



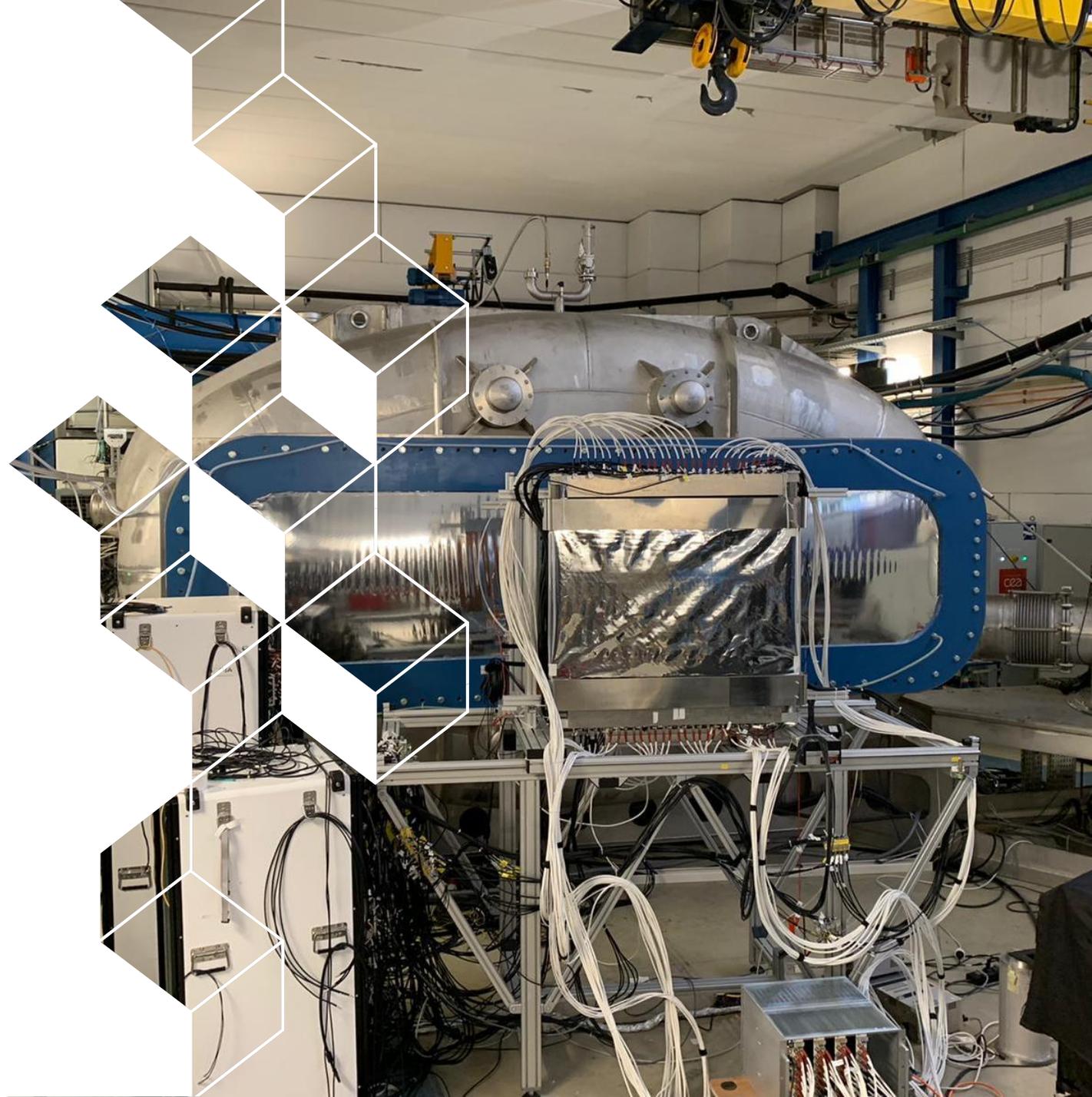
# Fission yields measurements in inverse kinematics at relativistic energies

SOFIA : Studies On Fission with GLAD

PhyNuBE 3 – Fission and Astrophysics Workshop

October 2024 – CNRS center of Oleron

A. Chatillon (CEA, DAM, DIF) for the R3B/SOFIA collaboration



- 
- 1/ Fission yields: influence of the nuclear structure in the yields**
  - 2/ Inverse kinematics at relativistic energy**
  - 3/ The SOFIA experiment**
  - 4/ Selection of results with SOFIA**



# 1 ■ Fission yields

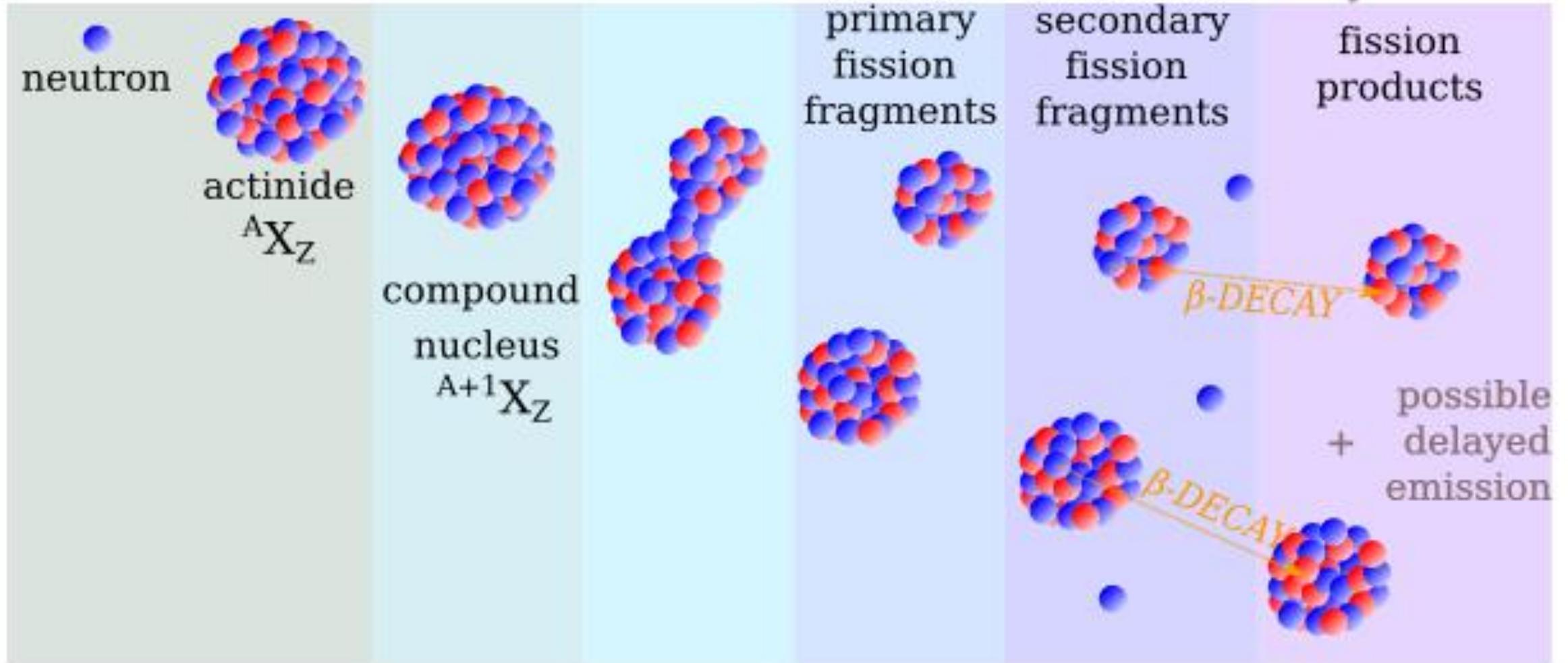
Basic definition

Nuclear structure effects in fission yields

Introduction to fission modes

# Fission yields

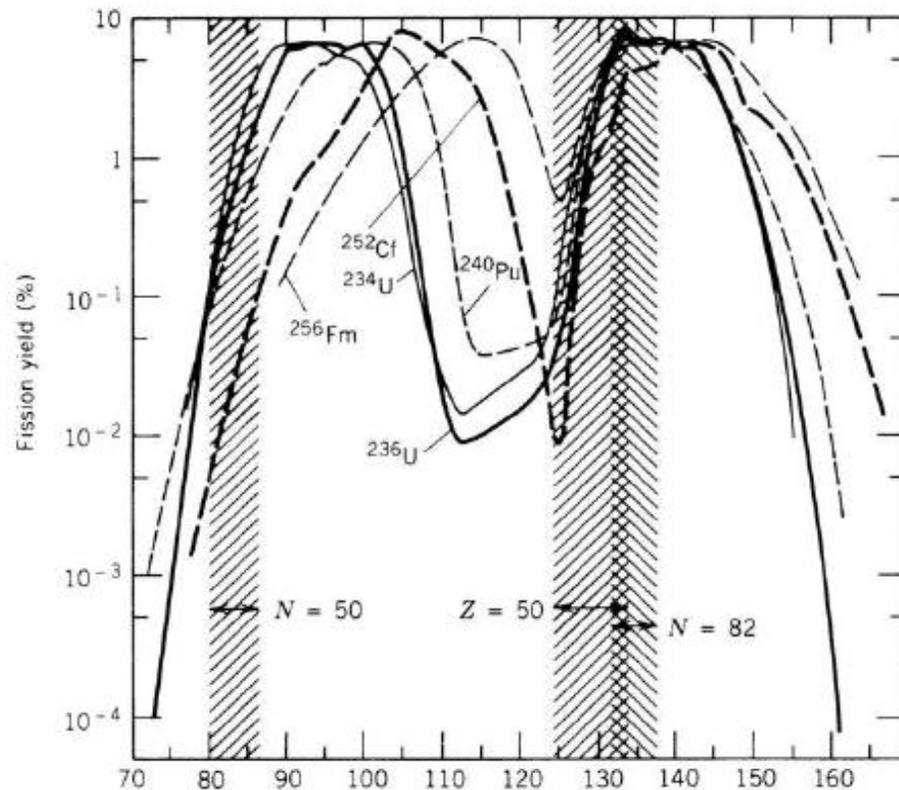
Fraction of a nucleus to be produced by fission



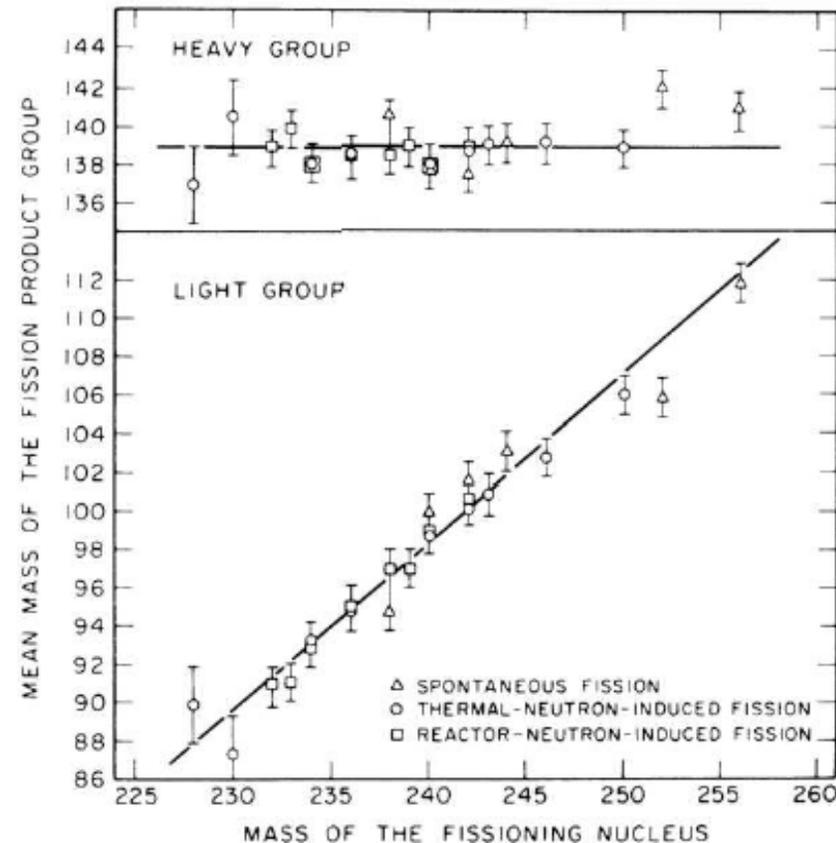
# Fission yields

Some signatures of the underlying nuclear structure effects in the fission yields

- Fission is asymmetric: one of the first observation of shell effects of shell effects
- Heavy fission fragments mean mass stable for different actinides



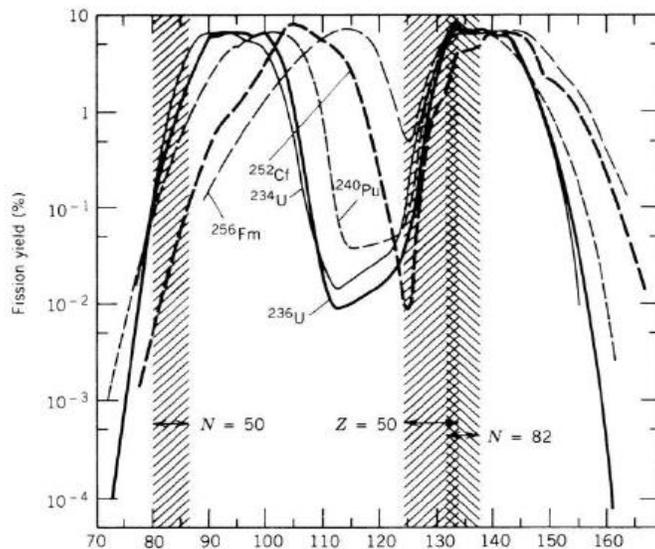
FLYNN *et al.*, PRC 5 (1972) 1725



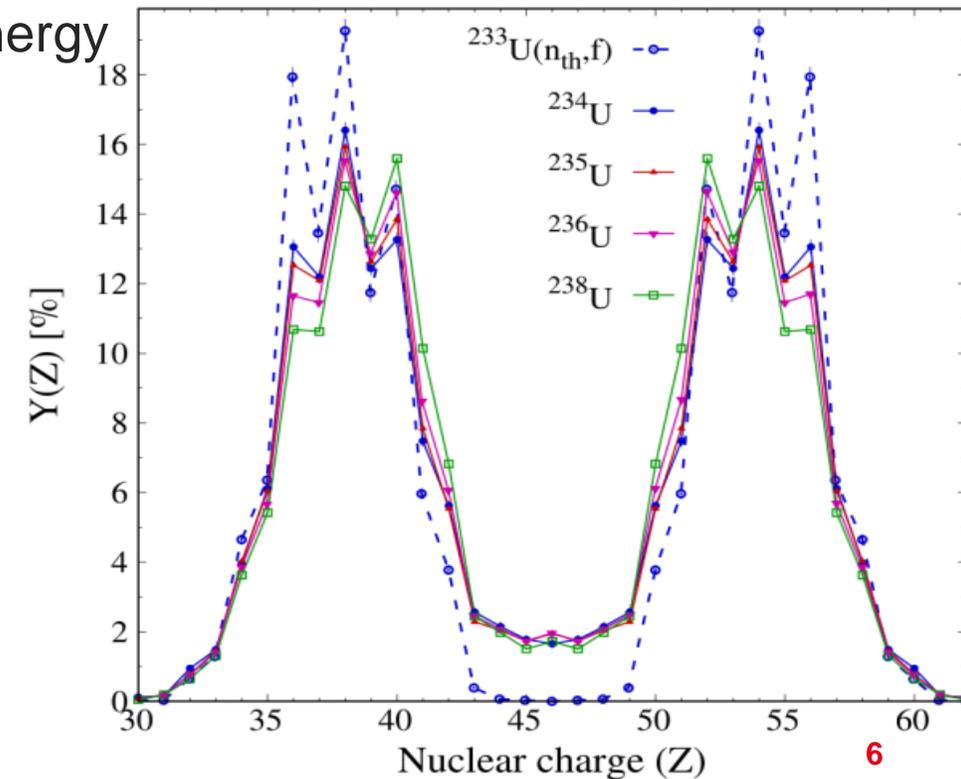
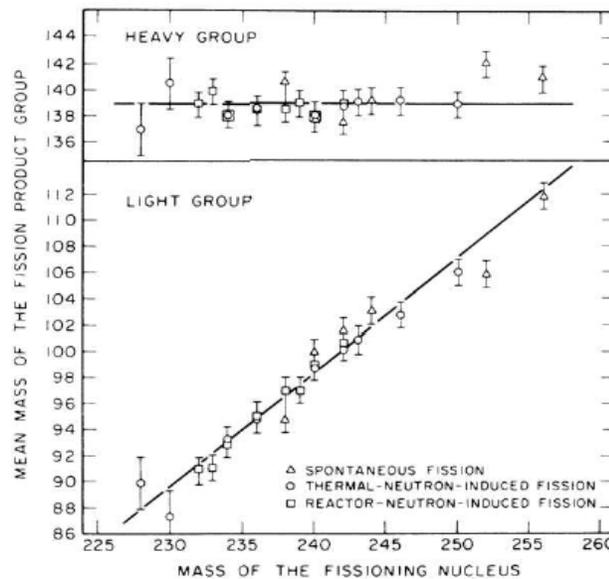
# Fission yields

