



University of Paris

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Isostasy Revisited: A Novel Approach to an Age-Old Theory

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Supervisors:
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Dr. Marianne Greff

March 2024



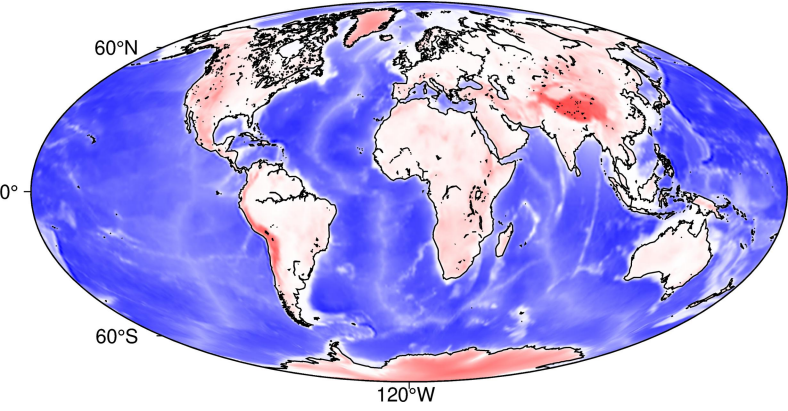
Introduction

Method

Results

Conclusion

Observed Topography





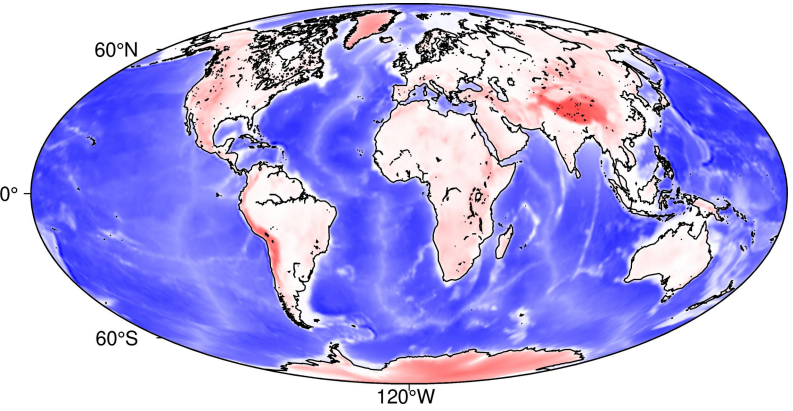
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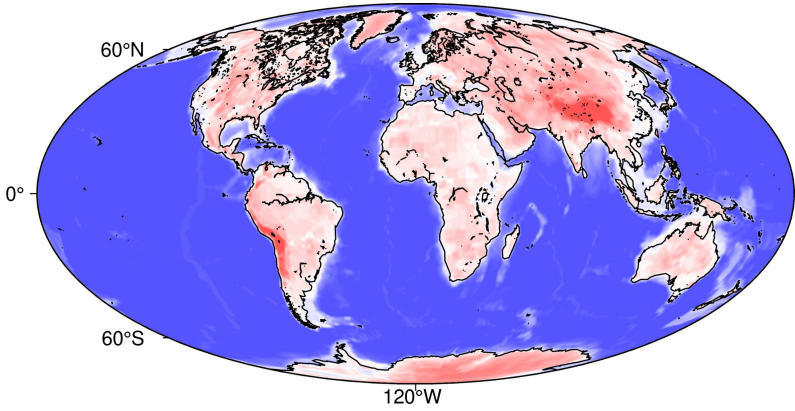
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Isostatic Topography





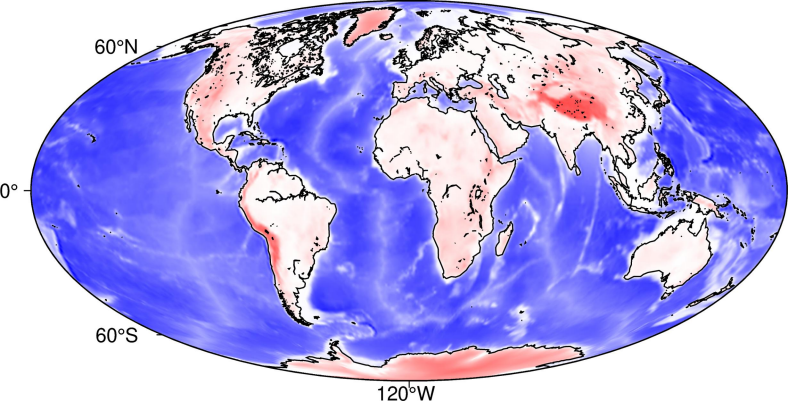
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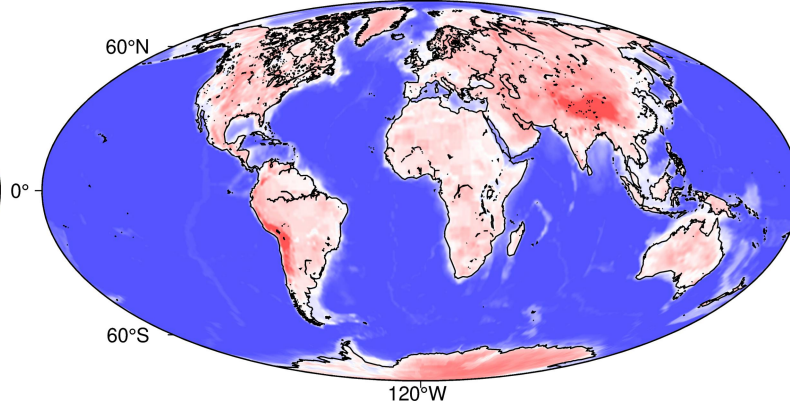
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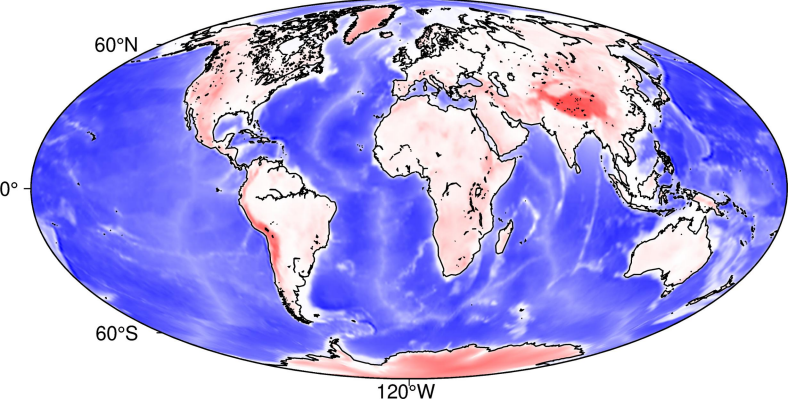
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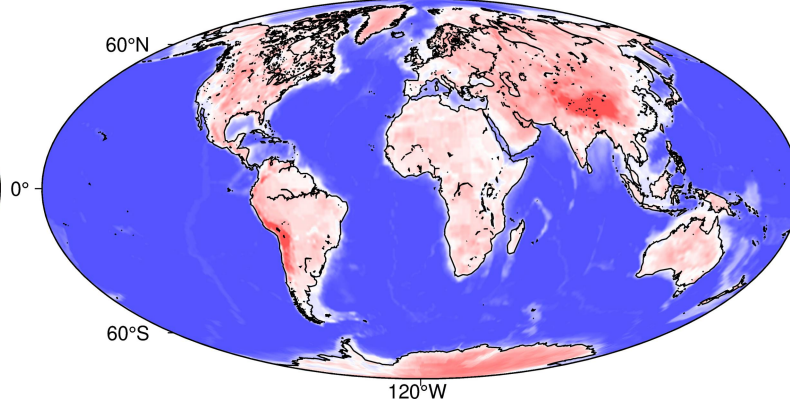
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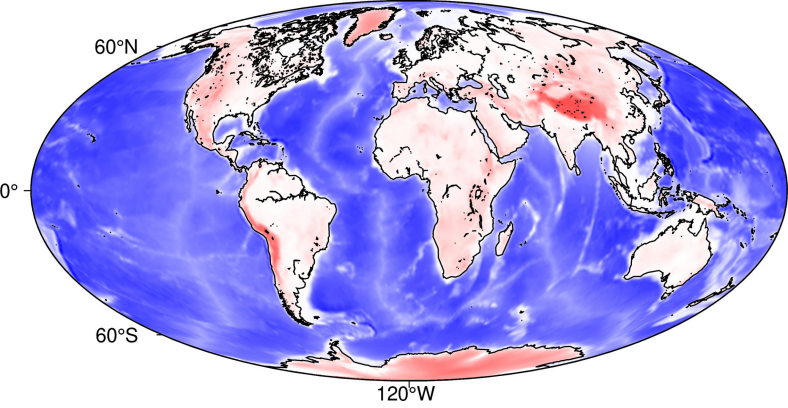
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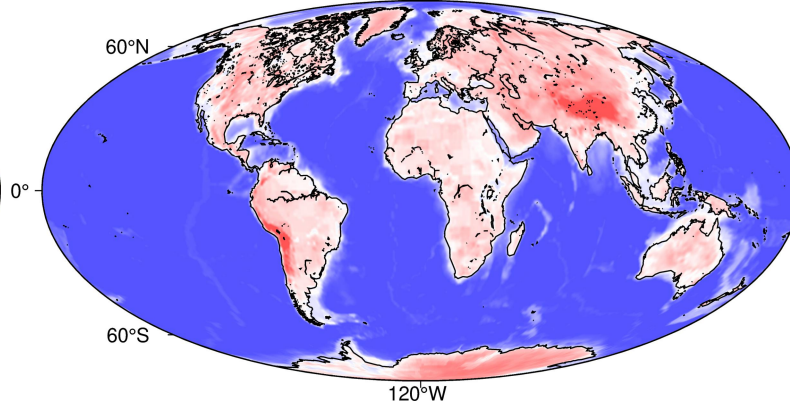
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Isostatic Topography



Residual topography and geoid provides global constraints on the amplitude and spatial distribution of density anomalies in the convecting mantle.



