

# Shell evolution near and beyond the neutron dripline

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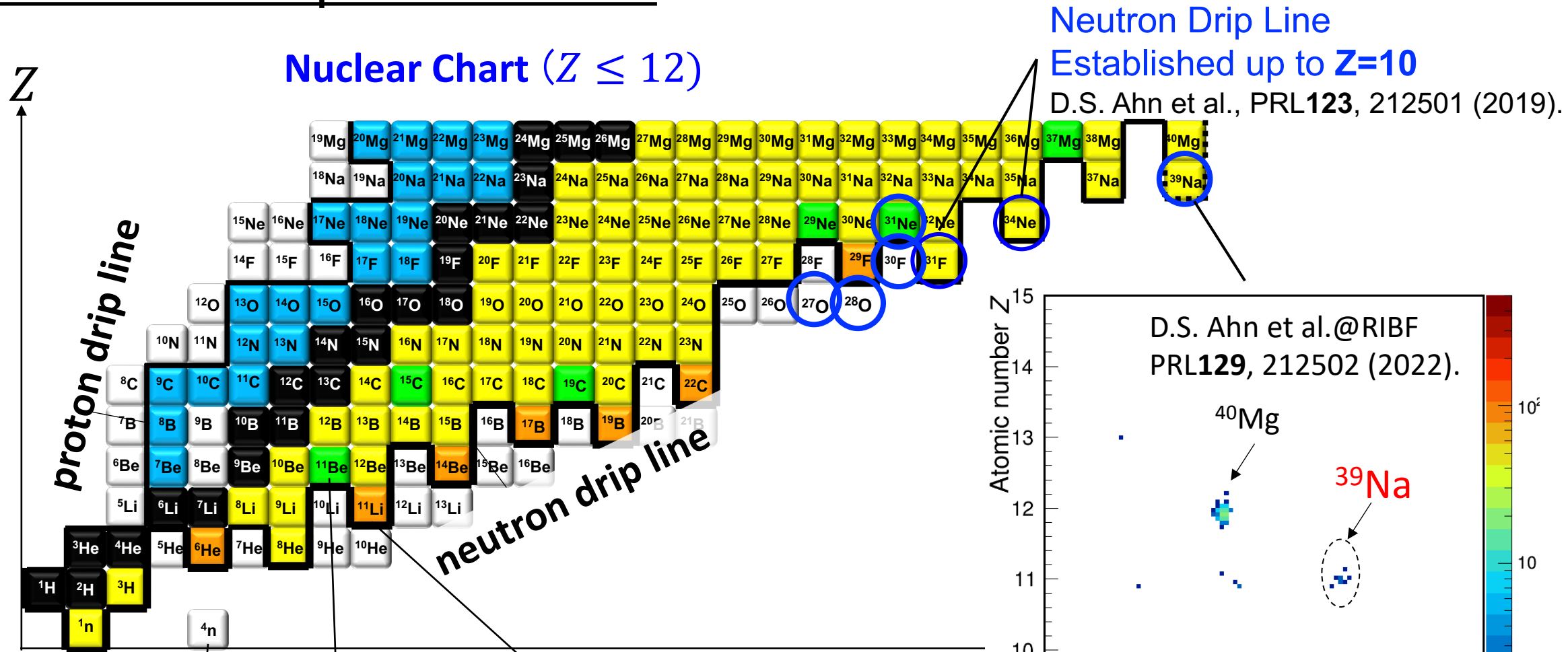
SSNET'2024

Int. Conf. on Shapes and Symmetries in Nuclei:

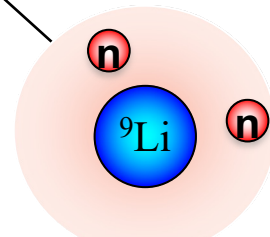
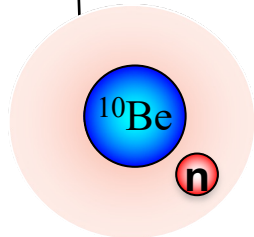
from Experiment to Theory, IJC Lab Orsay, 4-8 Nov 2024

- Introduction : Nuclear landscape at the limit
- Observation of  $^{28}\text{O}$  ( $Z=8$ ,  $N=20$ : doubly magic candidate)
- Observation of  $^{30}\text{F}$  ( $Z=9$ ,  $N=21$ )
- Halo-Shell/Shape Interplay— $^{31}\text{Ne}$  ( $Z=10$ ,  $N=21$ )
  - Exclusive Coulomb breakup and double-component halo in  $^{31}\text{Ne}$
- Summary and Perspectives

# Nuclear Landscape at the limit



Tetra  
neutron

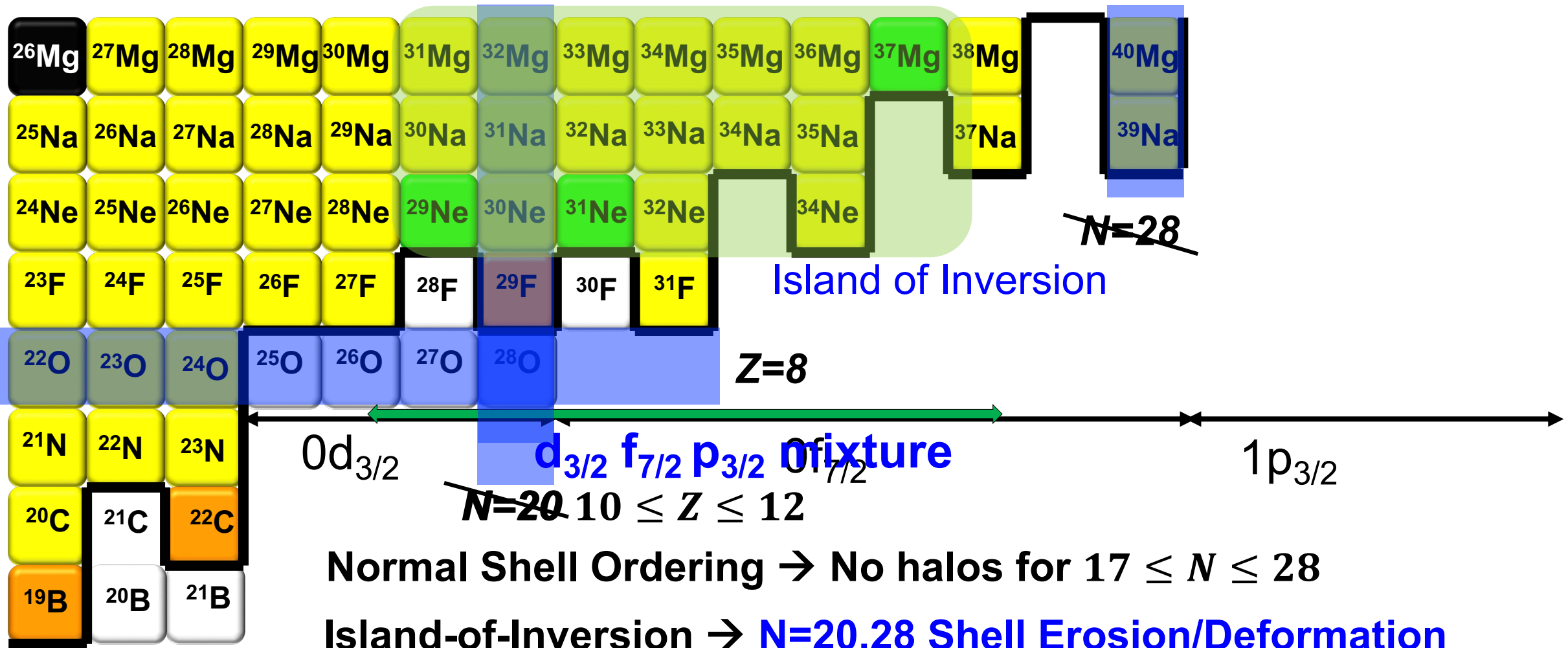


M.Duer et al.  
Nature **606**, 678 (2022).  
@SAMURAI-RIBF

$^{11}\text{Be}$  (1n halo)

$^{11}\text{Li}$  (2n halo, Borromean)

# Shell Evolution At the Edge of Nuclear Landscape?



Bagchi PRL2020, Kobayashi PRC2016, Nakamura PRL2009, PRL2014, Kobayashi PRL2014

$\rightarrow$  Is  $^{28}\text{O}$  doubly magic?

# Key Question on the neutron dripline nuclei

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- What are the interplay between the **Shell evolution, Shape evolution, and the Phenomena due to proximity to the Neutron Drip-line?**

Weakly Bound : Halos

Weakly Unbound: Resonances

# Observation of $^{28}\text{O}$ and $^{27}\text{O}$

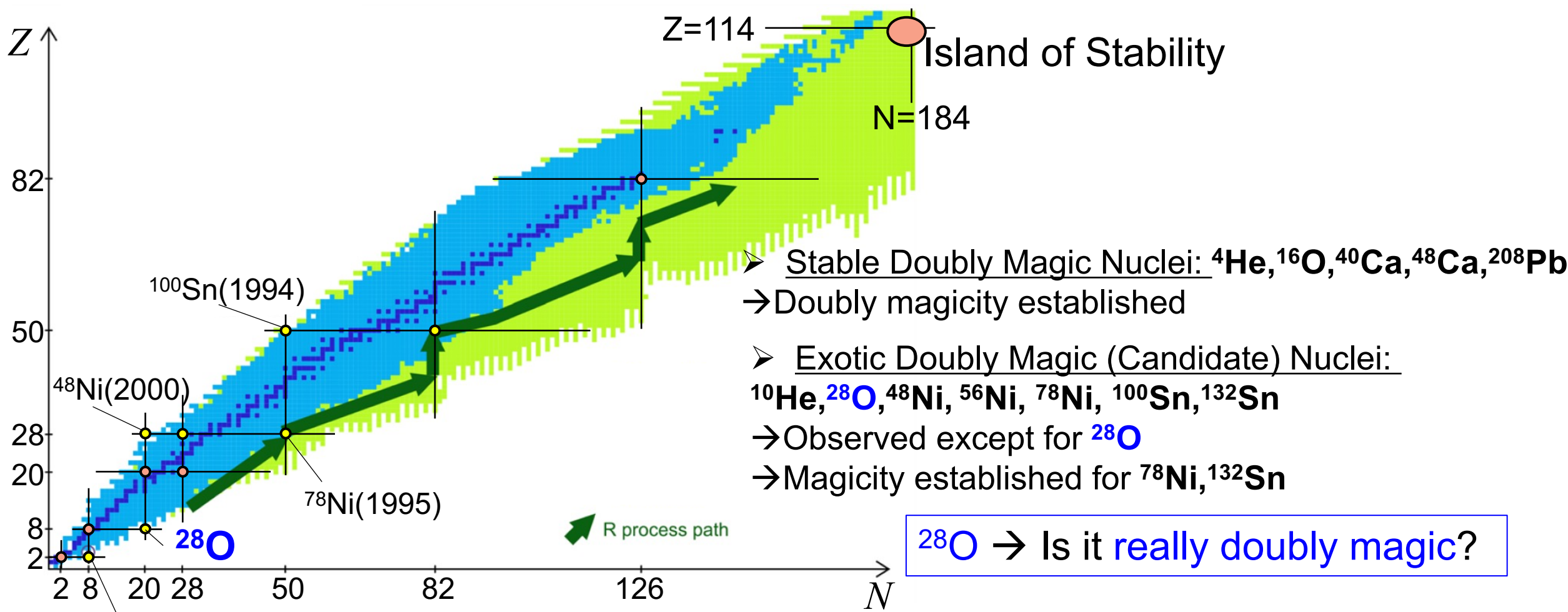
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Y.Kondo et al., Nature **620**, 965-970 (2023).



