

# Advances and challenges for ab initio calculations of medium-mass to heavy nuclei

Achim Schwenk

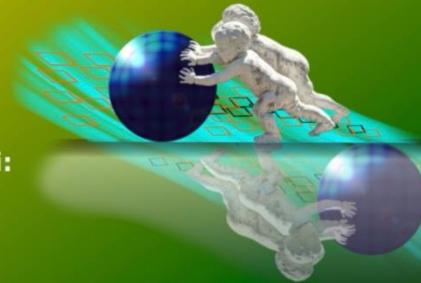


TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



**SSNET'24**  
International Conference on  
Shapes and Symmetries in Nuclei:  
from Experiment to Theory

Orsay, 4 - 8 November 2024



SSNET'24

Orsay, Nov. 6, 2024

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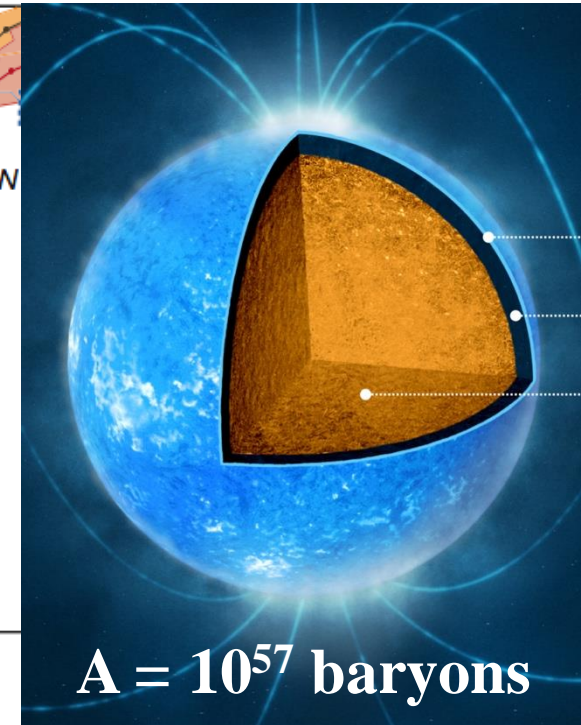
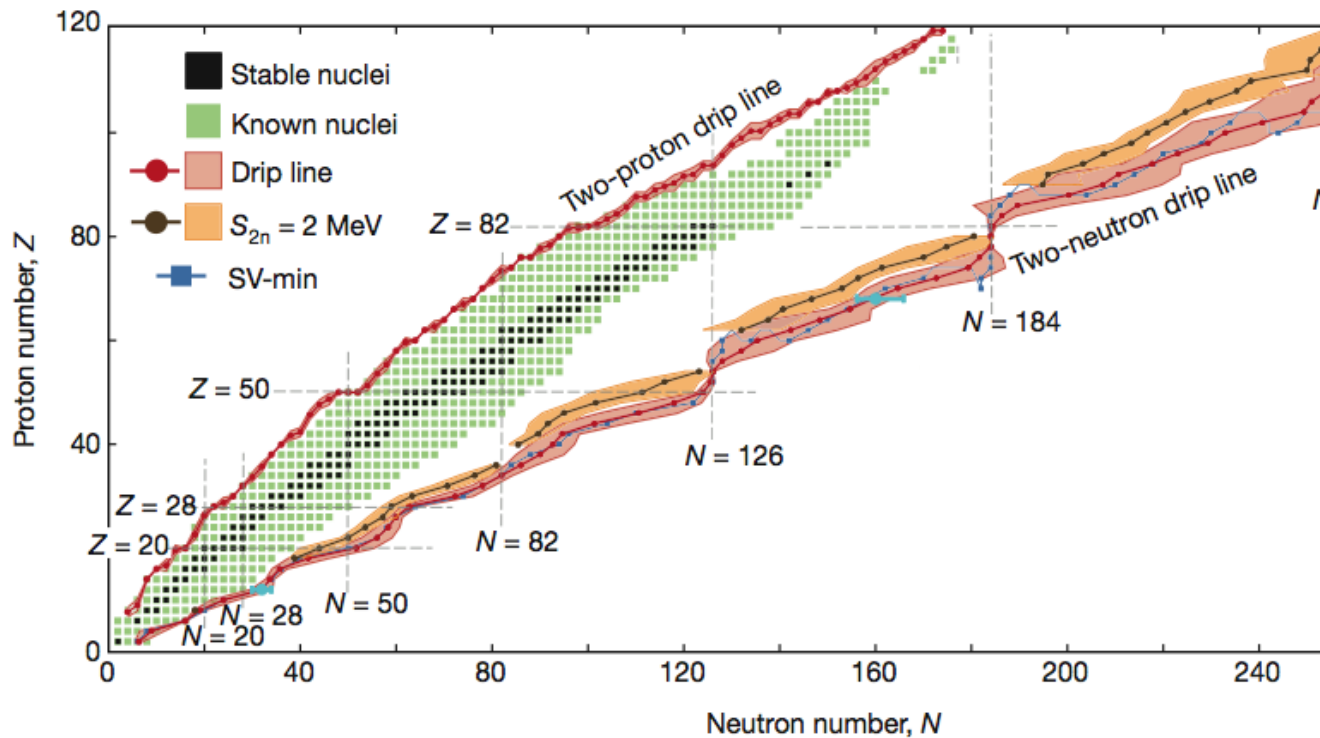
# Structure of nuclei and dense matter in neutron stars

doi:10.1038/nature11188

## The limits of the nuclear landscape

Jochen Erler<sup>1,2</sup>, Noah Birge<sup>1</sup>, Markus Kortelainen<sup>1,2,3</sup>, Witold Nazarewicz<sup>1,2,4</sup>, Erik Olsen<sup>1,2</sup>, Alexander M. Perhac<sup>1</sup> & Mario Stoitsov<sup>1,2,†</sup>

~ 4000 ± 500 nuclei unknown, **extreme neutron-rich**



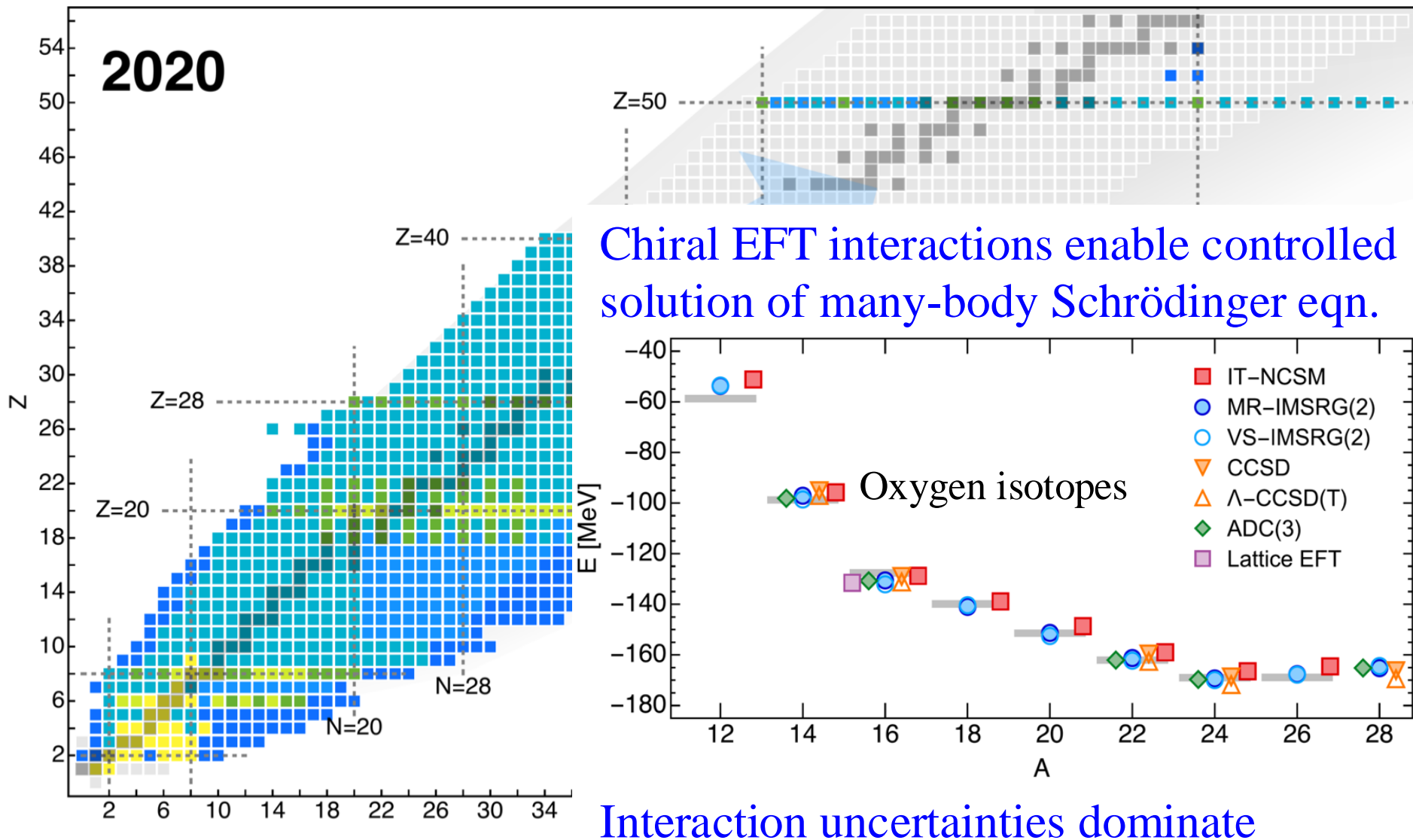
**Extreme neutron-rich matter** in neutron stars

# Chiral effective field theory for nuclear forces

Systematic expansion (power counting) in low momenta  $(Q/\Lambda_b)^n$

	NN	3N	4N	
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$				based on symmetries of strong interaction (QCD)
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$				long-range interactions governed by pion exchanges  powerful approach for many-body interactions
N <sup>2</sup> LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$				all 3- and 4-neutron forces predicted to N <sup>3</sup> LO Tews et al., PRL (2013)
N <sup>3</sup> LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$				
	+ ...	(2011) ...	(2006) ...	

