

# Prospects for the search of $B_{(c)}^+ \rightarrow \mu^+ \nu_{\mu} \gamma$ decays at LHCb

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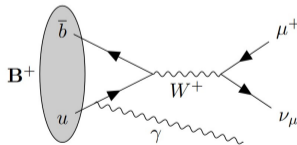


## Why $B^+ \rightarrow \ell^+ \nu_\ell \gamma$ is interesting

- Standard Model tree level process
- Strong helicity suppression is lifted by emission of additional photon
- Decay  $B^+ \rightarrow \ell^+ \nu_\ell \gamma$  has never been observed
- Current best upper limit from Belle using  $\ell = e, \mu$  [PRD 98 (2018) 11, 112016]

$$\mathcal{B}(B^+ \rightarrow \ell^+ \nu_\ell \gamma) < 3.0 \times 10^{-6} \text{ @90\%CL}$$

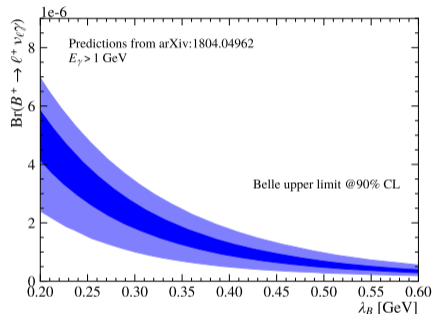
- Considered the golden mode to probe  $B^+$  meson substructure



Leading order Feynman diagram for the decay  $B^+ \rightarrow \mu^+ \nu_\mu \gamma$ .

# Probing the $B^+$ meson substructure

- Emission of  $\gamma$  probes first inverse moment  $\lambda_B$  of  $B$  meson light-cone distribution amplitude  
[Eur.Phys.J.C 71 (2011) 1818]
- Value of  $\lambda_B$  not well known but vital theory input  
[PRD 69 (2004) 034014] [Nucl.Phys.B 832 (2010) 109-151] [PLB 848 (2024) 138345]
- Strong dependence of predicted BR for  $B^+ \rightarrow \ell^+ \nu_\ell \gamma$  on  $\lambda_B$
- Theory predictions only valid for  $E_\gamma^* > 1.5 \text{ GeV}$  with extrapolation to  $E_\gamma^* > 1.0 \text{ GeV}$  [JHEP 07 (2018) 154]



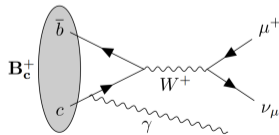
Predicted BR for  $B^+ \rightarrow \ell^+ \nu_\ell \gamma$  from [JHEP 07 (2018) 154] with the upper limit from Belle. The colored bands correspond to different theory models.

## On the decay $B_c^+ \rightarrow \mu^+ \nu_\mu \gamma$

- Should be very similar to decay of  $B^+$
- Never been searched for
- Potential background for the analysis of  $B^+ \rightarrow \mu^+ \nu_\mu \gamma$
- Expect roughly similar rate [Phys.Rev.D 100 (2019) 11, 112006][PTEP 2022 (2022) 083C01]

$$\frac{N_{sig}(B_c^+ \rightarrow \mu^+ \nu_\mu \gamma)}{N_{sig}(B^+ \rightarrow \mu^+ \nu_\mu \gamma)} \approx \frac{|V_{cb}|^2 f_c}{|V_{ub}|^2 f_u} \approx 1$$

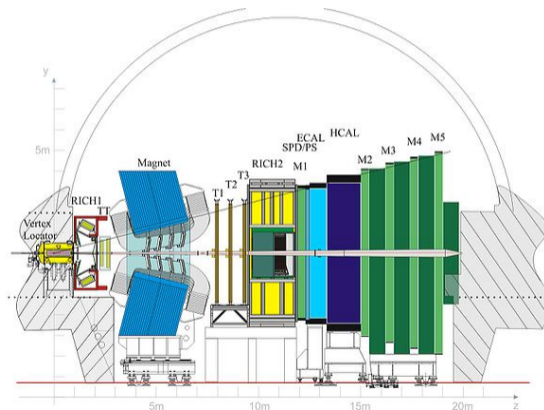
- In general limited knowledge of the  $B_c^+$  meson
- What can we learn from  $B_c^+ \rightarrow \mu^+ \nu_\mu \gamma$ ?



