

# The Need for a Higgs, Electroweak and Top Factory



$N_1$   $E_1$   $E_1$   $D_2$



Milada Margarete Mühlleitner  
Karlsruhe Institute of Technology



$N_1$   $E_1$   $E_1$   $D_2$

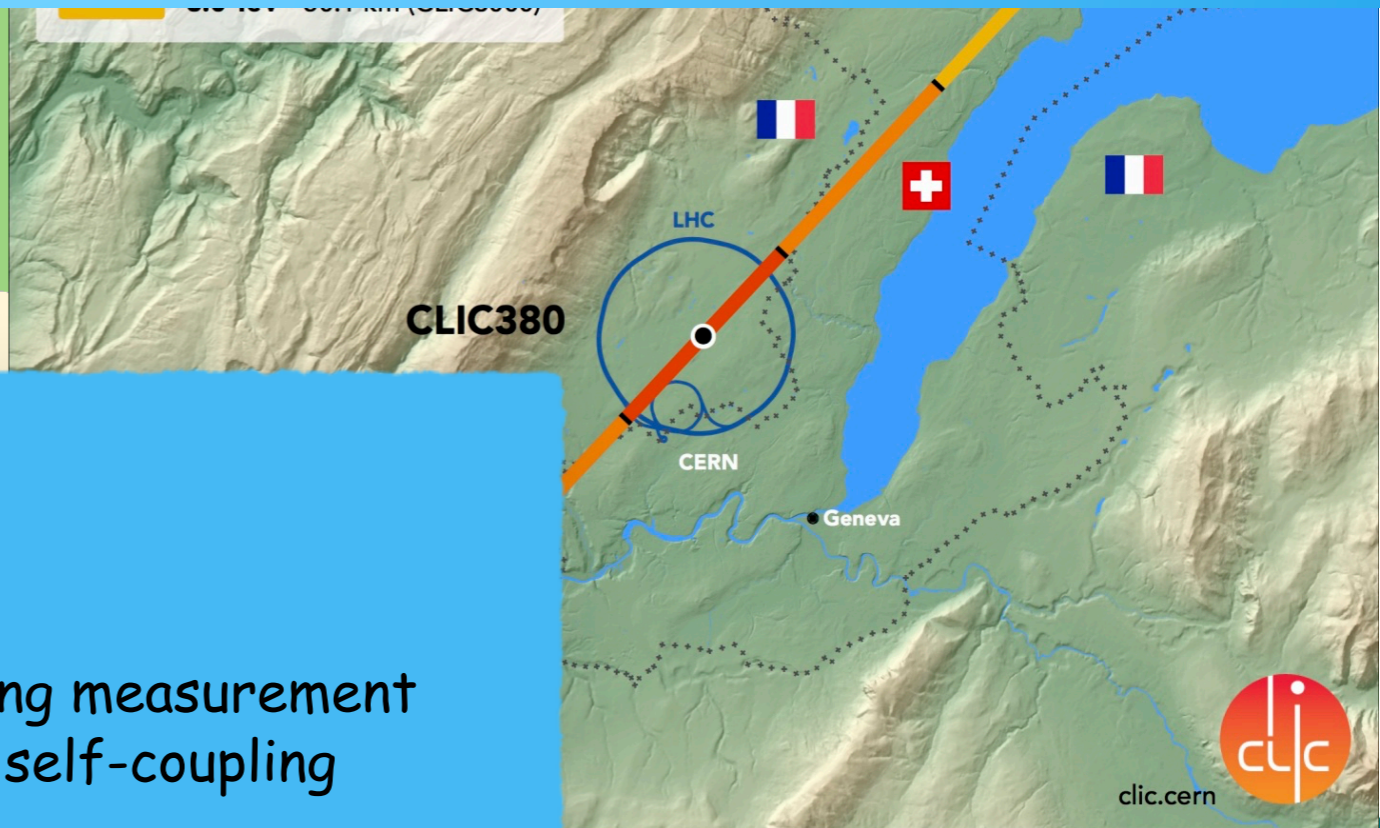


3rd ECFA  
Workshop

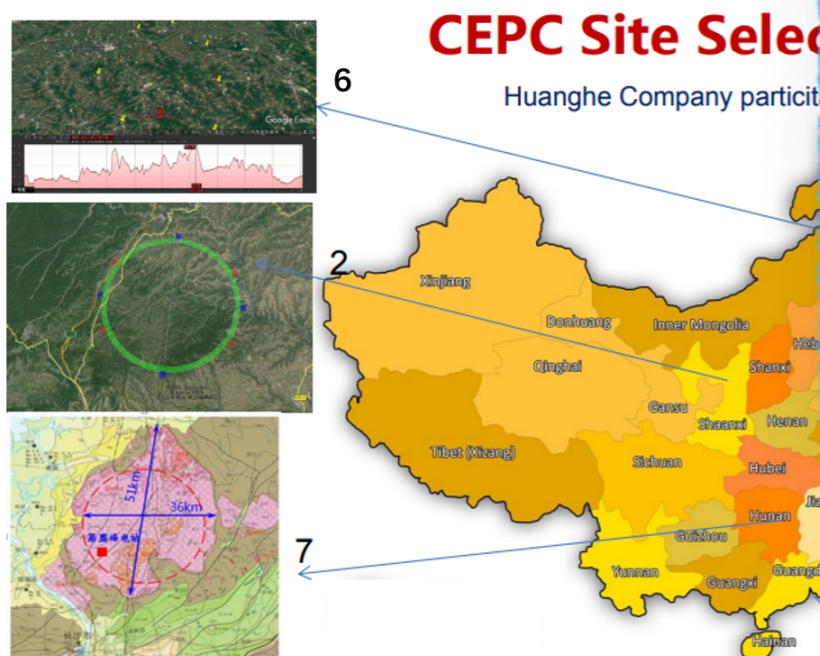
Paris

9-11 Oct 2024

# Outline



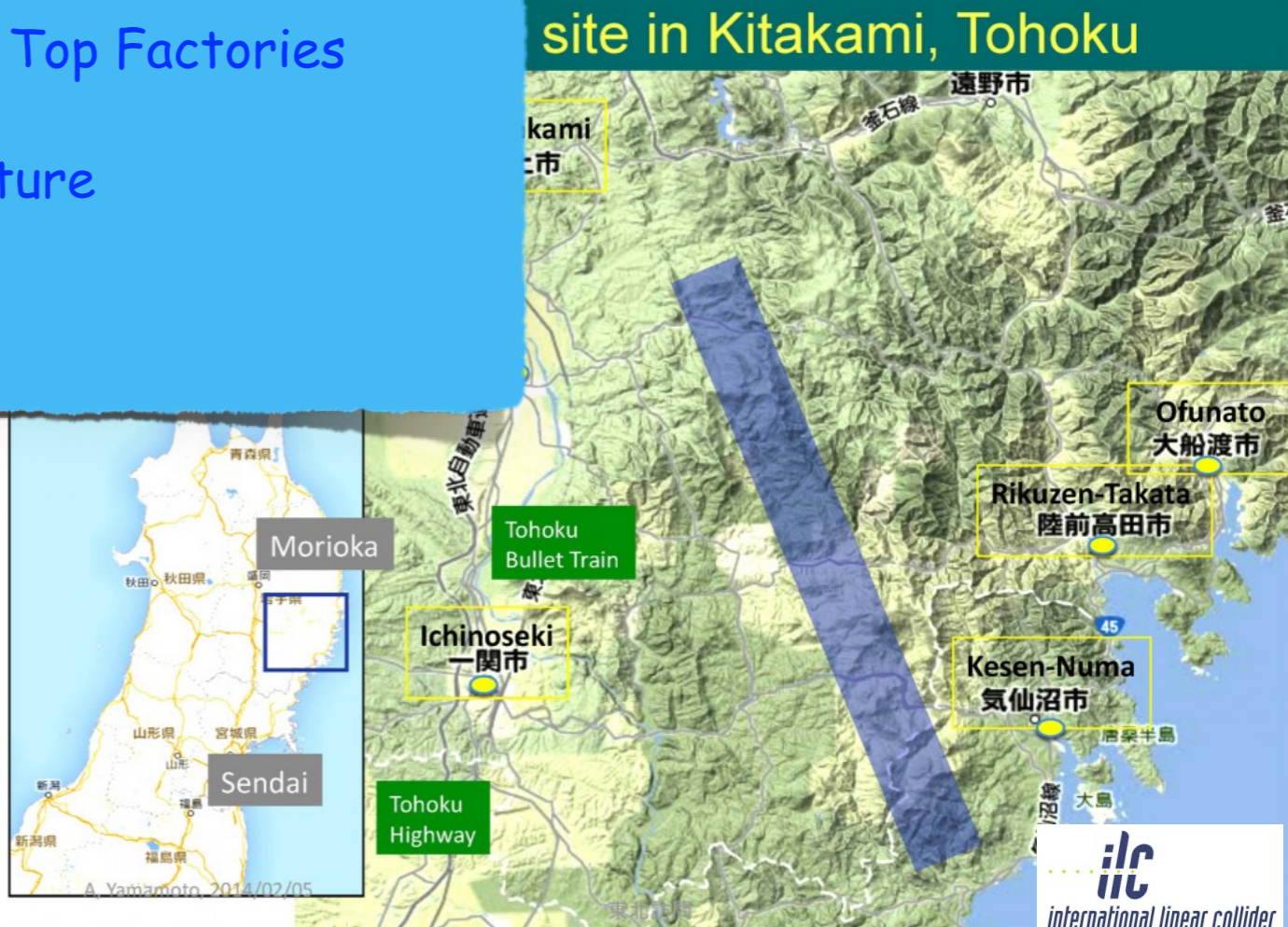
- ◆ Introduction
- ◆ Higgs Factory
  - absolute coupling measurement
  - trilinear Higgs self-coupling
- ◆ Electroweak and Top Factories
- ◆ A Look in the Future
- ◆ Conclusions



## CEPC Site Selection

Huanghe Company participated

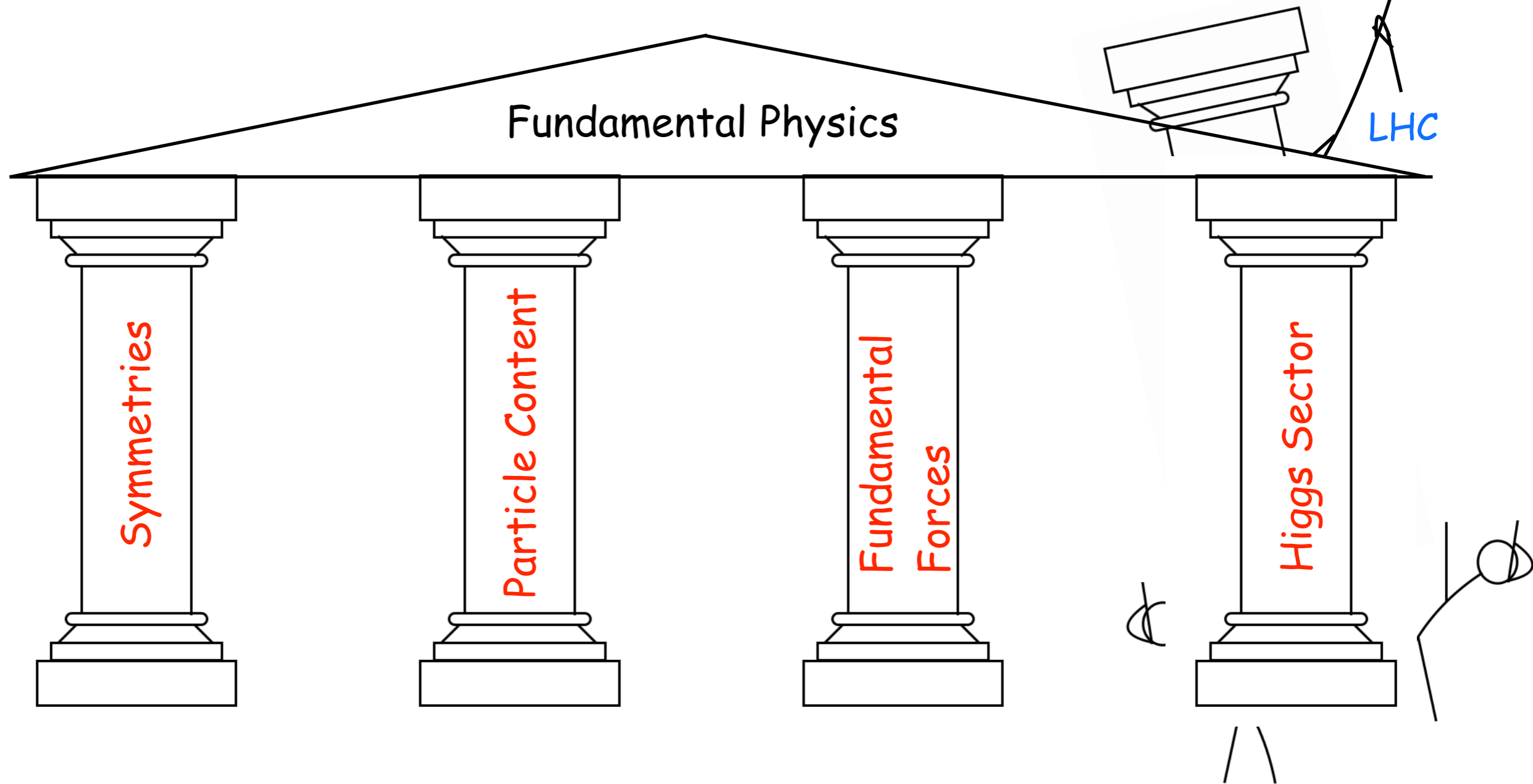
- 1) Qinhuangdao, Hebei Province (Completed in 2014)
- 2) Huangling, Shanxi Province (Completed in 2017)
- 3) Shenshan, Guangdong Province (Completed in 2016)
- 4) Baoding (Xiong'an), Hebei Province (Started in August 2017)
- 5) Huzhou, Zhejiang Province (Started in March 2018)
- 6) Jiamusi, Heilongjiang Province (Started in May 2018)
- 7) Changde, Hunan Province (Started in Dec. 2018)



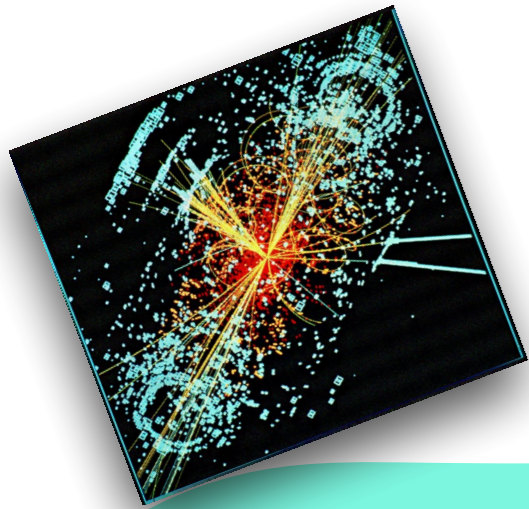
# Introduction



# The Standard Model is Structurally Complete

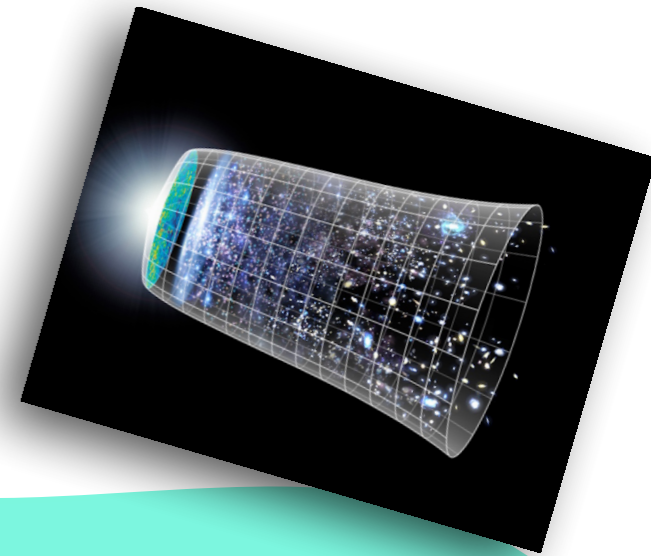


# Open Questions



## Particle physics

- ❖ origin of electroweak symmetry breaking
- ❖ hierarchy problem
- ❖ nature of the Higgs boson
- ❖ fermion mass and flavor puzzle
- ❖ origin of neutrino masses



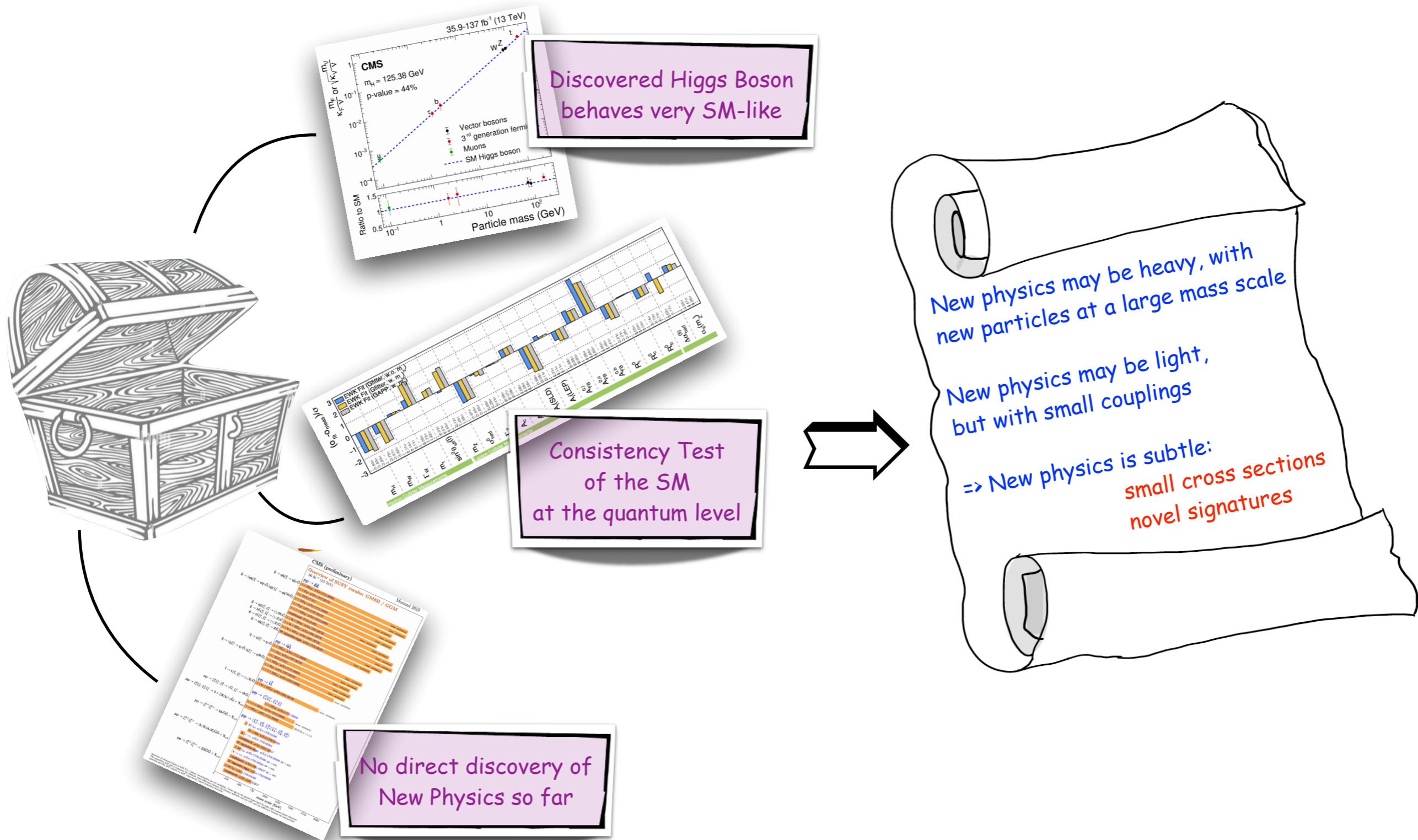
## Cosmology

- ❖ nature of Dark Matter
- ❖ matter-antimatter asymmetry
- ❖ dark energy
- ❖ inflation
- ❖ how to incorporate gravity

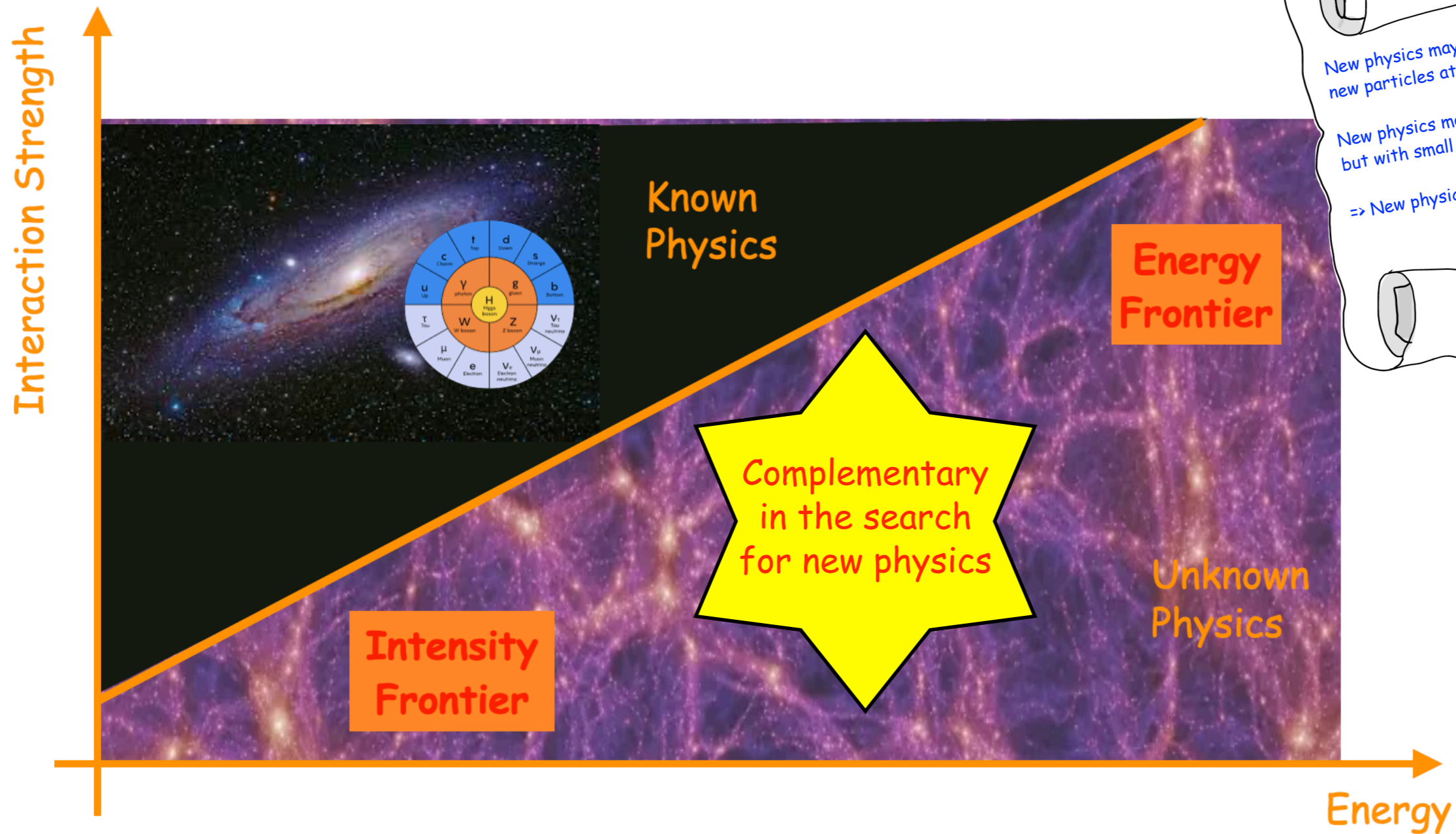
Decipherment of fundamental laws of nature:  
judicious combination of  
theoretical methods/interpretation  
and experimental input/scrutiny

New physics is required, but there is no clear indication at which energy scale

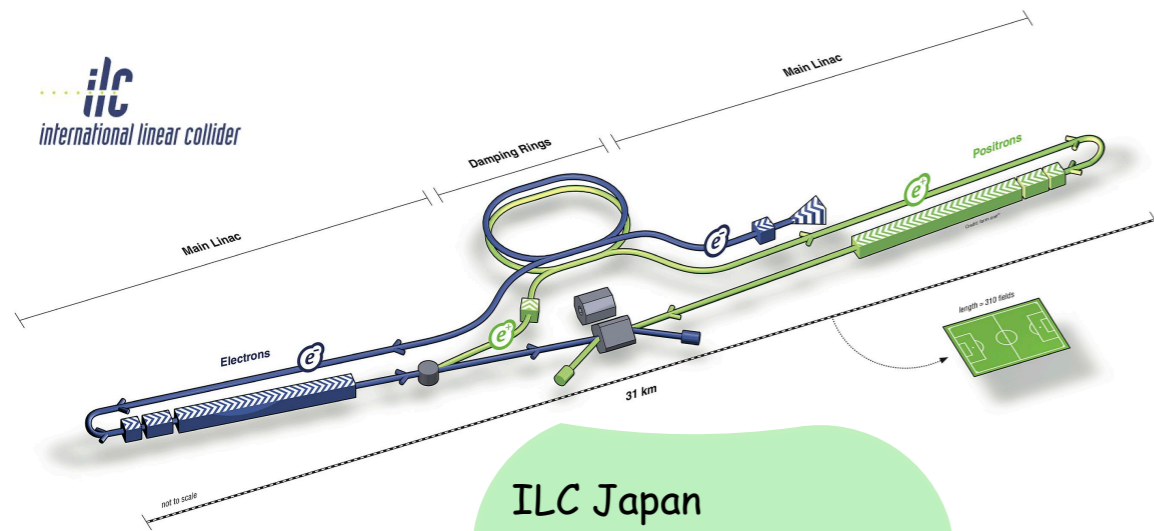
# The Challenge



# Search for New Physics



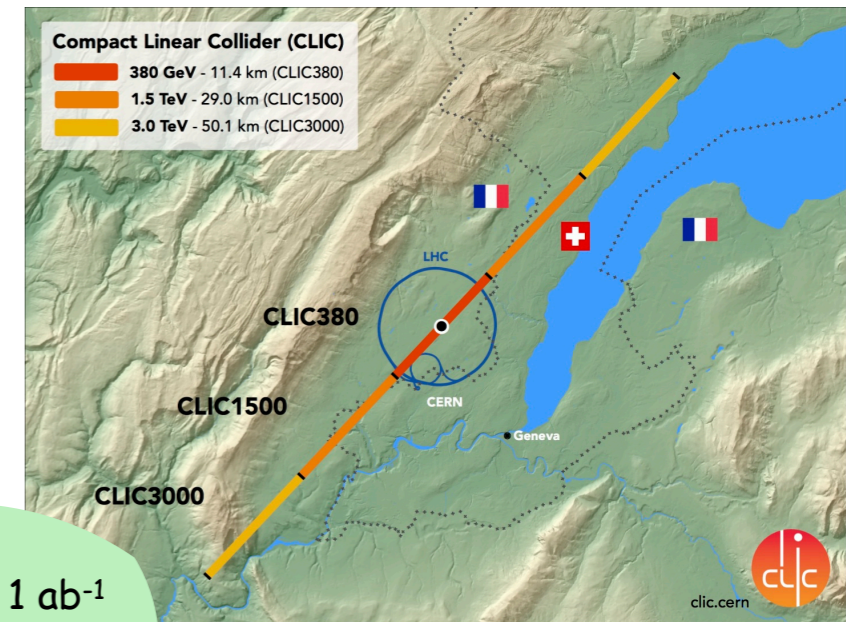
# Future $e^+e^-$ Collider Projects



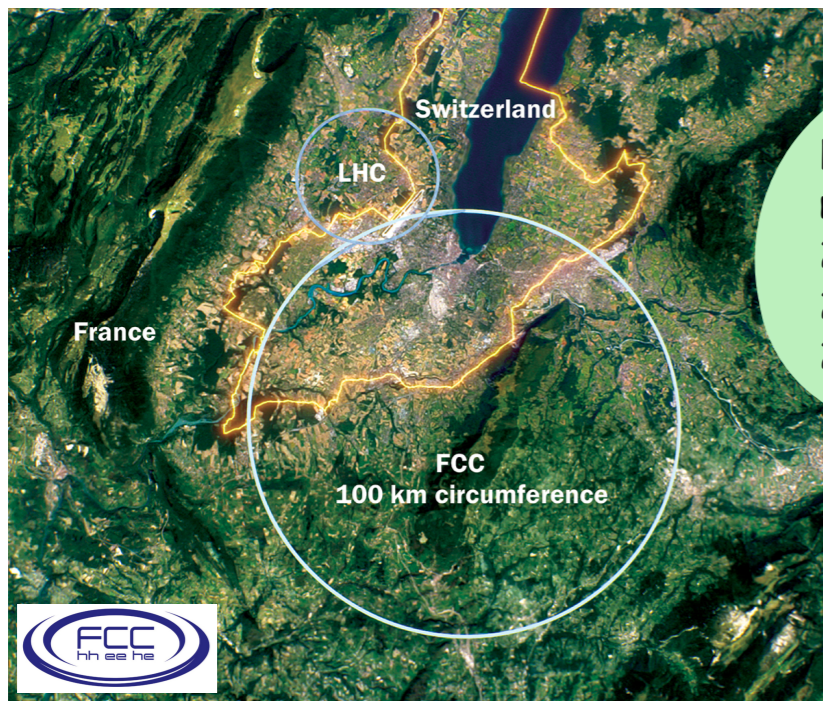
**ILC Japan**  
 250 GeV, 11y  $\rightarrow$  2  $ab^{-1}$   
 500 GeV, 8.5y 4  $ab^{-1}$   
 1000 GeV, 8.5y 8  $ab^{-1}$



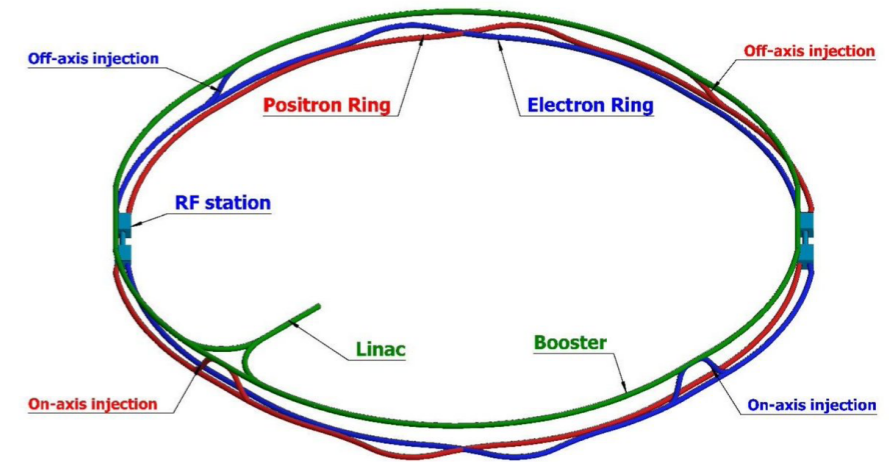
**Cool Copper Collider**  
 250 GeV  $\rightarrow$   $1.3 \times 10^{34}/cm^2s$   
 550 GeV  $2.4 \times 10^{34}/cm^2s$



**CLIC, CERN**  
 380 GeV, 8y  $\rightarrow$  1  $ab^{-1}$   
 1500 GeV, 7y 2.5  $ab^{-1}$   
 3000 GeV, 8.5y 5  $ab^{-1}$



**FCC-ee, CERN**  
 mz, 4y  $\rightarrow$  150  $ab^{-1}$   
 2 mw, 1-2y 10  $ab^{-1}$   
 240 GeV, 3y 5  $ab^{-1}$   
 2  $m_{top}$ , 5y 1.5  $ab^{-1}$

