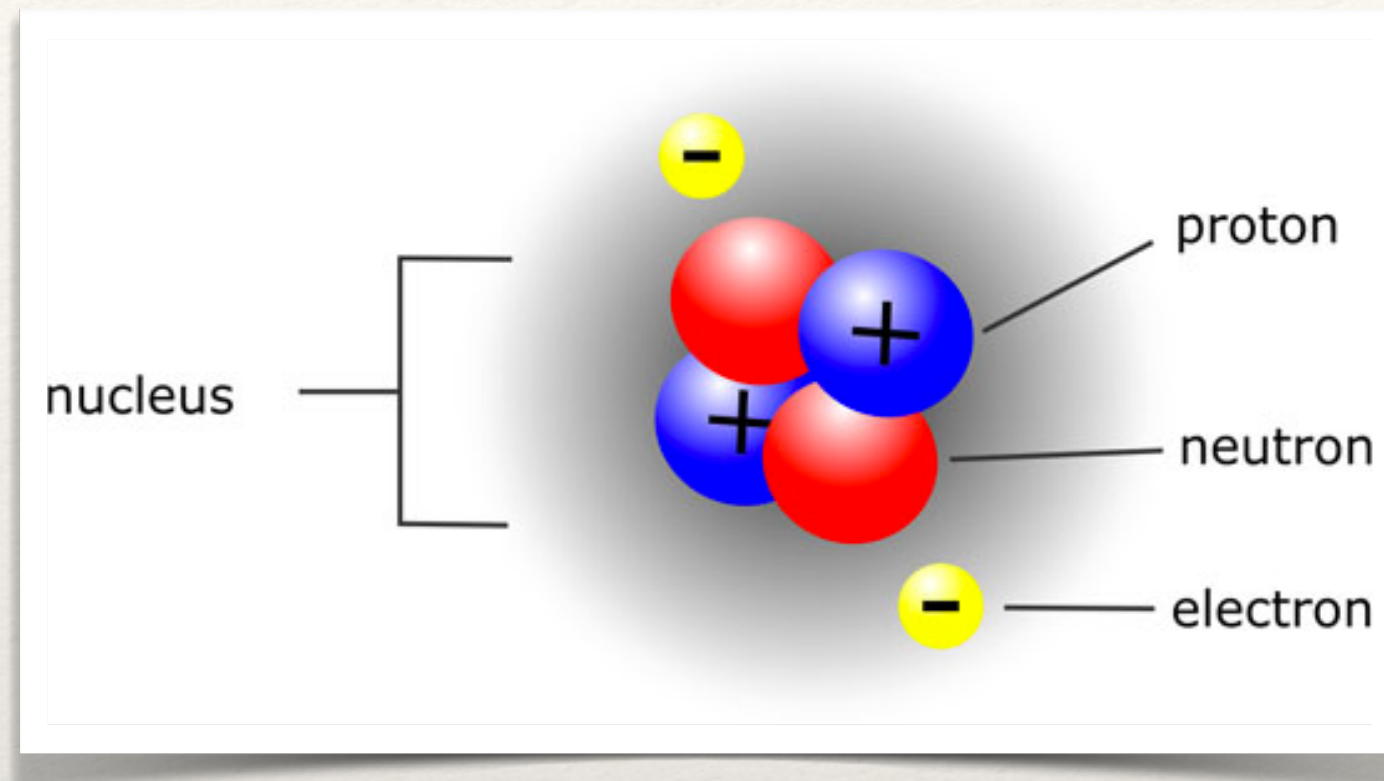


Sarah NAIMI (IJCLab/Paris-Saclay University)

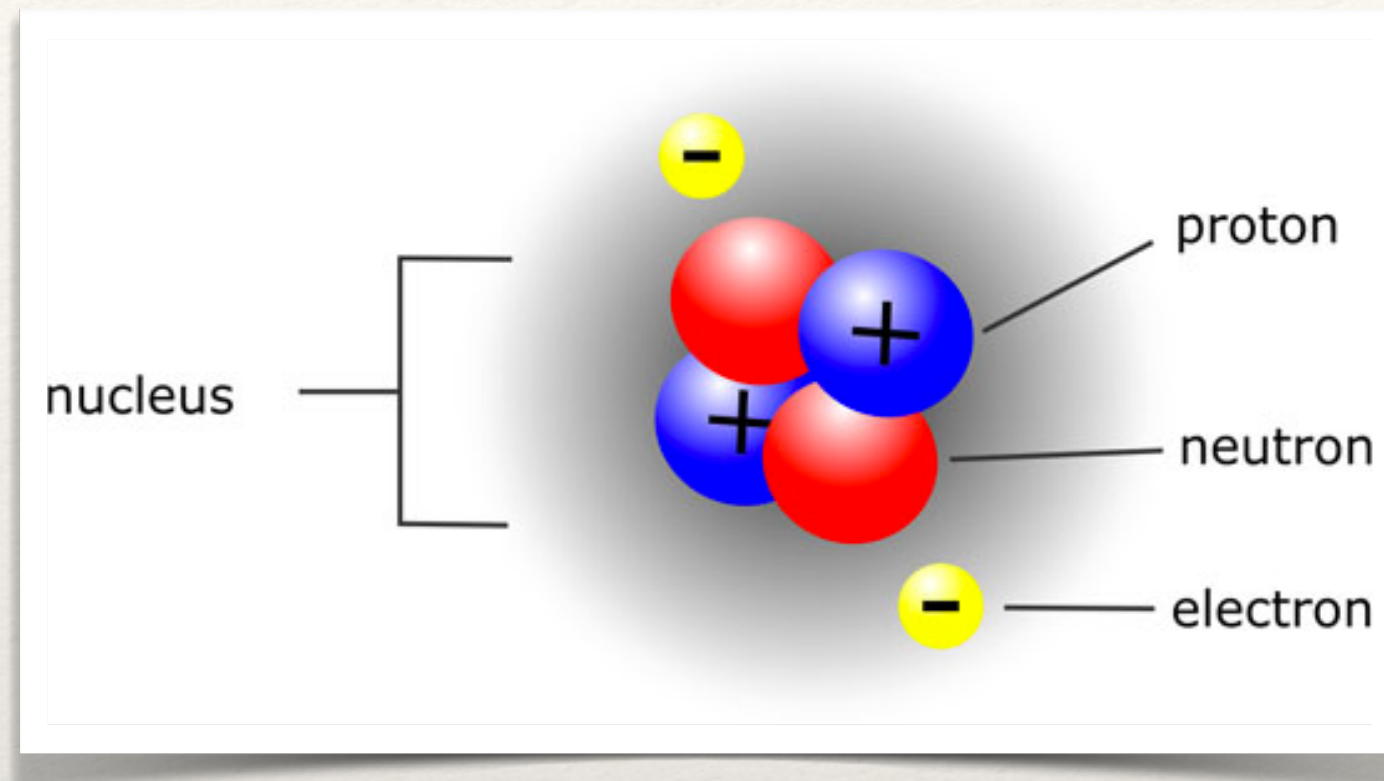
3rd Rencontre PhyNuBe 6-11 Oct. 2024

Mass Measurements for Nuclear Astrophysics

Reminder: Atomic mass

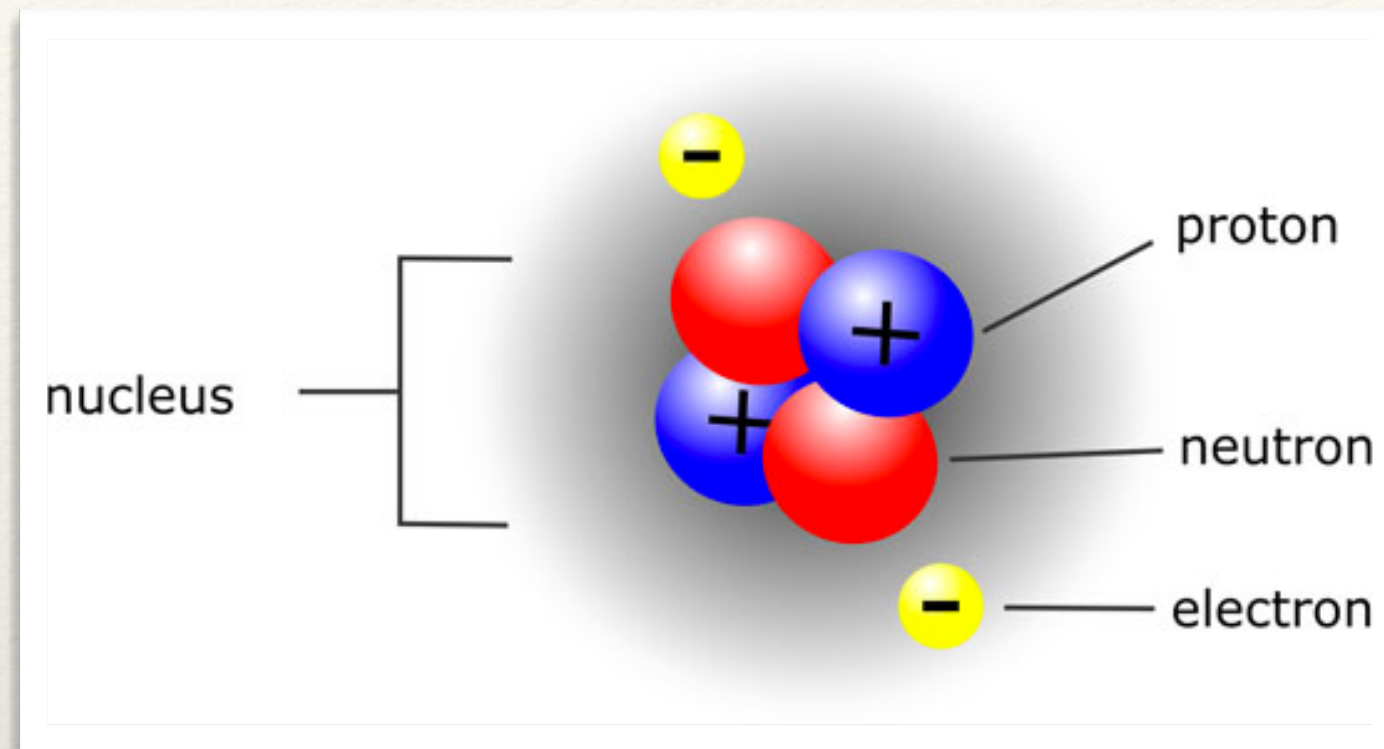


Reminder: Atomic mass

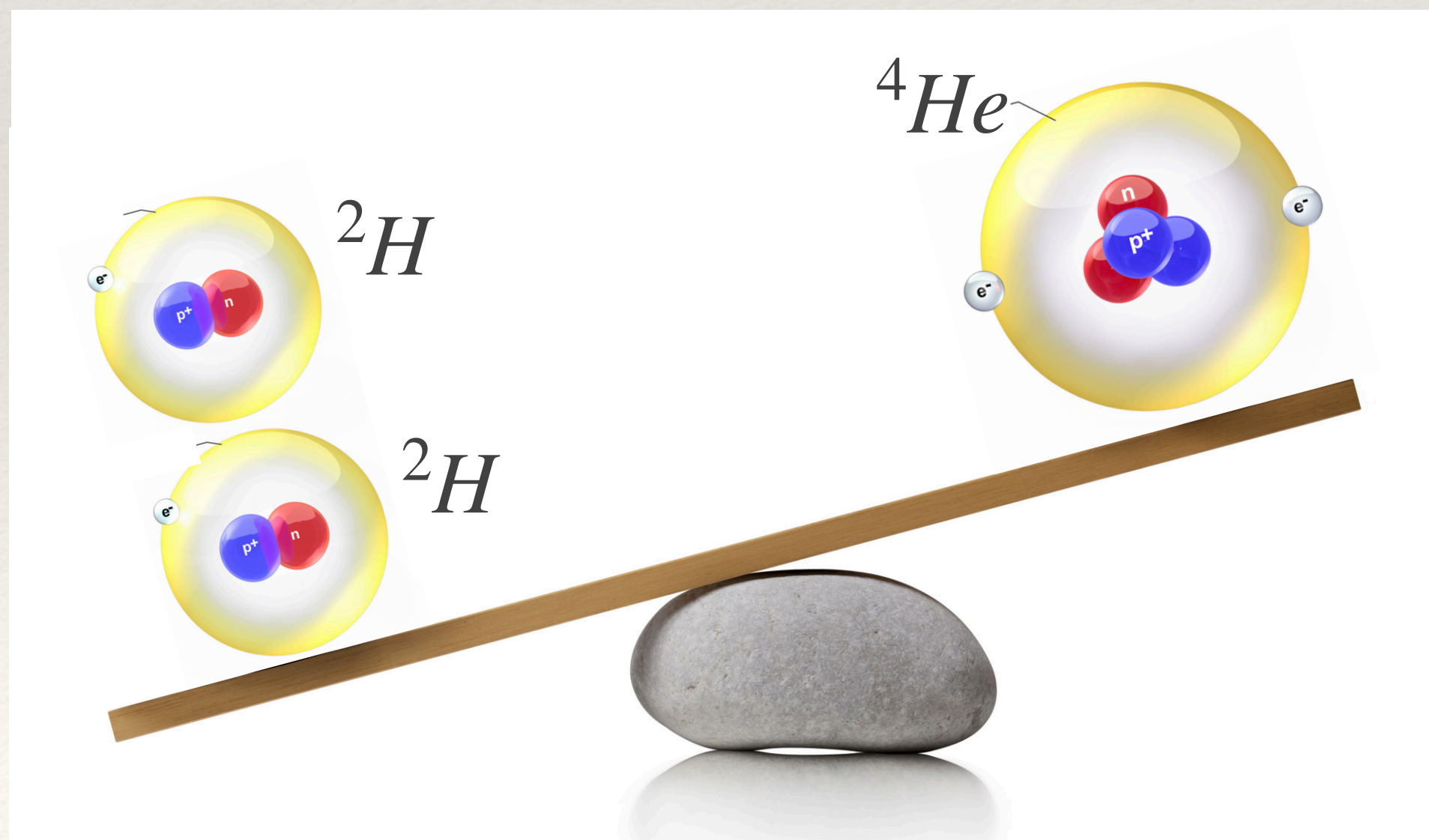


$$M(^4\text{He}) = 2 \cdot m_p + 2 \cdot m_n + 2 \cdot m_e$$

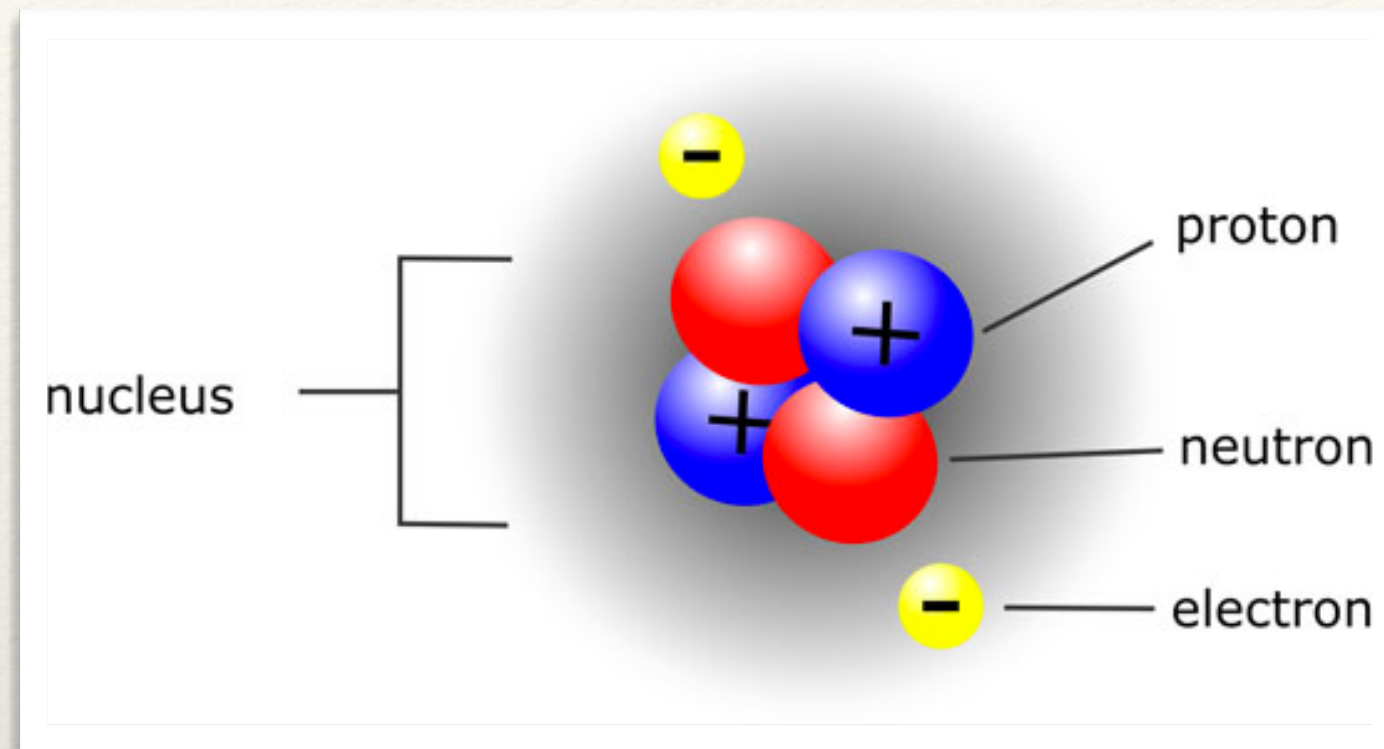
Reminder: Atomic mass



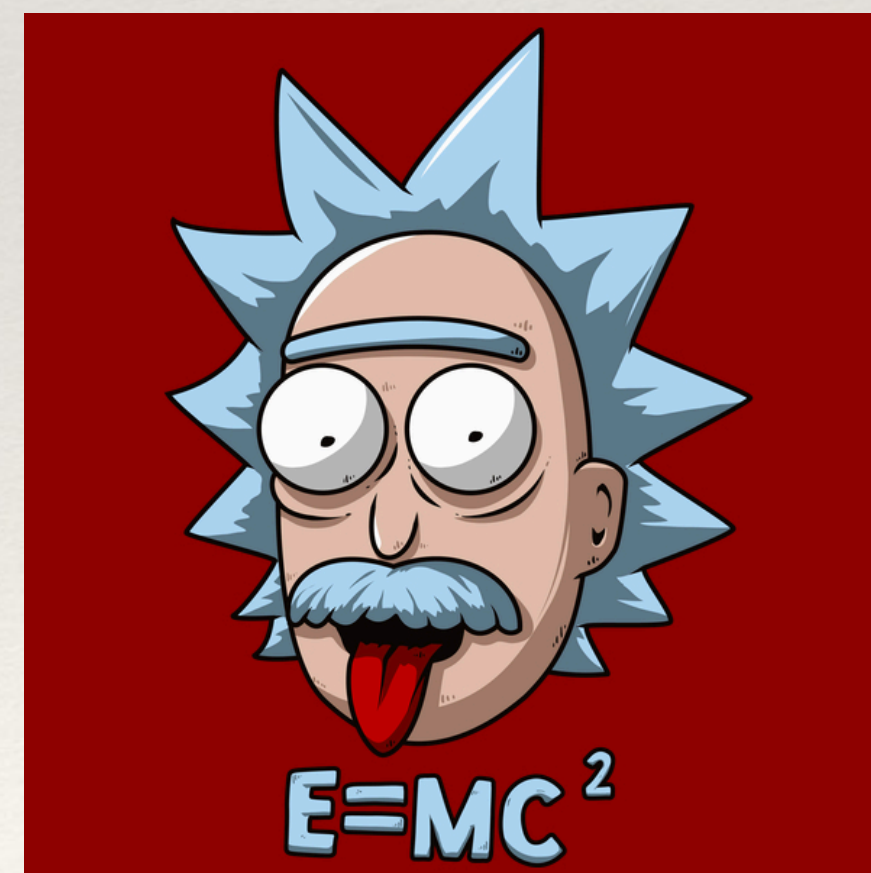
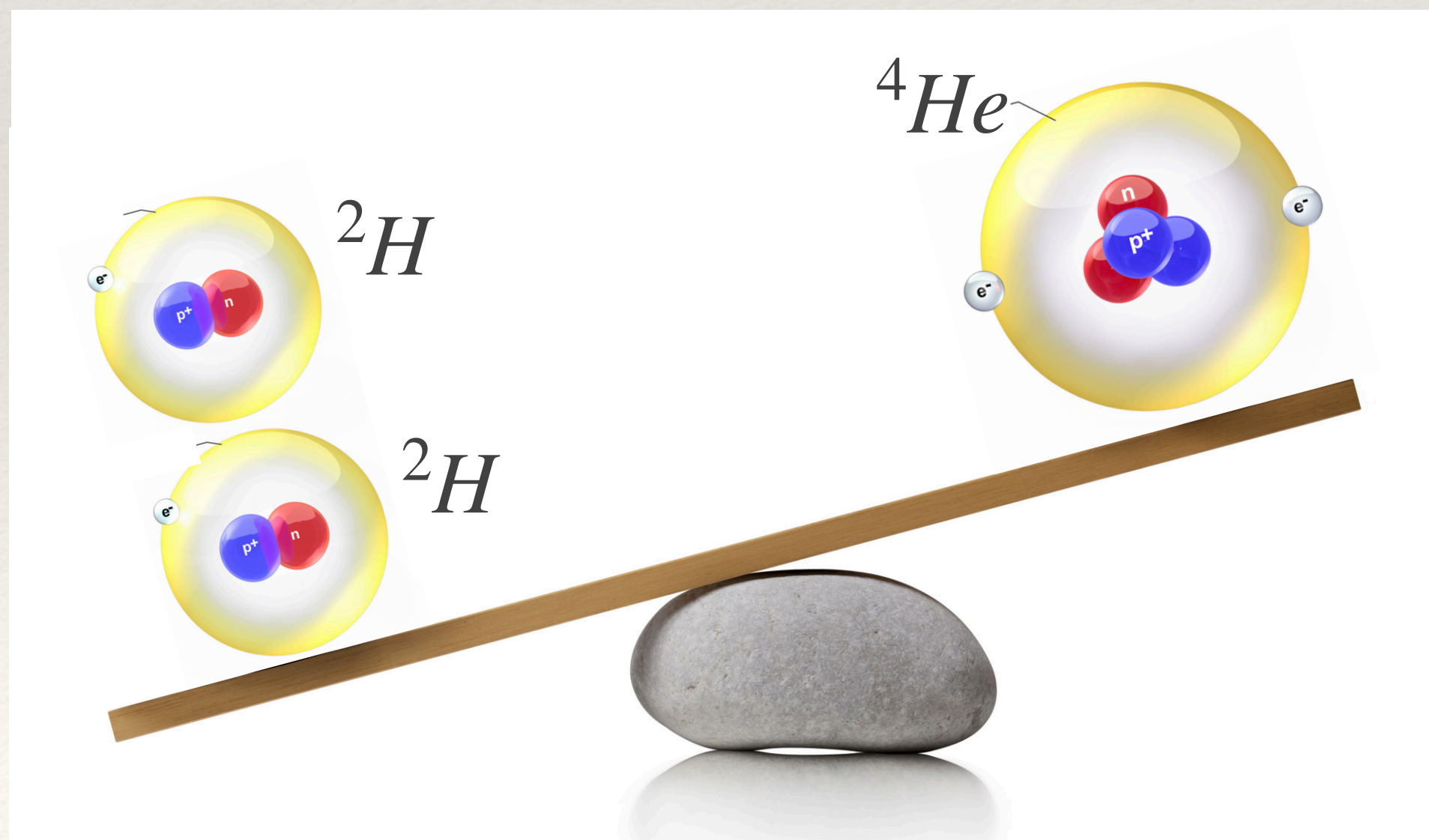
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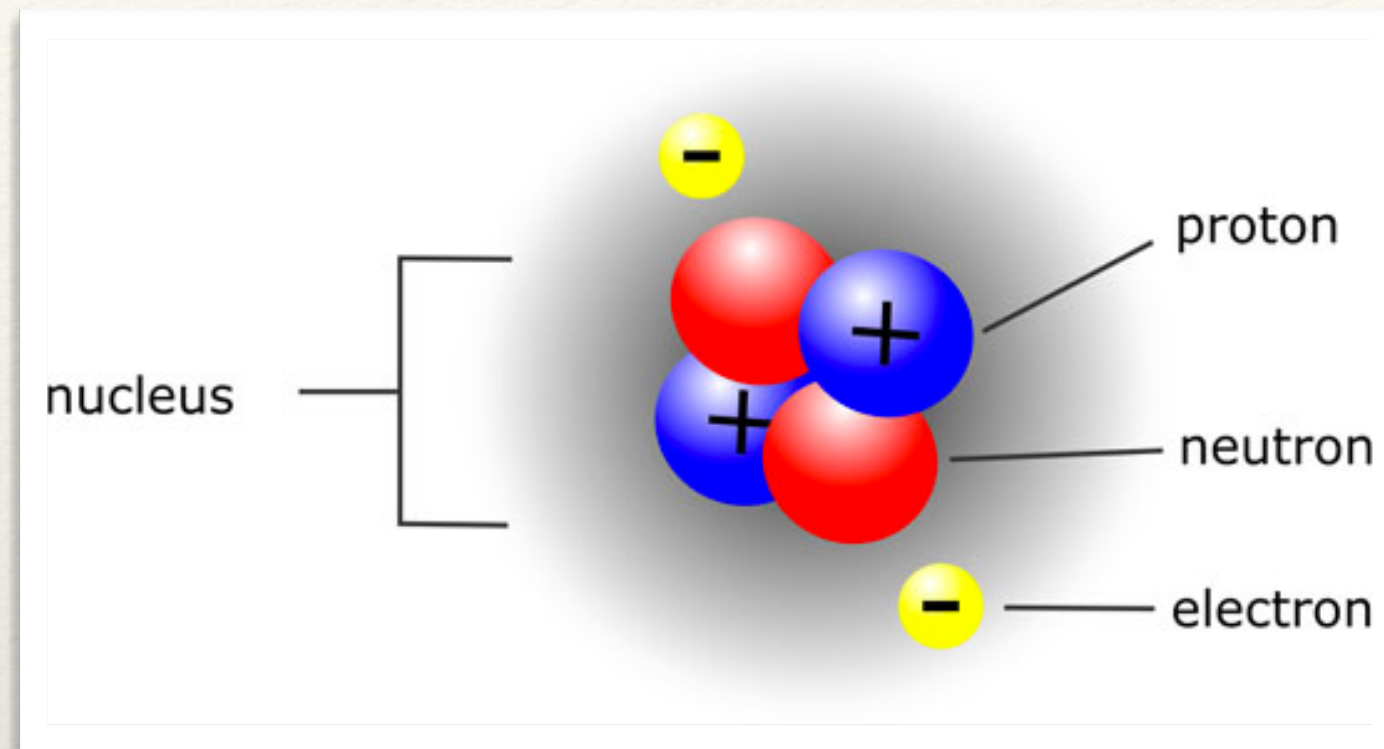
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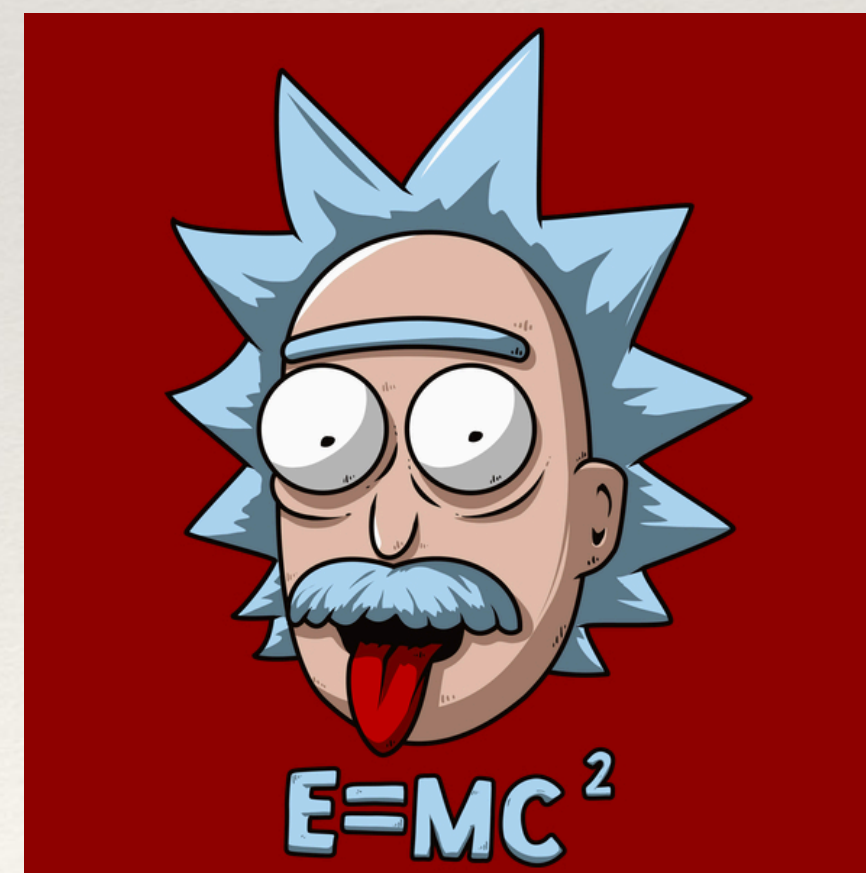
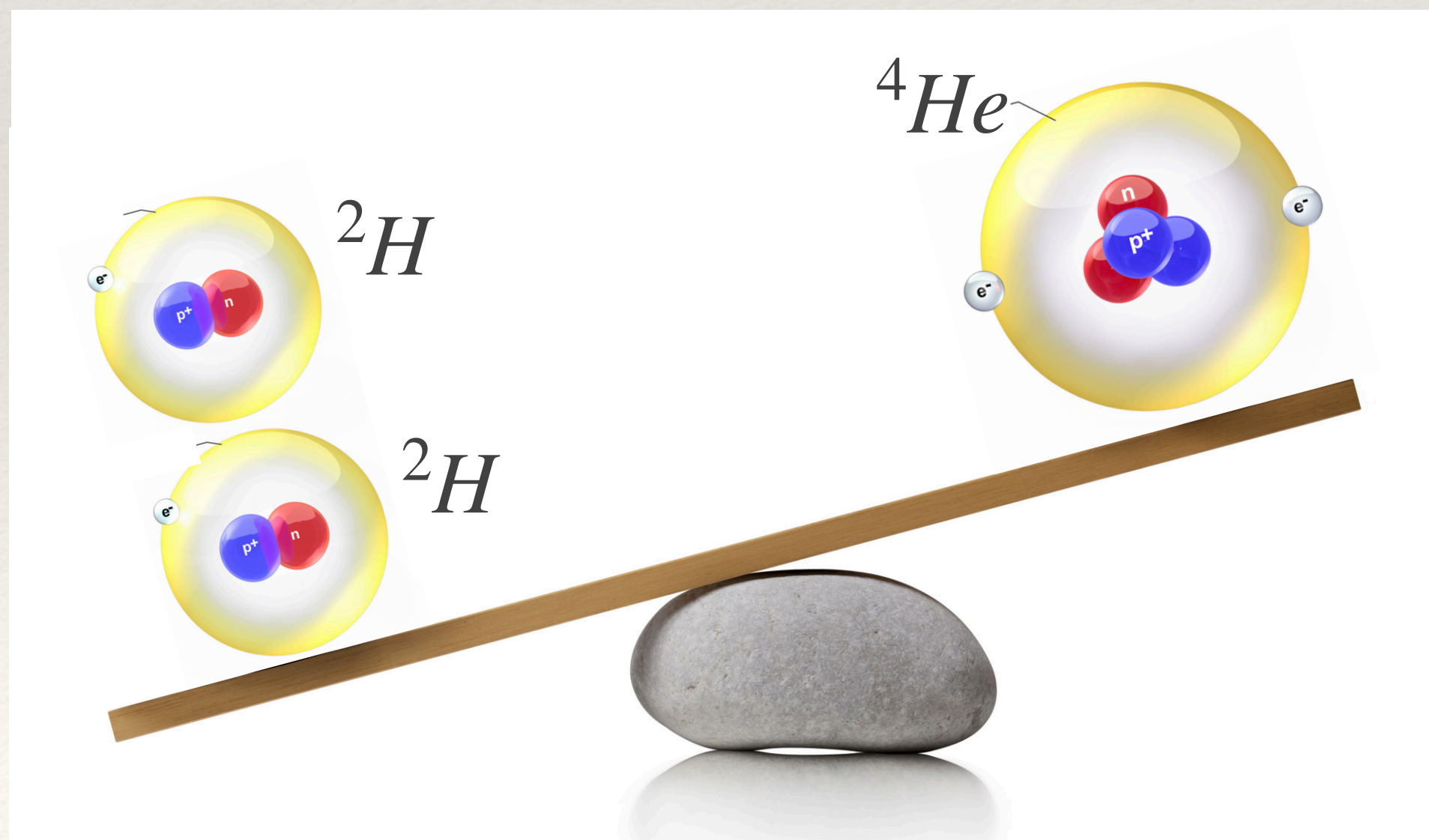
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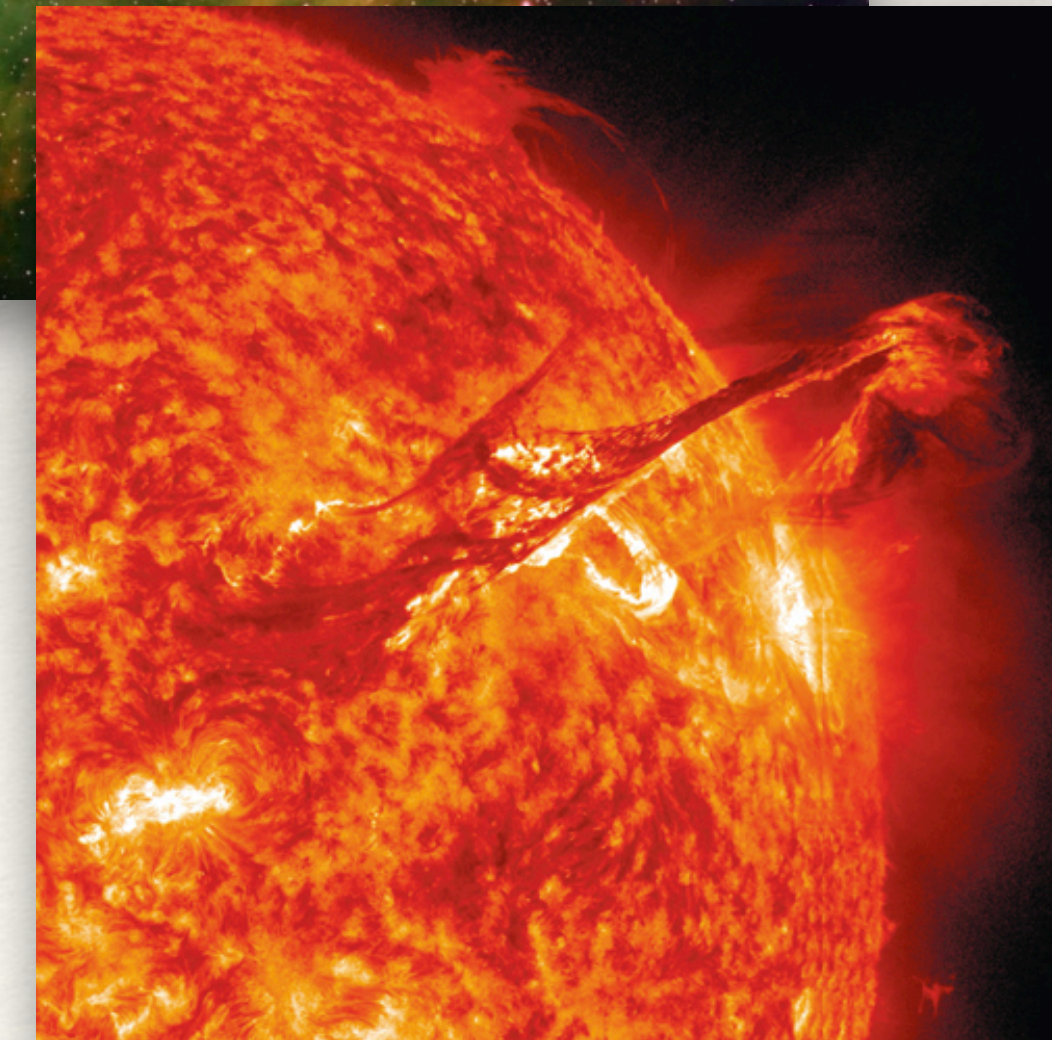
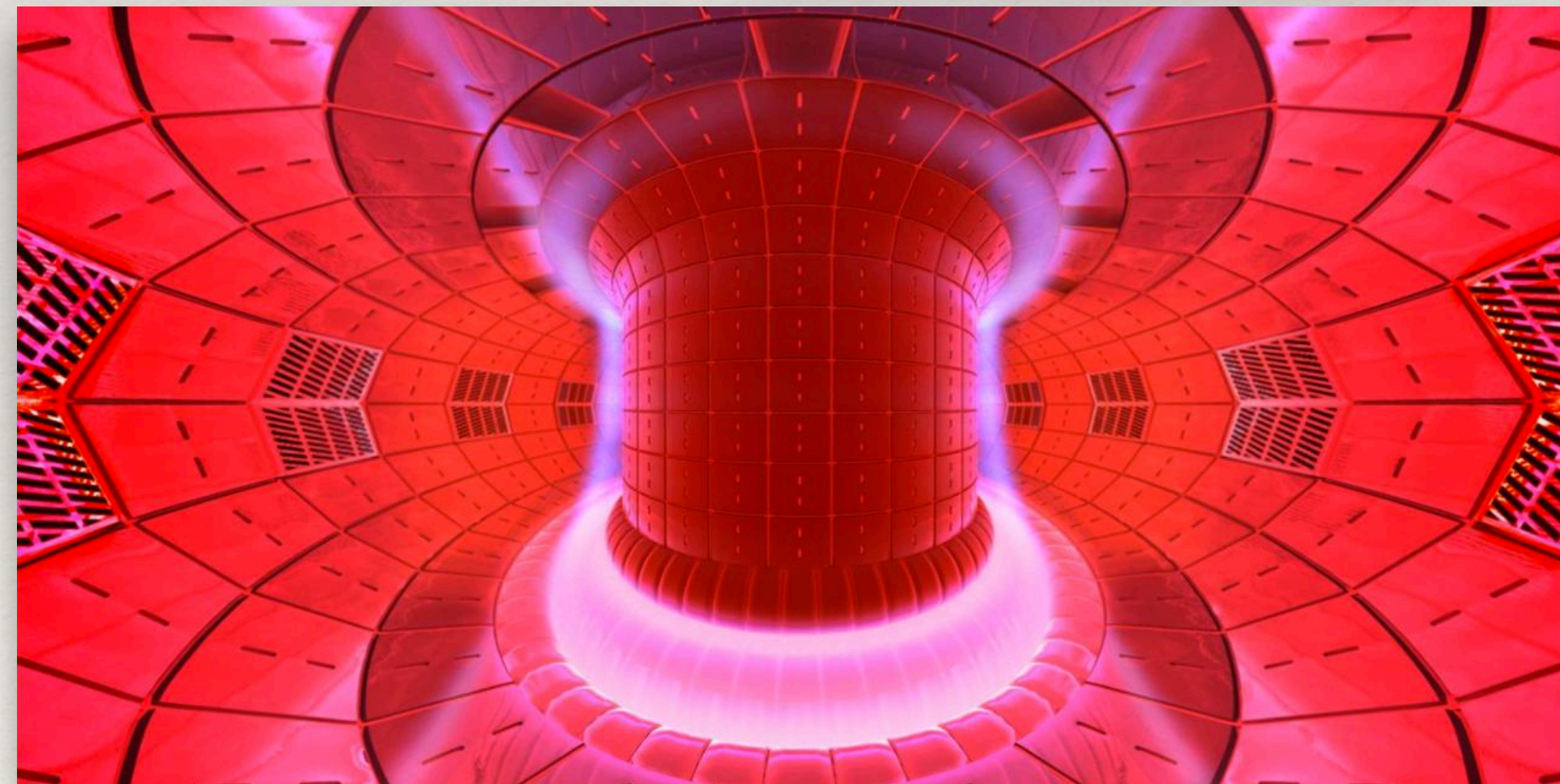
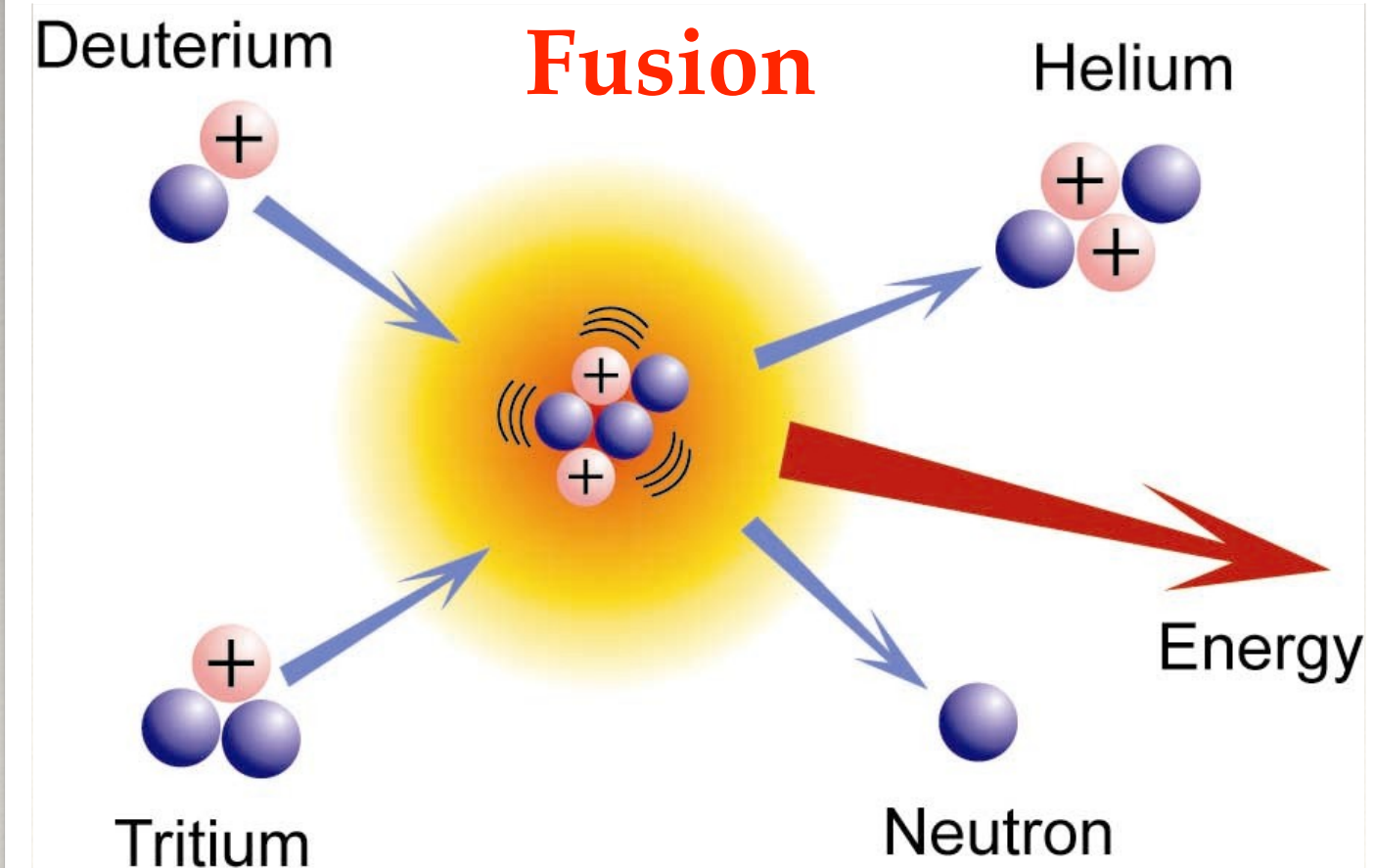
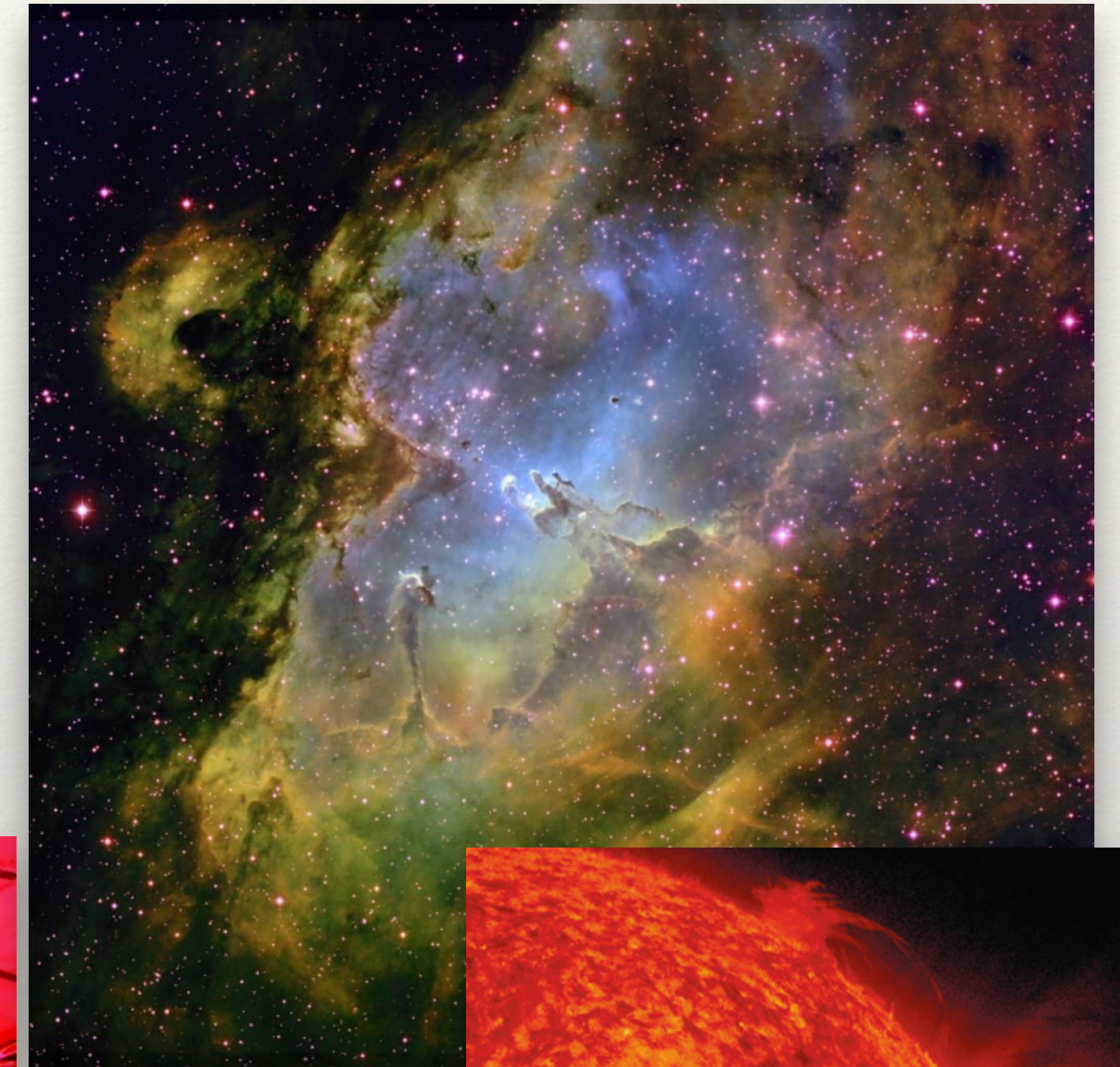
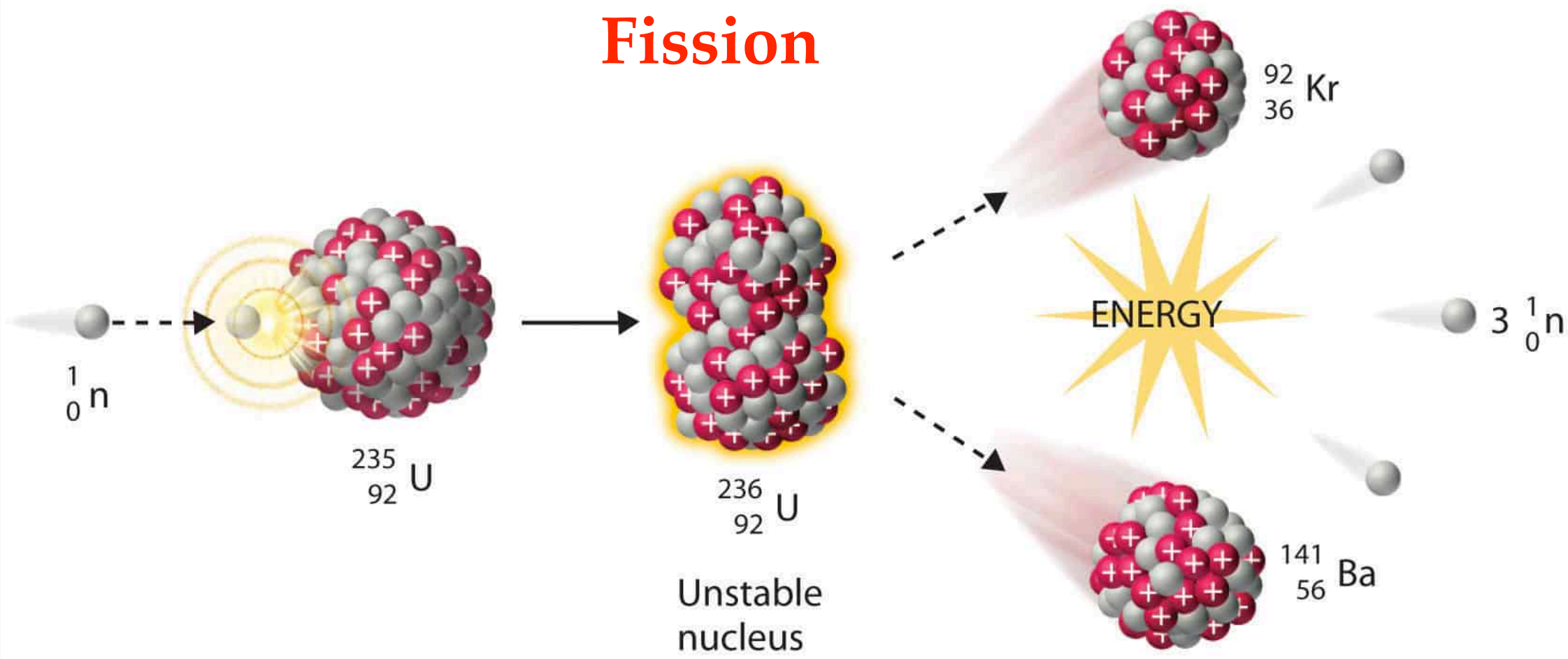


$$M(^4\text{He}) = 2 \cdot m_p + 2 \cdot m_n + 2 \cdot m_e - \text{Binding Energy}$$

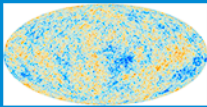
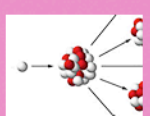






Source of Energy in the Universe

Fission



The Origin of the Solar System Elements

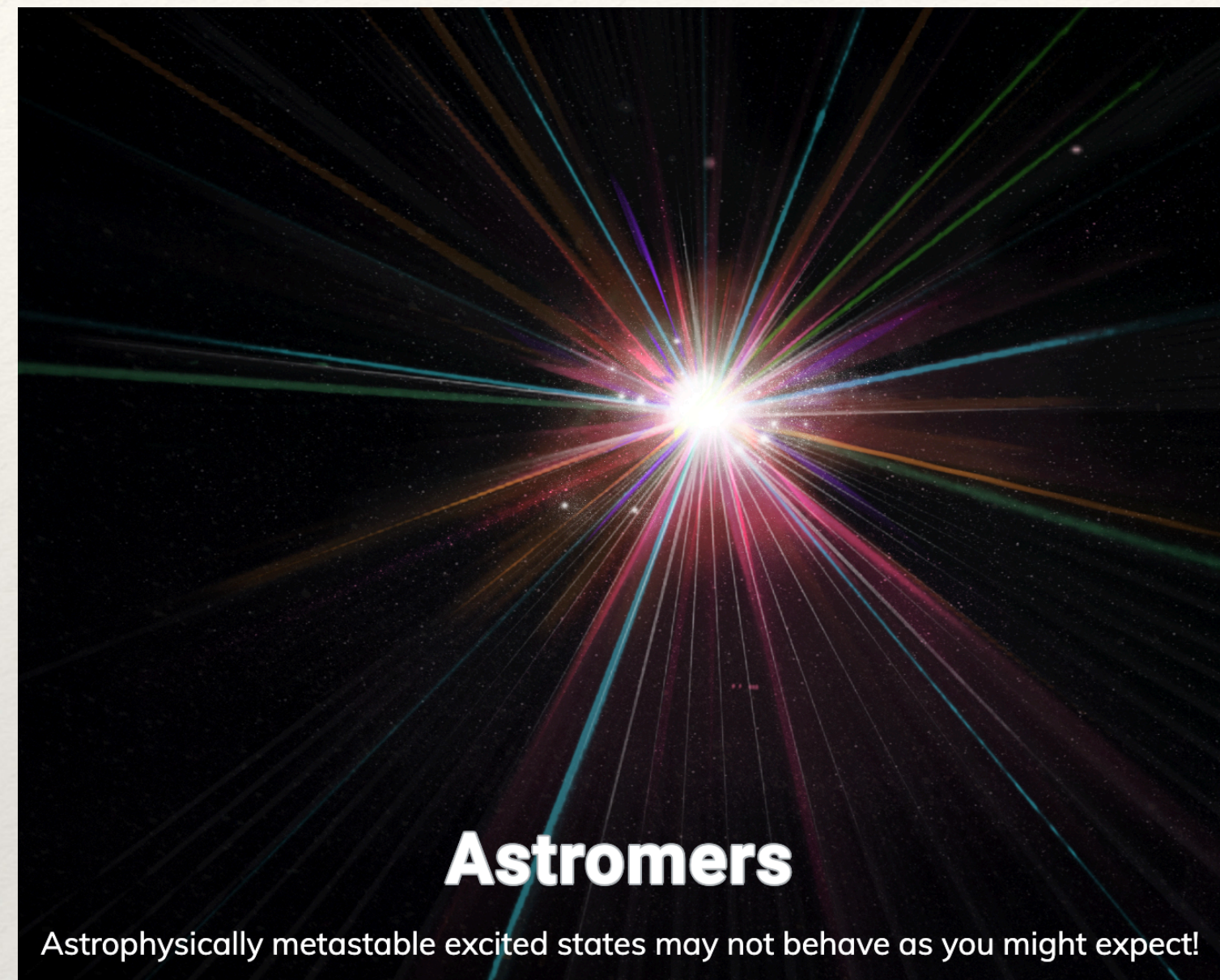
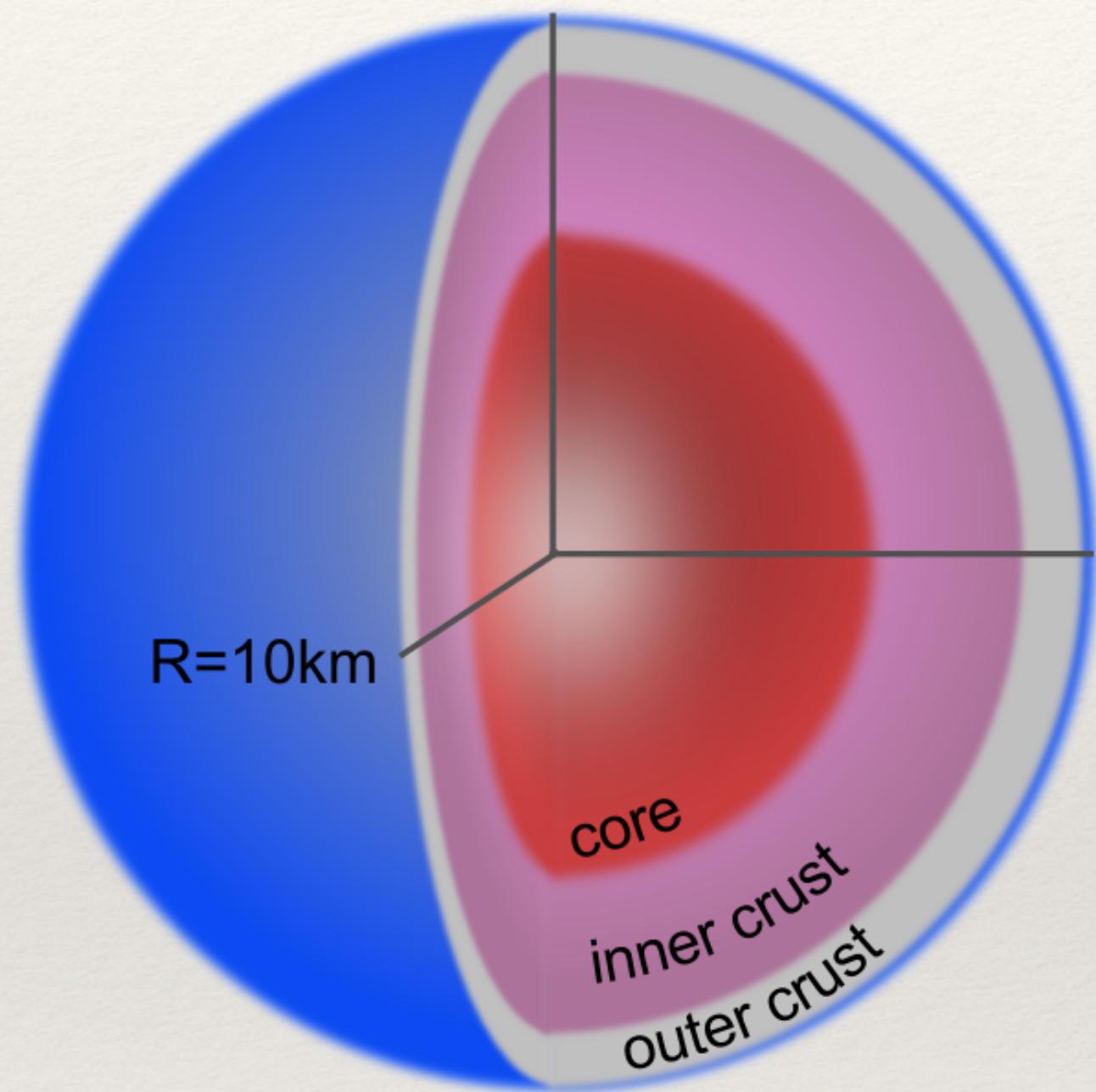
1 H	big bang fusion 										cosmic ray fission 					2 He						
3 Li	4 Be	merging neutron stars 										exploding massive stars 					5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg	dying low mass stars 										exploding white dwarfs 					13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr					
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe					
55 Cs	56 Ba	72 Hf		73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn					
87 Fr	88 Ra																					
		57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu						
		89 Ac	90 Th	91 Pa	92 U																	

Graphic created by Jennifer Johnson

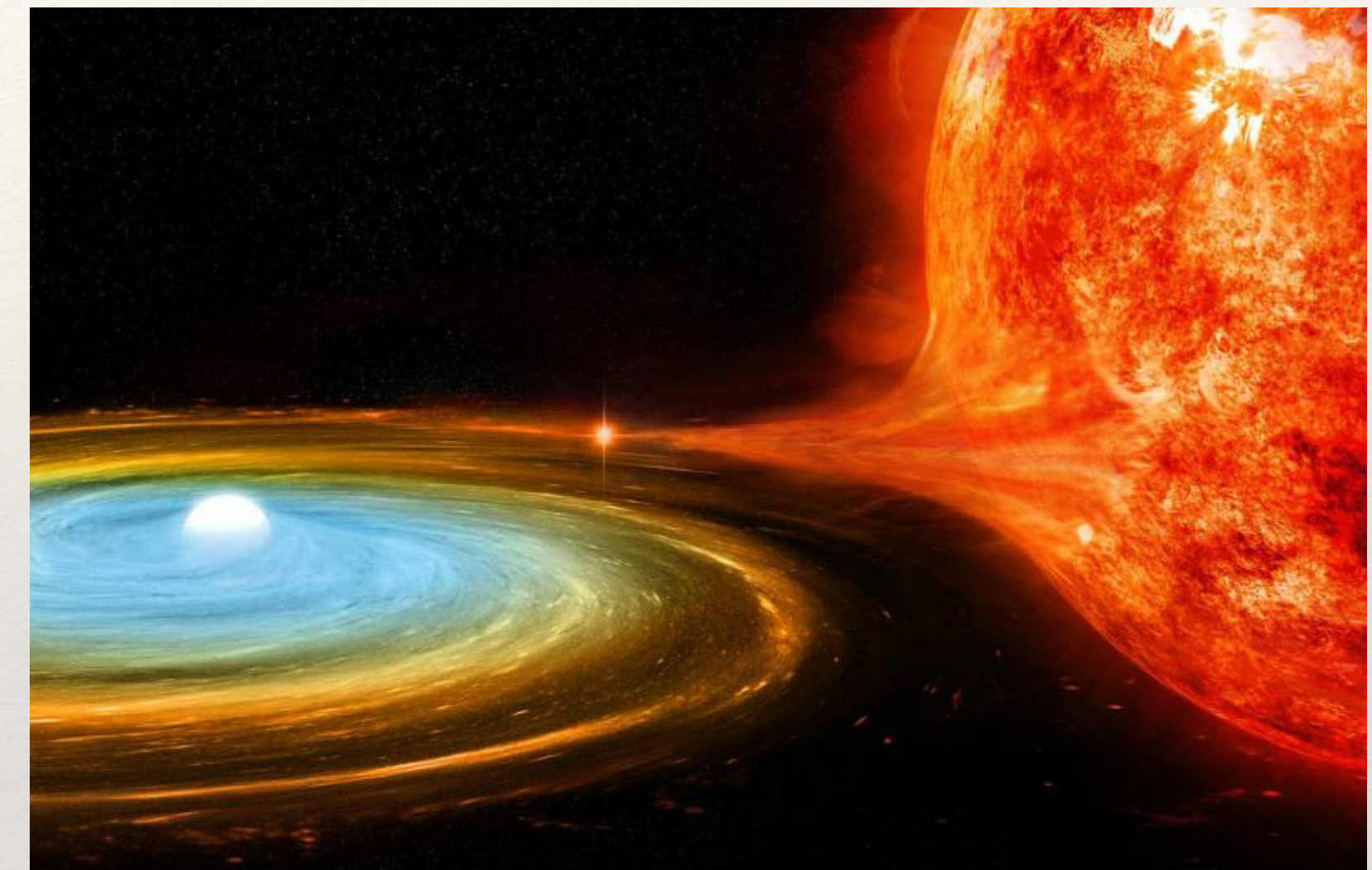
Astronomical Image Credits:
ESA/NASA/AASNova

Other topics

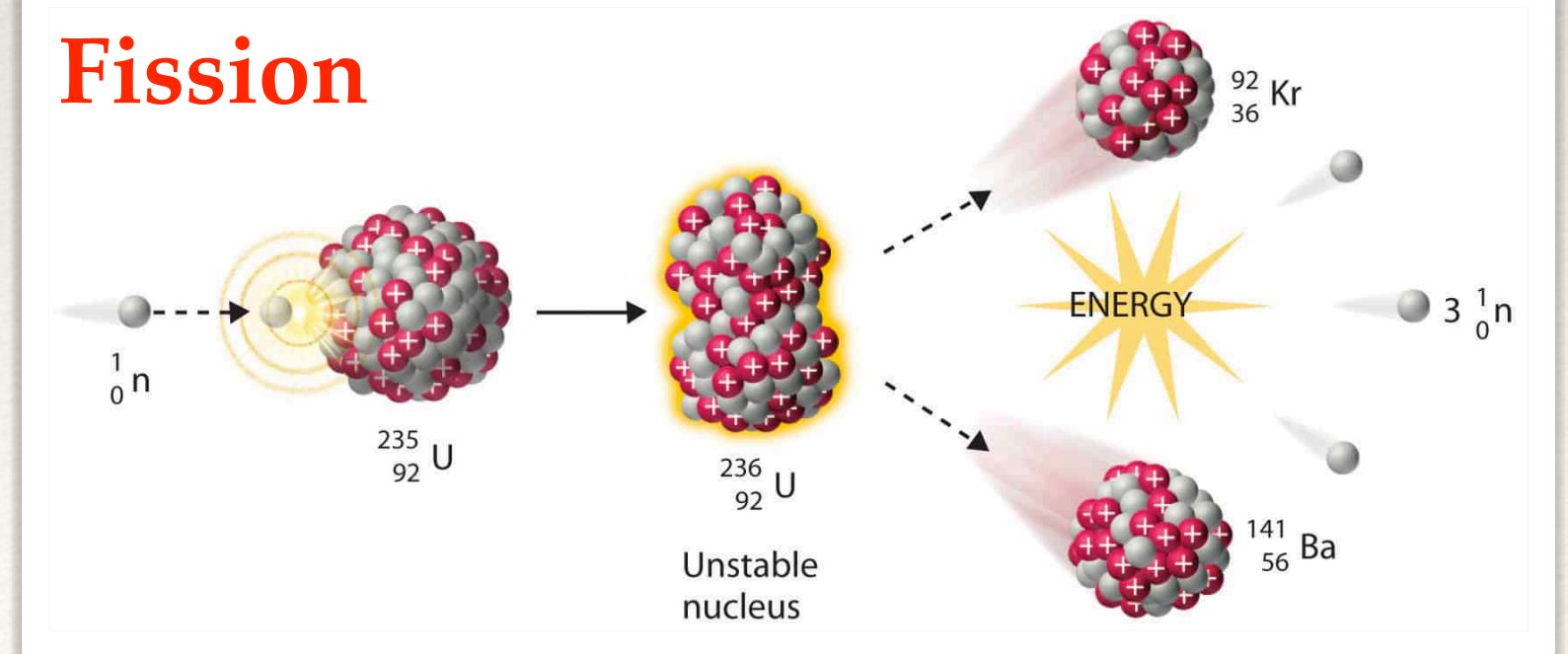
Neutron stars structure



rp-process (Type I X-ray Bursts)

