

Quantum computing for high-energy physics simulations

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15th of January 2024



Outline:

→ Introduction:

Why quantum computing and high-energy physics?

- Basics of high-energy physics

- How to compute a cross section

- Basics of quantum computing

- How to build a quantum circuit

- Applications

- Quantum integration [**Agliardi, Grossi, MP, Prati; 2201.01547**]

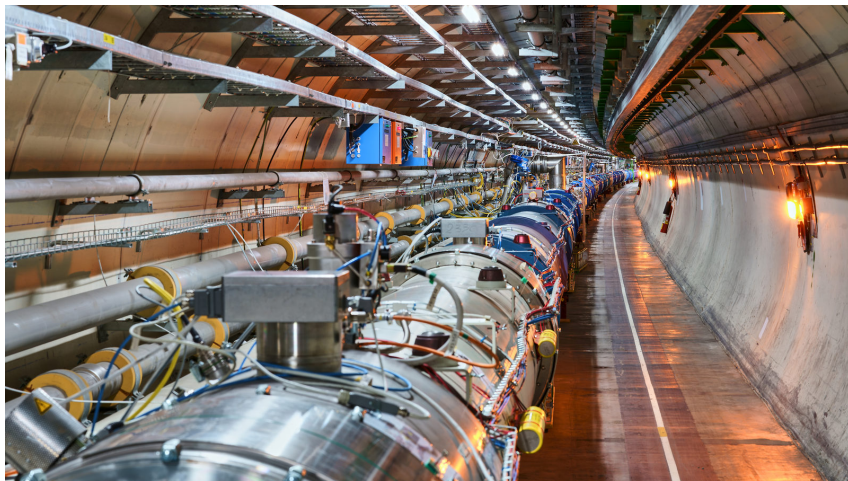
- Colour amplitudes [**Chawdhry, MP; 2303.04818**]

- Last discovery in high-energy physics (2012 @ LHC, CERN):
the Higgs boson!

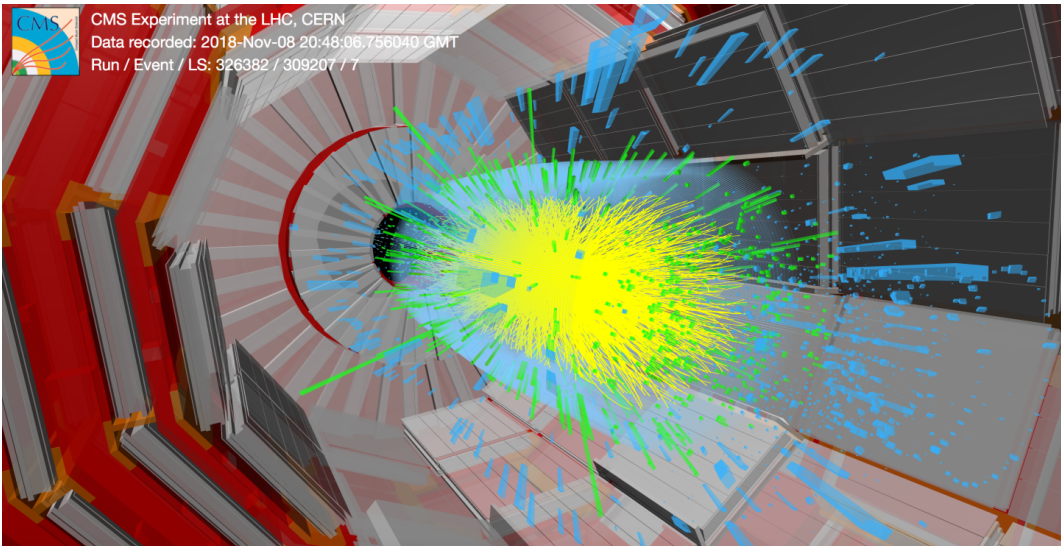


LHC @ CERN, Geneva (Switzerland)

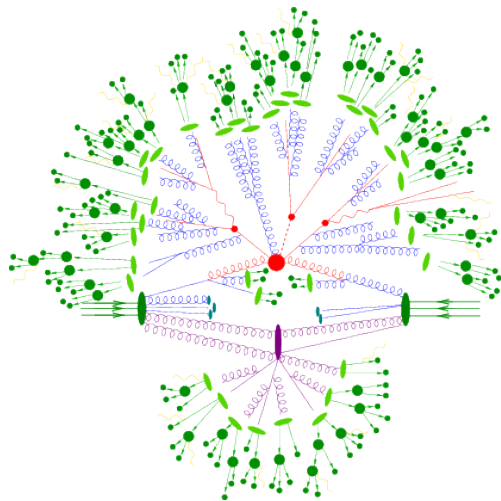
- 27km-long tunnel where protons are collided at high-energy (13.7 TeV currently)
- Allow to probe fundamental interactions



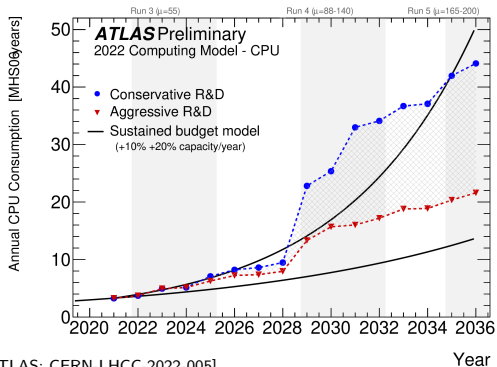
Life at the LHC (in reality)



- Factorisation of mechanisms at:
 - high-energy (perturbative)
 - Hard-scattering, parton-shower
 - low-energy (non-perturbative)
 - parton-distribution function, hadronisation, underlying events, ...
- Monte Carlo method/integration!
- All aspects are relevant when comparing theory predictions against experimental measurements!



