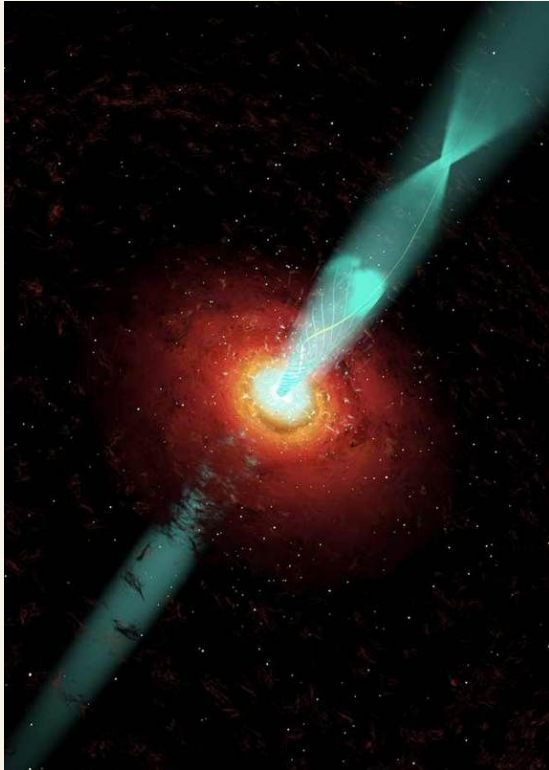


# Exploring the physical origin of blazar flares with a time-dependent one-zone model

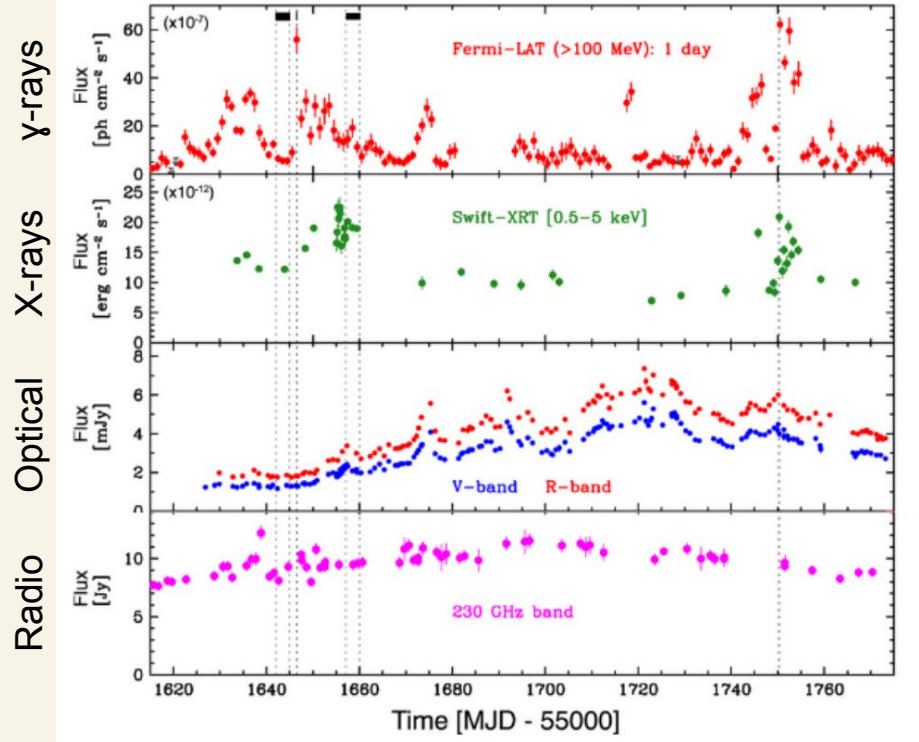
P. Thevenet, A. Zech, C. Boisson  
LUTH - Observatoire de Paris, PSL Université,  
Université Paris Cité, CNRS

Workshop on Numerical Multi-Messenger Modeling  
APC Laboratory, February 22nd 2024

# Introduction: blazar emission variability



Credit: Marscher  
et al., Wolfgang  
Steffen,  
NRAO/AUI/NSF

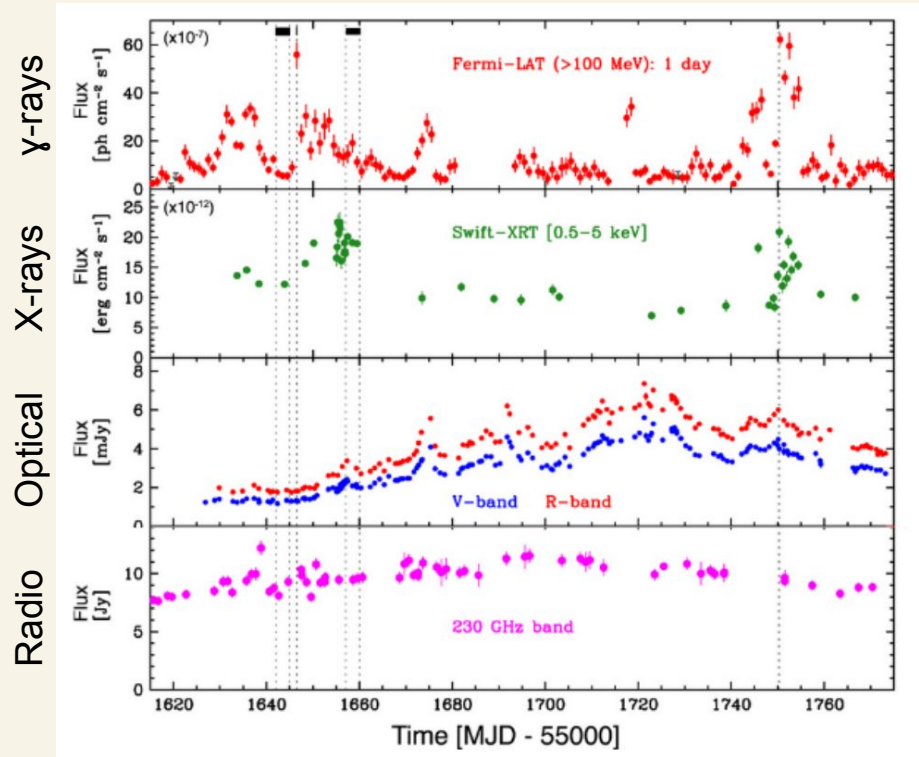


Example of multiwavelength (MWL) light curves of 3C 279 covering the 2013–2014 active period. Adapted from Hayashida et al. 2015

# Introduction: blazar emission variability

Problem: lack of a general picture of the physical origin of blazar flares

Objective: simulate isolated short-term blazar flares from different scenarios with a **leptonic single-zone SSC model** and identify characteristic signatures in the light curves



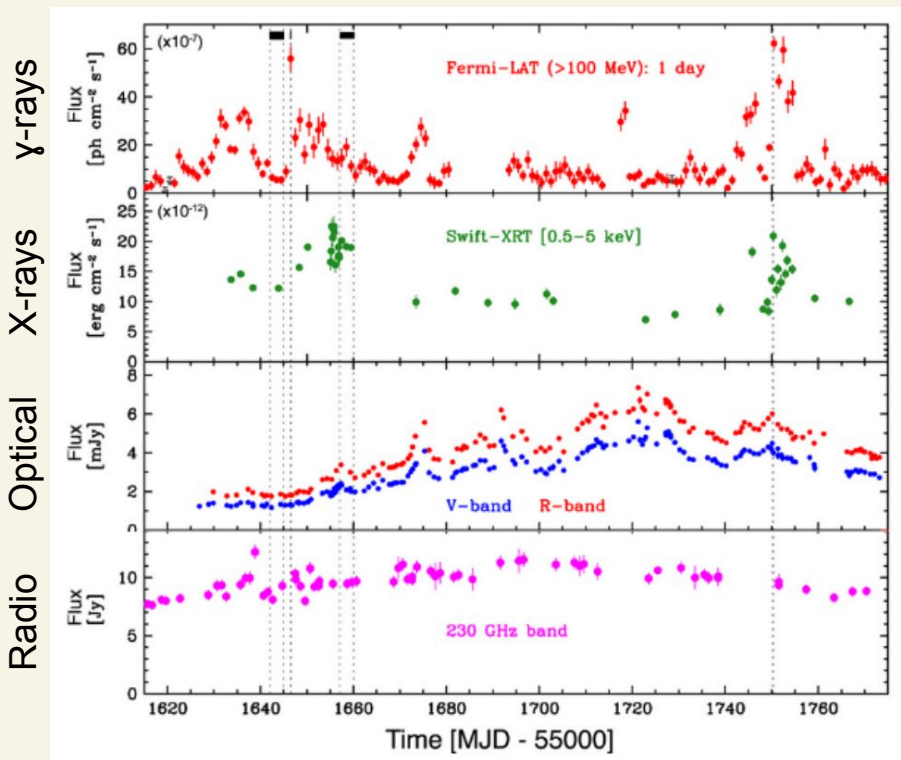
Example of multiwavelength (MWL) light curves of 3C 279 covering the 2013–2014 active period. Adapted from Hayashida et al. 2015

# Introduction: blazar emission variability

Problem: lack of a general picture of the physical origin of blazar flares

Objective: simulate isolated short-term blazar flares from different scenarios with a **leptonic single-zone SSC model** and identify characteristic signatures in the light curves

- Systematic study of particle injection/acceleration flares
- Comparison of different scenarios



Example of multiwavelength (MWL) light curves of 3C 279 covering the 2013–2014 active period. Adapted from Hayashida et al. 2015

# 1. Radiative model

Fokker-Planck equation solved in the EMBLEM code, Dmytriiev et al. (2021):

$$\frac{\partial N_e(\gamma, t)}{\partial t} = \frac{\partial}{\partial \gamma} \left[ \underbrace{(b_c(\gamma, t)\gamma^2 + \frac{1}{t_{ad}}\gamma - a(t)\gamma - \frac{2}{\gamma}D_{FII}(\gamma, t))}_{\text{Cooling terms}} N_e(\gamma, t) \right] + \frac{\partial}{\partial \gamma} \left( \underbrace{D_{FII}(\gamma, t)}_{\text{Acceleration terms}} \frac{\partial N_e(\gamma, t)}{\partial \gamma} \right) - \underbrace{N_e(\gamma, t) \left( \frac{1}{t_{esc}} + \frac{3}{t_{ad}} \right)}_{\text{Injection term}} + Q_{inj}(\gamma, t)$$

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## Cooling

- Synchrotron and Inverse Compton:  $b_c(\gamma, t)$
- Adiabatic expansion:  $t_{ad}(t) = \frac{R(t)}{\beta_{exp}c}$
- Escape:  $t_{esc}^{(turb)} = \left(\frac{R_t}{c}\right)^2 \left(\frac{\delta B}{B}\right)^2 \frac{c}{\lambda_{max}} \left(\frac{r_L}{\lambda_{max}}\right)^{q-2}$

