



The Ohio State University



# Investigating the nature of the $K_0^*(700)$ state with $\pi^\pm K_S^0$ correlations with ALICE at the LHC

## ALICE Collaboration

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### Outline of talk

- Introduction
- Previous ALICE study of  $a_0(980)$
- **New** results from ALICE study of  $K_0^*(700)$
- Summary

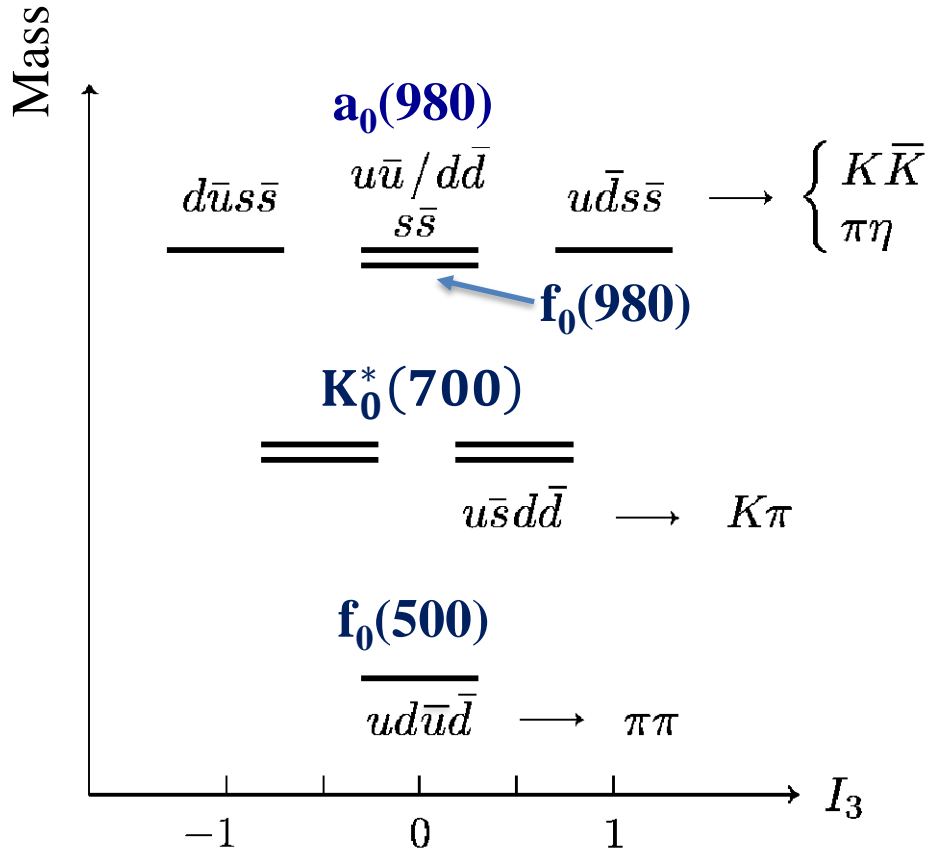
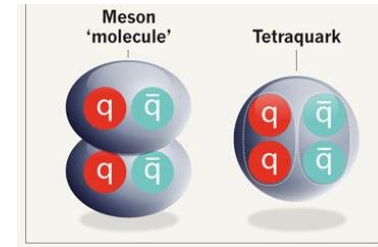
WPCF 2024

welcomes you in Toulouse  
France

# Predicted low-lying tetraquark nonet with candidate mesons

## Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



Low-lying tetraquark states have been predicted for  $> 40$  years.

Candidate mesons with the expected masses, isospins and decay channels have been found:

e.g.  $a_0(980)$ ,  $f_0(980)$ ,  $K_0^*(700)$ ,  $f_0(500)$ ..

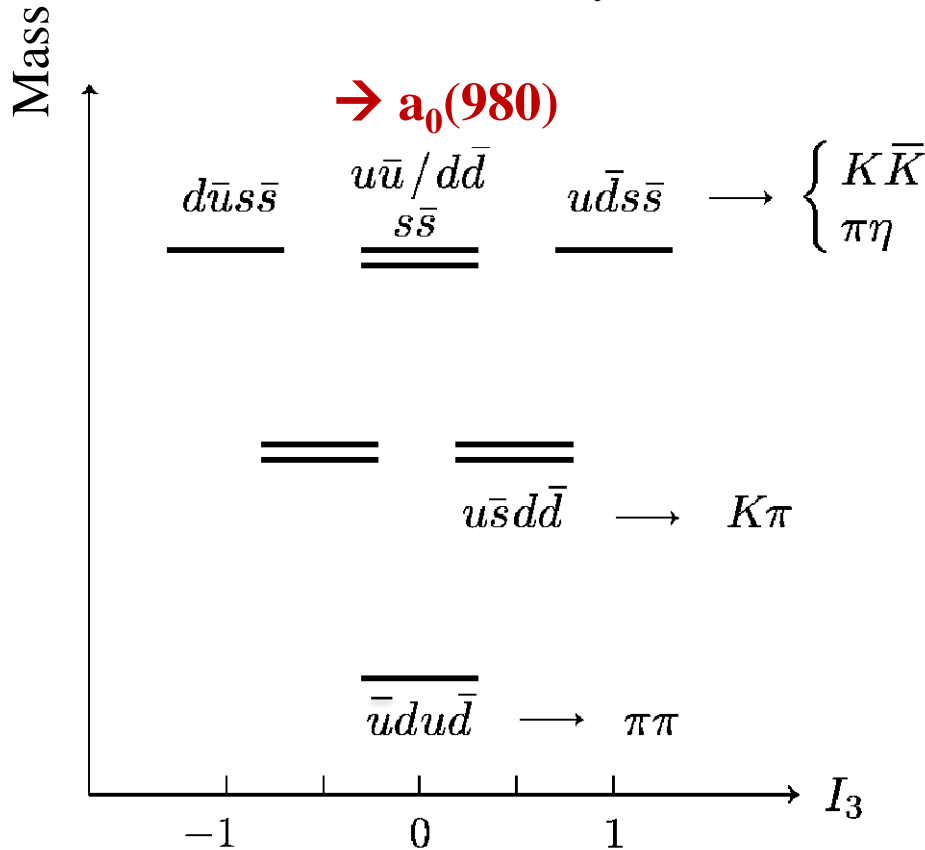
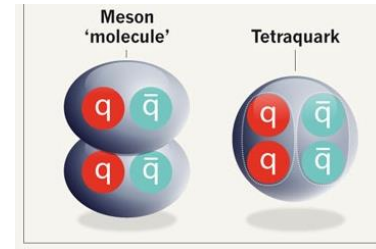
→ But, it is still controversial whether or not these mesons are four-quark states (e.g. see “Non- $qq$ -bar Mesons” in 2021 Review of Particle Physics).

