



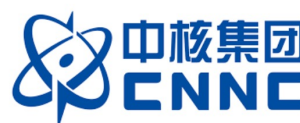
# Comparison of collective flow parameters for different isotopic combinations in Xe+Sn collisions from 65 to 150 MeV/u

NuSym 2024, XIIth International Symposium on Nuclear Symmetry Energy  
GANIL, Caen, France

2024. 9 .10 .Tue

Seon Ho Nam

GANIL



# Physics Motivation

- Nuclear Equation of State

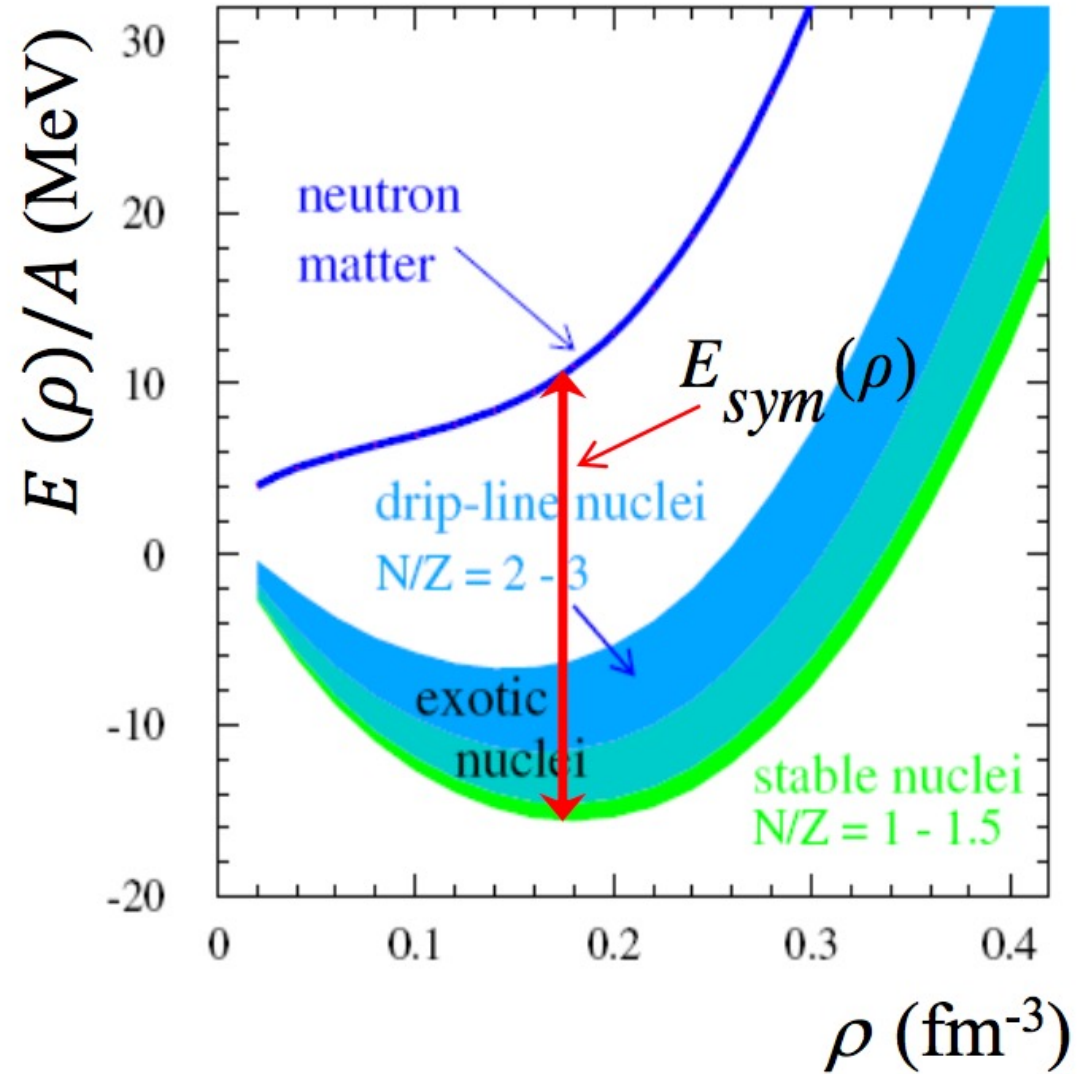
$$E(\rho, \delta)/A = \underbrace{E(\rho_n = \rho_p)}_{\text{Iso-scalar}} + \underbrace{E_{sym}(\rho)\delta^2}_{\text{Iso-vector}}$$

$$E_{sym}(\rho) = \frac{1}{2} \frac{\partial^2 E}{\partial \delta^2} \approx E(\rho)_{\text{pure neutron matter}} - E(\rho)_{\text{symmetric nuclear matter}}$$

$$\text{with } \rho = \rho_n + \rho_p, \quad \delta = (\rho_n - \rho_p)/\rho$$

- Nuclear Symmetry Energy

$$E_{sym}(\rho) = S + \frac{L_{sym}}{3} \left( \frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left( \frac{\rho - \rho_0}{\rho_0} \right)^2 \dots$$



