

Credit: NASA/Swift Dana Berry



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GW and dense matter

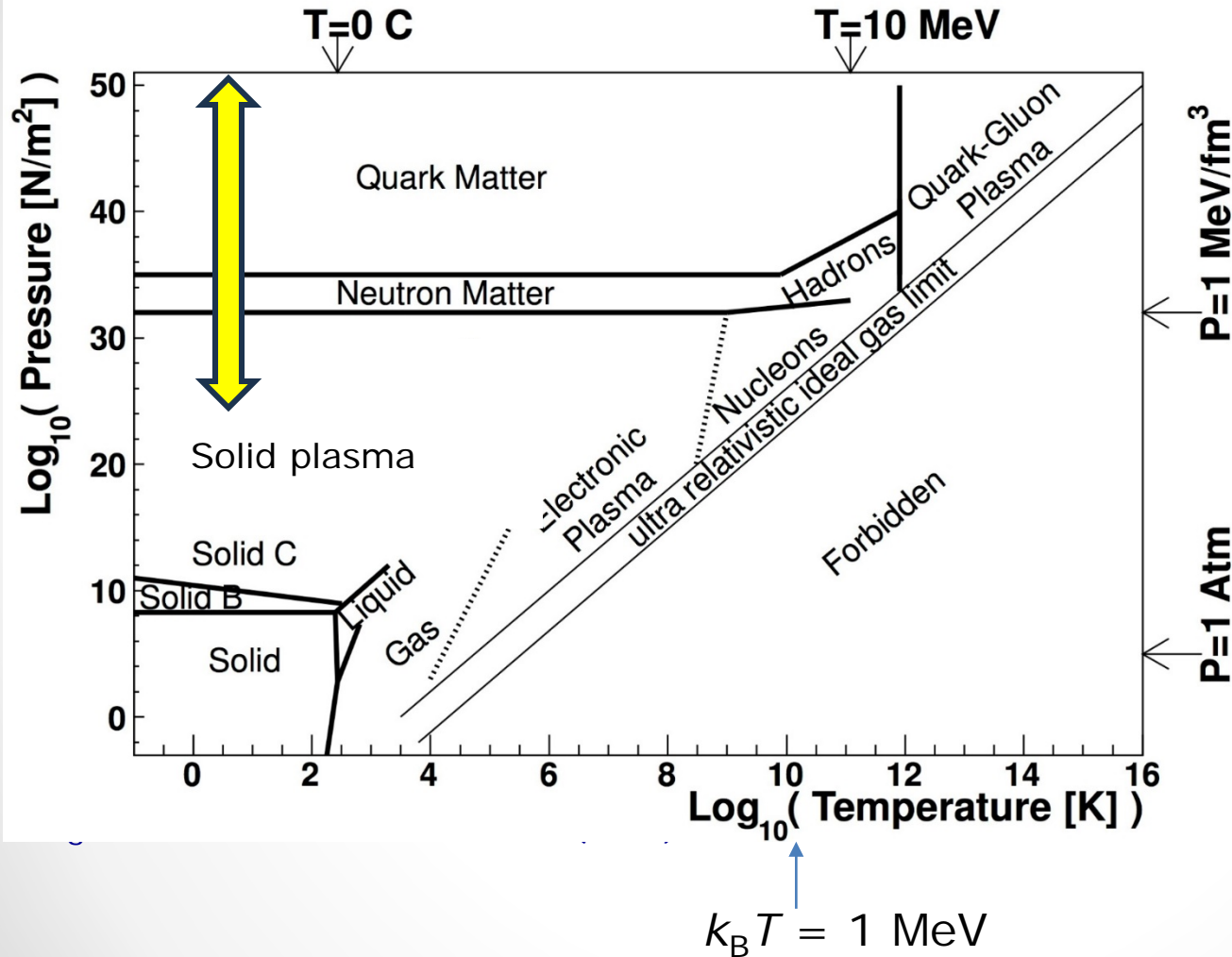
*Francesca Gulminelli - Université de
Caen-Normandie*

*3rd MaNiTou summer school on gravitational waves,
1-6 July, 2024*

Lecture plan

1. Introduction: dense matter in the universe
 - a. The sites
 - b. The signals
 - c. The big questions
2. The gravitational wave probe for dense matter
 - a. Neutron star modelling and the equation of state (EoS)
 - b. Observations
 - c. EoS and observables: constraining the parameters

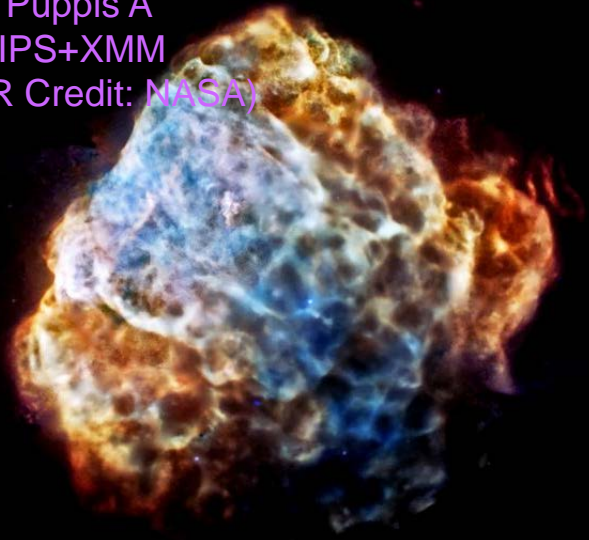
The phases of matter



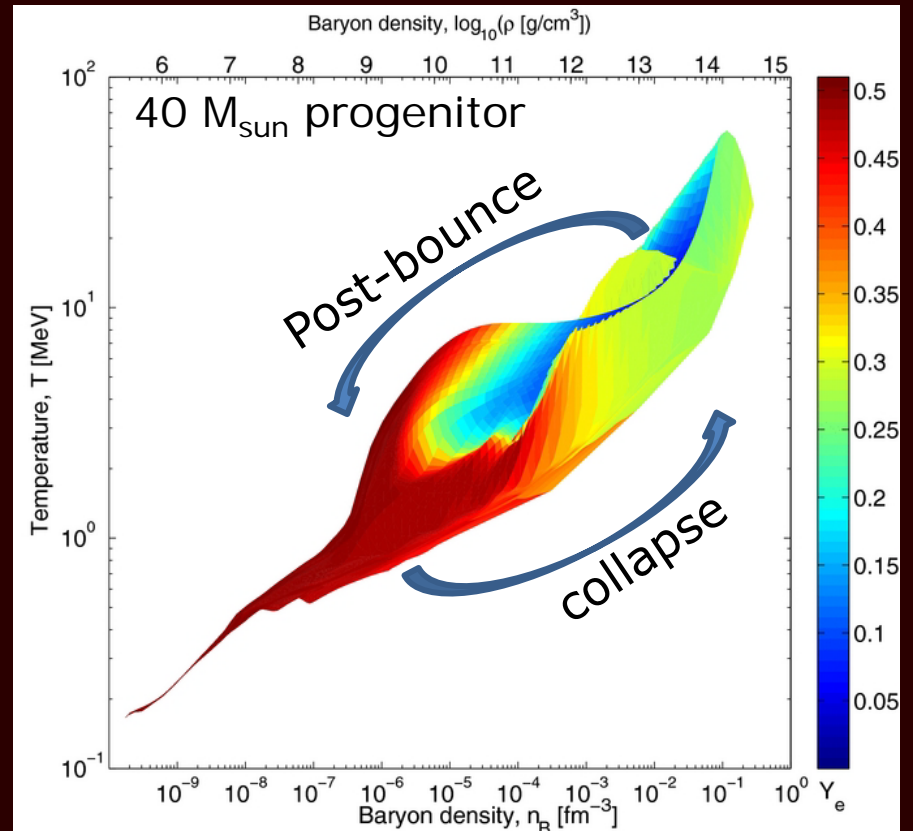
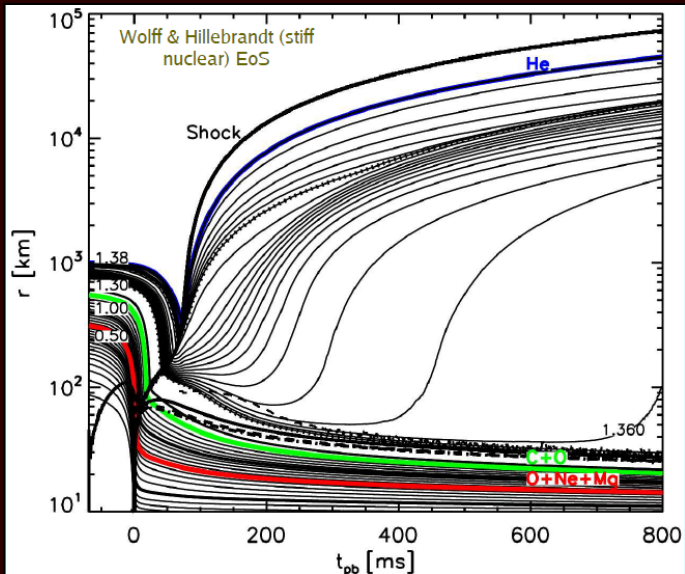
Where can ultra-dense matter be found in nature?

Supernova remnant
in Puppis A
MIPS+XMM
IR Credit: NASA)

Dense matter in the Universe: CCSN



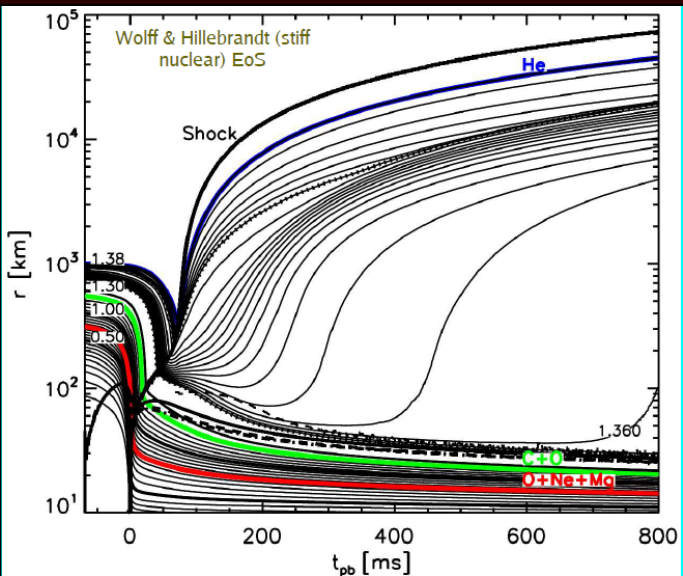
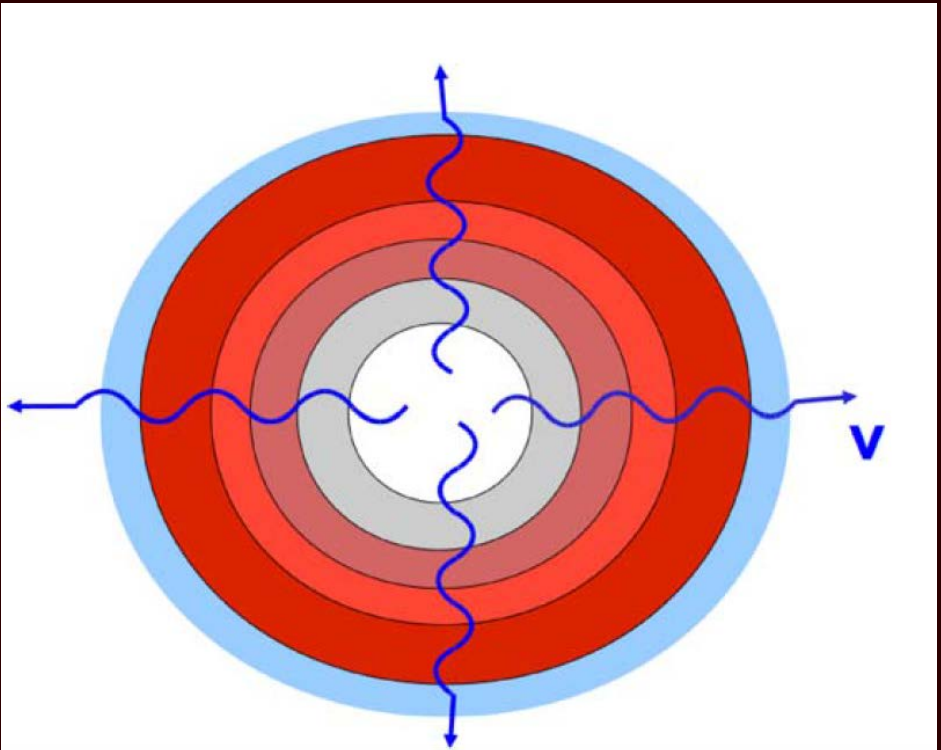
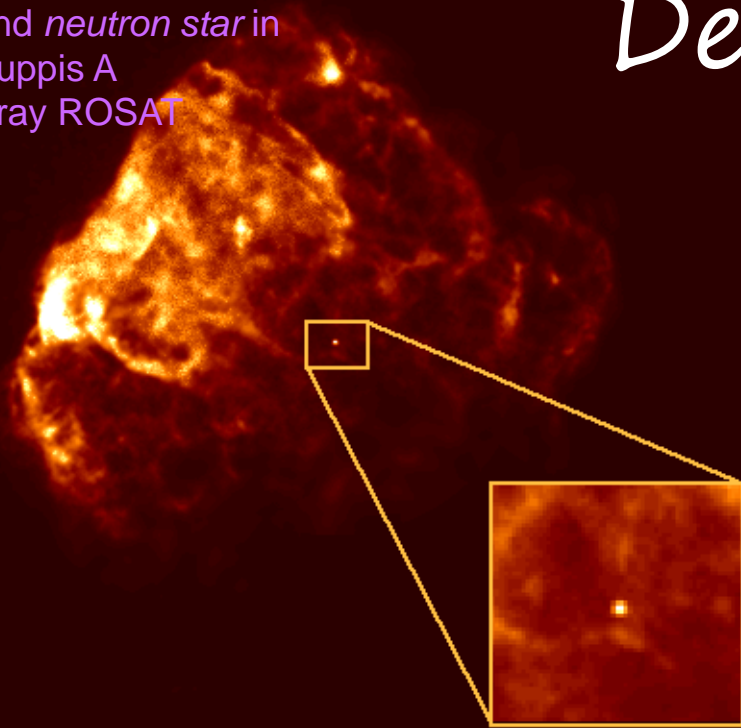
F.S.Kitaura et al, A&A 450 (06) 345



T.Fischer et al, 2011 ApJS 194 39

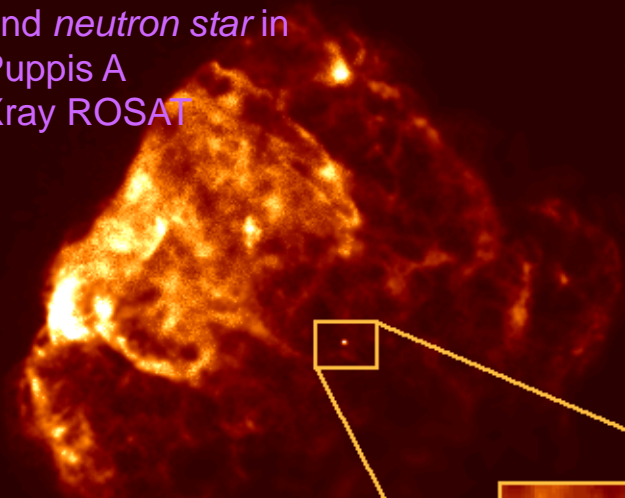
Supernova remnant
and *neutron star* in
Puppis A
Xray ROSAT

Dense matter in the Universe: PNS

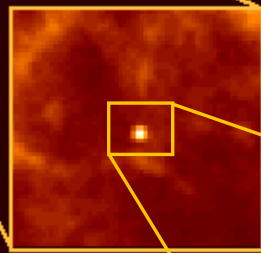


Supernova remnant
and neutron star in
Puppis A
Xray ROSAT

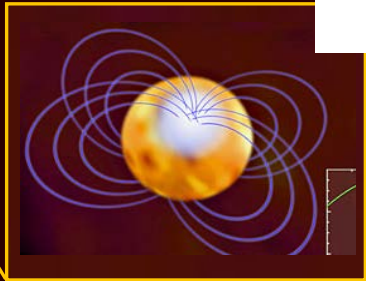
Dense matter in the Universe: NS



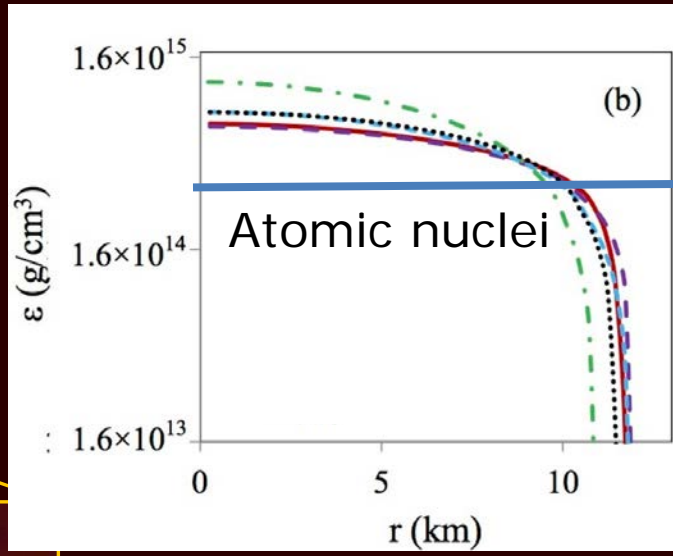
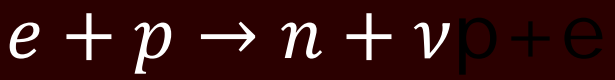
$y_e \cong 1/2$
 $T \sim 10^{12} K$



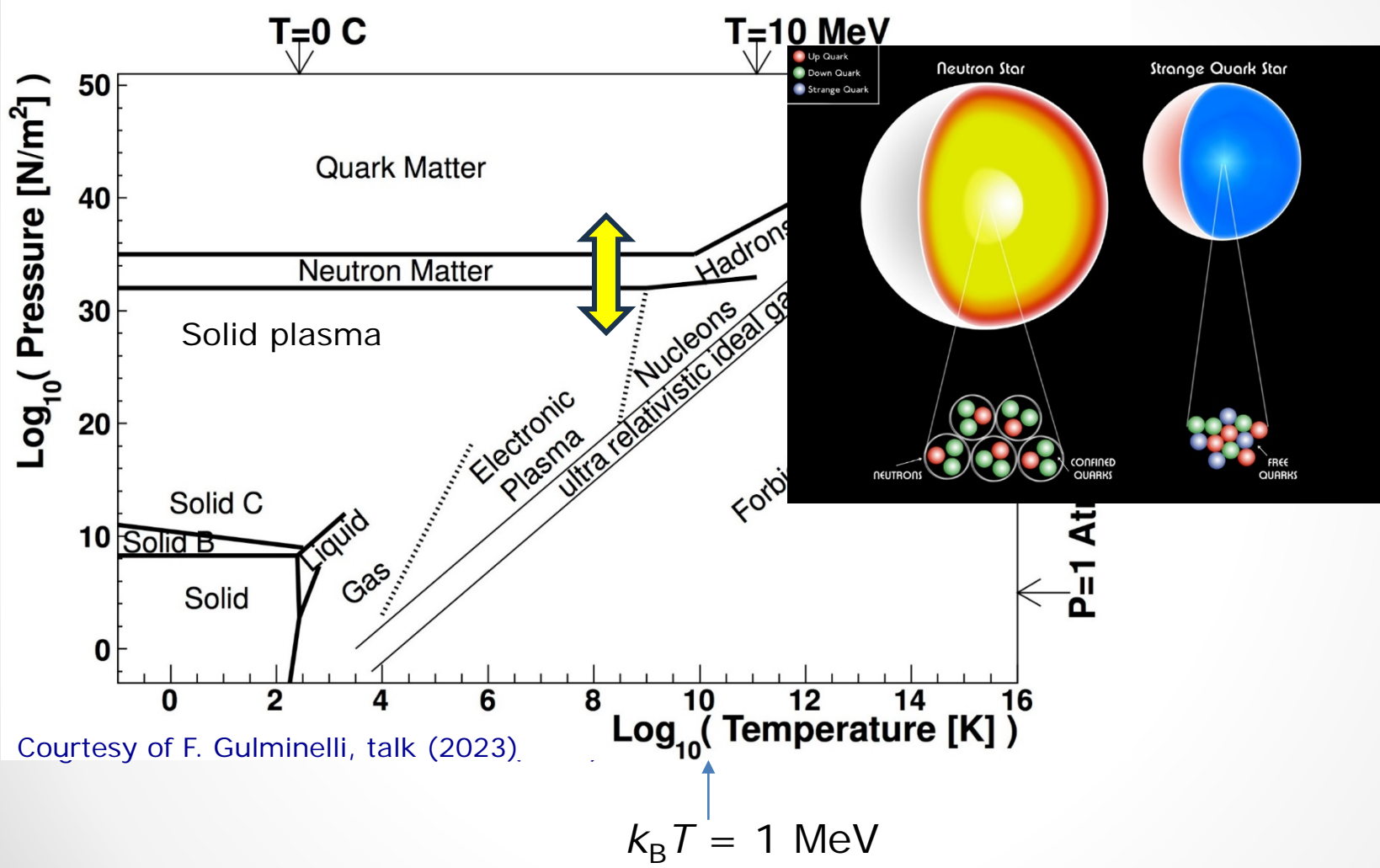
$y_e \cong 1/3$
 $T \sim 10^{11} K$



$y_e \cong 1/5$
 $T \sim 6K$



The phases of matter



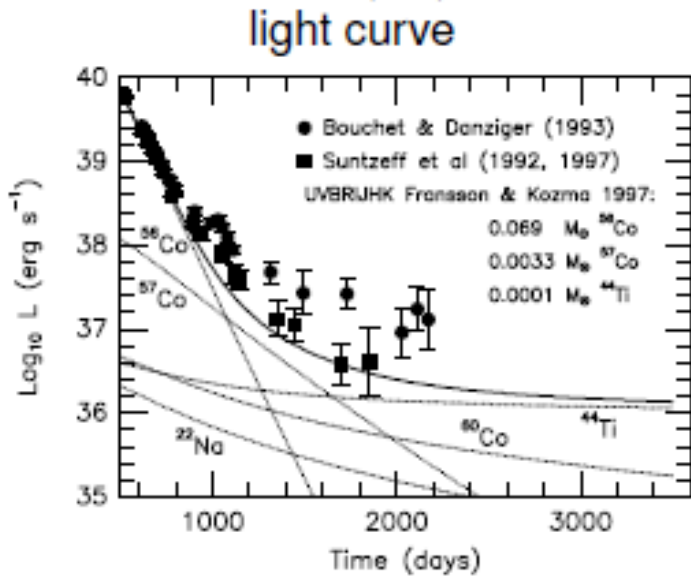
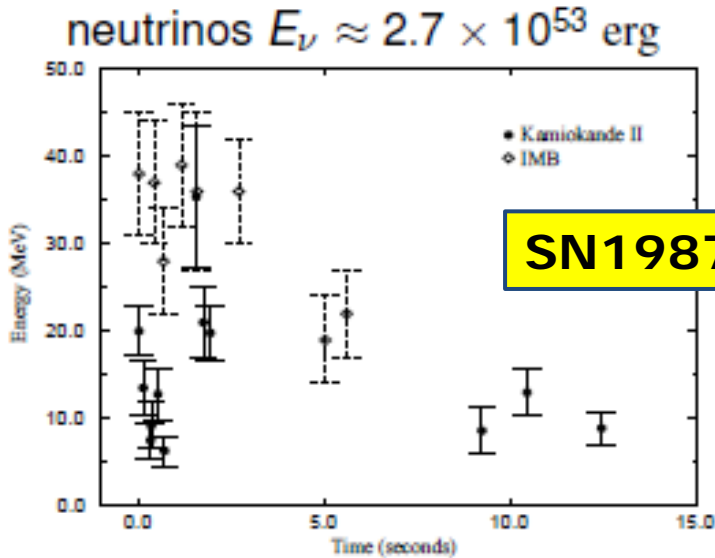
Credits: CXC/M. Weiss

Courtesy of F. Gulminelli, talk (2023).