# Great progress in ab initio calculations of nuclei

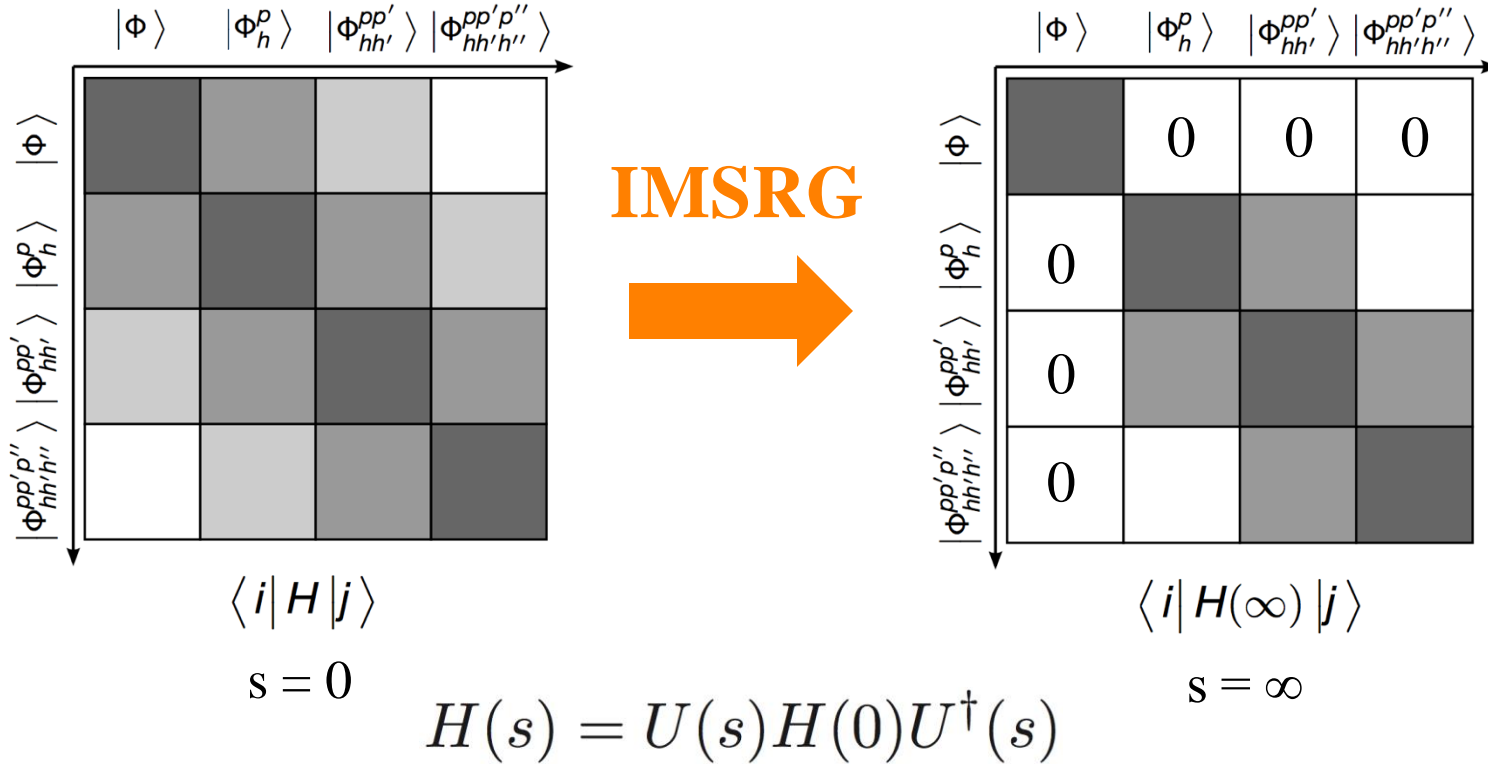


figures from Hergert (2020)

# In-medium similarity renormalization group (IMSRG)

Tsukiyama, Bogner, AS, PRL (2011), Hergert et al., Phys. Rep. (2016)

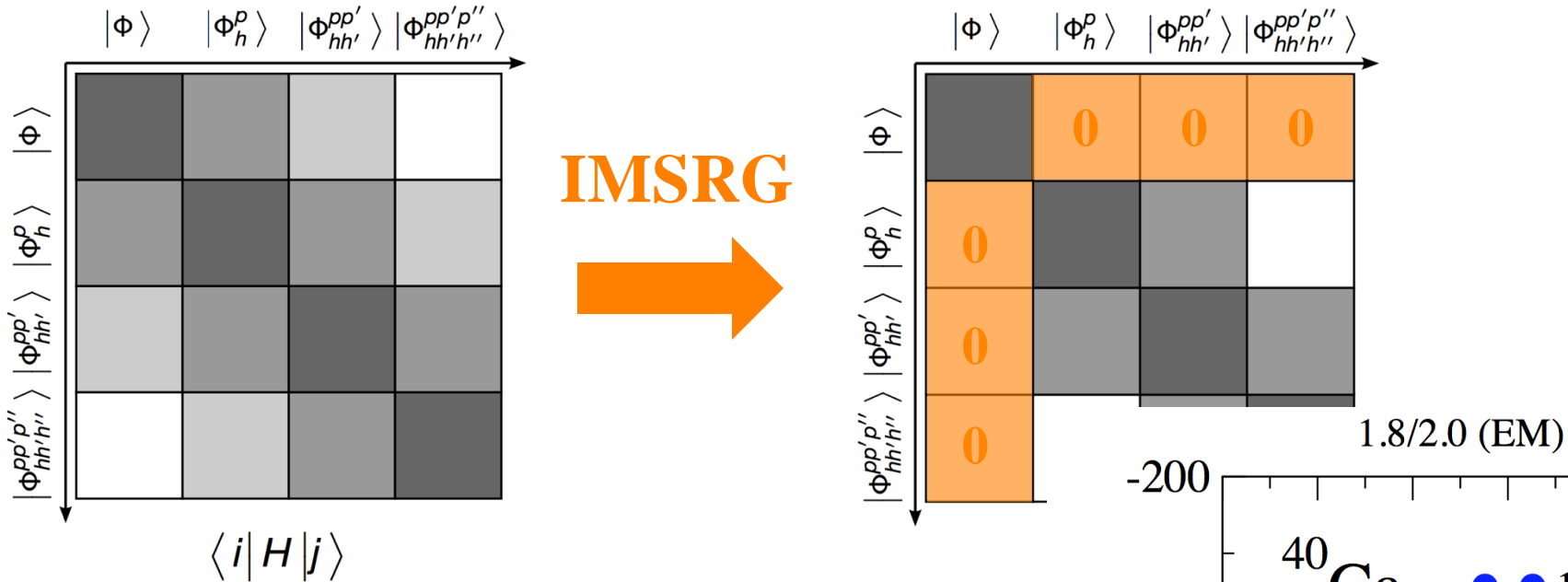
RG flow equations to decouple higher-lying particle-hole states



# In-medium similarity renormalization group (IMSRG)

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RG flow equations to decouple higher-lying particle-hole states

