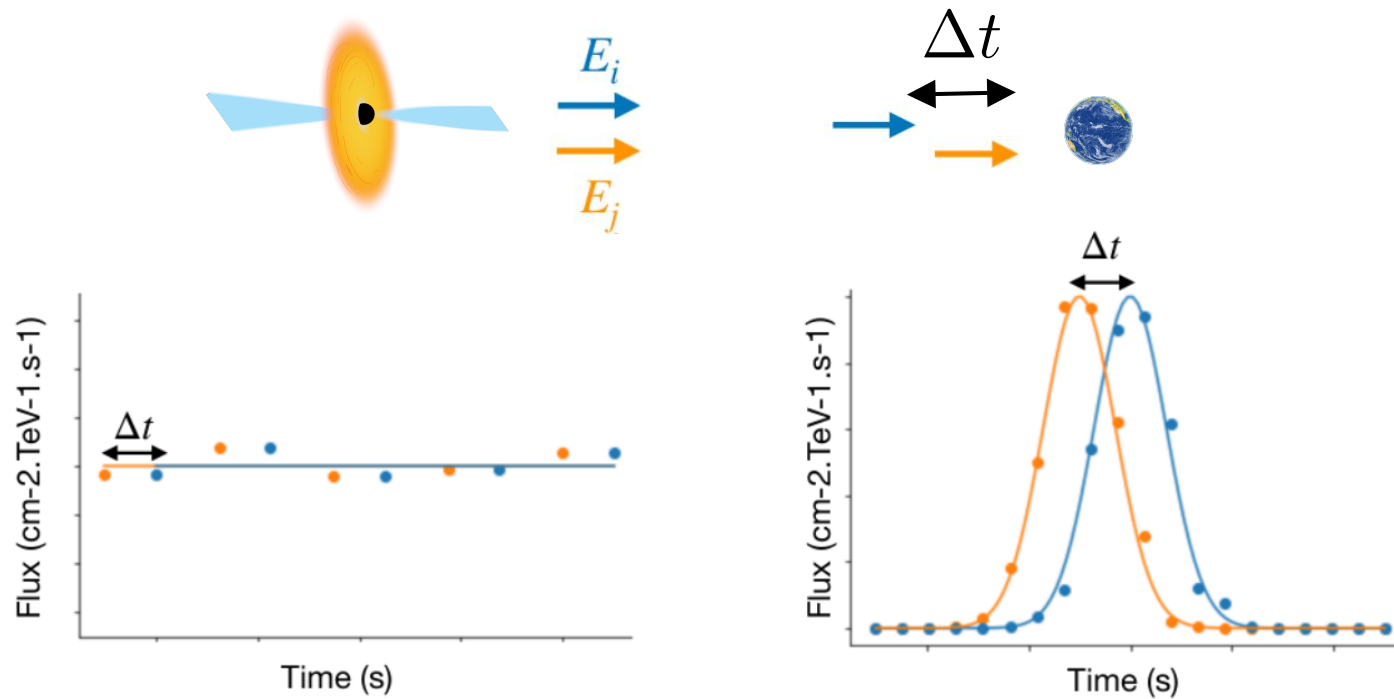


Lorentz invariance violation (LIV)

$$E^2 = p^2 c^2 \rightarrow E^2 = p^2 c^2 \times \left[1 \pm \sum_{n=1}^{\infty} \alpha_n \left(\frac{E}{E_{QG}} \right)^n \right] \rightarrow v_\gamma(E_\gamma) \neq c$$

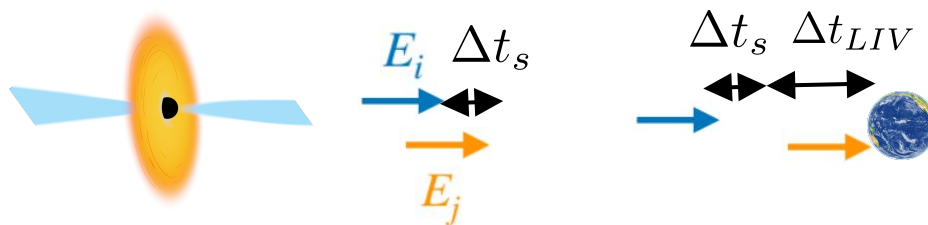


$$\lambda_n = \frac{\Delta t_n}{\Delta E_n \kappa_n(z)} = \pm \frac{n+1}{2H_0 E_{QG}^n}$$