## Acceleration

- Fermi I: injection with time-dependent maximum Lorentz factor
  - Fermi II:  $D_{FII}(\gamma, t) = \frac{p^2}{t_{FII}}$
- $$t_{FII} = \frac{1}{\beta_A^2} \left(\frac{\delta B}{B}\right)^{-2} \frac{\lambda_{max}}{c} \left(\frac{r_L}{\lambda_{max}}\right)^{2-q}$$



## 2. Scenarios studied

Quiescent steady-state injection:

$$Q_{inj}(\gamma) = N_{inj} \left( \frac{\gamma}{\gamma_{inj,pivot}} \right)^{\alpha_{inj}} \exp \left( -\frac{\gamma}{\gamma_{inj,cut}} \right)$$

Parameter	Variable	Value	Unit
Source			
Initial magnetic field	$B_0$	0.04	Gauss
Initial blob radius	$R_0$	2.8e16	cm
Blob Doppler factor	$\delta$	29	-
Redshift	$z$	0.0308	-
Continuous injection spectrum			
Spectrum normalization	$N_{inj}$	1.86e-14	$\text{cm}^{-3}\text{s}^{-1}$
Spectrum slope	$\alpha_{inj}$	-2.23	-
Pivot Lorentz factor	$\gamma_{inj,pivot}$	1.0e5	-
Cutoff Lorentz factor	$\gamma_{inj,cut}$	5.8e5	-
Minimal injected Lorentz factor	$\gamma_{inj,min}$	800	-

Parameters based on the study of Mrk421,  
Dmytriiev et al. (2021)

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Dmytriiev et al. (2021)

Flares resulting from a perturbation of the steady-state:

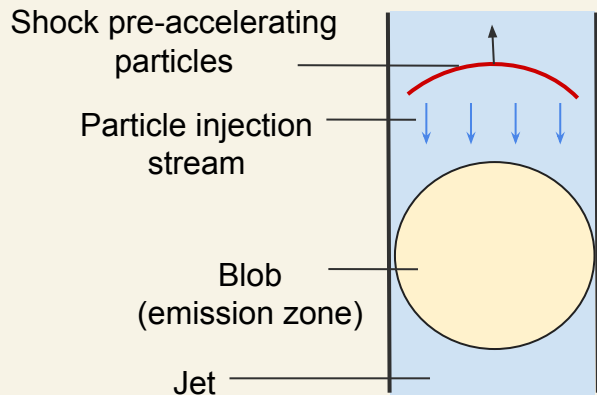
- Simple particle injection
- Particle injection and adiabatic expansion
- Diffusive shock acceleration (Fermi I)
- Stochastic acceleration (Fermi II)



## 2. Scenarios studied: simple particle injection

Power law with exponential cutoff:

$$Q_{add}(\gamma) = N_{add} \left( \frac{\gamma}{\gamma_{add,pivot}} \right)^{\alpha_{add}} \exp \left( -\frac{\gamma}{\gamma_{add,cut}} \right)$$



→ We vary the additional injection rate

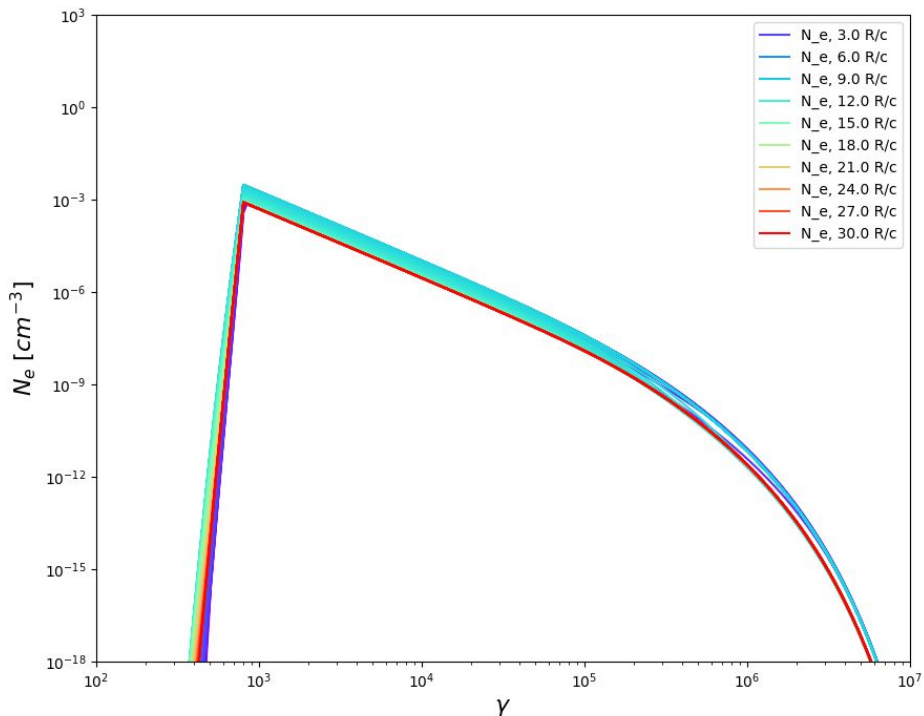
Flaring injection spectrum			
Spectrum slope	$\alpha_{add}$	-2.23	-
Pivot Lorentz factor	$\gamma_{add,pivot}$	1.0e5	-
Cutoff Lorentz factor	$\gamma_{add,cut}$	5.8e5	-
Minimal injected Lorentz factor	$\gamma_{add,min}$	800	-

Parameters of the flaring injection phase

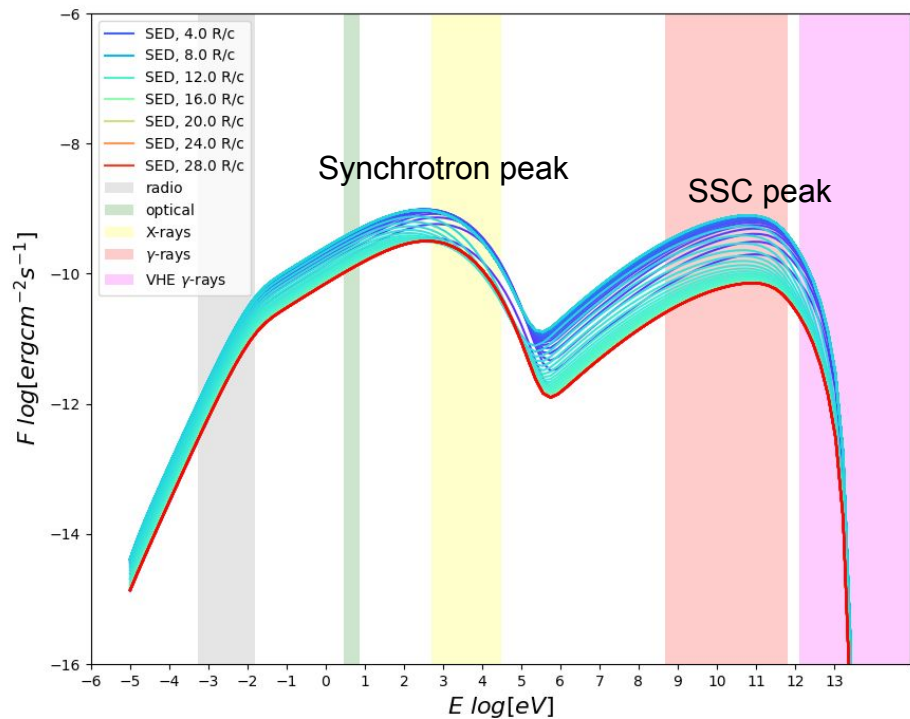
Sketch of a one-zone flaring scenario by particle injection

## 2. Scenarios studied: simple particle injection

Electron Distribution

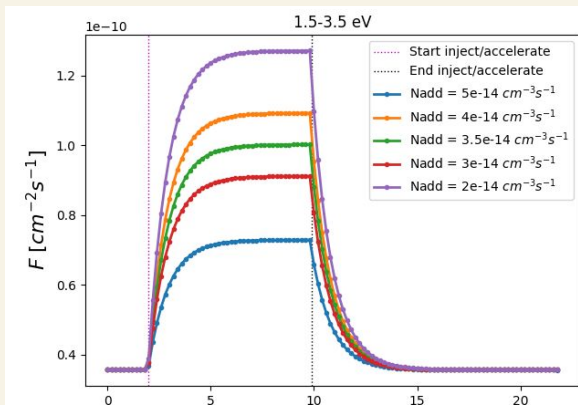


Spectral Energy Distribution (SED)

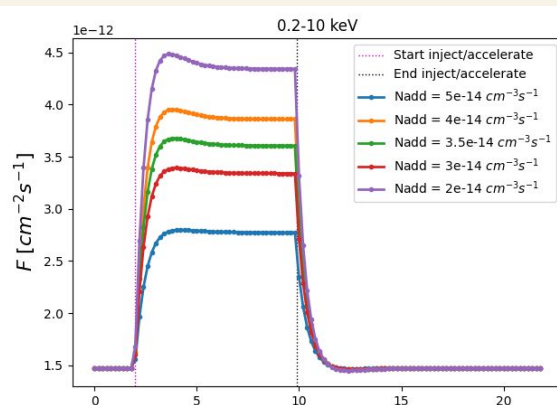


## 2. Scenarios studied: simple particle injection

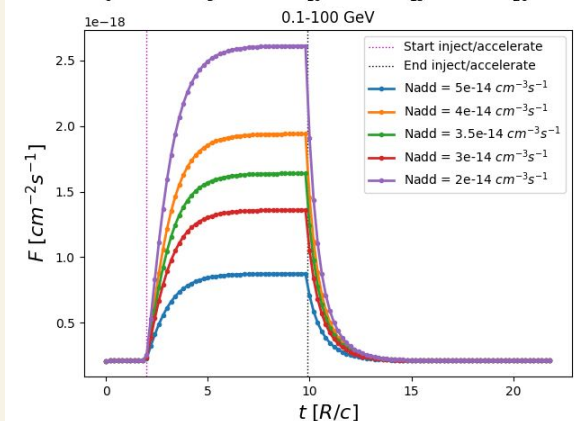
Optical



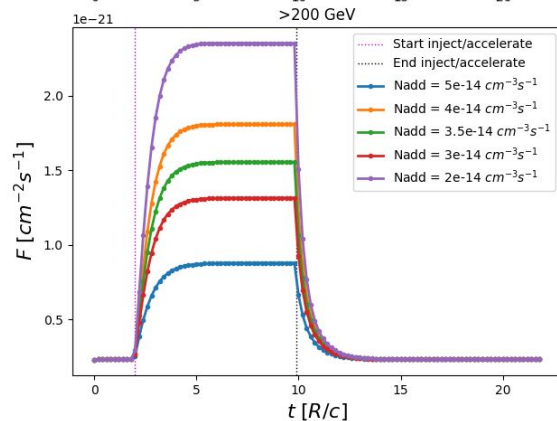
X-rays



$\gamma$ -rays



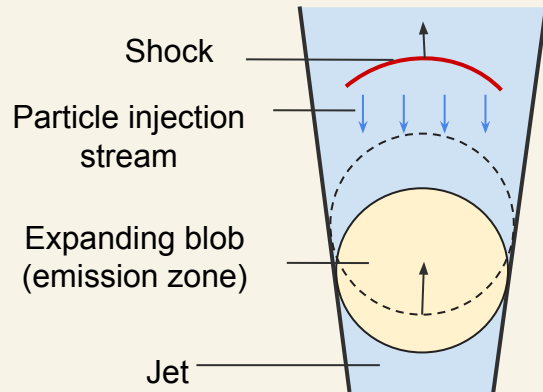
VHE  $\gamma$ -rays



## 2. Scenarios studied: injection and adiabatic expansion

Power law with exponential cutoff: 
$$Q_{add}(\gamma) = N_{add} \left( \frac{\gamma}{\gamma_{add,pivot}} \right)^{\alpha_{add}} \exp \left( -\frac{\gamma}{\gamma_{add,cut}} \right)$$

