

A 3D visualization of a particle detector simulation. It shows a central interaction point from which numerous tracks radiate outwards. The tracks are color-coded: blue for primary particles, orange for secondary particles, and green for muons. The detector's internal structure is visible as a complex grid of lines. In the top right corner, four muons are explicitly labeled with the Greek letter μ .

Decays to four charged leptons at LHCb

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Impostor alert

- A Belle II person speaking about LHCb measurements :)
 - Some slides refurbished from Harry Cliff (thanks!)

When you lie on the application but still get the job



Why multileptons?

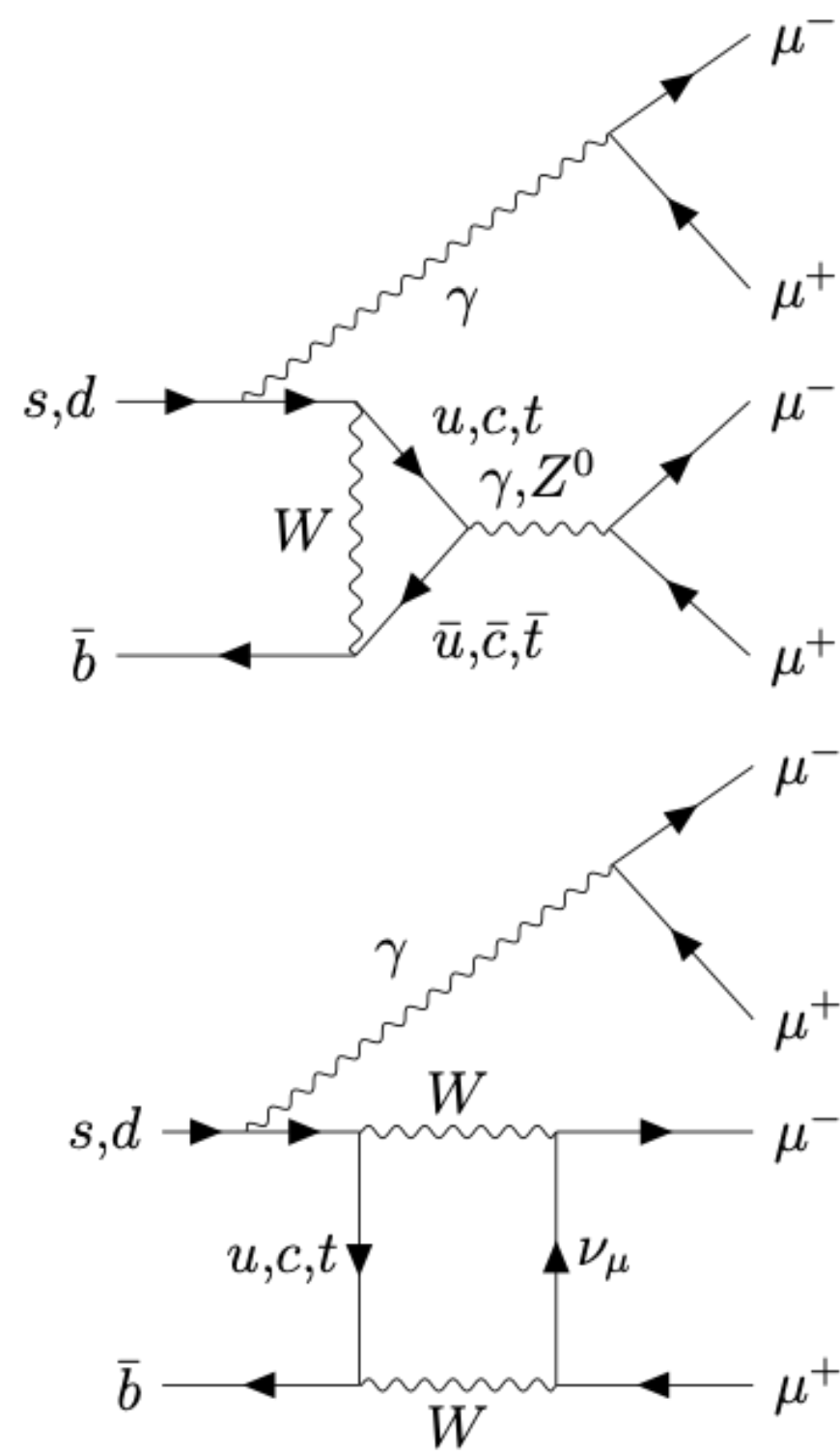
- Previous talks (Pierre et al) motivated $B^\pm \rightarrow \ell^\pm \ell^\mp \ell^\pm \nu_\ell$ as hadron-collider-friendly siblings of $B^\pm \rightarrow \ell^\pm \nu_\ell$ and $B^\pm \rightarrow \ell^\pm \nu_\ell \gamma$
- **The same idea can be applied to (already friendly) decays without neutrinos:**
 - $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ or $B_{(s)}^0 \rightarrow \gamma\gamma$ are linked to $B_{(s)}^0 \rightarrow \ell^+ \ell^- \ell^+ \ell^-$
 - Helicity-suppression (partially?) lifted \rightarrow all lepton flavours are okay
 - Very rare nevertheless (loop and α^2)
 - Can also play the same trick on electromagnetic decays: $\psi \rightarrow \ell^+ \ell^- \ell^+ \ell^-$ to validate the experimental procedure, more on this later
 - Not so rare (tree but α^2), allows to see an actual signal peak

B to four leptons

- Several important SM contributions:

Each of those three contributions is treated separately in the analysis.

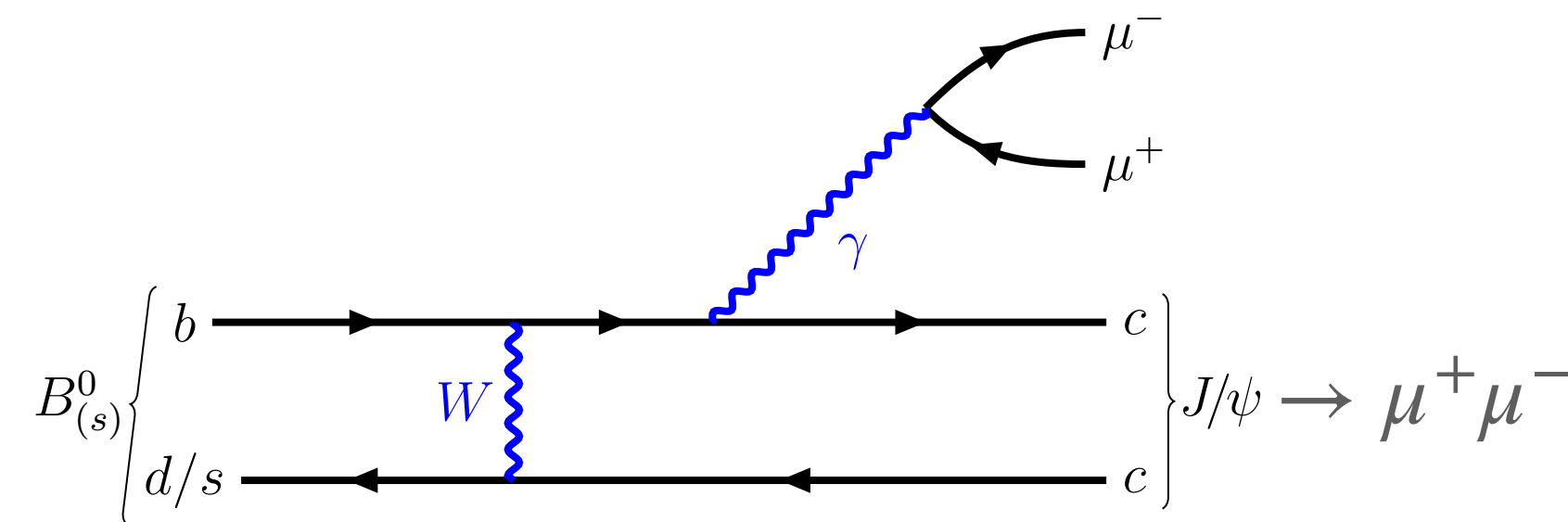
penguin+box
ISR/FSR



rate $\sim 10^{-10}$ for B_s^0 , 10^{-12} for B^0

[Danilina, Nikitin, Phys. Atom. Nuclei 81, 347–359 (2018)]

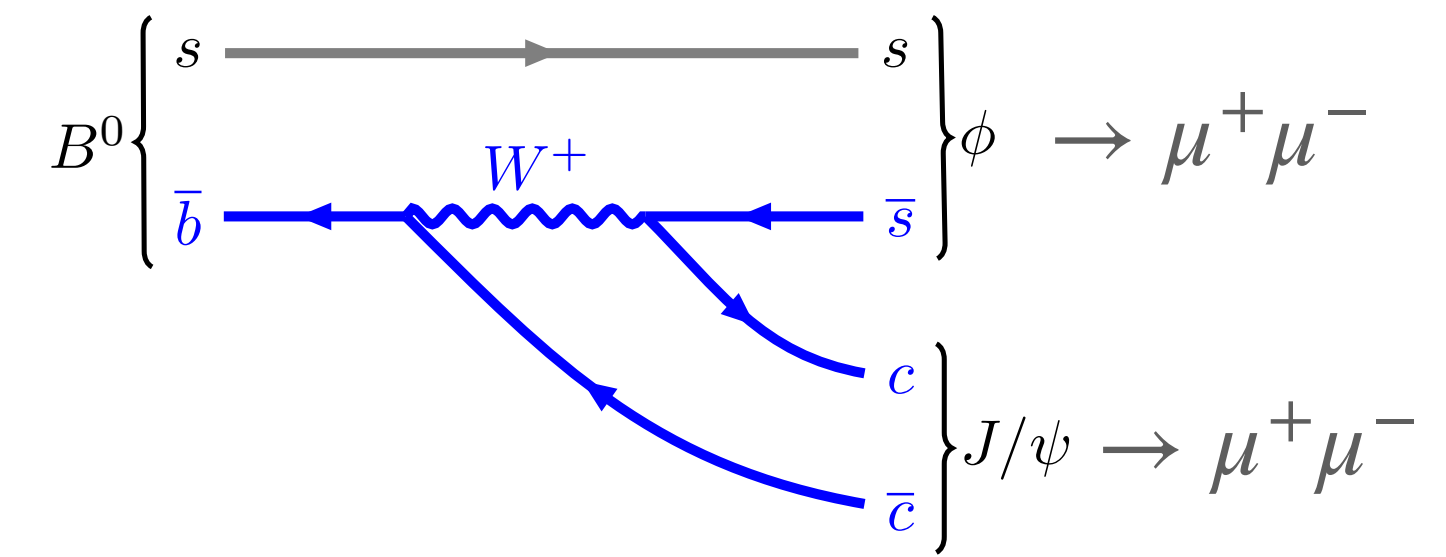
W exchange
FSR/ISR



rate $\sim 10^{-10}$ for B_s^0 but mind $\mathcal{B}(J/\psi \rightarrow \mu\mu)$
 [Nucl.Phys.B 577 (2000) 240-260]
 Related to $B_s^0 \rightarrow J/\psi\gamma$ for which LHCb limit is $<7.3e-6$