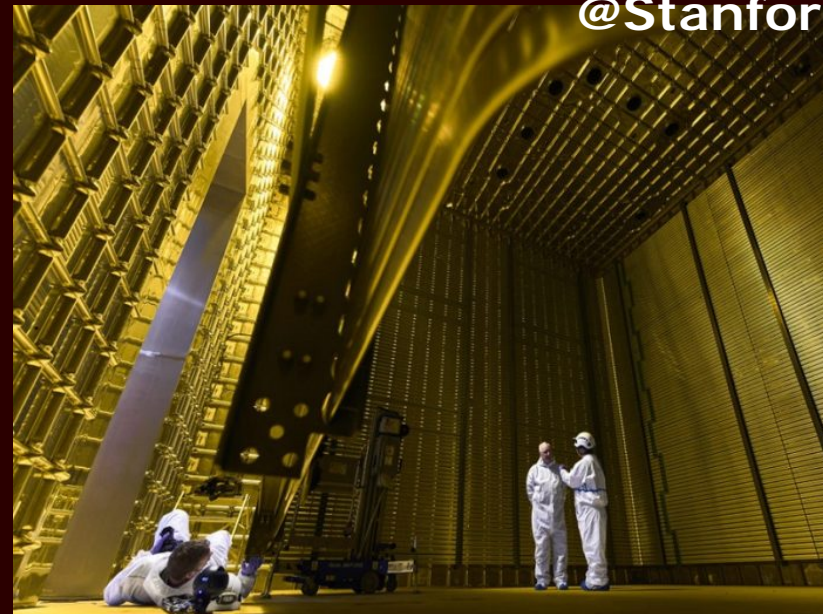
$$k_B T = 1 \text{ MeV}$$

CCSN

Signals

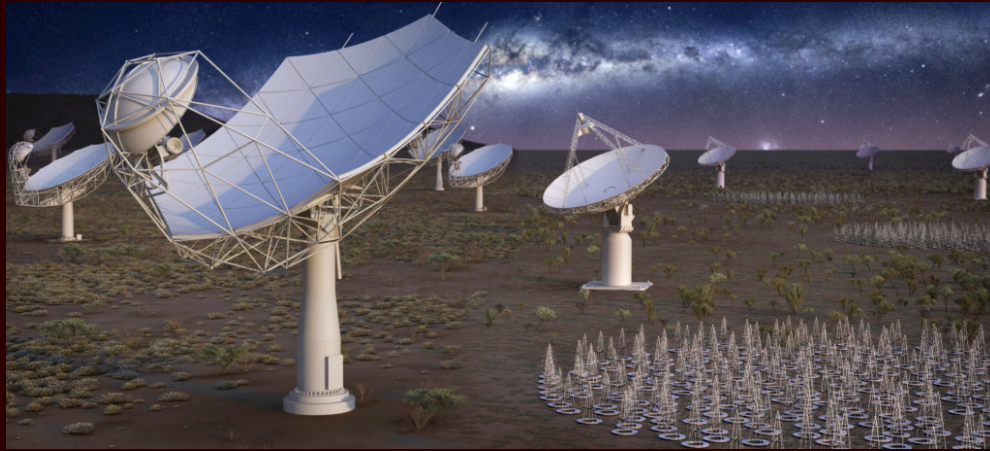


DUNE
@Stanford

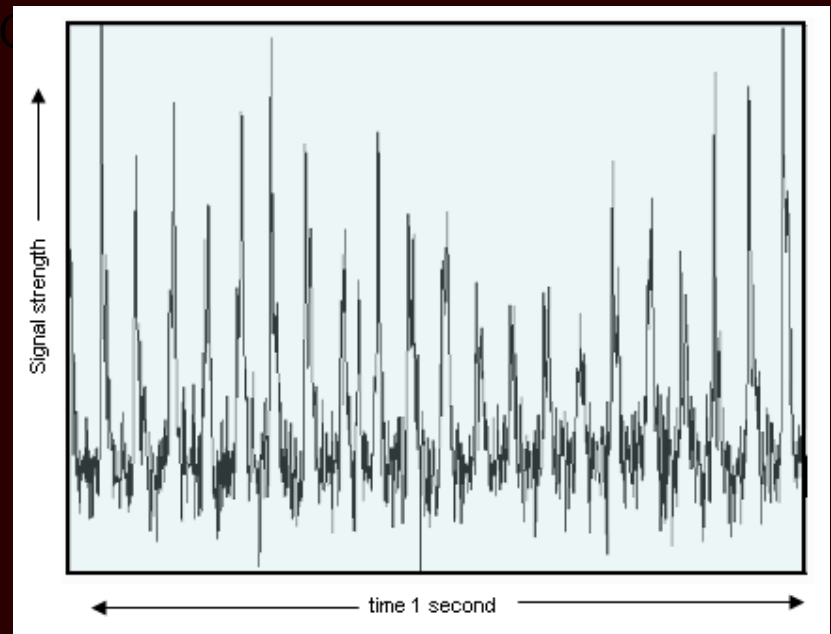


Signals

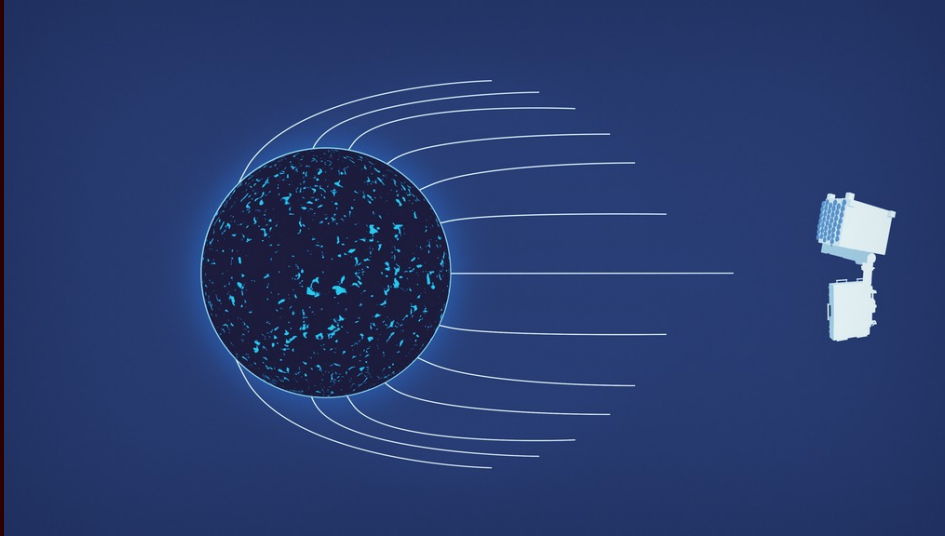
Pulsars



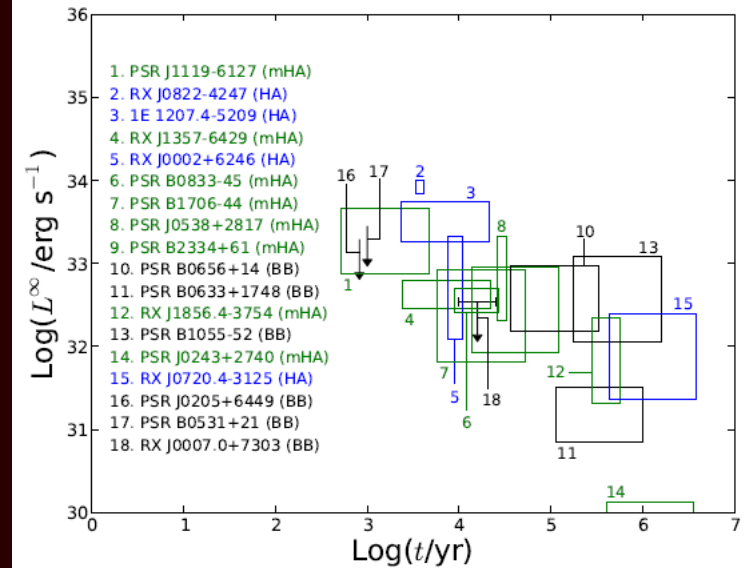
SKA@ South Africa



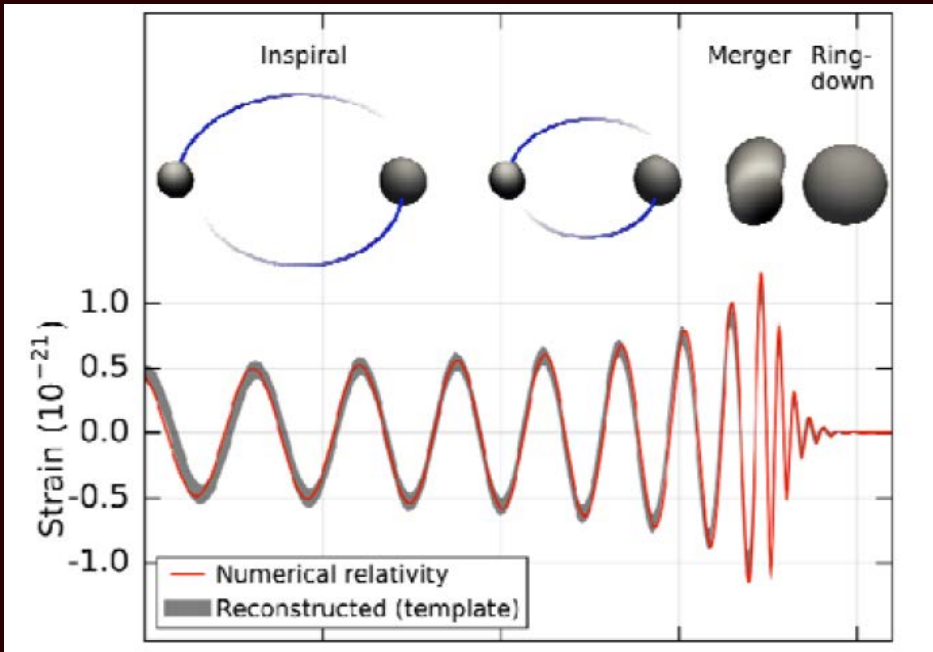
Signals



XR sources



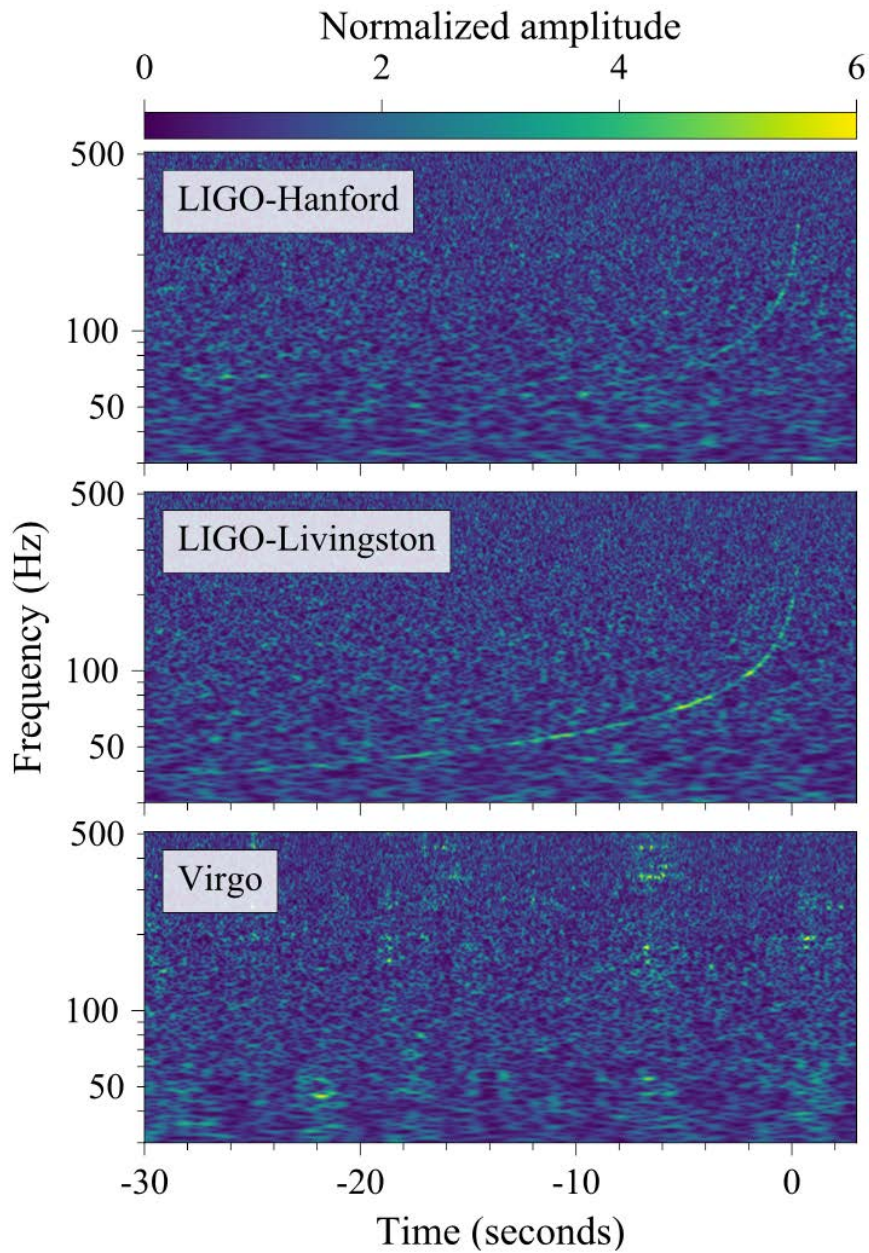
Signals



SN

Mergers

Signals



Mergers



Multi-messenger Observations of a Binary Neutron Star Merger

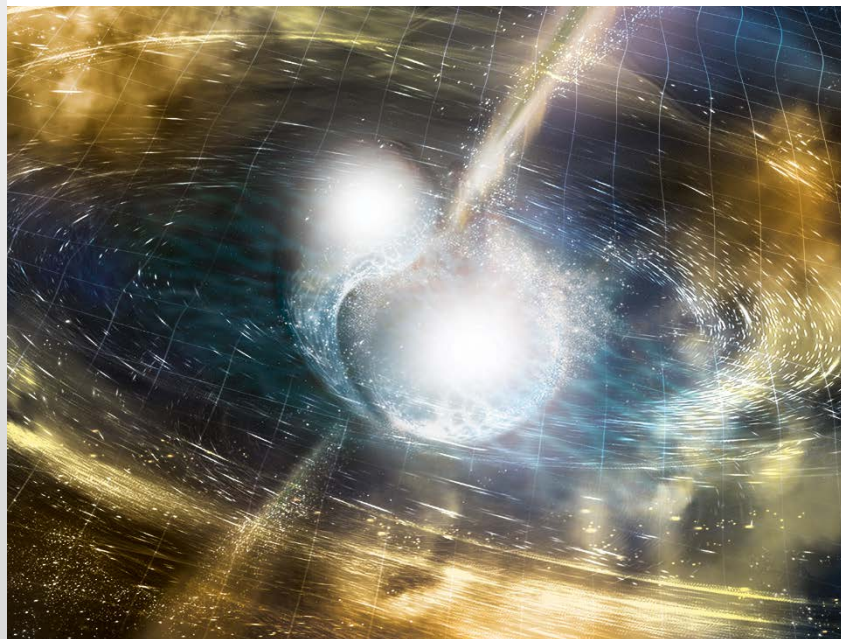
LIGO Scientific Collaboration and Virgo Collaboration, Fermi GBM, INTEGRAL, IceCube Collaboration, AstroSat Cadmium Zinc Telluride Imager Team, IPN Collaboration, The Insight-Hxmt Collaboration, ANTARES Collaboration, The Swift Collaboration, AGILE Team, The 1M2H Team, The Dark Energy Camera GW-EM Collaboration and the DES Collaboration, The DLT40 Collaboration, GRAWITA: GRAVitational Wave Inaf TeAm, The Fermi Large Area Telescope Collaboration, ATCA: Australia Telescope Compact Array, ASKAP: Australian SKA Pathfinder, Las Cumbres Observatory Group, OzGrav, DWF (Deeper, Wider, Faster Program), AST3, and CAASTRO Collaborations, The VINROUGE Collaboration, MASTER Collaboration, J-GEM, GROWTH, JAGWAR, Caltech-NRAO, TTU-NRAO, and NuSTAR Collaborations, Pan-STARRS, The MAXI Team, TZAC Consortium, KU Collaboration, Nordic Optical Telescope, ePESSTO, GROND, Texas Tech University, SALT Group, TOROS: Transient Robotic Observatory of the South Collaboration, The BOOTES Collaboration, MWA: Murchison Widefield Array, The CALET Collaboration, IKI-GW Follow-up Collaboration, H.E.S.S. Collaboration, LOFAR Collaboration, LWA: Long Wavelength Array, HAWC Collaboration, The Pierre Auger Collaboration, ALMA Collaboration, Euro VLBI Team, Pi of the Sky Collaboration, The Chandra Team at McGill University, DFN: Desert Fireball Network, ATLAS, High Time Resolution Universe Survey, RIMAS and RATIR, and SKA South Africa/MeerKAT
(See the end matter for the full list of authors.)

