

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A new set of data from a dedicated experiment



Tumpa Bhattacharjee,
Variable Energy Cyclotron Centre, Kolkata, India

Competition between Tetrahedral and Octahedral
Symmetries in ^{152}Sm Nucleus: A New set of data
from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in
Nuclei - From Experiment to Theory (SSNET -2024)
JJC Lab, France, November 04th - 08th, 2024

We are Here

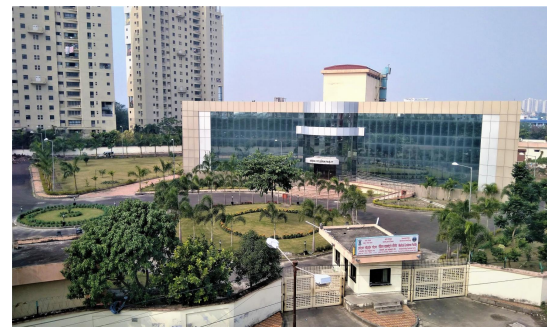


Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
JJC Lab, France, November 04th - 08th, 2024

We are Here



Variable Energy Cyclotron Centre



Homi Bhabha National Institute

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

The institute and City of Cyclotrons

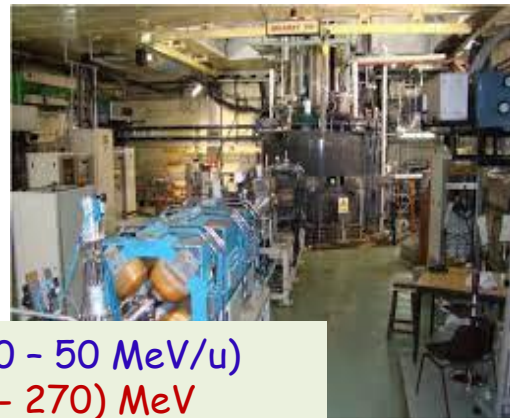


K-130 (E ~ 7 - 10 MeV/u)

$^{14}\text{N}^{4+}$, $^{16}\text{O}^{5+}$, $^{20}\text{Ne}^{6+}$, $^{32}\text{S}^{10+}$,etc.

^1H , ^2H , ^4He

- High energy Light ion beam



K-500 (E ~ 10 - 50 MeV/u)

$^{14}\text{N}^{4+}$ (252- 270) MeV

$^{16}\text{O}^{5+}$ (330 - 362) MeV,

$^{20}\text{Ne}^{6+}$ (397 - 434) MeV



Medical Cyclotron

30 MeV H Cyclotron

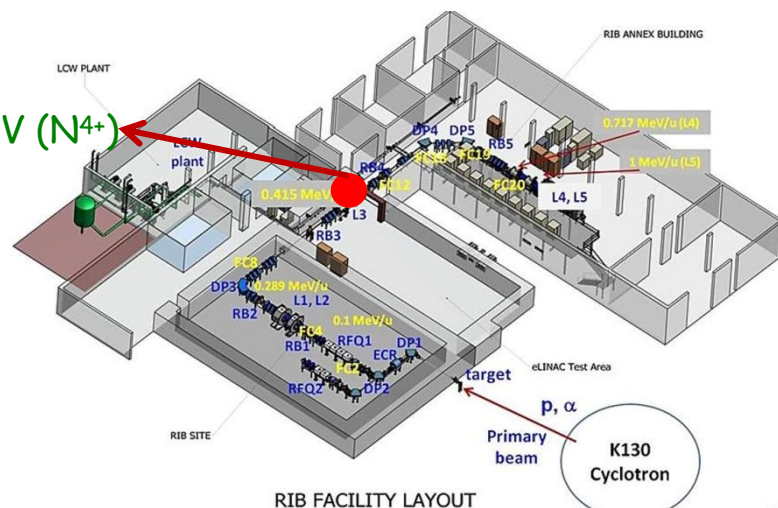
- Adjustable from 15- 30 MeV

- I ~ 350 μA

^{18}F (produce FDG for PET)

^{67}Ga , ^{201}Tl , ^{123}I (SPECT)

E ~ 415 keV (N^{4+})



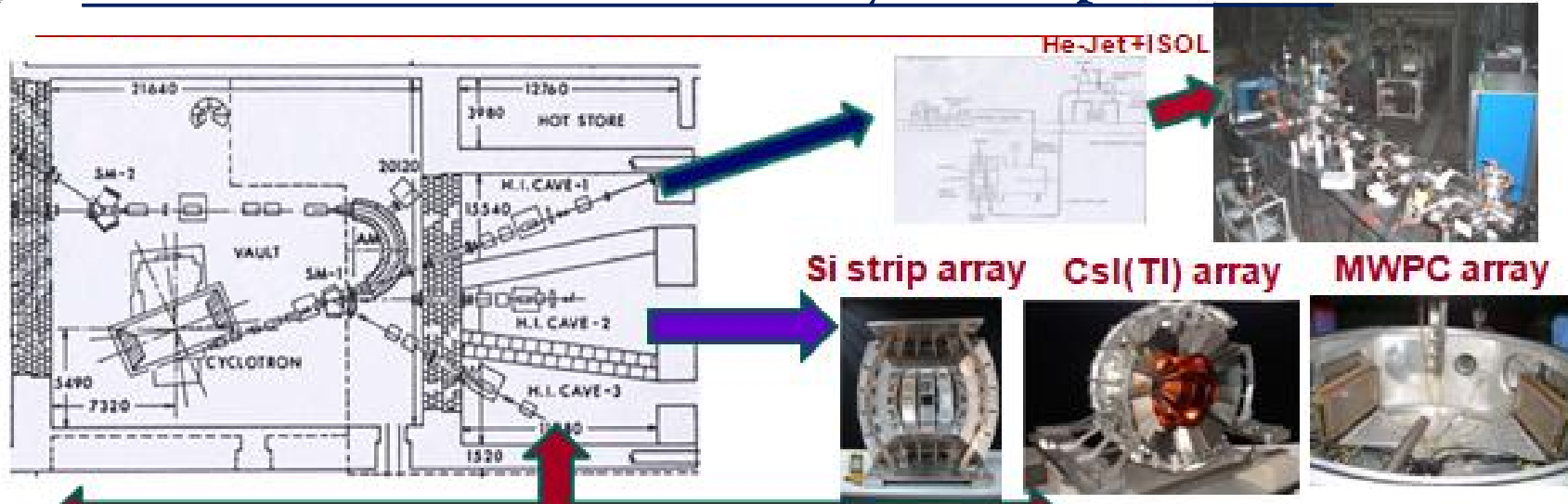
RIB (E ~ 100keV/u, I ~ 8000 p/sec)
 ^{11}C , ^{11}CO , $^{11}\text{CO}_2$, ^{14}O , ^{43}K , ^{41}Ar

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

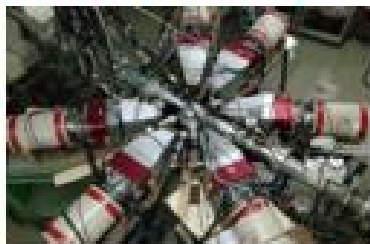
Tumpa Bhattacharjee,
 VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
 JY Lab, France, November 04th - 08th, 2024

Instruments for Nuclear Physics Experiment



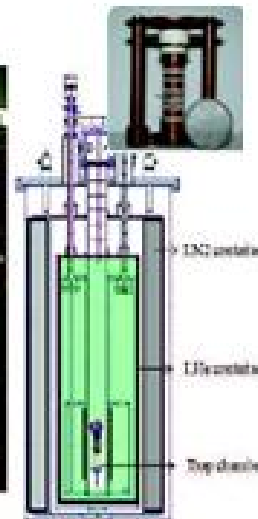
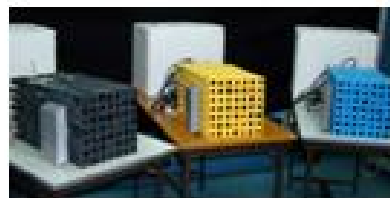
VENUS+VENTURE



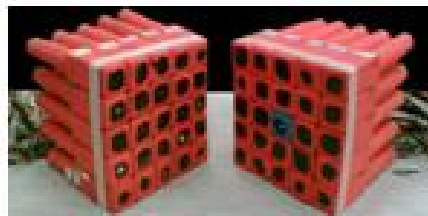
INGA



LAMBDA array



n-TOF array



γ-multiplicity array



4p n-multiplicity Detector

Penning Trap

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

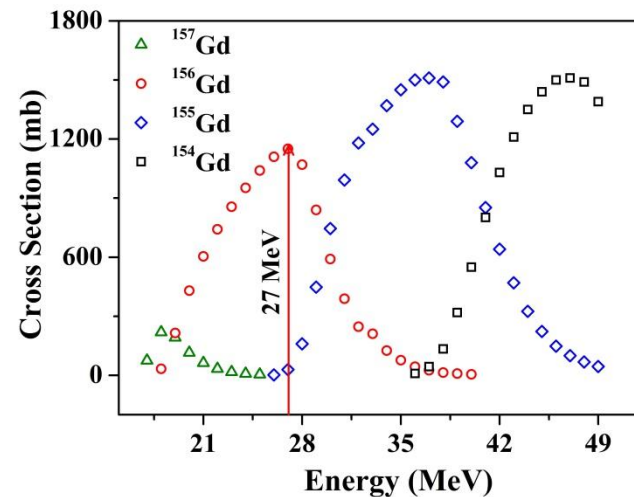
International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
JC Lab, France, November 04th - 08th, 2024

Setup for high resolution γ -ray Spectroscopy



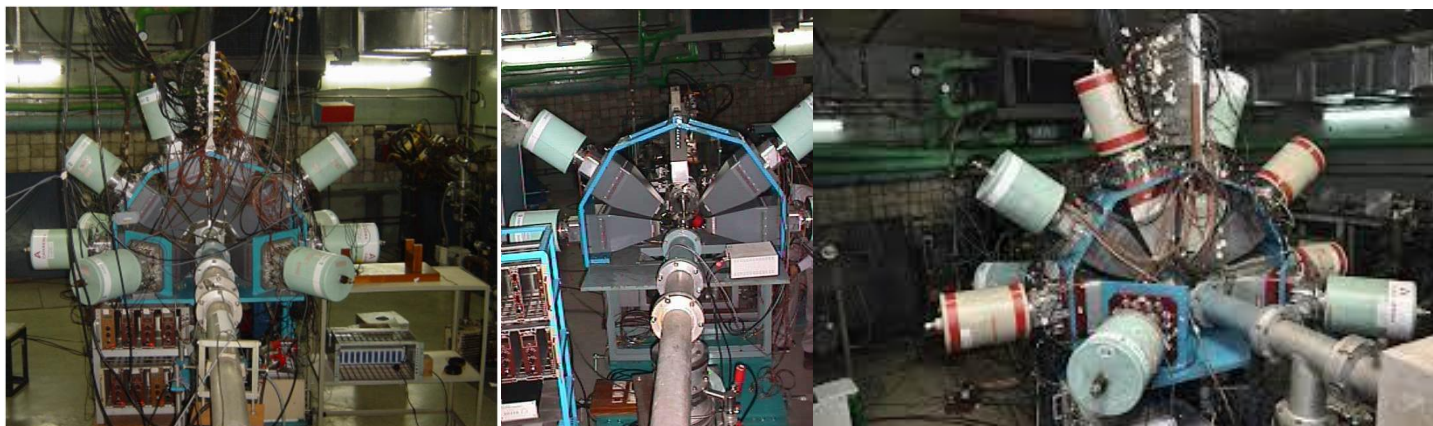
A. Saha et al., Nucl. Phys. A **976**, 1 (2018)

Soumik Bhattacharya et al., Phys. Rev. C **98**, 044311 (2018)



Spectroscopy with light ion beam

VECC array for NUclear Spectroscopy
EIGHT Compton suppressed Clover HPGe detectors



Indian National Gamma Array (INGA)

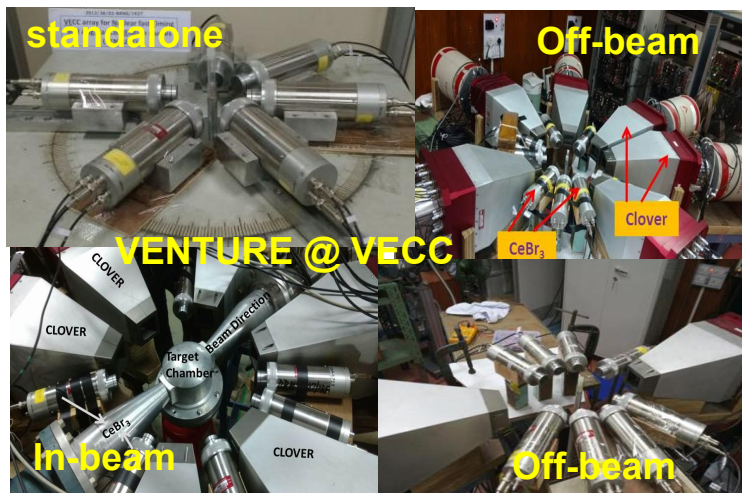
Compton suppressed Clover HPGe detectors – pulled from many institutes

Competition between Tetrahedral and Octahedral Symmetries in ¹⁵²Sm Nucleus: A New set of data from a dedicated experiment

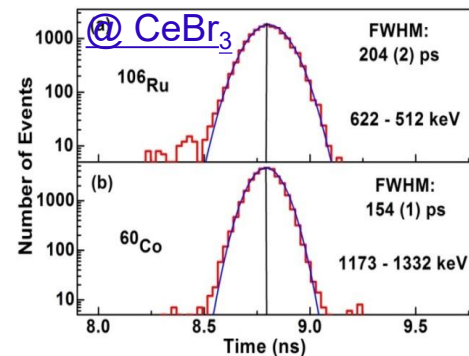
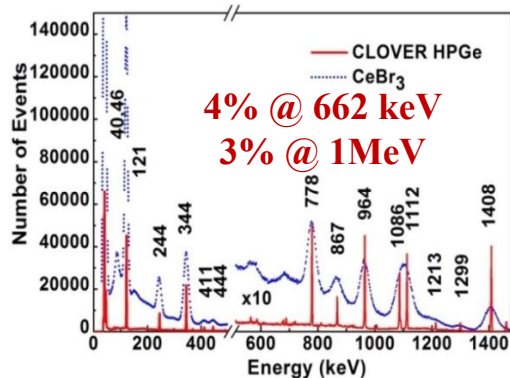
Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei – From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th – 08th, 2024

Setups for γ - γ fast timing Spectroscopy



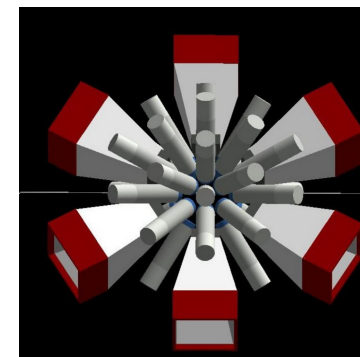
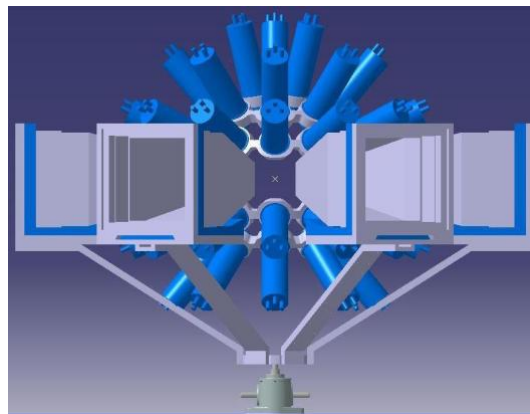
VECC array for Nuclear fast Timing and angular CorRELation studies (VENTURE)



1. S. S. Alam, TB, et al., NIM Phys. Res. A **874** 103 (2017)
2. S. S. Alam, TB, Phys. Rev. C **99**, 014306 (2019).
3. S. Basak, TB, Phys. Rev. C **104**, 024320 (2021).
4. S. S. Alam, D. Banerjee, TB et al., Eur. Phys. Jour. A **56**, 269 (2020).

Recent measurement
Lifetimes in ^{154}Gd

Poster at SSNET 2024



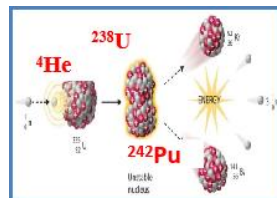
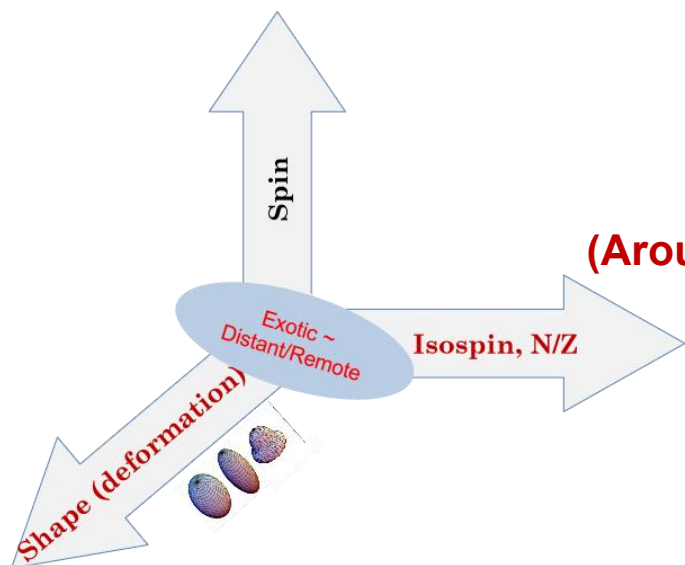
VENTURE - 2.0 with 2in. x 1 in. LaBr/CeBr

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

Setups for γ - γ fast timing Spectroscopy



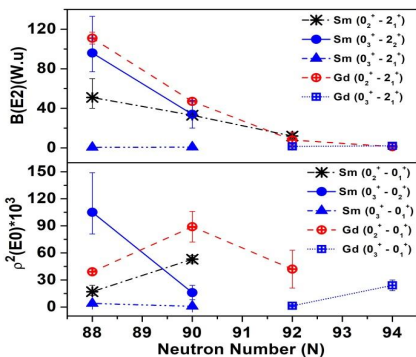
Radiochemical separation at VECC OR LOHENGRIN at ILL

(Around $Z = 50, N = 82$)

(Around $Z = 64, N = 90$ & $Z = 40, N = 60$)
Measurement of lifetime to determine $E0$ rates

^{130}Xe	^{131}Xe (stable)	^{132}Xe (stable)	^{133}Xe (5d)	^{134}Xe (stable)	^{135}Xe (9h) $N/Z=1.5$	^{136}Xe (stable)	^{137}Xe	54
^{129}I	^{130}I	^{131}I (8d)	^{132}I (2h)	^{133}I (21h)	^{134}I (53h)	^{135}I (6.6h)	^{136}I	53
^{128}Te	^{129}Te	^{130}Te (stable)	^{131}Te (33h)	^{132}Te (3.2d)	^{133}Te (55m)	^{134}Te (42m)	^{135}Te	52
^{127}Sb	^{128}Sb	^{129}Sb	^{130}Sb (40m)	^{131}Sb	^{132}Sb (4 min)	^{133}Sb	^{134}Sb	51
^{126}Sn	^{127}Sn	^{128}Sn	^{129}Sn (2 min)	^{130}Sn	^{131}Sn	^{132}Sn $N/Z=1.6$	^{133}Sn	50
76	77	78	79	80	81	82	83	

$N \rightarrow$



S. Basak, S. S. Alam, D. Kumar, A. Saha, D. Banerjee and TB
Phys. Rev. C **104**, 024320 (2021).

D. Kumar, TB et al., Phys. Rev. C **106**, 034306 (2022)
D. Kumar,TB et al., Phys. Rev. C **109**, 024304 (2024)

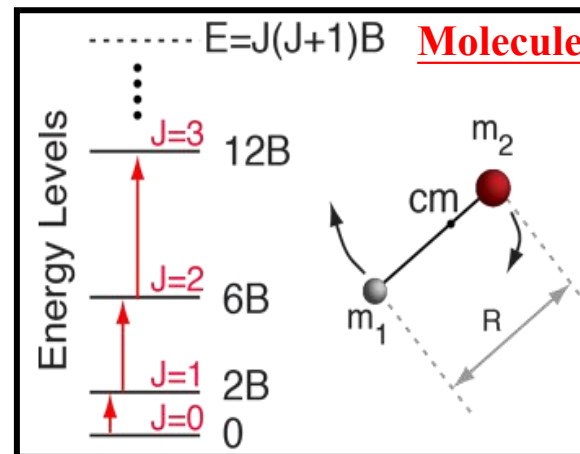
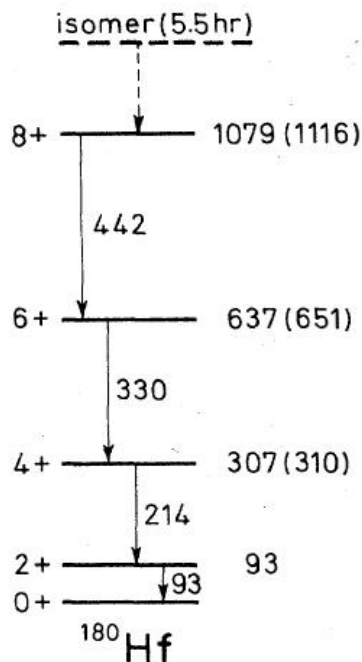
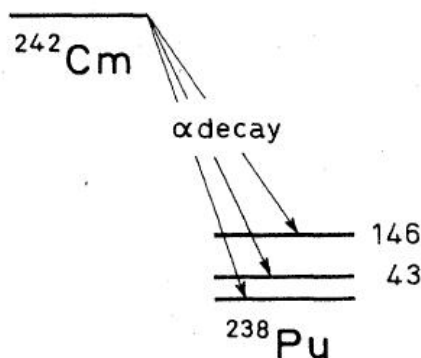
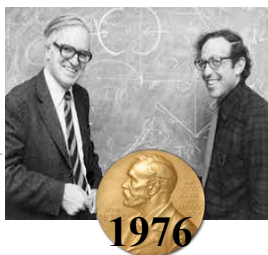
$Z \uparrow$

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

Deformed Nuclei – Rotational Symmetry breaking



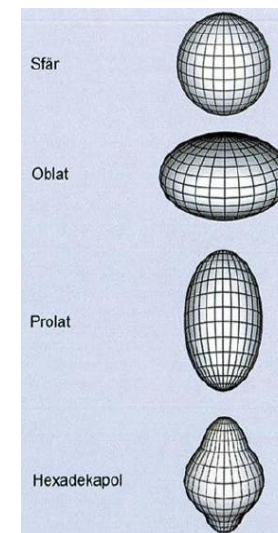
Collective excitation

$$E = \left(\frac{\hbar^2}{2\mathcal{I}} \right) \cdot J(J+1)$$

Aage Bohr and Ben R. Mottelson,
Phys. Rev. 89, 316 (1953); Phys.
Rev. 90, 717 (1953).