Computing problem in high-energy physics



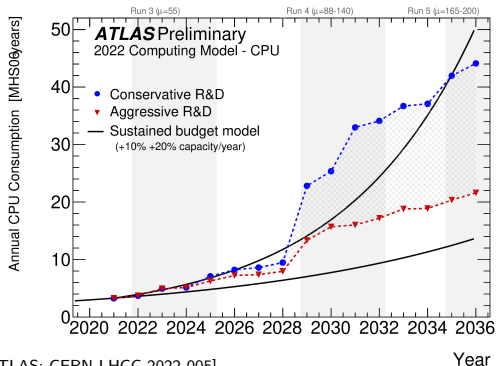
[ATLAS; CERN-LHCC-2022-005]

→ Event generation:

~ 15% of ~ 3 billion cpu.h.y^{-1}

→ More in: [Buckley; 1908.00167], [Valassi et al.; 2004.13687]

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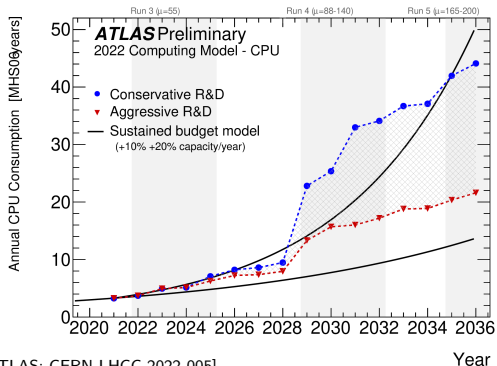
• One possible solution: GPU

→ Selected references: [Borowka et al.; 1811.11720],

[Carrazza et al.; 2002.12921, 2009.06635, 2106.10279], [Bothmann et

al.; 2106.06507] + [▶ Talk1](#) + [▶ Talk2](#)

Computing problem in high-energy physics



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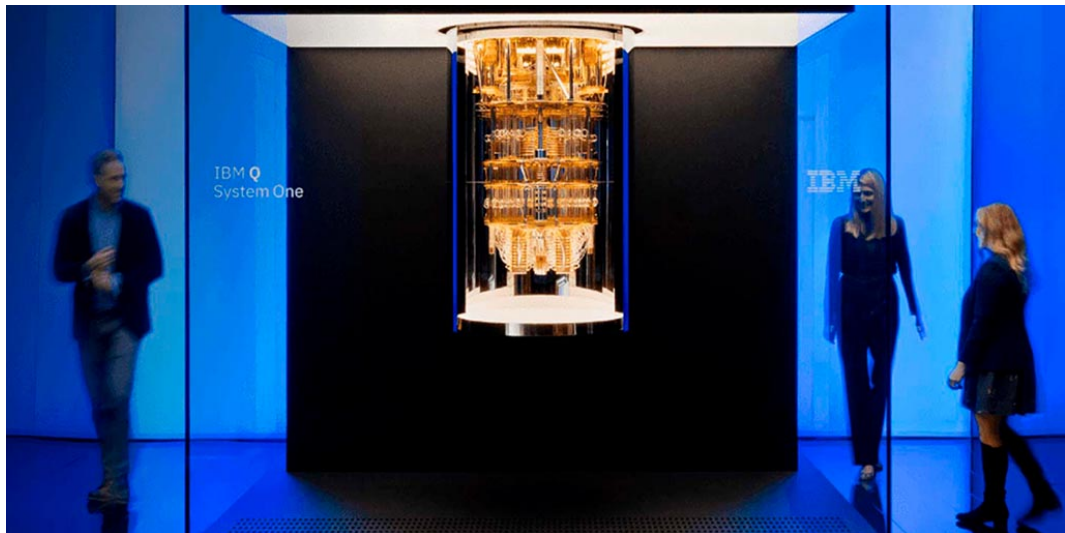
al.; 2106.06507] + [▶ Talk1](#) + [▶ Talk2](#)

• Can quantum computing be of any use in HEP?

→ to compute things faster/more efficiently?

→ to compute new things?

Quantum computers



[IBM]



[Landscape with the worship of the Golden calf, Claude Lorrain, Staatliche Kunsthalle, Karlsruhe (Germany)]

→ Quantum applications still in their infancy!

- Is it possible?

- Is there a (theoretical) quantum advantage?

- Is it more resource efficient than CPU/GPU?

→ Look at the example of quantum simulation/integration in HEP!

Reviews

- [Gray, Terashi; Gray:2022fou] (selected topics)
- [Delgado et al.; 2203.08805] (Snowmass)
- [Klco et al.; 2107.04769] (lattice)

Selected references

- **Amplitude/loop integrals:** [Ramirez-Uribe et al.; 2105.08703], [Bepari, Malik, Spannowsky, Williams; 2010.00046], [Chawdhry, MP; 2303.04818]
- **Parton shower:** [Bauer, de Jong, Nachman, Provasoli; 1904.03196], [Bepari, Malik, Spannowsky, Williams; 2010.00046], [Williams, Malik, Spannowsky, Bepari; 2109.13975], [Chigusa, Yamazaki; 2204.12500], [Gustafson, Prestel, Spannowsky, Williams; 2207.10694], [Bauer, Chigusa, Yamazaki; 2310.19881]
- **Machine learning:** [Filipek et al; 2105.04582], [Bravo-Prieto et al; 2110.06933], [Alvi, Bauer, Nachman; 2206.08391]
- **Others:** [Ciavarella; 2007.04447], [Perez-Salinas, Cruz-Martinez, Alhajri, Carrazza; 2011.13934], [Bauer, Freytsis, Nachman; 2102.05044], [Martenez de Lejarza, Cieri, Rodrigo; 2204.06496], [Agliardi, Grossi, MP, Prati; 2201.01547], [Martenez de Lejarza et al.; 2401.03023], [Cruz-Martinez, Robbiati, Carrazza; 2308.05657]

- Basics of high-energy physics
 - How to compute a cross section

Cross section (definition)

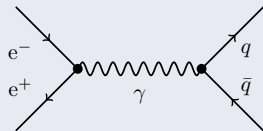
- Probability to measure a scattering process
- Predictable theoretically and measurable experimentally!

$$\sigma \propto \int d\Phi |\mathcal{M}|^2$$

- $d\Phi$: phase-space, depends on final-state particles
 - encodes kinematics
- $|\mathcal{M}|^2$: matrix element of the scattering process
 - encodes underlying theory and depends on kinematics

