

# CKM Matrix Elements from W Decays

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3<sup>rd</sup> ECFA workshop on  $e^+e^-$  Higgs,  
Top & ElectroWeak Factories  
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HELMHOLTZ



# Motivation

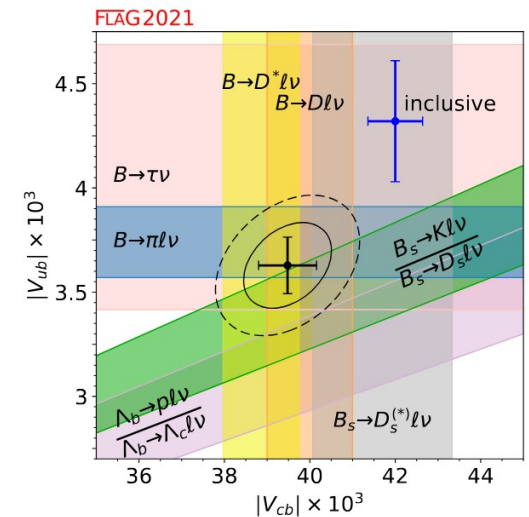
- Target: determine CKM matrix elements with optimal precision
- Why do we want that?
  - New Physics can affect couplings at ‘low’ energies → deviations from SM expectation
  - Does the unitarity triangle actually close?
  - Specifically: tension between inclusive and exclusive measurements of  $V_{cb}$  at  $\sim 3\sigma$

$$|V_{cb}| \text{ from inclusive } B \text{ decays} \quad (42.19 \pm 0.78) \times 10^{-3}$$

$$|V_{cb}| \text{ from exclusive } B, B_s \text{ and } \Lambda_b \text{ decays} \quad (39.10 \pm 0.50) \times 10^{-3}$$

→ Focus topic WW-CKM, along with 2 more W-based focus topics ( $m_W$ ,  $W_{\text{diff}}$ ) making use of large statistics at  $E_{\text{cm}} \geq 2m_W$  at any future HTE factory

- Direct W decays allow to directly measure 6 ‘non-top’ elements
- See also [2-day meeting of flavour sub-group](#)



# CKM precision: status & outlook

- $V_{cs}$  prospects to reach 0.2%
- $V_{cb}$  already now systematically limited, reach possibly  $\sim 2\%$  with HL-LHC
- Statistics at future HTE factory can allow for 1 order of magnitude higher precision

from study with FCC-ee:

$ V_{ij} $	Current (PDG)		FCC-ee ( $\delta_\epsilon = 1\%$ )	FCC-ee ( $\delta_\epsilon = 0.1\%$ )
$ V_{cs} $	$0.975 \pm 0.006$	(0.6%)	0.36%	0.05%
$ V_{cb} $	$(40.8 \pm 1.4) \times 10^{-3}$	(3.4%)	0.52%	0.16%



- For  $10^8$  W with perfect efficiency and no background:

$W^- \rightarrow$	$\bar{u}d$	$\bar{u}s$	$\bar{u}b$	$\bar{c}d$	$\bar{c}s$	$\bar{c}b$
BR	31.8%	1.7%	$4.5 \times 10^{-6}$	1.7%	31.7%	$5.9 \times 10^{-4}$
$N_{ev}$	$64 \times 10^6$	$3.4 \times 10^6$	900	$3.4 \times 10^6$	$63 \times 10^6$	$118 \times 10^3$
$\delta_{V_{ij}}^{th}$	0.0063 %	0.027 %	1.7 %	0.027 %	0.0063 %	0.15 %

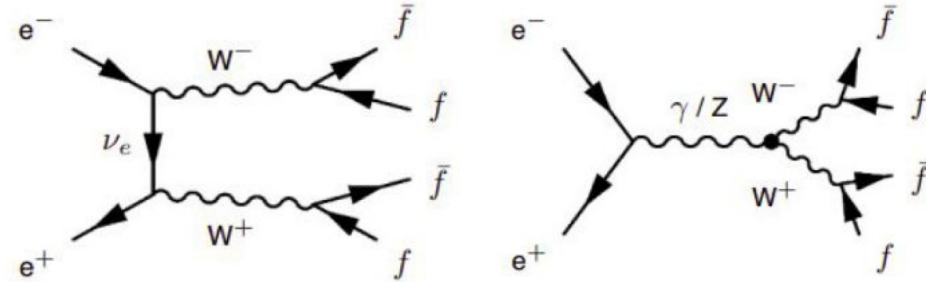
- W branching fraction into quarks  $u_i + d_j$  directly proportional to  $|V_{ij}|^2$
- Identify W events, simply tag and count decays into different quark combinations!
- Simply tag...? → crucial: high efficiency & purity & well-understood flavour tagger!
- Measuring CKM elements from B/D-meson decays suffers from significant non-perturbative hadronic contributions to the matrix element, not at  $m_W \gg \Lambda_{\text{QCD}}$
- Great prospects with perfect efficiency and no systematics, but what is realistic?

$W^- \rightarrow$	$\bar{u}d$	$\bar{u}s$	$\bar{u}b$	$\bar{c}d$	$\bar{c}s$	$\bar{c}b$
BR	31.8%	1.7%	$4.5 \times 10^{-6}$	1.7%	31.7%	$5.9 \times 10^{-4}$
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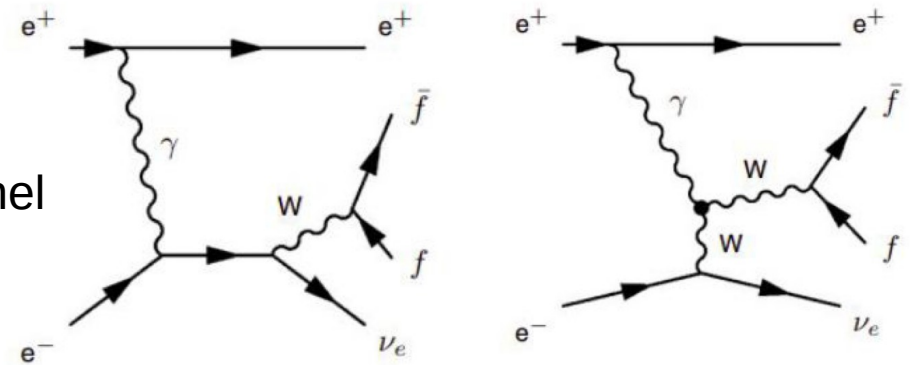
# W Physics Working Points

- W threshold
  - needed anyway for  $m_W$
  - cross section  $\sim 5$  pb
  - more interesting for CC
- Higgs (240-250 GeV)
  - needed anyway for H
  - cross section  $\sim 20$  pb
  - more interesting for LC
- W(W) production profits greatly from polarisation
- Both CC and LC expect some  $10^8$  Ws
- Note: fully hadronic channel has colour reconnection!