Other possible contributions e.g. $B_s^0 \rightarrow \phi(\mu\mu)\mu\mu$ or $B_s^0 \rightarrow \phi(\mu\mu)\phi(\mu\mu)$ are not considered, below experimental sensitivity

Tree

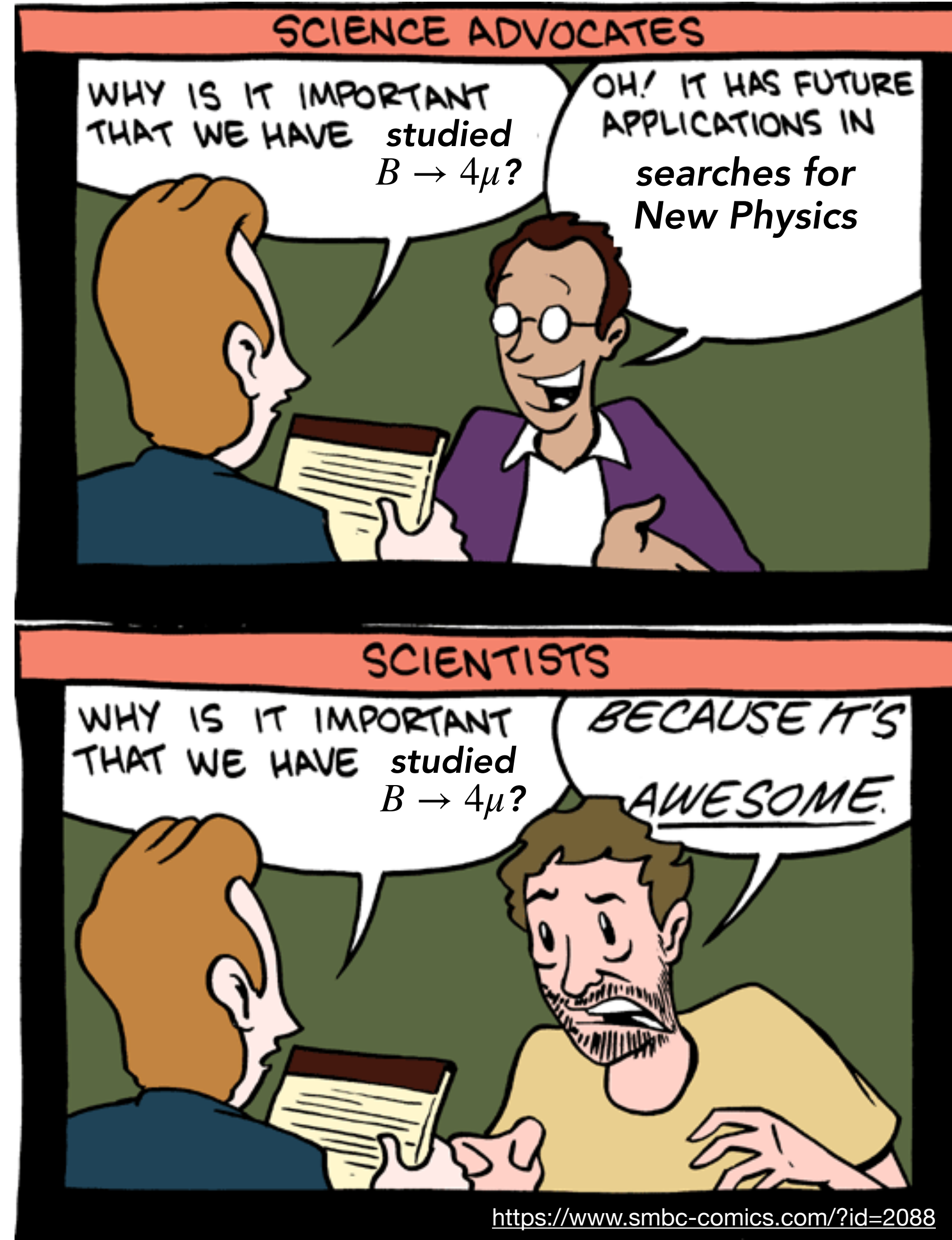


"huge" compared to the rest:
 effective BF $\sim 1.7e-8$,
 used as a normalisation mode

B to four leptons: BSM?

- Essence of the proposed BSM scenarios: $B \rightarrow aa^{(\prime)} \rightarrow 4\mu$
 - Several models on the market: some inspired by the $(g - 2)_\mu$ or R_K which were superstars back 5 years ago; others are 
- A selection of models: (*don't ask me about it please*)
 - Light scalars and heavy vectors (Chala et al, [Eur.Phys.J.C 79 \(2019\) 5, 431](#))
 - Hierarchical new physics with multiple scalars (Ramos et al, [JHEP 11 \(2022\) 027](#))
 - Sglodstino pair production scalar+pseudoscalar (Demidov et al, [Phys.Rev.D 85 \(2012\) 077701](#))
 - HyperCP anomaly...
 - *apologies for missing your favourite model here*
- Note: experimental signature is different if the BSM particle is long-lived: not covered by any published search yet.

B to four leptons: experimentalist's approach



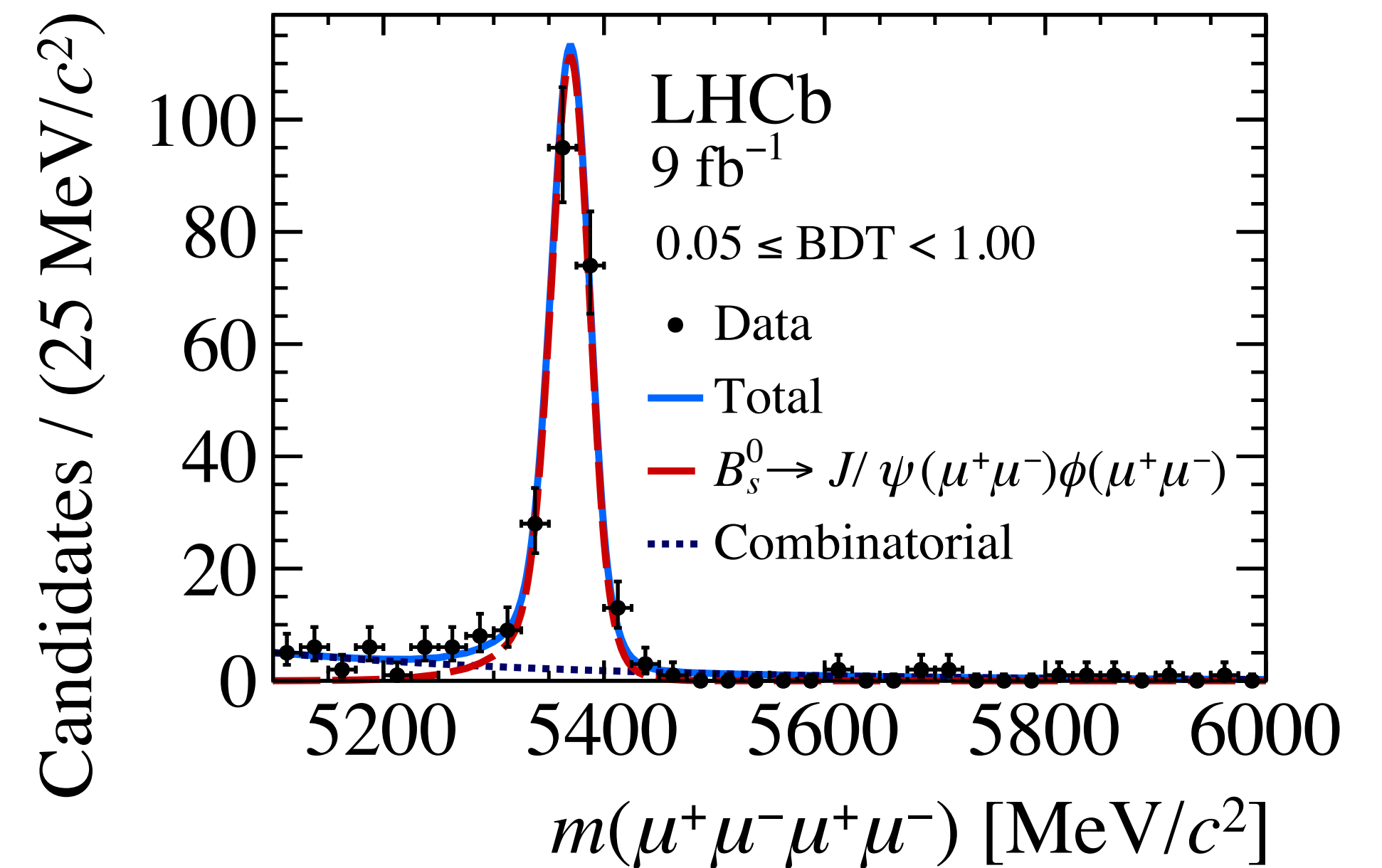
- Require one dimuon combination around the ϕ and one around the J/ψ
- The yield is quite small (~ 220 evts) due to low $\mathcal{B}(\phi \rightarrow \mu\mu)$

I will not bore you with selection details:
they are quite straightforward in this analysis.