# Analysis

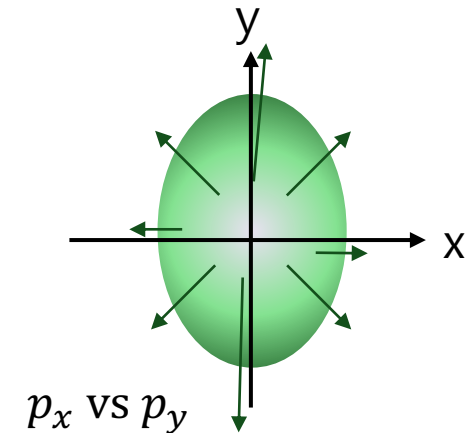
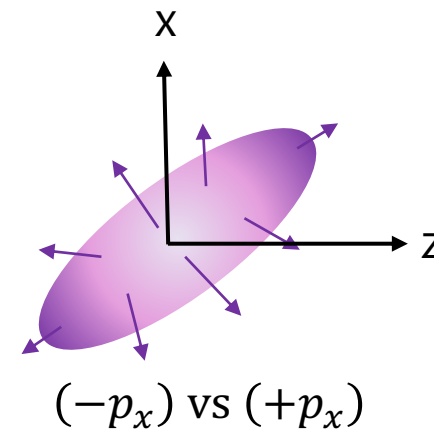
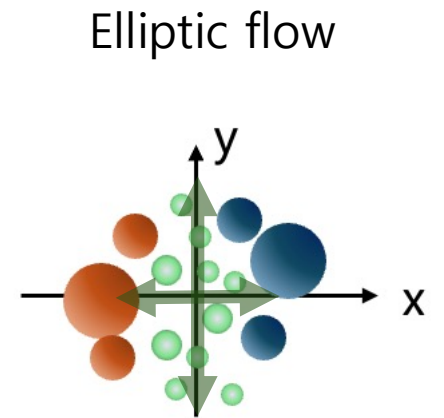
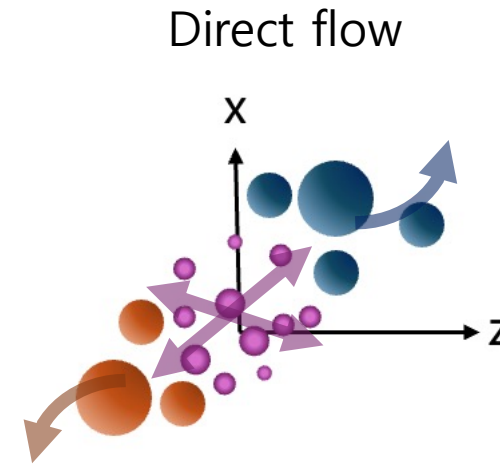
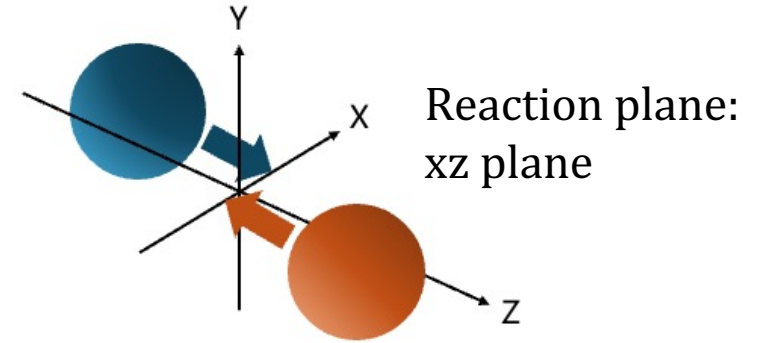
- Collective flow
- Fourier expansion of azimuthal distributions :  

$$\frac{dN}{d(\phi - \psi_r)} = \frac{N_0}{2\pi} \left( 1 + 2 \sum_{n \geq 1} v_n \cos n(\phi - \psi_r) \right)$$
 where,  $\psi_r$  : azimuthal angle of reaction plane

- $v_1$  is direct flow and  $v_2$  is elliptic flow.

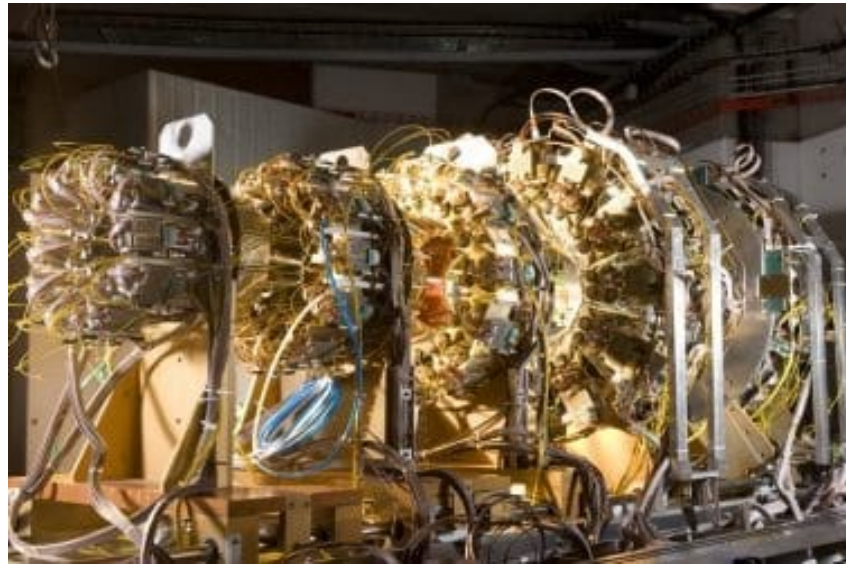
$$v_1 \equiv \langle \cos(\phi - \psi_r) \rangle = \left\langle \frac{p_x}{p_t} \right\rangle$$