## Some signatures of the underlying nuclear structure effects in the fission yields

- Fission is asymmetric: one of the first observation while studying the heavy actinides
- Heavy fission fragments mean mass stable for different actinides
- Proton even-odd staggering in even-Z fissioning system due to pairing
- Proton Evolution of the fission yields with the excitation energy



FLYNN *et al.*, PRC 5 (1972) 1725



# Fission modes around the U actinides

3 fission modes: 2 asymmetric modes and 1 symmetric mode

U. Brosa *et al.*, PRC 38 (1988) 1944

- One path on PES per mode
  - Valley from different underlying shell effects
  - Path reach the scission line at different  $(Q_{20}, Q_{30})$
  - Each mode has different configuration at scission

## ■ STANDARD 1 (ST1)

almost spherical FF<sub>H</sub>  
<sup>132</sup>Sn spherical shells  
compact configuration  
high TKE, low  $\nu$

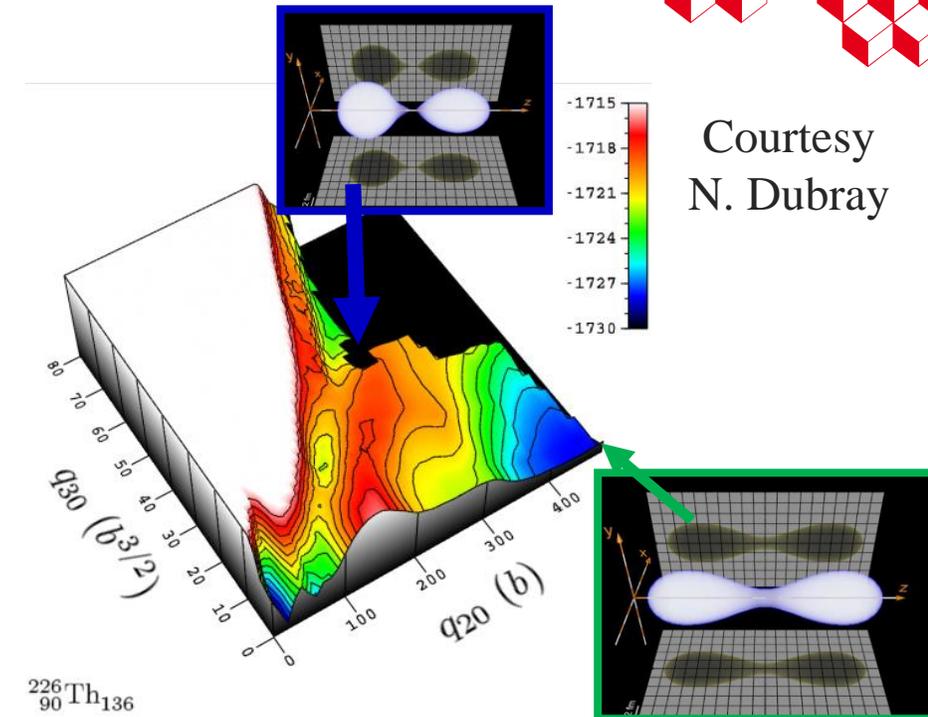
## ■ STANDARD 2 (ST2) main

deformed FF  
octupole shells Z=52, Z=56  
G. Scamps *et al.*, Nature 564 (2018) 382

## ■ SUPER-LONG (SL) with E\*

highly deformed FF  
shell effects washed-out  
deformed configuration  
low TKE, high  $\nu$

■ Importance of correlated data: yields, TKE, prompt neutrons, excitation energy, ...





# 2 ■ Fission studies in inverse kinematics at relativistic energies

Why ?

How to induce low energy fission at relativistic energies ?

Experimental method at GSI: double -  $\Delta E$  /  $B\rho$  / ToF

# Limitation of the direct kinematics

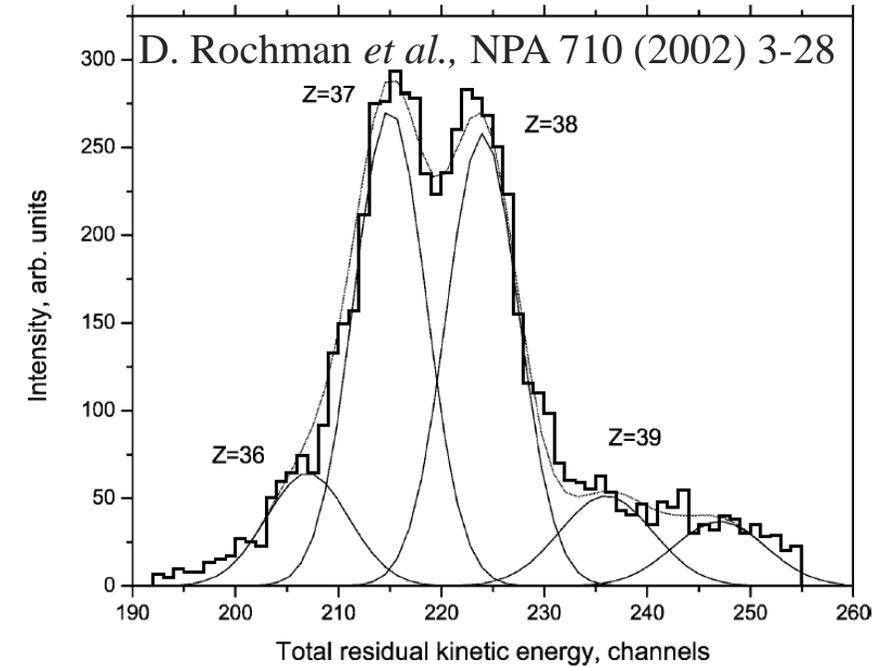
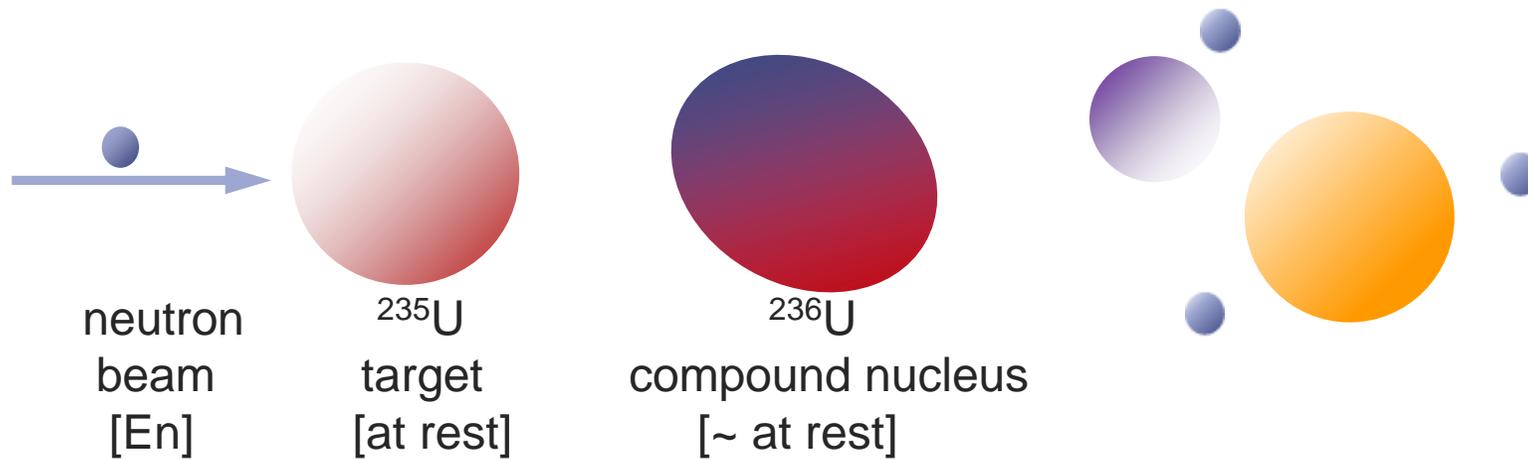
- Fission in direct kinematics:



- A neutron-, proton- or light charged particle beam impinges on an actinide target
- Production of an excited compound nucleus which may de-excite by fission
- Fission fragments are emitted with low energy in the lab frame

# Limitation of the direct kinematics

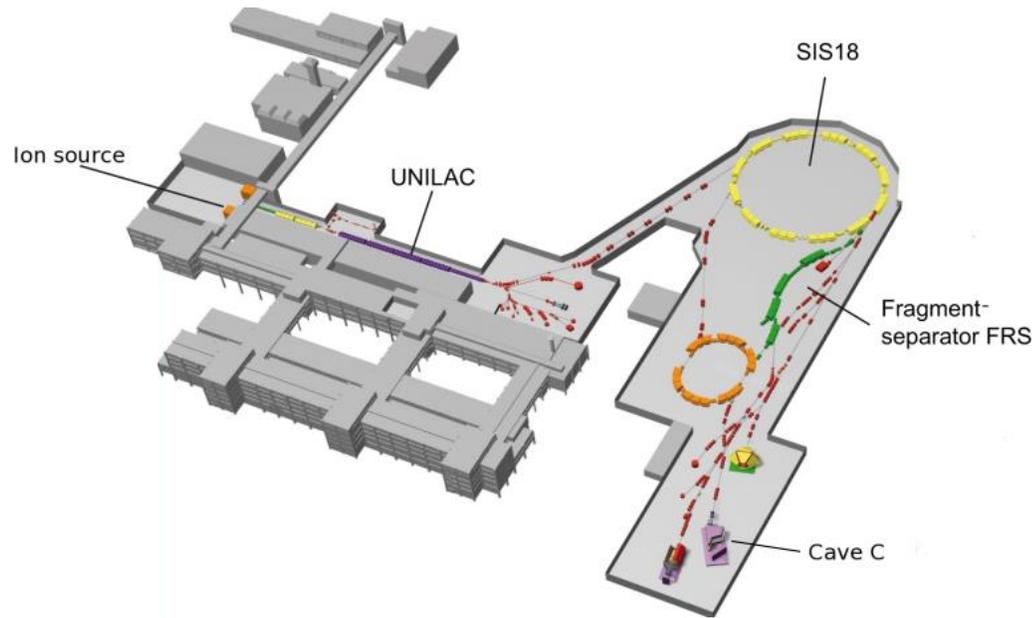
- Fission in direct kinematics:



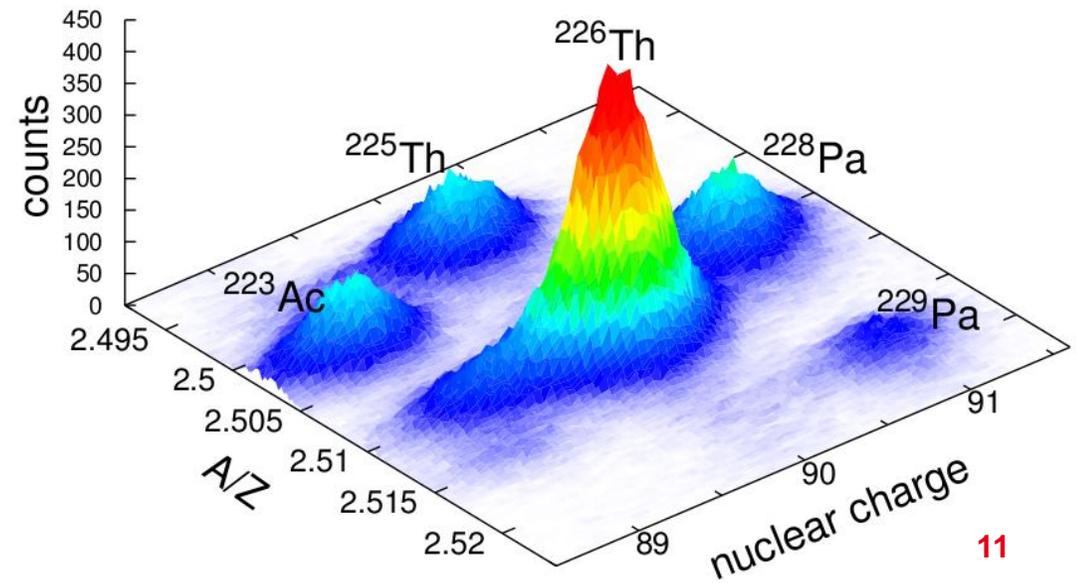
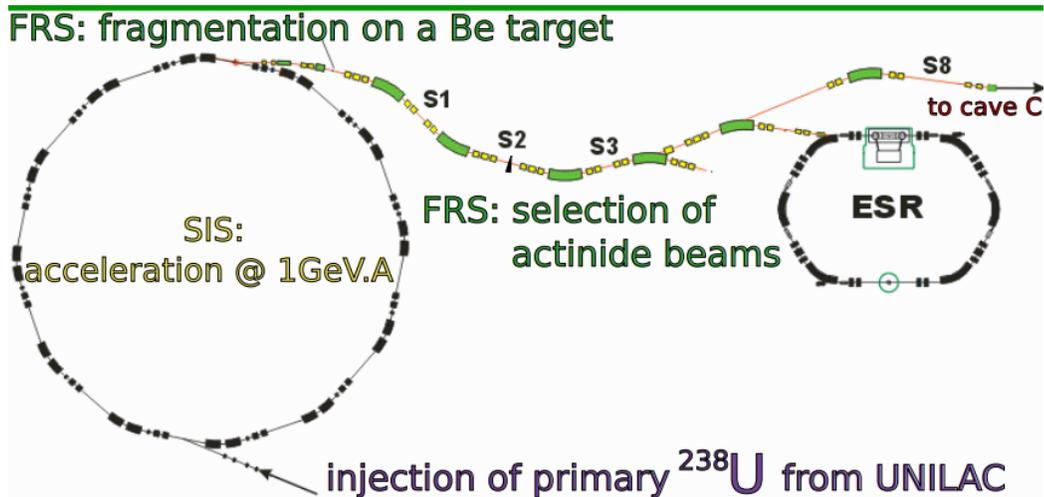
- Nuclear charge measurement limited to  $Z \leq 40$  due to ionic charge states
- Targets limited to long-lived actinides
- Very low efficiency due to  $4\pi$  emission

