

# Characterization of the de-excitation path of fission fragments during the spontaneous fission of $^{252}\text{Cf}$

## N-SI-125 data analysis status

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<sup>a</sup> - Université Paris-Saclay, CNRS/IN2P3, IJC Laboratory, Orsay, France

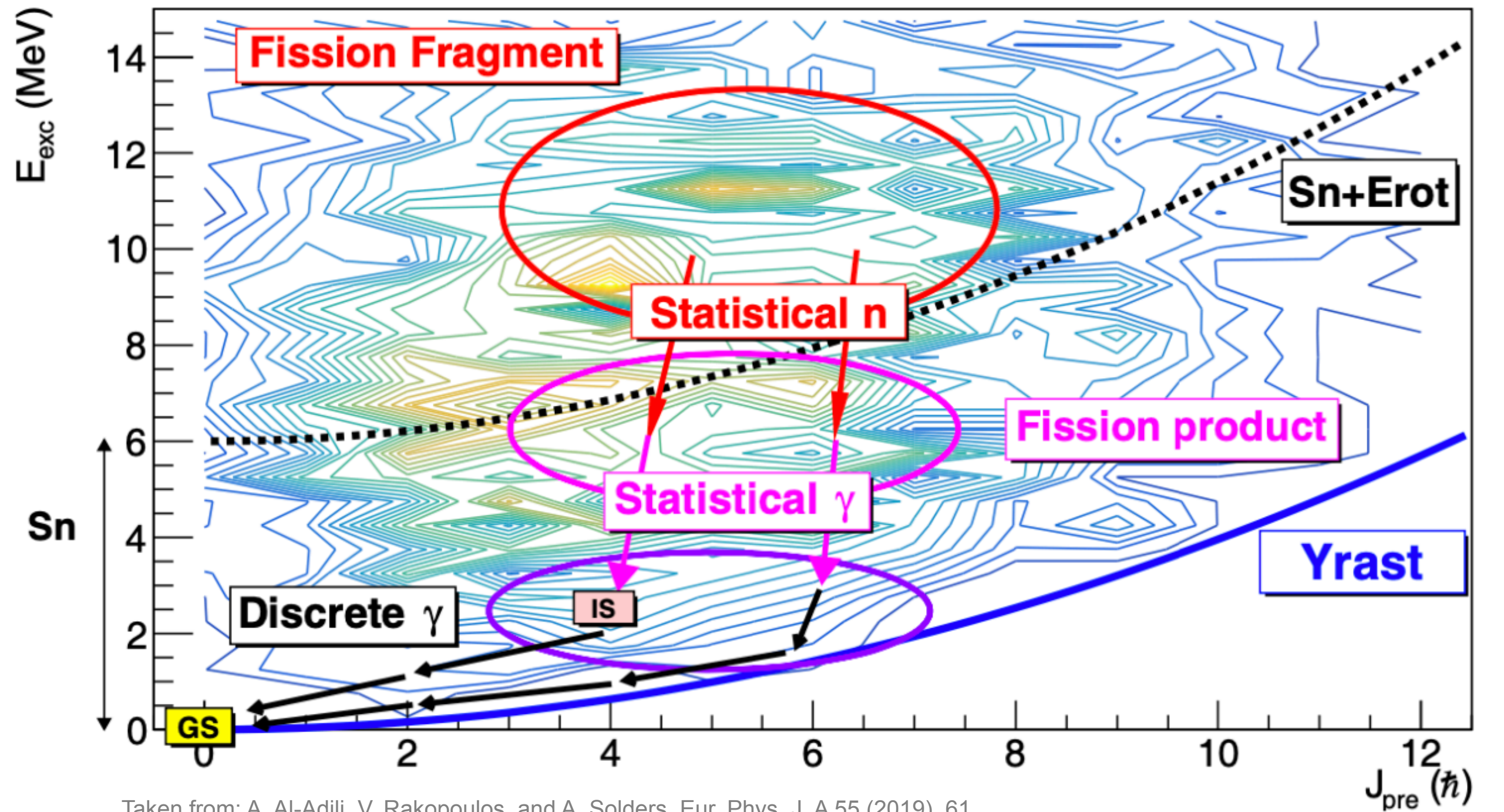
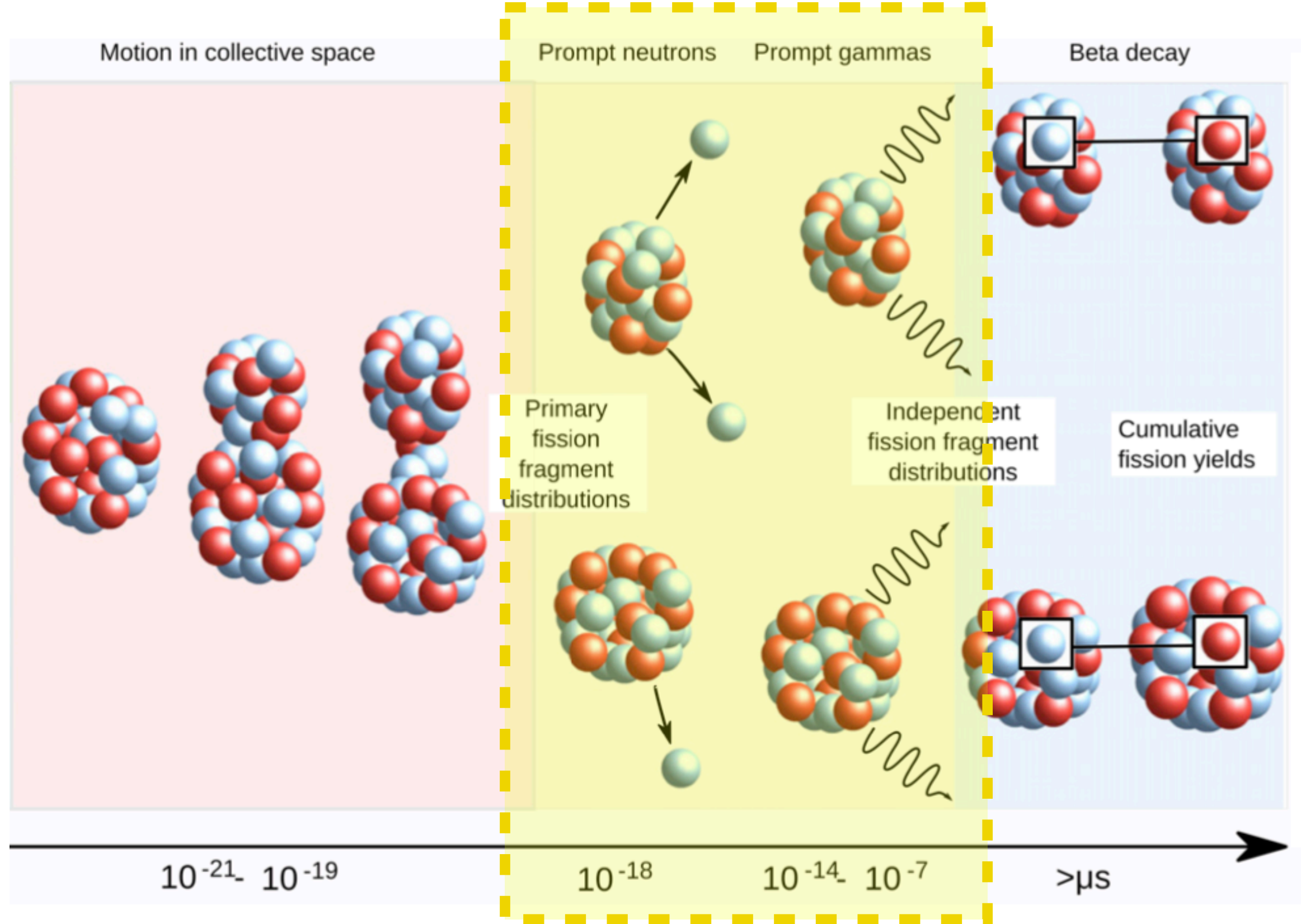
<sup>b</sup> - European Commission, Belgium

<sup>c</sup> - Atomic Energy Commission (CEA), France



# Physics motivation for the FRØZEN project

## FRØZEN

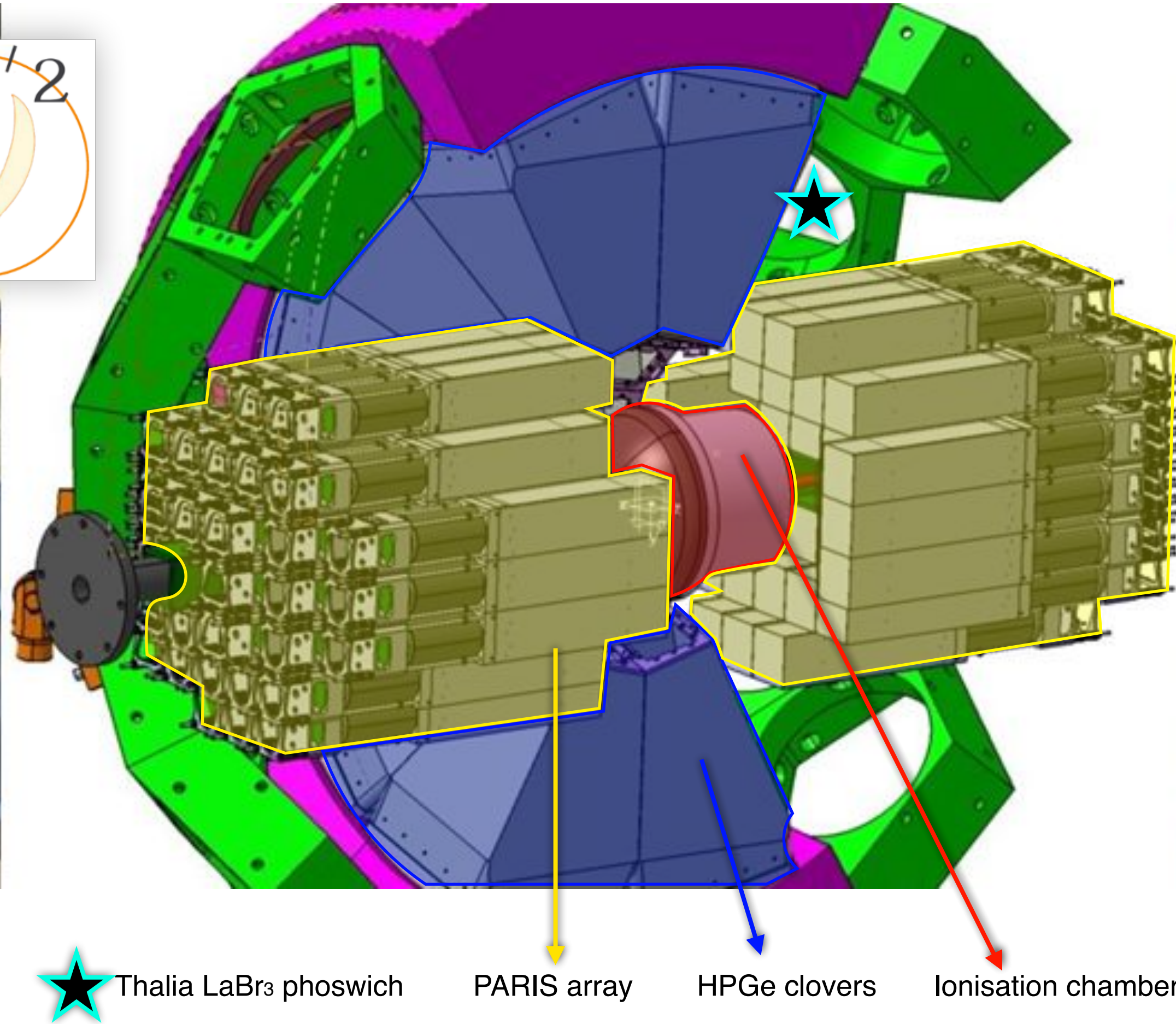
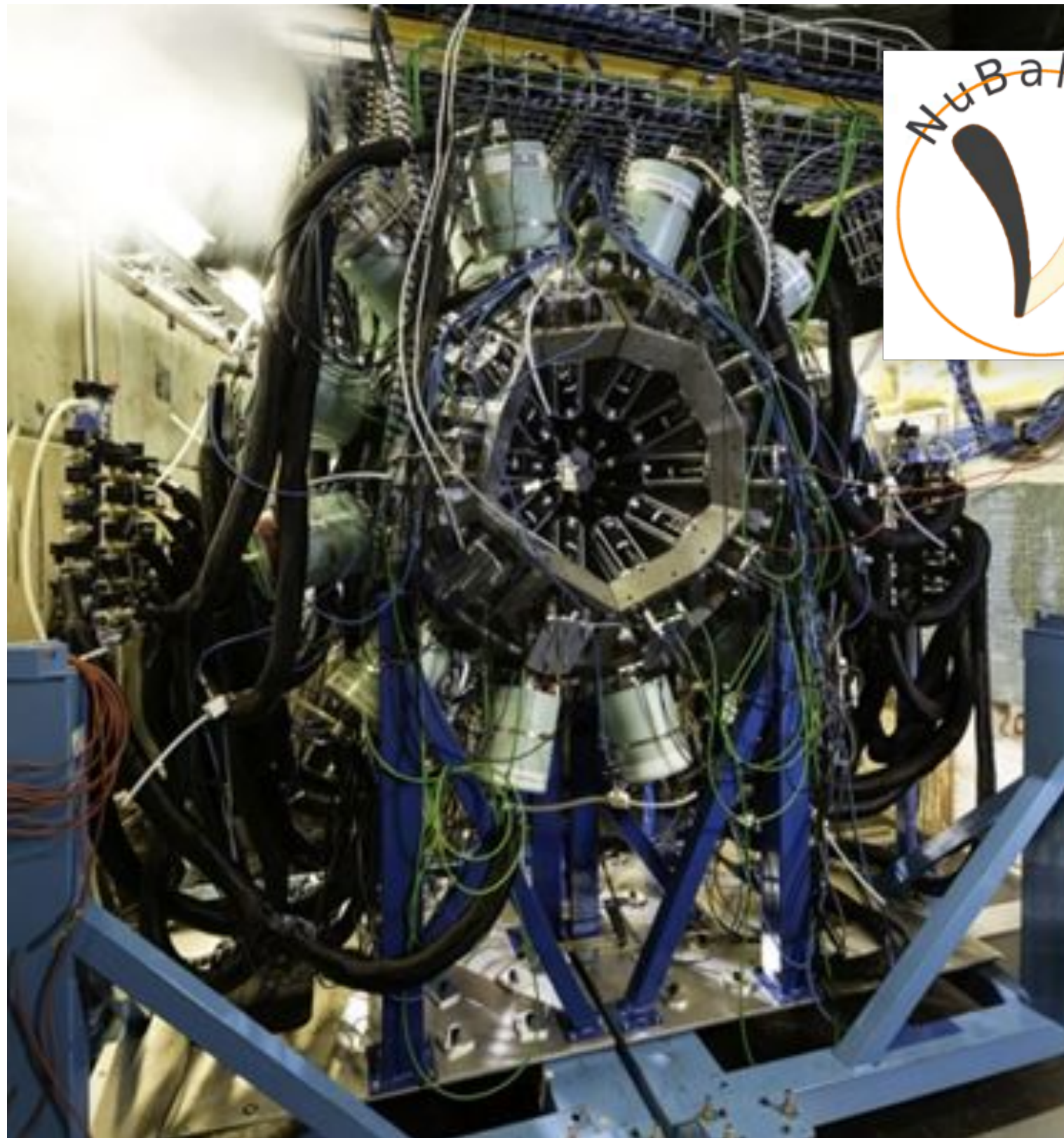


Taken from: A. Al-Adili, V. Rakopoulos, and A. Solders, Eur. Phys. J. A 55 (2019), 61.

Adapted from: M. Bender, *et al.* Future of nuclear fission theory. Journal of Physics G: Nuclear and Particle Physics, 47(11):113002, oct 2020.



# The N-SI-125 experiment setup



## Gamma detection energy and multiplicity

24 High-Purity Germanium clovers (HPGe)

PARIS array  
72 phoswiches  $\text{La}(\text{Ce})\text{Br}_3:\text{NaI}$

Thalia  $\text{LaBr}_3$

## Neutron detection energy and multiplicity

PARIS array

Thalia  $\text{LaBr}_3$

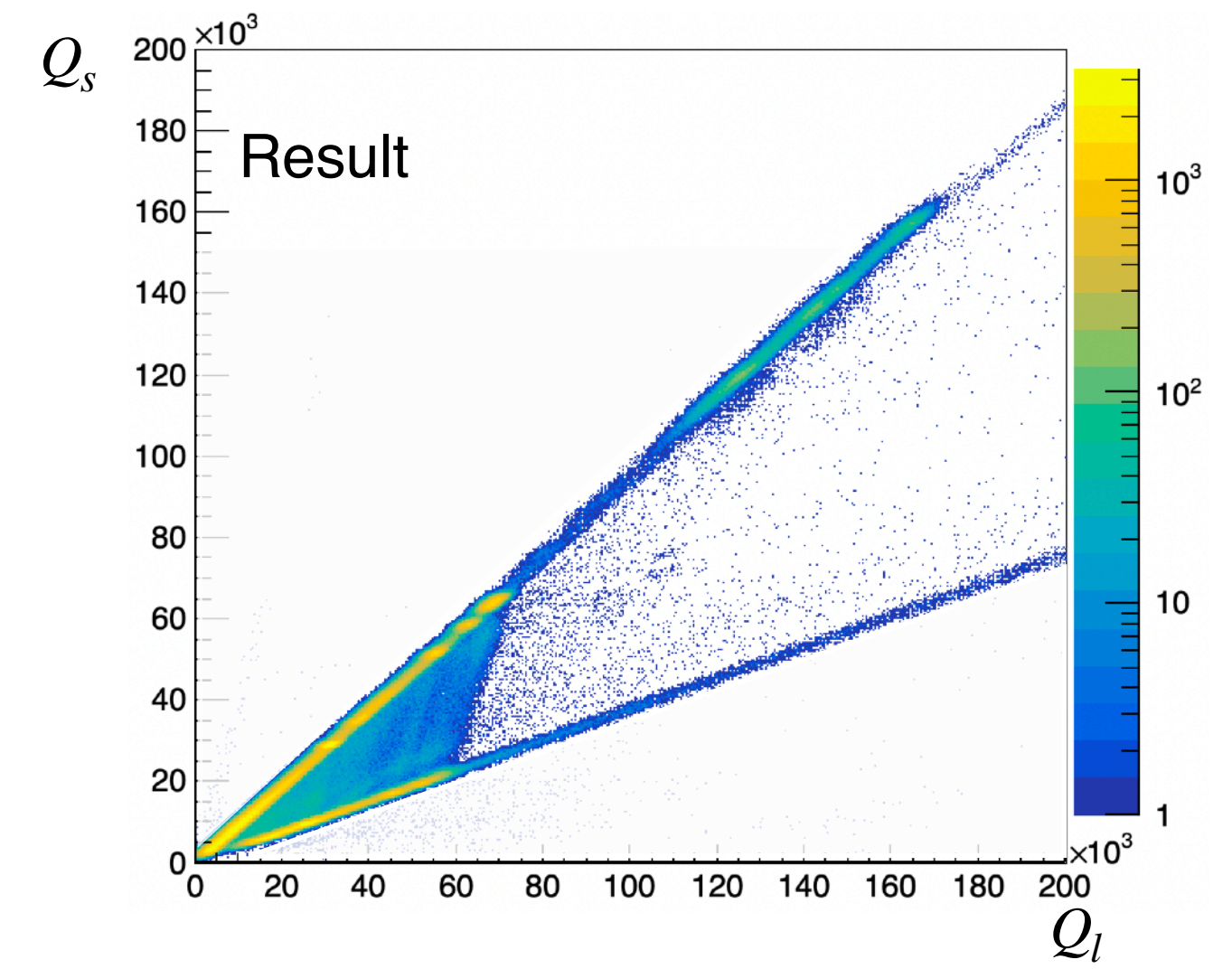
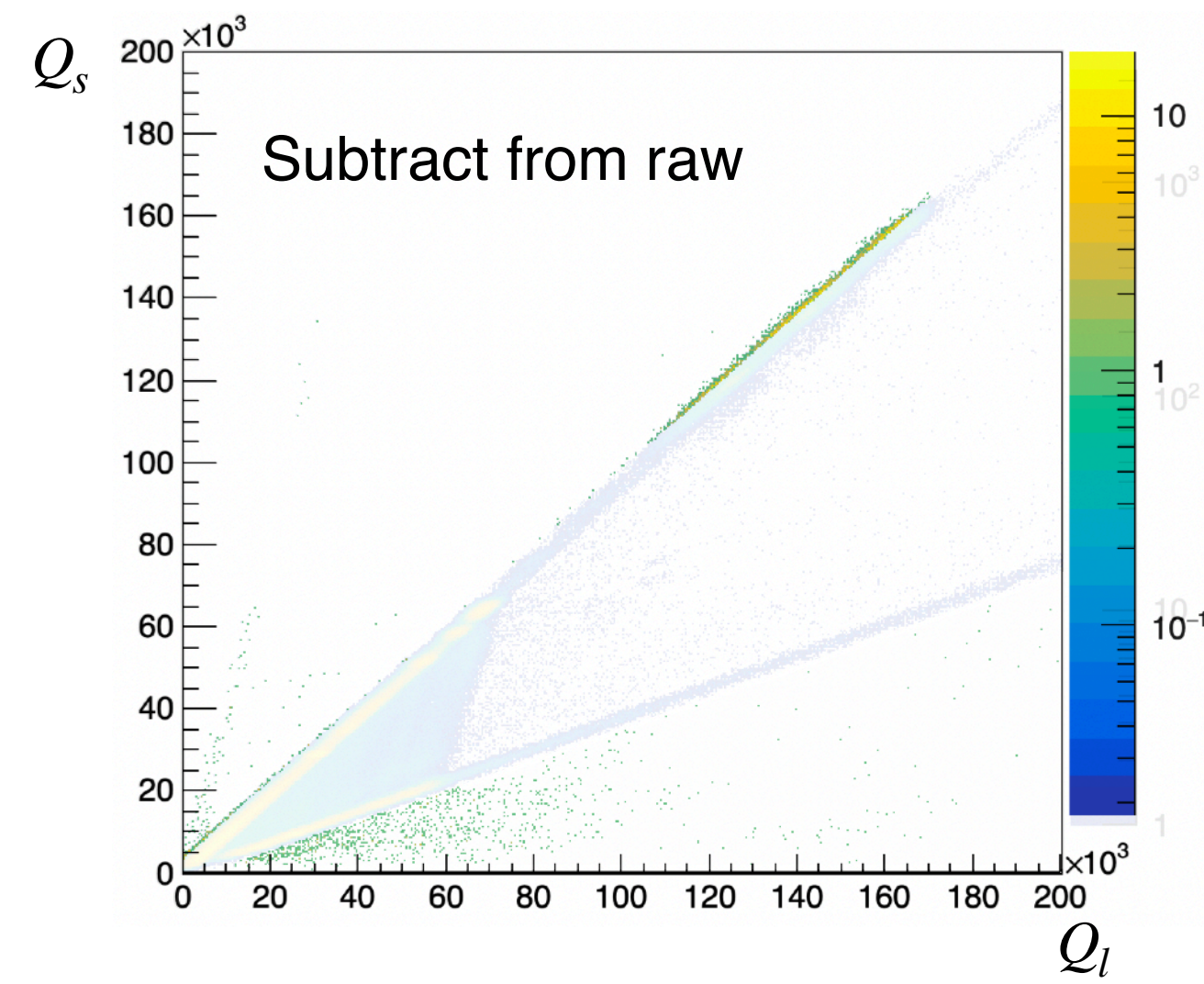
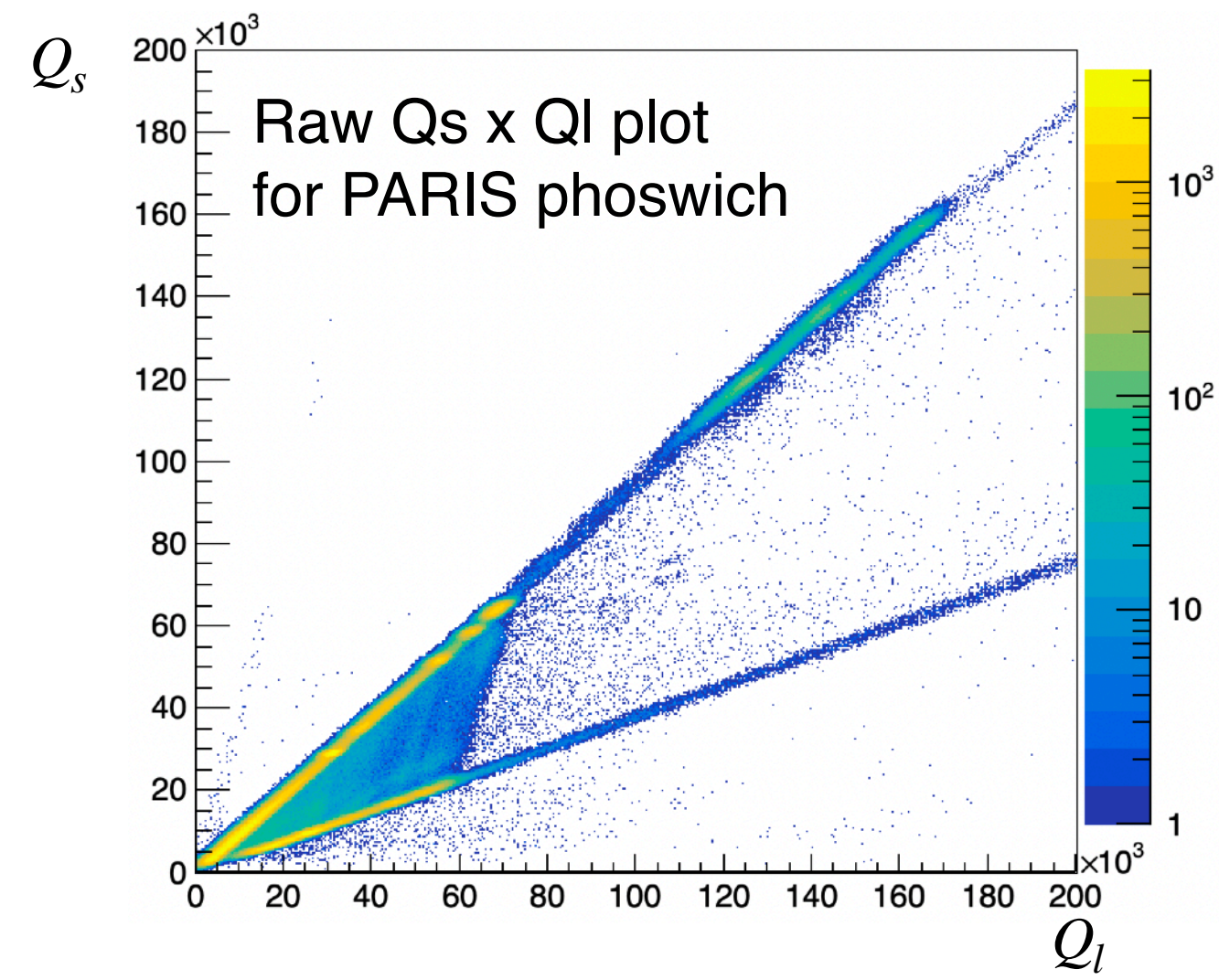
## Fission fragments detection