Limit at n=1

- Blazars, GRBs, pulsars
- Intrinsic lag

$$\Delta t = \Delta t_{LIV} + \Delta t_{source}$$



$$\Delta t_{source}$$

Redshift-independent
Sources and flares -dependent

$$\Delta t_{LIV}$$

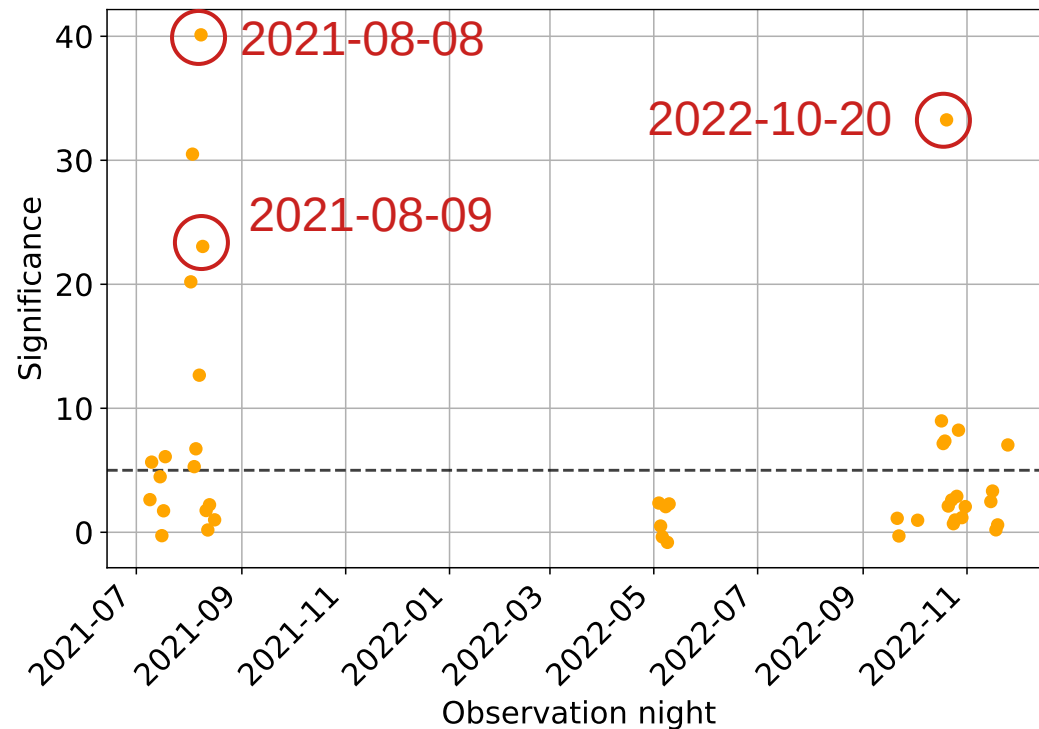
Redshift-dependent
Sources and flares -independent

- Combine different flares and sources
- Consortium H.E.S.S. , MAGIC, VERITAS, LST-1