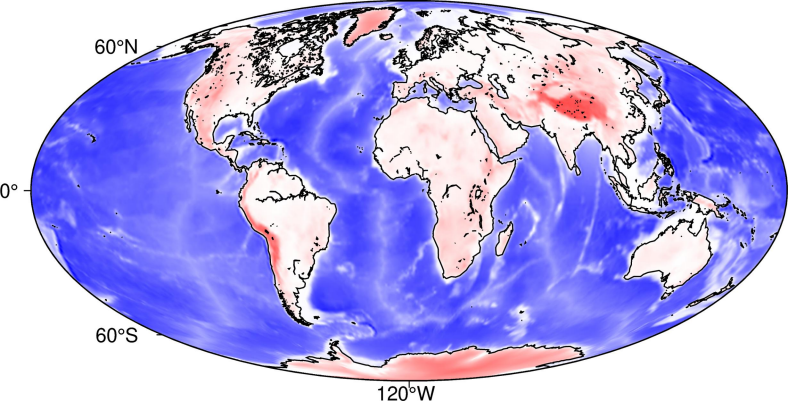
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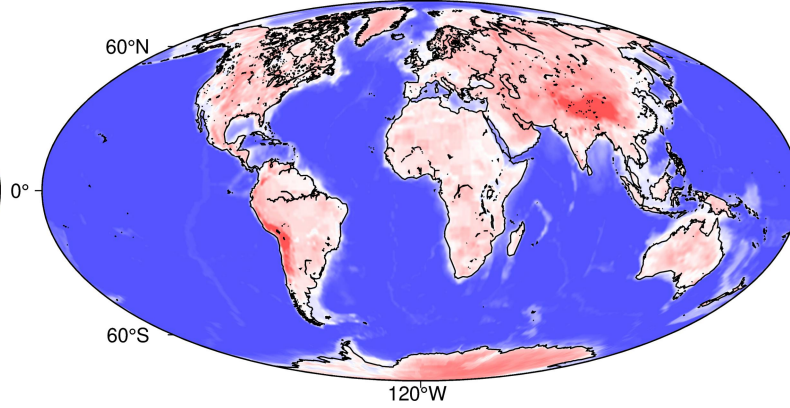
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Isostatic Topography



Simplification

- Viscous
- Compressible
- Self-gravitating
- Density heterogeneity

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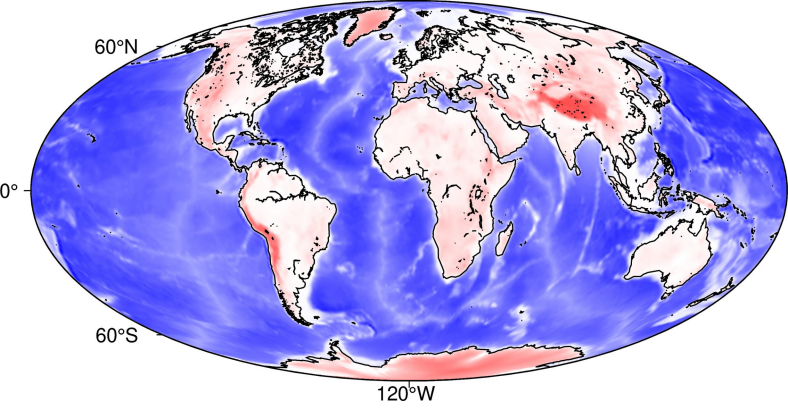
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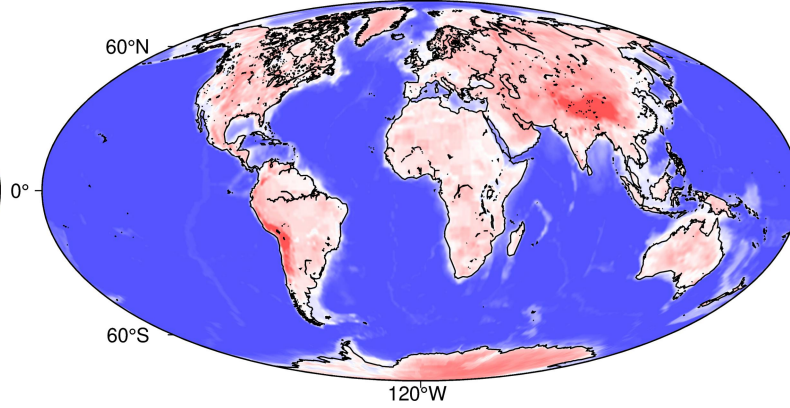
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Isostatic Topography



Questions

- How much these constraints are uncertain due to crustal models uncertainty?
- How can isostasy be geodynamically consistent?

Residual topography and geoid provides global constraints on the amplitude and spatial distribution of density anomalies in the convecting mantle.



Simplification

- Viscous
- Compressible
- Self-gravitating
- Density heterogeneity



- **Geodynamic observable and lateral density variation**

Corresponding kernel function

$$\delta O_{\ell}^m = f_{\ell} \int_b^a K_{\ell}(\eta; r') (\rho_1)_{\ell}^m(r') dr'$$

Geodynamic observable

Lateral density variation



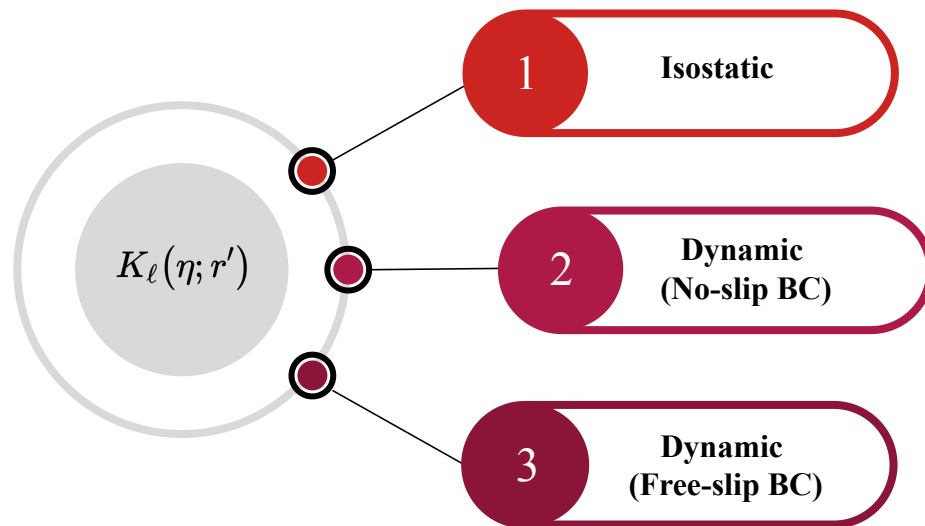
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Geodynamic observable

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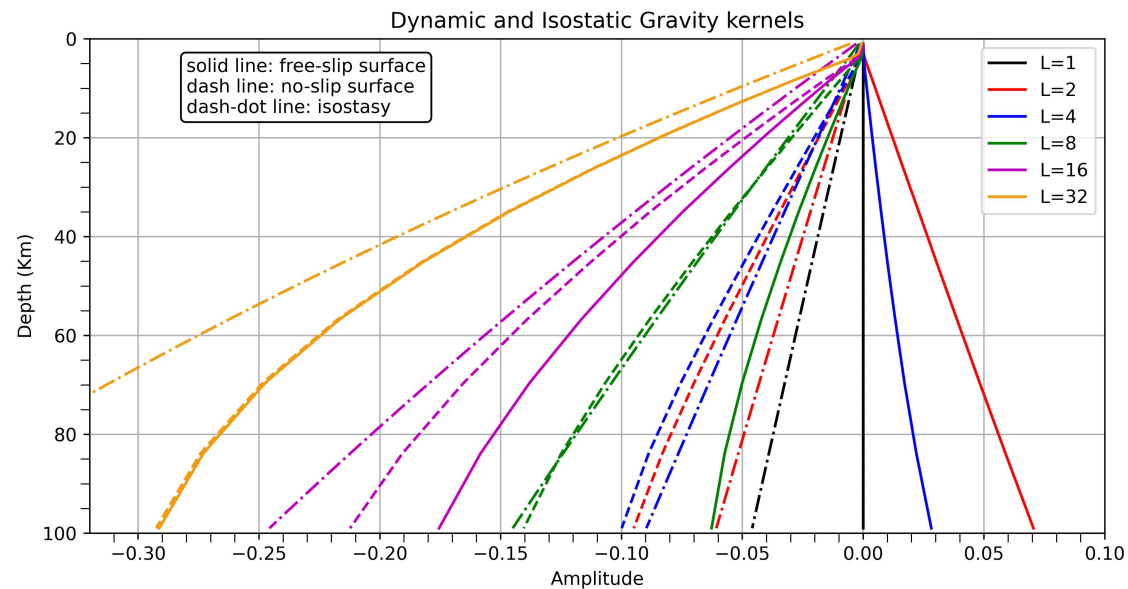
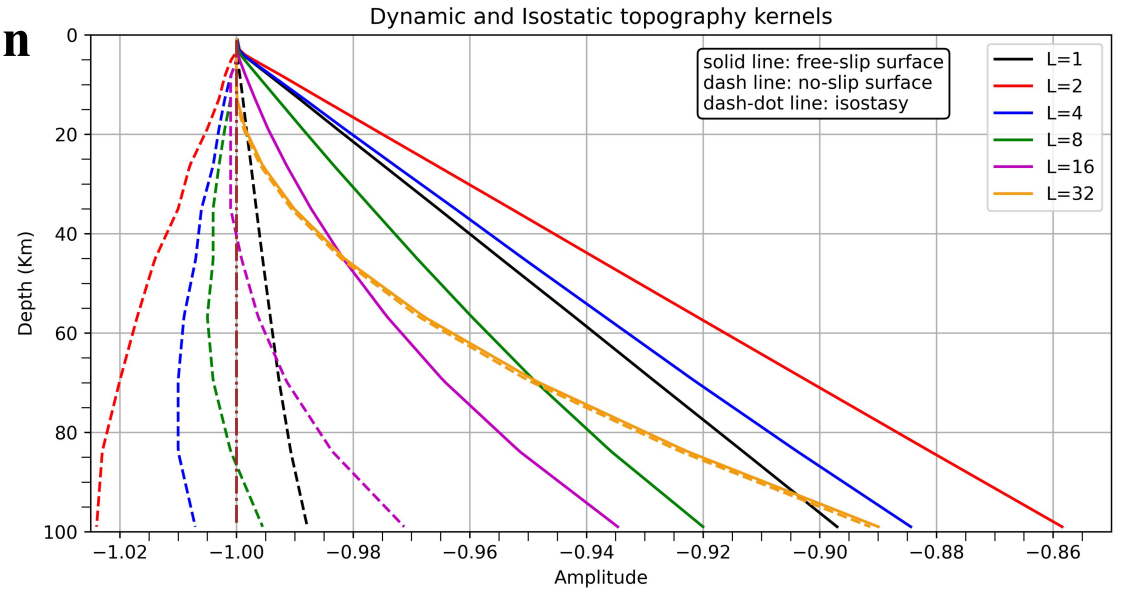
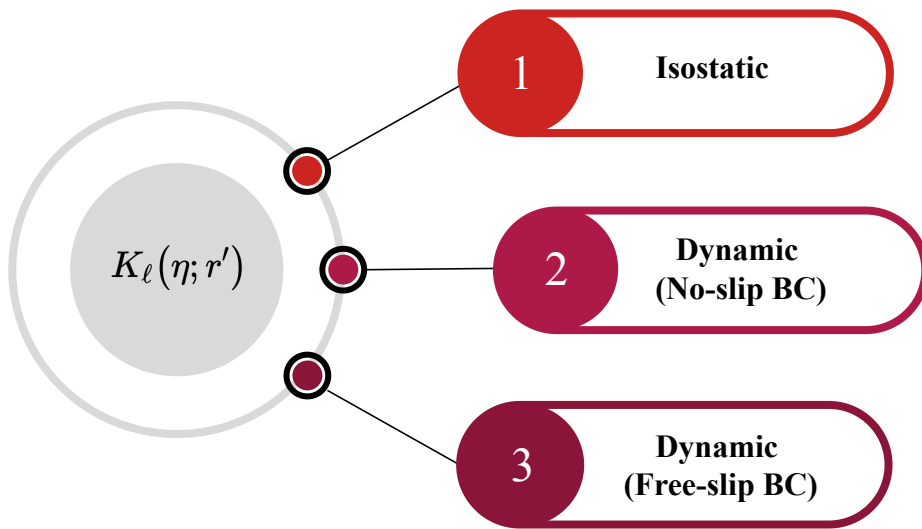
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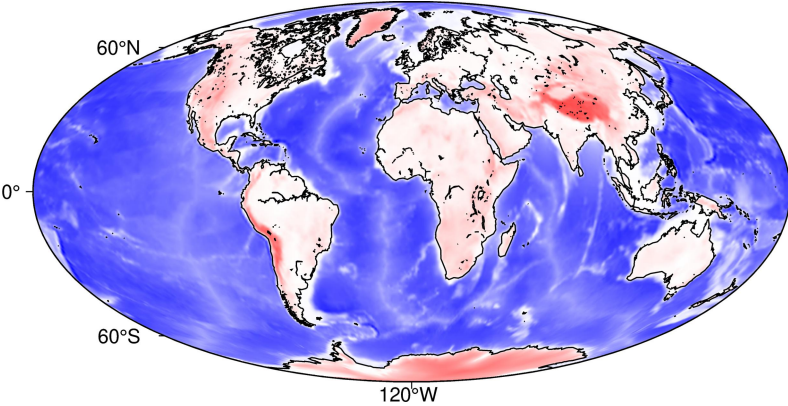
Geodynamic observable

