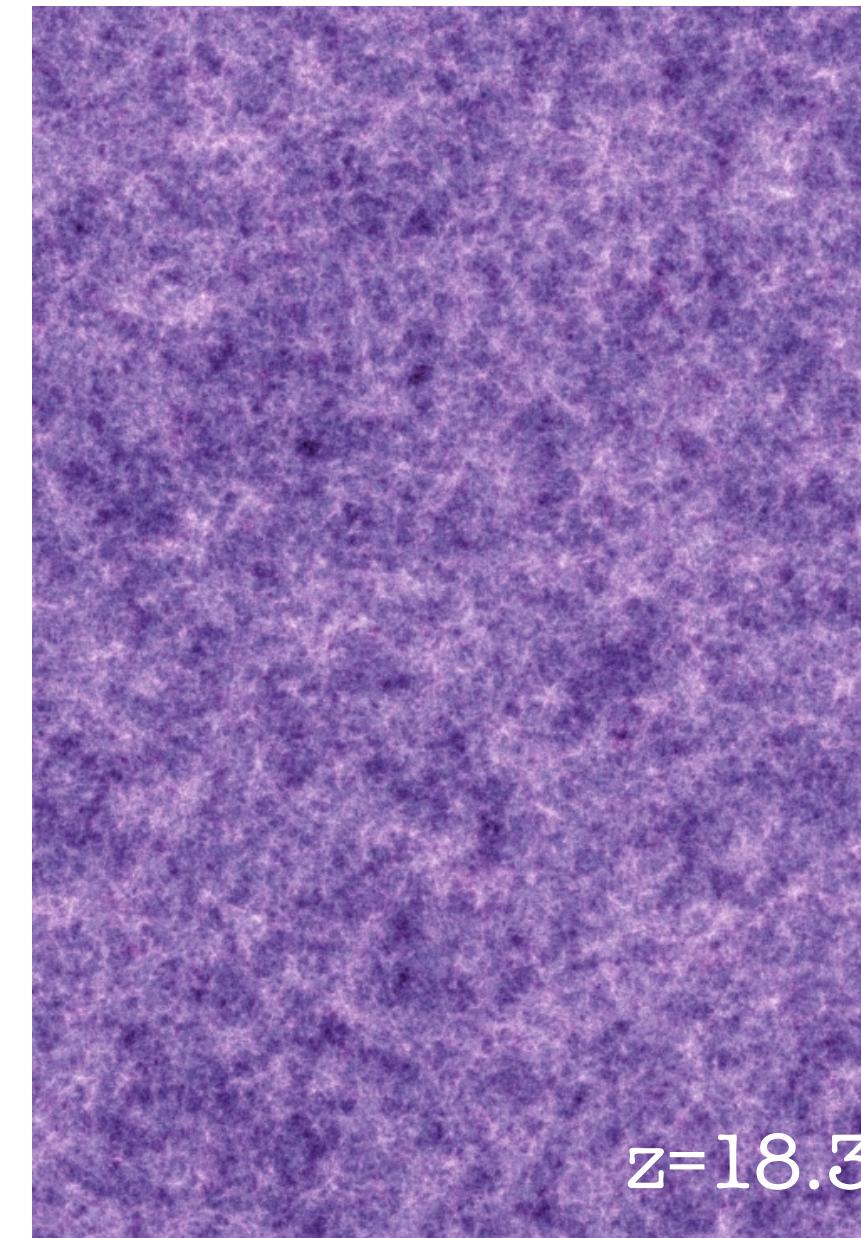
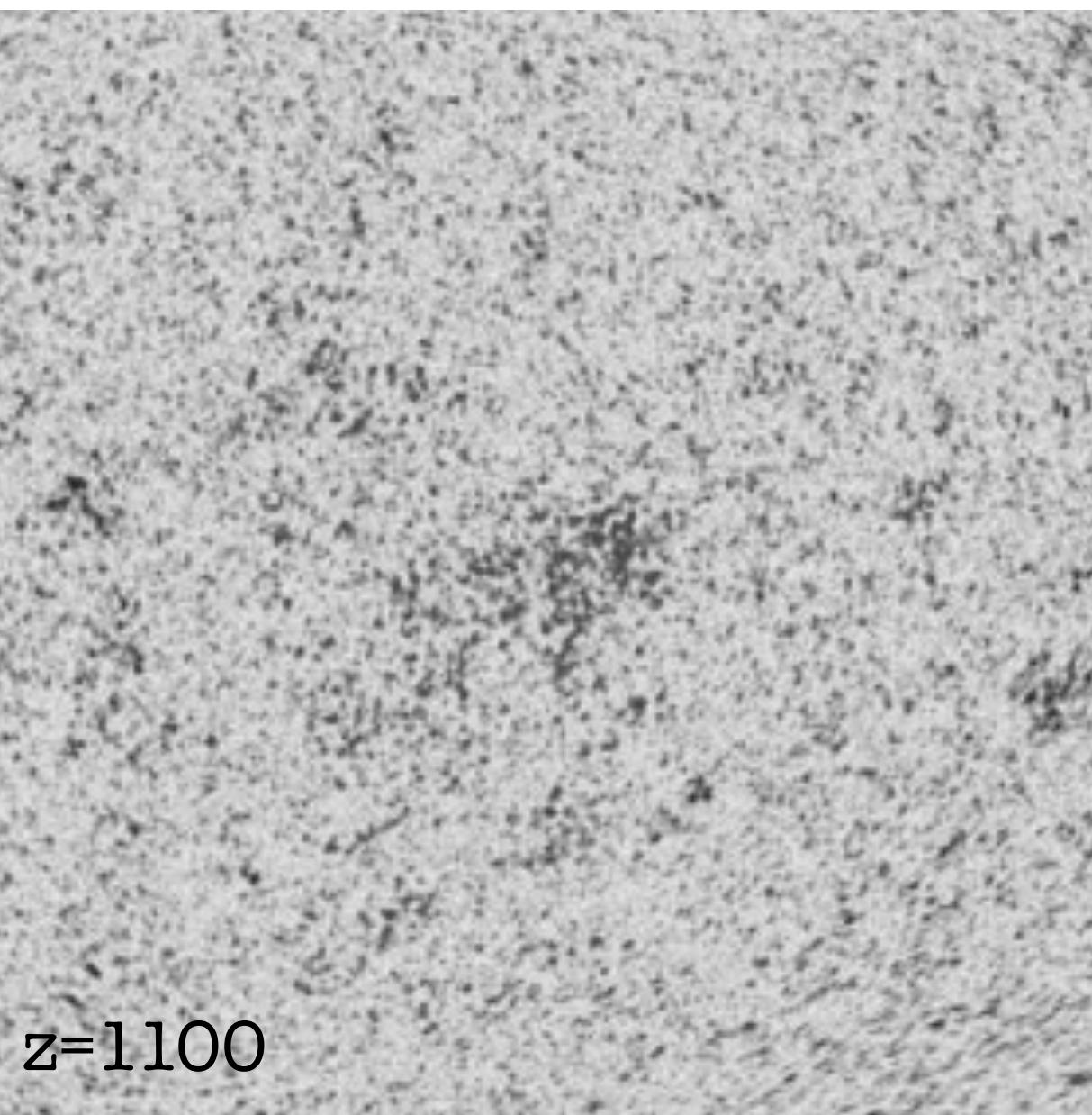
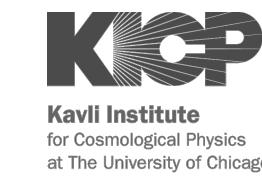


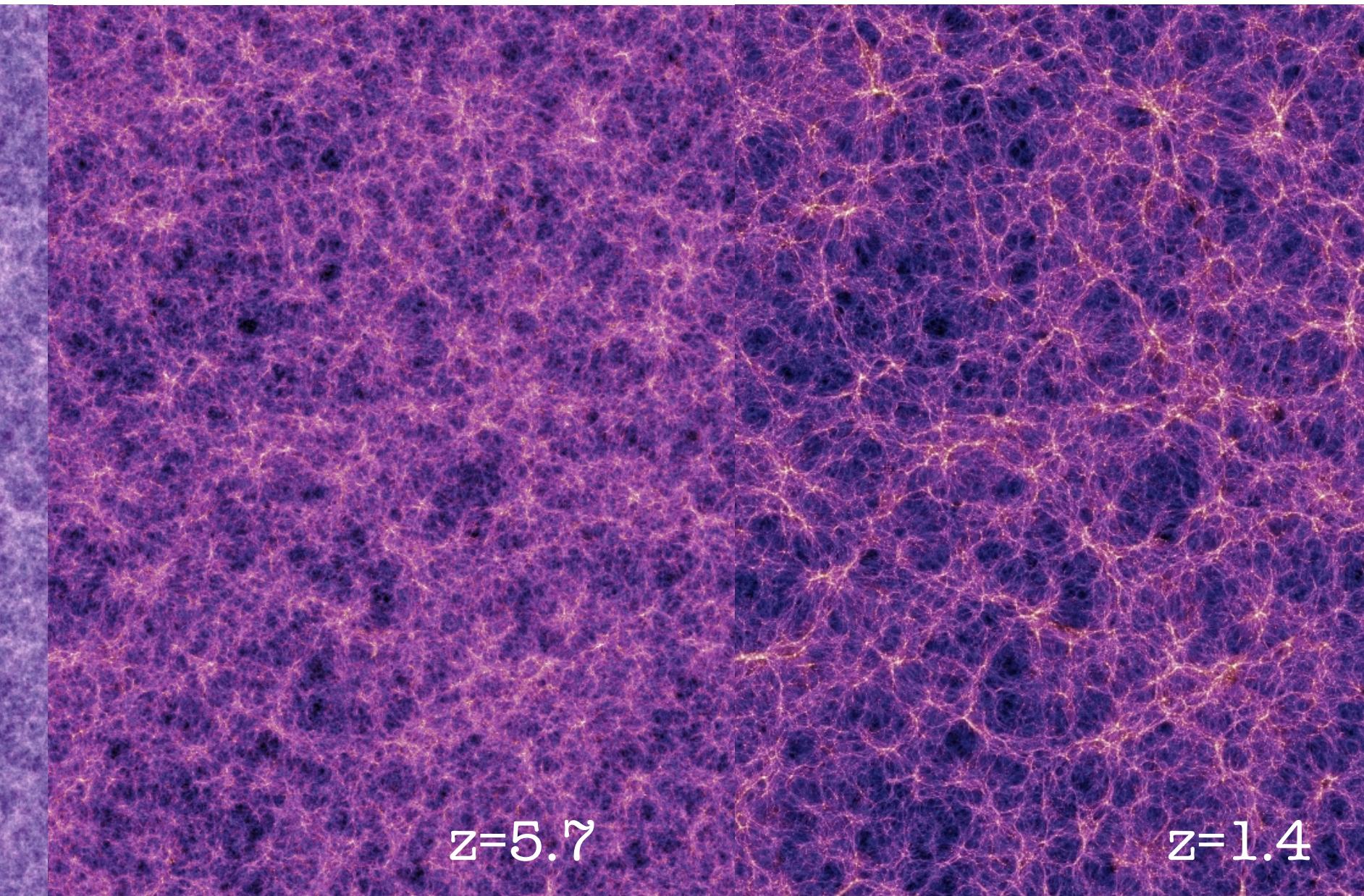
Cosmic fields beyond 2pt: practical challenges and opportunities

Chihway Chang (UChicago/KICP)

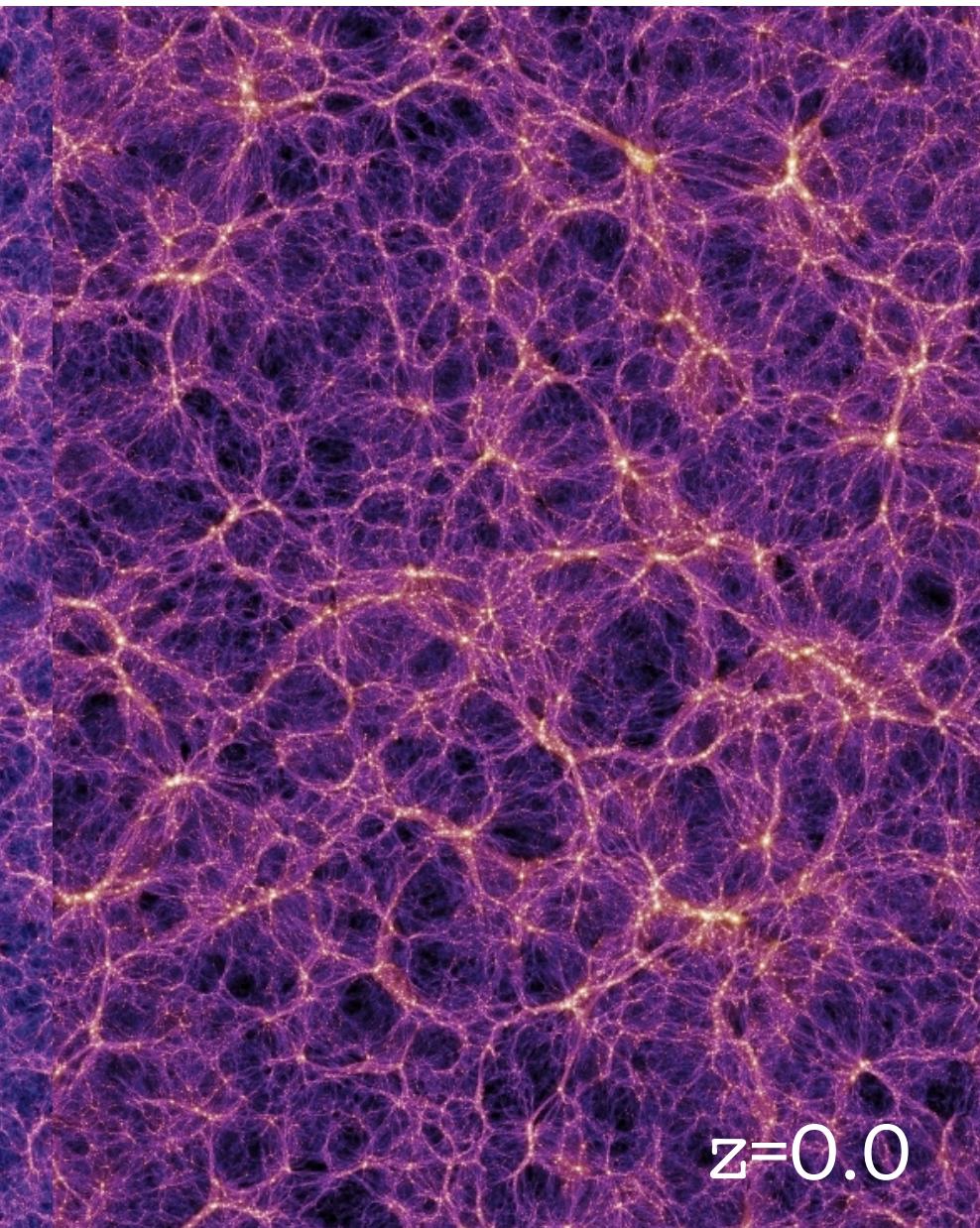
with Dhayaa Anbajagane, Yuuki Omori and many others in DES/DESC



$z=18.3$



$z=5.7$



$z=1.4$

$z=0.0$

Outline

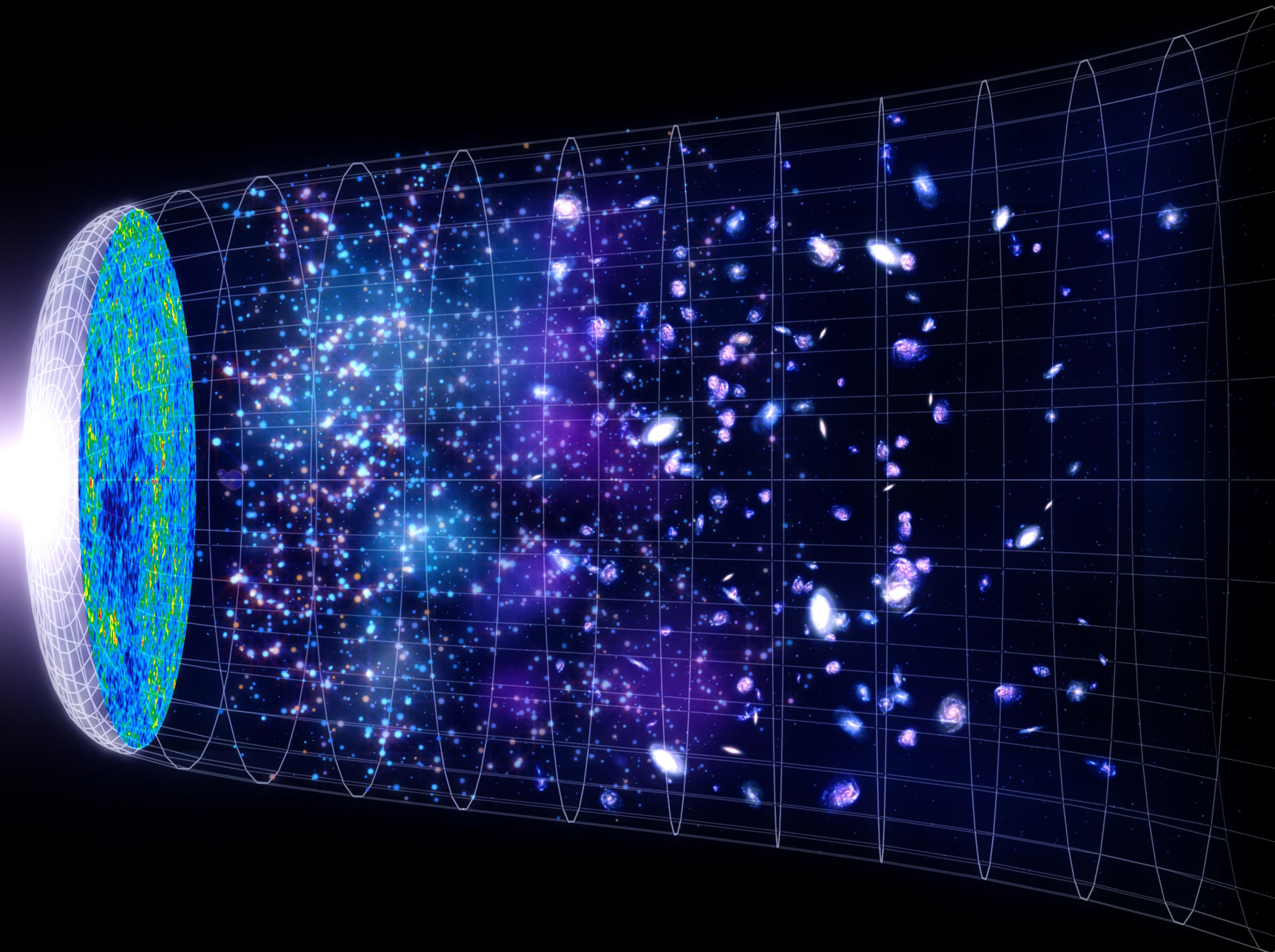
- The Λ CDM paradigm and extracting information beyond 2pt
- Practical challenges: beyond 2pt systematics
- Opportunities: primordial non-Gaussianity
- Towards field-level inference
- Summary & outlook

Outline

- The Λ CDM paradigm and extracting information beyond 2pt
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Cosmology as we know it today

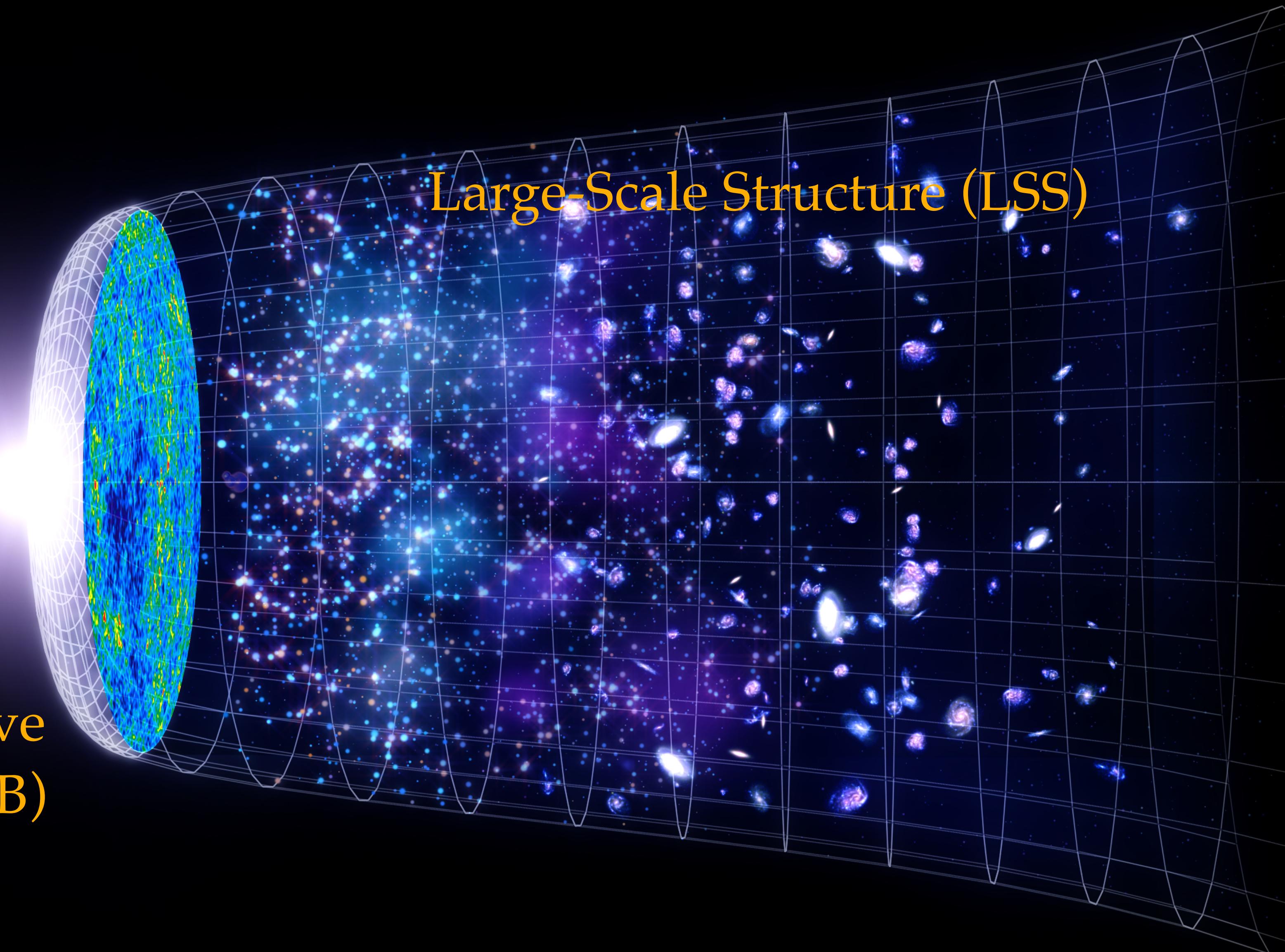
- Λ CDM works very well
- Key questions: dark matter, dark energy, inflation
- Curiosities within Λ CDM:
 H_0 , S8, w_0w_a



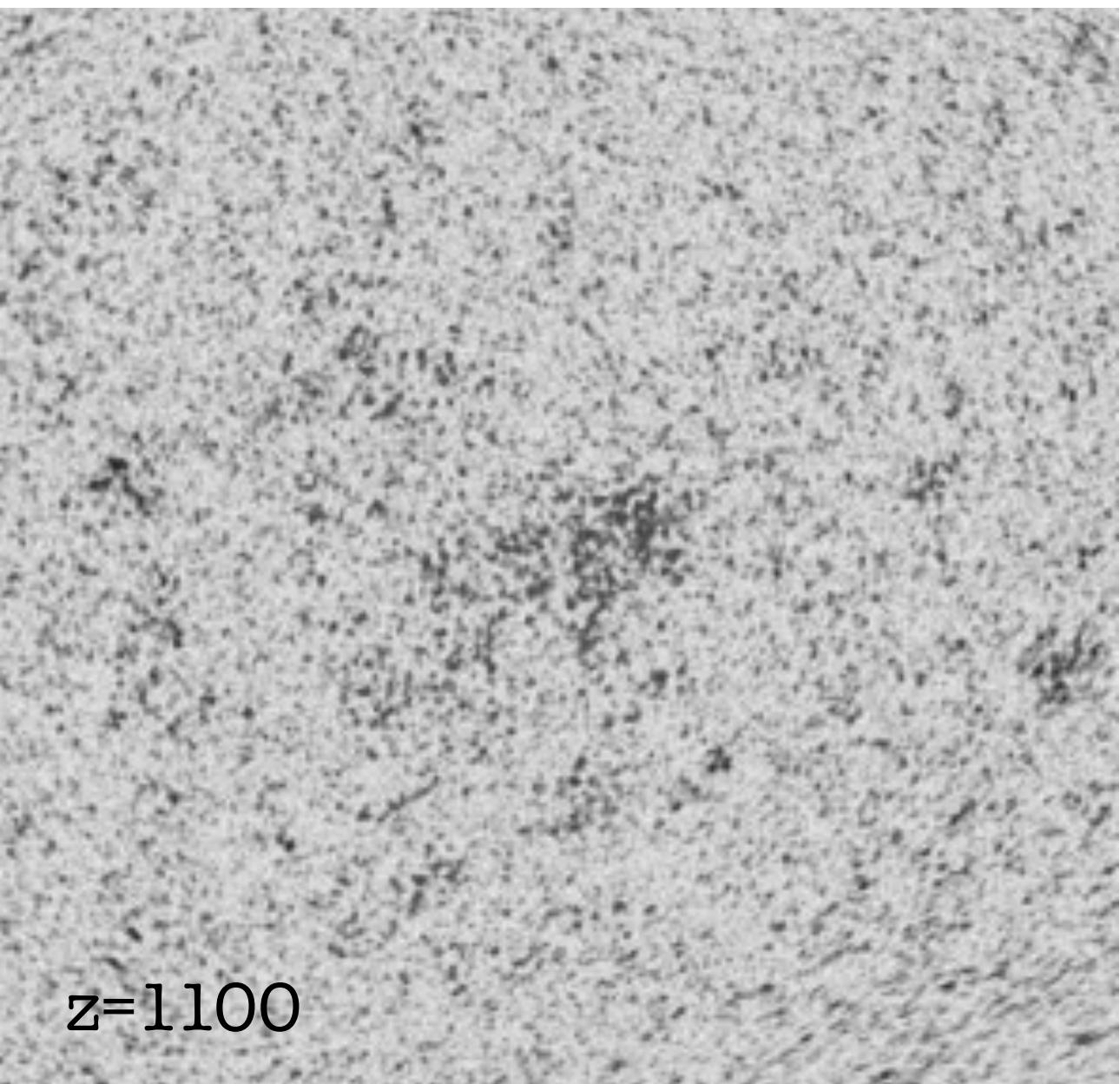
Cosmology as we know it today

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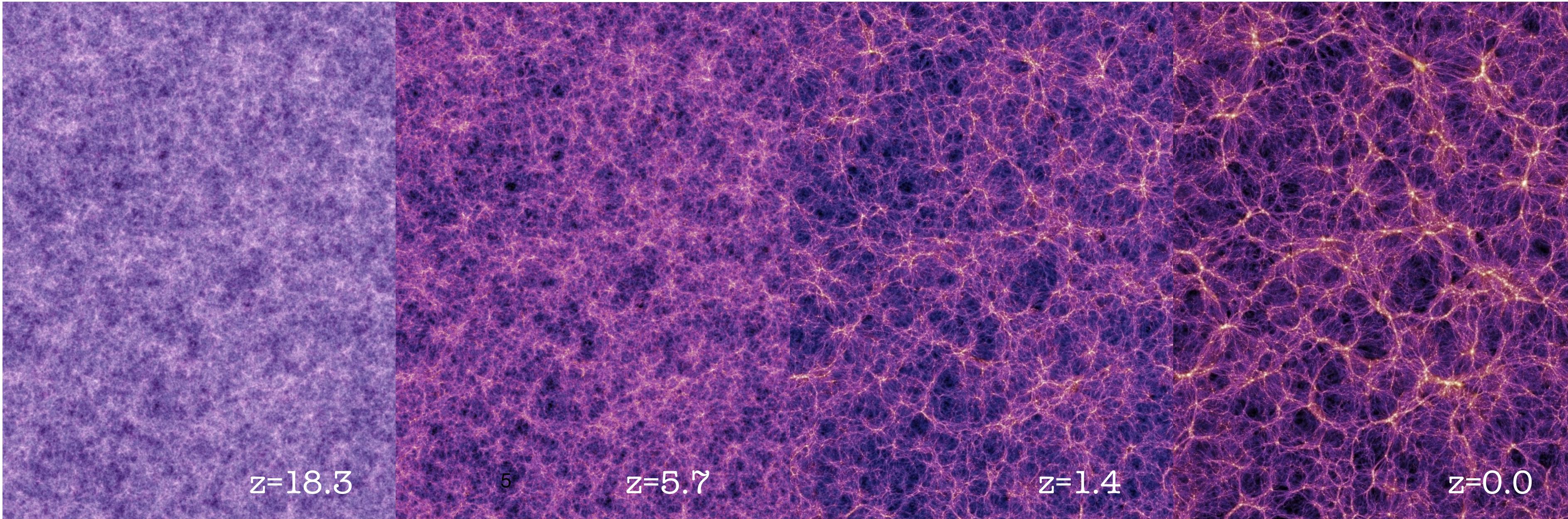
Cosmic Microwave
Background (CMB)