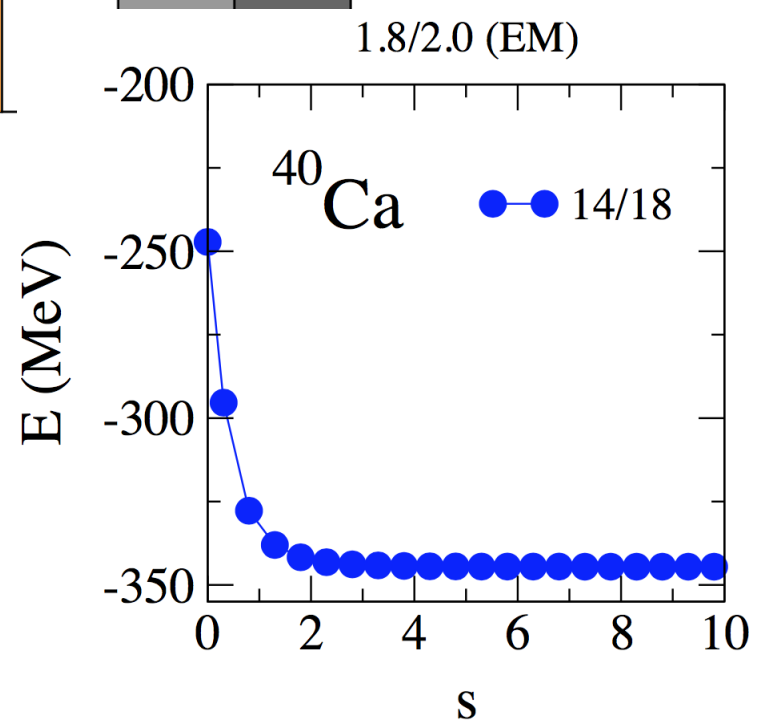


$\langle i|H|j\rangle$   
 $s = 0$

$$H(s) = U(s)H(0)U^\dagger(s)$$

$$\frac{d}{ds}H(s) = [\eta(s), H(s)]$$

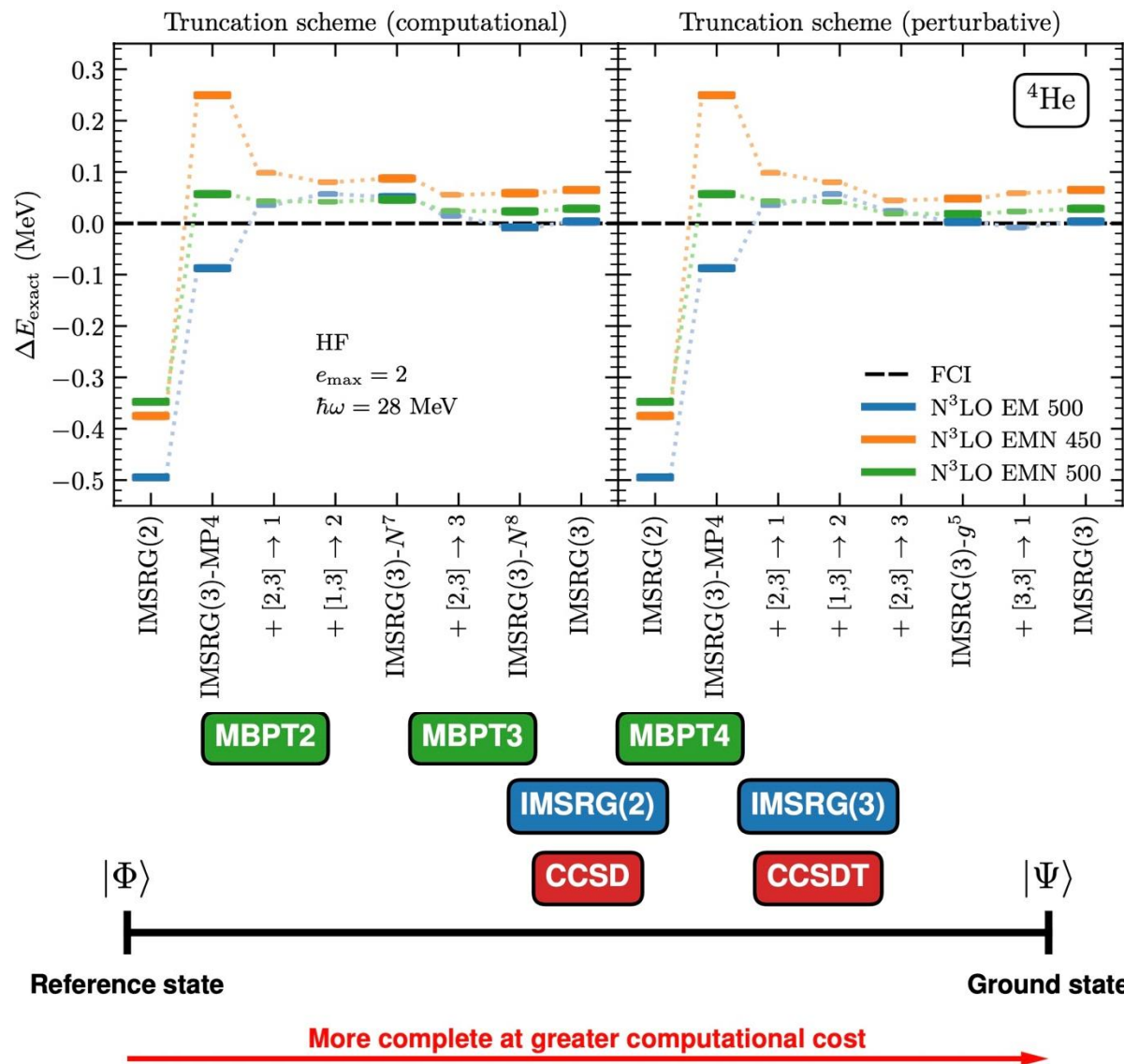
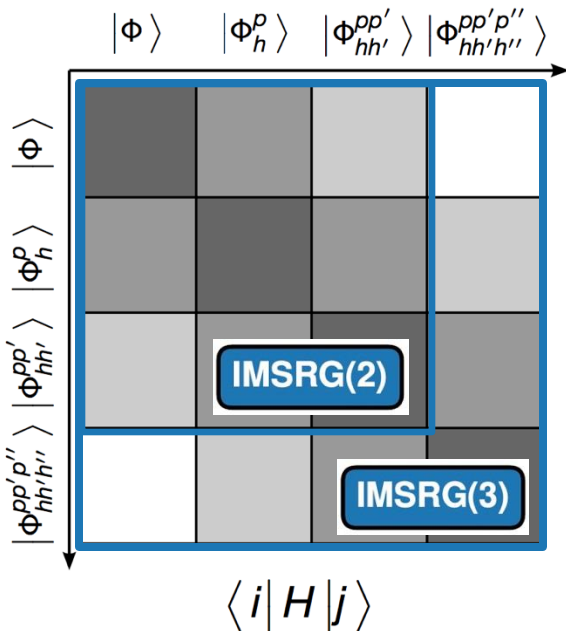
with generator  $\eta(s) = [H_{\text{od}}(s), H_{\text{d}}(s)]$



# In-medium similarity renormalization group (IMSRG)

Tsukiyama, Bogner, AS, PRL (2011), Hergert et al., Phys. Rep. (2016)

RG flow equations to decouple higher-lying particle-hole states



Standard truncation of IMSRG flow equations at normal-ordered 2-body level: IMSRG(2)

First IMSRG(3) results

Heinz et al., PRC (2021)

# Outline

New chiral low-resolutions interactions

**Pierre Arthuis**, Hebeler, AS, arXiv:2401.06675

Probing nuclear structure with nonlinear King plots  
in ytterbium isotopes

**Door, Yeh, Matthias Heinz, Kirk, Lyu, Takayuki Miyagi** et al., arXiv:2403.07792

Uncertainty quantification for low-resolution interactions

**Tom Plies, Matthias Heinz**, AS, preliminary

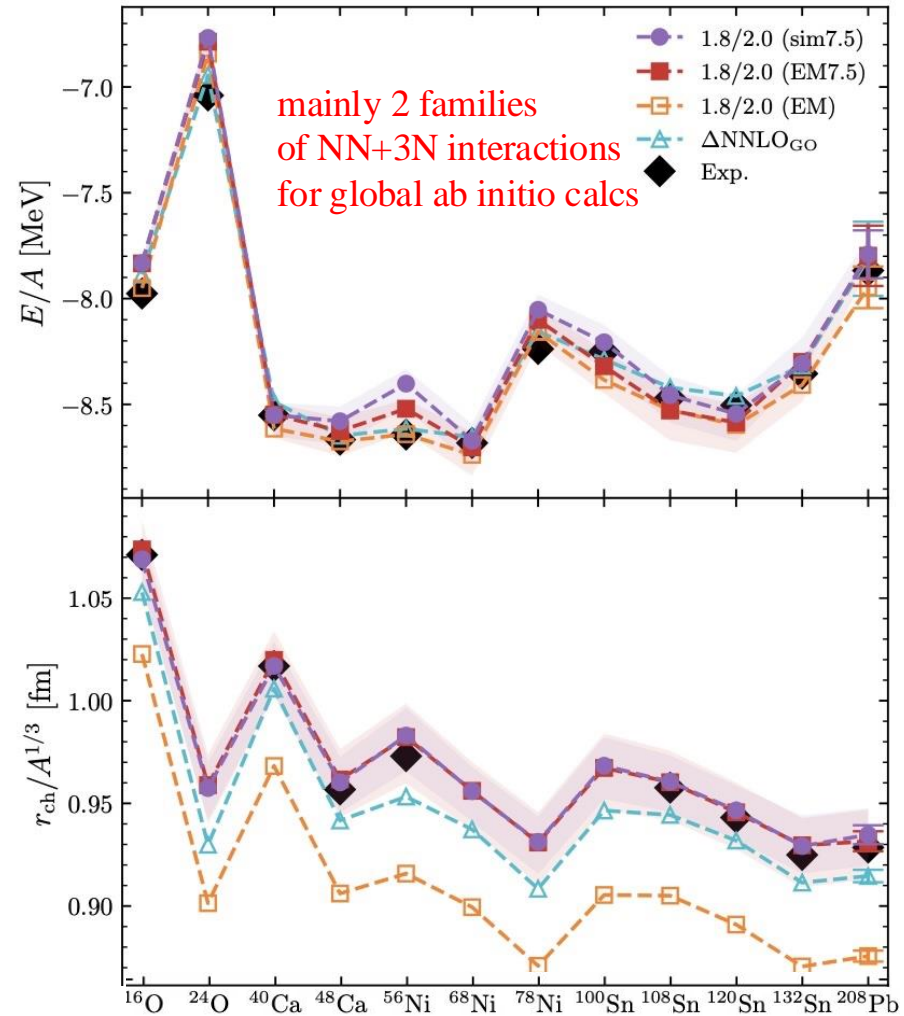
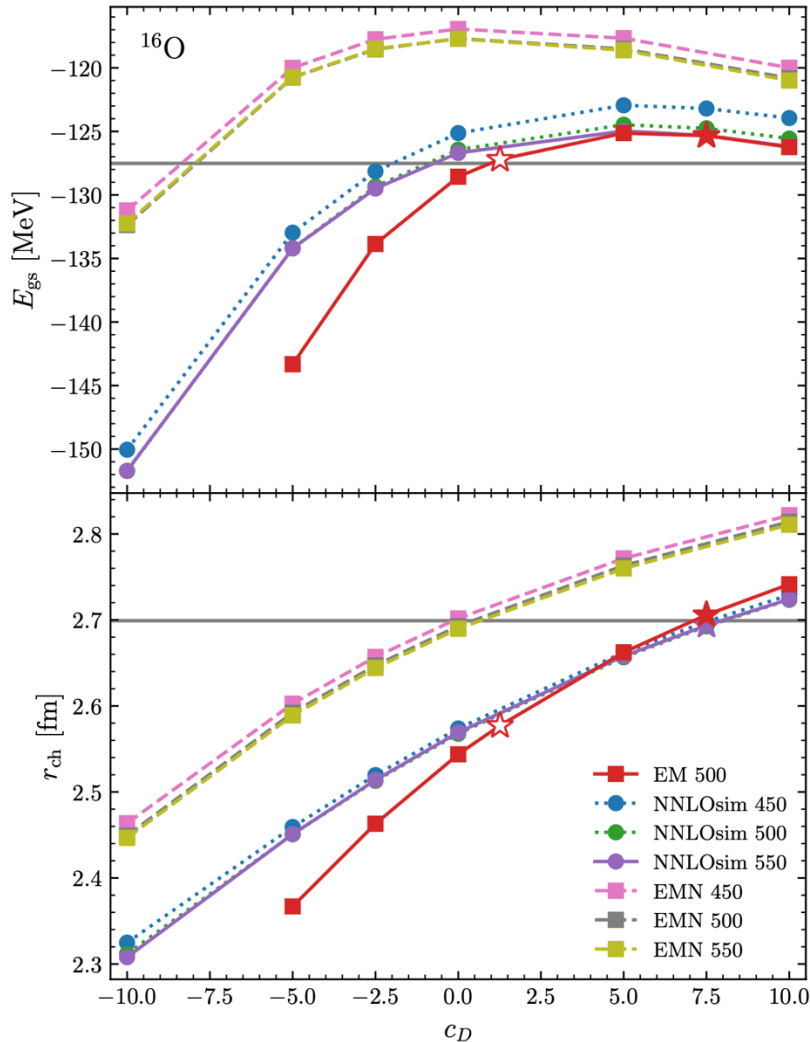