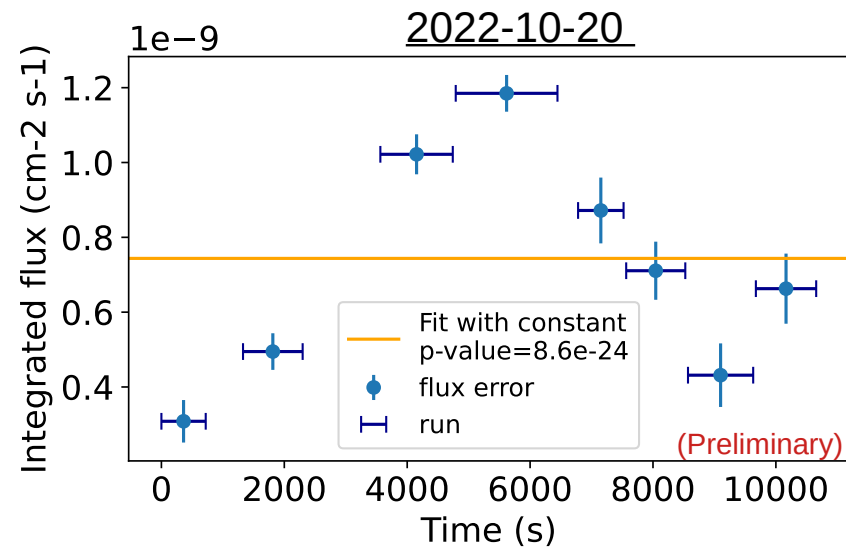
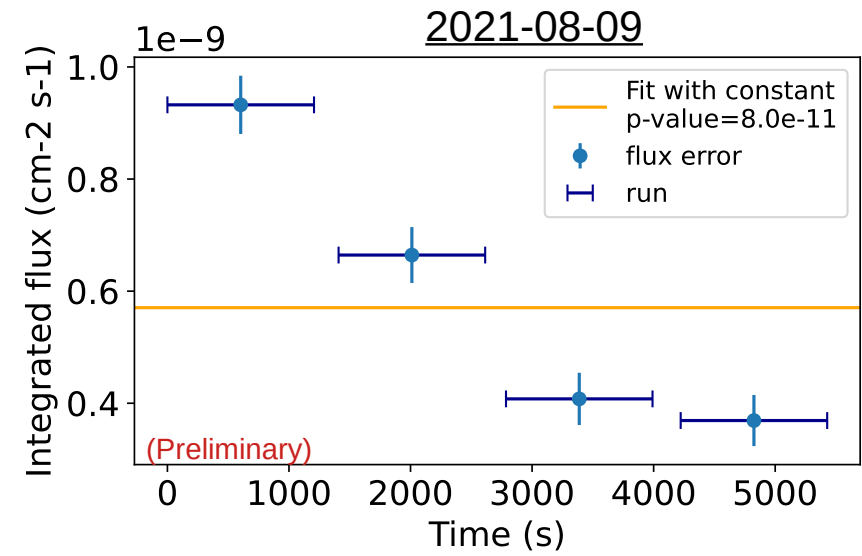
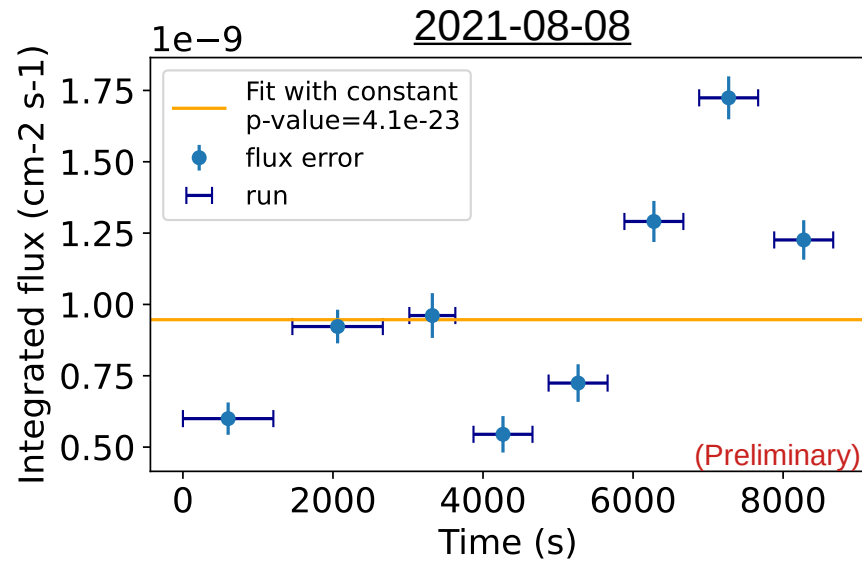
All blazar data of LST-1 from January 2021 to June 2023

- Standard run quality selection
- Standard gammaness cut at 0.6
- All sky MC IRFs and RFs
- Energy range = [150GeV ; 10TeV]
- Search for significant nights (Li&Ma) , $S > 5\sigma$
- Variability : fit lightcurve with constant function, variable if pvalue $< 5\sigma$

Significance of BL Lac ($z=0.069$) observation nights

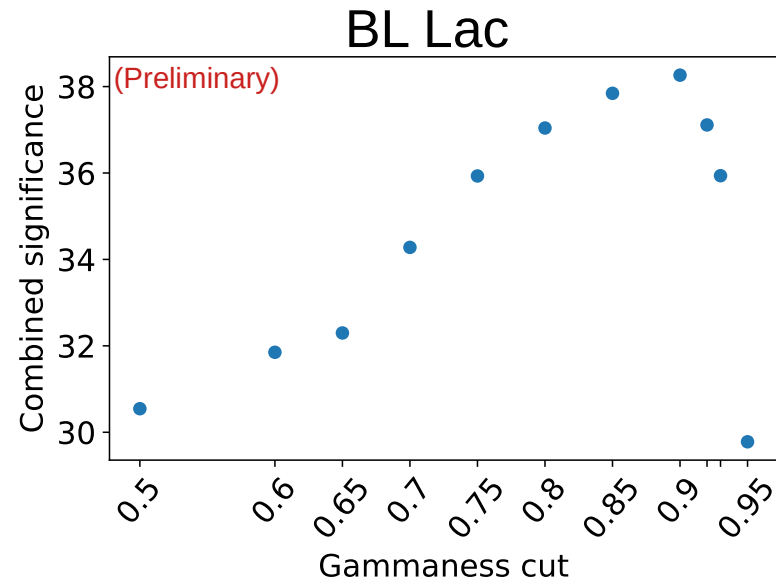
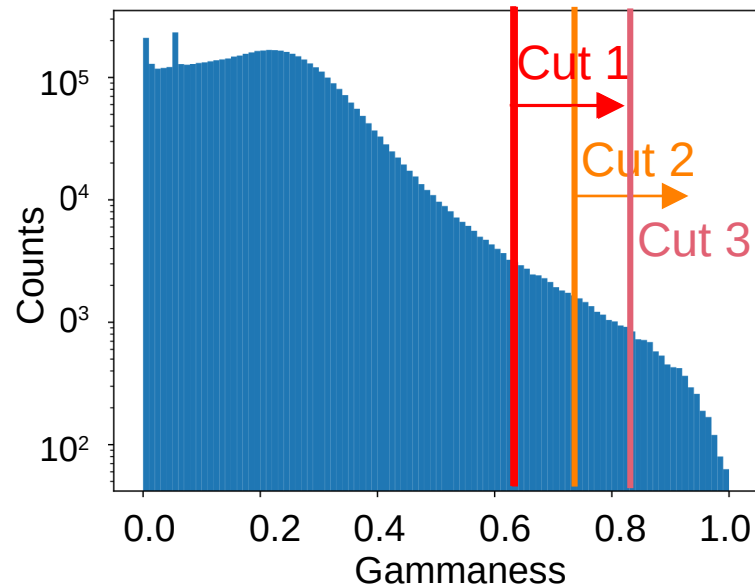


