

(experimental)

# LHC physics



**GrASP2024**  
**Summer SCHOOL**  
on Particle and Astroparticle Physics

16 July ANNECY  
23 2024 FRANCE

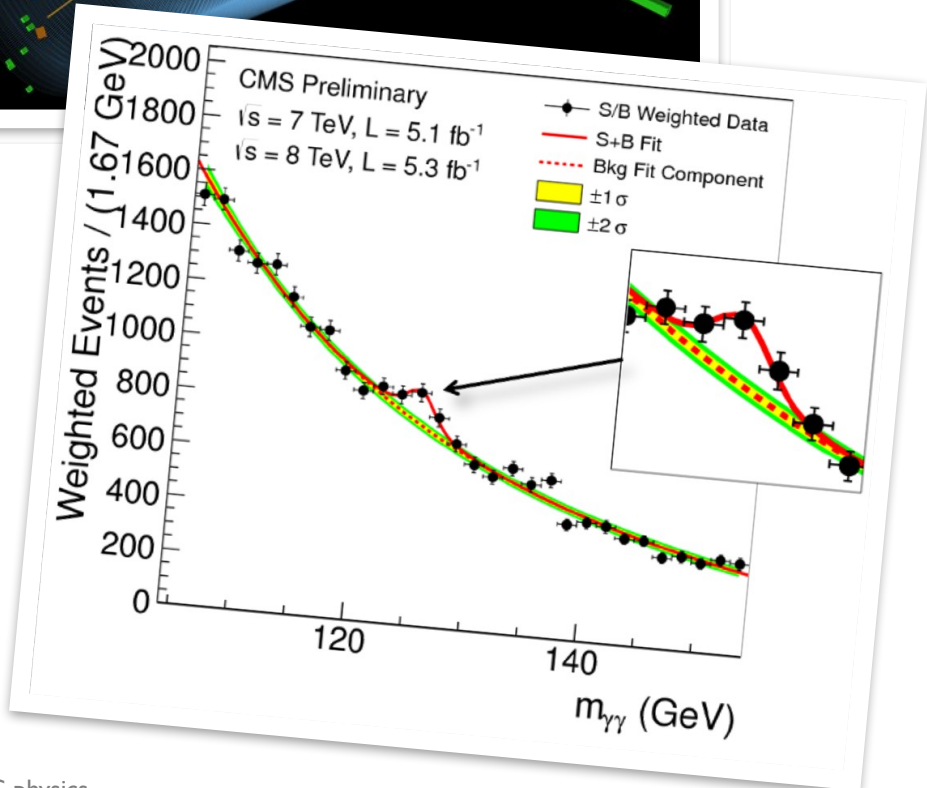
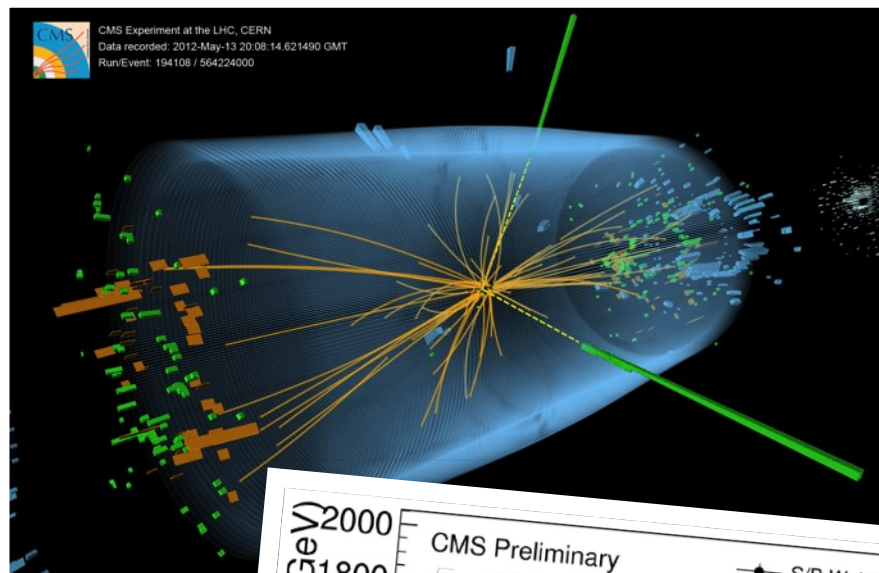
CLAPP LAFETL CNRS IN2P3 UNIVA UGA PIGA

{ how (which) particles are produced and measured? }

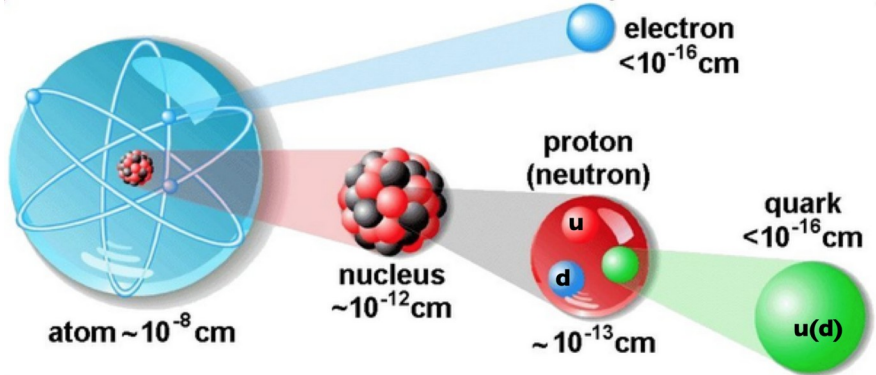
*Riccardo Bellan*

# Experiment = probing/building theories with data!

$$\begin{aligned}
 & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\mu^a g_\mu^b g_\mu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\mu^c g_\mu^d g_\mu^e + \\
 & \frac{1}{2}ig_s^2 (\bar{q}_i^\mu \gamma^\mu q_j^\mu) g_\mu^a + G^a \partial^2 C^a + g_s f^{abc} \partial_\mu \bar{C}^a C^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2}\partial_\mu H \partial_\mu H - \\
 & \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w} M \phi^0 \phi^0 - \beta_h \frac{[2M^2]}{g^2} + \\
 & \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) + \frac{2M^4}{g^2} \alpha_h - ig_{cw} [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - Z_\mu^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\nu^- \partial_\mu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^- \partial_\mu W_\mu^+)] - ig_{sw} [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^- \partial_\mu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\mu W_\mu^+)] - \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\nu^+ W_\mu^- + \\
 & \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\nu^0 W_\mu^+ W_\nu^-) + \\
 & g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^-] - g\alpha [H^3 + H\phi^0 \phi^0 + 2H\phi^+ \phi^-] - \\
 & \frac{1}{8}g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2] - \\
 & gM W_\mu^+ W_\nu^- H - \frac{1}{2}g \frac{M}{c_w} Z_\mu^0 Z_\nu^0 H - \frac{1}{2}ig [W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - \\
 & W_\nu^- (\phi^0 \partial_\nu \phi^+ - \phi^+ \partial_\nu \phi^0)] + \frac{1}{2}g [W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\nu^- (H \partial_\nu \phi^+ - \\
 & \phi^+ \partial_\nu H)] + \frac{1}{2}g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - ig_{cw} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \\
 & ig_{sw} M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + \\
 & ig_{sw} A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4}g^2 W_\mu^+ W_\nu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \\
 & \frac{1}{4}g^2 \frac{1}{c_w} Z_\mu^0 Z_\nu^0 [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{1}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) - \frac{1}{2}ig \frac{1}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\
 & g^1 s_w^2 A_\mu A_\nu \phi^+ \phi^- - \bar{e}^\lambda (\gamma \partial + m_e) e^\lambda - \bar{\nu}^\lambda \gamma \partial \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + m_u) u_j^\lambda + \\
 & \bar{d}_j^\lambda (\gamma \partial + m_d) d_j^\lambda + ig_{sw} A_\mu [-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)] + \\
 & \frac{ig}{4c_w} Z_\mu^0 [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - \\
 & 1 - \gamma^5) u_j^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 - \gamma^5) d_j^\lambda)] + \frac{ig}{2\sqrt{2}} W_\mu^+ [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + \\
 & (\bar{d}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)] + \frac{ig}{2\sqrt{2}} W_\mu^- [(\bar{e}^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)] - \\
 & \gamma^5 u_j^\lambda) + \frac{ig}{2\sqrt{2}} \frac{m_\lambda^2}{M} [-\phi^+ (\bar{\nu}^\lambda (1 - \gamma^5) e^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) \nu^\lambda)] - \\
 & \frac{g}{2} \frac{m_\lambda^2}{M} [H (\bar{e}^\lambda e^\lambda) + i\phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda)] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_\lambda^2 (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + \\
 & m_\lambda^2 (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa)] + \frac{ig}{2M\sqrt{2}} \phi^- [m_\lambda^2 (\bar{d}_j^\lambda C_{\lambda\kappa}^1 (1 + \gamma^5) u_j^\kappa) - m_\lambda^2 (\bar{d}_j^\lambda C_{\lambda\kappa}^1 (1 - \\
 & \gamma^5) u_j^\kappa)] - \frac{g}{2} \frac{m_\lambda^2}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_\lambda^2}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \\
 & \frac{ig}{2} \frac{m_\lambda^2}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + X^0 (\partial^2 - \\
 & \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + ig_{cw} W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + ig_{sw} W_\mu^+ (\partial_\mu \bar{X}^- X^+ - \\
 & \partial_\mu \bar{X}^+ X^-) + ig_{cw} W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^0 X^+) + ig_{sw} W_\mu^- (\partial_\mu \bar{X}^- X^+ - \\
 & \partial_\mu \bar{X}^+ X^-) + ig_{cw} Z_\mu^0 (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) + ig_{sw} A_\mu (\partial_\mu \bar{X}^+ X^+ - \\
 & \partial_\mu \bar{X}^- X^-) - \frac{1}{2}gM [\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w} \bar{X}^0 X^0 H] + \\
 & \frac{1-2c_w^2}{2c_w} igM [\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-] + \frac{1}{2c_w} igM [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \\
 & igMs_w [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \frac{1}{2}igM [\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0]
 \end{aligned}$$



# The Standard Model of particle physics in a nutshell



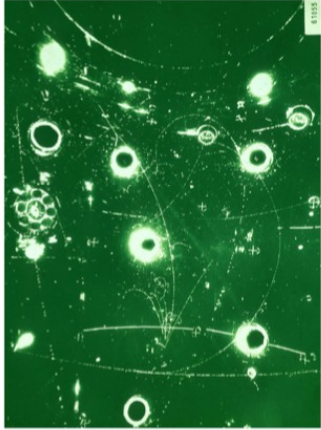
$$\mathcal{L} = \begin{matrix} \text{Gauge bosons} \\ -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ \text{Gauge boson coupling to fermions (EW, QCD)} \\ + i\bar{\Psi} \not{D} \psi \\ \text{Higgs coupling to fermions (fermion masses)} \\ + D_{\mu} \Phi^{\dagger} D^{\mu} \Phi - V(\Phi) \\ \text{Higgs coupling to bosons (boson masses)} \\ + \bar{\Psi}_L \hat{Y} \Phi \Psi_R + h.c. \\ \text{Higgs self-coupling (Higgs potential)} \end{matrix}$$

	three generations of matter (fermions)			interactions / force carriers (bosons)		
	I	II	III			
QUARKS	mass $= 2.2 \text{ MeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ <b>u</b> up	mass $= 1.28 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ <b>c</b> charm	mass $= 173.1 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ <b>t</b> top	0 0 1 <b>g</b> gluon	mass $= 125.09 \text{ GeV}/c^2$ 0 0 0 <b>H</b> higgs	
	mass $= 4.7 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ <b>d</b> down	mass $= 96 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ <b>s</b> strange	mass $= 4.18 \text{ GeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ <b>b</b> bottom	0 0 1 <b>\gamma</b> photon	SCALAR BOSONS	
	mass $= 0.511 \text{ MeV}/c^2$ charge $-1$ spin $\frac{1}{2}$ <b>e</b> electron	mass $= 105.66 \text{ MeV}/c^2$ charge $-1$ spin $\frac{1}{2}$ <b>\mu</b> muon	mass $= 1.7768 \text{ GeV}/c^2$ charge $-1$ spin $\frac{1}{2}$ <b>\tau</b> tau	0 0 1 <b>Z</b> Z boson		
	mass $< 2.2 \text{ eV}/c^2$ charge 0 spin $\frac{1}{2}$ <b>\nu_e</b> electron neutrino	mass $< 1.7 \text{ MeV}/c^2$ charge 0 spin $\frac{1}{2}$ <b>\nu_{\mu}</b> muon neutrino	mass $< 15.5 \text{ MeV}/c^2$ charge 0 spin $\frac{1}{2}$ <b>\nu_{\tau}</b> tau neutrino	0 0 1 <b>W</b> W boson		
				0 0 1 <b>Z</b> Z boson		GAUGE BOSONS VECTOR BOSONS
				0 0 1 <b>Z</b> Z boson		
			0 0 1 <b>W</b> W boson			

# A theory built (and probed) over time...

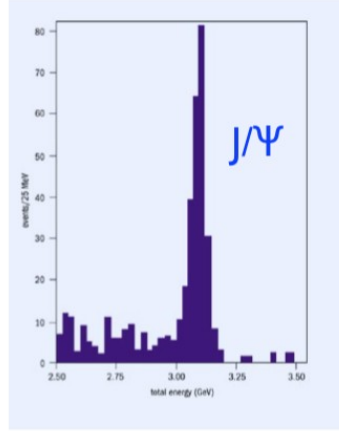
1972 — CERN

Neutral currents



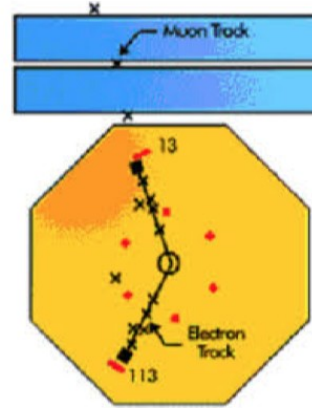
1974 — BNL, SLAC

Charm



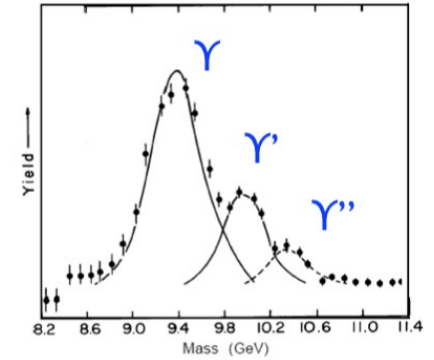
1976 — SLAC

Tau lepton



1979 — Fermilab

Beauty



1983 — CERN/SppS

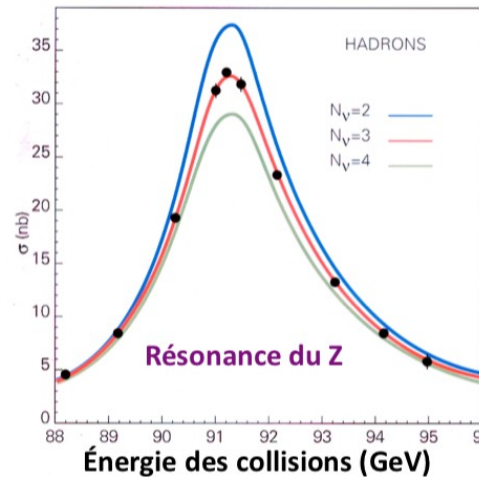
W and Z bosons



UA1, UA2

1990 — CERN/LEP

Three families of neutrinos

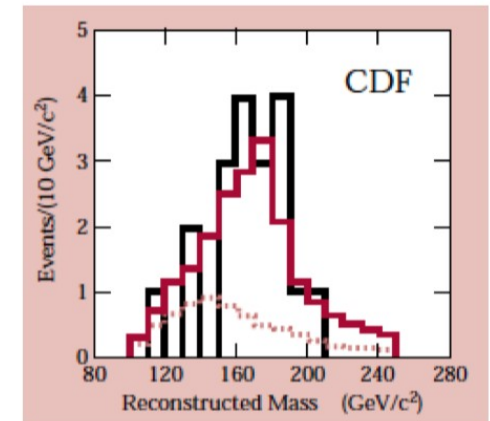


ALEPH, DEPHI, L3, OPAL

(experimental) LHC physics

1994 — Fermilab/TeVatron

Top quark



CDF, D0

# How do we compare experiment and predictions in a quantum field theory?

Through two fundamental quantities:

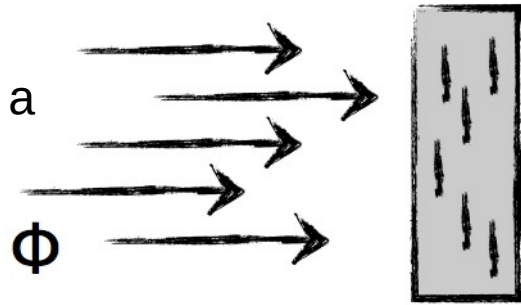
- $\sigma$  (cross section): probability of a particle of being produced in collisions at a given energy (es. 13 TeV at LHC)
  - ✓ May be *differential*, that is, as a function of the energy of the particle, the angles of its trajectory, or both of them, etc.
- $\Gamma$  (decay rate): probability (over time) of a particle of decaying into other particles
  - ✓ The sum of all possible decay rates  $\Gamma_i$ , gives the total decay rate, and because of resonance theory, it is the inverse of decay time:  $\tau = 1/\Gamma$

# How do we compare experiment and predictions in a quantum field theory?

Through two fundamental quantities:

- $\sigma$  (cross section): **probability** of a particle of **being produced** in collisions **at a given energy** (es. 13 TeV at LHC)
  - ✓ May be *differential*, that is, as a function of the energy of the particle, the angles of its trajectory, or both of them, etc.

# Interaction cross section



The flux  $\Phi = \frac{1}{S} \dot{N}_a$  represent the number of particles, per unit of time, sent over a surface  $S$  (the illuminated area) of the target.  $[\Phi] = [L^{-2} t^{-1}]$

The number of reactions per unit of time is proportional to the number of targets and the flux of the incoming particles

$$\dot{N}_r = \sigma \Phi N_{targets} \quad [\sigma] = [L^2]$$

$\sigma$  is the interaction cross section and the quantity  $\mathcal{L} = \Phi N_{targets}$  is the so called instantaneous luminosity. The integrated luminosity is defined as  $L = \int \mathcal{L} dt$ .

The reaction rate per single target and single incoming particle is

$$W_r = \frac{\dot{N}_r}{N_a N_{targets}} = \sigma \frac{v_a}{V} = \frac{2 \pi}{\hbar} |M_{fi}|^2 \rho(E')$$

# Interaction cross section

We can go to differentials

$$dW_r = \frac{2\pi}{\hbar} |M_{fi}|^2 \rho(E')$$

(the differential in the right part is hidden in the density state term)

With some math, see for example [], we can obtain, e.g., the cross section as a function of the solid angle

$$\frac{d\sigma_r}{d\Omega} = \frac{1}{4\pi^2 \hbar^4} \frac{p_f^2}{v_f v_i} |M(q^2)|^2 = \frac{1}{\mathcal{L}} \frac{\Delta \dot{N}_r}{\Delta \Omega}$$

**We can compare experiments and theory!**

The typical units in which the cross section is expressed is the *barn*

$$1 b = 100 \text{ fm}^2 = 10^{-24} \text{ cm}^2 \simeq \pi r_{\text{uranium}}^2$$



# Luminosity in a collider

Number of events  
in unit of time

$$\dot{N}_r = \sigma \mathcal{L}$$

We want to **explore very rare processes**,  
i.e., with very low cross sections (or very  
rare decays).

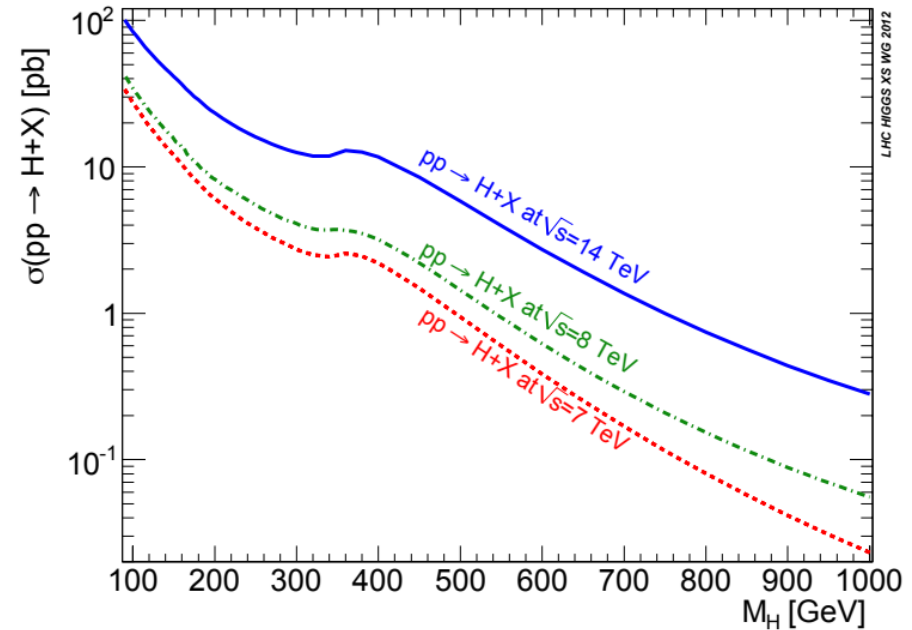
→ **go higher with instantaneous luminosity!**

In a collider ring:

$$\mathcal{L} = \frac{1}{4\pi} \frac{f N_1 N_2}{\sigma_x \sigma_y}$$

At LHC

- $N_1 = N_2 = 1.15 \cdot 10^{11}$  # of protons
- $f$  = bunch crossing frequency =  $j v / \ell$ ,  $v = c$  and  $\ell = 2\pi r$  with  $r = 26659$  m
  - $j = 2808$  effective bunches, one crossing every 25 ns ( $f = 40$  MHz), each bunch spaced 7.5 m. The effective number of bunches is 2808 ( $f = 31,6$  MHz)
- $\sigma_x \sim \sigma_y = 16 \mu\text{m}$
- $\mathcal{L} \sim 1.3 \cdot 10^{34} \text{ cm}^{-2}\text{s}^{-1}$



*Current*

*Beam sizes (RMS)*

# LHC

$pp$  collider (2008-present)

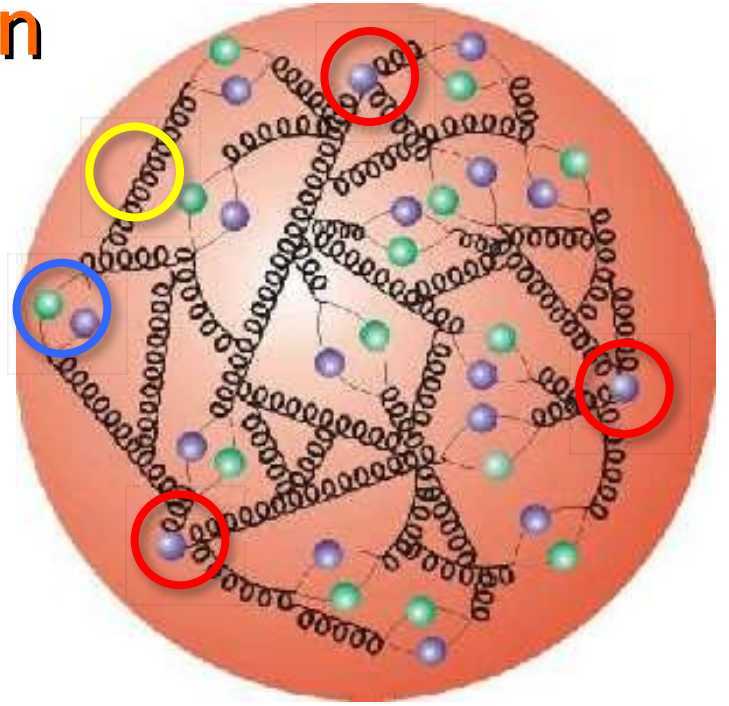
$\sqrt{s} = 7\text{-}8\text{-}13\text{-}13.6\text{ TeV}$