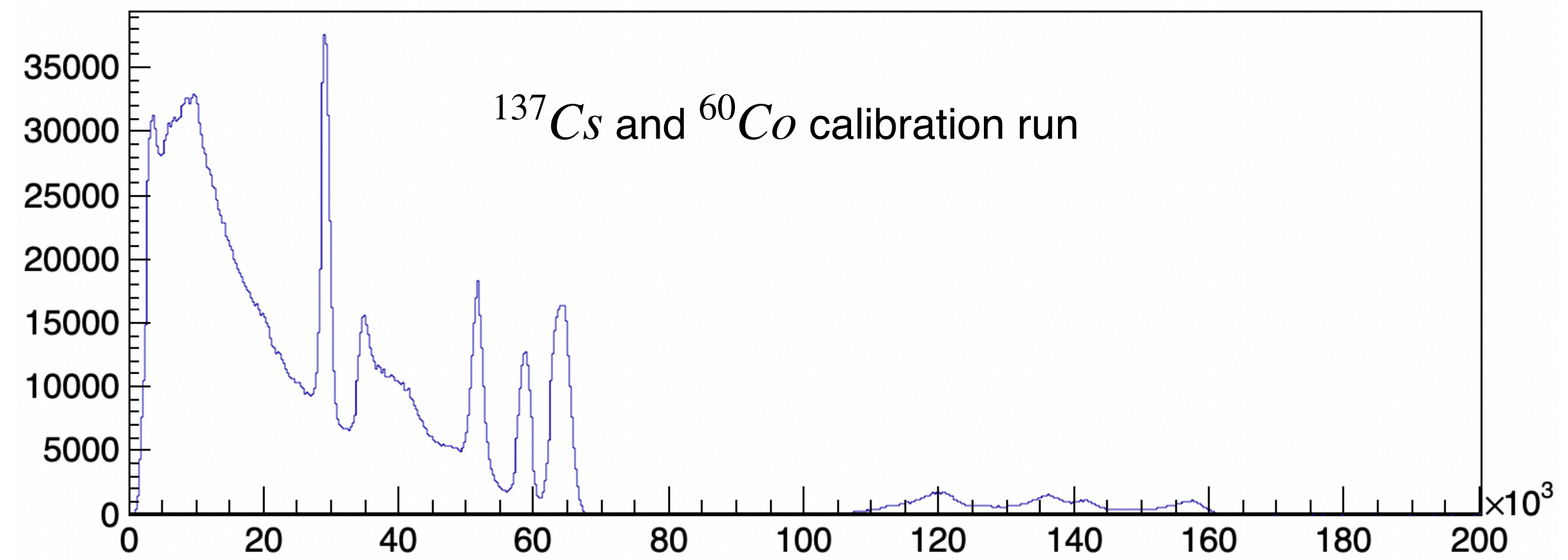
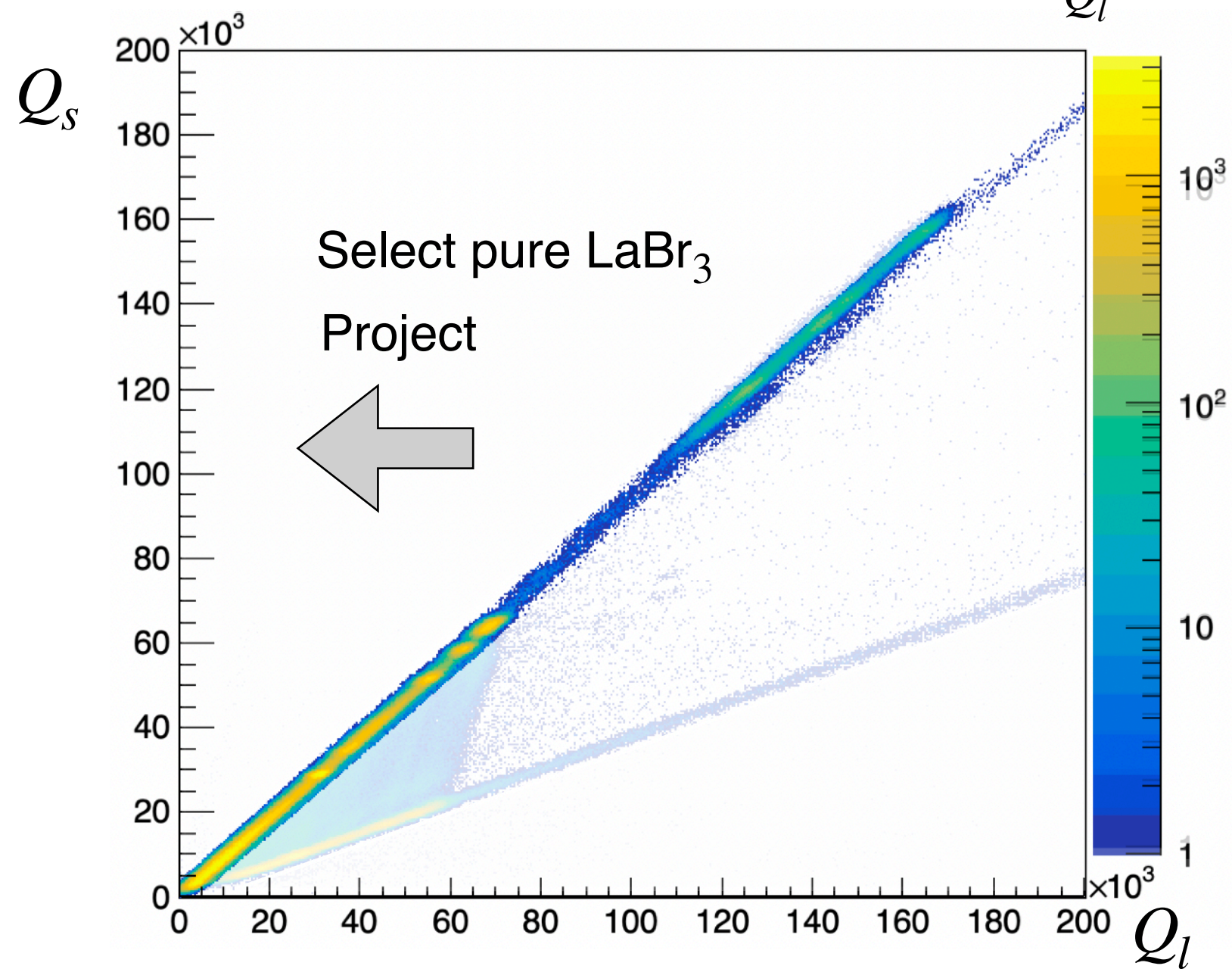
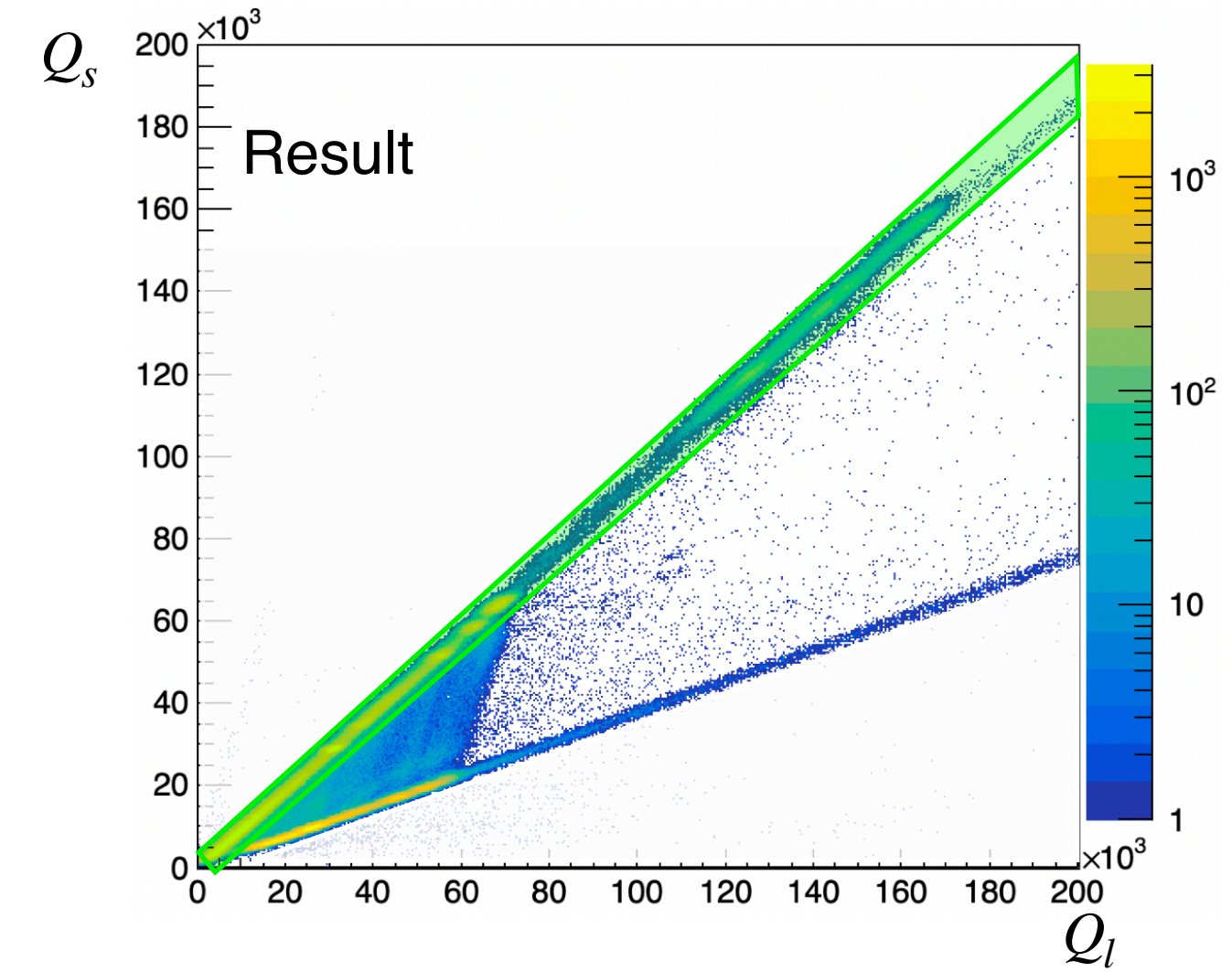
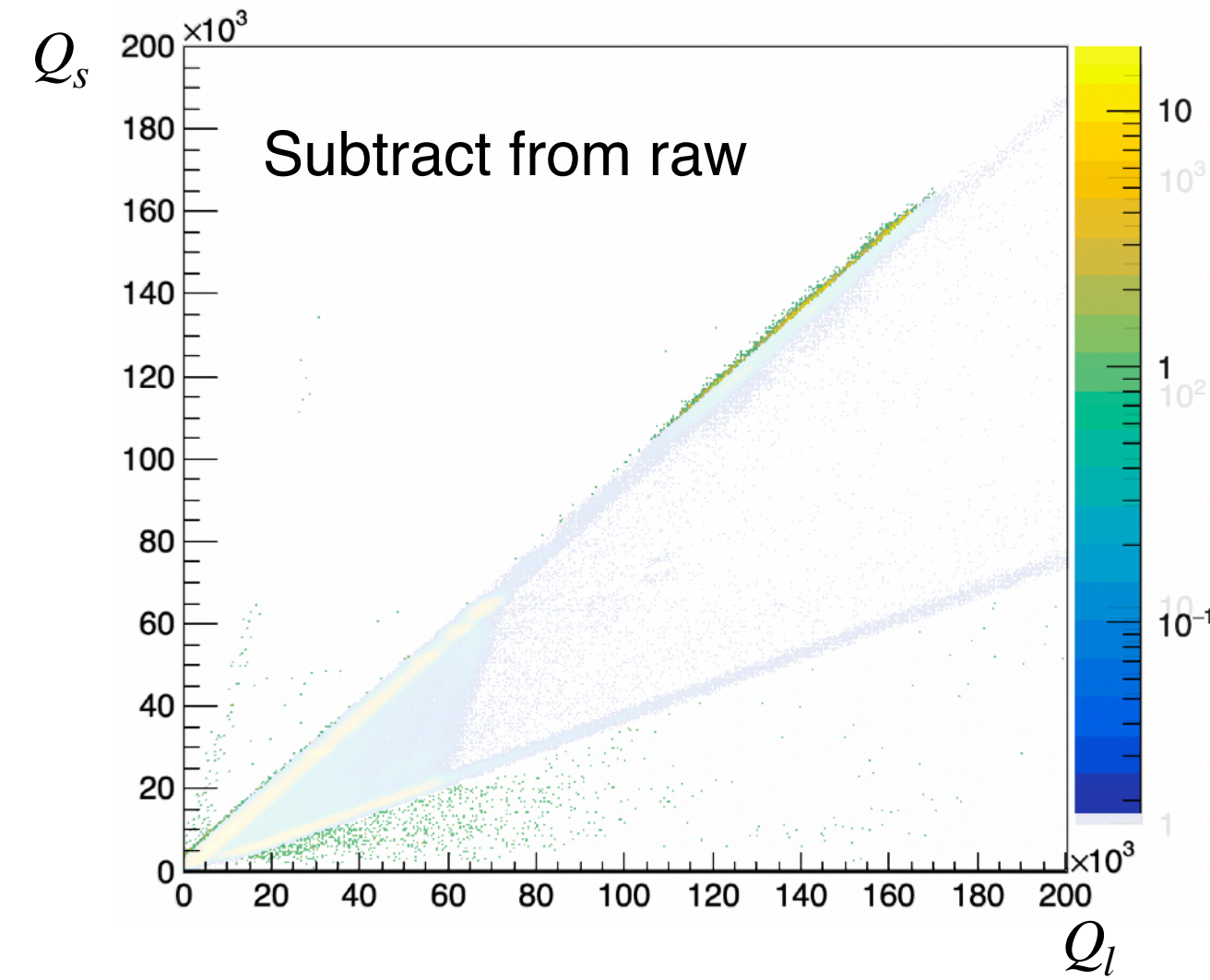
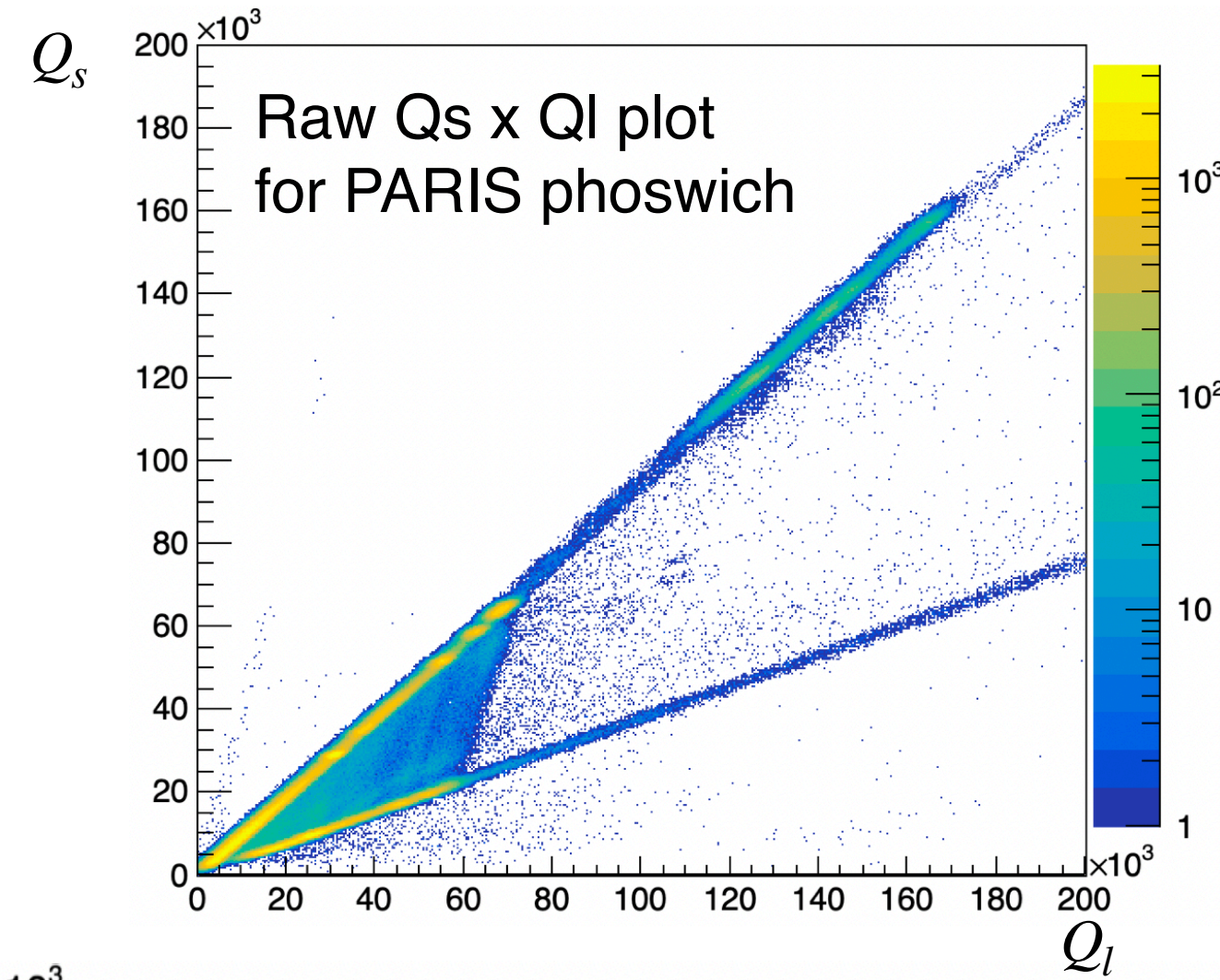
Ionisation chamber

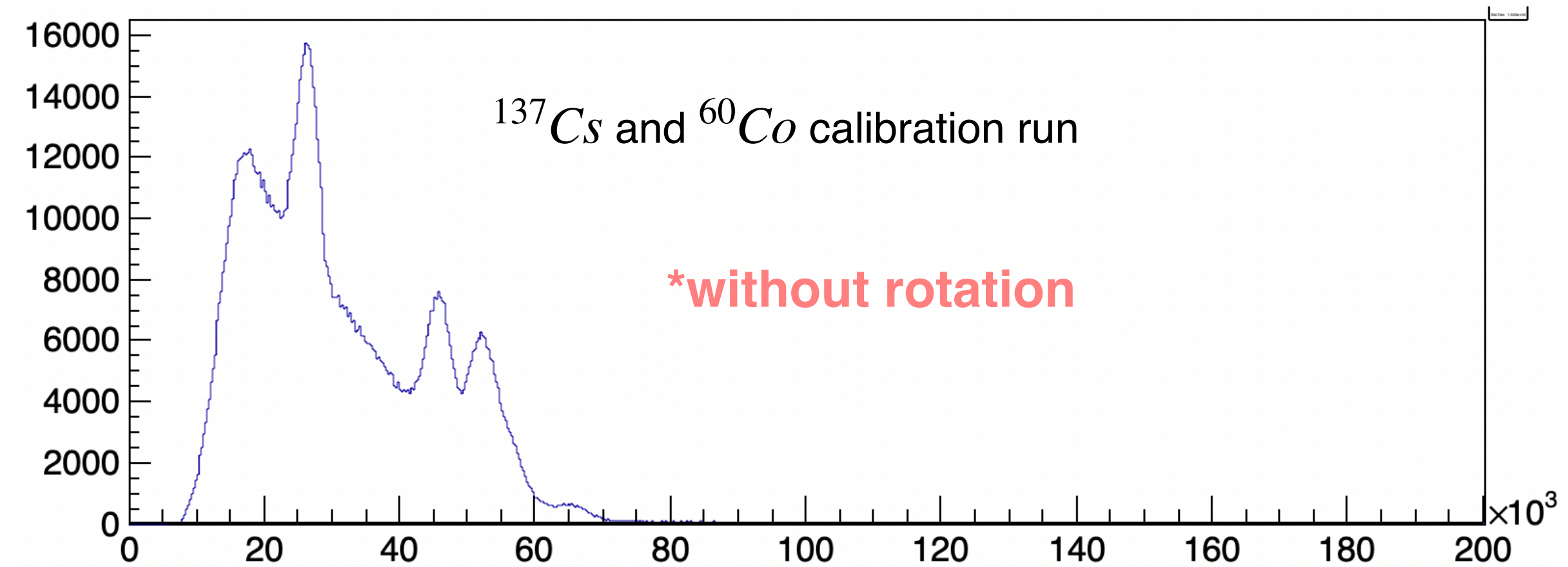
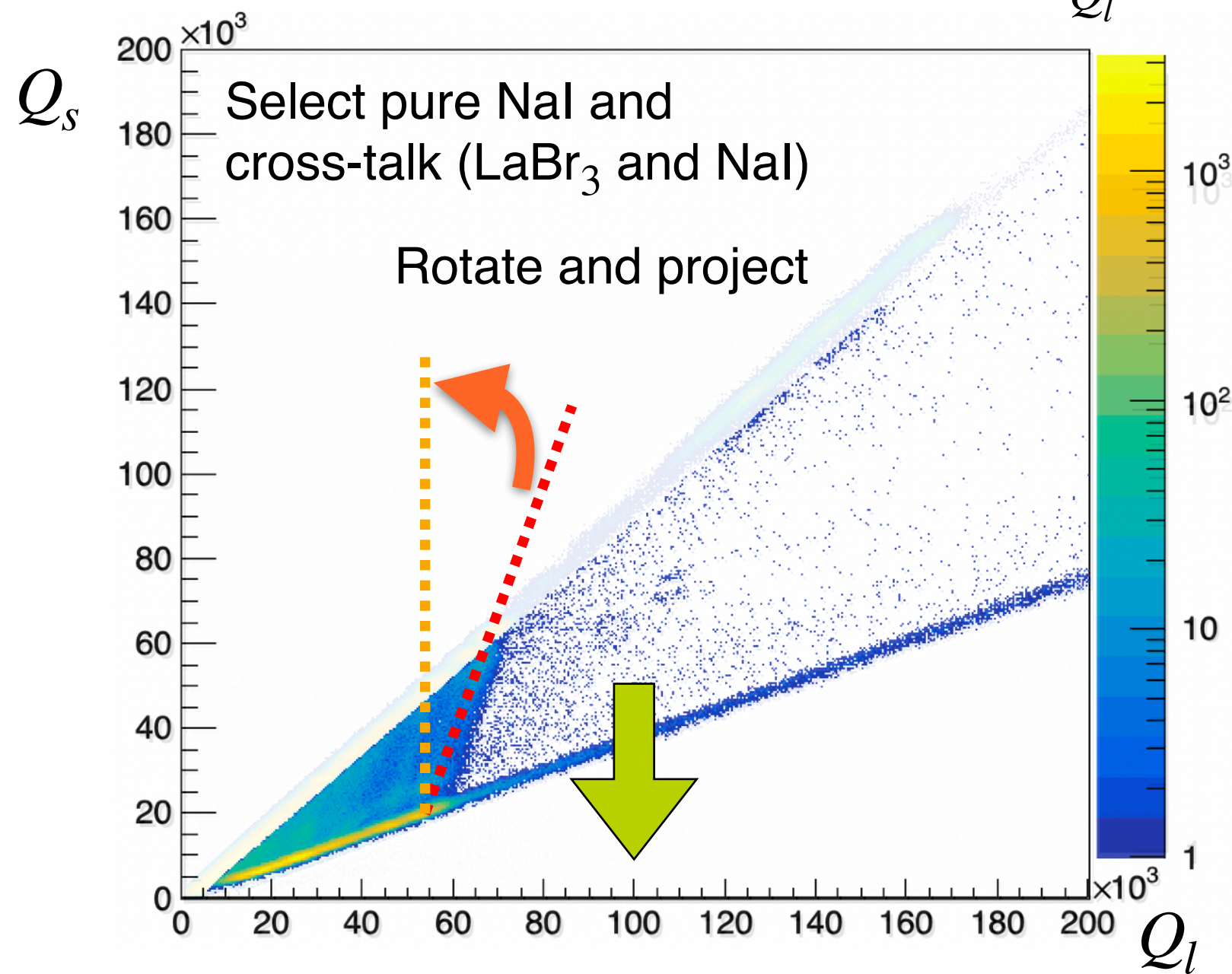
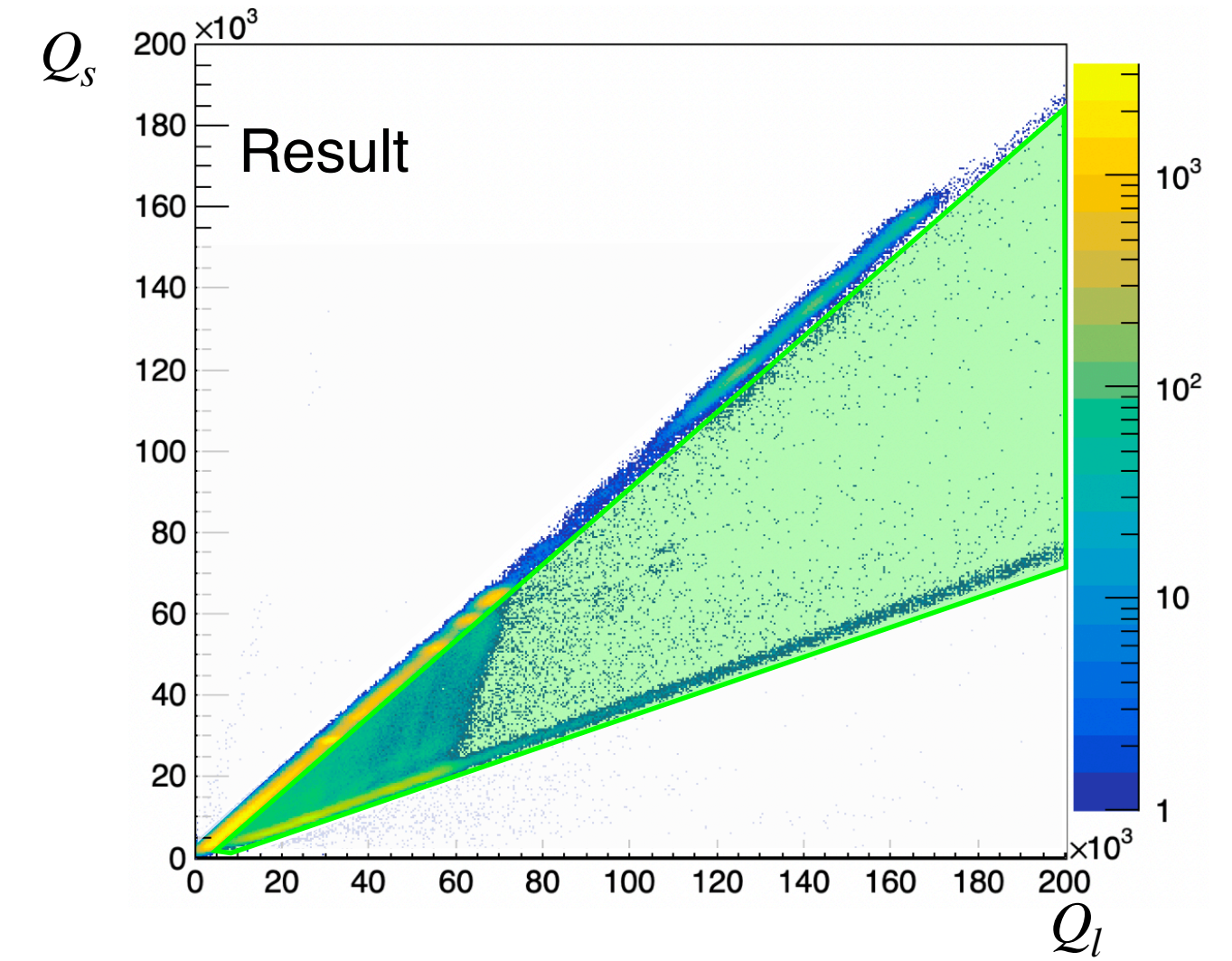
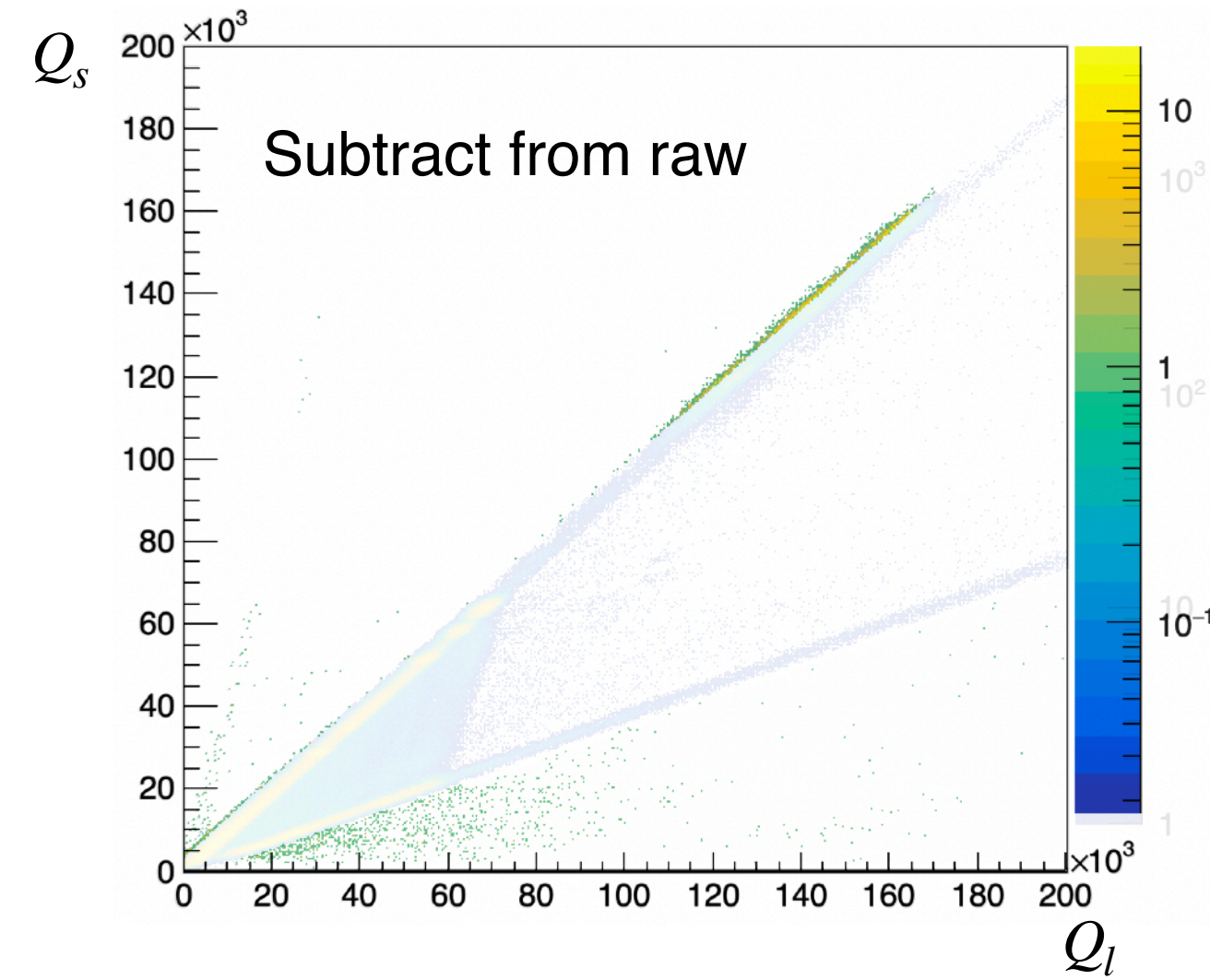
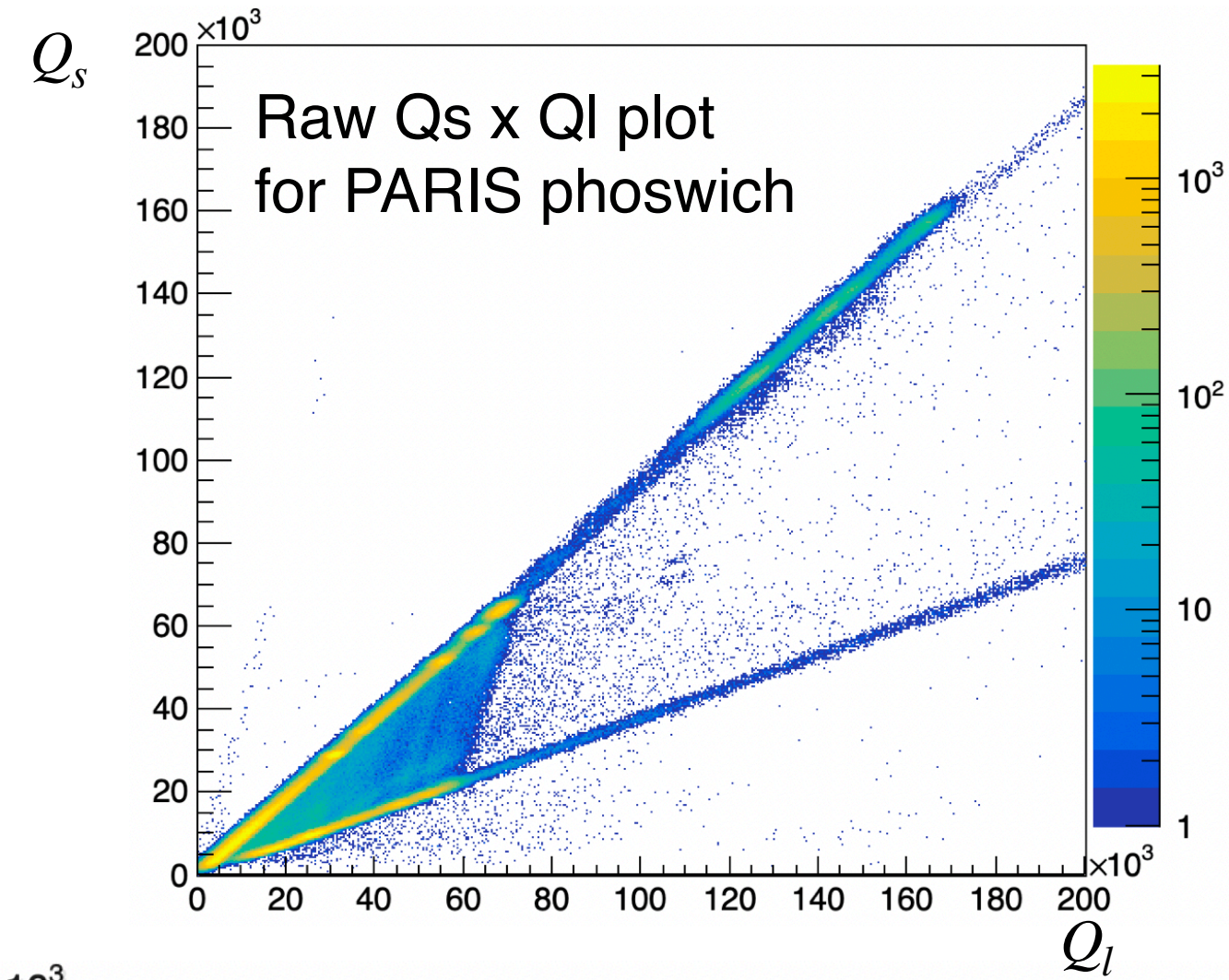
Taken from: <https://alto.ijclab.in2p3.fr/en/nu-ball2-online-scientific-workshop-2/>



★ Thalia  $\text{LaBr}_3$  phoswich    PARIS array    HPGe clovers    Ionisation chamber







## Calibration is ongoing...

24 HPGe clovers => 96 channels

PARIS array  
72 phoswiches La(Ce)Br<sub>3</sub>:NaI

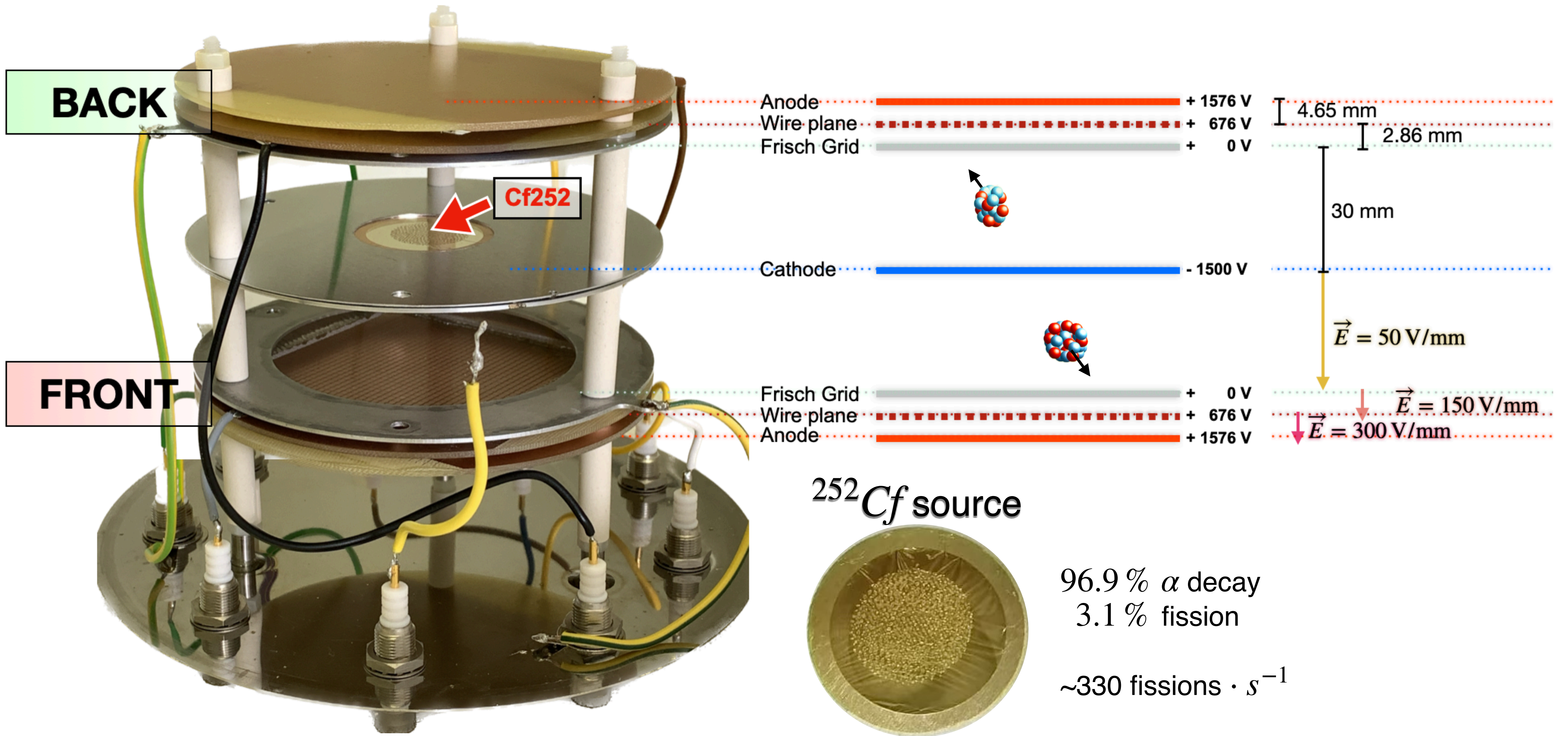


More than 200 channels

Calibration with  $^{152}\text{Eu}$ ,  $^{60}\text{Co}$ ,  $^{137}\text{Cs}$  and *AmBe*



