

Detectors: specific challenges for medical application

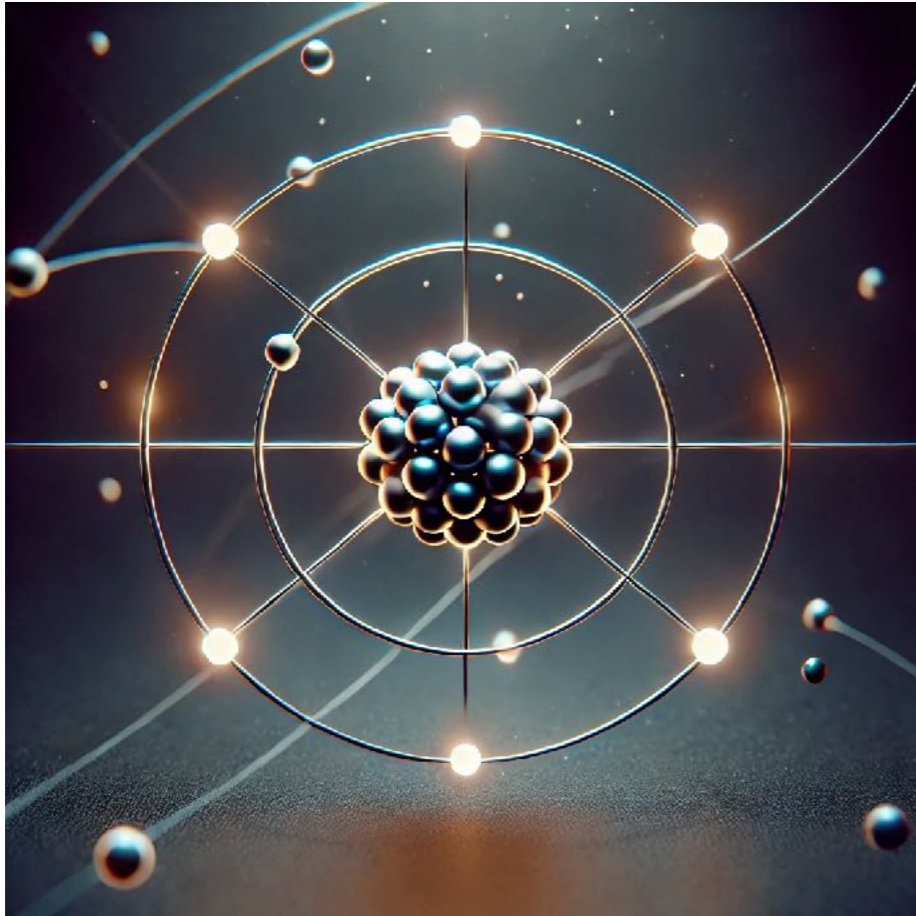
Detectors: specific challenges for medical application



Christophe Theisen alias Tof

Dedication to Tof:
This lesson will be “tout pourri”
(completely rotten)

Detectors: specific challenges for medical application



- Interaction particle-matter
- Gaseous Detectors
- Scintillators
- Semi-conductors
- Applications

➔ To detect a particle, an energy loss must be observed in the sensor

➔ I will not present ALL kind of detectors and ALL kind of medical applications

➔ “Personal” choice

Interaction particle - matter (i)

□ Energy loss for charged particles:

- Loss given by Bethe – Bloch formula:

$$-\frac{dE}{dx} = \frac{ZN}{4\pi\epsilon_0^2} \times \frac{z^2 e^4}{\beta^2 m_e c^2} \left[\ln\left(\frac{2m_e c^2 \beta^2 \gamma^2}{I_0}\right) - \ln(1 - \beta^2) - \beta^2 - \delta - \frac{C_k}{Z} \right]$$
$$\beta = v/c \quad \gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

Interaction particle - matter (i)

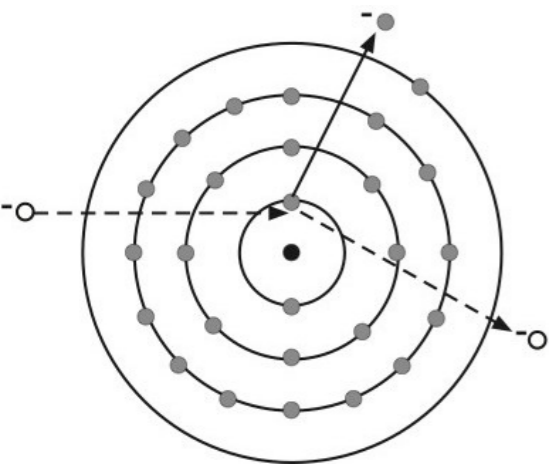
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Depend on

- Velocity β and charge z^2 of the impinging particle
- Charge density of medium ZN
- Ionisation factor I_0 , shell C_k and charge δ corrections



Interaction particle - matter (i)

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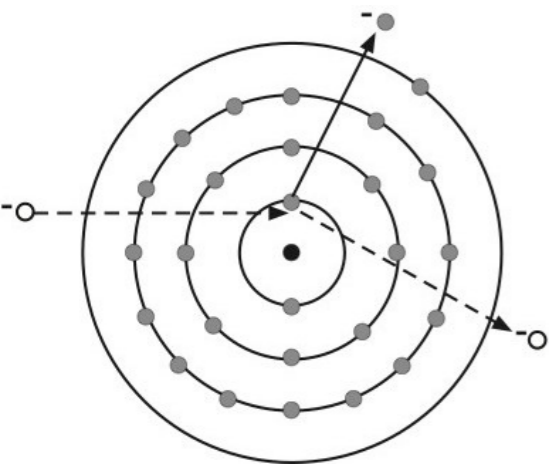
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Gas	formula	I_0 (eV)
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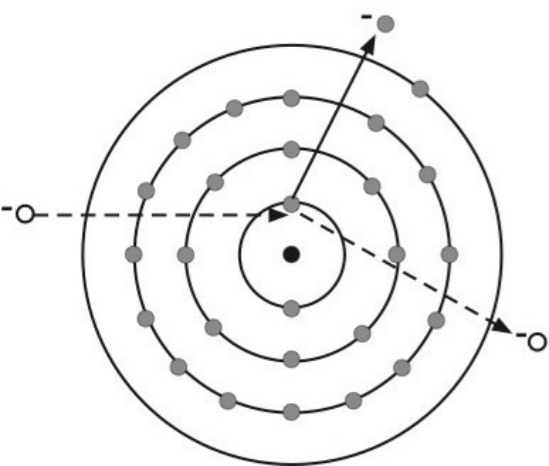
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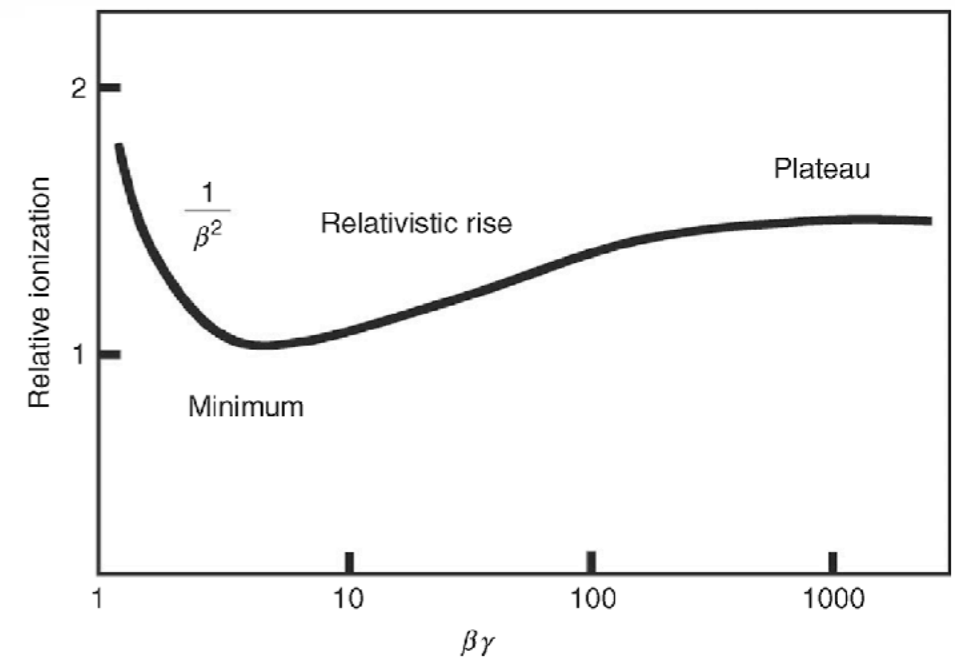
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Electromagnetic interactions of charged particles with matter, F. Sauli

- Minimum of ionisation: $\sim 95\%$ of mass
- Classical behaviour: $\beta \ll 1, \frac{dE}{dx} \propto 1/\beta^2$
- Relativistic rising: $\frac{dE}{dx} \propto \ln(\beta^2)$
- Fermi plateau: $\beta \gtrsim 0.95$

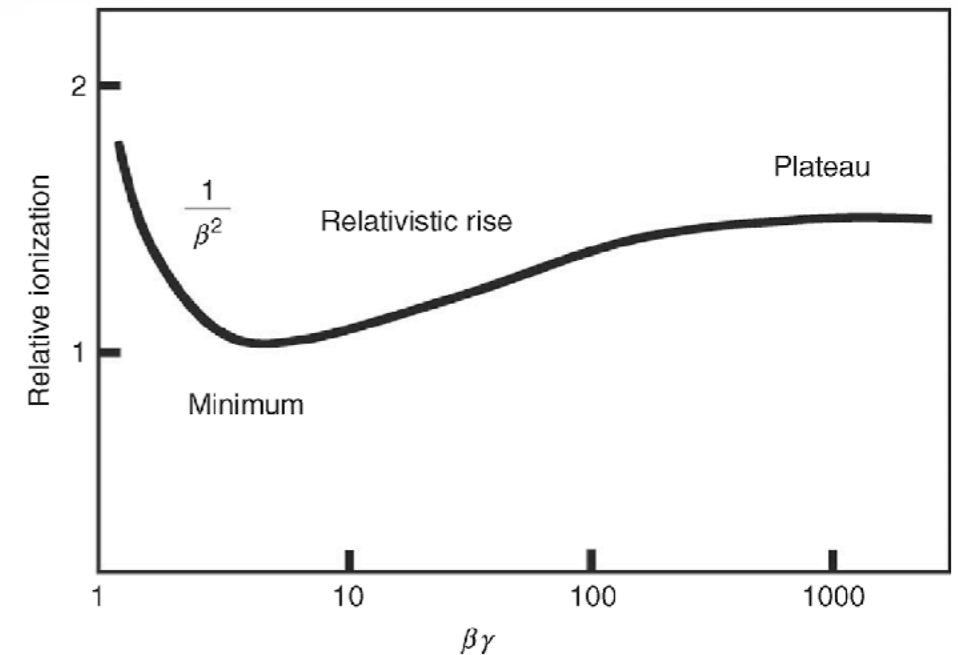
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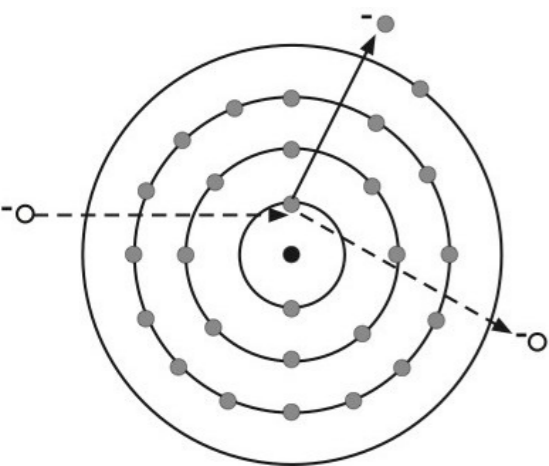
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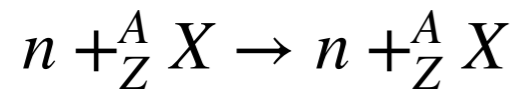
$\rightarrow \frac{dE}{dx} \nearrow \text{ when } \beta \searrow$

Interaction particle - matter (ii)

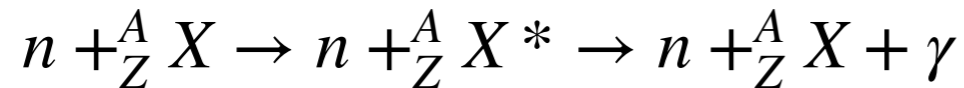
□ Energy loss for neutral particles:

- Loss by nuclear scattering:

- Elastic scattering

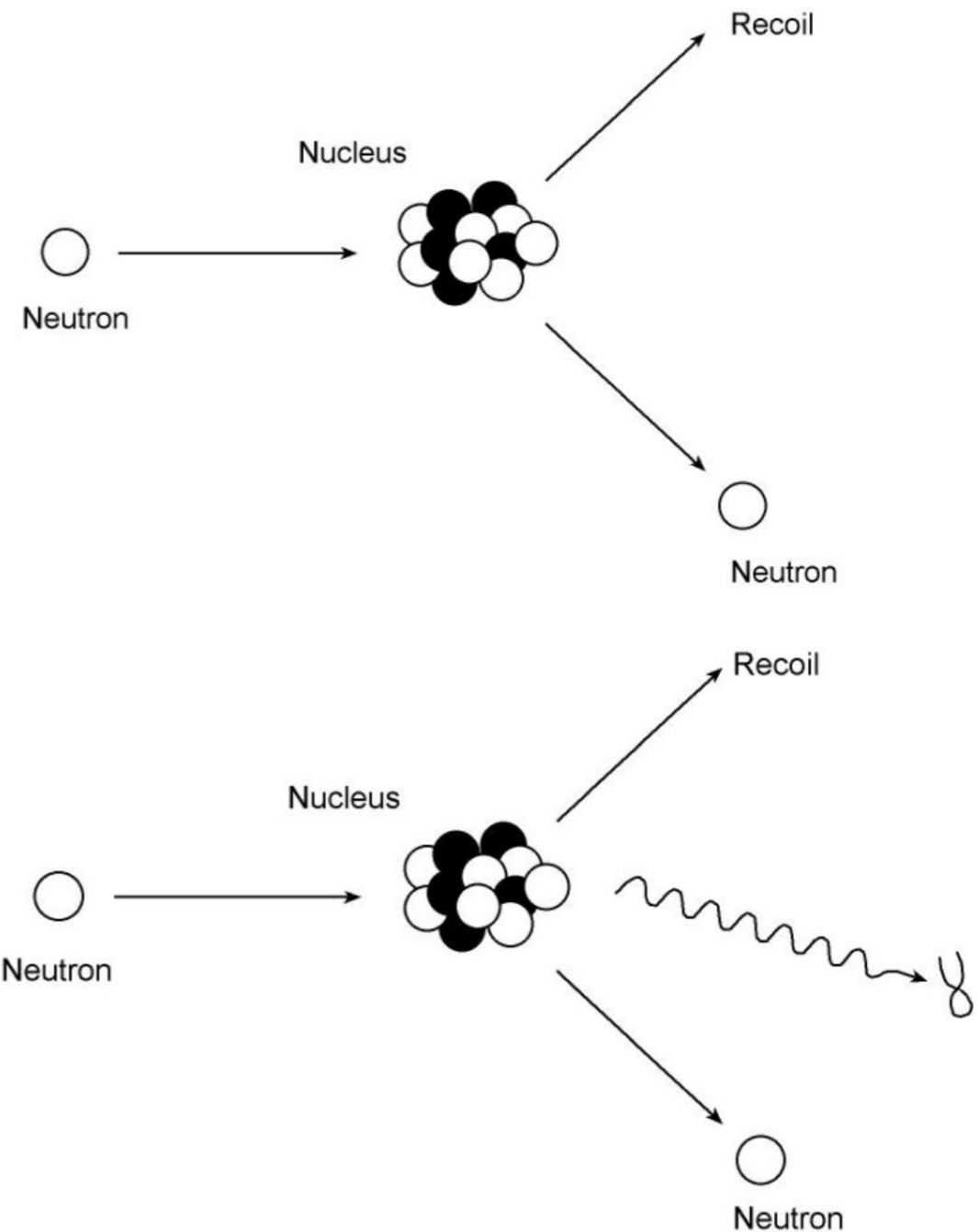


- Inelastic scattering



➔ Losing energy by successive collisions

➔ Does not include capture or fission reaction



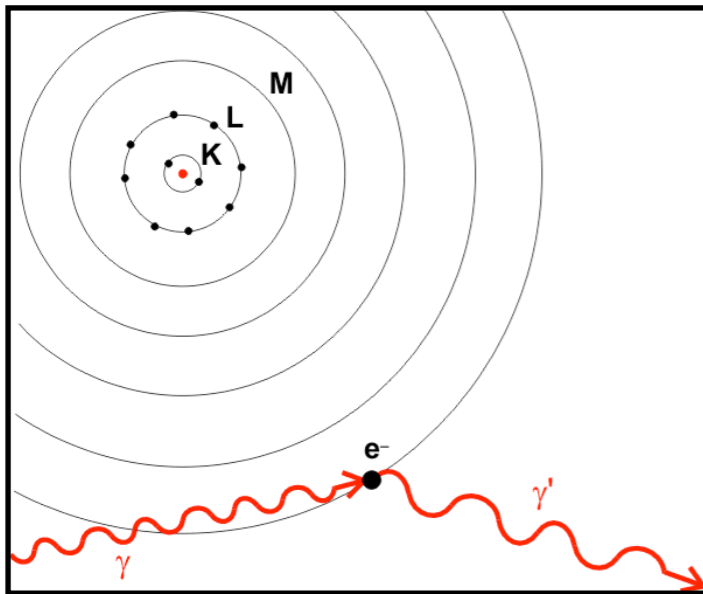
Interaction particle - matter (iii)

- ☐ Energie loss for photons:
 - 3 main processes:

Interaction particle - matter (iii)

☐ Energie loss for photons:

- 3 main processes:
 - Compton effect



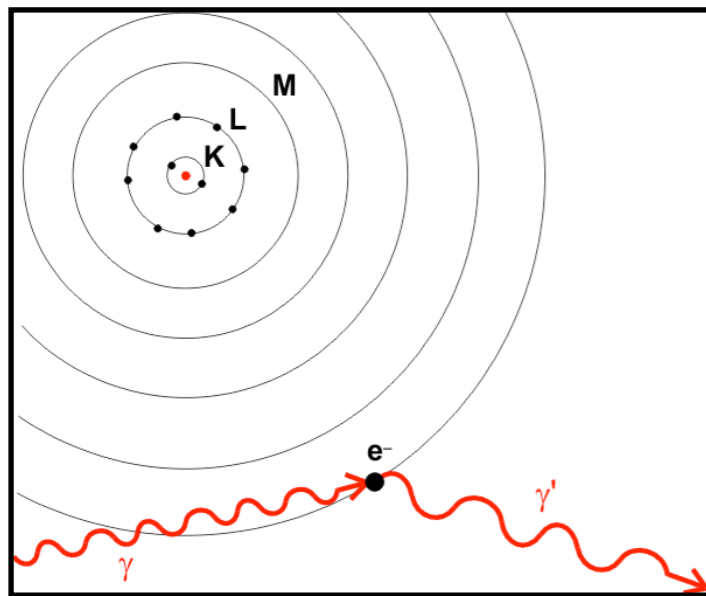
$$\sigma_c \propto (1 - \gamma)^2 \quad (1 - \gamma \ll 1)$$

$$\sigma_c \propto 1/\gamma \quad (\gamma \gg 1)$$

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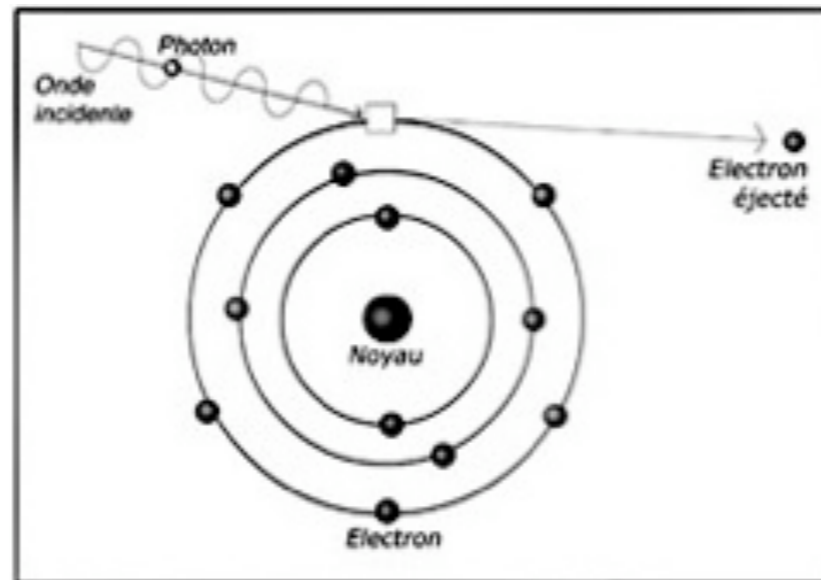
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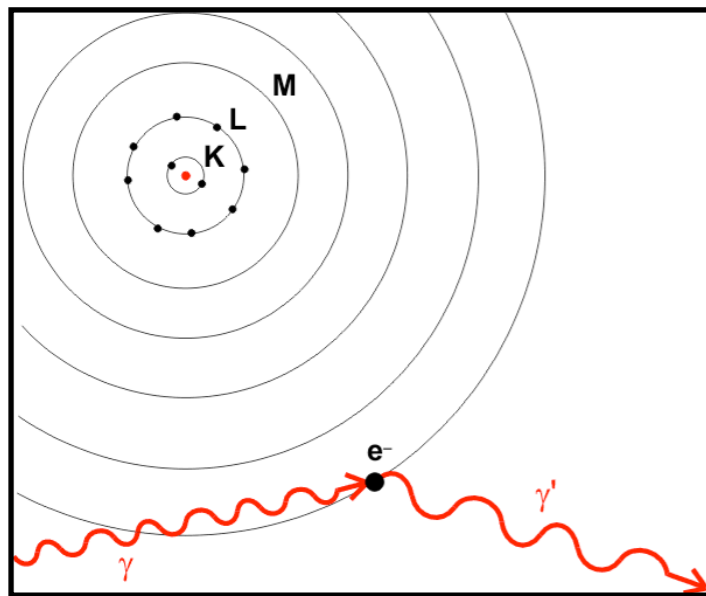


$$\sigma_{ph} \simeq \frac{Z^n}{E_\gamma^{3.5}} \quad n \sim [4, 5]$$

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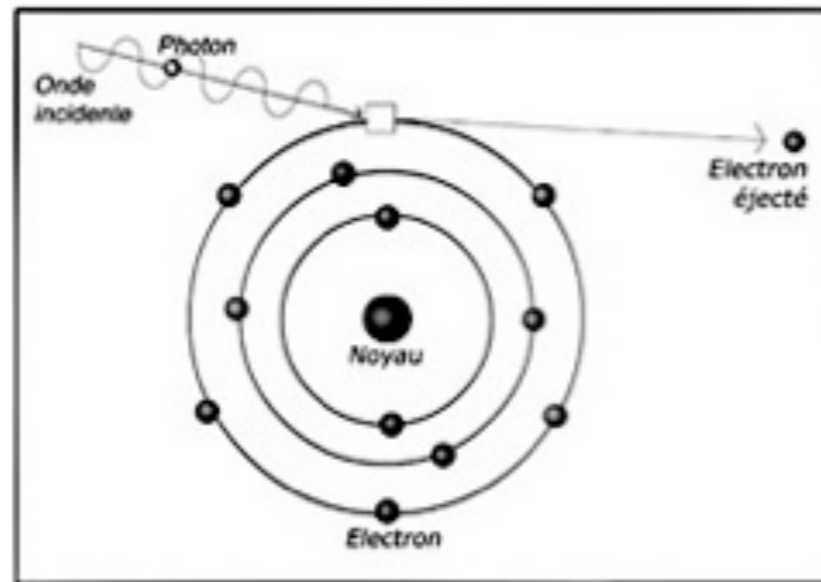
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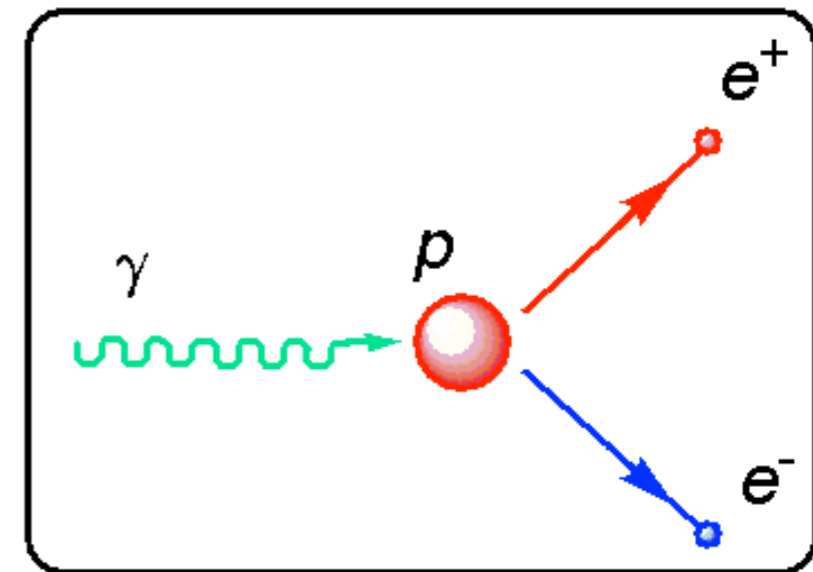


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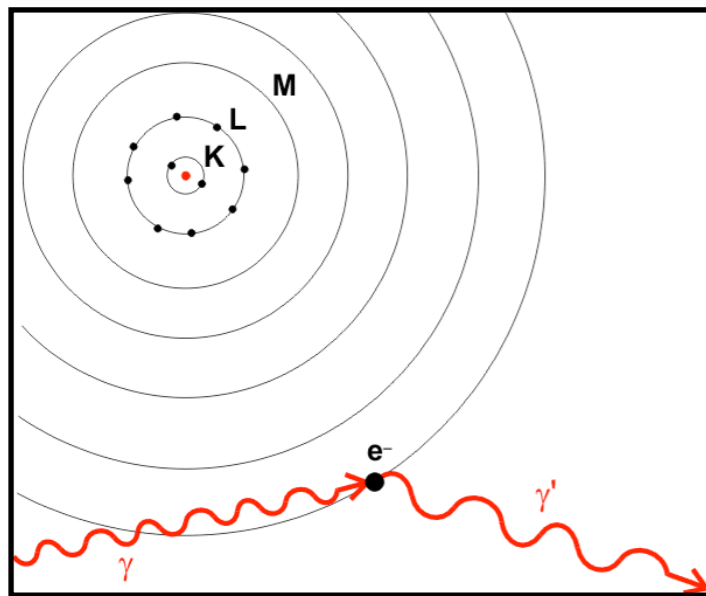
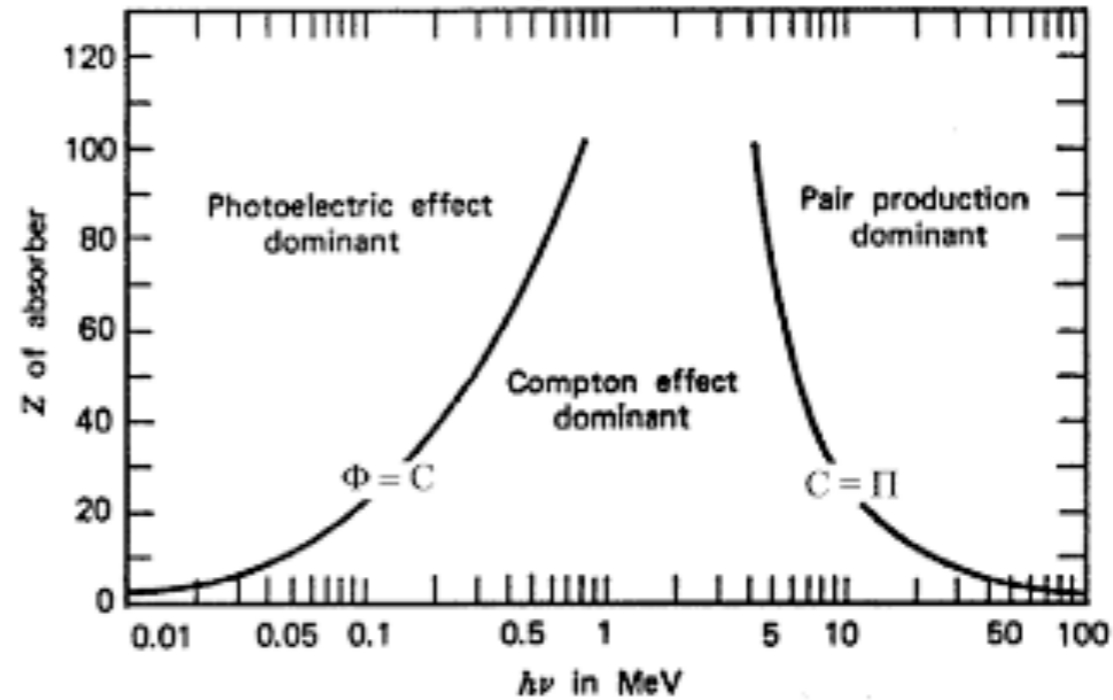


$$\sigma_c \propto Z^2 \ln(E_\gamma) \quad E_\gamma > 2m_e c^2$$

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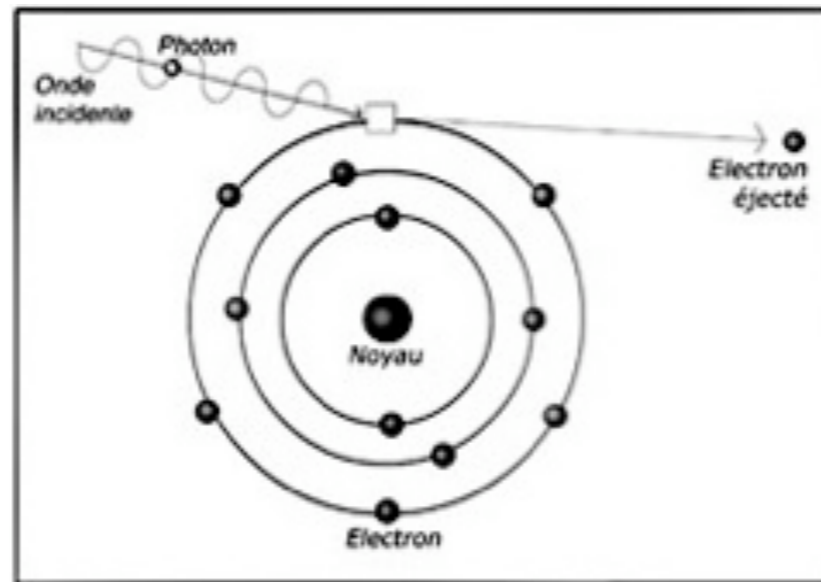
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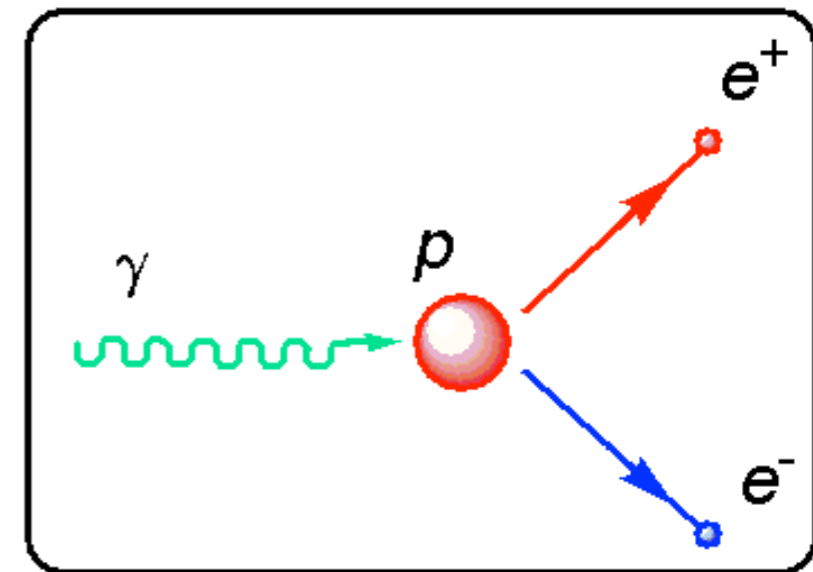


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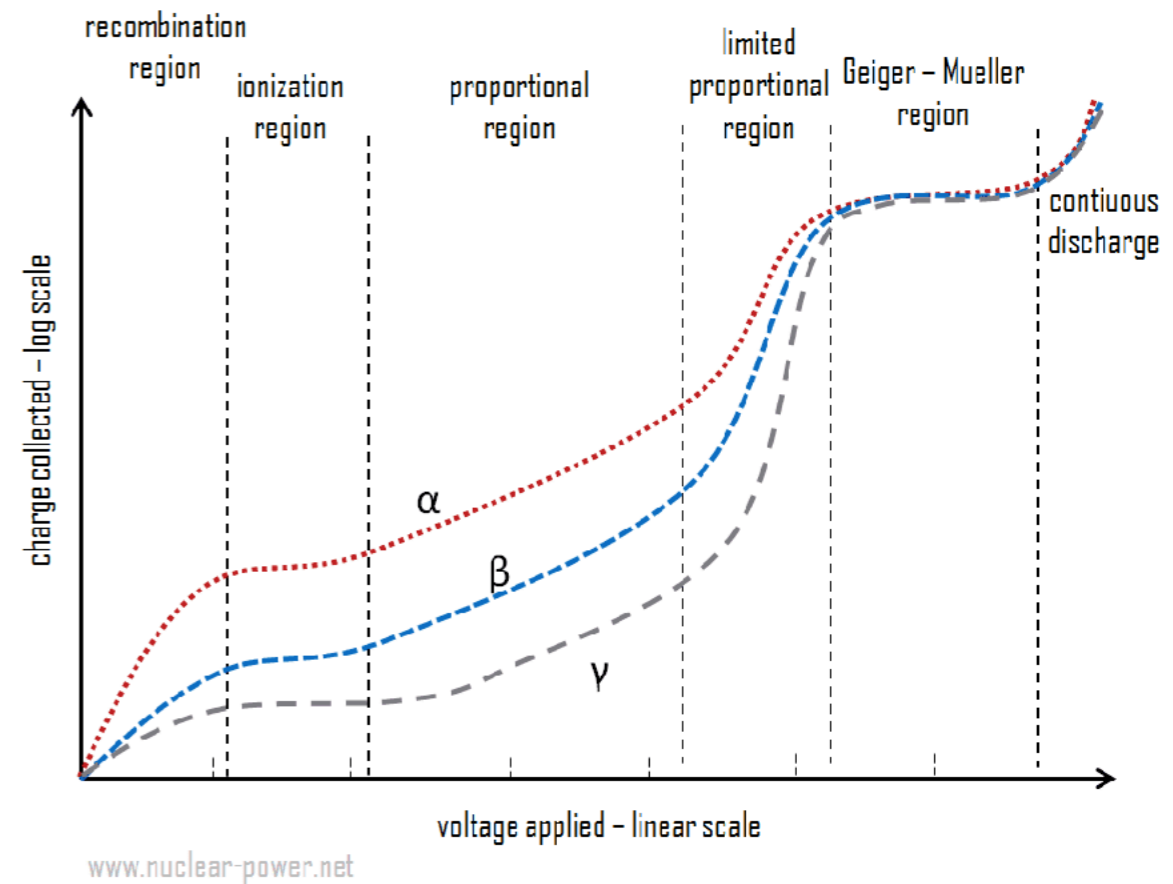
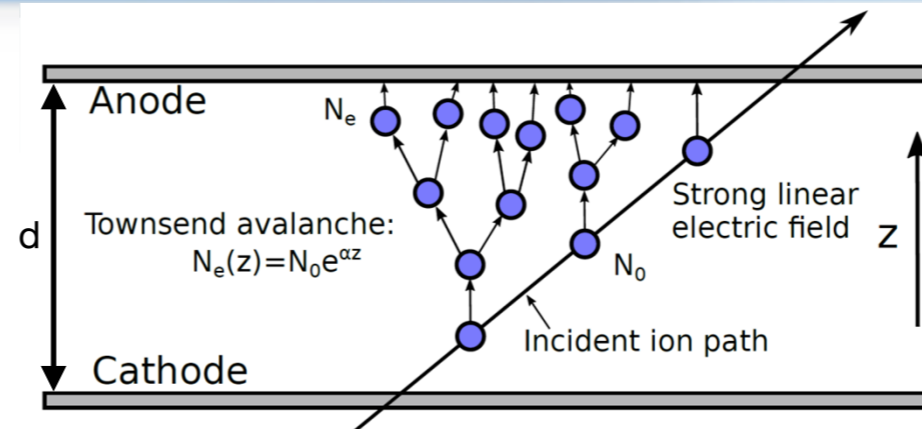
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Gaseous detector (i)

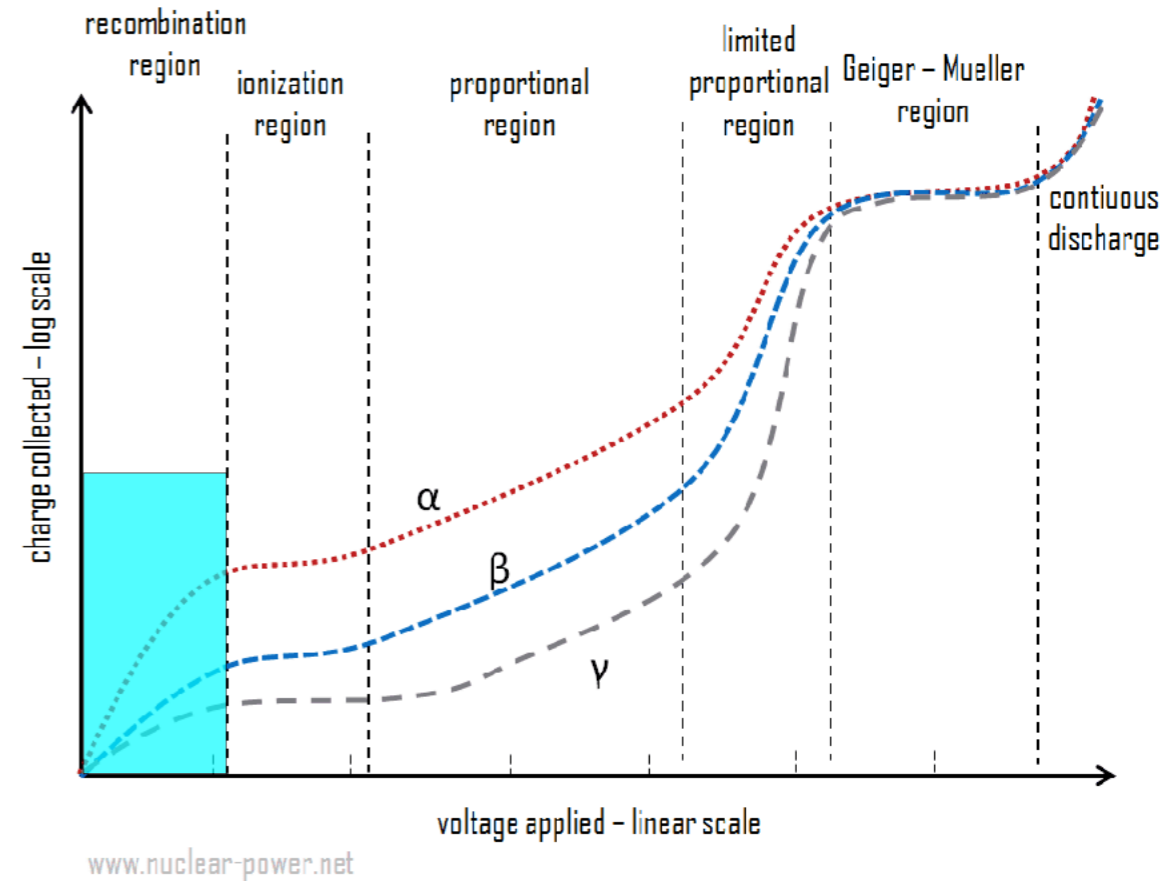
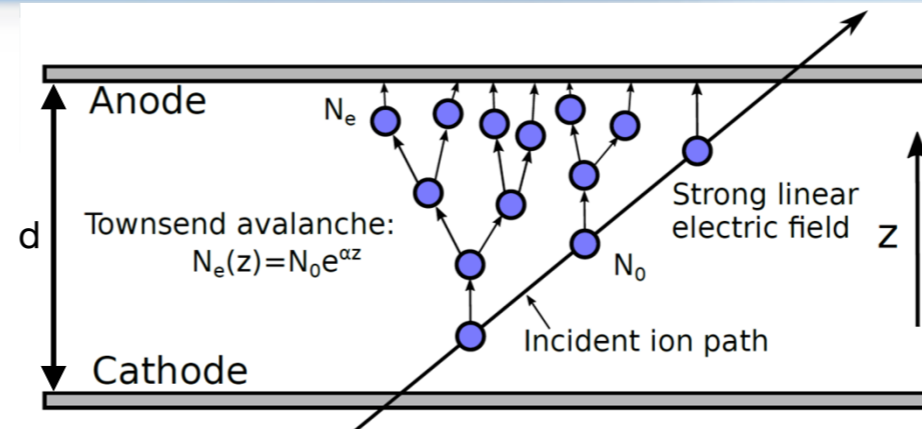
□ Response as function of HV:



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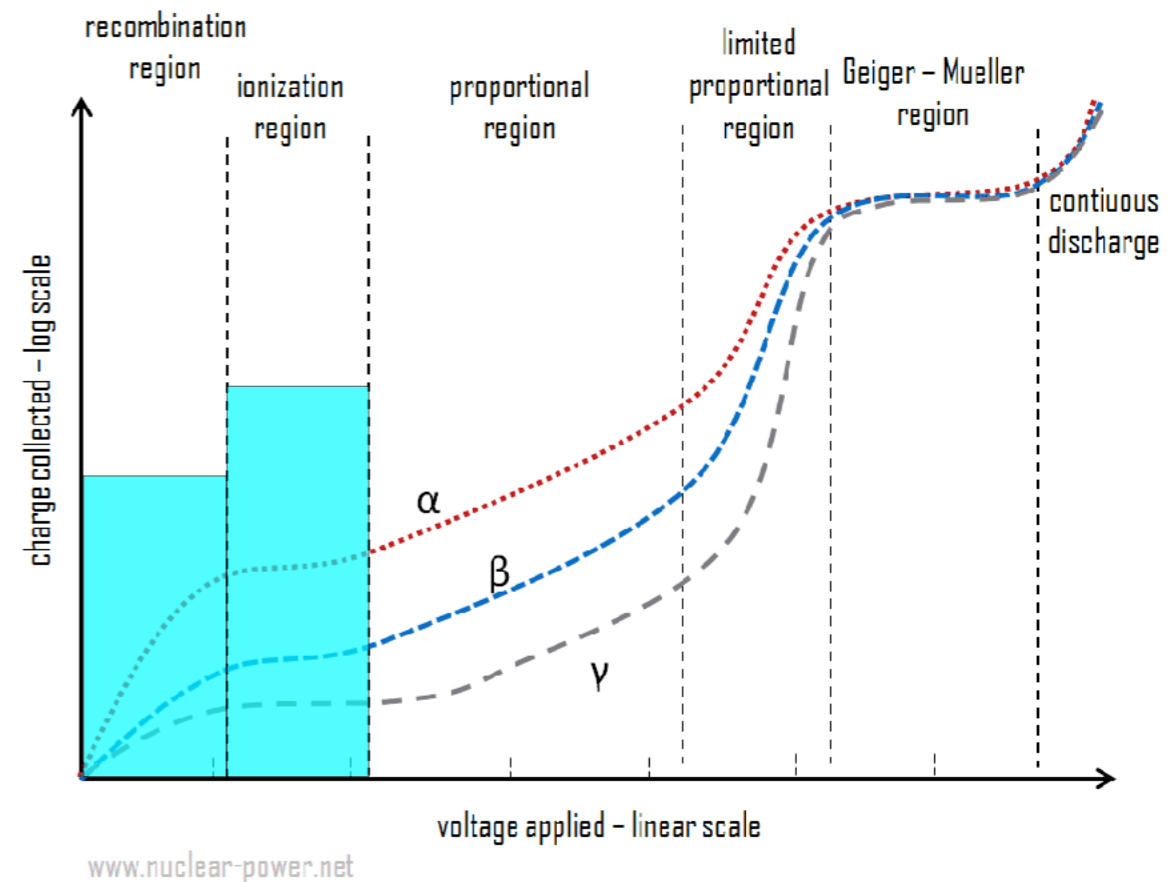
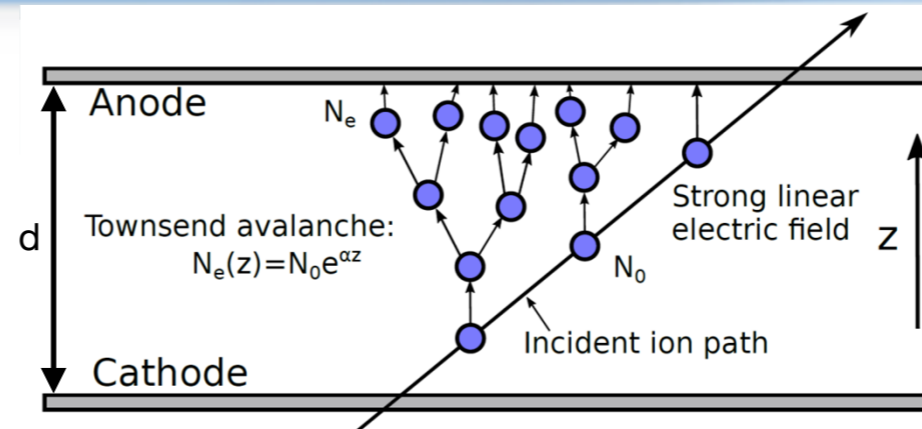
- $HT \ll 1$, recombinaison



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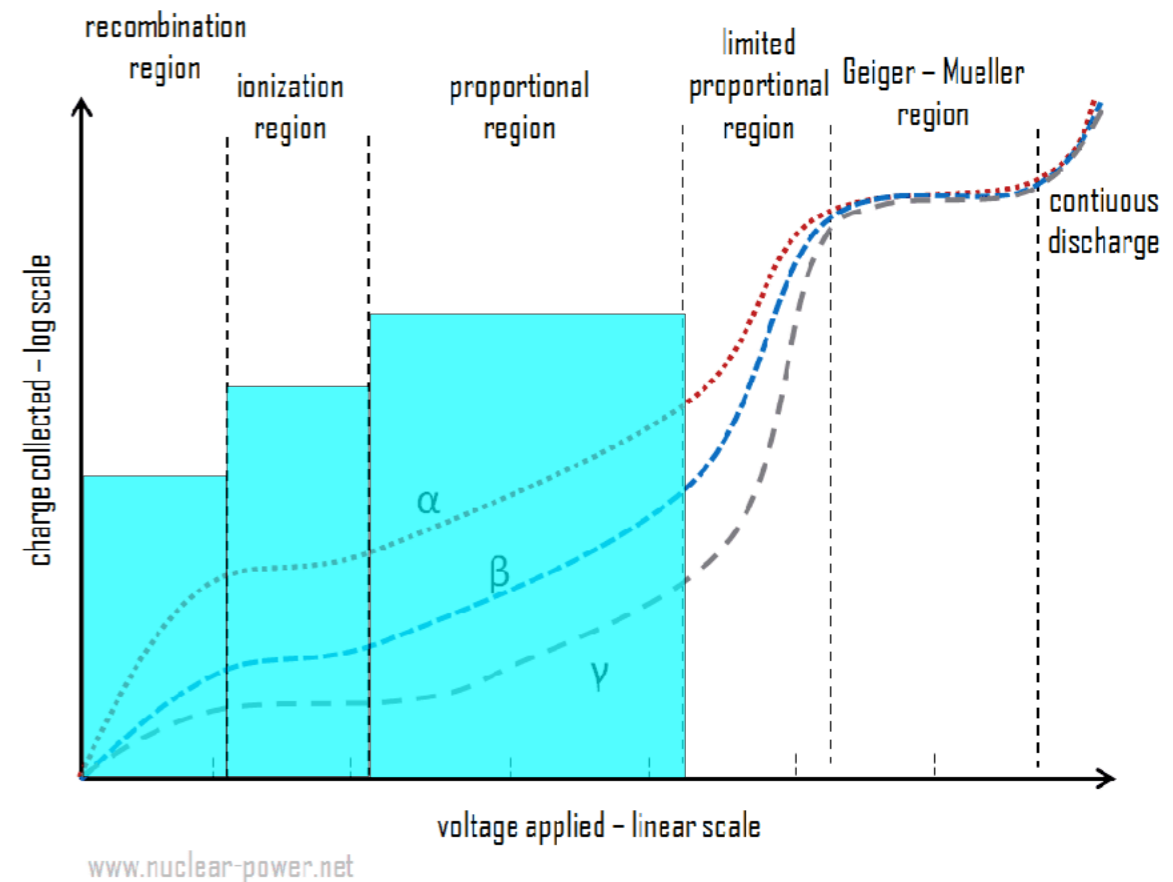
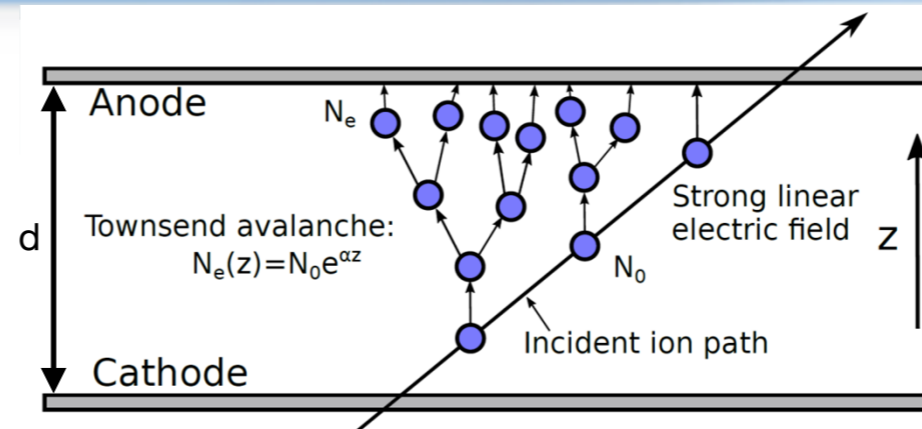
- $HT \ll 1$, recombinaison
- $HT \nearrow$, ionisation, without secondary process



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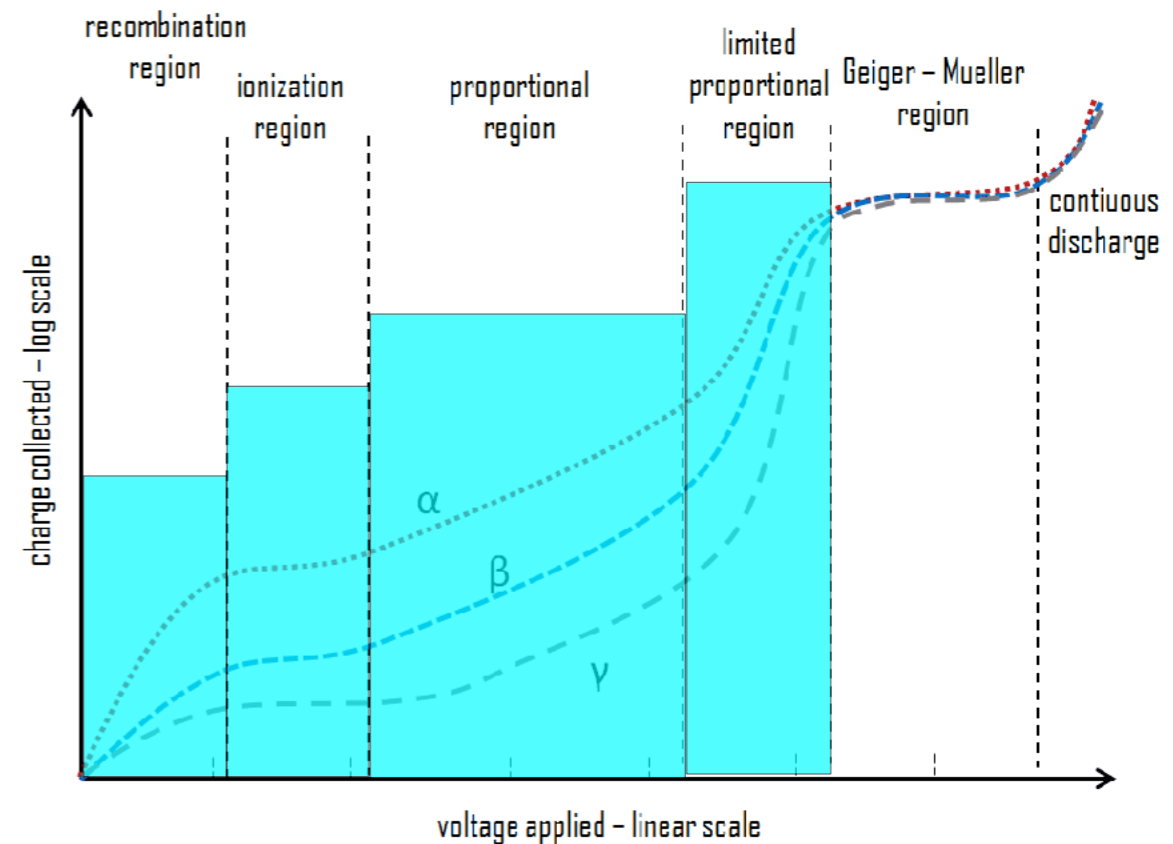
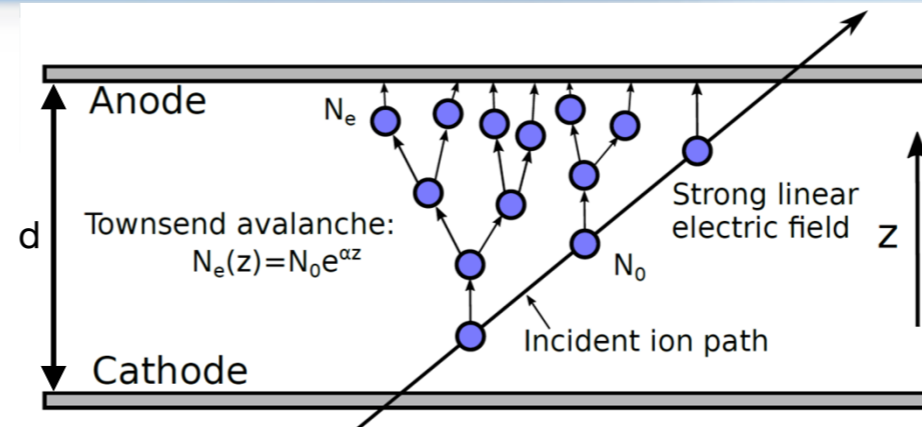
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Gaseous detector (i)

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- $HT \nearrow \nearrow$, proportional, secondary ionisations, avalanche effect
- $HT \uparrow$, degraded proportional, creation of photo-electrons

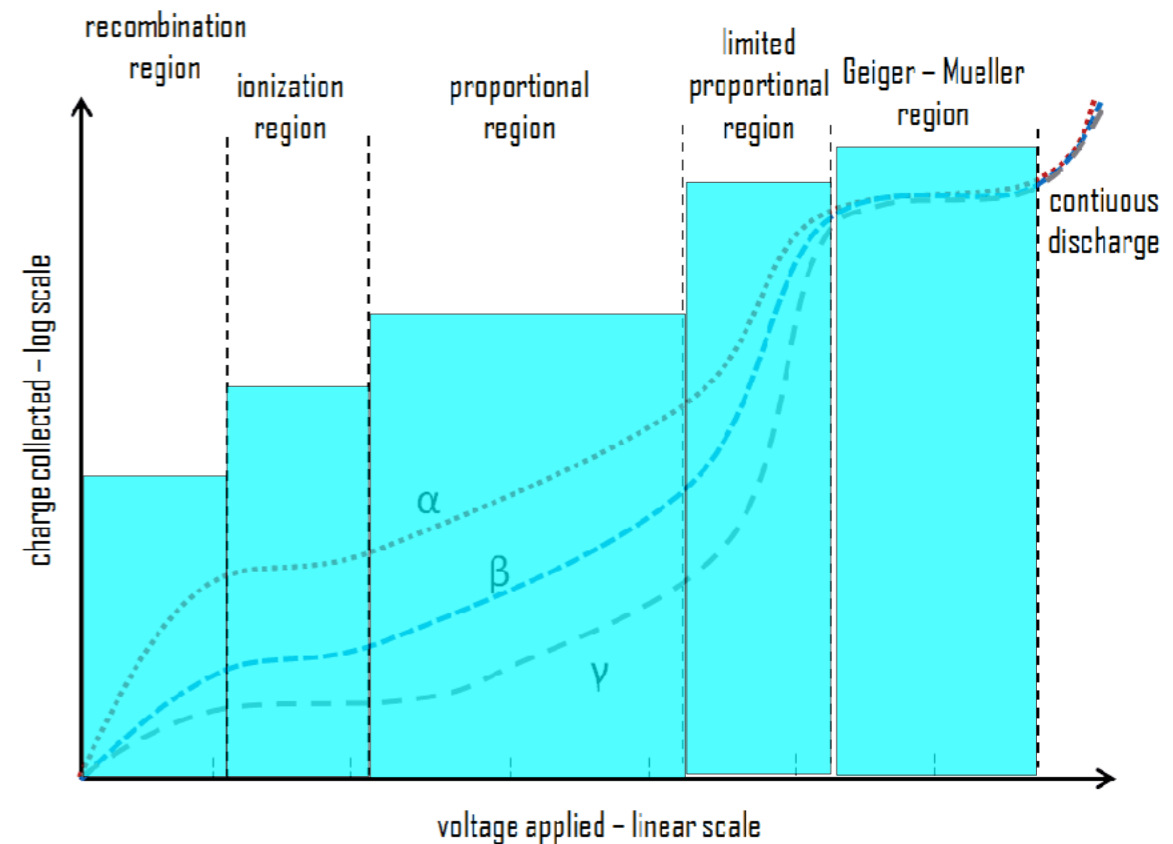
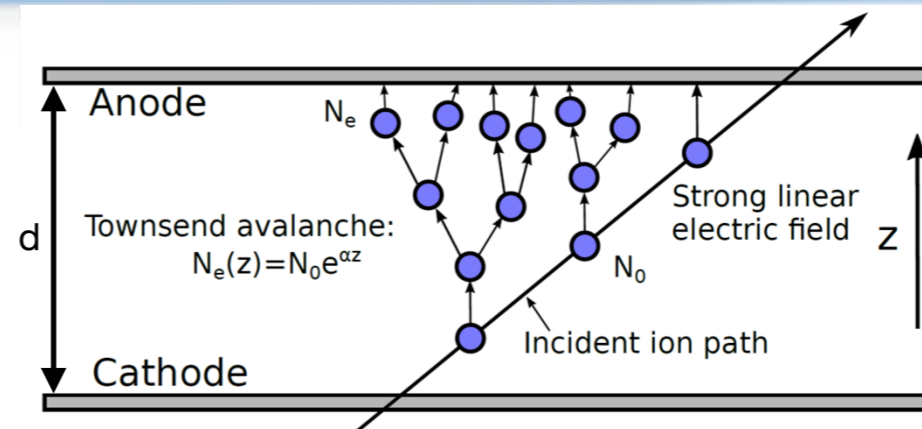


www.nuclear-power.net

Gaseous detector (i)

Response as function of HV:

- $HT \ll 1$, recombinaison
- $HT \nearrow$, ionisation, without secondary process
- $HT \nearrow \nearrow$, proportional, secondary ionisations, avalanche effect
- $HT \uparrow$, degraded proportional, creation of photo-electrons
- $HT \gg 1$, geiger-streamer mode, presence of important space-charge effects.



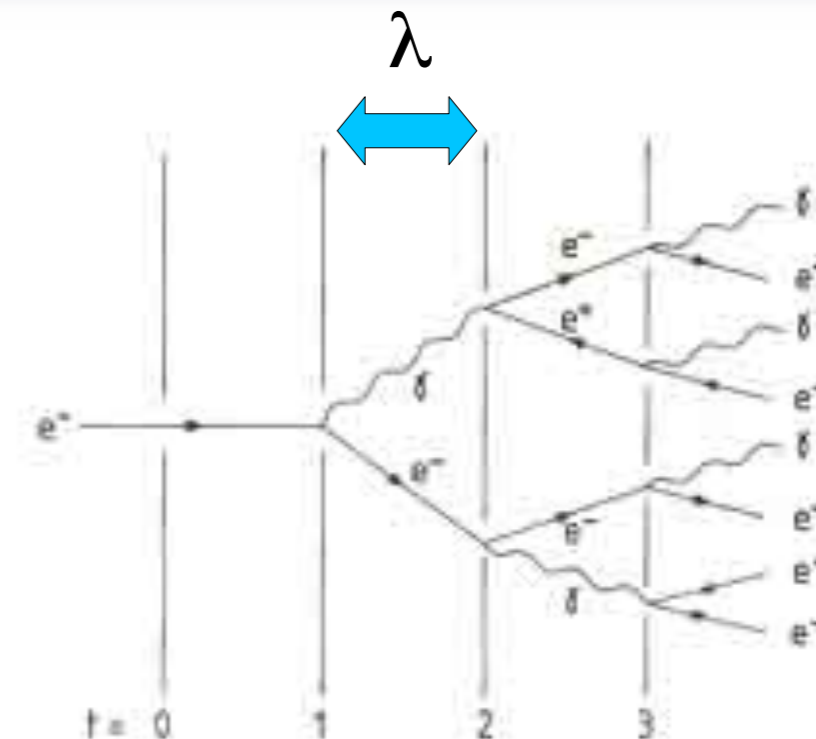
Gaseous detector (ii)

□ Primary ionisation:

- Probability to have n pairs of e^- -ion created for μ_0 ionisations created in gap d ($\mu_0 = d/\lambda$):

$$P(\mu_0, n) = \frac{\mu_0^n e^{-\mu_0}}{n!}$$

- n_{int} : nb of interactions per length
- W_i : energy to create a pair



- λ : mean free path btw 2 interactions

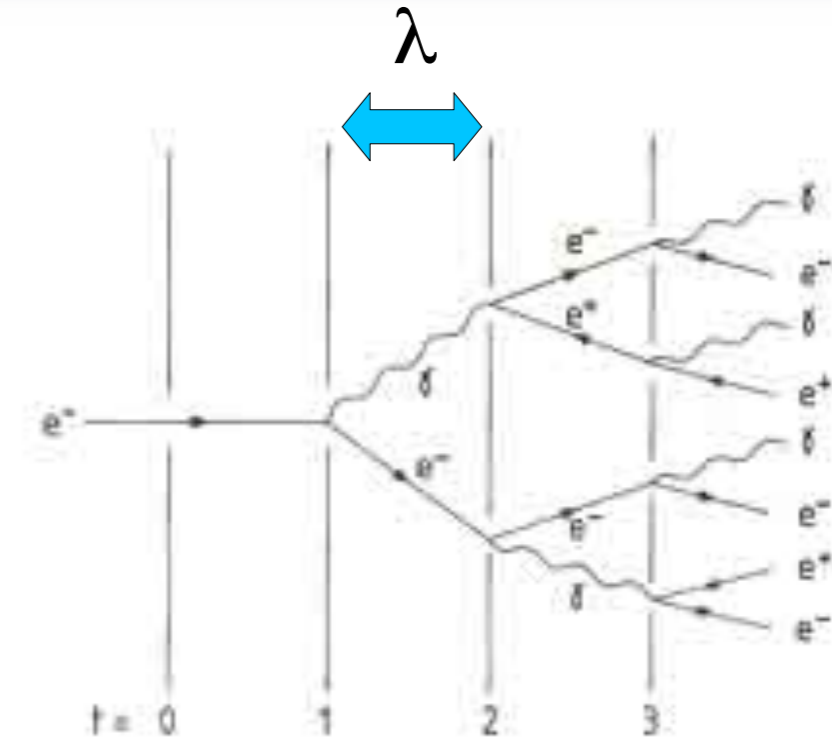
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Gas	formule	Z	n_{int} (cm^{-1})	W_i (eV)	ΔE (keV/cm)
Iso-butane	C_4H_{10}	34	46	23	4.50
Carbone dioxyde	CO_2	22	34	33	3.01
Argon	Ar	18	30	26	2.44
Neon	Ne	10	12	36	1.41

F. Sauli. Principles of operation of multiwire proportional and drift chambers. CERN Internal Report, vol. 09, 1977.

Gaseous detector (iii)

Charge amplification:

- Gain: $G(E, p) = \exp \left[\int_0^d \alpha(E, x) dx \right]$

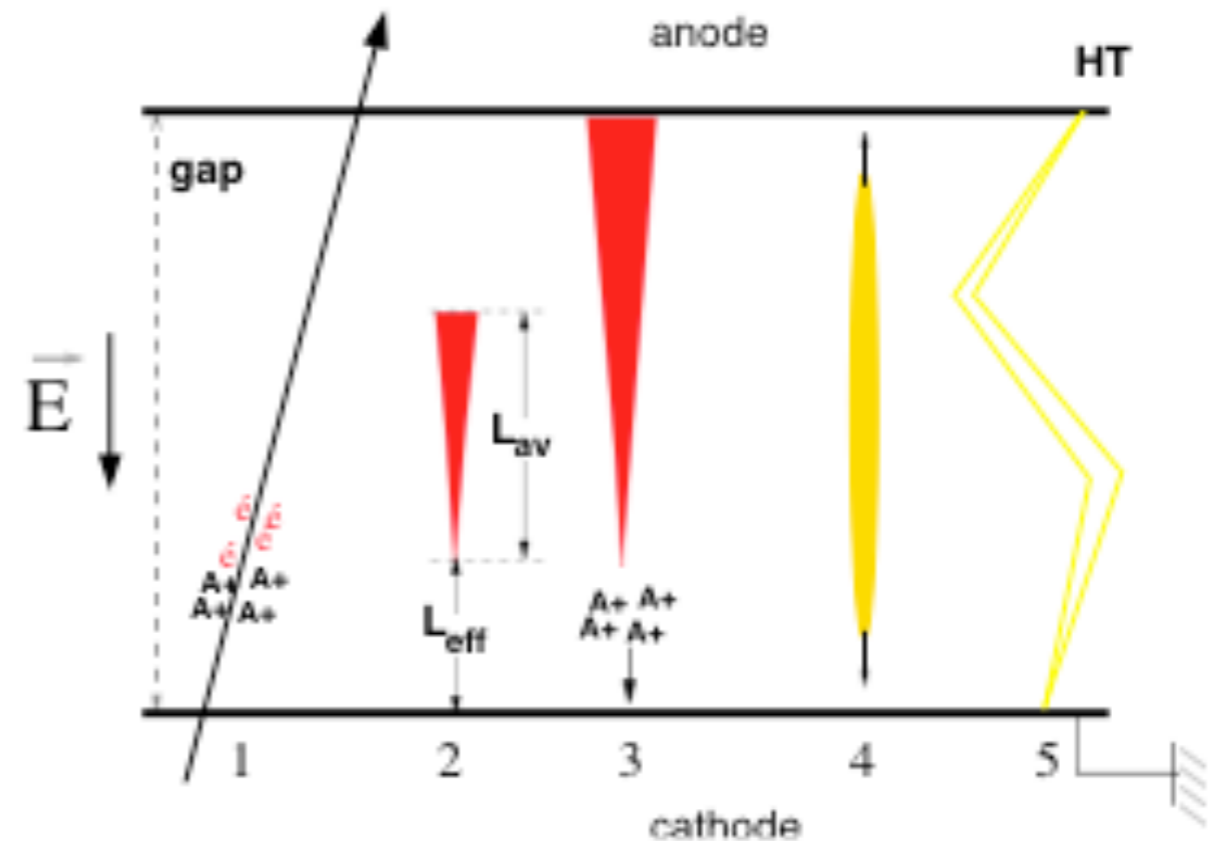
- Townsend coefficient: $\alpha = 1/\lambda$

- Avalanche length:

$$L_{av} = \frac{N_\lambda}{\alpha}$$

- Gap et E constants:

- Gain: $G(E, p) = e^{(\alpha d)}$



Gaseous detector (iv)

Charge mobility:

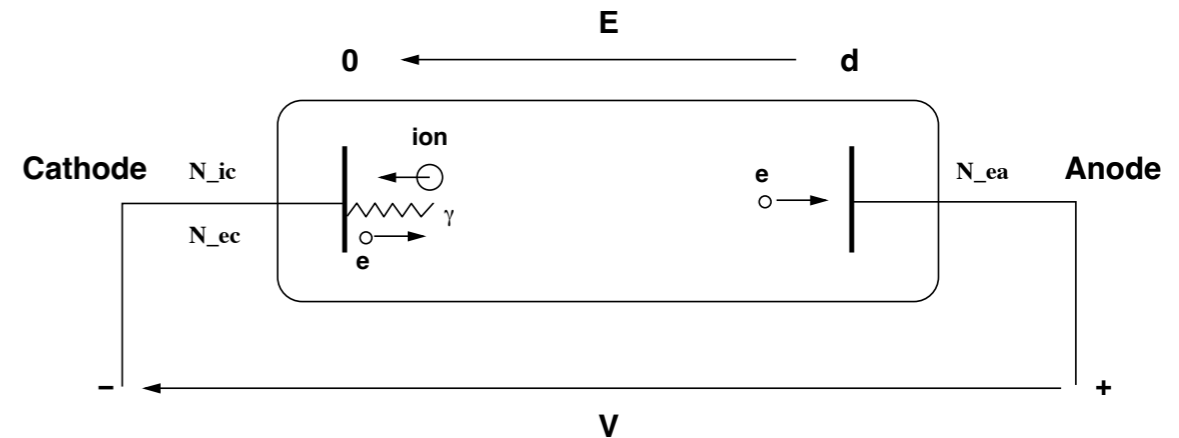
- Definition: $\vec{v} = \mu \vec{F}$ where $\vec{F} = e \vec{E}$ (electric field)

- Electrons:

$$\mu_e = \frac{e}{2m_e} E \times \tau \text{ (where } \tau = \lambda/v \text{)}$$

- Ions:

$$\mu_{ion} = \frac{v}{E}$$



Gas	Ion	Mobility ($cm^2/V/s$)
Neon	Ne^+	4.14
Argon	Ar^+	1.53
Carbone dioxyde	$[CO_2]^+$	1.09

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➔ Mobility of $\mu^e \sim 10\text{-}100$ times greater than μ^{ion}

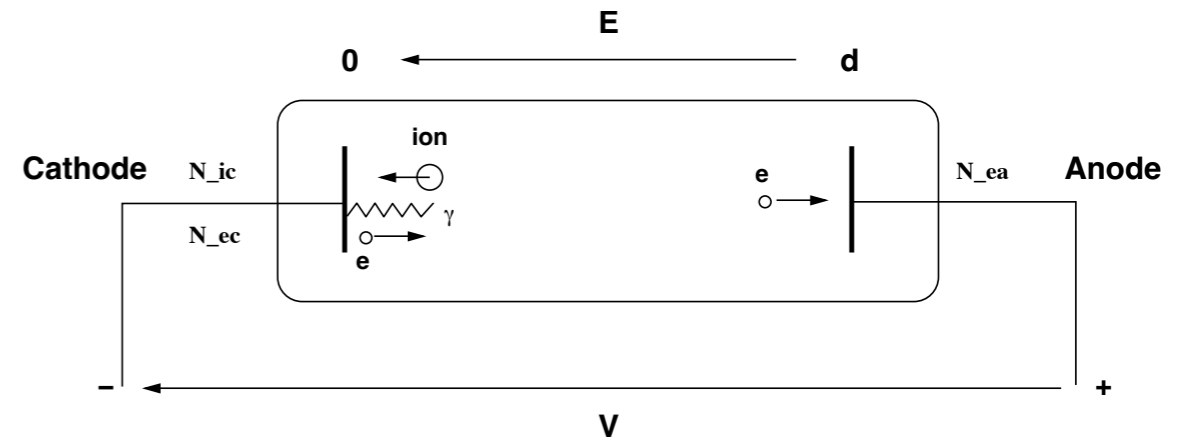
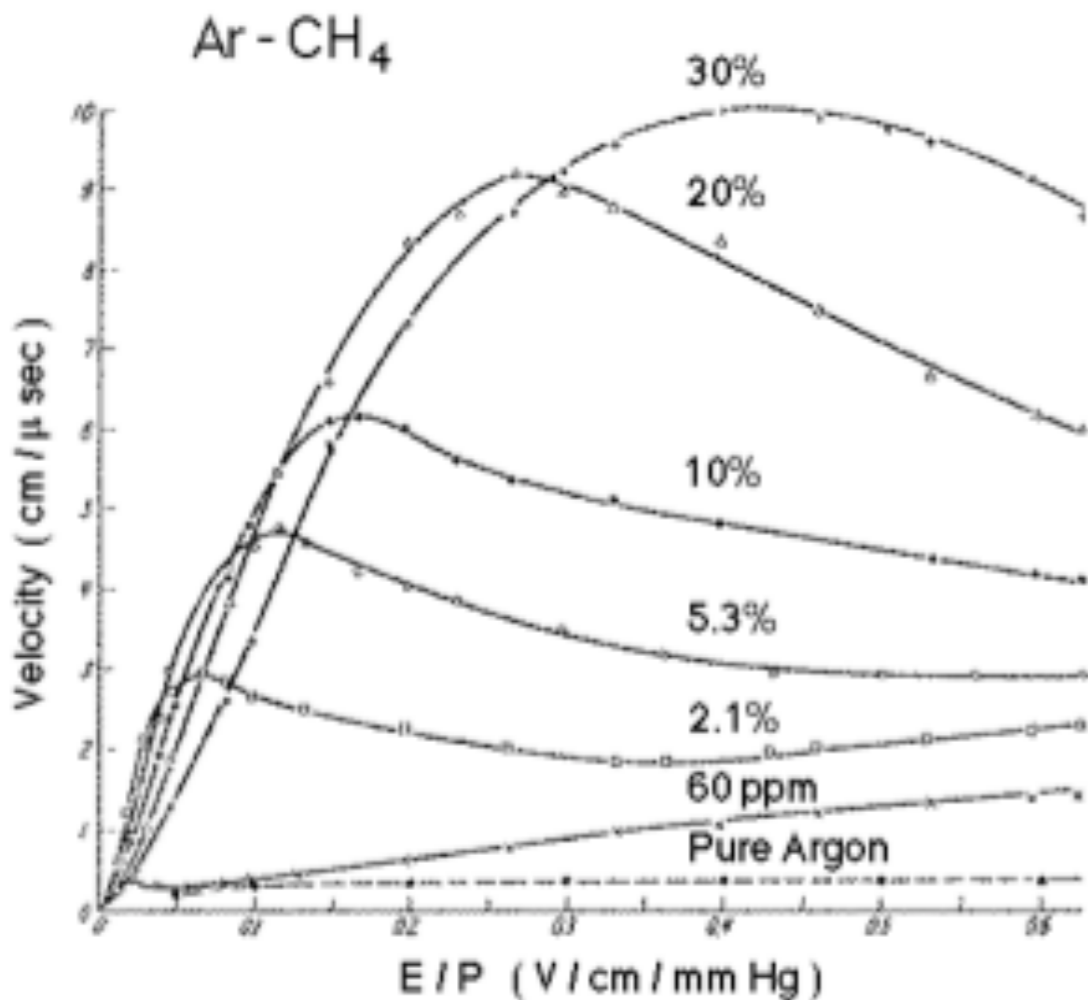
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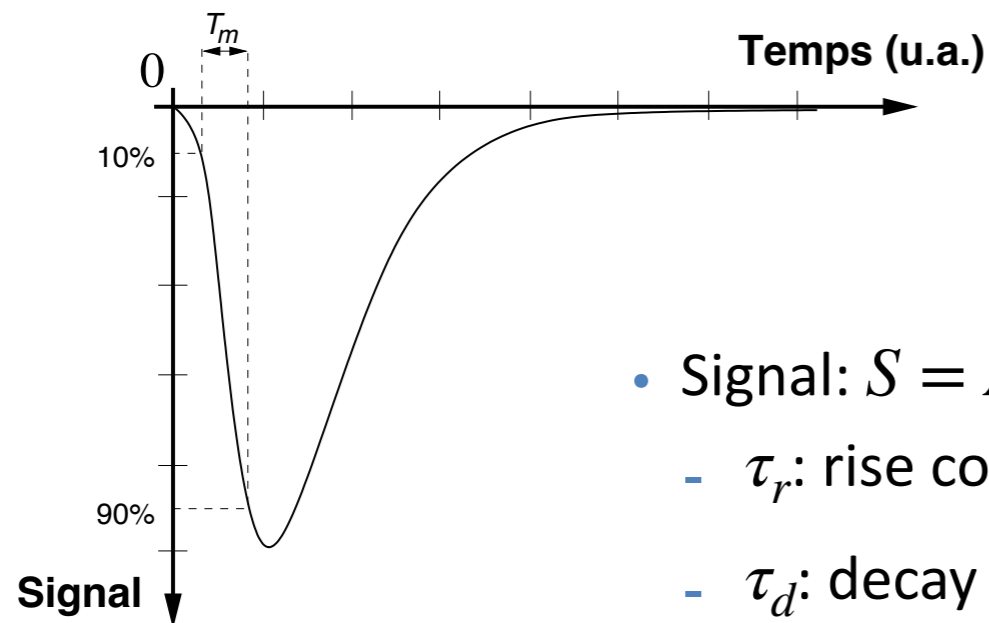
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➔ Mobility of μ^e ~10-100 times greater than μ^{ion}

Gaseous detector (v)

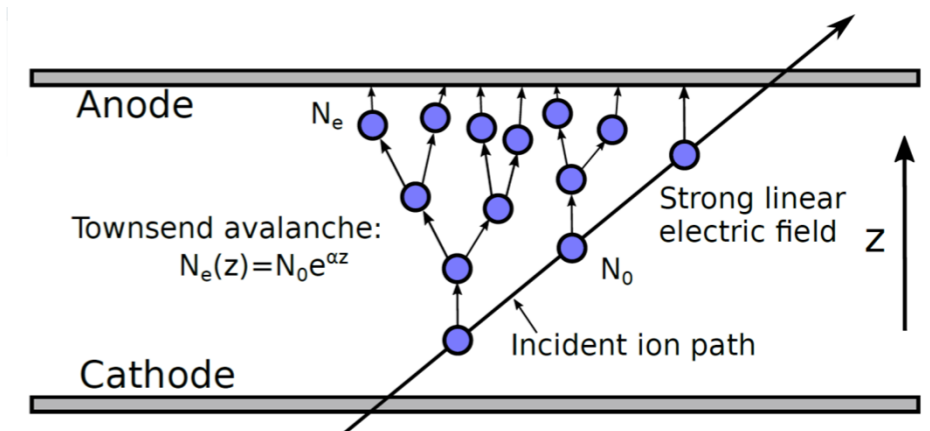
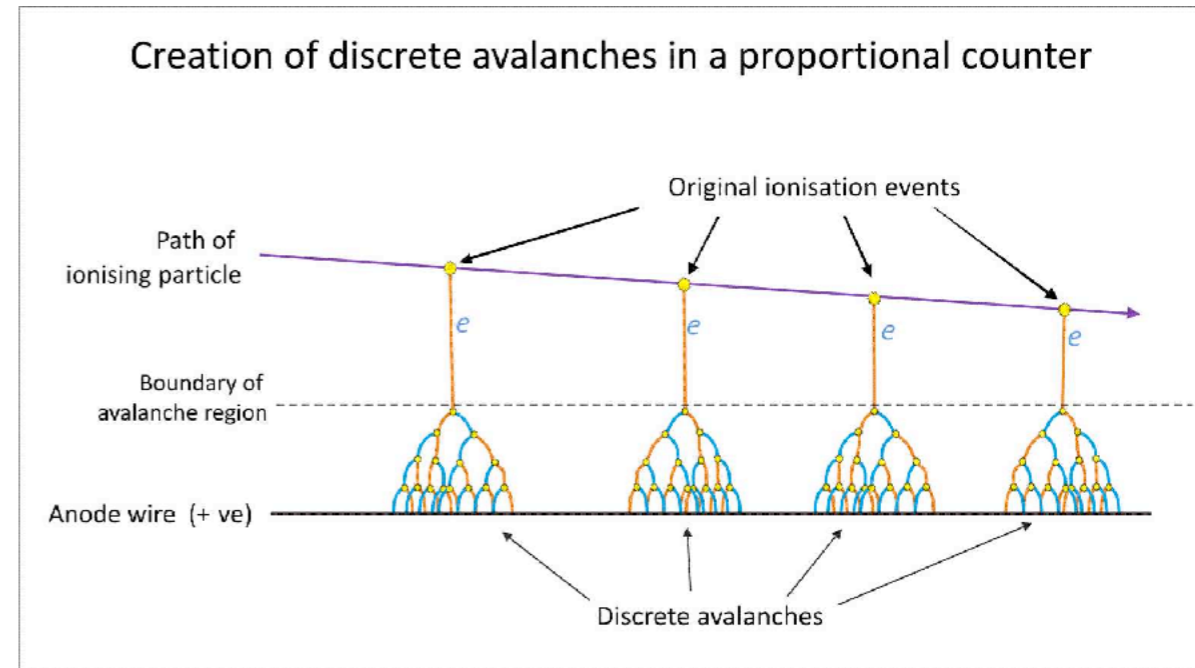
Collected charge

- Shape:
 - Rise time mostly induced by electron movement
 - Fall time mostly due to ion movement



- Signal: $S = Ae^{-\tau_r} \times Be^{\tau_d}$
 - τ_r : rise constant
 - τ_d : decay constant

- Total charge: $Q_{tot} = -e\mu_0e^{(\alpha d)}$



Scintillator (i)

□ Properties:

- Principle:

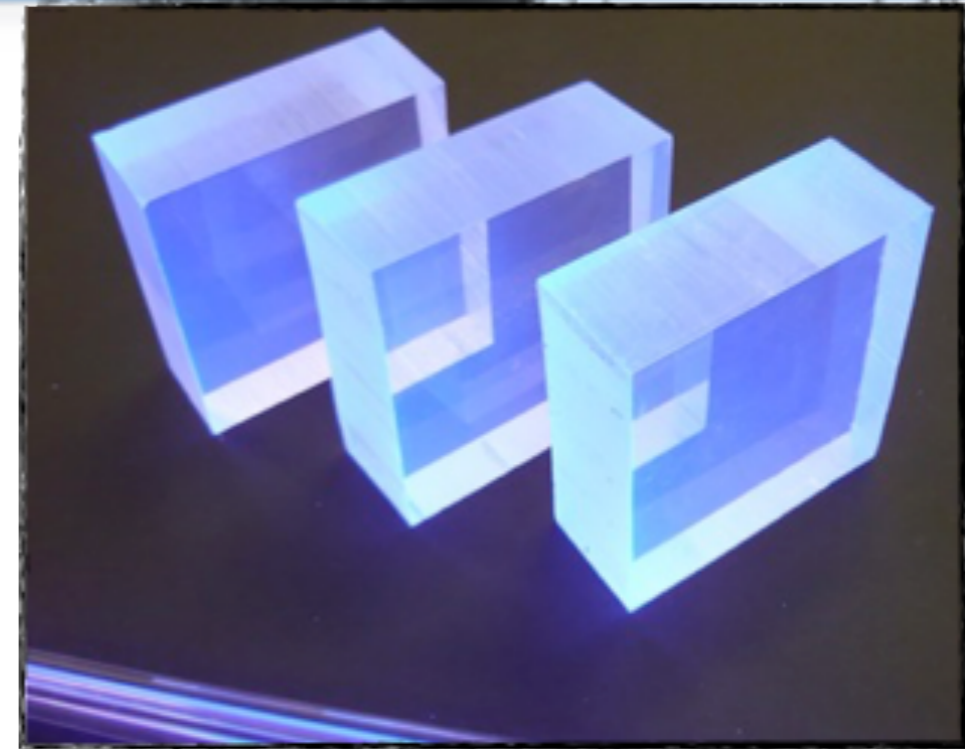
- dE/dx converted into light
- Detection via photosensor (e.g. photomultiplier, ...)