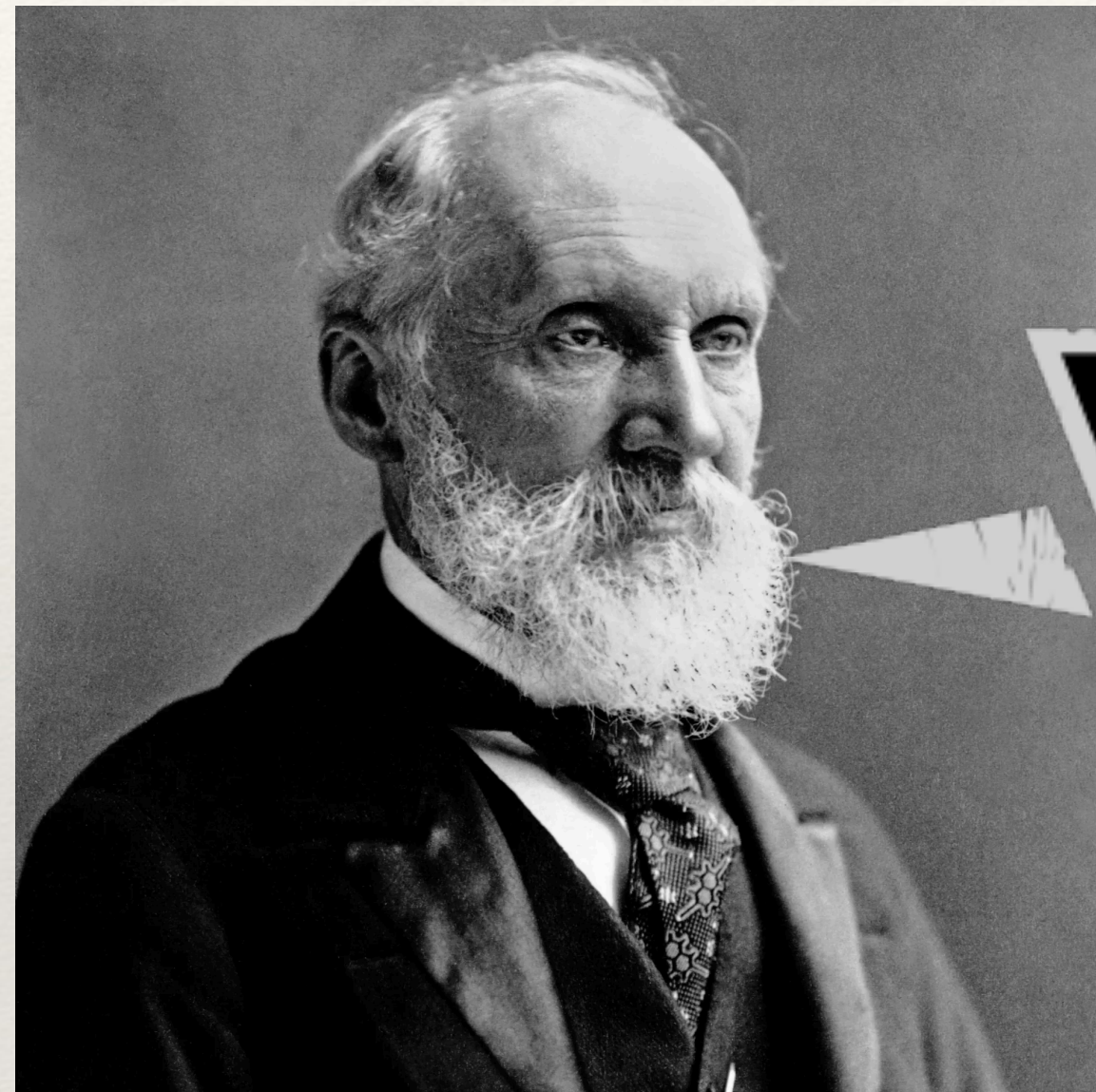


Fission



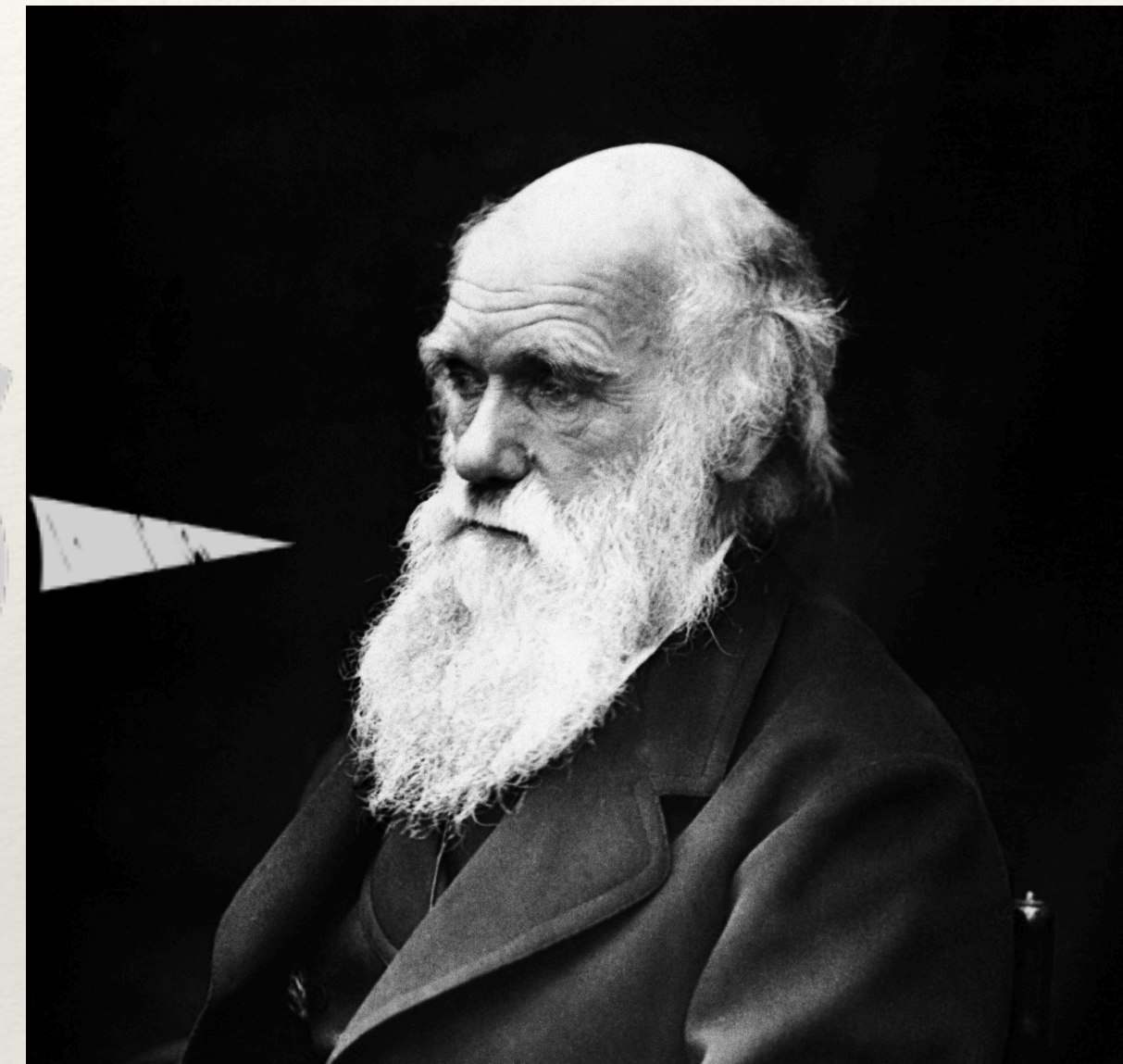
Age of the Earth crisis 1800s

Kelvin



Age of Sun: 20 million years

Darwin

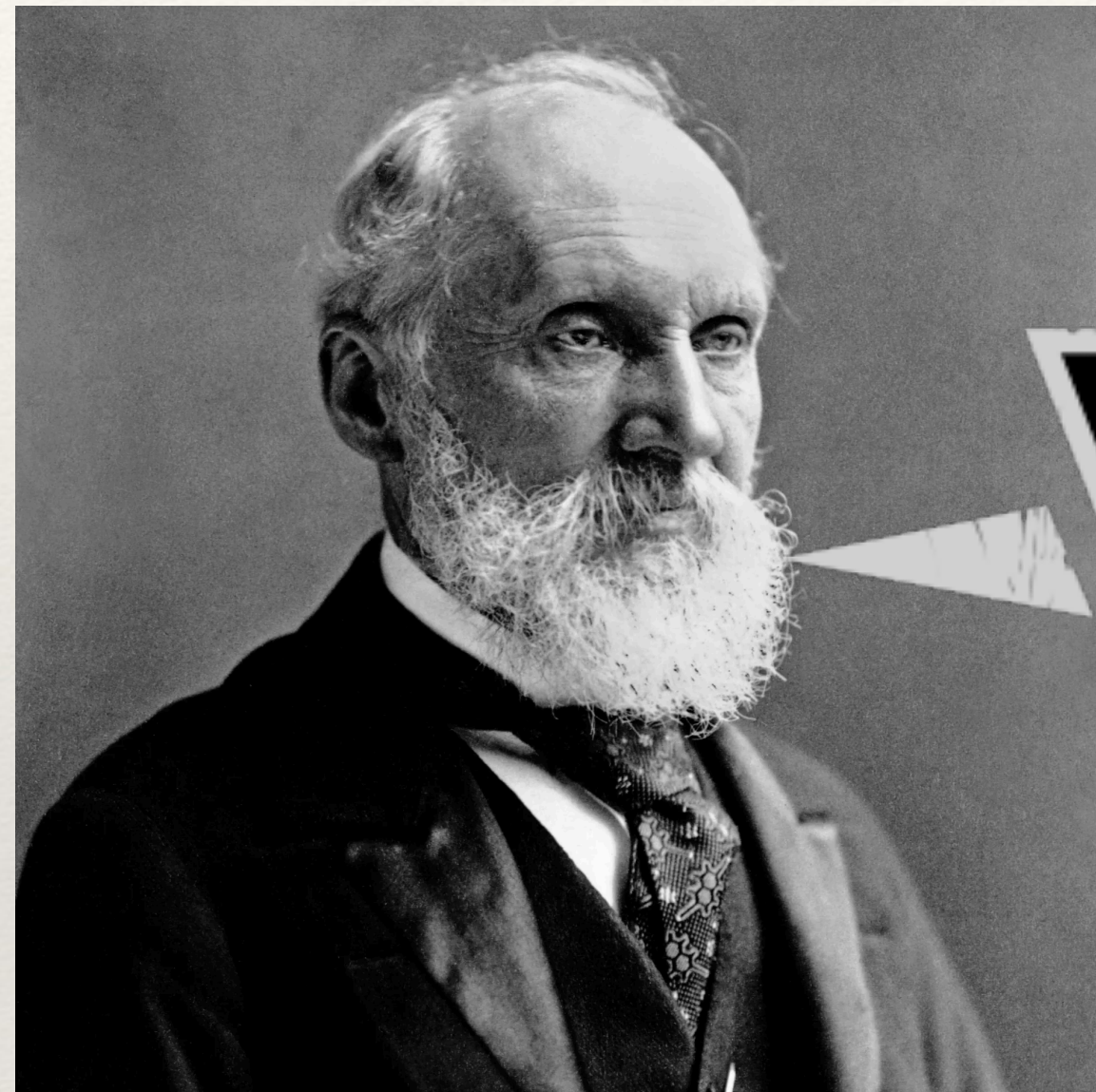


**Age of Earth: few 100s million years
Following geologist's estimation**



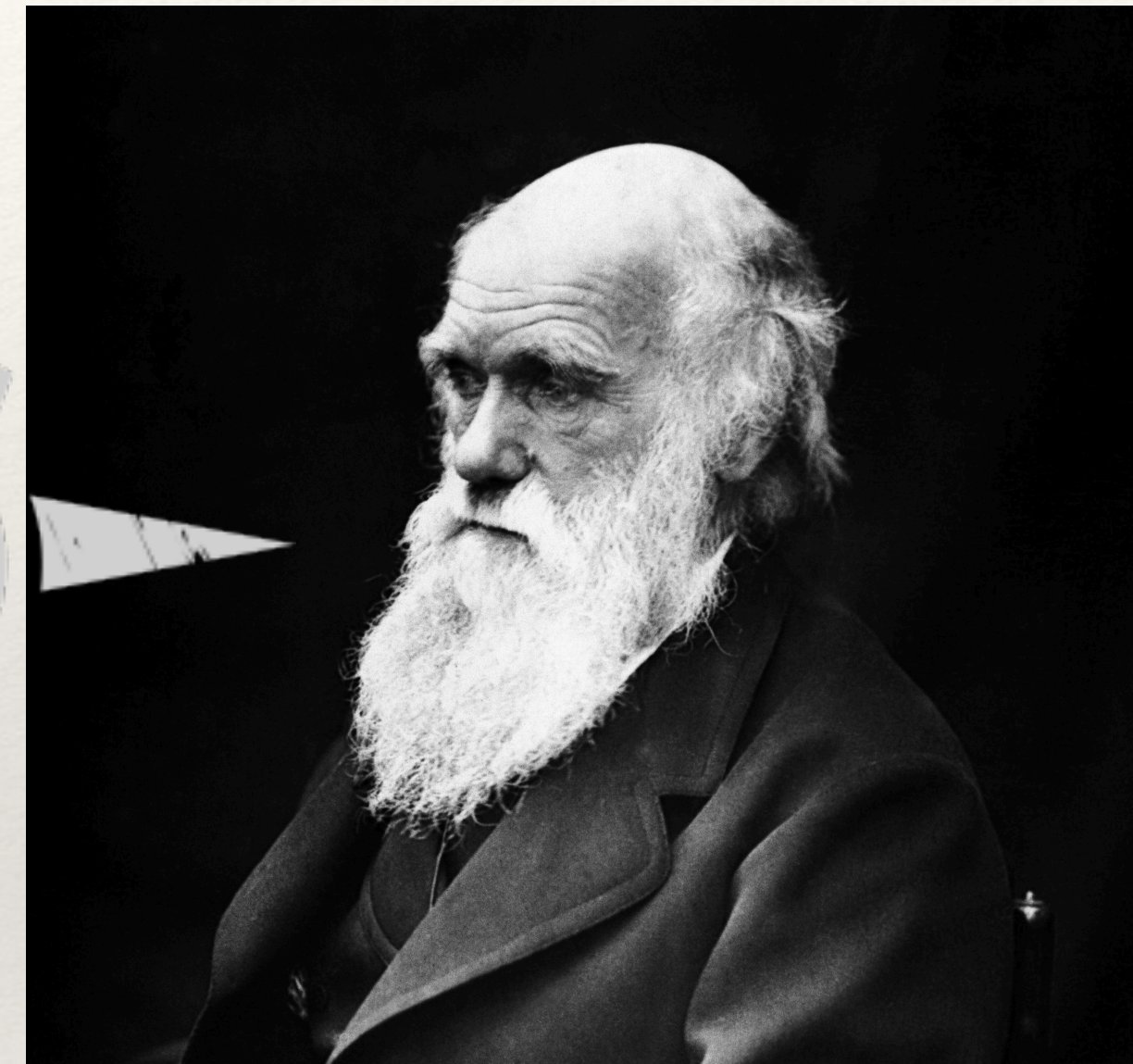
Age of the Earth crisis 1800s

Kelvin



Age of Sun: 20 million years

Darwin

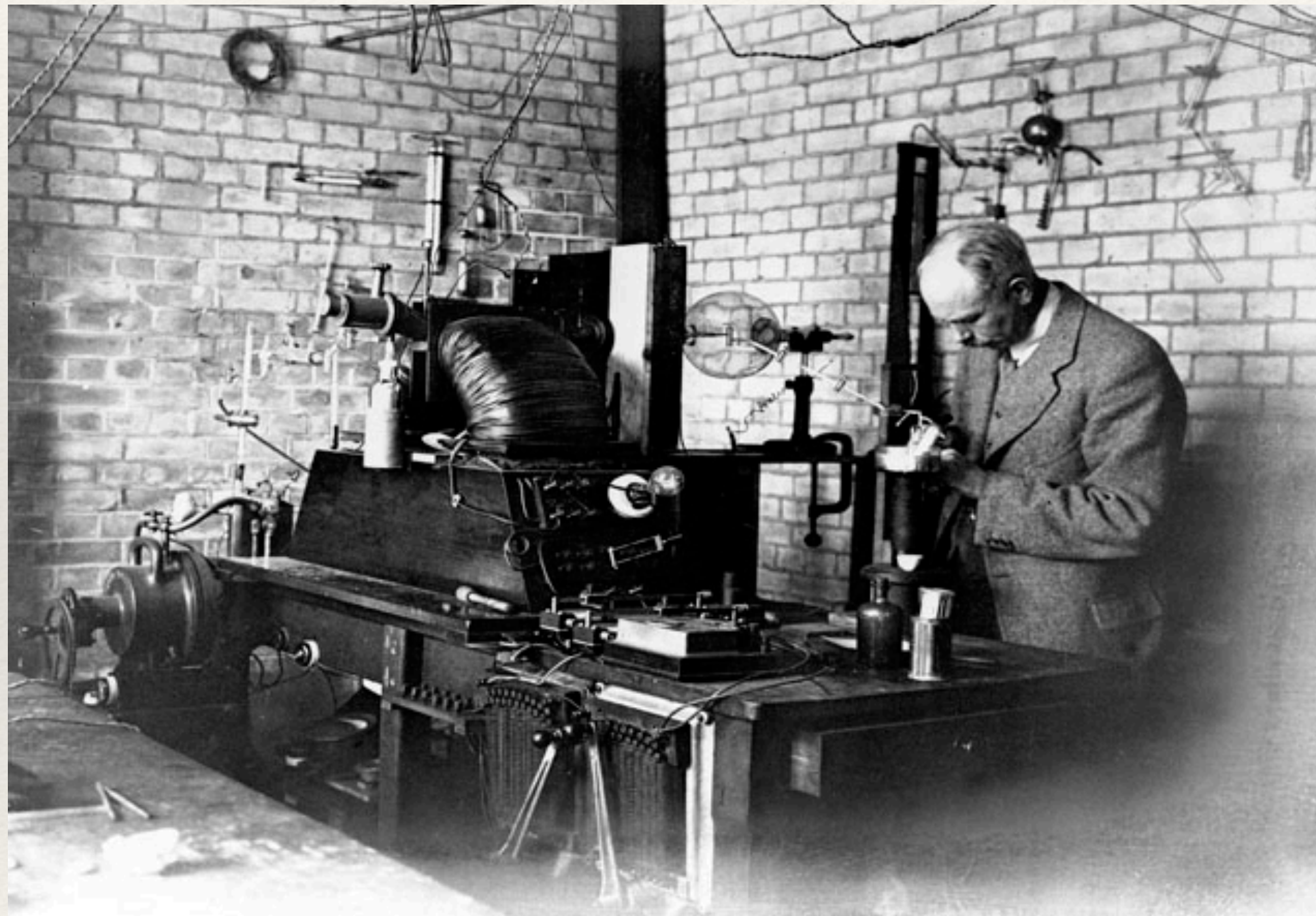


Age of Earth: few 100s million years
Following geologist's estimation

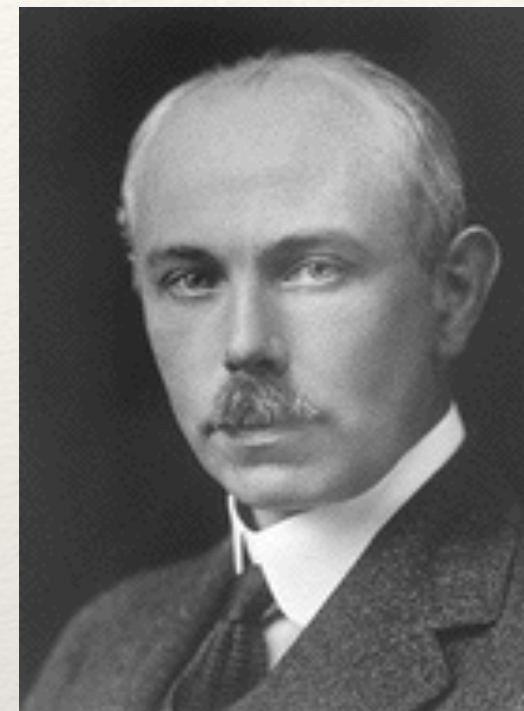


Discovery Atomic Mass defect

First Mass Spectrograph



F.W. Aston



Discovering about 200 isotopes

$$M_H = 1.008 \text{ u}$$

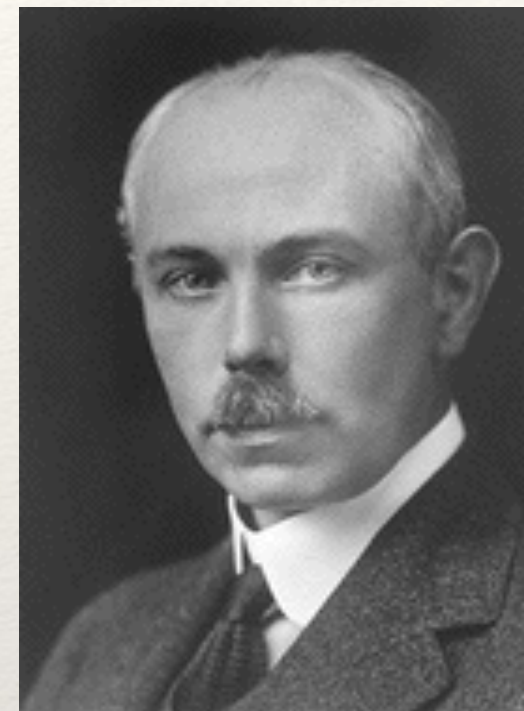
Discovery Atomic Mass defect

First Mass Spectrograph

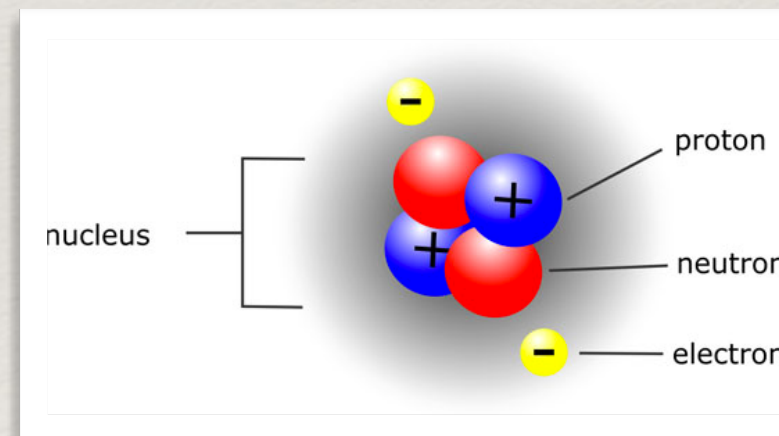


$$M_H = 1.008 \text{ u}$$

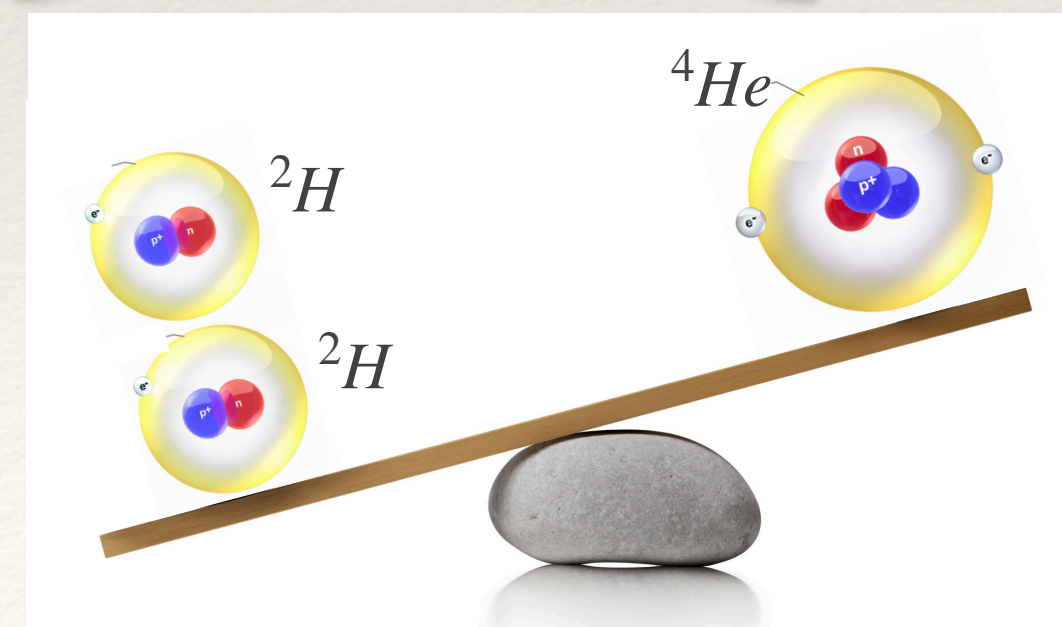
F.W. Aston



Discovering about 200 isotopes



$$M(^4\text{He}) = 2 \cdot m_p + 2 \cdot m_n + 2 \cdot m_e - \text{Binding Energy}$$



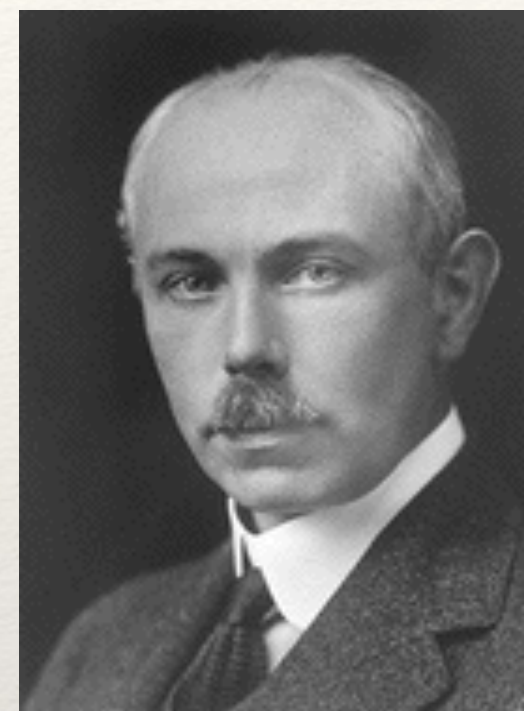
Discovery Atomic Mass defect

First Mass Spectrograph

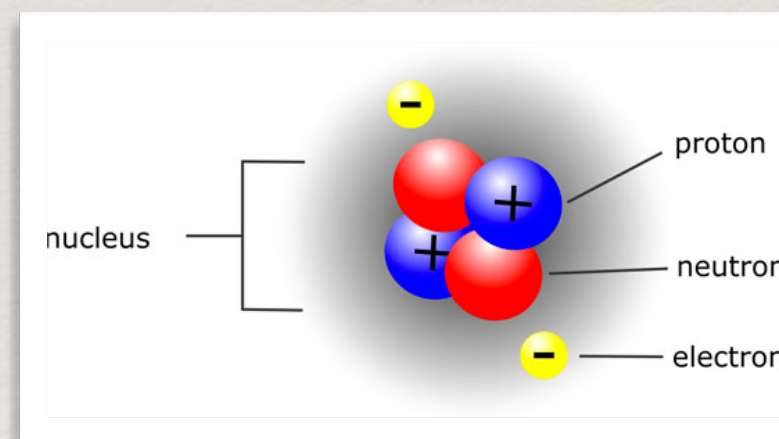


$$M_H = 1.008 \text{ u}$$

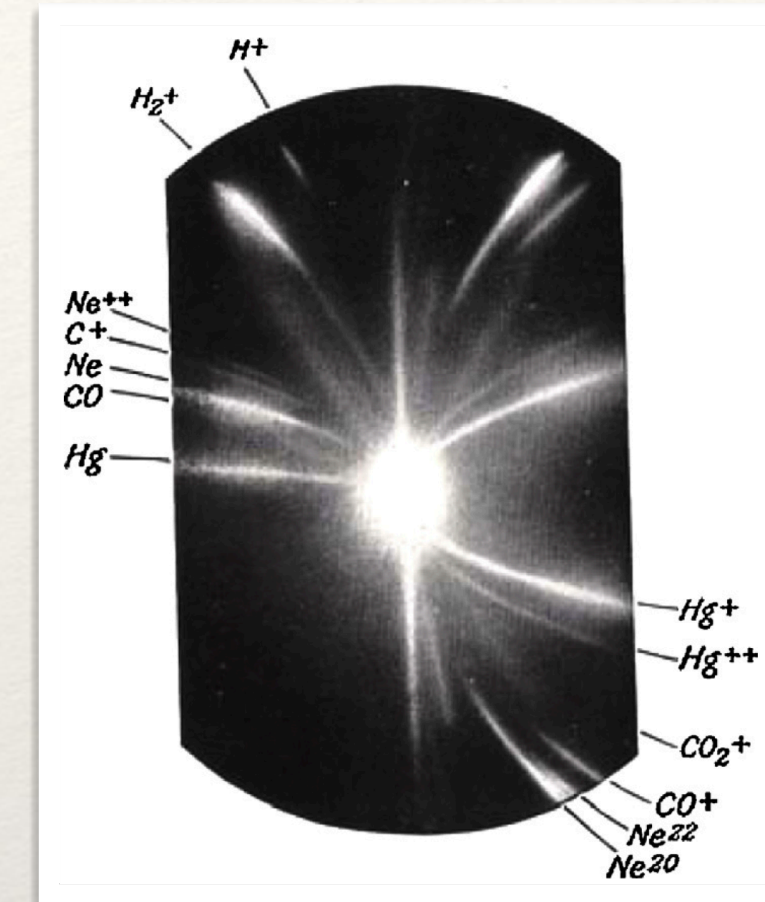
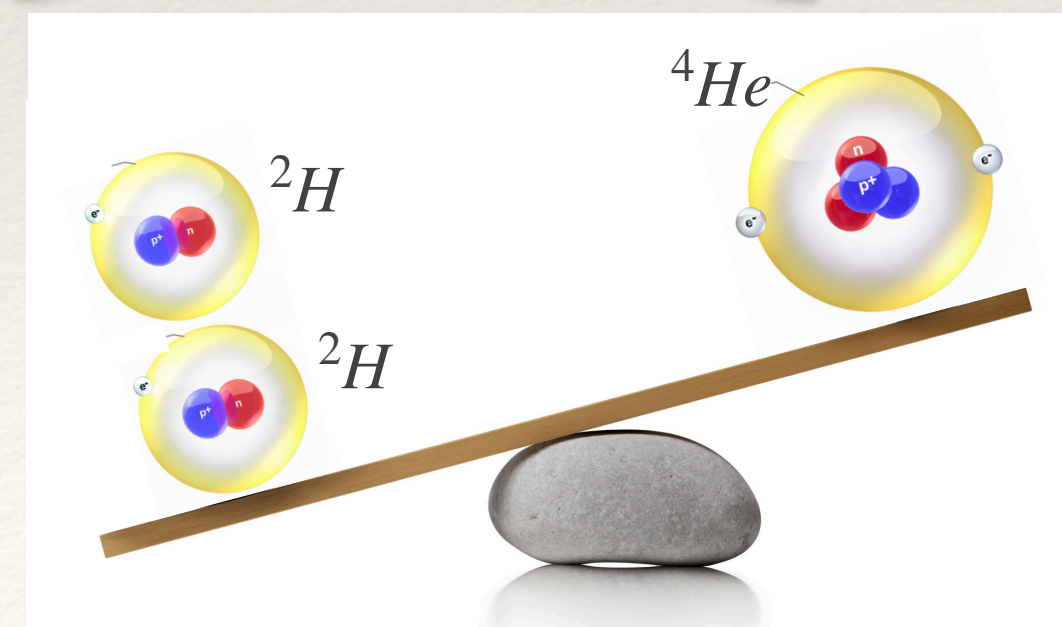
F.W. Aston



Discovering about 200 isotopes



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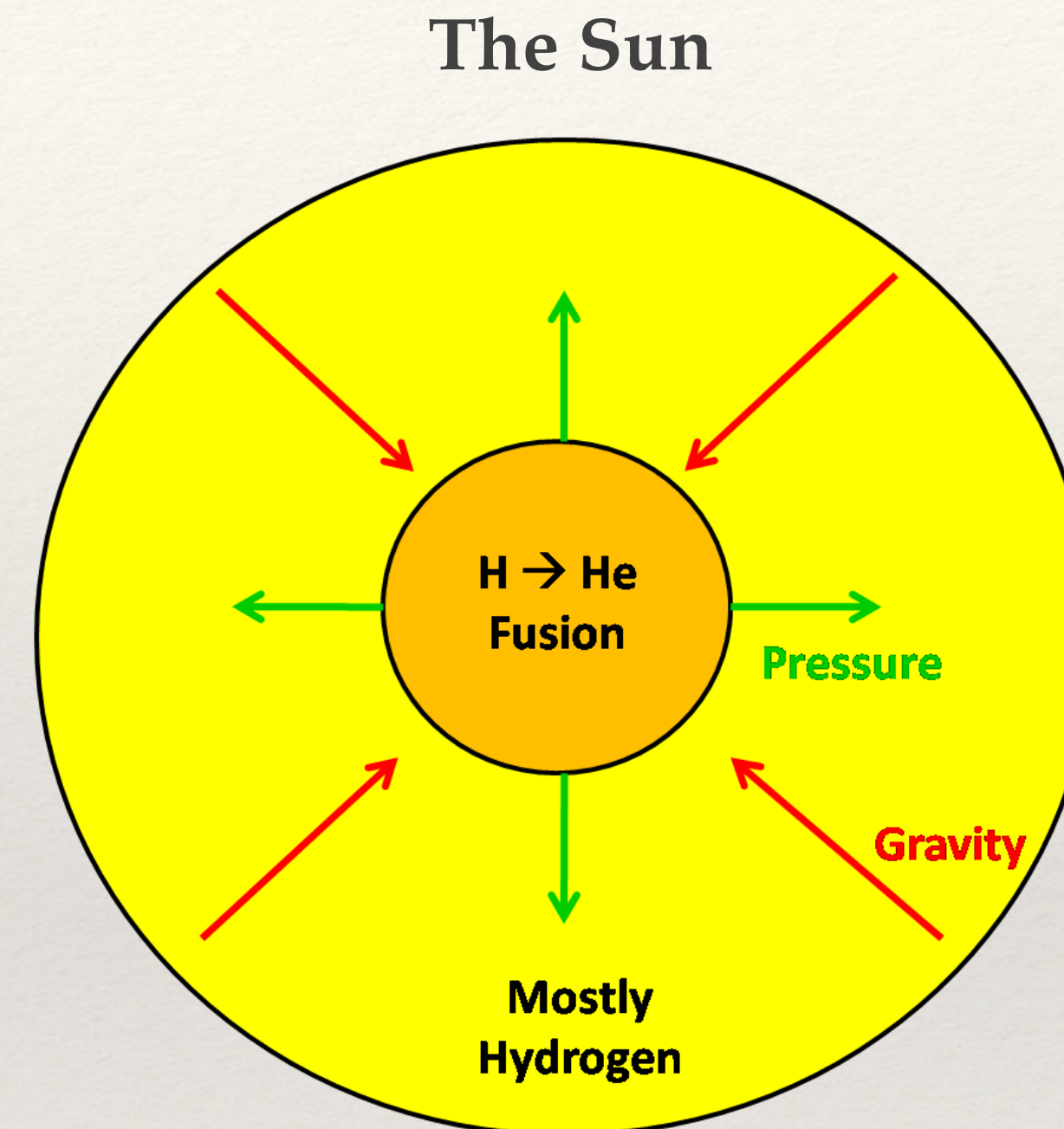


1913 discovery of isotopes (Ne)



Solving the age of the Earth crisis

Eddington

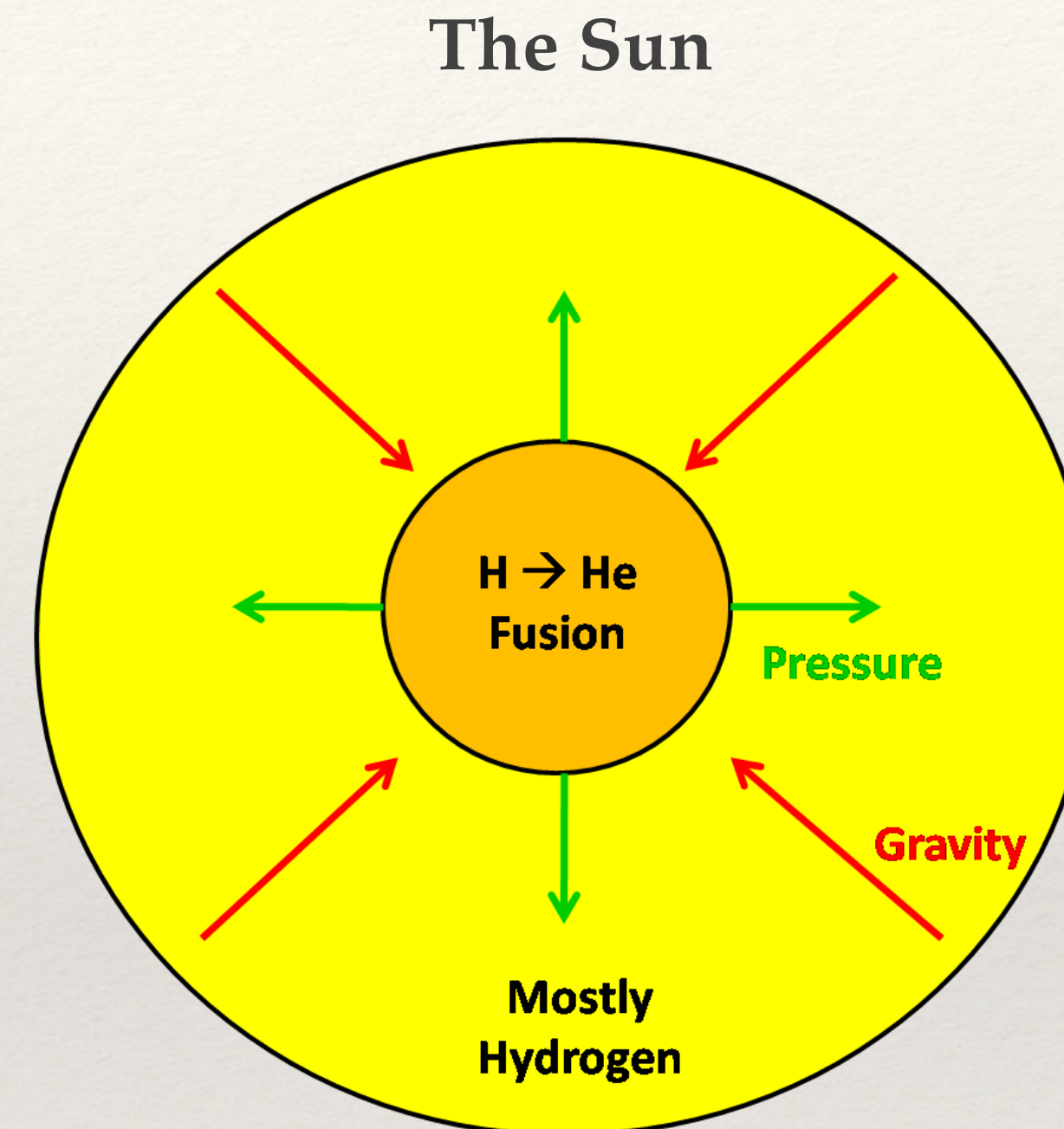


$$\text{Lifetime} = \frac{\text{Energy}}{\text{Luminosity}} = \frac{Mc^2}{L_{\text{sun}}} = \frac{0.007 \cdot 0.1 \cdot M_{\text{sun}} \cdot c^2}{L_{\text{sun}}} \approx 10 \text{ Billion years}$$

$$[L_{\text{sun}}] = E/t$$

Solving the age of the Earth crisis

Eddington



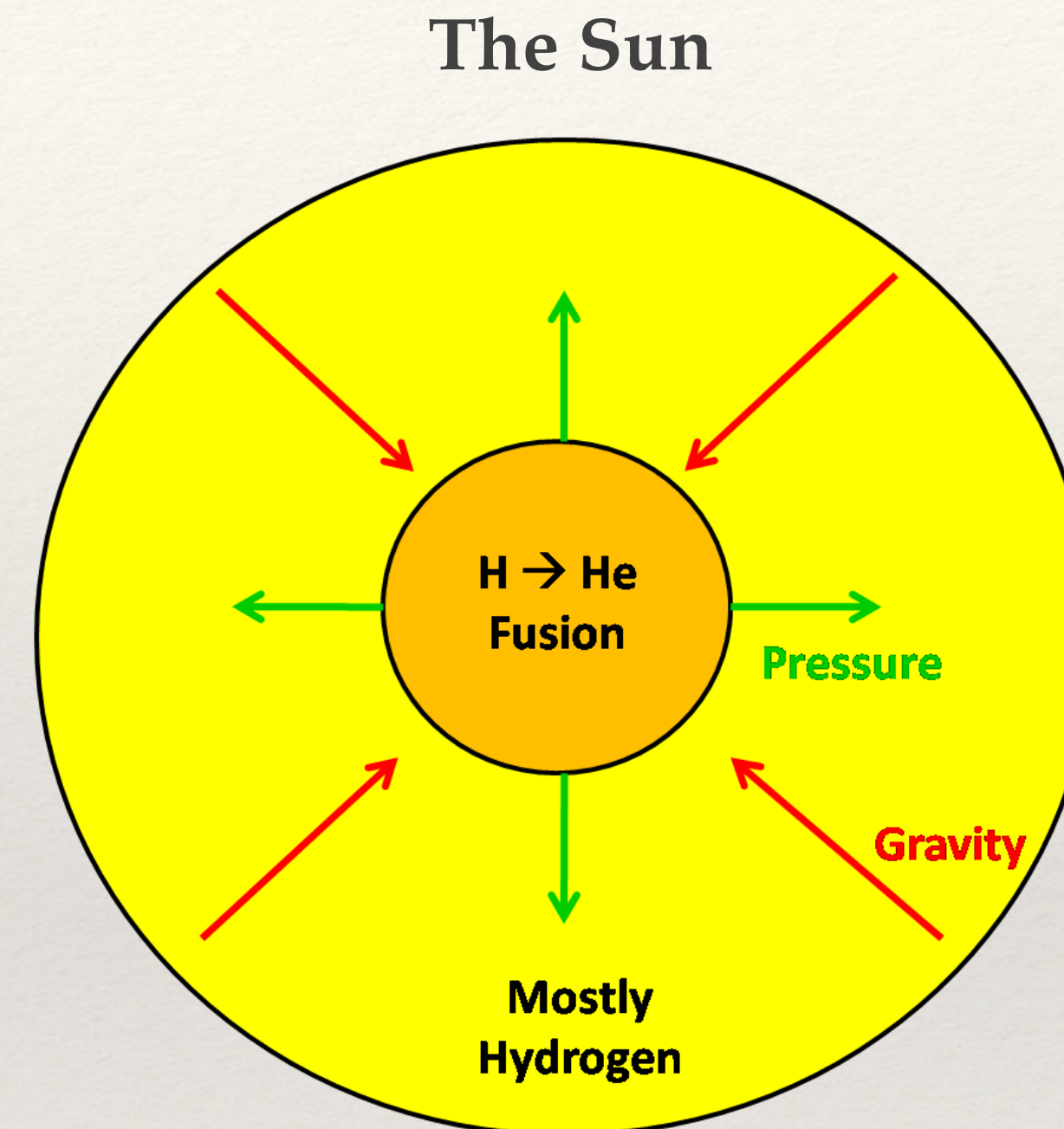
$$\text{Lifetime} = \frac{\text{Energy}}{\text{Luminosity}} = \frac{Mc^2}{L_{sun}} = \frac{0.007 \cdot 0.1 \cdot M_{sun} \cdot c^2}{L_{sun}} \approx 10 \text{ Billion years}$$

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10% of the Sun undergo fusion

Solving the age of the Earth crisis

Eddington



$$\text{Lifetime} = \frac{\text{Energy}}{\text{Luminosity}} = \frac{Mc^2}{L_{\text{sun}}} = \frac{0.007 \cdot 0.1 \cdot M_{\text{sun}} \cdot c^2}{L_{\text{sun}}} \approx 10 \text{ Billion years}$$

$$[L_{\text{sun}}] = E/t$$

10% of the Sun undergo fusion

0.7% atomic mass difference between 4xH and ⁴He

Nier's mass spectrometer

Transition from Spectrograph to Spectrometer



A. O. Nier 1951, Phys. Rev 81, 507

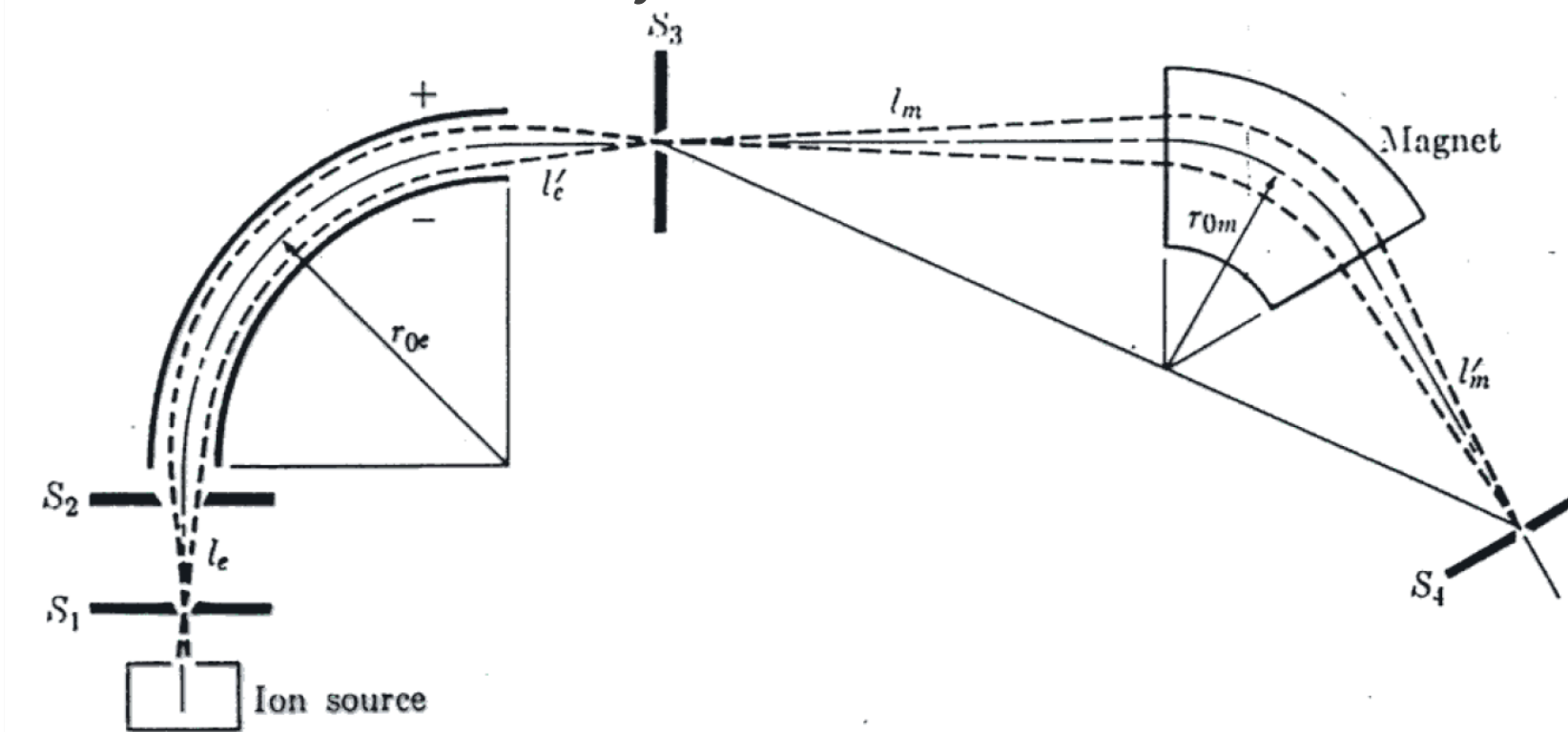


Fig. 4-3. Principle of operation of Nier's spectrograph.

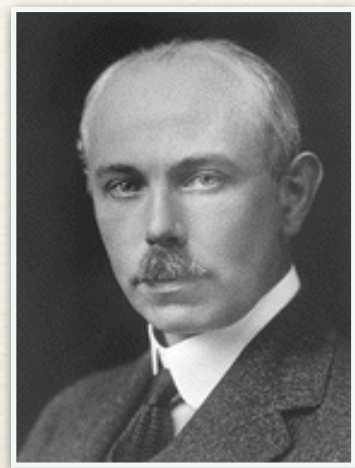


For NASA

Large impact in many areas:

- Geochronology
 - ^{40}K discovery \rightarrow K-Ar Geochronology
 - Age of the earth from U,Th-Pb technique
- Stable isotope geochemistry
- Nuclear physics (U isotopic separation \rightarrow fission 1st controlled nuclear chain reaction)
- Extra-terrestrial materials (Mars & Venus Atmosphere)

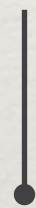
Atomic Masses & Nuclear Physics Discoveries



F.W. Aston

Mass defect

$$M_H = 1.008 \text{ u}$$



1919

1933-1934

1948

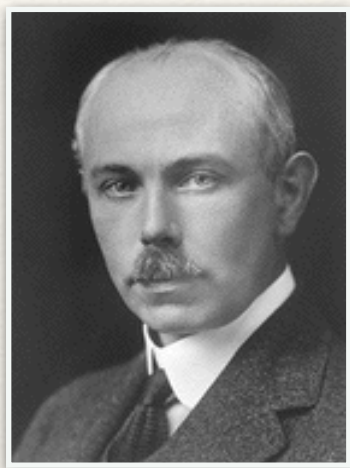
1951

1954

1974



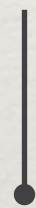
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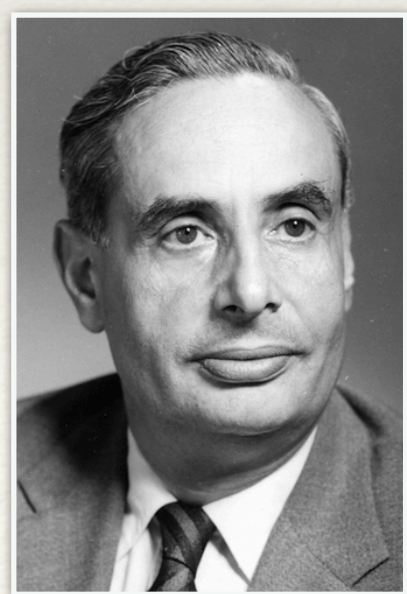
1948

1951

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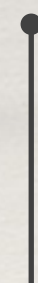
W. Elsasser



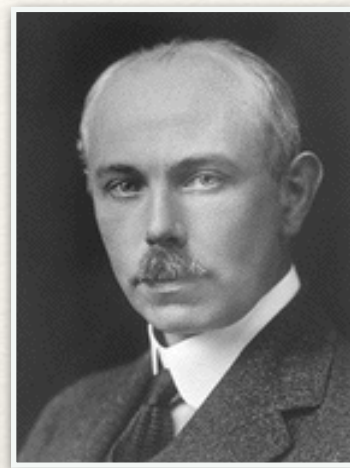
Discovery of
magic numbers

$$Z=2,8,20,28,50$$

$$N=126,82$$



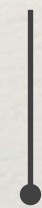
Atomic Masses & Nuclear Physics Discoveries



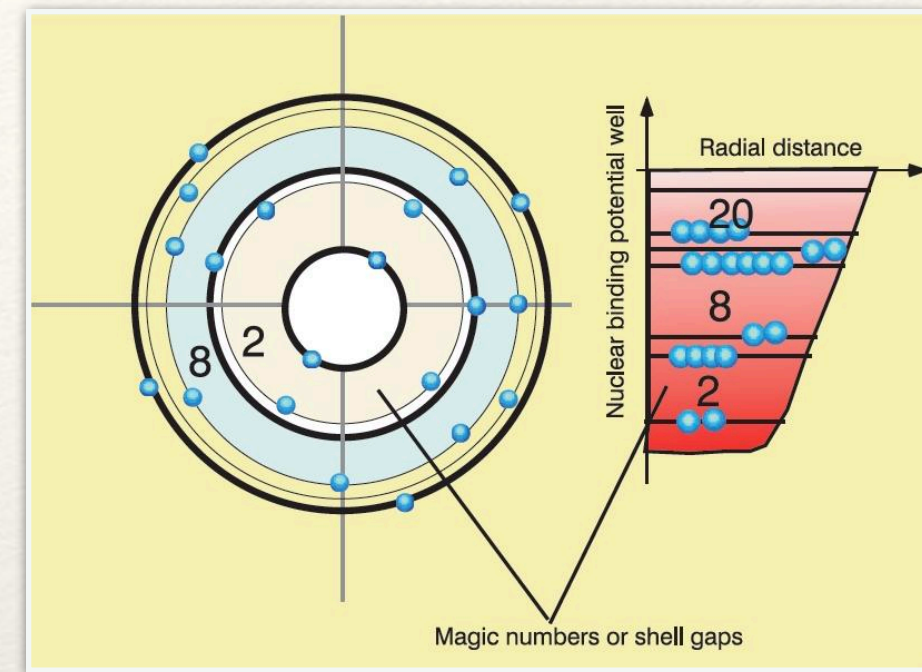
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Mass defect

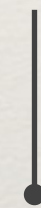
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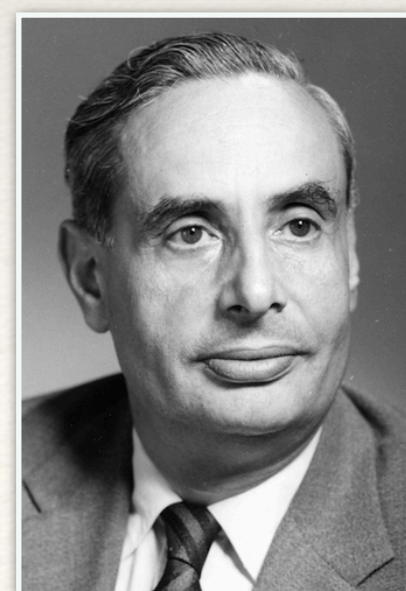


Nuclear Shell Model



1948

W. Elsasser



Discovery of
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$$Z=2,8,20,28,50$$

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Goeppert-Mayer

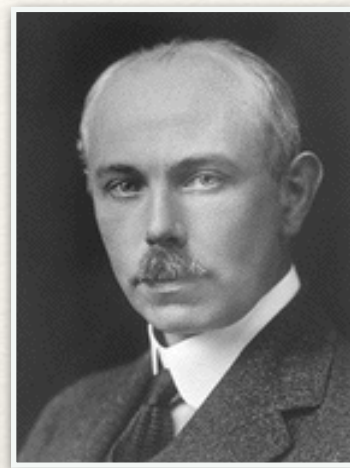


1951

1954

1974

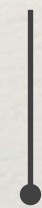
Atomic Masses & Nuclear Physics Discoveries



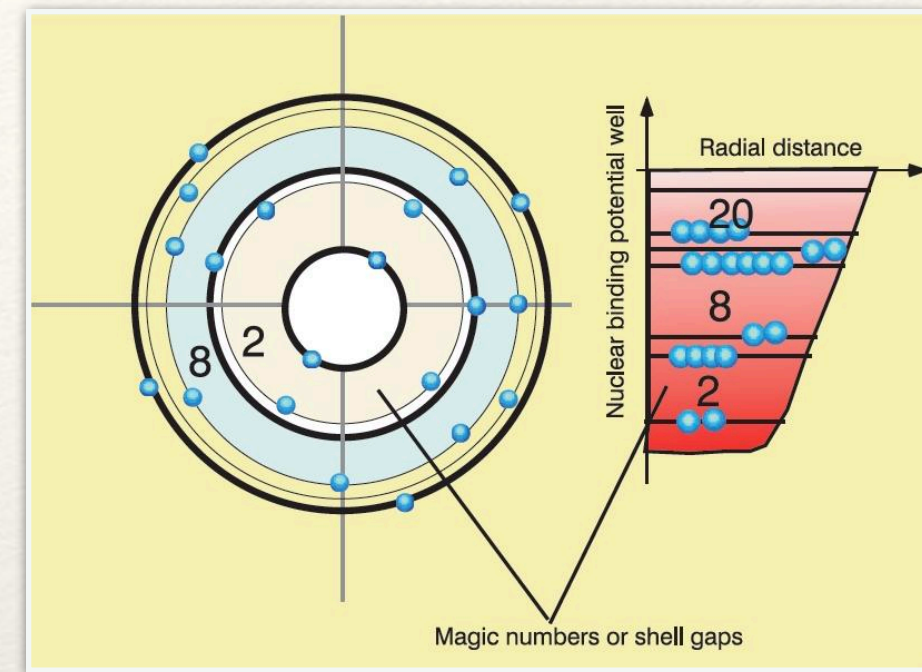
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Mass defect

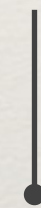
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1919



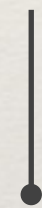
Nuclear Shell Model



1948



Nier's spectrometry

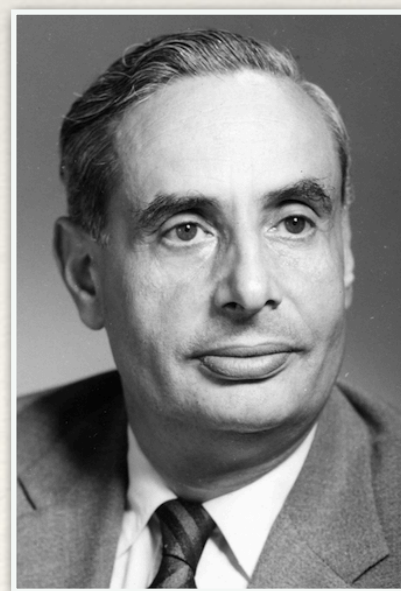


1951

1954

1974

W. Elsasser



Discovery of **magic numbers**

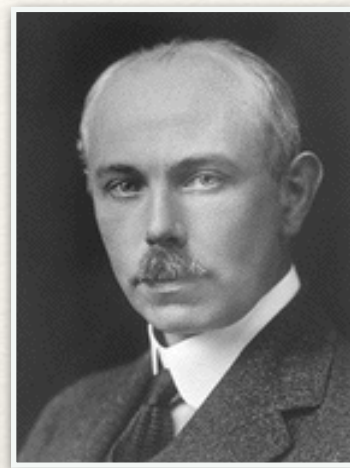
$$Z=2,8,20,28,50$$

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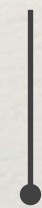
Atomic Masses & Nuclear Physics Discoveries



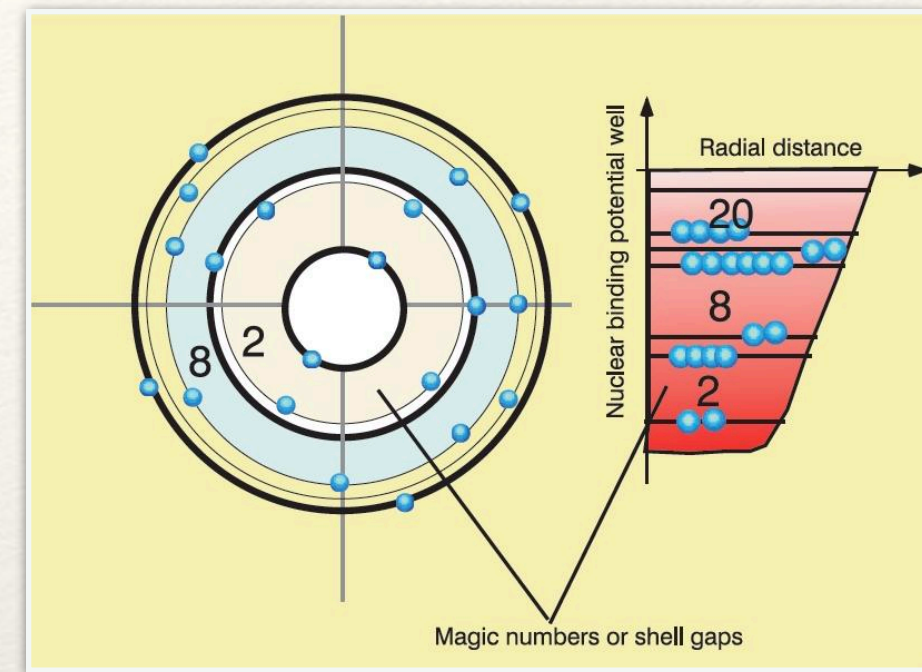
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Mass defect

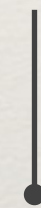
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1919



