

# BSS and deep learning

Victor Bonjean

Joint ARGOS-TITAN-TOSCA workshop - 6th/7th June 2024



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the European Union

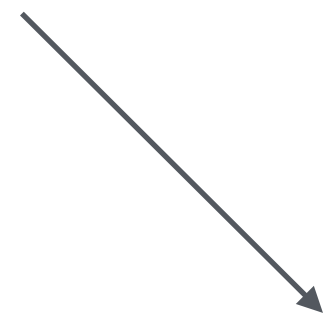
What is component separation?

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$$X = S_0 + S_1 + S_2$$

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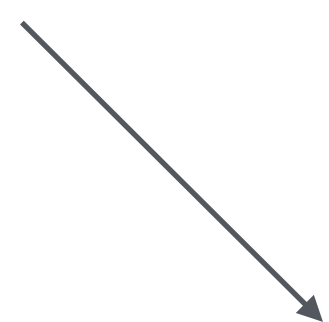
Observation



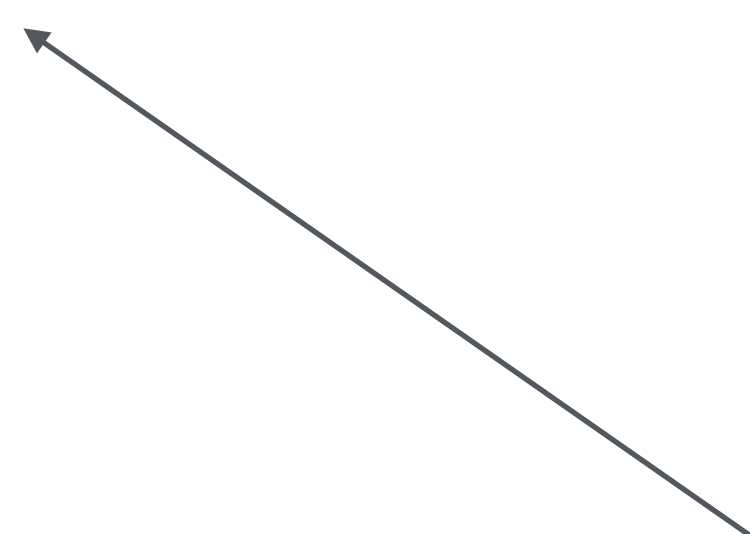
$$X = S_0 + S_1 + S_2$$

What is component separation?

Observation



$$X = S_0 + S_1 + S_2$$



3 components

What is component separation?

Observation

Multiple frequencies

$$X_i = a_i.S_0 + b_i.S_1 + c_i.S_2$$

3 components

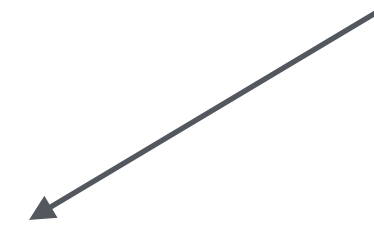
What is component separation?

$$\begin{pmatrix} X_0 \\ X_1 \\ \dots \\ X_n \end{pmatrix} = \begin{pmatrix} a_0 & b_0 & c_0 \\ a_1 & b_1 & c_1 \\ \dots & \dots & \dots \\ a_n & b_n & c_n \end{pmatrix} \cdot \begin{matrix} S_0 \\ S_1 \\ S_2 \end{matrix}$$

n frequencies

What is component separation?

$n \times 3$  « mixing matrix »



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n frequencies



What is component separation?

$$\mathbf{X} = \mathbf{A} \cdot \mathbf{S}$$

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1. We know  $\mathbf{A}$

« No problem »

$$\mathbf{S} = \mathbf{A}^{-1} \cdot \mathbf{X}$$

- Never the case

What is component separation?

$$\mathbf{X} = \mathbf{A} \cdot \mathbf{S} + \mathbf{N}$$

Blind Source Separation (BSS)

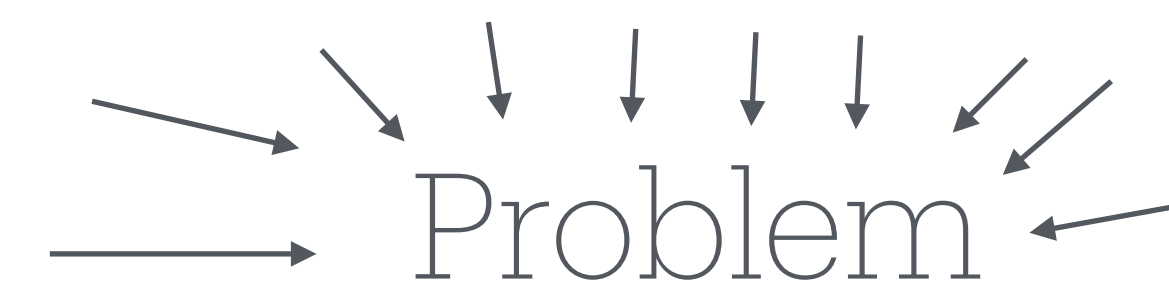
1. We know  $\mathbf{A}$

« No problem »

$$\mathbf{S} = \mathbf{A}^{-1} \cdot \mathbf{X}$$

- Never the case

2. We don't know  $\mathbf{A}$



- FastICA  $\longrightarrow$  Prior on  $\mathbf{S}$
- GMCA
- Unsupervised Learning

What is component separation?

$$\mathbf{X} = \mathbf{A}\mathbf{S} + \mathbf{N}$$

Blind Source Separation (BSS)

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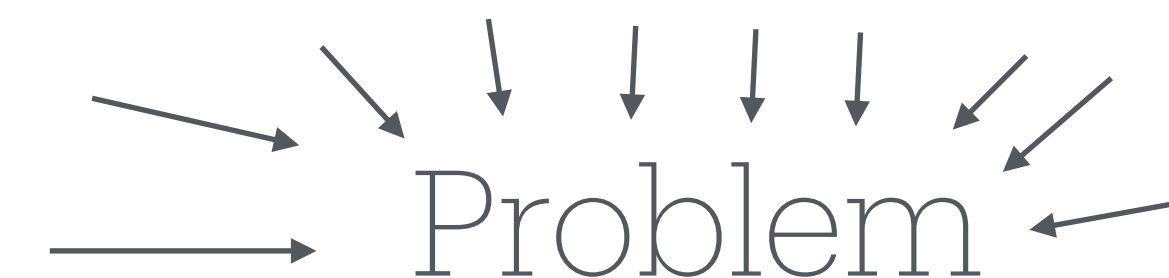
- Never the case

1.5. We know a bit of  $\mathbf{A}$

Problem

- ILC
- GMCA
- Self-supervised Learning
- Template based fitting  
→ Prior on  $\mathbf{A}$

2. We don't know  $\mathbf{A}$



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What is component separation?

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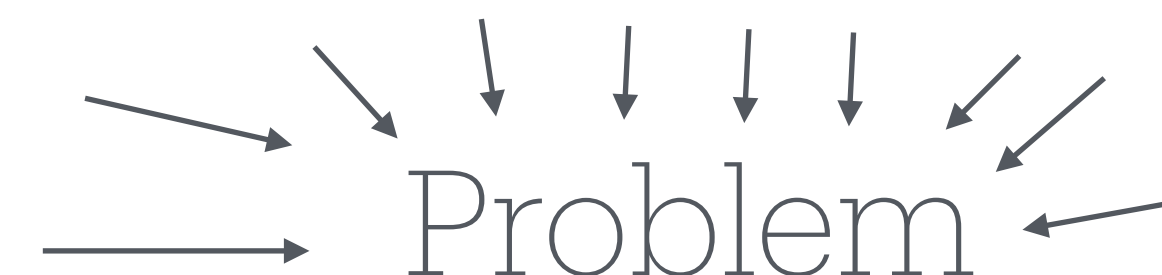
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- **Self-supervised Learning** ✓
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- **Unsupervised Learning** ✓

# What is component separation?

$$\mathbf{X} = \mathbf{A}\mathbf{S} + \mathbf{N}$$

Blind Source Separation (BSS)

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« No problem »

$$\mathbf{S} = \mathbf{A}^{-1}\mathbf{X}$$

- Never the case

1.5. We know a bit of  $\mathbf{A}$

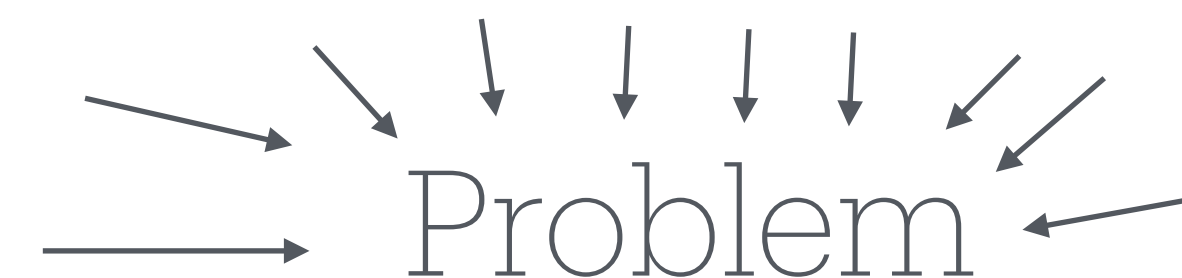
Problem

- ILC
- GMCA
- **Self-supervised Learning** ✓
- Template based fitting

→ Prior on  $\mathbf{A}$

1.75 My work

2. We don't know  $\mathbf{A}$

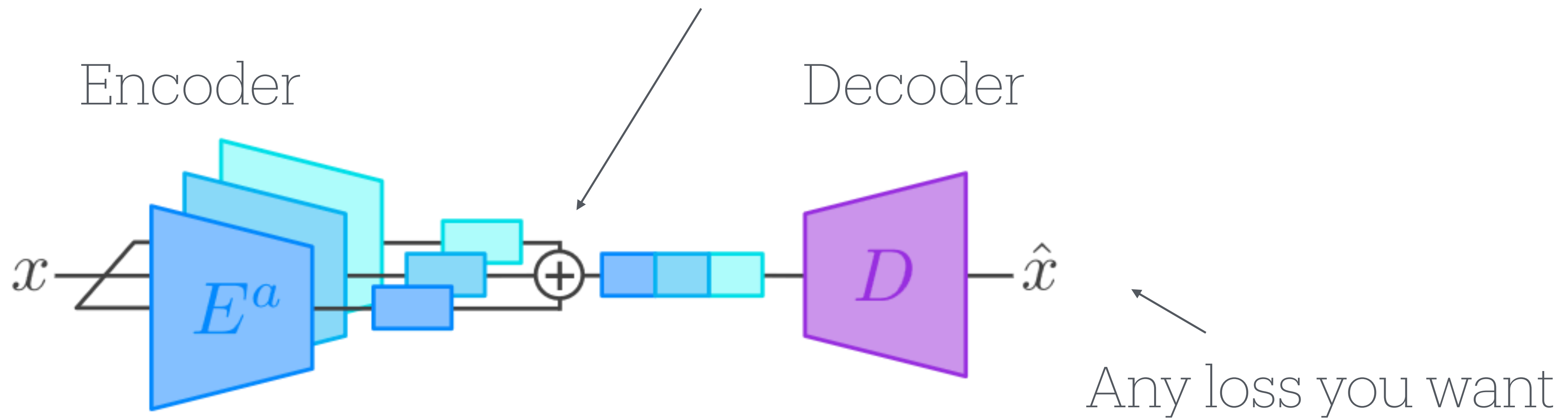


- FastICA → Prior on  $\mathbf{S}$
- GMCA

• **Unsupervised Learning** ✓

# Component separation with deep learning

Anything you want (fitted mixing matrix, **non linear model**...)