- Main Features:

- Sensitivity to energy
- Fast time response (rise time < 10 ns decay time $<$ few 100 ns)
- Pulse shape discrimination

- Requirements:

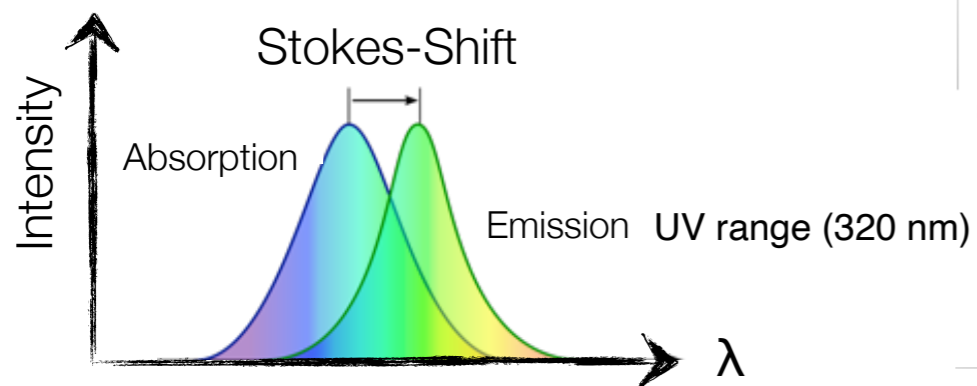
- **High efficiency** for conversion of exciting energy to fluorescent radiation
- **Transparency** to its fluorescent radiation to allow transmission of light
- **Emission of light** in a spectral range detectable for photosensors



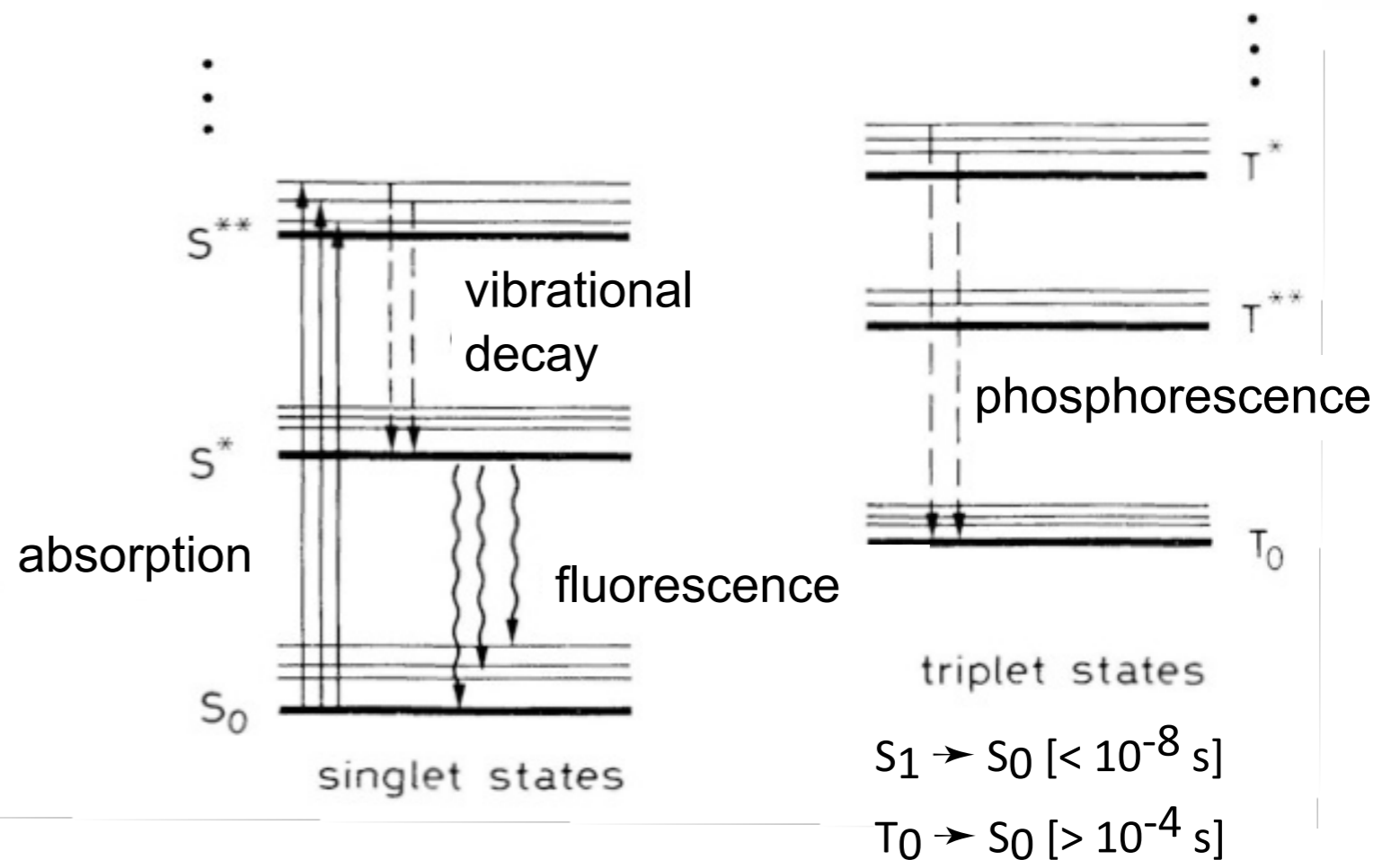
Scintillator (ii)

Organic scintillator (contains C):

- Mechanism:
 - Singlet molecular states
 - Triplet molecular states
- Emission/absorption spectrum :



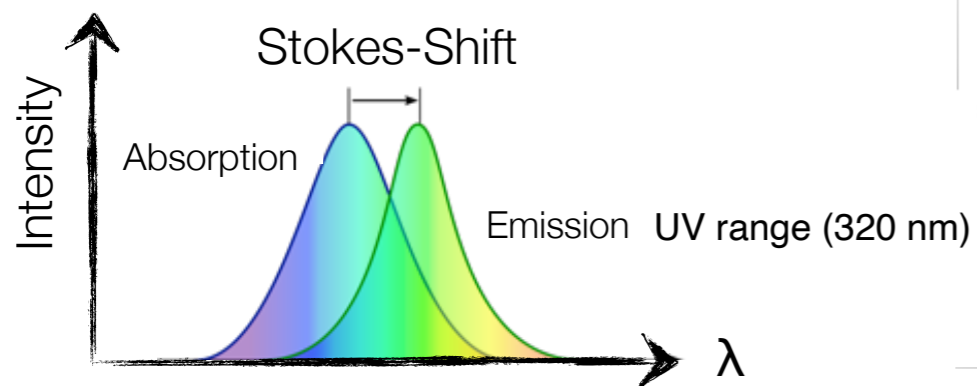
→ Transparent to its own light



Scintillator (ii)

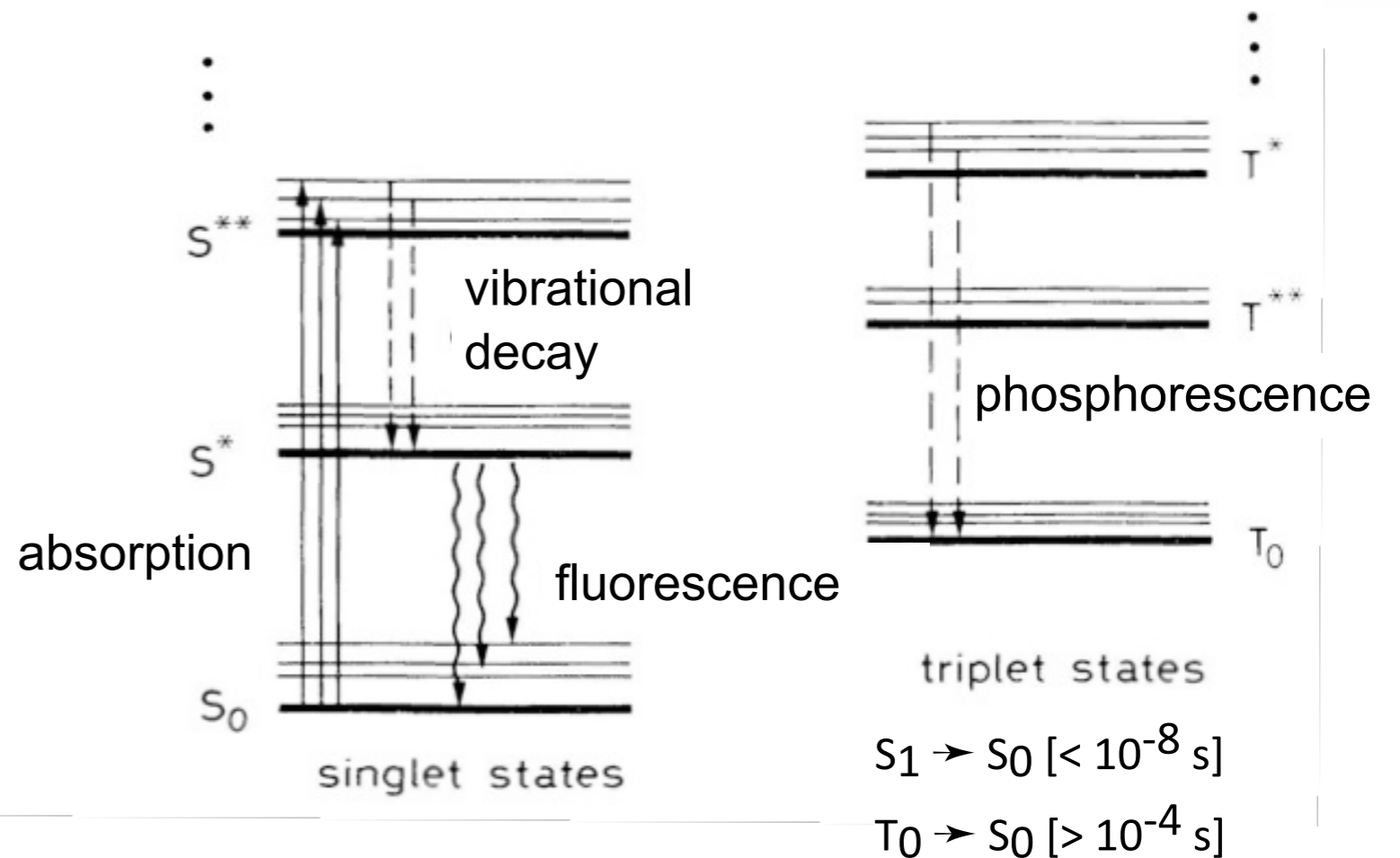
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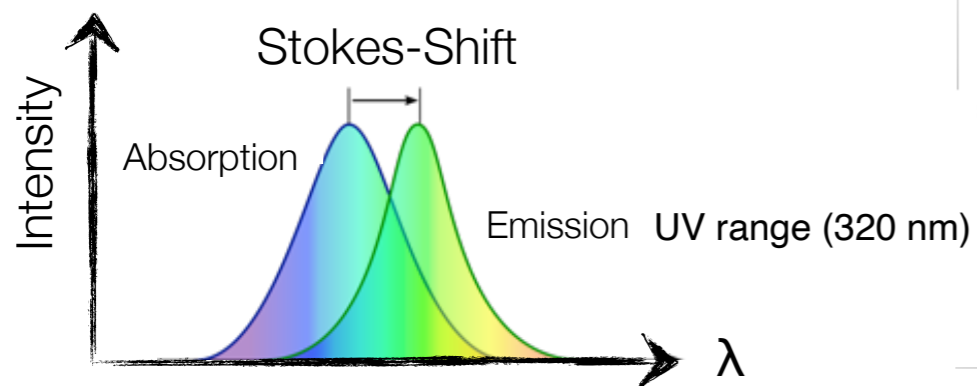
- Examples:
 - Anthracene ($C_{14}H_{10}$)
 - EJXXX ($C_{9}H_{10}$)
 - Etc...



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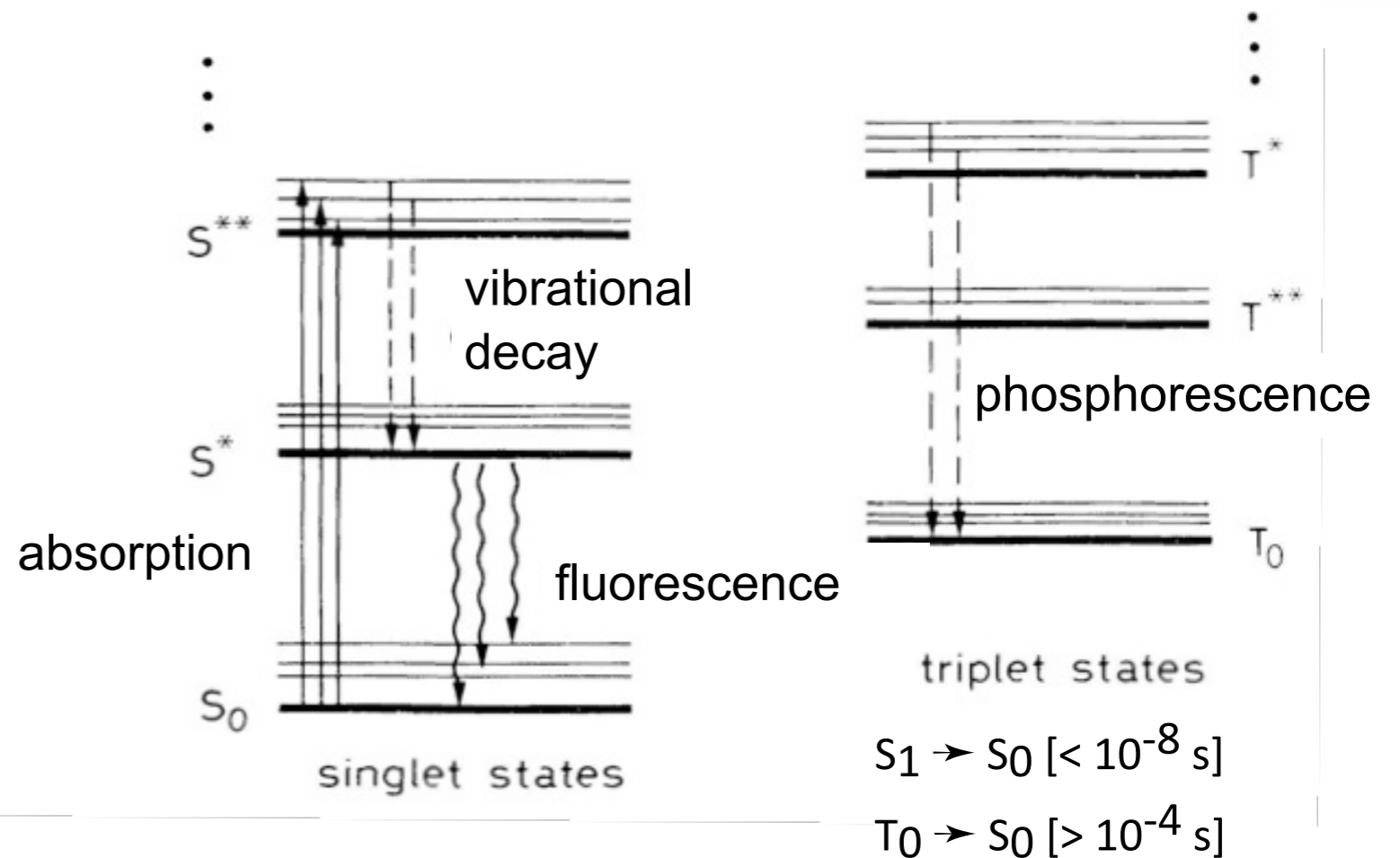
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Fast timing:

- Rise time $\ll 1$ ns
- Signal length < 2 ns

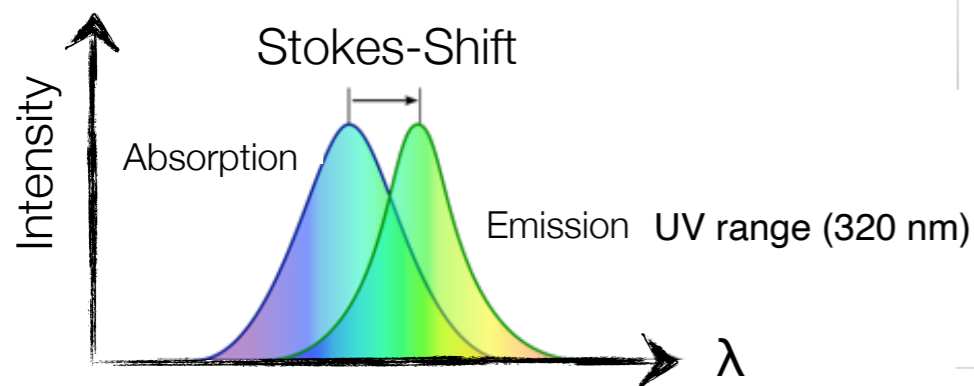
➔ Use for time measurements



Scintillator (ii)

Organic scintillator (contains C):

- Mechanism:
 - Singlet molecular states
 - Triplet molecular states
- Emission/absorption spectrum :



➔ Transparent to its own light

Examples:

- Anthracene ($C_{14}H_{10}$)
- EJXXX (C_9H_{10})
- Etc...

Fast timing:

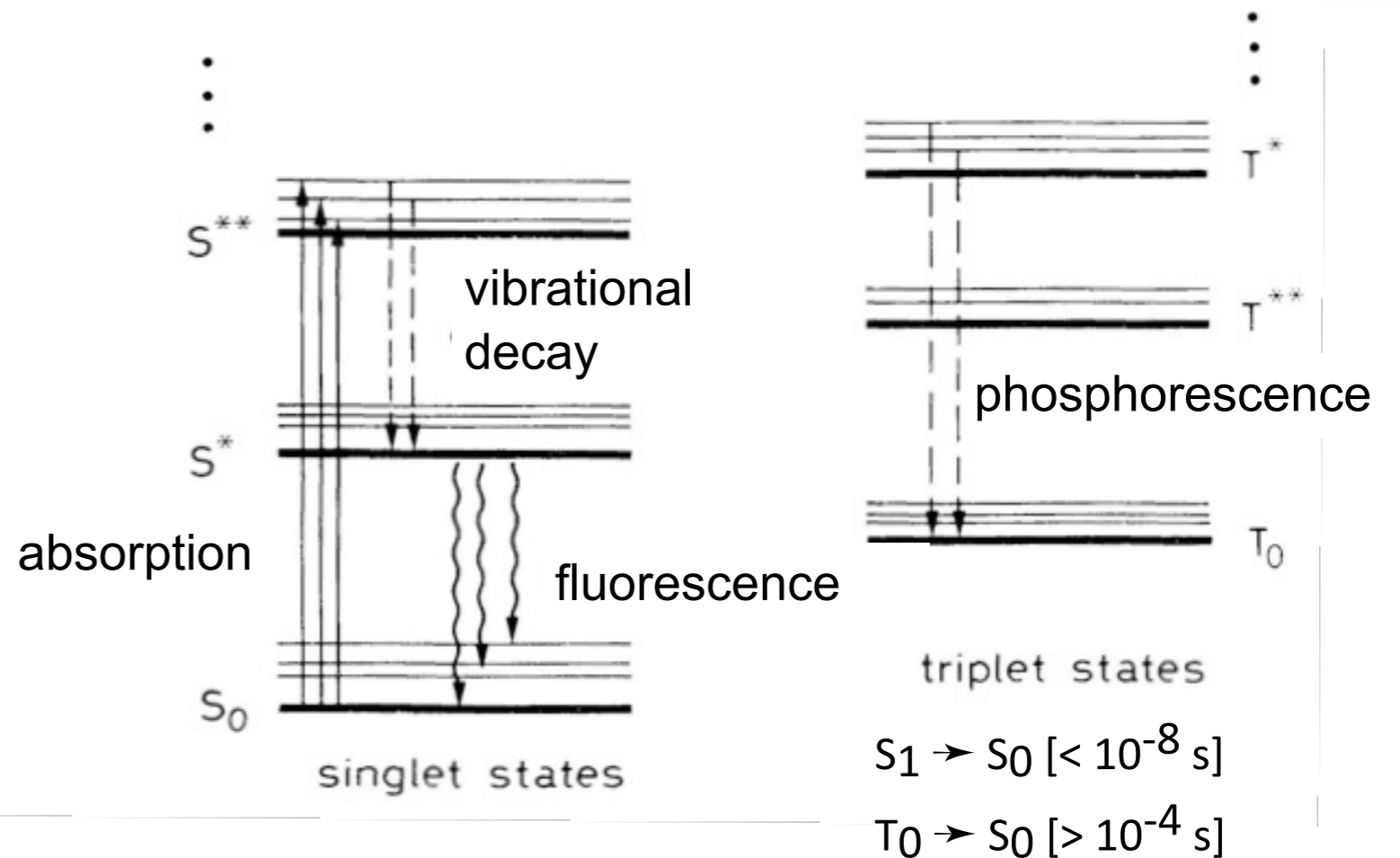
- Rise time $\ll 1$ ns
- Signal length < 2 ns

➔ Use for time measurements

Low light yield

- < 20 photons/keV

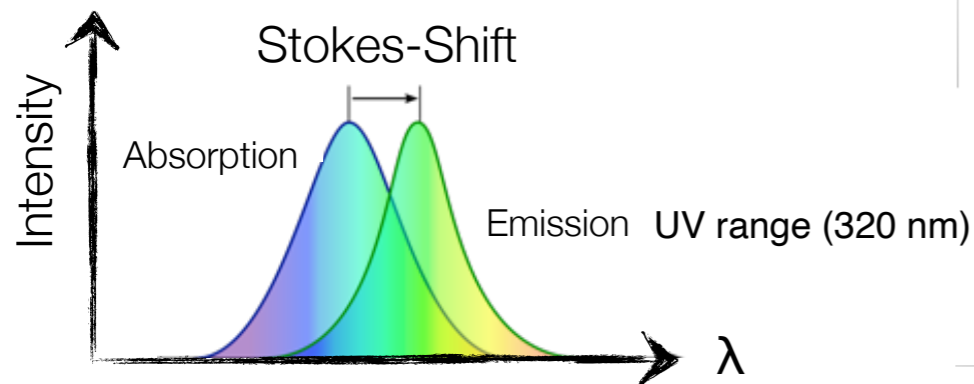
➔ Not suited for E measurements



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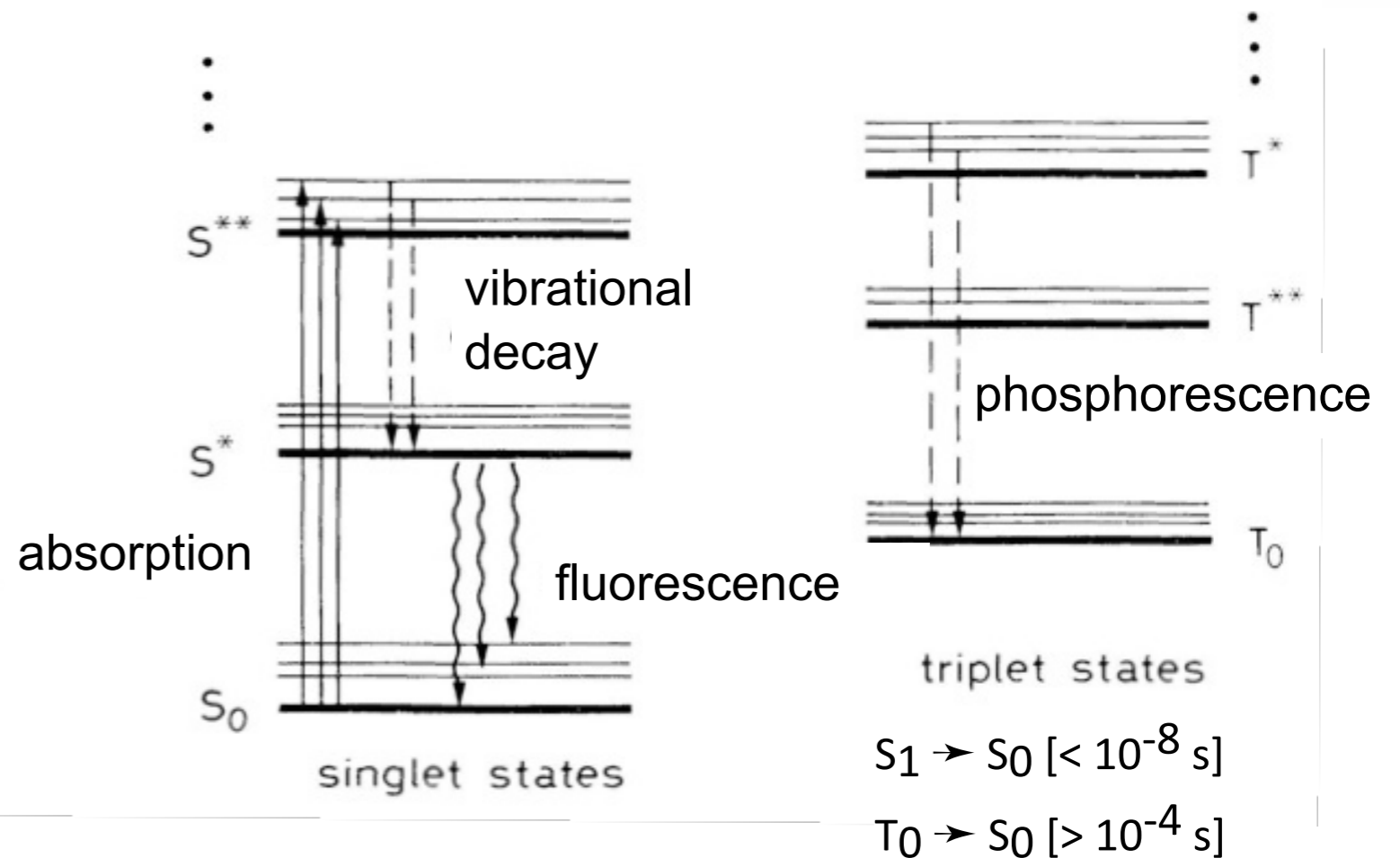
➔ Use for time measurements

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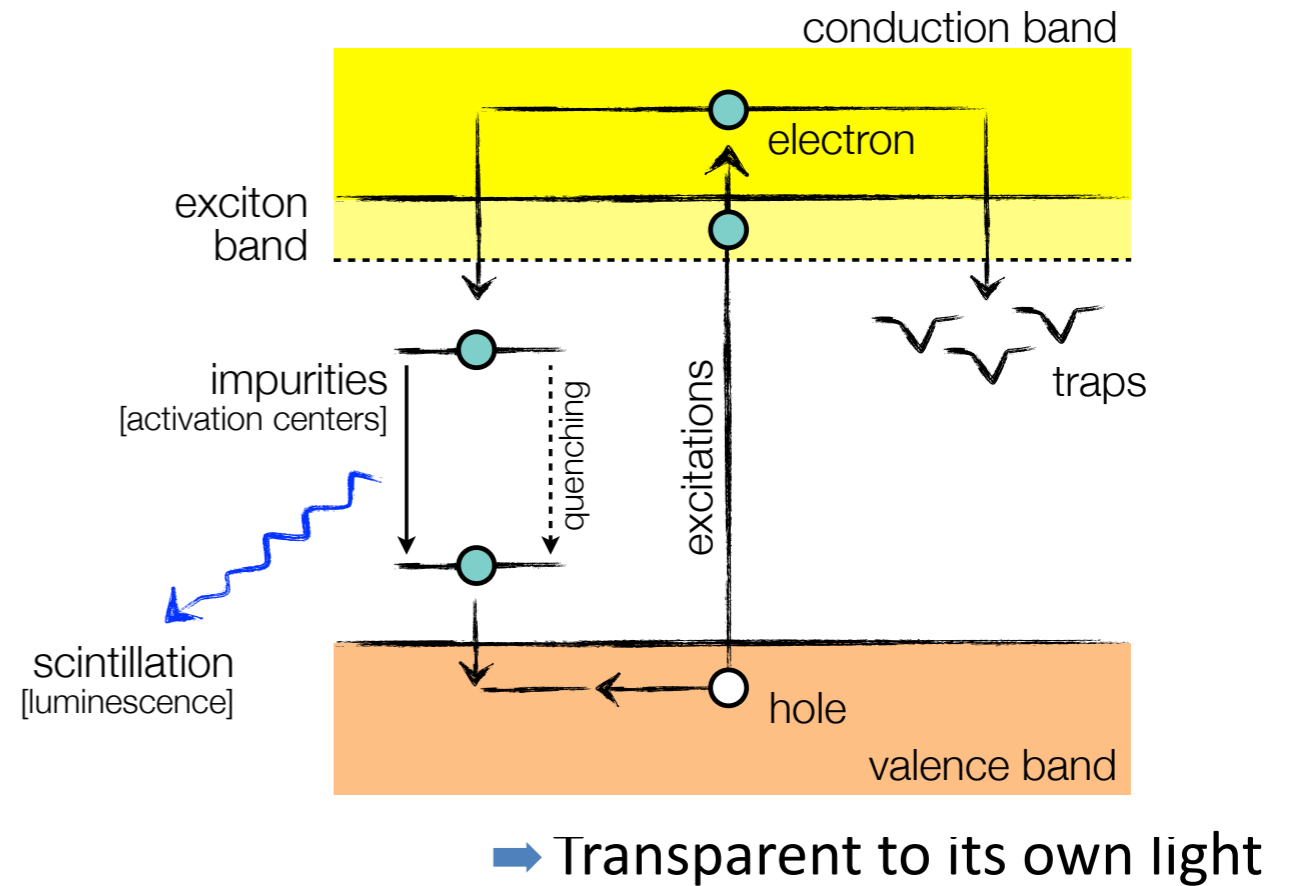
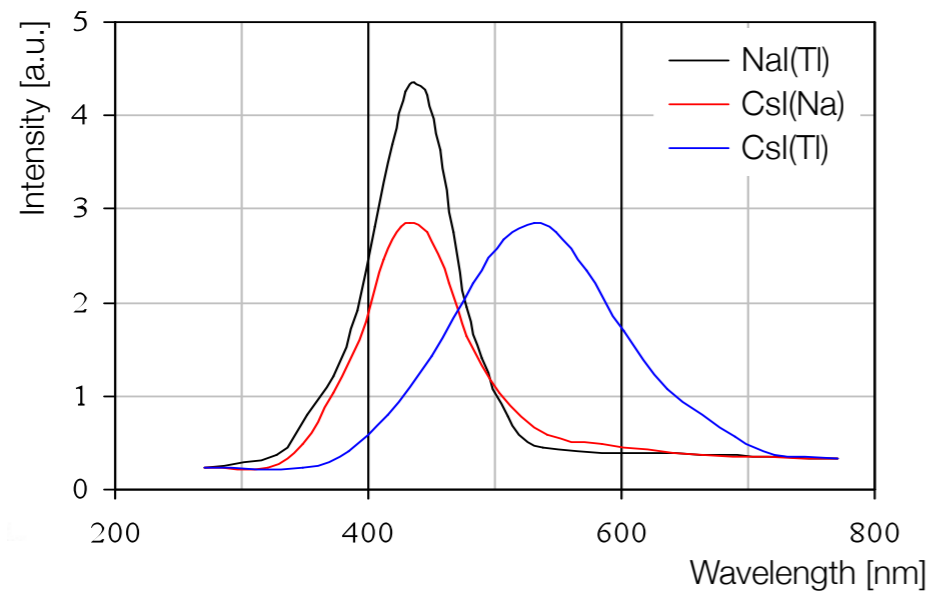
➔ Cheap and easy to produce



Scintillator (iii)

□ Inorganic scintillator (i):

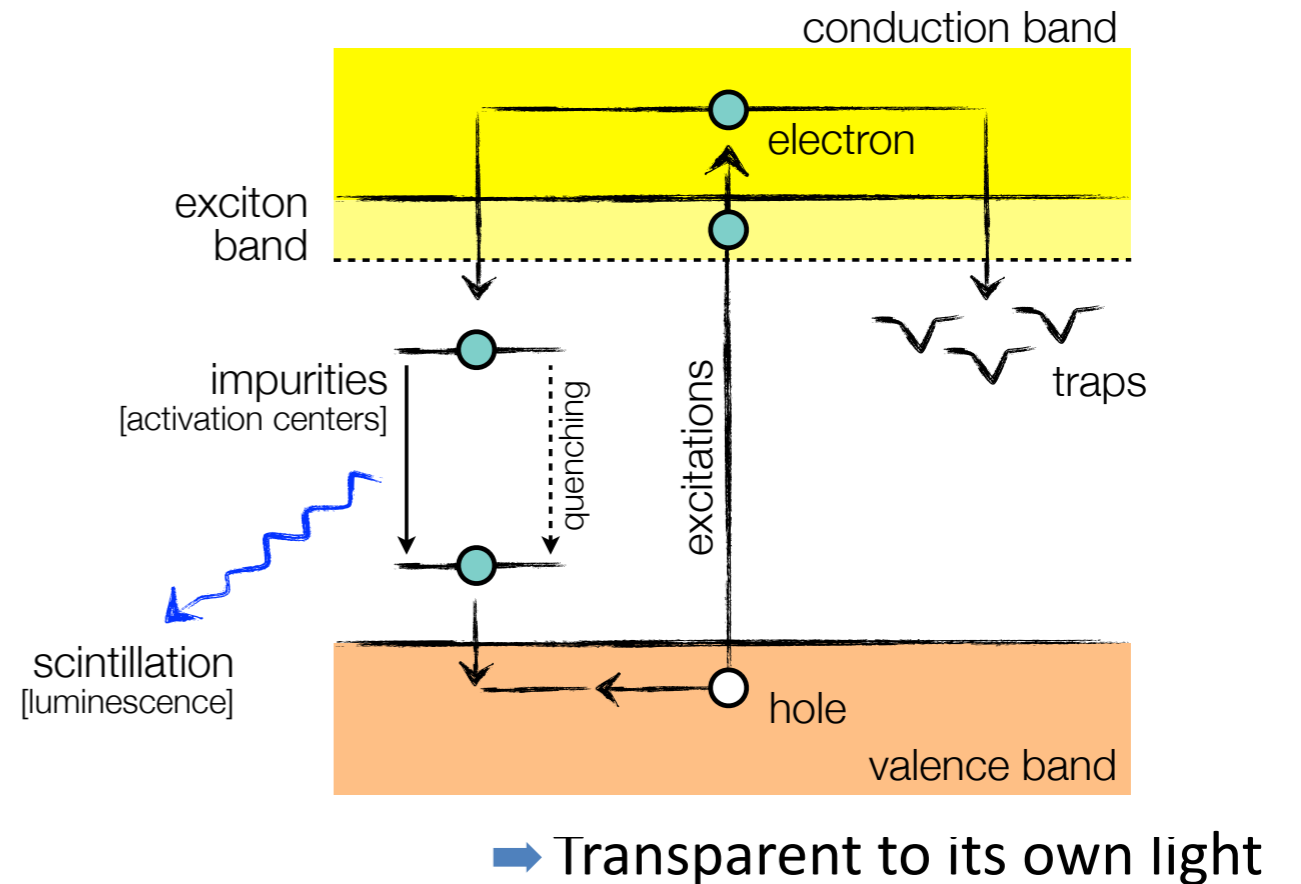
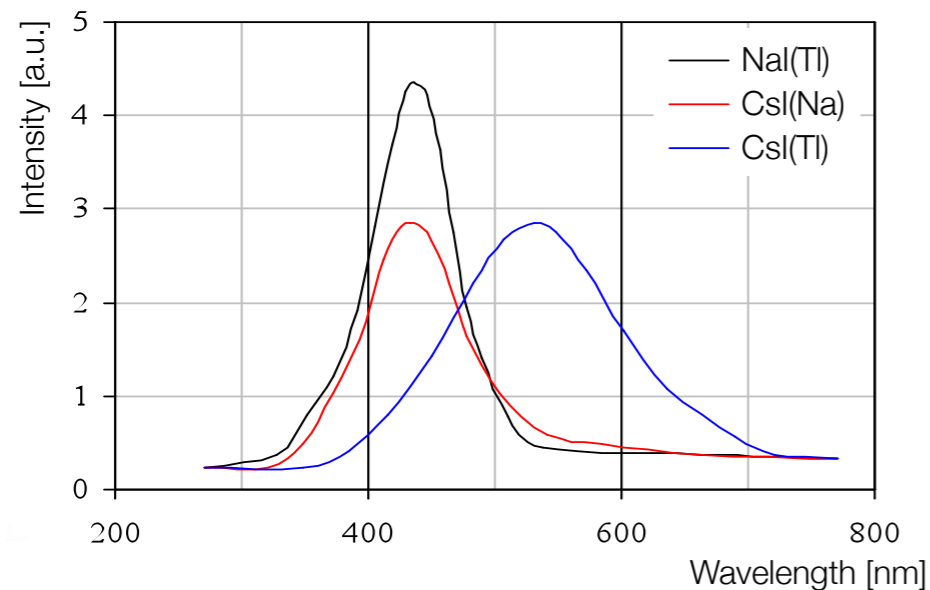
- Mechanism:
 - Energy deposition by ionisation
 - Energy transfer to impurities
 - Radiation of scintillation photons
- Emission/absorption spectrum (visible):



Scintillator (iii)

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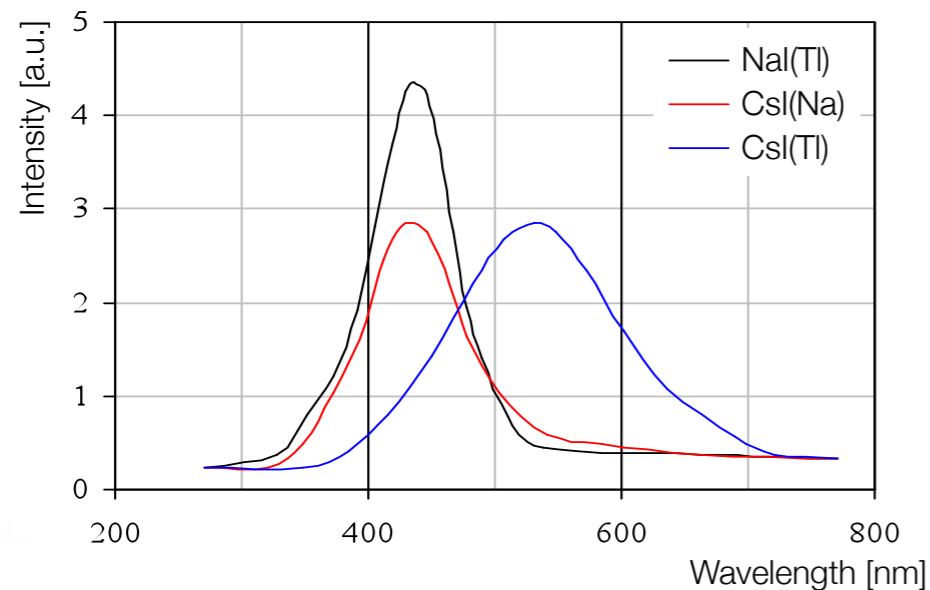


- High light yield
 - > 30-80 photons/keV
- ➔ Use for E measurements

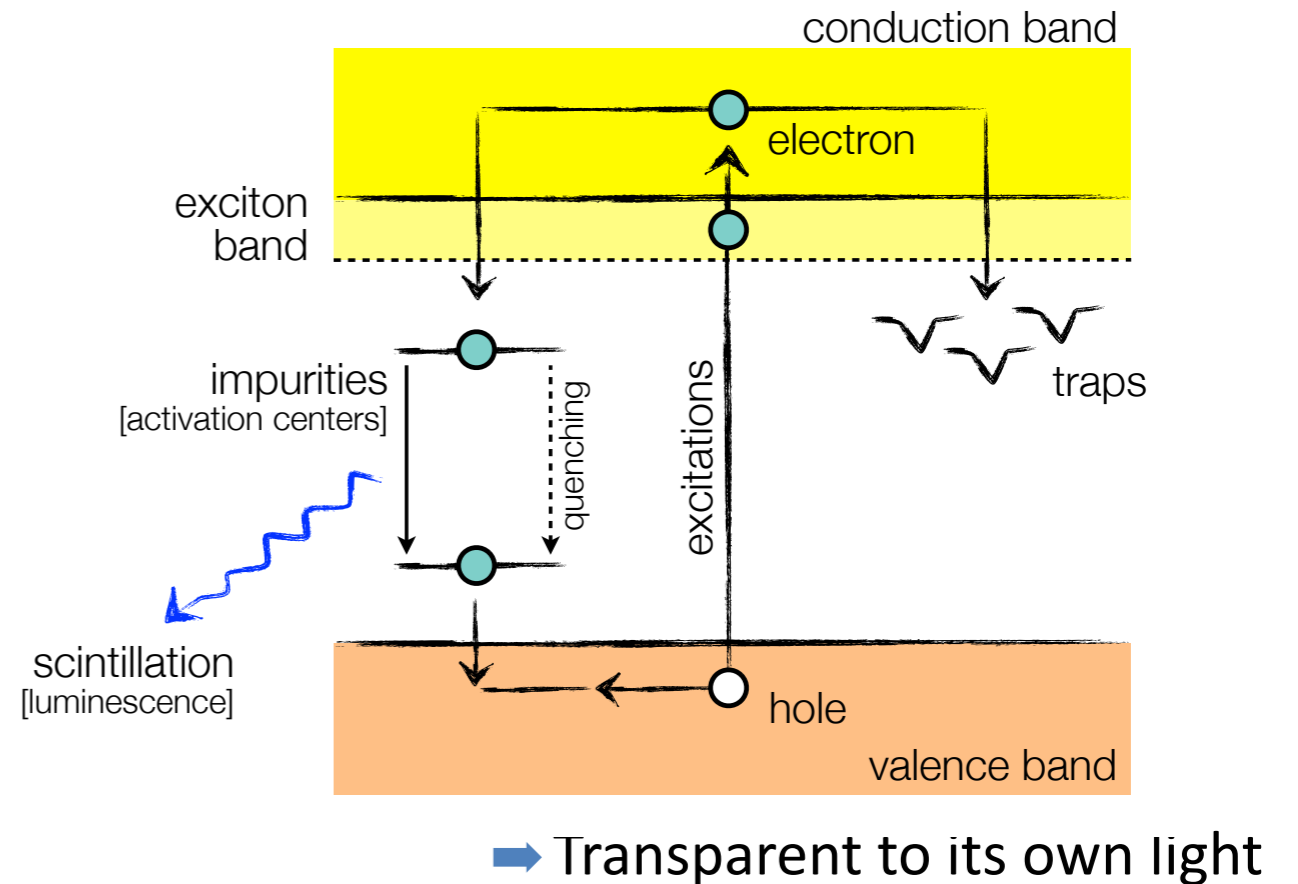
Scintillator (iii)

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- Mechanism:
 - Energy deposition by ionisation
 - Energy transfer to impurities
 - Radiation of scintillation photons
- Emission/absorption spectrum (visible):



- High light yield
 - > 30-80 photons/keV
- ➔ Use for E measurements



- Slow timing:
 - Rise time > 10 ns
 - Signal length > few 100 ns
- ➔ Not suited for time measurements

Scintillator (iv)

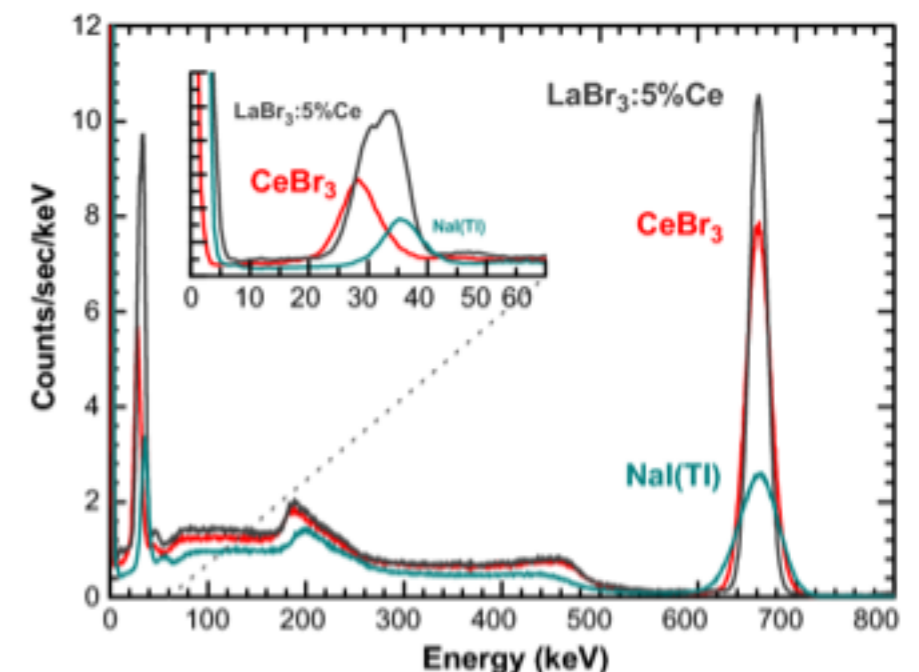
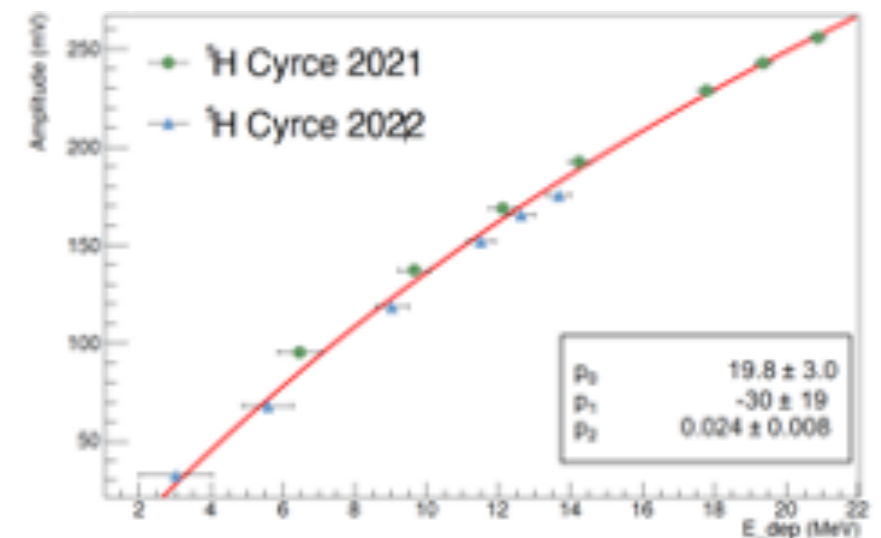
□ Inorganic scintillator (ii):

- Light production, Birk's Law:

$$\frac{dL}{dE} = L_0 \frac{\frac{dE}{dx}}{1 + k_B \frac{dE}{dx}} \text{ with } k_B \text{ Birk coefficient}$$

- Examples:

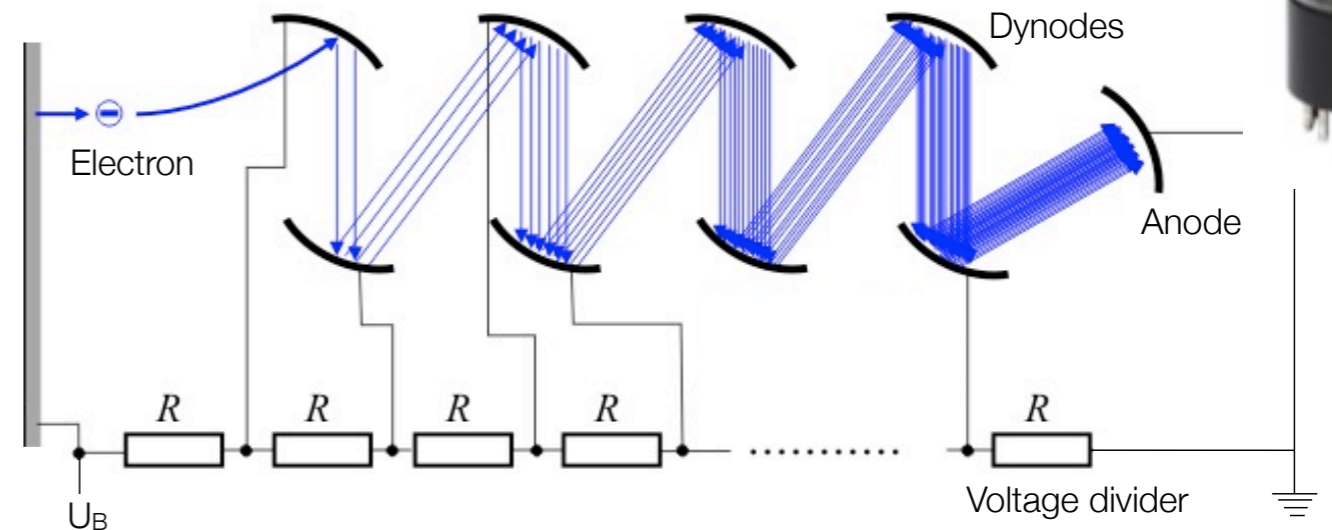
- **Sodium Iodide** (NaI): good photon yield, available in big volumes, cheap but hygroscopic.
- **Cesium Iodide** (CsI): better photon yield than NaI, but slow.
- **Baryum Fluoride** (BaF₂): fast timing (rise time $\ll 1$ ns), poor photon yield.
- **Bismuth Germanate** (BGO): highly efficient, but very slow (decay time : 300 ns), poor photon yield.
- **Lanthanum Bromide** (LaBr₃)/**Cerium Bromide** (CeBr₃): excellent photon yield, very fast (rise time ≈ 10 ns), but hygroscopic and expensive (+ lanthanum is radioactive).



