

# Reevaluating the SGWB from BNS in an Agnostic Framework: Post-Mergers Contribution

Léonard Lehoucq (speaker), I.Dvorkin, and L.Rezzolla

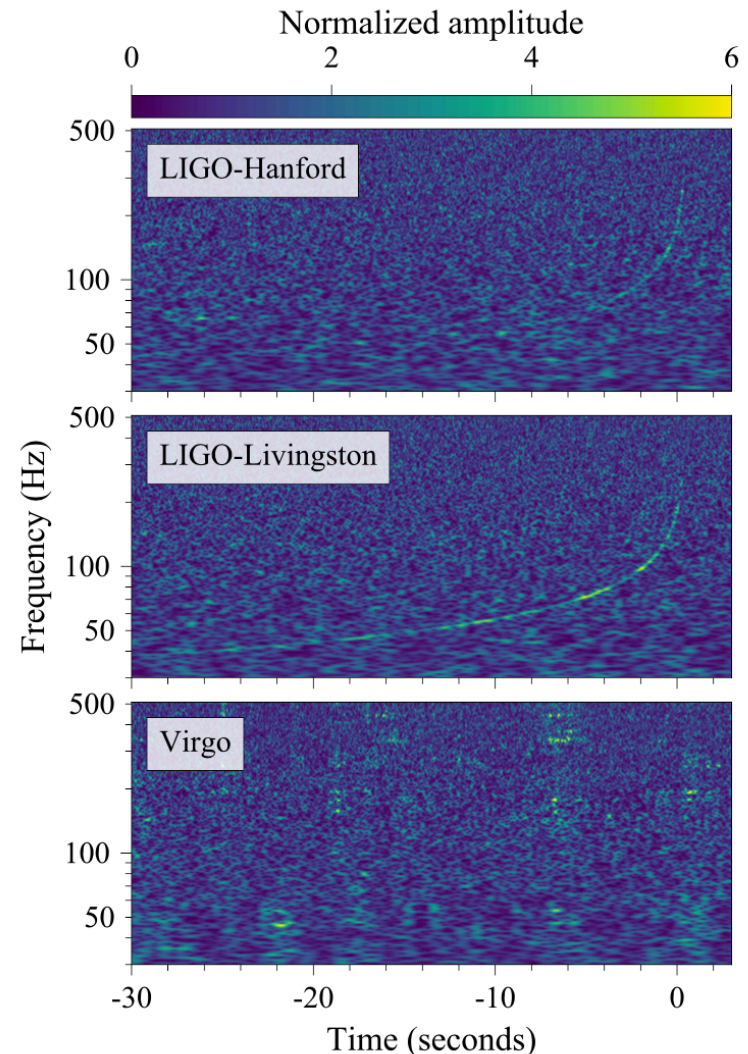
Institut d'Astrophysique de Paris

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# BNS mergers

- ~ 2 individual detections so far
- Amazing MMA events (GW, GRB, KN)
- But LVK sensible only up to ~500Hz, we are not looking at the full GW strain!
- What about higher frequencies > 1kHz that could be detectable with 3G detectors (ET, CE, ...)?



GW170817 chirp, <https://www.ligo.org>

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- Formation of a Hyper Massive Neutron Star (HMNS)  
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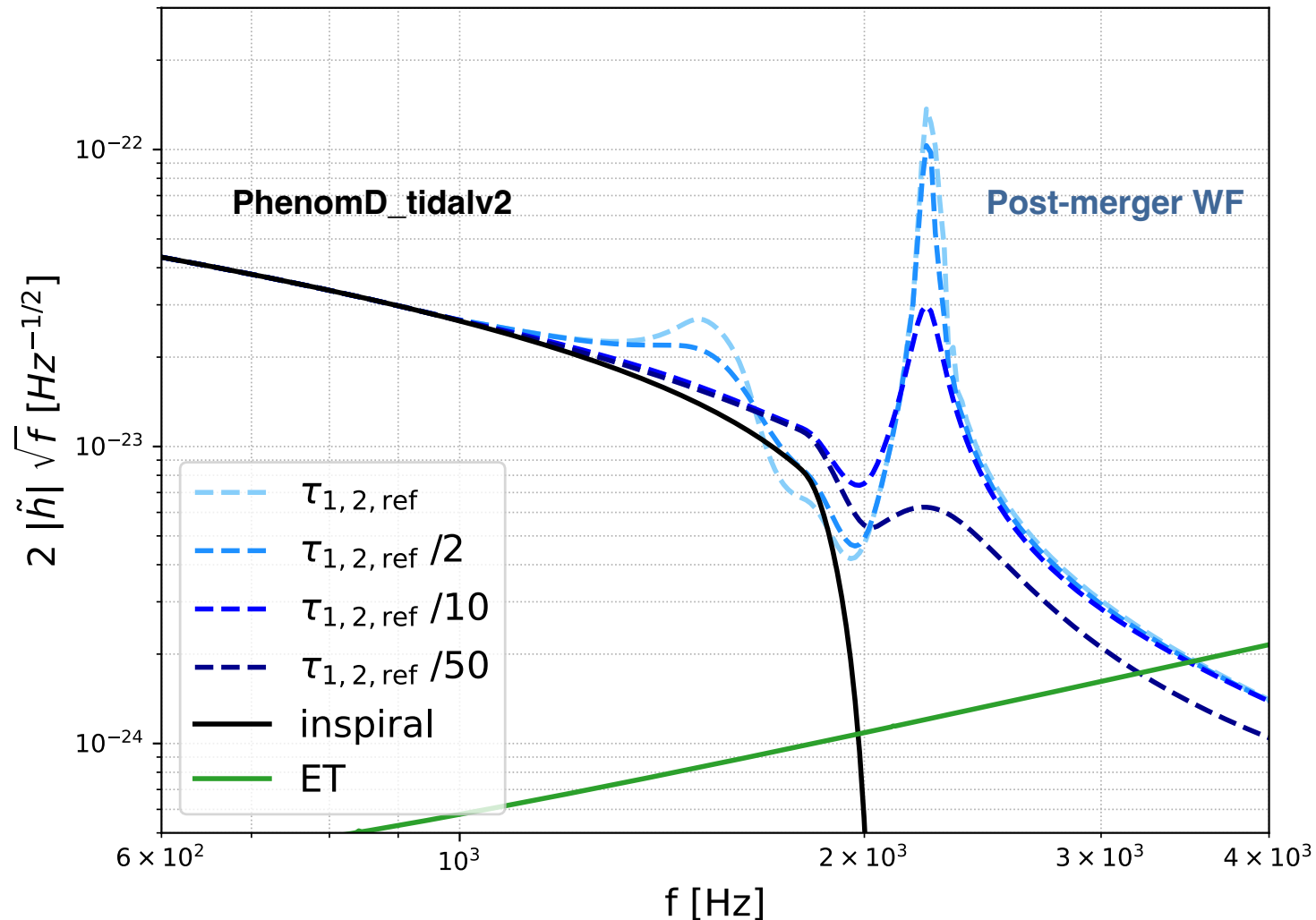
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$$h_+(t) = \alpha e^{-t/\tau_1} [\sin(2\pi f_1 t) + \sin(2\pi(f_1 - f_{1\epsilon})t) + \sin(2\pi(f_1 + f_{1\epsilon})t)] + e^{-t/\tau_2} \sin(2\pi f_2 t + 2\pi\gamma_2 t^2 + 2\pi\xi_2 t^3 + \pi\beta_2) \quad (1)$$