# New chiral low-resolution interactions

Arthuis, Hebeler, AS, arXiv:2401.06675

based on SRG-evolved NN interactions, 3N couplings fit to  ${}^3\text{H}$  and  ${}^{16}\text{O}$

accurate for ground-state properties from  ${}^{16}\text{O}$  to  ${}^{208}\text{Pb}$



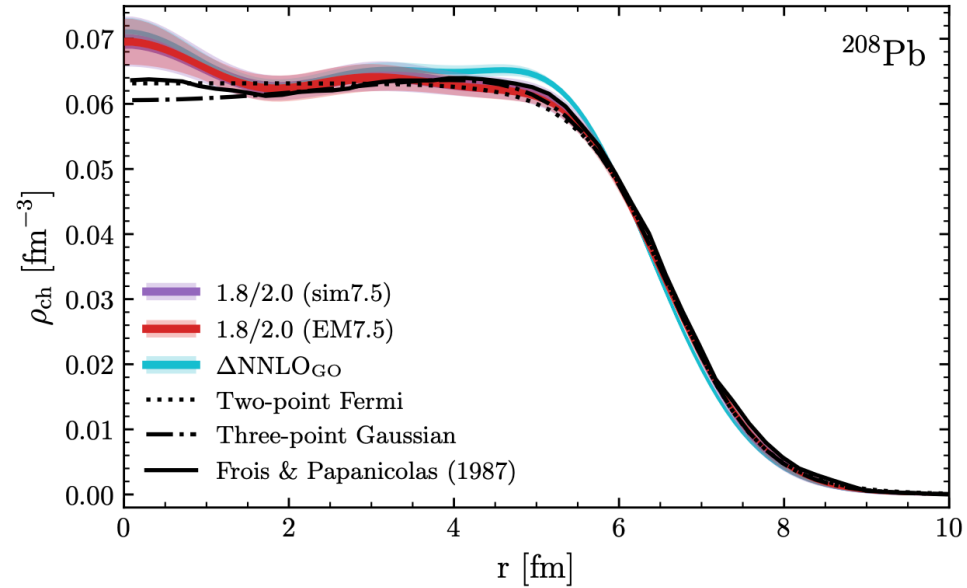
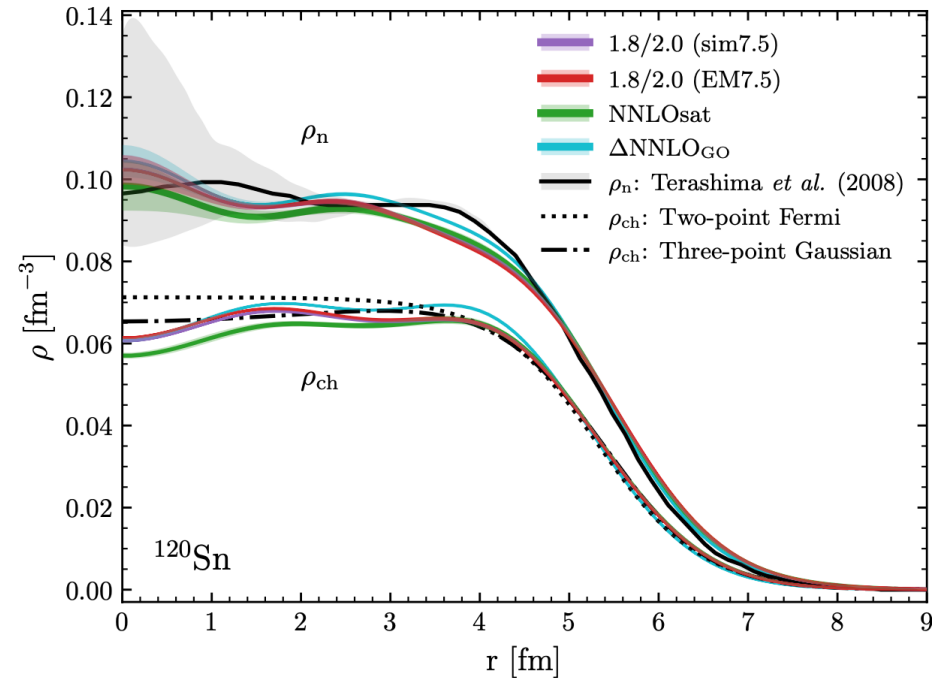
# Neutron/proton density distributions in medium-heavy nuclei

Arthuis, Hebeler, AS, arXiv:2401.06675

based on SRG-evolved NN interactions, 3N couplings fit to  $^3\text{H}$  and  $^{16}\text{O}$

accurate for ground-state properties from  $^{16}\text{O}$  to  $^{208}\text{Pb}$

very good agreement for density distributions in  $^{120}\text{Sn}$  and  $^{208}\text{Pb}$



# Neutron skins

Arthuis, Hebeler, AS, arXiv:2401.06675

very model independent

based on new (and previous)  
chiral NN+3N interactions

dependence of neutron skin

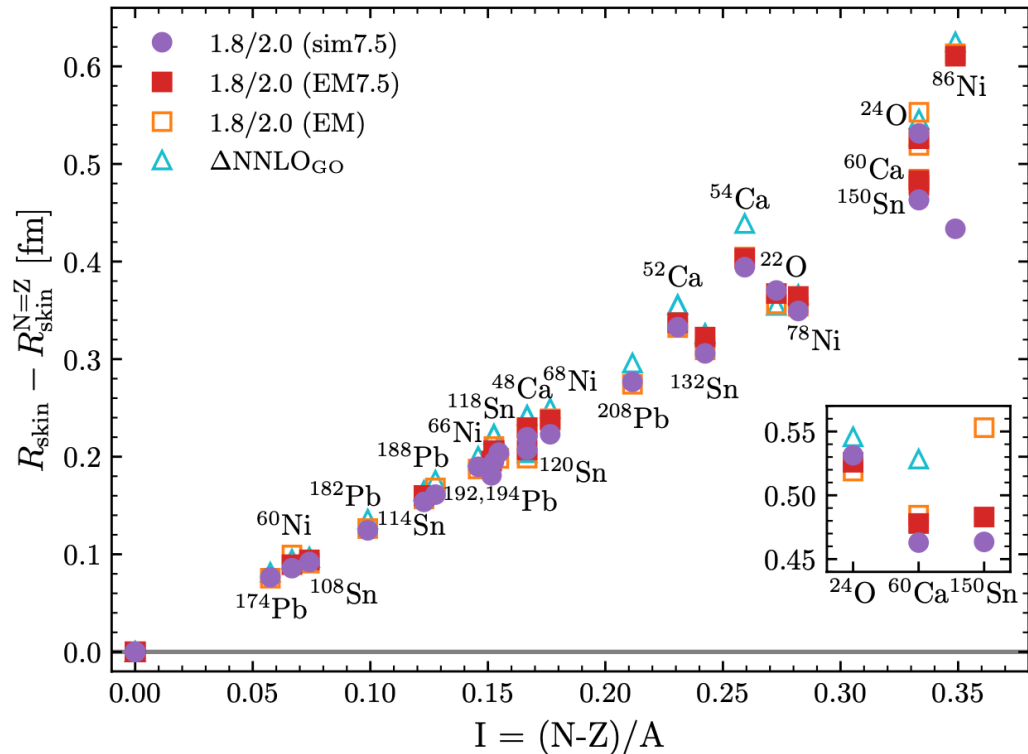
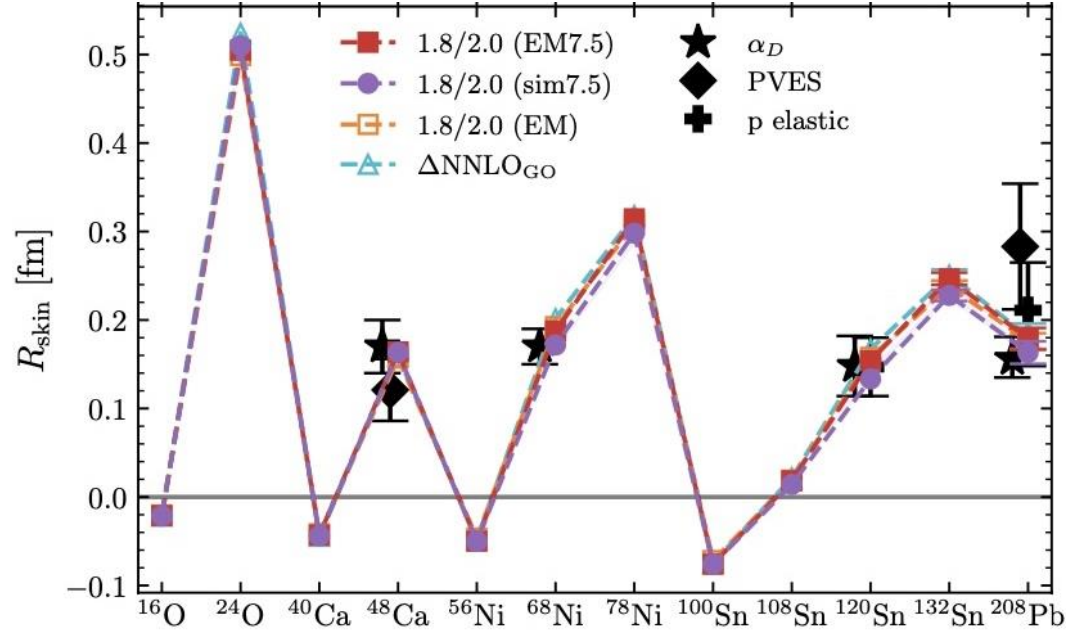
corrected for Coulomb is

linear in isospin

see also Novario et al., PRL (2023)

interesting predictions

for extreme n-rich nuclei



# Outline

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Probing nuclear structure with nonlinear King plots  
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Uncertainty quantification for low-resolution interactions