# Inverse kinematics at relativistic energies (I)

GSI/FRS facility to produce radioactive relativistic beam



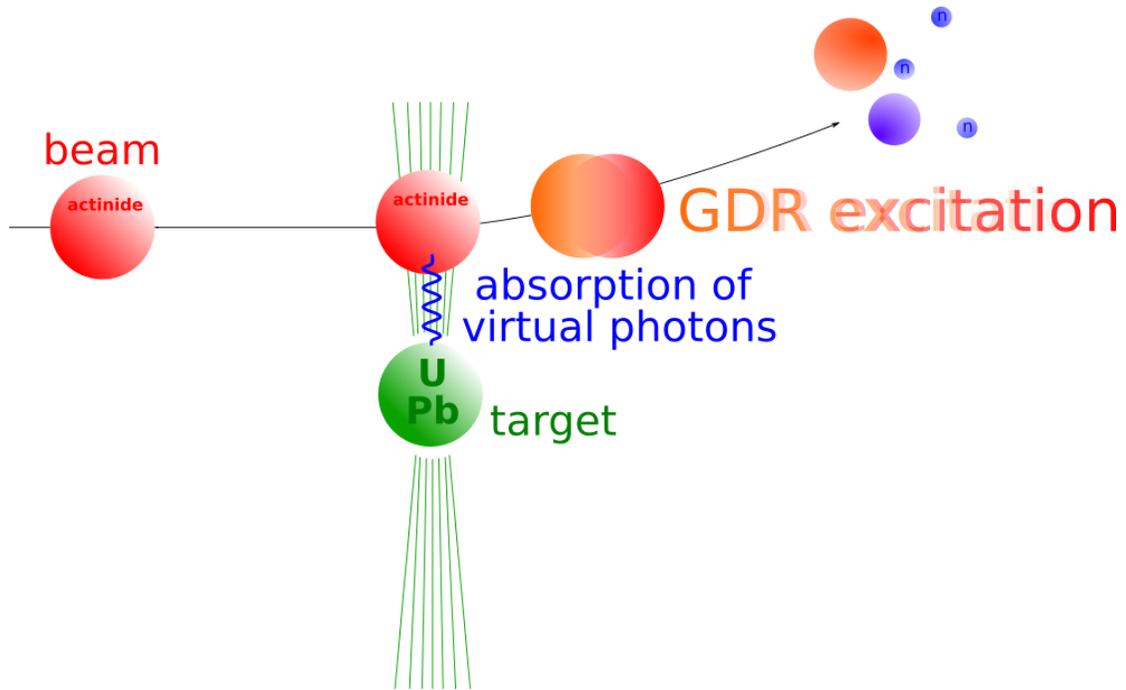
- @GSI:  $^{238}\text{U}$  beam at 1 A.GeV
- @FRS: Fragmentation of  $^{238}\text{U}$  on a Be target and production of cocktail beams with a selection in  $(B\rho, \Delta E)$  around  $(A/Z, Z)$  and sent to cave at  $\sim 750$  A.MeV



# Inverse kinematics at relativistic energies (II)

How to induce low energy fission at relativistic energies ?

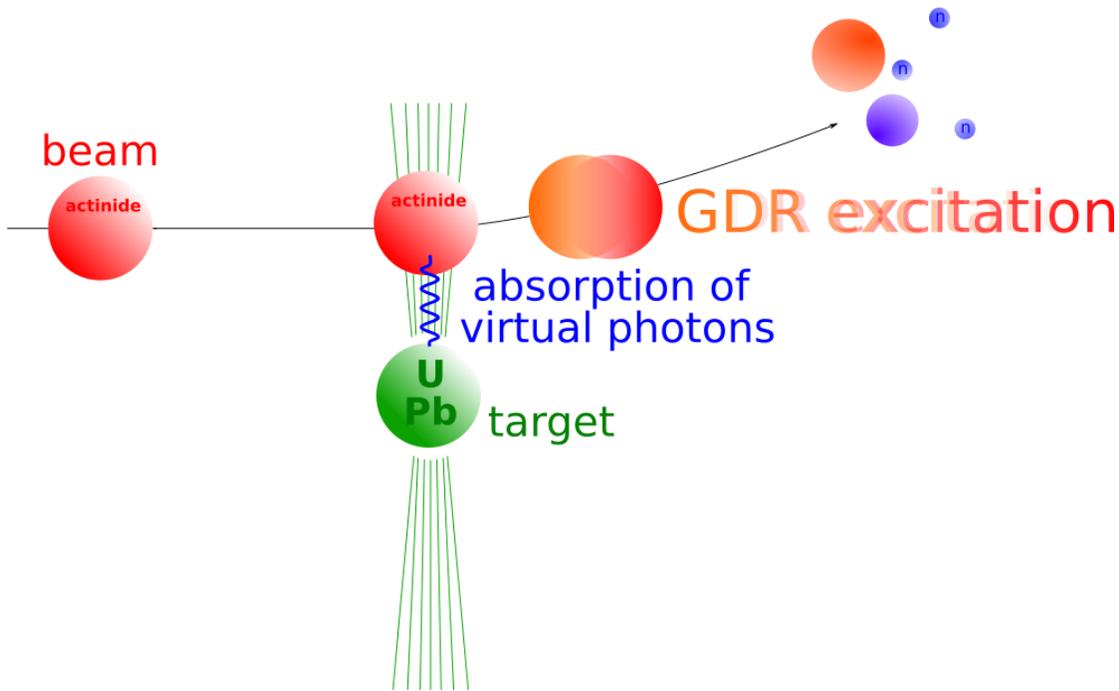
- Fission is induced by coulomb excitation



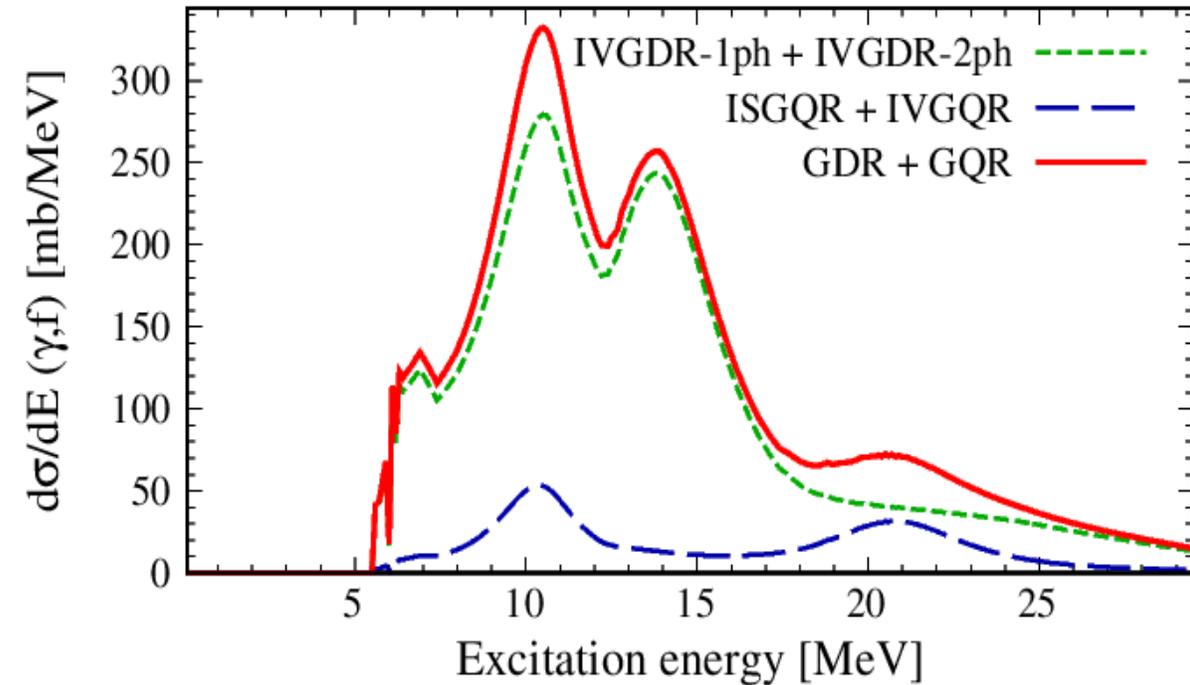
# Inverse kinematics at relativistic energies (II)

How to induce low energy fission at relativistic energies ?

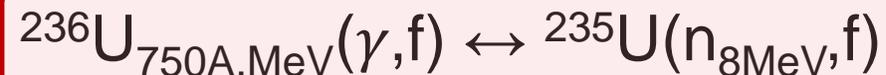
- Fission is induced by coulomb excitation



- Excitation energy:  $\langle E^* \rangle \sim 14 \text{ MeV}$



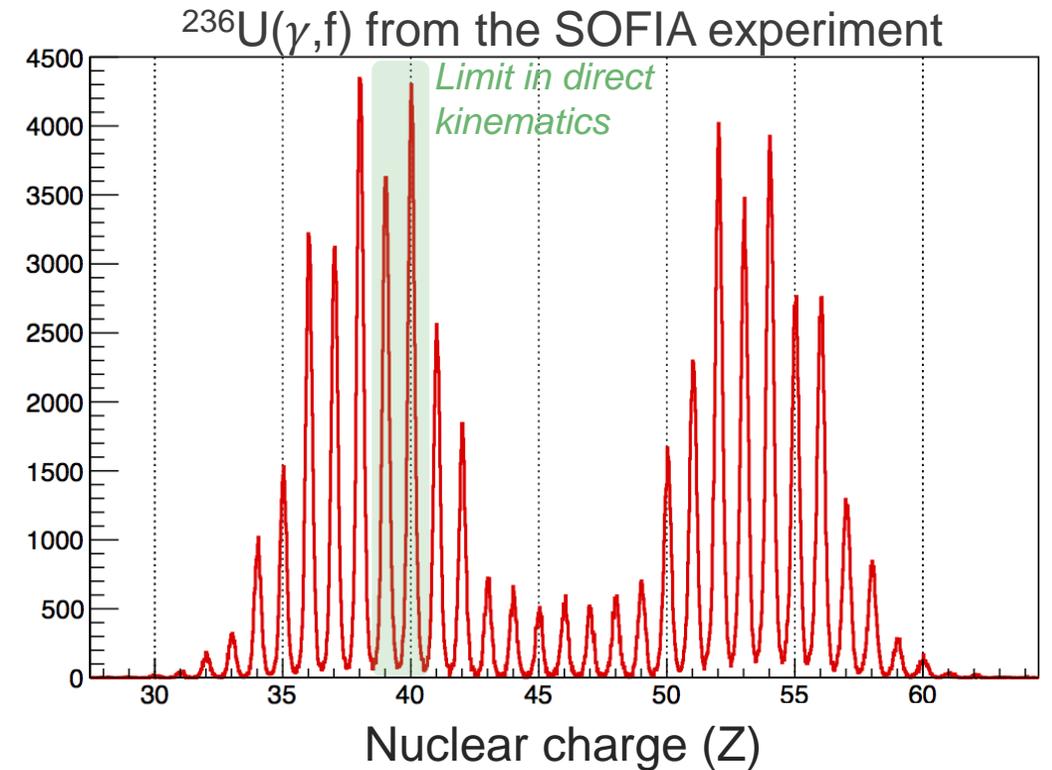
- Electromagnetic induced fission = surrogate reaction for 8 MeV neutron induced fission



# Inverse kinematics at relativistic energies (III)

## Advantages compare to direct kinematics

- ✓ Large cross section
  - Example for  $^{236}\text{U}(\gamma, f)$   $\sigma = 2 \text{ barns} \text{!!!!}$
  - Accurate and large scale measurements
- ✓ Relativistic ions are fully stripped:  $Q=Z$ 
  - Q measurement from energy loss:  $\Delta E \propto Q^2$
  - More accurate measurement of Z
  - **SOFIA resolution in charge :**  
 **$\Delta Z = 0.31 \text{ to } 0.34 \text{ charge unit FWHM}$**

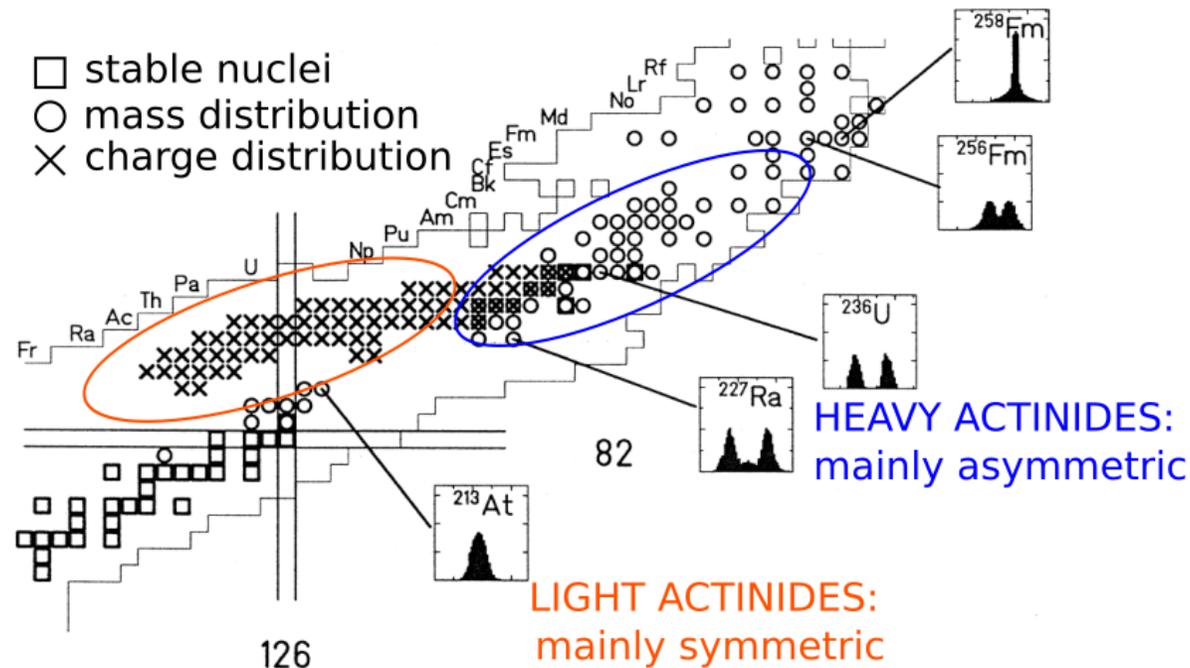


- ✓ Study of fission nuclei which can not be produced in direct kinematics

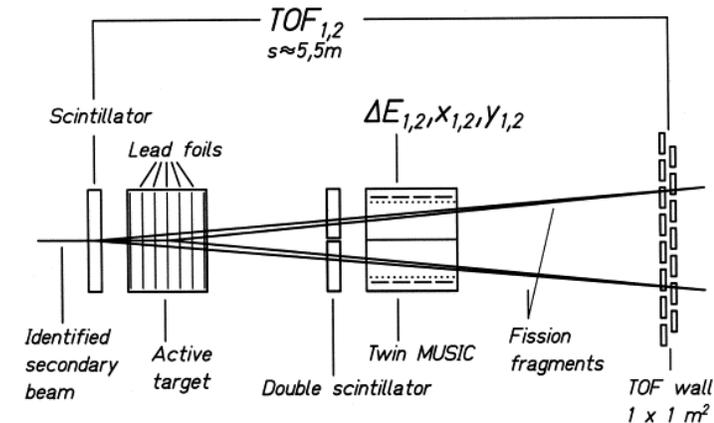
# Pioneer experiment at GSI / FRS in inverse kinematics

K.-H. Schmidt *et al.*, Nucl. Phys. A 665 (2000) 221: measurement of the charge only