# Predicted low-lying tetraquark nonet with $a_0(980)$ candidate meson



## Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



$f_0(980)$  [1]

$I^G(J^{PC}) = 0^+(0^{++})$

Mass  $m = 990 \pm 20$  MeV  
Full width  $\Gamma = 10$  to  $100$  MeV

$f_0(980)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$\pi\pi$	dominant	476
$K\bar{K}$	seen	36
$\gamma\gamma$	seen	495

$a_0(980)$  [1]

$I^G(J^{PC}) = 1^-(0^{++})$

Mass  $m = 980 \pm 20$  MeV  
Full width  $\Gamma = 50$  to  $100$  MeV

$a_0(980)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$\eta\pi$	dominant	319
$K\bar{K}$	seen	†
$\gamma\gamma$	seen	490

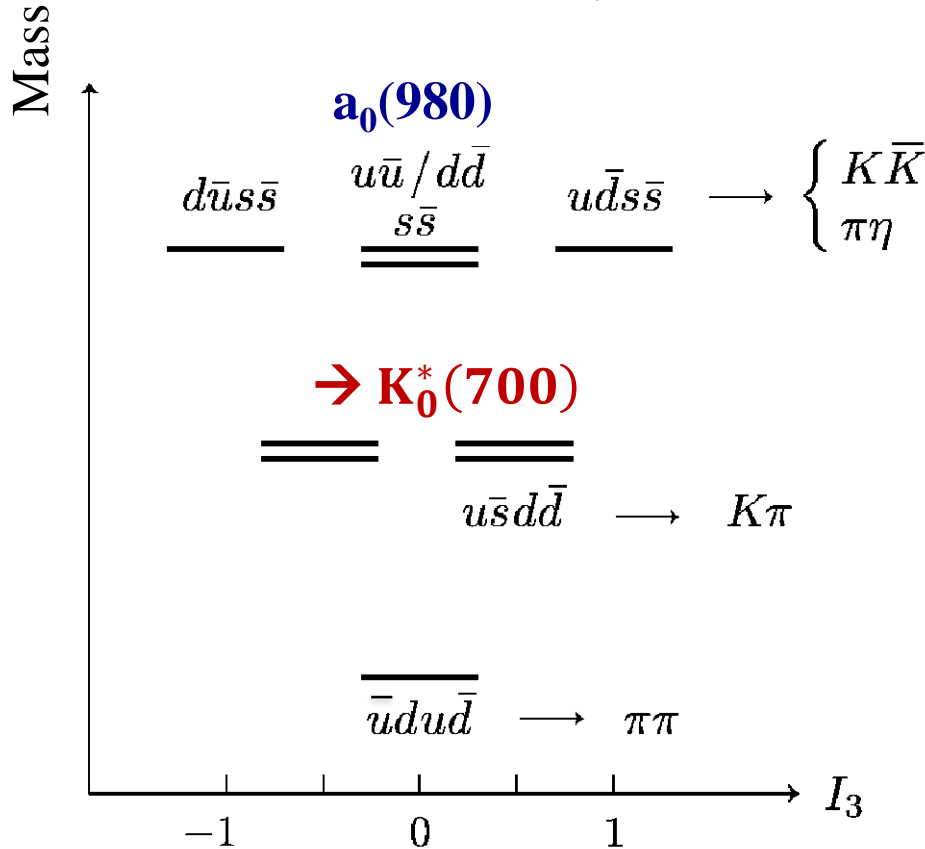
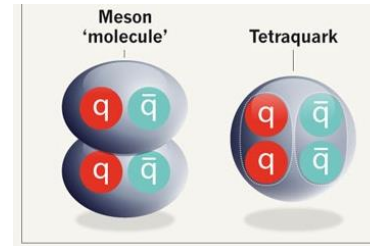
From Review of Particle Physics for light quark-antiquark mesons

The  $a_0(980)$  has been studied with  $K_S^0 K^\pm$  femtoscopy in pp and Pb–Pb collisions by ALICE  $\rightarrow$  PLB 774 (2017), PLB 790 (2019), PLB 833 (2022).

# Predicted low-lying tetraquark nonet with $K_0^*(700)$ candidate meson

## Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



$K_0^*(700)$

$$I(J^P) = \frac{1}{2}(0^+)$$

Mass (T-Matrix Pole  $\sqrt{s}$ ) = (630–730) – i (260–340) MeV  
 Mass (Breit-Wigner) =  $824 \pm 30$  MeV  
 Full width (Breit-Wigner) =  $478 \pm 50$  MeV

$K^*(892)$

$$I(J^P) = \frac{1}{2}(1^-)$$

$K^*(892)^\pm$  hadroproduced mass  $m = 891.76 \pm 0.25$  MeV  
 $K^*(892)^\pm$  in  $\tau$  decays mass  $m = 895.5 \pm 0.8$  MeV  
 $K^*(892)^0$  mass  $m = 895.55 \pm 0.20$  MeV ( $S = 1.7$ )  
 $K^*(892)^\pm$  hadroproduced full width  $\Gamma = 50.3 \pm 0.8$  MeV  
 $K^*(892)^\pm$  in  $\tau$  decays full width  $\Gamma = 46.2 \pm 1.3$  MeV  
 $K^*(892)^0$  full width  $\Gamma = 47.3 \pm 0.5$  MeV ( $S = 1.9$ )

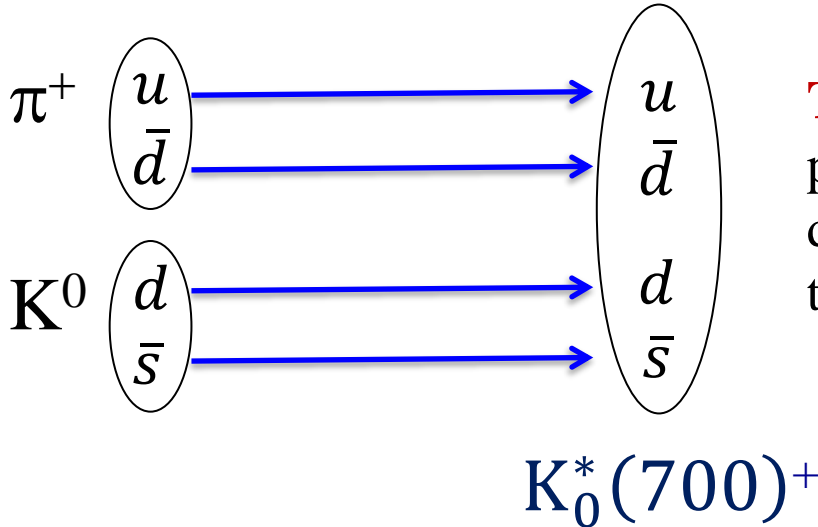
$K^*(892)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$P$ (MeV/c)
$K\pi$	$\sim 100$	%	290
$K^0\gamma$	$(2.46 \pm 0.21) \times 10^{-3}$		307
$K^\pm\gamma$	$(1.00 \pm 0.09) \times 10^{-3}$		309
$K\pi\pi\pi$	$< 7$	$\times 10^{-4}$	95% 223

$K_0^*(700)$  decay channel listed in RPP  
as 100%  $\pi K$  ..... same as for  $K^*(892)$

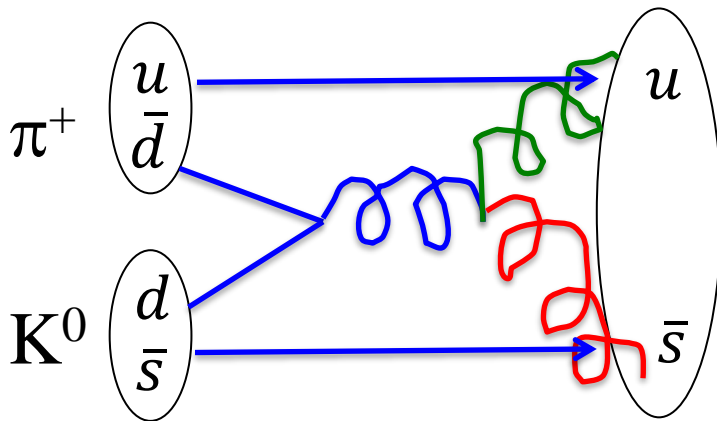
The  $K_0^*(700)$  has been studied with  $\pi^\pm K_0$ s femtoscopy in 13 TeV pp collisions by the ALICE Collaboration (Phys. Lett. B 856 (2024) 138915)

# Two scenarios for FSI of $\pi^+K^0 \rightarrow K_0^*(700)^+ \rightarrow \pi^+K^0$

## Tetraquark vs. Diquark



**Tetraquark** formation is a 1<sup>st</sup>-order process that proceeds through the direct transfer of existing quarks to the  $K_0^*(700)$  from the collision of  $\pi^+K^0$ .