Early-universe physics



$z=1100$



$z=18.3$

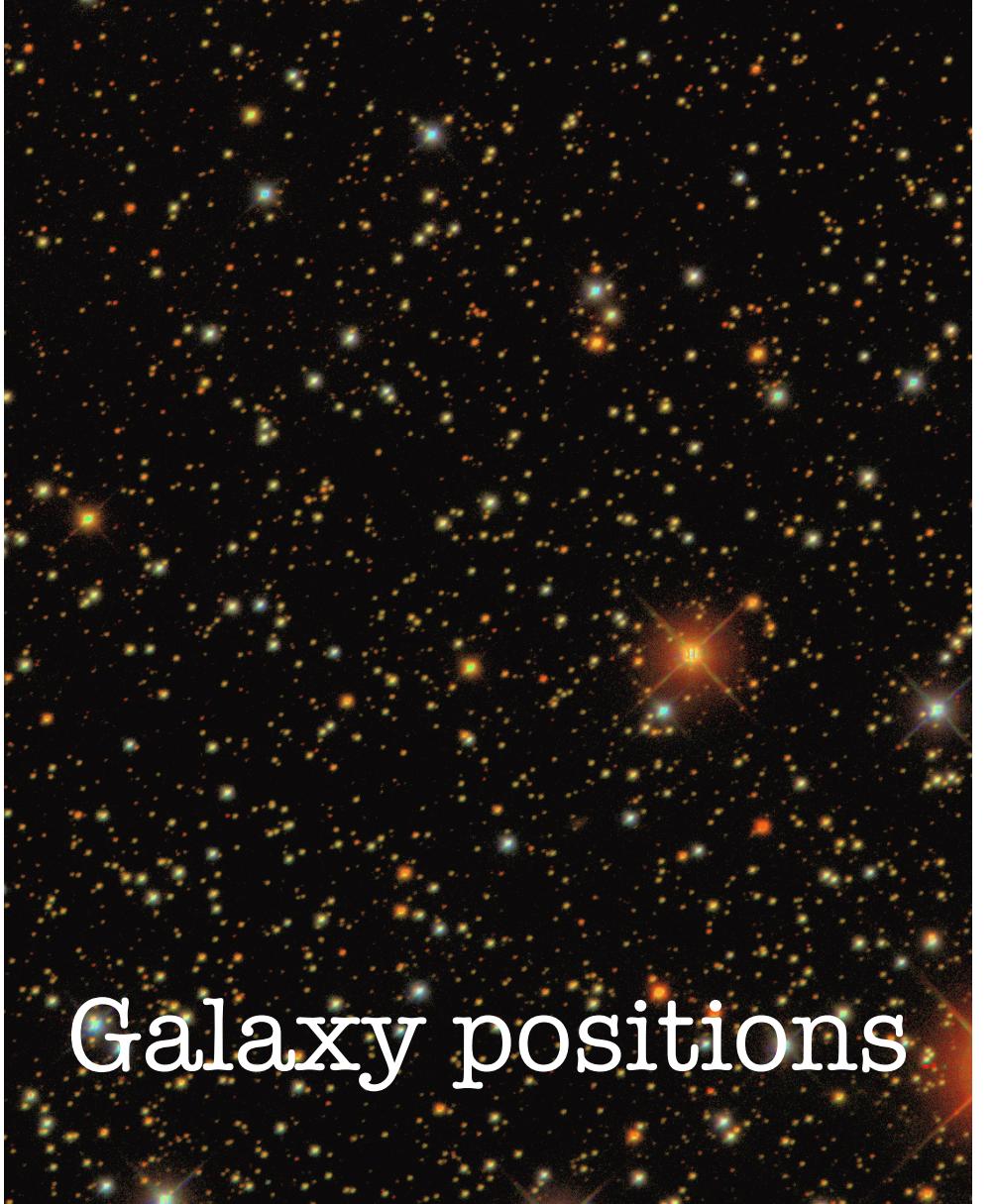
5

$z=5.7$

$z=1.4$

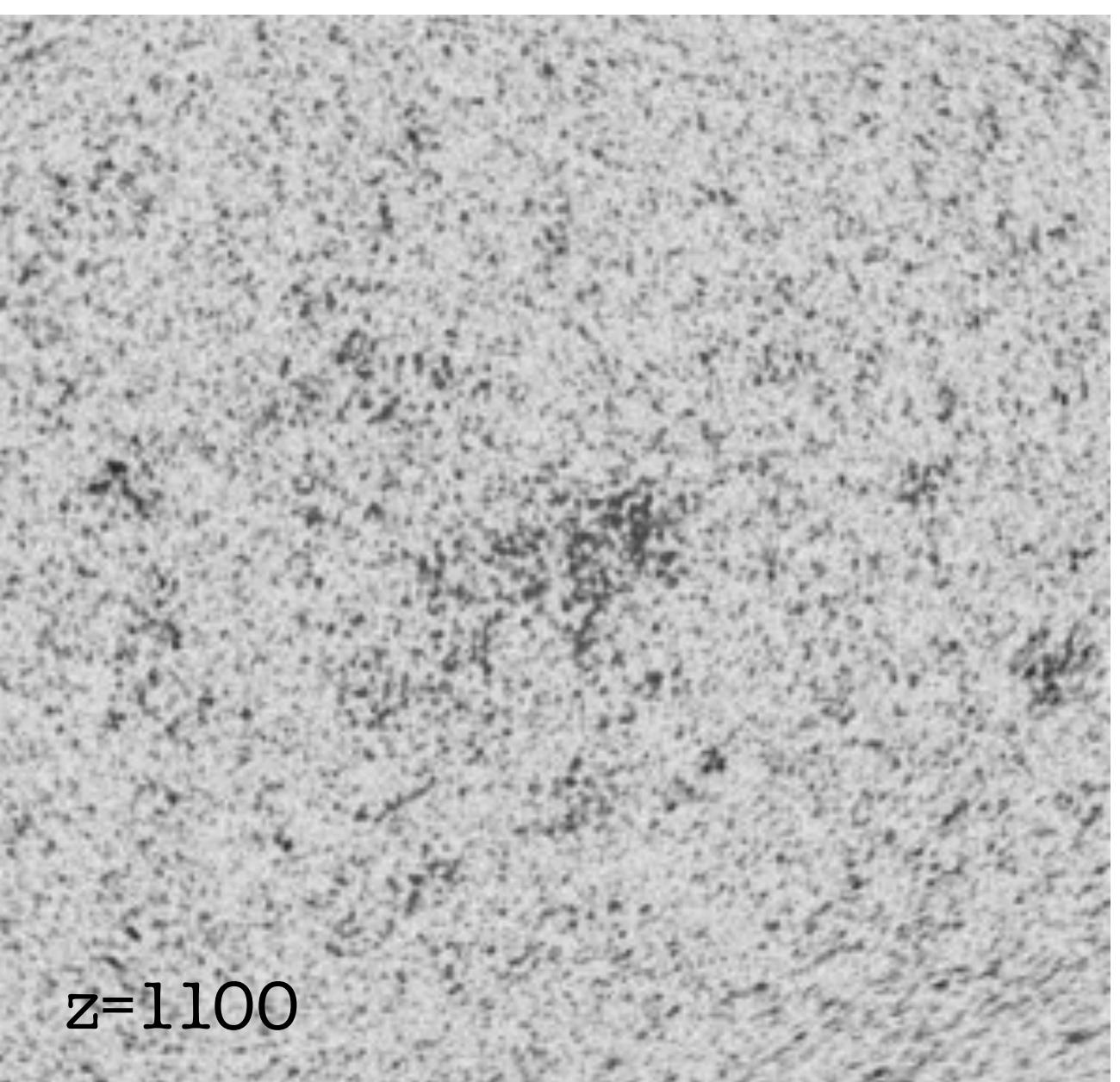
$z=0.0$

Gravity, dark matter, dark energy



Galaxy positions

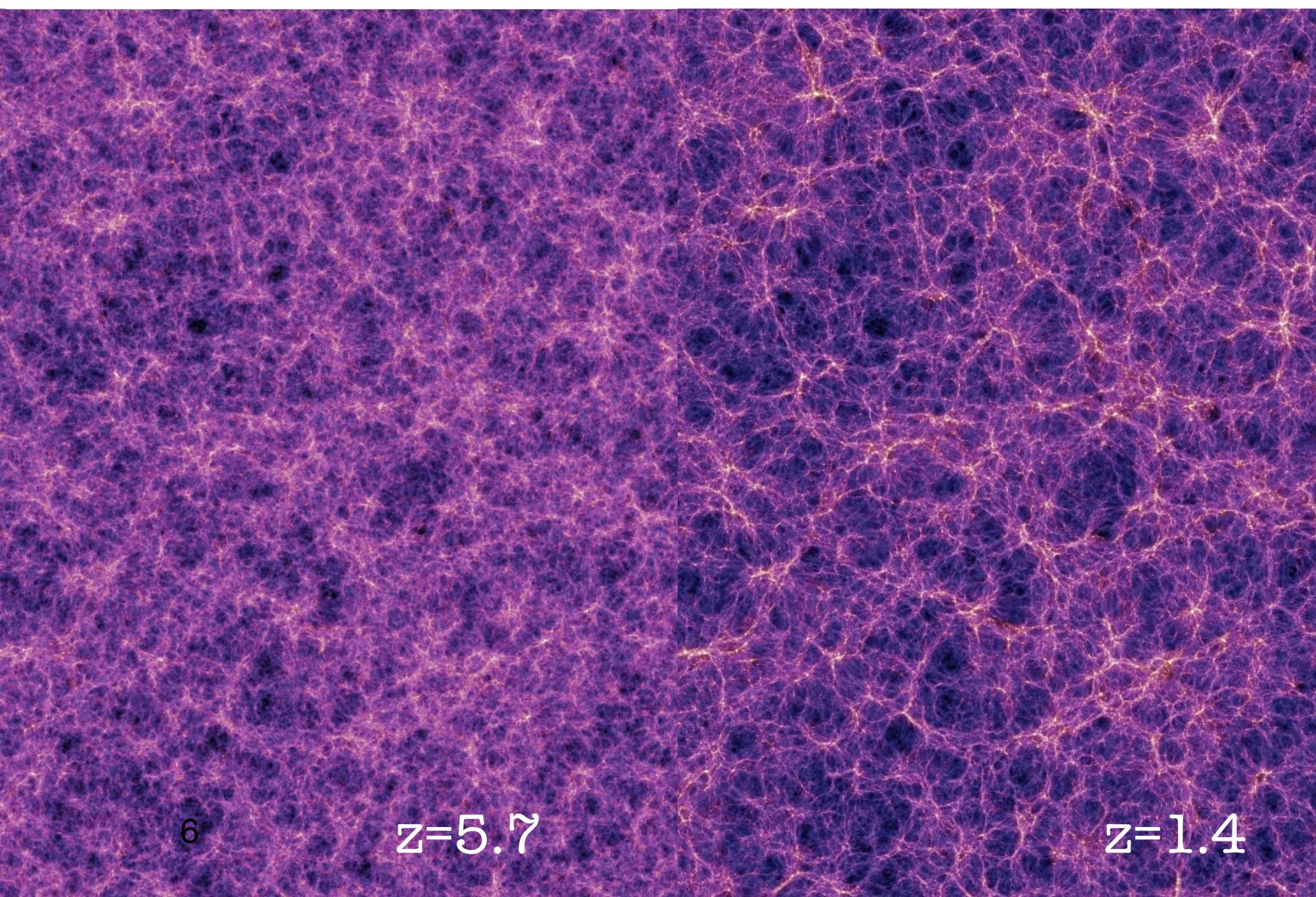
Astrophysics



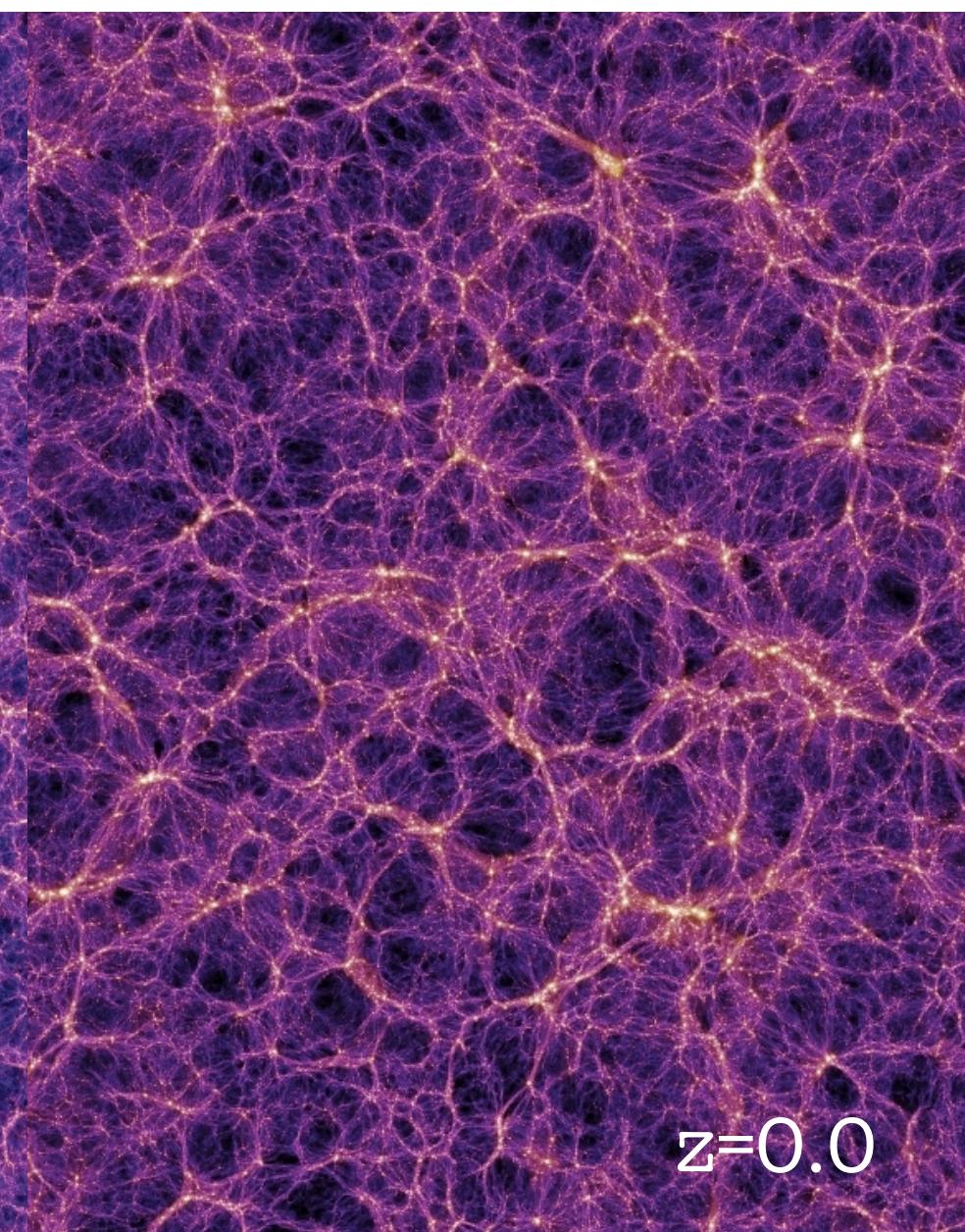
$z=1100$



$z=18.3$

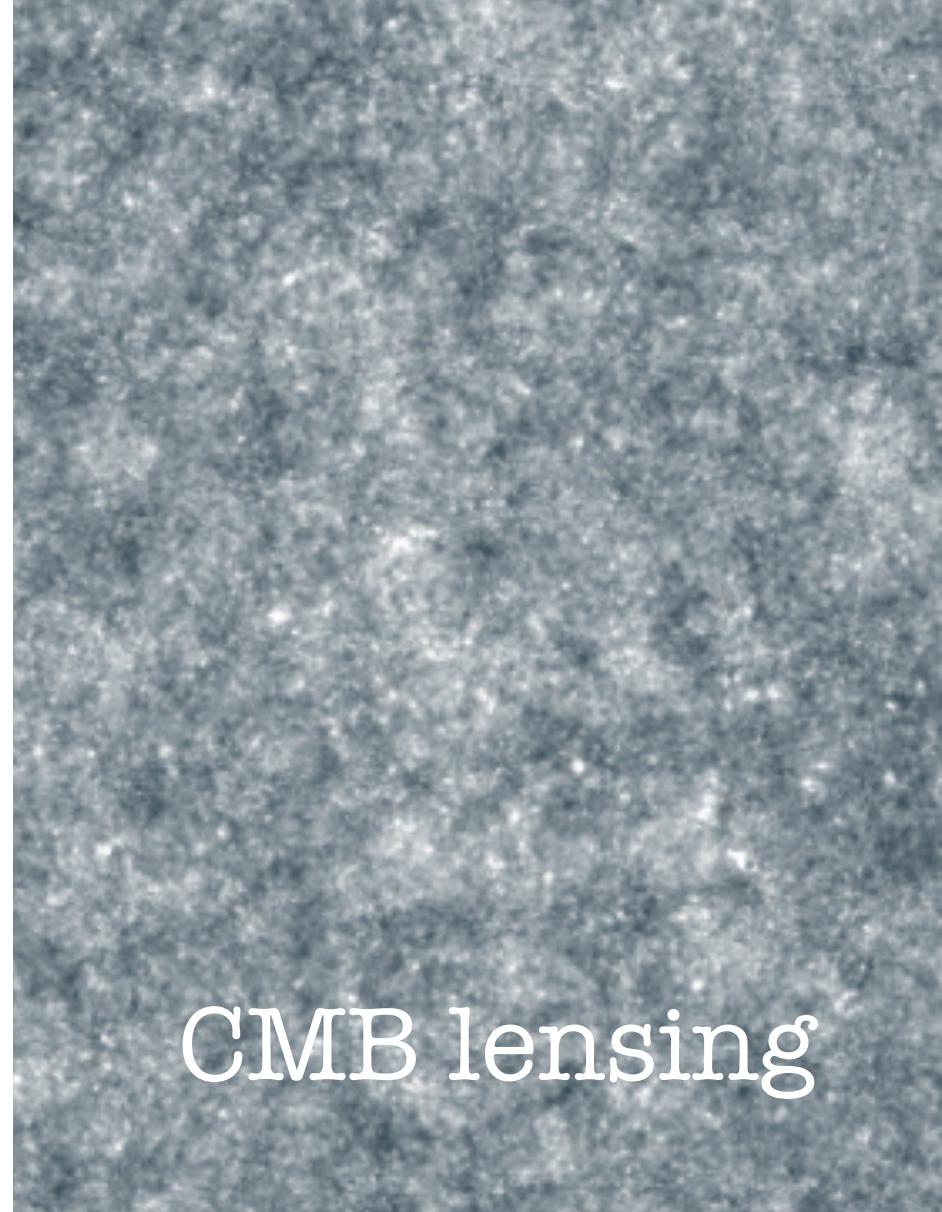


$z=5.7$

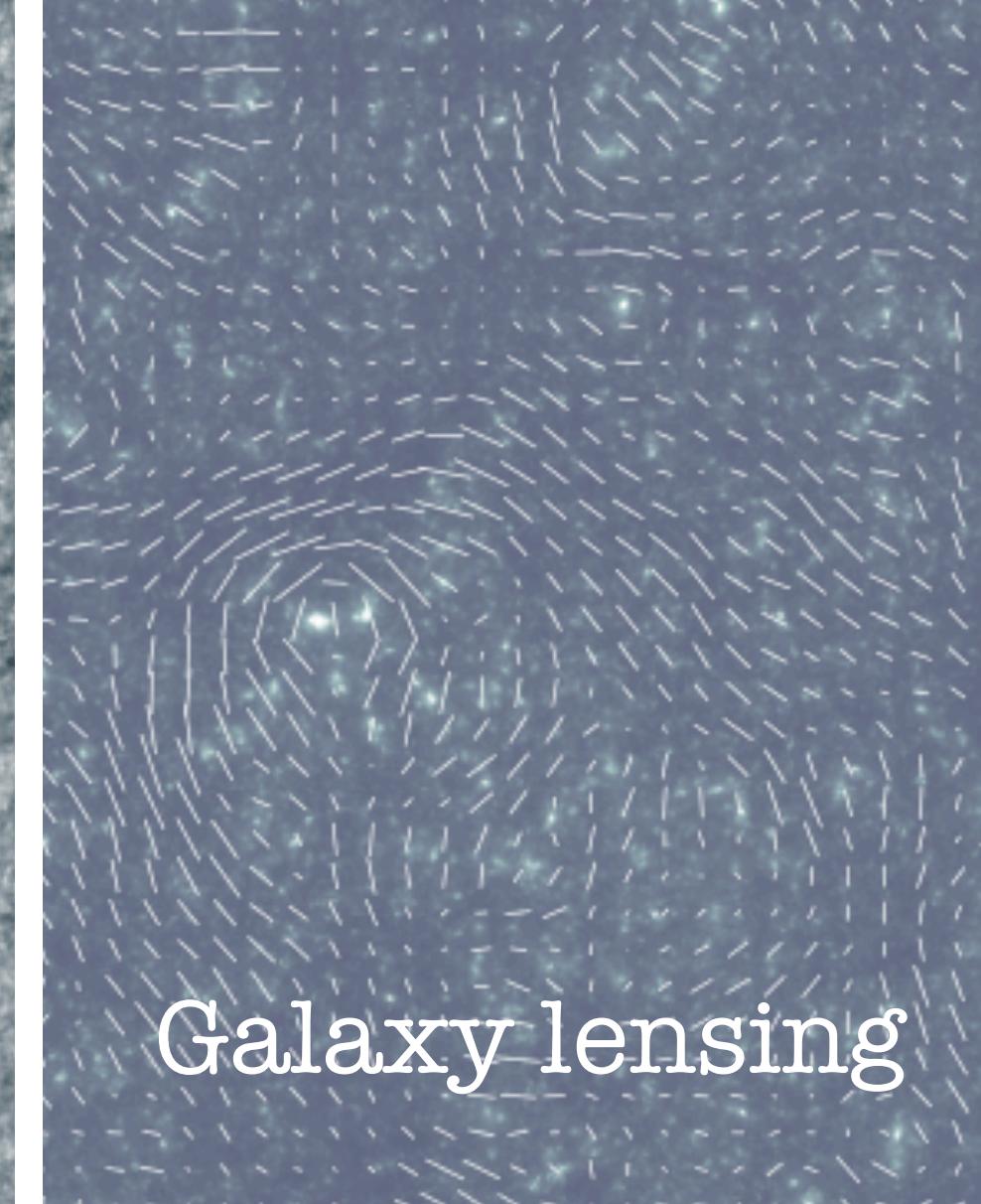


$z=1.4$

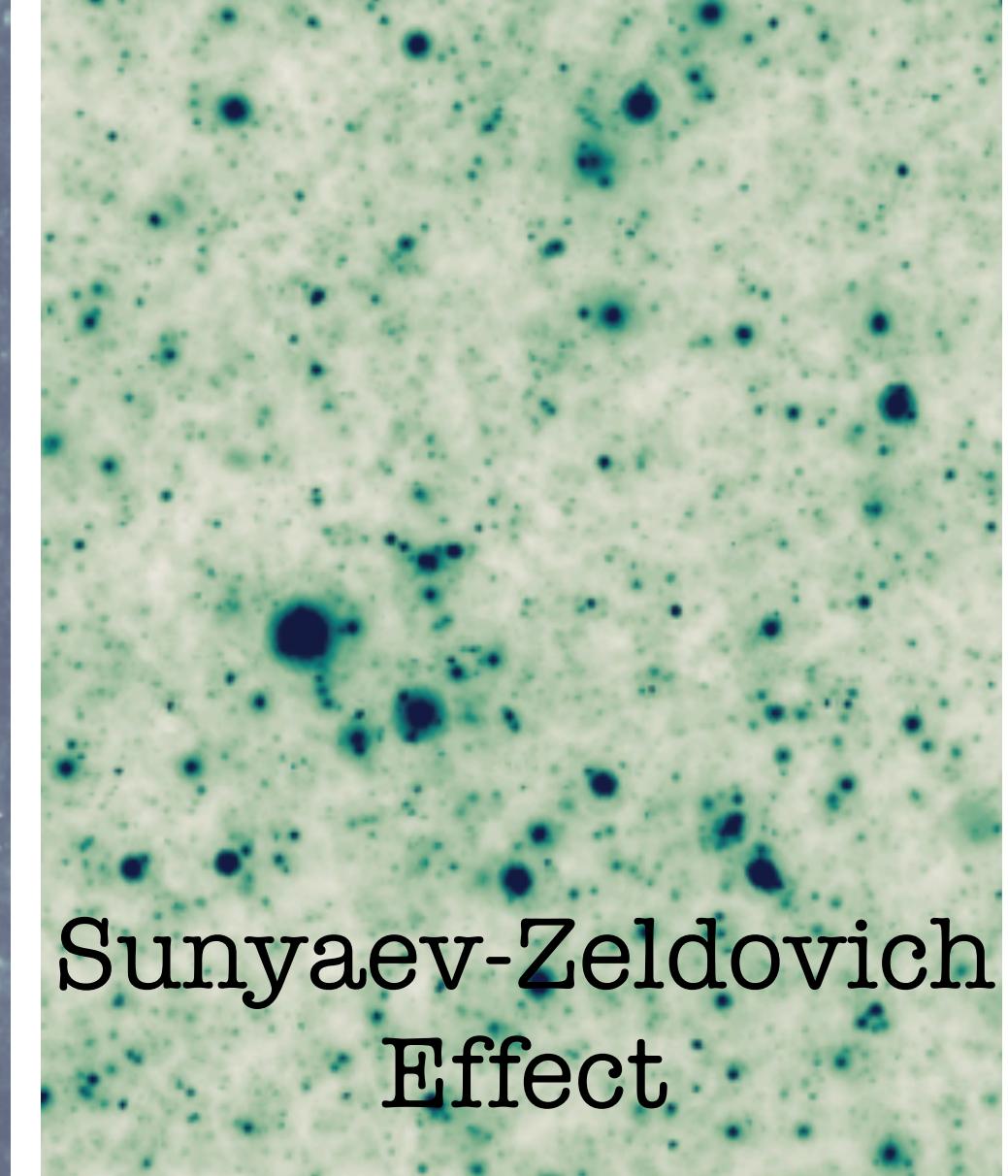
$z=0.0$



CMB lensing



Galaxy lensing

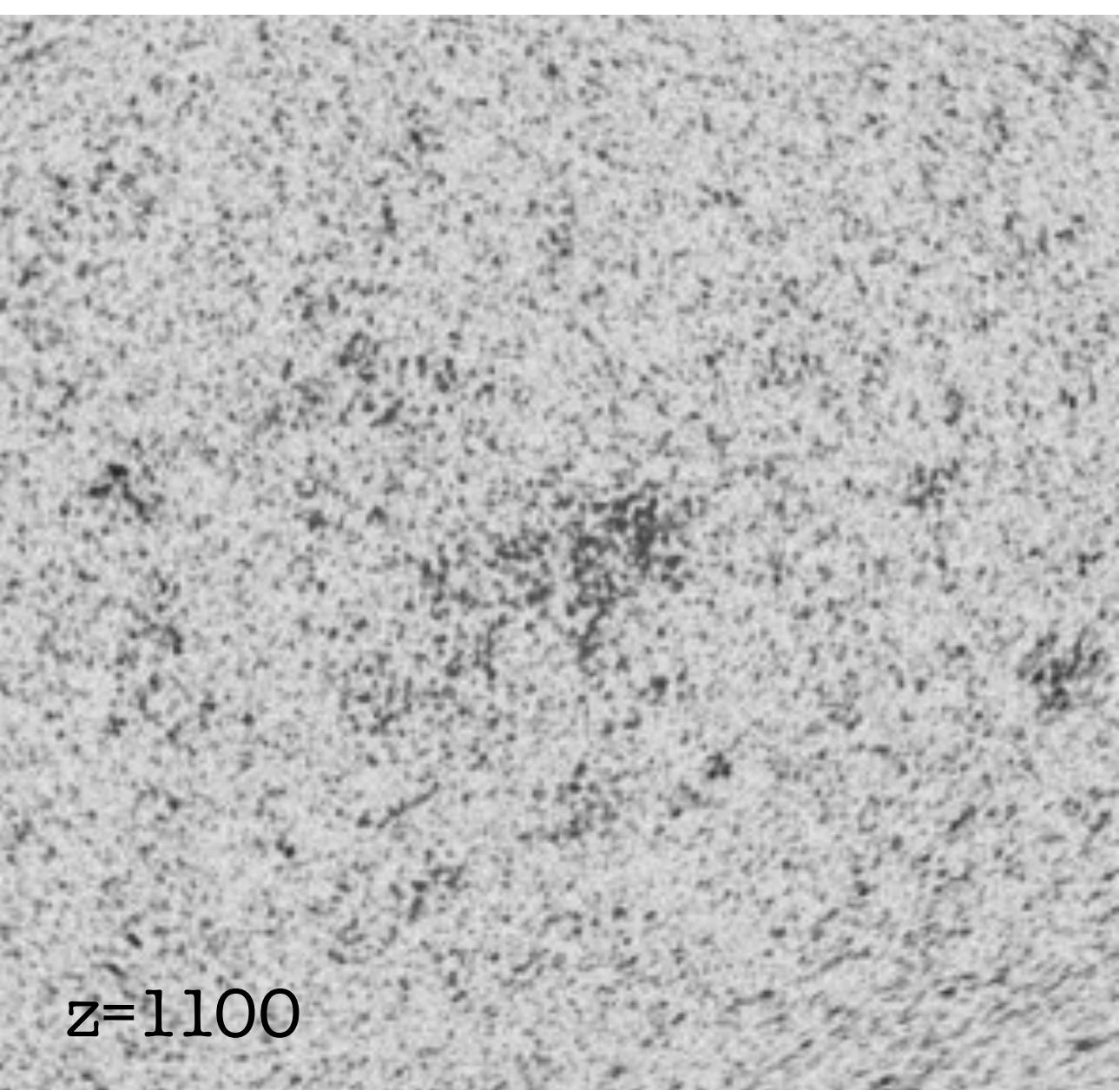


Sunyaev-Zeldovich
Effect

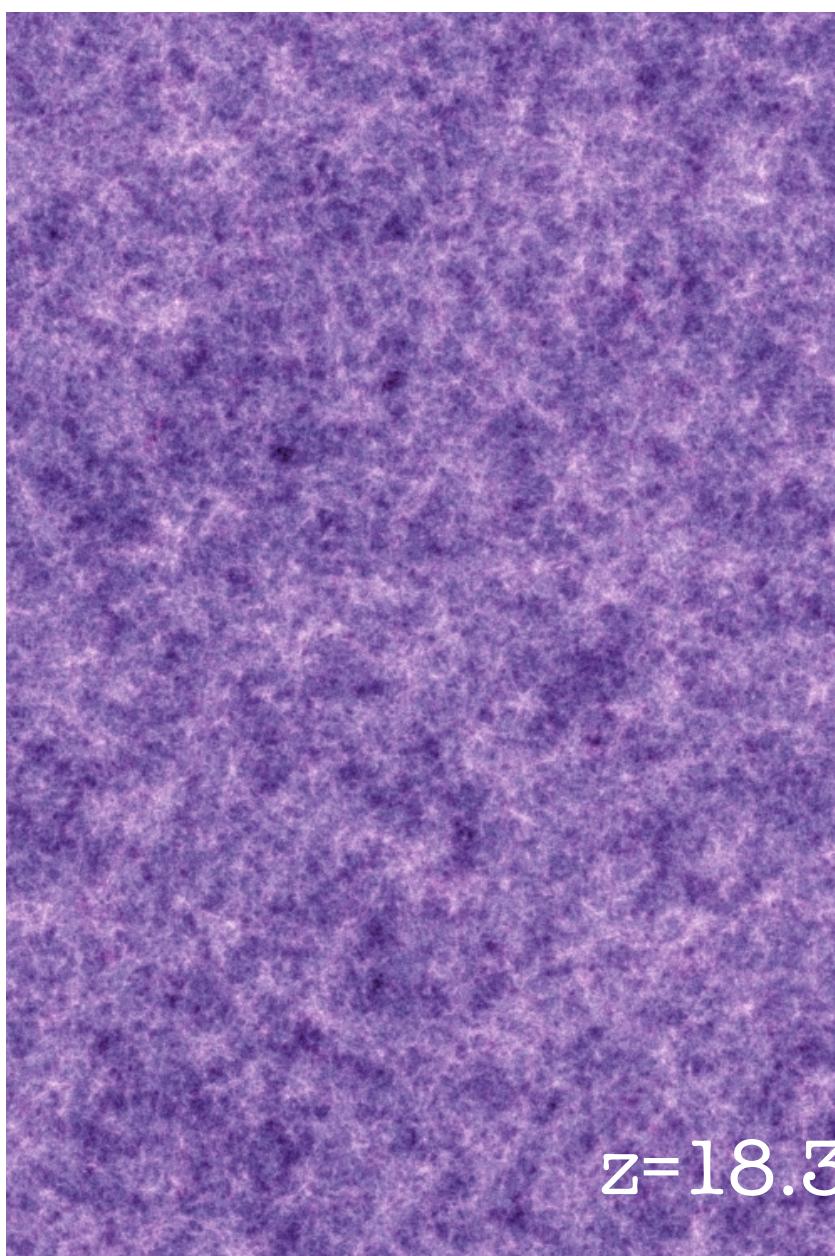


Galaxy positions

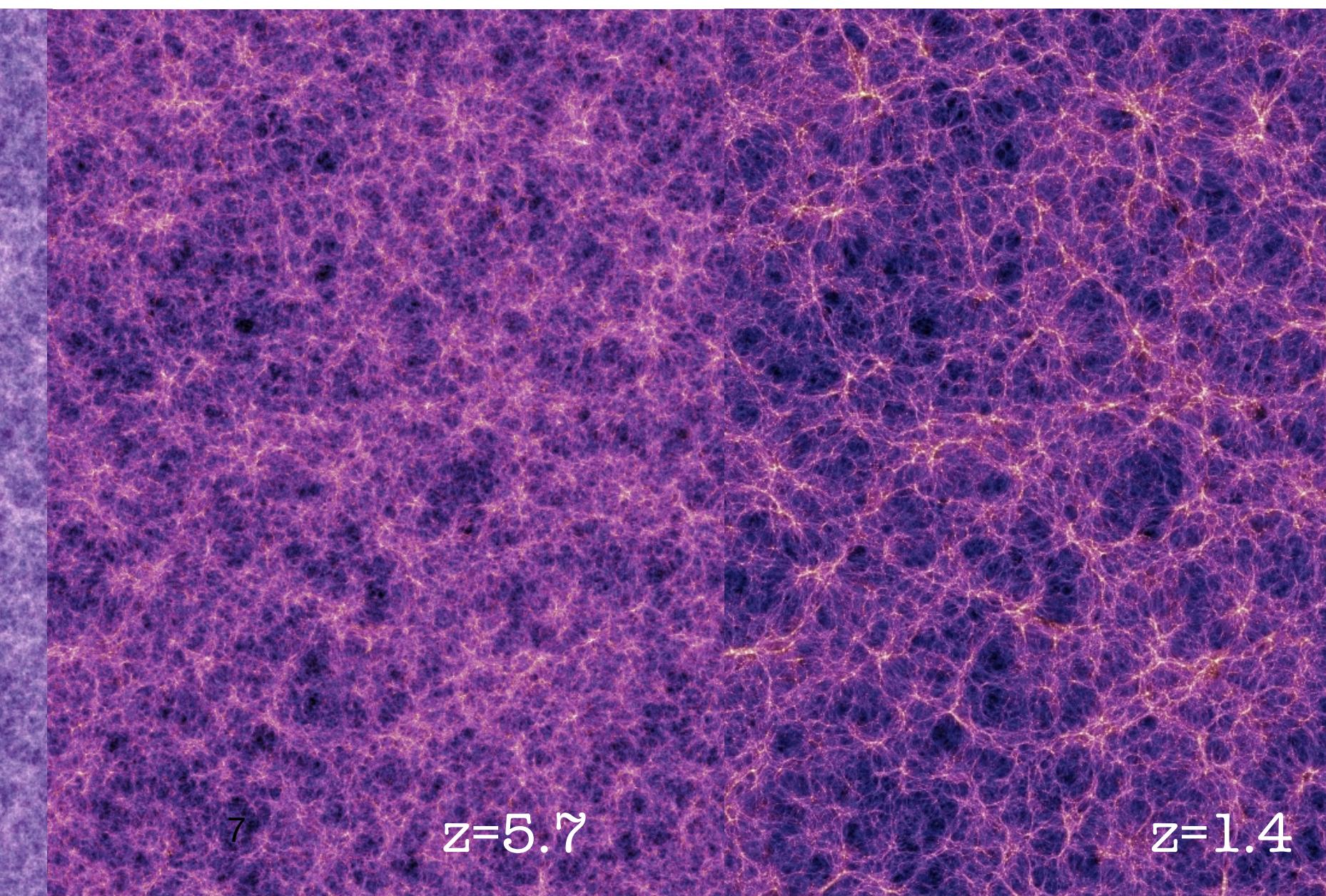
Astrophysics



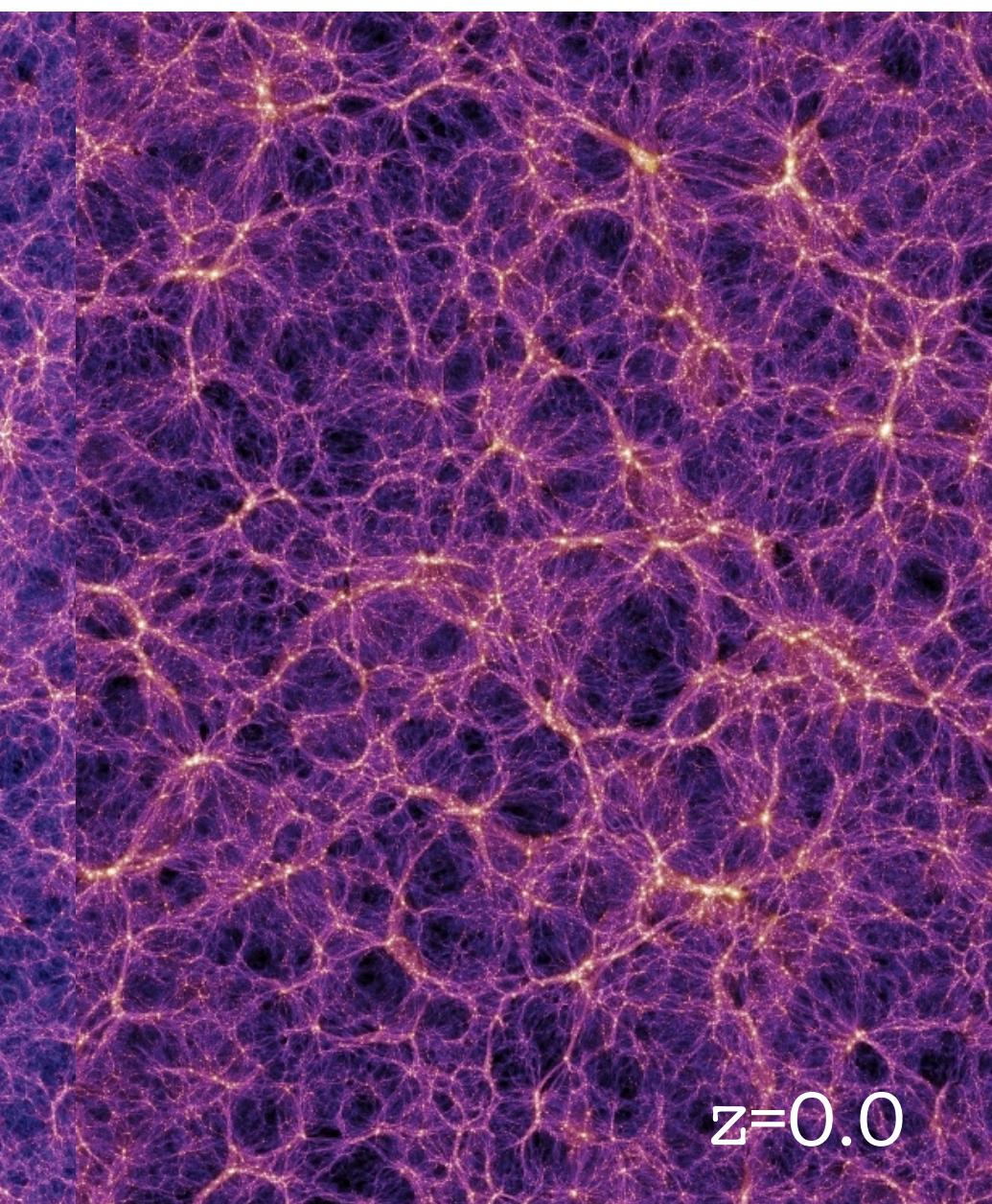
$z=1100$



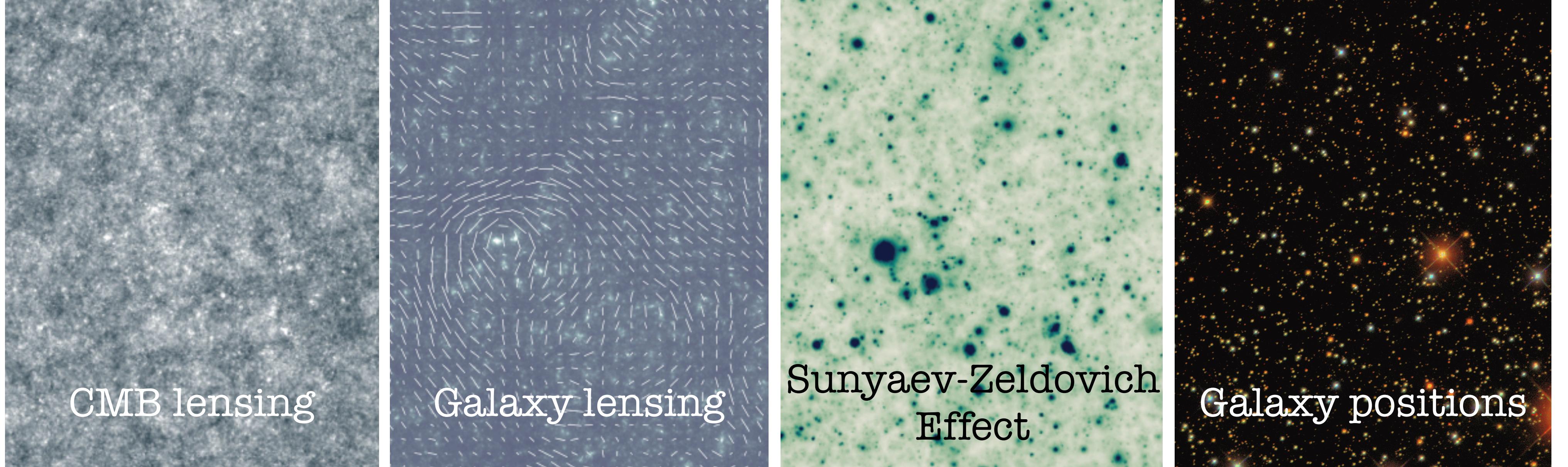
$z=18.3$



$z=5.7$



$z=1.4$



The LSS is a powerful probe for

Early-universe physics

Λ CDM (gravity, dark energy, dark matter)

Astrophysics (galaxy evolution)

$z=1100$

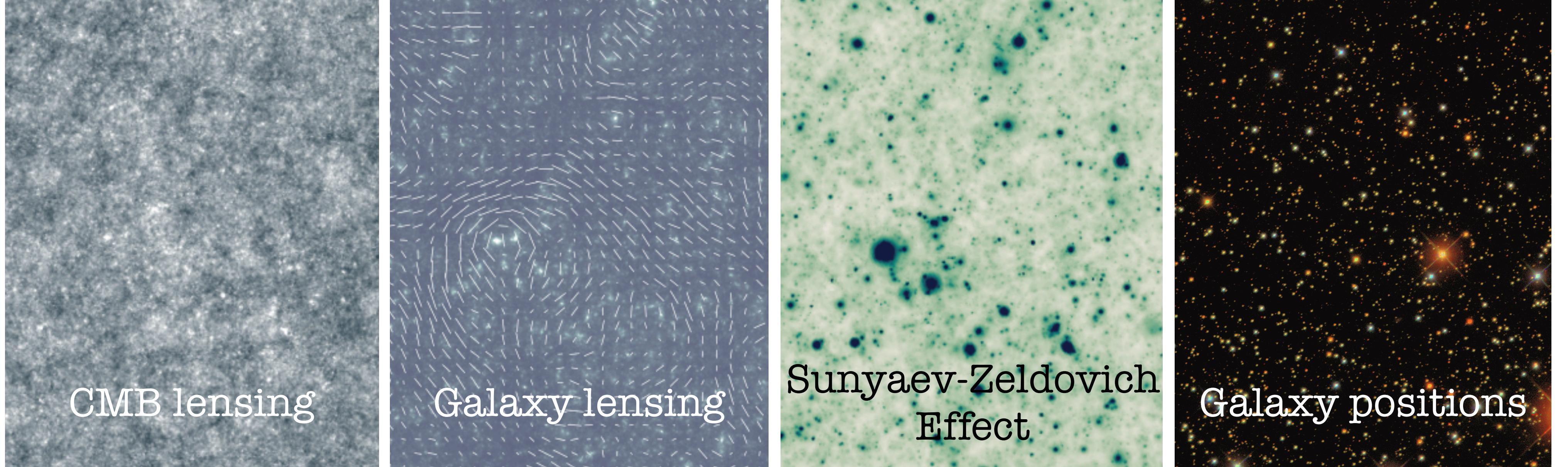
$z=18.3$

8

$z=5.7$

$z=1.4$

$z=0.0$



Compared to CMB

More overall information

The information is more complex

Non-Gaussianity

$z=1100$

$z=18.3$

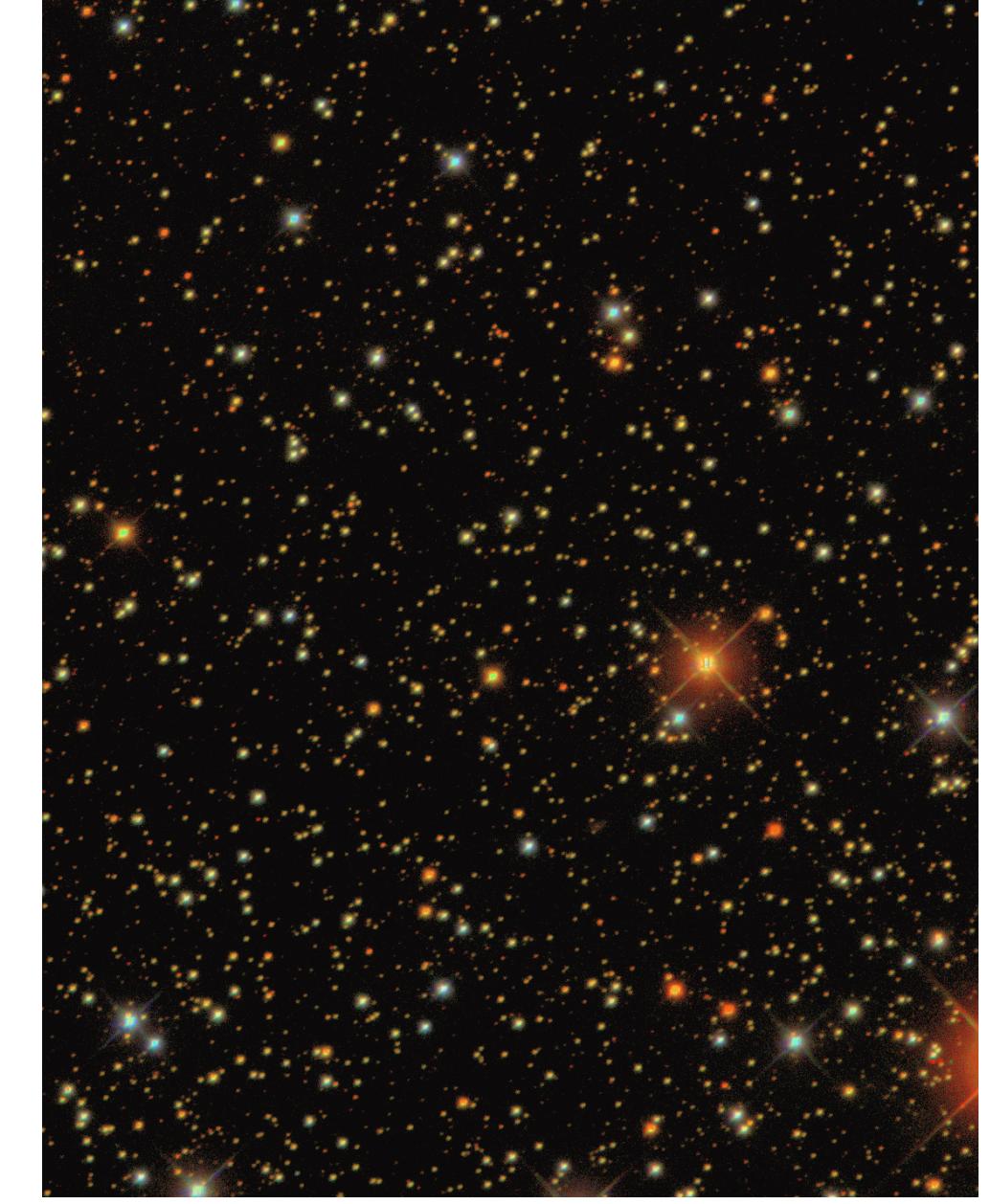
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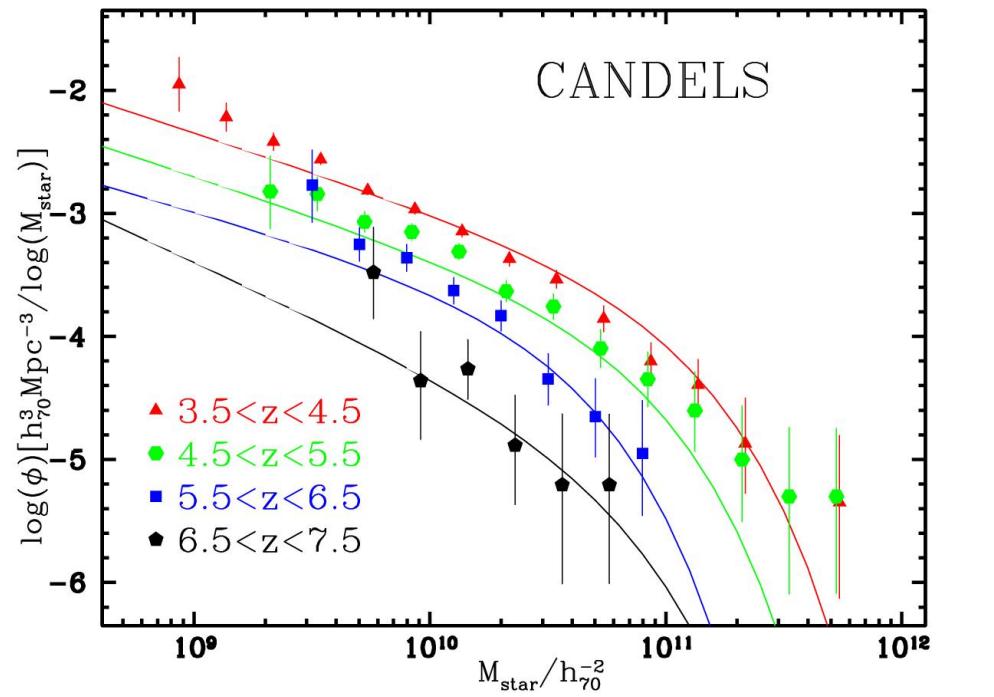
$z=5.7$