*Analytic WF from S.Bose, K.Chakravarti, L.Rezzolla et al. (2018)*

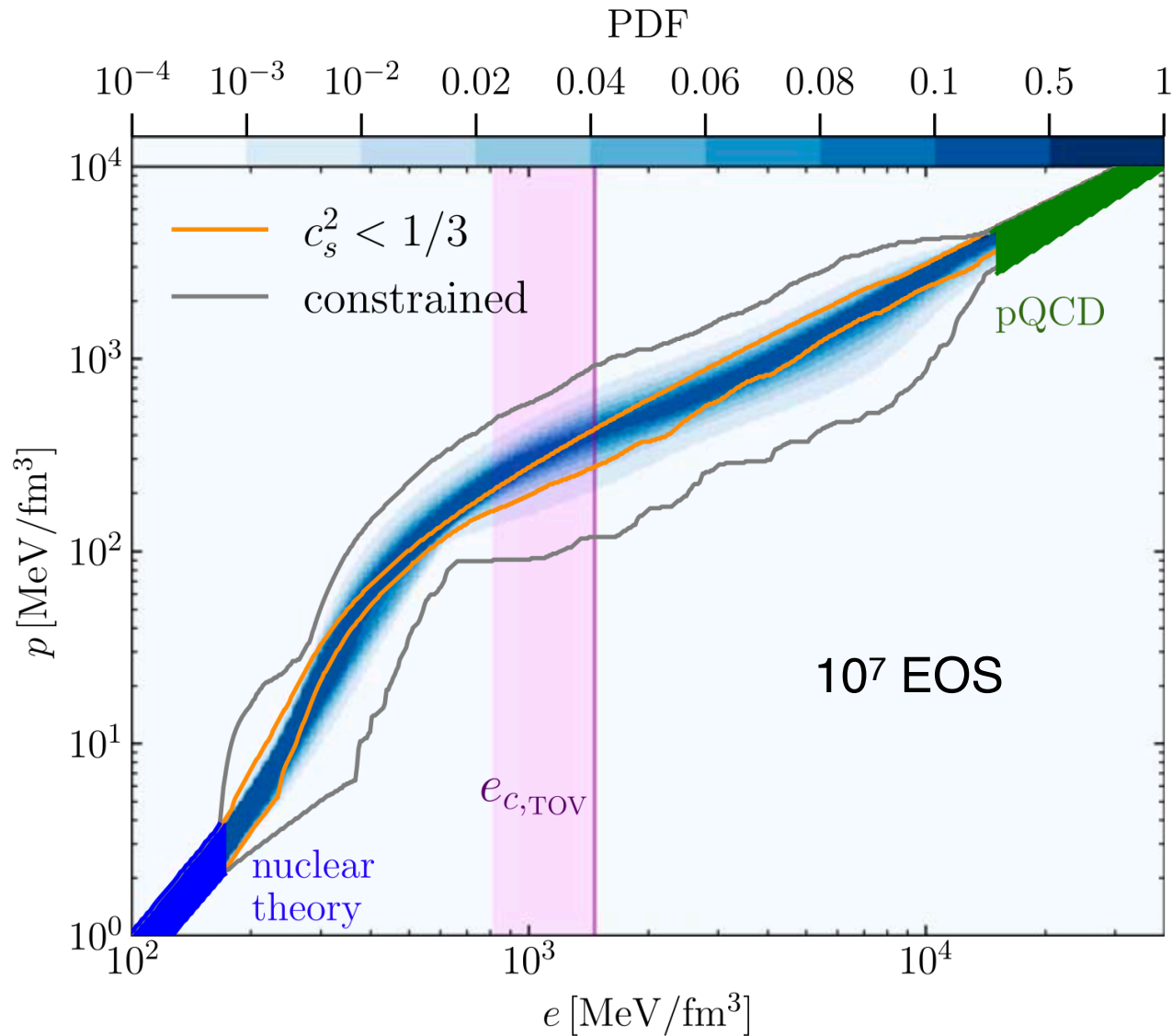
# BNS merger waveform



$M_1 = M_2 = 1.250M_\odot$ ,  $D = 50$  Mpc, for the GNH3 EOS

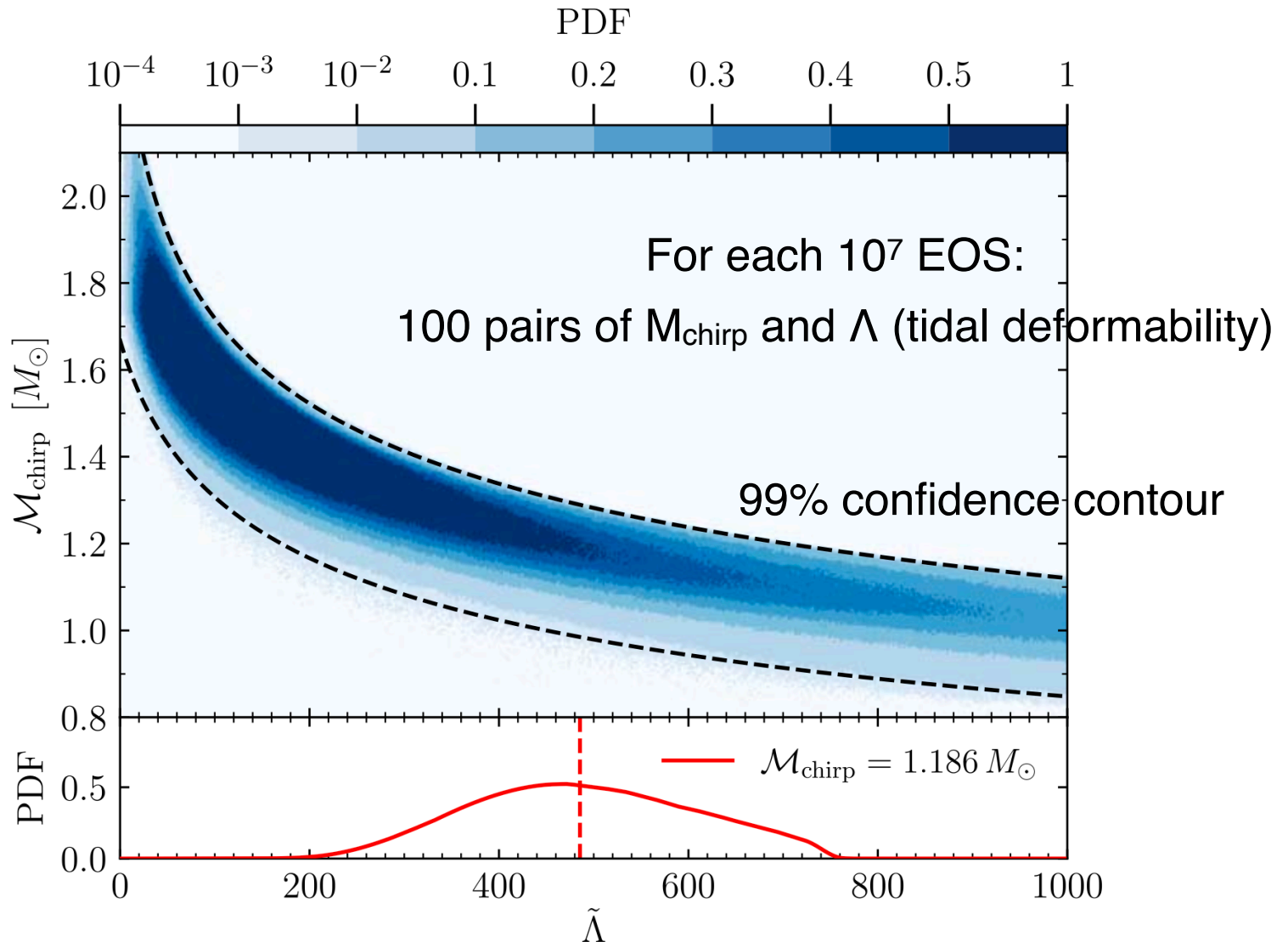
*L. Lehoucq, I. Dvorkin and L. Rezzolla in prep.*