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# Isotope shifts in $^{168,170,172,174,176}\text{Yb}$

Door, Yeh, Heinz, Kirk, Lyu, Miyagi et al., arXiv:2403.07792

isotope shifts of atomic transitions

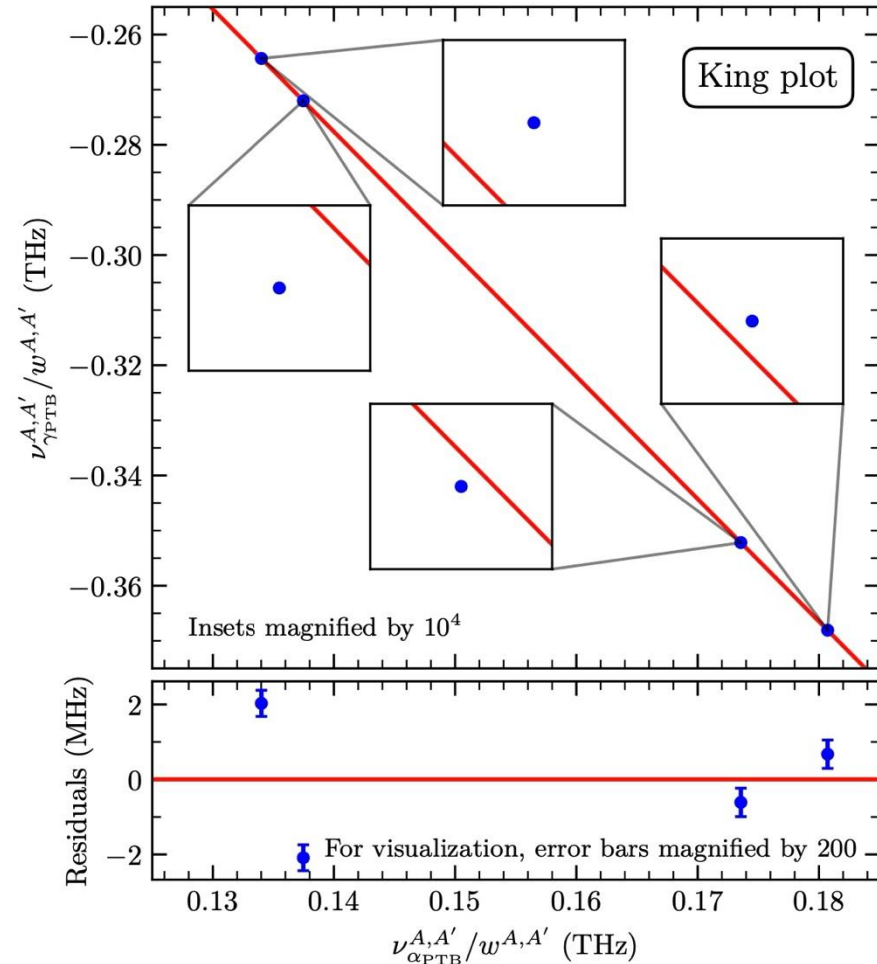
$$\nu_{\tau}^{A,A'} = \nu_{\tau}^A - \nu_{\tau}^{A'} \approx \underbrace{K_{\tau} w^{A,A'}}_{\text{mass shift}} + \underbrace{F_{\tau} \delta\langle r^2 \rangle^{A,A'}}_{\text{field shift}}$$

leading terms give linear King plot

nonlinearities from higher-order  
Standard Model and BSM

$$\nu_{\tau,\text{nonlin.}}^{A,A'} = \underbrace{G_{\tau}^{(2)} (\delta\langle r^2 \rangle^2)^{A,A'} + G_{\tau}^{(4)} \delta\langle r^4 \rangle^{A,A'}}_{\text{higher-order nuclear structure}} + \underbrace{\frac{\alpha_{\text{NP}}}{\alpha_{\text{EM}}} D_{\tau} h^{A,A'}}_{\text{possible new boson}} + \dots$$

laser spectroscopy (PTB) + Penning trap mass measurements (MPIK)  
show clear nonlinearities



# Isotope shifts in $^{168,170,172,174,176}\text{Yb}$

Door, Yeh, Heinz, Kirk, Lyu, Miyagi et al., arXiv:2403.07792

nonlinearity decomposition suggests one dominant contribution

$$\nu_{\tau, \text{nonlin.}}^{A, A'} = G_{\tau}^{(2)} (\delta \langle r^2 \rangle^2)^{A, A'} + G_{\tau}^{(4)} \delta \langle r^4 \rangle^{A, A'}$$

higher-order nuclear structure

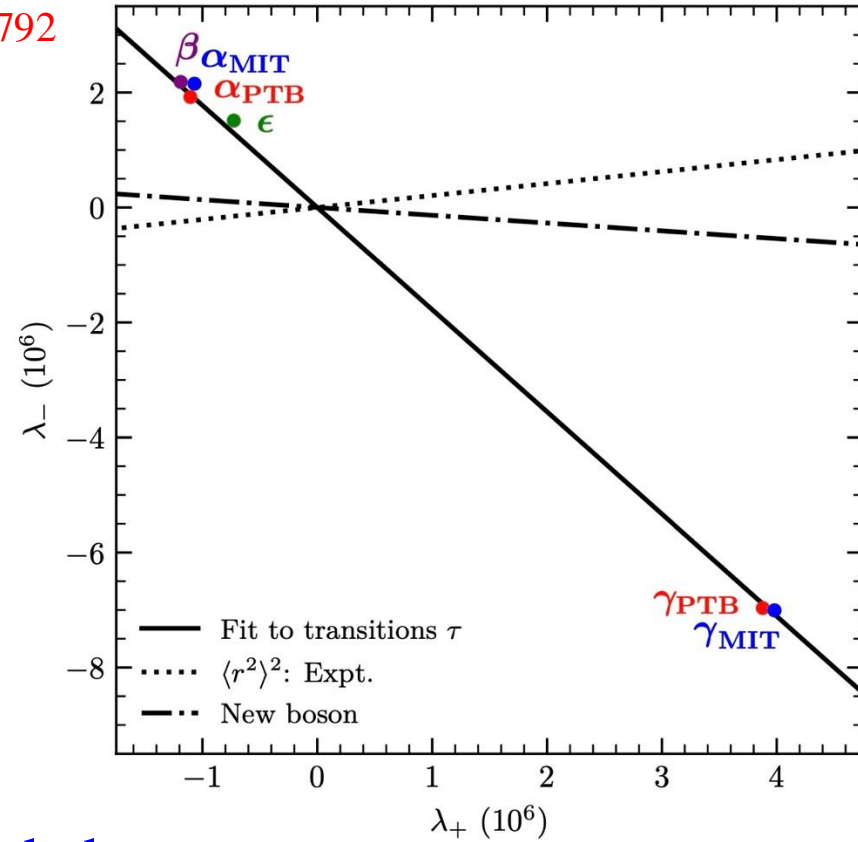
$$+ \frac{\alpha_{\text{NP}}}{\alpha_{\text{EM}}} D_{\tau} h^{A, A'} + \dots$$

possible new boson

→ not quadratic field shift

→ not new boson

theory predictions of quartic radius needed



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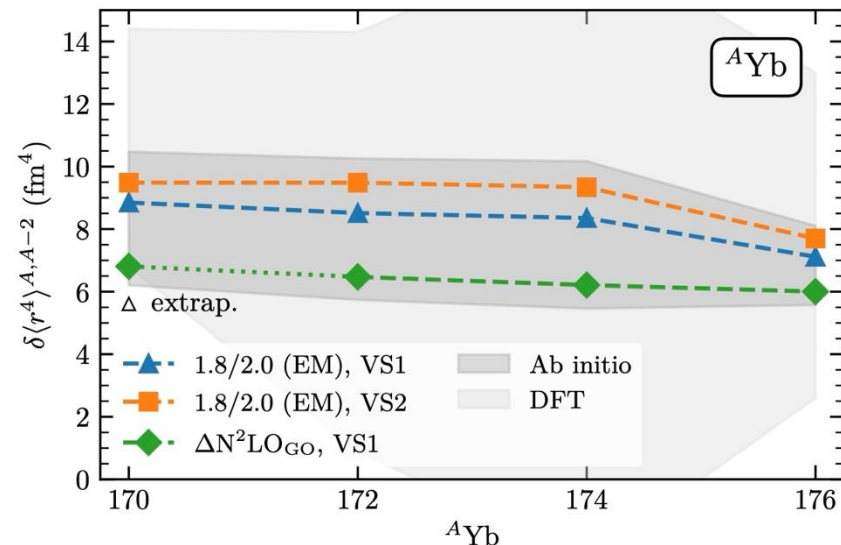
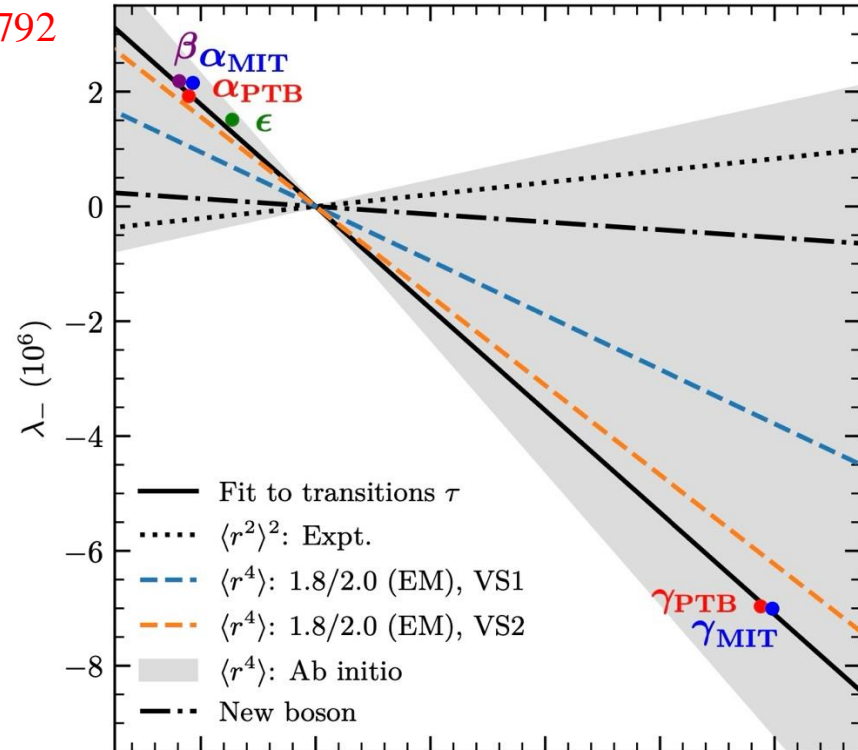
VS-IMSRG calculations,

uncertainty estimates from:

1.8/2.0 (EM),  $\Delta\text{N}^2\text{LO}_{\text{GO}}$  interactions,

two valence spaces,

many-body estimated from IMSRG(3)



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nonlinearity decomposition suggests  
one dominant contribution

$$\nu_{\tau, \text{nonlin.}}^{A, A'} = G_{\tau}^{(2)}(\delta\langle r^2 \rangle^2)^{A, A'} + G_{\tau}^{(4)}\delta\langle r^4 \rangle^{A, A'}$$

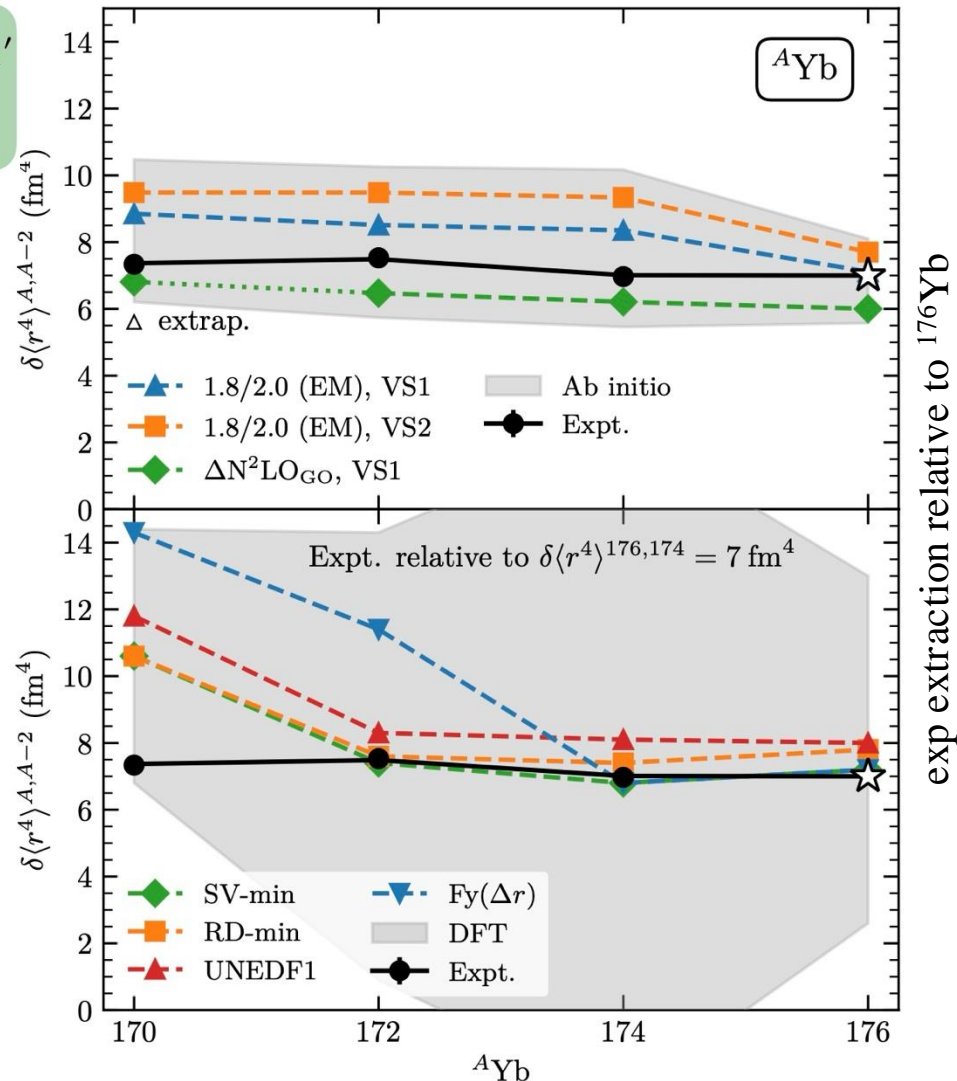
higher-order nuclear structure

$$+ \frac{\alpha_{\text{NP}}}{\alpha_{\text{EM}}} D_{\tau} h^{A, A'} + \dots$$

possible new boson

- not quadratic field shift
- not new boson
- dominant nonlinearity from quartic radius term

NEW: extract quartic radius from experimental data:  
observable related to deformation, trends consistent with ab initio





# Outline

New chiral low-resolutions interactions

**Pierre Arthuis**, Hebeler, AS, arXiv:2401.06675

Probing nuclear structure with nonlinear King plots  
in ytterbium isotopes

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Uncertainty quantification for low-resolution interactions

**Tom Plies, Matthias Heinz**, AS, preliminary

# EFT uncertainties for SRG-evolved interactions

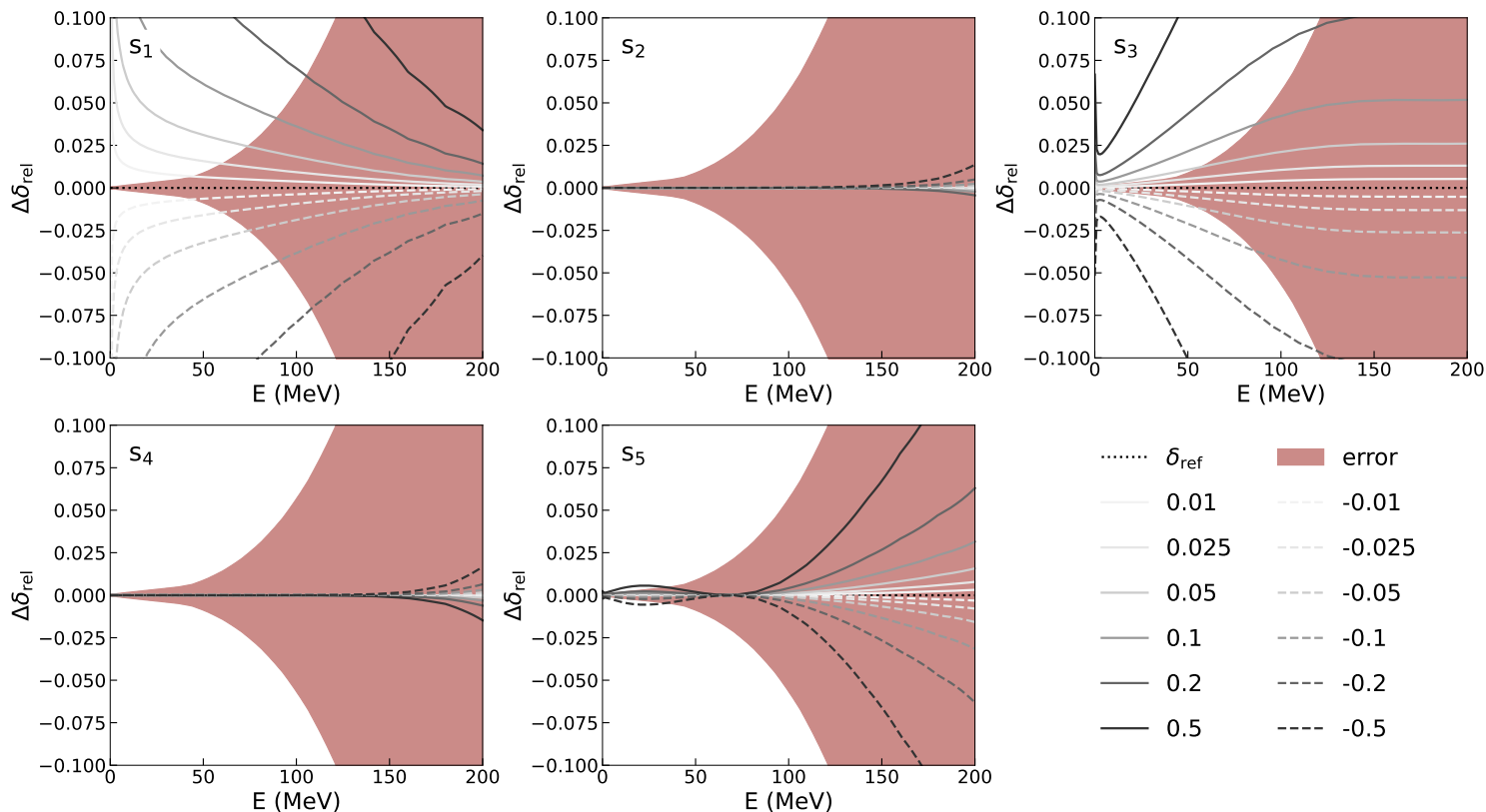
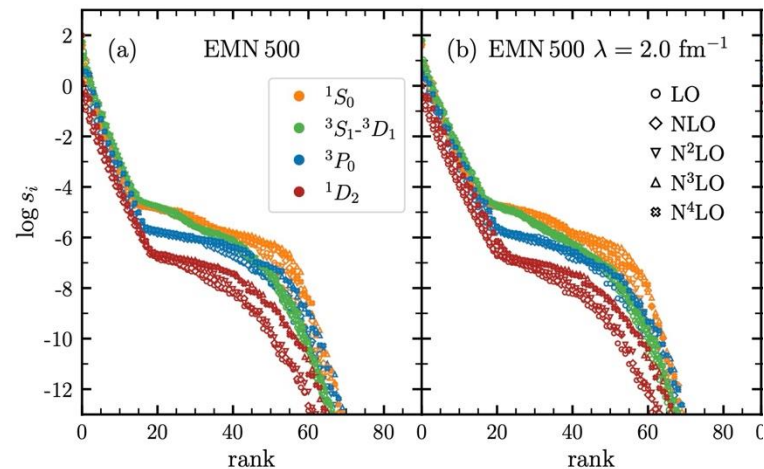
Tom Plies, Matthias Heinz, AS, preliminary

