

# Extensive air shower predictions: sufficiently constrained by accelerator data?

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arXiv: 2401.06202; 2403.16106; 2404.02085; 2409.05501

Jet production in MC generators: collinear factorization of pQCD

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- for  $Q_0 \sim$  few GeV, soft physics irrelevant
  - $\Rightarrow$  a perturbative mechanism missing
- **are MC predictions trustworthy, without such a mechanism?**

# Dynamical higher twist effects in hadronic scattering

Hint: collinear factorization of pQCD valid at leading twist level

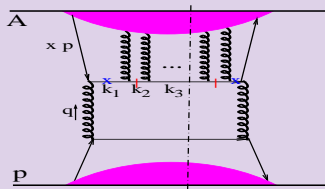
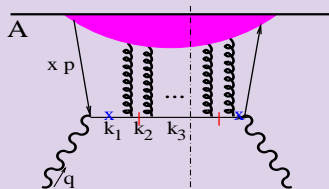
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HT effects in  $\gamma^*A/pA$ : coherent multiple scattering on 'soft' gluons  
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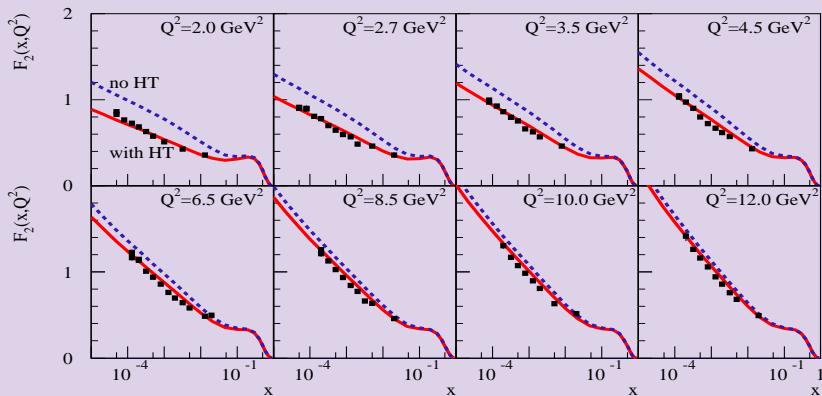
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Extrapolation to hadron-proton & light nuclei

[SO & Bleicher, Universe 5 (2019) 106; SO, arXiv: 2401.06202]

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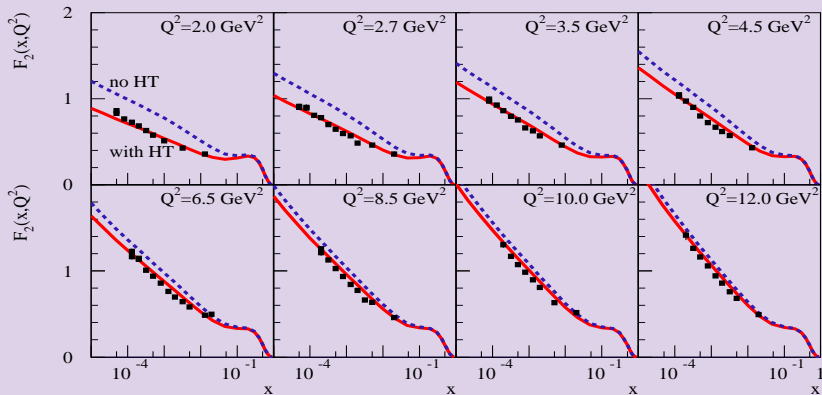
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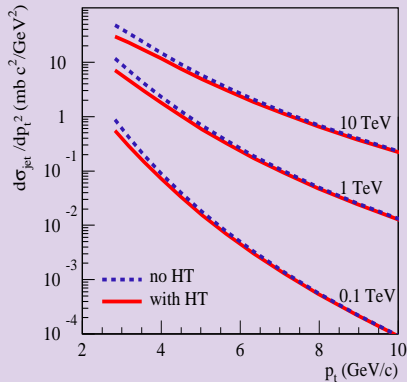
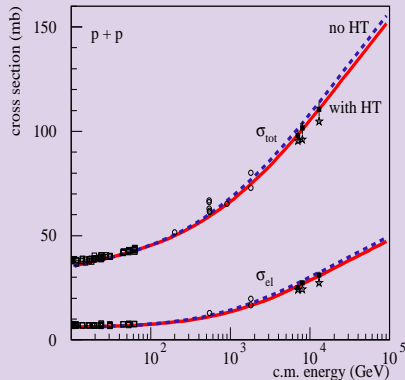
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- HT corrections important at low  $Q^2$ 
  - $\Rightarrow$  too strong corrections at tension with  $Q^2$ -evolution of  $F_2$
- known fact:  $Q^2$ -evolution of  $F_2$  is well-described by DGLAP
  - $\Rightarrow$  little space for HT or/and saturation effects

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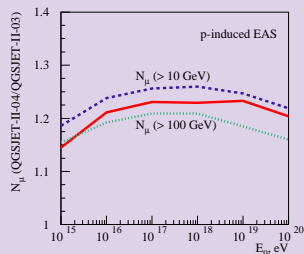
Small effect on  $\sigma_{pp}^{\text{tot/el}}$  but taming the low- $p_t$  rise of (mini)jet rates



• ⇒ the mechanism does its principal job

$\pi$ - over  $\rho$ -exchange dominance  $\Rightarrow \sim 20\%$  increase of  $N_\mu$