Scintillator (v)

□ Scintillator coupling (need to convert photon to signal):

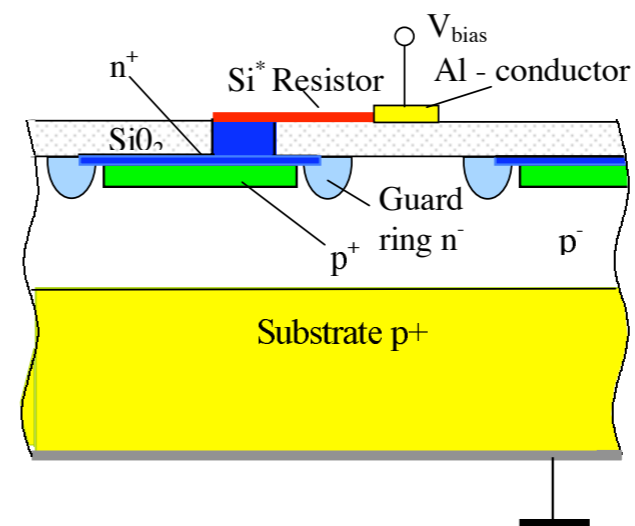
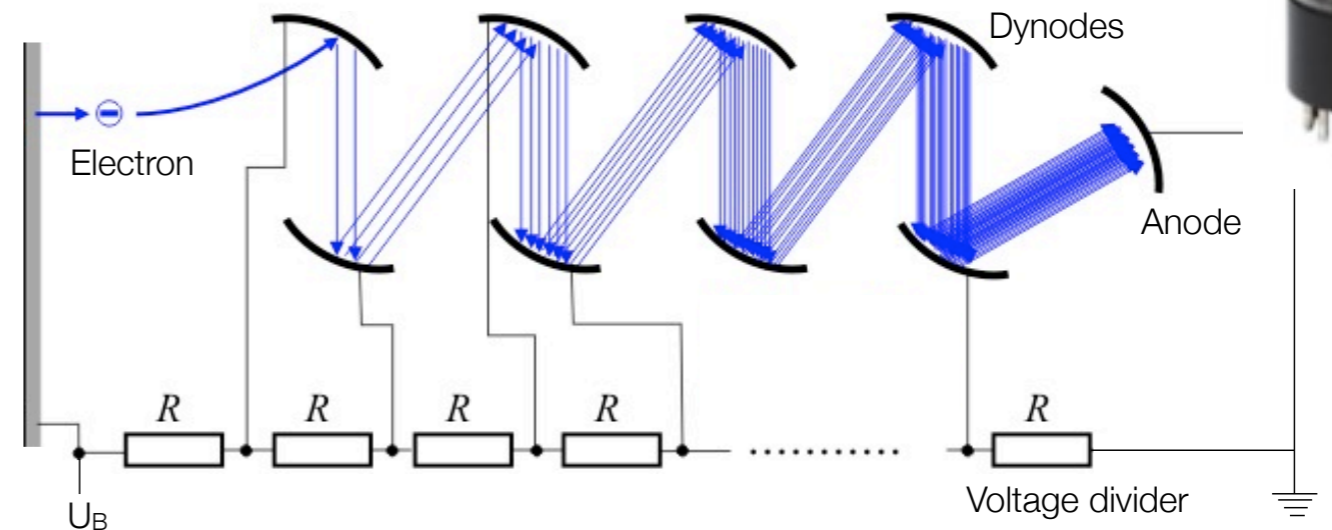
- Photomultiplier: (most used)
 - Photon converted in e- by photocathode (photoelectric effect)
 - Amplification of signal by set of dynodes
 - Efficiency \propto length wave
 - Quantum efficiency (e- emitted by a incident photon) at most 25%.
 - Gain: $A = \delta^n$, n number of dynodes ar
dynode emission coefficient: $\sim 10^6$ - 10^8
 - HV: 1-2 kV



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 - HV: 1-2 kV
- Silicon photomultiplier (APD, SiPM, ...):
 - Gain: $\sim 10^6$
 - HV: < 100 V
 - Not sensitive to magnetic field
 - Sensitive to temperature



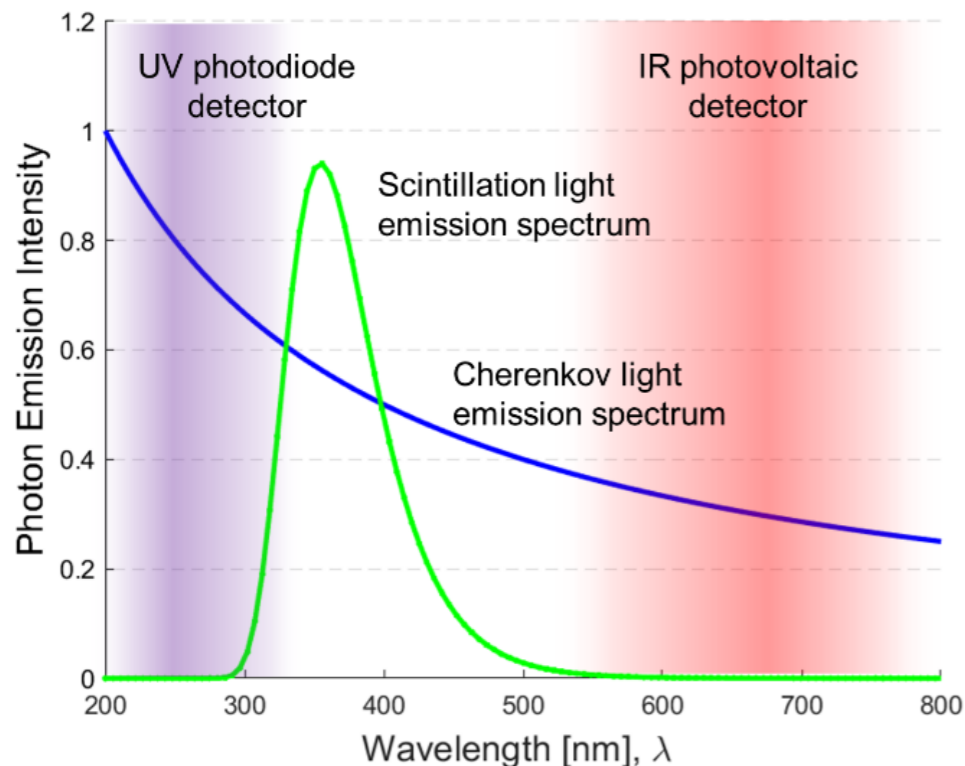
Scintillator (vi)

Cherenkov light in scintillator

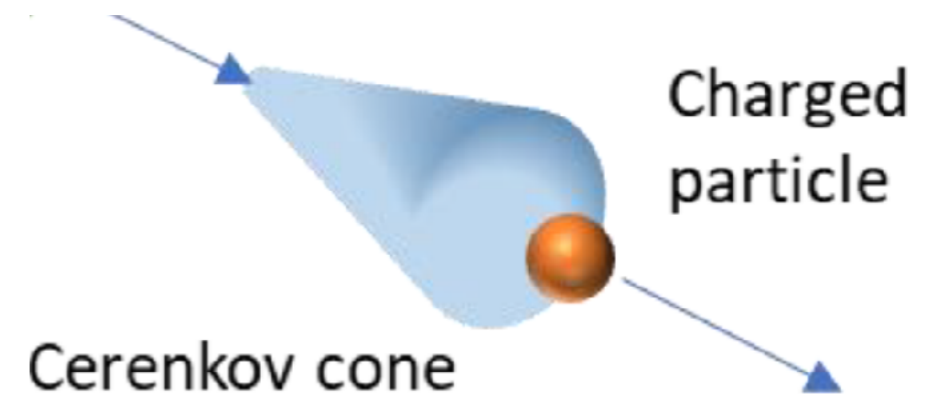
- Cherenkov radiation:
 - Happens when a particle velocity $\beta >$ light speed in material

- Light cone appears: $\cos(\theta) = \frac{1}{\beta n}$ where n is the

refraction index



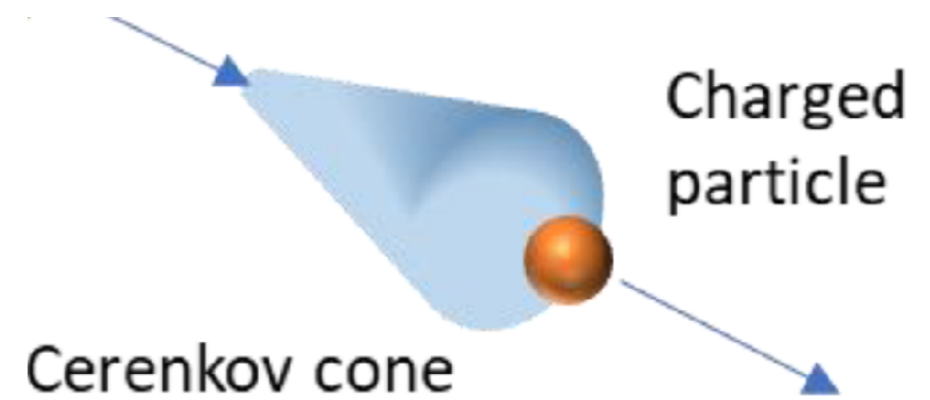
Junghyun Bae¹ et al., School of Nuclear Engineering, Purdue University, IN 47906



Scintillator (vi)

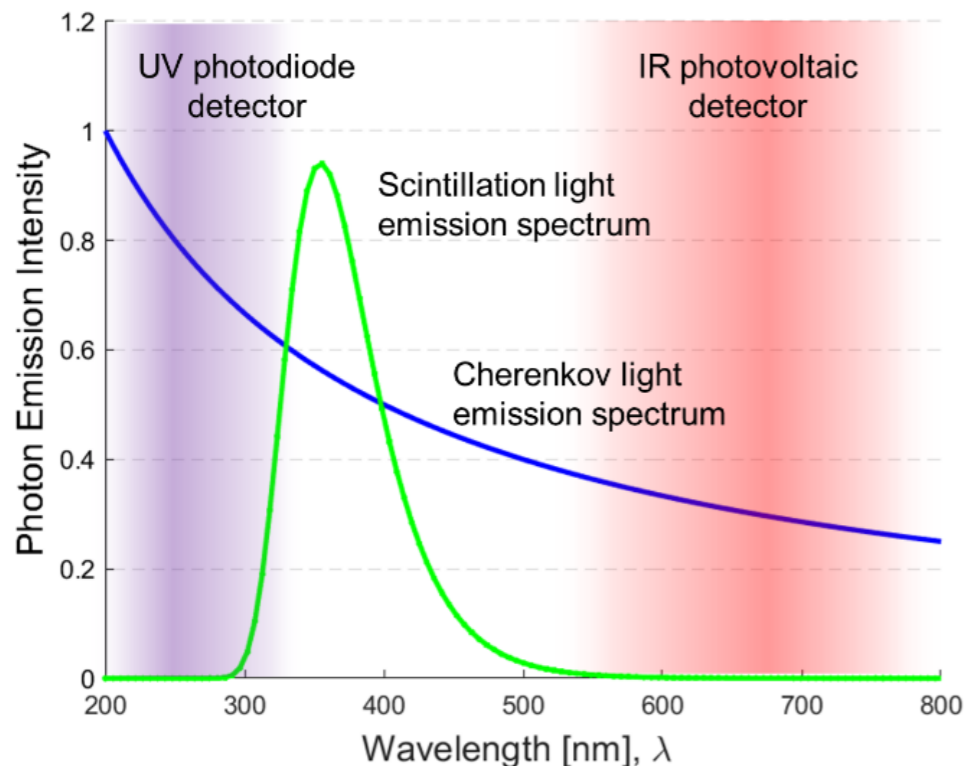
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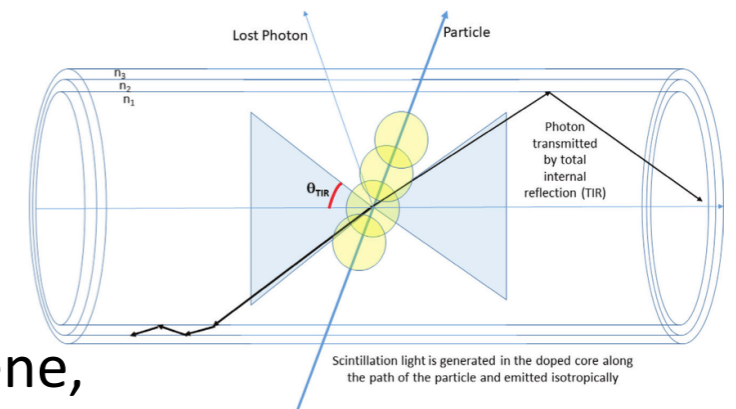
Light cone appears: $\cos(\theta) = \frac{1}{\beta n}$ where n is the

refraction index



Scintillating fiber

- Core: mainly polystyrene,
- Cladding: PMMA, plastic, ...
- Very thin diameter could < 0.5 mm
- Flexible



Junghyun Bae¹ et al., School of Nuclear Engineering, Purdue University, IN 47906

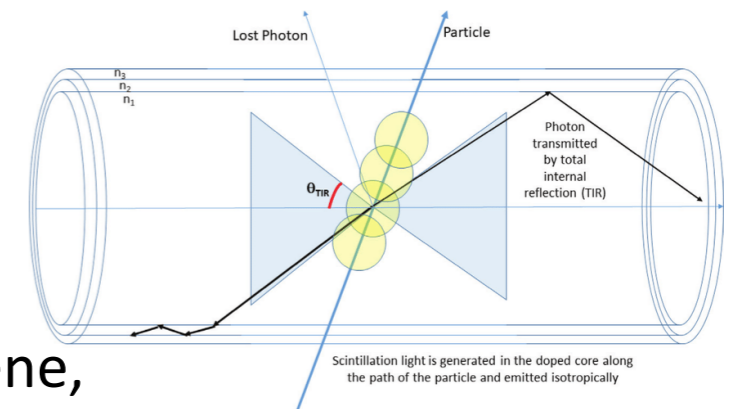
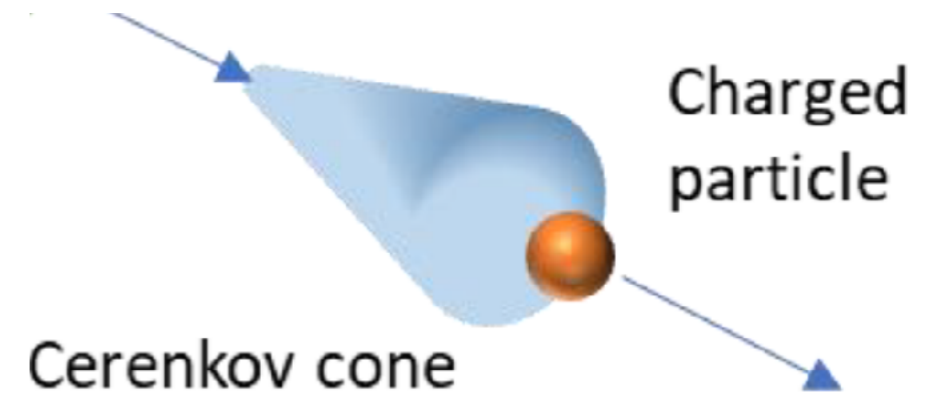
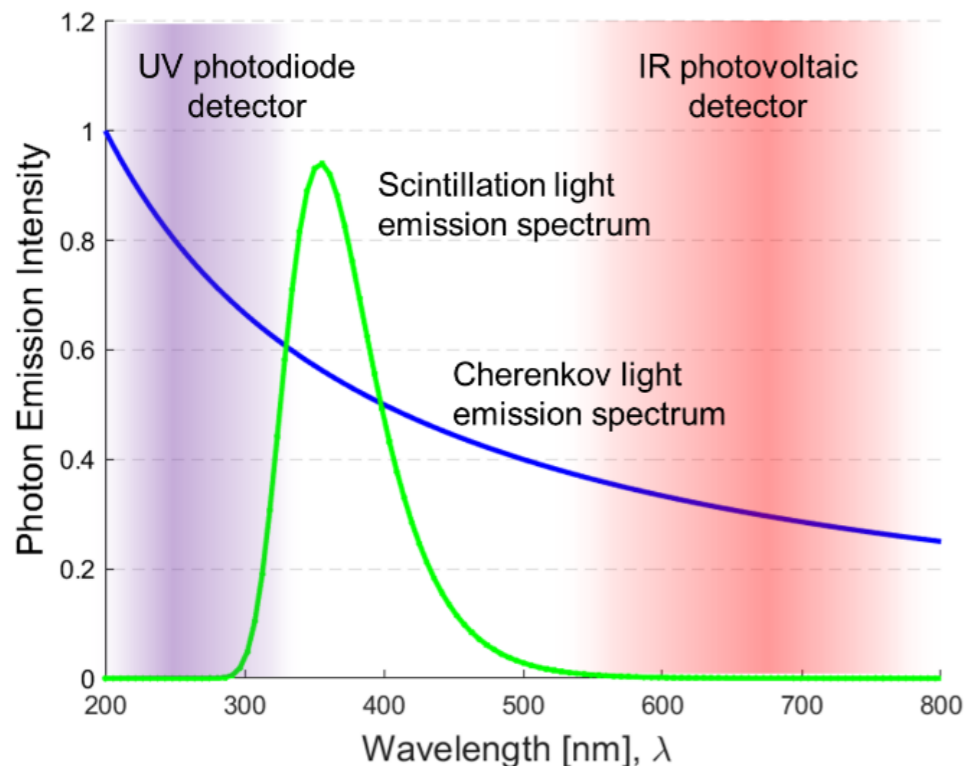
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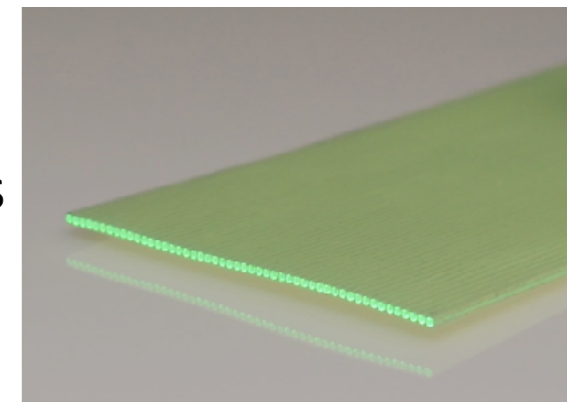
refraction index



Scintillating fiber

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- Very thin diameter could < 0.5 mm
- Flexible

➔ Could be assembled in ribbons



Junghyun Bae¹ et al., School of Nuclear Engineering, Purdue University, IN 47906

Scintillator (vii)

Scintillators comparison:

Scintillator Name	Density (g/cm^3)	Yield (photons/MeV)	Δ_E/E @ 662 keV (%)	Decay Constant (ns)
<i>Polystyrene</i>	1.05	10000	11	2.5
<i>BGO</i>	7.13	7500	12	300
<i>YAG</i>	4.60	8000	11	70
<i>BaF₂</i>	4.88	10000	9.0	0.8
<i>LYSO(Ce)</i>	7.10	32000	8.0	40
<i>CsI(Na)</i>	4.51	34000	7.5	630
<i>NaI(Tl)</i>	3.70	38000	6.0	230
<i>CeBr₃</i>	5.10	75000	4.0	20
<i>LaBr₃</i>	5.06	86000	3.0	16

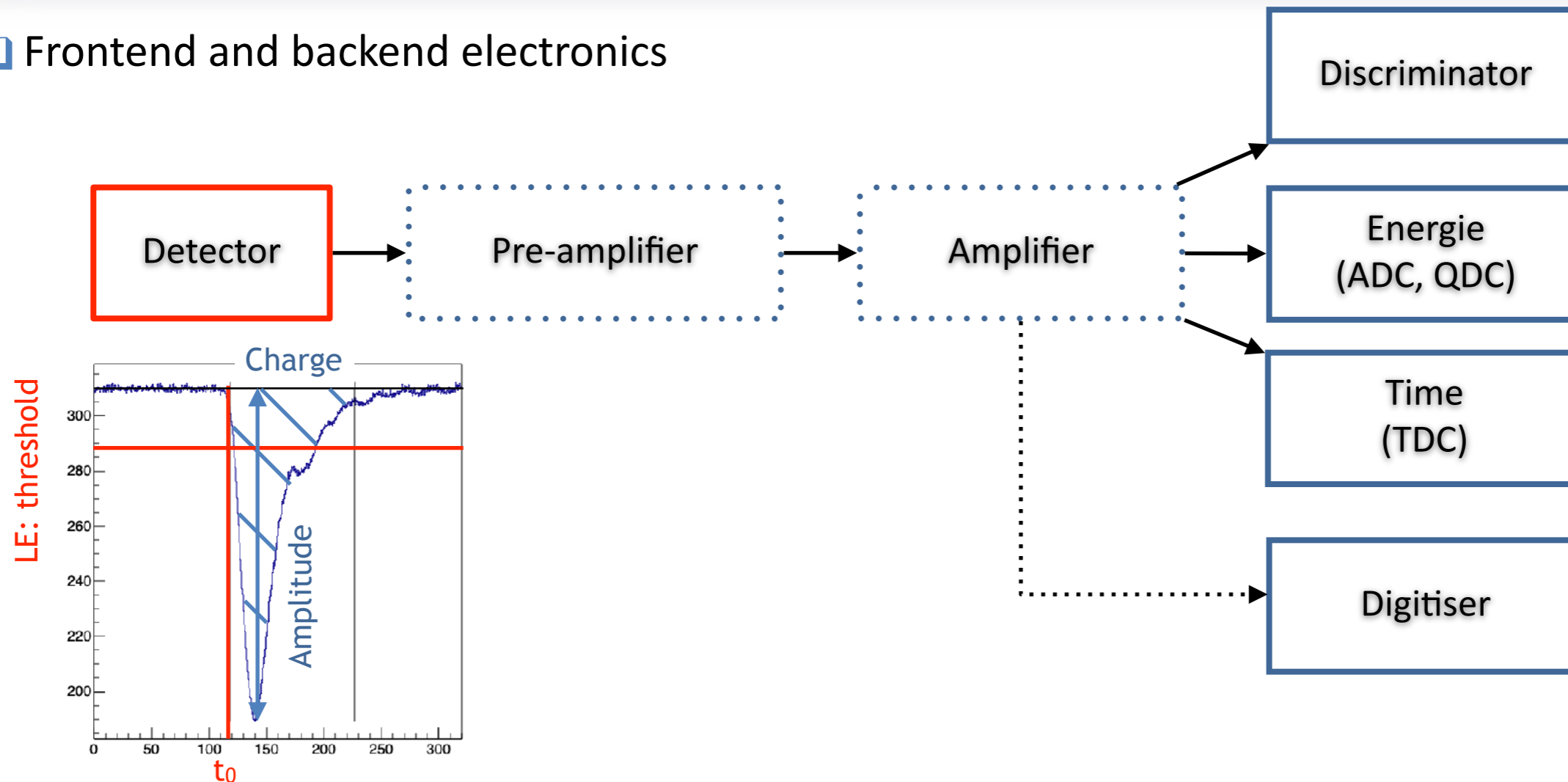
→ Efficiency proportional to density

→ Energy resolution proportional to yield

 Plastic

Electronics chain

□ Frontend and backend electronics

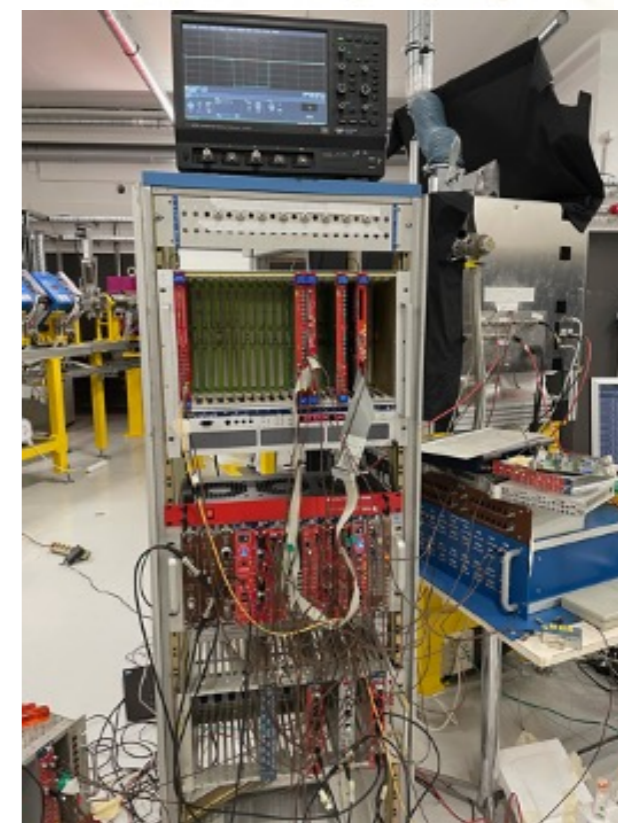
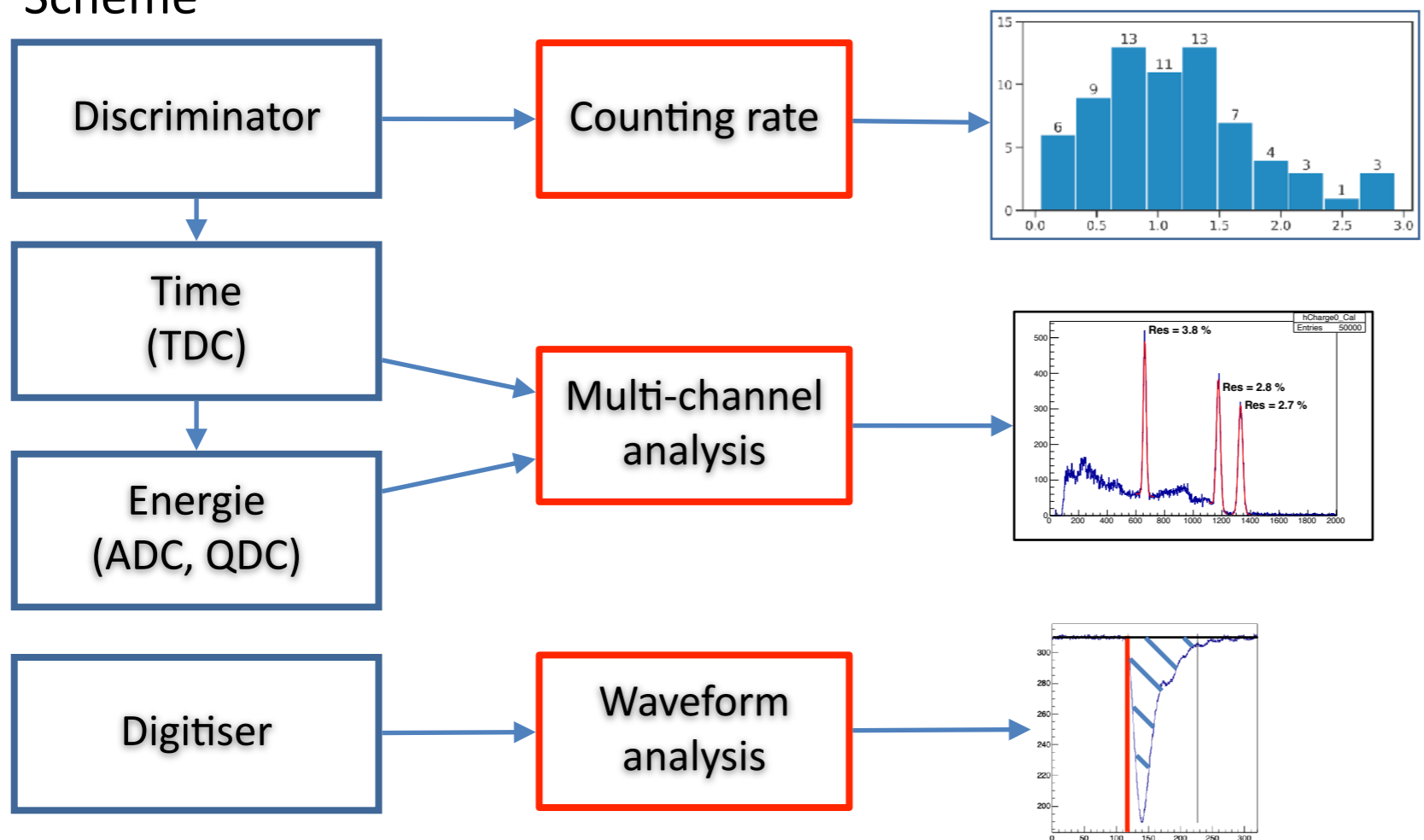


- Discriminator: compute start of signal t_0 (LE, CFD, etc... algorithms)
- ADC: Analog to digit converter, compute the amplitude of the signal
- TDC (TAC+ADC): time to digit converter, compute the time information
- QDC: charge to digit converter, compute the charge (integral) of the signal inside a give gate
- Digitiser (flash-ADC): compute the amplitude of the signal at a given frequency

Acquisition chain

Acquisition modules

Scheme



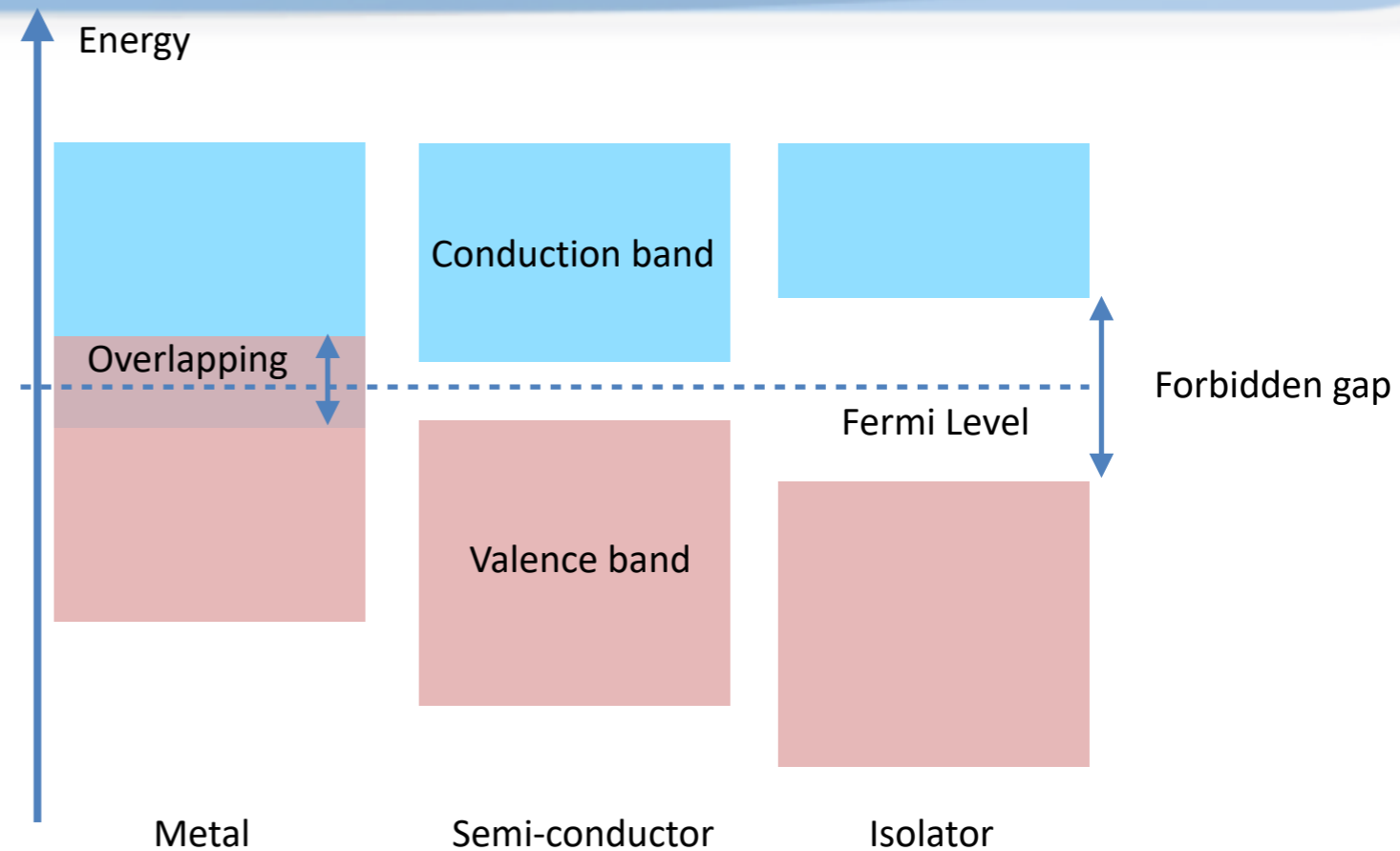
Event building:

- Build with data arriving in a given time (generated by dedicated detectors)
- Trigger-less, a common clock provides the TimeStamp
- ➔ Build event offline

Semi-conductive detector (i)

□ Properties (i):

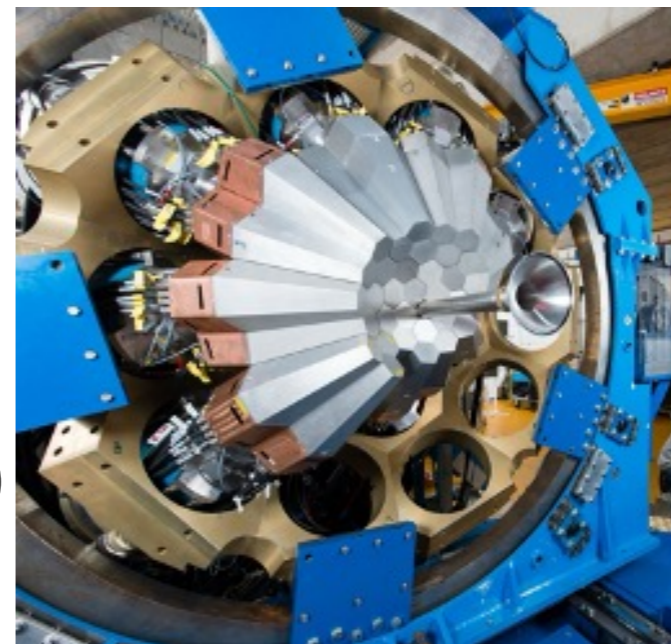
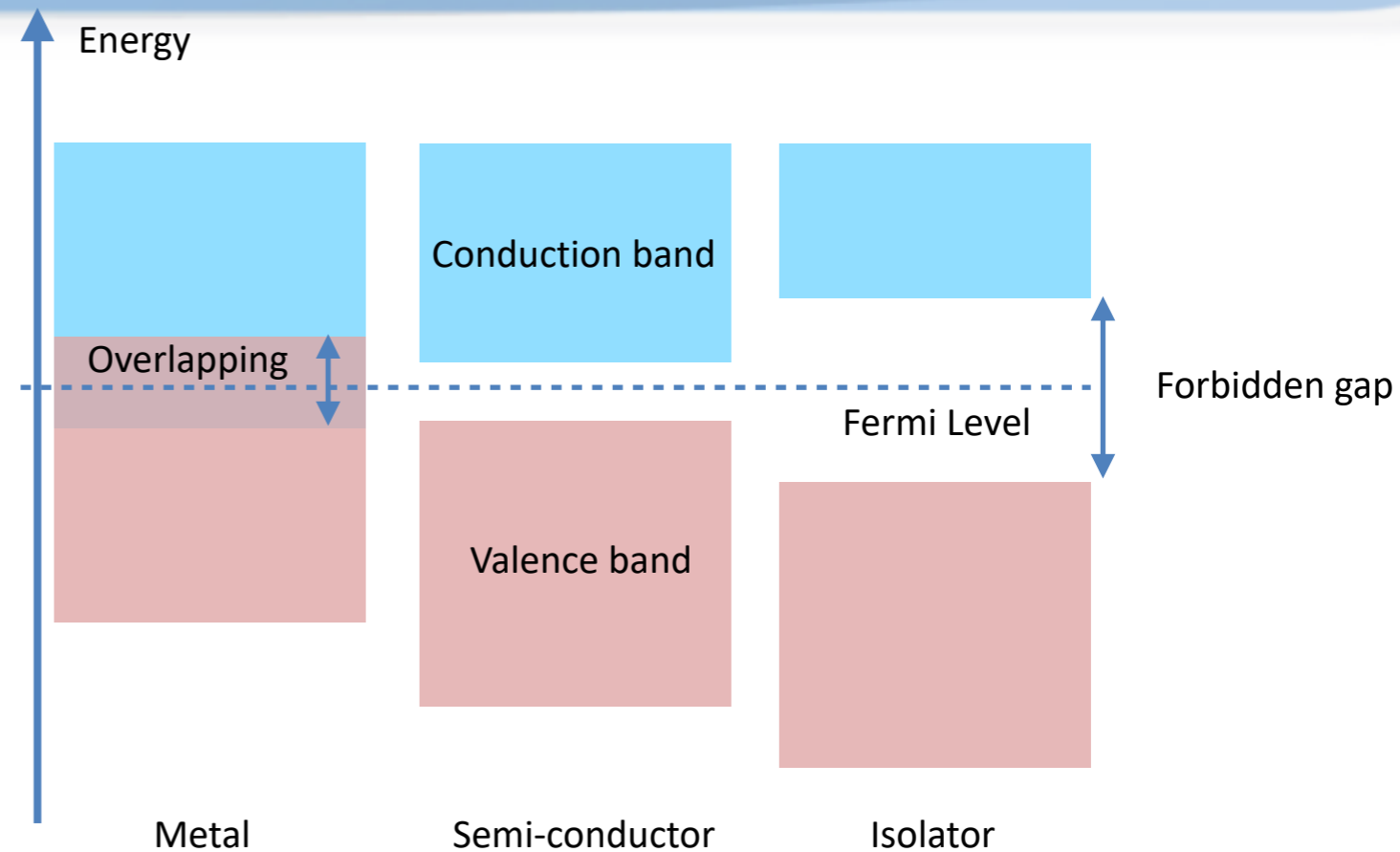
- Principle:
 - Based on electronic band structure
 - Ionising leads e- to conduction band
- Extrinsic detector:
 - n doping brings an e- in valence band
 - p doping remove an e- in the valence band
- Intrinsic detector:
 - No doping, hyper pur crystal