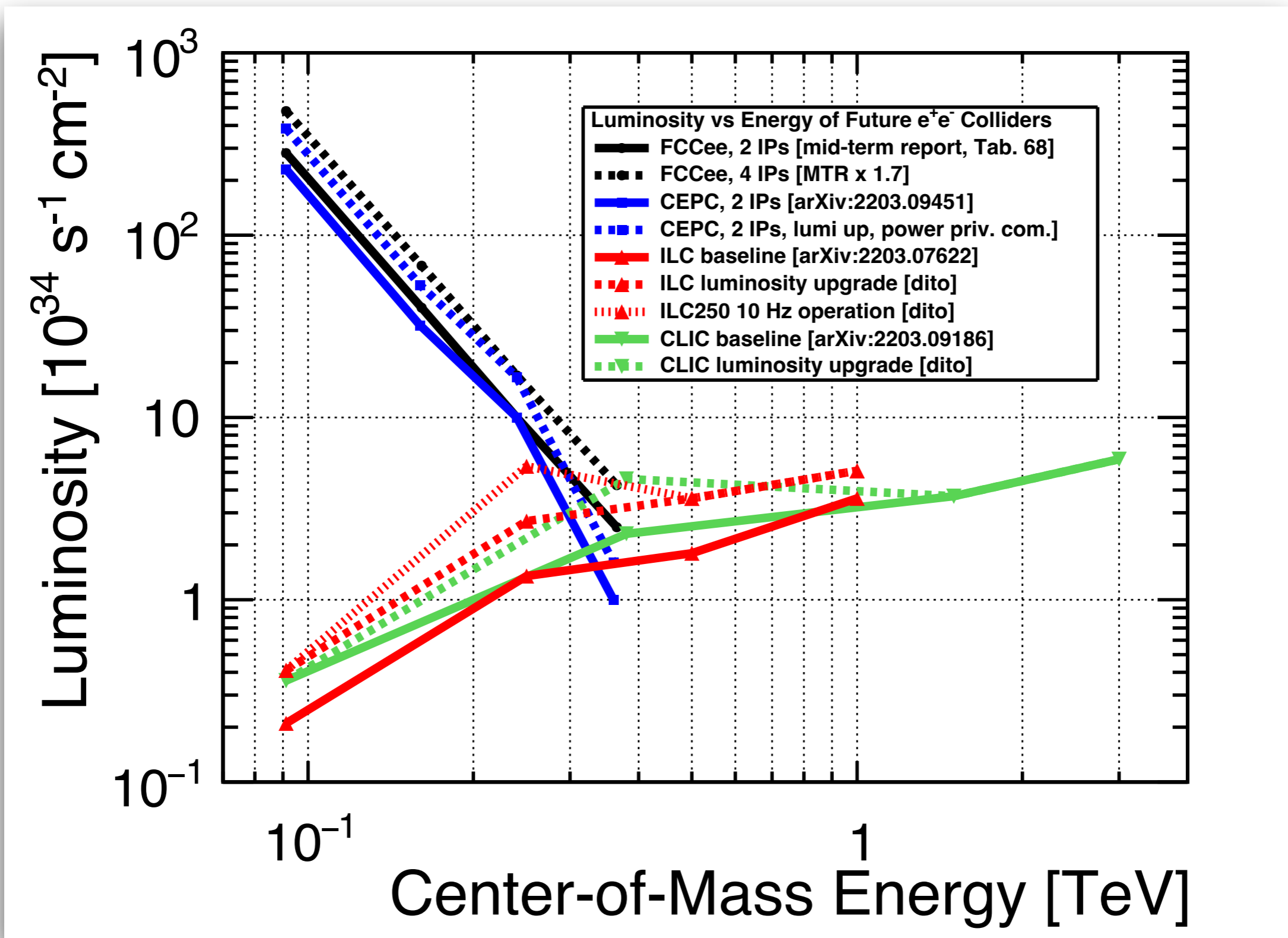


**CEPC, China**  
 mz, 2y  $\rightarrow$  16  $ab^{-1}$   
 2 mw, 1y 2.6  $ab^{-1}$   
 240 GeV, 7y 5.6  $ab^{-1}$

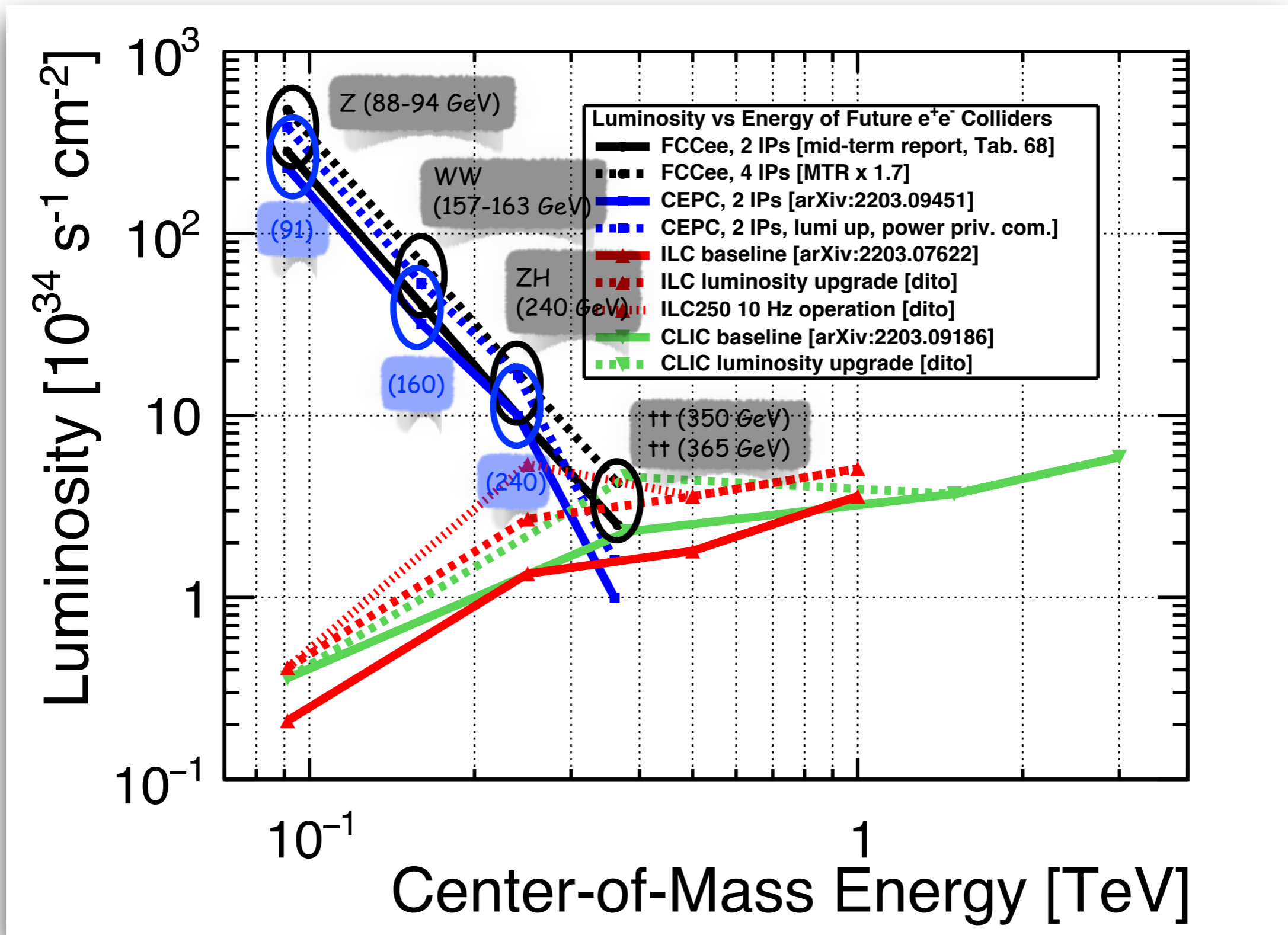




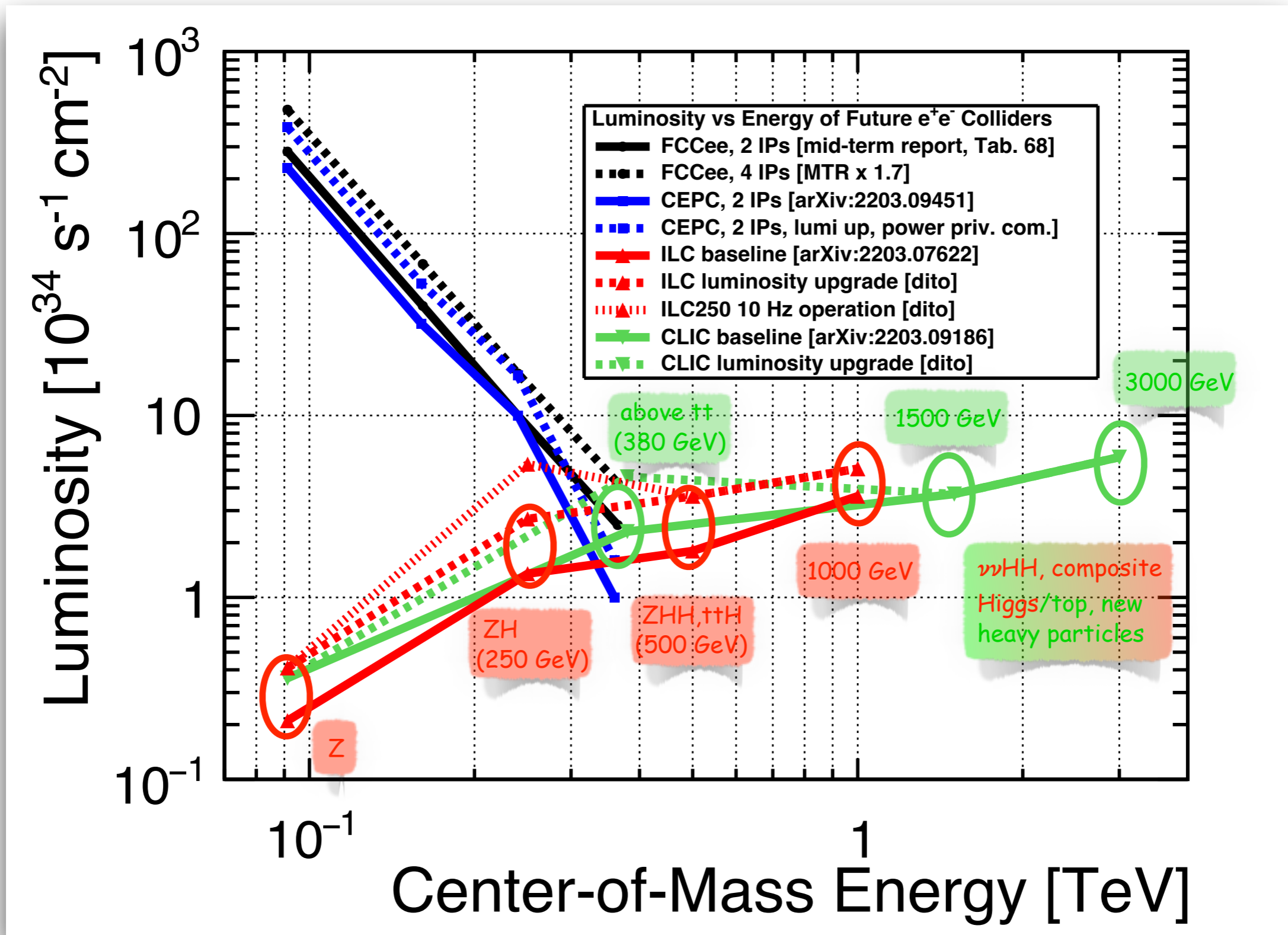
# ee-Colliders Energy Range & Luminosity



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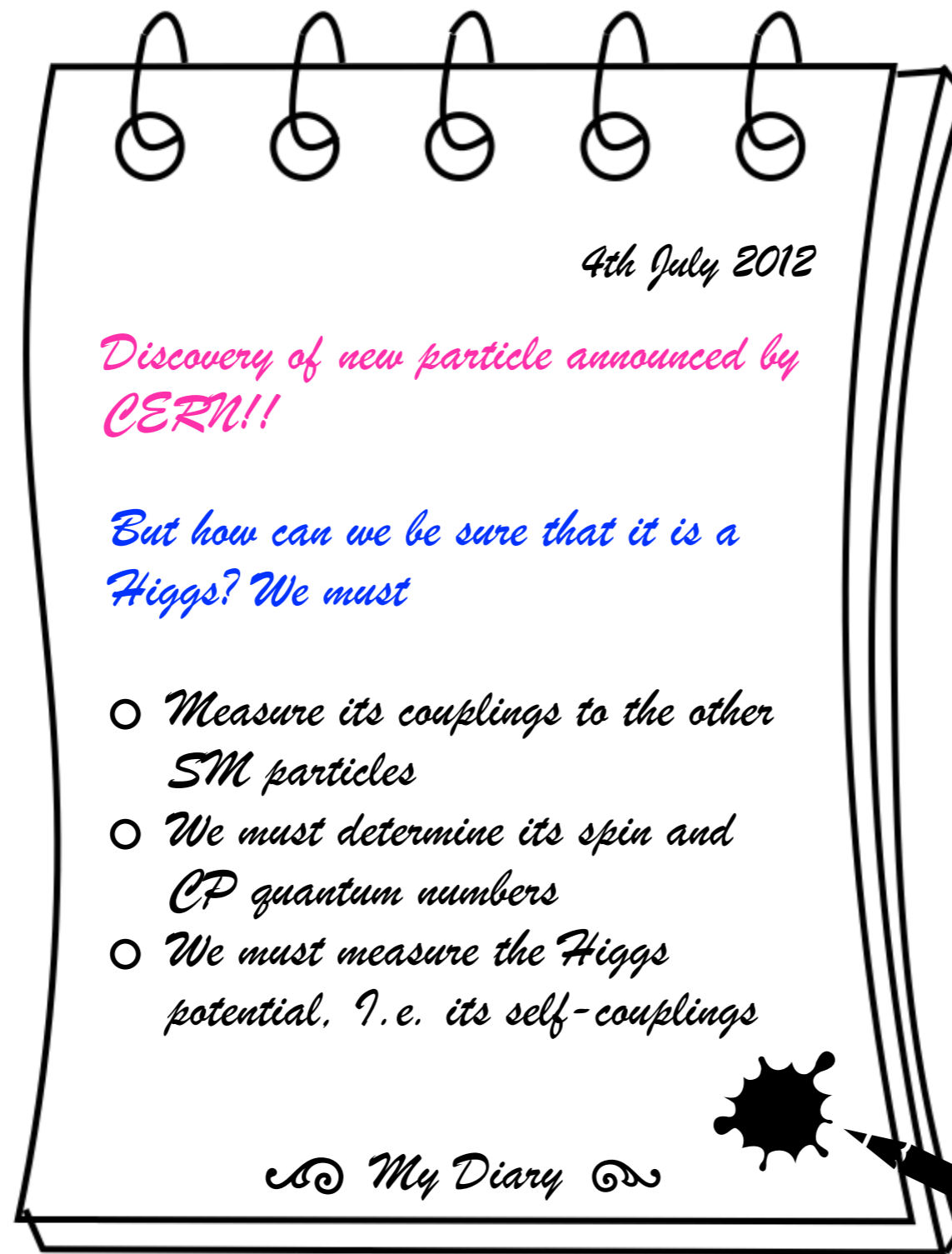
# ee-Colliders Energy Range & Luminosity



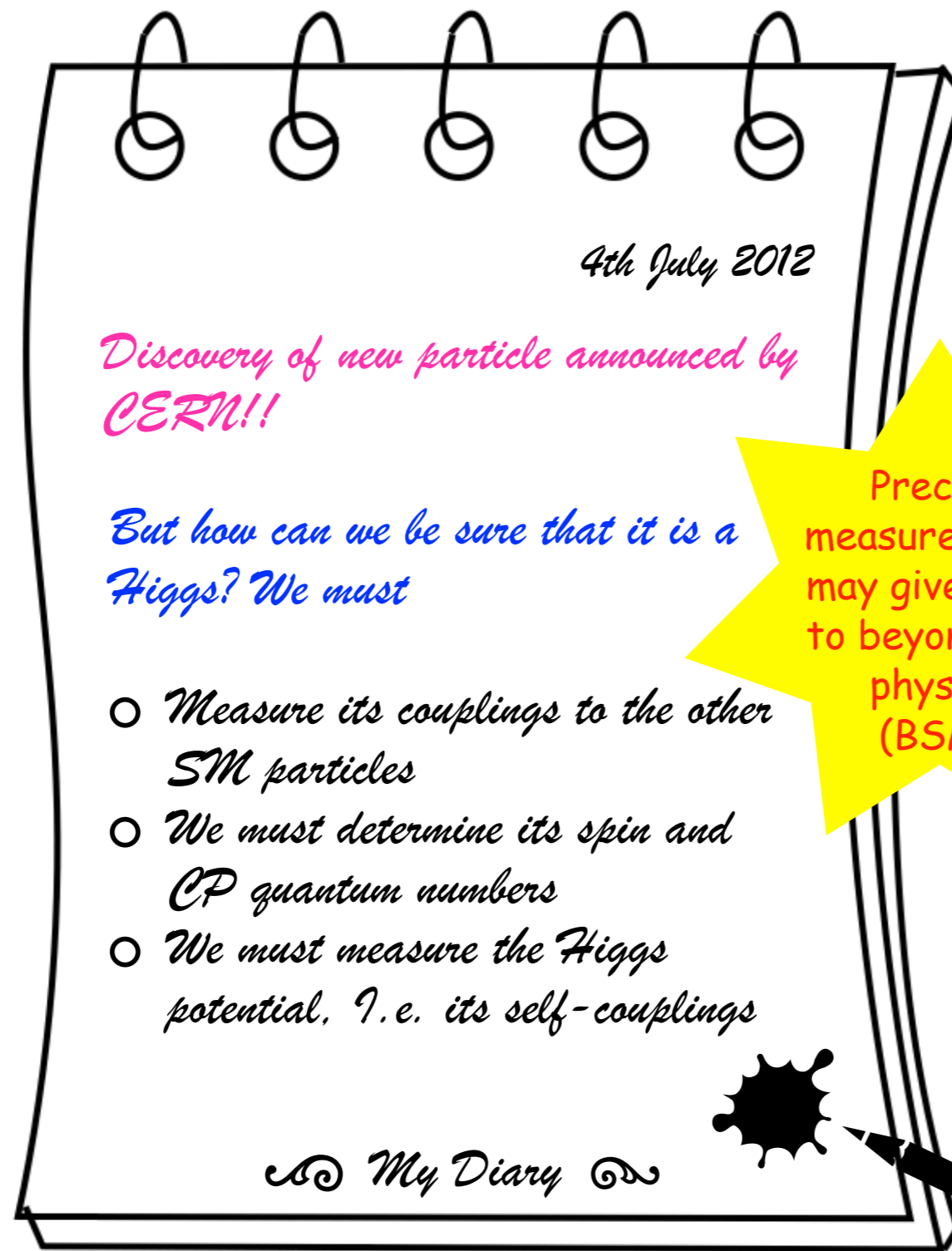
A photograph of a bougainvillea plant with vibrant pink and red flowers. The plant is growing against a white wall. To the right, there is a window with green shutters. The flowers are in various stages of bloom, with some showing bright pink and others a deeper red. The branches are woody and have some bare, thorny sections. The overall scene is brightly lit, suggesting a sunny day.

Higgs Factory

# Establishing the Higgs Mechanism



# Establishing the Higgs Mechanism



4th July 2012

Discovery of new particle announced by CERN!!

But how can we be sure that it is a Higgs? We must

- Measure its couplings to the other SM particles
- We must determine its spin and CP quantum numbers
- We must measure the Higgs potential, i.e. its self-couplings

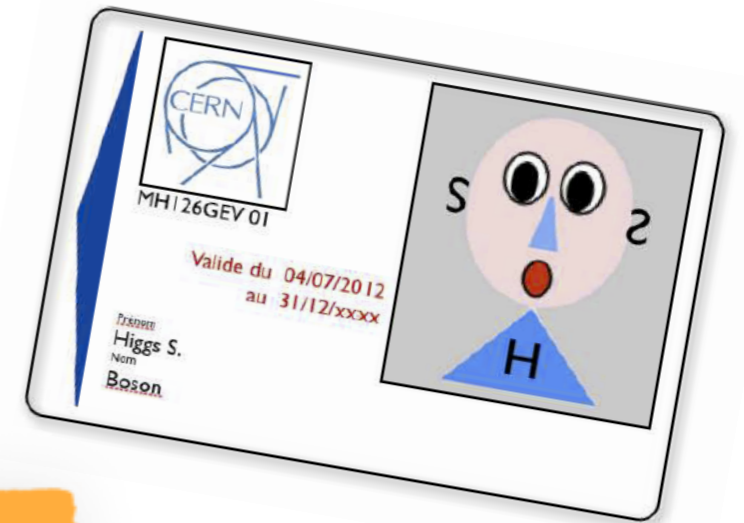
My Diary



Precise measurements may give hints to beyond-SM physics (BSM)

# Role of the Higgs Boson

- ♦ We have the SM-like Higgs boson
- What can we learn from Higgs physics?



- ♦ Corner new physics with the Higgs:

$$\mathcal{L}_{\text{Higgs}} = (\mathcal{D}_\mu \Phi_i)(\mathcal{D}^\mu \Phi_i)^\dagger - V(\Phi_i) + \mathcal{L}_{\text{Yukawa}}$$

- anomalous Higgs gauge couplings
- CP violation

- ⇒ New Physics & DM
- ⇒ Compositeness
- ⇒ Baryogenesis

- coupling relations  $g_x \sim m_x^{(2)}$

- ⇒ Establish Higgs mechanism/Unique?
- ⇒ Compositeness

- Higgs mass
- Higgs self-interaction
- vacuum structure
- CP violation
- portal to hidden sector

- ⇒ Self-consistency SM
- ⇒ Ultimate test Higgs mechanism
- ⇒ Vacuum stability
- ⇒ New Physics
- ⇒ Dark Matter
- ⇒ Matter asymmetry
- ⇒ Evolution of Universe
- ⇒ Baryogenesis

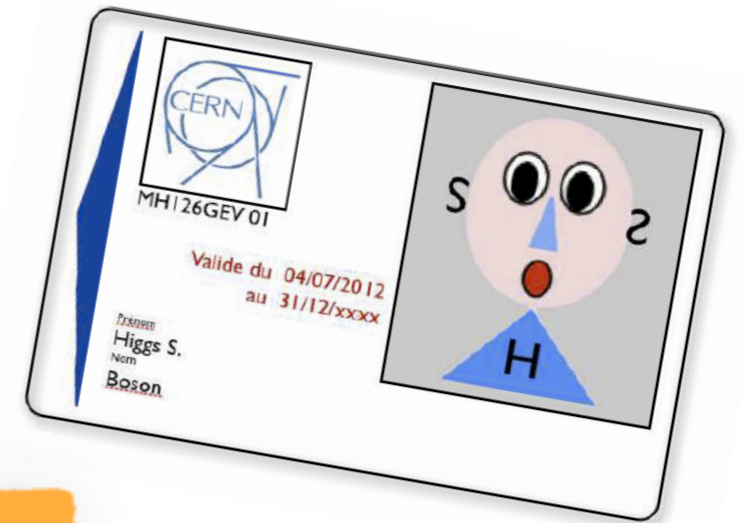
- anomalous Higgs fermion couplings
- CP violation

- ⇒ Flavor/Matter puzzle
- ⇒ Unique?
- ⇒ New Physics
- ⇒ Compositeness
- ⇒ Baryogenesis



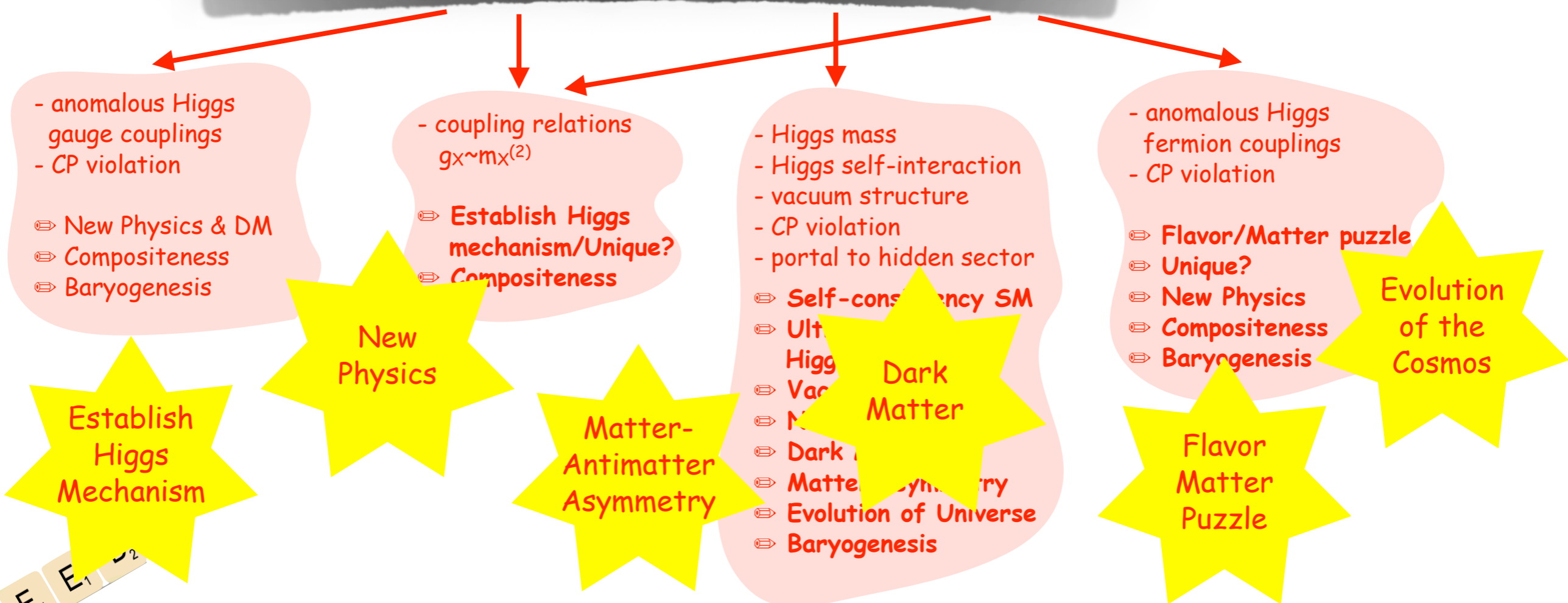
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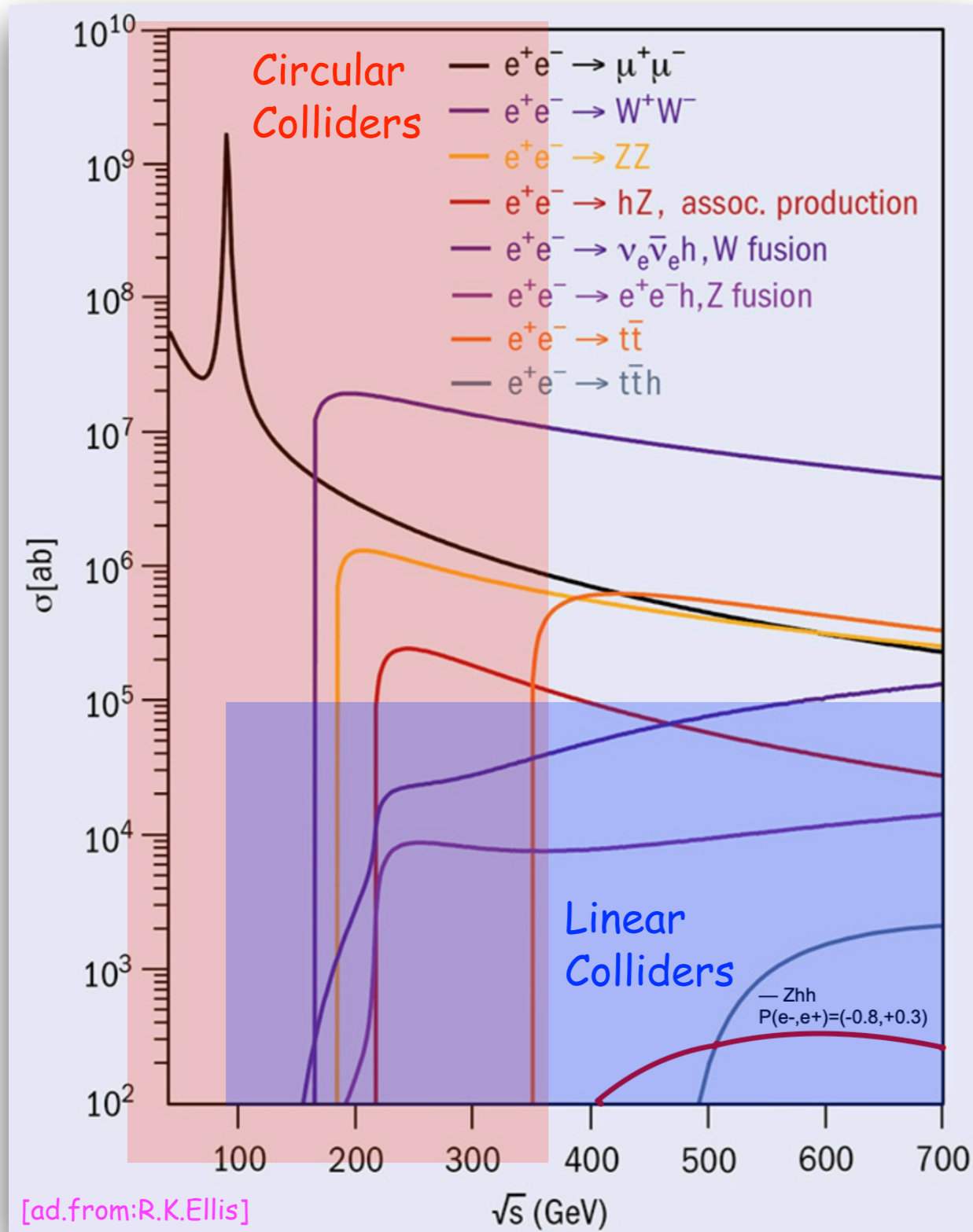




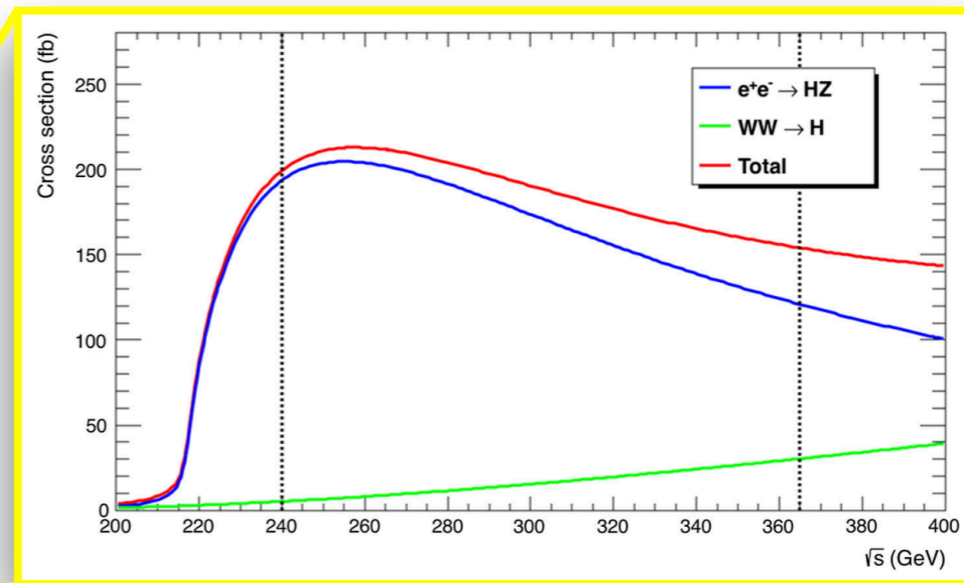
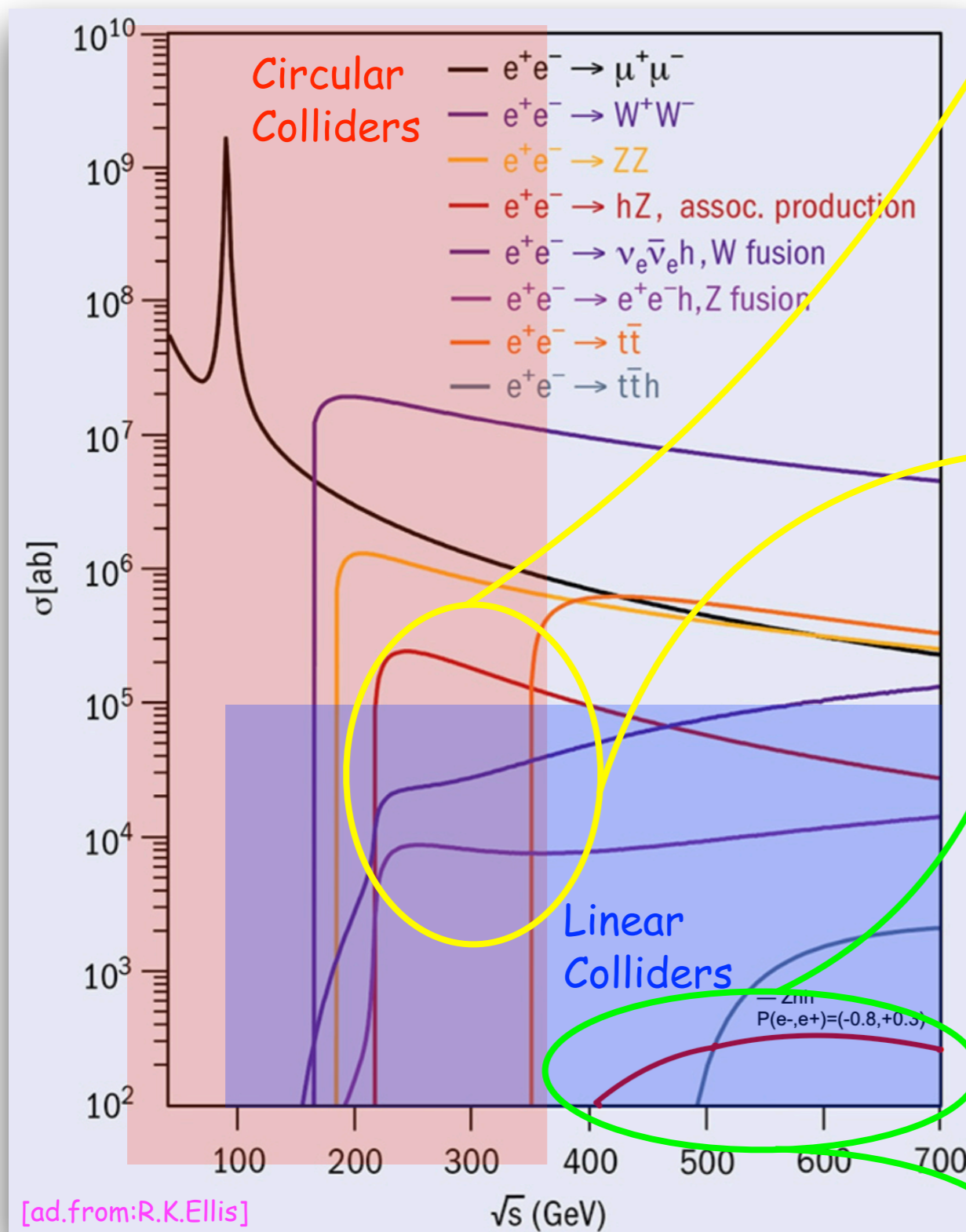
# The Higgs Factory



