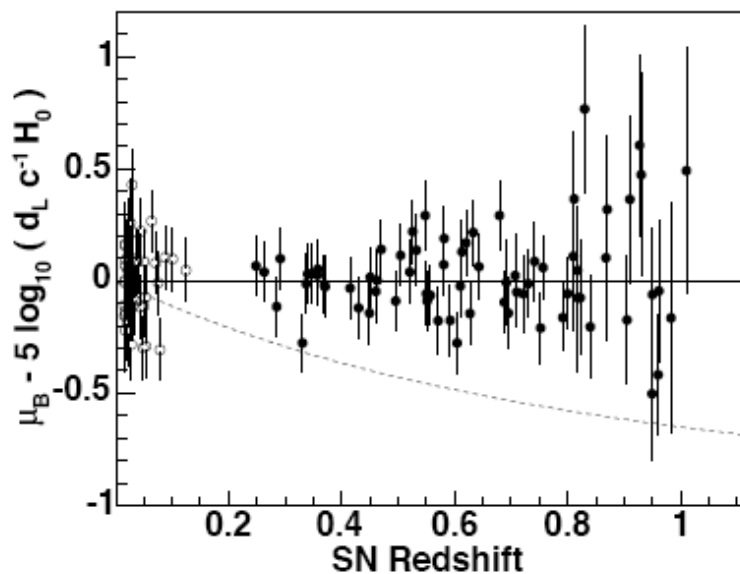
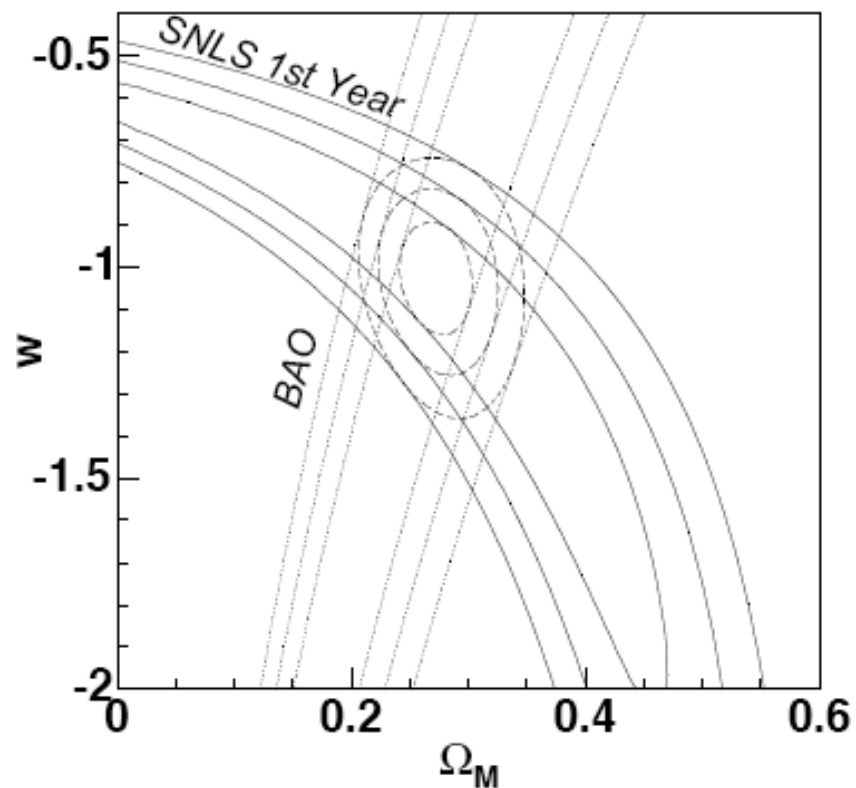
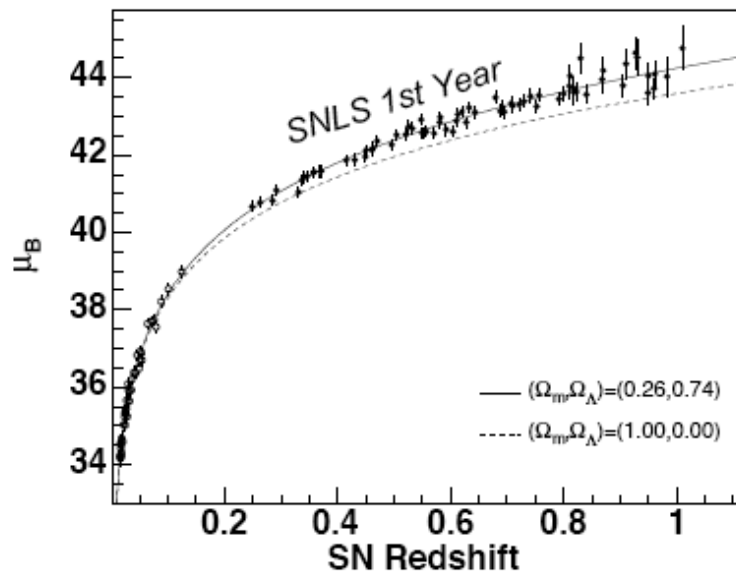




Gravitational lensing of SNLS the Supernova

# First Year Results from CFHT SNLS

Astier et al (astro-ph/0510447)



**Goal:** measure the dark energy equation of state

71 homogeneously studied SNe Ia

$$w = -1.023 \pm 0.090$$

# Gravitational lensing

One of the consequences of GR is that light rays are deflected by gravity

Gravitational lensing depends solely on the projected, two-dimensional mass distribution of the lens, and is independent of the luminosity and the composition of the lens.