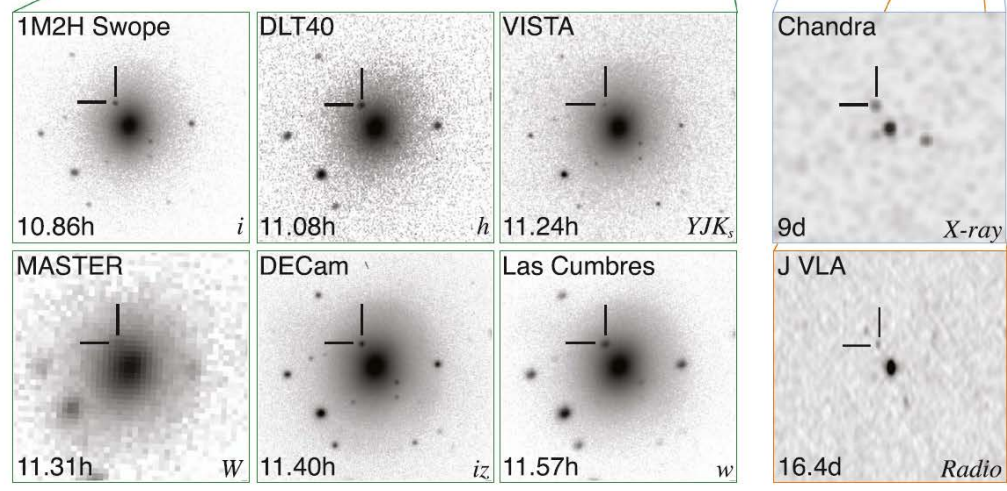
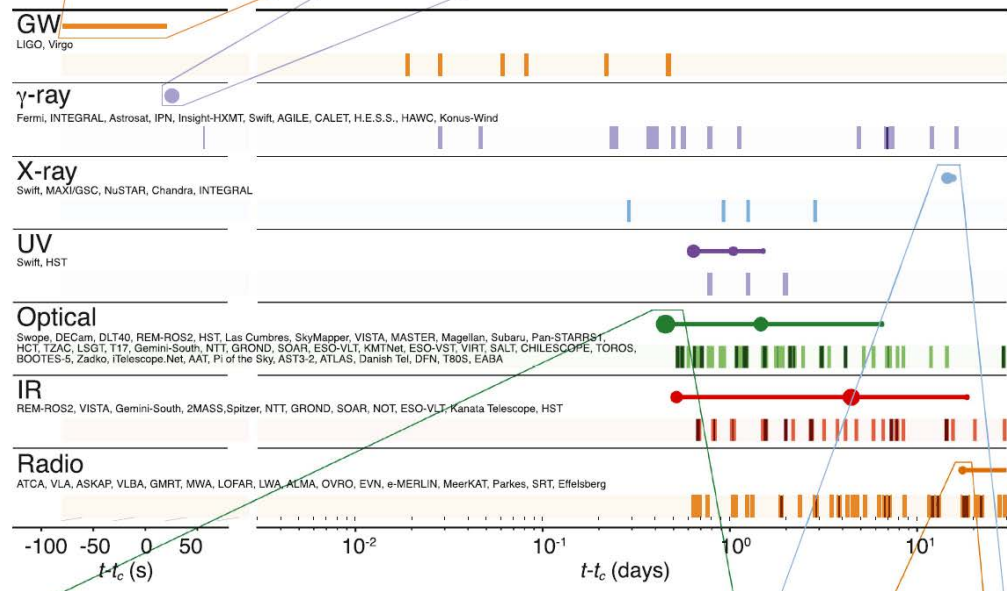
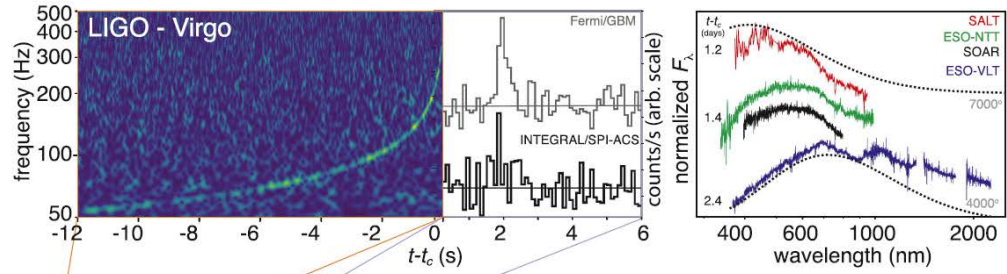
Received 2017 October 3; revised 2017 October 6; accepted 2017 October 6; published 2017 October 16

Foundation
Operated by Caltech and MIT

GW170817 Press Release
LIGO and Virgo make first
detection of gravitational
waves produced by colliding
neutron stars

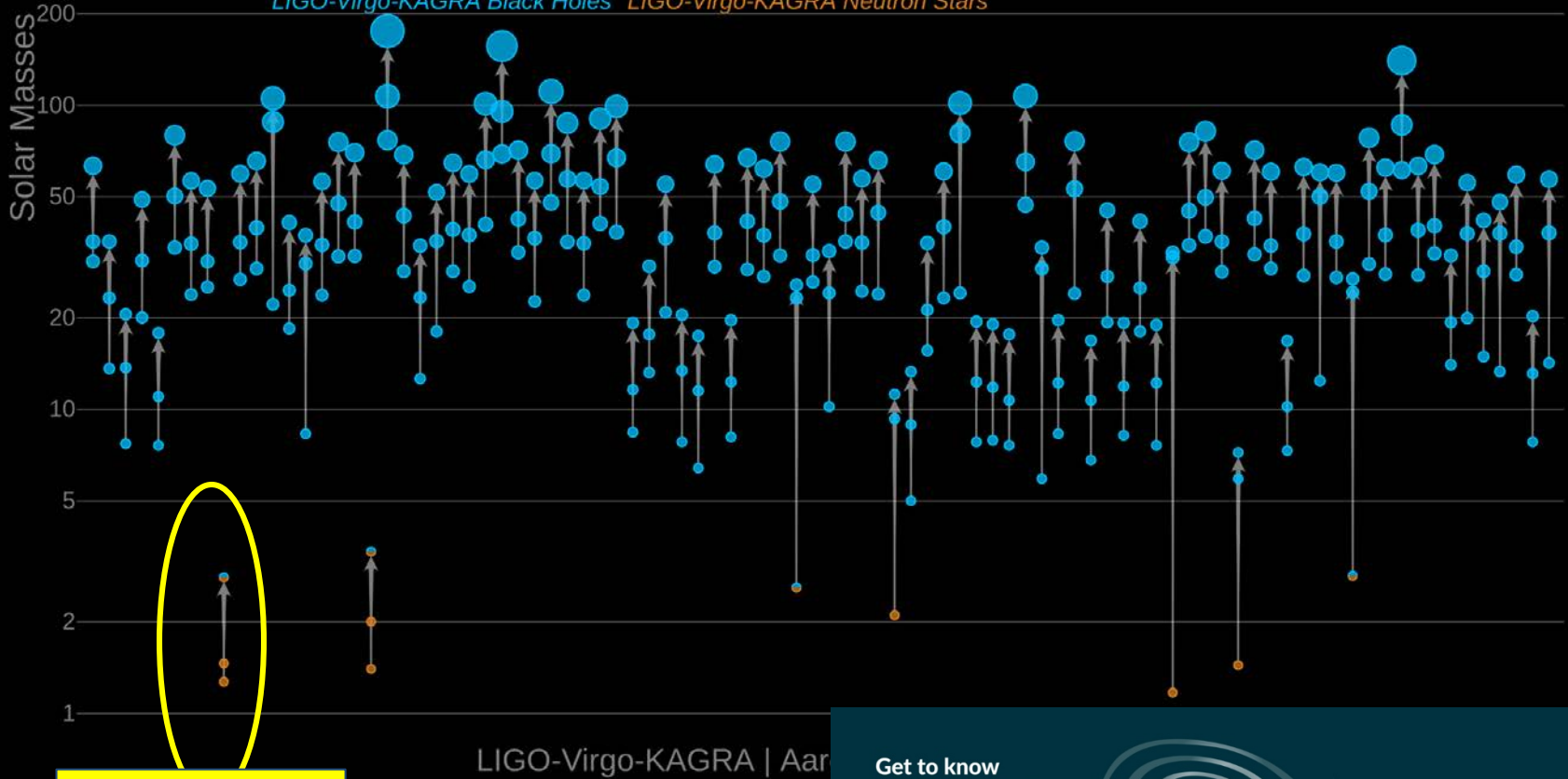
Discovery marks first cosmic event
observed in both gravitational
waves and light.





Masses in the Stellar Graveyard

LIGO-Virgo-KAGRA Black Holes LIGO-Virgo-KAGRA Neutron Stars



GW170817

LIGO-Virgo-KAGRA | Aar

5 years of LVK observations

Get to know GW230529

Full name GW230529_181500

Discovered on 29 May 2023 at 18h15 UTC

most likely a merger between a Neutron Star & Black Hole (NSBH)

~1.4 M_{\odot}

~3.6 M_{\odot}

Most symmetric NSBH event so far
more likely than prior GW NSBHs to have the neutron star ripped apart by the black hole

~ 650 million light years away

H

L

V

K

Detectors

- Offline OR not operational
- Online BUT not used for analysis*
- Online AND used for analysis

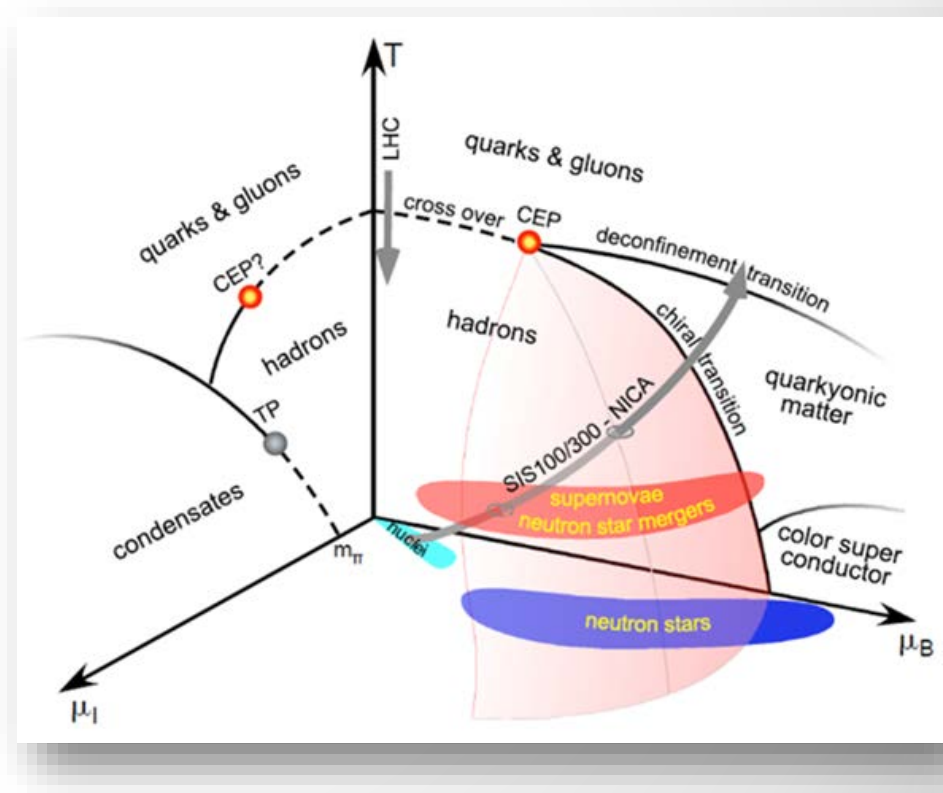
Primary object in lower mass gap
further supports that this region is not empty

Mass (M_{\odot}) 2 3 4 5 6

* Although the KAGRA detector was in observing mode, its sensitivity was insufficient to impact the analysis of GW230529

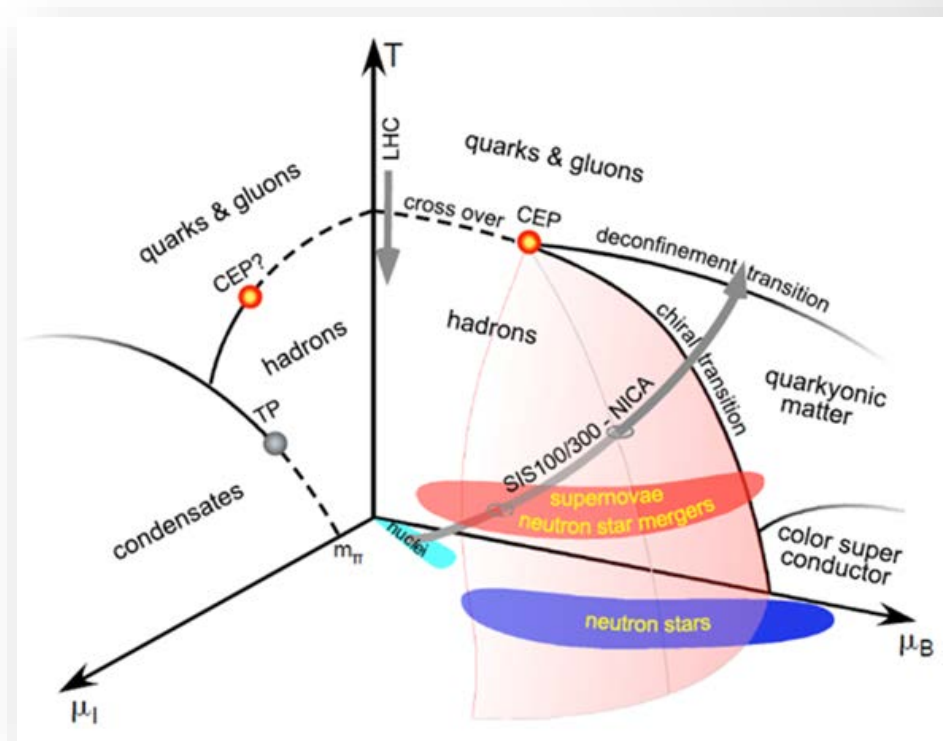
Dense matter: the Questions

1. What is the internal structure of the dense matter in neutron stars, supernova cores and mergers?
2. How does this structure reflect into the observable signals?
3. What can we learn on the underlying nuclear and hadronic physics?



The message I would like to convey:

Gravitational waves, and particularly the inspiral GW signal from NS mergers, opens the possibility of a ***DIRECT*** measurement of the QCD phase diagram



Lecture plan

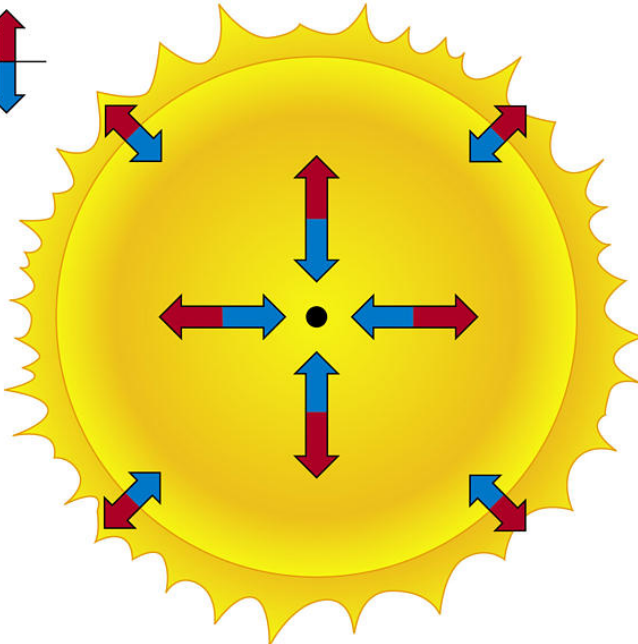
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Modelling (Neutron) Stars: hydrostatics

- Self-gravitation => Tolman Oppenheimer Volkoff (1939):

$$\frac{dP(\rho)}{dr} = -\frac{G}{r^2} \left[\rho(r) + \frac{P(\rho)}{c^2} \right] \left[m(r) + 4\pi r^3 \frac{P(\rho)}{c^2} \right] \left[1 - \frac{2Gm(r)}{rc^2} \right]^{-1}$$

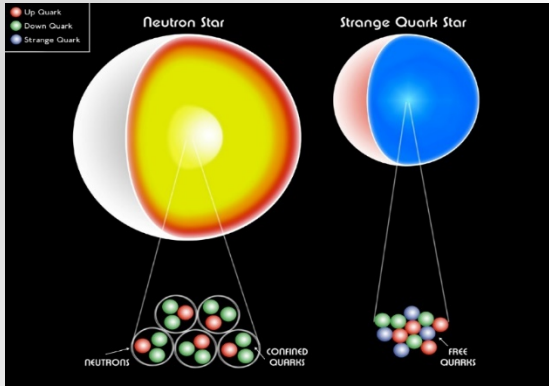
Pressure
out ↑
Gravity
in ↓



$$\begin{aligned} \forall \rho_c \\ R=r(P=0) \\ M=m(r=R) \end{aligned}$$

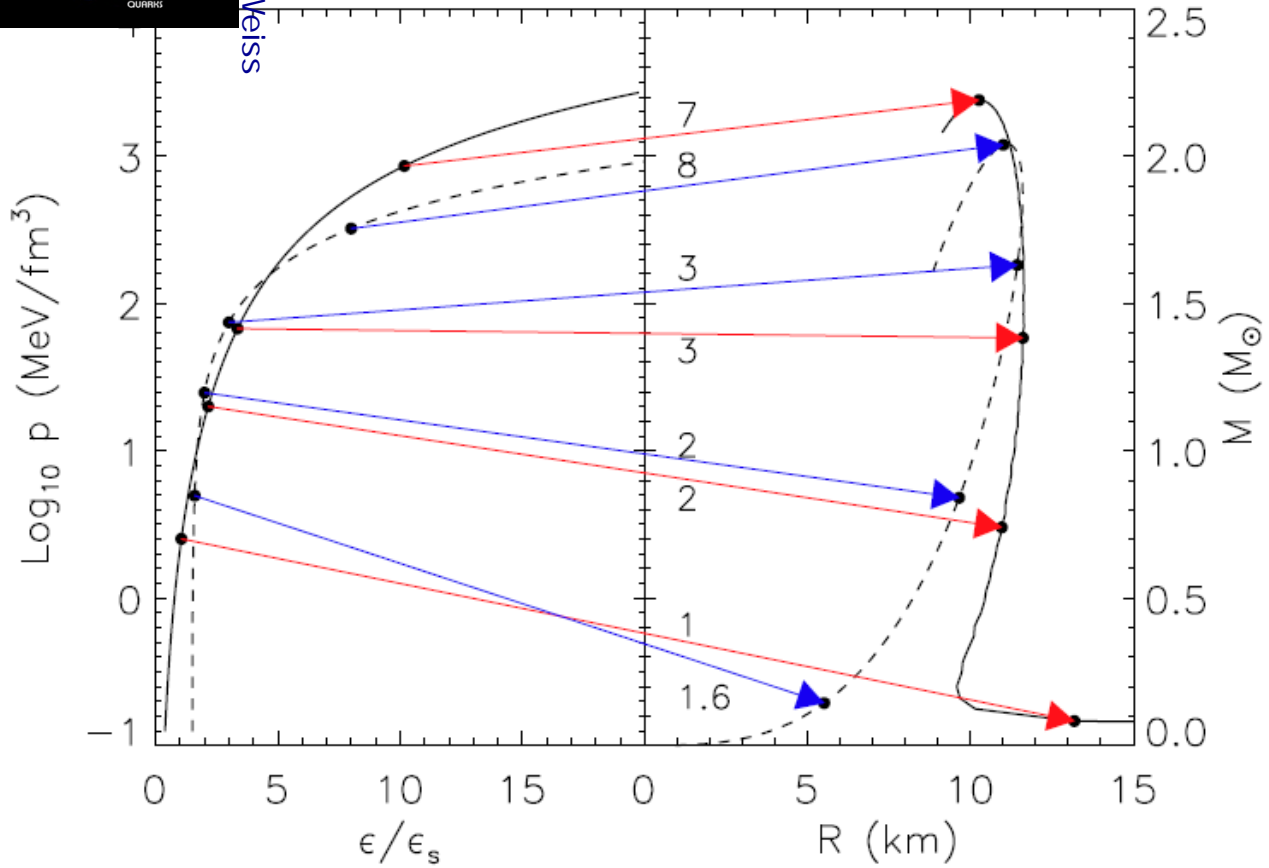
Mass and radius

**Needs ONLY $P(\rho)$
of NS matter**



Credits: CXC/M. Weiss

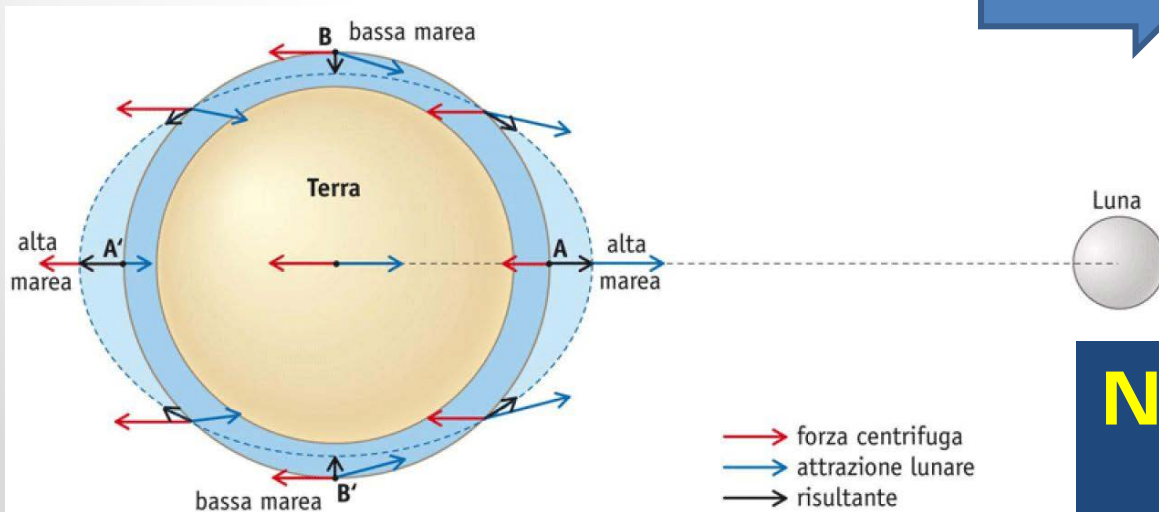
$$P(\rho) \leftrightarrow M(R)$$



Modelling (Neutron) Stars: hydrostatics

- Influence of a second body => Thorne and Campolattaro (1967):

$$\frac{d^2 H(r)}{dr^2} + \frac{dH(r)}{dr} \left[\frac{2}{r} + e^{\lambda(\mathbf{P}(\rho))} \left(\frac{2m(r)}{r^2} + 4\pi r (\mathbf{P}(\rho) - \rho(r)) \right) \right] + H(r) Q(\mathbf{P}(\rho)) = 0$$



$$\forall \rho_c$$

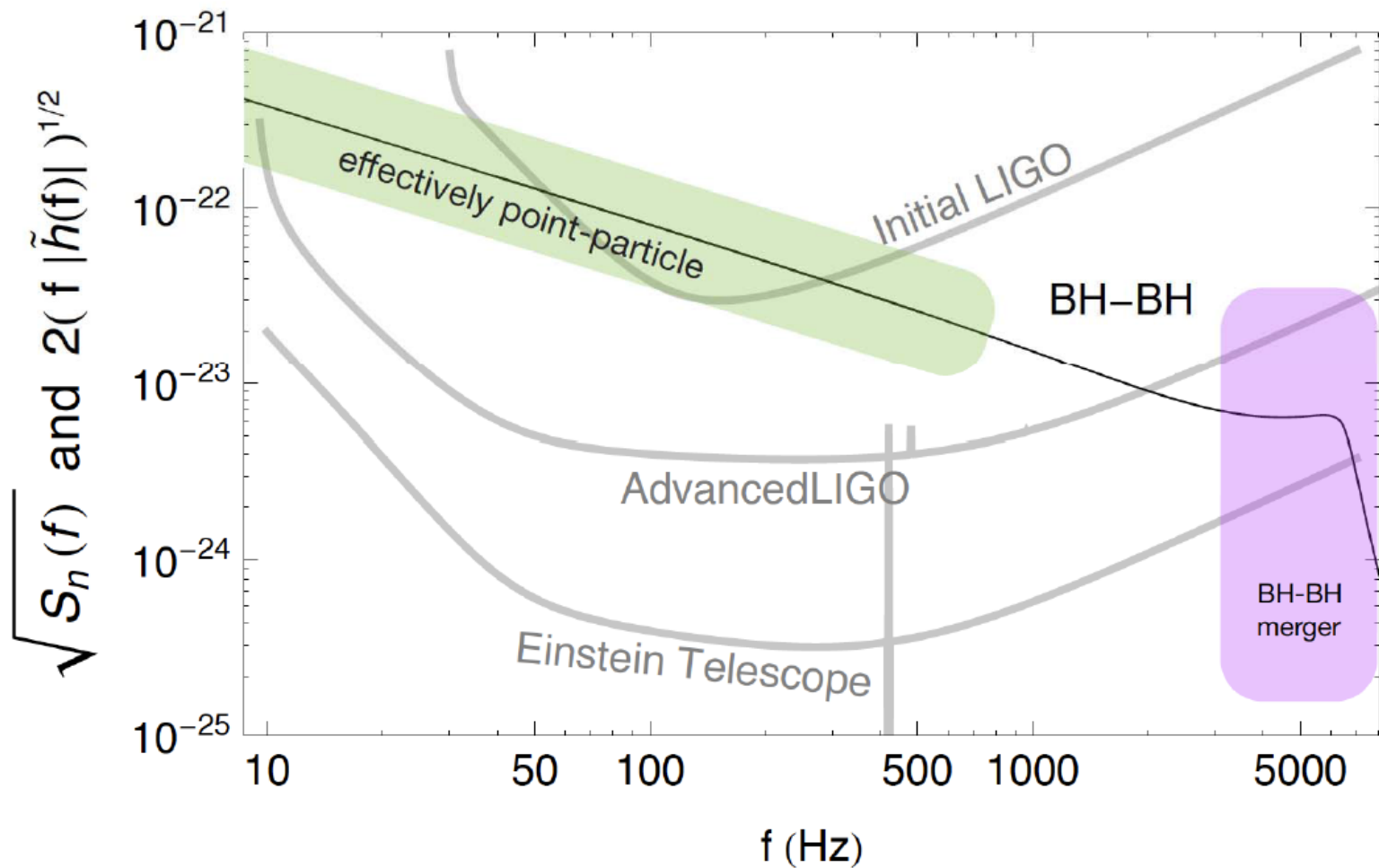
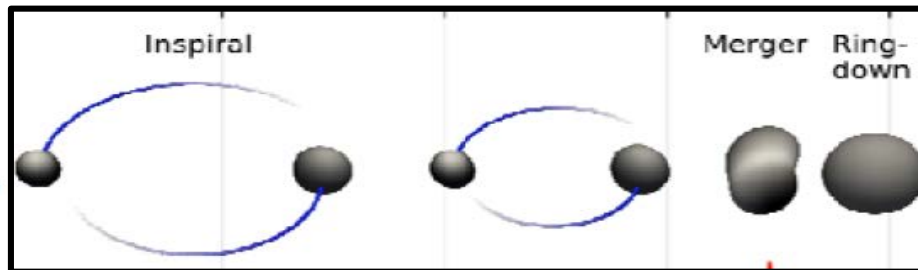
$$\Lambda = \frac{2}{3} k_2 \left(\frac{H'(r=R)}{H(r=R)} \right) \left(\frac{c^2 R}{G M} \right)^5$$

