



## A computing exercise using ROOT

**Aim:** give a taste of data analysis @ LHC

- What is ROOT?
  - ROOT is an object-oriented C++ analysis package
  - User-compiled code can be called to produce 1-d, 2-d, and 3-d graphics and histograms...



<https://root.cern.ch>

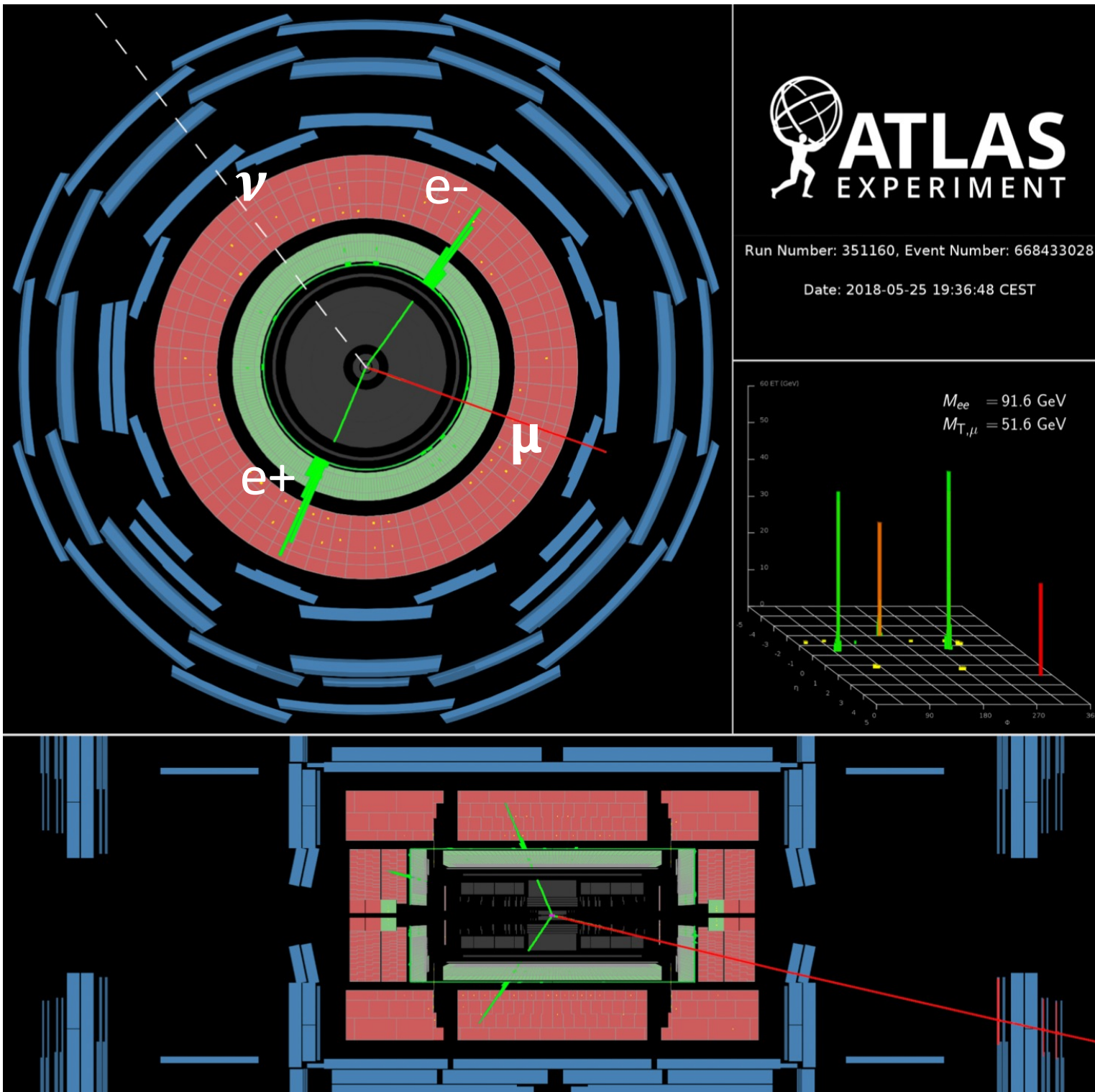
“open-source data analysis framework used by high energy physicist and others”

What  
is  
that?

(we know  
that from  
theory  
AND  
experiments)