$z=1.4$

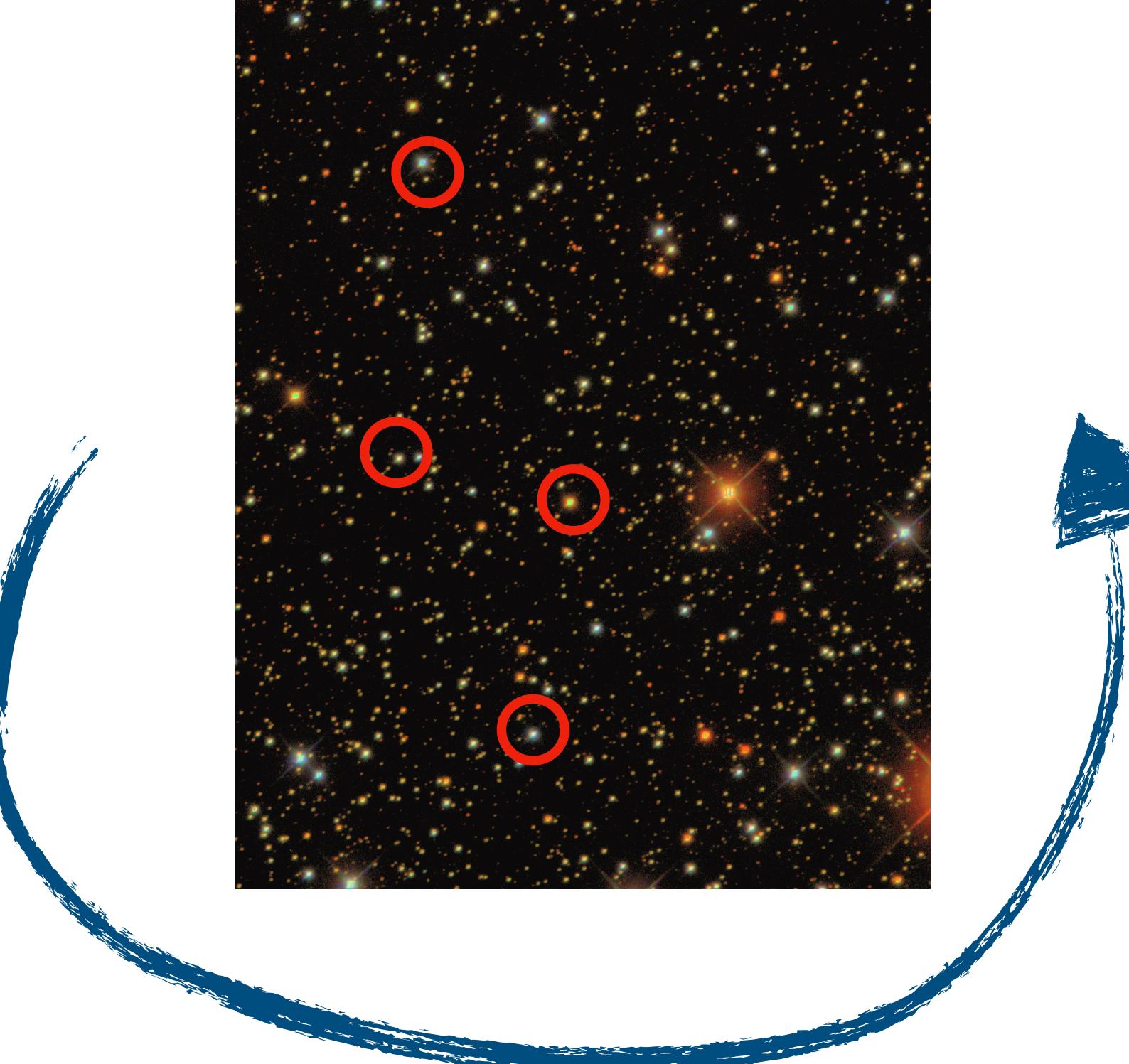
$z=0.0$

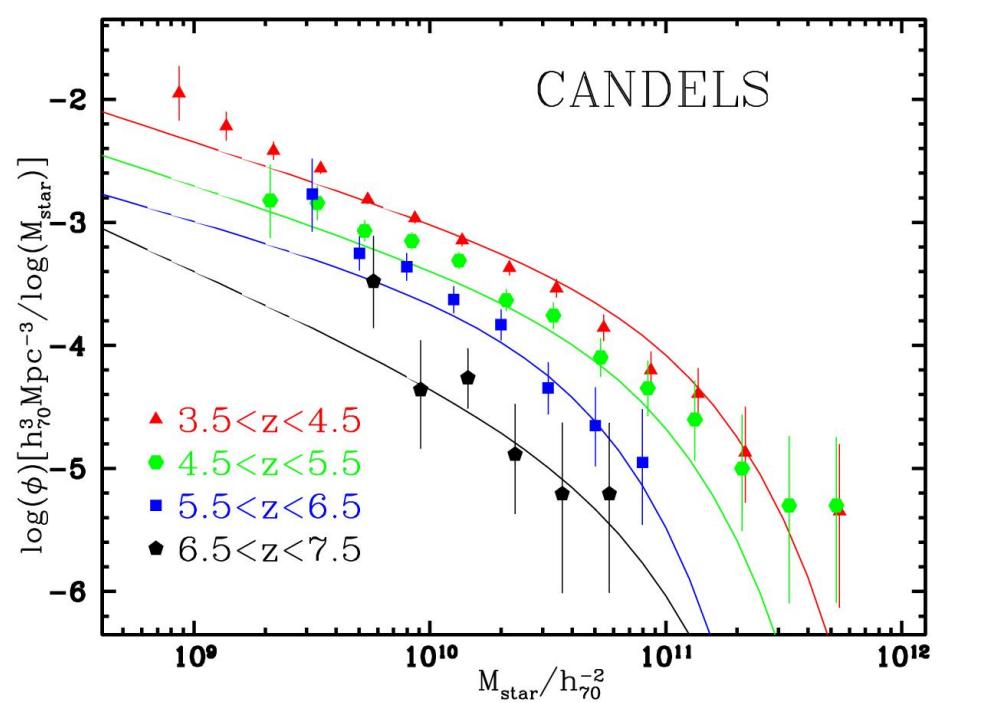




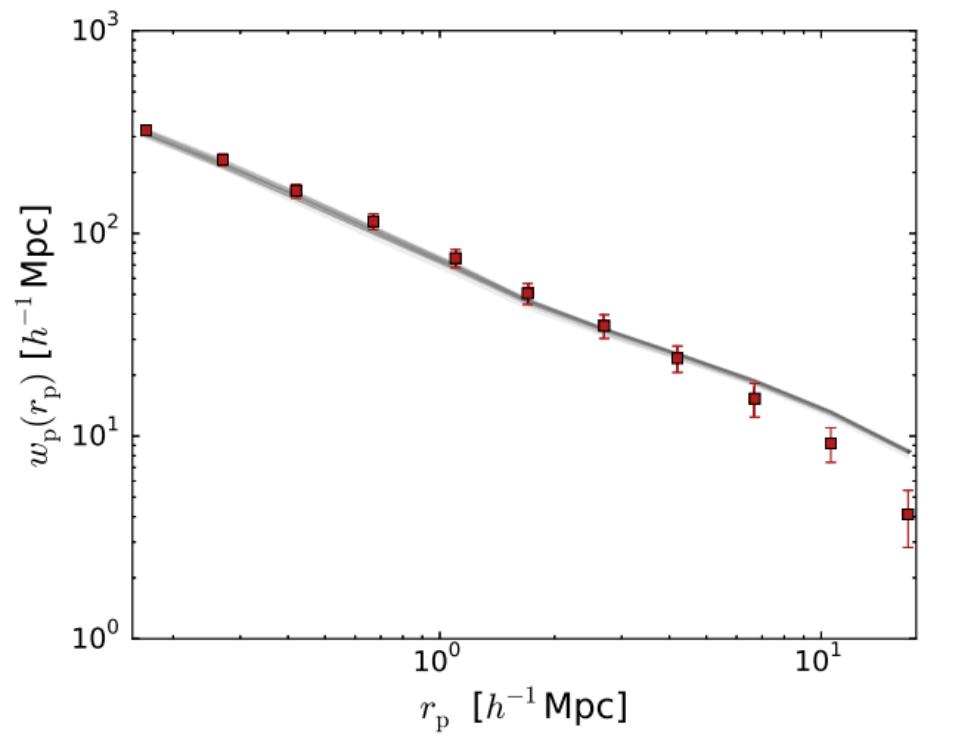
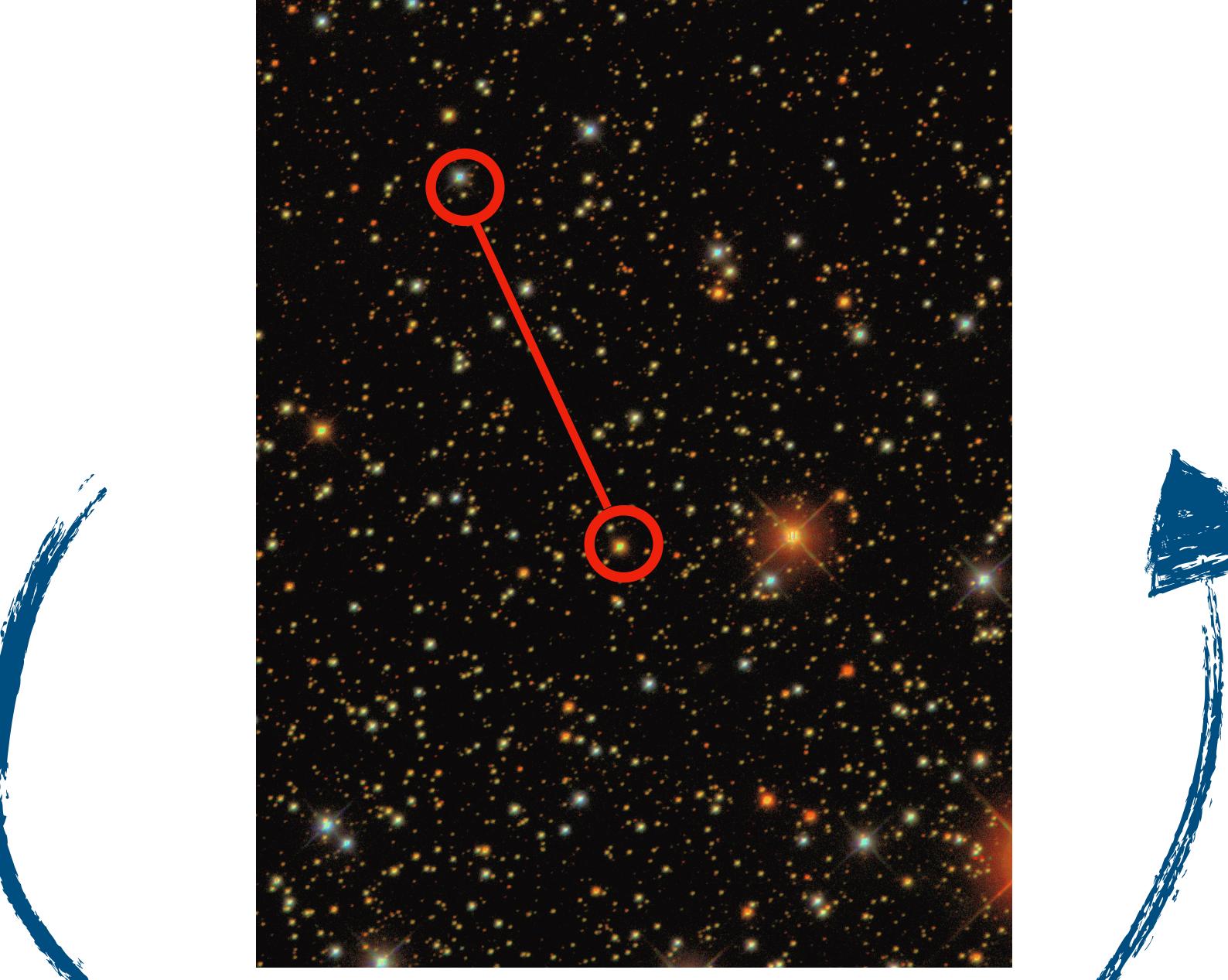


Number counts

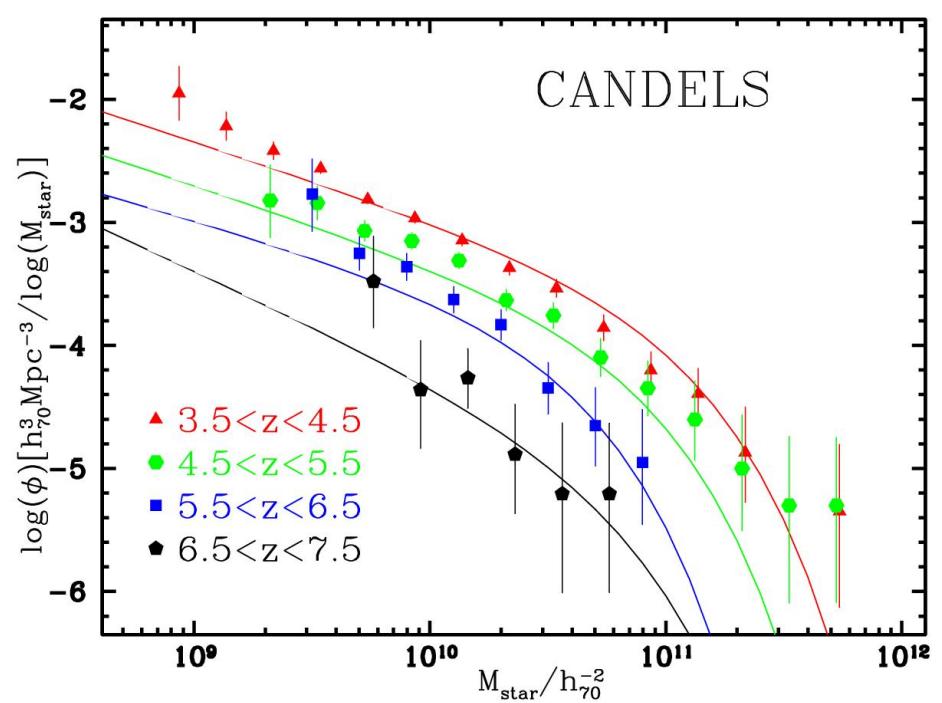




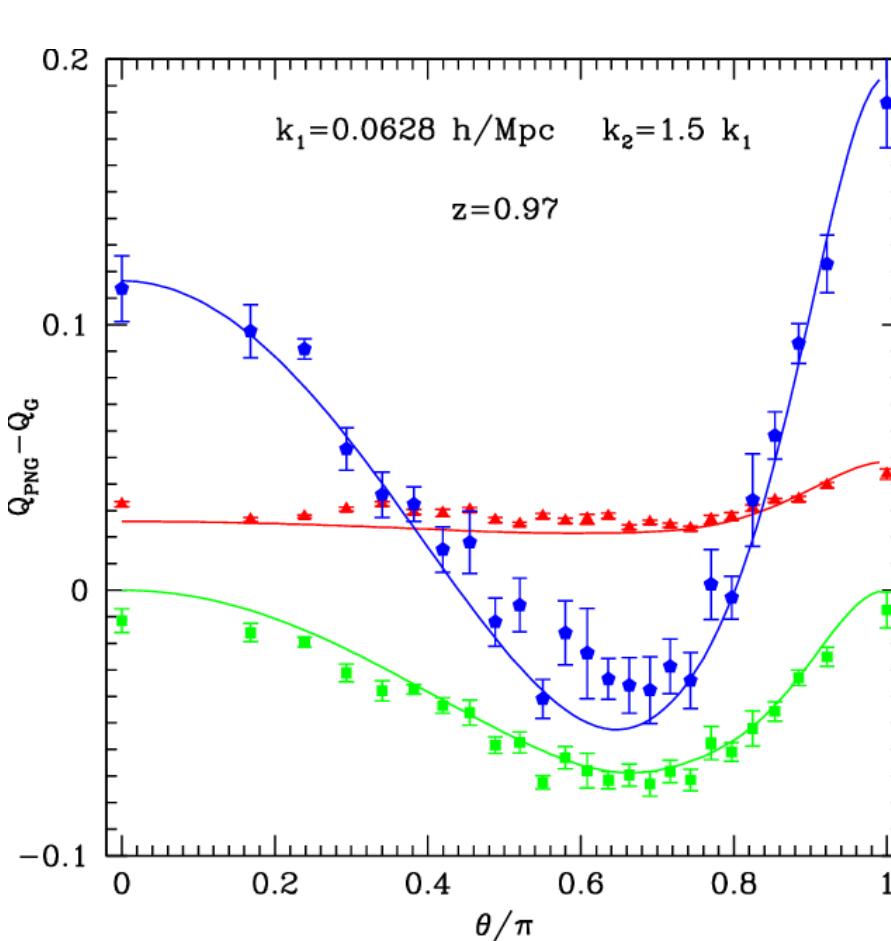
Number counts



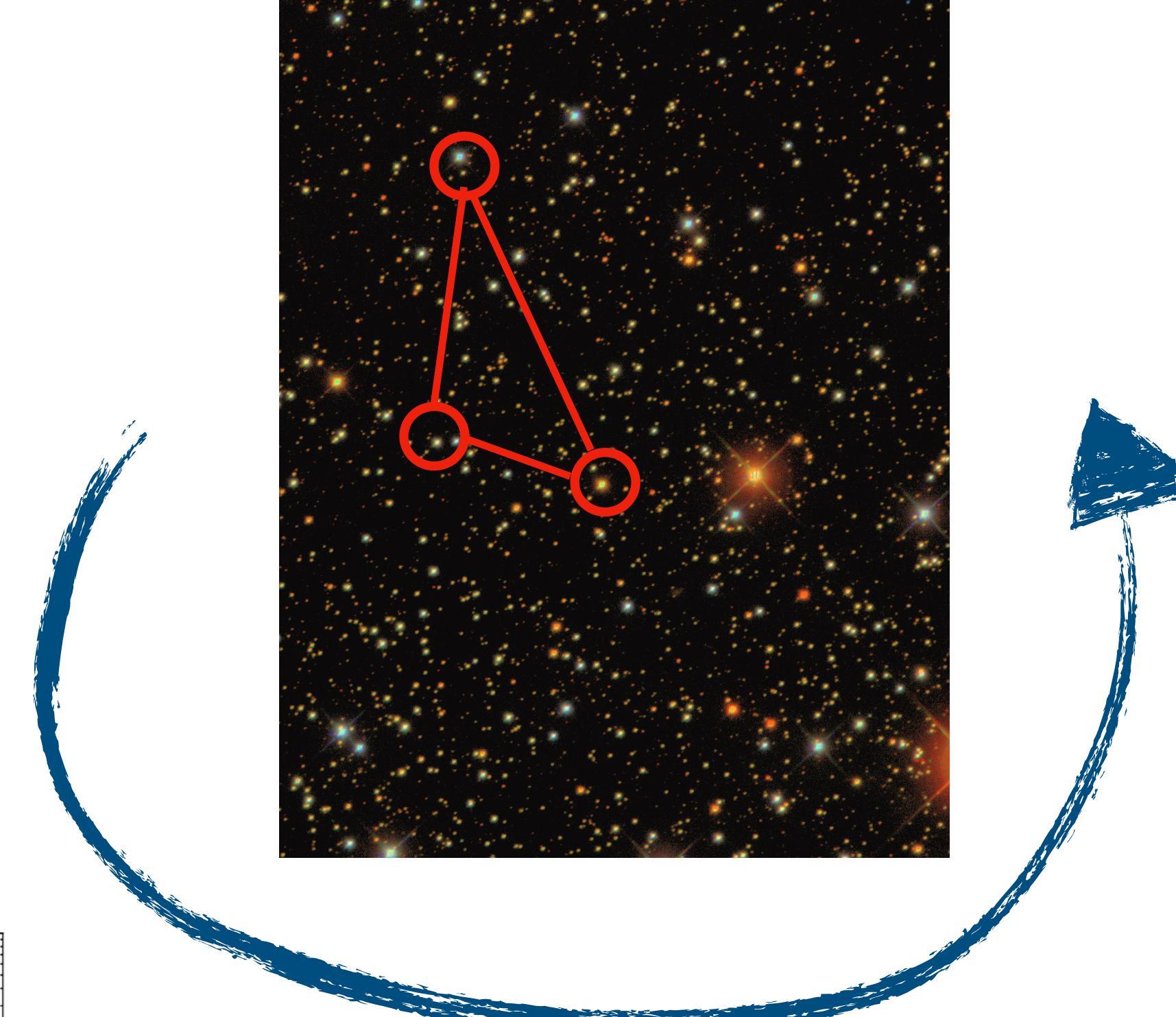
Two-point correlation



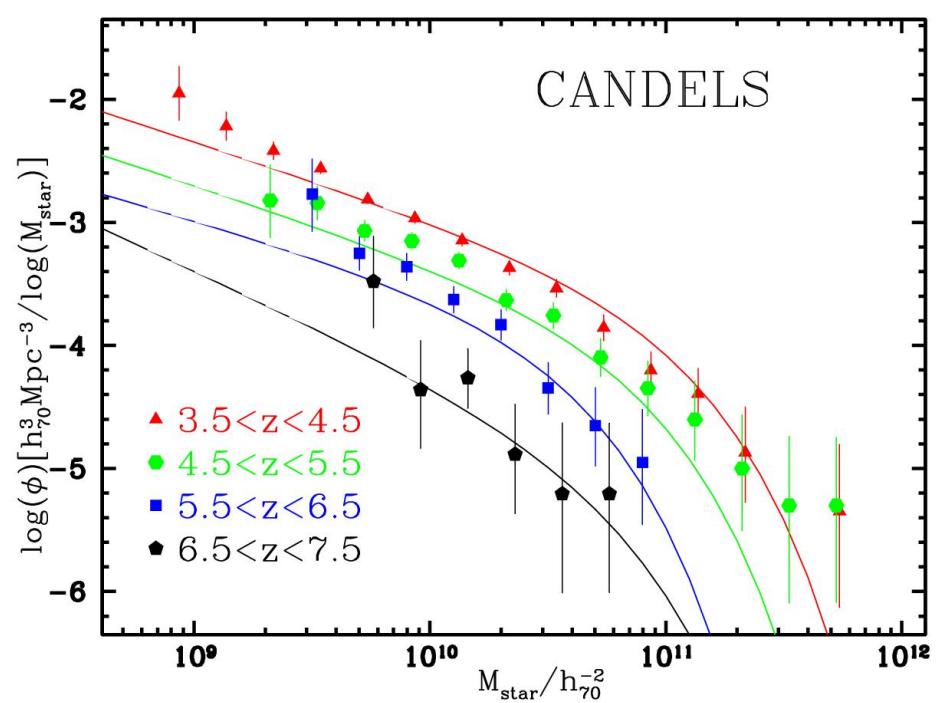
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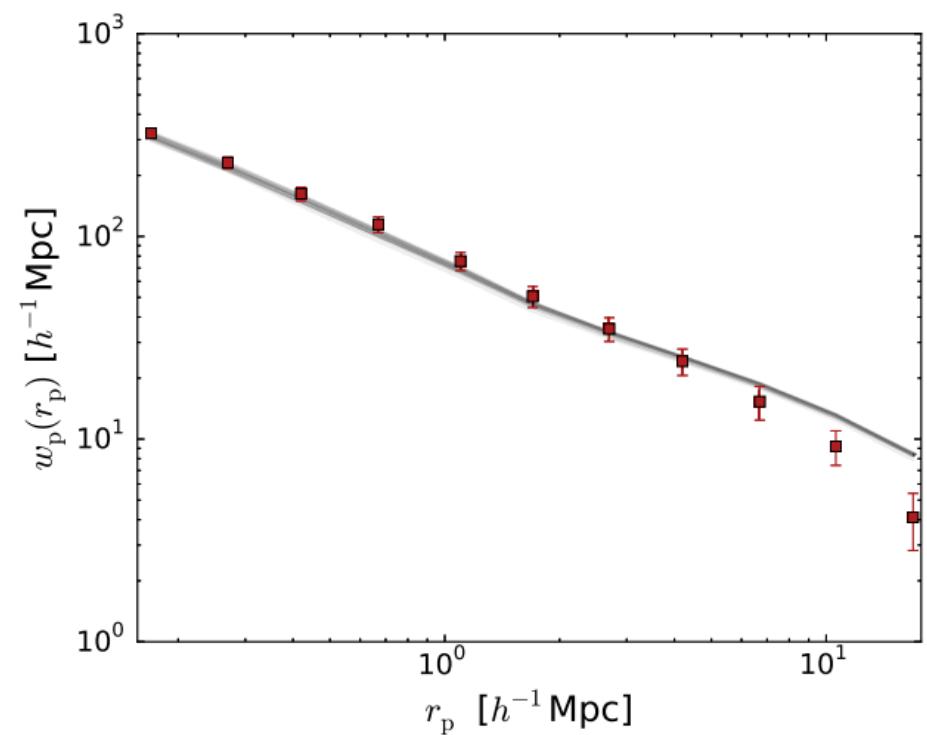
Two-point correlation



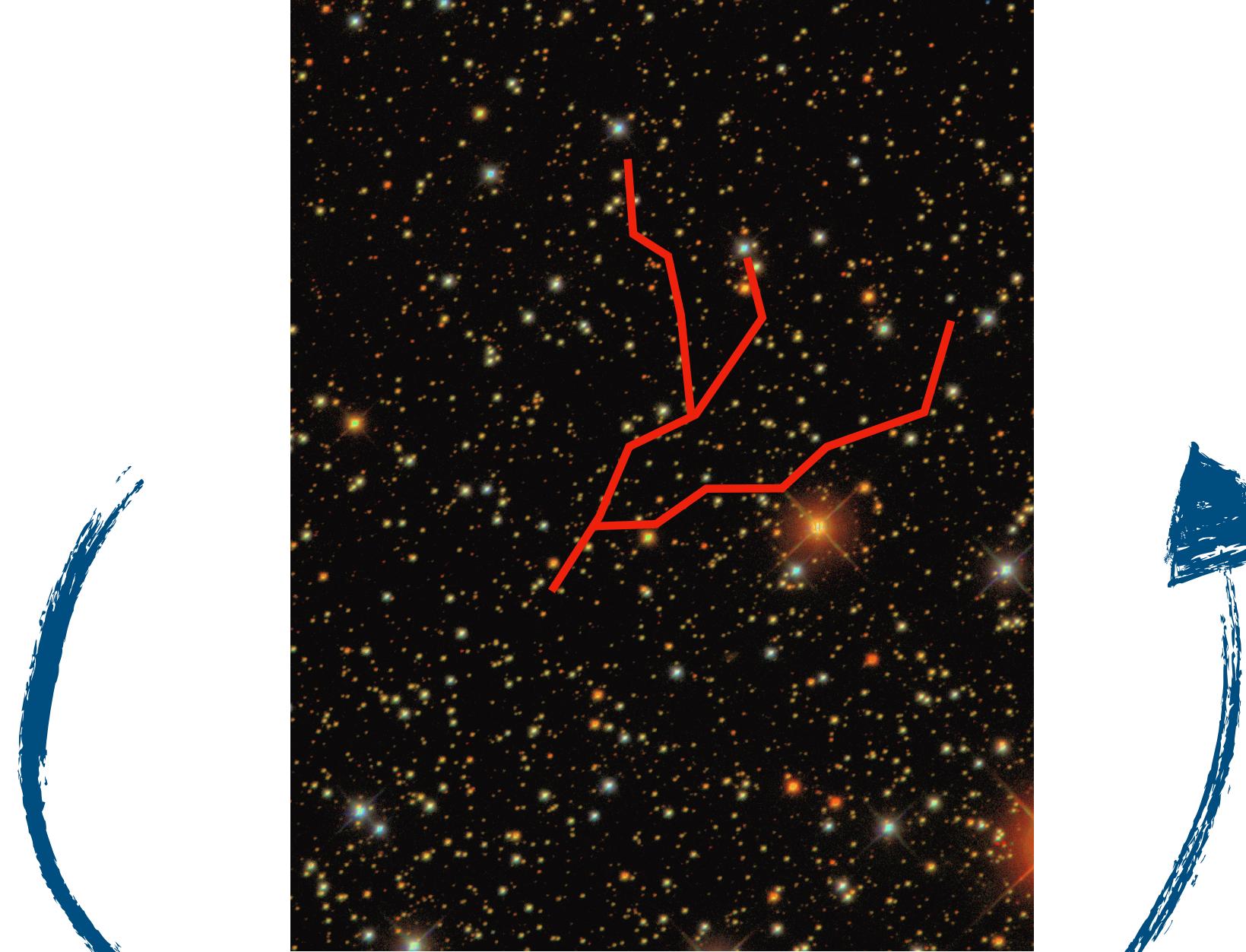
Three-point correlation



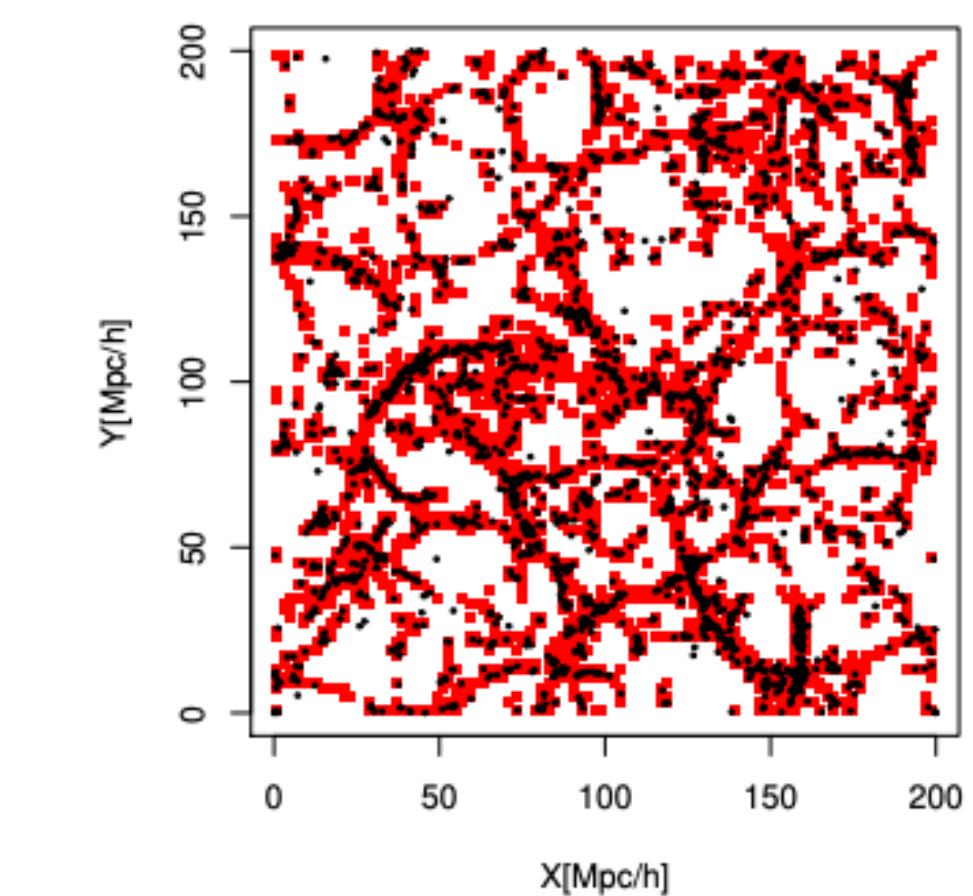
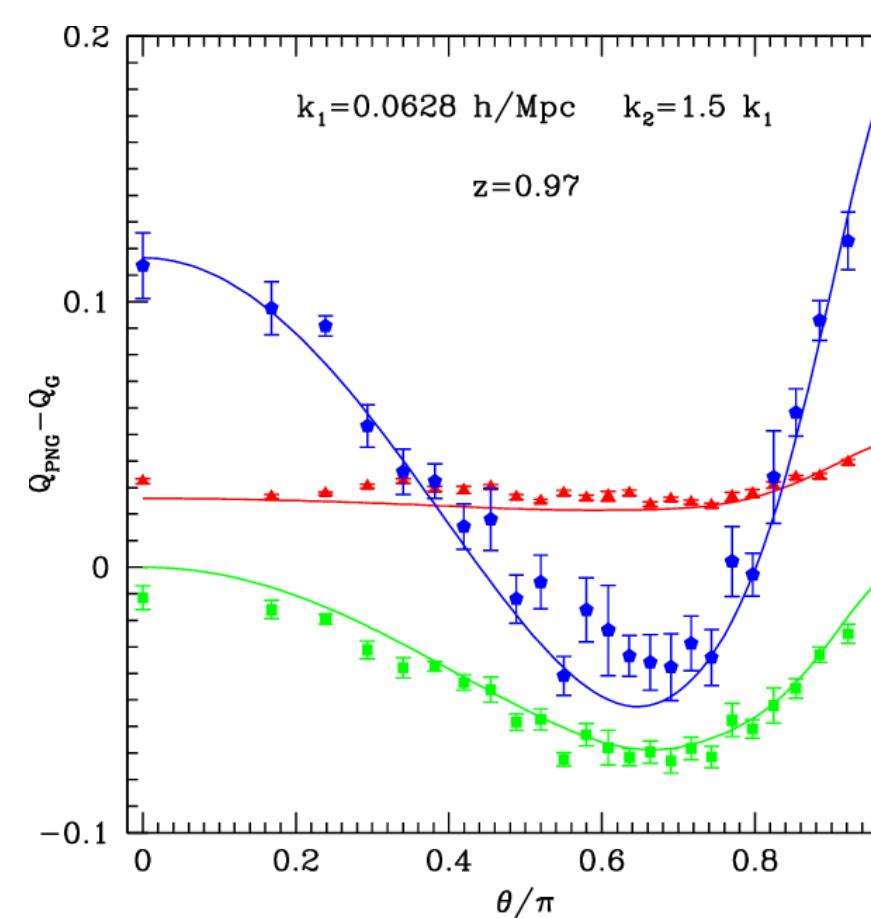
Number counts



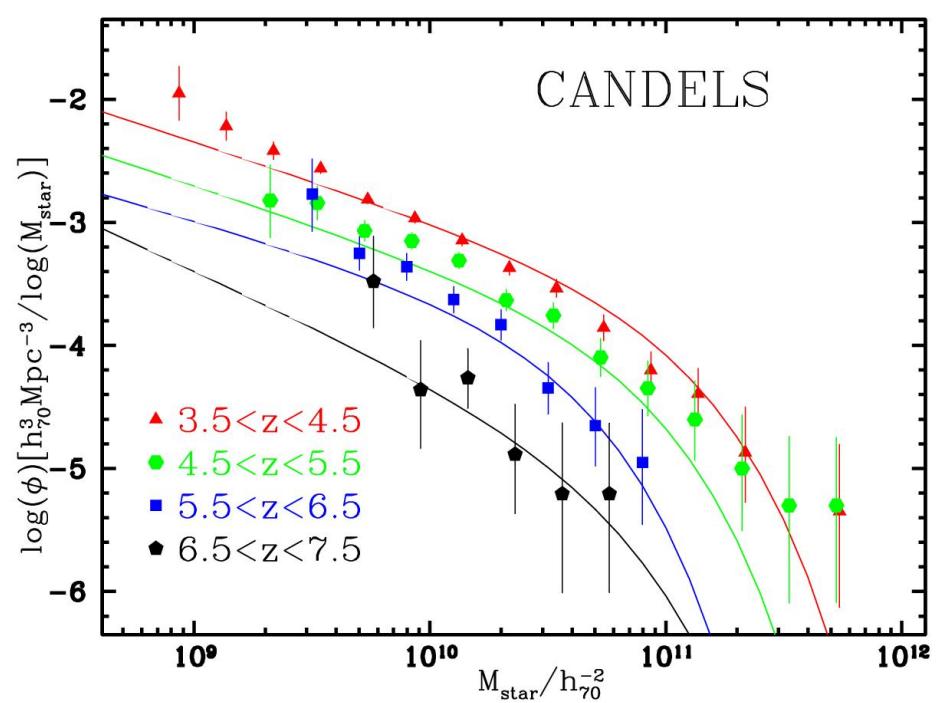
Two-point correlation



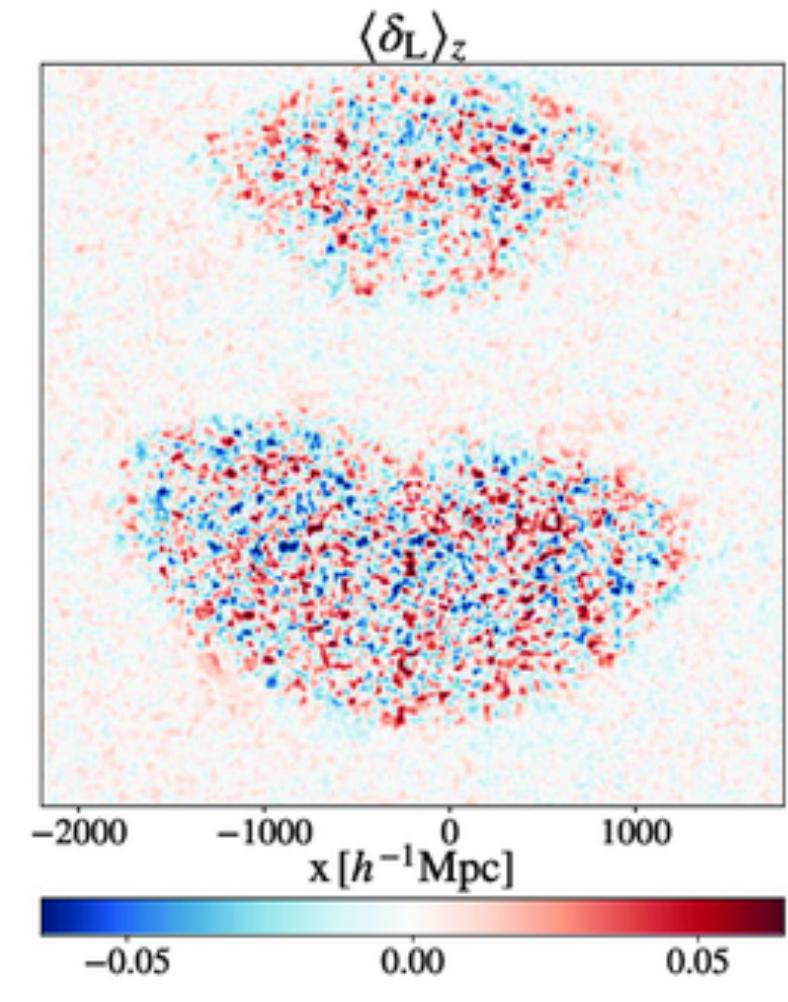
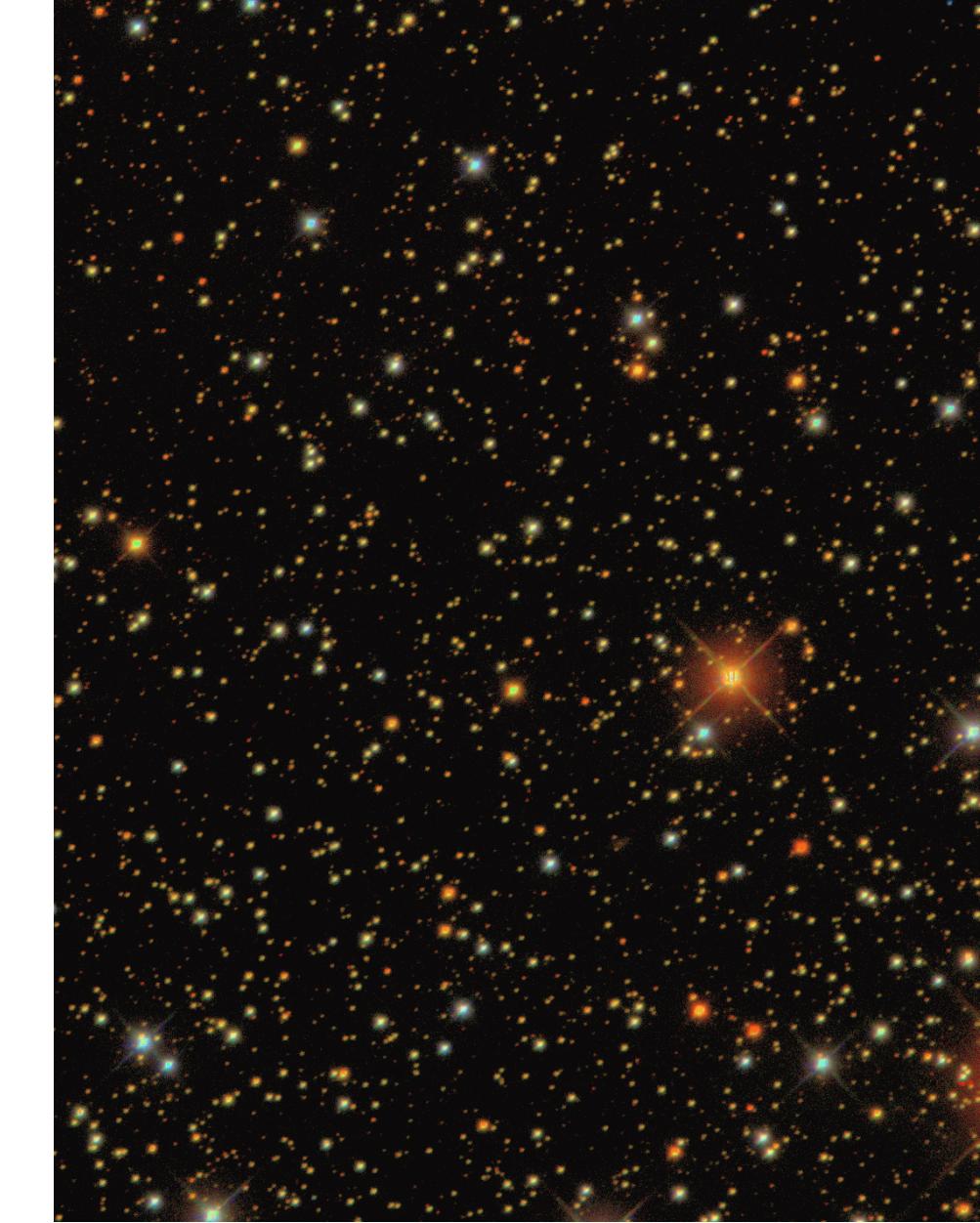
Three-point correlation



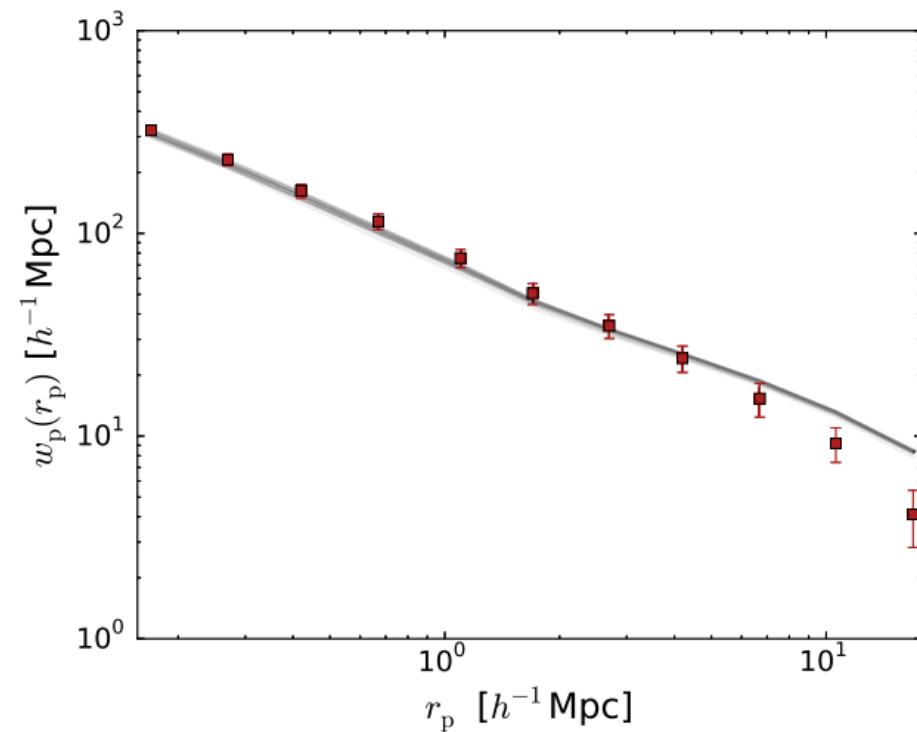
Complex structures
(filaments/voids)