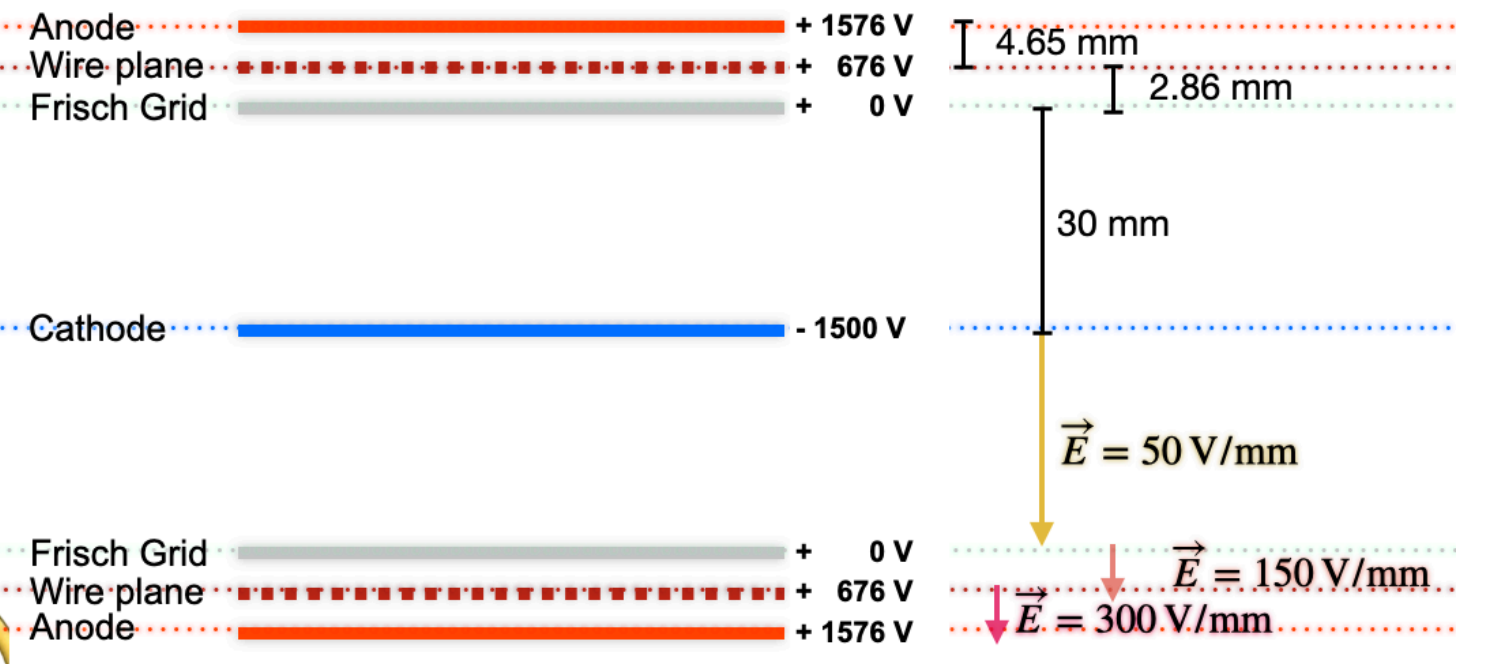
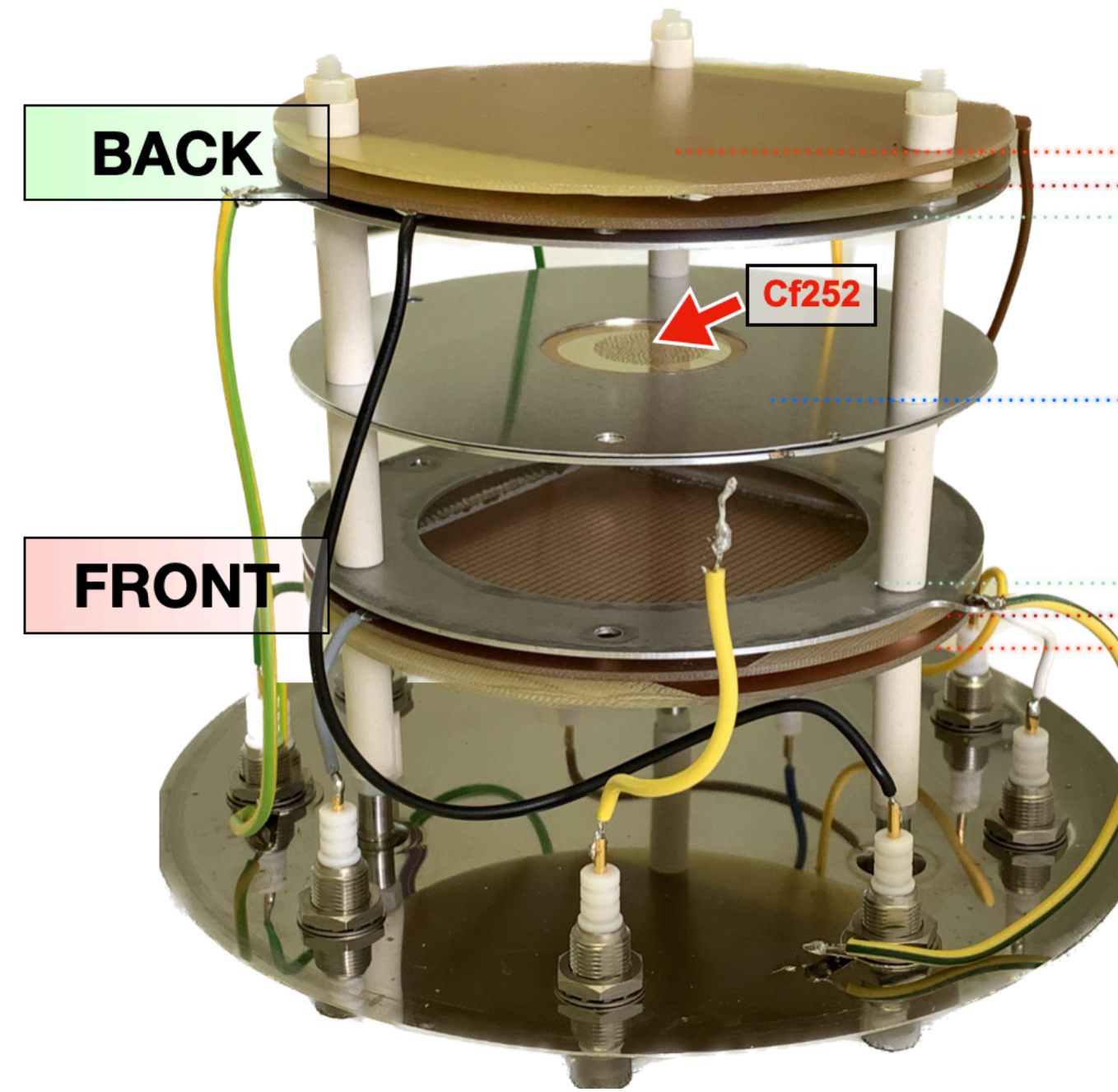
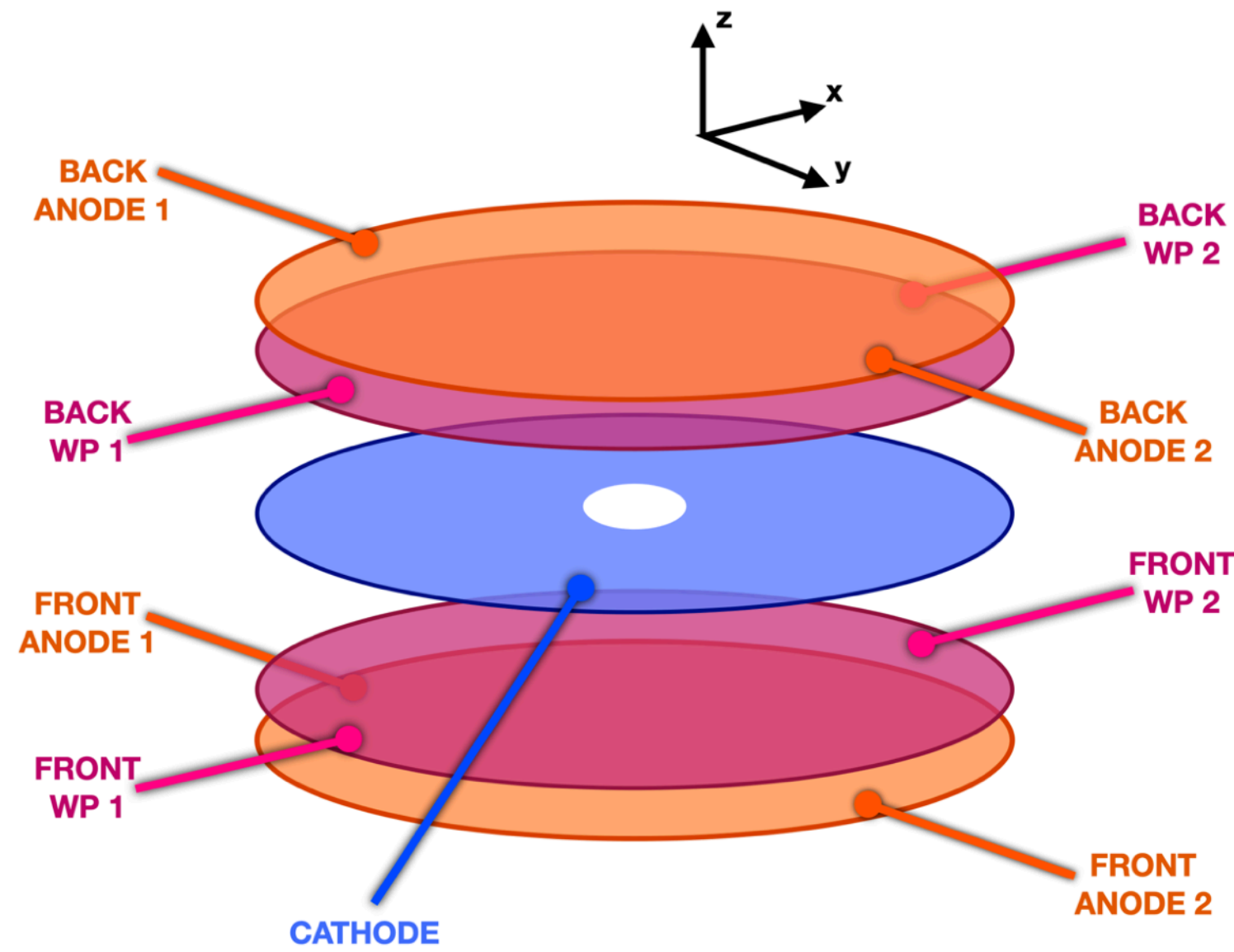
# Double Frisch-Grid Ionisation Chamber (dFGIC)







# Double Frisch-Grid Ionisation Chamber (dFGIC)



**CFD for a reliable cathode signal trigger:  
start of our fission event**

**CFD\* CONSTRAINT:**  
 $t_{delay} > t_r \cdot (1 - f)$ ,  
 where  $t_r$  is the signal rise time

$$\bar{x} = k_x \frac{P_1 - P_2}{P_1 + P_2}, \quad \bar{y} = k_y \frac{A_1 - A_2}{A_1 + A_2}$$

calibration constants

$$\bar{z} = v_d \cdot (\bar{t}_{(0^\circ, 0^\circ)} - \bar{t}_{(\theta_x^\circ, \theta_y^\circ)})$$

average electron drift time

electron drift velocity

The average electron drift time is the maxima of the resulting wave form of the anode sum signal shaped using the following equation:

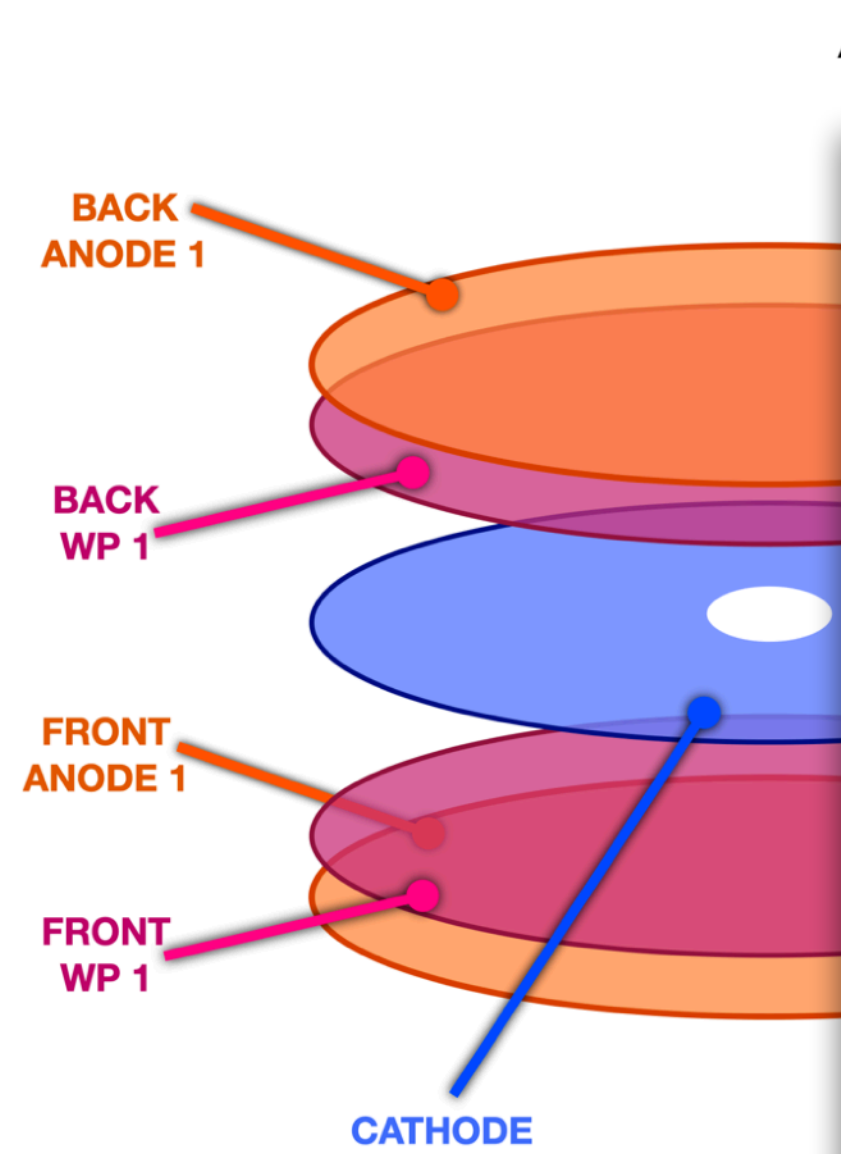
$$t_n = \frac{1}{Q_{max}} \cdot \sum_{k=k_0}^{k_0+n} (q_{k+1} - q_k)(k - k_0) \cdot \frac{1}{f_s}$$

\* CFD: Constant Fraction Discrimination

Adapted from: A. Göök, et al. A position-sensitive twin ionization chamber for fission fragment and prompt neutron correlation experiments. *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment*, 830:366–374, 2016.



# Double Frisch-Grid Ionisation Chamber (dFGIC)

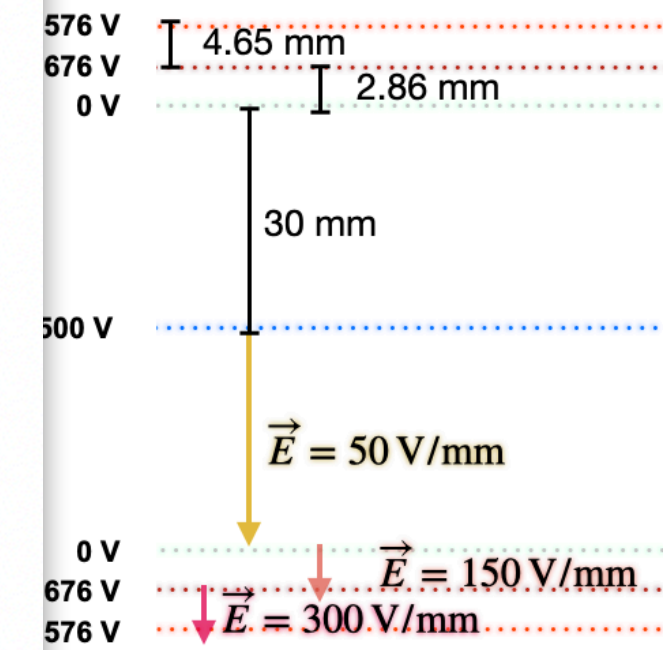
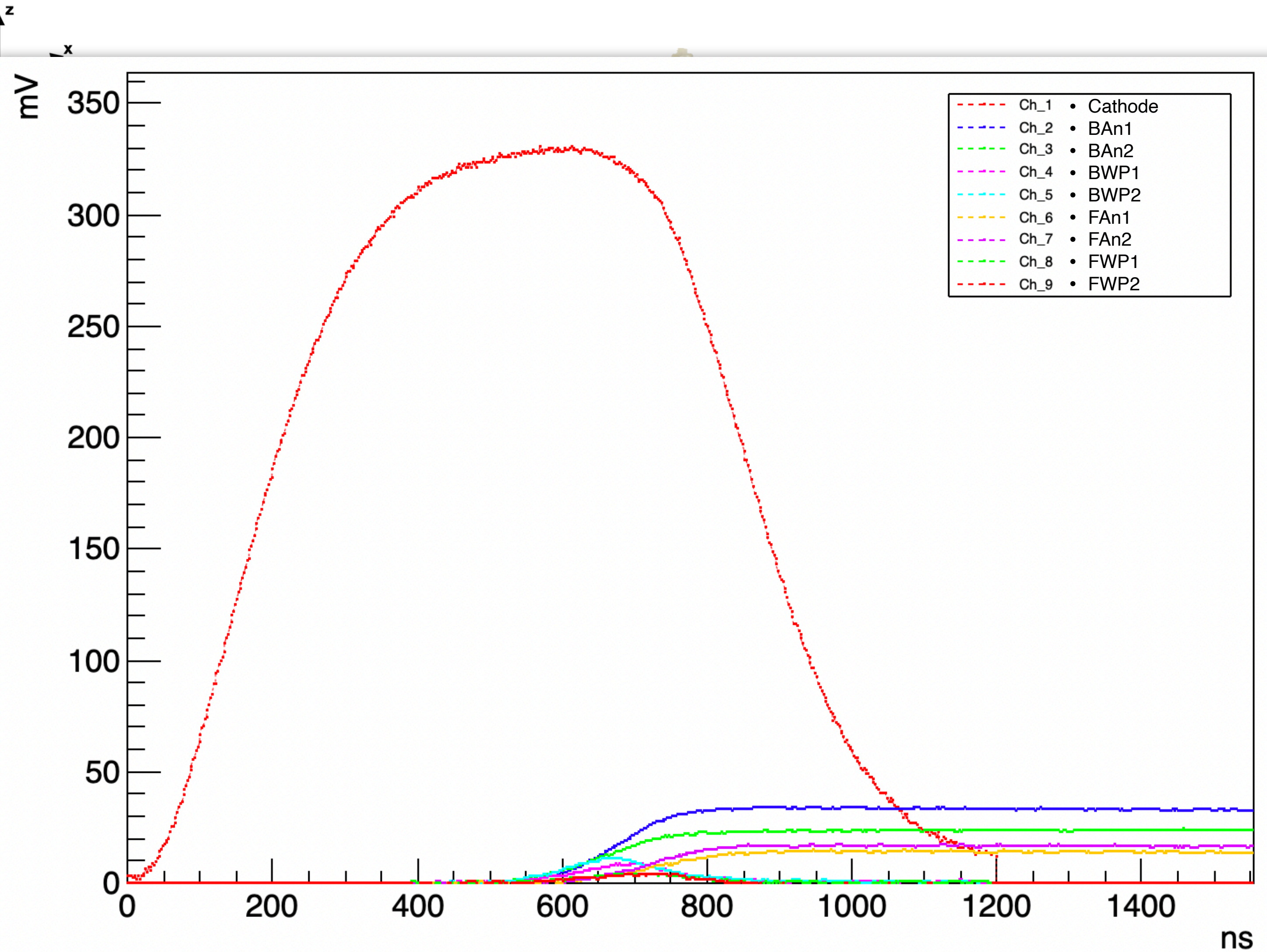


$$\bar{x} = k_x \frac{P_1 - P_2}{P_1 + P_2}, \quad \bar{y}$$

calibration

$$\bar{z} = v_d \cdot (\bar{t}_{(0^\circ, 0^\circ)} - \bar{t}_{(0^\circ, \theta)})$$

electron drift velocity



Cathode signal trigger:  
for fission event

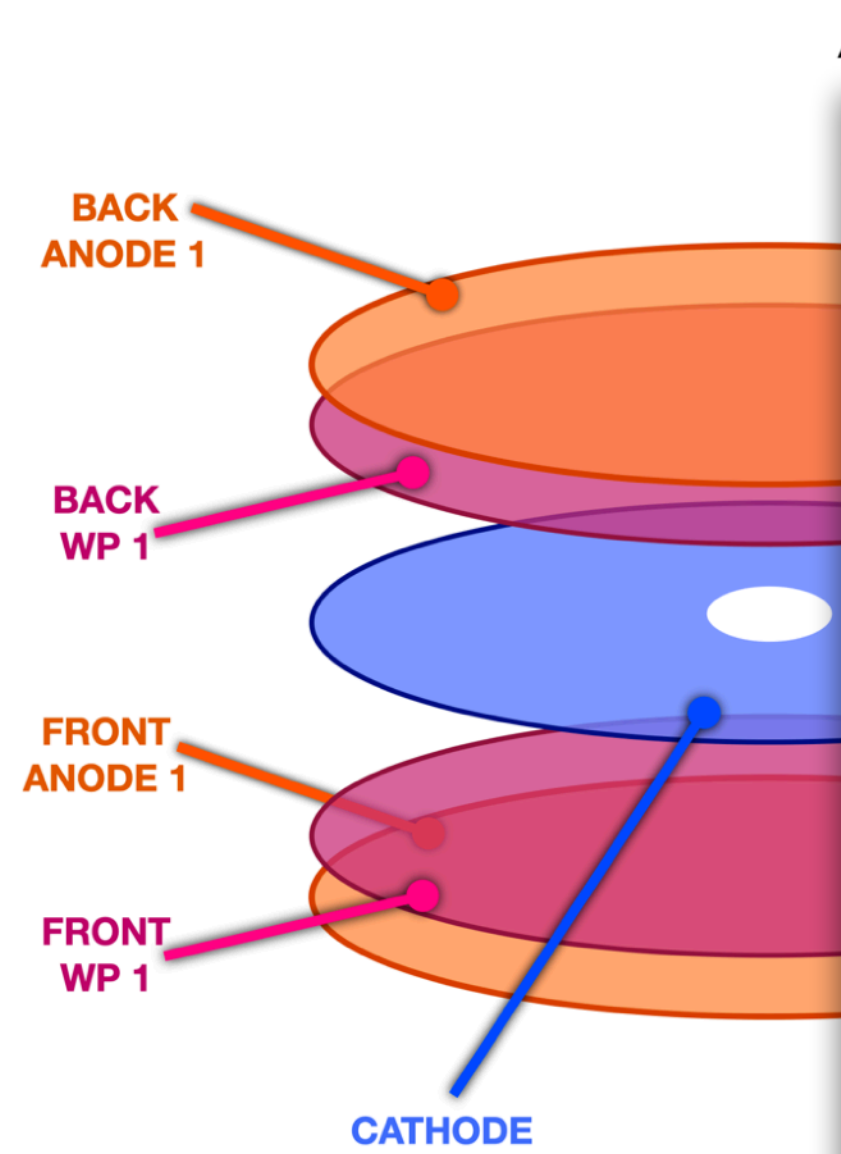
**CONSTRAINT:**  
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# Double Frisch-Grid Ionisation Chamber (dFGIC)

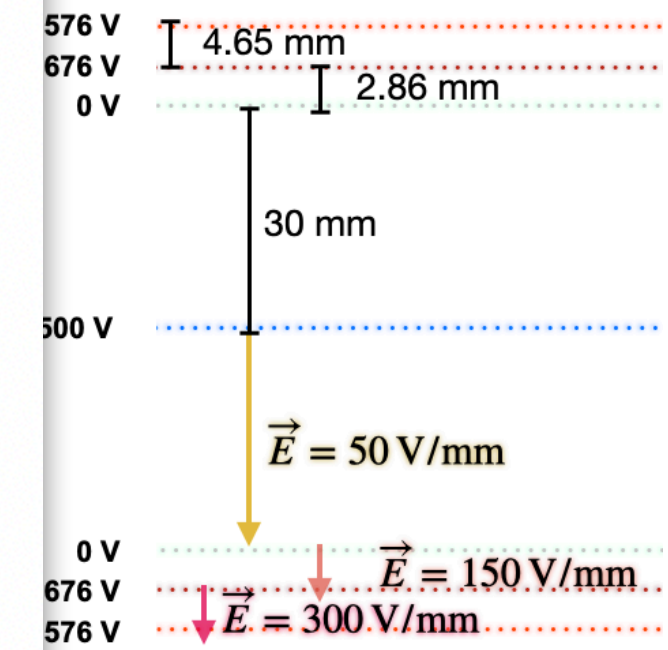
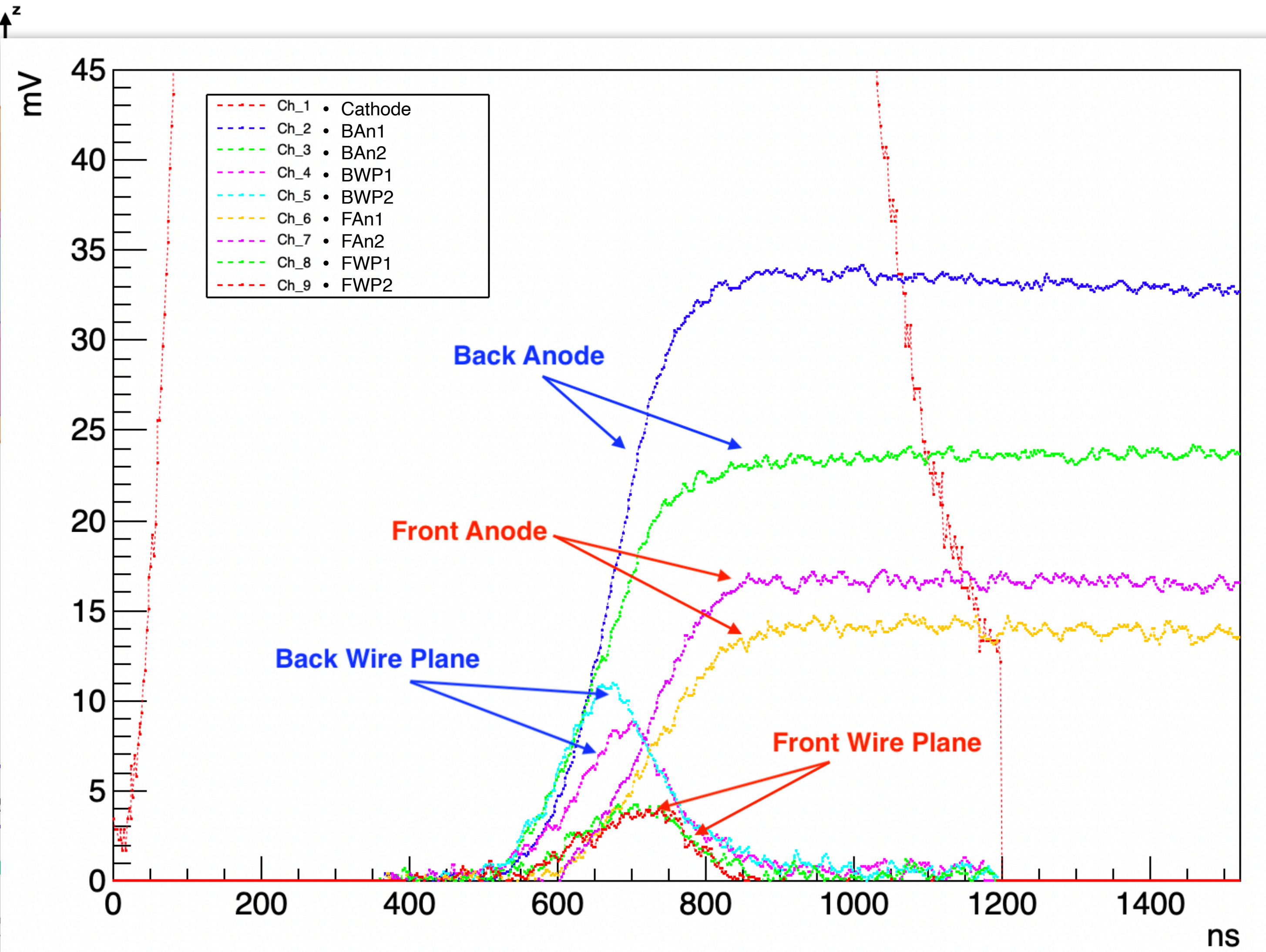


$$\bar{x} = k_x \frac{P_1 - P_2}{P_1 + P_2}, \quad \bar{y}$$

calibration

$$\bar{z} = v_d \cdot (\bar{t}_{(0^\circ, 0^\circ)} - \bar{t}_{(0^\circ, 0^\circ)})$$

electron



Cathode signal trigger:  
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\* CFD: Constant Fraction Discrimination



## Trace analysis through most frequently used methods

- Moving average algorithm;
  - RC filter;
  - Signal baseline correction;
  - CR-RC and CR-RC4 shaping filters;
  - Trapezoidal shaping filter;
  - Signal integration (deposited charge)
  - Constant Fraction Discrimination (CFD)
- BOTH TIME AND ENERGY MEASUREMENTS**
- « ENERGY » MEASUREMENTS**
- TIME MEASUREMENTS**



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**How do we know if the method works?**

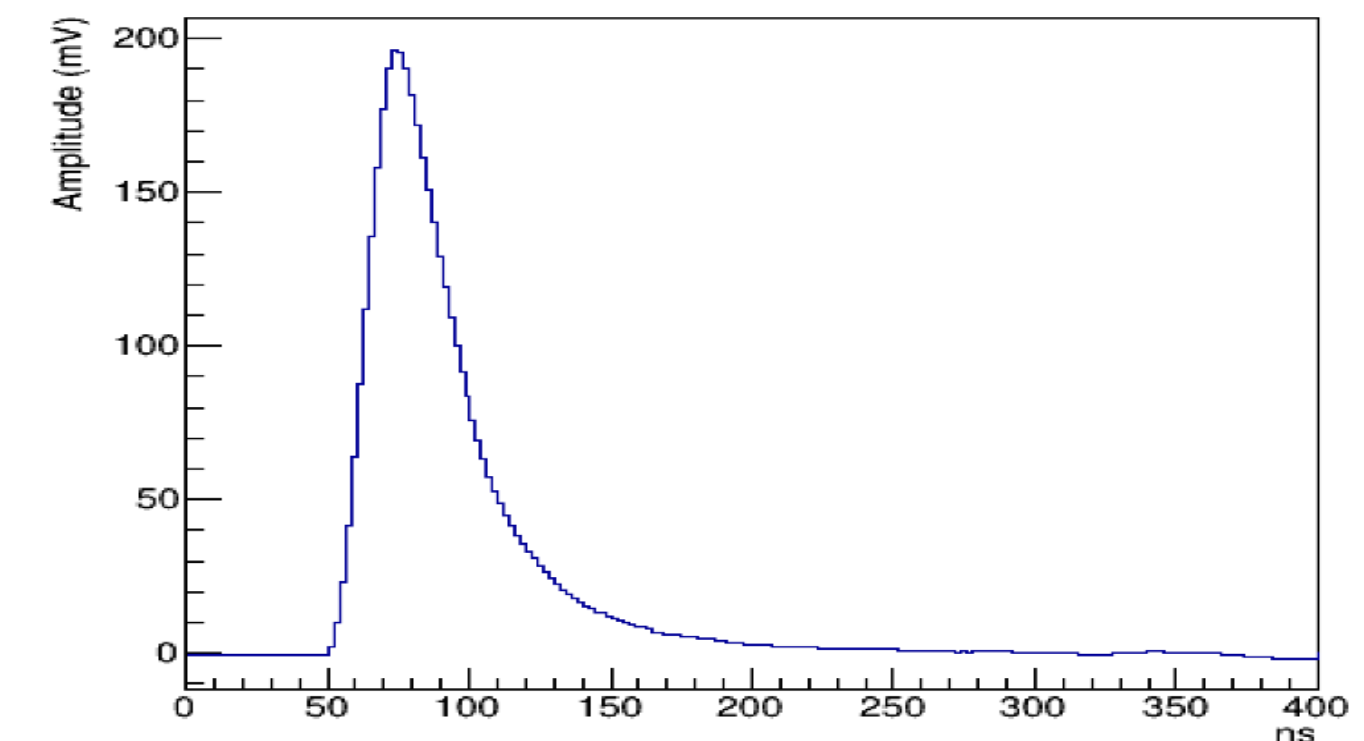
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## How do we know if the method works?