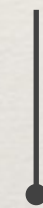
Nuclear Shell Model



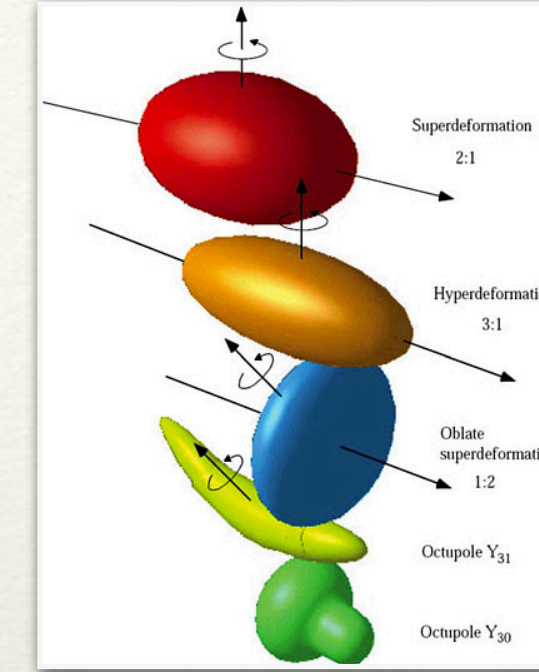
1948



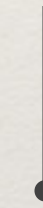
Nier's spectrometry



1951



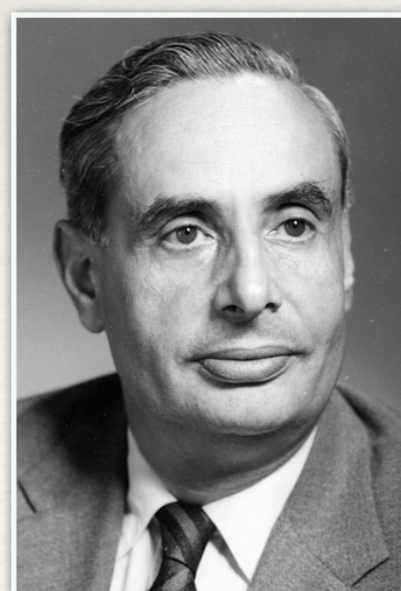
Nuclear deformation at N=90



1954

1974

W. Elsasser



Discovery of **magic numbers**

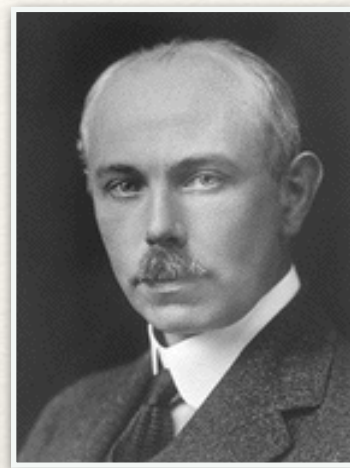
$$Z=2,8,20,28,50$$

$$N=126,82$$

Goeppert-Mayer



Atomic Masses & Nuclear Physics Discoveries

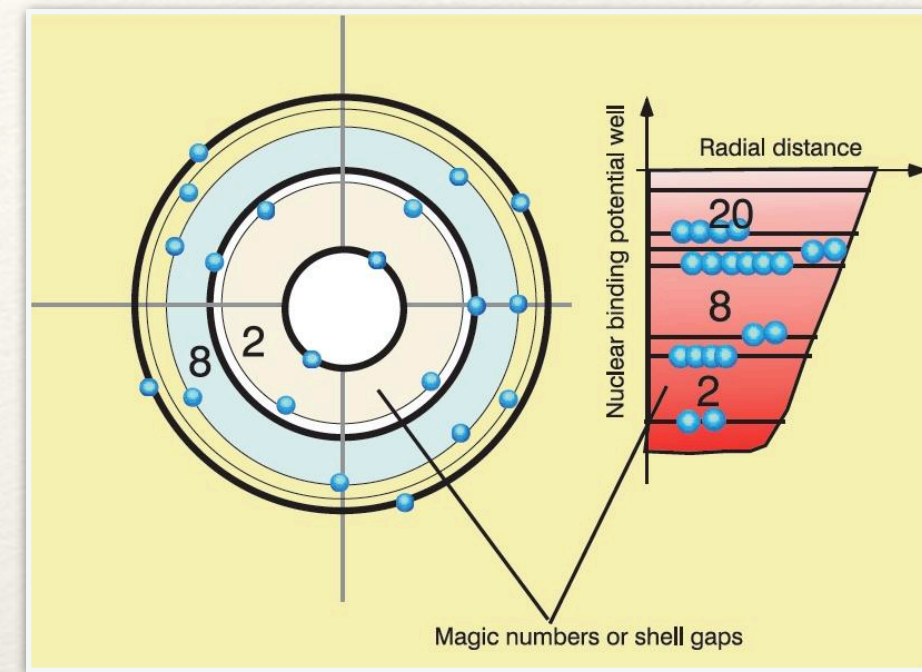


F.W. Aston

Mass defect

$$M_H = 1.008 \text{ u}$$

1919



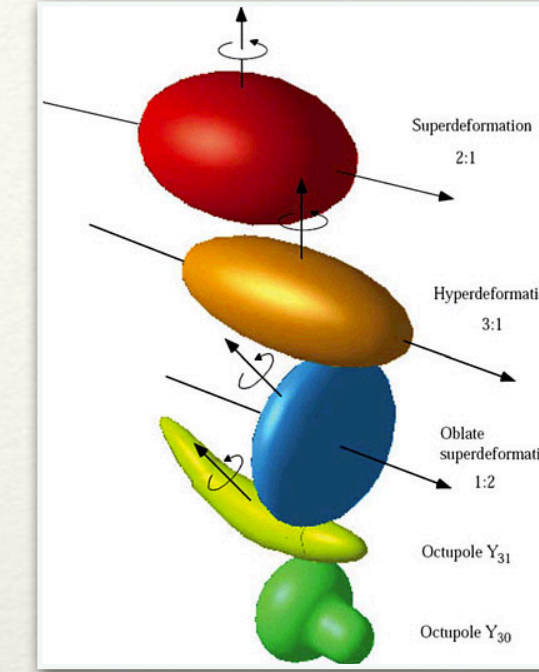
Nuclear Shell Model

1948



Nier's spectrometry

1951

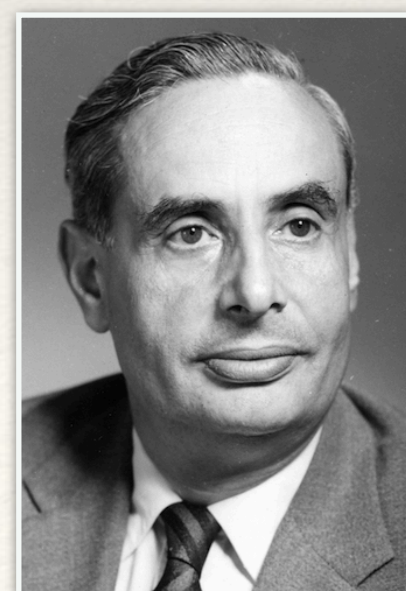


Nuclear deformation at N=90

1954

1974

W. Elsassner



Discovery of **magic numbers**

$$Z=2,8,20,28,50$$

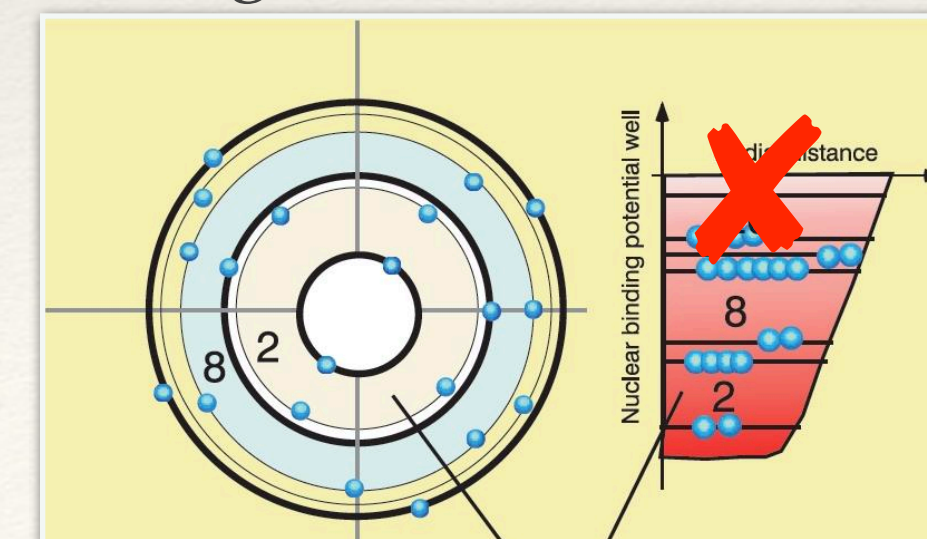
$$N=126,82$$

1933-1934

Goeppert-Mayer

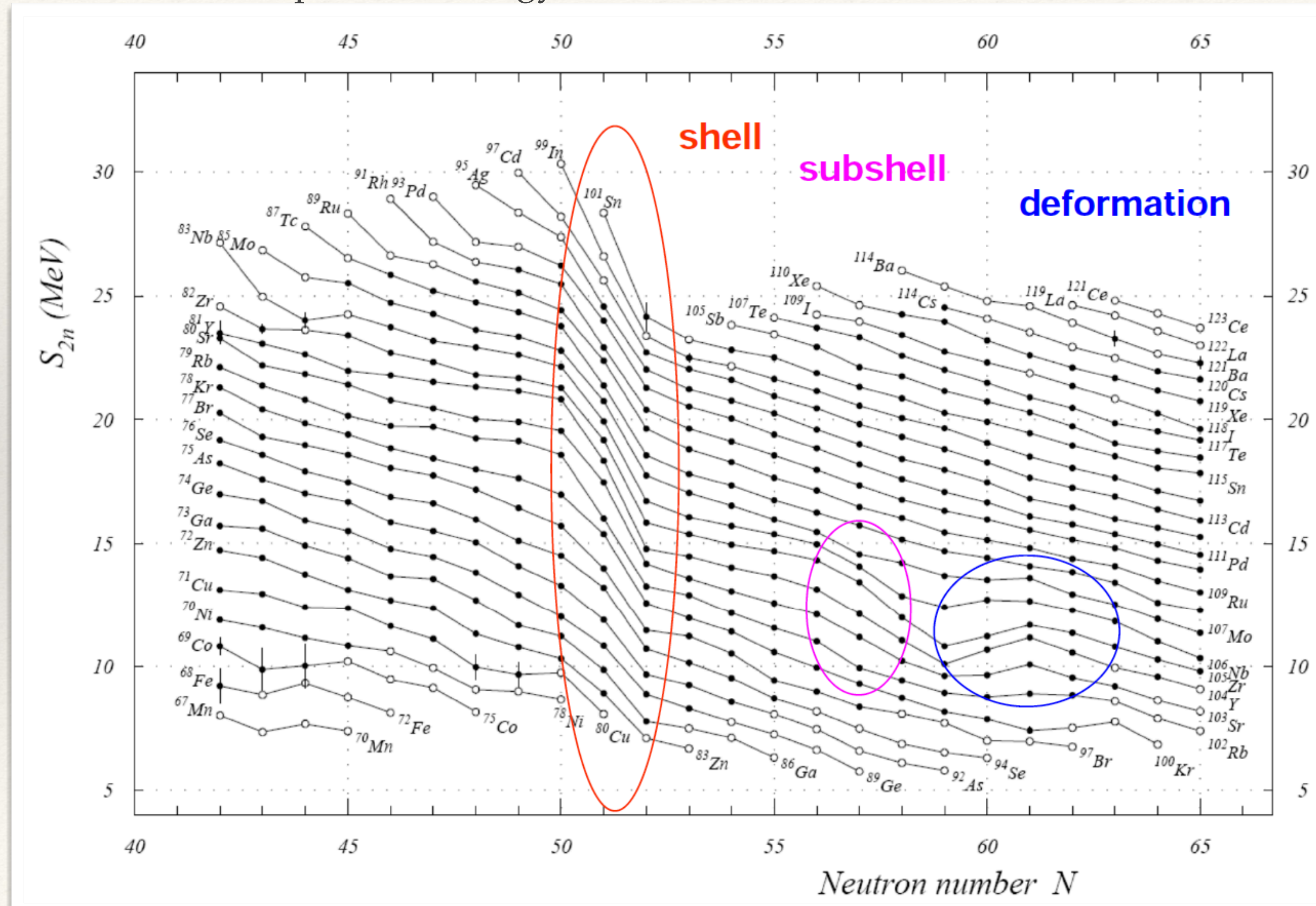


Disappearance of magic number N=20

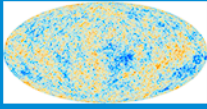
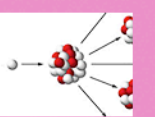
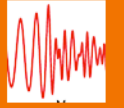





Nuclear Structure from Atomic Masses

Two neutron separation energy $S_{2n}(Z, N) = B(Z, N) - B(Z, N - 2)$



The Origin of the Solar System Elements

1 H	big bang fusion 										cosmic ray fission 					2 He						
3 Li	4 Be	merging neutron stars 										exploding massive stars 					5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg	dying low mass stars 										exploding white dwarfs 					13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr					
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe					
55 Cs	56 Ba		72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn					
87 Fr	88 Ra																					
			57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu					
			89 Ac	90 Th	91 Pa	92 U																

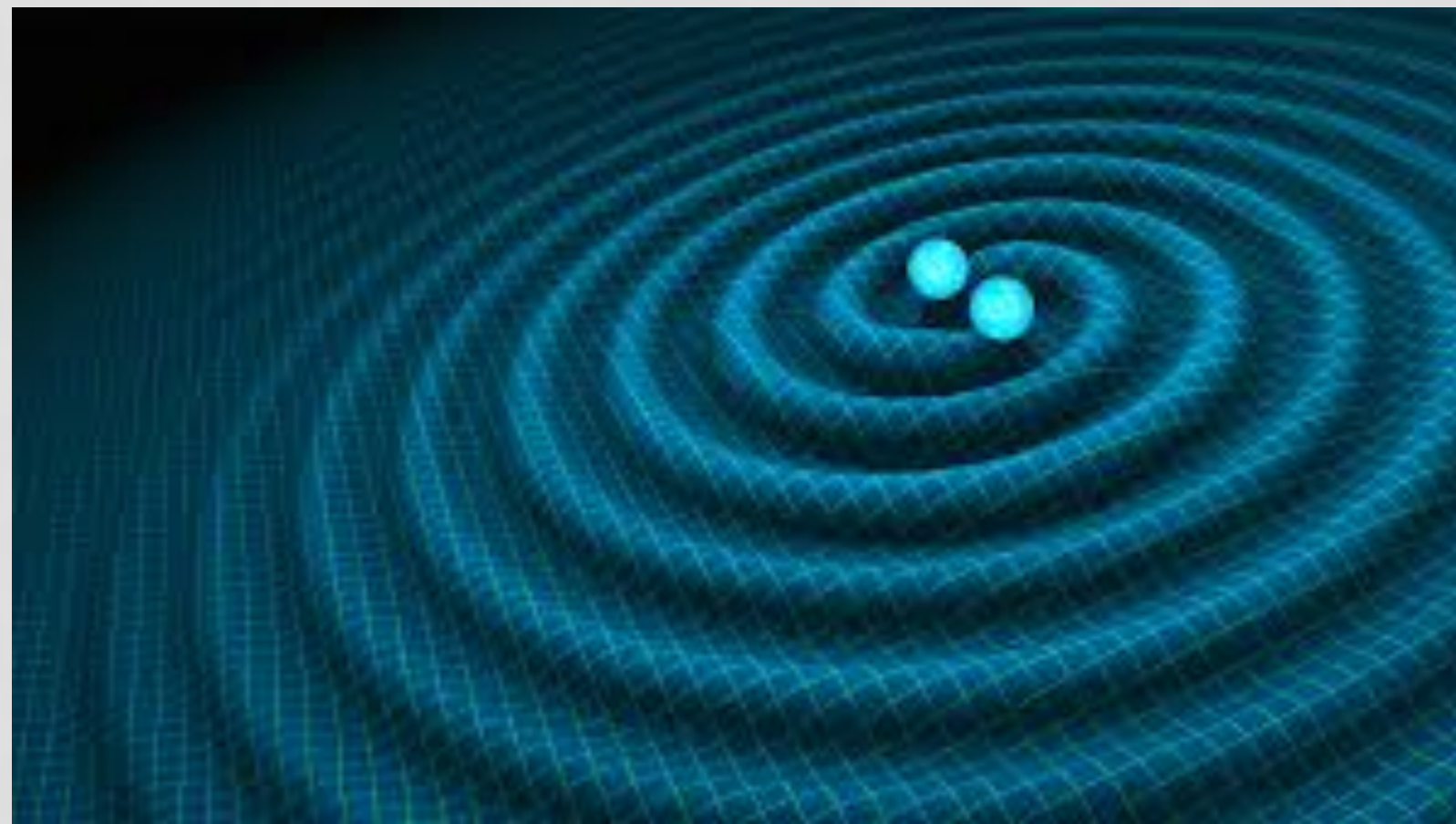
Graphic created by Jennifer Johnson

Astronomical Image Credits:
ESA/NASA/AASNova

GRAVITATIONAL WAVES DISCOVERY

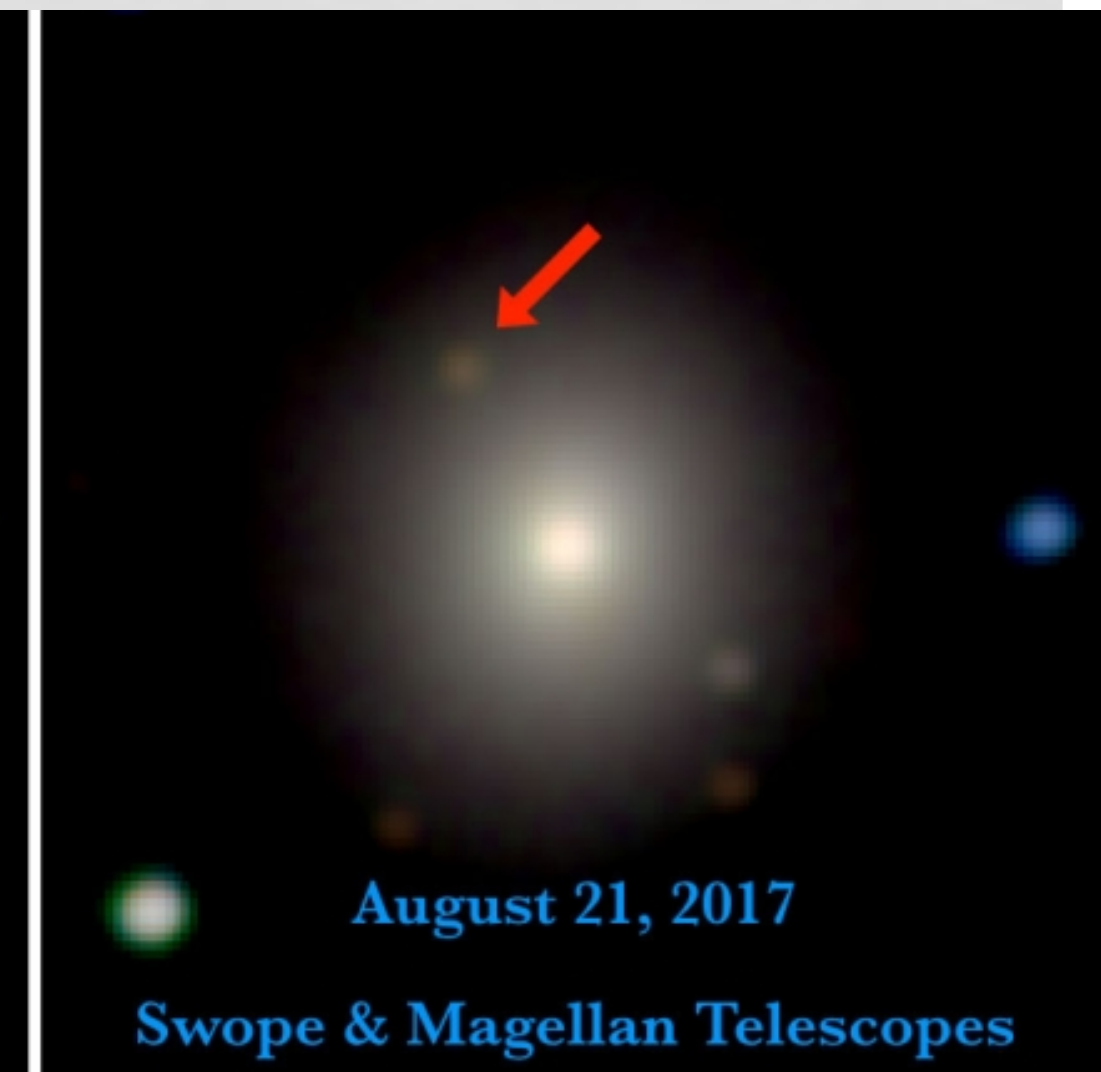
Neutron star mergers!

LIGO observatory is USA

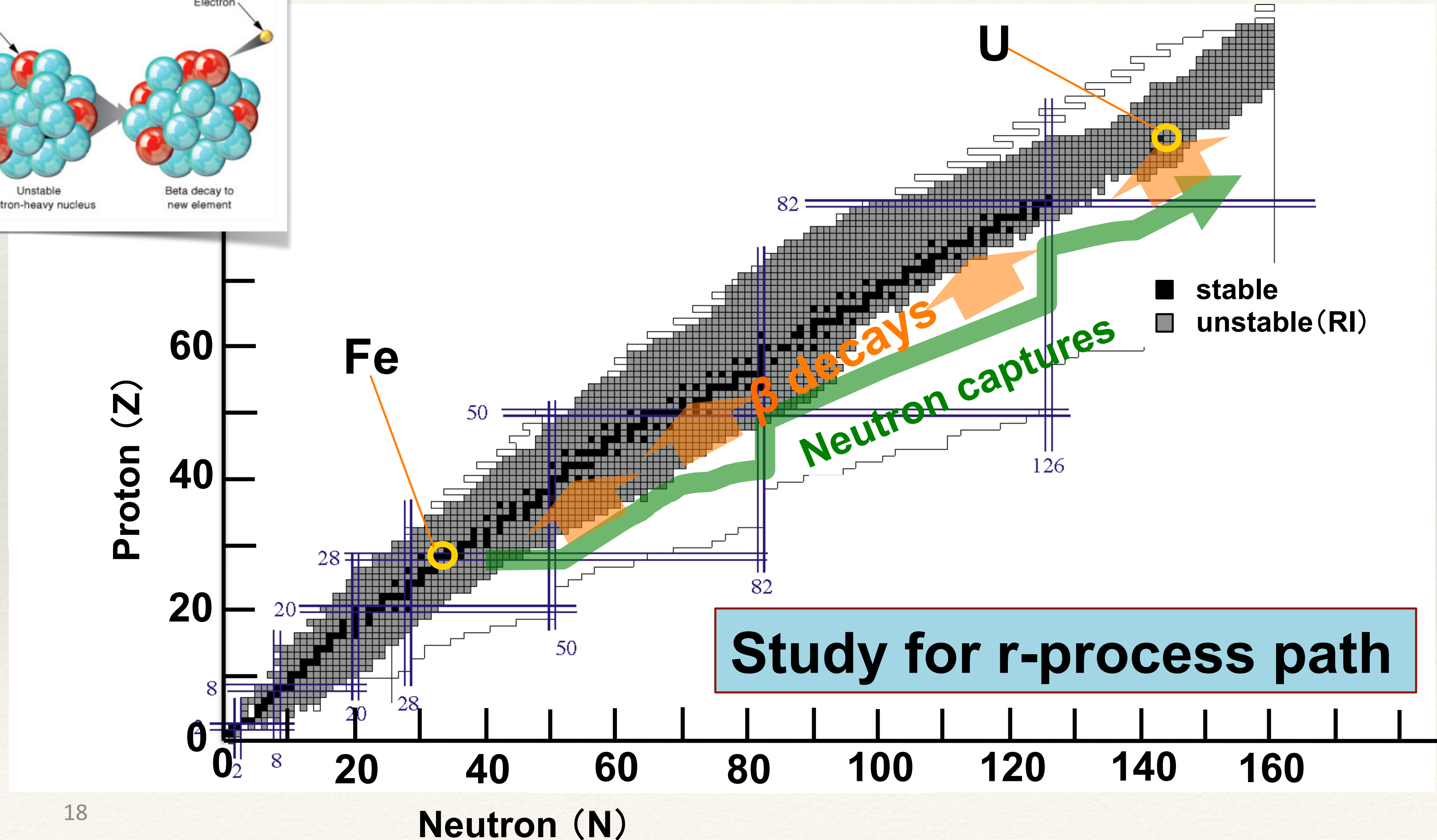
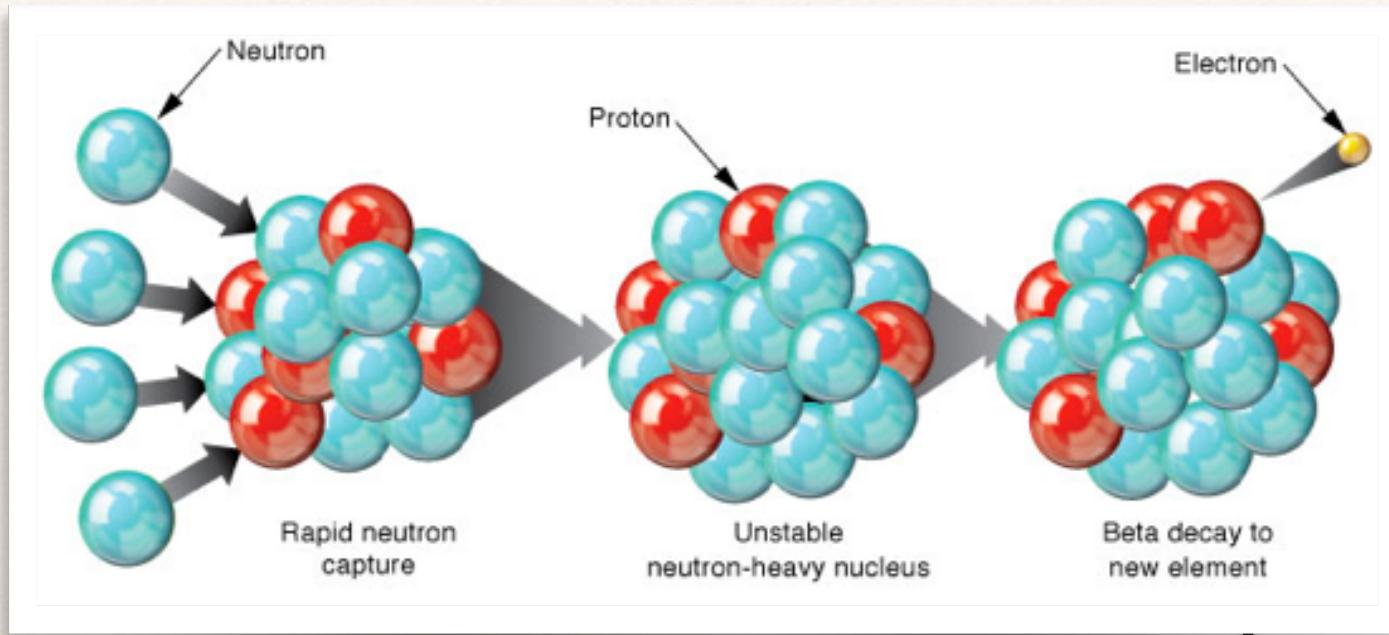


The light was also observed
This is very exciting for our field!!!

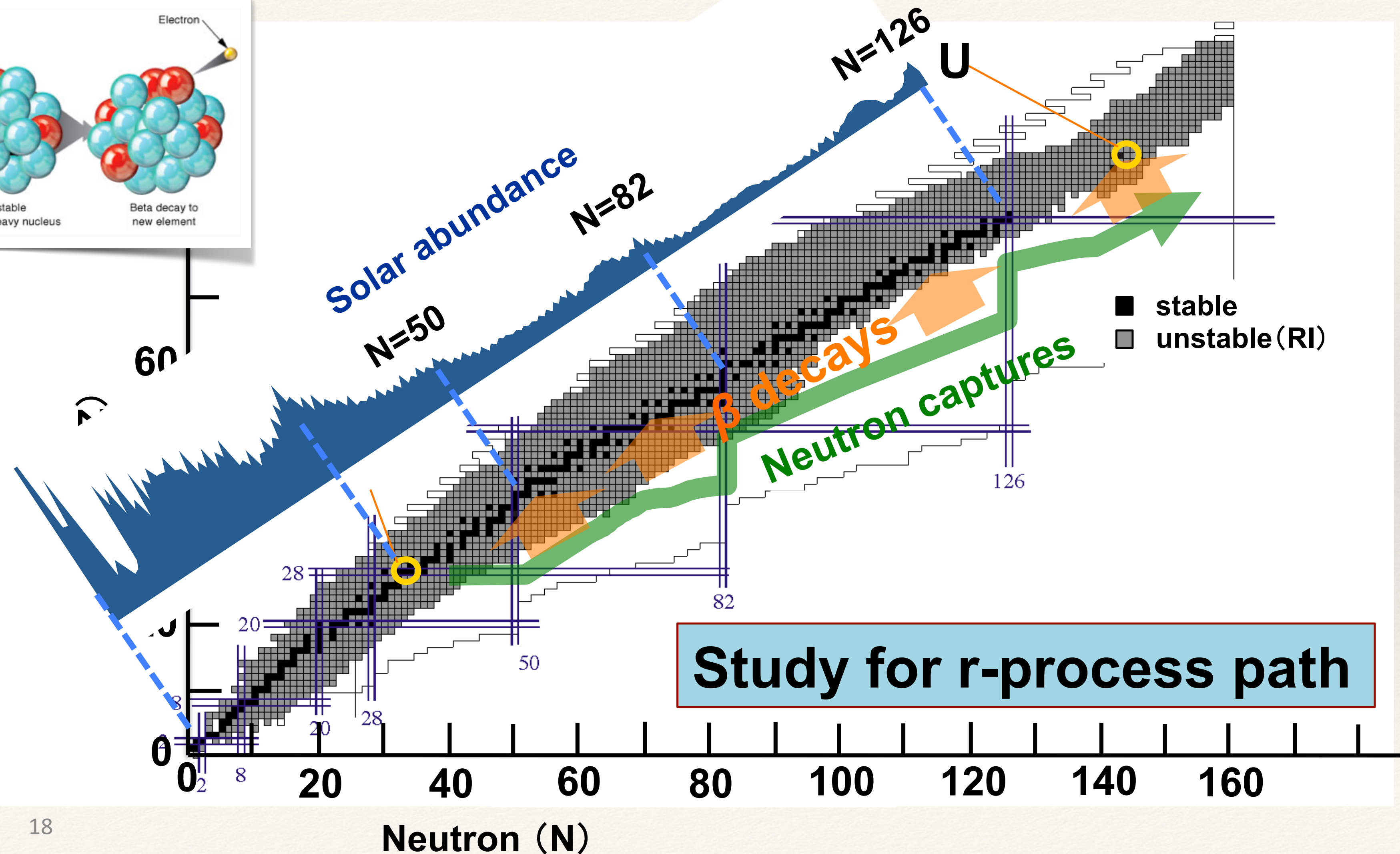
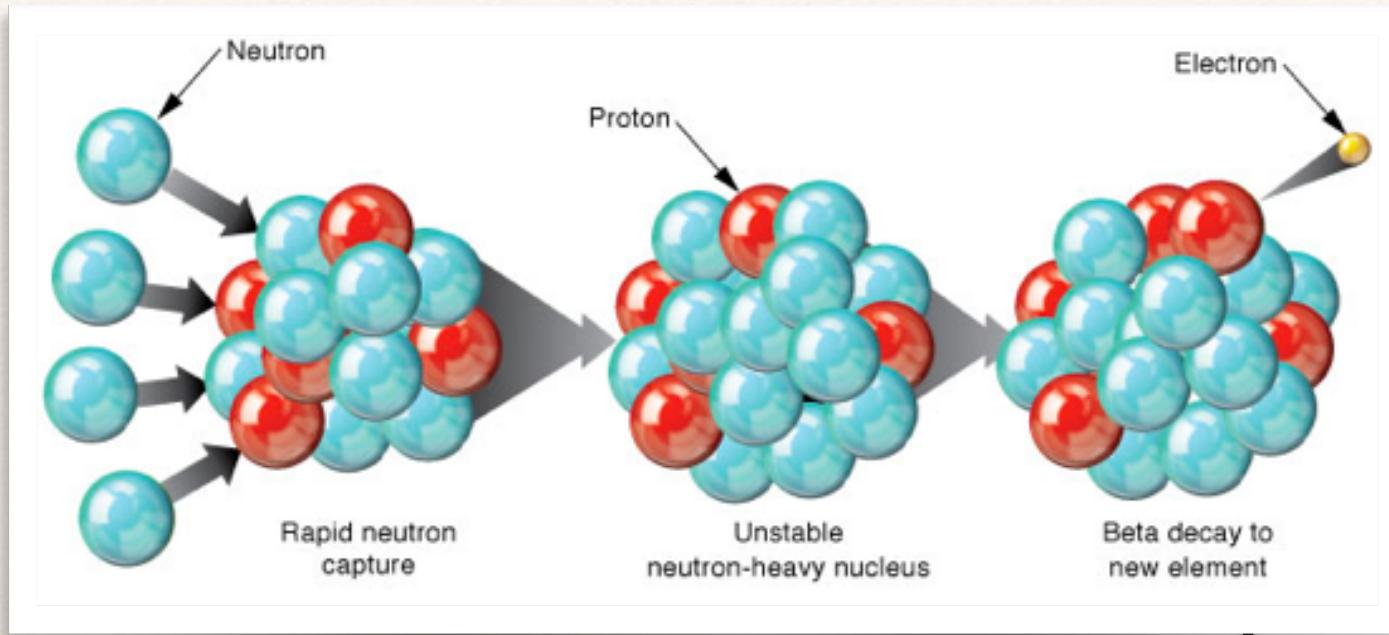
SSS17a



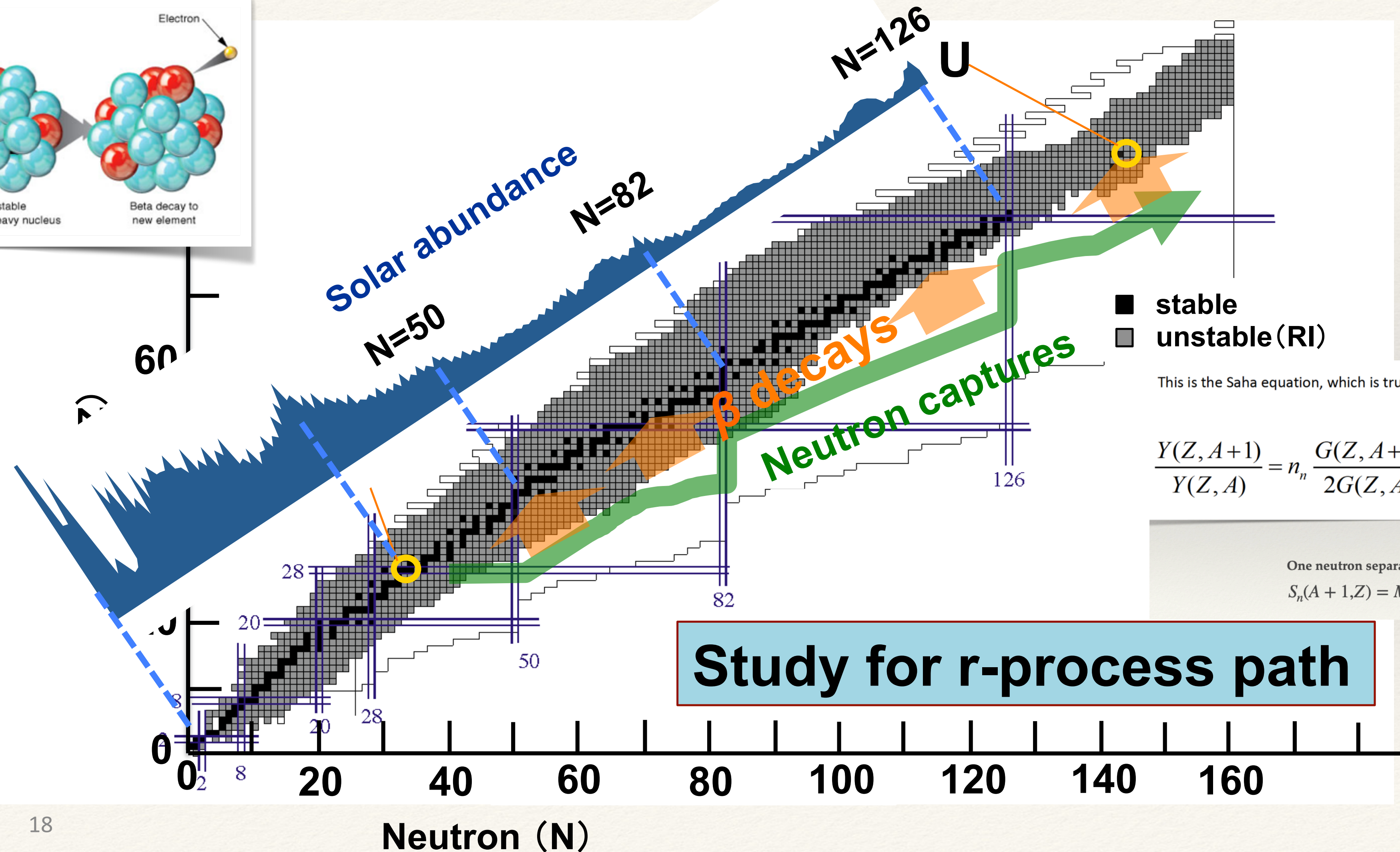
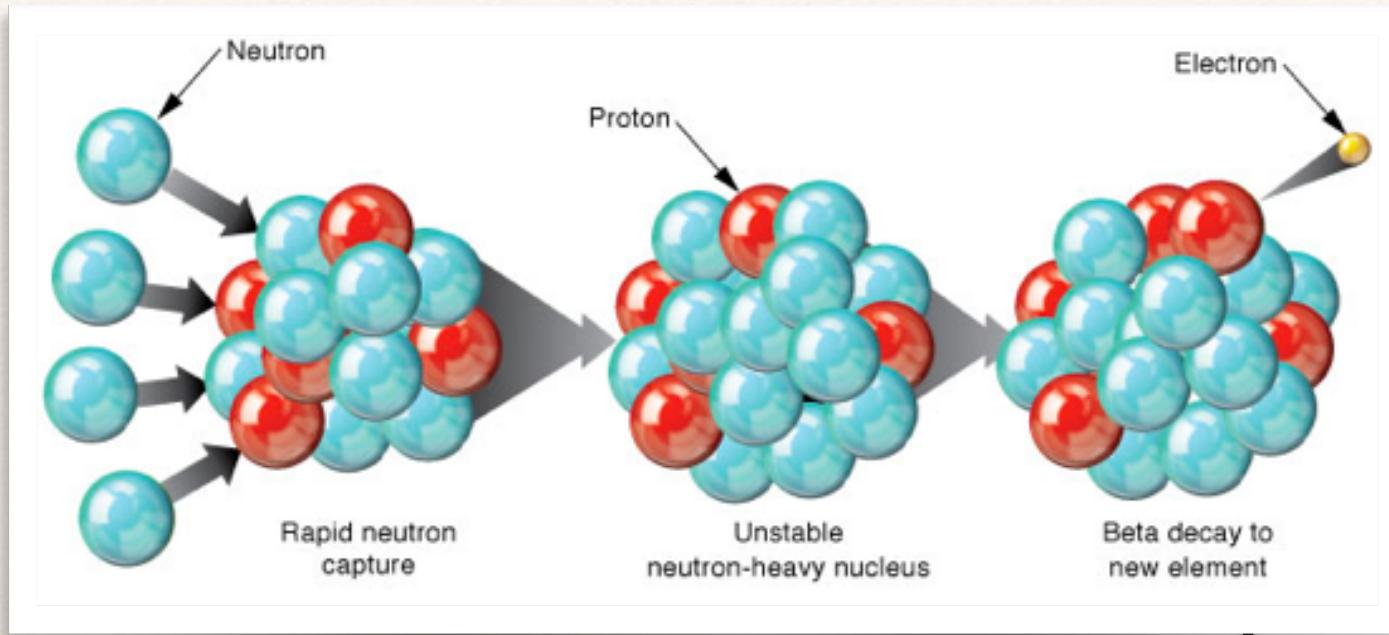
Chemical element synthesis: r-process



Chemical element synthesis: r-process



Chemical element synthesis: r-process



stable
 unstable (RI)

This is the Saha equation, which is true when $(n,g)=(g,n)$ equilibrium holds:

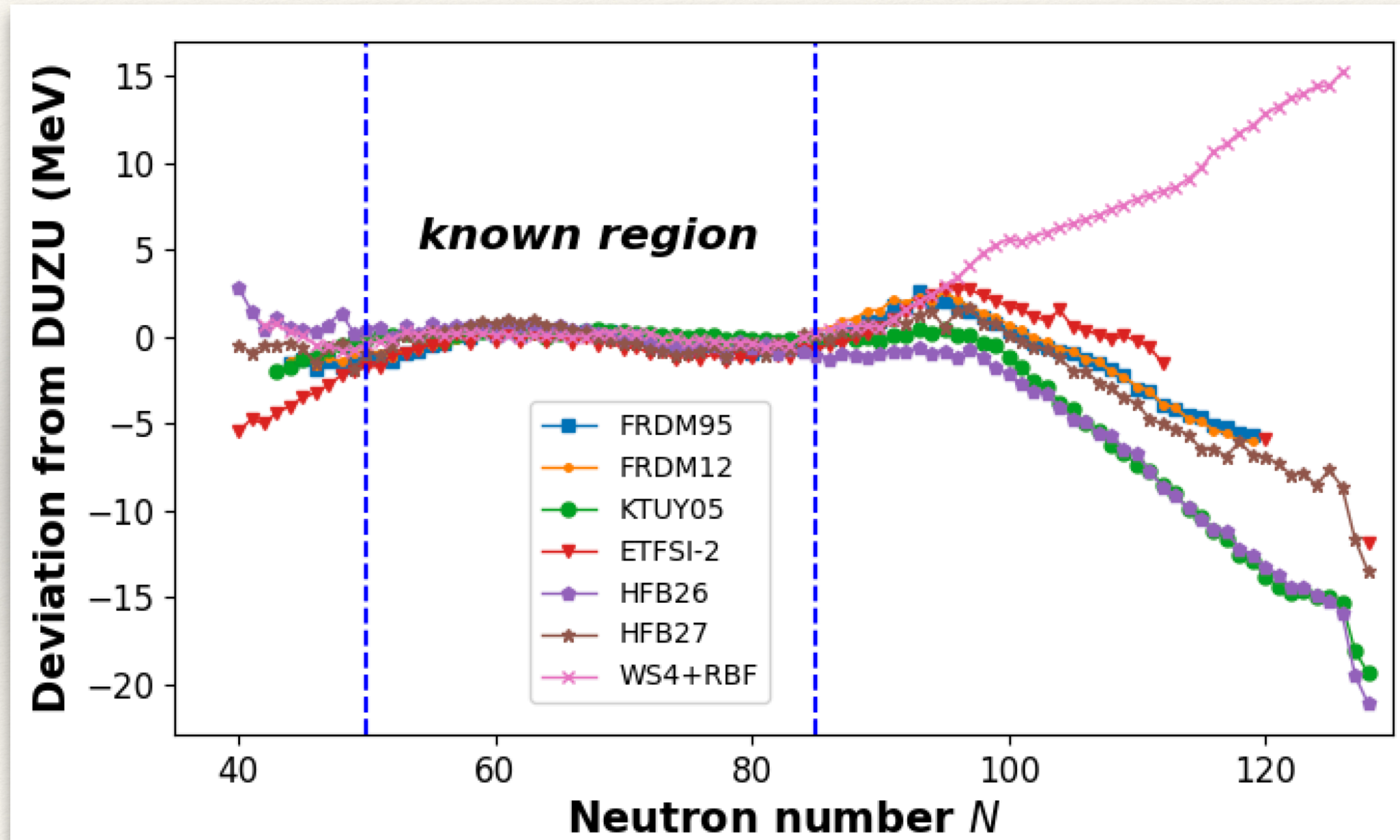
$$\frac{Y(Z, A+1)}{Y(Z, A)} = n_n \frac{G(Z, A+1)}{2G(Z, A)} \left[\frac{A+1}{A} \frac{2\pi\hbar^2}{m_n kT} \right]^{3/2} \exp(S_n / kT)$$

One neutron separation energy:

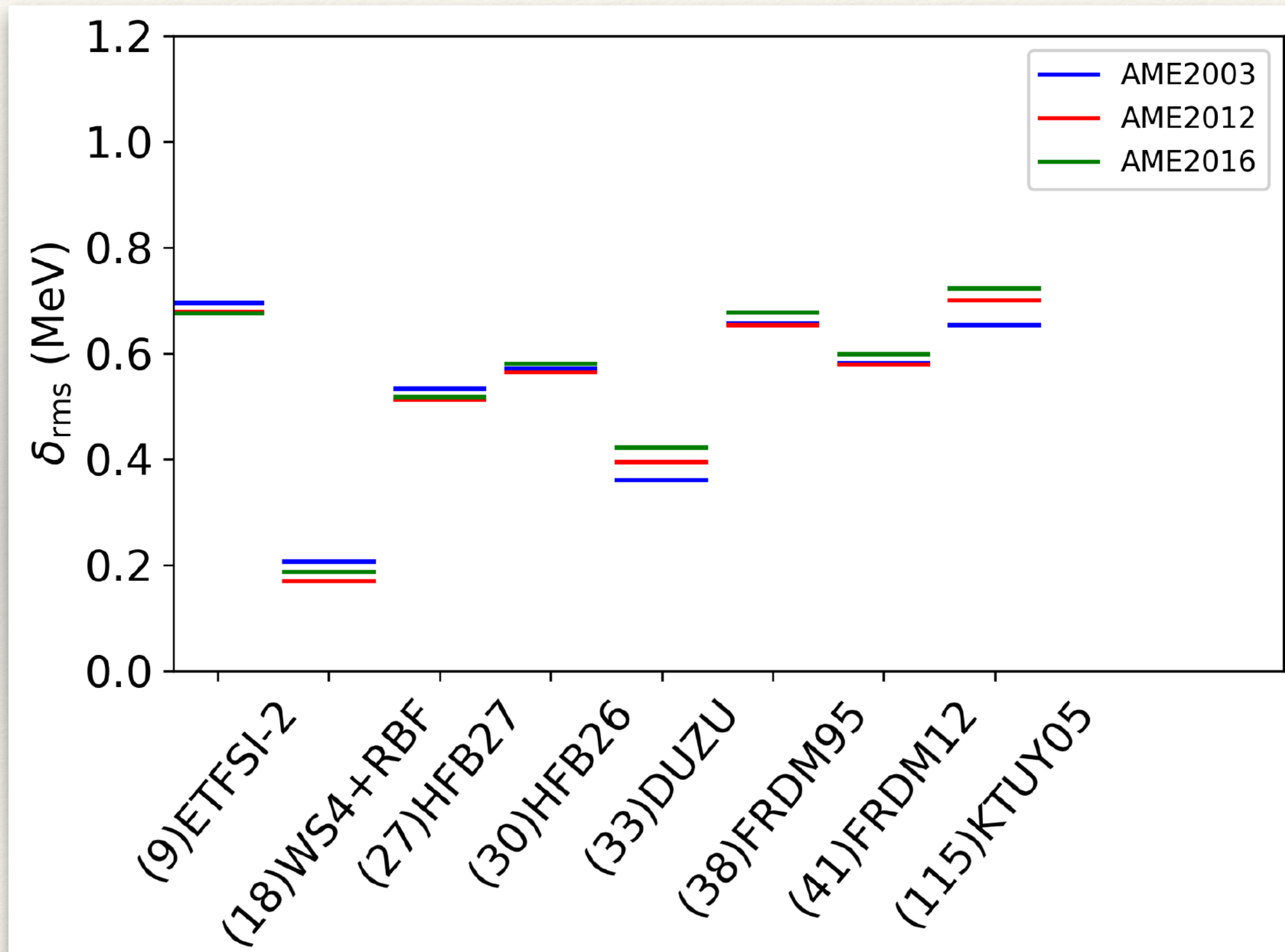
$$S_n(A+1, Z) = M(A, Z) + m_N - M(A+1, Z)$$

Study for r-process path

Why measure masses?



Why measure masses?



Mass Measurement Market

Low Energy

High Energy

Penning, MR-TOF-MS

Storage Rings

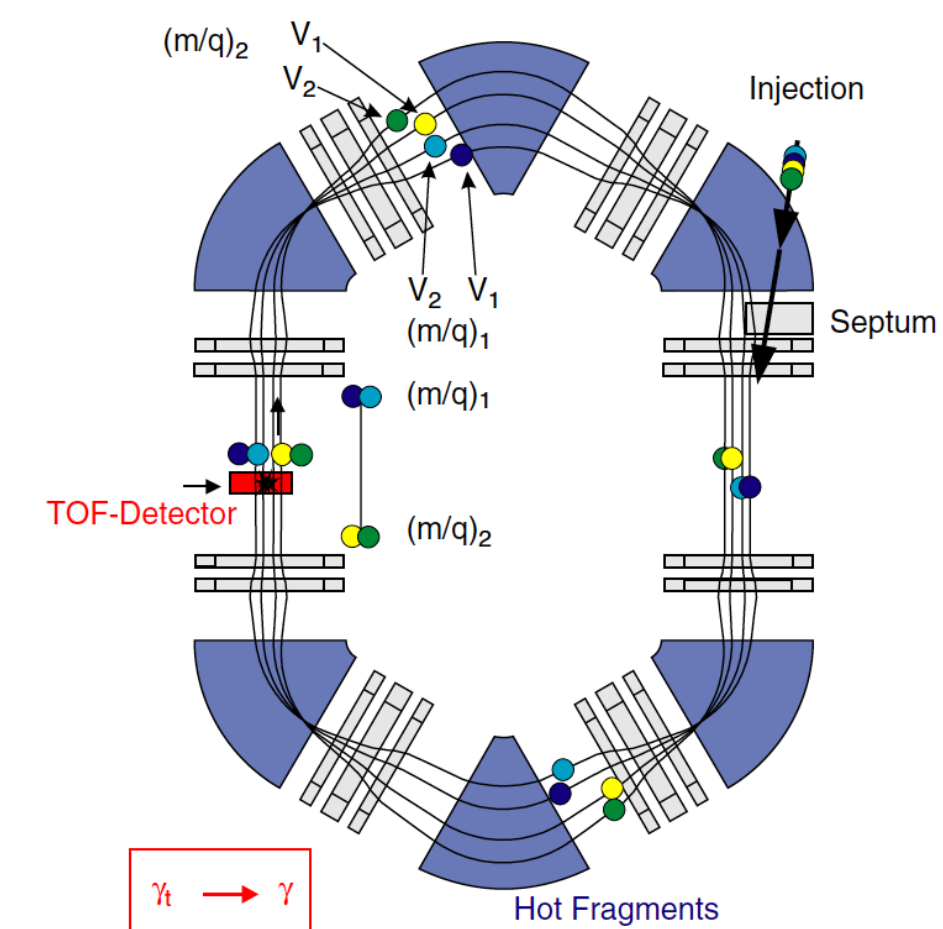
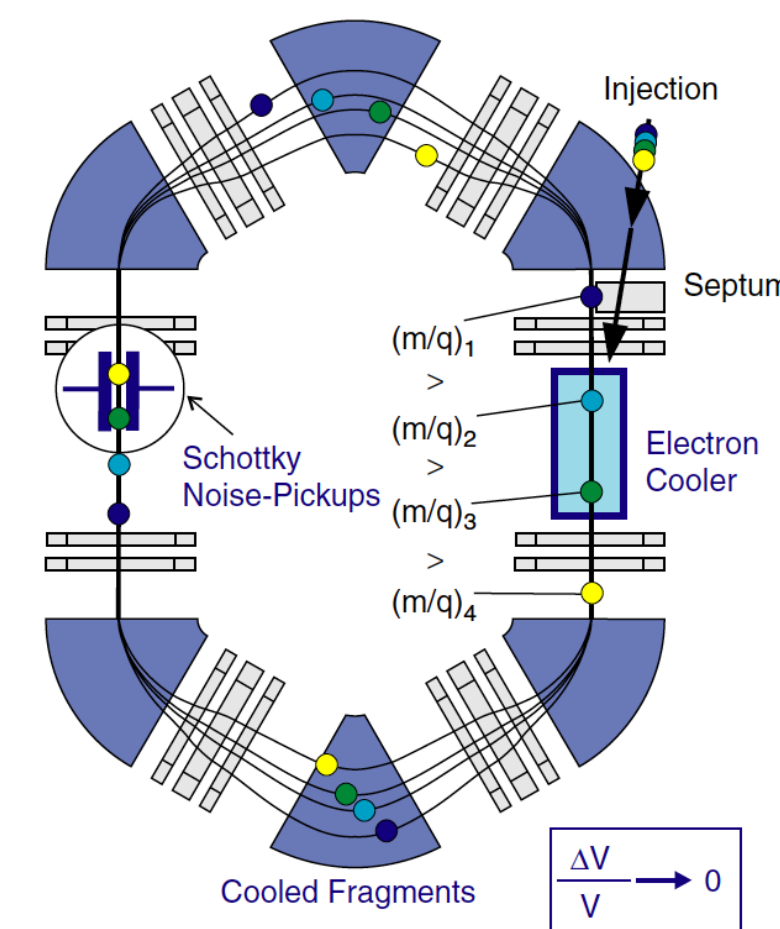
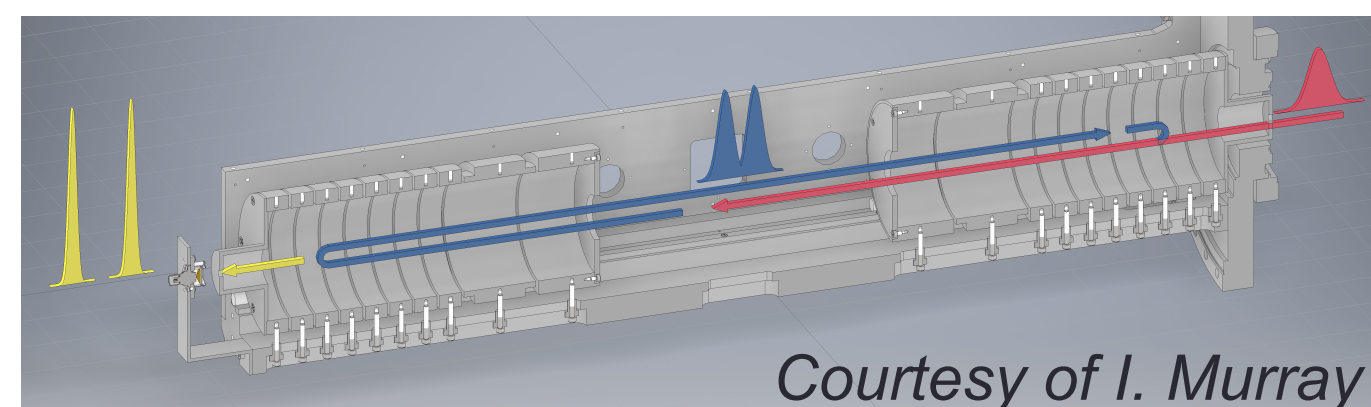
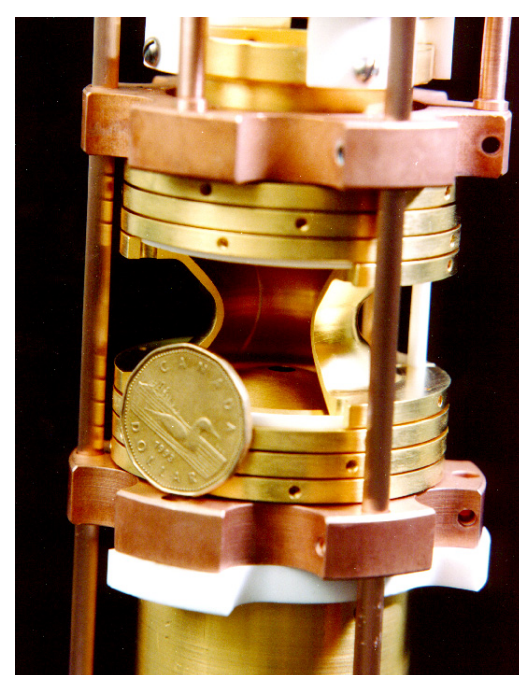
100ms~1s

1~10 ms

1~10 s

Isochronous

< 1ms



Precision 10^{-8}

Precision 10^{-7}

Precision 10^{-7}

Precision 10^{-6}

Low energy vs. High energy

Low precision



Fast measurement time

High precision



Long measurement time

The Atomic Mass Evaluation (AME)

Mass measurement: ✗ absolute mass ✓ connection between masses

Basic properties of the atomic mass: constant & additive

Experimental data
→ linear equations

All data available for 135Ba

68De17	162731	48	C8 N O H9-135Ba
68De17	117822	77	C11 H3-135Ba
68De17	154160	46	C12 H7-135Ba 0
20De20	288.43	0.32	135Cs-135Ba
66Be10	-203860	20	135Ba-C10 H14
66Be10	1177	2	135Ba-134Ba
68De17	1161	70	135Ba-134Ba
68De17	1168	78	135Ba-134Ba
77Ko.A	6973.2	0.4	134Ba(n,g)135Ba
90Is07,Z	6972.17	0.18	134Ba(n,g)135Ba
93Bo01,Z	6971.84	0.17	134Ba(n,g)135Ba
93Ch21	6973.24	0.22	134Ba(n,g)135Ba
06Fi.A	6971.87	0.18	134Ba(n,g)135Ba
70Vo04	4746	15	134Ba(d,p)135Ba
53Li01	205	5	135Cs(B-)135Ba
71Ba18,*	1200	10	135La(B+)135Ba
66Be10	-1115	3	136Ba-135Ba
68De17	-1119	50	136Ba-135Ba
68De17	-1074	50	136Ba-135Ba
69Ge07	9106.4	0.8	135Ba(n,g)136Ba
90Is07,Z	9107.74	0.04	135Ba(n,g)136Ba
06Fi.A	9107.73	0.19	135Ba(n,g)136Ba
70Vo04	6886	15	135Ba(d,p)136Ba
10Mc04	3089.1	0.6	137Ba 35Cl-135Ba 37Cl
66Be10	143	3	137Ba-135Ba
68De17	69	63	137Ba-135Ba
68De17	106	46	137Ba-135Ba

All data available for 134Ba

66Be10	205025	20	C10 H14-134Ba
68De17	205010	46	C10 H14-134Ba
68De17	111125	48	C11 H2-134Ba
68De17	156063	78	C8 N O H8-134Ba
68De17	147531	64	C12 H6-134Ba 0
134Ba+0	-91442	54	134La-u
134Ba+0	-91528	32	134La-u
66Be10	-197229	20	134Ba-C10 H13
66Be10	-553	4	134Ba-132Ba
68De17	-550	121	134Ba-132Ba
68Hs01,*	2058.6	0.4	134Cs(B-)134Ba
65Bi12	3772	50	134La(B+)134Ba
73Al20	3692	30	134La(B+)134Ba
66Be10	1177	2	135Ba-134Ba
68De17	1161	70	135Ba-134Ba
68De17	1168	78	135Ba-134Ba
77Ko.A	6973.2	0.4	134Ba(n,g)135Ba
90Is07,Z	6972.17	0.18	134Ba(n,g)135Ba
93Bo01,Z	6971.84	0.17	134Ba(n,g)135Ba
93Ch21	6973.24	0.22	134Ba(n,g)135Ba
06Fi.A	6971.87	0.18	134Ba(n,g)135Ba
70Vo04	4746	15	134Ba(d,p)135Ba
66Be10	67	5	136Ba-134Ba
68De17	69	128	136Ba-134Ba
68De17	72	78	136Ba-134Ba

All data available for 136Ba

68De17	126737	56	C11 H4-136Ba
68De17	171635	56	C8 N O H10-136Ba
68De17	163094	40	C12 H8-136Ba 0
136Ba+0	-92344	75	136La-u
10Mc04	2639.6	0.6	136Xe-136Ba
11Ko03	2638.62	0.52	136Xe-136Ba
11Ko03	2553.46	0.29	136Ce-136Ba
12Ne10	2553.42	0.37	136Ce-136Ba
66Be10	-1115	3	136Ba-135Ba
68De17	-1119	50	136Ba-135Ba
68De17	-1074	50	136Ba-135Ba
66Be10	67	5	136Ba-134Ba
68De17	69	128	136Ba-134Ba
68De17	72	78	136Ba-134Ba
69Ge07	9106.4	0.8	135Ba(n,g)136Ba
90Is07,Z	9107.74	0.04	135Ba(n,g)136Ba
06Fi.A	9107.73	0.19	135Ba(n,g)136Ba
70Vo04	6886	15	135Ba(d,p)136Ba
540I05,*	2548.1	2.0	136Cs(B-)136Ba
65Re07,*	2549	5	136Cs(B-)136Ba
59Gi50	2870	70	136La(B+)136Ba
66Be10	1249	3	137Ba-136Ba
68De17	1222	50	137Ba-136Ba
68De17	1227	44	137Ba-136Ba
69Gr31	6891	5	136Ba(n,g)137Ba
90Is07,Z	6905.54	0.10	136Ba(n,g)137Ba
95Bo03,Z	6905.70	0.12	136Ba(n,g)137Ba
06Fi.A	6905.74	0.16	136Ba(n,g)137Ba
60Ge01	-6949	38	137Ba(g,n)136Ba
70Vo04	4680	15	136Ba(d,p)137Ba
10Mc04	3621.1	0.6	138Ba 35Cl-136Ba 37Cl
66Be10	676	3	138Ba-136Ba
68De17	658	98	138Ba-136Ba
68De17	628	43	138Ba-136Ba

$$\sum_{\mu=1}^M k_i^{\mu} m_{\mu} = q_i \pm dq_i$$

$$m_A + m_a - m_b - m_B = q_i \pm dq_i$$

Example 1, linear system of equations:

$$x_1 = 10 \pm 0.5,$$

$$x_1 - x_2 = 5 \pm 1,$$

$$x_1 + x_2 = 13 \pm 0.5,$$

$$x_3 - x_1 = 4 \pm 1;$$

Overdetermined systems

The AME least-square method

$$\begin{aligned} 2x + y &= 7, \\ x + 3y &= 6, \\ 3x - y &= 3. \end{aligned}$$

No solution

$$\begin{bmatrix} 2 & 1 \\ 1 & 3 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = x \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} + y \begin{bmatrix} 1 \\ 3 \\ -1 \end{bmatrix} = \begin{bmatrix} 7 \\ 6 \\ 3 \end{bmatrix}$$

$$A\mathbf{x} = x\mathbf{a}_1 + y\mathbf{a}_2 = \mathbf{b}.$$

No combination of a_1 & a_2 can give b

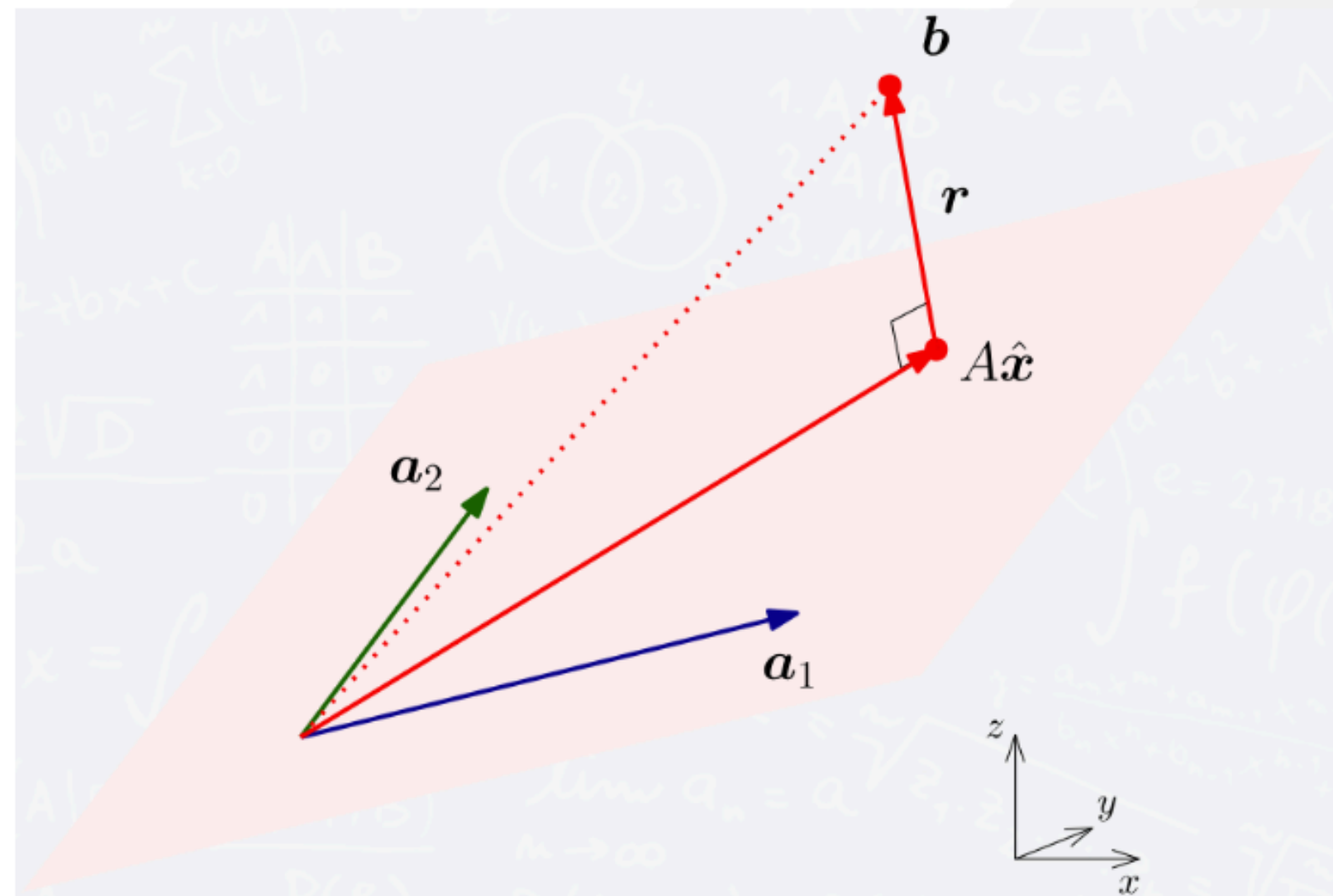
But the best solution could be found by minimizing $\|A\hat{\mathbf{x}} - \mathbf{b}\|^2$

Which is the sum of squares of deviations

How do experimental uncertainties affect the mass determination?

Example 1, linear system of equations:

$$\begin{aligned} x_1 &= 10 \pm 0.5, \\ x_1 - x_2 &= 5 \pm 1, \\ x_1 + x_2 &= 13 \pm 0.5, \\ x_3 - x_1 &= 4 \pm 1; \end{aligned}$$



Nuclear Instruments and Methods in Physics Research A249 (1986) 443–450
North-Holland, Amsterdam

443

A METHOD OF DETERMINING THE RELATIVE IMPORTANCE OF PARTICULAR DATA ON SELECTED PARAMETERS IN THE LEAST-SQUARES ANALYSIS OF EXPERIMENTAL DATA

Georges AUDI *

Laboratoire René Bernas du CSNSM, Bat, 108, 91406 Orsay, France

Walter G. DAVIES and Graham E. LEE-WHITING

Atomic Energy of Canada Limited Research Company, Chalk River Nuclear Laboratories, Chalk River, Ontario, Canada KOJ 1J0

Received 17 March 1986

In the framework of least-squares analysis of experimental data, a “flow-of-information” matrix is defined. This matrix displays the flow of information within the least-squares adjustment. Its elements, called “influences”, show the relative importance of each datum in the determination of each of the adjusted parameters. The “significance”, or quantity of information brought by each datum is defined. Illustrative examples are given.