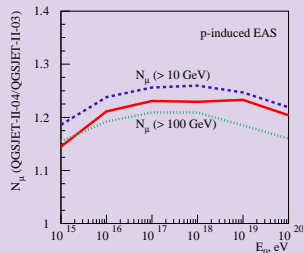
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[SO, talk at ISVHECRI-2012]

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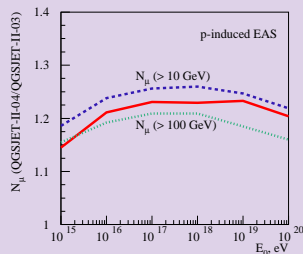
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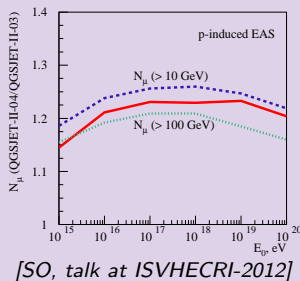
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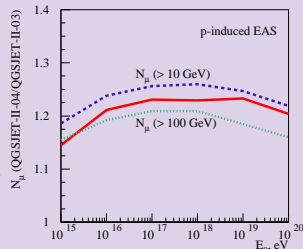
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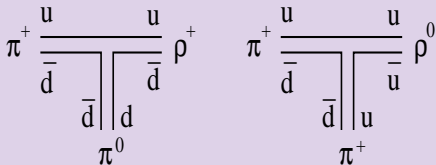
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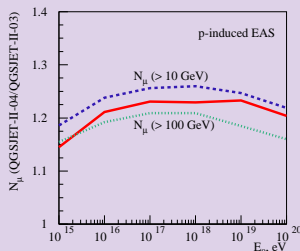
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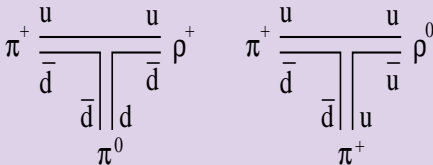
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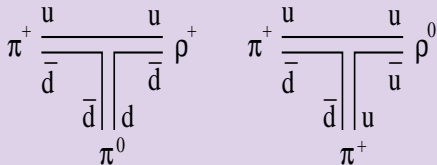
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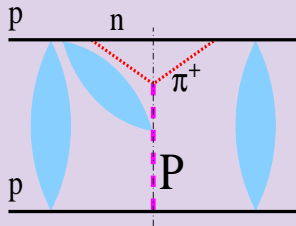
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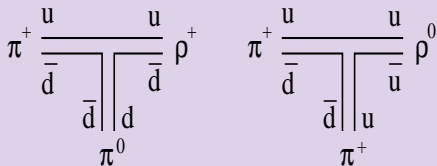
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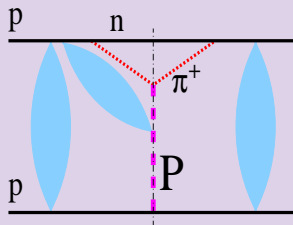
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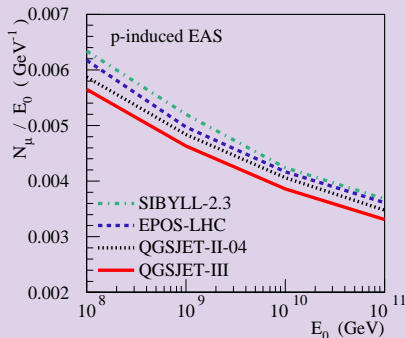
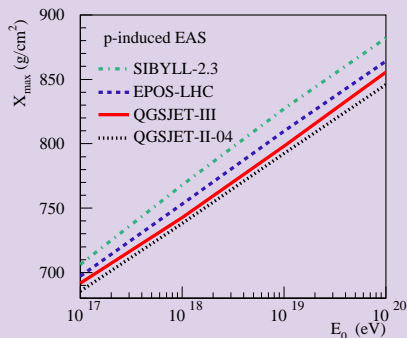


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- now can be tested in  $pp \rightarrow nX$  thanks to LHCf data [backup slides]

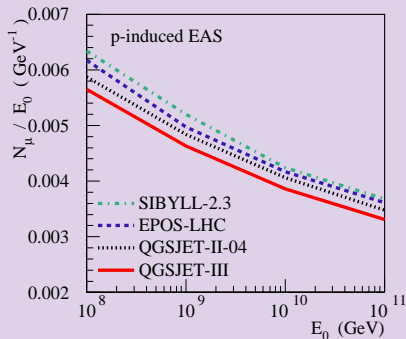
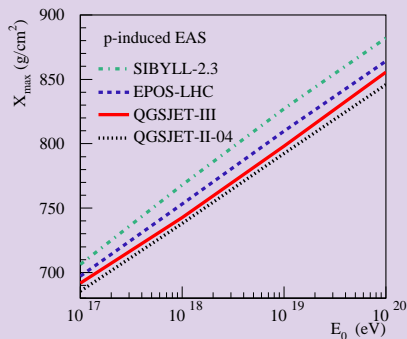


## Rather small changes for $X_{\max}$ and $N_{\mu}$ (wrt QGSJET-II-04)



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## What is the reason for the stability of the predictions?

- the model sufficiently constrained by LHC data?
- or a mere consequence of a particular model approach?