Yosuke Kondo

# Why $^{28}\text{O}$ ? -- Doubly Magic Nuclei by Mayer-Jensens view



- Stable Doubly Magic Nuclei:  $^4\text{He}, ^{16}\text{O}, ^{40}\text{Ca}, ^{48}\text{Ca}, ^{208}\text{Pb}$   
 → Doubly magicity established
- Exotic Doubly Magic (Candidate) Nuclei:  
 $^{10}\text{He}, ^{28}\text{O}, ^{48}\text{Ni}, ^{56}\text{Ni}, ^{78}\text{Ni}, ^{100}\text{Sn}, ^{132}\text{Sn}$   
 → Observed except for  $^{28}\text{O}$   
 → Magicity established for  $^{78}\text{Ni}, ^{132}\text{Sn}$

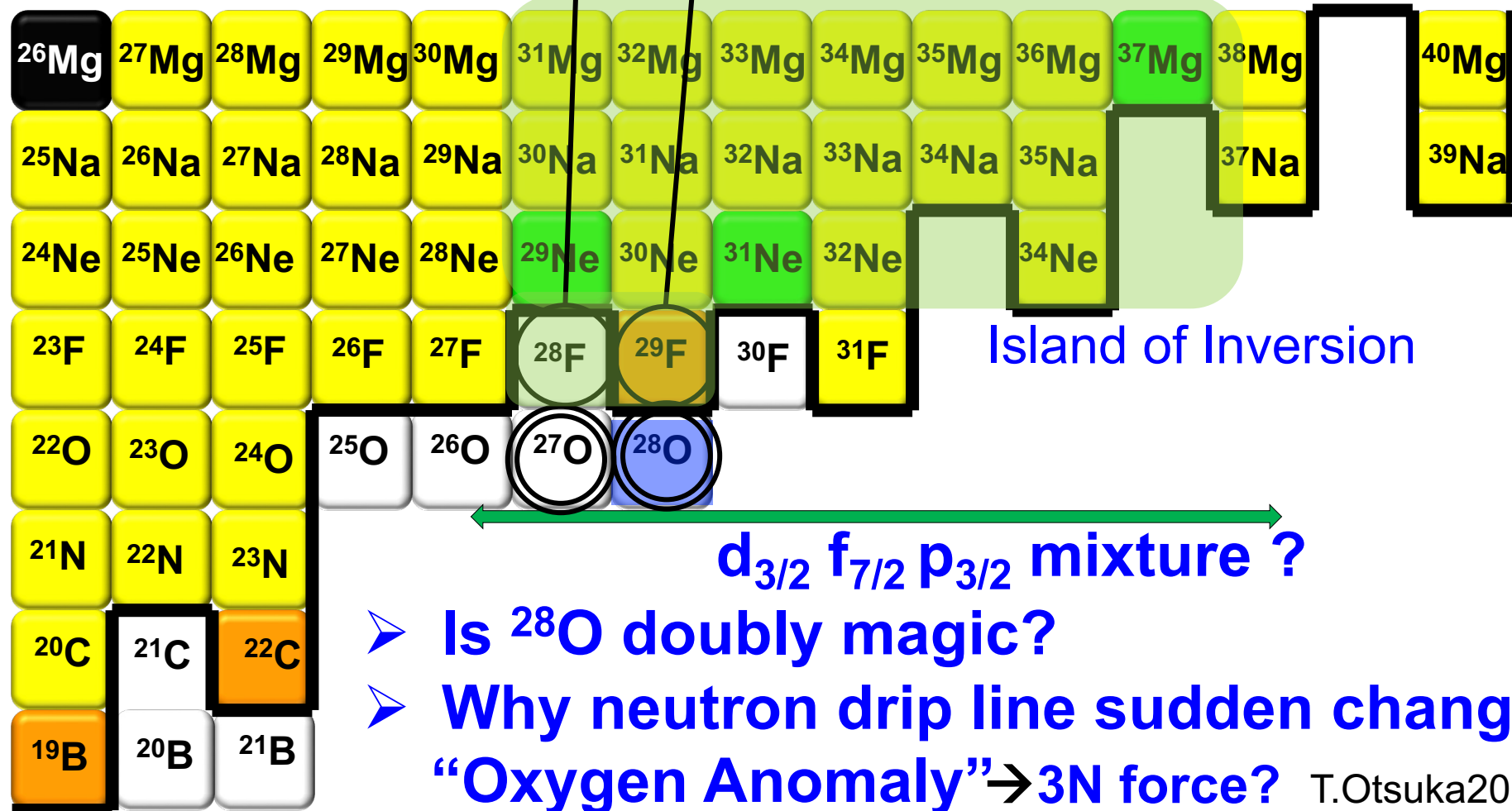
(modified from) T.Otsuka et al., Rev. Mod. Phys. 92, 015002 (2020).

# Shell Evolution At the Edge of Nuclear Chart?

$^{28}\text{F}$ : A.Revel, PRL124, 152502(2020) p-wave ground state

$^{29}\text{F}$ : S. Bagchi et al., PRL124, 222504, (2020): p-wave 2n halo

P. Doornenbal, et al., PRC95, 041301(R), (2017): N=20 magicity lost



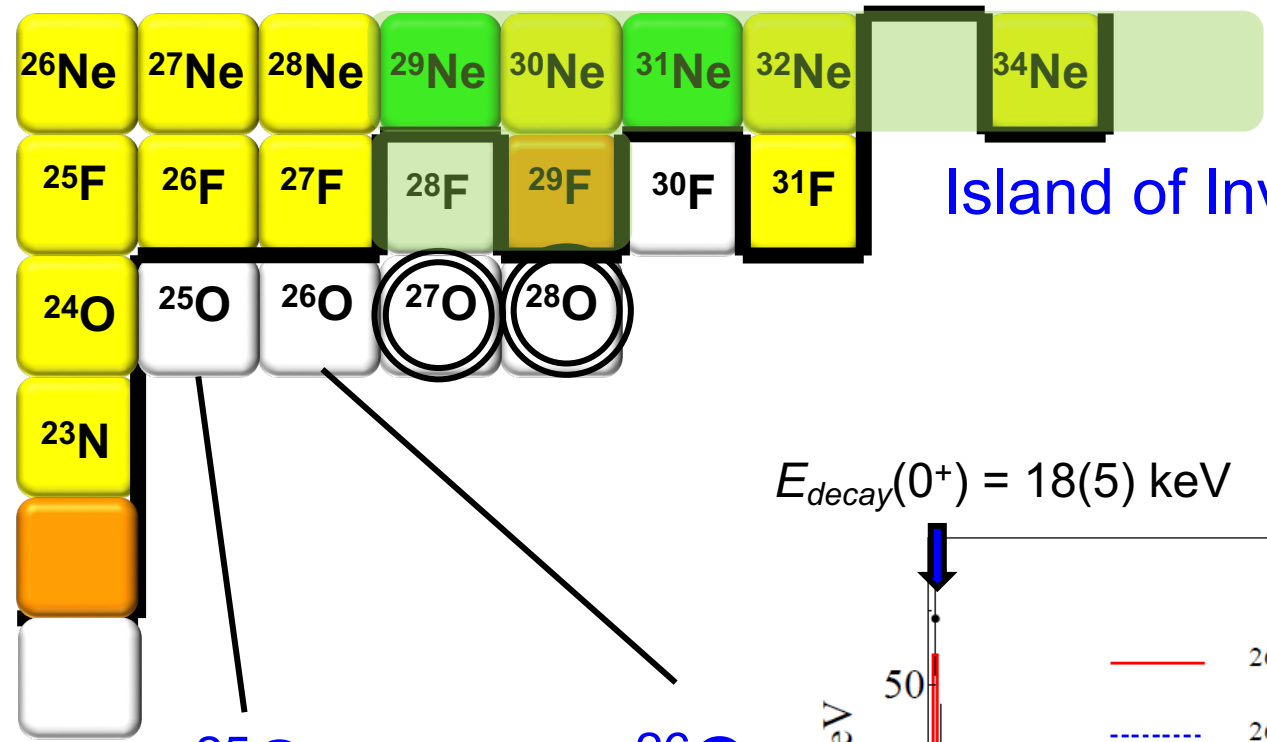
Island of Inversion

$d_{3/2} f_{7/2} p_{3/2}$  mixture ?

- Is  $^{28}\text{O}$  doubly magic?
- Why neutron drip line sudden change from O to F?
- “Oxygen Anomaly” → 3N force? T.Otsuka2010, G.Hagen 2012, J.Holt 2013
- “4n” in  $^{28}\text{O}$ ?

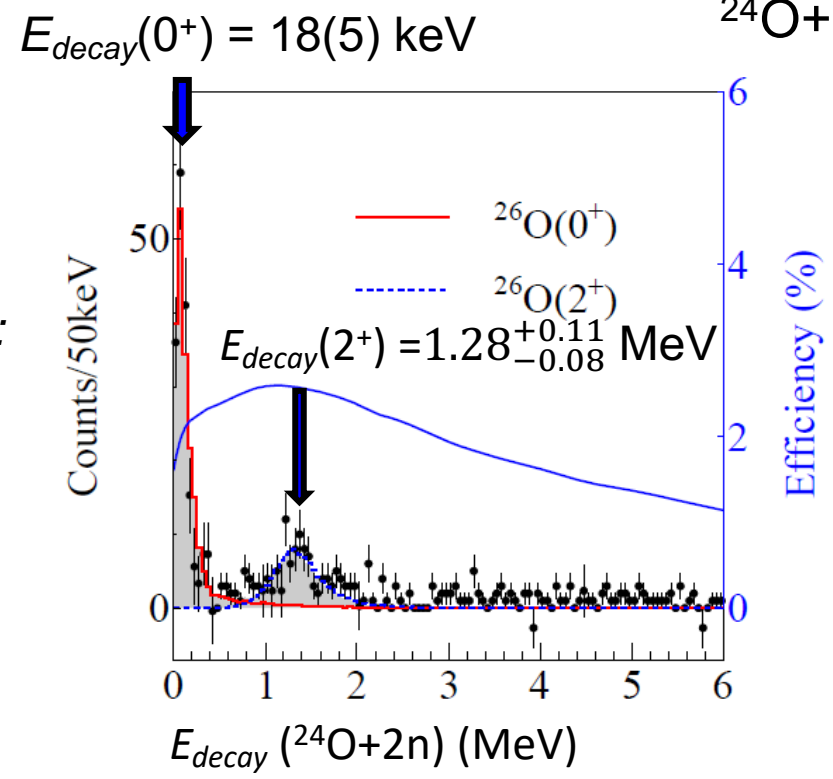
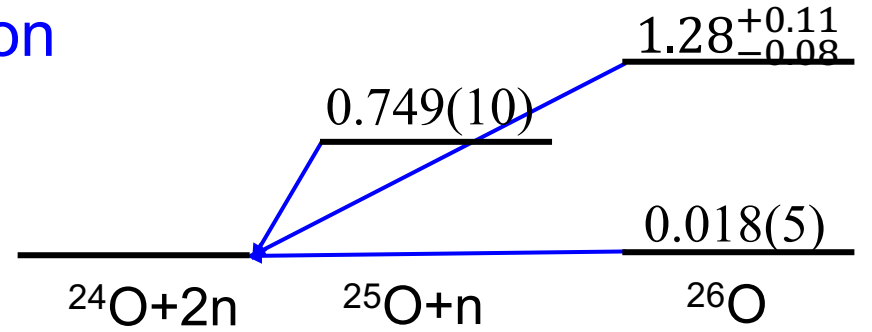