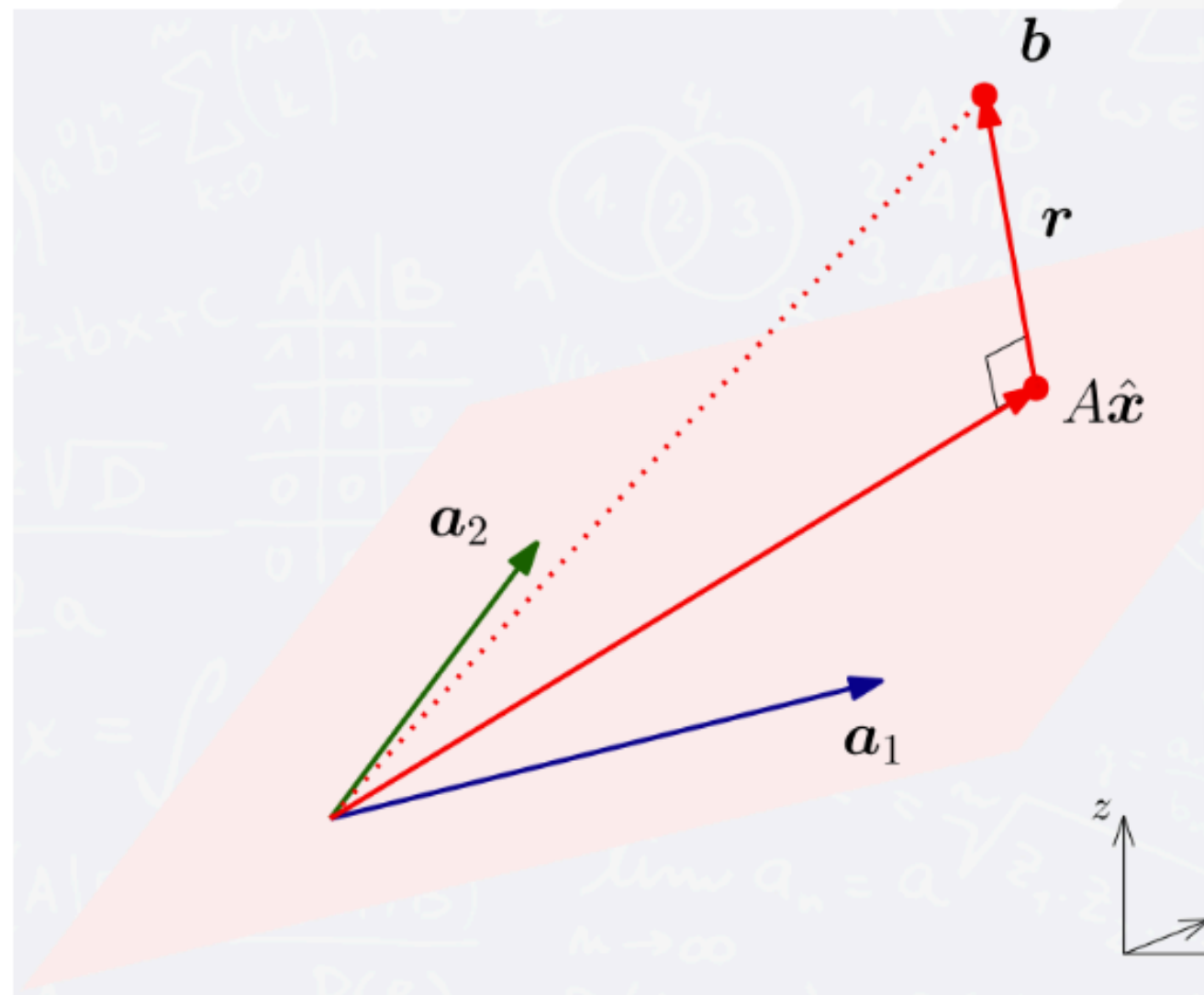
The AME least-square method

$$\begin{aligned} 2x + y &= 7, \\ x + 3y &= 6, \\ 3x - y &= 3. \end{aligned}$$

No solution

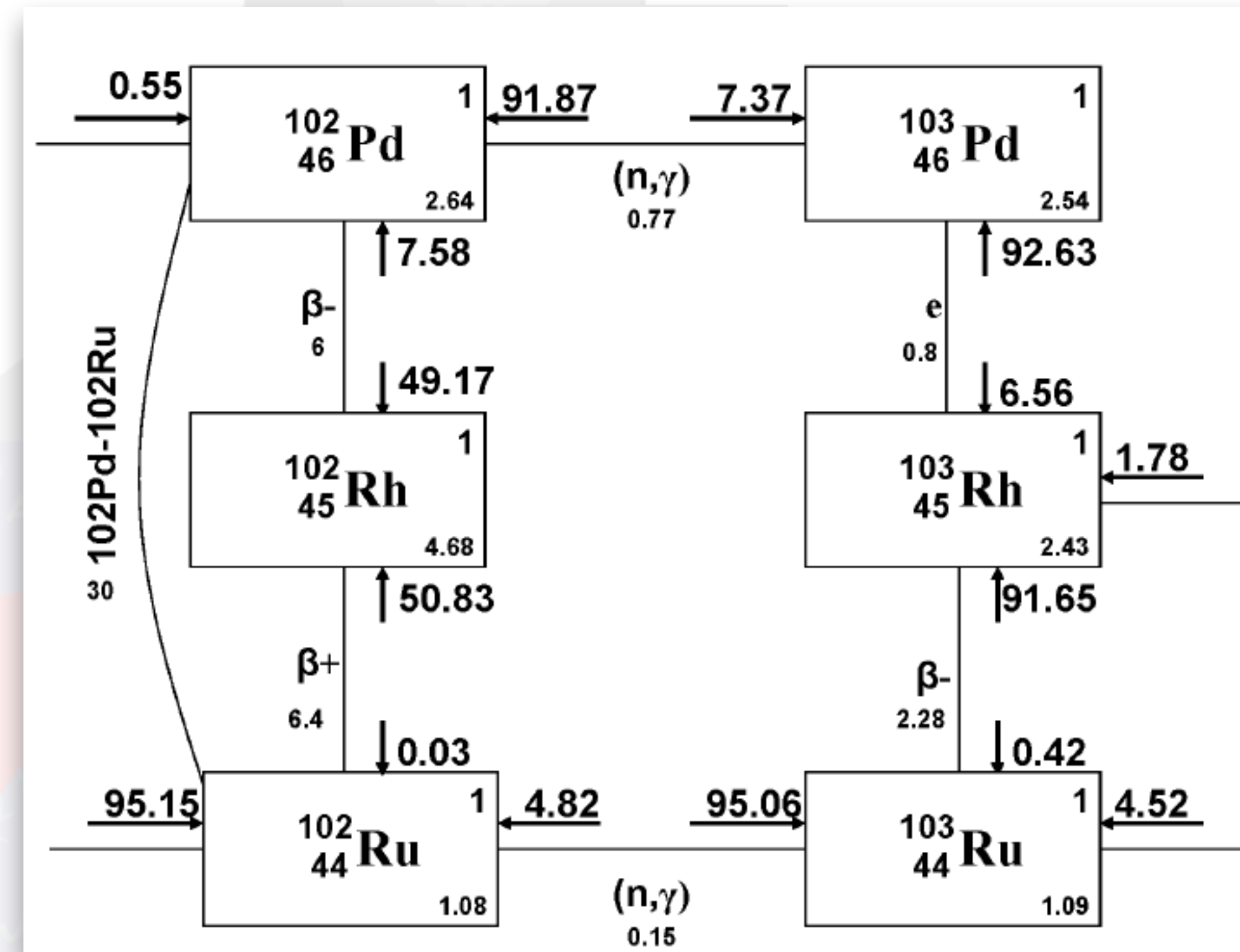
$$\begin{bmatrix} 2 & 1 \\ 1 & 3 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = x \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} + y \begin{bmatrix} 1 \\ 3 \\ -1 \end{bmatrix} = \begin{bmatrix} 7 \\ 6 \\ 3 \end{bmatrix}$$

$$Ax = xa_1 + ya_2 = b.$$



No combination of a_1 & a_2 can give b

But the best solution could be found by



How do experimental uncertainties affect the mass determination?

Example 1, linear system of equations:

$$\begin{aligned} x_1 &= 10 \pm 0.5, \\ x_1 - x_2 &= 5 \pm 1, \\ x_1 + x_2 &= 13 \pm 0.5, \\ x_3 - x_1 &= 4 \pm 1; \end{aligned}$$

49 (1986) 443-450

443

RELATIVE IMPORTANCE OF PARTICULAR DATA ON LEAST-SQUARES ANALYSIS OF EXPERIMENTAL DATA

France

ITING

Chalk River Nuclear Laboratories, Chalk River, Ontario, Canada KOJ 1JO

In the framework of least-squares analysis of experimental data, a "flow-of-information" matrix is defined. This matrix displays the flow of information within the least-squares adjustment. Its elements, called "influences", show the relative importance of each datum in the determination of each of the adjusted parameters. The "significance", or quantity of information brought by each datum is defined. Illustrative examples are given.



Brief history of AME (11 tables since 1955)

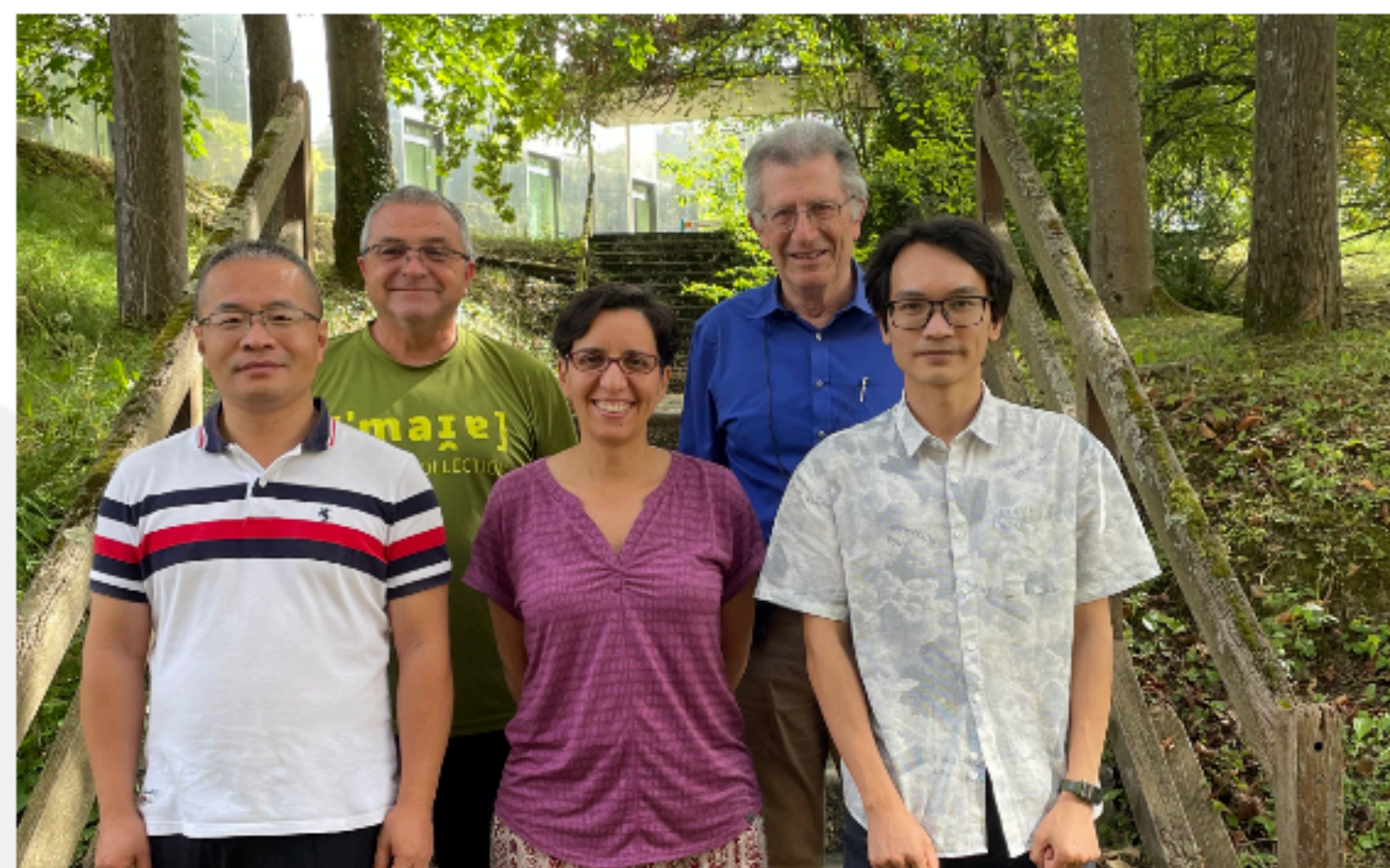
1955: A.H. Wapstra established least-squares method to solve the overdetermination problem

1986: G. Audi discovered the flow of information matrix

2006: A.H. Wapstra passed away

2008: G. Audi established the AME collaboration with China

Tables: **AME1955, AME1961, AME1964, AME1971, AME1977, AME1983, AME1993, AME2003, AME2012, AME2016, AME2020**



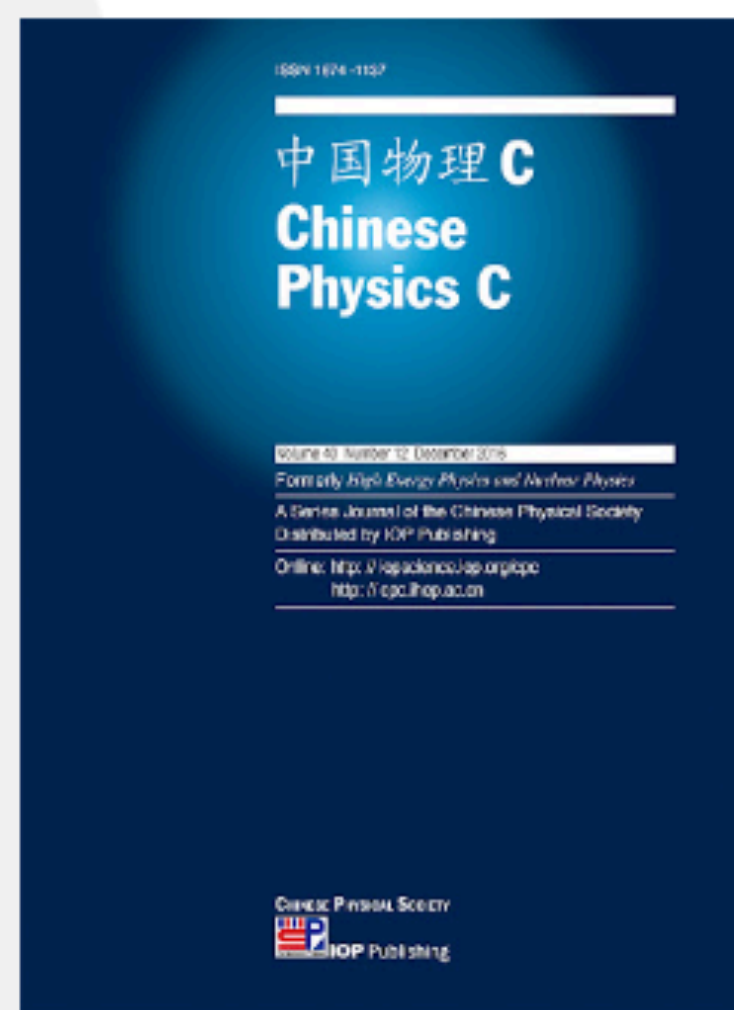
Collaboration meeting in Orsay Sep. 2023



A.H. Wapstra

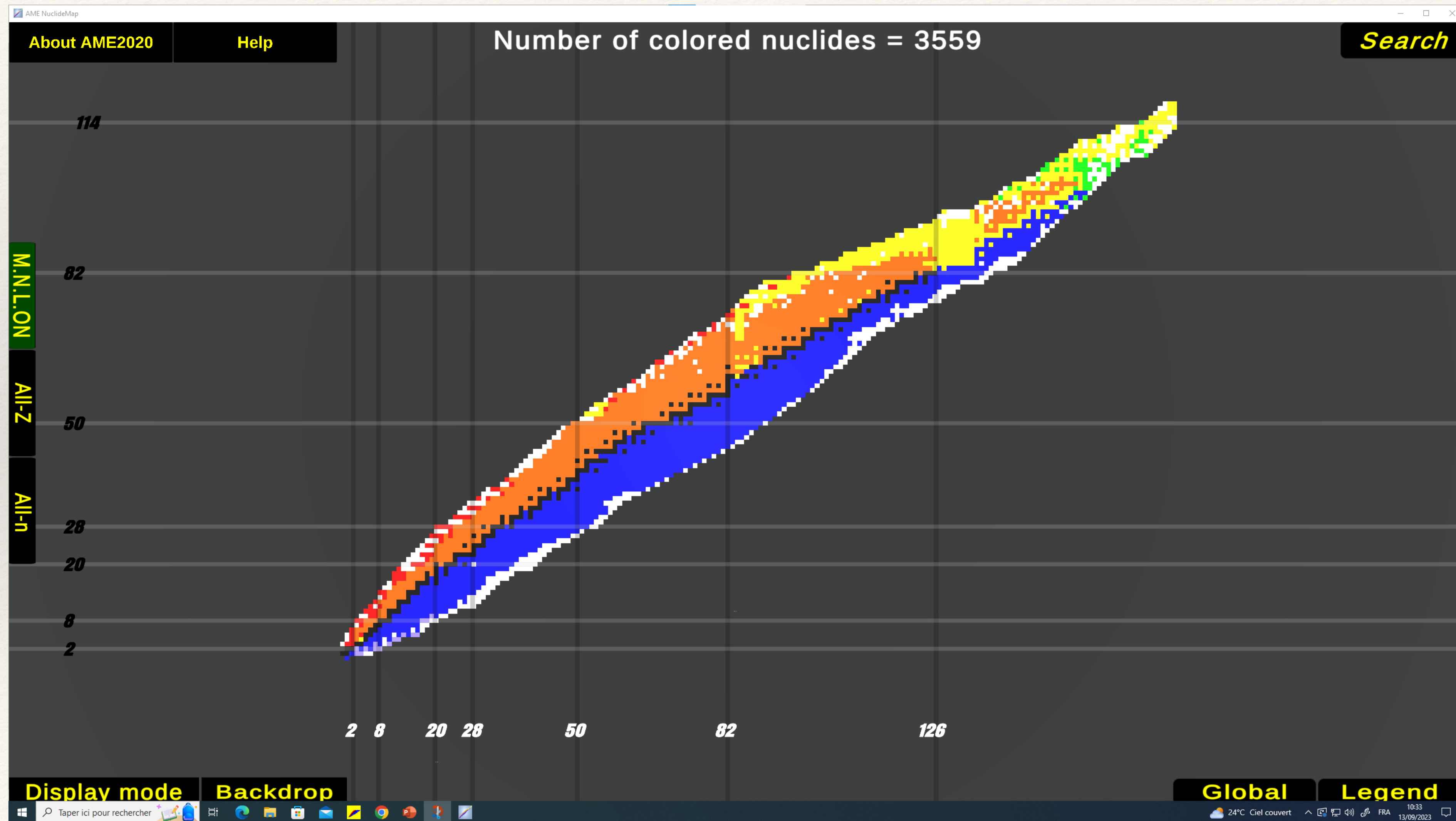


Memorandum signing in China



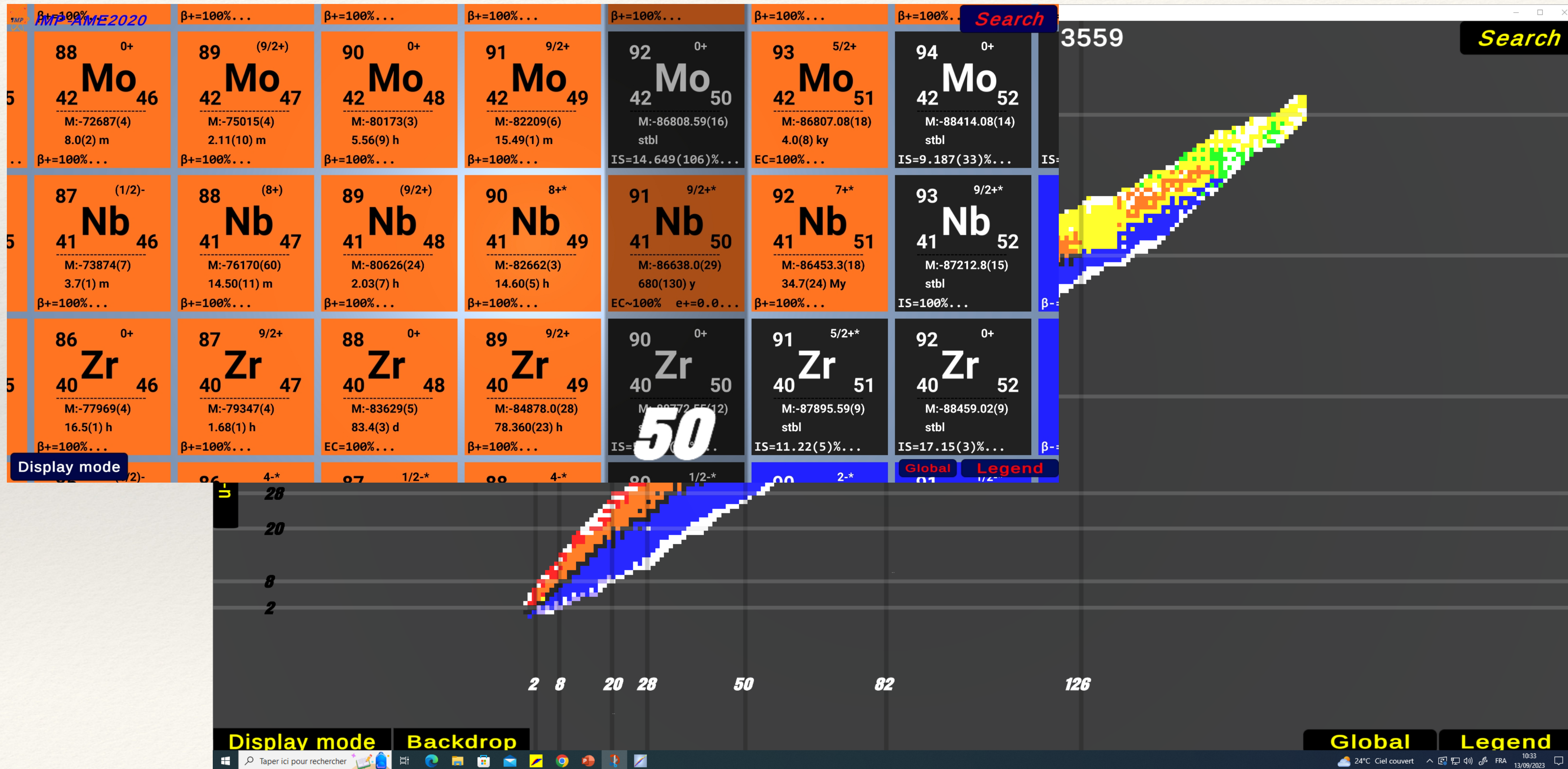
New tool: Nucleus++

Download here: <http://amdc.impcas.ac.cn/>
available on Windows, Mac, Android, (iOS)
JY. Shi et al, NST 35 (2024)



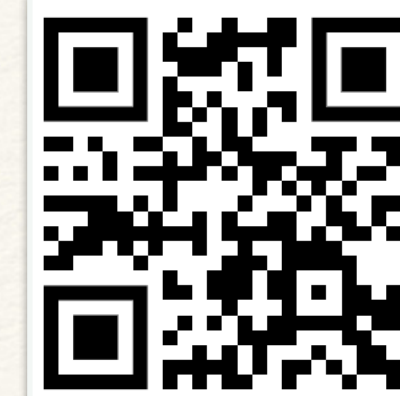
New tool: Nucleus++

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New tool: Nucleus++

Download here: <http://amdc.impcas.ac.cn/>
 available on Windows, Mac, Android, (iOS)
 JY. Shi et al, NST 35 (2024)



IMP-AME2020

88 ⁰⁺ Mo ₄₂ 46 M:-72687(4) 8.0(2) m β+=100%...

89 ^(9/2+) Mo ₄₂ 47 M:-75015(4) 2.11(10) m β+=100%...

90 ⁰⁺ Mo ₄₂ 48 M:-80173(3) 5.56(9) h β+=100%...

91 ^{9/2+} Mo ₄₂ 49 M:-82209(6) 15.49(1) m β+=100%...

92 ⁰⁺ Mo ₄₂ 50 M:-86808.59(16) stbl IS=14.649(106)%...

87 ^{(1/2)-} Nb ₄₁ 46 M:-73874(7)

88 ⁽⁸⁺⁾ Nb ₄₁ 47 M:-76170(60)

89 ^(9/2+) Nb ₄₁ 48 M:-80626(24)

90 ^{8+*} Nb ₄₁ 49 M:-82662(3)

91 ^{9/2+*} Nb ₄₁ 50 M:-86638.0(29)

90Nb Z=41 n=49 Isomer: 6

Year of discovery: 1951

Source: 68.71 90Nb(B+)90Zr **Primary** Example: Influence % + Data sources 31.29 90Mo(B+)90Nb

Decay Mode: β+=100%

Isomer	Mass excess(keV)	Half Life	Excitation energy(keV)	Decay Modes	Spin and Parity
gs	-82662(3)	14.60(5) h		β+=100%	8+*
m	-82540(3)	63(2) us	122.370(22)	IT=100%	6+
				IT=100%	4-*
				IT=100%	7+
				IT=100[gs=0,m=100]%	1+
				IT=100%	(11-)

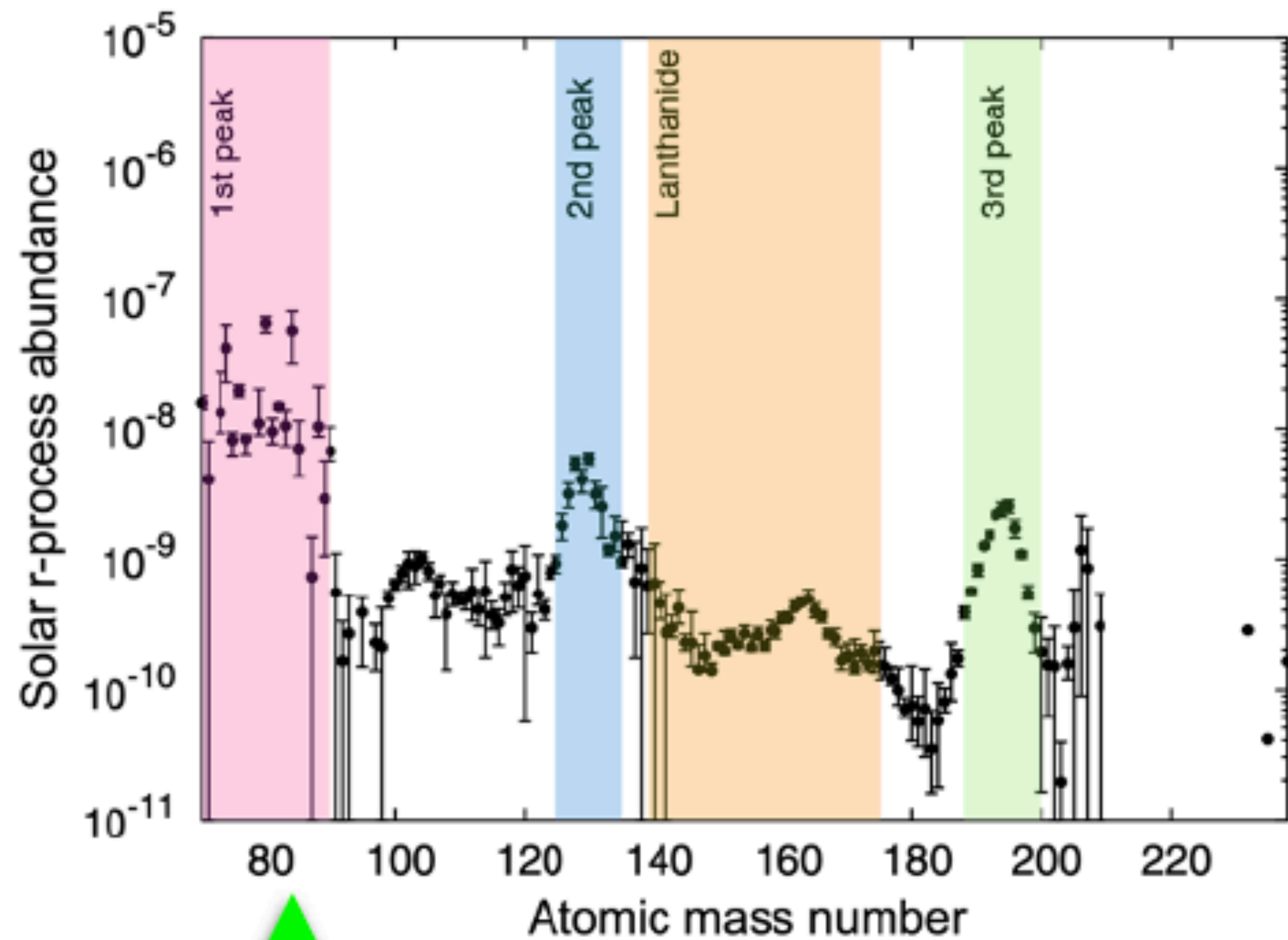
Particle separation energy possible impossible No Data

S(n)=10107(24) S(2n)=22630(60)
 S(p)=5073(4) S(2p)=12940(4)
 Q(α)=-5803(15) Q(2β-)=-11937(3)
 Q(β-)=-2489(3) Q(2β+)=3835(3)
 Q(β+)=6111(3)
 Q(Ep)=-2239(3)
 Q(β-,n)=-15718(5)

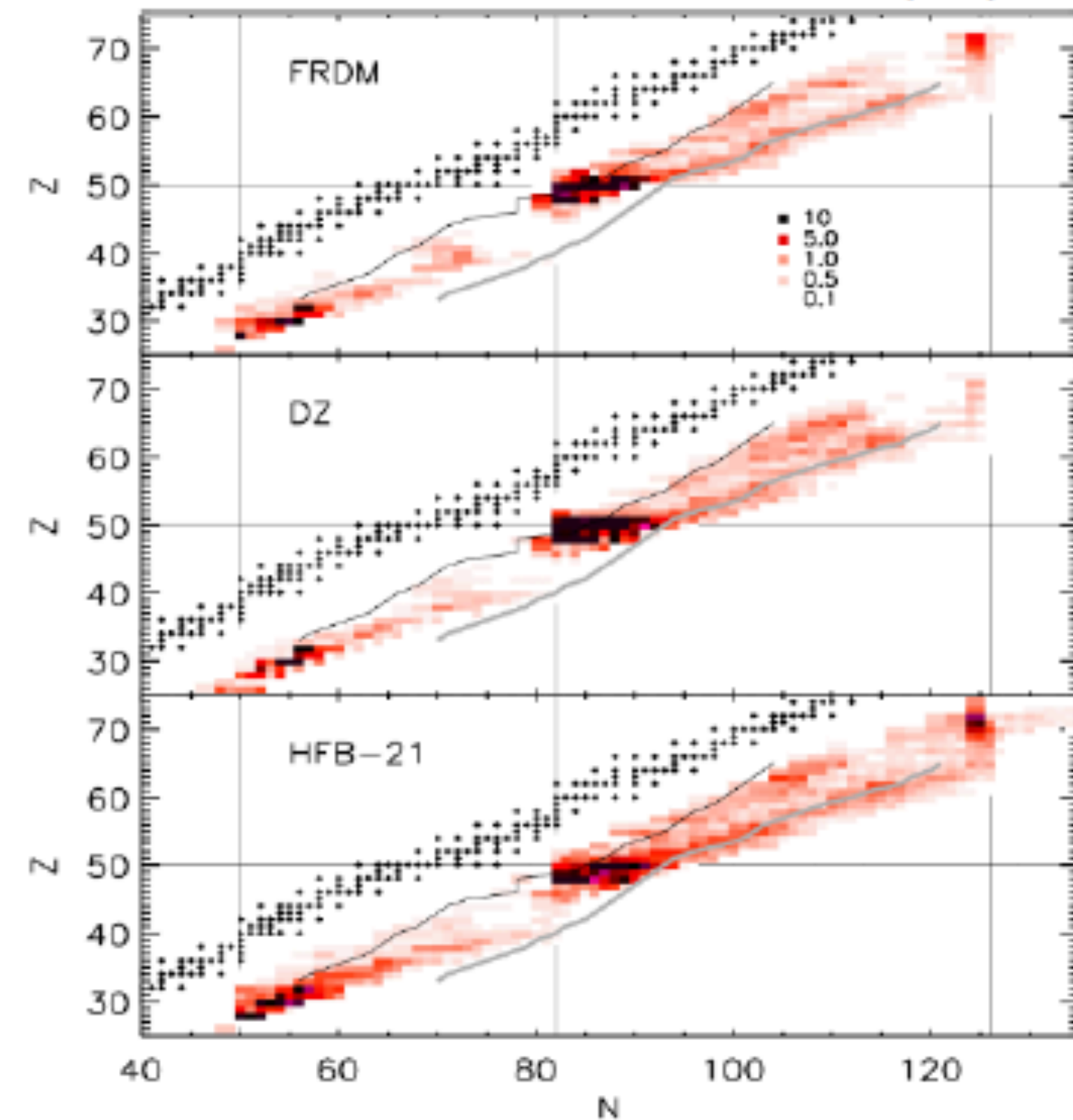
Global Legend

24°C Ciel couvert 10:33 13/09/2023

r-process: which masses to measure?



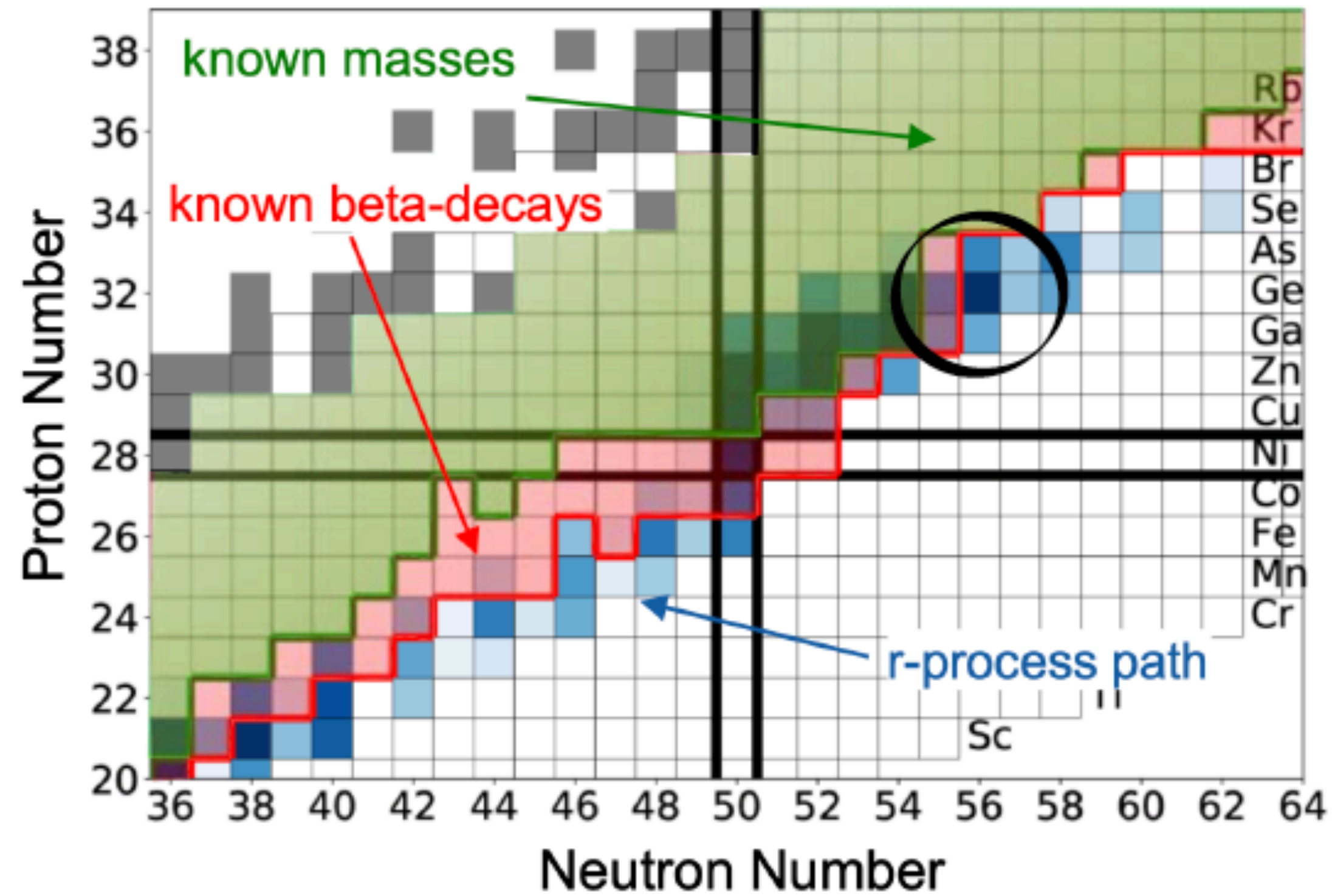
M. P. Reiter et al., PRC 101, 025803 (2020); Brett et al., EPJA (2012) 48



These masses have the largest impact on abundance peak as concluded in sensitivity studies.

The masses of neutron-rich nuclei with the largest impact

S. Nikas *et al.*, NPA-IX 1668, 012029 (2020).

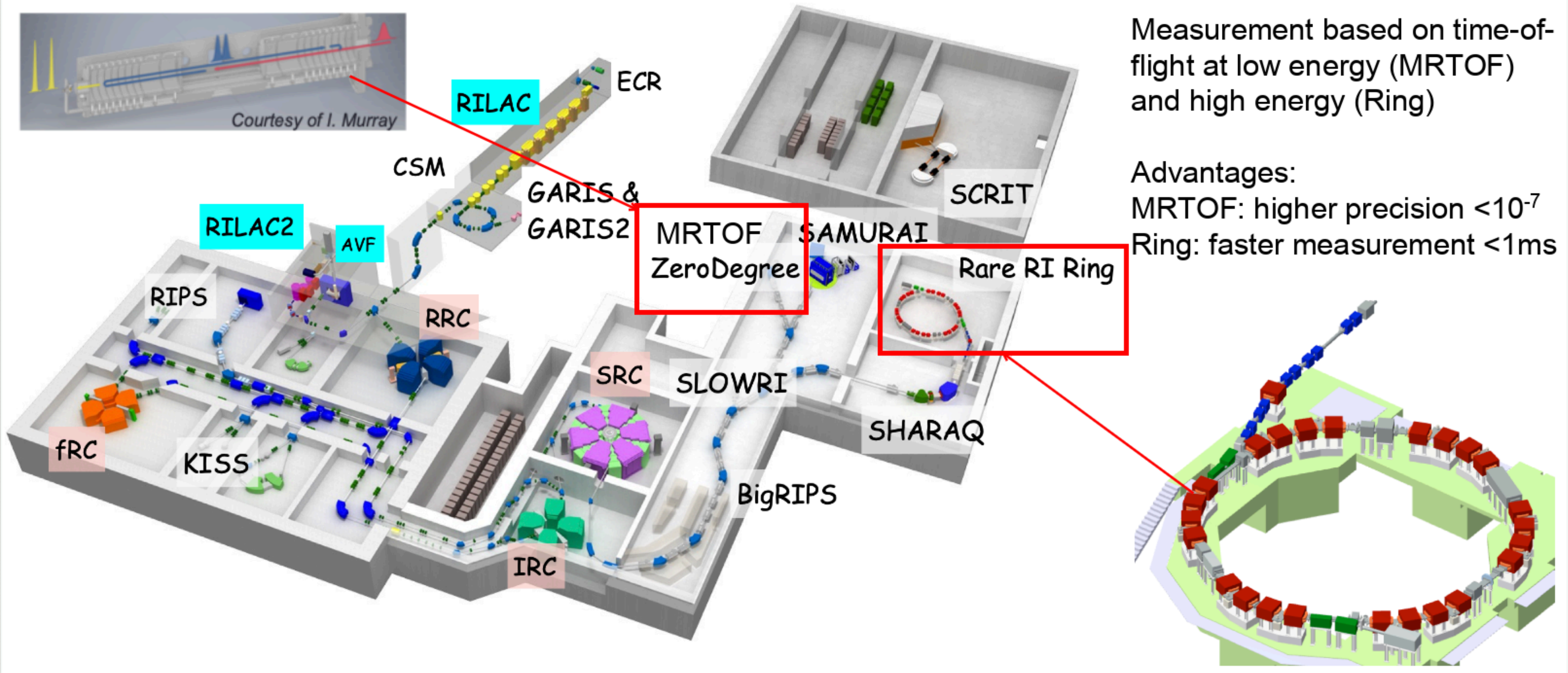
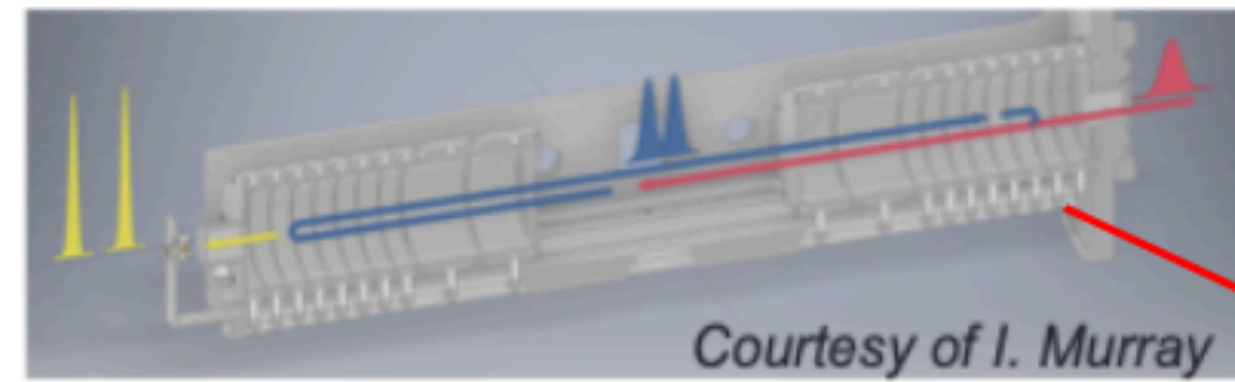


Isotopes of interest: Ga, Ge, As

- These isotopes have a direct influence on the production of Sr, Y, Zr.
- Masses of very neutron-rich Ge will help to understand additional fine features of the abundance pattern, for instance, the production of Sr in neutron star mergers.

The path of r-process in the region of $N=50$ including the isotopes of interest at $N=55$, $N=56$ (sub-shell closure) and $N=57$.

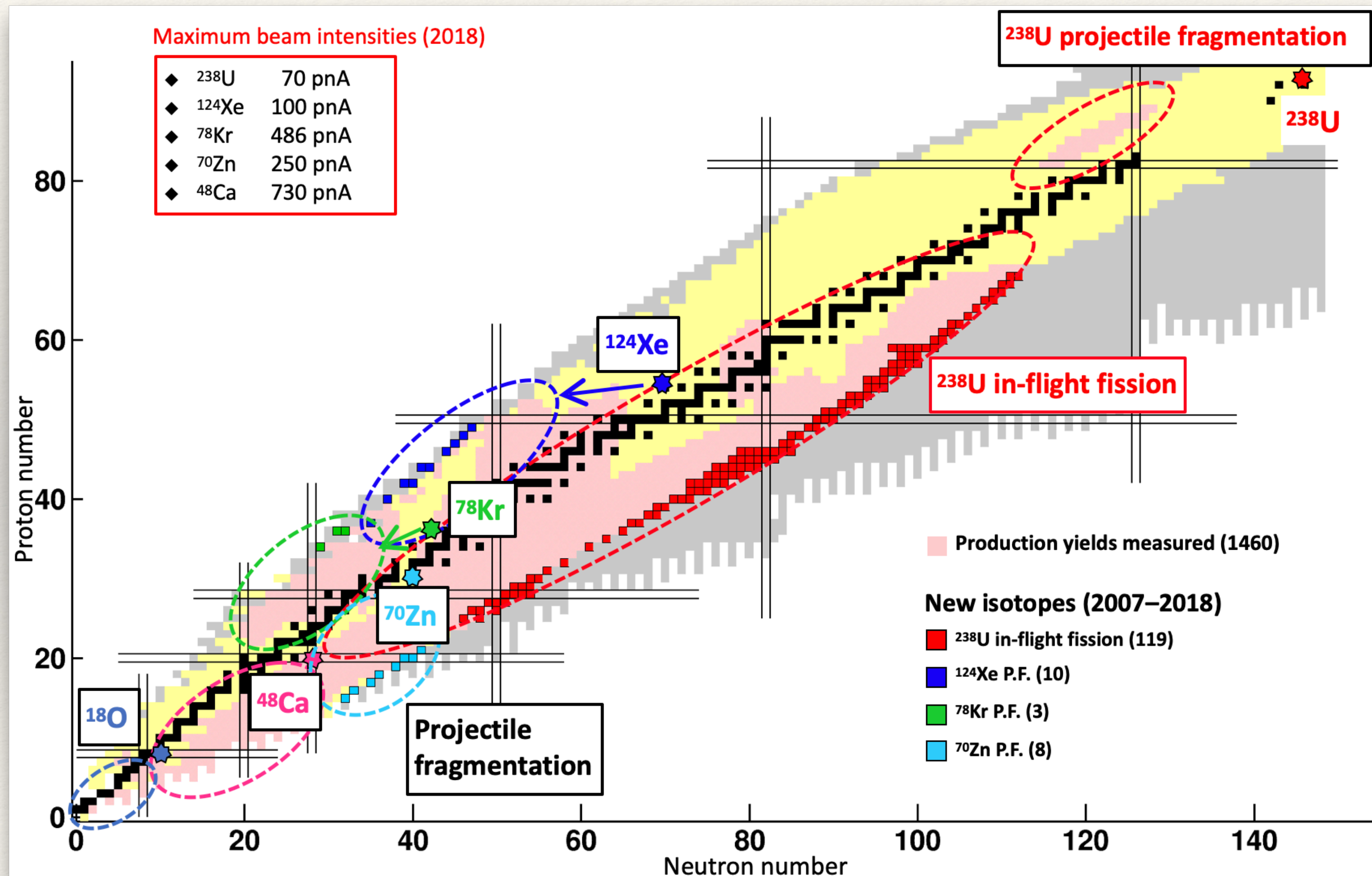
Mass measurements at RIBF/Riken



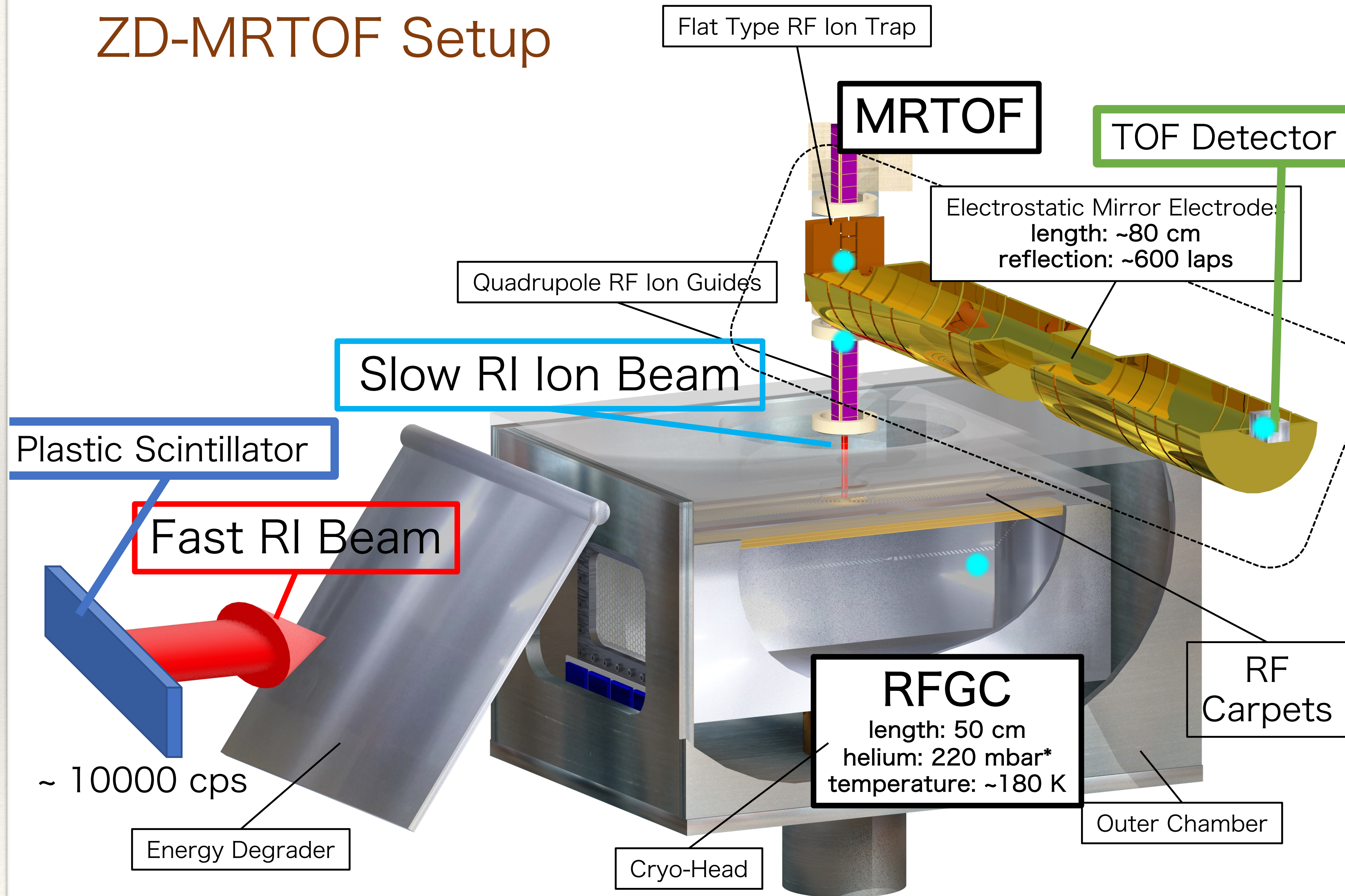
Measurement based on time-of-flight at low energy (MRTOF) and high energy (Ring)

Advantages:
MRTOF: higher precision $<10^{-7}$
Ring: faster measurement $<1\text{ms}$

Production of n-rich nuclei at Riken/Japan



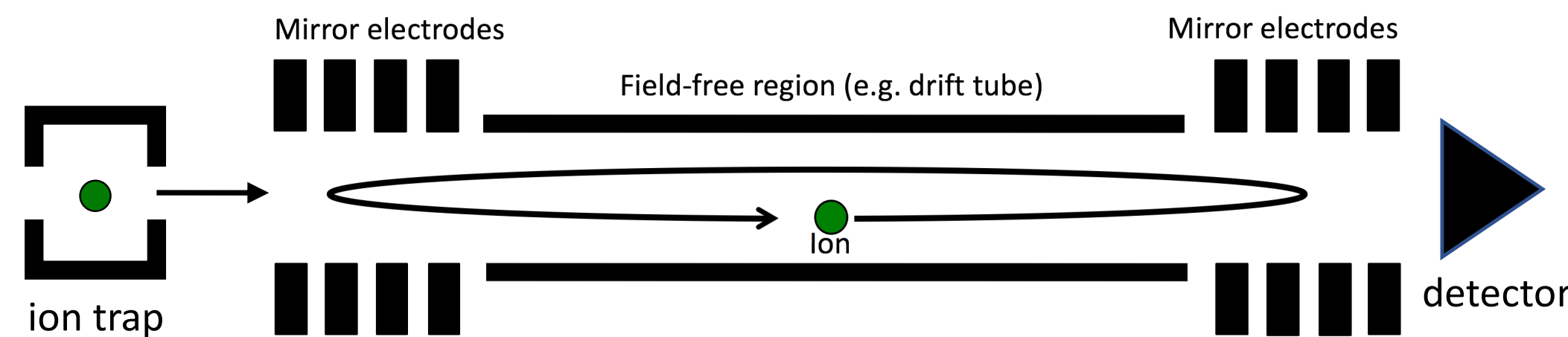
ZD-MRTOF Setup



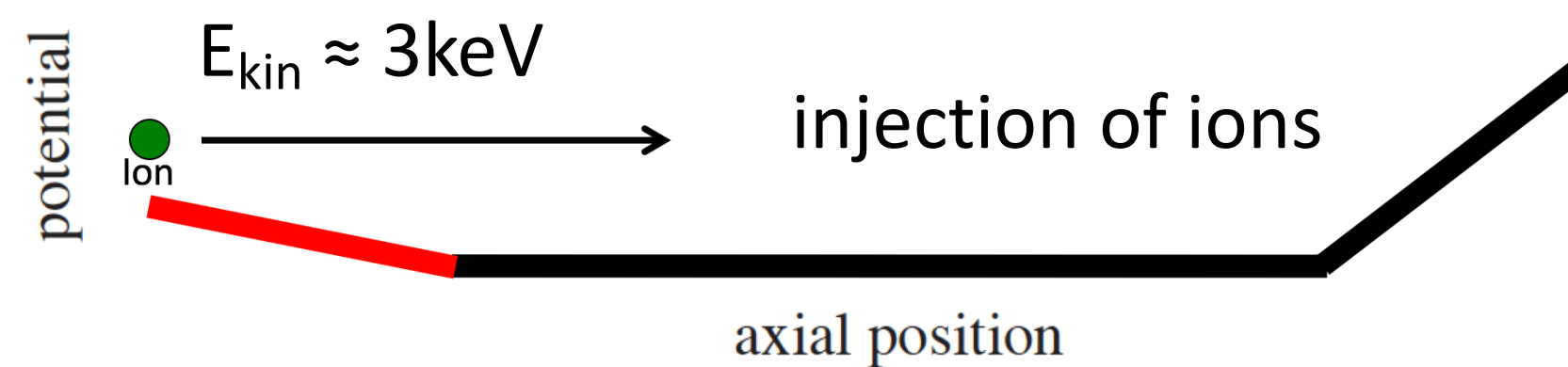
* room temperature equivalent pressure

The MR-TOF-MS principle

H.Wollnik and M. Przewloka, Int. J. Mass Spectrom. Ion Proc. 96, 267 (1990)



Total time of flight predominantly determined by the **electrostatic term** of the system

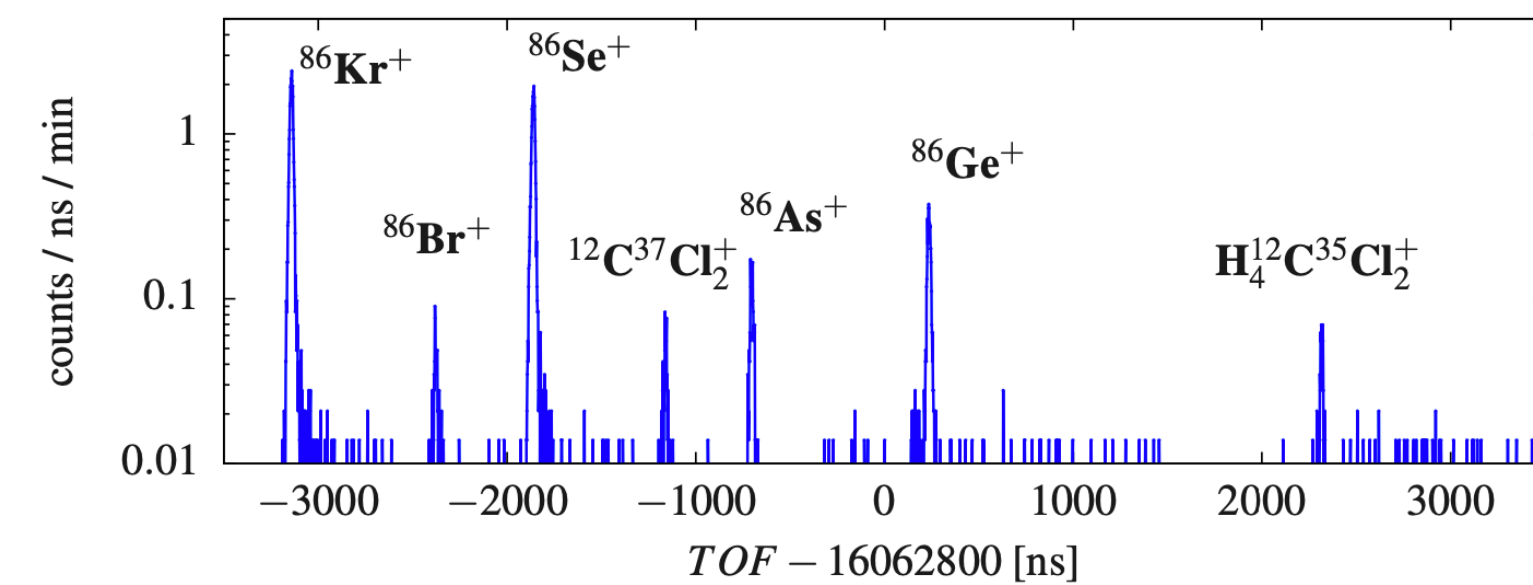
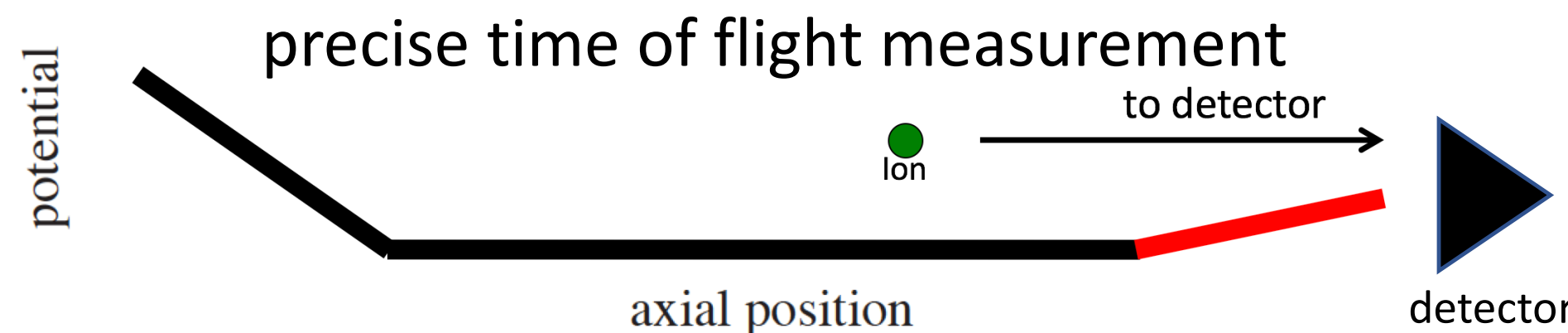
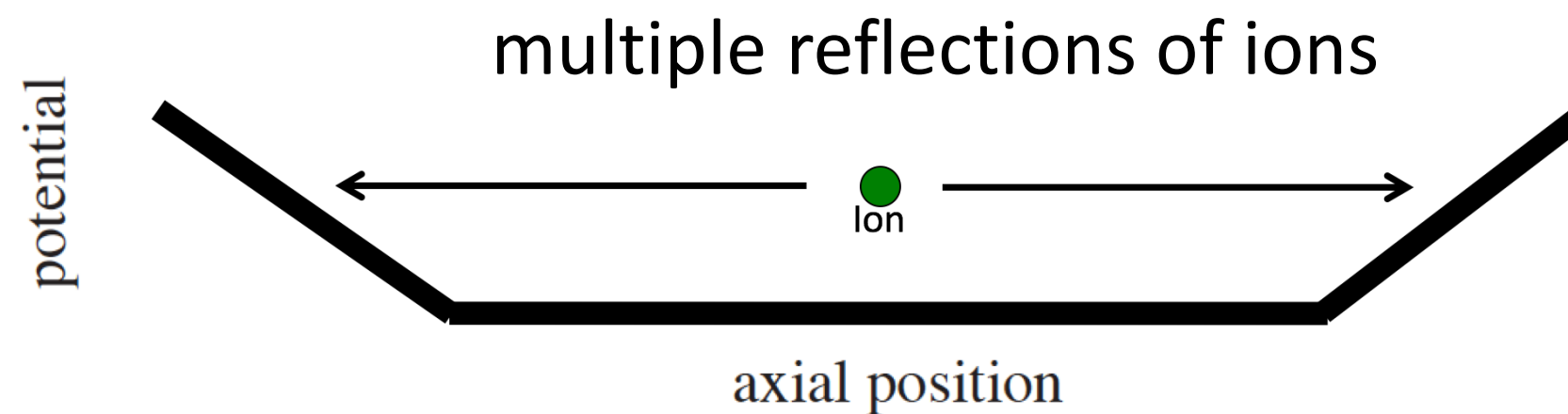


$$\overline{t(q, m)} = A \cdot \sqrt{\frac{m}{q}}$$

average from ion distribution

device constant

electrostatic contribution



Flight path of a few kilometers possible

Courtesy of M. Rosenbusch

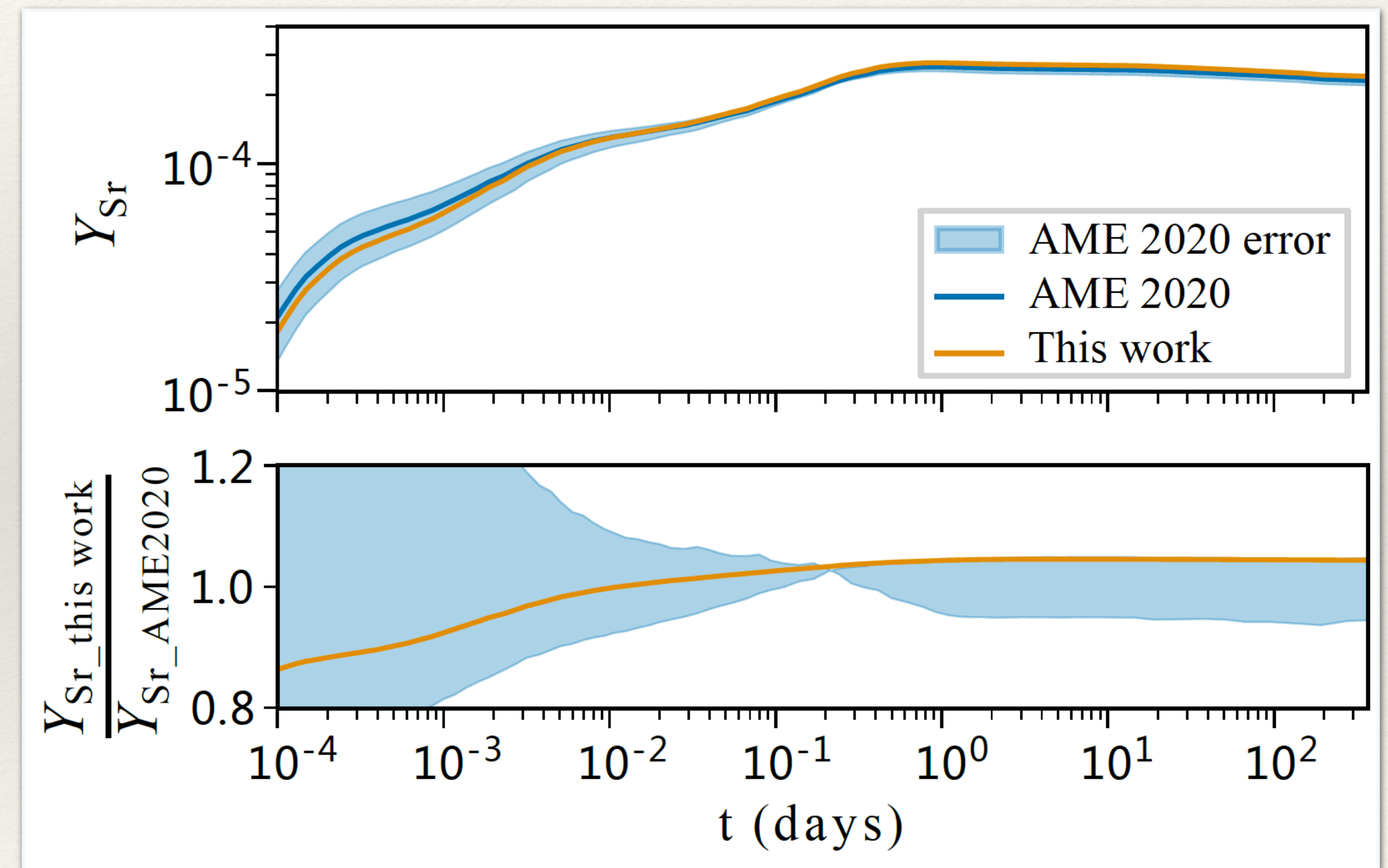
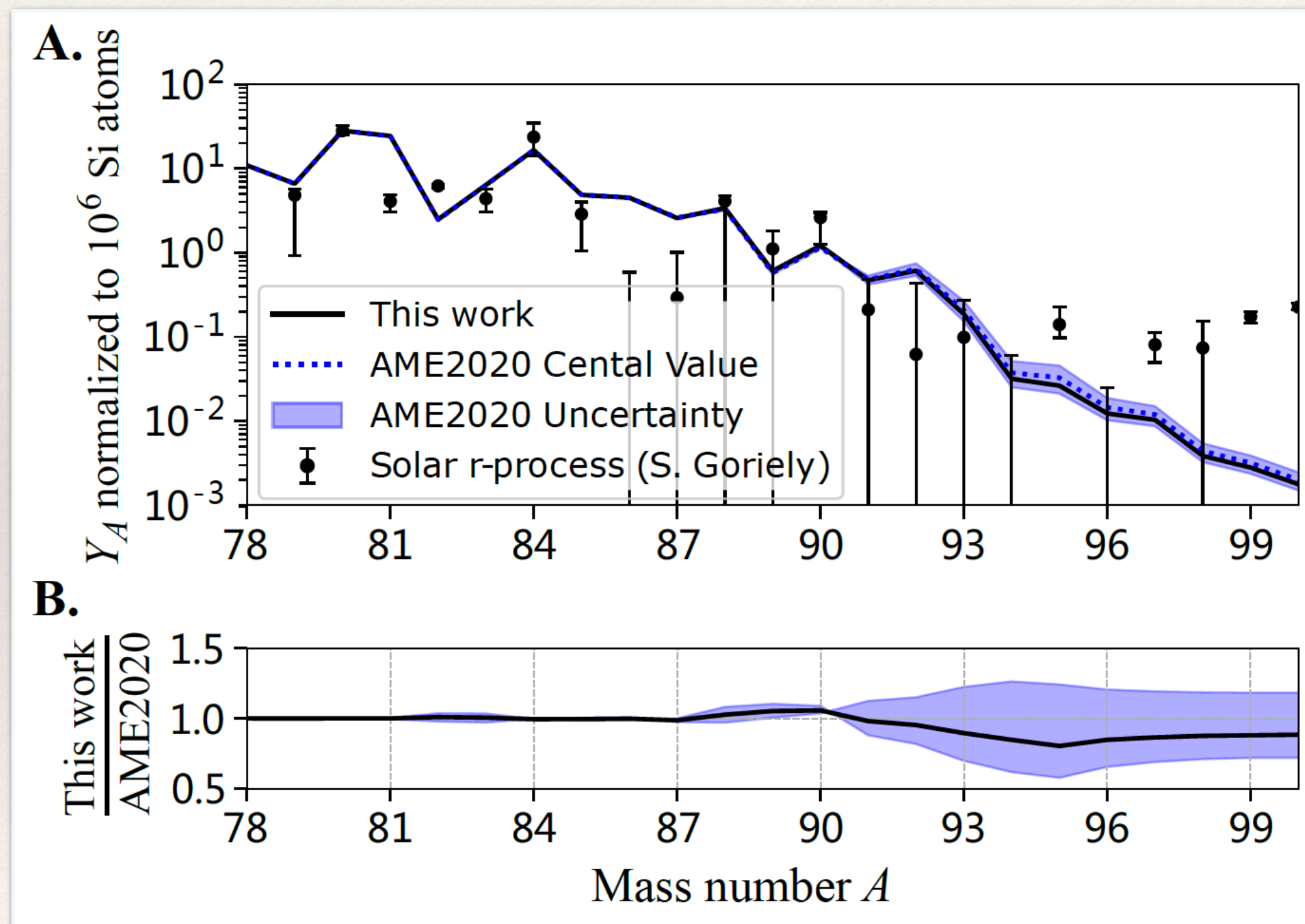
Mass measurements around $A=90$