Lateral density variation

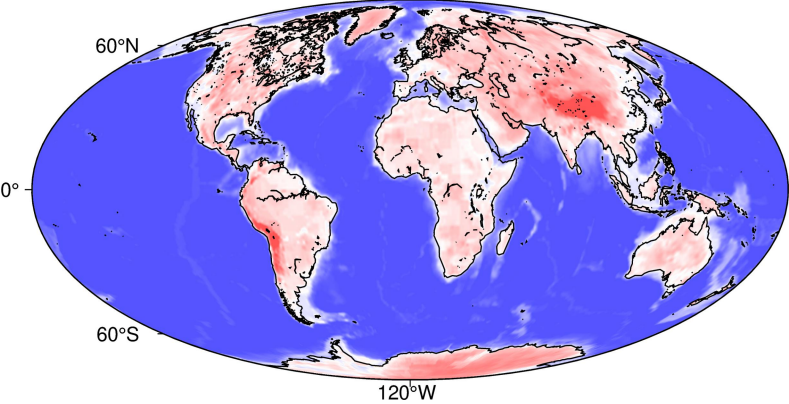


- Residual topography

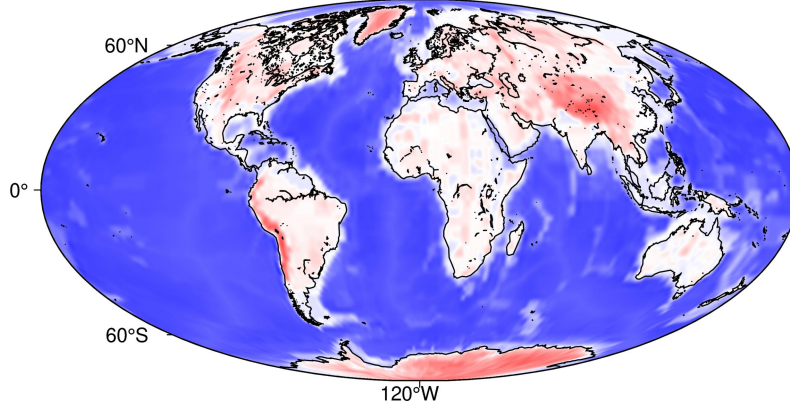
ETOPO 1



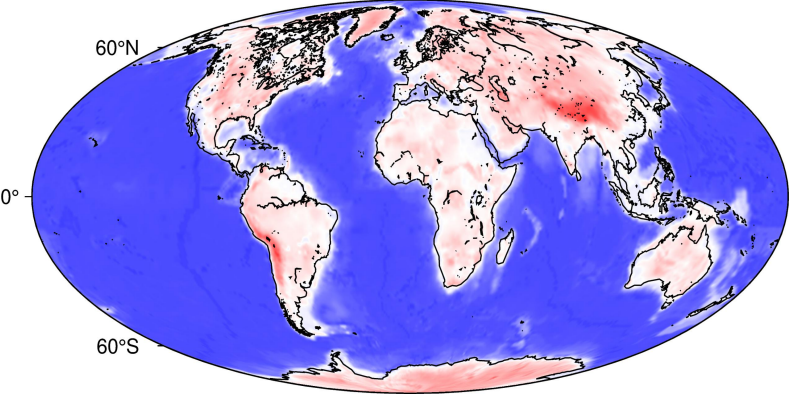
Crust 1.0



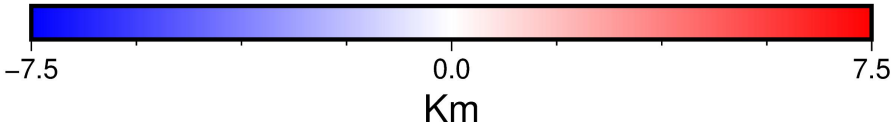
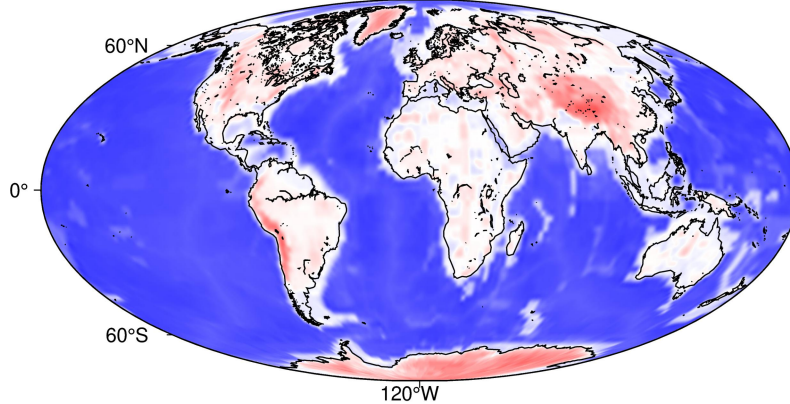
Crust 2.0