Kinematic range for hadron production, relevant for  $N_\mu$  predictions

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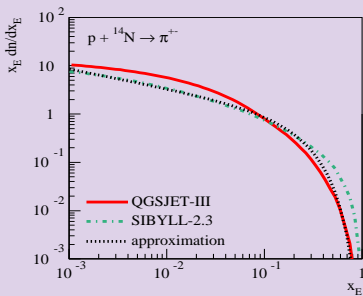
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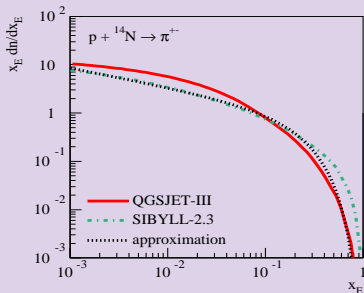
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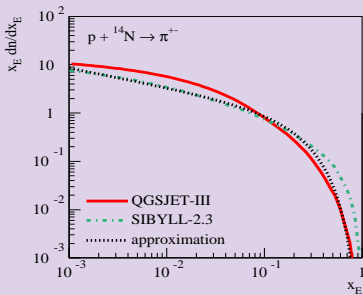
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- relevant  $\langle x_\pi \rangle$  for  $\pi$ -air interactions follows similarly



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- NB:  $\sum_{h=\text{stable}} \langle x_E^h \rangle \simeq 1 - \langle x_E^{\pi^0} \rangle$



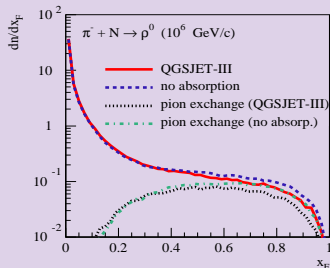
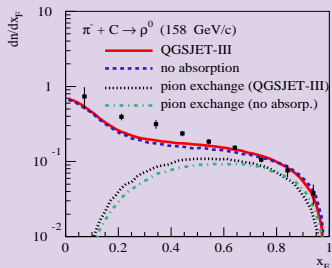
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- change the energy dependence of the pion exchange process  
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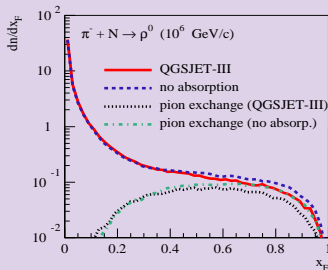
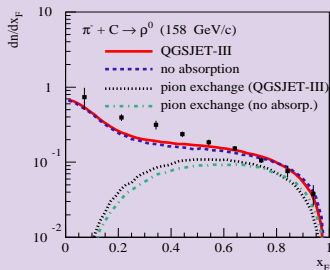
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- change the energy dependence of the pion exchange process  
 $\Rightarrow$  larger forward yield of  $\rho$ -mesons  $\Rightarrow$  higher  $\langle E_{\pi^\pm} \rangle / \langle E_{\pi^0} \rangle$
- **change the model calibration** (e.g. based on NA61 data):  
more kaons & (anti)nucleons

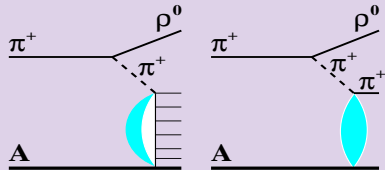
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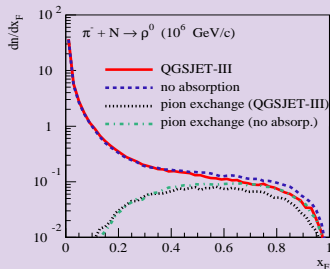
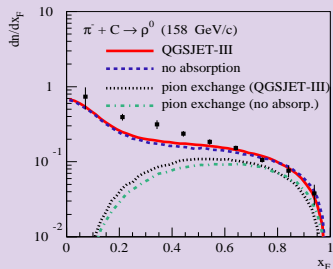


In such a case: large contribution of pion elastic scattering

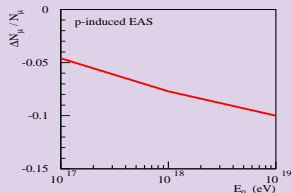


- $\sigma_{\pi\text{-air}}^{\text{el}} \rightarrow \frac{1}{2} \sigma_{\pi\text{-air}}^{\text{tot}}$  at  $E_0 \rightarrow \infty$
- $\Rightarrow$  scarce hadron production!

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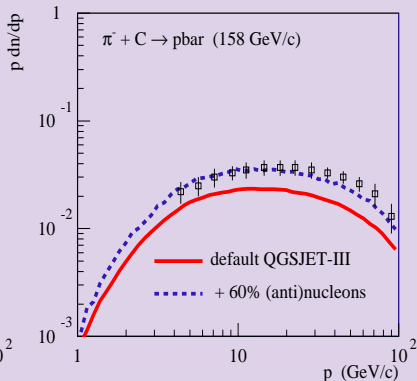
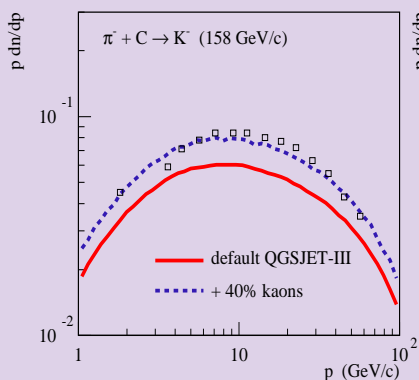