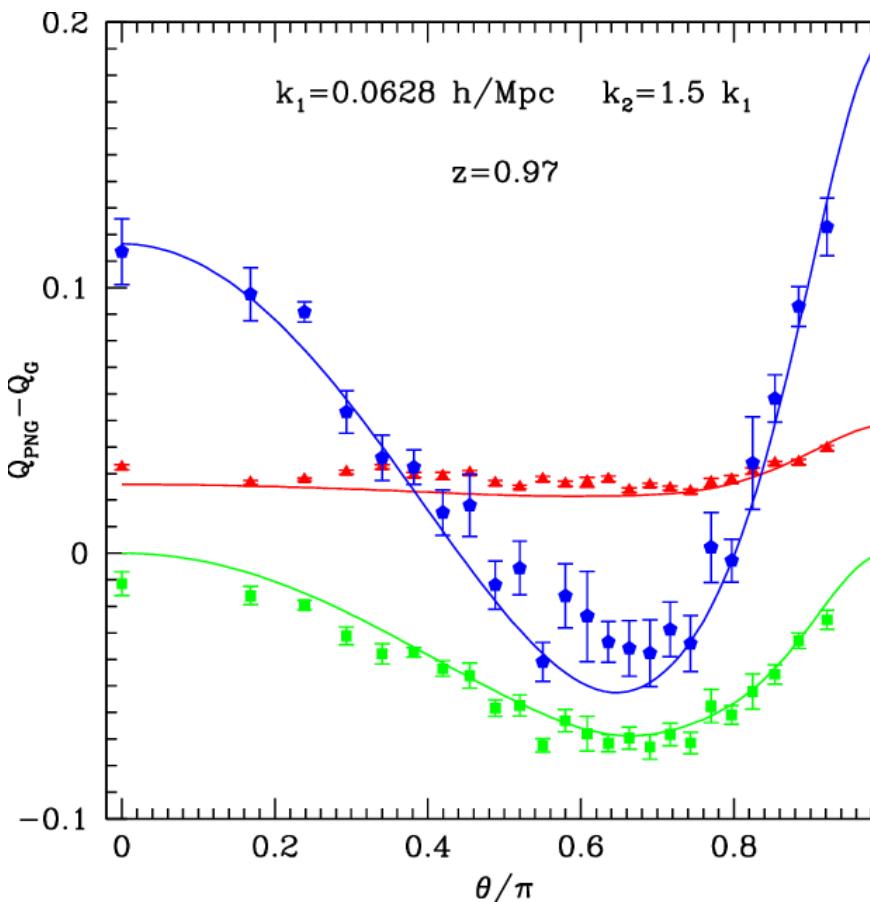
Number counts



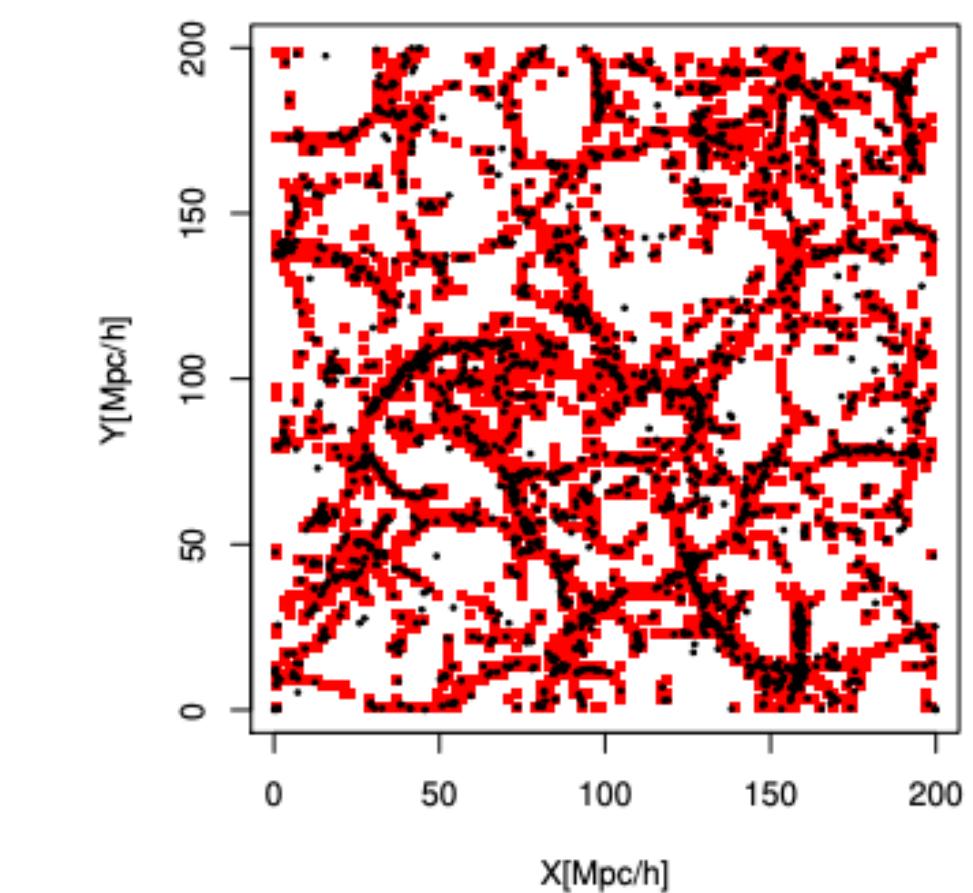
Full-field



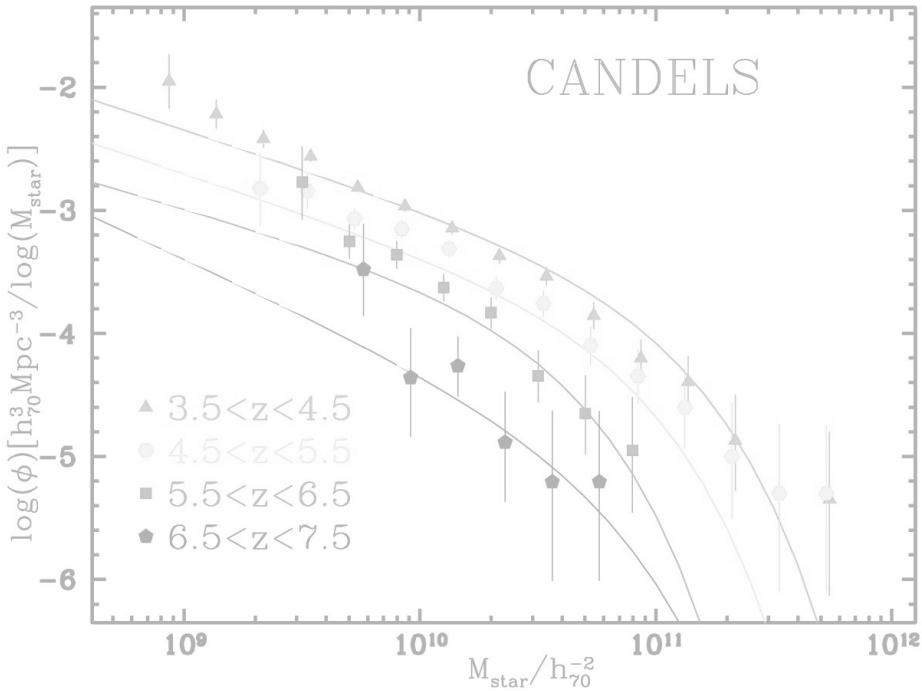
Two-point correlation

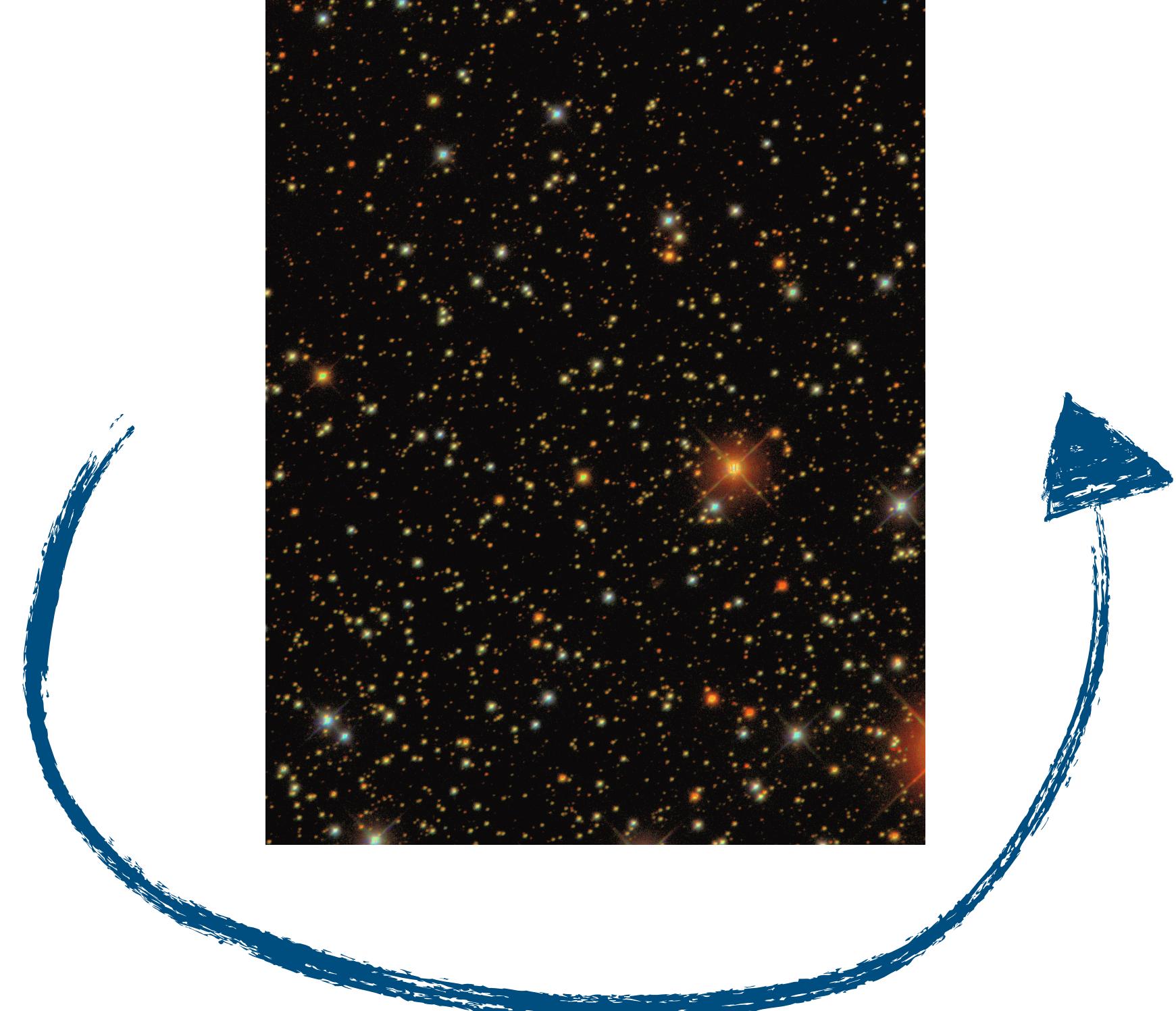


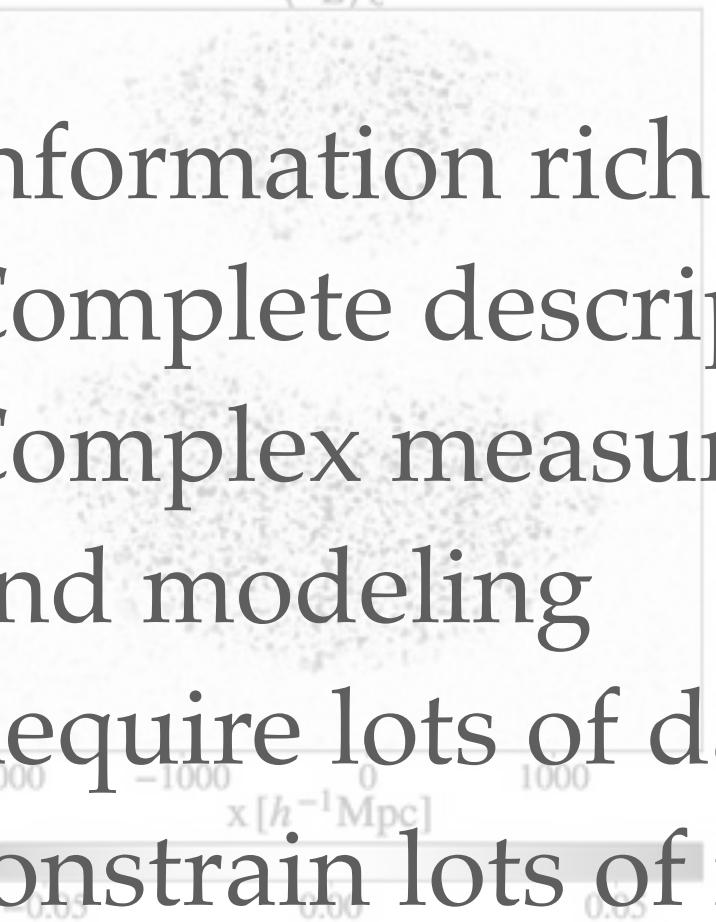
Three-point correlation

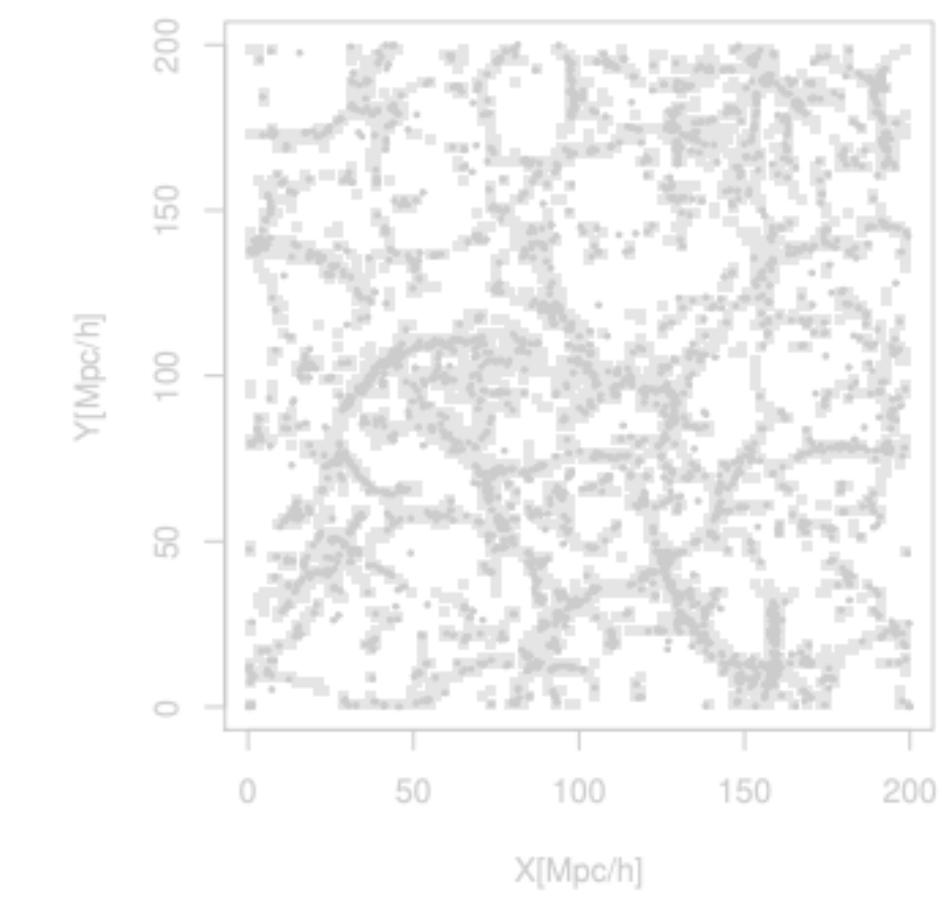
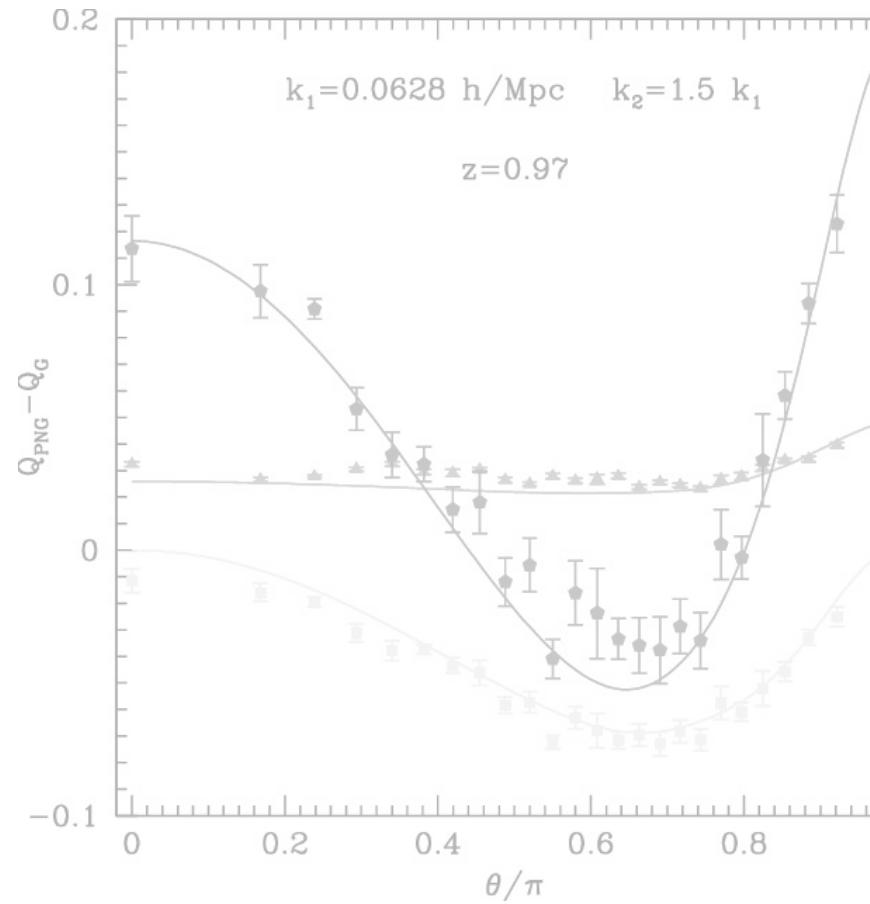


Complex structures
(filaments/voids)

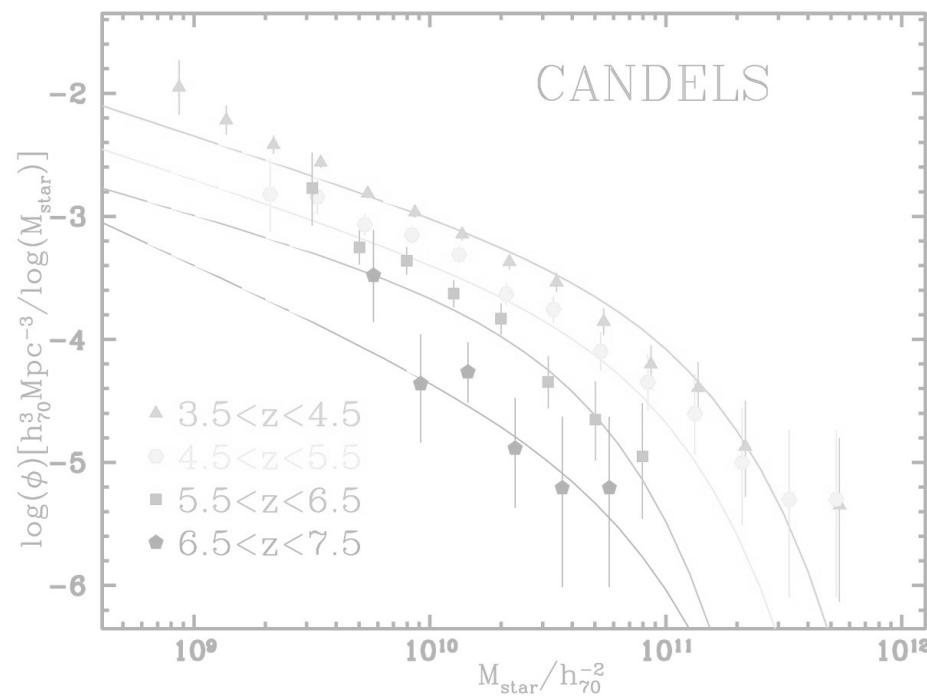
- + Simple measurement and modeling
 - + Require less data and more robust to nuisance parameters
 - Less information
 - Can only test limited range of models
- 
- CANDELS
- $\log(\phi)[h_{70}^3 \text{Mpc}^{-3}/\log(M_{\star})]$
- M_{\star}/h_{70}^{-2}
- Legend: $3.5 < z < 4.5$ (triangles), $4.5 < z < 5.5$ (circles), $5.5 < z < 6.5$ (squares), $6.5 < z < 7.5$ (diamonds)



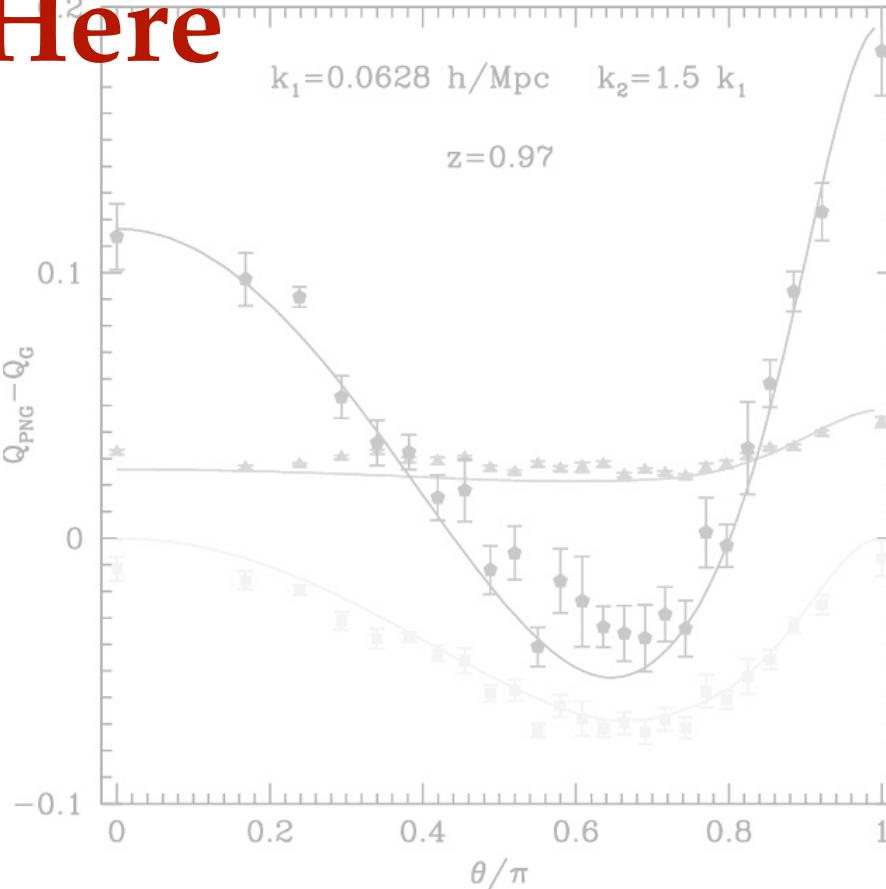
- + Information rich
 - + Complete description
 - Complex measurement and modeling
 - Require lots of data to constrain lots of model parameters
- 
- $\langle \delta_L \rangle_z$
- $x [h^{-1}\text{Mpc}]$



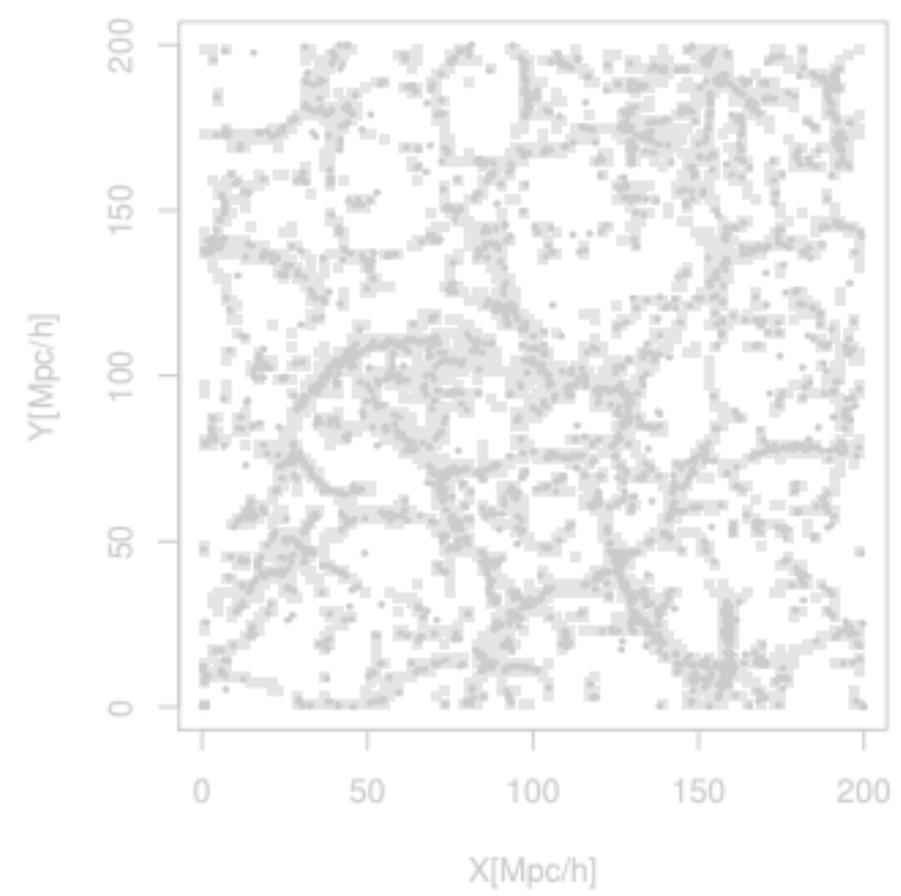
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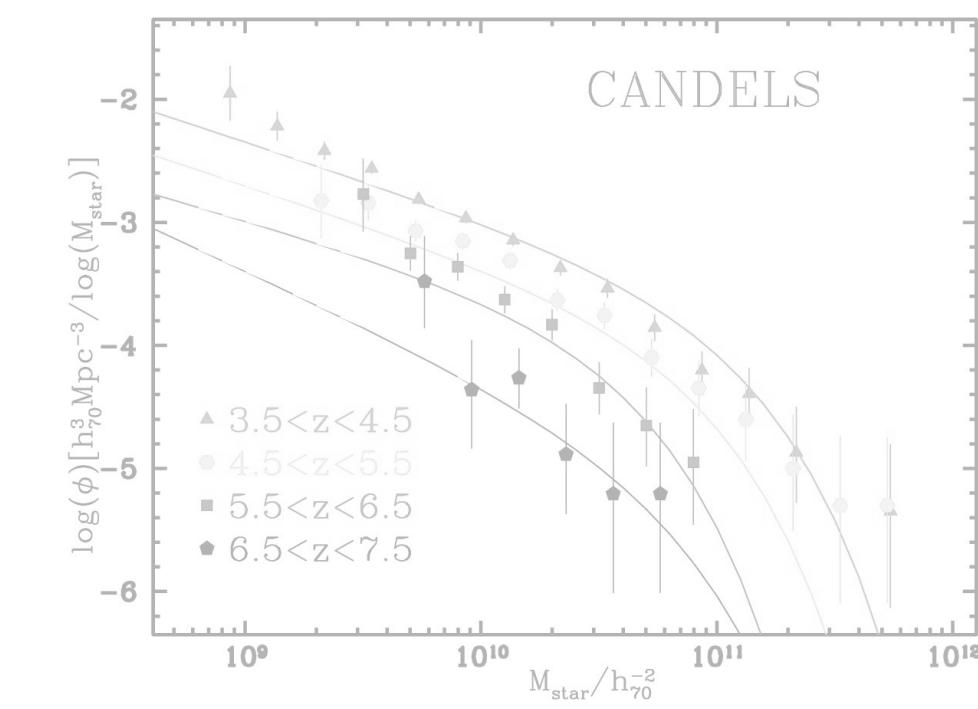


We Are Here

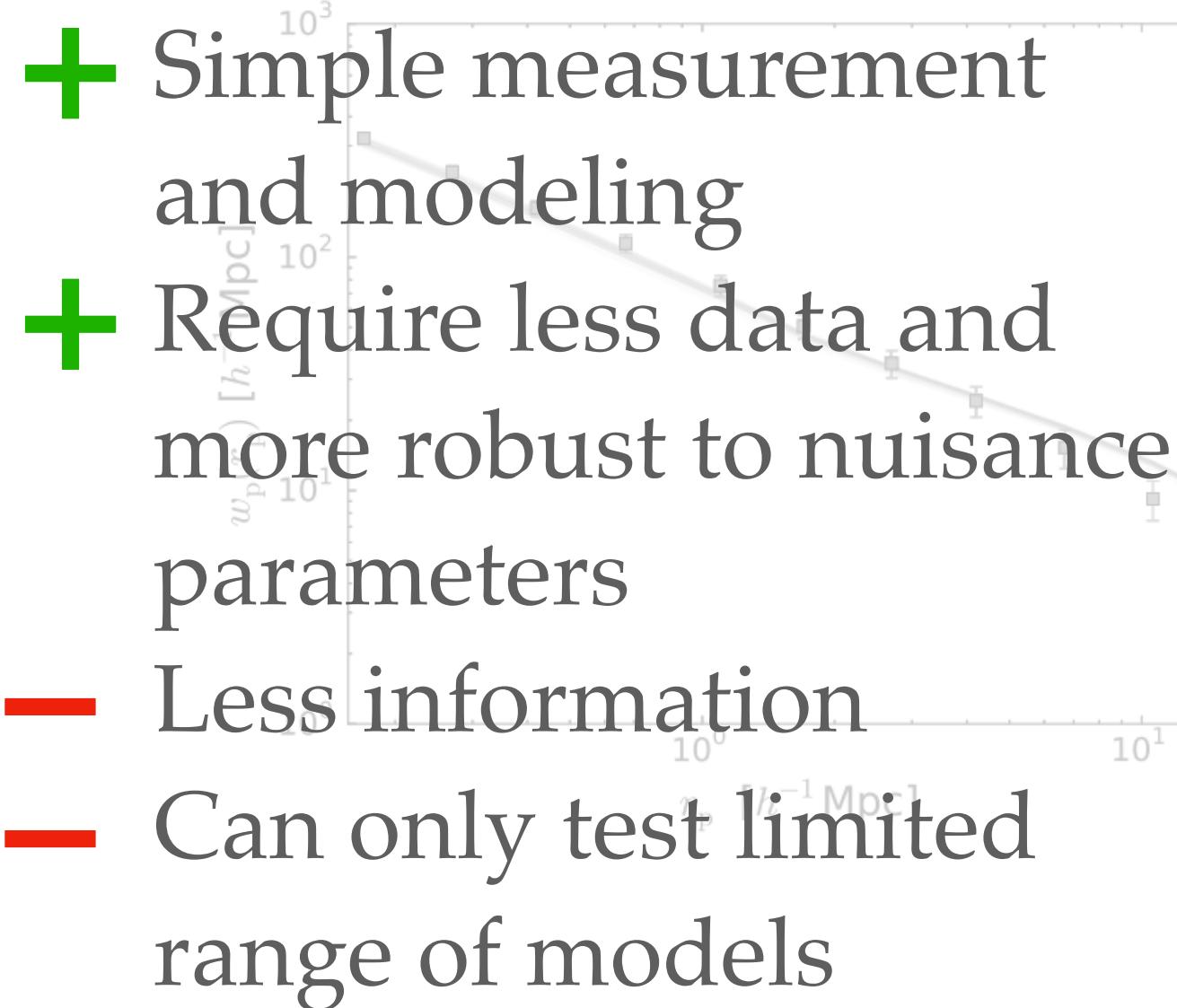
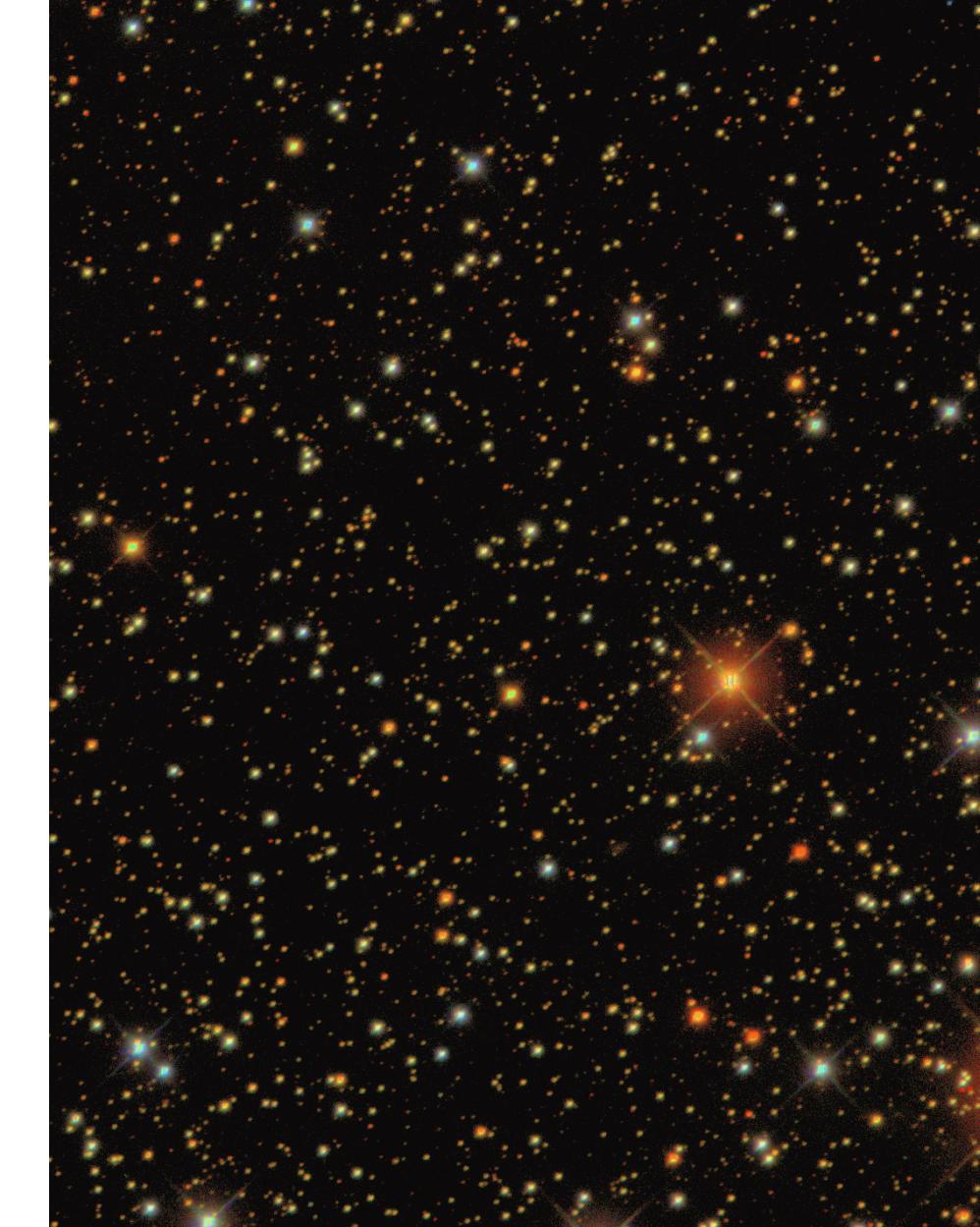


- + Information rich
- + Complete description
- Complex measurement and modeling
- Require lots of data to constrain lots of model parameters

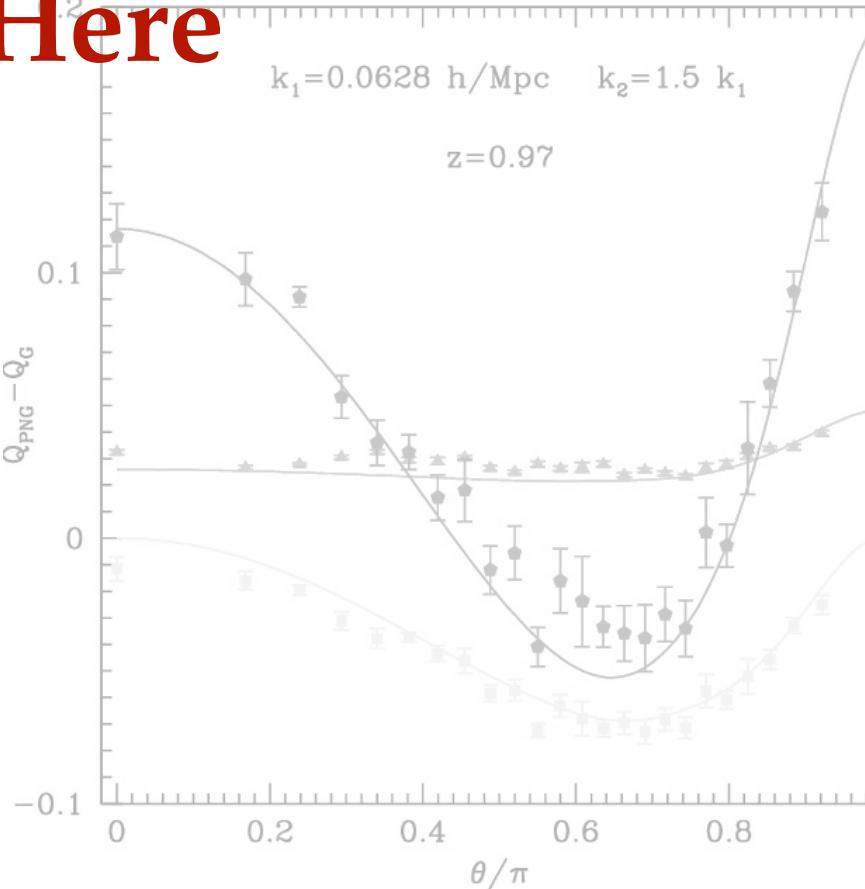




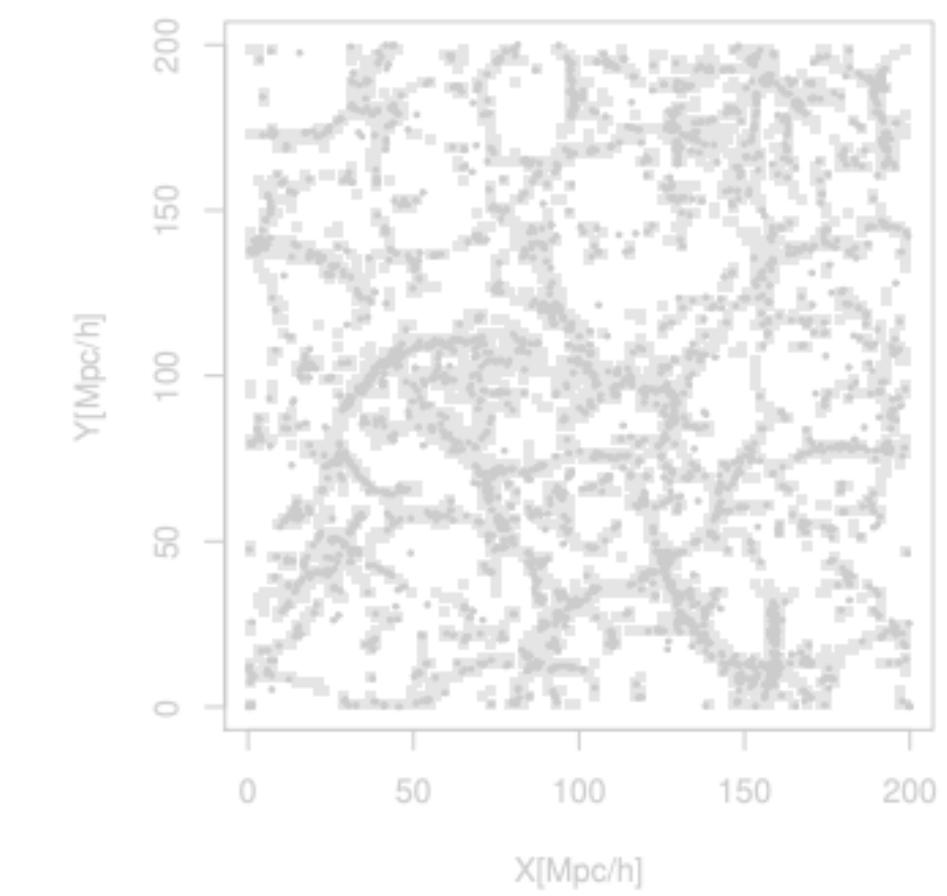
10 years ago



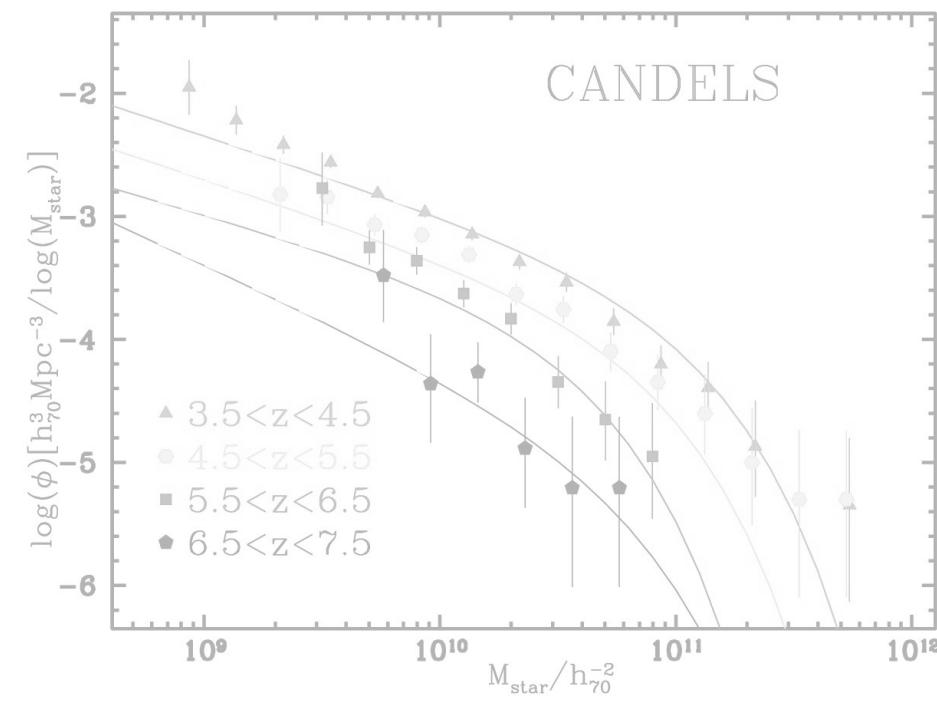
We Are Here



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- + Complete description
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- Require lots of data to constrain lots of model parameters