$Z \rightarrow e^+e^-$

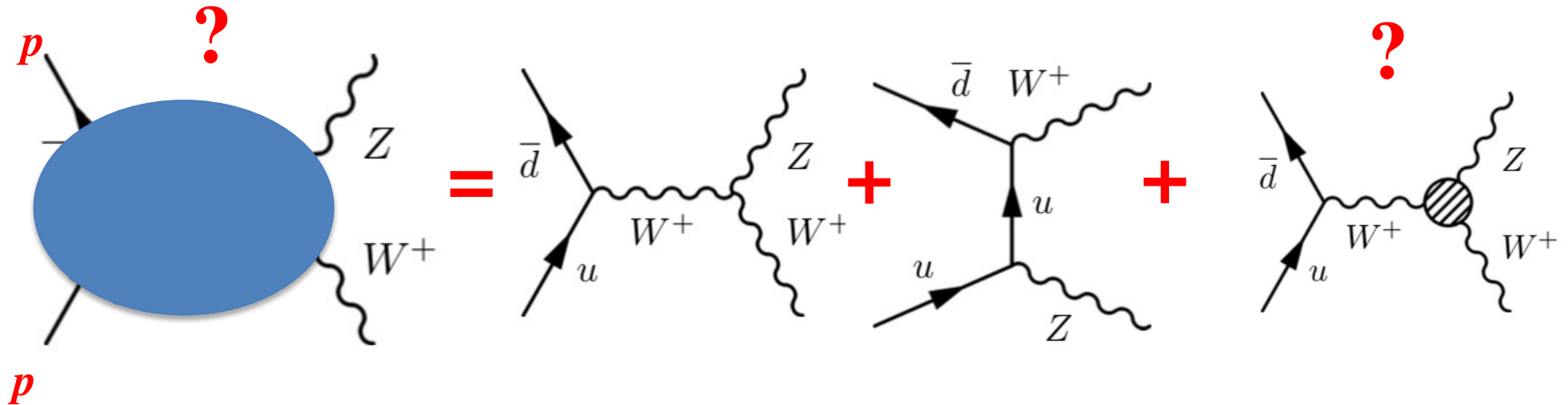
$W \rightarrow \mu\nu$



# Hands-on on diboson physics



topic @ LHC



**Test of SM**  
(measure interaction probability)

**Discover New Physics**  
(look inside the blob)

**Advantage of accelerator physics: controlled and known initial conditions**



→ most of things discovered about fundamental interactions so far thanks to accelerator physics

# Outline of the presentation

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- **Kinematic variables** used in the analysis of  $p - p$  collisions
- **Useful relations**
- **Concept of invariant mass** (example: ‘inclusive’ Z boson production)
- **Example of analysis in  $p - p$  collisions :**
  - \* **Signal: Production of a W and a Z**  $p - p \rightarrow W Z X$
  - \* **Background: Production of a pair of top-antitop**

- **Example: Macro.C**

$p - p$  = proton - proton

$X$  = additional  
undetected  
particles  
( $X$ ) =  
part1, part2, part3, ...

In all the following slides we assume the speed of the light

$c=1$

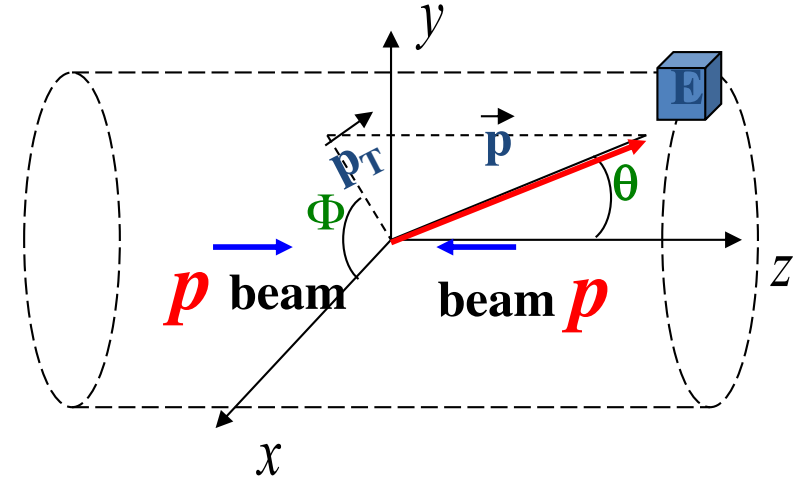
# Variables used in the analysis of $p - p$ collisions

A particle (  $Z$ ,  $W$ ,  $e+$ ,  $e-$ , etc ...) is described by its **four-momentum**:

$$\tilde{p} = ( E, p_x, p_y, p_z )$$

The particle mass is  $m = \sqrt{E^2 - p_x^2 - p_y^2 - p_z^2}$

When dealing with  $p-p$  collisions the following variables are used:



For **each** particle (  $Z$ ,  $W$ ,  $e+$ ,  $e-$ , etc ...):

• 1. **Transverse momentum/energy** :  $p_T = p \sin \theta$        $E_T = E \sin \theta$

• 2. **Rapidity**  $Y = \frac{1}{2} \ln \frac{E+p_z}{E-p_z}$

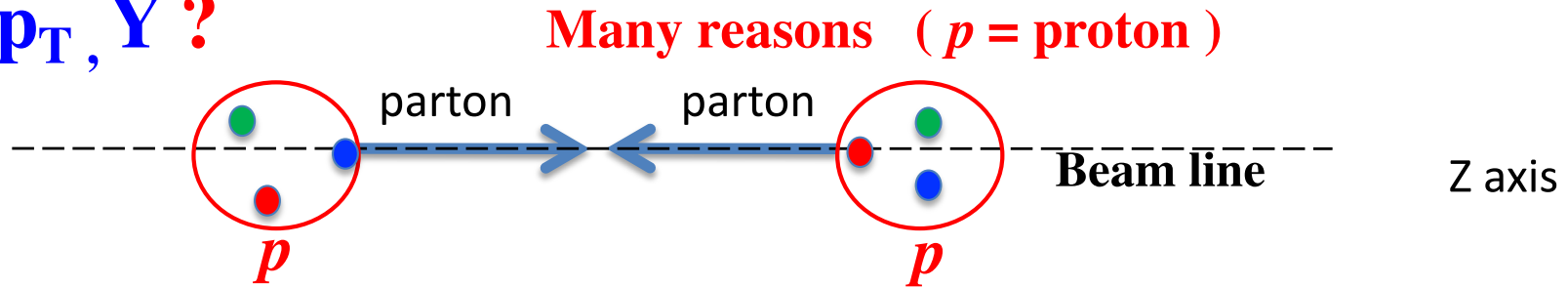
or Pseudorapidity  $\eta = - \ln \left( \tan \frac{\theta}{2} \right)$