Muon ID + a standard multivariate selection
against accidental combinations do all the job.

Important to know:

LHCb muon system requires $p > 3$ GeV for each muon!

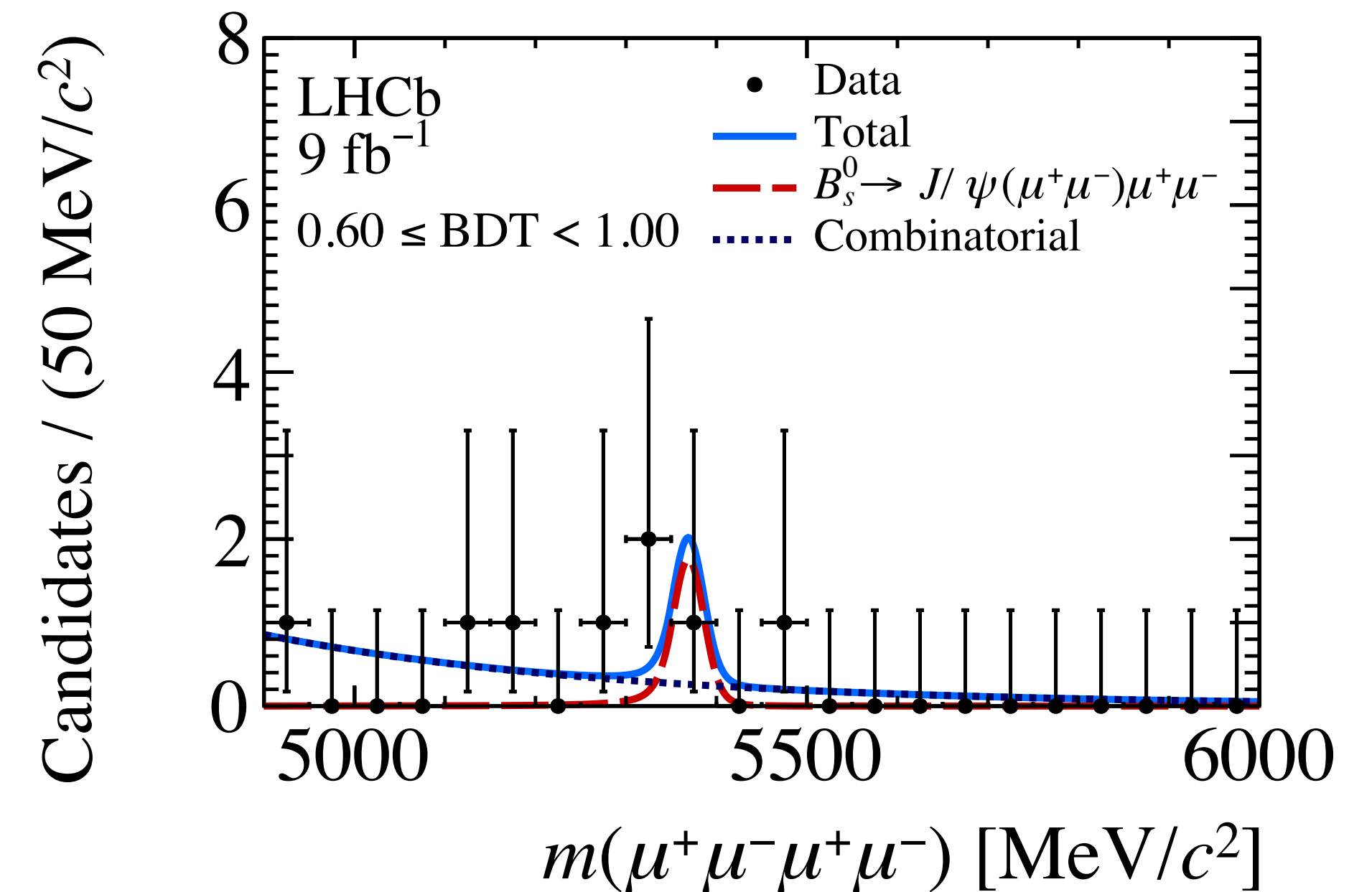


- Require one dimuon combination around the J/ψ , veto the ϕ
- Misidentified $B \rightarrow J/\psi h h'$ could contribute: tight muon ID applied
- No significant signals, upper limits set at 95% CL:

$$\mathcal{B}(B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\mu^+\mu^-) < 2.6 \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow J/\psi(\mu^+\mu^-)\mu^+\mu^-) < 1.0 \times 10^{-9}$$

(this includes $\mathcal{B}(J/\psi \rightarrow \mu^+\mu^-)$)



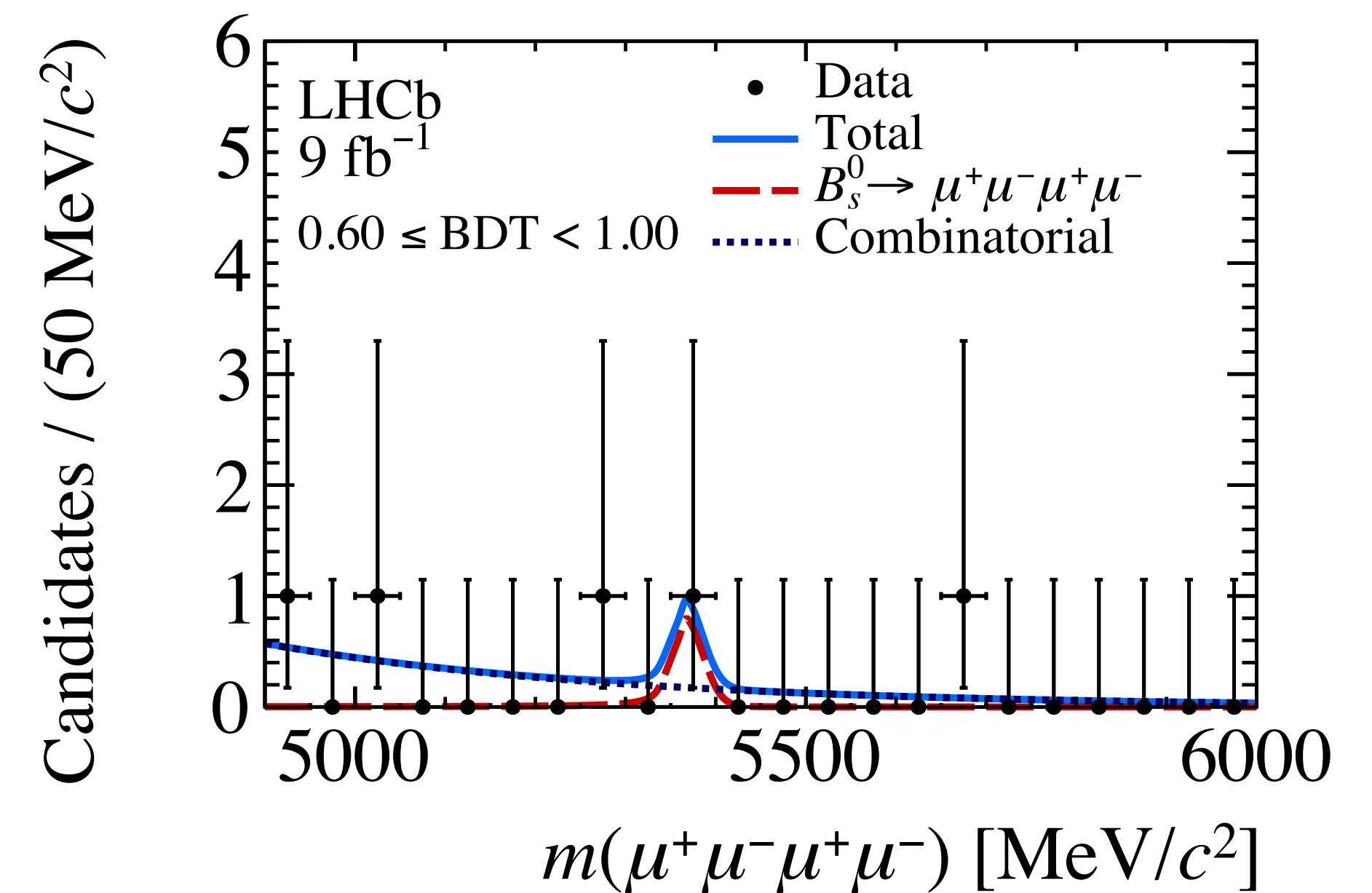
- Veto the $\phi, J/\psi, \psi(2S)$ in any dimuon combination and consider all the rest

- No significant signals, either, upper limits set at 95% CL:

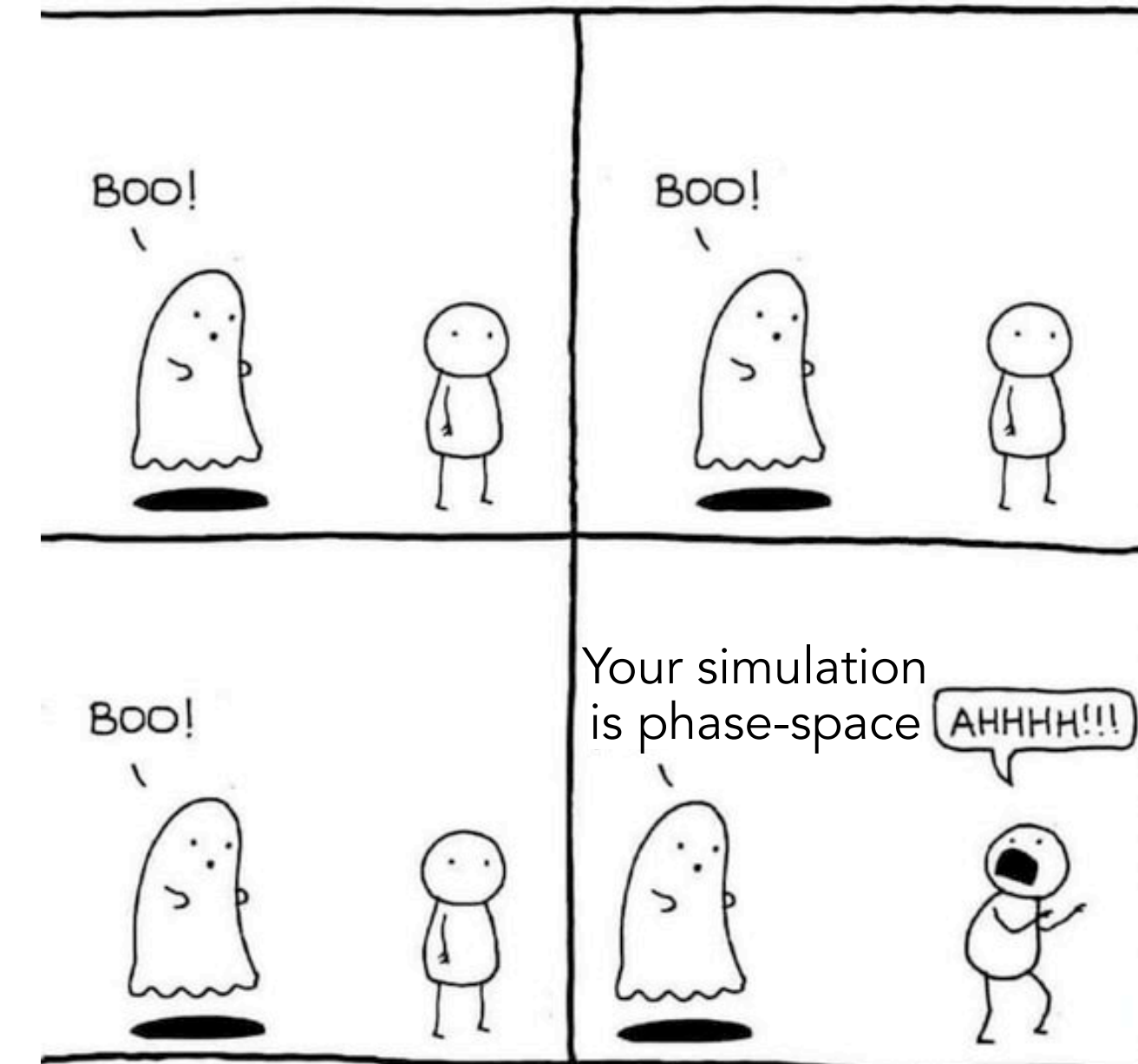
$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-) < 8.6 \times 10^{-10} \quad \text{factor } < 10 \text{ above the SM rate}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-) < 1.8 \times 10^{-10}$$

- Upper limits also set on a specific NP model:
a pair of 1-GeV scalar (otherwise does not pass the phi veto)
- See also the Run 1 paper [JHEP 03 \(2017\) 001](#) for limits on sgoldstino scenarios



- For the nonresonant $B_s^0 \rightarrow \mu^+ \mu^- \mu^+ \mu^-$ decays, the phase-space model is used
- But: muon reconstruction efficiencies depend on muon momenta
 - If there is a photon pole = more soft muons = lower efficiency!
- **20% systematic uncertainty** due to efficiency variations across the phase-space
 - Can actually be an important effect if we saw the signal, ok for an upper limit
- A theory+experiment initiative at TU Dortmund (Stamou, Wagner, Albrecht et al) to develop a reliable SM prediction and an EvtGen model targeting the Run3 analysis



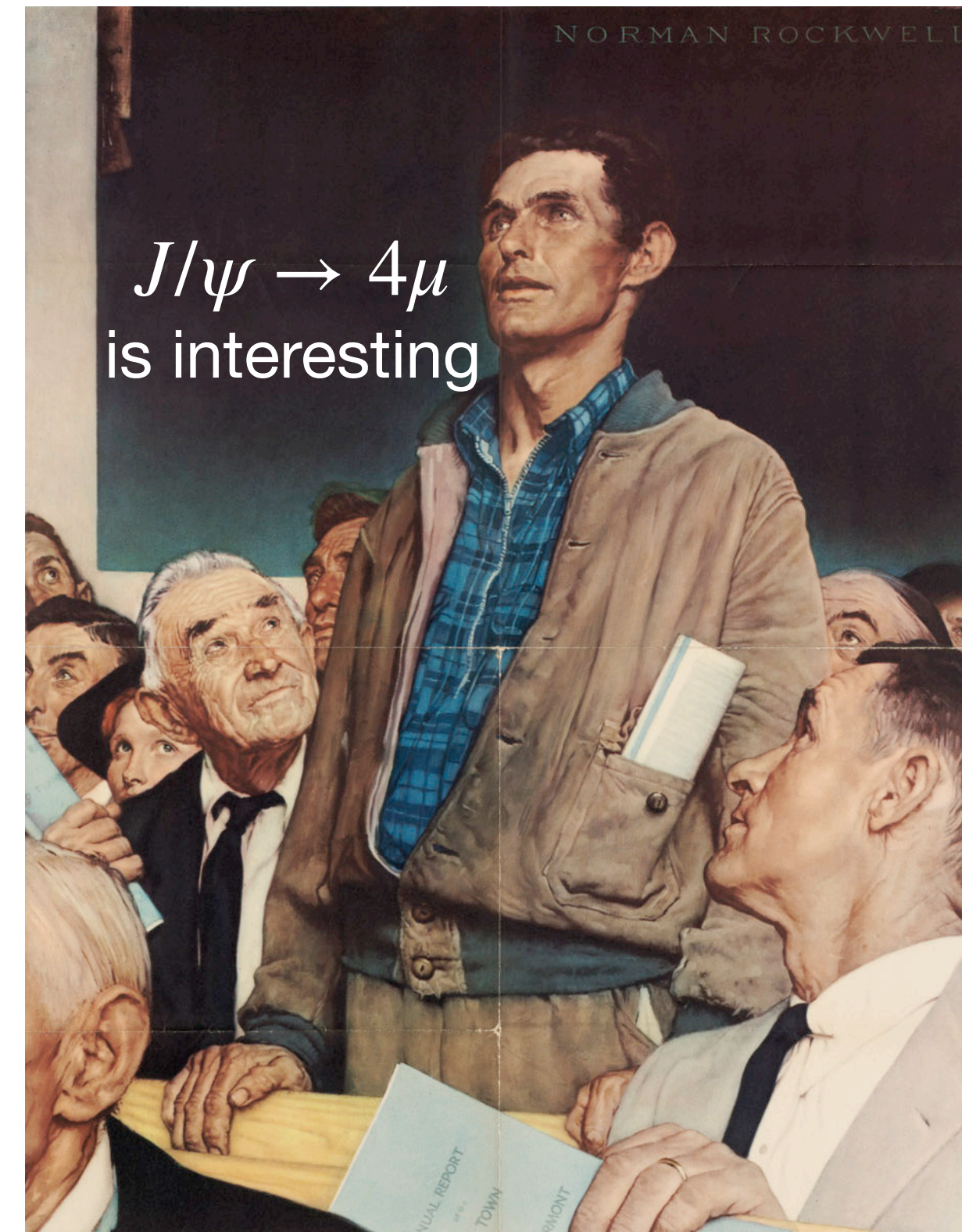
B to four leptons: what next?

- Run 3 data can actually help to reach the SM sensitivity goalpost for $B_s^0 \rightarrow \mu\mu\mu\mu$!
 - Reliable SM predictions can be useful ;)
- Straightforward next steps (planned/ongoing at LHCb):
 - $B_s^0 \rightarrow \mu\mu ee$: interesting interplay with the $B_s^0 \rightarrow \mu\mu\gamma$ at very low q^2 (+ photon conversions in the material).
 - $B^+ \rightarrow K^+ \mu\mu\mu\mu$: larger B^+ production rate helps
 - $B \rightarrow \mu\mu\mu\mu(K)$ with long-lived intermediate particles decaying to dimuons
 - Six muons, anyone? [see [Phys.Rev.D 100 \(2019\) 11, 115015](#)]