Ideal way to detect and study dark matter

# The thin screen approximation

Valid when the distance between observer and lens and lens and source is much bigger than the size of the lens

The mass of the lens is projected onto a mass sheet orthogonal to the line-of-sight

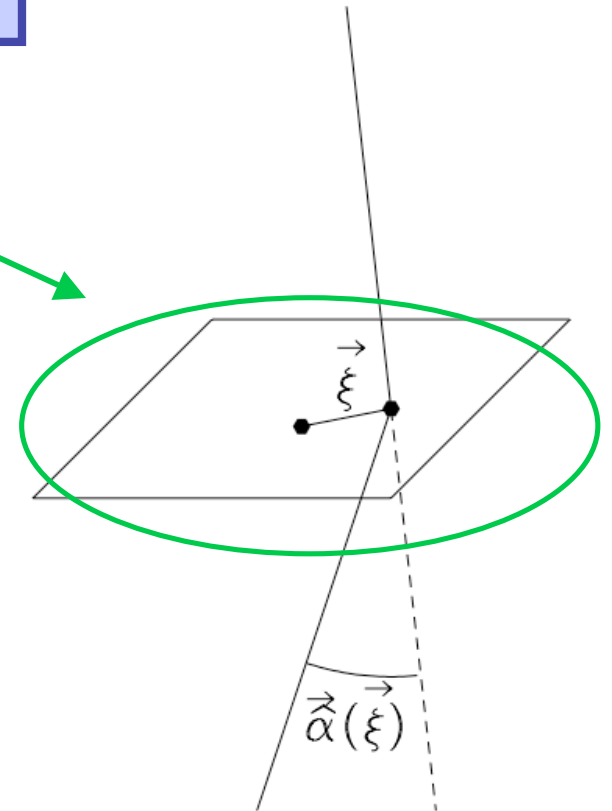
= lens plane

Surface mass density

$$\Sigma(\vec{\xi}) = \int \rho(\vec{\xi}, z) dz$$

Sum of deflection angles due to all mass elements in the plane

$$\vec{\hat{\alpha}} = \frac{4G}{c^2} \int d^2\xi' \Sigma(\vec{\xi}') \frac{\vec{\xi} - \vec{\xi}'}{|\vec{\xi} - \vec{\xi}'|^2}$$



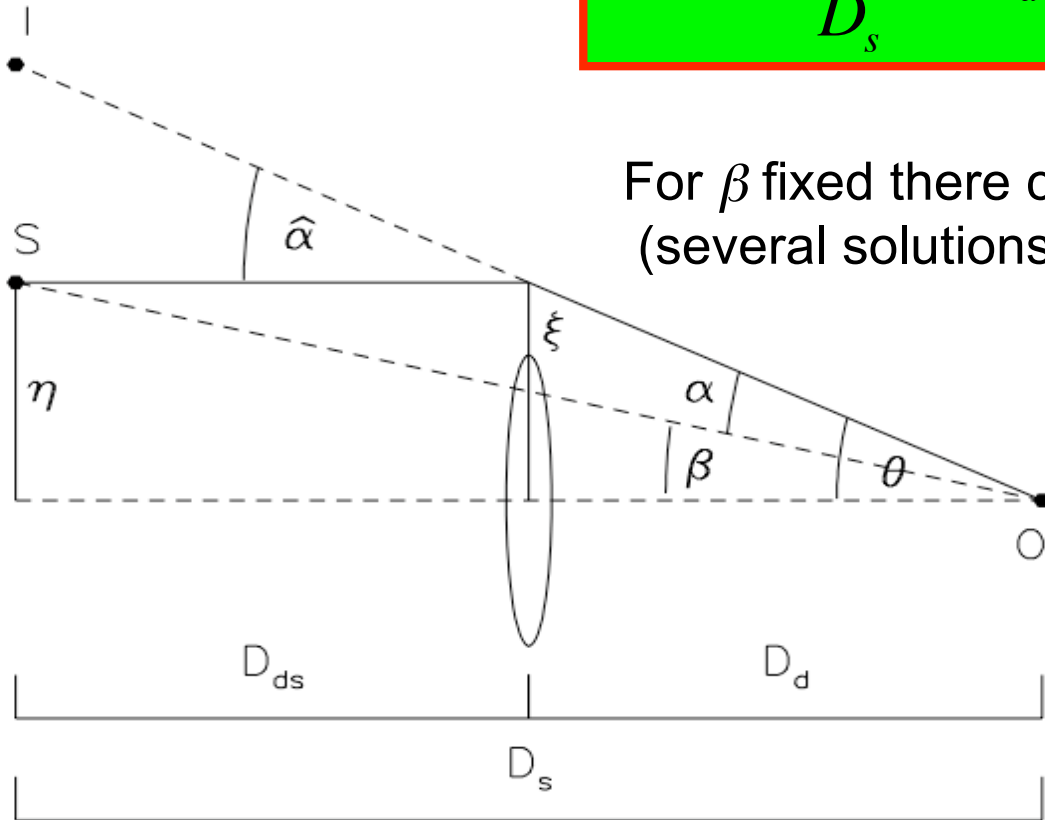
# The lens equation

$$\vec{\xi} = D_d \vec{\theta}$$

$$\vec{\eta} = D_s \vec{\beta}$$

$$\vec{\beta} = \vec{\theta} - \frac{D_{ds}}{D_s} \hat{\alpha}(D_d \vec{\theta}) = \vec{\theta} - \hat{\alpha}(\vec{\theta})$$

For  $\beta$  fixed there can be several positions in the sky  
(several solutions)