# What is known for oxygen isotopes beyond the dripline?



$^{25}\text{O}$ :  
 $E_{decay} = 749(10) \text{ keV}$   
 $\Gamma = 88(6) \text{ keV}$

$^{26}\text{O}$ :

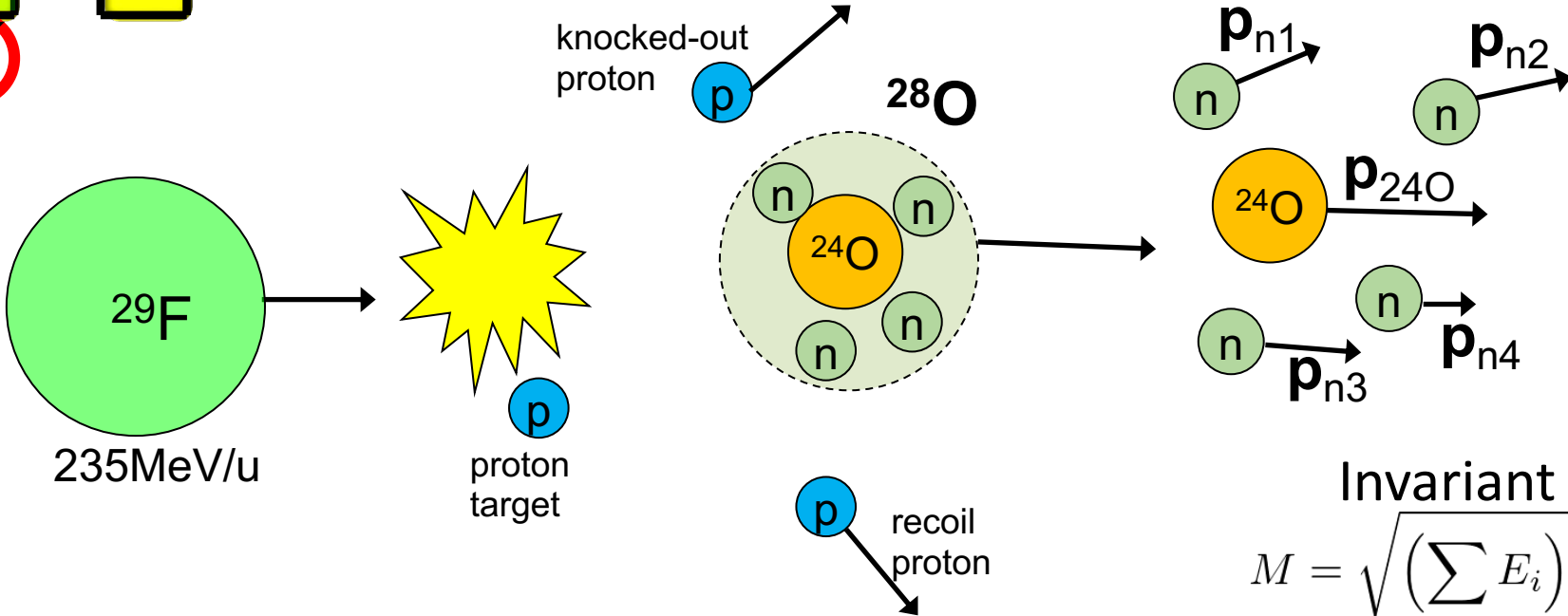
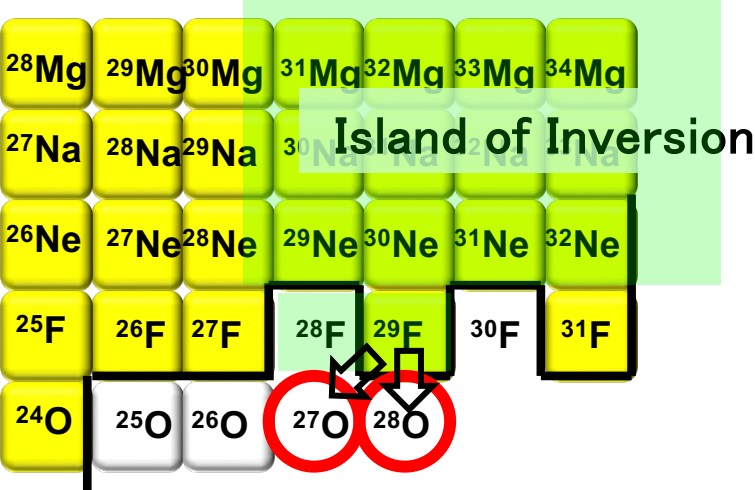


Y. Kondo et al., PRL116, 102503 (2016)  
 C.R. Hoffman et al., PRL100, 152502 (2008)  
 C. Caesar et al., PRC88, 034313 (2013)

Y. Kondo et al., PRL116, 102503 (2016)

# Method: Invariant mass spectroscopy of $^{27}\text{O}$ and $^{28}\text{O}$

Y.Kondo et al.  
Nature 620, 965 (2023).



$^{28}\text{O}$ : 1p removal reaction of  $^{29}\text{F}$   
 $^{27}\text{O}$ : 1p1n removal reaction of  $^{29}\text{F}$