ECM 1

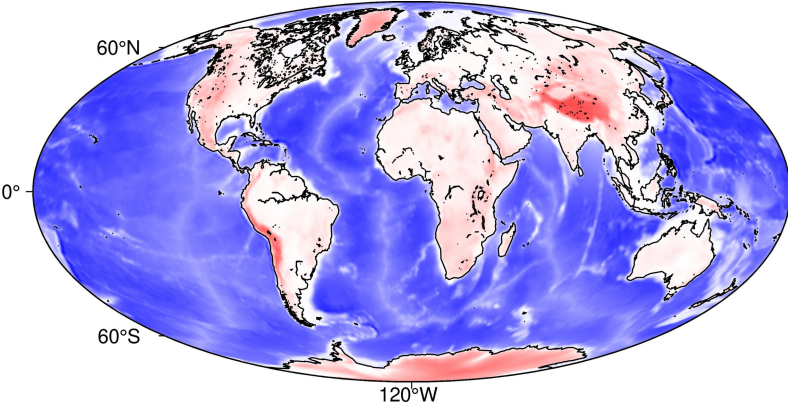


CG2

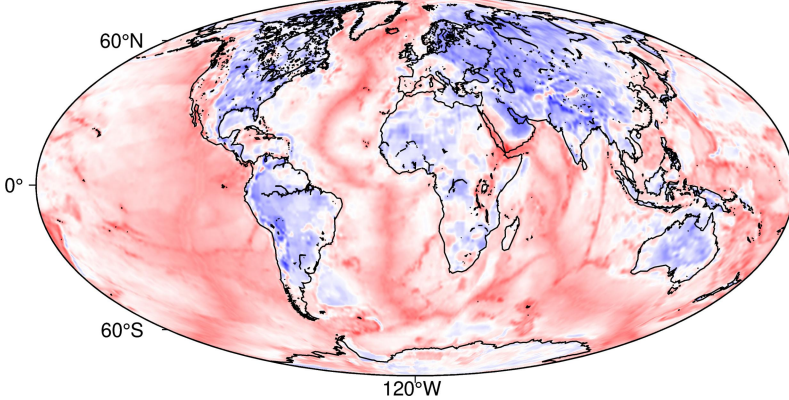


- Residual topography

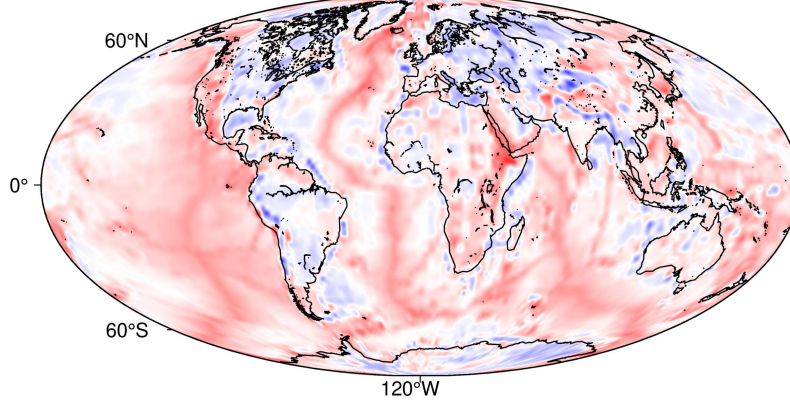
ETOPO 1



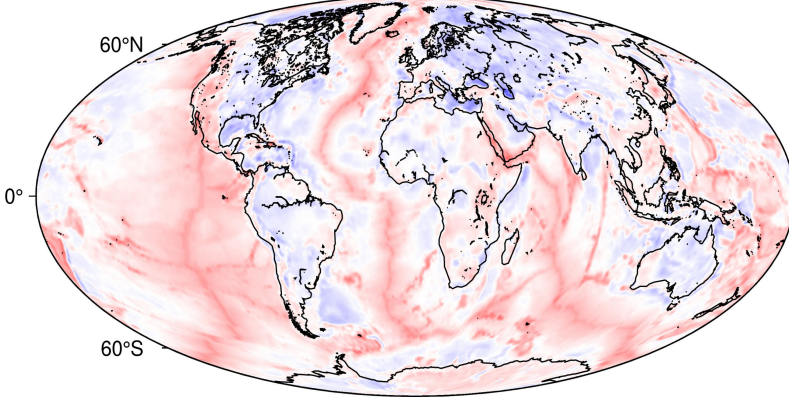
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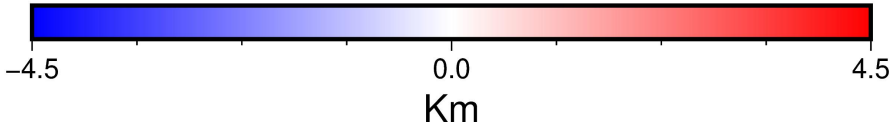
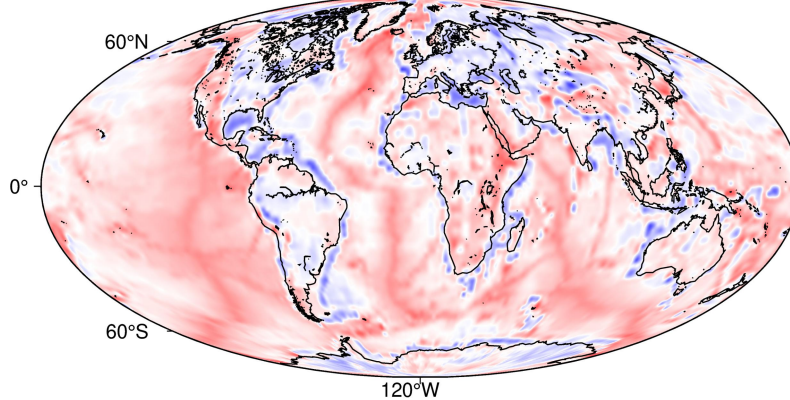
Crust 2.0



ECM 1

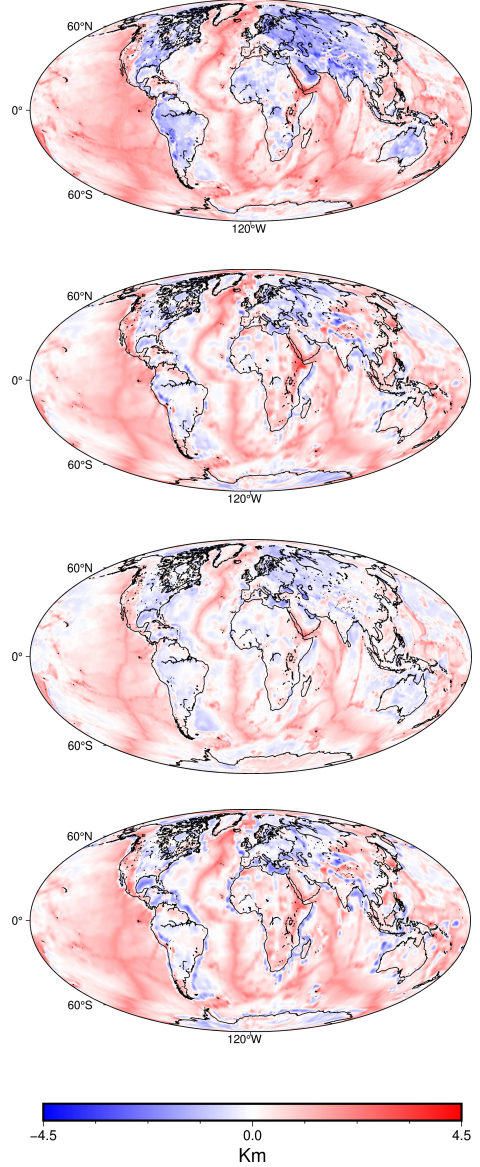
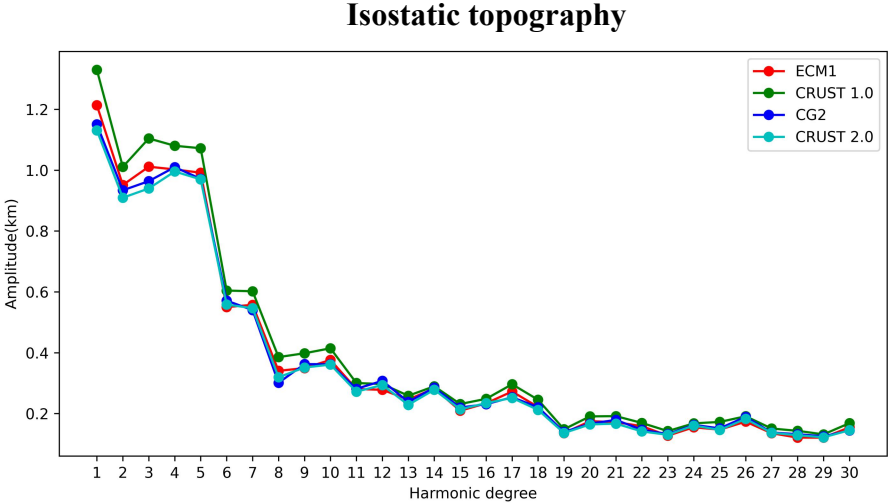
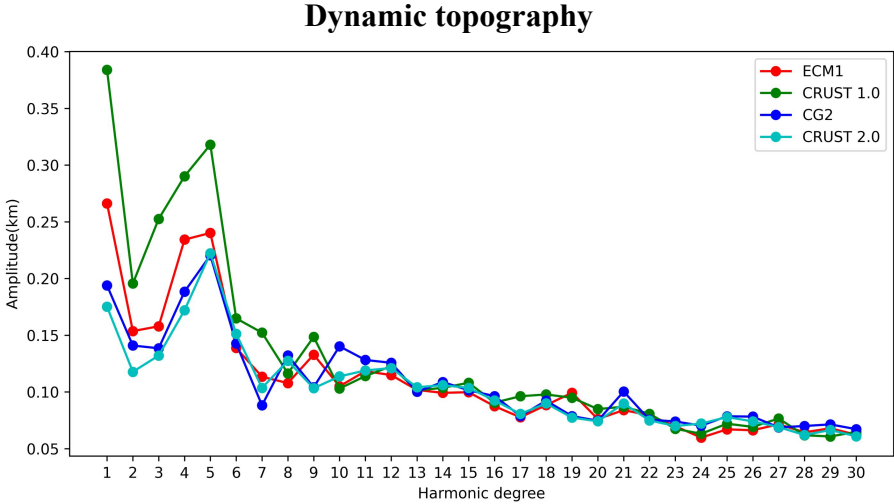