# Agnostic approach of the EOS



*S. Altıparmak, C. Ecker, and L. Rezzolla (2022)*

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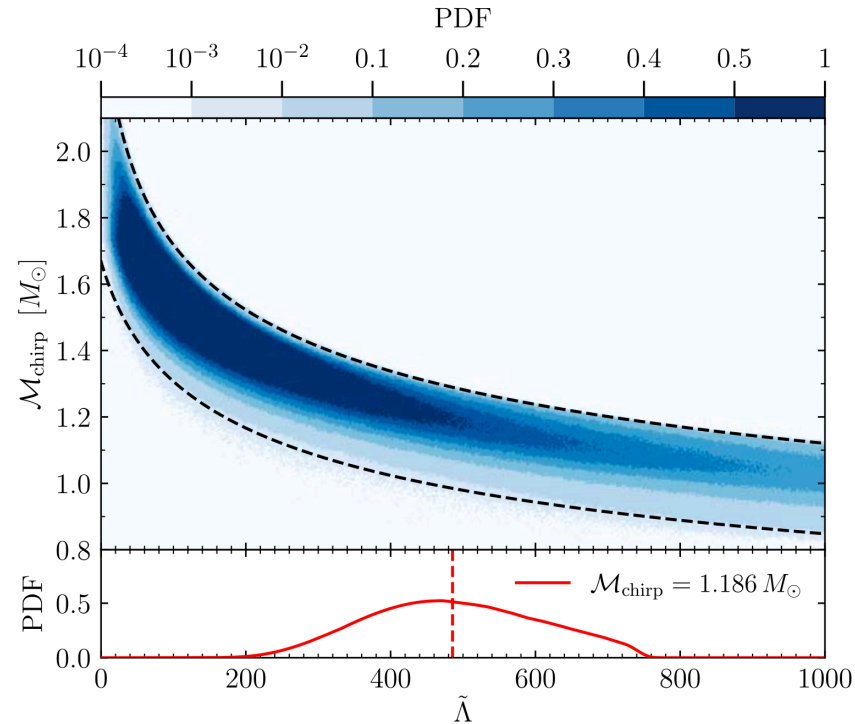


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# Agnostic approach of the EOS