Multiple images

Jacobien matrix of the lens equation

$$A(\vec{\theta}) = \frac{\partial \vec{\beta}}{\partial \vec{\theta}}$$



Magnification factor

$$\mu = \frac{1}{\det A}$$

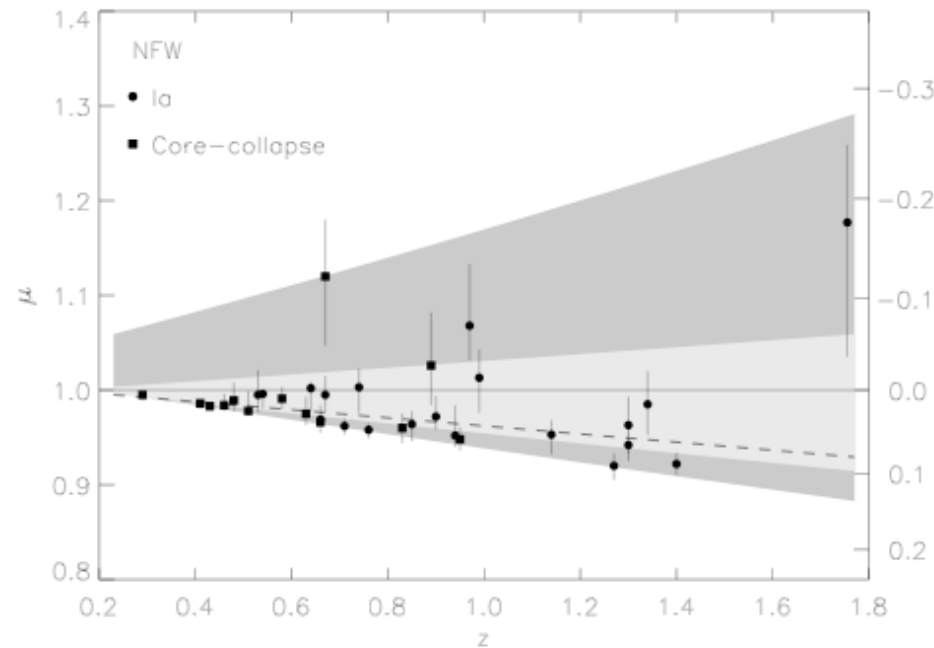
# Why is this interesting for us?

The light from a supernova will experience gravitational lensing due to galaxies, clusters or other matter densities in the line-of-sight and this will cause an additional dispersion in the observed source luminosities

Most of the SNe are demagnified and some are significantly magnified

## Questions to be addressed:

- Can the intrinsic scatter in the Hubble diagram be further reduced?
- Is it possible to detect a correlation between residuals and magnification?
- Is it possible to say something about the dark matter distribution of the galaxies?



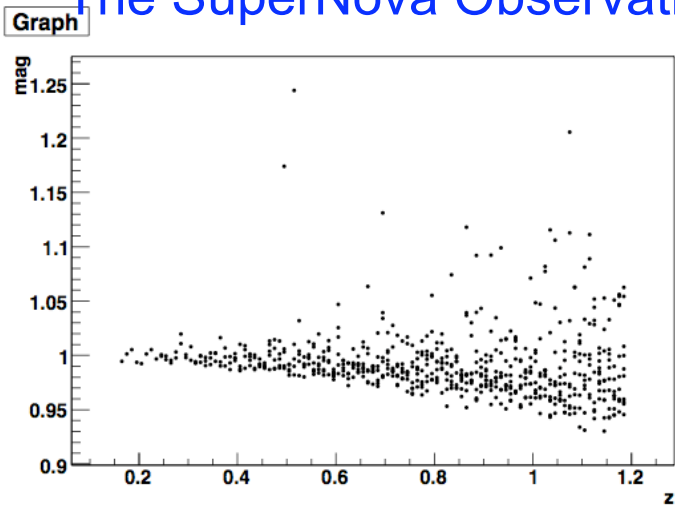
*Jonsson et al. 2006*

# First estimate (a feasibility check)

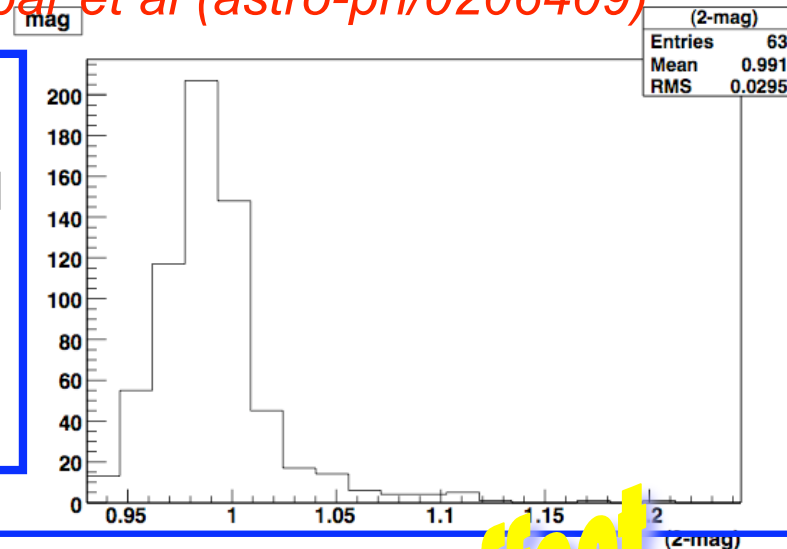
700 simulated type Ia SNe using SNLS SNe observations  
(Astier et al 2006)

Magnification of each supernova is estimated using SNOOC

The SuperNova Observation Calculator *Goobar et al (astro-ph/0206409)*



Most SNe are demagnified and some are significantly magnified



## Cosmological results

$\delta\Omega_M$  and  $\delta w$  due to lensing  $\sim 2-3\%$

Uncertainties due to lensing  $\sim 1-2\%$

small effect

$$w = w_0 + w'(a - a_0) \rightarrow$$

Lensing accounts for **7.5%** of the dark energy task force figure of merit

# Is it possible to detect a signal ?

Expected standard candle  
brightness  
(calculated from a cosmological model)