**(a) Blind source separation training procedure.**

Webster et al, 2023



# Component separation with deep learning

## Single channel mixture:

Webster et al, 2023

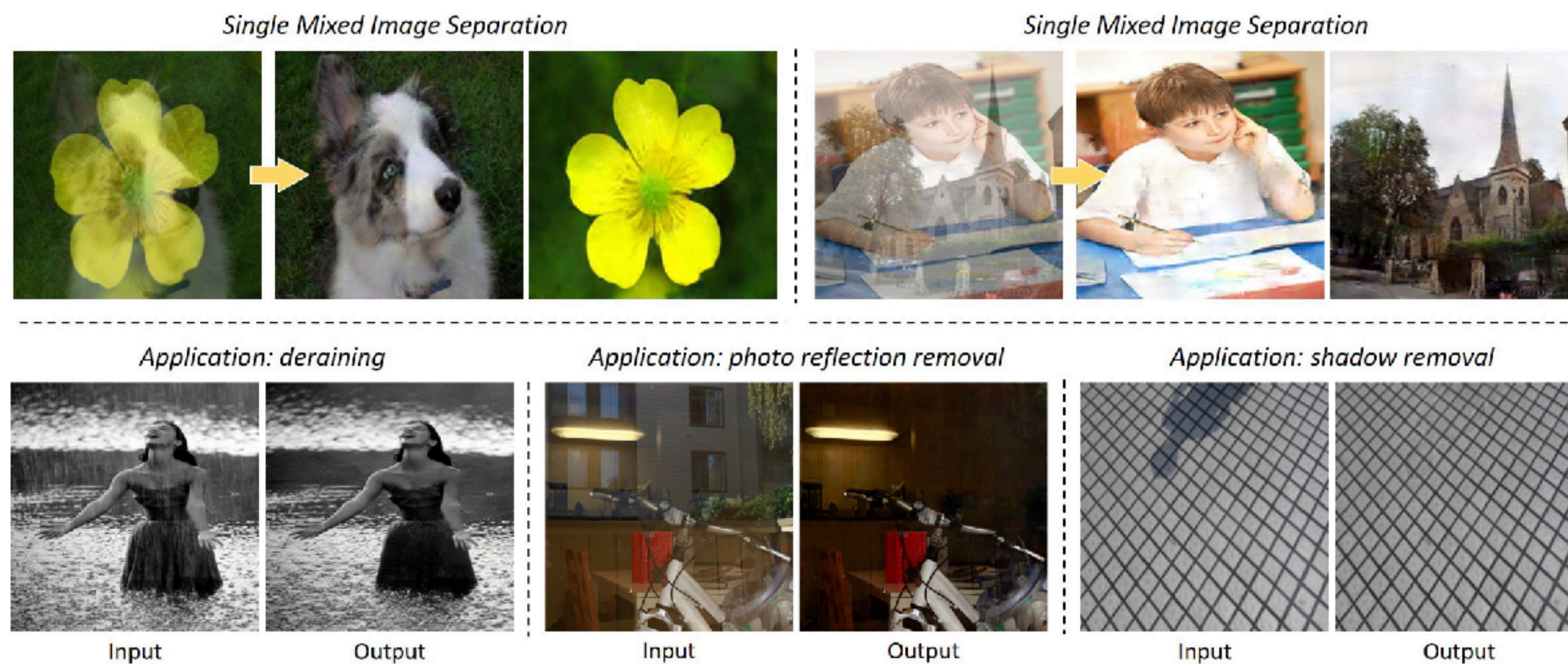


Figure 1: We propose a unified framework for single mixed image separation under an adversarial training paradigm. Our method can be applied to a variety of real-world tasks, including image deraining, photo reflection removal, image shadow removal, etc.

(+ regularization term on (non) correlation)



# Component separation with deep learning

« Double-DIP »

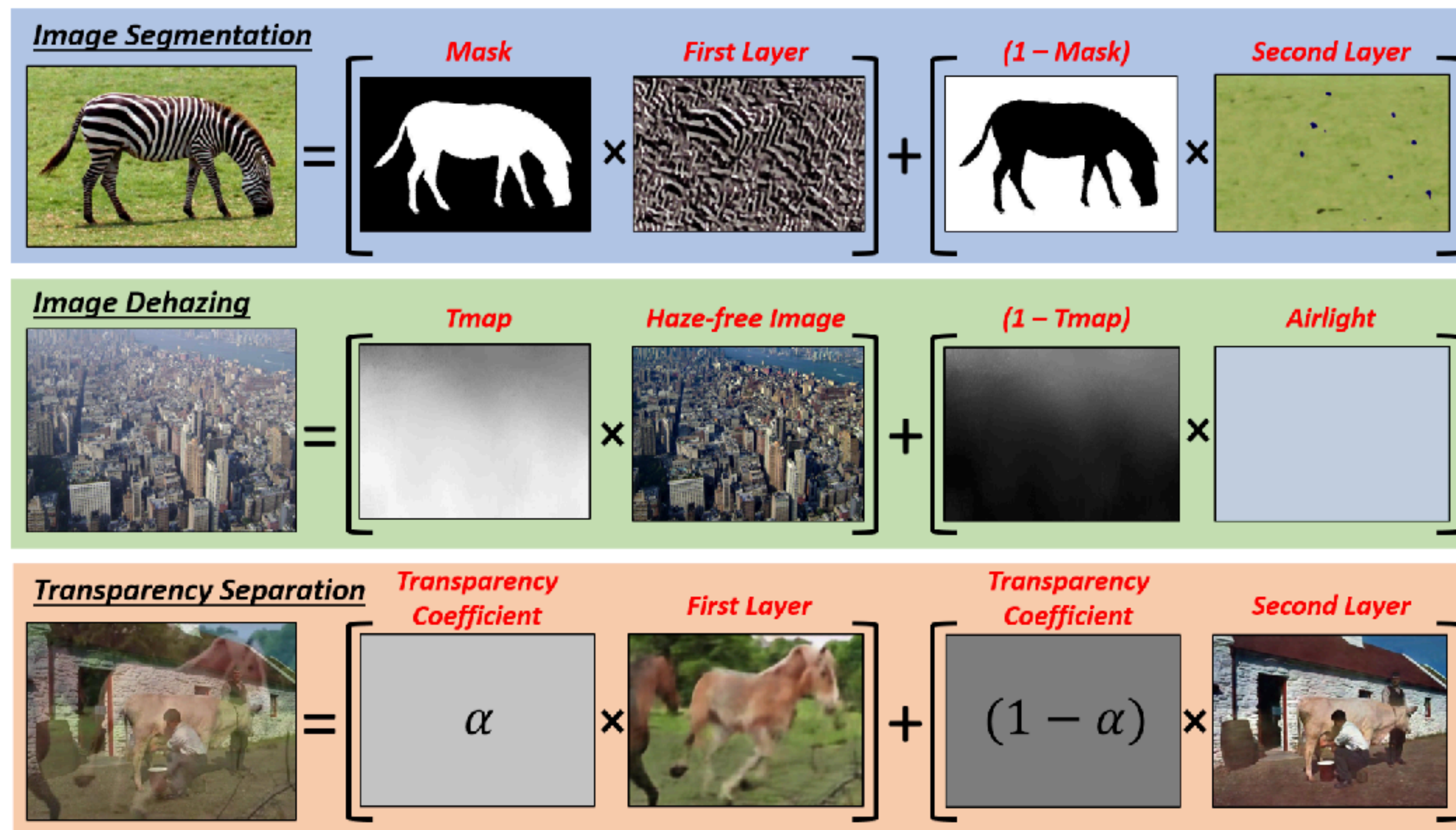


Figure 1: **A unified framework for image decomposition.** An image can be viewed as a mixture of “simpler” layers. Decomposing an image into such layers provides a unified framework for many seemingly unrelated vision tasks (e.g., segmentation, dehazing, transparency separation). Such a decomposition can be achieved using “Double-DIP”.

