

$$= \int df df' \tilde{V}^*(f) \tilde{V}(f') \langle \tilde{n}(f) \tilde{n}^*(f') \rangle$$