WW-channel



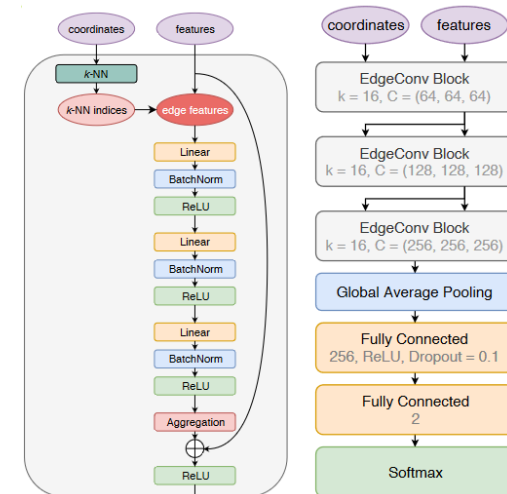
single-W channel



# Flavour Taggers

- Long-time (> 10 a) standard tool: LCFIPlus, now out-of-date with BDT and b/c/light tag
- A number of new flavour taggers have been developed, making use of neural networks and advanced machine learning
  - ParticleNet (ILD/CLD) [Meyer]
  - ParticleNet (IDEA) [Selvaggi e.a.]
  - ParticleNet (CEPC baseline) [Ruan e.a.]
  - Particle Transformer (ILD, IDEA) [Suehara]
  - Particle Transformer (CLD, Si-IDEA) [Aumiller e.a.]
- Adding strange-tag via PID (kaonID), possibly individual u- and d-tag via FSR
- Systematic uncertainties on flavour taggers?
  - calibrate at Z-pole with double-tag method and  $10^{12}$  events (FCC-ee) or some  $10^9$  (LC)
  - limits to detector adaptations to center-of-mass energy?

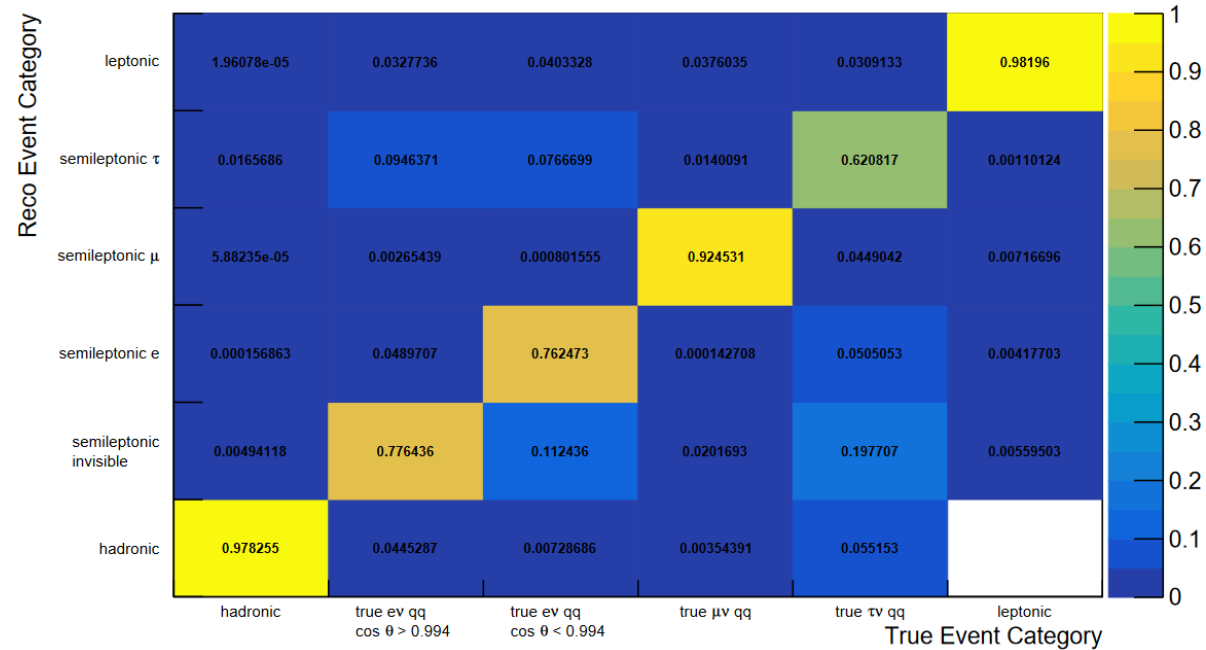
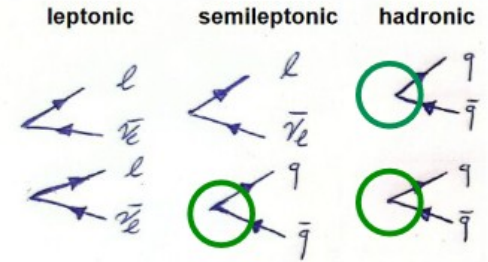
ParticleNet: <https://arxiv.org/abs/1902.08570>



- Approach: full-sim incl. backgrounds, using 250 GeV MC production (ILC) of  $\sim 12 \text{ ab}^{-1}$  ( $\sim 6$  times data from target luminosity)
- Goal: ILD post-processing of 250 GeV MC production (from DST to MiniDST) by adding new high-level-reco features, to provide easy-to-access analysis basis
  - Work in progress
- WW categorisation
- Flavour tagger, implementation in standard reco chain