# About the inner life of a proton

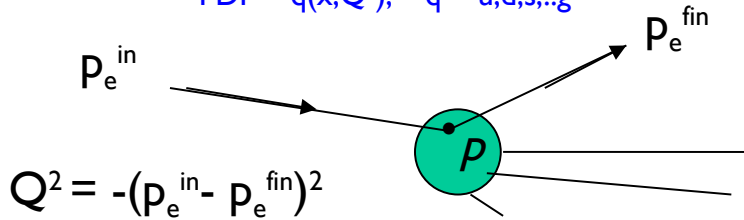
- **Protons have substructure!**

- ✓ partons = quarks & gluons
- ✓ 3 valence (colored) quarks bound by gluons
- ✓ Gluons (colored) have self-interactions
- ✓ Virtual quark pairs can pop-up (sea-quark)
- ✓  $p$  momentum shared among constituents
  - described by  $p$  structure functions



- **Parton energy not 'monochromatic'**

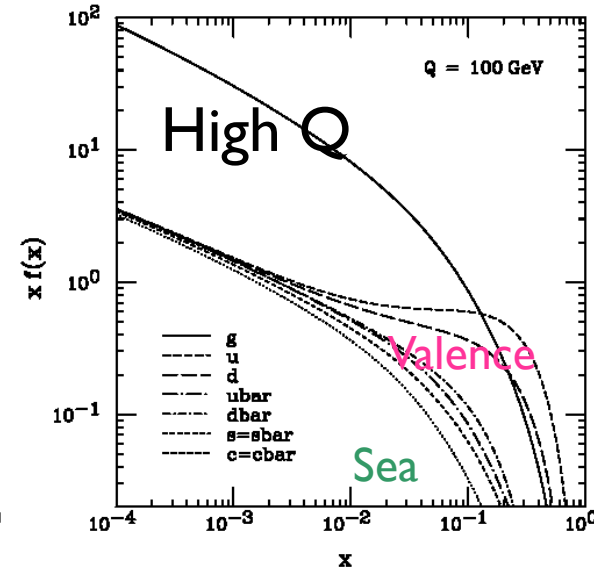
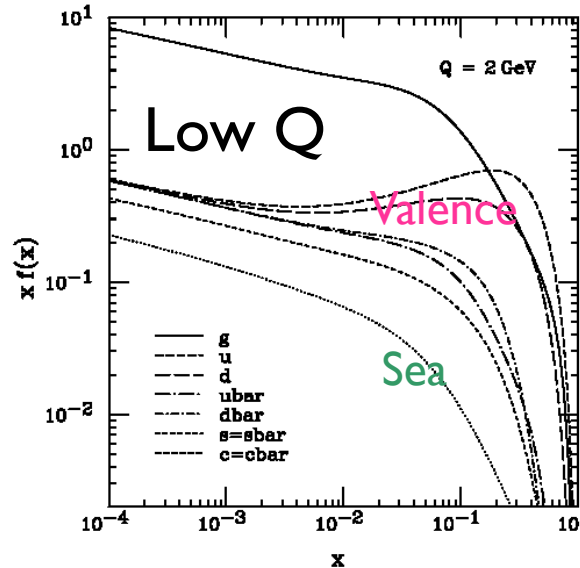
- ✓ Parton Distribution Function
  - PDF =  $q(x, Q^2)$ ,  $q = u, d, s, \dots, g$



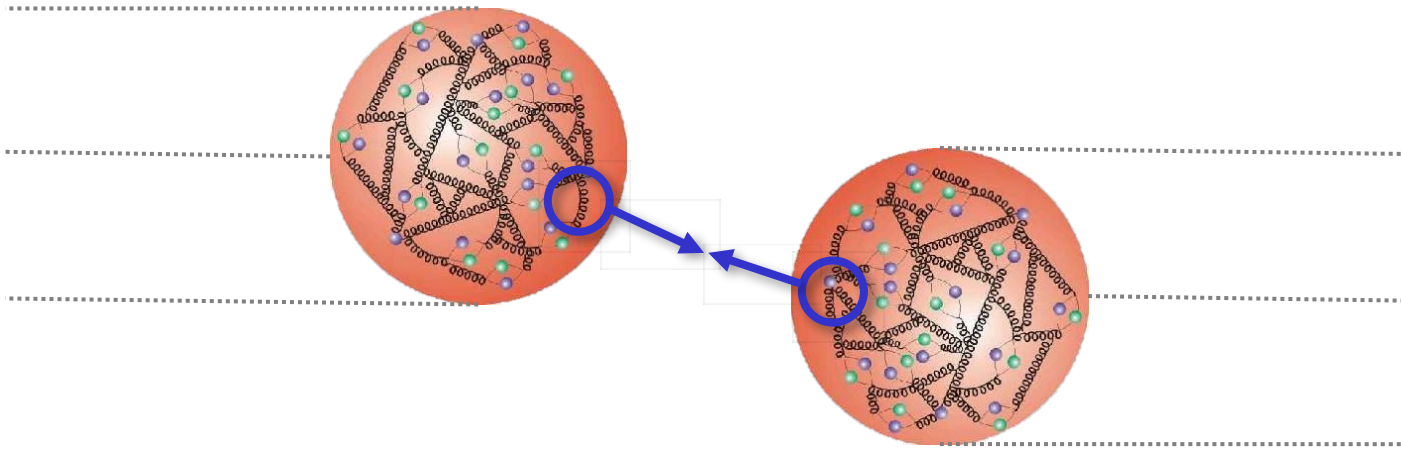
$$Q^2 = -(p_e^{\text{in}} - p_e^{\text{fin}})^2$$

- **Kinematic variables**

- ✓ Bjorken- $x$ : fraction of the proton momentum carried by struck parton
  - $x = p_{\text{parton}} / p_{\text{proton}}$
- ✓  $Q^2$ : 4-momentum<sup>2</sup> transfer

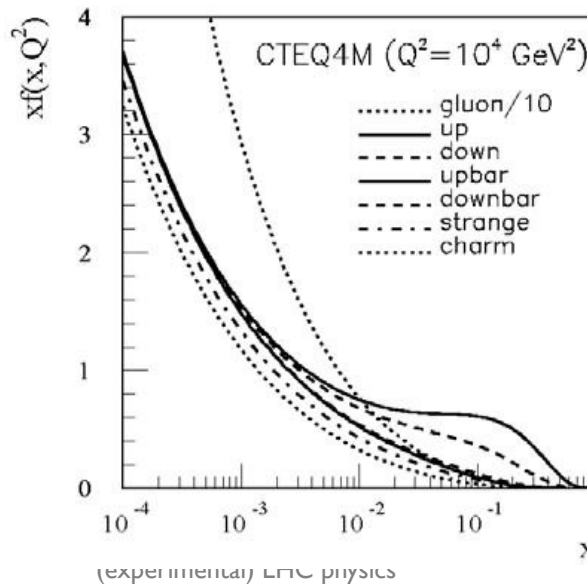
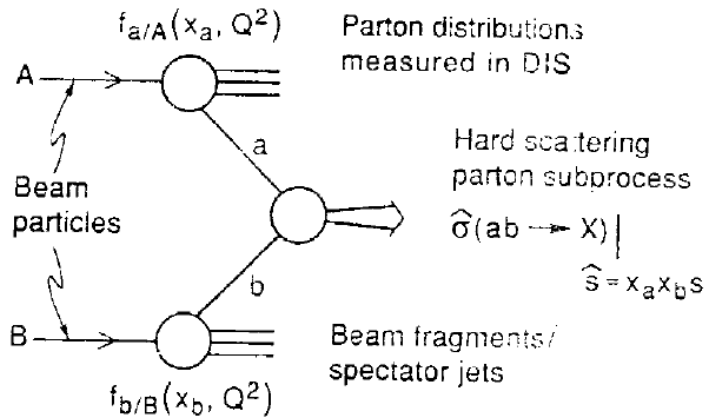


# Cross sections at a proton-proton collider



$$\sqrt{\hat{s}} = \sqrt{x_a x_b S}$$

$$\sigma = \sum_{a,b} \int dx_a dx_b f_a(x, Q^2) f_b(x, Q^2) \hat{\sigma}_{ab}(x_a, x_b)$$

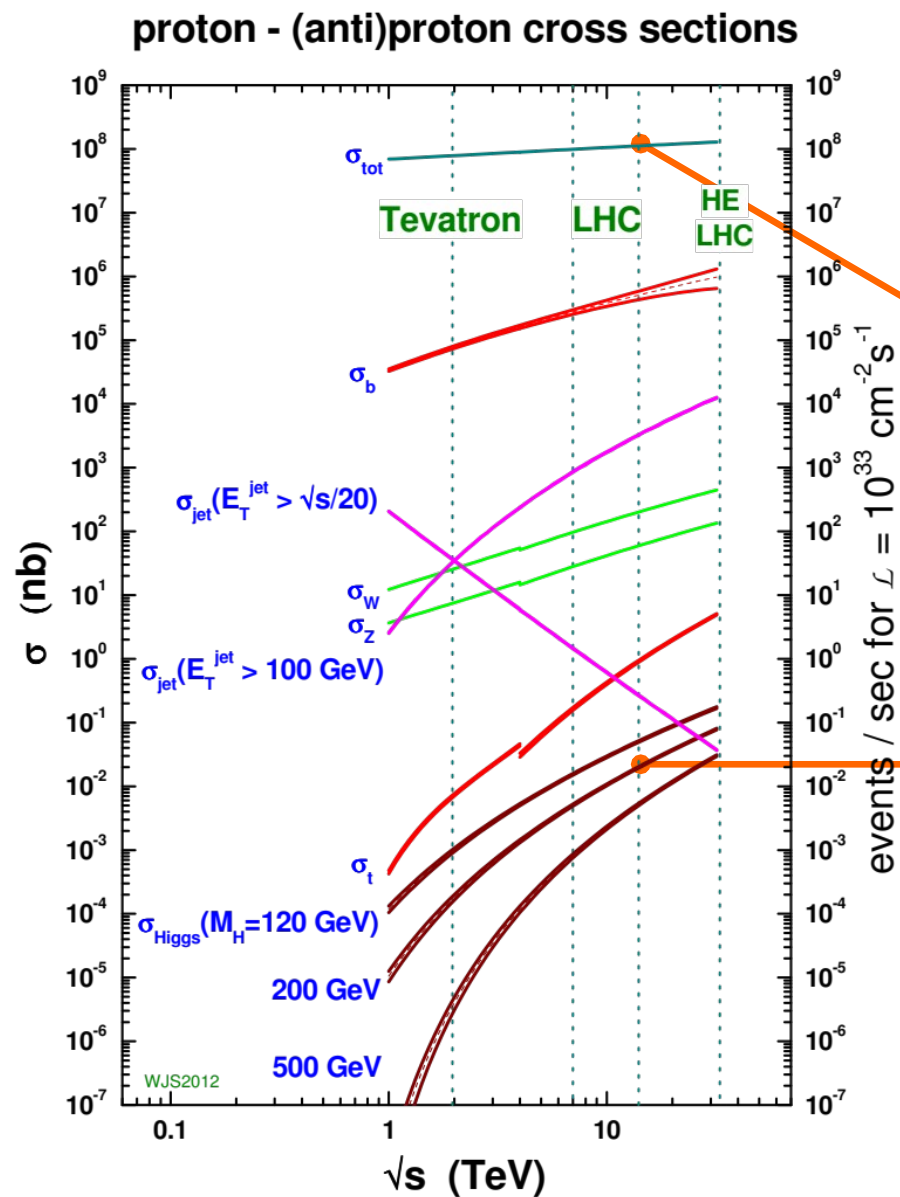


Example: to produce a particle with mass  $m = 100 \text{ GeV}$

$$\sqrt{\hat{s}} = 100 \text{ GeV}$$

$$\sqrt{s} = 14 \text{ TeV} \Leftrightarrow x_a x_b = 0.007$$

# Cross-sections at LHC



$$1 \text{ nb} = 10^{-33} \text{ cm}^2$$

$$\sigma_{\text{tot}} (13 \text{ TeV}) = 10^8 \text{ nb} = 10^{-25} \text{ cm}^2$$

$$\sigma_H (13 \text{ TeV}) = 0.05 \text{ nb} = 5 \cdot 10^{-35} \text{ cm}^2$$

$$\text{LHC instantaneous luminosity } L = 1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$$

total  $pp$  collisions

$10^9$  events/s

$\sim 10^{10}$

$10^{-1}$  events/s

$\sim 1$  Higgs boson  
every 2 seconds

$[m_H \sim 125 \text{ GeV}]$

events / sec for  $\mathcal{L} = 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

# How do we compare experiment and prediction in a quantum field theory?

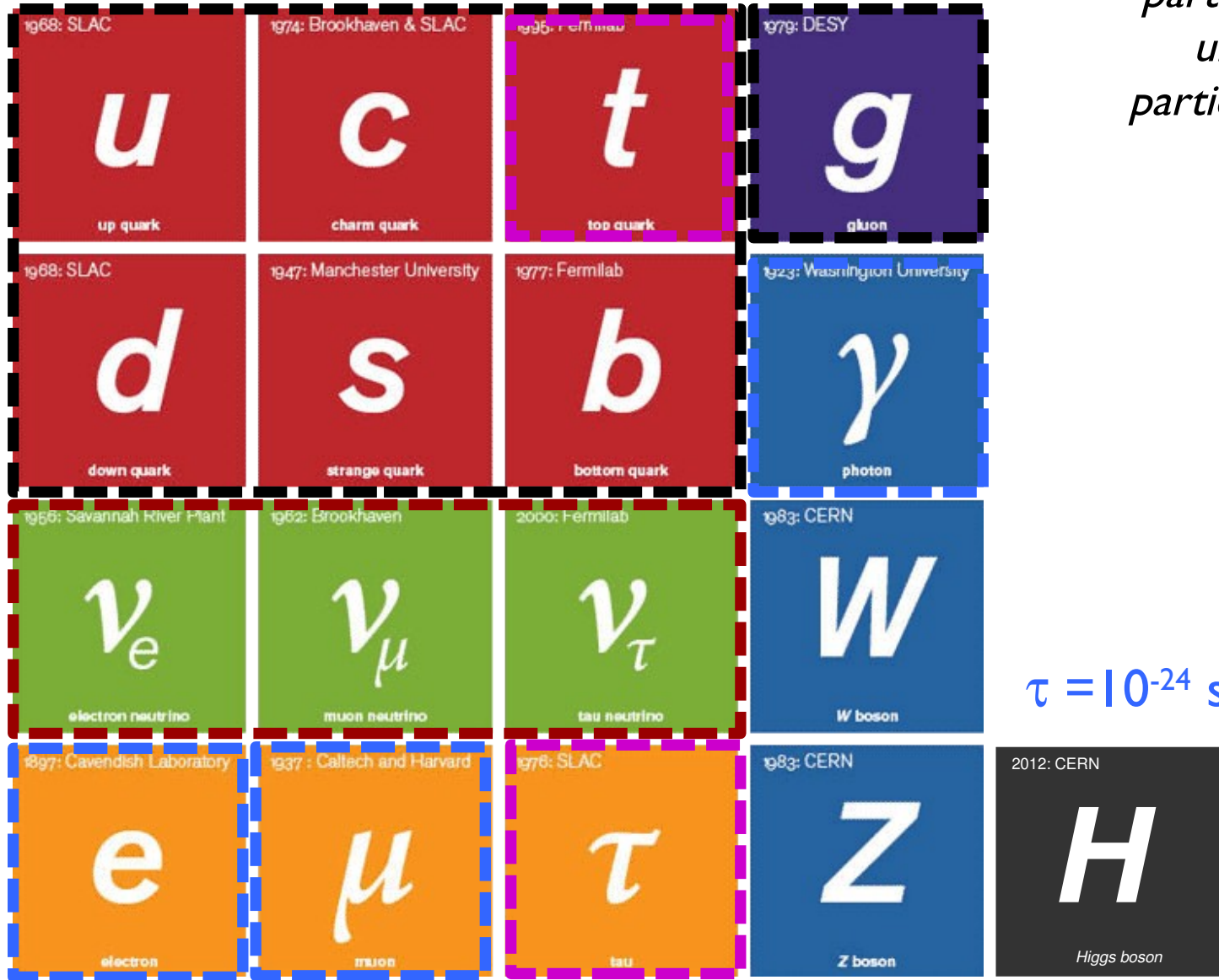
Through two fundamental quantities:

- $\sigma$  (cross section): probability of a particle of being produced in collisions at a given energy (es. 13 TeV at LHC)
  - ✓ May be *differential*, that is, as a function of the energy of the particle, the angles of its trajectory, etc.
- $\Gamma$  (decay rate): **probability** of a particle of **decaying into certain specific final particles**
  - ✓ The sum of all  $\Gamma$ 's is the **total decay rate**, and because of **resonance theory** it is the inverse of its **decay time**:  $\tau = \hbar/\Gamma$

$$W_r = \frac{\Gamma}{\hbar}$$

# What do we want to measure?

... “stable”  
particles from  
unstable  
particle decays!



$\tau = \infty$

$\tau = 10^{-24} \text{ s}$

$\tau = 2.2 \mu\text{s}$

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# What do we want to measure?

decays?

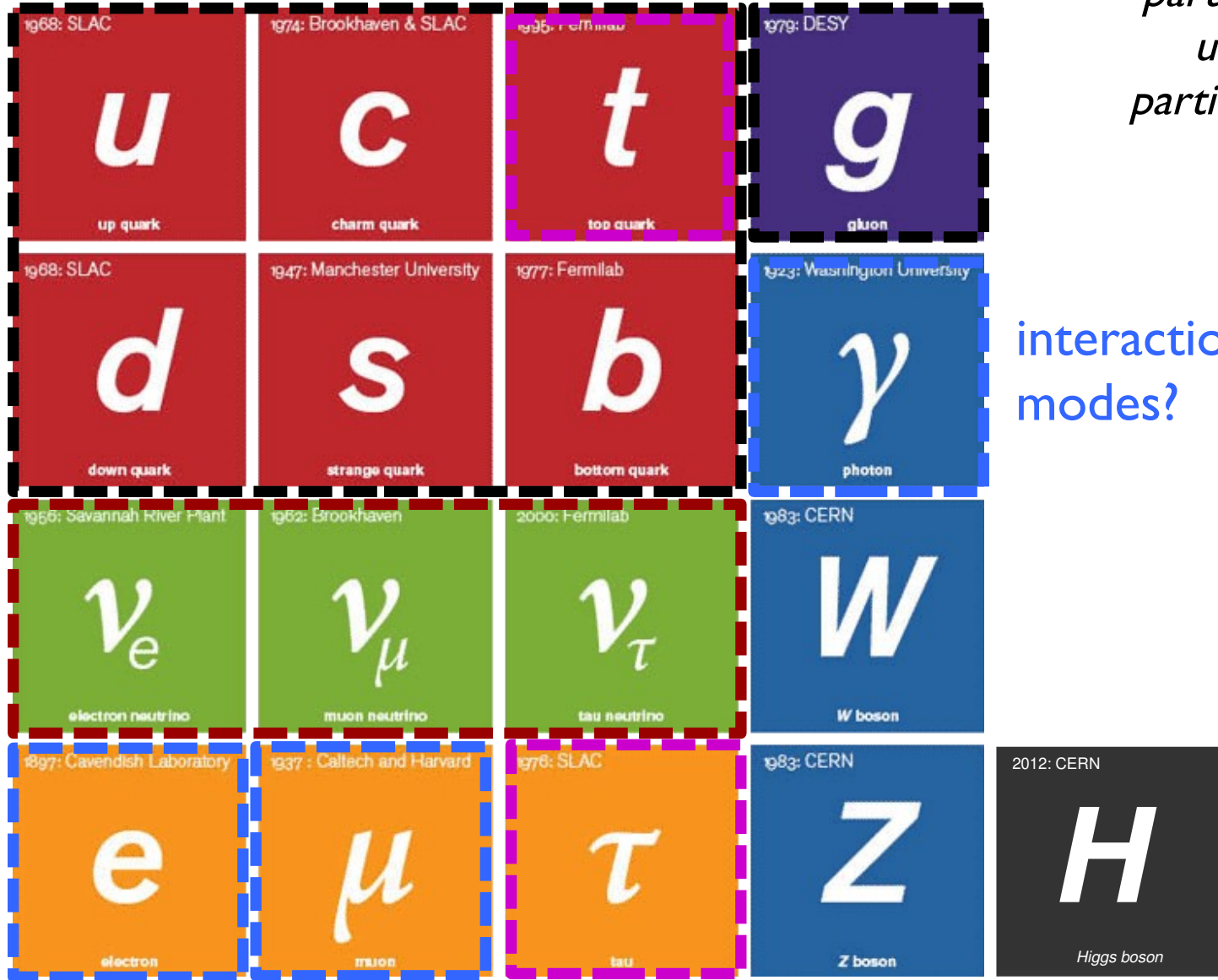
... “stable”  
particles from  
unstable  
particle decays!

hadron  
jets

interaction  
modes?

invisible  
*in particle  
detectors at  
accelerators*

interaction  
modes?



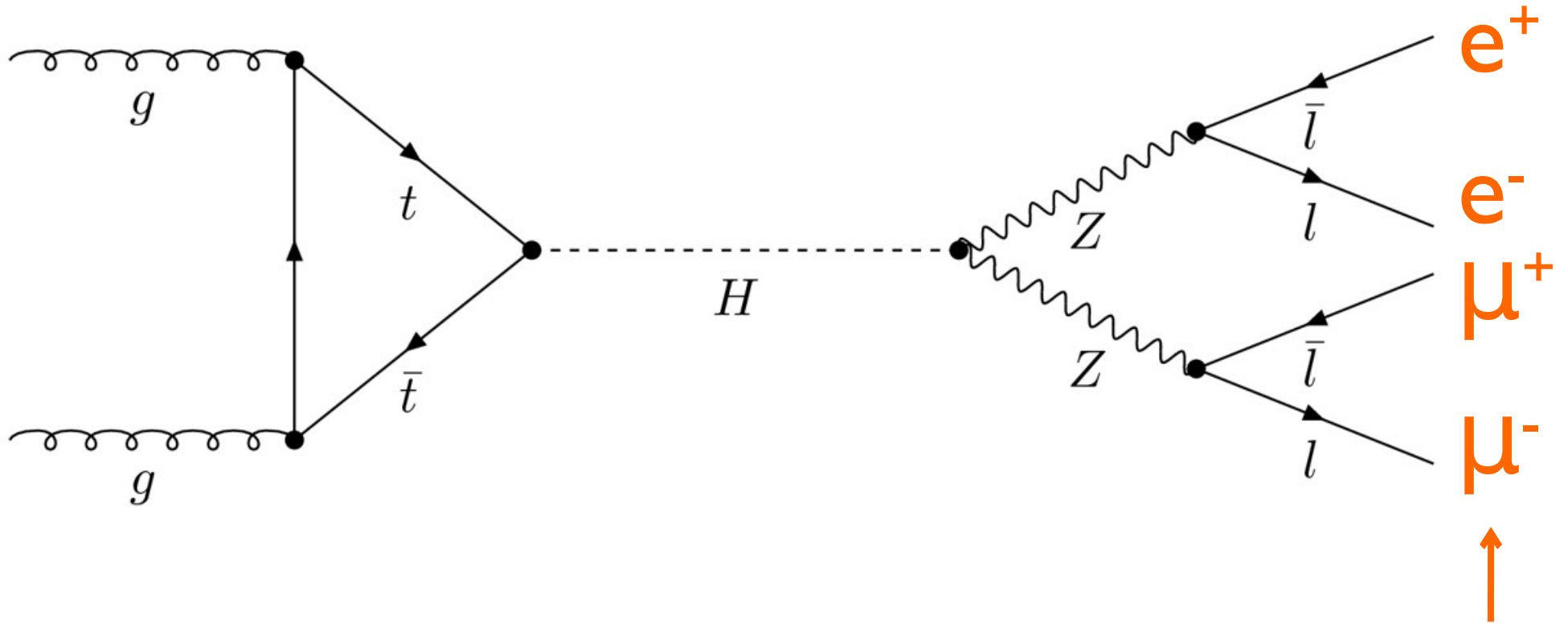
decays?



# What do we want to measure?

*Example: let's assume a Higgs boson is produced at the LHC ...  
It is a **SM** particle, we can predict how and how frequently*

*... we look for “stable” particles from an unstable particle decays*



this is what we are looking for...