# Component separation with deep learning

## « Double-DIP »

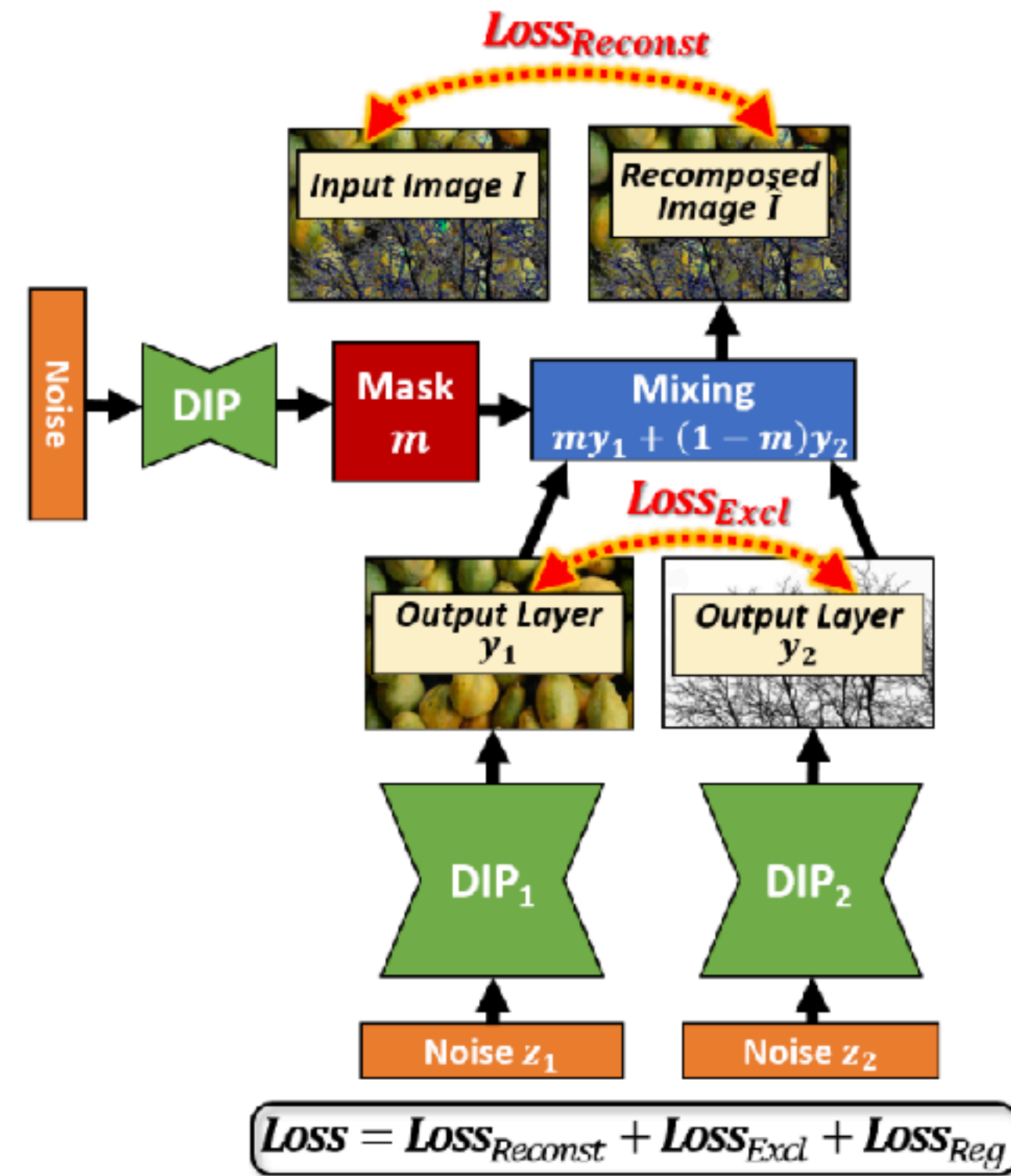
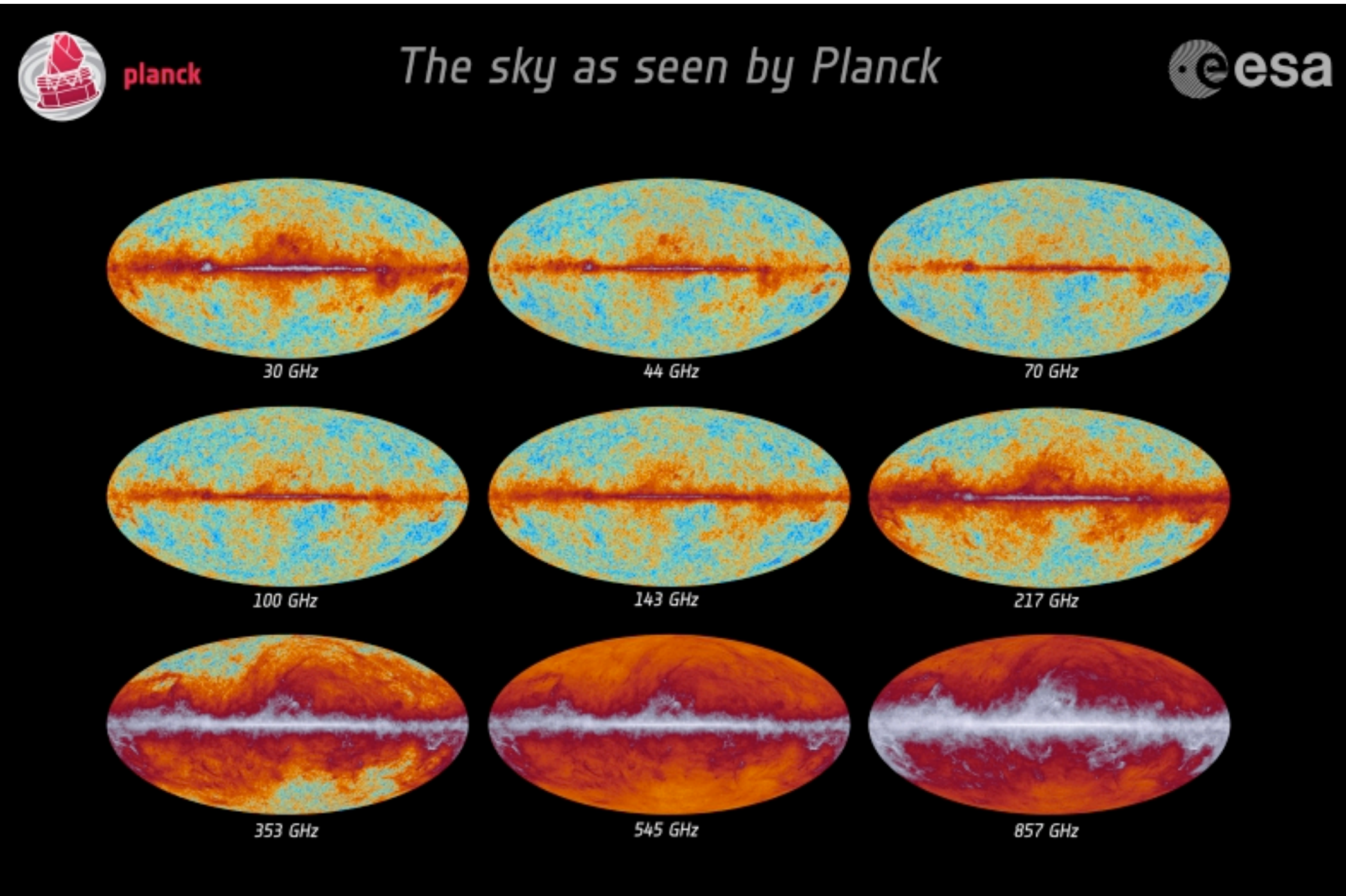


Figure 2: **Double-DIP Framework.** Two Deep-Image-Prior networks ( $DIP_1$  &  $DIP_2$ ) jointly decompose an input image  $I$  into its layers ( $y_1$  &  $y_2$ ). Mixing those layers back according to a learned mask  $m$ , reconstructs an image  $\hat{I} \approx I$ .



# An application to CMB data - CIB removal - SZ extraction

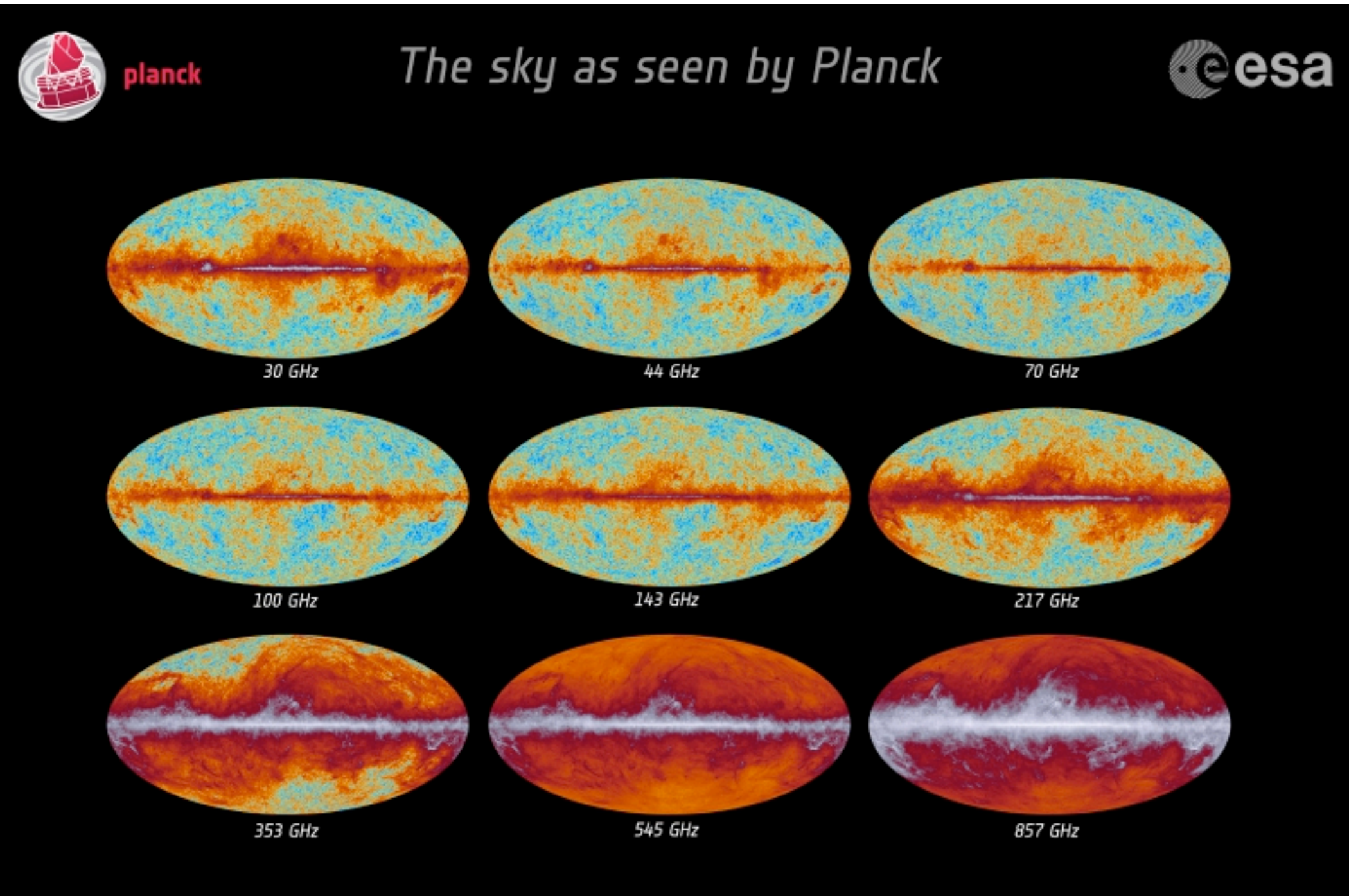


- CMB constant weights
- CIB approximated weights
- tSZ known weights
- Noise known
- Beam known
- kSZ constant weights
- Radio freq. > 90GHz
- Foregrounds (CO + dust + radio)

Major issue



# An application to CMB data - CIB removal - SZ extraction



- CMB constant weights
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Major issue