**Diquark** formation is a higher-order process requiring the annihilation of the  $d$  quarks in the  $\pi^+K^0$  collision and transfer of energy via gluons to  $K_0^*(700)$ .

**Can we see a signature of tetraquark vs. diquark in femtoscopy?**

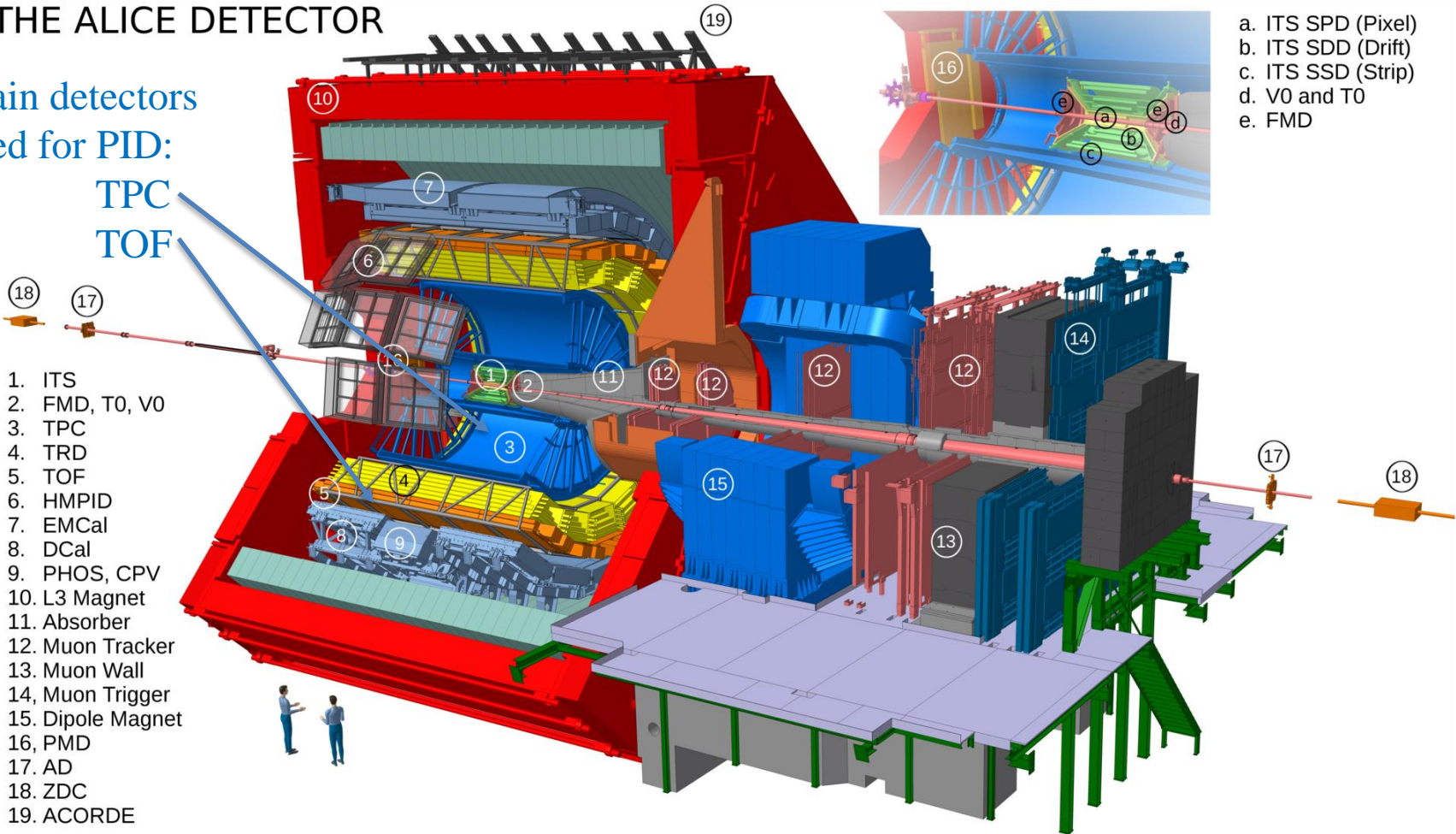


ALICE

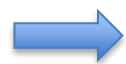
# THE ALICE DETECTOR

Main detectors used for PID:

TPC  
TOF



Run 2 data set used in this analysis



$\sqrt{s} = 13$  TeV pp collisions, minimum bias trigger



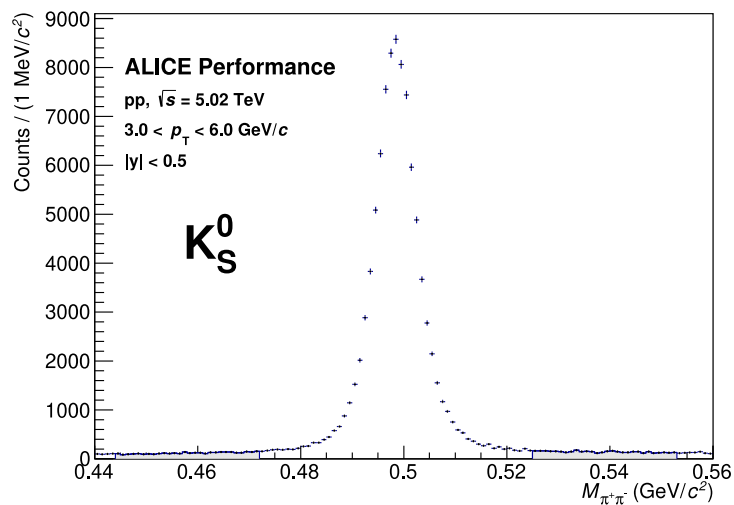


ALICE

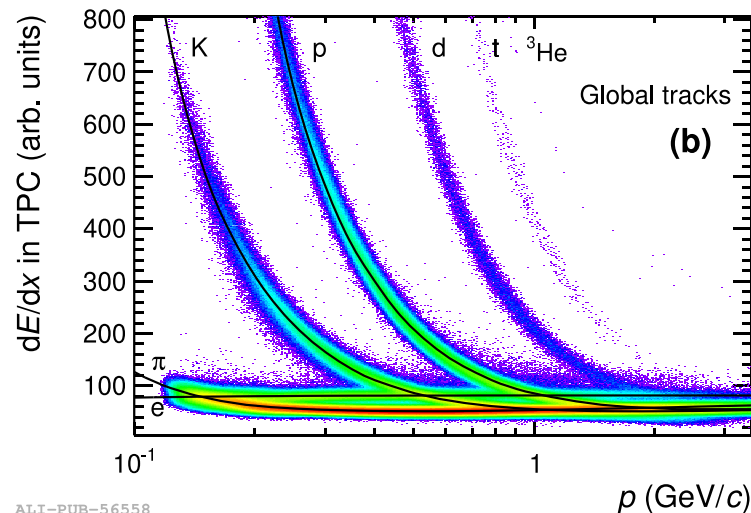
# Excellent PID purity for $K_S^0$ and $\pi^\pm$