• 3. **Azimuthal angle**  $\Phi$

**Why?**

# Variables used in the analysis of $p - p$ collisions

## Why $p_T, Y$ ?

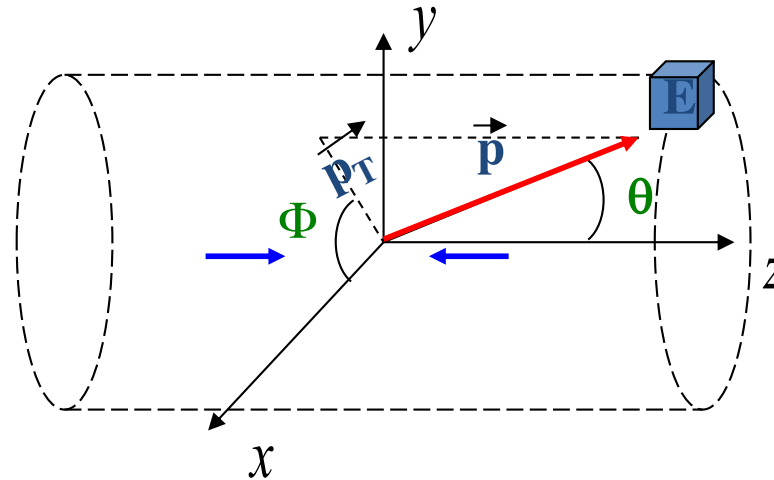


1.  $p_T$  and  $\Delta Y$  are invariants for Lorentz transformations along the z axis 
2. The **longitudinal** momentum of the initial partons is ‘**unknown**’, while we know that  $\vec{p}_T^{\text{initial parton}} \sim 0$   
 → Exploit momentum conservation **in the plane  $\perp$  to the beam** using *transverse* quantities → Example:  

$$\sum^{\text{initial partons}} \vec{p}_T = \sum^{\text{vis fin}} \vec{p}_T + \sum^{\text{invis fin}} \vec{p}_T \approx 0 \quad \rightarrow \text{Allows to evaluate the } p_T \text{ of not detected (v) particles}$$

$$\sum^{\text{invis fin}} \vec{p}_T = - \sum^{\text{vis fin}} \vec{p}_T \quad | \sum^{\text{invis}} p_T | \text{ is the “missing } E_T \text{ (MET)”}$$
3. The “interesting” physics is in the **hard scattering** processes → high  $p_T$  particles (selection of high  $p_T$  particles ensures “interesting” physics)

# Useful relations



$$\mathbf{p}_T = p \sin \theta$$

$$p_x = \mathbf{p}_T \cdot \cos(\Phi);$$

$$p_y = \mathbf{p}_T \cdot \sin(\Phi);$$

$$p_z = \mathbf{E} \cdot \tanh(\eta);$$

$$\eta = -\ln \left( \tan \frac{\theta}{2} \right)$$

NB:

- $m \ll E \quad \rightarrow Y \approx \eta \quad (\eta \text{ doesn't require particle identification})$
- $m \ll E \quad \rightarrow \mathbf{p}_T \approx \mathbf{E}_T \quad \mathbf{E}_T = E \sin \theta$

## Concept of *invariant mass* $M_A$

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Particle A decays to B and C

$A \rightarrow B \ C$

$$M_A^2 = \tilde{p}_A^2 = (\tilde{p}_B + \tilde{p}_C)^2$$

**The invariant mass is the same in all frames of reference related by Lorentz transformations**



# Concept of *invariant* mass: inclusive Z boson production

$$p - p \rightarrow Z(\mathbf{X}) \text{ with } Z \rightarrow e+e-$$

( $\mathbf{X}$ ) = part1, part2, part3, ...

$M_{ee}$  = Invariant mass of  $ee$  system  
( it allows to measure the Z mass,  $M_Z$  ):