By evaluating the results obtained from a well-known detector => LaBr<sub>3</sub>

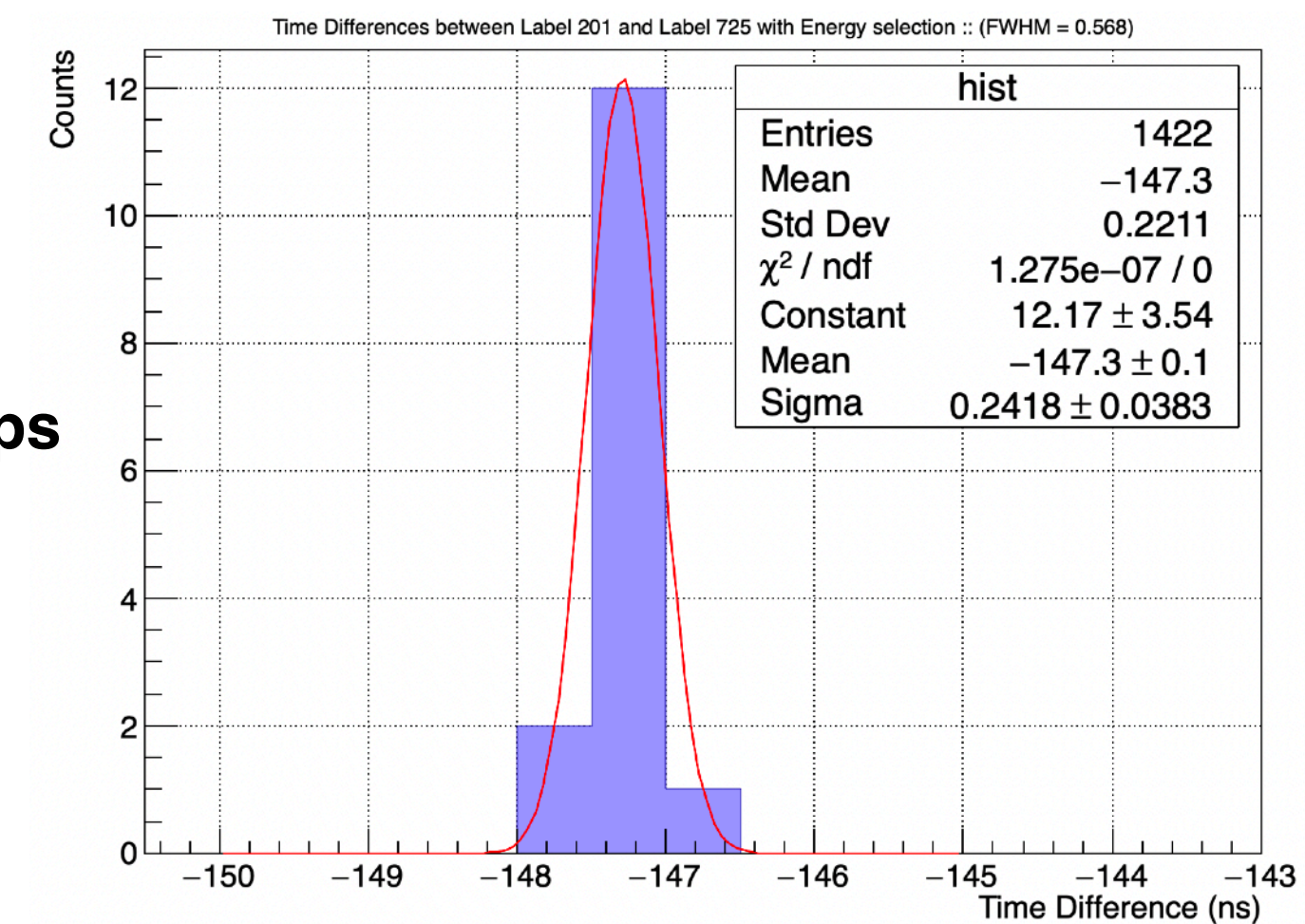
## THALIA LaBr<sub>3</sub> data stored as a trace:



~31.7 keV @ 1170 keV

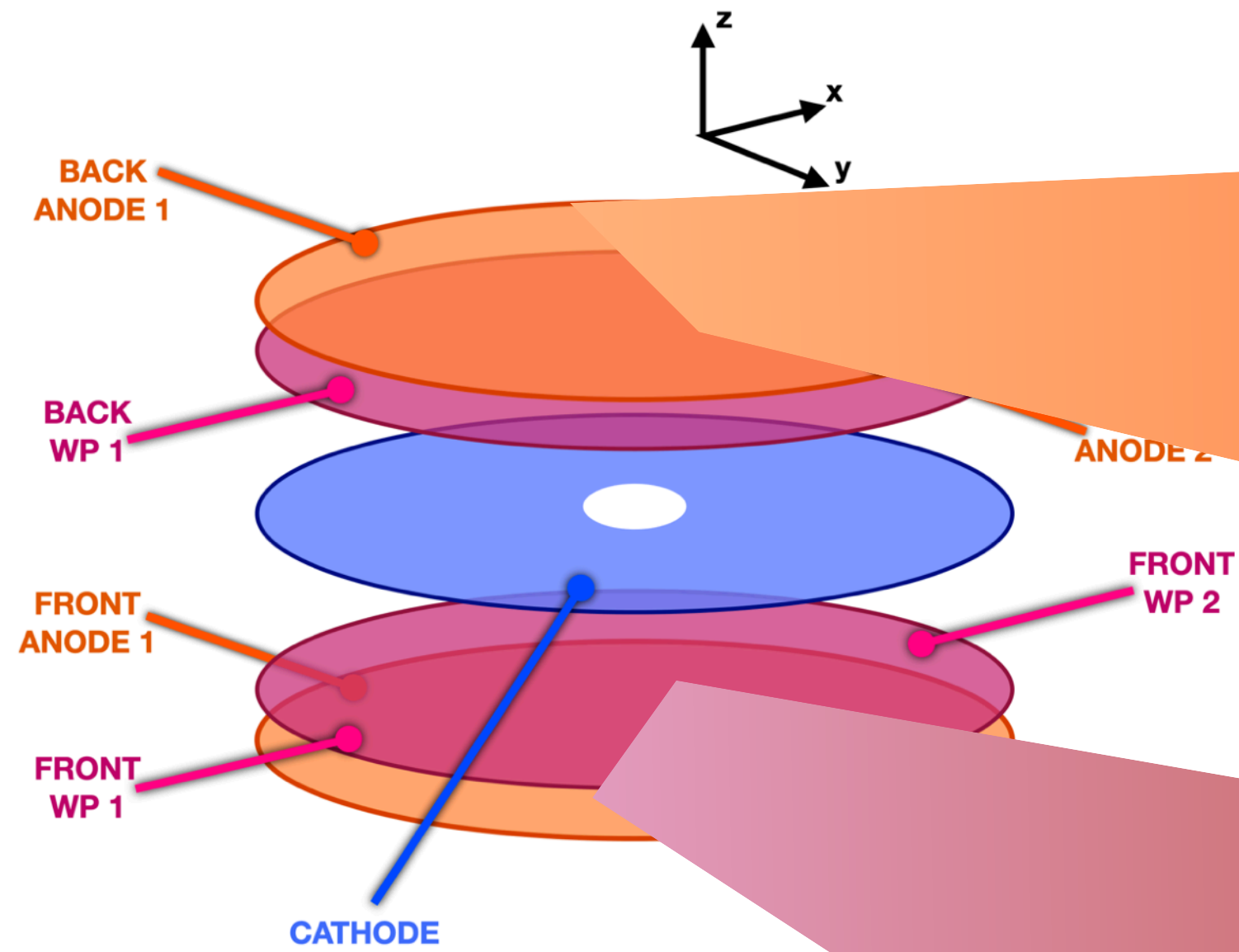
Time resolution of ~570 ps

\* with gamma energy selection: 1170 & 1330 peaks on <sup>60</sup>Co calibration run





# Double Frisch-Grid Ionisation Chamber (dFGIC)



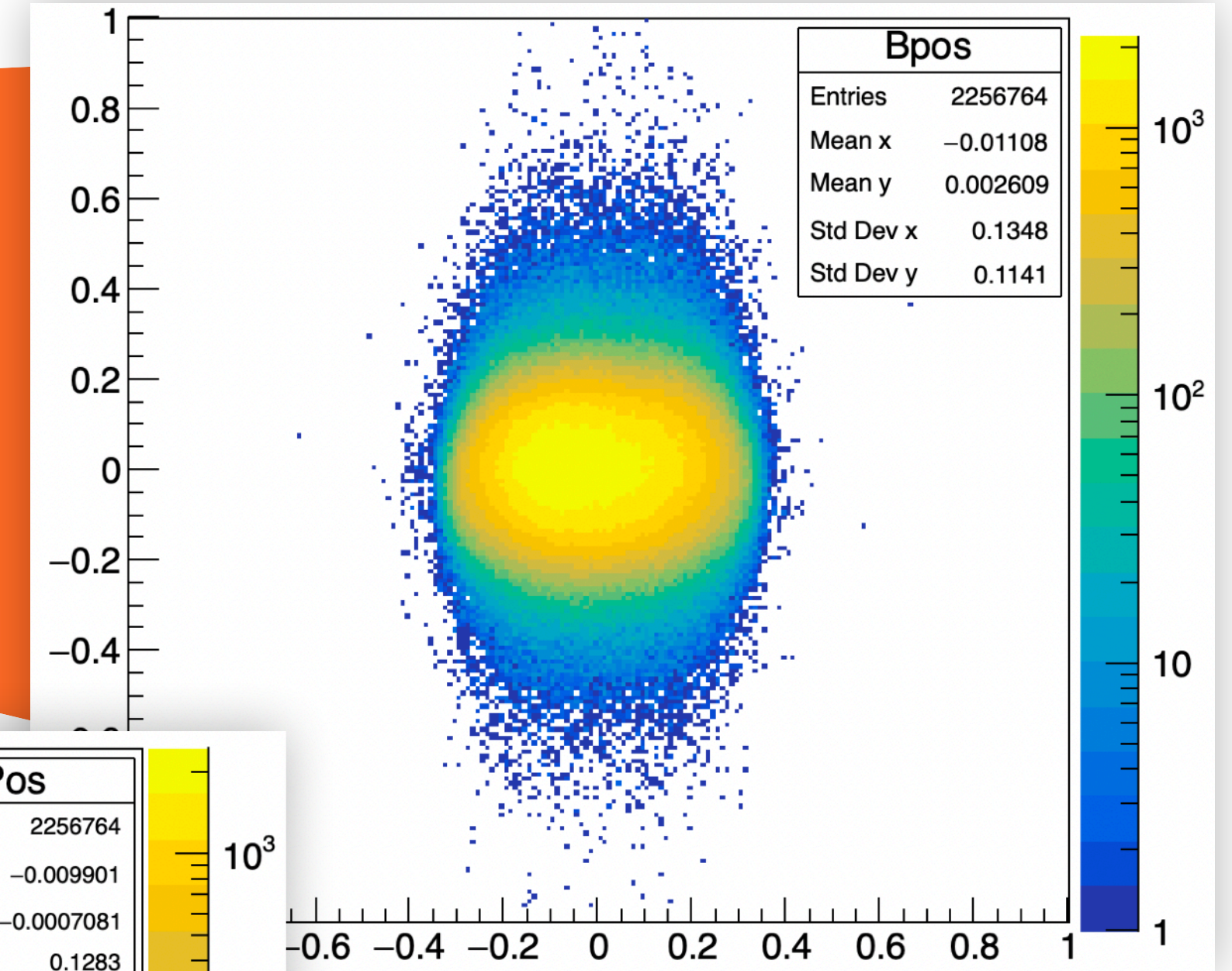
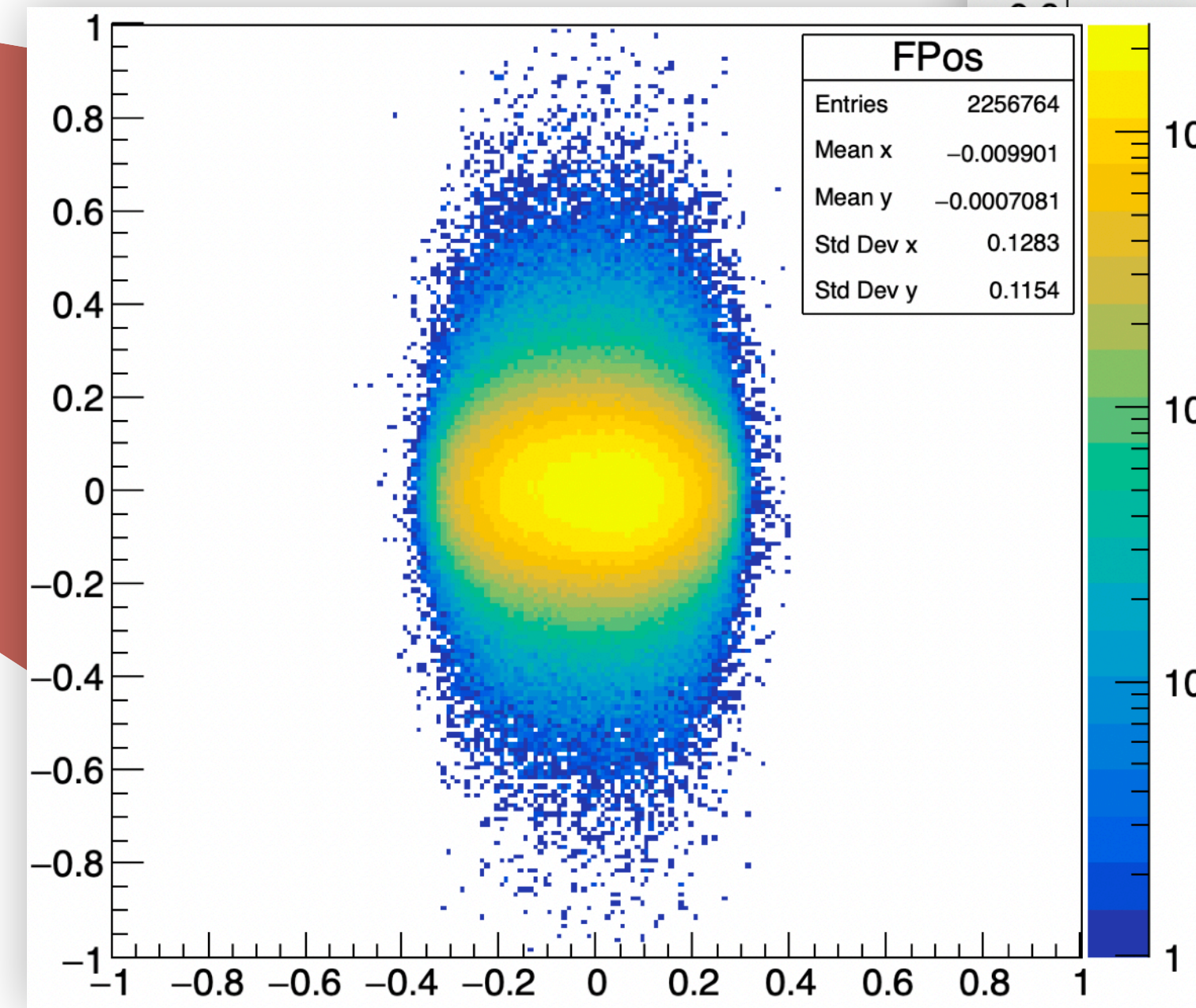
Back Anode

Front Anode

$$\bar{x} = k_x \frac{P_1 - P_2}{P_1 + P_2}, \quad \bar{y} = k_y \frac{A_1 - A_2}{A_1 + A_2}$$

calibration constants

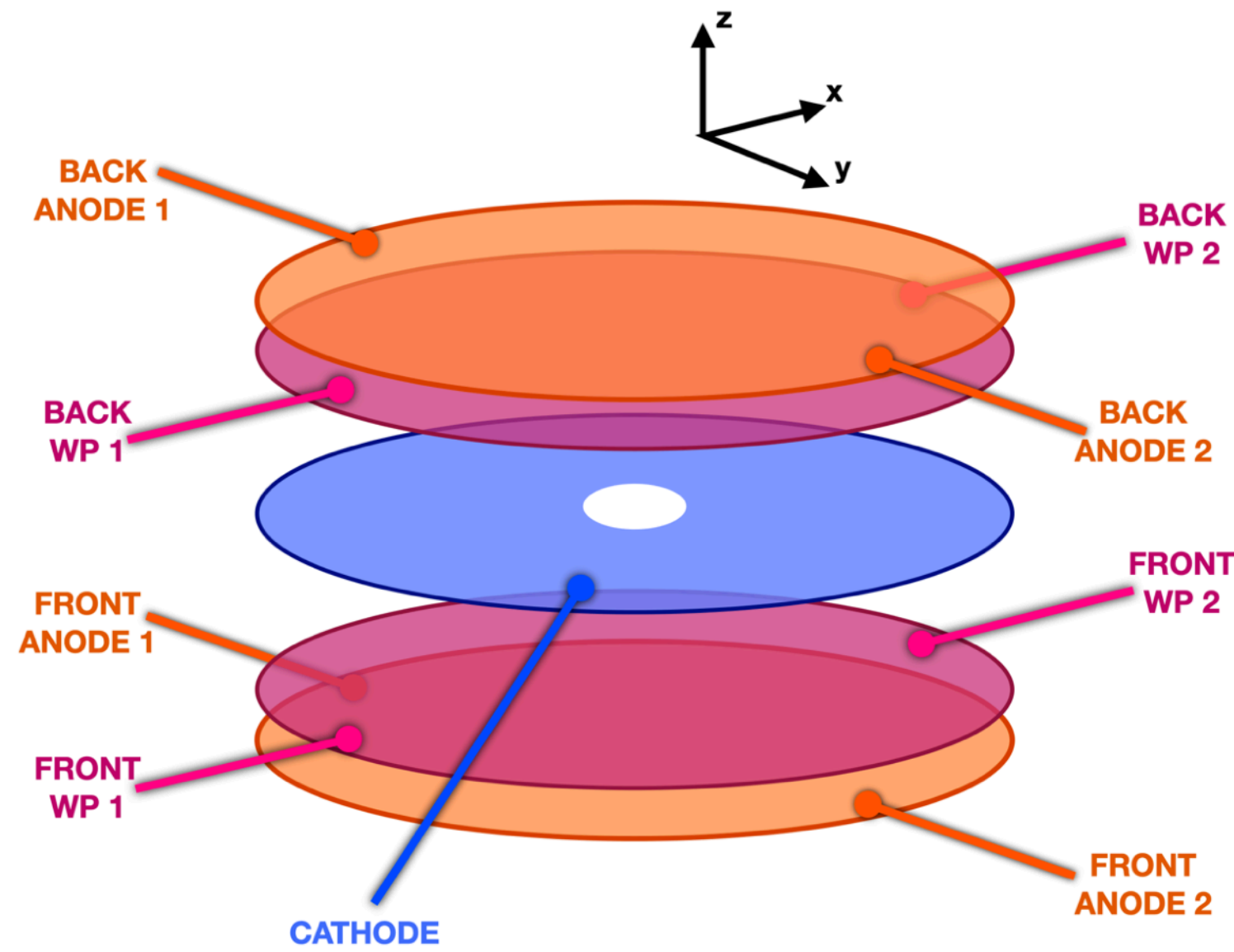
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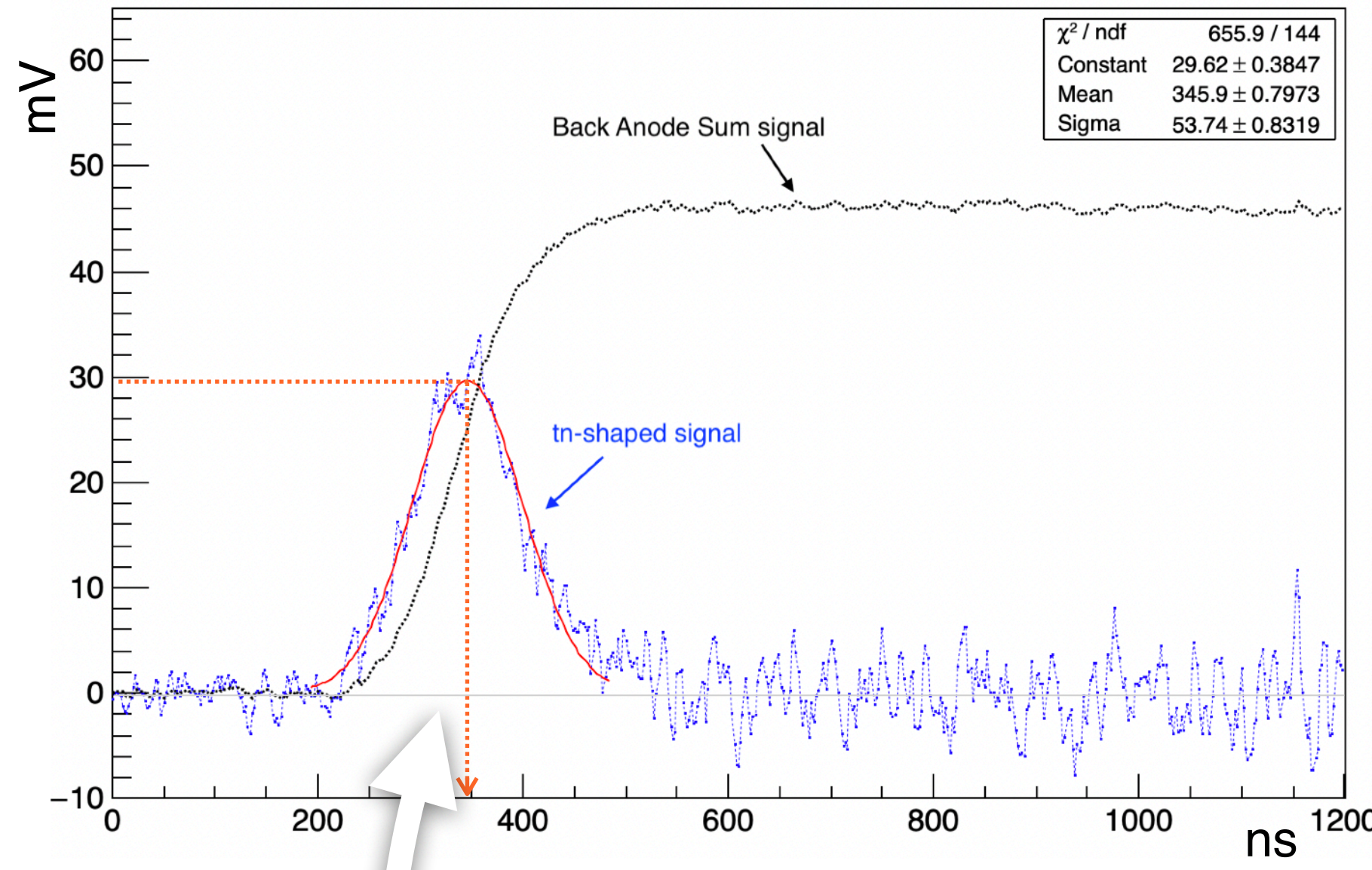
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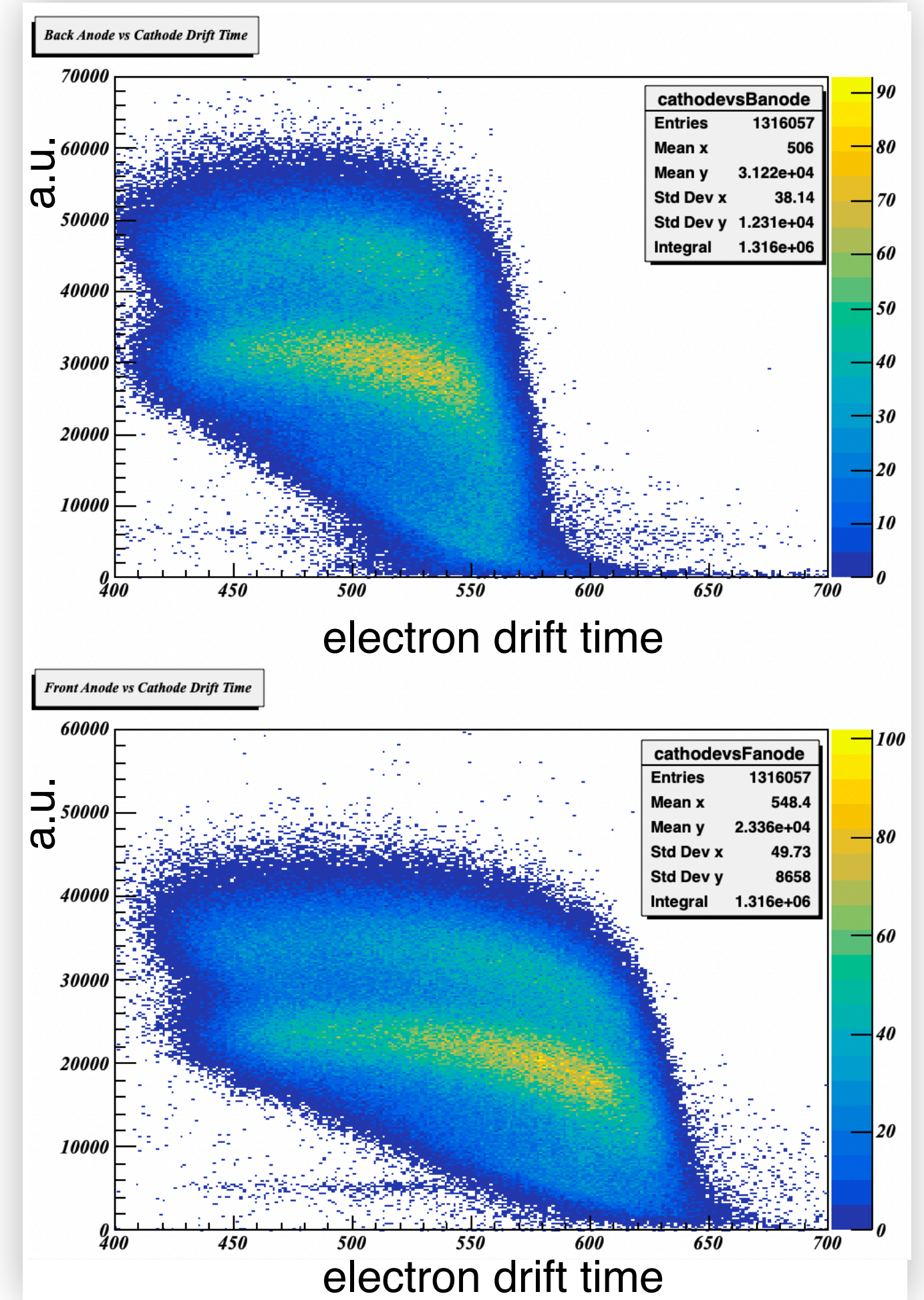
$$\bar{z} = v_d \cdot (\bar{t}_{(0^\circ, 0^\circ)} - \bar{t}_{(\theta_x^\circ, \theta_y^\circ)}) \rightarrow \text{average electron drift time}$$

Electron drift velocity



$$t_n = \frac{1}{Q_{max}} \cdot \sum_{k=k_0}^{k_0+n} (q_{k+1} - q_k)(k - k_0) \cdot \frac{1}{f_s}$$

## Energy vs. Electron drift time



Adapted from: A. Göök, *et al.* A position-sensitive twin ionization chamber for fission fragment and prompt neutron correlation experiments. *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment*, 830:366–374, 2016.





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**TIME CONSUMING**

Trace analysis takes **~2s per 1k fission events**

3 weeks of data acquisition -> 600M events

**300 h or 13 days to process the traces**

*=> yes, we are working with an optimized multi-threading algorithm*

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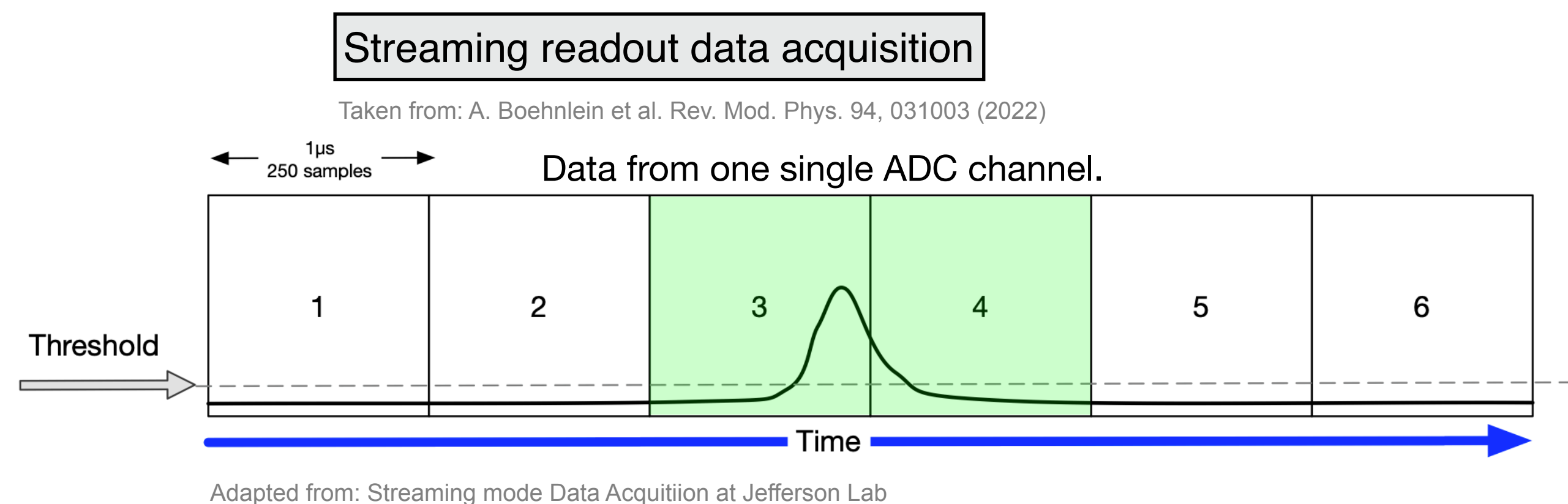
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## An example...