Intrinsic opening angle of the jet leading to the blob's adiabatic expansion, Tramacere et al. (2022):



$$t_{ad}(t) = \frac{R(t)}{\beta_{exp}c}$$

$$\beta_{exp} = \beta_{jet} \tan(\alpha)$$

Opening angle from best-fit value  $\rho=0.26$  rad based on VLBI observations, Pushkarev et al. (2009)

$$\alpha = \rho/\Gamma$$

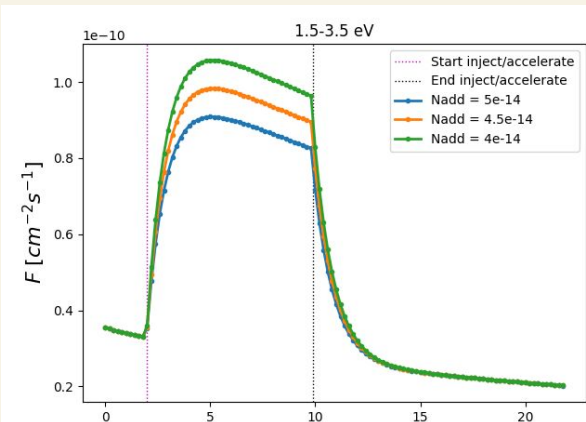
Chosen opening angle:  $\alpha \approx 0.44^\circ$

→ We vary the additional injection rate

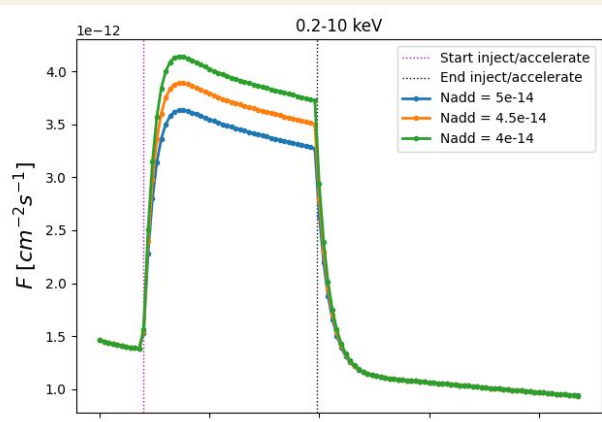
Sketch of a one-zone flaring scenario by particle injection with adiabatic expansion

## 2. Scenarios studied: injection and adiabatic expansion

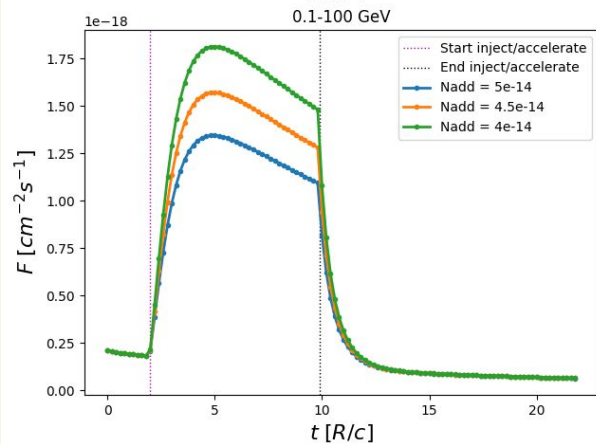
Optical



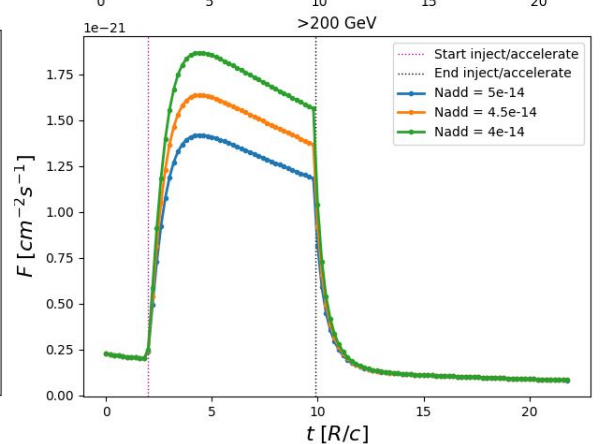
X-rays



$\gamma$ -rays



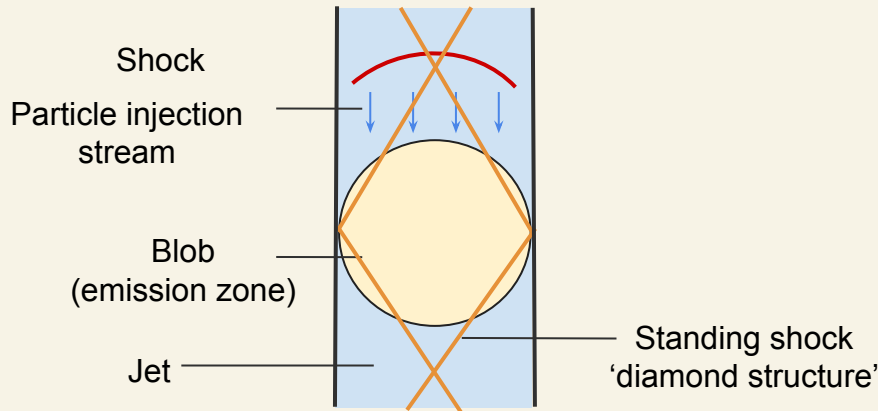
VHE  $\gamma$ -rays



## 2. Scenarios studied: Fermi I acceleration

Equivalent to an additional injection, Kirk et al. (1998):

- Power law with exponential cutoff
- Time-dependent cutoff and maximum Lorentz factor



$$Q_{add}(\gamma) = N_{add} \left( \frac{\gamma}{\gamma_{add,pivot}} \right)^{\alpha_{add}} \exp \left( -\frac{\gamma}{\gamma_{add,cut}} \right)$$
$$\gamma_{add,cut} = \left[ \frac{1}{t_{max}} + \left( \frac{1}{\gamma_{add,min}} - \frac{1}{\gamma_{max}} \right) e^{-t/t_{shock}} \right]^{-1}$$

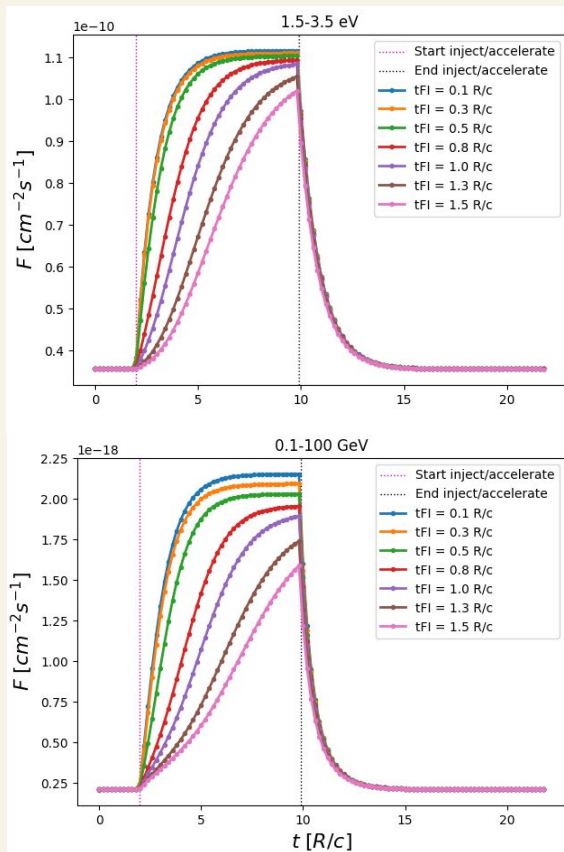
$$\gamma_{max} = (\beta_s t_{shock})^{-1}$$
$$\beta_s = \frac{4\sigma_T}{3m_e c} \left( \frac{B^2}{2\mu_0} \right)$$

- Fixed injection rate
- We vary the shock timescale

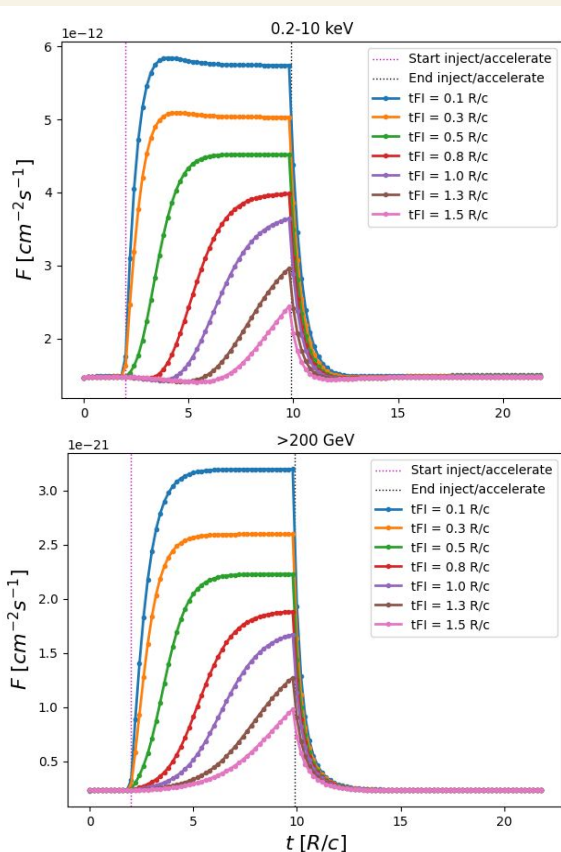
Sketch of a one-zone flaring scenario by Fermi I acceleration