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- Intrinsic detector:
 - No doping, hyper pur crystal
- Production pair (e- hole): $W_i \lesssim 3 eV$
 - ➔ ~10 times smaller than for gaseous detector
 - ➔ Except for wide-bandgap detectors:
 - SiC, GaN, ZnO ($W_i \gtrsim 2 eV$), diamond ($W_i \lesssim 13 eV$)
- Most used: silicon and germanium detector



Semi-conductive detector (ii)

☐ Germanium detector:

- Advantages

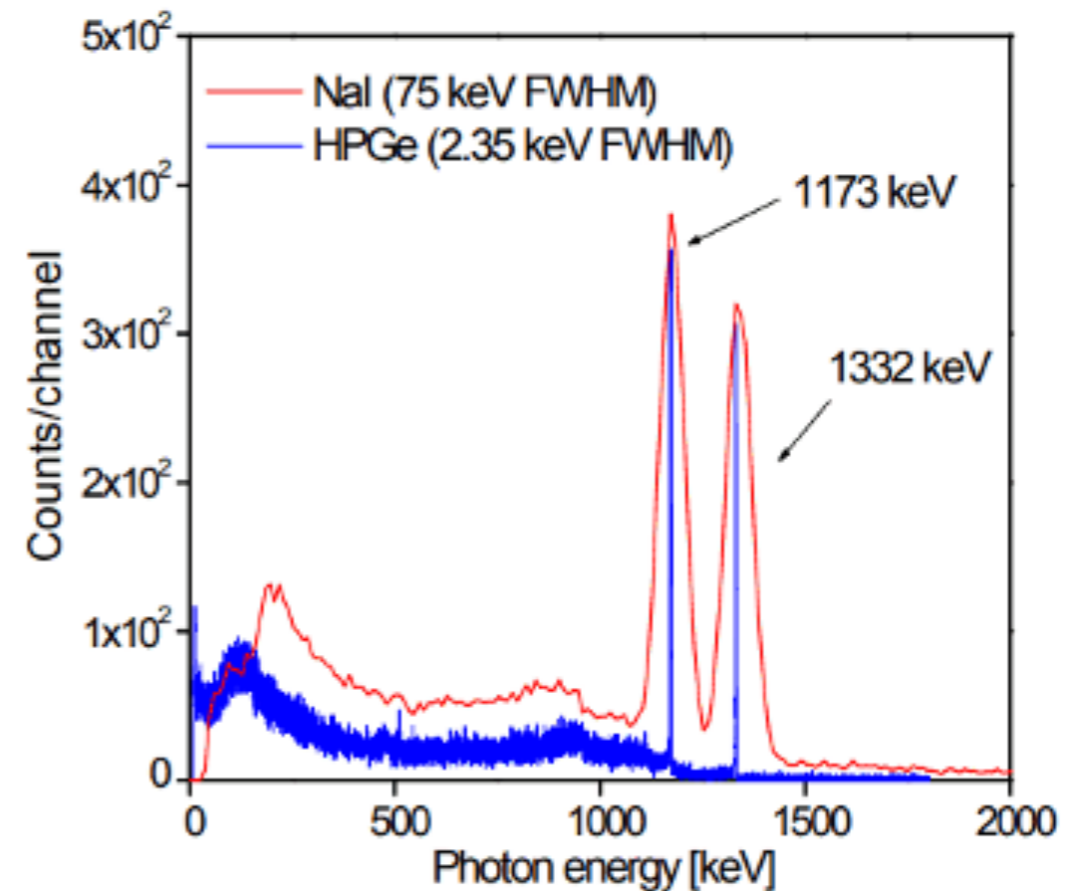
- High energy resolution: $\sim 0.1\%$

- ➔ Use for E measurements

- Drawbacks

- Poor efficiency: $\sim 50\%$ of NaI crystal
- Slow charge collection: few ten of μs
- Need to amplify the signal
- Need to cool down cos $W_i = 2.62 eV$ very low (77° K)
- Very expensive for large volume (when possible)

- ➔ Not portable measurements



Semi-conductive detector (iii)

□ Silicon detector:

- Properties

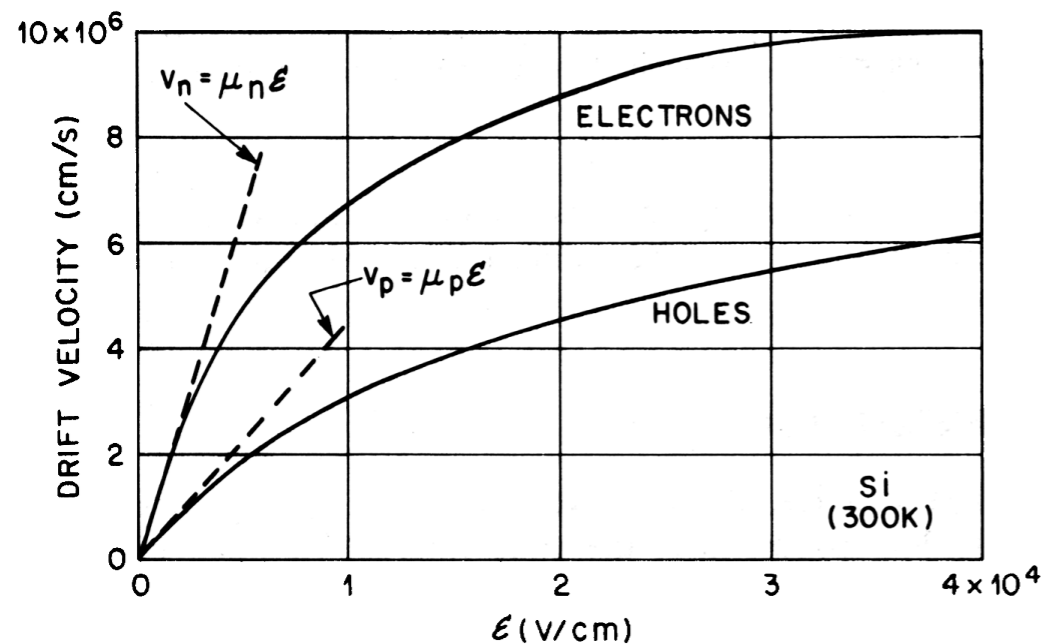
- Pair creation energy: $W_i = 3.69 \text{ eV}$

- Mobility:

$$\mu_{(e,h)} = \frac{e}{2m_{(e,h)}} E \times \tau_{(e,h)}$$

E : electrical field

$\tau_{(e,h)}$: mean free time between 2 collisions (cf. gaseous detector)



$$\mu_e(300K) \simeq 1450 \text{ cm}^2/\text{V/s}$$

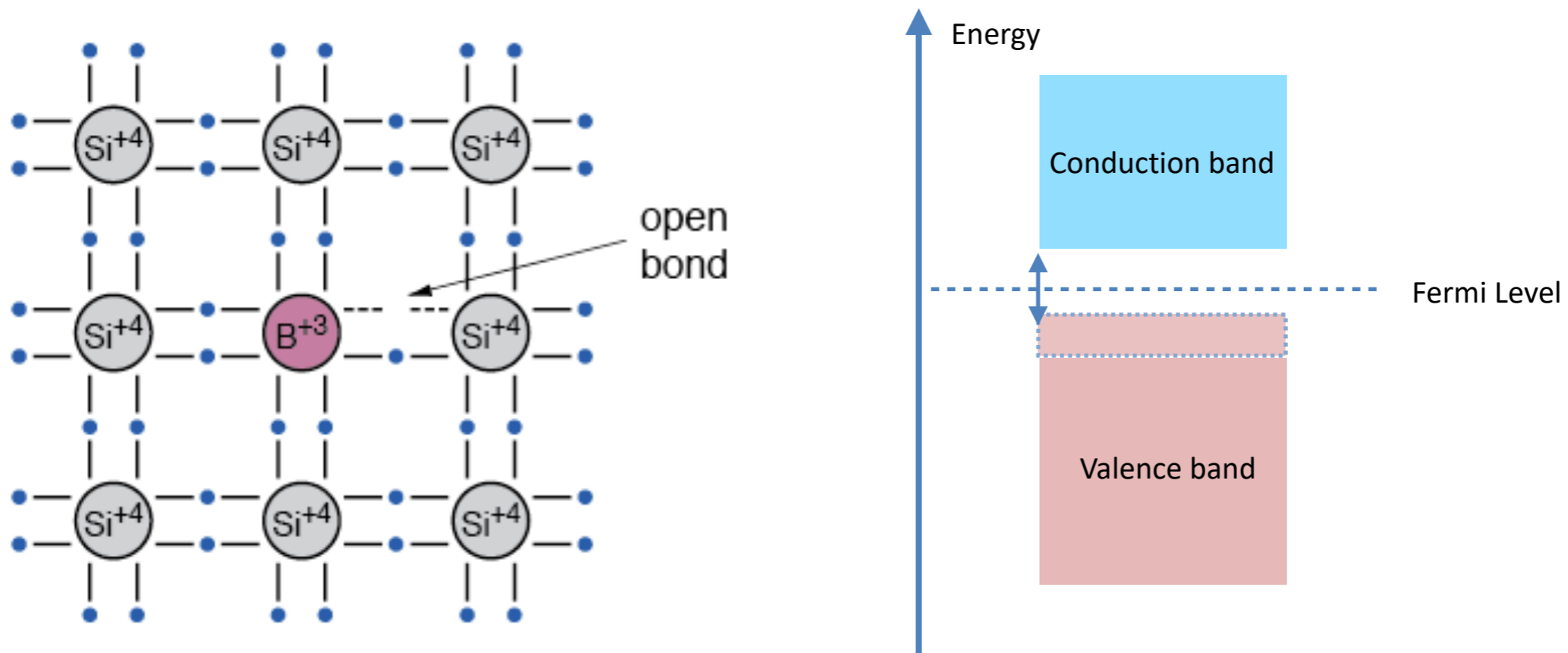
$$\mu_h(300K) \simeq 450 \text{ cm}^2/\text{V/s}$$

S.M. Suze, *Semiconductor Devices*, J. Wiley & Sons, 1985

Semi-conductive detector (iv)

□ p-doping:

- Doping 3 atom (e.g. B, Al, Ga, In). One valence bond remains open. This open bond attracts electrons from the neighbour atoms:

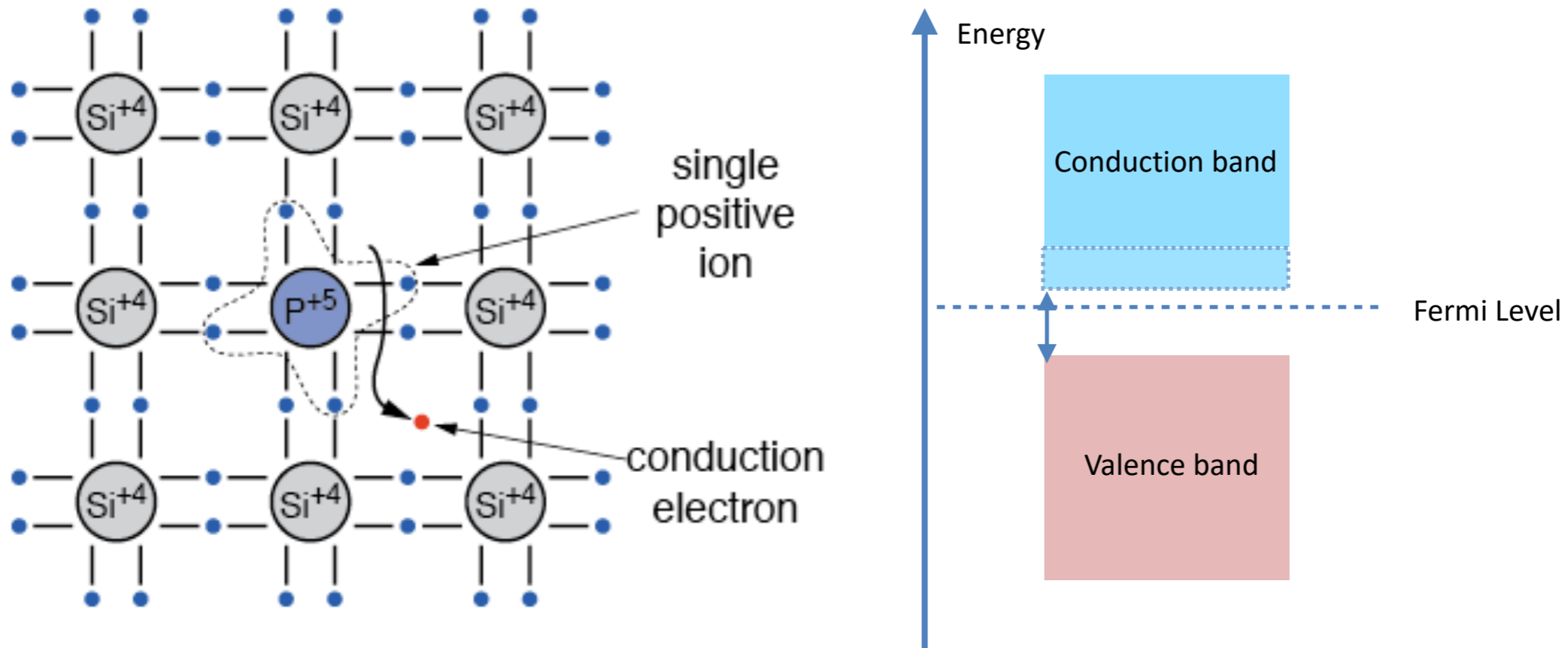


➔ Less electron density (acceptor of e)

Semi-conductive detector (v)

□ n-doping:

- Doping with 5 atom (e.g. P, As, Sb). The 5th valence electron is weakly bound:

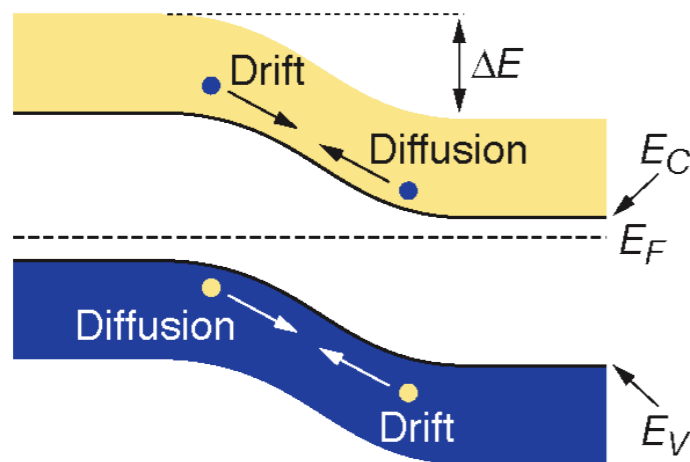
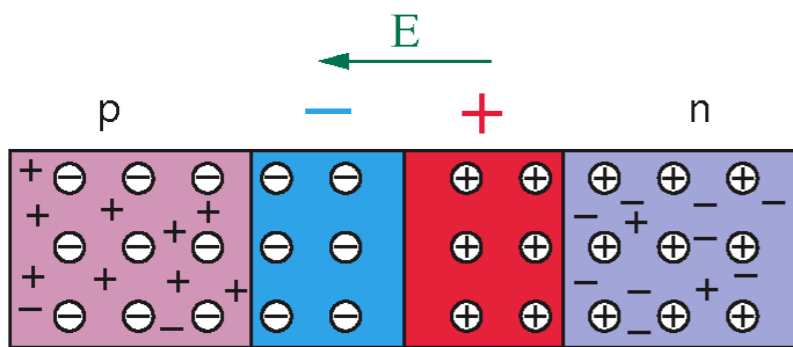


➔ Higher electron density (donor of e)

Semi-conductive detector (vi)

□ The p-n junction

- At the interface of an n-type and p-type semiconductor:
 - Fermi level different: diffusion til ions space charge stops it
 - The stable space charge region is free of charge carries and is called the depletion zone



- Depletion width depend on electric field

- Without external field:

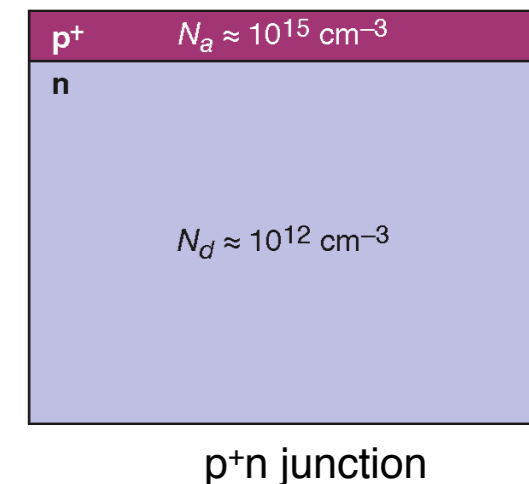
$$W_p = 0.02 \mu m$$

$$W_n = 23 \mu m$$

- With external field:

$$W_p = 0.4 \mu m$$

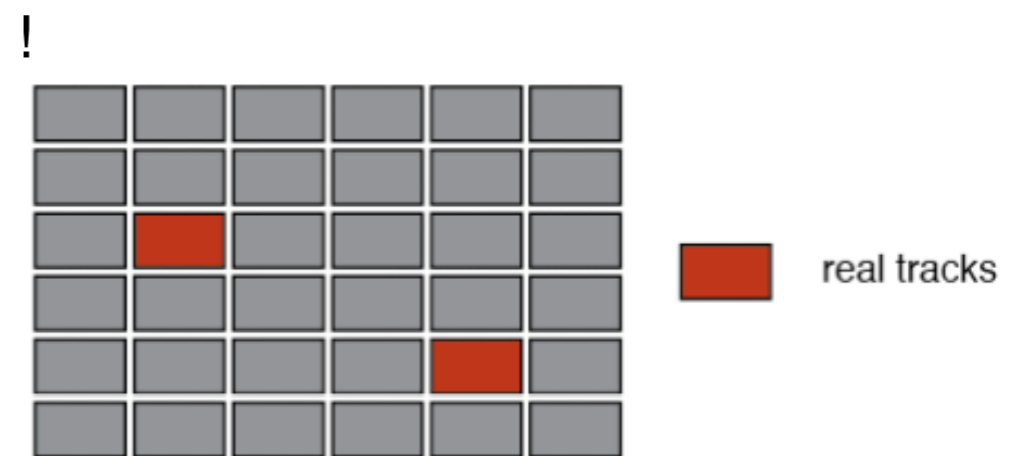
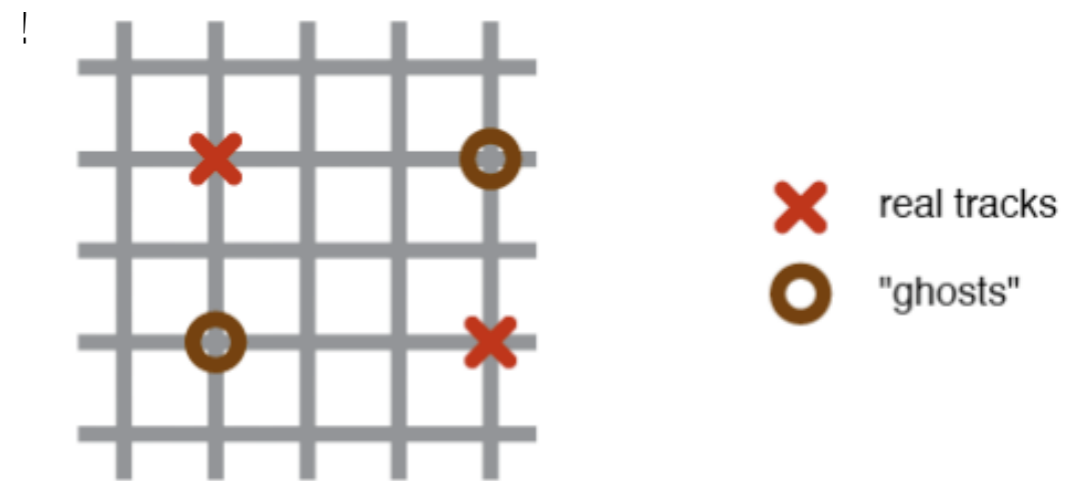
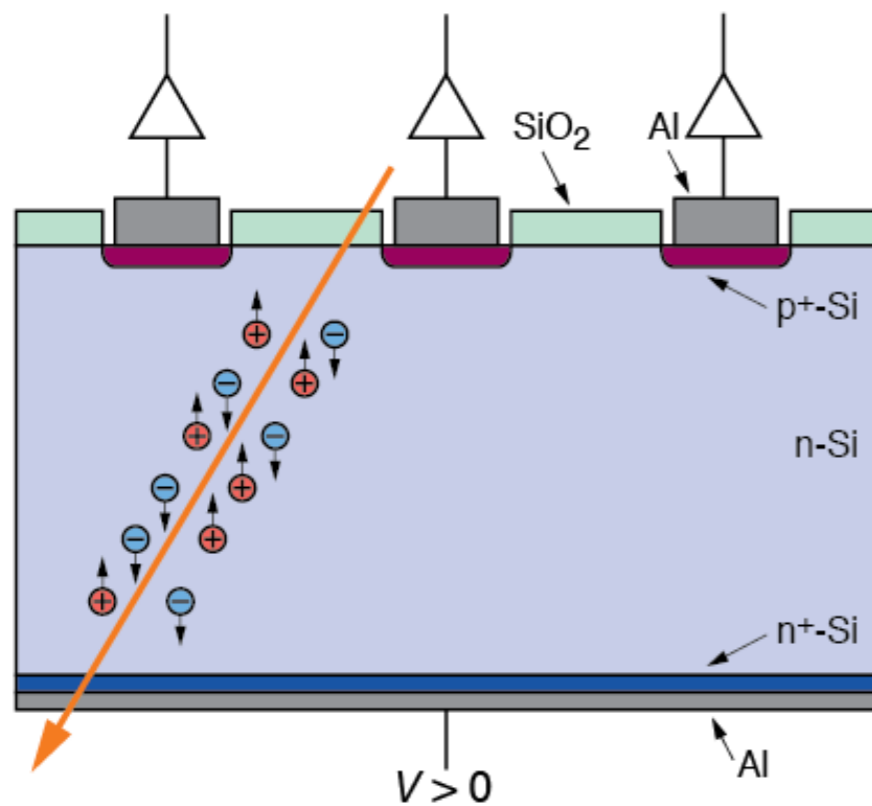
$$W_n = 360 \mu m$$



Semi-conductive detector (vii)

□ p-n junction silicon detector

- Impinging charged particles create e-h+ pairs in the depletion zone. These charges drift to the electrodes. The drift (current) creates the signal on each strip/pixel.
- From fired strips/pixels possible position reconstruction.

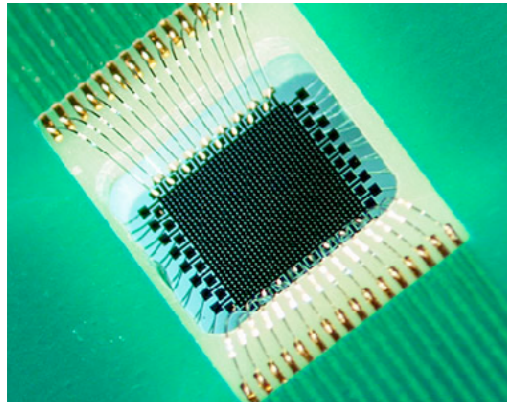
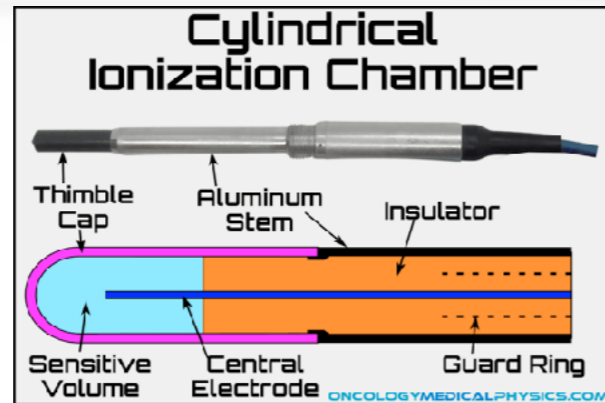


→ Front/backend electronics mostly directly on the chip

Detectors for medical applications

□ Beam monitoring:

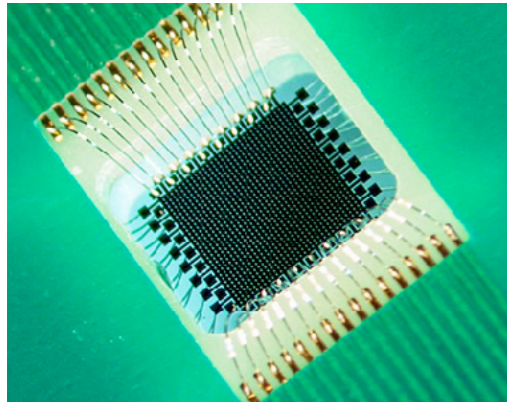
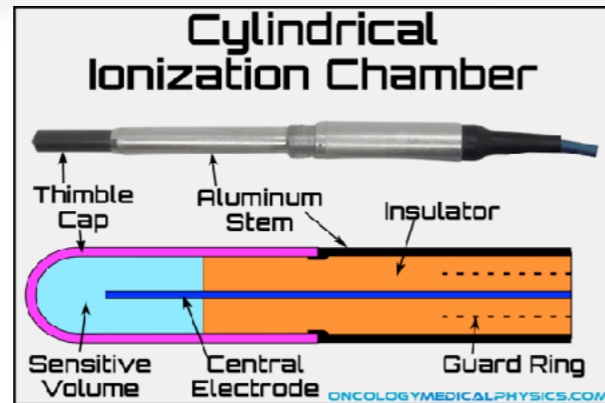
- Gaseous detectors
- Semi-conductors



Detectors for medical applications

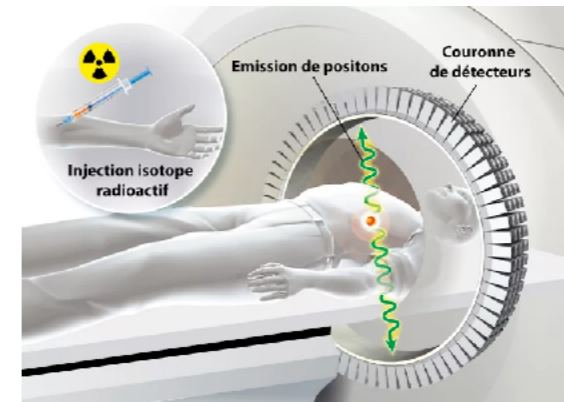
☐ Beam monitoring:

- Gaseous detectors
- Semi-conductors



☐ PET-(SPECT)- pCT imaging:

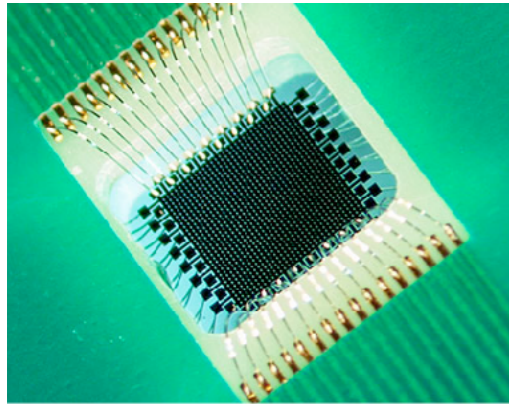
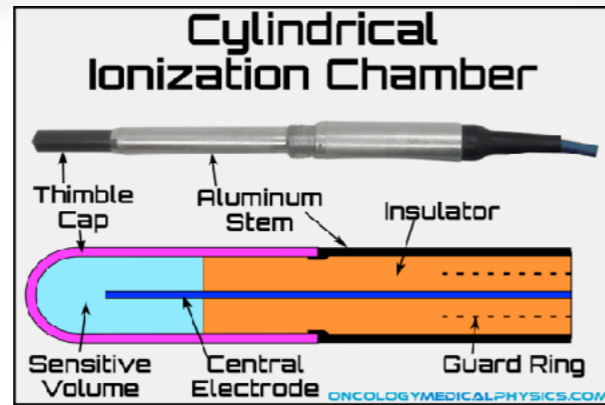
- Scintillators



Detectors for medical applications

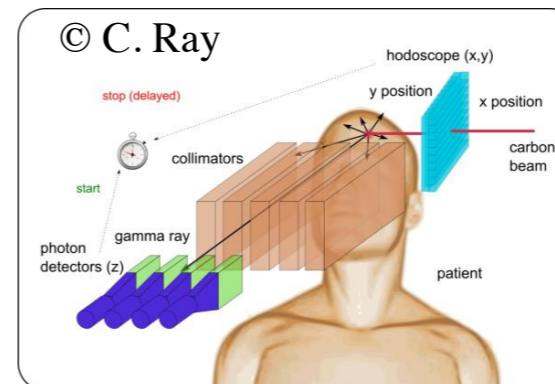
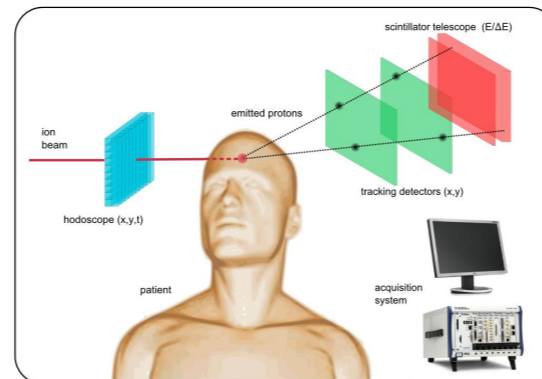
☐ Beam monitoring:

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- Semi-conductors



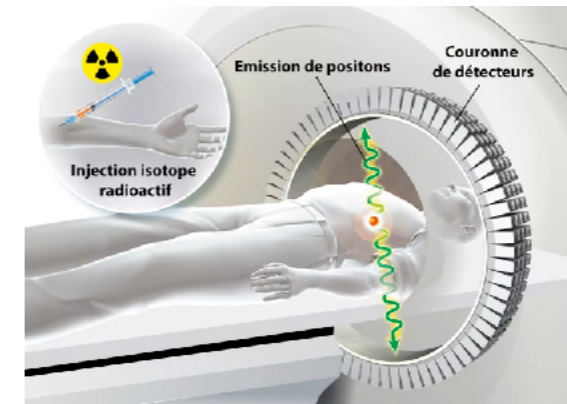
☐ Online dose control:

- Scintillators
- Silicon tracking devices



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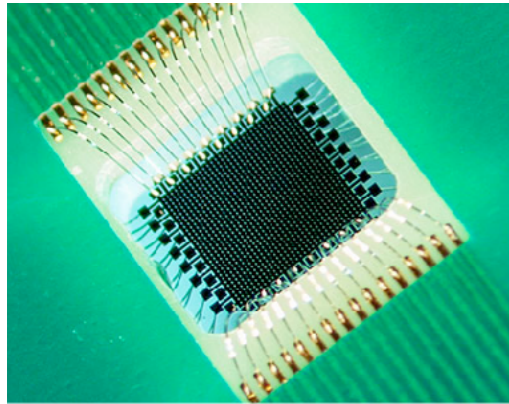
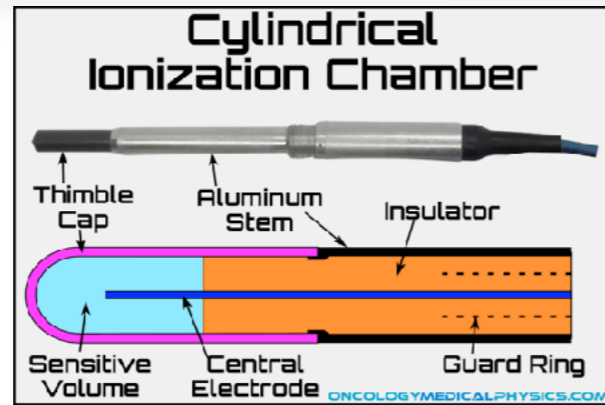
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Detectors for medical applications

Beam monitoring:

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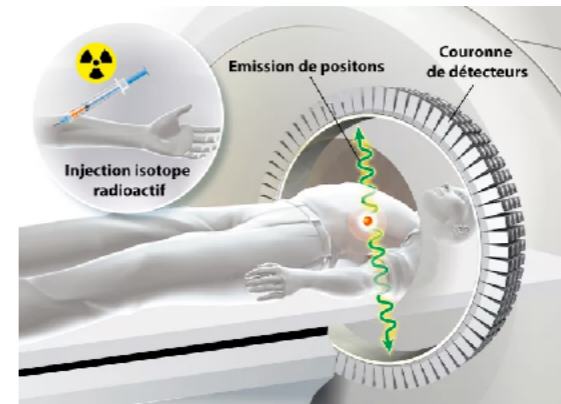


Online dose control:

- Scintillators
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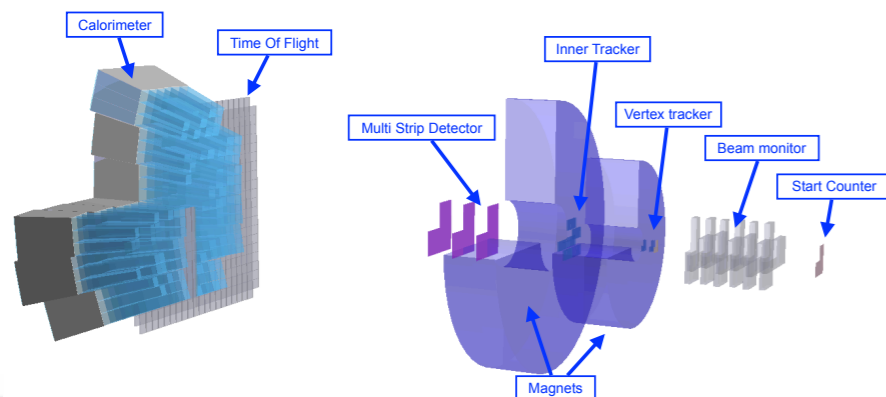
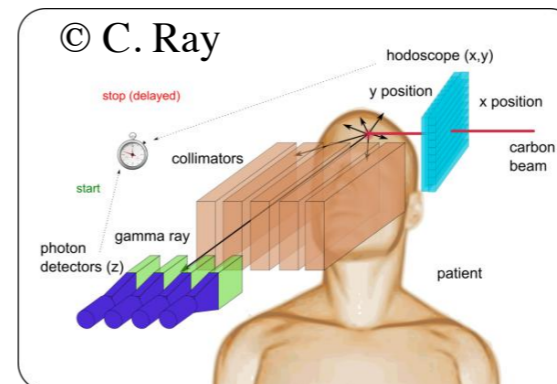
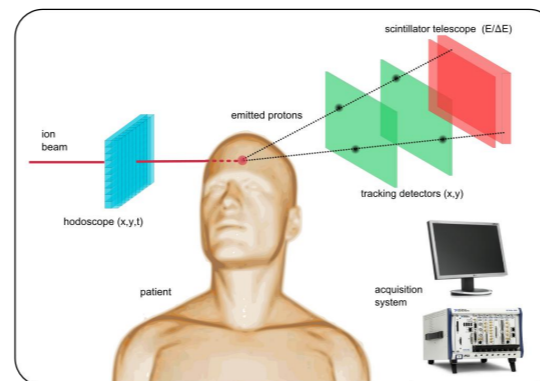
PET-(SPECT)- pCT imaging:

- Scintillators



Cross-section measurement:

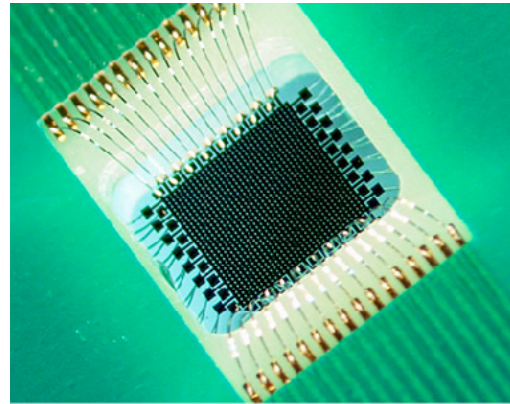
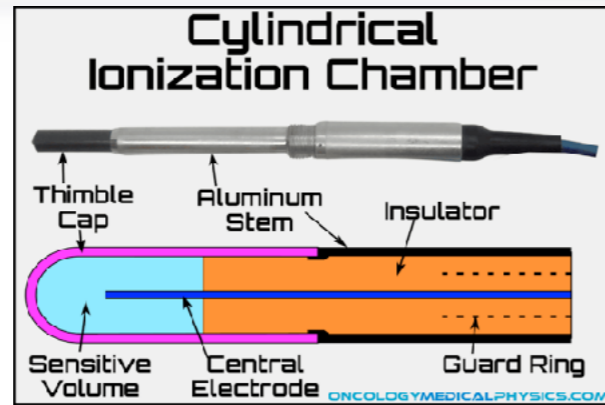
- Scintillators (in-organic)
- Silicon tracking devices
- Gaseous detectors



Detectors for medical applications

Beam monitoring:

- Gaseous detectors
- Semi-conductors

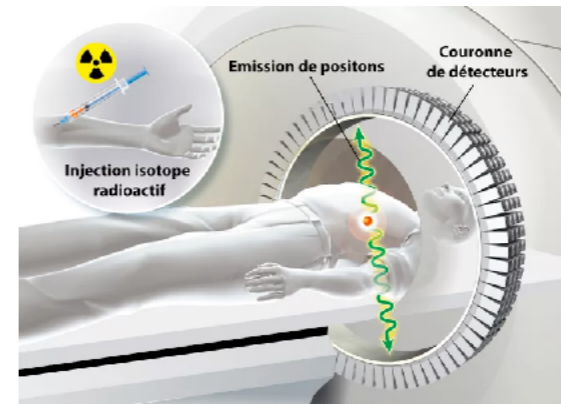


Online dose control:

- Scintillators
- Silicon tracking devices

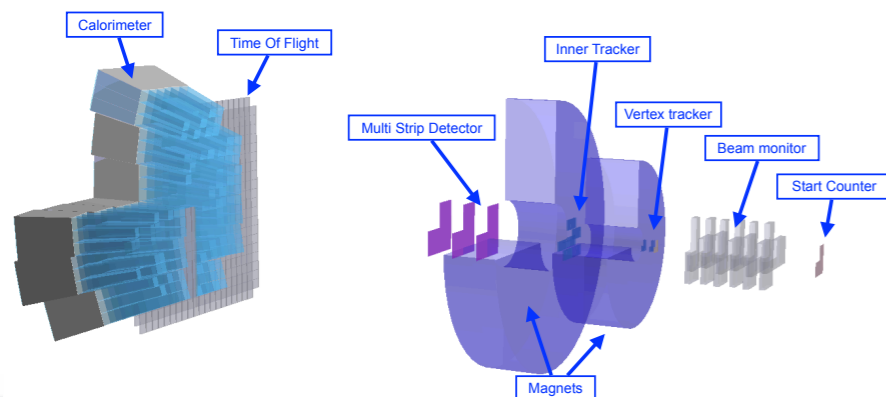
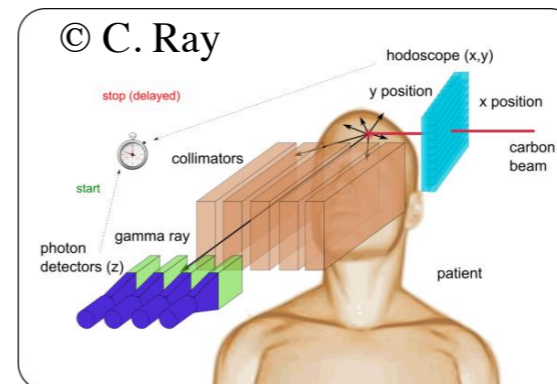
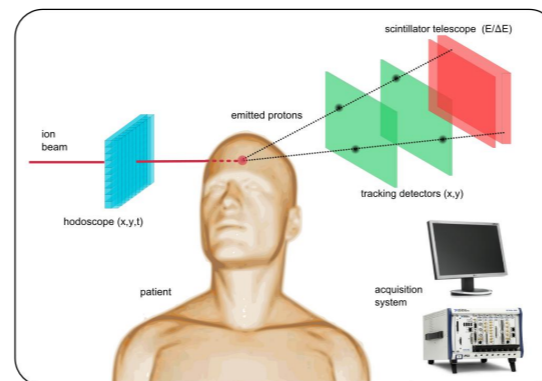
PET-(SPECT)- pCT imaging:

- Scintillators



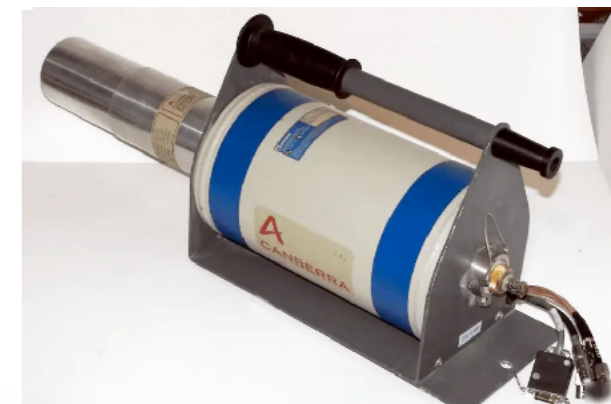
Cross-section measurement:

- Scintillators (in-organic)
- Silicon tracking devices
- Gaseous detectors



Dosimetry:

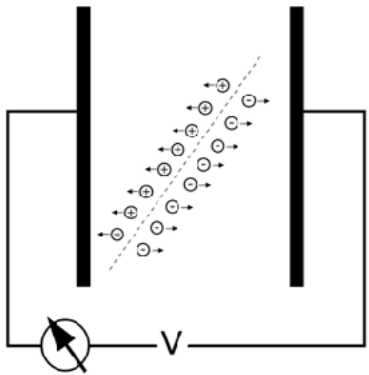
- Passive detectors
- Gaseous detectors
- Semi-conductors