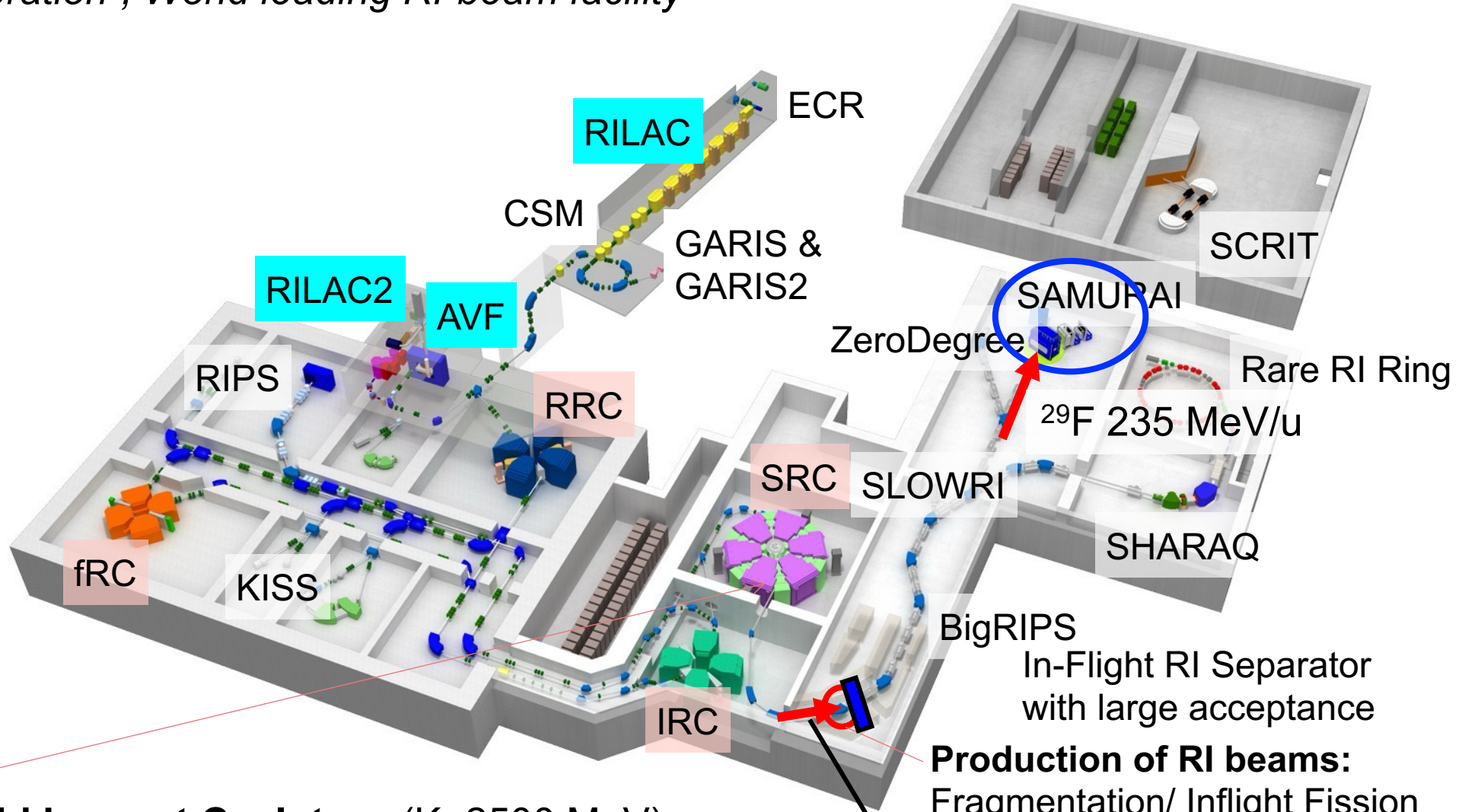
Invariant mass

$$M = \sqrt{\left(\sum E_i\right)^2 - \left(\sum \mathbf{p}_i\right)^2}$$

→4-neutron coincidence

# RI Beam Factory (RIBF) at RIKEN

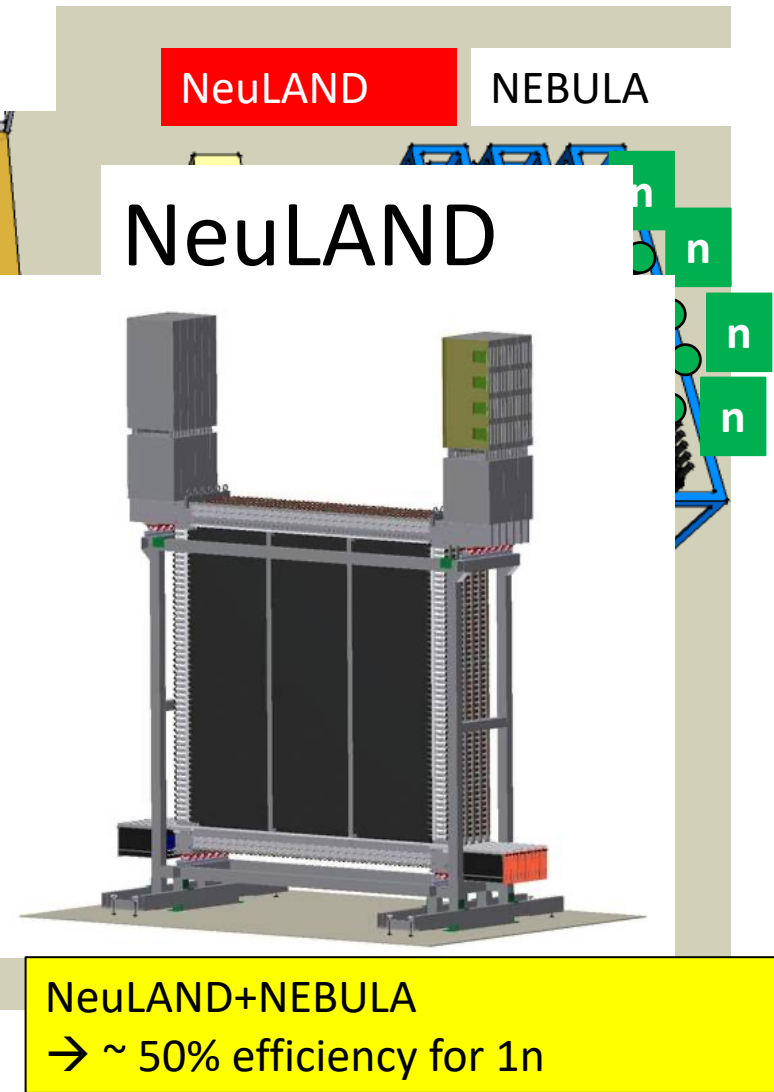
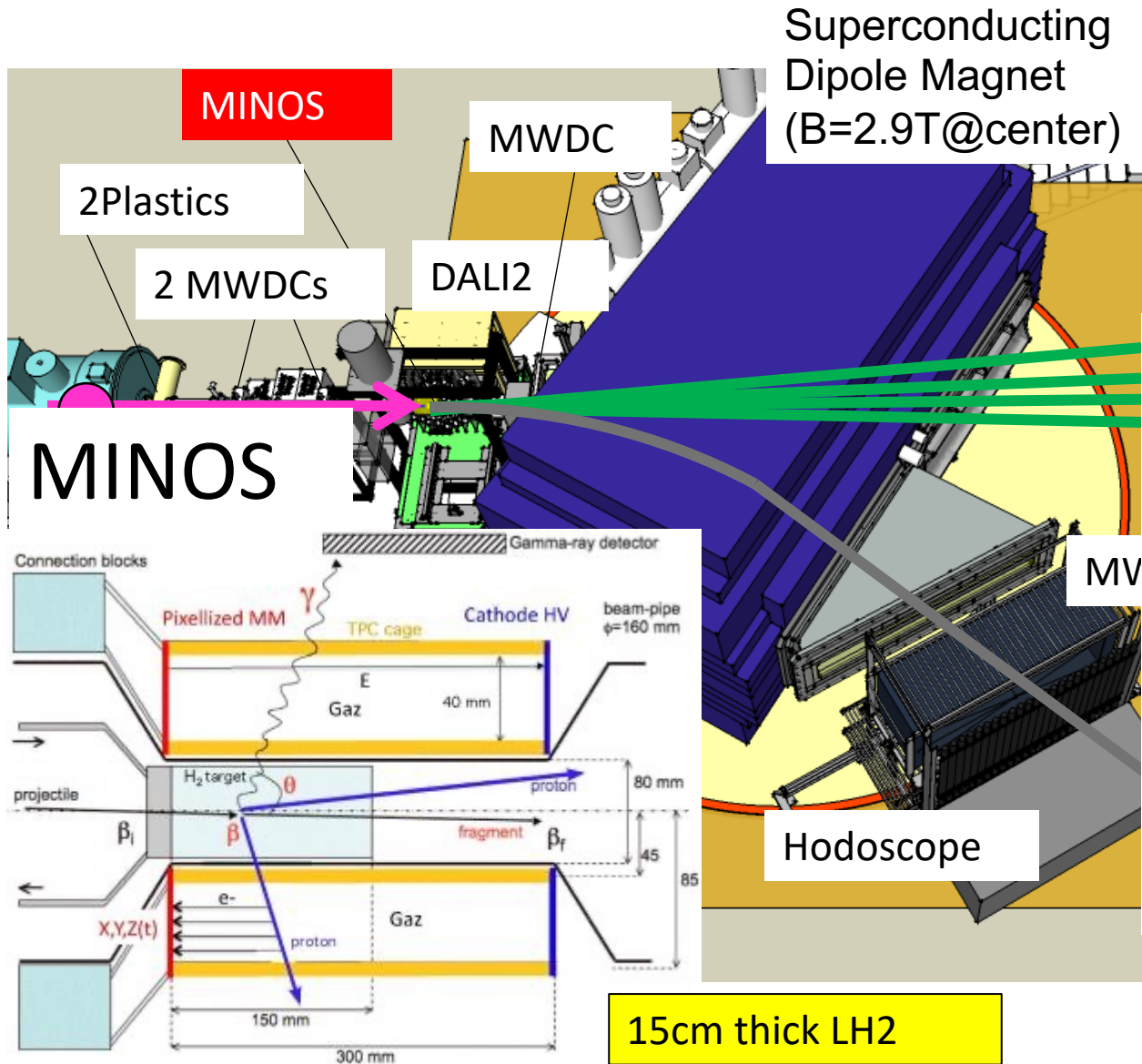
The 3rd-generation-, World leading RI-beam facility



**SRC: World Largest Cyclotron** (K=2500 MeV)  
**High-Intense Heavy Ion Beams**  
up to  $^{238}\text{U}$  at 345MeV/u

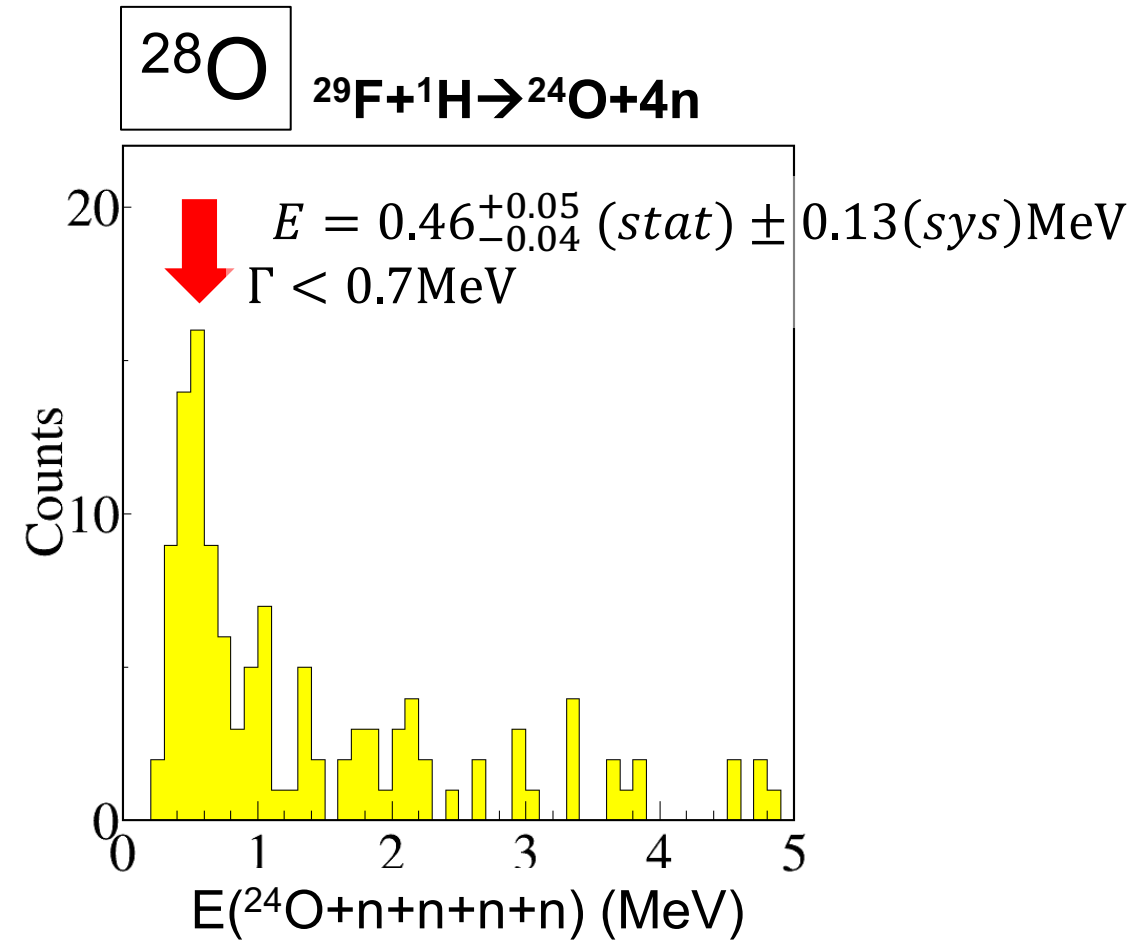
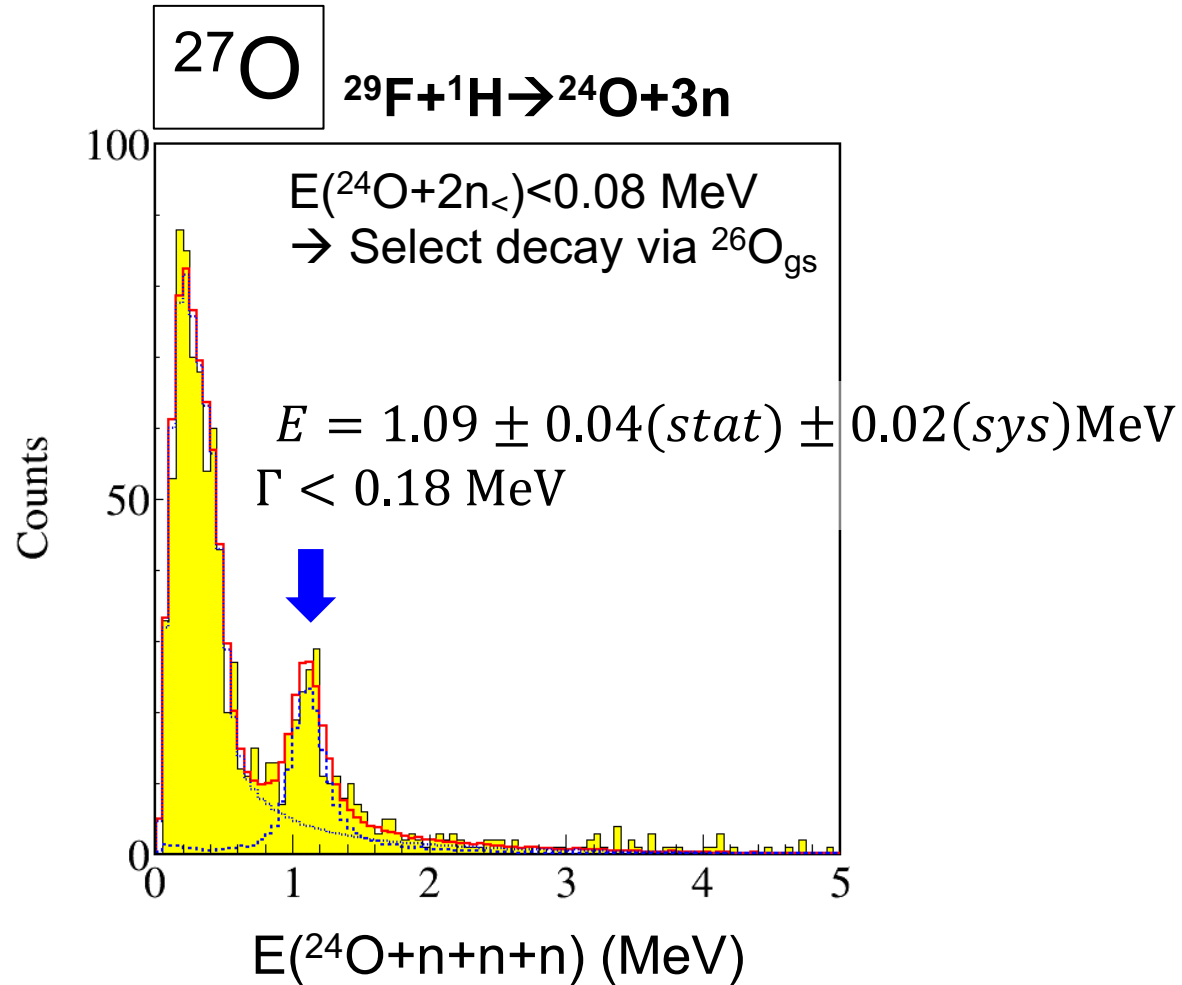
$^{48}\text{Ca}$  345 MeV/u  
 $\sim 700\text{pA}$