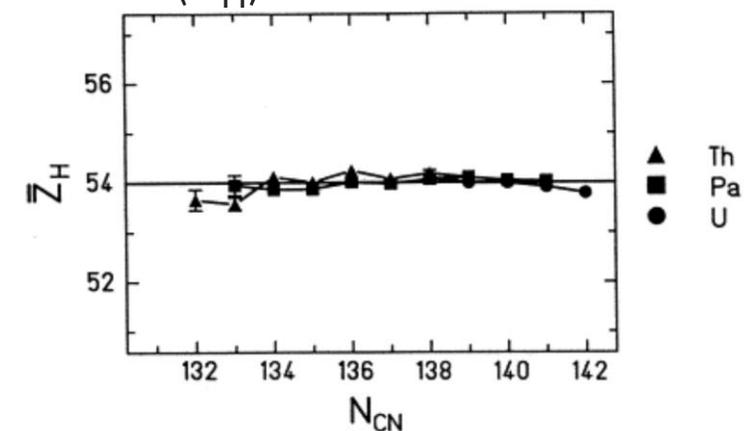
- Y(Z) measured for Rn to U fissioning isotopes



- Experimental setup:  $\Delta E$  and ToF



- Important result:  $\langle Z_H \rangle = 54$





# 2 ■ The SOFIA experiment

A dedicated spectrometer for fission studies @ GSI

Experimental program

# SOFIA: (Z,A) identification

$\Delta E - B\rho - \text{ToF}$  method after prompt emission and before any  $\beta$ -decay

## ■ Nuclear charge Z

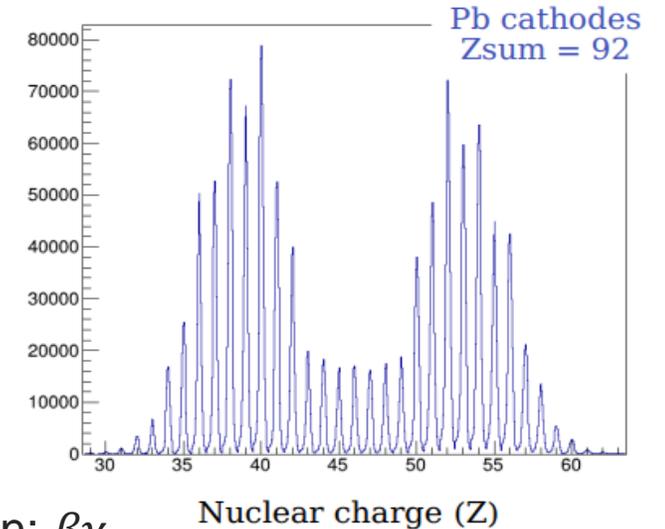
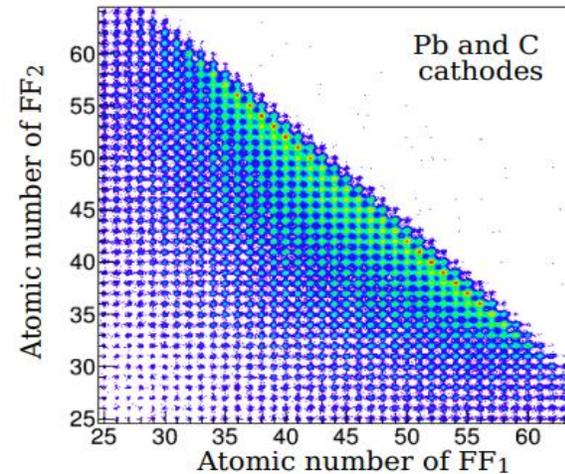
- Energy loss ( $\Delta E$ )  $\sim Q^2 = Z^2$
- Z is « easy » to obtain

## ■ Mass A

- Time-of-flight measurement (ToF) combined with flight path reconstruction:  $\beta\gamma$
- Tracking of the ions in a magnetic field ( $B\rho$ )
- $A/Q \sim B\rho / \beta\gamma$

## ■ Total prompt-neutron multiplicity $\nu_{\text{tot}}$

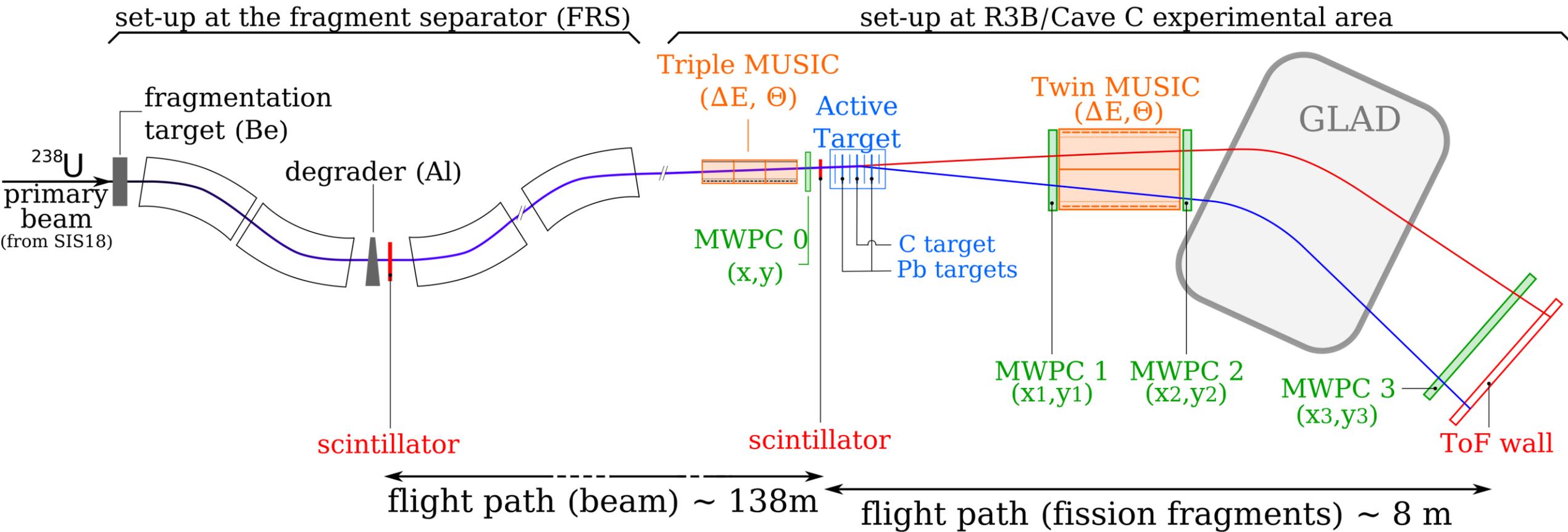
- Method at FRS for (Z,A) identification of beam
- Method at cave C for (Z,A) identification of both fission fragments in coincidence



**CHALLENGING RESOLUTION**  
 $\Delta x = 100$  to  $300 \mu\text{m}$   
 $\Delta \text{ToF} = 35 \text{ ps}$   
**FWHM**

# SOFIA spectrometer

3 types of detectors : **MUSIC** **MWPC** **scintillators**



# Identification of the fission fragments in $^{236}\text{U}(\gamma, f)$

## RESOLUTIONS [FWHM]:

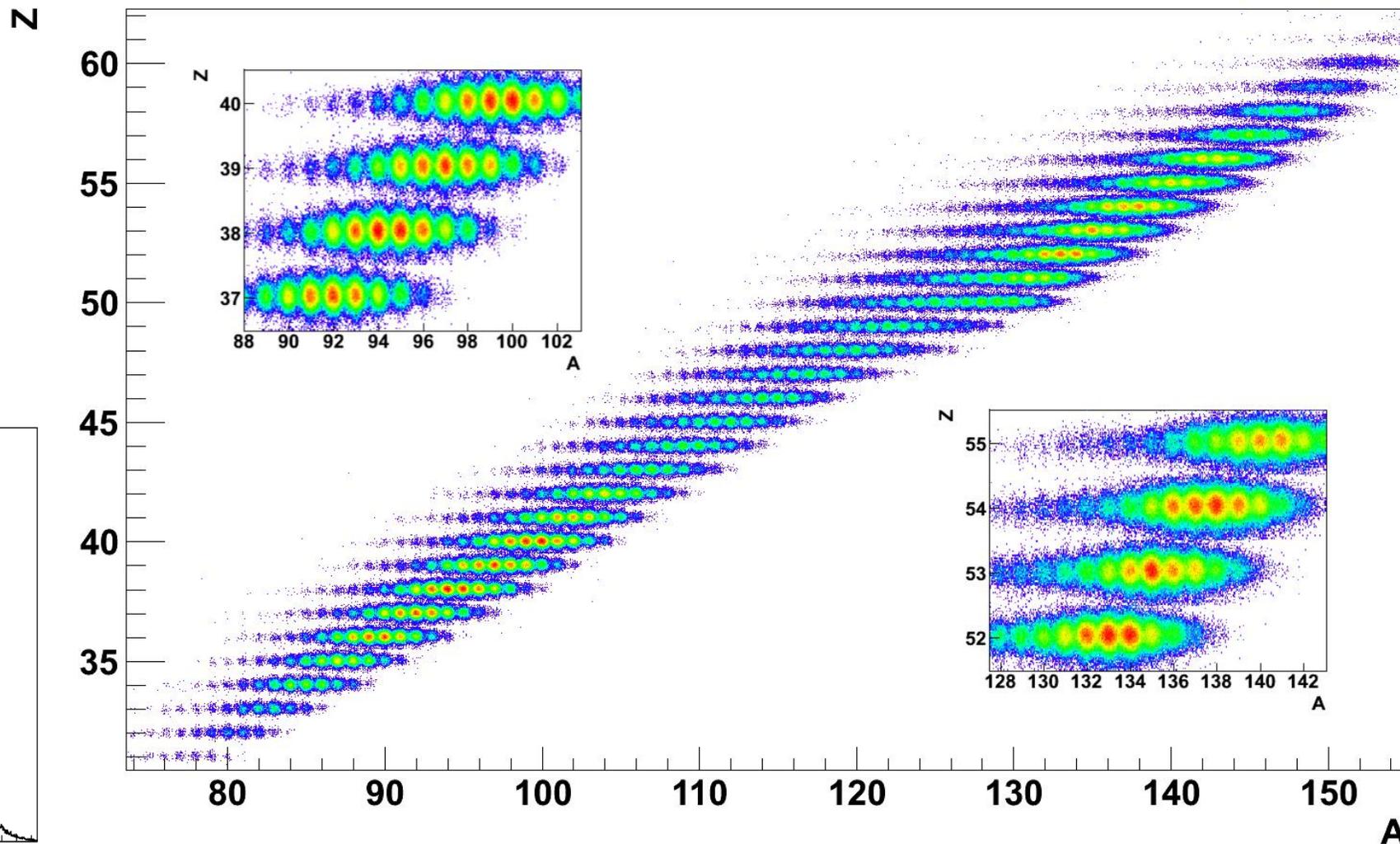
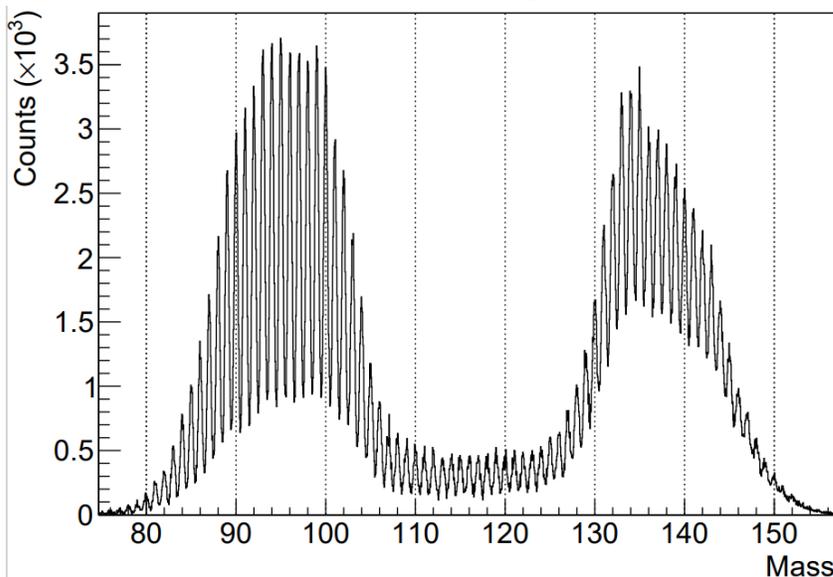
$\Delta Z = 0.31$  to  $0.34$  charge unit

$\Delta A = 0.55$  to  $0.80$  mass unit



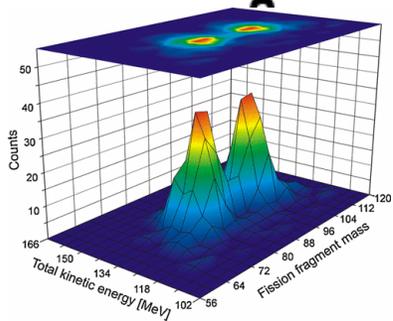
$\Delta x = 100$  to  $300 \mu\text{m}$

$\Delta\text{ToF} = 35 \text{ ps}$

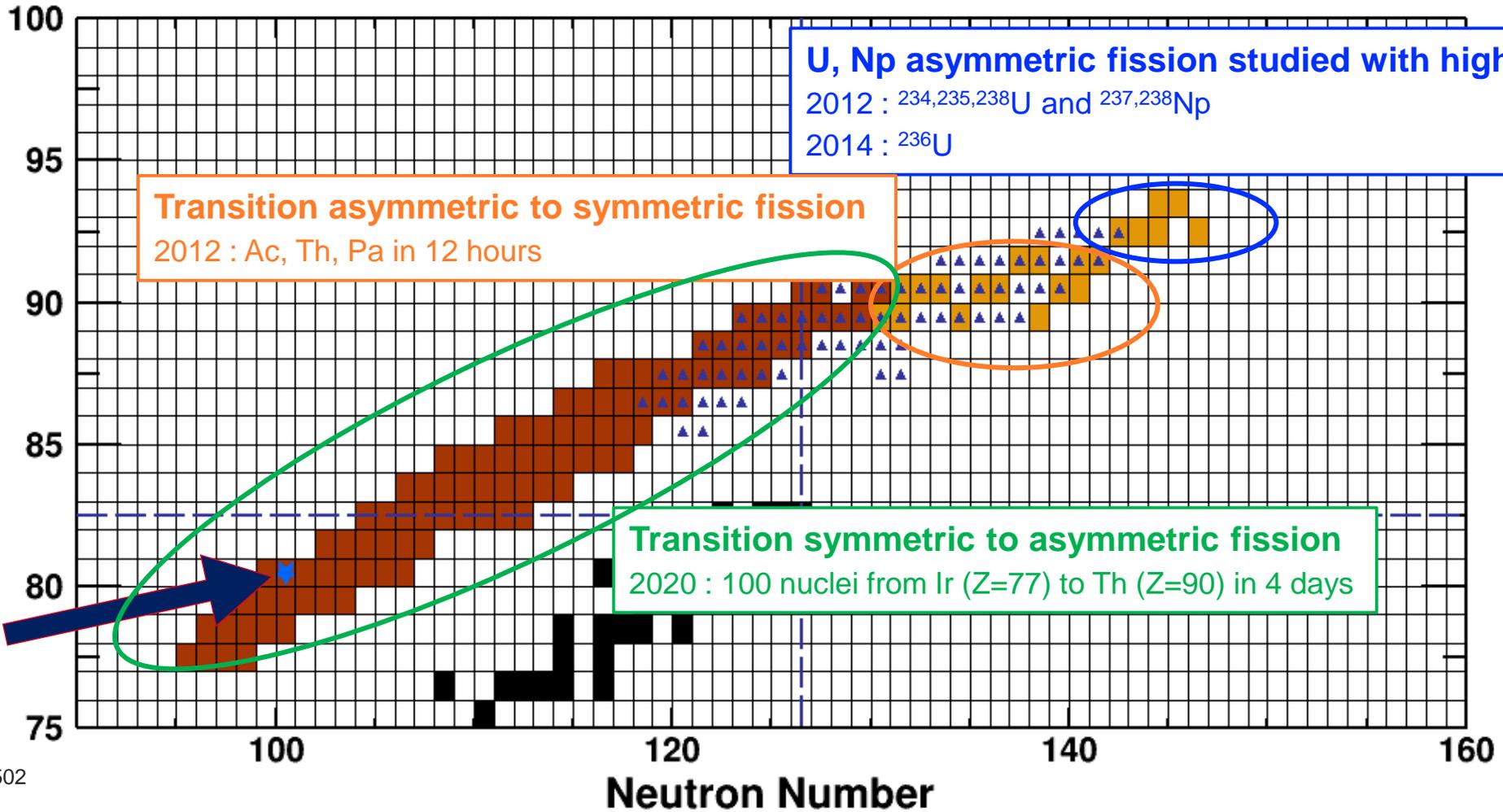


Analysis by L. Grente (CEA, DAM, DIF)