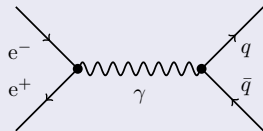
Cross section [example] (I)

$$e^+(p_1) e^-(p_2) \rightarrow q(k_1) \bar{q}(k_2)$$



Cross section [example] (I)

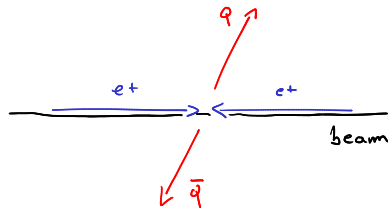
$$e^+(p_1) e^-(p_2) \rightarrow q(k_1) \bar{q}(k_2)$$



- $d\Phi \propto d\phi d\cos\theta$

- $|\mathcal{M}|^2 \propto 1 + \cos^2\theta$

$$\Rightarrow \sigma_{\text{incl}} \propto \int_0^{2\pi} d\phi \int_{-1}^{+1} d\cos\theta (1 + \cos^2\theta)$$



→ No dependence on ϕ
(symmetry around z axis)

→ inclusive cross section
(integration over whole phase space)

Cross section [example] (II)

- Experimental measurements performed in parts of the phase space
- Experiments also measure observables
 - angles, transverse momentum
- Analytical integration not an option!

Cross section [example] (II)

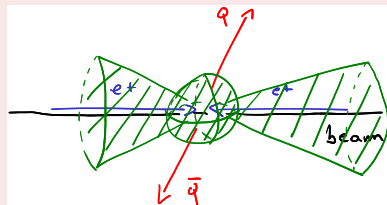
- Experimental measurements performed in parts of the phase space
- Experiments also measure observables
→ angles, transverse momentum
- Analytical integration not an option!

⇒ Solution: Monte Carlo integration!

$$\rightarrow \phi = 2\pi \cdot x_1, \quad \cos \theta = 2 \cdot x_2 - 1$$

$$\Rightarrow \sigma \propto 2\pi \int_0^1 dx_1 \int_0^1 dx_2 (1 + (2x_2 - 1)^2) \Theta(g(x_1, x_2))$$

- $\Theta(g(x_1, x_2))$ encodes experimental selection
- Error scaling as $1/\sqrt{N_{\text{points}}}$



→ In general:

$$\sigma \propto \int_0^1 dx_1 \cdots \int_0^1 dx_n f(x_1, \cdots, x_n) \Theta(g(x_1, \cdots, x_n))$$

Cross section (Monte Carlo)

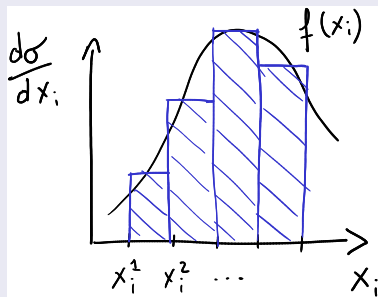
→ In general:

$$\sigma \propto \int_0^1 dx_1 \cdots \int_0^1 dx_n f(x_1, \dots, x_n) \Theta(g(x_1, \dots, x_n))$$

- For a given observable $\mathcal{O} = \mathcal{O}(x_1, \dots, x_n)$:

$$\sigma = \sum_i \frac{d\sigma}{d\mathcal{O}^i} = \sum_{i,l} c_{il} \frac{d\sigma}{dx_l^i}$$

- **Integrating = guessing the values of a function at specific points (Riemann sum)**
- More complex calculations ...
 - ... more integration variables ...
 - ... more computing resources!



- Basics of quantum computing
 - How to build a quantum circuit

Literature:

- *Quantum Computation and Quantum Information*, Nielsen and Chuang
- *Programming Quantum Computers*, Johnston, Harrigan, and Gimeno-Segovia

FEBRUARY 17, 2014

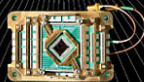
French Advances / My Doctor Fired Me / Love App-tually

TIME

IT PROMISES TO SOLVE SOME OF HUMANITY'S
MOST COMPLEX PROBLEMS. IT'S BACKED
BY JEFF BEZOS, NASA AND THE CIA.
EACH ONE COSTS \$10,000,000 AND OPERATES
AT 459° BELOW ZERO. AND NOBODY KNOWS
HOW IT ACTUALLY WORKS

THE INFINITY MACHINE

BY LEV GROSSMAN



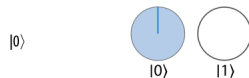
→ Any state can be written as

$$|\psi\rangle = \alpha |0\rangle + \beta |1\rangle = \begin{pmatrix} \alpha \\ \beta \end{pmatrix},$$

with $\alpha^2 + \beta^2 = 1$

→ Representation

Possible values of a qubit Graphical representation



→ Any state can be written as

$$|\psi\rangle = \alpha |0\rangle + \beta |1\rangle = \begin{pmatrix} \alpha \\ \beta \end{pmatrix},$$

with $\alpha^2 + \beta^2 = 1$

→ In quantum mechanics (and in quantum computing), any operation A is unitary

$$\psi \xrightarrow{A} \psi'$$

$$A |\psi\rangle = |\psi'\rangle \quad \text{with} \quad A^*A = AA^* = \text{Id}$$



Example of gates (I)

Pauli-X (X)

$$X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$\alpha |0\rangle + \beta |1\rangle \rightarrow \alpha |1\rangle + \beta |0\rangle$$



Hadamard (H)

$$H = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$\alpha |0\rangle + \beta |1\rangle \rightarrow \alpha \frac{|0\rangle + |1\rangle}{\sqrt{2}} + \beta \frac{|0\rangle - |1\rangle}{\sqrt{2}}$$



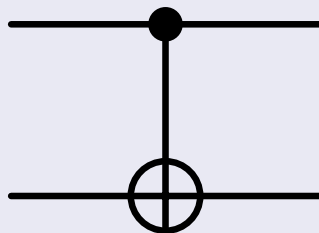
Example of gates (II)

Controlled not (CNOT, CX)

$$CX = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

$|00\rangle \rightarrow |00\rangle$; $|01\rangle \rightarrow |01\rangle$;
 $|10\rangle \rightarrow |11\rangle$; $|11\rangle \rightarrow |10\rangle$.