# Identifying and measuring “stable” particles

- Particles are characterized by
  - ✓ **Mass** [Unit: eV/c<sup>2</sup> or eV]
  - ✓ **Charge** [Unit: e]
  - ✓ **Energy** [Unit: eV]
  - ✓ **Momentum** [Unit: eV/c or eV]
  - ✓ (+ spin, lifetime, ...)

Particle identification via measurement of:

e.g. (E, p, q) or (p, β, q)  
(p, m, q) ...

- ... and move at **relativistic speed** (here in “natural” unit:  $\hbar = c = 1$ )

$$\beta = \frac{v}{c} \quad \gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

$$l = \frac{l_0}{\gamma} \quad \text{length contraction}$$

$$t = t_0 \gamma \quad \text{time dilation}$$

$$E^2 = \vec{p}^2 + m^2$$
$$E = m\gamma \quad \vec{p} = m\gamma\vec{\beta}$$
$$\vec{\beta} = \frac{\vec{p}}{E}$$

# Center of mass energy

- In the **center-of-mass frame** the total 3-momentum is 0
- In **laboratory frame**, the center of mass energy can be computed as:

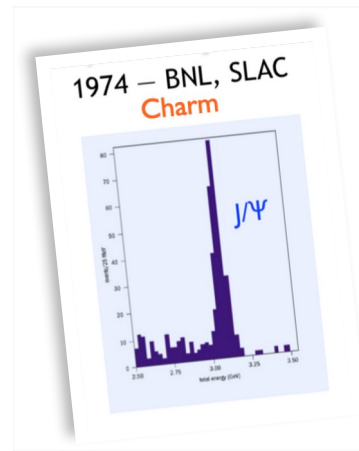
$$E_{\text{cm}} = \sqrt{s} = \sqrt{\left(\sum E_i\right)^2 - \left(\sum \vec{p}_i\right)^2}$$

Hint: it can be computed as the “length” of the total four-momentum, that is invariant:

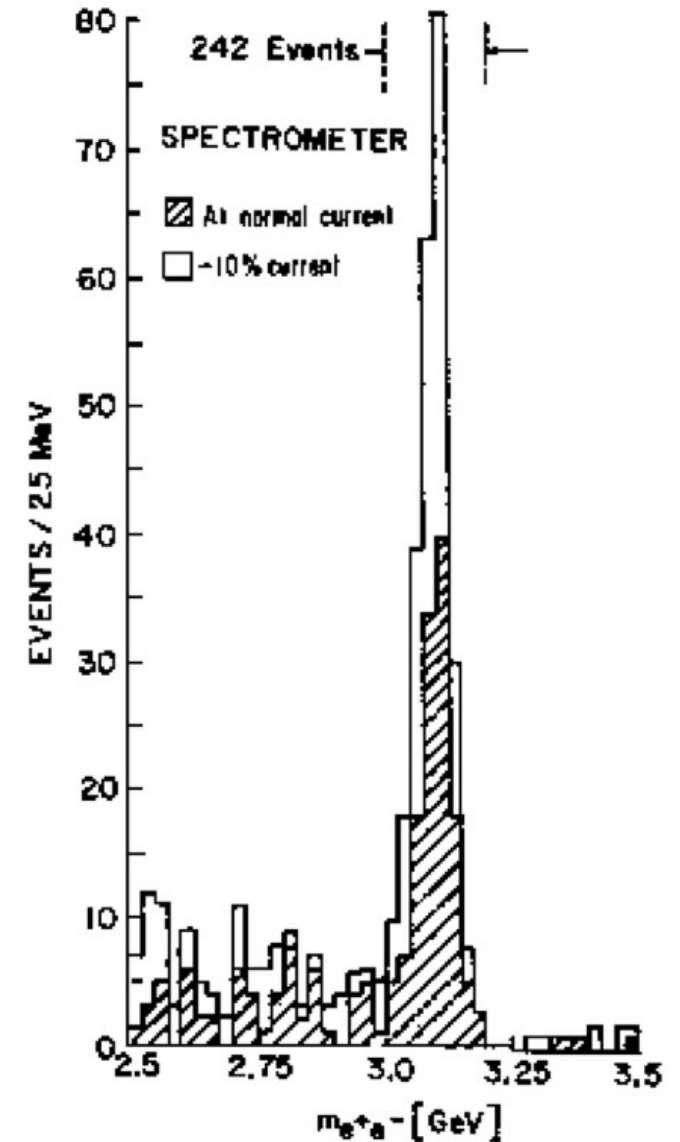
$$p = (E, \vec{p}) \quad \sqrt{p \cdot p}$$

What is the “length” of a the four-momentum of a particle?

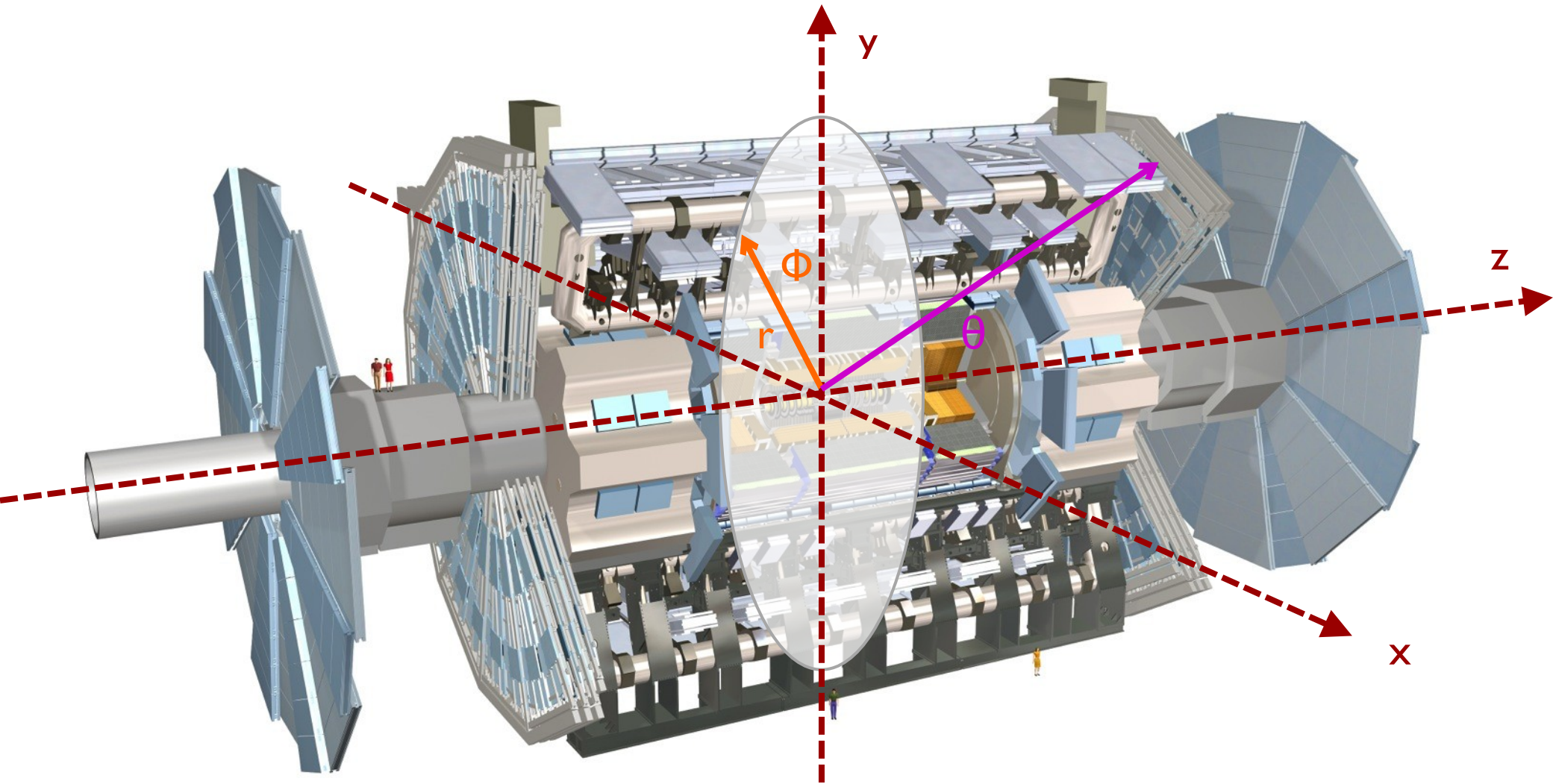
# Invariant mass



$$M = \sqrt{\left(\sum E_i\right)^2 - \left(\sum \vec{p}_i\right)^2}$$



# A collider experiment



Presudorapidity  $\eta = -\ln \left[ \tan \left( \frac{\theta}{2} \right) \right]$

# Interaction mode cheat sheet (“light” particles)



- electrically charged
- ionization ( $dE/dx$ )
- *electromagnetic shower...*



- electrically charged
- ionization ( $dE/dx$ )
- can emit photons
  - ✓ electromagnetic shower induced by emitted photon...
  - but it's rare...

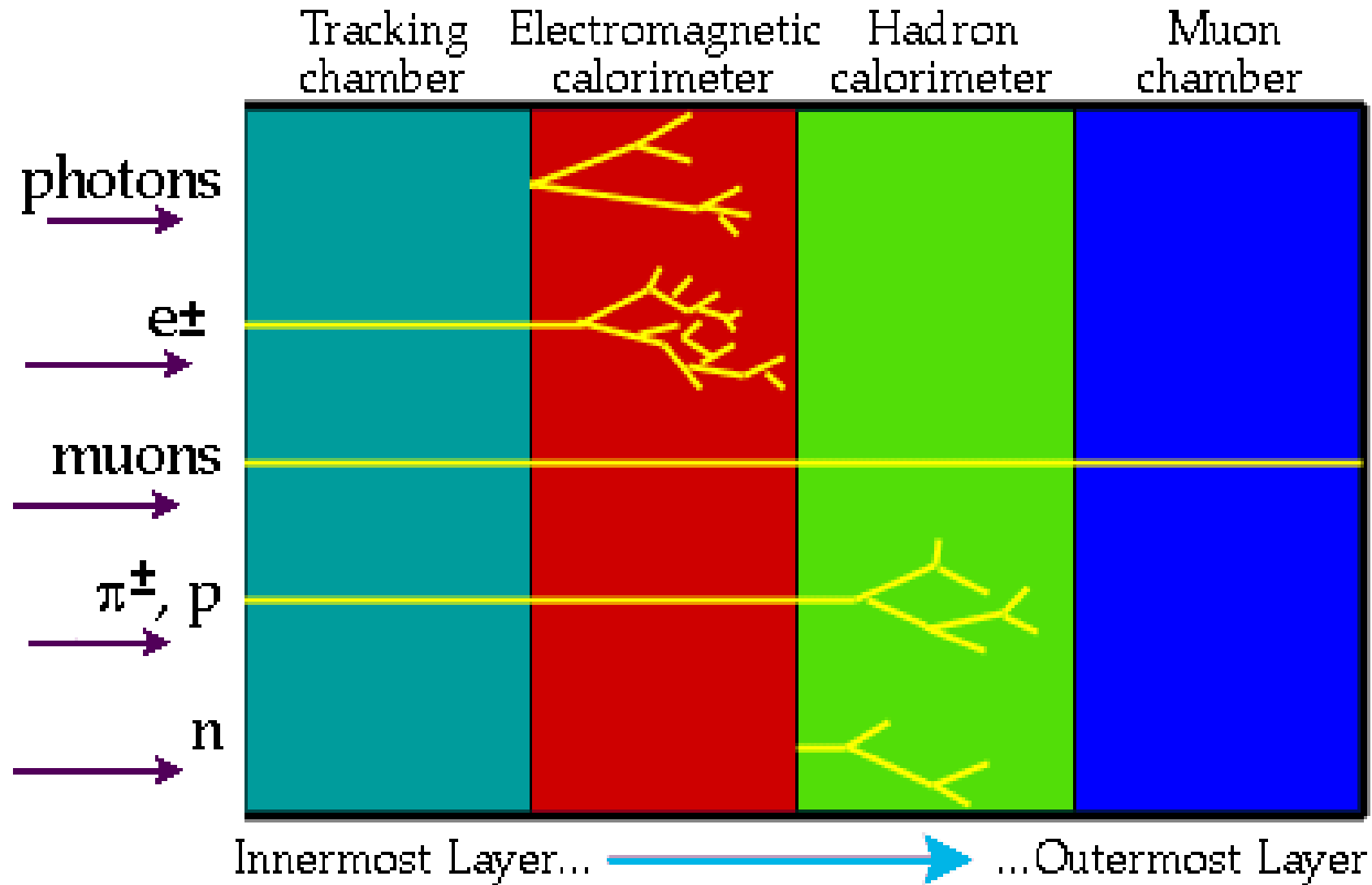


- electrically neutral
- pair production
  - ✓  $E > 1 \text{ MeV}$
- *electromagnetic shower...*



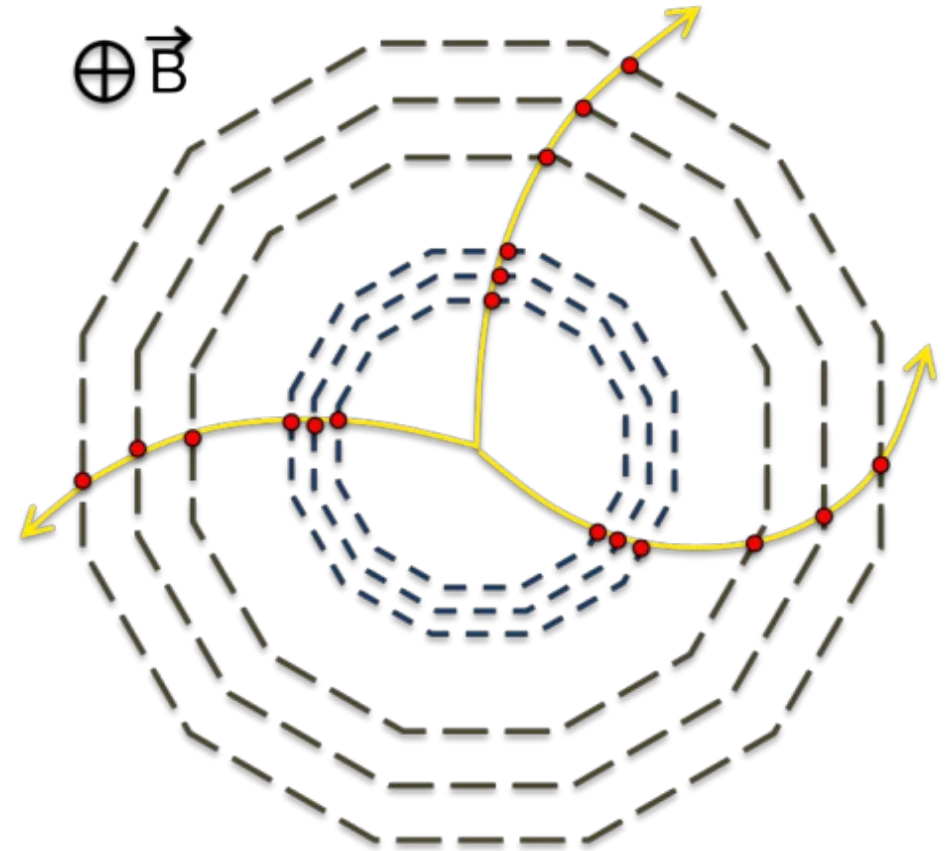
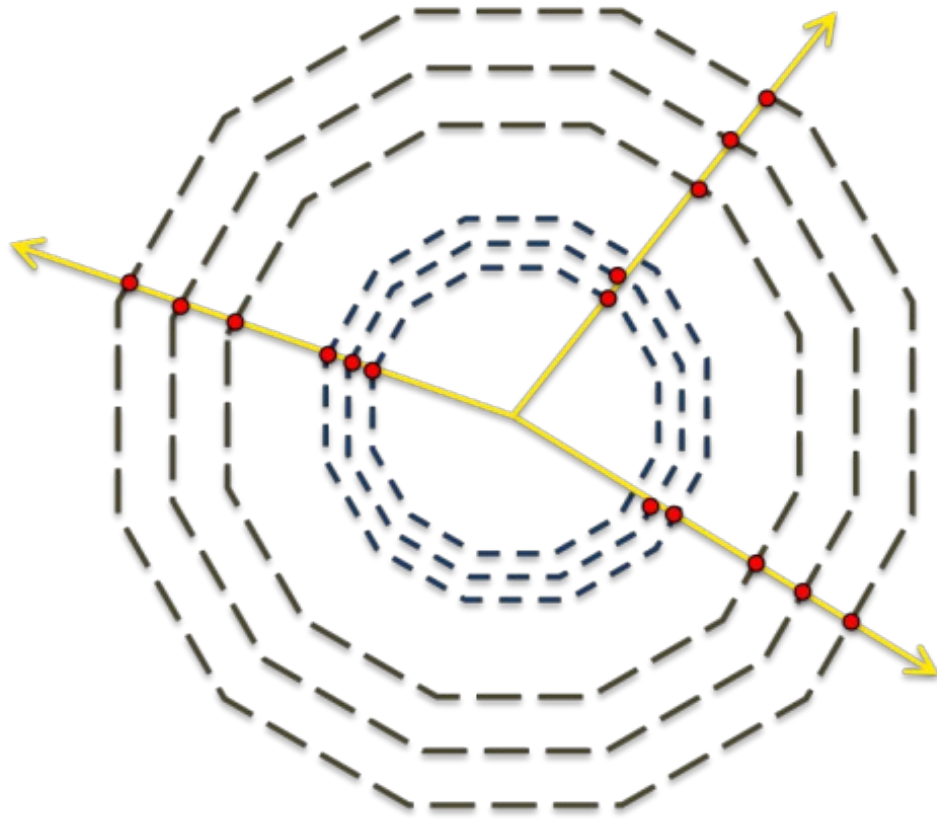
- produce *hadron(s)* jets via QCD hadronization process

# Interaction mode cheat sheet (“light” particles)



# Magnetic spectrometer for ionizing particles

- A system to measure (charged) particle momentum
- Tracking device + magnetic field



$$p[\text{GeV}] = 0.3B[\text{T}]\rho[\text{m}]$$

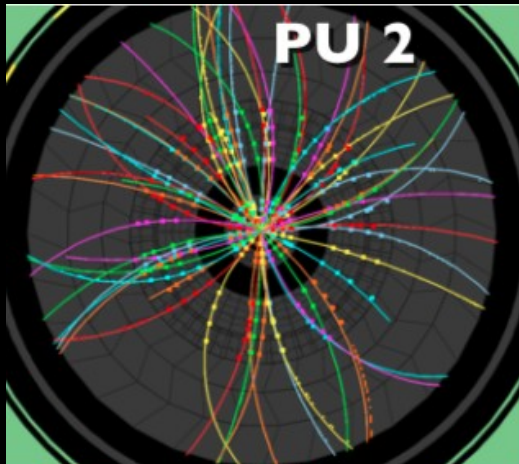
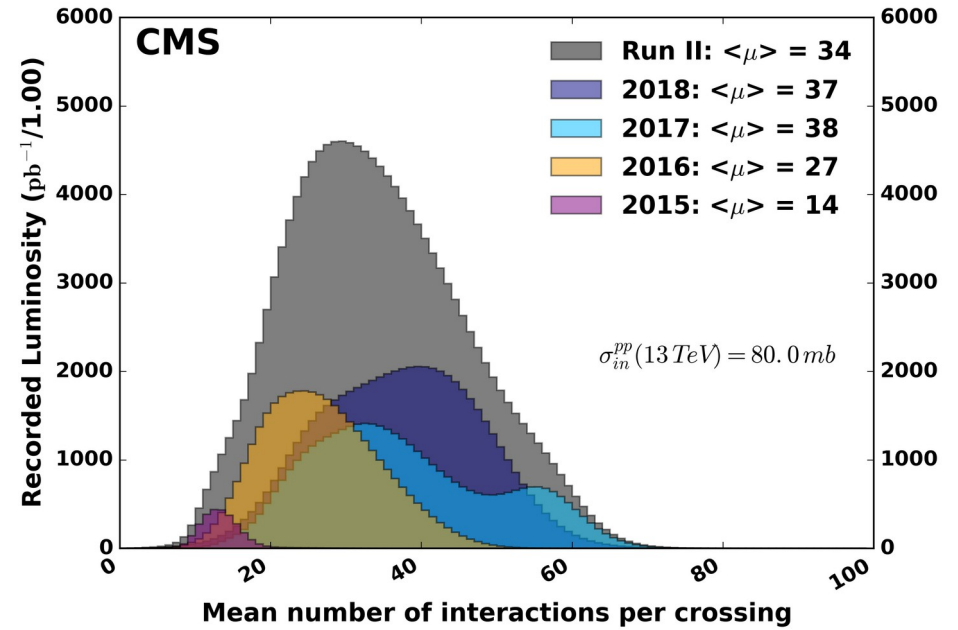


# Pile-Up

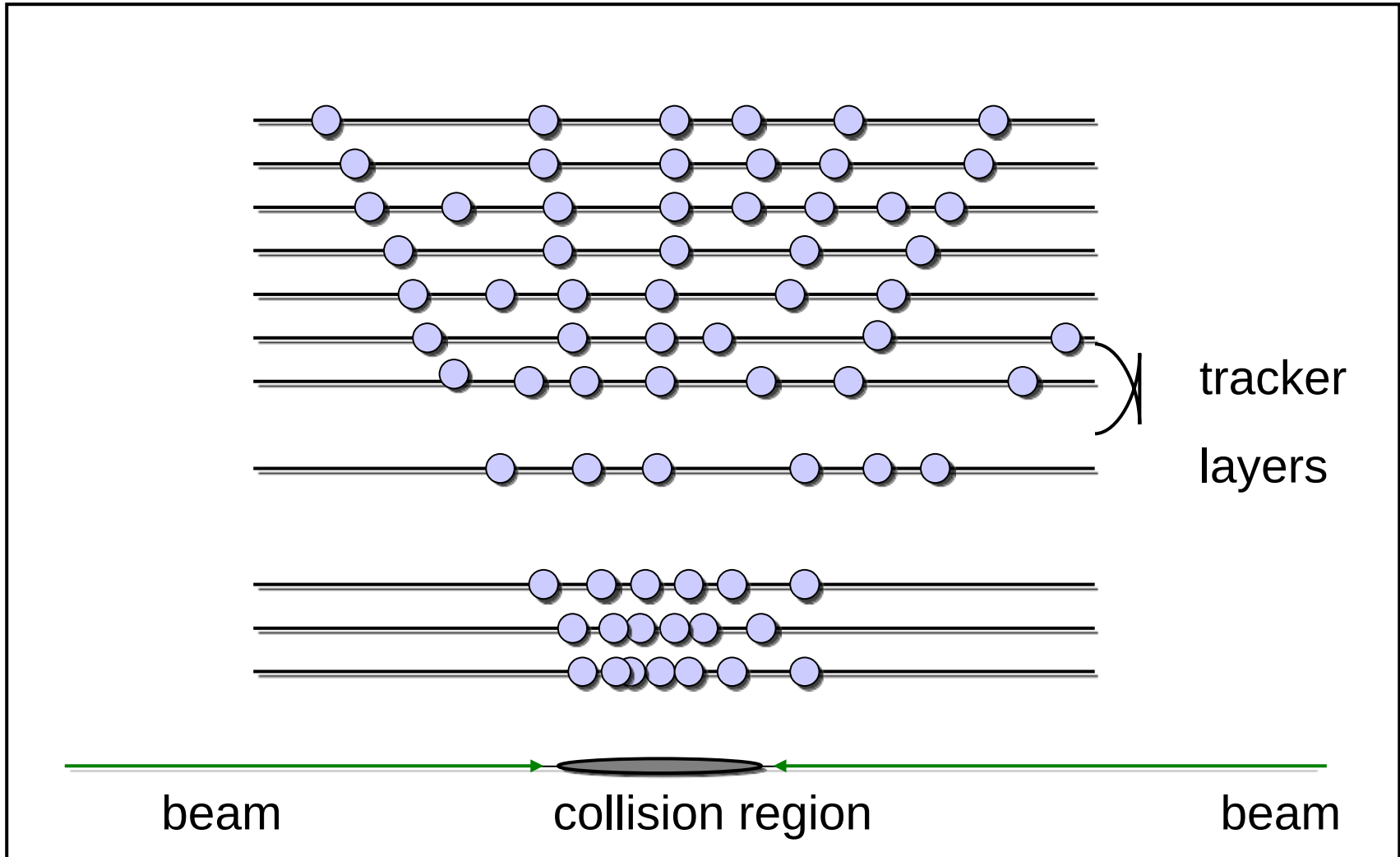
$$\mathcal{L} = \frac{1}{4\pi} \frac{f N_1 N_2}{\sigma_x \sigma_y}$$