## 2. Scenarios studied: Fermi I acceleration

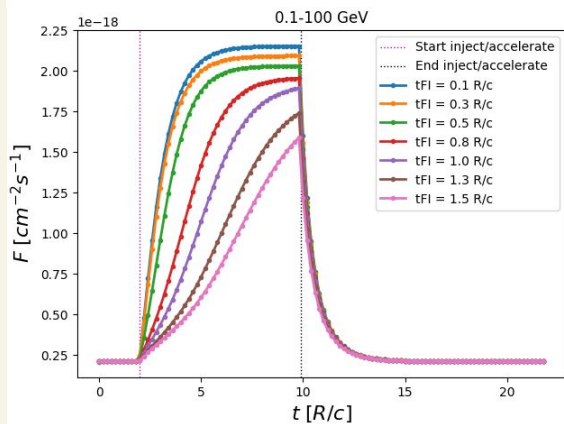
Optical



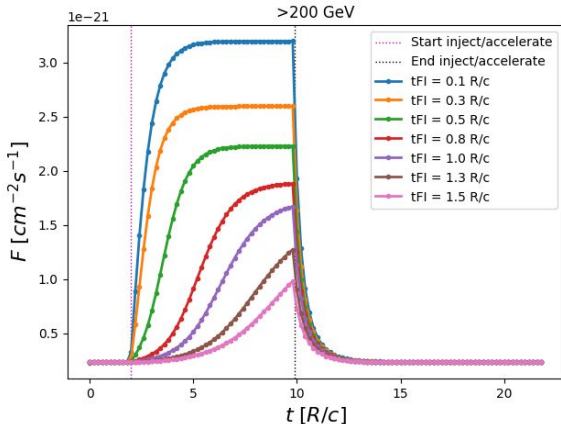
X-rays



$\gamma$ -rays



VHE  $\gamma$ -rays



⇒ Different rise and plateau times, shift in peak maximum with the acceleration timescale



## 2. Scenarios studied: Fermi II acceleration

We study three turbulence regimes:

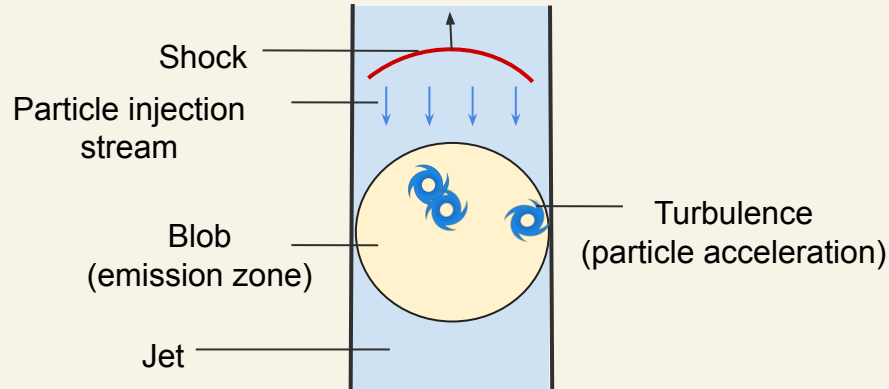
- Hard-sphere:  $q=2$
- Kolmogorov:  $q=5/3$
- Kraichnan:  $q=3/2$

Escape  
timescale

$$t_{esc}^{(turb)} = \left(\frac{R_t}{c}\right)^2 \left(\frac{\delta B}{B}\right)^2 \frac{c}{\lambda_{max}} \left(\frac{r_L}{\lambda_{max}}\right)^{q-2}$$

Acceleration  
timescale

$$t_{FII} = \frac{1}{\beta_A^2} \left(\frac{\delta B}{B}\right)^{-2} \frac{\lambda_{max}}{c} \left(\frac{r_L}{\lambda_{max}}\right)^{2-q}$$



Constraints on the parameters:

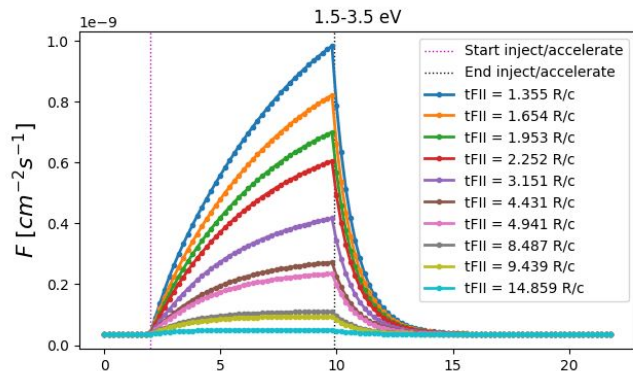
$$r_L < \lambda_{max} < R$$

$$0 < \frac{\delta B}{B} < 1$$

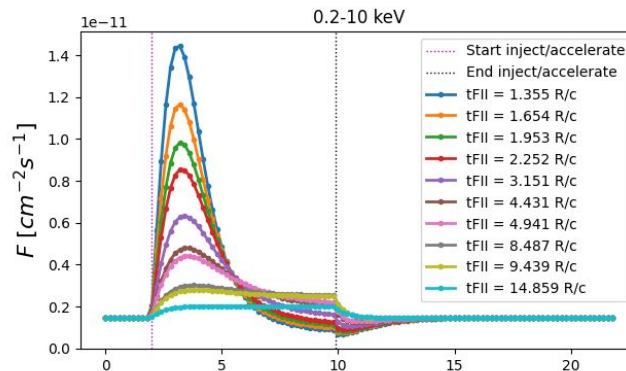
Sketch of a one-zone flaring scenario by Fermi II acceleration

## 2. Scenarios studied: hard-sphere Fermi II acceleration

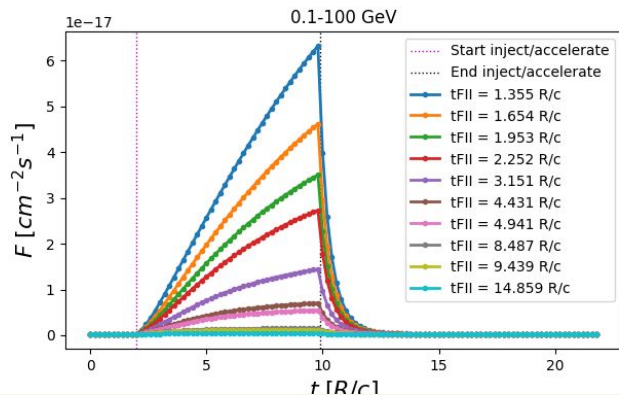
Optical



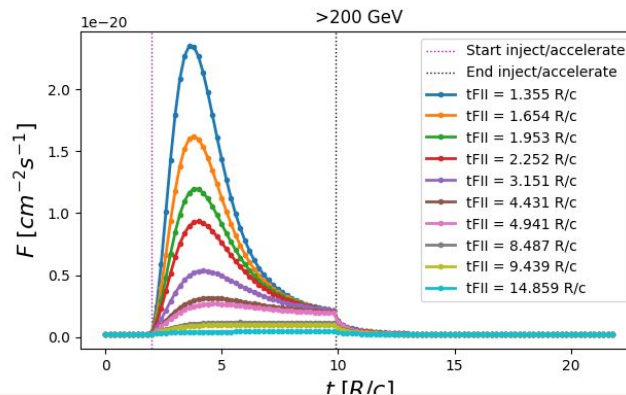
X-rays



$\gamma$ -rays



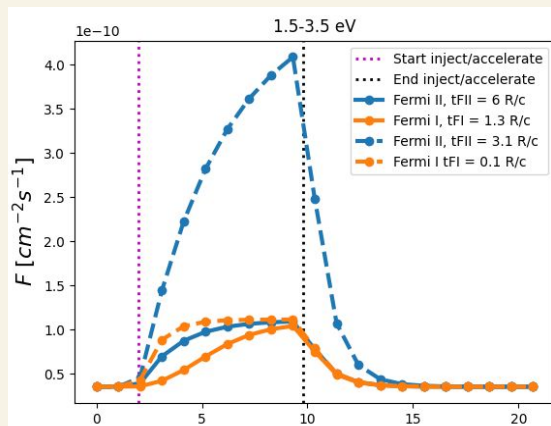
VHE  $\gamma$ -rays



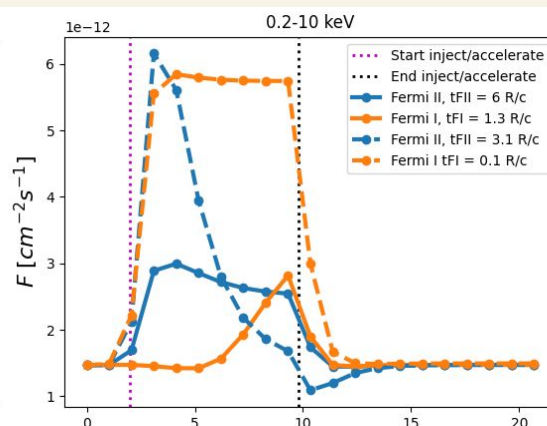
⇒ Shift of the peak maximum and peak time with the acceleration timescale

# 3. Comparison: Fermi I and Fermi II acceleration

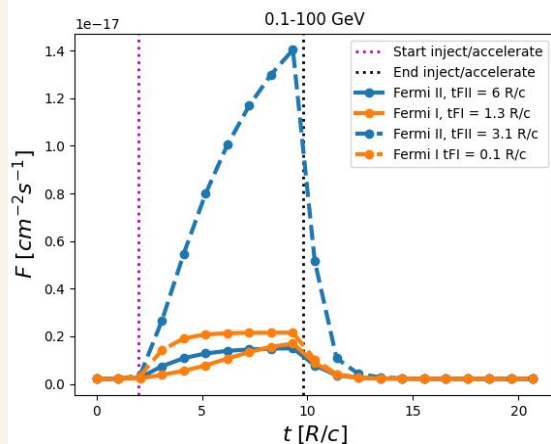
Optical



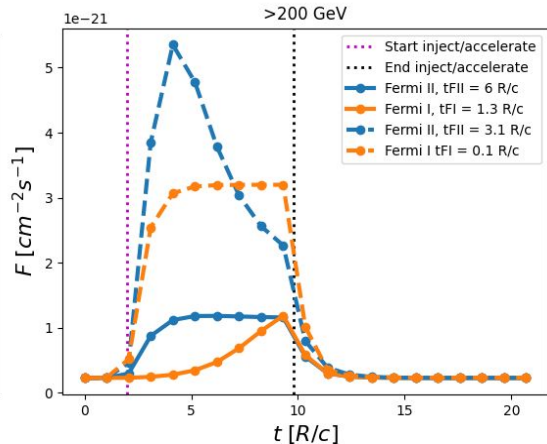
X-rays



$\gamma$ -rays



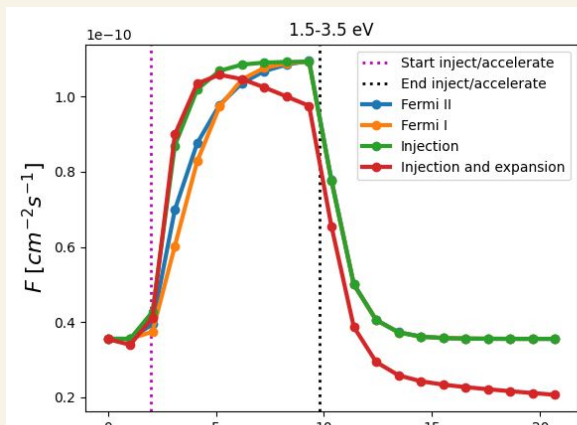
VHE  $\gamma$ -rays



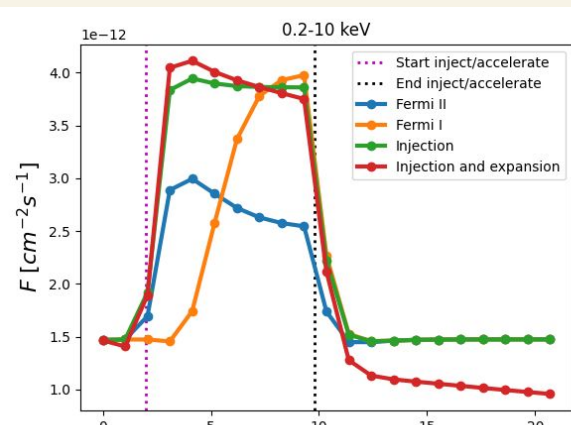
⇒ Differences in asymmetry, variability amplitude, rise and plateau times