Particle ID using  $K_S^0 \rightarrow \pi^+\pi^-$

$dE/dx$

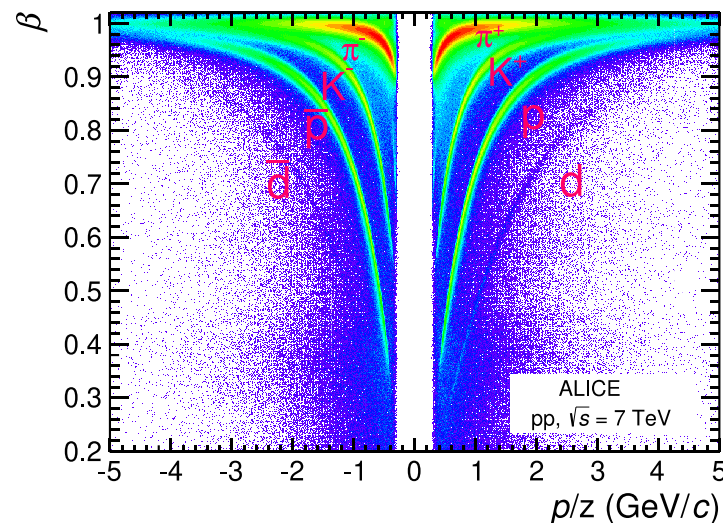


$K_S^0$  purity  $\sim 98\%$



ALI-PUB-56558

TOF



ALI-PUB-92279

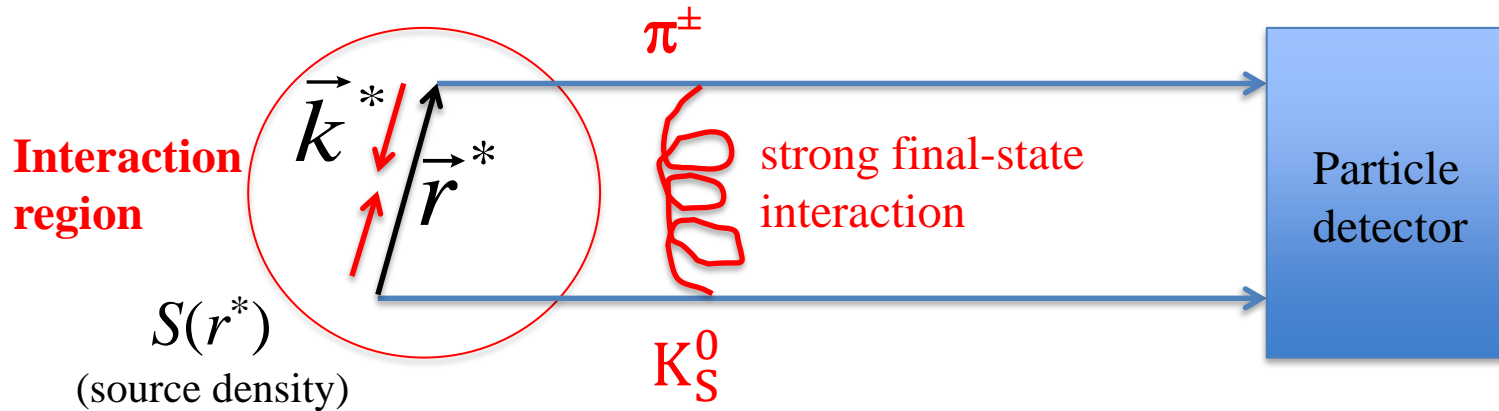
$\pi^\pm$  purity  $\sim 98\%$

# Femtoscscopy using strong final-state interactions

R. Lednický and V.L. Lyuboshits, (Sov. J. Nucl. Phys. 35 (1982) 770)



Consider the correlations of two **non-identical particles**, e.g.  $\pi^\pm K_S^0$ , emitted from the interaction region



$\vec{r}^*$  → relative distance between the particle emission points in the pair reference frame.  
 $\vec{k}^*$  → momentum of the particles in the pair reference frame.

The wave function describing the elastic interaction between the particles is:

$$\Psi_{-\vec{k}^*} = e^{-\vec{k}^* \cdot \vec{r}^*} + f(\vec{k}^*) \frac{e^{i\vec{k}^* \cdot \vec{r}^*}}{r^*}$$

plane wave      S-wave scattering amplitude      S-wave final-state interaction (FSI) term





ALICE

Correction to spherical outgoing wave assumption

# Two-particle correlation function:

$$C(k^*) = \int d^3\vec{r}^* S(r^*) |\Psi_{-\vec{k}^*}(\vec{r}^*)|^2, \text{ where } S(r^*) \sim e^{-\frac{r^{*2}}{4R^2}}$$

Radius parameter  $\nearrow$

Lambda parameter  $\searrow$

$$C(k^*) = 1 + \lambda\alpha \left[ \frac{1}{2} \left| \frac{f(k^*)}{R} \right|^2 + \frac{2\Re f(k^*)}{\sqrt{\pi}R} F_1(2k^*R) - \frac{\Im f(k^*)}{R} F_2(2k^*R) + \overline{\Delta C} \right]$$

Integral functions  $\nearrow$

Assume the FSI of the  $\pi^\pm K_S^0$  is due to a **Resonance**  $\Rightarrow f(k^*) = \frac{\gamma}{M_R^2 - s - i\gamma k^*}$

$\gamma$  is the coupling parameter for the decay of the resonance into  $\pi^\pm K_S^0$   $\Rightarrow \Gamma_R = \frac{\langle k^* \rangle}{M_R} \gamma$

where  $M_R$  and  $\Gamma_R$  are the mass and width of the FSI resonance, and  $\langle k^* \rangle$  is the average  $k^*$  over the fit range.

**$C(k^*)$  is measured experimentally as**  $\Rightarrow C(k^*) = \frac{A(k^*)}{B(k^*)}$

where  $A(k^*)$  is the measured distribution of particle pairs from the same event in a  $k^*$  bin, and  $B(k^*)$  is the reference distribution of particle pairs from mixed events in a  $k^*$  bin.

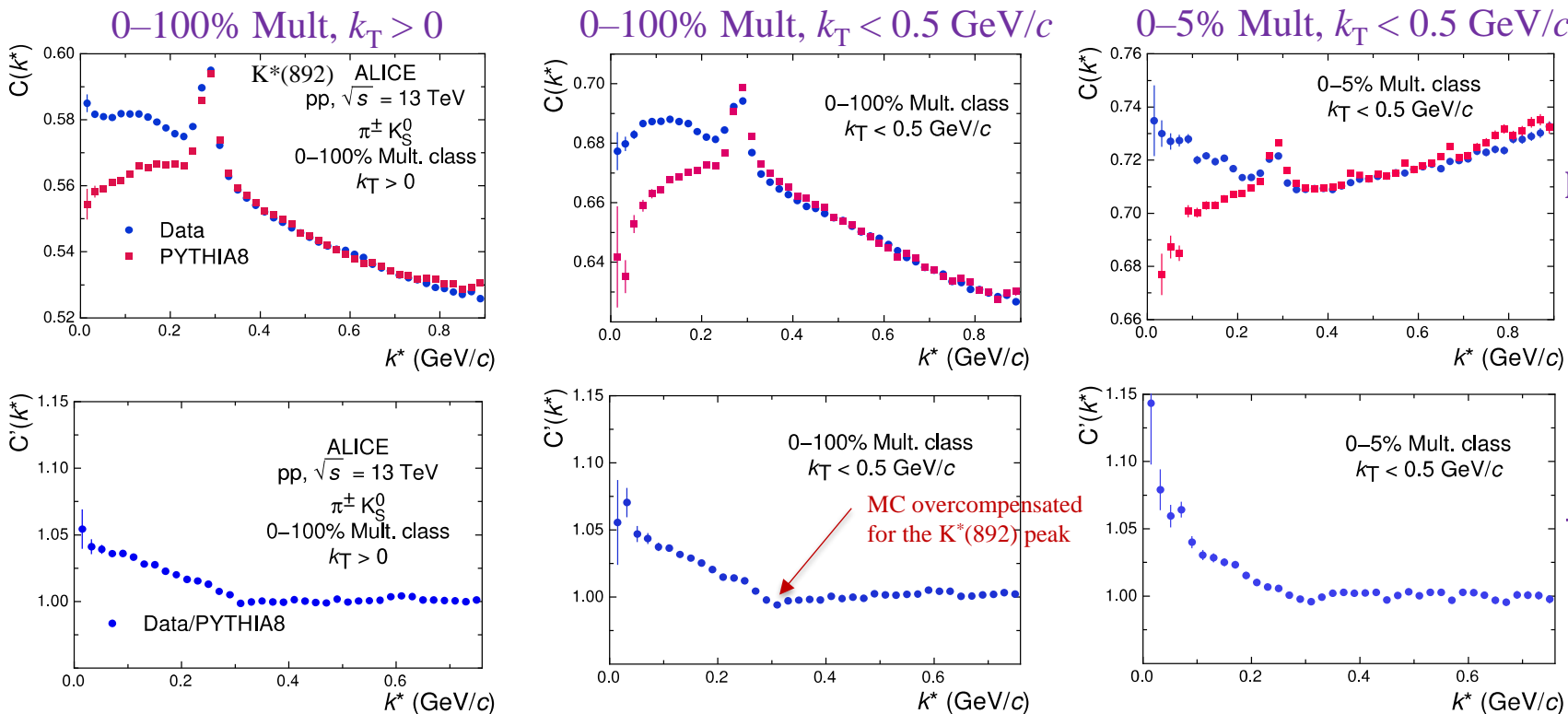
# Raw $C(k^*)$ from 13 TeV $pp \rightarrow \pi^\pm K_S^0$ data compared with PYTHIA8