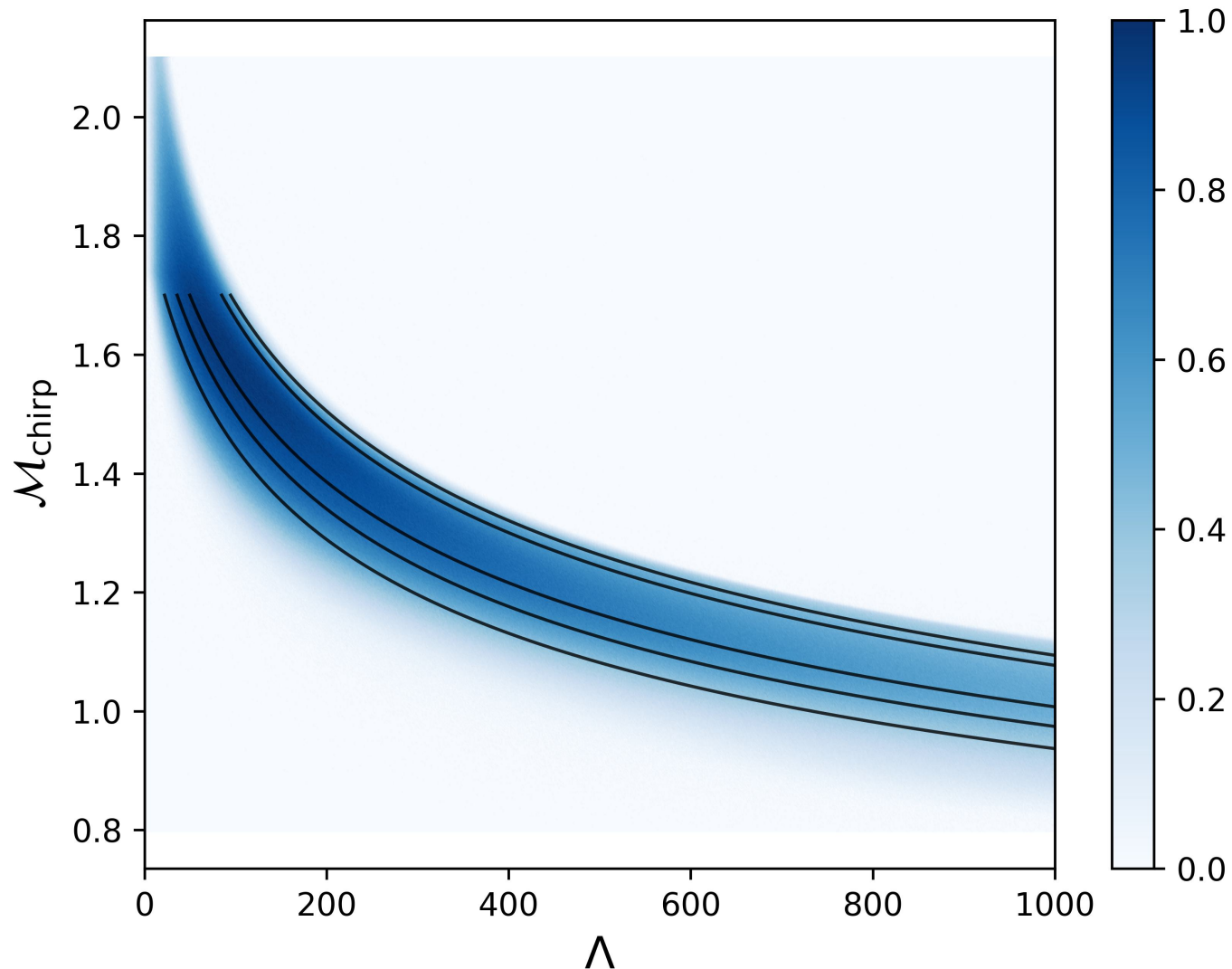
- A priori, an EOS is not defined by a single  $M_{\text{chirp}}-\Lambda$  relation
- But with only symmetric binaries, there is unicity of the relation!
- We can generate a valid EOS in accordance with the PDF, it takes the form of a power-law :



*S.Altiparmak, C.Ecker, and L.Rezzolla (2022)*

$$\Lambda = a + b M_{\text{chirp}}^{\alpha}$$

# Agnostic approach of the EOS



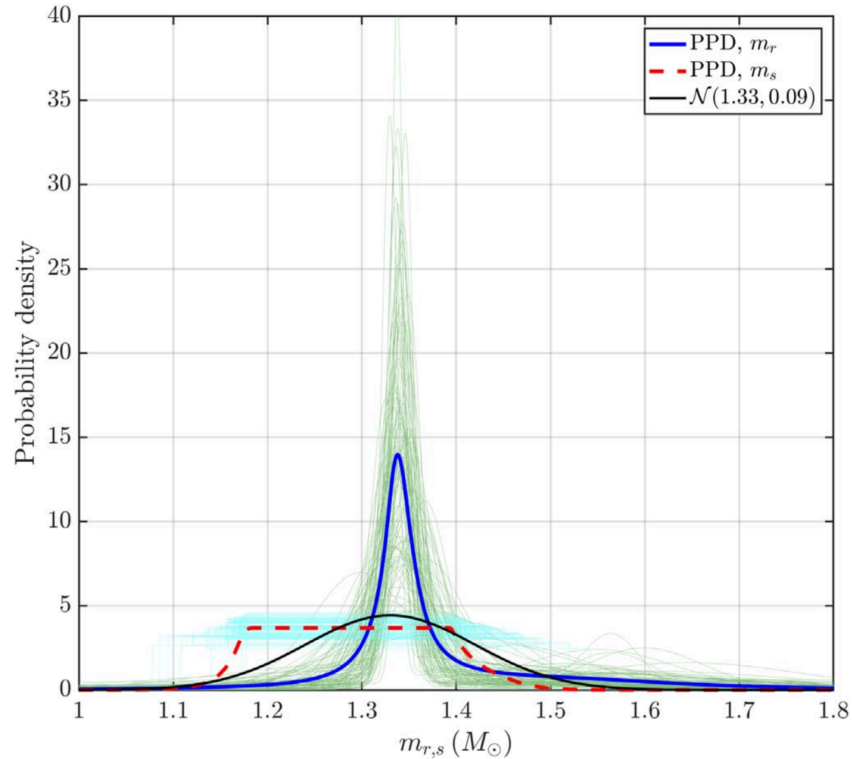
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# BNS population modelling

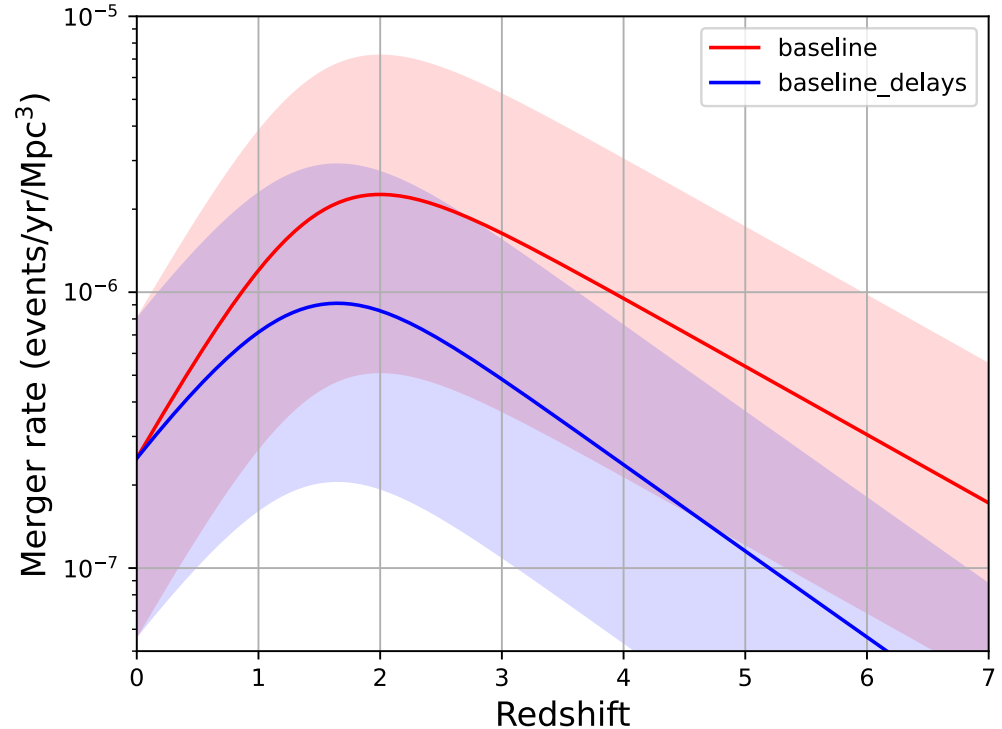
18  $\rightarrow$  9 BNS parameters: non-eccentric, spinless, symmetric