# 3. Comparison: all four scenarios

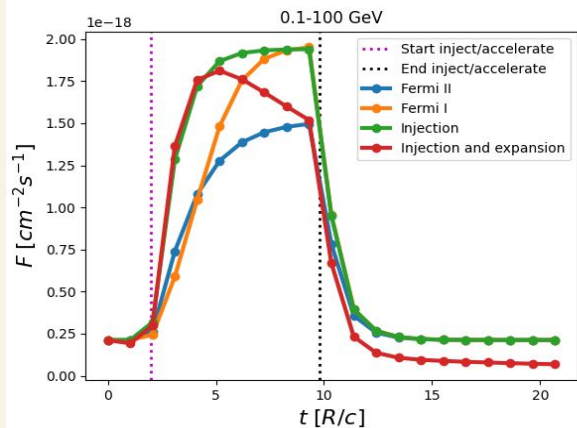
Optical



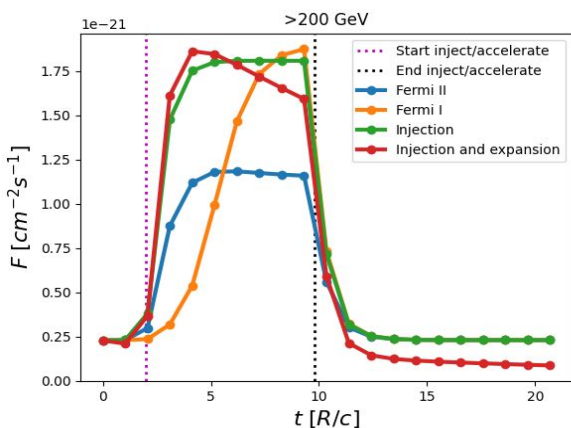
X-rays



$\gamma$ -rays



VHE  $\gamma$ -rays



$\Rightarrow$  Differences in asymmetry, plateau reaching time, variability amplitude

# Conclusion

- Recognizable patterns between flares by injection, injection and expansion, Fermi I and Fermi II acceleration using different energy bands:  
Rise time, relative variability amplitude, asymmetry, possible plateau phases
- Short timescale Fermi II flares → high Compton dominance flares described without external photon field
- Kolmogorov and Kraichnan turbulence: same flare shapes as in the high Compton dominance hard-sphere regime

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## Outlook:

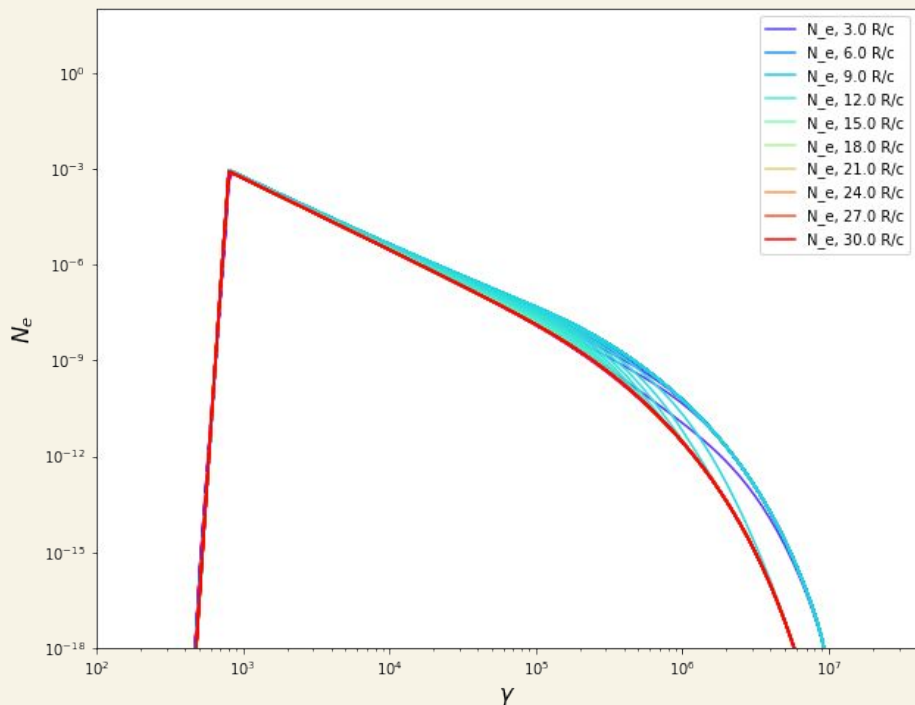
- Compare the observed behaviour with SEDs in the Thomson regime
- Determine a method to constrain the emission mechanism of observed MWL rapid flares
- Simulate LCs including external photon fields

Extra slides

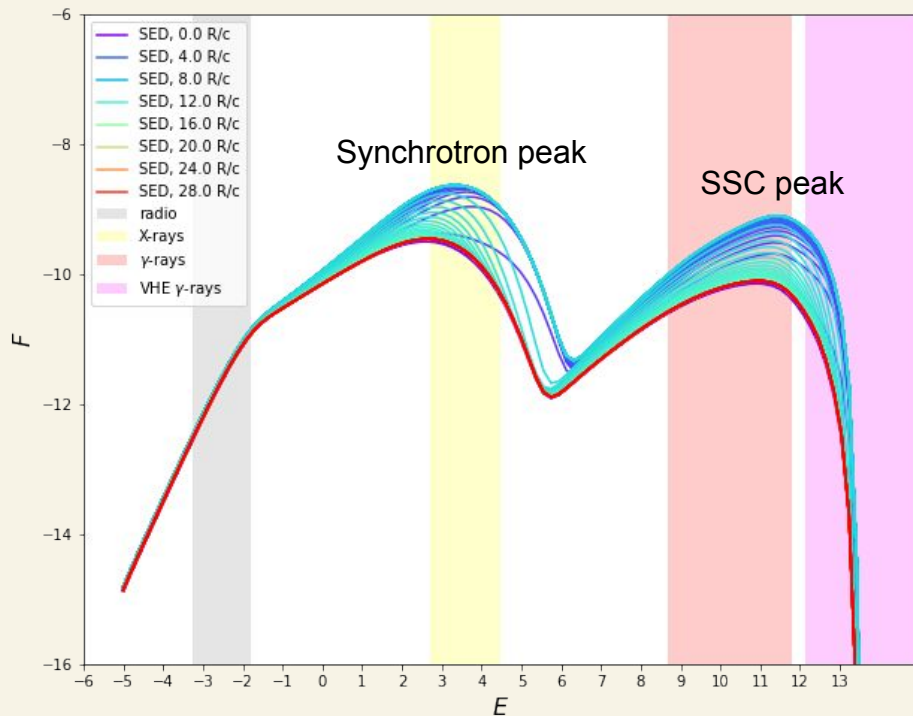


## 2. Extra - Different flaring spectrum injection

Electron Distribution

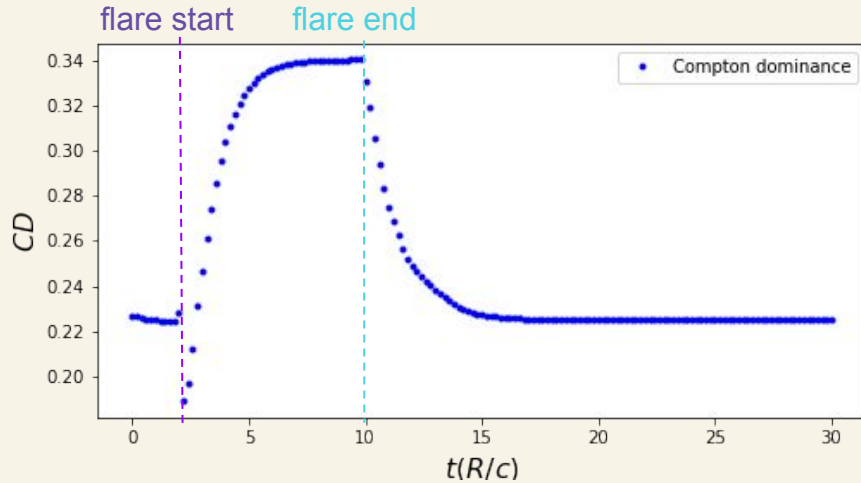


Spectral Energy Distribution (SED)

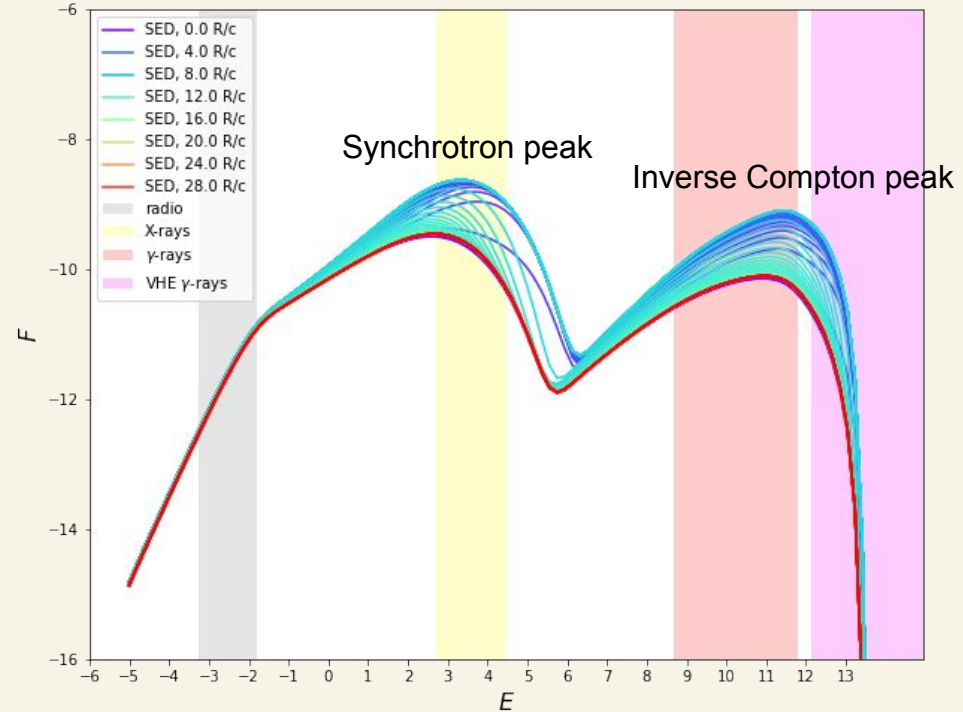


# Extra - Particle injection

Compton dominance: ratio of the flux at the IC peak to the flux at the Synchrotron peak