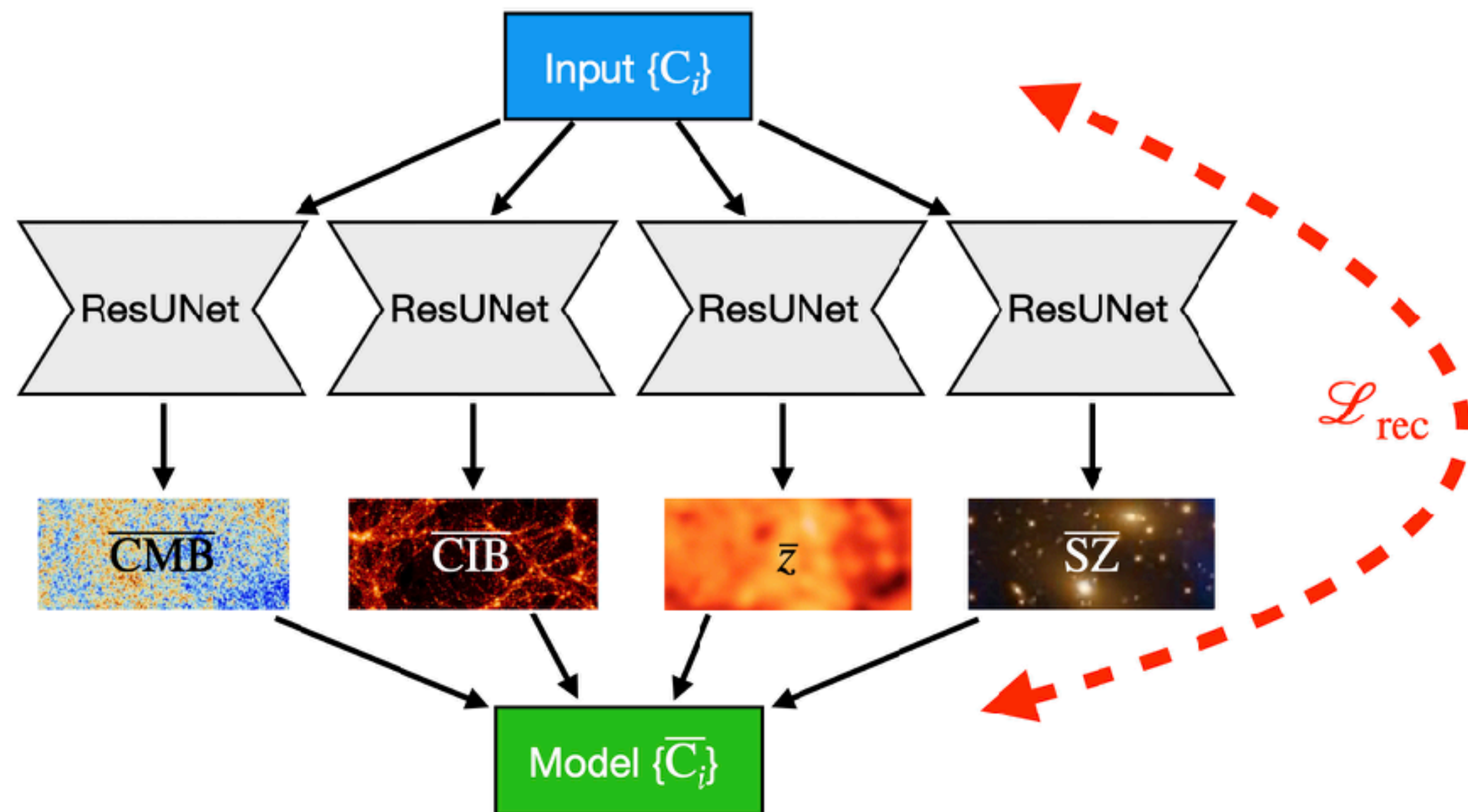
Not statistically independent

$$\longrightarrow \{C_i\} = B_i \circ (1 * (\text{CMB} + \text{kSZ}) + f_i * \text{SZ} + \text{CIB}_i) + N_i$$

Non linear

# An application to CMB data - CIB removal - SZ extraction

$$\rightarrow \{C_i\} = \mathbf{B}i \circ (1 * \text{CMB} + f_i * \text{SZ} + \text{CIB}i) + \mathbf{N}i$$



$$\mathcal{L}_{\text{rec}} = \sum_i \frac{\text{MSE}(C_i, \bar{C}_i)}{\sigma(C_i)}$$

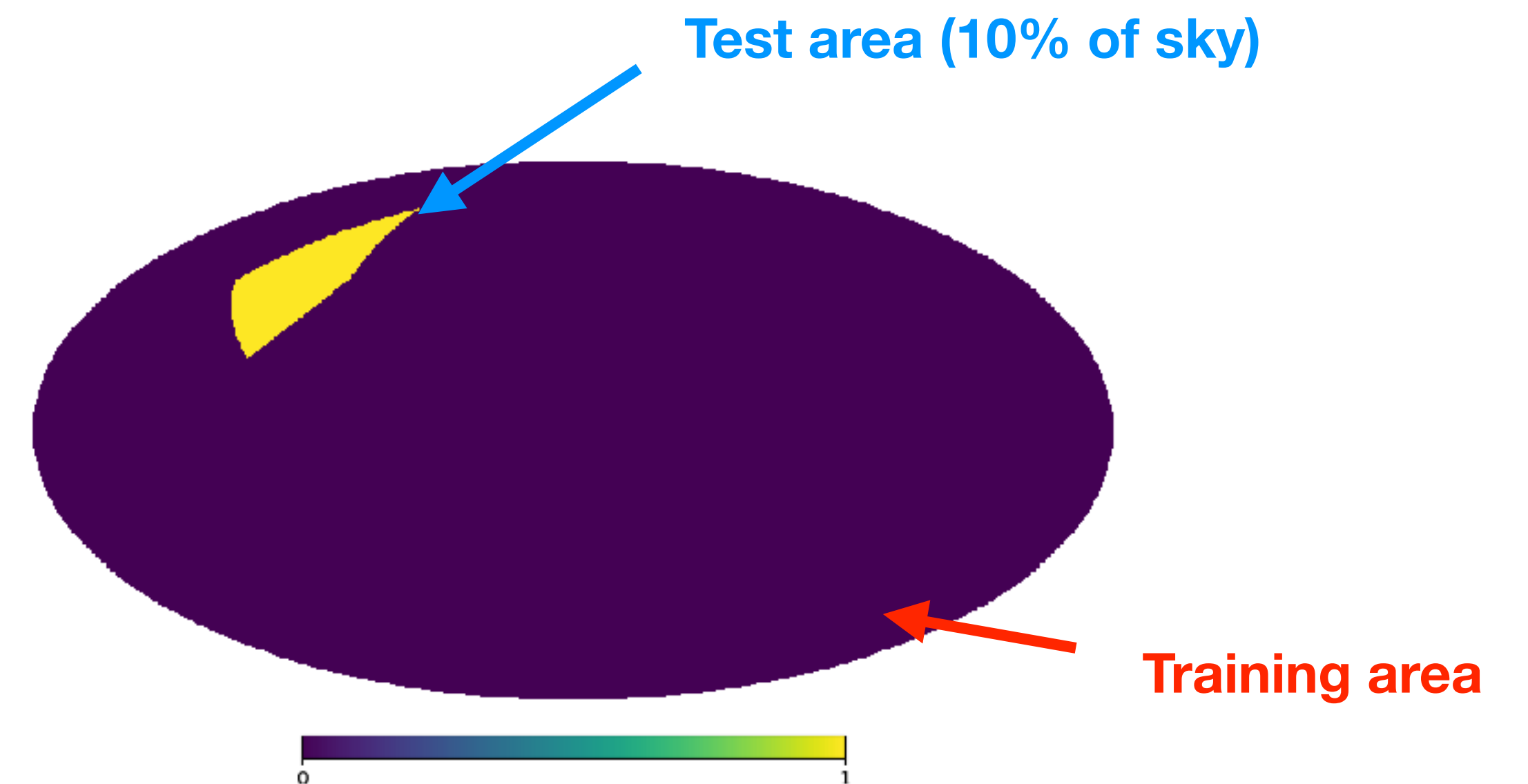
$$\rightarrow \{\bar{C}_i\} = \mathbf{B}i \circ (1 * \text{CMB} + f_i * \text{SZ} + g_i(\bar{z}) * \text{CIB})$$

( $g_i \rightarrow$  Greybody)