A virtual trigger based on an unsupervised hierarchical cluster algorithm selects the relevant data to reconstruct the physics event



Supervised vs. unsupervised learning

Regression vs. classification model

### Hyperparameters

Activation function

Batch size

Epochs

Learning rate

Loss function

Number of hidden layers

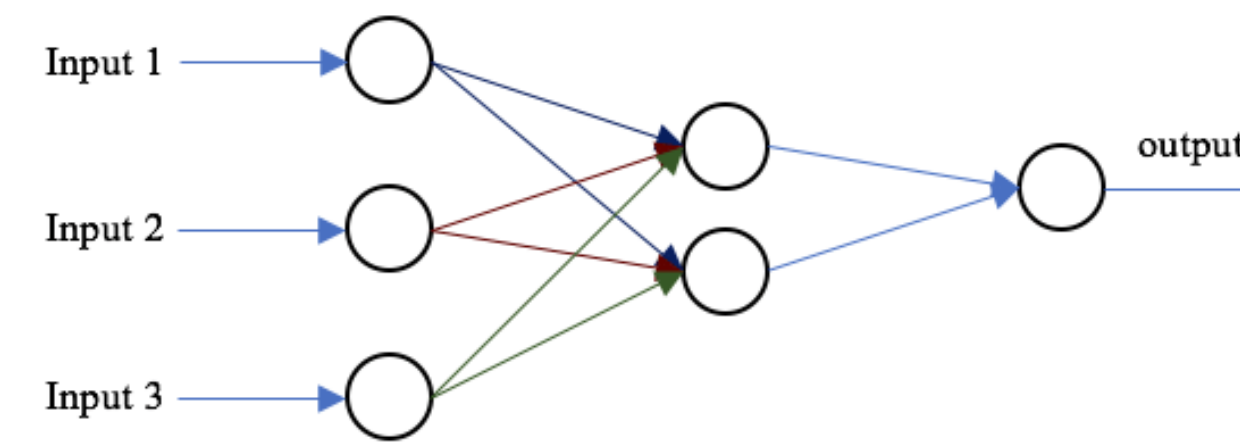
Number of neurons per layer

### Parameters

Weights and biases

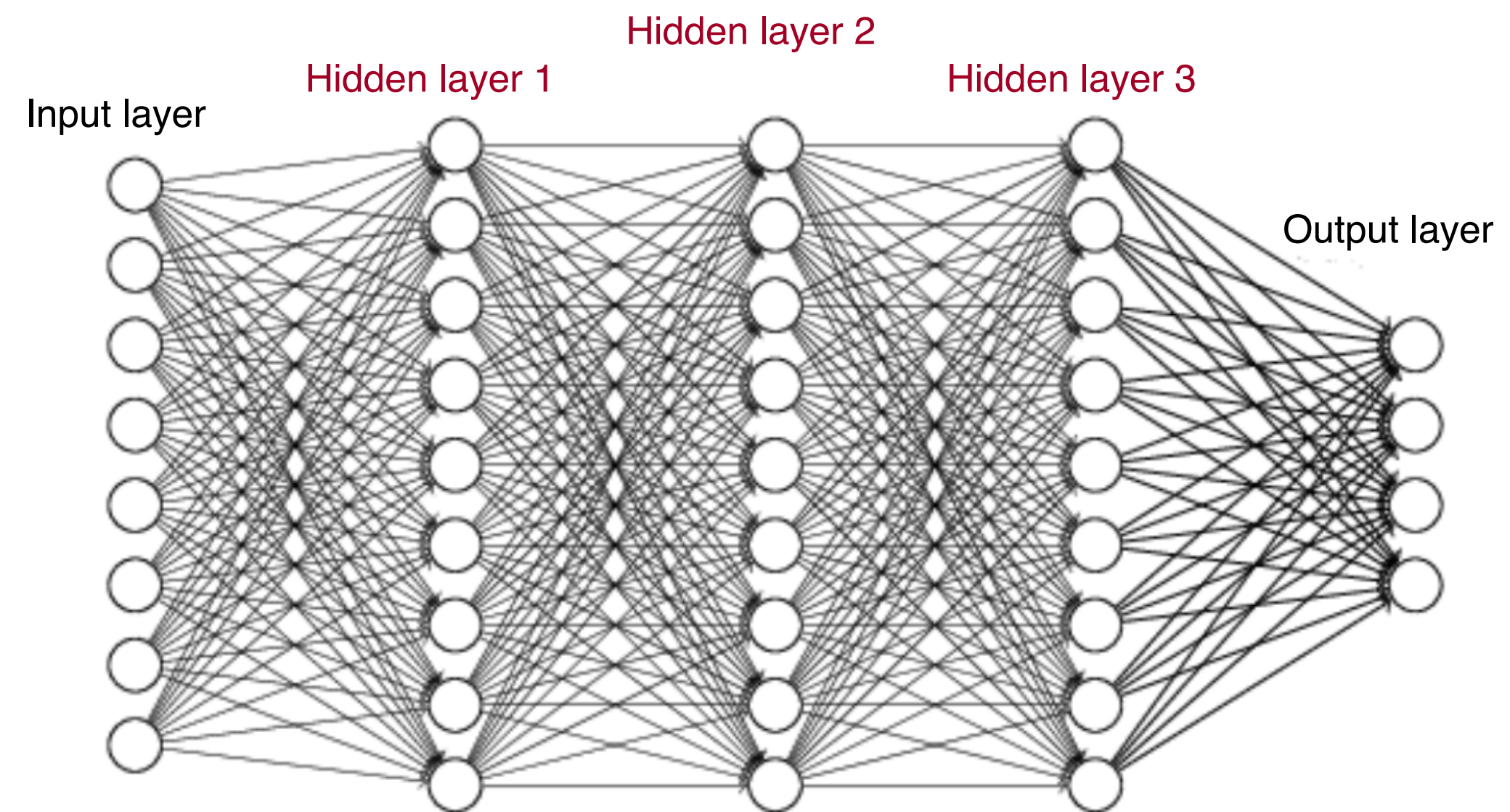
$$Y = \sum_i (weight_i \cdot input_i) + bias$$

## Fully Connected Neural Networks (FCNN)



Input layer      Hidden layer      Output layer

Taken from: A. Said and F. Sayed Ibrahim. Comparative study of segmentation techniques for detection of tumors based on mri brain images. *International Journal of Biochemistry and Biotechnology*, 8:10, 09 2017



Taken from: <https://math.stackexchange.com/q/2048722>



Supervised vs. unsupervised learning

Regression vs. classification model

## Hyperparameters

Activation function

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Loss function

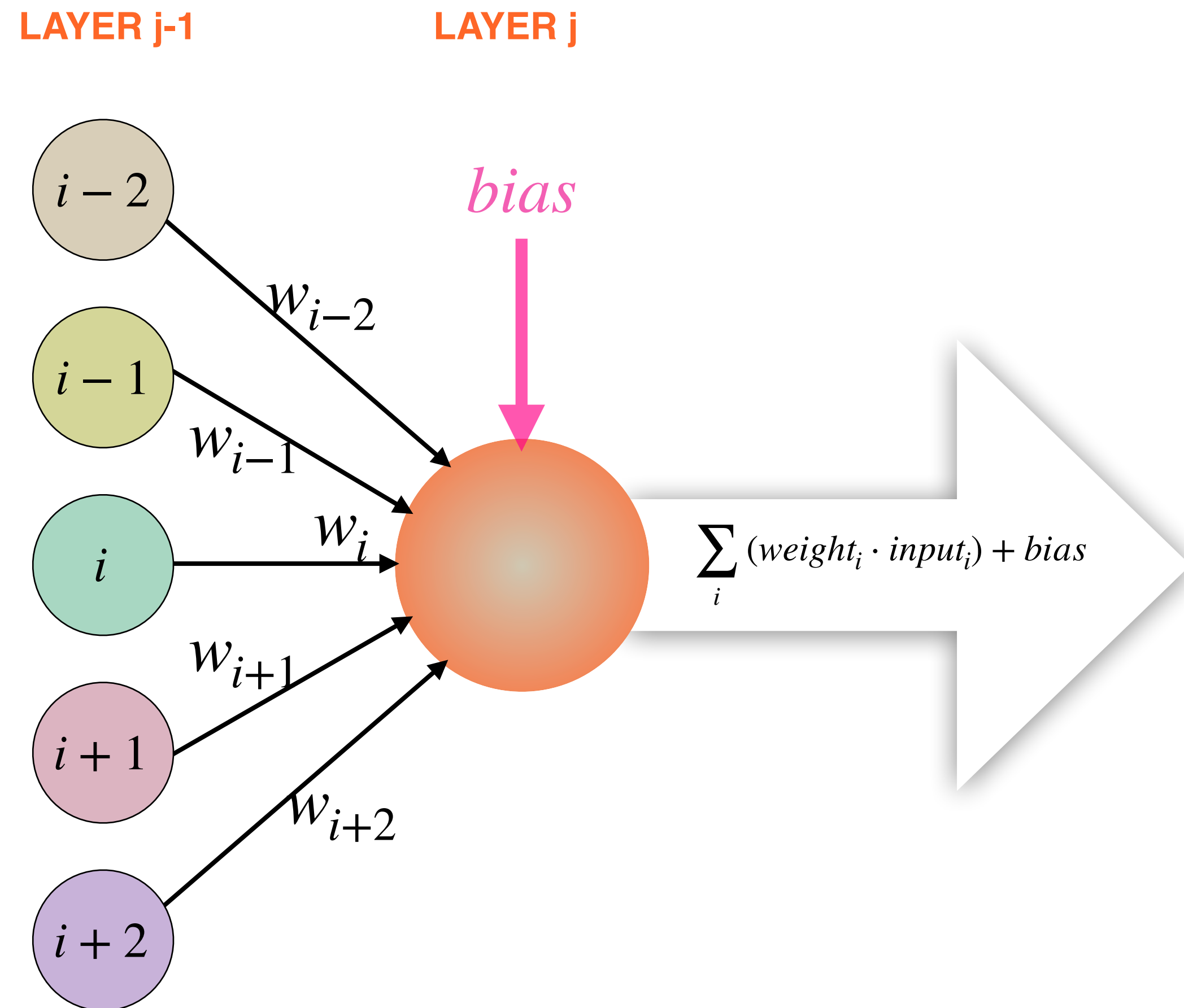
Number of hidden layers

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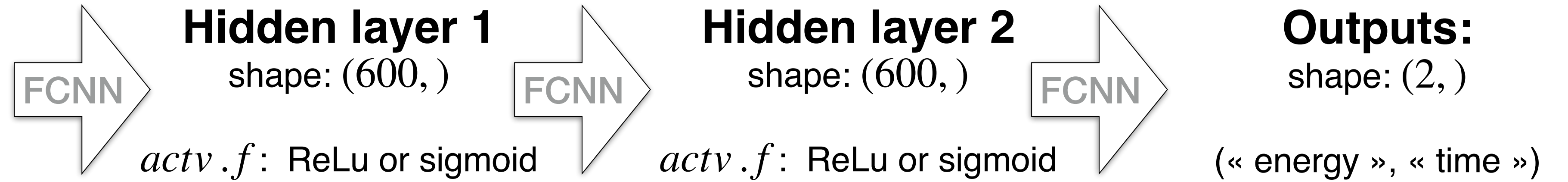
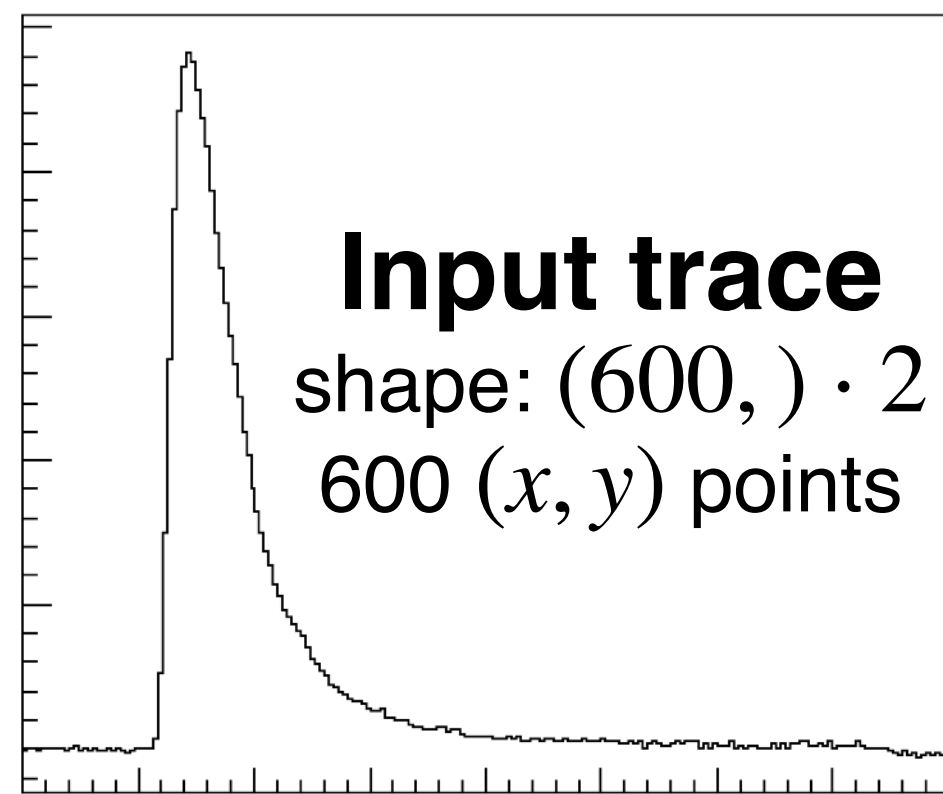
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$$Y = \sum_i (weight_i \cdot input_i) + bias$$



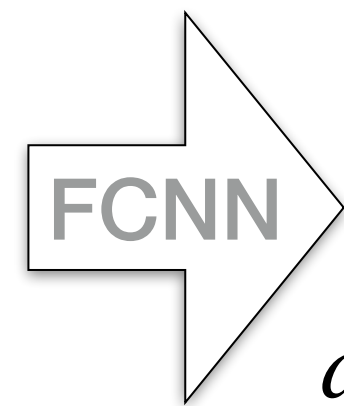
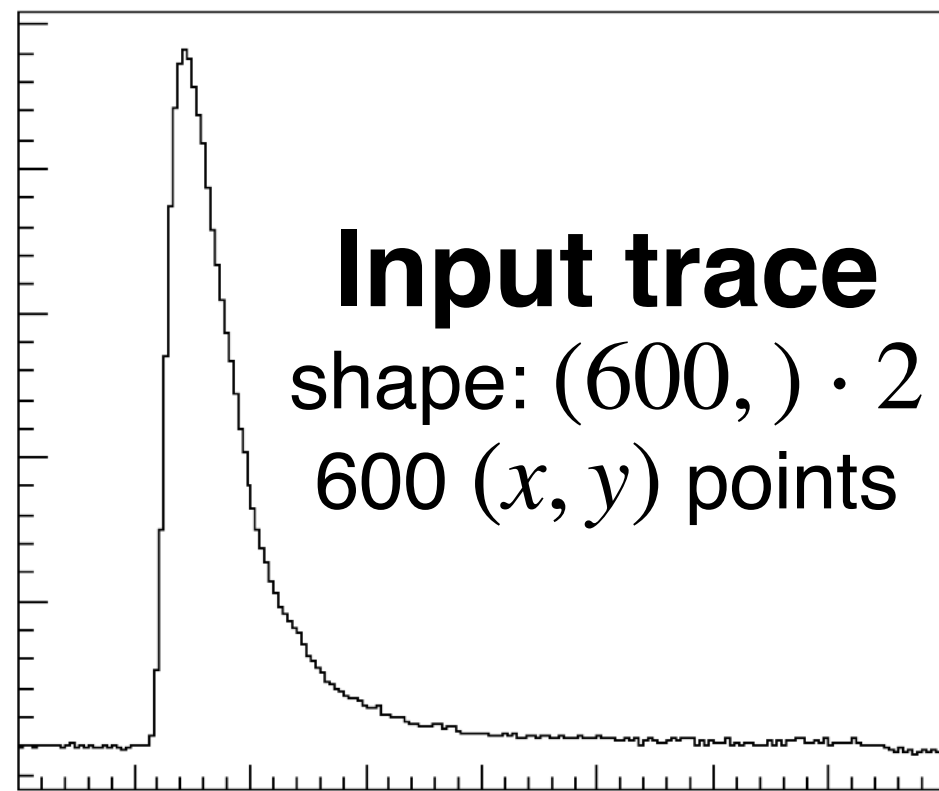
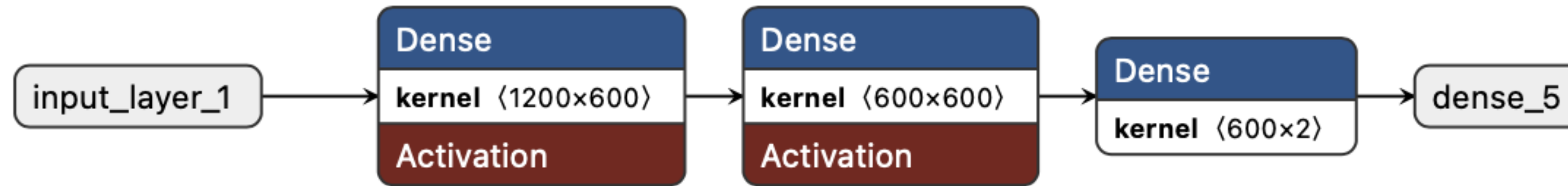


# FCNN models for trace analysis



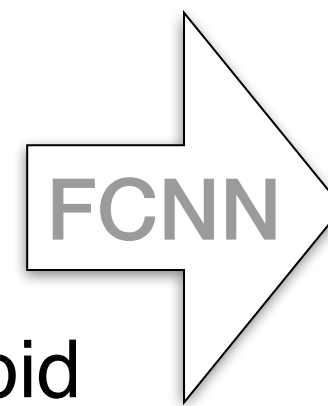


# FCNN models for trace analysis



**Hidden layer 1**  
shape: (600, )

*actv .f*: ReLu or sigmoid



**Hidden layer 2**  
shape: (600, )

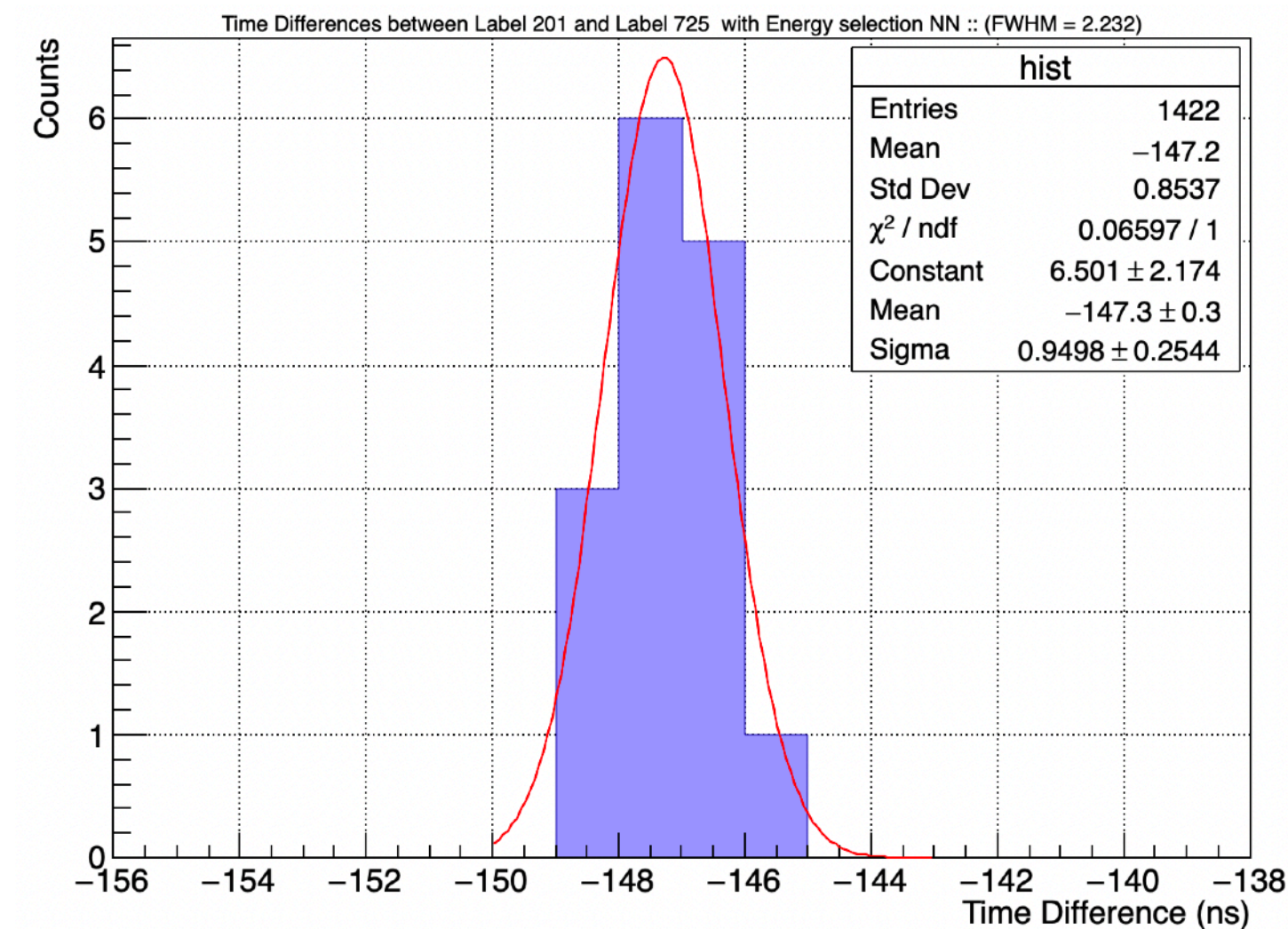
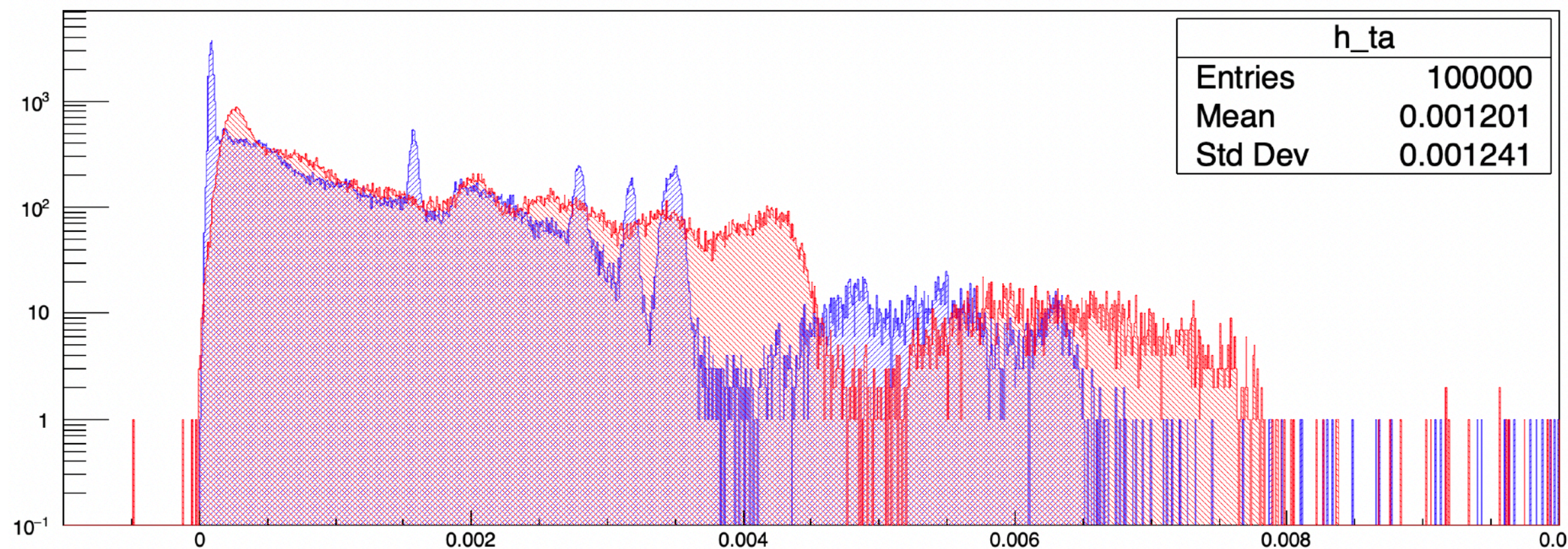
*actv .f*: ReLu or sigmoid



**Outputs:**  
shape: (2, )

(« energy », « time »)

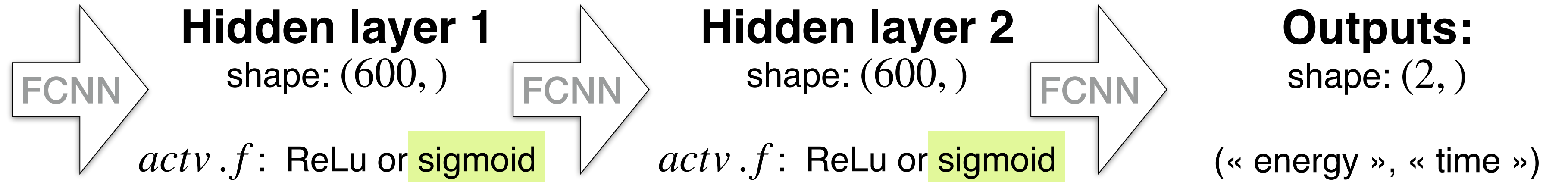
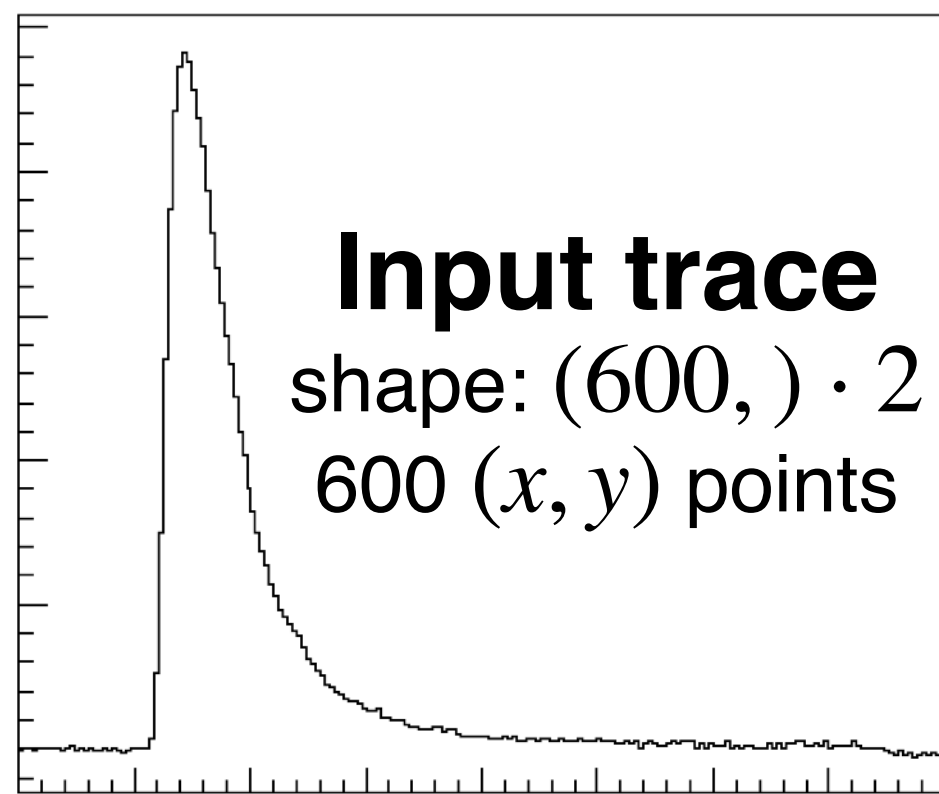
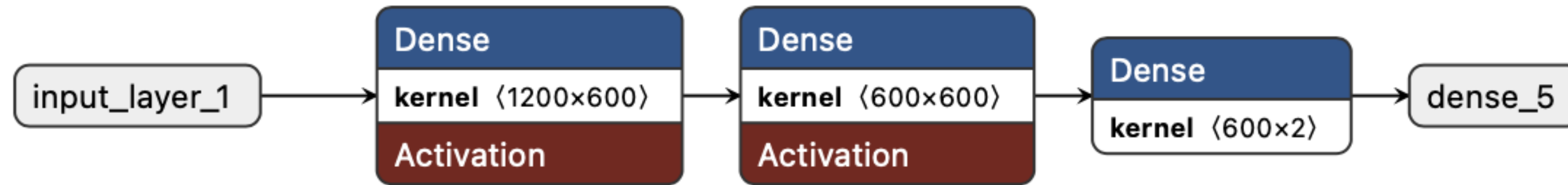
Prediction takes ~ 80s for 1M traces  
-> should be able to perform much faster in C++/C



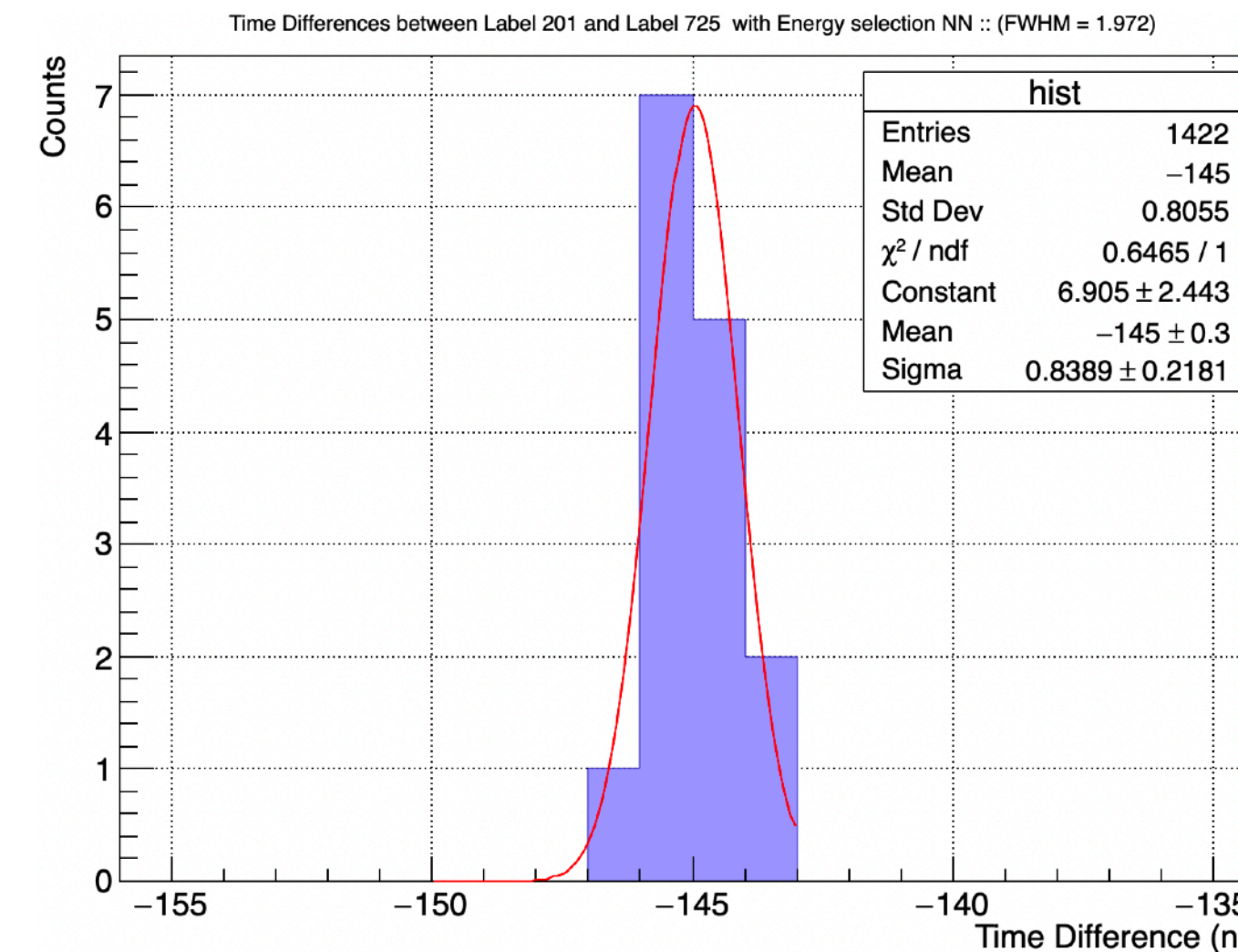
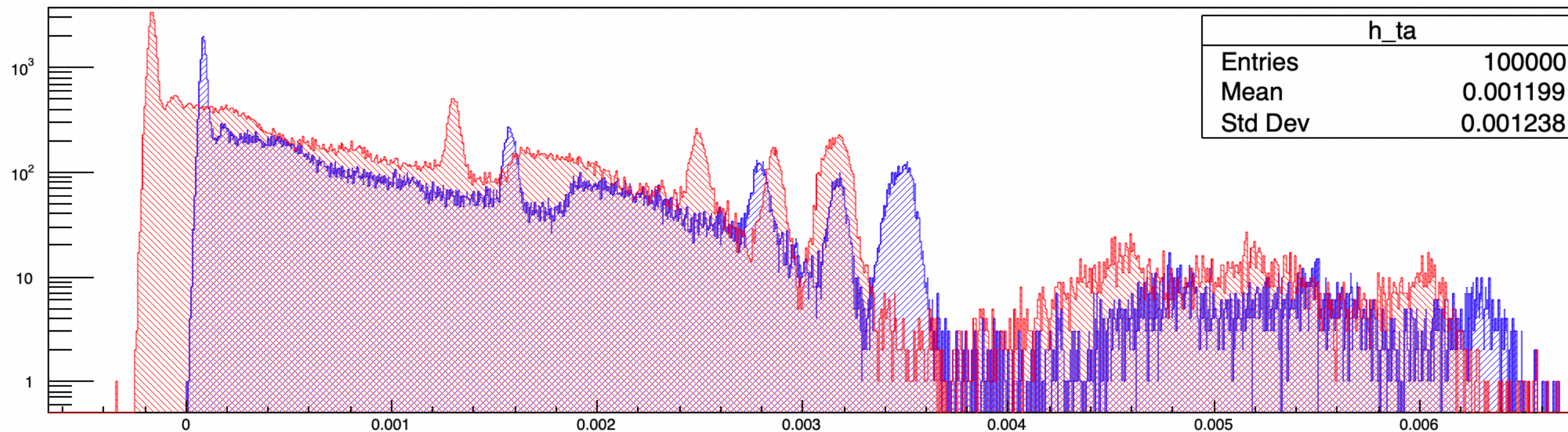
$$R(t) = 2232 \text{ ps}$$