Feynman diagram for the decay  $B_c^+ \rightarrow \mu^+ \nu_\mu \gamma$ .

# The LHCb experiment

- Single arm forward spectrometer covering  $2 < \eta < 5$
- Tracking and vertexing: Vertex Locator (VELO), TT, Magnet, T1-T3
- Particle identification (PID): RICH, Calorimeters, Muon stations M1-M5



# Reconstructing $B_{(c)}^+ \rightarrow \mu^+ \nu_\mu \gamma$ at LHCb

- Very challenging to reconstruct at hadron colliders, deemed impossible
- Two major challenges: Vertex reconstruction and Neutrino momentum recovery

## Vertex reconstruction

- $B$  mesons produced in  $pp$  collisions
- Select  $B$  candidates from displaced secondary decay vertex
- Single charged track in  $\mu^+ \nu_\mu \gamma$   
⇒ no vertex reconstruction possible
- Crucial to require  $\gamma \rightarrow e^+ e^-$  conversions  
⇒ multiple charged tracks allow for vertex reconstruction
- Conversions in LHCb's vertex locator (VELO) provide excellent vertex resolution

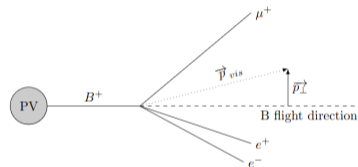
# Reconstructing $B_{(c)}^+ \rightarrow \mu^+ \nu_\mu \gamma$ at LHCb

## Neutrino momentum recovery

- At LHCb cannot infer neutrino momentum from initial decay kinematics
- Correct for momentum imbalance  $p_\perp$  perpendicular to  $B$  flight direction

$$m_{corr} = \sqrt{m^2(\mu^+ \gamma ee) + |p_\perp|^2 + |p_\perp|}$$

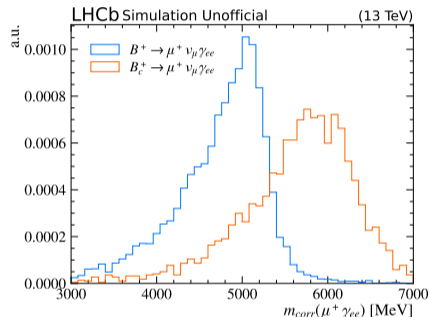
- Requires precise reconstruction of  $B$  decay vertex



- Using data recorded with LHCb experiment from 2016-2018 corresponding to  $\mathcal{L}_{int} = 5.4\text{fb}^{-1}$
- Reconstruct the photon using  $\gamma \rightarrow e^+e^-$  conversions in LHCb's VELO
- Search for signal peak in  $m_{corr}$  using binned template fit
- Background modelling from data-driven templates

## Blinding strategy

- Signal region  $4500\text{ MeV} < m_{corr}(\mu^+\gamma_{ee}) < 6500\text{ MeV}$  remains blinded



Corrected mass distribution for  $B_{(c)}^+ \rightarrow \mu^+ \nu_\mu \gamma$  simulation. The grey area is the blinded signal region.



- Trigger selection (hardware + software)
- Cut based selection: kinematics, decay topology, reconstruction quality
- Boosted Decision Trees (BDT) to suppress:
  - Random combination of  $\mu^+$  and  $\gamma_{ee}$
  - Decays with additional charged tracks e.g.  $B^+ \rightarrow D^0(\rightarrow K^- \pi^+ \gamma_{ee})\mu^+ \nu$
  - Decays with additional neutral clusters e.g.  $\pi^0 \rightarrow \gamma_{ee}\gamma$
- Currently optimising the signal selection

Trigger	Requirement
L0 trigger	LOElectron or LOMuon
HLT1	B_TrackMVA or B_TwoTrackMVA
HLT2	B_Topo[2,3]Body or B_TopoMu[2,3]Body

Trigger requirements to select  $B_{(c)}^+ \rightarrow \mu^+ \nu_{\mu} \gamma$  candidates.