# An application to CMB data - CIB removal - SZ extraction

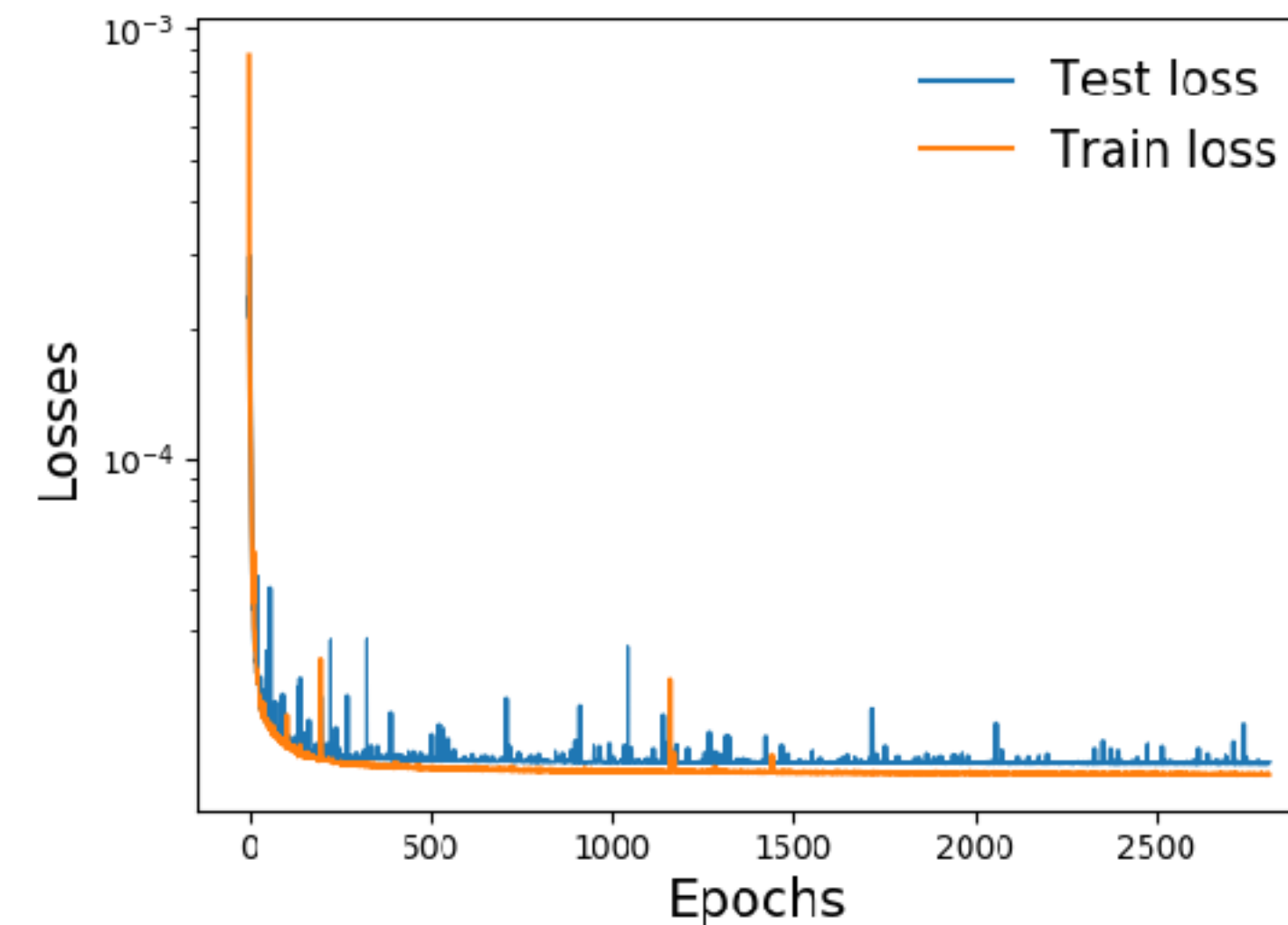
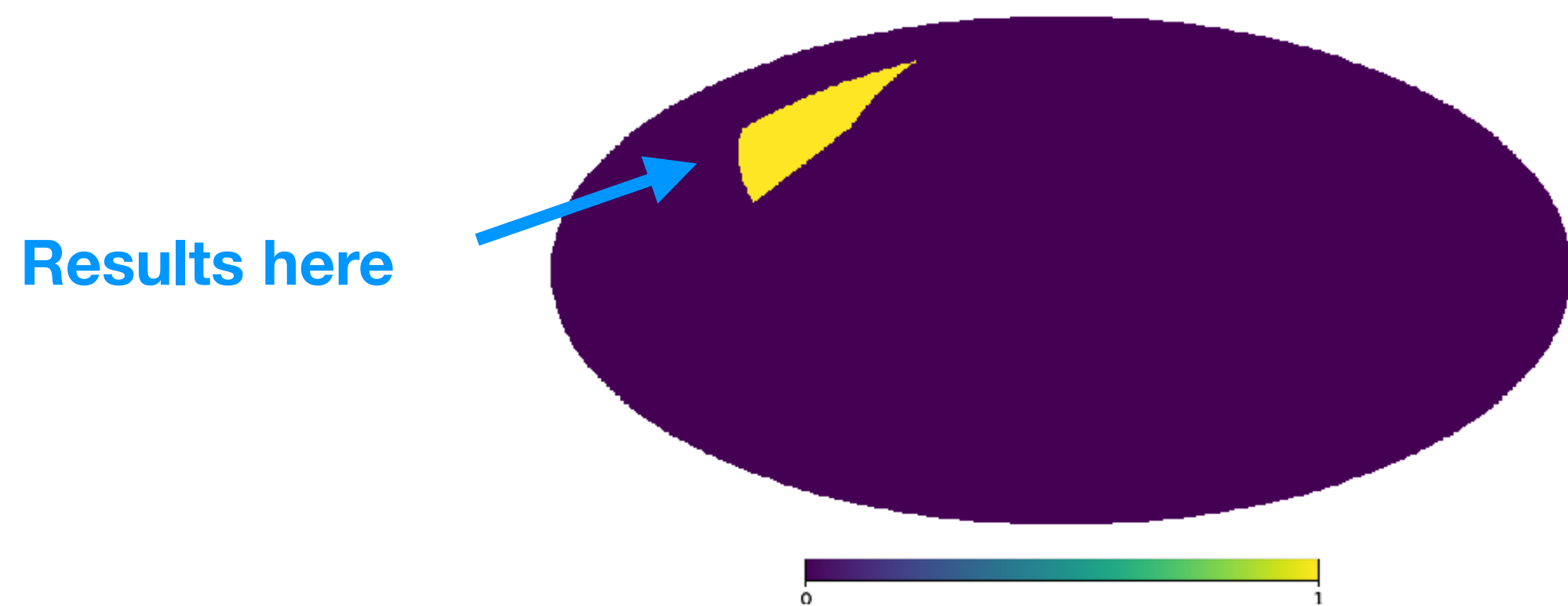
Healpix maps from WebSky numerical simulations (Stein et al., 2020):

- 90, 100, 143, 145, 217, 225, 280, 353, 545 GHz (Planck and SO)
- Healpix nside=4096
- CMB, CIB (all dust IR emission including point sources), SZ
- No noise, no beams
- 100,000 patches of 64x64 pixels ( $0.8^\circ \times 0.8^\circ$ )

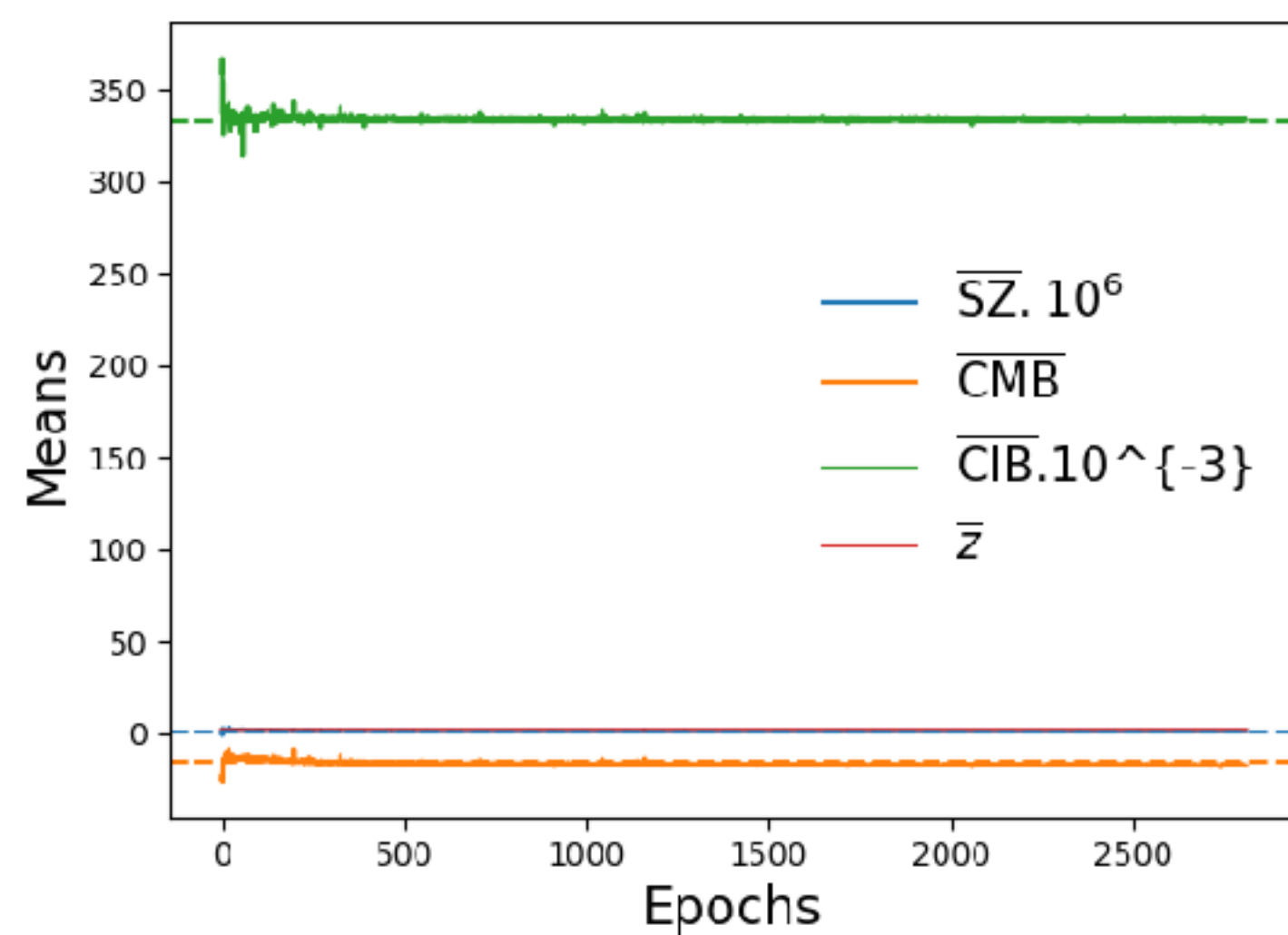




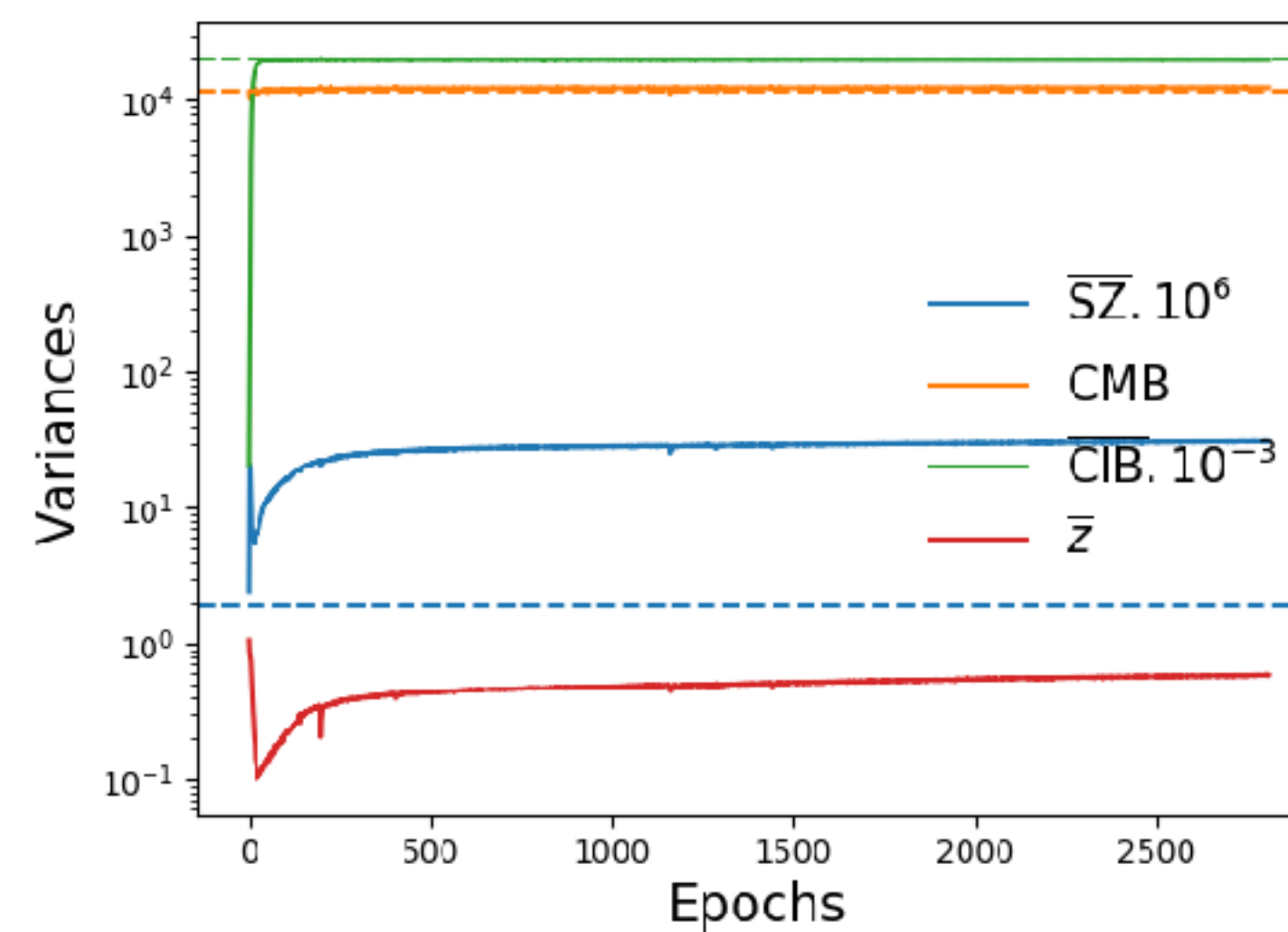
# An application to CMB data - CIB removal - SZ extraction