Beam Monitoring (i)

□ Gaseous detectors

- Parallel plate Ionisation chamber
 - Gas at atmospheric (low) pressure
 - Applied HV $\sim 100V$
 - Simply read out a current
 - ➔ Sustains high beam flux
 - ➔ Need calibration



Beam Monitoring (i)

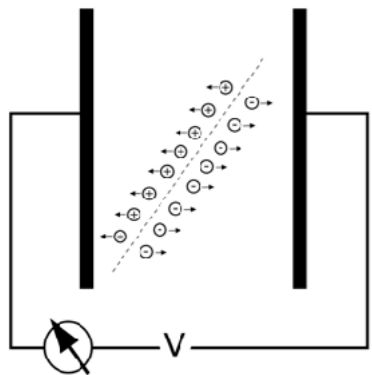
□ Gaseous detectors

- Parallel plate Ionisation chamber

- Gas at atmospheric (low) pressure
- Applied HV $\sim 100V$
- Simply read out a current

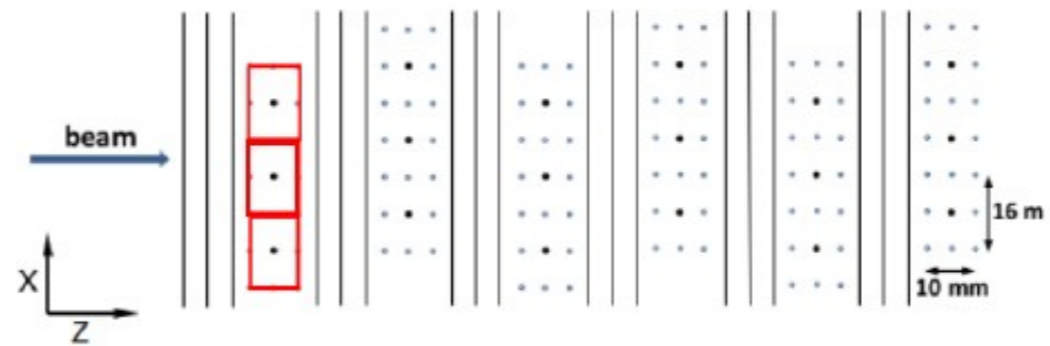
➔ Sustains high beam flux

➔ Need calibration

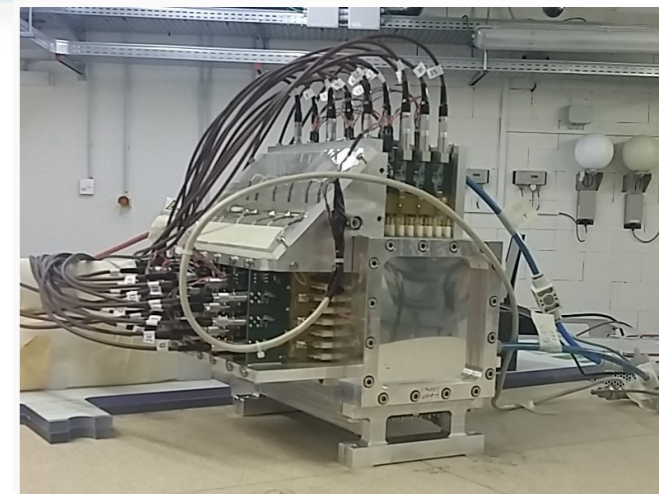


- Drift chamber

- Field wire at HV potential ($\sim 1-2kV$)
- Sense wire to read out the charge



- Gas mixture Ar+Iso/CO₂ (10-20%)
- Beam profile resolution $\sim 100-200 \mu m$
- ➔ Limited by beam flux ($\ll 10^4/cm^2/s$)
- ➔ Need calibration for drift velocity



Beam Monitoring (ii)

□ Semi-conductors

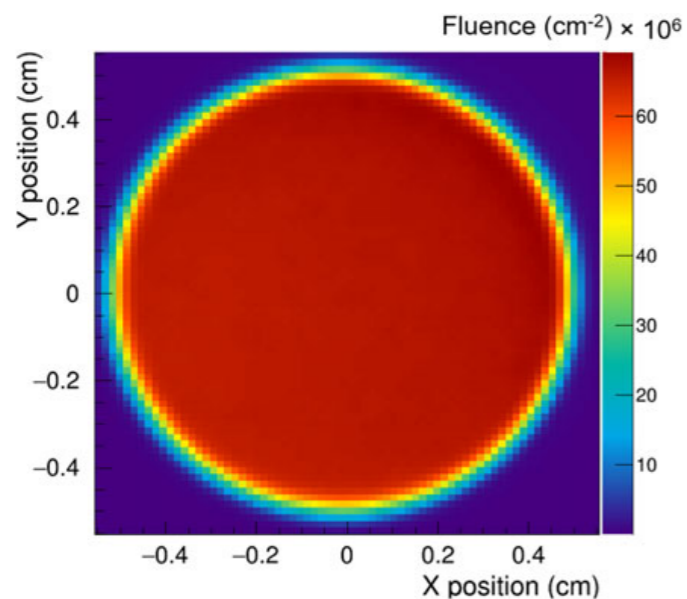
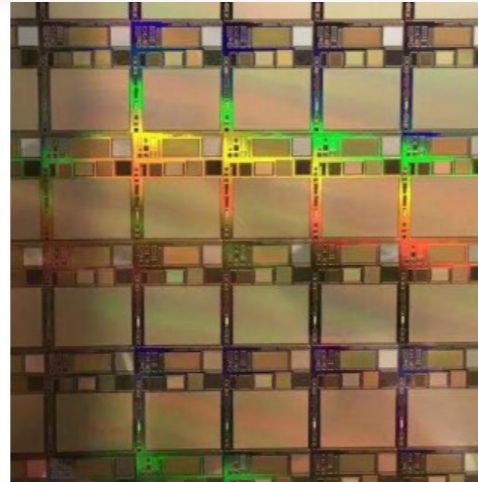
- Silicon detector

- Bulk, strip or pixels
- Good radiation tolerance

➔ Charge resolution $\sim 3\text{-}4\%$

➔ Excellent beam profile resolution ($\ll 100\ \mu\text{m}$)

➔ Limited beam flux tolerance ($\ll 10^7\ \text{cm}^{-2}/\text{s}$)

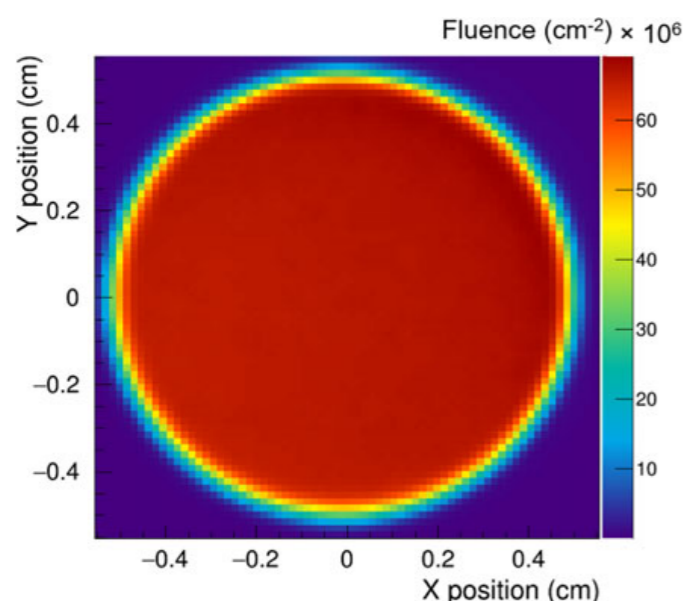
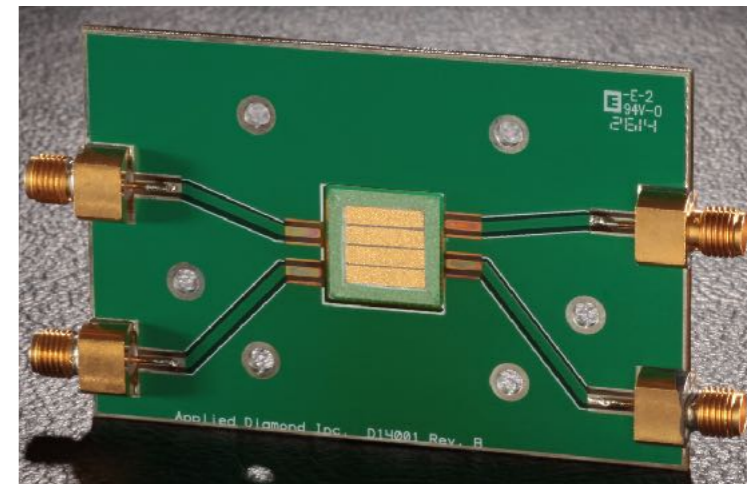
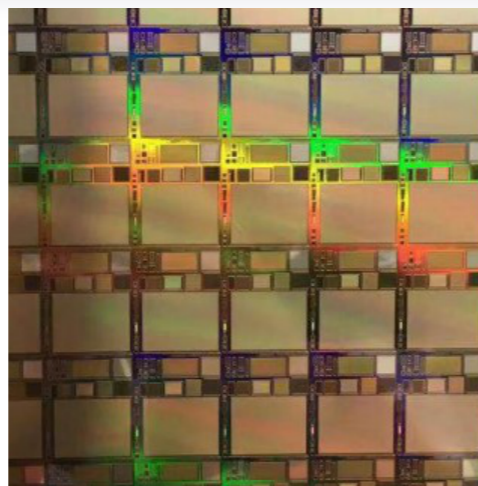


Beam Monitoring (ii)

□ Semi-conductors

- Silicon detector

- Bulk, strip or pixels
- Good radiation tolerance
- ➔ Charge resolution $\sim 3\text{-}4\%$
- ➔ Excellent beam profile resolution ($\ll 100\ \mu\text{m}$)
- ➔ Limited beam flux tolerance ($\ll 10^7/\text{cm}^2/\text{s}$)



- Diamond detector

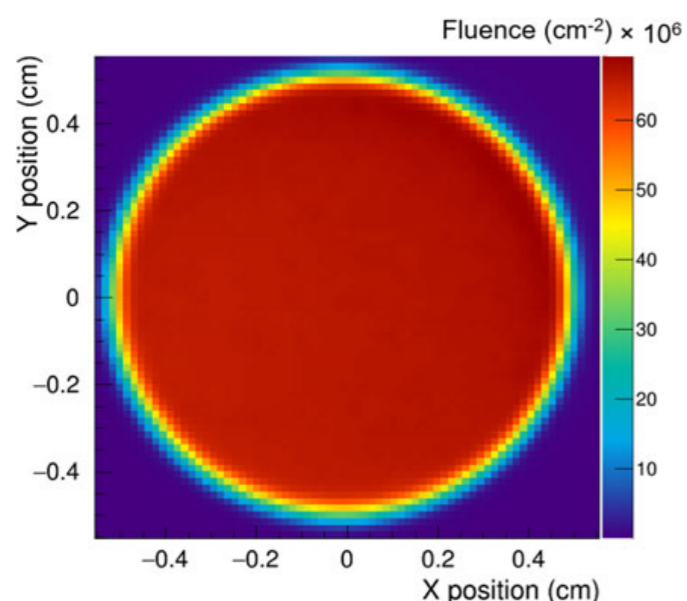
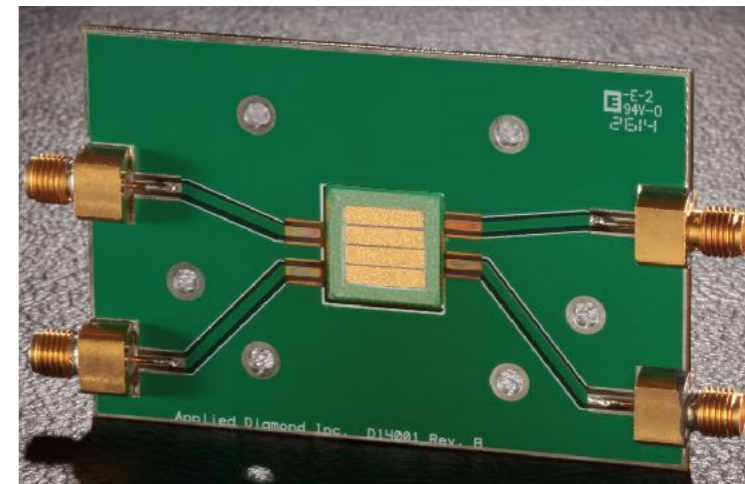
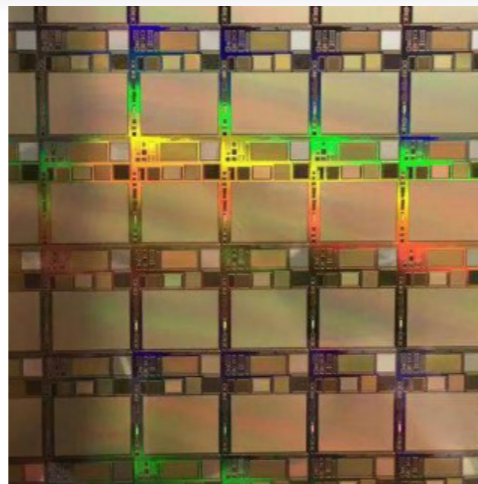
- Wide-bandgap (low noise)
- Very good radiation tolerance
- Fast time response ($< 2\ \text{ns}$)
- ➔ Excellent beam profile resolution ($\ll 100\ \mu\text{m}$)
- ➔ Good beam flux tolerance ($\sim (10^9 - 10^{12})/\text{cm}^2/\text{s}$)

Beam Monitoring (ii)

□ Semi-conductors

- Silicon detector

- Bulk, strip or pixels
- Good radiation tolerance
- ➔ Charge resolution $\sim 3\text{-}4\%$
- ➔ Excellent beam profile resolution ($\ll 100 \mu\text{m}$)
- ➔ Limited beam flux tolerance ($\ll 10^7 / \text{cm}^2 / \text{s}$)



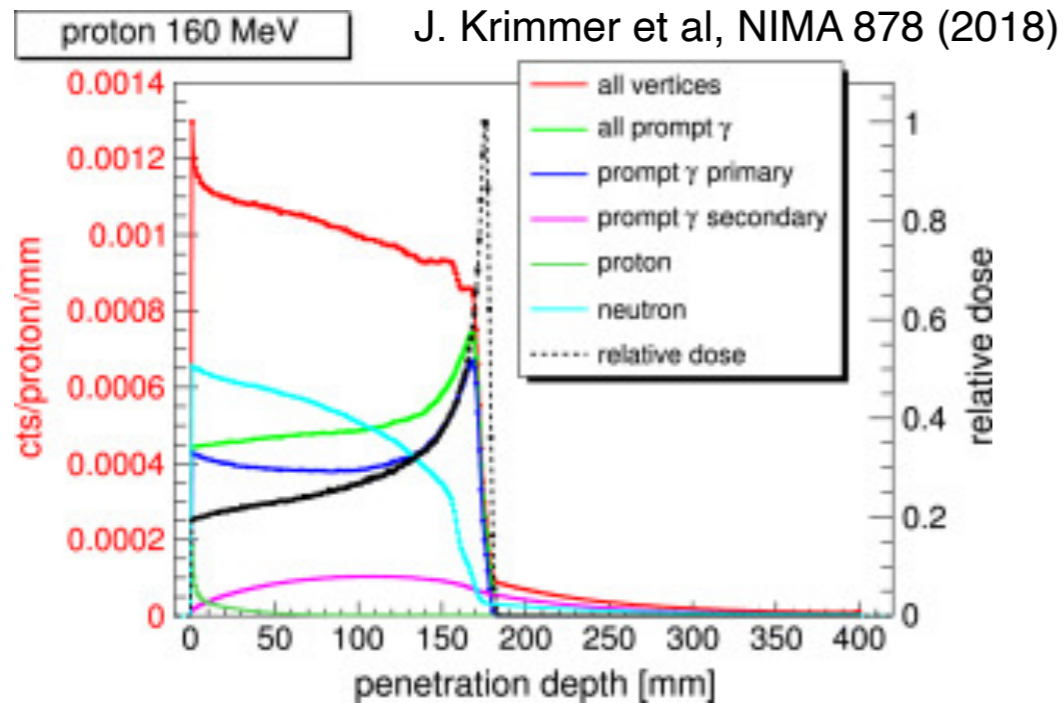
- Diamond detector

- Wide-bandgap (low noise)
- Very good radiation tolerance
- Fast time response ($< 2 \text{ ns}$)
- ➔ Excellent beam profile resolution ($\ll 100 \mu\text{m}$)
- ➔ Good beam flux tolerance ($\sim (10^9 - 10^{12}) / \text{cm}^2 / \text{s}$)

➔ Also other detectors exist: PEPITES, FastPix, micromegas, GEM, plastic, fibres, etc....

Online dose control (i)

- Mostly three techniques used, correlation btw Bragg peak and nuclear reactions
 - Prompt gamma method reconstruction

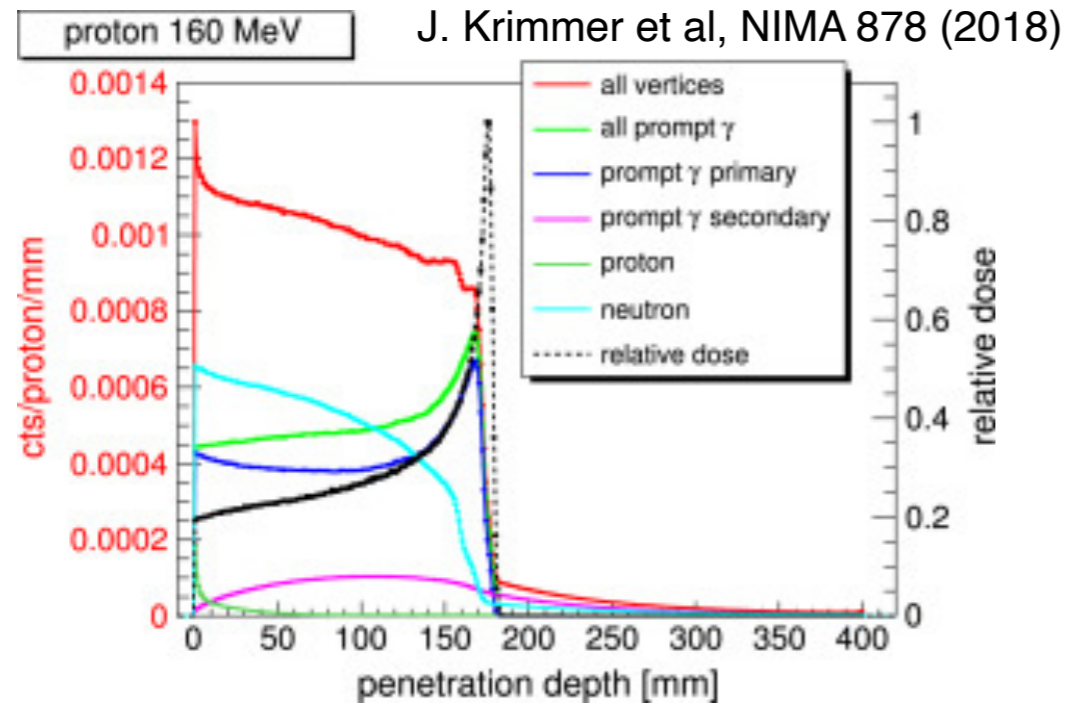


S. Jan et al., IEEE (2012)

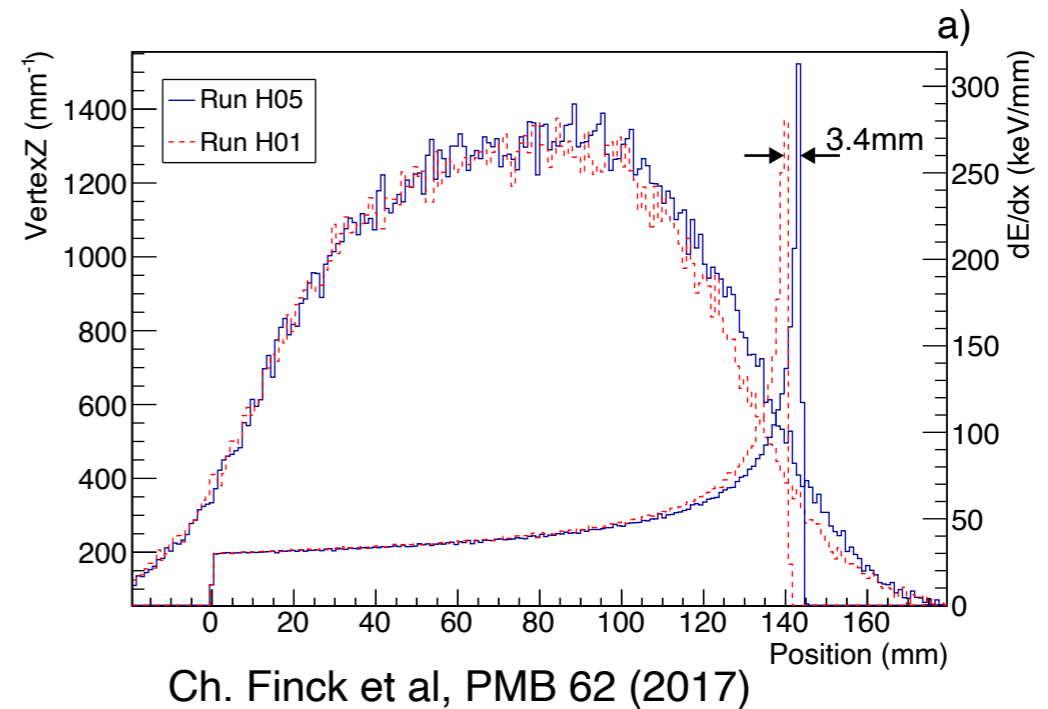
Online dose control (i)

☐ Mostly three techniques used, correlation btw Bragg peak and nuclear reactions

- Prompt gamma method reconstruction



- Secondary particle vertex reconstruction

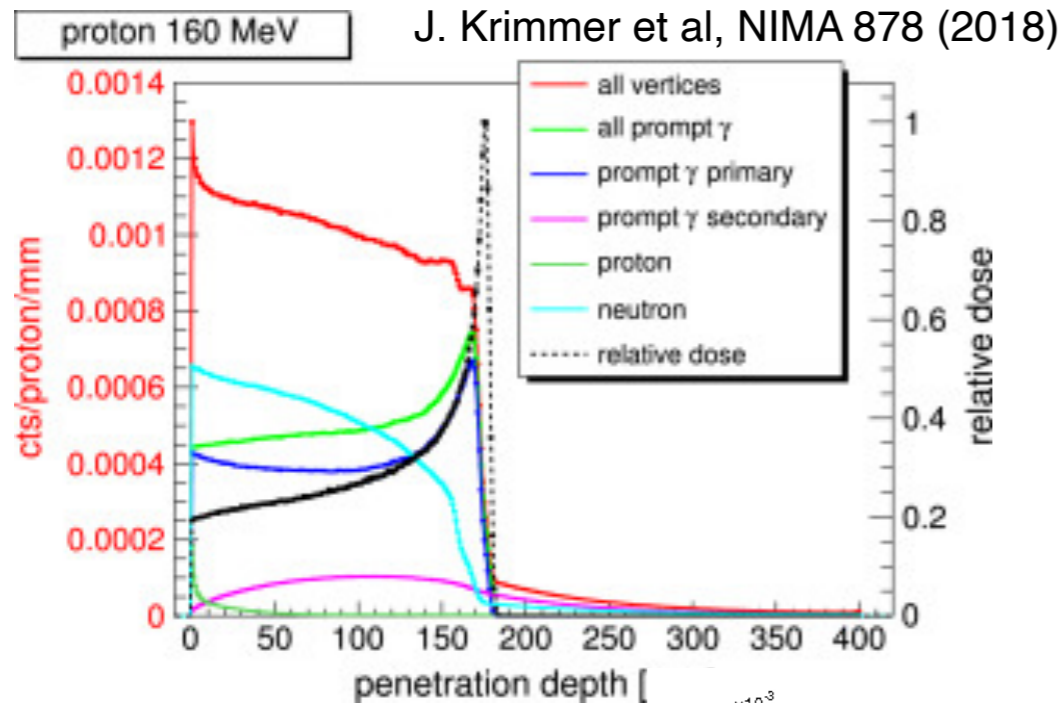


S. Jan et al., IEEE (2012)

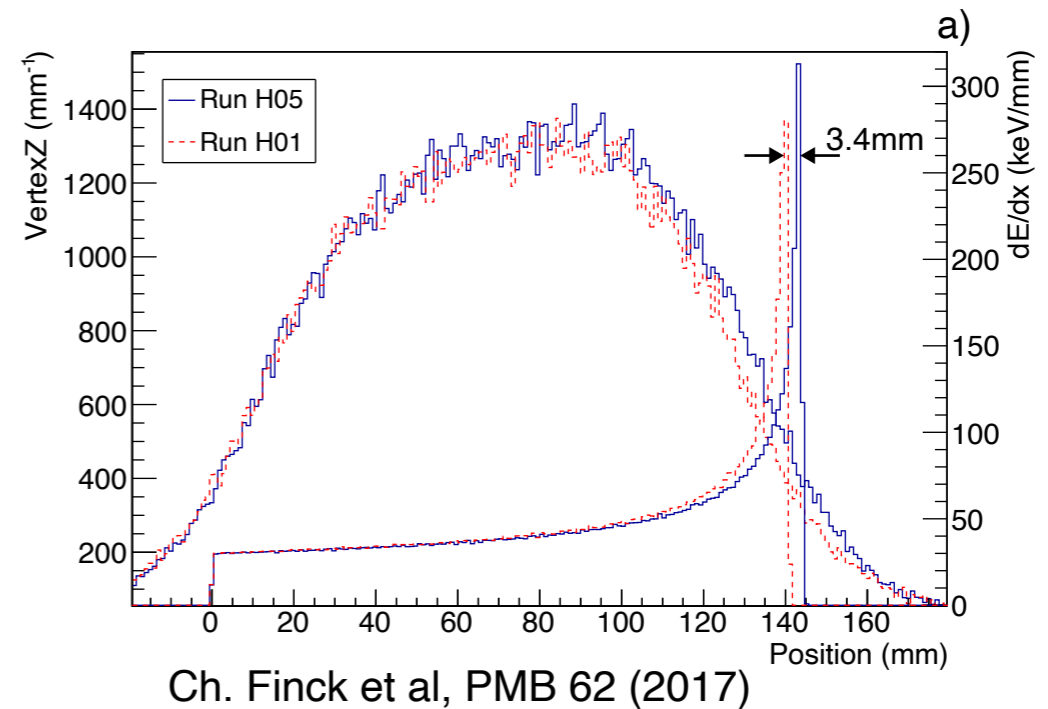
Online dose control (i)

☐ Mostly three techniques used, correlation btw Bragg peak and nuclear reactions

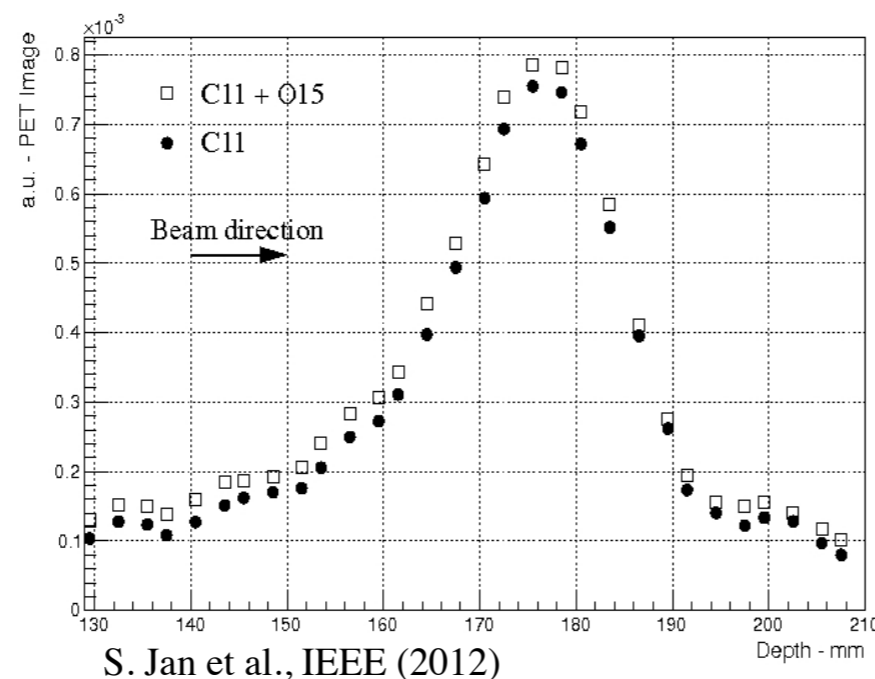
- Prompt gamma method reconstruction



- Secondary particle vertex reconstruction



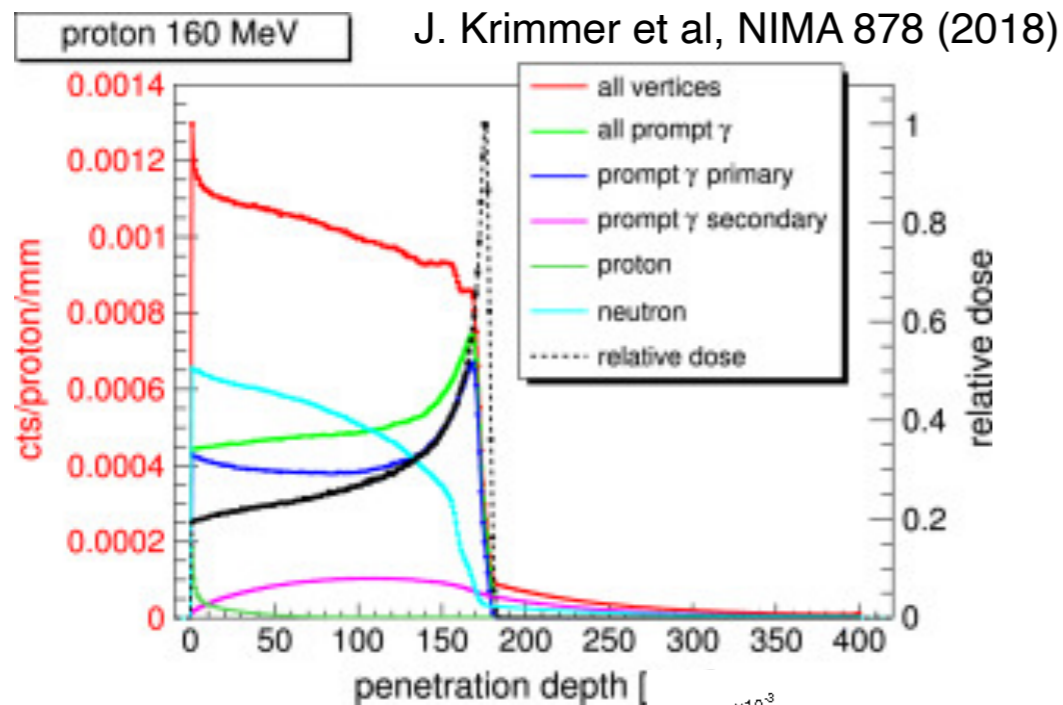
- Inline PET reconstruction



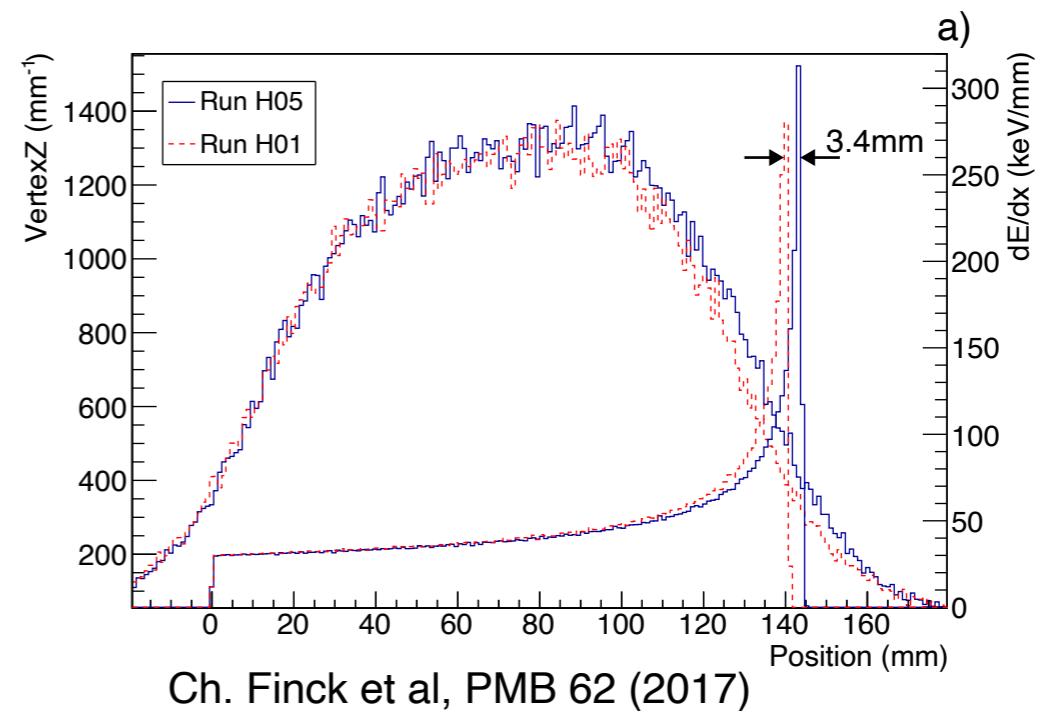
Online dose control (i)

☐ Mostly three techniques used, correlation btw Bragg peak and nuclear reactions

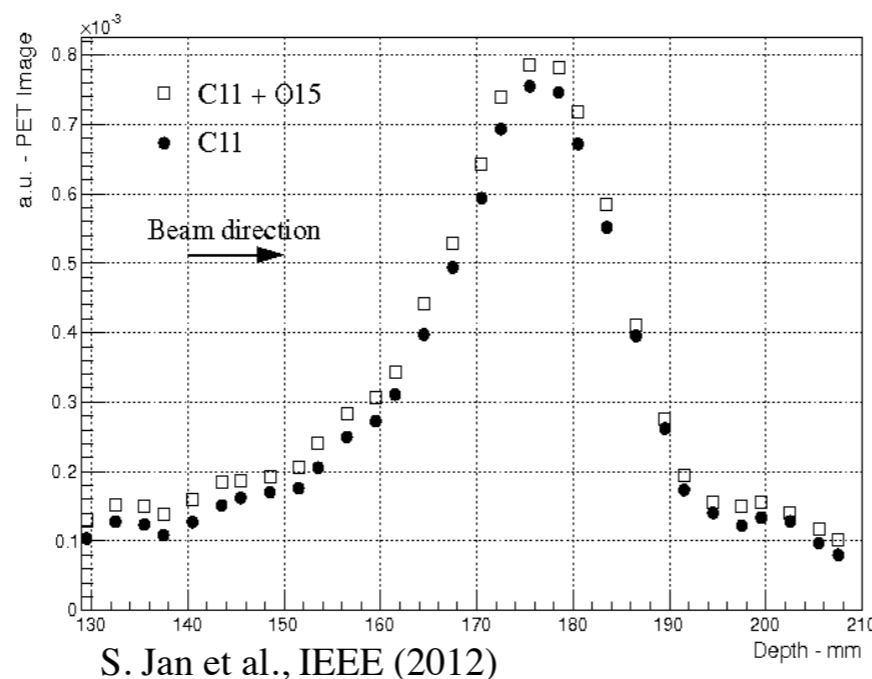
- Prompt gamma method reconstruction



- Secondary particle vertex reconstruction



- Inline PET reconstruction

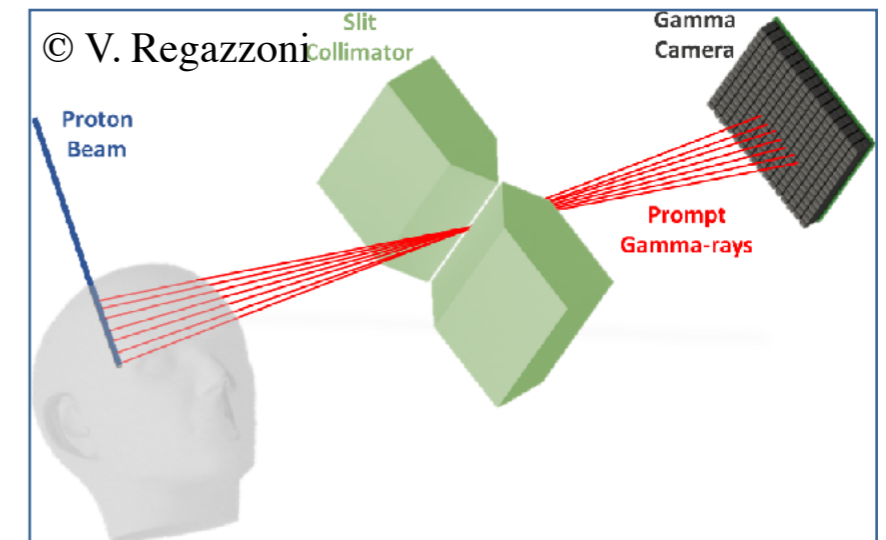
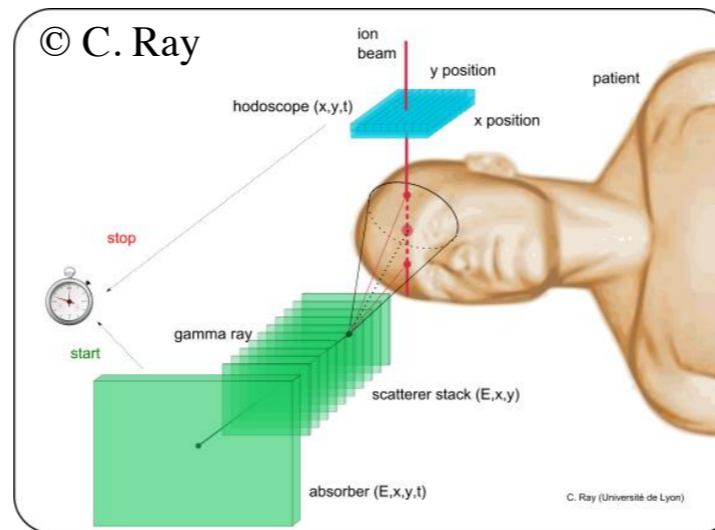
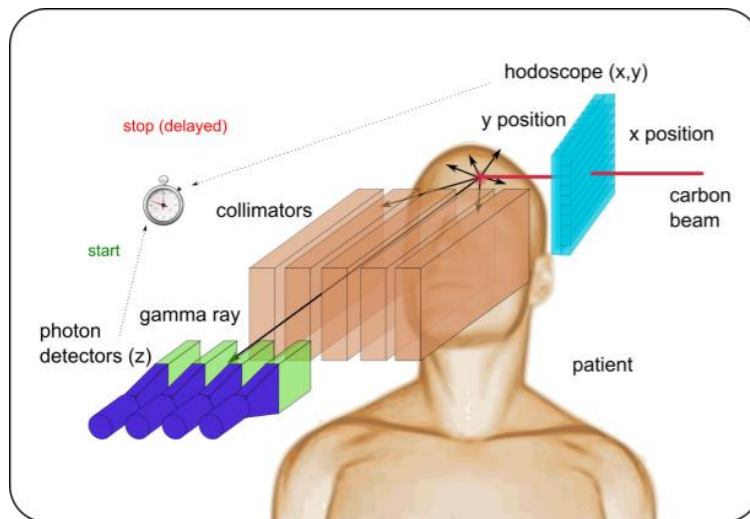


➡ Tag the Bragg peak at best ≈ 1 mm

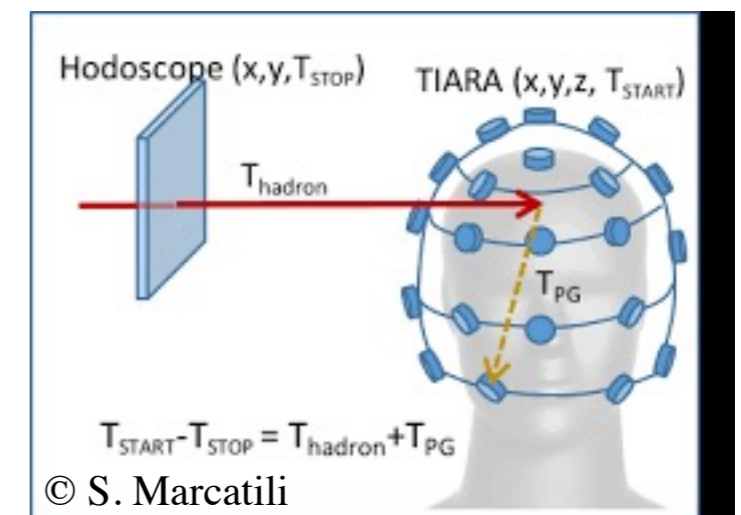
Online dose control (ii)

□ Prompt gamma method reconstruction

- Collimated, slitted devices or Compton camera



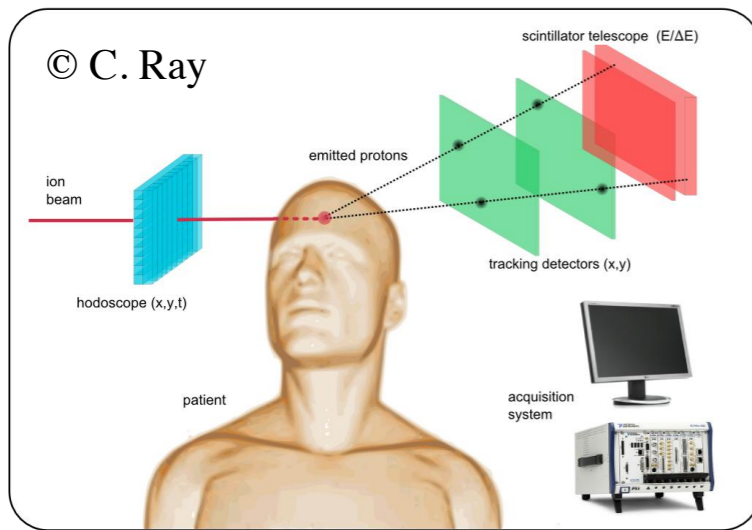
- ➔ Since low statistics need efficient crystal
- ➔ Fast time response if time gating
- ➔ Good energy resolution if ray tagging
- ➔ Mostly used: NaI, LYSO, most recently PbF_2
- ➔ good compromise btw properties and prices