# $^{28}\text{O}$ measurement @ RIBF-SAMURAI



# Decay energy spectrum

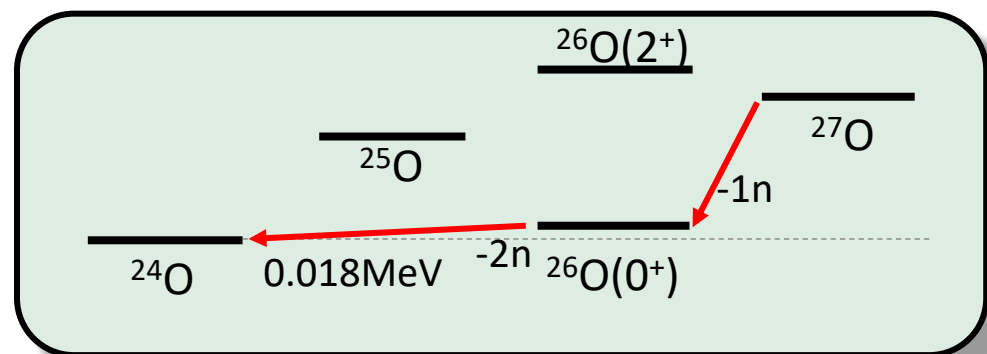
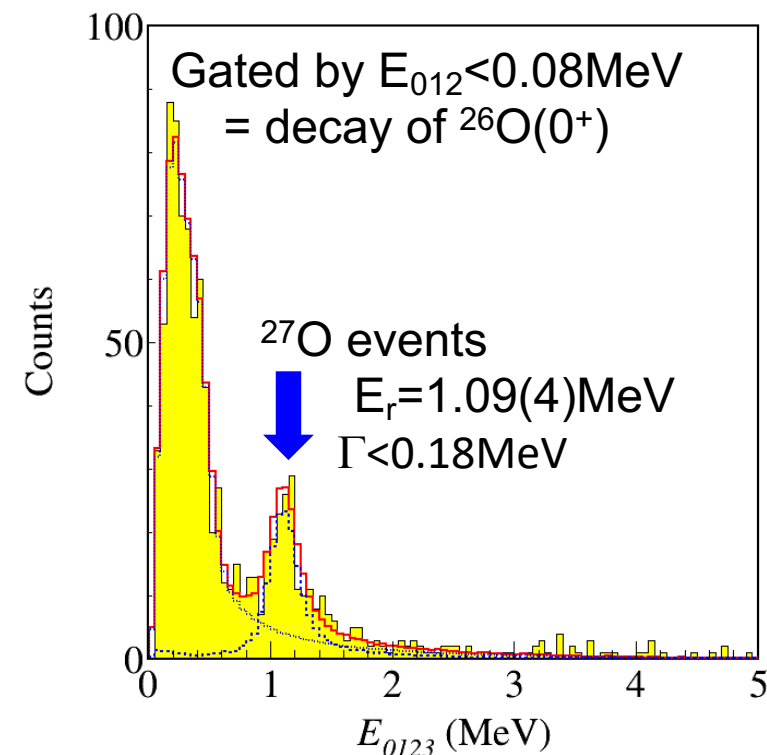
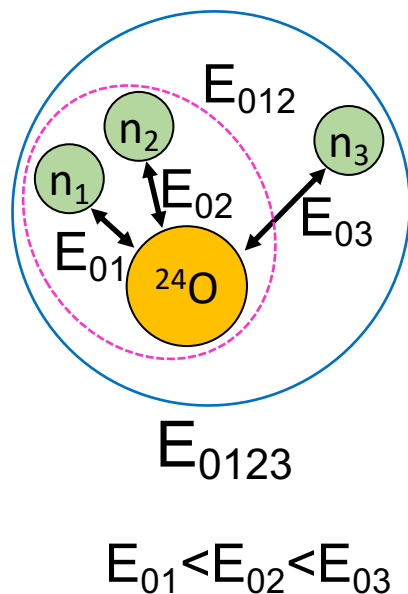
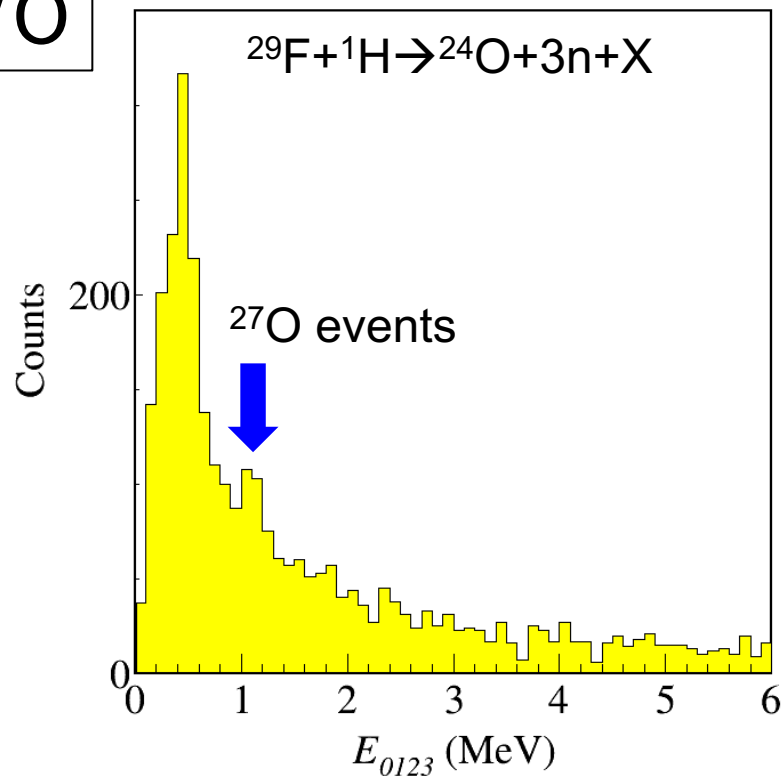
Y.Kondo et al.  
Nature **620**, 965 (2023).



# Decay energy spectrum ( $^{24}\text{O}+3\text{n}$ coincidence)

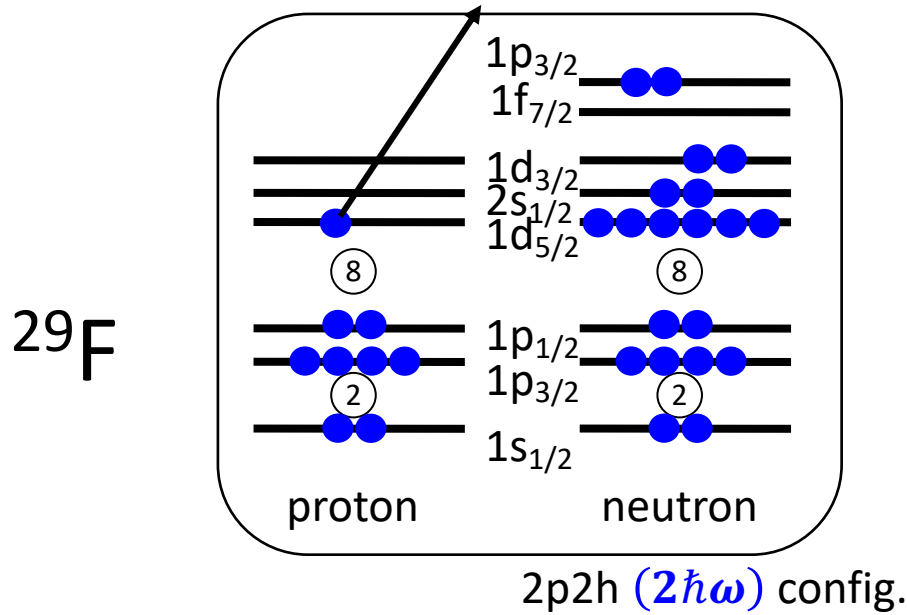
Y.Kondo et al.  
Nature **620**, 965 (2023).

$^{27}\text{O}$





# Is $^{28}\text{O}$ doubly magic?



$C^2S(\pi 1d_{5/2}) \sim 0 \rightarrow ^{28}\text{O}$  can be doubly magic  
(neutron configurations between  $^{29}\text{F}$  and  $^{28}\text{O}$ : different)

$C^2S(\pi 1d_{5/2}) \sim 1 \rightarrow$  neutron config. of  $^{28}\text{O} \sim ^{29}\text{F}$

Current result

$$\sigma_{-1p} = 1.36_{-0.14}^{+0.16} \text{ mb (syst. error 0.13 mb)}$$

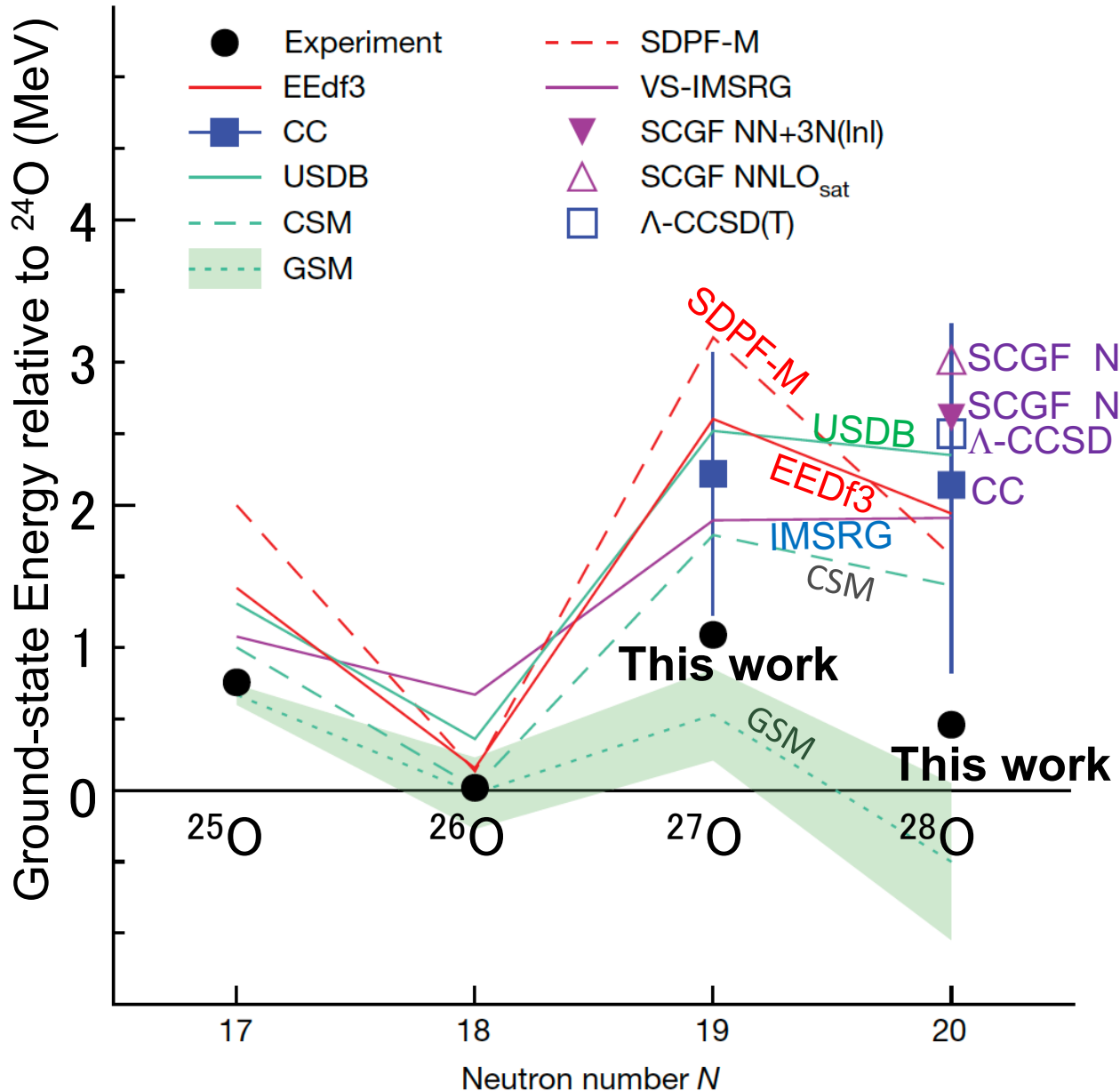
$$\Rightarrow C^2S(\pi 1d_{5/2}) = 0.48_{-0.06}^{+0.05}(\text{stat}) \pm 0.05(\text{syst})$$