PU = number of inelastic interactions per beam bunch crossing

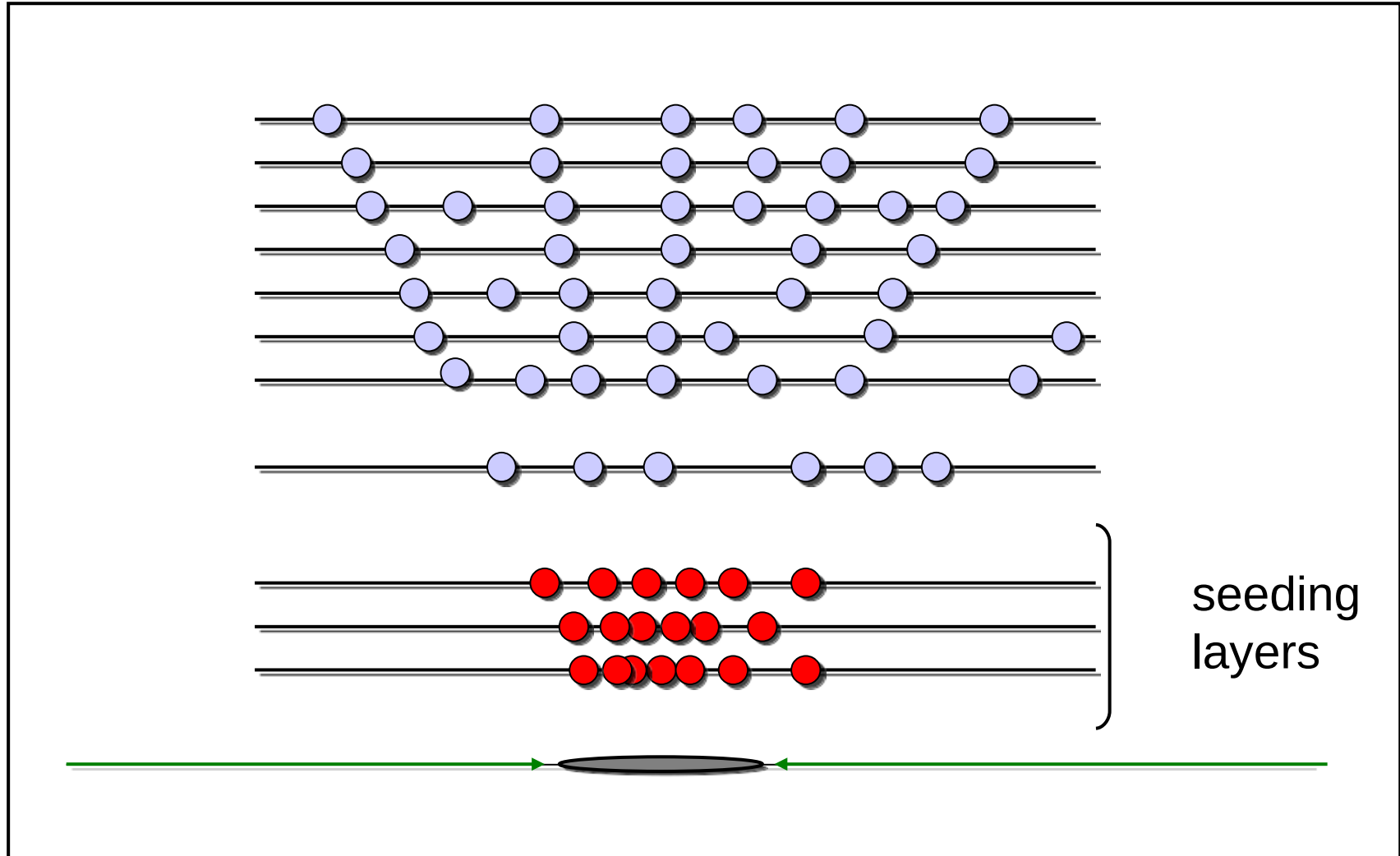
CMS Average Pileup (pp,  $\sqrt{s}=13$  TeV)