$^{83,84}\text{Ga}$, $^{82-86}\text{Ge}$, $^{82-89}\text{As}$, $^{82,84-91}\text{Se}$, $^{85,86,89-92}\text{Br}$, $^{89,91,92}\text{Kr}$, and ^{91}Rb

Xian et al, PRC109 (2024)

Some mass uncertainties improved from hundreds keV to $<10\text{keV}$

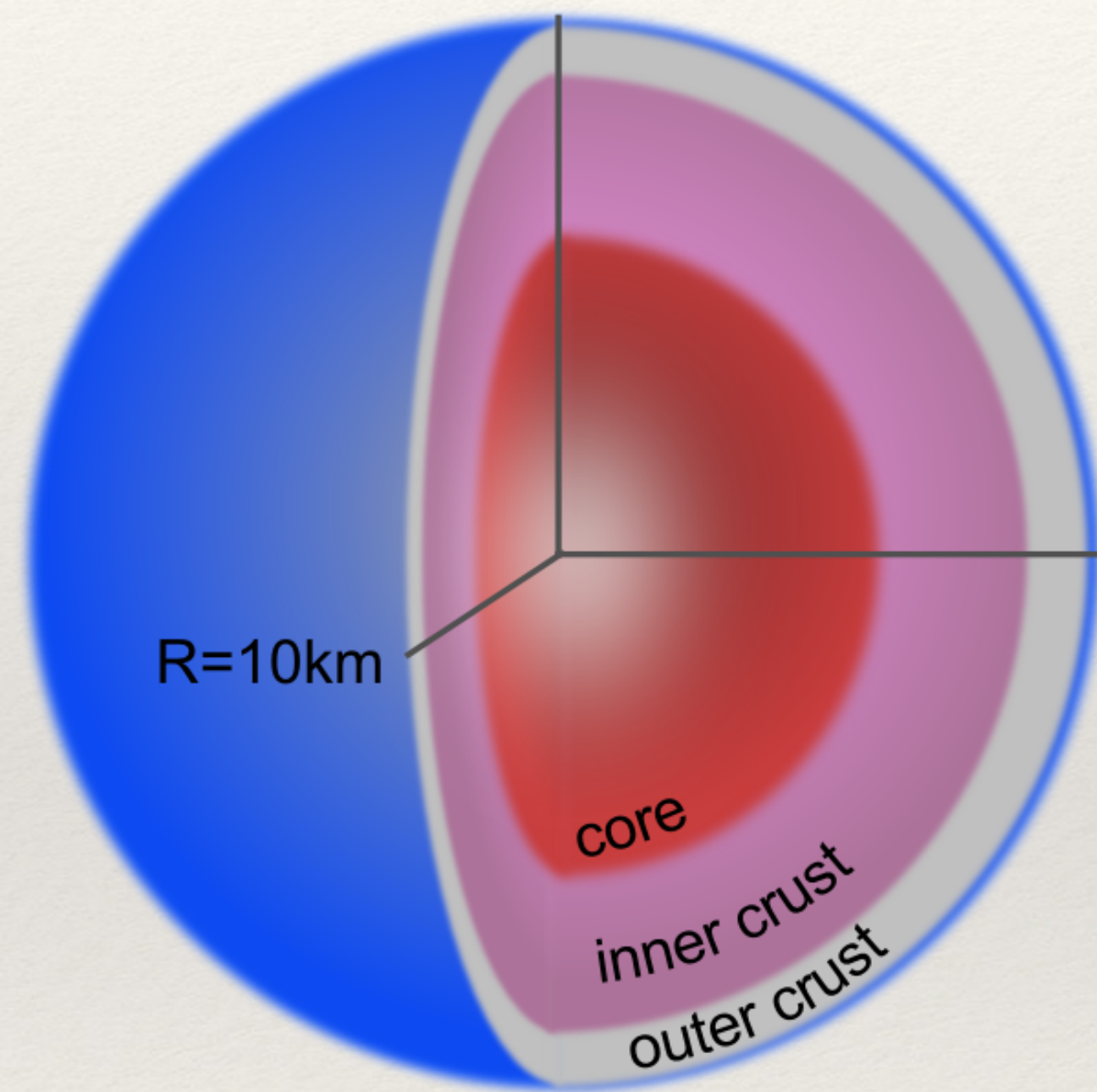
Reaction rates for all these nuclei were calculate then used to estimate the final r-process abundances



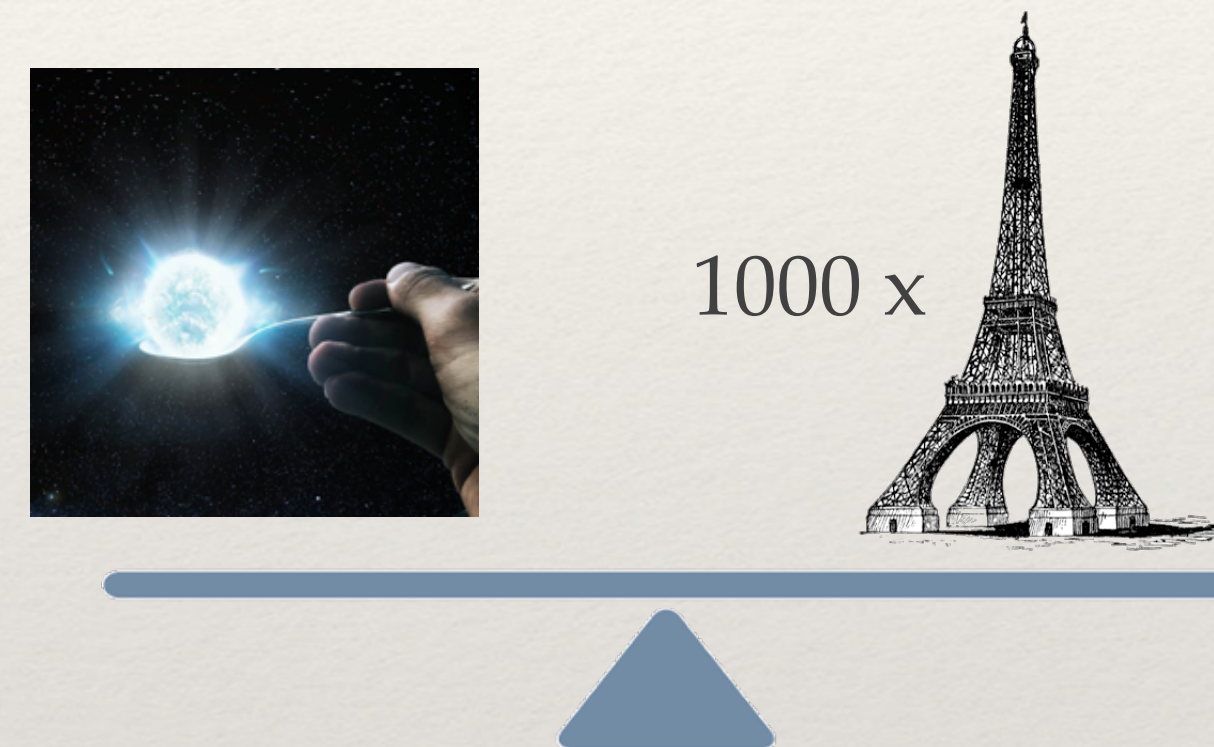
Astrophysical conditions $0.3 < Y_e < 0.42$ and entropy $S = 10 \text{ kb/baryon}$
 up to 20% difference in abundances compared to AME2020
 Moderately n-rich

Later time \rightarrow smaller difference in Sr abundance

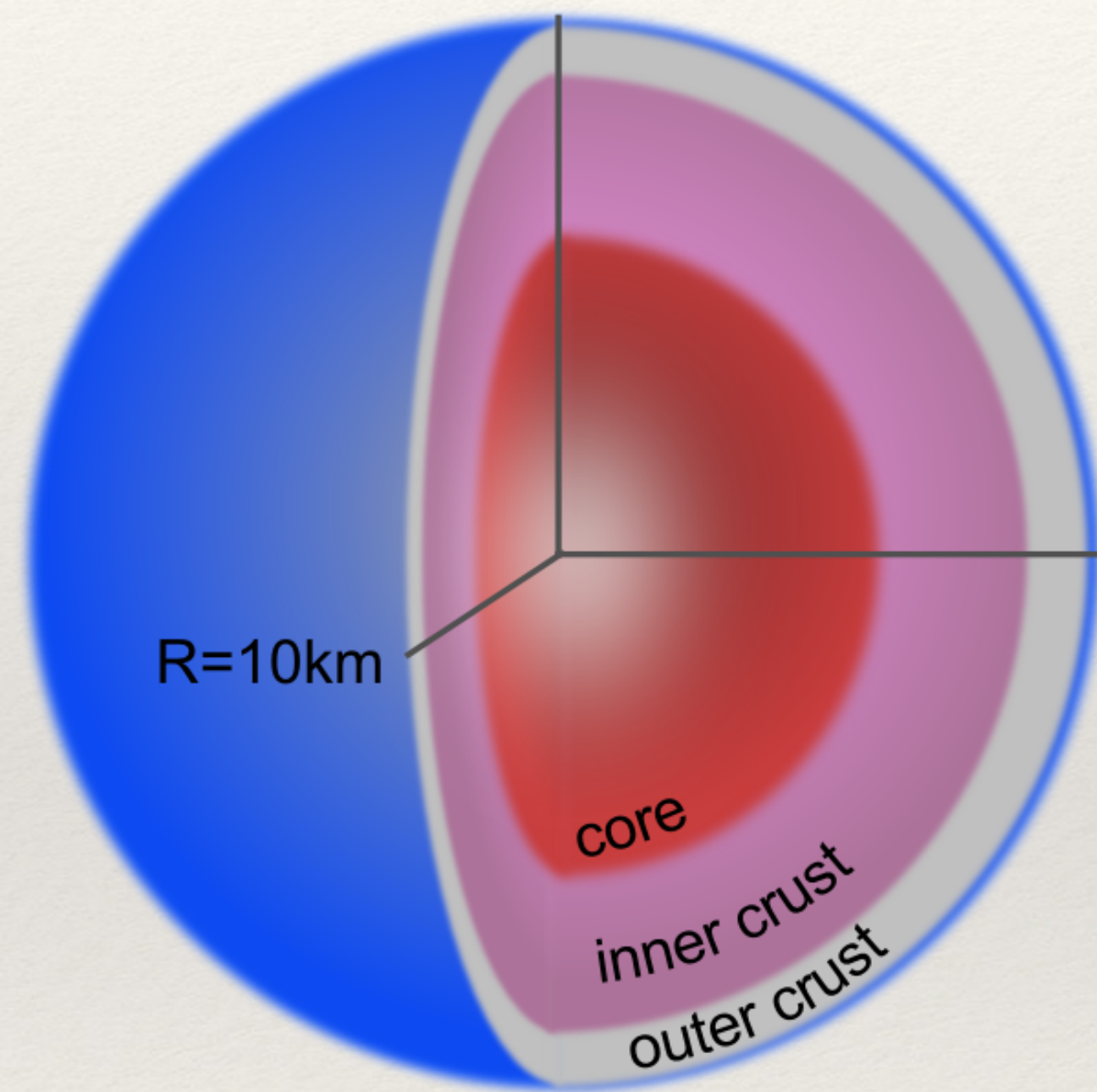
The Structure of Neutron Stars



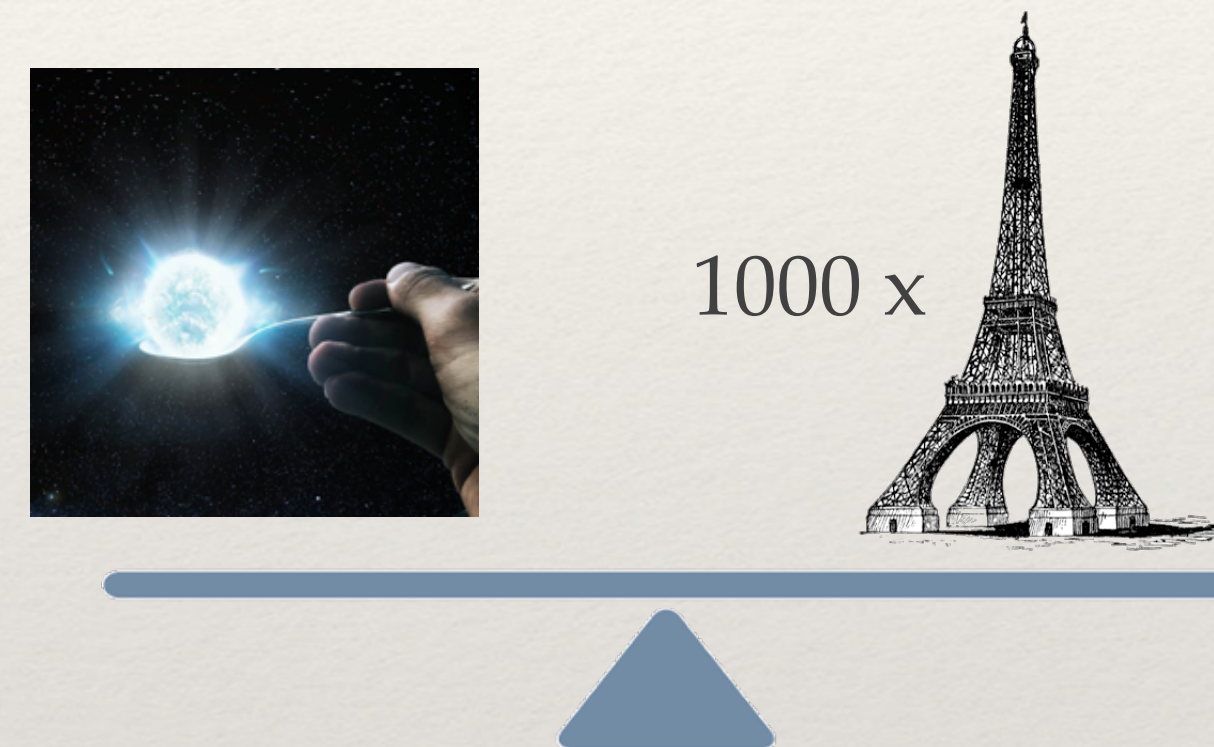
Neutron star: very compact object
 $1 M_{\odot}$ in about 10km



The Structure of Neutron Stars

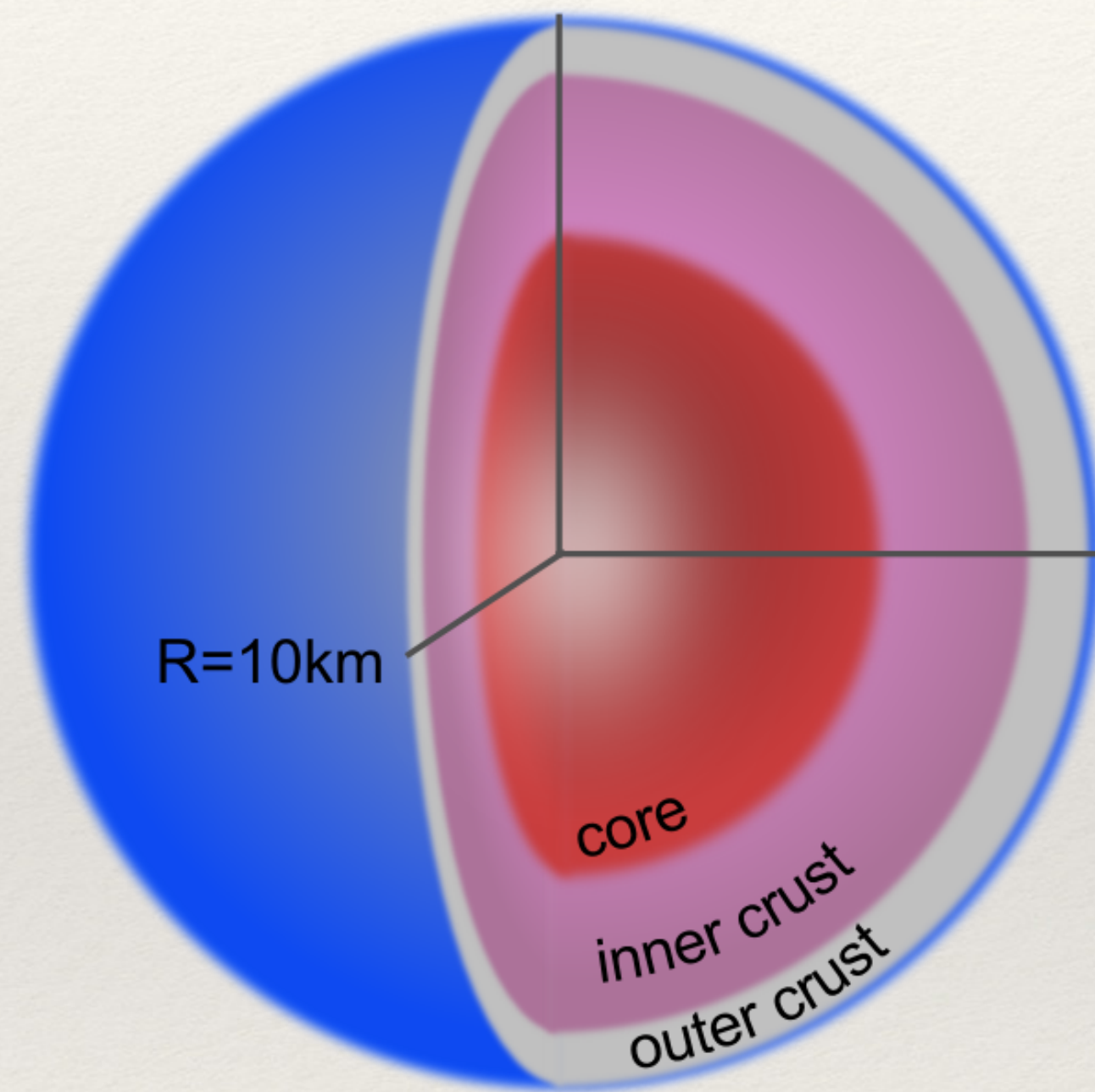


Neutron star: very compact object
 $1 M_{\odot}$ in about 10km

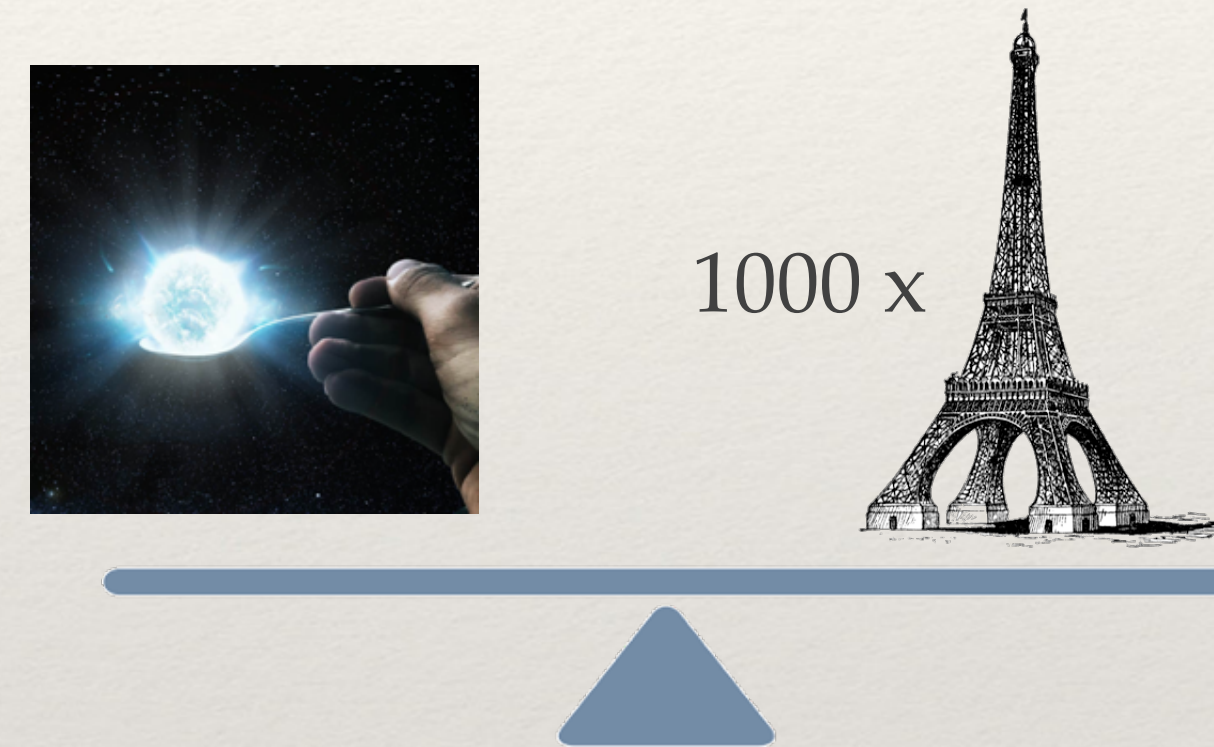


The outer crust contains
neutron-rich isotopes

The Structure of Neutron Stars



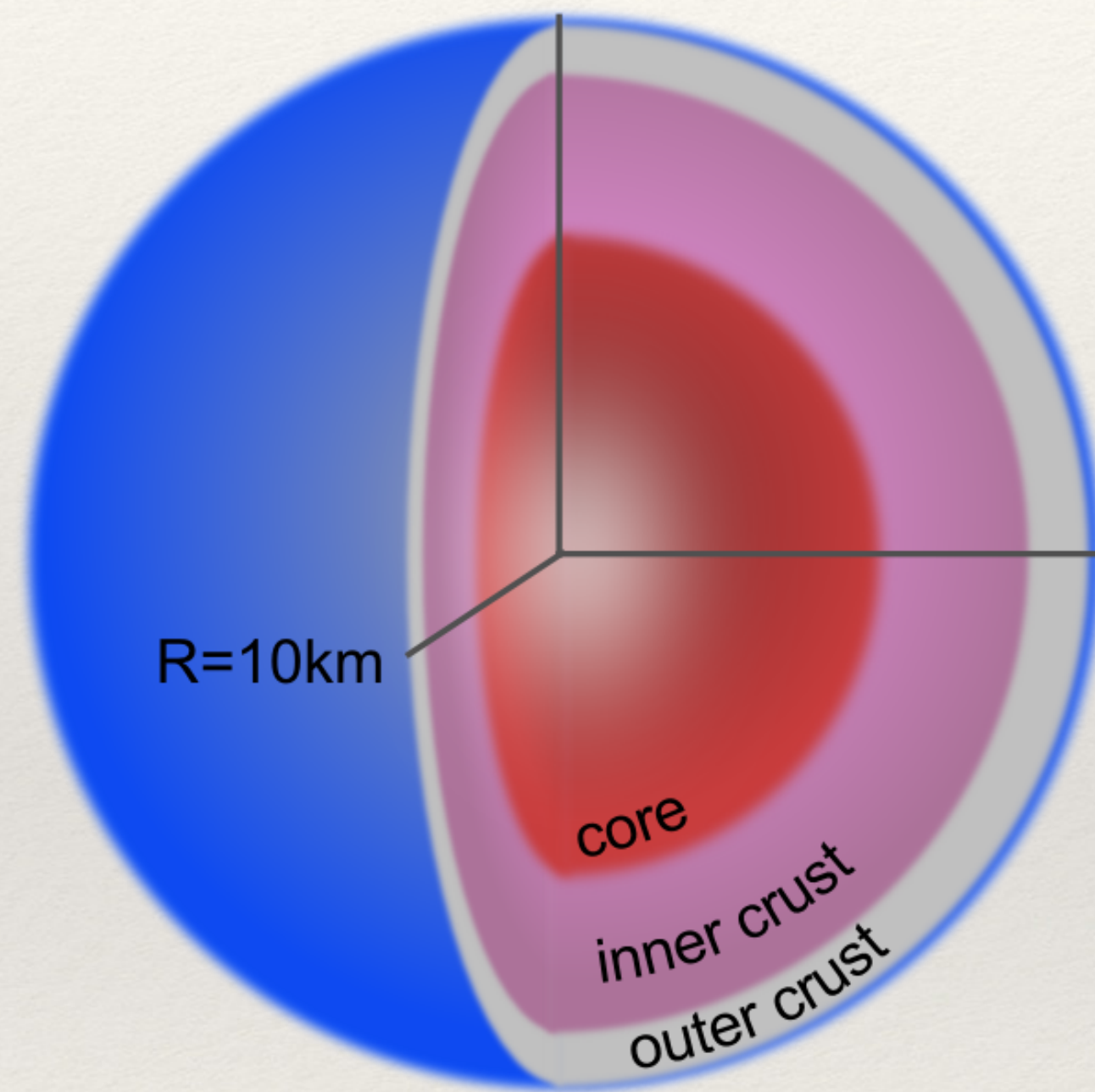
Neutron star: very compact object
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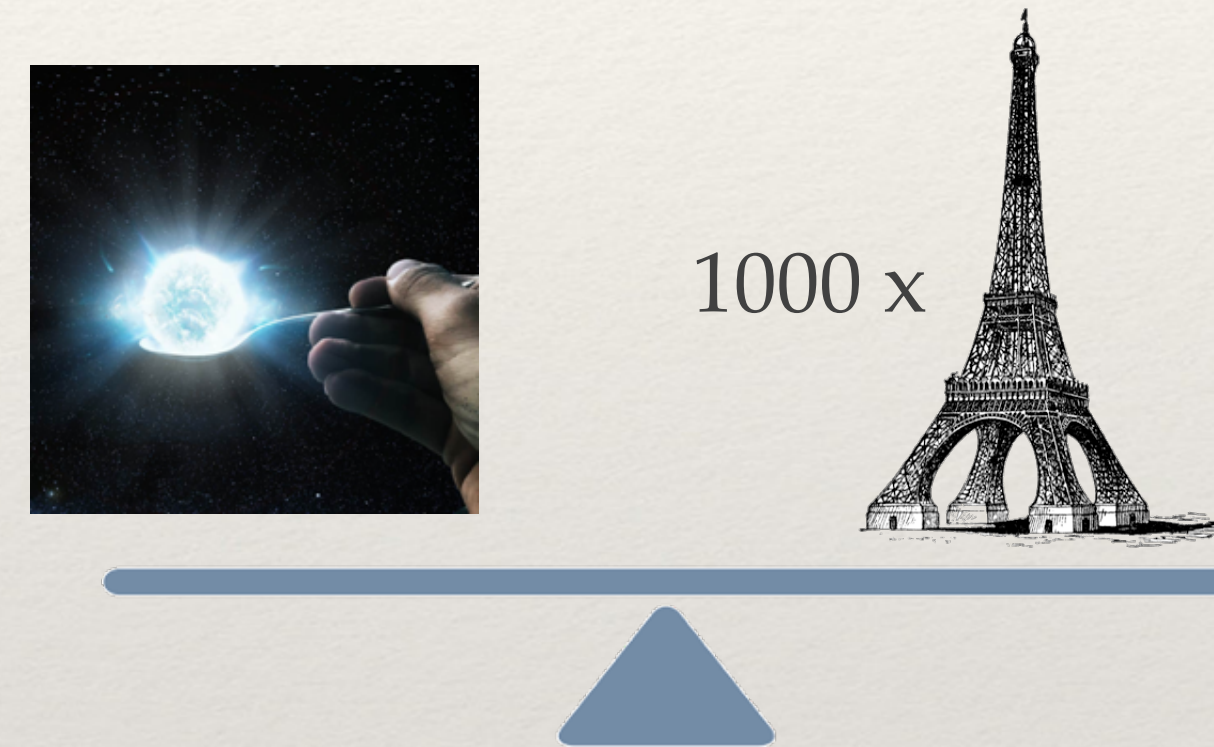
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The Structure of Neutron Stars



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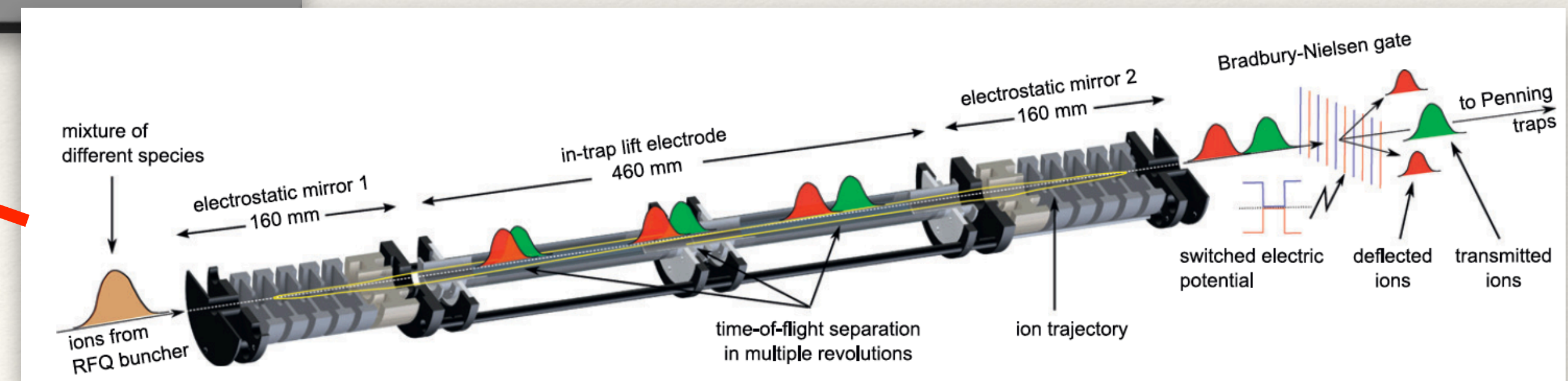
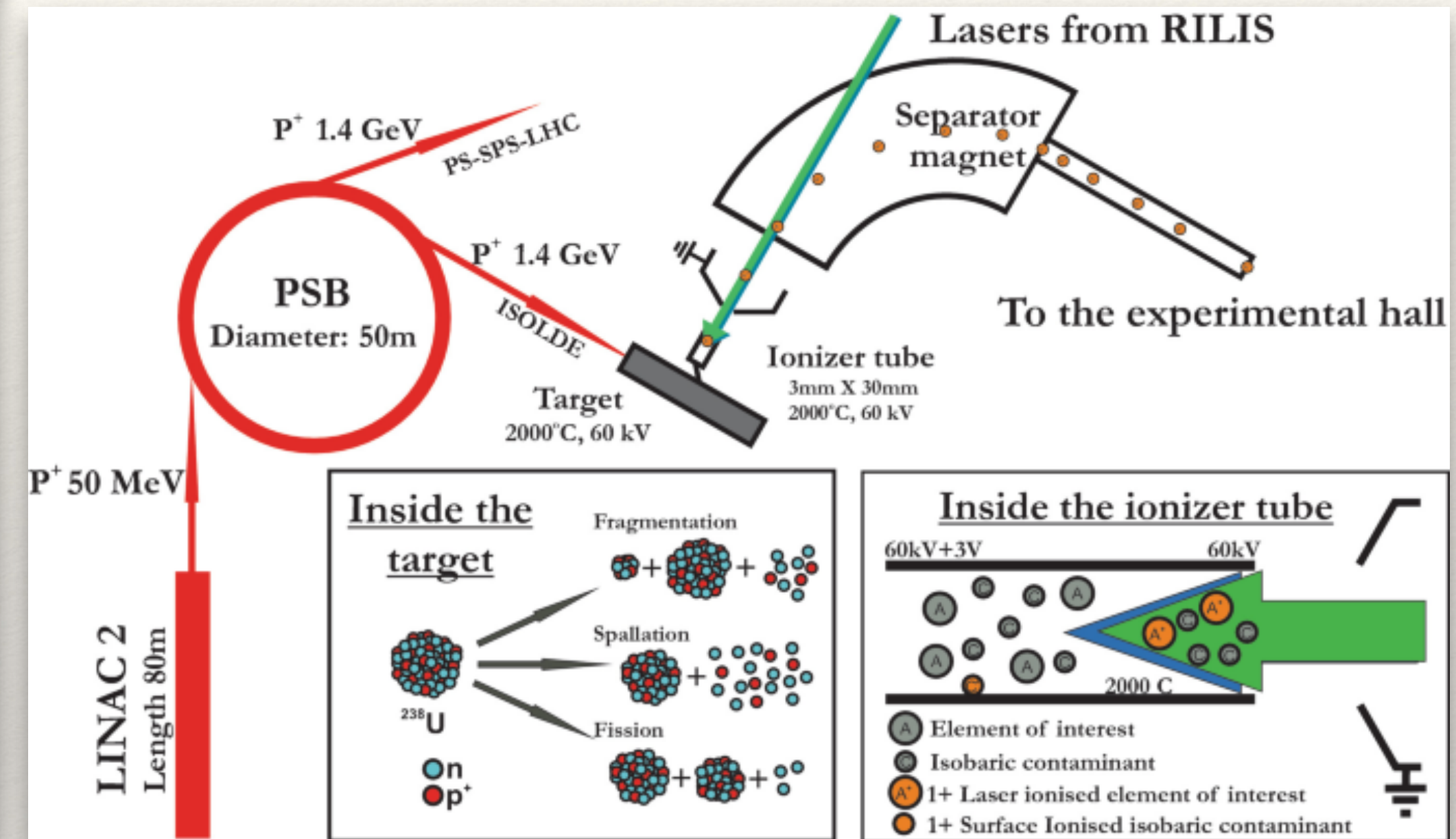
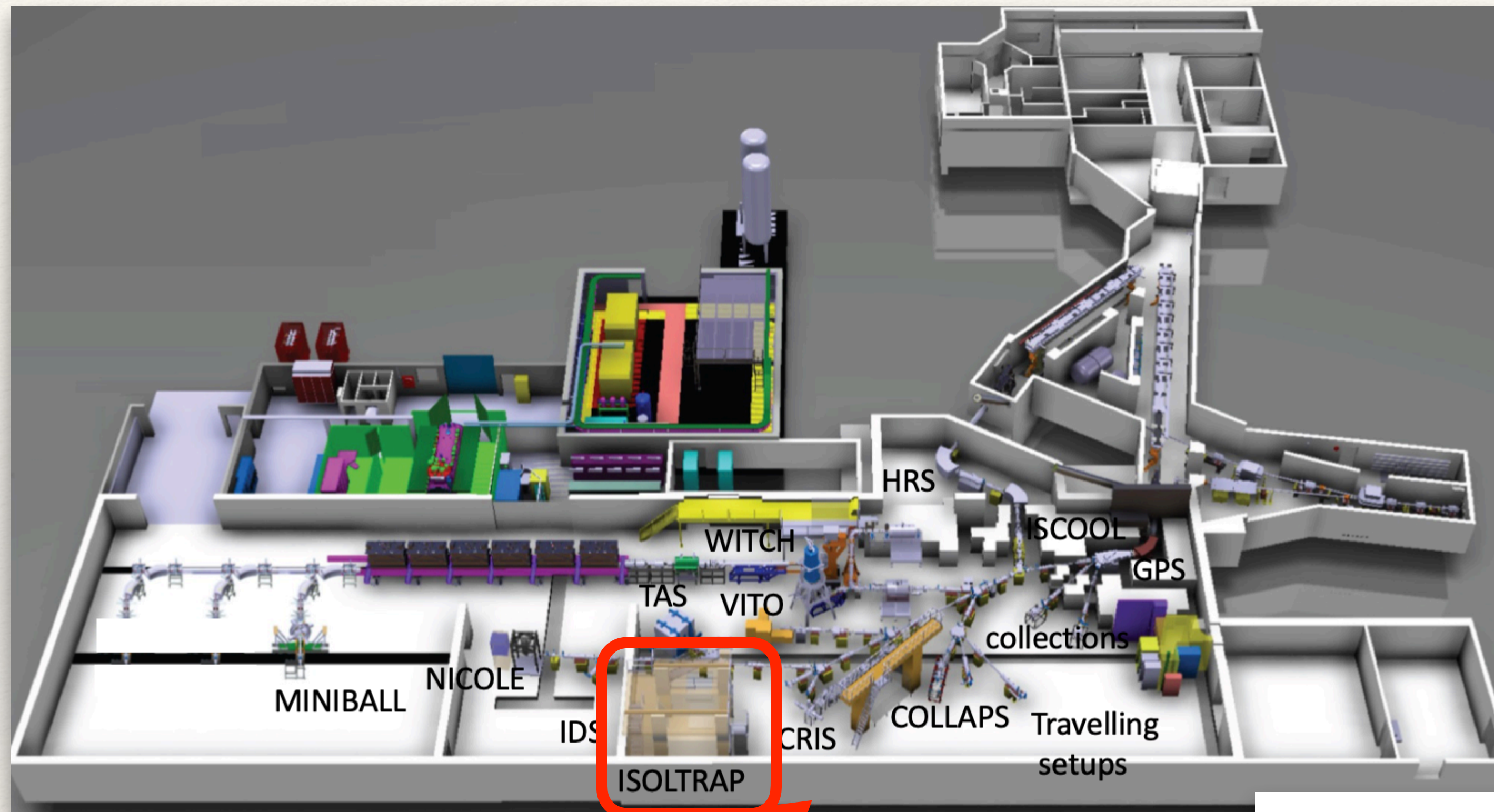


The outer crust contains
neutron-rich isotopes



Neutron-rich isotopes properties?

Mass measurement at ISOLDE/CERN



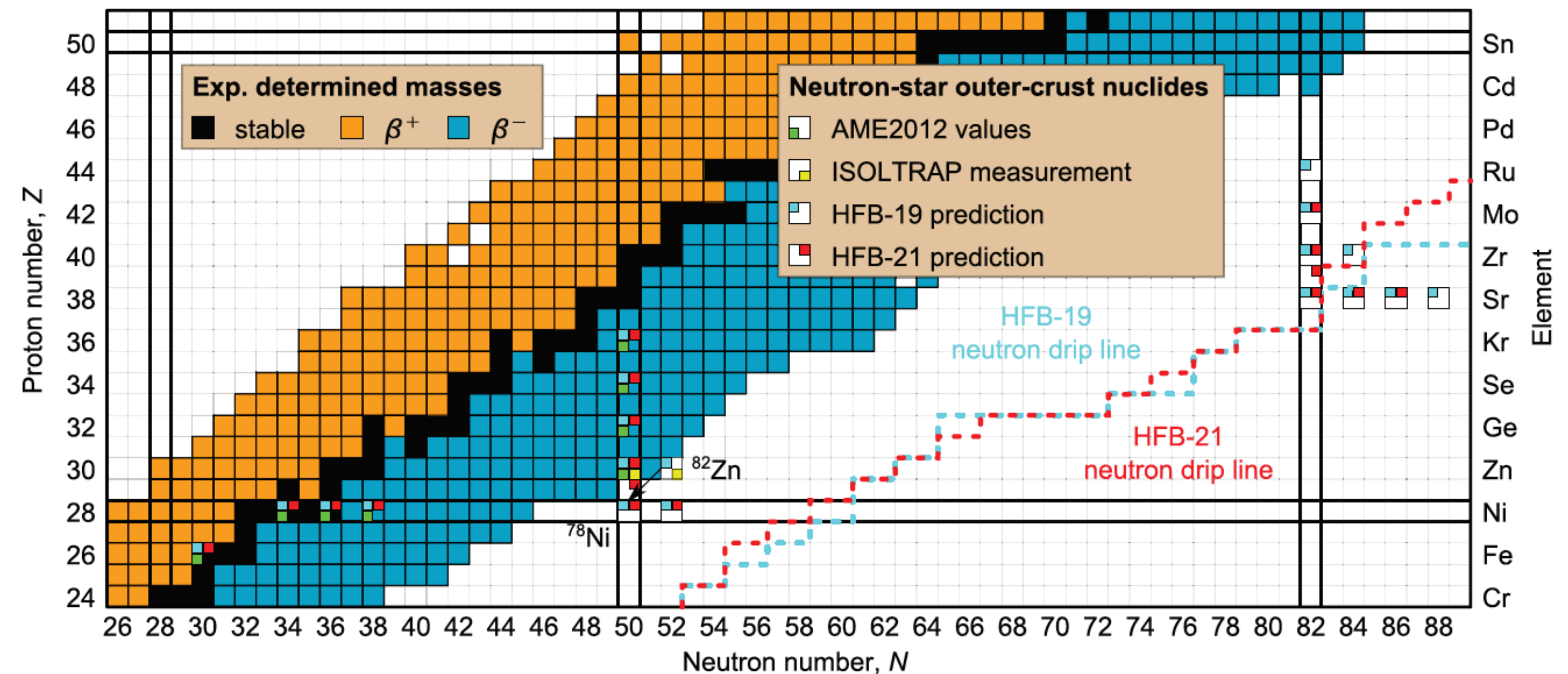
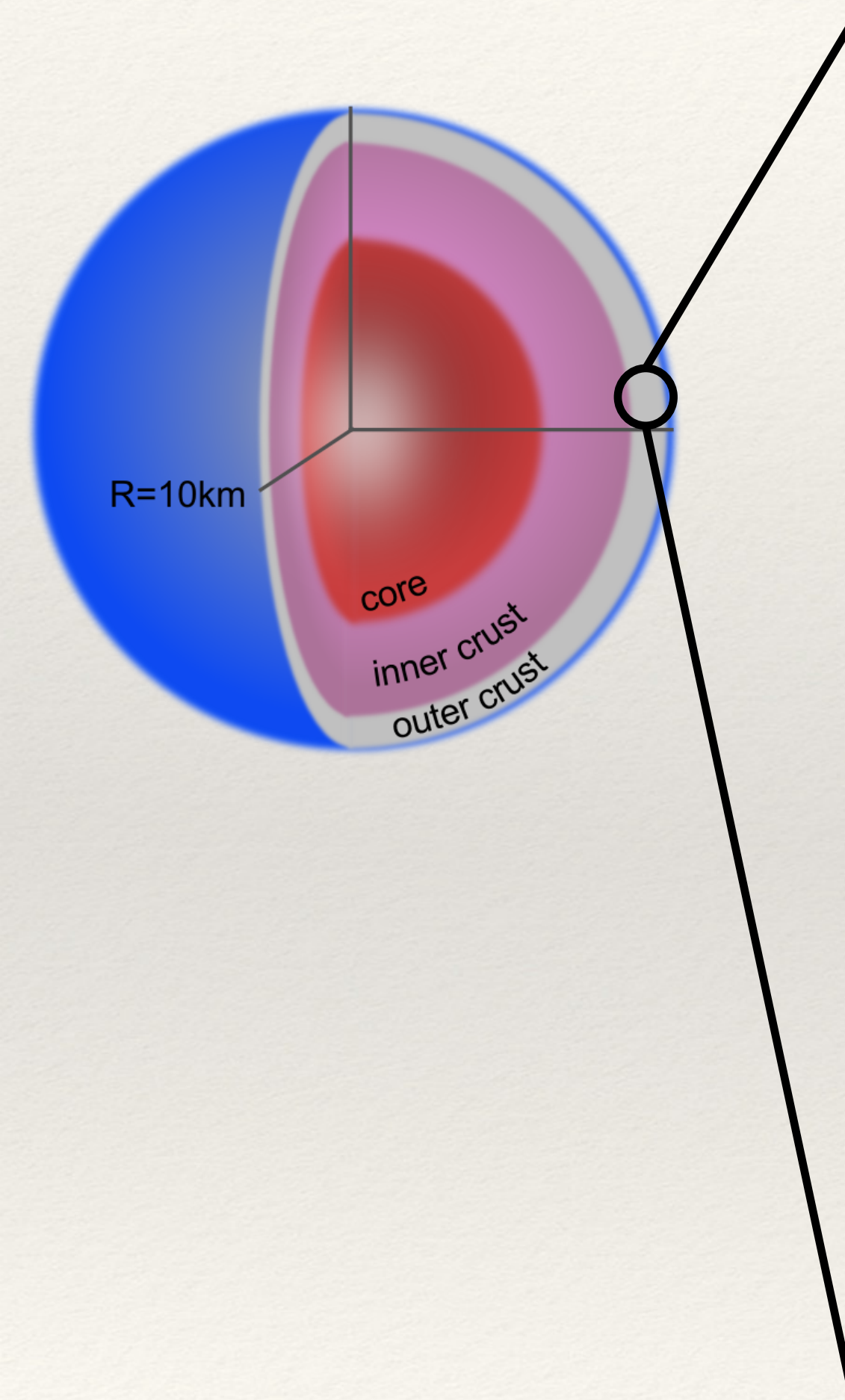
Impact on neutron star crust

R.N. Wolf et al., PRL110, 041101 (2013)

Neutron star crust composition:

General relativity equations for hydrostatic equilibrium (TOV equations)

Relate pressure, mass-energy density with the neutron star mass and radius

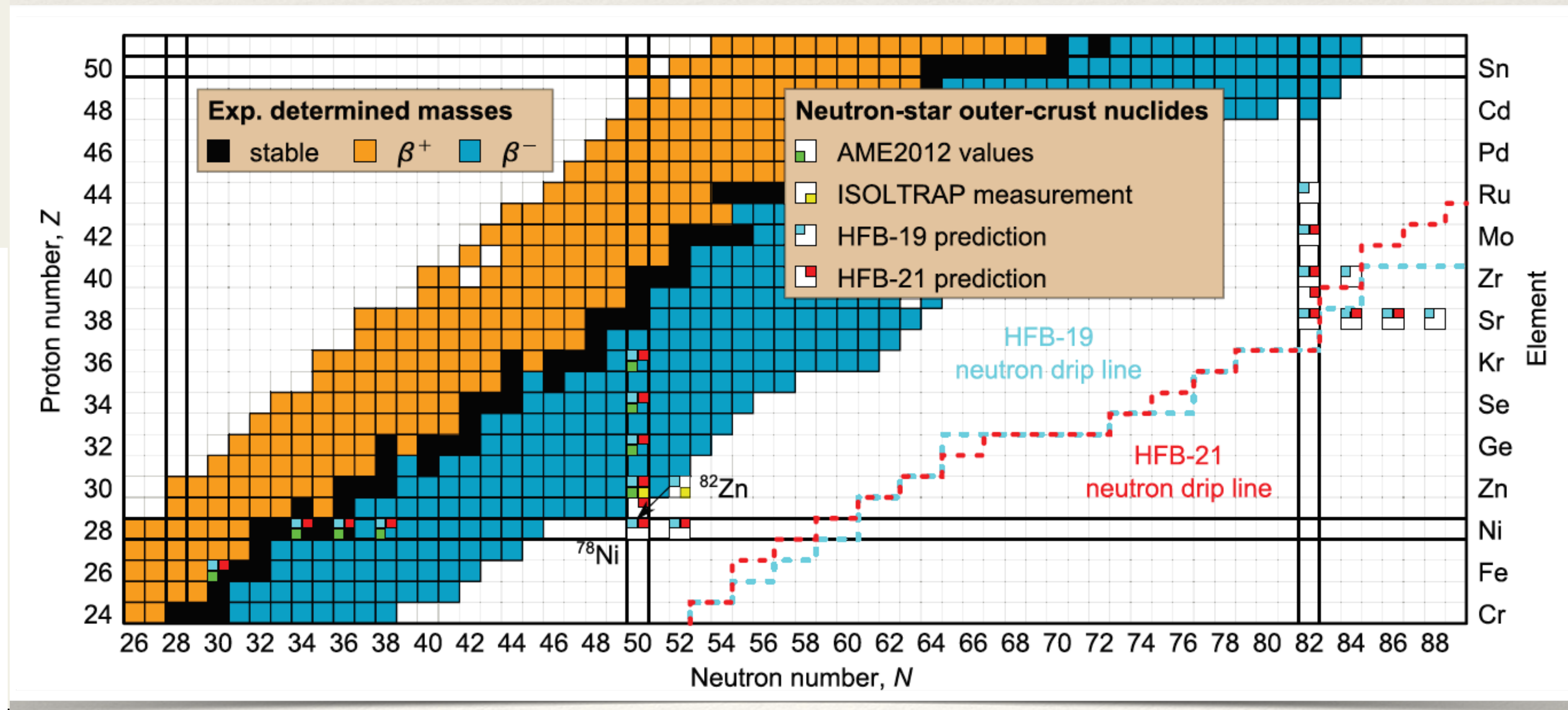
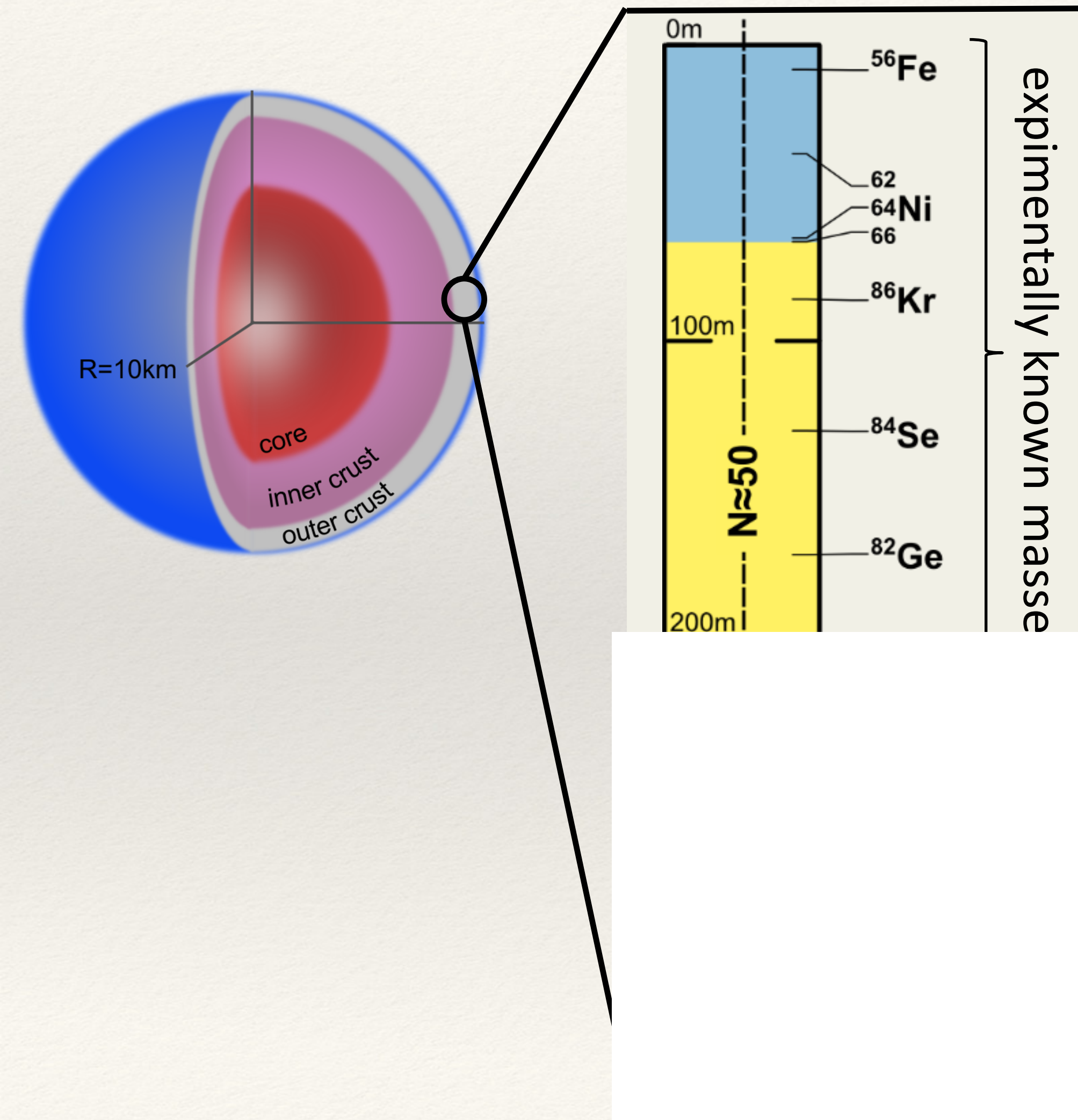


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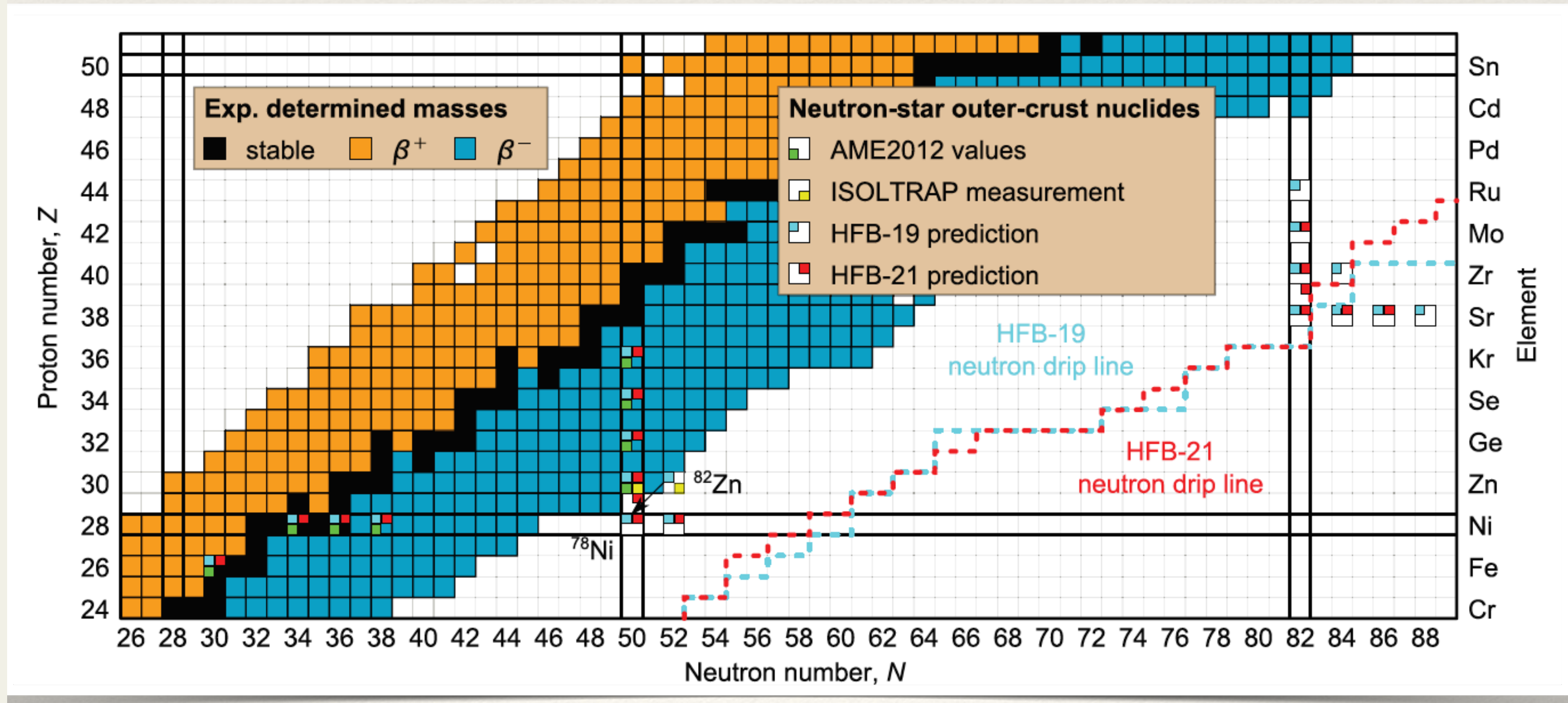
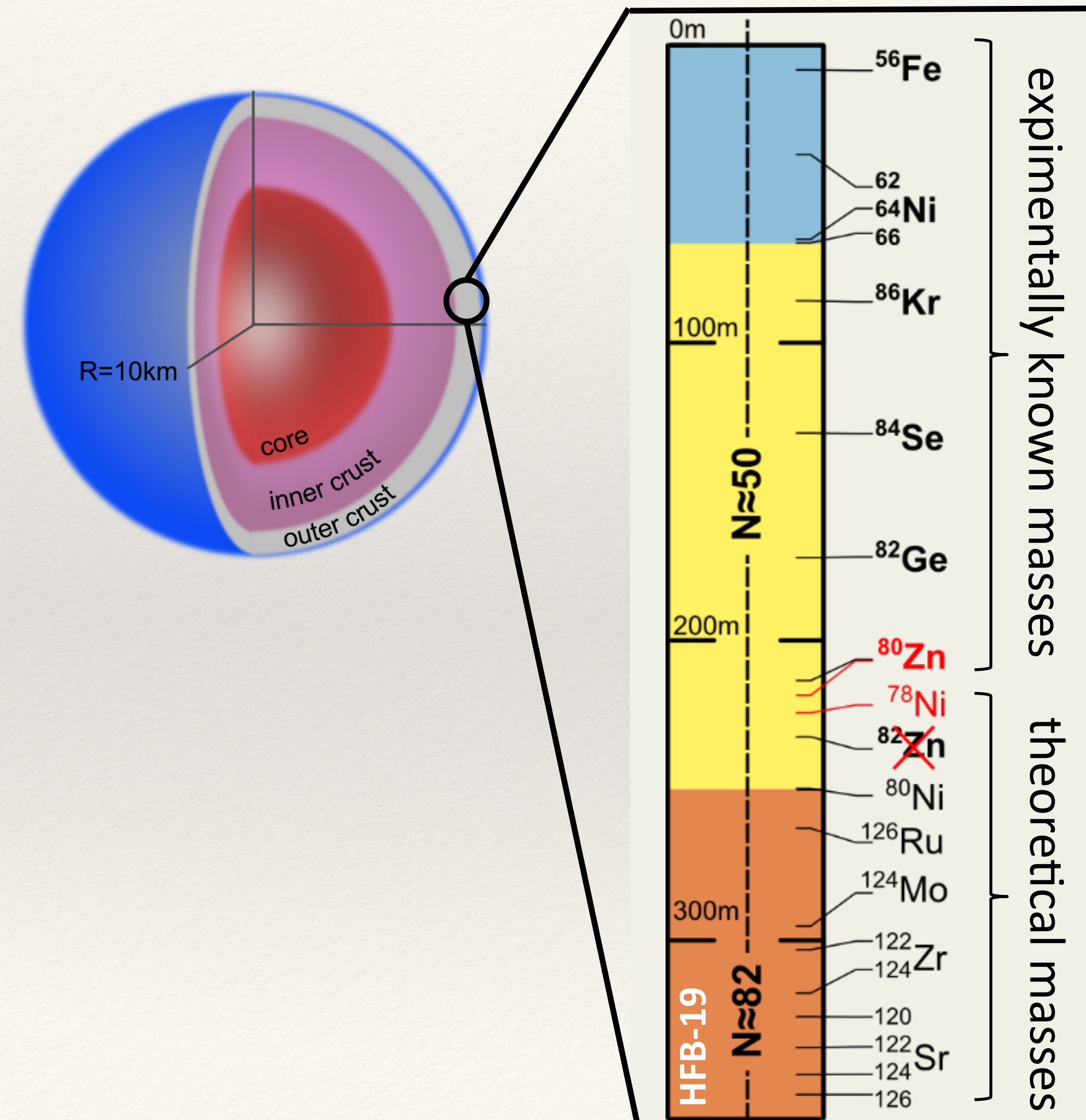


Impact on neutron star crust

R.N. Wolf et al., PRL110, 041101 (2013)

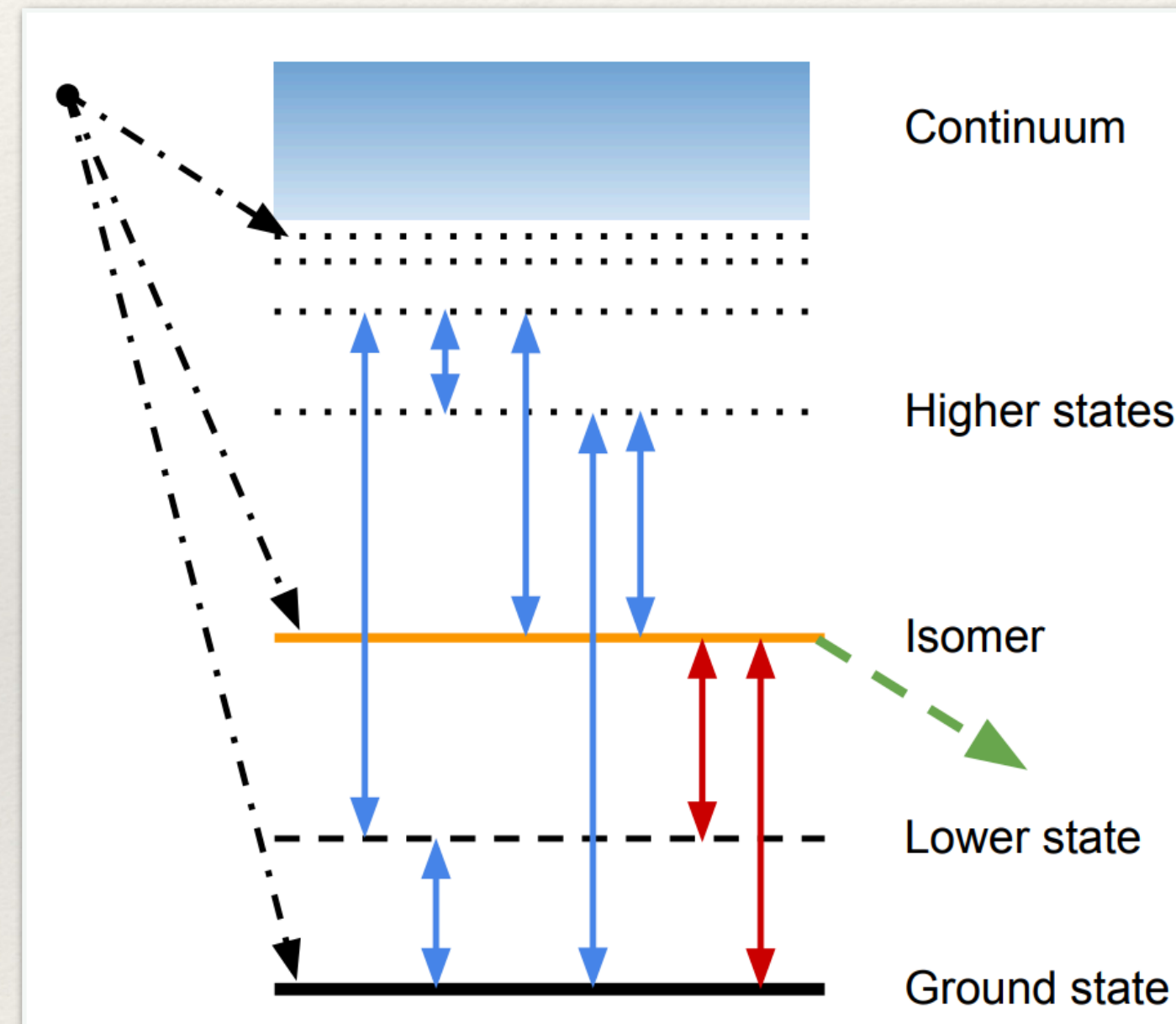
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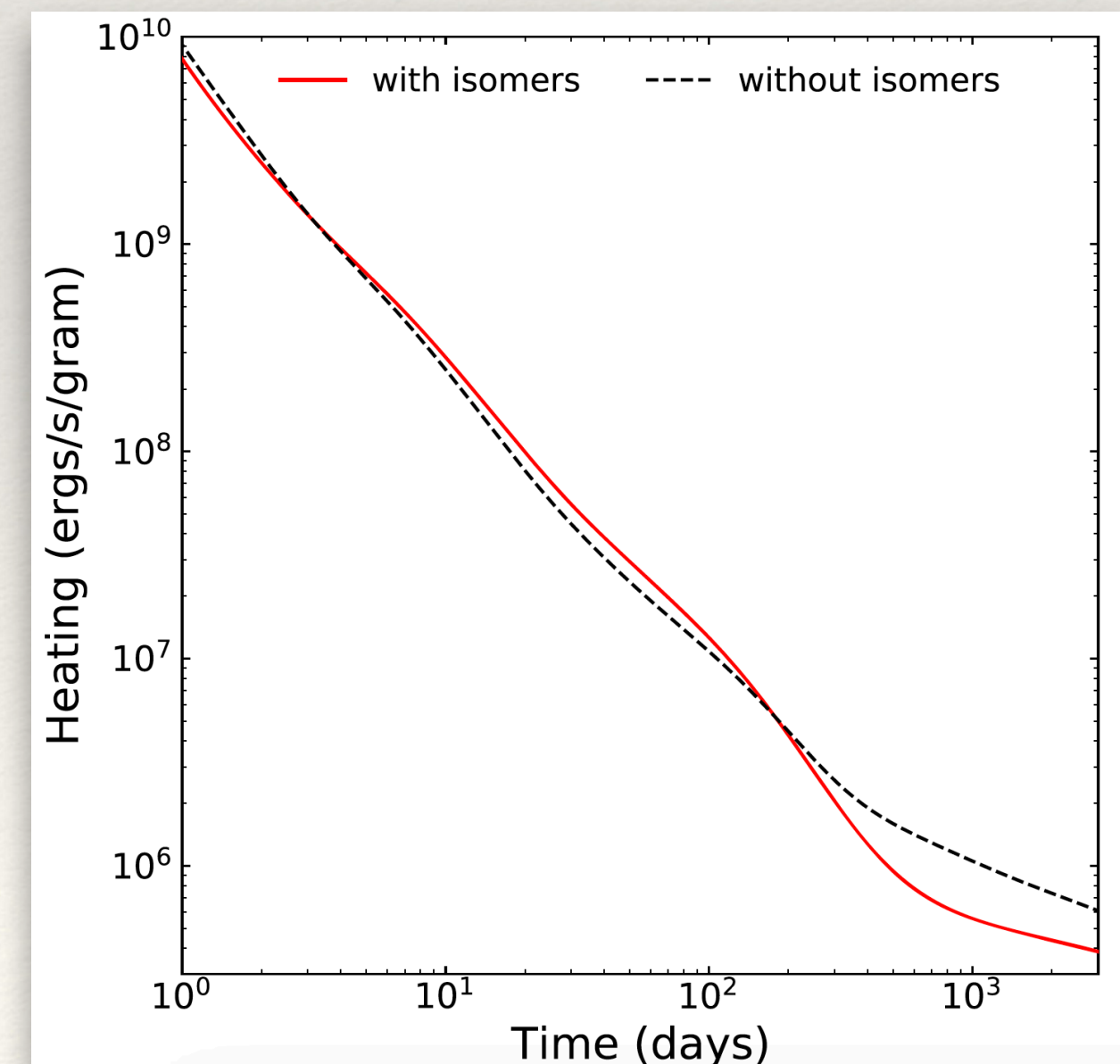
Mass spectrometry and Astromers

Astromer: a nuclear isomer that retains its metastable character in an astrophysical environment
Misch et al., ApJS 252 2 (2021)



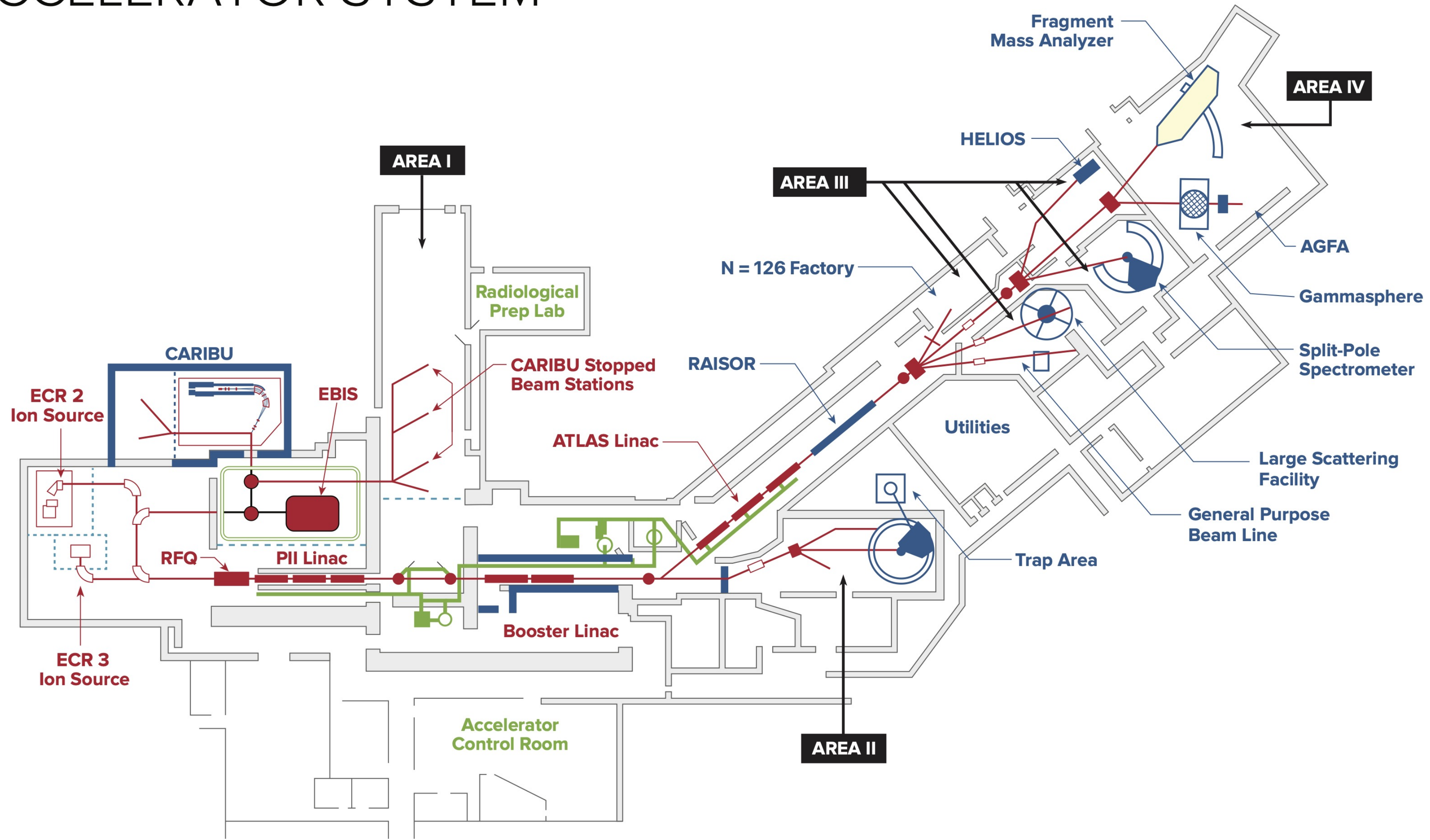
In the hot thermal bath of the stellar environment, the isomeric state is excited to higher intermediate states which in turn populate the ground state after de-excitation.