Reviews of Modern
Physic, Vol. 48, No. 3,
July 1976

All nuclei are not
spherical!! Some are like
Cigar or Disc!!



Competition between Tetrahedral and Octahedral
Symmetries in ^{152}Sm Nucleus: A New set of data
from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

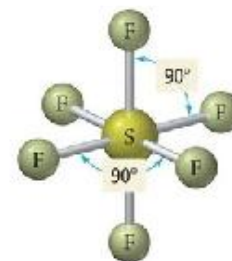
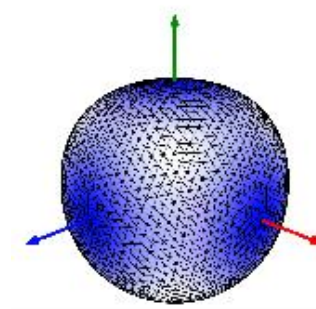
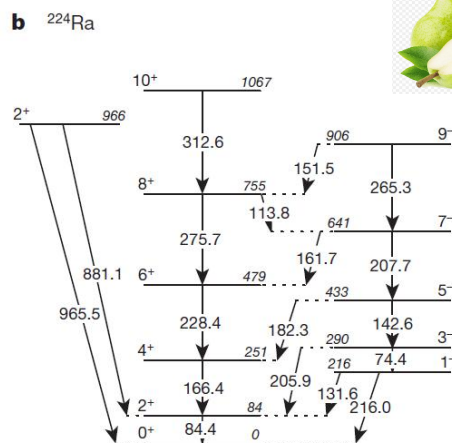
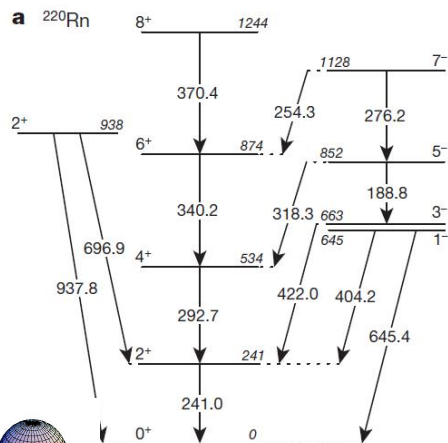
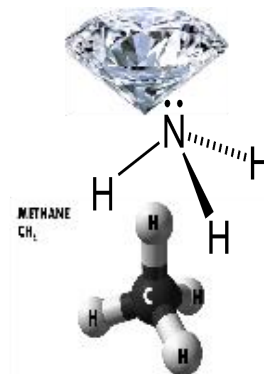
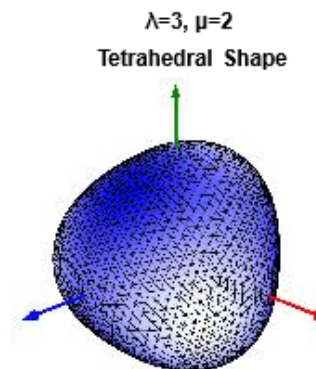
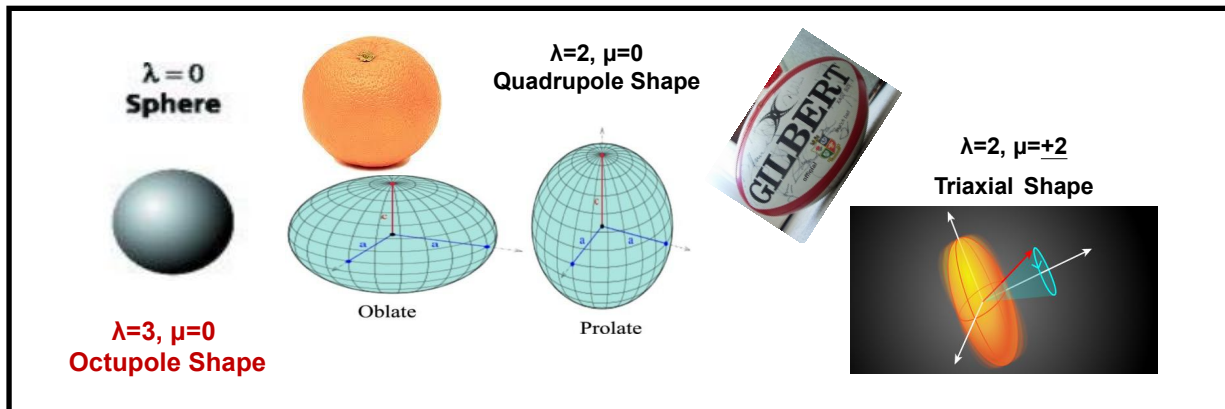
International Conference on Shapes and Symmetries in
Nuclei – From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th – 08th, 2024

Shapes of Atomic Nuclei

$$R(\theta, \varphi) = R_0 [1 + \sum_{\lambda} \sum_{\mu} \alpha_{\lambda\mu} Y_{\lambda\mu}(\theta, \varphi)]$$

R_0 = radius of a sphere

$\alpha_{\lambda\mu}$ = coefficients represent distortions from the equilibrium spherical shape



L. P. Gaffney et al., [Nature 497, 199 \(2013\)](#)

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

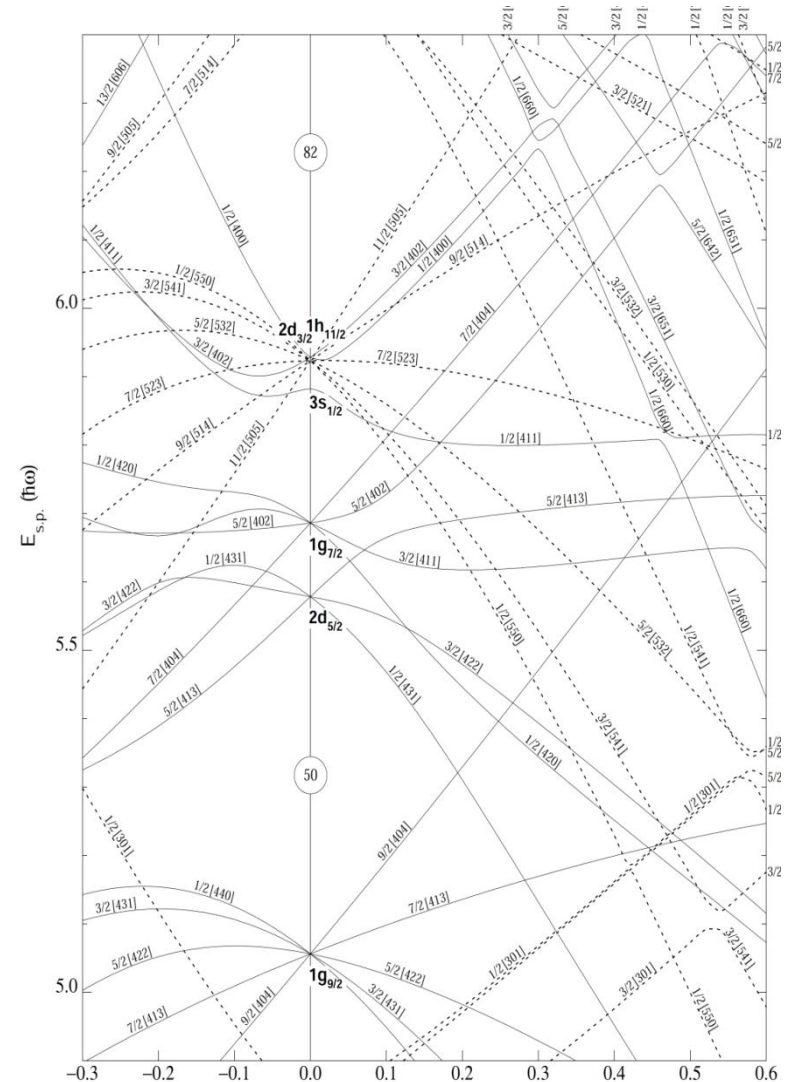
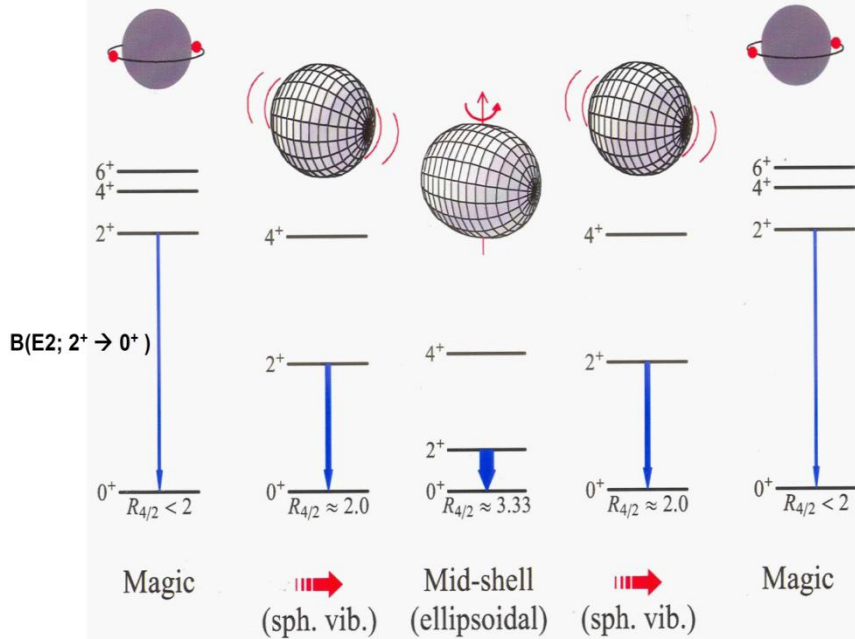
Nuclear Shell Gaps – Spherical & Deformed Nuclei



$$\mathcal{H} = \frac{P^2}{2m} + \frac{1}{2}m[\omega_{\perp}^2(x^2 + y^2) + \omega_z^2 z^2] + C\vec{l} \cdot \vec{s} + D\vec{l} \cdot \vec{l}$$

Binding states of individual nucleons in strongly deformed nuclei

Evolution of nuclear structure (as a function of valence nucleon number)



S. G. Nilsson, Kgl. Danske Videnskab. Selskab, Mat.-fys.Medd. **29**, No.16 (1955).

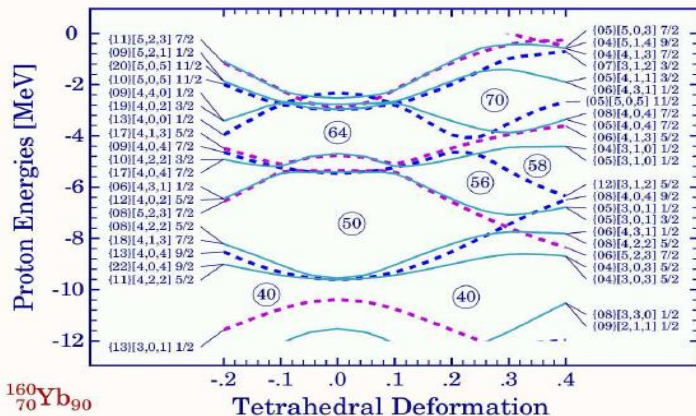
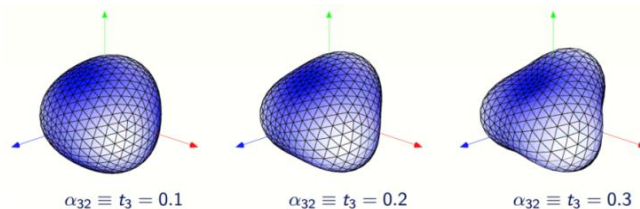
Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee, VECC, Kolkata

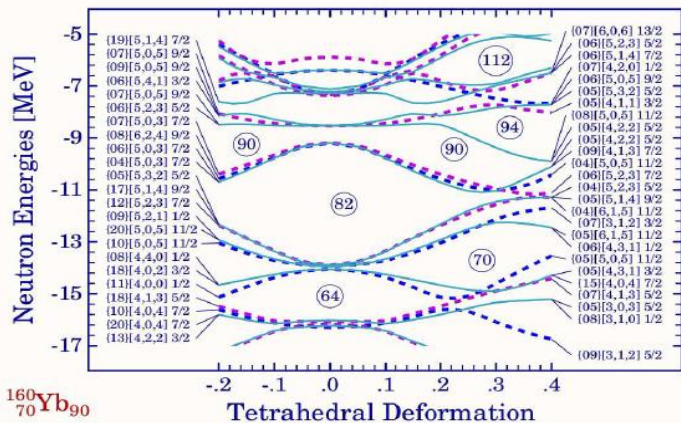
International Conference on Shapes and Symmetries in Nuclei – From Experiment to Theory (SSNET -2024) IJC Lab, France, November 04th – 08th, 2024

Tetrahedral Symmetry breaking ($\alpha_{32} \neq 0$)

$$\Sigma: R(\vartheta, \varphi) = R_0 c(\{\alpha\}) \left[1 + \sum_{\lambda} \sum_{\mu} \alpha_{\lambda\mu}^* Y_{\lambda\mu}(\vartheta, \varphi) \right]$$



$^{160}_{70}\text{Yb}_{90}$



$^{160}_{70}\text{Yb}_{90}$

No.	Group	No. Irr.	No. x Dimensions
01.	O_h^D	6	4 x 2D and 2 x 4D
02.	O^D	3	2 x 2D and 1 x 4D
03.	T_d^D	3	2 x 2D and 1 x 4D
04.	C_{6h}^D	12 → 6	12 x 1D
05.	D_{6h}^D	6	6 x 2D
06.	T_h^D	6	6 x 2D
07.	D_{4h}^D	4	4 x 2D
-	D_{2h}^D	2	2 x 2D (reference)

$T_d^D \rightarrow$ Tetrahedral double point group
(48 symmetry elements)

2 families of 2 fold degenerate energy levels,
1 family of 4 fold degenerate energy levels

Higher fold degeneracies of nucleonic levels

\rightarrow Exotic symmetry breaking in nuclei

Phys. Rev. Lett. 88, 252502 (2002),
Phys. Rev. Lett. 97, 072501 (2006)

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

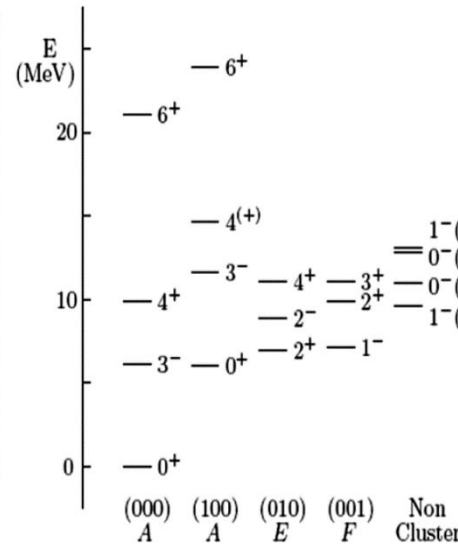
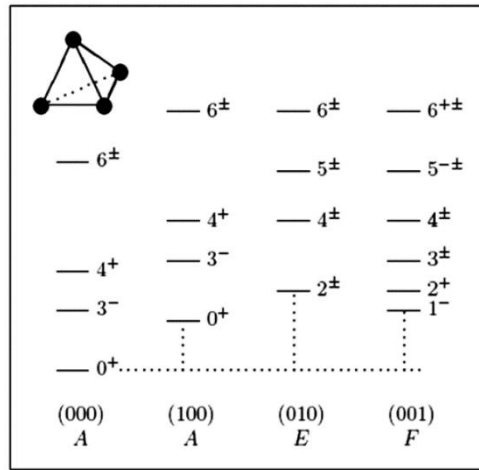
Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
JJC Lab, France, November 04th - 08th, 2024

Tetrahedral Symmetry breaking ($\alpha_{32} \neq 0$)

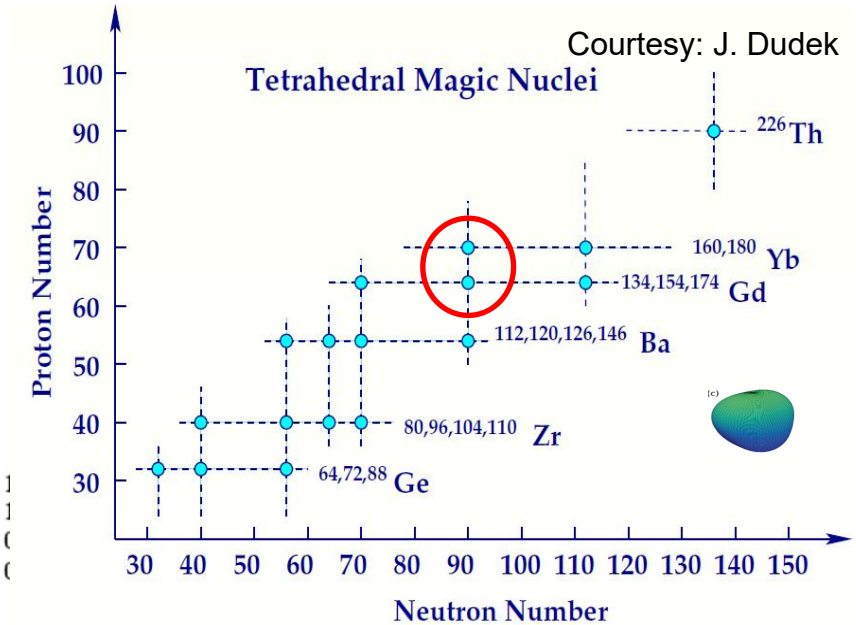
Evidence of tetrahedral shape in Nuclei :
Cluster state in ^{16}O (Light nuclei)

PRL 112, 152501 (2014)



Theory
(Algebraic Cluster Model)

Experiment



$Z/N \rightarrow 16, 20, 32, 40, 56, 64, 70, 90$
 $N \rightarrow 112, 136, 142$
 (Tetrahedral Magic Gaps)

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

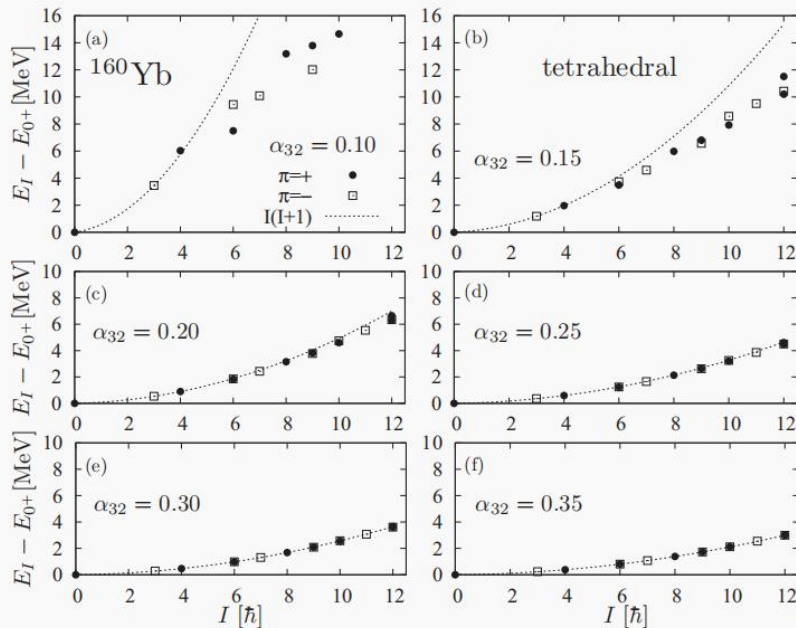
International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
JJC Lab, France, November 04th - 08th, 2024

Tetrahedral Symmetry breaking ($\alpha_{32} \neq 0$)

TABLE VI. The number of states $a_i^{(I\pi)}$ belonging to the five irreducible representations of T_d for integer spins; those for each parity are separately shown.