Means:



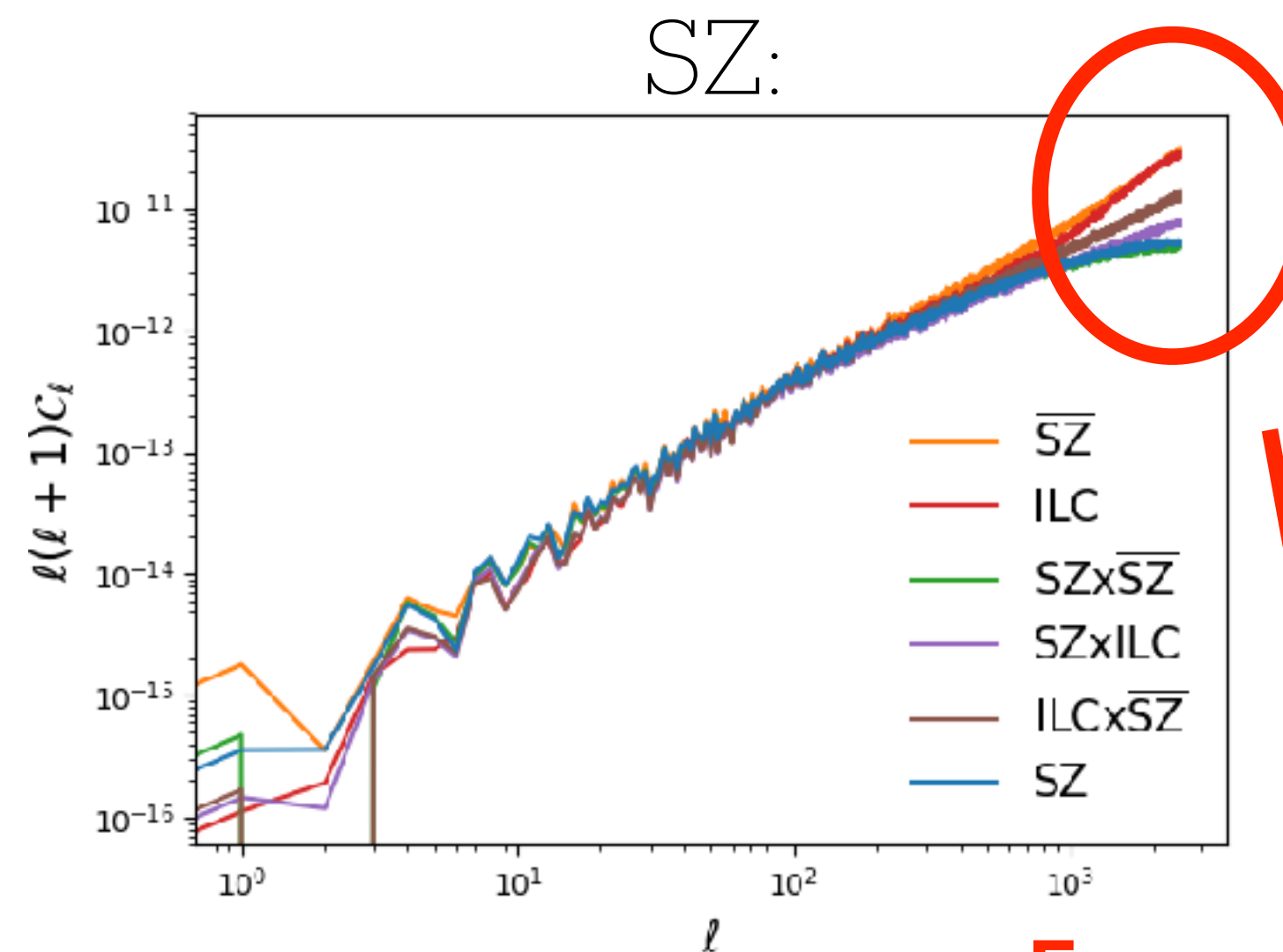
Variances:



# An application to CMB data - CIB removal - SZ extraction

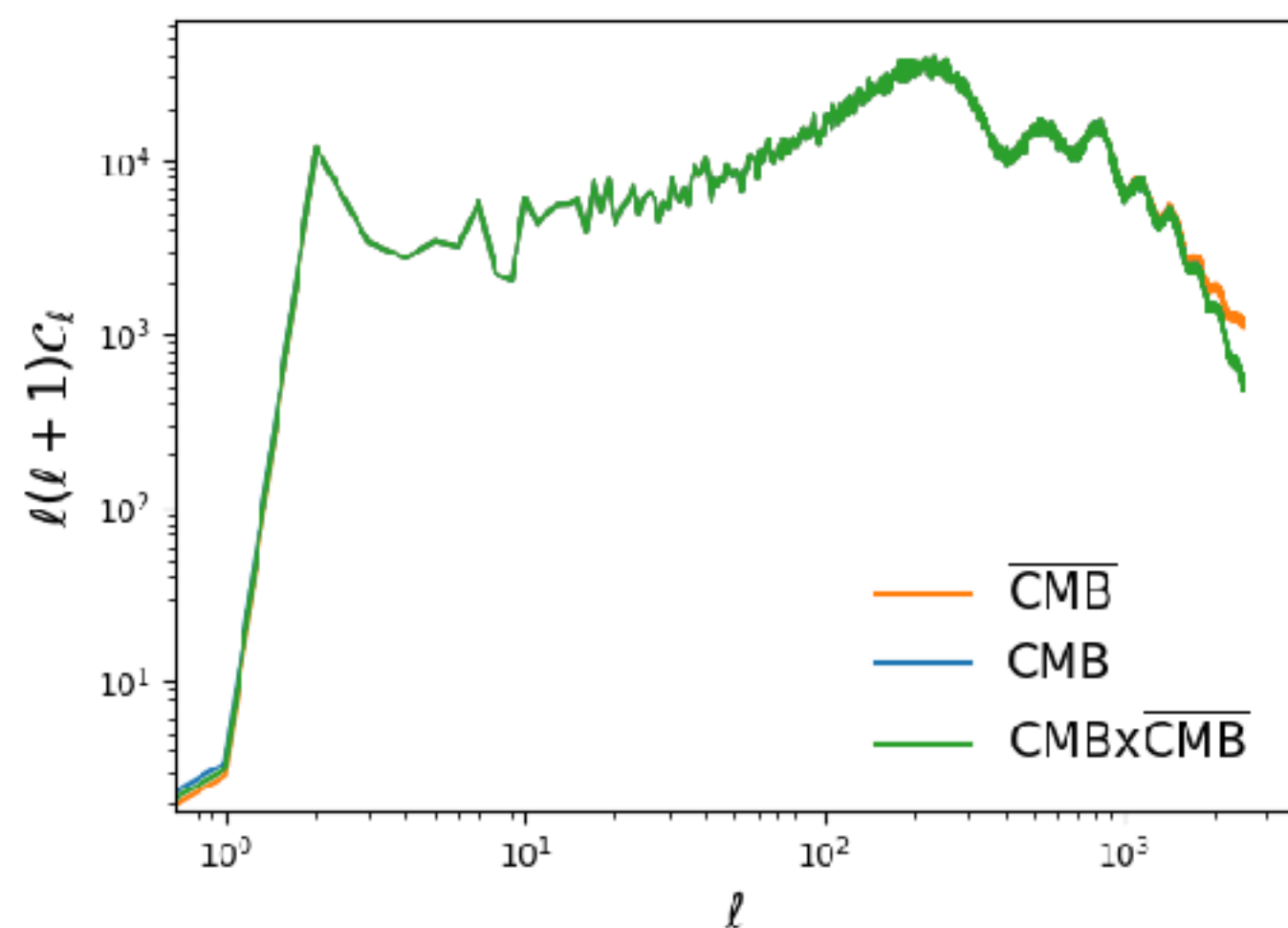
Power-spectra:

Comparison with MILCA  
applied on very same maps

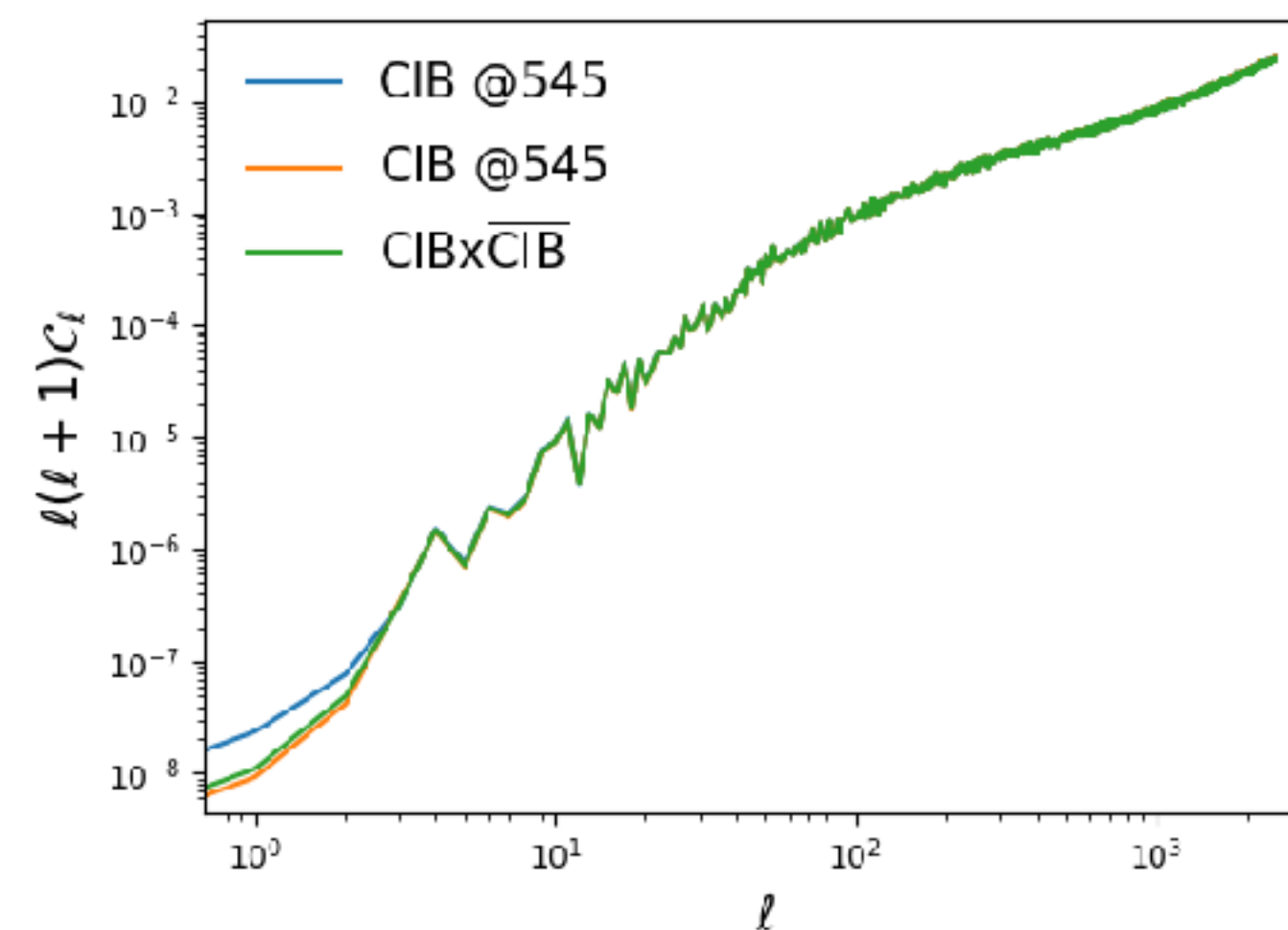


**Excess of signal in  
SZxMILCA**

CMB:



CIB:



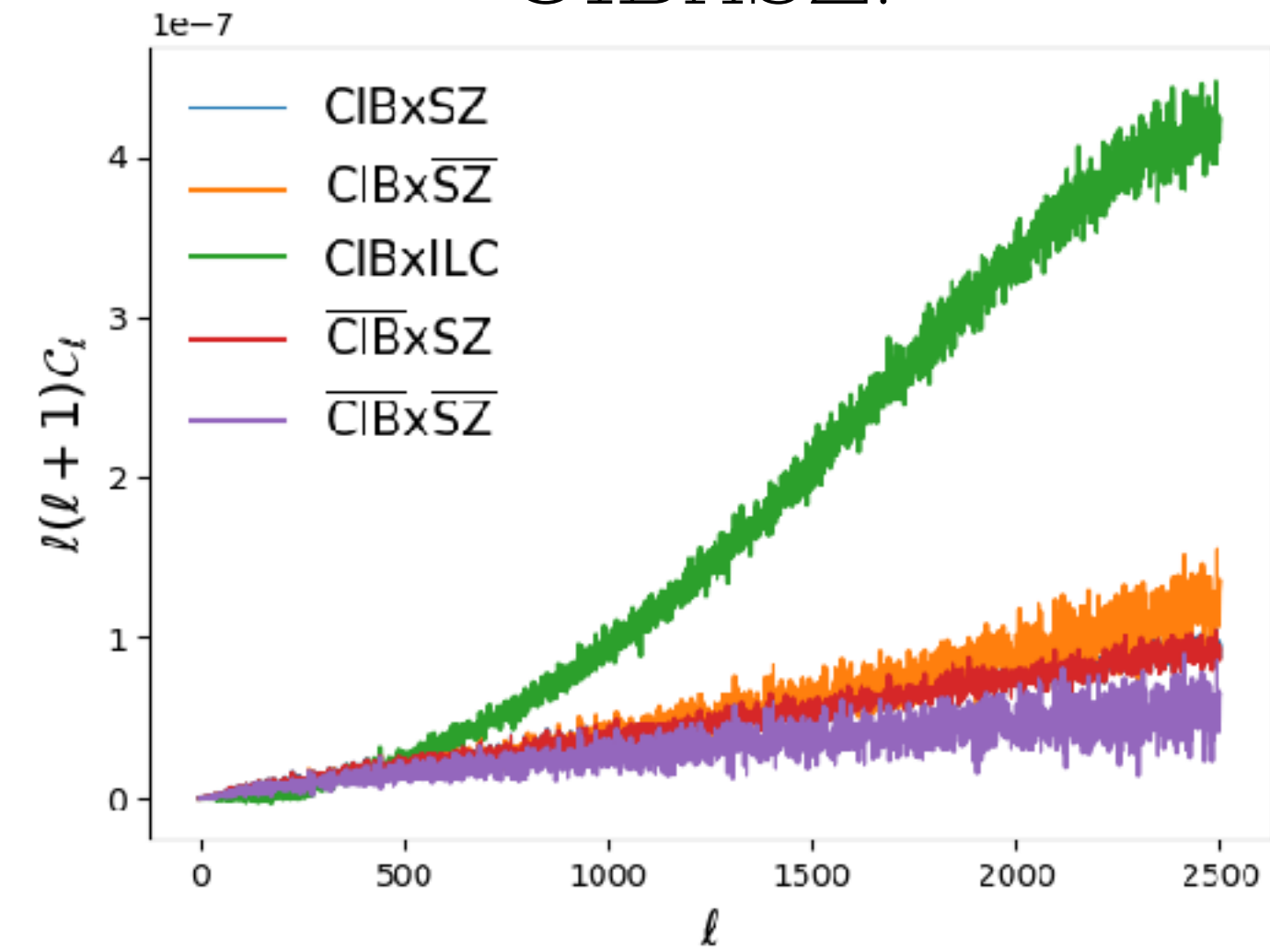


# An application to CMB data - CIB removal - SZ extraction

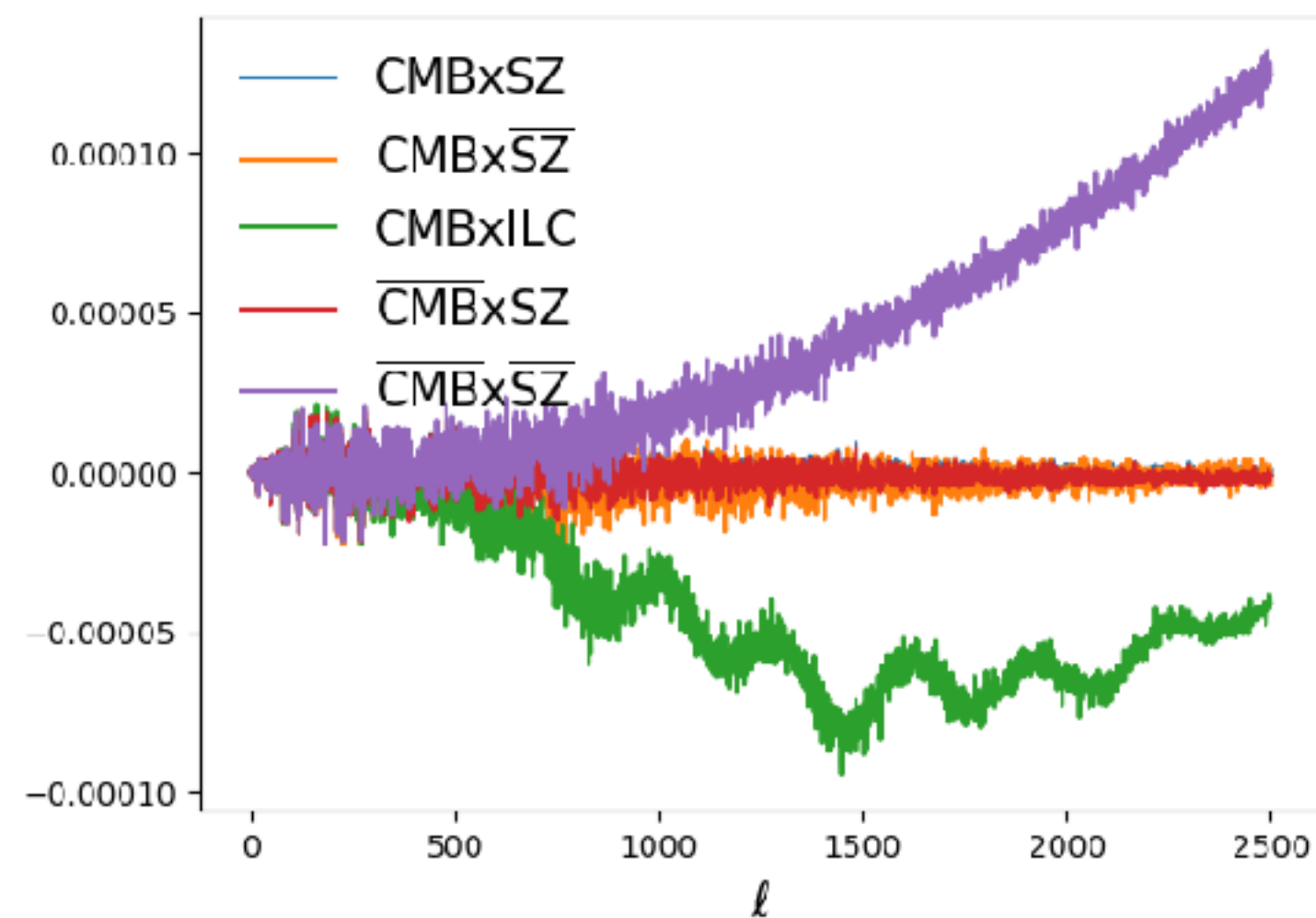
Cross-spectra:

**SZ map less contaminated  
by other components**

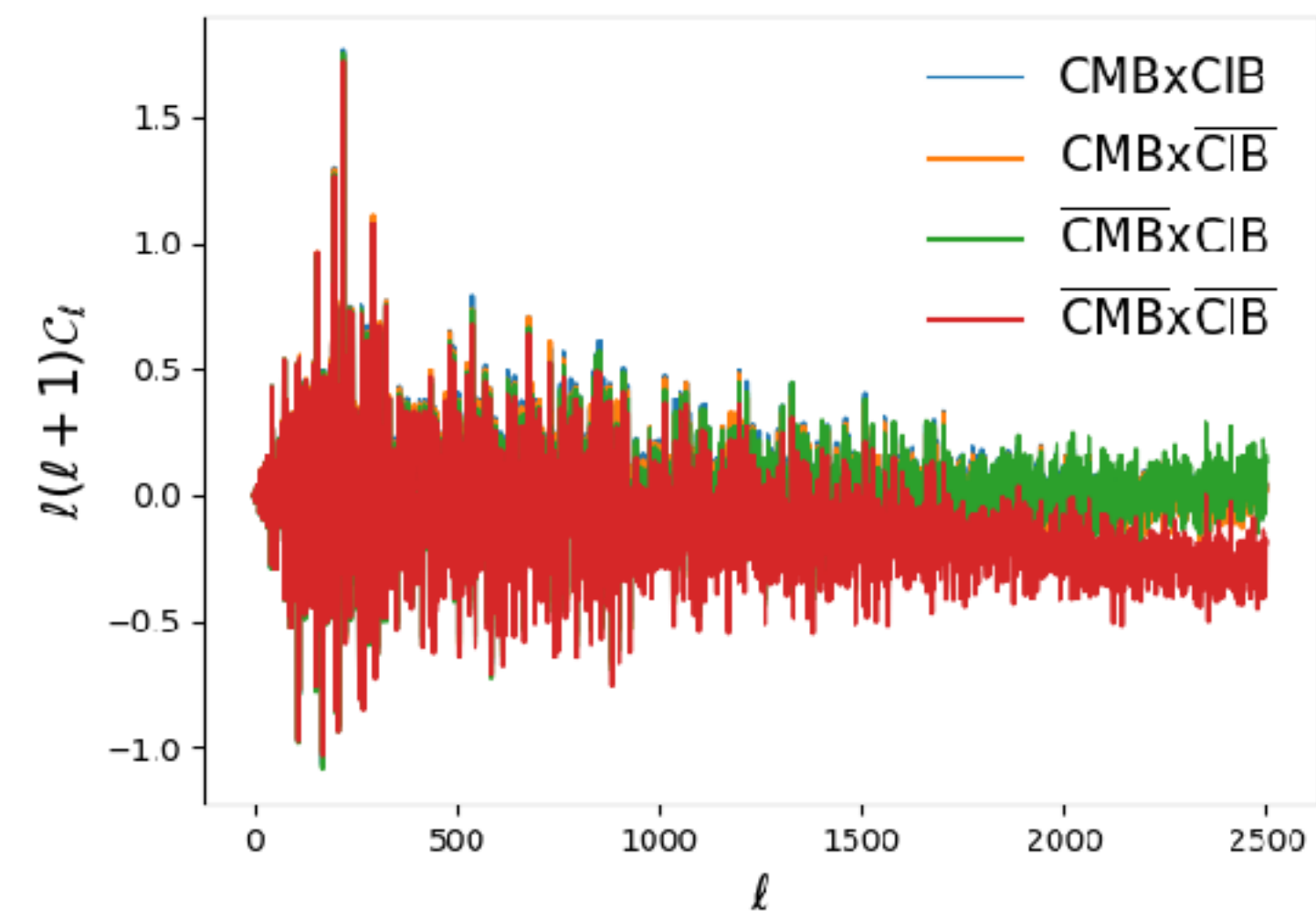
CIBxSZ:



CMBxSZ:

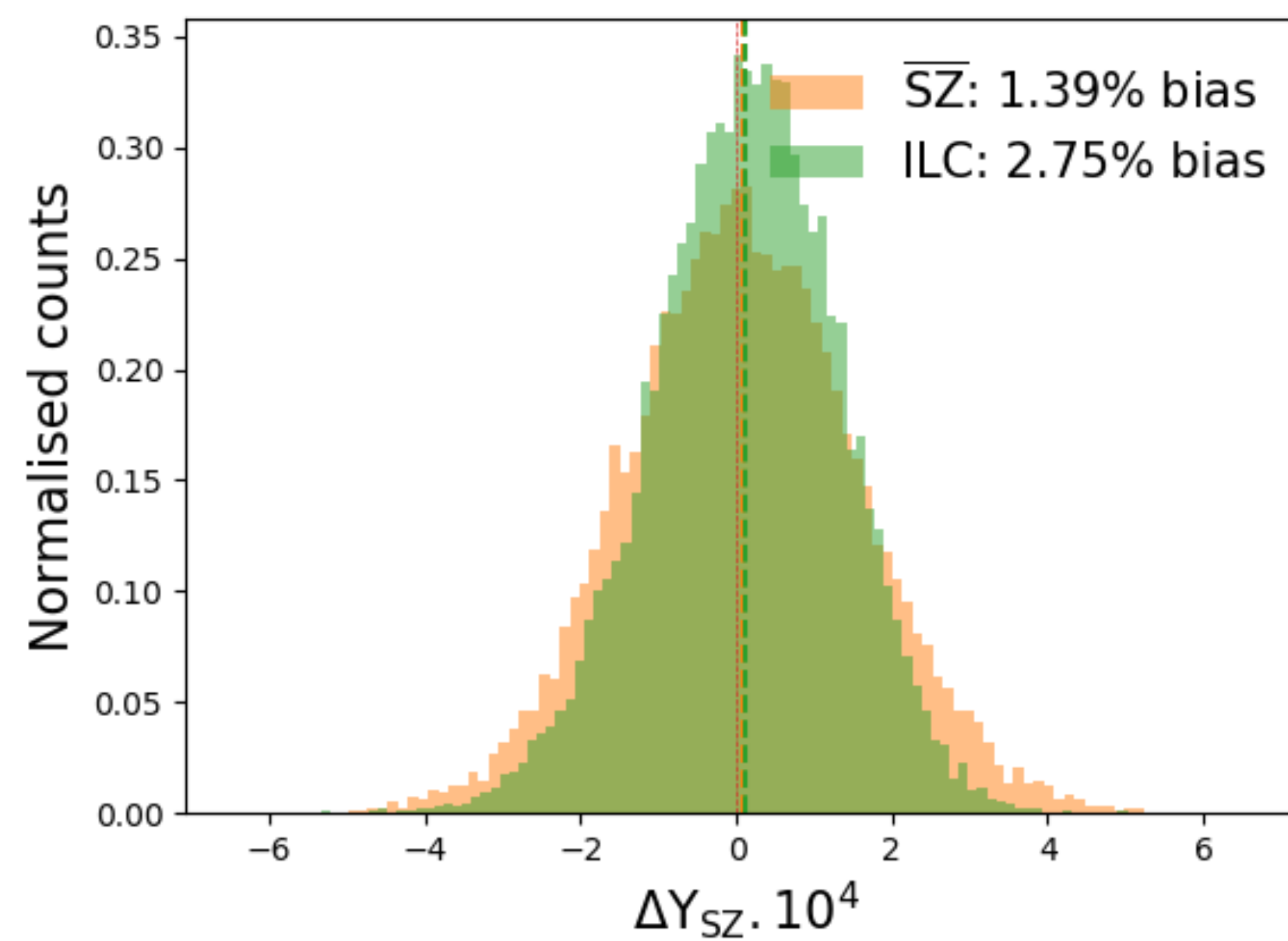
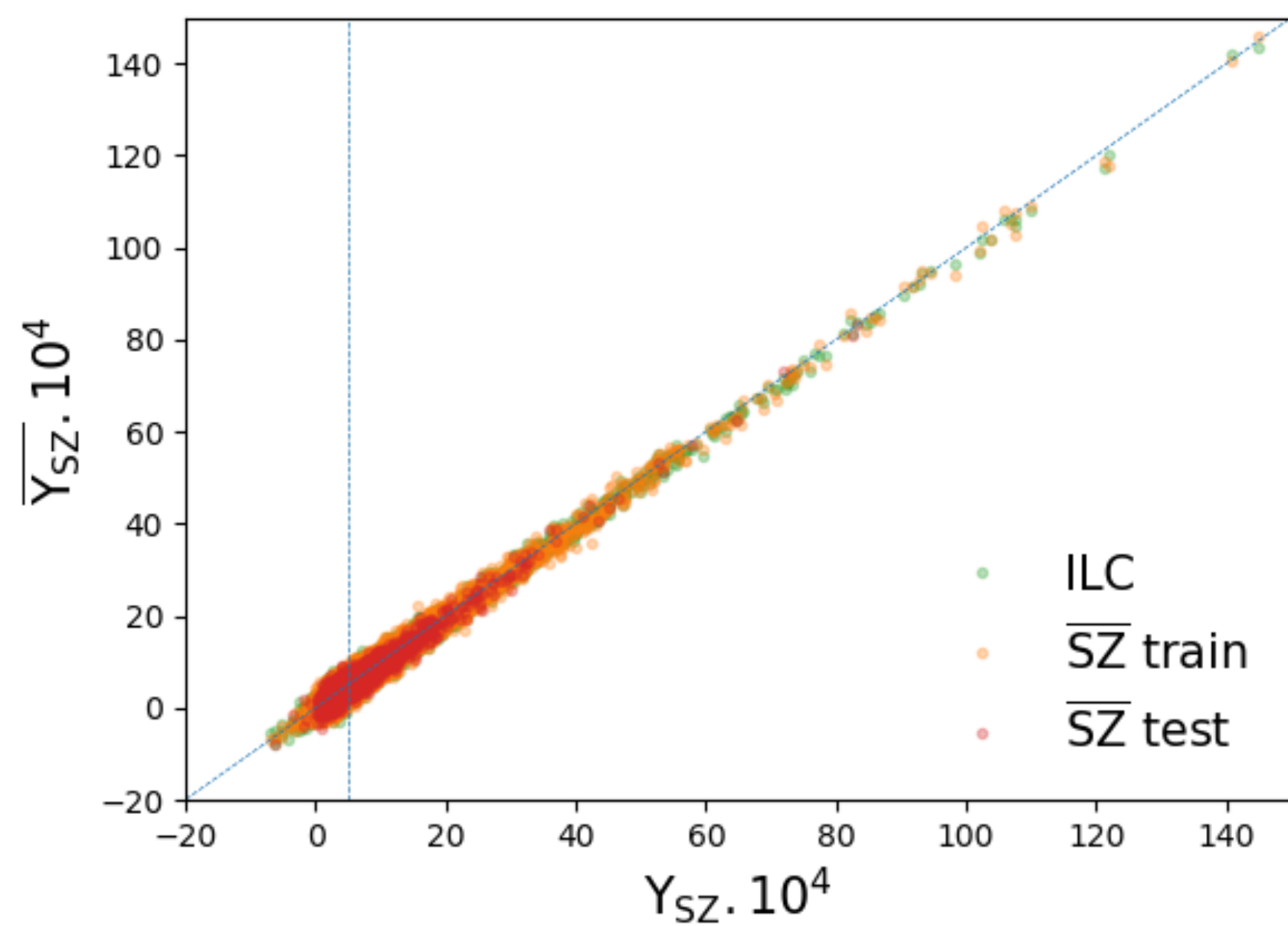


CMBxCIB:



# An application to CMB data - CIB removal - SZ extraction

Focus on SZ fluxes around clusters:



# Future applications

- CIB removal for CO/CII studies (Sia's talk)
- Single Channel Mixture for CO/CII separation?
- Foreground removal in radio (SKA) for HI and/or EoR?