# W(W) channel categorisation

- Categorise W(W) decay channels: each event receives one 'tag'
- → Overlap-free categories allow for easy combination of exclusive analyses of any W-related study
- Basis: number & flavour of leptons
- Refine with number of reco particles ( $n_{\text{PFOs}}$ ),  $m_{\text{inv}}$ ,  $E_{\text{miss}}$ ,  $p_{\text{T,miss}}$

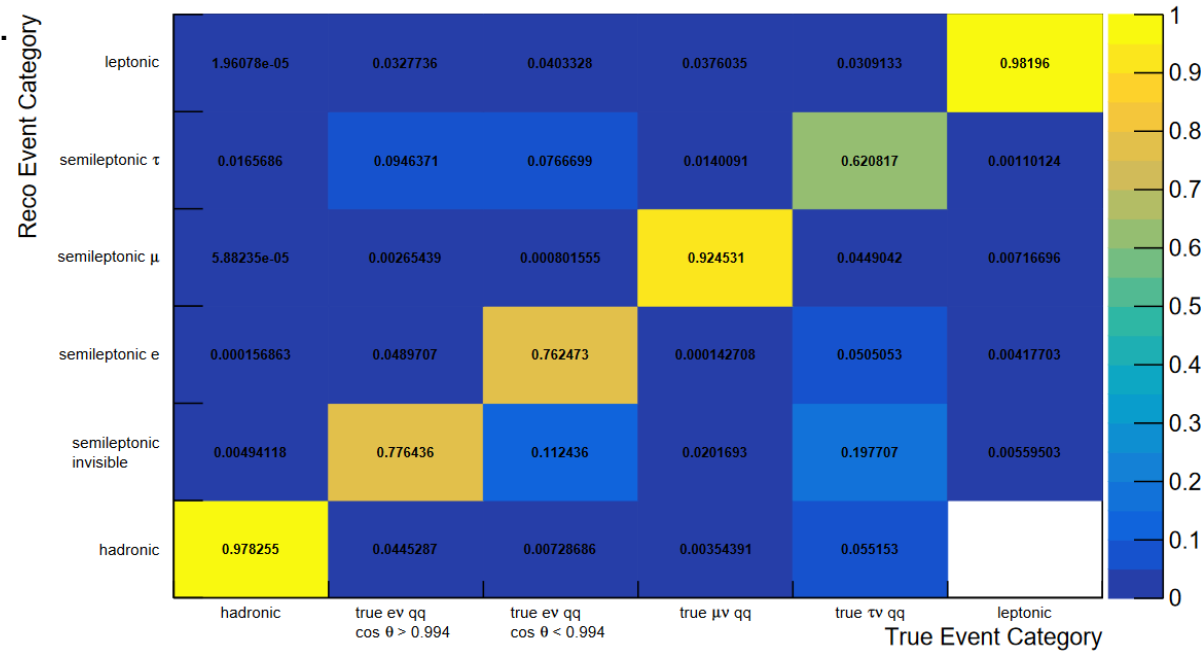
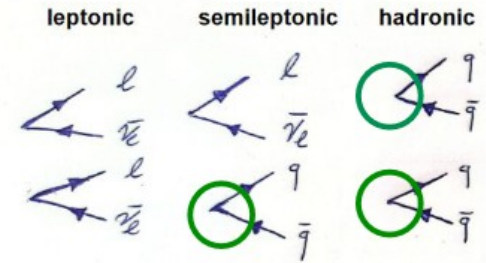
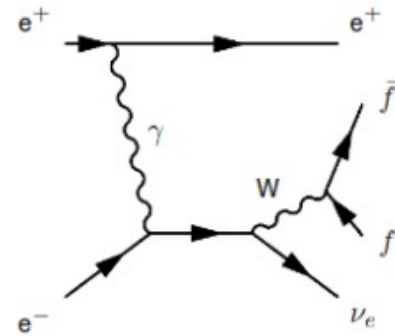


[A. Silva]



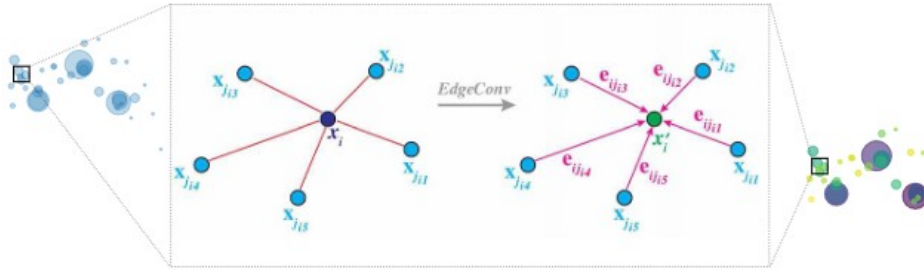
# W(W) channel categorisation

- Good diagonality
  - hadronic & leptonic  $\sim 98\%$  eff.
  - semilep.  $\mu \sim 92\%$  eff.
  - confusion at the edge of det. acc. in semilep e vis./invis.  $\sim 77\%$  eff.  $\rightarrow$  invis. ( $\cos \theta > 0.994$ ) mostly from t-channel contribution
  - some more confusion with semilep.  $\tau \sim 62\%$  eff.
- Study: increase and understand electron detection efficiency at detector acceptance edge [L. Reichenbach]
- Potential study:  $\tau$  tagger



[A. Silva]