Parameters	BNS
$m$	Galactic BNS mass distribution ( <a href="#">Farrow et al. 2019</a> )
$\Lambda$	Calculated based on $\mathcal{M}$ and the EOS, $\Lambda = a + b\mathcal{M}_{\text{chirp}}^\alpha$
$z$	Merger rate model <i>baseline_delays</i> ( <a href="#">Lehoucq et al. 2023</a> )
$\cos i$ $\cos \delta$	Uniform in $[-1, 1]$
$\alpha, \psi, \Phi_c$	Uniform in $[0, 2\pi]$
$t_c$	0

# BNS population modelling



*N.Farrow et al. 2019*



*L.Lehoucq et al. 2023*

We take  $T = 1$  year of observation  $\rightarrow N_{\text{merger}} \sim 3.8e5$

# Calculation of the background

**Background definition:**

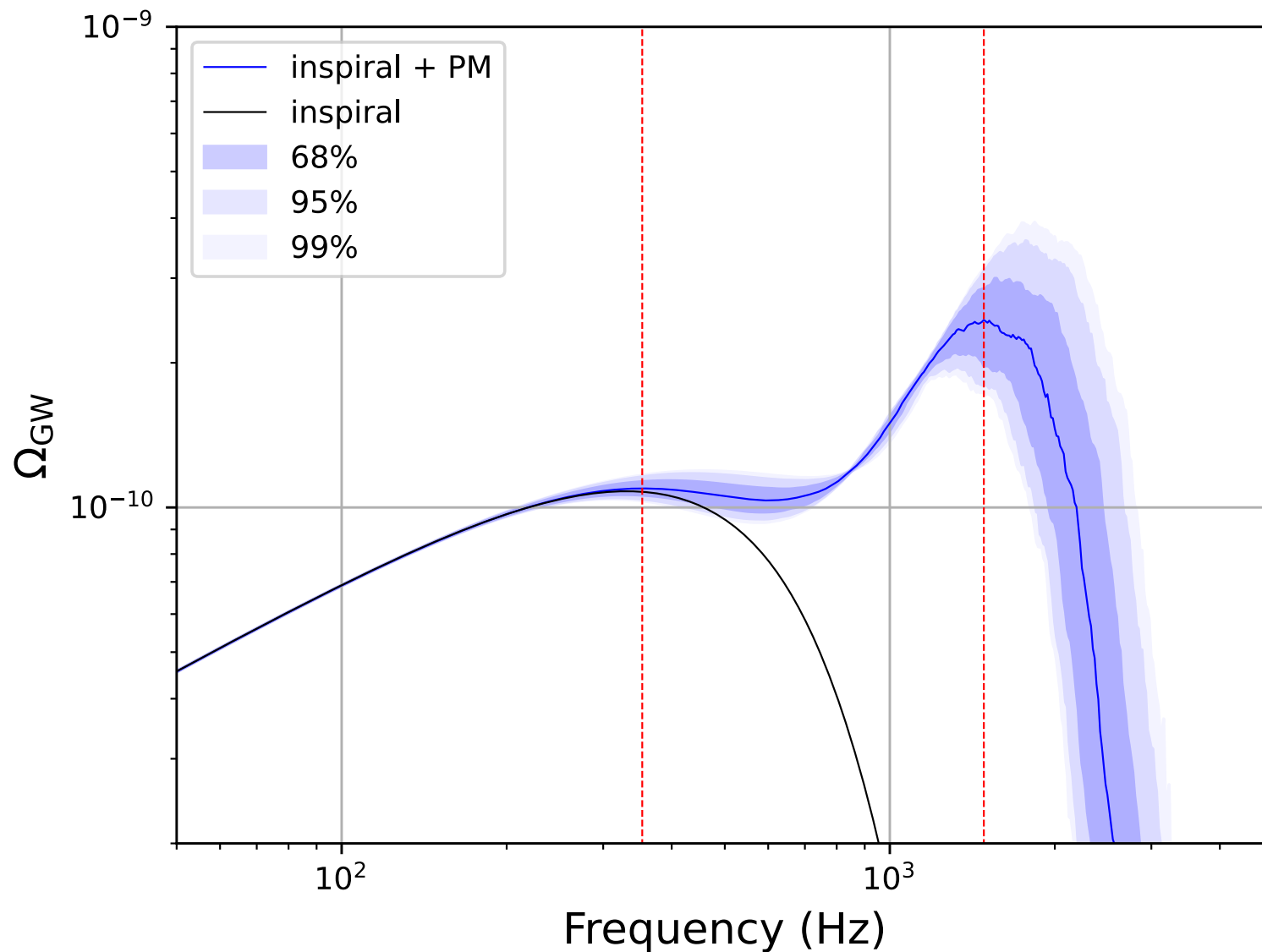
$$\Omega_{\text{GW}} = \frac{1}{\rho_c} \frac{d\rho_{\text{GW}}}{d \ln f} = \frac{f}{\rho_c c} F(f) \quad \text{with} \quad \rho_c = 3H_0/8\pi G$$

**Total GW flux:**

$$F_{\text{tot}}(f) = \frac{\pi c^3}{2G} \frac{f^2}{T} \sum_{i=1}^N \left[ |\tilde{h}_i^+(f)|^2 + |\tilde{h}_i^\times(f)|^2 \right]$$