## Background modelling $\pi^0/\eta \rightarrow \gamma ee\gamma$

Partially reconstructed  $\pi^0/\eta \rightarrow \gamma ee\gamma$

- By far the dominant source of background
- Expect much higher level of background compared to Belle

- Many sources including

$b \rightarrow u\ell\nu$ :

- $B^+ \rightarrow \pi^0 \mu^+ \nu_\mu$
- $B^+ \rightarrow \eta \mu^+ \nu_\mu$
- $B^0 \rightarrow \rho(770)^- (\rightarrow \pi^- \pi^0) \mu^+ \nu_\mu$

$b \rightarrow c\ell\nu$ :

- $B^+ \rightarrow \bar{D}^{(*)0} (\rightarrow h^+ h^- \pi^0 \dots) \mu^+ \nu_\mu$
- $B^0 \rightarrow D^{(*)-} (\rightarrow h^- \pi^0 \dots) \mu^+ \nu_\mu$

Decays of  $B_s$ ,  $B_c$ ,  $\Lambda_b$ :

- $B_s \rightarrow D_s^- (\rightarrow h^- \pi^0 \dots) \mu^+ \nu_\mu$

Random combinations of  $\pi^0/\eta + \mu^+$

- Modeling all backgrounds from  $\pi^0/\eta \rightarrow \gamma ee\gamma$  not feasible using simulation

⇒ **Data-driven template including all sources of  $\pi^0$  and  $\eta$**

# Background modelling $\pi^0/\eta \rightarrow \gamma ee \gamma$

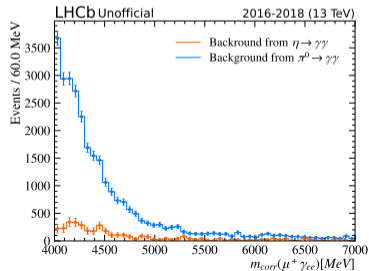
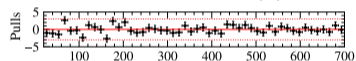
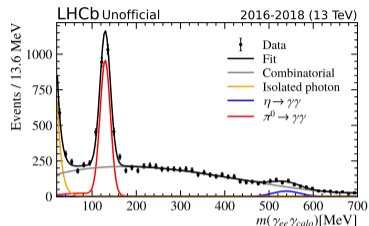
## Get $\pi^0/\eta \rightarrow \gamma ee \gamma$ background shape from data

- Search region in the calorimeter for missing photon from  $\pi^0/\eta \rightarrow \gamma ee \gamma$  decays
- Fit resulting distribution in  $m(\gamma ee \gamma_{calo})$
- Subtract background to get shape in  $m_{corr}(\mu^+ \gamma ee)$
- Correct for efficiency of finding additional photon and resolving  $\pi^0/\eta$

⇒ Representative of all  $\pi^0/\eta \rightarrow \gamma ee \gamma$  backgrounds scaled to expected yield

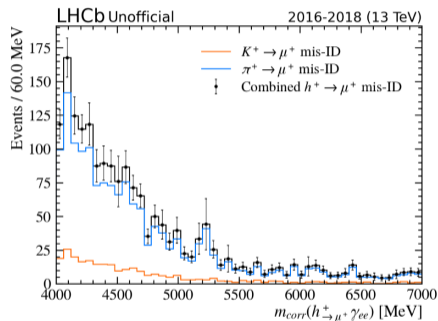
⇒ Crucial to get the background modelling correct