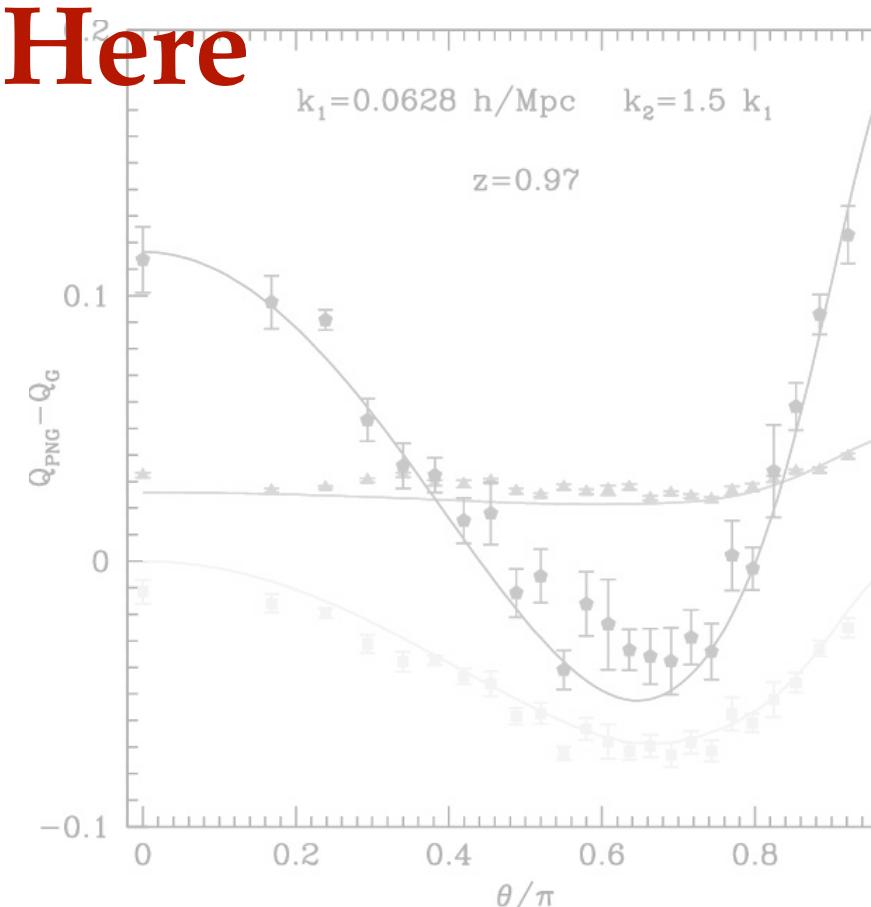


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- Can only test limited range of models



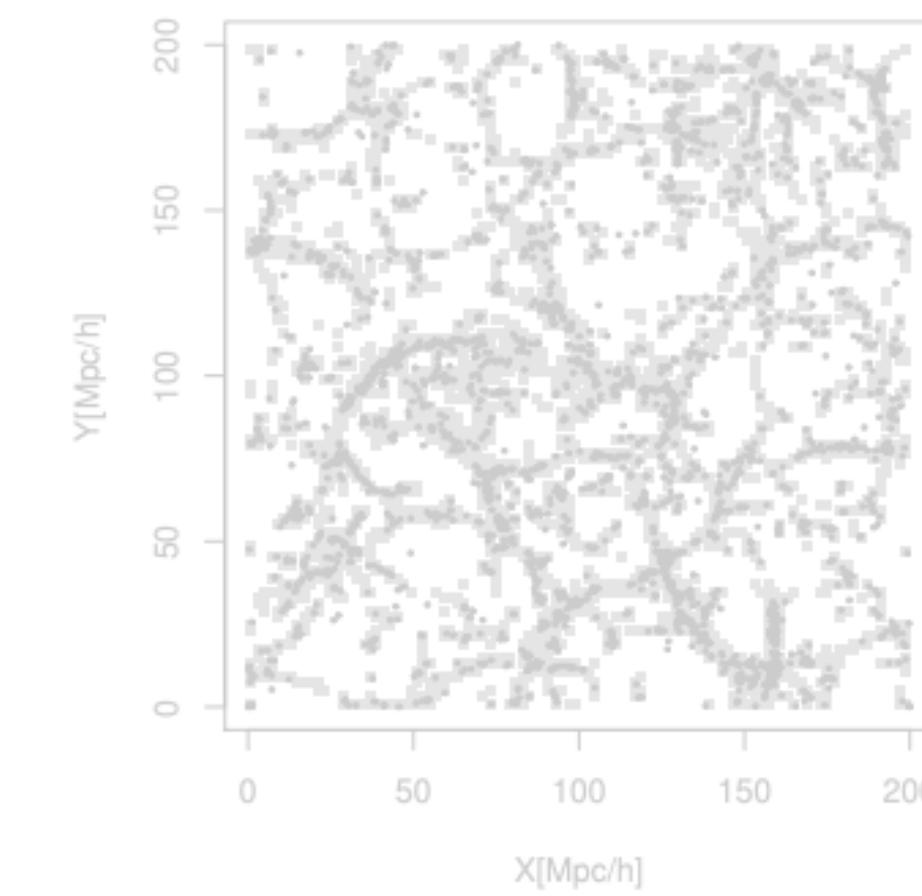
10 years ago

We Are Here



- + Information rich
- + Complete description
- Complex measurement and modeling
- Require lots of data to constrain lots of model parameters

10 years from now?



Lensing Higher-Order Statistics (HOS)

N-point correlations and related

N-point correlation function / N-spectrum

Mass aperture statistics and their moments

Moments / Cumulative Distribution Functions

Integrated N-point correlation function

Density-split statistics

Peaks / voids

Topological statistics (Minkowski, Betti #, persistent homology)

Wavelets / scattering transform

Field-level inference

*Bayesian hierarchical
modelling*

Deep learnings, e.g. CNN

Summary statistics

Petri et al. (2015), Gruen et al. (2018), Allys et al. (2020), Halder et al. (2021), Zücher et al. (2021),
Banerjee & Abel (2021), Fluri et al. (2022), Lanzieri et al. (2023)...

Lensing Higher-Order Statistics (HOS)

See also talk (and references) from

N-point correlations and related

N-point correlation function / N-spectrum

Mass aperture statistics and their moments

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Jia

Bhuv

Joachim

Daniela

Niall

Judit

Lucas

Jason

Eleni

Arthur

Supranta

Adrian

Sihao

Luisa

...

Outline

- The Λ CDM paradigm and extracting information beyond 2pt
- **Practical challenges: beyond 2pt systematics**
- Opportunities: primordial non-Gaussianity
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- Summary & outlook

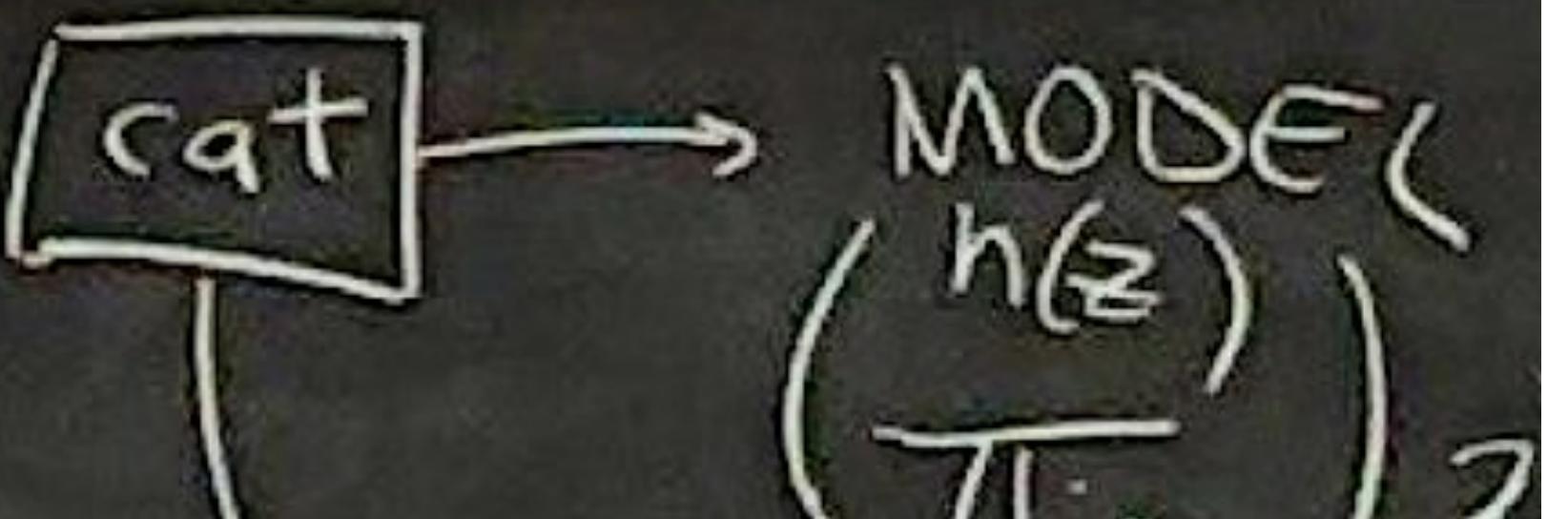
Anbajagane, CC, Banerjee et al. (2024)



Dhayaa Anbajagane

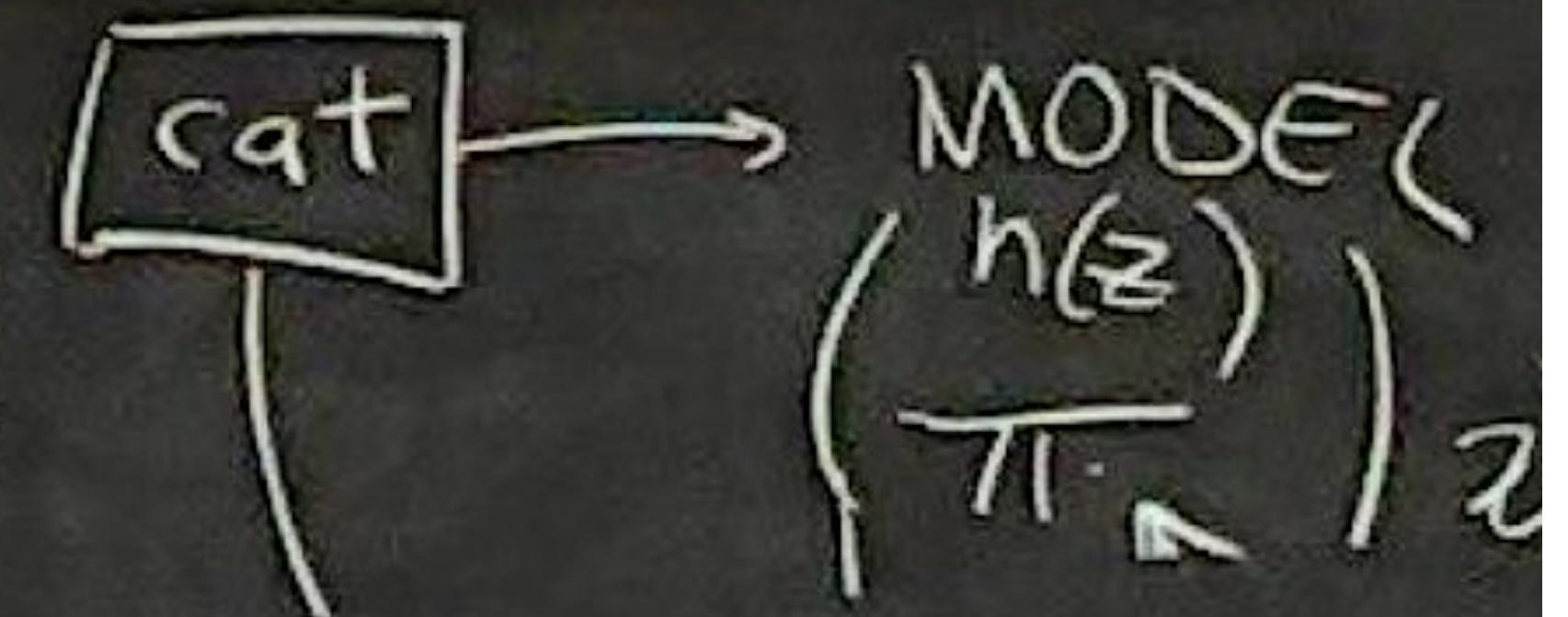
Arka Banerjee

What does it take for you
to trust HOS @ same level as 2pt?



• What does it take for you
to trust HOS @ same level as 2pt?

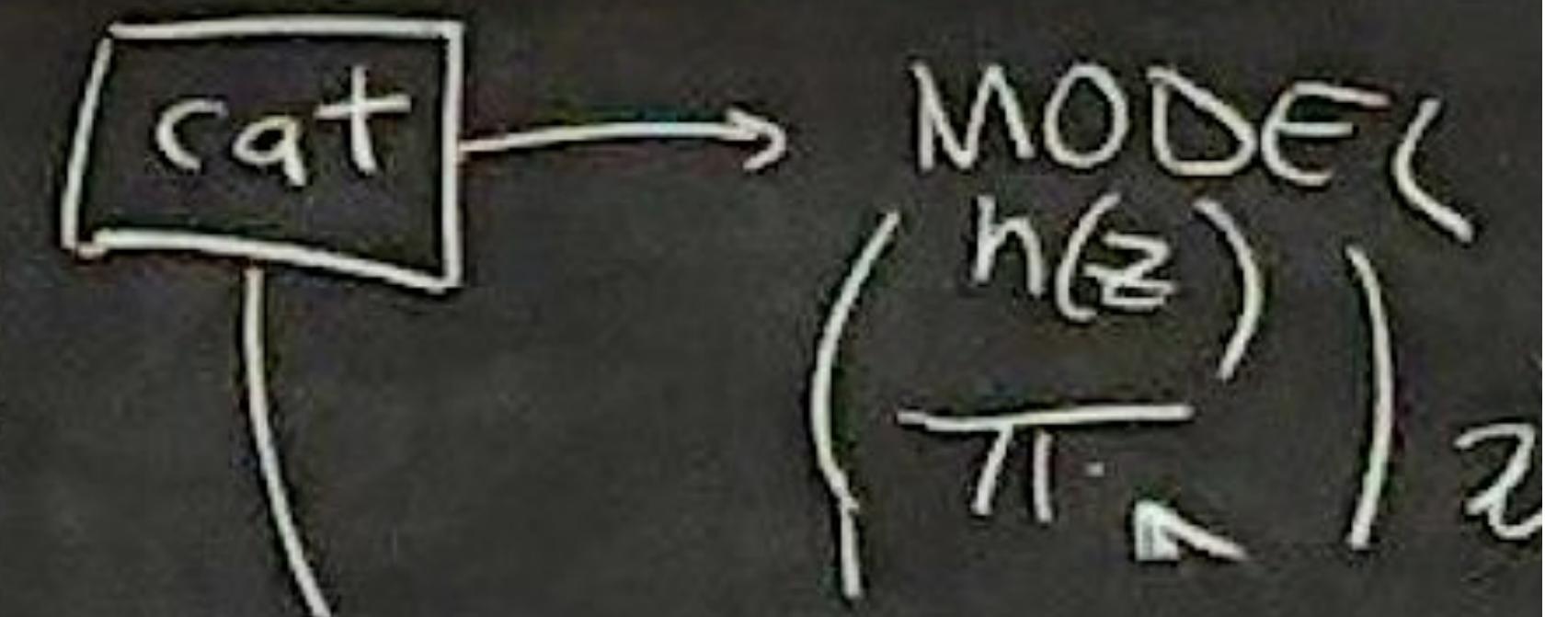
- ① Blinding
- ② Covariance (zpt is mature)
- ③ no analytical cross-check (cf. sim-based)
- ④ Gaussian likelihood ($\rightarrow LFI$)
- ⑤ EMULATOR
 - ⑥ knowing limits
of method
- ⑦ Null tests
- ⑧ Simplicity



easy to test w/ diff stats?
can recycle part of 2pt info?

• What does it take for you
to trust HOS @ same level as 2pt?

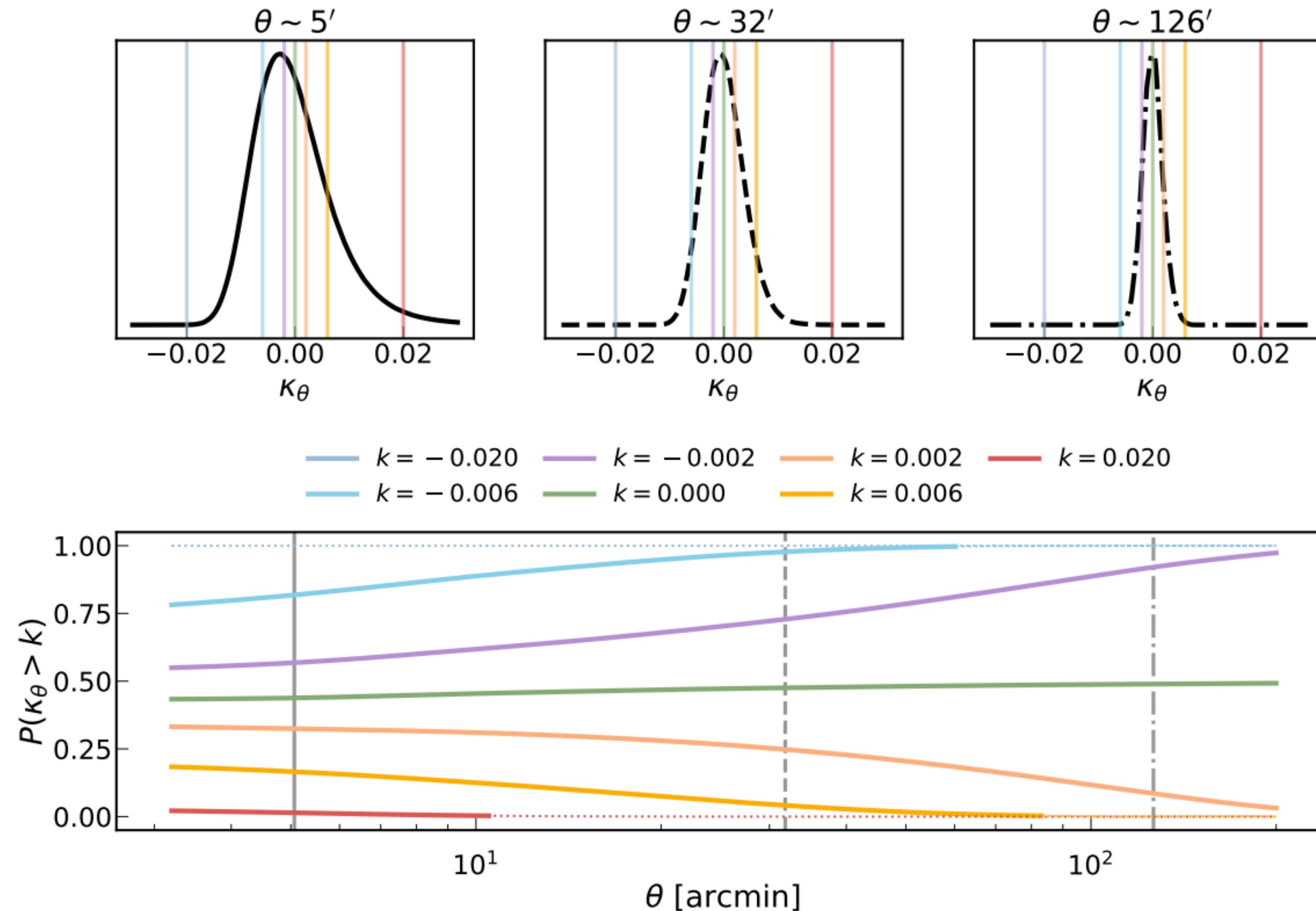
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easy to test w/ diff stats?
can recycle part of 2pt info?

Bridging the gap between communities
(Many of you are working on this!)

Towards robust HOS: scale-dependent CDFs



The first question to ask

- How much information is there in the field? And how much can we practically extract considering both systematic effects and computational limitations?

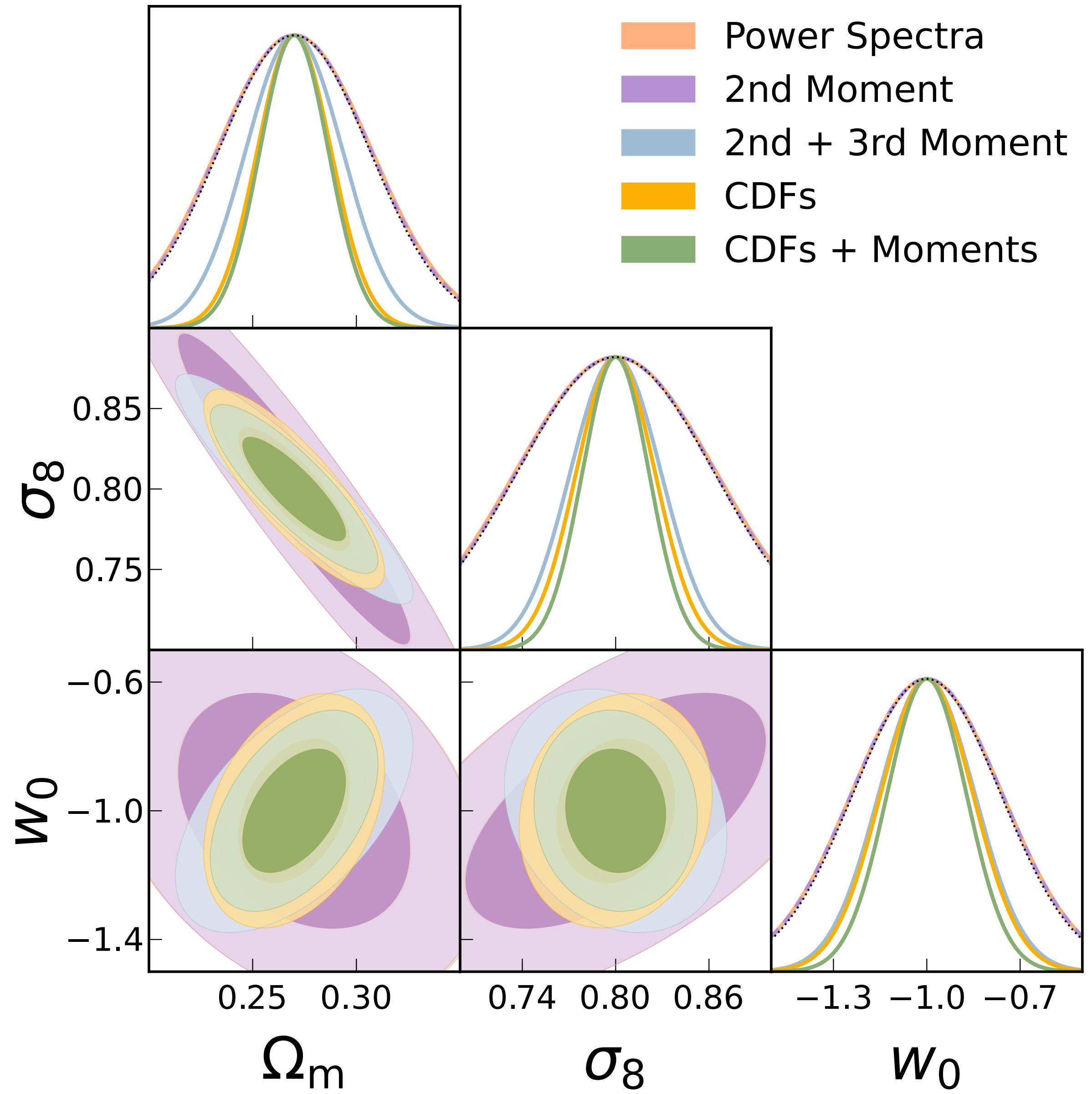
The first question to ask

- How much information is there in the field? And how much can we practically extract considering both systematic effects and computational limitations?
- The answer to these questions depends on
 - The science question of interest (w / LCDM, EDE, fNL, non-CDM)
 - The dataset (density / galaxy, redshift, noise, systematics)
 - The implementation (statistics, inference, sampling)

A simple exploration

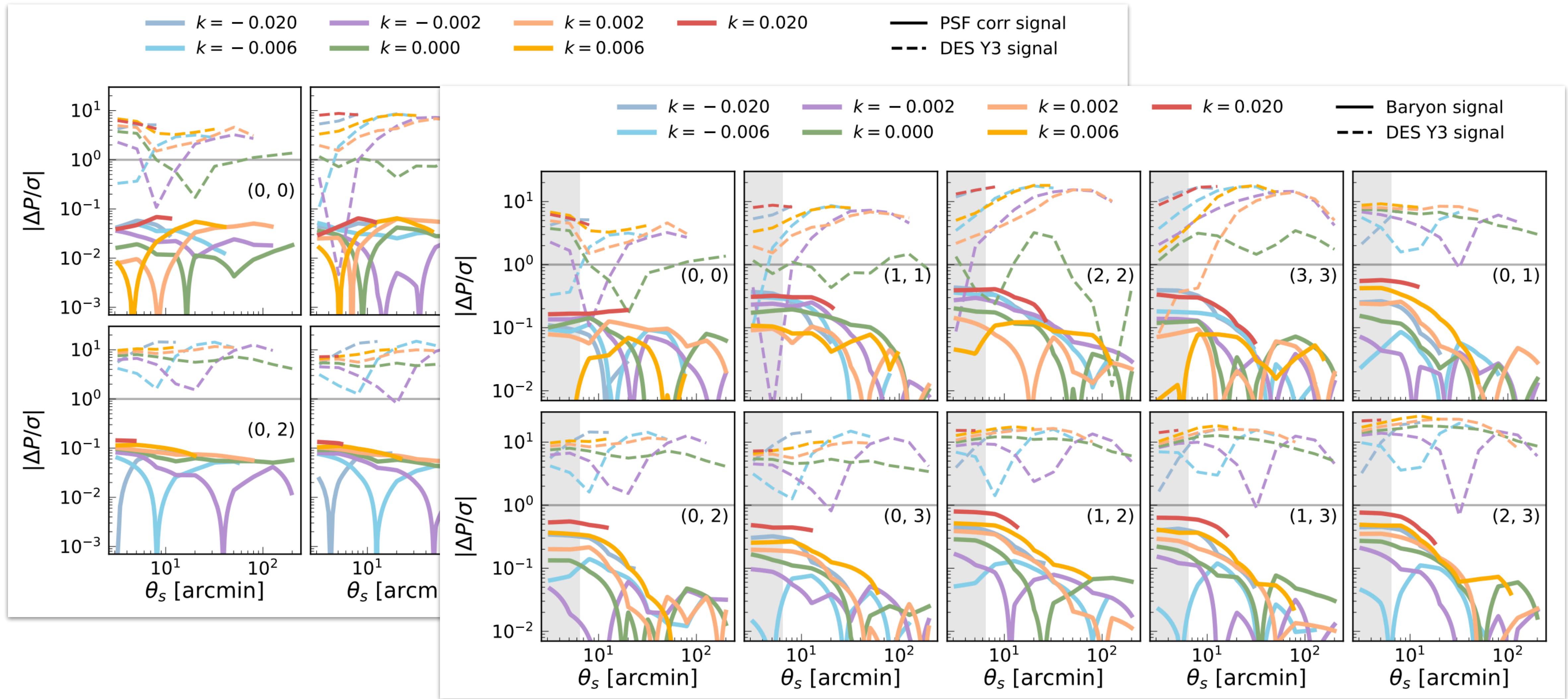
- Assuming
 - wCDM
 - DES Y3-like lensing
 - Fixed scale
 - Moments and CDFs*
- A simple analysis says that we gain significantly (3x in area) going from 2pt to 3pt, and much less after that

Recall Bhuv and Sihao's talk



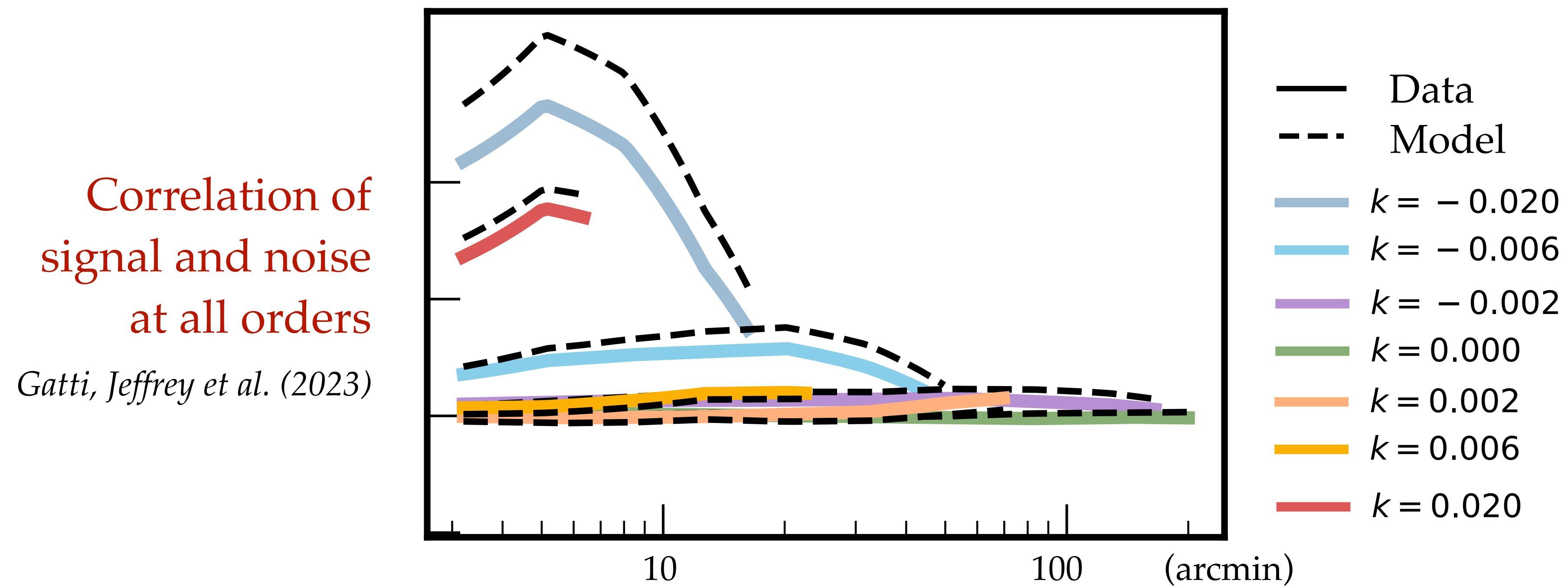
* no directional information

Next, redo all the 2pt tests...



But that may not be sufficient!

- New systematic effects could appear at higher order



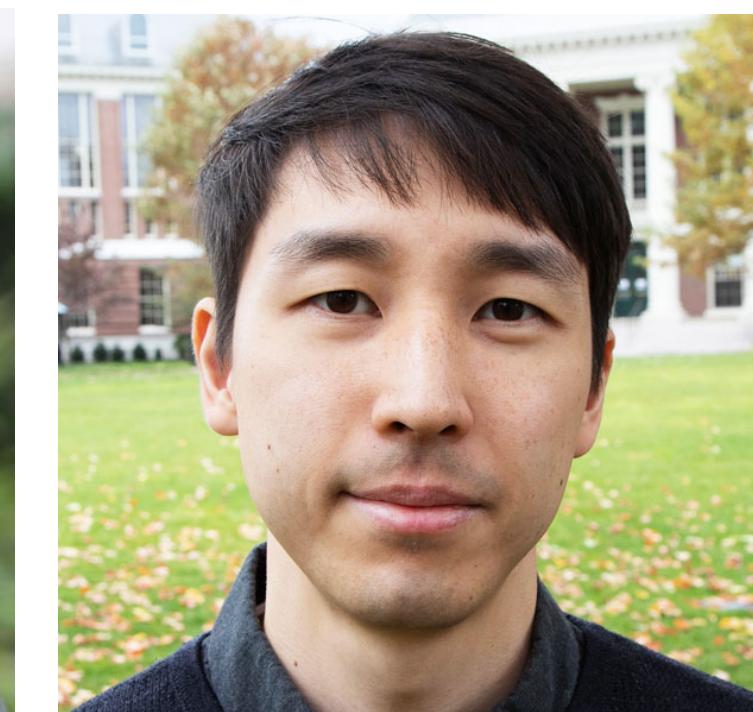
Robust HOS

- For data in the near future and wCDM/LCDM, having a 3pt-level pipeline could bring us a long way way to extracting all the accessible non-Gaussian information
- Ensuring that the analysis is robust to all sources of systematic effects (at least at the 3pt level) is crucial for having HOS be trusted to the same level as 2pt
- It is encouraging that people are working on these (sometimes tedious) tasks and working together with people familiar with 2pt analyses

Outline

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- Practical challenges: beyond 2pt systematics
- **Opportunities: primordial non-Gaussianity**
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- Summary & outlook

Anbajagane, CC, Lee, Gatti (2024)



Dhayaa Anbajagane

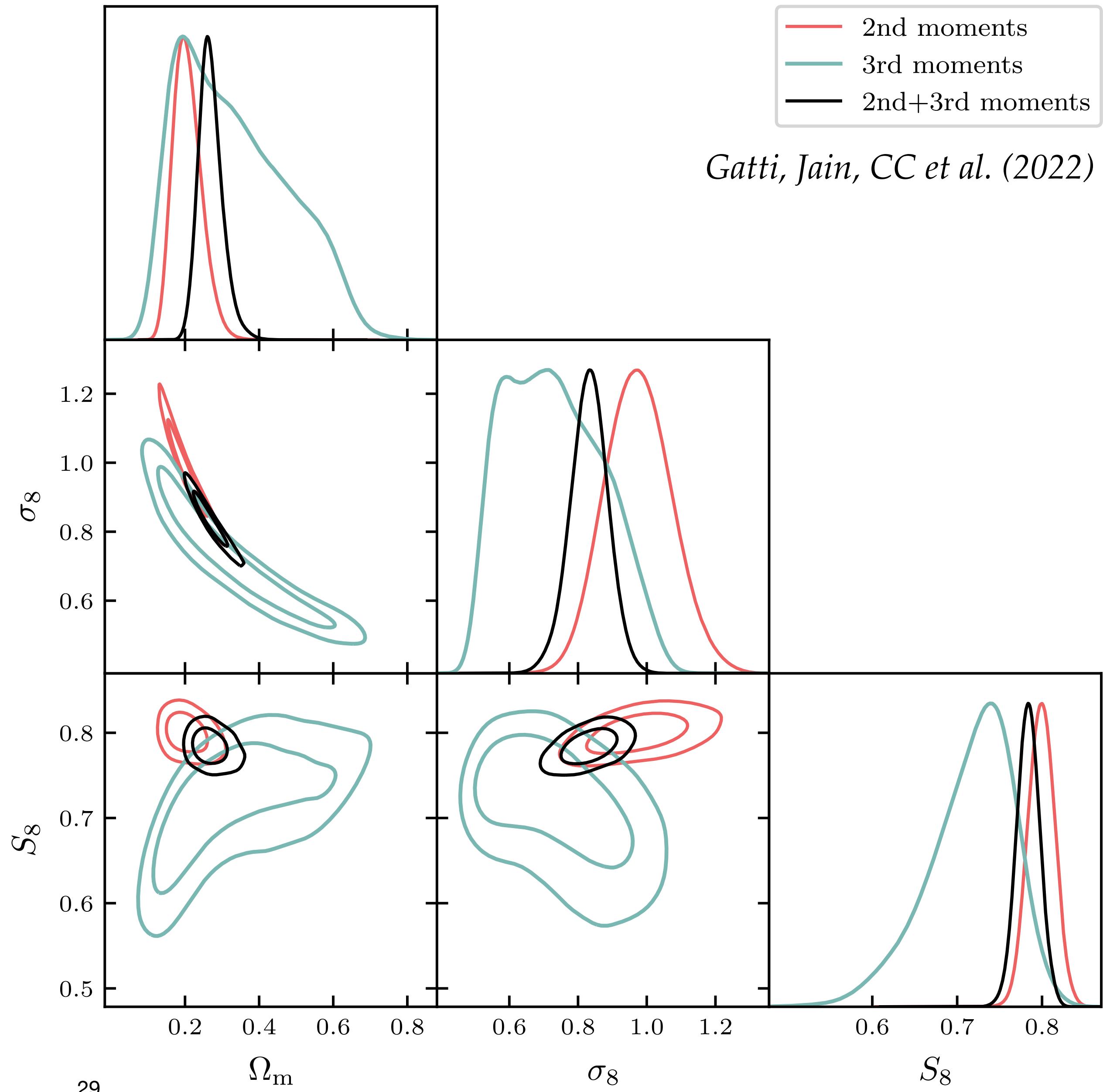
Hayden Lee

Marco Gatti

wCDM/LCMD

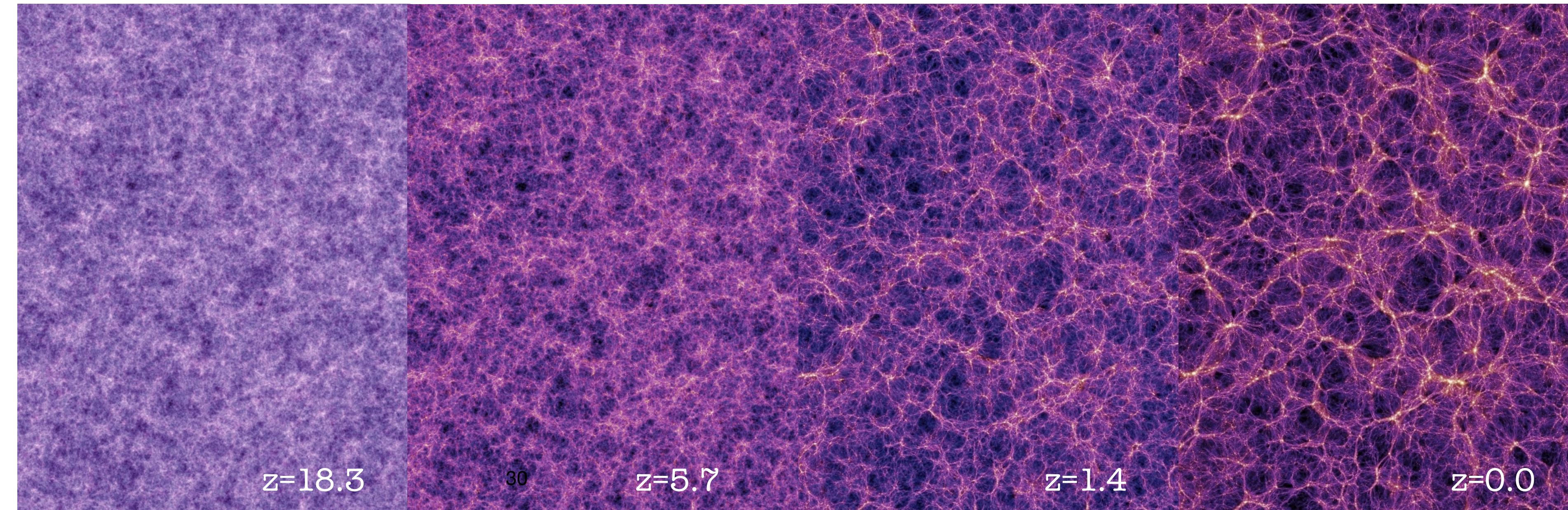
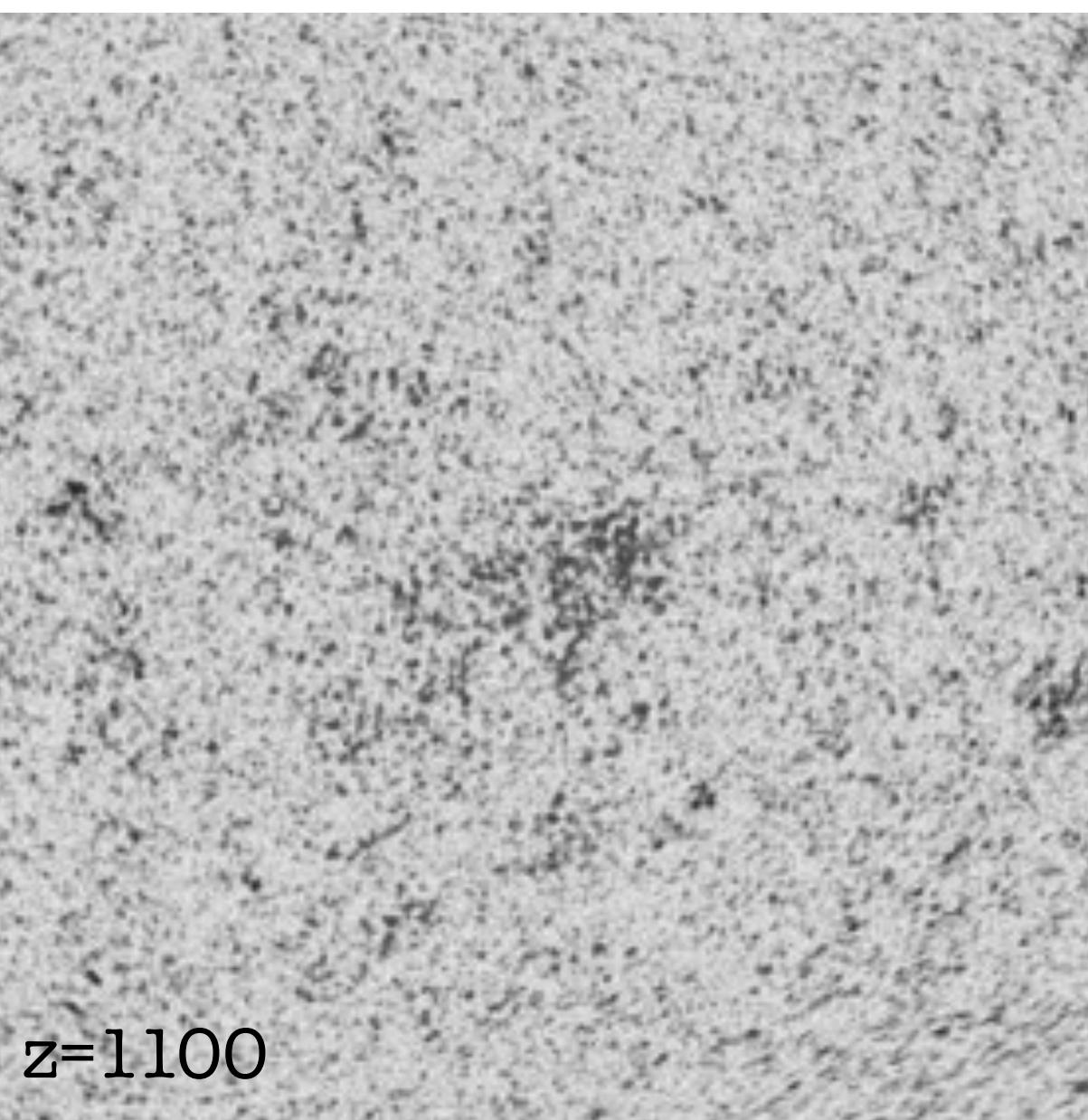
- Most literature today use HOS to extract information beyond 2pt in the field to constrain wCDM/LCDM
- This makes sense since gravity is highly non-Gaussian, there's a lot of information we are leaving behind when we only do 2pt

See talks from Bhuv, Joachim, Daniela, Niall, Judit, Supranta...