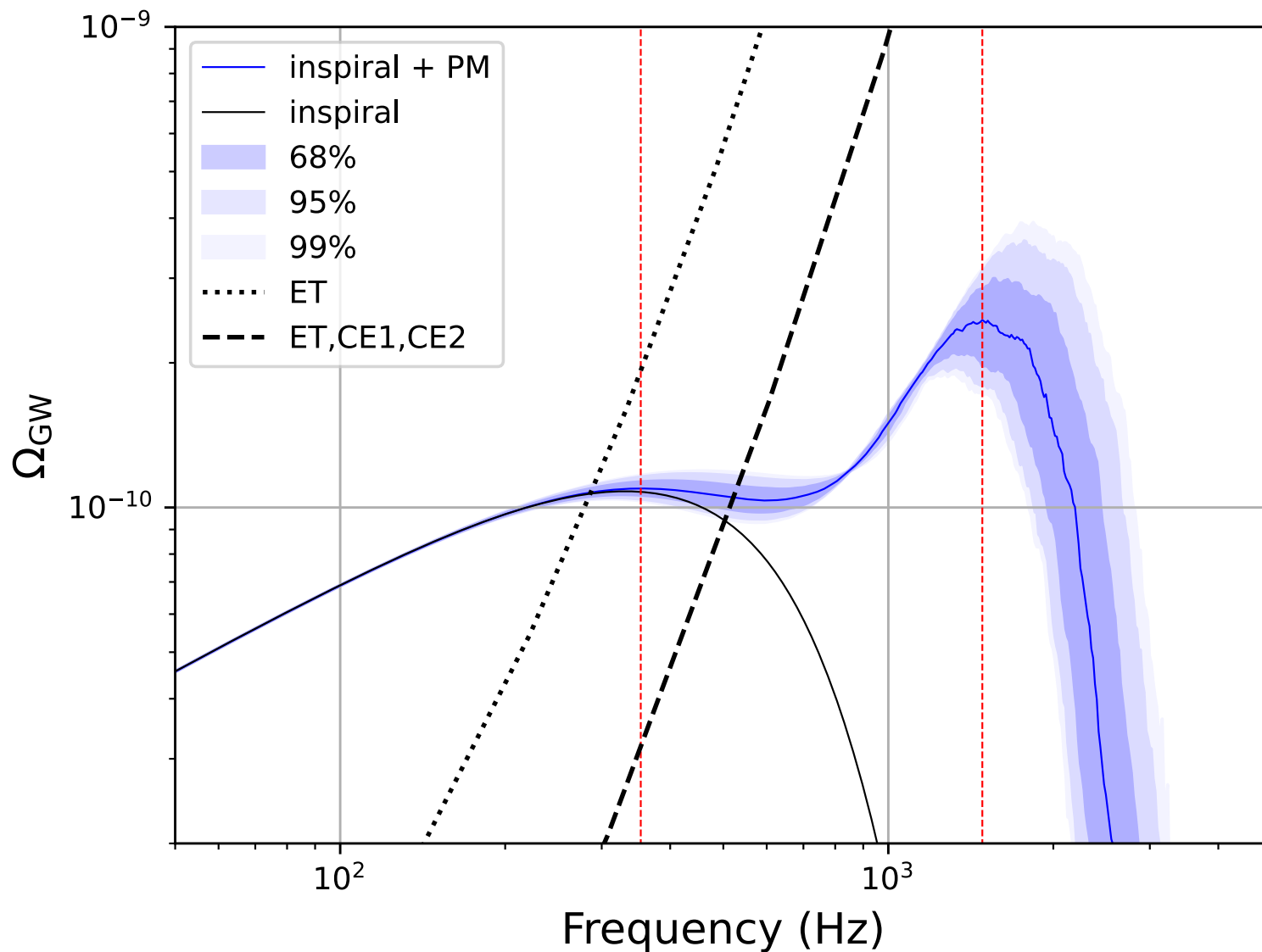
—> Sources are into 2 categories: resolved and **unresolved** (thus forming the background) based on a  $\text{SNR}_{\text{thr}}$ , usually taken to 12. Detectability using GWFish (*Dupletsa et al. 2023*).

# Results (preliminary)



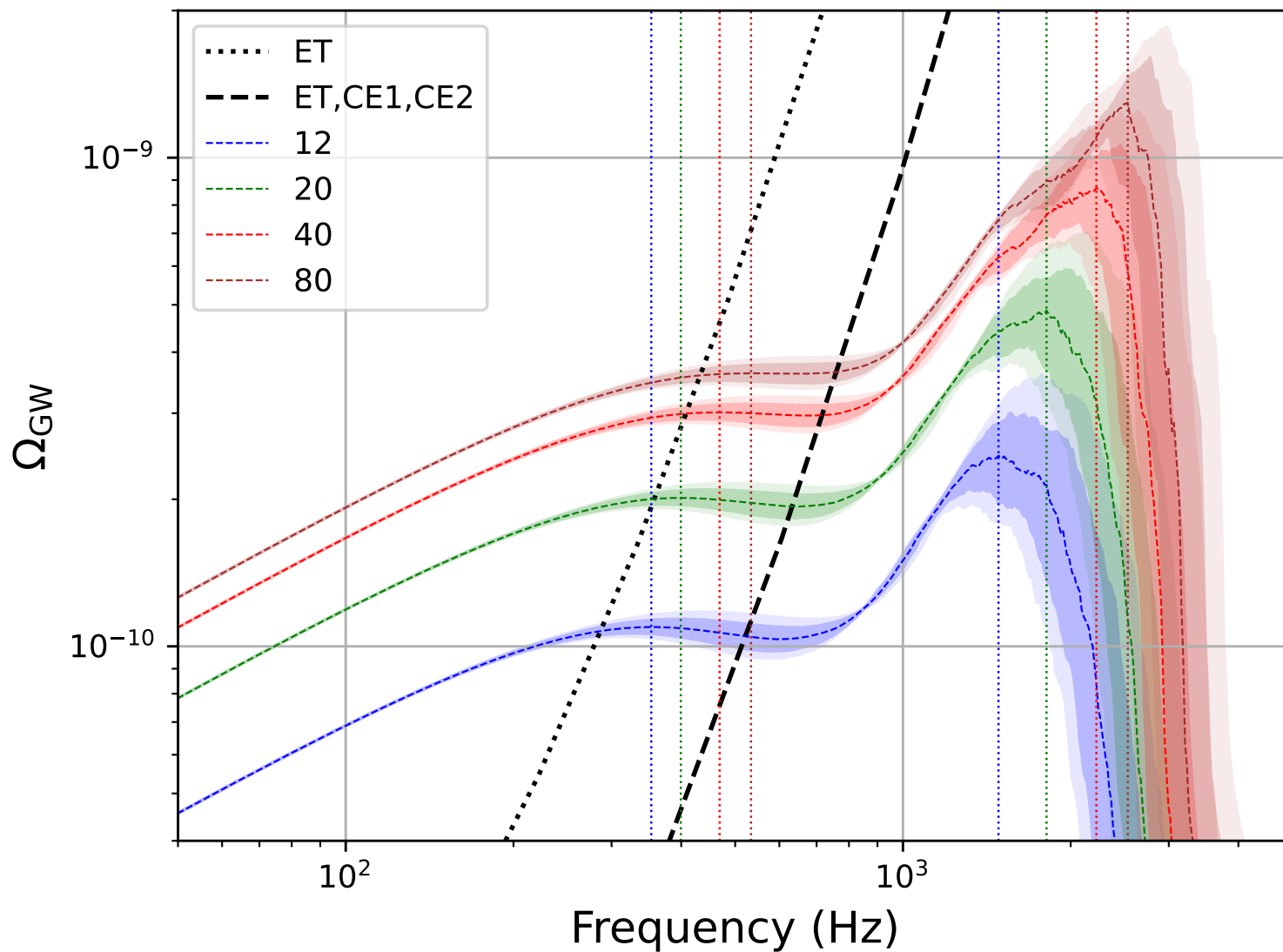
*L.Lehoucq, I.Dvorkin and L.Rezzolla in prep.*