## Correlation

Magnification

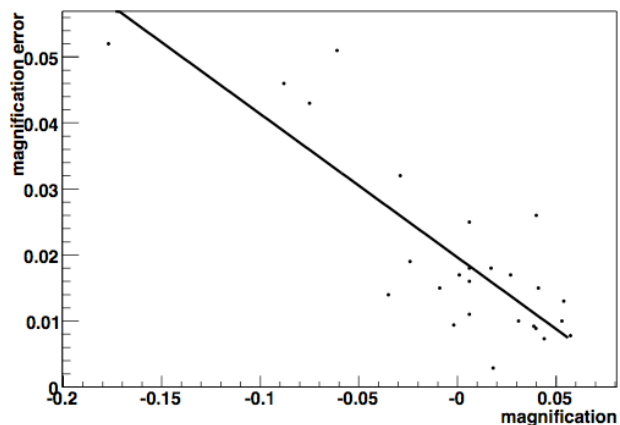


## Plots of residuals vs magnification

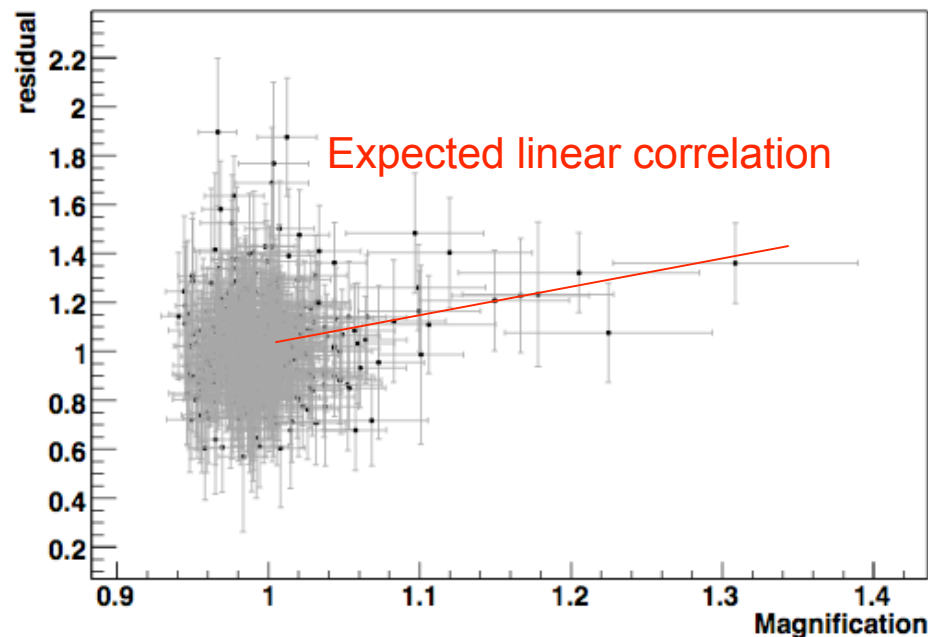
For estimations of the magnification errors, a work on the GOODS fields has been used

*(Jonsson et al astro-ph/0612324)*

Graph



Graph





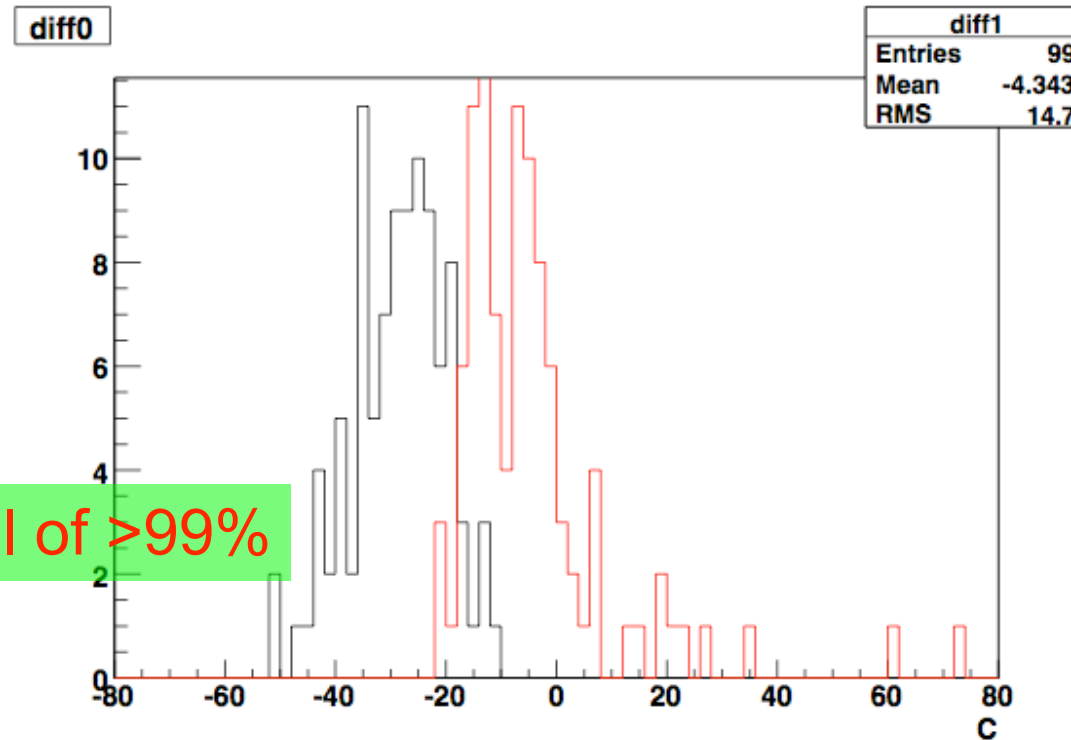
# Likelihood ratio

$$C = \chi^2(\text{no correlation}) - \chi^2(\text{linear correlation})$$

2 different samples:  
-with lensing effects  
-without lensing effects



Confidence level of >99%



# **ANALYSIS OF THE SNLS DATASET**

# Analysis chain

## Actual data

Galaxy catalogue including magnitudes in the g r i (u) and z - bands + photometric redshift

Using PEGASE : a UV to NIR spectral evolution model of galaxies

- type
- absolute magnitudes
- all sorts of things

Galaxy type + B-band absolute magnitude

Using Q-LET, a multiple lens plane algorithm which calculates the magnification with respect to a homogeneous universe

Conversion of luminosity into velocity dispersions or virial masses using results based on galaxy-galaxy lensing or the Faber-Jackson / Tully-Fisher relations.