BL Lac variable nights



Non-variable sample

Select different gammaness cuts
and search for the significance



$$S_{cut} = \sqrt{\sum_{non-var\ night} S_n^2}$$

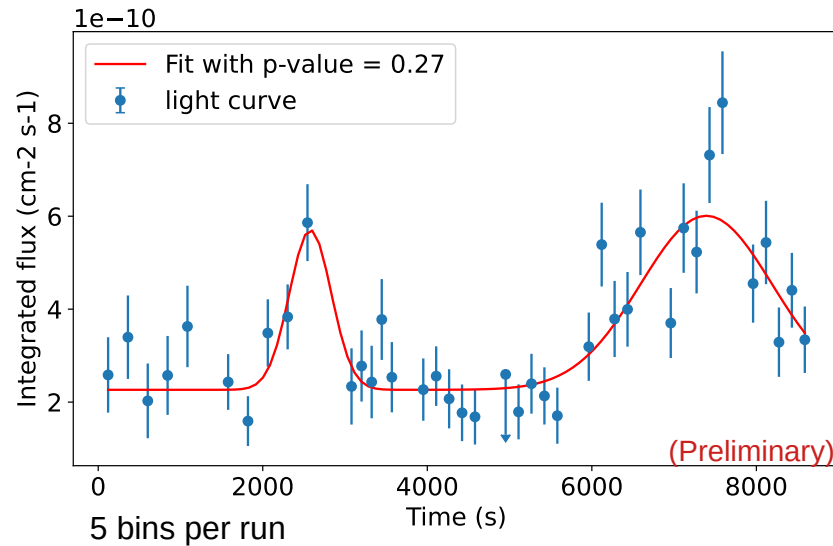
→ For BL Lac : 0.9

Search for a variability template and extract sample properties (energetic and temporal distributions)

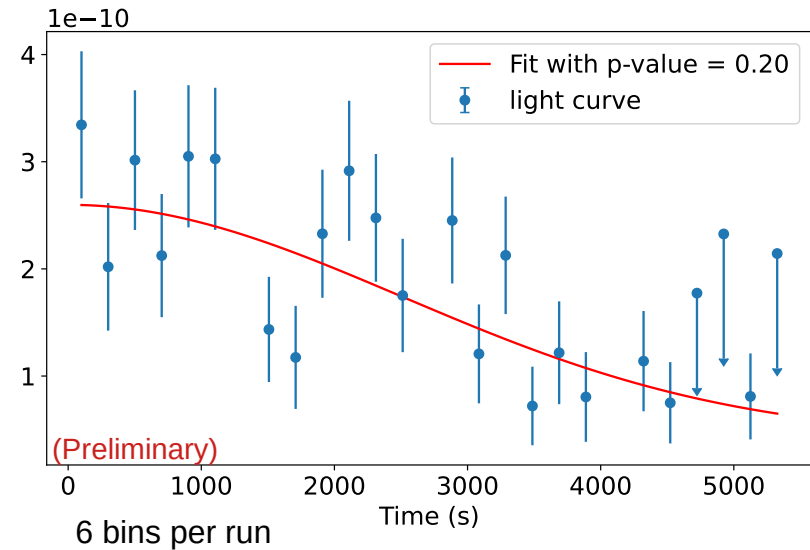


- Define two energy bins : **lower** and **higher** than median of counts
- Find a parametric model for the lightcurve of the low energies sample : selected if p-value > 0.05 (2σ)
- No significant disagreement between low and high energies