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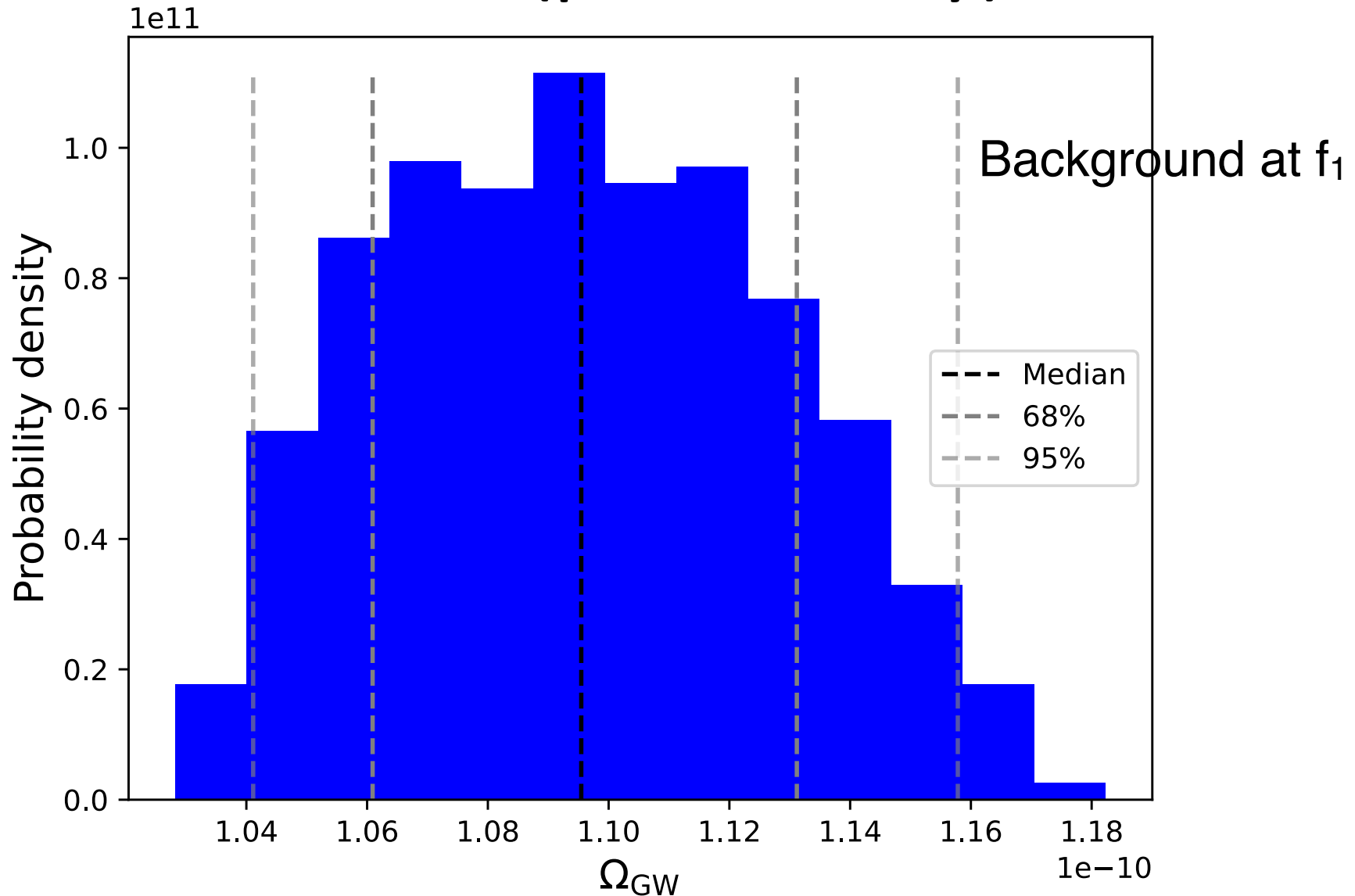
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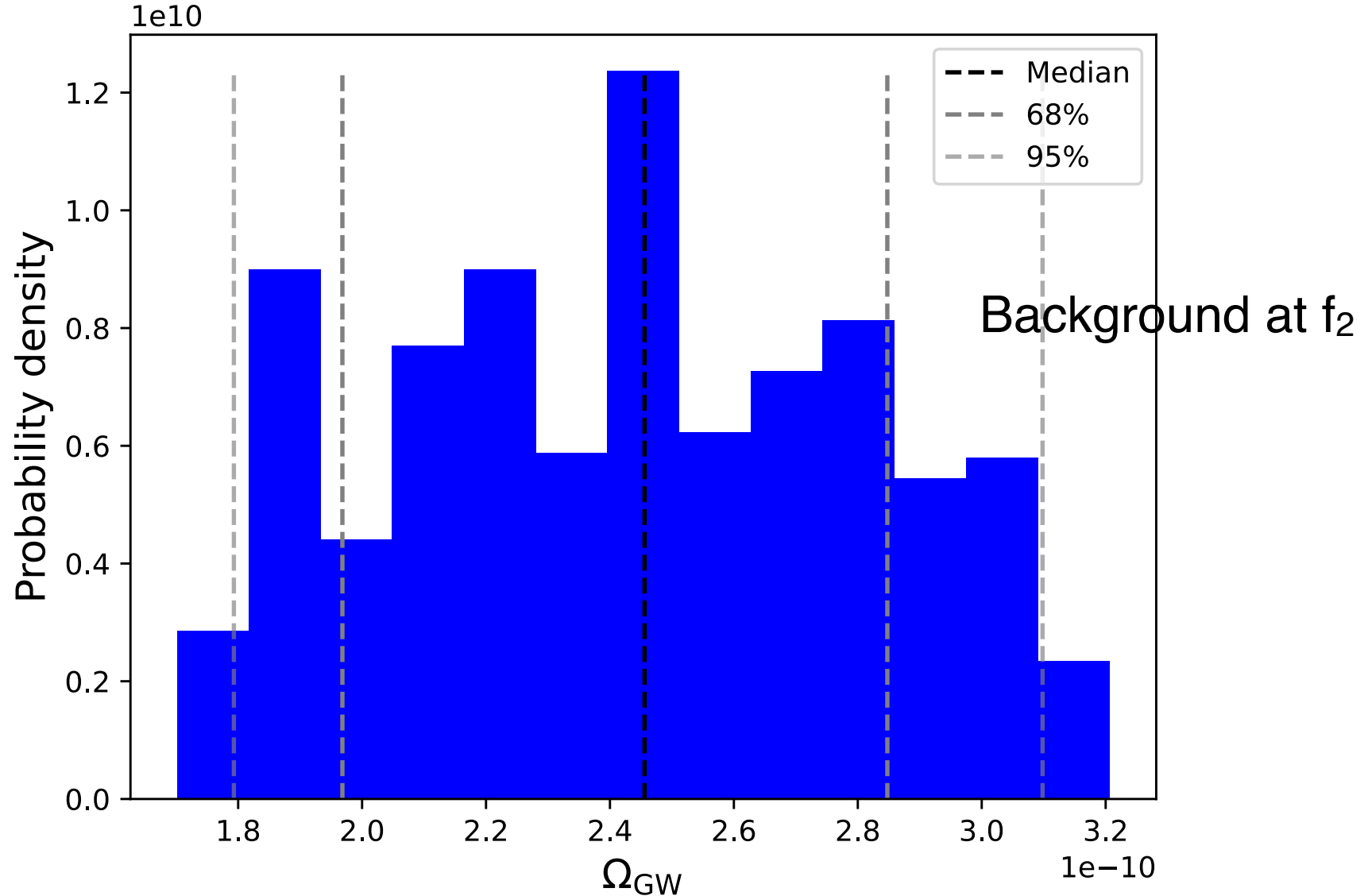