(PYTHIA8 run through GEANT to simulate ALICE data)



ALICE

NEW



PLB 856 (2024)

Analyze these three sets of  $C(k^*)$  with different kinematic cuts in order to extract the multiplicity and  $k_T$  dependences of  $\lambda$  and  $R$ .

PYTHIA8 does a good job describing the baseline of the data.

Data show large enhancement at  $k^* \sim 0$  compared with PYTHIA8.

→ Is the extra enhancement in the data due to  $K_0^*(700)$  FSI ??

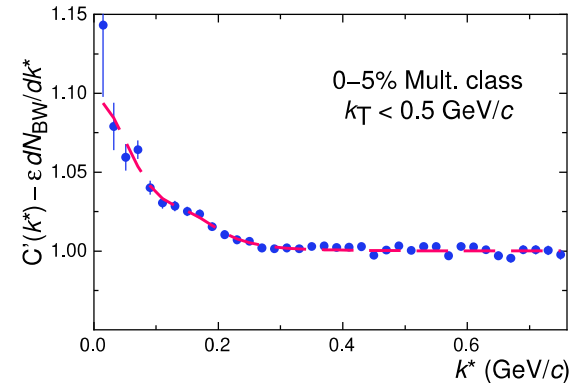
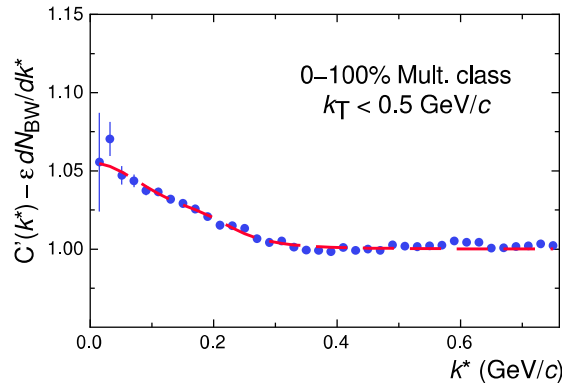
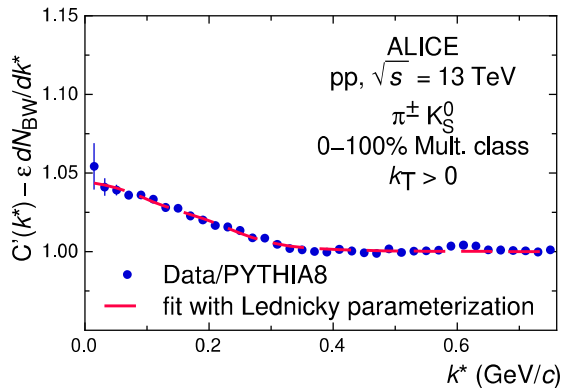
Add a Breit-Wigner resonance term to the Lednický equation to fit out the small  $K^*(892)$  overcompensation in the MC:

$$C'(k^*) = C(k^*) + \varepsilon \frac{dN_{BW}}{dm} \frac{dm}{dk^*} \quad \text{where,} \quad \frac{dN_{BW}}{dm} \propto \frac{\Gamma_{892}}{(m - m_{892})^2 + \Gamma_{892}^2/4}$$

→ Fit  $C'(k^*)$  to  $C_{\text{data}}(k^*)/C_{\text{MC}}(k^*)$ , with fit parameters  $R$ ,  $\lambda$ ,  $M_R$ ,  $\gamma$  and  $\varepsilon$

NEW

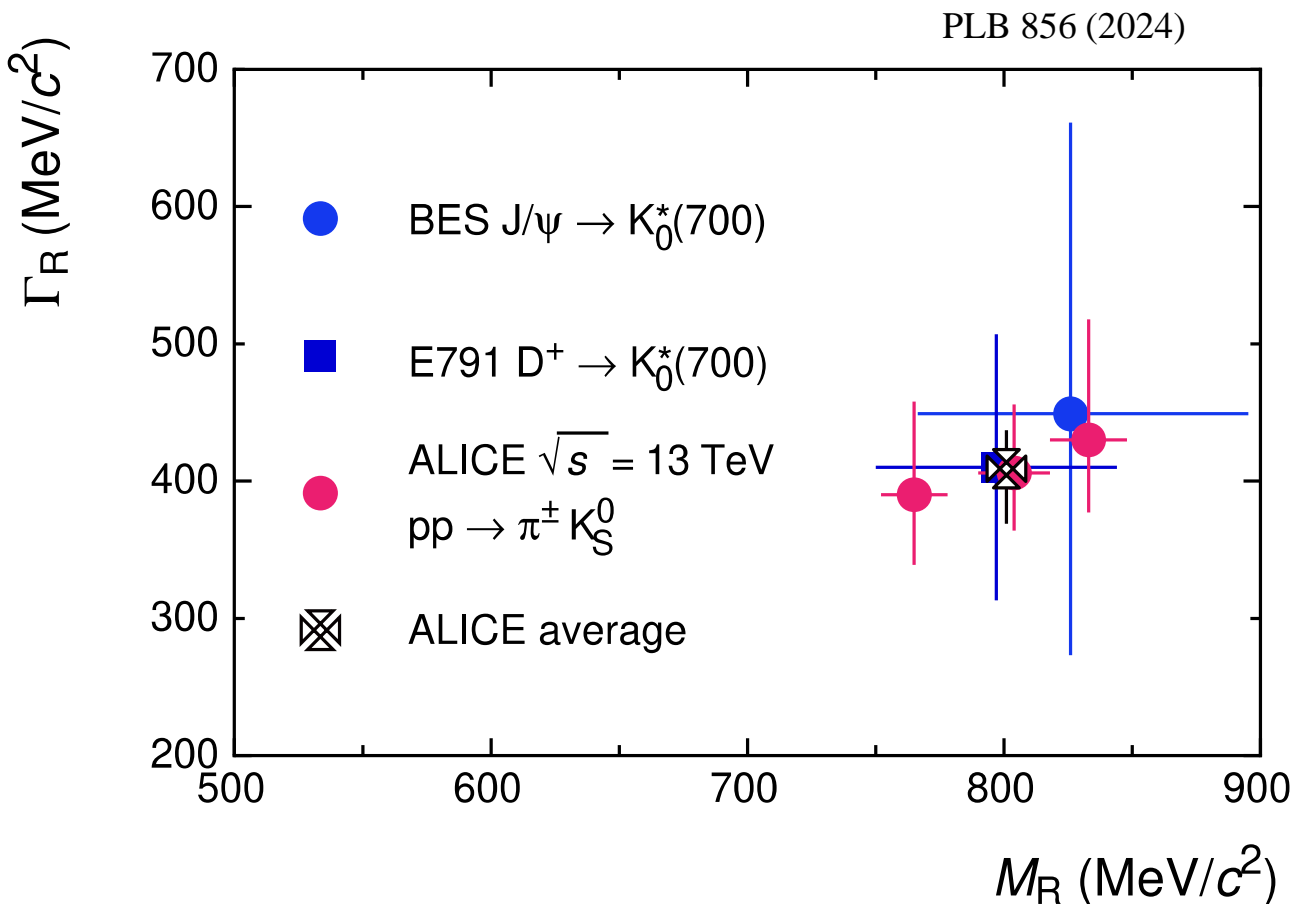
Lednický + BW fits to data/PYTHIA8 for 13 TeV pp →  $\pi^\pm K_S^0$