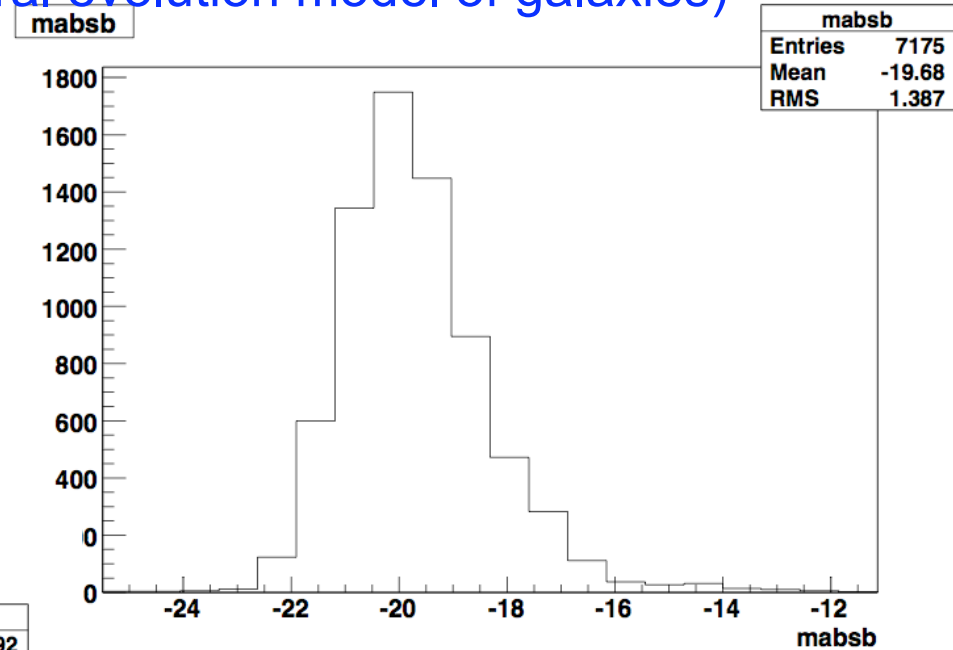
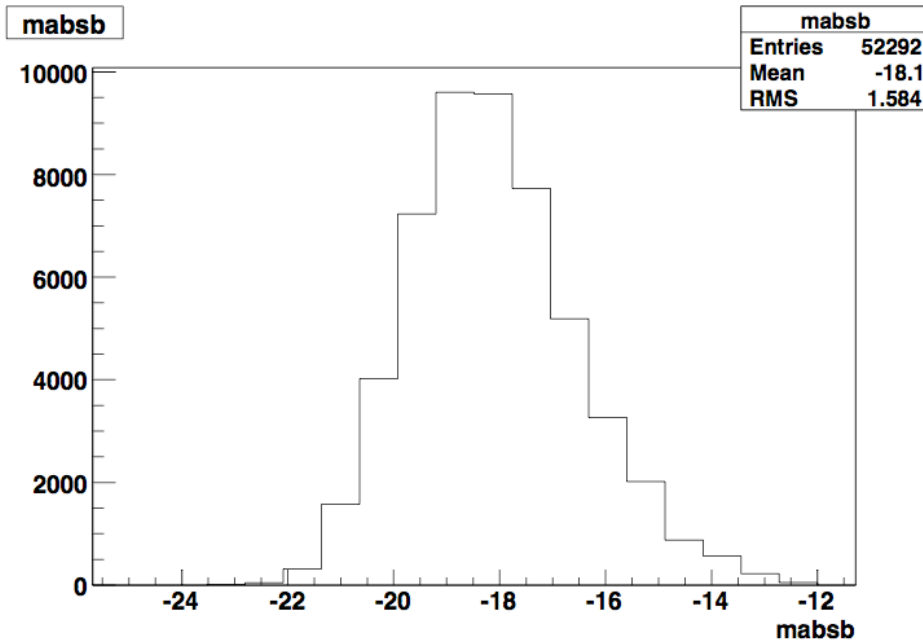
Estimation of the mass of the galaxy using galaxy models like SIS or NFW  
Estimation of the eta-parameter

Estimation of the magnification of each SNe

# Pegase (a UV to NIR spectral evolution model of galaxies)

-Photometric redshift code

-Fits redshifted spectral templates



templates



Absolute B-band magnitudes

# Conversion of luminosity into velocity dispersion or virial mass

2 promising methods:

Galaxy-galaxy lensing

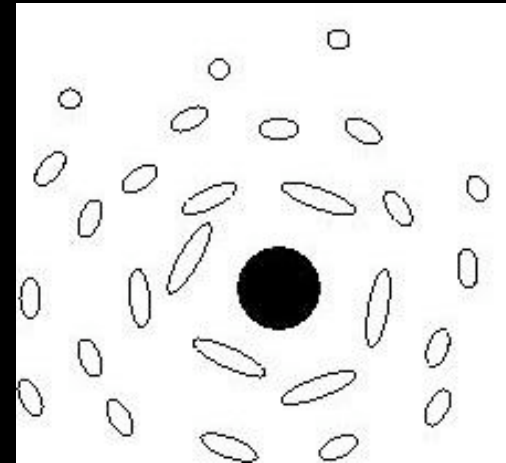
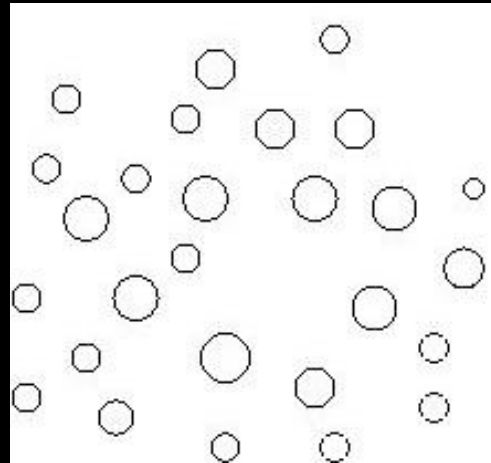
Faber-Jackson / Tully-Fisher relations

Investigation of 5 different papers and their results  
(3 galaxy-galaxy lensing papers and 2 FJ/TF papers)

Hoekstra et al. 2004/2005 RCS    Bohm et al. (2004) FORS Deep Field  
Kleinheinrich et al. 2005 COMBO-17    Mitchell et al. (2005) SDSS

# Galaxy-galaxy lensing

Images of background galaxies are distorted by foreground galaxies.