$$v_2 \equiv \langle \cos 2(\phi - \psi_r) \rangle = \left\langle \frac{p_x^2 - p_y^2}{p_t^2} \right\rangle$$



# Experiment & Model

❖ INDRA Campaign 4<sup>th</sup>



- $^{129}_{54}\text{Xe} + ^{124}_{50}\text{Sn} @ 150, 80 \text{ and } 65 \text{ MeV/u}$
  - $^{129,124}_{54}\text{Xe} + ^{124,112}_{50}\text{Sn} @ 100 \text{ MeV/u}$
- N/Z : 1.433, 1.386, 1.317 and 1.269

❖ ImQMD model

Improved Quantum Molecular Dynamics with Skyrme parameter set SkM\* and SLy4 are used.

Para.	$\rho_0$	$E_0$	$K_0$	$S_0$	$L$	$K_{sym}$	$m^*/m$	$m_n^*/m$	$m_p^*/m$
SLy4	0.160	-15.97	230	32	46	-120	0.69	0.68	0.71
SkM*	0.160	-15.77	217	30	46	-156	0.79	0.82	0.76

*Y. Zhang et al. / Physics Letters B 732 (2014) 186–190*

# $v_{1,2}^s$ vs $p_t^0$ from Experiment and ImQMD

- Flow parameters of isotopes of LCPs and IMFs are calculated at IW1 ( $0.21 < b_0 < 0.42$ ) window.


Z = 1 : 1H, 2H, 3H      Z = 2 : 3He, 4He, 6He -> LCPs

Z = 3 : 6Li, 7Li, 8Li      Z = 4 : 7Be, 9Be, 10Be -> IMFs

- A consistent correlation with the N/Z ratio of collision system and N/Z ratio of particle of interest is founded by difference of  $v_1^s$ .
- Experimental data analysis results (Xe+Sn@100AMeV) are compared with ImQMD model with SkM\* and SLy4 parameter sets

# Summary

- Flow parameters are calculated using Xe + Sn isotopic collision systems from INDRA campaign 4<sup>th</sup> experiment.
- Relation between N/Z ratio of collision system and N/Z of poi is founded
- Analysis results are compared with ImQMD model with its two parameter sets.



Thank you for your attention!

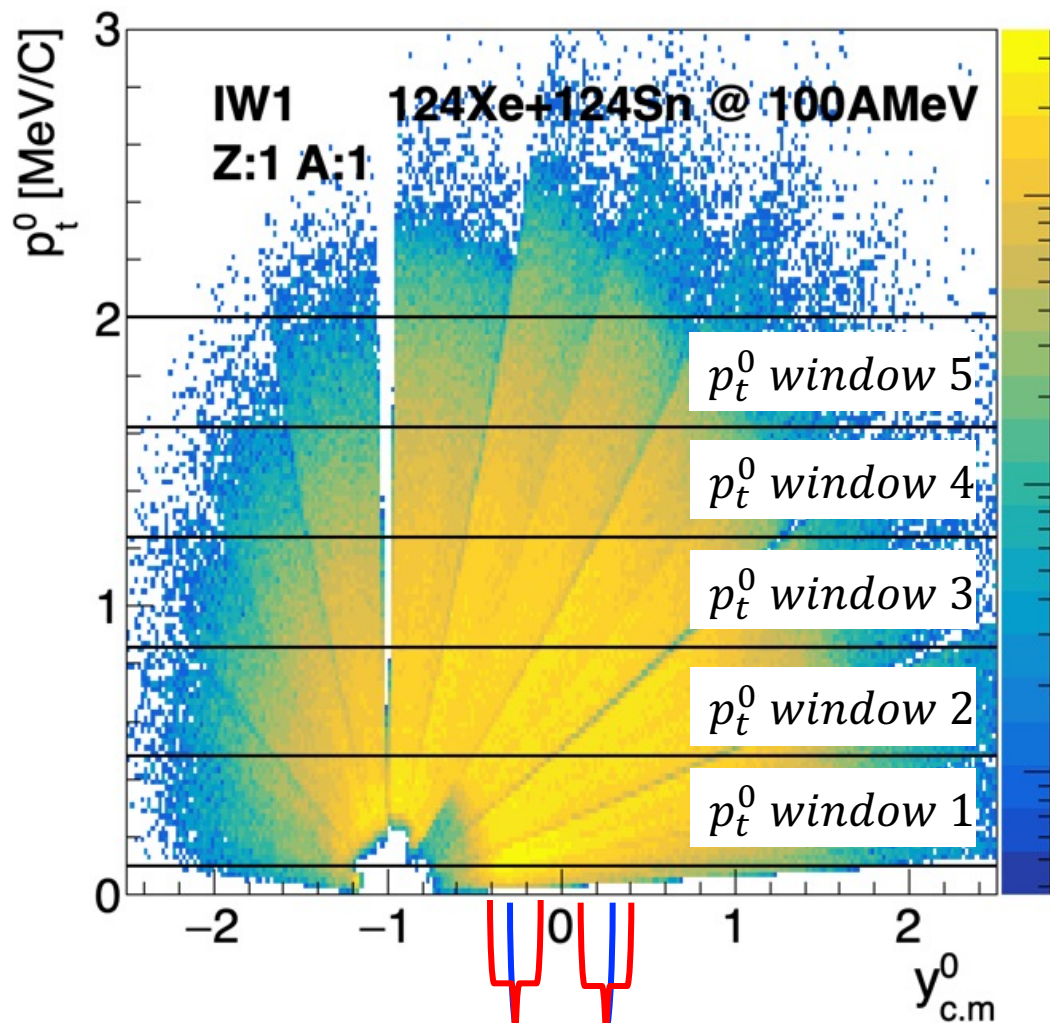
Merci de votre attention !