- If 0 nothing happens, if 1 CX!
- *Control* qubit (top) and *target* qubit (bottom)

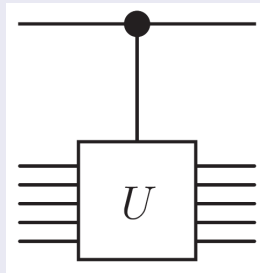


Example of gates (III)

Generalised controlled gate (CU)

$$CU = \begin{bmatrix} \text{Id}_2 & 0 \\ 0 & U \end{bmatrix}$$

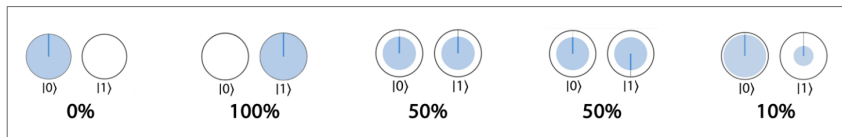
→ One *control* qubit and ...
... many *target* qubits



Measurement process

→ State: $|\psi\rangle = \alpha |0\rangle + \beta |1\rangle$

→ Probabilities: $\begin{cases} \text{for } |0\rangle : \alpha^2 \\ \text{for } |1\rangle : \beta^2 \end{cases}$

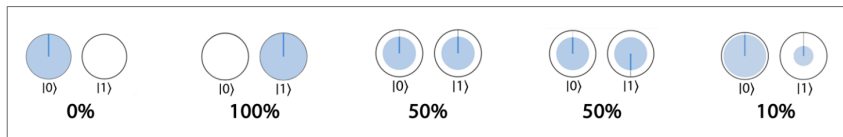


NB: Probability obtained after many measurements!

Measurement process

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NB: Probability obtained after many measurements!

→ α and β encode information that can be measured/computed!

- Applications

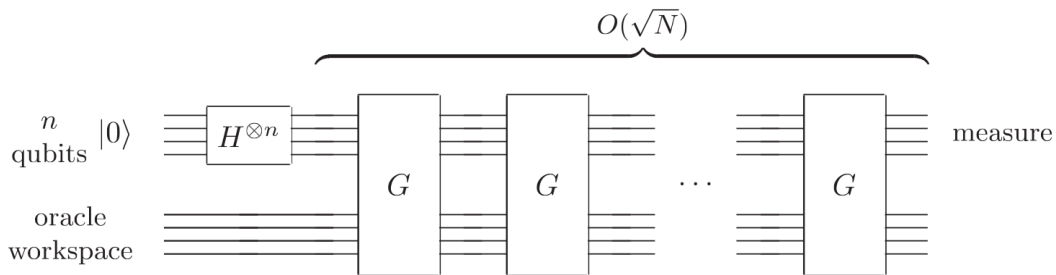
- Quantum integration

- [Agliardi, Grossi, MP, Prati; 2201.01547]

- Colour amplitudes

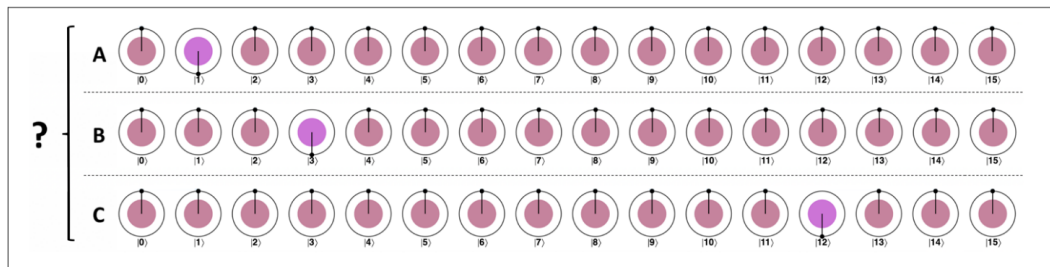
Grover algorithm/iteration

- Very general quantum algorithm
- Quadratic speed up
→ $\mathcal{O}(\sqrt{N})$ operations instead of $\mathcal{O}(N)$
- Most famous example: unstructured database search



Grover algorithm/iteration

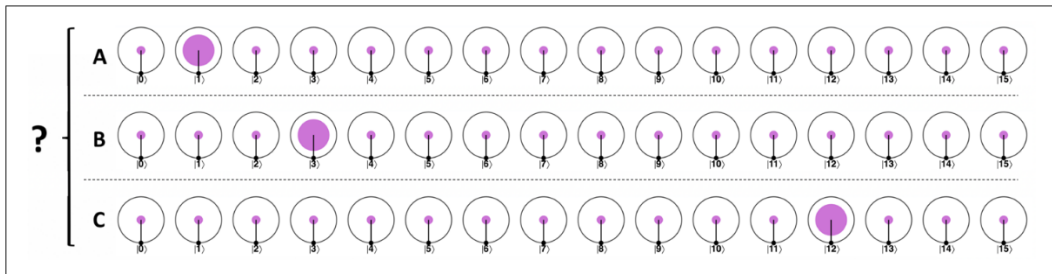
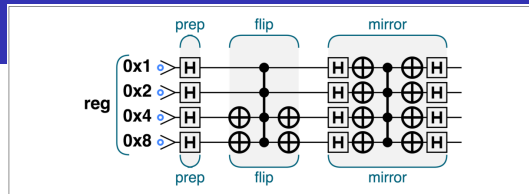
- Example (from [Johnston, Harrigan, Gimeno-Segovia; Programming Quantum Computers])



→ What solution is contained in our quantum register?