use singular value decomposition (SVD)

as operator basis see Tichai et al., PLB (2021)

consider lowest 5 singular values/operators

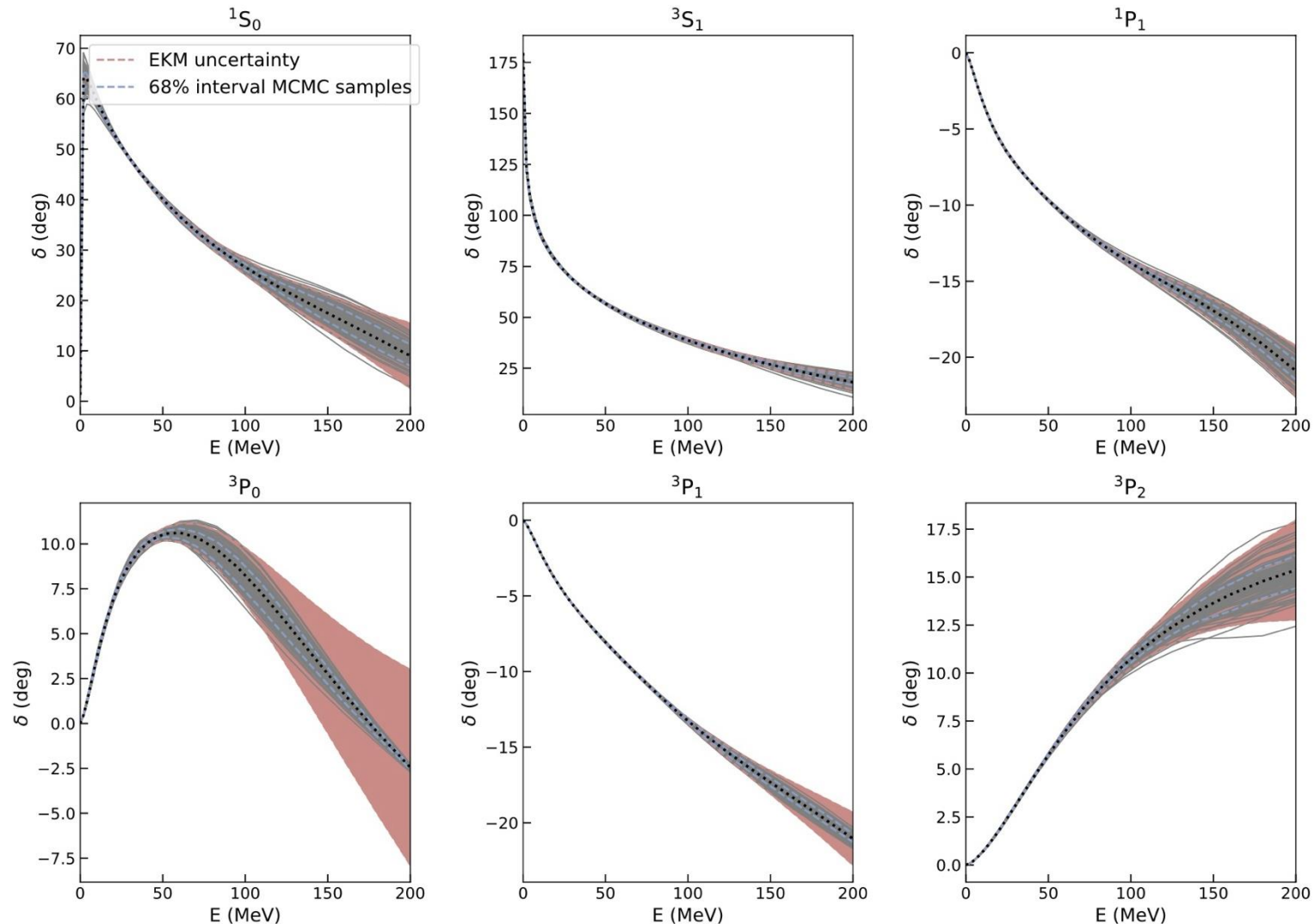
effectively 3 generate phase shift variation



# EFT uncertainties for SRG-evolved interactions

Tom Plies, Matthias Heinz, AS, preliminary

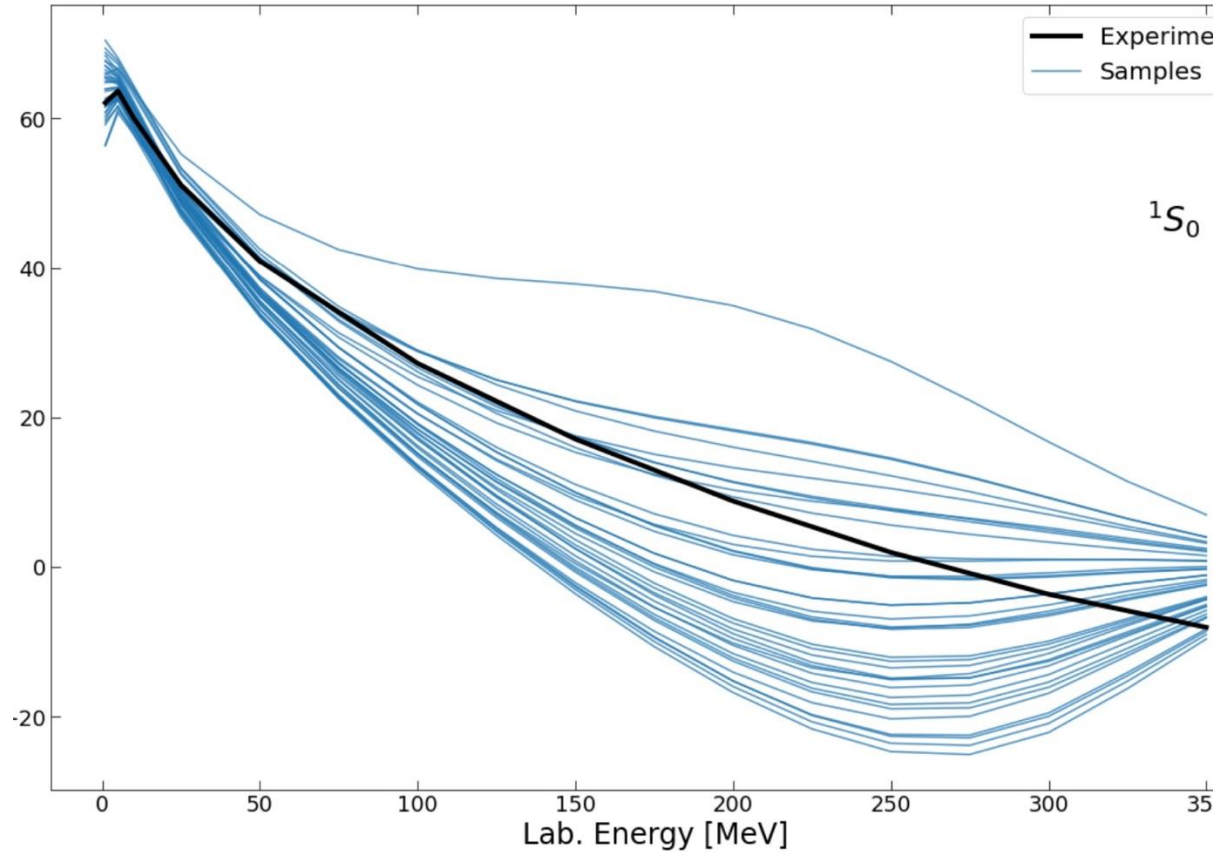
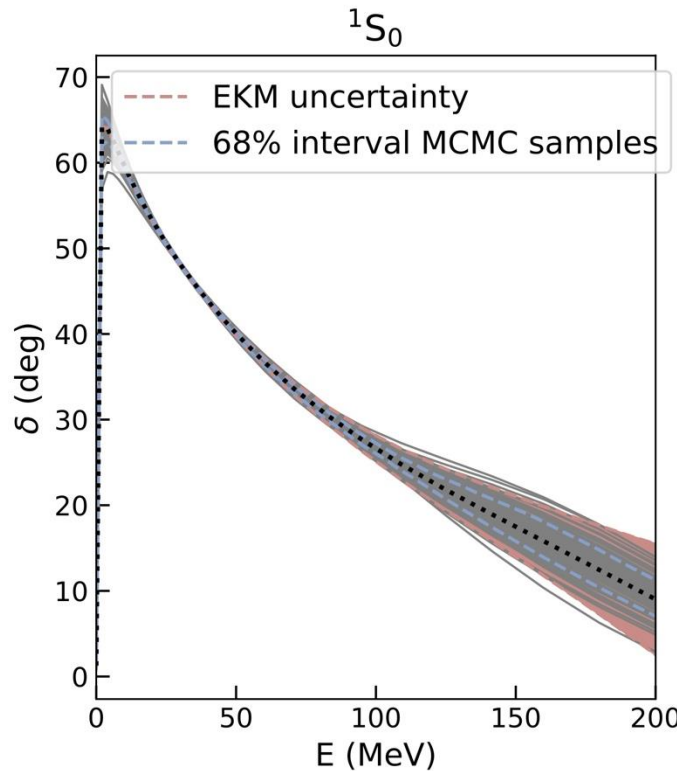
generate range of low-resolution NN interactions from random draws among 3 singular values with likelihood given by EFT uncertainties



# EFT uncertainties for SRG-evolved interactions

Tom Plies, Matthias Heinz, AS, preliminary

generate range of low-resolution NN interactions from random draws among 3 singular values with likelihood given by EFT uncertainties



comparison to nonimplausible  $\Delta N^2LO$  interactions Ekström, Forssen et al.