# Tracking



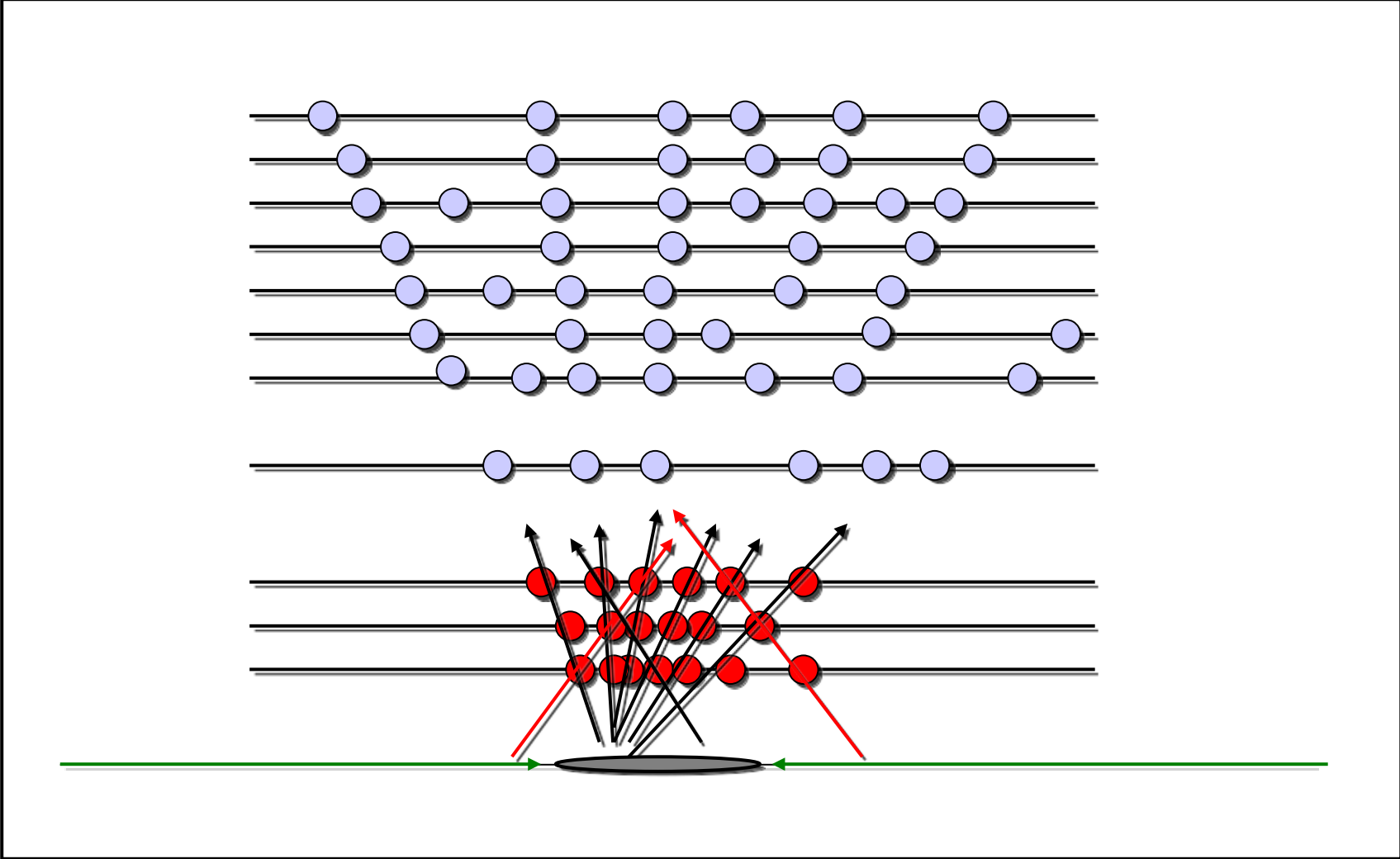
# Tracking



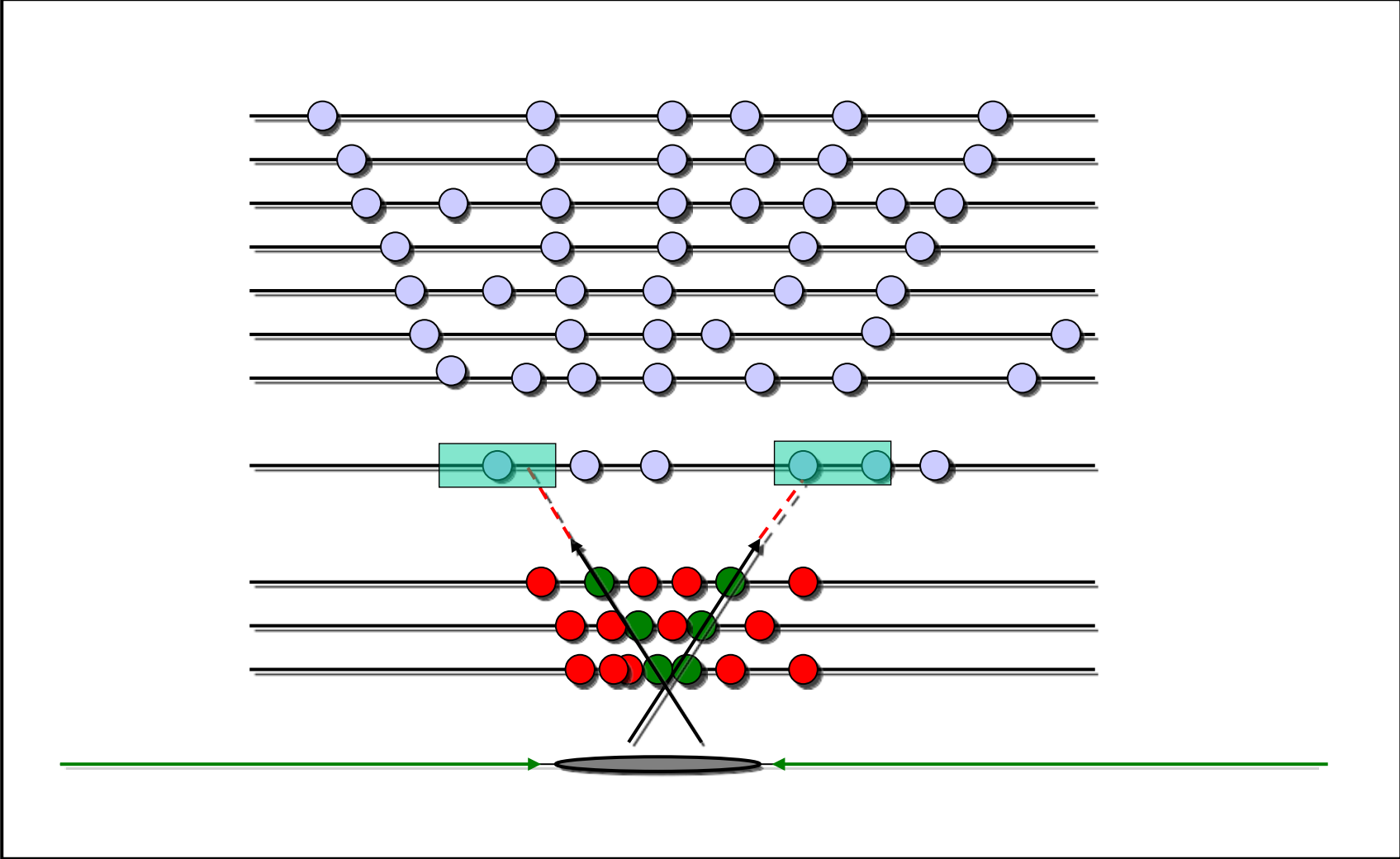
Only a subset of layers is used for

the construction of **trajectory seeds**

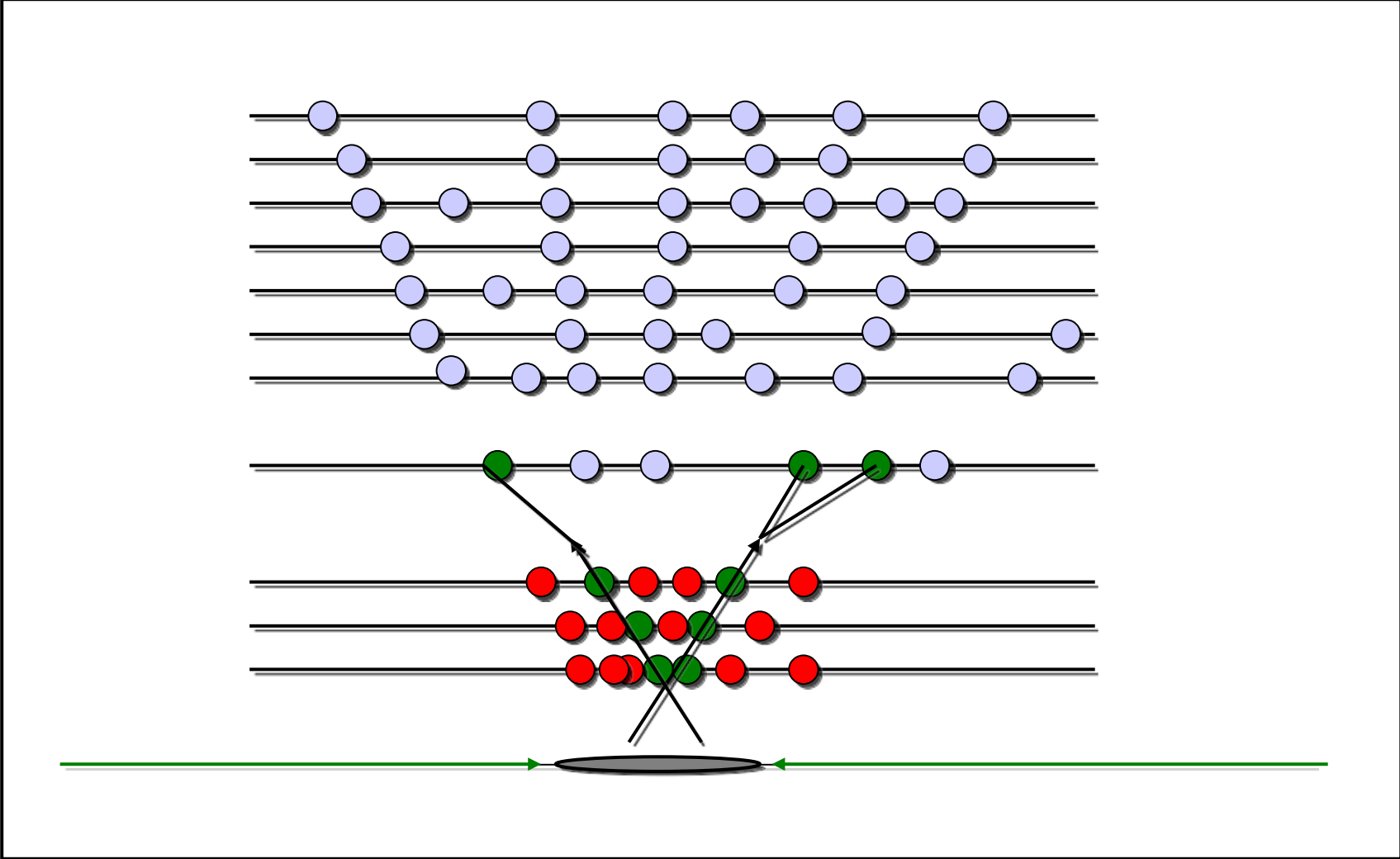
# Tracking



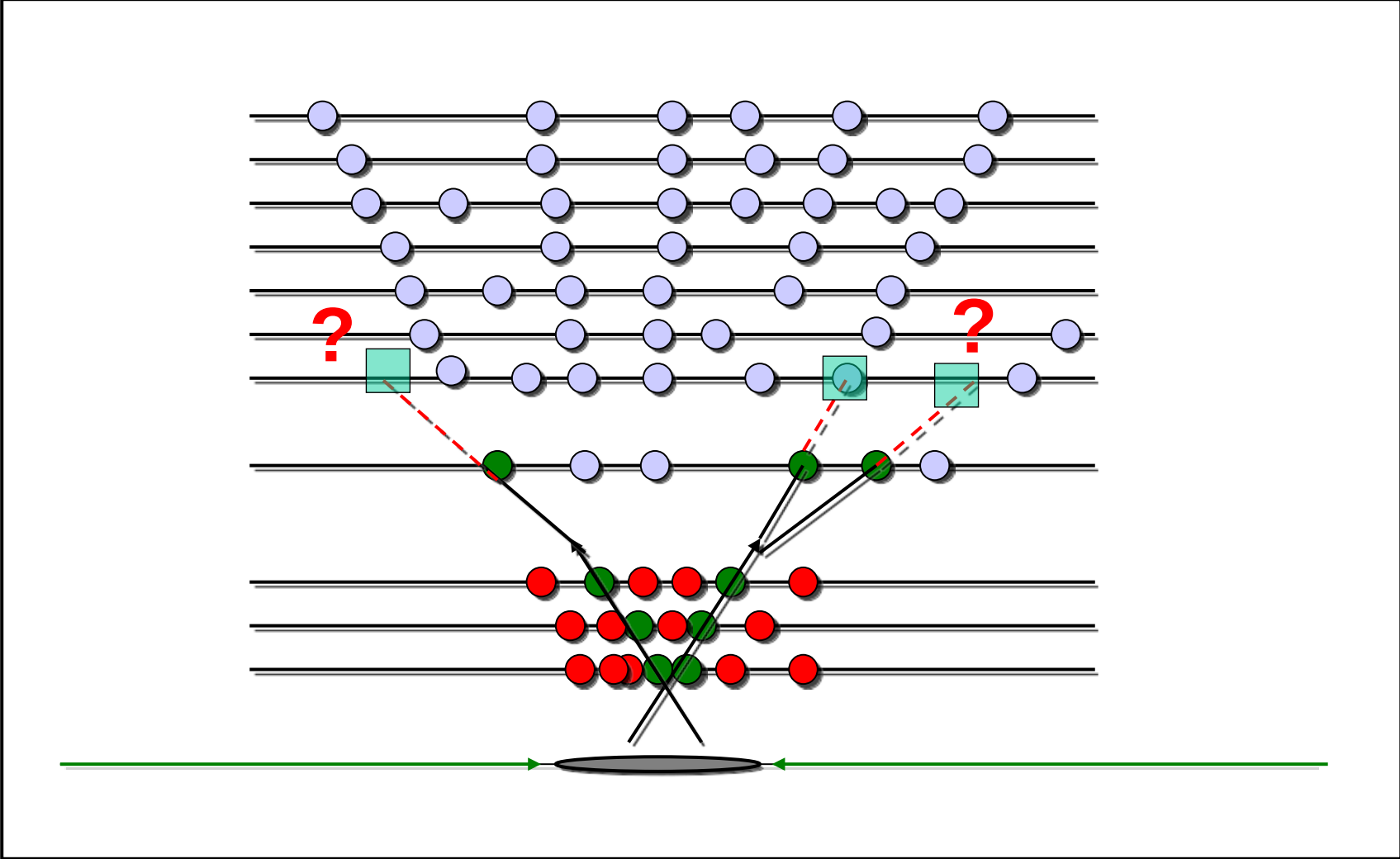
# Tracking



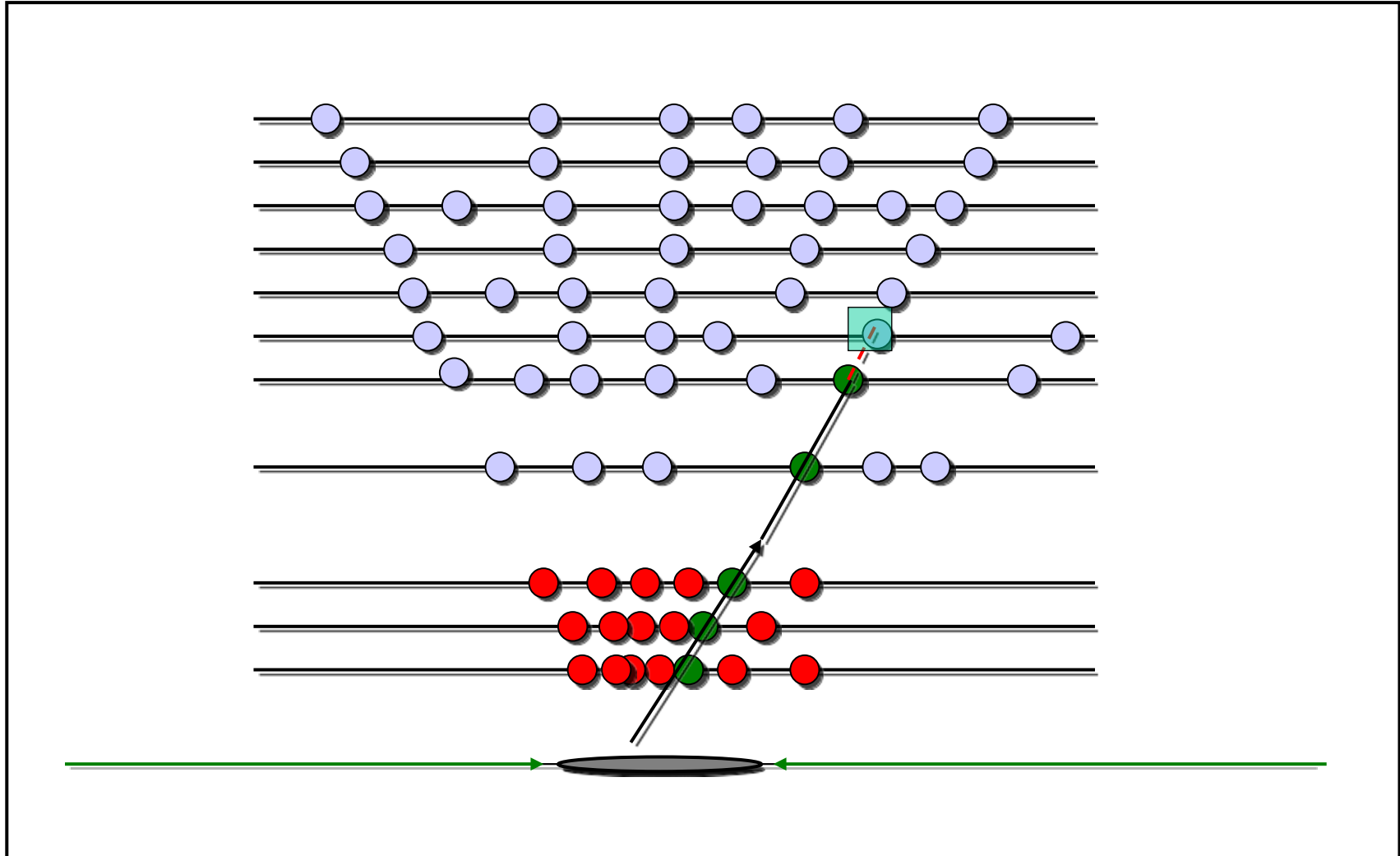
# Tracking



# Tracking

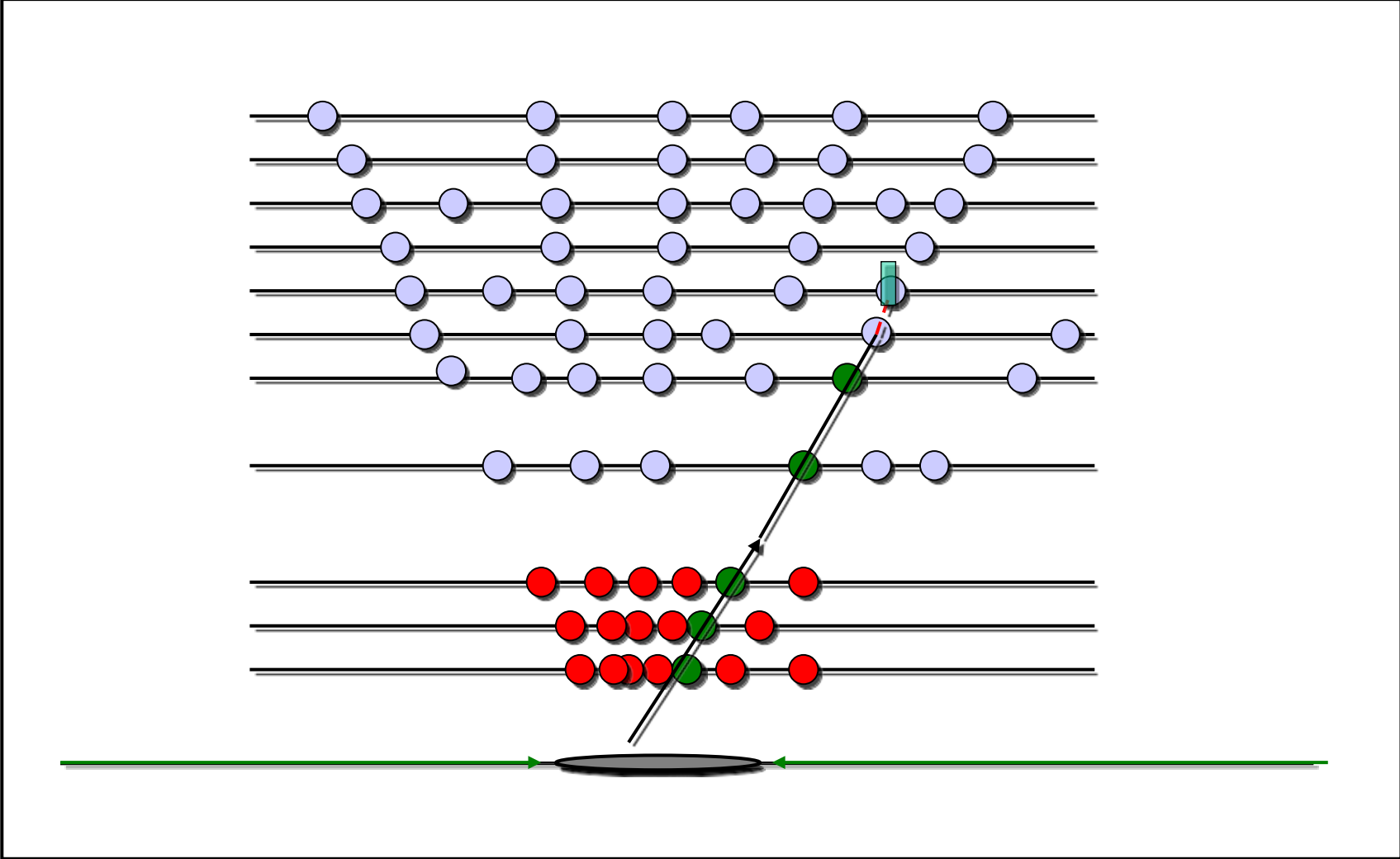


# Tracking

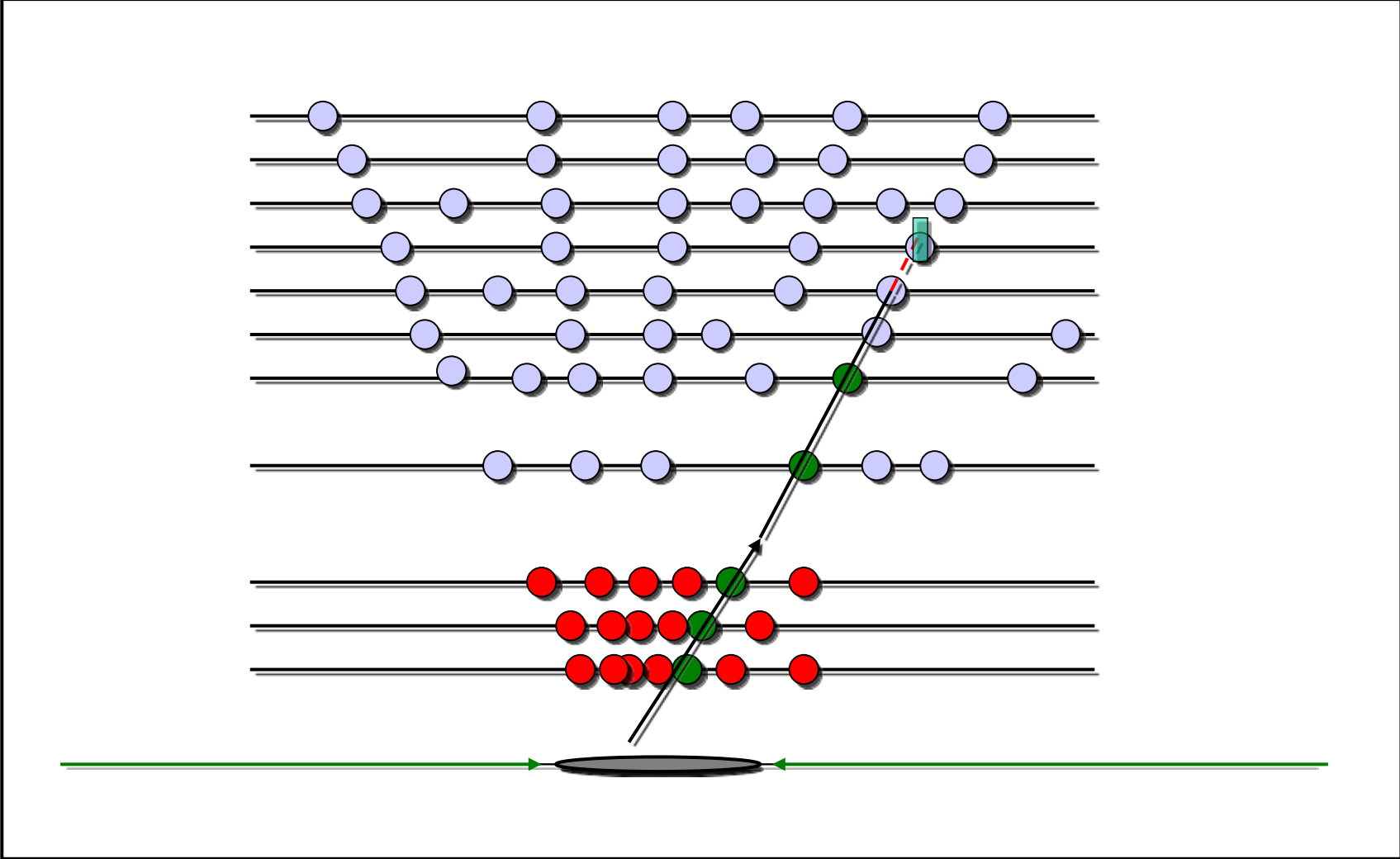




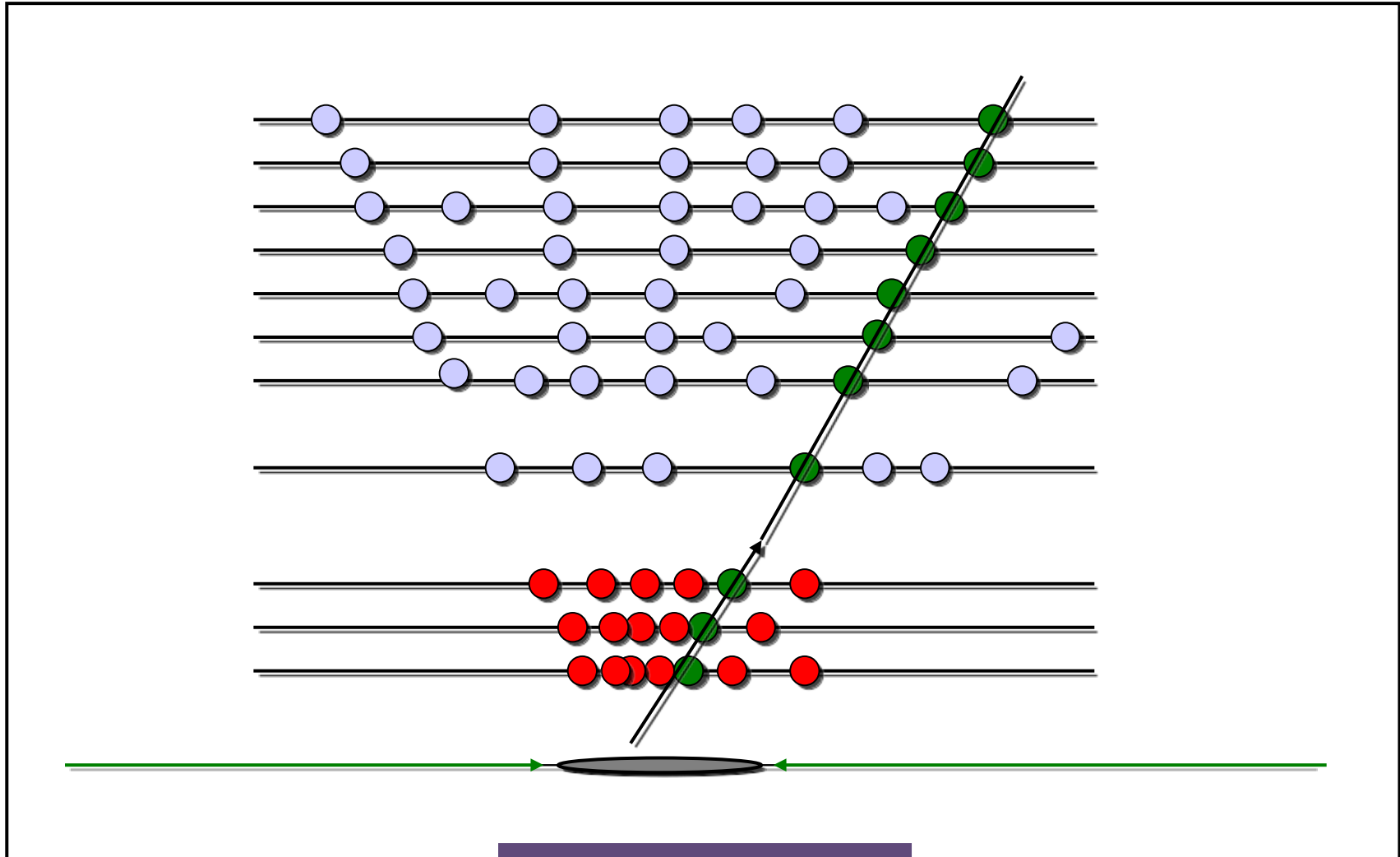
# Tracking



# Tracking

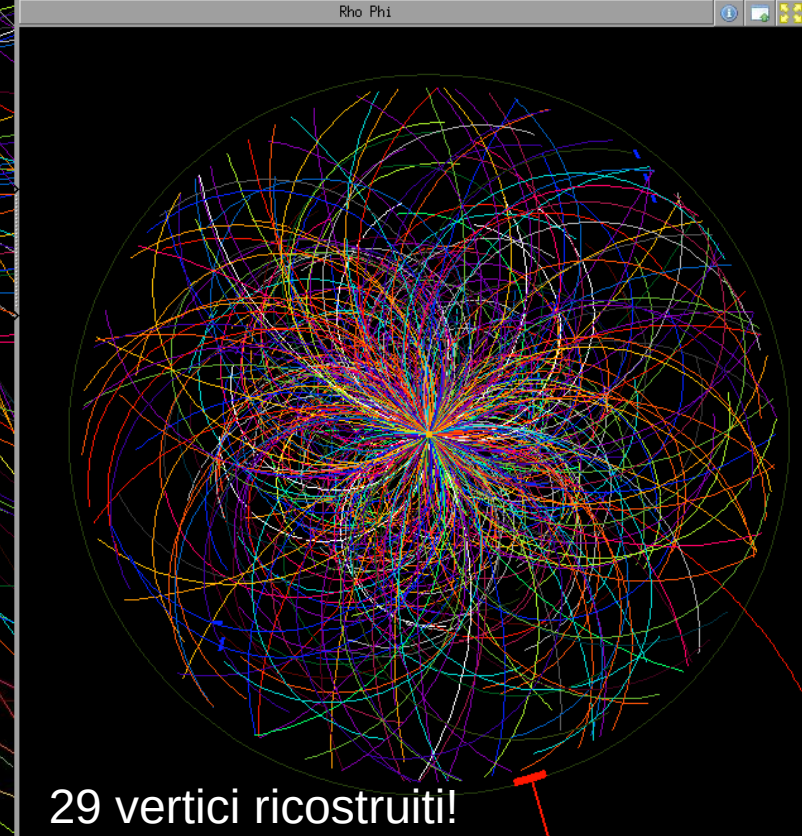
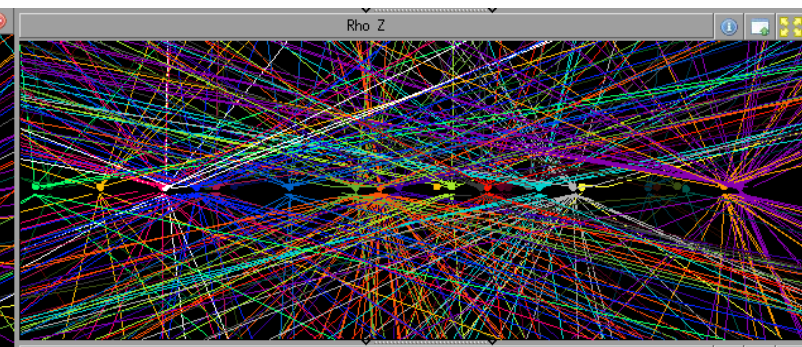
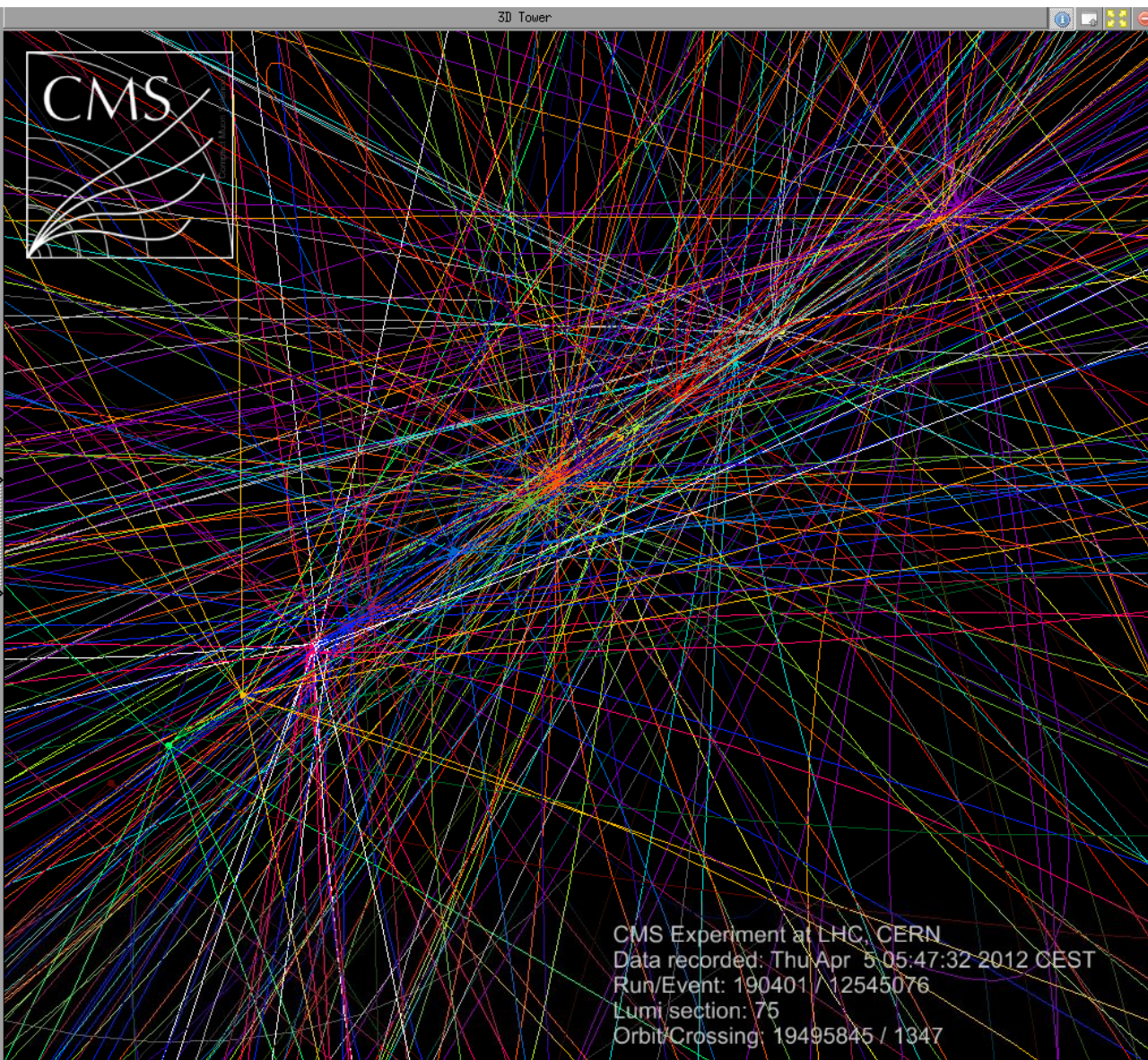


# Tracking



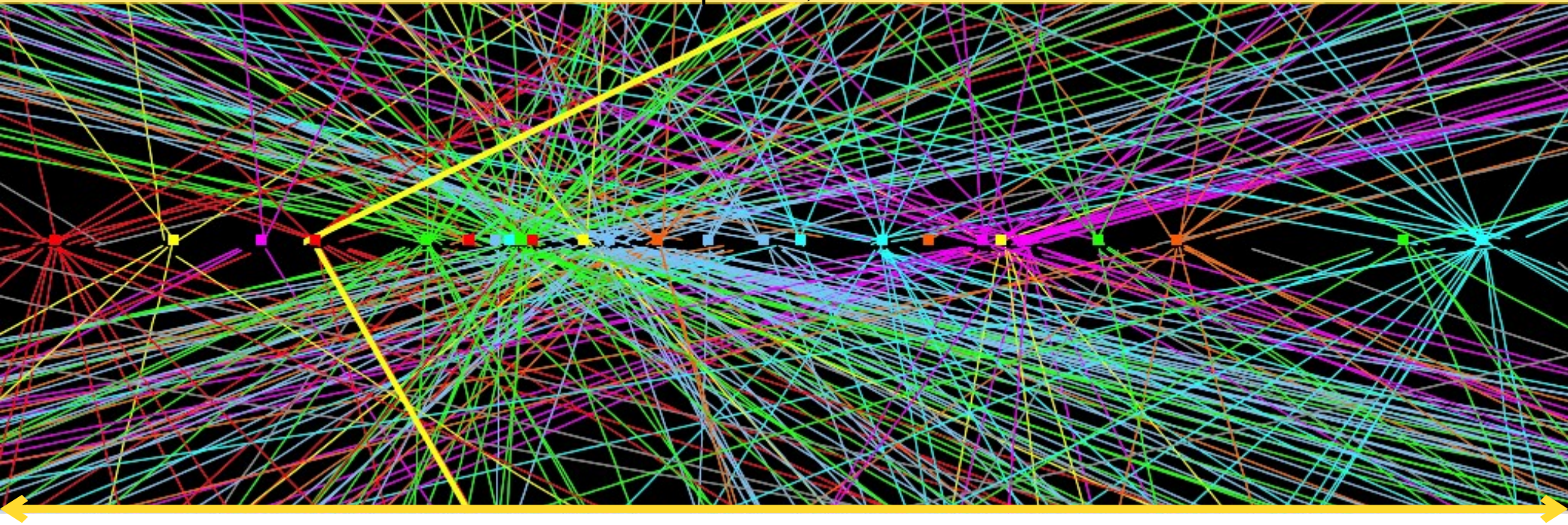
Pattern  
recognition

# Tracking in dense environment



# $Z \rightarrow \mu\mu$ event with 25 reconstructed vertices

April 15<sup>th</sup>, 2012



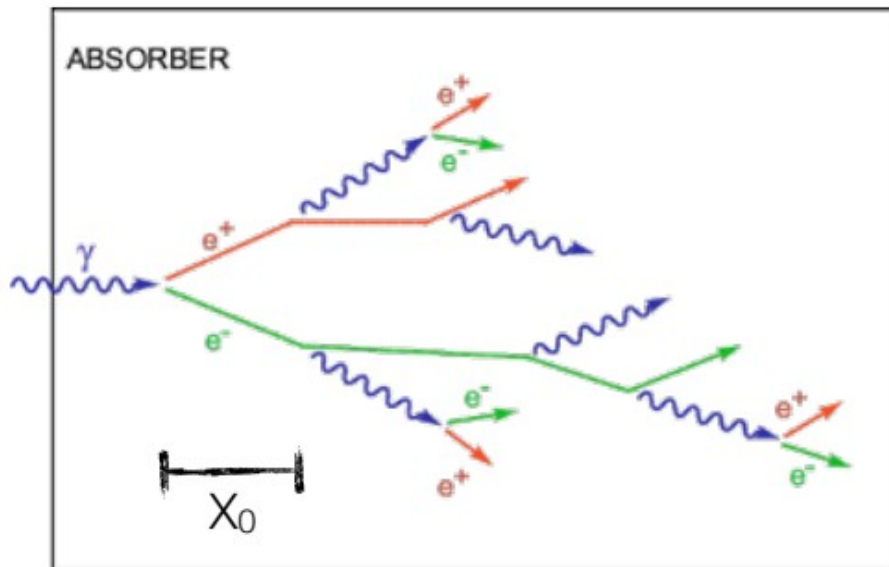
~5 cm

# Calorimeters for showering particles

- Electromagnetic shower

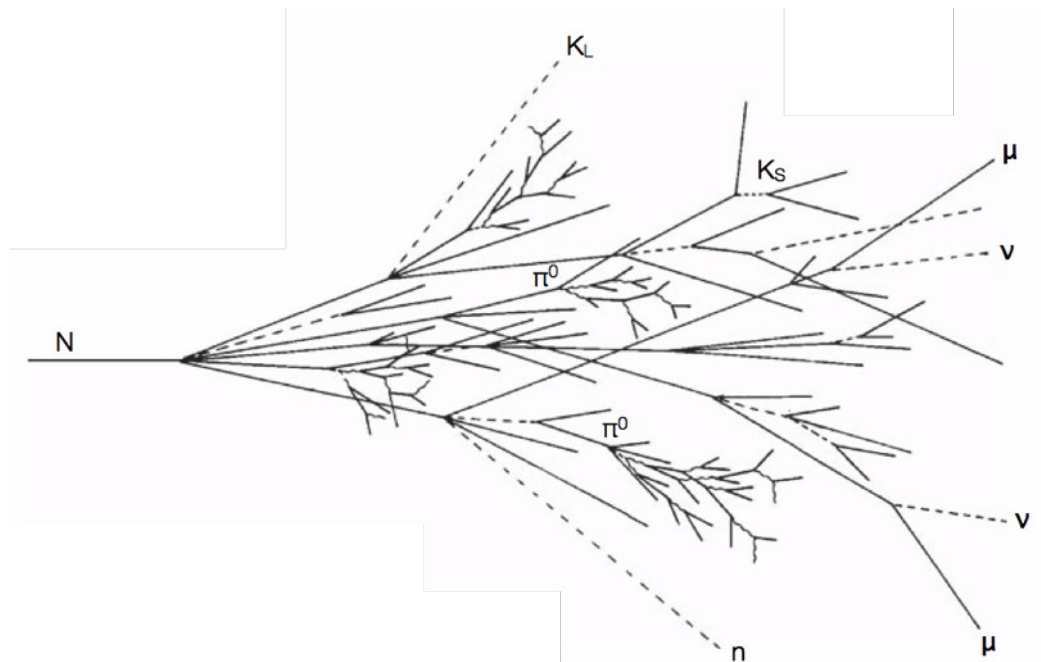
- ✓ Photons: pair production
  - stops below  $e^+e^-$  threshold
- ✓ Electrons: bremsstrahlung
  - Dominates, till brem cross section become smaller than ionization

$$\left. \frac{dE}{dx}(E_c) \right|_{\text{Brems}} = \left. \frac{dE}{dx}(E_c) \right|_{\text{Ion}}$$