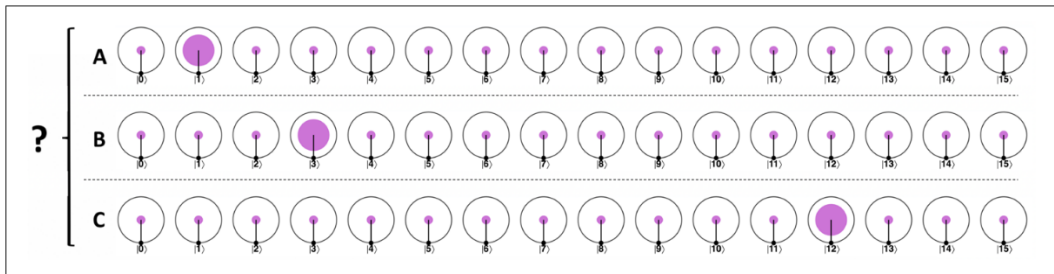
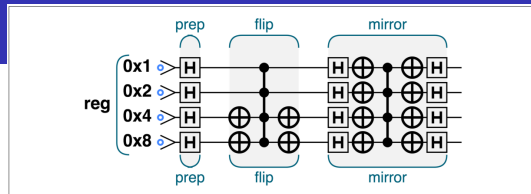
Grover algorithm/iteration

→ Applying a Grover iteration

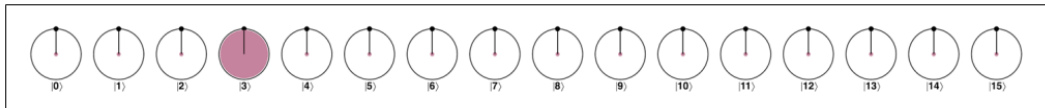


Grover algorithm/iteration

→ Applying a Grover iteration



→ Applying it twice



Quantum Amplitude Estimate (QAE)

[Brassard, Hoyer, Mosca, Tapp; Quantum Amplitude Amplification and Estimation]

$$\mathcal{A}|0\rangle = \sqrt{1-a}|\Psi_0\rangle + \sqrt{a}|\Psi_1\rangle$$

QAE estimates a with high probability such that the estimation error scales as $\mathcal{O}(1/M)$
[as opposed to $\mathcal{O}(1/\sqrt{M})$]

M : number of applications of \mathcal{A}

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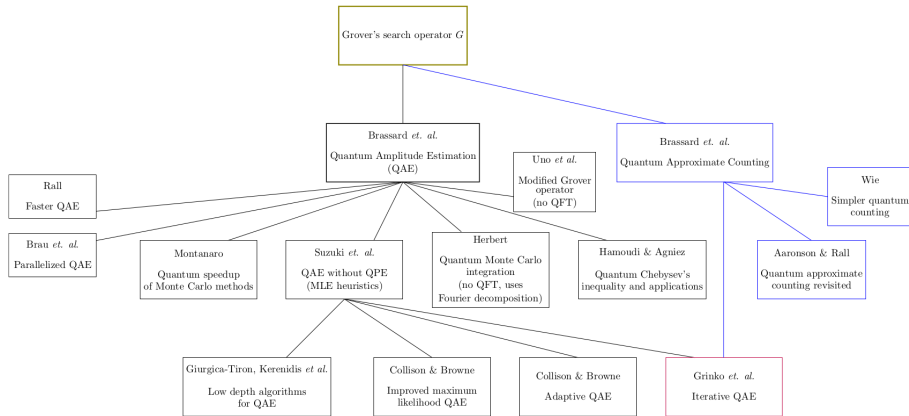
M : number of applications of \mathcal{A}

→ What the (original) algorithm provides:

- An estimate: $\tilde{a} = \sin^2(\tilde{\theta}_a)$
with $\tilde{\theta}_a = y\pi/M$, $y \in \{0, \dots, M-1\}$, and $M = 2^n$
- A success probability (that can be increased by repeating the algorithm)
- A bound: $|a - \tilde{a}| \leq \mathcal{O}(1/M)$

Quantum Amplitude Estimate (QAE)

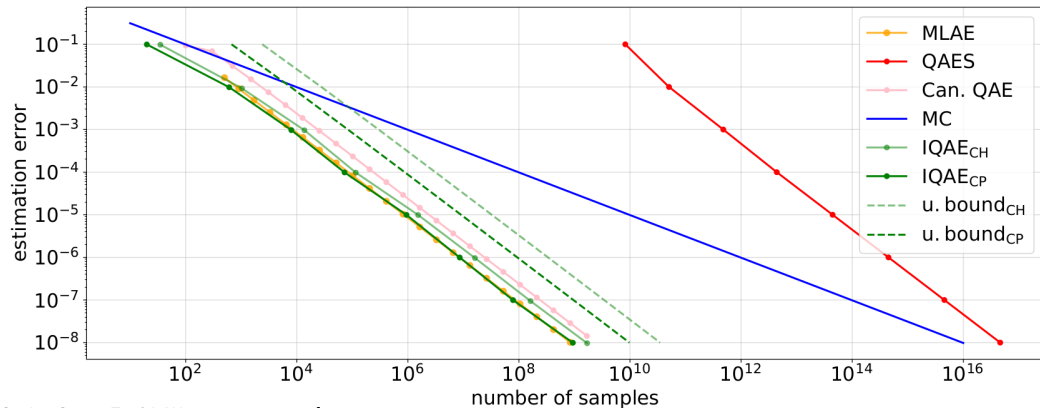
- Basis of quantum Monte Carlo integration and $\mathcal{O}(1/M)$ scaling
- Various algorithms/implementations available



[Intallura et al.; 2303.04945]

Quantum Amplitude Estimate (QAE)

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- Various algorithms/implementations available



[Grinko, Gacon, Zoufal, Woerner; 1912.05559]

Resulting estimation error for $a = 1/2$ and 95% confidence level with respect to the required total number of oracle queries.

Quantum integration

Extension to

$$\mathcal{A}|0\rangle = \sum_i a_i |\Psi_i\rangle$$

→ Definition of a piece-wise function with $f(x_i) = a_i$.

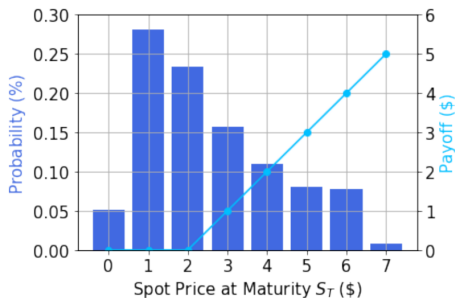
Quantum integration

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→ Definition of a piece-wise function with $f(x_i) = a_i$.