Shell model calculation (EEdf3, mod ver. of EEdf1)  $\rightarrow C^2S=0.68$   
consistent with exp. ( $\sim 30\%$  reduction factor considered)

If  $^{28}\text{O}$  is 100% closed-shell config  $\rightarrow C^2S=0.13$

$N=20$  neutron magicity disappears in  $^{28}\text{O}$

# Comparison with theories $^{25-28}\text{O}$



**Conventional SM**

**USDB:**  
B. A. Brown, W.A. Richter, PRC74, 034315 (2006).

**Large-scale SM**

**SDPF-M:** Y.Utsuno et al., PRC60, 054315 (1999).  
**EEdf3:** N.Tsunoda et al., PRC95, 021304(R) (2017).; N.Tsunoda et al., Nature 587, 66(2020).

**Ab-initio Calculations**

**SCGF:** V. Somà et al., PRC101, 014318 (2020).  
**L-CCSD:** G. Hagen et al., Phys. Scr. 91, 063006 (2016).  
**CC (Coupled-Cluster method with statistical approach):** This work (Nature 2023)  
**IMSRG:** S.R. Stroberg et al., PRL126, 022501 (2021).

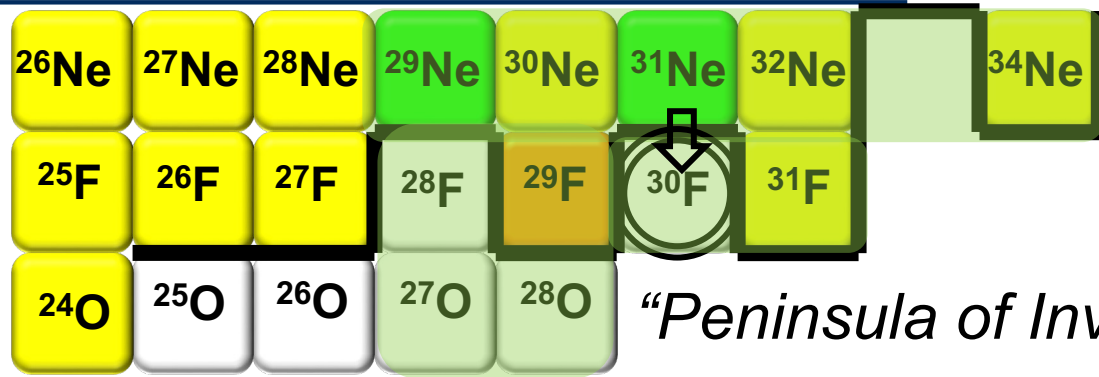
**SM with continuum effects**

**CSM:** A. Volya et al., PRC74, 064314, (2006).  
**GSM:** K. Fosseiz et al., PRC 96, 024308 (2017).  
J.G. Li et al., PRC 103, 034305 (2021).



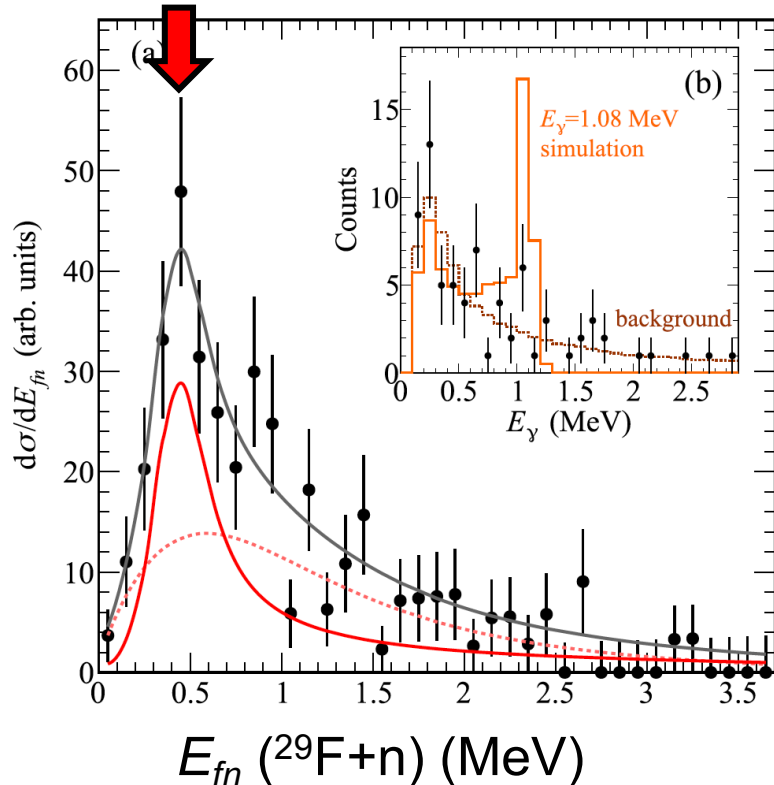
# Observation of $^{30}\text{F}$

J.Kahlbow, T.Aumann, O.Sorlin, Y.Kondo, TN et al.,  
**PRL 133, 082501 (2024).** @SAMURAI at RIBF

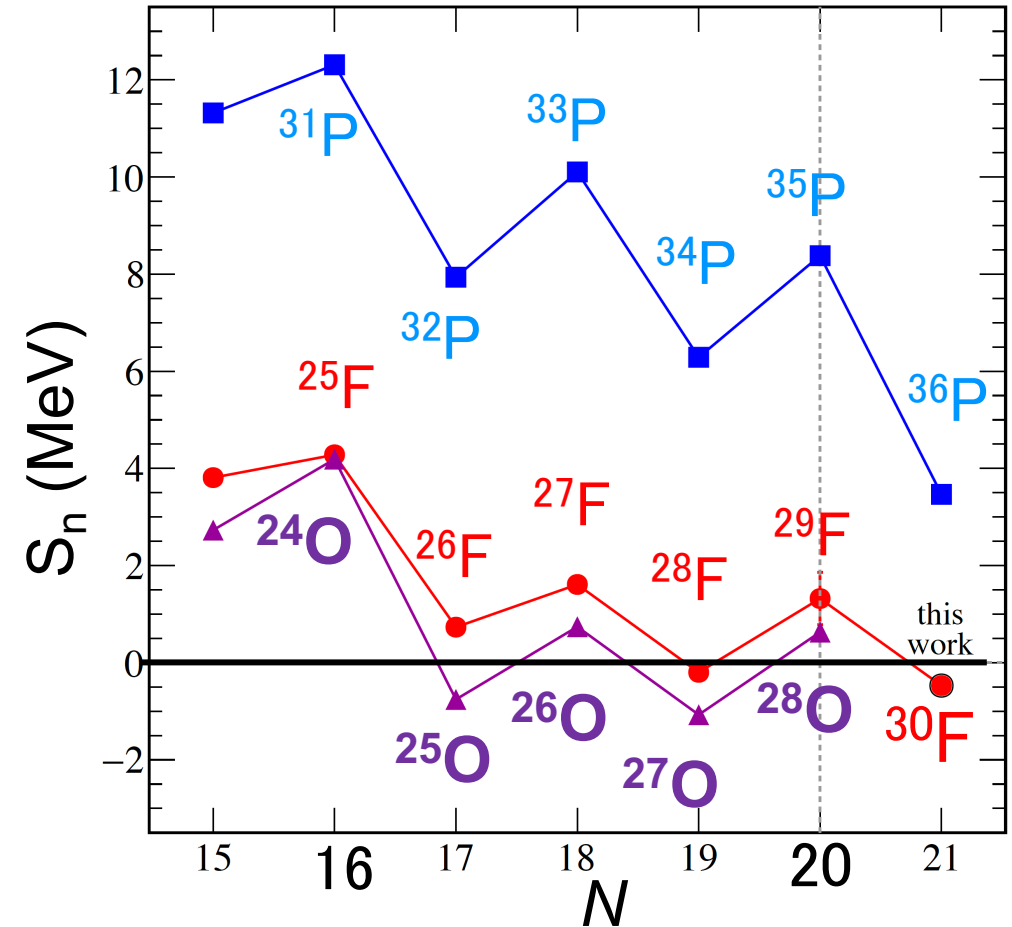


*“Peninsula of Inversion”*

$$E_{fn} (^{29}\text{F}+n) = 472 \pm 58(\text{stat}) \pm 33(\text{sys}) \text{ keV}$$



Heaviest resonance  
 so far observed  
 beyond  
 neutron dripline



$S_n$  for **O** and **F** with  $N > 16$  : **Similar, Nearly-Flat Trend**

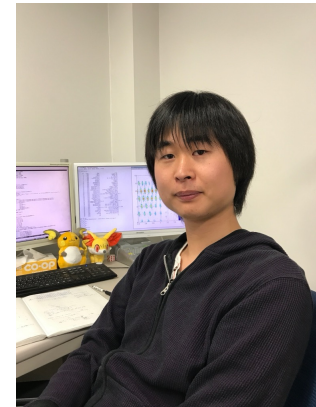
→ **N=20 magicity Lost** also at  $^{30}\text{F}$  →  $^{31}\text{F}$  : p-wave halo

→ **Superfluidity** due to d-f-p mixture for n with **Z=8** closure

Slight Deviation with SM (SDPF-U-MIX20) → Continuum Effects ?