### **Acknowledgement**

This work was supported by the National Research Foundation funded by MSIT of Korea (Grant No. 20181A5A1025563) and Grand Accélérateur National d'Ions Lourds (GANIL).

Back up





$$v_2^S : -0.3 < y_{cm}^0 < 0.3$$

$$v_1^S : 0.1 < y_{cm}^0 < 0.4$$

$$-0.4 < y_{cm}^0 < -0.1$$

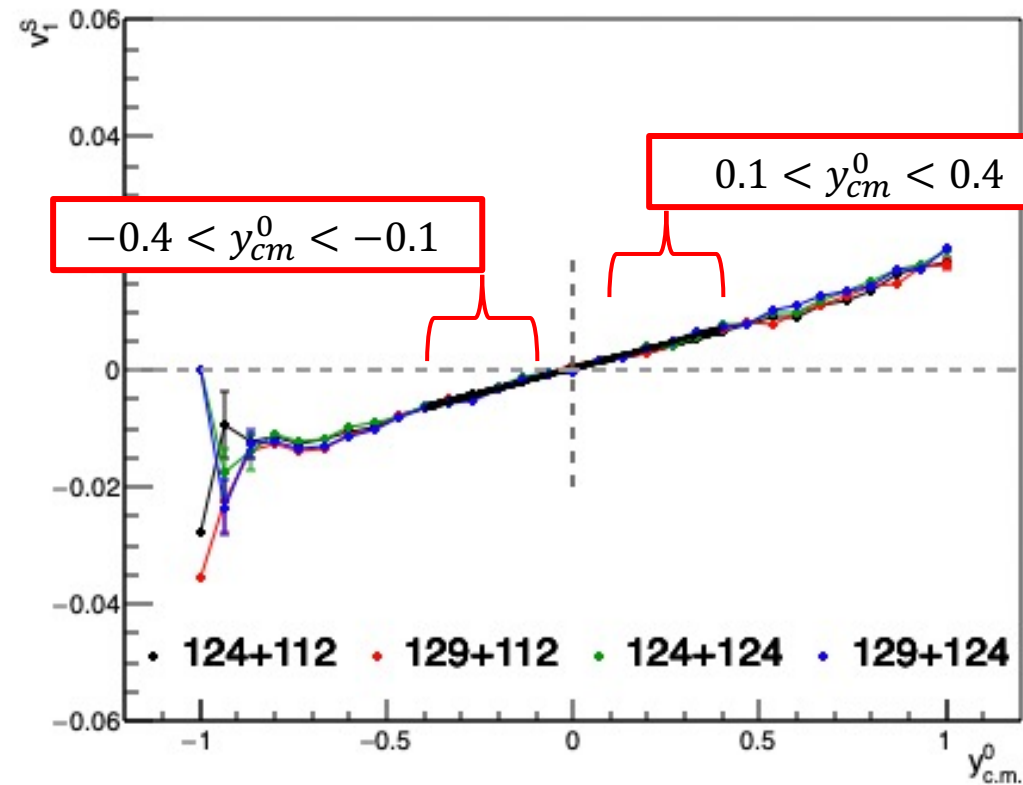
$$p_t^0 \equiv \left( \frac{p_t^{cm}}{A} \right) * \left( \frac{\left( \frac{A_P + A_t}{2} \right)}{p_{beam}^{cm}} \right)$$