- So far used in finance for simple functions in 1D
→ Applicable to HEP? What are the limitations?



$$I = \int dx f(x)g(x)$$

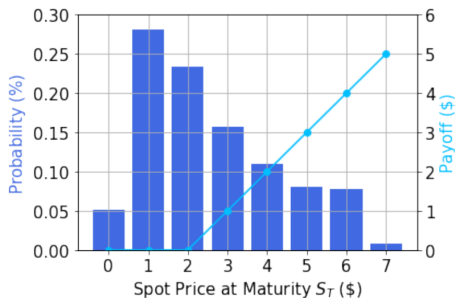
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$$I = \int dx f(x)g(x)$$

- In finance:
 - f : probability
 - g : payoff
- In HEP:
 - f : $|\mathcal{M}|^2$
 - g : $\Theta(\Phi - \Phi_c)$

- $e^+e^- \rightarrow q\bar{q}$ (in QED)

$$\sigma \sim \int_{-1}^1 \int_0^{2\pi} d\cos\theta d\phi (1 + \cos^2\theta)$$

- $e^+e^- \rightarrow q\bar{q}'W$

$$\begin{aligned}\sigma &\sim \int_{M_W^2}^s \int_0^{s_1^{\text{Max}}} \int_{-1}^1 \int_0^{2\pi} \int_0^{2\pi} d\Phi_3 |\mathcal{M}_{e^+e^- \rightarrow q\bar{q}'W}|^2 \\ &\sim \int_{M_W^2}^s \int_0^{s_1^{\text{Max}}} d\tilde{\Phi}_3 |\mathcal{M}'|^2\end{aligned}$$

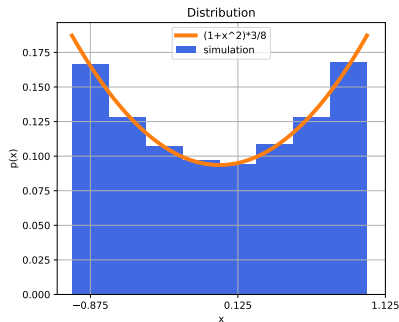
with $\mathcal{M}' = \mathcal{M}_{e^+e^- \rightarrow q\bar{q}'W}(\cos\theta_1 = 0, \phi_1 = \pi/2, \phi_2 = \pi/2)$.

Encoding the distribution to be integrated into qubits

- Exact loading [Shende, Bullock, Markov, quant-ph/0406176] (resource intensive)
- Using quantum machine learning (qGAN) [Zoufal, Lucchi, Woerner; 1904.00043] (not exact)

Encoding the distribution to be integrated into qubits

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- Using quantum machine learning (qGAN) [Zoufal, Lucchi, Woerner; 1904.00043] (not exact)
- Example: Exact loading $\sigma - 1 + x^2$



→ 3 qubits: $2^3 = 8$ bins

- Matching boundary of integration (3 qubits $\Rightarrow 2^3$ bins)

Domain	low stat.		high stat.		very high stat.		exact	
	σ	$\delta[\%]$	σ	$\delta[\%]$	σ	$\delta[\%]$	σ	$\delta[\%]$
$[-0.75; 0]$	0.345	-3.31	0.332	0.706	0.334	0.0331	0.334	-8.31×10^{-3}
$[-0.5; 0]$	0.215	-5.86	0.201	1.15	0.203	0.0986	0.203	-0.0161
$[-0.25; 0]$	0.112	-17.1	0.0939	1.87	0.0960	-0.284	0.0957	-0.0389

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$[-0.5; 0]$	0.215	-5.86	0.201	1.15	0.203	0.0986	0.203	-0.0161
$[-0.25; 0]$	0.112	-17.1	0.0939	1.87	0.0960	-0.284	0.0957	-0.0389

- Non-matching boundary of integration

Qubits number	$[-0.7; 0.6]$				$[-0.625; 0.375]$			
	high stat.		exact		high stat.		exact	
	σ	δ [%]	σ	δ [%]	σ	δ [%]	σ	δ [%]
3	0.402	-28.0	0.406	-27.1	0.296	-28.1	0.299	-27.5
4	0.463	-17.0	0.468	-16.0	0.408	-1.07	0.412	5.96×10^{-3}
5	0.527	-5.46	0.532	-4.62	0.408	-1.07	0.412	5.96×10^{-3}
6	0.542	-2.76	0.547	-1.81	0.408	-1.07	0.412	5.96×10^{-3}

Remarks

- Use Qiskit (IBM python software) subroutines and noiseless quantum simulation (perfect quantum computer)
- For present application, too many qubits for test on real hardware
 - 4 qubits for representation → 9 total qubits
 - 6 qubits for representation → 13 total qubits
- Largest quantum computer on IBM quantum experience:
 - 7 qubits previously (127 qubits now)
 - Simulators can go up to 5000 qubits

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Summary

- First application of quantum integration in HEP
- Theoretical quadratic speed-up
(→ generation of classical data/analytical knowledge required)
- Main challenge: error estimate

- Applications

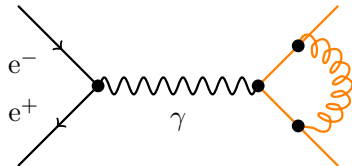
- Quantum integration

- **Colour amplitudes**

- [Chawdhry, MP; 2303.04818]

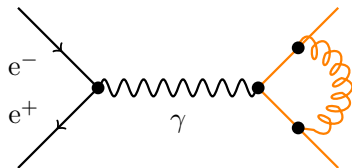
$$\mathcal{M} \sim \sum \text{Tr}(T^{a_1} \dots T^{a_n}) \mathcal{K}(1, \dots, n)$$

- **Kinematic part**: made of spinors and tensors
- **Colour part**: made of SU(3) generators of QCD



$$\mathcal{M} \sim \sum \text{Tr}(T^{a_1} \dots T^{a_n}) \mathcal{K}(1, \dots, n)$$

- **Kinematic part**: made of spinors and tensors
- **Colour part**: made of SU(3) generators of QCD



Remarks

- First step towards a full quantum amplitude/Monte Carlo
- Useful for a quantum parton shower

- $[T^a, T^b] = if_{abc} T^c$.
- T^a, T^c, \dots : SU(3) generators
- Gell-Mann matrices

$$T^1 = \frac{1}{2} \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad T^2 = \frac{1}{2} \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad T^3 = \frac{1}{2} \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad T^4 = \frac{1}{2} \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix},$$
$$T^5 = \frac{1}{2} \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix}, \quad T^6 = \frac{1}{2} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}, \quad T^7 = \frac{1}{2} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix}, \quad T^8 = \frac{1}{2\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}.$$

Attention! T^a are not unitary!