from the 4-momentum conservation

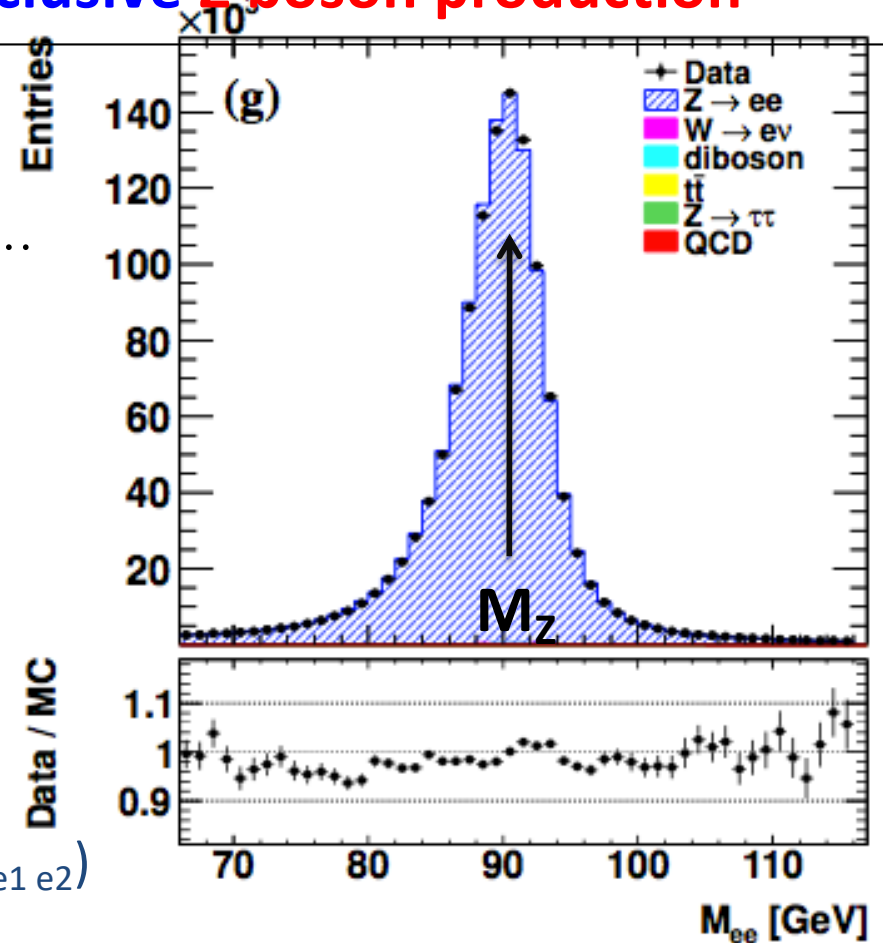
$$\tilde{p}_Z^2 = (\tilde{p}_{e1} + \tilde{p}_{e2})^2$$

$$M_{ee}^2 = (\tilde{p}_{e1} + \tilde{p}_{e2})^2 \approx 2 (E_{e1} E_{e2} - |\vec{p}_{e1}| |\vec{p}_{e2}| \cos \vartheta_{e1 e2})$$

$$M_{ee} \approx \sqrt{2 E_{e1} E_{e2} (1 - \cos \vartheta_{e1 e2})} \text{ (electron mass is neglected)}$$

Very ‘clean’ distribution (low bkg)!!

Why  $M_{ee}$  gives a distribution  
and not a single value?



