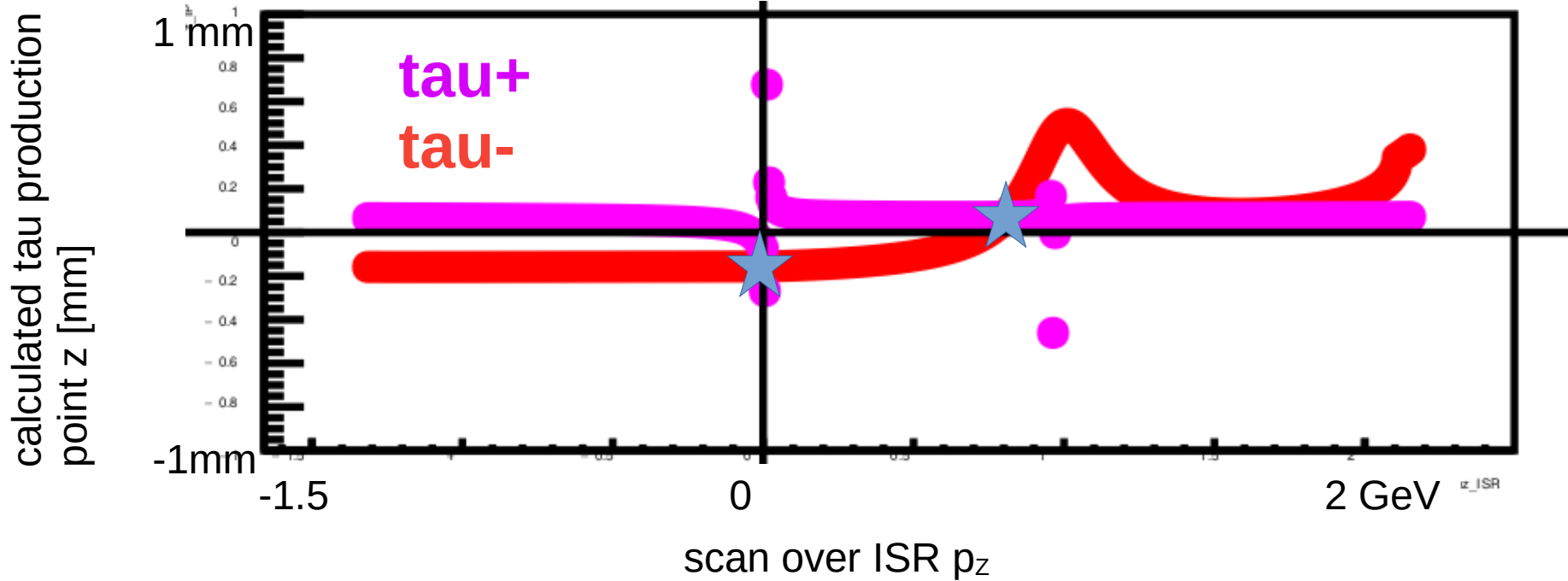
under-constrained system

→ several possible solutions per event

scan across unseen ISR momentum, check for consistency



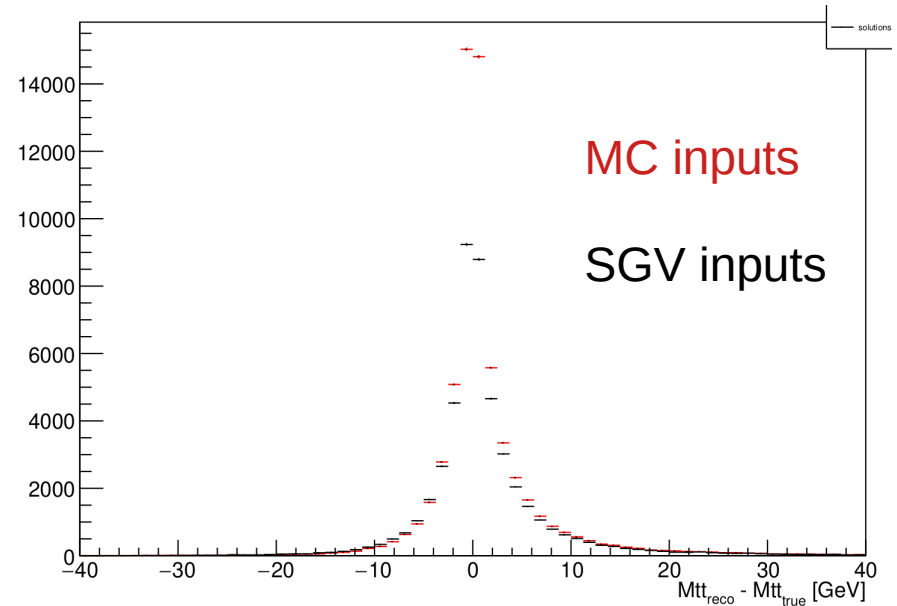
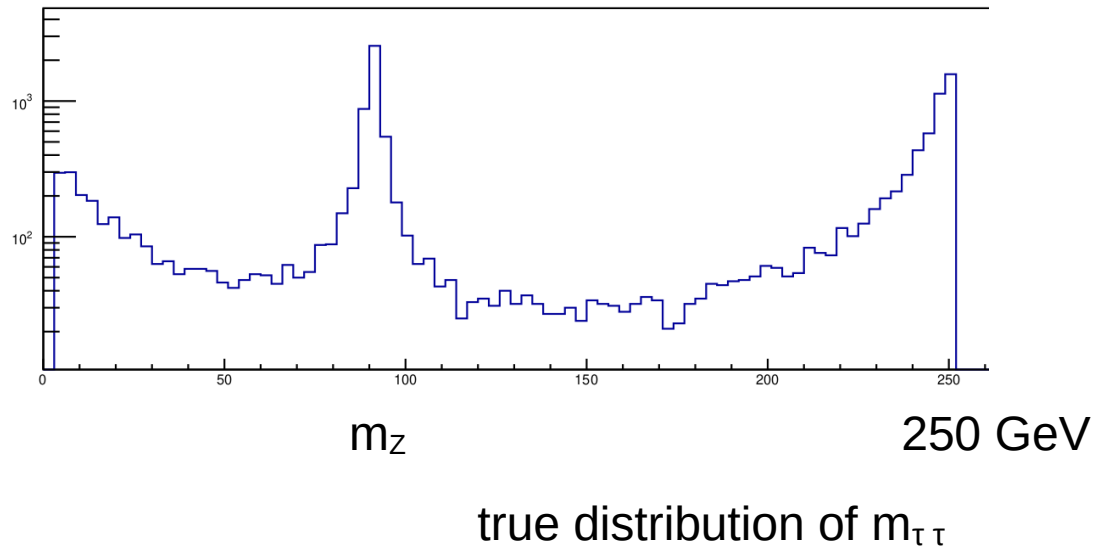
example, for one event



this event has **2 solutions**

look at performance at 250 GeV using

- MC truth values of visible particle momenta
- fast detector simulation SGV [by M. Berggren, based on ILD]