I^+	0^+	1^+	2^+	3^+	4^+	5^+	6^+	7^+	8^+	9^+	10^+	11^+	12^+	13^+	14^+	15^+	16^+
A_1	1	0	0	0	1	0	1	0	1	1	1	0	2	1	1	1	2
A_2	0	0	0	1	0	0	1	1	0	1	1	1	1	1	1	2	1
E	0	0	1	0	1	1	1	1	2	1	2	2	2	2	3	2	3
$F_1(T_1)$	0	1	0	1	1	2	1	2	2	3	2	3	3	4	3	4	4
$F_2(T_2)$	0	0	1	1	1	1	2	2	2	2	3	3	3	3	4	4	4
I^-	0^-	1^-	2^-	3^-	4^-	5^-	6^-	7^-	8^-	9^-	10^-	11^-	12^-	13^-	14^-	15^-	16^-
A_1	0	0	0	1	0	0	1	1	0	1	1	1	1	1	1	2	1
A_2	1	0	0	0	1	0	1	0	1	1	1	0	2	1	1	1	2
E	0	0	1	0	1	1	1	1	2	1	2	2	2	2	3	2	3
$F_1(T_1)$	0	0	1	1	1	1	2	2	2	2	3	3	3	3	4	4	4
$F_2(T_2)$	0	1	0	1	1	2	1	2	2	3	2	3	3	4	3	4	4

Microscopic mean-field and residual-interaction Hamiltonians with angular-momentum and parity projection method



S. Tagami et al., PRC **87**, 054306 (2013)

Lowest Irrep for T_d symmetry

$A_1 : I^\pi = 0^+, 3^+, 4^+, 6^+, 7^-, 8^+, 9^+, 10^+, 11^-, \dots \rightarrow$ Exact T_d pattern

Two lowest irreps for O_h symmetry

$A_{1g} : 0^+, 4^+, 6^+, 8^+, 9^+, 10^+, \dots, I^\pi = I^+, \rightarrow$ Exact $O_h, I_\pi = 0^+$

$A_{2u} : 3^-, 6^-, 7^-, 9^-, 10^-, 11^-, \dots, I^\pi = I^-, \rightarrow$ Exact $O_h, I_\pi = 0^-$

\rightarrow Tetrahedral double point group (T_d^D) is a subgroup of Octahedral double point group (O_h^D)

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee, VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024) JJC Lab, France, November 04th - 08th, 2024



Tetrahedral Symmetry breaking ($\alpha_{32} \neq 0$)

Rotational band with $E \sim I(I+1) \rightarrow$ Bohr Theory

Lowest Irrep for T_d symmetry

$$A_1 : I^\pi = 0^+, 3^-, 4^+, 6^\pm, 7^-, 8^+, 9^\pm, 10^\pm, 11^-, \dots$$

$$E_I \propto \frac{\hbar^2}{2\mathcal{J}_{T_d}} I(I+1)$$

Two lowest irreps for O_h symmetry

$$A_{1g} : 0^+, 4^+, 6^+, 8^+, 9^+, 10^+, \dots, I^\pi = I^+,$$

$$E \propto = \frac{h^2}{2I_{A_{1g}}} I(I+1)$$

$$A_{2u} : 3^-, 6^-, 7^-, 9^-, 10^-, 11^-, \dots, I^\pi = I^-,$$

$$E \propto = \frac{h^2}{2I_{A_{2u}}} I(I+1)$$

Pure tetrahedral structure

$$\mathcal{J}_{A_{1g}} \approx \mathcal{J}_{A_{2u}} \approx \mathcal{J}_{A_1}$$

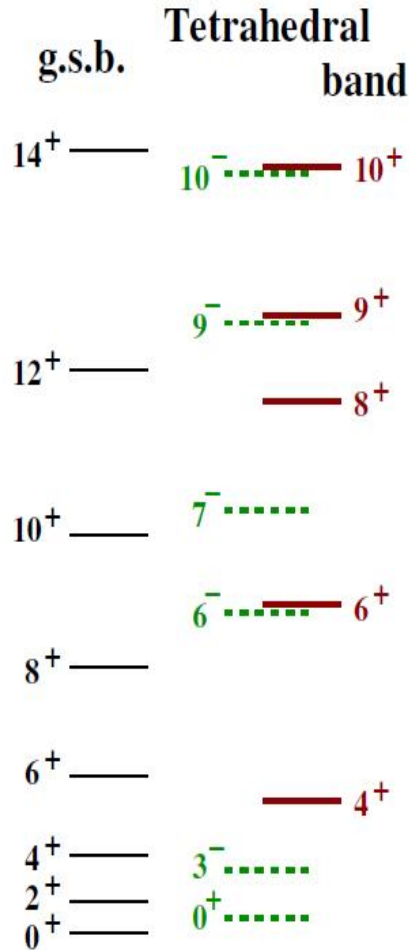
Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
JJC Lab, France, November 04th - 08th, 2024

Tetrahedral Symmetry breaking ($\alpha_{32} \neq 0$)

Courtesy: J. Dudek



- For small deformations we may use Taylor expansion:

$$Q_{\lambda\mu}(\alpha) \approx Q_{\lambda\mu}|_{\alpha=0} + Q'_{\lambda\mu}|_{\alpha=0} \Delta\alpha + \frac{1}{2} Q''_{\lambda\mu}|_{\alpha=0} \Delta\alpha \Delta\alpha$$

- We set $\lambda = 2, \mu = 0$ and $\lambda_1 = \lambda_2 = 3, \Delta\alpha \approx \alpha_{3\mu}|_{\alpha \text{ small}} \rightarrow$

$$\alpha_{30} : Q_{20} = 4/(3\sqrt{5\pi}) \cdot \alpha_{30}^2 \cdot \rho_0 R_0^5$$

$$\alpha_{31} : Q_{20} = 6/(3\sqrt{5\pi}) \cdot \alpha_{3+1}\alpha_{3-1} \cdot \rho_0 R_0^5$$

$$\alpha_{32} : Q_{20} = 0 \leftarrow \text{Tetrahedral symmetry}$$

$$\alpha_{33} : Q_{20} = 10/(3\sqrt{5\pi}) \cdot \alpha_{3+3}\alpha_{3-3} \cdot \rho_0 R_0^5$$

E2 decay forbidden!!

E3 decay enhanced

$B(E3) = ??$ (order of magnitude)

$$T(E1) = 1.59 \cdot 10^{15} \cdot E^3 B(E1)$$

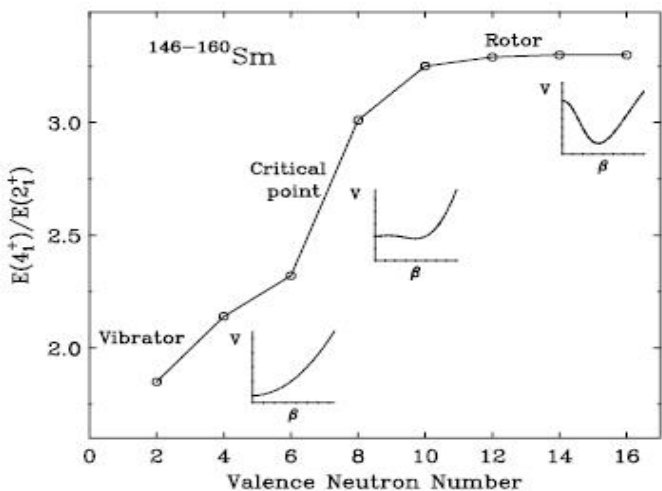
$$T(E2) = 1.22 \cdot 10^9 \cdot E^5 B(E2)$$

$$T(E3) = 5.67 \cdot 10^2 \cdot E^7 B(E3)$$

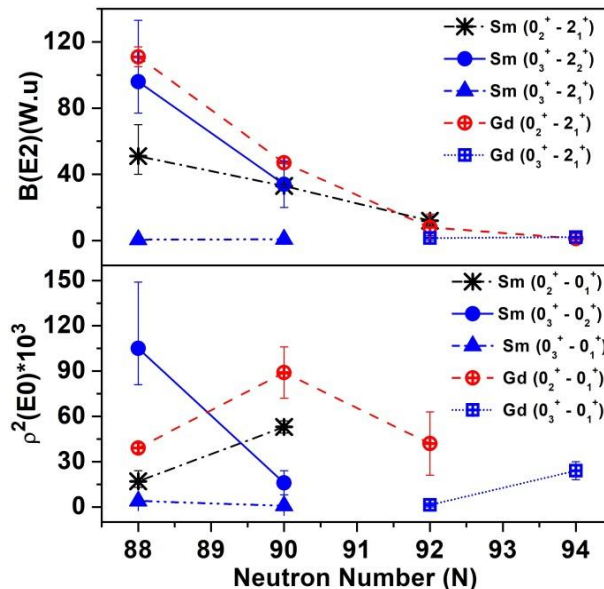
Existence of an isomeric band!!

Experimental identification becomes extremely challenging!!

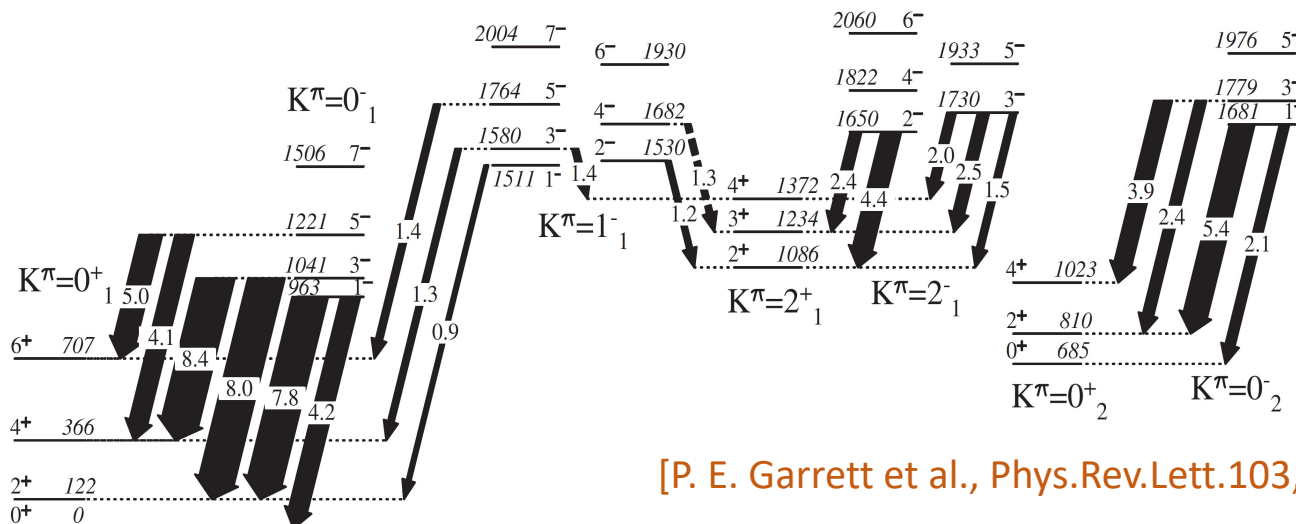
Physics Interest in ^{152}Sm



Phys. Rev. Lett. **87**, 052503 (2001)



S. Basak, S. S. Alam, D. Kumar, A. Saha, D. Banerjee and TB Phys. Rev. C **104**, 024320 (2021).



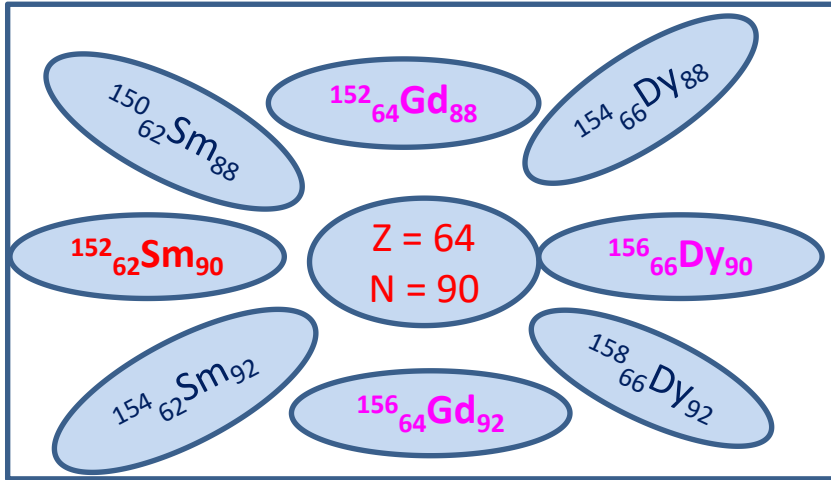
[P. E. Garrett et al., Phys.Rev.Lett.103,062501(2009)]

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

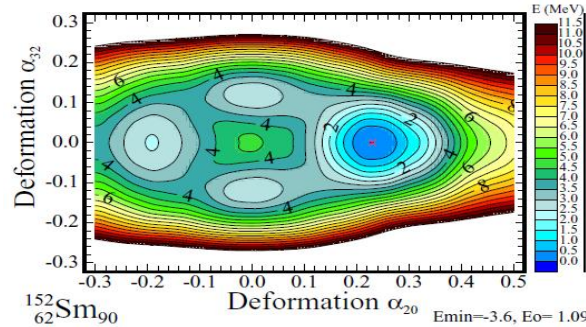
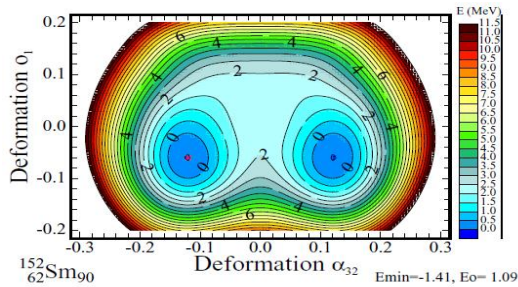
Physics Interest in ^{152}Sm



We are at Tetrahedral Magic Gap!!

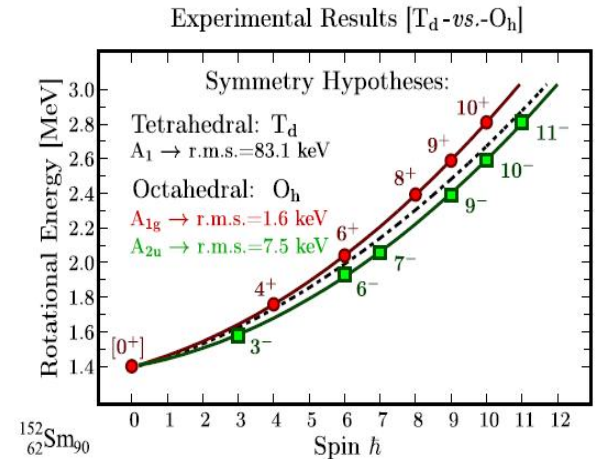
Spin	E[keV]	No. D-out	No. Feed	Reaction
3 ⁻	1579.4	10	none	CE & α
4 ⁺	1757.0	9	1+(1)	CE & α
6 ⁻	1929.9	2	(1)	CE & α
6 ⁺	2040.1	7	none	CE & α
7 ⁻	2057.5	6	2+(1)	CE & α
8 ⁺	2391.7	3	1	CE & α
9 ⁻	2388.8	4	3	CE & α
9 ⁺	2588	2	1	α
10 ⁻	2590.7	4	1	α
(10 ⁺)	2810	2	none	α
11 ⁻	2808.9	2	none	CE

J. Dudek et al., PRC 97, 021302(R) (2018)



➤ At vanishing quadrupole deformation, the minima in the PES is visible for non-zero a_{32} .

➤ The energy of this minima decreases with the presence of non-zero octahedral deformation.



$T_d(1)$ Band

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
JY Lab, France, November 04th - 08th, 2024

Population of ^{152}Sm

➤ High statistics →

High cross section

Increased Target thickness

High Beam current

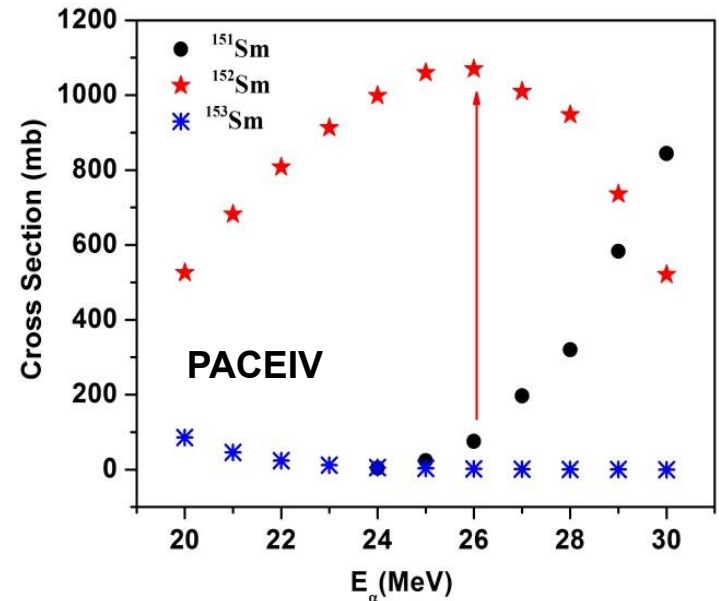
High efficiency Clover HPGe array

Long beamtime

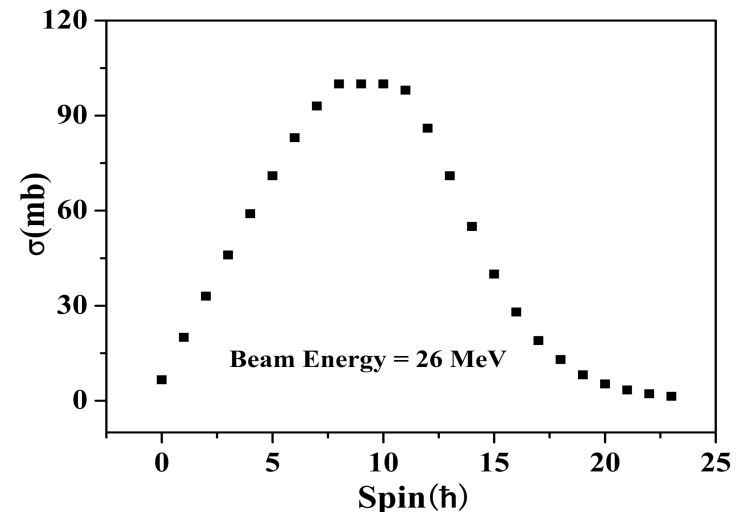
Keeping in mind: Limitation in Count rate in HPGe crystal 5- 6k/sec)

➤ Low angular momentum population

➤ Less contamination from neighboring evaporation channel



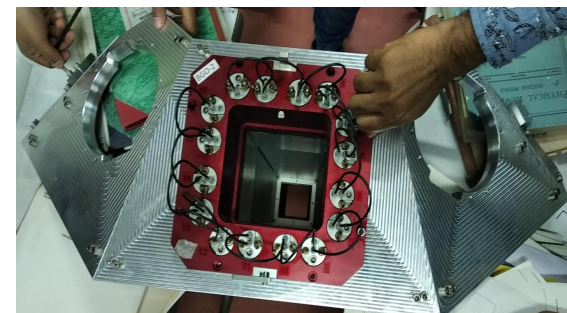
$^{150}\text{Nd} (^4\text{He}, 2n) ^{152}\text{Sm} @ 26 \text{ MeV}$



Gamma Array with local collaboration in Kolkata (VECC, SINP, UGC-DAE-CSR)



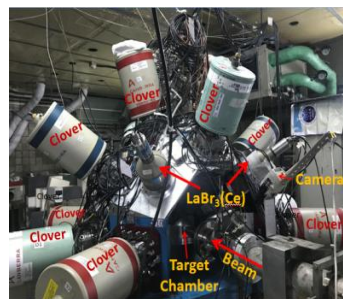
Before the augmentation



New segments MEG, VECC



Placing BGOs in the array

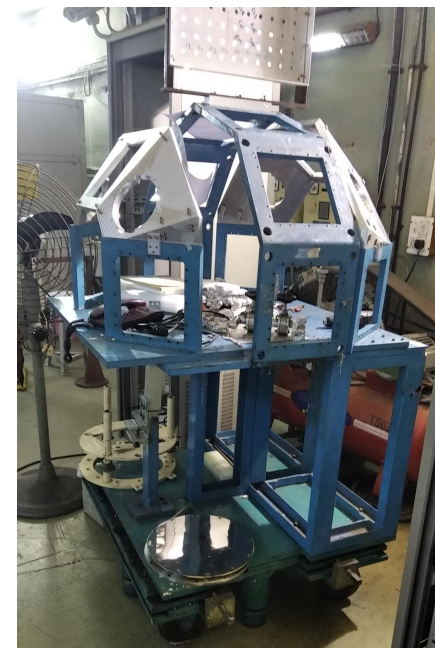


12 Detectors at:

90° : 6 Nos

40° : 3 Nos

125° : 3 Nos



Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
JJC Lab, France, November 04th - 08th, 2024