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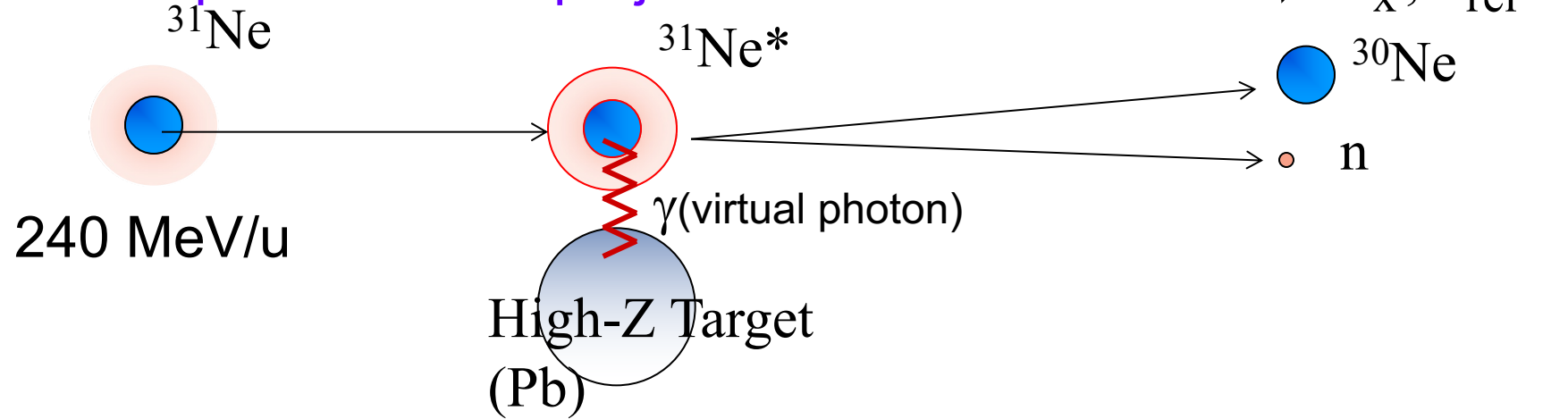
# Halo-Shell Interplay— $^{31}\text{Ne}$ ( $Z=10$ , $N=21$ )



[Takato Tomai, PhD Thesis](#)

# Exclusive Coulomb Breakup

→ Photon absorption of a fast projectile



$\vec{P}(n), \vec{P}(^{30}\text{Ne})$   
 Invariant Mass  
 $\Rightarrow E_x, E_{\text{rel}}$

## Equivalent Photon Method

$$\frac{d\sigma_{CB}}{dE_x} = \frac{16\pi^3}{9\hbar c} N_{E1}(E_x) \frac{dB(E1)}{dE_x}$$

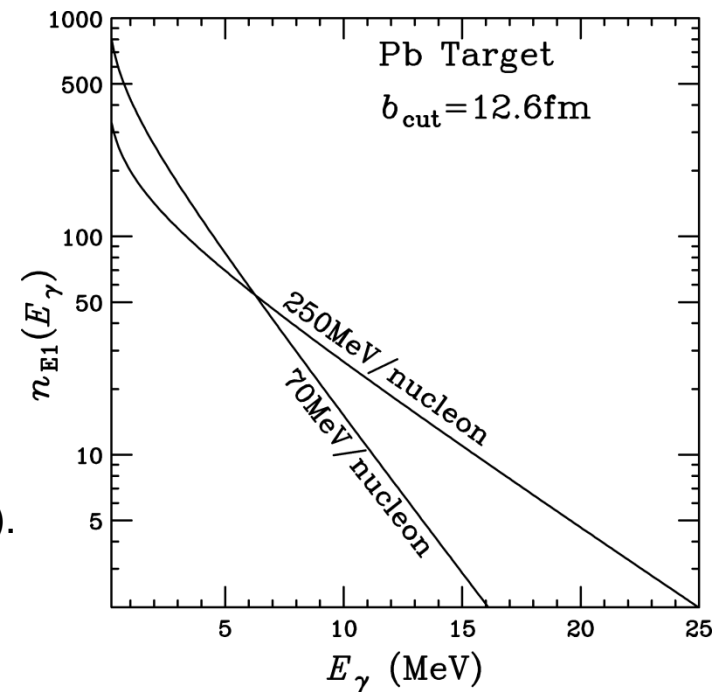
Cross section = (Photon Number) x (Transition Probability)

C.A. Bertulani, G. Baur, Phys. Rep. **163**, 299(1988).

T. Aumann, T. Nakamura, Phys. Scr. T**152**, 014142(2013).

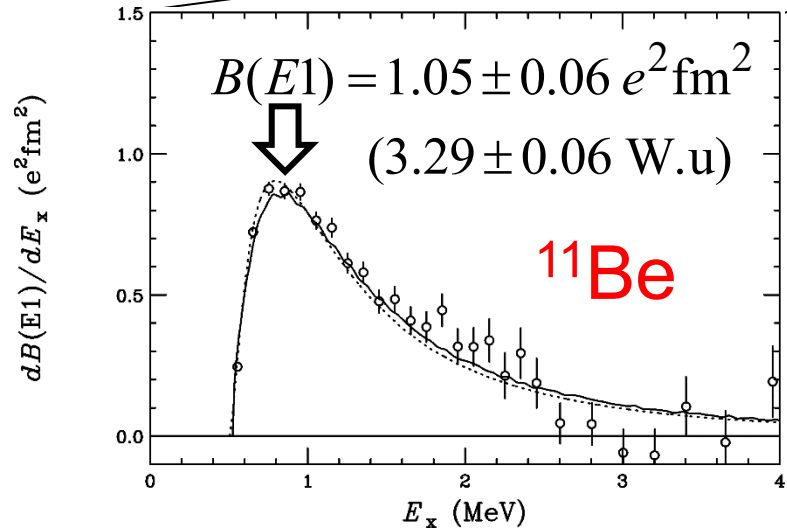
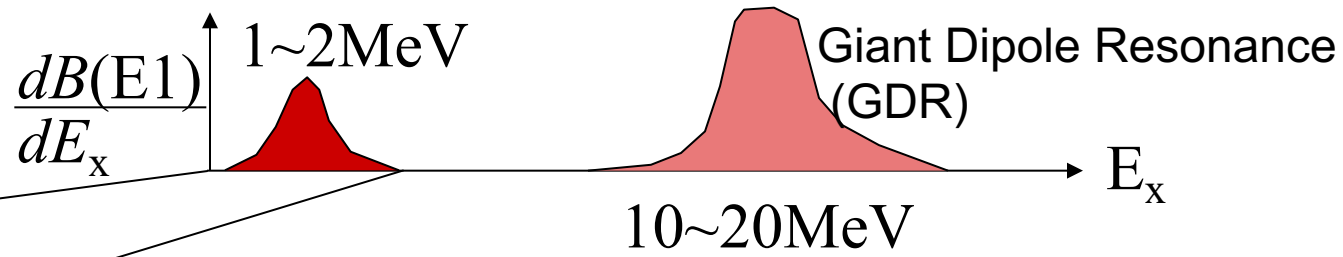
**Halo → Soft E1 Excitation**

**(E1 Concentration at  $E_x < 1\text{MeV}$ )**



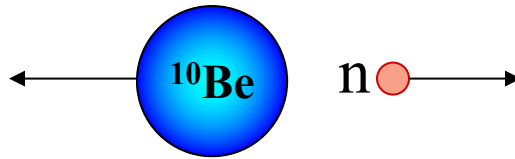
# Coulomb Breakup and E1 Response--Case of 1n Halo

**Low-lying  
E1 Strength  
(Soft E1 excitation)**



N.Fukuda, TN et al., PRC70, 054606 (2004)  
TN et al., PLB 331, 296 (1994)  
Palit et al., PRC68, 034318 (2003)

**Direct Breakup Mechanism**

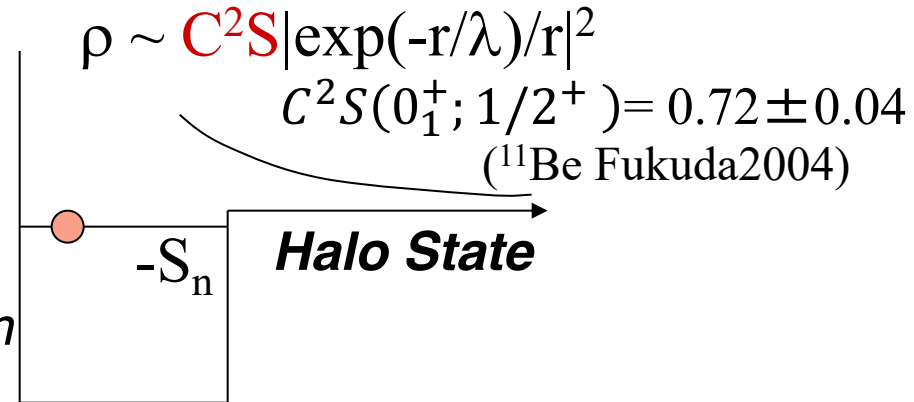


**E1 Strength**

$$\frac{dB(E1)}{dE_x} \propto \left| \langle \exp(iqr) \left| \frac{Z}{A} r Y^1_m \right| \Phi_{gs} \rangle \right|^2$$

$$\propto C^2S \left| \langle \exp(iqr) \left| \frac{Z}{A} r Y^1_m \right| s_{1/2} \rangle \right|^2$$

Fourier  
Transform



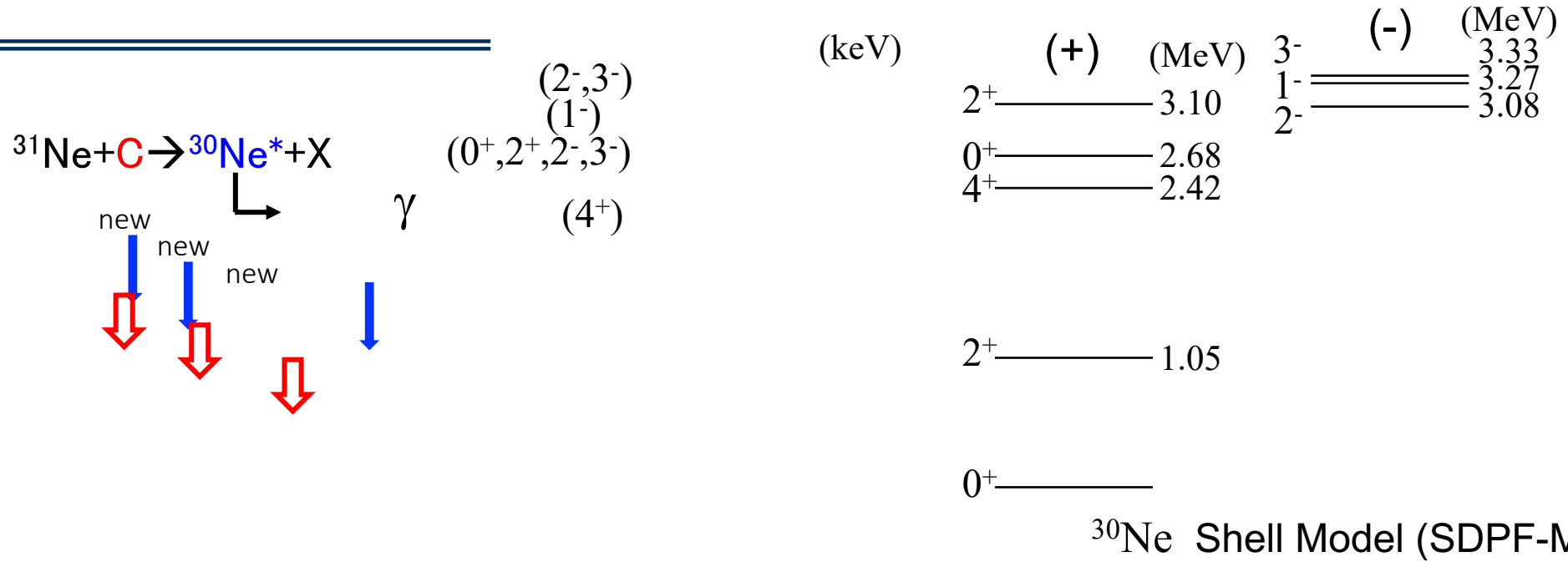
**Soft E1 Excitation of 1n halo—Sensitive to  $S_n, l, C^2S$**