# ParticleNet (ILD/CLD)



- treat jet as „particle cloud“
- input: **jet constituents**

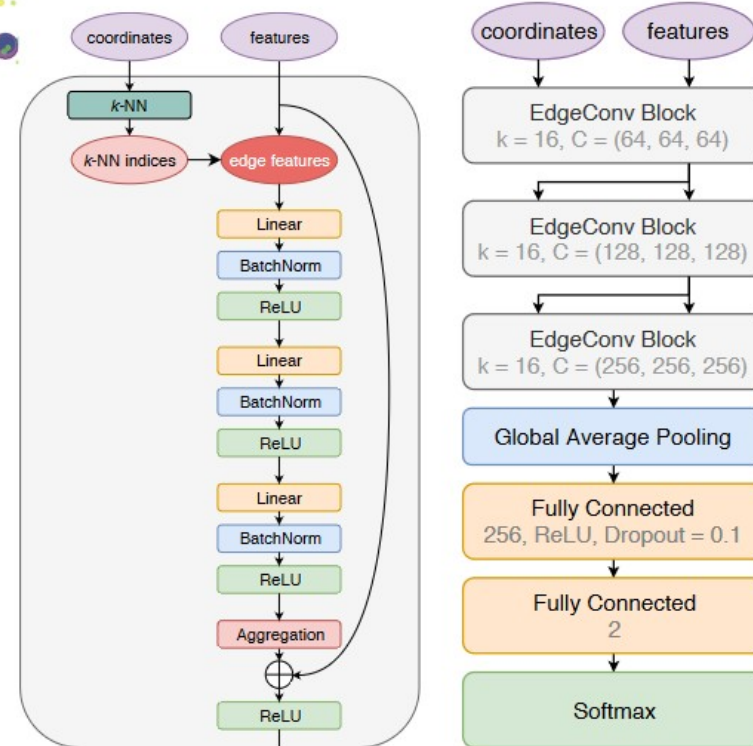
key building block: **edge convolution**

- particle cloud: graph, each point: vertex, connections between each point & k nearest neighboring points: edges
- learn an „**edge feature**“ for each pair:

$$e_{ij} = \text{MLP}(x_i, x_j)$$

- **MLP**: parameters **shared among all edges**
- **aggregation** of edge features:  $x'_i = \text{mean}_j e_{ij}$

arXiv:1902.08570, *Pushing the Limit of Jet Tagging With Graph Neural Networks*, Huilin Qu, talk at ML4Jets2021, July 7, 2021



**edge convolution**

**ParticleNet**

from <https://agenda.infn.it/event/34841/contributions/207748/>

## jet constituents: coordinates

$\Delta\eta, \Delta\Phi$

## jet constituents: features

$\Delta\eta, \Delta\Phi, \eta$

$\log(p_T), \log(E), \log(p_T/p_T^{\text{jet}}), \log(E/E^{\text{jet}}),$   
 $\vec{p}^{\text{track}} \cdot \vec{p}^{\text{jet}}/p^{\text{jet}}$

$\Delta R$

$q$

isElectron, isMuon, isChargedHadron,  
isNeutralHadron, isPhoton

impact parameter & significances

impact parameter tag probabilities

track used in PV?

lepton related variables

pid variables → now including CPID:  
{e,  $\mu$ ,  $\pi$ , K, p} scores

$E_{\text{HCAL}}/E_{\text{HCAL}+\text{ECAL}}$

$\chi^2/\text{ndf}$

**34 39 input features**

## secondary vertices: coordinates

[M. Meyer, UE]

$\Delta\eta, \Delta\Phi$

## secondary vertices: features

$\Delta\eta, \Delta\Phi$

$\log(p_T), E_{\text{SV}}/E_{\text{jet}}, E_{\text{SV}}$

$\eta$

$m_{\text{SV}}$

$N_{\text{tracks in SV}}$

$\chi^2/\text{ndf}$

impact parameters & significances

$\cos(\text{flight direction}_{\text{SV}}, \vec{p}_{\text{SV}})$

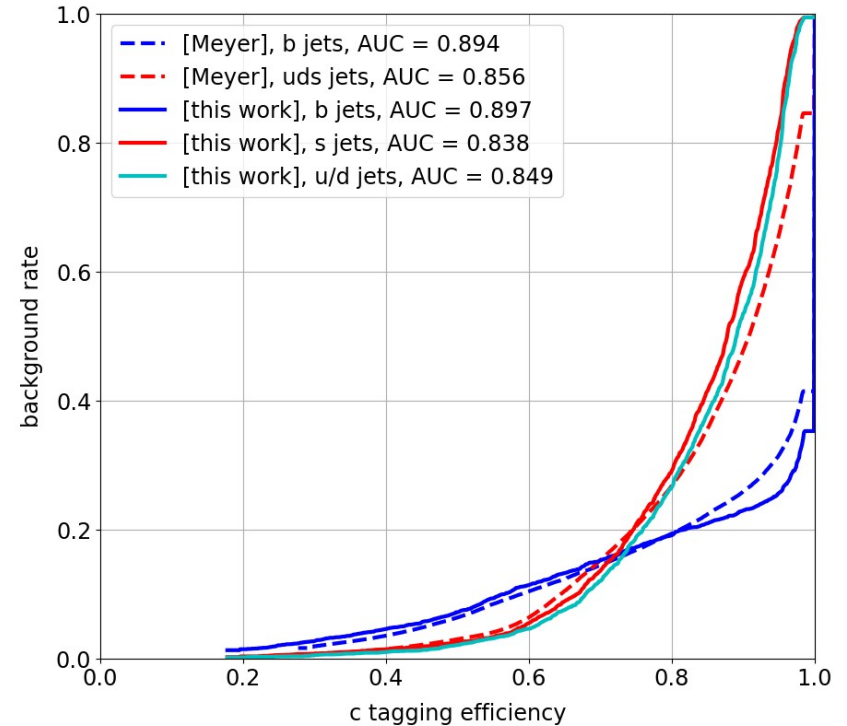
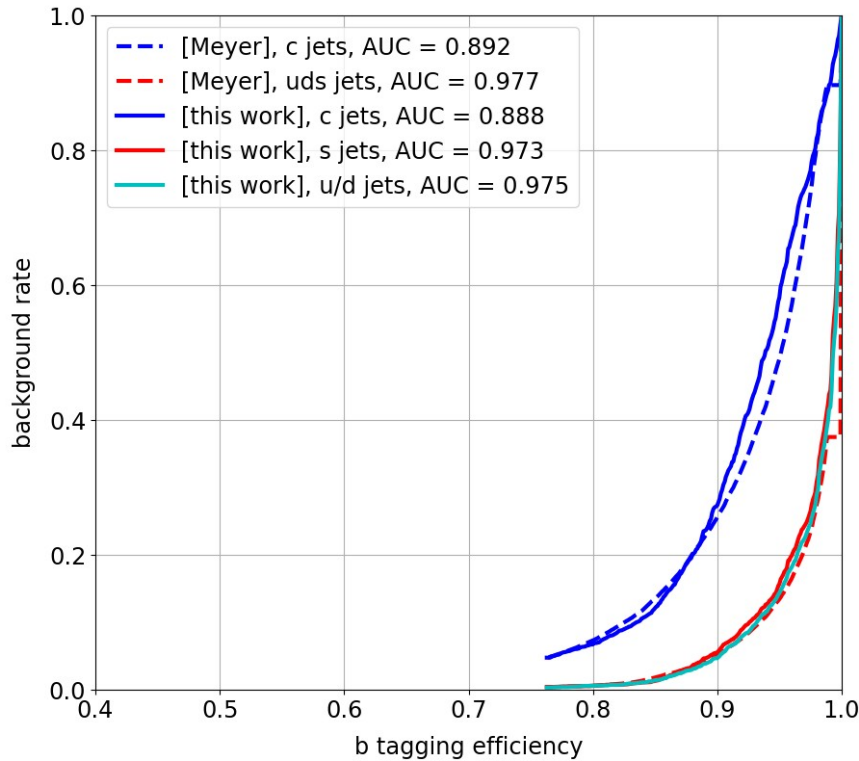
**14 input features**