# FCNN models for trace analysis



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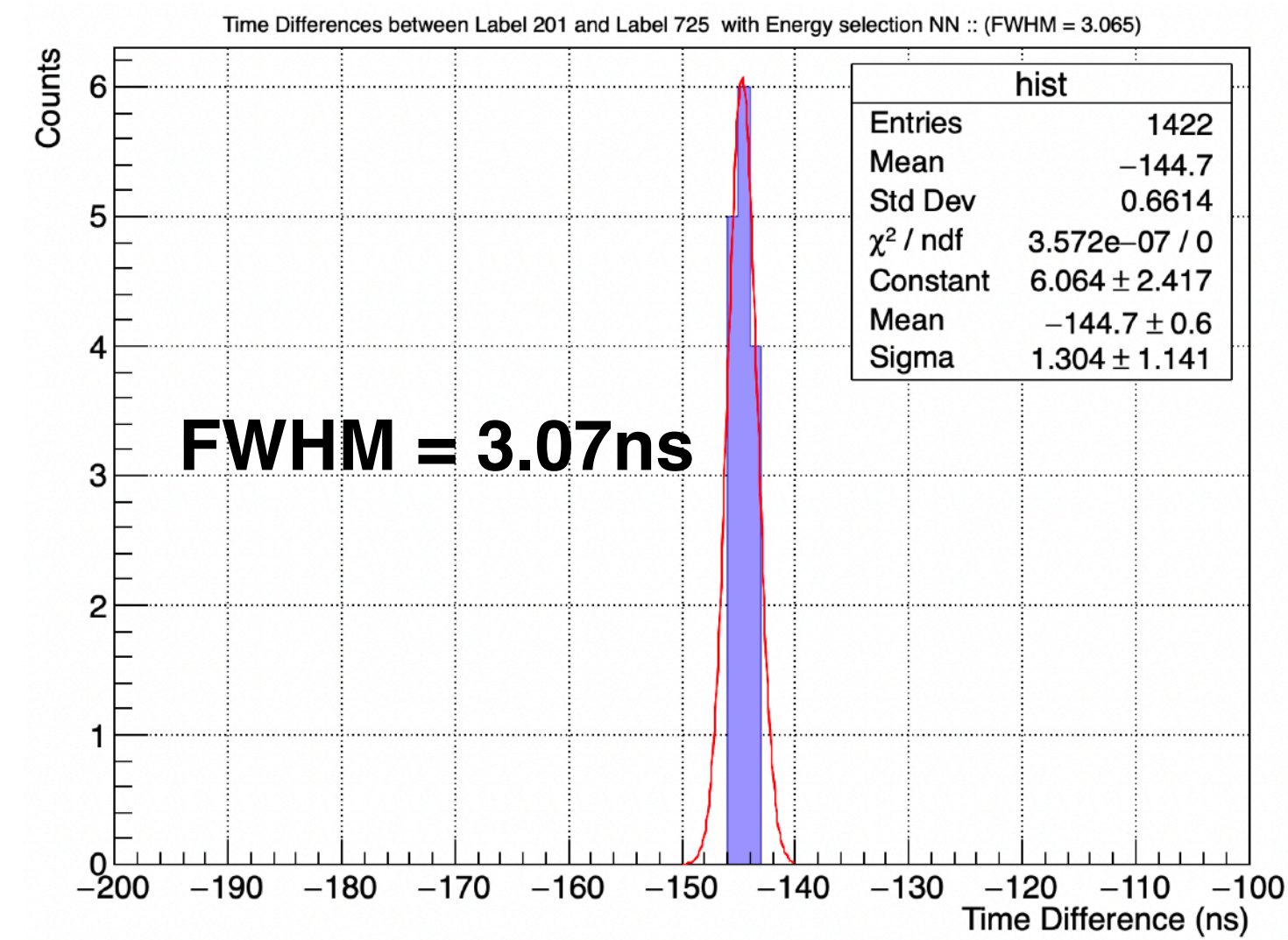
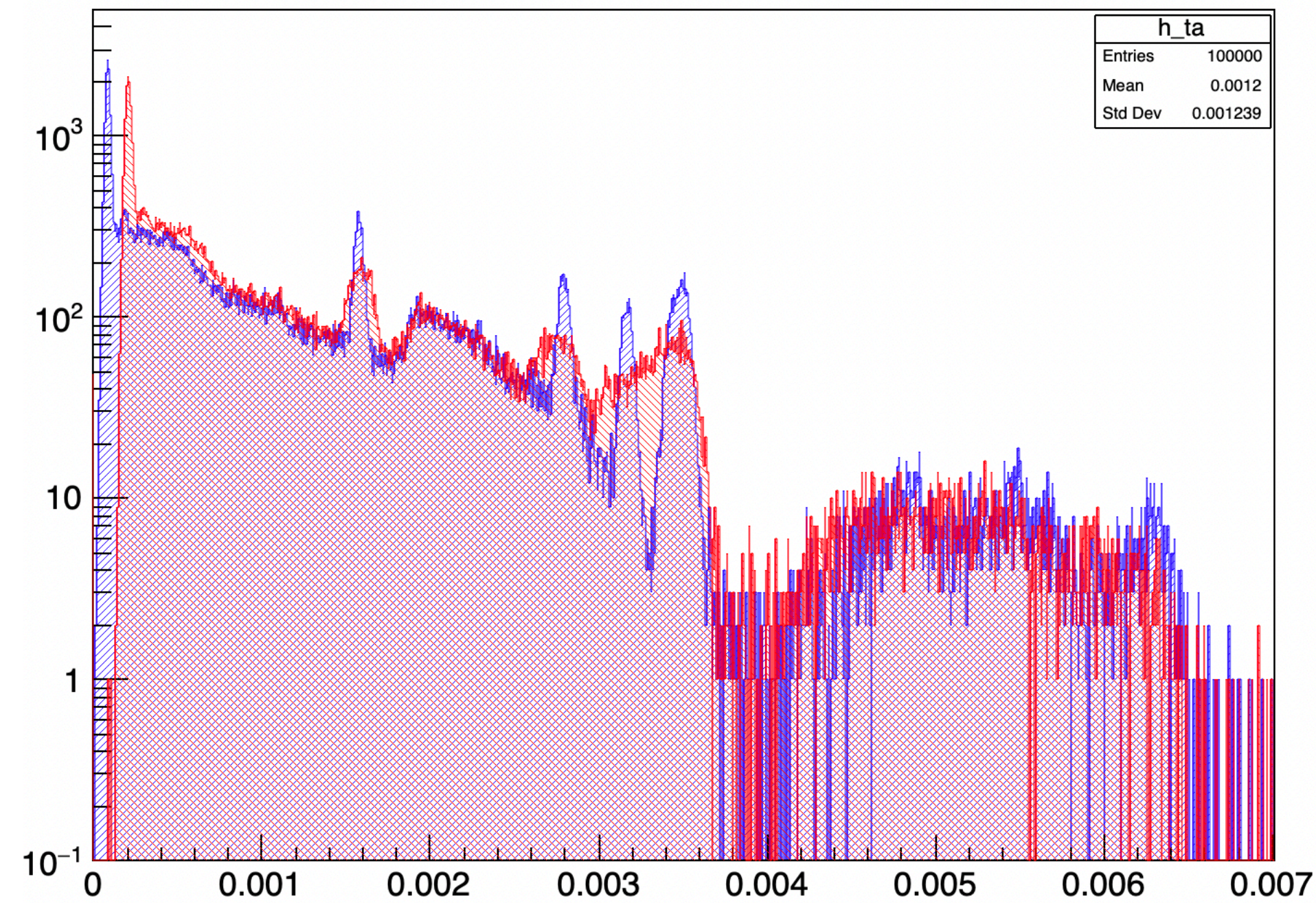
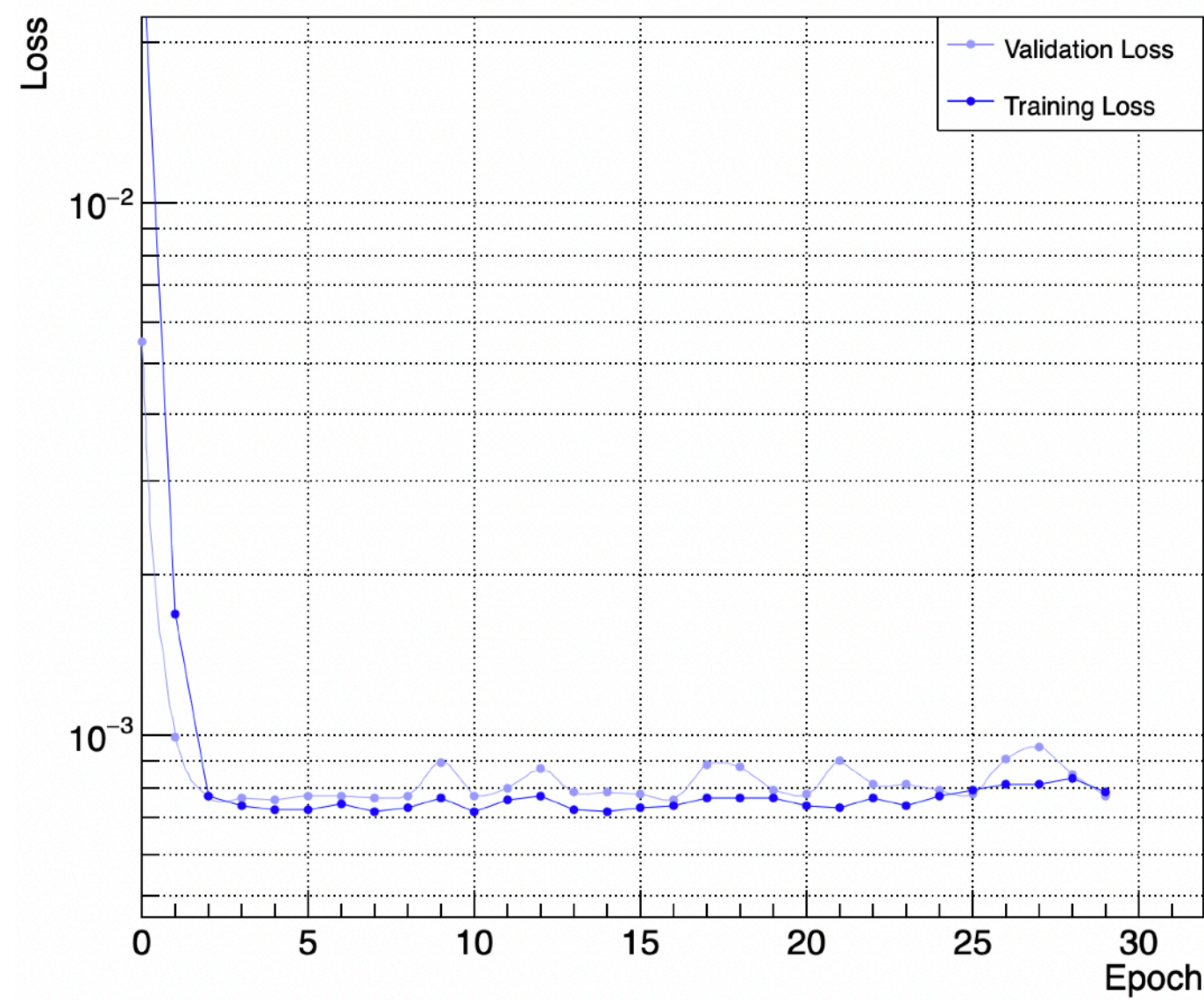
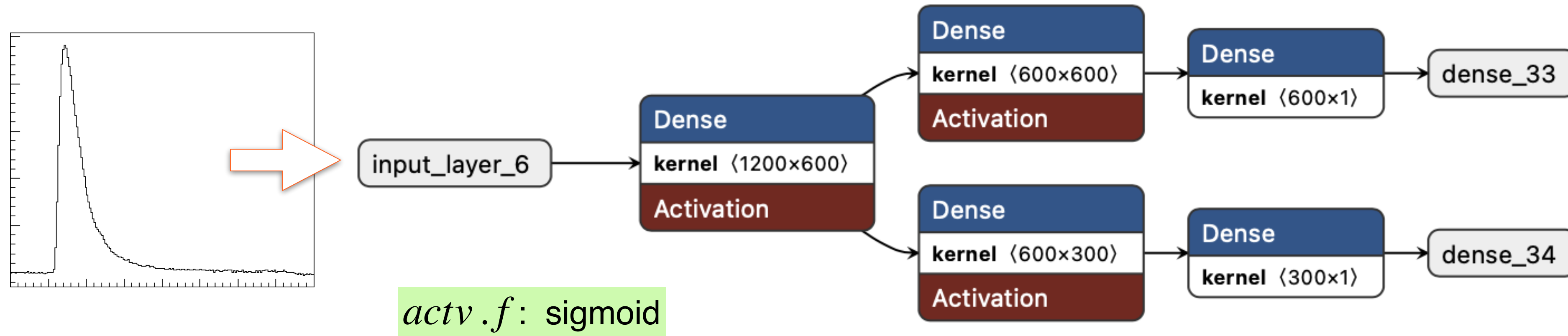
31.7 keV @ 1170 keV  
 $R(t) = 569 \text{ ps}$

**With NN:**  
37 keV @ 1170 keV  
 $R(t) = 1970 \text{ ps}$



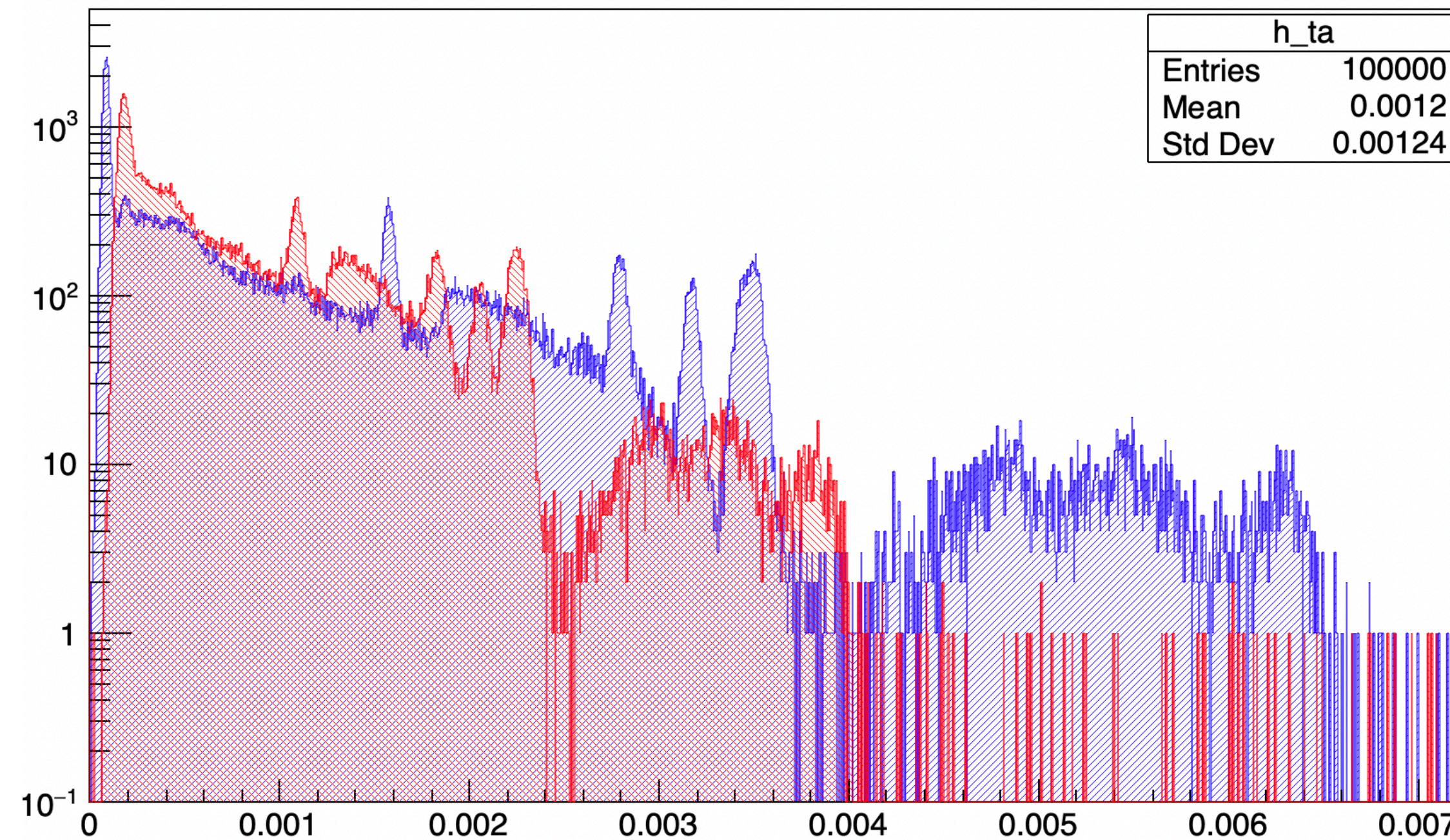
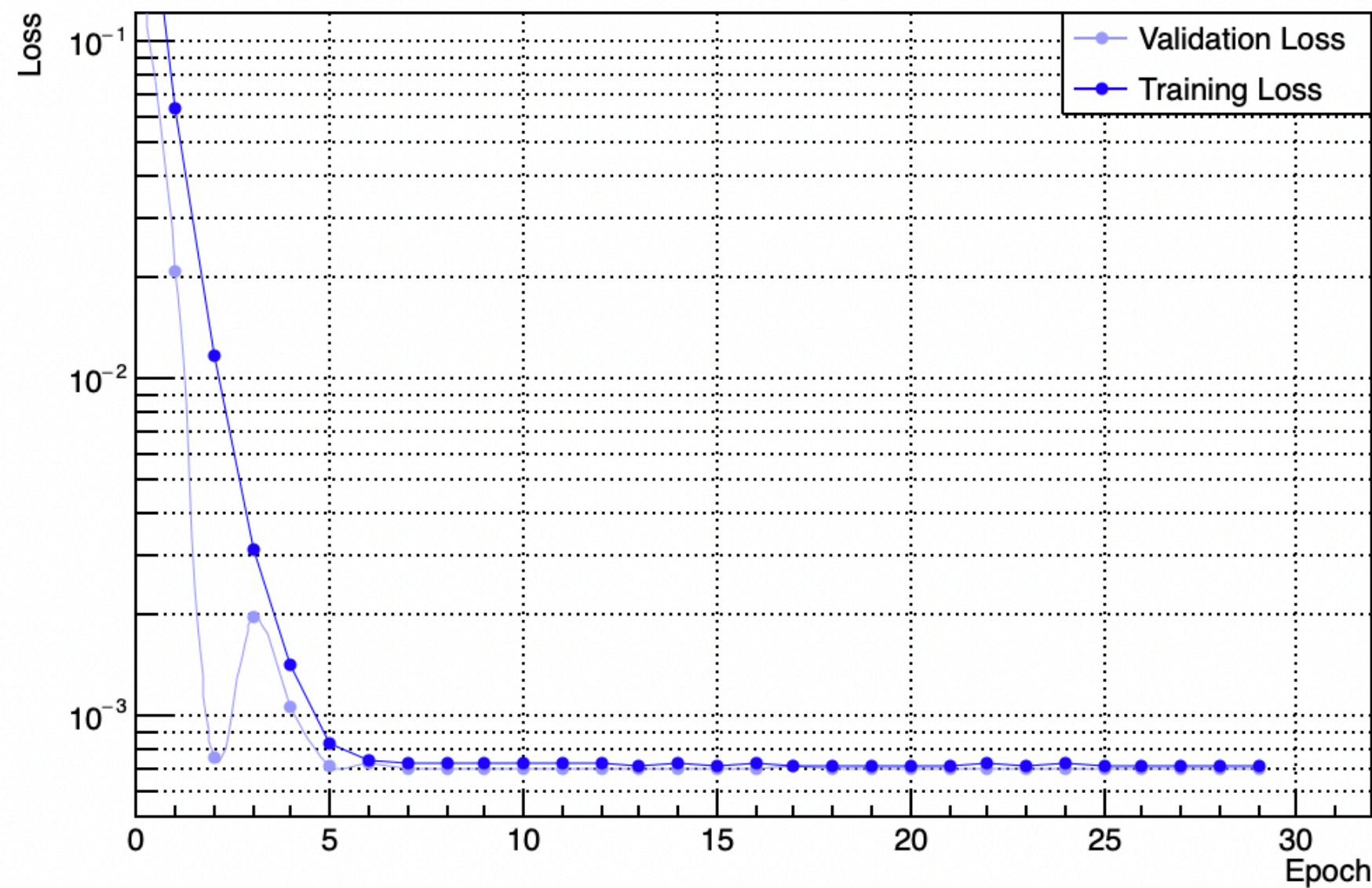
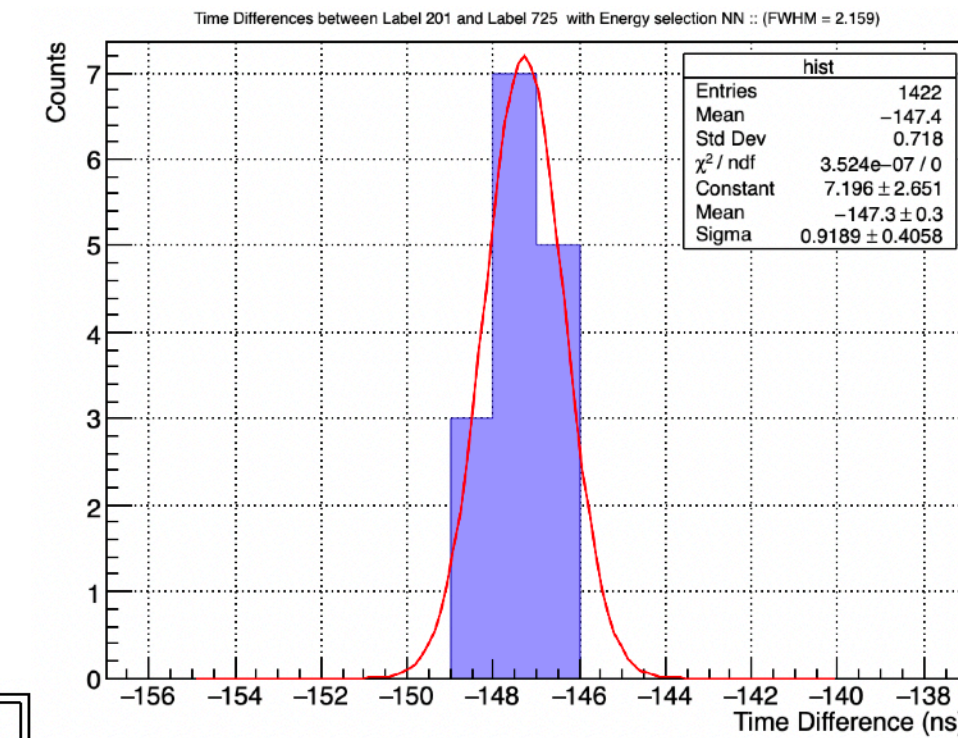
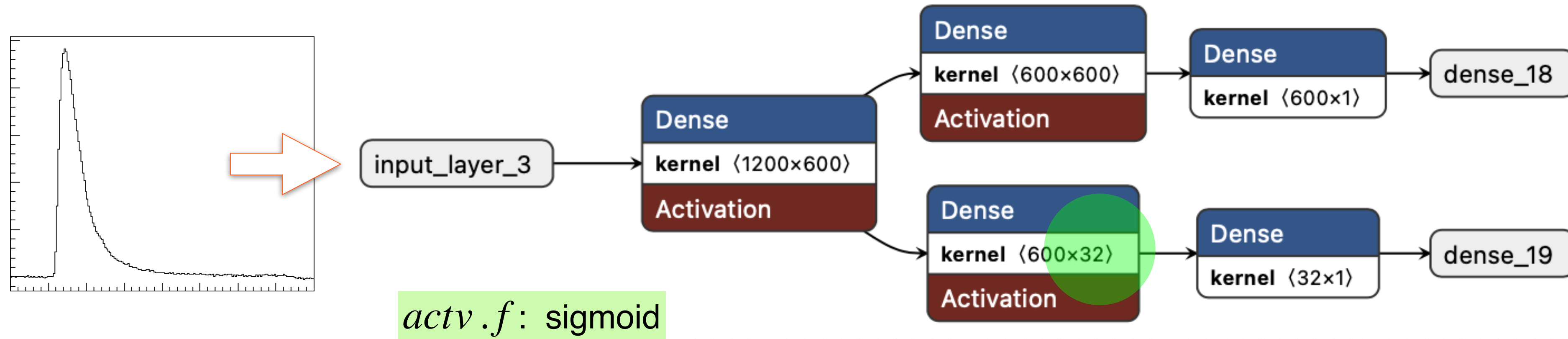


# FCNN models for trace analysis





# FCNN models for trace analysis



31.7 keV @ 1170 keV  
 $R(t) = 569$  ps

With NN:  
59.6 keV @ 1170 keV  
 $R(t) = 2158$  ps



Supervised vs. unsupervised learning

Regression vs. classification model

### Hyperparameters

Activation function

Batch size

Epochs

Learning rate

Loss function

Number of hidden layers

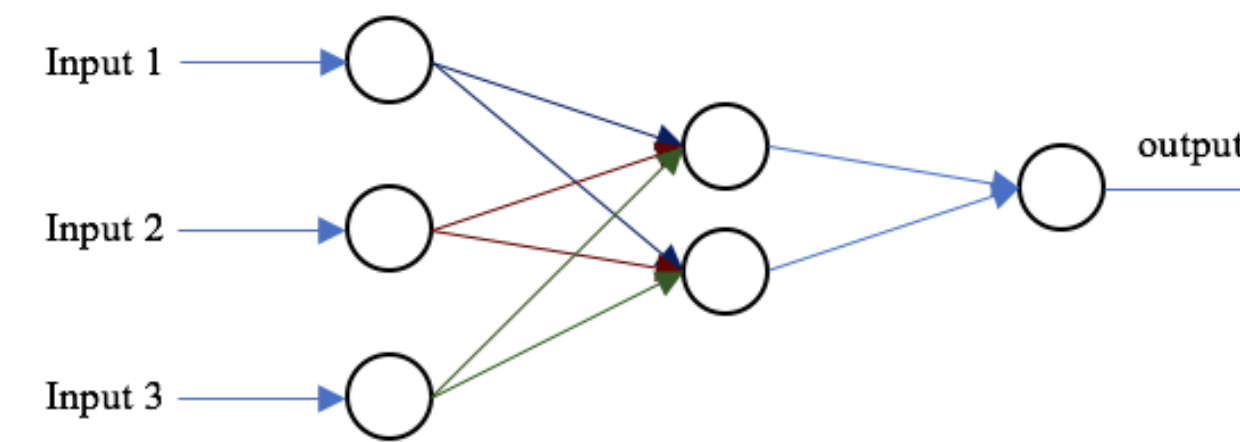
Number of neurons per layer

### Parameters

Weights and biases

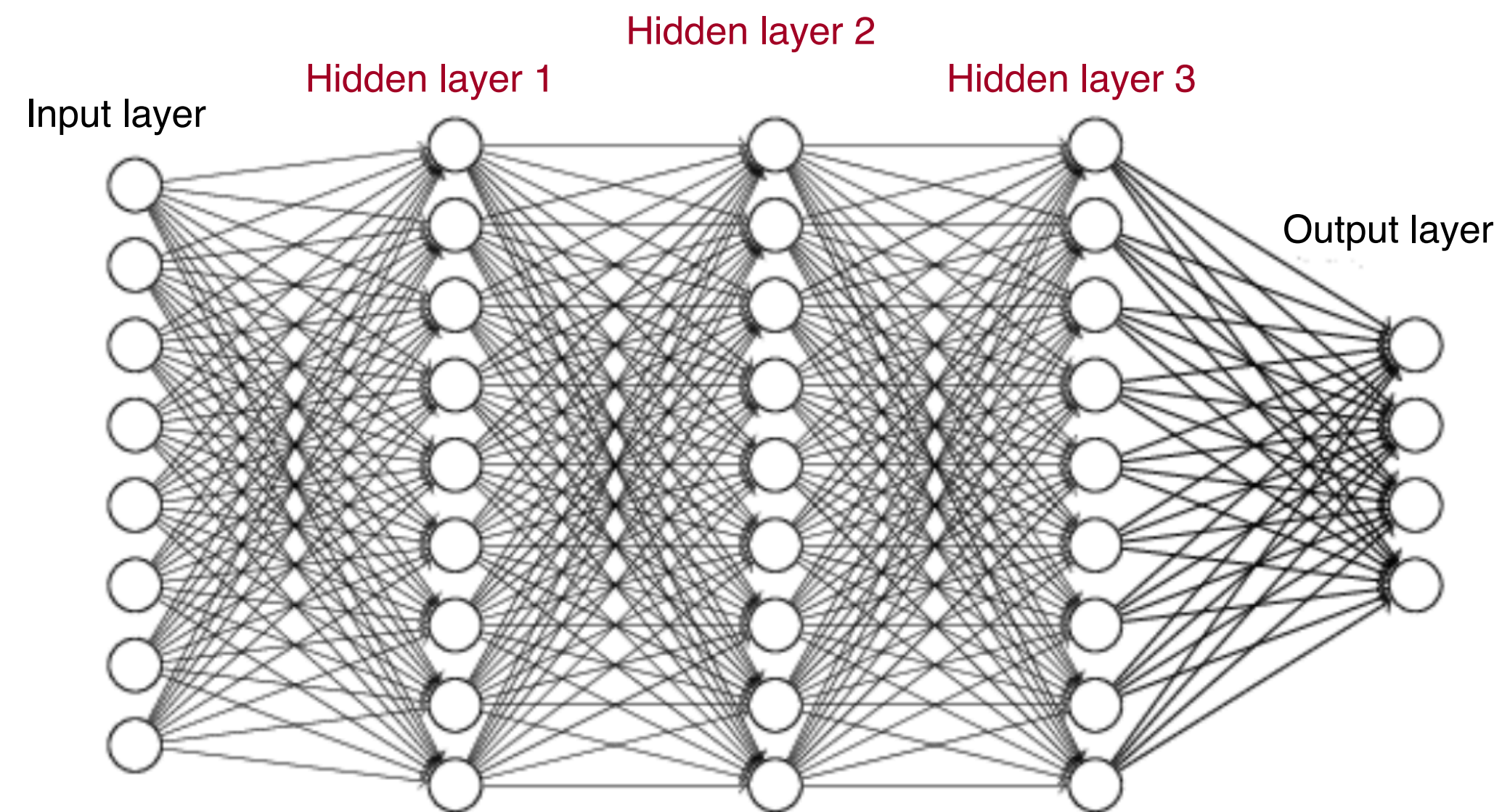
$$Y = \sum_i (weight_i \cdot input_i) + bias$$