CG2





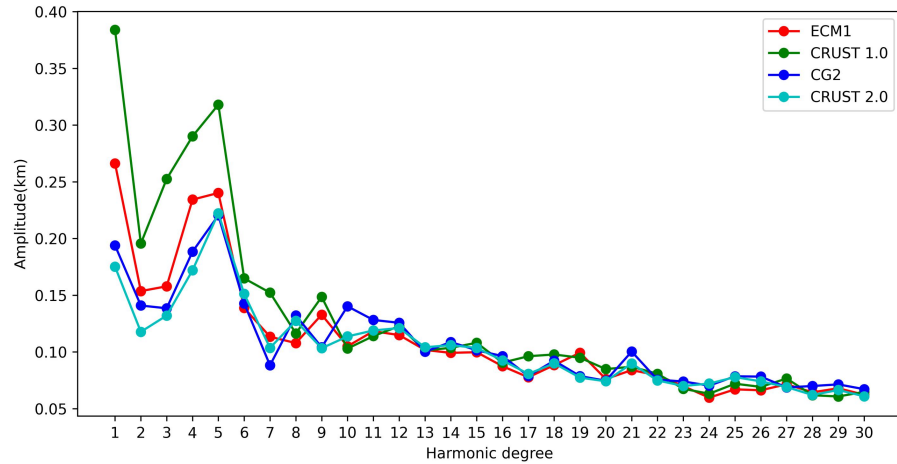
- Residual topography



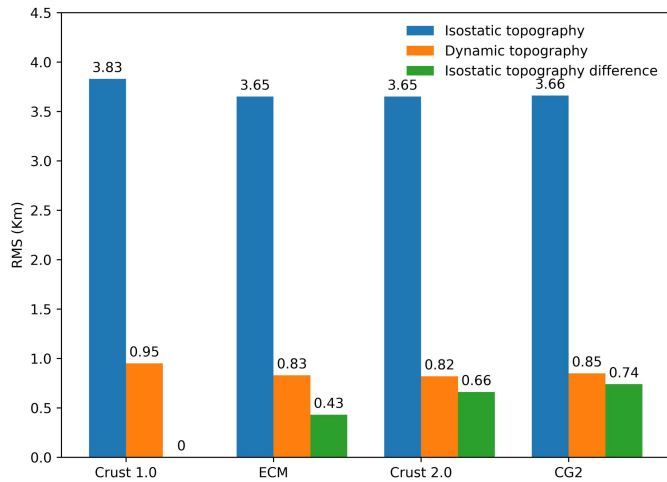
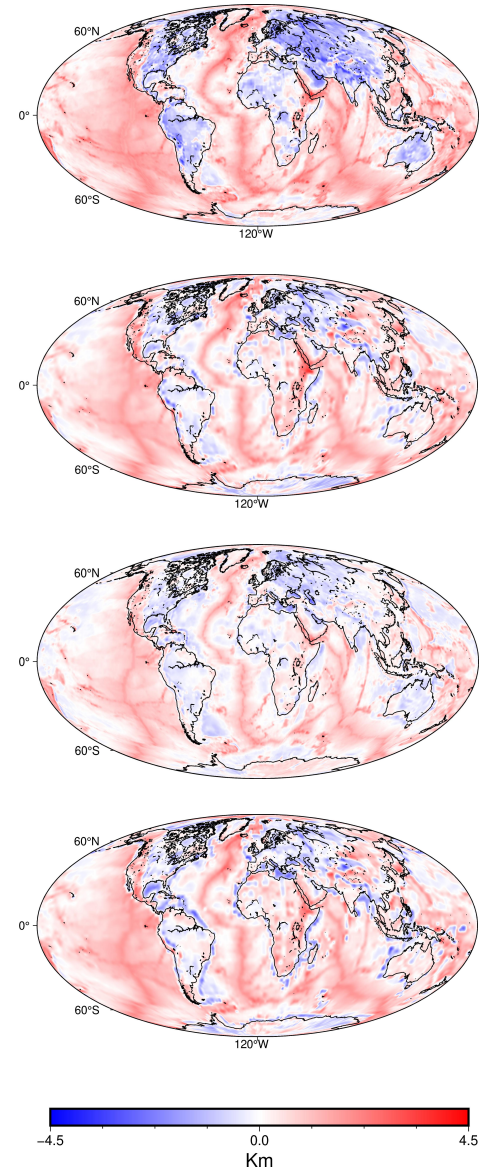
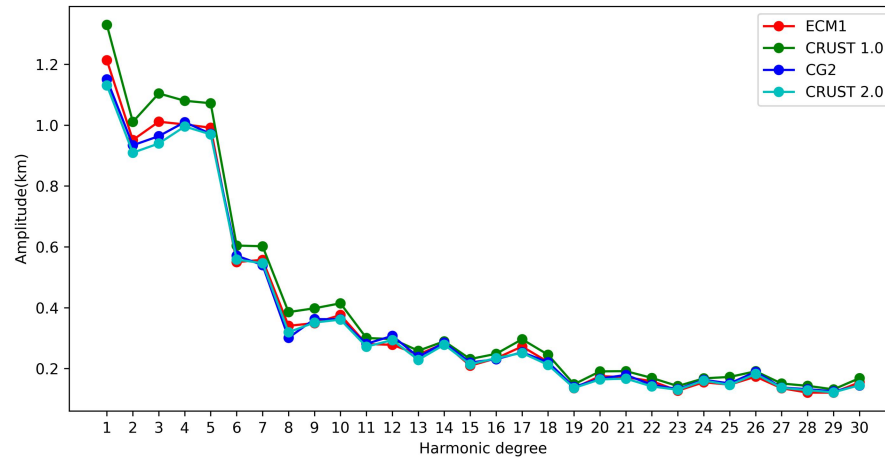


Residual topography

Dynamic topography

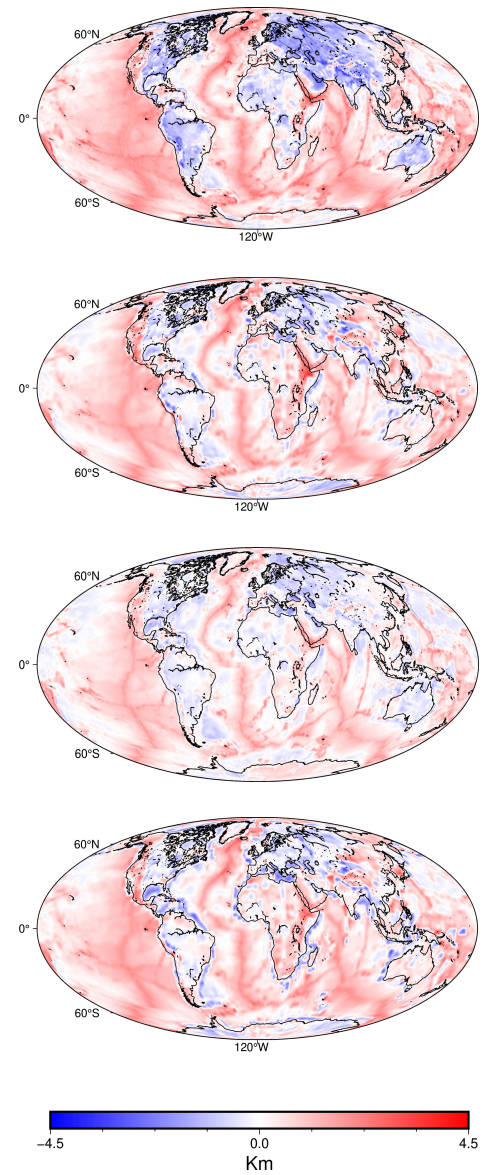
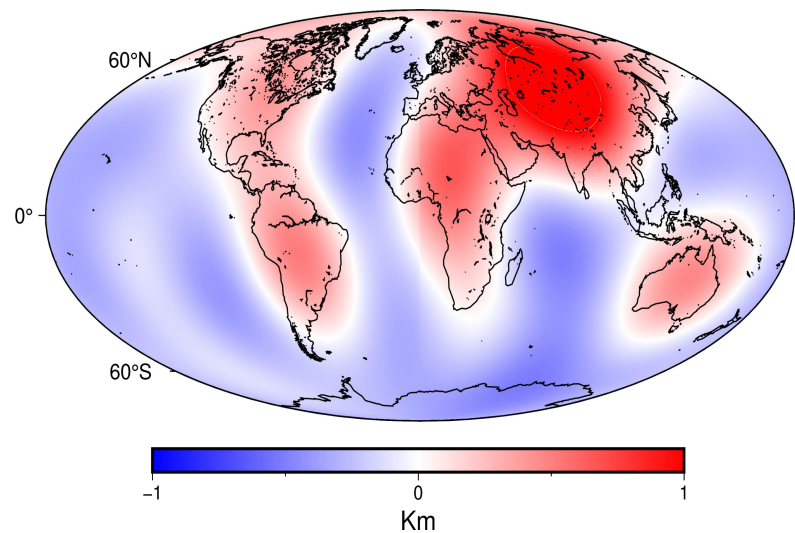
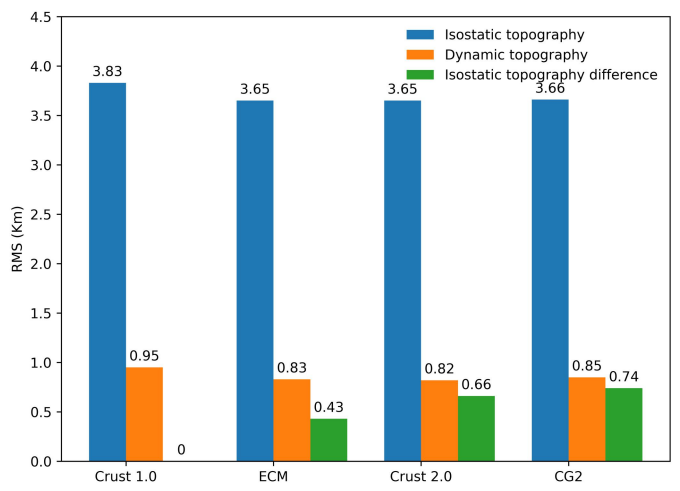
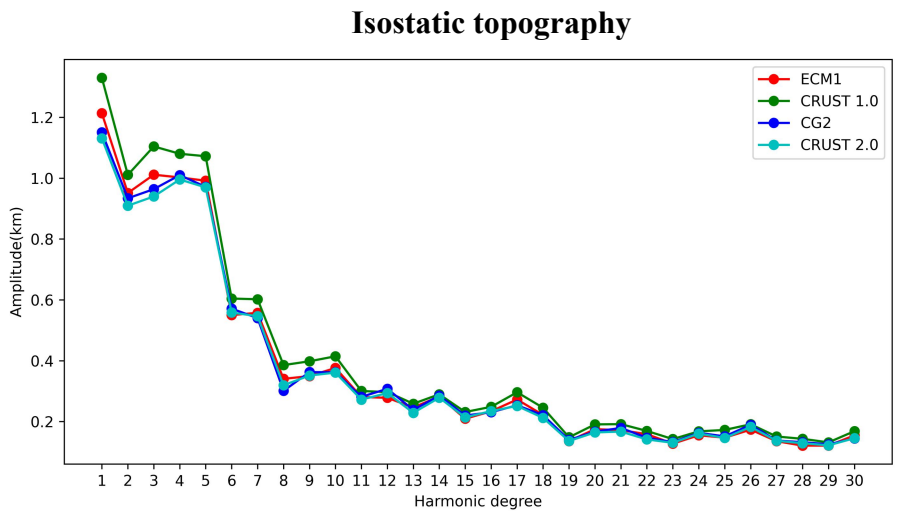
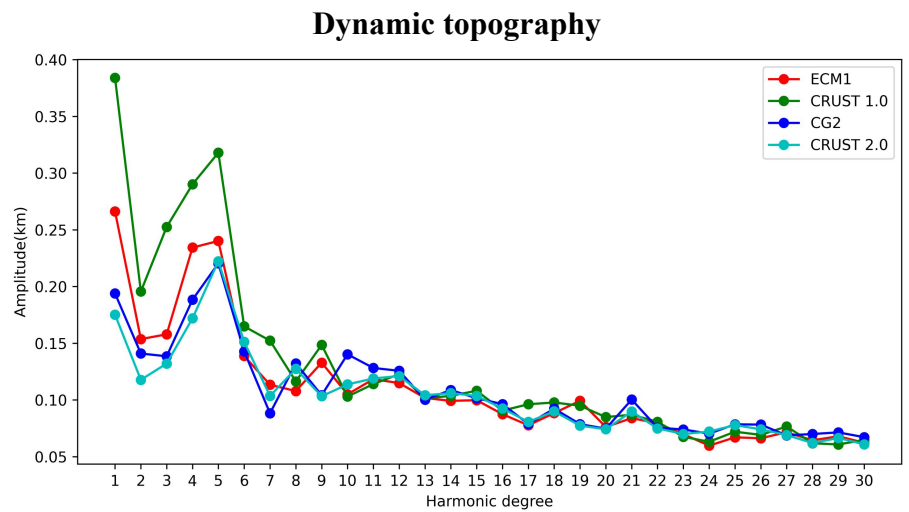