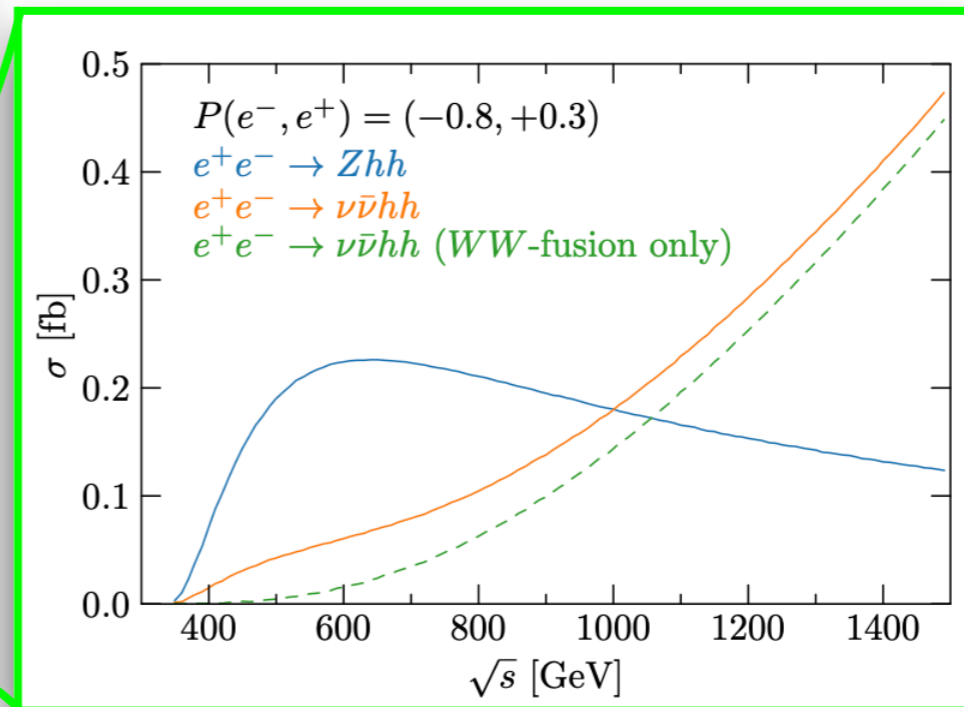
N<sub>1</sub> E<sub>1</sub> E<sub>1</sub> D<sub>2</sub>



# The Higgs Factory

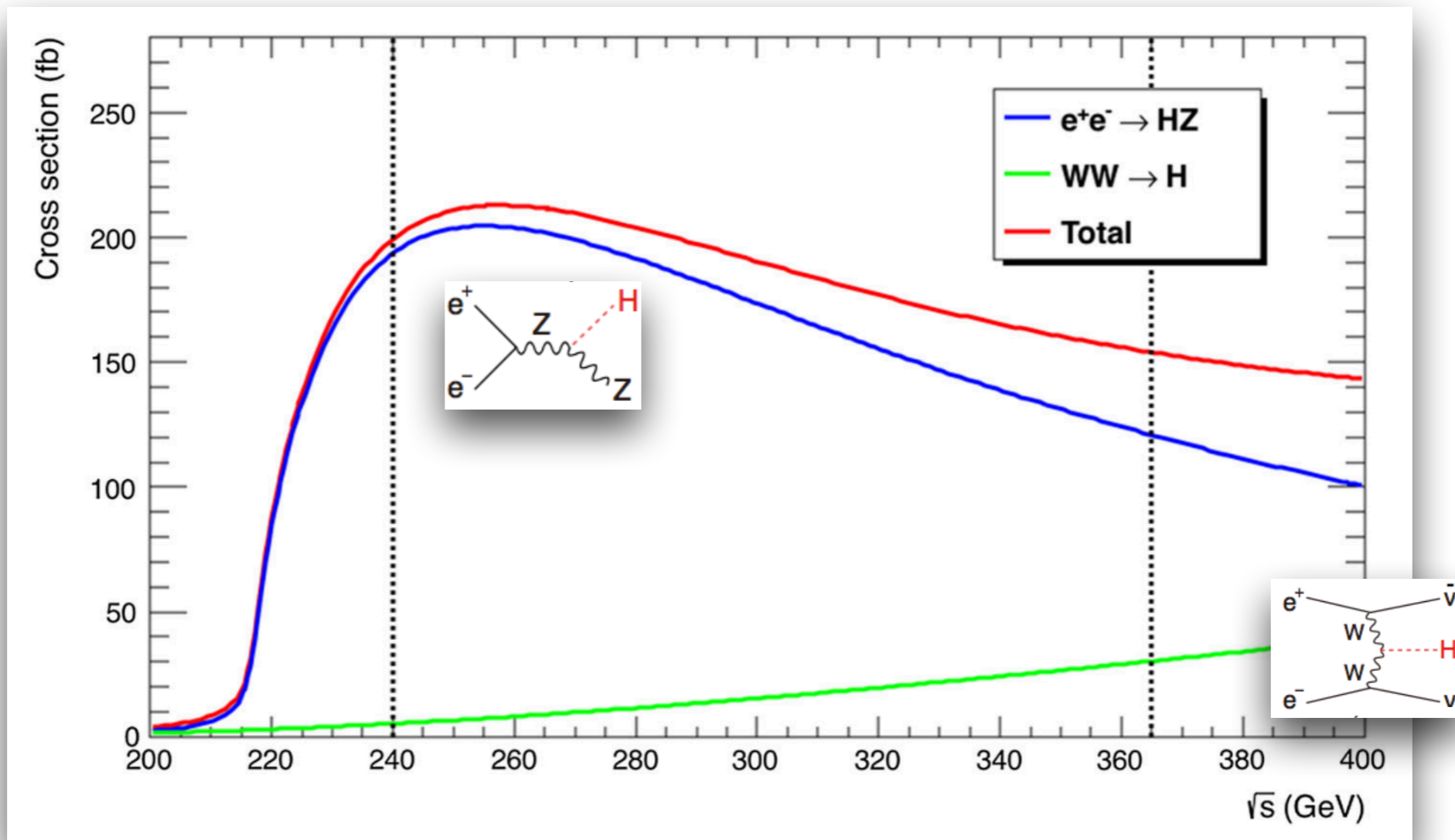


Single Higgs Production



Double Higgs Production

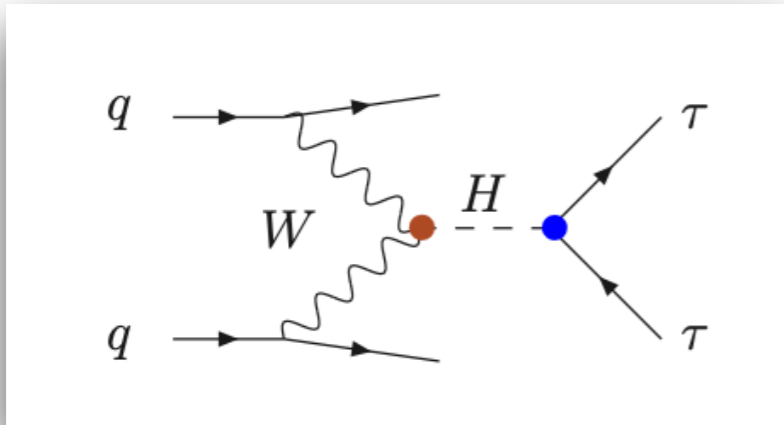
# The Higgs Factory



$O(10^6)$  Higgs bosons from  $ZH$   
 $O(10^5)$  Higgs bosons from  $H\nu\nu$

# Higgs Coupling Measurements

- ❖ **Higgs mechanism:** Higgs couplings to SM particles  $\sim$  to masses of the particles
- ❖ **Experimental test:** various production and decay channels  $\leadsto$  extract couplings

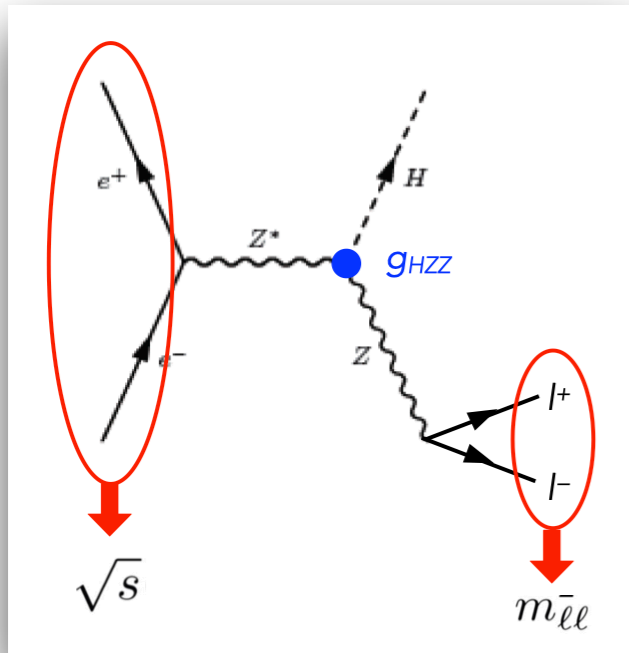


$$\sim \Gamma_{WW} \times \text{BR}(H \rightarrow \tau\tau) \sim \Gamma_{WW} \times \Gamma(H \rightarrow \tau\tau) / \Gamma_{\text{tot}}$$

**at LHC:** not all final states are accessible  
small SM  $\Gamma_{\text{tot}}$  non measurable

# Higgs Coupling Measurements

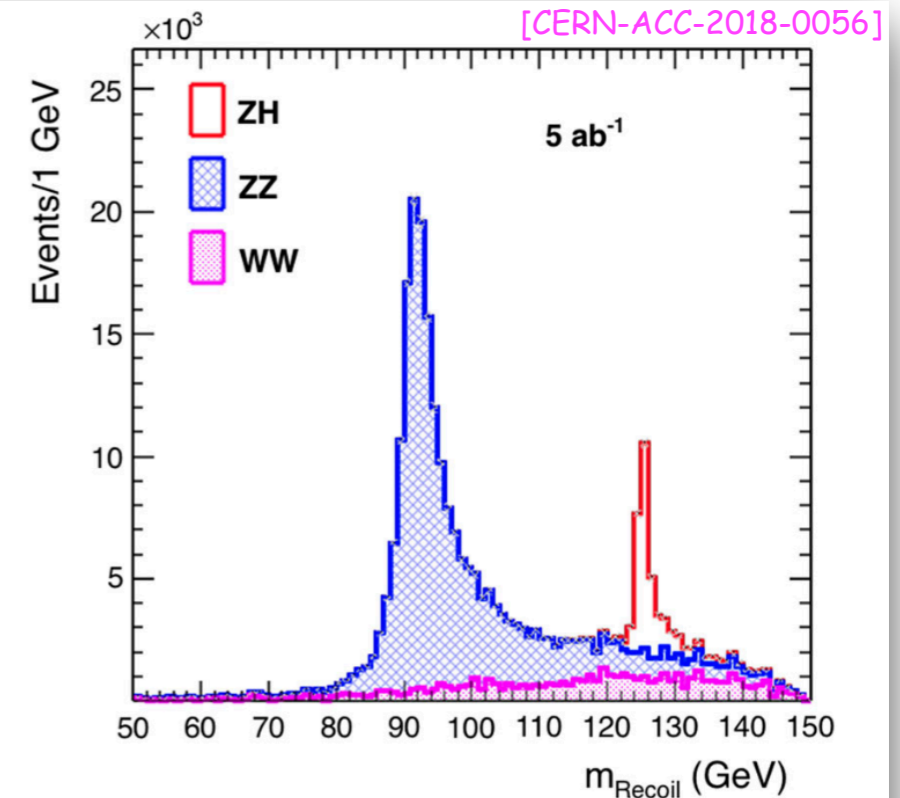
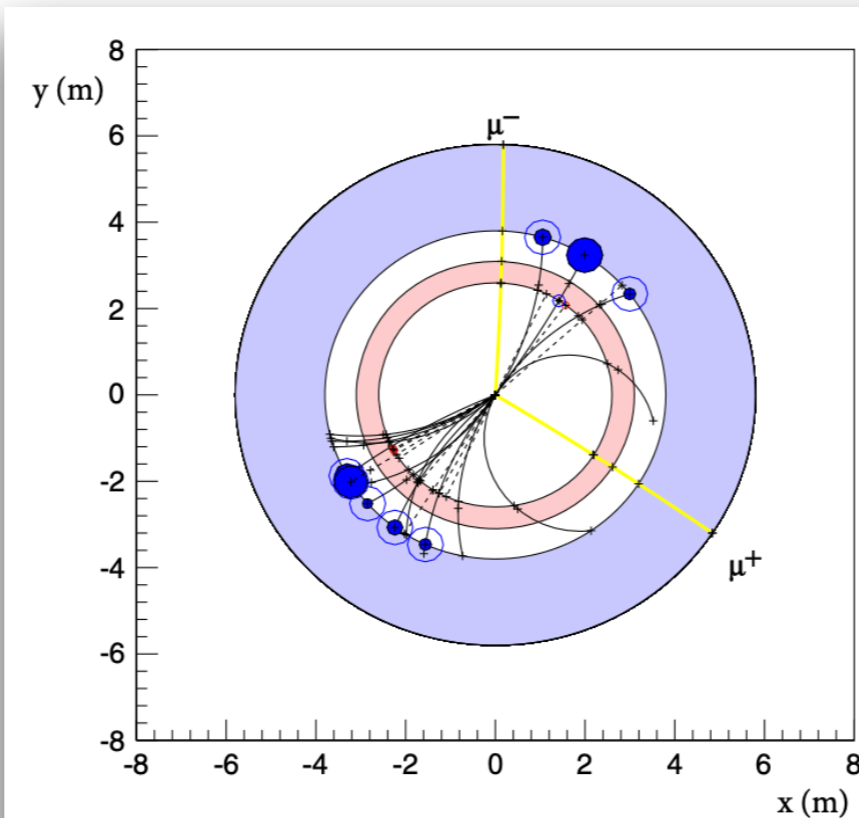
## ❖ $e^+e^-$ Collider: Absolute coupling measurement



$$m_{\text{recoil}}^2 = s + m_{\ell\bar{\ell}}^2 - 2\sqrt{s}(E_{\ell^+} + E_{\ell^-})$$

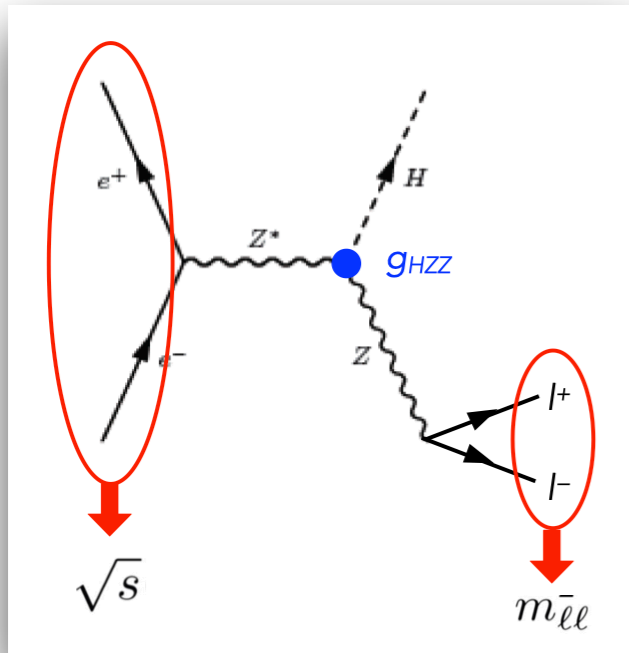
Fit to recoil mass distribution:

- $\sigma(\text{ZH})$  measurement independent of Higgs decay
- $\Rightarrow$  absolute determination of  $g_{\text{HZZ}}$



# Higgs Coupling Measurements

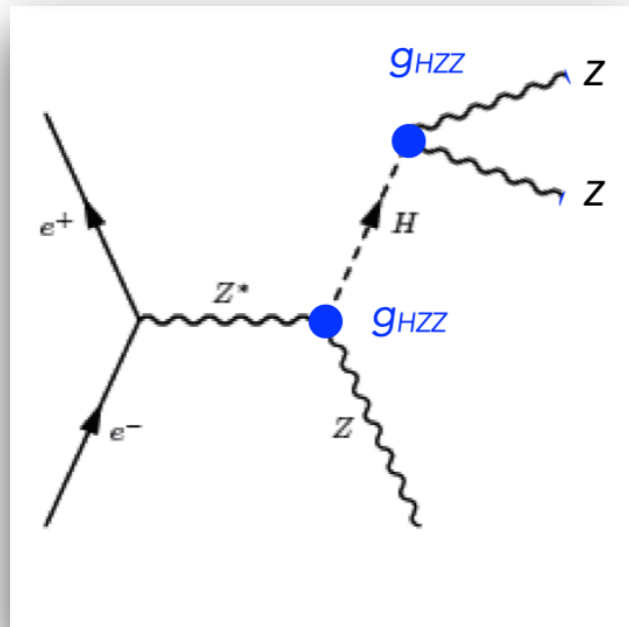
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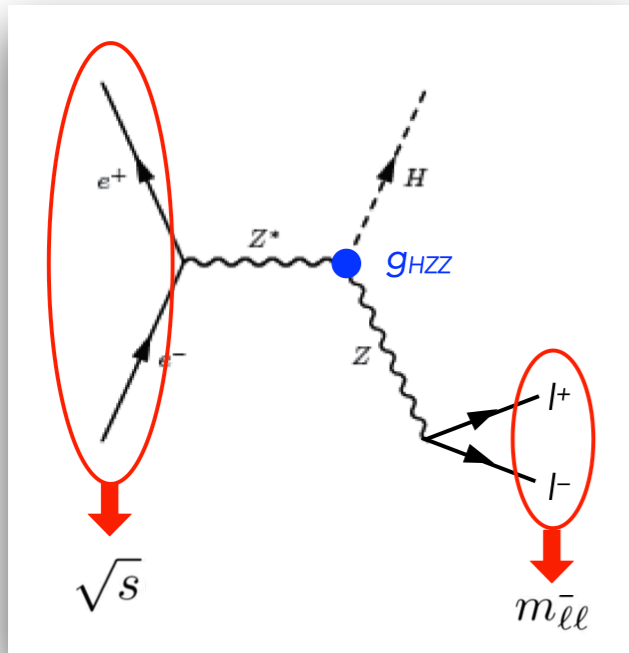


$$\sigma_{HZ} \times \Gamma(H \rightarrow ZZ)/\Gamma_H \sim (g_{HZZ})^4/\Gamma_H$$

$\Rightarrow$  extraction of  $\Gamma_H$

# Higgs Coupling Measurements

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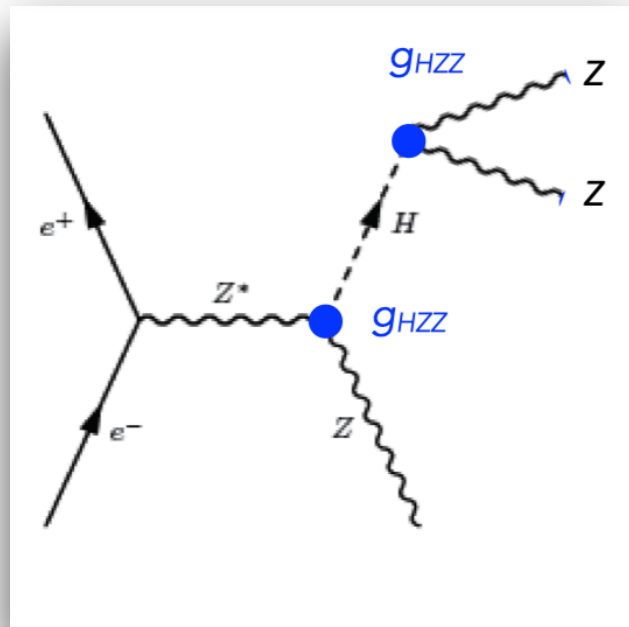


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Exclusive decays into  $XX = bb, cc, gg, \tau, \mu\mu, WW, \gamma\gamma, Z\gamma$ , invisible, other new BSM states  $\Rightarrow$  absolute coupling extraction  $g_{HXX}$



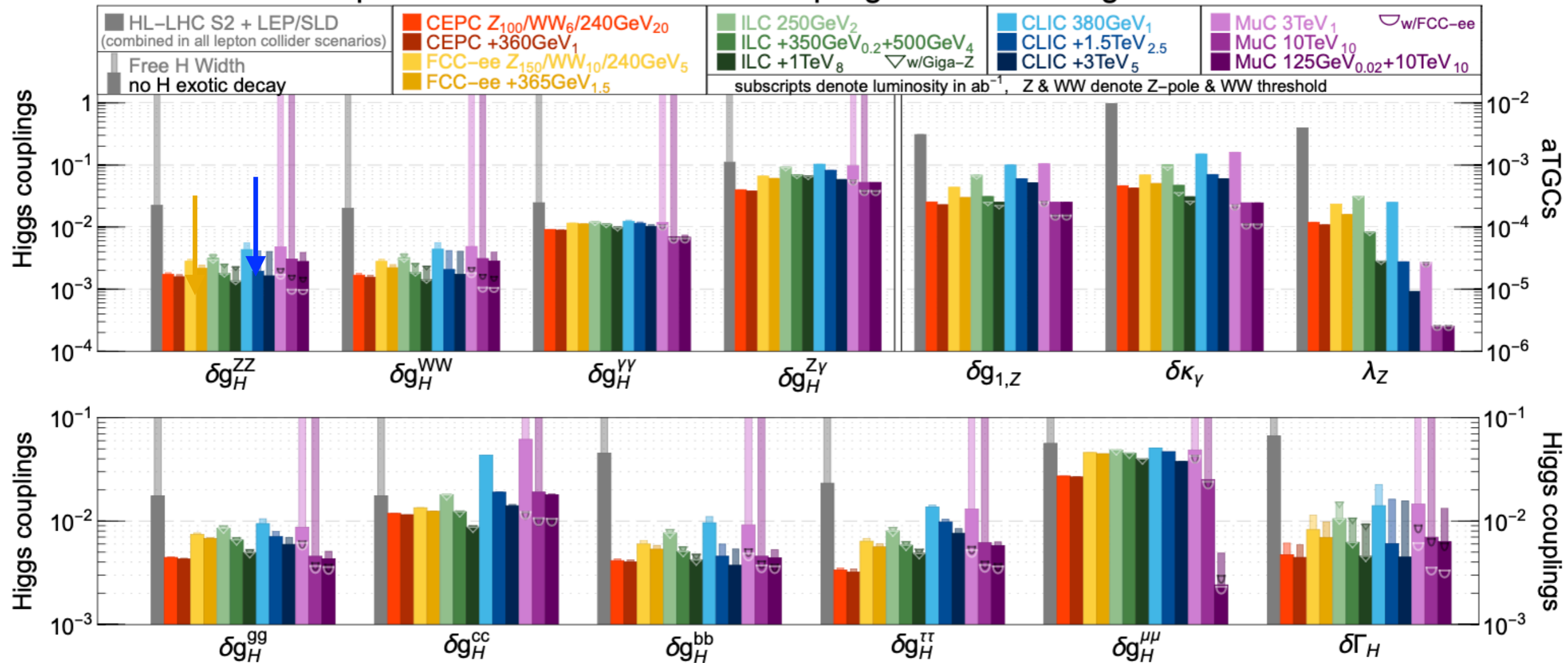
$$\sigma_{HZ} \times \Gamma(H \rightarrow ZZ) / \Gamma_H \sim (g_{HZZ})^4 / \Gamma_H$$

$\Rightarrow$  extraction of  $\Gamma_H$

# Higgs Coupling Measurements

precision reach on effective couplings from SMEFT global fit

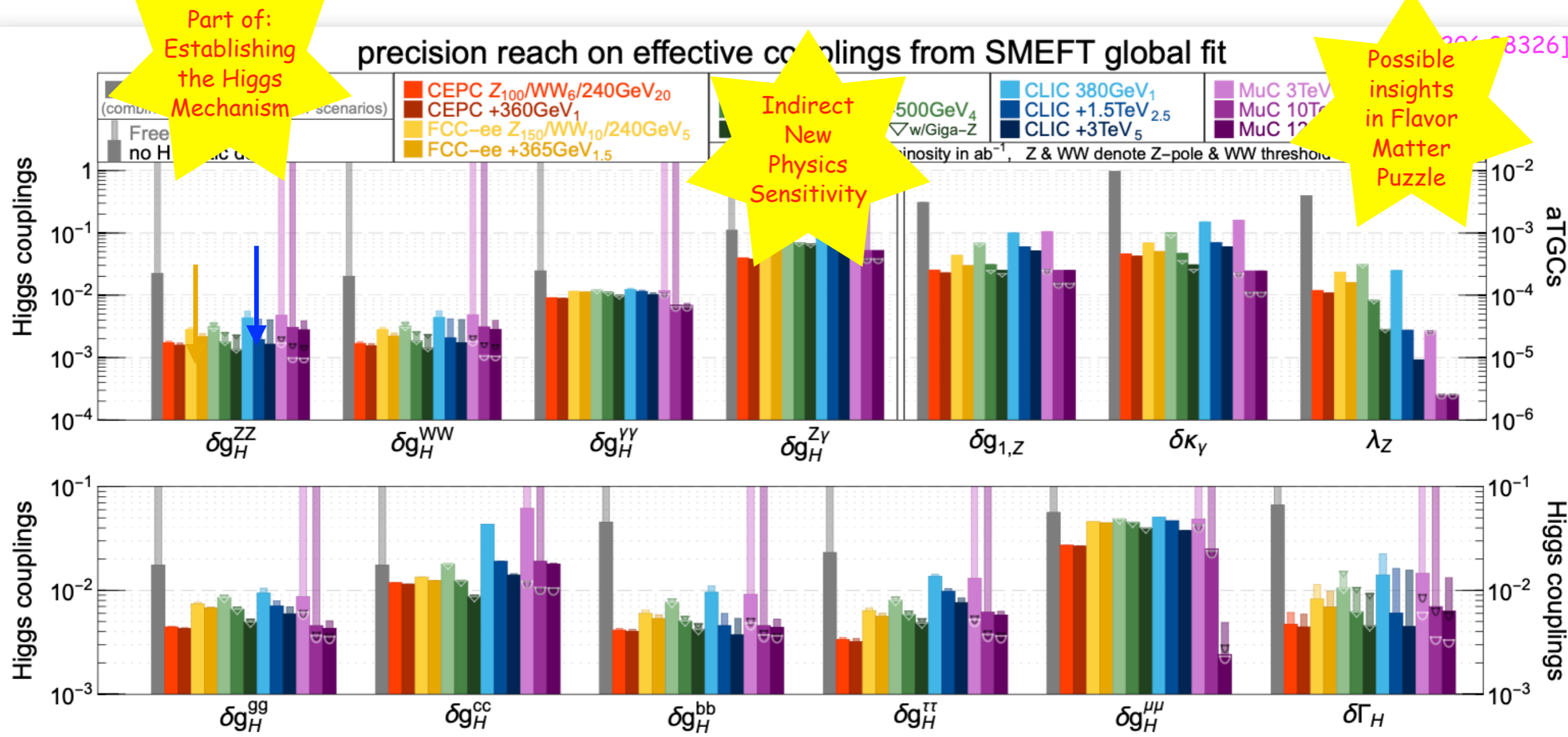
[2206.08326]



- ⇒ all Higgs factories perform similar: luminosity vs. polarization
- ⇒ couplings will be pushed to single percent - few per mille
- ⇒ at least 1 order of magnitude precision gain compared to HL-LHC



# Higgs Coupling Measurements



- ⇒ all Higgs factories perform similar: luminosity vs. polarization
- ⇒ couplings will be pushed to single percent - few per mille precision
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# What do we Learn?

- \* **What do we learn about new physics from indirect measurements** through enhanced precision (~factor 10 better than HL-LHC) in comparison to direct new physics searches at the HL-LHC?
- \* **Which new physics scales** can we probe?
- \* **What can we learn from the patterns of the coupling deviations** about the **underlying model**?
- \* **How well can we distinguish between different realizations** of possible BSM physics?

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⇒ Coupling deviations due to new physics\*:  $g = g_{SM}[1 + \Delta] : \Delta = O(v^2/\Lambda^2)$

Experimental accuracy  $O(0.2) \dots O(0.01) \Rightarrow$   
Probed new physics scale:  $\Lambda = 550 \text{ GeV} \dots 2.5 \text{ TeV}$

\* Unless violation of decoupling theorem

# What do we Learn?

⇒ Coupling deviations due to new physics:  $g = g_{SM}[1 + \Delta]$  :  $\Delta = O(v^2/\Lambda^2)$

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Probed new physics scale:  $\Lambda = 550 \text{ GeV} \dots 2.5 \text{ TeV}$

Mixing effects:  $\sim v^2/M^2$

- Higgs mixes w/ other high-mass scalar fields
- singlet, doublet, triplet extensions
- strongly interacting

Loop effects:  $\sim 1/(16\pi^2) v^2/M^2$

- from new gauge bosons, scalars, fermions
  - supersymmetry, strong dynamics, extra dimensions, see-saw, extended gauge groups
- ↪  $\Lambda = 200 \text{ GeV}$  for  $\Delta = 0.01$

# What do we Learn?

[Englert,Freitas,MM,Plehn,Rauch,Spira,Walz,'14]

Scenario/framework	LHC	HL-LHC	LC	HL-LC
Higgs portal	0.23	0.28	0.44	0.56
2HDM type-II ( $\tan \beta \approx 1$ )	0.52	0.58	1.15	1.6
2HDM type-II ( $\tan \beta \approx 10$ )	0.33	0.36	0.7	1.0
$D = 6$ effective operators:				
$hVV$	0.78	0.87	2.6	3.3
$hff$	0.45	0.50	1.0	1.4
$hgg$ contact	0.55	1.1	1.3	1.8
$h\gamma\gamma$ contact	0.15	0.18	0.24	0.36
Strong interactions	0.9	1.1–2.0	2.8–5.1	3.4–5.6
$hgg$ loop effects:				
scalar triplet	0.16	0.31	0.37	0.52
scalar octet	0.39	0.75	0.92	1.3
vector octet	1.8	3.5	4.2	5.8
$h\gamma\gamma$ loop effects:				
scalar triplet	0.15	0.18	0.24	0.36
scalar octet	0.25	0.29	0.39	0.60
vector octet	1.1	1.3	1.8	2.7
Vector-like leptons	—	—	1.2	1.5

\* LC: 250+500 GeV/250+500 fb<sup>-1</sup> — HL-LC: 250+500+1000 GeV/ 1150+1600+2500 fb<sup>-1</sup>

# What about Coupling Patterns?

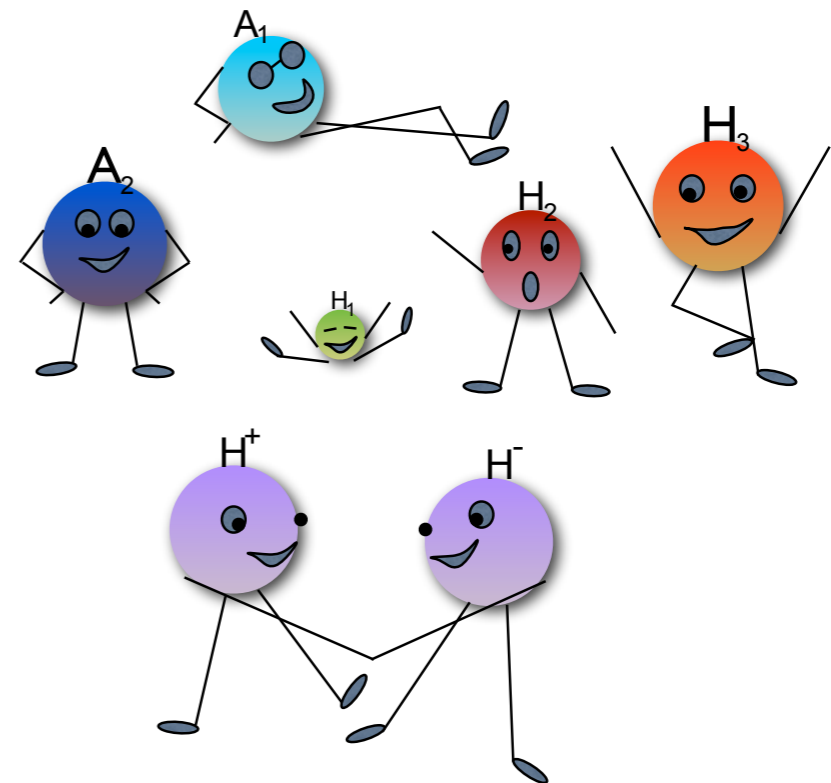
⇒ Exploit coupling sum rules!