Not Astromer: Ground state = isomeric state
Astromer: Ground state \neq isomeric state



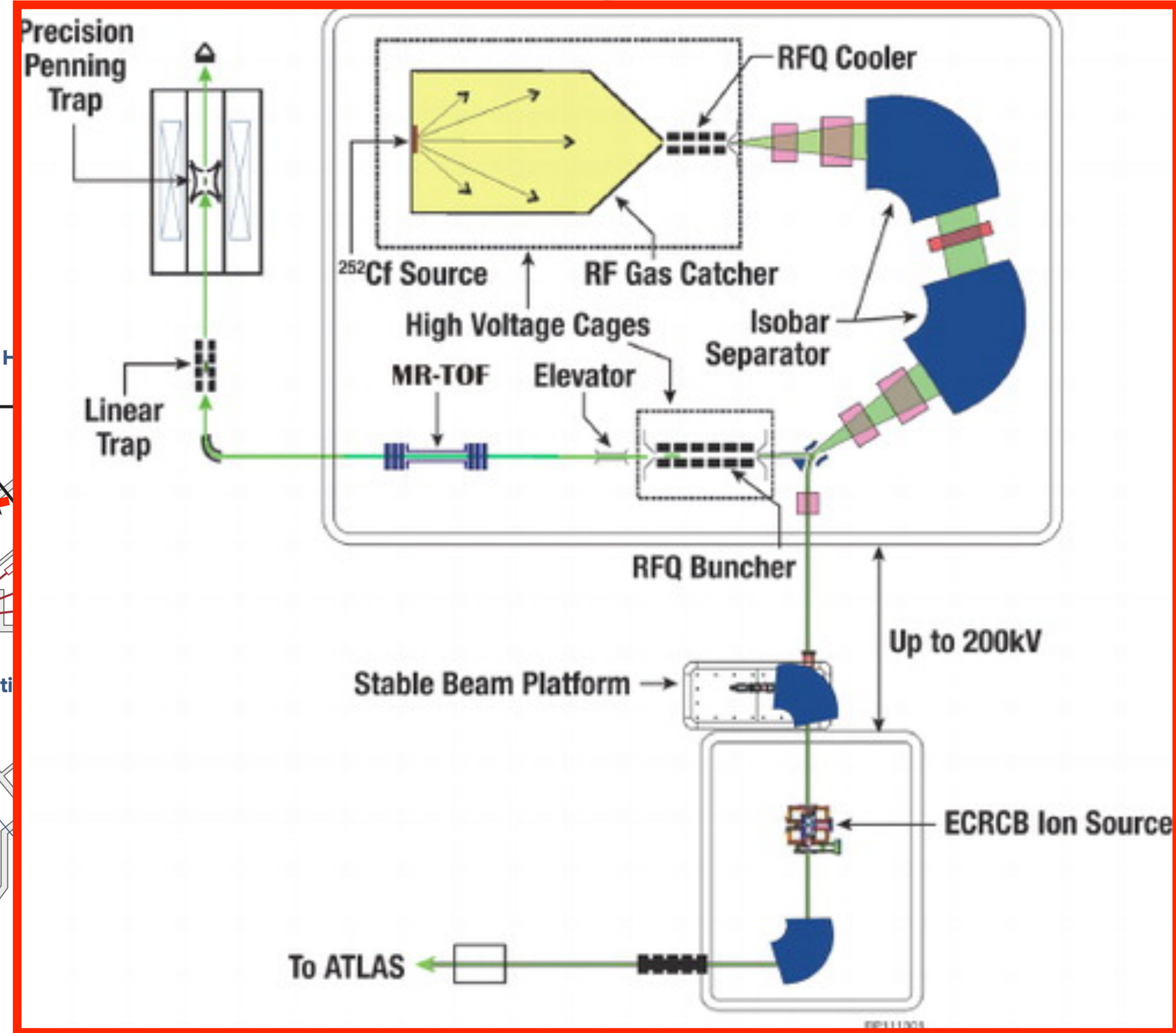
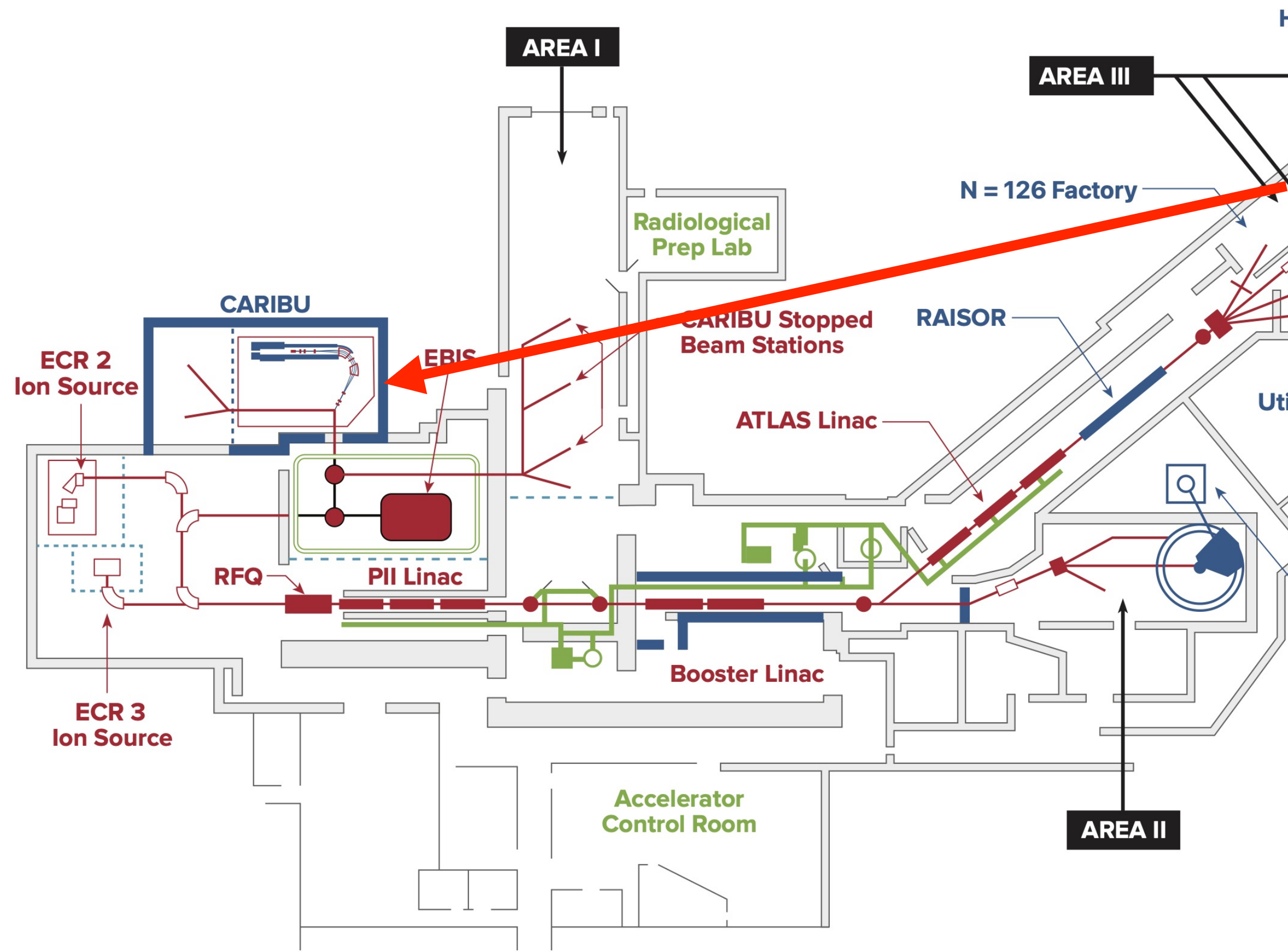
ATLAS

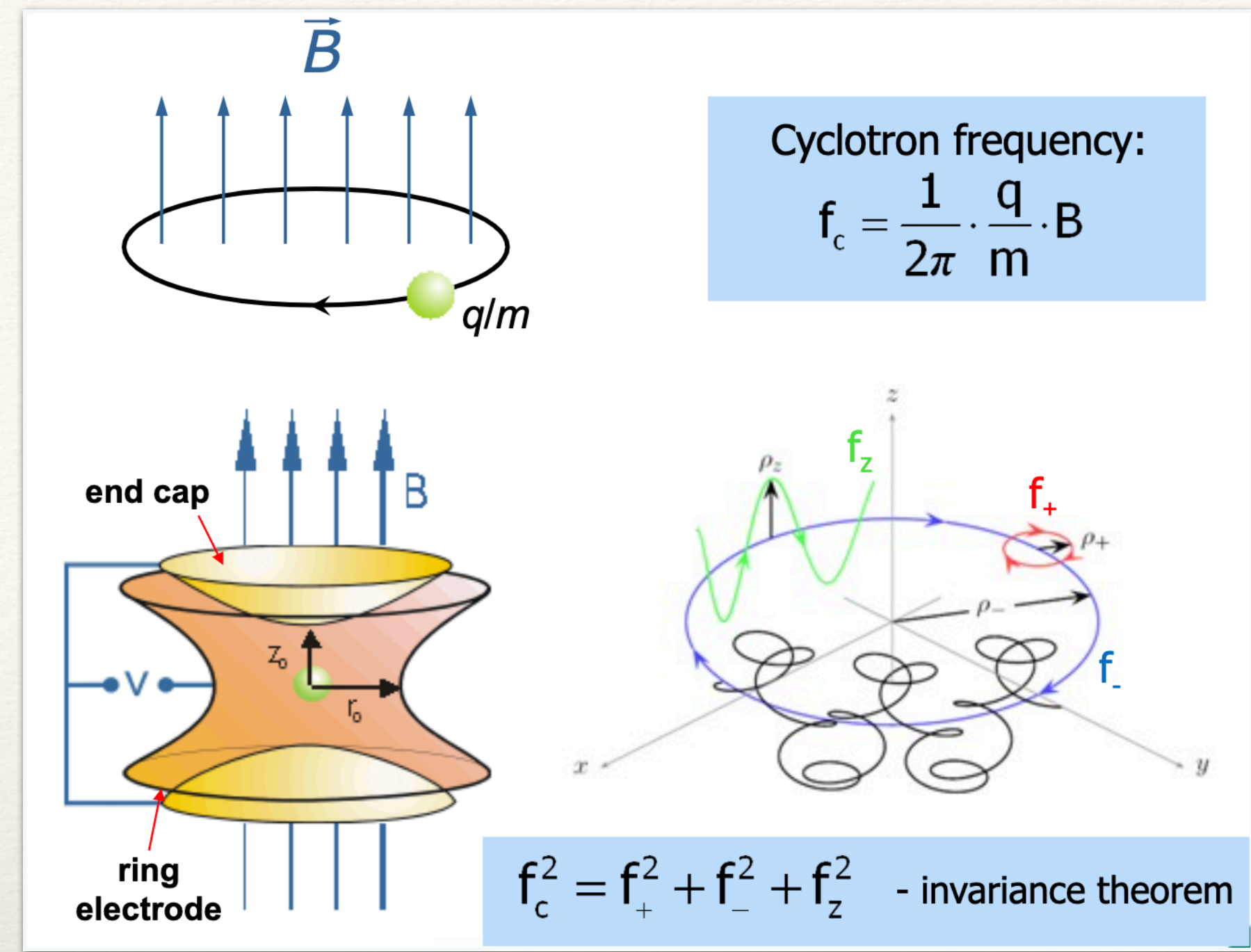
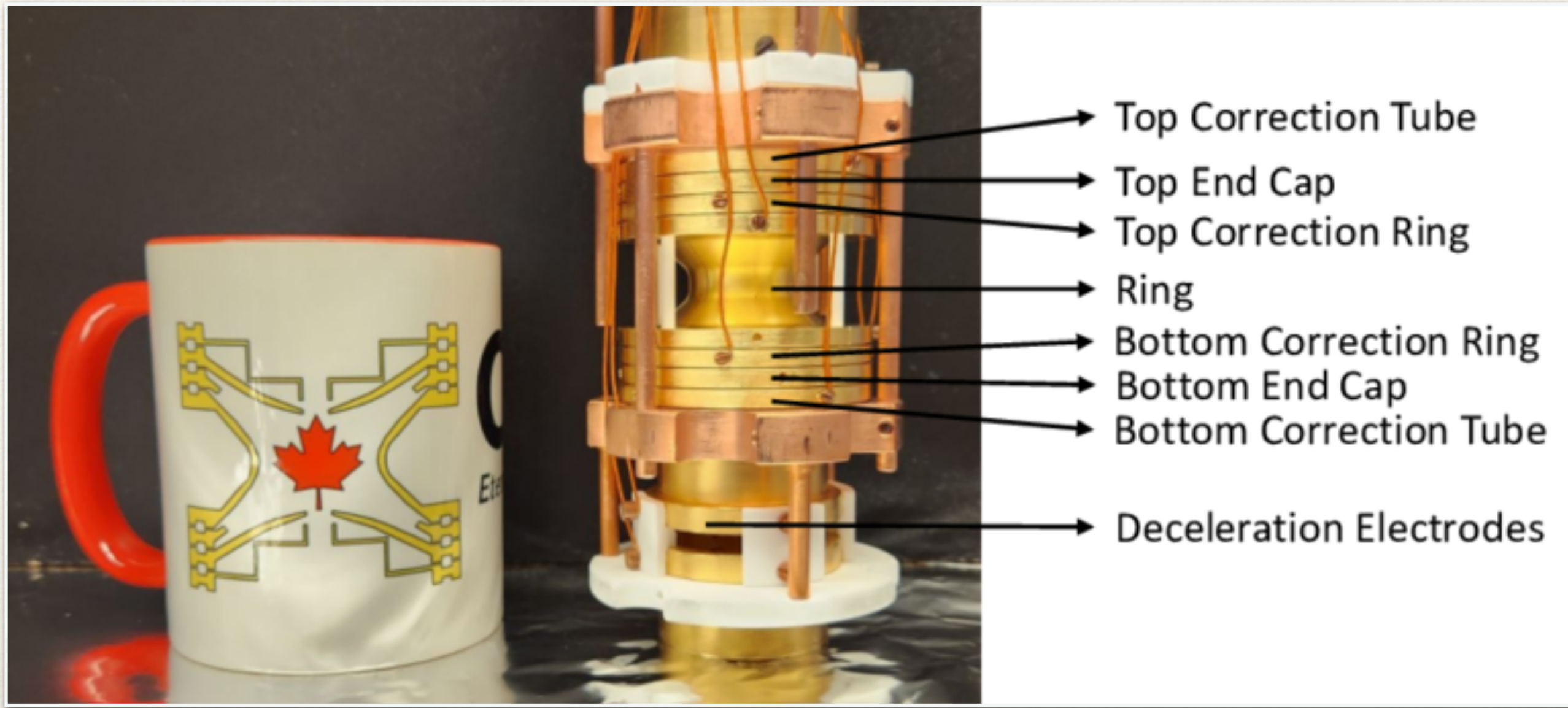
ARGONNE TANDEM LINAC ACCELERATOR SYSTEM

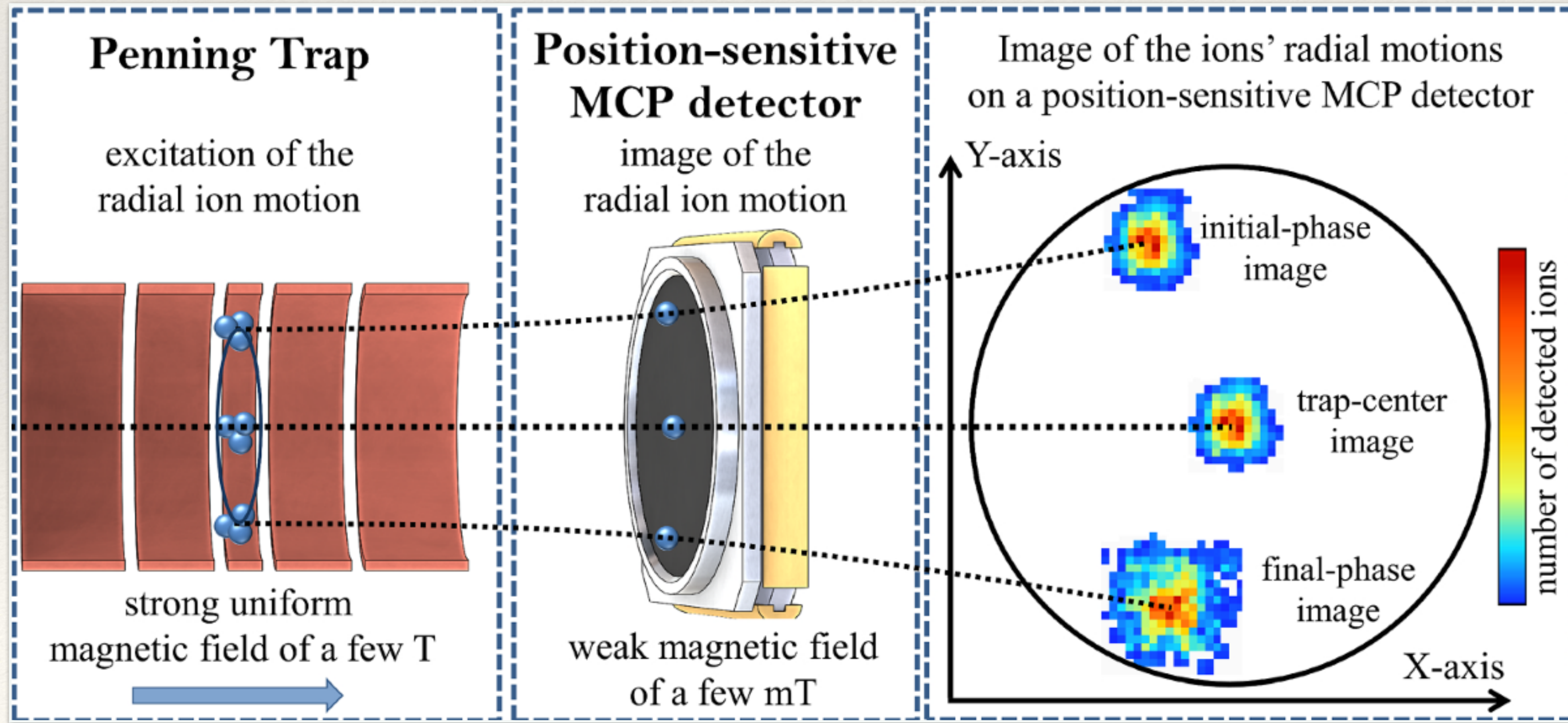
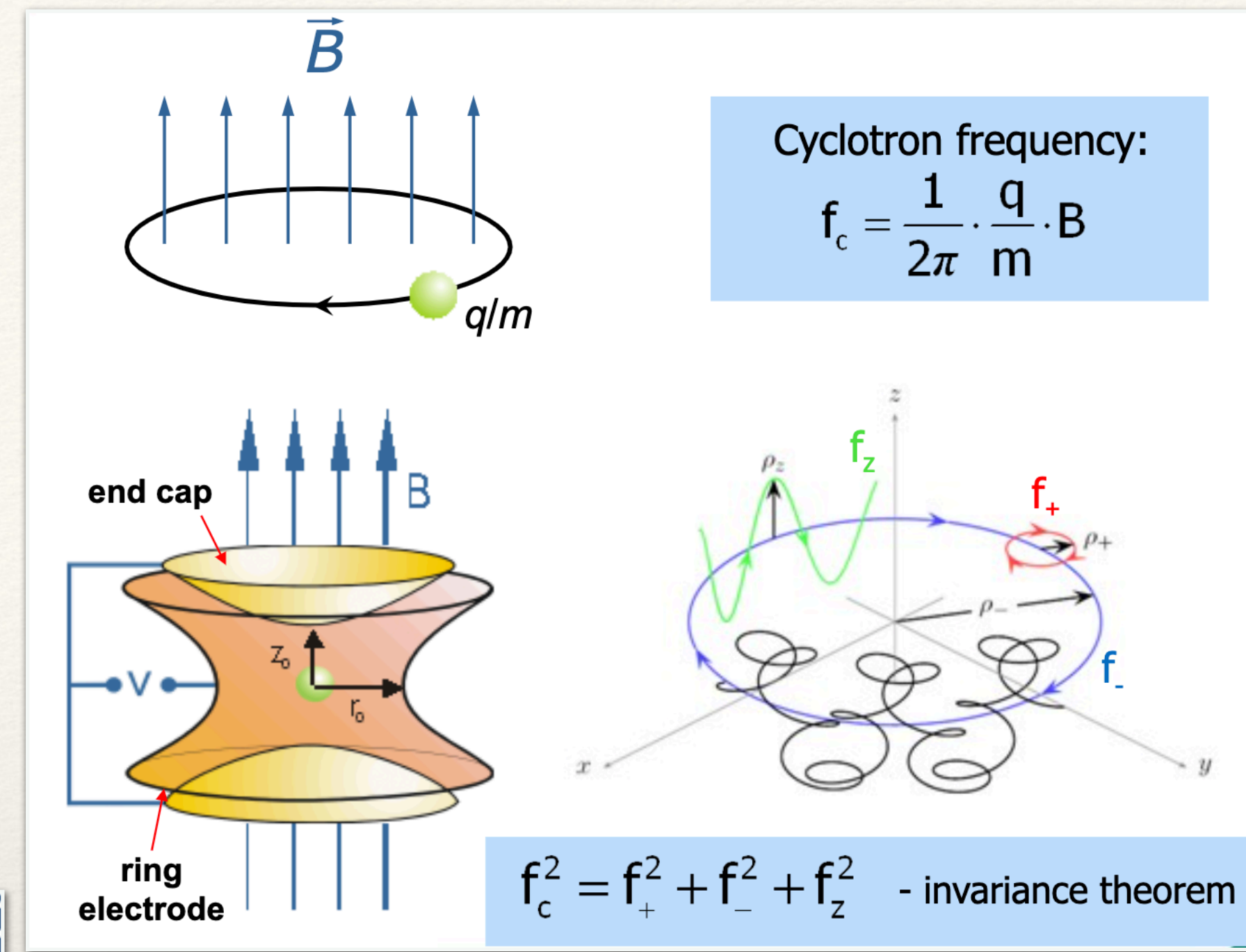
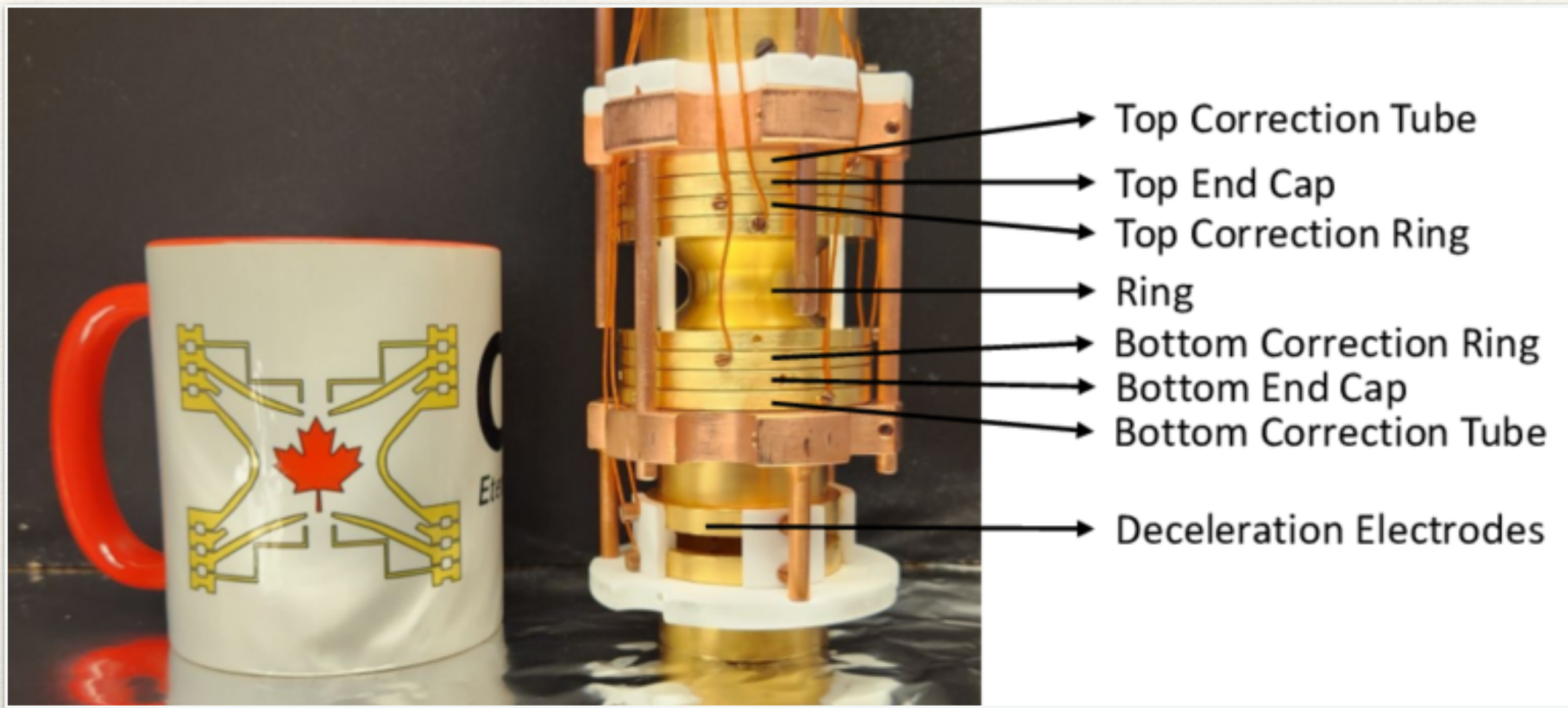


ATLAS

ARGONNE TANDEM LINAC ACCELERATOR SYSTEM

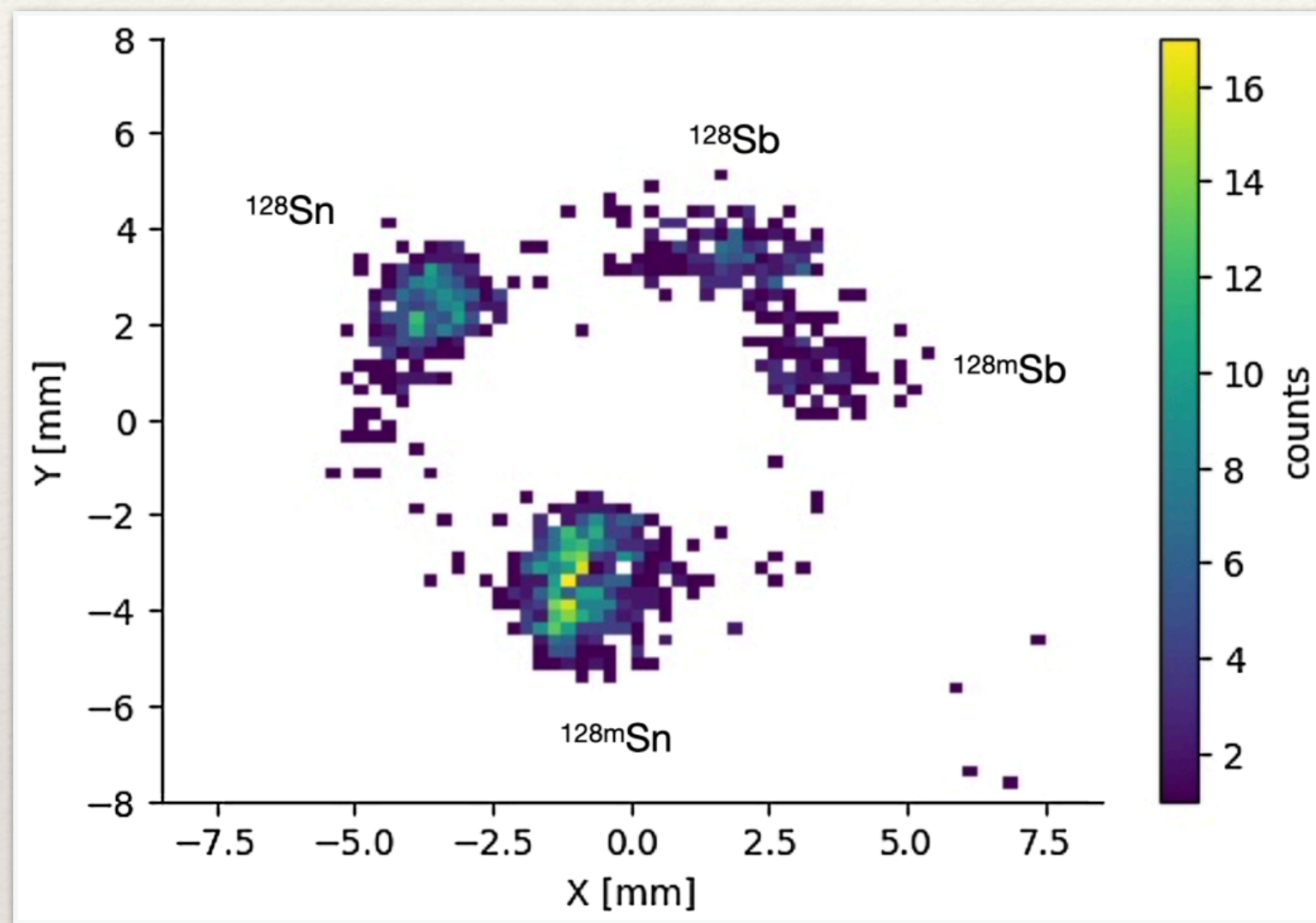




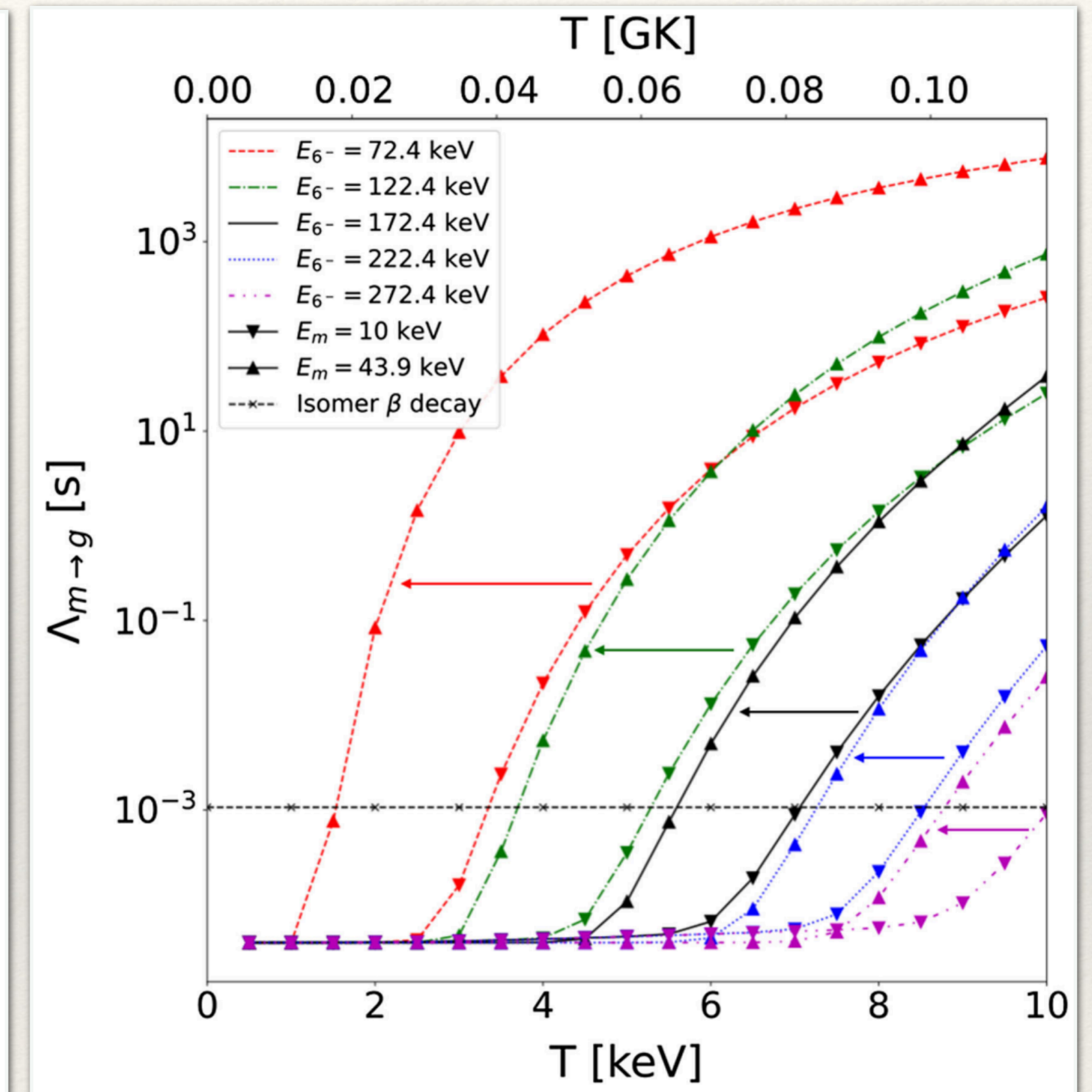
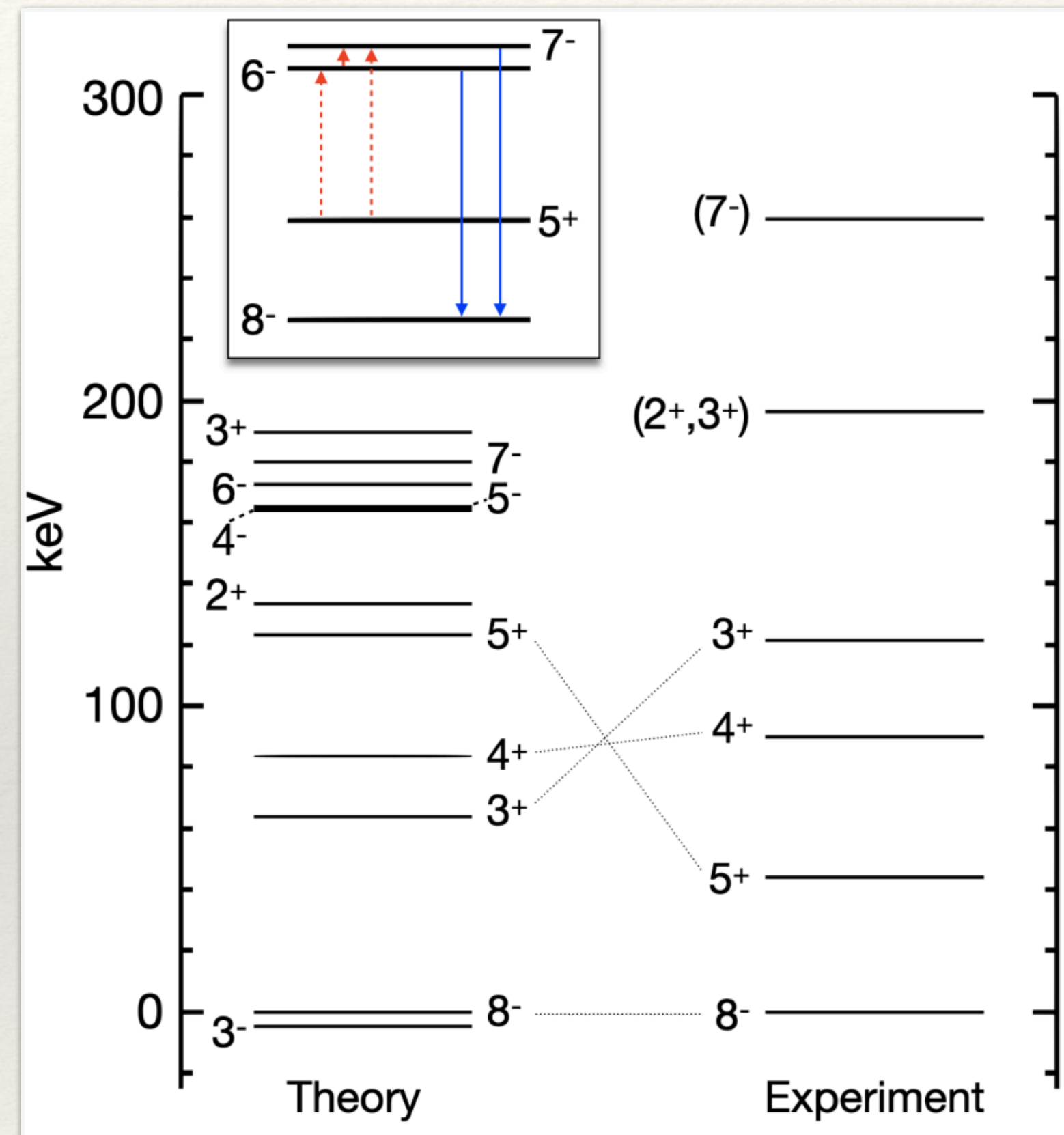


Excitation energy measurement of ^{128}Sb

Hoff et al, PRL131 (2023)



Species	$r = (\nu_c^{\text{cal}}/\nu_c)$	Mass excess (keV) this Letter	Mass excess (keV) evaluated
$^{128}\text{Sb}^+$	0.962407089(17)	-84608.8 ± 2.1	-84630 ± 19^a
$^{128\text{m}}\text{Sb}^+$	0.962407444(20)	-84564.8 ± 2.5	-84620 ± 18^b
	Excitation energy	43.9 ± 3.3	10 ± 6^b

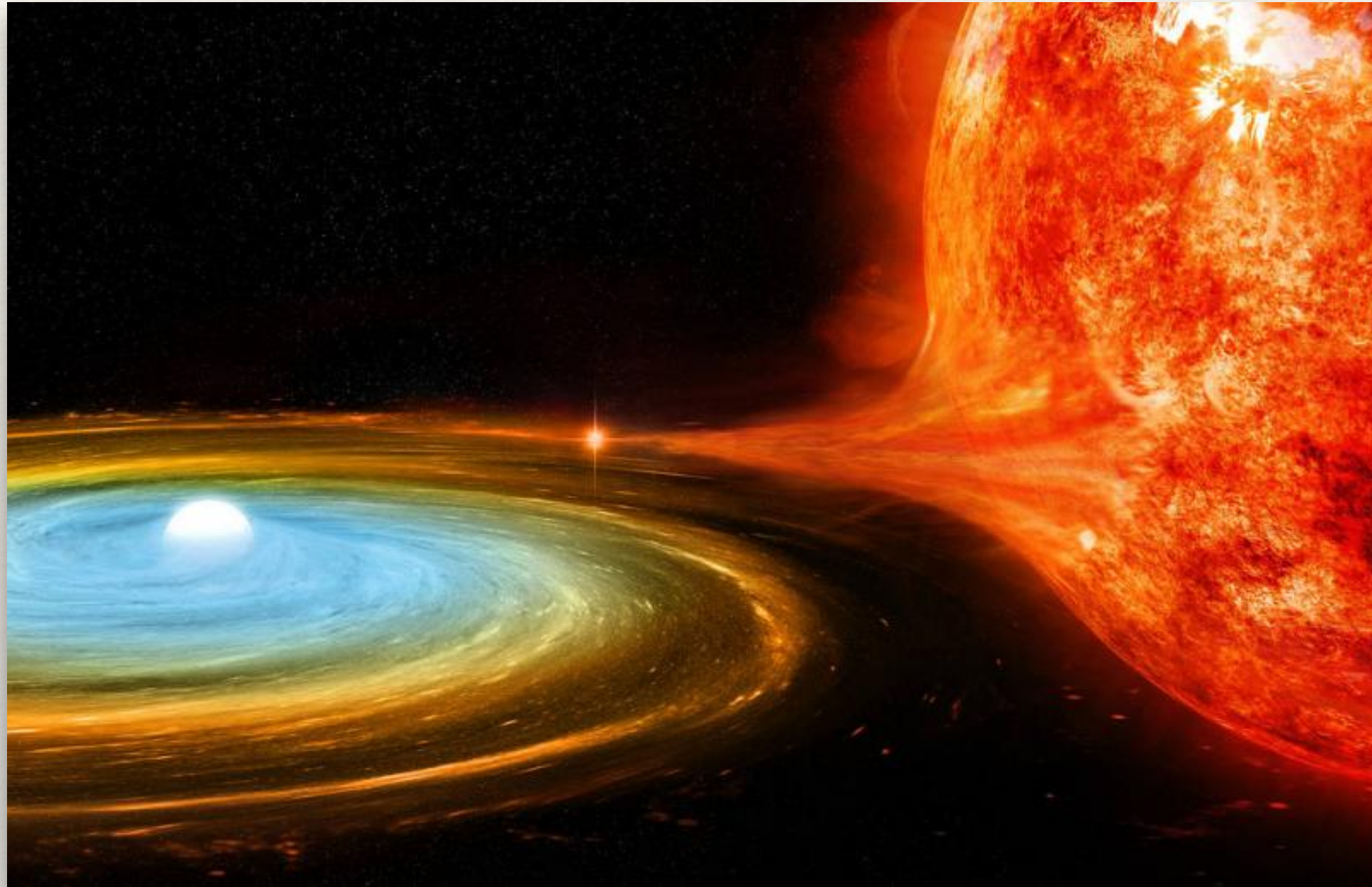


Calculated transition rates $m \rightarrow g$ s through 6^- state vs thermalization temperature

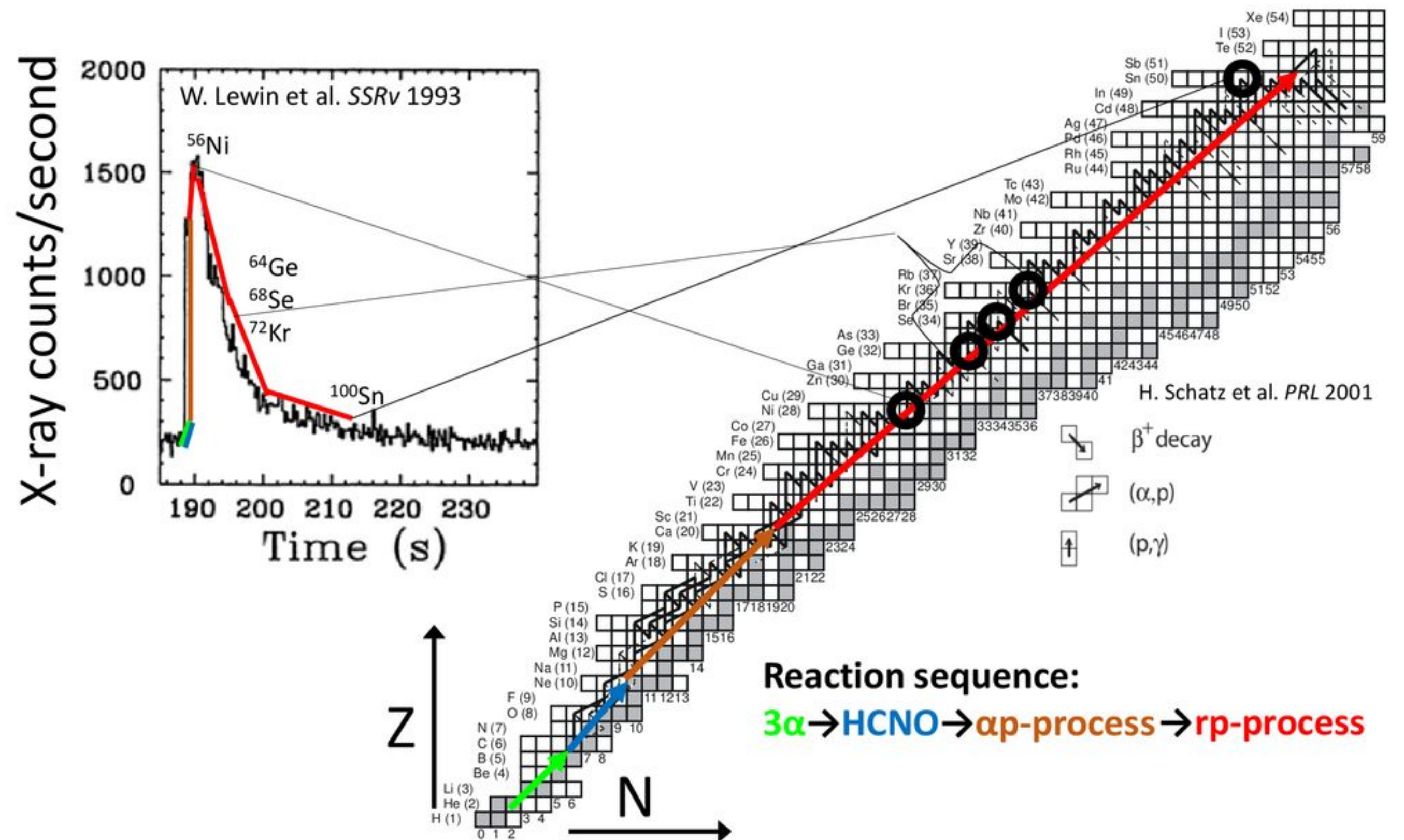
during r-process ^{128}Sb is populated in 10min (1keV)

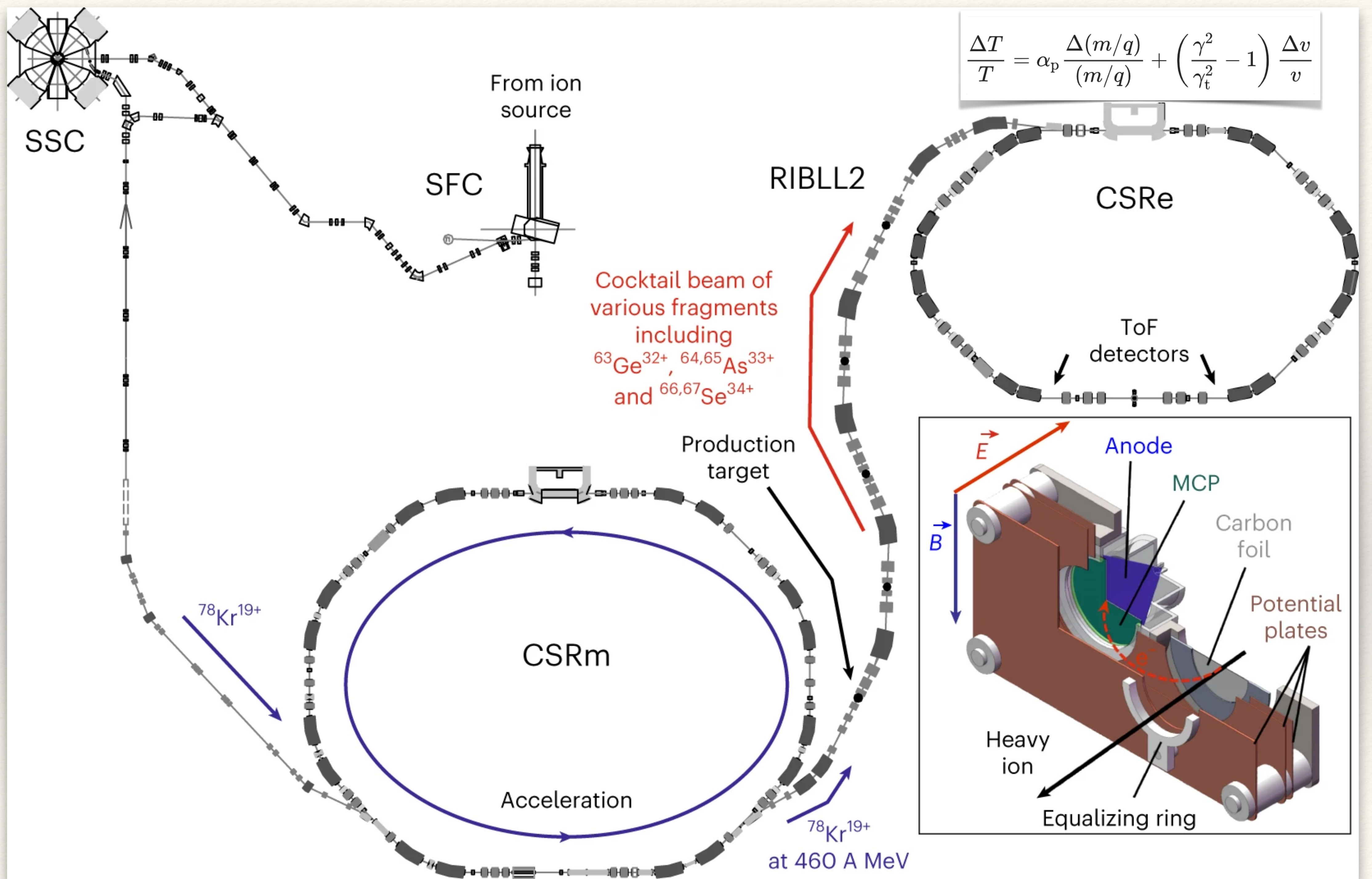
Conclusion: $^{128\text{m}}\text{Sb}$ is an astromer and accelerant ($t_{1/2}$ 10min vs. gs 9h)

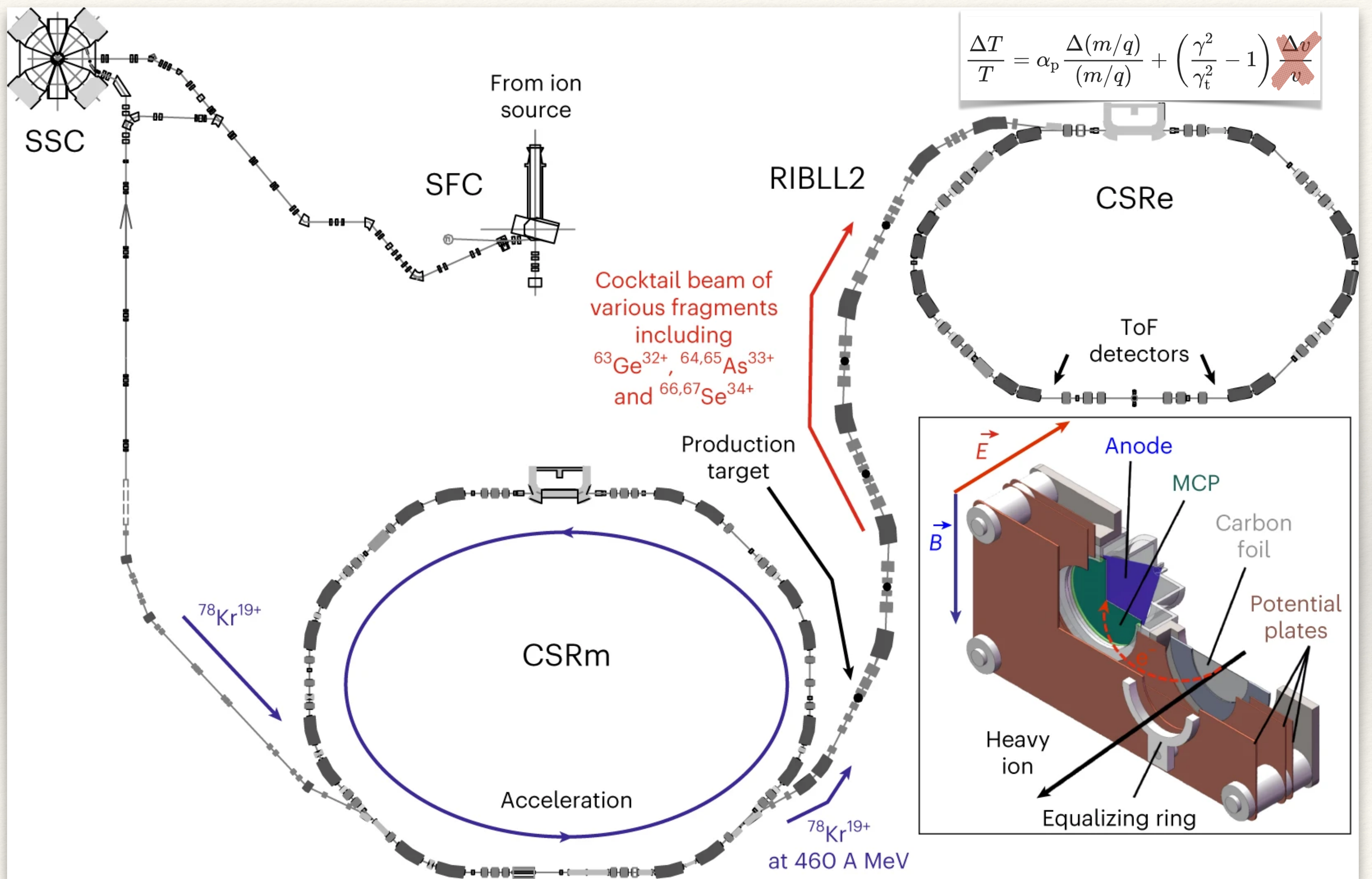
rp-process in Type I X-ray Bursts



rp-process reaction sequence & waiting points

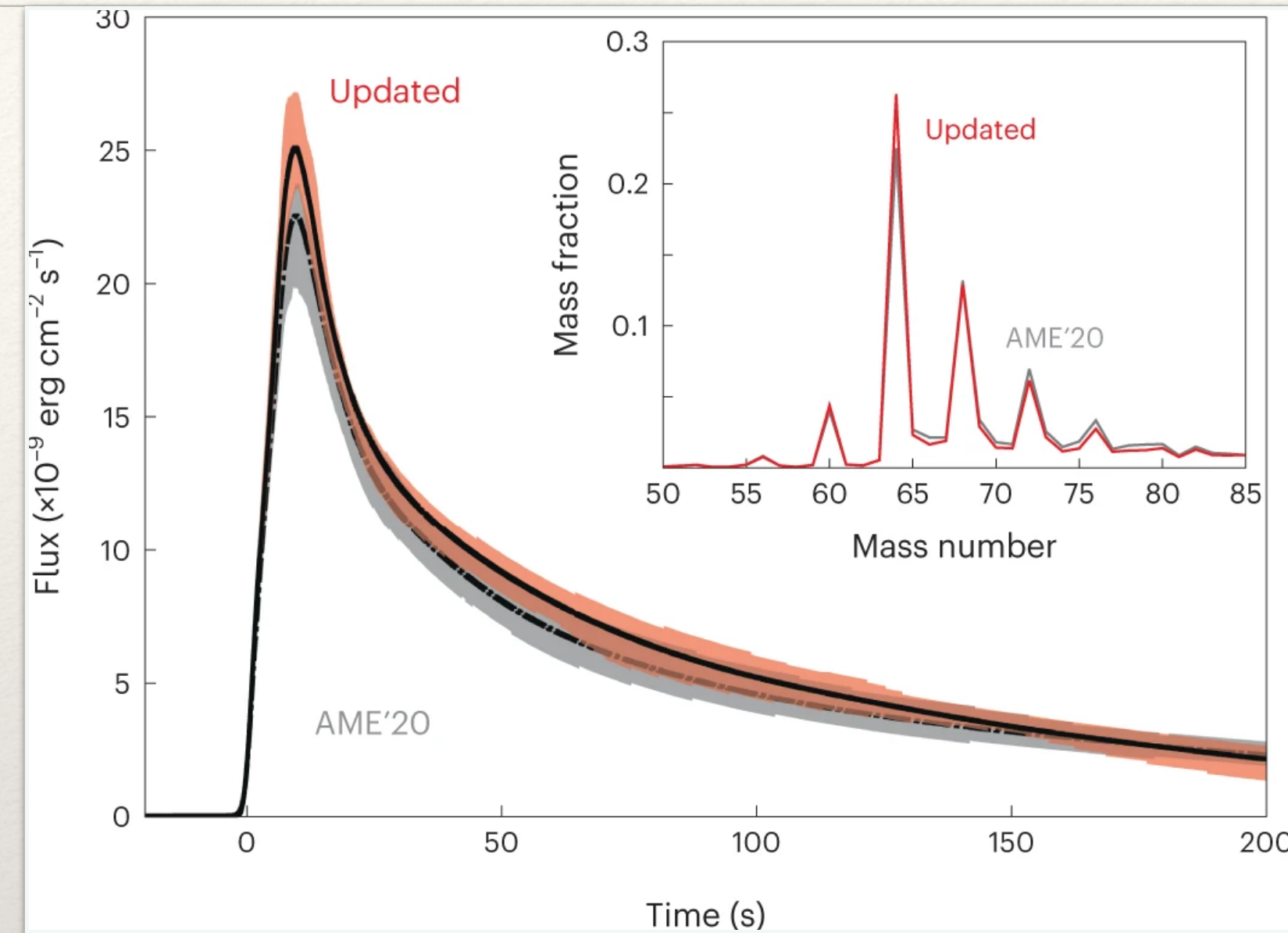
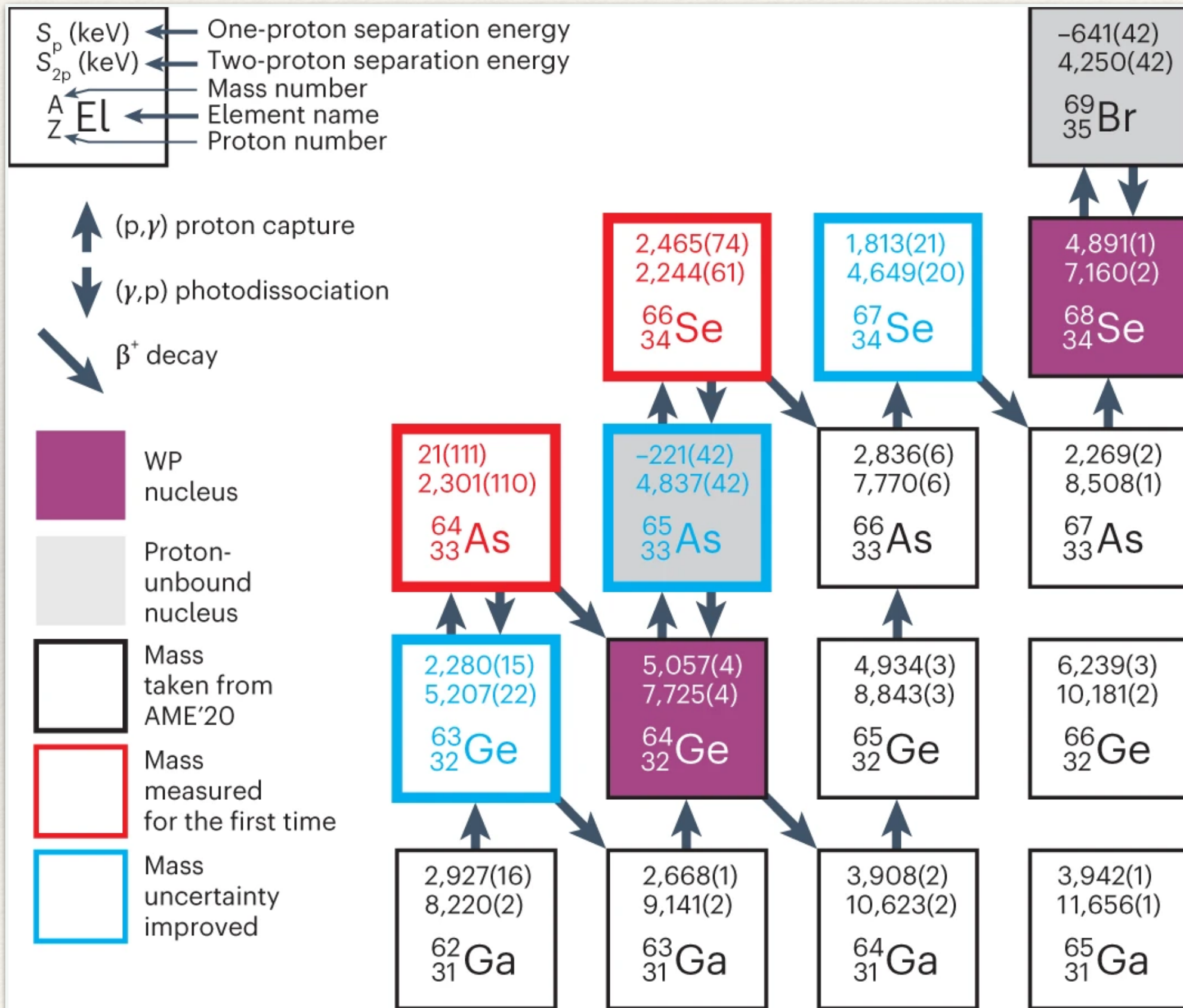