→ In our example, colour factor: $T_{ij}^a T_{ij}^a = C_F$

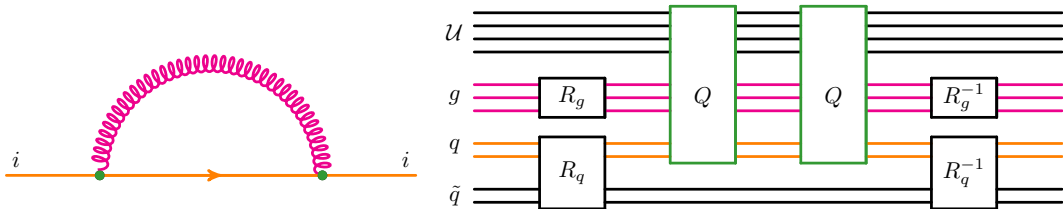
Quantum implementation of colour

- Gluon: 8 colours \rightarrow 3 qubits (2^3)
- Quark: 3 colours \rightarrow 2 qubits (2^2)

\rightarrow Make non-unitary matrices unitary: extend dimension and modify them

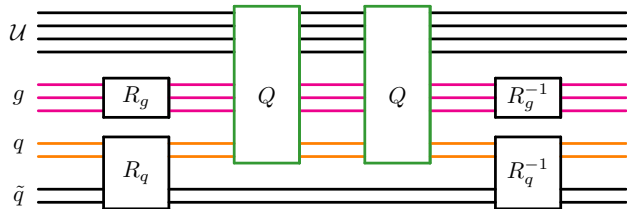
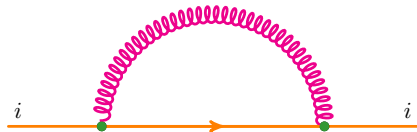
$$\begin{aligned}\overline{T^1} &= \frac{1}{2} \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, & \overline{T^2} &= \frac{1}{2} \begin{pmatrix} 0 & -i & 0 & 0 \\ i & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, & \overline{T^3} &= \frac{1}{2} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, & \overline{T^4} &= \frac{1}{2} \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, \\ \overline{T^5} &= \frac{1}{2} \begin{pmatrix} 0 & 0 & -i & 0 \\ 0 & 1 & 0 & 0 \\ i & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, & \overline{T^6} &= \frac{1}{2} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, & \overline{T^7} &= \frac{1}{2} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & -i & 0 \\ 0 & i & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, & \overline{T^8} &= \frac{1}{2\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}.\end{aligned}$$

Example

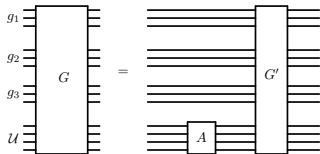


- One-to-one correspondence between Feynman diagram and circuit
- Gates for qqg (Q) and ggg (G) vertices to simulate QCD (colour) interaction

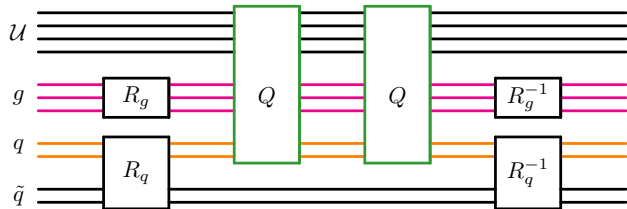
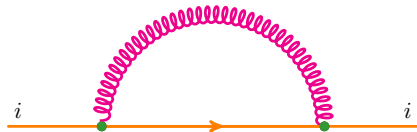
Example



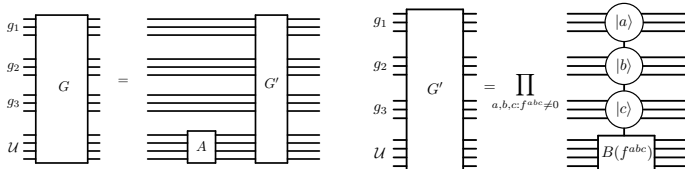
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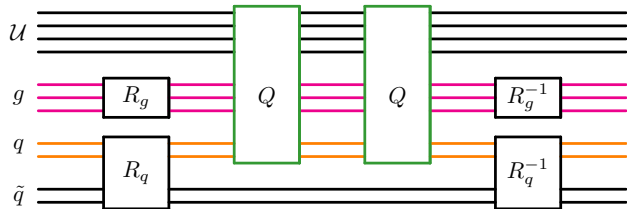
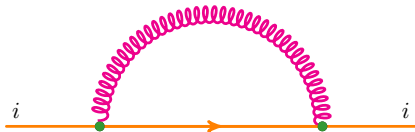
Example



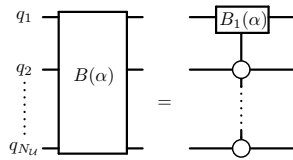
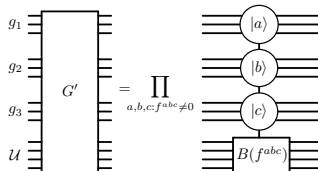
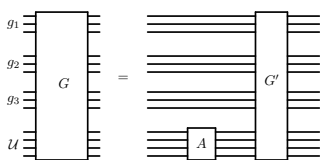
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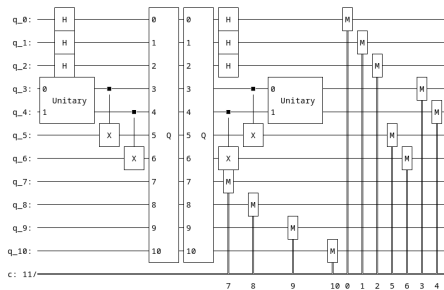
Example