BL Lac 2021-08-08



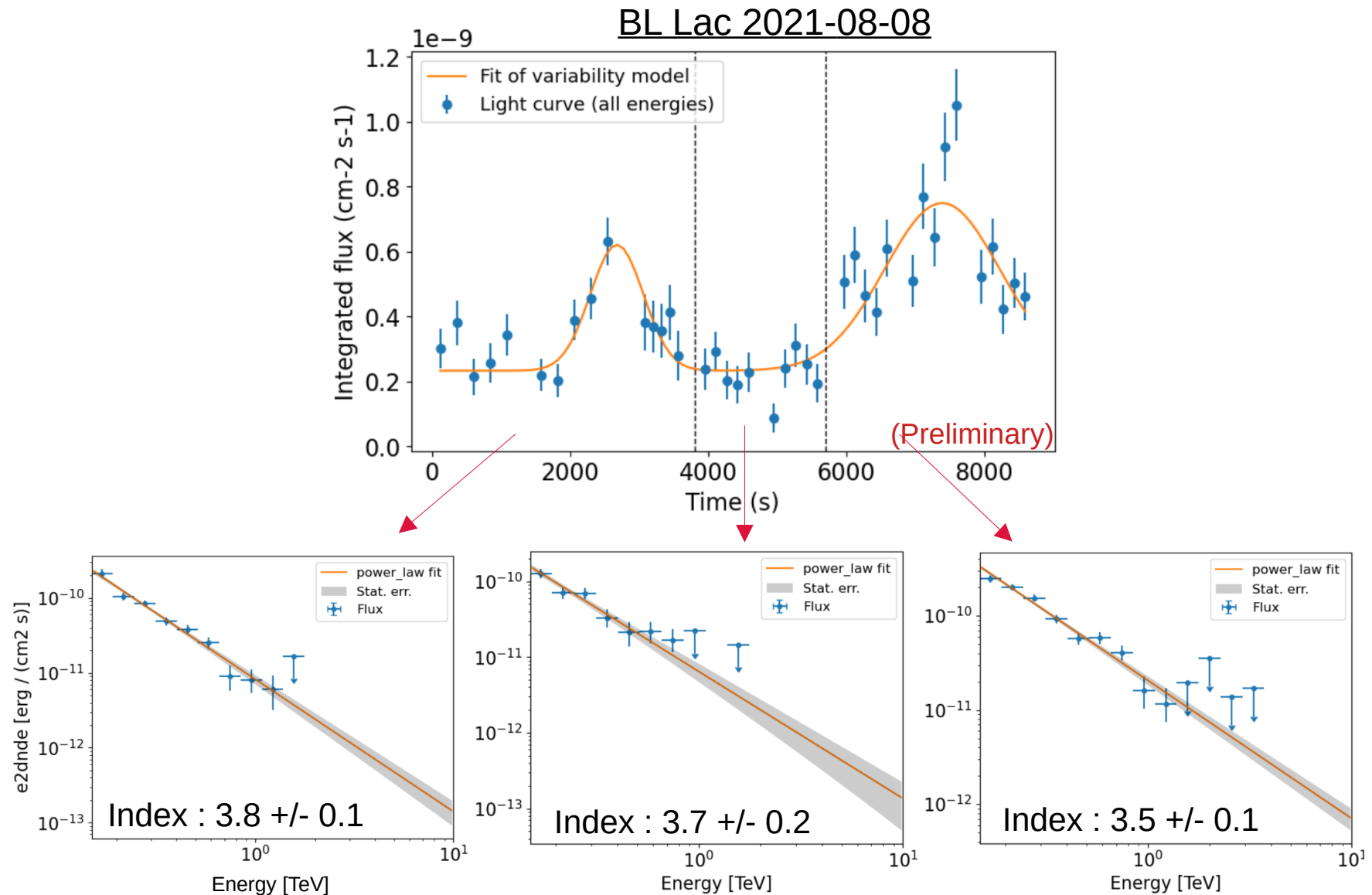
BL Lac 2021-08-09



$$f(t) = A_1 e^{-\frac{(t-\mu_1)^2}{2\sigma_1^2}} + A_2 e^{-\frac{(t-\mu_2)^2}{2\sigma_2^2}} + C_0$$