## Fully Connected Neural Networks (FCNN)



Input layer      Hidden layer      Output layer

Taken from: A. Said and F. Sayed Ibrahim. Comparative study of segmentation techniques for detection of tumors based on mri brain images. *International Journal of Biochemistry and Biotechnology*, 8:10, 09 2017



Taken from: <https://math.stackexchange.com/q/2048722>



Supervised vs. unsupervised learning

Regression vs. classification model

Hyperparameters

Activation function

Batch size

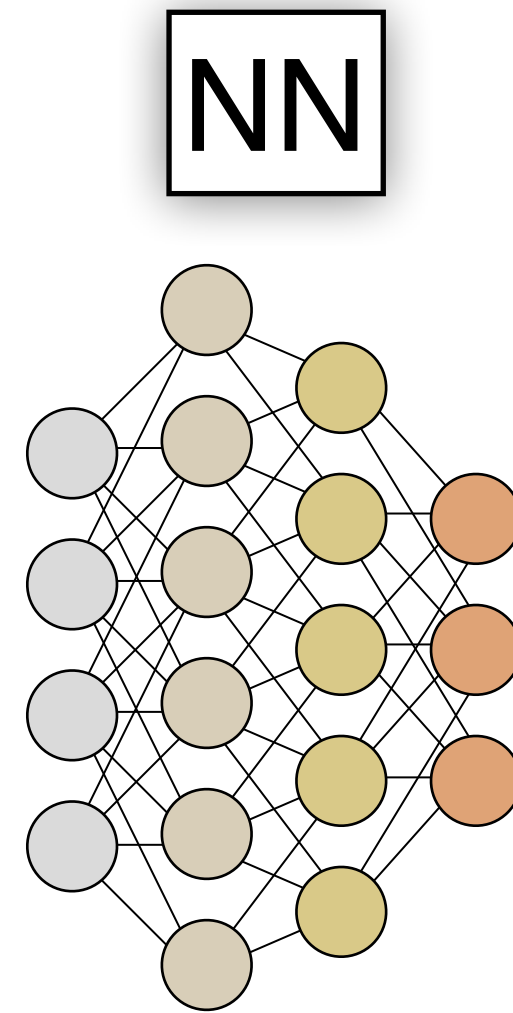
Epochs

Learning rate

Loss function

Number of hidden layers

Number of neurons per layer



Parameters

Weights and biases

**simple NN**

$$Y = \sum_i (weight_i \cdot input_i) + bias$$



Supervised vs. unsupervised learning

Regression vs. classification model

Hyperparameters

Activation function

Batch size

Epochs

Learning rate

Loss function

Number of hidden layers

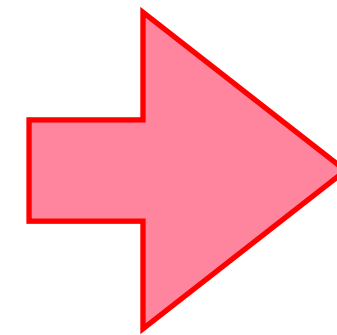
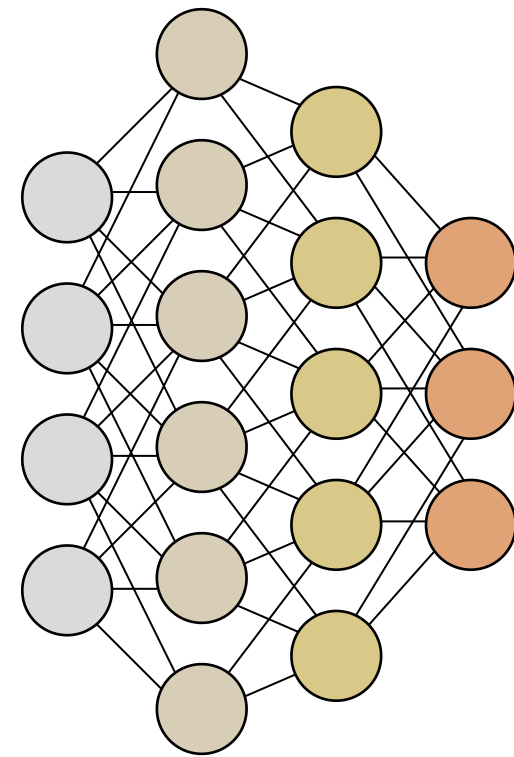
Number of neurons

Parameters

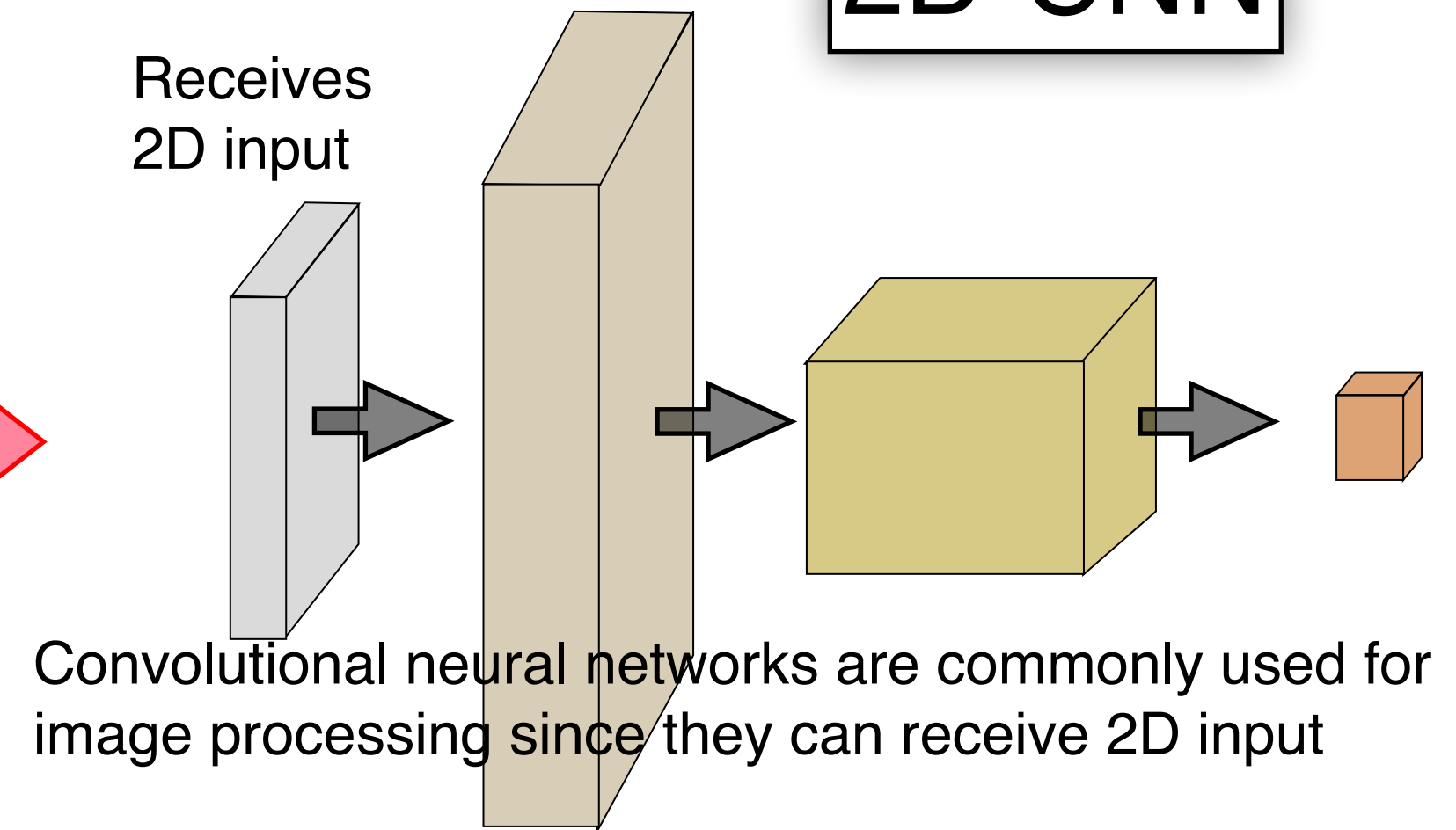
Weights and biases

$$Y = \sum_i (weight_i \cdot input_i) + bias$$

NN



2D-CNN



$$Y_{i,j,k} = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} \sum_{c=0}^{C-1} (X_{i+m,j+n,c} \cdot W_{m,n,c,k}) + bias_k$$



Supervised vs. unsupervised learning

Regression vs. classification model

Hyperparameters

Activation function

Batch size

Epochs

Learning rate

Loss function

Number of hidden layers

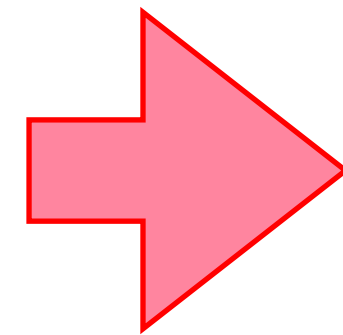
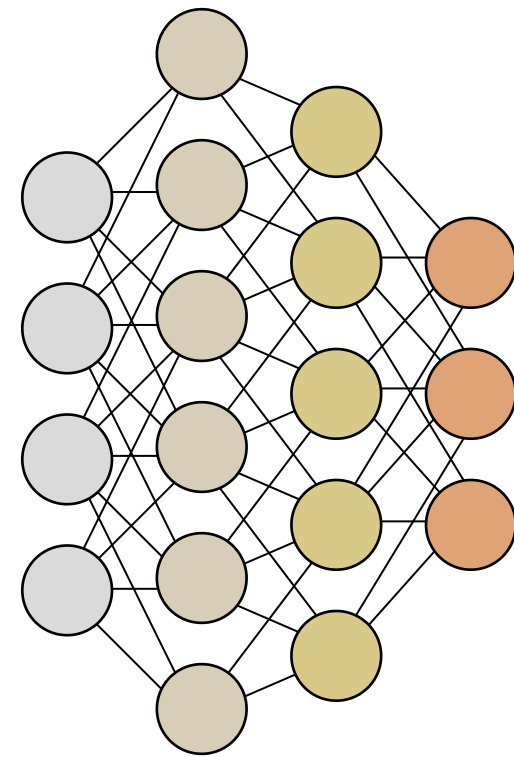
Number of neurons

Parameters

Weights and biases

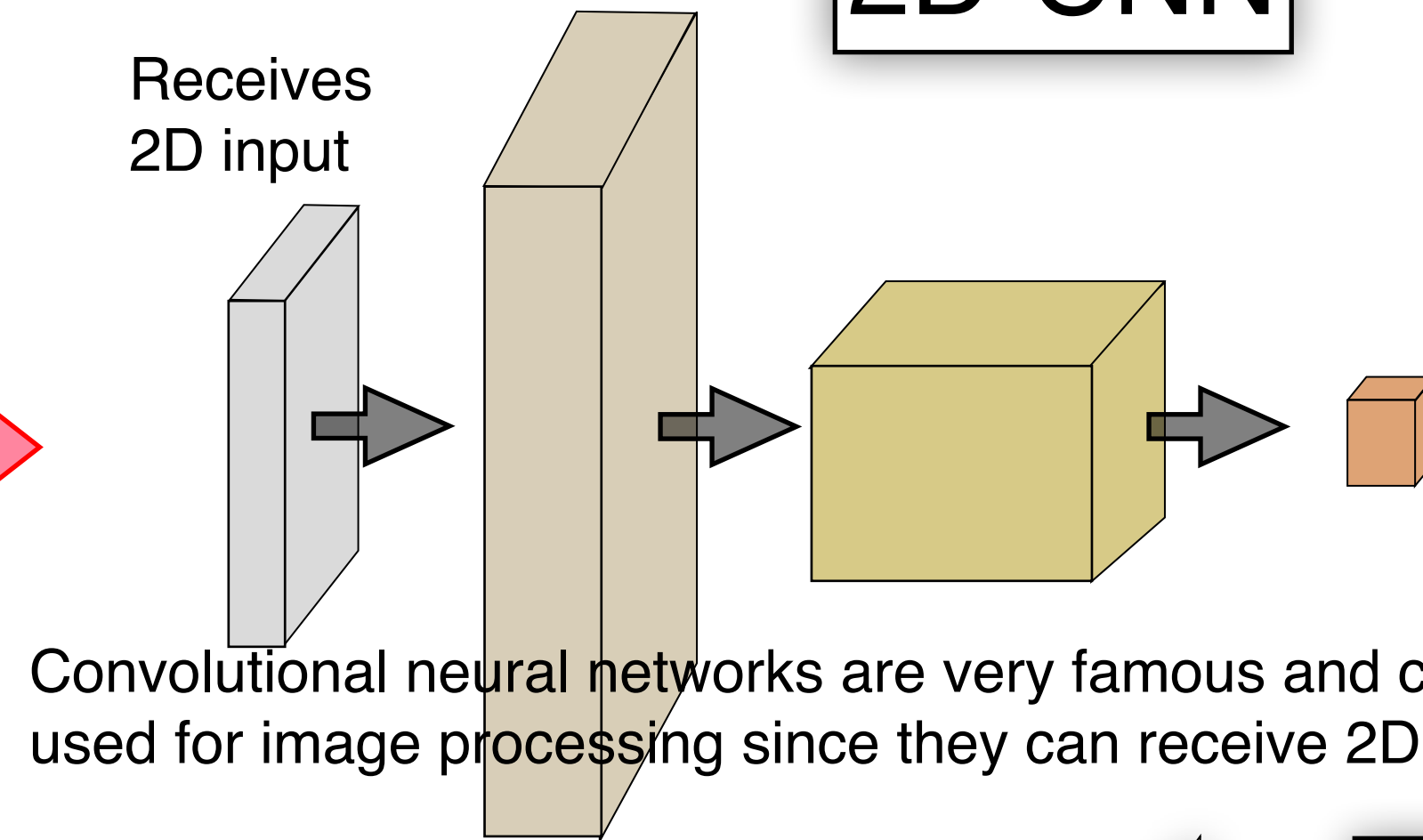
$$Y = \sum_i (weight_i \cdot input_i) + bias$$

**NN**



**2D-CNN**

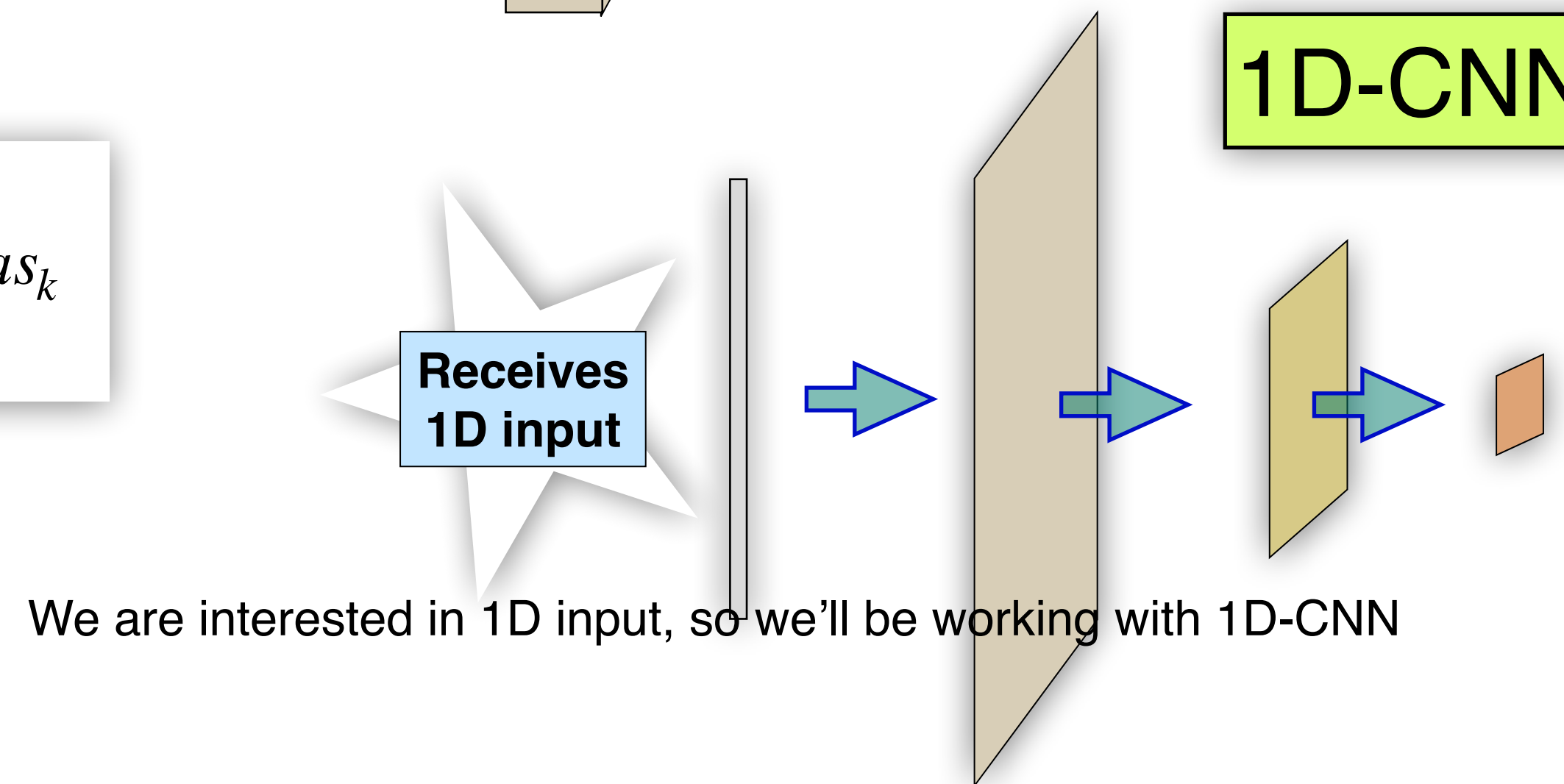
Receives 2D input



Convolutional neural networks are very famous and commonly used for image processing since they can receive 2D input

**1D-CNN**

Receives 1D input



We are interested in 1D input, so we'll be working with 1D-CNN



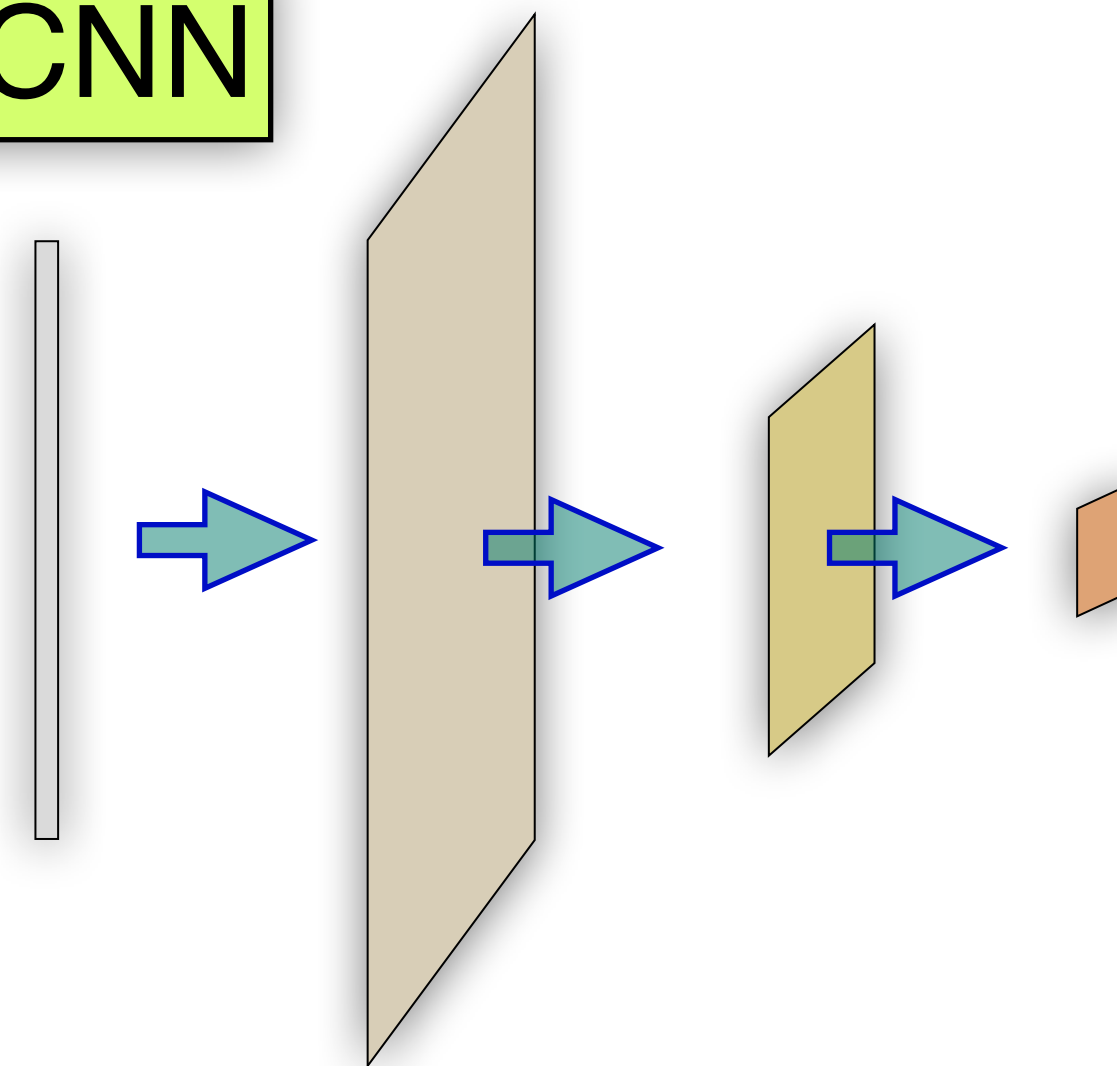
## 1D-CNN

### Parameters

Weights and biases

$$Y_{i,j,k} = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} \sum_{c=0}^{C-1} (X_{i+m,j+n,c} \cdot W_{m,n,c,k}) + bias_k$$

Kernel size vs. filters





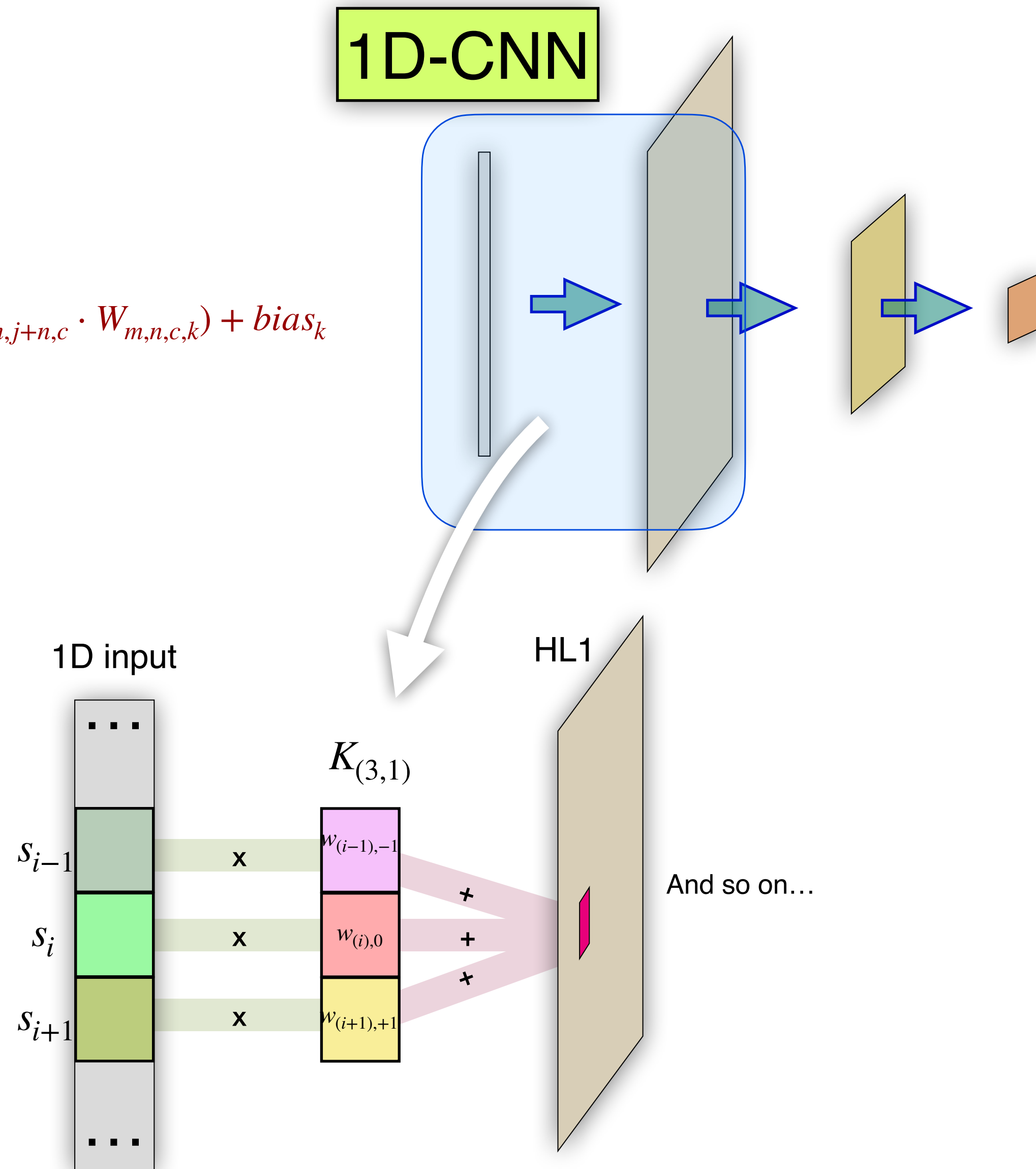
## Parameters

Weights and biases

$$Y_{i,j,k} = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} \sum_{c=0}^{C-1} (X_{i+m,j+n,c} \cdot W_{m,n,c,k}) + bias_k$$

## Kernel size vs. filters

- Kernel size  $K_{(n,m)}$
- Number of filters







## 1D-CNN

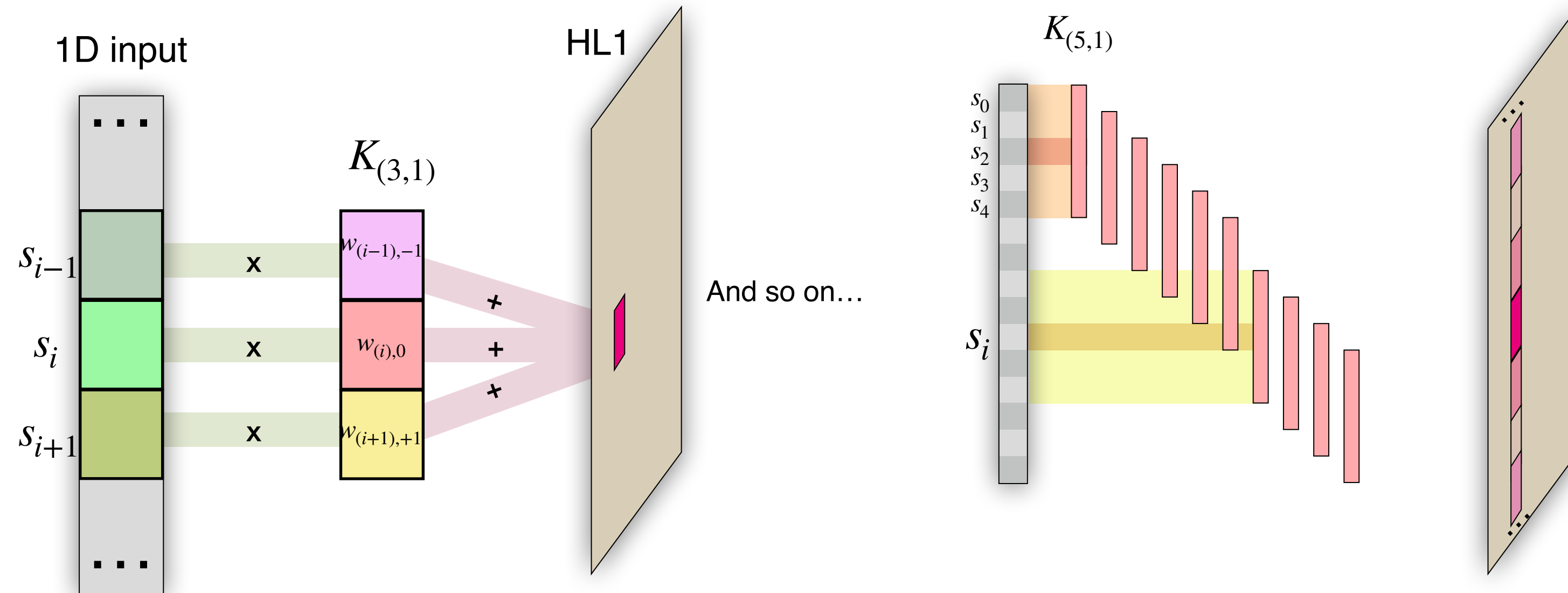
### Parameters

Weights and biases

$$Y_{i,j,k} = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} \sum_{c=0}^{C-1} (X_{i+m,j+n,c} \cdot W_{m,n,c,k}) + bias_k$$

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## 1D-CNN

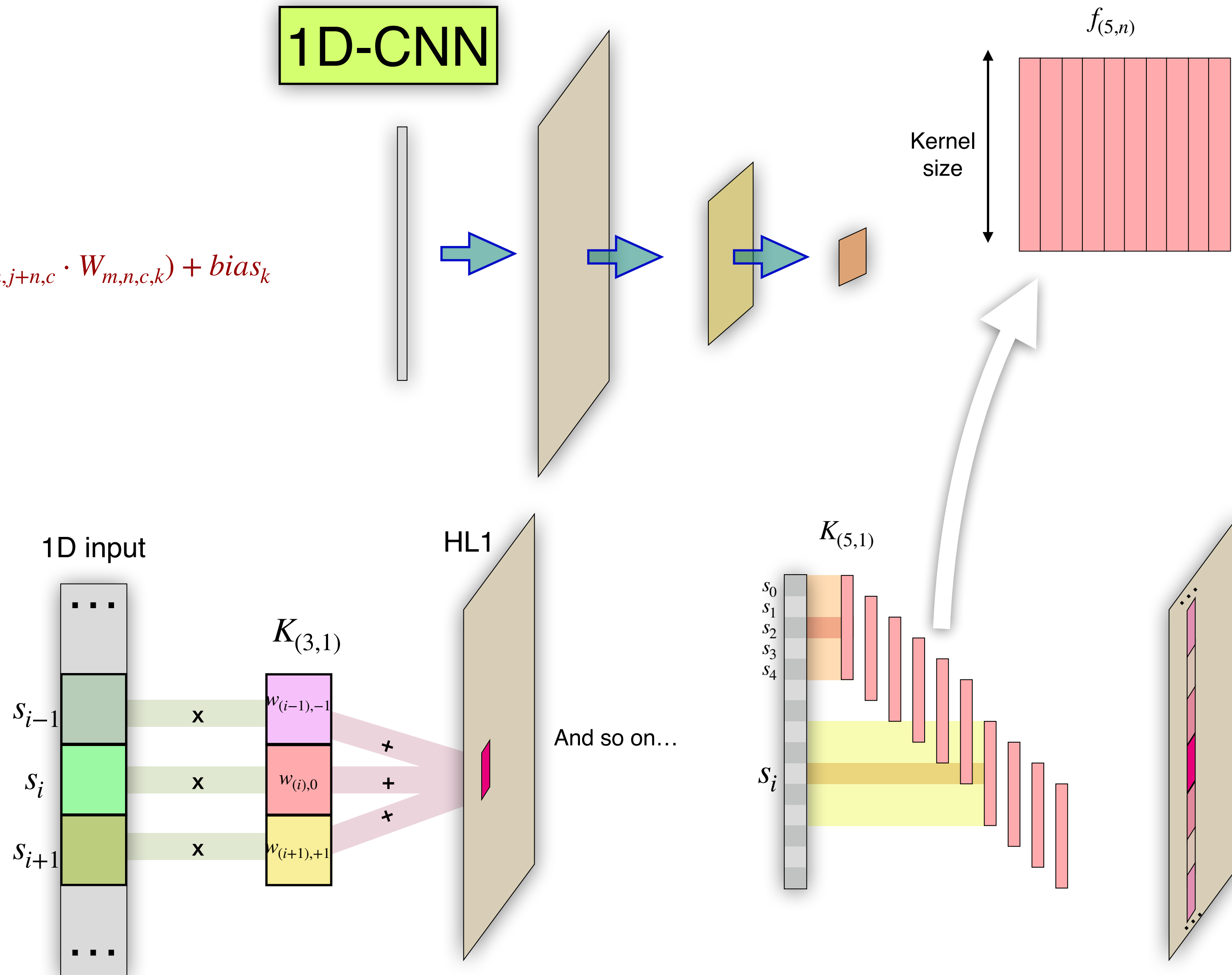
### Parameters

Weights and biases

$$Y_{i,j,k} = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} \sum_{c=0}^{C-1} (X_{i+m,j+n,c} \cdot W_{m,n,c,k}) + bias_k$$