Example Next-to-Minimal Supersymmetric Model (NMSSM) w/ 3 Higgs CP-even bosons  $H_i$  ( $i=1,2,3$ )

$$\sum_{i=1}^3 g_{H_i VV}^2 = 1$$

$$\frac{1}{\sum_{i=1}^3 g_{H_i tt}^2} + \frac{1}{\sum_{i=1}^3 g_{H_i bb}^2} = 1$$

**Violation of sum rule:** - hints to not discovered Higgs boson  
- allows distinction from minimal supersymmetric model (MSSM)



# Coupling Violation Patterns in BSM Extensions

[MM,Sampaio,Santos,Wittbrodt,'17]

Models w/  $H_i$  ( $i=1,2,3$ )

$H_\downarrow, H_{125}, H_\uparrow$ :

**CxSM:**

SM+complex singlet

**C2HDM:**

CP-violating 2HDM

**N2HDM:**

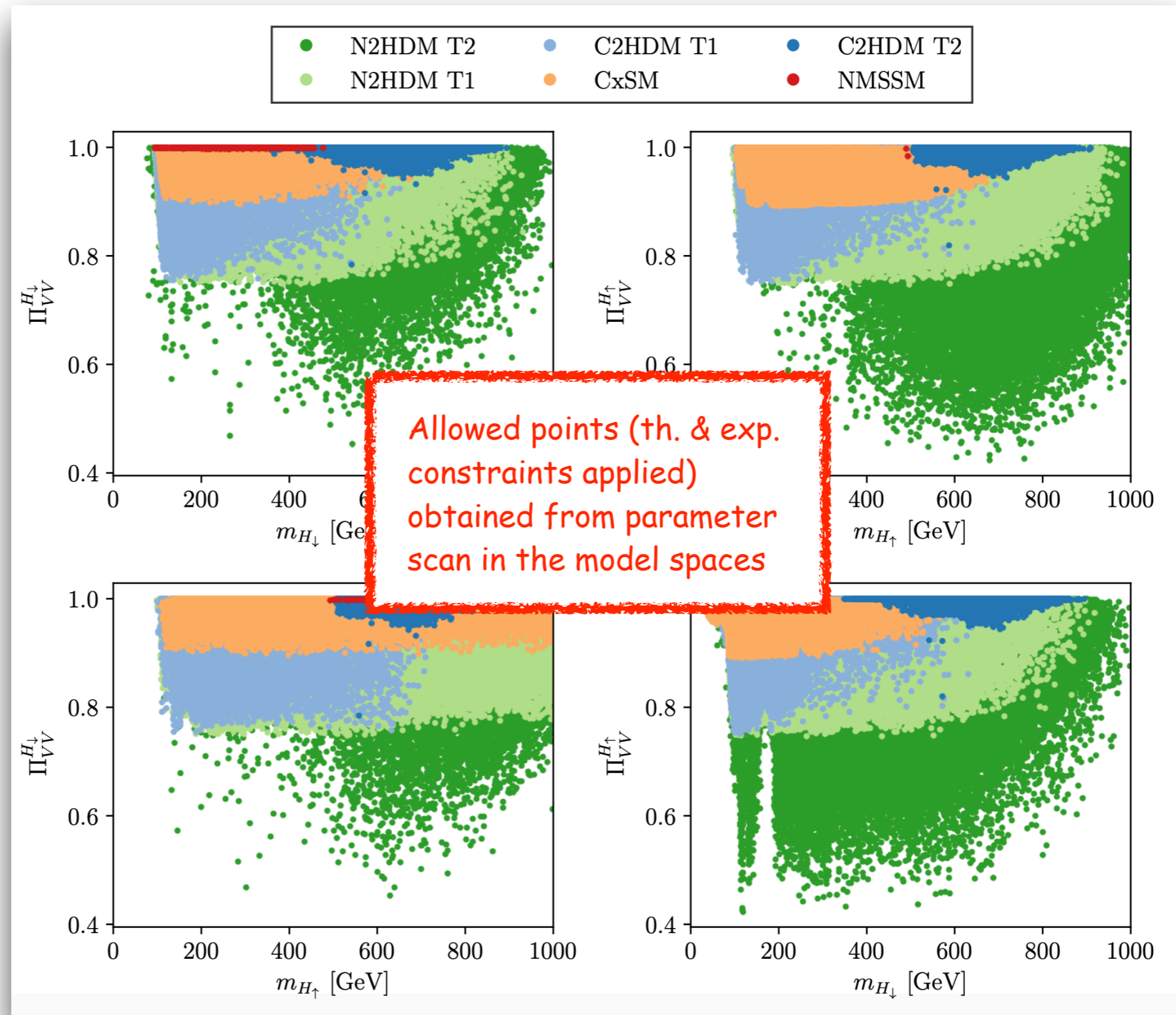
Next-to-2HDM

**NMSSM**

Partial sum  $\Pi_{VV}$ :

$$\sum_i g_{H_i VV}^2 \quad (i=1,2)$$

in case of only two out of three discovered Higgs bosons



# Coupling Violation Patterns in BSM Extensions

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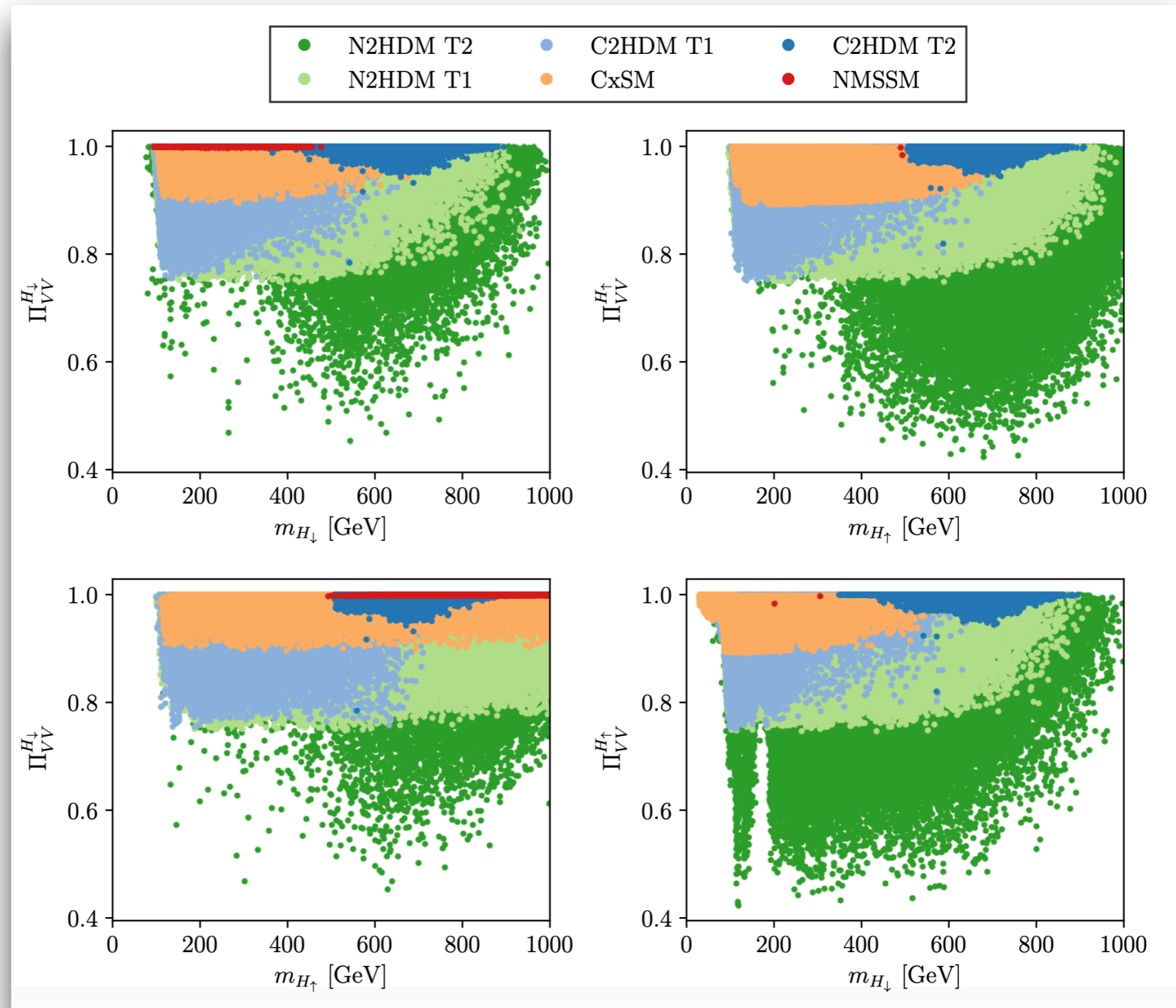
Next-to-2HDM

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in case of only  
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# Trilinear Higgs self-coupling

We must measure the Higgs potential, i.e. self-couplings

❖ SM Higgs potential: in physical gauge

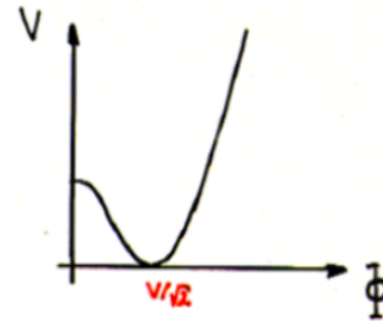
$$V(H) = \frac{1}{2} M_H^2 H^2 + \frac{M_H^3}{2v} H^3 + \frac{M_H^4}{8v^2} H^4$$

Higgs mass :  $M_H = \sqrt{2\lambda} v$

trilinear Higgs self-coupling :  $\lambda_{HHH} = 3M_H^2/M_Z^2$

quadrilinear Higgs self-coupling :  $\lambda_{HHHH} = 3M_H^2/M_Z^4$

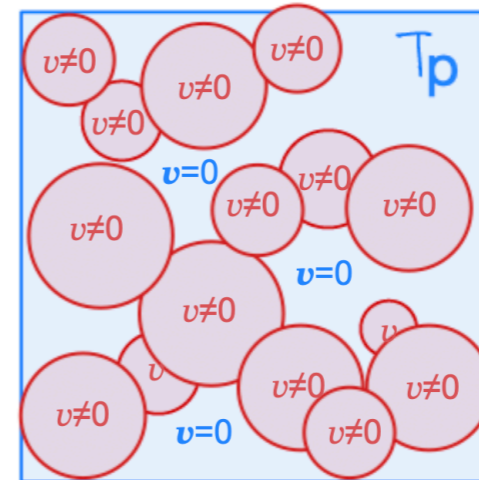
(units  $\lambda_0 = 33.8 \text{ GeV}/\lambda^2$ )



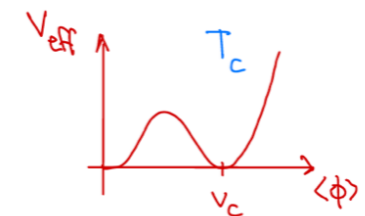
Measurement of the scalar boson self-couplings and Reconstruction of the EWSB potential } Experimental verification of the scalar sector of the EWSB mechanism

❖ Importance of the trilinear Higgs self-coupling:

- Determines shape of the Higgs potential
- Sensitive to beyond-SM physics
- Important input for electroweak phase transition\*



\*matter-asymmetry through electroweak baryogenesis



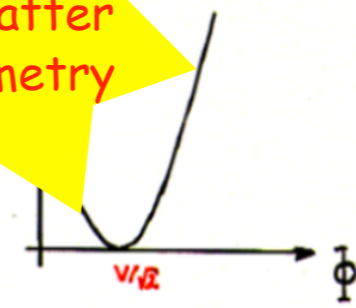
# Trilinear Higgs Self-Coupling

*We must measure the Higgs potential, i.e. self-couplings*

❖ SM Higgs potential: in physical gauge

$$V(H) = \frac{1}{2} m^2 H^2 + \frac{M_H^2}{2v} H^3 + \frac{M_H^2}{8v^2} H^4$$

**Matter-Antimatter Asymmetry**



**Evolution of Cosmos**

Higgs mass :  $M_H = \sqrt{2\lambda} v$

trilinear coupling :  $\lambda_{HHH} = 3M_H^2/M_Z^2$

quartic coupling :  $\lambda_{HHHH} = 3M_H^2/M_Z^4$

(unit  $\lambda = 33.8 \text{ GeV}/\lambda^2$ )

**Ultimate test Higgs Mechanism**

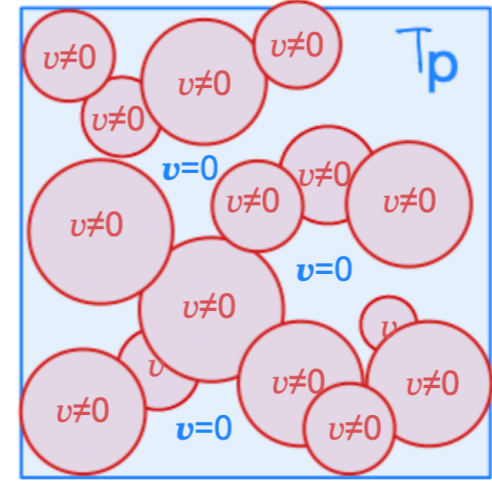
Measurement of trilinear and quartic Higgs boson self-couplings  
 and  
 Reconstruction of the EWSB potential

Experimental verification  
 Of the scalar sector of the  
 EWSB mechanism

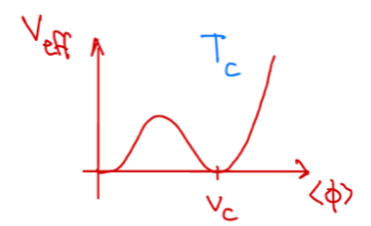
**New Physics**

❖ Importance of the trilinear Higgs self-coupling:

- Determines shape of the Higgs potential
- Sensitive to beyond-SM physics
- Important input for electroweak phase transition\*

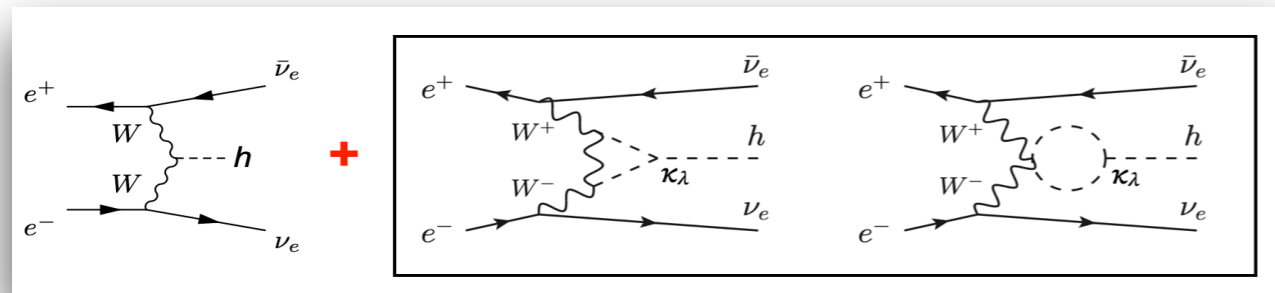
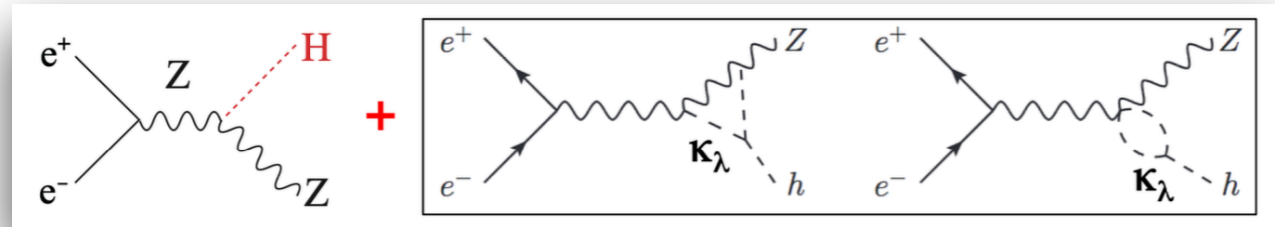


\*matter-asymmetry through electroweak baryogenesis

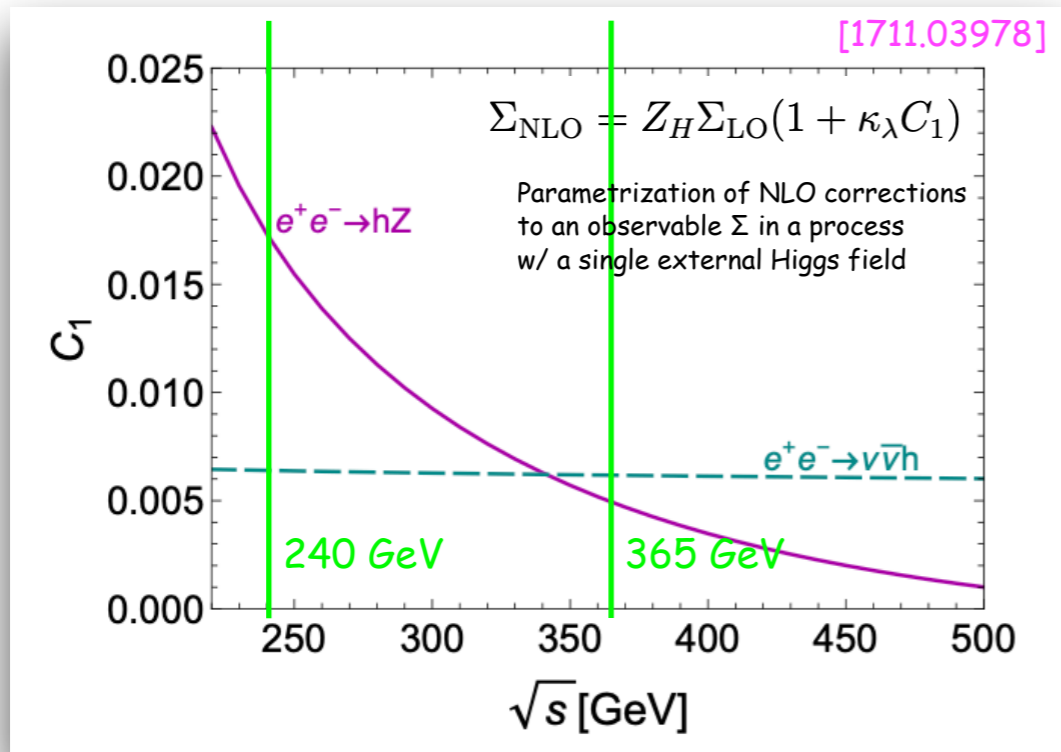


# Single-Higgs Access To $\lambda_{HHHH}$

## Indirect Access below Higgs pair threshold

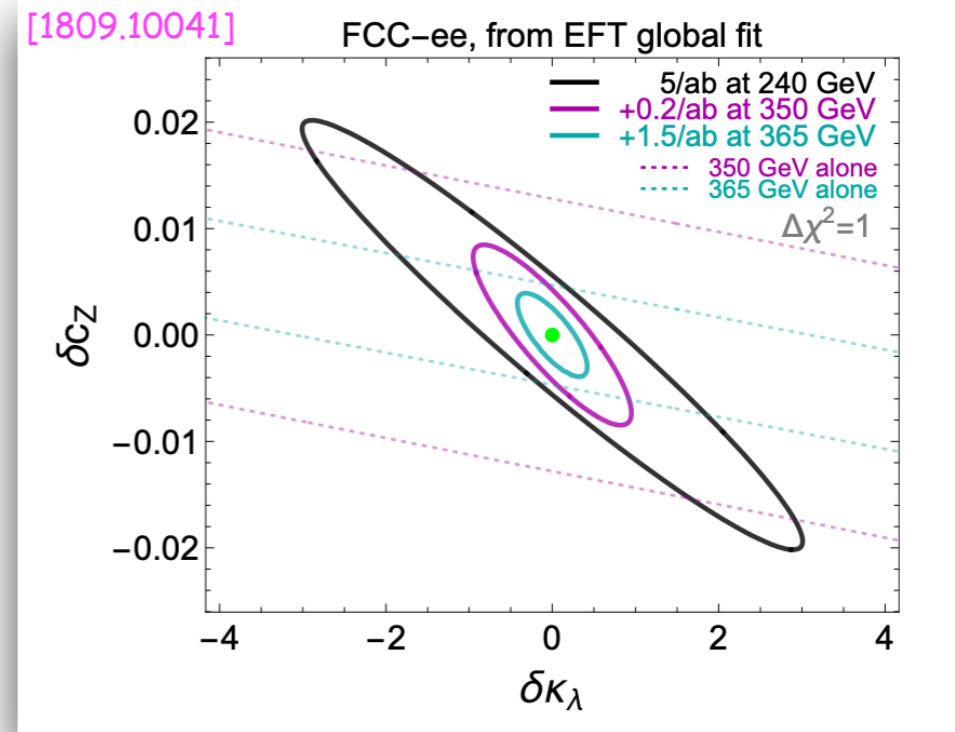


$$\kappa_\lambda = \lambda_{HHHH} / (\lambda_{HHHH})^{SM}$$



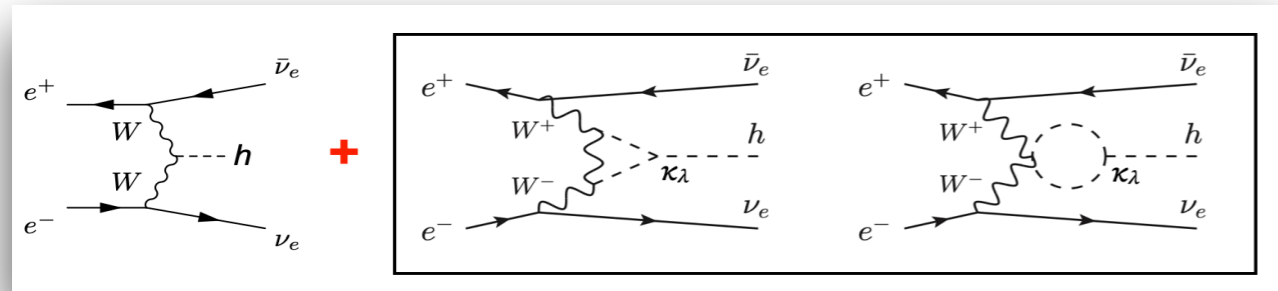
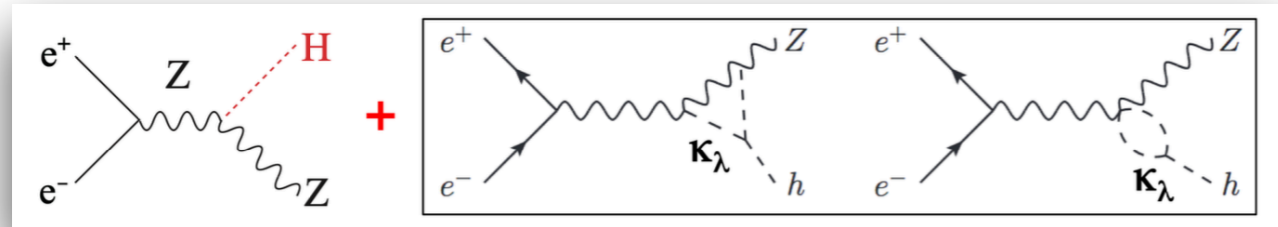
### Single Higgs:

- **Global** analysis:  
 FCC-ee<sub>365</sub>, ILC<sub>500</sub>: **~35%** when combined w/ HL-LHC
- FCCee<sub>365</sub> w/ 4PIs: **~24%**
- **Exclusive** analysis: too sensitive to other new physics to draw conclusions

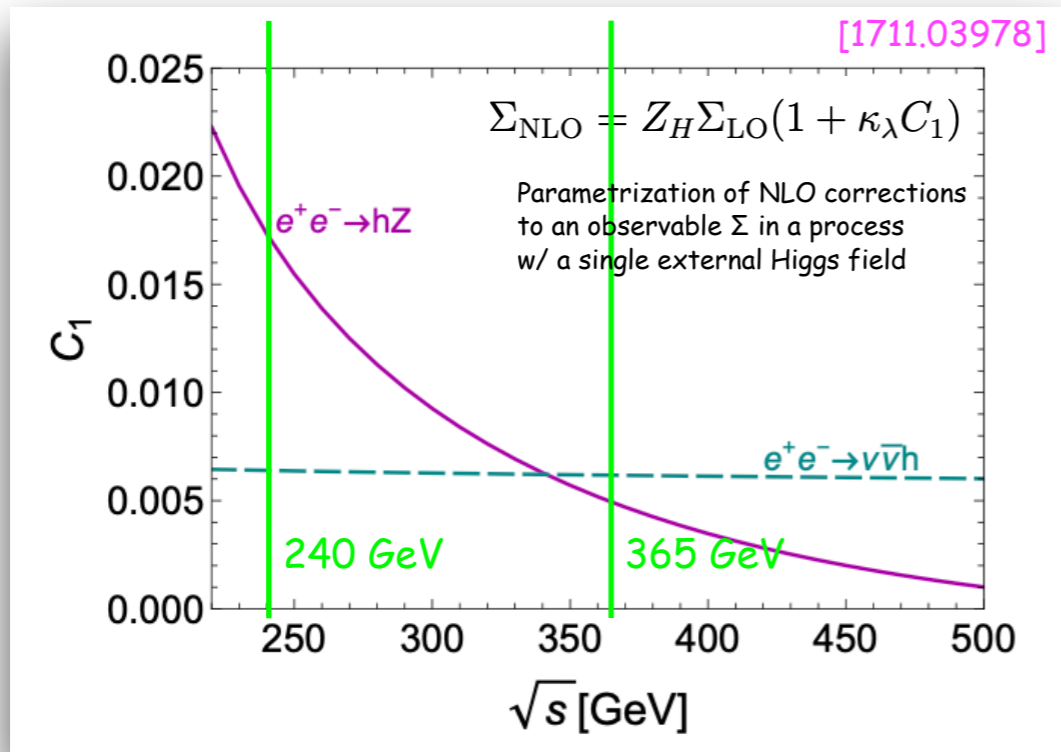


# Single-Higgs Access To $\lambda_{HHH}$

Indirect Access below Higgs pair threshold



$$\kappa_\lambda = \lambda_{HHH} / (\lambda_{HHH})^{SM}$$



$\lambda_{hhh}$  enters at one-loop in single Higgs process

**Challenge!** Competition with other effects

- competition w/ much larger LO contributions
- other numerically more dominant SM loops
- BSM: modified couplings, loop contributions
- contributions from (poorly constrained) eett operators affect interpretation

[Asteriadis et al, 2406.03557]

**Sensitivity limitations:**

- exp. and theor. uncertainties

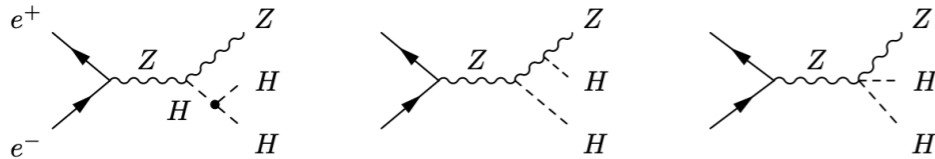
**Interpretation:**

- possibly observed deviation due to  $\lambda_{hhh}$  or other BSM/higher-order contributions?

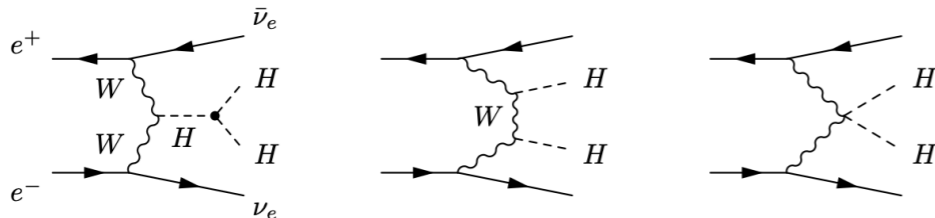
# Di-Higgs Access To $\lambda_{HHHH}$

## Direct Access above Higgs pair threshold

double Higgs-strahlung:  $e^+e^- \rightarrow ZHH$



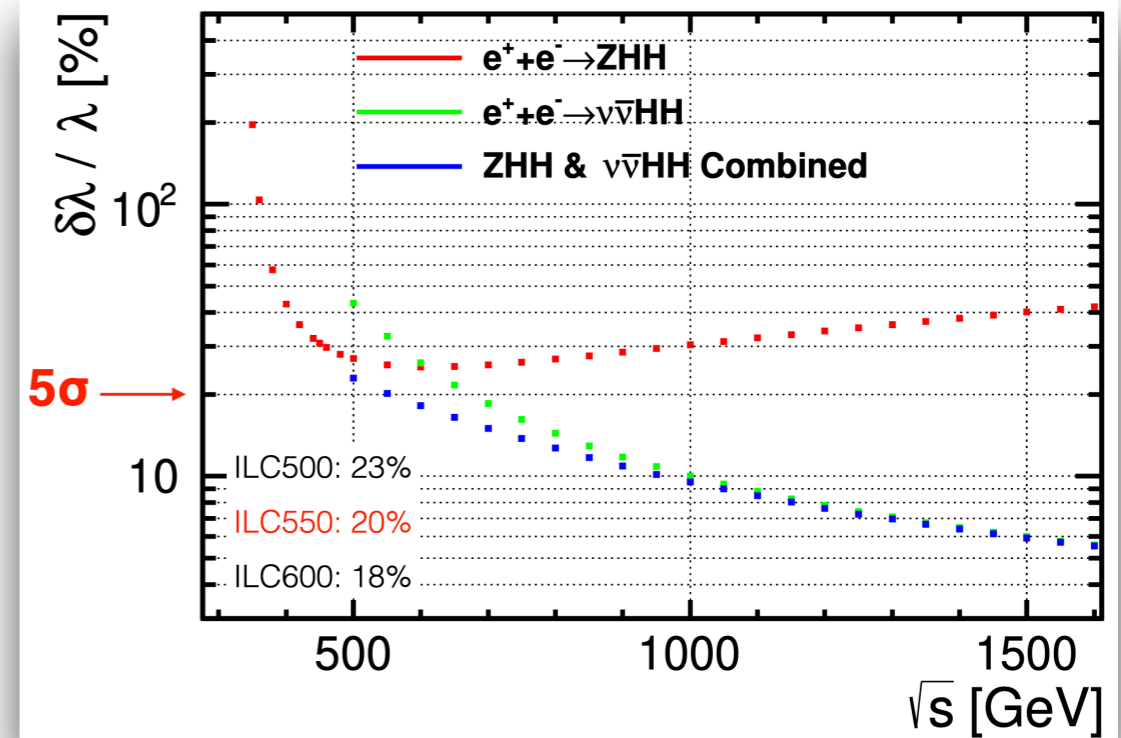
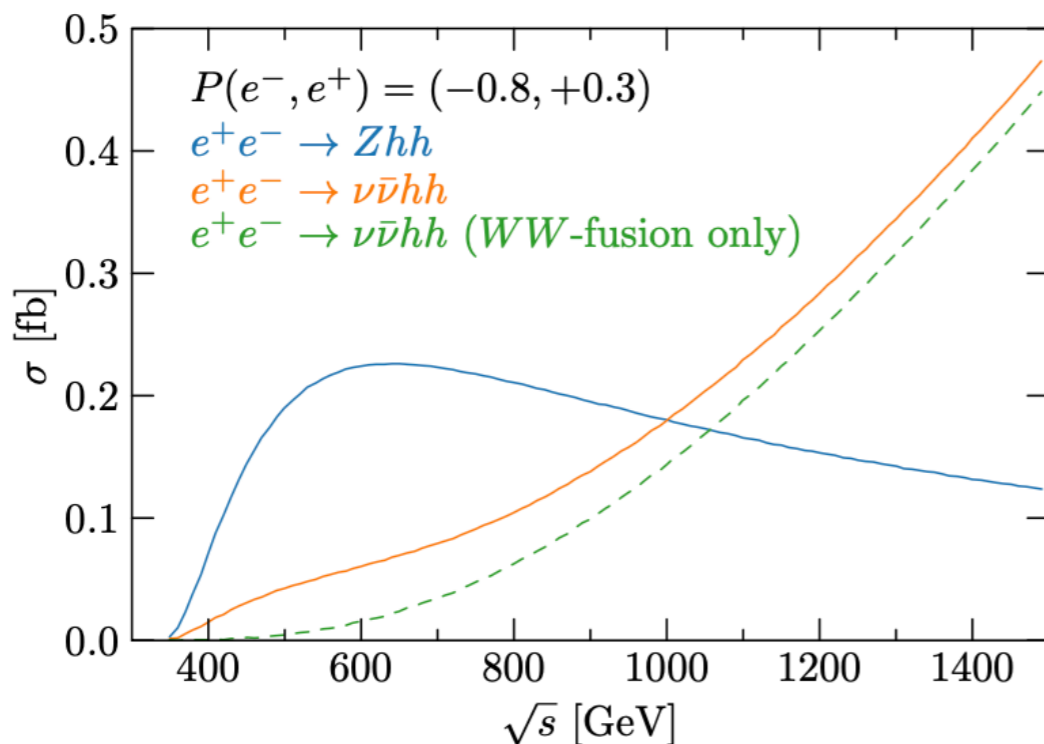
WW double-Higgs fusion:  $e^+e^- \rightarrow \bar{\nu}_e \nu_e HH$



### Di-Higgs:

- HL-LHC: **~50% or better?**
- improved by HE-LHC (**~15%**), ILC<sub>500</sub> (**~27%**), CLIC<sub>1500</sub> (**~36%**)
- Precision by CLIC<sub>3000</sub> (**~9%**), FCC-hh (**~5%**)
- Robust w.r.t. other operators

[Taken from J.Tian, LCWS2024]