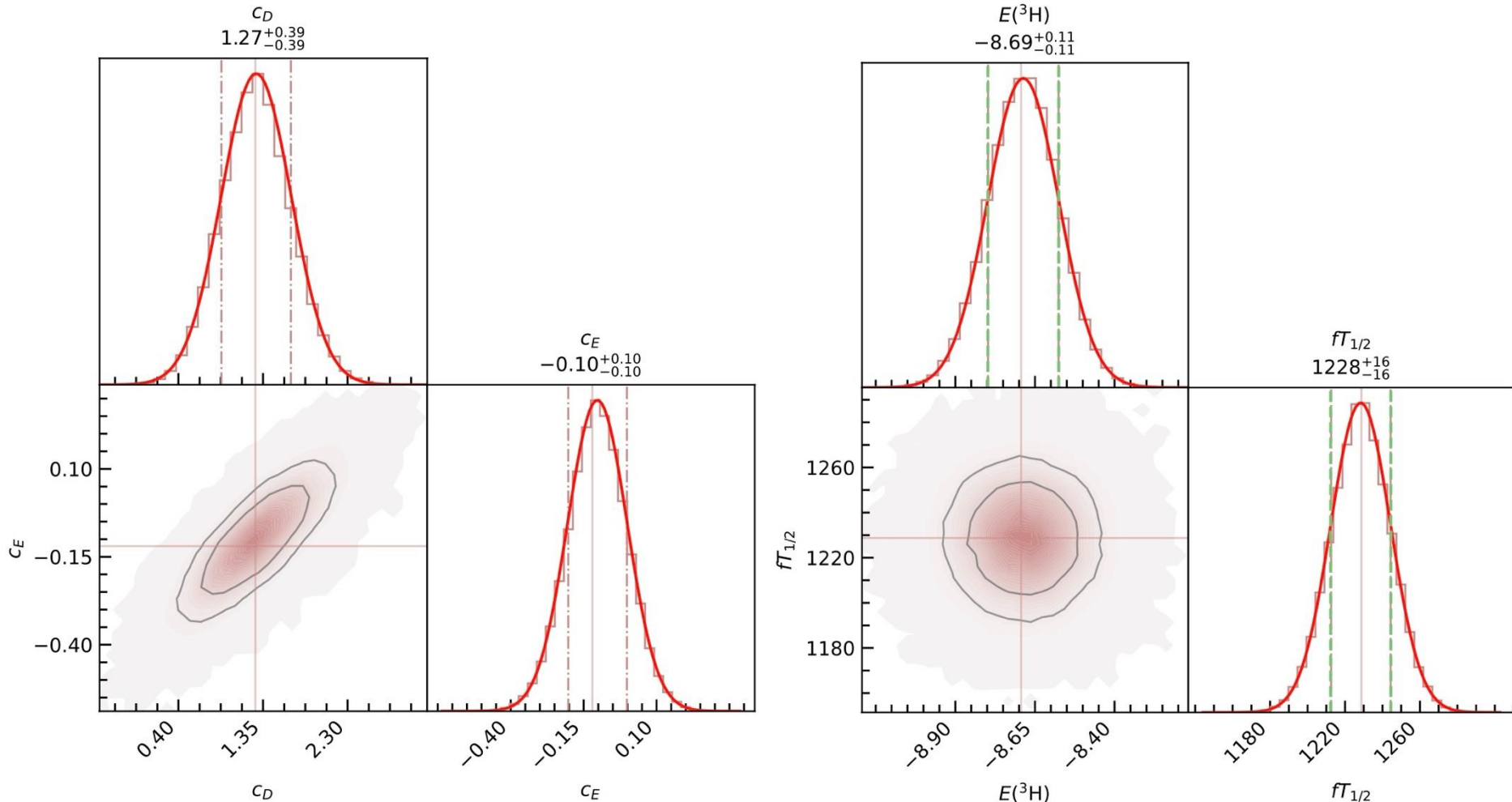
# EFT uncertainties for SRG-evolved interactions

Tom Plies, Matthias Heinz, AS, preliminary

generate range of low-resolution NN+3N interactions

here: S and P waves, higher partial waves unvaried,

3N uncertainties from  ${}^3\text{H}$  binding energy and half-life EFT uncertainties



# EFT uncertainties for SRG-evolved interactions

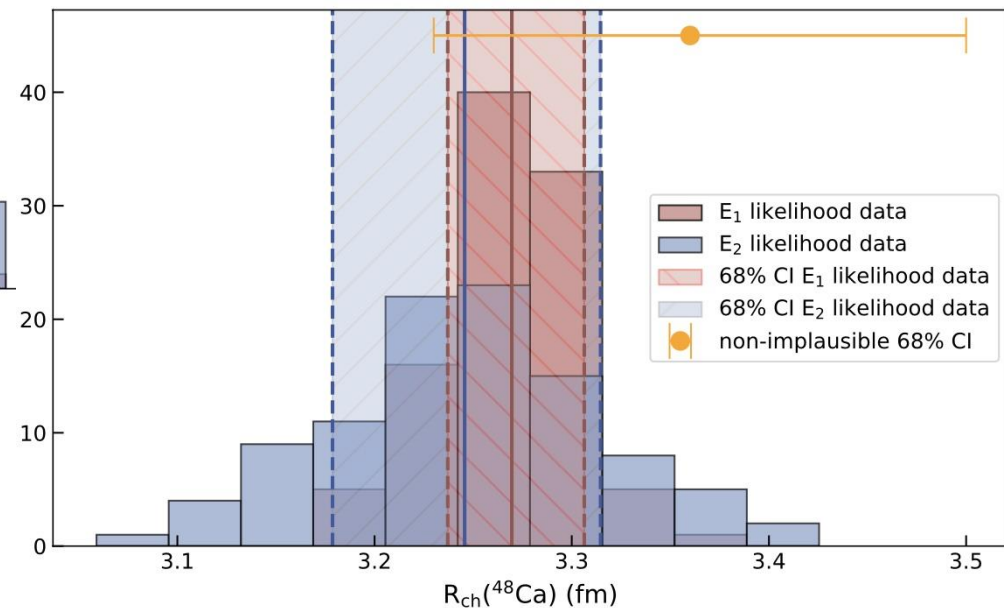
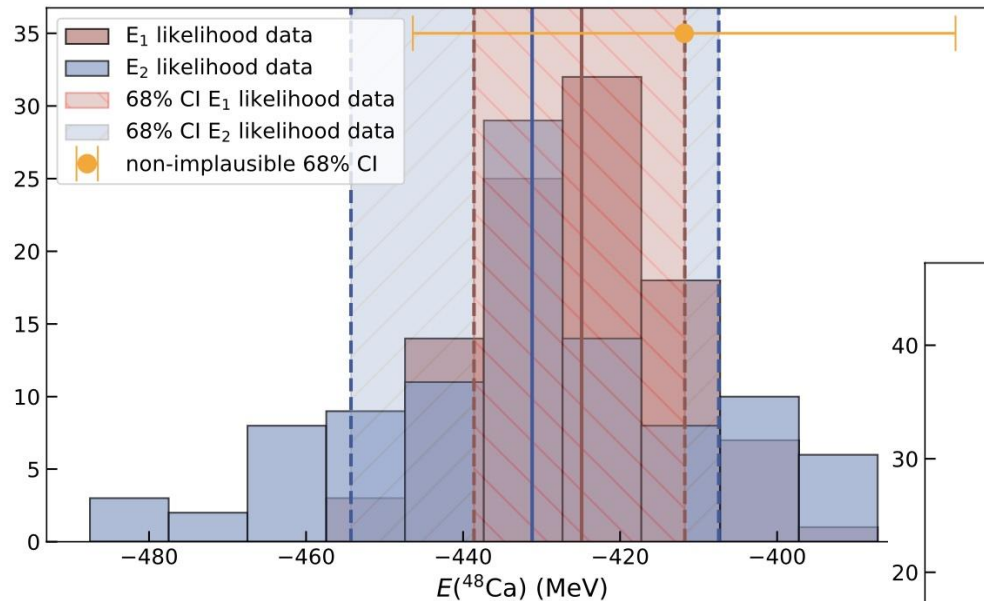
Tom Plies, Matthias Heinz, AS, preliminary

generate range of low-resolution NN+3N interactions

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3N uncertainties from  ${}^3\text{H}$  binding energy and half-life EFT uncertainties

resulting posterior distributions for  ${}^{48}\text{Ca}$  ground-state energy and radius



# Summary

## Chiral EFT interactions + powerful many-body methods

- great progress for ab initio calculations of nuclei

## New chiral low-resolutions interactions

**Pierre Arthuis**, Hebeler, AS, arXiv:2401.06675

- neutron skins remarkably similar up to  $^{208}\text{Pb}$  for chiral NN+3N

## Probing nuclear structure with nonlinear King plots in ytterbium isotopes

**Door, Yeh, Matthias Heinz, Kirk, Lyu, Takayuki Miyagi** et al., arXiv:2403.07792

- first extraction of  $\delta R_{\text{ch}}^4$  from isotope shifts, evolution along heavy Yb isotopes in good agreement with IMSRG calculations

## Uncertainty quantification for low-resolution interactions

**Tom Plies, Matthias Heinz**, AS, preliminary

- SVD basis to sample EFT uncertainties, first results for  $^{48}\text{Ca}$