PLB 856 (2024)

The Lednický equation, assuming a resonance FSI, does a good job fitting the correlation function for each case.

# Results of Lednický fits to 13 TeV pp $\rightarrow \pi^\pm K_S^0$ for $(M_R, \Gamma_R)$ and comparisons with other measurements



NEW

BES Collab.  
PLB 698 (2011)

E791 Collab.  
PRL 89 (2002)

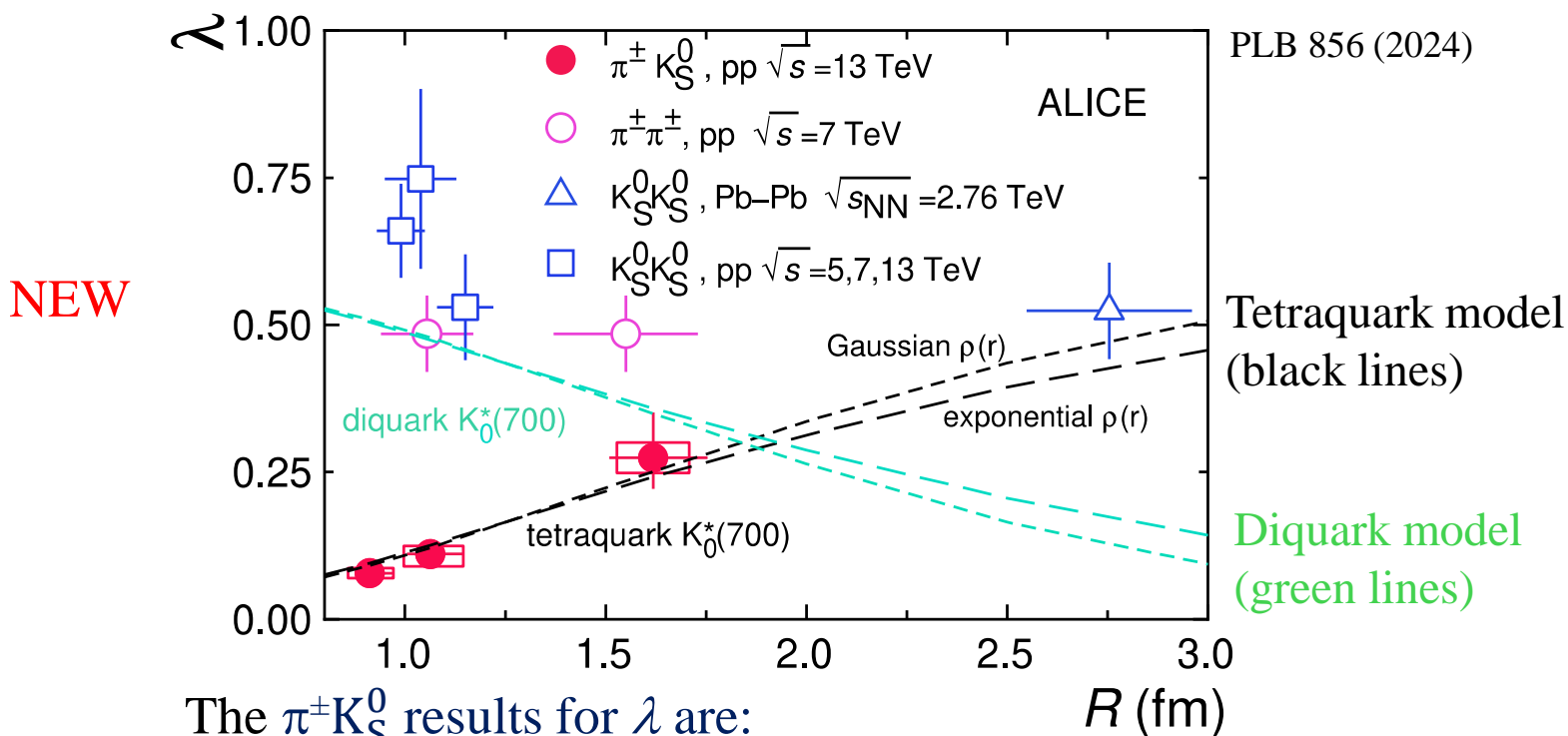
The  $\pi^\pm K_S^0$   $\Gamma_R$  and  $M_R$  agree with BES and E791 measurements of  $K_0^*(700)$ .  
 **$\rightarrow$  Shows that the  $\pi^\pm K_S^0$  FSI is due to the  $K_0^*(700)$ .**

# Results of Lednický fits to 13 TeV pp $\rightarrow \pi^\pm K_S^0$ for $(R, \lambda)$ and comparisons with other measurements and a toy model



ALICE

$\lambda$  vs  $R$  from published ALICE pp, Pb–Pb  $\rightarrow K_S^0 K_S^0$ ,  $\pi\pi$  (PLB 833 (2022), PRC92 (2015), PRD84 (2011)) and the new 13 TeV pp  $\rightarrow \pi^\pm K_S^0$  results.



The  $\pi^\pm K_S^0$  results for  $\lambda$  are:

- smaller than for  $K_S^0 K_S^0$  and  $\pi\pi$ .
  - increase with  $R$ , unlike  $K_S^0 K_S^0$ ,  $\pi\pi$ .
  - consistent with the Tetraquark toy model  $R$  dependence.
- Behavior expected for a tetraquark  $K_0^*(700)$ .**

# Summary

- $K_S^0 K^\pm$  femtoscopic analyses in  $\sqrt{s_{NN}} = 2.76$  TeV Pb–Pb, and  $K_S^0 K^\pm$  and  $K_S^0 K_S^0$  analyses in  $\sqrt{s} = 5.02, 7$  and  $13$  TeV pp collisions from ALICE are published in PLB

## Main physics take-away:

**A simple geometric model used to explain these results is suggestive of the  $a_0(980)$  being a tetraquark state.**

- $\pi^\pm K_S^0$  femtoscopic analysis in  $\sqrt{s} = 13$  TeV pp collisions from ALICE was shown.