**2 SVs & all jet constituents  
considered, no ordering of inputs  
output classes: b, c, light**

→ **b, c, s, u/d**

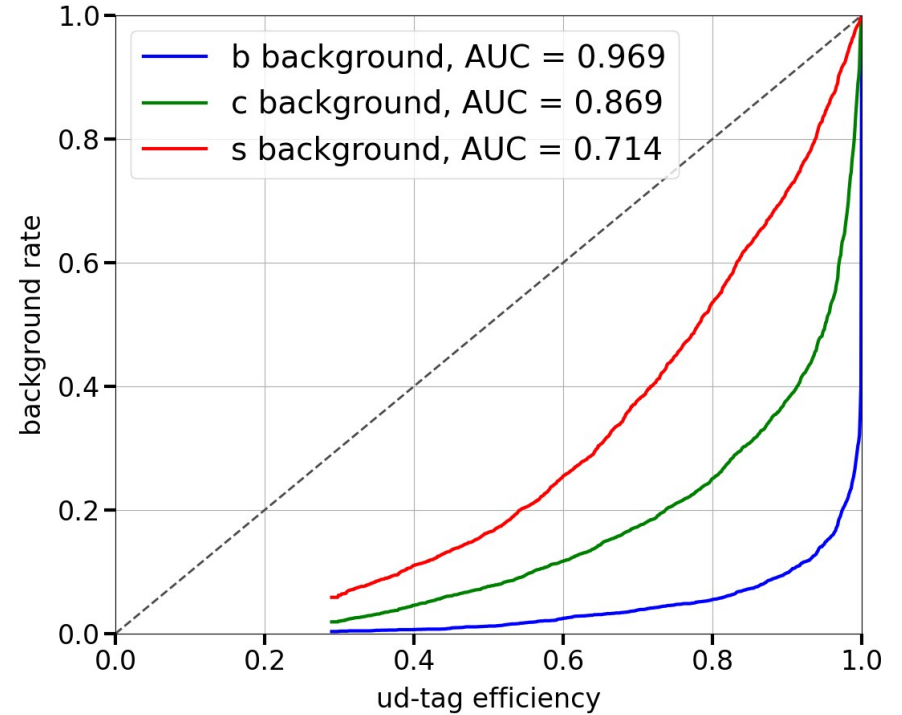
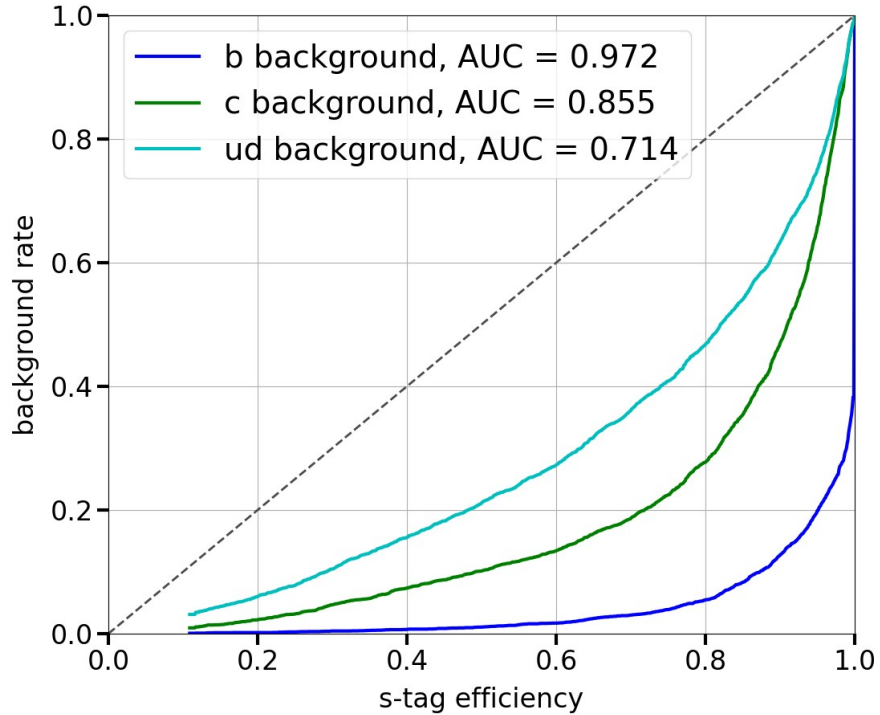
adapted  
from <https://agenda.infn.it/event/34841/contributions/207748/>