Tidal polarizability

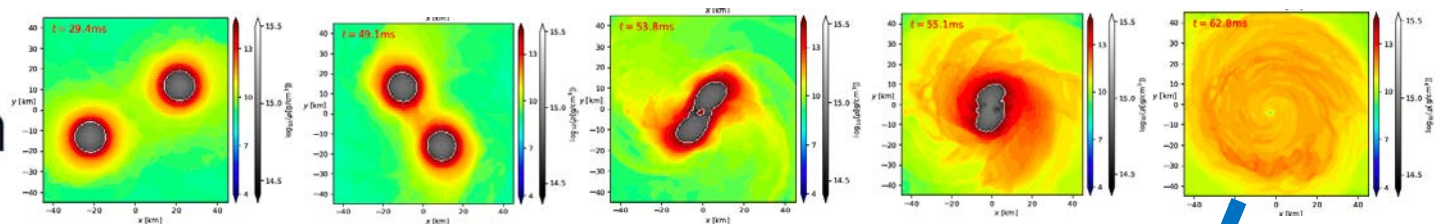
**Needs ONLY $P(\rho)$
of NS matter**



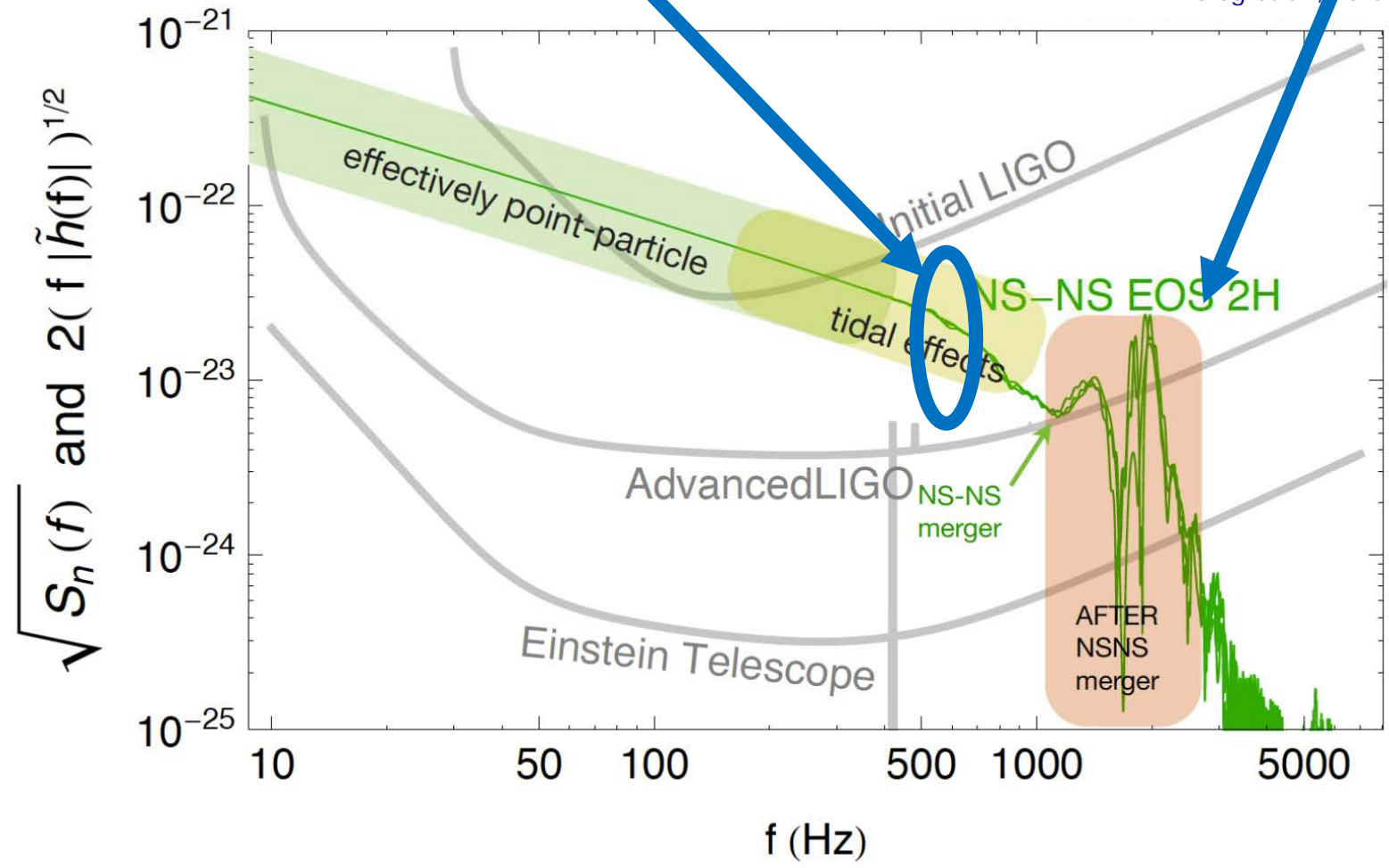
Spectrum of BBH inspiral,



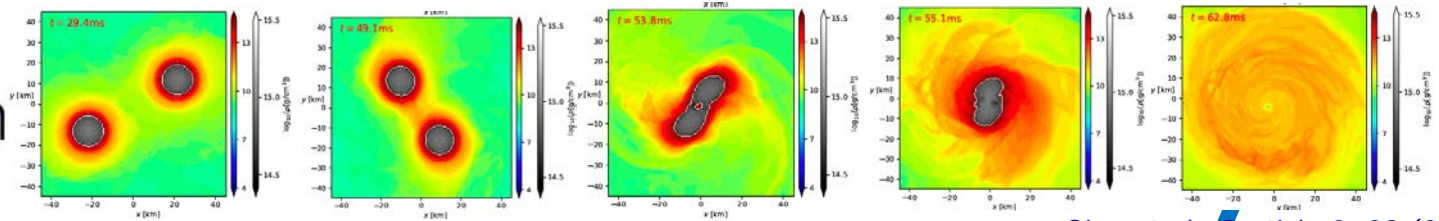
Spectrum



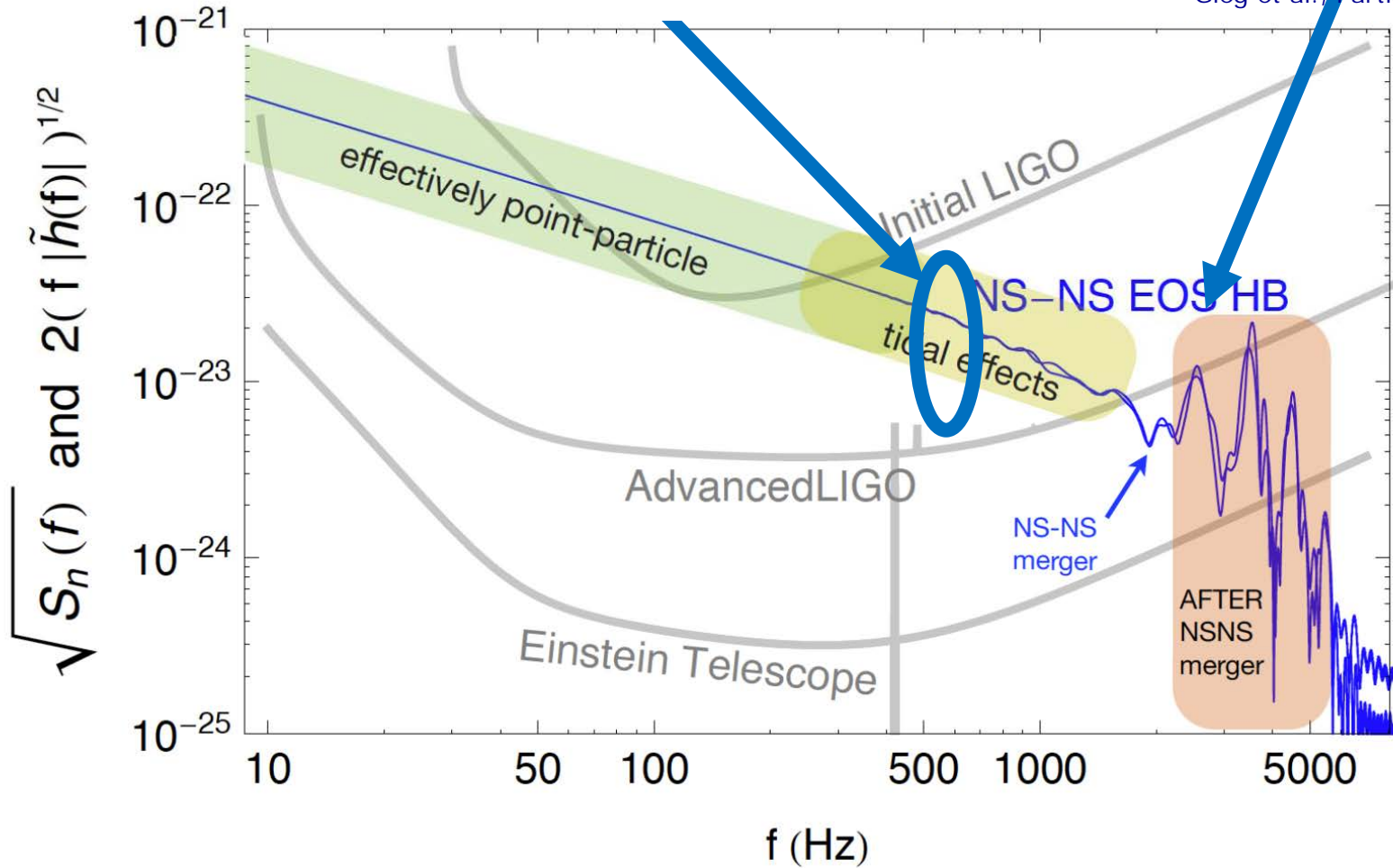
Gieg et al., Particle 2, 23 (201...)



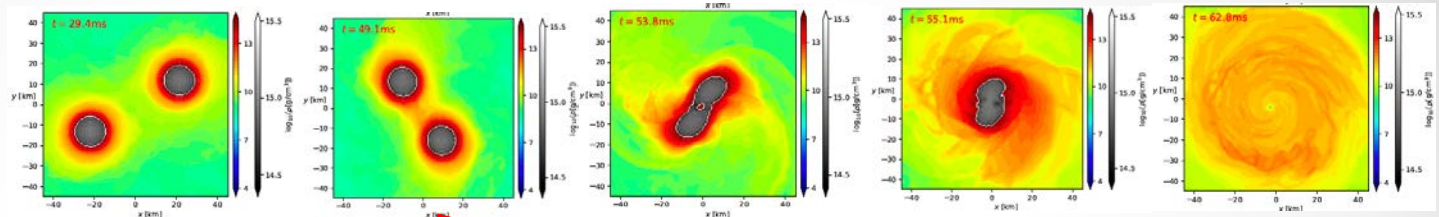
Spectrum



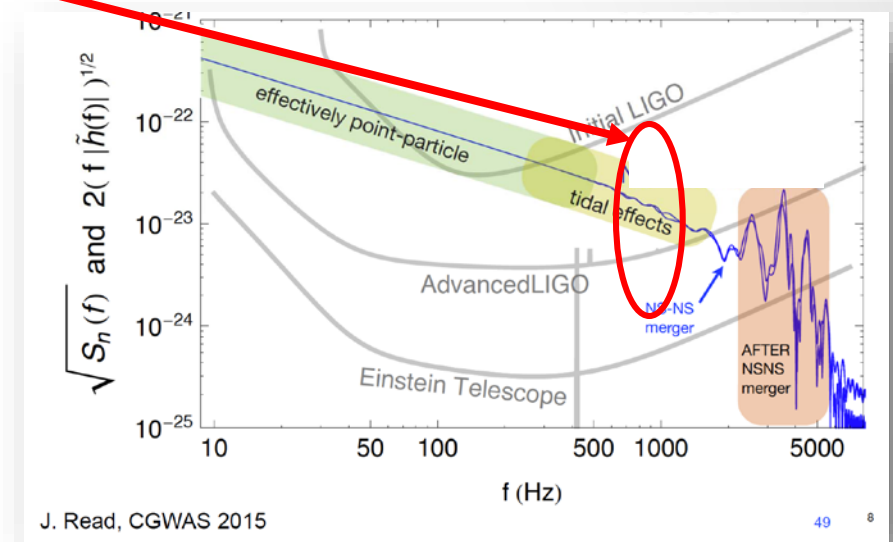
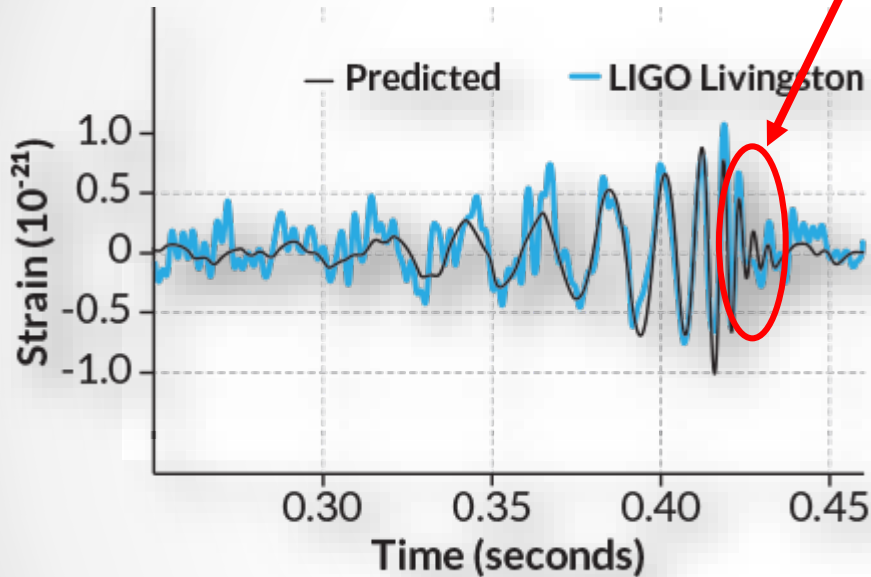
Gieg et al., Particle 2, 23 (2011)



Extraction of the tidal effects



Gieg et al., Particle 2, 23 (2010)



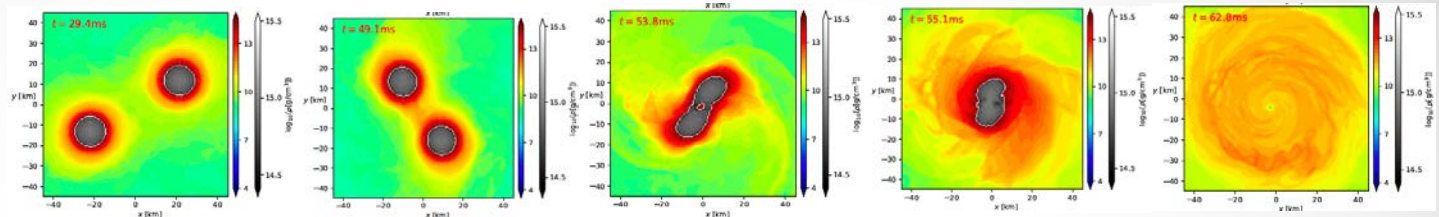
J. Read, CGWAS 2015

49 8

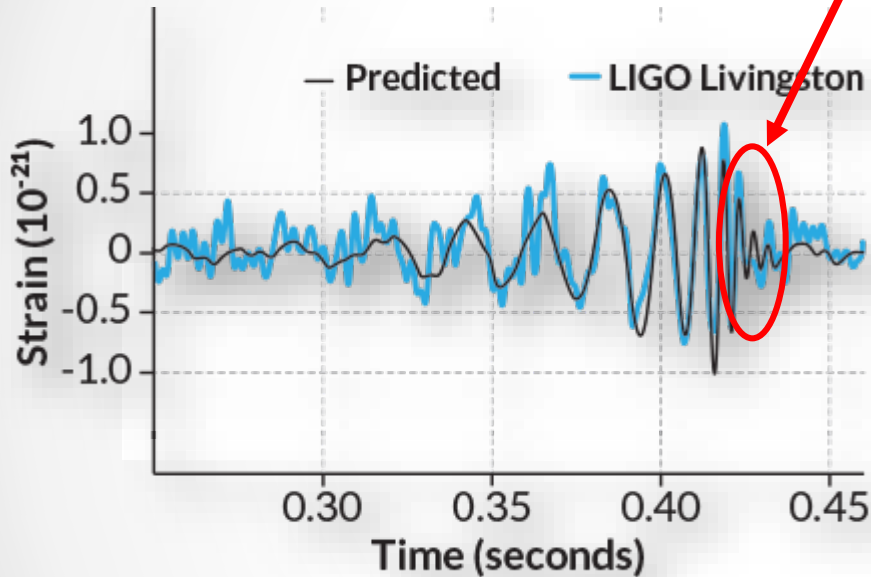
<https://www.ligo.org/detections.php>

Tidal effects: modification of the gravitational waveform wrt a GR point-particle calculation, due to the star deformation just before merging

Extraction of the tidal effects



Gieg et al., Particle 2, 23 (2010)



$$\delta\psi_{\text{tidal}} = \frac{3}{128\eta x^{5/2}} \left[\left(-\frac{39}{2} \tilde{\Lambda} \right) x^5 \right]$$

Quadrupole moment

Companion tidal field

$$\bar{Q}^{(i)} = -\Lambda_i \bar{\mathcal{E}}^{(j)}$$

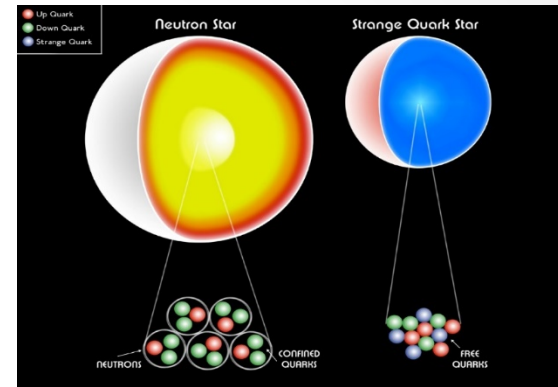
<https://www.ligo.org/detections.php>

Tidal effects: modification of the gravitational waveform wrt a GR point-particle calculation, due to the star deformation just before merging

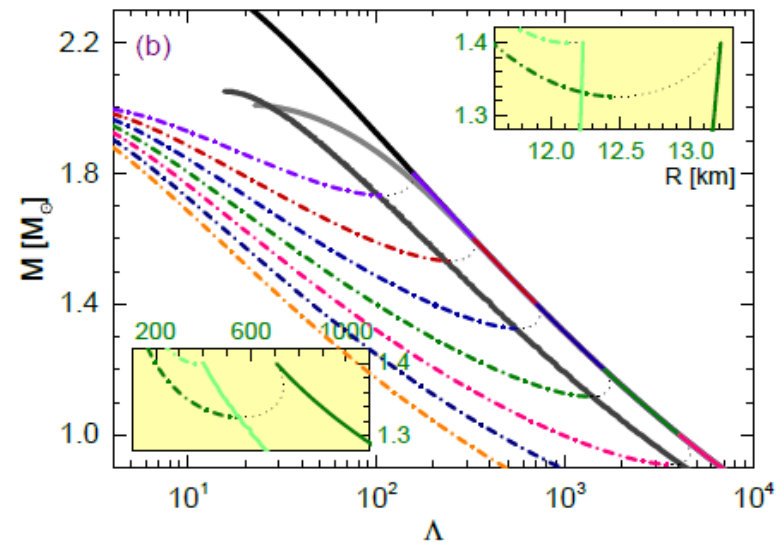
...a brief summary

$$\langle O \rangle \Leftrightarrow P(\rho)$$

- GR imposes a 1-to-1 correspondence between the nuclear EoS and static properties of NS ($M(R)$ - $M(\Lambda)$)
- Different compositions \Rightarrow different $M(\Lambda)$ \Rightarrow different gravitational signals!
- Systematics due to the astrophysical modelling in principle under control