$$g(t) = A e^{-\frac{(t-\mu)^2}{2\sigma^2}} + C$$

- No significant time-variation of spectra parameters



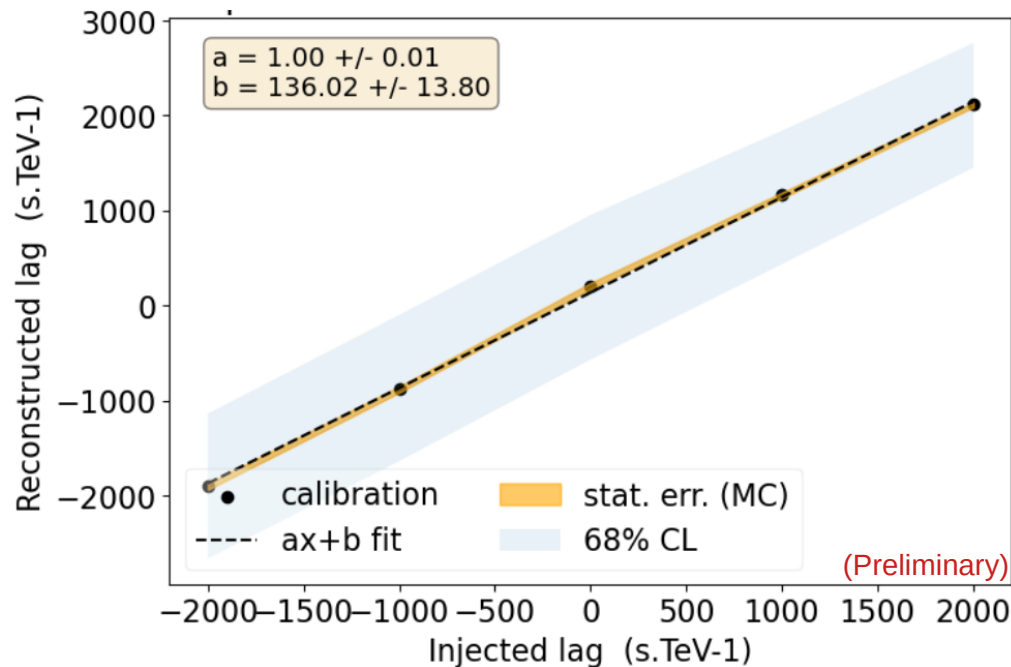
- LIVelihood software : likelihood method
- Lag λ = free parameter that minimizes the likelihood

Sample simulations to
validate LIV analysis



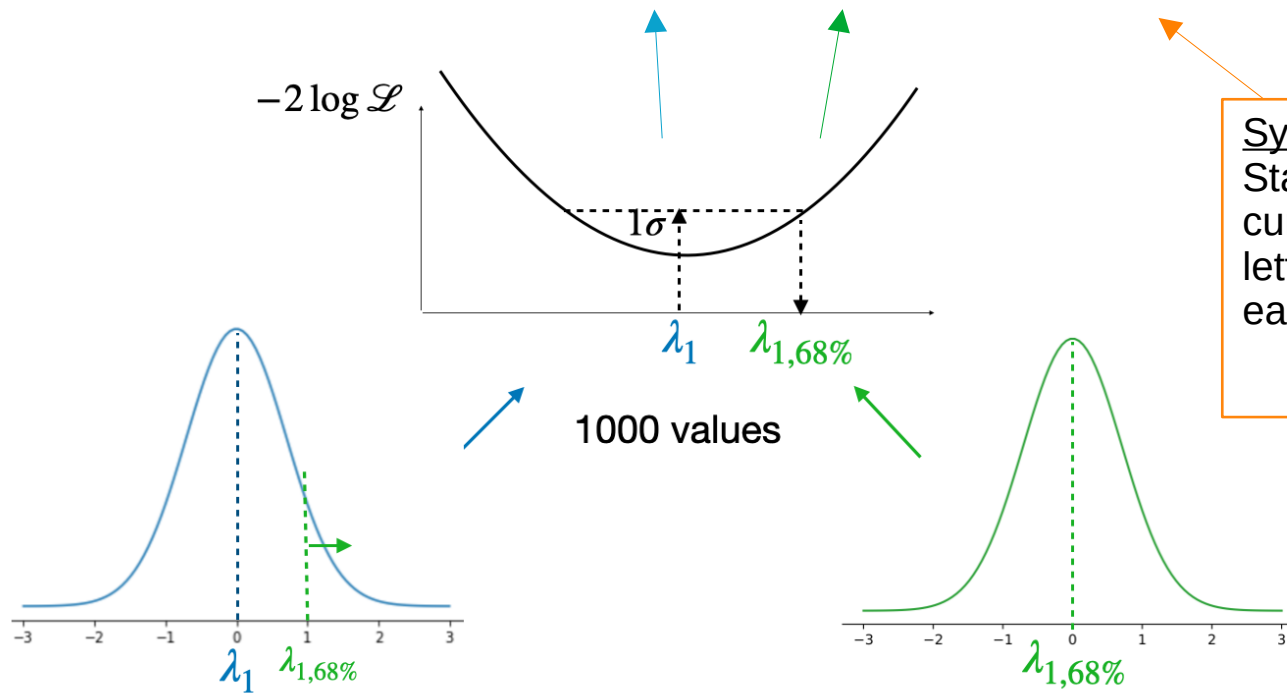
- Perform 1000 dataset simulations
- Calibration : inject lag to verify that LIVelihood reconstructs it well

BL Lac 2021-08-08 and 08-09 combined



LIV analysis on real data

Time delay : $\lambda_1 = (2060 \pm 2811 \pm 2479) \text{ s.TeV}^{-1}$
 $\phantom{\text{Time delay : }} \phantom{\text{ s.TeV}^{-1}}$