# Comparison with 'best of' training by M. Meyer



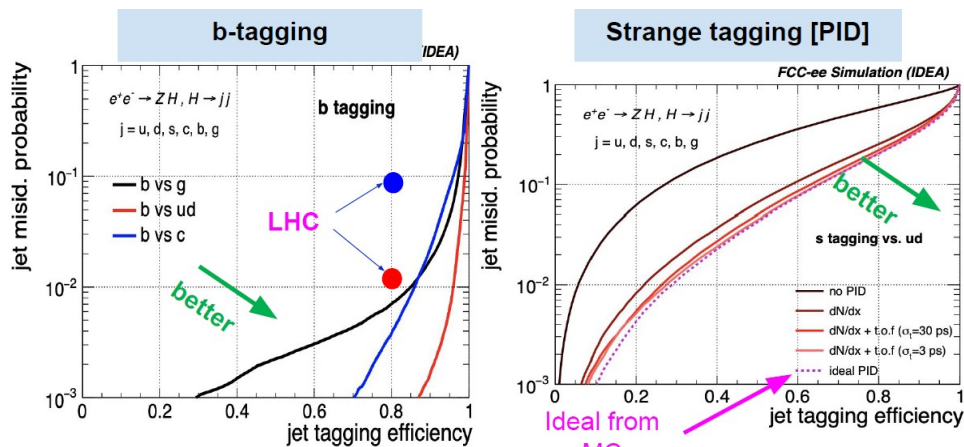
very similar performance, overall slightly worse → space for CNN parameter improvements

# ROC Curves of strange and u/d tagging



→ D. Marzocca, M.Szewc, M.Tammaro: <https://arxiv.org/abs/2405.08880>

- Assessment of prospects with given systematics, starting from quarks from the W decays at the parton level, using  $3 \times 10^8$  Ws at the W threshold
- Background: only 2q (+2j) considered
- Showing measurement estimates in dependence of parton-to-flavour-tag systematics
- Focus on  $V_{cb}$  and  $V_{cs}$



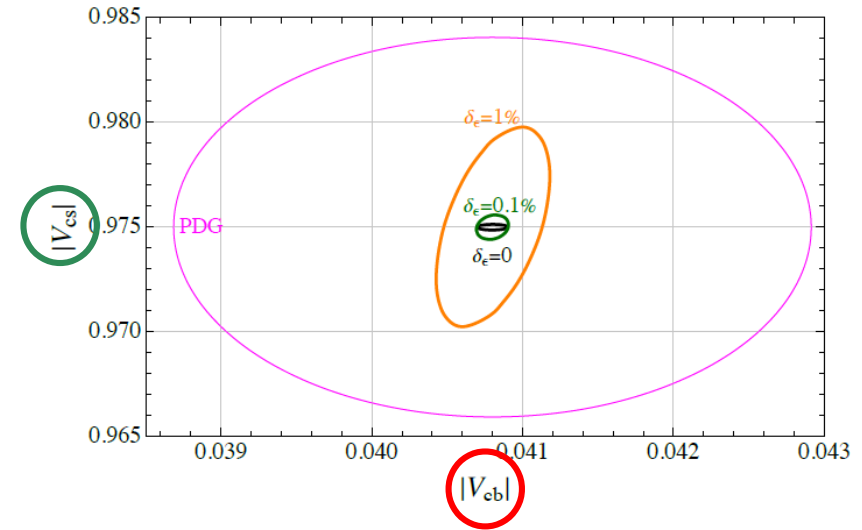
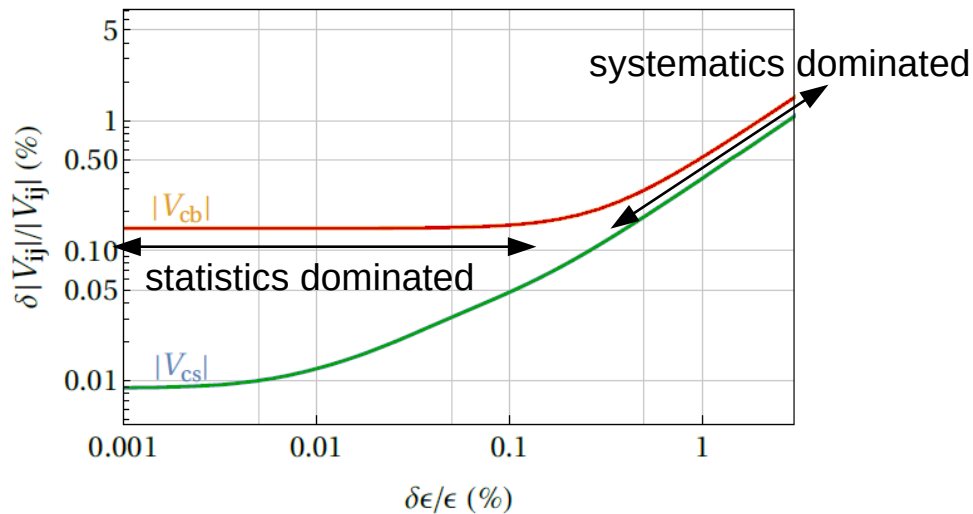
EPJ C 82 646 (2022)

ParticleNet (IDEA) flavour tag working points used:

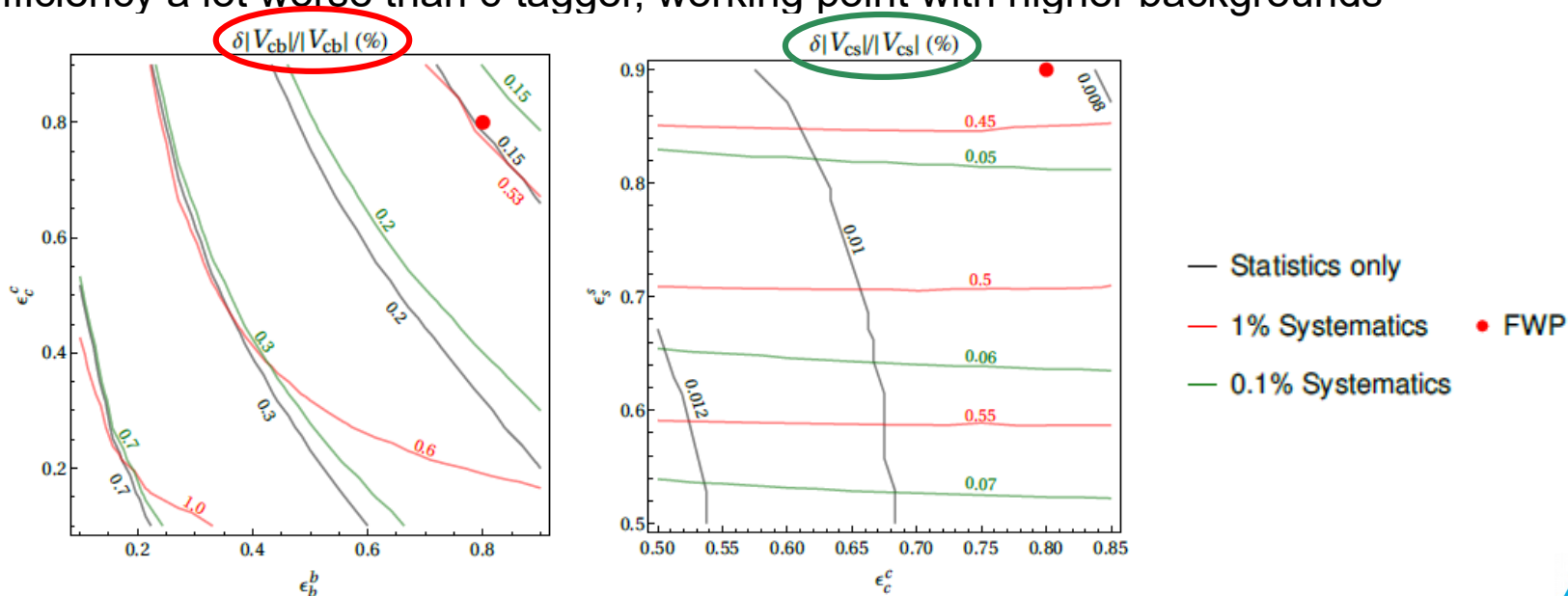
	b	s	c	u	d	g
$\epsilon_{\beta}^b$	0.8	0.0001	0.003	0.0005	0.0005	0.007
$\epsilon_{\beta}^c$	0.02	0.008	0.8	0.01	0.01	0.01
$\epsilon_{\beta}^s$	0.01	0.9	0.1	0.3	0.3	0.2



- Achievable uncertainties on  $V_{cb}$  and  $V_{cs}$ , depending on systematics uncertainties
- $V_{cs}$  would profit from systematics below 0.01%
- $V_{cb}$  stronger limited through statistics, flat below 0.1% systematics



- Systematic impact assessment:
- For  $V_{cb}$ , both c- and b-tagger uncertainties are of somparable impact
  - fewer b-jets than c-jets, but b-tagger has higher purity working point than c-tagger
- For  $V_{cs}$ , the uncertainty is dominated by the contribution from the s-tagger
  - efficiency a lot worse than c-tagger, working point with higher backgrounds



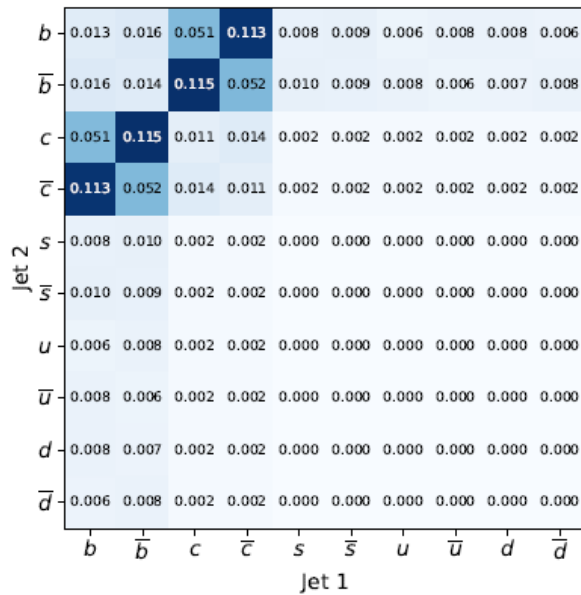


- H. Liang, L. Li, Y. Zhu, X. Shen, M. Ruan: <https://arxiv.org/abs/2406.01675>
- Approach: full-sim with CEPC-baseline detector (ILD-like) at 240 GeV
  - Focus on  $V_{cb}$  in semileptonic channel  $WW \rightarrow l\nu cb$
  - Extrapolation to running scenarios for various future HTE factories
  - Uncertainty assessment: theoretical uncertainties  $\sim 0.1\%$ , flavour taggers dominating at  $\sim 2\%$  → need for excellent calibration!
  - Backgrounds:  $WW(\text{other})$ , 2f, 4f, Higgs  
→ one conclusion: 2f is least important background

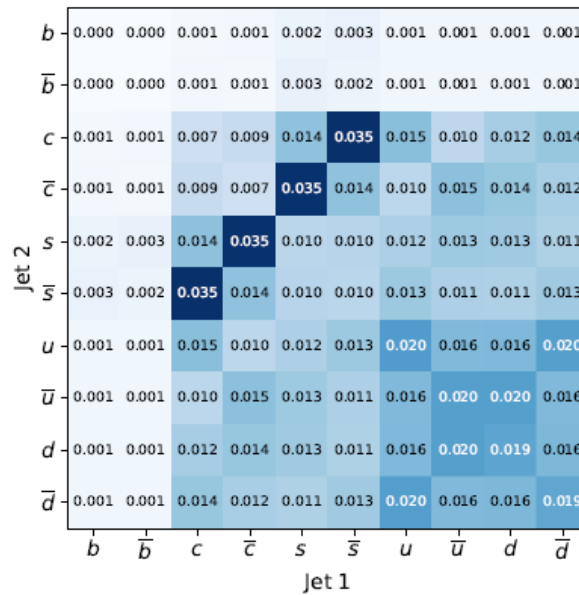
# Flavour Tagger: ParticleNet (CEPC)

- 5 quarks + 5 anti-quarks  $\rightarrow$  10x10 confusion matrix for 2 tagged jets
- Use jet scores in BDT to identify cb-decays