Comparison with existing experiment on ^{152}Sm

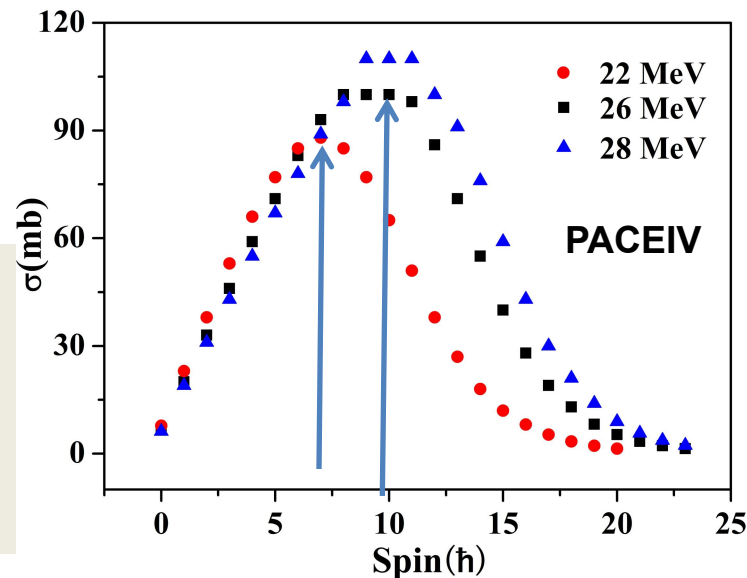
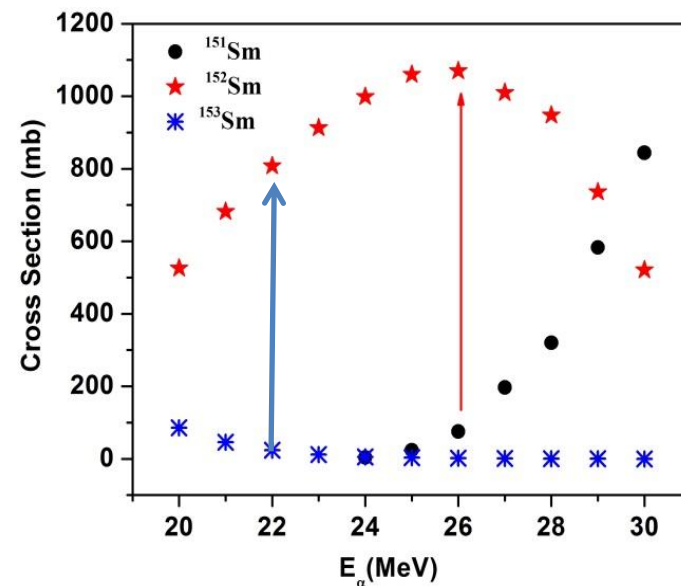
P. E. Garrett et al., J. Phys. G: Part & Nucl. Phys. 31, S1855 (2005)

- Performed with 9 single crystal HPGe and one Cluster HPGe detector
- Gathered 2×10^9 γ - γ events, Used 1×10^9 γ - γ events for the development of level scheme
- Beam energy : 22 MeV
- P/T ~ 0.28 (av)

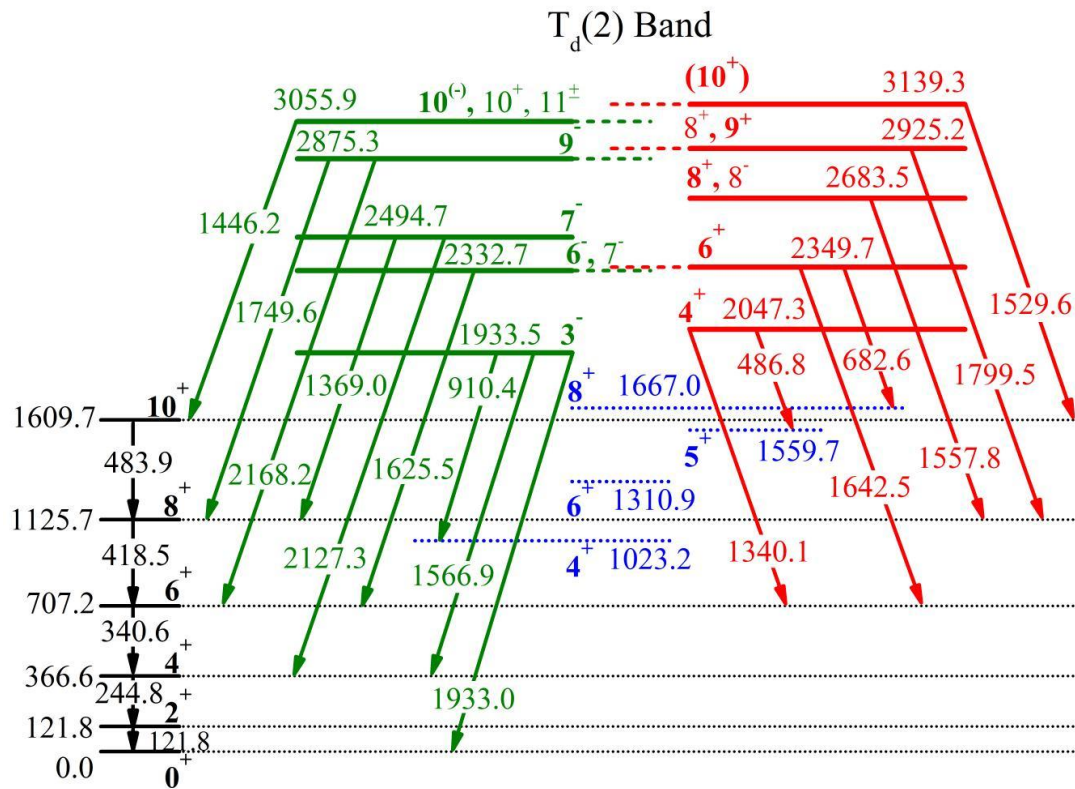
PRESENT EXPERIMENT:

- 12 Compton suppressed Clover HPGe detectors
- Beam Energy : 26 MeV
- γ - γ statistics $> 2 \times 10^9$
- P/T ~ 0.45

Gain
P/T ~ 1.6
Statistics ~ 2
 $1/\sqrt{N} \sim 0.5$



New candidate Tetrahedral sequence in ^{152}Sm



Beam current $\sim 2.5\text{nA}$

BOT ~ 11 days (effective)

Digital DAQ \rightarrow data written in Compton suppressed singles mode

Conventional γ - spectroscopy techniques

Measured

1. γ - γ & γ - γ - γ coincidences
2. Angular distribution a_2, a_4
3. Angular Correlation $\rightarrow R_{DCO}$
4. Linear Polarization P

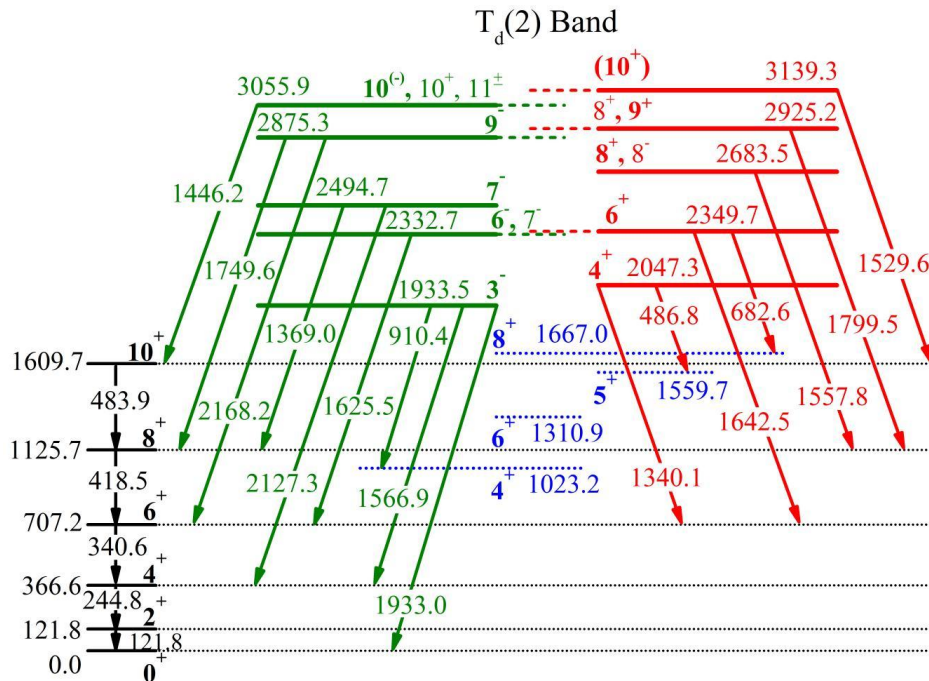
Calculated

P vs R_{DCO} contours

P vs a_2 contours

New candidate Tetrahedral sequence in ^{152}Sm

Relative Intensity



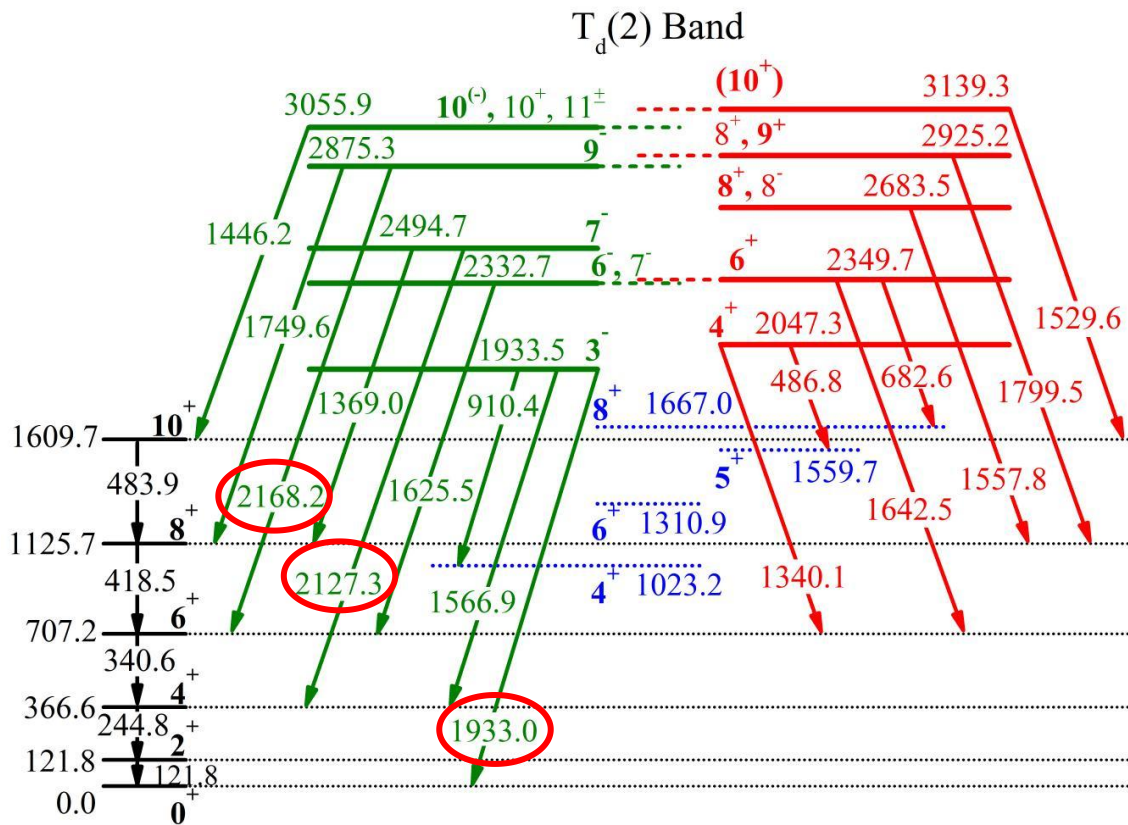
E_i (keV)	E_f (keV)	I_i^π	$\rightarrow I_f^\pi$	E_γ (keV)	I_γ
1933.5(8)	1023.22(4)	3^-	$\rightarrow 4^+$	910.4(1)	0.20(2)
	366.60(2)		$\rightarrow 4^+$	1566.9(2)	0.18(2)
	0.0		$\rightarrow 0^+$	1933.0(8)	0.05(1)
2047.3(3)	1559.71(4)	4^+	$\rightarrow 5^+$	486.8(3)	0.71(13)
	707.21(4)		$\rightarrow 6^+$	1340.1(1)	0.77(6)
2332.7(2)	707.21(4)	6^-	$\rightarrow 6^+$	1625.5(1)	0.35(2)
2349.7(2)	1667.97(6)	6^+	$\rightarrow 8^+$	682.6(1)	0.14(2)
	707.21(4)		$\rightarrow 6^+$	1642.5(2)	0.12(1)
2494.7(4)	1125.75(6)	7^-	$\rightarrow 8^+$	1369.0(1)	0.10(1)
	366.60(2)		$\rightarrow 4^+$	2127.3(4)	0.07(1)
2683.5(2)	1125.75(6)	8^+	$\rightarrow 8^+$	1557.8(1)	0.46(2)
2875.3(5)	1125.75(6)	9^-	$\rightarrow 8^+$	1749.6(1)	0.15(1)
	707.21(4)		$\rightarrow 6^+$	2168.2(5)	0.05(1)
2925.2(2)	1125.75(6)	9^+	$\rightarrow 8^+$	1799.5(1)	0.27(2)
3055.9(2)	1609.69(7)	10^-	$\rightarrow 10^+$	1446.2(1)	0.14(2)
3139.3(2)	1609.69(7)	(10^+)	$\rightarrow 10^+$	1529.6(1)	0.17(3)

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

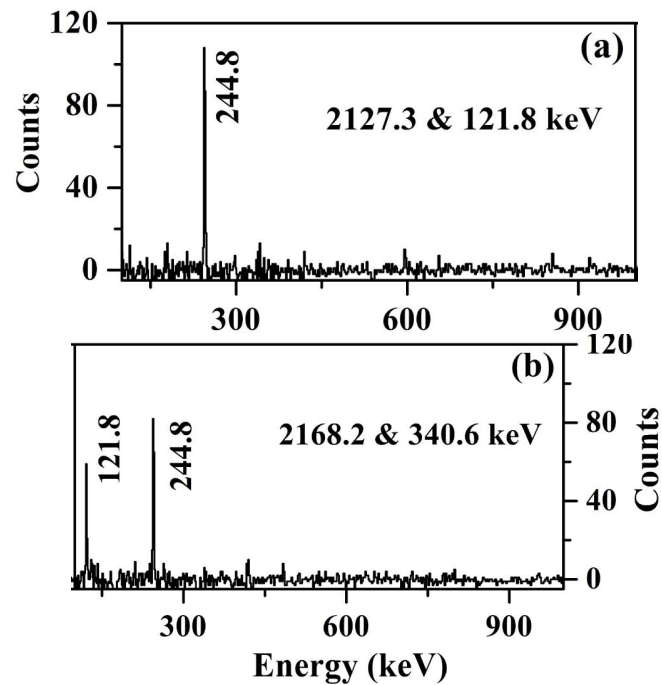
Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
JJC Lab, France, November 04th - 08th, 2024

New candidate Tetrahedral sequence in ^{152}Sm



E3 Transitions



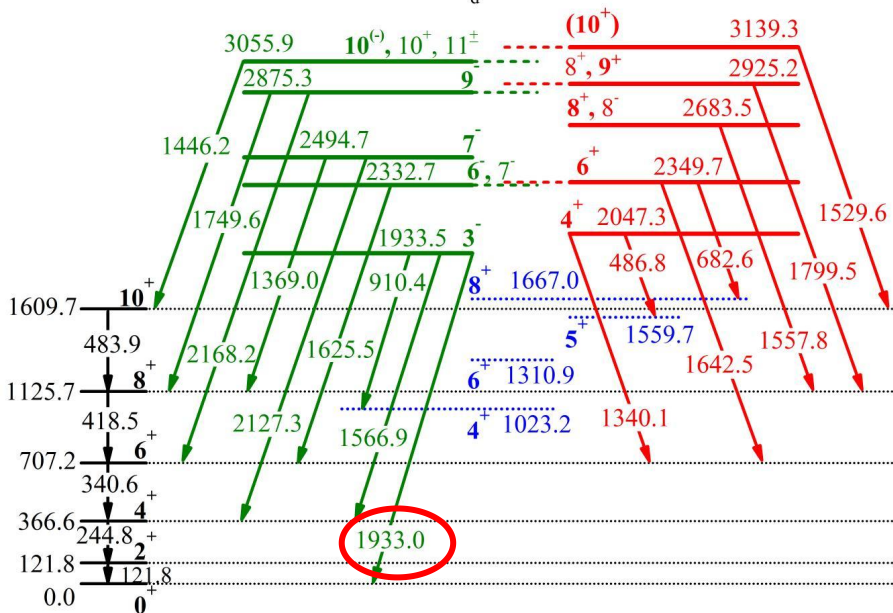
Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

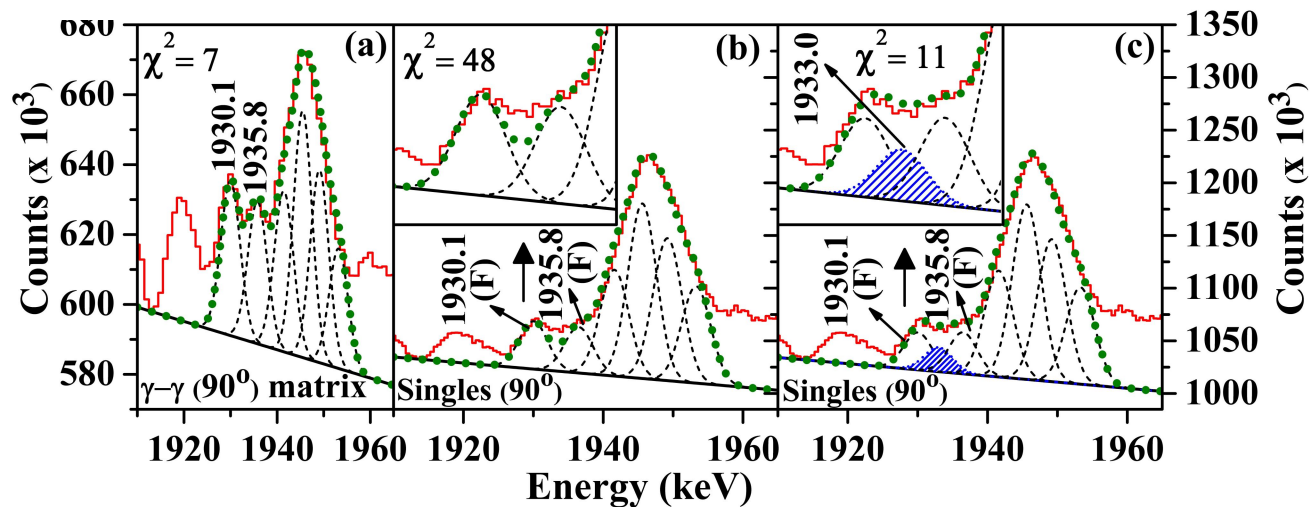
International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

New candidate Tetrahedral sequence in ^{152}Sm

$T_d(2)$ Band



- Fitting singles projection at 90° , we observe a new transition with energy 1933.0(8) keV
- This 1933.0 keV is placed as $3^- \rightarrow 0^+$ decay



Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

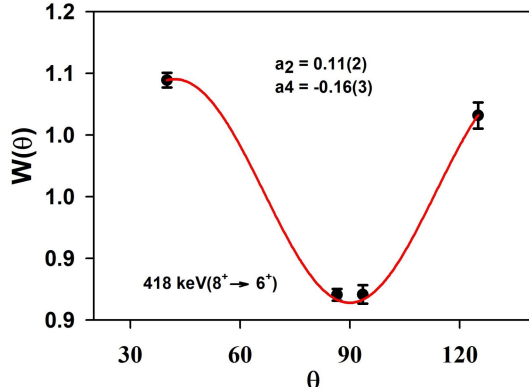
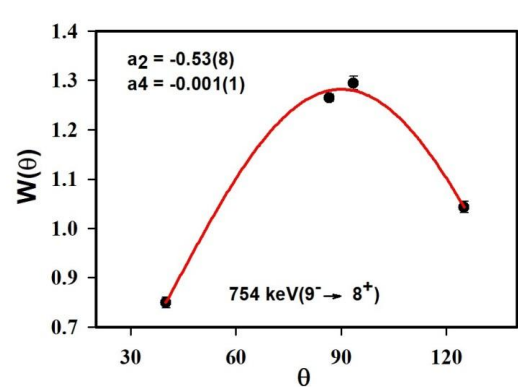
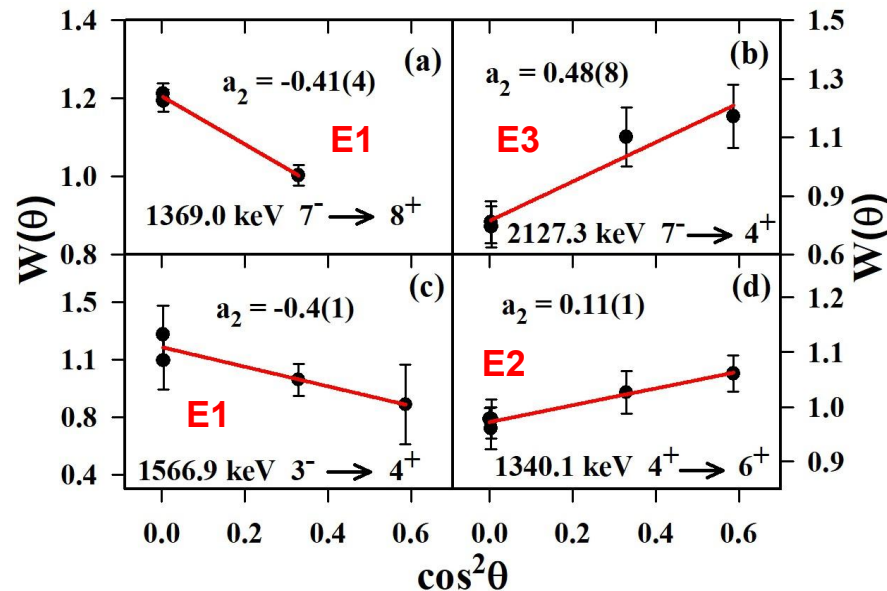
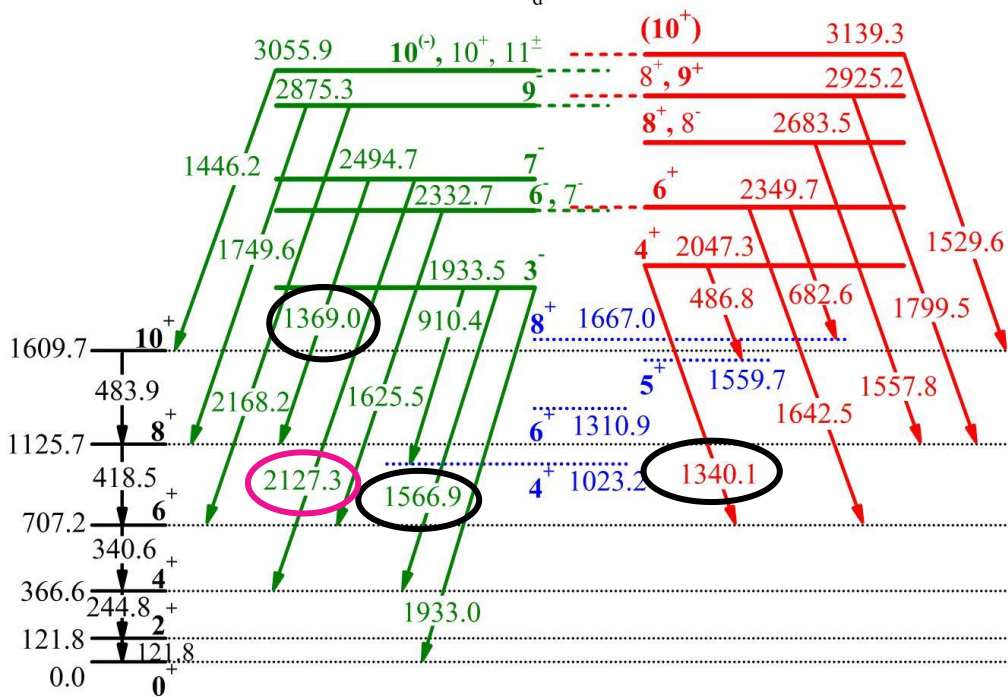
Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

New candidate Tetrahedral sequence in ^{152}Sm

Zs Podolyak, C. M. Shand, E. Wilson, B. A. Brown
 H. Grawe, C. J. Chiara, S. Zhu, B. Fornal
 R. V. F. Janssens, *Jour. Phys. Conf. Ser.* **580**, 01201(2015).