$$y_{cm}^0 (y > 0) = (y/|y_p|)^{cm}$$

$$y_{cm}^0 (y < 0) = (y/|y_t|)^{cm}$$

System size scaled parameter

$$v_n^S = v_n \langle p_t^0 \rangle / \left( A_P^{1/3} + A_T^{1/3} \right)$$



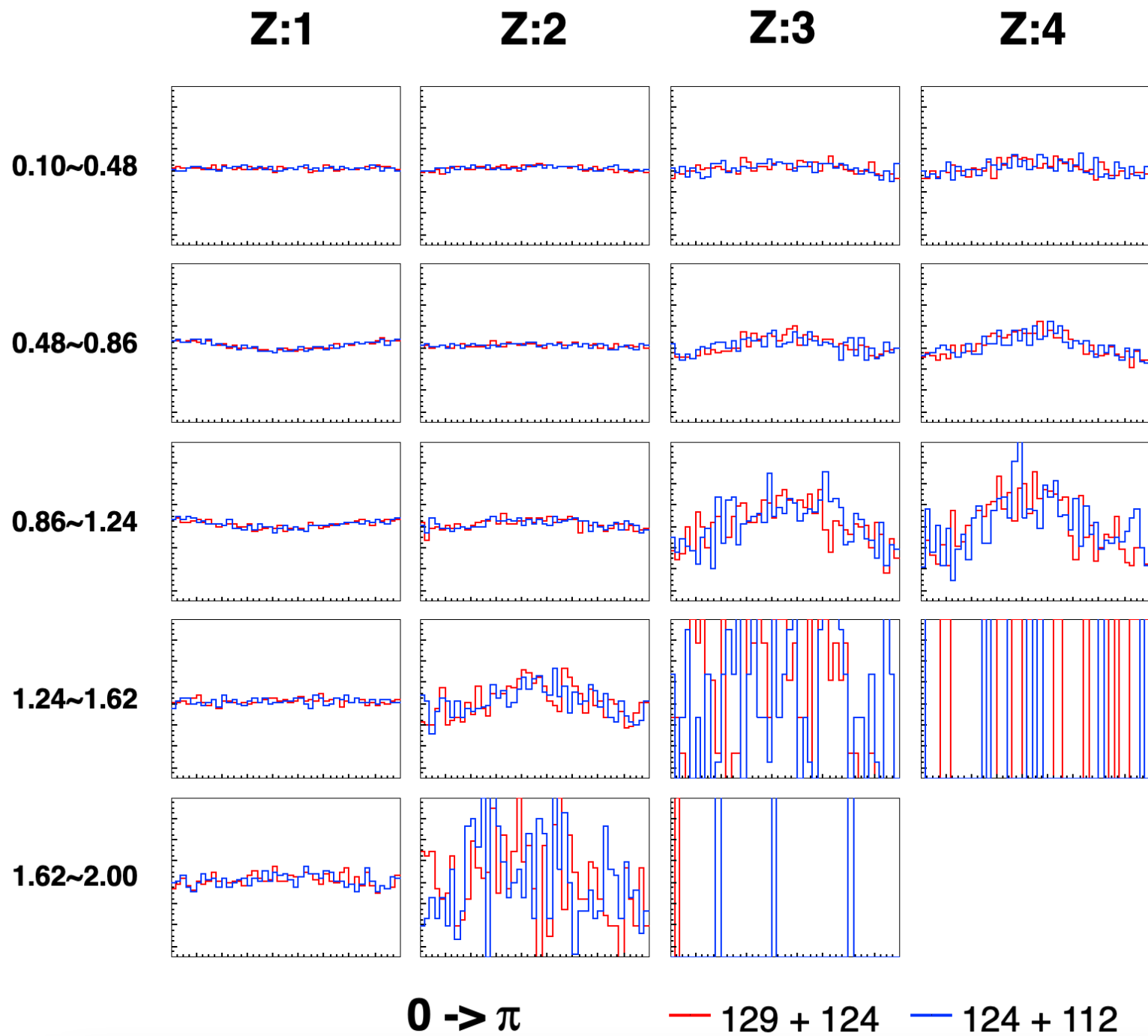
$v_1^S$  :