Tangential ellipticity is proportional to tangential shear,  $\gamma_t$

$$\gamma_t = \epsilon_t$$

Shear is a measure of the total mass (dark and luminous)

$$\gamma_t(r) \sim \Sigma(<r) - \Sigma(r)$$

# BUT

One can only study ensemble averaged properties, because the weak lensing signal induced by an individual galaxy is too low to be detected.

Measured quantity = the **mean** tangential shear divided into angular bins.

Fit the signal with an assumed halo model

NFW

SIS

Extraction of physical properties of the halo such as velocity dispersion and masses.



# Halo models

## SIS Isothermal Sphere

$$\rho(r) = \frac{\sigma_v^2}{2\pi G} \frac{1}{r^2}$$

$$\gamma_T = \frac{2\pi\sigma_v^2}{c^2\theta} \beta$$



Velocity dispersion

## NFW Navarro Frenk White

$$\rho(r) = \frac{\delta_c \rho_c}{(r/r_s)(1+r/r_s)^2}$$

$$M_{vir} = \frac{800\pi}{3} \rho_c r_{vir}^3$$



Virial mass/radius



# Scaling relations

The lensing signal depends on the angular diameter distance between observer, lens and source which is different for each survey.

## What to do?

Answer:

**Scale the results to a fiducial luminosity  $L_*$**

$$\frac{\sigma}{\sigma_*} = \left( \frac{L}{L_*} \right)^\alpha$$

$$\frac{M}{M_*} = \left( \frac{L}{L_*} \right)^\beta$$

$$L_* = 10^{10} h^{-2} L_{B\oplus}$$

# Difficulties

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K-corrections

the fiducial luminosity is given in different bands



3-4%

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The lensing signal is not probed out to the same radius



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Cutoff radius

The models have infinite mass so we must have a cutoff usually referred to as the virial radius/mass or  $r_{200}/m_{200}$



A lot of different definitions

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A lot of different definitions

Selection and contamination

Contamination by groups or clusters  
Different color splits

# The Faber-Jackson/Tully-Fisher relations

The Faber-Jackson or Tully-Fisher relations relates the velocity dispersion and the Luminosity of the galaxy.

F-J relation (ellipticals)  
Mitchell et al. (2005)

$$\log_{10} \sigma = -0.091(M_B - 4.74 + 0.85z)$$

$$L \propto \sigma^\beta$$

30,000 galaxies

T-F relation (spirals)  
Bohm et al. (2004)

$$\log_{10} V_{\max} = -0.134(M_B + 3.61 + 1.22z)$$

$$\sigma = V_{\max} / \sqrt{2}$$

77 galaxies

paper	scaling parameter $\alpha$	$\sigma_*$ km/s
Hoekstra et al. 2004	0.3	$140 \pm 4 \pm 3$
Kleinheinrich et al. full sample	$0.28^{+0.12}_{-0.09}$	$136^{+18}_{-26}$
blue sample (but scale = $150h^{-2}$ kpc)	$0.22^{+0.15}_{-0.15}$	$130^{+30}_{-36}$
red sample (but scale = $150h^{-2}$ kpc)	$0.28^{+0.15}_{-0.12}$	$185^{+24}_{-30}$
Tully-Fischer relation (spirals)	0.33	$115^{+12}_{-10}$
Faber-Jackson relation (ellipticals)	0.23	$149^{+30}_{-29}$

Table 1: Results for the SIS model.

paper	scaling parameter $\beta$	$M_{vir} 10^{11} h^{-1} M_{\odot}$
Hoekstra et al. 2005	$1.5 \pm 0.3$	$5.9^{+1.5}_{-1.3}$
Kleinheinrich et al. full sample	$0.9^{+0.36}_{-0.48}$	$7.1^{+2.6}_{-2.7}$
blue sample	$0.54^{+0.60}_{-0.36}$	$4.1^{+3.3}_{-2.4}$
red sample	$1.26^{+0.38}_{-0.60}$	$8.02^{+7.1}_{-3.8}$
Hoekstra et al. 2004	1.2	$8.4 \pm 0.7 \pm 0.4$

Table 2: Results for the NFW model.



# Velocity dispersions

Graph

Faber-Jackson (ellipticals)