$T_d(2)$ Band



$a_2 = 0.55$ for the pure octupole transition of the $7^- \rightarrow 4^+$ decay

→ calculated from ANCORR code

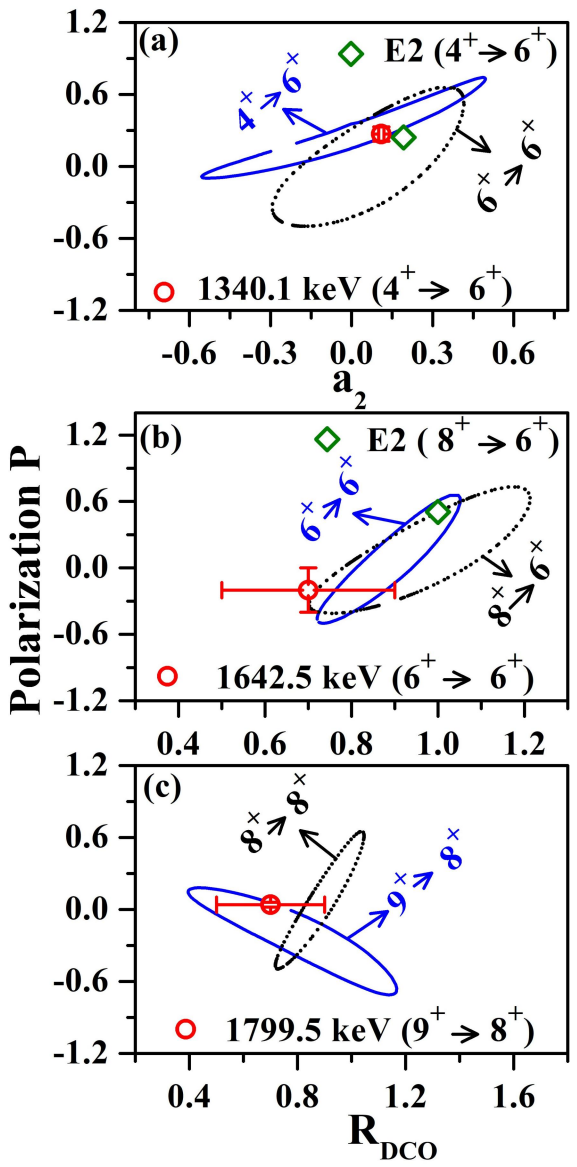
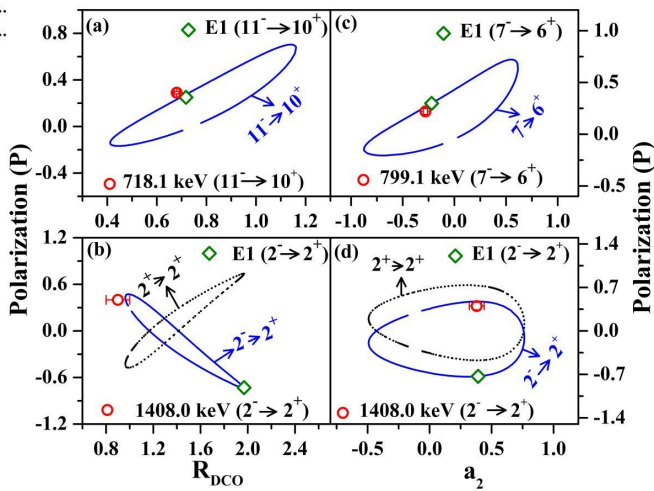
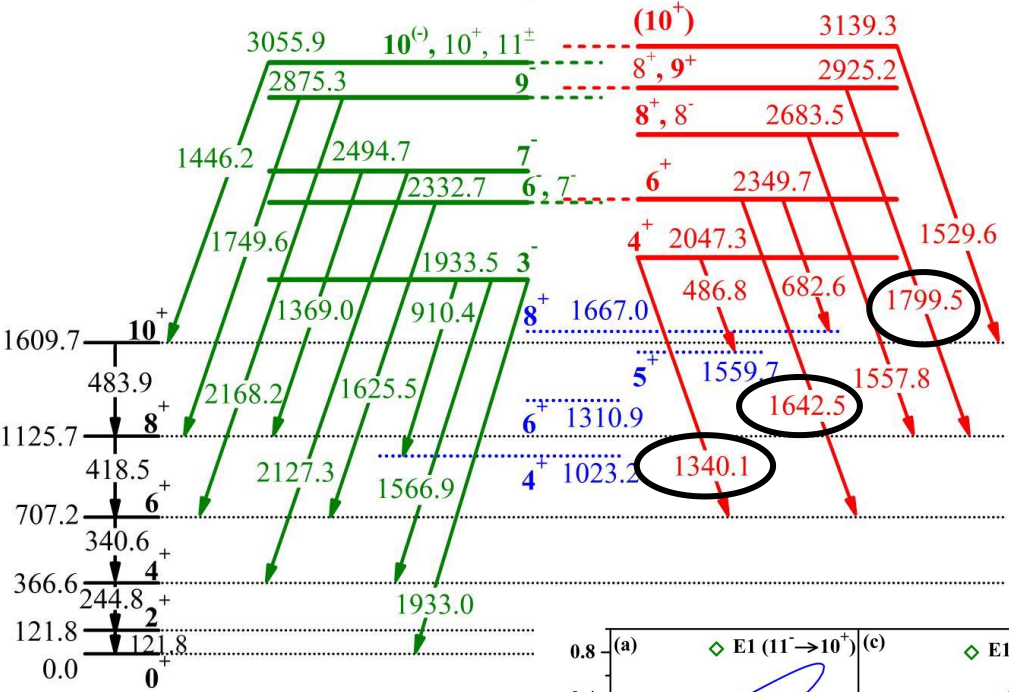
Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
 VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
 IJC Lab, France, November 04th - 08th, 2024

New candidate Tetrahedral sequence in ^{152}Sm

$T_d(2)$ Band



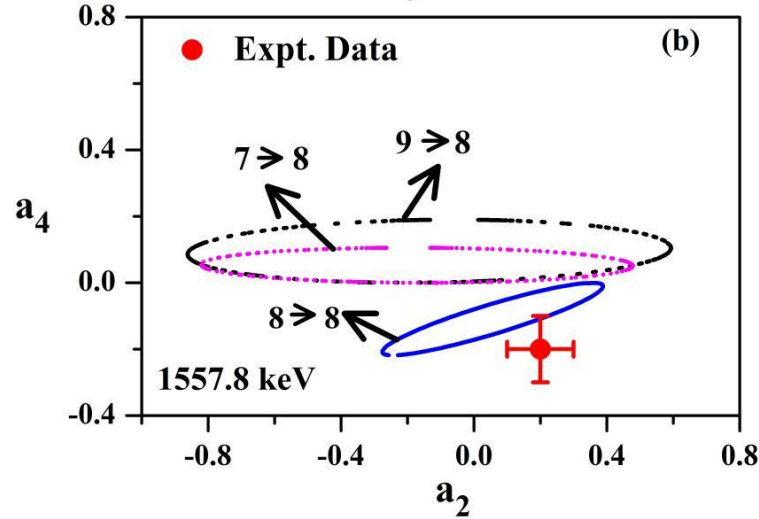
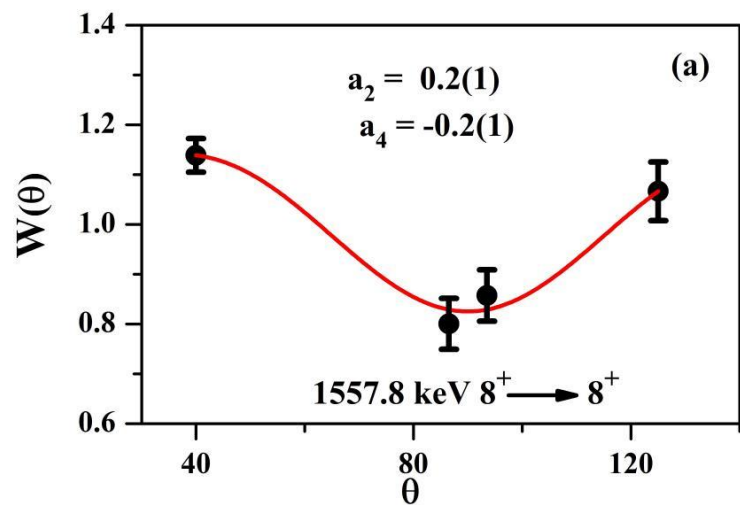
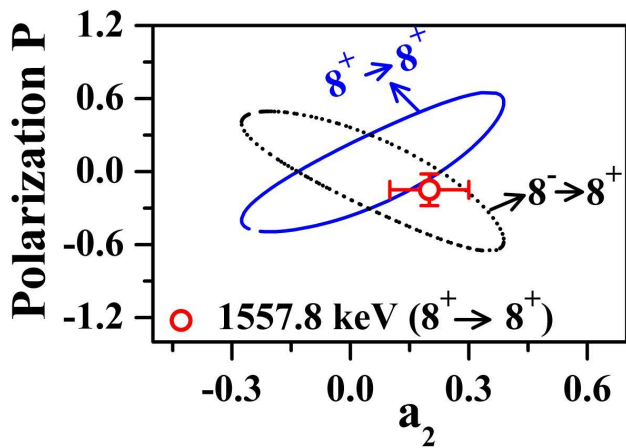
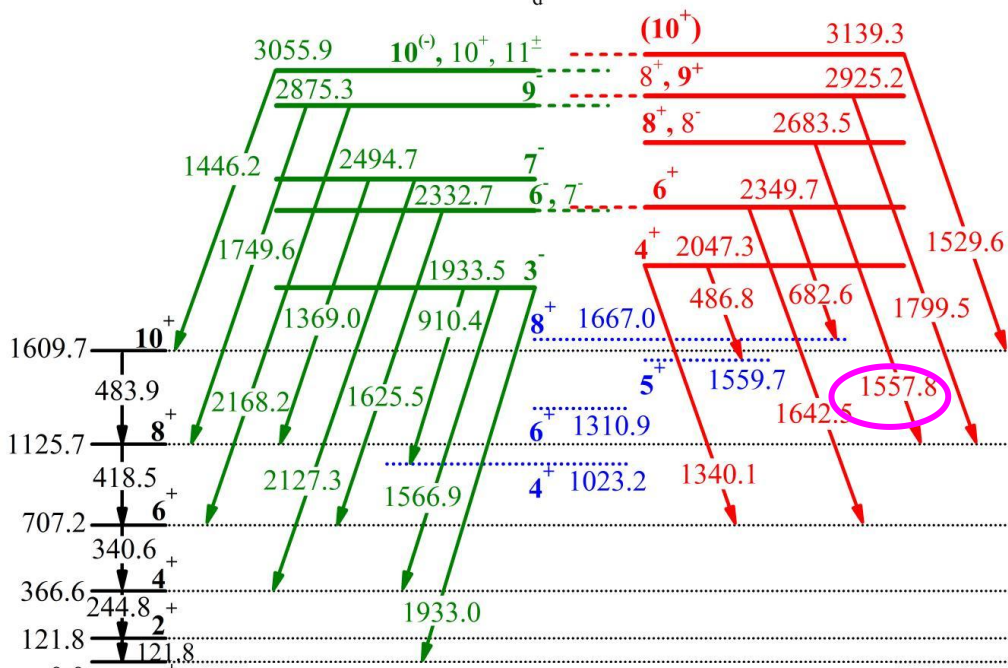
Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

New candidate Tetrahedral sequence in ^{152}Sm

$T_d(2)$ Band

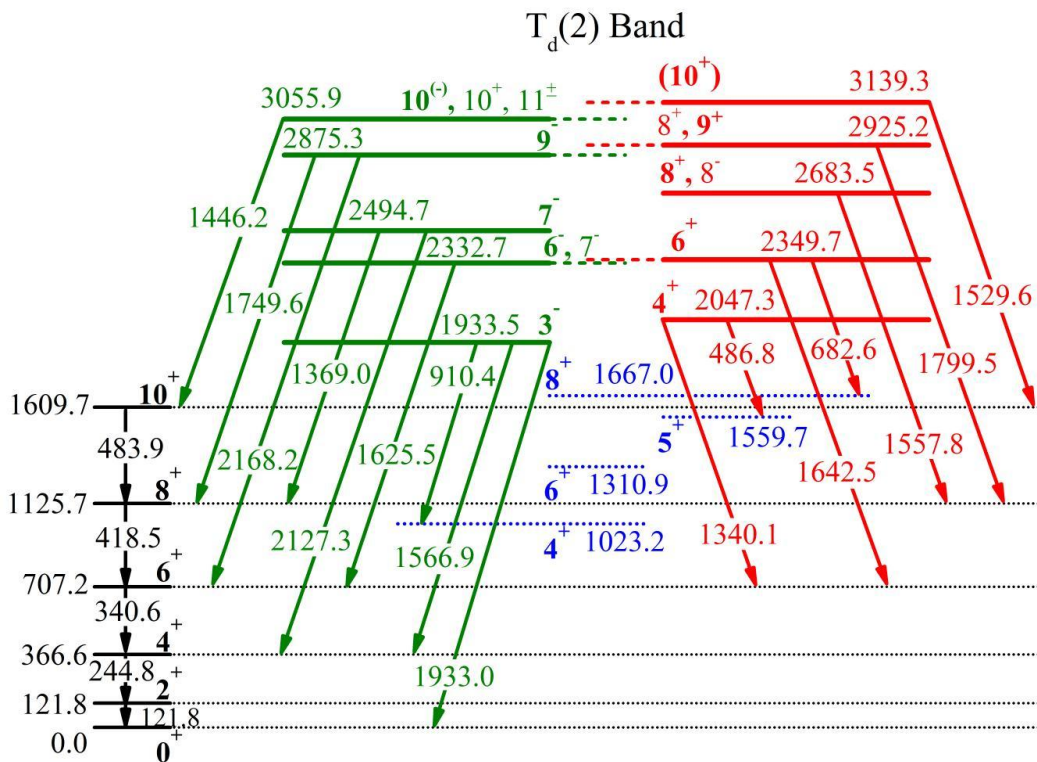


Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee, VECC, Kolkata

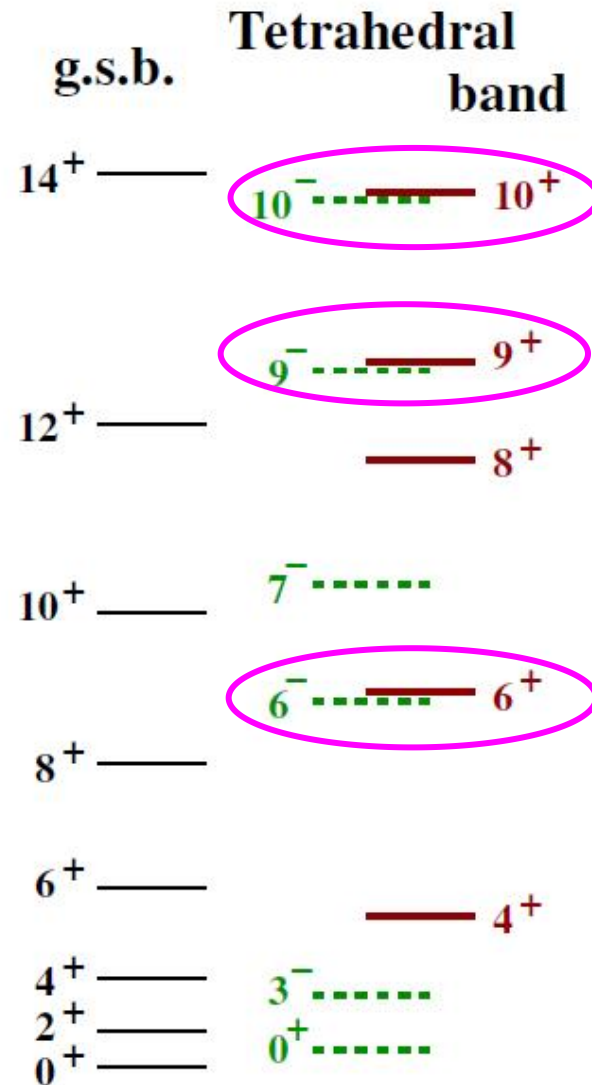
International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024) IJC Lab, France, November 04th - 08th, 2024

New candidate Tetrahedral sequence in ^{152}Sm



Level degeneracy

- Energies of 6^+ , 6^- levels
- Energies of 9^+ , 9^- levels
- Energies of 10^+ , 10^- levels



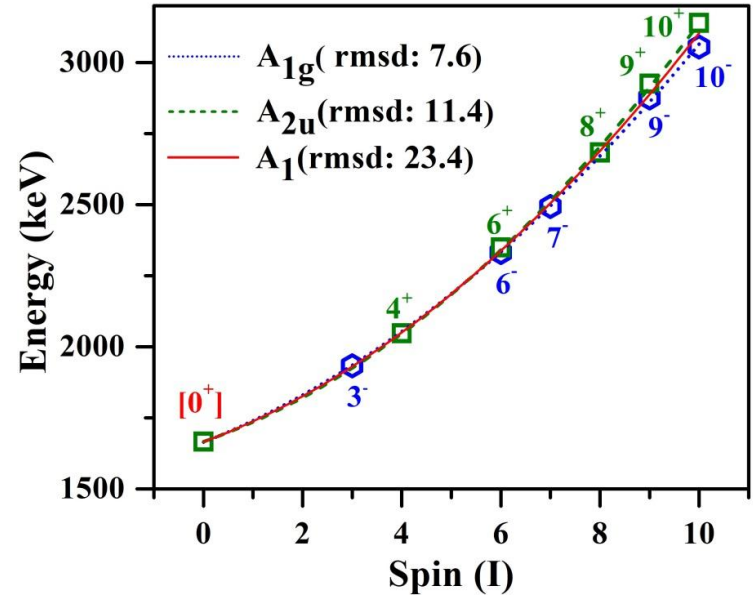
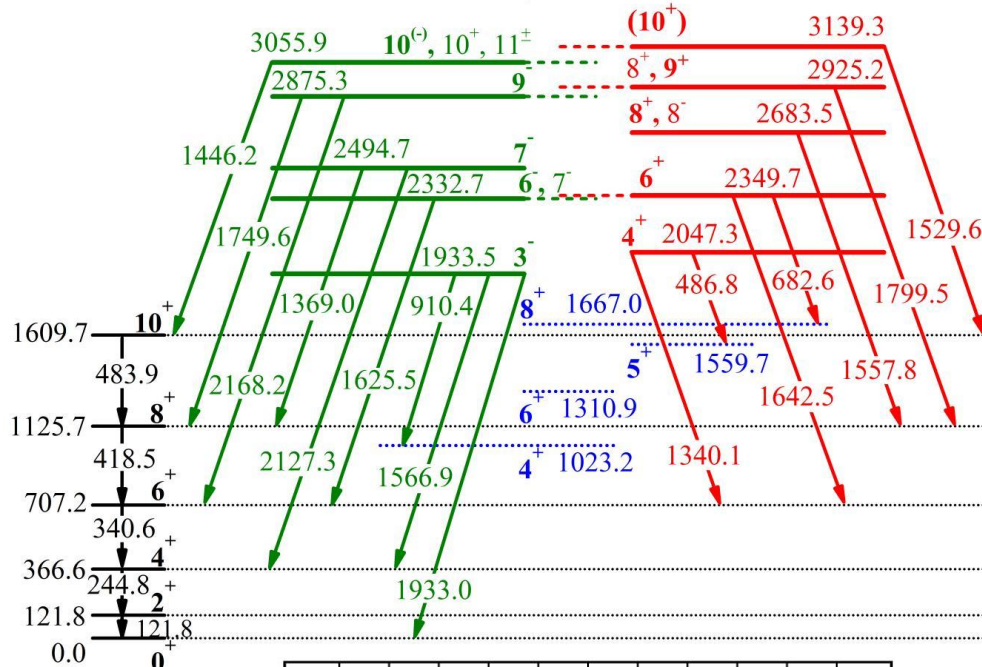
Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