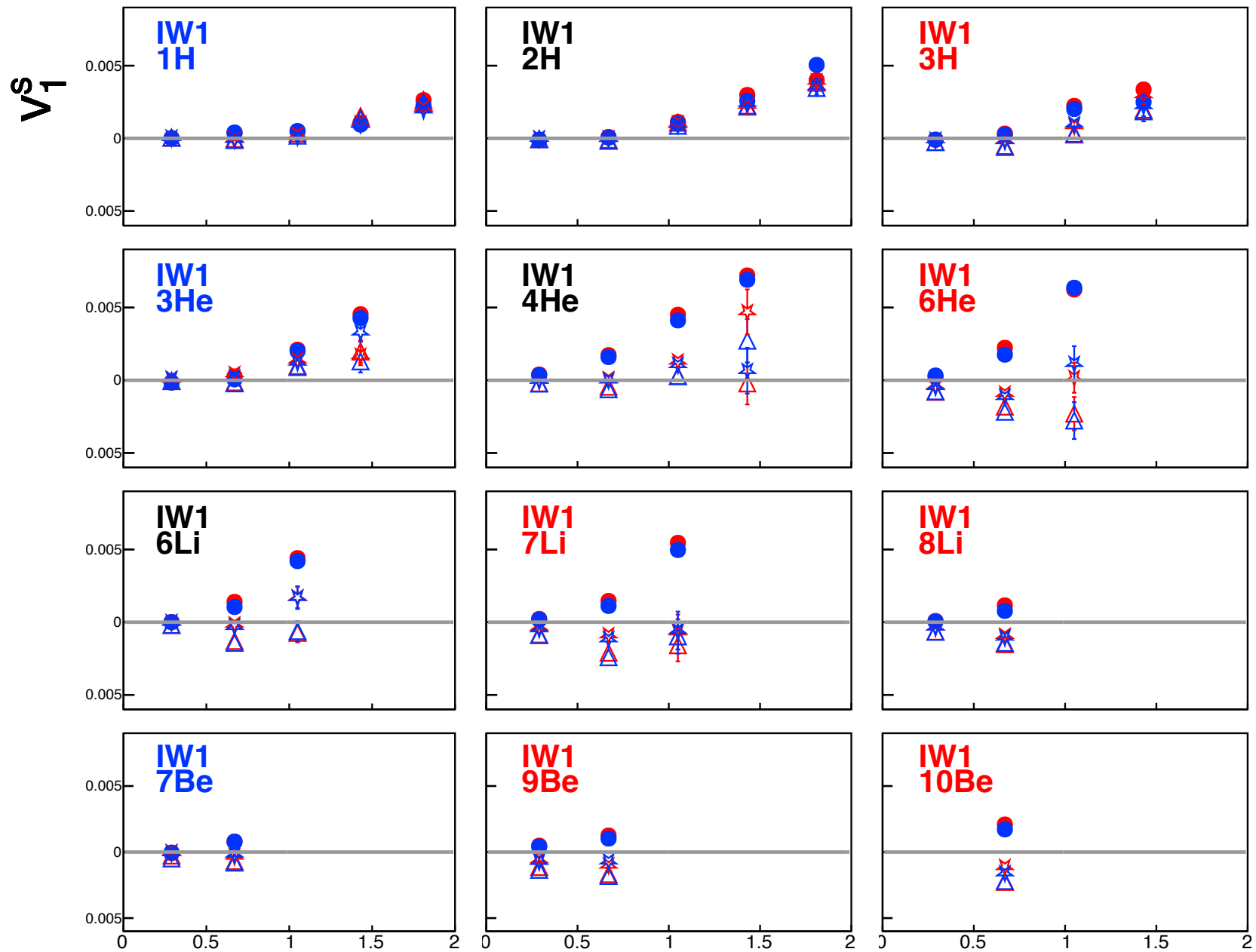
$$0.1 < y_{cm}^0 < 0.4 \rightarrow p_x/p_t$$