# SOFIA experiments



Proton Number



A. Andreyev, PRL 105 (2010) 252502



# 3 ■ Results

Accurate measurement: Isotopic yields and isobaric yields

TKE and  $\nu_{\text{tot}}$ : a probe of scission configuration

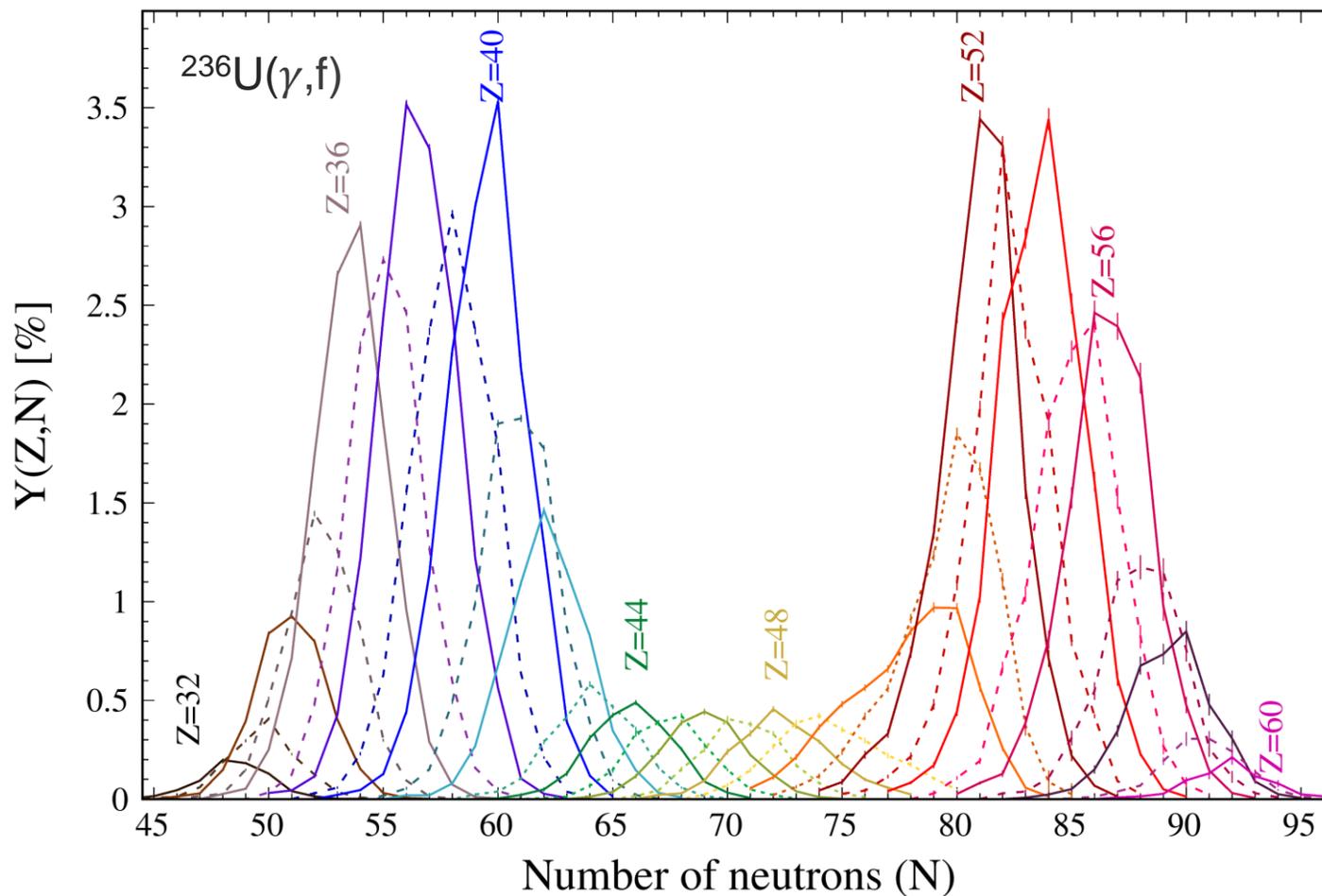
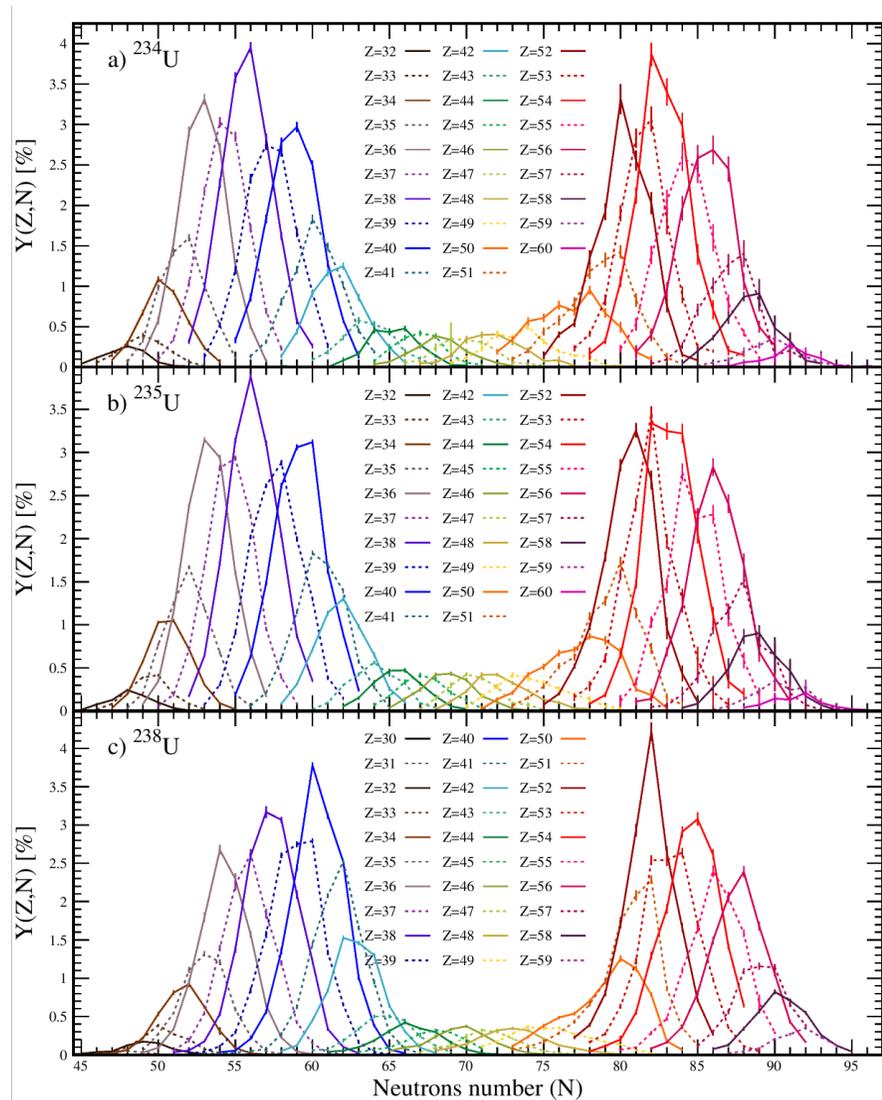
Signatures of energy sorting:  $\nu(A)$  and even-odd staggering

Large scale measurement: investigating new fission modes

# Isotopic yields along the uranium chain



E. Pellereau *et al.*, PRC 95 (2017) 054603  
 J. F. Martin *et al.*, PRC 104 (2021) 044602



$0.5\% \leq \sigma \leq 1.5\%$

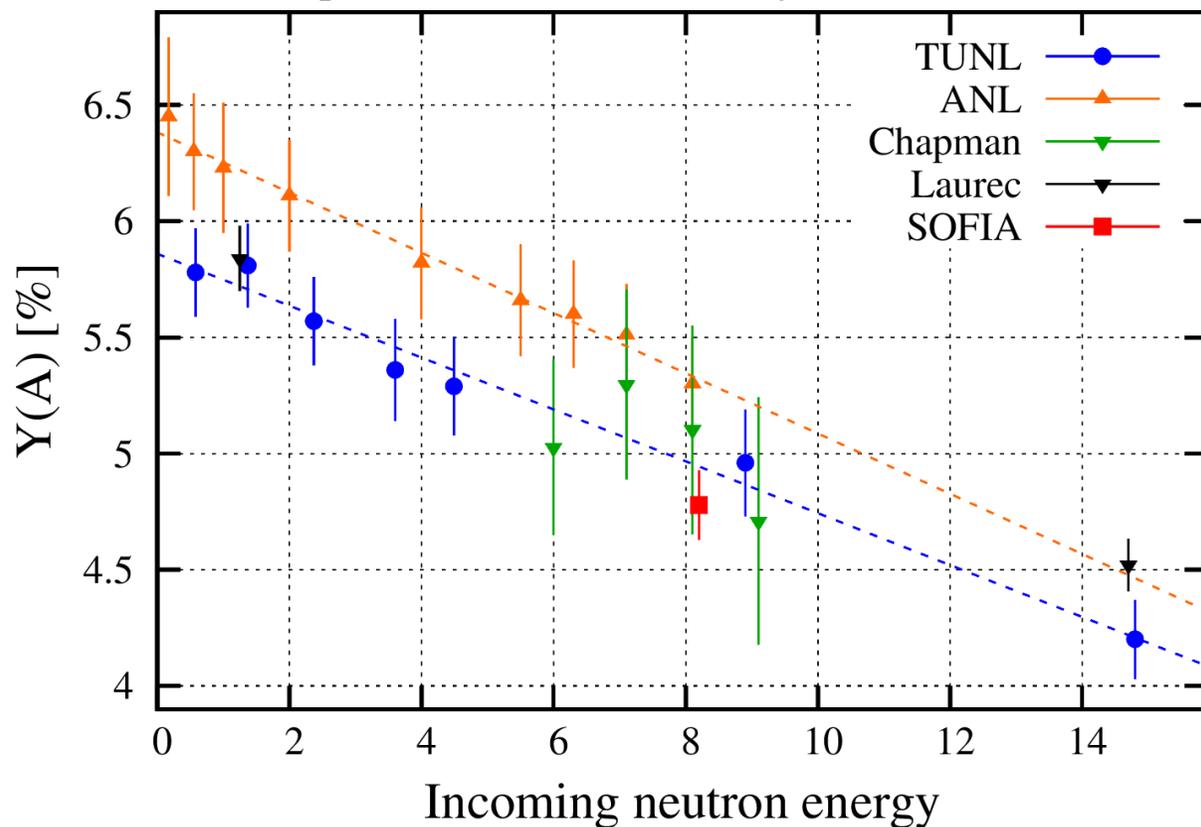
$1.3\% \leq \sigma \leq 3.5\%$



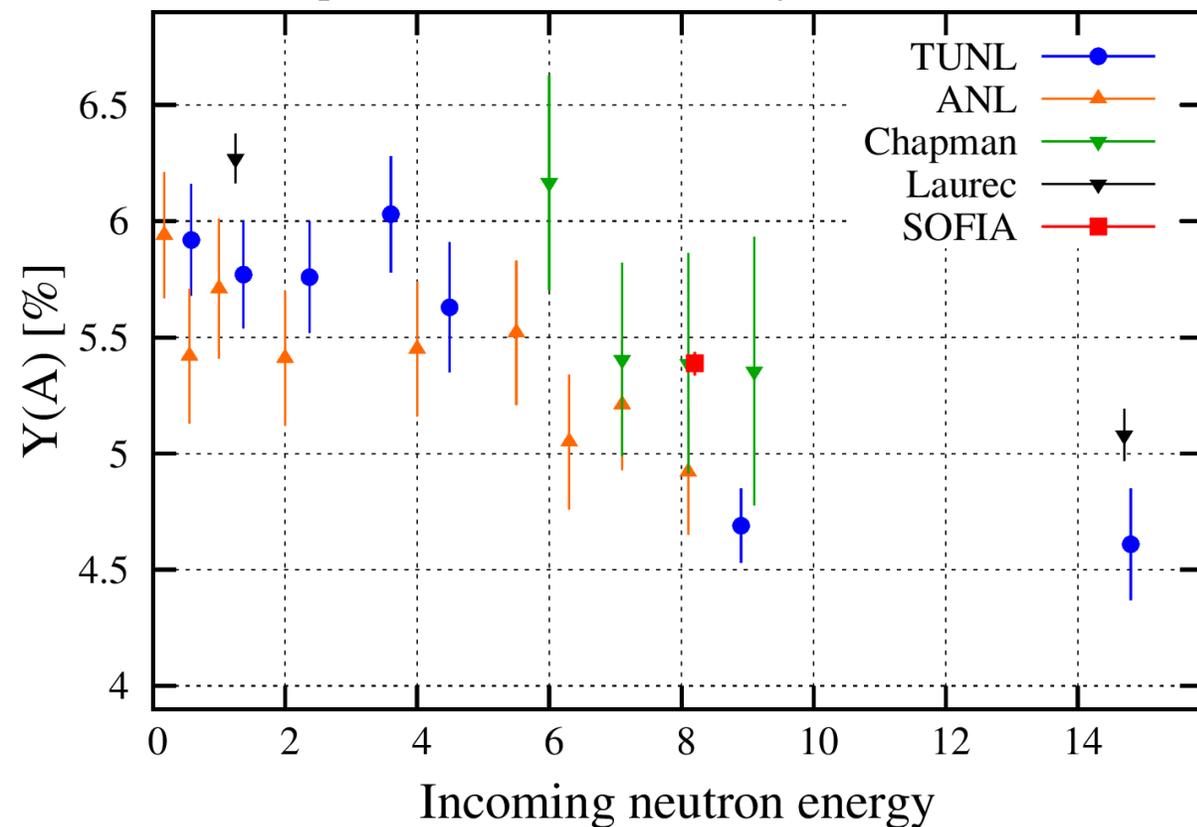
# Cumulative yields: $^{236}\text{U}(\gamma, f)$ vs $^{235}\text{U}(n, f)$ cumulative yields