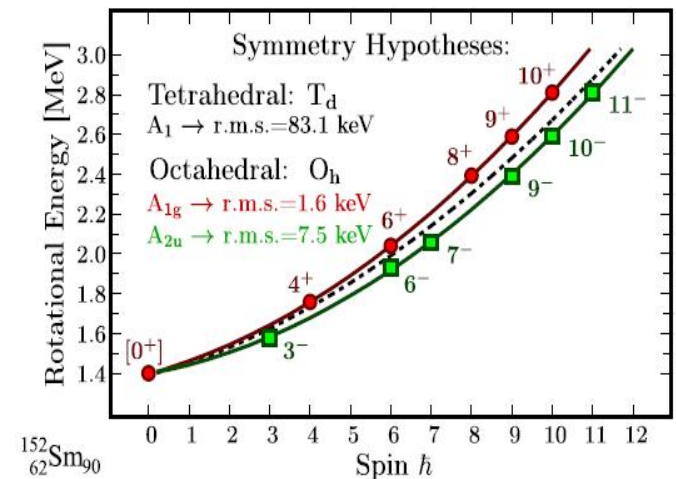
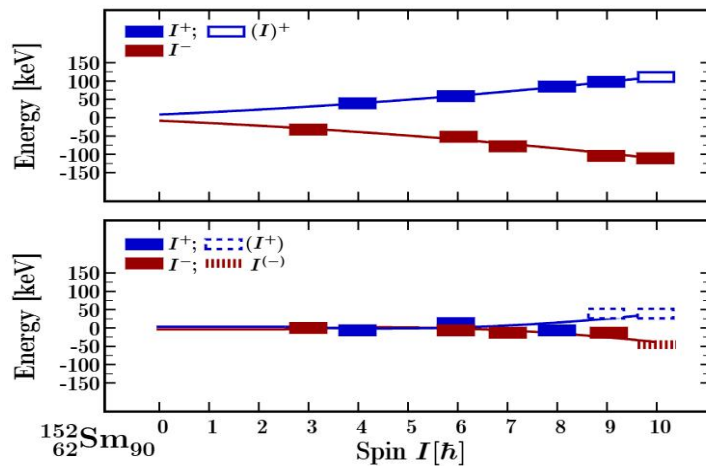
International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

New candidate Tetrahedral sequence in ^{152}Sm

$T_d(2)$ Band



Experimental Results [T_d -vs.- O_h]

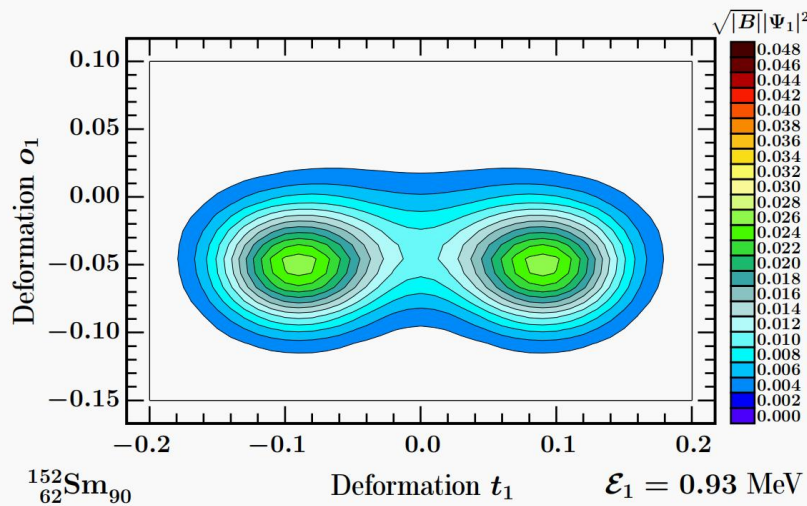


Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

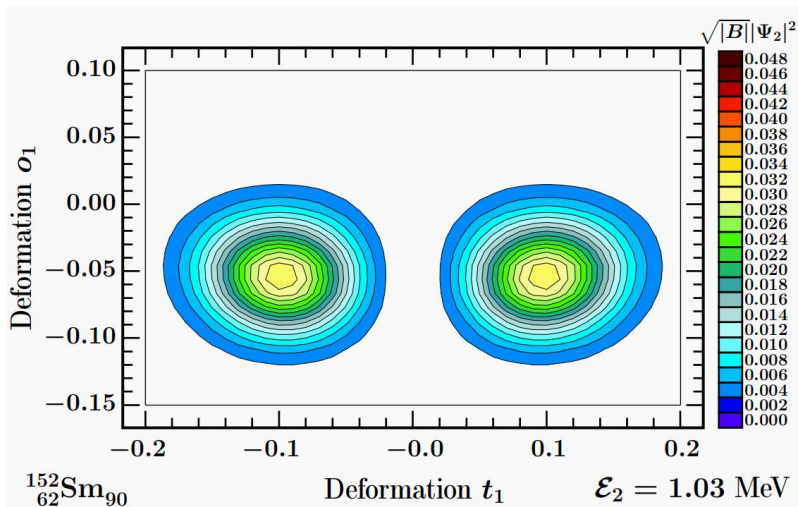
Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

New candidate Tetrahedral sequence in ^{152}Sm



$$q_n^{\text{dyn}} \equiv \sqrt{\langle q_n^2 \rangle}, \quad t_1^{\text{dyn}} \approx 0.09 \quad \text{and} \quad o_1^{\text{dyn}} \approx -0.04$$



J. Dudek, I Dedes et al.,

$$\hat{H}\Psi_i = \mathcal{E}_i\Psi_i,$$

$$\hat{H} = -\frac{\hbar^2}{2}\hat{\Delta} + V(q),$$

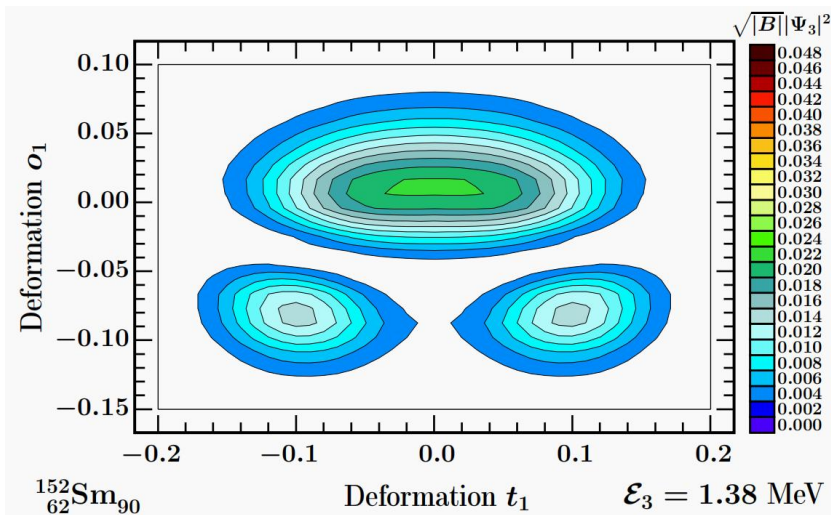
$$\hat{\Delta} = \sum_{m,n=1}^{d=2} \frac{1}{\sqrt{|B|}} \frac{\partial}{\partial q^n} \left(\sqrt{|B|} B^{nm} \frac{\partial}{\partial q^m} \right),$$

- Probability density function for each of the solutions
- Quantum probability of finding the system within a deformation volume dV

$$dP(q) \stackrel{\text{df.}}{=} \Psi_i^*(q)\Psi_i(q)\sqrt{|B|}dV, \quad dV \equiv dq_1dq_2$$

$$\langle q_n^2 \rangle \stackrel{\text{df.}}{=} \int \Psi_i^*(q)q_n^2\Psi_i(q)\sqrt{|B|}dV, \quad dV \equiv dq_1dq_2$$

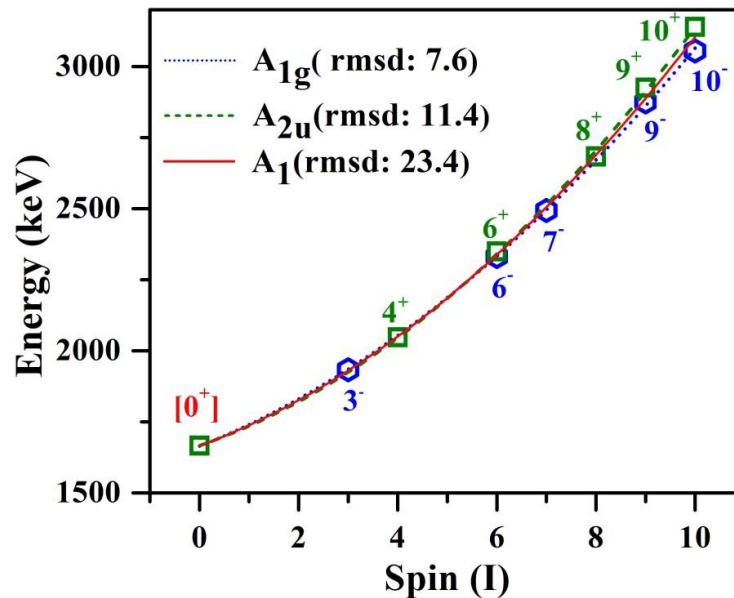
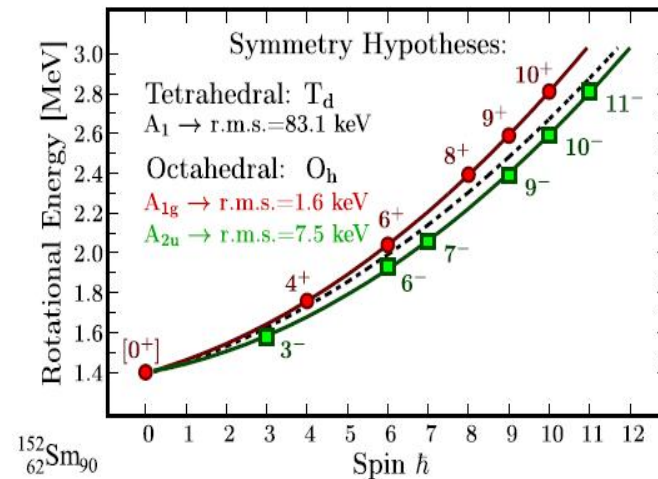
New candidate Tetrahedral sequence in ^{152}Sm



$$t_1^{\text{dyn}} \approx 0.07 \text{ and } o_1^{\text{dyn}} \approx 0$$

New candidate tetrahedral sequence is pure and preserve the octahedral symmetry

Experimental Results [T_d -vs.- O_h]



Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024



Summary

- ^{152}Sm : Rich example of shapes and shape co-existence
- The first tetrahedral candidate band was proposed in 2018
- Second tetrahedral candidate band is identified in the present work
- The new band shows the signature of pure tetrahedral structure retaining the octahedral symmetry
- Both the symmetry breaking compete in ^{152}Sm as found from the theoretical calculations

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

*Tumpa Bhattacharjee,
VECC, Kolkata*

*International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024*

Collaborators



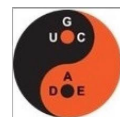
Devesh Kumar, Shefali Basak, Anandagopal Pal, Safikul alam, Arindam Kumar Sikdar, Joydip Nandi, Parnika Das



Abhijit Bisoi, sangeeta Das, Rozina Rahaman, Anik Adhikari, Arkadip Bera, Yajnya Sapkota, Ananya Das



Arunabha Saha



Saradindu Samanta, Suvronil Chatterjee, Rajarshi Raut, Sandeep S. Ghugre



Arnab Bhattacharyya, Priyabrato Das, Ushasi Datta



Manipal University
Jaipur

Sathi Sharma



Jerzy Dudek, Gilbert Duchene, Dominique Curien



J. Yang



Irene Dedes, A. Gaamouci

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

Acknowledgement:

Dr. Sumit Som, Director, VECC, Kolkata

Prof. Jane Alam, Ex Head, Physics Group, VECC, Kolkata

Prof Sukalyan Chattopadhyay, Ex Head Physics Group, SINP, Kolkata

Dr. Sandip Ghugre, Director, UGC-DAE-CSR, Kolkata

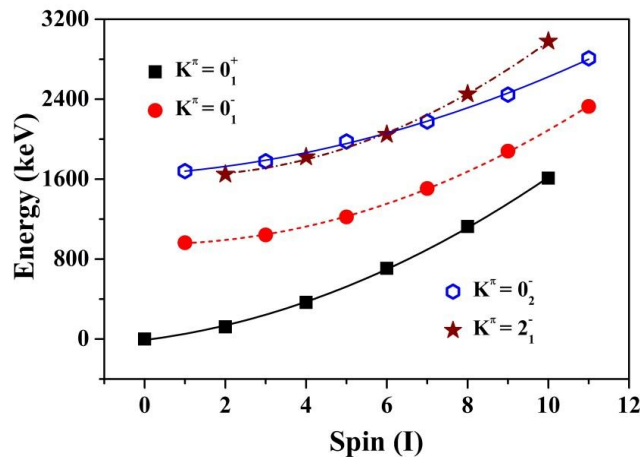
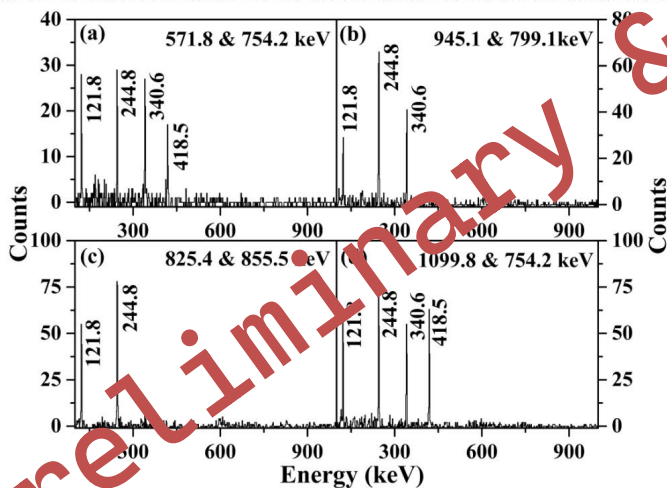
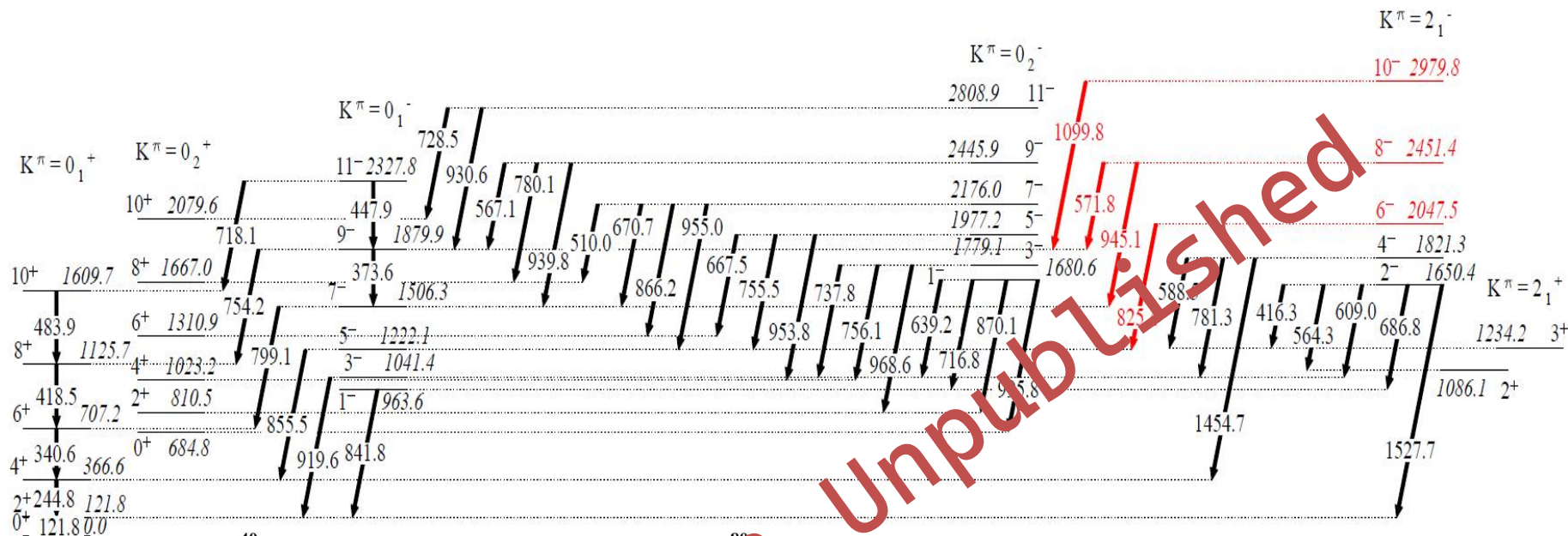
Thank you for your attention!!

Competition between Tetrahedral and Octahedral
Symmetries in ^{152}Sm Nucleus: A New set of data
from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in
Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

Shape Coexistence in ^{152}Sm

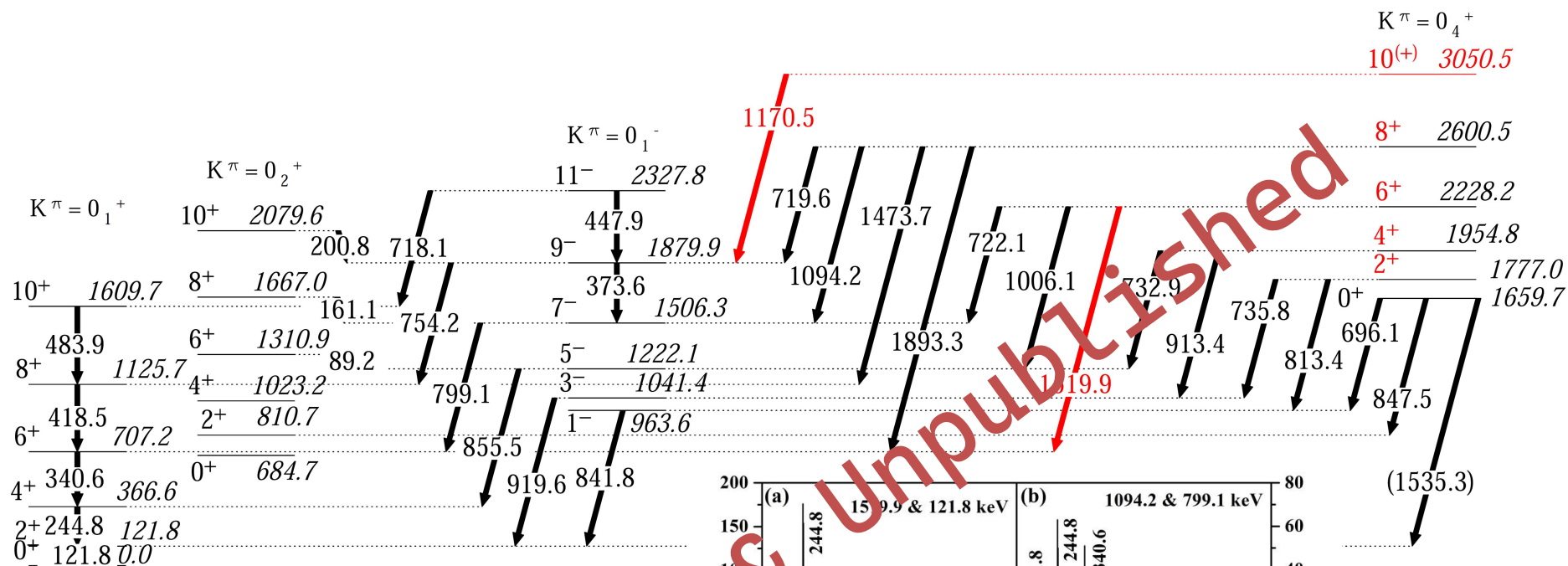


Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

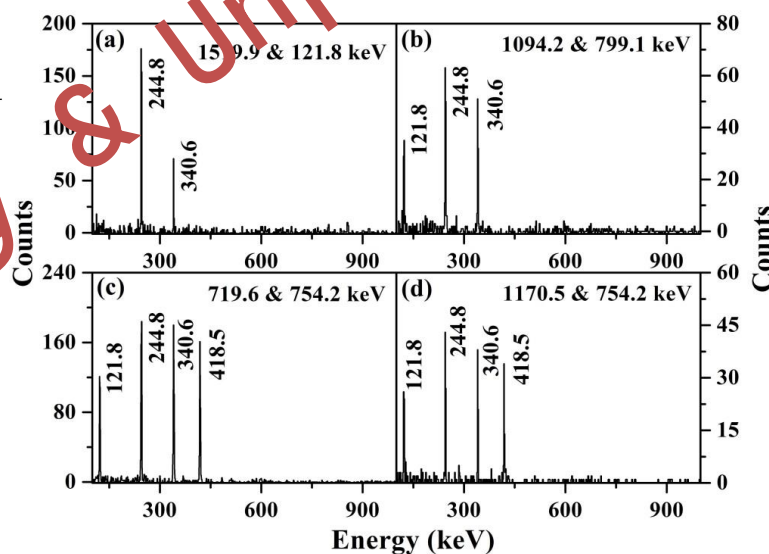
International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