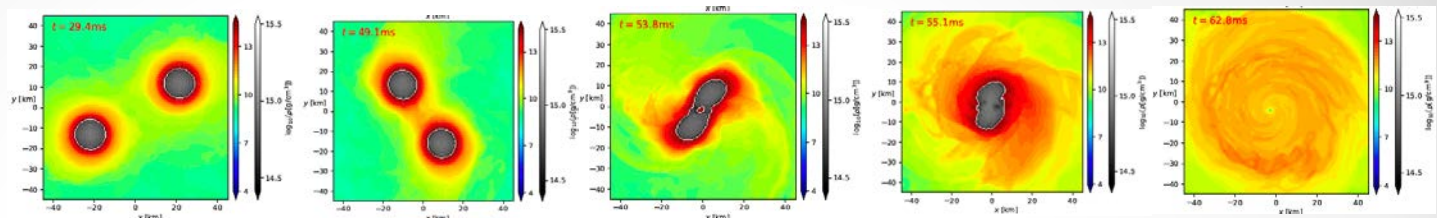


Credits: CXC/M.Weiss

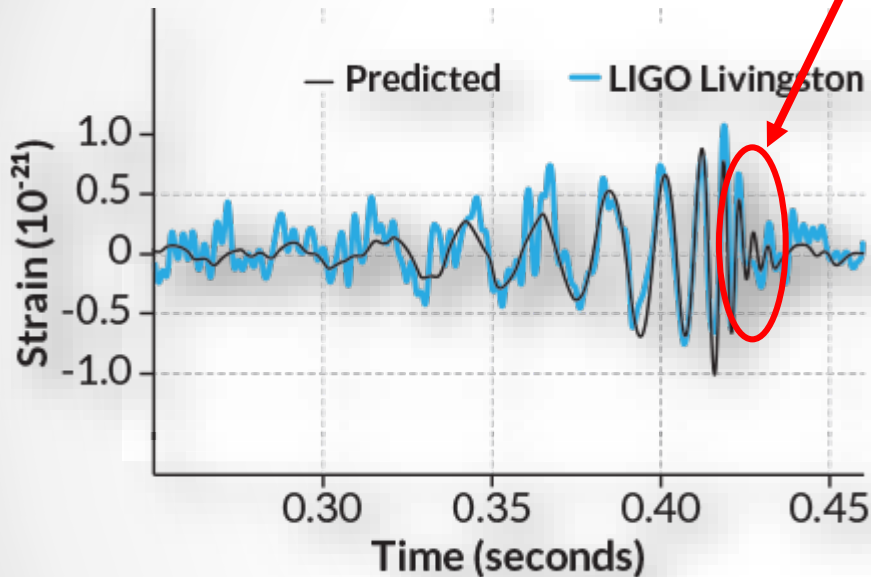


J.J.Li, A.Sedrakian, M.Alford,
PRD101 (2020) 063022

Problem 1 : the Λ info is hard to measure



Gieg et al., Particle 2, 23 (2010)



Quadrupole moment

Companion tidal field

$$\bar{Q}^{(i)} = -\Lambda_i \bar{\mathcal{E}}^{(j)}$$

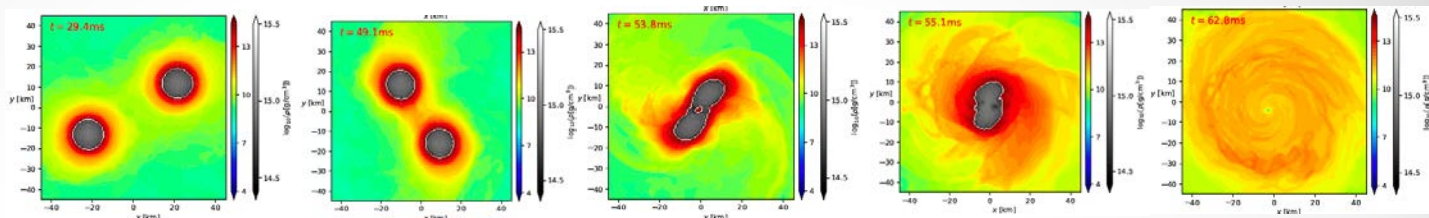
R.Wade et al., PRD89(2014)103012

$$\delta\psi_{\text{tidal}} = \frac{3}{128\eta x^{5/2}} \left[\left(-\frac{39}{2} \tilde{\Lambda} \right) x^5 + \left(-\frac{3115}{64} \tilde{\Lambda} + \frac{6595}{364} \sqrt{1-4\eta\delta\tilde{\Lambda}} \right) x^6 \right]$$

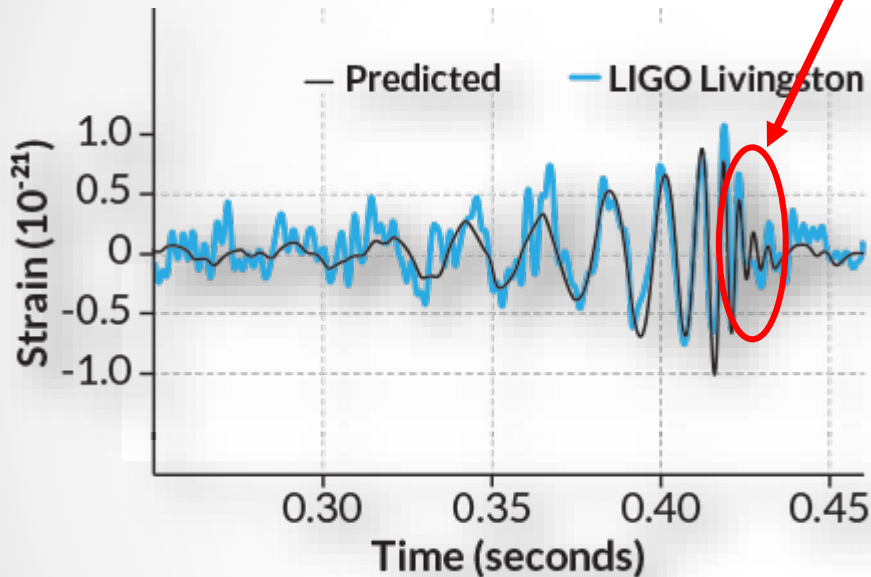
$$(\Lambda_1, \Lambda_2) \leftrightarrow (\tilde{\Lambda}, \delta\tilde{\Lambda})$$

=> Only the combined $\tilde{\Lambda}$ is measurable, and with error bars

Problem 1 : the Λ info is hard to measure



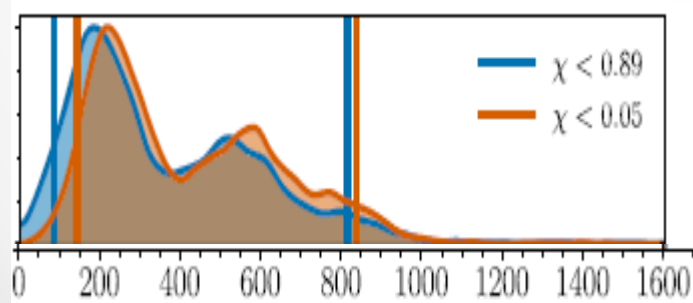
Gieg et al., Particle 2, 23 (2019)



Quadrupole moment

Companion tidal field

$$\bar{Q}^{(i)} = -\Lambda_i \bar{\mathcal{E}}^{(j)}$$



LVC, PRX 9 (2019), 011001

$$(\Lambda_1, \Lambda_2) \leftrightarrow (\tilde{\Lambda}, \delta\tilde{\Lambda})$$

=> Only the combined $\tilde{\Lambda}$ is measurable, and with error bars

Problem II : no ab-initio theory of dense matter

=> Density Functional Approach

$\varepsilon_{tot} = \varepsilon_B + \varepsilon_L$ (baryons and leptons decoupled, leptons free FG)

• **NS core:** $\rho_q(r) = \rho_q$ ($\forall q$ constituent)

• **Effective single particles:** $e_q(k) = \sqrt{m_q^*{}^2 + k^2} + V_q(\rho_q, \rho_{q'})$

$\Rightarrow m_q^*, V_q$ from an effective Hamiltonian (Skyrme, Gogny, M3Y..) or Lagrangian (RMF)

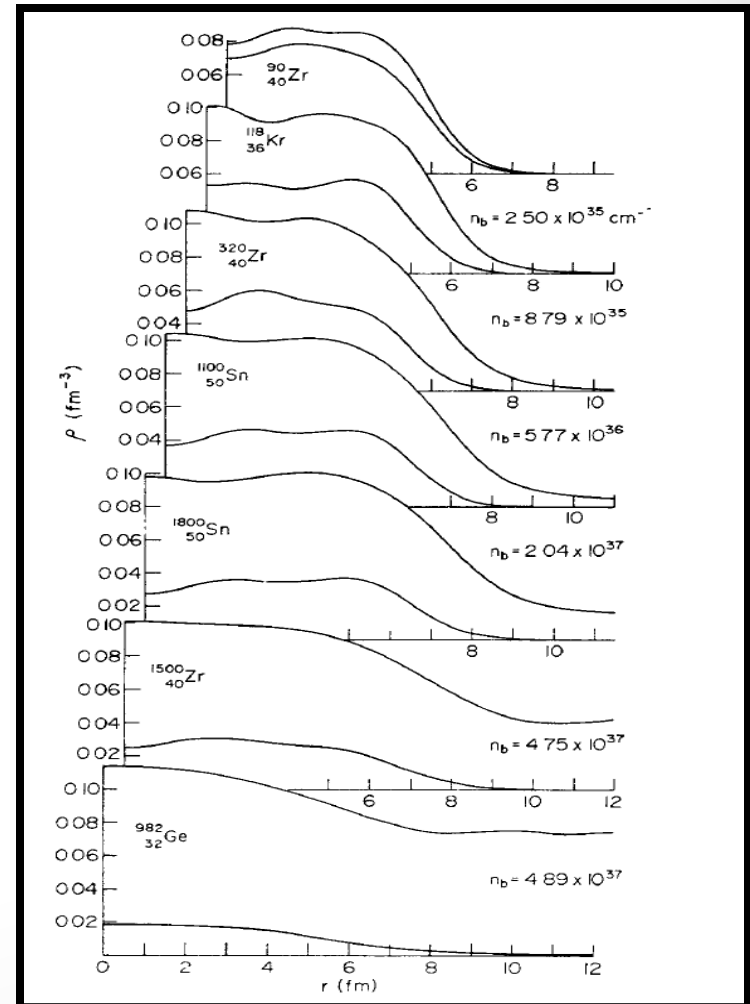
\Rightarrow Coupling constants fitted on nuclear data and/or ab-initio calculations

$\Rightarrow e(\rho_B, \rho_L, \rho_S) \quad P(\rho) = -\rho_B^2 \left. \frac{\partial e}{\partial \rho_B} \right|_{\mu_L=0, \mu_S=0}$

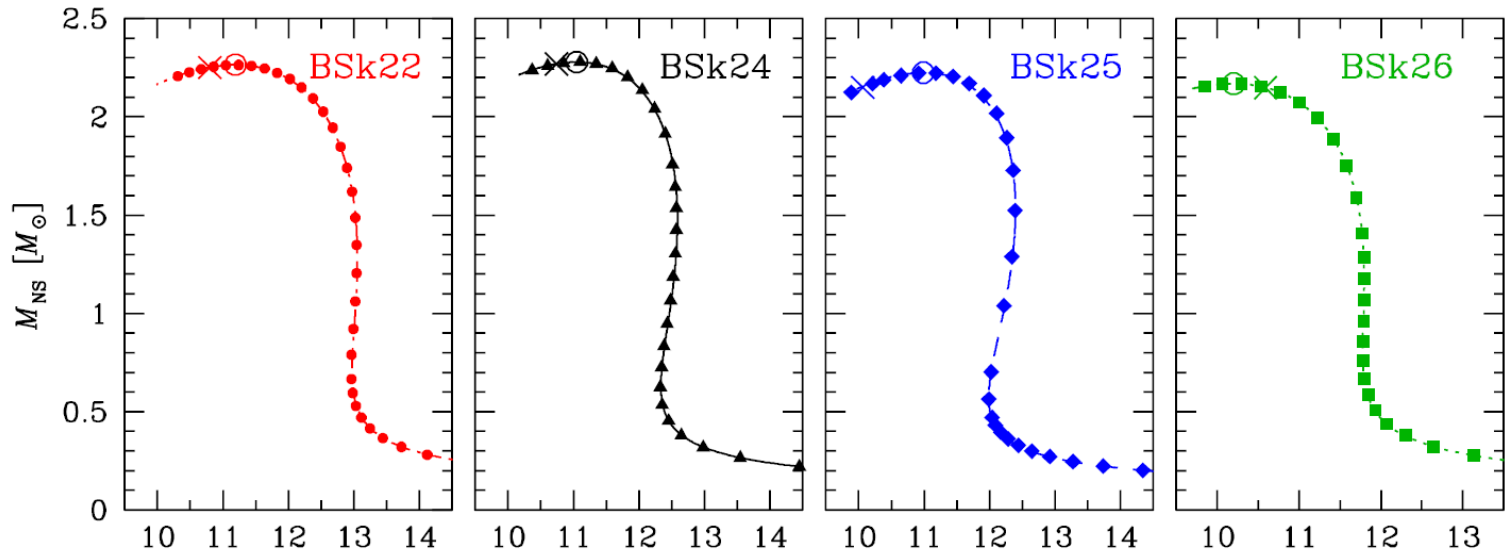
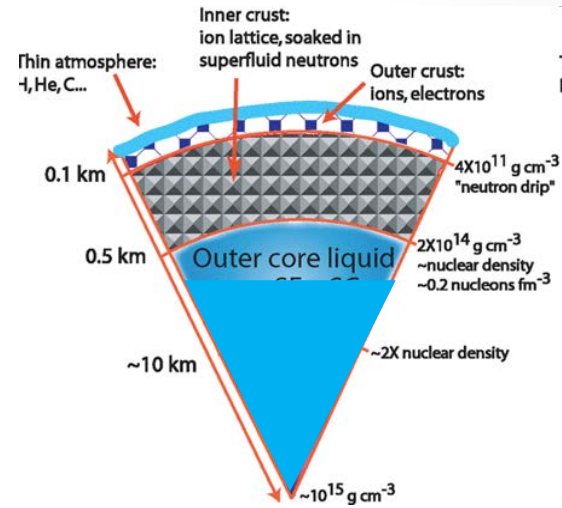
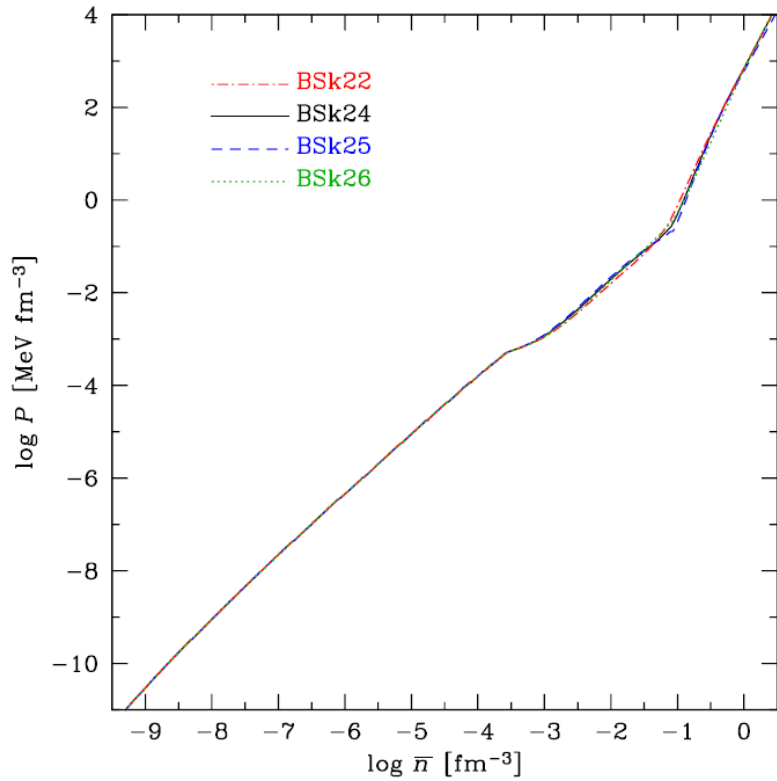
Problem II : no ab-initio theory of dense matter

=> Density Functional Approach

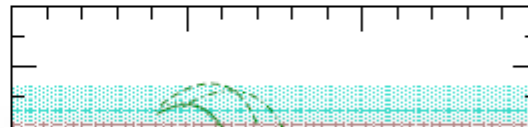
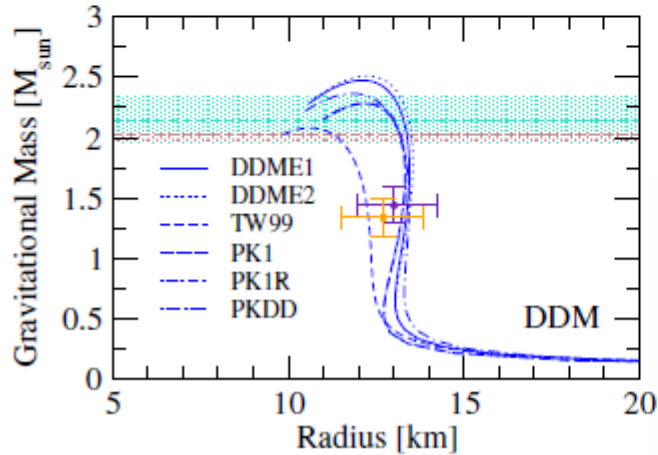
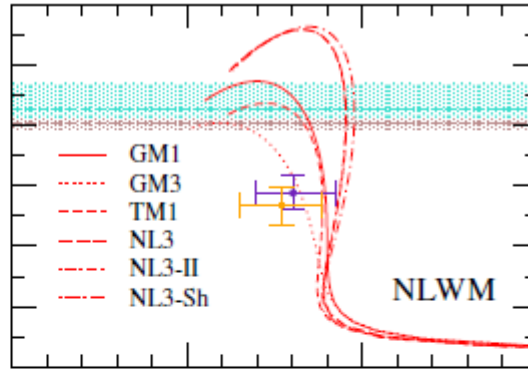
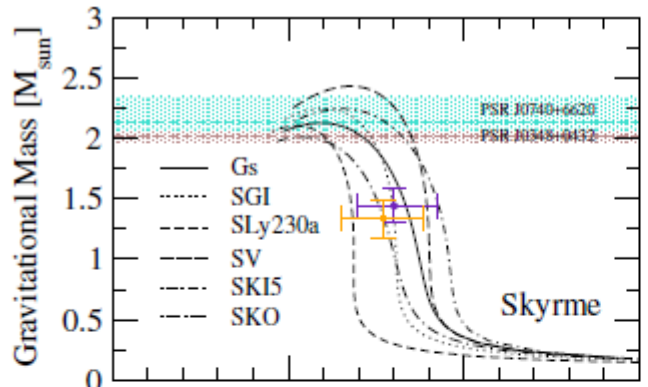
- **NS crust: $q=n,p$** variational calculation of the single particle wave-functions => $\rho_q(r)$ within the Hartree-Fock-(Bogoliubov) theory



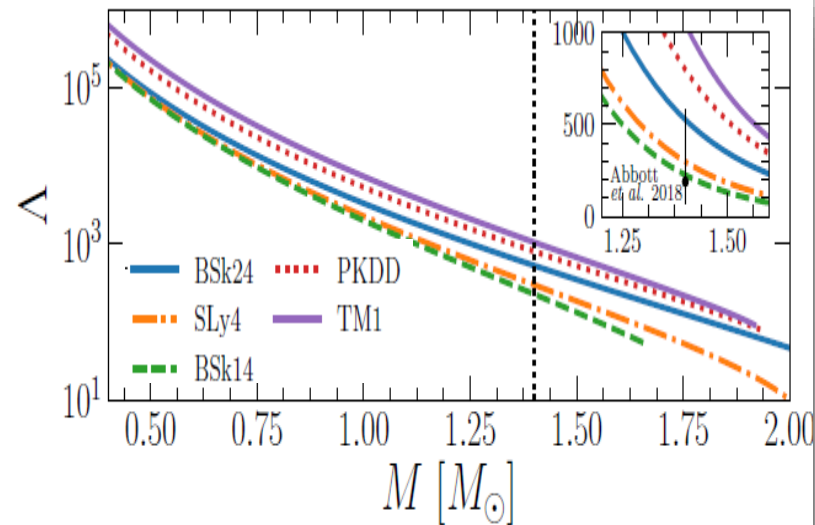
An example: the Brussels-Montreal functionals BSk



Problem 11 : no ab-initio theory of dense matter



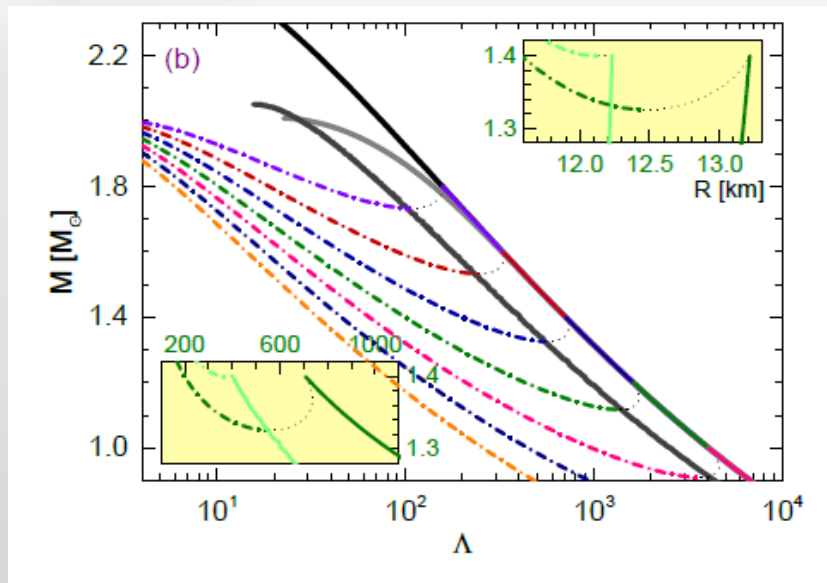
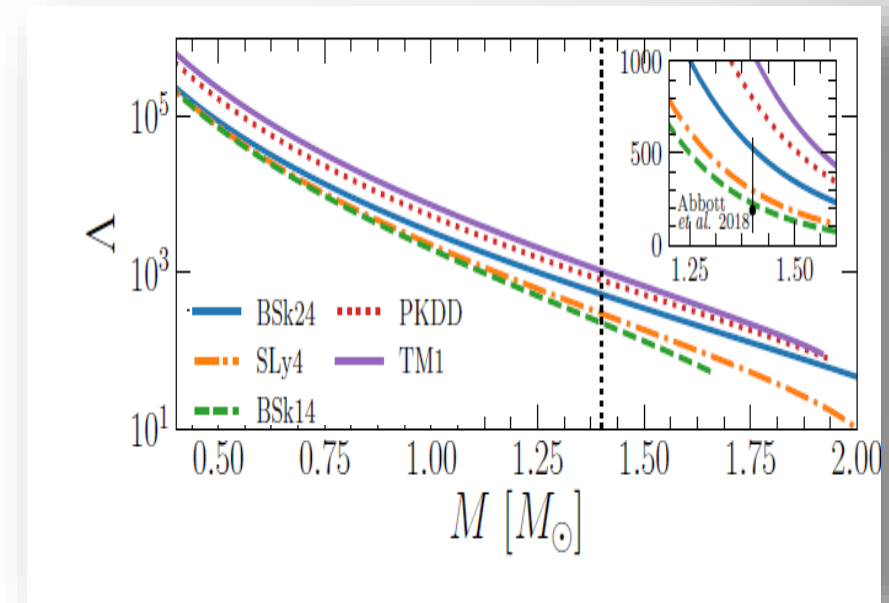
- **Model dependence: choice of functional form (Lagrangian versus Hamiltonian) and fitting protocol lead to different predictions**