comparison of the cumulative yields for the  $^{140}\text{Ba}$



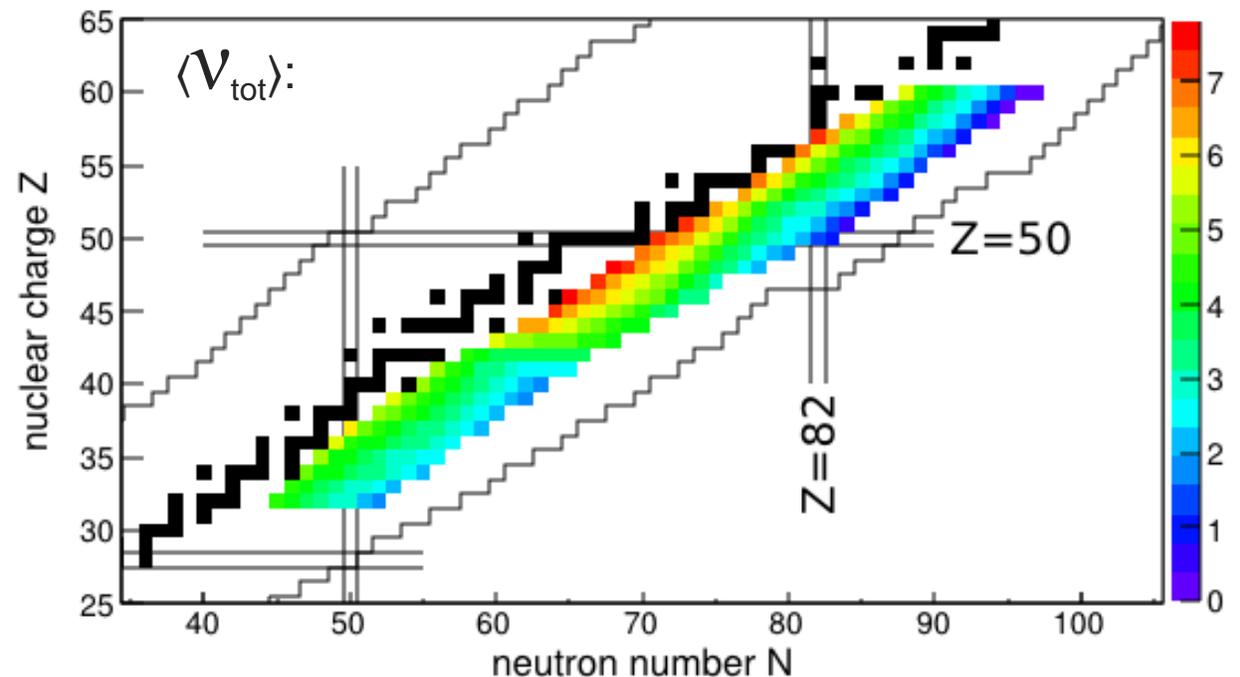
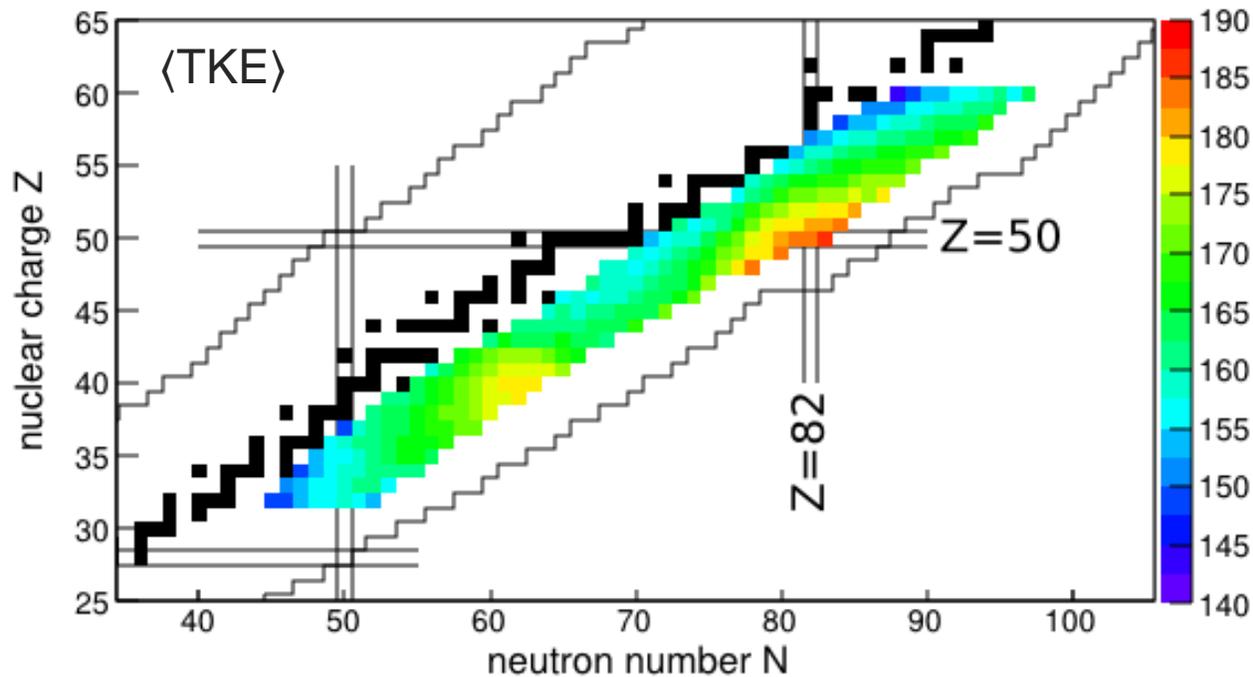
comparison of the cumulative yields for the  $^{99}\text{Mo}$



*Analysis by L. Grente (CEA,DAM,DIF)*

# $\langle TKE \rangle$ vs $\langle V_{\text{tot}} \rangle$ : $^{235}\text{U}(\gamma, f)$

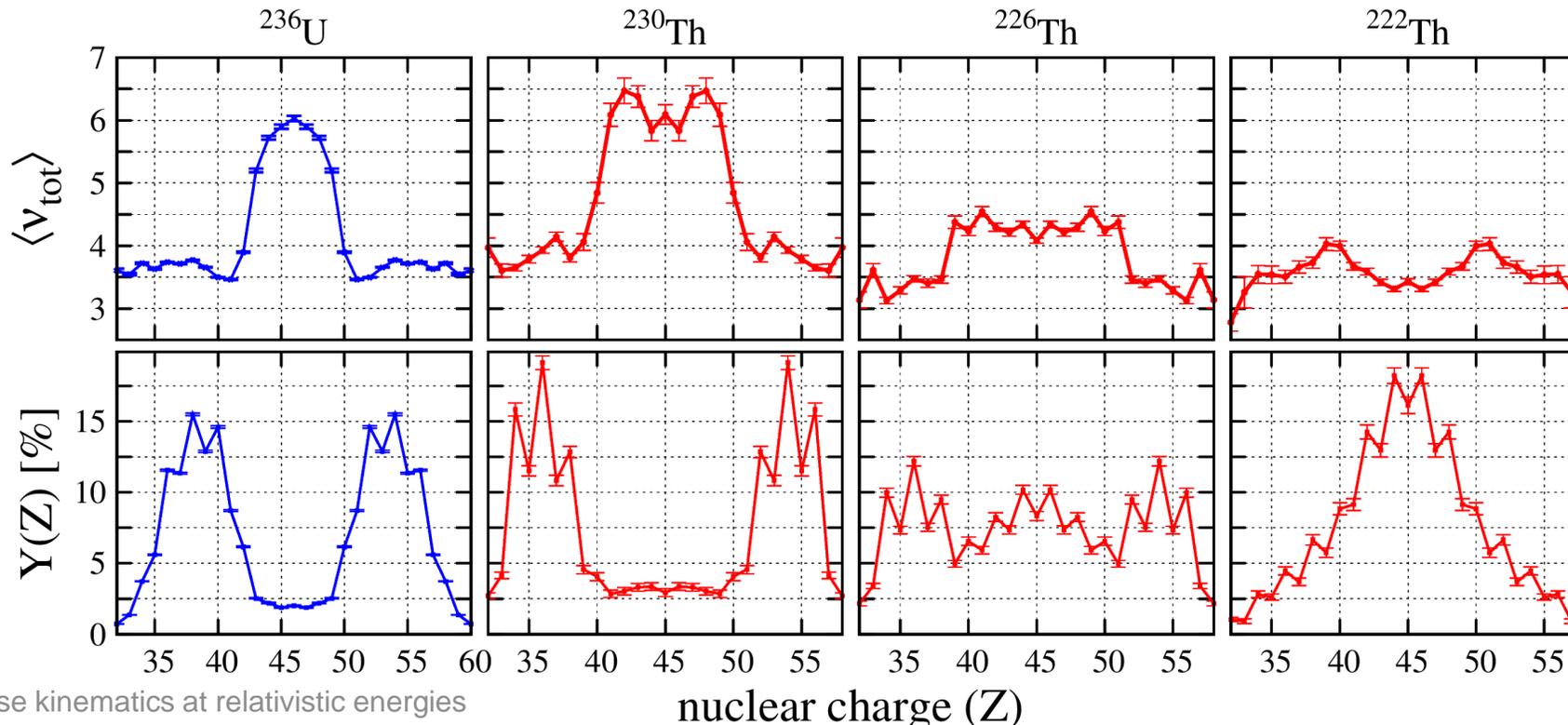
- Both observables probe the scission configuration
- Large deformation: high  $V_{\text{tot}}$ , but low TKE
- Highly deformed symmetric mode compared to compact asymmetric mode



# $Y(Z)$ vs $V_{\text{tot}}$ : $^{222,226,230}\text{Th}(\gamma, f)$ and $^{236}\text{U}(\gamma, f)$

For neutron-deficient thorium isotopes

- Symmetric fission becomes the main fission mode
- Even-odd staggering remains, but  $V_{\text{tot}}$  drops around 2.7 MeV (effect of 19 MeV)
- New symmetric fission mode observed with a compact configuration at scission

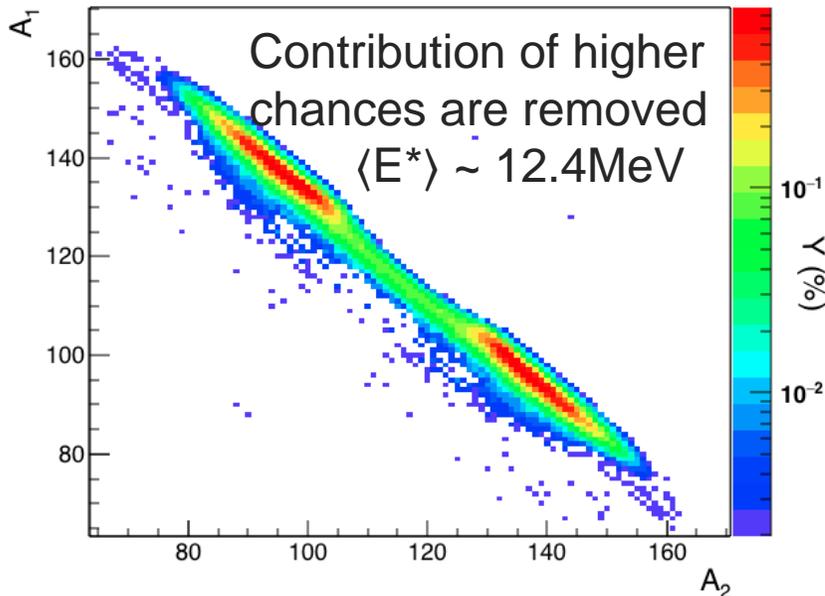


# $^{236}\text{U}(\gamma, f)$ : Prompt neutron multiplicity per fission fragment



From the correlated mass yield  $Y(A_1, A_2)$  to  $\langle \nu \rangle(M)$

Analysis by L. Grente (CEA, DAM, DIF)



$$Y(A_1, A_2) = \sum_{\nu_1=0}^{A_B - A_1 - A_2} P^{M_1}(\nu_1) P^{M_2}(\nu_2) X(M_1)$$

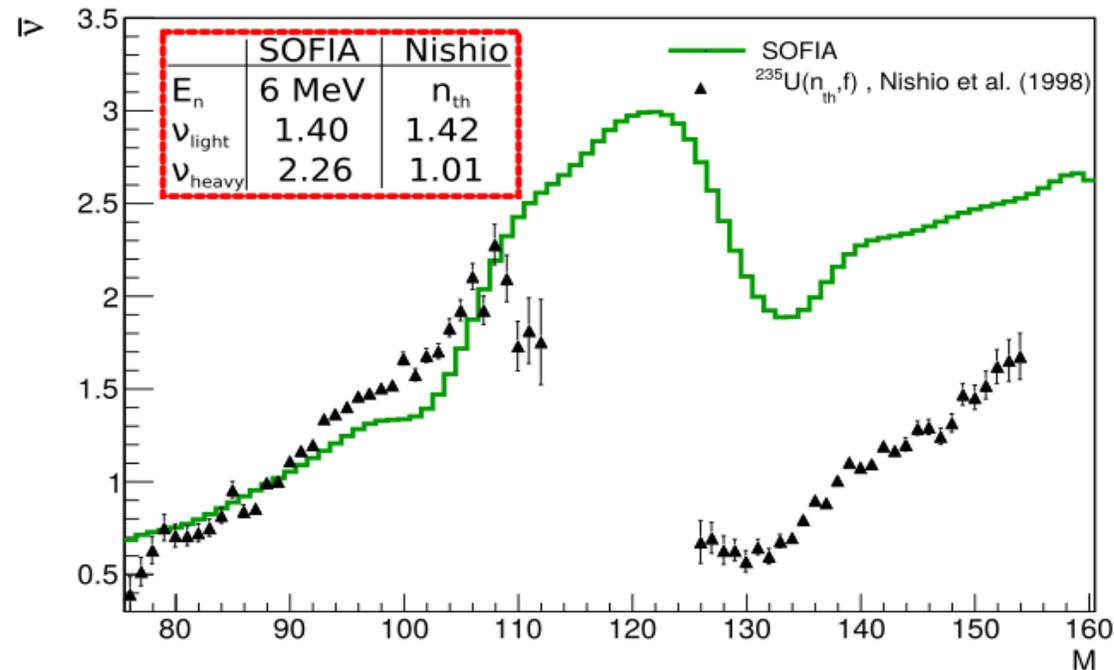
$A_i$ : mass of the fragment after neutron emission

$X(M_i)$ : mass yields before neutron emission

$Y(A_i)$ : mass yields after neutron emission

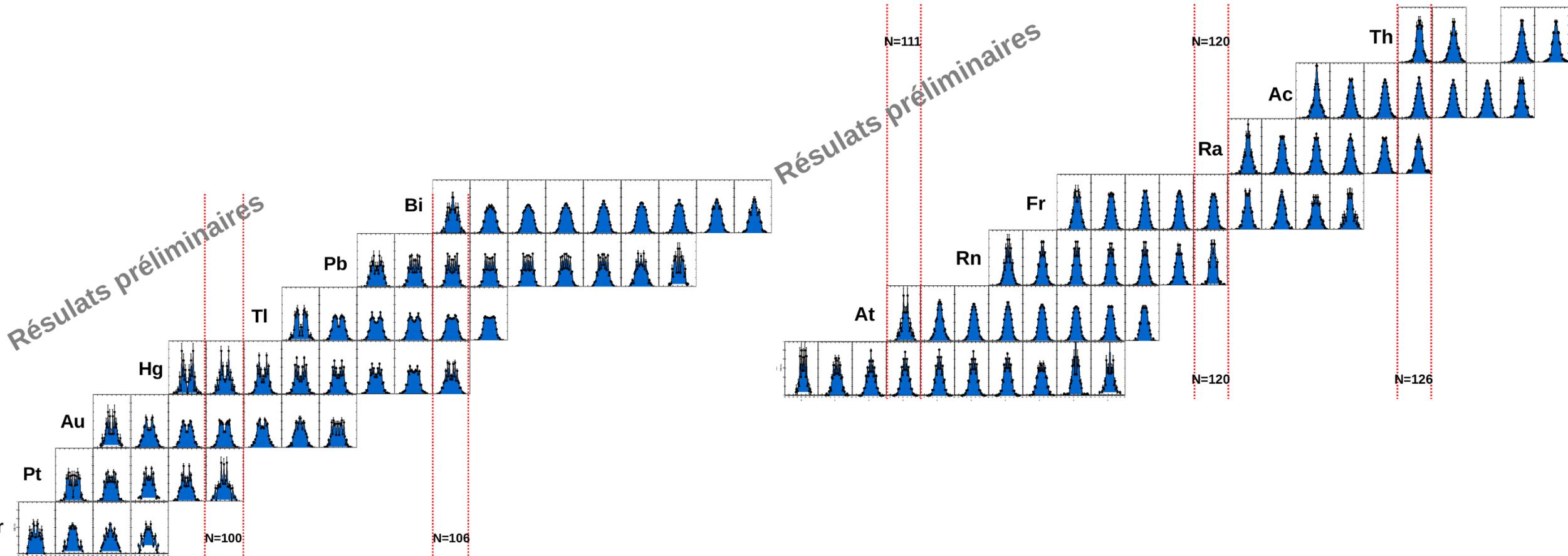
$P^{M_i}(\nu_i)$ : probability for a primary fragment of mass  $M$ , to emit  $\nu$  neutrons