$$-0.4 < y_{cm}^0 < -0.1 \rightarrow -(p_x/p_t)$$

Squeeze out angle  
distribution

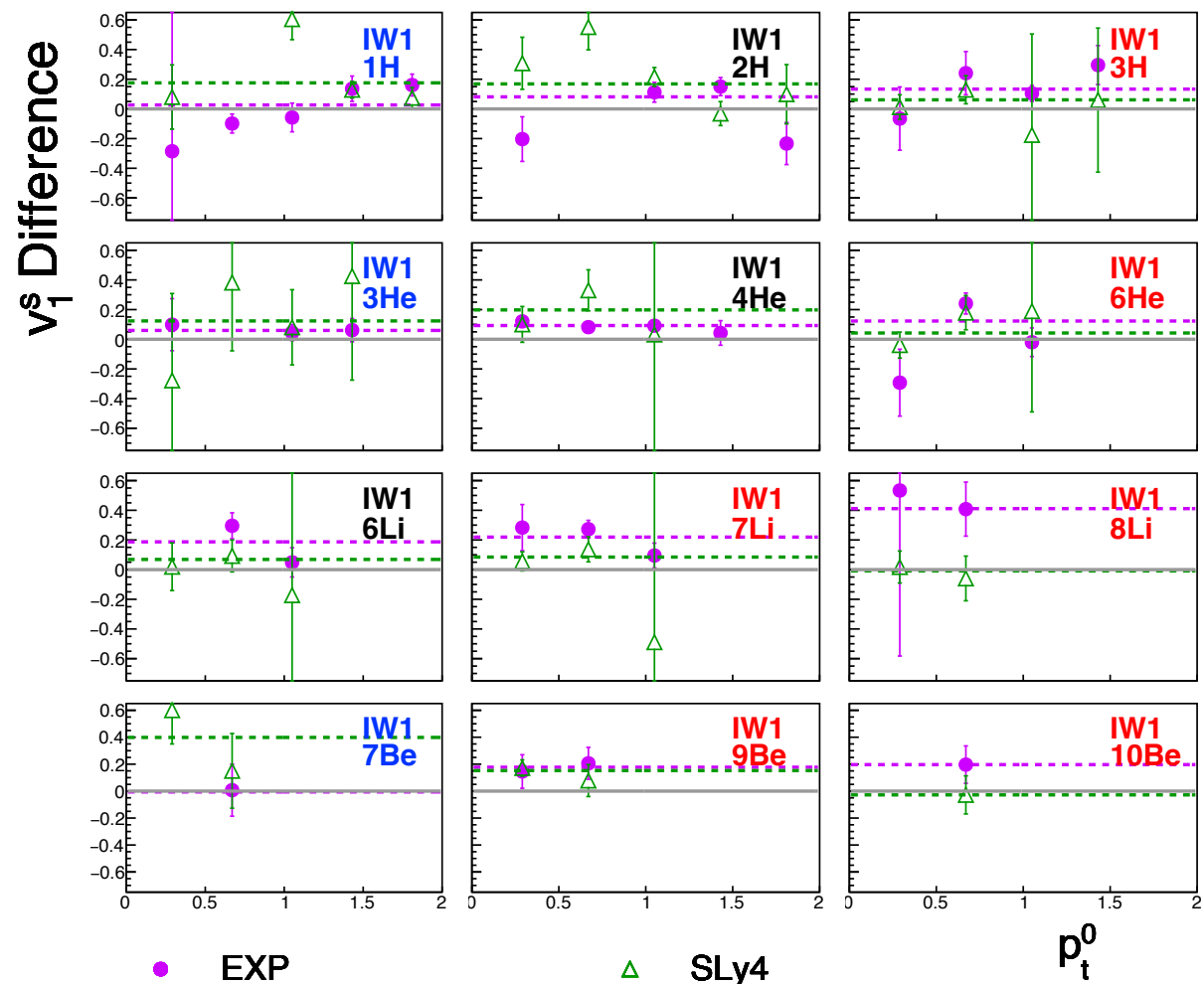
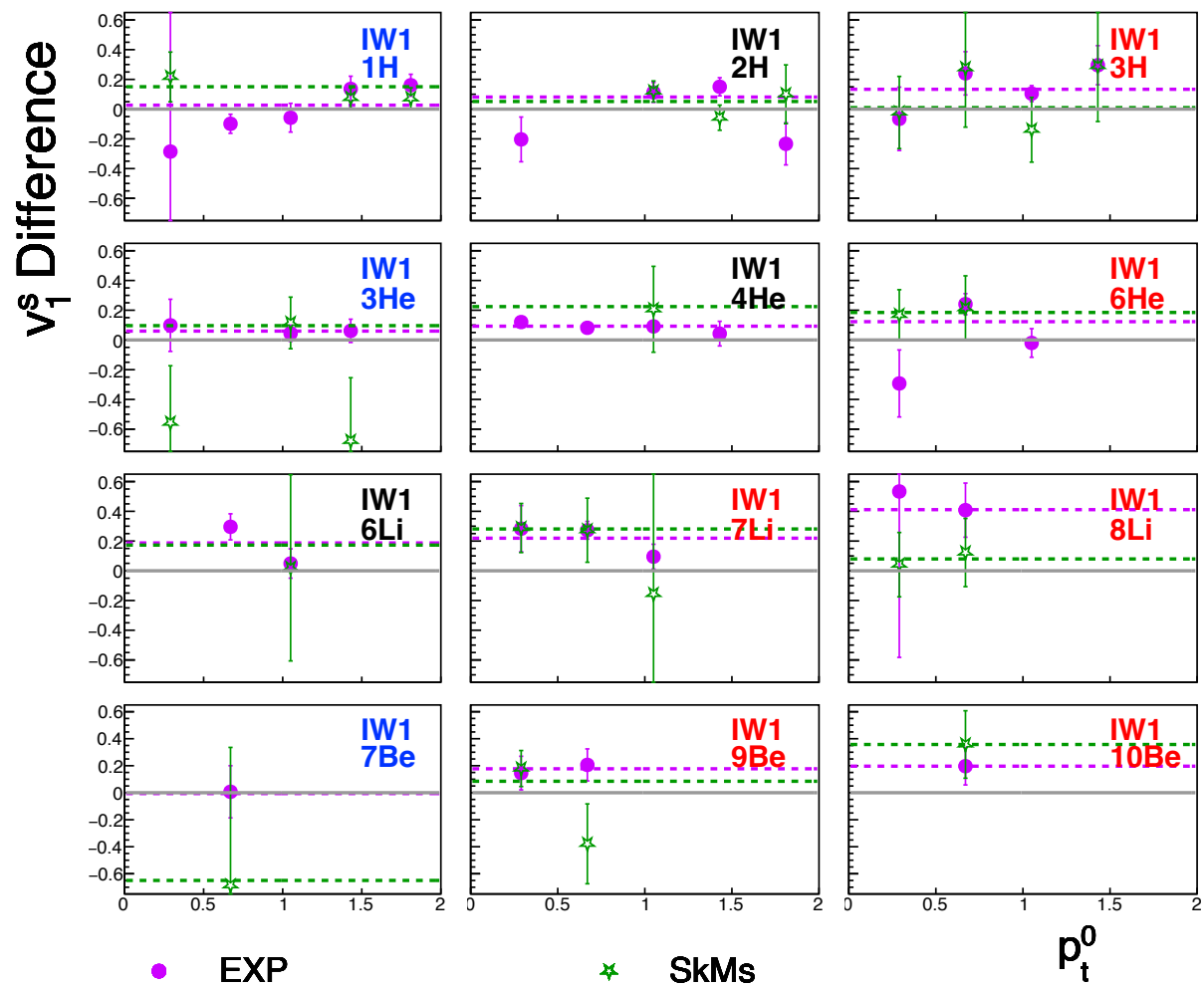
$$-0.3 < y_{cm}^0 < 0.3 \rightarrow (p_x^2 - p_y^2)/p_t^2$$