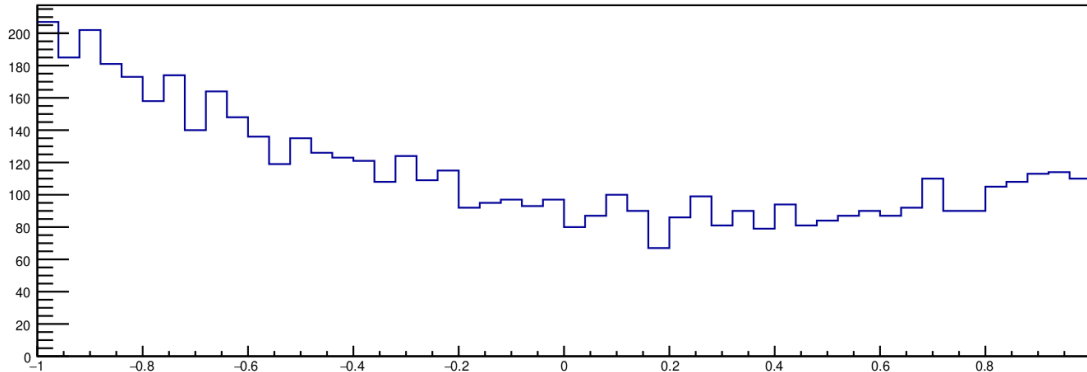


$m_{\tau\tau}$ : reconstructed – true  
resolution  $\sim$  GeV

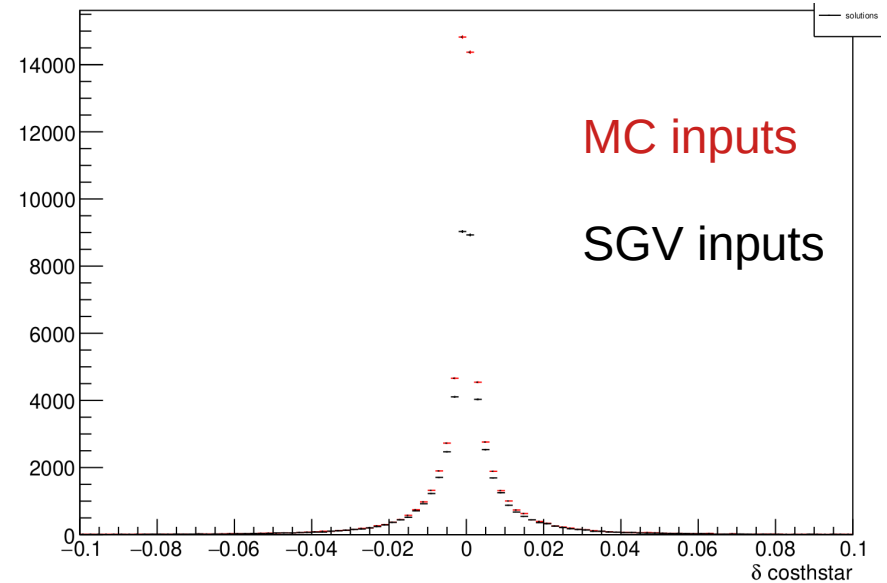
efficiency smaller with SGV

look at performance at 250 GeV using

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true distribution of CM scattering angle:  $\cos \theta^*$

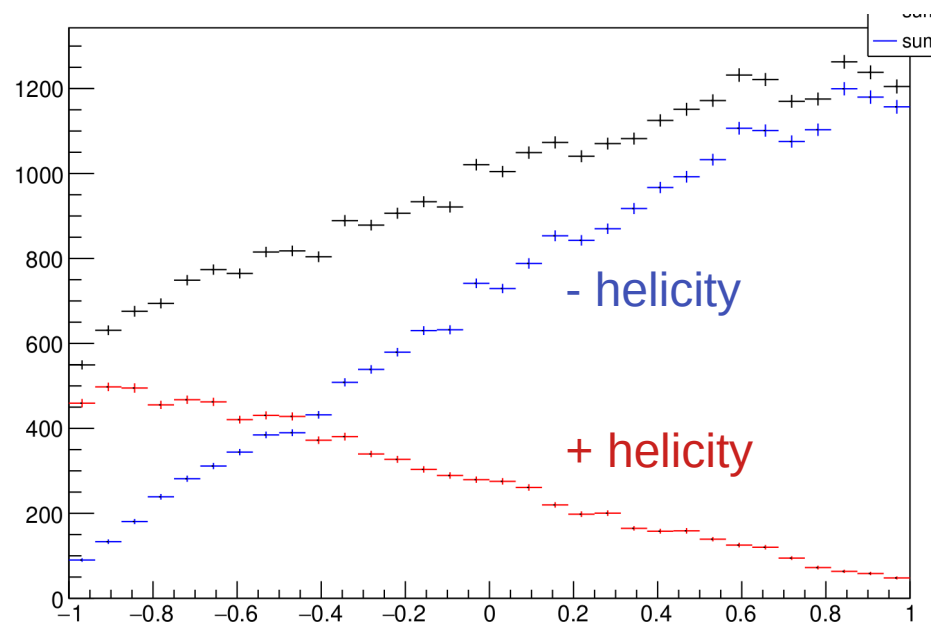


$\cos \theta^*$  : reconstructed – true

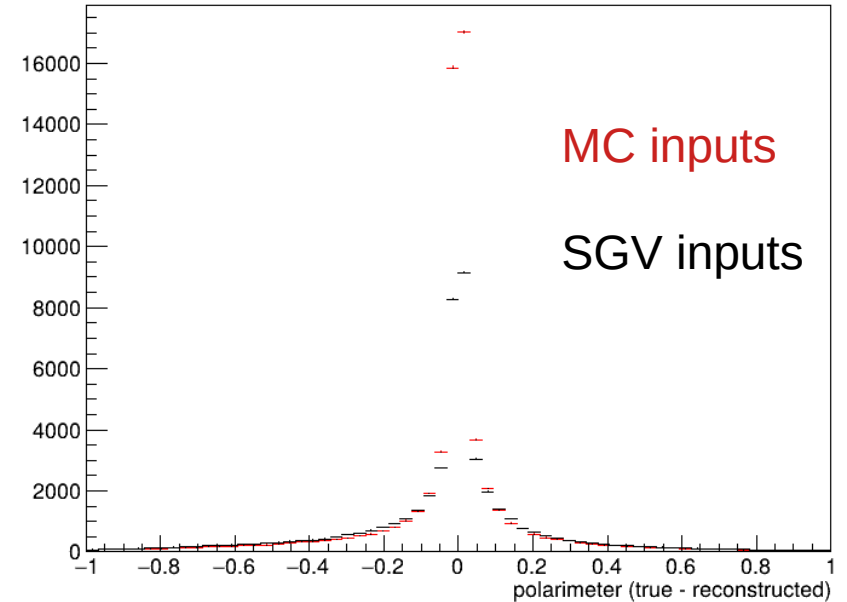
resolution < 0.01

look at performance at 250 GeV using

- MC truth values of visible particle momenta
- fast detector simulation SGV [by M. Berggren, based on ILD]



reconstructed longitudinal  
polarimeter component



long. polarimeter : true – reco

resolution < 0.1

## Summary

tau polarisation (longitudinal, transverse) at high energy is a unique probe for BSM  
e.g. via constraints of SMEFT operator coefficients  
relation to weak dipole moments of tau

attempt to use maximal information to extract tau polarisation  
in continuum  $e^+ e^- \rightarrow \tau^+ \tau^-$  : an under-constrained system

developed a rather (over-?) complicated method

it seems to work OK:

$m_{\tau\tau}$  , scattering angle, polarimeter reconstructed with sufficient precision

relies on several aspects of detector performance

impact parameter

$\pi^0$  reconstruction

track momentum

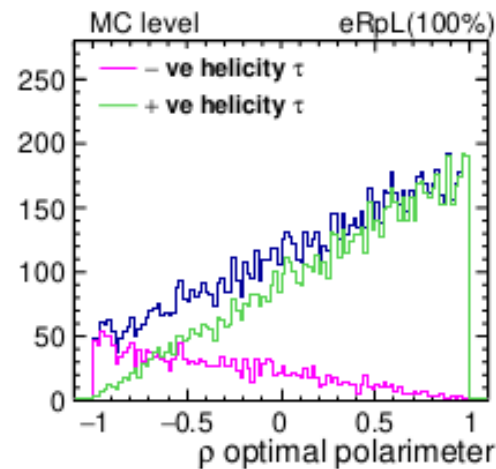
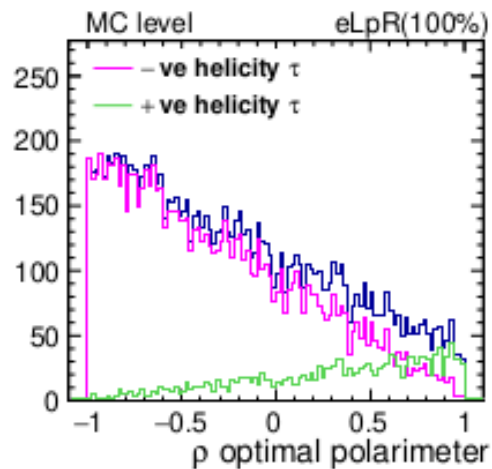
→ now being investigated using fast detector simulation

no time for firm physics results for this ECFA strategy update...

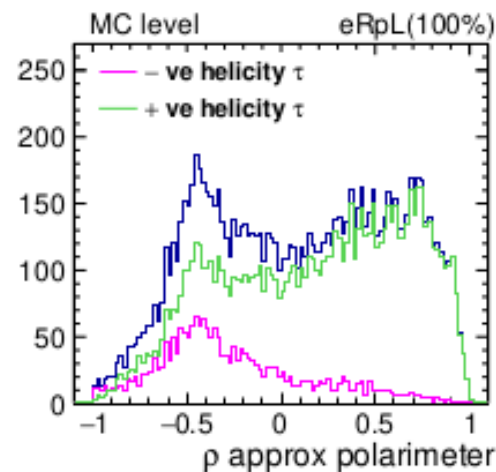
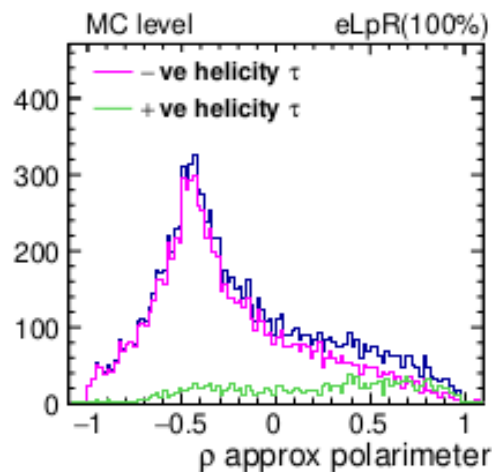
backup



optimal: using neutrino momentum



approx: without



madgraph5\_@NLO

+

SMEFTsim

+

TauDecay

<http://madgraph.phys.ucl.ac.be/>

<https://smeftsim.github.io/>

arXiv:1212.6247

**Process:  $e^- e^+ \rightarrow \tau^- \tau^+$  , (  $\tau^- \rightarrow \nu_\tau \pi^-$  ) , (  $\tau^+ \rightarrow \bar{\nu}_\tau \pi^+$  )**

**QED=2**

**NP=1**

**Model: SMEFTsim\_general\_MwScheme\_UFO\_taudecay\_UFO**