Online dose control (iii)

□ Secondary particle vertex reconstruction

- Using silicon tracking device to reconstruct vertices

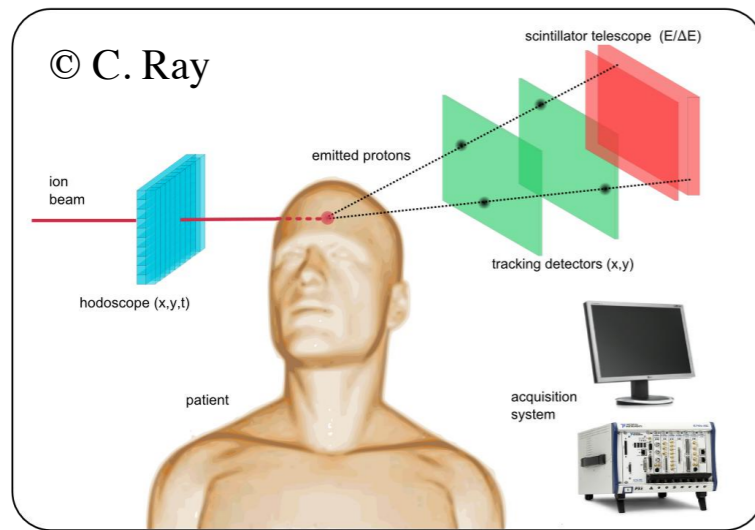


- ➔ Since low statistics need efficient sensor
- ➔ Good spatial resolution
- ➔ Pixelised silicon detector

Online dose control (iii)

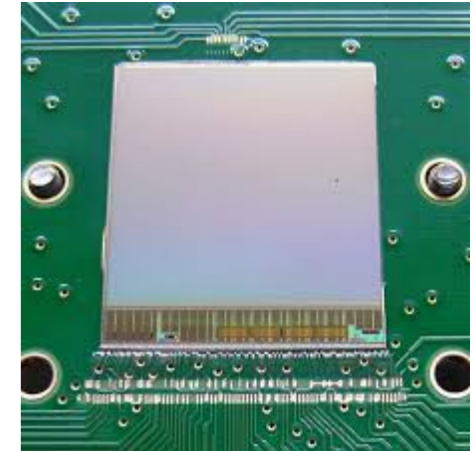
□ Secondary particle vertex reconstruction

- Using silicon tracking device to reconstruct vertices

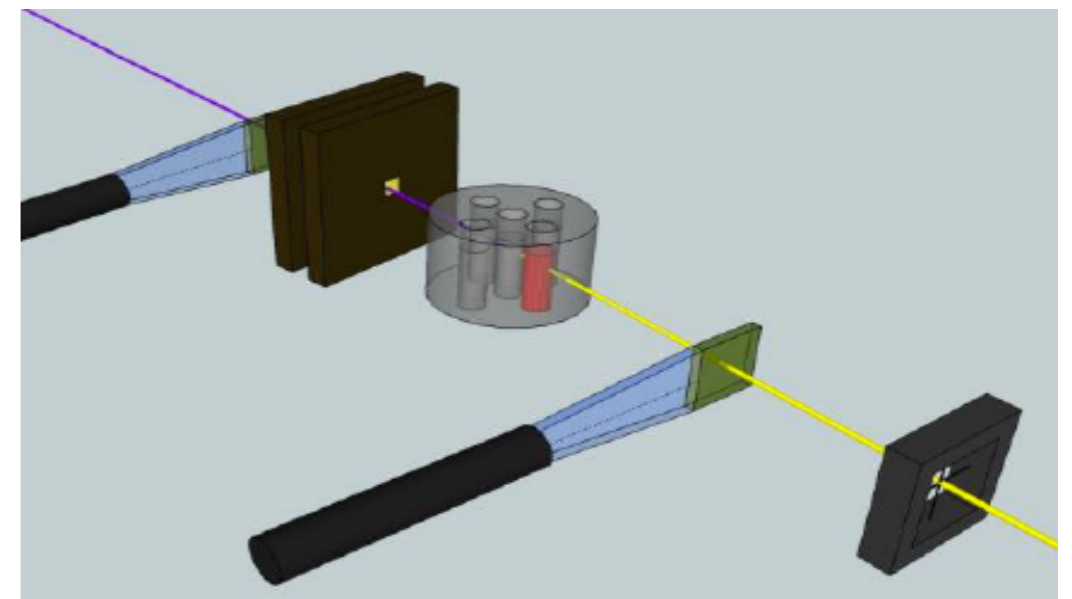


• Example M28

- Area 2x2 cm²
- 1 Mpixels
- Efficiency > 99 %
- Spatial resolution $\ll 10 \mu\text{m}$



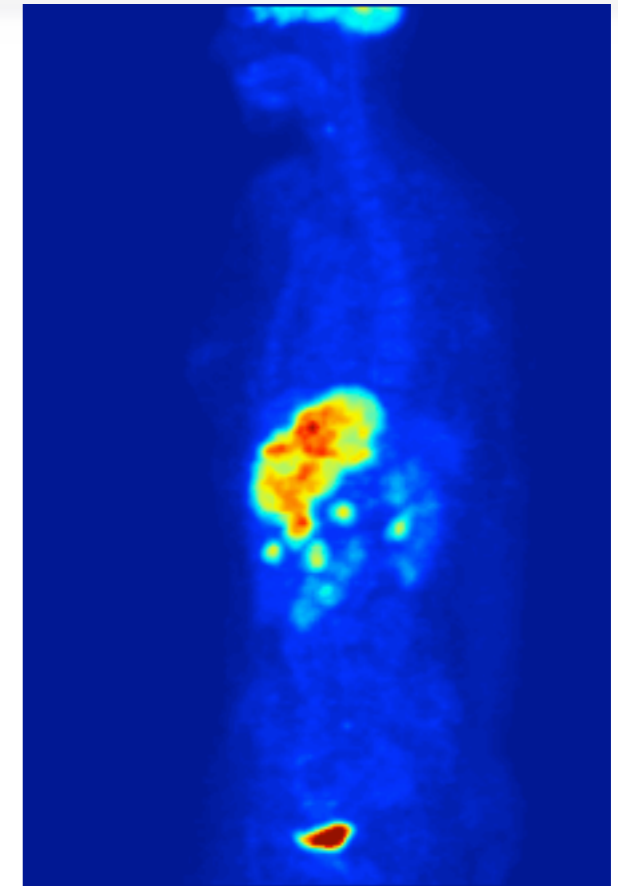
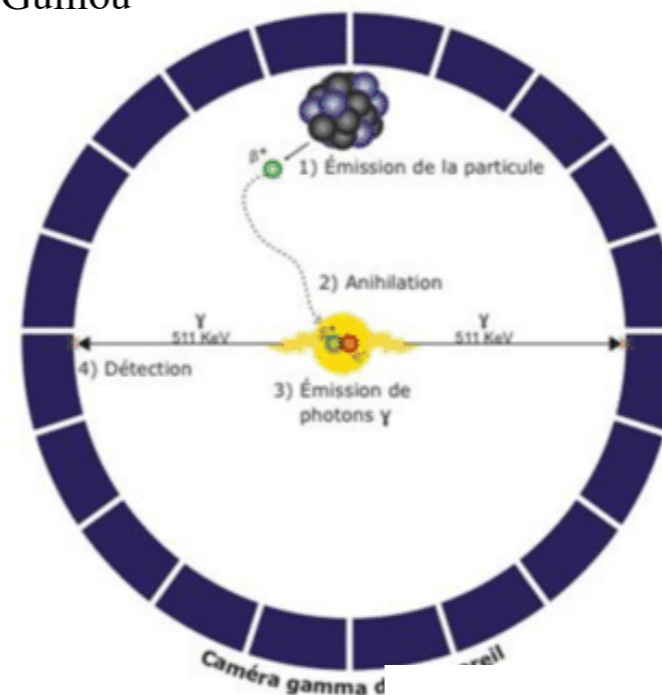
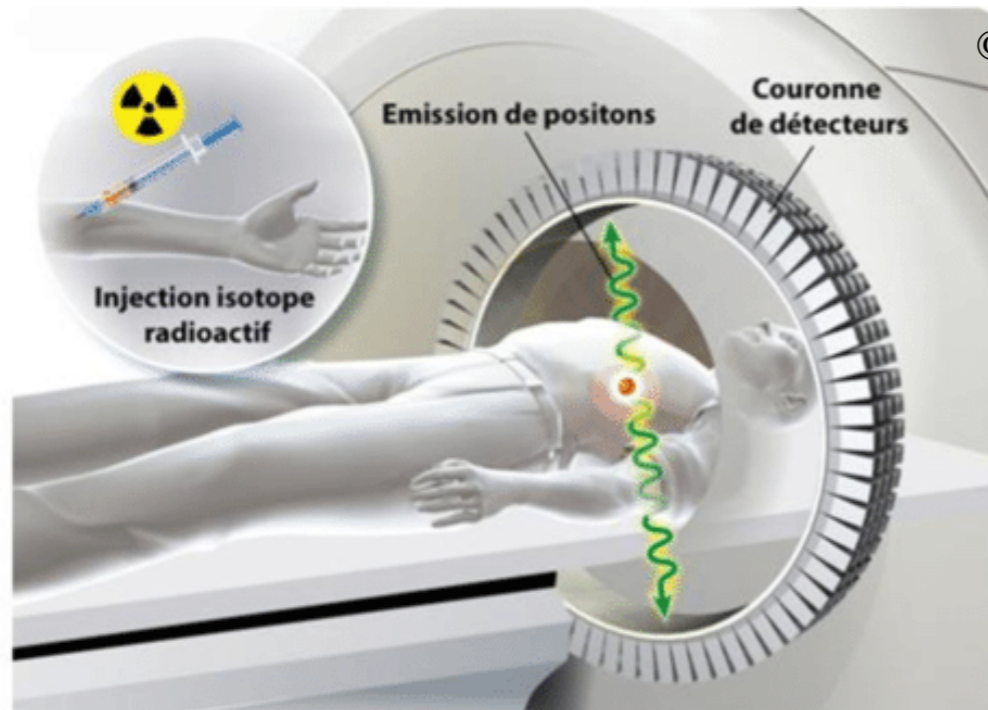
- ➔ Since low statistics need efficient sensor
- ➔ Good spatial resolution
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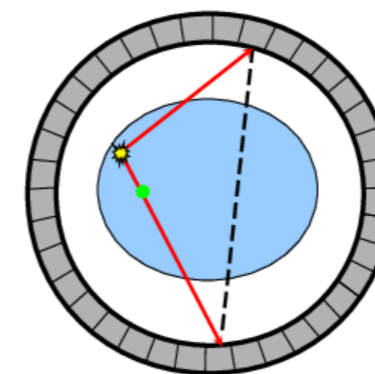
Online dose control/PET-Imaging

□ Inline (offline) Positron Emission Tomography reconstruction

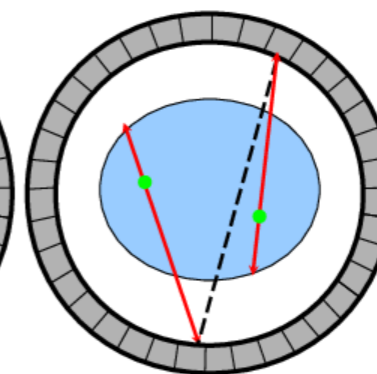
- Using the 511 keV γ -rays from annihilation β -decay with medium



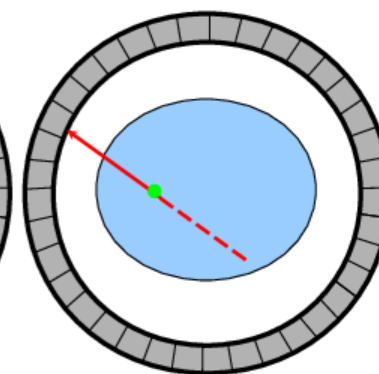
- Need to reconstruct the road of the two γ -rays
- Good timing resolution to avoid false reconstruction
- Wash out phenomena
- Need a 3D reconstruct (could take time)



Scattered coincidence



Random coincidence



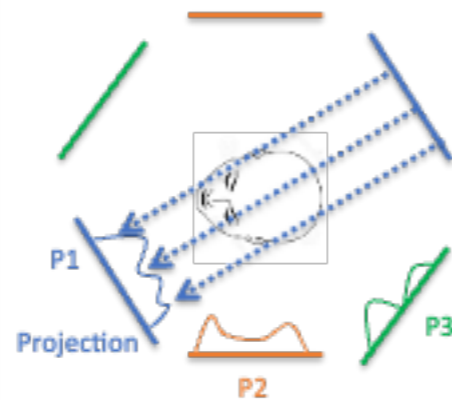
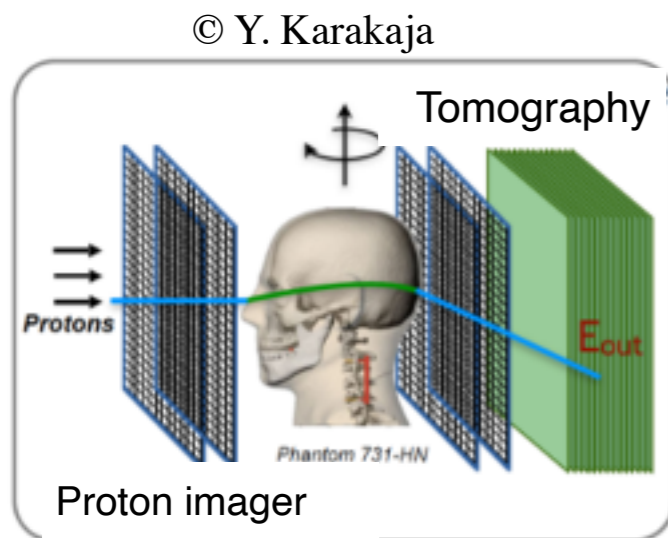
Attenuation

➔ Mostly used: LYSO, good comprise btw properties and prices

pCT-Imaging

□ Proton(carbon)-computed tomography

- Using same particle for treatment and imaging (avoid conversion)



Sinogram



A. C. Kak and Malcolm Slaney (2001)

Proton
Tomography
Imaging



Vladimir A. B et al . (2016)

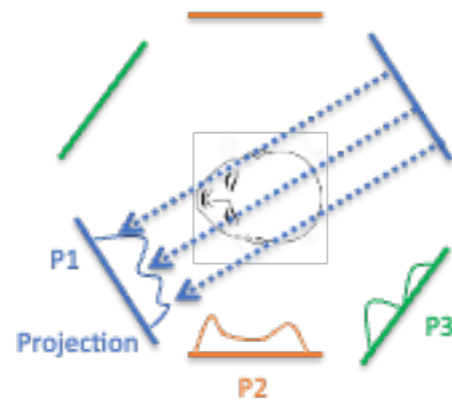
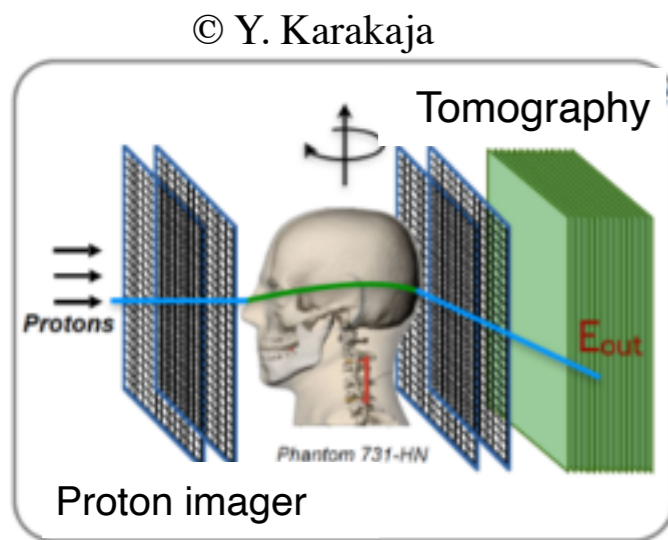
Reconstruction

- Need to reconstruct the most probable part of protons
 - ➔ Fast tracking system
 - ➔ Good resolution on energy or path

pCT-Imaging

□ Proton(carbon)-computed tomography

- Using same particle for treatment and imaging (avoid conversion)



Sinogram



A. C. Kak and Malcolm Slaney (2001)

Proton Tomography Imaging



Vladimir A. B et al. (2016)

- Need to reconstruct the most probable part of protons

- ➔ Fast tracking system

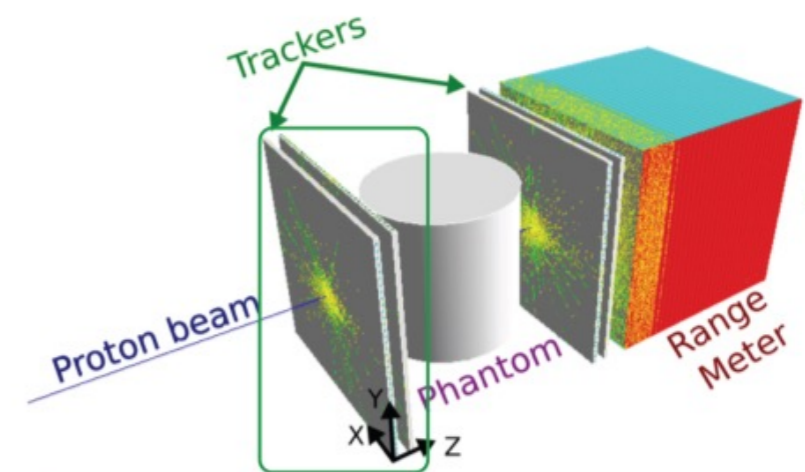
- ➔ Good resolution on energy or path

- ➔ Mostly proposed:

- Tracking: Scintillating fibers diameter < 1 mm

- Residuals: (stack of) scintillators for energy or range-meter

Reconstruction



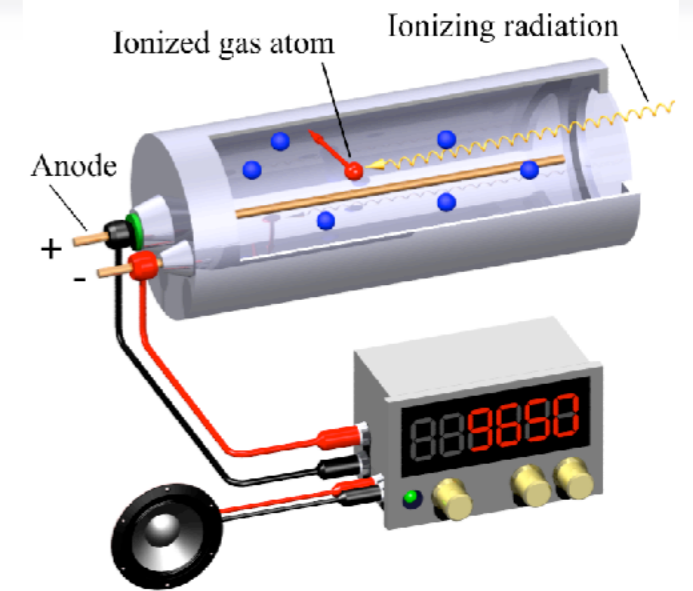
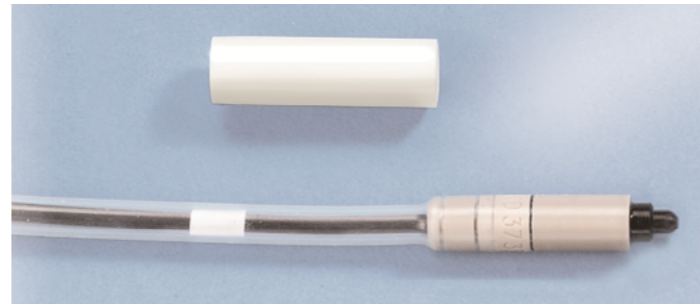
Geant4 simulation

Dosimetry

Using different type of detector for different purpose

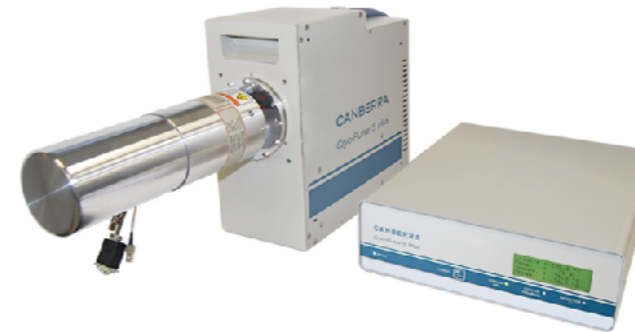
- Geiger-Müller counter
 - Simple ionisation wired tube
 - Count number of interaction (wide range in energy/particle)

- Ionisation chamber (see before)
 - Give an good dose measurement
 - Wide dynamic range



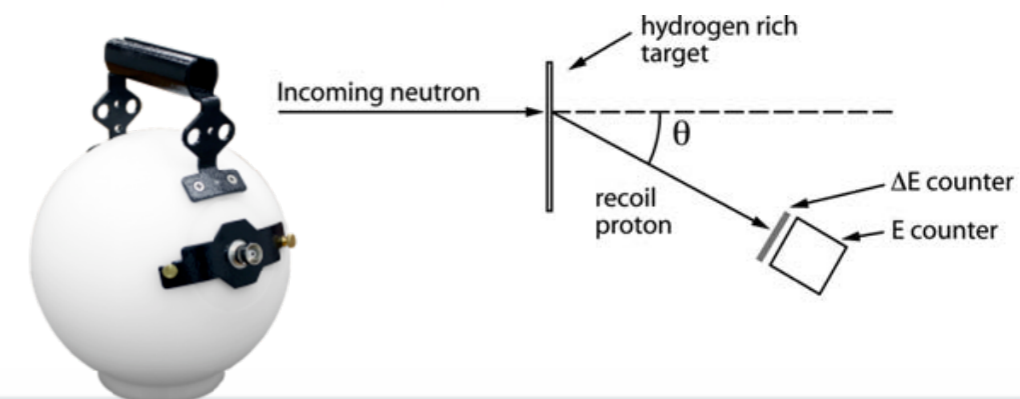
• Etc...

- Semi-conductors
 - Use for γ -spectroscopy (isotope identification)
 - Accurate energy resolution



- Proton recoiled neutron detector
 - Using a converter (hydrogenated)
 - Detect the proton to reconstructed neutron properties:

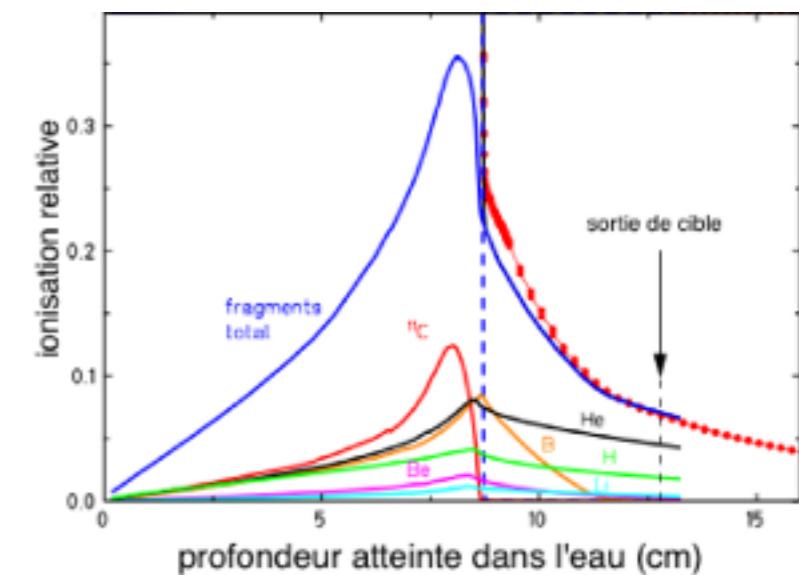
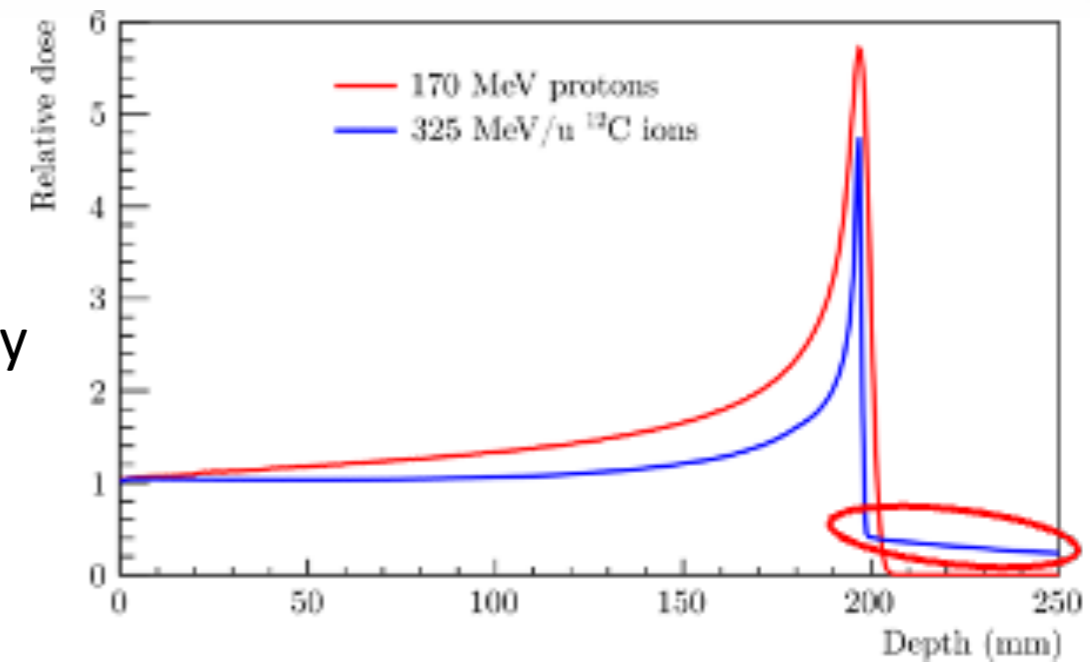
$$E_n = E_p / \cos^2(\theta)$$



Cross-section measurement (i)

□ Nuclear reactions during hadrontherapy (^{12}C and ^{16}C)

- During treatment $\sim 50\%$ of beam loss due to reactions
- Extra dose after Bragg peak
- Need to measure cross-section as function of angle/energy



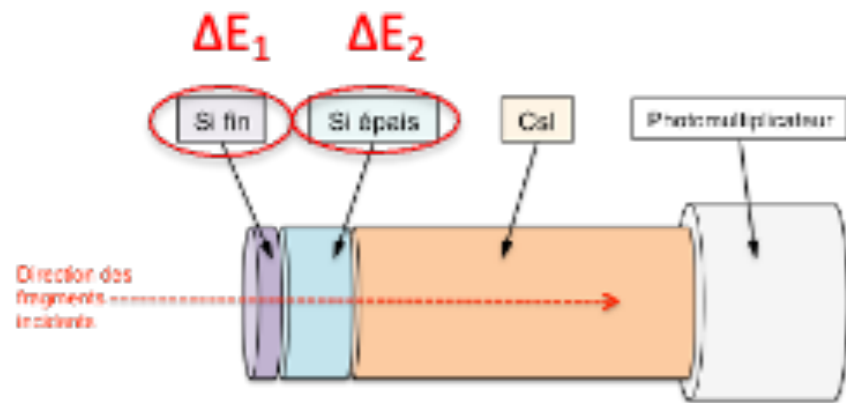
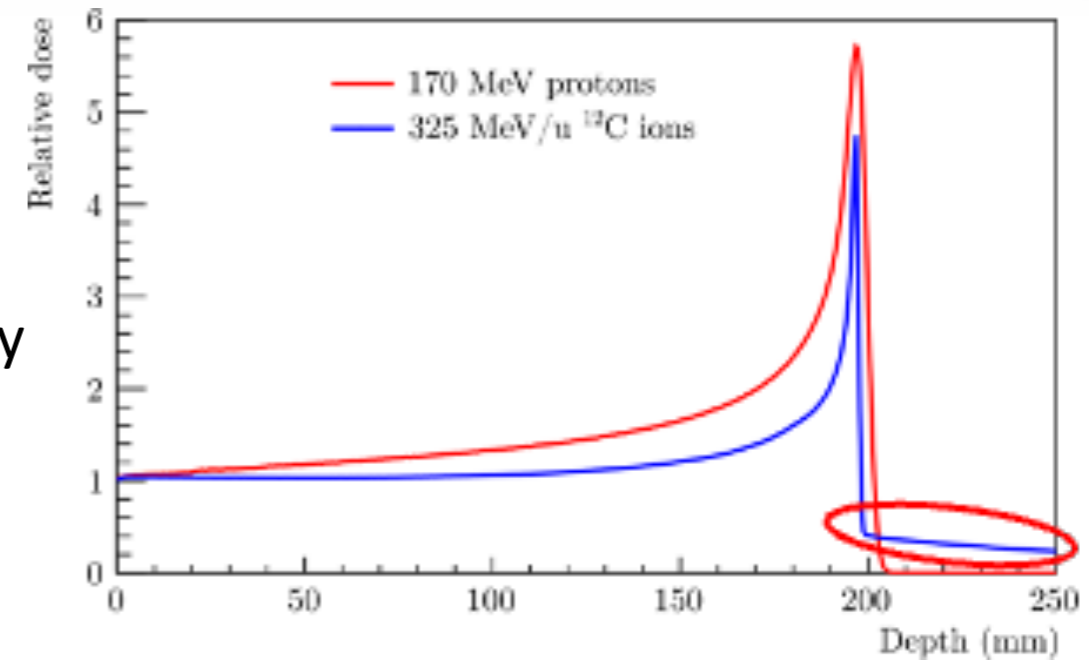
Cross-section measurement (i)

□ Nuclear reactions during hadrontherapy (^{12}C and ^{16}C)

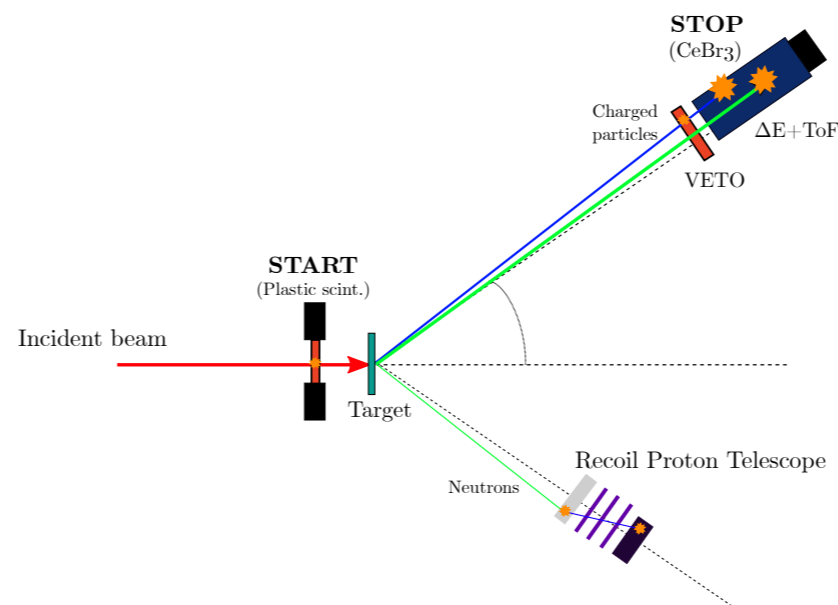
- During treatment $\sim 50\%$ of beam loss due to reactions
- Extra dose after Bragg peak
- Need to measure cross-section as function of angle/energy

□ Exclusive measurements (i)

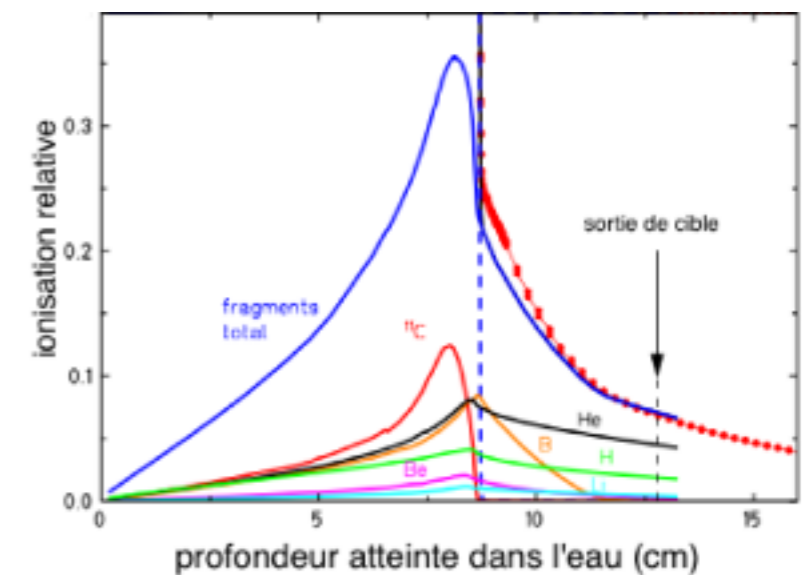
- Placing detector at given angles
- Using $\Delta E_1(-\Delta E_2)$ -E telescope or ΔE -ToF telescope for isotope Id



E600 experiment @ Ganil



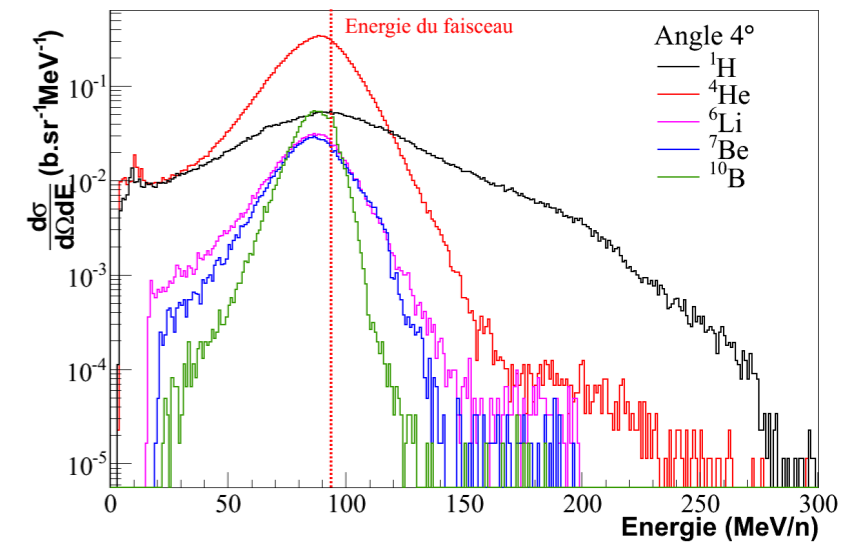
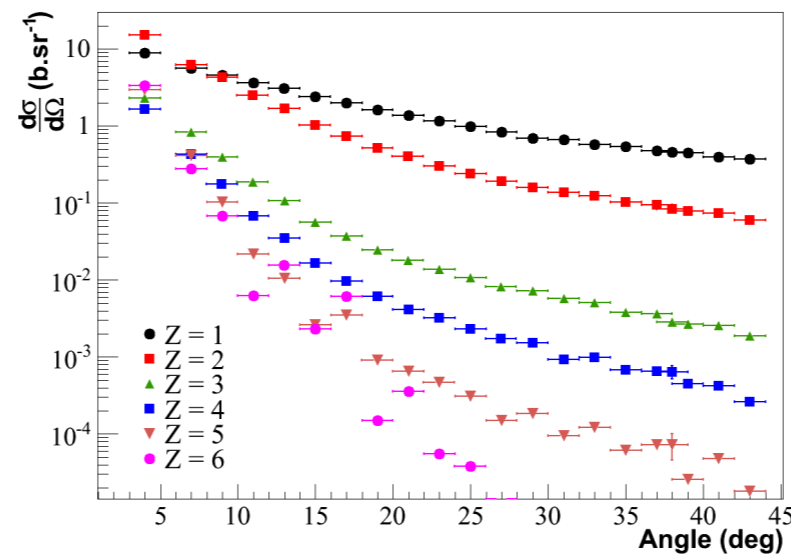
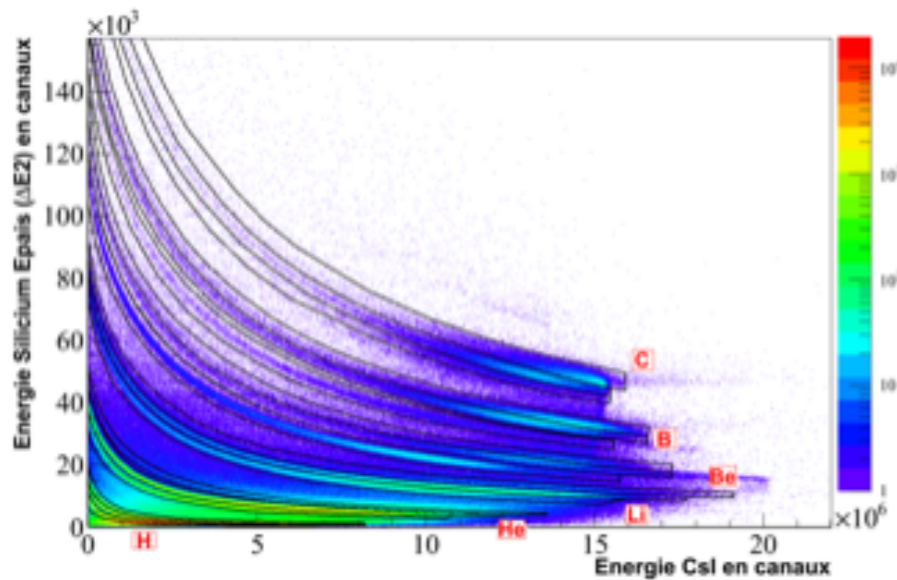
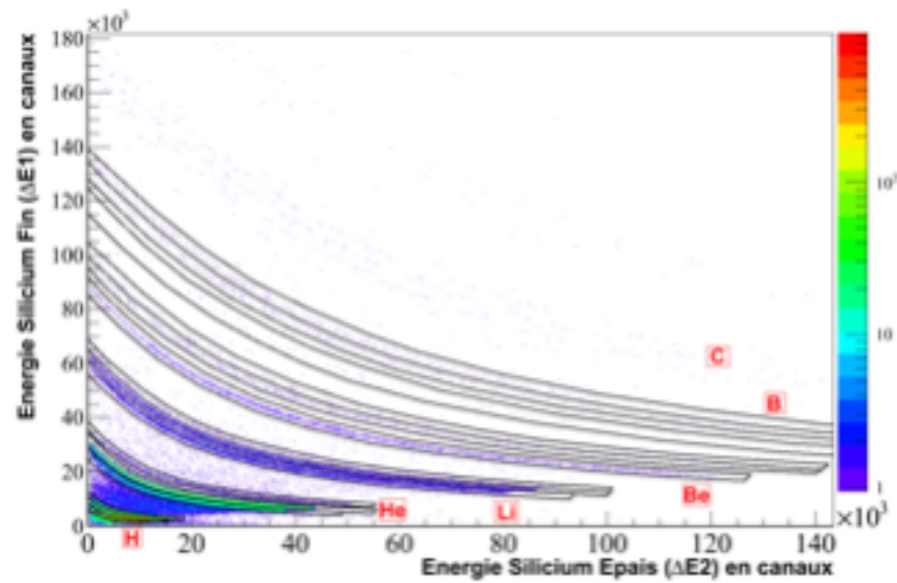
CLINM experiment @ CNAO



Cross-section measurement (ii)

Exclusive measurements (ii):

Results (highlights):

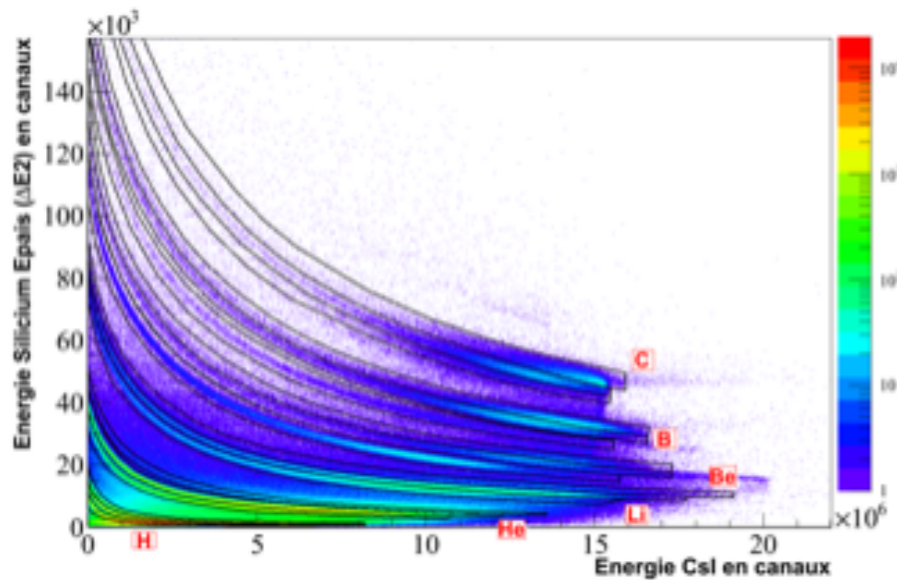
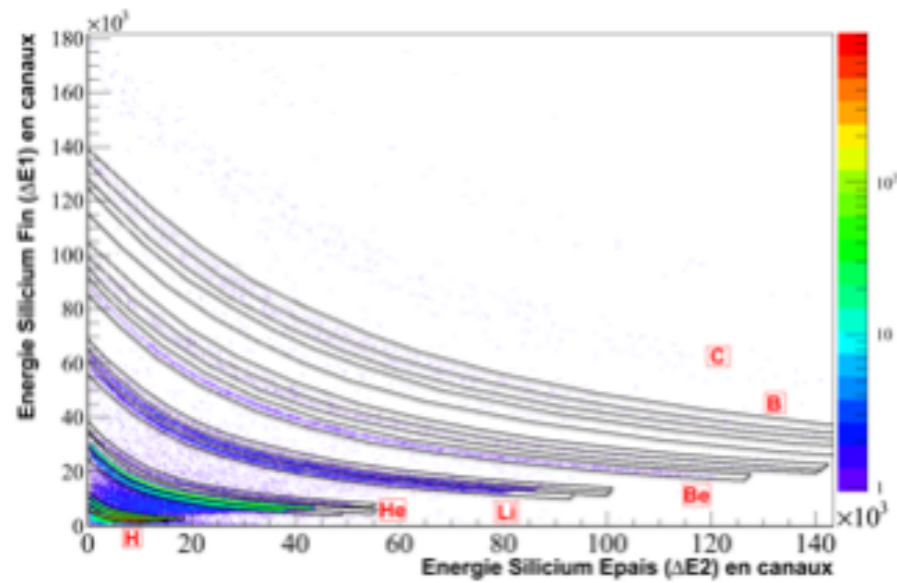