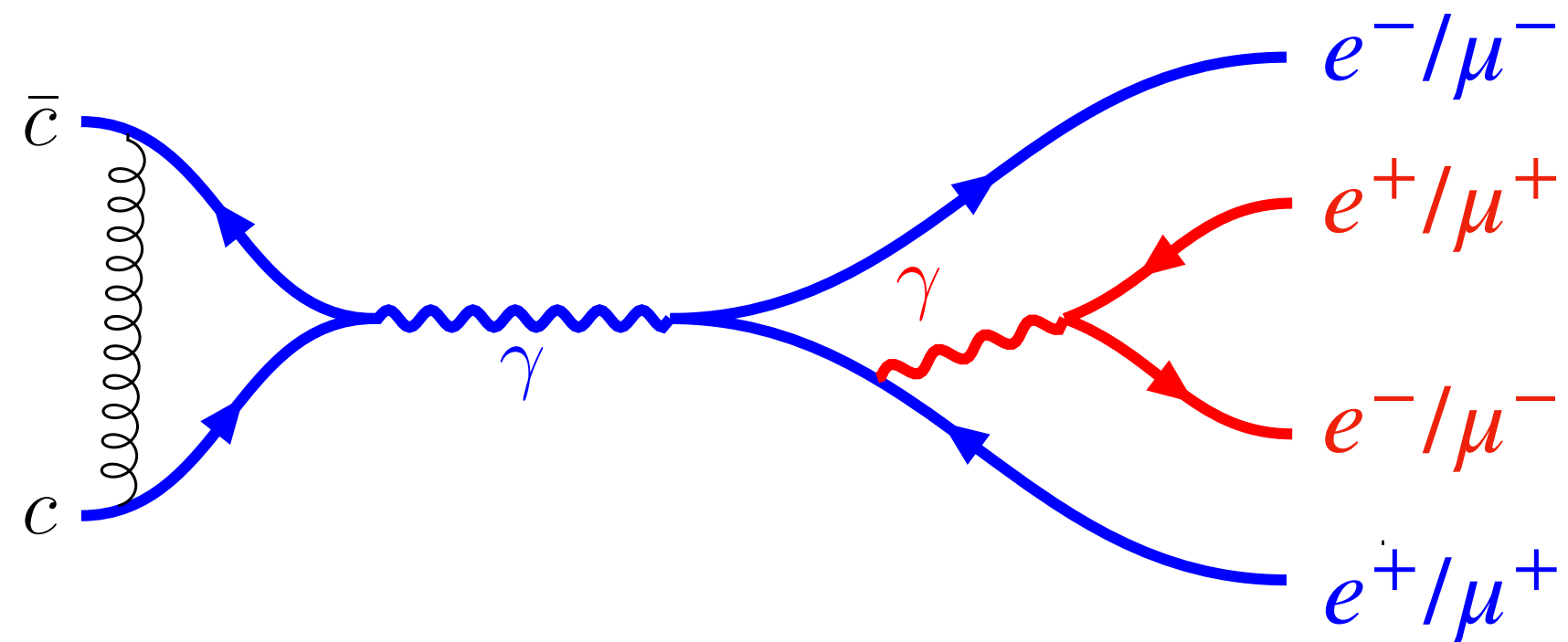
An experimentalist's digression

- I mentioned $B^+ \rightarrow K^+ \mu \mu \mu \mu$.
- What kind of resonant contributions does one expect here?
 - $B^+ \rightarrow K^+ J/\psi(\mu\mu)\mu\mu$ with all the possible $B^+ \rightarrow K^+(\chi_c \rightarrow J/\psi(\mu\mu)\mu\mu)$,
 $B^+ \rightarrow K^+ J/\psi(\mu\mu)V(\mu\mu)$ etc
 - $B^+ \rightarrow K^+ J/\psi(\mu\mu\mu\mu)$
- At this point we realised that the decay $J/\psi \rightarrow \mu\mu\mu\mu$ was not seen yet!
- **Let's talk about it.**



J/ψ decays to four leptons

- Final-state radiation of a virtual photon from the $J/\psi \rightarrow \mu^+ \mu^-$ or $J/\psi \rightarrow e^+ e^-$

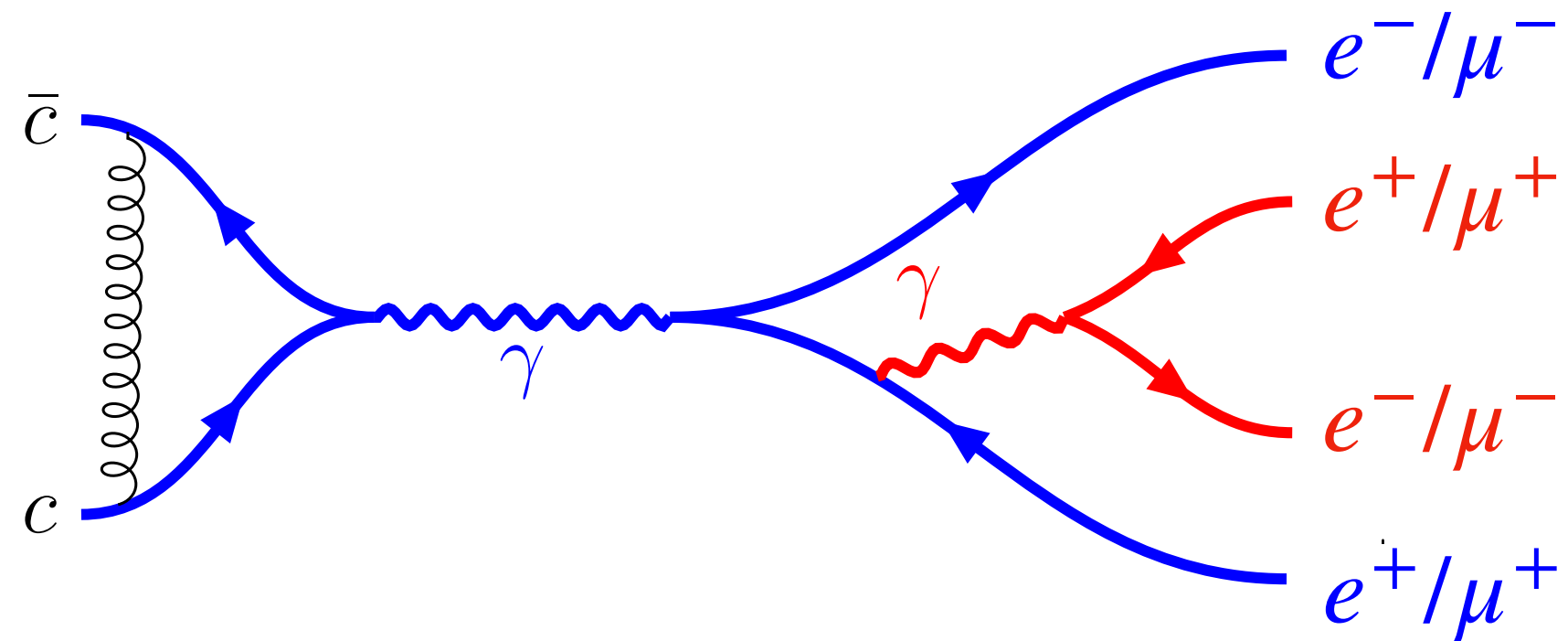


- Initial-state radiation process suppressed by C parity: $J/\psi \rightarrow \gamma\gamma$ is forbidden
 - strictly 0 for on-shell photons (Landau-Yang theorem)
 - *is this still true for virtual photons?*
- No significant contribution from intermediate vector resonances: $J/\psi \rightarrow VV \rightarrow 4\mu$ violates C parity
- A clean FSR process with future applications and sensitivity to possible BSM $J/\psi \rightarrow XX \rightarrow 4\mu$ scenarios

Observing the $J/\psi \rightarrow \mu^+ \mu^- \mu^+ \mu^-$ signal would allow to validate the simulated description of the $\gamma^* \rightarrow \mu^+ \mu^-$.

J/ψ decays to four leptons

- Final-state radiation of a virtual photon from the $J/\psi \rightarrow \mu^+\mu^-$ or $J/\psi \rightarrow e^+e^-$



- Ratio of decay rates to **4 leptons** / **2 leptons** can be predicted in QED

- Predicted LO-QED decay rates [Chen et al., [PRD 104 \(2021\) 9, 094023](#)]:

Decay	$\mathcal{B}(4\ell)/\mathcal{B}(2\ell)$	$\mathcal{B}(4\ell)$
$J/\psi \rightarrow e^+e^-e^+e^-$	8.85×10^{-4}	5.288×10^{-5}
$J/\psi \rightarrow e^+e^-\mu^+\mu^-$	6.31×10^{-4}	3.763×10^{-5}
$J/\psi \rightarrow \mu^+\mu^-\mu^+\mu^-$	0.163×10^{-4}	0.0974×10^{-5}

- Virtual photon \rightarrow decay rates falls with $\sim 1/m_{\ell^+\ell^-}^2$
- Rate larger for e^+e^- modes: enhancement at low $m_{e^+e^-}$ (below the dimuon threshold)
- Identical leptons create interference

size of QED/QCD uncertainties unclear

Can we trust these predictions?

- The BES III experiment studied four-lepton J/ψ decays [[arXiv:2111.13881](https://arxiv.org/abs/2111.13881)]
- Original arXiv submission (late 2021) claimed a discrepancy with the SM

Using a data sample of 4.481×10^8 $\psi(3686)$ events collected with the BESIII detector, we report the first observation of the four-lepton-decays $J/\psi \rightarrow e^+e^-e^+e^-$ and $J/\psi \rightarrow e^+e^-\mu^+\mu^-$ utilizing the process $\psi(3686) \rightarrow \pi^+\pi^-J/\psi$. The branching fractions are determined to be $[4.32 \pm 0.26 \text{ (stat)} \pm 0.19 \text{ (syst)}] \times 10^{-5}$ and $[2.45 \pm 0.21 \text{ (stat)} \pm 0.10 \text{ (syst)}] \times 10^{-5}$, respectively. The results deviate from theoretical predictions, by 2.8 and 5.2 σ , respectively. No significant signal is observed for $J/\psi \rightarrow \mu^+\mu^-\mu^+\mu^-$, and an upper limit on the branching fraction is set at 1.6×10^{-6} at the 90% confidence level. A CP asymmetry observable is constructed for the first two channels, which is measured to be $(-0.019 \pm 0.067 \pm 0.025)$ and $(-0.016 \pm 0.081 \pm 0.003)$, respectively. No evidence for CP violation is observed in this process.