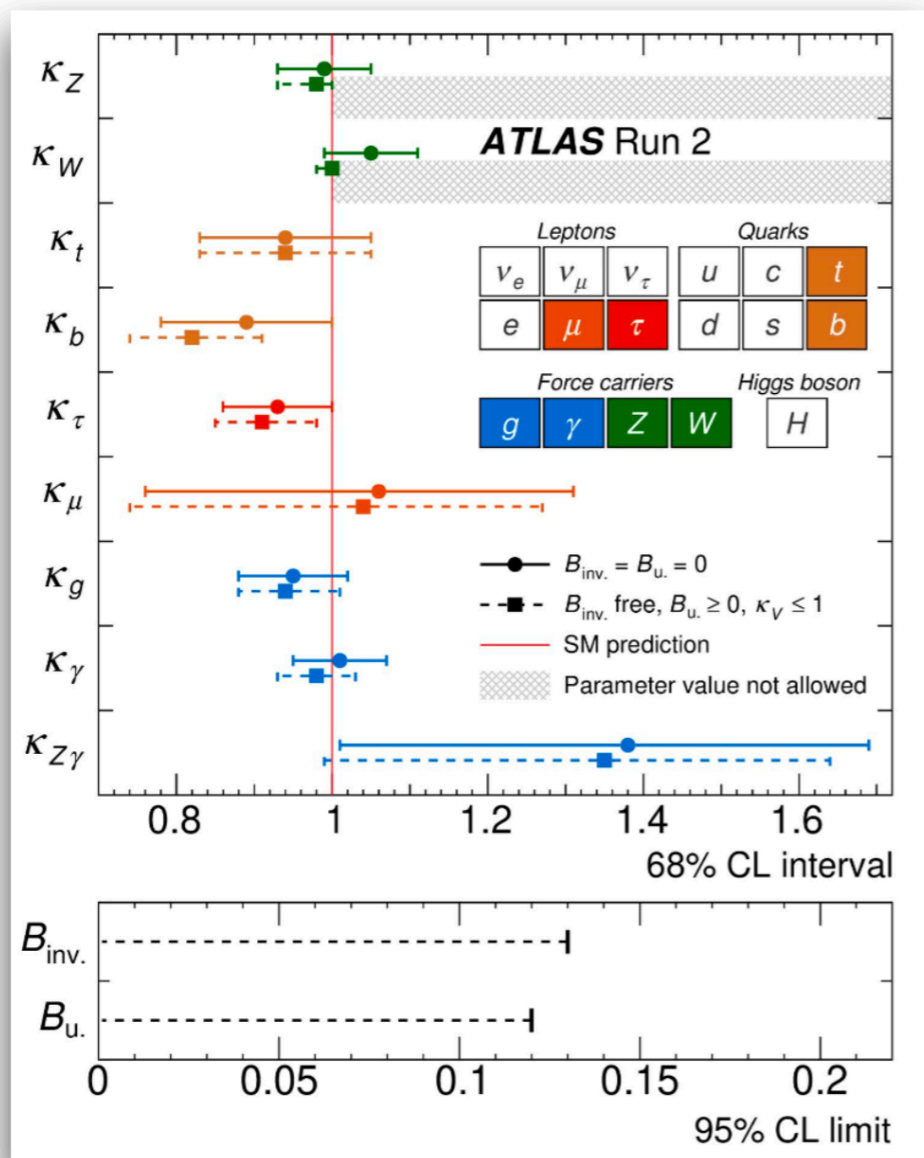


# BSM Effects in the Higgs Self-Coupling

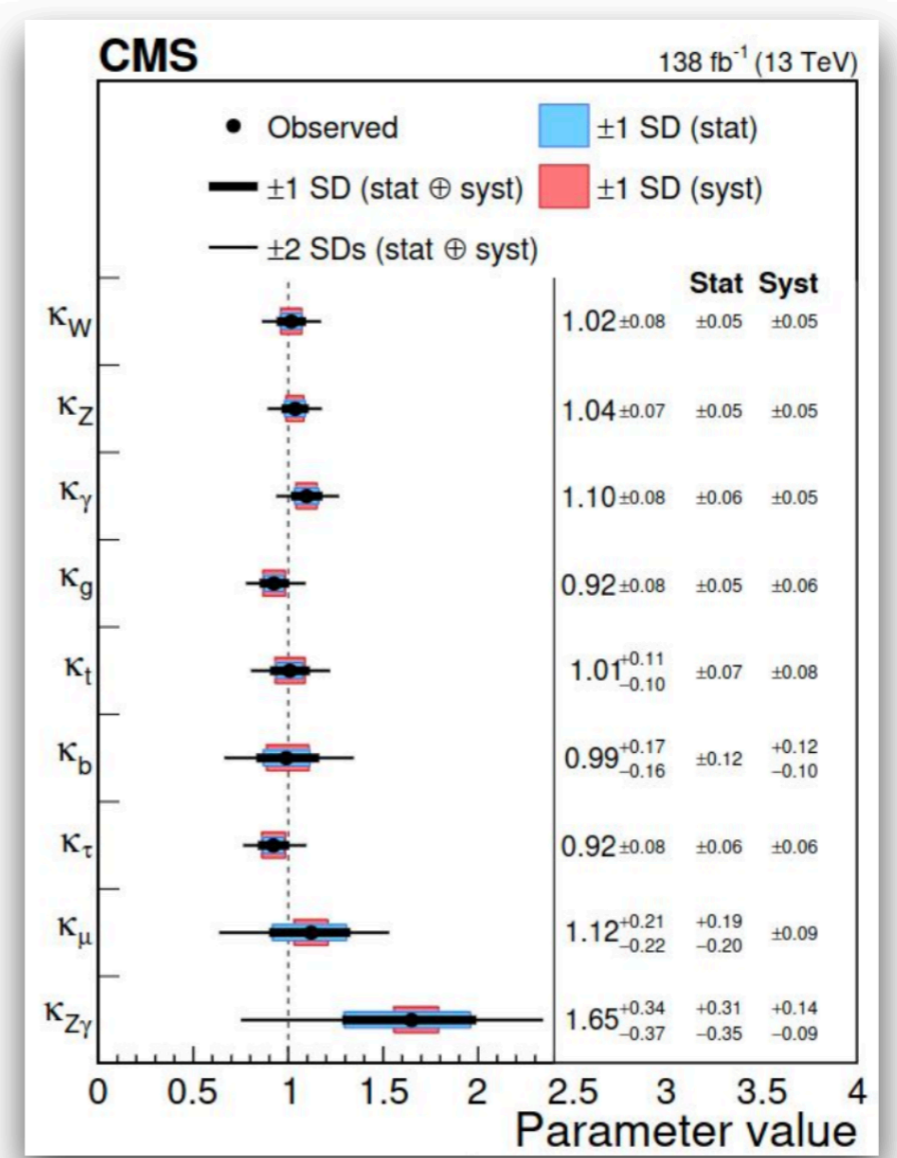
- Extended Higgs sectors: mixing effects w/ other Higgs bosons
  - BSM particles: loop contributions
- ↔ coupling deviations

$g_{HSM SM}$  very SM-like

[ATLAS,Nature607(2022)52]



[CMS,Nature607(2022)60]



# BSM Effects in the Higgs Self-Coupling

- Extended Higgs sectors: mixing effects w/ other Higgs bosons  $\rightsquigarrow$  coupling deviations
- BSM particles: loop contributions

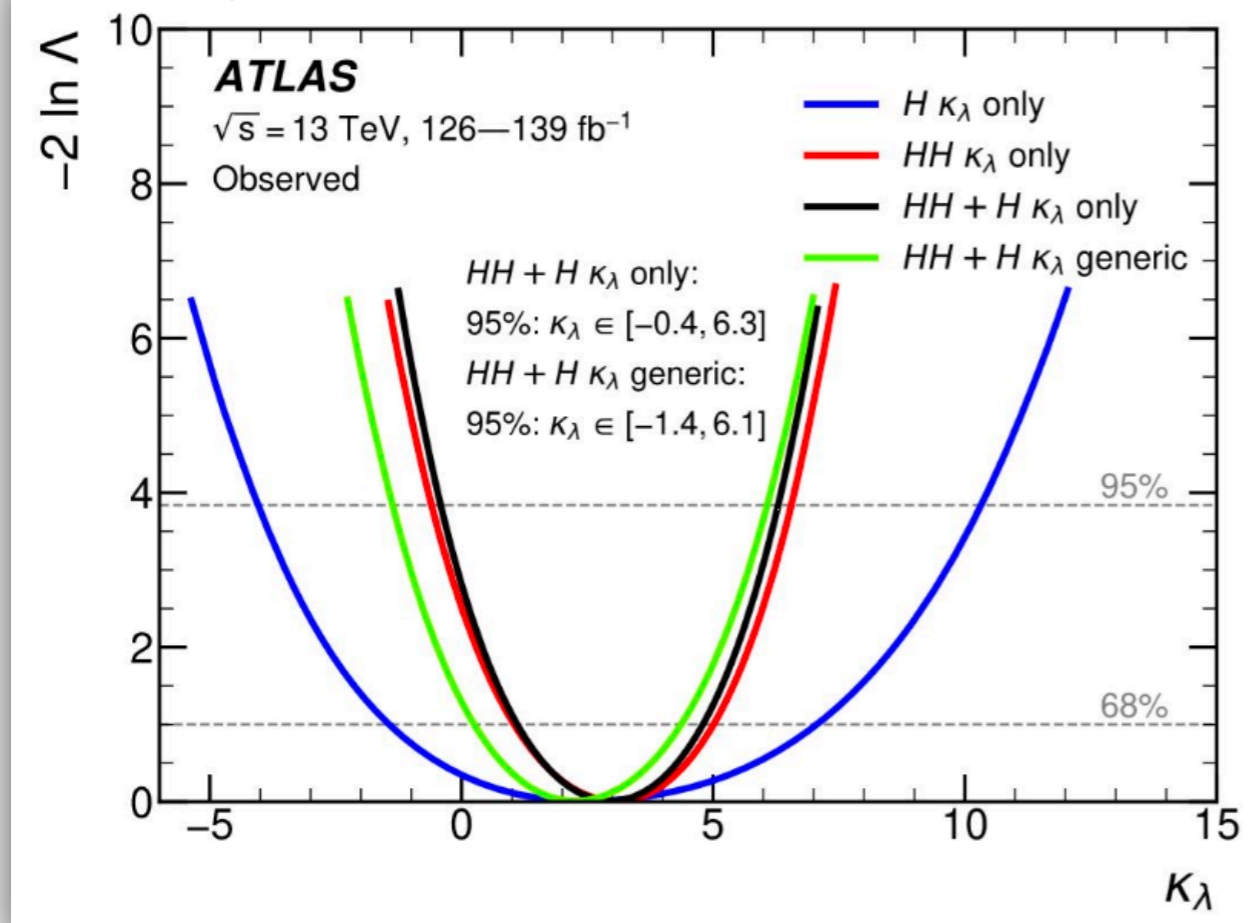
$\lambda_{HHH}$  can still deviate from SM



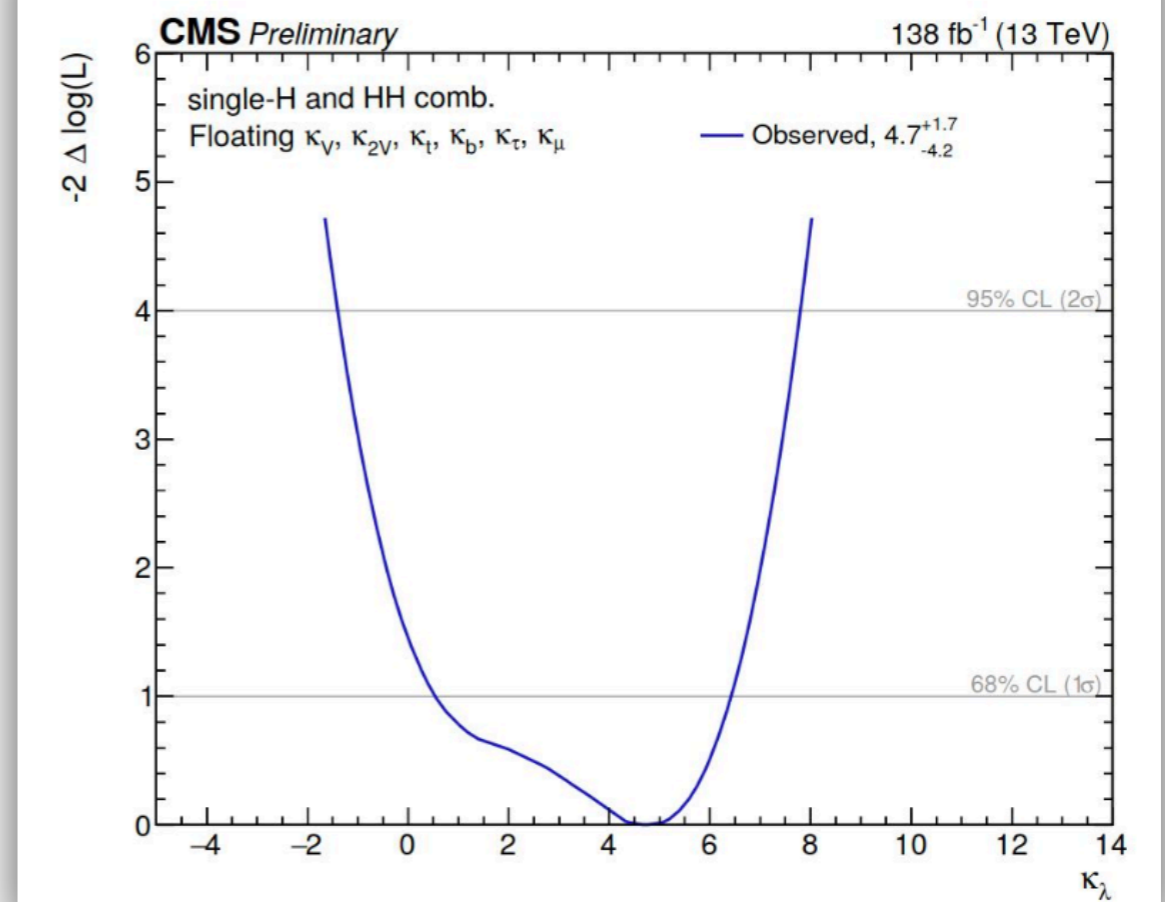
ATLAS:  $-1.4 < \kappa_\lambda < 6.1$  at 95 % CL

CMS:  $-1.2 < \kappa_\lambda < 7.5$  at 95 % CL

[Phys. Lett. B 843 \(2023\) 137745](#)



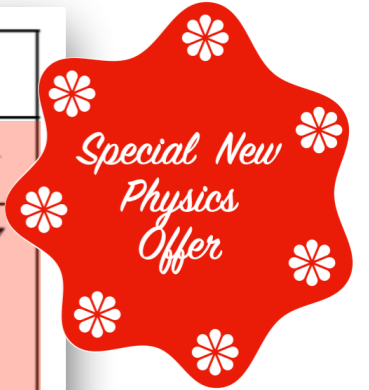
[CMS-HIG-23-006](#)



# BSM Effects in the Higgs Self-Coupling

[Abouabid, Arhrib, Azevedo, ElFalaki, Ferreira, MM, Santos, '21]

Scan in parameter space of the models check for compatibility w/ relevant theor. and exp. constraints



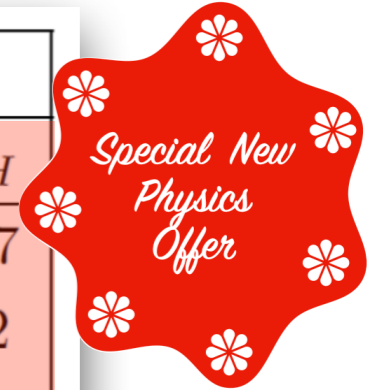
	R2HDM		C2HDM	
	$y_{t,H_{SM}}^{R2HDM} / y_{t,H}$	$\lambda_{3H_{SM}}^{R2HDM} / \lambda_{3H}$	$y_{t,H_{SM}}^{C2HDM} / y_{t,H}$	$\lambda_{3H_{SM}}^{C2HDM} / \lambda_{3H}$
	0.893...1.069	-0.096...1.076	0.898...1.035	-0.035...1.227
	n.a.	n.a.	0.889...1.028	0.251...1.172
heavy I	0.946...1.054	0.481...1.026	0.893...1.019	0.671...1.229
light II	0.951...1.040	0.692...0.999	0.956...1.040	0.096...0.999
medium II	n.a.	n.a.	—	—
heavy II	—	—	—	—
	N2HDM		NMSSM	
	$y_{t,H_{SM}}^{N2HDM} / y_{t,H}$	$\lambda_{3H_{SM}}^{N2HDM} / \lambda_{3H}$	$y_{t,H_{SM}}^{NMSSM} / y_{t,H}$	$\lambda_{3H_{SM}}^{NMSSM} / \lambda_{3H}$
light I	0.895...1.079	-1.160...1.004	n.a.	n.a.
medium I	0.874...1.049	-1.247...1.168	n.a.	n.a.
heavy I	0.893...1.030	0.770...1.112	n.a.	n.a.
light II	0.942...1.038	-0.608...0.999	0.826...1.003	0.024...0.747
medium II	0.942...1.029	0.613...0.994	0.916...1.000	-0.502...0.666
heavy II	—	—	—	—



# BSM Effects in the Higgs Self-Coupling

[Abouabid, Arhrib, Azevedo, ElFalaki, Ferreira, MM, Santos, '21]

	R2HDM		C2HDM	
	$y_{t,H_{SM}}^{R2HDM} / y_{t,H}$	$\lambda_{3H_{SM}}^{R2HDM} / \lambda_{3H}$	$y_{t,H_{SM}}^{C2HDM} / y_{t,H}$	$\lambda_{3H_{SM}}^{C2HDM} / \lambda_{3H}$
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medium II	n.a.	n.a.	—	—
heavy II	—	—	—	—
	N2HDM		NMSSM	
	$y_{t,H_{SM}}^{N2HDM} / y_{t,H}$	$\lambda_{3H_{SM}}^{N2HDM} / \lambda_{3H}$	$y_{t,H_{SM}}^{NMSSM} / y_{t,H}$	$\lambda_{3H_{SM}}^{NMSSM} / \lambda_{3H}$
light I	0.895...1.079	-1.160...1.004	n.a.	n.a.
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medium II	0.942...1.029	0.613...0.994	0.916...1.000	-0.502...0.666
heavy II	—	—	—	—



# Effect of Higher-Order Corrections

⇒ Higher-order corrections: potentially large in BSM Higgs sectors

e.g. 2HDM: [Kanemura,Kiyoura,Okada,Senaha,Yuan,'02;Braathen,Kanemura,'19,'20]  
[Bahl,Braathen,Weiglein,'22]

⇒ Example 2HDM: Parameter scan (taking into account theor. & single Higgs constraints)

Type	LO $\kappa_\lambda^{(0)}$	NLO $\kappa_\lambda^{(1)}$
I	[-0.19, 1.17]	[0.24, 6.79]
II	[0.63, 1.00]	[0.74, 5.66]
LS	[0.48, 1.00]	[0.63, 6.29]
FL	[0.65, 1.00]	[0.76, 5.77]

[Arco,Heinemeyer,MM,in prep.]

LHC experiments start being sensitive

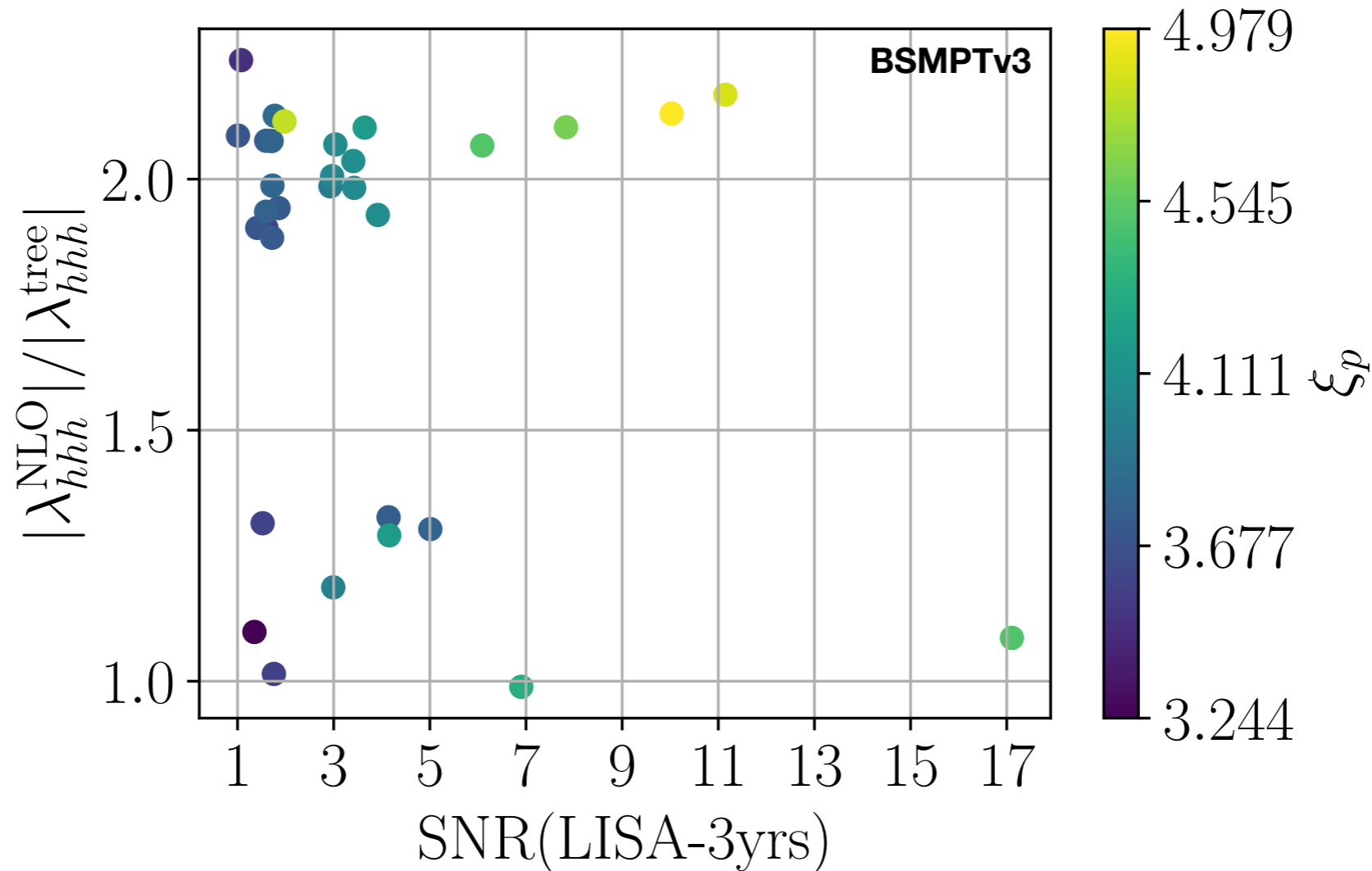
↔ higher-order corrections important for proper interpretation of limits!

⇒ First-order Phase Transition (electroweak baryogenesis): prefers larger  $\lambda_{HHH}$

# Higgs Self-Coupling & Evolution of the Universe

- Model CP in the Dark: SM-Higgs ( $\lambda_{hhh}^{tree} = \lambda_{hhh}^{SM}$ ) + Dark Sector  
GW signal from strong first-order phase transition

[Basler, Biermann, MM, Müller, Santos, Viana, '24]



[Biermann, Borschensky, Erhardt, MM, Santos, Viana]

- Vector DM Model: two visible Higgs bosons + Dark photon  
Strong first-order phase transition:  $\delta\lambda_{hhh}^{NLO} / \lambda_{hhh}^{LO} = 8\%$

# Higgs Self-Coupling & Evolution of the Universe

Model CP in the Dark: SM-Higgs ( $\lambda_{hhh}^{tree} = \lambda_{hhh}^{SM}$ ) + Dark Sector  
 GW signal from strong first-order

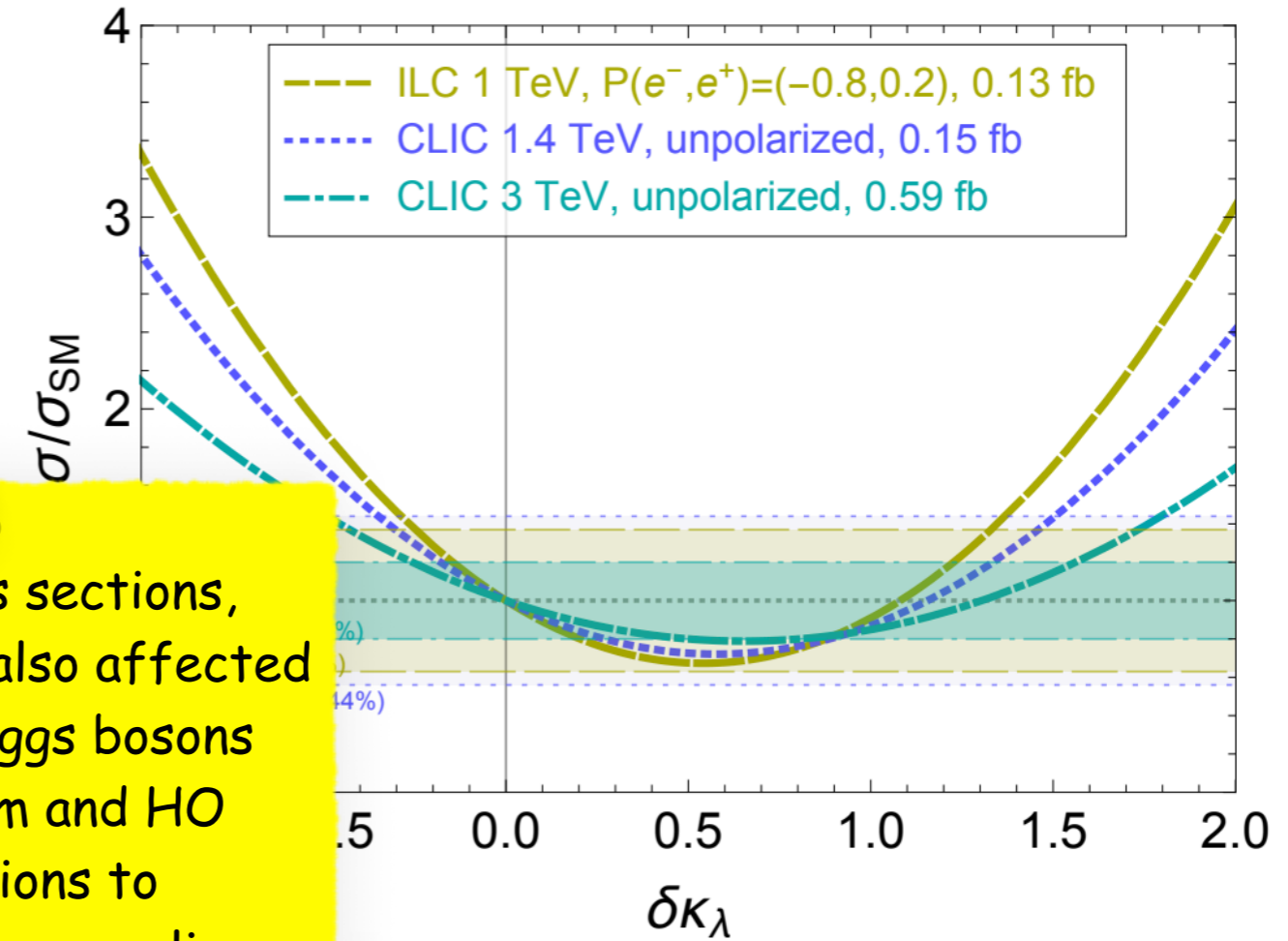
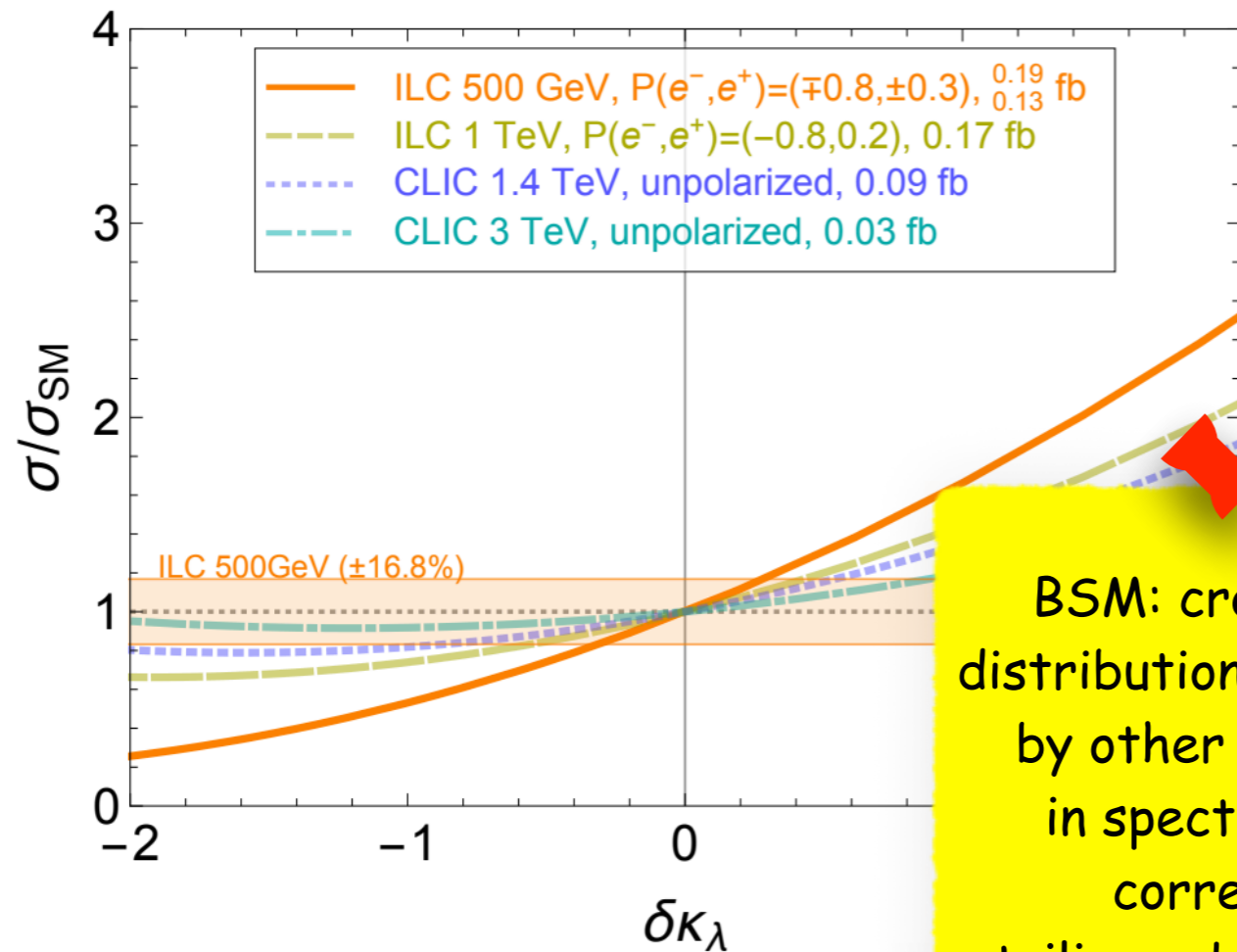
[Basler, Biermann, MM, Müller, Santos, Viana, '24]

Changes Linear Collider Sensitivities

[1711.03978]

$e^+e^- \rightarrow Zhh$

$e^+e^- \rightarrow \nu\bar{\nu}hh$



BSM: cross sections, distributions also affected by other Higgs bosons in spectrum and HO corrections to trilinear Higgs couplings  
 [cf. talk by Arco @LCWS2024]

Vector DM Model: two visible Higgs bosons  
 Strong first-order phase transition:  $\delta\lambda_{hhh}^{tree} / \lambda_{hhh}^{tree} \approx 8\%$

# Precision Measurements at Z/WW/tt



# Why do we need EWPOs?

- Relations between SM parameters affected by loop corrections =>

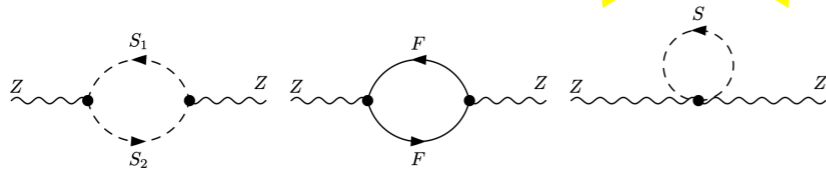
Consistency test of SM at quantum level

$$\frac{r_\mu}{\sqrt{2}} = \frac{\pi\alpha}{2M_W^2 s_W^2} (1 + \Delta r)$$

- New particles in the loops =>

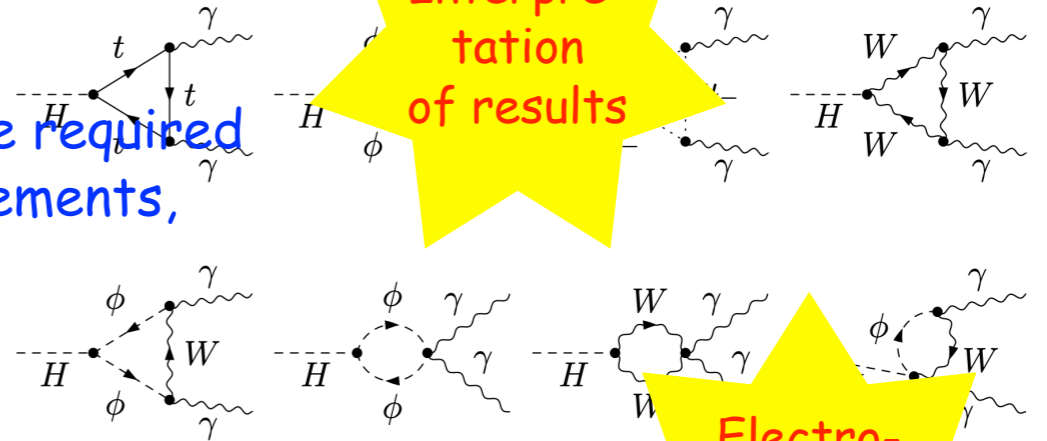
New Physics

$$M_W^2 = \frac{M_Z^2}{2} \left\{ 1 + \sqrt{1 - \frac{4\pi\alpha}{\sqrt{2}G_\mu M_Z^2} (1 + \Delta_{\text{NMSSM CALC } r}^{(n)})} \right\}$$