Mass measurements with storage ring

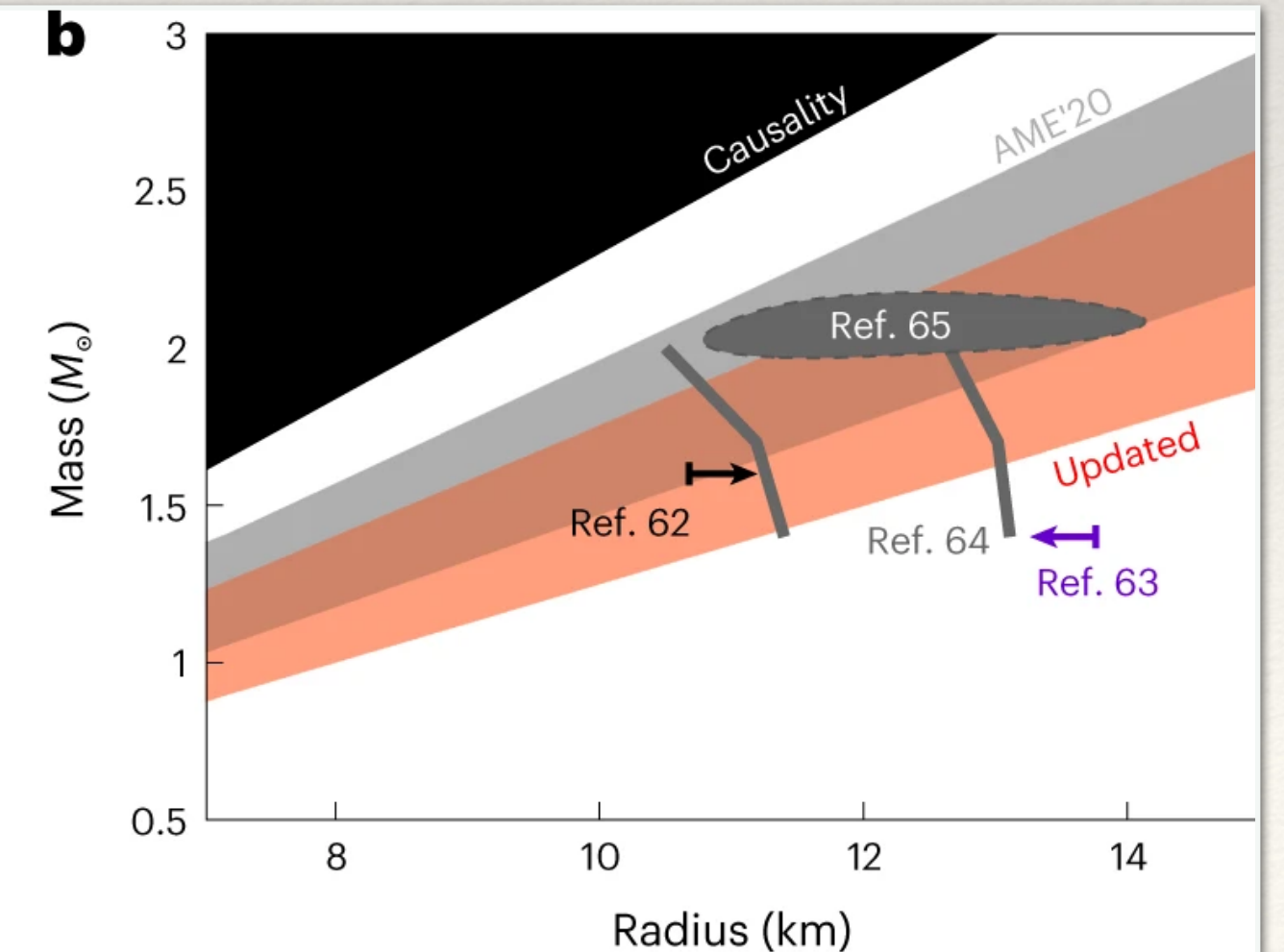
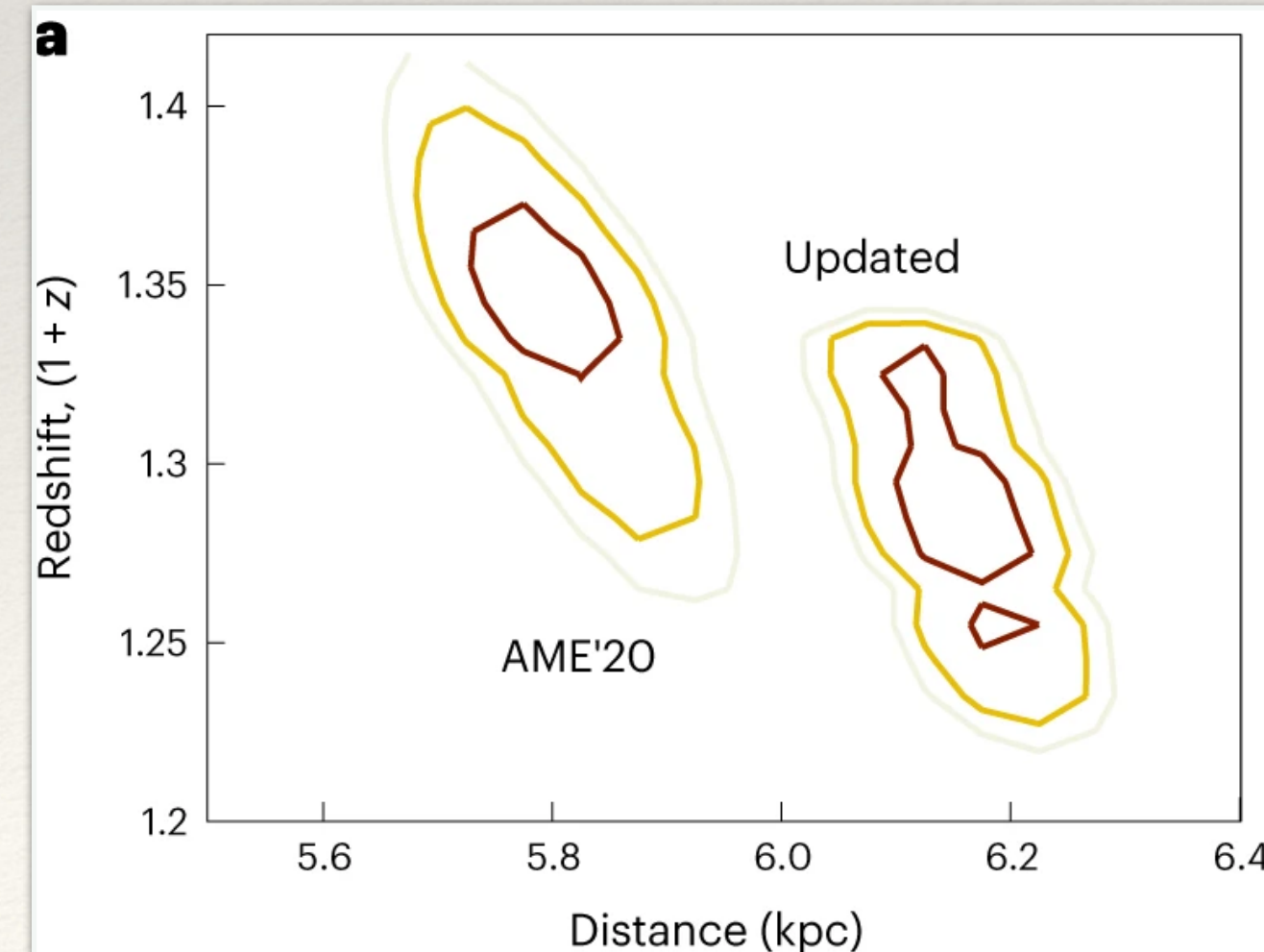
Zhou et al., Nature Physics 19 (2023)



Modified light curve
Modified ash composition

Possibly warmer accreted neutron-star crust

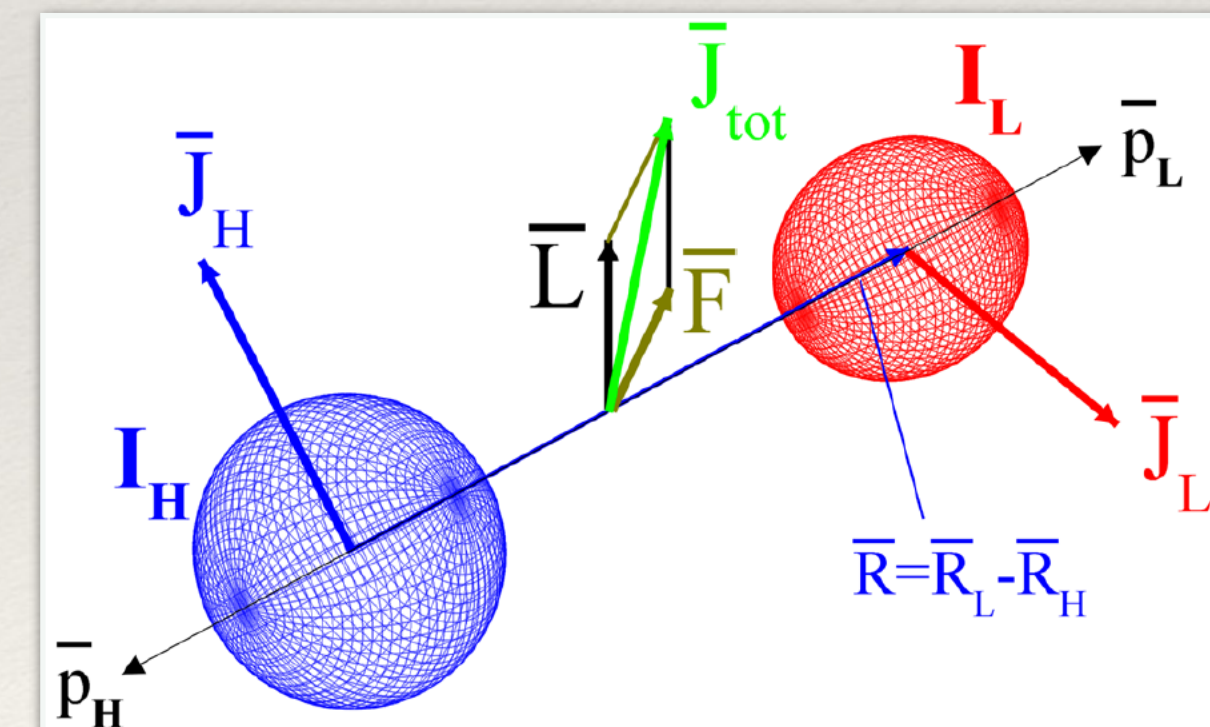
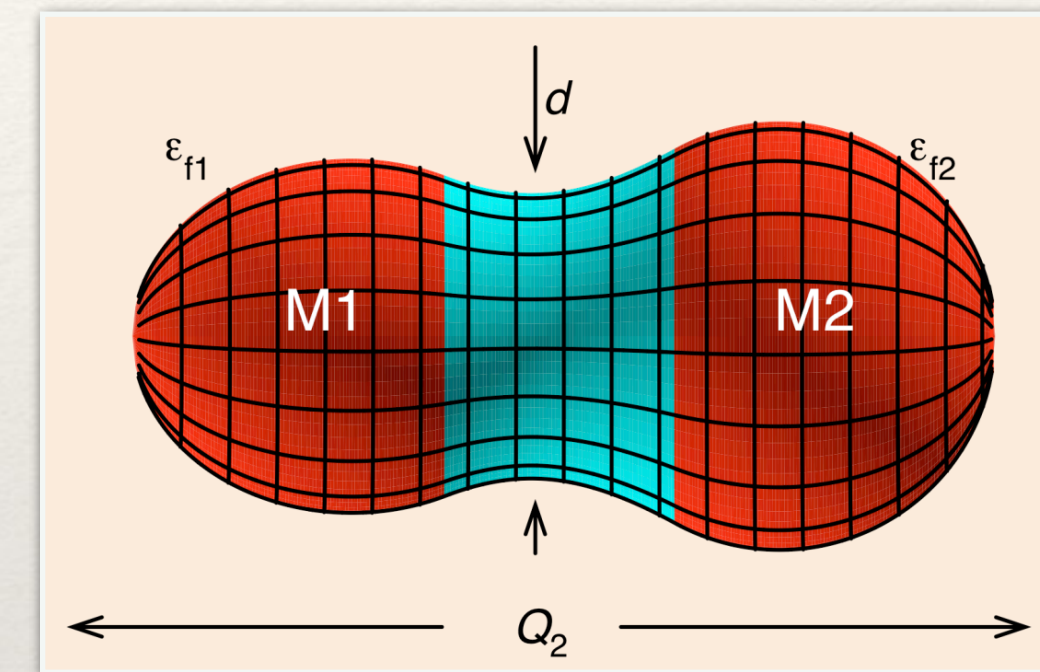
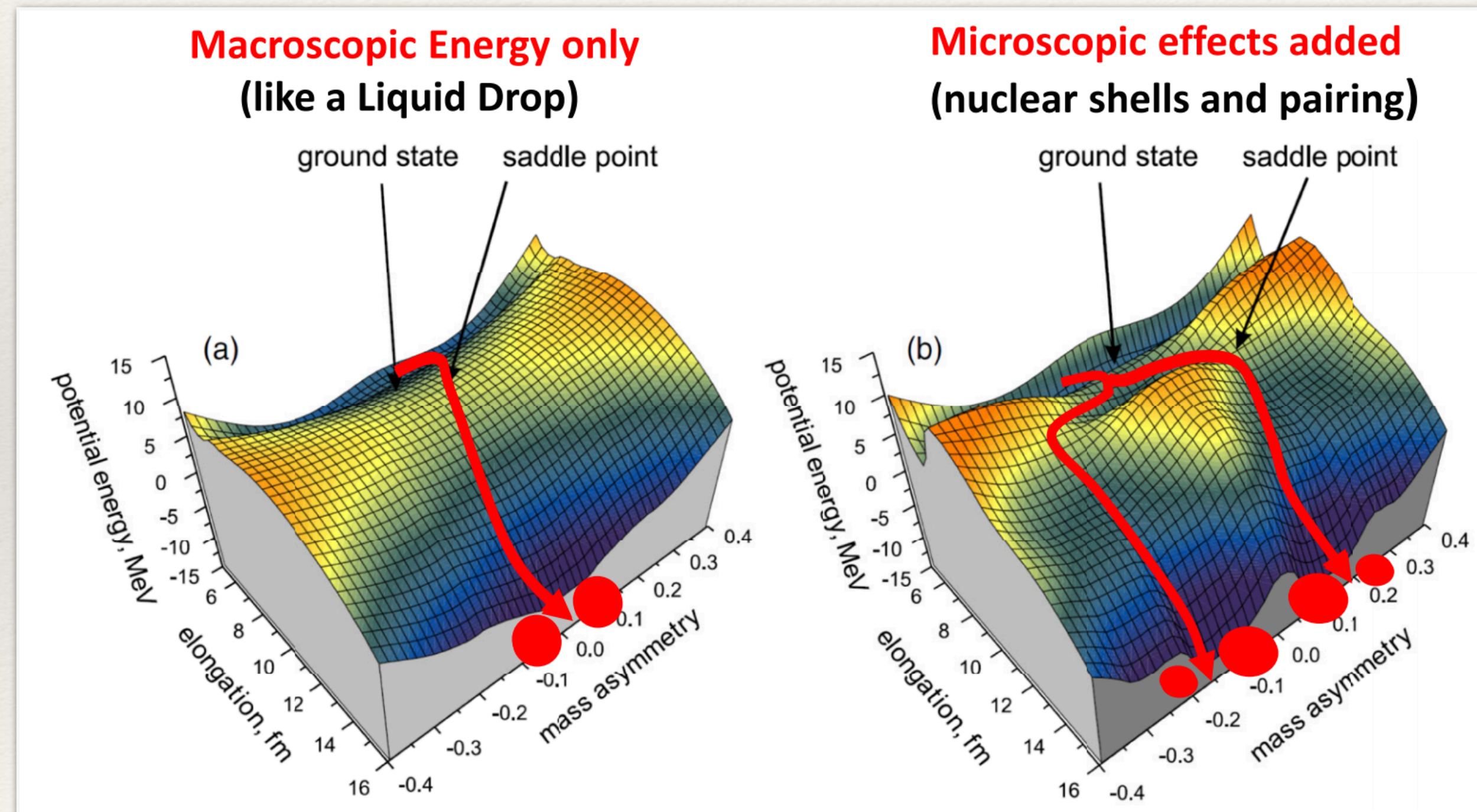
GS 1826–24 event would be further and less compact neutron star



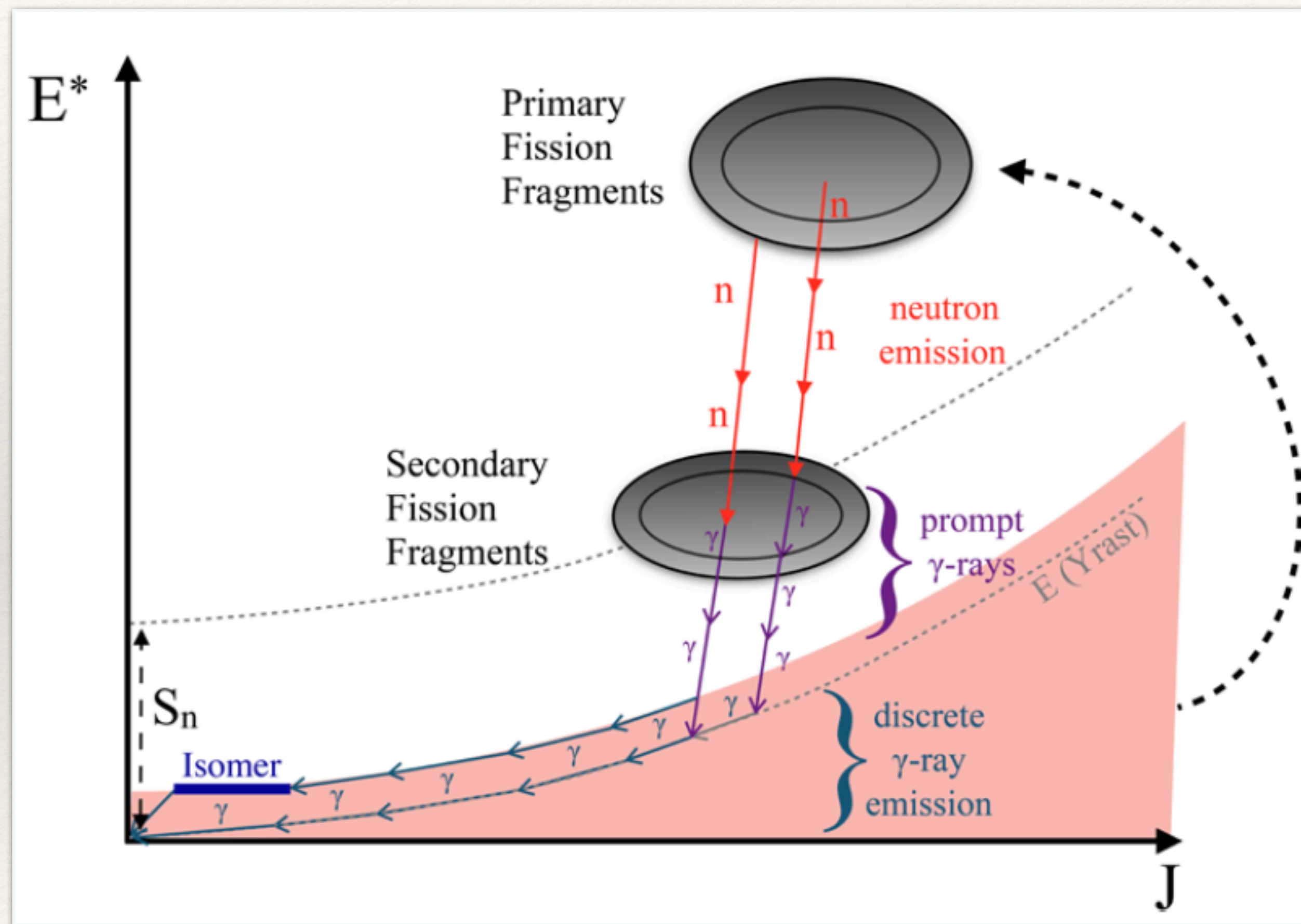
Fission study from isomeric ratios

Andreyev et al., Rep. Prog. Phys. 81 (2018)

Open question in fission: **What is the origin of angular momentum?**



Fission study from isomeric ratios



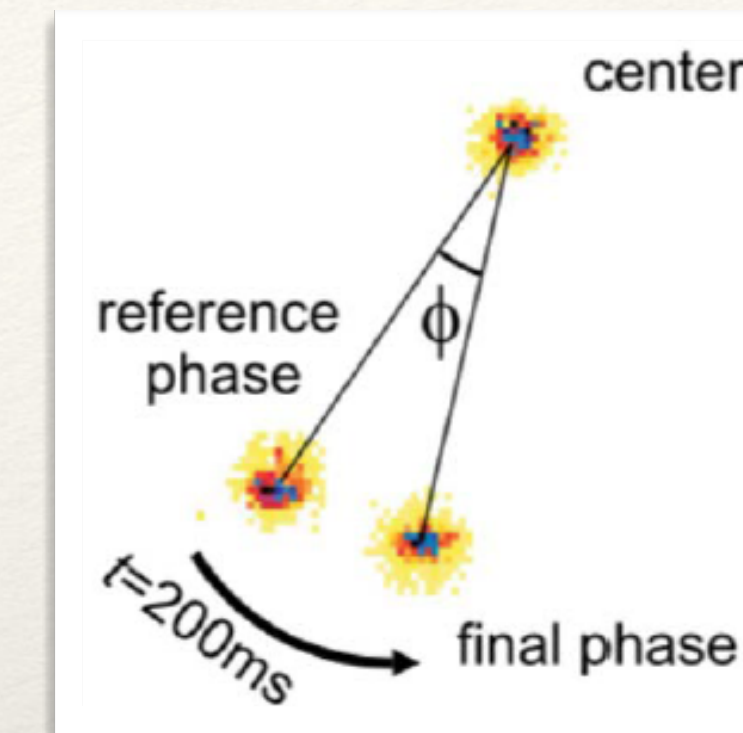
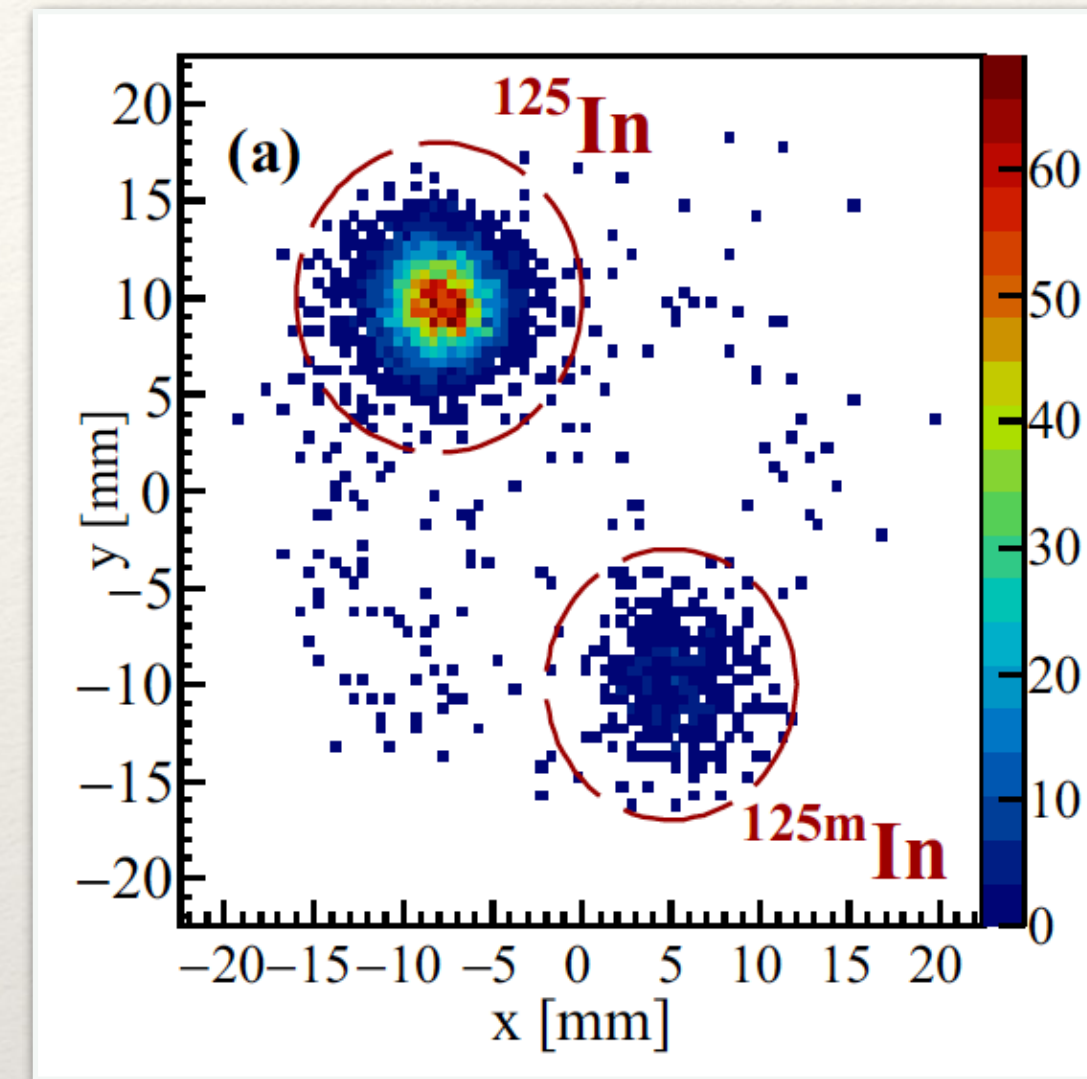
Fission study from isomeric ratios

Rakopoulos et al., PRC98(2018)

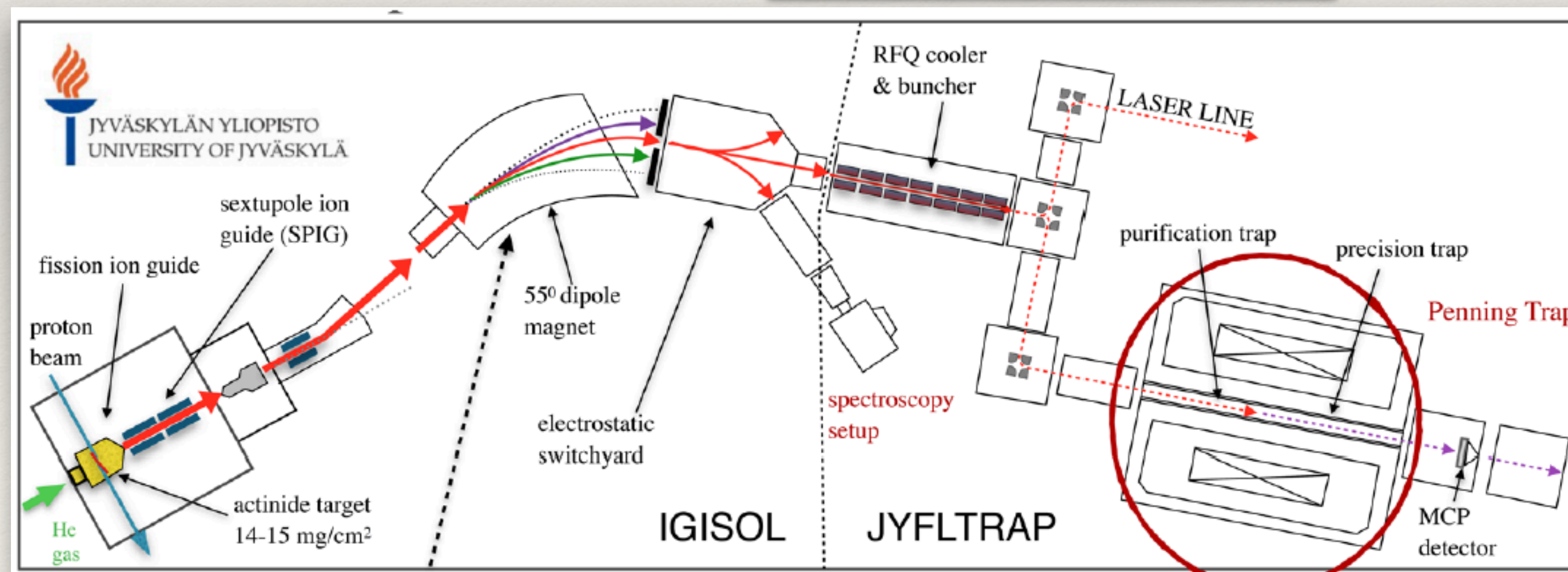
Isomeric ratios of fission fragments of proton induced fission on U and ^{232}Th @IGISOL

—> dependence on fission system

—> sensitive to nuclear structure effects



Phase-Imaging Ion Cyclotron Resonance (PI-ICR) $R > 10^6$



Fission study from isomeric ratios

Rakopoulos et al., PRC98(2018)

Isomeric ratios of fission fragments of proton induced fission on U and ^{232}Th @IGISOL

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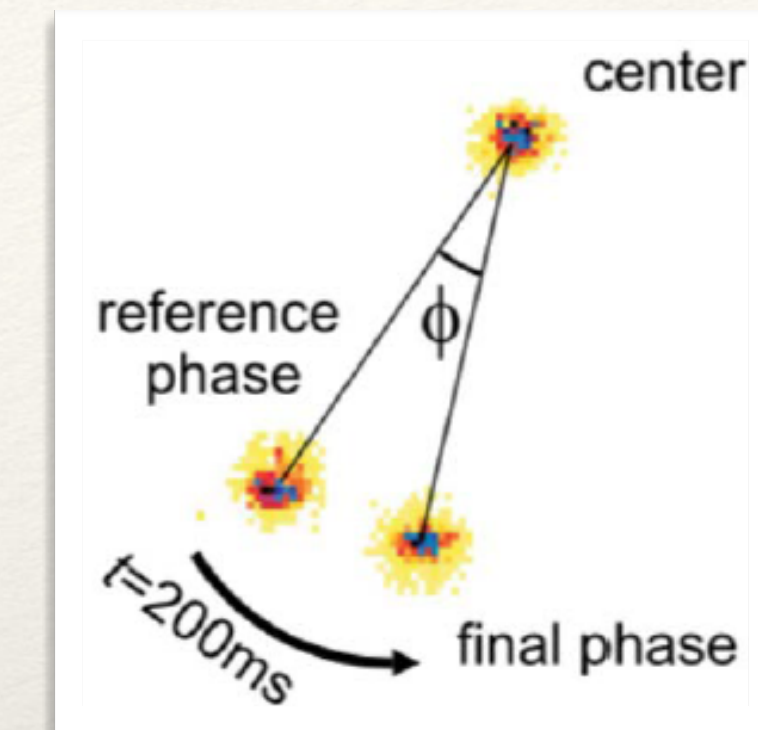
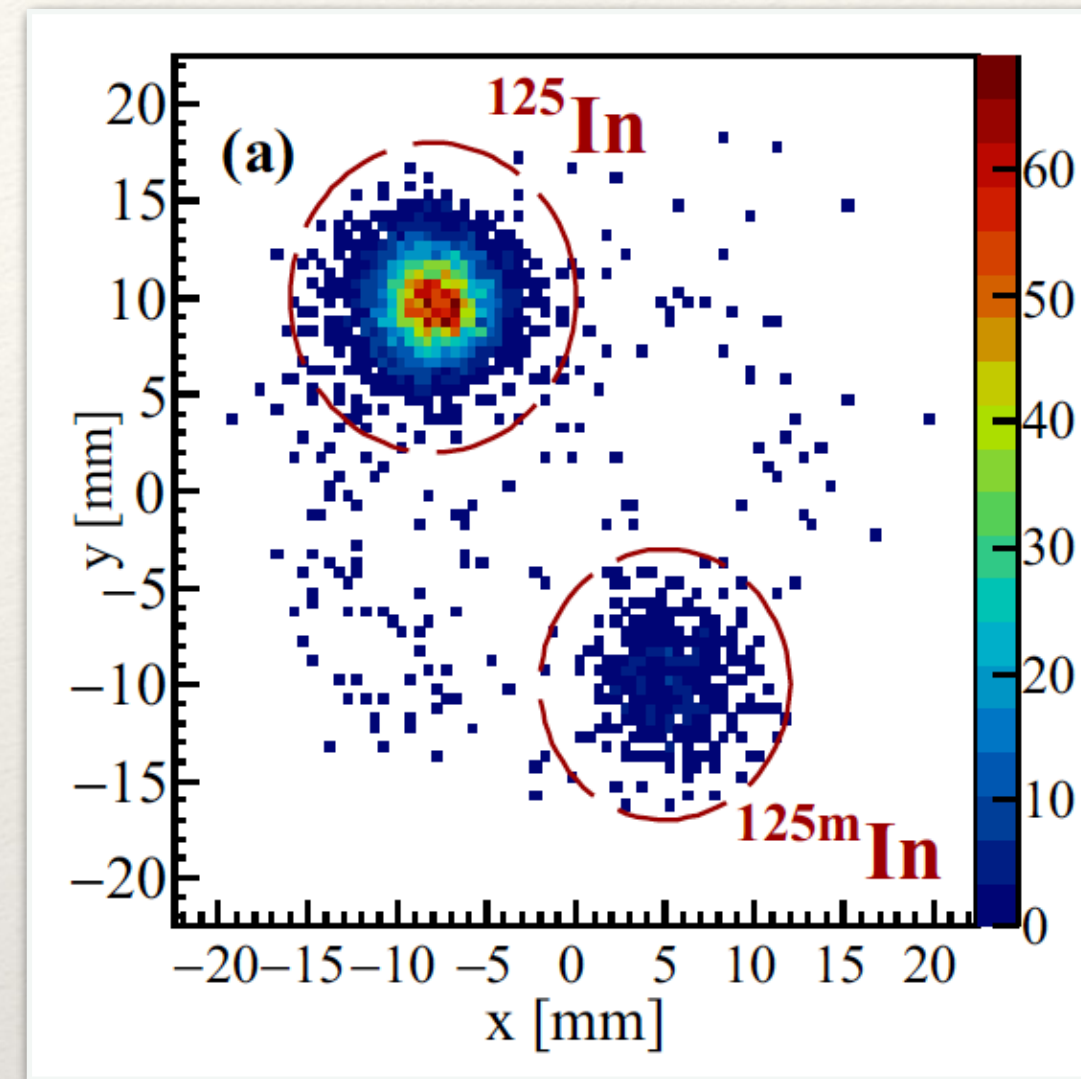
—> sensitive to nuclear structure effects

Other possible fission systems:

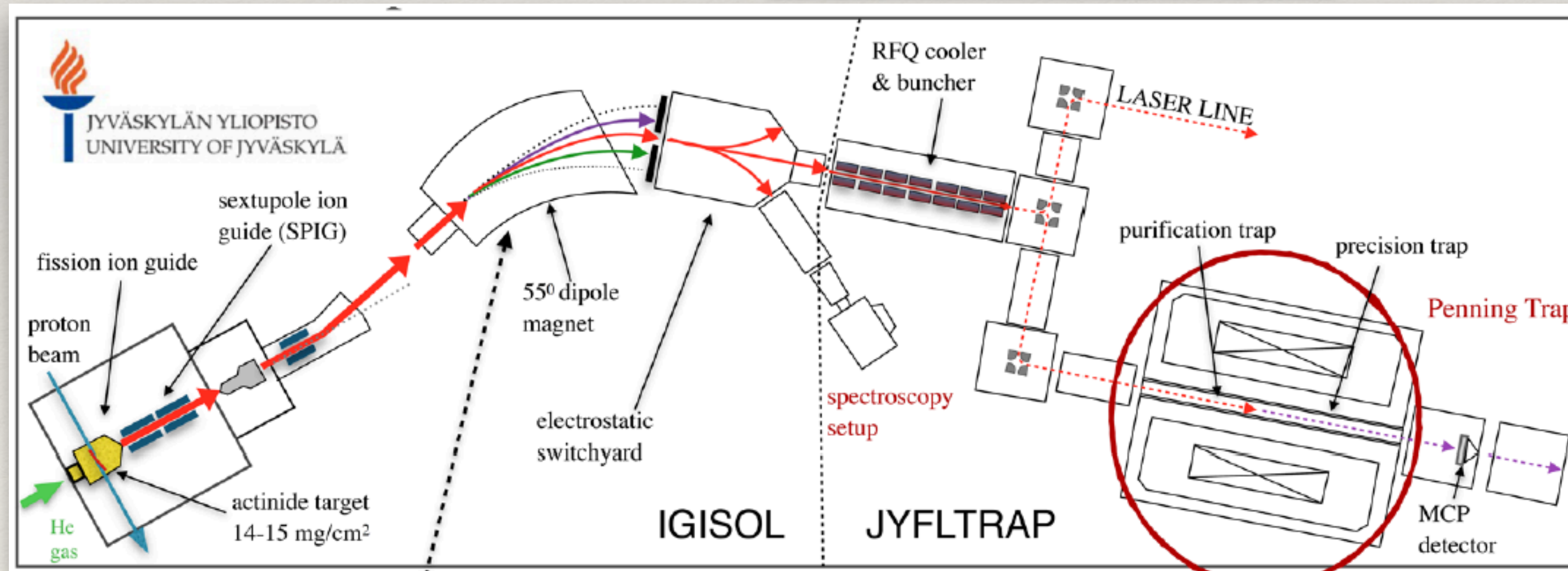
In-flight fission —> MRTOF & R3 @RIBF

Photofission —> MLLTrap/? @ALTO

n-induced fission —> ? @NFS/GANIL

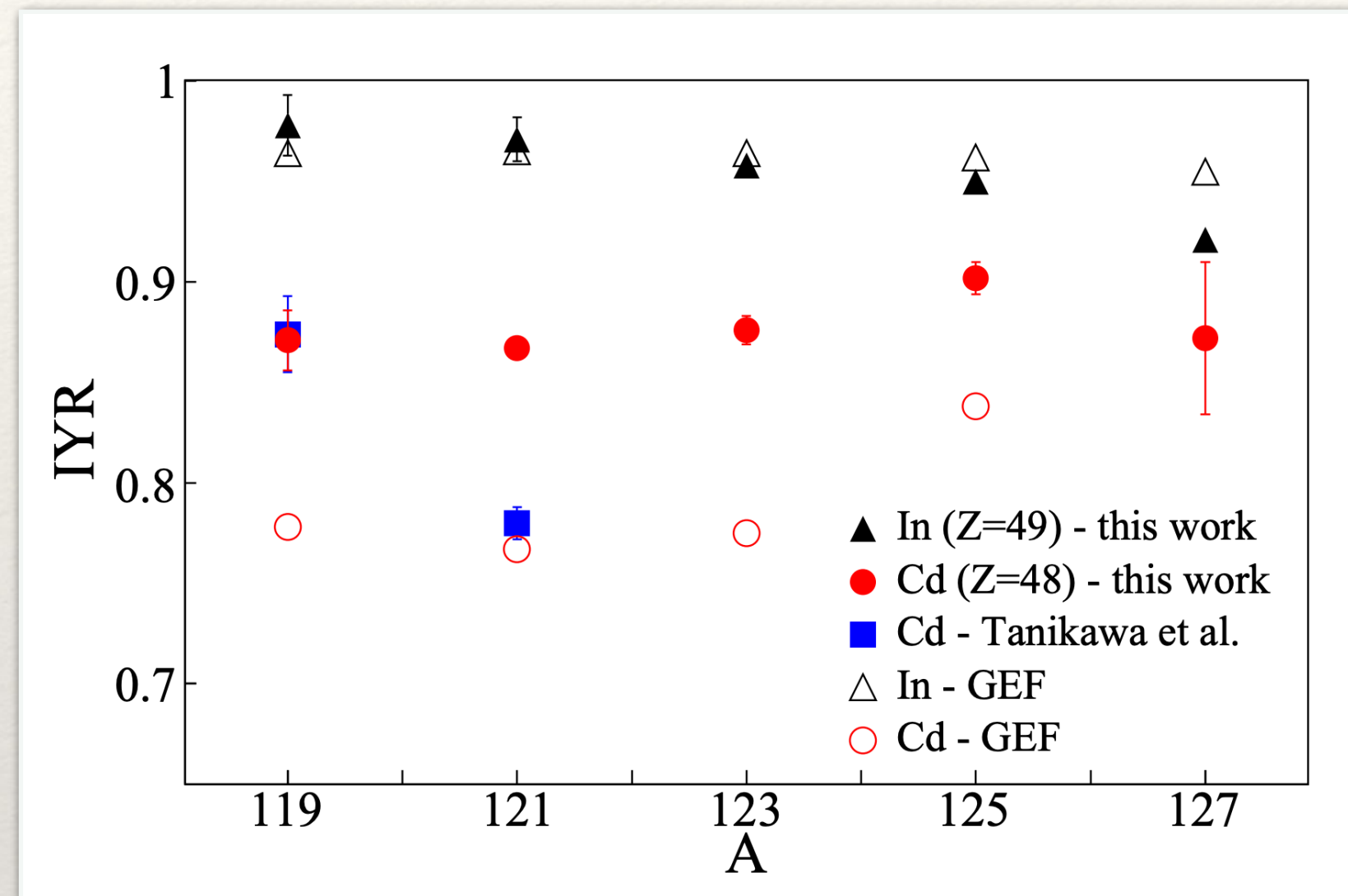


Phase-Imaging Ion Cyclotron Resonance (PI-ICR) $R > 10^6$



First study at IGISOL/JYFLTRAP

Rakopoulos et al., PRC66(2019)

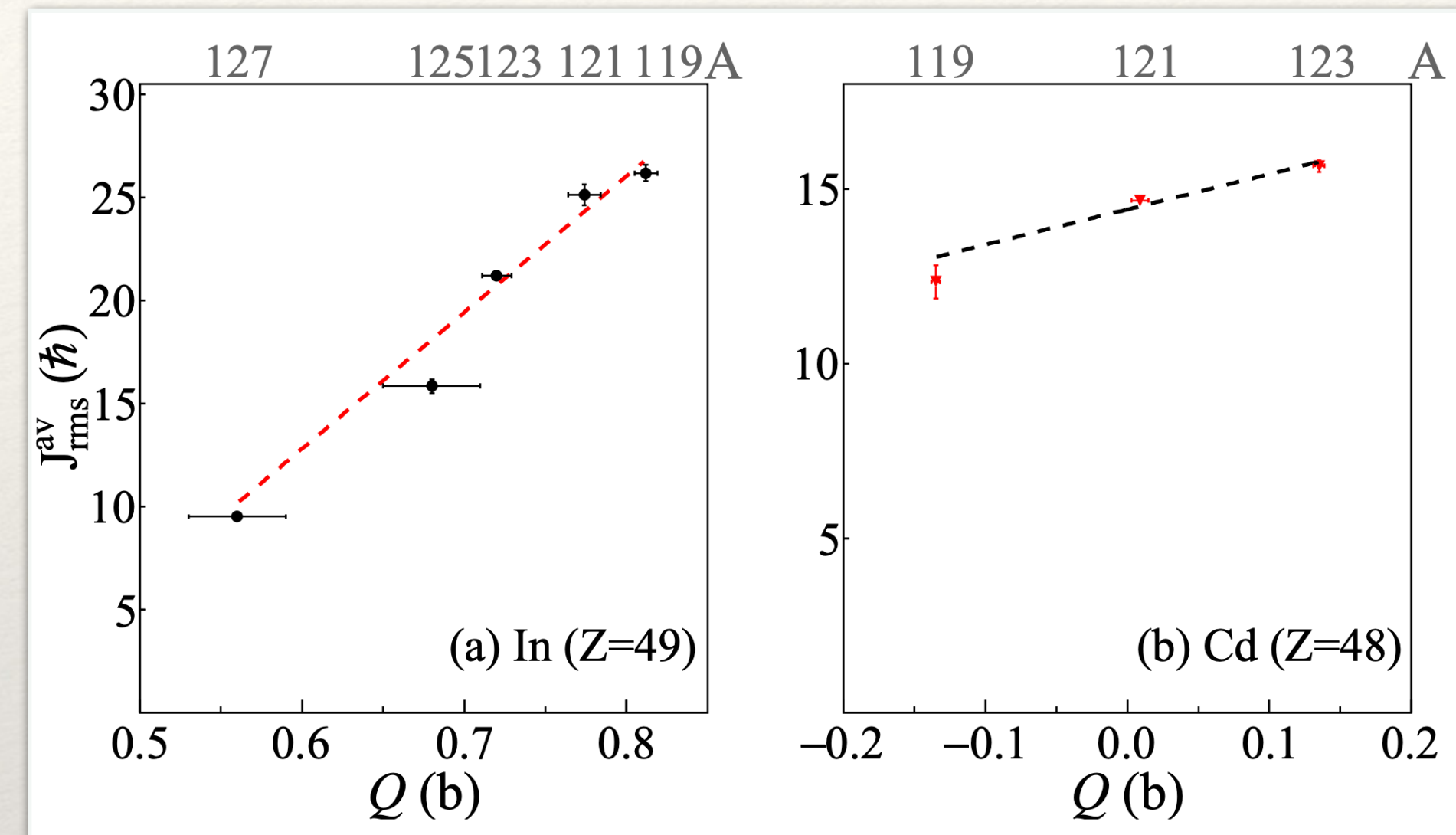
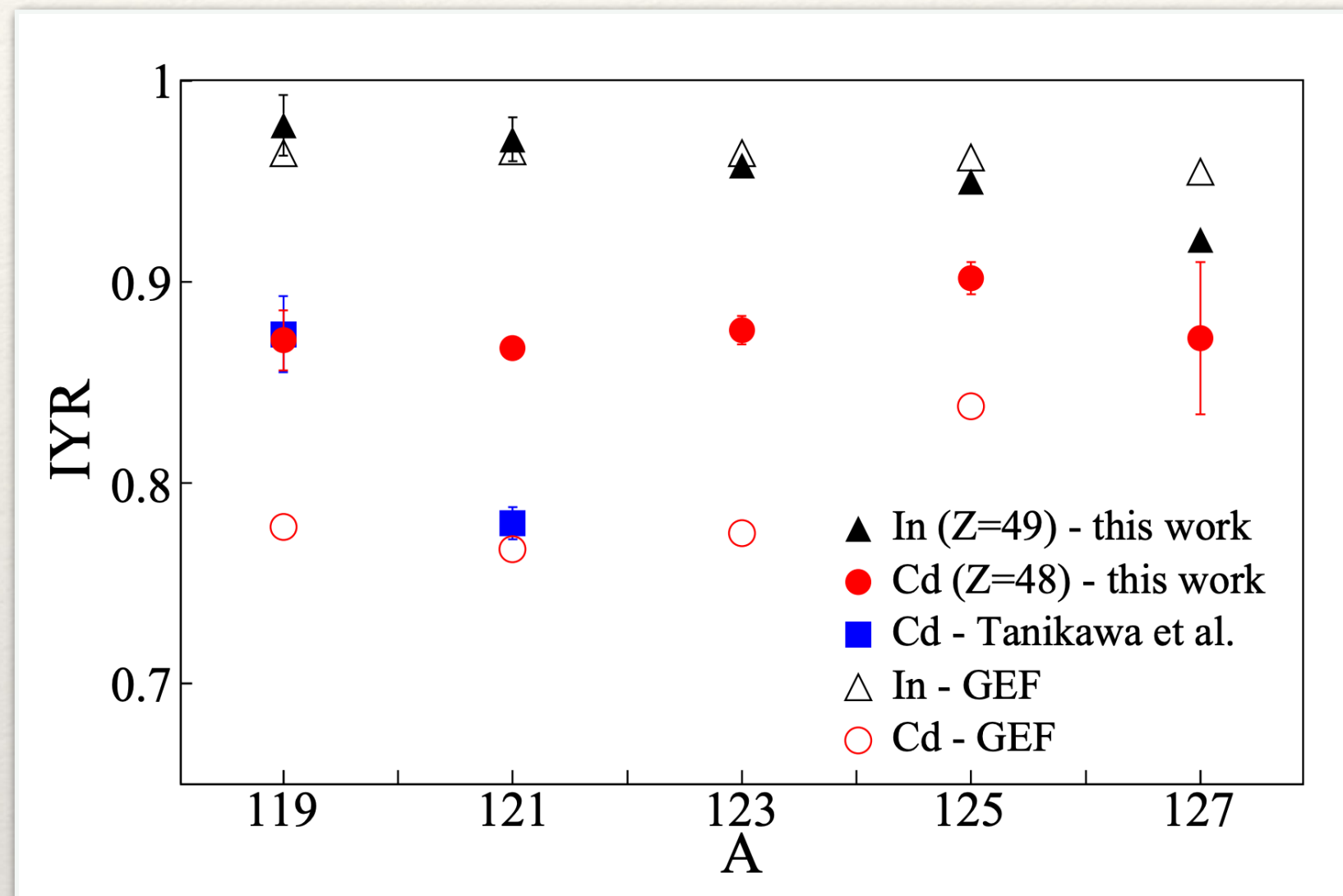


Most yields are not reproduced by theoretical models

—> Need more data, which will lead to better theoretical description

First study at IGISOL/JYFLTRAP

Rakopoulos et al., PRC66(2019)



Most yields are not reproduced by theoretical models
—> Need more data, which will lead to better theoretical description

Strong correlation of In isotopes' angular momentum with electric quadrupole moment
—> fission fragments of In retain part of their deformation during their relaxation after scission. Coulomb force might contribute to the primary fission fragments momentum in In isotopes.

Takeaway

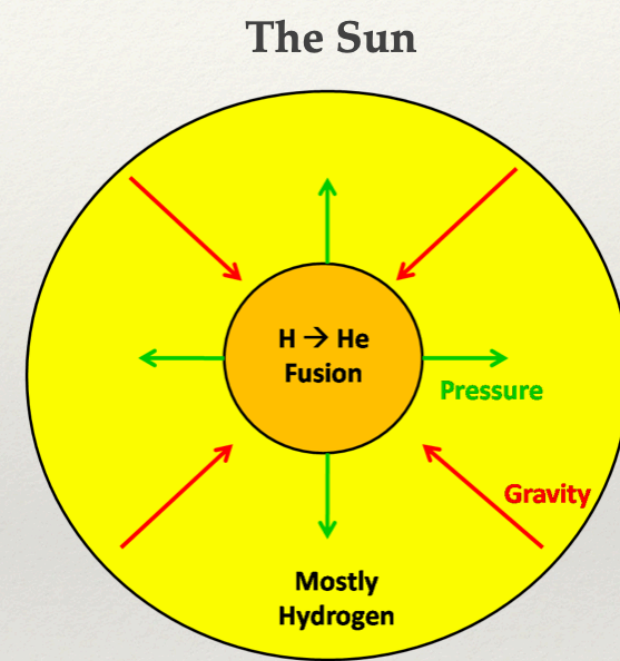
Mass spectrometry applications

Takeaway

Mass spectrometry applications

Solving the age of the Sun crisis

Eddington



$$\text{Lifetime} = \frac{\text{Energy}}{\text{Luminosity}} = \frac{Mc^2}{L_{\text{sun}}} = \frac{0.007 \cdot 0.1 \cdot M_{\text{sun}} \cdot c^2}{L_{\text{sun}}} \approx 10 \text{ Billion years}$$

$$[L_{\text{sun}}] = E/t$$

10% of the Sun undergo fusion

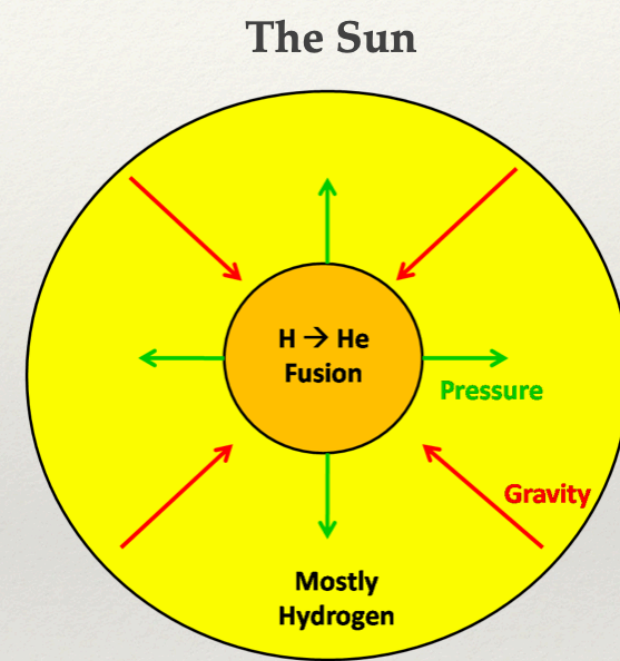
0.7% atomic mass difference between 4xH and ⁴He

Takeaway

Mass spectrometry applications

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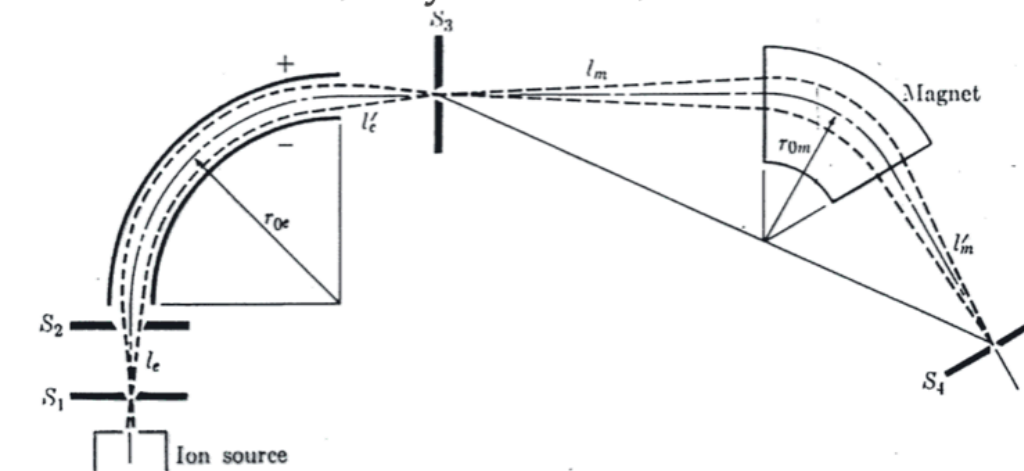
0.7% atomic mass difference between 4xH and ⁴He

Nier's mass spectrometer

Transition from Spectrograph to Spectrometer



A. O. Nier 1951, Phys. Rev 81, 507

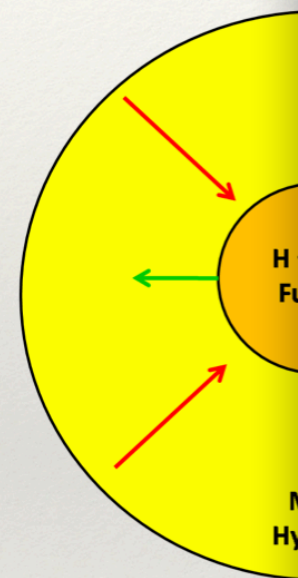


Takeaway

Mass spectrometry applications

Solving the age of the Sun crisis

Eddington



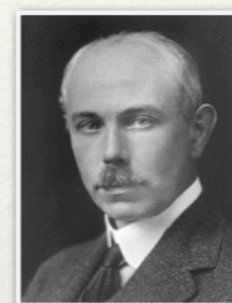
$$\text{Lifetime} = \frac{\text{Energy}}{\text{Luminosity}} = \frac{Mc^2}{L_{\text{sun}}} = \frac{0.007 \cdot 0.1 \cdot M_{\text{sun}} \cdot c^2}{L_{\text{sun}}} \approx 10^{10} \text{ years}$$

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0.7% atomic mass difference

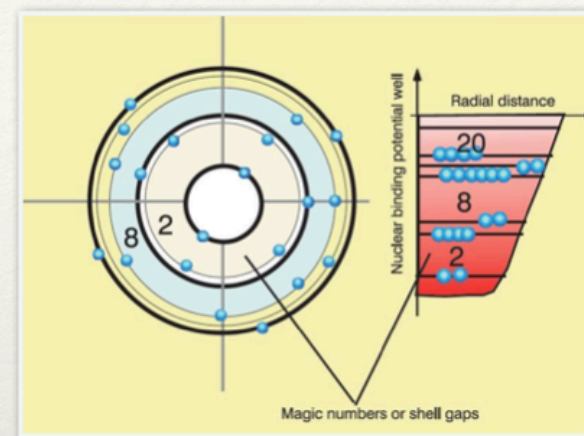
Nier's mass spectrometer

Atomic Masses & Nuclear Physics Discoveries



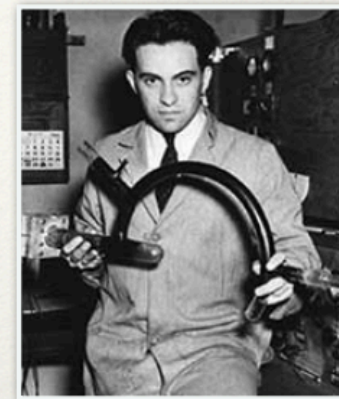
F.W. Aston
Mass defect
 $M_H = 1.008 \text{ u}$

1919



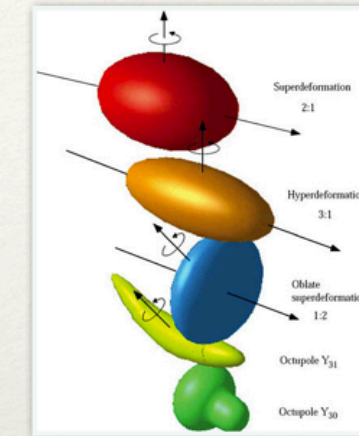
Nuclear Shell Model

1948



Nier's spectrometry

1951

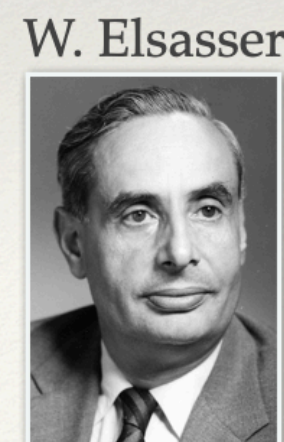


Nuclear deformation at N=90

1954



1974

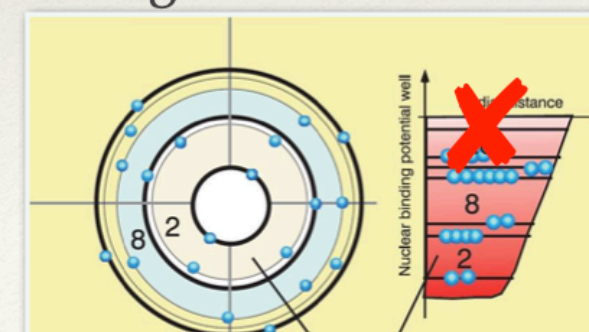


W. Elsasser
Discovery of magic numbers
 $Z=2,8,20,28,50$
 $N=126,82$

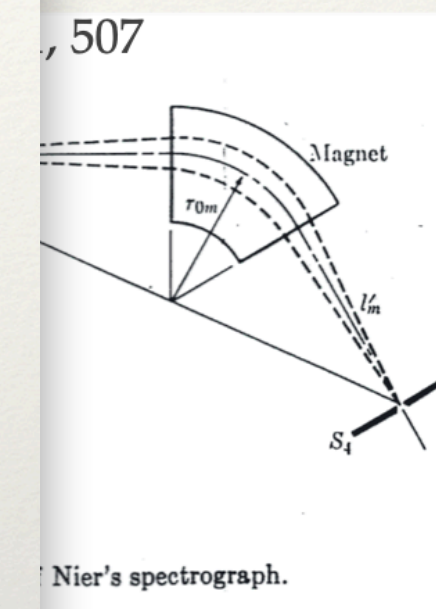
Goeppert-Mayer



Disappearance of magic number N=20



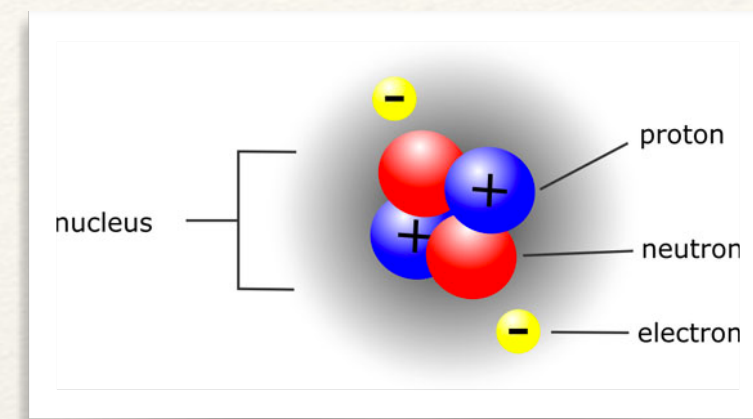
meter



Nier's spectrograph.