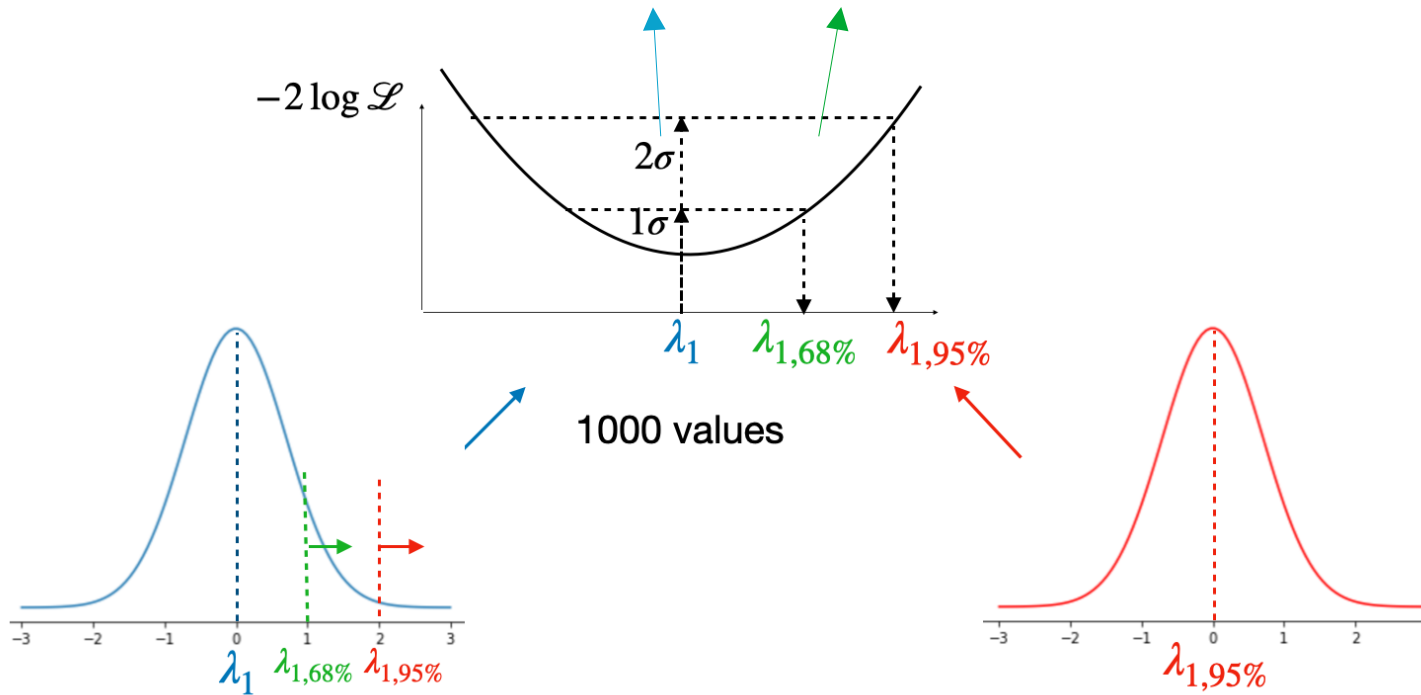


Systematics :

Statistical uncertainty of the light curve template : obtained by letting all parameters free in each of the 1000 simulations