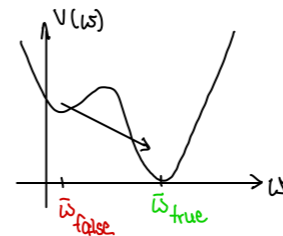
- SM parameters enter observables => precise knowledge required for meaningful interpretation of the precision measurements, for meaningful predictions of further observables

Interpretation of results

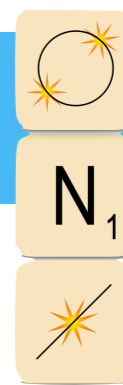


- Parameter values of direct relevance for stability of electroweak vacuum, evolution of the universe, matter-antimatter-asymmetry

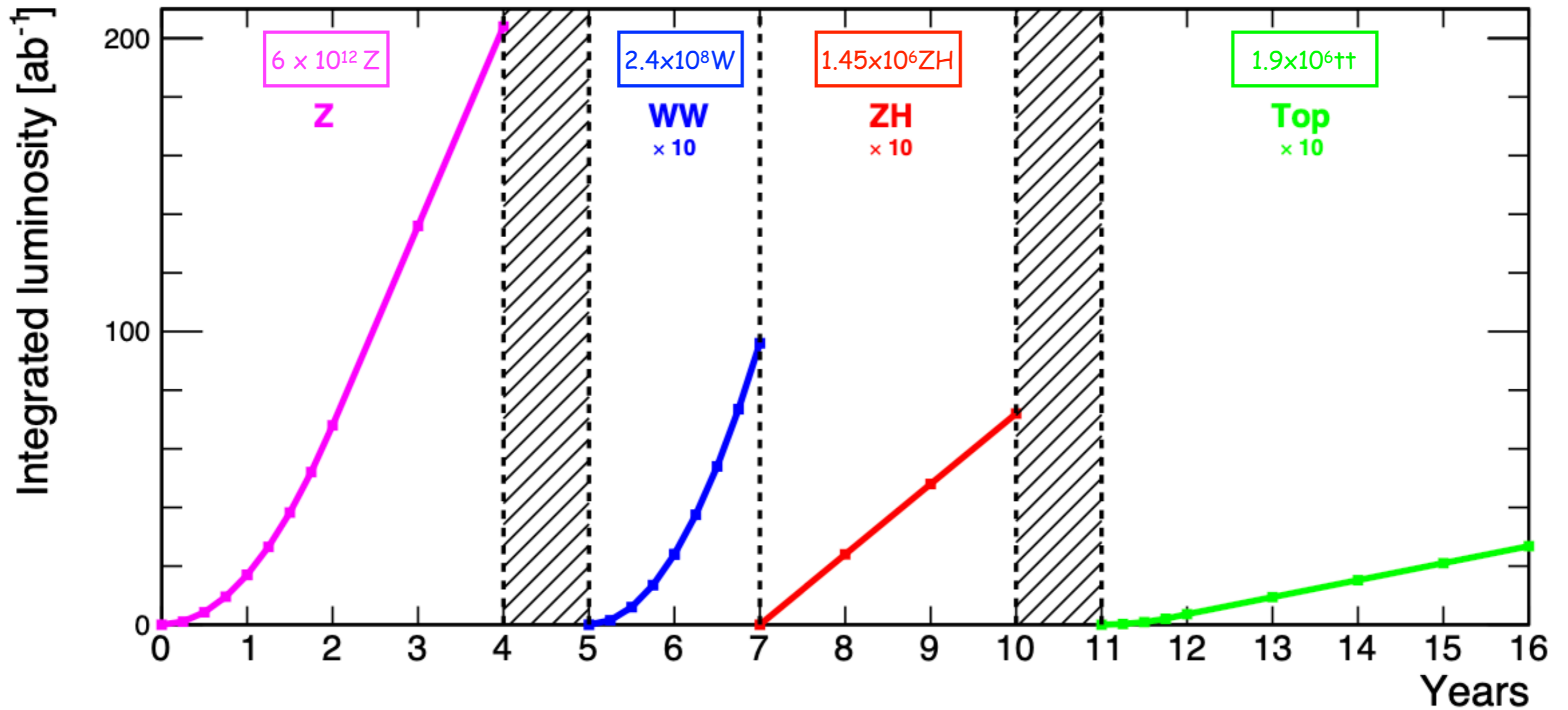
Electroweak Vacuum



# Precision at Electroweak & Top Factories



N<sub>1</sub> E<sub>1</sub> E<sub>1</sub> D<sub>2</sub>



# Precision at Z, WW, tt

[2209.08078]

Collider	$\sqrt{s}$	P [%] $e^-/e^+$	$L_{\text{int}}$ $\text{ab}^{-1}$
ILC	250 GeV	$\pm 80 / \pm 30$	2
	350 GeV	$\pm 80 / \pm 30$	0.2
	500 GeV	$\pm 80 / \pm 30$	4
	1 TeV	$\pm 80 / \pm 20$	8
ILC-GigaZ	$m_Z$	$\pm 80 / \pm 30$	0.1
CLIC	380 GeV	$\pm 80 / 0$	1
	500 GeV	$\pm 80 / 0$	2.5
	1 TeV	$\pm 80 / 0$	5
CEPC	$m_Z$		60 / 100
	$2m_W$		3.6 / 6
	240 GeV		12 / 20
	$2m_t$		- / 1
FCC-ee	$m_Z$		150
	$2m_W$		10
	240 GeV		5
	$2m_t$		1.5

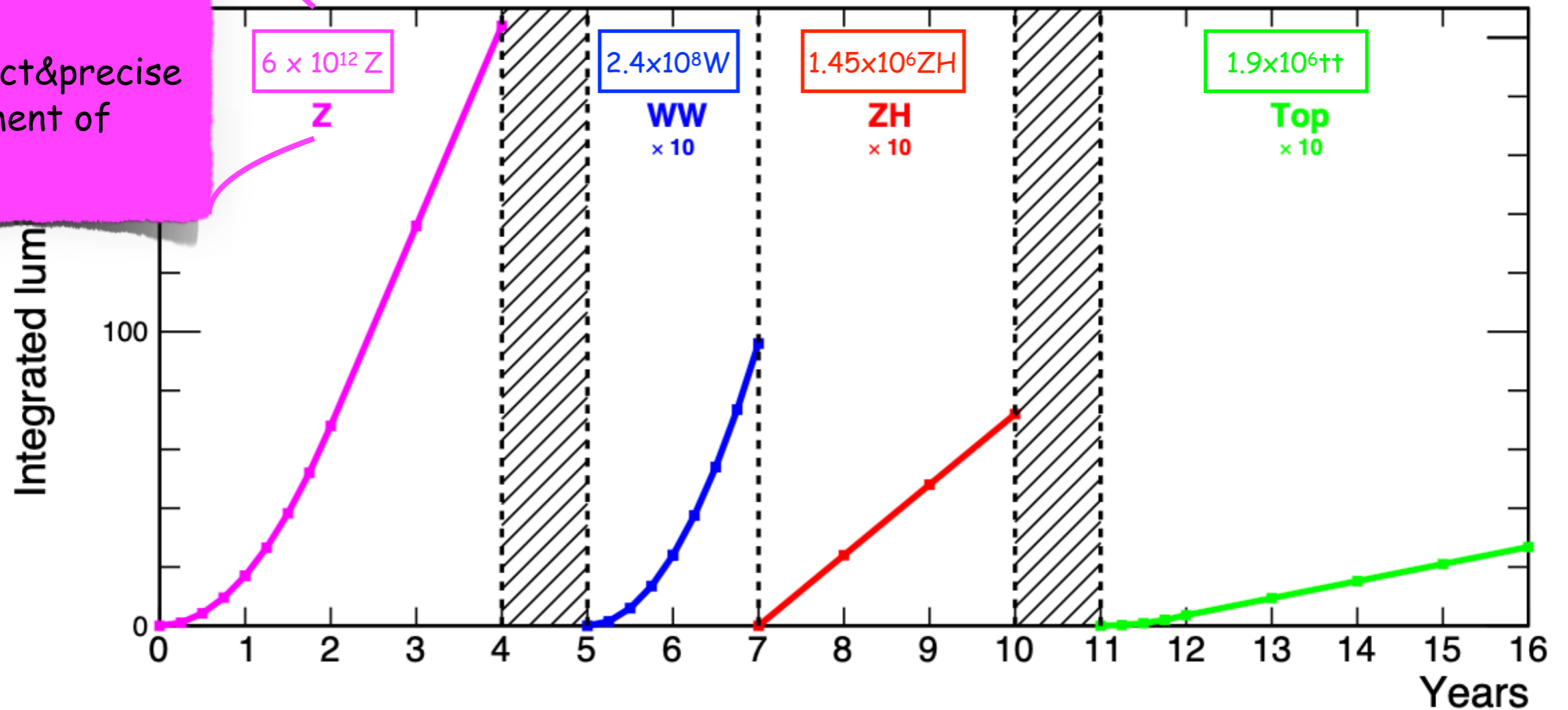
Electron-positron run scenarios used for the Snowmass 2021 study



# Precision at Z, WW, tt

$m_Z, \Gamma_Z, \alpha_s(m_Z), \dots$   
improvement by  
factor 20-50 w.r.t.  
today

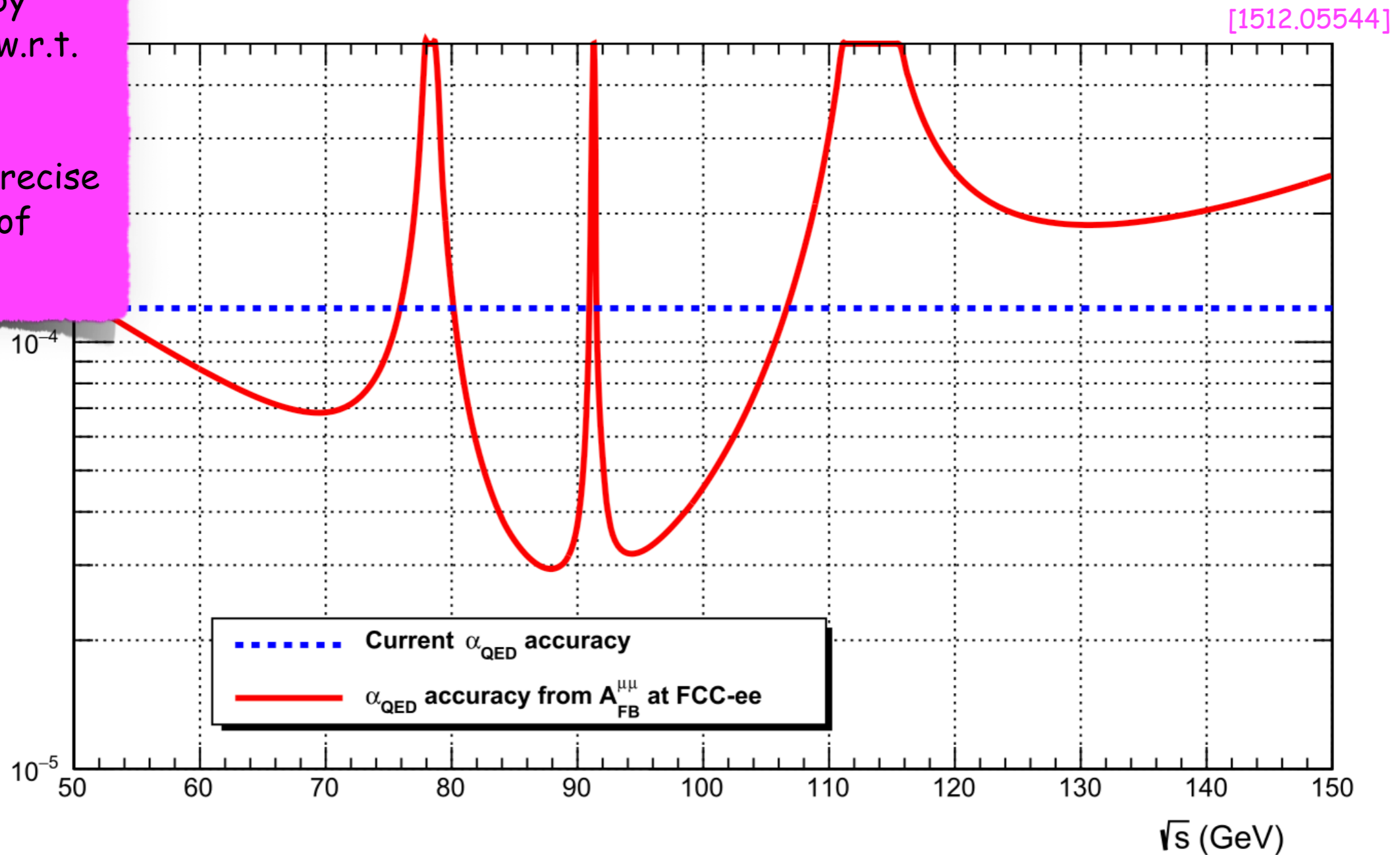
first direct & precise  
measurement of  
 $\alpha_{\text{QED}}(m_Z)$



# Precision at Z, WW, tt

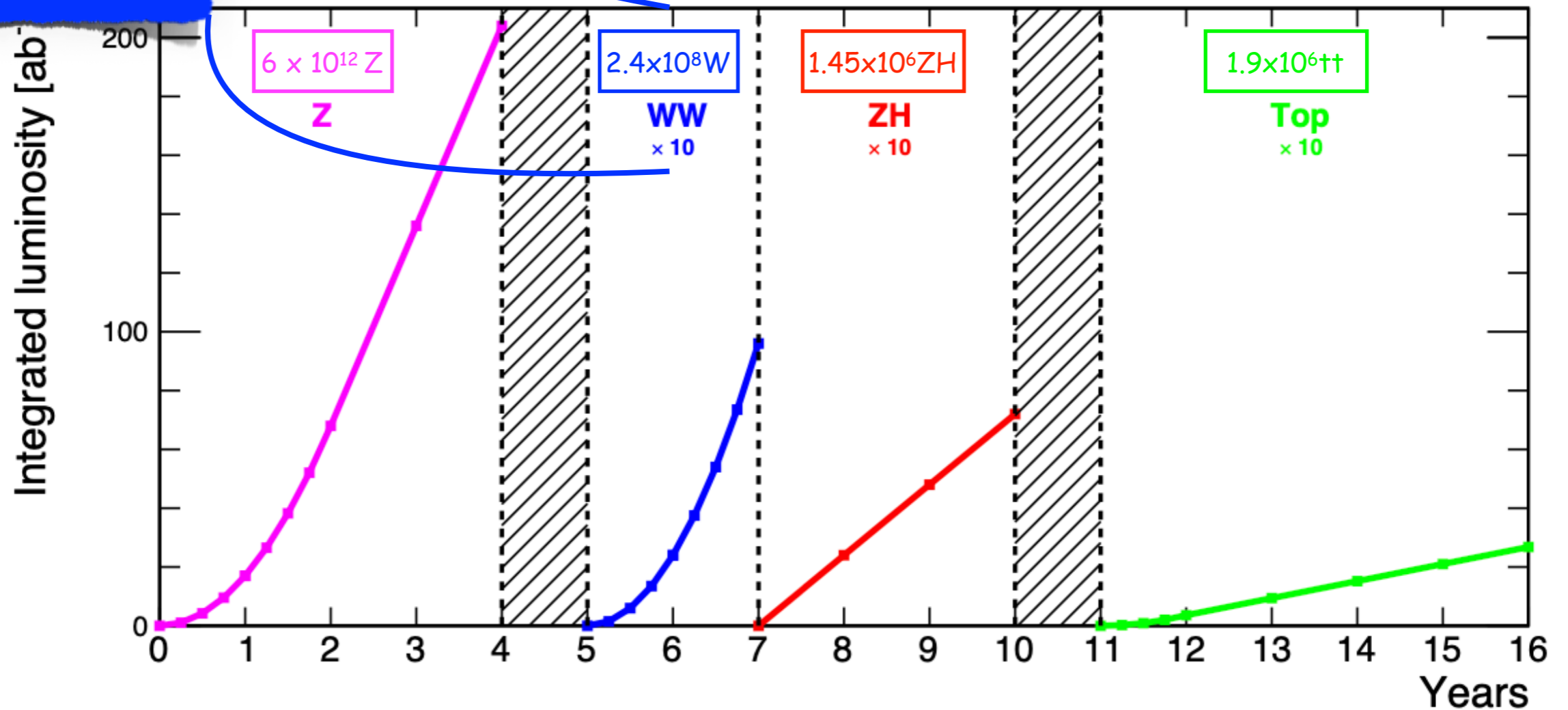
$m_Z, \Gamma_Z, \alpha_s(m_Z), \dots$   
improvement by  
factor 20-50 w.r.t.  
today

first direct&precise  
measurement of  
 $\alpha_{\text{QED}}(m_Z)$



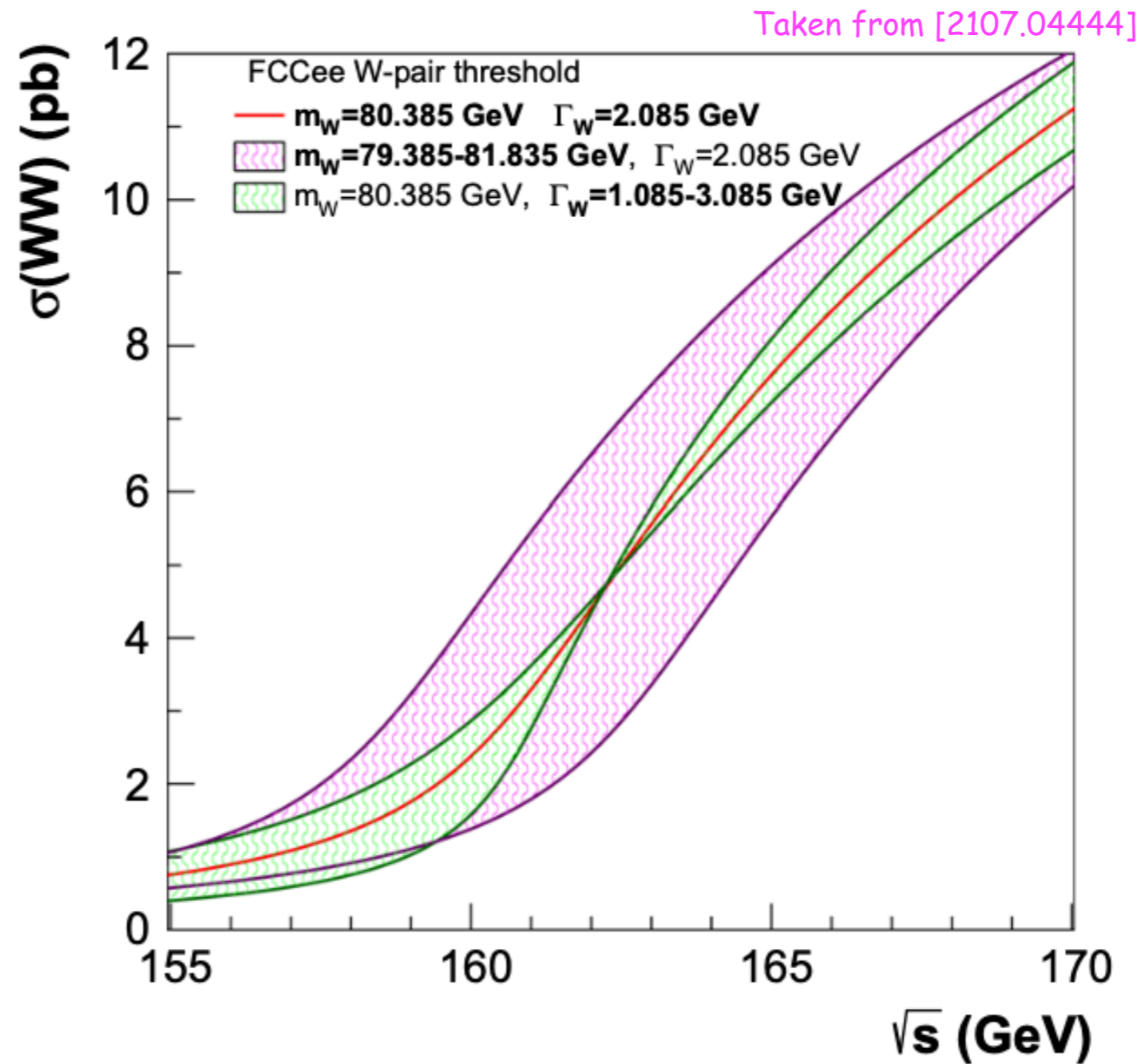
# Precision at Z, WW, tt

$m_W, \Gamma_W, \alpha_s(m_W), \dots$   
improvement by  
factor 20-100 w.r.t.  
today



# Precision at Z, WW, tt

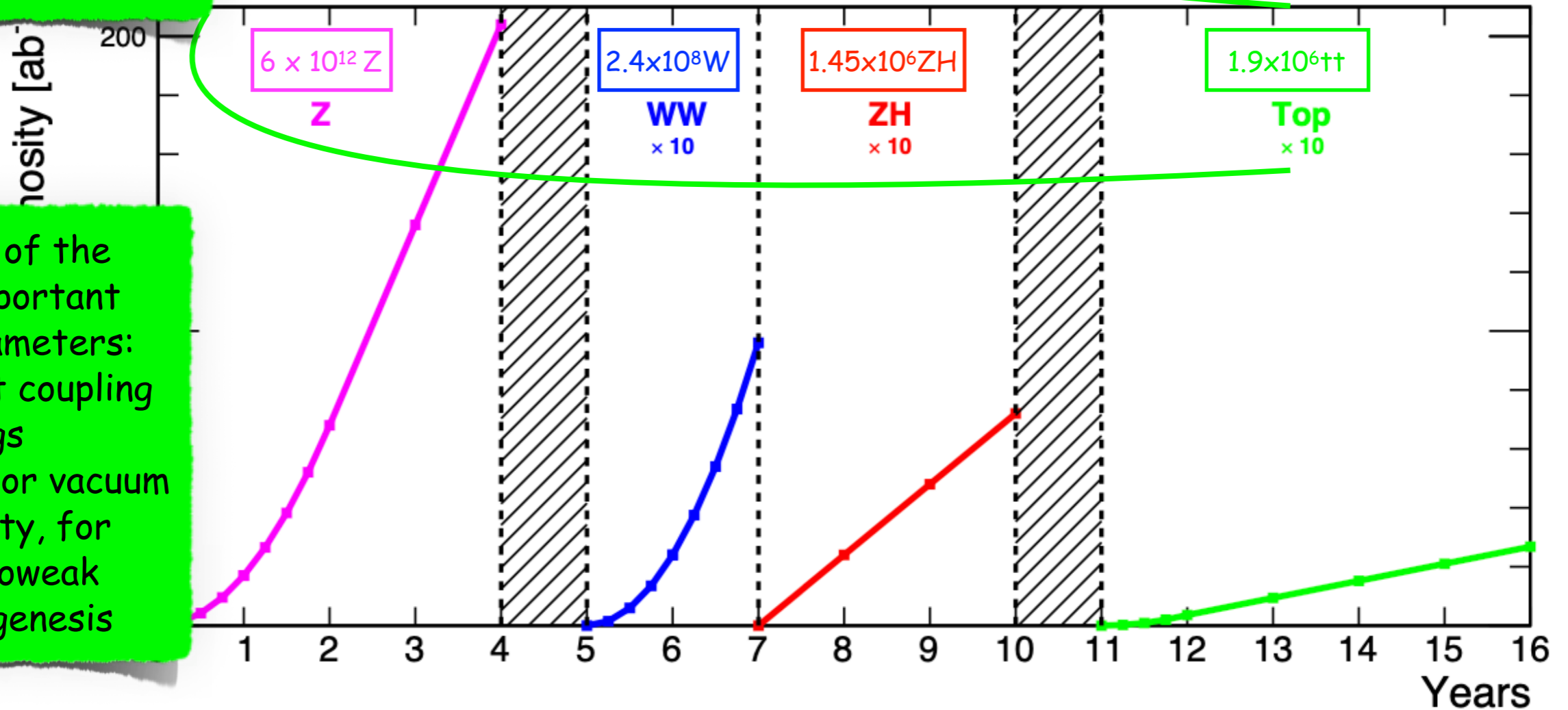
$m_W, \Gamma_W, \alpha_s(m_W), \dots$   
improvement by  
factor 20-100 w.r.t.  
today



# Precision at Z, WW, tt

$\delta m_t \approx 50 \text{ MeV}$   
 $\delta \Gamma_t = 45 \text{ MeV}$   
 theory uncertainty  
 limiting factor

Top one of the  
 most important  
 SM parameters:  
 - largest coupling  
 to Higgs  
 - input for vacuum  
 stability, for  
 electroweak  
 baryogenesis



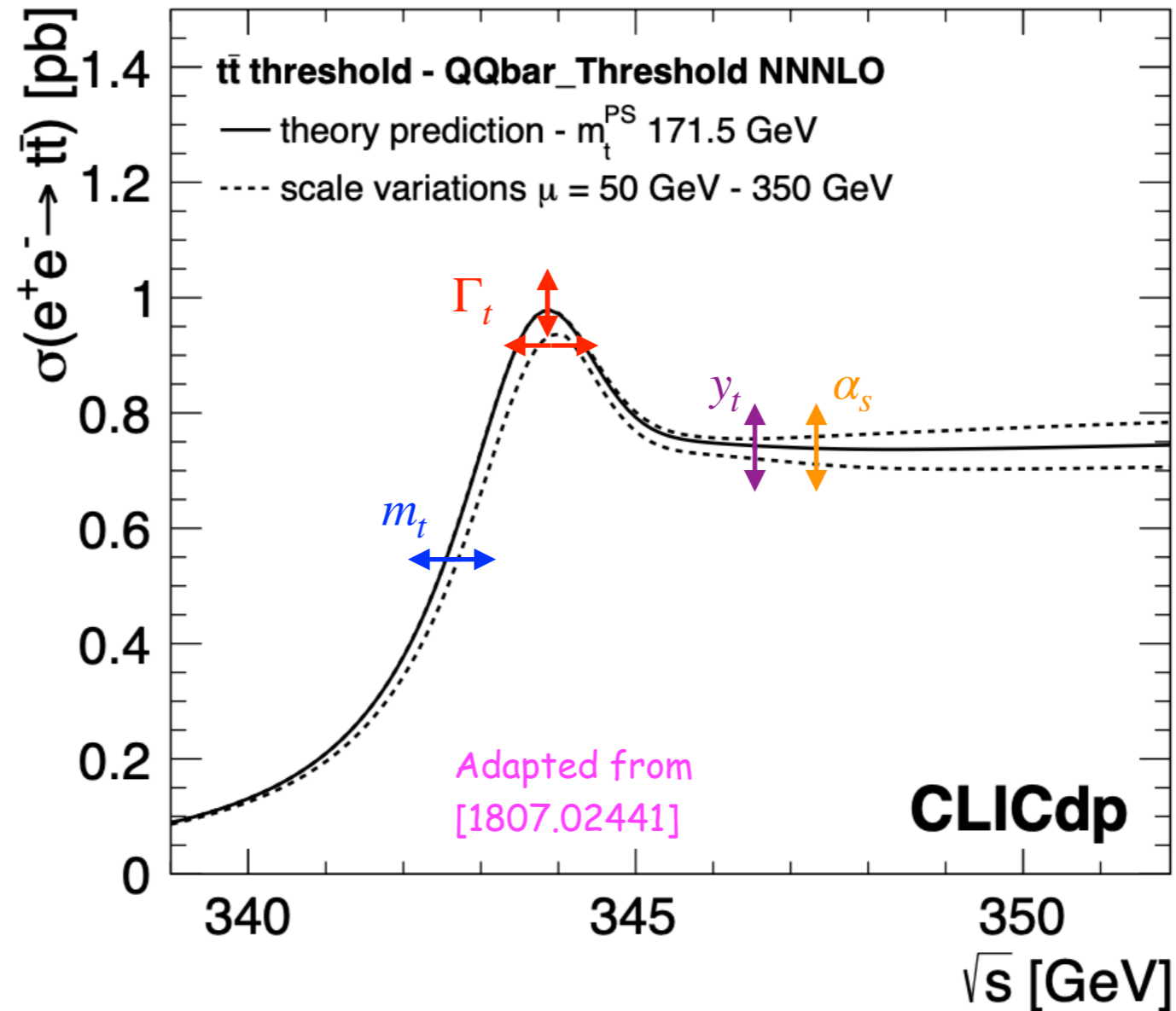
# Precision at Z, WW, tt

$$\delta m_t \approx 50 \text{ MeV}$$

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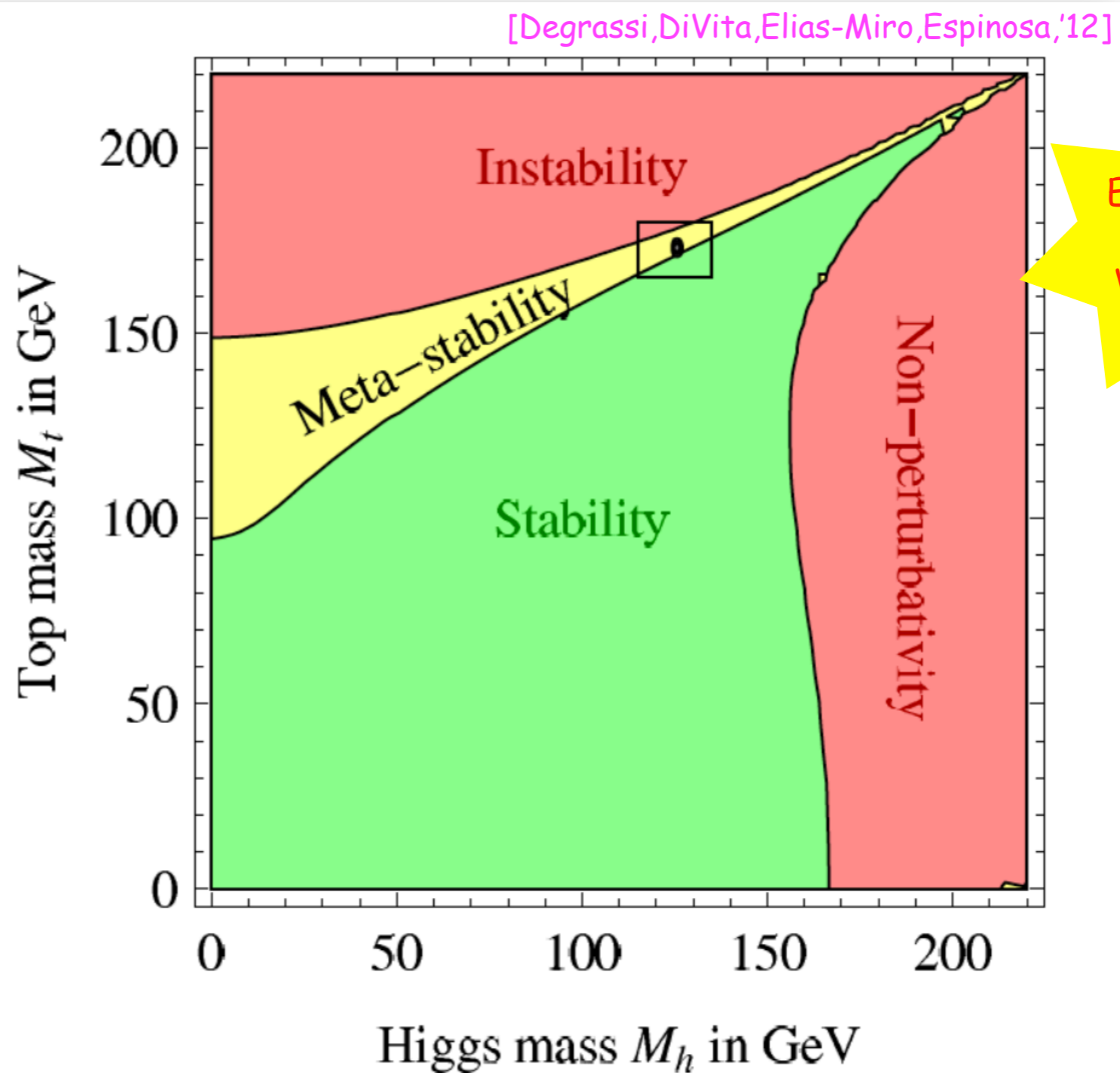
# Precision at $Z$ , $WW$ , $tt$

$$\delta m_t \approx 50 \text{ MeV}$$

$$\delta \Gamma_t = 45 \text{ MeV}$$

theory uncertainty  
limiting factor

Top one of the most important SM parameters:  
- largest coupling to Higgs  
- input for vacuum stability, for electroweak baryogenesis