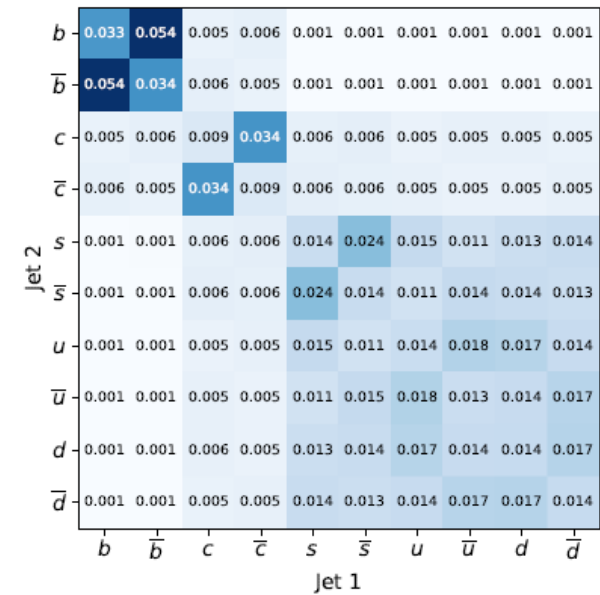
signal:  $W \rightarrow \mu\nu cb$



bkg: other W decays

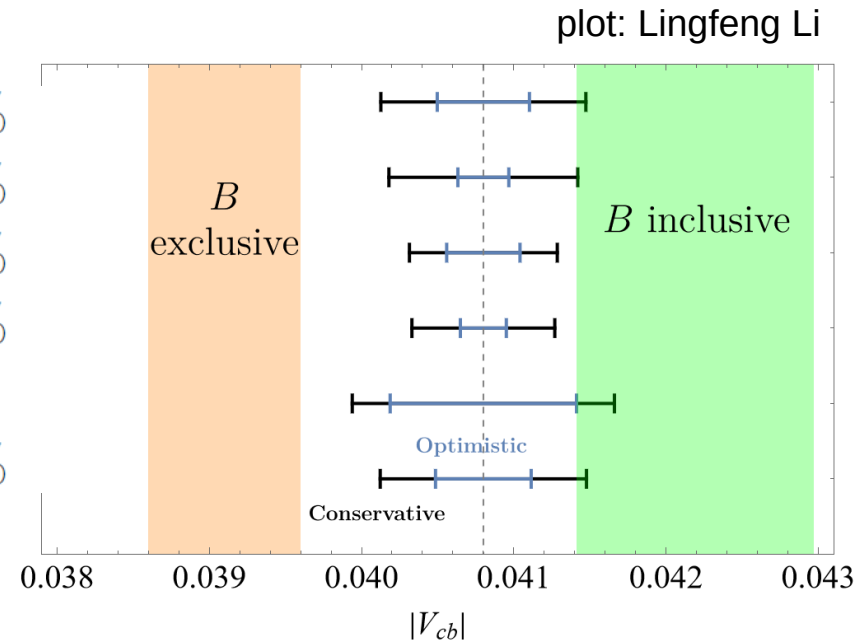


bkg: other



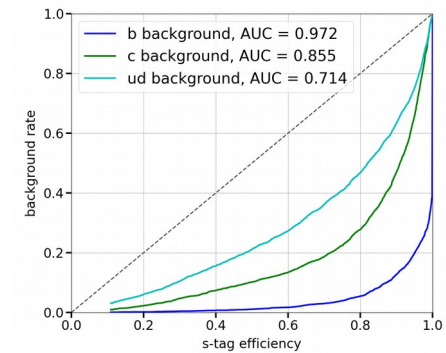
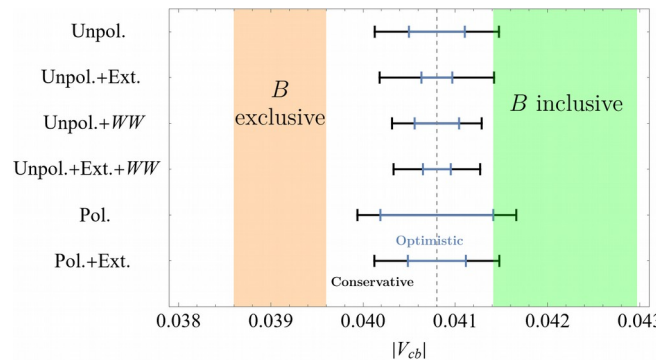
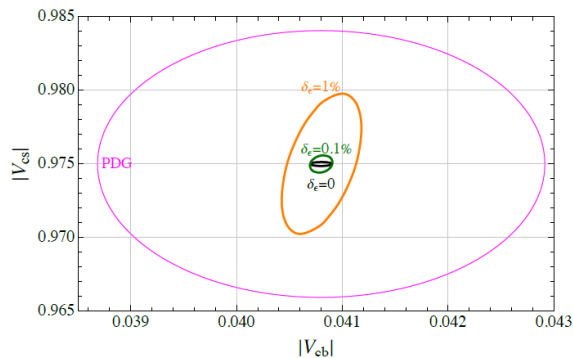
- Results, depending on running scenarios for various future HTE factories
- Combined statistical uncertainty on  $V_{cb}$  with sl (e,  $\mu$ ) channels; plot includes optimistic (0.2%) and conservative (1.5%) scenario on systematics

Unpolarized, Baseline ( $5 \text{ ab}^{-1}$ )	0.72%
Unpolarized, Extended ( $20 \text{ ab}^{-1}$ )	0.36%
Unpolarized, Baseline + $WW$	0.58%
Unpolarized, Extended + $WW$	0.34%
Polarized, Baseline ( $0.5 \text{ ab}^{-1}$ )	1.5%
Polarized, Extended ( $2 \text{ ab}^{-1}$ )	0.75%



# Outlook & Conclusions

- CKM matrix elements great opportunity for  $e^+e^-$  precision physics
- Focus on  $V_{cs}$  and  $V_{cb}$ , where HL-LHC and Belle II are limited already/soon, and standing tension in  $V_{cb}$  at  $3\sigma$
- Studies ongoing, first papers are out – prospects of 1 order of magnitude or more in enhanced precision, resolve tension
- Discussions ongoing how to continue, expand and refine results
- Critical: systematics, in particular of the flavour taggers
- Also: great ongoing progress in theory, in particular LQCD!



# CEPC study: cross check jet tagging in Z vs. H

plots from M. Ruan