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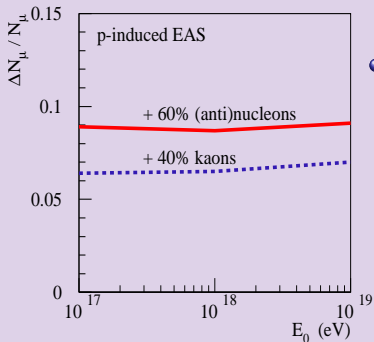
- $\sigma_{\pi\text{-air}}^{\text{el}} \rightarrow \frac{1}{2}\sigma_{\pi\text{-air}}^{\text{tot}}$  at  $E_0 \rightarrow \infty$
- $\Rightarrow$  scarce hadron production!
- $\Rightarrow$  decrease of  $N_\mu$  (instead of an enhancement)

## NA61 data: very high yields of kaons & (anti)protons in $\pi^-C$



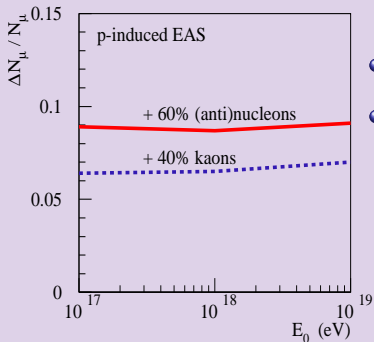
- $\simeq 40\%$  more kaons &  $\simeq 60\%$  more (anti)protons required
- NB: such enhancements create a tension with other data on kaon & (anti)proton production in  $\pi p$  &  $pp$  interactions

## Relative changes of the calculated $N_\mu$ : $< 10\%$



• why?

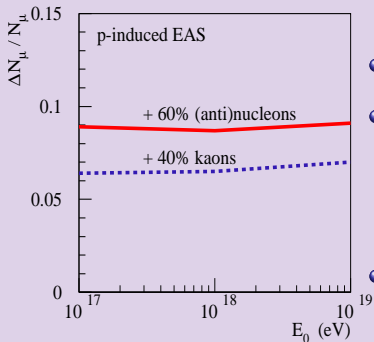
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- **small impact of the the considered enhancements on  $\sum_{h=\text{stable}} \langle x_E^h \rangle$**  (changes mostly affect central hadron production)



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- small impact of the the considered enhancements on  $\sum_{h=\text{stable}} \langle x_E^h \rangle$  (changes mostly affect central hadron production)
- $\Rightarrow$  **accelerator data allow one to enhance  $N_\mu$  by up to  $\sim 10\%$**

## Predictions for EAS maximum depth $X_{\max}$ : 3 main 'switches'

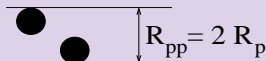
- inelastic proton-air cross section ( $\sigma_{p\text{-air}}^{\text{inel}}$ )
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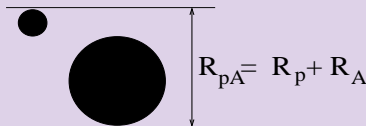
## Inelastic cross section: well constrained by LHC data

- **< 3% difference for  $\sigma_{pp}^{\text{inel}}$  between ATLAS & TOTEM**  
( $79.5 \pm 1.80$  &  $77.41 \pm 2.92$  mb)



- even smaller difference for  $pA$ :

$$\sigma_{pp}^{\text{inel}} \propto R_p^2, \quad \sigma_{pA}^{\text{inel}} \propto (R_p + R_A)^2$$

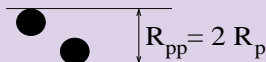


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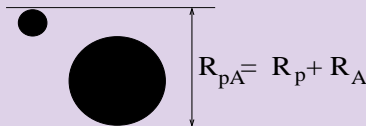
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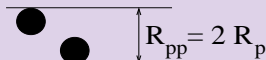


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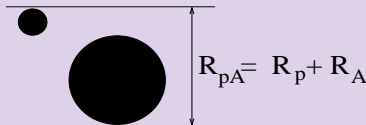
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Diffraction uncertainties:  $\Delta X_{\max} \lesssim 5 \text{ g/cm}^2$  [SO, PRD89 (2014) 074009]

The only significant freedom left: inelasticity for  $p - \text{air}$

- higher energy  $\Rightarrow$  **higher multiple scattering**  $\Rightarrow$  higher  $K_{p-\text{air}}^{\text{inel}}$

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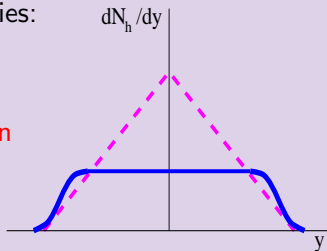
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## How to give less energy away to secondary hadrons?

- central rapidity density of secondaries: constrained by data
- main 'switch': **constituent parton (string end) momentum distribution** ( $x^{-\alpha_q}$ ) [SO, *J.Phys. G29 (2003) 831*]