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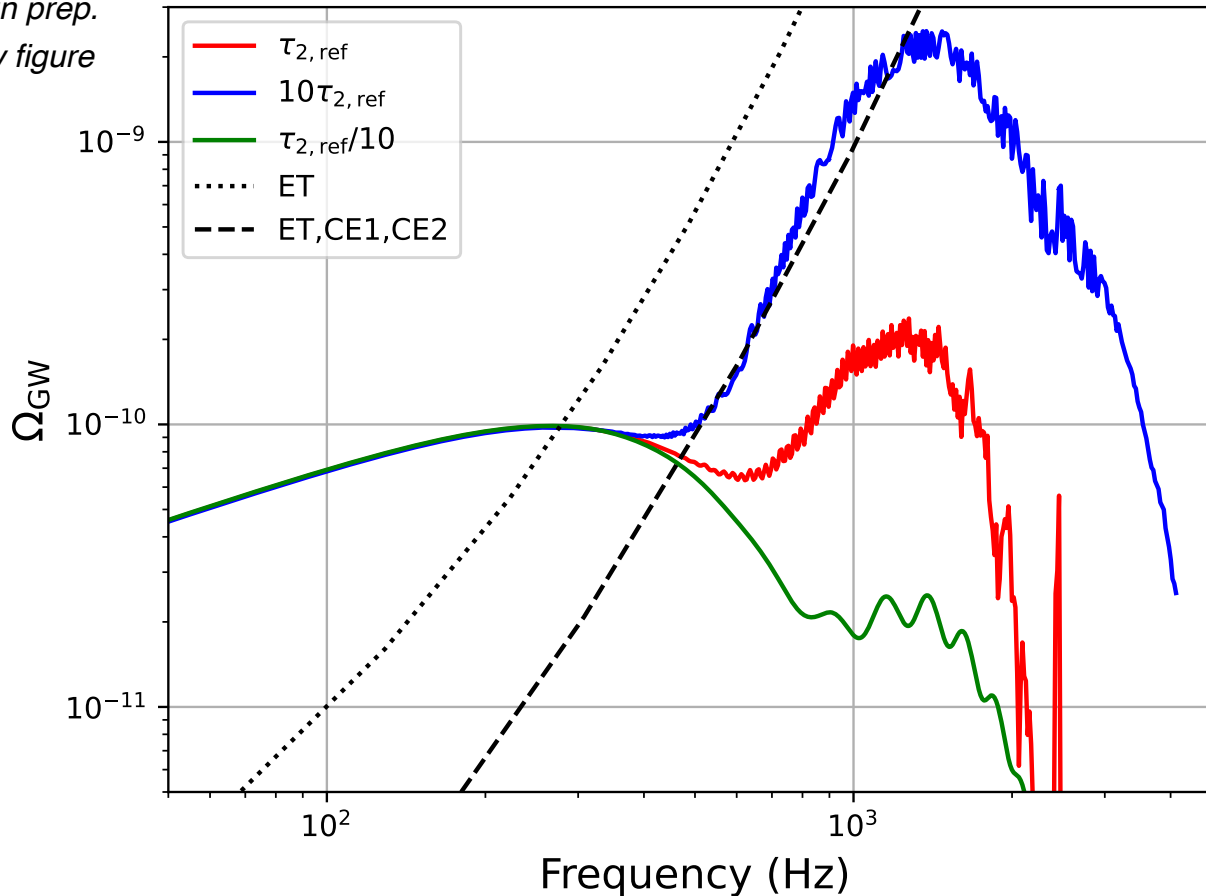
*L. Lehoucq, I. Dvorkin and L. Rezzolla in prep.*

# Results (preliminary)

Lifetimes  $\tau_1$  and  $\tau_2$  are not well constrained, numerical relativity suggests:

$\tau_{1,\text{ref}} \sim \text{few ms}$  and  $\tau_{2,\text{ref}} \sim 20 \text{ ms}$ .

*L. Lehoucq, I. Dvorkin  
and L. Rezzolla in prep.  
Very preliminary figure*



In this example, we could set constraints up to  $10 \tau_{2,\text{ref}} \sim 200 \text{ ms}$

# Conclusions

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# Conclusions

- Whatever the EOS, there is quite some power in the background at high frequencies ( $>1\text{kHz}$ ) due only to the post-merger.
- The amplitudes of the post-merger peaks are proportional to the lifetimes of the proper modes of the HMNS.
- Unfortunately, these lifetimes are not well constrained, but 3G detectors could set interesting upper limits on them and even potentially detect the lowest frequency modes.