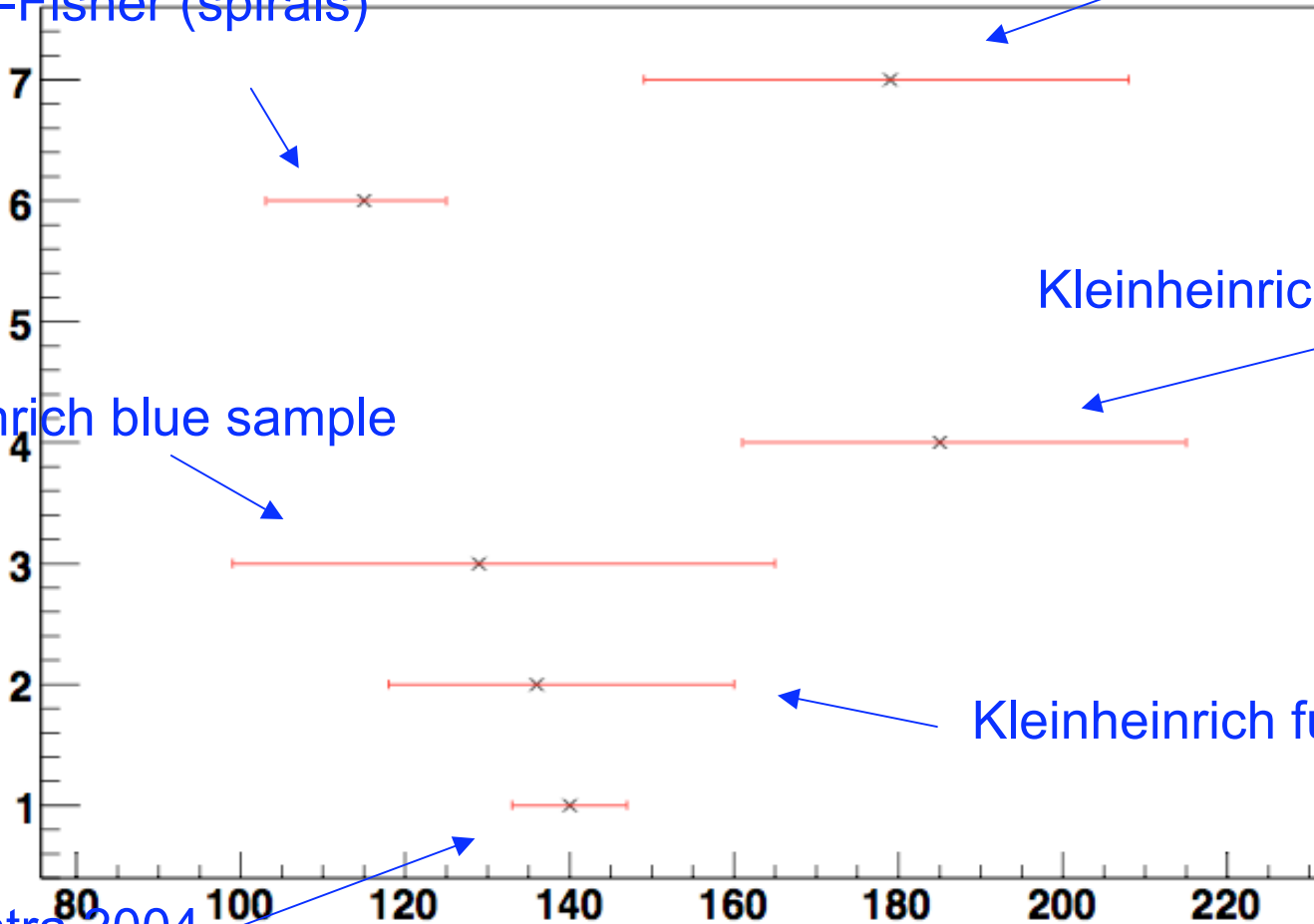
Tully-Fisher (spirals)

