

$$\langle \tilde{n}_k \tilde{n}_l^* \rangle = \frac{1}{2\Delta f} S_n(f_k) \delta_{kl}$$