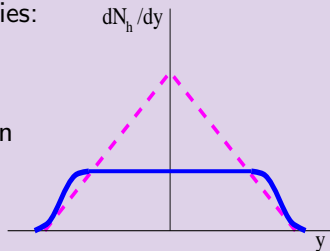


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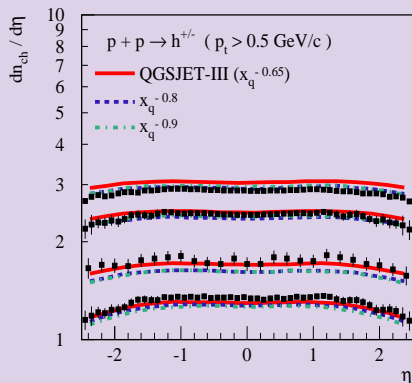
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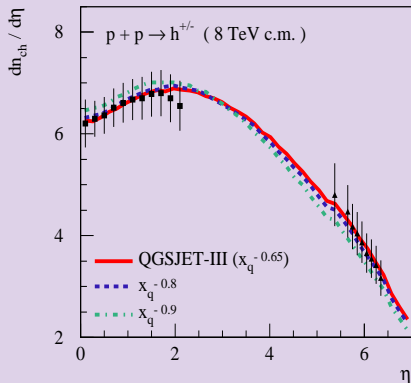
- $\alpha_q \rightarrow 1$ : approximate Feynman scaling for forward spectra
- NB: may not work for semihard scattering (minijet production)

Vary the string end distributions,  $x^{-\alpha_q}$ : with  $\alpha_q = 0.65, 0.8, 0.9$



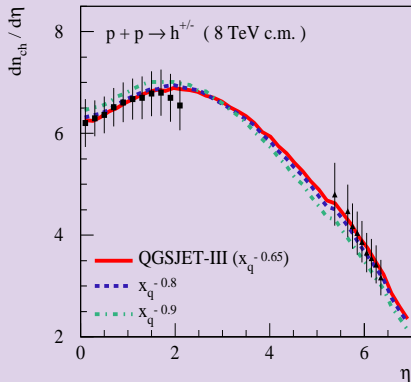
- same model tuning:
  - to fixed target data
  - and to central production at LHC

## Check with more forward data from CMS & TOTEM



- the trend towards larger  $\alpha_q$  not supported
- but can not yet be disproved

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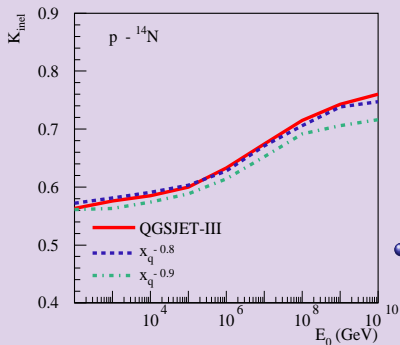


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- NB: higher discrimination power expected from combined studies with central & forward detectors (e.g. LHCf & ATLAS)

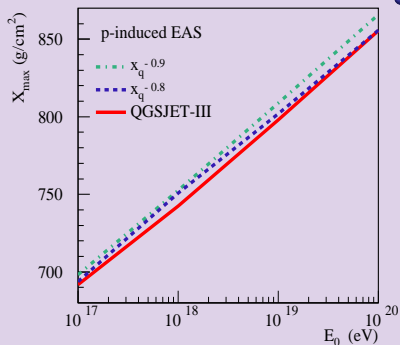
[SO, Bleicher, Pierog & Werner, PRD94 (2016) 114026]

## Choice of string end distribution ( $x^{-\alpha_q}$ ): impact on $K_{p\text{-air}}^{\text{inel}}$



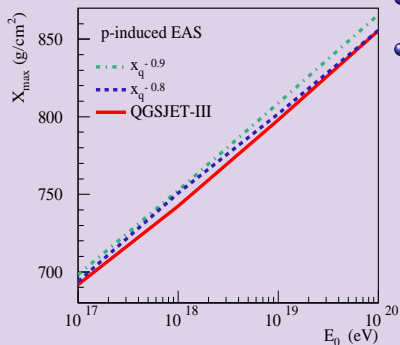
- up to  $\simeq 6\%$  reduction of  $K_{p\text{-air}}^{\text{inel}}$

## Choice of string end distribution ( $x^{-\alpha_q}$ ): impact on $X_{\max}$



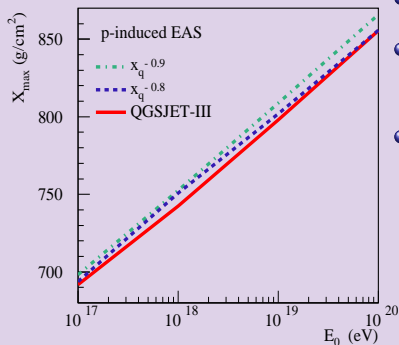
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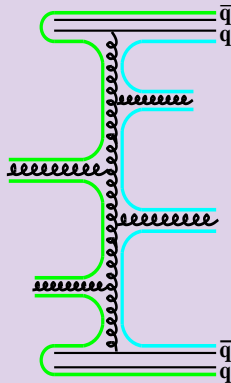
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- up to  $\simeq 10$  g/cm<sup>2</sup> shift of  $X_{\max}$
- why a moderate effect on particle production &  $X_{\max}$ ?
- 'warranted' scaling violation due to semihard scattering (energy fraction taken by perturbatively generated partons  $\Rightarrow$  lower bound on  $K_{p\text{-air}}^{\text{inel}}$ )  
[see backup slides]



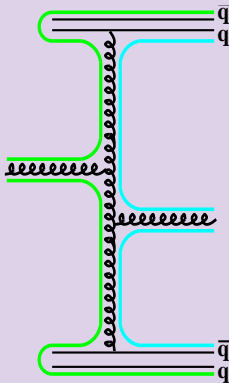
## Exotic: modification of the hadronization by 'collective effects'



- standard treatment: strings of color field stretched between constituent partons and/or all perturbatively produced partons
  - $\Rightarrow$  production of partons (& hadrons) covers the full rapidity range