Electro-weak  
Vacuum

# EWPOs at Future $e^+e^-$ Colliders

[2209.08078]

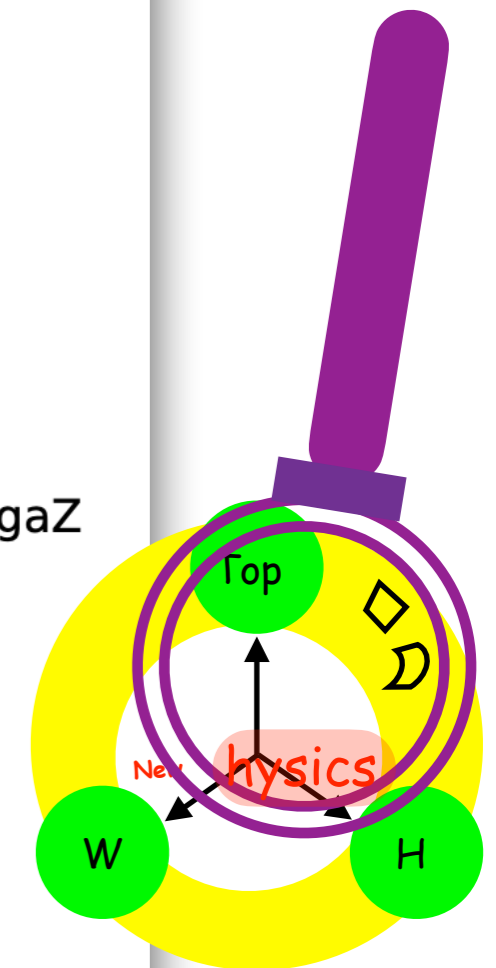
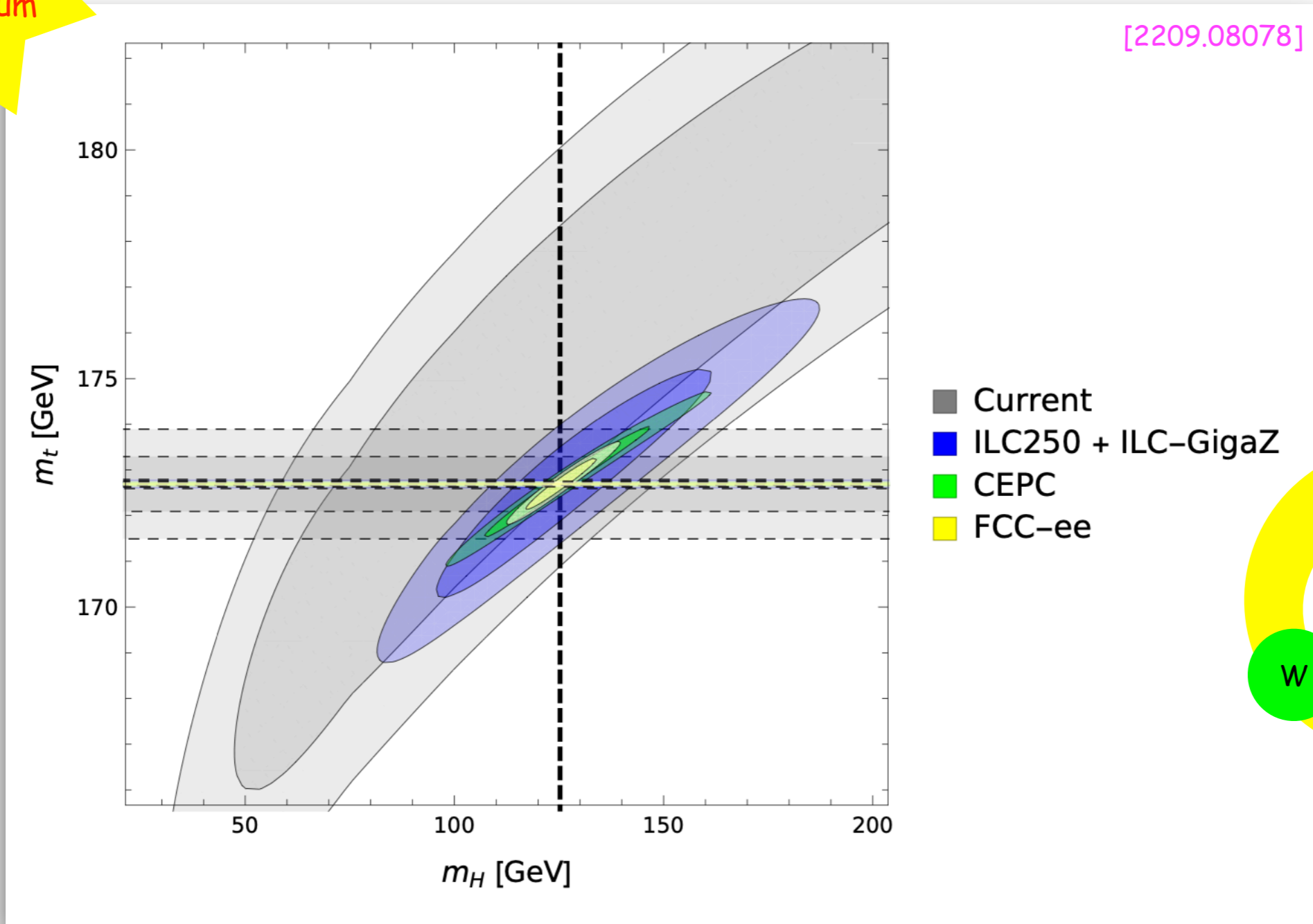
Quantity	current	ILC250	ILC-GigaZ	FCC-ee	CEPC	CLIC380
$\Delta\alpha(m_Z)^{-1} (\times 10^3)$	17.8*	17.8*		3.8 (1.2)	17.8*	
$\Delta m_W$ (MeV)	12*	0.5 (2.4)		0.25 (0.3)	0.35 (0.3)	
$\Delta m_Z$ (MeV)	2.1*	0.7 (0.2)	0.2	0.004 (0.1)	0.005 (0.1)	2.1*
$\Delta m_H$ (MeV)	170*	14		2.5 (2)	5.9	78
$\Delta\Gamma_W$ (MeV)	42*	2		1.2 (0.3)	1.8 (0.9)	
$\Delta\Gamma_Z$ (MeV)	2.3*	1.5 (0.2)	0.12	0.004 (0.025)	0.005 (0.025)	2.3*
$\Delta A_e (\times 10^5)$	190*	14 (4.5)	1.5 (8)	0.7 (2)	1.5 (2)	60 (15)
$\Delta A_\mu (\times 10^5)$	1500*	82 (4.5)	3 (8)	2.3 (2.2)	3.0 (1.8)	390 (14)
$\Delta A_\tau (\times 10^5)$	400*	86 (4.5)	3 (8)	0.5 (20)	1.2 (20)	550 (14)
$\Delta A_b (\times 10^5)$	2000*	53 (35)	9 (50)	2.4 (21)	3 (21)	360 (92)
$\Delta A_c (\times 10^5)$	2700*	140 (25)	20 (37)	20 (15)	6 (30)	190 (67)
$\Delta\sigma_{\text{had}}^0$ (pb)	37*			0.035 (4)	0.05 (2)	37*
$\delta R_e (\times 10^3)$	2.4*	0.5 (1.0)	0.2 (0.5)	0.004 (0.3)	0.003 (0.2)	2.5 (1.0)
$\delta R_\mu (\times 10^3)$	1.6*	0.5 (1.0)	0.2 (0.2)	0.003 (0.05)	0.003 (0.1)	2.5 (1.0)
$\delta R_\tau (\times 10^3)$	2.2*	0.6 (1.0)	0.2 (0.4)	0.003 (0.1)	0.003 (0.1)	3.3 (5.0)
$\delta R_b (\times 10^3)$	3.1*	0.4 (1.0)	0.04 (0.7)	0.0014 (< 0.3)	0.005 (0.2)	1.5 (1.0)
$\delta R_c (\times 10^3)$	17*	0.6 (5.0)	0.2 (3.0)	0.015 (1.5)	0.02 (1)	2.4 (5.0)

Table 3: EWPOs at future  $e^+e^-$  colliders: statistical error (estimated experimental systematic error).  $\Delta$  ( $\delta$ ) stands for absolute (relative) uncertainty, while \* indicates inputs taken from current data [6]. See Refs. [23, 30, 35, 36, 46, 47].



# SM Fit to all EWPOs

Consistency test of SM at quantum level



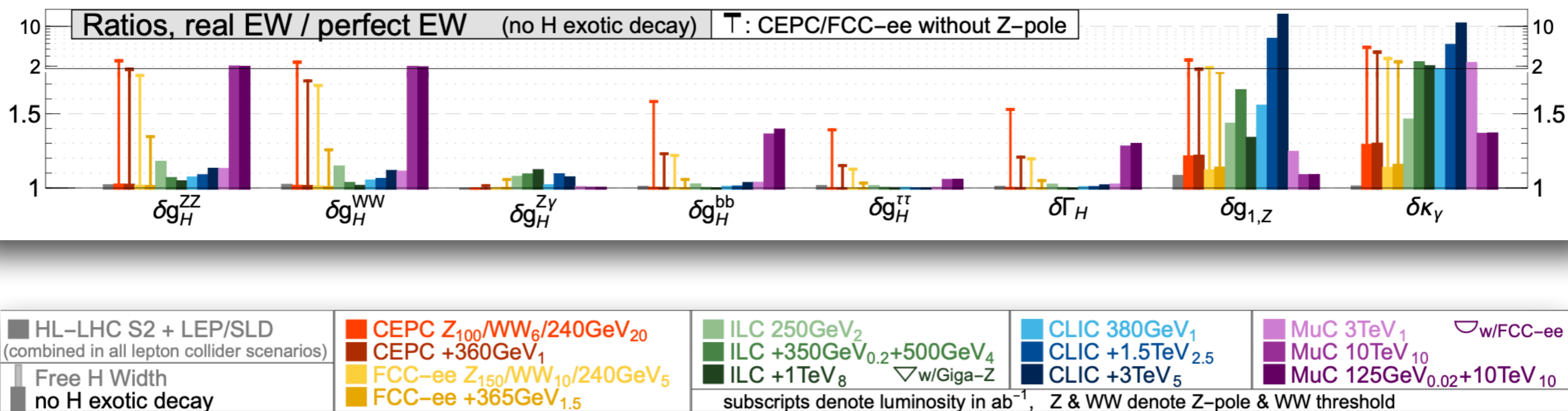
# Interplay EW Measurements and Higgs Precision

- Z pole run essential to isolate Higgs measurements and ensure that uncertainties from EW coupling do not affect Higgs couplings

Test of  
New physics  
Interpretation  
of results

- Precision measurements at the Z pole and WW threshold affect significantly achievable precision for Higgs couplings and  $\alpha$ TGCs: improvement by about a factor of 2

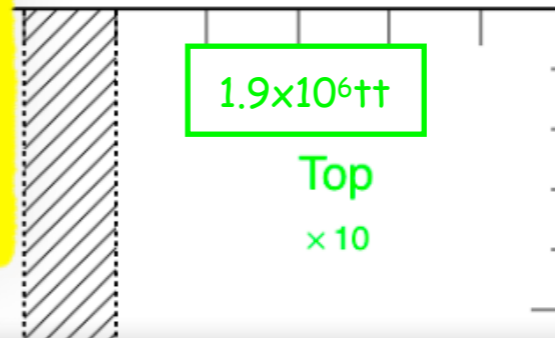
[2209.08078]



# Precision at Z, WW, tt

## Requirements from Theory:

- Match experimental precision
- At least 3-(fully massive!)/4-loop EW corrections are needed!
- Numerical integration  $\leadsto$  convergence? CPU time? Grids?
- Non-perturbative effects may become relevant
- Identify (ratios of) observables w/ reduced theor. uncertainties



[Freitas, Heinemeyer, Beneke, Blondel, Dittmaier, Gluza, Hoang, Jadach, Janot, Reuter, Reimann, Schwinn, Skrzypek, Weinzierl]

	current exp.	FCC <sub>ee</sub> , CEPC /ILC	current th.	$\sim 3(4)$ -loop
$M_W$ [MeV]	12	0.5/3	4 ( $\alpha^3, \alpha^2\alpha_s$ )	1
$\Gamma_Z$ [MeV]	2.3	0.1/1	0.4 ( $\alpha^3, \alpha^2\alpha_s, \alpha\alpha_s^2$ )	0.15
$R_\ell$ [ $10^{-3}$ ]	25	1/10	5 ( $\alpha^3, \alpha^2\alpha_s$ )	1.5
$R_b$ [ $10^{-5}$ ]	66	6/15	10 ( $\alpha^3, \alpha^2\alpha_s$ )	5
$\sin^2 \theta_{eff}^\ell$ [ $10^{-5}$ ]	$\sim 13$	0.6/1.3	4.5 ( $\alpha^3, \alpha^2\alpha_s$ )	1.5

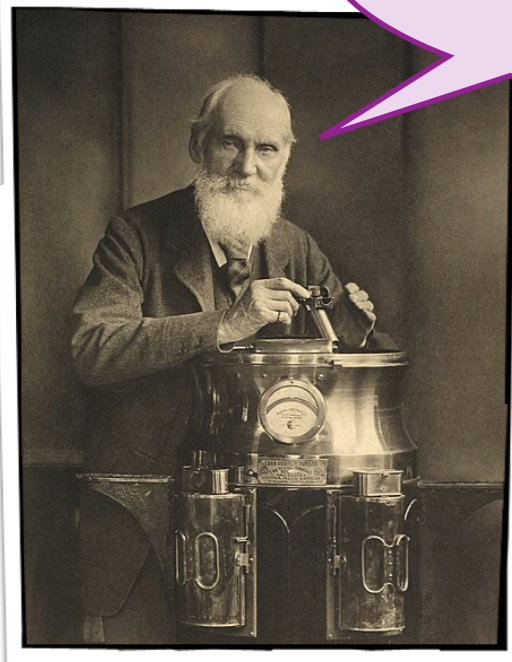
# A Look Into the Future



# What to Expect?

- Situation at the end of HL-Luminosity LHC:  
suppose: no new physics + Higgs behaves very SM-like

There is nothing new to be discovered  
in physics now. All that remains is  
more and more precise measurement.  
Lord Kelvin (1824-1907)



The most important is  
that we never stop asking questions.  
Madame Curie, 1867-1934



# Light on the Horizon

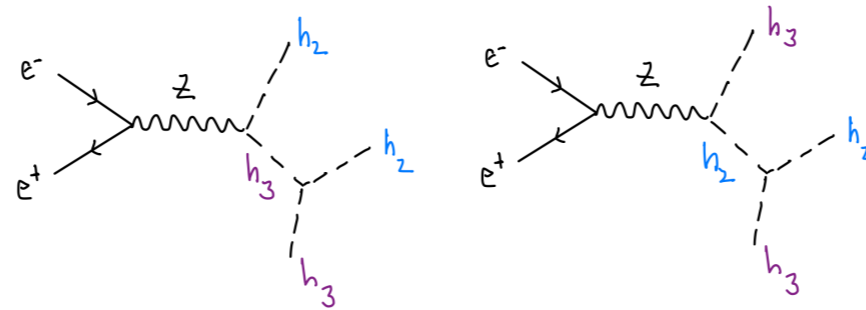
⇒ Future colliders may still reveal new physics!

Example CP-violating 2-Higgs-Doublet Model:

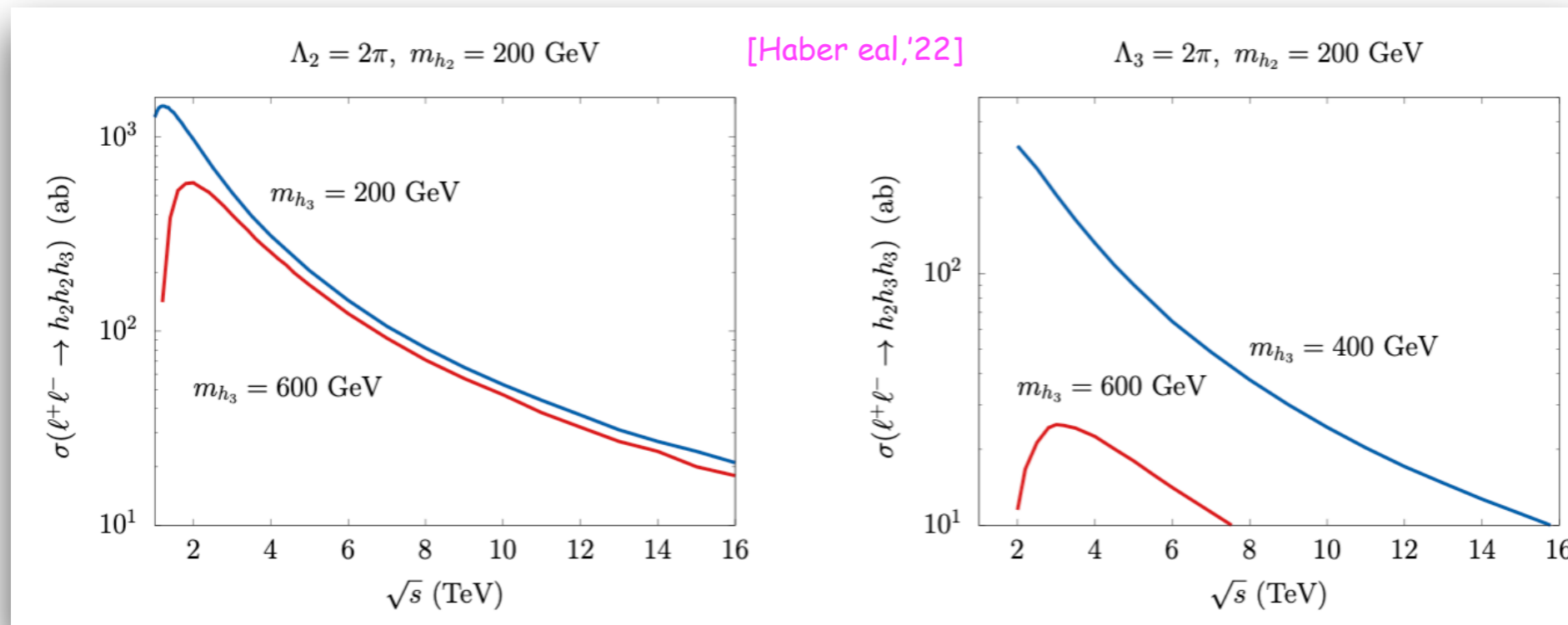
Could be that 125 GeV Higgs is very close to the alignment limit and be very CP-even!

Can we still see new physics at future colliders?

Study multi Higgs boson production!



Simultaneous measurement of  $Zh_2h_2h_3$ ,  $Zh_2h_3h_3$ ,  $Zh_2h_3$  sign of CP violation



Still: Extremely hard

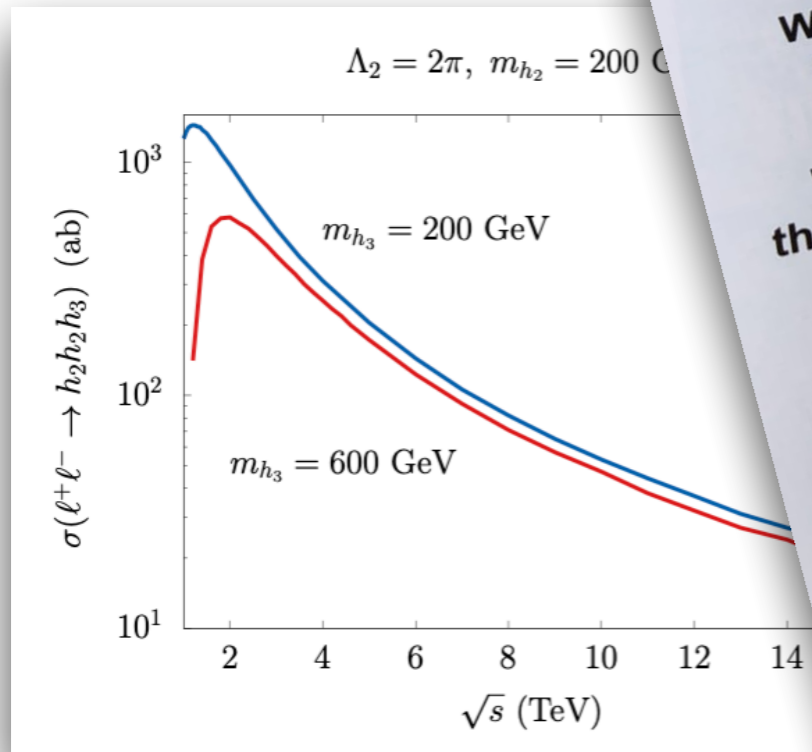
# Light on ...

Future colliders ...

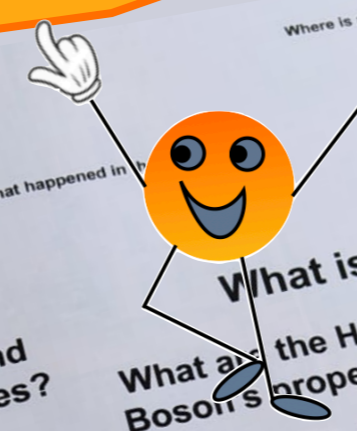
Example CP-violation  
Could be that 125 GeV ...

Can we still see new ...

Study multi Higgs boson  
production!



Have you asked any big questions today?



- What is our universe made of?
- Why are neutrinos so light?
- Can we understand quark bound states?
- What will we find at the 14TeV Large Hadron Collider?
- What is beyond the Standard Model?
- Why are there three generations?
- Is gravity related to the other forces?
- Are neutrinos their own antiparticle?
- What are the forces of nature?
- What is the origin of mass?
- What are the symmetries of the universe?
- Why is the top quark so heavy?
- Where is all the antimatter?
- Is the universe supersymmetric?
- What is Dark Matter?
- What are the Higgs Boson's properties?
- How is antimatter different from matter?
- Are there extra dimensions?

CP-even!

simultaneous measurement of  $h_2h_3, Zh_2h_3h_3, Zh_2h_3$  of CP violation

extremely hard

# FOCUS TOPICS

[Maestre et al, 2401.07564]

In order to stimulate new engagement and trigger some concrete studies in areas where further work would be beneficial towards fully understanding the physics potential of an  $e^+e^-$  Higgs / Top / Electroweak factory, we propose to define a set of focus topics. The

<b>HtoSS</b> — $e^+e^- \rightarrow Zh: h \rightarrow s\bar{s}$ ( $\sqrt{s} = 240/250$ GeV) . . . . .
<b>ZHang</b> — $Zh$ angular distributions and CP studies . . . . .
<b>Hself</b> — Determination of the Higgs self-coupling . . . . .
<b>Wmass</b> — Mass and width of the $W$ boson from the pair-production threshold cross section lineshape and from decay kinematics . . . . .
<b>WWdiff</b> — Full studies of $WW$ and $e\nu W$ . . . . .
<b>TTthres</b> — Top threshold: Detector-level simulation studies of $e^+e^- \rightarrow t\bar{t}$ and threshold scan optimisation . . . . .
<b>LUMI</b> — Precision luminosity measurement . . . . .
<b>EXscalar</b> — New exotic scalars . . . . .
<b>LLPs</b> — Long-lived particles . . . . .
<b>EXtt</b> — Exotic top decays . . . . .
<b>CKMWW</b> — CKM matrix elements from $W$ decays . . . . .
<b>BKtautau</b> — $B^0 \rightarrow K^{0*}\tau^+\tau^-$ . . . . .
<b>TwoF</b> — EW precision: 2-fermion final states ( $\sqrt{s} = M_Z$ and beyond) . . . . .
<b>BCfrag</b> and <b>Gsplit</b> — Heavy quark fragmentation and hadronisation, gluon splitting and quark-gluon separation . . . . .



# Conclusions

- ◆  $e^+e^-$  Colliders: Higgs/Electroweak/Top Factories in clean  $e^+e^-$  environment
- ◆ Absolute Higgs couplings access @ unprecedented precision
- ◆ Unique measurement of  $H e^+e^-$  coupling
- ◆ Higgs self-coupling measurement
- ◆ EWPOs tremendously improved precision

What do we learn from indirect measurements at Higgs/EW/top factories about the underlying model? How can we combine information from all possible observables, experiments and research areas to get maximum insight?

Lot of work ahead! Exciting times!

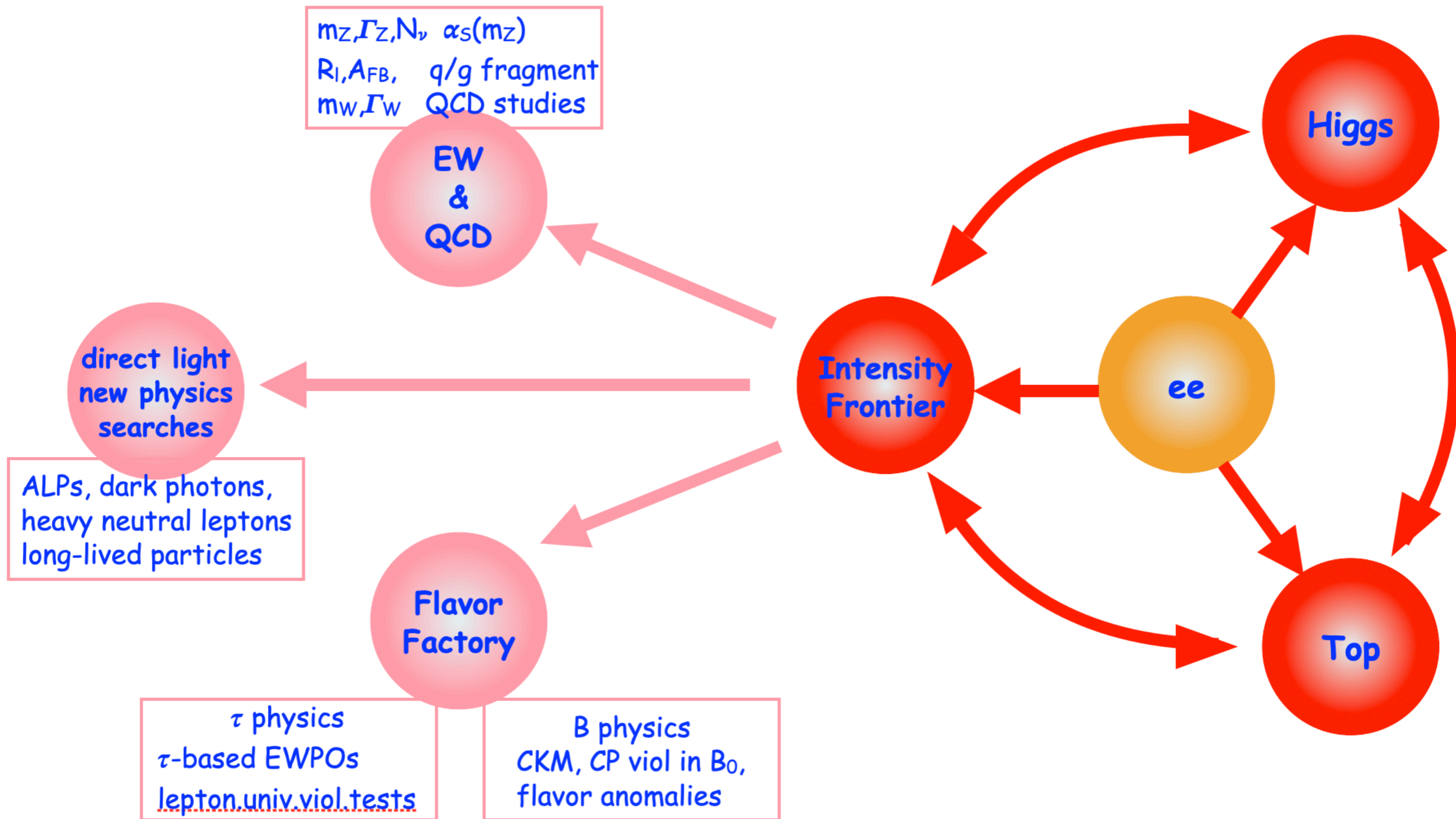




*Thank you for  
your attention!*



# Physics Program at ee-Colliders



# What do we Learn?

[Englert,Freitas,MM,Plehn,Rauch,Spira,Walz,'14]

coupling	LHC	HL-LHC	LC	HL-LC	HL-LHC + HL-LC
$hWW$	0.09	0.08	0.011	0.006	0.005
$hZZ$	0.11	0.08	0.008	0.005	0.004
$htt$	0.15	0.12	0.040	0.017	0.015
$hbb$	0.20	0.16	0.023	0.012	0.011
$h\tau\tau$	0.11	0.09	0.033	0.017	0.015
$h\gamma\gamma$	0.20	0.15	0.083	0.035	0.024
$hgg$	0.30	0.08	0.054	0.028	0.024
$h_{\text{invis}}$	—	—	0.008	0.004	0.004

TABLE I: Expected accuracy at the 68% C.L. with which fundamental and derived Higgs couplings can be measured; the deviations are defined as  $g = g_{SM}[1 \pm \Delta]$  compared to the Standard Model at the LHC/HL-LHC (luminosities 300 and 3000  $\text{fb}^{-1}$ ), LC/HL-LC (energies 250+500 GeV / 250+500 GeV+1 TeV and luminosities 250+500  $\text{fb}^{-1}$  / 1150+1600+2500  $\text{fb}^{-1}$ ), and in combined analyses of HL-LHC and HL-LC. For invisible Higgs decays we give the upper limit on the underlying couplings. Constraints on an invisible Higgs decay width involve model-specific assumptions at the LHC, see e.g. [15]. Therefore, we allow for additional contributions to the total Higgs width only in the linear collider scenarios, where these can be constrained model-independently by exploiting the recoil measurement [14].

# Higgs Coupling Measurements

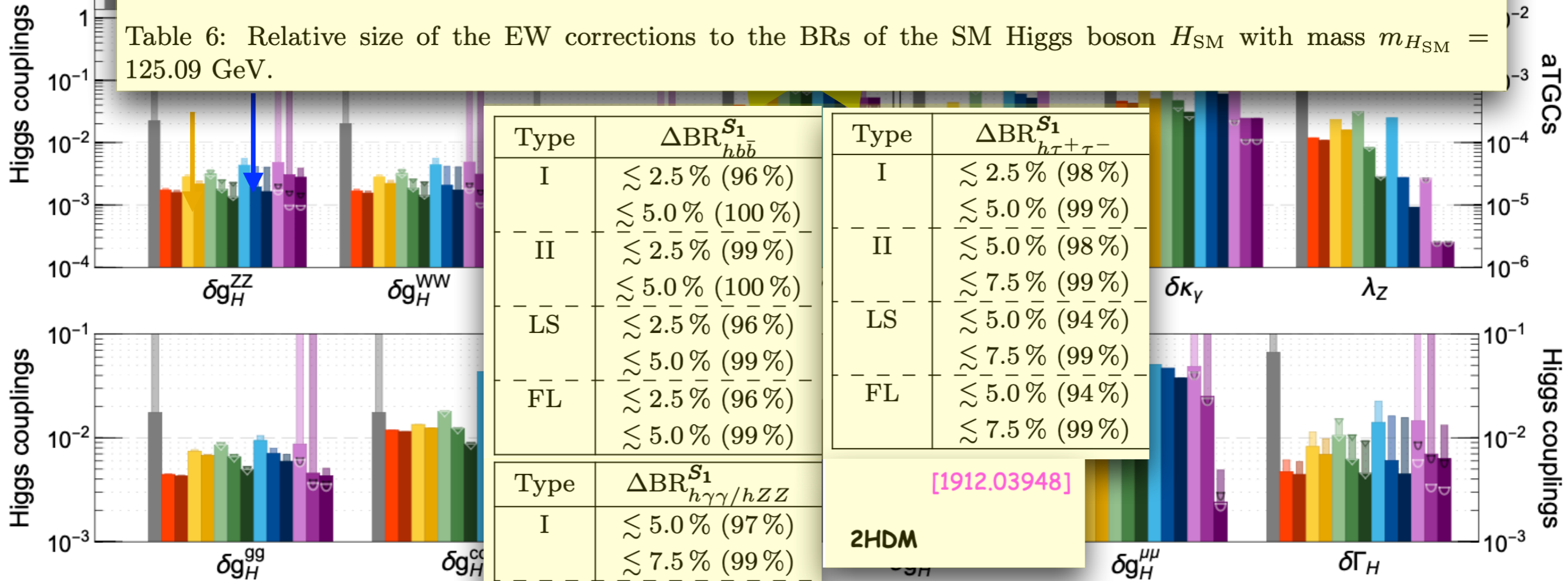
Part of:  
Establish

precision reach on effective couplings from SMEFT global fit

[2012.03326]

$\Delta\text{BR}$	$b\bar{b}$	$\tau^+\tau^-$	$\mu^+\mu^-$	$s\bar{s}$	$c\bar{c}$	$gg$	$\gamma\gamma$	$Z\gamma$	$W^+W^-$	$ZZ$
	-1.76%	-1.59%	-3.52%	2.24%	-3.81%	4.34%	-2.29%	-0.71%	3.68%	1.61%

Table 6: Relative size of the EW corrections to the BRs of the SM Higgs boson  $H_{\text{SM}}$  with mass  $m_{H_{\text{SM}}} = 125.09$  GeV.