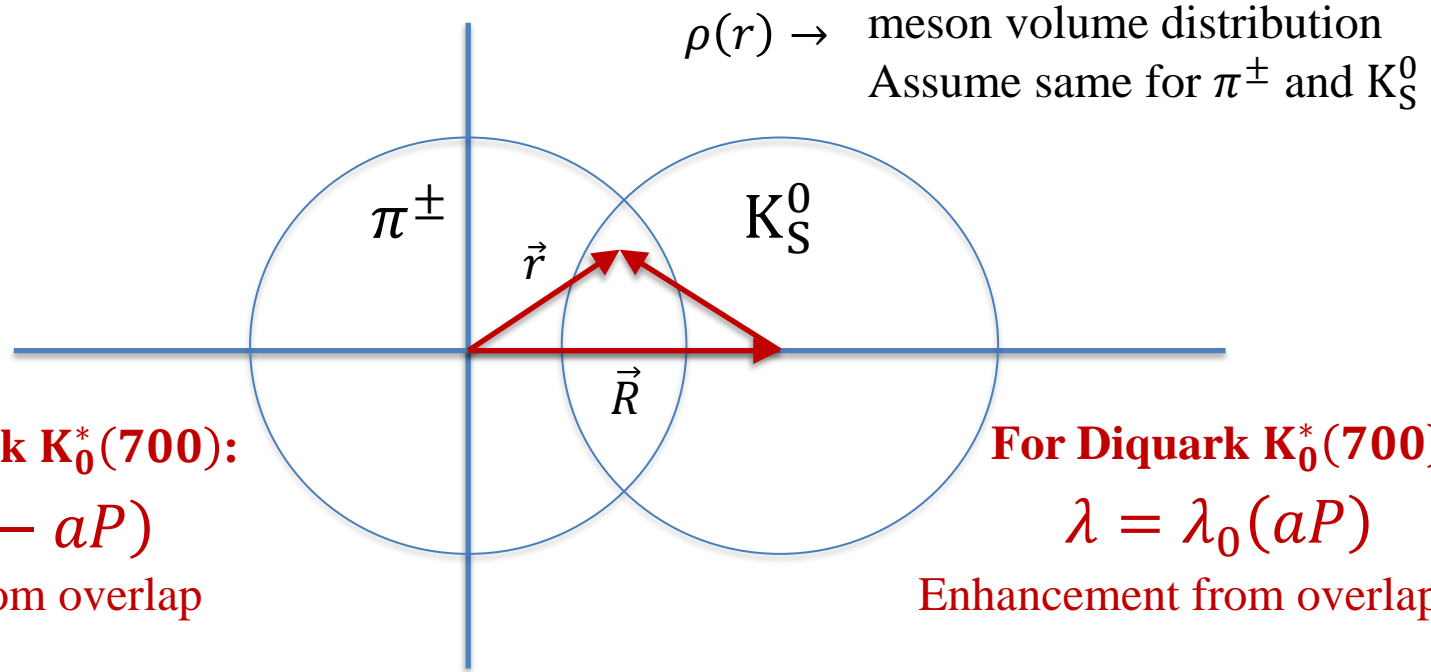
## Main physics take-aways:

- 1) The FSI is shown to be due to the formation of the  $K_0^*(700)$ .
- 2) The extracted  $R$  parameters are comparable to those from published  $\pi\pi$  and  $K_S^0 K_S^0$  measurements in pp collisions.
- 3) The  $\lambda$  parameter is much smaller than in the identical boson measurements.
- 4) The dependence of  $\lambda$  on  $R$  is as expected by a geometric toy model assuming a tetraquark  $K_0^*(700)$ .**

# Backup slides



# Toy model based on geometry to describe R dependence of $\lambda$ for 13 TeV $pp \rightarrow \pi^\pm K_S^0$



**For Tetraquark  $K_0^*(700)$ :**

$$\lambda = \lambda_0(1 - aP)$$

Suppression from overlap

**For Diquark  $K_0^*(700)$ :**

$$\lambda = \lambda_0(aP)$$

Enhancement from overlap

$$P \equiv \frac{\int \rho(r)\rho(|\vec{r} - \vec{R}|)dV}{\int [\rho(r)]^2 dV}$$

“Overlap Probability”

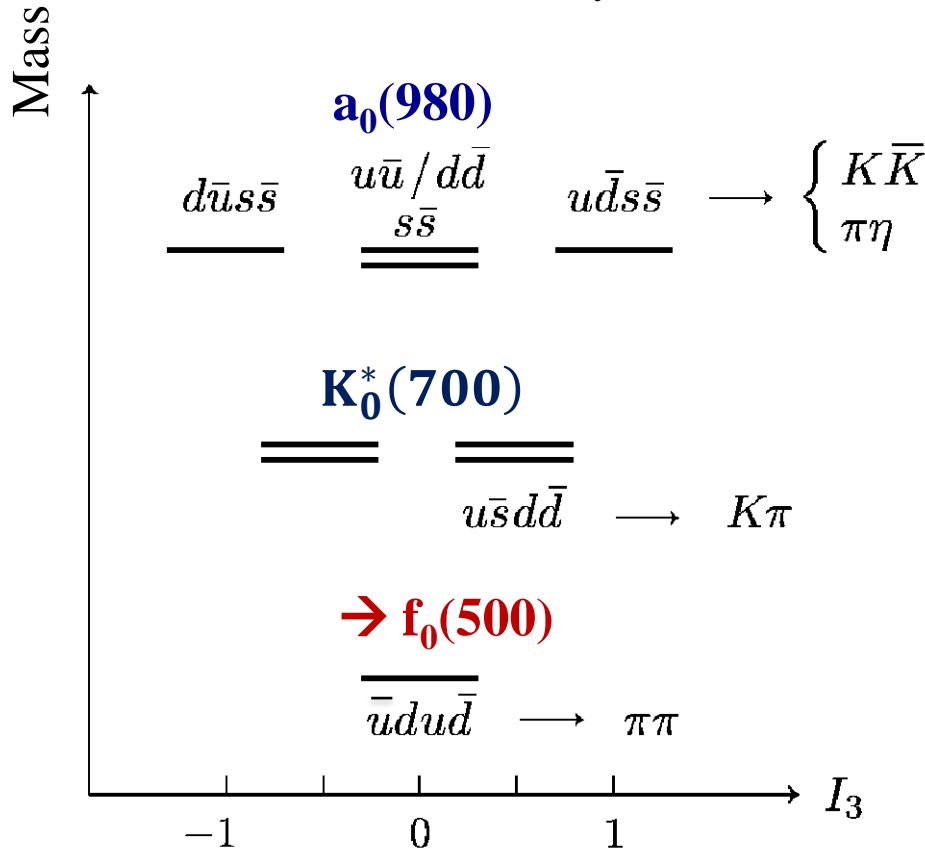
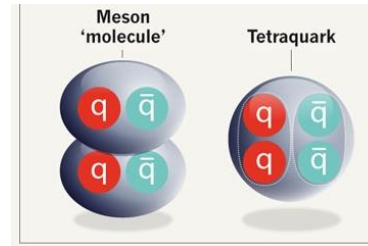
$a \rightarrow$  “ $d - \bar{d}$  annihilation efficiency”

Try two cases:  $\left\{ \begin{array}{ll} \rho(r) \propto e^{-r^2/2\sigma^2} & \lambda_0 = 0.6, \quad \sigma = 1.1 \text{ fm}, \quad a = 1 \\ \rho(r) \propto e^{-r/r_0} & \lambda_0 = 0.6, \quad r_0 = 0.85 \text{ fm}, \quad a = 1 \end{array} \right.$

# Predicted low-lying tetraquark nonet with $f_0(500)$ candidate meson

## Tetraquark nonet

Alford and Jaffe, Nucl. Phys. B 578 (2000)



**$f_0(500)$**      $J^G(J^{PC}) = 0^+(0^{++})$

also known as  $\sigma$ ; was  $f_0(600)$

See the review on "Scalar Mesons below 1 GeV."