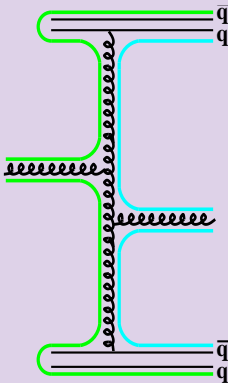
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- assuming this is modified by 'collective effects' & neglecting parton cascades:  
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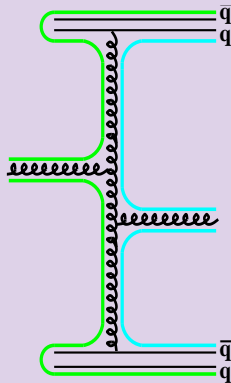


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  - $\Rightarrow$  small impact on  $K_{p\text{-air}}^{\text{inel}}$

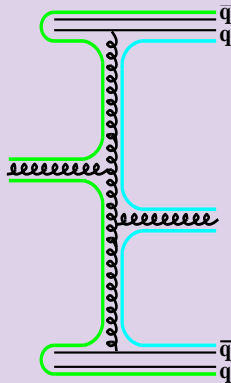


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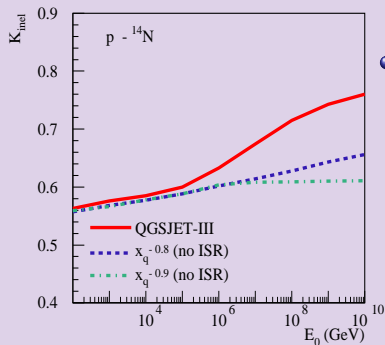
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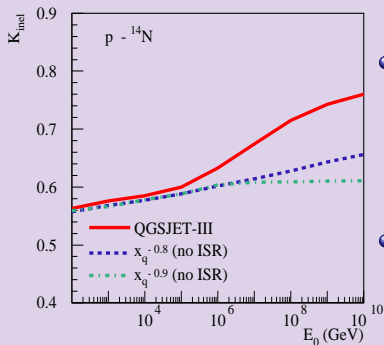
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- rather nonphysical: collective effects may be strong in central (small  $b$ ) collisions only
  - $\Rightarrow$  **should not have large impact on the average parton production pattern** (dominated by peripheral collisions)

## Impact of string end distribution on $K_{p\text{-air}}^{\text{inel}}$ (no parton cascades)



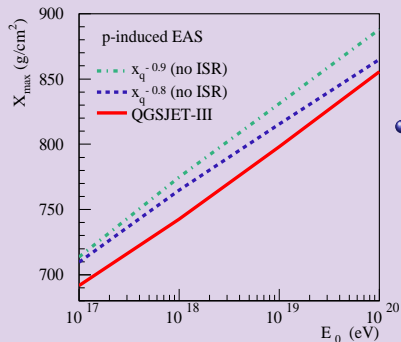
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- $\Rightarrow$  (mini)jet production has no impact on the inelasticity in the  $\alpha_q \rightarrow 1$  limit

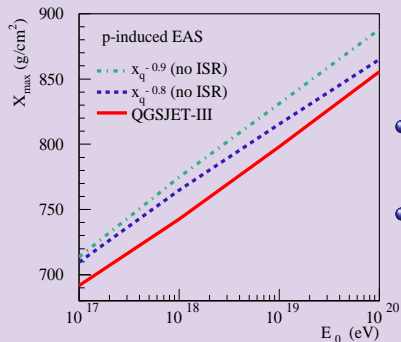
## Impact of string end distribution on $X_{\max}$ (no parton cascades)



- up to  $\simeq 30$  g/cm<sup>2</sup> shift of  $X_{\max}$  ( $\alpha_q = 0.9$ )