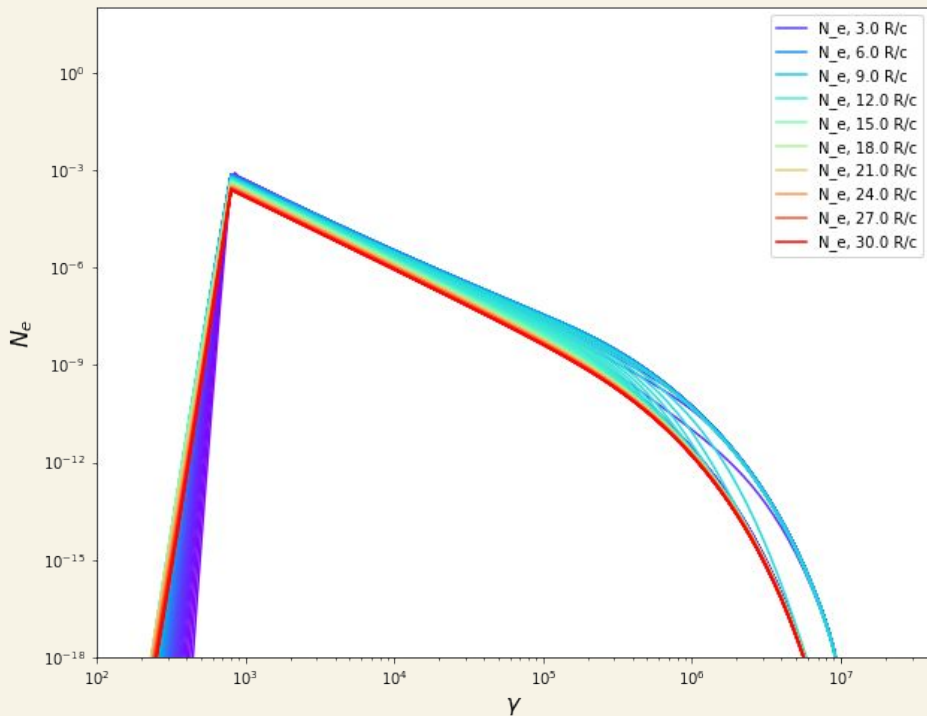


## Spectral Energy Distribution

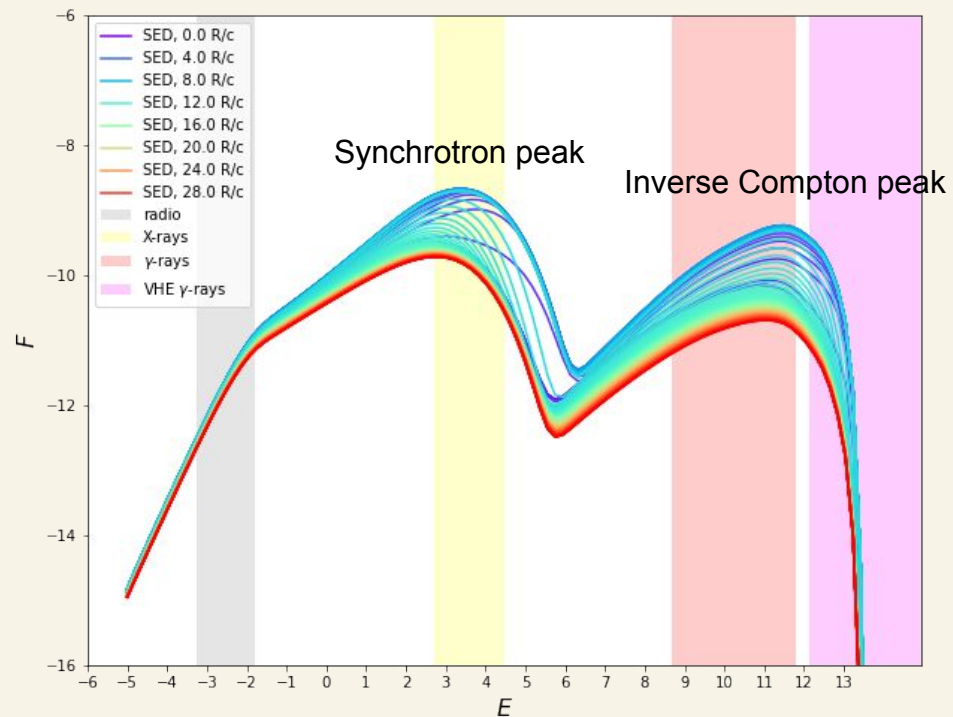


# Extra - Injection with adiabatic expansion

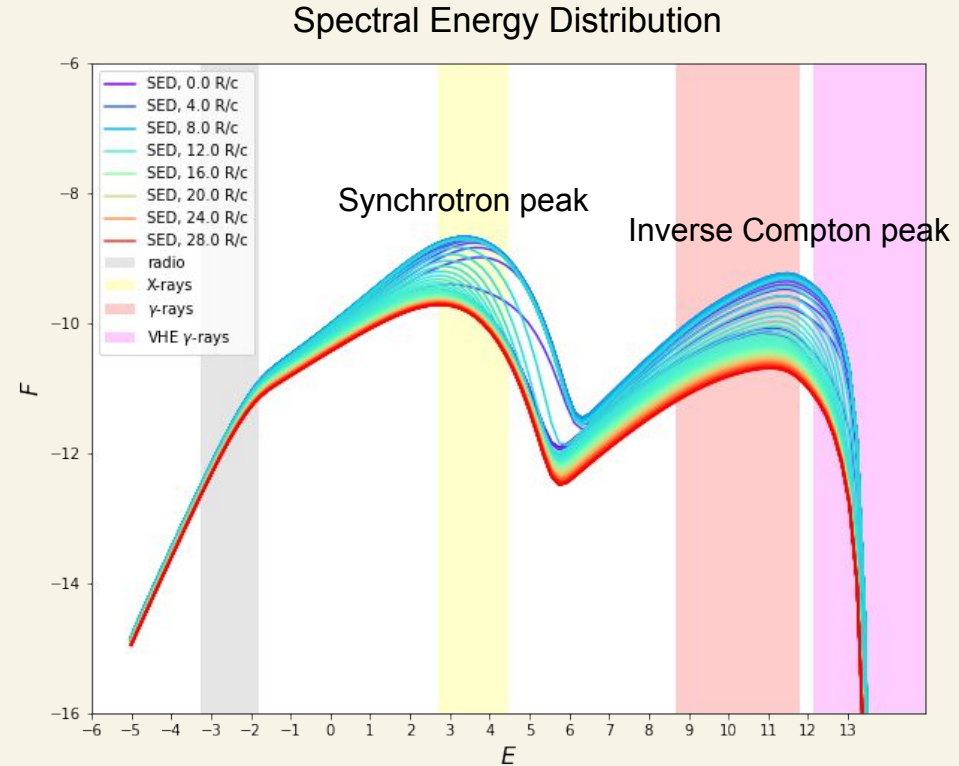
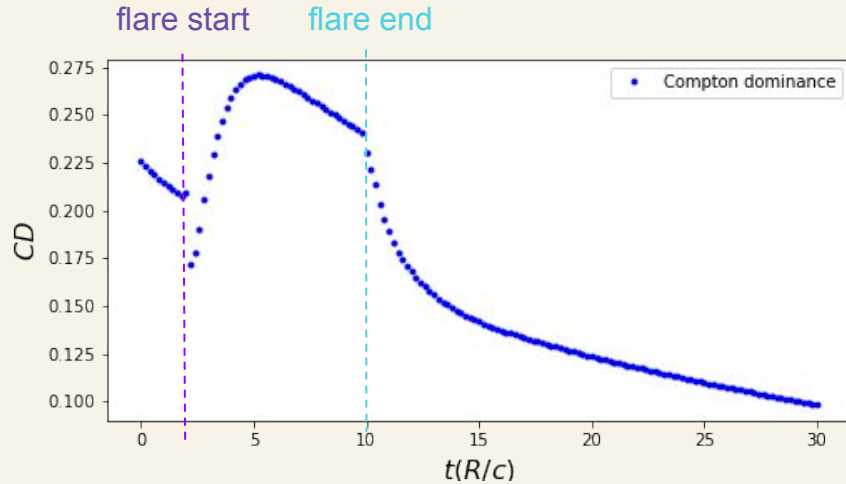
Electron Distribution