Shape Coexistence in ^{152}Sm



Newly proposed band on 0_4^+ level

Strong decay to the 0_1^- octupole band

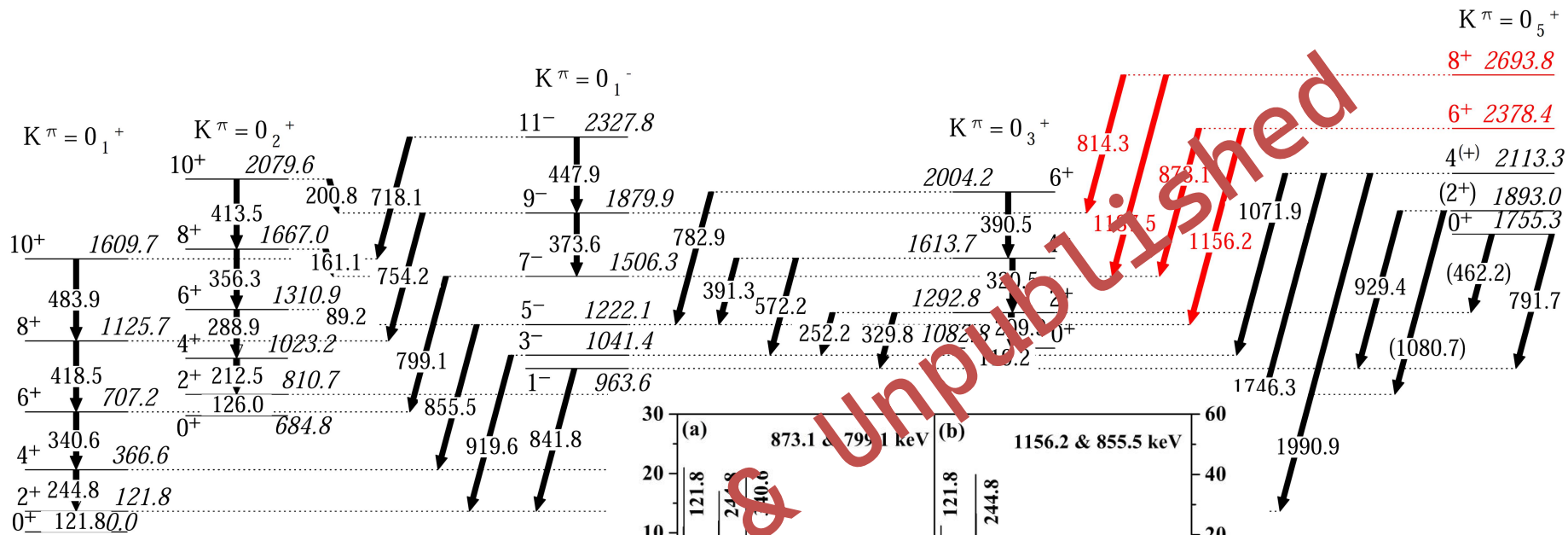


Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

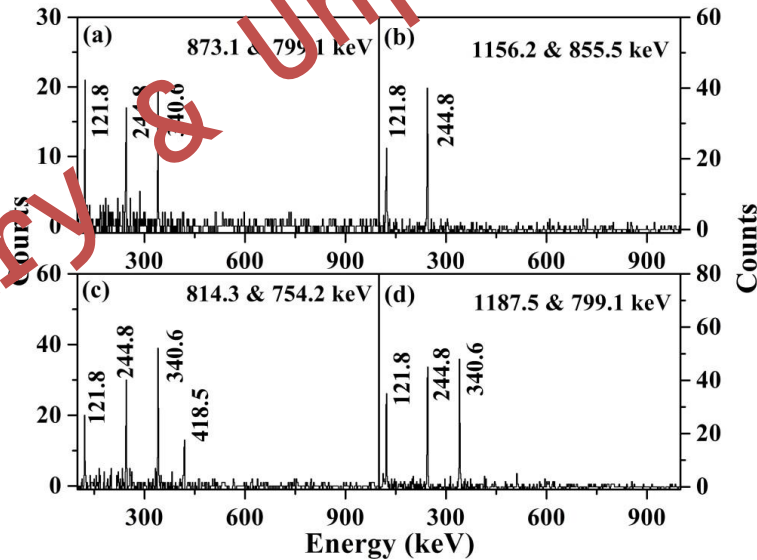
International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

Shape Coexistence in ^{152}Sm



Newly proposed band on 0_5^+ level

Strong decay to the 0_1^- octupole band

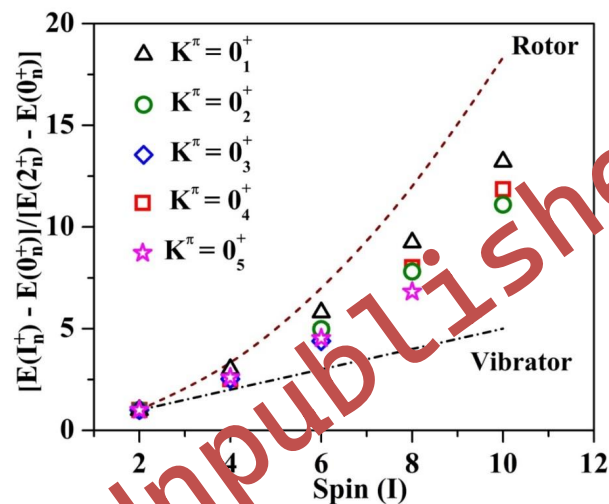
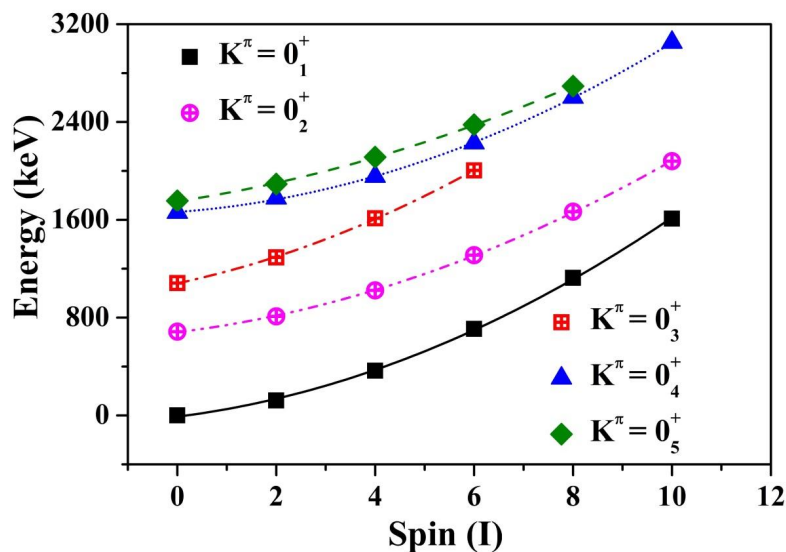


Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

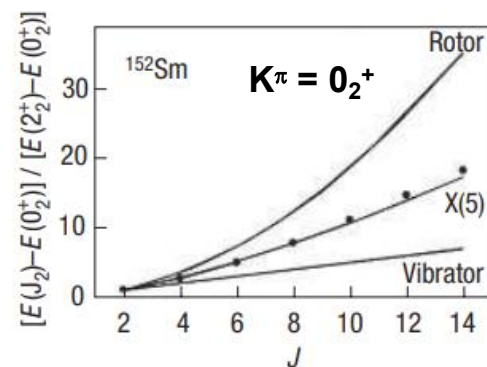
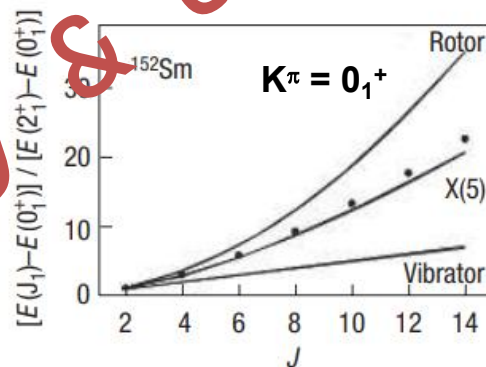
International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

Shape Coexistence in ^{152}Sm



(X5 symmetry)

$N = 90$ ^{152}Sm displays all of quadrupole – quadrupole, quadrupole – octupole, octupole – octupole shape co-existence



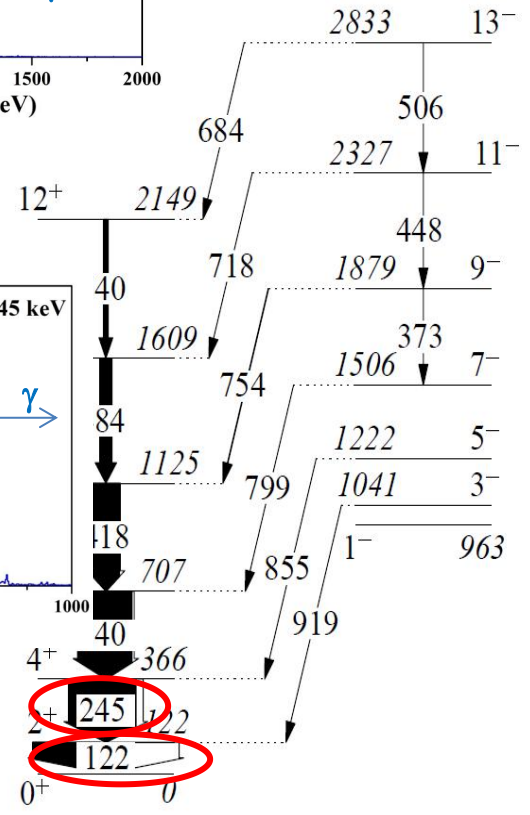
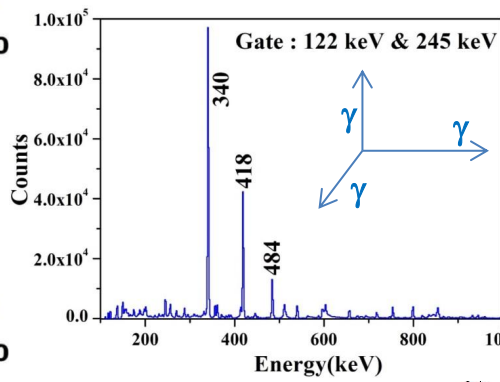
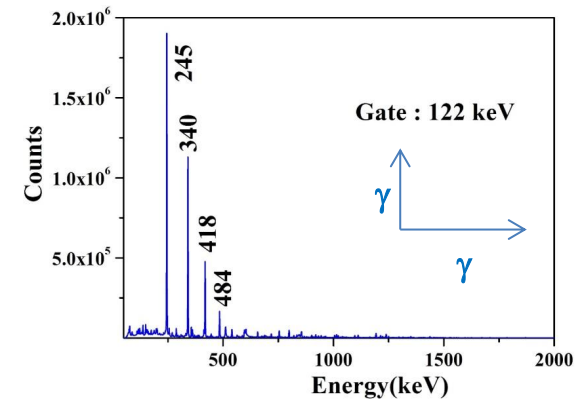
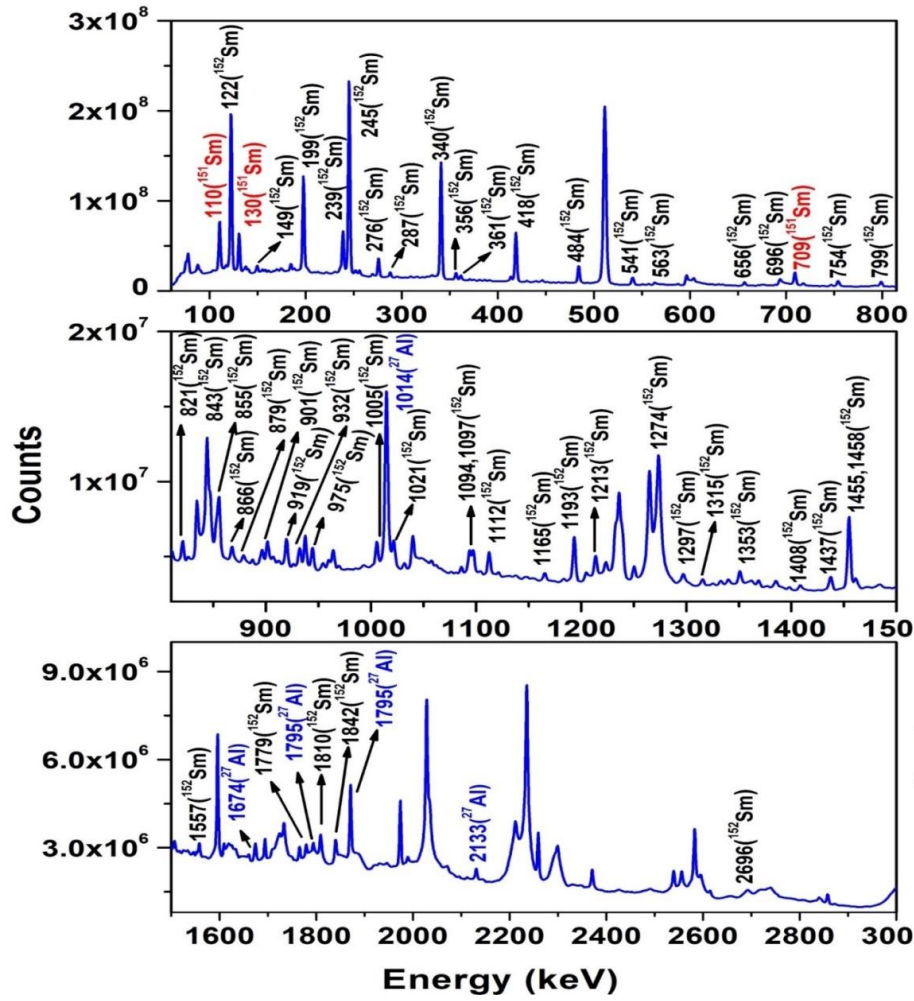
R.F. Casten, *Nature Physics* 2, 811 (2006)

Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei – From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th – 08th, 2024

γ - γ Matrix & γ - γ - γ cube - Development of level scheme

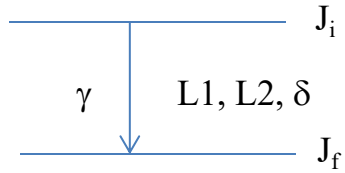


Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

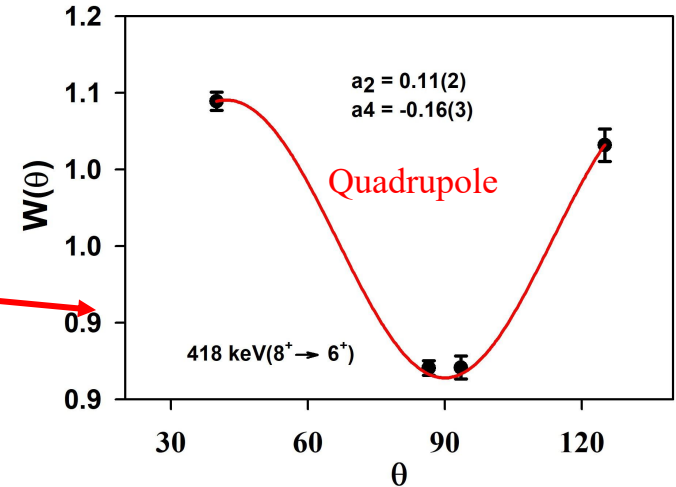
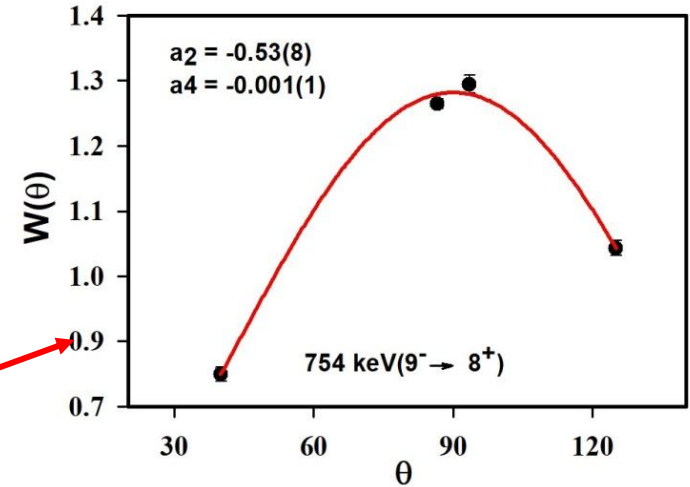
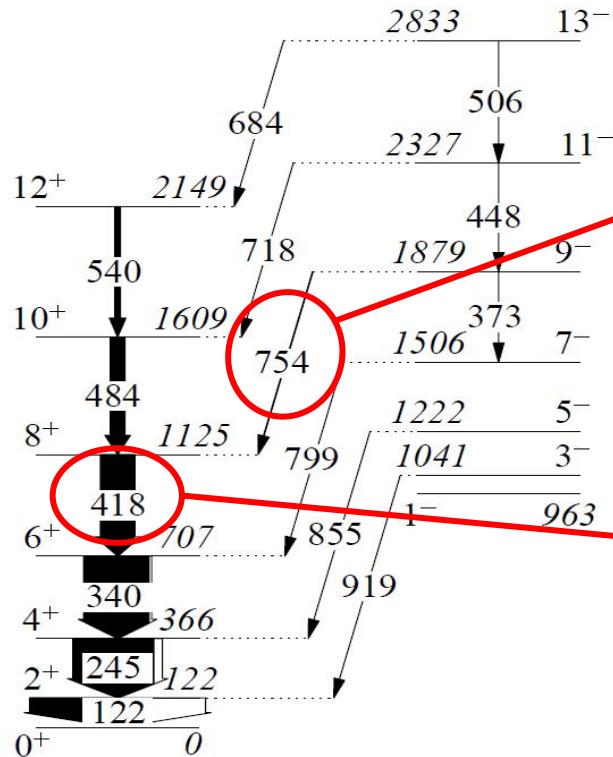
International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

Angular Distribution measurement for determination of Multipolarity



$$W(\theta) = A_0 + A_2P_2(\cos\theta) + A_4P_4(\cos\theta) = A_0[1 + a_2P_2(\cos\theta) + a_4P_4(\cos\theta)]$$

- $\theta: 40^\circ, 86.5^\circ, 93.5^\circ, 125^\circ$
- 86.5° and $93.5^\circ \rightarrow$ from 90° clovers opening angle of the Clover as 7°



Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

DCO Ratio for determination of Multipolarity

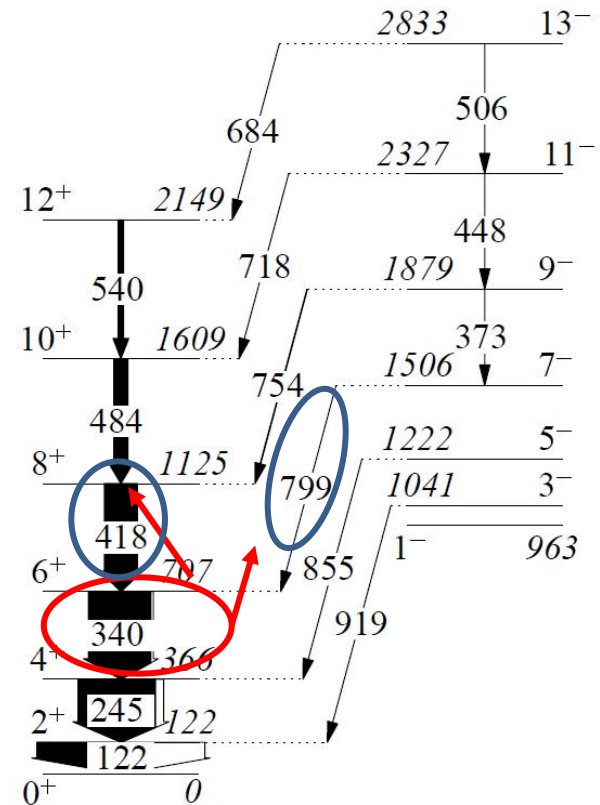
$$\text{DCO}(\gamma_1) = \frac{I_{\gamma_1}(125^\circ), \text{ gated by } \gamma_2 \text{ at } 90^\circ}{I_{\gamma_1}(90^\circ), \text{ gated by } \gamma_2 \text{ at } 125^\circ}$$

For 418 keV transition (E2) : $R_{\text{DCO}} = 0.98(2)$ in Quadrupole gate

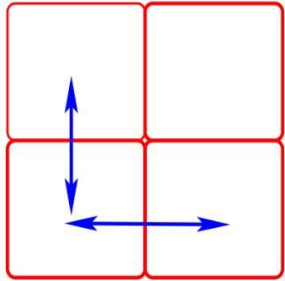
For 799 keV transition (E1) : $R_{\text{DCO}} = 0.67(1)$ in Quadrupole gate