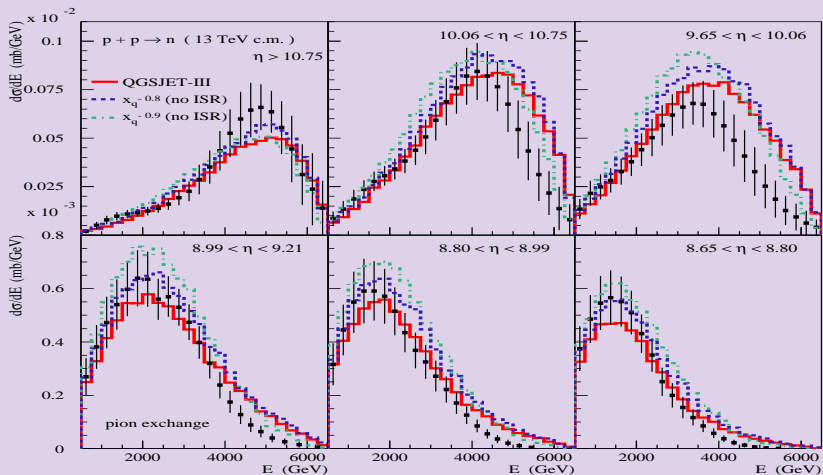


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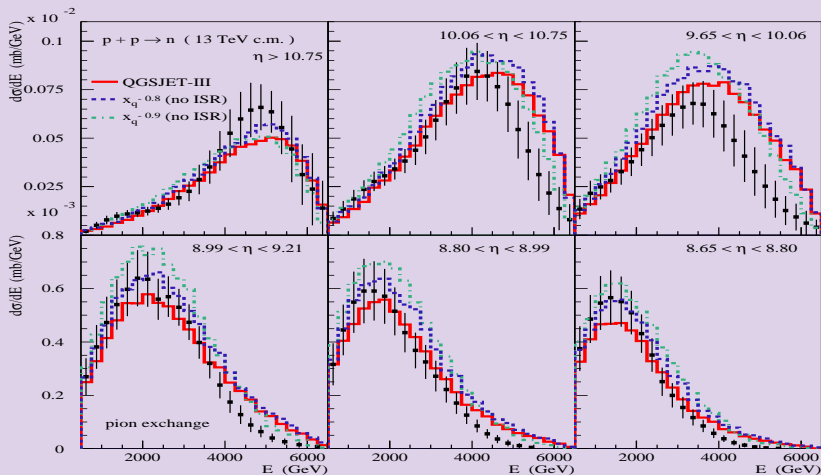
- up to  $\simeq 30 \text{ g}/\text{cm}^2$  shift of  $X_{\max}$  ( $\alpha_q = 0.9$ )
- can be refuted/constrained by LHC data?

The limit  $\alpha_q \rightarrow 1$ : disfavored by LHCf data on forward neutrons



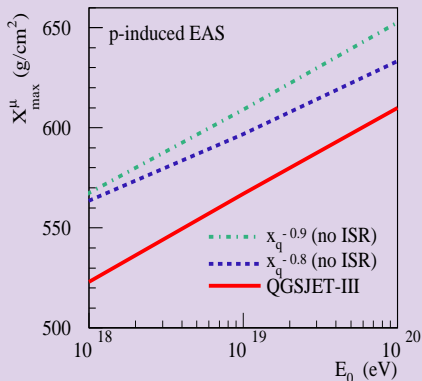
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- $\alpha_q \rightarrow 1$ : forward neutron yield exceeds the measured one
- $\Rightarrow$  energy loss of leading nucleons is underestimated

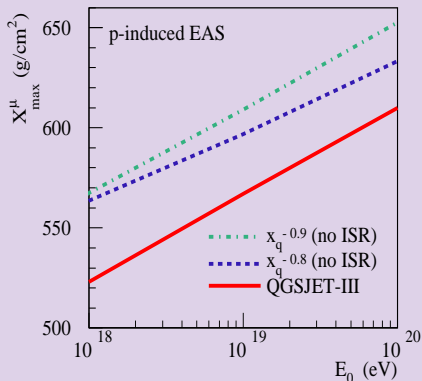
## More important constraints: from PAO measurements of $X_{\max}^{\mu}$



- any change of  $X_{\max}$   $\Rightarrow$  similar (or even larger) shift of  $X_{\max}^{\mu}$

[see backup slides]

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[see backup slides]
- $\alpha_q \rightarrow 1$ : up to  $\sim 40 \text{ g}/\text{cm}^2$  larger  $X_{\max}^{\mu}$ 
  - $\Rightarrow$  strong tension with PAO measurements of  $X_{\max}^{\mu}$

- Major development in QGSJET-III: **phenomenological treatment of HT corrections to hard scattering processes**
  - tames the low  $p_t$  rise of (mini)jet rates
  - reduces the model dependence on the low  $p_t$  cutoff  $Q_0$
- Technical improvement: treatment of  $\pi$ -exchange process
  - energy-dependence: due to absorptive corrections (probability not to have additional inelastic rescattering)
- Rather small changes for EAS characteristics (wrt QGSJET-II)
  - up to  $\simeq 10$  g/cm<sup>2</sup> shift of  $X_{\max}$  and up to  $\simeq 5\%$  change of  $N_\mu$
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# Outlook

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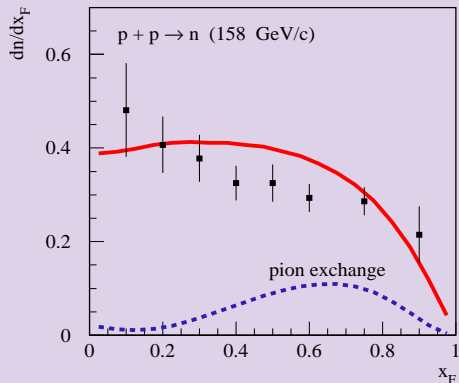
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Extra slides follow

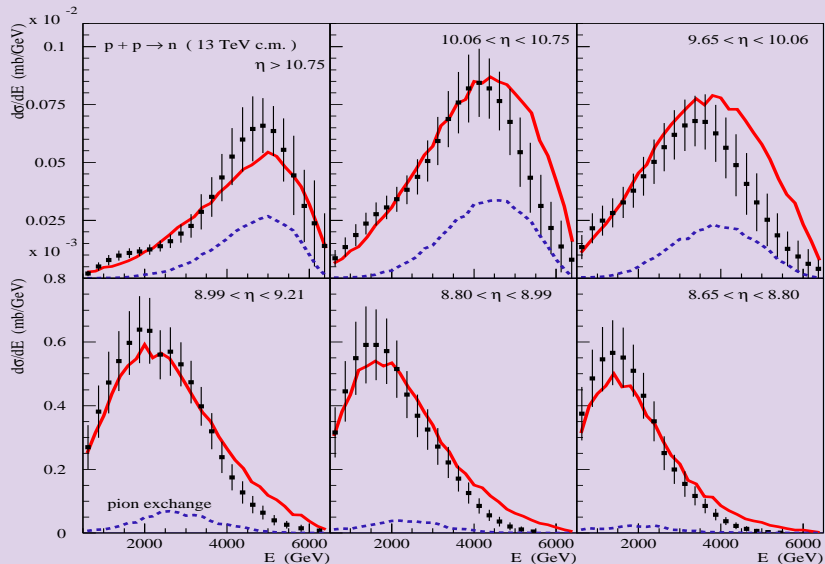
# (1) Technical improvement: $\pi$ -exchange process

Starting with NA49 data at 158 GeV/c



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And moving over 6 energy decades to 13 TeV c.m.