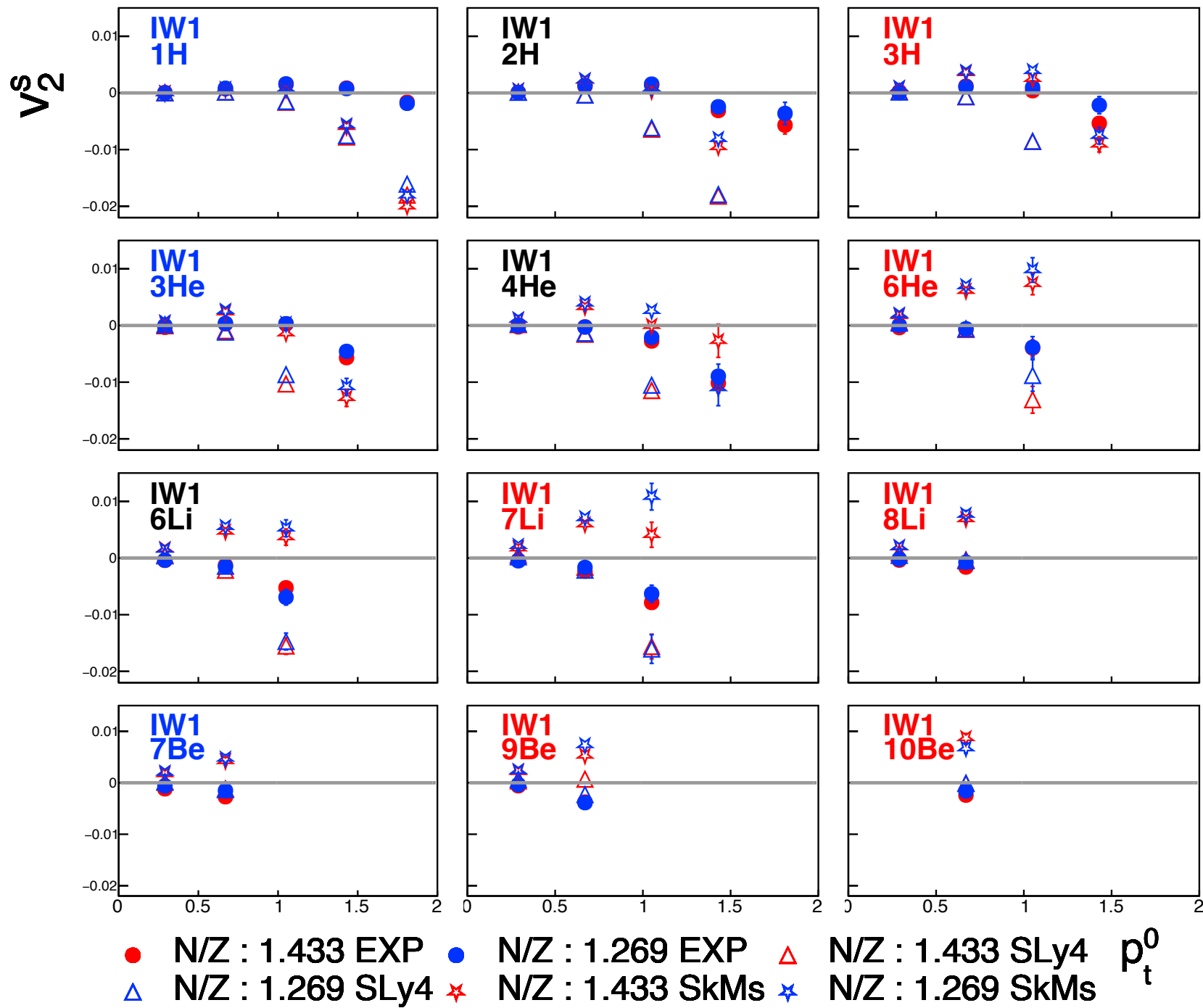




● N/Z : 1.433 EXP    ● N/Z : 1.269 EXP    △ N/Z : 1.433 SLy4     $p_t^0$   
△ N/Z : 1.269 SLy4    ★ N/Z : 1.433 SkMs    ★ N/Z : 1.269 SkMs

$$v_1^s \text{ Difference} \equiv \frac{v_1^s(\text{N/Z higher}) - v_1^s(\text{N/Z lower})}{\sqrt{v_1^s(\text{N/Z higher})^2 + v_1^s(\text{N/Z lower})^2}}$$





$$v_2^S \text{ Difference} \equiv \frac{v_2^S(\text{N/Z higher}) - v_2^S(\text{N/Z lower})}{\sqrt{v_2^S(\text{N/Z higher})^2 + v_2^S(\text{N/Z lower})^2}}$$