- One-to-one correspondence between Feynman diagram and circuit
- Gates for qqg (Q) and ggg (G) vertices to simulate QCD (colour) interaction



(real-life) Example



Total counts are: {'00000010101': 226, '00010010011': 342, '00000010110': 225, '00000001101': 696, '00010010010': 362, '00000010001': 872, '00010001101': 2006, '00000001100': 643, '00010001100': 2006, '00010000110': 1051, '00000001111': 638, '000000010010': 904, '00010000010': 1057, '001000010101': 52353, '000100010100': 3342, '00100000101': 6942, '000100000111': 1046, '000000010111': 210, '00100001101': 36223, '00100010111': 51877, '00000001110': 643, '000100010000': 4838, '000000010100': 5421, '000100000100': 1035, '00100000000': 107280, '00010000011': 1075, '001000000111': 6795, '001000001011': 145043, '00100010010': 10275, '000100000000': 65548, '000000000000': 27415, '000100001111': 2031, '00100000110': 7004, '00000001011': 2551, '001000001111': 36471, '00010010111': 8966, '000100000101': 1077, '001000010110': 52220, '00010010110': 9080, '001000010100': 185056, '001000001100': 36173, '000100101010': 8960, '001000010000': 14129, '00100001110': 36925, '00100000100': 6058, '001000010011': 10182, '001000000001': 6950, '000100001110': 2018, '00100000011': 6983, '000000010011': 815, '000100010111': 7957, '00010010001': 340, '00100010001': 10163, '00010000001': 1092, '00100000010': 7010}

→ Trace defined in $|00000000000\rangle = |0_{11}\rangle$

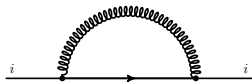
state: $|\psi\rangle = \frac{c}{N} |0_{11}\rangle + \dots$

$\Rightarrow \frac{27415}{N_{\text{shots}}=1000000} \sim$

$$\left(\frac{c}{N} = \frac{(N_c=3)C_F}{N_c^{n_q=1}(N_c^2-1)^{n_g=1}} \right)^2$$

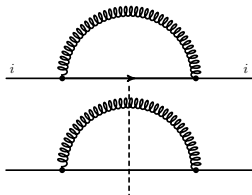
→ Colour factors encoded in one single state (as needed for QAE)

→ Any colour factor computable



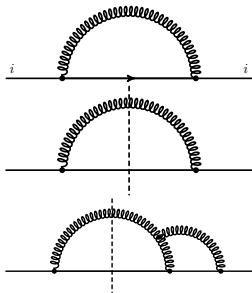
- Colour factors as squared (**done**)

- First building blocks for full amplitude
- Quantum advantage? (in addition to QAE)
To compute colour factors for many gluons? (difficult problem)



- Colour factors as squared (**done**)
- Colour factor as amplitudes (**on-going**)

- First building blocks for full amplitude
- Quantum advantage? (in addition to QAE)
To compute colour factors for many gluons? (difficult problem)



- Colour factors as squared (done)
- Colour factor as amplitudes (on-going)
- Interferences (on-going)
 - special feature of quantum computing
 - relevant for parton-shower

- First building blocks for full amplitude
- Quantum advantage? (in addition to QAE)
To compute colour factors for many gluons? (difficult problem)

Road map for quantum Monte Carlo



- Reliable error estimate
 - Taking into account binning effects / multi-dimension integrand

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 - **On-going** collaboration with QUANTINUUM (Cambridge, UK)



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 - Example of colour algebra
- Estimate of resources needed for actual computation on near-term quantum computers (noise, connections, ...)
 - **On-going** collaboration with QUANTINUUM (Cambridge, UK)
- Can there be quantum advantage for event generation?

- Is it possible?
→ **Yes.**

- Is it possible?

→ **Yes.**

- Is there a quantum advantage?

→ **In principle, yes. In practice, no.**

- Is it possible?

→ **Yes.**

- Is there a quantum advantage?

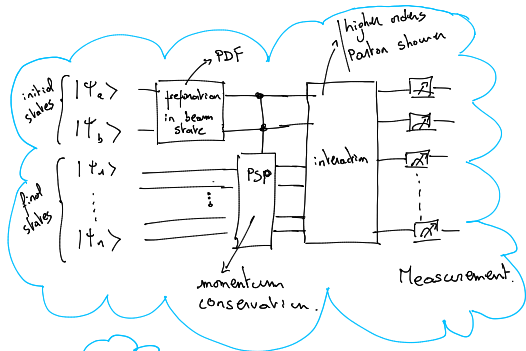
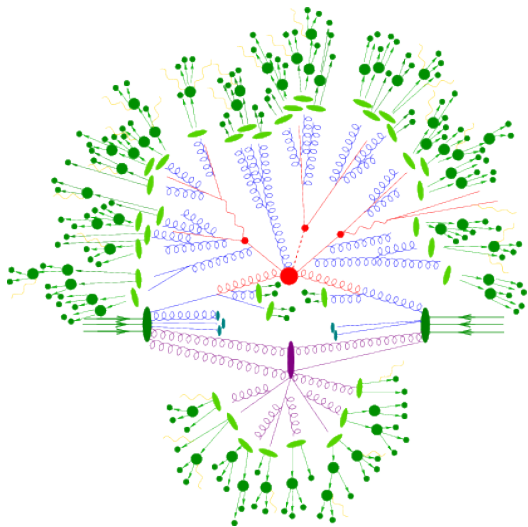
→ **In principle, yes. In practice, no.**

- Is it more resource efficient than CPU/GPU?

→ **At the moment, no. In the future, not known.**



- Are we witnessing a quantum revolution?
- When can we do *useful* quantum computations in the future?



Thank you -

BACK-UP