Spectral Energy Distribution

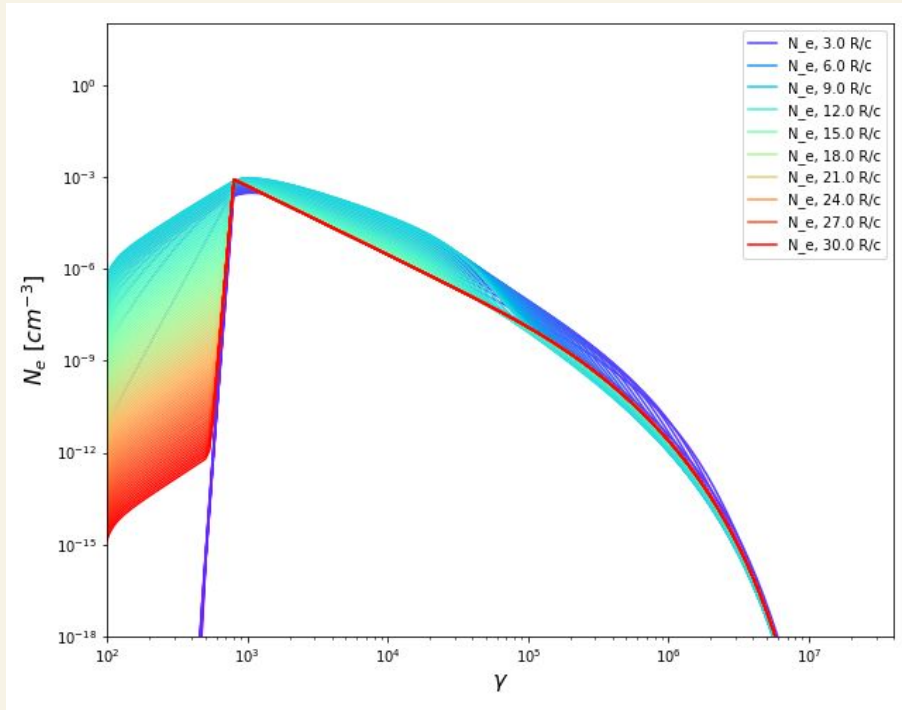


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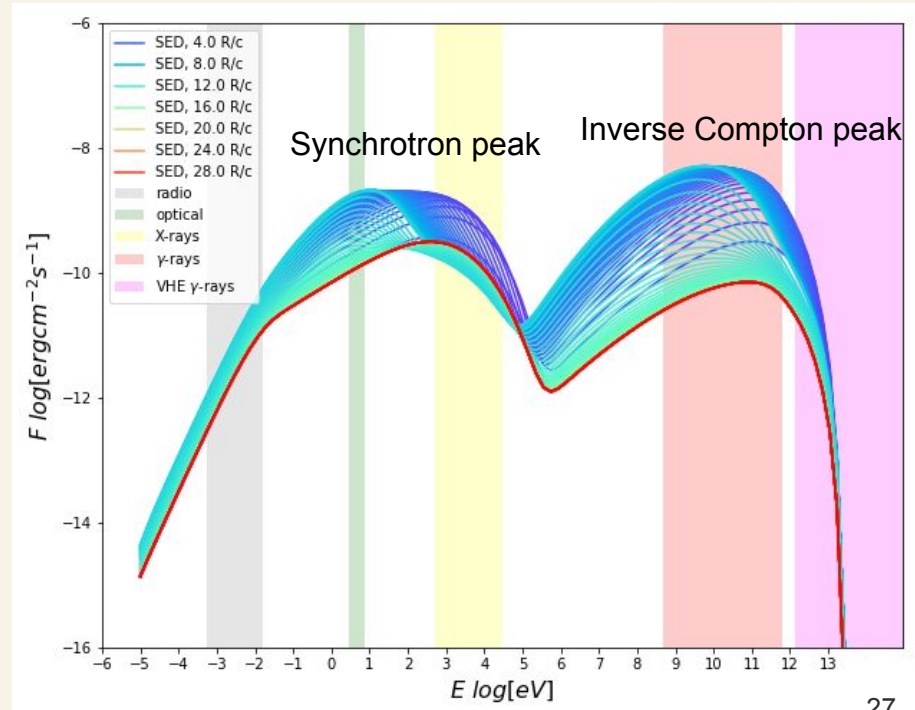


# Extra - Fermi II acceleration: hard-sphere regime

Electron Distribution



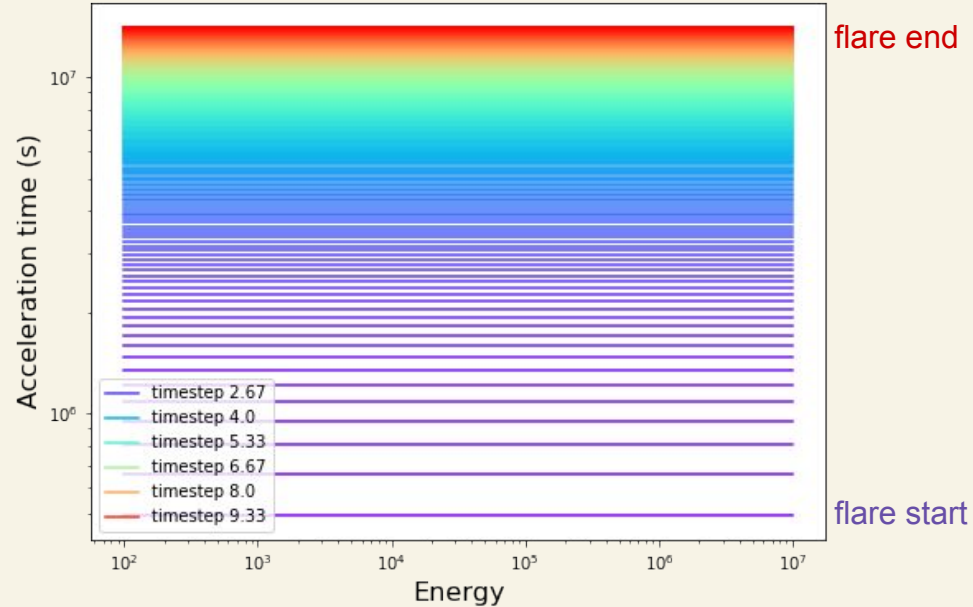
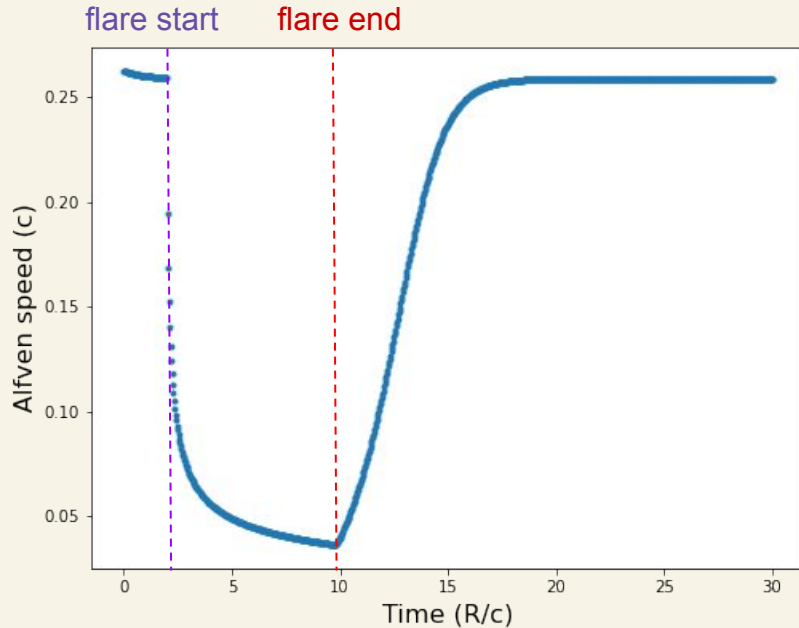
Spectral Energy Distribution (SED)



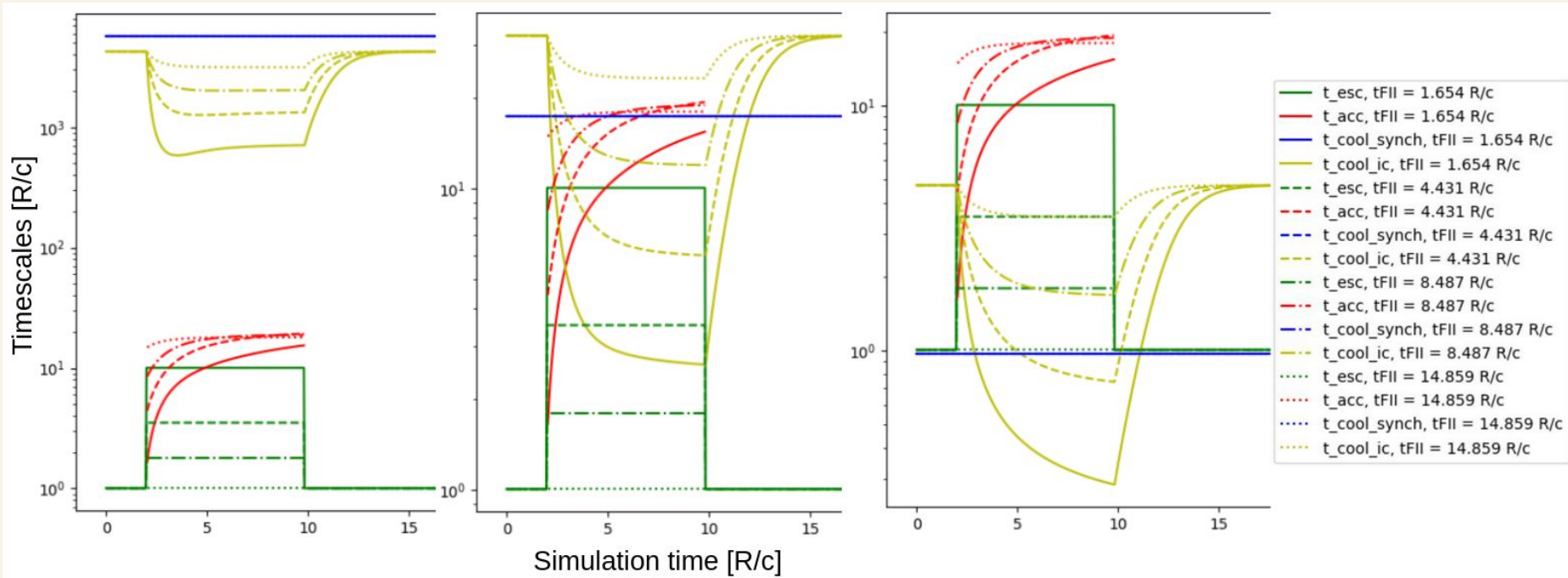
# Extra - Fermi II acceleration: hard-sphere regime

Alfvén speed:

$$\beta_A = \frac{1}{\sqrt{1 + \frac{4\mu_0\epsilon}{3B^2}}}$$



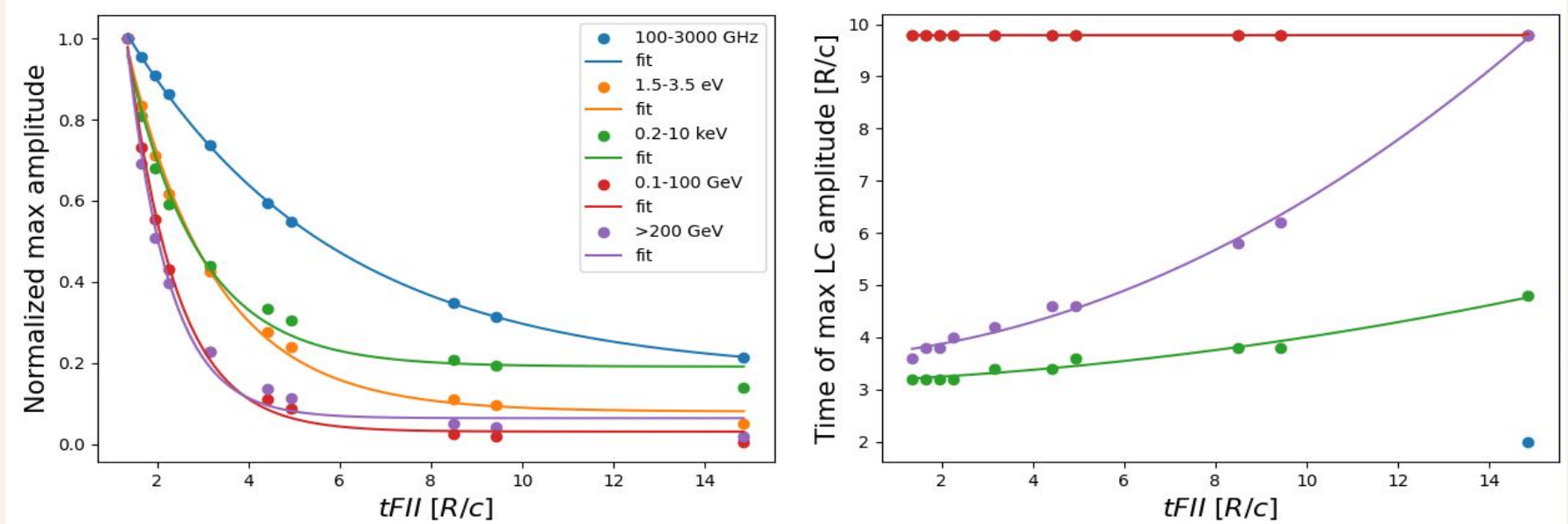
# Extra - Fermi II acceleration: hard-sphere regime