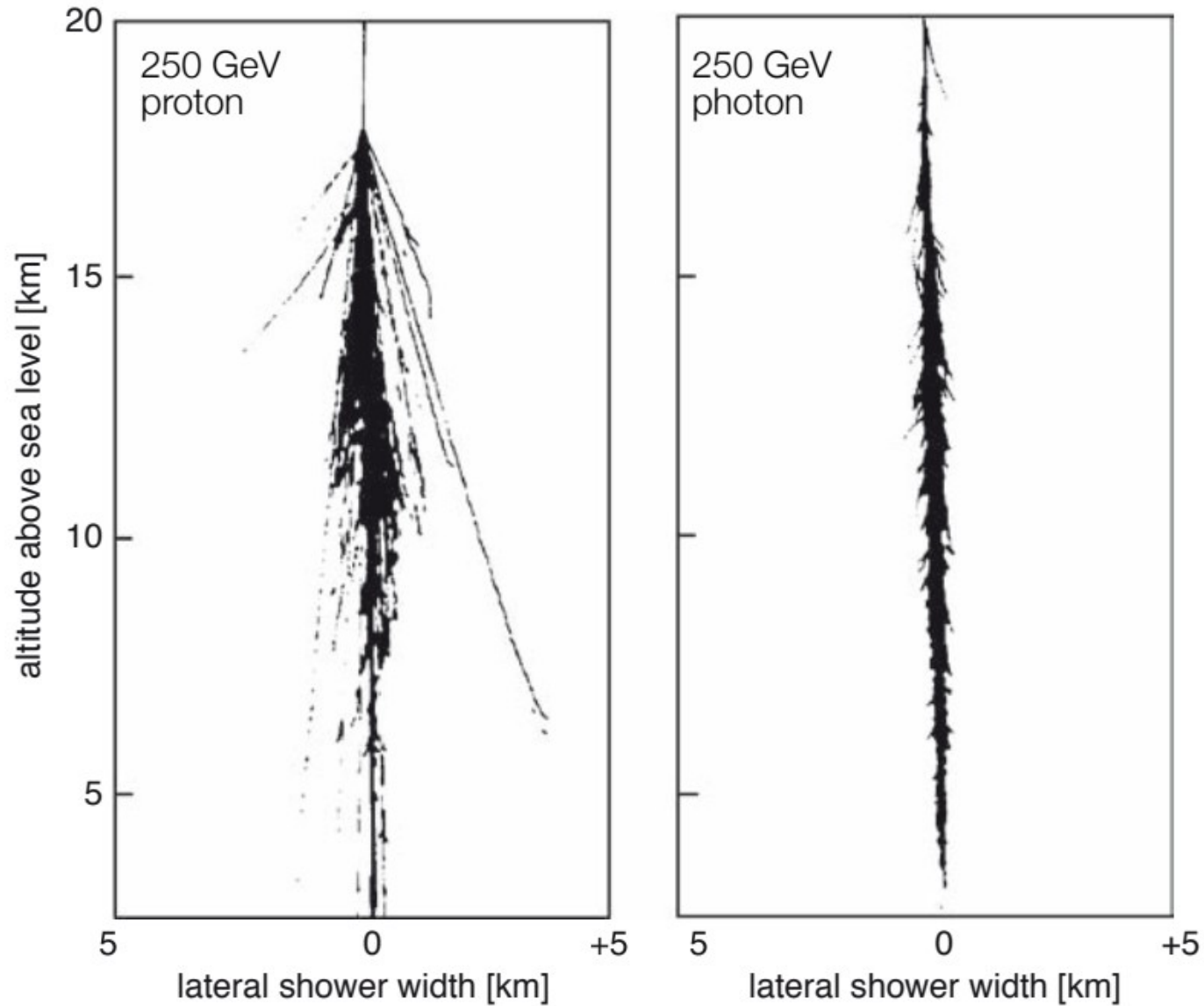


- Hadronic showers

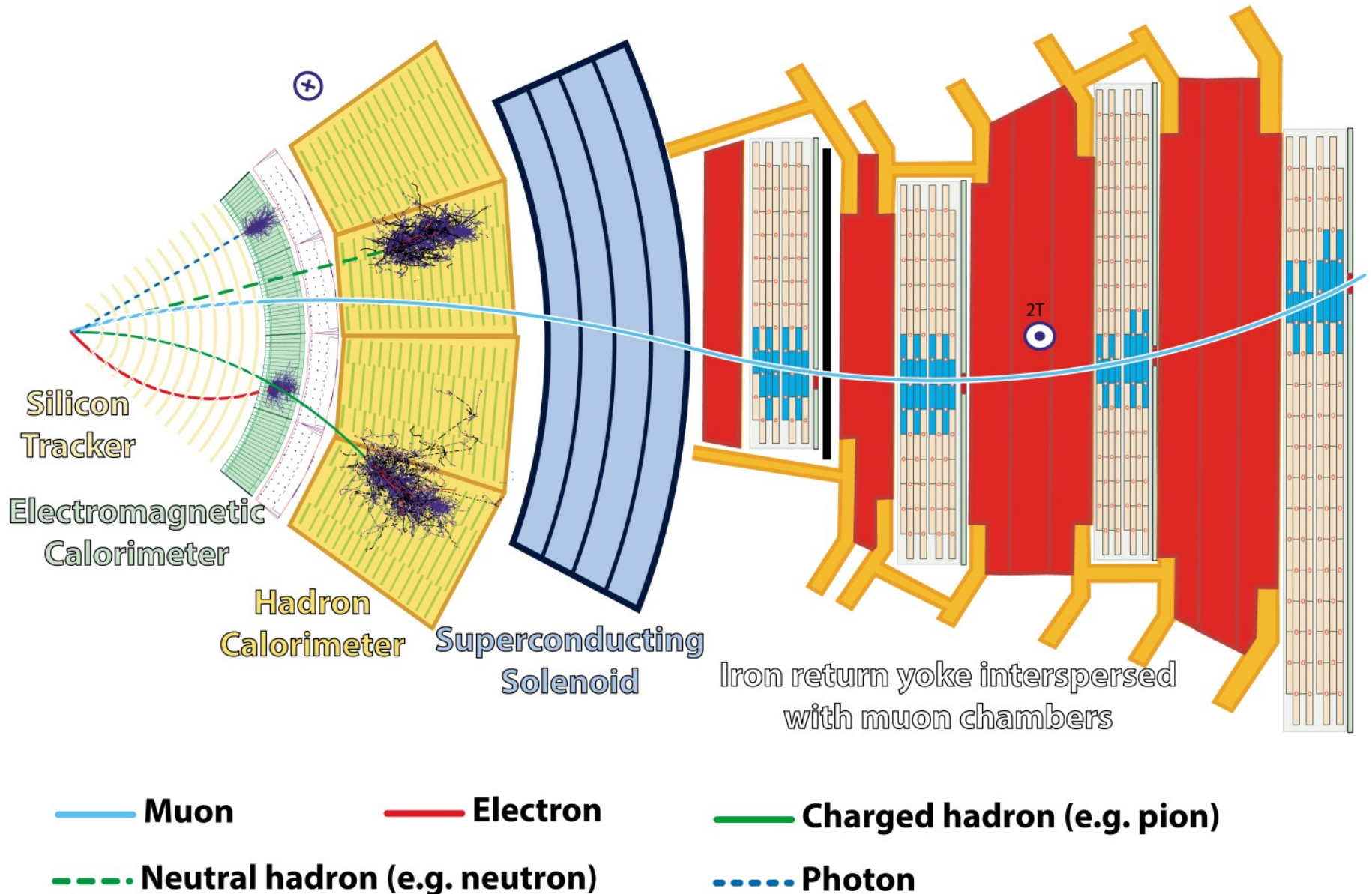
- ✓ Inelastic scattering w/ nuclei
  - Further inelastic scattering until below pion production threshold
- ✓ Sequential decays
  - $\pi^0 \rightarrow \gamma\gamma$
  - Fission fragment:  $\beta$ -decay,  $\gamma$ -decay
  - Neutron capture, spallation, ...



# Hadronic vs. EM showers

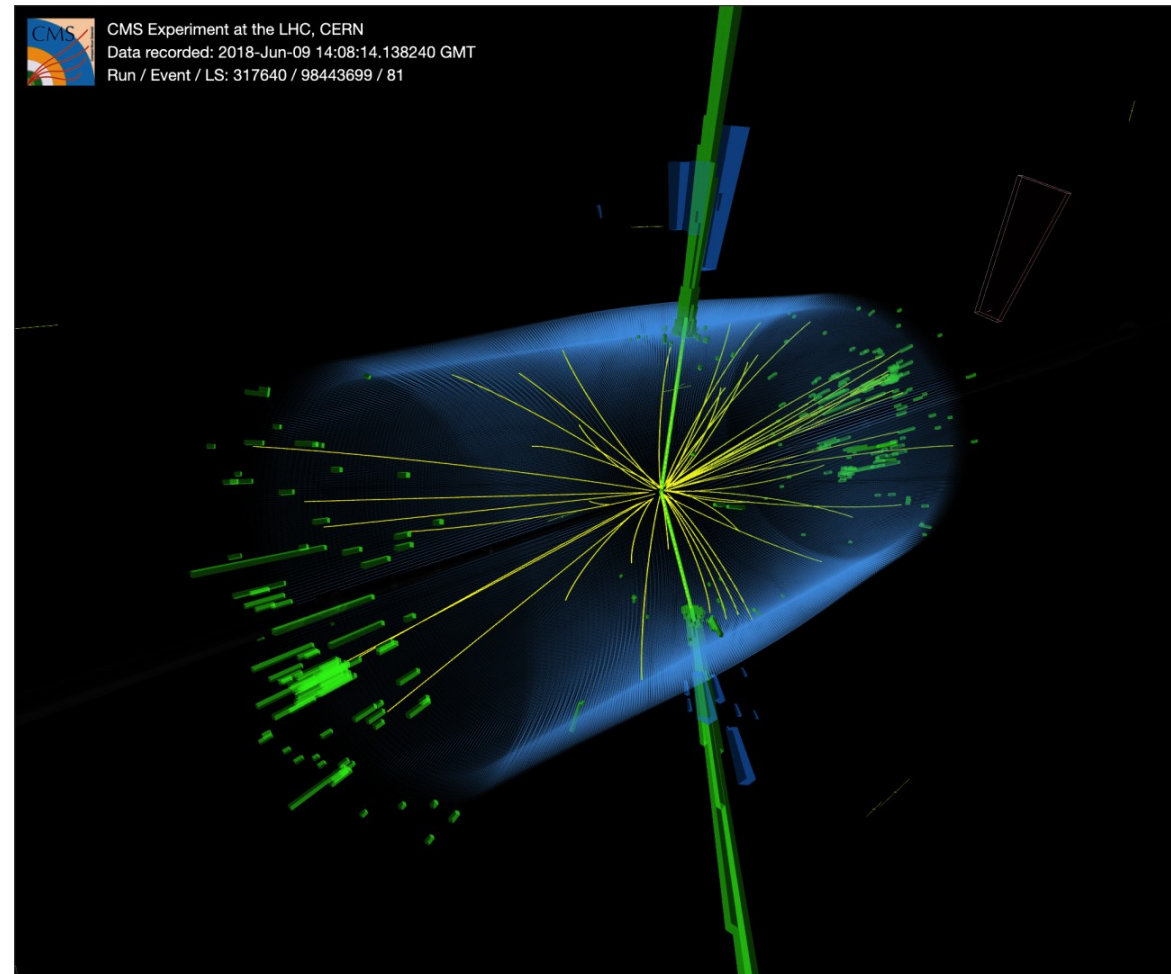
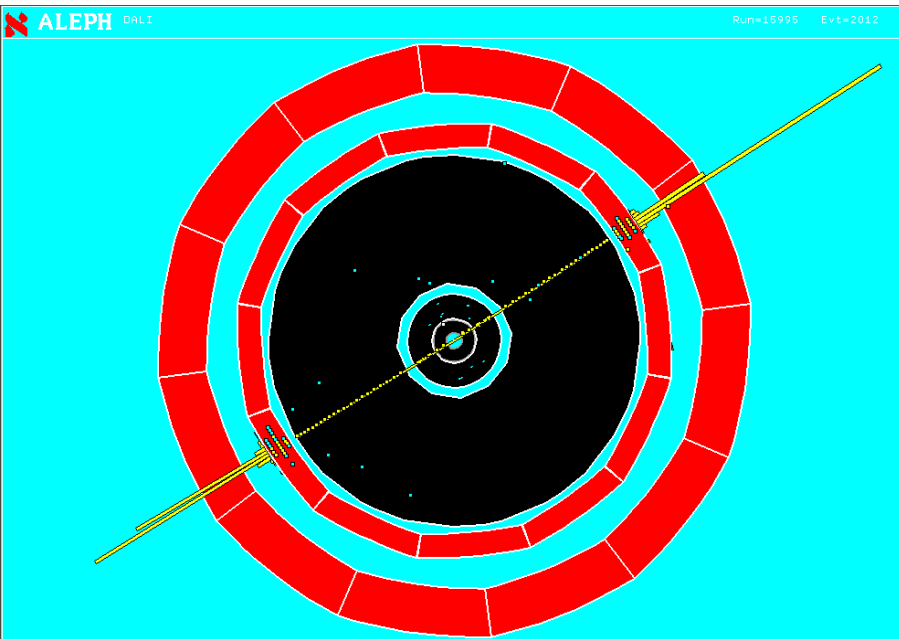


# Particle identification with CMS@LHC





# A $Z \rightarrow e^+e^-$ event at LEP and ad LHC



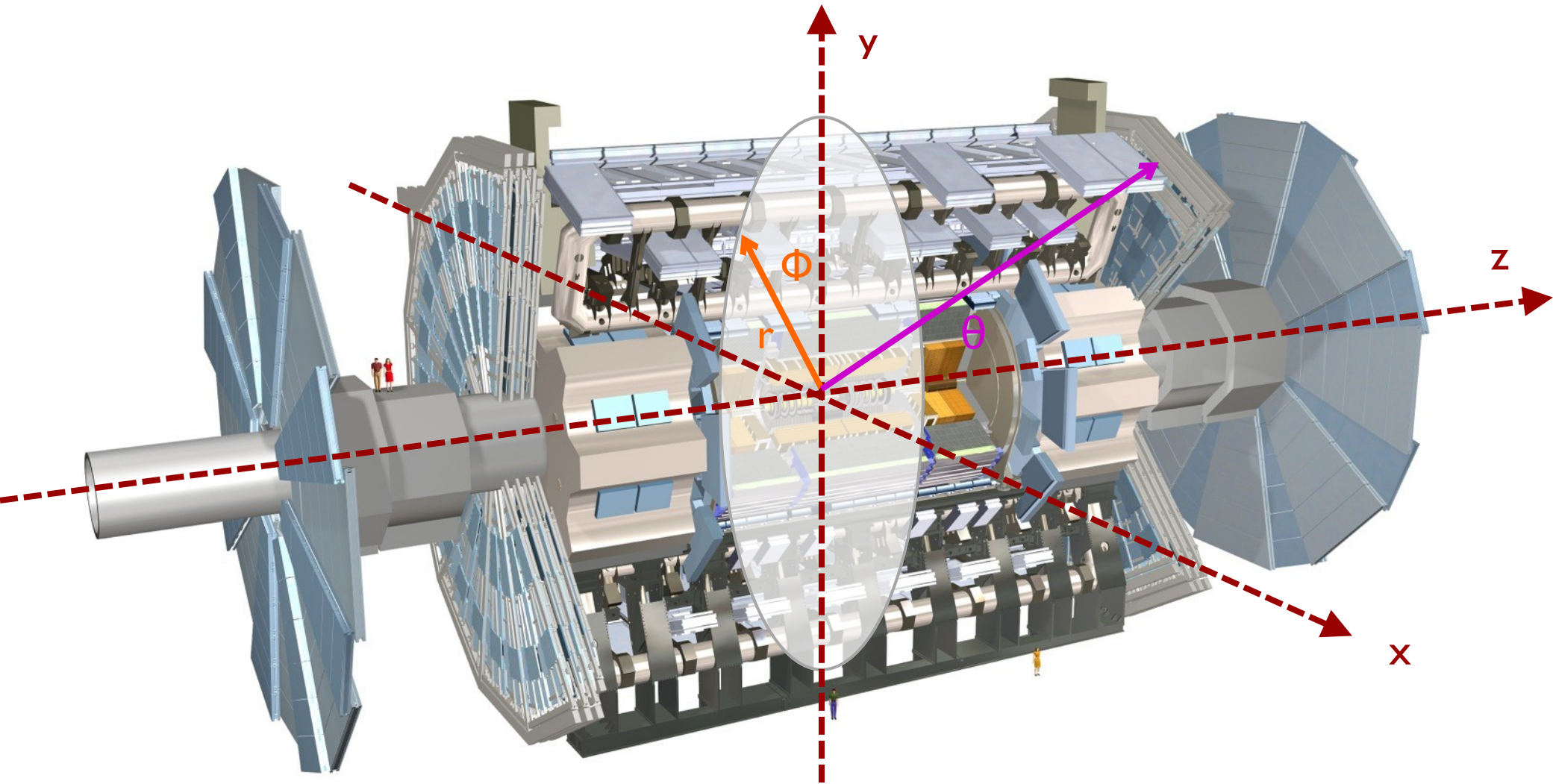
ALEPH @ LEP

CMS @ LHC

# Additional information

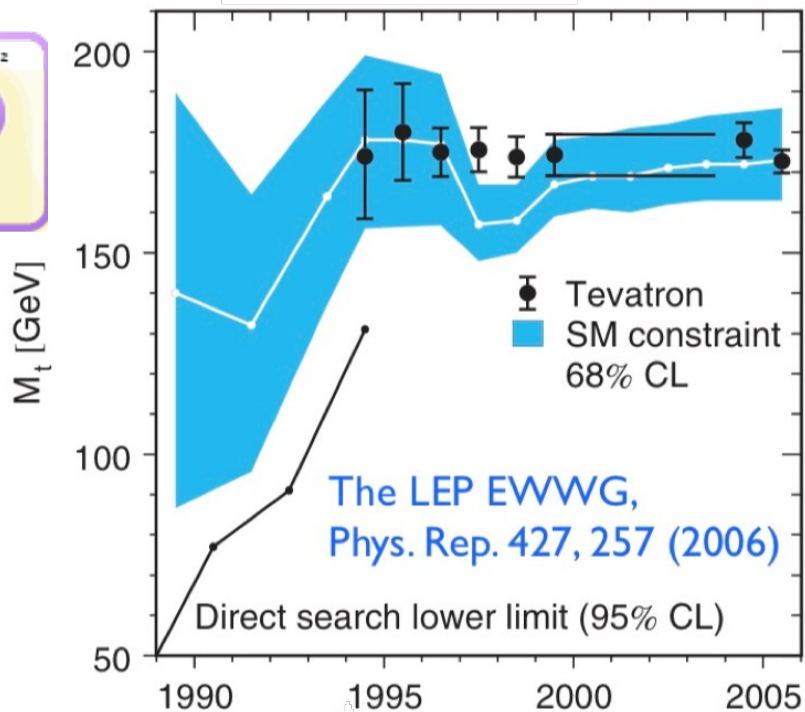
(I find you lack of faith disturbing)

# Collider experiment coordinates



# Before the LHC startup

$\approx 173.1 \text{ GeV}/c^2$   
 $\frac{2}{3}$   
 $\frac{1}{3}$   
**t**  
**top**



$m_W$  measurement at SppS and LEP-I precision measurements

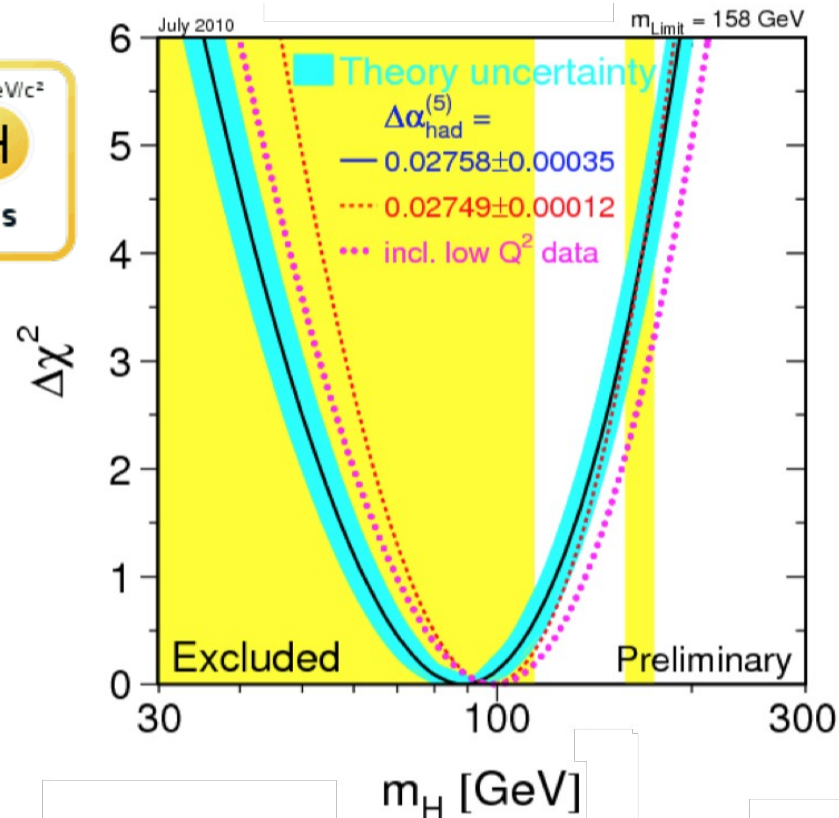
top quark discovery (1994)

$m_W$  measurement at LEP-2

electroweak fit and indirect limit on  $m_H$

Direct limits on Higgs production from LEP-2 and Tevatron

$\approx 125.09 \text{ GeV}/c^2$   
 0  
 0  
**H**  
**higgs**



*LHC “no lose theorem”*

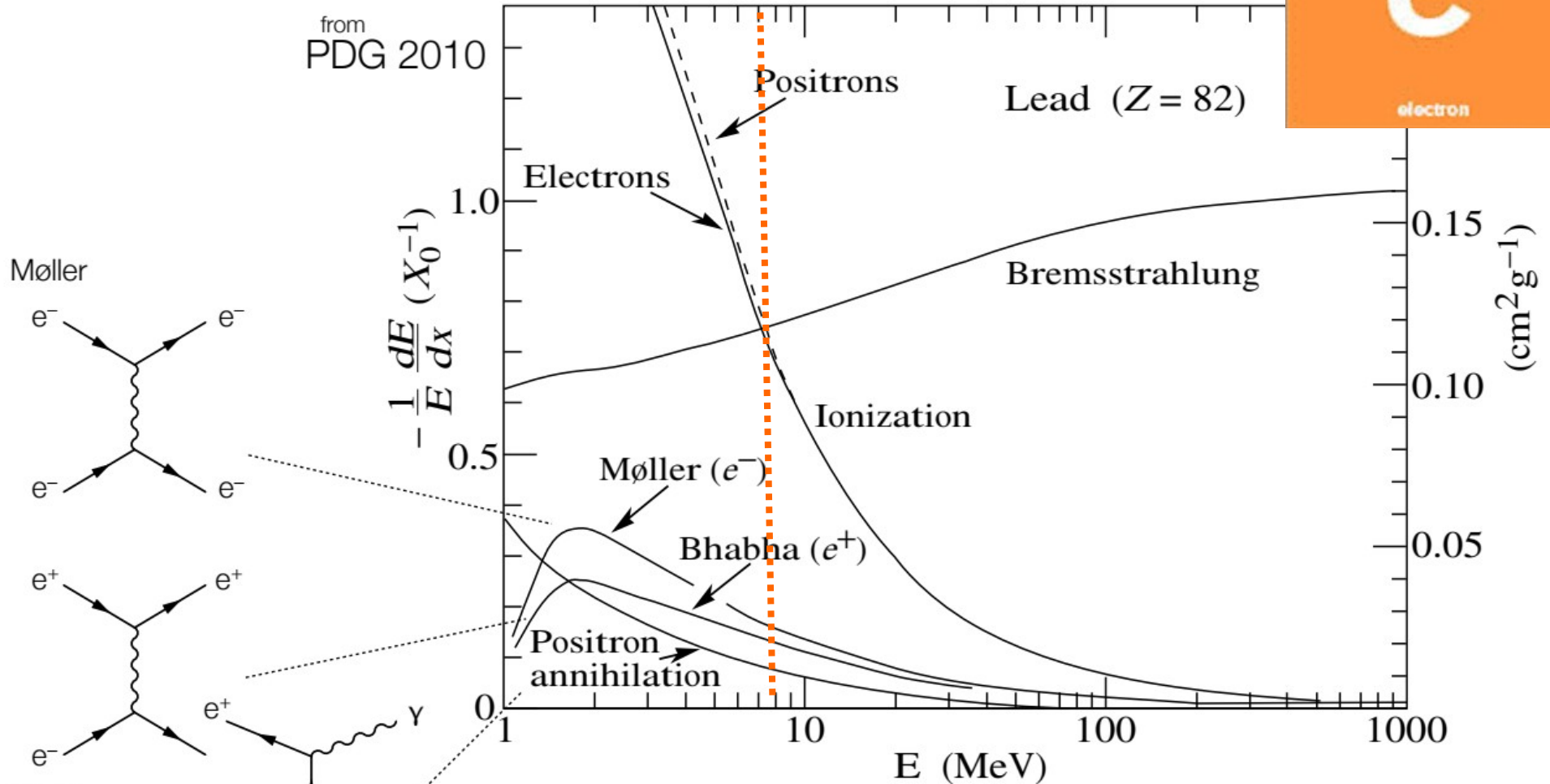
*Either the Higgs boson is discovered,  
 or New Physics should manifest to avoid unitarity violation in WW scattering at TeV scale*