**e.g. Peak Energy**

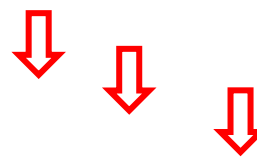
s-wave halo:  $E_{rel}^{(peak)} \cong \frac{3}{5} S_n$

p-wave halo (p→s):  $E_{rel}^{(peak)} \cong 0.18 S_n$

# $\gamma$ -ray spectrum : Excited $^{30}\text{Ne}$ -core component

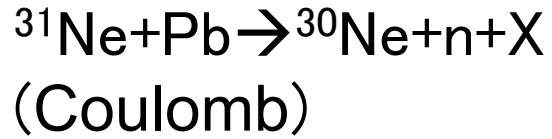


$^{31}\text{Ne} + \text{Pb}$



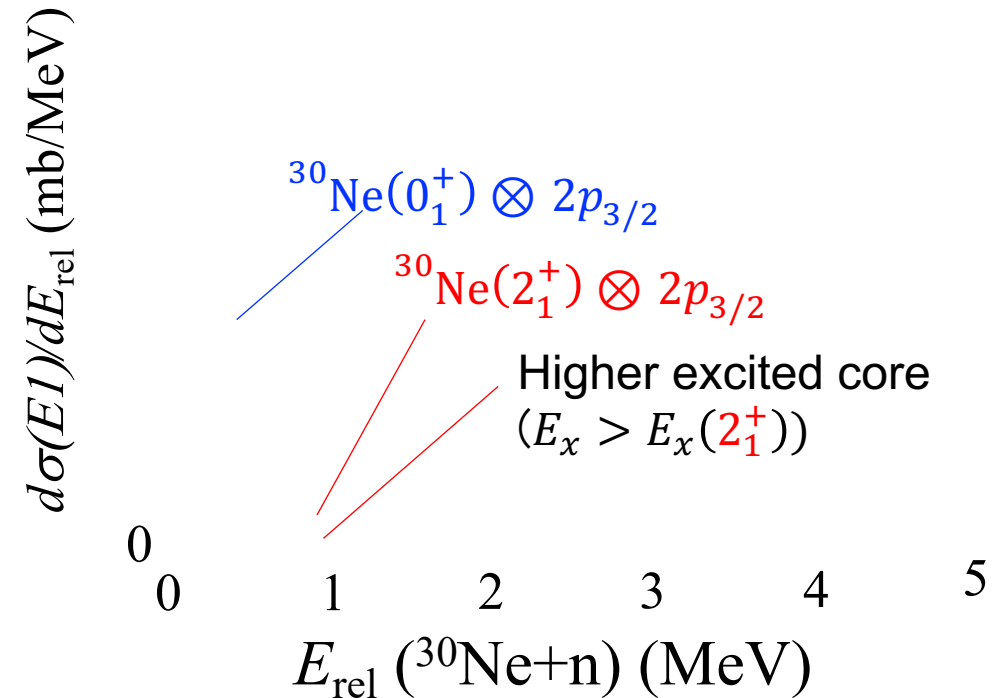
$$|^{31}\text{Ne}(3/2^-) \rangle = \alpha |^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2} \rangle + \beta |^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2} \rangle + \dots$$

# Coulomb breakup of $^{31}\text{Ne}$ : Energy Spectrum



$$|^{31}\text{Ne}(3/2^-) \rangle = \alpha |^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2} \rangle + \beta |^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2} \rangle + \dots$$

$$\alpha^2 = C^2 S(0_1^+; 3/2^-) \quad \beta^2 = C^2 S(2_1^+; 3/2^-)$$



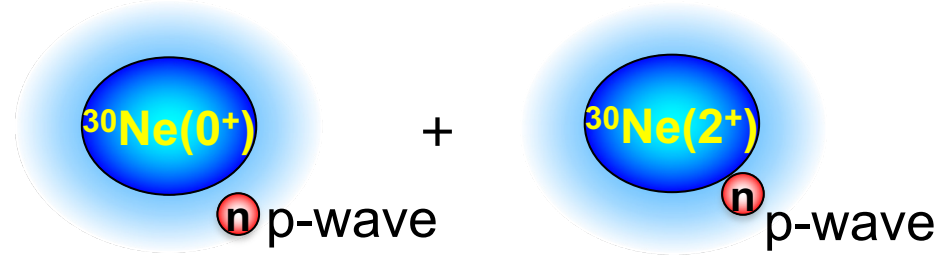
$$^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2} \quad ^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2}$$

\*TN, N. Kobayashi et al., PRL112, 142501 (2014).

# Double-Component Halo: Unique to p-wave halo

$$|^{31}\text{Ne}(3/2^-) \rangle = \alpha |^{30}\text{Ne}(0_1^+) \otimes 2p_{3/2} \rangle + \beta |^{30}\text{Ne}(2_1^+) \otimes 2p_{3/2} \rangle$$

$$S_n^{(\text{eff})} = S_n + E_x(2_1^+) \sim 1.0 \text{ MeV}$$



## Double-Component Halo:

*Preliminary*

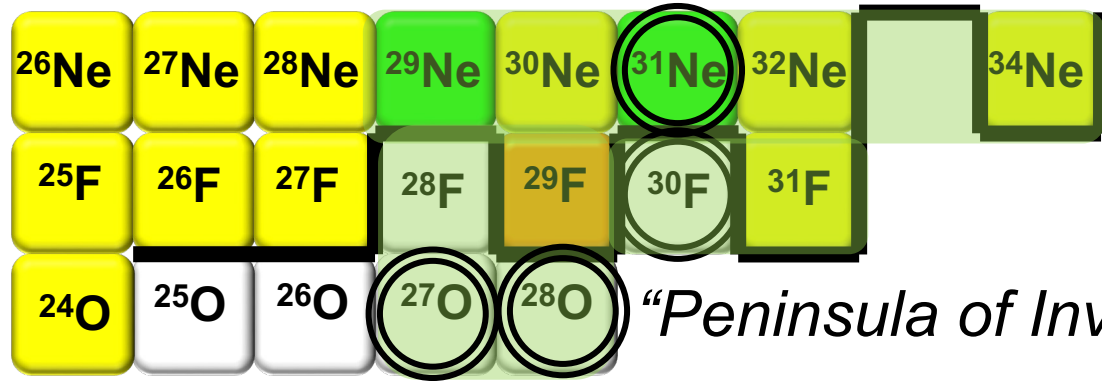
✓ Unique feature of **p-wave halo**

c.f. **Single-component for s-wave halo**

$$|^{11}\text{Be}(1/2^+) \rangle = \alpha |^{10}\text{Be}(0_1^+) \otimes 2s_{1/2} \rangle + \beta |^{10}\text{Be}(2_1^+) \otimes 1d_{5/2} \rangle$$

s-wave halo
non-halo

# Summary



$^{27}\text{O}, ^{28}\text{O}$ : Y.Kondo Nature **620**, 965 (2023).

$^{30}\text{F}$ : J.Kahlbow, PRL **133**, 082501 (2024).

$^{30}\text{Ne}$ : T.Tomai, *In preparation*

“Peninsula of Inversion”

- ✓ Neutron dripline → Boundary of Open/Closed Quantum Systems → Universal features
- ✓  $^{29}\text{F}(p,2p)^{28}\text{O}$ ,  $^{29}\text{F}(p,2pn)^{27}\text{O}$ ,  $^{31}\text{Ne}(p,2p)^{30}\text{F}$  at SAMURAI at RIBF
  - ✓ World-first invariant mass spectroscopy with  $4n$ +fragment in coincidence
  - ✓  $^{28}\text{O}$ : unbound by  $4n$  emission with  $E = 0.46_{-0.04}^{+0.05} (stat) \pm 0.13(sys)\text{MeV}$
  - ✓  $^{27}\text{O}$ : unbound by  $3n$  emission with  $E = 1.09 \pm 0.04(stat) \pm 0.02(sys)\text{MeV}$
  - ✓  $^{28}\text{O}$ :  $N=20$  magicity is lost: Not a doubly magic nucleus
  - ✓  $^{30}\text{F}$ :  $E = 0.472 \pm 0.058(stat) \pm 0.033(sys)\text{MeV}$
  - ✓  $^{30}\text{F}$ :  $N=20$  magicity lost: →  $^{31}\text{F}$  p-wave halo, Superfluidity for O/F with  $N>16$
- ✓ Halo-Shell Interplay:  $^{31}\text{Ne}$  :
  - Exclusive **Coulomb Breakup** of  $^{31}\text{Ne}$ 
    - ✓ Soft-E1 Excitation → **Double halo components: Unique feature of p-wave halo**



# Perspectives

➤ More exotic weakly bound and unbound nuclei along the neutron drip line  
 ${}^6\text{n}$ ,  ${}^{28}\text{O}(2_1^+)$ ,  ${}^{29}\text{O}$  ...

→ Understand Microscopically Shell-Halo Interplay

→ Many-body effects at the boundary open-closed quantum systems

→ Universal Features with Exotic hadrons and Ultra-cold atoms

➤ Multi-neutron detections

→ Key to understanding physics near and beyond the neutron drip line

# SAMURAI21 collaboration— $^{27,28}\text{O}$ , $^{28}\text{F}$ , $^{30}\text{F}$



**Y.Kondo**, **T.Nakamura**, N.L.Achouri, H.Al Falou, L.Atar, T.Aumann, H.Baba, K.Boretzky, C.Caesar, D.Calvet, H.Chae, N.Chiga, A.Corsi, H.L.Crawford, F.Delaunay, A.Delbart, Q.Deshayes, Zs.Dombrádi, C.Douma, Z.Elekes, P.Fallon, I.Gašparić, J.-M.Gheller, J.Gibelin, A.Gillibert, M.N.Harakeh, A.Hirayama, C.R.Hoffman, M.Holl, A.Horvat, Á.Horváth, J.W.Hwang, T.Isobe, **J.Kahlbow**, N.Kalantar-Nayestanaki, S.Kawase, S.Kim, K.Kisamori, T.Kobayashi, D.Körper, S.Koyama, I.Kuti, V.Lapoux, S.Lindberg, F.M.Marqués, S.Masuoka, J.Mayer, K.Miki, T.Murakami, M.A.Najafi, K.Nakano, N.Nakatsuka, T.Nilsson, A.Obertelli, F.de Oliveira Santos, N.A.Orr, H.Otsu, T.Ozaki, V.Panin, S.Paschalis, **A.Revel**, D.Rossi, A.T.Saito, T.Saito, M.Sasano, H.Sato, Y.Satou, H.Scheit, F.Schindler, P.Schrock, M.Shikata, Y.Shimizu, H.Simon, D.Sohler, O.Sorlin, L.Stuhl, S.Takeuchi, M.Tanaka, M.Thoennessen, H.Törnqvist, Y.Togano, T.Tomai, J.Tscheuschner, J.Tsubota, T.Uesaka, H.Wang, **M.Yasuda**, Z.Yang, K.Yoneda



Tokyo Tech, Argonne, ATOMKI, CEA Saclay, Chalmers, CNS, Cologne, Eotvos, GANIL, GSI, IBS, KVI-CART, Kyoto Univ., Kyushu Univ., LBNL, Lebanese-French University of Technology and Applied Science, LPC-CAEN, MSU, Osaka Univ., RIKEN, Ruđer Bošković Institute, SNU, Tohoku Univ., TU Darmstadt, Univ. of Tokyo

88 Participants (+analysis) 25 Institutes

Y.Kondo et al., Nature **620**, 965-970 (2023).

A. Revel et al., PRL124,152502(2020). ( $^{28}\text{F}$ )

J. Kahlbow et al., PRL in Press ( $^{30}\text{F}$ )

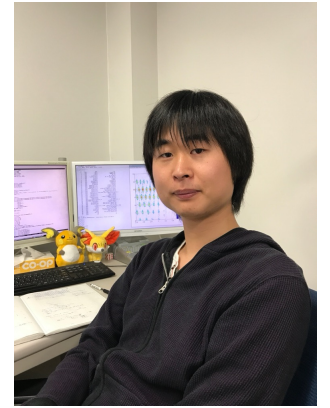
# Exclusive Coulomb/nuclear breakup of $^{31}\text{Ne}$

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