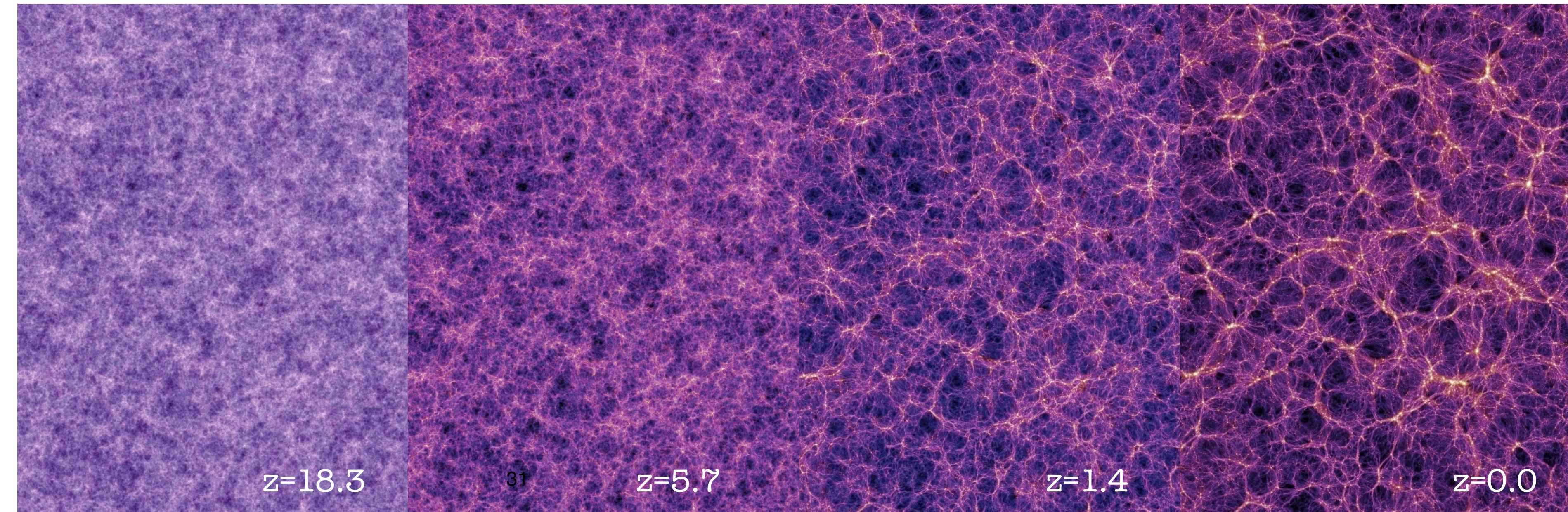
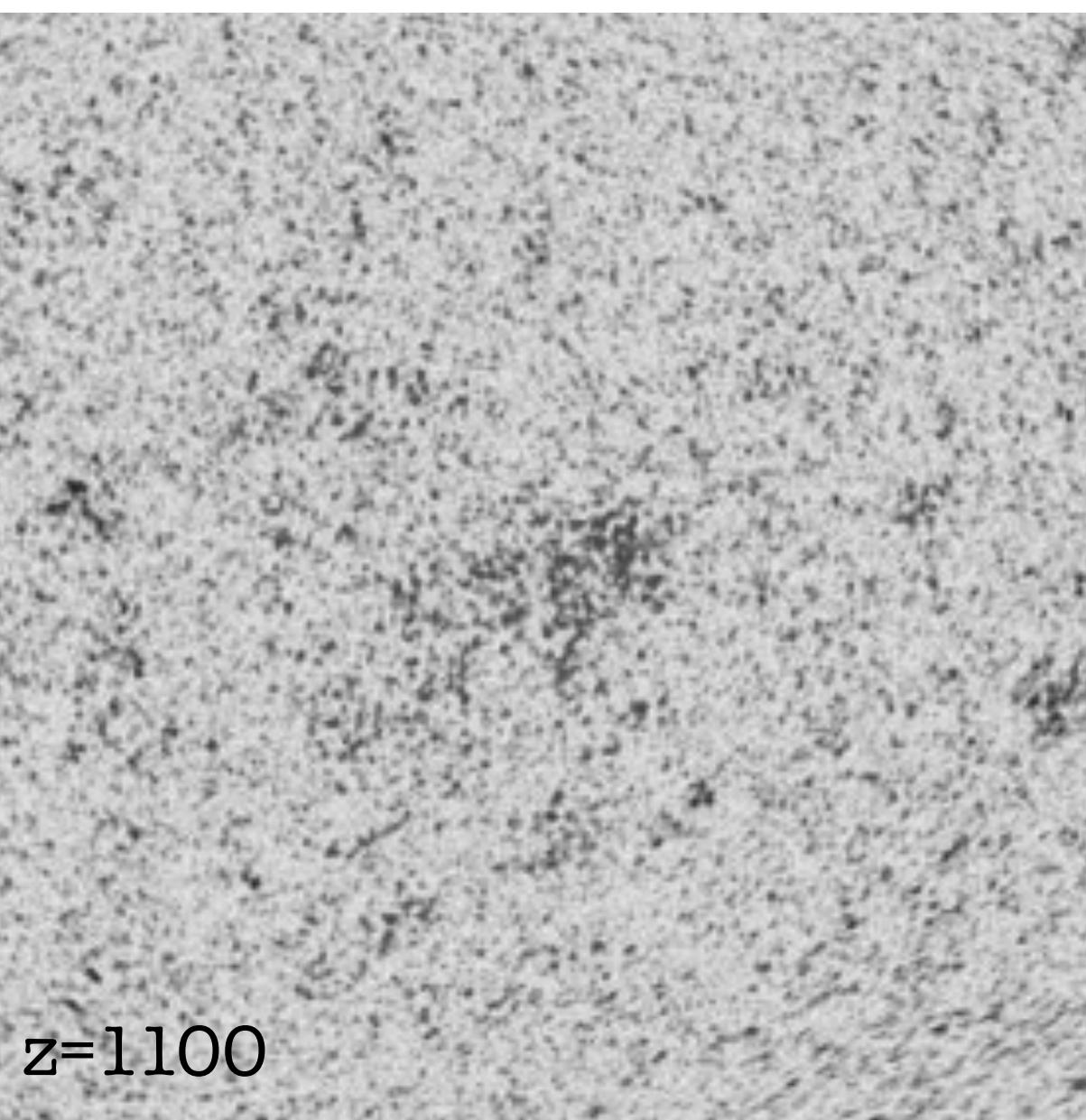
What else can we do with this information?

- We can try to test different models of the early universe (e.g. primordial non-Gaussianity, or PNG)



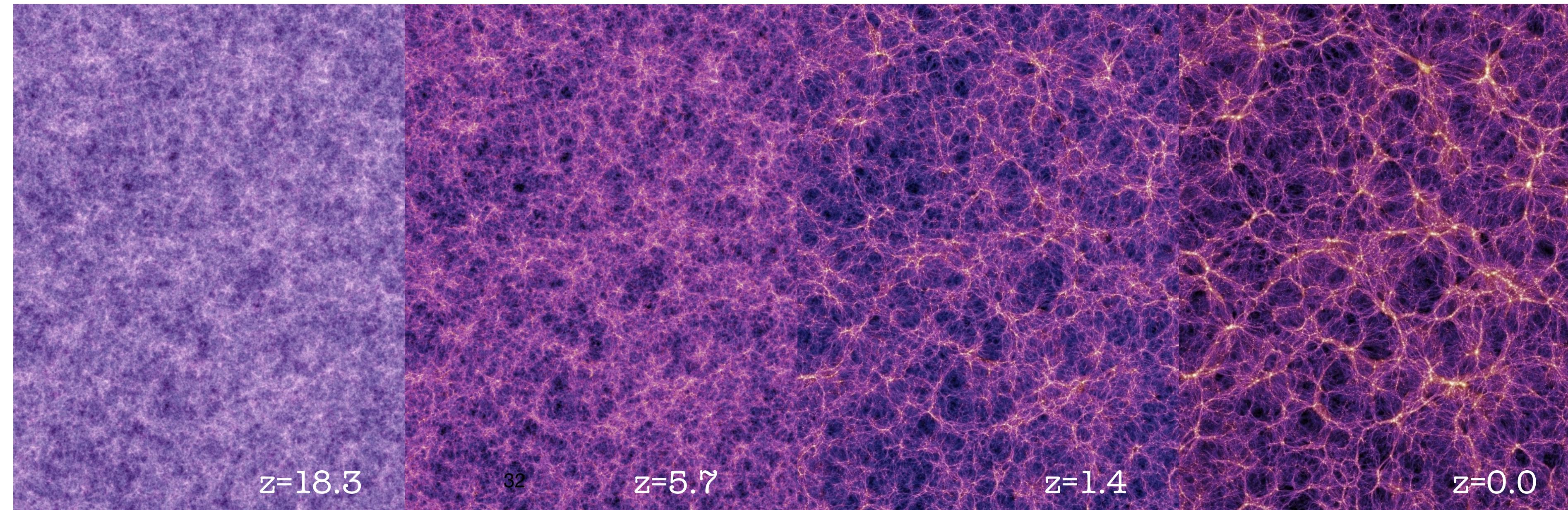
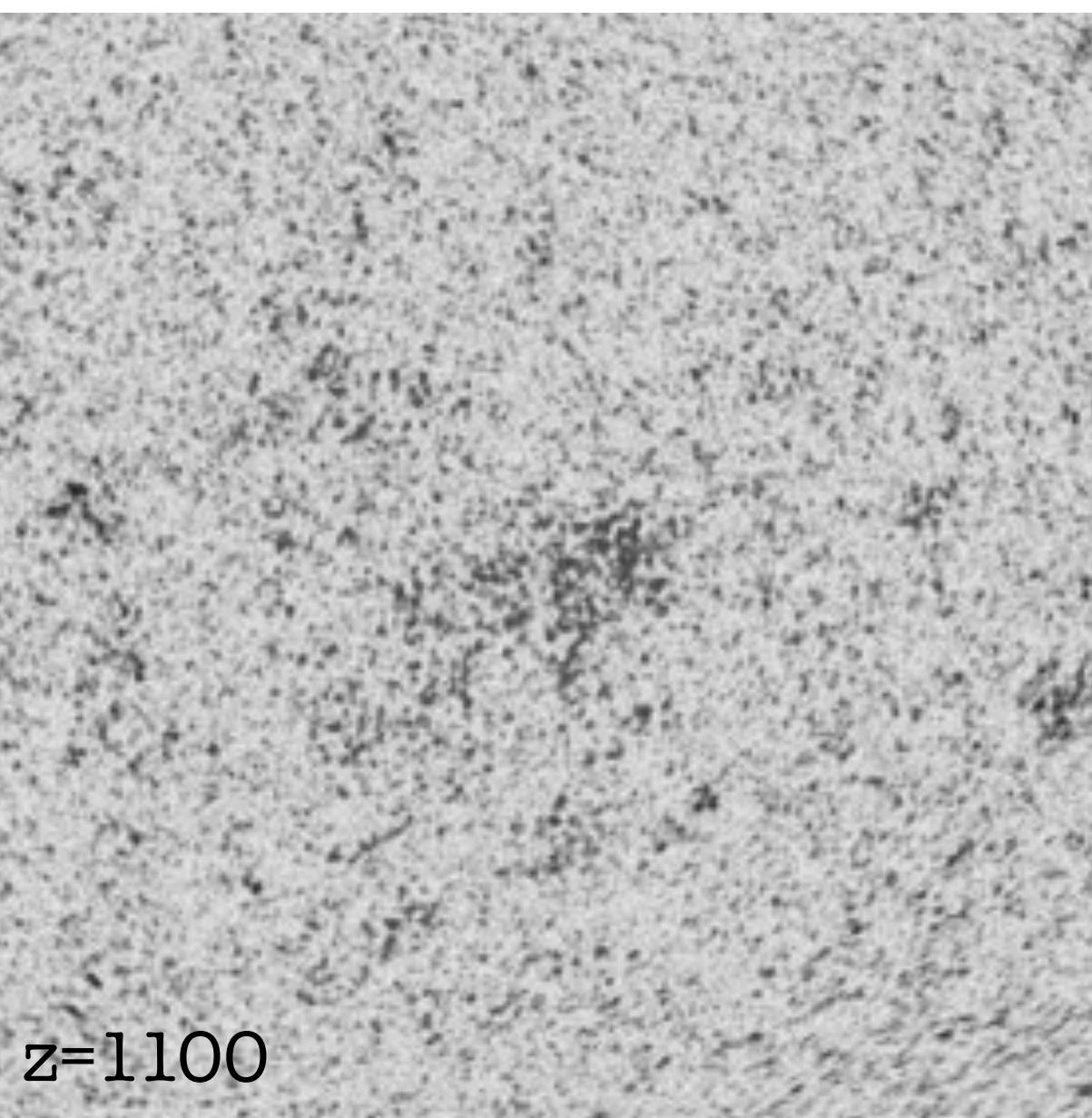
What else can we do with this information?

- However, gravity is highly non-Gaussian, the low-redshift observables contain both primordial and late-time non-Gaussianity (cf. CMB)



What else can we do with this information?

- But, perhaps not all hope is lost, we do know fairly well how to forward-model gravity. Can we disentangle the primordial and late-time non-Gaussianity via simulations?



What else can we do with this information?

- But, perhaps not all hope is lost, we do know fairly well how to forward-model gravity. Can we disentangle the primordial and late-time non-Gaussianity via simulations?

Inject bispectrum templates ($f_{\text{NL}}^{\text{eq}}$, $f_{\text{NL}}^{\text{or,lss}}$, $f_{\text{NL}}^{\text{loc}}$, $f_{\text{NL}}^{\text{or,cmb}}$)



$z=1100$

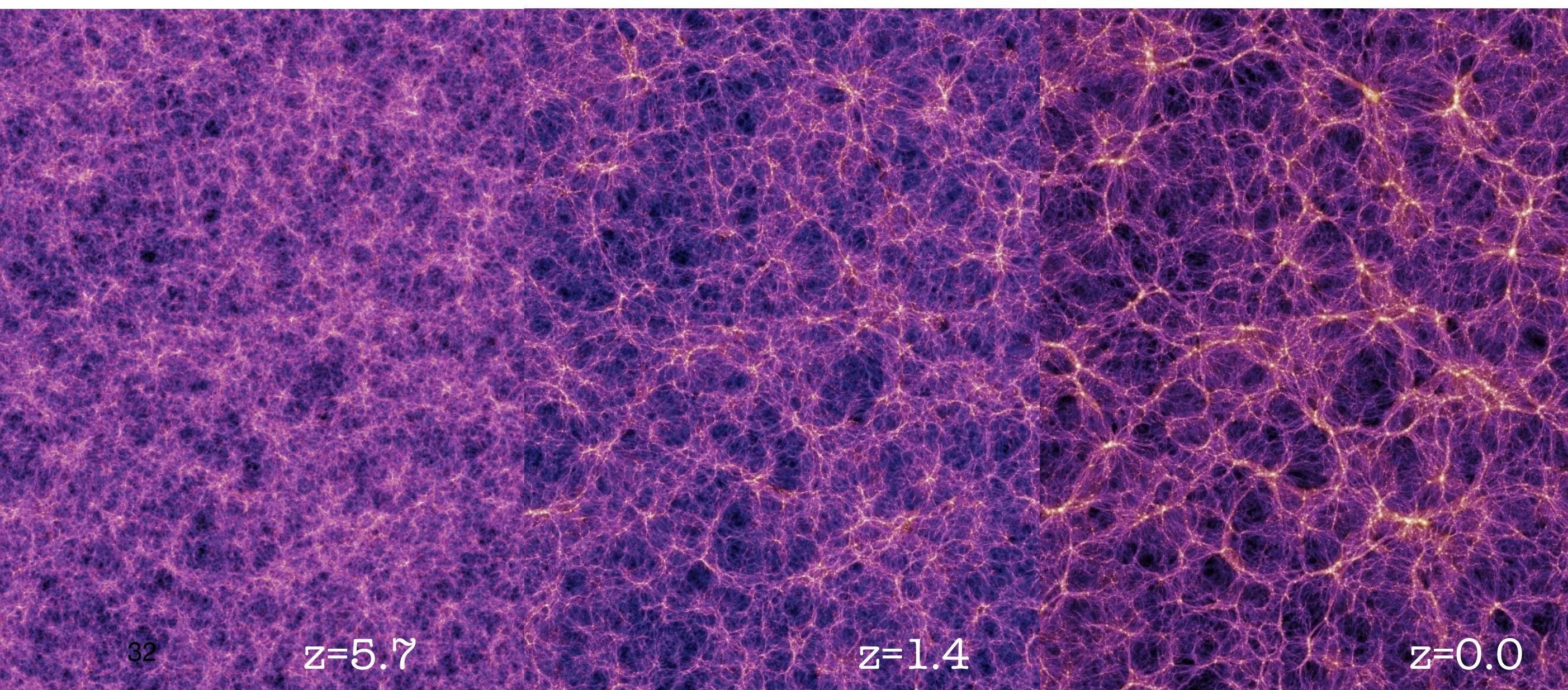
$z=18.3$

32

$z=5.7$

$z=1.4$

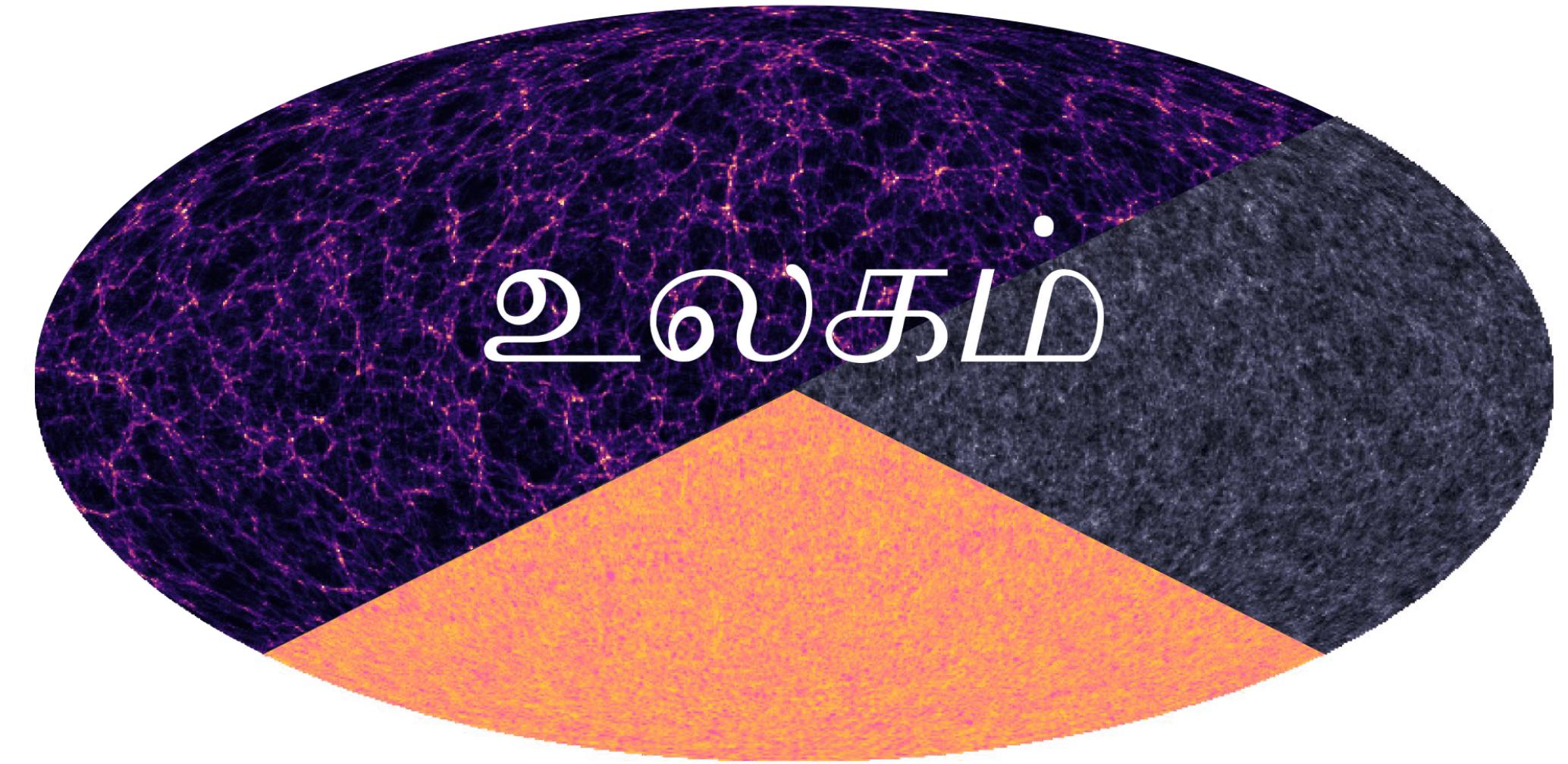
$z=0.0$



“The World”

The Ulagam Simulations

- N-body simulation suite designed for full-sky analyses of wide-field surveys for fNL
- Initial conditions from **Quijote** (Villaescusa-Navarro et al. 2020) and **Quijote-PNG** (Coulton et al. 2022)



<https://ulagam-simulations.readthedocs.io/>

$$N = 512^3$$

$$L = 1 \text{ Gpc}/h$$

$$\{\Omega_m, \sigma_8, n_s, w, f_{\text{NL}}^X\}$$

Accurate to $k < 1 [\text{h/Mpc}]$, $\ell < 1000$

Gravitational potential

$$\Phi(\mathbf{k}) = \phi(\mathbf{k}) + \int f_{\text{NL}}[\delta_D] K(\mathbf{k}_1, \mathbf{k}_2) \phi(\mathbf{k}_1) \phi(\mathbf{k}_2) d^3 k_1 d^3 k_2$$

↑
Gaussian

$$B_\Phi = 2f_{\text{NL}} K(\mathbf{k}_1, \mathbf{k}_2) P_{\Phi,1} P_{\Phi,2} + \text{cyc.}$$

$f_{\text{NL}}^{\text{loc}}$ Presence of second scalar field

$f_{\text{NL}}^{\text{eq}}$ Presence of “non-canonical” kinetic terms

$f_{\text{NL}}^{\text{or,cmb}}$ Approx. orthogonal to local and equilateral

$f_{\text{NL}}^{\text{or,lss}}$ Similar to above, but better approximation at squeezed

Analysis setup

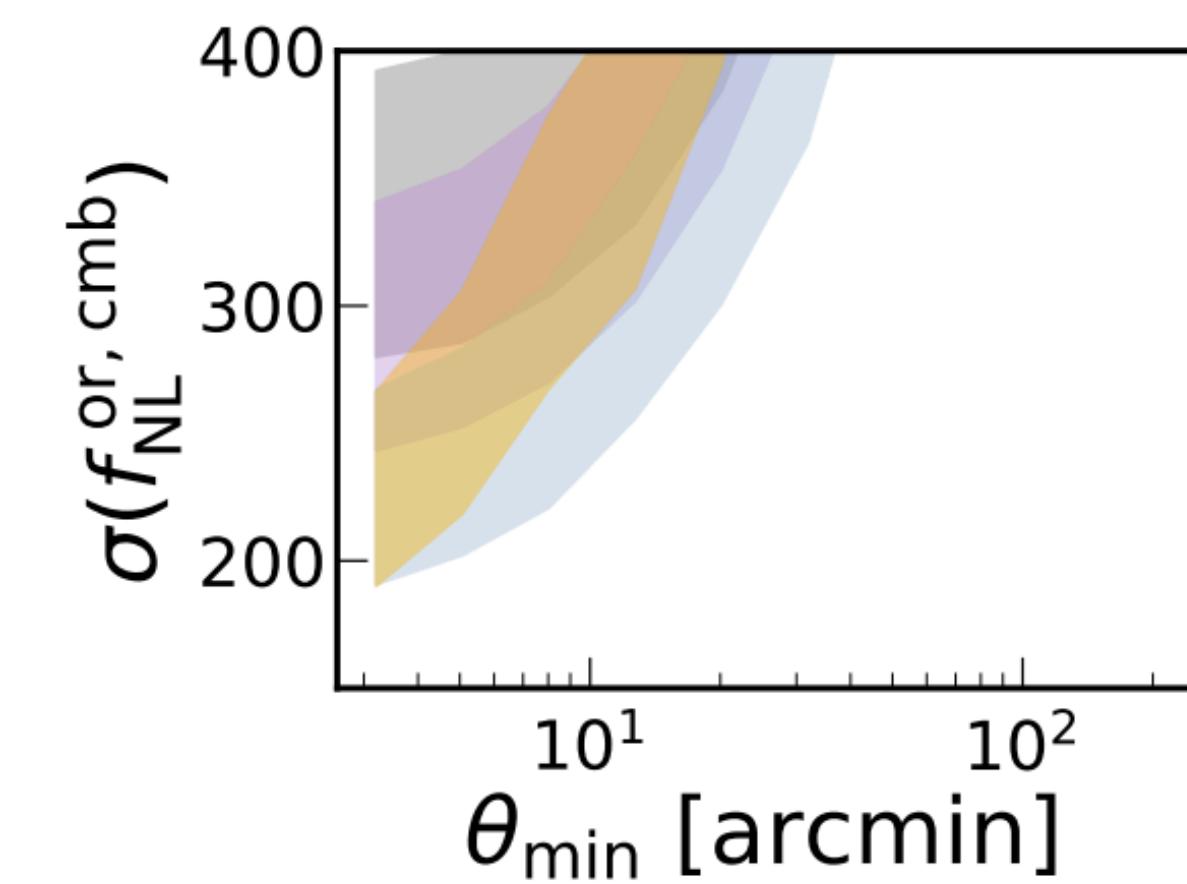
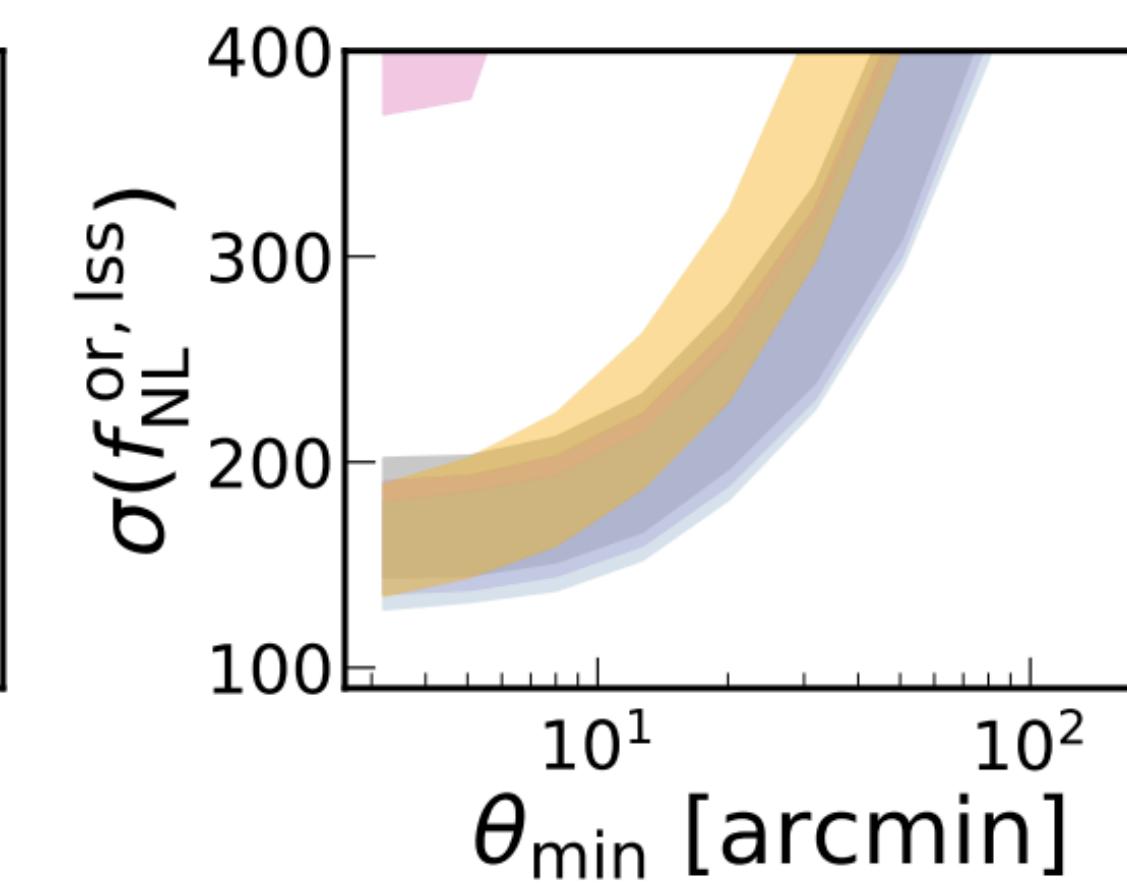
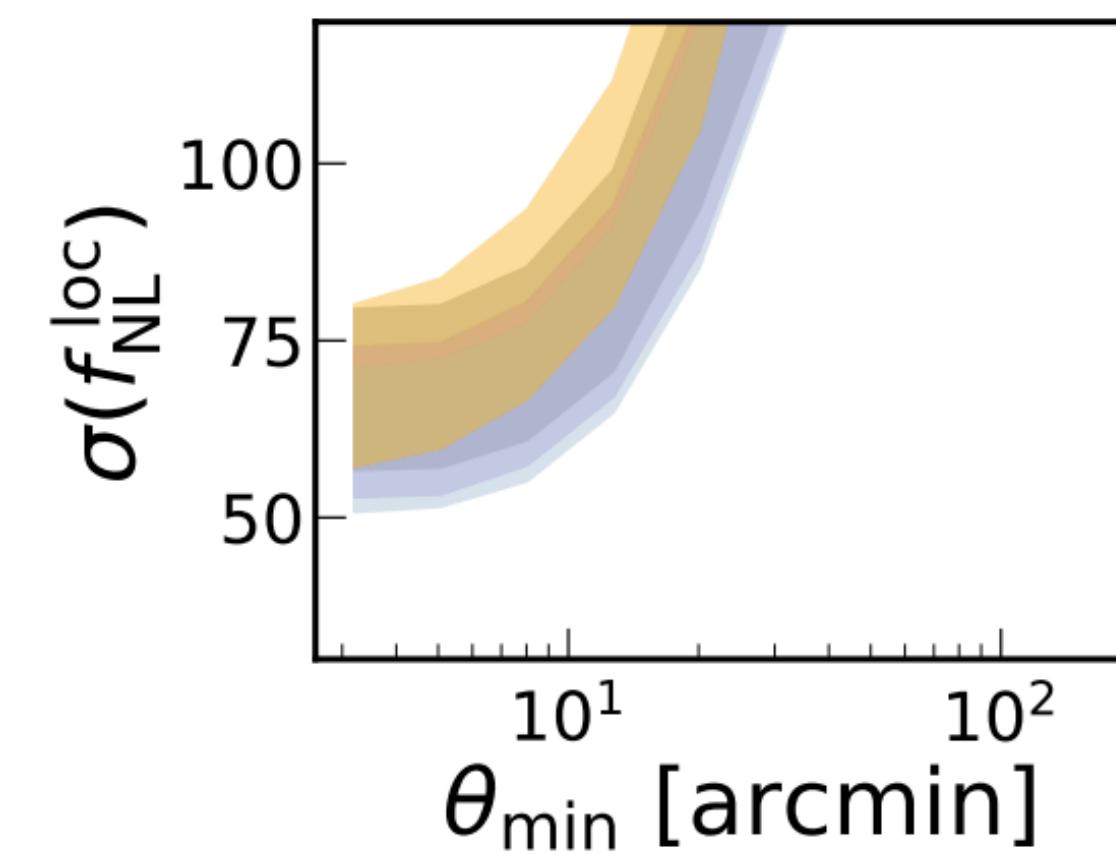
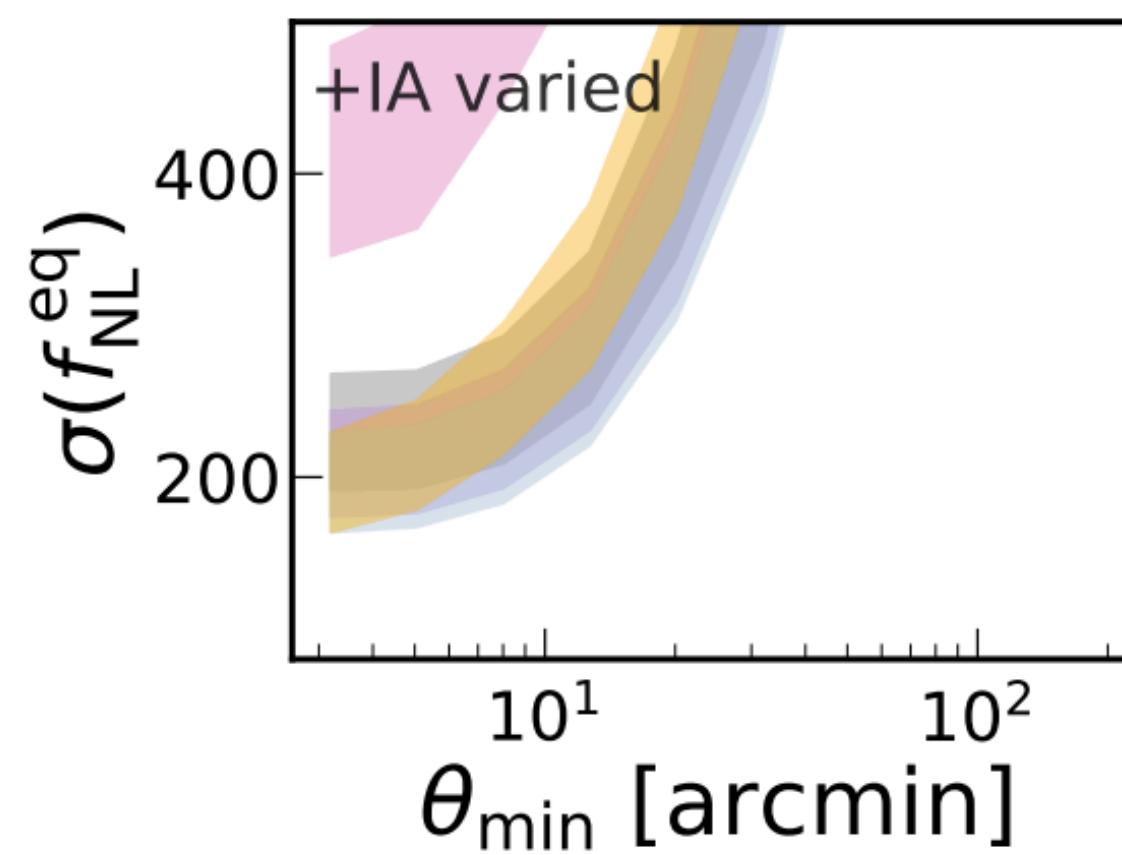
- Weak lensing convergence maps
- Moments ($N=2-5$), CDFs
- Fisher forecast on constraints on fNL
- Simulation covariance at fiducial cosmology
- Compare DES Y3, DES Y6, LSST Y1, LSST Y10

Run	$\mathbf{P}_{\text{fid}} \pm \Delta P$	N_{sim}
Fiducial	—	2000
Local PNG, $f_{\text{NL}}^{\text{loc}}$	0 \pm 100	100
Equilateral PNG, $f_{\text{NL}}^{\text{eq}}$	0 \pm 100	100
LSS Orthogonal PNG, $f_{\text{NL}}^{\text{or, lss}}$	0 \pm 100	100
CMB Orthogonal PNG, $f_{\text{NL}}^{\text{or, cmb}}$	0 \pm 100	100
Matter density, Ω_m	0.3175 \pm 0.01	100
Density fluctuations amplitude. σ_8	0.834 \pm 0.015	100
Dark energy EoS w_0	-1 \pm 0.05	100
Spectral index n_s	0.9624 \pm 0.02	100

In which order is the information stored?