## (2) Hard scattering: importance of the parton cascade

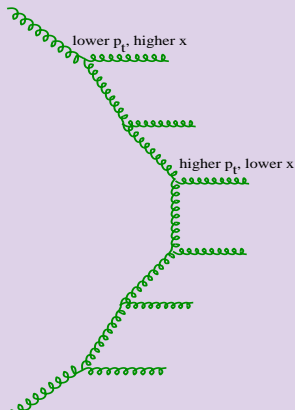
- high energies  $\Rightarrow$  **quick rise of (mini)jet production**
  - small  $\alpha_s(p_t^2)$  - compensated by infrared and collinear logs (arising from parton cascading):  $\ln(x_i/x_{i+1})$ ,  $\ln(p_{t_{i+1}}^2/p_{t_i}^2)$

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- hadron jets: typically produced in central region ( $y \sim 0$ ) in c.m.s.
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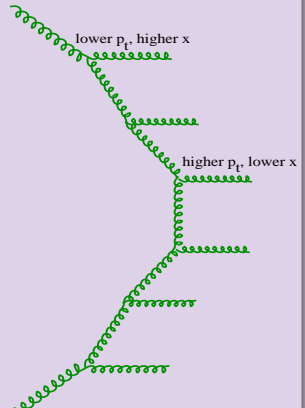


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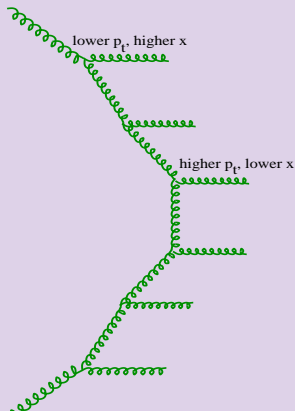


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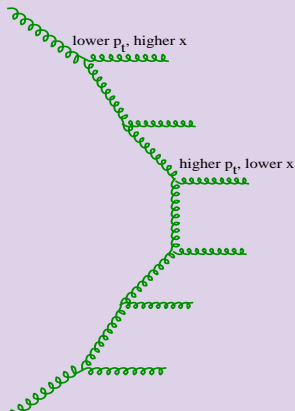


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- no:  $x$ -distribution of those gluons is weighted with the hard scattering!



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Virtual gluons emitted by protons are indeed soft:  $\propto x^{-1-\Delta_g}$

- but the probability for hard scattering: convolution with  $\sigma_{gg}^{\text{hard}}$

$$w_{\text{hard}}(s) \propto \int dx^+ dx^- f_g(x^+, Q_0^2) f_g(x^-, Q_0^2) \sigma_{gg}^{\text{hard}}(x^+ x^- s, Q_0^2)$$

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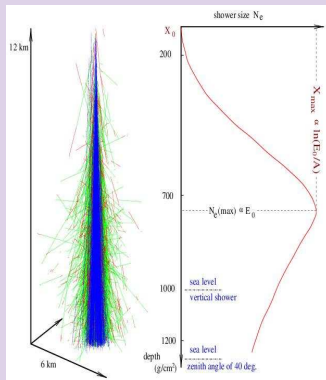
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- $\sigma_{gg}^{\text{hard}}(\hat{s}, Q_0^2) \propto \hat{s}^{\Delta_{\text{hard}}}$  – contribution of the DGLAP 'ladder'
- $\Rightarrow$  **gluons which succeed to interact have large  $x$ :  $\propto x^{\Delta_{\text{hard}}-\Delta_g-1}$**   
(iff  $\Delta_{\text{hard}} \simeq 0.3 > \Delta_g$ )
  - i.e., first partons in a perturbative cascade are 'valence-like' (independently on our assumptions for string end distribution)

### (3) Most general warning regarding large $X_{\max}$ predictions

Changing  $X_{\max}$  implies equal or larger changes for  $X_{\max}^{\mu}$

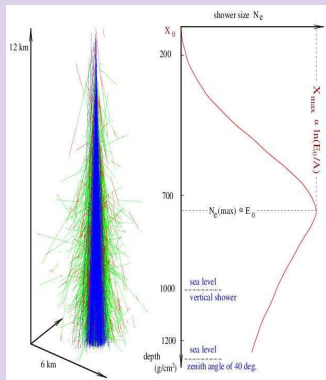
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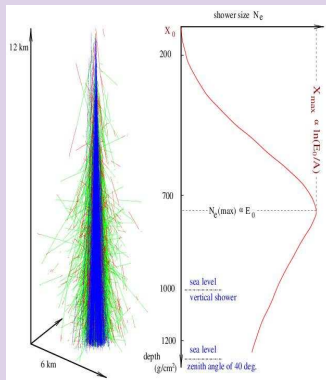
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- $\Rightarrow$  parallel up/down shift of the cascade profile (same shape)
- $\Rightarrow$  same effect on  $X_{\max}$  &  $X_{\max}^{\mu}$
- additionally: **the corresponding change of physics impacts  $\pi$ -air interactions at all the steps of the cascade development**
  - $\Rightarrow$  cumulative effect on  $X_{\max}^{\mu}$