- **hyp 1:  $P^{M_i}(\nu_i)$  gaussian**  
 $\Rightarrow$  3 sets of independant parameters  
 $\langle \nu \rangle(M), \sigma(M), X(M_i)$
- **hyp 2:  $\langle \nu \rangle(M), \sigma(M)$  Fourier series**  
 $\Rightarrow$  cut in the high frequency domain
- **$\chi^2$  minimization using MIGRAD**  
 $\Rightarrow$  from the CERN library MINUIT



# Study of the new island of asymmetry

Fission study of more than 100 nuclei in 4 days of beam time



# Conclusions

**Inverse kinematics at relativistic energy for accurate fission yields and  $V_{tot}$**

**Fission study of exotic nuclei with the underlying microscopic effect**

**Few limitation: no  $E^*$  measurement**

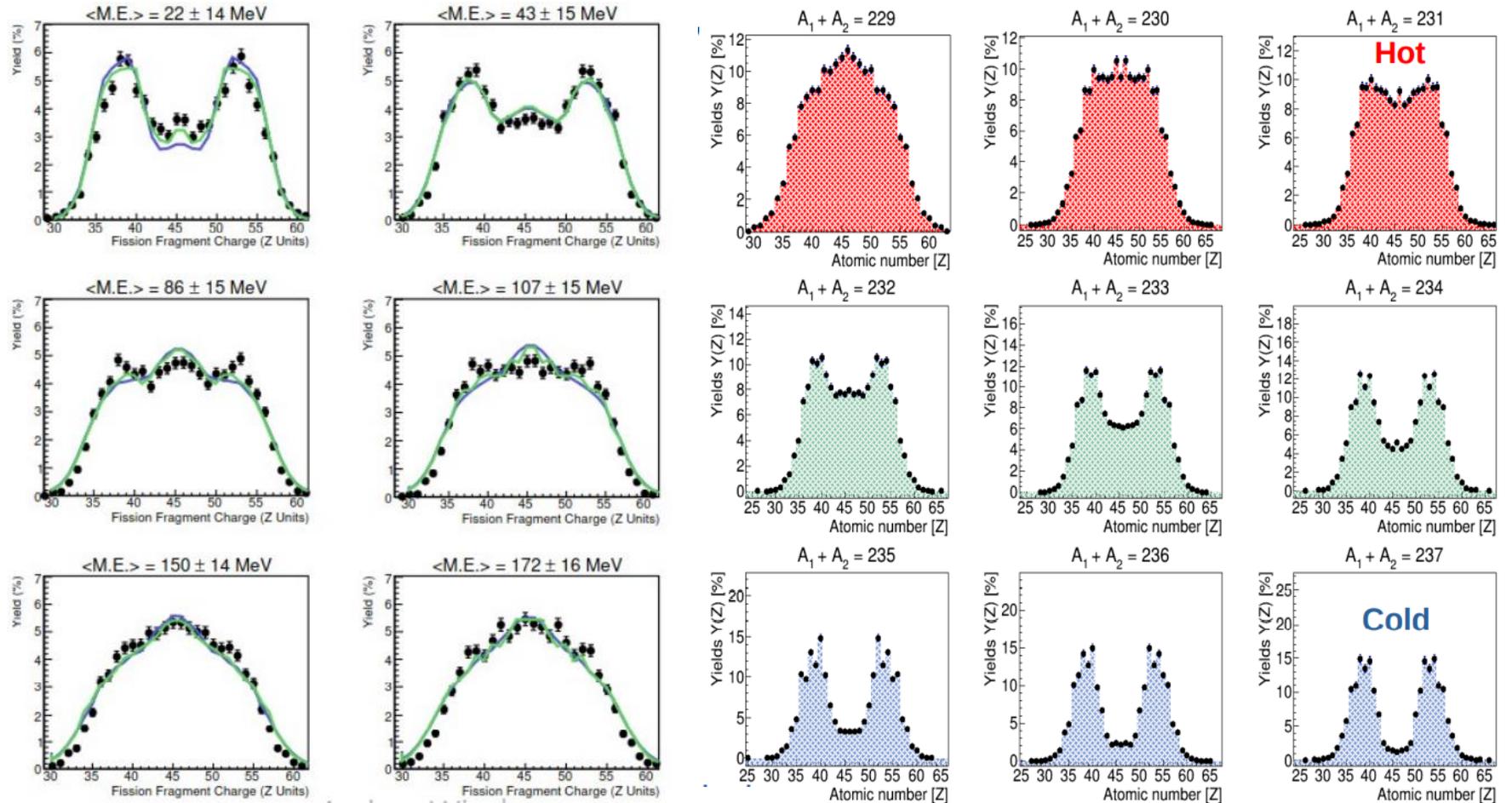
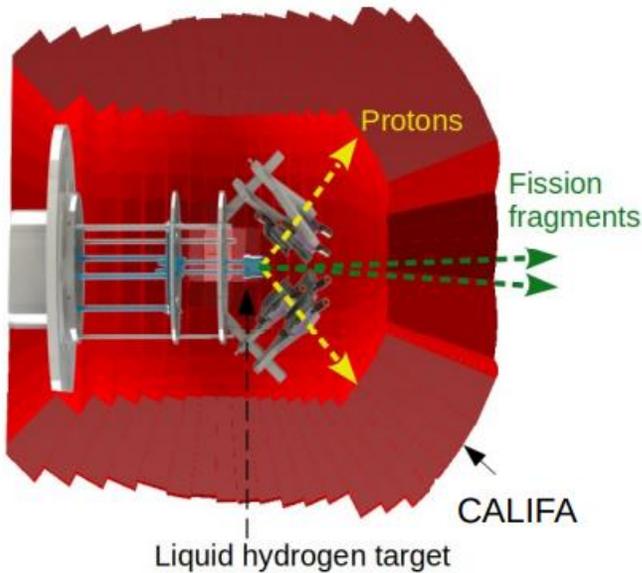
*→  $(p,2p)$  reaction to get  $E^*$  instead of Coulex but with lower statistics*

# Fission induced by quasi-free nucleon-knockout collisions

$^{238}\text{U}(p,2p)^{237}\text{Pa}$  in inverse kinematics used to induce fission and measure  $E^*$

*Analysis by G. Garcia and A. Grana (Univ. Santiago de Compostella) supervised by J. L. Rodríguez-Sánchez (Univ. Coruña)*

Same set-up but liquid H target surrounded by Si array and the CALIFA calorimeter



# Conclusions

**Inverse kinematics at relativistic energy for accurate fission yields and  $V_{tot}$**

**Fission study of exotic nuclei with the underlying microscopic effect**

**Few limitation: no  $E^*$  measurement,  $A_{CN} \leq 238$**

→ *(p,2p) reaction to get  $E^*$  instead of Coulex but with lower statistics*

→ *complementary to measurement at GANIL/VAMOS (see Diego's talk)*



# 4. More info

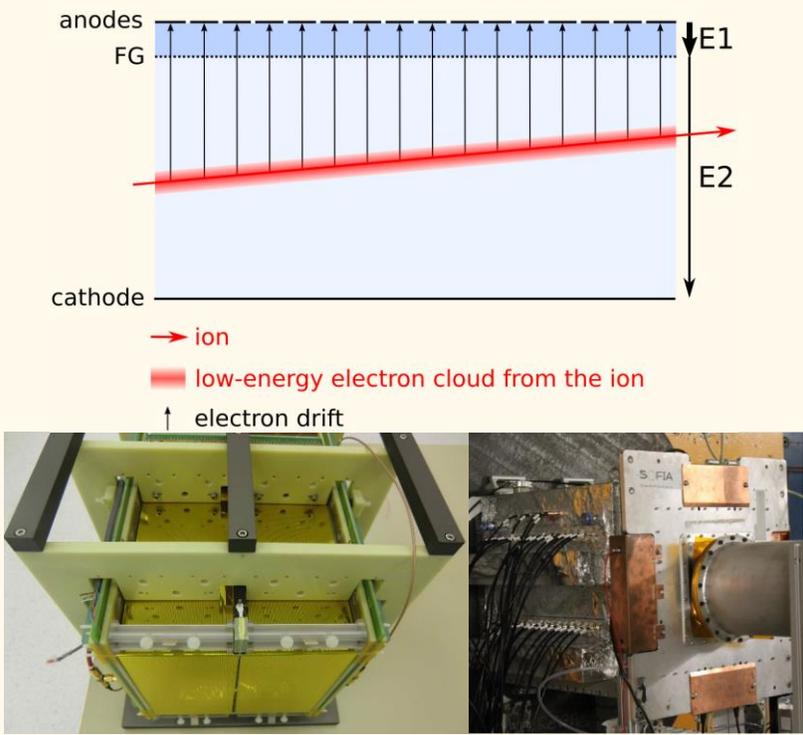
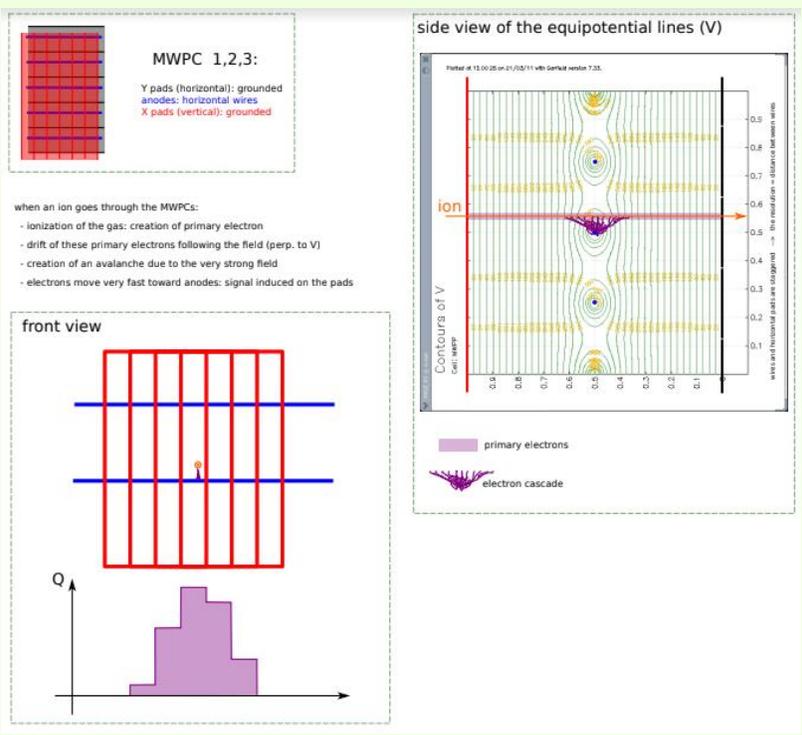
Set-up

Analysis: nuclear component subtraction

Fission modes

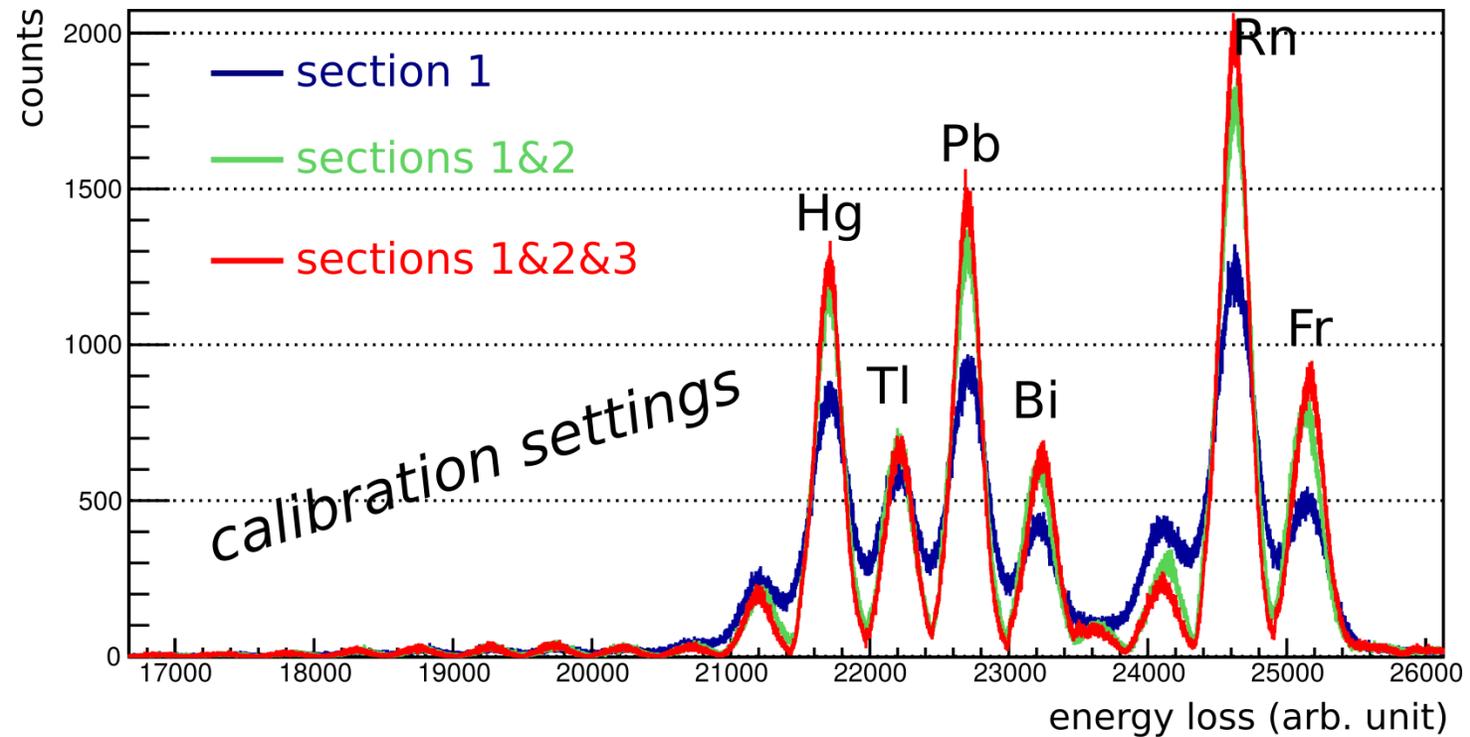
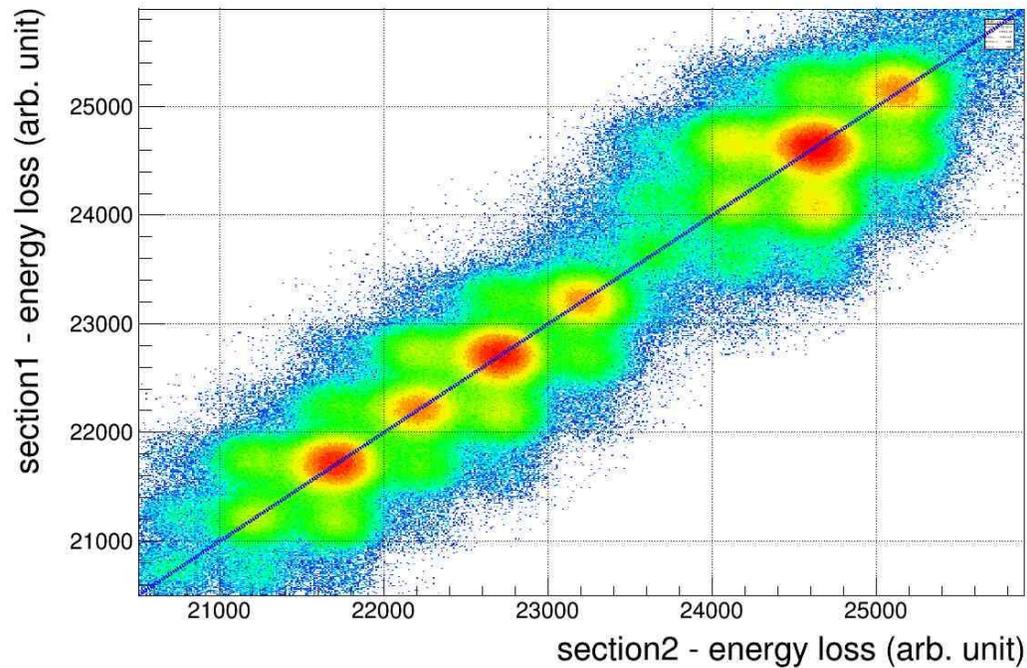
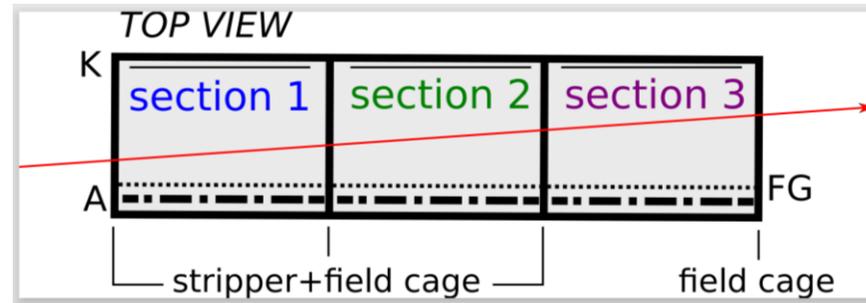
# SOFIA spectrometer