- This version has never been published in a journal
- A corrected version (Sept 2023, v3 on arXiv): good agreement with the SM

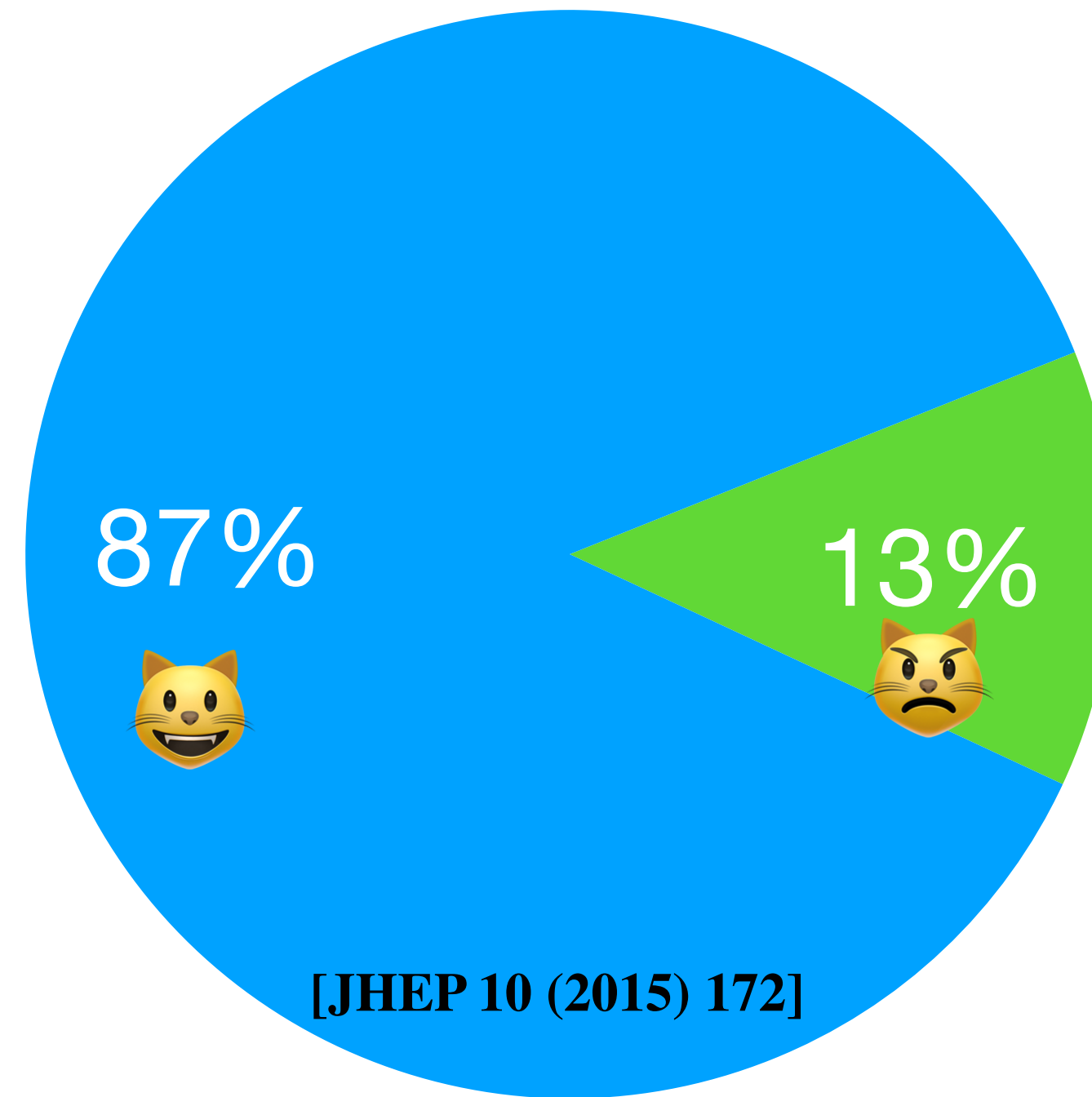
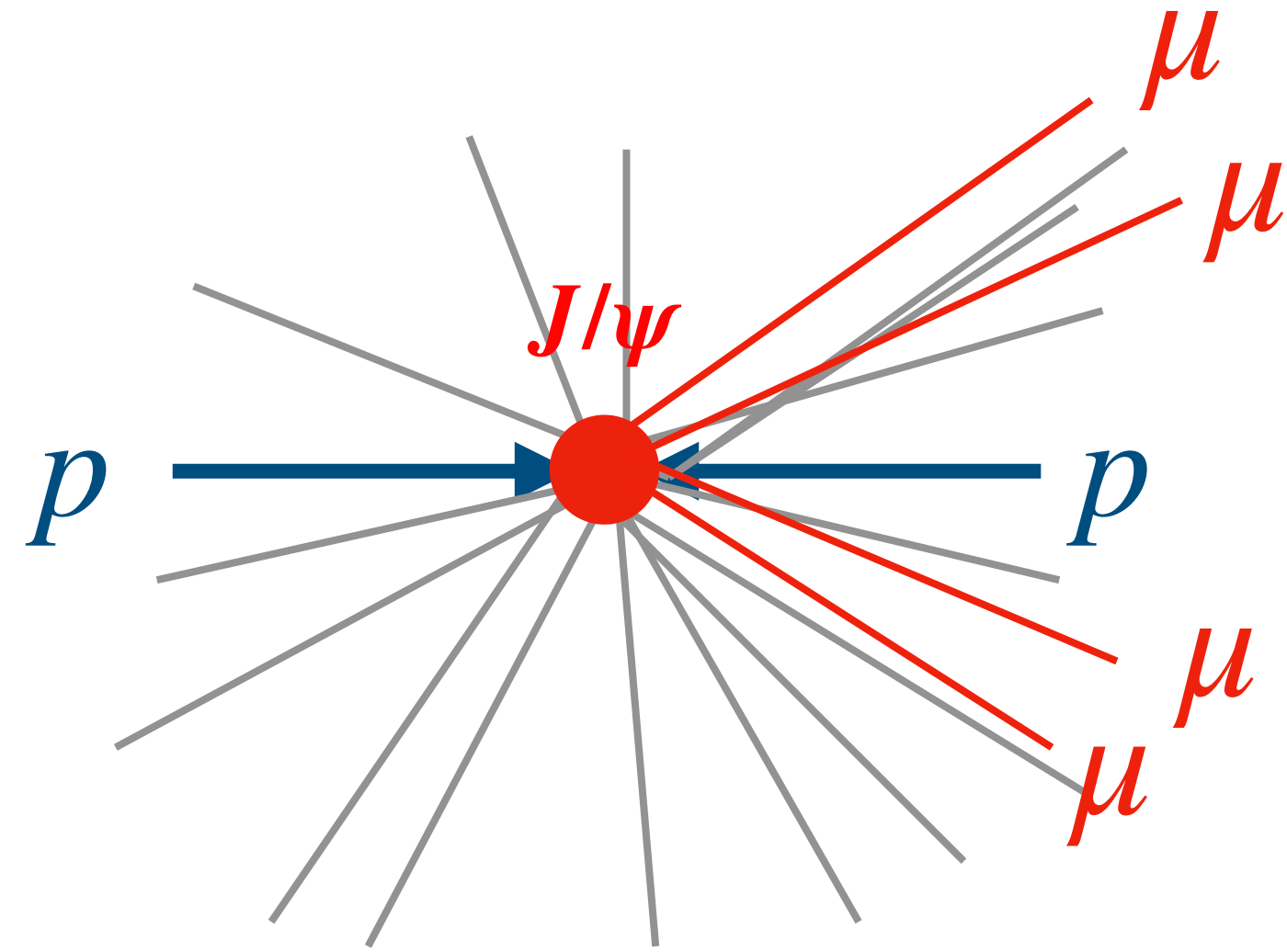
Using a data sample of 4.481×10^8 $\psi(3686)$ events collected with the BESIII detector, we report the first observation of the four-lepton-decays $J/\psi \rightarrow e^+e^-e^+e^-$ and $J/\psi \rightarrow e^+e^-\mu^+\mu^-$ utilizing the process $\psi(3686) \rightarrow \pi^+\pi^-J/\psi$. The branching fractions are determined to be $[5.48 \pm 0.31 \text{ (stat)} \pm 0.45 \text{ (syst)}] \times 10^{-5}$ and $[3.53 \pm 0.22 \text{ (stat)} \pm 0.13 \text{ (syst)}] \times 10^{-5}$, respectively. The results are consistent with theoretical predictions. No significant signal is observed for $J/\psi \rightarrow \mu^+\mu^-\mu^+\mu^-$, and an upper limit on the branching fraction is set at 1.6×10^{-6} at the 90% confidence level. A CP asymmetry observable is constructed for the first two channels, which is measured to be $(-0.012 \pm 0.054 \pm 0.010)$ and $(0.062 \pm 0.059 \pm 0.006)$, respectively. No evidence for CP violation is observed in this process.