Mass (T-Matrix Pole  $\sqrt{s}$ ) = (400–550)–i(200–350) MeV

Mass (Breit-Wigner) = 400 to 800 MeV

Full width (Breit-Wigner) = 100 to 800 MeV

$f_0(500)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$\pi\pi$	seen	–
$\gamma\gamma$	seen	–

**$\rho(770)$**      $J^G(J^{PC}) = 1^+(1^{--})$

See the review on "Spectroscopy of Light Meson Resonances."

Mass  $m = 775.26 \pm 0.23$  MeV

Full width  $\Gamma = 149.1 \pm 0.8$  MeV

$\rho(770)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	$p$ (MeV/c)
$\pi\pi$	$\sim 100$	%	363

→ Recently initiated the study of the  $f_0(500)$  with  $\pi^+\pi^-$  femtoscopy in 13 TeV pp collisions by ALICE → Work in progress!

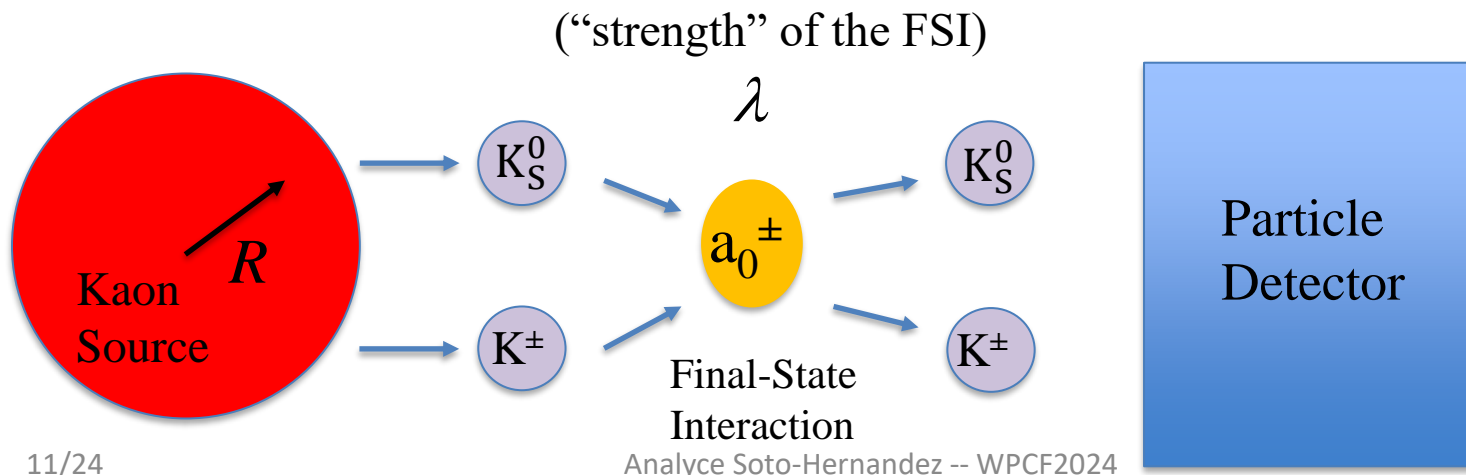
# $K_S^0 K^\pm$ femtoscopy

(ALICE first to study this!)

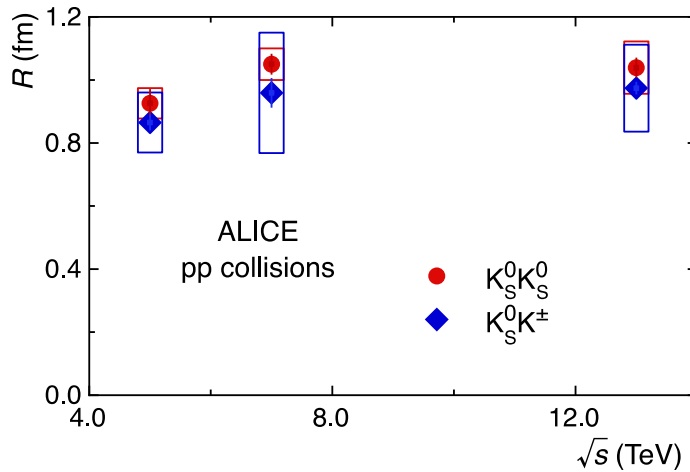
## Pair-wise interactions present (or absent) for $K_S^0 K^\pm$ pairs

- Non-identical pairs  $\rightarrow$  no quantum statistics.
  - $K_S^0$  is uncharged  $\rightarrow$  no Coulomb interaction.
  - $f_0(980)$  resonance is isospin = 0  $\rightarrow$  no  $f_0(980)$  strong interaction.
  - $a_0(980)$  resonance is isospin = 1  $\rightarrow$   $a_0(980)$  strong interaction.
- should be present for both  $K_S^0 K^+$  and  $K_S^0 K^-$  pairs.

$\rightarrow$   $K_S^0 K^\pm$  femtoscopy selects for the  $a_0(980)^\pm$  as the Final-state Interaction (FSI).



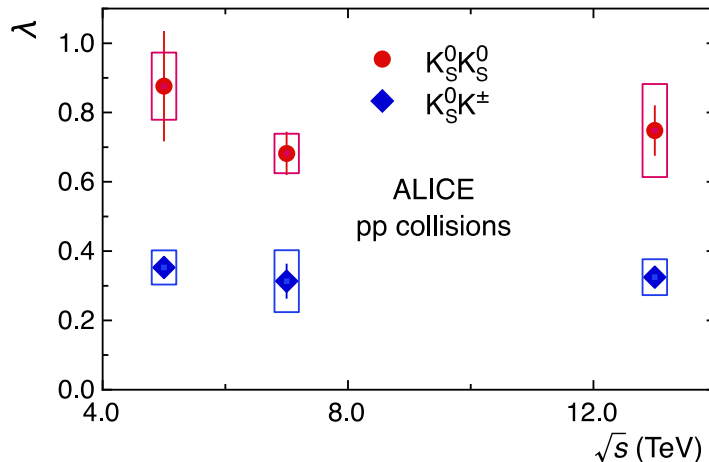
# ALICE results for $K_S^0 K_S^0$ and $K_S^0 K^\pm$ femtoscopy in 5.02, 7 and 13 TeV pp collisions (*Phys. Lett. B833 (2022)*)



➤  $a_0(980)$  is the FSI for the  $K_S^0 K^\pm$  pair. The  $K_S^0 K_S^0$  correlation function is dominated by quantum statistics due to identical-boson pairs.

➤  $\lambda$  from  $K_S^0 K^\pm$  is significantly smaller than  $\lambda$  from  $K_S^0 K_S^0$ .

➔ **tetraquark signature for the  $a_0(980)$ ?**



$$\left\langle \frac{\lambda_{K_S^0 K^\pm}}{\lambda_{K_S^0 K_S^0}} \right\rangle \approx 0.44 \pm 0.07$$

# A simple geometric picture in pp collisions

**Tetraquark  $a_0^-$  FSI** -- suppressed due to strange quark annihilation opening up a non-resonant channel.

**Diquark  $a_0^-$  FSI** -- favored from the annihilation process.

$\frac{\Gamma^0}{\Gamma_{K^0 K^-}} / \frac{\Gamma}{\Gamma_{KK}}$  for  $\bar{u}s\bar{s}d$  vs.  $\bar{u}d$   $a_0^-$  expected from geometry

Identical kaon  $\lambda$  - parameter