E600 experiment @ Ganil (D. Juliani)
 $^{12}\text{C}+^{12}\text{C}$ @ 95MeV/u

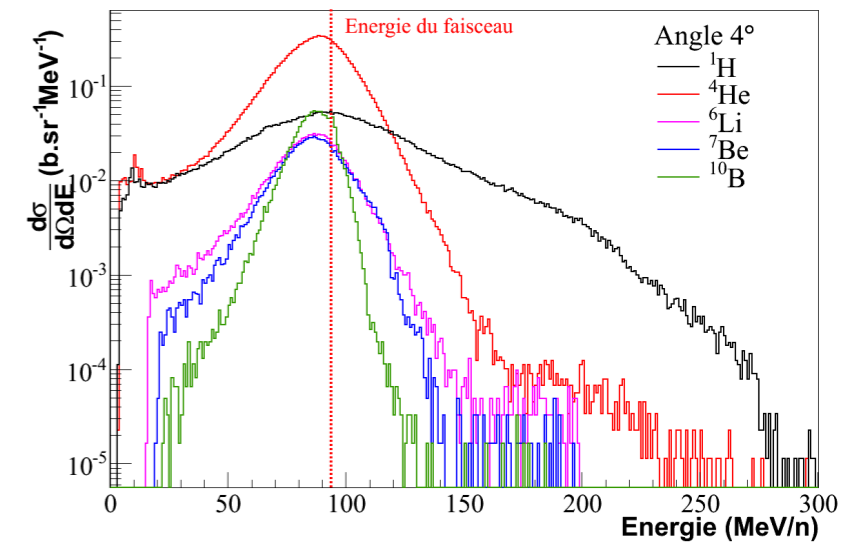
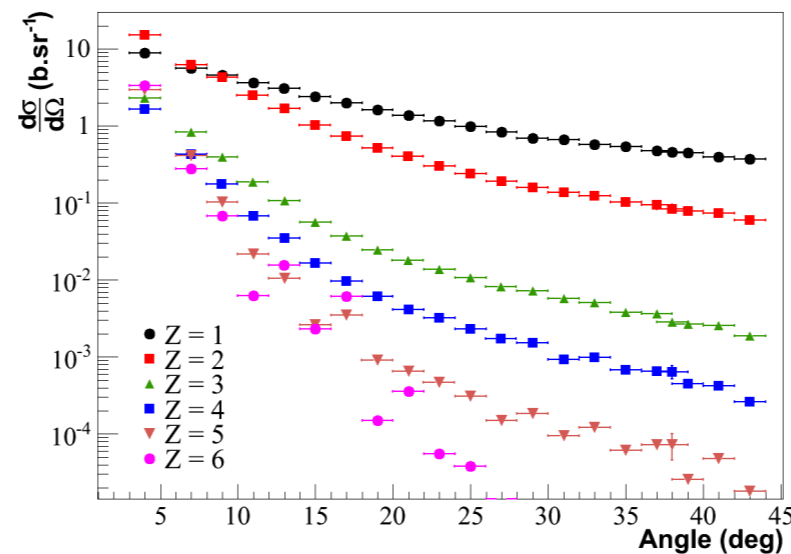
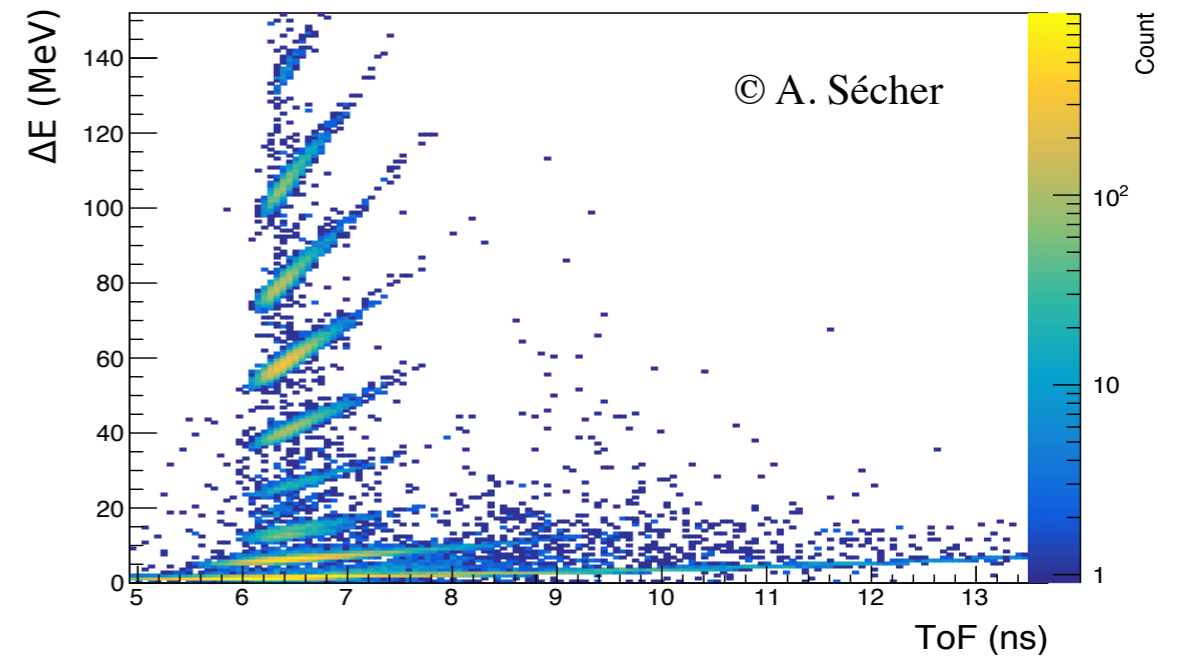
Cross-section measurement (ii)

Exclusive measurements (ii):

Results (highlights):



CLINM experiment (Geant4 simulation)



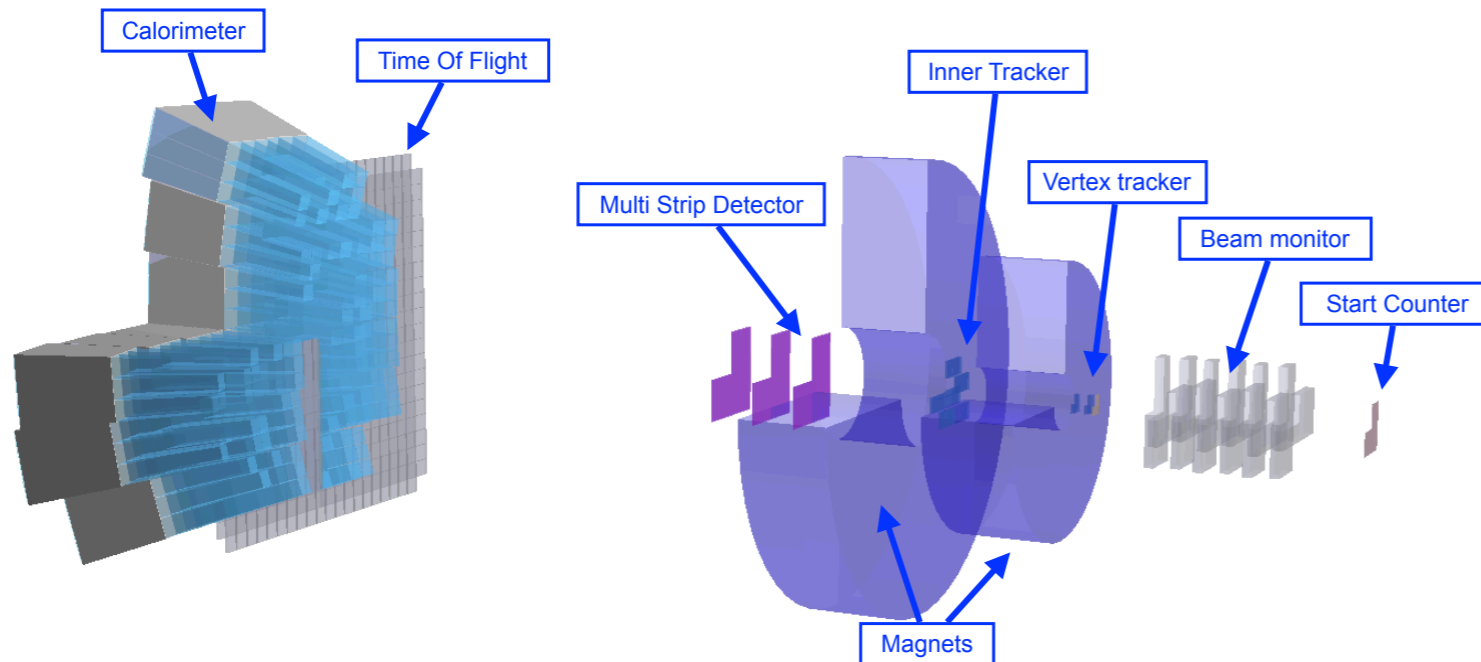
E600 experiment @ Ganil (D. Juliani)
 $^{12}\text{C}+^{12}\text{C}$ @ 95MeV/u

Cross-section measurement (iii)

☐ Inclusive measurements:

- Full coverage for a given angular acceptance
- Need different type of detector

FOOT experiment @ CNAO



- Beam monitoring: drift chamber
- Tracking system: silicon pixel and strip detector
- Momentum reconstruction: Permanent magnet
- Time of flight: plastic scintillators
- Calorimeter: BGO crystal

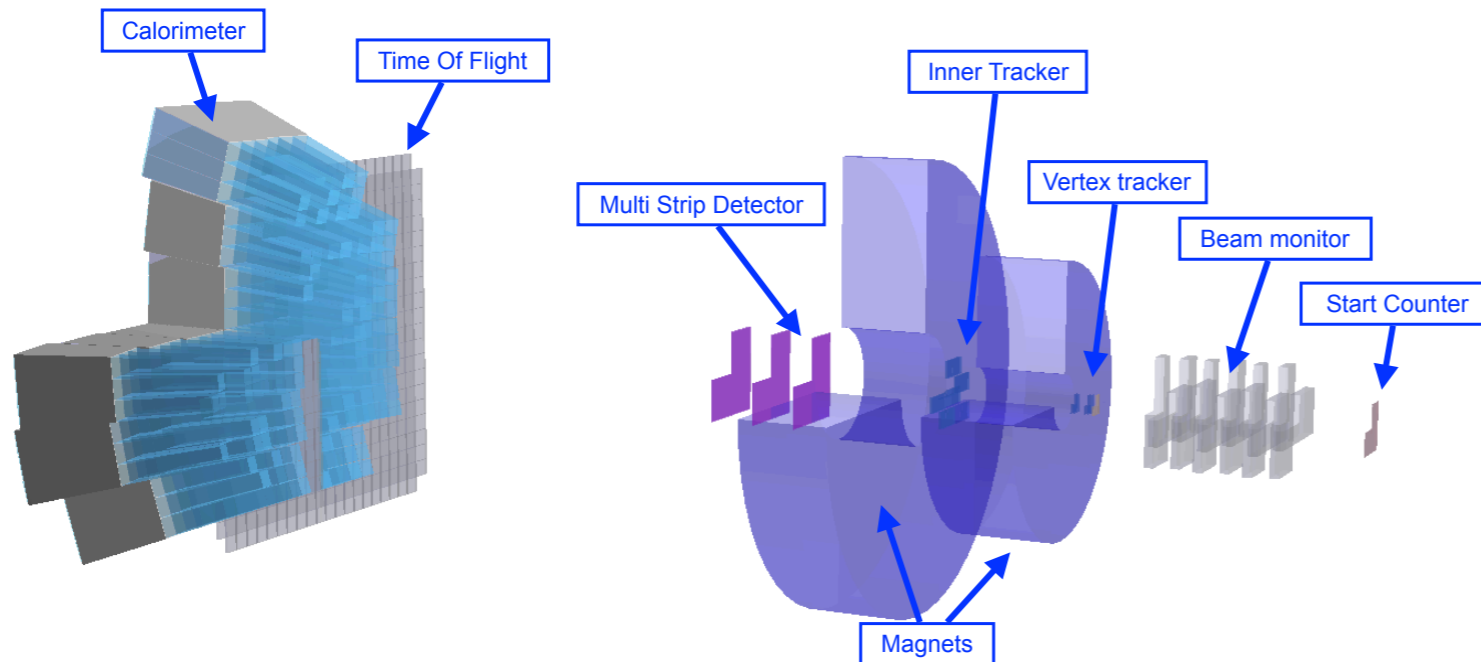
Cross-section measurement (iii)

☐ Inclusive measurements:

- Full coverage for a given angular acceptance
- Need different type of detector

• Results (highlights)

FOOT experiment @ CNAO



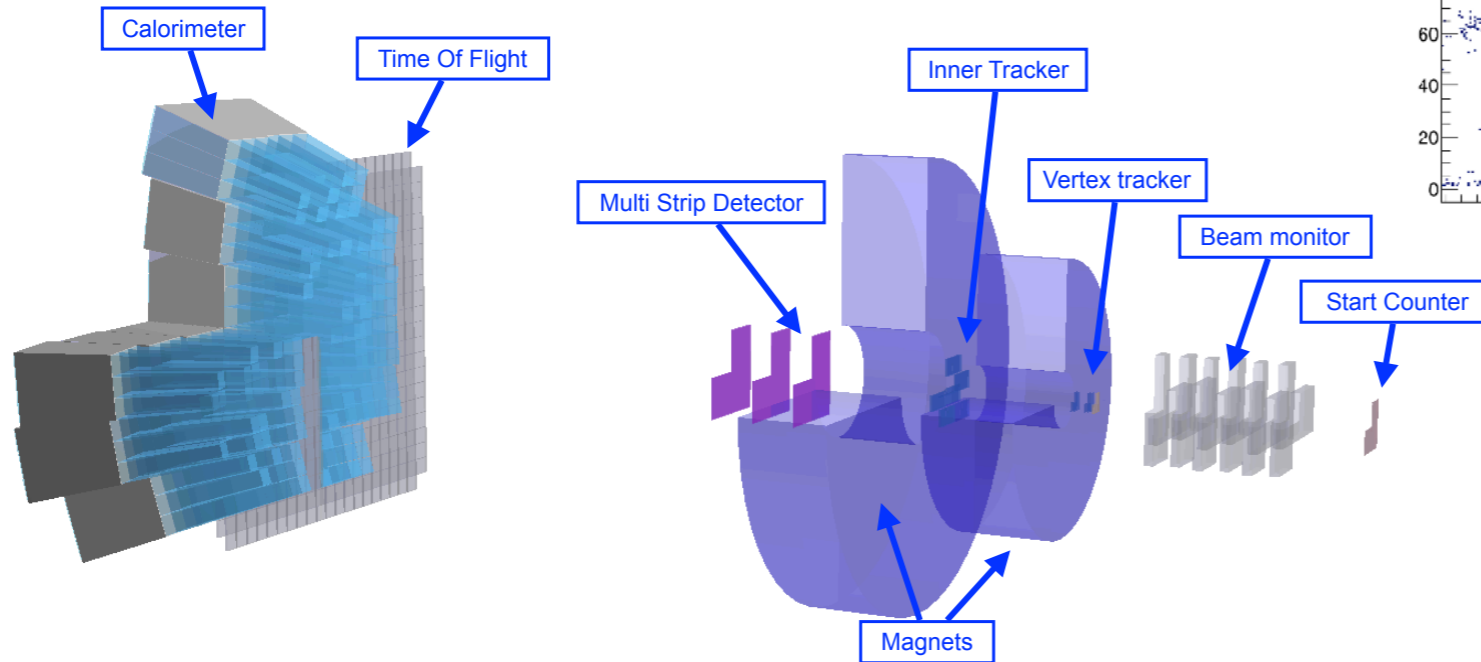
- Beam monitoring: drift chamber
- Tracking system: silicon pixel and strip detector
- Momentum reconstruction: Permanent magnet
- Time of flight: plastic scintillators
- Calorimeter: BGO crystal

Cross-section measurement (iii)

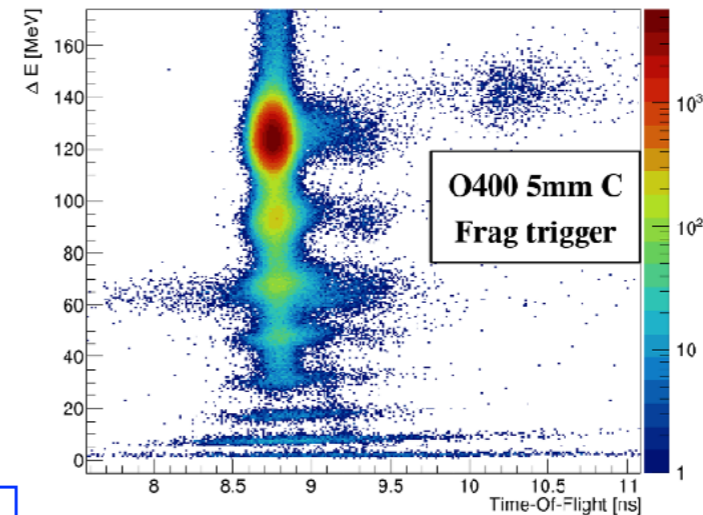
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FOOT experiment @ CNAO



• Results (highlights)



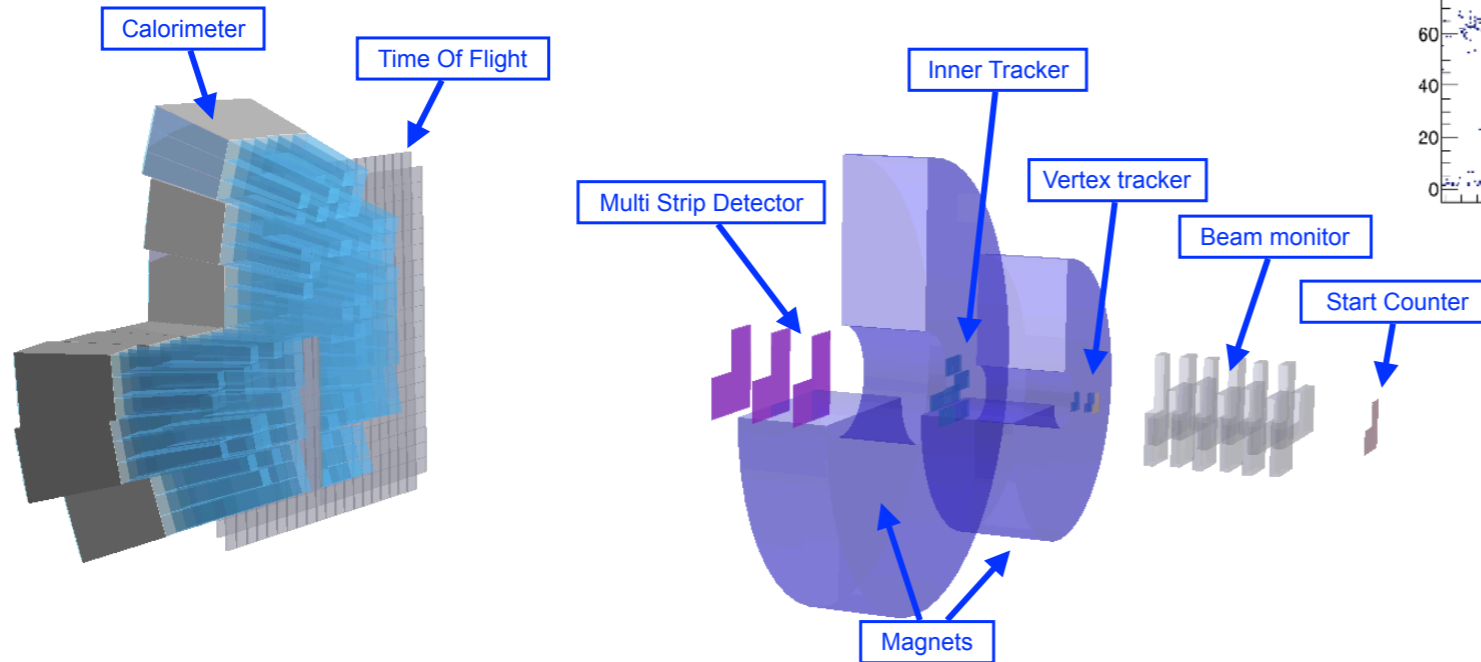
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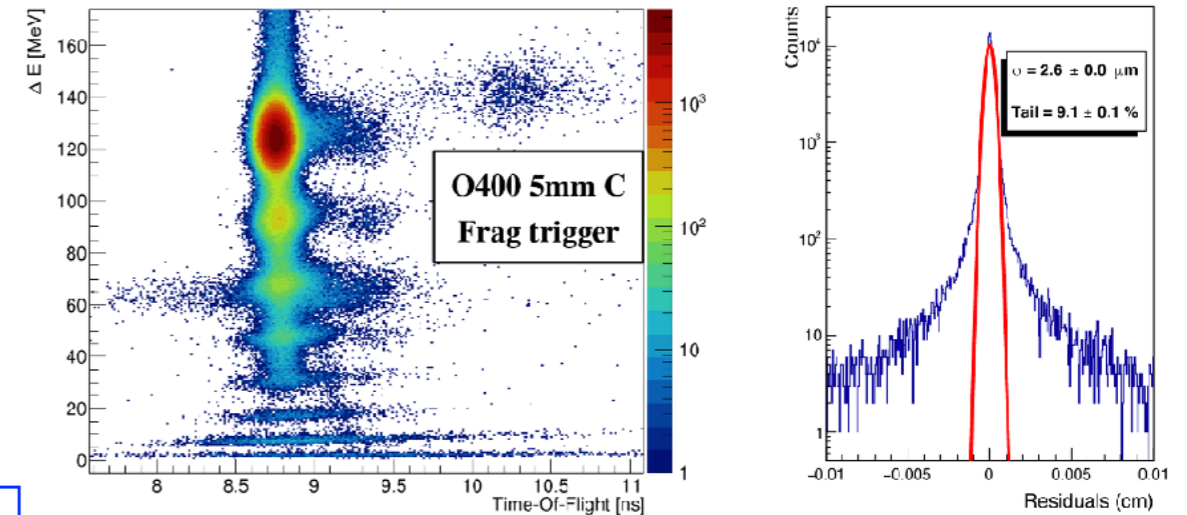
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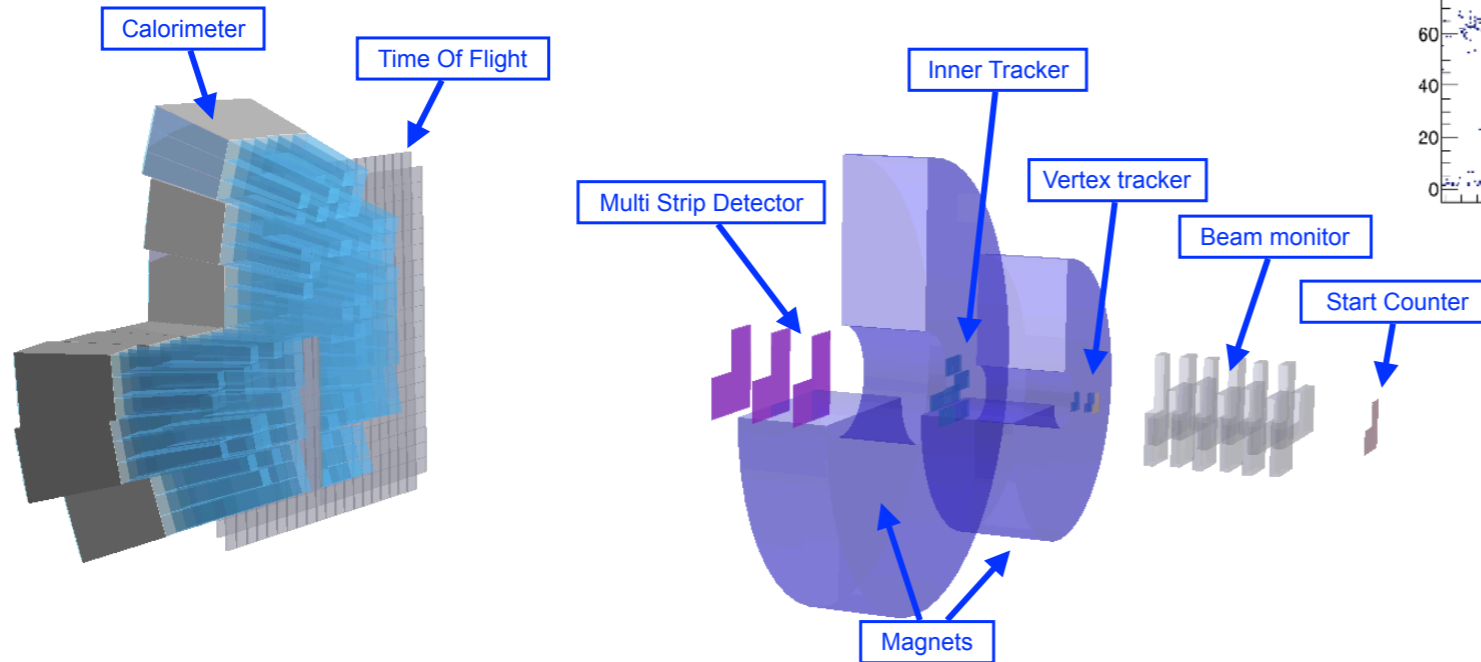


Cross-section measurement (iii)

Inclusive measurements:

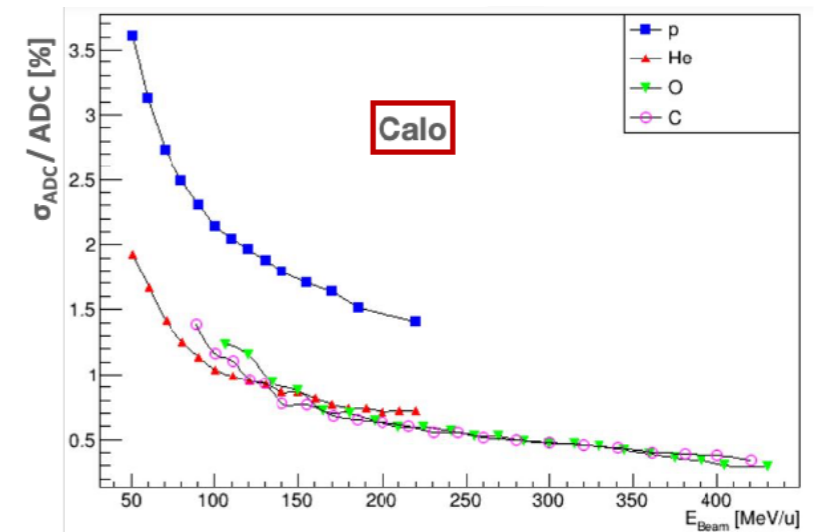
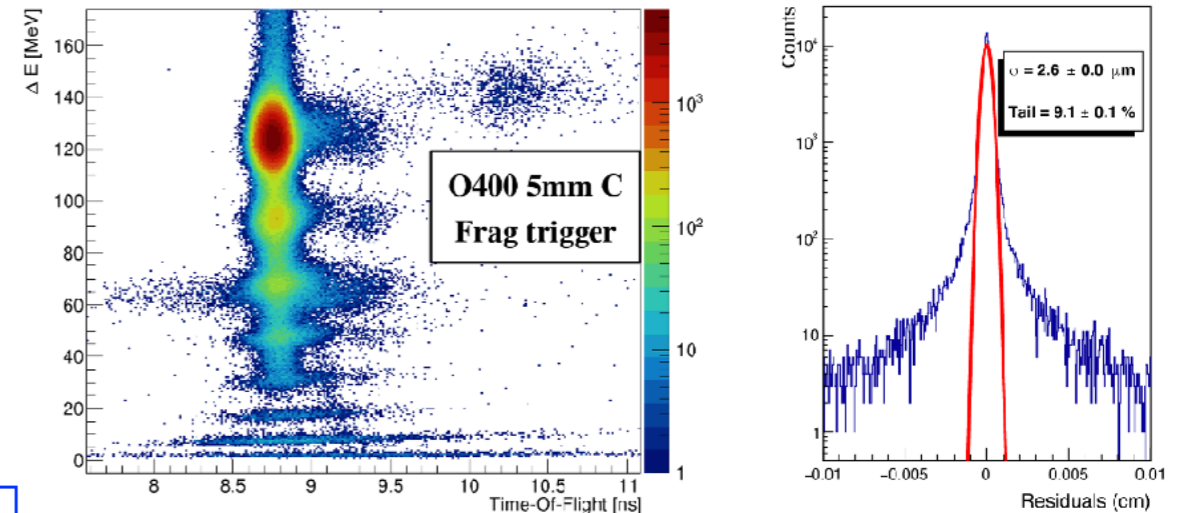
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Results (highlights)

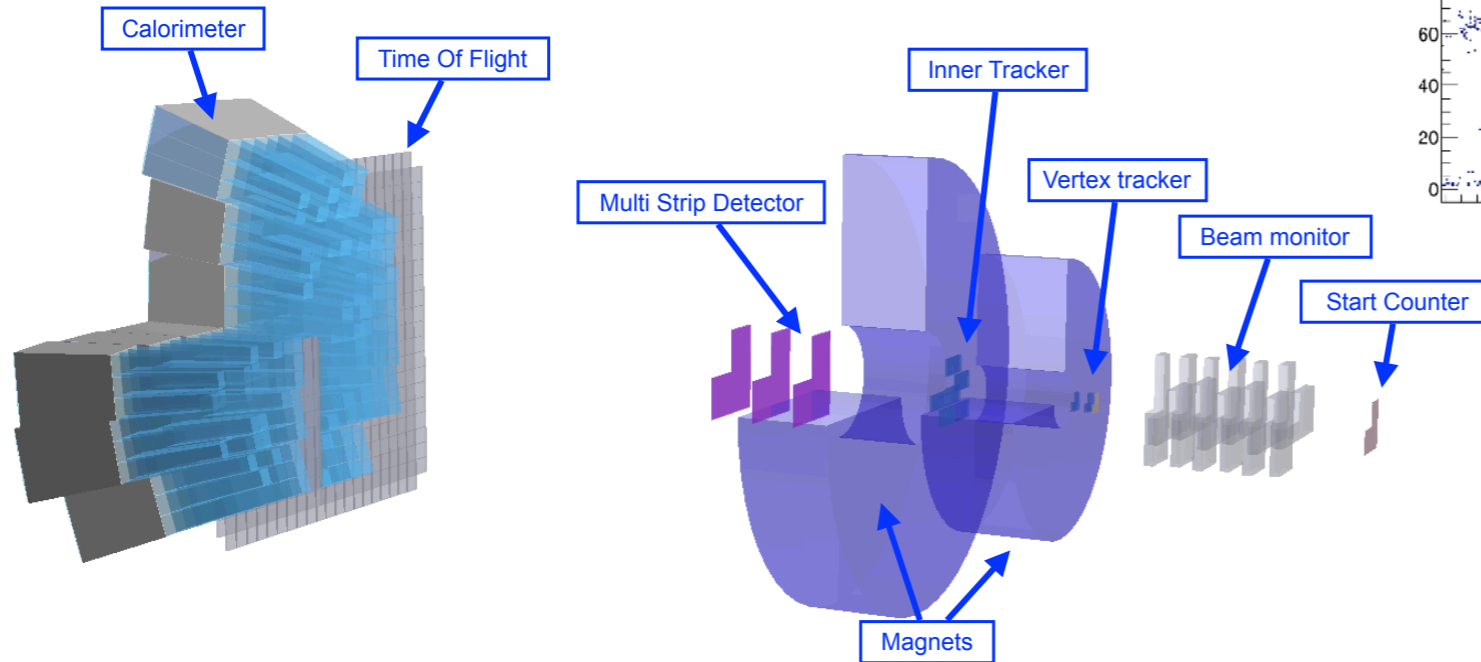


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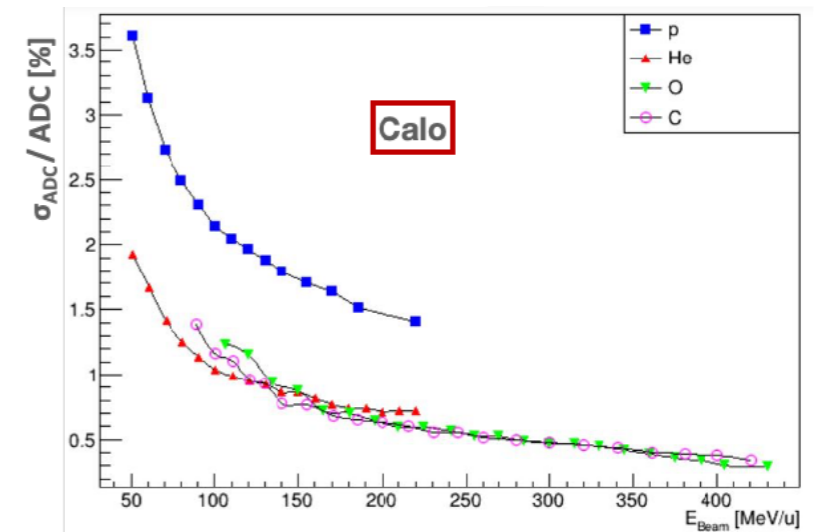
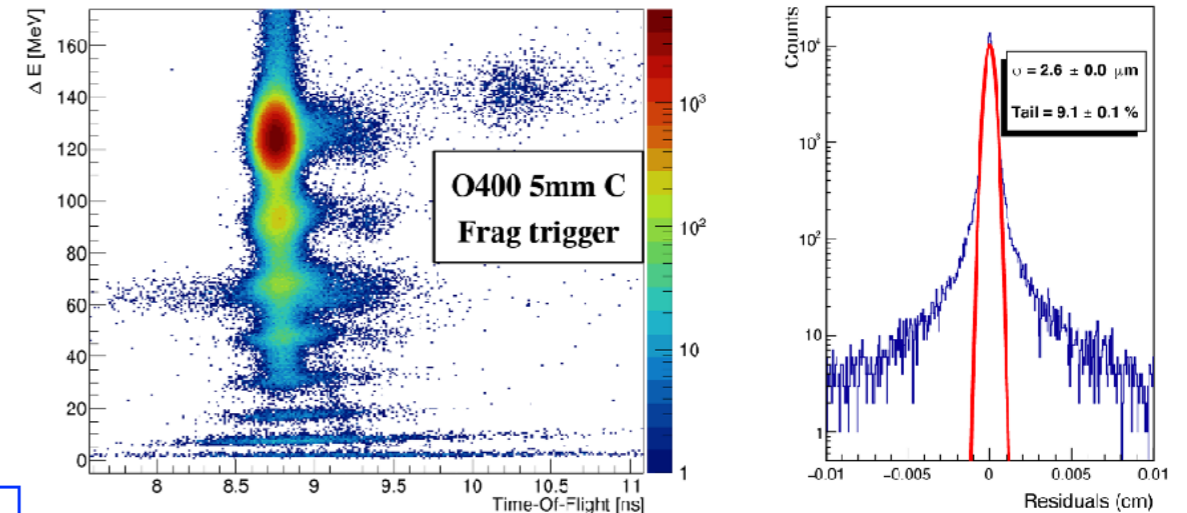
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FOOT experiment @ CNAO



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Results (highlights)



Required performances:

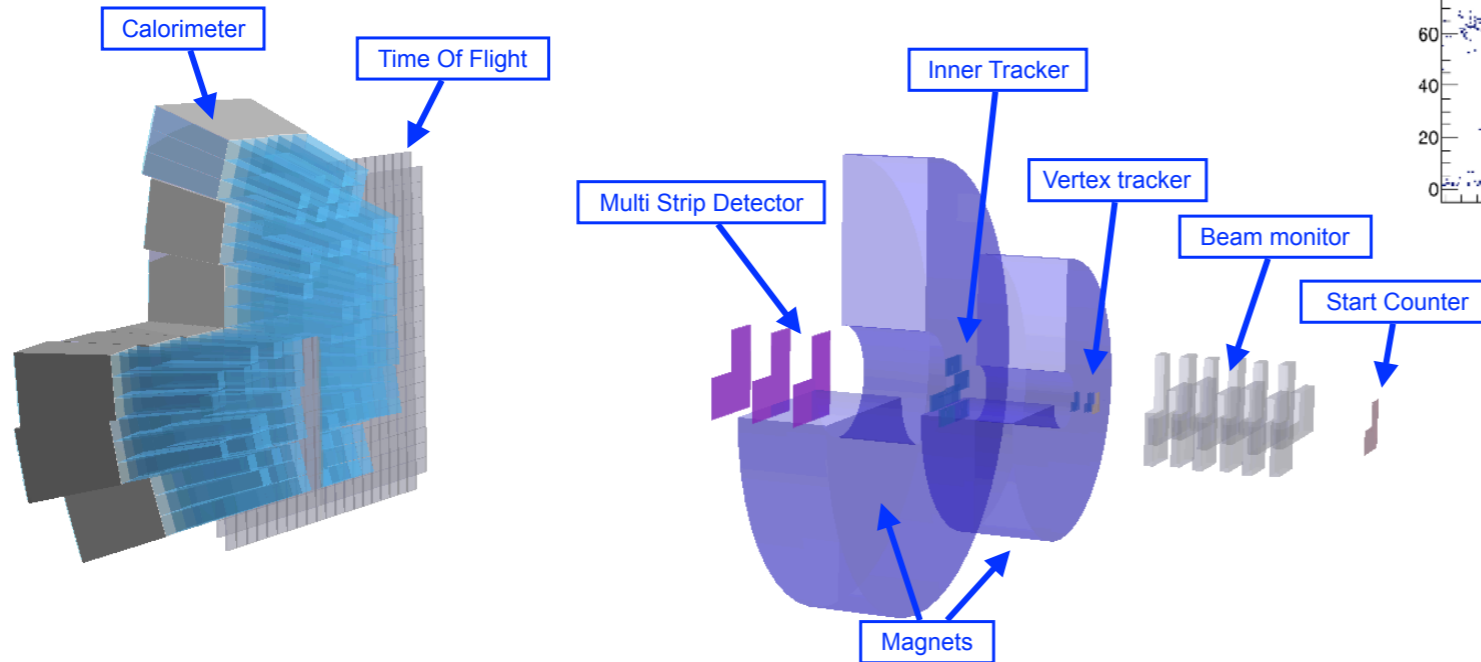
- $\sigma(p)/p < 5\%$
- $\sigma(\Delta E)/E < 5\%$
- $\sigma(ToF) < 50 ps$

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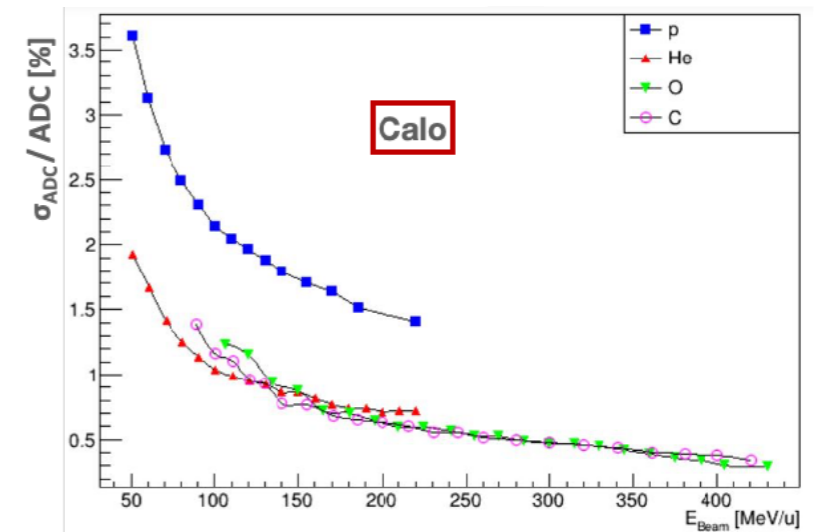
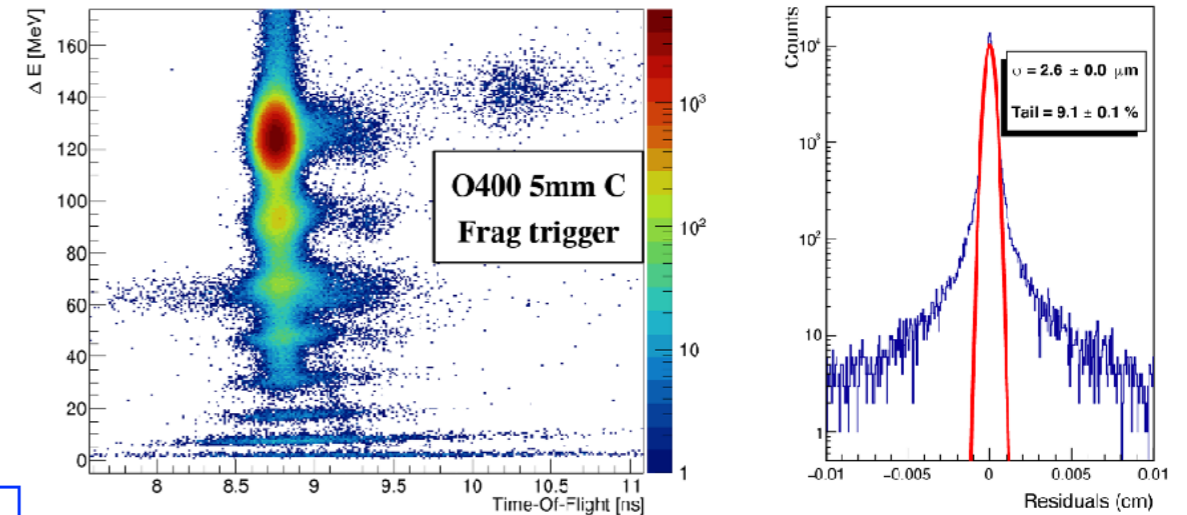
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Results (highlights)



Required performances:

- $\sigma(p)/p < 5\%$
- $\sigma(\Delta E)/E < 5\%$
- $\sigma(ToF) < 50 ps$

➔ Analysis ongoing

Conclusions

□ In many fields (not all covered here) in medical applications, nuclear physics detectors are used

- Beam monitoring
- PET-SPECT-pCT Imaging
- Cross-section measurement
- Online dose control
- Dosimetry
- Etc....

Outlooks

- Also many fields were still improvement and development are need to face existing or forthcoming challenges:
 - Beam monitoring: flash therapy
 - ➔ Sustain high flux in a short time (40-100 Gy/s)
 - PET-pCT Imaging:
 - ➔ increase time resolution and decrease acquisition time
 - Online dose control:
 - ➔ Increase Bragg peak correlation resolution (new technique / new detectors ?)
 - Cross-section measurement:
 - ➔ Increase the number of measurements, including the existing data in TPS
 - Dosimetry:
 - ➔ Increase sensitivity (neutrons for instance) and decrease acquisition time
 - Etc....

Backup