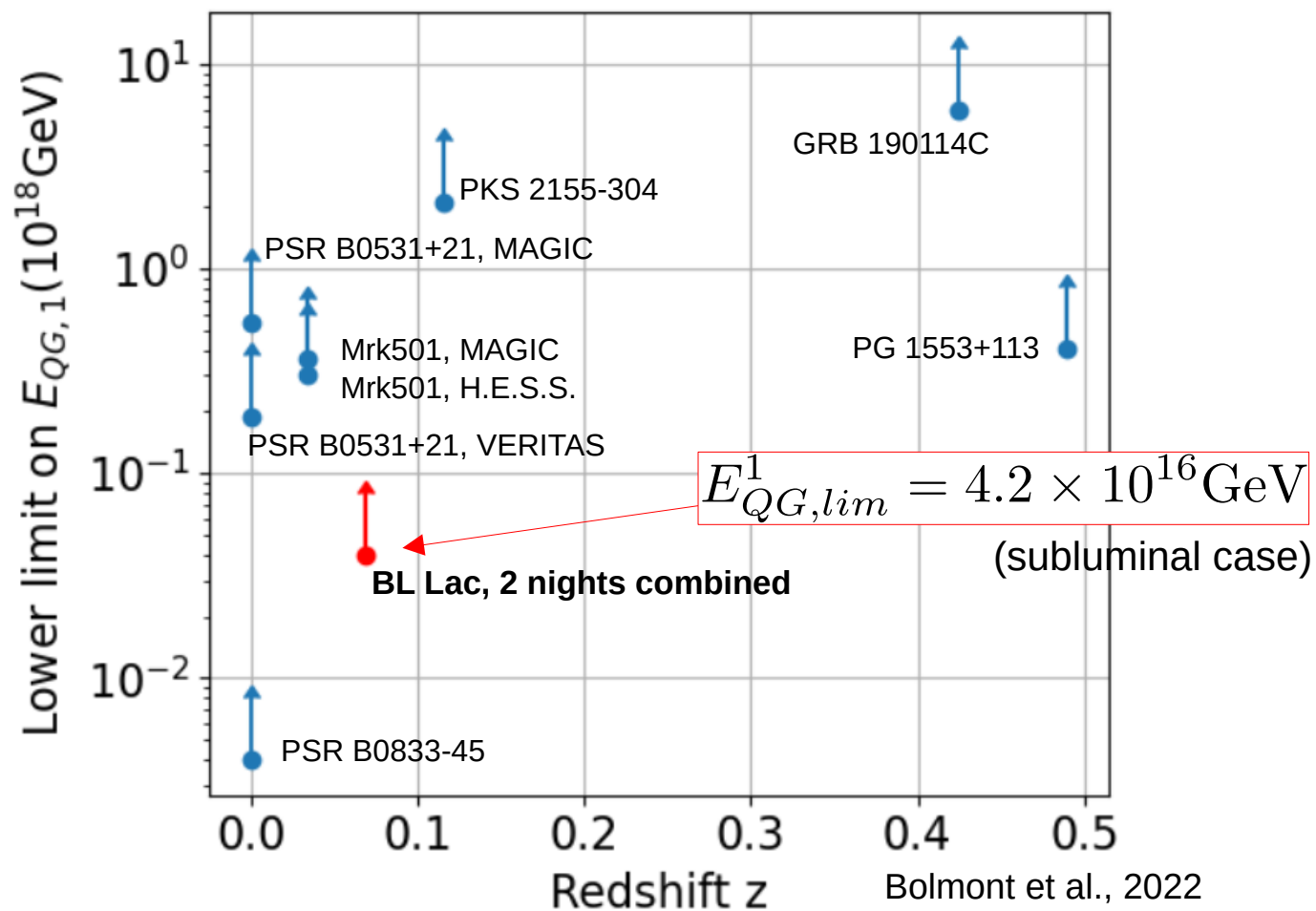
LIV analysis on real data

Time delay : $\lambda_1 = (2060 \pm 2811 \pm 2479) \text{ s.TeV}^{-1}$
 $\phantom{\text{Time delay : }} \phantom{\text{ s.TeV}^{-1}}$



Use $\lambda_{1,95\%} = \pm \frac{n+1}{2H_0 E_{QG,lim}^1}$ to extract : $E_{QG,lim}^1 = 4.2 \times 10^{16} \text{ GeV}$
 (subluminal case)

Comparison with other limits



Ongoing work :

- Until now, used arbitrarily $E_{\min} = 0.15\text{TeV}$;

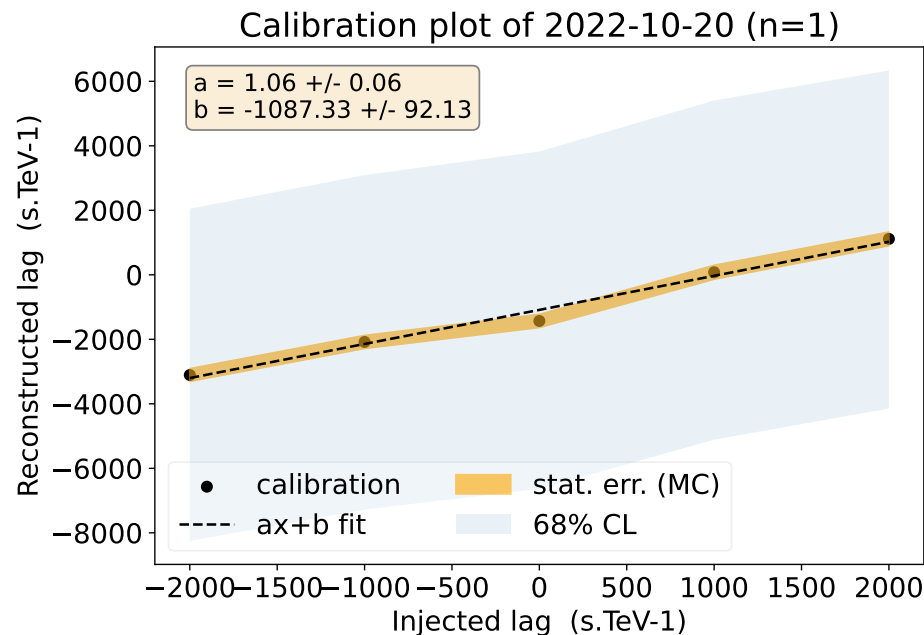
Updated the analysis with a safe mask threshold on the energy range : percentage of the effective area (10%) ;

21-08-08 : $E_{\min} = 0.25\text{TeV}$

21-08-09 : $E_{\min} = 0.19\text{TeV}$

22-10-20 : $E_{\min} = 0.40\text{TeV}$

→ Combining 3 nights : offset in 2022-10-20 calibration plot → investigating



- Producing data for gammaness E-dependent (θ^2 E-dependent in the future)