- all Higgs
- couplings
- at least

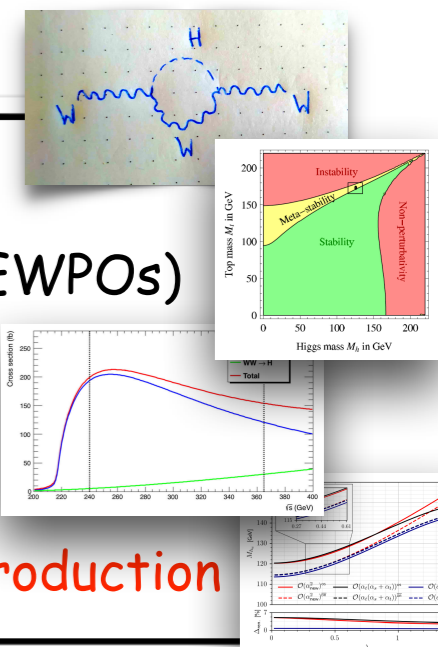
luminosity vs. polarization  
percent - few per mille precision  
precision gain compared to HL-LHC

# Higgs Mass Measurement

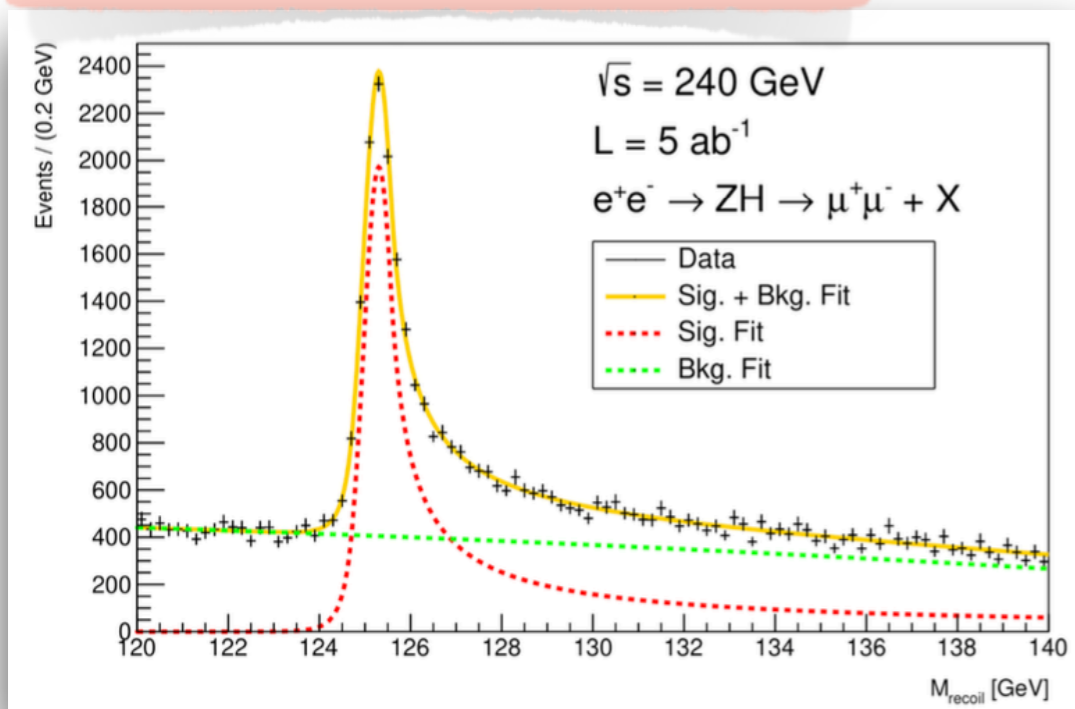
## ❖ Higgs mass and ZH cross section:

Why precision?

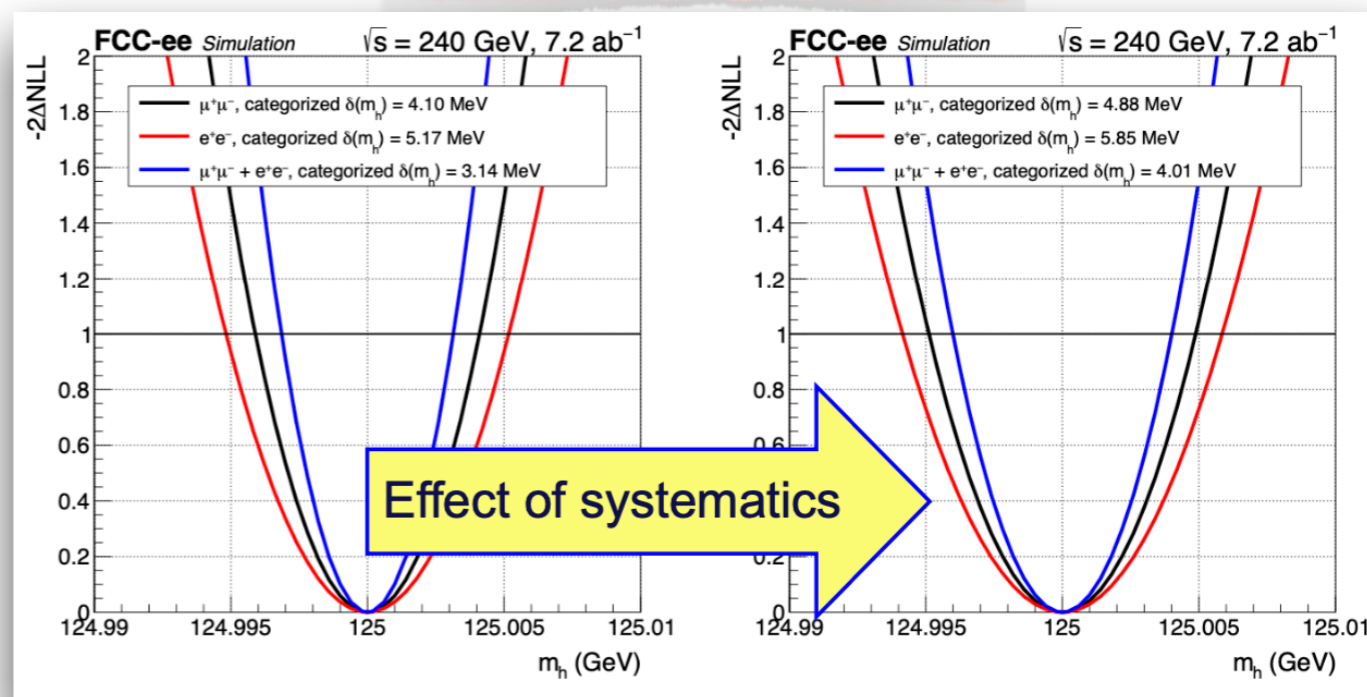
- \* Self-consistency test of SM at quantum level (e.g.: Higgs loop corrections to EWPOs)
- \*  $M_H \leftrightarrow$  stability of the electroweak vacuum
- \* Higgs mass uncertainty feeds back in uncertainty on Higgs observables
- \* Test parameter relations in beyond-SM theories
- \* **Required for electron Yukawa coupling determination from  $e^+e^- \rightarrow H$  resonant production**



$M_H$  fitted from actual exp.  $m_{\text{recoil}}$  distribution



$\delta(m_H) = 3.1 (4.0) \text{ MeV stat(syst)}$



[Eysermans, Bernardi, Li]

# Higgs Mass Measurement

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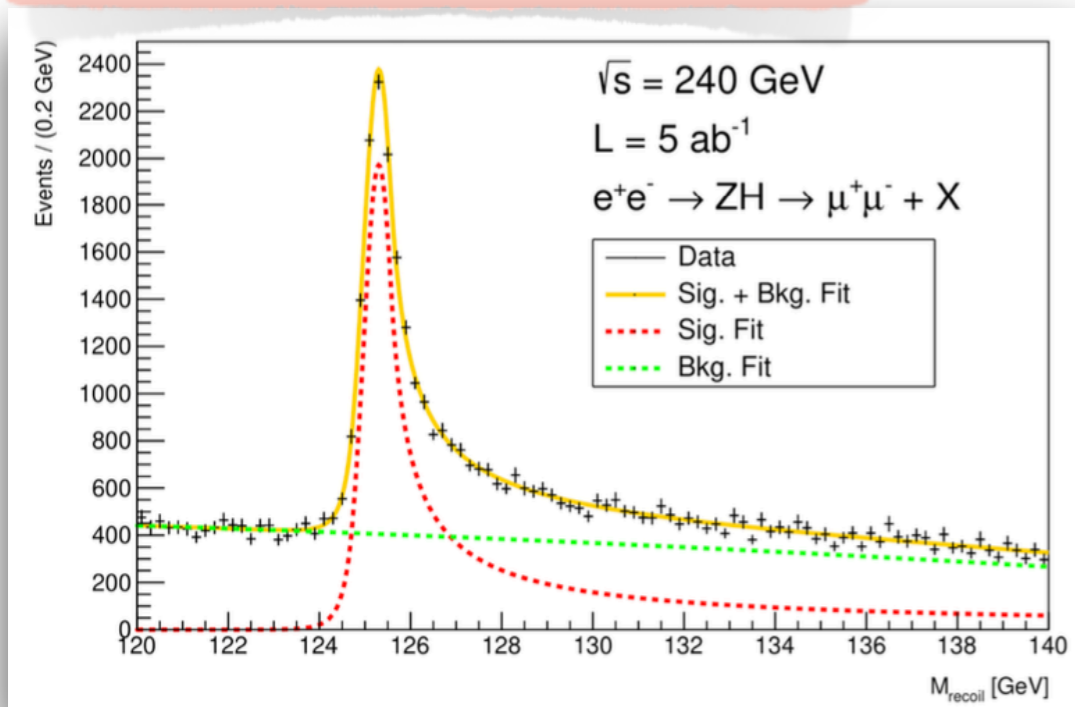
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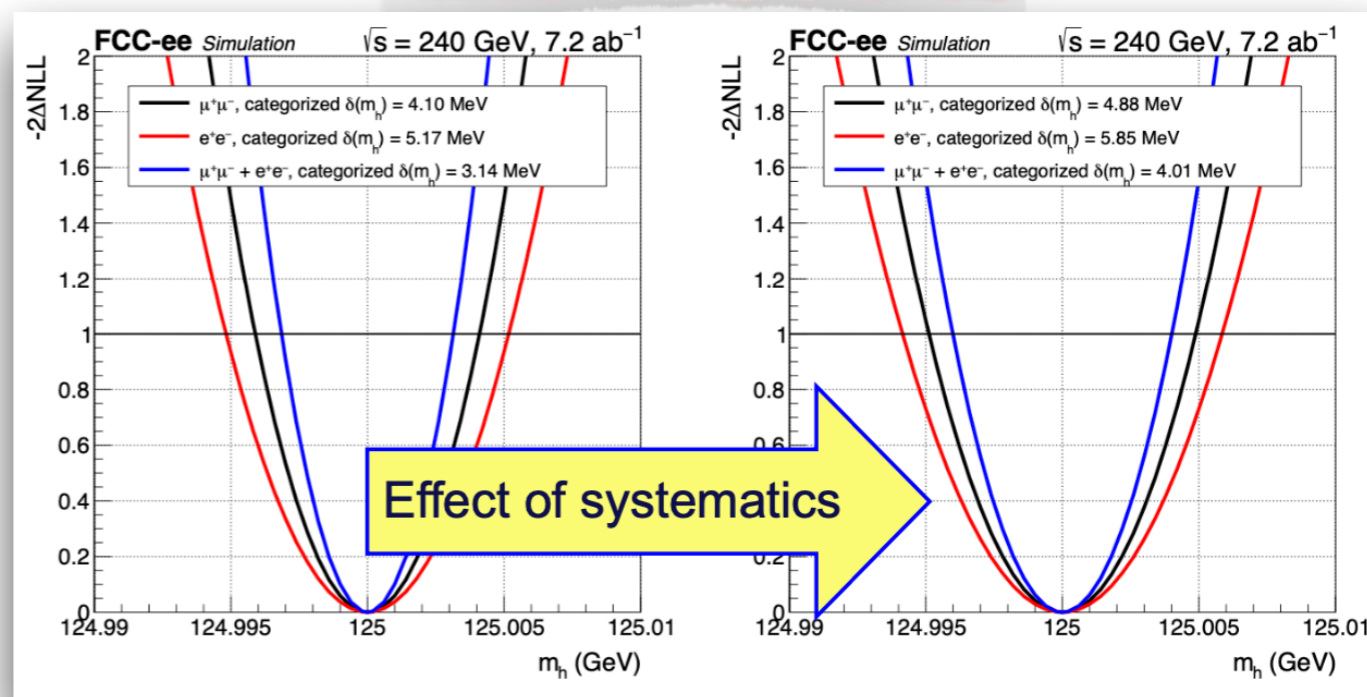
$O(10 \text{ MeV})$  need for permille precision of  $g_H^{ZZ}, g_H^{WW}, g_H^{Z\gamma}$

$O(\Gamma_H=4 \text{ MeV})$  to measure electron Yukawa coupling

$M_H$  fitted from actual exp.  $m_{\text{recoil}}$  distribution



$\delta(m_H) = 3.1 (4.0) \text{ MeV stat(syst)}$



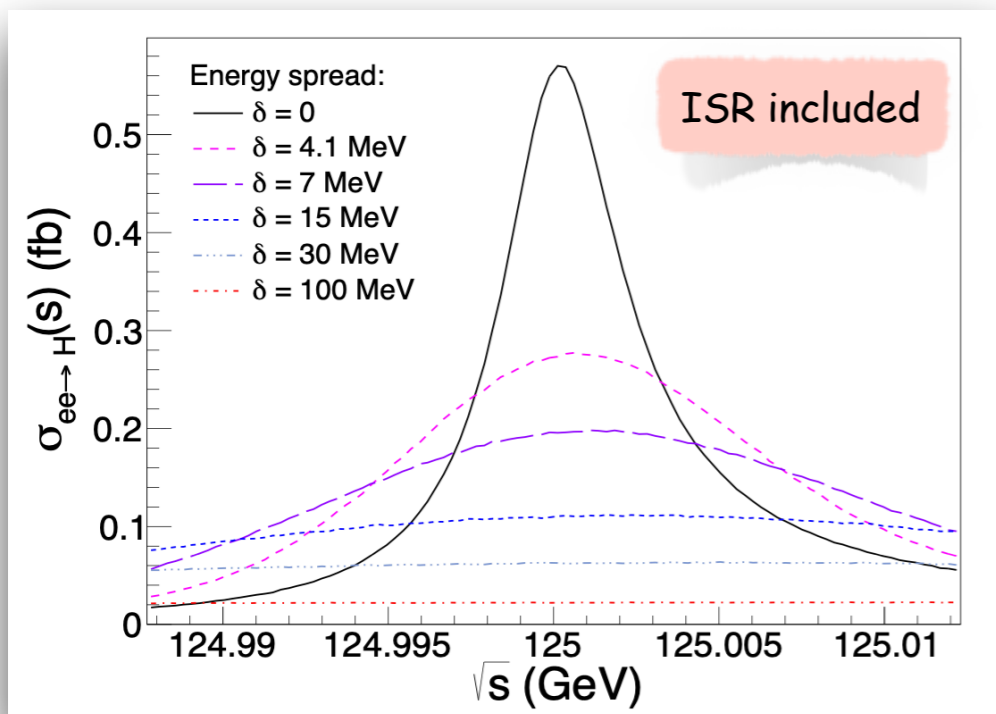
[Eysermans, Bernardi, Li]

# Electron Yukawa Coupling - Unique!

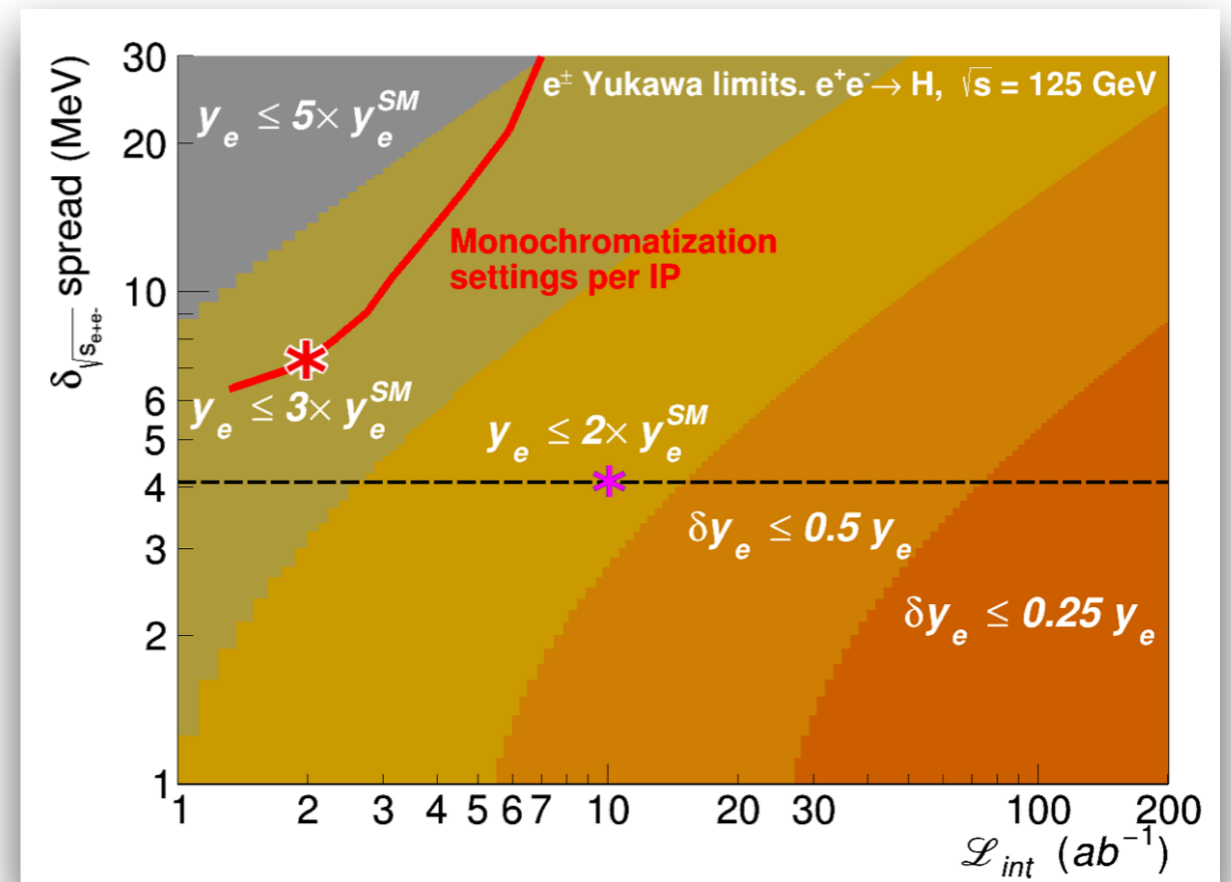
- ❖ **Why electron Yukawa coupling:** establish experimentally the Higgs coupling to *all* generations  $\leadsto$  also to the 1st generation!
- ❖ **How?:** from  $e^+e^- \rightarrow H$  at  $\sqrt{s} = M_H$  ❖ **Challenge:** coupling extremely tiny

## Requirements

- \*  $M_H$  knowledge at  $\mathcal{O}(\text{few MeV})$  precisely
- \* Huge luminosity (i.e. several years w/ 4 IPs)
- \* (Mono)chromatization  $\Gamma_H(4.2 \text{ MeV}) \ll \delta_{\sqrt{s}}(100 \text{ MeV})$
- \* continuous  $\sqrt{s}$  monitoring & adjustment
- \* extremely sensitive event selection against SM backgrounds



[d' Enterraia, Poldaru, Wojcik, 2107.02686]



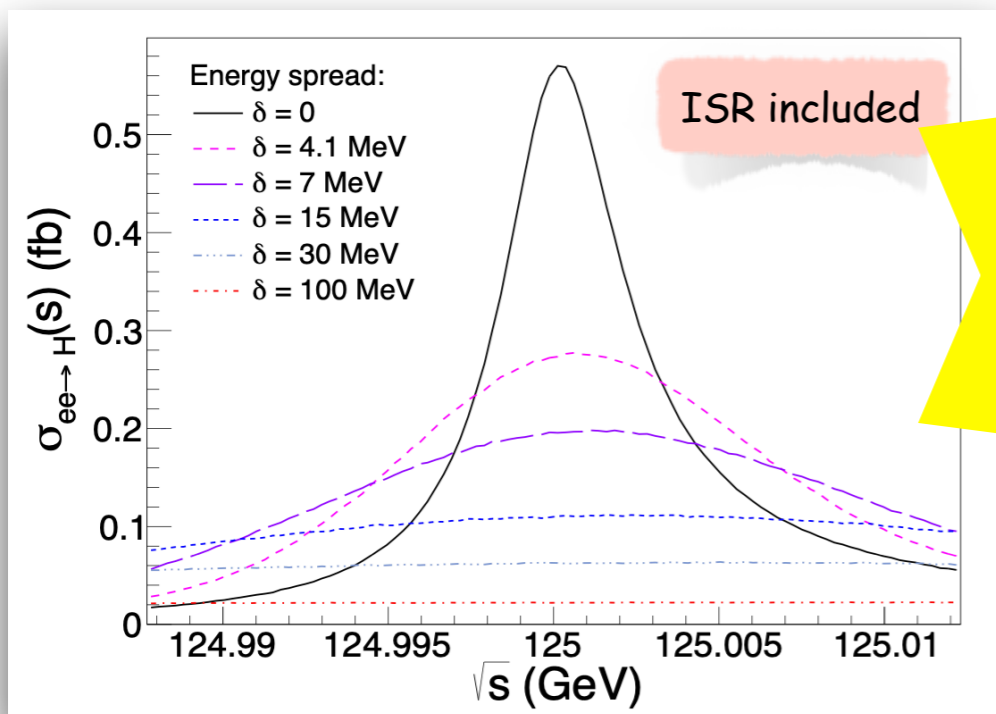


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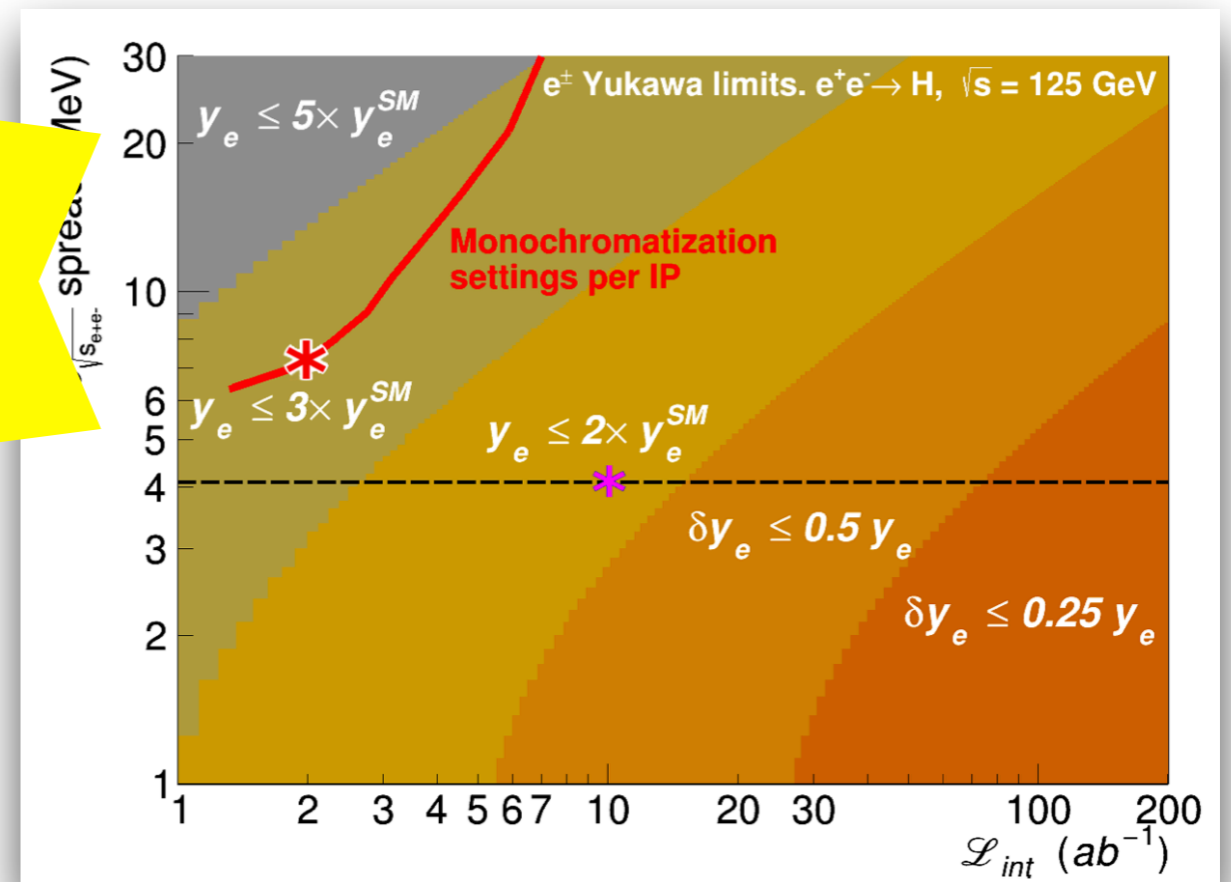
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Huge challenge  
but only place  
where you can  
ever measure  
1st gen Yukawa!

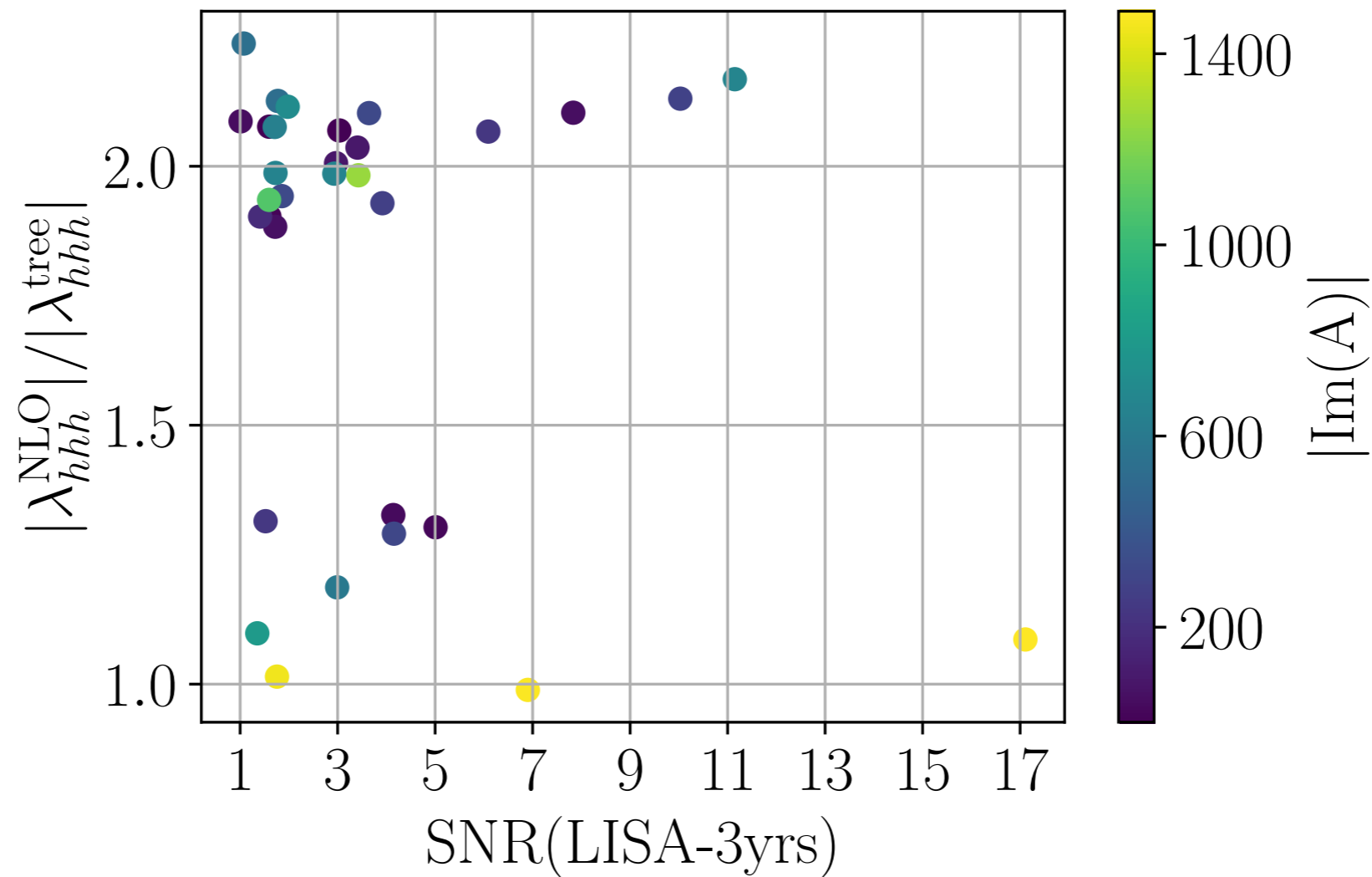


[d' Enterra, Poldaru, Wojcik, 2107.02686]

# Higgs Self-Coupling & Evolution of the Universe

- ⇒ **Model CP in the Dark:** SM-Higgs ( $\lambda_{hhh}^{tree} = \lambda_{hhh}^{SM}$ ) + Dark Sector  
GW signal from strong first-order phase transition

[Basler, Biermann, MM, Müller, Santos, Viana, '24]

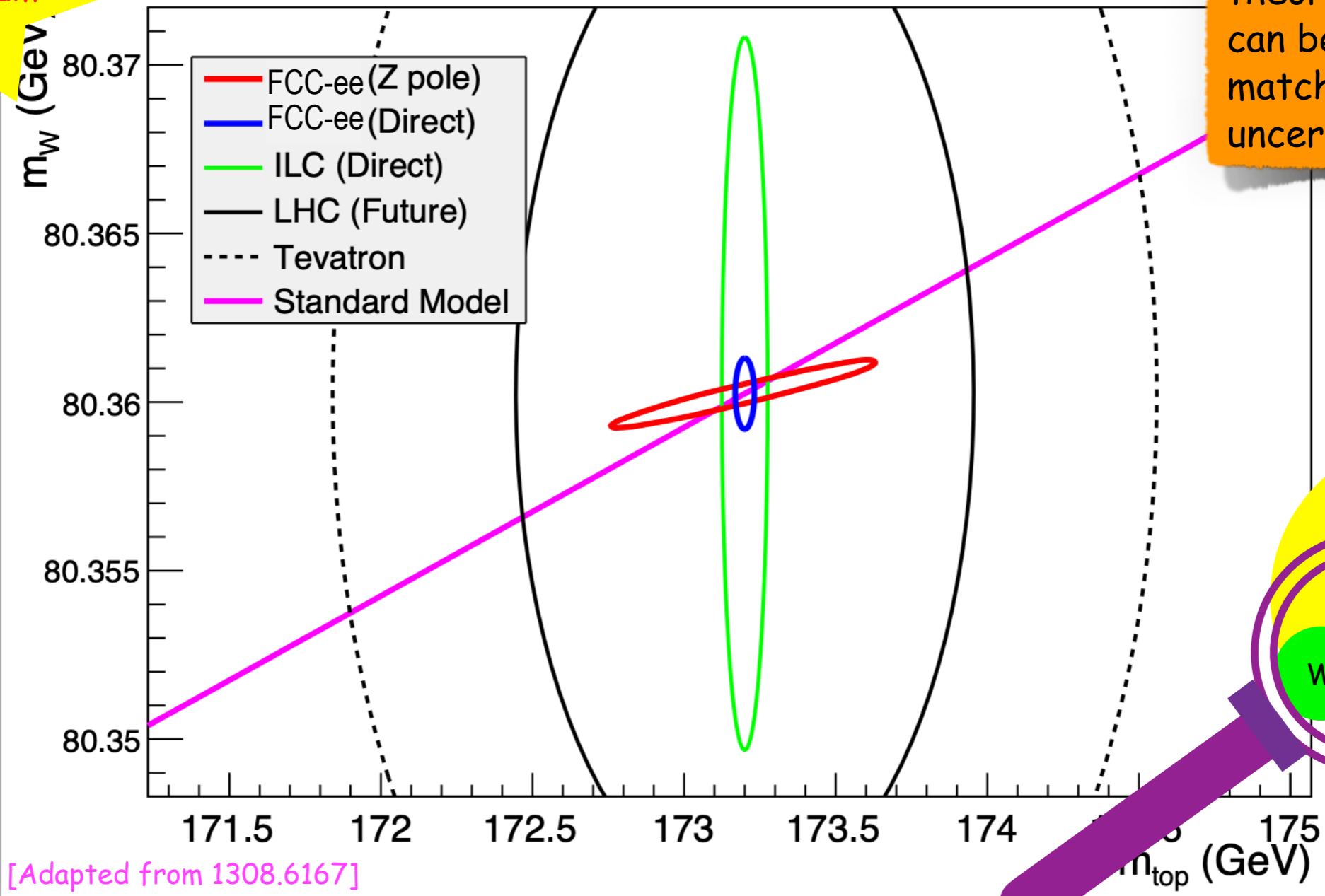


[Biermann, Borschensky, Erhardt, MM, Santos, Viana]

- ⇒ **Vector DM Model:** two visible Higgs bosons + Dark photon  
Strong first-order phase transition:  $\delta\lambda_{hhh}^{NLO} / \lambda_{hhh}^{LO} = 8\%$

# SM Fit to all EWPOs

Consistency test of SM at quantum level



Assumes that all theor. uncertainties can be reduced to match the exp. uncertainties!