3 types of detectors : **MUSIC**, **MWPC**, **scintillators**

|  |  |  |
|--|--|--|
| <p><b>MULTIPLE Sample Ionisation Chamber</b></p> <p><b>ENERGY LOSS: Z &amp; DRIFT TIME: x , <math>\theta</math></b></p>  | <p><b>Multi Wire Proportional Counter</b></p> <p><b>Q DISTRIBUTION ON PADS: x , y</b></p>  | <p>scintillator readout by 2 PMTs</p> <p><b>TIME PER PMT: x , <math>T_{of}</math></b></p>  |
| <p>Triple-MUSIC for incoming beam<br/>Twin-MUSIC for fission fragments</p>   | <p>MWPC0 for incoming beam<br/>MWPC1, MWPC2, MWPC3 for fission fragments</p>   | <p>2 scintillators for incoming beam<br/>scintillator + ToF wall for fission fragments</p> |
|  <p>anodes<br/>FG<br/>cathode</p> <p><math>E1</math><br/><math>E2</math></p> <p>→ ion<br/>→ low-energy electron cloud from the ion<br/>↑ electron drift</p> |  <p>MWPC 1,2,3:<br/>Y pads (horizontal): grounded<br/>anodes: horizontal wires<br/>X pads (vertical): grounded</p> <p>when an ion goes through the MWPCs:<br/>- ionization of the gas: creation of primary electron<br/>- drift of these primary electrons following the field (perp. to V)<br/>- creation of an avalanche due to the very strong field<br/>- electrons move very fast toward anodes: signal induced on the pads</p> <p>side view of the equipotential lines (V)</p> <p>Contours of V</p> <p>ion</p> <p>primary electrons<br/>electron cascade</p> <p>front view</p> <p>Q</p> |        |

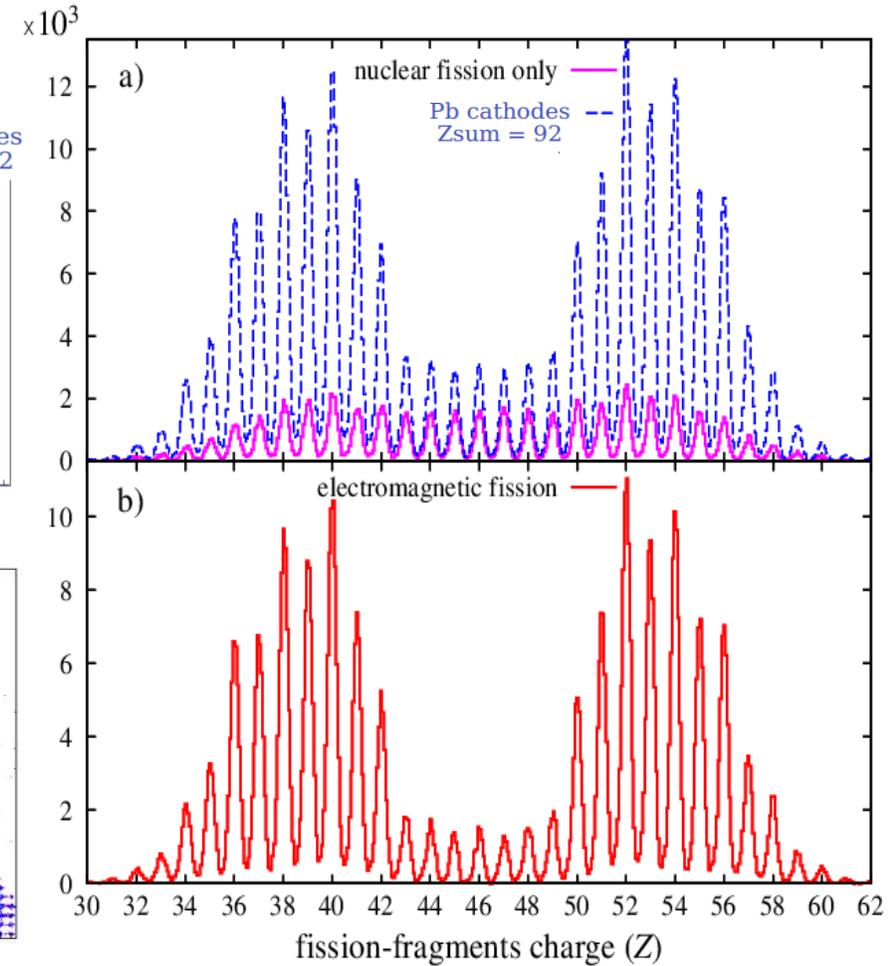
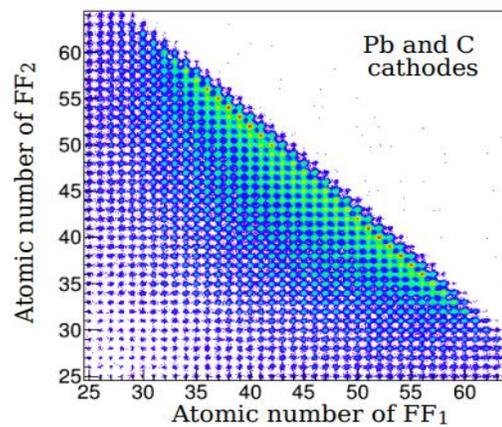
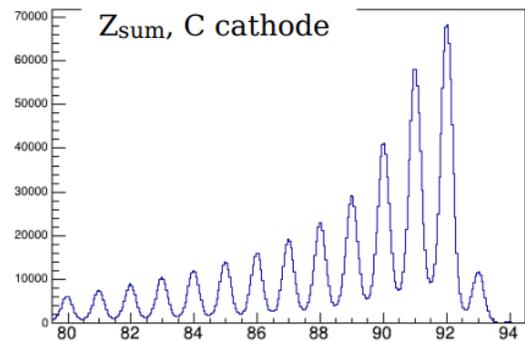
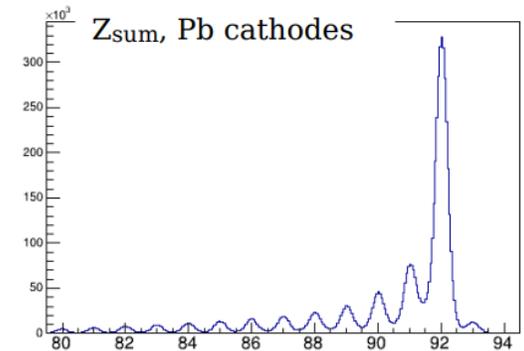
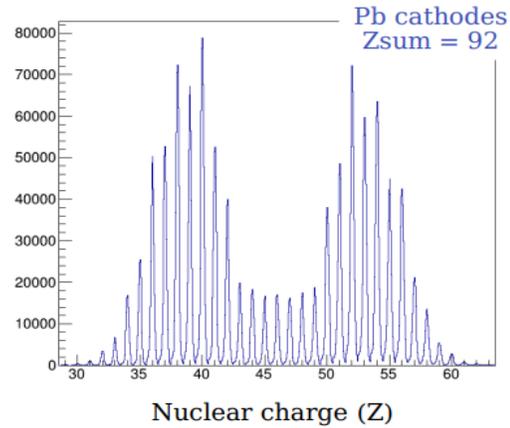
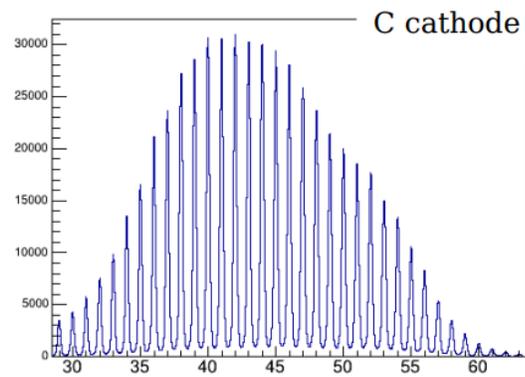
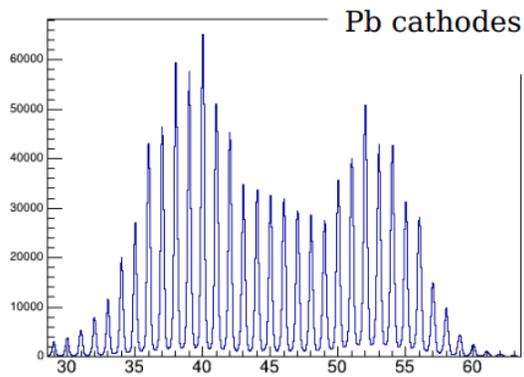
# Specificities of the detection of beam vs fission fragment

Beam with ionic charge states, even at 750 A.MeV: Triple-MUSIC



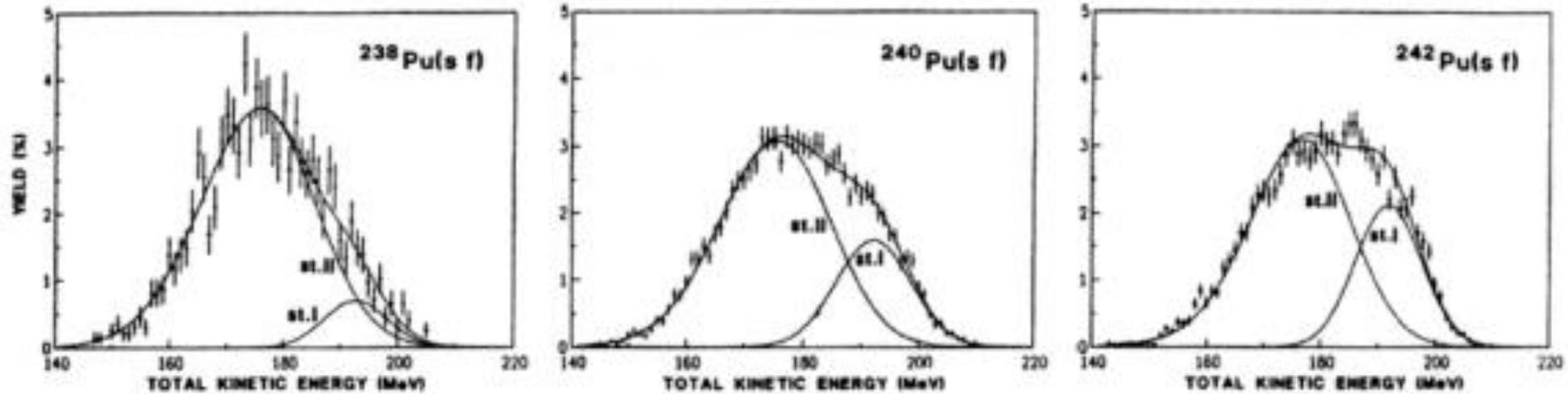
# Analysis: Nuclear reaction subtraction

How to select coulomb induced fission only ?

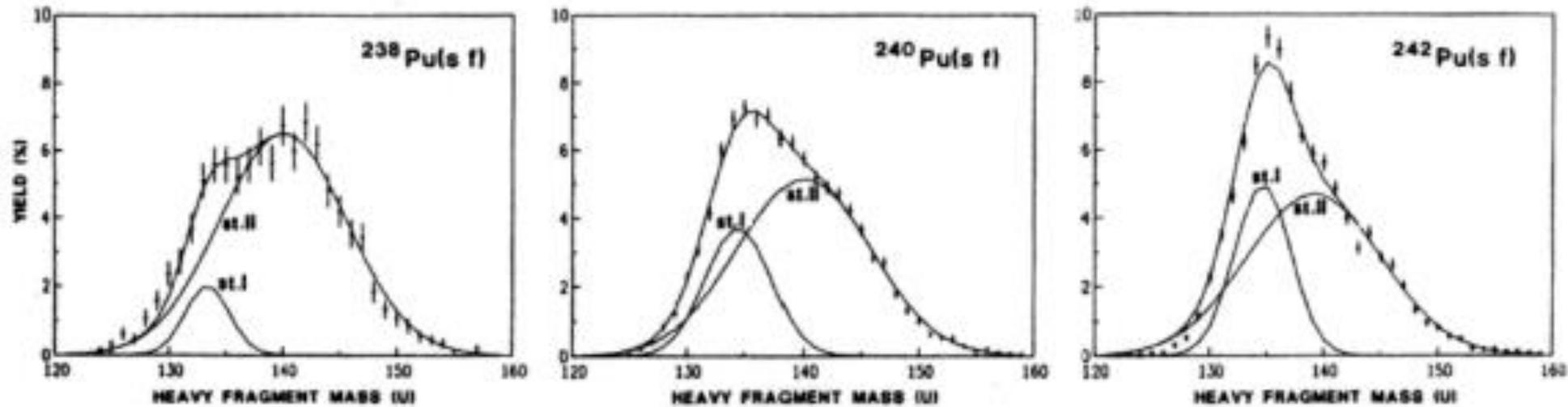


# Standard 1 and standard 2 asymmetric modes in Pu (sf)

TKE



Mass (A)



# Asymmetric to symmetric fission in Fm isotopes