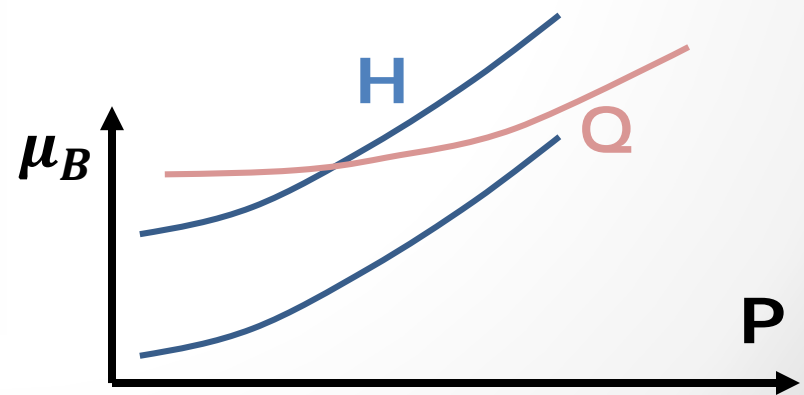
F.Burgio, I.Vidana,
Universe 2020, 6,
119

Problem II : no ab-initio theory of dense matter

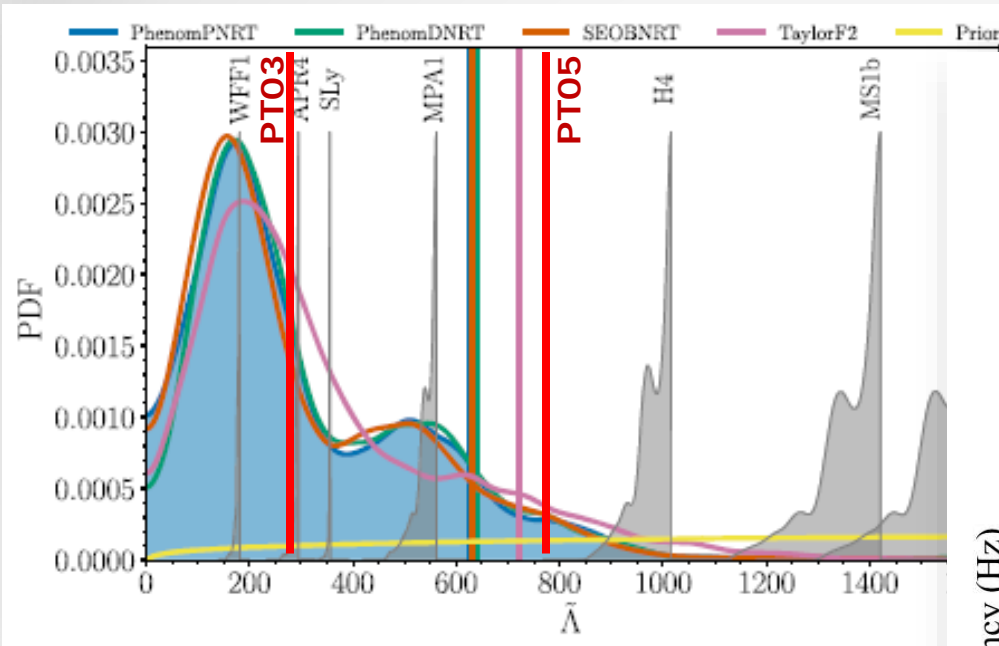
- Hybrid stars: a first order phase transition between a nucleonic (RMF, Skyrme..) and a quark ((p)NJL, Bag, CSS...) EoS
- Huge uncertainties on both the Q and the H side!!



J.J.Li, A.Sedrakian, M.Alford,
PRD101 (2020) 063022

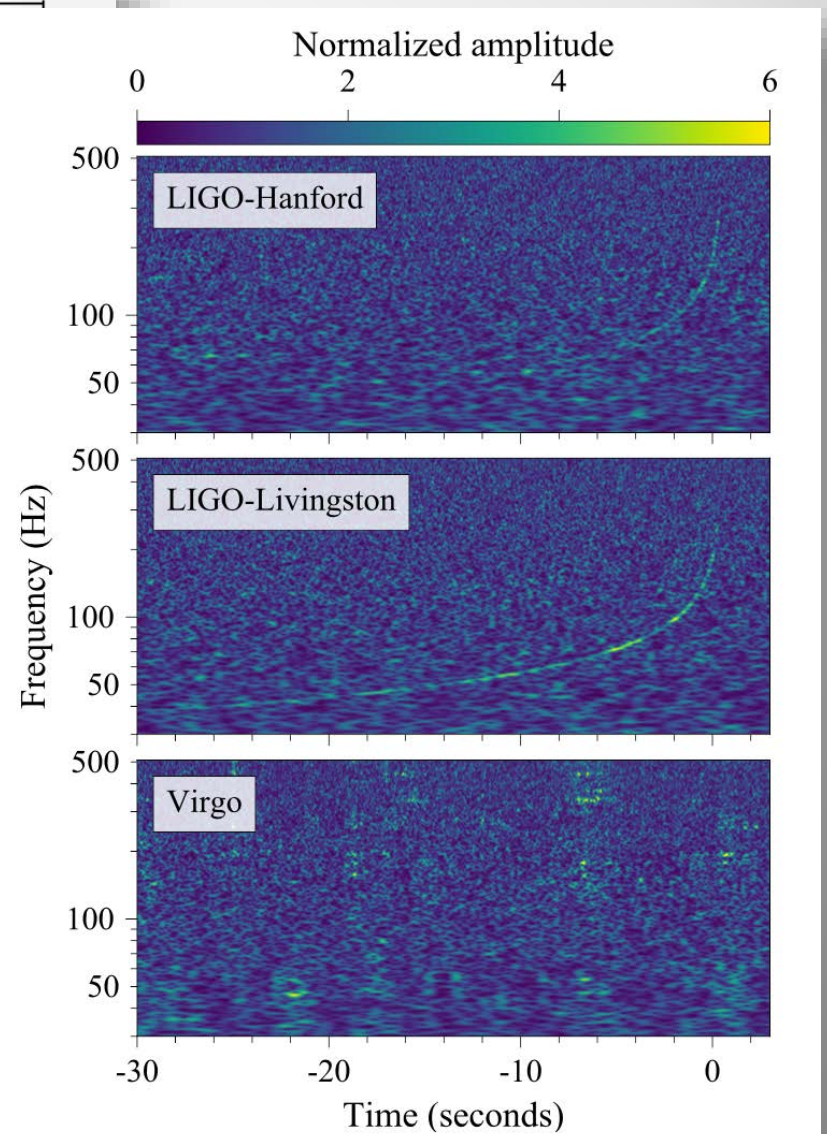


Present status: GW170817



LVC, APJL2017 & PRX9 2019

- The observation cannot discriminate



Problem II : no *ab-initio* theory of dense matter

⇒ Nucleonic « *ab-initio* » approach

⇒ 2- and 3-body interactions from chiral perturbation theory

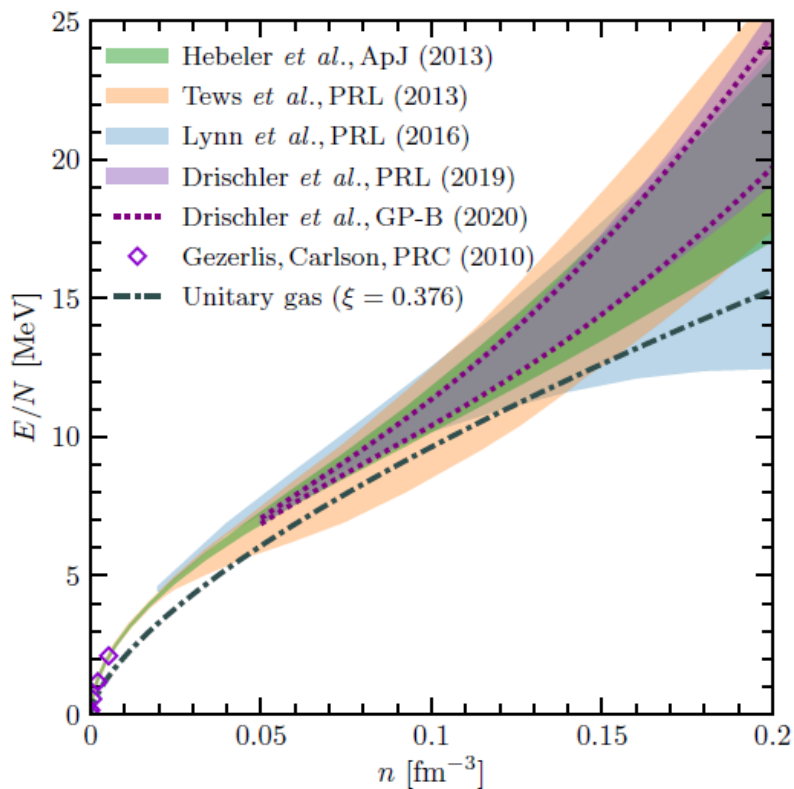
⇒ GS from beyond-MF many body techniques (variational, CC, MBPT, QMC...)

⇒ Coupling constants fitted on scattering data and light nuclei

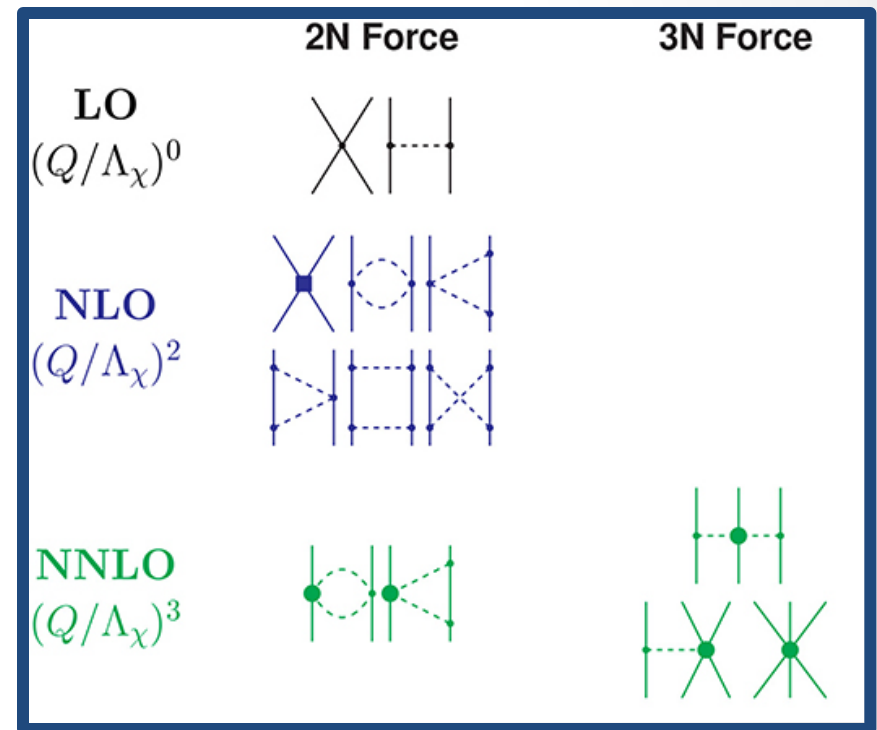
$$\Rightarrow e(\rho_n, \rho_p) \quad P(\rho) = -\rho_B^2 \left. \frac{\partial e}{\partial \rho_B} \right|_{\mu_n - \mu_p = \mu_e}$$

Nucleonic « ab-initio » approach

- Diagrammatic expansion: controlled uncertainties!
- Still, power counting & regularization valid only up to $\sim 2\rho_0$
- Extrapolations needed

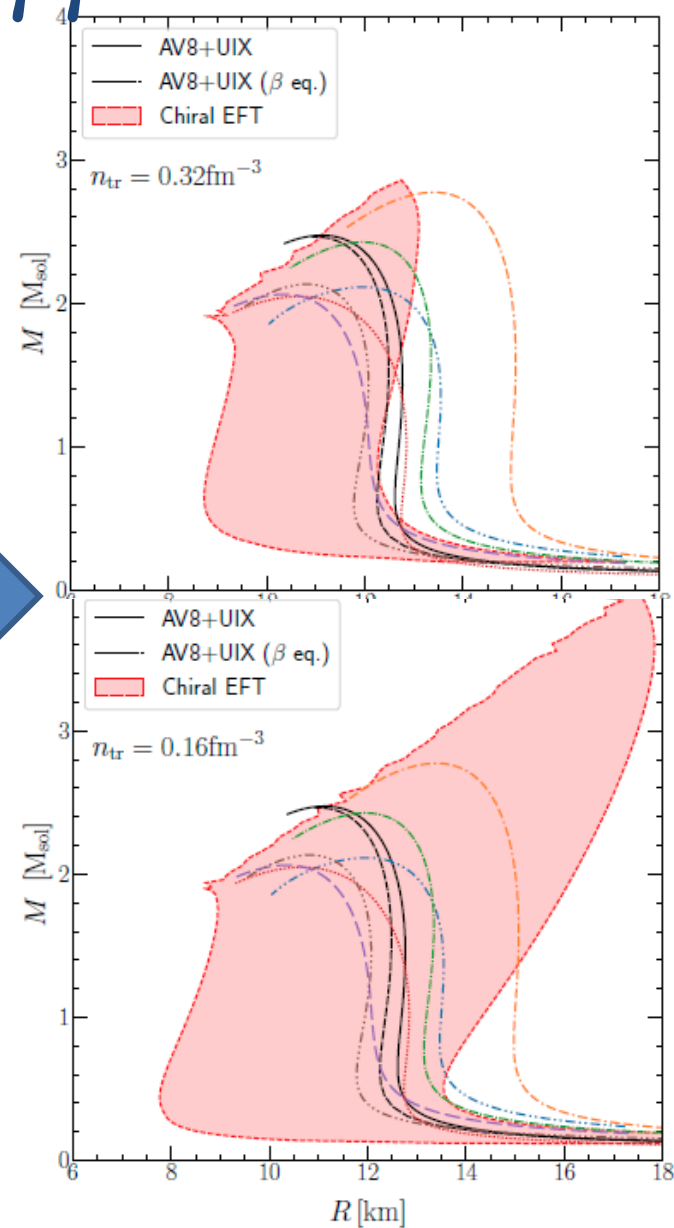
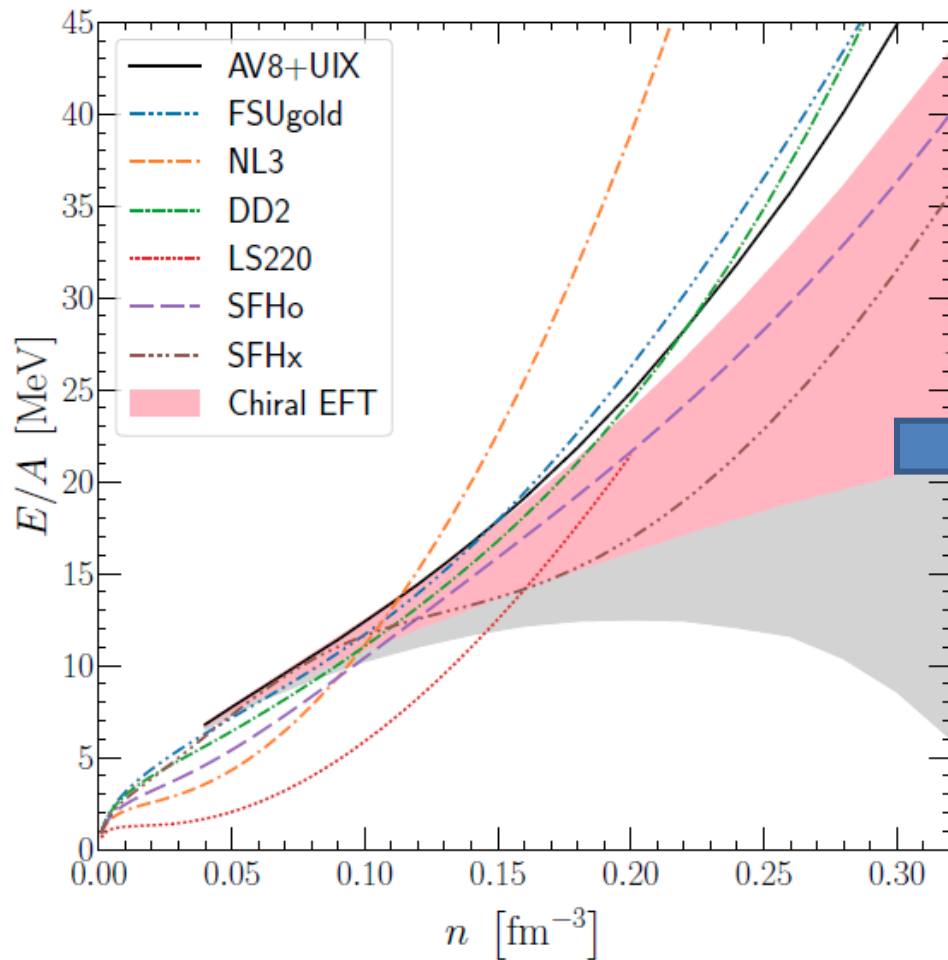


Machleidt R., Int J Mod Phys. (2017)

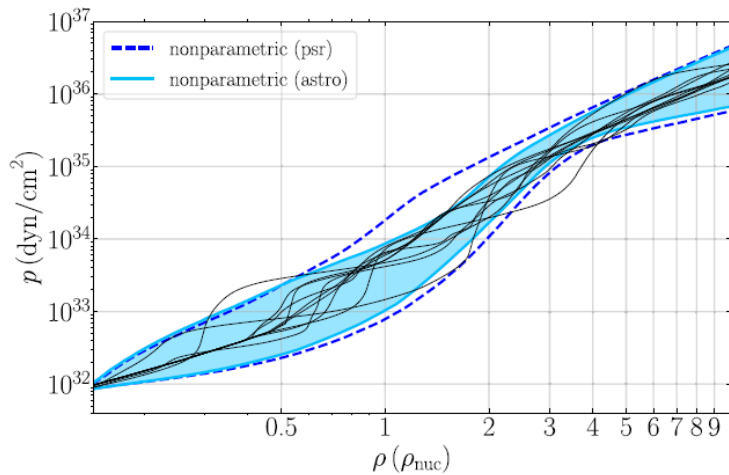
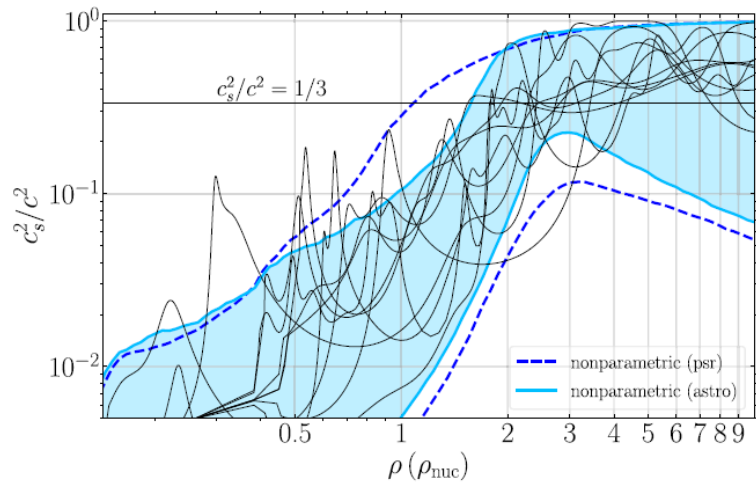


Nucleonic « ab-initio » approach

Tews, Carlson, Gandolfi, Reddy 2018



The inversion strategy



- Agnostic EoS only respecting causality and thermodynamical stability
- Example: non-parametric EoS from Gaussian Process

$$\phi(p) = \log \left(\frac{c^2}{c_s^2} - 1 \right) = N \left(\mu(p_i), K(p_i, p_j) \right)$$

- Bayesian inference

$$P(EoS | \vec{f}) = \frac{P(EoS) \prod_i P(f_i | EoS)}{P(\vec{f})}$$

f₁. max.mass (radio)

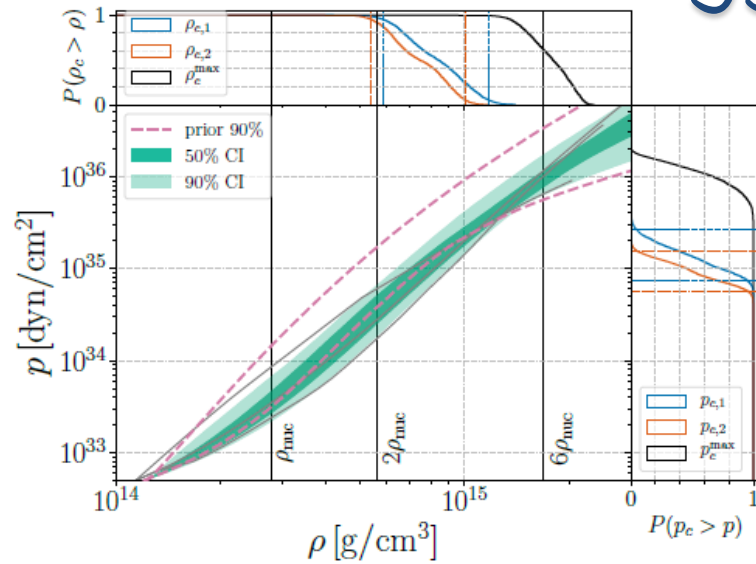
f₂. tidal polarisability (GW)

f₃. radius (X-ray)