An LHCb measurement of

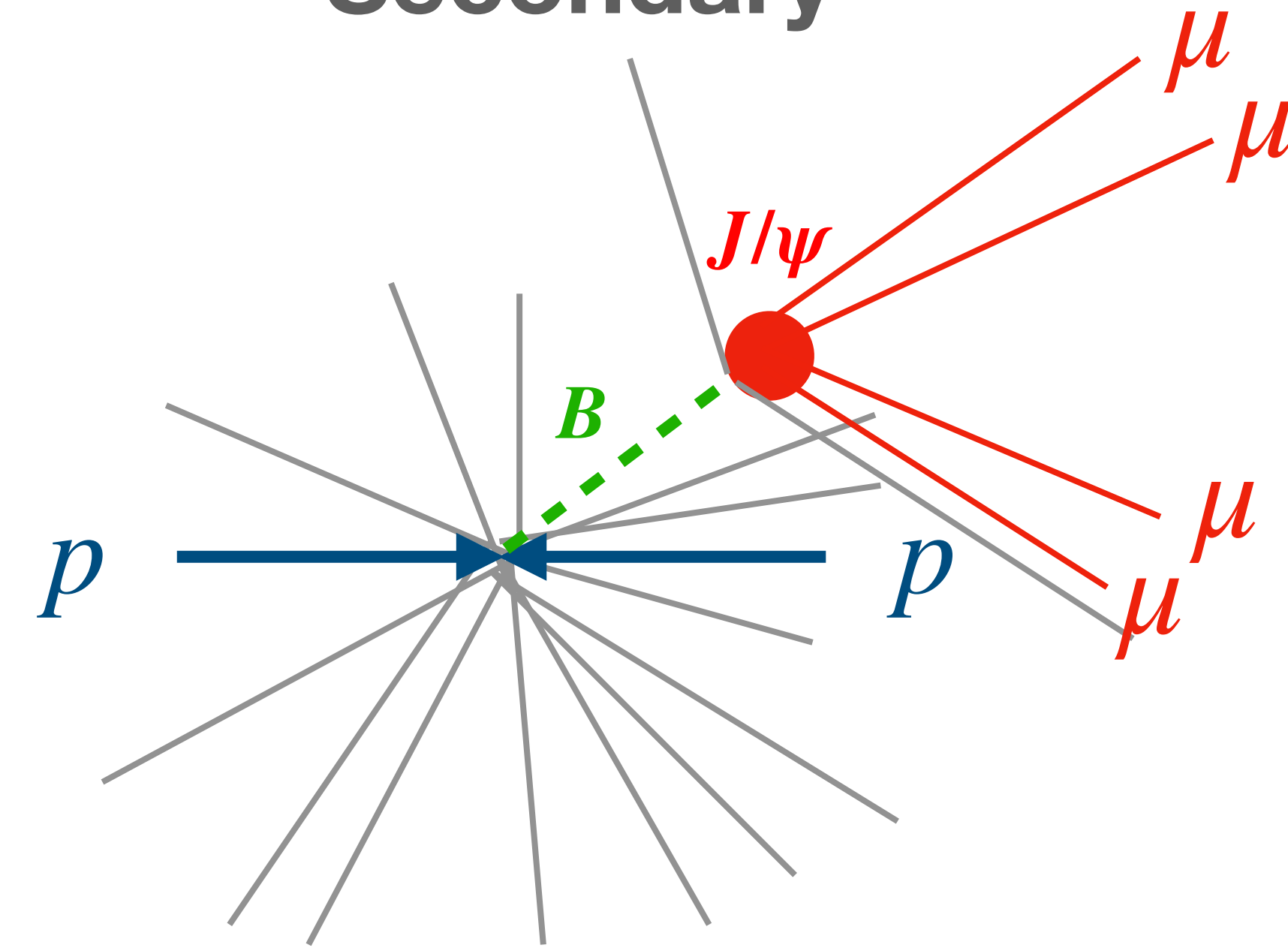
$J/\psi \rightarrow \mu^+\mu^-\mu^+\mu^-$ would help to complete the puzzle

Production of J/ψ mesons at LHCb

Prompt



Secondary



High background 😡

Displacement: lower background 😸

Tight trigger selection 😡

Profit from B-physics triggers 😸



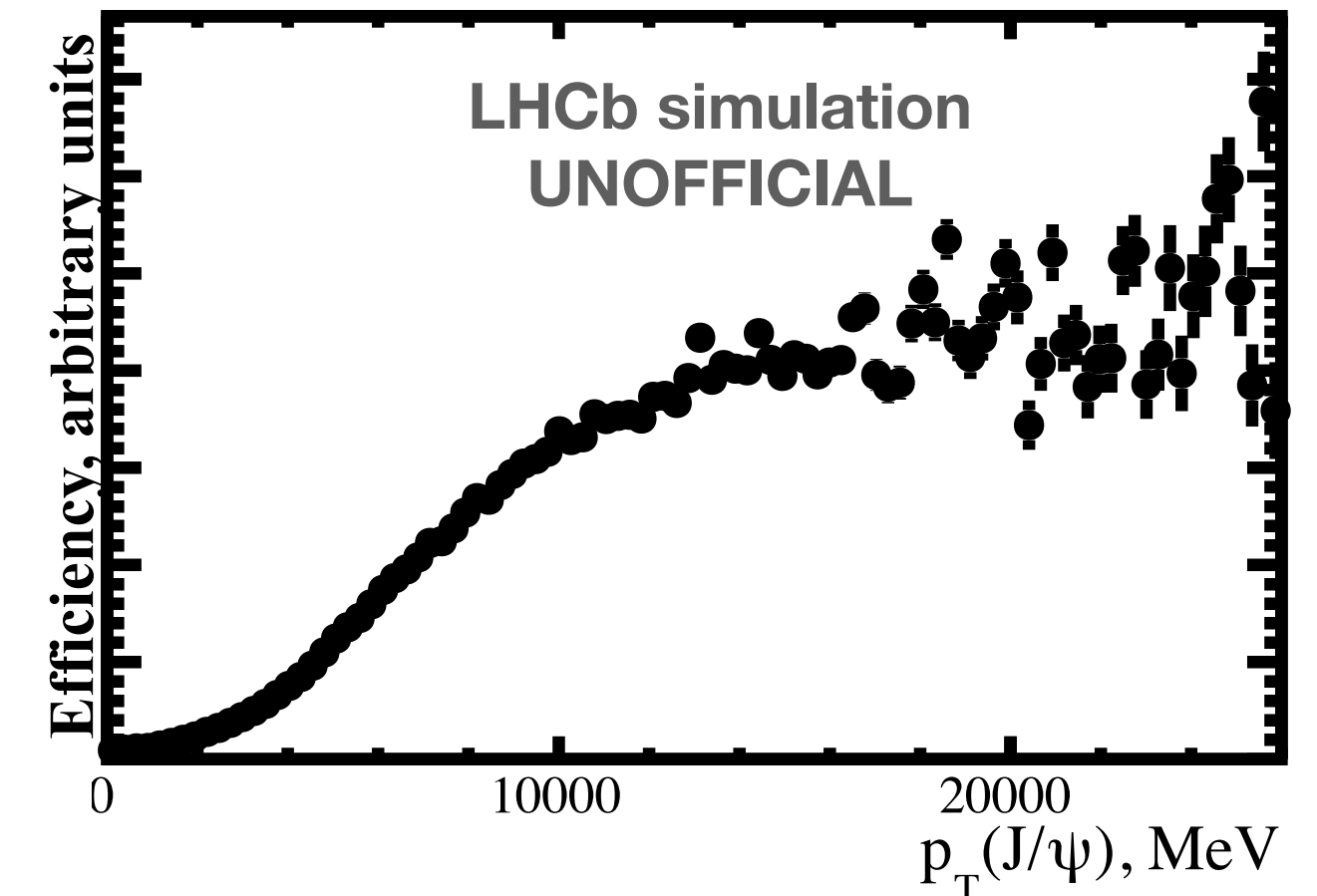
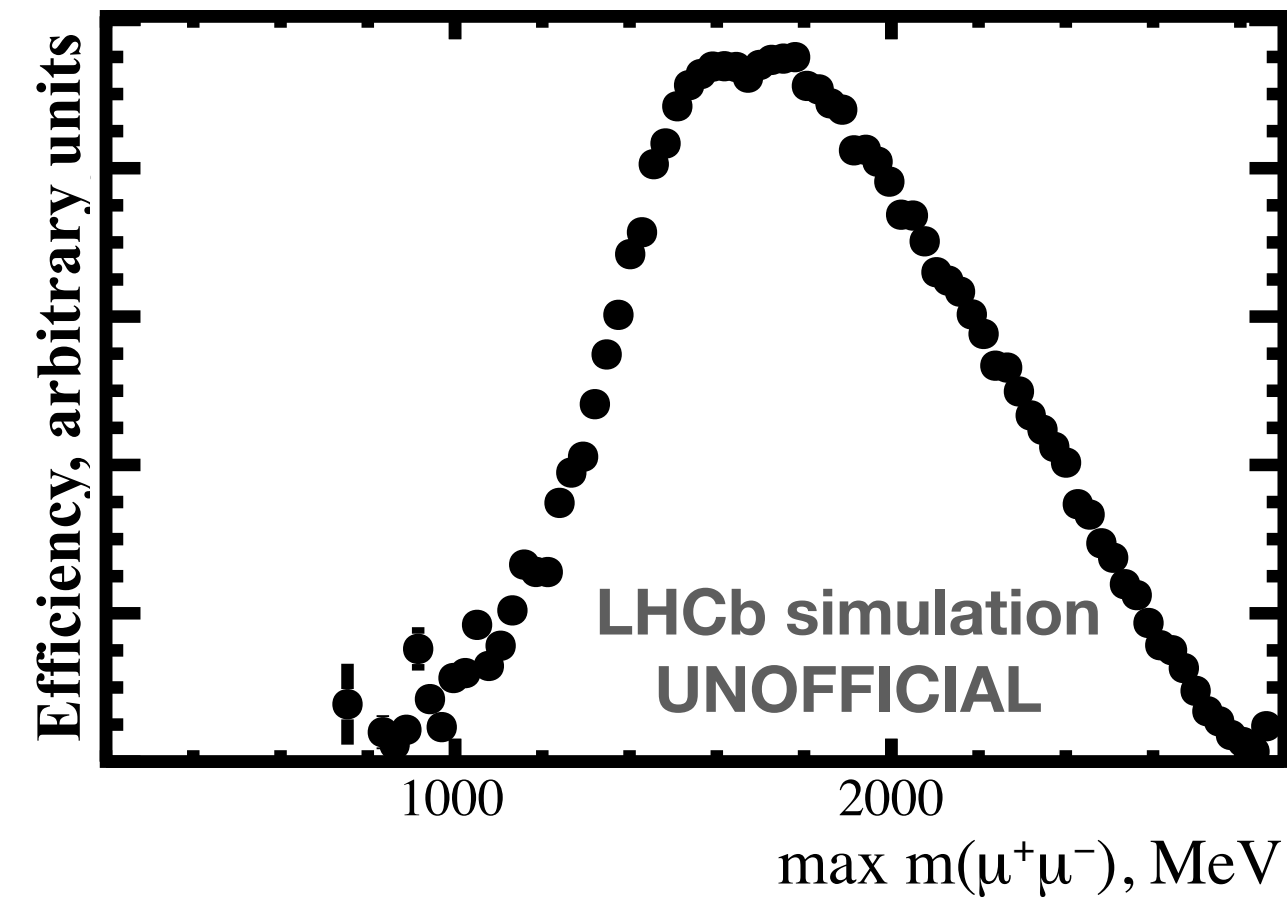
The two methods provide a valuable cross-check of experimental procedure.