Isostatic topography



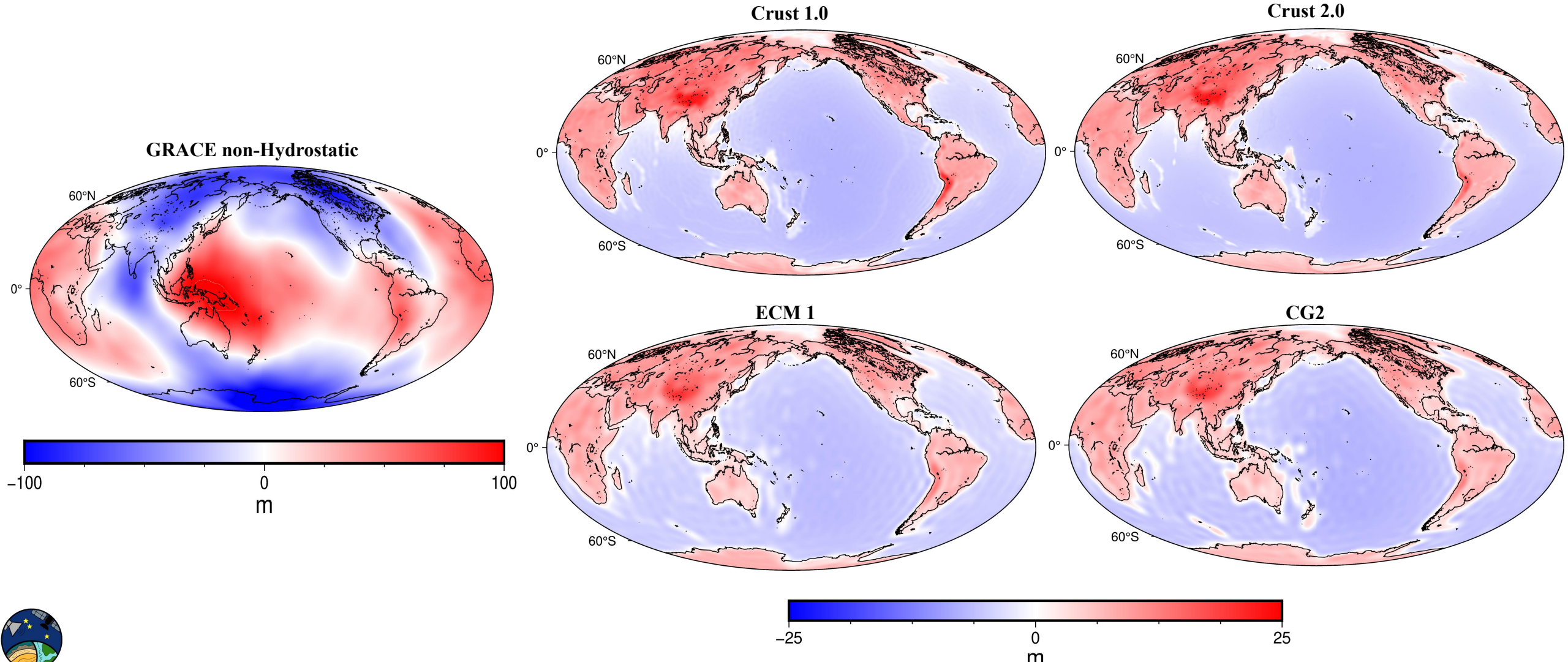


Residual topography



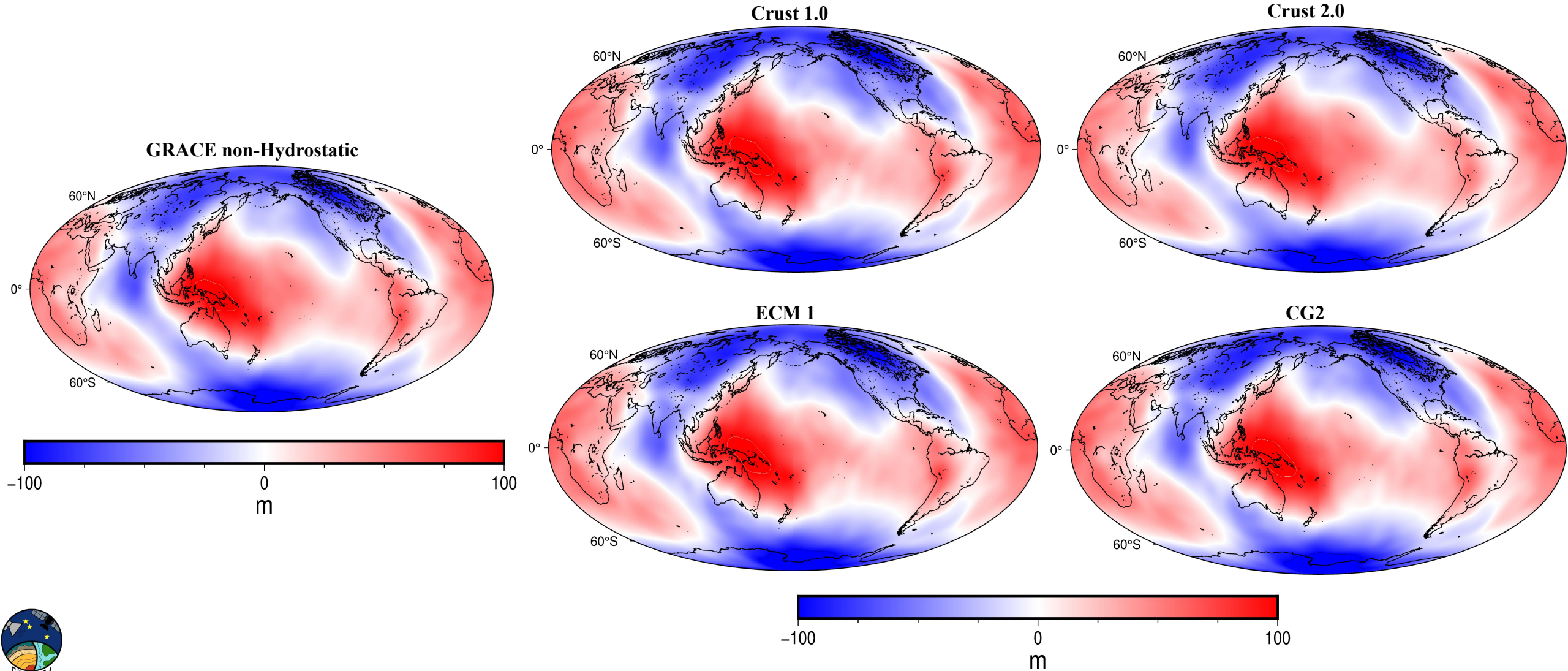


- Residual geoid





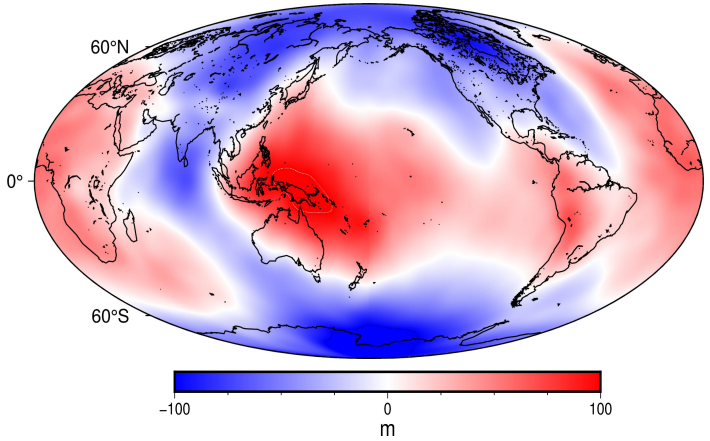
- Residual geoid



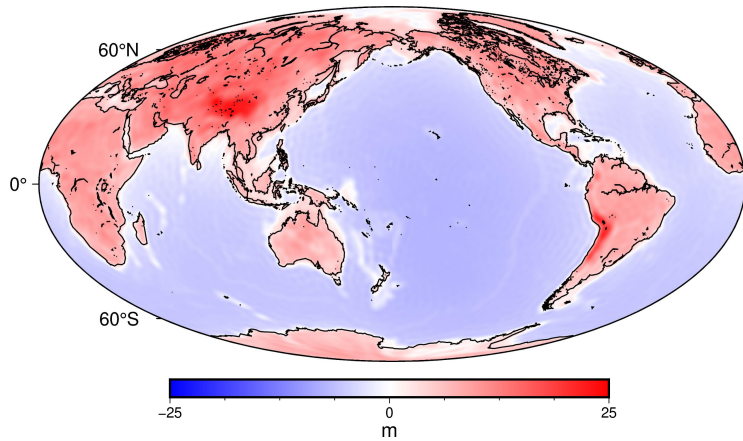


- Residual geoid

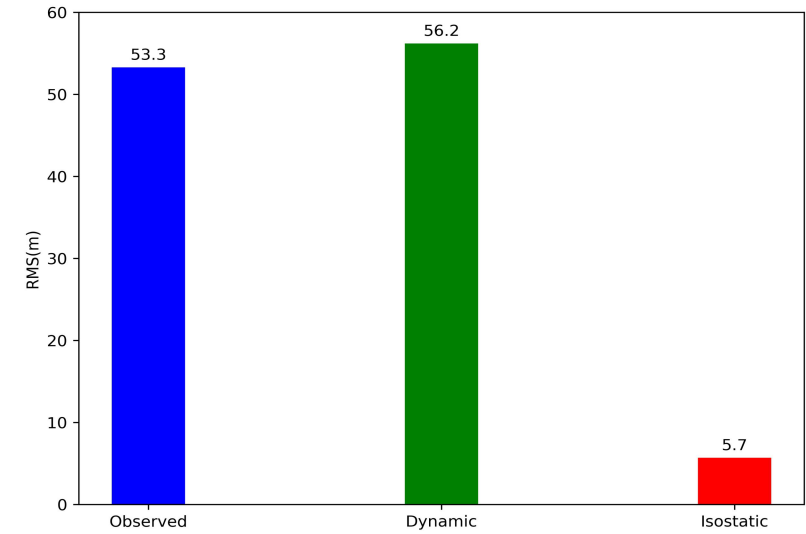
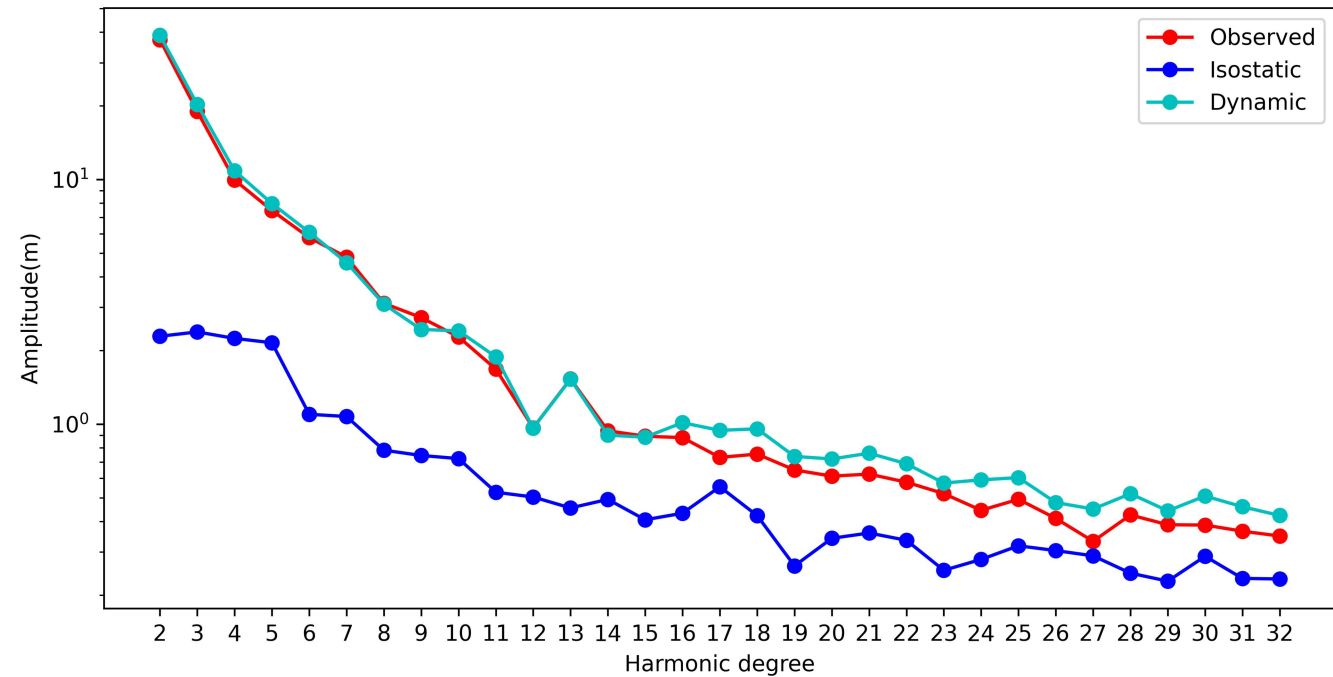
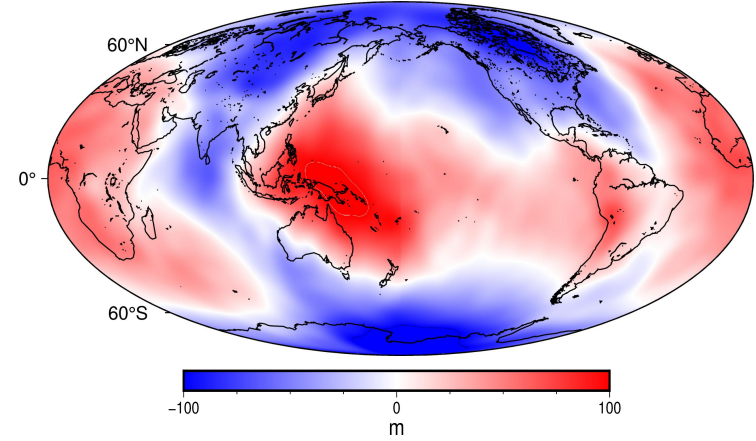
Observed



Isostatic



Dynamic





- **Geodynamically consistent approach**