# Electron energy loss

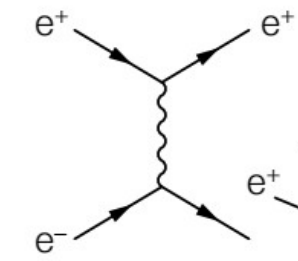
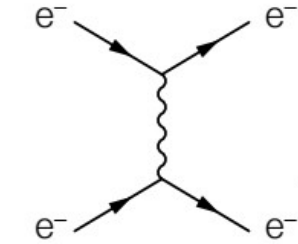


electron

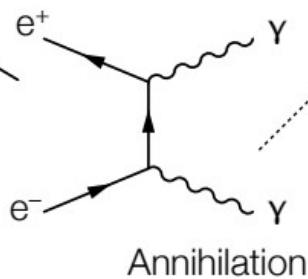
from PDG 2010



Møller

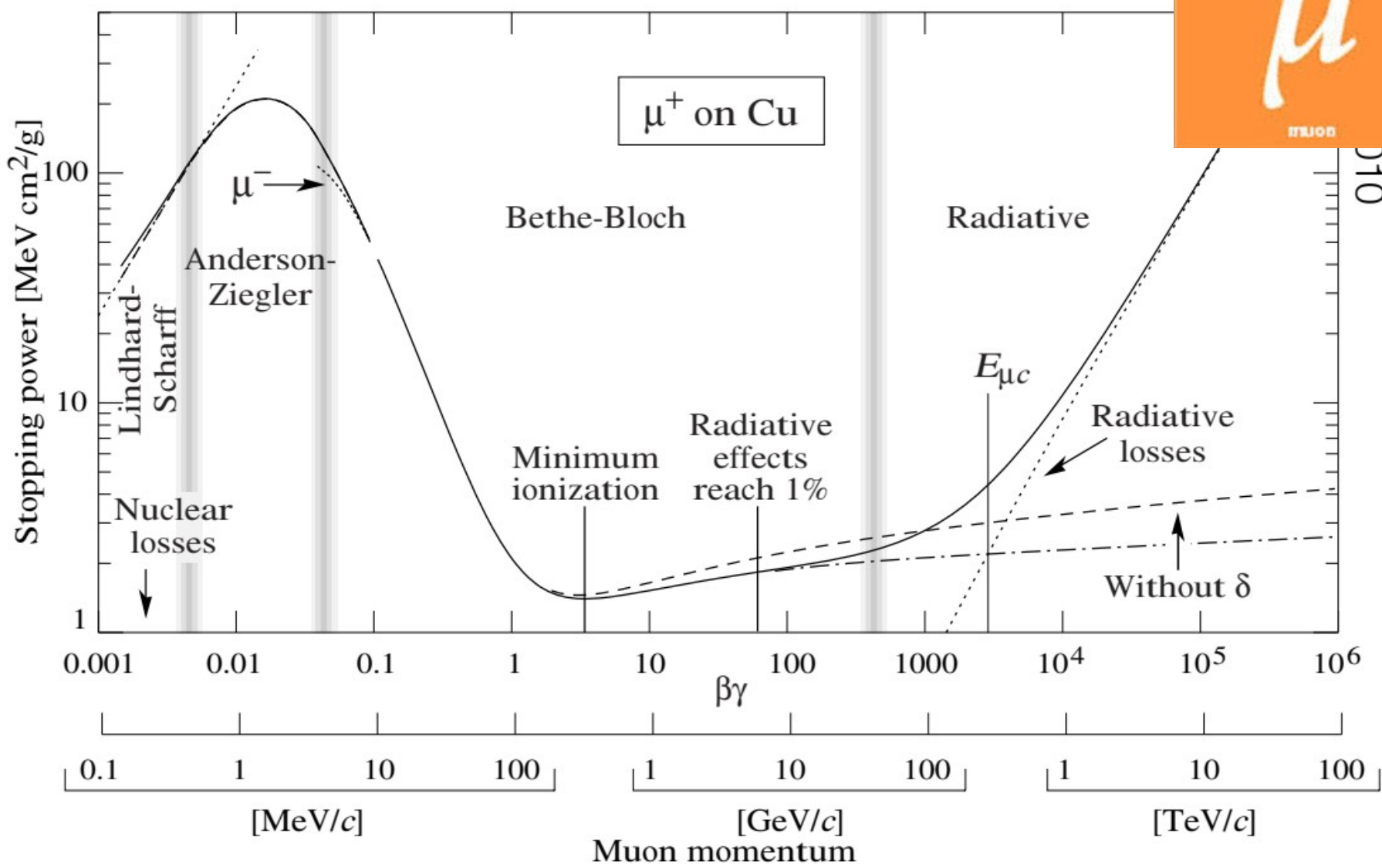
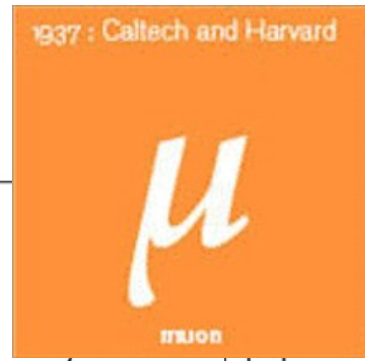


Bhabha



Fractional energy loss per radiation length in lead as a function of electron or positron energy

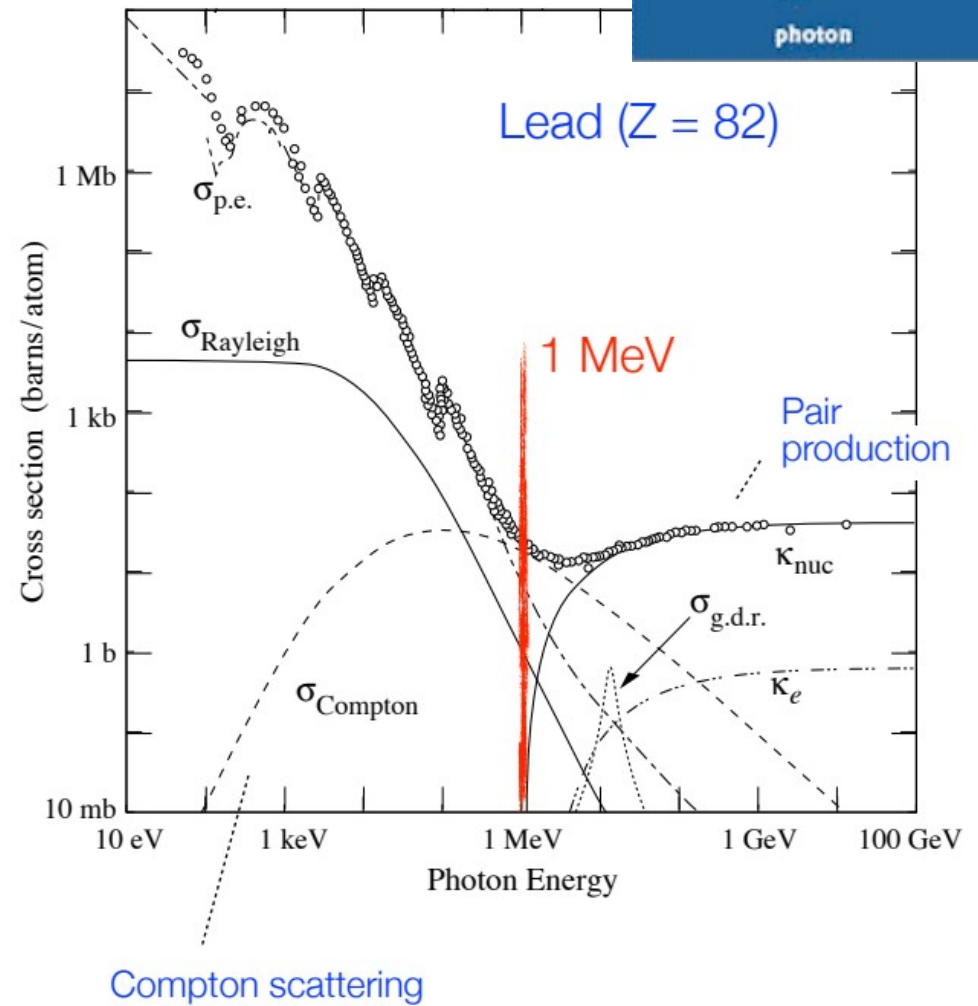
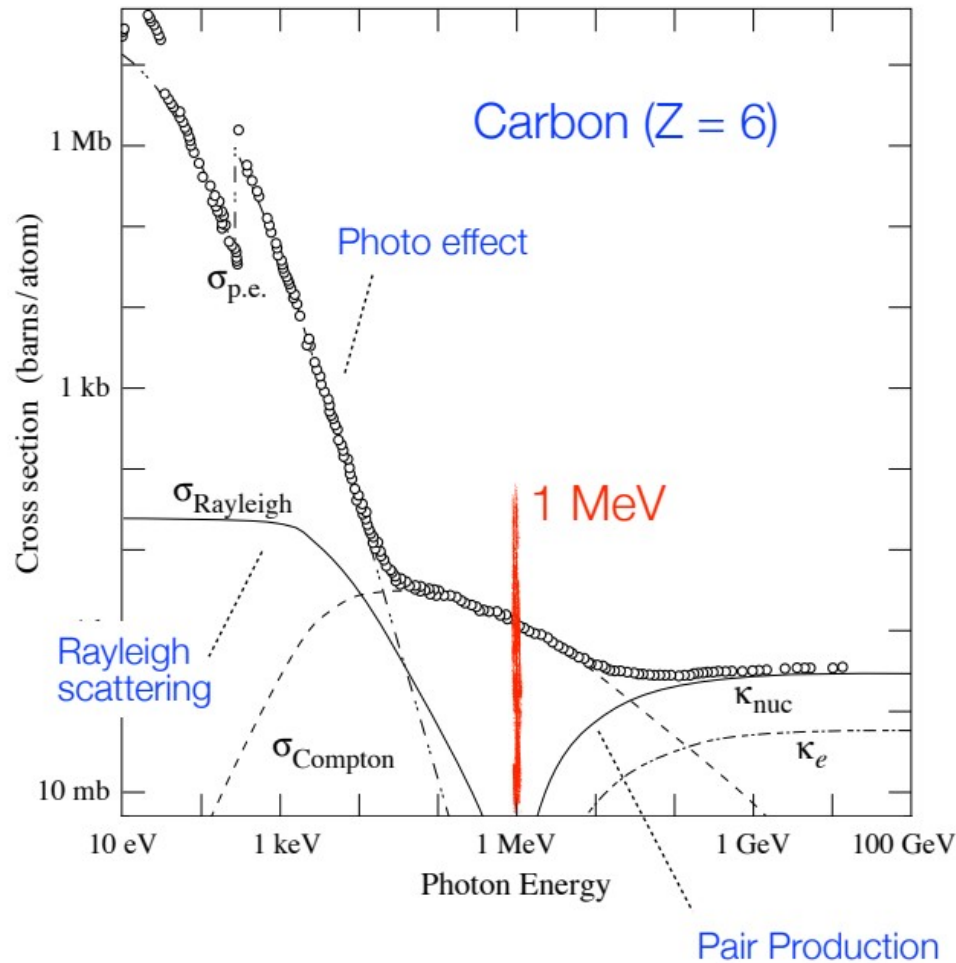
# Muon energy loss



# Interaction of photons with matter



photon



# HEP, SI and “natural” units

Quantity	HEP units	SI units
length	1 fm	$10^{-15}$ m
charge	e	$1.602 \cdot 10^{-19}$ C
energy	1 GeV	$1.602 \times 10^{-10}$ J
mass	1 GeV/c <sup>2</sup>	$1.78 \times 10^{-27}$ kg
$\hbar = h/2\pi$	$6.588 \times 10^{-25}$ GeV s	$1.055 \times 10^{-34}$ Js
c	$2.988 \times 10^{23}$ fm/s	$2.988 \times 10^8$ m/s
$\hbar c$	197 MeV fm	...

## “natural” units ( $\hbar = c = 1$ )

mass	1 GeV
length	1 GeV <sup>-1</sup> = 0.1973 fm
time	1 GeV <sup>-1</sup> = $6.59 \times 10^{-25}$ s



# Relativistic kinematics in a nutshell

$$E^2 = \vec{p}^2 + m^2$$

$$l = \frac{l_0}{\gamma}$$

$$E = m\gamma$$

$$t = t_0\gamma$$

$$\vec{p} = m\gamma\vec{\beta}$$

$$\vec{\beta} = \frac{\vec{p}}{E}$$

# Cross section: magnitude and units

Standard

cross section unit:

$$[\sigma] = \text{mb}$$

with  $1 \text{ mb} = 10^{-27} \text{ cm}^2$

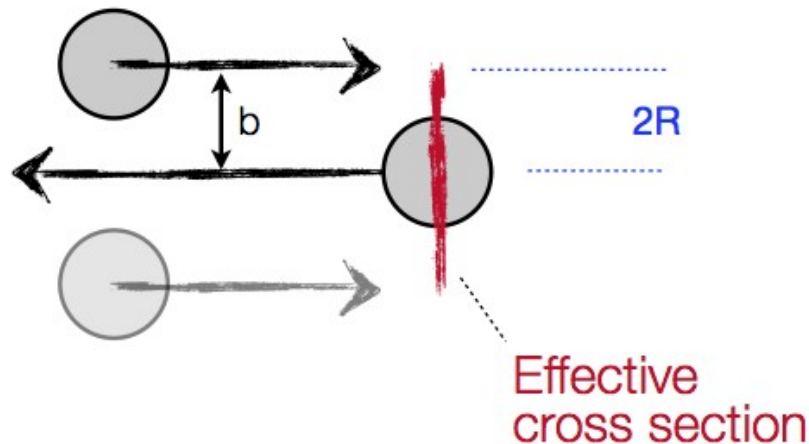
or in

natural units:

$$[\sigma] = \text{GeV}^{-2}$$

with  $1 \text{ GeV}^{-2} = 0.389 \text{ mb}$   
 $1 \text{ mb} = 2.57 \text{ GeV}^{-2}$

Estimating the  
proton-proton cross section:



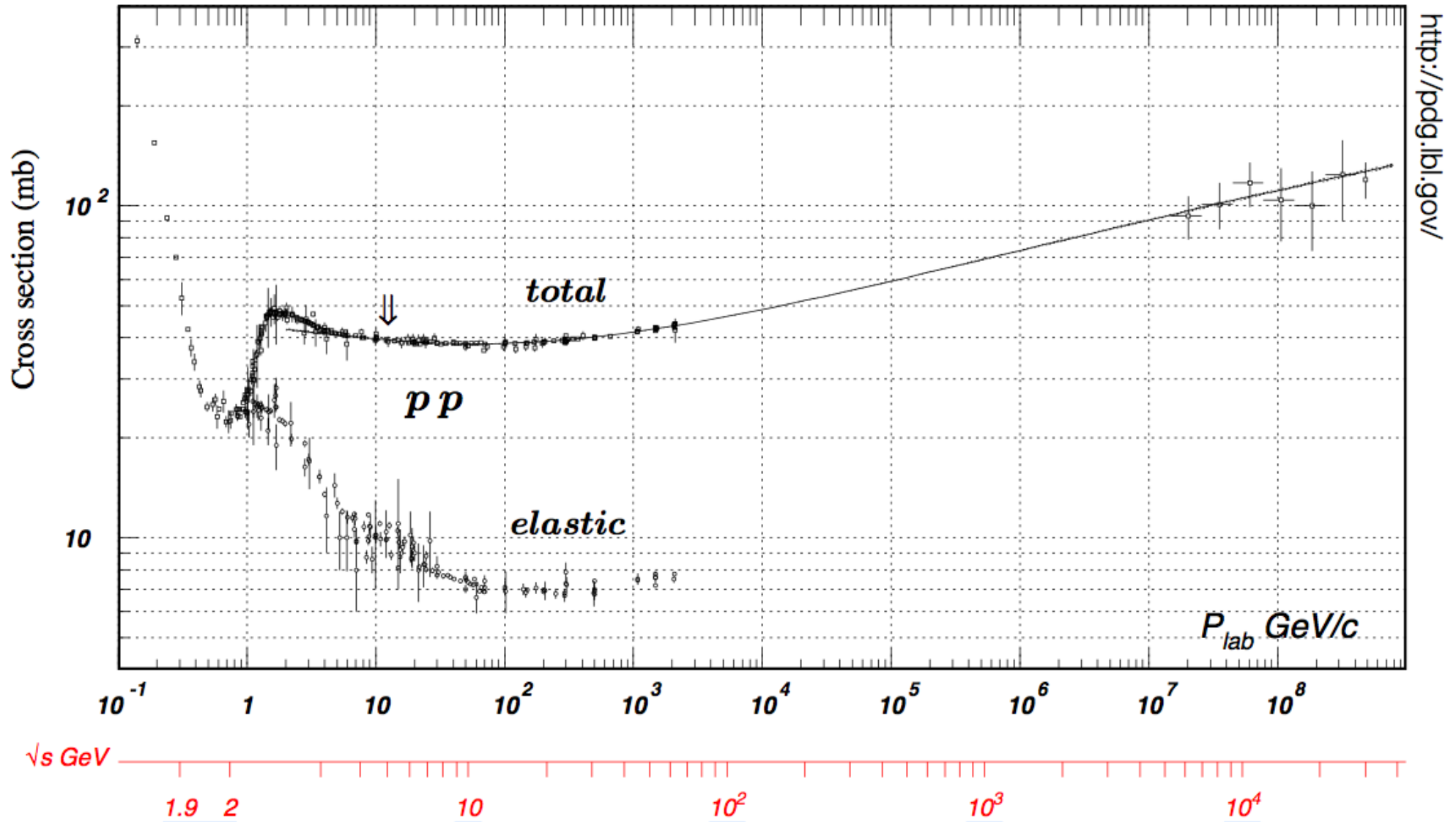
---

using:  $\hbar c = 0.1973 \text{ GeV fm}$   
 $(\hbar c)^2 = 0.389 \text{ GeV}^2 \text{ mb}$

Proton radius:  $R = 0.8 \text{ fm}$   
Strong interactions happens up to  $b = 2R$

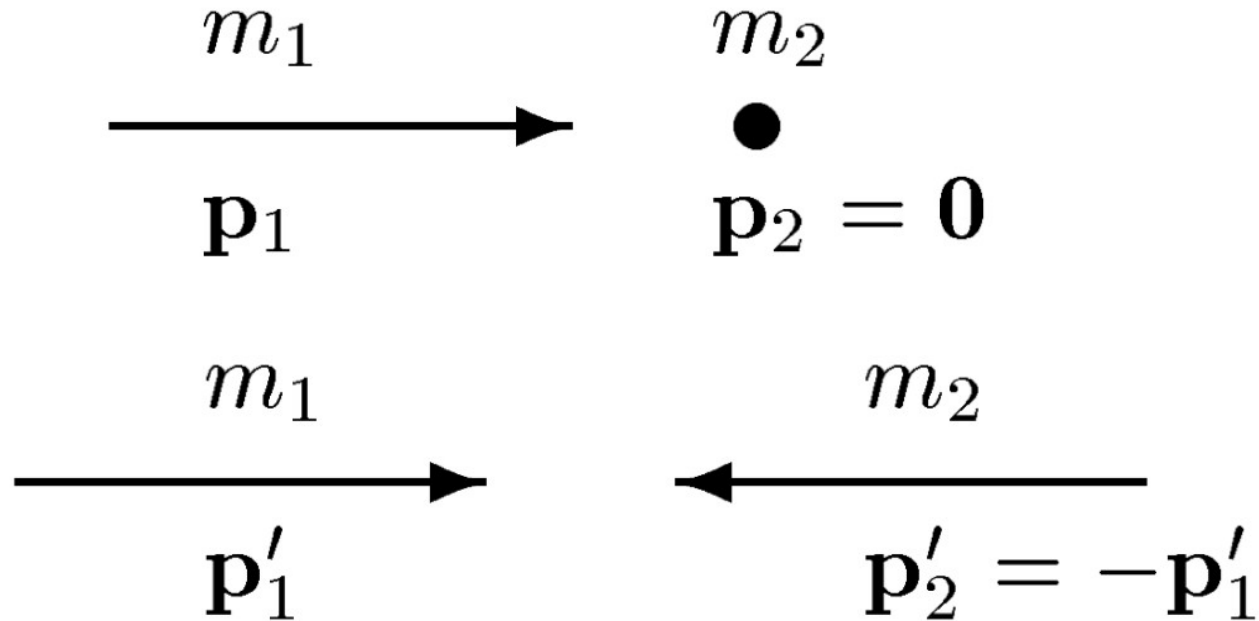
$$\begin{aligned}\sigma &= \pi (2R)^2 = \pi \cdot 1.6^2 \text{ fm}^2 \\ &= \pi \cdot 1.6^2 \cdot 10^{-26} \text{ cm}^2 \\ &= \pi \cdot 1.6^2 \cdot 10 \text{ mb} \\ &= 80 \text{ mb}\end{aligned}$$

# Proton-proton scattering cross-section



<http://pdg.lbl.gov/>

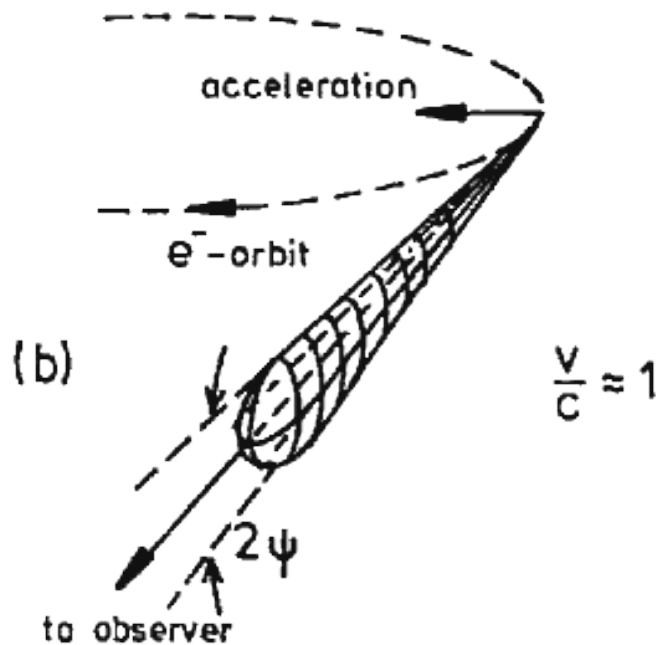
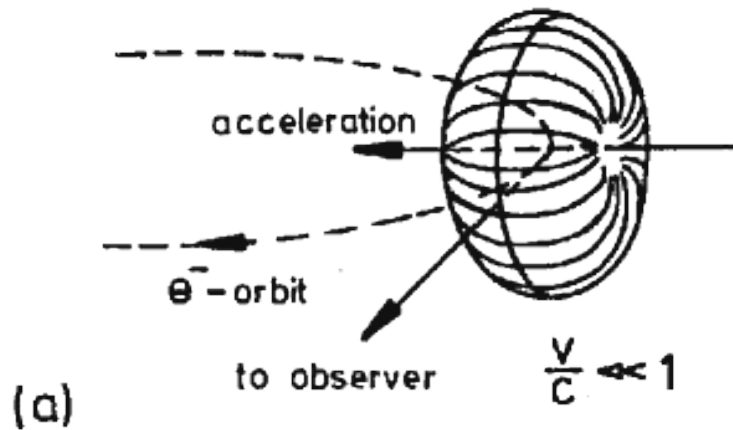
# Fixed target vs. collider