$$1. \Delta E * \Delta t > \hbar/2 \quad \Delta m * \tau > \hbar/2$$

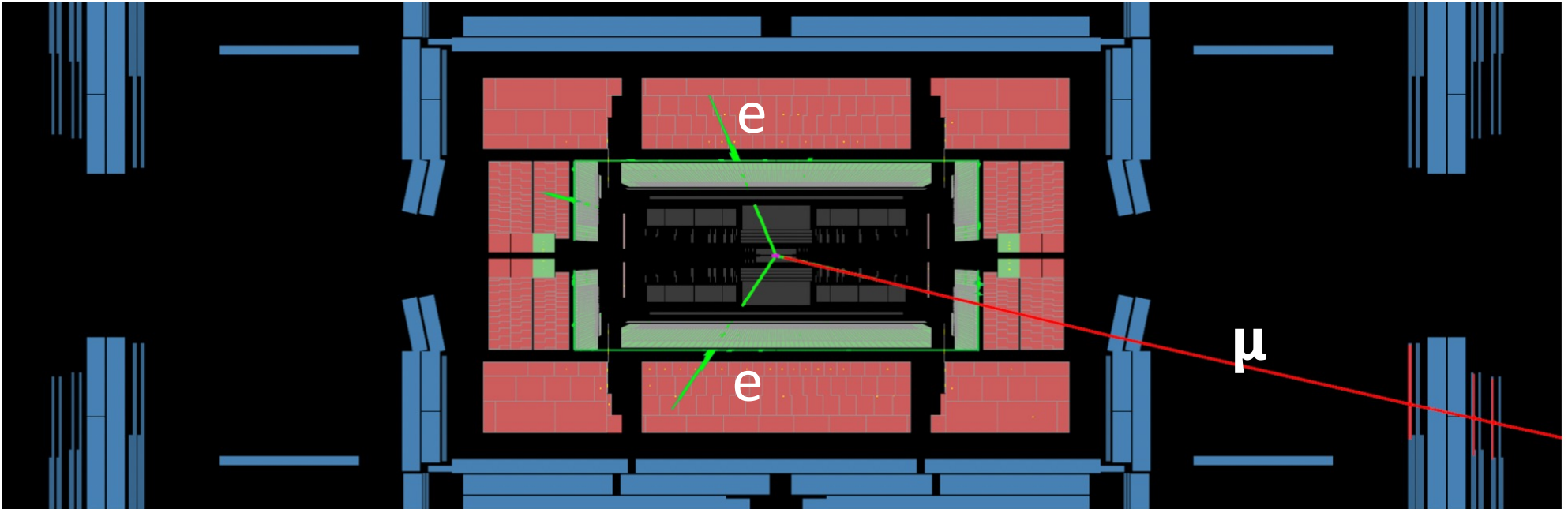
$$\Gamma * \tau > \hbar/2$$

width

lifetime

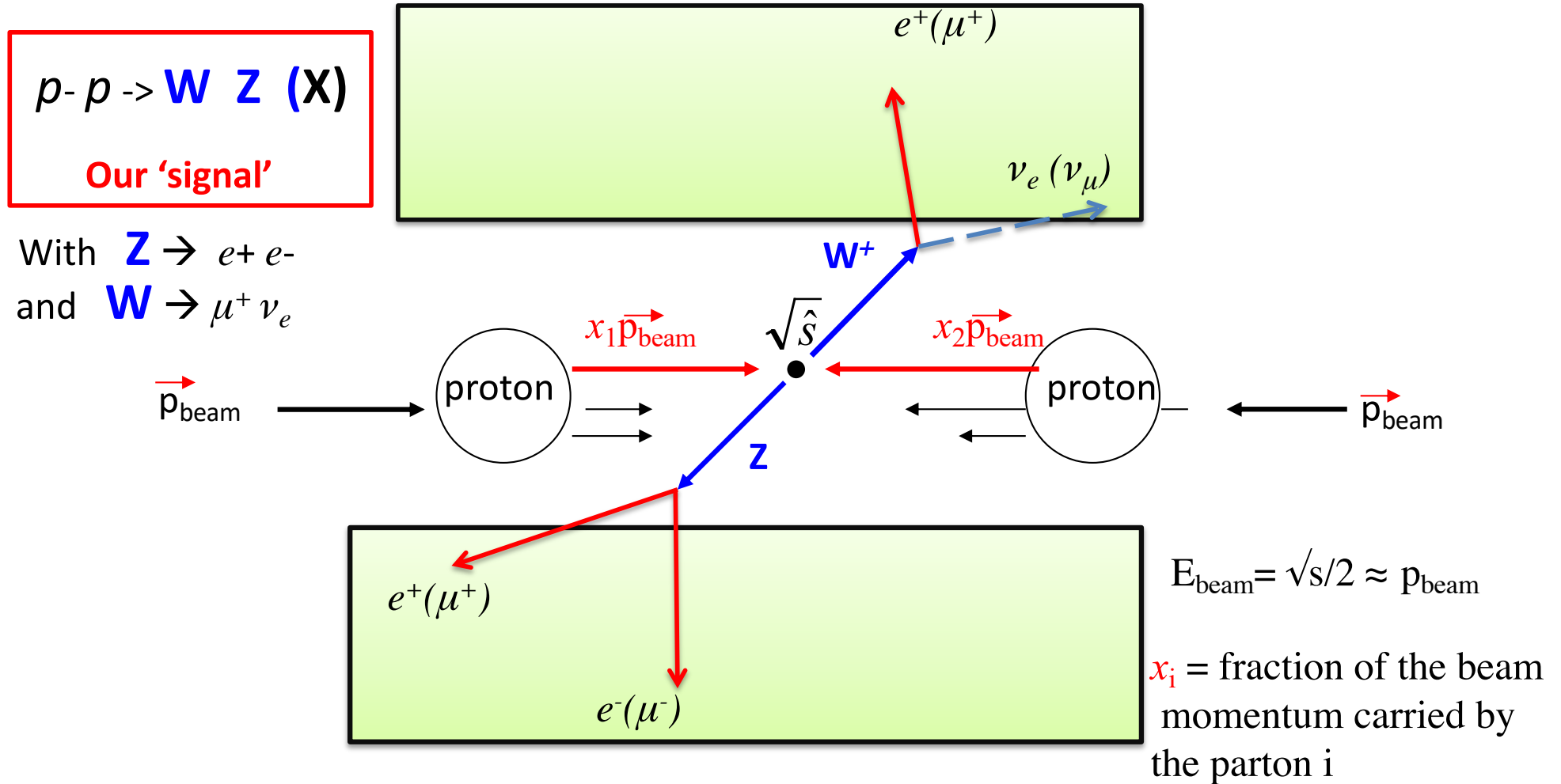
2. Experimental resolution

# What is that?



# Our signal : production of a W and a Z (decaying leptonically)

$p$ - $p$  'hard' collisions in the  $q_1 \bar{q}_2$  center of mass:

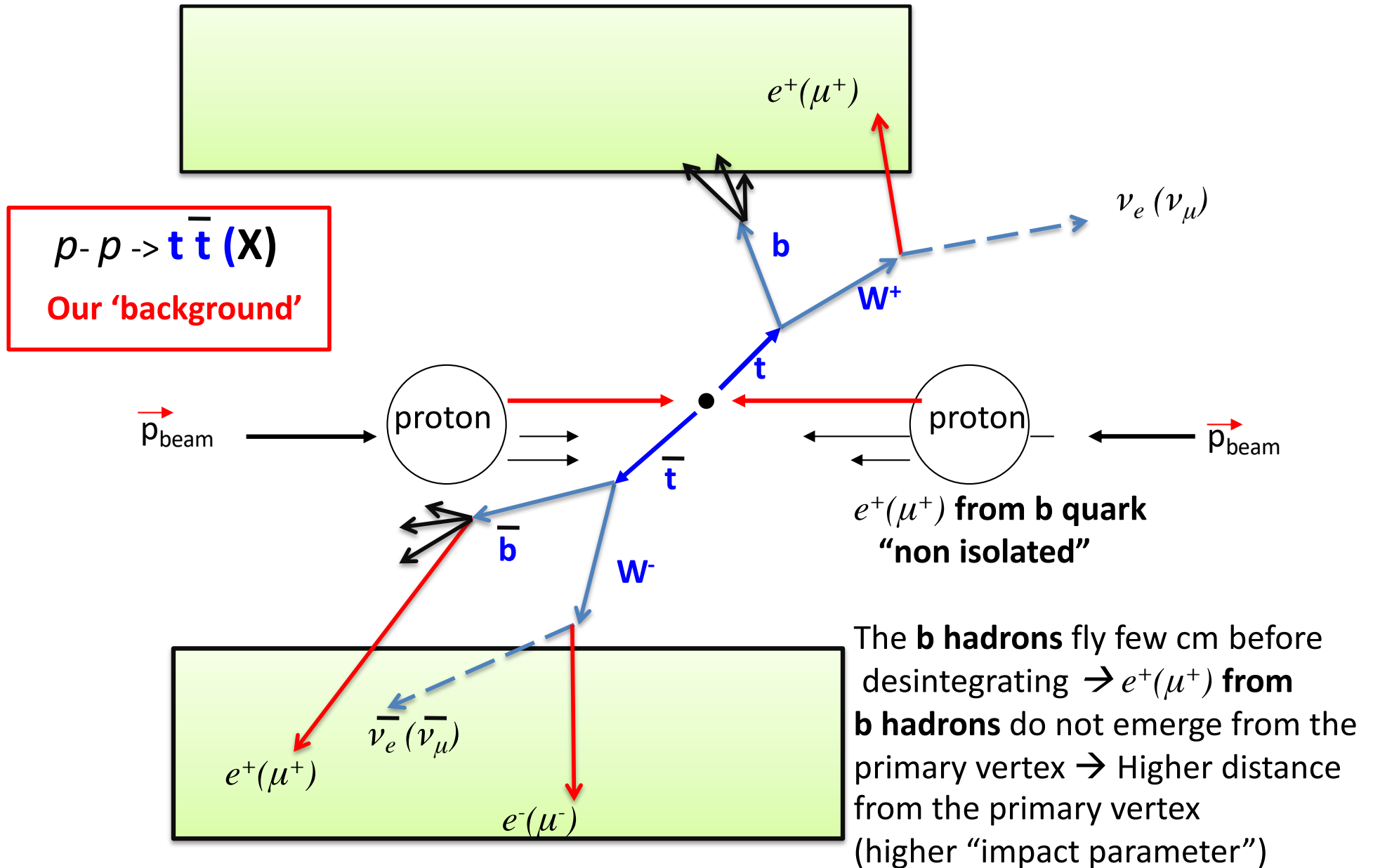


## Kinematics of $p$ - $p$ collisions

★ 4-mom of the initial partons :  $[(x_1+x_2)E_{\text{beam}}, 0, 0, (x_1-x_2) p_{\text{beam}}]$

# Our background: Production of a pair of top-antitop

$p$ - $p$  'hard' collisions. In the  $\bar{q}_1 q_2$  center of mass:



**Aim of the exercise (note, this are the first steps of an analysis):**

- 1) look at some important variables,**
- 2) build the Z invariant mass,**
- 3) how one can discriminate between the 'signal' and the 'background' ?**

You will have:

**GRASPA2024explanation.pptx.pdf (this slides)**

**Exercise2024.pdf (what we ask to do)**

**Selected\_All\_EEM.root (« data file » (simulated data))**

**macro.C (draft of an analysis program)**

**macro\_final.C (solution: final analysis program)**

**<https://root.cern.ch/root/html/doc/guides/primer/ROOTPrimer.html>**

# 1) The **input file** containing the physics: **Selected\_All\_EEM.root**

=== MOST ENERGETIC LEPTON FROM THE Z

Br 4 :pt1 : pt1

Br 5 :eta1 : eta1

Br 6 :phi1 : phi1

Br 7 :E1 : E1

=== SECOND ENERGETIC LEPTON FROM THE Z

Br 8 :pt2 : pt2

Br 9 :eta2 : eta2

Br 10 :phi2 : phi2

Br 11 :E2 : E2

=== LEPTON FROM W

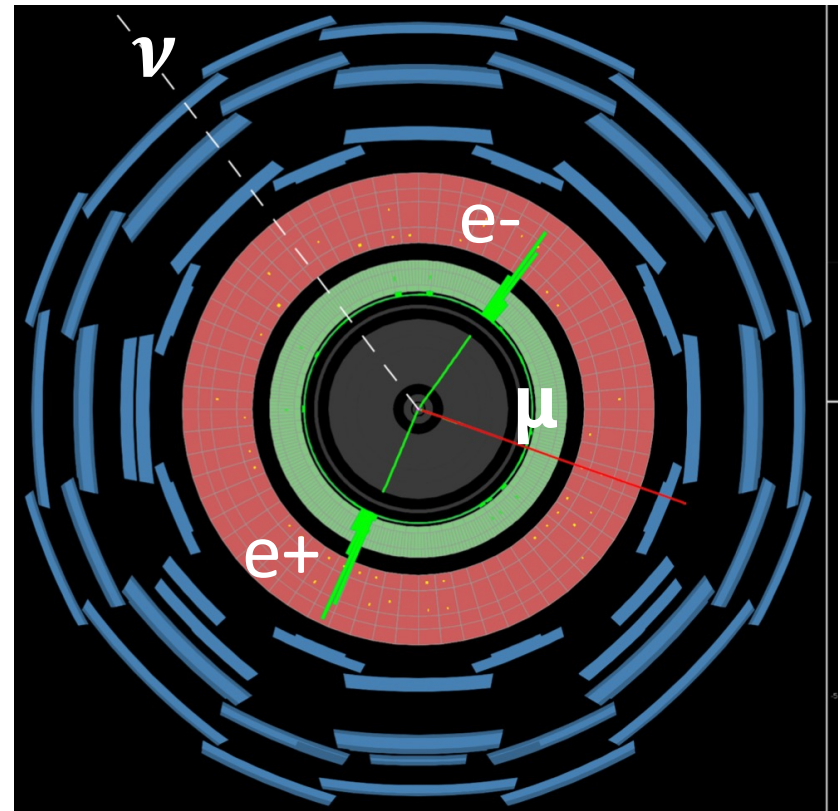
Br 12 :pt3 : pt3

Br 13 :eta3 : eta3

Br 14 :phi3 : phi3

Br 15 :E3 : E3

List of variables given  
per each collision event  
(kinematics of the final  
state leptons)



List of Variables in the ntuple (Br 0,1.. means "Branch 0, 1, ...")

== **IMPACT PARAMETER and ISOLATION of the lepton from W**

Br 0 :Trackd0cutWMu : Trackd0cutWMu

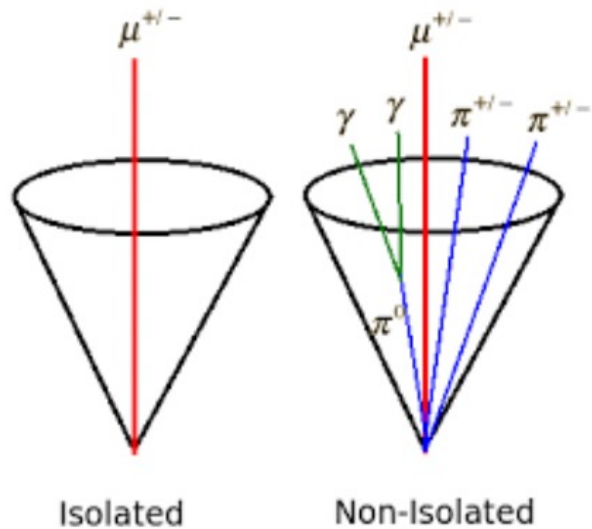
Br 1 :TrackIsoWmu : TrackIsoWmu

== **MISSING TRANSVERSE ENERGY**

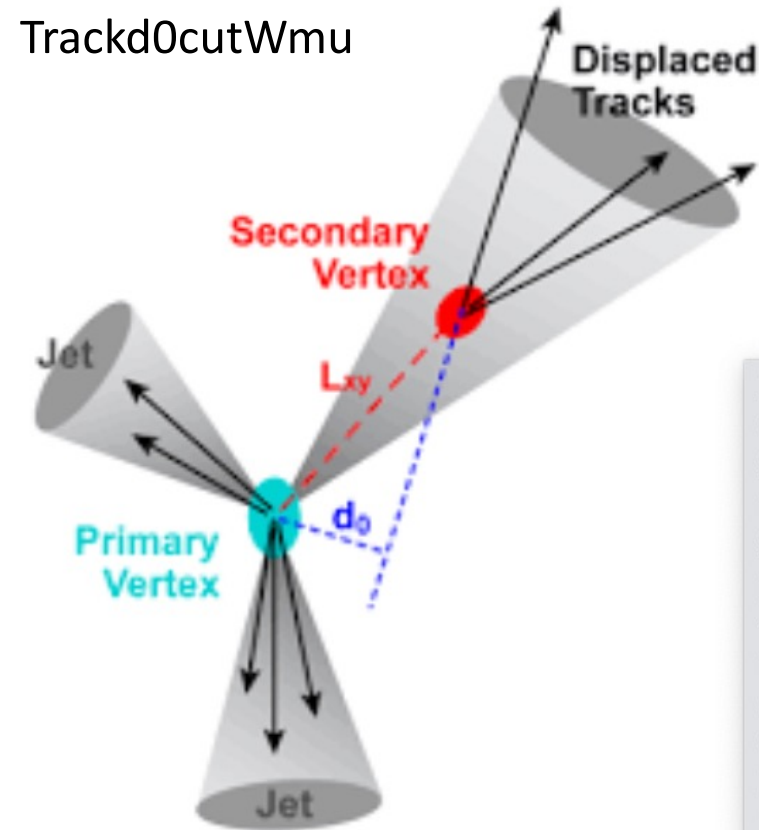
Br 2 :MET : MET

=== **MASS of Z**

Br 3 :MZ : MZ



TrackIsoWmu  
Energy in the  
cone



## 2) Instructions to make the computing exercise : [Exercise2024.pdf](#)

GRASPA 2024

16-23 July 2024



### COMPUTING EXERCISE

#### Study of the production of a pair of gauge bosons ( $W$ and $Z$ ) at the LHC

The data to analyse are organised into a '**Root n-tuple**' which we will provide to you. The Root n-tuple is a file containing information about the kinematics of "events", each resulting from a **proton-proton interaction**.