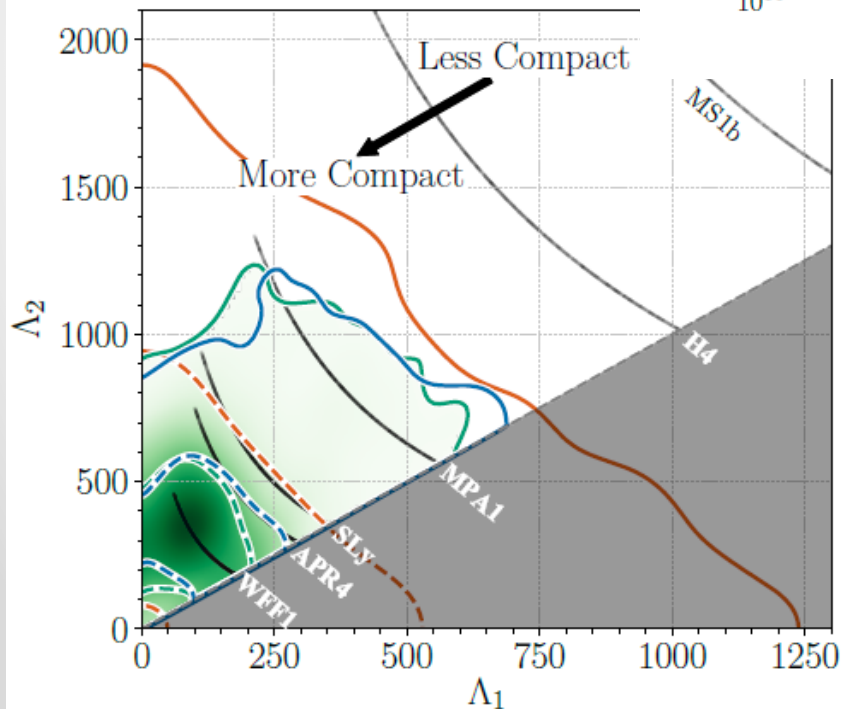
P. Landry and R. Essick, PRD 99, 084049 (2019)

I. Legred et al PRD105, 043016 (2022)

The inversion strategy



A. Abbott et al, PRL 2018

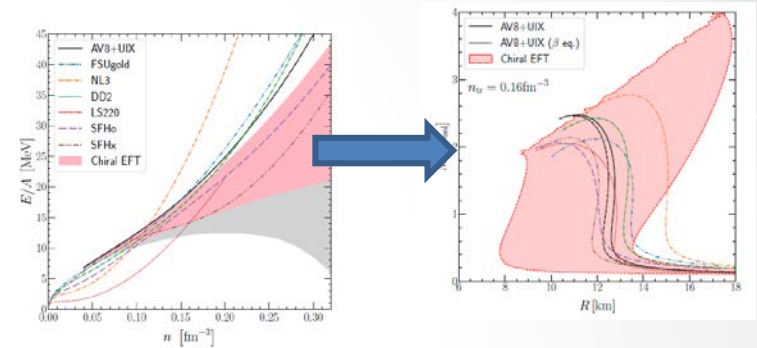


- (Almost) model independent evaluation of the EoS
- Still, we do not learn much about nuclear physics
- We do not exploit our nuclear physics knowledge either

...a brief summary $\langle O \rangle \Leftrightarrow P(\rho)$

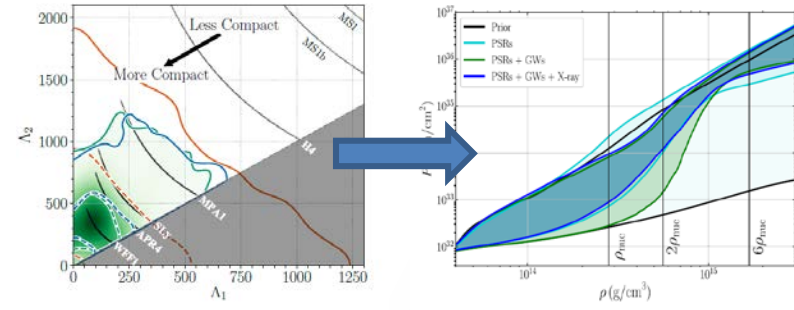
The nuclear physicist viewpoint: $e(\rho_n, \rho_p) \Rightarrow P(\rho) \Rightarrow \langle O \rangle$

- Controlled dof, hypotheses and approximations, exp data included
- Still, the predictive power is limited



The astrophysicist viewpoint: $\langle O \rangle \Rightarrow P(\rho)$

- Non-parametric representation: model independent evaluation of the EoS
- Still, we do not learn much about nuclear physics



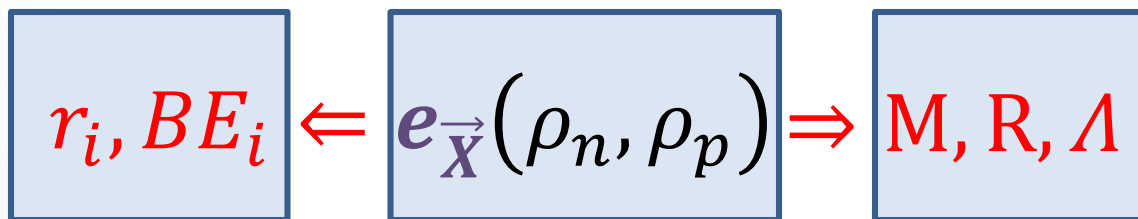
A nuclear-astrophysicist viewpoint: meeting in the middle...

General EoS modelling: the syllabus

- A flexible analytic representation $e_{\vec{X}}(\rho_n, \rho_p)$: the variation of the parameter set \vec{X} allows reproducing the different nuclear models and interpolating among them ~ 15 parameters – RMF and EDF version
- The X_i variation explores the equation of state space compatible with the hypothesis of a matter of neutrons and protons

$$P(\rho) = -\rho^2 \left. \frac{\partial e(\rho_n, \rho_p)}{\partial \rho} \right|_{\mu_L=0}$$

A.Steiner et al ApJ 2010
A.Bulgac et al 2016
J.Margueron et al PRC 2018
Y. Lim, J.W. Holt, PRL 2018
C.Mondal et al, PRC 2022
P.Char et al, PRD 2023



Laboratory
observables

~~EoS~~
Nuclear model

Astronomical
observables

Bayesian Inference

$$P(\vec{X}|\vec{f}) = \frac{P(\vec{X}) \prod_i P(f_i|\vec{X})}{P(\vec{f})} \quad (+\text{MCMC or Nested Sampling})$$

- f_1 . nuclear data
- f_2 . ab-initio theory

} **Nuclear physics**

- f_3 . max.mass (radio)
- f_4 . tidal polarisability (GW)
- f_5 . radius (X-ray)

} **Astrophysics**

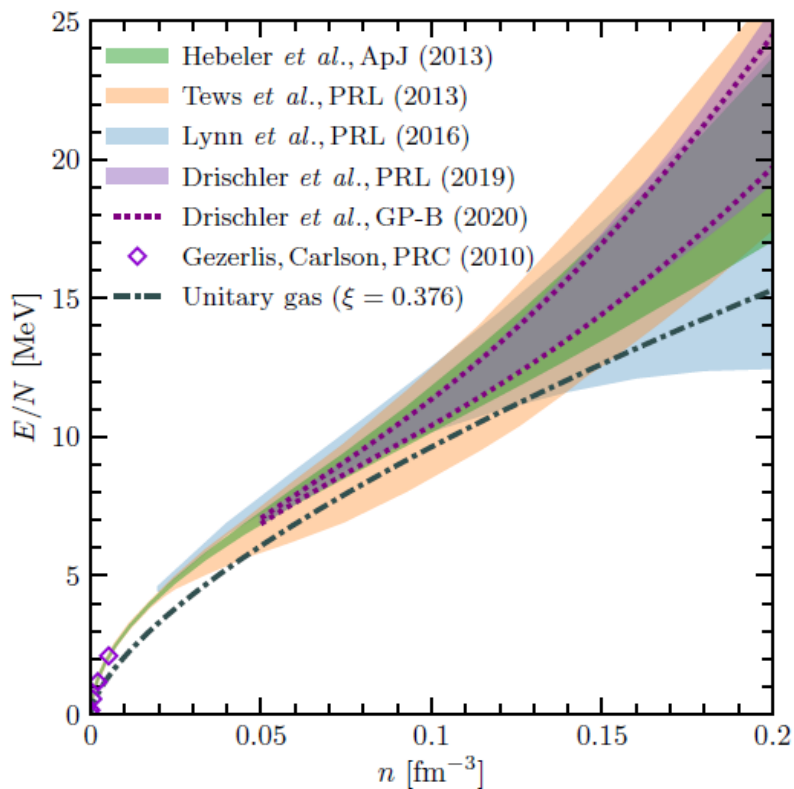
(3) PSR J0348+0432 $M=2.01\pm 0.04 M_{\odot}$

(4) GW170817 $\tilde{\Lambda}(M)$ LVK

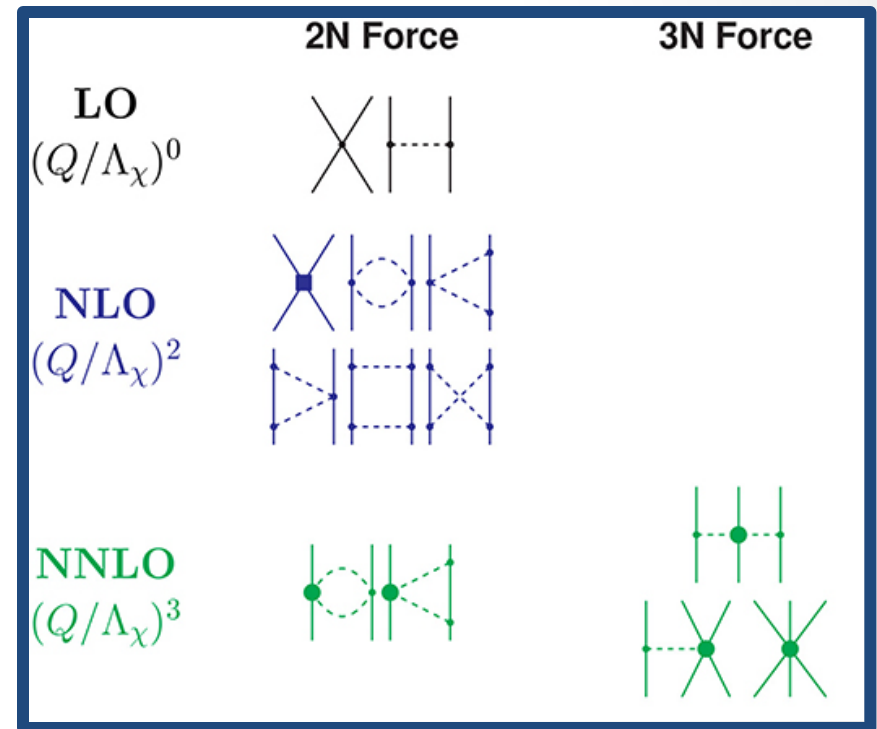
(5) PSR J0030+0451, PSR J0740+6620 NICER

Ab-initio nuclear theory

- interaction from χ -EFT, different many body methods (MBPT, AFMC)
- Diagrammatic expansion : controlled truncation errors
- Moment expansion! Only valid at low density



Machleidt R., Int J Mod Phys. (2017)



- S. Huth, C. Wellenhofer, and A. Schwenk, Phys. Rev. C 103, 025803 (2021).

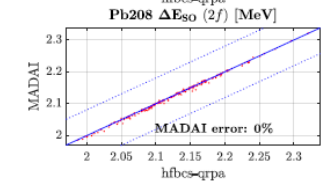
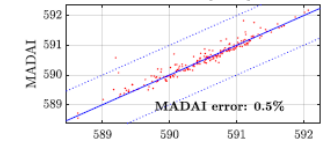
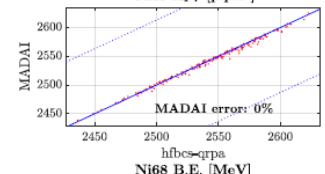
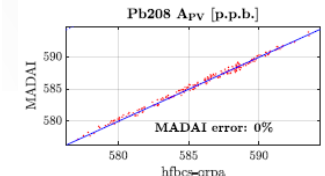
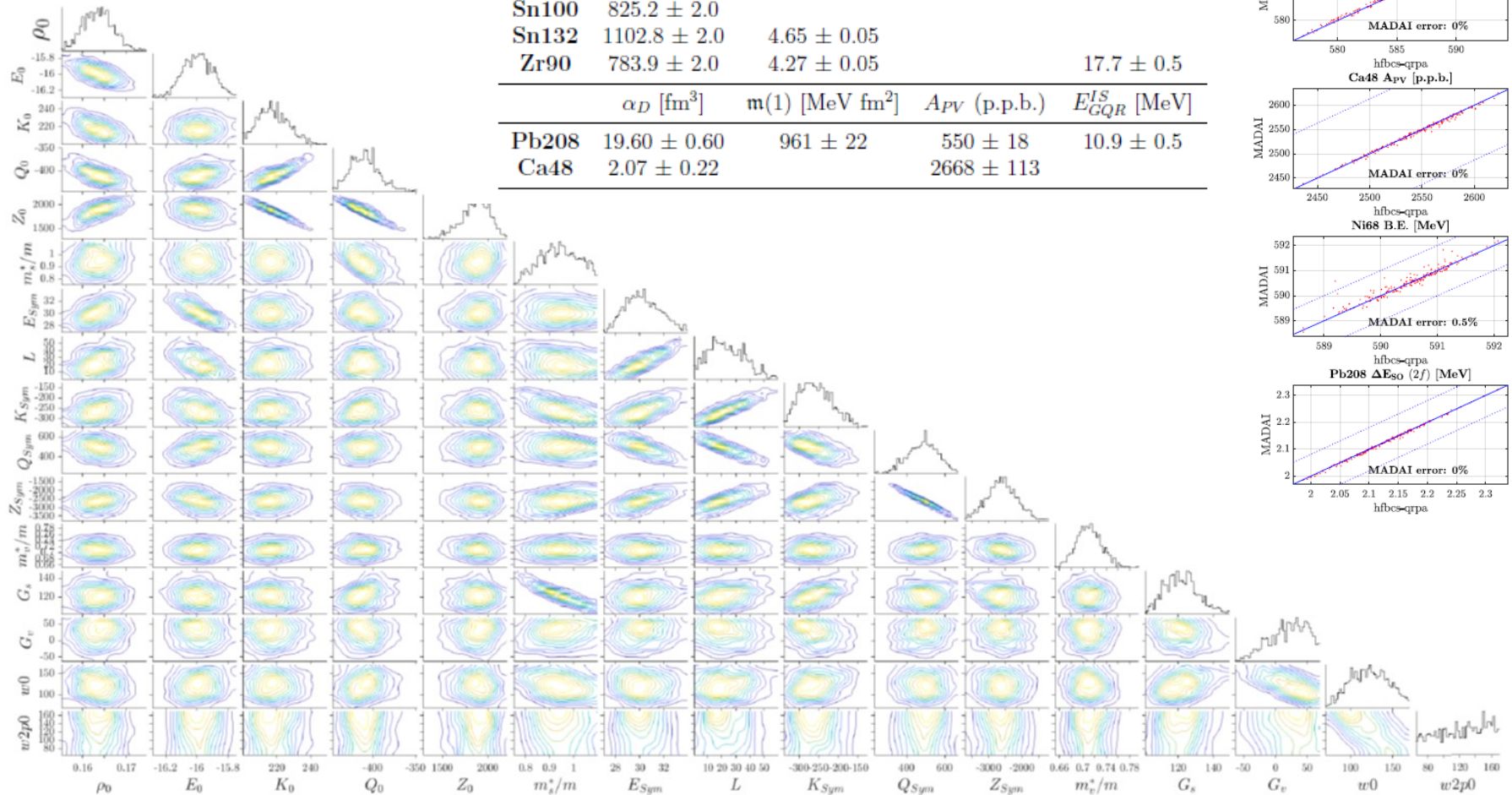
Laboratory experiments

P.Klausner, X.Roca Maza, G.Colo,
to be published

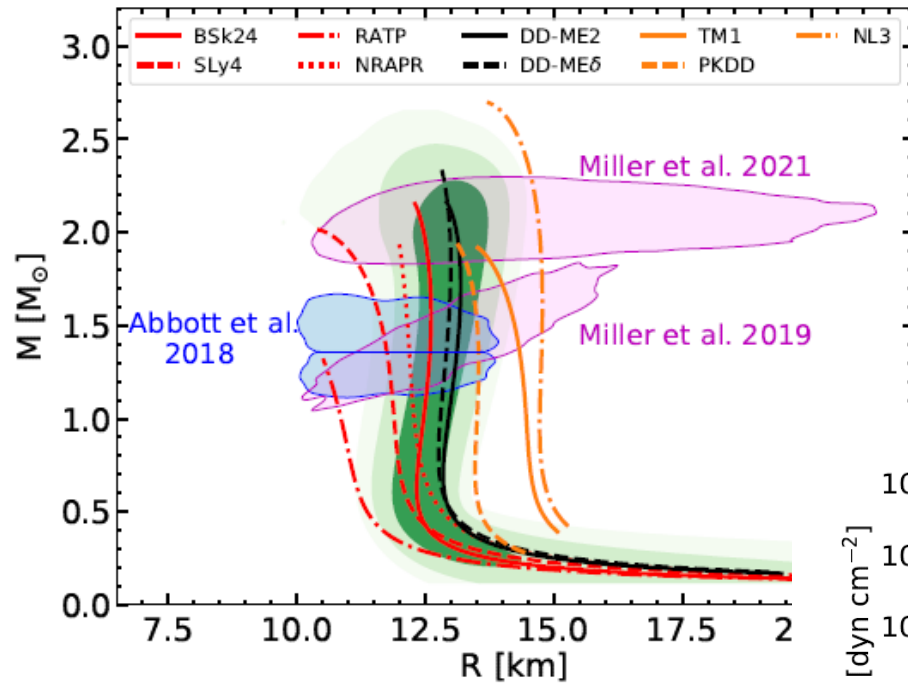
	$B.E.$ [MeV]	R_{ch} [fm]	ΔE_{SO} [MeV]	E_{GMR}^{IS} [MeV]
Pb208	1636.4 ± 2.0	5.50 ± 0.05	2.02 ± 0.50	13.5 ± 0.5
Ca48	416.0 ± 2.0	3.48 ± 0.05	1.72 ± 0.50	
Ca40	342.1 ± 2.0	3.49 ± 0.05		
Ni56	484.0 ± 2.0			
Ni68	590.4 ± 2.0			
Sn100	825.2 ± 2.0			
Sn132	1102.8 ± 2.0	4.65 ± 0.05		
Zr90	783.9 ± 2.0	4.27 ± 0.05		17.7 ± 0.5

	α_D [fm ³]	$m(1)$ [MeV fm ²]	A_{PV} (p.p.b.)	E_{GQR}^{IS} [MeV]
Pb208	19.60 ± 0.60	961 ± 22	550 ± 18	10.9 ± 0.5
Ca48	2.07 ± 0.22		2668 ± 113	

madai.phy.duke.edu

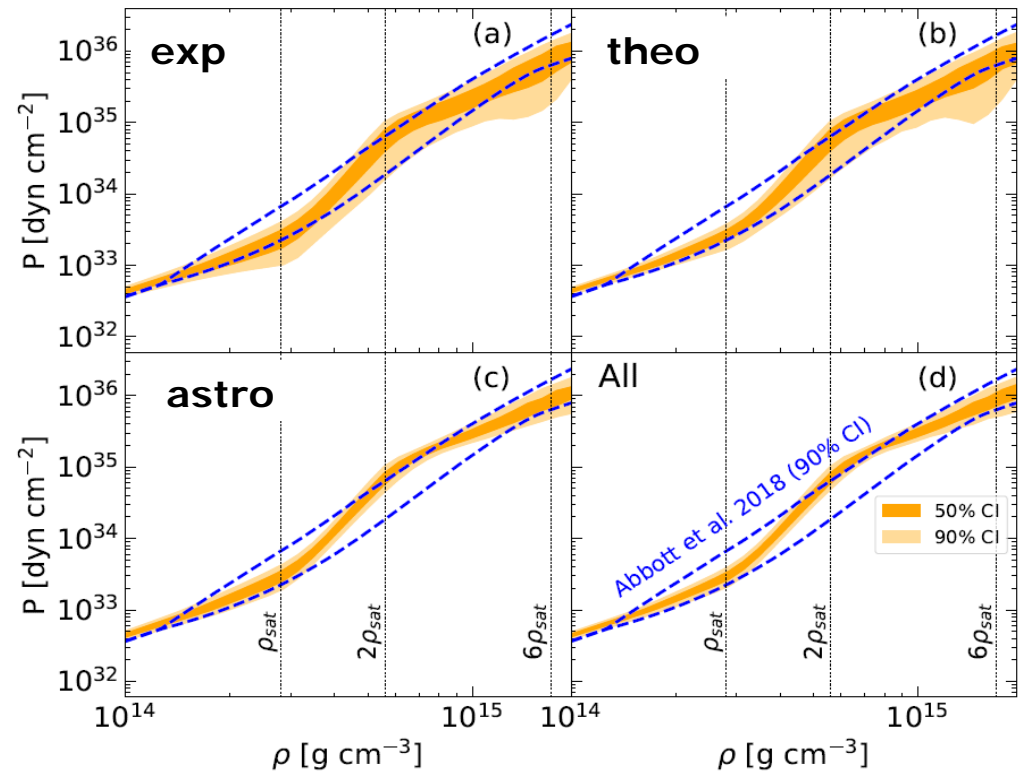


Nuclear physics informed predictions

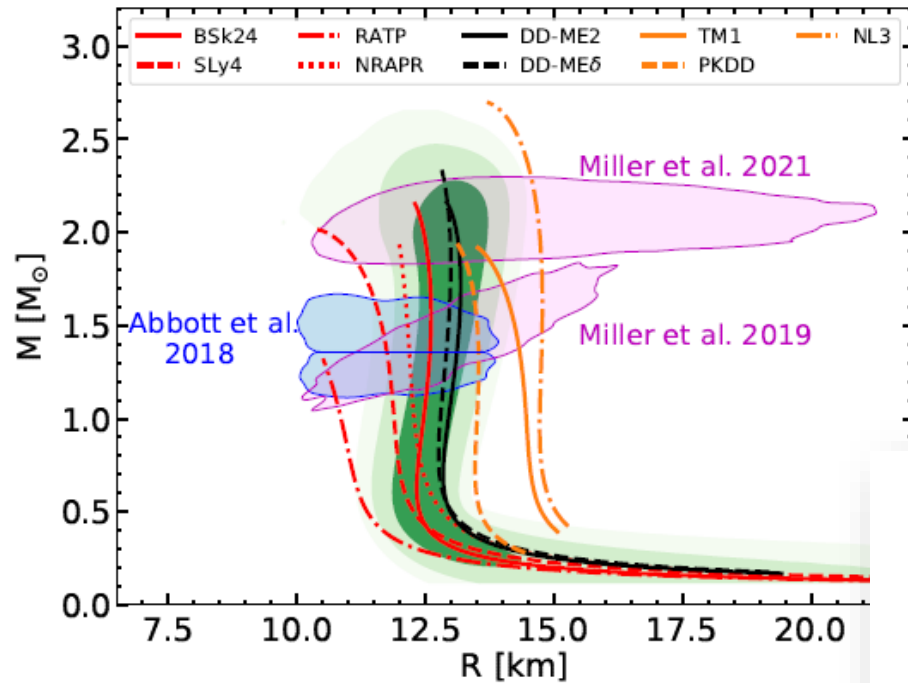


H.Dinh Thi et al, A&A 2021

- Nuclear constraints are very important up to $\sim 2n_{\text{sat}}$
- Many models can be excluded
- A neutrons and protons composition is compatible with the observations