Efficiency dependence

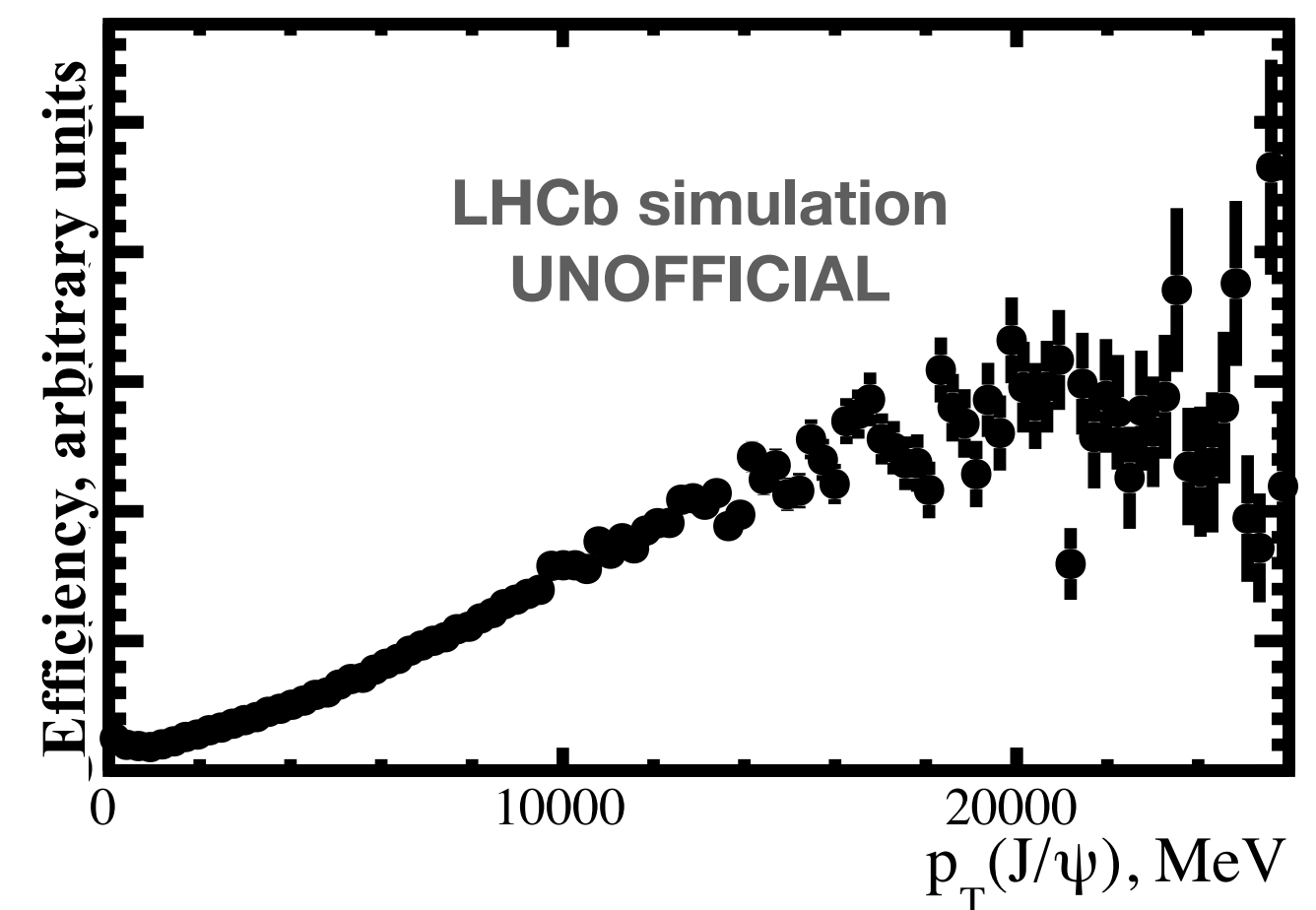
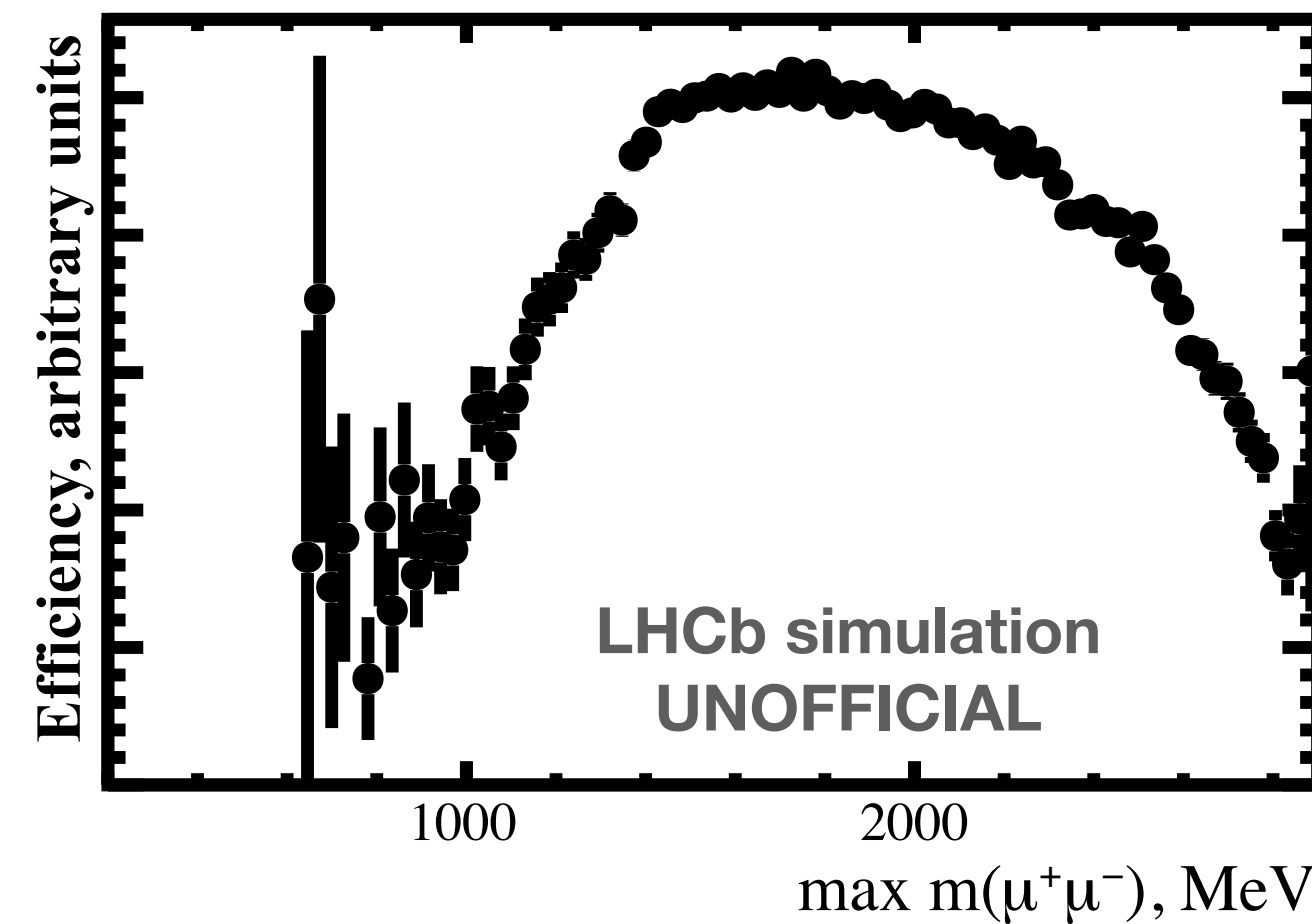
Even more important
for $J/\psi \rightarrow e^+e^-\mu^+\mu^-$
(photon pole)

The LHCb reconstruction+preselection efficiency as a function of kinematics:
(The *total* efficiency trend will be even more complicated)

Prompt



Secondary



Highlights importance of having the correct decay model in simulation!

Discussion item: model-independent presentation of results?

- Multilepton decays await to be explored, many possible surprises
- LHCb Run3 data would be interesting, as well as data from other experiments
 - I did not talk about: recent CMS result on $\eta \rightarrow 4\mu$ (two-photon diagram = not FSR), similar BES results...
- Theory guidance would be helpful
 - **Reliable simulation models (EvtGen) are crucial**, large biases possible otherwise!
 - Measured BF values depend on the theory assumptions in LHCb simulation



<https://www.smbc-comics.com/?id=2088>