⇒ IC cooling dominates for high energies and short acceleration timescales



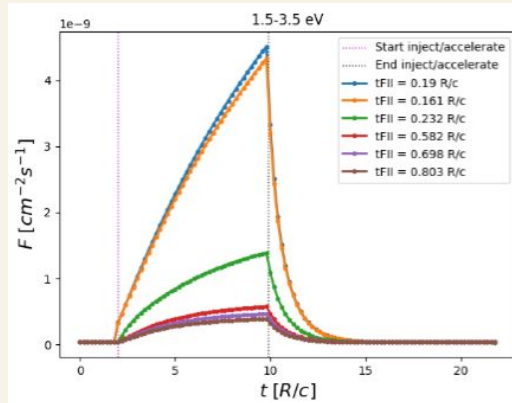
# Extra - Fermi II acceleration: hard-sphere regime



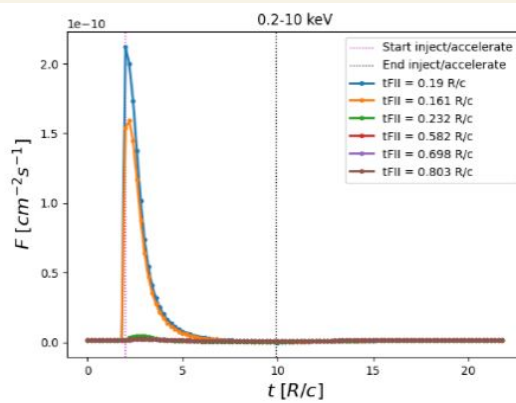
⇒ Known variability amplitude and peak shift behaviour, possible parametrization of the flares

# Extra - Fermi II acceleration: Kolmogorov regime

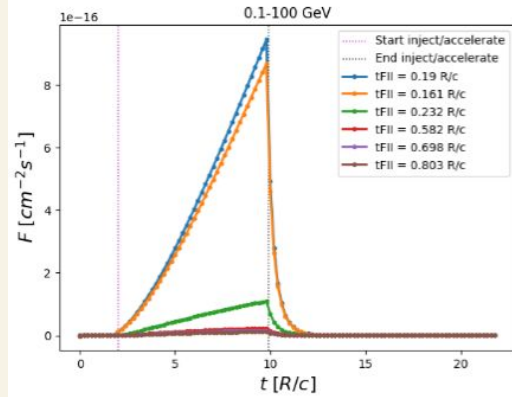
Optical



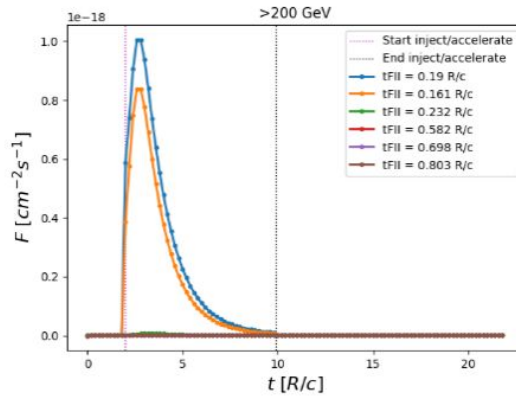
X-rays



$\gamma$ -rays



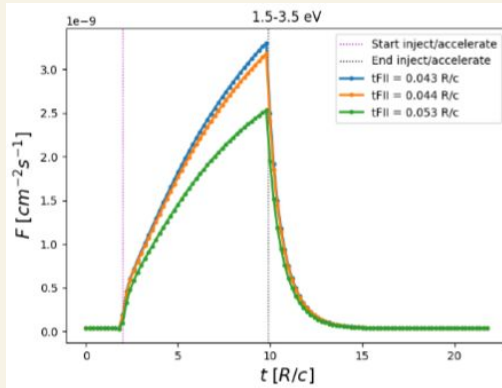
VHE  $\gamma$ -rays



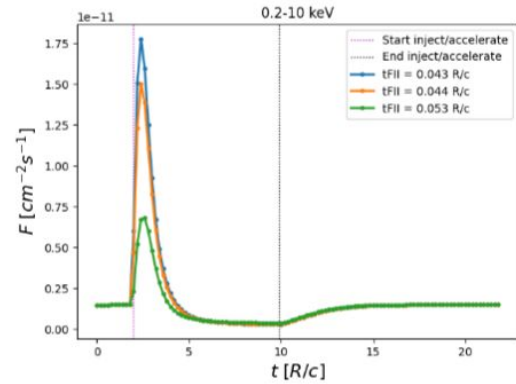
⇒ Same shapes as high CD hard-sphere turbulence

# Extra - Fermi II acceleration: Kraichnan regime

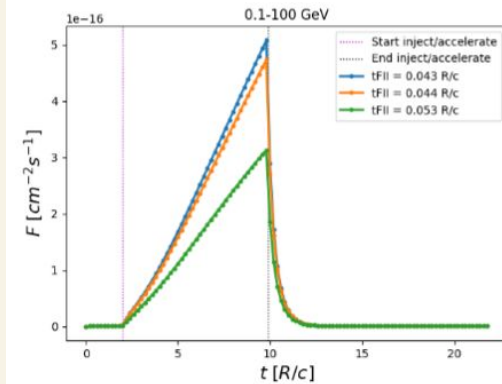
Optical



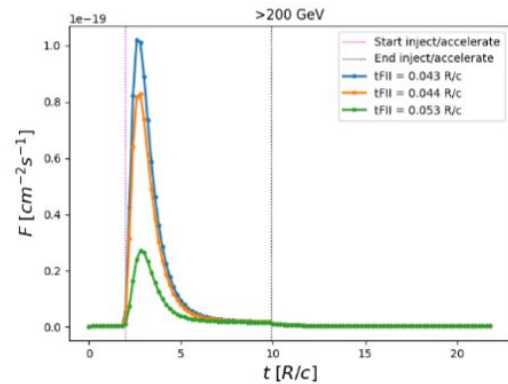
X-rays



$\gamma$ -rays



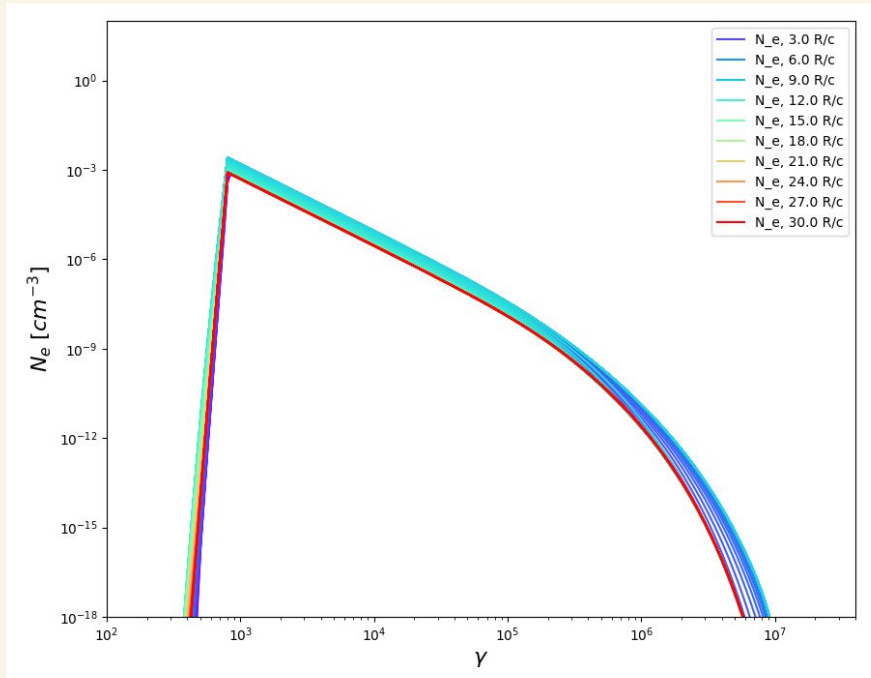
VHE  $\gamma$ -rays



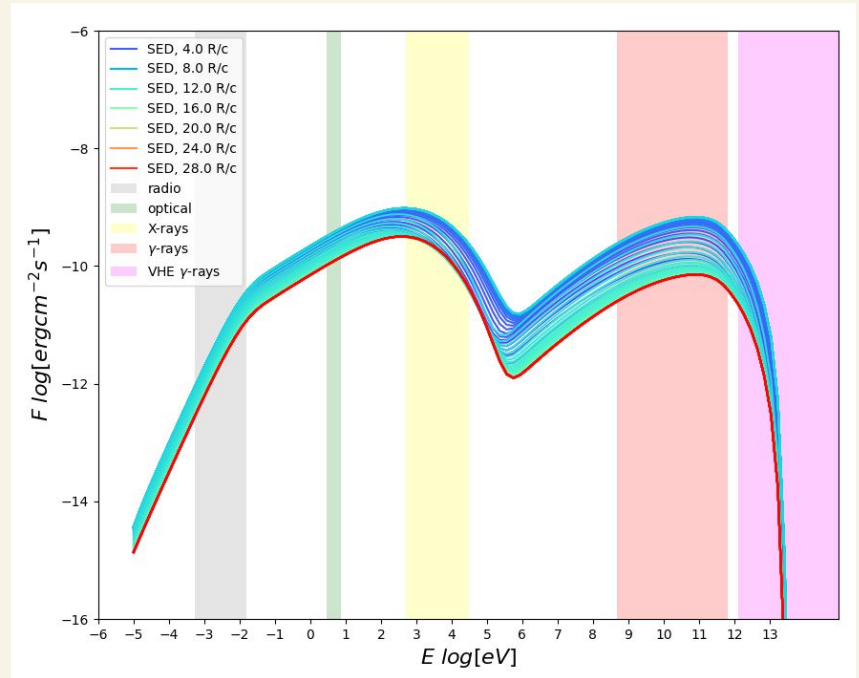
⇒ Same shapes as high CD hard-sphere turbulence

# Extra - Fermi I acceleration

## Electron Distribution



## Spectral Energy Distribution (SED)



# Extra - Fermi I acceleration