For 251 keV transition (E1) : $R_{\text{DCO}} = 1.1(1)$ in Dipole gate

For 446 keV transition (E2) : $R_{\text{DCO}} = 1.6(2)$ in Dipole gate



Linear Polarization - Determination of Parity



Experimental Method of Linear Polarization Measurement

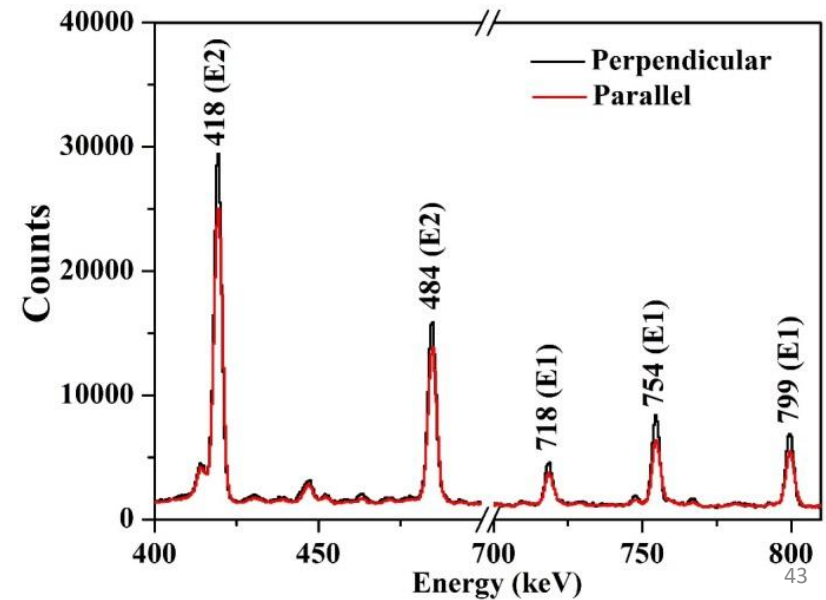
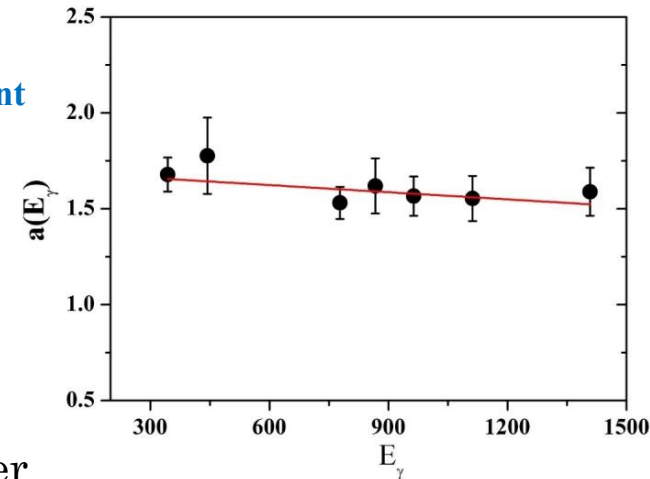
$$P(\theta) = \frac{IPDCO}{Q(E_\gamma)} \quad Q(E_\gamma) = Q_0(a + b \times E_\gamma)$$

$$Q_0 = \frac{(1 + \alpha)}{(1 + \alpha + \alpha^2)} \quad \text{with } \alpha = \frac{E_\gamma \text{ (keV)}}{511}$$

Q_0 = polarization sensitivity for the ideal Compton polarimeter

$$IPDCO = \frac{a(E_\gamma)N_\perp - N_\parallel}{a(E_\gamma)N_\perp + N_\parallel} \quad a(E_\gamma) = \frac{N_\parallel}{N_\perp}$$

- +ve → Electric Transition
- -ve → Magnetic Transition
- 0 → Mixed Transition

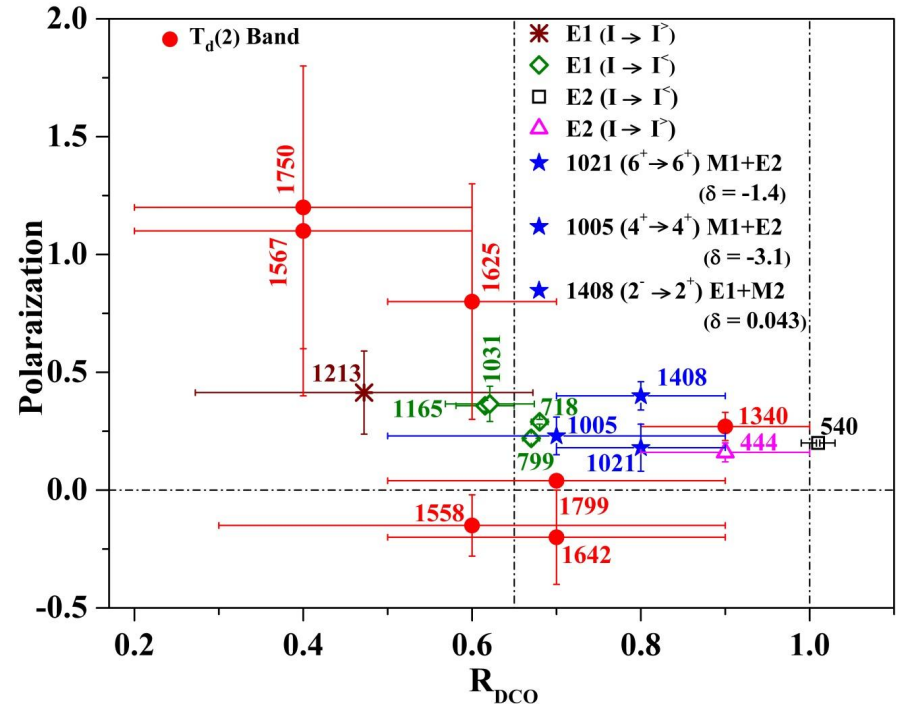
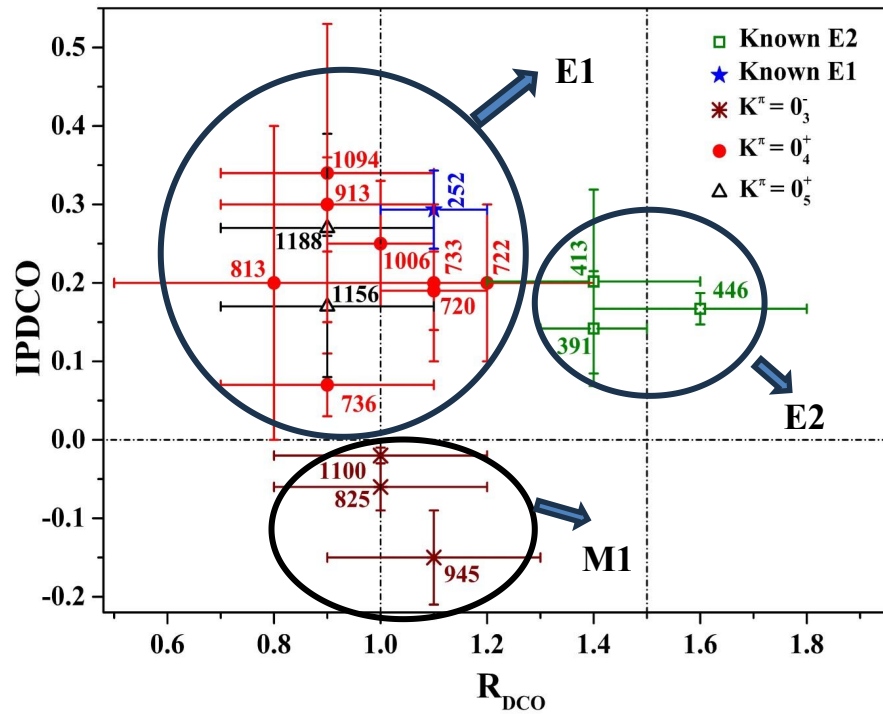


Competition between Tetrahedral and Octahedral Symmetries in ¹⁵²Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

R_{DCO} & IPDCO values in ^{152}Sm

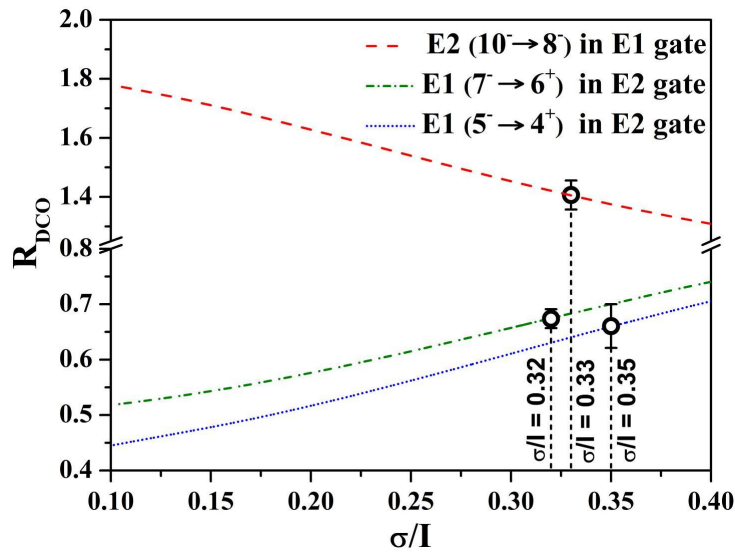


Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

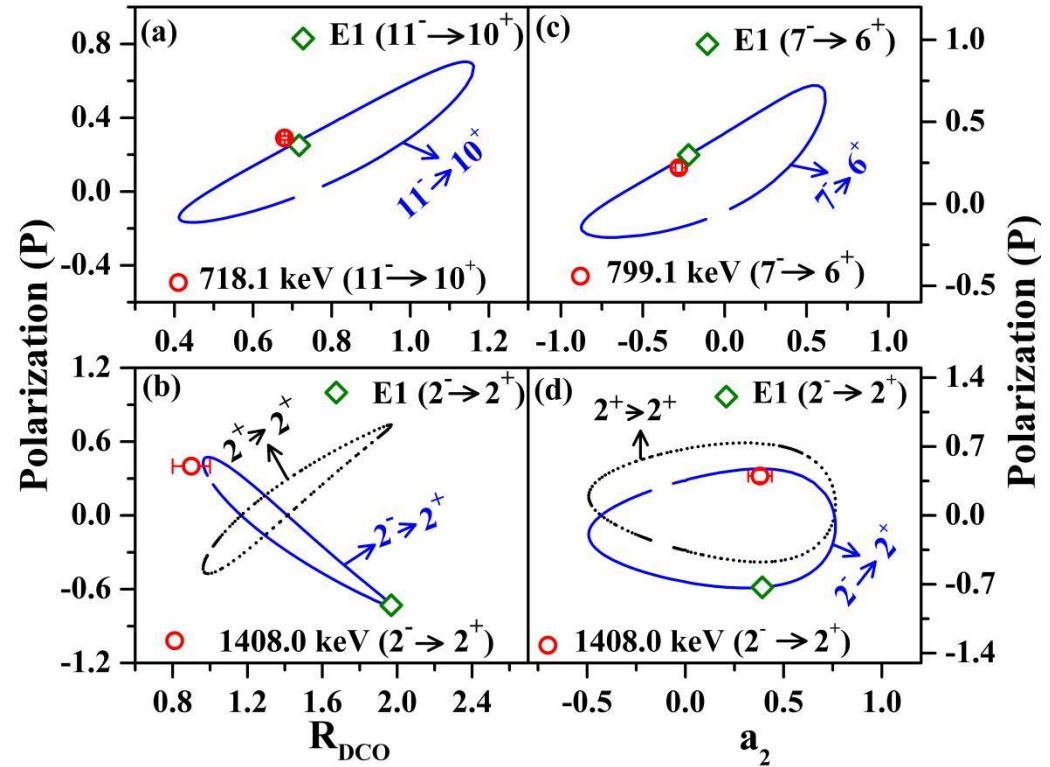
Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024

Calculation of angular distribution coefficients, DCO Ratio and Polarization



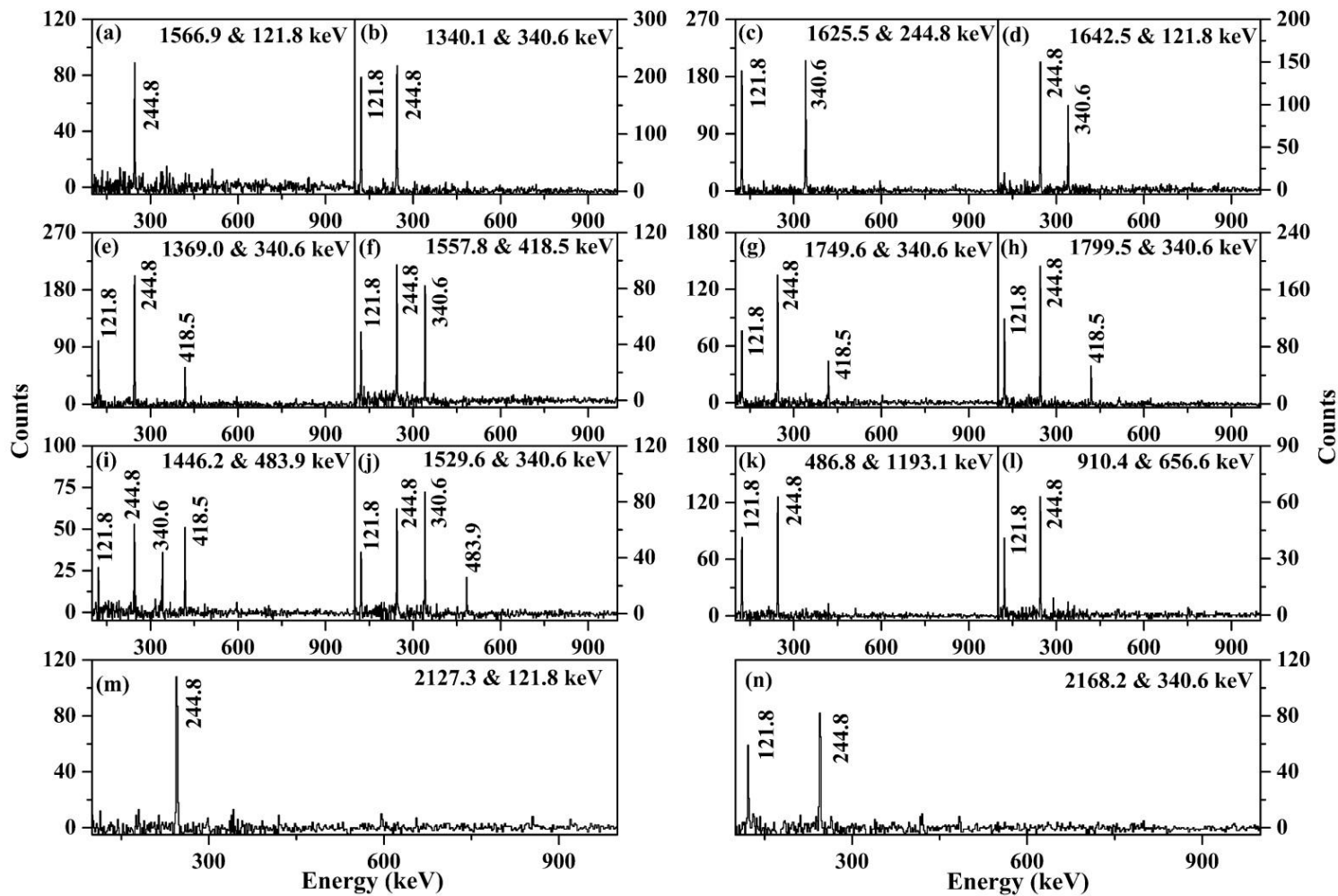
$\sigma/J = 0.33$

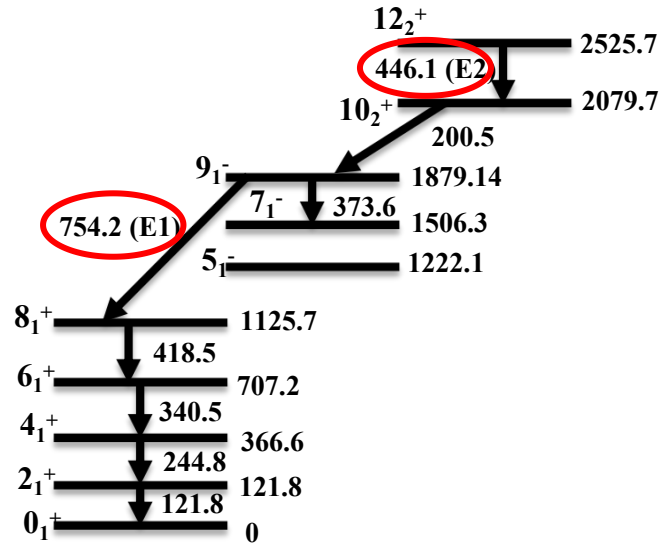
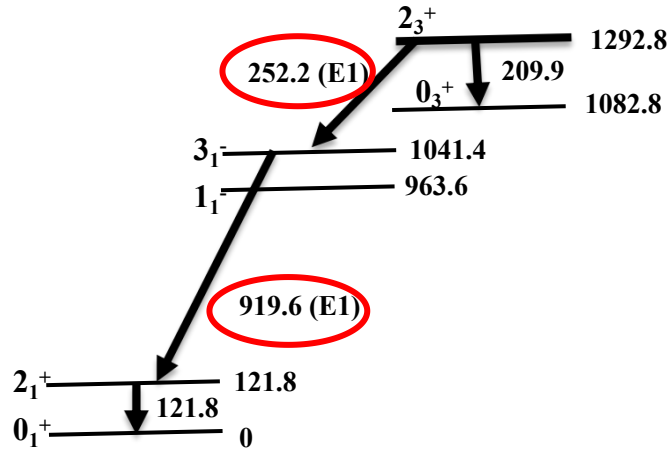


Competition between Tetrahedral and Octahedral Symmetries in ^{152}Sm Nucleus: A New set of data from a dedicated experiment

Tumpa Bhattacharjee,
VECC, Kolkata

International Conference on Shapes and Symmetries in Nuclei - From Experiment to Theory (SSNET -2024)
IJC Lab, France, November 04th - 08th, 2024





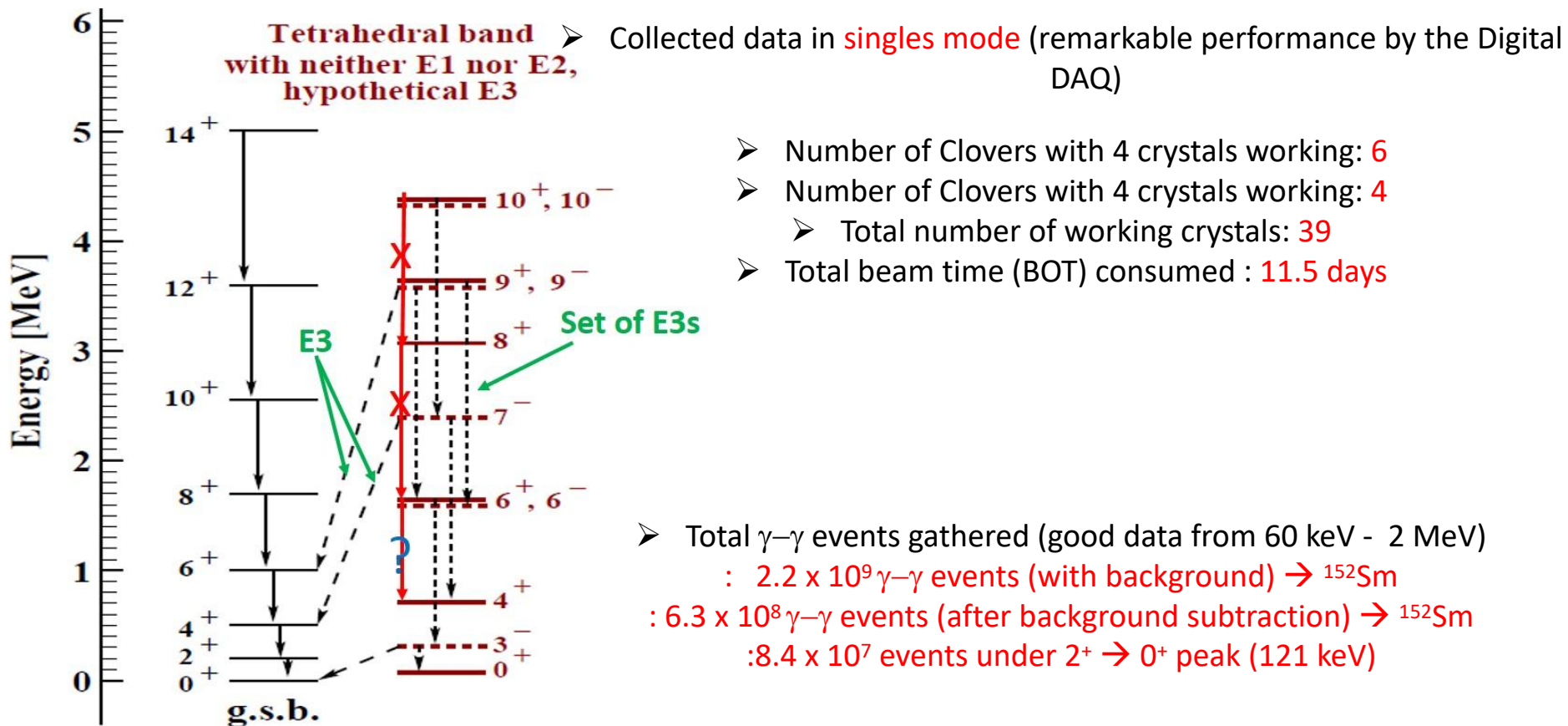


Thank You

Array Configuration

$$P(\theta) = (\pm) \frac{\sum_{\nu} a_{\nu} \kappa(l, l') P_{\nu}^2(\cos\theta)}{1 + \sum_{\nu} a_{\nu} P_{\nu}(\cos\theta)}.$$

Nuclear Structure @ Tetrahedral Shape



Gain drift \rightarrow 80 sets of list files to be sorted \rightarrow 76 matrices with pixisort [S. Das et al., NIMA **893**, 138(2018)] that were added to generate the matrix