### Kernel size vs. filters

- Kernel size  $K_{(n,m)}$
- Number of filters





## 1D-CNN

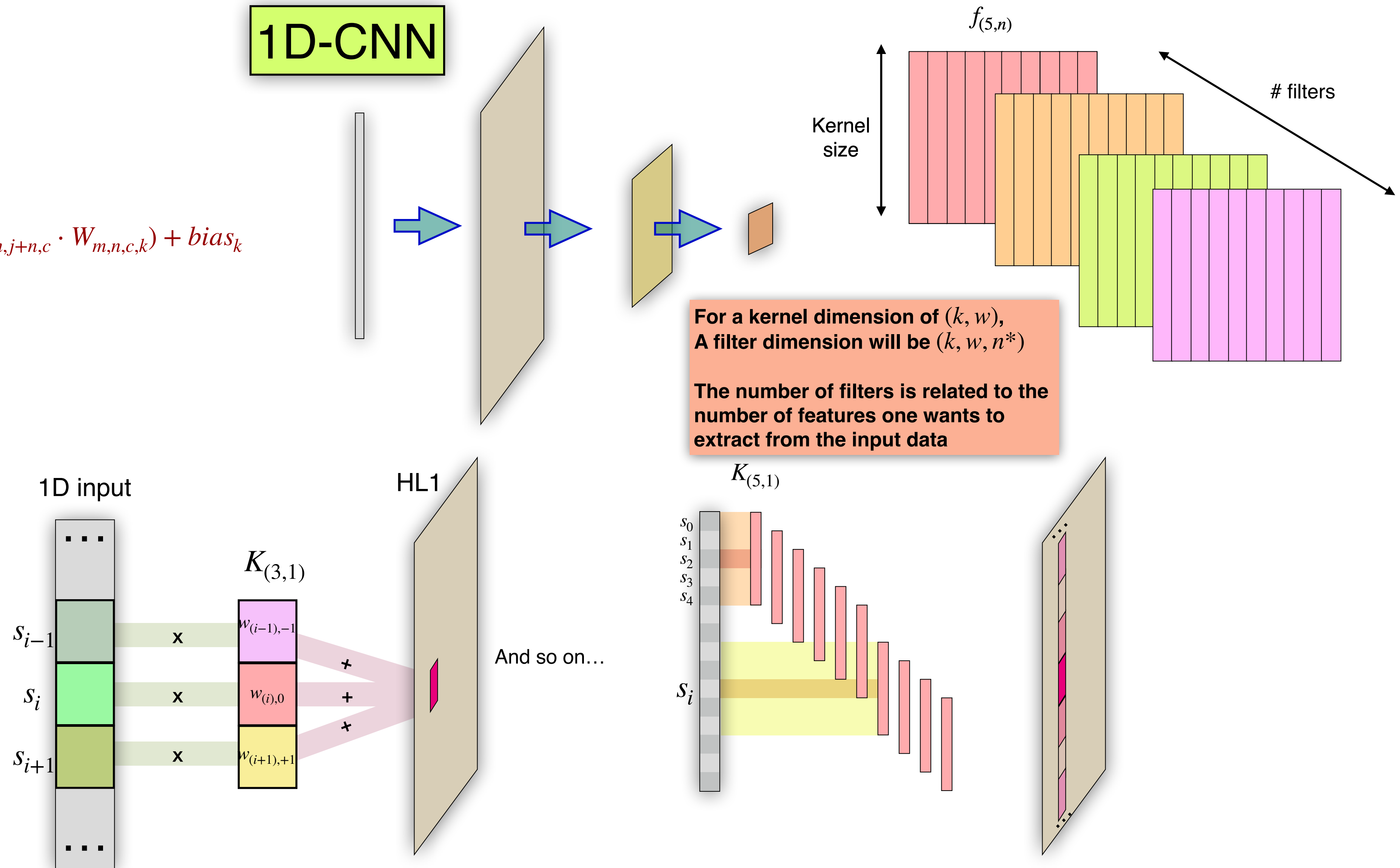
### Parameters

Weights and biases

$$Y_{i,j,k} = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} \sum_{c=0}^{C-1} (X_{i+m,j+n,c} \cdot W_{m,n,c,k}) + bias_k$$

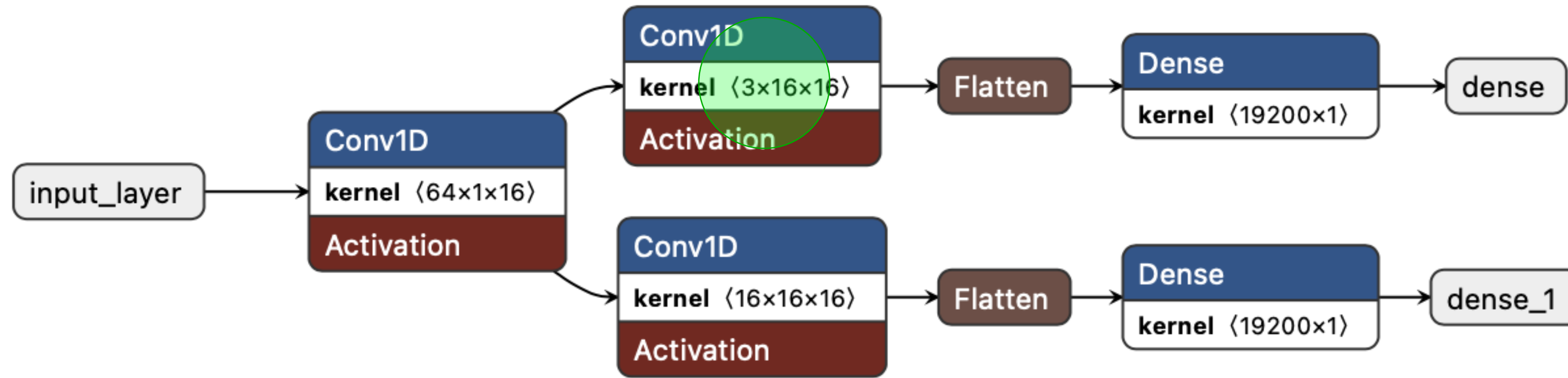
### Kernel size vs. filters

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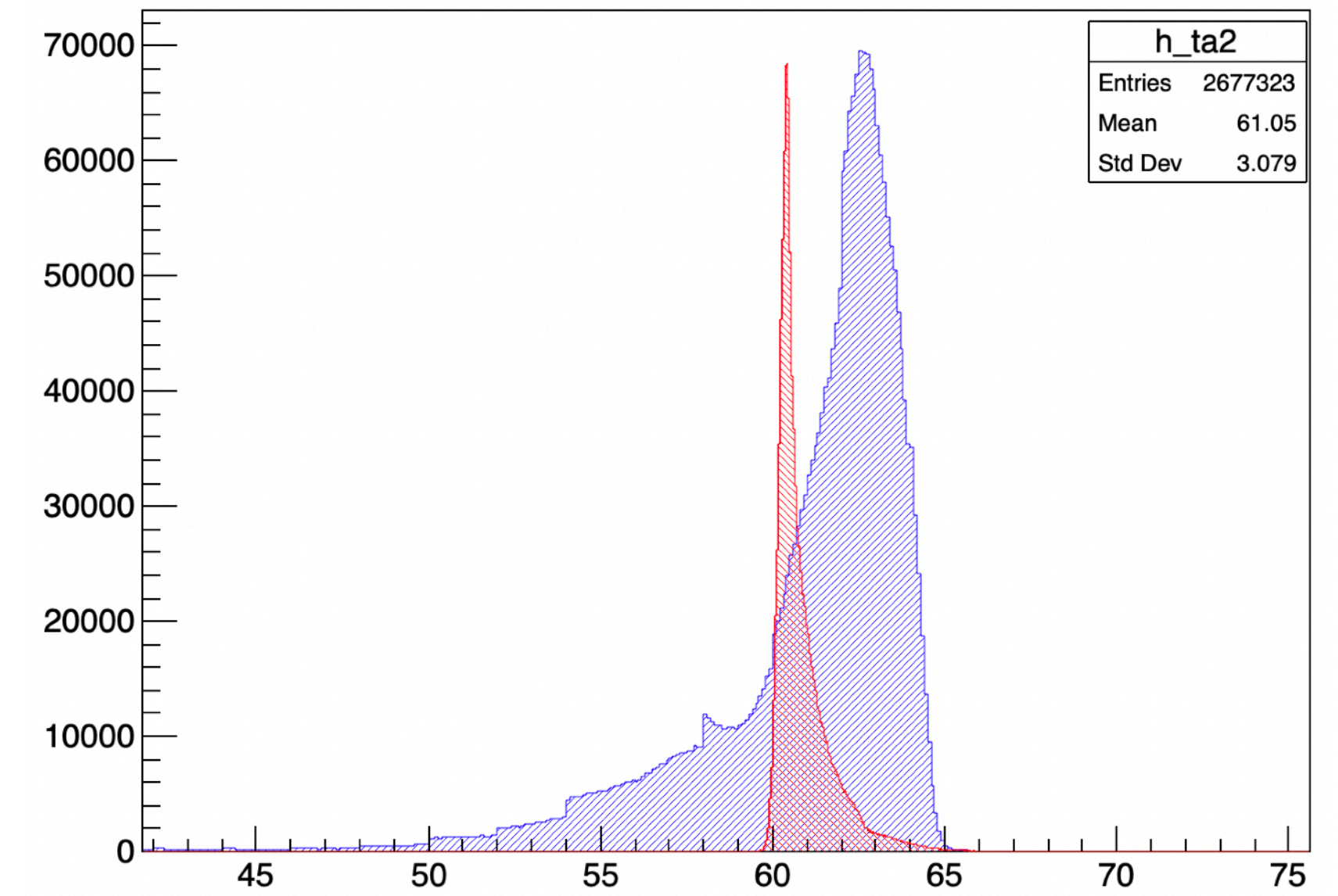
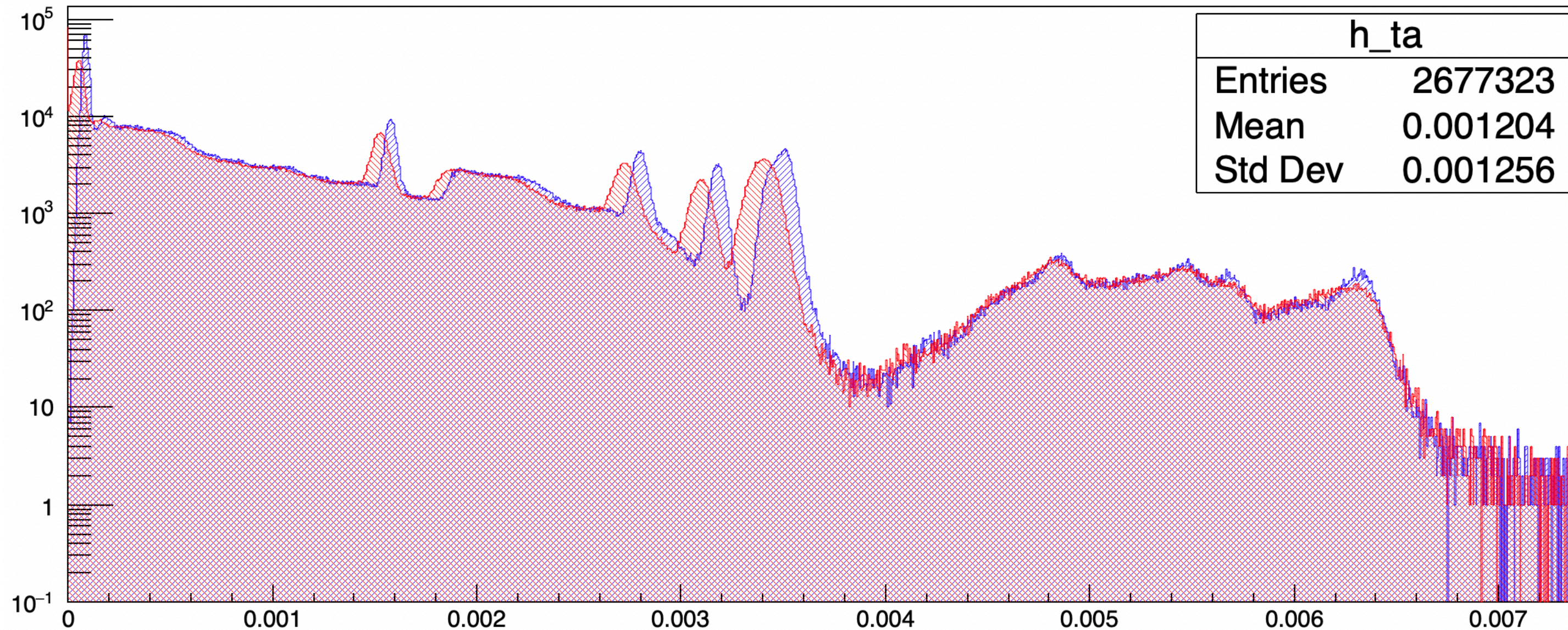




# CNN 1D models for trace analysis



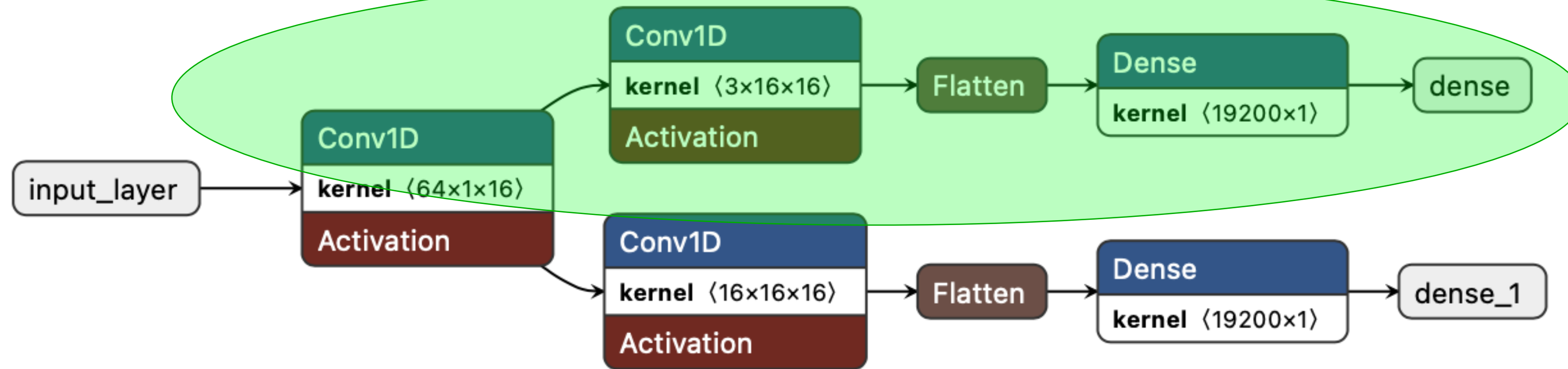
*actv.f*: ReLu





# CNN 1D models for trace analysis

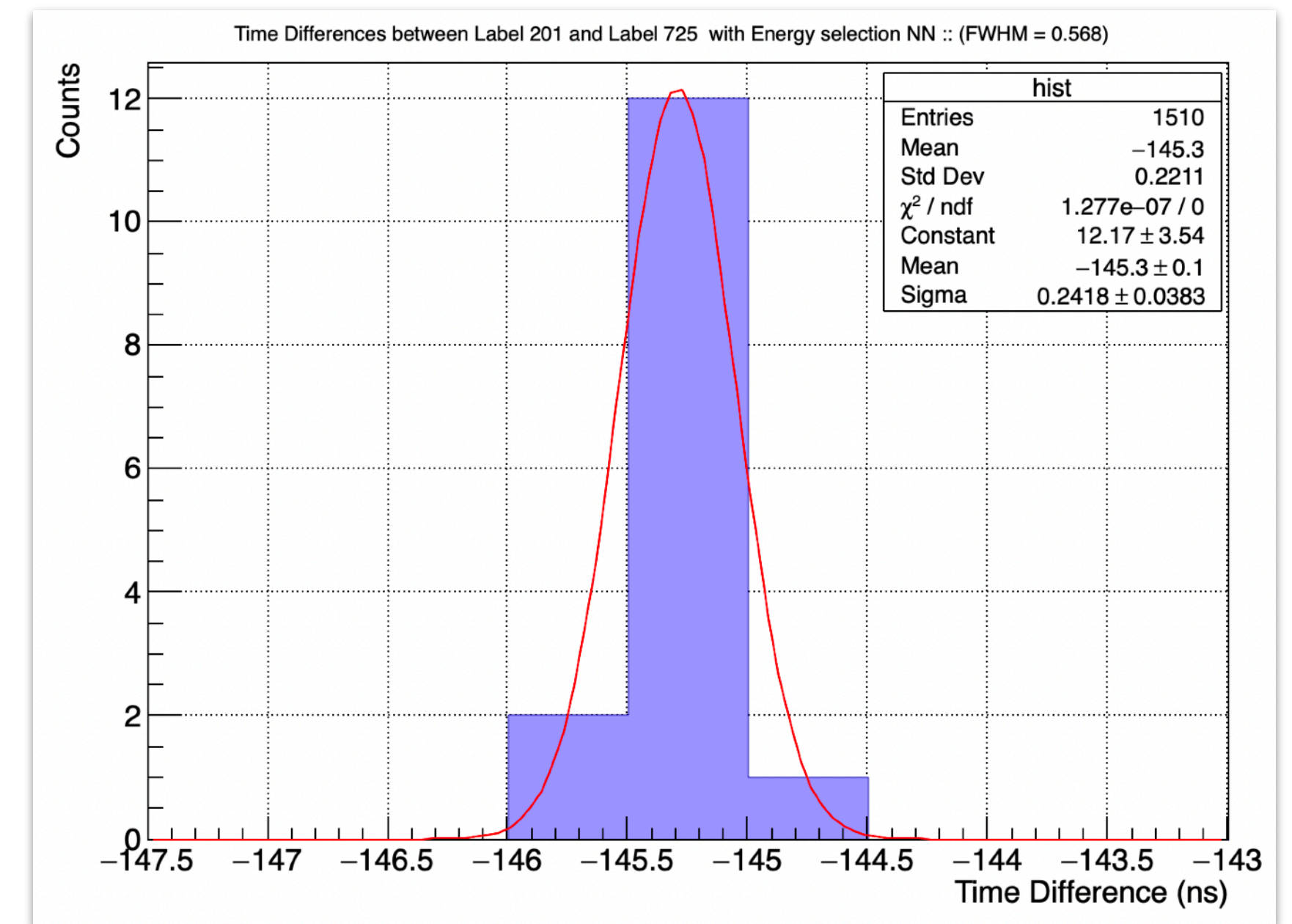
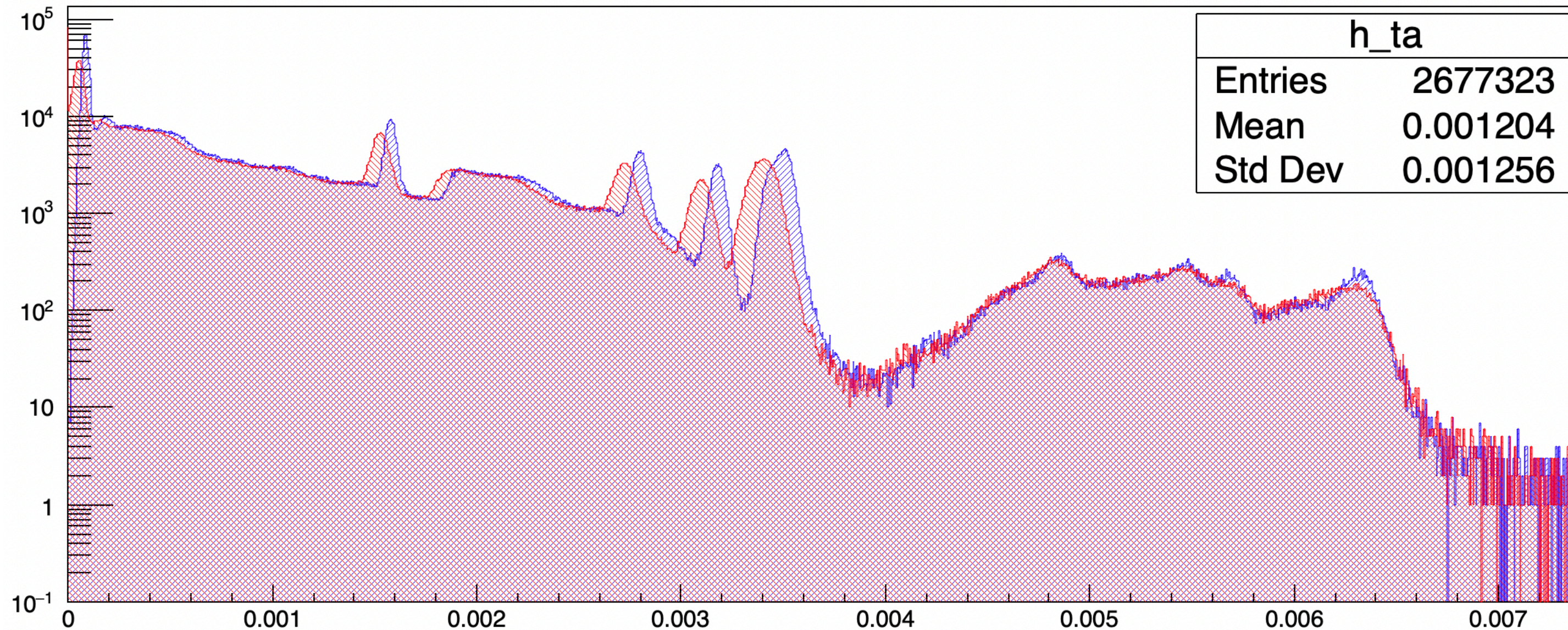
Best time result for kernel size close to signal rise time (size 3 -> 6 ns)



31.7 keV @ 1170 keV  
 $R(t) = 569$  ps

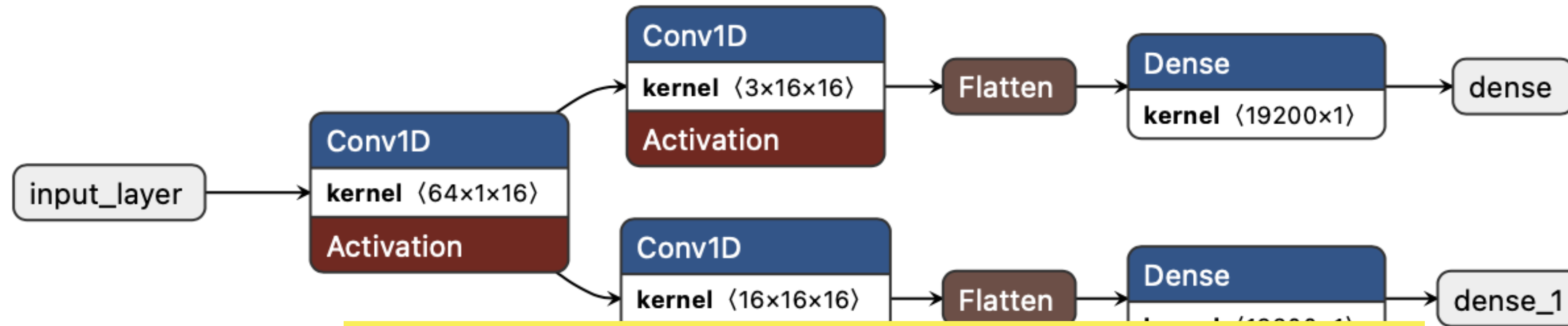
With NN:  
46.4 keV @ 1170 keV  
 $R(t) = 568$  ps

*actv .f*: ReLu





# CNN 1D models for trace analysis

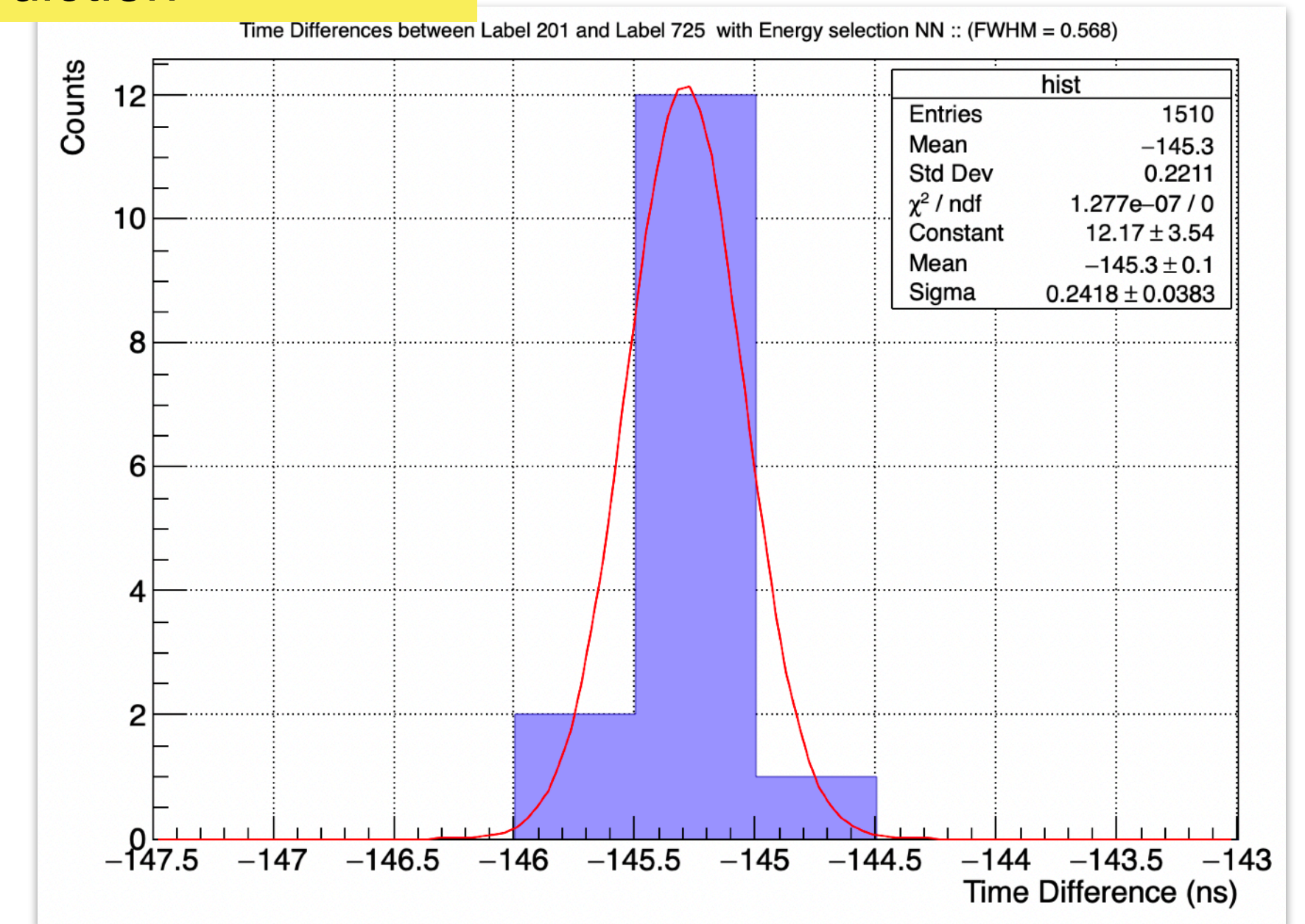
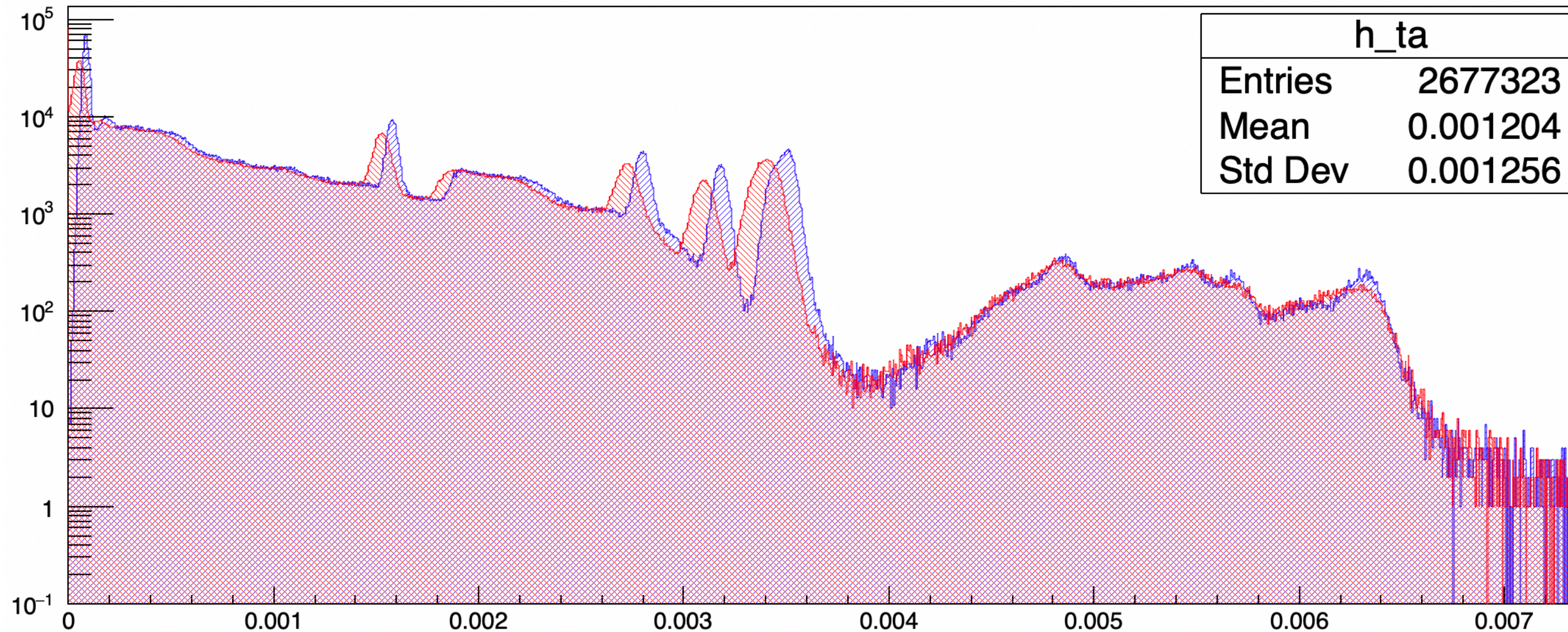


31.7 keV @ 1170 keV  
 $R(t) = 569$  ps

**With NN:**  
**46.4 keV @ 1170 keV**  
 $R(t) = 568$  ps

*actv.f*: ReLu

New step: new CNN or FCNN model with sigmoid activation function for « energy » value prediction



## Short term

- Converge for a more robust NN model for trace analysis
- Implement the model for dFGIC adapting the hyperparameters
- Detailed evaluation of computational costs
  - Prediction time
  - Number and complexity of operations ...
- $\nu$ -Ball2 finish calibration and get resolutions/efficiencies

## Long term

- Develop new AI algorithms for fission trigger based on  $\nu$ -Ball2 response function
- Evaluate the correlation between fission observables such as energy and multiplicity of neutrons and gammas for fission recognition

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# Constant Fraction Discrimination (CFD)

## CFD CONSTRAINT:

$$t_{delay} > t_r \cdot (1 - f),$$

where  $t_r$  is the signal rise time

### Constant Fraction Discrimination (CFD)