⇒ Requires further cross-checks



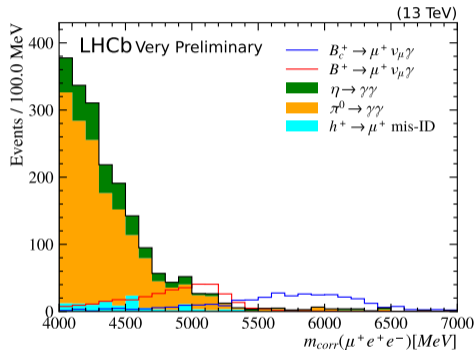
# Background modelling muon mis-identification

- Studied using control sample without PID requirement on muon track
- Select representative samples of  $\pi^+/K^+ \rightarrow \mu^+$
- Get  $m_{corr}(h^+ \rightarrow \mu^+ \gamma ee)$  shape with muon-mass hypothesis on the hadron
- Correct for the PID efficiency



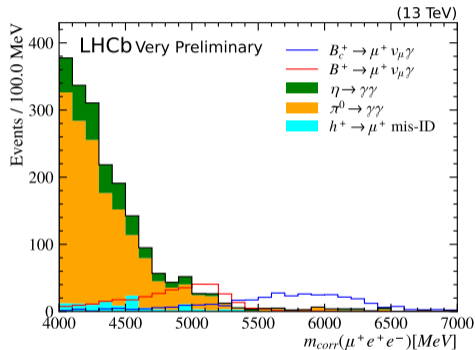
Template for background from  $h^+ \rightarrow \mu^+$  mis-identification.

- Optimisation performed of pseudo-experiments
- Generate background only pseudo-data from derived templates
- Fit including signal shapes for  $B_{(c)}^+ \rightarrow \mu^+ \nu_{\mu} \gamma$
- Binned template fit using method from Conway [arXiv:1103.0354] to account for template uncertainties
- Signal selection not yet finalised



Background-only pseudo-data and signal shapes with arbitrary normalisation.

- Idea: Maximise sensitivity on  $\mathcal{B}(B^+ \rightarrow \mu^+ \nu_\mu \gamma)$
- For optimisation: Bayesian method with flat prior
- Computationally less demanding
- In the case of no significant signal after unblinding:  
CL<sub>S</sub> method [J.Phys.G 28 (2002) 2693-2704]

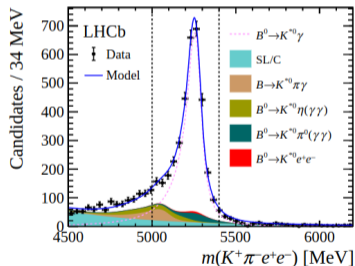


Background-only pseudo-data and signal shapes with arbitrary normalisation.

## Normalisation channel

$$B^0 \rightarrow K^{*0} \gamma_{ee} \text{ with } K^{*0} \rightarrow K^+ \pi^-$$

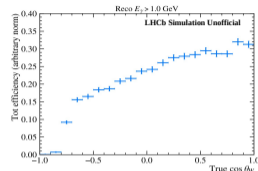
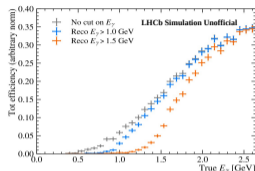
- No muon but very clean and can largely follow previous LHCb analysis [JHEP 12 (2020) 081]
- $\mathcal{B}(B^0 \rightarrow K^{*0} \gamma) = (4.18 \pm 0.25) \times 10^{-5}$  [PTEP 2022 (2022) 083C01]
- Align selection as much as possible with selection of  $B_{(c)}^+ \rightarrow \mu^+ \nu_{\mu} \gamma$
- Expect about 1200 events for 2016-2018



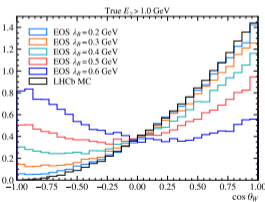
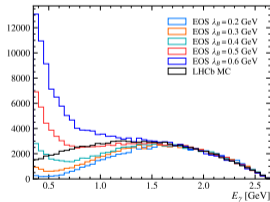
Massfit from the  $B^0 \rightarrow K^{*0} e^+ e^-$  analysis at very low  $q^2$  using Run 1+2 [JHEP 12 (2020) 081].