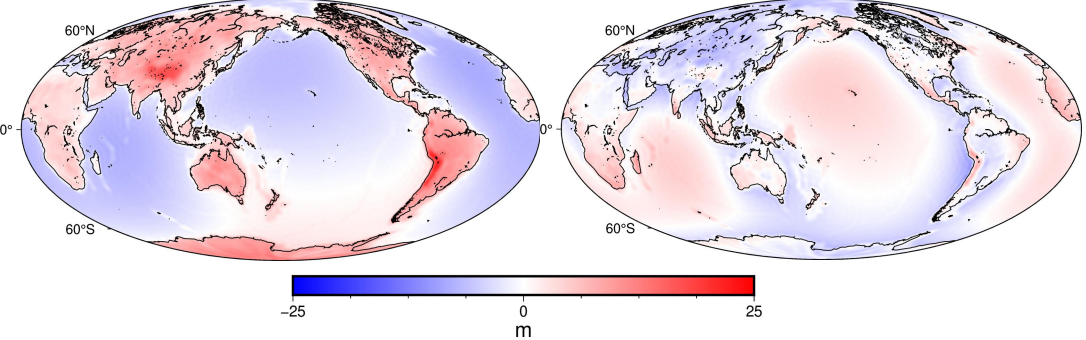
Simplification

- **Viscous**
- **Compressible**
- **Self-gravitating**

- **Geodynamically consistent approach**

No-slip BC

Free-slip BC



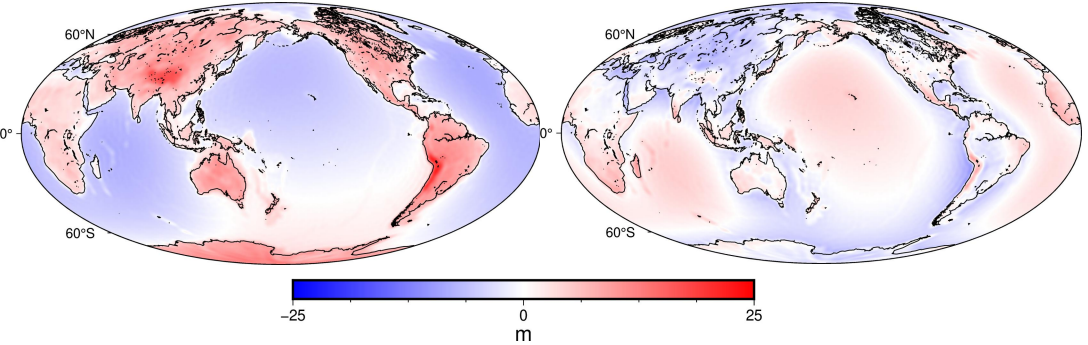
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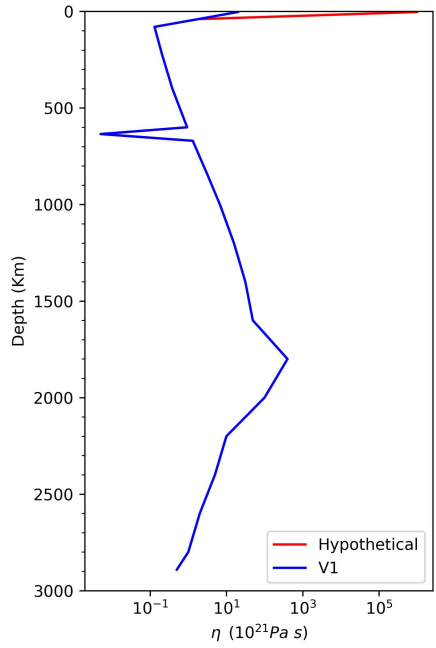
No-slip BC

Free-slip BC



Simplification

- Viscous
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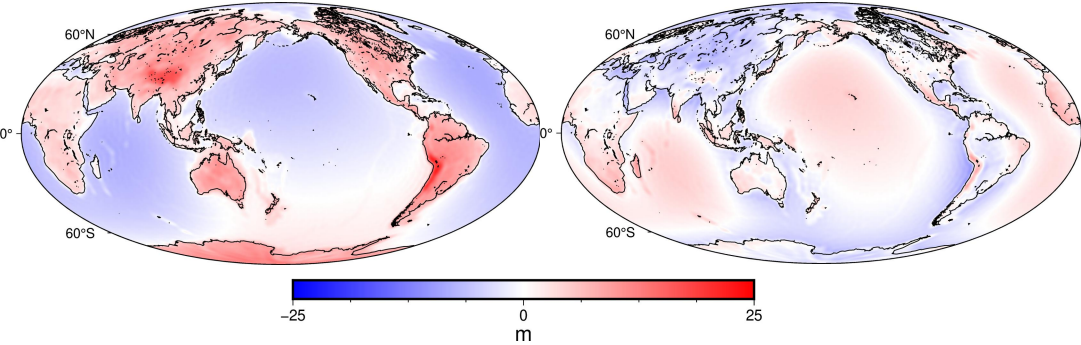