These events have three leptons (electrons or muons) and are of two kinds:

- 1) **SIGNAL EVENTS**: corresponding to  $pp \rightarrow W Z X$  with both bosons disintegrating leptonically ( $X$  stands for non identified generic particles ),
- 2) **BACKGROUND EVENTS**: top-antitop events  $pp \rightarrow t\bar{t}X$ .

We remind that the leptonic decays of the  $W$  and  $Z$  are:

$W \rightarrow \ell\nu$  and  $Z \rightarrow \ell^+\ell^-$  with  $\ell = e$  or  $\mu$ .



### 3) A skeleton of an analysis program using ROOT: **macro.C**

```
#include "TCanvas.h"
#include "TR00T.h"
#include "TFile.h"
#include "TTree.h"
#include "TBrowser.h"
#include "TH2.h"
#include "TRandom.h"

void tree1r()
{
    // Read Selected_All_EEM.root file
    //Root file
    TFile *f = new TFile("Selected_All_EEM.root");

    // Signal events
    TTree *sig = (TTree*)f->Get("WZSignal");
    Double_t pt1, eta1, phi1, E1;
    Double_t pt2, eta2, phi2, E2;
    Double_t pt3, eta3, phi3, E3;
    Double_t MZ, MET, trackd0cutWMu, TrackIsoWmu;
    Double_t Weight;

    //get some variables for SIGNAL EVENTS
    sig->SetBranchAddresses("pt1",&pt1);
```

# Example of analysis program

macro.C

23/07/2013 00:21

```
#include "TCanvas.h"
#include "TRoot.h"
#include "TFile.h"
#include "TTree.h"
#include "TBrowser.h"
#include "TH2.h"
#include "TRandom.h"

void tree1r()
{
    // Read Selected_All_EEM.root file
    //Root file
    TFile *f = new TFile("Selected_All_EEM.root");

    // Signal events
    TTree *sig = (TTree*)f->Get("WZSignal");
    Double_t pt1, eta1, phi1, E1;
    Double_t pt2, eta2, phi2, E2;
    Double_t pt3, eta3, phi3, E3;
    Double_t MZ, MET, trackd0cutWMu, TrackIsoWmu;
    Double_t Weight;

    //get some variables for SIGNAL EVENTS
    sig->SetBranchAddress("pt1",&pt1);
    sig->SetBranchAddress("eta1",&eta1);
    sig->SetBranchAddress("phi1",&phi1);
    sig->SetBranchAddress("E1",&E1);
    sig->SetBranchAddress("MZ",&MZ);
    sig->SetBranchAddress("Weight",&Weight);
    // add other variables ...
}
```

**Header files**

**Open the input file**

**Access the Signal info**

**Define the name  
variables per each SIGNAL lepton**

```
////get some variables for BACKGROUND EVENTS
TTree *ttbar = (TTree*)f->Get("ttbar");
Double_t pt1_bkg, eta1_bkg, phi1_bkg, E1_bkg;
Double_t MZ_bkg;
Double_t Weight_bkg;
```

**Access the background info**

```
//get some variables for ttbar
ttbar->SetBranchAddresses("pt1",&pt1_bkg);
ttbar->SetBranchAddresses("eta1",&eta1_bkg);
ttbar->SetBranchAddresses("phi1",&phi1_bkg);
ttbar->SetBranchAddresses("E1",&E1_bkg);
ttbar->SetBranchAddresses("MZ",&MZ_bkg);
ttbar->SetBranchAddresses("Weight",&Weight_bkg);
// add other variables ...
```

**Define the name  
variables per each bkg lepton**

```
//create two histograms (for sig and ttbar)
TH1F *h_MZ = new TH1F("h_MZ","MZ distribution All events",40,65,115);
TH1F *h_MZ_bkg = new TH1F("h_MZ_bkg","MZ distribution BKG",40,65,115);
TH1F *h_MZ_sig = new TH1F("h_MZ_sig","MZ distribution SIG",40,65,115);
```

```
//read all SIGNAL entries and fill the histograms
Int_t nentries = (Int_t)sig->GetEntries();
```

```
for (Int_t i=0;i<nentries_bkg;i++) {
    ttbar->GetEntry(i);
    h_MZ_bkg->Fill(MZ_bkg,Weight_bkg);
    h_MZ->Fill(MZ_bkg,Weight);
}
```

**Loop on events**

Page 1 of 2

```
// example how Draw and save histograms
```

```
TCanvas *c = new TCanvas();  
c->cd();  
h_MZ_sig->Draw();  
h_MZ_bkg->SetLineColor(kRed);  
h_MZ_bkg->Draw("same");
```

```
c->Print("test_MZ.eps");  
}
```

```
void macro()  
{  
  tree1r();  
}
```

**Draw and save histograms**

**Main program**

---

**To start root you may type:**

**root -l**

**root [1] .x macro.C**

**and look at what you get ....**

Useful in-line commands:

```
TFile f("Selected_All_EEM.root");  
f.ls();  
WZSignal->Scan();  
WZSignal->Print();
```

Where to find help:

**<https://root.cern.ch/root/html/doc/guides/primer/ROOTPrimer.pdf>**

**Have fun !!**



W(jj) Z (jj)

jj = J (1 fat jet)

# Another example: search for di-boson resonances

- Is there something hiding in the data, waiting to be discovered?