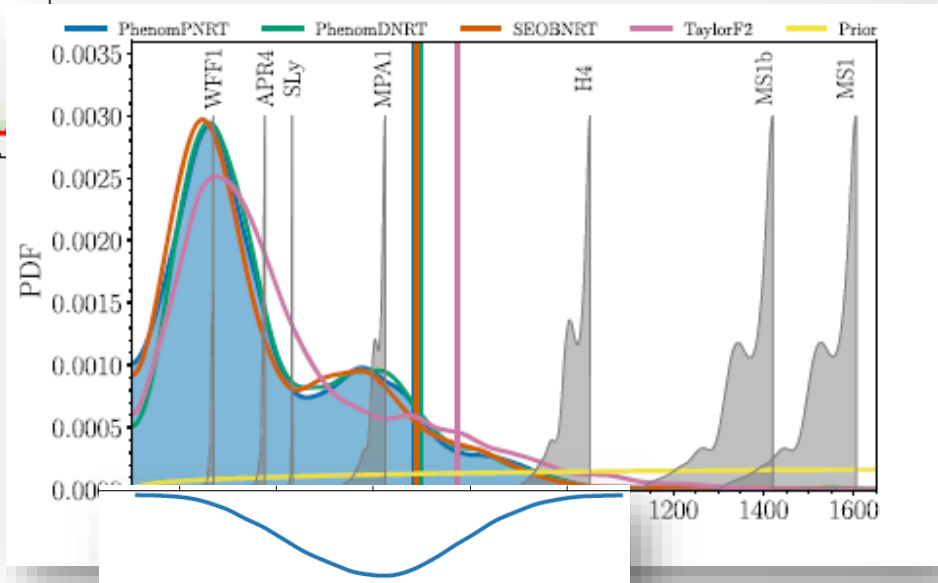


Nuclear physics informed predictions

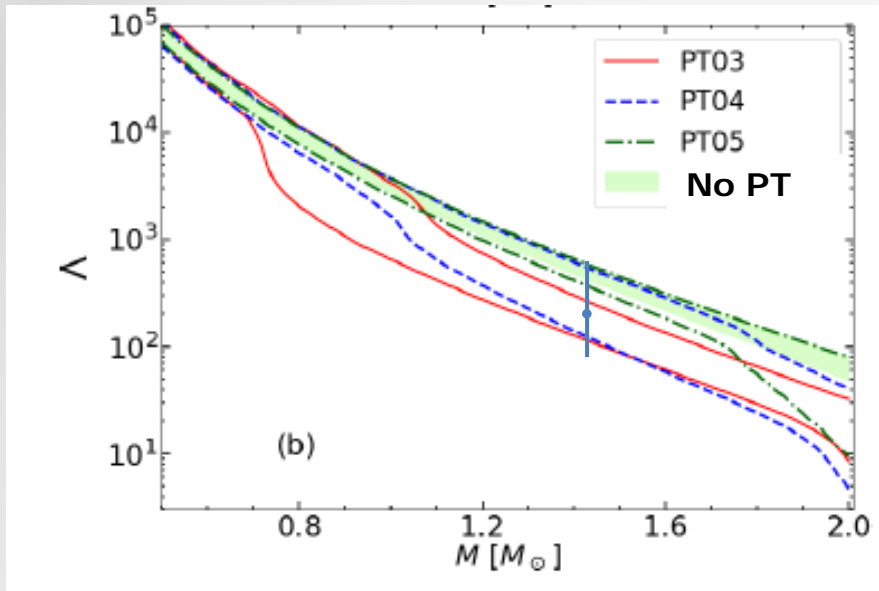


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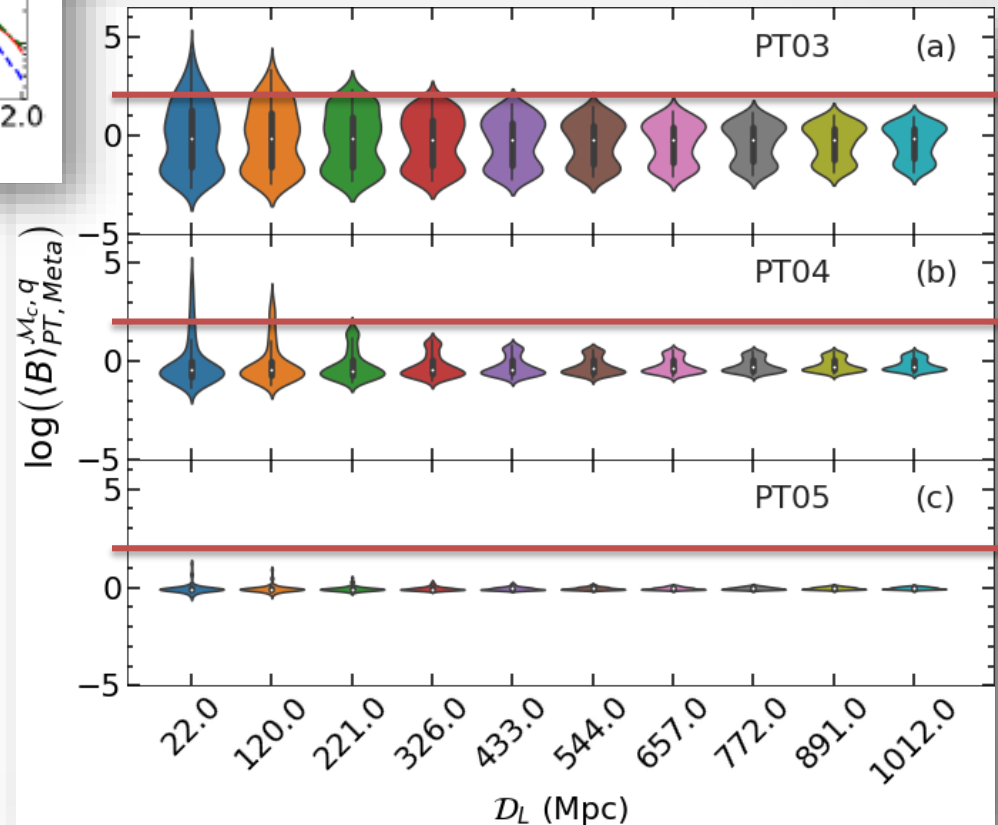
Quarks in the core of neutron stars ?



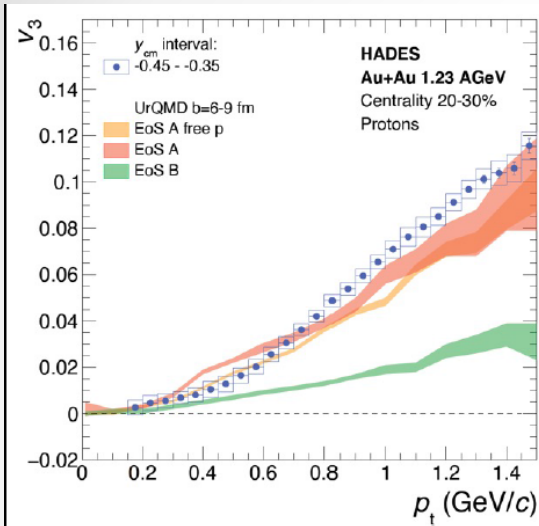
- Even with AdV+ sensitivity, only a very close detection would allow identifying deconfined matter, and only if the quark core is large

C.Mondal et al, MNRAS 2023

- Need to reduce the uncertainties!
 - New nuclear observables
 - Multiple detections with better SNR => Einstein Telescope, Cosmic Explorer

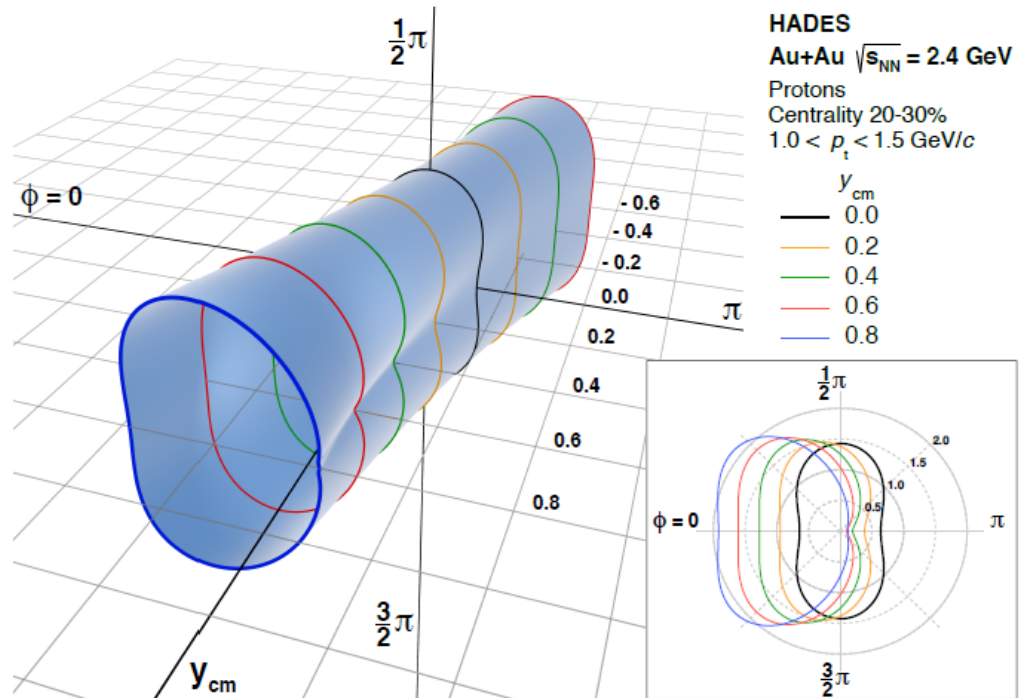
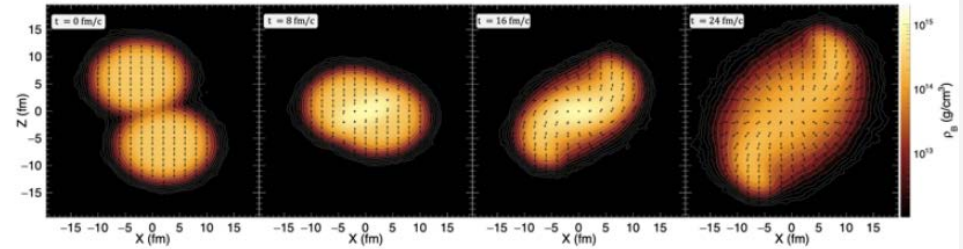


The HI collisions probe

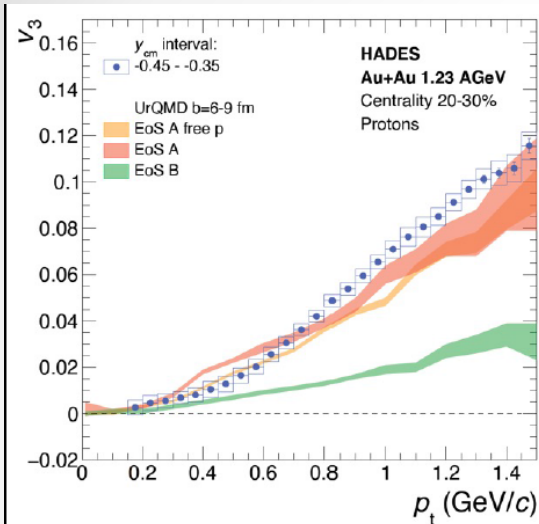


HADES collaboration
PRL 125 (2020)
262301

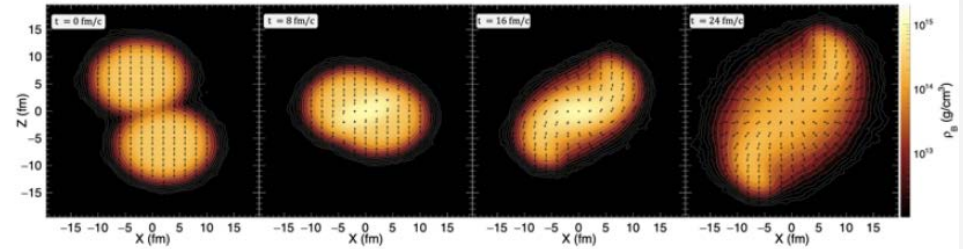
Au+Au $\sqrt{s_{NN}} = 2.4$ GeV (UrQMD)
 $\phi = 16$ fm $\tau \sim 10^{-23}$ s



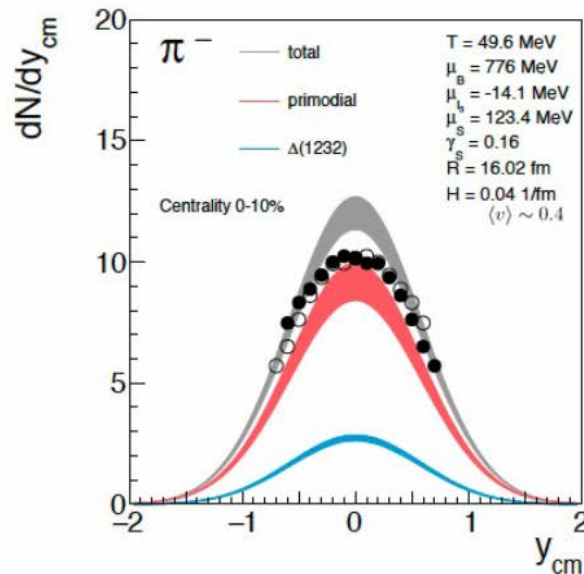
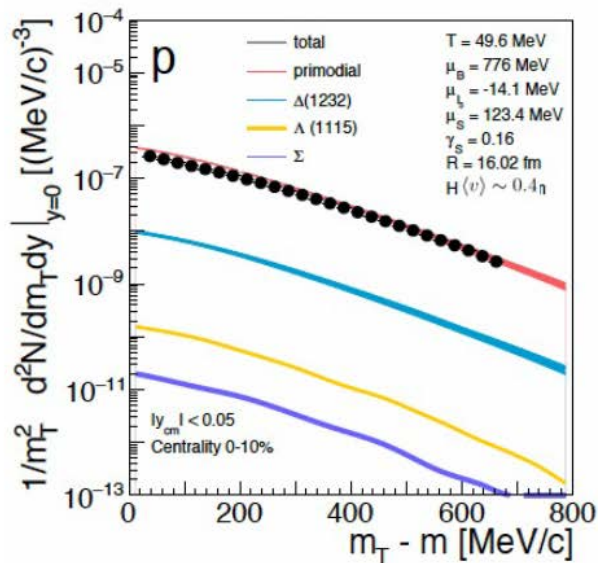
The HI collisions probe



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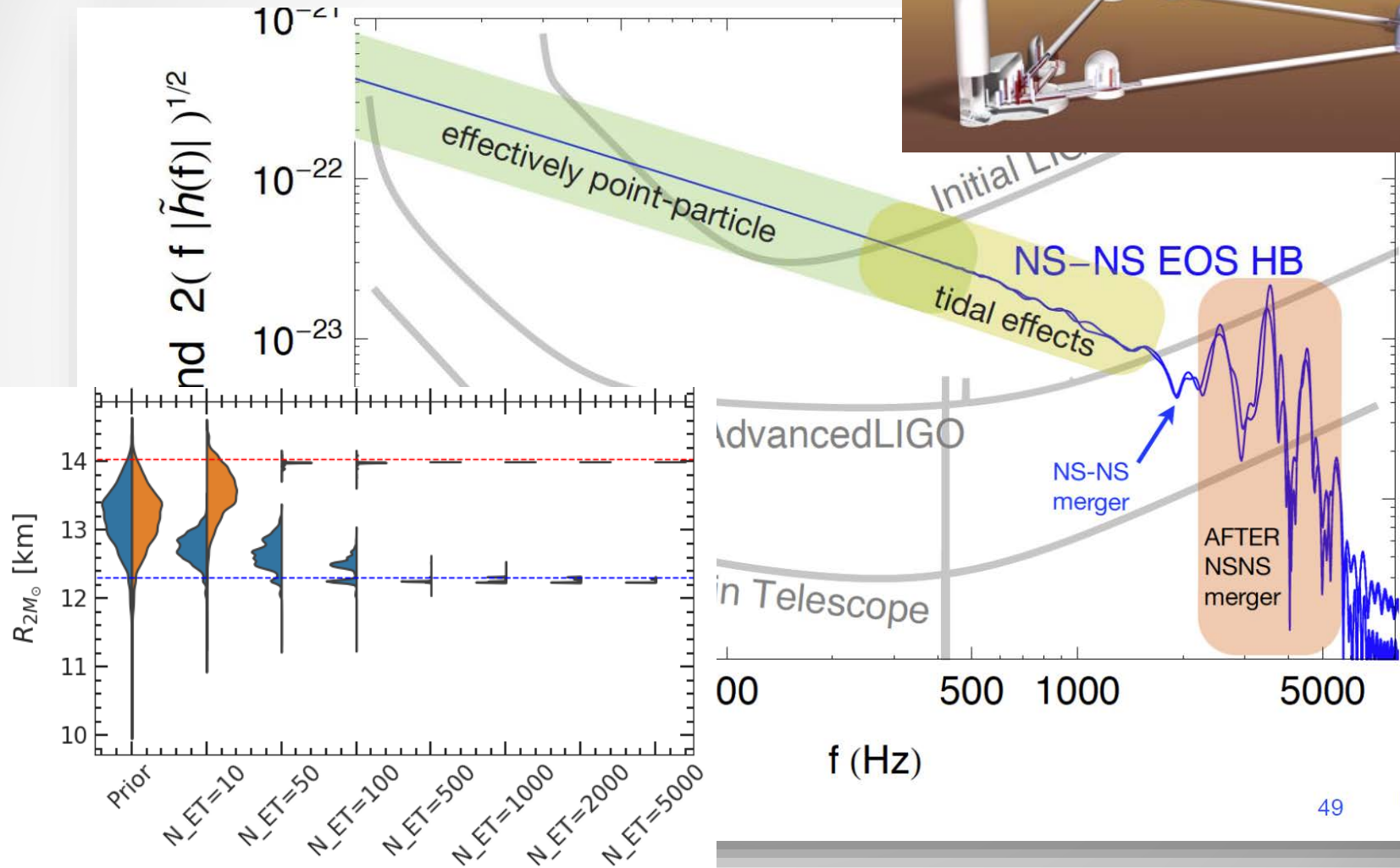
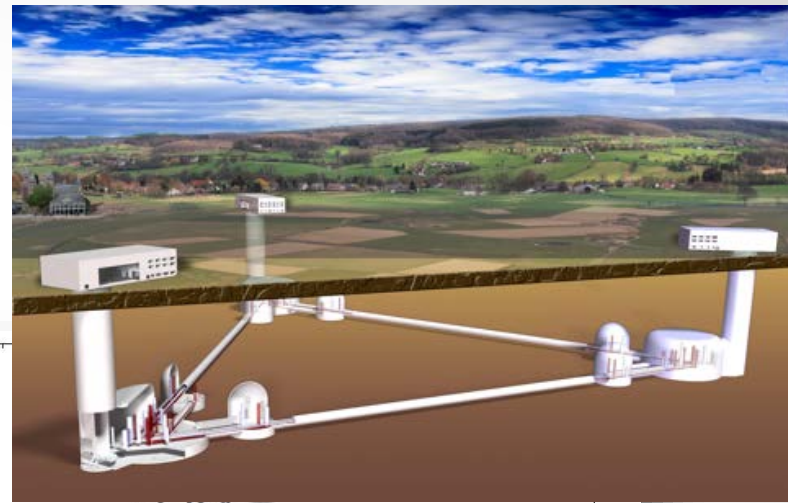


S.Harabasz PRC102 (2020) 054903



The Einstein Telescope project

F.Iacovelli, C.Mondal et al, PRD 2023



Summary & Conclusions

- The Equation of State can be univocally mapped to the static properties of NS \Leftrightarrow to the GW signals from NS mergers
- No ab-initio model of nuclear matter for all densities! But Bayesian techniques allow controlled extrapolations of low density constraints from nuclear theory and experiments
 - => No present indication of exotic degrees of freedom**
- Relatively tight observable prediction within the nucleonic hypothesis
 - => A 1st order phase transition to deconfined matter can potentially be detected with 3G interferometers**