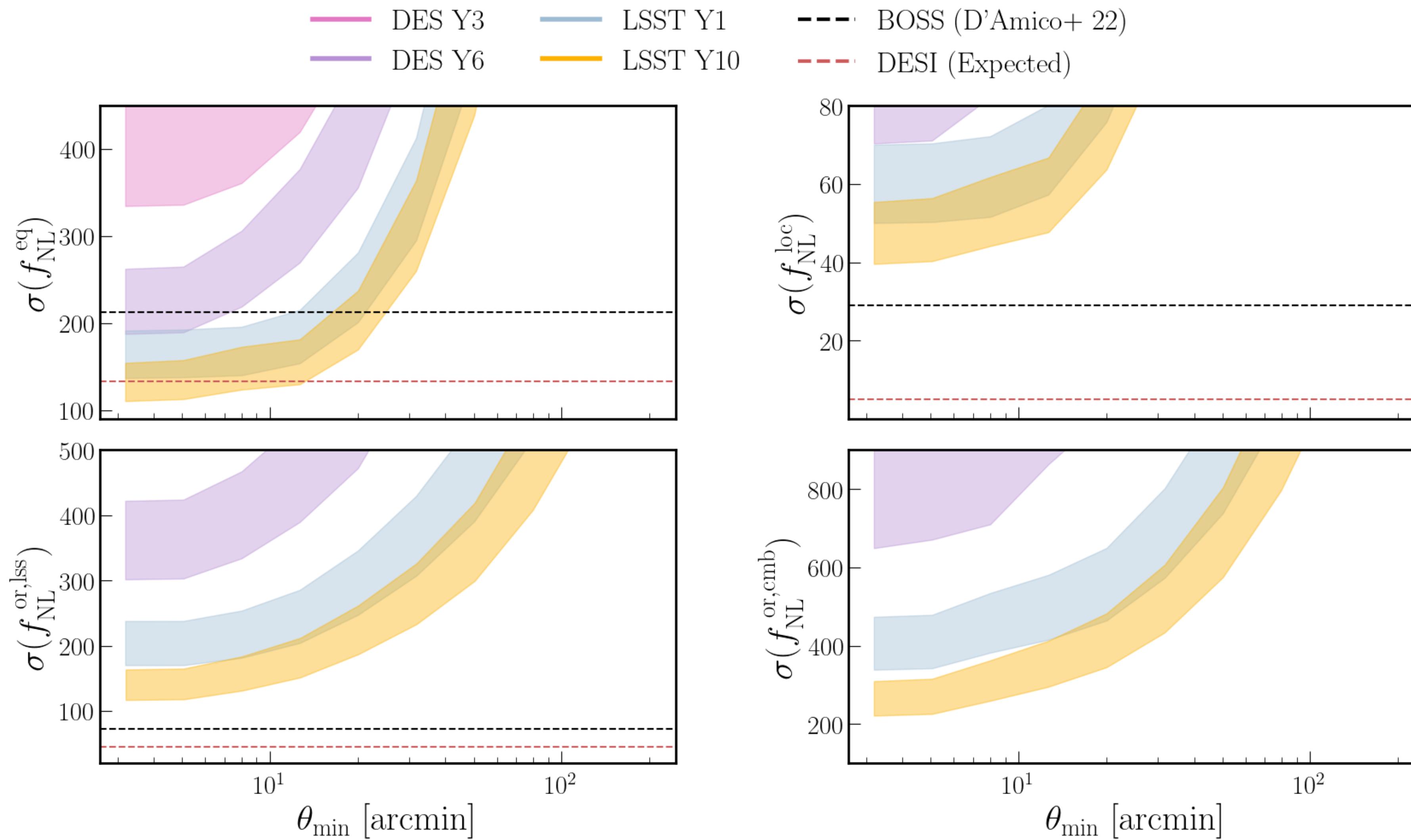
LSST Y10-like

Moments ($N = 2$) Moments ($N \leq 4$) CDFs
Moments ($N \leq 3$) Moments ($N \leq 5$)

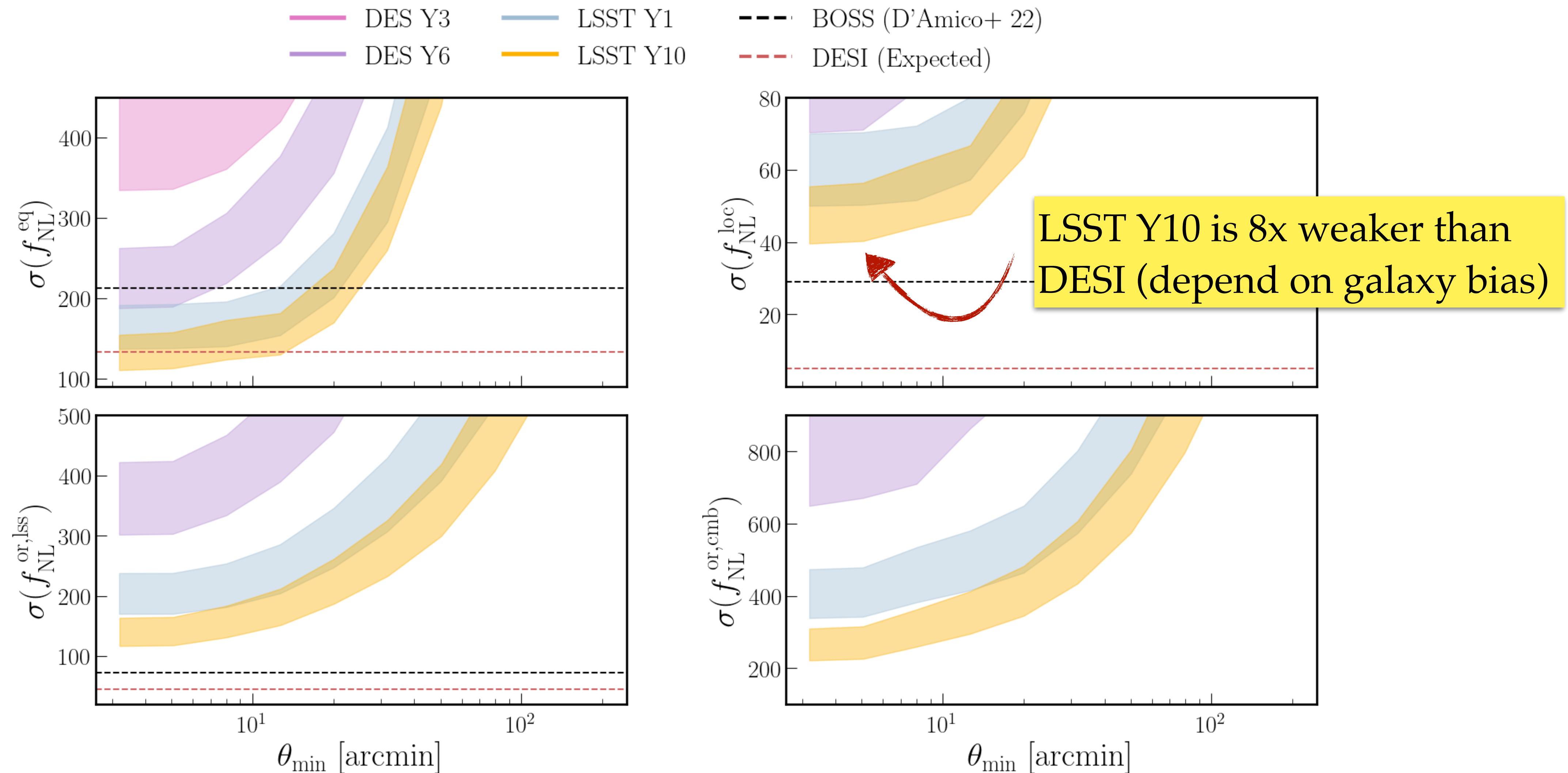


A reasonable scale to look at is $\sim 10'$ (5-15 Mpc)

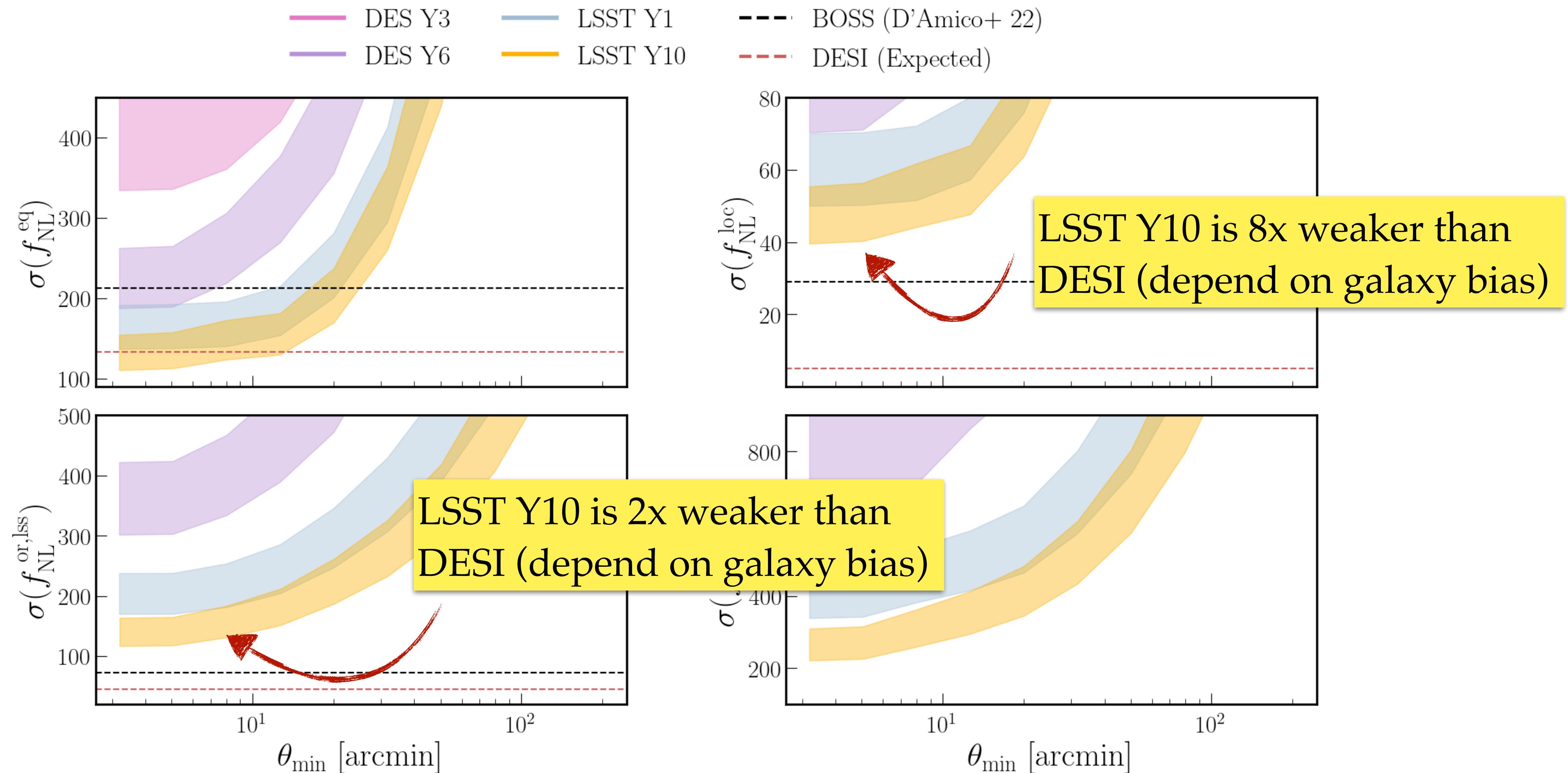
Comparison between datasets



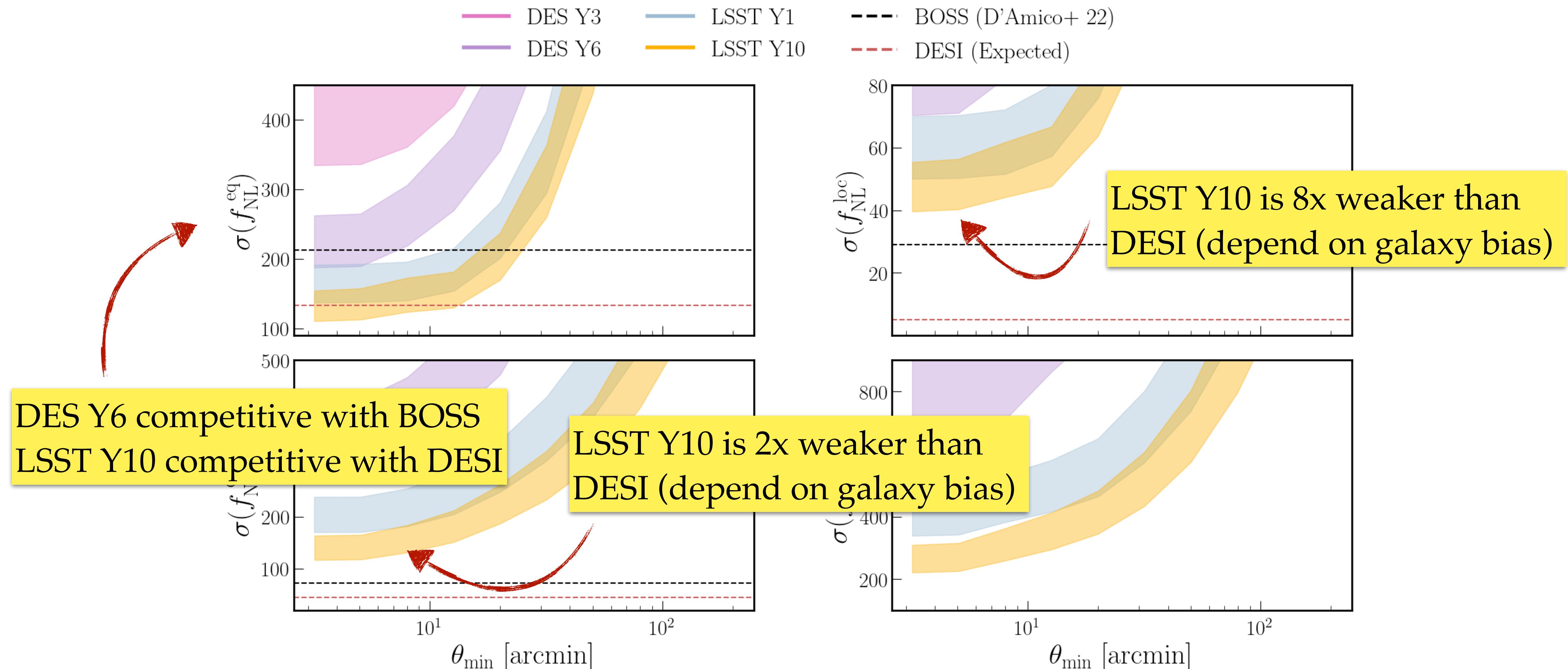
Comparison between datasets



Comparison between datasets



Comparison between datasets



Lensing HOS for early-universe physics

- We expect lensing HOS could contribute meaningfully to the constraints on fNL
- Advantages of doing this:
 - Independent cross-check with scale-dependent galaxy bias measurements
 - Offer potential detection of scale-dependent PNG
 - Lensing simulations are faster than galaxies
 - Combined with galaxies could potentially calibrate galaxy bias
- Be imaginative in new things we can already test!

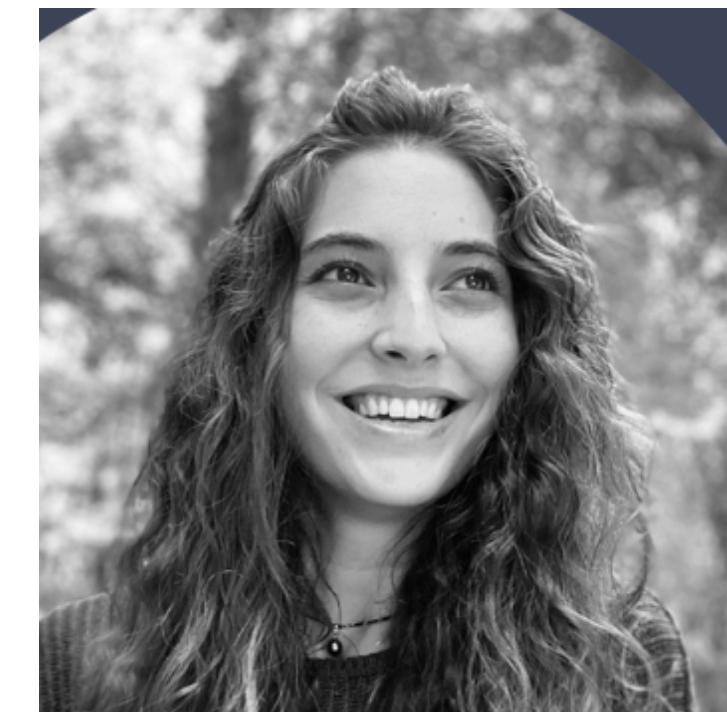
Outline

- The Λ CDM paradigm and extracting information beyond 2pt
- Practical challenges: beyond 2pt systematics
- Opportunities: primordial non-Gaussianity
- **Towards field-level inference**
- Summary & outlook

Omori, Zeghal, Lanusse, CC et al. (in prep)



Yuuki Omori



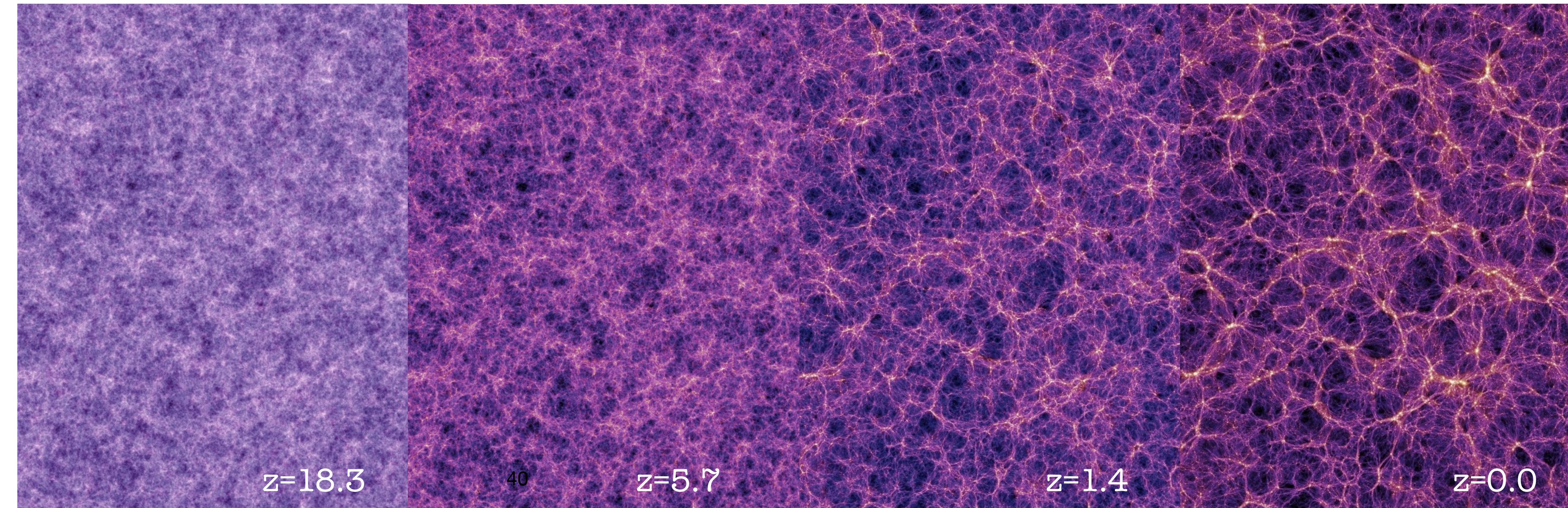
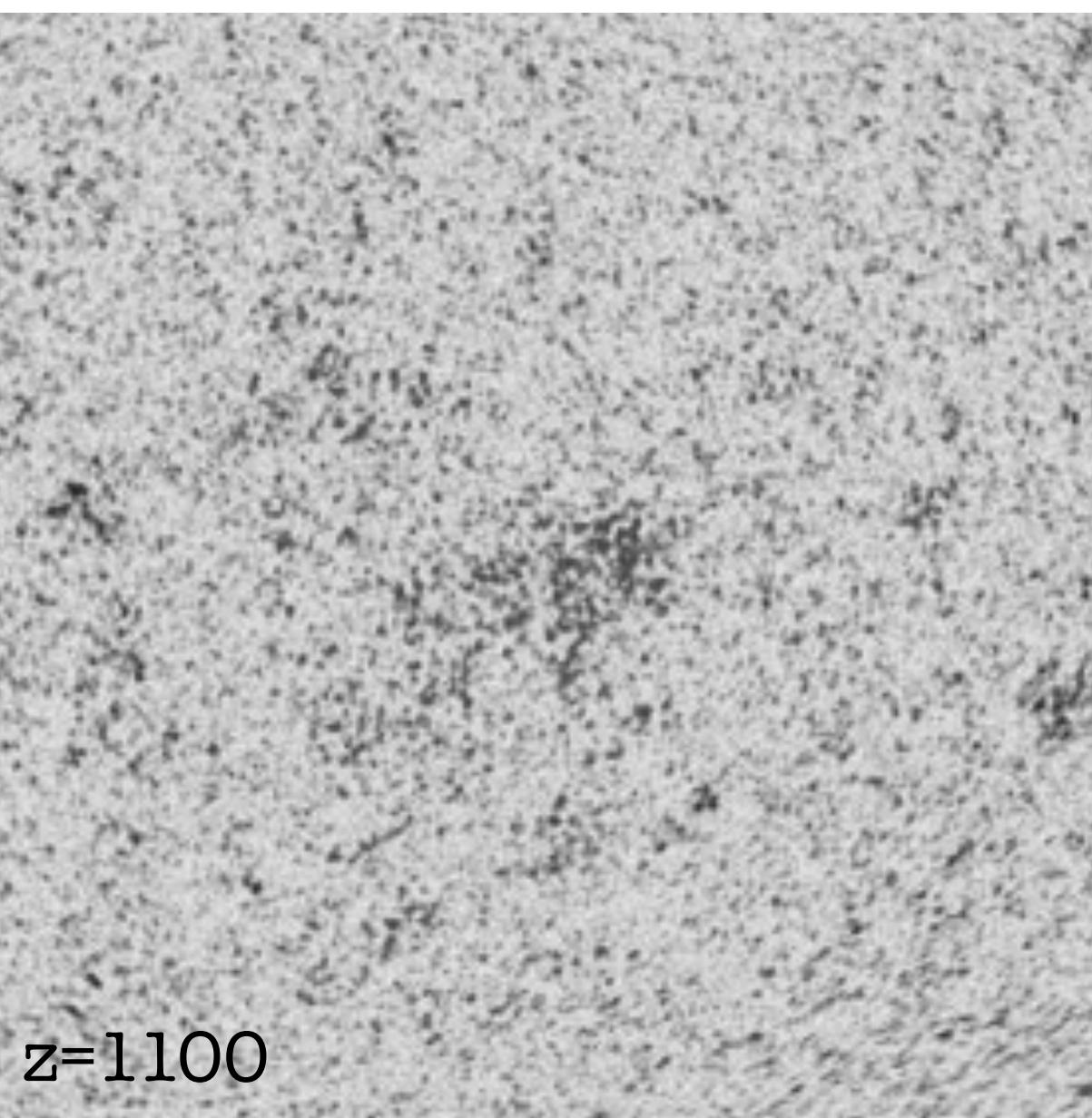
Justine Zeghal



François Lanusse

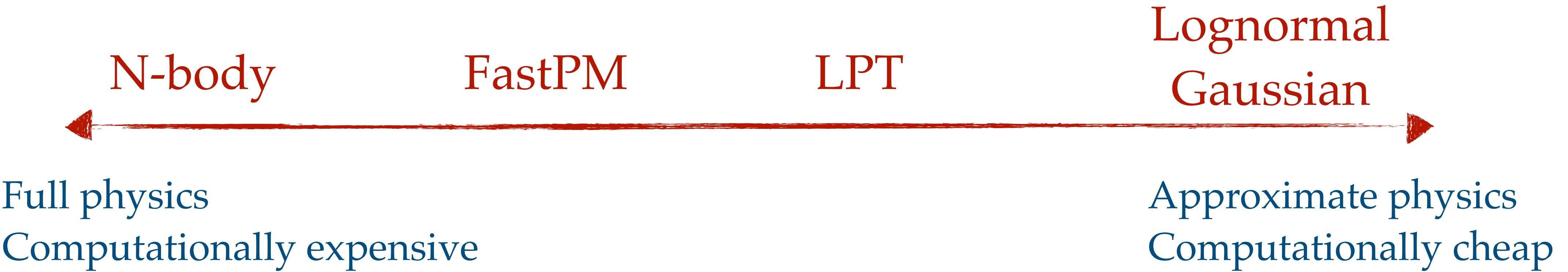
Full-field inference

- The ultimate level of modeling the LSS is when we have a field-level model of what we see — maps of initial conditions + cosmological and nuisance parameters
- Individually we know how to do these steps, the most non-trivial step is evolving gravity over cosmic time



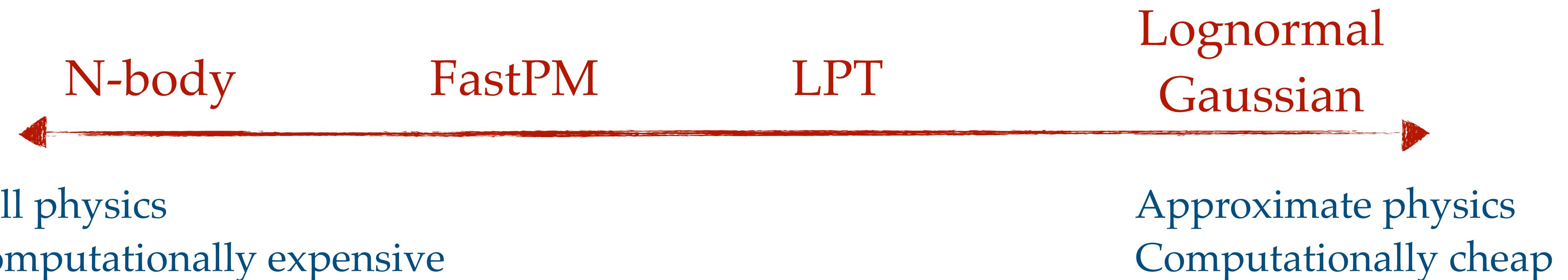
Forward-model structure formation

There is a spectrum of implementations to forward-model structure formation

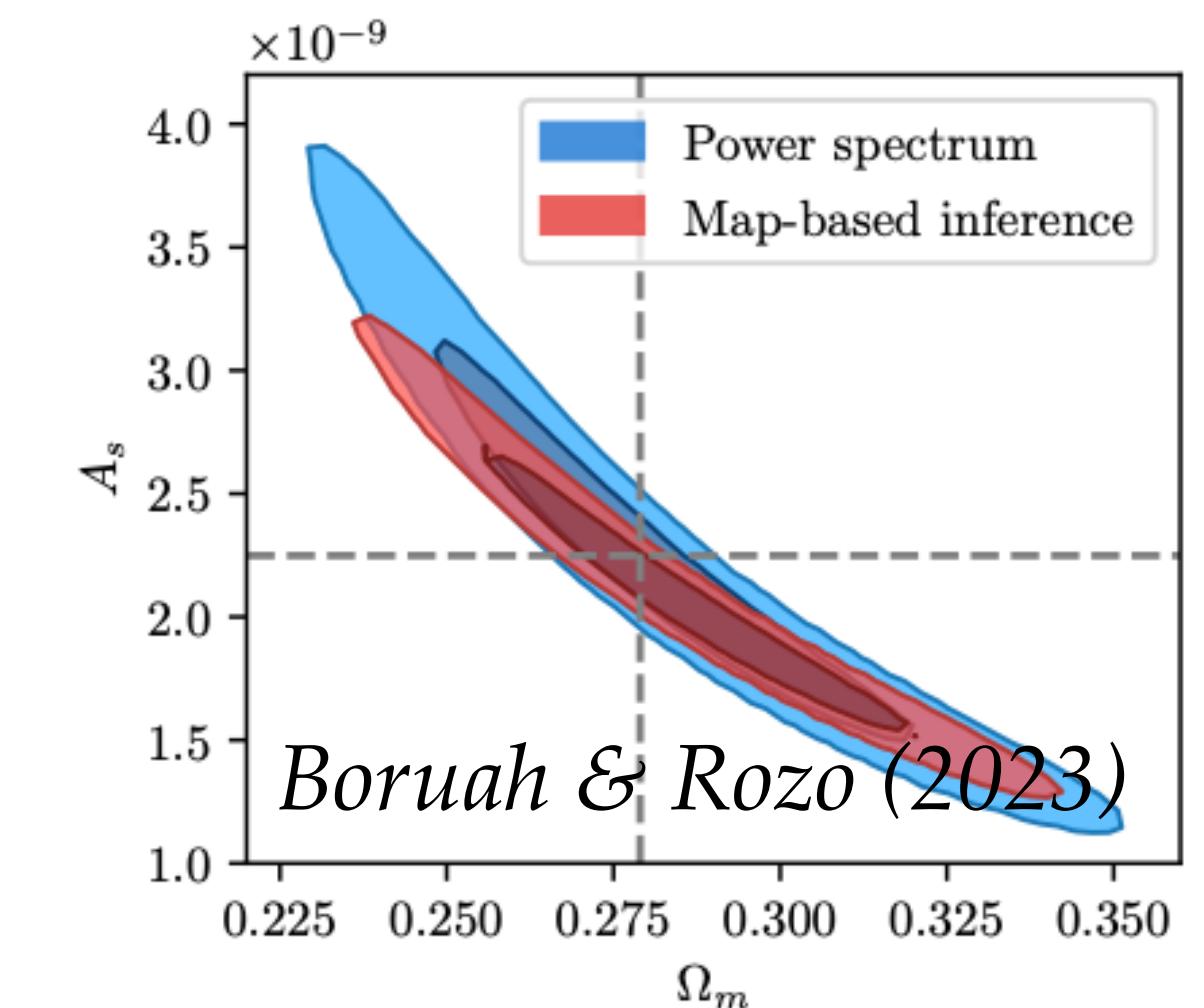
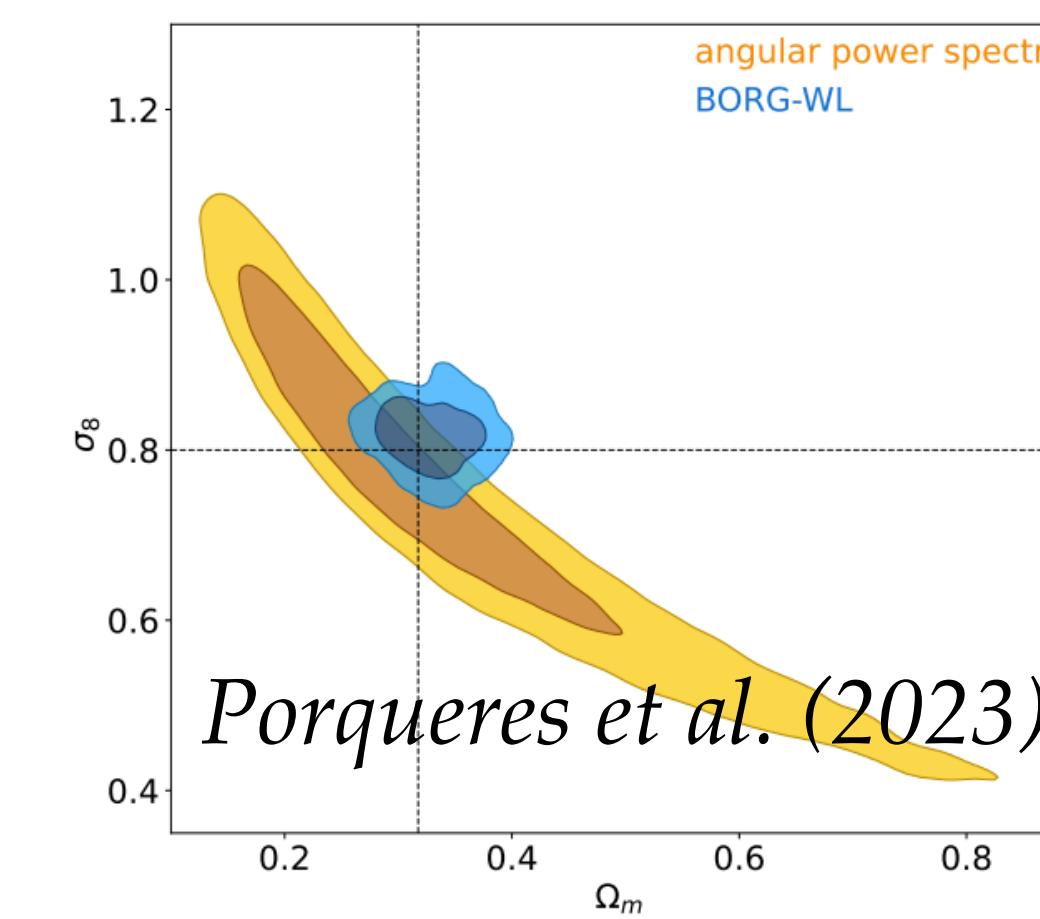


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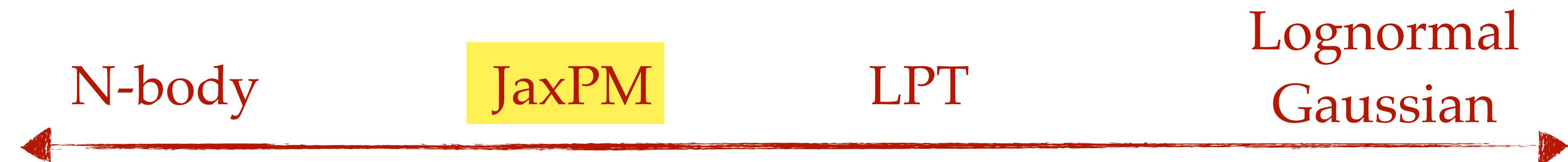


See talks from Florent, Eleni,
Supranta, Arthur, Adrian...



Forward-model structure formation

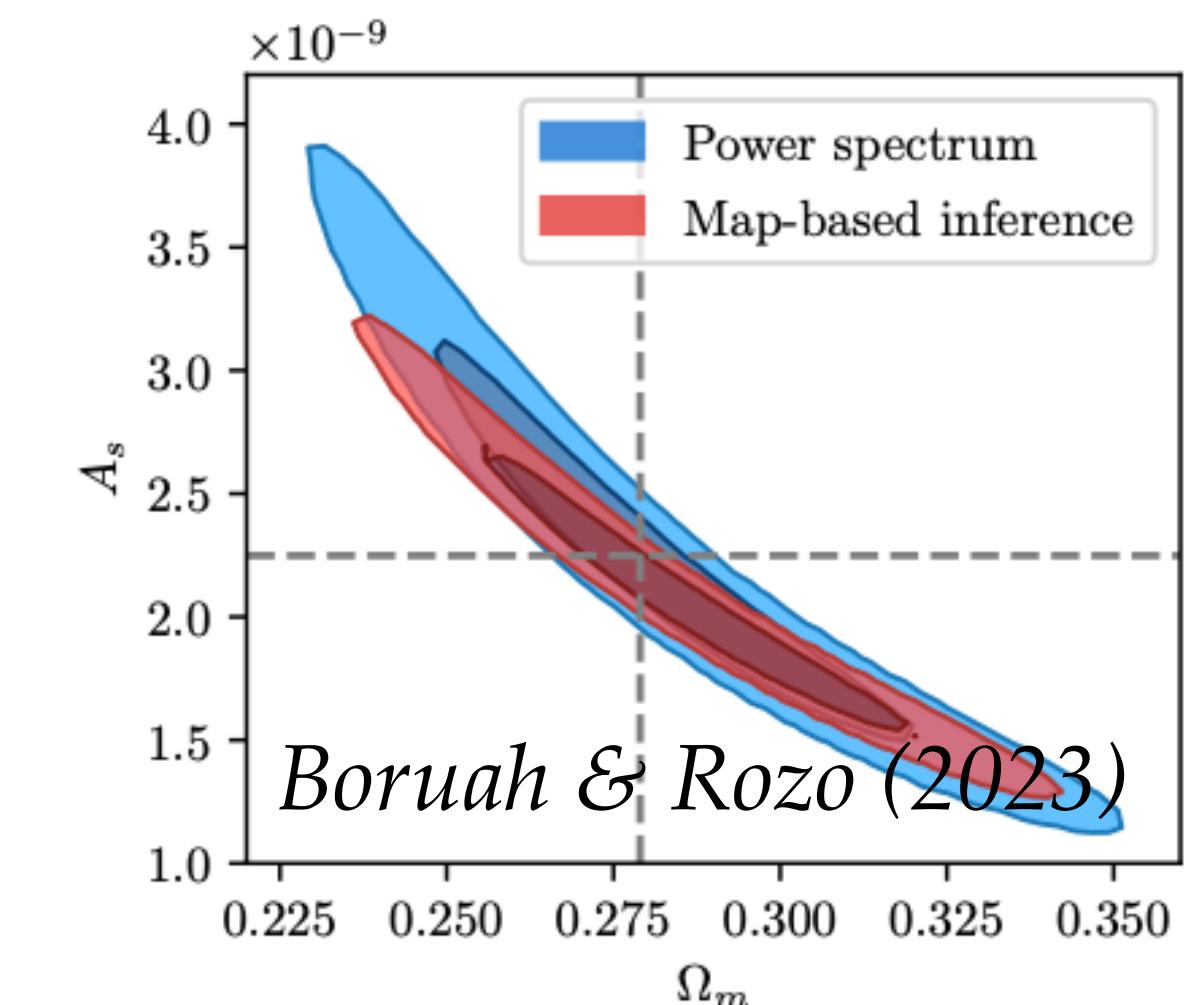
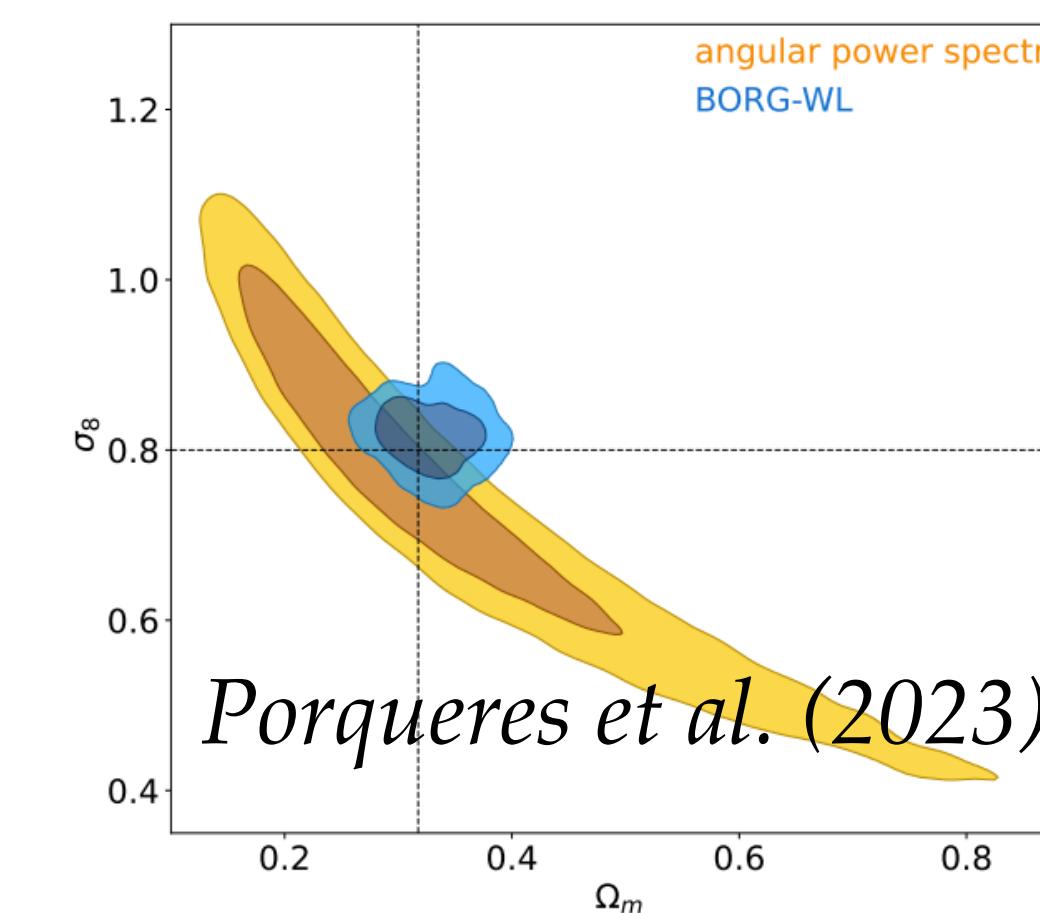
There is a spectrum of implementations to forward-model structure formation



Full physics
Computationally expensive

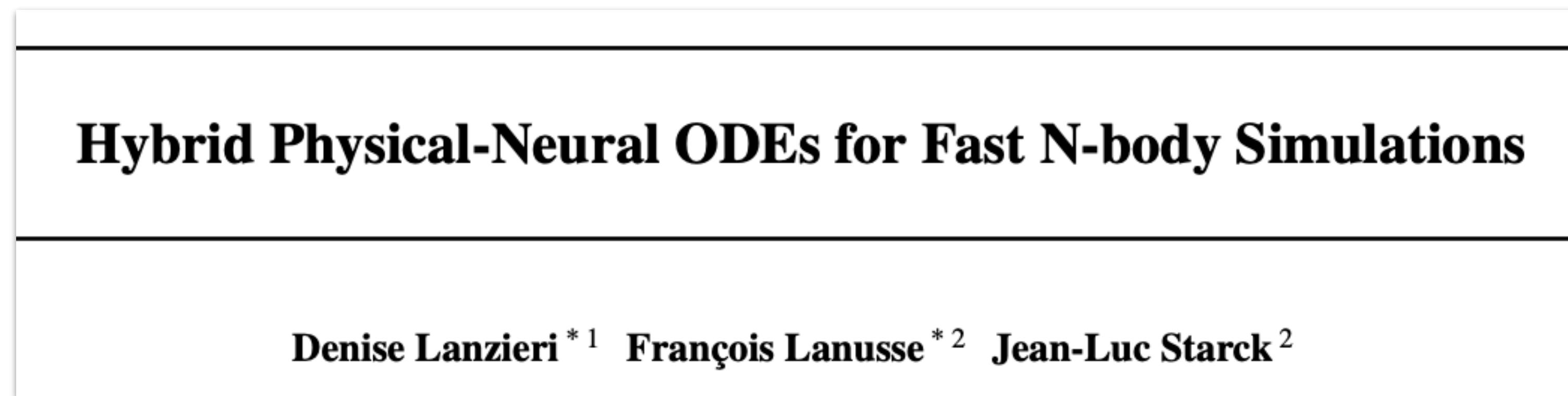
Approximate physics
Computationally cheap

See talks from Florent, Eleni,
Supranta, Arthur, Adrian...