Geodynamically consistent approach

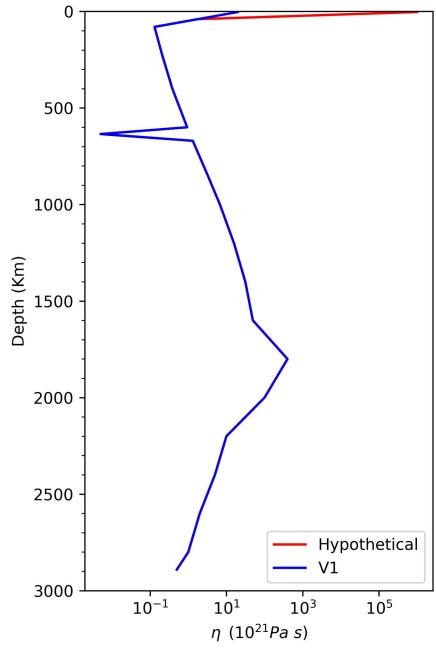
No-slip BC

Free-slip BC

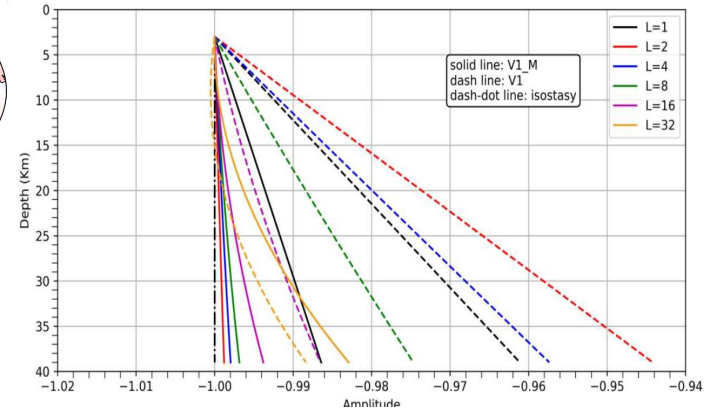


Simplification

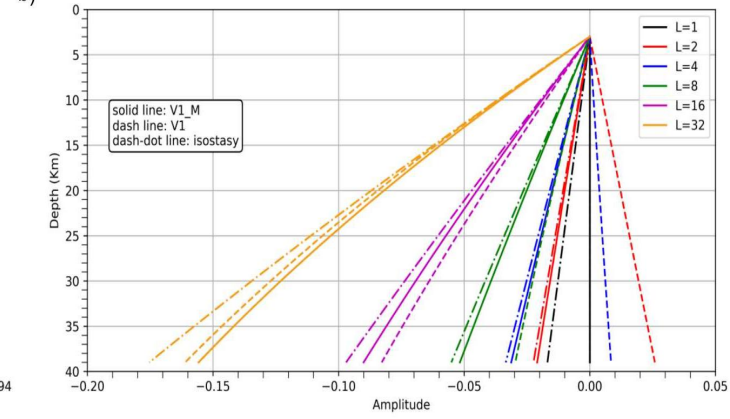
- Viscous
- Compressible
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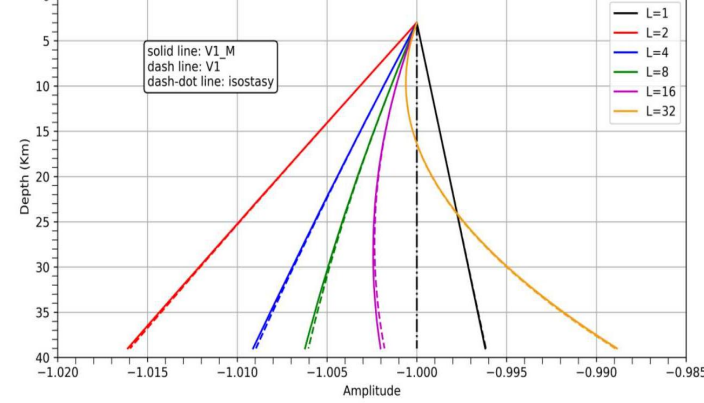
Topography kernels (Free-slip BC)



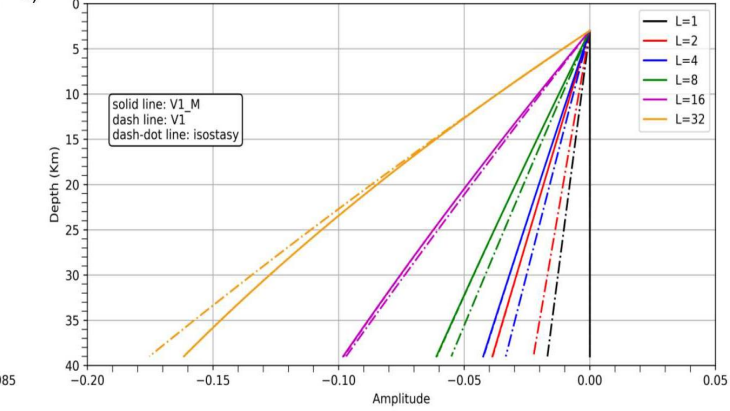
Geoid kernels (Free-slip BC)



Topography kernels (No-slip BC)



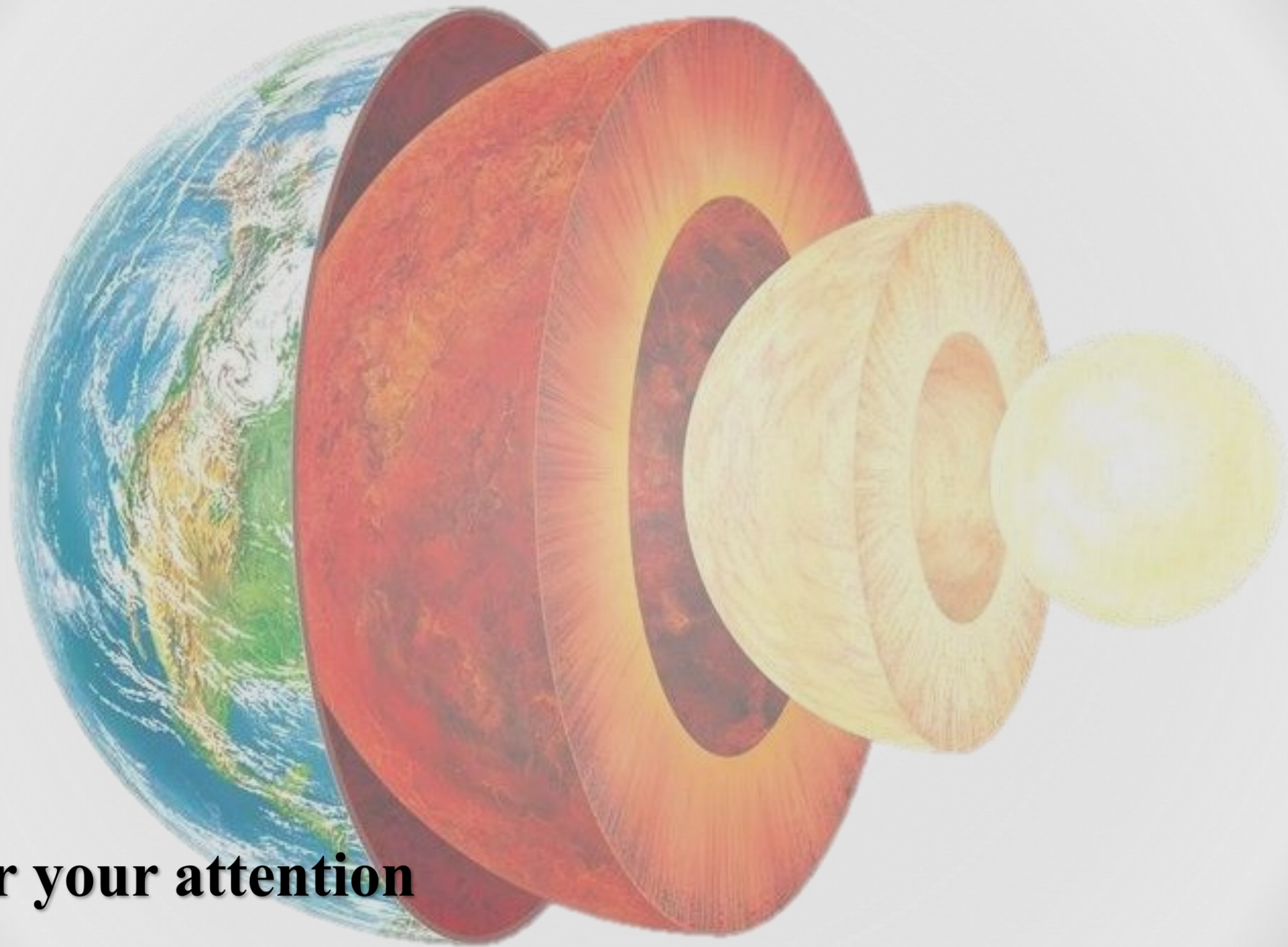
Geoid kernels (No-slip BC)





- Residual topography and geoid is a consequence of dynamic processes occurring within the mantle.
- Residual geoid is not identically zero, and it must be used in combination with topography as constraint on the mantle density heterogeneity.
- Residual topography uncertainty due to different crustal models has often been overlooked.
- Uncertainty in the multi-layer crustal models can lead to significant uncertainty ($\sim 50\%$) in the dynamic topography.
- Classic isostasy theory is a simplified model for mantle-crust system by ignoring mantle compressibility and self-gravitating.
- Geodynamically consistent approach, derived from viscous flow model, compensates to some extent the simplifications of the classical isostasy theory.





Thanks for your attention