Takeaway



Atomic Mass

$$M(^4\text{He}) = 2 \cdot m_p + 2 \cdot m_n + 2 \cdot m_e$$

- Binding Energy

Takeaway

Low Energy

High Energy

Penning, MR-TOF-MS

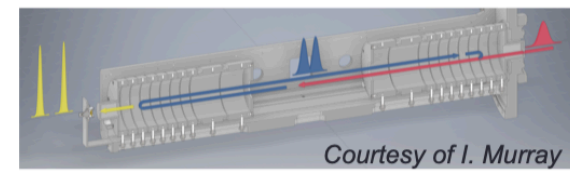
Storage Rings

100ms~1s

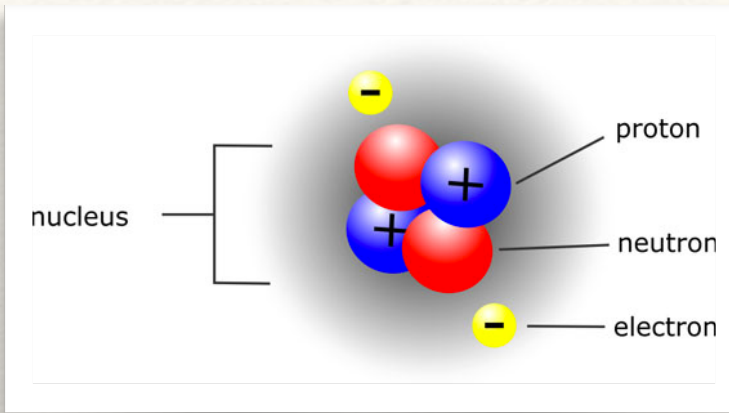
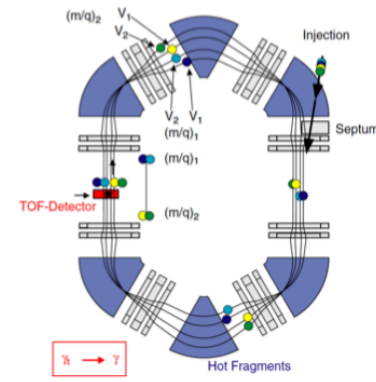
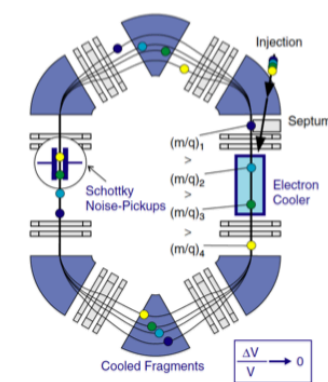
1~10 ms

1~10 s

Isochronous
< 1ms



Courtesy of I. Murray



Atomic Mass

$$M(^4\text{He}) = 2 \cdot m_p + 2 \cdot m_n + 2 \cdot m_e - \text{Binding Energy}$$

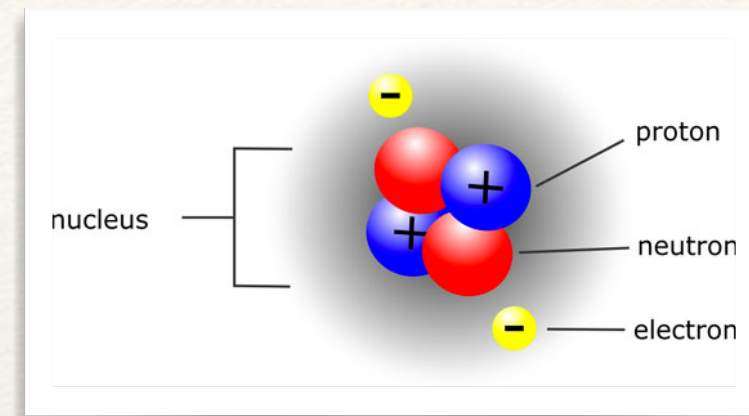
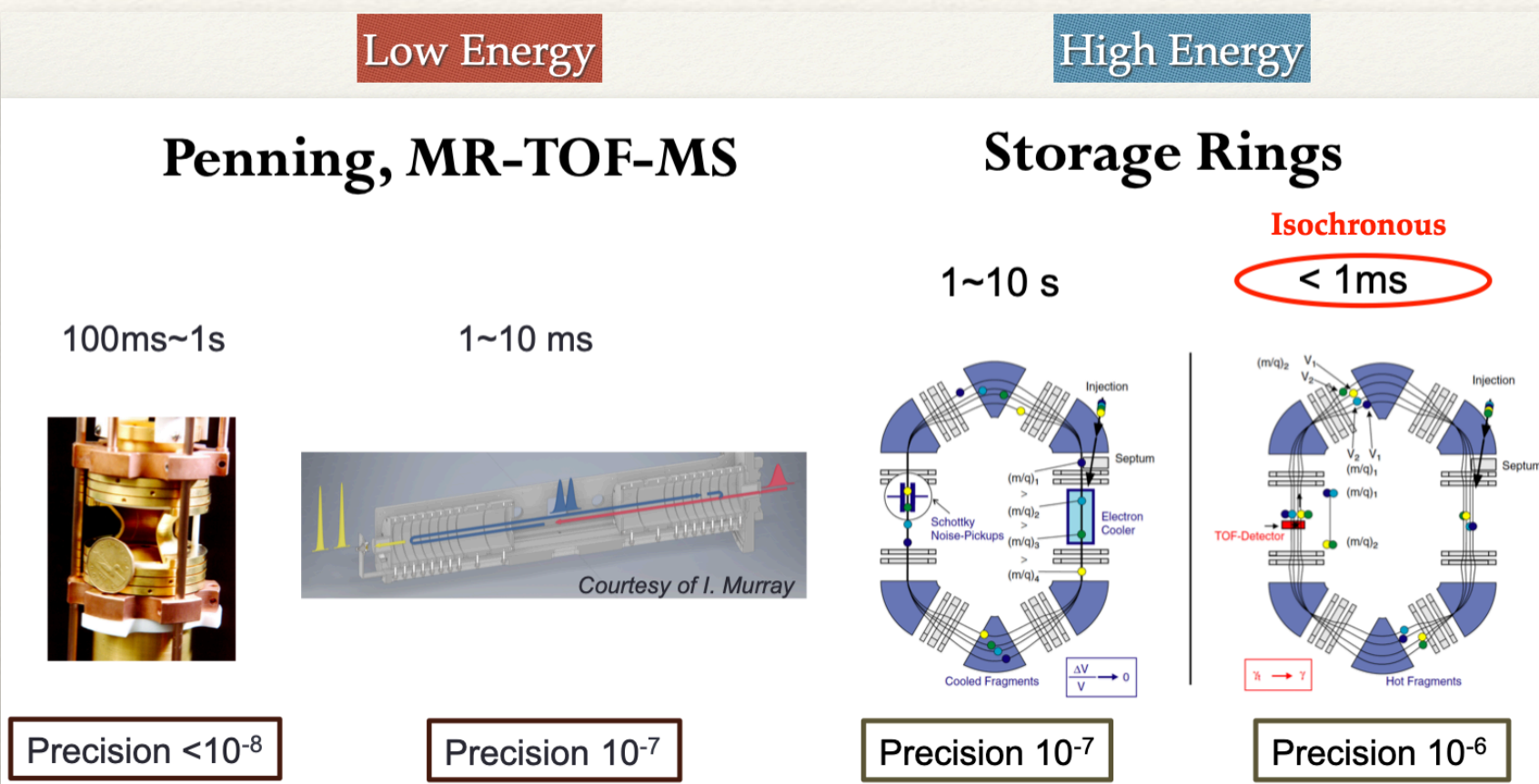
Precision $<10^{-8}$

Precision 10^{-7}

Precision 10^{-7}

Precision 10^{-6}

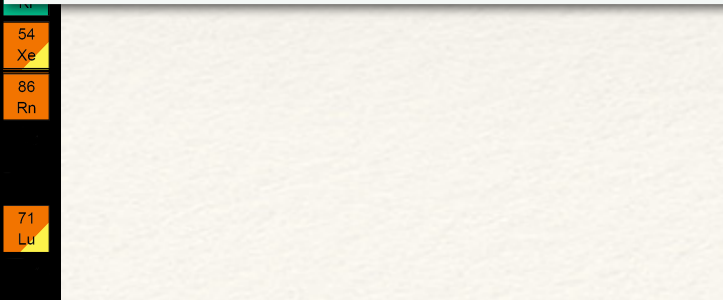
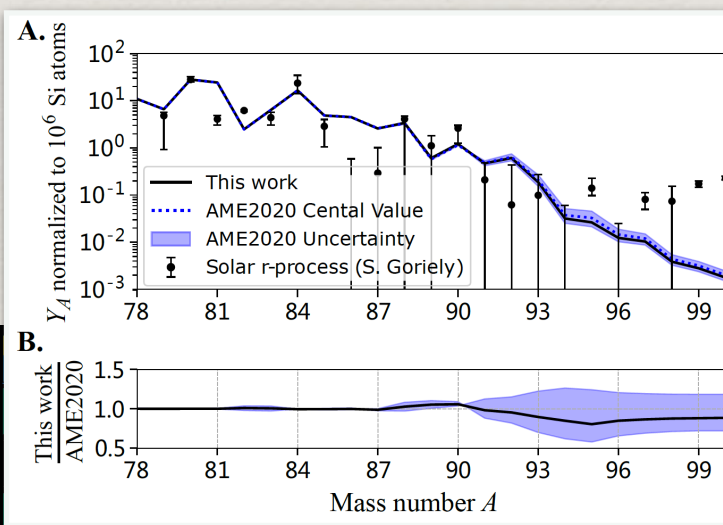
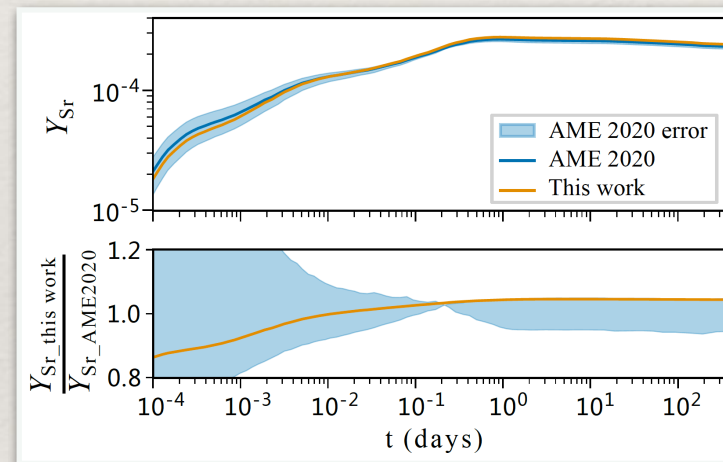
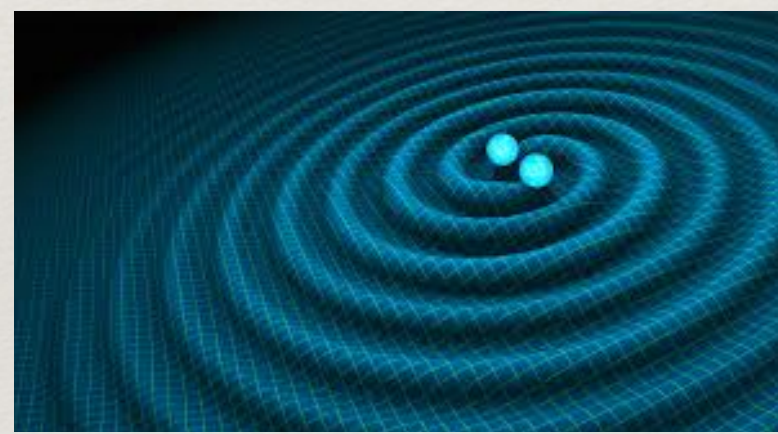
Takeaway



Atomic Mass

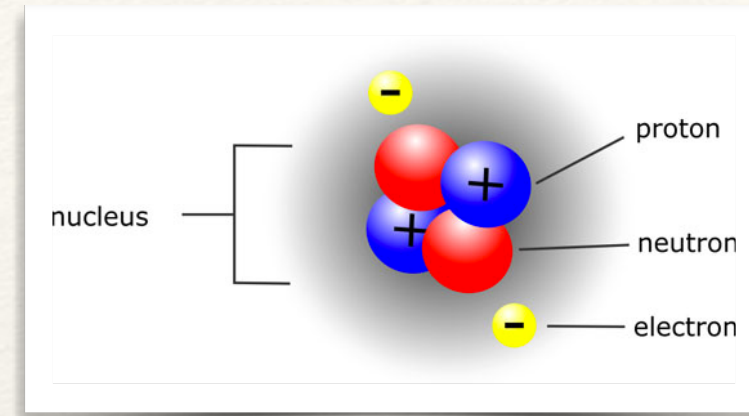
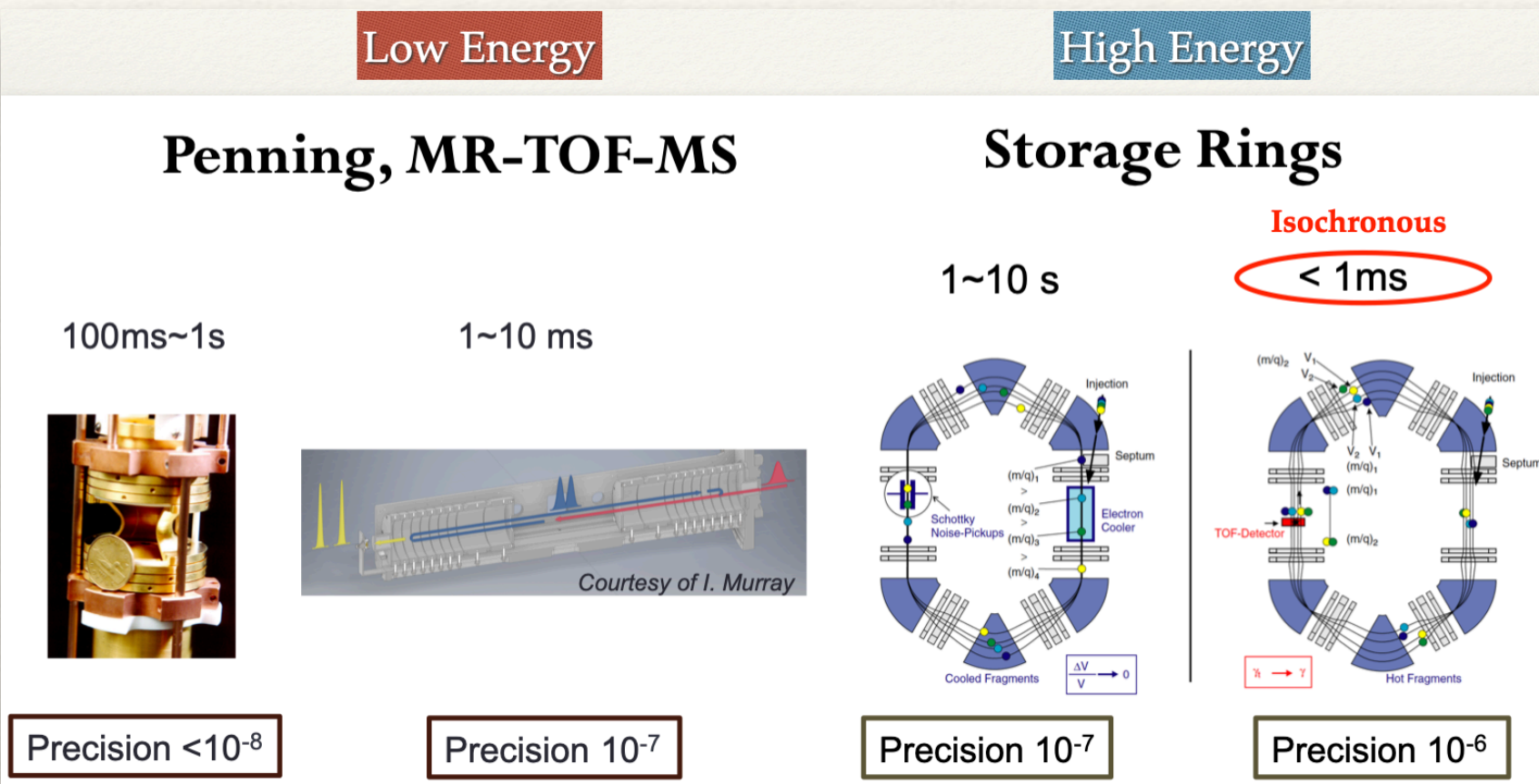
$$M(^4\text{He}) = 2 \cdot m_p + 2 \cdot m_n + 2 \cdot m_e - \text{Binding Energy}$$

Mass measurement for the r-process



1	H	big bang fusion	cosmic ray fission
2	He		
3	Li	merging neutron stars	exploding massive stars
4	Be		
5	B		
6	C		
7	N		
8	O		
9	F		
10	Ne		
11	Na	dying low mass stars	exploding white dwarfs
12	Mg		
13	Al		
14	Si		
15	P		
16	S		
17	Cl		
18	Ar		
19	K		
20	Ca		
21	Sc		
22	Ti		
23	V		
24	Cr		
25	Mn		
26	Fe		
27	Co		
28	Ni		
29	Cu		
30	Zn		
31	Ga		
32	Ge		
33	As		
34	Se		
35	Br		
36	Kr		
37	Rb		
38	Sr		
39	Y		
40	Zr		
41	Nb		
42	Mo		
43	Tc		
44	Ru		
45	Rh		
46	Pd		
47	Ag		
48	Cd		
49	In		
50	Sn		
51	Sb		
52	Te		
53	I		
54	Xe		
55	Ba		
56	Lanthanides		
57	La		
58	Ce		
59	Pr		
60	Nd		
61	Pm		
62	Sm		
63	Eu		
64	Gd		
65	Tb		
66	Dy		
67	Ho		
68	Er		
69	Tm		
70	Yb		
71	Lu		
72	Hf		
73	Ta		
74	W		
75	Re		
76	Os		
77	Ir		
78	Pt		
79	Au		
80	Hg		
81	Tl		
82	Pb		
83	Bi		
84	Po		
85	At		
86	Rn		
87	Fr		
88	Ra		
89	Actinides		
90	Th		
91	Pa		
92	U		

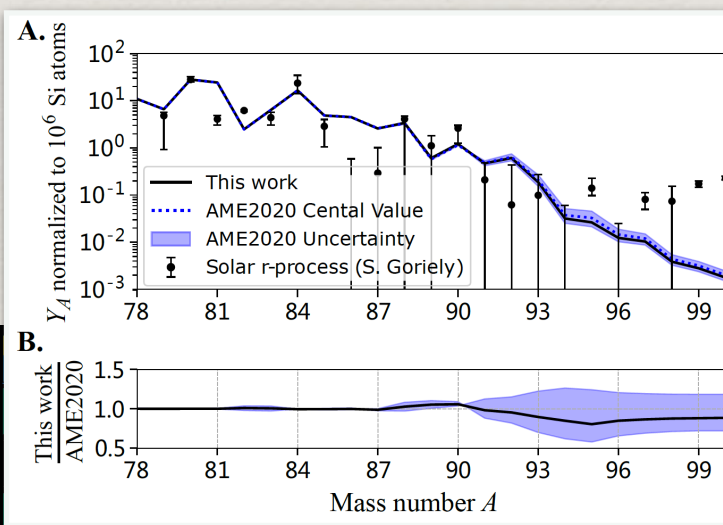
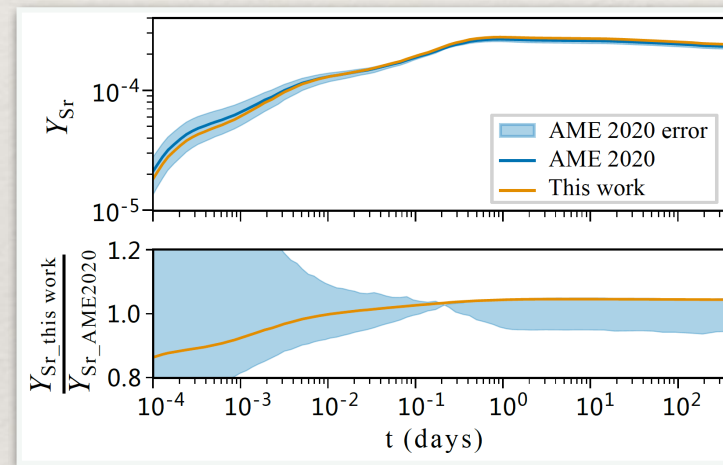
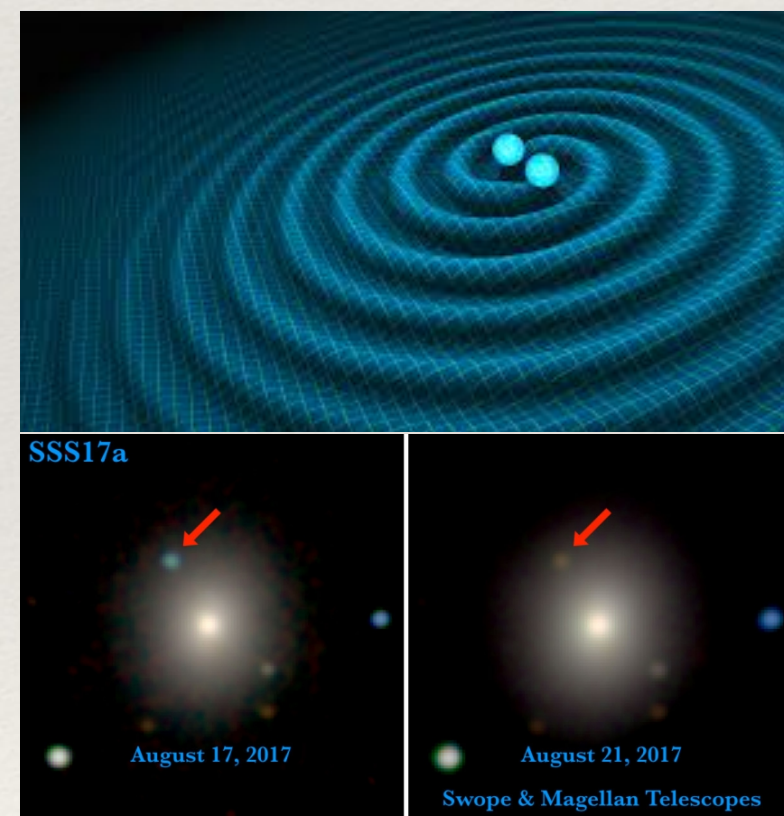
Takeaway



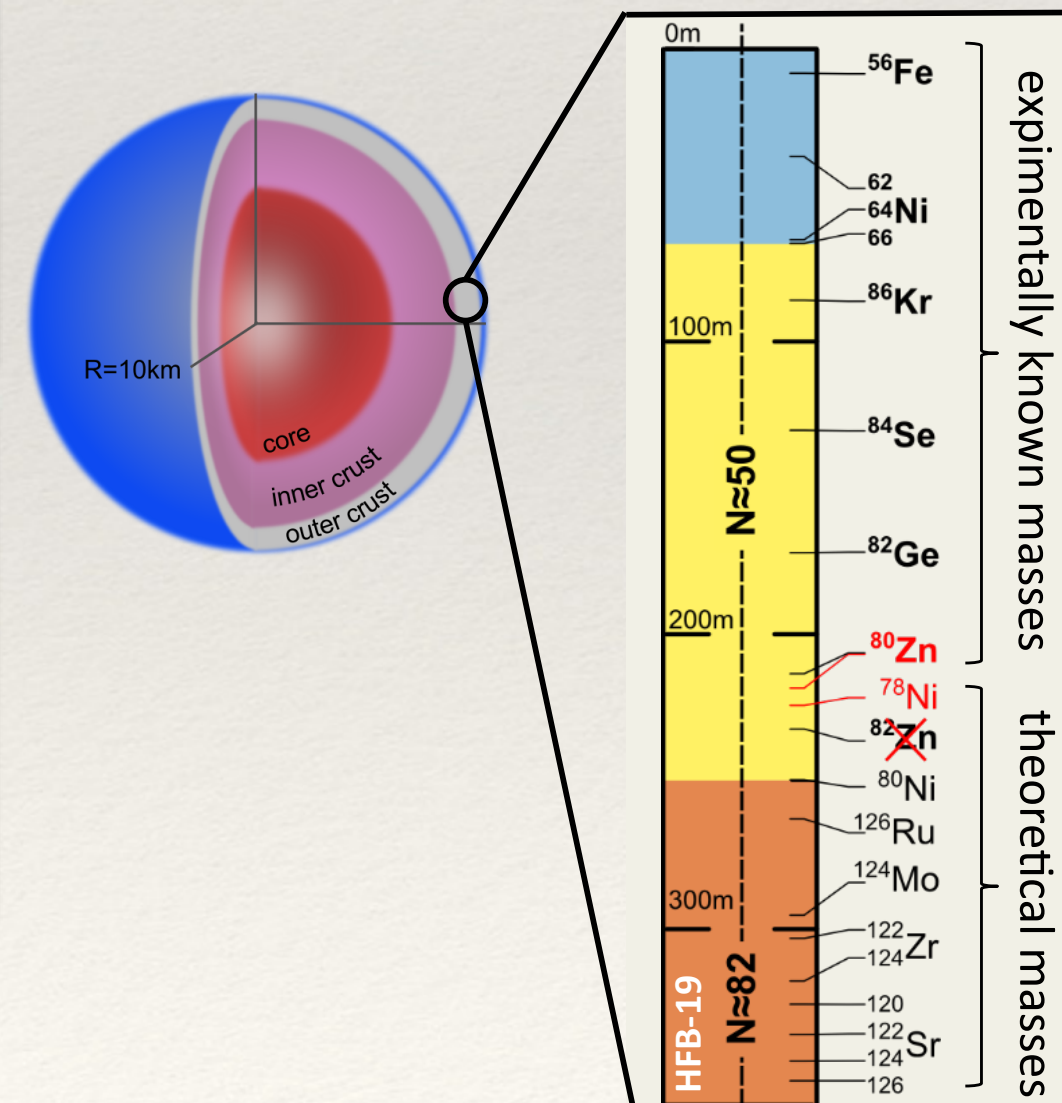
Atomic Mass

$$M(^4\text{He}) = 2 \cdot m_p + 2 \cdot m_n + 2 \cdot m_e - \text{Binding Energy}$$

Mass measurement for the r-process

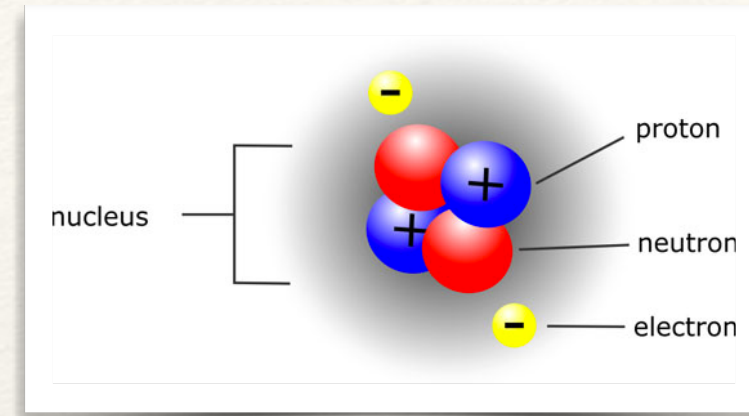
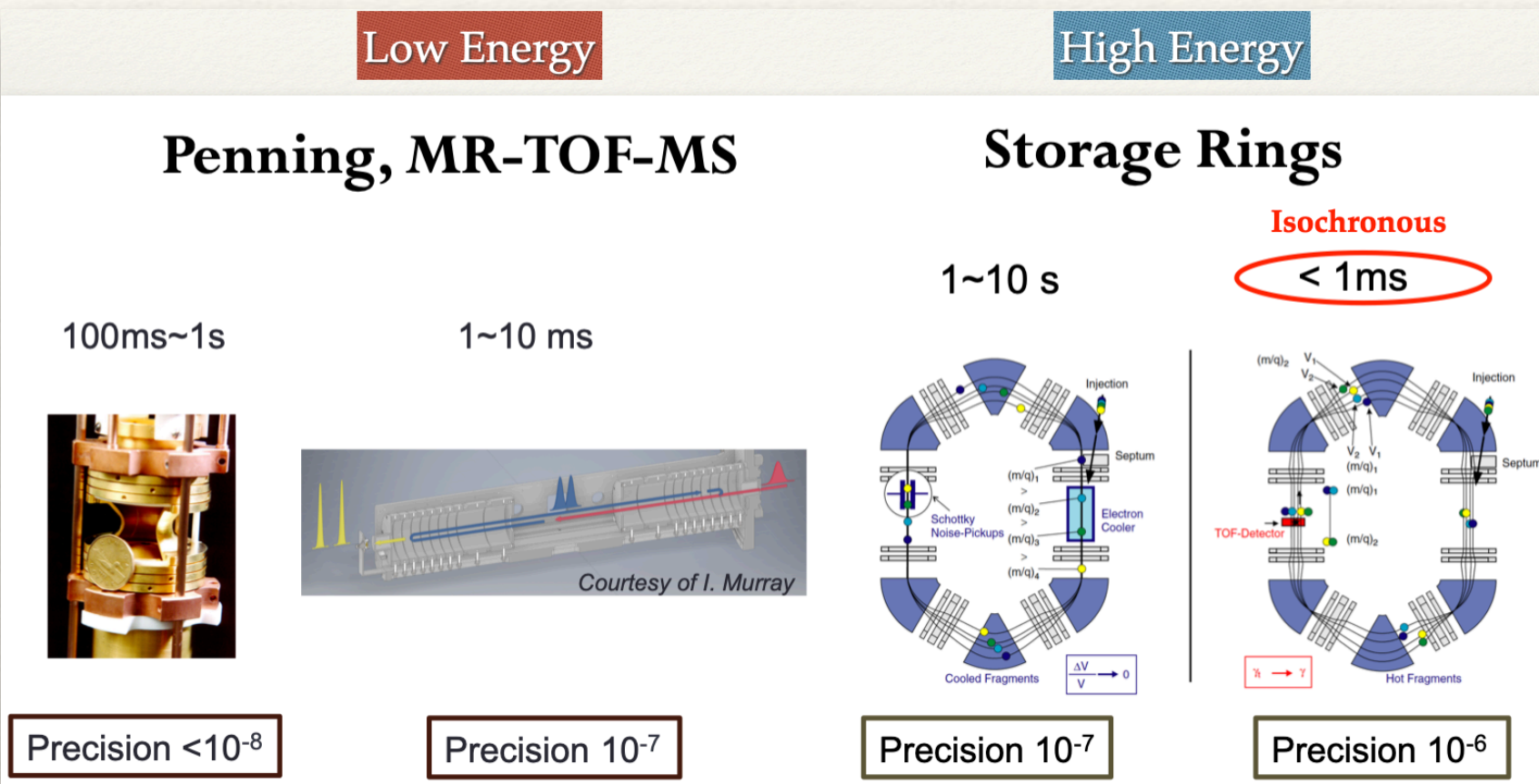


We can "drill" into the neutron star to reveal its composition



1	H	big bang fusion	cosmic ray fission
2	He	merging neutron stars	exploding massive stars
3	Li	dying low mass stars	exploding white dwarfs
4	Be		
5	B		
6	C		
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8	O		
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65	Tb		
66	Dy		
67	Ho		
68	Er		
69	Tm		
70	Yb		
71	Lu		
72	Hf		
73	Ta		
74	W		
75	Re		
76	Os		
77	Ir		
78	Pt		
79	Au		
80	Hg		
81	Tl		
82	Pb		
83	Bi		
84	Po		
85	At		
86	Rn		
87	Fr		
88	Ra		

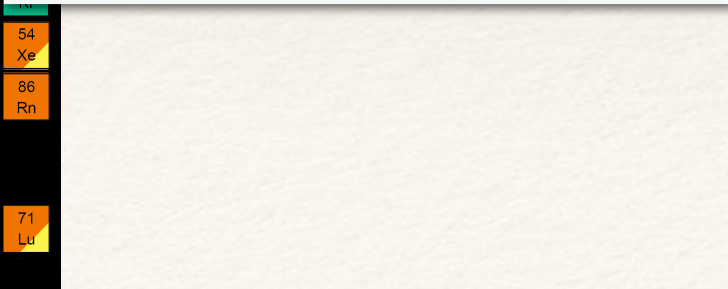
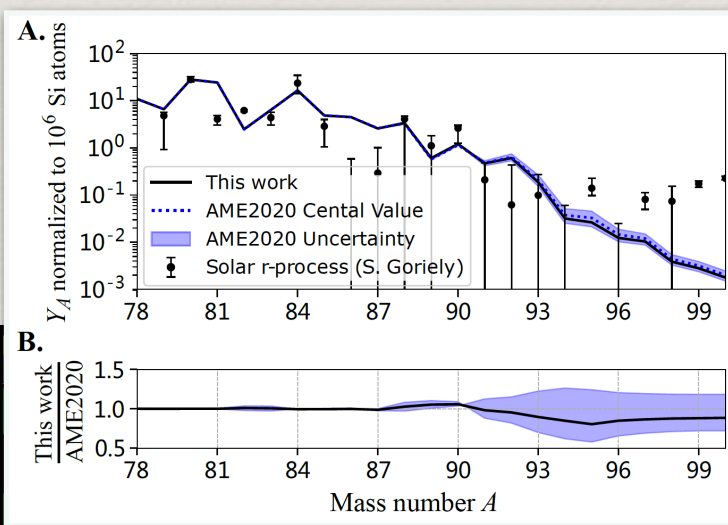
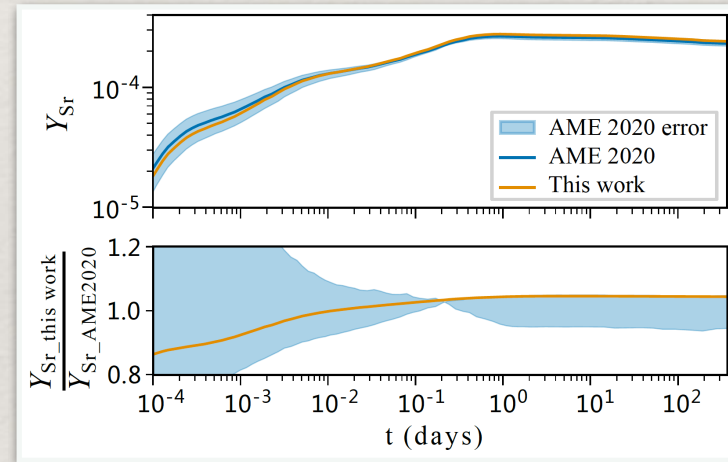
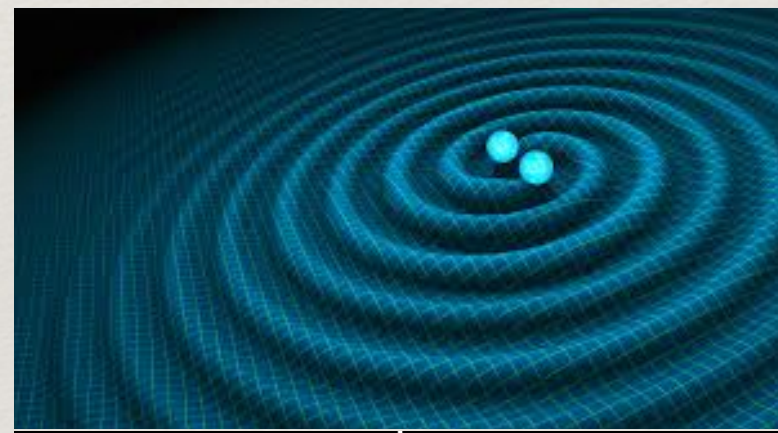
Takeaway



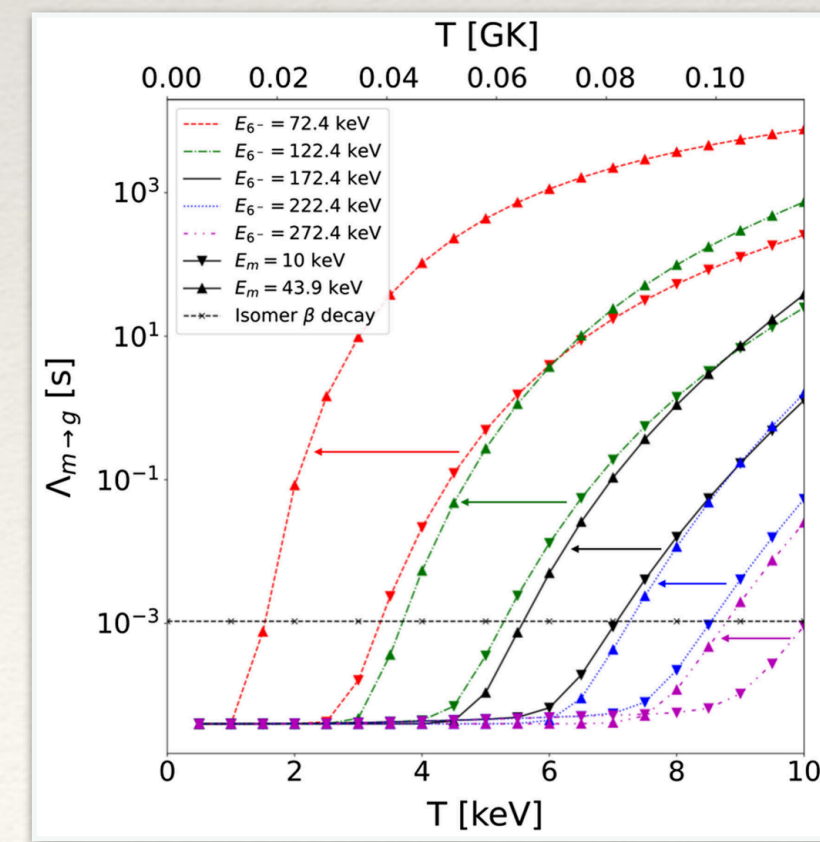
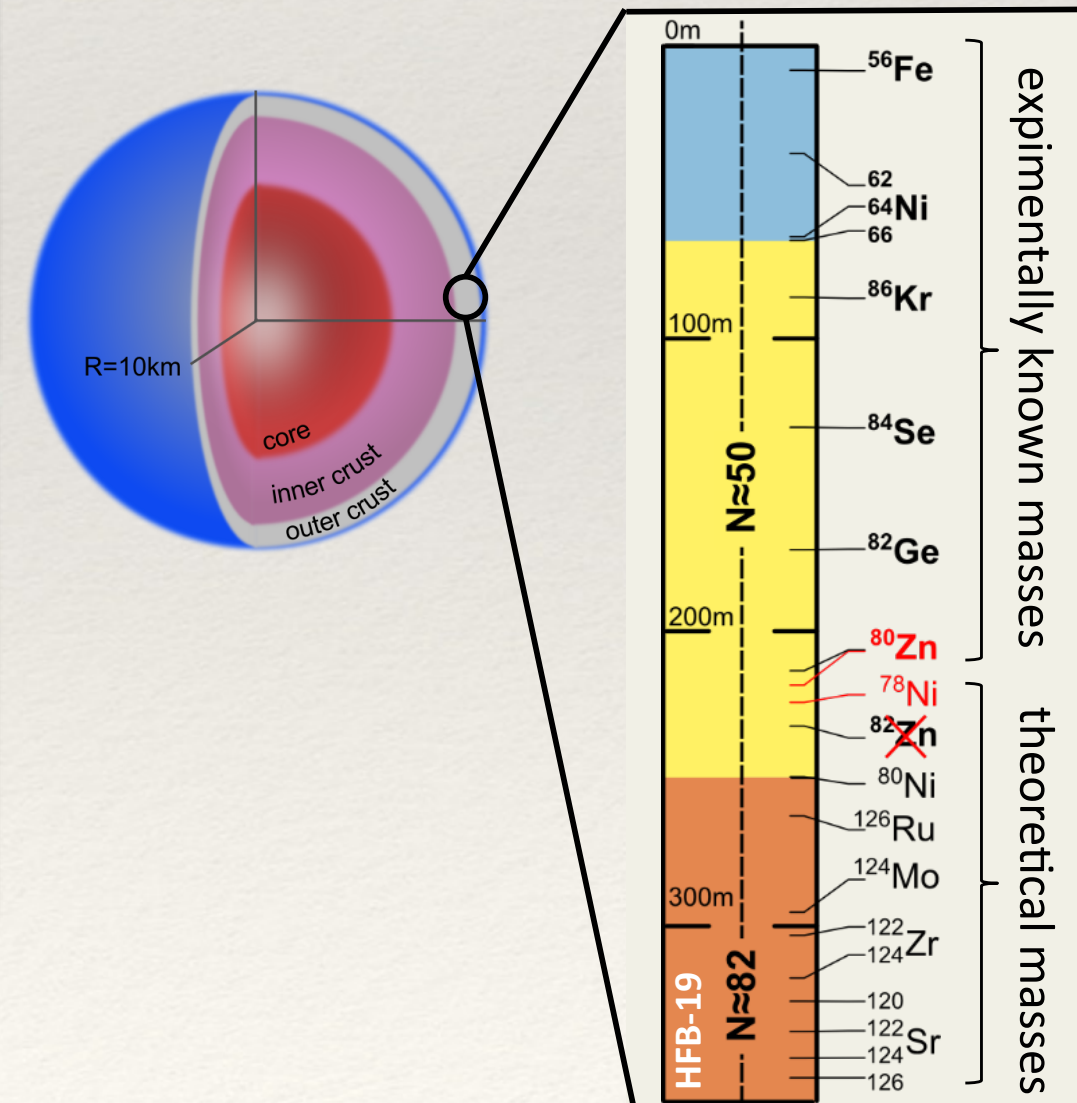
Atomic Mass

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Mass measurement for the r-process

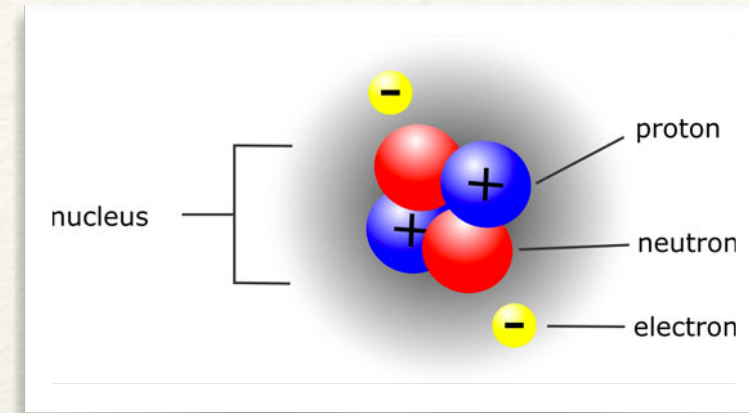
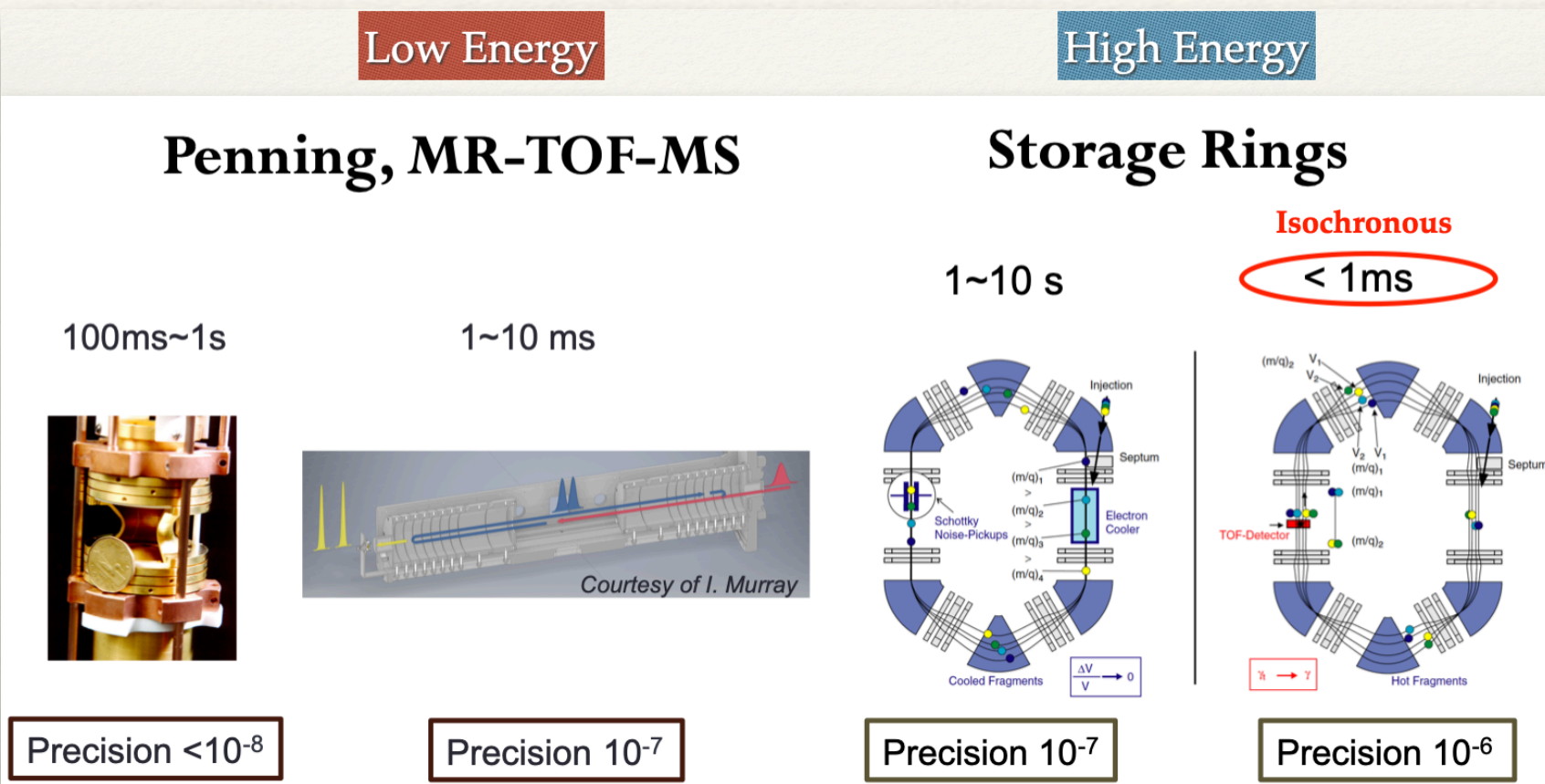


We can "drill" into the neutron star to reveal its composition



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87 Fr	88 Ra		
57 La	58 Ce		
89 Ac	90 Th		

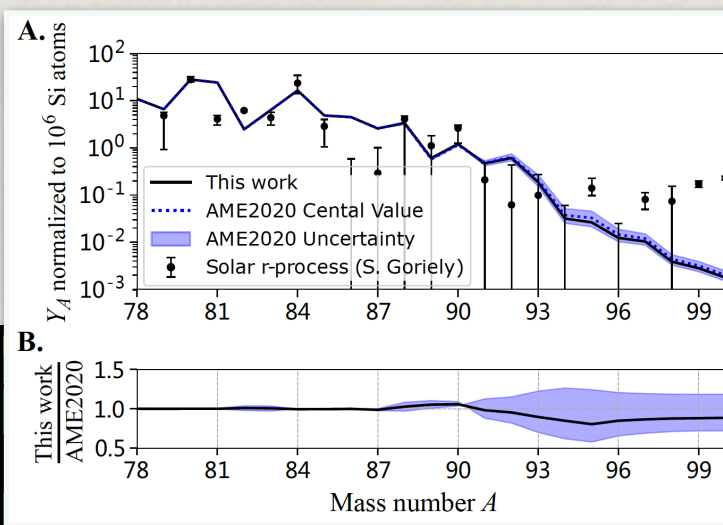
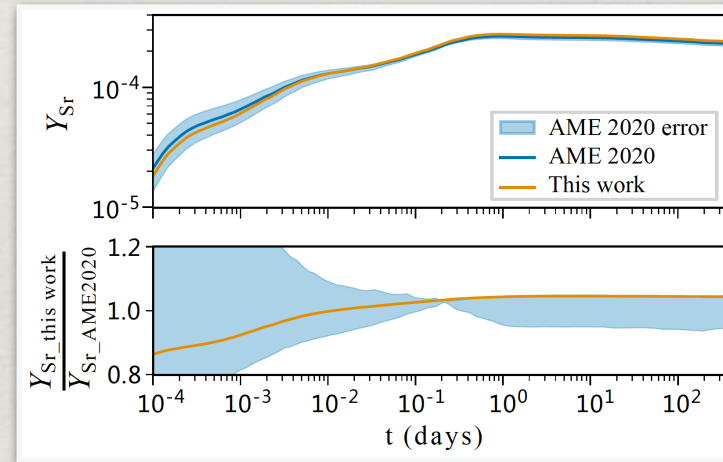
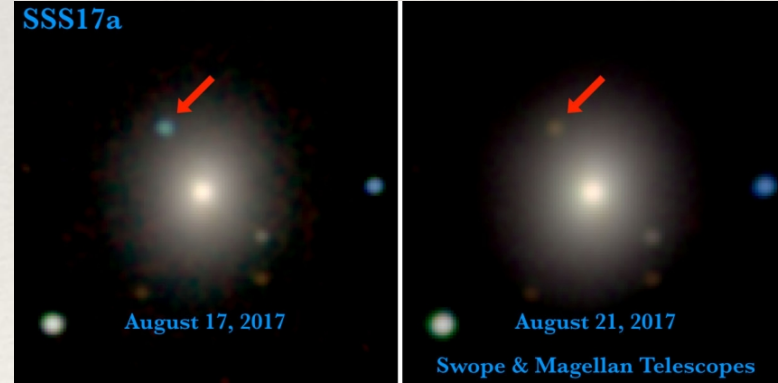
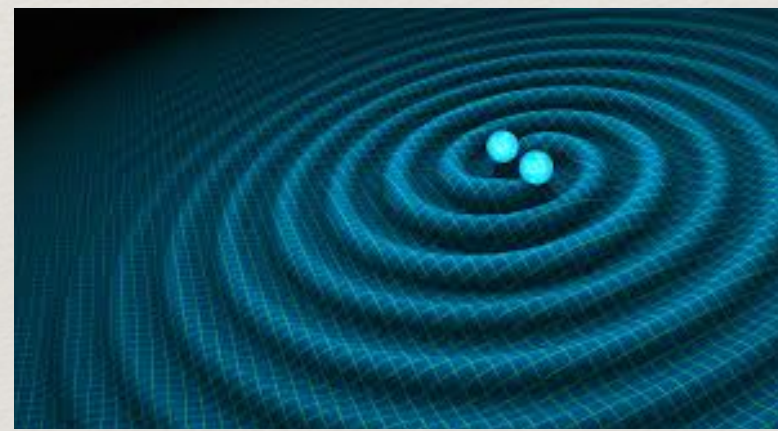
Takeaway



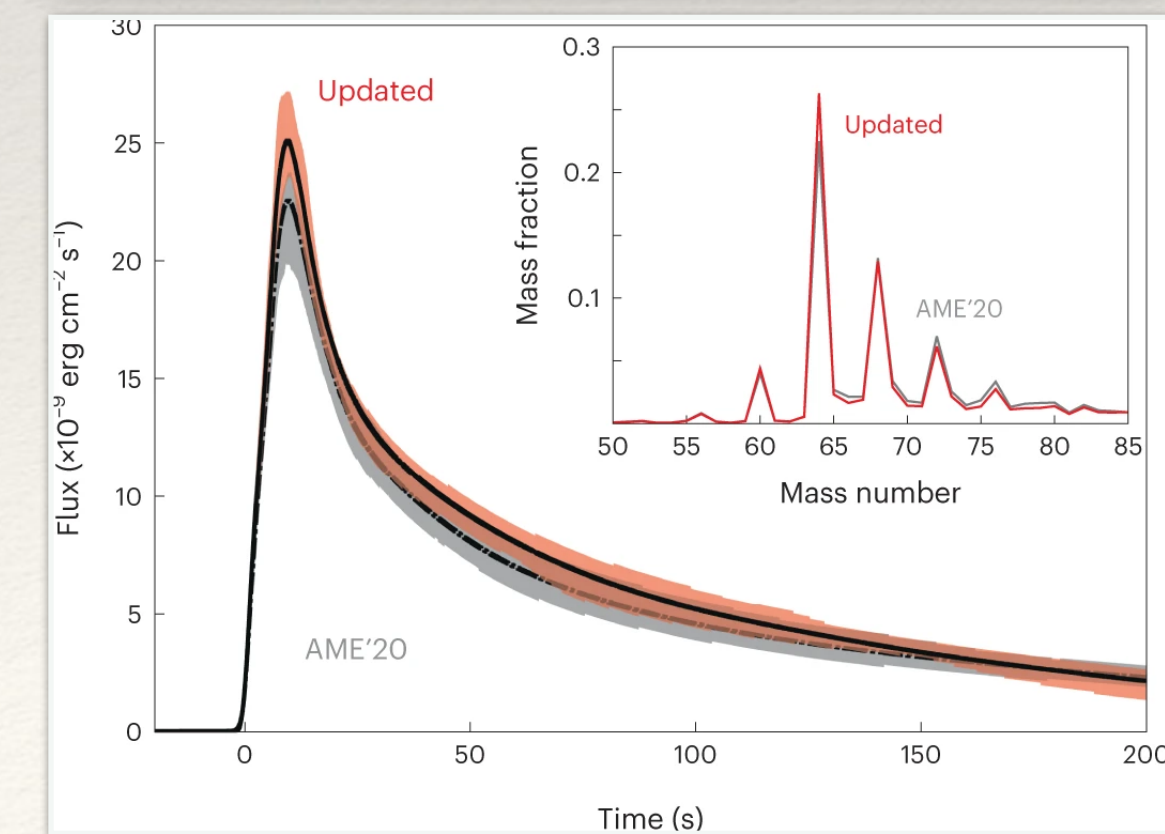
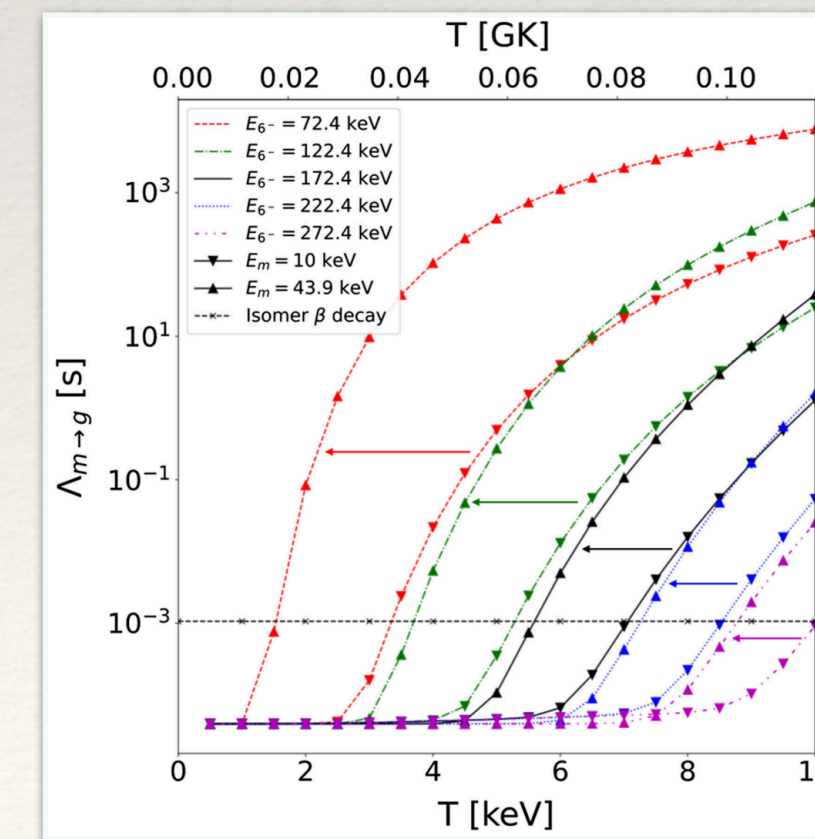
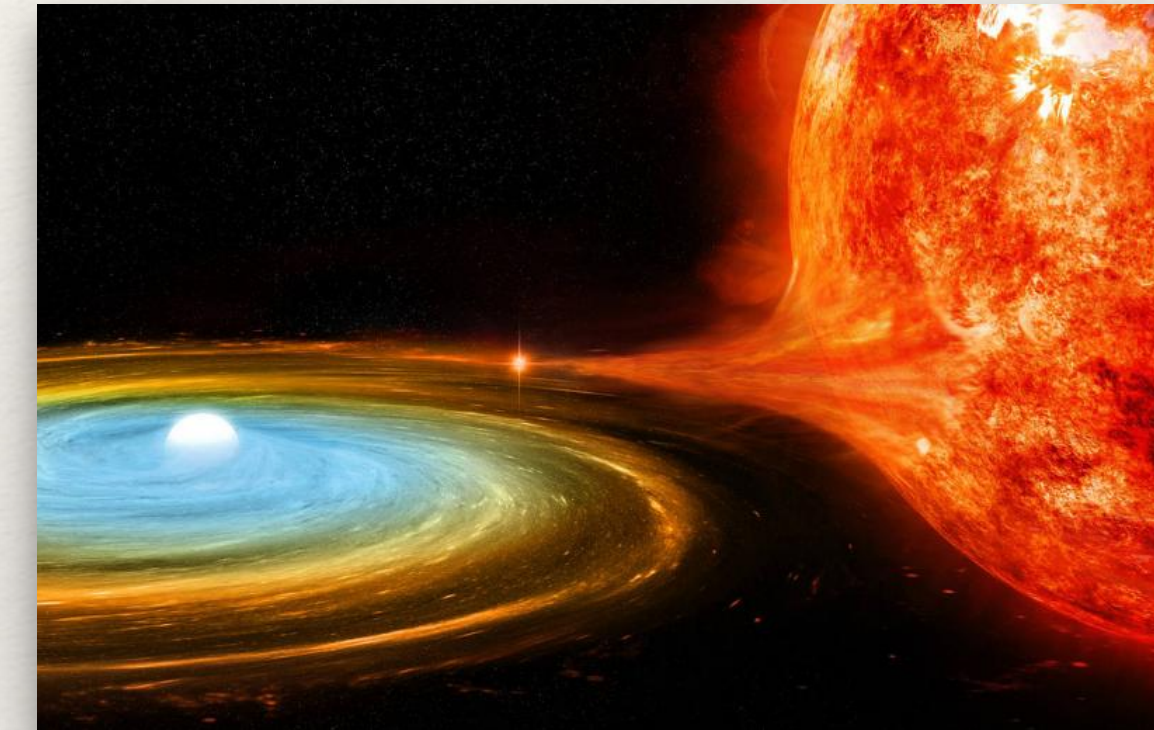
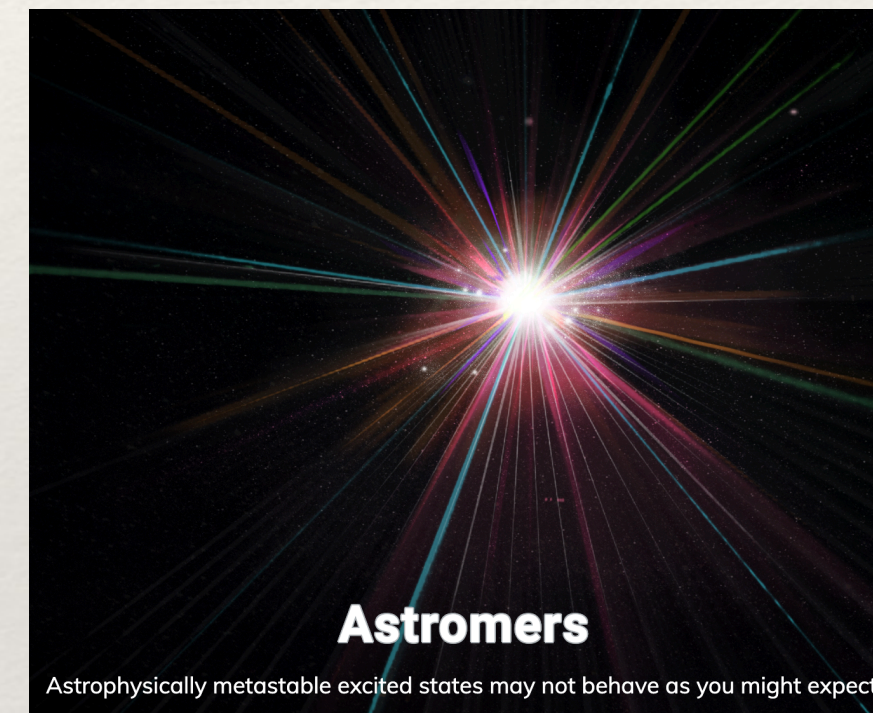
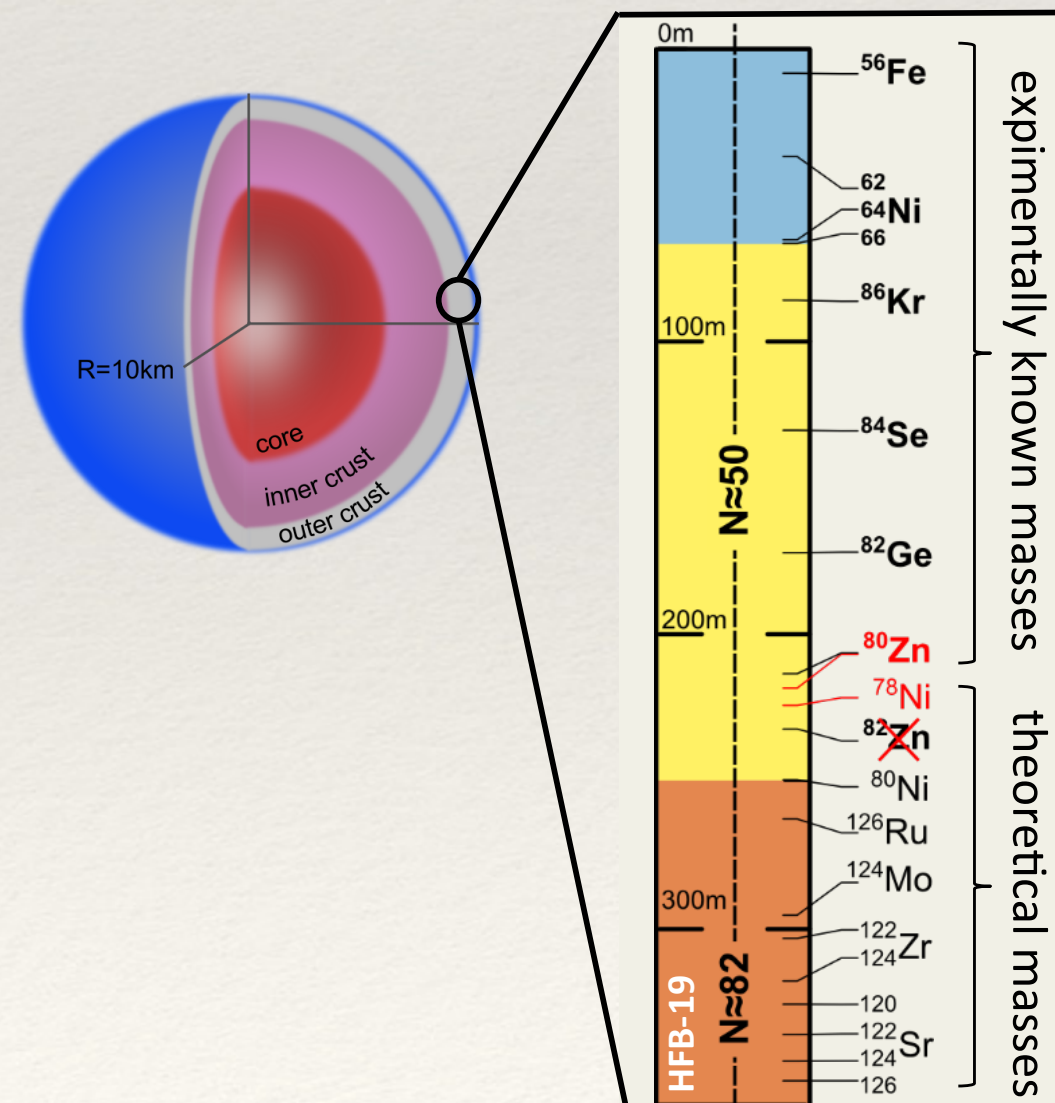
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Mass measurement for the r-process



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21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn
31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	37 Rb	38 Sr	39 Y	40 Zr
41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn
51 Sb	52 Te	53 I	54 Xe	55 Cs	56 Ba	57 La	58 Ce	59 Pr	60 Nd
61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb
71 Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg
81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn	87 Fr	88 Ra	89 Ac	90 Th
91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm
101 Md	102 No	103 Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds
111 Rg	112 Cn	113 Nh	114 Fl	115 Lv	116 Ts	117 Og	118 Uu	119 Uub	120 Uuq