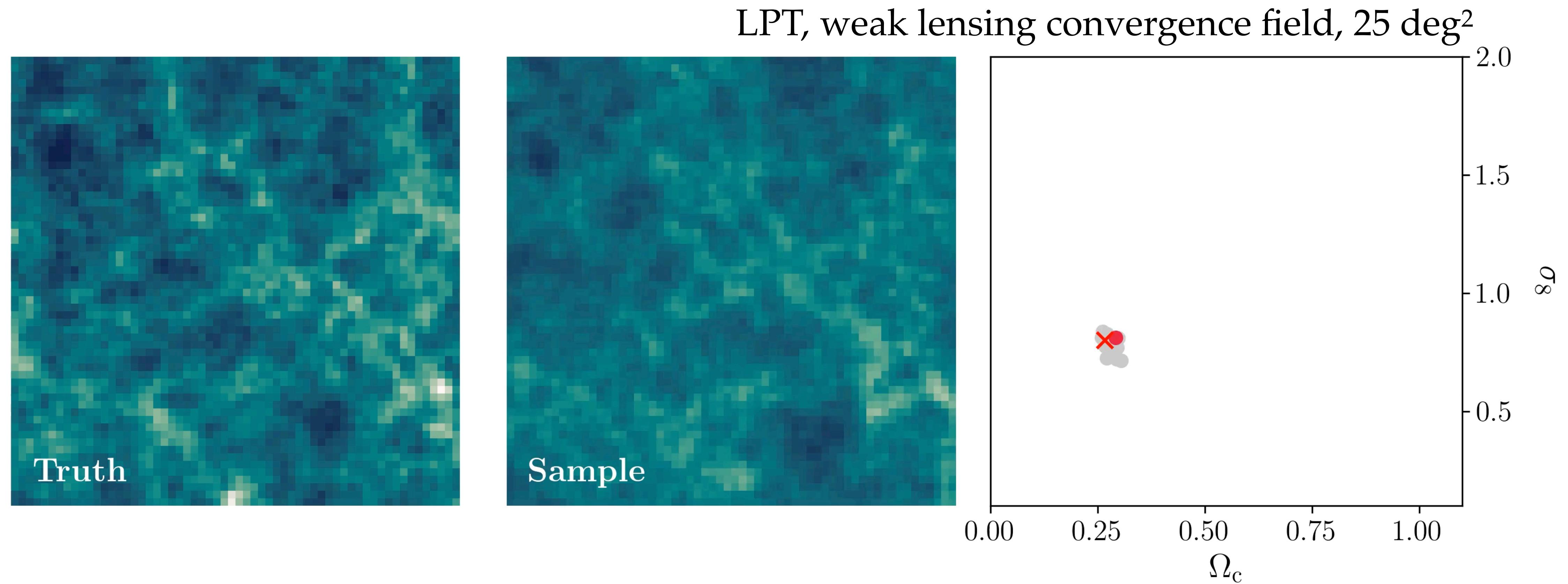
JaxPM-based field-level inference framework

- <https://github.com/DifferentiableUniverseInitiative/JaxPM>



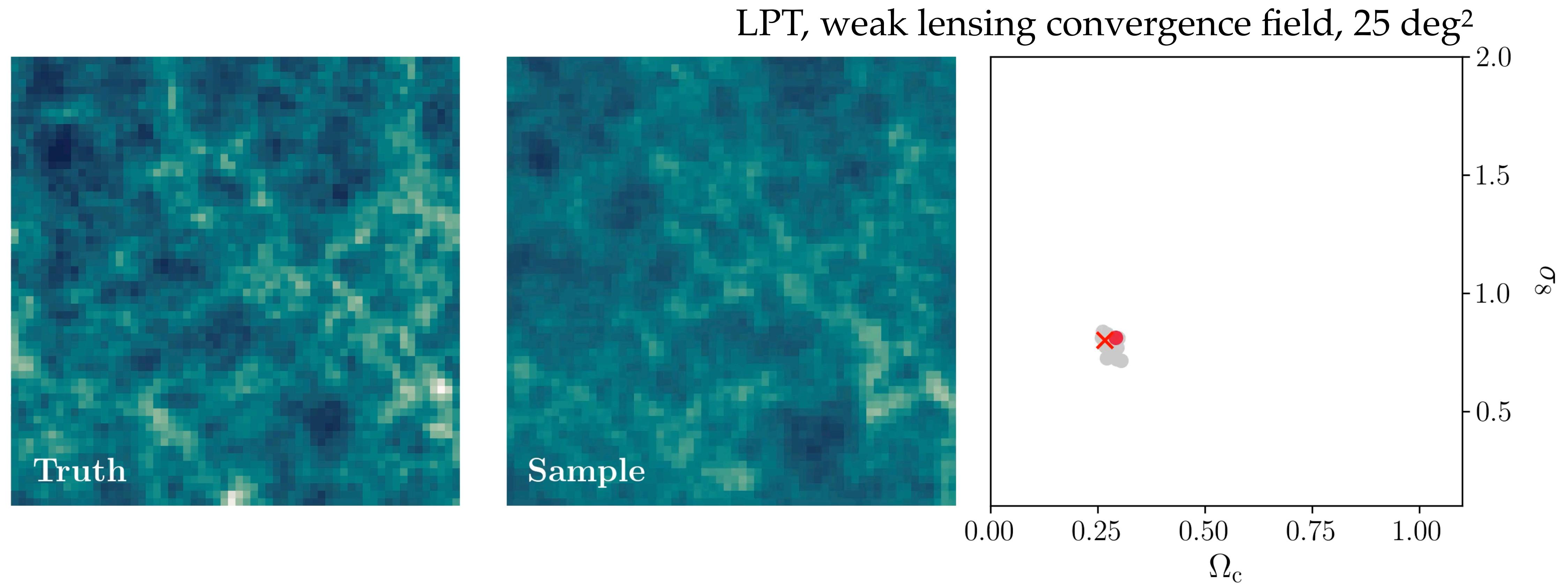
- Example: 2s (LPT), 90s (JaxPM) for single HMC step
 - LSST Y10-like, 5 redshift bins
 - 5x5 deg², 400x400x4600 Mpc/h, 200x200x128 pixels
- Require sampling ~5M parameters (!!)

The challenge of sampling



Lots of fine-tuning is still needed to recover contours that make sense (ongoing work...)
Focus on being constantly grounded by the 2pt analysis we think we know how to do, and fair comparison between different methods

The challenge of sampling



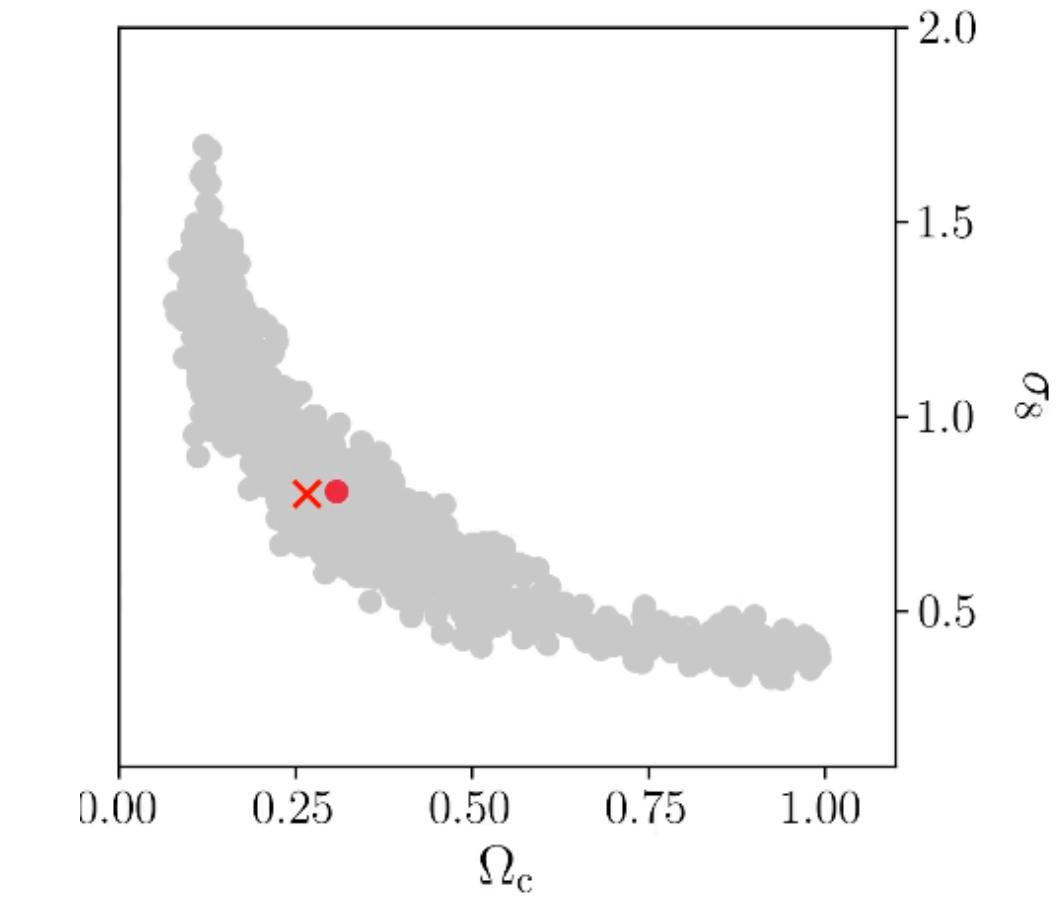
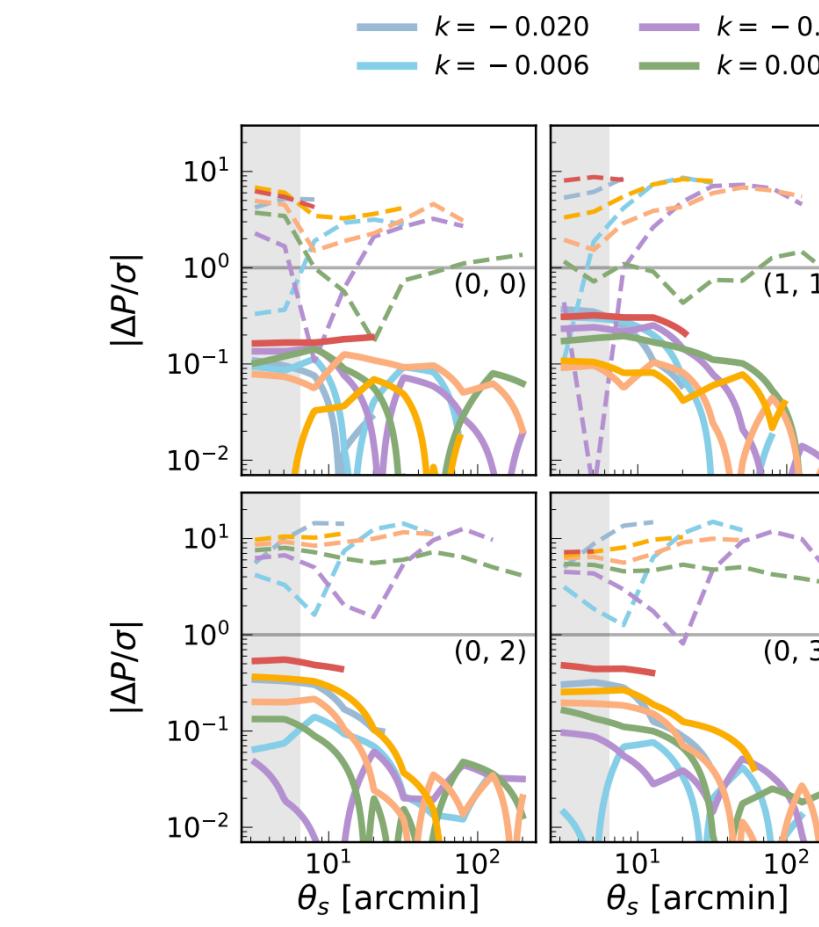
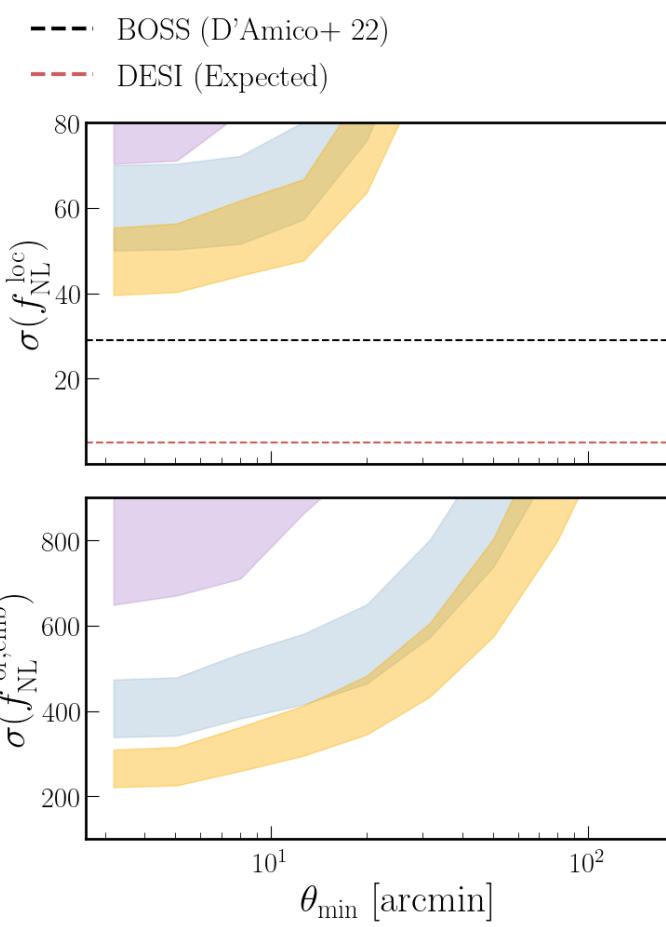
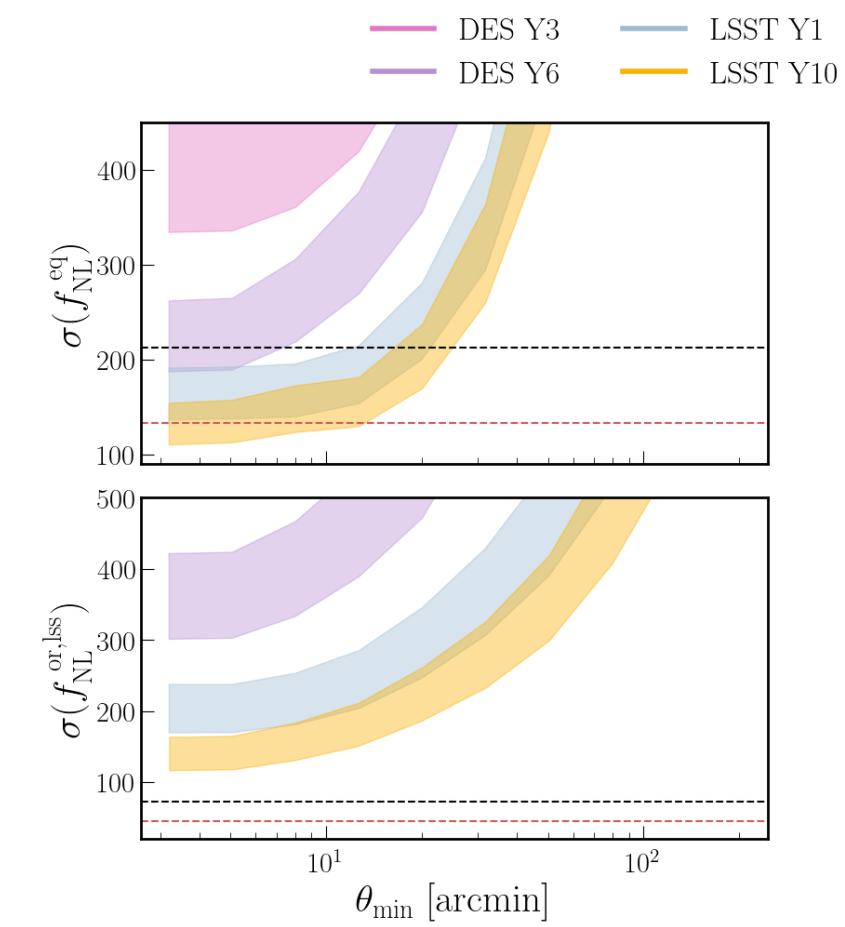
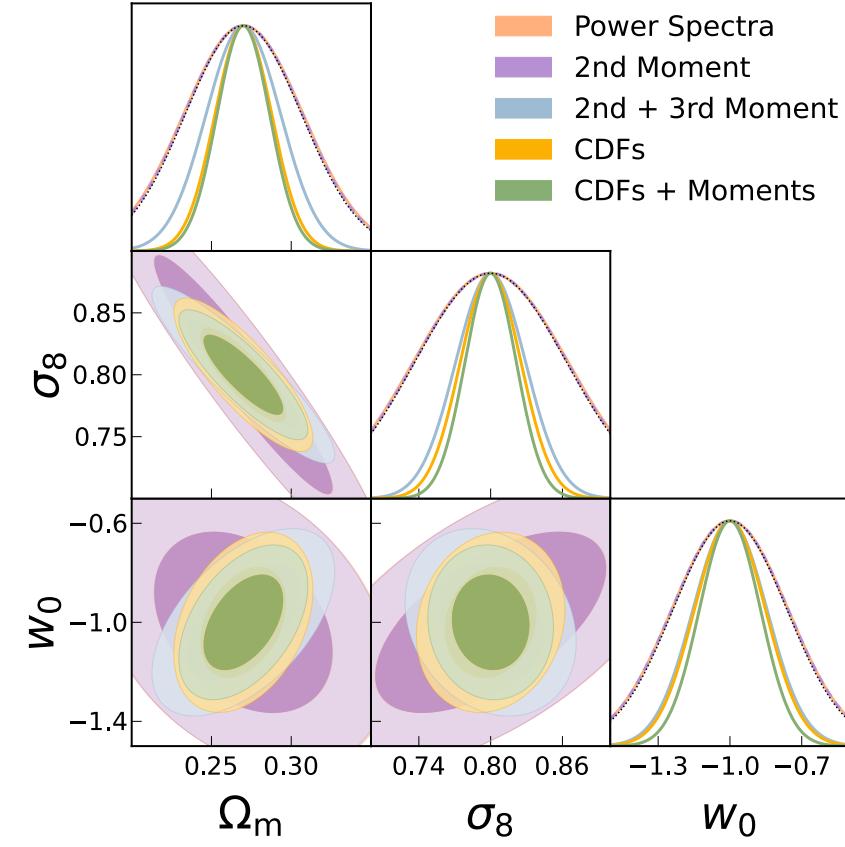
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Outline

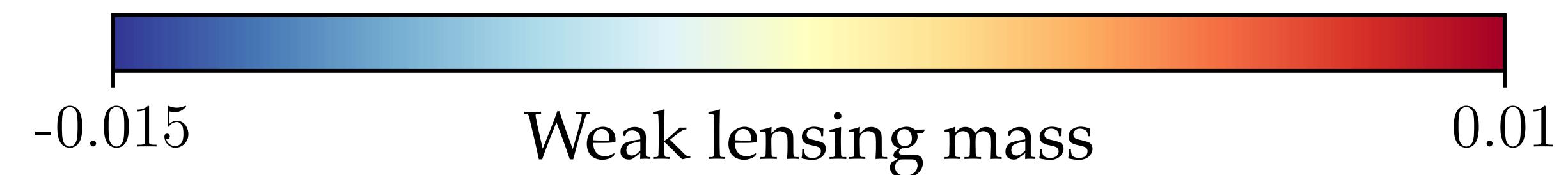
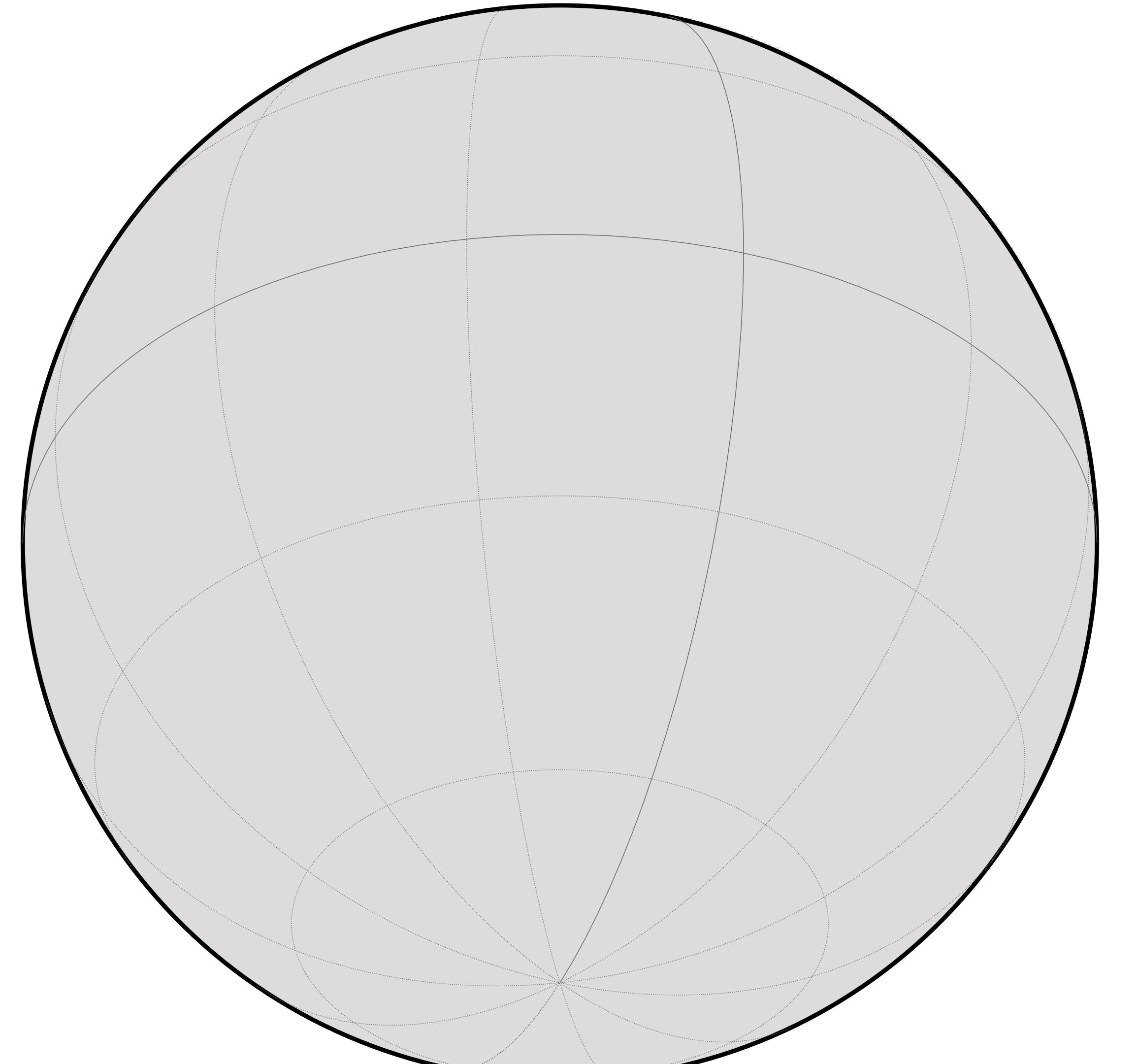
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Summary & Outlook

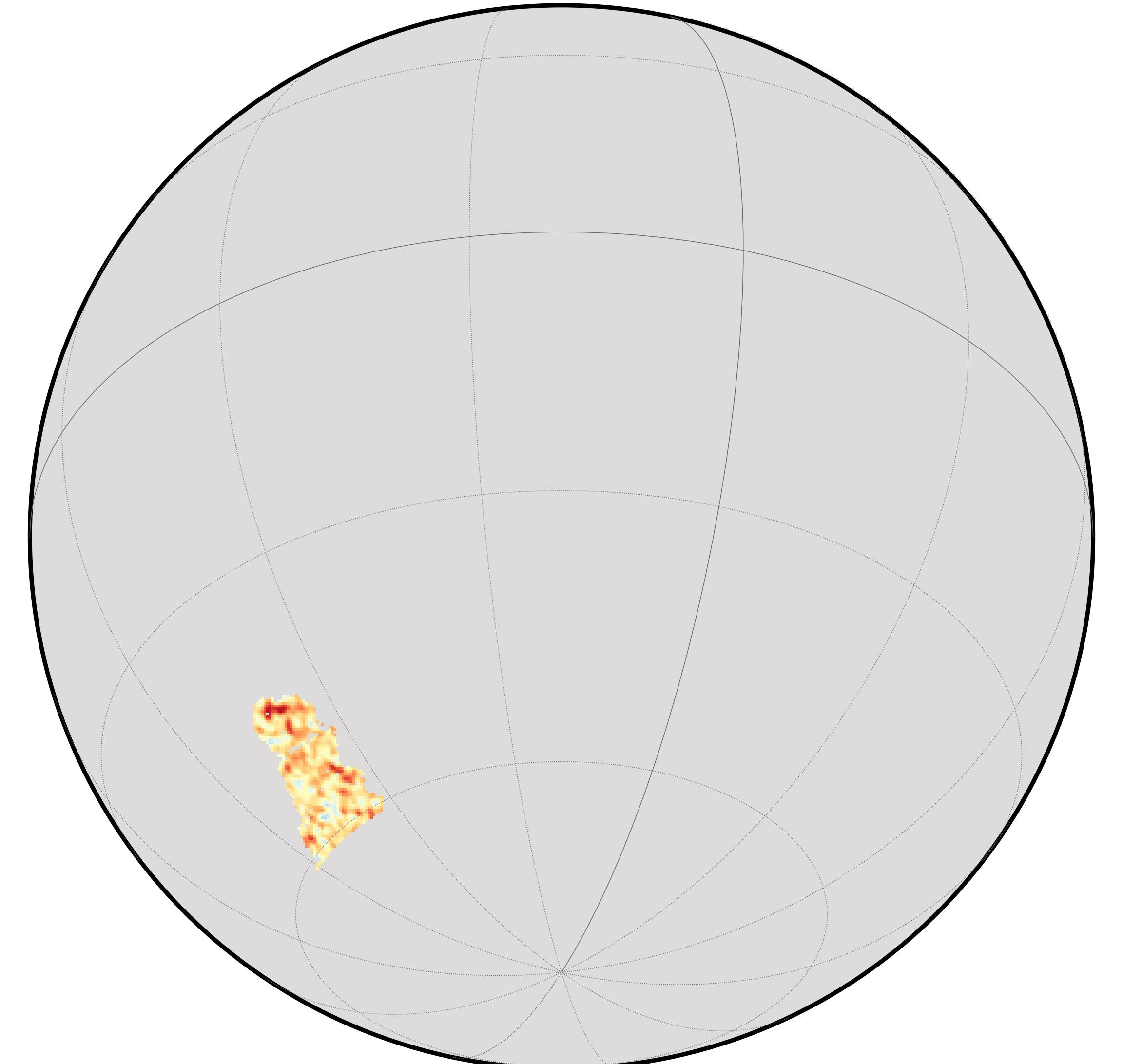
- The gain in beyond 2pt statistics depends on **the science, the dataset, and how we extract the signal** — it may not always make sense to go to the highest order
- There are practical challenges that we are working on to make HOS **more robust**
- There is great opportunities for learning about the **new physics** via lensing HOS
- **Field-level inference** is the final frontier — lots of work needed to do full-physics



The community has
made a lot of
progress making
these maps!



SV (2015)

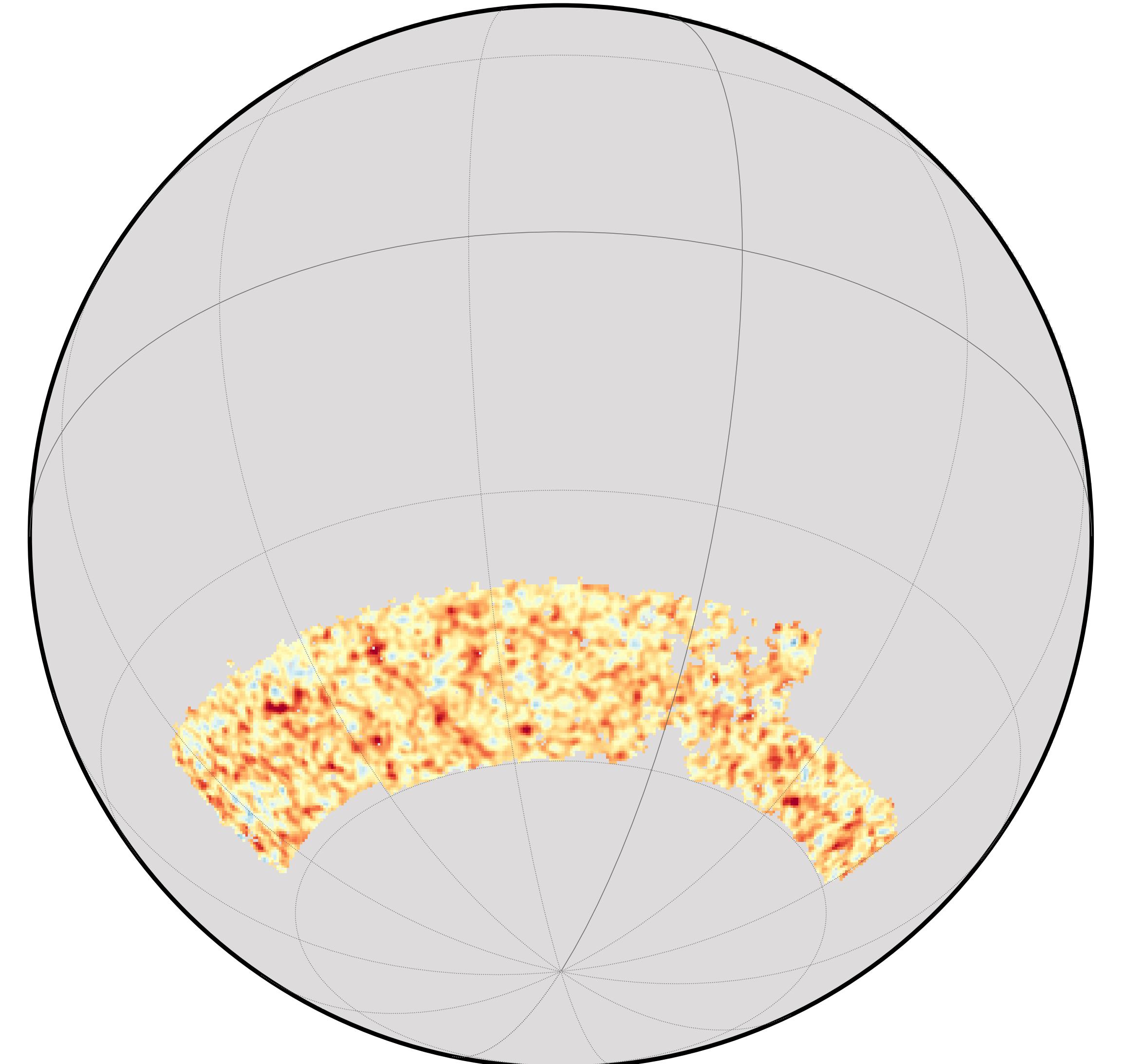


-0.015 Weak lensing mass 0.01

150 deg²
3.4 M galaxies

Vikram, CC, Jain et al. (2015)
CC, Vikram, Jain et al. (2015)

Y1 (2018)



-0.015

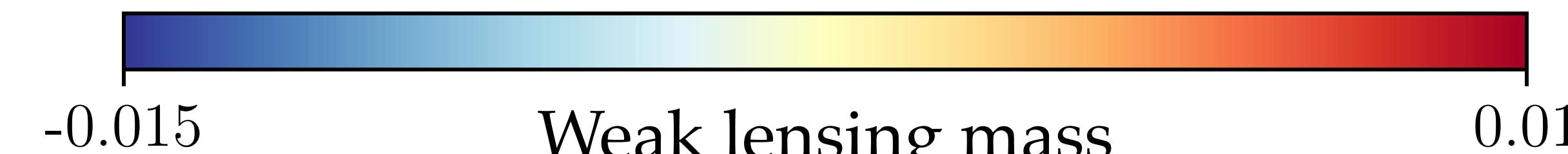
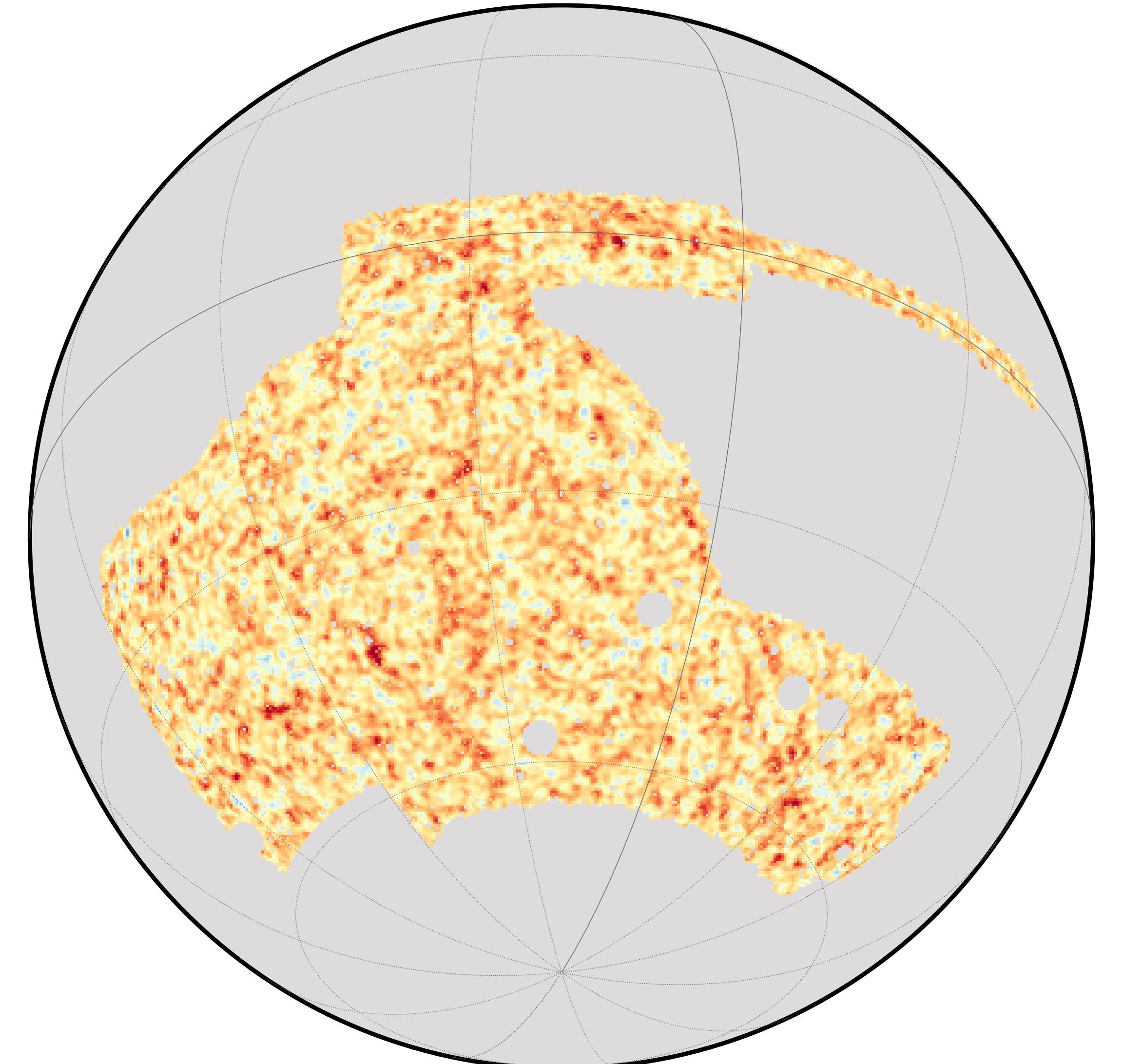
Weak lensing mass

0.01

1,300 deg²
35 M galaxies

CC et al. (2018)
DES Collaboration

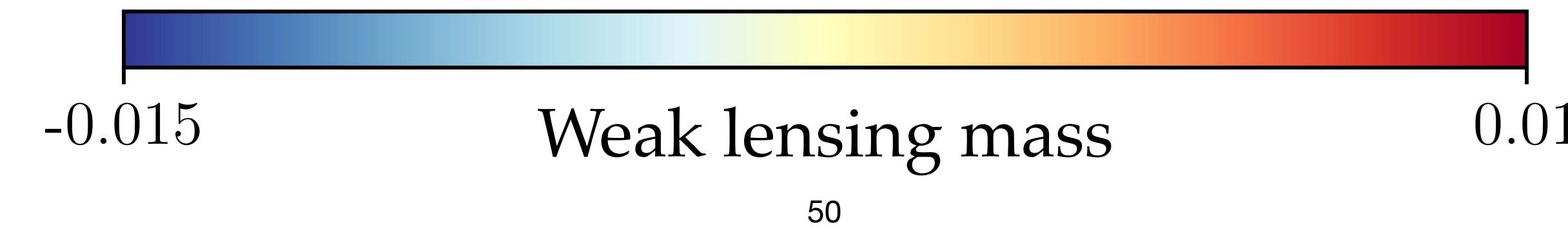
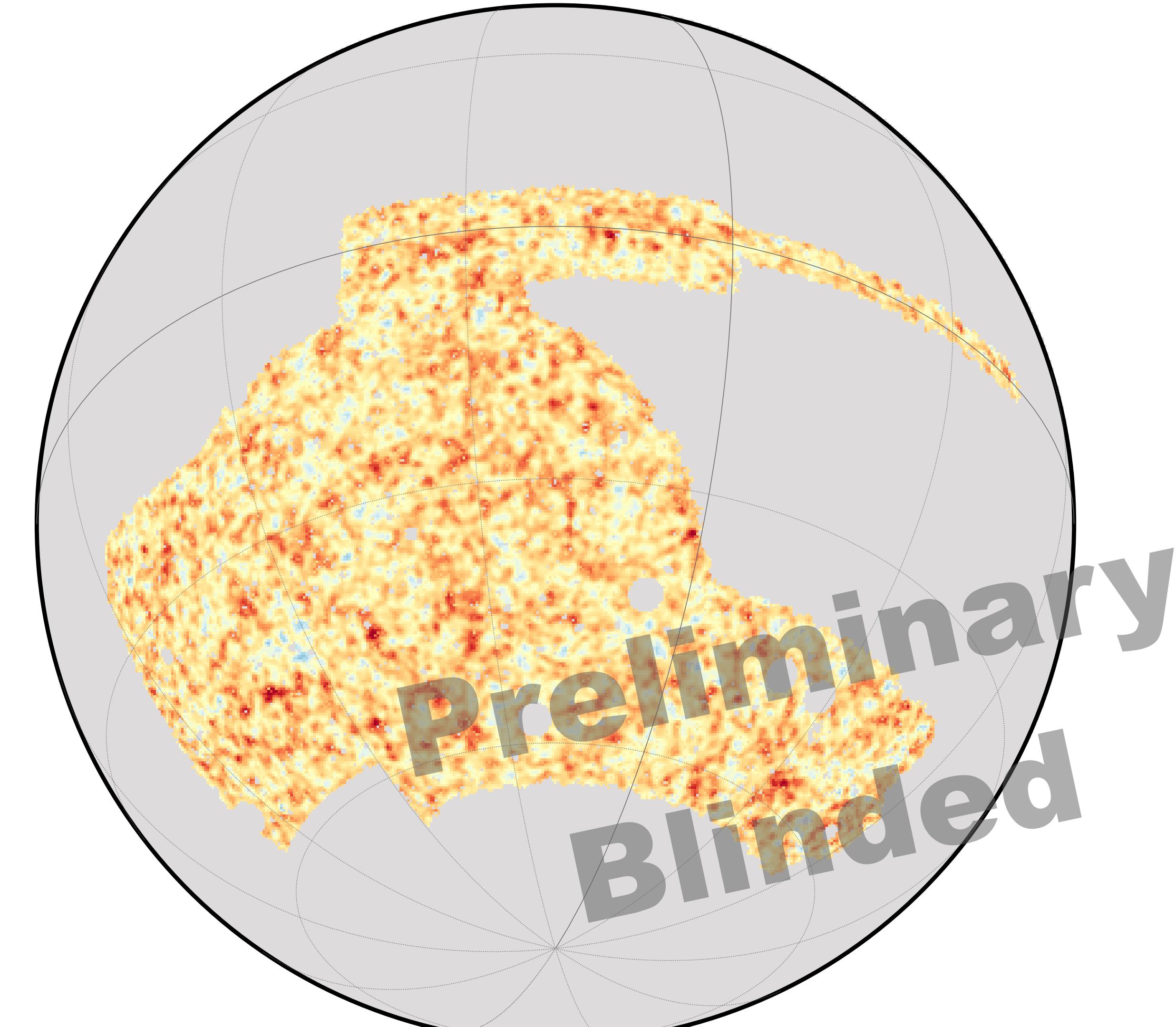
Y3 (2021)



4,300 deg²
100 M galaxies

*Jeffrey, Gatti, CC et al. (2021)
DES Collaboration*

Y6 (2024)
expected



$\sim 4,300 \text{ deg}^2$
 $\sim 150 \text{ M galaxies}$

DES Collaboration

May 16



Summary & Outlook

- The gain in beyond 2pt statistics depends on **the science, the dataset, and how we extract the signal** — it may not always make sense to go to the highest order
- There are practical challenges that we are working on to make HOS **more robust**
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