# Model dependence

- BR prediction reliable for  $E_\gamma^* > 1.5$  GeV
- Decided to cut at  $E_\gamma^* > 1.0$  GeV following Belle
- Distributions in  $E_\gamma^*$  and  $\cos\theta_W$  depend on  $B^+$  meson LCDA
- Studied using EOS [Eur.Phys.J.C 82 (2022) 6, 569] with the model from [JHEP 10 (2022) 162]
- Non-uniform efficiency in  $\cos\theta_W$  introduces strong model dependence



Reconstruction efficiency for  $E_\gamma^*$  and  $\cos\theta_W$

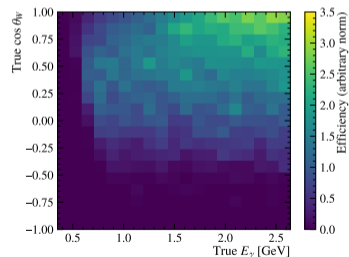
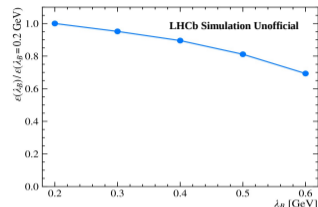


Model dependence of  $E_\gamma^*$  and  $\cos\theta_W$  on the parameter  $\lambda_B$



# Presentation of results

- Model dependence on  $\lambda_B$  of up to 30%
- Calculated using phase-space simulation reweighted in  $\cos\theta_W$  and  $E_\gamma^*$
- Interpreting BR in terms of  $\lambda_B$  also non-trivial, LCDA not only depends on  $\lambda_B$
- Currently no LCDA model for  $B_c^+ \rightarrow \mu^+ \nu_\mu \gamma$
- Present main result for  $E_\gamma^* > 1.0 \text{ GeV}$  using simple well-defined LCDA model to allow easy comparison with Belle
- Provide full efficiency map in  $E_\gamma^*$  and  $\cos\theta_W$  to allow for re-interpretation and change of model parameters



Efficiency dependence on  $\lambda_B$  (top) and exemplary efficiency map in  $E_\gamma^*$  and  $\cos\theta_W$  (bottom).

- First search for  $B^+ \rightarrow \mu^+ \nu_\mu \gamma$  at LHCb
- First search for  $B_c^+ \rightarrow \mu^+ \nu_\mu \gamma$ 
  - Comes for free in LHCb analysis
  - Which information can we gain from  $B_c^+ \rightarrow \mu^+ \nu_\mu \gamma$ ?
- Analysis possible using photon conversion in VELO for vertex reconstruction and peaking  $m_{corr}$
- Analysis strategy is in place
  - Developed new data-driven method to model background from  $\pi^0$  and  $\eta$
  - First optimisation maximising sensitivity on  $\mathcal{B}(B^+ \rightarrow \mu^+ \nu_\mu \gamma)$  in place
- Selection of candidates still being optimised
- Further cross-checks of the background modelling required
- Expected sensitivity towards  $\mathcal{B}(B_{(c)}^+ \rightarrow \mu^+ \nu_\mu \gamma)$  soon to be evaluated

## Future prospects

- Expect to collect three times more data during Run 3 of the LHC
- Commissioning almost completed and expect good quality data in 2024 and 2025
- Removed LHCb's hardware trigger
- Improved algorithms for reconstruction of  $\gamma \rightarrow e^+e^-$
- Hopefully LHCb can contribute to the Belle2 studies of  $B^+ \rightarrow \mu^+ \nu_\mu \gamma$  and provide clean experimental constraints on  $B$  meson LCDA