Kleinheinrich blue sample

Kleinheinrich red sample

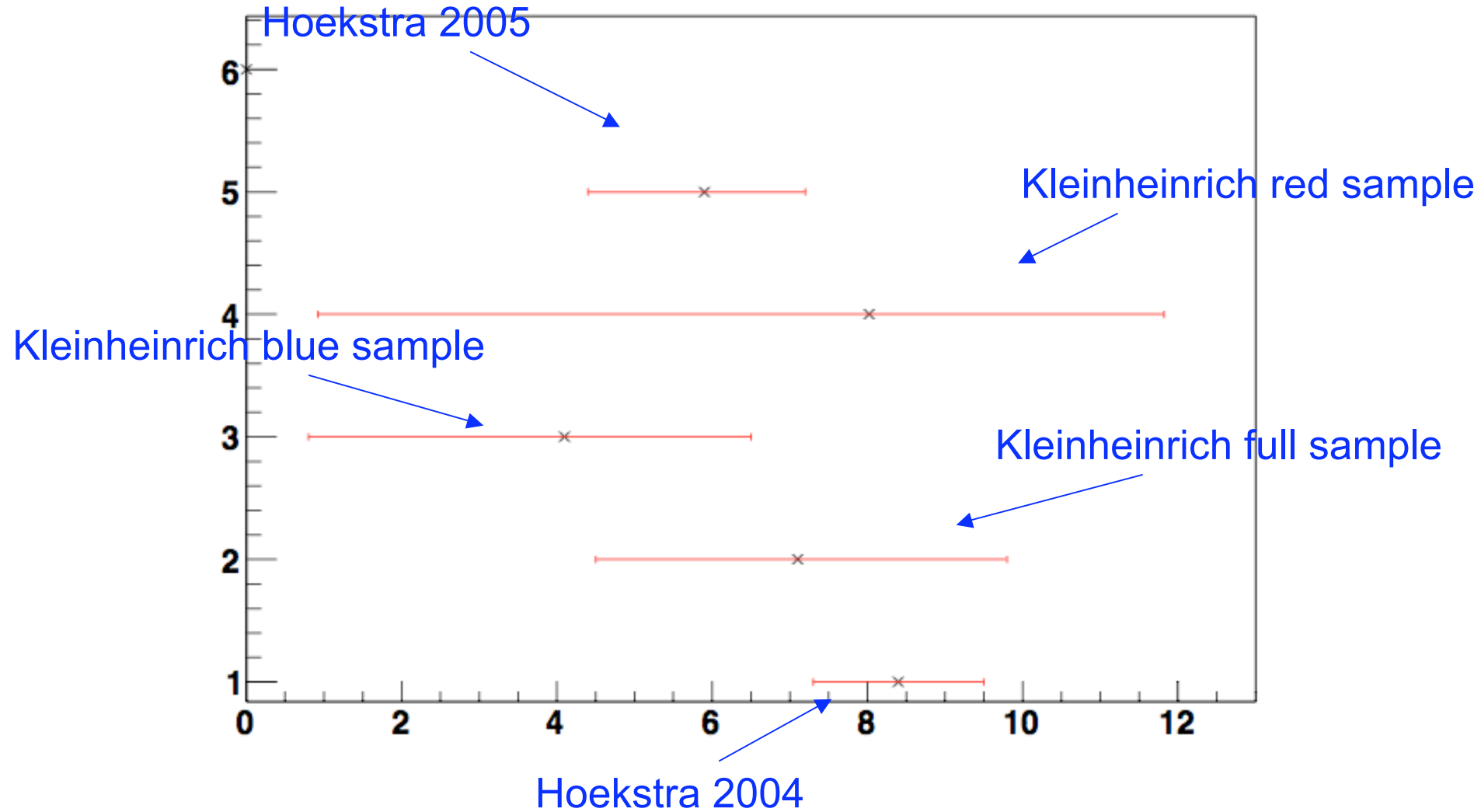
Kleinheinrich full sample

Hoekstra 2004



# Virial mass

Graph



# $\eta$ The **Smoothness** parameter

All “unobserved” matter is put into a smoothly distributed component.

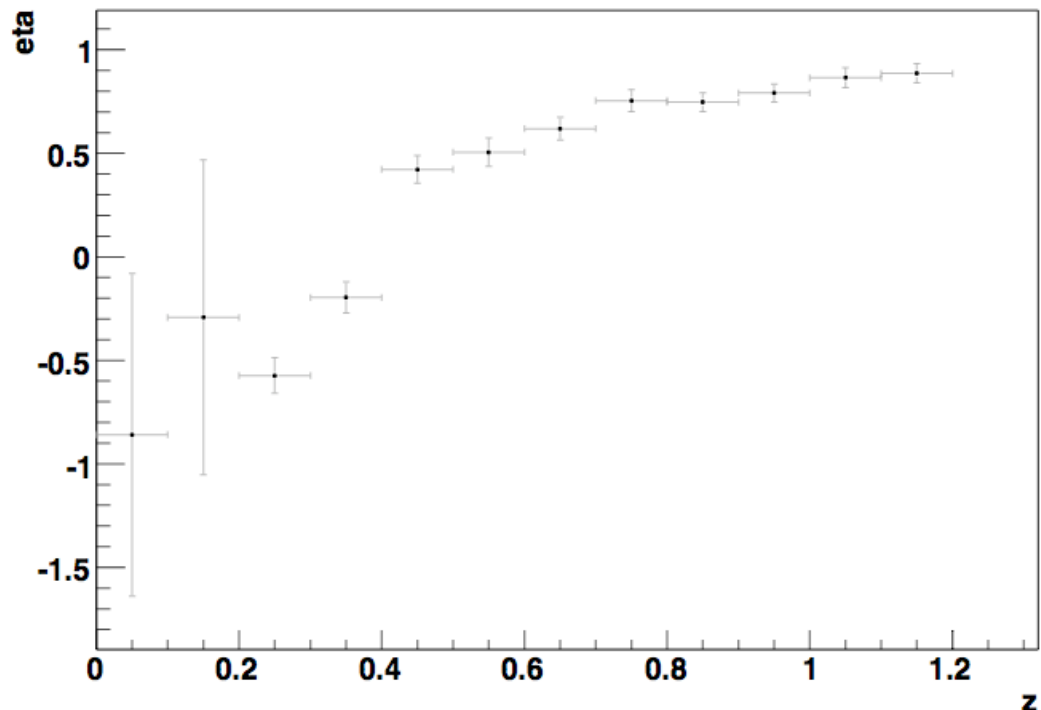
$$\eta(z) = 1 - \frac{\rho_g(z)}{\rho_m(z)}$$

Difficulty:

How to infer the “correct” total mass of each galaxy?

Results from SIS and NFW give different mass

Graph



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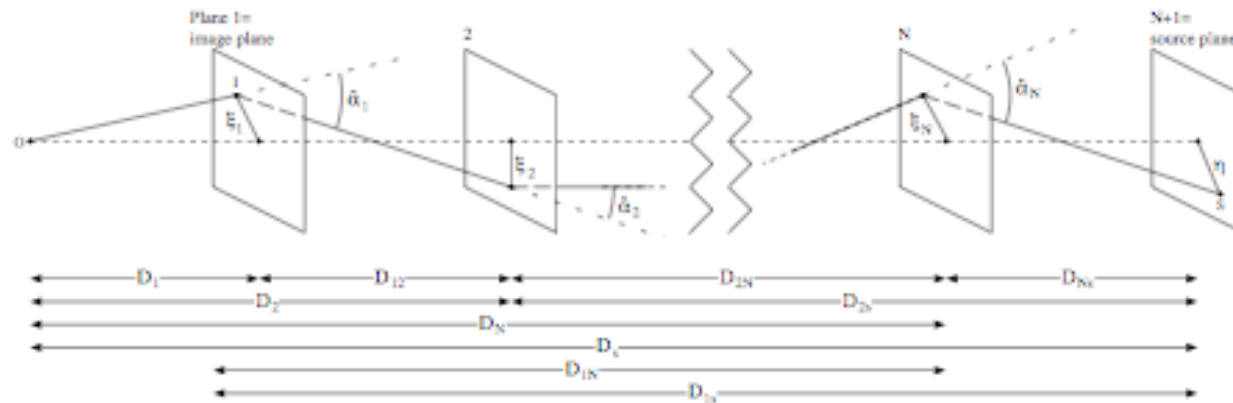
Estimation of the magnification of each SNe

# Q-LET

Q-LET is a program that enables a quick estimate of the gravitational lensing effects on a point source

*Q-LET — Application to SN2003es*

3



Multiple  
lens-plane  
method

## Input

- Cosmological parameters +  $z$  of the sn
- List of redshifts, distances to the line of sight, mass or velocity dispersions, halo models for all the galaxies in the line of sight

## Output

The magnification factor

# Future work

- Estimation of the magnification of the 500 final SNe
- Look for the lensing signal (a correlation between the residuals in the Hubble diagram and the magnification)
- See whether it is possible to constrain the halo masses of the galaxies



*"That's all Folks!"*