How much energy should a fixed target experiment have to equal the center of mass energy of two colliding beam?

$$E_{\text{fix}} = 2 \frac{E_{\text{col}}^2}{m} - m$$

# Synchrotron radiation



energy lost per revolution

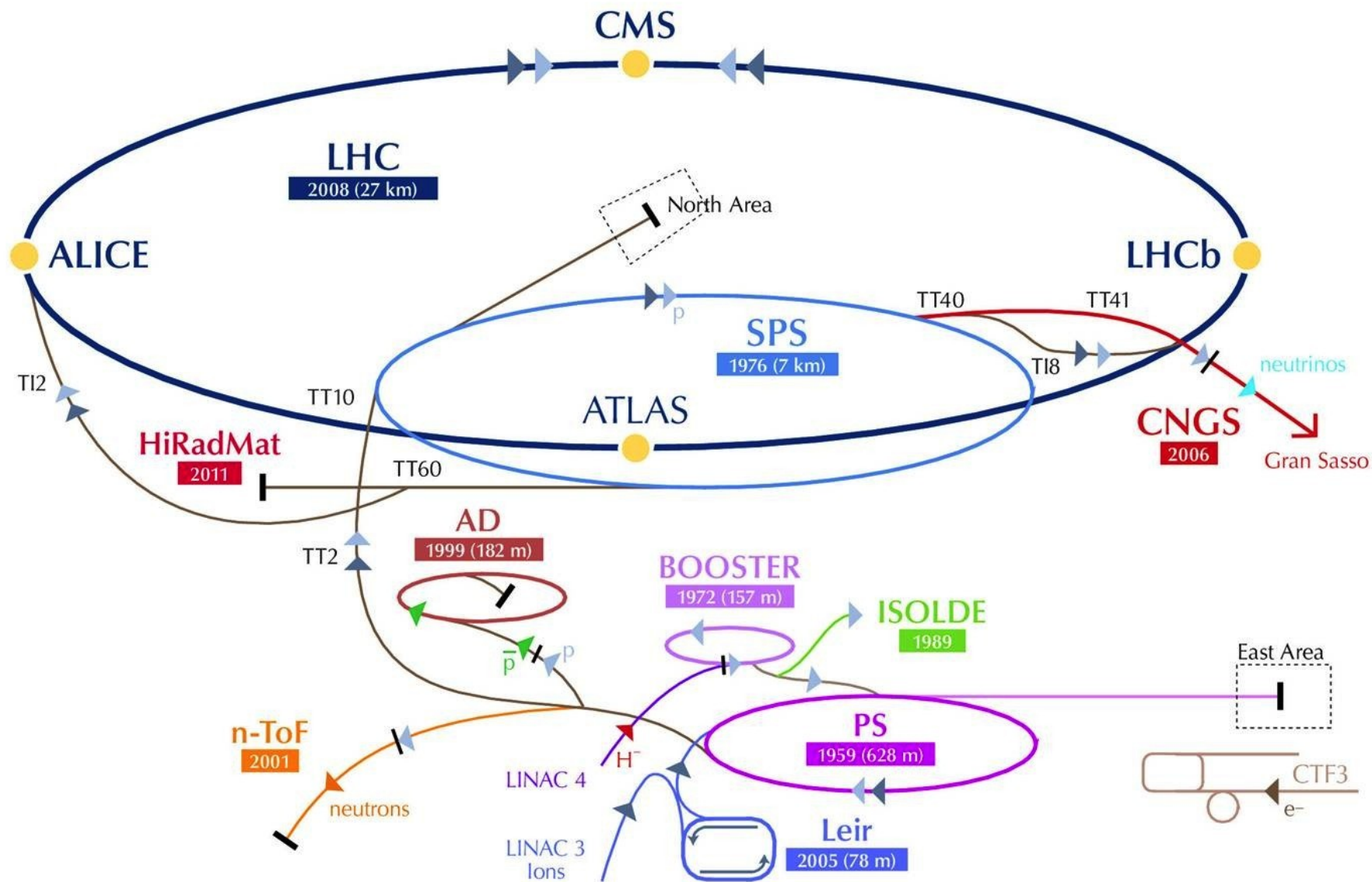
$$\Delta E = \frac{4\pi}{3} \frac{1}{4\pi\epsilon_0} \left( \frac{e^3 \beta^3 \gamma^4}{R} \right)$$

electrons vs. protons

$$\frac{\Delta E_e}{\Delta E_p} \simeq \left( \frac{m_p}{m_e} \right)^4$$

It's easier to accelerate protons to higher energies, but protons are fundamentals...

# CERN accelerator complex



# Magnetic spectrometer

Charged particle in  
magnetic field

$$\frac{d\vec{p}}{dt} = q\vec{\beta} \times \vec{B}$$

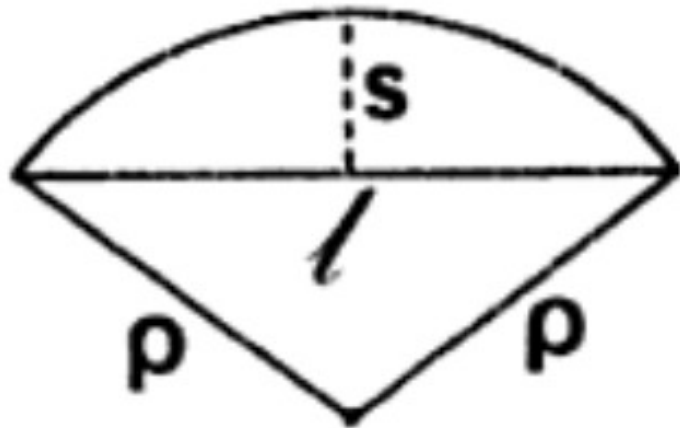
If the field is constant and we neglect presence of matter, **momentum magnitude is constant** with time, **trajectory is helical**

$$p[\text{GeV}] = 0.3B[\text{T}]\rho[\text{m}]$$

Actual trajectory differ from exact helix because of:

- **magnetic field inhomogeneity**
- **particle energy loss** (ionization, multiple scattering)

# Momentum measurement



$s$  = sagitta

$l$  = chord

$\rho$  = radius

$$\rho \simeq \frac{l^2}{8s} \quad p = 0.3 \frac{Bl^2}{8s}$$

$$\left| \frac{\delta p}{p} \right| = \left| \frac{\delta s}{s} \right|$$

*smaller for larger number of points*

*measurement error (RMS)*

Momentum resolution due to measurement error

$$\left| \frac{\delta p}{p} \right| = A_N \underbrace{\frac{\epsilon}{L^2}}_{\text{projected track length in magnetic field}} \frac{p}{0.3B}$$

*Momentum resolution gets worse for larger momenta*

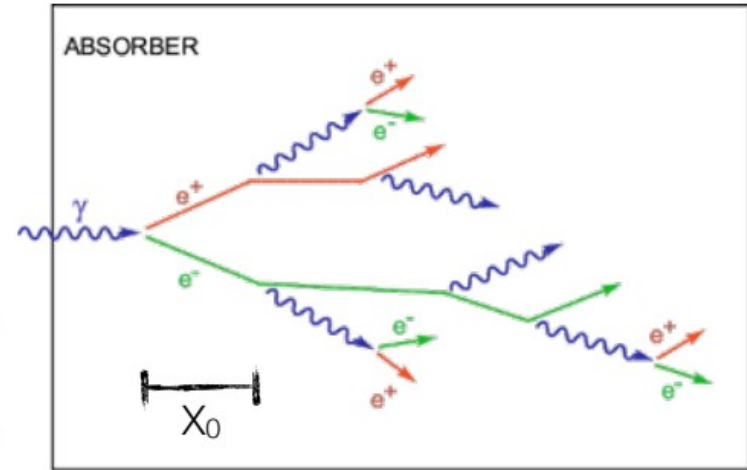
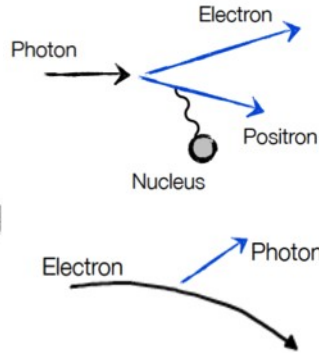
*resolution is improved faster by increasing L than B*



# Electromagnetic showers

Dominant processes  
at high energies ...

Photons : Pair production  
Electrons : Bremsstrahlung



Pair production:

$$\sigma_{\text{pair}} \approx \frac{7}{9} \left( 4 \alpha r_e^2 Z^2 \ln \frac{183}{Z^{1/3}} \right)$$

$$= \frac{7}{9} \frac{A}{N_A X_0} \quad [\text{X}_0: \text{radiation length}]$$

[in cm or g/cm<sup>2</sup>]

Absorption  
coefficient:

$$\mu = n\sigma = \rho \frac{N_A}{A} \cdot \sigma_{\text{pair}} = \frac{7}{9} \frac{\rho}{X_0}$$

Bremsstrahlung:

$$\frac{dE}{dx} = 4\alpha N_A \frac{Z^2}{A} r_e^2 \cdot E \ln \frac{183}{Z^{1/3}} = \frac{E}{X_0}$$

$$\rightarrow E = E_0 e^{-x/X_0}$$

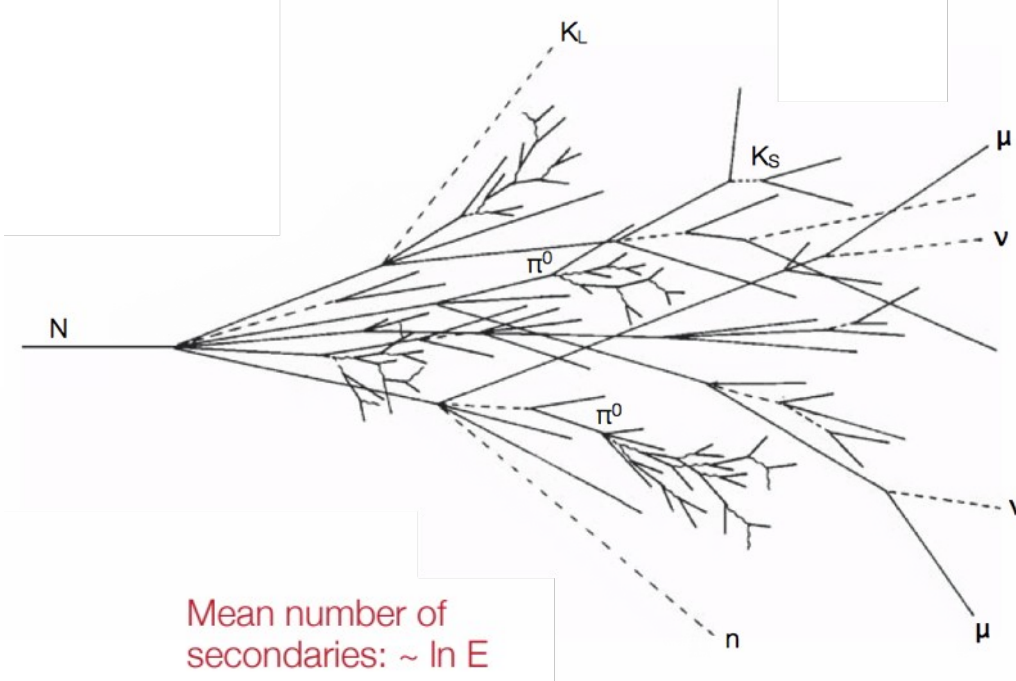
After passage of one  $X_0$  electron  
has only (1/e)<sup>th</sup> of its primary energy ...  
[i.e. 37%]

Critical energy:  $\left. \frac{dE}{dx}(E_c) \right|_{\text{Brems}} = \left. \frac{dE}{dx}(E_c) \right|_{\text{Ion}}$

# Hadronic showers

## Shower development:

1.  $p + \text{Nucleus} \rightarrow \text{Pions} + N^* + \dots$
2. Secondary particles ...  
undergo further inelastic collisions until they fall below pion production threshold
3. Sequential decays ...  
 $\pi_0 \rightarrow \gamma\gamma$ : yields electromagnetic shower  
 Fission fragments  $\rightarrow \beta$ -decay,  $\gamma$ -decay  
 Neutron capture  $\rightarrow$  fission  
 Spallation ...



Mean number of secondaries:  $\sim \ln E$

Typical transverse momentum:  $p_t \sim 350 \text{ MeV}/c$

Substantial electromagnetic fraction

$$f_{em} \sim \ln E$$

[variations significant]

### Cascade energy distribution:

[Example: 5 GeV proton in lead-scintillator calorimeter]

Ionization energy of charged particles ( $p, \pi, \mu$ )	1980 MeV [40%]
Electromagnetic shower ( $\pi^0, \eta^0, e$ )	760 MeV [15%]
Neutrons	520 MeV [10%]
Photons from nuclear de-excitation	310 MeV [6%]
Non-detectable energy (nuclear binding, neutrinos)	1430 MeV [29%]
	<hr/>
	5000 MeV [29%]

# Homogeneous calorimeters

- ★ In a homogeneous calorimeter the whole detector volume is filled by a high-density material which simultaneously serves as absorber as well as as active medium ...

Signal	Material
Scintillation light	BGO, BaF <sub>2</sub> , CeF <sub>3</sub> , ...
Cherenkov light	Lead Glass
Ionization signal	Liquid noble gases (Ar, Kr, Xe)

- ★ Advantage: homogenous calorimeters provide optimal energy resolution
- ★ Disadvantage: very expensive
- ★ Homogenous calorimeters are exclusively used for electromagnetic calorimeter, i.e. energy measurement of electrons and photons

# Sampling calorimeters

Scheme of a sandwich calorimeter

Principle:

Alternating layers of absorber and active material [sandwich calorimeter]

Absorber materials:  
[high density]

Iron (Fe)

Lead (Pb)

Uranium (U)  
[For compensation ...]

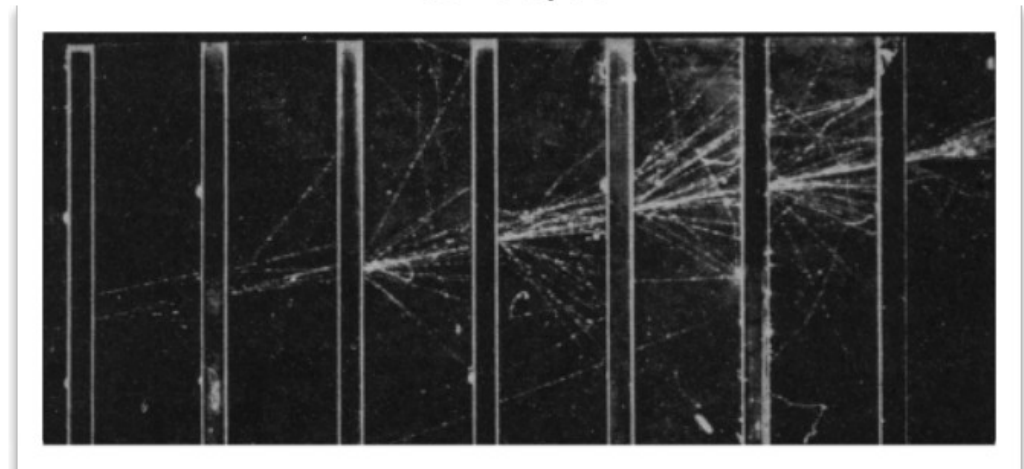
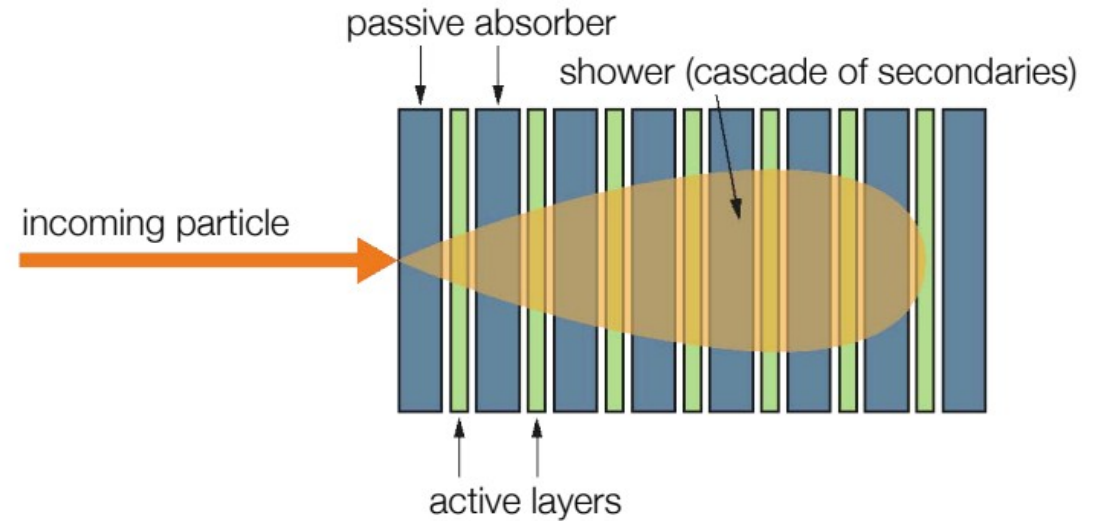
Active materials:

Plastic scintillator

Silicon detectors

Liquid ionization chamber

Gas detectors



Electromagnetic shower

# A typical HEP calorimetry system

Typical Calorimeter: two components ...

Electromagnetic (EM) +  
Hadronic section (Had) ...

Different setups chosen for  
optimal energy resolution ...

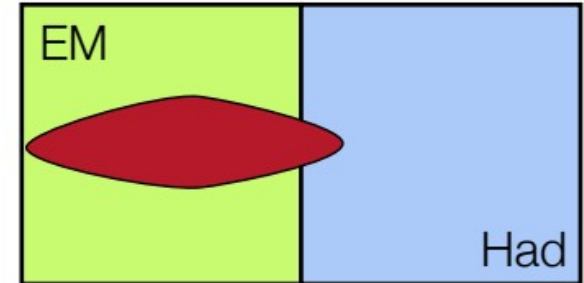
But:

Hadronic energy measured in  
both parts of calorimeter ...

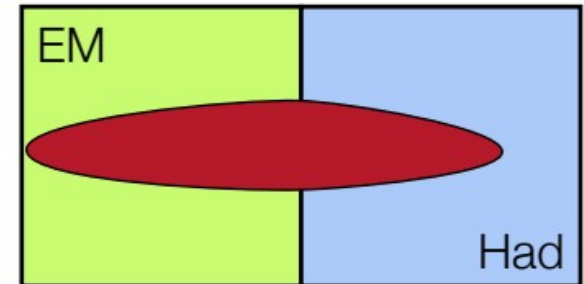
Needs careful consideration of  
different response ...

Schematic of a  
typical HEP calorimeter

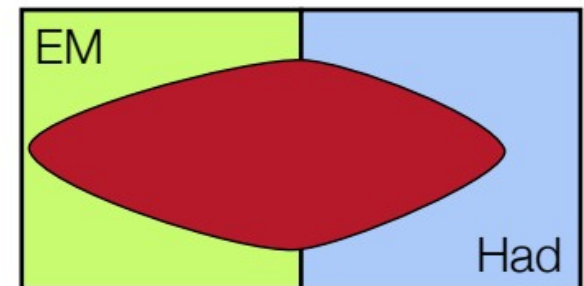
Electrons  
Photons



Taus  
Hadrons



Jets



# Energy resolution in calorimeters

Energy resolution:

e.g. inhomogeneities  
shower leakage

e.g. electronic noise  
sampling fraction variations

$$\frac{\sigma_E}{E} = \frac{A}{\sqrt{E}} \oplus B \oplus \frac{C}{E}$$

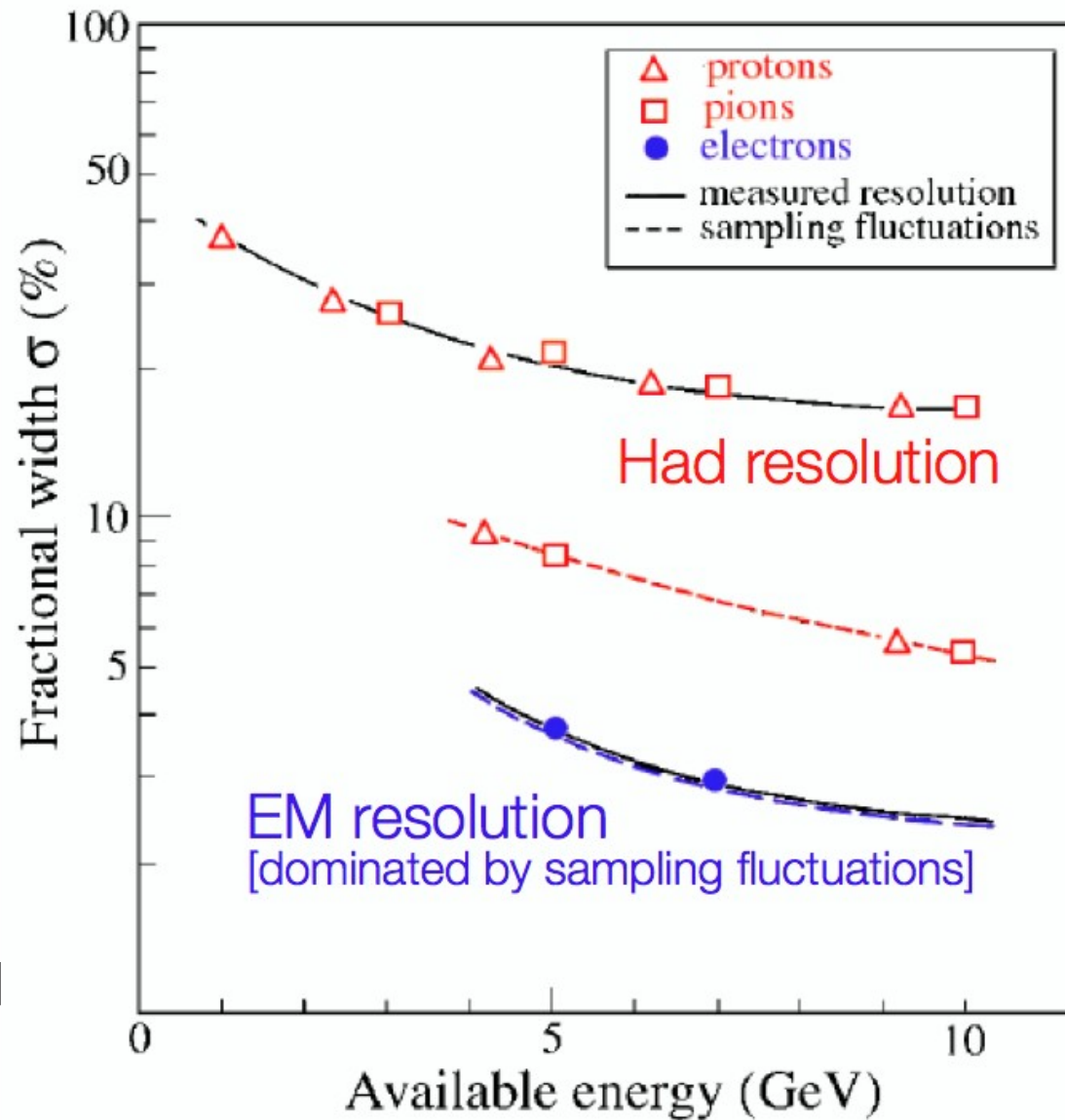
Fluctuations:

- Sampling fluctuations
- Leakage fluctuations
- Fluctuations of electromagnetic fraction
- Nuclear excitations, fission, binding energy fluctuations ...
- Heavily ionizing particles

Typical:

- A: 0.5 – 1.0 [Record:0.35]
- B: 0.03 – 0.05
- C: few %

# Resolution: EM vs. HAD



Sampling fluctuations only minor contribution to hadronic energy resolution

[AFM Collaboration]